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# General Electric Review 

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# General Electric Review 

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Manager．M．1＇R1CE
Eわtor，JoHNR HEWETT

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By̆ R. E. Helfaer

Communication by High Frequency Waves ．
By̆ J. B. TAylor




## THE ENGINEER AND CHRISTMAS

As our January issue comes off the press just at Christmas time we should like, in this number, to wish all our friends a very Happy Christmas and a Prosperous New Year.

We are fortunate in being able to announce the establishment of the Charles A. Coffin Foundation at this time as there is a good deal of the Christmas spirit in the intent of the awards that will be made each year from this fund.

How many Christmas presents of the best and most useful kind has the electrical industry made to mankind during the marvelous age in which Mr. Coffin has been the leading spirit in this leading industry! Since electricity has been used as the driving force of industry we have made more material progress each decade than we made in a century before. And the pace quickens rather than slackens!

Still we talk of the good old times with regret and sometimes shake our heads in doubt as to where our modern notions of progress are to carry us.

Think-would either the millionaire or the laborer go back to live as his grandfather lived: The laborer has many comforts and luxuries today that the millionaire could not procure with all his wealth a few decades ago, because they did not exist.

Science is a fairy godmother to mankind.
The more immature man may, like Tiny Tim, call out "God bless every one" and leave it at that-we like the sentiment. But the engineer and the scientist must call out "God has blessed every one but they must labor to reap the harvest that He has sown."

All possible blessings are on the earth and have been for many long centuries. The bottled sunshine and the many brilliant colors that make our Christmas greeting attractive were latent blessings long before man discovered them and learned the processes that
make them useful and bring them to oun homes. All the materials for our trains, ships, motor cars, flying machines, telephones, telegraphs, wireless etc. ete. and the energy for working them lay hidden for untold centuries. It was not just shouting out "Cod bless every one" that turned these fatent blessings into actual blessings-it was work.

Perhaps the greatest blessing of all is the privilege of doing this useful work and the knowledge that opportunities to do useful work increase rather than decrease with each new invention and discovery.

The blessings to be unfolded in the future are greater than those as yet revealed by work and we are proud in the belief that our in-dustry-the electrical industry-is to be the medium through which many of these blessings are to be secured for mankind in the future.

## OPPORTUNITY

With doubt and dismay you are smitten, You think there's no chance for you, son?
Why, the best books haven't been written, The best race hasn't been run,
The best score hasn't been made yet, The best song hasn't been sung,
The best tune hasn't been played yet; Cheer up, for the world is young!
No chance? Why, the world is just eager For things that you ought to create;
Its store of true wealth is still meagre, Its needs are incessant and great;
It yearns for more power and beauty, More laughter and love and romance.
More loyalty, labor and duty, No chance-why, there's nothing but chance!
For the best verse hasn't been rhymed yet, The best house hasn't been planned,
The highest peak hasn't been climbed yet, The mightiest rivers aren't spanned;
Don't worry and fret, faint-hearted, The chances have just begun,
For the Best jobs haven't been started, The Best work hasn't been done.

> - Berton Braley:
J. R. H.

## THE COFFIN FOUNDATION

(An Editorial from the New York Herald, December 5, 1922)

The Gemeral Electric Company has established a fund of s 100,000 , to be known as the Clarles $\lambda$. Coffin Foundation, the income from which is to be devoted to encouraging the study and the application of the seience of clectricity: The Ceneral Electric Company thus pays public and endmring tribute to the man who was its president from its organization until $191: 3$ and chairman of its board from 1913 until this year to Charles A. Coffin, business man and financier, to whom the electrical inchustry in the Lnited States owes much of its rapid and sound development.

Mr. Coffin is a Maine man. endowed with the cuality of common sense so conspicuously possessed by the leaders of thought and action the Pinc Tree State has given to the nation, and gifted with breadth of vision that enalles him to risualize business as something. more than an opportmity to pay fair wages to workers and to earn fair profits for stockholders. The history of the General Electric Company is the history of Charles A. Coffin, and the history of Charles $A$. Coffin is one of constant striving to improve on the best that has yet been done.

The Research Laboratory of the General Electric Company at Schenectady, with the distinguished scientist Dr. Willis R. Whitney at the head of its numerous staff of innestigators, is one of the concrete examples of the practical application of Mr. Coffin's ambition to put American industry in the forefront. In this great institution Mr. Coffin has used for
the adrancement of science all the resources of the great eorporation he has built up. The fruits of its expensive and patient inquiries have been made available to the public; no selfish purpose has animated its administration. The recorl of its contribution to the cause of the nation in the war has never been told. When it is, another inspiring chapter of devoted patriotism will be written.

The policy and the practices of the corporation which Mr. Coffin has directed as it forged its way to world-wide importance were the natural expressions of his keen intelligence, his wide sympathy and his ambition to achieve that success which those attain who raise the standard of mankind's comfort, safety and happiness by enlarging man's opportunity to do for himself. Mr. Coffin opened new fields of employment, gave new rewards to manual skill and intellectual capacity, offered new incentive to men and women to spend their talents in bettering the world they live in. It is in keeping with this that his monument should be a permanent foundation which will afford in the years to come recognition and encouragement to other toilers in the calling in which Mr. Coffin's genius has been displayed.

The circumstance that Mr. Coffin's associates have conferred this honor while he may personally influence the course of its development, should he be so inclined, gives added testimony to the respect and confidence those who know him most intimately repose in him.


## Charles A. Coffin Foundation


#### Abstract

 Electric Company.  founder and creator of the Cencral Electric Company of which he has feem the inspiration and leater for thirly years.

As an expression of appreciaton of Mr. Coffin's great work not only for the Comeral Eketrie (compatny but also for the entire electrical industry and with the desire to make this appectation enturing atrd ont structive, as Mr. Coffin's life and work have been, the Board of Ditectors of the Cencral Electric Company created on his retirement and now desire to anmonee the "Chorles d. Coffor Fommation." Gertrb SWopt, Presilent.


13y action of its Board of Directors, the General Electric Company has set aside a fund of $\$ 400,000$, to be known as the "CHARLES A. COFFIN FOL'NDATION"," the income from which, amounting to approximately $\$ 20,000$ per sear, will be arailable for encouraging and rewarding service in the electrical field by giving prizes to its emplovees, recognition to lighting, power and railway companies for improvement in service to the public and fellowships to graduate students and funds for research work at technical schools ancl colleges.

The foundation will be controlled and administered by a Foundation Committee appointed by the Board. This Committee, within the limits of the purposes for which the foundation is created, will have power to change the conditions applicable to the distribution of the fund and the amounts for cach particular purpose.

The Committee proposes to distribute the income of the foundation as follows:

First. Eleven thousand dollars in prizes for the most signal contributions by employees of the General Electric Company toward the increase of its efficiency or progress in the electrical art. Particularly, the prizes are to further encourage suggestions from workmen. With each prize, the Company will give a certificate of award.

Foremen's prizes are to be awarded for the best department, taking into account its appearance, efficiency of operation, and conditions which add to the better conduct of the work and the welfare of the employees.

All emplorees of the Company. except Executive Officers. Heads of Departments. Works Managers. Superintendents. District Office Managers and similar executives are eligible for such prizes.

In works where Emplosees' Representation has been adopted, such representatives will cooperate with the Prize Committee in awarding prizes in such works.

Scoond. A gold merdal, to 1 e known as the "Charles A. Coffin Medal," will be awarded annually to the Pulblic C'tility (Operating Company within the Conterl States which, during the year, has made the greatest comtribution towards increasing the advantages of the use of electric light and power for the eonvenience and well-being of the pul) lic and the benefit of the industry: The Company receiving the medal will also receite one thousand dollars for its Employees' Bencfit or similar fund

A Committee to be named be the National Eleetric Light Association and known as the "Charles A. Coffin Prize Committee of the National Electric Light Association," which shall consist of its President. (hairman of its Public Policy Committee and a third member nominated by them, will award this medal. acting with the advice and cooperation of a Committee appointed be the Foundation Committee. The expenses of the Committee are to be paid out of the ineme of the foundation.

Third. A gold medal, to be known as the "Charles A. Coffin Medal," will be awarded annually to the Electric Railway Company within the United States which, during the year. has made the greatest contribution towards increasing the advantages of electric transportation for the convenience and wellbeing of the publie and the benefit of the industry. The Company receiving the medal will also receive one thonsand dollars for its. Employees' Benefit or similar fund.

A Committee, to be named by the Ameriean Electric Railway Association and known as the "Charles A. Coffin Prize Committee of the American Railway Association," which shall consist of its President, the Chairman of the Committee on Policy, and a third member nominated by them. will award this medal acting with the adrice and cooperation of a committee appointed by the Foundation Committee. The expenses of the Committee are to be paid out of the income of the foundation.

Fourth. Five thousand dollars is to be awarded ammally for followships to graduates of American colleges and technical schools who, by the character of their work, and on the recommendation of the factilty of the institution where they have studied, could with advantage continue their research work either here or abroat ; or some portion or all of the fund may be used to further the research work at any of the colleges or technical schools in the United States. The fields in which these fellowships and funds for research work are to be awarded are:

## Electricity

Physies
Physical Chemistry.
A Committee appointed by the Foundation Committee will award such fellowships and funds for research work, with the advice and cooperation of a Committee of three, one to be appointed by each of the following:

National Academy of Sciences
American Institute of Electrical Engineers Society for the Promotion of Engineering Education.
This Committee is to be known as the "Charles A. Coffin Fellowship and Research Fund Committee" and the fellowships are to be known as the "Charles A. Coffin Fellowships." The expenses of the Committee are to be paid out of the income of the foundation.

Fifil. In each annual report of the General Electric Company a statement will be made of the awards under the "Charles A. Coffin

Foundation," and other publicity will be given to such awards

The Board of Directors of the General Electric Company has appointed as the "Charles $A$. Coffin Foundation Committee" the following officers of the Company:

> Mr. A. W. Burchard
> Mr. J. R. Lovejoy
> Mr. E. W. Rice, Jr.
> Mr. Gerard Swope
> Mr. O. D. Young.

The Advisory Committee of the General Electric Company will administer the fund within the organization of the General Electric Company.

The following Committees to administer the fund and to act with organizations outside the Company have been appointed:

Committee to cooperate with the National Electric Light Association:

Mr. A. H. Jackson, Vice President
Mr. J. R. Lovejoy, Vice President.
Committee to cooperate with the American Electric Railway Association:

Mr. J. G. Barry, Vice President
Mr. A. H. Jackson, Vice President.
Committee to cooperate with the National Academy of Sciences, American Institute of Electrical Engineers and the Society for the Promotion of Engineering Education:

Mr. E. W. Rice, Jr., Honorary Chairman
Mr. A. H. Jackson, Vice-President
Mr. W. R. Whitney, Director of Research Laboratory:


# Some Developments in the Electrical Industry During 1922 

By John Liston<br>prblcation Bureat, General Electric Company


#### Abstract

It is our usual practice in the first issue of a new year to review the developments of the previous twelve months. Any one who has followed these articles can not fail to be impressed with the ernstant and persistent progress made in the electrical industry. Our present contribution shows that our curve of progress is still traveling on the up grade at a most satisfactory rate.-Editor.


The general industrial revival which characterized the year 1922 resulted in greatly increased activity in the production of all classes of electrical apparatus while the improvement in financial conditions rendered possible a much needed cxpansion in central station equipment and a resumption of development in numerous hydro-electric projects.

While progress in the electrical industry was mainly along established lines, there was a well defined tendency in practically every phase of electrical apparatus construction to
up an interesting field of considerable importance in view of the great number of craft of this trpe which serve our inland and coastal waterways.

Automatic station practice made further technical and commercial gains with a steady increase in the unit capacities of the equipments and improvements in the design of the small sized but very important devices which make automatic operation not only feasible but fully as reliable as hand operation. While railway service continued to


Fig. 1. The First Electrically Propelled Ferryboat, the Golden Gate, placed in service in July, 1922
concentrate the generation, transformation and distribution of electrical energy in units of greater capacities and with higher guaranteed efficiencies than in previous years.

The maximum rating for steam turbine generator sets was adranced to $62,500 \mathrm{kv}-\mathrm{a}$. and for waterwheel generators to 6.J,000 kv-a. with corresponding increment in the capacities of the transformers and switching and auxiliary apparatus required.

The adoption of electric propulsion for ferryboats, Fig. 1, and the positive economies secured in their operation by this method opens
be the most active field for this class of apparatus, its use was further extended in central station systems and applied to numerous other industries.

Among other items of interest in widely varying fields were a new type of induction furnace for melting non-ferrous metals, the production of a highly efficient steam generator for use where surplus electrical energy is available, the "Pallophotophone" for recording and reproducing sound, the thirtykilowatt incandescent lamp, radio and power tubes of unprecedented capacity, and further

1. Velopment of the million-volt lesting set with its preat possibilities for commercial athd research work

As in prevons articles on this sthbered, the electrical apparatus, turbinces, ole referoed lo, are all products of the ciencral


Fig. 2. Two-stage Mechanica!-drive Curtis Steam Turbine

Electric Company: but references to their cevelopment will serve as an indication of the tendencies in design and construction as well as the greneral trend of progress in the electrical manufacturing industry as a whole.

## TURBINES

The improvements made in Curtis turbines of $\overline{500-k w}$ capacity and larger during the year may be stmmarized as follows: Diaphragms except in the low pressure stages were so constructed that the nozzles can be easily removed and replaced. Nozzle partitions of superior mechanical design were produced for diaphragms in the low pressure stages. Both types of nozzles give a very high efficiency.

A steam sealed labyrinth type of packing with non-corrodible teeth was adopted and it is now standard practice to use cast steel for valve casings, turbine heads and other parts which may be subjected to temperatures above 4.0 deg. $F$. or more than $\overline{5}$ deg. $F$. superheat.

The vertical joint in the high pressure portion of the turbine casing was eliminated.

The standard emergency governor was redesigned so that it can be reset at 101 per cent of normal speed and the entire gorernor mechanism can be tested out without disconnecting the gencrator from the line.

There were under construction for the American Gas \& Electric Company four $3.5,000-\mathrm{kw}$ base load turbines designed for the following steam conditions: Pressure, .5001 lb . gauge, temperature, 72.5 deg. F. at
the throttle, vatumm, 1 in. absolute. Spectal features are incorporited in the design which should produce a plant economy greater thatn any heretofore reatized.

Among the large units under eronstruction Was a single casing turbine direet connected (6) a single gencrator which has a capacity
 kroil. It will operate at looto r.p.m.

A new type of small steam turbine, Fig. 2, for driving centrifugal pumps and similar apparatus was placed on the market. It is mate with a horizomtally split wheel casing and is arranged with one lwo or three stages to meet varying conditions of operation.

A eomplete line of small speed reduction gears, Fig. $\therefore$, was developed and they are already being extensively used for driving relatively low speed apparatus by means of turbines which normally run at higher speeds. These gears give speed ratios of from 2 to 1 up to 10 to 1 in various capacities up to $\delta(0)$ horse power.

## ELECTRIC PROPULSION

It the close of the year, there were completerl or under construction electric propelling equipments for seven double ended ferryboats, the first of which was completely equipped and placed in service in July.

This is an entirely new field for electric propulsion and, while less spectacular than


Fig 3. Single-reduction Gear for Steam Turbine Mechanical Drive
the operation of battleships or seagoing merchant craft, is of considerable economic importance due to the efficiency with which the electrical equipment meets the peculiar power requirements inherent in double ended ferryboat operation.

## 

Three distinct types of electrical equipment are represented in these boats. Two of them are equipped for Diesel engine electric directcurrent service two for turbine electric direct-current service and three for turbine clectric alternating-wiment service.

Two important factors determine the adoption of electric propulsion for these boats. First, they reguire propellers fore and aft ; and second, the most effieient method of propulsion is bye means of the stern propeller. Prior to the adoption of electric propulsion, numerous tests of existing ferryboats showed a high pereentage of loss due to the bow propeller and this meant that, in order to get the required speed, excess power in the equipment had to be provided to take care of the bow propeller losses. With the adoption of electric drive however, each propeller was prowided with an individual motor and the desired speed of rotation of either the bow or stem propeller could be obtained for each, independently of the other.

The first electrically propelled ferryboat to go into serrice was the Golden Gate. Fig. 1, plying between San Francisen and


Fig. 4. $360-\mathrm{kw}$. Diesel-engine-driven Generators on Ferryboat Golden Gate

Sausalito. Her propulsion equipment consists of two $500-\mathrm{h} . \mathrm{p}$. Diesel engines, each direct connected to a $360-\mathrm{kw}$., $2.5(0)-\mathrm{vol}$ d-c. generator. Fig. 4. and two ন.jo-h.p.. .o() ()rolt motors. Fig. .). one on each propeller shaft. The control of the electrical equipment
 houses or the chgine romen ats desiral

In weration, the stern prapeller rowna at full sped. whike the ben propeller is
 sated in driving tha bow propedter in this


Fig. 5. One of the Two 750-h.n. Propelling Motors on Ferryboat Golden Gate
way is of considerable coonomic importance.

The different speeds of the motors are oltained by varying the voltage of the generators. After the proper speed for the bow propeller has once been determined, it can be automatically controlled. On the boats using alternating current, this feature is secured by providing the propeller motors with two sets of poles, with suitable provision for shifting from one to the other, through the control panel.

The equipment for each of the two San Francisen-Oakland boats consists of a geared turbine operating at $3600 \mathrm{r} . \mathrm{p} . \mathrm{m}$. driving a $1000-\mathrm{kw}$., .300 -volt generator at $900 \mathrm{r} . \mathrm{p} . \mathrm{m}$. and two double-armature direct-current motors for the propellers, each rated at $120(0)$ h.p.. 500 volts at 12.5 r.p.m.

In addition to the above, there were under construction equipments for three ferryboats for operation between New York and Staten Island. The propelling equipment of each consists of one $2.2(0)-\mathrm{h} . \mathrm{p}$.. $3240-\mathrm{r} . \mathrm{p} . \mathrm{m} ., 2300-$ rolt, :3-phase turbine generator set which will supply power to two 2100 100-h.p.. Titi 12.2r.p.m.. 36.2 -pole, $230(1)-\mathrm{rolt}, 3$-phase induction motnrs, these double-rated motors being

Wenged to permit the operation of the bow propeller at the most efficient idling speed. These boats will be of execptional size, having an ower-all length of 216 ft , with 6 f -ft. overgraare beam and a depth of hull amidships of $1 \times .5 \mathrm{~F}$

The state owned lines of Italy are being electrified as rapidly as possible, employing the 3 -phase system, which has been in successful operation for a number of years. In the south of Italy, however, it is understood that extensive trials of $300(0)$-volt direct


Fig. 6. Electric Locomotives will Replace this Double-ended Type of Steam Locomotive on the Mexican Railway tetween Mexico City and Vera Cruz

## ELECTRIC RAILWAYS

## Steam Road Electrification

There was evidenced a renewed interest in steam road electrification throughout the world but actual electrification work was more marked in foreign countries than in the United States. This was due to a certain extent to the much higher price of coal and other fuel, in these countries, than in the United States.

On the European Continent, decided progress was made by France. Switzerland and Italy. The French Government, following its decision to standardize on 1.000 -volt direct current, initiated a program of electrification on the main lines of the ParisOrleans, the Midi, and the Paris-LyonsMediterranean systems, aggregating 5200 miles of track to be completed within 2() years. Contracts were placed, with affiliated companies representing the International General Electric Company, for more than $\$ 15,000,000$. Ineluded in this order is a large amount of substation and high tension line equipment to be supplied directly from the United States and a complete gearless electric passenger locomotive, as a sample equipment. A large quantity of other material built in accordance with G-E designs. will be manufactured in France.

Included in the initial program is a changewer of the present electrified lines of the Paris-Orleans Railway at Paris ( 600 volts d-e.) and of the Midi lines in the south of France (single-phase) to 1.500 volts direct current.
current are being made, pending the electrification of the southern lines.

In other parts of the world high voltage direct current has been selected as the most economical method of handling heavy freight and passenger trains electrically. It is of interest to note that altogether there are now nine railroad electrifications at 2400


Fig. 7. Interior of New Locomotive for Imperial Government Railways of Japan showing High-speed Circuit Breaker
and 3000 volts direct current. With one exception the General Electric Company has taken the principal part in designating equip)ment for these roads. The distribution of these lines is as follows:

An interesting leature of thas ehe rification will be the seplacement of a mosel t:on of steam locomotive, Fig 6, which was dubunt for operation in either direction and carmen all weight on the driving axles 'The praten
United States
Canada
South America
Mexico......
Spainn Sfrica.
South Afren

The successful operation of the Bethlehem Chile Iron Mines Company railway equipment, installed sercral years ago, was doubtless a factor in the selection of similar equipment for the Paulista Railway in Braziland the Chilean State Lines between Valparaiso and Santiago.

The experience of the Butte, Anaconda \& Pacific and the Chicago, Milwaukee \& St. Paul Railways conrinced the officials of the Mexican Railway that this was the proper system for the electrification of their severe grade line between Mexico City and Vera Cruz. The entire order for this equipment placed with the International General Electric Company includes ten 1.50 -ton 3000 -rolt


Fig. 9. Light-weight Chicago Surface Car
direct-current locomotives and a complete overhead distribution system. Energy will be purchased from the local power company and the entire 30 miles will be supplied from one substation.


Fig. 8. Light-weight Car, Detroit Railways
on the Mexican Railway include a maximum of $41 / 2$ per cent and regenerative electric braking will be employed on the new locomotives.

In the Cnited States one of the most active prospective electrifications at present is that of the Illinois Central Railroad. An engineering commission was appointed some time ago and after giving the subject the most careful consideration over a period of many months decided to adopt the 1.500 -volt direct-current system with overhead trolles.

In order to take care of increased traffic, the Baltimore \& Ohio Railroad recently ordered two 120-ton locomotires similar in most respects to those which they now have in operation.

The Imperial Government Railways of Japan laid out an extensive program of electrification and considerable equipment is already under construction. Two sample locomotives, Fig. 7. were shipped for trial on the 1200 -rolt lines between Tokio and Yokohama. All new electrifications will be at 1500 rolts and all of the

- proment will be capable of operating at this - mitage.

The most extensive edectrification intiater during the fear was that of the Sonth African Government Railways, (onalling 17.1 miles of route. All of the high (ension and sub)-
for 50 operating companies wated 3.s) larger items being as follows:
lllinois Traction System.
Virginia Railway \& Power
Lonisville Railways 75

Stone \& Webster Properties $10 \%$
Buffalo \& Lake Eric Traction (\%........ 2.


Fig. 10. Trackless Trolley Buses on Staten Island
station equipment will be furnished jointly by the International General Electric Company and the British Thomson-Houston Company. An interesting feature of these substations is the use of automatic equipment in both single-unit and two-unit stations. All of the motor-generator sets will be of the three-unit type of $2000-\mathrm{kw}$. capacity each.

## Light Weight Double Truck Cars

In the city and interurban electric railway field the outstanding activity was the continued purchase of light weight safety cars and light weight double truck cars. The trend toward light weight has extended from the interurban lines to the city roads as is evidenced by the number of these cars completed or under construction at the close of the year for service in large eities:

| Eoston Elevated Railway | 160 |
| :---: | :---: |
| United Electric Railway, Providenc | 150 |
| Detroit Strect Railways (Fig. 8) | 200 |
| Chicago Surface Lines (Fig. (1) | 45 |
| City Railway Co. of Dayton | 30 |

These ears are all equipped with light weight motors.

In addition to these, 21 other railway companies called for a total of 112 equipments for light weight double truck cars.

The demand for light weight safety cars continued and two-motor 2. 5 -h.p. equipments

The trackless trolley bus which has been operated with considerable success in New York City on Staten Island gave sufficiently good results to warrant the opening during the month of November of 10 miles of additional line with a new fleet of trackless trolley buses. All of these buses, Fig. 10,


Fig. 11. New High-speed Circuit Breaker
are equiped with (a-E motors, control and collecting devices.

Three sample trolley buses are also in operation; at Mimeapolis, Minn: Los Angeles, Calif.; and Petersturg, Vas

High Speed Circuit Bucakers






Fig. 12. Automatic Substation, Los Angeles Railway


Fig. 13. Control Equipmeni for Two Synchronous Motor-generators.
Star Cosl \& Coke Company, Red_Star, W. Va,

Pr. 11. were perfeeted for other than : 3000 ants and a latre mumber of installations were made on eootoolt ralwass. These cirenit breakers are being used not only for the protection of stations and melividual man chiness, but also for feceler protection. 'The high speed of rupture insures 100 per cent protection wherever this device is in use and short rirenits are interrupted withont affeeting the operation of the machines.

An accessory (beviee which was plateed in prombetion is the electrically locked and unlocked tumstike and farebox which is
the most notable foreign example being that of the South African Rathavs. In this comatry the Oregon Electric Railway will shortly place in service two stations of 1000 kw. and five of 500 kw . each on the 1200rolt lines operating out of Porthand, Ore. When this equipment is installed all of the substations on this system will be atutomatic, with the exception of one in Portland. Another important group) comprises five Tolokw. automatic control equipments for the substations of the Wilkes Barre \& Hazelton Railway; and what is probably the largest


Fig. 14. Main Relay Panels and Master Switches, Station R, Kansas City Power \& Light Company


Fig 15. $5000-\mathrm{kw}$. Waterwheel Generator Automatic Control Equipment
being installed in the stations of the New York subways.

## Automatic Railway Substations

The electric railways continued to be the principal users of the automatic substation. The intermittent and widely varying load to which railway substations, Fig. 12, are subjected makes the automatic control with the load adjusting equipment particularly suitable for this service.

During the year work on some exceptionally large installations was begun not only in the United States but in foreign countries,
order, in terms of total capacity, was placed by the United Railways of St. Louis for four $1000-\mathrm{kw}$. and two $2000-\mathrm{kw}$. control units. The Chicago, Aurora \& Elgin Railroad will install two $1000-\mathrm{kw}$. units as the result of a number of years trial service of a $500-\mathrm{kw}$. station at Warrenville. These stations will also use the new supervisory control.

In order to supplement substation capacity on the New York Central Terminal electrification, an automatic substation will be installed at 110th St. midway between the present station at 50 th St. and Station No. 2 at Mott Haven. This apparatus includes a

2000-kw. motor-gencrator set which will be remote controlled from one of the adjacent stations. Another 2000-kw, station is being installed by the Northwestern Elevated Railroad in Chicaro. This is the first application of the automatie substation to metropolitan elevated service. Other interesting construction for automatic railway substations included the following:

| Toronto Hydroclectric Commission | Three | 1000 |
| :---: | :---: | :---: |
| Pacific Electric Railway | One | 1.000 |
| Publie Scruice Co. of New Jersey | One | \% |

Cincinnati, Georgetown \& Porrsmouth
St. Railway. ......................... . . Four

Fig. 16. Control of Motor-generators for Three-wire System, with drum controller mounted on center panel

## AUTOMATIC STATIONS

Important advances were made in automatic station control equipments, both in the number and capacity of installations and in the development of indiridual derices.

Operating engineers are aware of the successful and economic operation of those equipment: which have been installed during the past fow years and today no investigation of proposed installations or revision of existing ones is complete without a full consideration of the application of automatic control equipment.

While the railways were the first to recognize the adrantages gained under automatic

operation, other industries hater mpidly followed their sxample with the result that this method has simee been applied to prattically all phases of power generation and distribntion, execpt steam-friven anits. Records to date show that there are more than 300 (i-E automatic units installed, controlling about $200,000 \mathrm{kw}$, of rotating clectrical machinery.

The largest, fully automatic, single-mit, hydro-electric station in the world. Fig. In, has equipment which controls a $2: 300$-volt, . 2000 -kw., (io-cyele waterwhed-driven generator.


Fig. 17. Reciosing Alternating-current Equipment Utilizing Direct-current Solenoids

An interesting application of the automatic principle was made. Fig. 14, to the existing a-c. distribution system of the Kansas City Power \& Light Company: Because of the shifting of the load centers and the increase in load demand, extensions of the system became necessary. Automatic control equipment successfuliy and economically solved the problem of operating substations having two or more incoming lines with two or more transformer banks, and the usual number of outgoing feeders.

In the control of motor-generators for 19.) 2.50-wh: 3 -wire systems. Fig. 16, pro-
watom is whaned during orepload perioxls b cutting in the differmtial fied. The motordriven drum controller, which fixes pesitively the sequence of operation of the equipunent. wats designed for patme monting.

Sn outstandin! development in mining: service wats the adontion loy the star Coal


Fig. 18. Reclosing Alternating-current Equipment Utilizing Alternating-current Motor Mechanism
\& Coke Company, Red Star, W. Ya., of control equipment, Fig. 13, for a two-unit motor-generator station, which has relay control throughout and uses the automatic reclosing feeder feature as part of the regular equipment.

## Alternating-current Reclosing Equipments

Among the new a-c. reclosing equipments produced, one utilizes a d-c. solenoid, Fig. 17, for reclosing, while in another an a-c. motor mechanism, Fig. 1s, is used. These equipments will reconnect the load to the source at the end of a definite time interval after it has opened on overload or short circuit. If the overload remains and the breaker opens three successive times within a definite time interval, it is locked out and must be reset by hand before automatic operation can be resumed.

A new type of device, Fig. 19, was dereloped for this service, whereby one, two or three breakers mar be reclosed three times in sequence. The device is motor operated and has three different time intervals between reclosures, with a maximum of approximately

212 minutes for the total timing. If one or two brobkers are looked out after three surerssive openings, the deviee will operate the remaining breakers. A slight positive time delay is provided between the reclosing of the breakers

## Direct-current Reclosing Equipments

Direct-current reclosing equipments were prepared for service in both 27.5 -volt mining, and for)-rolt rablway servier and have been standardizer for use on stul) end feed or combined stub) end and multiple feed conclitions.

The 2\%-5-volt equipment, Fig. 20, will automatically fulfill the following functions:

1. Disconnect the load from the source of power in case the voltage fails or the load exceeds a predetermined value.
2. The load will remain discomected a definite minimum time interval regardless of the cause of the opening.
3. At the expiration of this time interval, it will immediately reconnect the load 10 the source of power, provided the voltage is restored, or the overload is reduced to a predetermined value. There will be no attempt to reclose as long as a short circuit or heavy overload exists.

For 600 -volt railway service there was produced a reclosing equipment, Fig. 21, which makes use of the characteristics and


Fig. 19. Motor-operated Timer
advantages of the high speed circuit breaker. This equipment will:

1. Discriminate between short circuit and useful load such as is obtained on a typical railway feeder, and will allow current to be supplied for a maximum
time 10 all useful loads, but will instantly discomect the equipment from loads that indicate that power is being dissipated in short circuits.
2. Discomsect the equipment if curvent is beyond a maximum value, be means of "steady" overload setting of the high speed breaker.
B. Allow the breaker to remain closed during peak currents (below value stated in No. ©), which are caused ley useful loads: but if the rate of rise of current is such as to indicate a shom circuit, the braker will:
3. Trip out with high speed.

万. Operate on either stuh encl or multiple feed in either direction.
(i. "Trip free" from resetting mechanism if closed on overload, as in the case of manual operation (which is provided for this equipment). with the above mentioned high speed characteristics.
7. Open due to voltage failure.


The application of eromtor equipment to a single matit symedrombes motor-wemerator set for fort-volt railway service miluzal as panch-momed drum controller and a mow



Fig. 21. 600-volt Railway Service
Reclosing Equipment
the resistor type of load limiting equipment being used.

For a single-unit synchronous motorgenerator 3 -wire system, all devices, relays and auxiliary switches were mounted on the front of the panel. The equipment comprises relays for load control and the differential field type of load limiting equipment and a panel-mounted controller.

## Supervisory Systems

Due to the rapid increase in the number of automatic stations. there was a demand for some means of centralized supervision orer these units in a large power system. This demand was met successfully by two different methods of control and indication.

The first system known as the Selector Flye is for use where but few operations are desired per station and where the stations. cover a wide areat. A typical example of this is in interurban railwas service. 'The control wires in this case are of the ordinary telephone size, three in number, and run continuously from station to station. Impulses of alternate midirectional current are sent by eorle keys in the dispateher's office to


Fig. 22. Rotor Spider of $40,000-\mathrm{kv}-\mathrm{a}$ Generator for Shawinigan Engineering Company, Ltd., Canada
operate a particular selector in the outlying station which in turn closes a local circuit and performs a specific operation. Auxiliary switches are mechanically closed when the operation is completed and this in turn causes the release of a particular code which on the local motor drives a sending key. This operates a selector in the dispatcher's office which in turn lights a red or green lamp, indicating at all times the electrical position of the apparatus in the outlying station.

The second system is of the distributor trpe which finds use in power systems within a radius of 20 miles and where a large number of operations per station are required. Two cabinets, one in the dispatcher's office and one in the outlying station, have apparatus to control and indicate 50 circuit breakers.

The distributors operate in synchronism and distribute either a positive or negative impulse, originating at a particular dispatcher's key to a certain two-position relay at the outlying station. This rełay closes one of two local circuits depending on whether it receives a positive or negative impulse, and this action performs the lesired operation. Originating from an auxiliary switch on the controlled apparatus, an impulse
is similarly sent back over a separate wire to operate a relay in the dispatcher's office and indicate the electrical position of the controlled apparatus. Four wires are required between each pair of distributors.

## New Devices

(a) $\Lambda$ busbar thermal relay which provides a reliable means of insuring protection to feeders from overheating. It disconnects the feeder in case of overheating and reconnects it when it has cooled to a safe operating temperature.
(b) A slip relay to perform the necessary switching operations when a synchronous motor is pulled out of step by a heavy overload. This is a balanced relay which operates on line and exciter frequency.
(c) A new field relay constructed with a heavy copper dampening sleeve which prevents it from dropping out on a momentary dip in the field current. Because of its construction it will not pick up on a-c. but does on d-c. and this characteristic makes it suitable for a synchronous speed indicating device when connected across a synchronous converter armature. Also a similar type except that the dropout is instantaneous, and because of its low pickup and dropout values it is used as an exciter or generator relay.
(d) Another relay of similar construction is used as a field building relay, which permits the rapid building up of a generator field by short circuiting a portion of the field resistance and then opening its contacts at a predetermined value of voltage.
(e) A new type of notching relay which is adjustable and functions after two, three or four operations, depending on the setting.
(f) A high speed circuit breaker with added trip free and discriminating features. The trip free feature permits the automatic tripping of the breaker if overload exists when it is reset. The discriminating feature is obtained by the use of an inductive shunt, which sends the current through the "bucking bar" when the rate of rise of current is rapid as in the case of a short circuit, and this opens the breaker. On a normal rise in current as in the case of a useful load, the inductive shunt takes its share of the current and the breaker does not open unless the maximum setting is reached.
(g) An a-c. motor mechanism for operating oil circuit breakers with the least amount of energy demand, which makes use of the energy stored in a rotating mass to operate the breaker. It has found particular application in a-c, automatic reclosing equipments.

## WATERWHEEL GENERATORS

There were several notable hydro-electric developments undertaken during the year as well as a considerable expansion of existing plants and, as a result, a large number of machines of exceptional size were produced. At the close of the year, there were under construction waterwheel gencrators agyregating about $(600,000 \mathrm{kr}-\mathrm{a}$. in capacity

The shipments during the year included a vertical shaft unit for Shawinigan Engineering Company, Fig. 2.2, rated at $4(0,0)(0) \mathrm{kr}^{-2} .$, 11,000 volts. 3 phase, 60 cycles, for operation at $1381 / 3 \mathrm{r} . \mathrm{p} . \mathrm{m}$. At the time of its completion, this was the largest $\mathrm{G}-\mathrm{E}$ waterwheel generator constructed.

There were also completed three 20.000 -$\mathrm{kv}-\mathrm{a} ., \quad 6600$-volt. $100-\mathrm{r}$ p.m. generators for the Alabama Power Compans, and one $11,500-\mathrm{kr}-\mathrm{a} . .4200$-rolt, $106-\mathrm{r} . \mathrm{p} . \mathrm{m}$. unit for the Washington Water Power Company:

Among the foreign shipments were included four $13.750-\mathrm{kv}-\mathrm{a} ., 16600-$ rolt, $180-\mathrm{r} . \mathrm{p} . \mathrm{m}$. and two $13,000-\mathrm{kv}-\mathrm{a} . .6600-\mathrm{rol}$, , 37 . 5 -r.p.m. units for Japan. These were all vertical shaft machines. There were also two horizontal shaft machines each rated at $14.44 \mathrm{kv}-\mathrm{a}$., 6600 rolts, 600 r.p.m. for the Mexican Light and Power Company.

Among the units under construction were two of the largest vertical shaft waterwheeldriven generators in the world. They are rated at $65,000 \mathrm{kr}-\mathrm{a}$, , 12.000 volts, 2.5 cycles, 107 r.p.m. and are being built for the Niagara Falls Power Company.

The last three years have seen notable advances in the unit capacity of this type of G-E machine, the maximum for the three years being 1920, 32,500 kr-a.; 1921, 40,000 kv-a.; 1922, 65,000 kv-a.

Each of the $65,000-\mathrm{kr}-\mathrm{a}$. units has a $6.50-$ $\mathrm{kr}-\mathrm{a}$., $2 \varrho 00$-rolt exciter mounted between the rotor spider and the upper bearing bracket. The stators of these machines each weigh 443.000 lb ., rotor and shaft $767,000 \mathrm{lb}$. and miscellaneous parts 168.000 lb., the suspension thrust bearing having imposed on it a live load of $1,250,000 \mathrm{lb}$. The thrust bearing housing is provided with water coils for cooling the lubricating oil, and in addition, a small oil circulating system
for the bearing. equippect wath at filter, is provided.

These large machines hater the highest guaranted efficiencies exer given los waterwhed generators. At 6. (0) (N-kw mity bowerfactor, the efficioncy is !as I per cent and at 0.9 powerfactor, it is 17 -s per cent.

An musual extension to ath existing hydroelectric development was provided for be the construction of a $31,2.20-\mathrm{kr}-\mathrm{a}, \mathrm{B}, 200-$


Fig. 23. 31,250-kv-a. Generator to be mounted on top of an existing $18,000-\mathrm{kv}-\mathrm{a}$. vertical-shaft waterwheel generator
volt, 60 -cycle, 1.5612 -r.p.m. vertical generator, Fig. 23, for the Tallassee Power Company. This unit is designed for mounting on top of an existing $18,000-\mathrm{kr}-\mathrm{a}$., 36 -cycle generator which is provided with a waterwheel of sufficient power to operate the larger machine.

This special arrangement is due to commercial conditions and will permit the generation and sale of 60 -cycle energy during periods when the 36 -cycle service is not required. It also renders it possible to utilize the combined unit as a frequency changer if required.

Among the large generators under construction for foreign shipment there are two vertical shaft $25.000-\mathrm{kr}-\mathrm{a}$, 6600 -volt, .50-cycle, 12.5 -r.p.m. units for the Brazilian Hydro-electric Company and five horizontal shaft $22,22 \cdot 2-\mathrm{kr}-\mathrm{a} ., 11.000$-volt, 60 -cycle, $300-$ r.p.m. units for Japan. These latter machines are intended for a hydro-electric development in Formosa and are the largest machines of their type produced for foreign
-hmment Their installation will complete the largest capacity hydro-clectric station ontside of the Luited States. Other construction for Japan includes three Ift.14-ki-a., 11,000 -volt, 0 orevele generators.

As the result of assistance given to a hedroclectric plant in ladia in rebuilding four W.(0)O-ki-a. gencrators originally supplied he a European manulacturer, an additional gencrator rated at $10,000 \mathrm{kv}-\mathrm{a}$. , $\mathbf{0} 000$ volts, it eycles, 300 r.p.m. is being constructed.

Comstruction for domestic installation inclucles four 20,000-kr-a., 11,0000 -volt, 2.0)r.pm. units for the Itetch fletchy project,
 for the Southern California Edison Company
 units for the Western States Gas and Electric Company:

## SYNCHRONOUS CONDENSERS

While the maximum rating of previous years for these machines was not exceeded. there were under construction two units of record size.

One of these is for the Department of Public Service, Los Angeles. California. It is rated at $30,000 \mathrm{kv}-\mathrm{a}$., 7920 volts, 60 cycles . (i0) r.p.m. It can also be operated at . 0 () cycles, $500 \mathrm{r} . \mathrm{p} . \mathrm{m}$. and under these conditions it has a rating of $2.5,000 \mathrm{kr}-\mathrm{a}$., 6600 volts.

The other unit is rated at $30,000 \mathrm{kv}-\mathrm{a}$., 6600 volts, 50 cycles, 600 r.p.m., and is intended for the Southern California Edison Company. It is a duplicate of a machine already installed.

In addition to these, there were two synchronous condensers which exceeded in unit capacity any machines of this type preriously constructed for foreign installation. They are rated at $2.5,000 \mathrm{kv}-\mathrm{a} ., 11,000$ volts. (i0) cycles. $600 \mathrm{r} . \mathrm{p} . \mathrm{m}$. and are for the Nippon Electric Company of Japan.

## SYNCHRONOUS MOTORS

A new form of synchronous motor. Fig. 24 , for high starting duty was developed, which obriates by its method of operation the disadvantages heretofore considered inherent in symelhonous motor drive where overload starting conditions are involved.

The motor is so constructed that it is possible when starting to bring the armature, which is normally the stator, up to synchronous speed without any reference to the load. When the armature is at synchronous speed, the field is applied in the ordinary way and the rotor gradually brought
${ }^{11} 1$ ) to speed. The specd of the revolving stator is meanwhile brought down to zero by means of a powerful band brake which is locked in position when synchronons speed of the load has been attained.

By this methorl, the torque is applied gradually and the driven machine is brought up) (ospeed without a shock: 'Thereafter the motor functions, with its stator held stationary by the band brake, as an ordinary synchromous motor.

By means of this method of rotating the stator, this type of motor ean develop a starting torque of from 1.50 per cent to 300 per cent of normal throughout the entire starting period, as the torque available at the shaft is equal to anything below the pullout torque of the motor and is proportional to the current.

The new design economizes space as compared with previous methods of synchronous motor drive in that it eliminates the necessity for clutches between the motor and the load and the floor space normally required for additional bearings.

This new type of motor will make it possible to secure full advantage of the high power-factor characteristics of the synchronous motor without the disadvantages of additional equipment which have heretofore been necessary when the synchronous motor was required to start under overload.

## STEEL MILLS

During the year there was added 40,820 h.p. (normal continuous rating) to the existing capacity of main roll drives installed by the General Electric Company, bringing the total capacity to $52,800 \mathrm{~h} . \mathrm{p}$.

The fact that the substitution of electric main roll drives for existing steam driven units will show an excellent return on the investment is continually being demonstrated by additional installations. During the year, a number of steam engines were replaced by motor drive.

Probably foremost in importance is the equipment for the Youngstown Sheet and Tube Company for the electrical operation of a $30-\mathrm{in}$. reversing Universal skelp mill which will replace a twin simple reversing engine. The rolling mill motor is rated $4000 \mathrm{~h} . \mathrm{p}$. continuously at $80 \mathrm{r} . \mathrm{p} . \mathrm{m}$. and 11,500 h.p. maximum at 75 r.p.m. The maximum speed is 13.5 r.p.m. The flywheel set which furnishes power to the reversing motor consists of a $2.500-1$ l.p., $500-\mathrm{r} . \mathrm{p} . \mathrm{m}$., (6600-volt, 2.5 -cycle induction motor, two $1800-\mathrm{kw}$.,
(65) ()-volt direct-current generators and steel plate hywhee. This is the third enginedriven mill to be changed over to eleetric drive by the Youngstown Sheet and Tube Company, as early in 192.2 their two sheet mill engines were replaced be two $2000-\mathrm{h} . \mathrm{p}$, 2.50-r.p.m., 6600 -volt, 2.5 -cyele induction motors.

Another important installation which supersedes an engine drive is that of a motor rated 18.50 1450/92.5 h.p., $120 / 9+60 \mathrm{r} . \mathrm{p} . \mathrm{m}$. . $(6600$ volts, 2.$)$ eycles, which is direct connected to a 16 -in. hand bar mill at the Lackawama Plant of the Bethlehem Steel Company. This motor is provided with a double range Scherbius speed regulating set by means of which speed control is obtained from (60 up to $120 \mathrm{r} . \mathrm{p} . \mathrm{m}$.

At the Aliquippa Works of the Jones and Laughlin Steel Company a $5 \overline{5} 0$ ( h-h.p., 94r.p.m. 6600-volt, 2.j-cycle motor was installed to drive $21-\mathrm{in}$. and $1 \mathrm{~S}-\mathrm{in}$. billet mills, which were previously engine driven.

The engine which drove the $3: 3-\mathrm{in}$. structural mill at the Homestead Works of the Carnegie Steel Company was replaced by a 4000 -h.p.. 833 -r.p.m.. $6(600$-volt, 2.)-cycle induction motor with flywheel which is a duplicate of that driving the Liberty 110in. plate mill at the same plant.

Electric drives were under construction for a large number of new steel mill installations, among which are the following:

For driving a 40 -in. reversing blooming mill at the Riverside Works of the Otis Steel Company, an electrical equipment duplicating that which drives the $40-\mathrm{in}$. mill at the Sparrows Point Plant of the Bethlehem Steel Company. This equipment consists of a reversing motor rated $6.500 \mathrm{~h} . \mathrm{p}$. continuously at 50 r.p.m. and $17,000 \mathrm{~h} . \mathrm{p} . \mathrm{max}-$ imum at to r.p.m. The maximum speed is 120 r.p.m. The flywheel set which furnishes power to this reversing motor consists of a 3750 -h.p., 375 -r.p.m1., $6600-\mathrm{volt},$,2.5 -crcle induction motor, two $2.900-\mathrm{kw}$., 600 -volt directcurrent generators and a 50 -ton flywheel. Further installations at this same plant consist of electric drive for a 20 -in. hot strip mill, which consists of one $1800-\mathrm{h} . \mathrm{p}$., $500-$ r.p.m., 6600 -volt, 2.5-cycle constant-speed induction motor which drives the roughing stands. The first three finishing stands are driven by three $1.500-\mathrm{h} . \mathrm{p} ., 2 \mathrm{~S} 0420-\mathrm{r} . \mathrm{p} . \mathrm{m}$. . 600 -volt, shunt-wound. direct-current motors which are geared to the mills. The last three finishing stands are driven by direct-connected, 600 -volt, shunt-wound, direct-current
motors, one lano h.jp, 11.5 liti fom. one
 1.53 230 r.p.m. Power for the bote-wht direct-current rolling mill monors is Anatined from three ligot-kw, spachronoms converters

A high speed 10 -in. rod mill is being installed at the Portsmouth lant of the Whitaker-(ilessner Company, which will be
 (80)-volt, direct-current moter and three


Fig. 24. Old form (above) new form (below) of Synchronous Motors of identical rating
 current motors

For anxiliary drives it has been ahmost universal practice in the past to install totally enclosed mill-type, direct-current motors. Fig. -2.), but the engincers of the Otis Steel Company have departed from this practice and will use a number of open type. direct-current mill motors. Fig. 26. whose performance under the usual steel mill conditions will be watched with interest.

In June the electrical equipment for drising the 14 -in. hot-strip mill at the plant of the Trumbull Steel Company was put into successful operation. This installation, Fig. $2^{2}$, consists of a $12.50-\mathrm{h} . \mathrm{p}$. , 17.5 3.50r.p.m. motor, geared to four $14-\mathrm{in}$. roughing





 to the last four l-f-in. finishing stands. All


Fig. 25. A Typical Enclosed Mill-type Motor
motors are $i 00$ volts direct eurrent with speed control obtained by control of the motor field. Power is obtained from two 2300-kw. synchronous motor-generator sets.

It was necessary to depart from the usual practice of installing slip-ring type induction motors with speed regulating sets and to use direct-current motors on account of the special control required to maintain the exact speed relation between stands which is essential in a continuous mill of this type. So far as is known, this is the first installation of a high speed continuous mill with finishing stands driven by individual motors.

The kencrating equipment in steel mill power plants was increased chring the year by twelve installations of Curtis steam turbinc driven gencrators totaling 52,700 kw. In this list are included four 10,000)kw. madelnes, one for the Jones and daughlin


Fig. 26. A Typical Open Mill-type Motor

Steel Company, one for the Homestead Works of the Carnegie Steel Company, one for the Riverside Works of the Otis Steel Company and one for the Sparrows Point Plant of the Bethlehem Steel Company.

## ELECTRIC WELDING

A new design 400-ampere constant-potential are welding set, Fig. 2S, was produced. It is furnished with three resistors, two of


Fig. 27. Motor Room of $14-\mathrm{in}$. Hot-strip Mill of Trumbull Steel Co.

200 amperes for metallic are welding and one of 300 amperes for carbon welding． The 200 －ampere resistors for metallic welding have a current range from to to 200 amperes in 10 －ampere steps．The 300 －ampere resistor for carbon welding has a range from zero to 300 amperes in 30 －ampere steps．The combination of a 200 －ampere and a 300 －am－ pere resistor for carbon welding has a current range from 20 to 100 amperes in 5 －ampere steps，from 100 to 180 amperes in 10 －ampere steps，from 180 to 300 amperes in 15 －ampere steps and from 300 to 400 amperes in 20 － ampere steps．It is possible to use the two 200 －ampere and the one 300 －ampere resistor each independently of the other，thus allow－ ing two men to work at metallic are welding and one man on light carbon work at the same time．

A new design of portable semi－automatic welding equipment．Fig． 29 ，allows the oper－ ator to direct the are as required by the conditions of the work，yet retains the con－ tinuous feed features of the automatic equipment．

## A NEW INDUCTION FURNACE

In its earlier and simpler form，Fig．30， the induction furnace consists of an annular channel shaped crucible in which the entire charge is contained，and a primary winding interlinking with a laminated iron core which is common to both．When an alternating roltage is impressed on the primary winding． heat is generated by a secondary current flowing around the circuit of molten metal within the crucible．The very low resistance of the secondary circuit，combined with the
high leakage reactance，resth in fery bow power－factor，and make it lifficult fore large amomes of power into this furnate These objectionable features are exaggerated with higher comductivity metals．It is，in fact，impossible to operate the furnate on


Fig．29．Portable Semi－automat ic Welding Equipment
such metals as brass and copper，since the magnetic field surrounding the secondary becomes so powerful as to cause magnetic choking．It severs the continuity of the molten metal in the channel，causing periodic interruptions of the current and a continuous agitation of the molten metal．All of these difficulties and disadrantages have been overcome in the new furnace．

In the general construction of the new furnace，Fig．31，the melting pot and molten


Fig．28．400－amp．Constant－potential Are－welding Set

Went semblate of heating element have fern segremated The latter is in the form of a hollow evinder of comsiderable length, which sumames the ortimatral primare winding and ene It is located beneath the meltimg per and commmanates with it throweh soparate ports or ducts from both conds of the cerlimer. The secomdare circuit complenes itscli without passing through He medting pot.

The fore of dectromagnetio repulsion. whid exists between primary and secomdary in all 1 ramsformers, is mitized in this fumace (1) produce a brisk automatio circulation of


Fig. 30 Vertical and Horizontal Sections Illustrating the Simplest Form of Induction Furnace. The primars; winding is shown in section over the horizontal ring crucible
the molten metal between the heating circuit and the melting jot. The axial displacement between the primary and the secondary crilinders results in a variation throughout the length of the secondary of the fluid pressure caused by this force, giving maximum pressure at one end of the cylinder and minimum pressure at the other. This results in a flow of the metal from one end of the heating cylinder to the melting pot through one of the ducts, and from the melting pot through the other duct to the other end of the cylinder. In the cylinder itself, the flow is in an axial direction, transserse to the direction of the secondary current, and the flange shaped enlargements at the ends of the cylinder assist in distributing the incoming stream around one end, and in collecting the outgoing stream at the other. A free.
mintiferetional circulation of the metal is Homs obtained, in atream of large cross section, the rate of which may be varied as desired by merely shifting the axial position of the primary windling.

Athough the heat is gencrated and utilized in ent irely different parts of the farnace, this free, atutomatic, uni-directional circulation results in a small variation in temperature throughont the bath. Another result secured with this circulation is the climination of the possibility of magnetio choking. Under its own head, phas atmospheric pressure, metal woudd be supplied to the heating cylin-


Fig. 31. Two Vertical Sections at Right Angles to Each Other Illustrating the General Form of the New Repulsion Induction Furnace
(1) Molten metal bath in the melting pot. (2) Molten metal secondary cylinder in which heat is generated by induced current. (3) Ducts for uni-directional circulation of the molten metal. (4) Primary winding. (5) Laminated iron core. (6) Refractory lining. (7) Thermal insulation. (S) Charging door. (9) Pouring spout.
der through the ample duct provided for this purpose much more rapidly than it could be forced out through the other duct, against this same head, by the magnetic leakage field which constitutes the medium of repulsion between primary and secondary. These results make it practicable to force this furnace to any extent which is feasible for the primary winding and core, and particularly adapts it for the melling of high conductivity metals, such as copper, as well as for metals of lower conductivity. The size and rating for furnaces of this type is limited, if at all. only by such considerations as mechanical strength and reliability of the refractory linings, which may appear in large sizes.

Although this fumace, Fig. 32 , is new, it is already being used with pronomenced suecess on brass, bronze and copper, and its application will undoubtedly extend to other metals, beth mon-ferrous and ferrous. The power-factors oldained, eren with the high conductivity metals, approximate these ohtained with induction motors. Another important advantage which has been ineorporated in the commereial development of this furnare consists in the preformed and prefired linings, which can be installed in a fraction of the time and at a fraction of the cost required for the ordinary rammed lining. All parts of these linings ean be thoronglaly inspected before installation, thus. insuring a goed lining.

## INDUSTRIAL HEATING

There was a notable expansion in the use of industrial heating devices, ovens, furnaces. ete., employing metallic resistor heating units. As compared with $1!221$, the volume of applications of this mature for 1922 showed an increase of more than in per cent in kw. capacity. This particular method of applying


Fig. 32. 75 -kw. Repu!sion Induction Furnace
electricity for industrial heating has now been on a commercial basis for about six years during which time the heating units installed have aggregated about $.300,000 \mathrm{kw}$. in capacity.

## ELECTRIC STEAM GENERATOR

Is the reatit of womal loar int figh
 lypes of clectrically heated bunleg mak molustrial comblitims, at 170 ly gencrator was proxlacel. which grow lasl


Fig. 33. Internal Arrangement of Electric Steam Cenerator
effeciency for the current consumed and insures the utment simplicity and reliabibity in control and operation

The new steam generator is a compact self-contained unit. In the shell there are two compartments. Fig. :3:3, the upper where the steam is generated he passing electric current from the electroles through the water, and the fower, which serves as a hou well to which water is supplied be a feed water fump.

Water is continually circulated from the hot well to the electrole chamber be means of a centrifugal pump. Nore water is circulated than evaporated and perforations in the bottom of the upper compartment permit the excess water to drain hack into the hot well. By throttling the diseharge pipe of the circulating pump a definite water level can be maintainet in the electrode chamber and thereby a constant energy inpu1 is secured which is in no way dependent
unan the operation of the feed water pump) In antomatic doat type of feed water regulator maintains an adequate amome of water in the loot wedl.

The energy input into the grenerator ean be either increased or decreased by simply adjusting the throttle valve in the circulating pump discharge line. When it is desired to


Fig. 34. Electric Steam Generator Installed in a Paper Mill
reduce the power input into the generator it is unnecessary to remove any water from the shell.

By this ingenious combination of the hot well, circulating pump, and steam generator, all the water in the system is at practically the same temperature so that if the steam pressure drops, due to an increased demand, more of it is immediately turned into steam than in the types of boilers where only the upper section of the water is in contact with the electrodes.

By the use of suitable auxiliary apparatus, it is possible to maintain either constant steam pressure, constant temperature, constant power input, or variable power input so that the generator will absorb all excess power above that required by the normal power demand.

There has already feen established a wide field of application for the electric steam generator and a brief outline of some of the eonditions under which its operation may be profitalby undertaken may be of interest:

The utilization of surplus power when available in industrial plants, Fig. 3 - 4 , having their own water power generating equipments. Many industries must maintain steam on Sundays and holidays during which the total steam load can economically be taken over by the electric steam generating equipment, banking the fires of the coal furnaces, or shutting down oil fired boilers.

When industrial concerns purchase power on a fixed annual charge up to a certain maximum capacity, it is practically impossible to maintain this maximum capacity throughout the year, many kilowatt-hours of energy are paid for and not used. Some power systems have an excess of water power during the off peak period of the day which, due to lack of storage capacity, would be wasted. They must also maintain their boilers under pressure to carry the peak loads. With these conditions and especially where oil is used as fuel it would pay to put out the oil fires and maintain the boilers under pressure from electric steam generators using the surplus power which would otherwise be going over the dam.

There are often instances in industrial plants where comparatively small amounts of process steam are necessary at a considerable distance from the boiler house. It will often be found more profitable to transmit power from the generating plant and install a steam generator at the point of utilization than to transmit the steam long distances.

Another application which is in use both in Canada and the United States is for central power stations, that have excess energy, to install and maintain electric boilers in industrial plants and sell the energy on the basis of metered steam.

## ELECTRIC DYNAMOMETERS

The electric dynamometer was successfully introduced as a standard machine for the service station and garage, giving them facilities for testing out overhauled jobs and putting customers' cars in shape in the same way that new production in the automobile factories is tested out.

A special machine was developed for this purpose and a complete electrical-mechanical
unit constructed for taking the power from the rear wheels of the car. The unit includes the drums upon which the rear wheels run, together with a shaft, bearings, frame dynamometer, transmission and control. The car may be loaded with the driver in the seat, Fig. 3i, and the load and speed changed through a wide range by the handle of an enclosed safetr-tope controller within easy reach of the driver. This dynamometer forms a convenient, accurate means of testing the car under full load through a wide range of


Fig. 35. Dynamometer Chassis Test System for Garage Service
speeds right in the service shop; practically reproducing road conditions.

## SPRAGUE ELECTRIC HOISTS

A new hoist was brought out, having a capacity of $1 / 2$ ton and 1 ton and designed for manufacture in large quantities as a general purpose portable unit. The lift is 25 feet and the speed 25 feet per minute. It is built upon the unit principle, and consists of six sub-assemblies which are carried through manufacture separately and can be stocked separately. These sub-assemblies are the motor, the controller, the limit switch, the transmission, the brake, and control.

There are fewer parts in this hoist, Fig. 36 , than in any other ever developed for the same class of service. Its application is not limited to the field in which hoists have been generally used, such as ice plants, machine shops, foundries, newspaper offices, etc., but it can be applied wherever handling is
to be carried sut he overleatel moms and it offers a high spect, efficiont, labor-saving substitute for the chain block in comatless fields that have hitherto emplesedspurely mechanical means.


Fig. 36. $1 / 2$-ton Hoist with Push-button Control

## THE MAGNAR BATTERY CHARGER

An improved mechanical rectifier of the vibrating type was developed, particularly for charging storage batteries used in railway signal systems.


Fig. 37. Mechanical Rectifier for Railway Signal Service

In this service storage batteries are used to supply power for the operation of automatic block signals. Separate batteries are required at each signal location and each
bury is charged enontimunoly at a very -s rate by means of a rectifier. This statem is termed "thating charge" or "trickle charge." The charging rate is adiusted to a ralue which will just compensate for the arerage discharge of the battery. This rate rarely excecels ome ampere and frequemty is as low as one-tenth ampere

In the new rectitier, Fig. :3i. the armature (1) vibrating reed is tuned magnetically bey the thex of a permanent magnet. The armature is prosided with a face plate held in tension in the field of the magnet so that be barying this field the frequence of the armature can be changed.

## TRANSFORMERS

The renewed activities in hydro-electric development and the expansion of central station equipment resulted in an unprecedented production of transformers of all classer.

Among the large water-cooled type, there were under construction seven .0 -cyele. $20.0100-\mathrm{kr}-\mathrm{a}$. thase units which are larger in their physical dimensions than any transformers of this type previously built.

Among auto transformers, there were dighteen jo-cycle, single-phase units with an output capacity of $17,500 \mathrm{kT}-\mathrm{a}$. each. They are normally rated at $5.50 \mathrm{kr}-\mathrm{a}$. 220.000 volts Y or 200,000 rolts $\mathrm{Y} / 150,000$ volts 1 . They are supplied with a tertiary winding for full rated capacity. and are intended for interconnection between the 1.50 .000 -rolt and 220,000 -rolt lines of the Southern California Edison Company. An unusual feature of their operation is the fact that they are to be connected in the line without the usual high tension switches or lightning arrester protection.

The actirity in the construction of these large high roltage units is indicated by the fact that in 1921 , there were eleven $20.000-$ rolt transformers under construction, whereas in 1420 there were thirtr-fire with a total capacity of about $400,000 \mathrm{kr}-\mathrm{a}$. These figures include construction by both the General Electric Company and other manufacturers.

For wise with the $60.000-\mathrm{kr}-\mathrm{a}$. waterwheel generators which will be installed by the Niagara Falls Power Company, there were under construction ten water-cooled. ...)crocle. single-phase. $2.0 .000-\mathrm{kr}-\mathrm{a} . .65 .000 \mathrm{~T}^{\circ}$ 12.010 -volt transformers. While not exceeding in over-all phrsical dimensions transformers of this type previously built, they
required core and coils which, due to the low frequency at which they will operate, were of record size.

The largest $;$-phase water-cooled transformers consisted of eleren 60 -cyele, $15,750-$ ki-at., 10‥000 fif0(0)-volt units for the W'ateree Division of the Southern Power Company. This rating is based on a 40 -degree rise but


Fig. 38. 12,000-kv-a. Self-cooled Transformer. viewed from low-voltage side
these transformers will have the exceptional continuous rating of approximately 2., 000 kr-a.

The largest self-cooled. 3-phase transformers. Fig. 33. exer constructed, were completed and shipped during the year. Ther consist of two 60 -crele. $12.000-\mathrm{kr}-\mathrm{a}$., $44.000-13.60023004000$-volt units with a 50 per cent orerload capacity for two hours.

These transformers are provided with three windings. Fig. 39. for simultaneous operation, the 4.000 -rolt winding being designed for $12.000 \mathrm{kr}-\mathrm{a}$., the 13,600 -rolt winding for 8000 $\mathrm{kT}-\mathrm{a}$. and the 4000 -rolt winding for 4000 $\mathrm{kr}-\mathrm{a}$. This gives them an equiralent kr-a. rating greater than any other self-cooled transformer.

The general tendency toward the use of transformers of ever increasing capacity is indicated by the fact that the arerage size
of all wepe of mits produced during 102 . was about $1000 \mathrm{kr}-\mathrm{a}$. greater than the average for 1921. This development is indicated clearly by the figures in Table $A$, and is more uniform for the self-cooled type than the water-cooled type.

TABLE A
AVERAGE UNIT SIZE OF POWER TRANS. FORMERS IN KV-A.

| Year | Self Cooled | Wrater Cooled | All Types |
| :---: | :---: | :---: | :---: |
| 1919 | 117. | 432.5 | 21.50 |
| 1920 . | 1325 | 3175 | 2175 |
| 1921. | 1575 | +150 | 27 ¢0 |
| 1922 | 1700 | 60000 | 37.50 |

Another indication of the growth in the average size of transformers is the fact that during 1922 there were more units of 10.000 -kr-a. capacity and above, either completed or under construction, than the combined output in excess of $10.000 \mathrm{kr}-\mathrm{a}$. for all previous years.

There was a steady growth in the demand for transformers equipped with oil conservators and a much greater range of sizes and voltages were so furnished than in previous years. The voltage limitations for this equipment were abolished for all units of $2000 \mathrm{kr}-\mathrm{a}$, and above and the conservator was provided in special cases for even smaller capacities. The widespread adoption of this important auxiliary for securing maximum efficiency in the operation of transformers is indicated by the fact that, at the close of the year, there were in service approximately 1000 transformers with an aggregate.capacity of about $5,000,000 \mathrm{kv}-\mathrm{a}$. equipped with G-E conservators.

Important advances were made in another modern feature of transformer equipment by the application of ratio adjusters to larger sizes and higher voltages than in previous years. It has now been standardized for current capacities up to 500 amperes and a modified trpe was provided for four 12.50 -amp., 13,200 -rolt units. There were also under construction twenty-two 100-amp.. $1.50,0001-\mathrm{rolt}$ units each of which will be so equipped.

While the ratio adjuster was originally considered principally as a convenience by operators, its practical utility has been fully demonstrated in the saving of time effected by its use, especially on systems where transformers are utilized on interconnecting
lines. This experience has resulted in mumerous demands for the ration alluster for installation in large pewer transformers whel were installed prion to its development.

There was develoned a new system of cooling large oil insulated transfonners which must be operated in locations where an adequate supply of cooling water is mot


Fig. 39. Coils of $12.000-\mathrm{kv}-\mathrm{a}$. Self-cooled Transformer, viewed from high-voltage side
available. This ststem comprises a battery of radiators, installed either on the transformer or in a separate location, and in which the natural flow of oil between the transformer tank and the radiator is accelerated by the extemal application of low pressure air currents. Piping is run from the source of air supply to the radiator and the air is directed against the radiator sections by numerous small jets. In effect, these small streams of air wash the heat from large areas of the radiator and do it rery cfficiently with air delivered at only a few ounces pressure, thereby rendering it possible to cool large transformers economically by this method.

Another interesting auxiliary derice, Fig. 40, for transformer operation consists of an oil drying and purifying outfit which utilizes

Whe principle of the eentrifugal separator. The necessary heat is applied electrically and the rotating element is actuated by a geared motor drive the entire equipment being self-contained and mounted on a truck so as whe readily portable.


Fig. 40. Centrifugal Oil De-hydrator, capacity 300 gallons per hour

In order to meet a growing demand for reduced weight in distribution transformers designed for pole mounting, a complete new line of welded steel tanks was placed in production for transformers of from $10 \mathrm{kv}-\mathrm{a}$. to $100 \mathrm{kv}-\mathrm{a}$. These tanks are plain, corrugated or tubular, Figs. 41 and 42, and are electrically welded.

## MILLION-VOLT TEST

A million-volt, three-phase testing set, Fig. 43, was completed and placed in service in the high voltage engineering laboratory of the Pittsfield Works. A detailed description of this equipment appeared in the last issue of the Review. The design and construction is entirely new and intended expressly for operation at one million volts three-phase with grounded neutral, and one million volts single-phase to ground, although various other connections are possible, and it has actually been operated at $1,200,000$ volts single-phase with grounded neutral, and $1,500,000$ volts single-phase with ground 500,000 volts from one end, giving arcs up to $1+\mathrm{ft}$. in length between sharp points.

The spectacular features of this testing set are, however, of less importance than its
usefulness in exploring certain fiek of pure science which have always been the subject of conjecture, and in aiding in the design, construction and test of electrical apparatus of the highest voltage.

The design is similar to that of standard testing transformers of lower voltages and has many points of resemblance with power transformers, although it contains some unusual features and refinements of detail made necessary by the extreme high voltage and the special requirements of testing and research work.

## INDUCTION VOLTAGE REGULATORS

The necessity for extremely close regulation in the operation of induction voltage regulators resulted in the production of a new magnetic type of brake, Fig. $4+$, which is absolutely noiseless in operation and which insures practically instantancous stopping of the motor.

The brake consists of a base with two brake arms held in contact with the brake pulley by an adjustable spring. In addition there is provided an angular pull magnet which, when excited, operates a cam and releases the brake pressure on the motor pulley.

The field core for this magnet is assembled in the base casting and is held in place by a


Fig. 41. Plain Welded Steel Tank for Distribution Transformers


Fig. 42. Corrugated Welded Steel Tank for Distribution Transformers
clamping screw. This casting also contains the step bearing and bottom aligning bearing for the magnet armature. The upper bearing for the armature is contained in a drawn steel shell which is pressed on over the field core.

The upper end of the armature shaft is flatened on opposite sides to form a cam, which operates against two studs on the brake arms to release the brake pressure when the brake winding is excited. These studs are threaded and provided with lock nuts so that they may be adjusted to compensate for wear of the brake shoes.

Just below the cam on the brake armature shaft is a knurled collar by which the armature may be turned through an angle of 90 deg. in which position the cam will hold the brake open to permit operation of the regulator by hand.

## X-RAY TUBES

A new high voltage, high power X-ray tube was produced for deep therapy which operates on 200,000 volts, at $\delta$ milliamperes. This represents a considerable advance in voltage for X-ray tube operation.

The new tube has already been utilized industrially as well as for therapeutic work and is now in commercial production.

## THE MAGNETRON

The largest vacuum tube ever made consists essentially of a water-cooled cylindrical anode 30 in . long and $1 \frac{3}{4} \mathrm{in}$. in diameter. In the axis of the anode is a tungsten filament 0.4 in. in diameter and 22 in . long. This


Fig. 43. General Arrangement of Million-volt Testing Set
filament is excited by current of 1800 amp . at 10,000 cycles, the filament excitation requiring about 20 kw . The electron current to the cathode is interrupted 20,000 times per second. By the use of properly tuned circuits this can be used for the production of high
frequency pewer for radin on :my other purpose.

This particular lype of tube, which is called the Magnetron, Fig. Ah. will sumply 1000 kw . of $20,000-\mathrm{eycle}$ power at an efficiency of 70 per cent, operating with atl anode potential of 20,000 volts direct current.


Fig. 44. Magnetic Brake for Induction Regulator

## PALLOPHOTOPHONE

A new method of recording and reproducing sound was developed, which is a distinct improvement in many ways over all previous methods used and opens up several entirely new fields of application.

There are two distinct devices in the Pallophotophone, Fig. 4 (i, one for recording and one for reproducing the sound, and either may be used independently.

The recording derice consists essentially of a tiny mirror on which is reflected a beam of light. This mirror is attached to a delicately adjusted vibrating diaphragm and when sound waves cause the diaphragm to vibrate, the mirror oscillates and the ray of light causes the projection of corresponding oscillations upon a strip of photographic film which passes in front of the mirror in a continuous motion.

The film is then developed in the usual way and shows a succession of delicate dark markings which constitute the sound record.

In the reproducing device, the film passes in front of an arrangement of vacuum tubes which are sensitive to light so that the variations in the light falling on them, caused by the lines recorded on the film, produce electromotive force variations in the circuit in which they are connected. Therefore, as the film is moved in this device, an electrie

2: 111 is croated which corresponds with
 This electric corrent ean be mate an acthate
 broatcoasting apporatus directly


Fig. 45. $1000-\mathrm{kw}$. Vacuum Tube

Many interesting applications of this new device have already been made and a few possibilities can be briefly outlined as follows.

It makes possible the talking motion picture. for on a film of the normal width, both sound and action can be recorded simultaneously and projected in absolute synchronism. It is practically unlimited as to the length of recorl it can make and reproduce and is, therefore, suitable for recording speeches, debates, concert programs, in the
laking of evidence and for any purpense where a lengthy record of sommel is repuired. It can be duplicated and used as a film phenombaph and applied in radio telegraphys is producing wirelose signals and for atodio amplification.


Fig. 46. The Pallophotophone
It has alrearly been successfully applied in radio broadcasting.

## RADIO

Important progress was made in the design and manufacture of radio telephone and telegraph apparatus, both for commercial and amateur purposes. The sale of amateur equipment made a spectacular increase, due to the suddenly aroused interest of the public in the new application of radio to broadcasting.


Fig. 47. Radio Keceiver, Frequency Amplifier, and Detector Amplifier

The line of standardized component parts which had been originally designed for commercial purposes was later produced for the amateur. Broadcast receivers were built. making use of these parts and a line of sectional units, Fig. 47, such as the tuming unit, the 3 -stage radio frequency amplifier unit and the detector-amplifier unit, was developed. The main idea in these sets was the production of receivers, each of which would serve a definite function separately, and could also be easily combined.

One of the interesting applications of broadcast receiving was the installation


Fig. 48. Antenna Construction on Pullman train for radio reception en route
aboard several Pullman trains of equipment, Figs. 48 and 49, for entertaining the passengers with concerts throughout their journey, and to keep them informed on such topics as weather, market and stock reports.

In the line of commercial equipments, new requirements were met, due in many cases to broadcasting. In one case, a power company sought a duplex radio telephone installation with which it could provide, during times of storm, against possible interruption of communication between several of its stations $\overline{7} \overline{5}$ miles apart. At the same time, signals from nearby broadcasting stations operating on 360 meters were not to interfere with operation of this station on the only available wavelength of 400 meters. The set was to be operated through remote control
from a desk stamd ley the regular power house switchboard operators and to require no attention except that usually given to such moving parts as motors and gencrators. This set was installed and is operating successfully.


Fig. 49. Radio Broadcast Receiver Installation on Pullman train

For the use of amateurs and for installation on small boats and yachts there was produced a small radio telephone transmitter, Fig. 50, having an output of 20 watts in the antenna. It is built so that it can be operated either from a motor-generator set or from a


Fig. 50. Kenotron Rectifier and back view of Radio Transmitter
kenotron rectifier which was designed for this equipment. It can also be used on telegraph transmitter either continuous wave or interrupted continuous wave.

A new tube attachment for converting spark transmitters into vacuum tube con-
fimmus wave framsmitters, makes it possible for owners of spark seds to realize the advantages of contimatons wave tansmassion at a minimman cost. It has an output in the anteman of approximalely $1, \ldots \mathrm{k}$. continuous ware and a wavelength range of from 2000


Fig. 51. Aircraft Radio Transmitter
to 2400 meters. It utilizes the power equipment and high potential transformer of the spark transmitter and includes necessary switching apparatus so that communication can be transferred from the spark set to the tube attaehment.

This equipment. Fig. 52, makes it possible not only to carry on commmication with stations now listening-in on 2200 meters, but to carry on communication over much greater ranges with a 2 -kw. spark transmitter. During actual service tests conducted with one of these transmitters, a range of 1500 miles daylight, over water, was realized.

An aircraft transmitter was constructed for telegraph communication only with a continuous ware output in the antenna of 300 watts. Provision was also made for interrupted continuous wave telegraphy. The transmitter, Fig. $\bar{j} 1$, was designed to operate from a double current stream line generator driven by an automatic speed regulating propeller.

Two telegraph transmitters having outputs of $\because$ and 4 kw. respectively into the antemna were produced for installation in Mexico. They were the first sets to include the method
of construction which has now been adopted as stamdard for medium power tube transmitters, atd were a radical departure from vacuum tube transmitters previously built.

Each equipment, Fig. Sis, includes a kenotron rectifier which supplies the necessary high voltage direct current for the plate sunply of the oscillator unit and a so-called "tank eircuit" by means of which the transmitted wavelength is kept particularly constant and free from undesirable harmonics.

A number of telephone and telegraph transmitters were built for installation on submarines of the U. S. Navy, which include many novel features of construction and operation. They are designed for transmitting either on the flat top antenna or a loop and include a break-in system whereby the operator can listen-in between dots and fashes of the transmitted message; they are


Fig. 52. Vacuum Tube Radio Transmitting Equipment for use in connection with spark sets
available for three methods of communication and have an output of 600 watts continuous wave in the antenna. The complete equipment, Fig. it, is extremely restricted in dimensions on account of the service for which it was built.

New apparatus designed and manufactured for use with $200-\mathrm{kw}$. Alexanderson alternator equipments consisted of antema tuning inductances, remotely controlled antema wavechange switches and remotely controlled antema variometers.

In the operation of remotely controlled antenna rariometers* for indoor service, means for remote control from switchboard and hand control at the variometer were provided.

These variometers are connected in series with $200-\mathrm{kw}$. Alexanderson alternators. feeding energy to multiple tuncd antennae.
temperatures at fractional load in the windings. Closed circuits in the pipe framework are broken up be suitable insulators to prevent circulating currents.

The stationary and movable windings may be connected in series or parallel. The average range of inductances in series comneetion is $0.1!1$ to 1.1 milli-henries. The maximum coupling averages.$j 0$ per cent.

## CARRIER CURRENT

Complete carrier current equipment for telephone eommanication over the high tonsion transmission lines of power companies


Fig. 53. Four-kilowatt Vacuum Tube Radio Transmitting Equipment

They are used to maintain close adjustment of antenna tuning, particularly when antema capacity is varied by wind and sleet. Porcelain supports are used throughout for all parts connected in circuit and the conductor is composed of 4270 strands of fire mil copper wire, each strand insulated with enamel. Varnished cambric and treated braid form the outside insulation.

Due to the high-intensity high-frequency electro-magnetic field produced by the windings, no metals of any kind are used inside the windings. The top supports of the framework are of brass. Iron pipes attained high

[^0]was developed and a number of set. were installed.

The transmitter has an output of 50 watts and is rated at 7.5 miles. providing there are not a great number of tie-ins or transformer stations in this distance. The equipment, Fig. 55, includes a calling system whereby a bell is rung at the station called when the station calling actuates a push button on a desk stand forming part of the equipment.

## SWITCHING APPARATUS

A new line of oil circuit breakers was produced for indoor and outdoor service, the design of which was based on that of the 220.000 -rolt breaker furnished to the

Southem Codifornia Edison Company. These Weakers are for heavier intermpting eapacity serviee than any previously constructed. Theg have round tanks, and are designed to be entirely tight and non-oil throwing, are provided with explosion chambers, Fig. sof, and separating chambers, and have an internal operating mechanism. By internal mechanism is meant the placing of the


Fig. 54. Vacuum Tube Transmitter and Power Panel for use on Submarines
mechanism underneath the cover of the breaker. Units of this type for voltages from $\bar{T}, 500$ to 220,000 were constructed but the line has not yet been completely developerd.

The largest unit, Fig. 57, so far constructed has a rated carrying capacity of 600 amperes at $220,0(0)$ volts and an interrupting capacity of $1,-500,000 \mathrm{kv}-\mathrm{a}$. Breakers of $800-$ and $1200-$ ampere capacities for 73,000 volts were also produced with interrupting capacities up to $1,000,000) \mathrm{kv}-\mathrm{a}$.

The main contacts of the s00- and $1200-$ ampere sizes, Fig. js, consist of stationary copper brushes making contact on a movable blade which is mounted on the wooden operating rod. The plunger type contacts consist of copper rods fastened to the blade, or bridging member. These plungers make contact with a set of segmental contacts mounted in the upper end of the explosion chamber. An adapter is fastened to the bottom of the bushing and a contact retainer is threaded into the base of the adapter. The explosion chamber is bolted to the adapter.

Motor operated breakers, Fig. 59, were redesigned to make them oil tight and explosion proof. That is, the throwing of oil was entirely eliminated as well as the danger of secondary explosion of the gas in the oil tank above the oil.

These results were accomplished by an oil and gas tight cap on the oil vessel, a stuffing box in the upper insulators around the contact rods, and "Separating Chambers," Fig. 60, leading from the top of the oil tank.


Fig. 55. Transmitter Receiver for 50 -watt Carrier-current Telephone


Fig. 56. Cross Section of Explosion Chamber for 220,000-volt Oil Circuit Breaker

When the breaker is opened under load the are is interrupted in the lower part of the oil tank. The gas that is generated passes upward, mixed with some oil, through the center hole in the lower baffe and the gas and oil are partially separated while passing through the upper baffles. They are finally carried to the separating chamber where complete separation of the gas and oil and cooling of the gas take place. The oil then returns to the tank.

From the separating chambers the gas is carried through a system of communicating pipes to a general outlet. This outlet should be connected to a switch house header which should be piped away so that the gas will not be liberated in the switch house.

A new type of oil circuit breaker was designed for use on constant current transformer panels for scrics lighting, where oil circuit breakers are desired in place of the standard plug switches.

This circuit breaker meets the requirements of a small interrupting capacity breaker and is available for non-automatic operation only. It is manufactured in two varieties: a double-pole single-throw breaker for either the primary or the secondary side of the constant current transformer; and a doublepole single-throw breaker, Fig. 61, with an additional blade for short-circuiting the lighting circuit, that is, in this form the


Fig. 57. View showing Physical Size of the Largest 220,000-volt Oil Circuit Breaker


Weaker performs the same duty as one short-circuiting and two open-circhiting phag switehes.

When the breaker is nsed on the primary side of a transformer, it is necessary to ase fuses for owerland protection.


Fig. 61. Oil Circuit Breaker with Short Circuiting Switch, Double-pole, Single-throw

The large cell-monnted motor-operated central station oil circuit breakers, the oil tanks of which are electrically dead, were adapted to the so-called isolated phase arrangement. That is all breaker poles, disconnceting switches and bus work for any particular phase are installed in a cell structure isolated from each of the other phases.

Two detailed schemes of phase separation were worked out, namely, the horizontal separation and the vertical separation. In the horizontal method of separation, the breakers of all three phases may be on the same floor but each pole of any phase is separated from any pole of any other phase by a considerable distance.

In the vertical method of separation, each pole of any phase, and the bus for that phase, is located on a separate floor and the operating mechanism is on a floor above or below.

The paralleling mechanism for these circuit breakers may be placed between the two oil vessels of each pole and forms part of the breaker unit so that it is not necessary to install and set up a separate paralleling mechanism. This is particularly advantageous where isolated phase arrangements are involved.

A motor-driven centrifugal device, Fig. 62, was developed for closing circuit breakers. It makes use of centrifugal force in a manner
similar to that of a governor on a steam engine and will close any circuit breaker or combination of breakers now using the standard minersal lever for manual operation.

Although primarily designed for operation by alternating current, the motor on this device may be either for alternating or direct current. The device with the alternating current motor is particularly adapted to the operation of breakers in sections where no direct current is available and to automatic stations where alternating current is available and automatic reclosing is desired.

The motor revolves a pair of weights attached to the motor shaft, thereby developing a centrifugal force which tends to throw the weights outward and causes the operating mechanism to close the breaker.

Current is thrown on the motor either by a control switch or a rclay. The breaker may be tripped by hand, by a control switeh, or a relay and provision is made for mounting from one to four a-c. or d-c. trip coils as required.

Four tower arrangements were adopted and standardized for small outdoor stations


Fig. 62. Motor-operated Centrifugal Circuit Breaker Closing Device
ranging in capacities from 300 to 3,000 kv-a., 13,200 to 50,000 volts, but the same tower is used in each case; the only difference being the size and location of the steel bracket which supports the low tension busses.

Outdoor switch honses, Fig. (63, were provided with panels equipped with automatic reclosing equipment.

In many cases outcloor sub-stations are located in isolated places and in case of overload on the low tension fecder which trips out the oil circuit breaker, it would be necessary to reclose it by hand. To overcome this, an a-c. reclosing oil circuit breaker is used. This means a standard outdoor switch house with the addition of notching and roclosing relay and a-c. single-phase, 220-volt motor-operated mechanism for controlling the oil circuit breaker.

When the oil circuit breaker trips out on an overload, Fig. 64, the reclosing relay will reclose the breaker after an interval of from 5 to 30 seconds. If the overload has been cleared the breaker will remain closed. Should the orerload still persist, it will


Fig. 63. Outdoor Switch House, 6600 volts 50 amp., 3 phase, 60 cycles
again trip out and close after another interval of from 5 to 30 seconds. Should the overload still be on the line, the oil circuit breaker will trip out for the third time and remain open and locked out until manually reclosed and reset.

The development of this athamatio revorsing alternating-current equipnonent has math comomically feasible the supplying of altornat ing-eurrent encrgy to small, isolated commminties.


Fig. 64. Automatic Reclosing and Metering Equipment
(1) Alternating-current feeder overload time delay relay
(2) Alternating-current feeder notching relay-
(3) Alternating-current feeder reclosing relay
(4) Alternating-current feeder locking-out relay

Truck type panels were changed from knockdown to permanent unit housing which is completely assembled into a rectangular cabinet with welded joints. Disconnecting derices are so assembled and adjusted that they bear a permanent relation to the tracks on which depend the interchangeability of the trucks.

A standard line of these switching units, Fig. 6.5, includes feeder. generator, motor and bus section panels and circuit breakers for potentials up to and including 15,000 rolts. For circuits up to 7.000 volts the busses are mounted on the disconnecting device supports at the rear of the housing. Above this voltage they are mounted in a superstructure so that a uniform depth of housing may be maintained for all voltages.

Where it is desirable, it is now feasible to use steel pancls instead of slate panels, thereby eliminating the possibility of breakage and making it possible to ship assembled units which can be readily bolted together when receivel at the point of installation.

Insulated rod heavy duty bus supports, Fig. bif, were designed for use on low potential cirenits 110 ) 0 : $30(0)$ volts alternating or direct current, and up) to 10,000 amperes.

The construction comprises $1 \frac{1}{4}$-inn. pipe encased in colindrical insulators which en-


Fig. 65. Mechanism of Improved Truck-type Panel
ables it to withstand high tensile and torsional strains and the cantilever strength of the support is insured by anchoring the top and bottom of the insulated rods. Standard top and bottom fittings are used so that the supports may be pipe mounted and bolted to either a beam or bracket.

The busbar clamps are made to support 2 - and $4-\mathrm{in}$. busbars and require only two bolts. These clamps are so designed that when mounted on the insulated rod they are at a sufficient angle to give easy access for bolting together. This arrangement lends itself readily to the use of tier bus construction for minimizing heating in the conductors.

## Relays

The application of relay protection was extended to the protection of three-phase power cables against internal short circuits or short circuits to ground. This was accomplished by the combination of single-phase and polyphase directional relays.

The potential transformers used for the excitation of the potential coils of the directional relays are connected Y-delta instead of delta-delta as is customary. The poten-
tial coil of the single-phase directional relay is connected across an opening in the delta on the secondary side of the potential transformers, the potential coil of the polyphase relay is connected across the secondaries of the potential transformers as usual. In this scheme care must be taken in the selection of the potential transformers so that the ratio of transformation will make 110 volts available across the secondary coils.

A sheath transformer is wound about the cable and connected to the current coil of the single-phase directional relay while current transformers in each phase supply the excitation for the polyphase rclay.

In normal operation there will be no potential nor current impressed upon the single-phase relay nor will there be any operation of the polyphase relay. Should a fault develop in the cable, either between phases or to ground, the excess current flowing in the faulty member will induce a current in the sheath transformer supplying the single-phase relay and the fault will also be reflected by a potential across the open secondary delta, the direction of current flowing therefrom being determined by the location of the faulty leg or phase.

The standard induction type overload relay, Fig. 67, was improved and simplified.


Fig. 66. Insulated Rod-type Busbar Support for Heavy Duty 3500 volts up to $10,000 \mathrm{amp}$.

The saturating transformer was omitted and a single coil of edgewise wound copper now replaces the several windings previously used.

This relay is capable of carrying continuously the current required for operating at any tap setting.

Electrical clearances were increased in a number of cases and more accurate current adjustment is now possible. This adjustment *ean be made from the front of the panel without disturbing the relay.


Fig. 67. Imp-oved Induction Type Relay

A new induction orerload relay, Fig. 68, was produced for use in circuits where the available current for tripping is rery small, and where sensitiveness is desired without the use of current transformers. The capacity of its coil is one ampere and the relay must be used with the bushing transformer with which it is calibrated.


Fig. 69. Induction Polyphase Power Relay with Two Driving Elements

A relay was designed for reverse polarity service and also operates on under voltage. It is sensitive, having its movable armature, which actuates the relay contacts, and its potential coil lying in the field of a strong
permanent magnet. Lass of excitation of the potential coil or excitation with revorse polarity will cause the contacts woren). ('alibration adjustment is made be the mesement of a calibrating lever which changes the


Fig. 68. Induction Overload Relay for Low Currents
tension of a spring attached to the movable armature.

A new relay of the induction type was produced, similar in ajpearance to an induction watthour meter, and is used to indicate when load conditions exceed or fall below a predetermined value.

These relays, Fig. 69, are provided with two separate driving clements each element having a current and a potential coil which drive two disks mounted on a single vertical shaft. The shaft controls the operation of a set of double throw contacts which energize the coils of an auxiliary relay on over power and short circuit this coil on under power, thereby quickly and automatically relieving the main contacts of the relay of the burden of the circuit breaker tripping current by the use of the heavier contacts of the auxiliary relay which close instantaneously and remain closed as long as the tripping current flows.

An induction type balanced current relay was designed to give differential protection to delta connected machines when differential protection cannot be obtained in the usual manner. It is made with three elements each consisting of two magnets between which a disk revolves. The coil of one magnet, called the restraining coil, in each element is connected in one phase and exerts enough pull on the disk to hold the disk against a stop unless the pull of the other coil which is normally weaker, called the operating coil, and which is connected in another phase, is sufficient upon unbalanced loading to overcome the pull of the restrain-
my coil when the relay functions (o) trip the circuit breaker.

An interesting addition to a standard mit instantancous onerload relay consists of an indicating semaphore vane, Fig. 70 , by Which the fandy circuit is readily detected


Fig. 70. Overload Relay with Indicating Semaphore


Fig. 71. Inverse Time Delay Circuit Closing Overload Relay
after the operation of the relay. This relay is used to open the trip circuit of a feeder circuit breaker when the overload exceeds the interrupting capacity of the feeder circuit breaker, and thereby prevent the opening of the feeder breaker. The fault must then be cleared by a larger circuit breaker at a point nearer that of generation. Where a number of relays are used the semaphore indication is especially valuable.

A standard unit overload relay, Fig. 71, was provided with circuit opening and circuit closing contacts for controlling two circuits and can be used either for instantaneous or time delay operation. The arrangement of the fixed contacts provides for very flexible application and they may be changed by reversing the contacts to make the relay either circuit opening or circuit closing for controlling up to three circuits.

Another standard relay was provided with a notching lockout device to allow the circuit breaker to be closed a definite number of times on overload, within a given time, after which the circuit of the circuit breaker closing device is interrupted and locked open until the relay has been manually reset.

The notehing device can be adjusted to permit reclosing the circuit breaker one, two or three times before it is lorked out of service.

A potential auxiliary multi-contact relay, Figs. 72, was arranged for controlling ten circuits, nine of which are closed and one opened by the energizing of the relay coil.

It is applicable for use with other relays for machine protection when it is desirable to perform a number of separate functions at the same time. In the protection of synchronous generators it is often desirable to open two or more main circuit breakers, one or more field switches, operate a bell alarm circuit and perform other special functions. By using this relay for such applications the control wiring may be materially simplified.

Normally the relay contacts are held in place by a latch which is tripped upon operation of the relay and the contacts are rotated through an angle of 90 deg. from which latter position they must be manually reset to restore normal circuit conditions.

The circuit opening contacts are capable of opening the relay coil circuit, making the use of an auxiliary switch unnecessary with this device.


Fig. 72. Auxiliary Multi-contact Relay with Hand Reset

## LIGHTING

The estimated sales of tungsten filament lamps (excluding miniature, such as flashlight and automobile lamps) in the United States during 1922 were 205 million lamps. This is the greatest number of tungsten
filament lamps ever sold in any vear, Fig. 73, the previous record being in 1920 , when 202 millions were sold. In 1921 the sales were 160 millions.

The estimated carbon lamp sales in 19:2 were four millions; these lamps, therefore, represent less than $\xrightarrow[2]{ }$ per cent of the total In 1907 the carbon lamp sales reached their maximum of $6: 3$ millions which was the year the tungsten lamp was first put on the market. Ever since that time the percentage and actual number of carbon lamps has decreased each year. If this rate of decline continues, as it probably will, the carbon lamp will soon be a thing of the past.

As it never has been possible to make carbon lamps to an exact predetermined roltage, many central stations, in the carly years of the industry, co-operated with lamp manufacturers in adjusting their circuit roltage to something other than the then popular 110 volts. A demand was thus created for lamps for individual voltages between 100 and 130 . It became possible with the drawn tungsten filament lamp exactly to predetermine its voltage, and as the demand for carbon lamps rapidly declined, a movement, backed by all the electrical associations, was started in 1913 to reduce the number of lamp voltages to three standards: 110,115 and 120 . During the year 1922, about 90 per cent of the 100-130rolt lamps were of the three standards compared with 45 per cent in 1913. This has been accomplished by central stations gradually raising their circuit voltage to a standard as is indicated by the fact that in 1913 the average lamp voltage was 112.9 and in 1922 about 114.5. The odd roltage lamps sold in 1922, about 10 per cent of the $100-130$-volt range, cover mostly 112 - and 12.5 -volt lamps, about evenly divided.

While it is probably impractical in most cases to reduce 125 -volt circuits to 120 volts, there is little excuse for the use of 112 -volt lamps. Lamps labeled 110 volts should be used in their place as the continuation of the early practice, when tungsten lamps were fragile, of using 112 -volt lamps on 110 -volt circuits to obtain longer life, is no longer desirable with the present-day Mazda lamp, for it is done at a sacrifice of both candlepower and efficiency:

The most spectacular feature of incandescent lamp manufacture was the production of a 30,000 -watt unit, Fir. it, haring a capacity of about 60,000 mean spherical candle-power: the largest lamp of its kind
(ver manufactured. It hats a bull, 12 inches in diameter and $1 s^{1}$ a inches high and the filament is marle of tungsten wire, $1 / 10 \mathrm{inch}$ in diameter and 93 inches loms, constructed in four coils. This wire, if drawn into filament wire of the size used in the ewatt


Fig. 73. Number of Large Lamps Sold in the United States 1890-1922 (excluding miniature lamps)
lamp, would supply filaments for about 55,000 such lamps.

The lamp is gas fillecl and operates on a 120 -volt circuit, consuming 2.50 amperes. Its use up to the present time has been confined to experimental motion picture work and it has not yet been developed on a commercial basis.

The popularity of the 50 -watt white Mazda lamp together with the need of a similar lamp of a higher wattage resulted in the standardization of a ro-watt white Mazda lamp.

## Miniature Lamps

Considered mly as a part of the incandescent lamp industry of the country the position occupied by miniature lamps loes not seem very prominent. If riewed, however, as a separate inciustry, the figures are impressive
as there is every indication that approximately $83,000,000$ miniature lamps were used during 1922.

It is interesting to mote the trend of this branch of the industry from its beginning. Originally, manufacture consisted principally


Fig. 74. $10-\mathrm{kw} ., 30-\mathrm{kw}$. and $25-\mathrm{watt}$ Incandescent Lamps
of flashlight lamps, then considered only as novelties; the subsequent development of automobile lighting brought about a condition wherein the greater proportion of the lamps are now used in that service. Of the total quantity produced over $58,000,000$ were of distinctly automobile types.

However, it must not be thought that the flashlight industry has not developed during this same period. The consumption of flashlight lamps during the year amounted to practically $16,000,000$ lamps. At the time when flashlights were first considered commercially, the lamps required were only a few hundred thousands.

Besides automobile lighting and flashlight service there were other miscellaneous services which required nearly $9,000,000$ lamps. Of these practically all were for Christmas tree lighting outfits which required slightly over s,000,000 lamps.

There was a considerable increase in the application of small incandescent electric lamps to railway signals. These lamps are the 3.5 -volt, 0.3 -ampere type, operated from four cells of primary battery, and also the 13.5 -volt, 0.25 -ampere type operated from
sixteen cells of primary battery. In the former case the battery is used to light the lamp alone; in the latter case the battery is also used to operate the motors which raise the semaphore arms.

The lamps are used on what is known as "approach lighting" systems; that is, through track relays they light up on the approach of a train, and are extinguished when the train passes the signal. This is clone in order to conserve battery energy. Further conservation has been recently secured by the application of electric sun valves similar to those used in the lighthouse service. These valves automatically turn on the current on the approach of darkness, and shut it off when daylight comes.

One very great advantage of the incandescent lamp over the oil lamp which it is replacing in railway signal service is the fact that the oil lamp had to be refilled and cleaned at least every five days, whereas the incandescent electric lamp outfits have been run as long as a year without attention. This means a very great saving in labor.

There was also under development small transformers to operate these lamps where power circuits are available.

Some application of the same type of lamps and batteries was made to small range lights and buoy lights in the lighthouse service. Certain lenses previously equipped with oil and acetylene lamps were used with incandescent electric lamps, and tests have shown that the effective range of the incandescent lamp is materially greater than that of the acetylene or oil flame of equal candle-power.

In the case of the lighthouse service lamps, they are operated from a little electromagnetic flasher which causes the lamps to flash at any desired period. This flasher is so constructed as to consume very little battery energy.

The advantage of these electric lights over the oil light and acetylene light is that they do not need nearly so frequent attention as was the case with the previous lights. Furthermore, battery renewals can be handled in a very much smaller boat, and with less labor than was required to handle the large, heavy tanks of compressed gas previously used.

Incandescent lamps were also more generally utilized for highway crossing beacons. Tests have shown that a flashing red light is very much more effective than a fixed light. In the case of highway crossing beacons,
the lamps are being operated by batteries, and also by regular lighting circuits. In some cases where these flashing beacons are used at railroad grade crossings, they are operated by a storage battery, which, in turn, is charged by a primary battery, thus insuring the maximum reliability: In these cases, 6 -volt, 40 -watt lamps are being used, making an excecdingly conspicuous signal both by day and by night.

The success of light signals on railroads and in the handling of vehicular traffic on thoroughfares led to the demand for standardization of light signals throughout the country. At the request of the various safety and other organizations, the American Engineering Standards Committee appointed a sectional committee to undertake the problem of directing this standardization.

## Lighting Practice

In the lighting of a large number of small stores investigation showed that, within a decade, the popular type of luminaire or fixture had changed from the open glass reflector to the enclosing globe. A corresponding tendency was noted in the lighting of other classes of interiors.

Recently the styles in enclosing globes themselves have been changing so that now flat or squat shapes are becoming more and more common, Fig. 75. These tend to direct a relatively large proportion of the light in angles approaching the vertical and less light in those approaching the horizontal. This characteristic of distribution is advantageous, both on account of the better utilization of light and the reduction in glare.

There was a marked tendency prior to 1922, in luminaire design for home lighting, toward those styles which use candelabra and round bulb Mazda lamps, oftentimes without shades or external glassware. During the past year, there were indications of reaction, and an increasing number of luminaires were being equipped with shades and globes. Moreover, there appeared a number of types of special shading devices arranged for attaching to candle fixtures.

The annual fixture market is becoming more and more influential in directing styles in luminaire design. The market held in Milwaukee in the spring of 1922 was made the occasion for an extensive course in lighting practice, which should be influential in promoting proper applications of illumination, especially in connection with fixture design.

Portable luminaires, in the form of table and floor lamps, are becoming more and more popular in home lighting. Some of these have been made so as to direct light to the ceiling for the general illumination of the room. A new type of semi-indirect portable,


Fig. 75. A typical recent type of luminaire with globe so shaped as to direct as much light as practicable down. ward and upward rather than horizontally

Fig. 76, was put on the market which bids fair to further popularize the portable luminaire and improve the lighting of homes.

One of the most hopeful signs of improvement in home lighting was the issuance of a code on luminaire design, prepared by illuminating engineers in co-operation with fixture designers.

Extensive investigations of show window lighting in Clereland, Ohio, and Newark, N. J., definitely indicated the value of strong illumination, as well as colored light, in attracting attention to displays.

With the latest designs and arrangements of reflecting equipment, counts were made of the number of people stopping before the windows when lighted at various levelsfrom 15 foot-candles to 100 foot-candles. Similar counts were made with the light colored by means of screens over the openings of the reflectors. These figures were reduced to percentages, Fig. 77, of the number of people passing and showed remarkable increases in drawing power for the high intensity and colored lighting.

The investigators were convinced that, especially in the use of color, good taste is an important factor, and that the indiscriminate use of color is liable to defeat its own purpose.

Another investigation of show window lighting indicated that strong illumination provides the best known way of overcoming the interference of external reflection in window glass. This effect is most marked in the daytime, Fig. TS, and its correction, Fig. 79, de-


Fig. 76. Semi-indirect Portable Standard Providing Local Light and also throwing considerable light to the ceiling for general illumination
mands stronger lighting than is ordinarily required after dark. It is proposed to utilize powerful spotlights to accomplish this result.

Probably no other class of lighting has witnessed a greater advance in recent years than that of school rooms. One illuminating engineering organization reported having handled more school lighting installations during the year than of any other corresponding application. The pupils certainly need as good illumination as the office workers, and their requirements have been woefully neglected in the past. Three foot candles was apparently generally regarded as sufficient in installations made even as recently as two or three years ago, and it was not uncommon to find standard classrooms equipped with only one outlet capable of carrying not over a 100 -watt lamp. Much of the practice in the past year provided $S$ foot candles or more. While considerable progress has been made, the rast majority of
school rooms still seriously need more artificial light with modern diffusing equipment.

The engineers of the lamp manufacturers continued their investigations of the lighting requirements and conditions in various indlustries, issuing the results of these in bulletin form. Among others completed during the year were the wood-working industry, the textile industry, the food industries and the paper and pulp industry.

The action of artificial light on plant growth is still being given considerable altention. New investigators started experiments in this field and it is anticipated that in the near future elaborate equipment for experimental purposes will be available. A systematic and thorough study, with the various elements which enter into consideration of the problem carefully controlled, is planned. These tests should add appreciably to our knowledge of the subject.

Several temporary installations of mobile indirect lighting, made for certain special occasions, seem to suggest possibilities of enriching the artificial lighting of fine interiors and introducing some of the evanescence peculiar to daylight. In one instance,


Fig. 77. Resuit from 106 Tests made in two different cities on show windows in four stores

Fig. S0, by means of a motor rheostat device, colored lamps in indirect lighting pedestals projected bands of blending colors on the ceiling. These bands or waves of color moved across the ceiling so slowly that the motion was practically imperceptible. The
colors were so balanced that color wats mot dominant in the lighting of the tables. Shaded lamps of various colors were strewn along the tables and enriched the illumination

Diytight has gemerally been rexarded as a free gift. L'nder imodern conditions, however, with large high haiddinge erowted together, the cost of providing light wells,


Fig. 78. View of figure in window by natural light with the camera so located as to show the reflections of the sky line of the street opposite the store. It will be noted that the upper part of the figure is practically invisible


Fig. 80. Lighting pedestals which project slowly moving bands of blended color on the ceiling by means of a motor rheostat device
with spots of color. The effect was recornized as remarkably attractive and interesting by those who dined under the illumination.
and of supplying the heat lost through windows, is oftentimes greater than that of artificial light. During the year a paper was presented, which, without going to the other

- Dimeme points ont that these fatemos shouk the rationally eomsichered in eommection with Ho financial side of the lighting frob) lem.
latorler to farilitate the starly amd demonstration of lighting effeets in for home an expuisite moklel of two floors of atr aport-
installations. The model presents a very unusual opportunity of comparing and contrasting lighting effects, room by room.

During ly2l, street lighting was the only phase of electrical atetivity in which progression was unimperted. I bring 1922, still


Fig._81. Model Living Room, DiningiRoom and Hall used in teaching good lighting practice


Fig. 82. Bracket-type Street Lighting Units at East Cleveland, Ohio
ment house was built, with all furniture and lighting equipment exactly to the scale of one inch to the foot. The two stories of the model are furnished and finished the same-one apartment having excellent lighting and the other illustrating many of the common faults in ordinary home lighting
further advances were made and more street lighting material was purchased and installed than in any previous year. There was a greater appreciation on the part of the general public of the value of brighter streets, and financial conditions made it possible for public utility corporations to at least par-
tially meet the demand thereby created. Many improvements were made in deviees and in operating methods.

The application of ornamental lighting was chiefly limited to "White Ways" but during the year there was a definite trend toward a wider use of this class of lighting. not only in business districts but also in residential streets, boulevards and parks. The conditions to be met with respect to foliage and distribution of light stimulated the development of units which were not only ornamental but highly efficient.

A bracket type of unit was adopted for relighting East Cleveland, Ohio. The pole lines were all carried in alleys, and the feeder
lighting. Rochester, New Jork, eontinued to extend its illumination of this character and several other cities mate similar installations. Maywool, llinois, is being completely lighted by over 1 boo of these units.
lmprovements in luminous are lamps inclutled the use of rippled globes, more effective refleeting devices, and electrodes of longer life and higher efficiency. Compressed electrodes of square or oval shapes were found to give double the life previously secured and proportionately diminished trimming costs. For the highest class of illumination, the luminous are lamp still finds extensive use. Important extensions to existing systems were made in Detroit,


Fig. 83. Ornamental Lantern Type Lighting Unit


Fig. 84. Great Northern Ore Docks, Superior, Wis., illuminated by Highway Lighting Units
lines were brought out underground to slender, graceful standards in which the Mazda lamp is surrounded first by a Holophane dome refractor to divert the rays to the street surface, Fig. S2. and then inclosed in an alabaster rippled globe.

The location of a large number of ornamental units spread over a wide area gives added importance to features which reduce the cost of maintenance. Lantern type units, Fig. S3, with comparatively small flat panels of glass not easily broken in handling, and replaceable at low cost, were selected for a number of important installations; Cleveland and St. Paul being notable examples.

The elimination of globes as exemplified in a specially designed unit has demonstrated its value for certain types of residential

Salt Lake City, Buffalo, Toledo, Philadelphia, Pittsburgh, and other large cities.

There was an increasing realization by the general public of the dangerous conditions which exist at night, on unlighted highways handling high speed congested traffic. The Novalux highway lighting unit introduced in 1921 has made a splendid record of progress and installations have already been made in every section of the country, with the result that public sentiment is demanding the use of light as a preventative of present highway conditions.

About 48 per cent of the inhabitants of the United States live in the country and must use highways to reach shopping and market centers and an increasing percentage of the urban dwellers are also now using these
hoshmays at might. Vig. Sis, both for pleasure and commeree Congestion at many points is such at the present time that the installation of highway lighting units is justifiable from an economical standpoint alone.

It is almost unbelievable that with all the interest in the lighting of streets such momporant by-ways as alleys hate been ahmost
cities are now giving this problem careful consideration.

Other important uses were found for the highway lighting unit and during the year they were applied in the illumination of ore docks, Fig. St, bridges, ralway crossings, industrial railways, factory strects and for the gencral lighting of longr narrow areas.


Fig. 85. Highway Lighting tllumination, Miami, Fla.


Fig. 86 Arch of Jewels Illuminated at Salt Lake City
entirely neglected. Crime prevention is not complete when brightly lighted streets are paralleled by dark alleys. The distribution of light from the highway lighting unit suggests an ideal solution for this problem. The narrow alley-way may be brilliantly illuminated for a total length of 600 or 800 feet by the installation of these units with 250 -candle-power Mazda lamps. A number of

A complete line of small tubes with tungsten contacts immersed in mercury was developed for low voltage switching operations. These units find numerous applications in electrical systems for making and breaking contacts. They can be utilized not only in connection with traffic signals and street lighting units, but also in the control of electrical units operating in the industrial field.

An improvement in the projection of motion pictures using the Mazda lamp as a light source was made possible by the introduction of a split condenser. Sufficient
estimates and designs for this daborate lighting project were completed in seven weeks and the entire contrace including the manufacture of all electrical equipment. glass was taken from the center of the condenser to make the two halves slightly offset the projection of the filament images, thereby interposing on the curtain the bright bands of one fiek on the dark bands of the other. The resultant field is evenly illuminated and the intensity increased by 50 per cent dute to greater permissible concentration of light on the film.

Following the success of the magazine type of film for use in the series socket for street lighting, the same idea of using a roll of ribbon fuse was incorporated in a renewable plug fuse for interior wiring

The outstanding lighting demonstration of the year was the illumination of the Brazilian Centennial Exposition at Rio de Janeiro. In general, a lighting scheme similar to that used at the Panama-Pacific Exposition was selected except that in many instances the lighting sources were not concealed; brilliancy being subdued, however, by decorative fixtures and the use of color. Prominent features were the dome of the Palace of States,* decorated with 40,000 jewels, and the Avenue of Nations which was


Fig. 87. Panchromatic Fountain at the Pittsburgh Electric Show lighted by thirty standards, each carrying five 1000 -candle-power incandescent lamps in lanterns. The general illumination of the building façades was by means of banner and cartouche standards, each with four 1000 -watt lamps. Towers, domes and minarets were floodlighted by incandescent projectors and searchlights and the shadows thus created relieved by concealed red light.

It is noteworthy that the engincering.

[^1]fixtures, etc., and their installation, was executed in six months.

Spectacular lighting played prominent roles at the Rocky Mountain Electrical Exposition at Salt Lake City and the Pittsburgh Electric Show. At the former an arch of jewels, Fig. S6, was lighted by arc searchlights and at the latter show the principal feature was an illuminated panchromatic foumtain. Fig. 57. surmounted by a huge crystalier composed of 20,000 jewels.

# Electric Drive for Turbine Auxiliaries 

By John M. Drabelle<br>Mechanical ani Eldetrical Engineler, Iowa Rablway \& Light Company

The author gives the rating of the electrically-driven turbinc auxiliaries in his power station, describes their automatic operating features, and gives operating data of the results obtained. He is a strong advocate for driving power house auxiliaries with clectric motors in preference to any other method.-EDITOR.

The application of the electric drive to station anxiliaries of all kinds, due to the economies that are possible in the way of greater efficiency and lower costs of maintenance when compared with a small steam engine or turbine, is recciving more and more attention. The general tendency in power plant design is towards the auxiliary turbine for securing heat balance and to drive the various auxiliaries of the station with
rotor type for variable speed control. The vacurim pump is of Worthington manufacture of the Laidlaw feather valve type, size 29 in . by 18 in., driven by a 900 -r.p.m. G-E variable speed induction motor. The hotwell pump of the same manufacture is a two-stage centrifugal with a four-inch discharge, working against an external head of approximately 45 ft . It is driven by a 220 -volt, 725 -r.p.m. G-E wound rotor induction motor.


Fig. 1. Electric Drive of Turbine Auxiliaries permits of their centralized control by a panel such as that shown in the center of this illustration, which serves a $12,500-\mathrm{kv}-\mathrm{a}$. turbine generator
electric motors, with the exception however of the boiler ${ }_{4 i}$ feed pump. This article presupposes the condition that an auxiliary turbine laas been installed for the purpose of maintaining a heat balance and supplying the auxiliaries with electric power.

An application of the all-electric drive for a steam turbine has been made by the Iowa Railway and Light Company at Cedar Rapids, Iowa, on their unit No. 5. This unit is a Curtis turbine $-10,000 \mathrm{kw}$., $12,500 \mathrm{kv}-\mathrm{a} .$, $1800 \mathrm{r} . \mathrm{p} . \mathrm{m}$. The condenser is of the surface type supported on spring supports and has $18,000 \mathrm{sq} . \mathrm{ft}$. of surface. The circulating pump is a Worthington pump with 24 in. discharge and 30 in . stuction. This is driven by a 2200 -volt G-E induction motor, of the wound

The control of the hotwell, air, and circulating pump motors is handled by means of automatic controllers located in the basement near the auxiliaries to which they belong. The control of these contactor panels, however, is centralized on the control panel. The last named panel contains the watthour meter, ammeter and a push button station for each of the three auxiliaries, and in addition thereto an auxiliary drum controller for opening and closing the various contactors on the air and circulating pump panels. This permits the watch engineer to vary the speed of these auxiliaries from the main operating floor. With such an arrangement, the maximum flexibility can be secured, as well as greater ease in starting. Also from the watthour
meters a record can be kept of the input into the several auxiliaries, thereby giving a continuous check on their performance from hour to hour. The voltage of the hotwell and air pump motors is 220 volts, supplied by a bank of transformers located beside the control board. The circulating pump motor is operated directly from the 2300 -volt auxiliary bus and the control for this is an oil immersed contactor on the high voltage side, with standard contactors that short circuit the various banks of resistors on the low voltage side. Figs. 1 and 2 show the control panel with its push button stations, auxiliary drum controller, ammeters and watthour meters.

The time required for starting up the auxiliaries is rechuced to an absolute minimum, it being only necessary for the operating engineer to push a button and that particular auxiliary will start up at once. The starting, being entirely controlled by an automatic current limiting relay on the contactor panel, insures the maximum of protection to the equipment at all times. The air, circulating, and hotwell pumps require but about one minute to start. Consequently, in case the prime mover is needed quickly there are no long delays in going to the basement and opening and closing various valves, as in the case with steam driven auxiliaries, or when han-


Fig. 2. Turbine Generating Unit No. 5_ in the Cedar Rapids Power House of the Iowa Railway \& Light Company served by electrically-driven auxiliaries controlled by_ a panel shown in the backg;ound, and close up in Fig. I

This method of operating the auxiliaries with extreme flexibility and speed control is interesting. Except at very low loads, it is possible to operate entirely on the rise of temperature through the condenser. In other words, it is possible to maintain a constant temperature rise through the condenser at all times regardless of the load on the prime mover. As the load comes on, the watch engineer operates the controller increasing the speed of the circulating pump with a consequent increase in the amount of circulating water handled, thereby maintaining a constant temperature rise. The air pump is handled in the same way to maintain a constant absolute pressure. This pump is operated at the lowest possible speed without a drop in vacuum.
dling hand-operated devices if electrically driven.

For the month of October, 1921, the operating statistics of Unit No. 5 are as given below

Total generated. . . . . . . . . . . . . . . 3,882,000 Kw-hr.

| Vacuum pump. . . . . . . . . . . . . . . . . . | 10,587 <br> Hotwell pump . . . . . . . . . . . . <br> Circulating pump . . . . . . <br> 46,169 <br> Total auxiliaries . . . . . . | 63,314 |
| ---: | ---: | ---: |


|  | Per Cent of Total Generated |
| :---: | :---: |
| Vacuum pump. | 0.27 |
| Hotwell pump | 0.17 |
| Circulating pump | 1.17 |
| Total auxiliaries | 1.63 |

Two typical daily operating curves are given in Figs. 3 and 4 . These curves show the hourly generation of the mat and the total kilowatt-hour input into all of the auxiliaries, as well as the total separate input into the circulating, vacuum and hotwell pumps. Likewise, the percentage of amiliary power to the total generated is shown. The absolute pressure in inches of mercury and the rise in the circulating water temperature through the condenser is plotted. In the month of November, shown in Fig. 4, the circulating


Fig. 3
(2) That the variable speed drive on the air pump permits of greater flexibility to take care of the variation in the quantity of non-condensable gases earricd over with the steam, and of permitting the operation of the air pump at the lowest possible speed at all times, for the wear on a reciprocating machine of any kind is reduced approximately as the square of the speed. These curves further show a


Fig. 4

Figs. 3 and 4. Typical Daily Performance Curves of the Equipment shown in Fig. 2, for the month of October on the left, and the month of November on the right
water temperatures were much lower than in October, with consequent improvement in absolute pressure. A careful study and analysis of these statistics and curves will show:
(1) That the variable speed electric drive permits of greater flexibility and economies than a two-unit circulating pump drive, using either a constant speed electric motor or small steam turbines. That only sufficient water need be circulated at all times to take care of given load conditions and temperature of the circulating water. With the variable speed drive the maximum advantage is taken of the speed-torque characteristics of a centrifugal pump.
very appreciable saving in power for the rotating dry vacuum pump when compared to the constant speed hydraulic vacuum pump whose power requirements are more or less constant and independent of the amount of air or noncondensable gases handled by the air pump.
(3) That it permits of extremely rapid starting of the station auxiliaries to take care of emergency conditions and requires but one man to start them.

This installation has been in continuous service since June 5, 1921, and has stood up successfully under every operating condition imposed on it without a single failure or case of trouble of any kind.

# Modern Jet Condensers in Small Lighting Plants 

By R. E. Mellamer<br>


#### Abstract

Condensing equipment is essential to the economical operation of a steam power ghant. For the purpose there are many makes of condensers lut all can be grouped into two classilications; surface condensers and jet condensers. The question as 10 which is the better type to employ in a particular power phant shondat be determined wholly by the operating condions that exist at the plant. In the following article the ant fors describes a varicty of installations of the type of condenser manufactured liy the comprany with which he is connected.-Domor.


Condensers are generally classified into surface condensers, in which the exhaust steam and the condensing water are kept separated by the heat transmitting surfaces, and into jet condensers wherein the steam comes into direct contact with the water-the condensed steam, water, air, and other non-condensible gases are removed either by suitable pumps, a barometric column, or by means of the kinetic energy of water jets.

The choice of a condenser depends primarily upon the quantity and quality of water available for condensing purposes.

Where there is an abundant supply of fresh water that is sufficiently pure for boiler feeding purposes, the most suitable type of condenser to install is some form of jet condenser. Under these conditions such a condenser is probably the lowest in first cost and the most economical in operation.

The surface condenser is ordinarily chosen in instances where there is an abundant supply of cheap water, but of quality unsuitable for boiler feed. If the feed water must be drawn from the same source of supply, a water softening or purifying plant or an evaporator is necessary to make up the loss of feed mater due to leakage.

If the water supply is limited, but of good quality for boiler feed, a jet condenser would probably be the best one to install, together with some form of recooling plant of sufficient capacity to reduce the condensing water temperature to a point low enough for continuous working. By limited supply is meant a supply that is not sufficient in quantity to be discharged to waste, and relatively expensive to obtain.

Where there is a limited supply of water, unsuitable for boiler feed, a surface condenser should preferably be installed and operated in combination with a water cooling plant of ample capacity for continuous working, and with a water softening or purifying apparatus to make up the loss in boiler feed.

The purpose of this article is to review briefly modern tendencies in jet condenser practice and to describe some typical small
lighting plants and central stations where the low-level jet condenser is being used.

Fig. 1 shows the arrangement of a 1000 kw. jet condenser serving a General Electric: turbine-generator unit installed in the Municipal Electric Light Plant, Lansclale, Pa. The condenser is designed to handle 22.000 1 h of steam per hour, and to produce a 27 -in


Fig. 1. Plan and Elevation of Jet Condenser Connected to a General Electric 1000-kw. Turbine-generator; Municipal Electric Light Plant, Lansdale, Pa.
vacuum with 95 deg. F. water. It is located immediately below the turbine exhaust and is connected to the turbine by means of a copper expansion joint as shown. The diagram clearly illustrates the arrangement of the motor-driven injection and spray pumps. The condenser injection pump takes its suction from a cold well outside the power house. This cold well is supplied with water
from a spray pond located 300 ft . away. Provision is made to maintain the water in the hot well at the desired leved by means of float controlled values and switches.

The low-level jet condenser shown is of the ejector type; that is, the condensed steam, water, air, and other non-condensible gases are entrained amd discharged by the water


Fig. 2. Sectional Elevation of the Jet Condenser Shown in Fig. 1
jets on the ejector principle. A sectional elevation of the condenser is shown in Fig. 2. The injection water is supplied under pressure to a closed cylindrical chamber (nozzle case) within the condenser and forced through a ring of converging nozzles, accurately designed to discharge a specified amount of water according to the conditions of flow as determined by the water pressure
and the existing vacumm. As the water jets emerge from the nozzles, they are directed into the throat of the tail diffuser where they unite to form a single jet. The exhaust steam enters the condensing chamber through a top or side inlet opening, flows through the annular passages between the tapering rings of the combining tube, comes into direct contact with the converging water jets, and is condensed. Due to the combined effect of the external water pressure, the vacuum existing in the condenser, and gravity, the jets attain a velocity sufficiently high to entrain the condensed steam, air and other non-condensible gases, and to discharge them into the hot well against the pressure of the atmosphere. The water jets create the vacuum by condensing the stcam, and maintain it by entraining and removing the air and other non-condensible gases.

The rings are so designed and arranged as to direct the steam flow parallel to the water flow. The discharge end of the tail pipe is submerged about six inches in the hot well, and is effectively water sealed against air entering the condenser body.

The condenser operates with a water pressure of 9 lb . per sq. in. at the condenser water inlet, equal to 21 ft . head. This pressure is sufficient to overcome friction in the tail pipe, and to discharge the water against the pressure of the atmosphere.

The motor-driven centrifugal injection water pump of the multi-jet condenser operates under conditions favorable to centrifugal pumps; that is, with a suction lift rarely exceeding 15 ft . Thus the maximum pump efficiency is obtained, which lies between 70 and 80 per cent.

Fig. 3 shows a typical twin-jet condenser installation that is finding favor with a large number of central stations. The installation shown is that at the Wellsboro Electric Co., Wellsboro, Pa. This plant operates a $300-$ kw. General Electric turbine-generator connected to two multi-jet condensers installed in parallel and provided with separate motordriven centrifugal injection pumps. The dual arrangement makes it possible to shut down one condensing unit during periods of light load or during the cold season. It also provides a spare unit in case there is a necessity to overhaul or repair one of the condensers or pumps. Gate valves in the exhaust line permit either condenser to be cut out or started up without interfering with the operation of the other condenser. The flexibility thus provided has proven highly satisfactory.

The Bangor Electric Co., Bangor, Pa., operates a $750-k w$. General Electric turbinegenerator served by a multi-jet condenser arranged in the peculiar manner shown in Fig. 4.
buibling up the furbine foundation about four feet above the floor, the entire equipment was accommodaterl without the necessity of any excavation. The injection water for the condenser is suppliced from an elewated flume,


Fig. 3. Dual Arrangement of Jet Condensers Serving a General Electric $300-\mathrm{kw}$. Turbine-generator; Wellsboro Electric Co., Welisboro, Pa.

The absence of a basement and the lack of sufficient head room to place the condenser in the customary yertical position made necessary its installation in a position inclined 45 deg. to the vertical. The pit containing the hot well was already in existence, and by
under a natural head of about 10 lb ., and is discharged under gravity from the hot well to a creek alongside the power house. The water jets unite in the diffuser throat without perceptible deflection from the inclined condenser axis. The condensing unit operates


Fig. 4. Jet Condenser Inclined at 45 Deg. and Connected to a General Electric 750 -kw. Turbine-generator; Bangor Electric Co., Bangor, Pa.


Fig. 5. Jet Condenser Mounted above the Floor Level and Connected to a General Electric $500-\mathrm{kw}$. Turbine-generator; Municipal Elect:ic Light Plant, Edenton, N. C.
without any pumps whatever, and maintains a vacuum of 28 in . with 70 deg . water under full-load conditions.

The layout shown in Fig. 5 represents the condenser installation at the Municipal Electric Light Plant, Edenton, N. C., and shows a $.500-\mathrm{kw}$. General Electric turbine-generator connected to a multi-jet condenser with motor-driven injection pump. The absence of a basement and the fact that the tide water from the adjoining bay rises to within two feet of the turbine room floor made it necessary to place the condenser above the floor line in order to provide for the gravity return of the hot-well overflow to the bay. The exhaust loop is drained by means of a vacuum trap installed about three feet below the lowest point of the exhaust pipe.

The Municipal Light Plant, Greenville, Texas, has recently installed a $500-\mathrm{kw}$. General Electric turbine-generator and multijet condenser designed to maintain a vacuum of $2_{7}^{7} \mathrm{in}$. with 85 deg. injection water.

Figs. 6 and 7 show the condenser with motor-driven injection spray pumps. It will be noted that both pumps are connected to one motor. The usual procedure in starting $u_{p}$ the unit is to run the turbine non-condensing until full speed and the desired voltage are obtained. Thereupon the motor-driven pumps are put into service, and after the full injection pressure on the condenser is secured, the atmospheric relief valve is closed. This installation is typical and is successfully being adopted in a large number of small municipal lighting plants.


Fig. 6. $500-\mathrm{kw}$. General Electric Turbine-generator Installed at the Municipal Light Plant, Greenville, Texas

Table I is of interest inasmuch as it itemizes the data of a performance test conducted on a low-level multi-jet condenser of the larger size. This condenser is rated at $50,000 \mathrm{lb}$. steam per hr. at 28 in. vacuum and 70 deg. F . water. Although the test was conducted in summer, with injection water temperatures varying from $\overline{7} 0$ to $\overline{79}$ deg. F ., the vacuum referred to a $30-\mathrm{in}$. barometer was maintained well above 28 in . The condenser served a
$3000-\mathrm{kw}$. General Electric Curtis turbine, and the test was rum mer commercial conditions.

Fig. s gives the all-year performance of a twin multi-jet condenser operating under three-quarters load and under full-load conditions corresponding to 24,000 and 112,000 1b. of steam per hour respectirely. This condenser is installed at the Westport Station of the Consolidated Gas, Eleetric Light $\&$ Power Co., of Baltimore, Md., and at no


Fig. 7. Multi-jet Condenser at Greenville, Texas, Serving the Genera: Electric Turbine-generator shown in Fig. 6. The condenser is shown in the background and is directly below the turbine
time does the vacuum fall below 28 in., not exers in summer when the temperature of the injection water is as high as 7s deg. F.

The low first cost of the low-level multijet condenser radily permits the use of a
separate condenser for each steam unit, which is an arrangement that insures flexibility and minimum operating cost wherever there are several steam units one or more of which are not in operation at all times.



Fig. 8. Curves of Twin Multi-jet Condenser Performance at Three-quarters Load and at Full Load; Consolidated Gas, Electric Light \& Power Co., Baltimore, Md.

TABLE I
PERFORMANCE TEST OF LOW-LEVEL MULTI-JET CONDENSER

| Item | Date of test 1917 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Aug. 20 | Aug. 20 | Aug. 20 | Aug. 20 | Aug. 20 | Aug. 20 | Aug. 21 | Aug. 22 | Aug. 23 | Aug. 25 | Aug. 25 |
| Barometer, observed | in. | 29.41 | 29.41 | 29.41 | 29.41 | 29.41 | 29.41 | 29.4 | 29.32 | 29.22 | 29.37 | 29.37 |
| Vacuum, observed. | in. | 27.75 | 27.7 | 27.85 | 27.85 | 27.85 | 27.65 | 28.0 | 27.94 | 28.0 | 28.0 | 27.5 |
| Absolute pressure. . . . . . . . . . . . . | in. | 1.66 | 1.71 | 1.56 | 1.56 | 1.56 | 1.76 | 1.4 | 1.38 | 1.22 | 1.37 | 1.87 |
| Vacuum, referred to $30-\mathrm{in}$. barometer |  | 28.34 | 28.29 | 28.44 | 28.44 | 28.44 | 28.24 | 28.6 | 28.62 | 28.78 | 28.63 | 28.13 |
| Injection water temperature | deg. F. | 79 | 78 | 79 | 79 | 79 | 78 | 79 | 78 | 77 | 76 | 76 |
| Hot well temperature. | deg. F. | 88 | 83 | 84 | 87 | 87 | 88 | 84 | 84 | 80 | 87 | 88 |
| Vapor tension corresponding to hot well temperature. | in. | 1.334 | 1.137 | 1.174 | 1.292 | 1.292 | 1.334 | 1.174 | 1.174 | 1.032 | 1.292 | 1.334 |
| Vacuum theoretical | in. | 28.666 | 28.863 | 28.826 | 28.708 | 28.708 | 28.666 | 28.826 | 28.826 | 28.968 | 28.708 | 28.666 |
| Air tension. | in. | 0.326 | . 573 | . 386 | . 268 | 2.68 | . 426 | . 226 | . 206 | . 188 | . 078 | . 536 |
| Percentage of theoretical vacuum obtained. |  | 98.7 | 98.0 | 98.7 | 99.0 | 99.0 | 98.3 | 99.3 | 99.3 | 99.4 | 99.7 | 98.0 |
| Water pressure, lb. per sq. in |  |  |  | 9.5 | 8.5 | 6 | 0 | 7 |  | 8.5 | 8 | 10.5 |
| Water.... . . . . . . . . . . . | g.p.m. | 5520 | 7100 | 7150 | 7000 | 6600 | 5500 | 6780 | 7000 | 7600 | 7100 | 7300 |
| Steam. | 1b. per hr . | 28300 | 16850 | 17000 | 26800 | 25200 | 26250 | 16200 | 20000 | 10900 | 37350 | 41800 |
| B.t.u. per one lb. steam. . . . . . . . . . |  | 1045.4 | 1050.8 | 1049.4 | 1046.4 | 1046.4 | 1046.3 | 1046.9 | 1046.7 | 1049.0 | 1043.7 | 1047.2 |

# Communication By High Frequency Waves 

By John B. Tayoor

Consulting Enginem, Lighting Department, (bieneral Elf:iric Confany


#### Abstract

This title may give the impression that radio "broadcasting" and the use of "carrier" currents superposed on power lines are to be treated in detail. But a broad view of man's methods will dischse the fact that practically all forms of communication depend wholly, or in part, on the use of "watves." "High1" anncl "low" are relative terms; most of the waves involved in all forms of communication are of "high " fredurncy in comparison with the " 60 cycles" familiar to electrical engineers. The substance of this article was given as an address to the Southeastern Division of the N.E.L.A. at Atlanta, Ga., Sept. 15, 1922.-EDutor.


"Communication" means the passing of a fact, thought or idea of one intelligent individual to another. Social intercourse and general carrying on of the business of the world demands the interchange of ideas or information between persons near each other or widely separated. Many and various devices have been utilized in the service. of cutche form in prehistoric times, and becoming more highly developed with the progress of the race. The accumulated experience of the past and the latest inventions and scientific facts of the more immediate present are called on to aid communication.

Since an indiridual can receive impressions only through the senses (which are usually classified as five in number), we may consider first the relative importance of the several senses as they serve for receiving communication. In this service, the eye and the ear stand so far ahead of the other sense organs that touch, taste and smell may, for the normal individual, be almost dismissed from further consideration.

Facial expression and gesture communicate many ideas and serve as a basis for many actions, but, by far the larger part of communication is carried on by sound in the form of the spoken word, relying for its reception on the sense of hearing.

Now since sound is carried in the form of waves in matter, while light is propagated in the form of waves in space, it is apparent that these age-old means of communication have been dependent on waves. Audible musical sounds have frequencies which are limited to values between approximately 16 cycles and 16,000 cycles. While the fundamental frequency of the unusually deep roice of a man may be around 60 creles, there are accompanying oscillations of higher frequencies than the fundamental. Recording methods indicate that the more important of these for the understanding of speech are in the neighborhood of 1000 cycles; so that, if we call 1000 cycles "high" on our reference scale of frequencies, communications by speech are by means of high frequency waves.

Those who are more interested in radio broadcasting than in power transmission may think of 1000 cycles as "low" frequency, but there should be no argument over whether the frequency for light waves (by which communications received by the eye are carried) is "high" or "low." The production of rainbow images from gratings composed of many ruled lines close together furnishes a method for computing the frequency of light waves of different colors, and if we set down the figure $51 / 2$, followed by 14 ciphers, we have what is approximately the average frequency of light. (.50,000,$000,000,000=5.50$ trillion per second.) A somewhat lower frequency, say 400 trillion, gives a red light, while the extreme violet which is risible has a frequency of over 700 trillion-in round figures we may call it a quadrillion.

Our lungs and rocal apparatus may be regarded as power plants for generating and modulating variable frequency waves which are broadcast through the air.

Glow worms and fircflies possess apparatus for generating and transmitting the very high frequency waves of greenish light which may serve as signals or communications to others of their kind. However, the more communicative humans are not endowed with light-producing apparatus and visual communications are dependent on outside agencies such as the sun, moon, candles or electric lamps as generators of highfrequency energy. These may be started and stopped, or controlled and modulated by human thought and action. From this it appears that the great central station for supply of energy for visual communication is the sun, and, to continue the simile, we may say that whenever we communicate by look or sign using artificial light, we are drawing on thergy from portalle or isolated generating stations of energy in the form of high frequency waves.

Also, from time immemorial, men have used supplementary devices to extend the range of communication by means of sound

W:aves. 'The drum, the trumpet, the alarm bell permit a man to convert a greater portion of his muscular conergy into sombl than do the lungs and rocal apparatus. Steam whistles and fog homs with motor driven atir compressors are extensions of the drumb and trumper ifloa, drawing on and controlling power in excess of all that a single man or group of men together can sujply.

The lower and mpper figures for the sound frequencies ordinarily used are set by the receptive limits of the receiving ear and brain. With supplementary generating and receiving apparatus, it is possible to signal and communicate by sound waves using frequencies below, and also above, the audible range. There are certain advantages from a strategic standpoint in warfare and possibly other advantages under special circumstances in communicating by means of fairly high frequency waves, which give musical pitches too high to make any impression directly on the maided ear. There are similar strategic and possibly commercial advantages in signaling and communicating, using light waves at frequencies outside of the comparatively restricted frequency sensibility of the eye. Thus, for example, infra-red rays or waves ponetrate fog better than visible rays, and special projectors and receivers may be devised to communicate ship positions and avoid collisions at sea.

Similarly, the use of ultra-violet light for communicating permits the use of very simple receiving devices in the form of fluorescent material and has advantages in secret communications.

The working distance with ultra-violet light is limited because these extremely high frequency waves are readily absorbed. The infra-red rays, while less obstructed by the fine particles of mist forming fog, will, however, be limited in working distances, so that waves of still lower frequency are advantageous where great distances, with intervening objects and substantial curvature of the earth, are encountered.

Now, while entirely different methods and apparatus are employed for generating and controlling the waves of radio telegraphy and teleplony than are used for producing and controlling light, many tests confirm the theory that the nature of X-rays, ultra-violet light, visible light, infra-red light, heat waves and electrical radiation differ only in numerical quantities and not at all in fundamental properties. The distinction between waves classified into these
several kroups, and sound waves (including those of too low pitch and too high pitch to be heard) is that sound waves are propagated in matter (cither as gas, liquicl or solid) while the "radiation" waves are propagated by space. And there is no known place or means of securing a cavity which will not carry electrical, heat, light or X-ray rarliation.

A single candle throws its beam so that, under moderately clear air conditions, it can be seen for several miles. It requires a heary bell or a powerful whistle or fog horn to be heard the same distance, even under highly favorable atmospheric conditions, and these favoring atmospheric conditions are seldom found. This comparison indicates one reason why communications over distances of several miles by lights or visual signals have been found more dependable and of greater range than sound signals. Though bell buoys and fog horns are used in large numbers, the navigator's principal reliance for many years has been on the lighthouse.

An earlicr statement was that red light or infra-red radiation penetrated fog better than blue light, and, as the frequency of radiation is further reduced from trillions down to millions and tens of thousands, the limiting working distances set by absorption are advanced. Thus, the radiation art has been so extended that there is fair evidence that communicating waves completely encircle the globe.

From this line of presentation, we see that man has always been ready to make use of supplementary devices to aid him in his communications. Every new discovery or invention that serves toward this end has been pressed into service.

The writer was born within a few months of the time, and within a few miles of the place of Bell's successful experiments in communicating by speech over a wire. The "marvelous toy" "proved to be something more than a plaything or a fad, and Alexander Graham Bell, who died this summer, lived long enough to see his invention so widely extended and generally used as to greatly modify the whole conduct of business and social communications.

In a parallel line, the experimental detection of electric radiation from a small spark has developed means for holding communication with ships in mid-ocean. There is even now no technical difficulty in so arranging that every individual in the country
may at the same instant listen to a single voice.

There is another adrantage in communicating by radiation waves in space rather than by sound waves in matter. The speed of propagation of sound waves in air is, roughly. a mile in five seconds, in water about four times as great, but in no known material is it more than 12 to 15 times as fast as in air. Imagine a solid rod of steel or wood in which sound is propagated with a velocity of, say, three miles in each second, and also imagine that this rod extends from Atlanta to Washington, a distance of 600 miles. If the absorption in the rod were so small that a sound wave started at one end could be detected at the other, the wave would require nearly 200 seconds (or about three minutes) to travel the distance. Six minutes would pass before hearing a reply to the first "Hello." Obviously, anything approaching a "conversation" over such a long distance telephone would be quite different from what we actually have with the electric telephone where the interval in a 600 -mile circuit is such a small fraction of a second as to be altogether inappreciable.

A light wave or electric wave is one million times as fast as sound in air.

Before the practical development of wireless telegraphy and radio telephone broadcasting, experiments had been conducted using radiation from a beam of light as a speech carrier from a sending to a recciving station. An arc lamp at the sending end furnished the extremely high frequency radiation, a diaphragm vibrated by the voice increased and decreased the light, and a selenium cell at the receiving end served as detector and converter of the radiation. With fundamental features the same, a popular " 360 -meter broadcasting station" sends out waves of lower frequency than the radiation from the arc lamp. The strength of these 360 -meter, or $\$ 33,000-$ cycle, waves goes up and down corresponding to the control exercised by each vibration of the spoken voice at the broadcasting station. Neither the eve, the ear nor any other human sense organ is adapted to take note of this radiation. The selenium cell which responded to the radiation from the arc lamp does not respond well at the broadcasting frequency of $\$ 33,000$ cycles per second. Other devices like crystals or vacuum tubes are able to respond accurately to the high frequency currents. These detectors rectify the high frequency current and deliver
to the telephone receiver a suitable form of current for producing sounds which reach the ear and are sensed by the listener.

Whether mankind will ever be endowed or acquire ability to receive electrical radiation as a sixth sense seems pure speculation.

It is common observation that light "travels in straight lines." 'This is equivalent to saying that intervening opaque objects cast sharply defined shadows.

We know, in dealing with sound waves, that there is a bending of the waves around objects of moderate size. It is a surprise to many to learn that quite small objects such, for example, as a ten-cent piece, may be held to cast a quite well defined sound shadow, provided the source of sound is of small dimensions and of ligh pitch. As a matter of fact, the sharpness of shadows and the bending of waves of any kind around opaque objects is determined by the relative dimensions of the object and the length of the wave.
"Wireless" waves are long in comparison with objects such as buildings, and it is difficult to find a spot effectively shielded from such radiation. This feature is an advantage in signals or conversations which are intended for broadcast reception, but a disadvantage where the communication is of a personal or private nature and a single line of transmission would be preferred. Such a single line of transmission, besides aiding the confidential nature of the communication, would permit the carrying on simultaneously of a large number of commumications without interference; and, in the present state of the art, the interfering nature of one communication with another is more troublesome than the lack of secrecs:

Before the days of the electric telephone, speaking tubes connecting one room of a building with another or between buildings not too widely separated were frequently installed. These not only permitted the use of sound waves for confidential communication but the restriction of the waves by the walls of the tube conserved some of the energy so that greater distances could be covered in rocal communication through the tube than through the open air.

Parallel with the use of pipes and tubes for directing sonnd waves, we now see the ordinary telegraph, telephone, trolley wires and transmission line conductors used for the purpose of guiding and conserving a relatively small power in high frequency waves. These waves are superposed on the larger and more
powerful currents for which the various electrical circuits have beon initially installed.

Without going into detail on the particular pieces of apparatus and schemes of connection, we may say very generally that sending and receiving equipment is of the same form as used for radio telegraphy and telephony through space. In place of the "antemna" a condenser of moderate dimensions provides a path to lead the communication bearing "carrier" current onto the signal wire, trolley or transmission line.

The field is a fascinating one but limitations of time prevent elaborating interesting features. Possibly, in closing, a few words on a point which seems to bother the novice may be in order: The tuning of a radio receiving set so as to pick up, at will, one broadeasting station or another, and then to pick up anateur stations, government time signals, ships and transatlantic stations, appears to be a wonderful proceeding.

It is true that, in the midst of a confusion of sounds, we are able to concentrate the attention on one particular speaker or instrument, but the concentration appears to be mental more than a screening or filtering action in the ear itself. Among many visual signals, the eye is able to focus principally on one particular point or object, excluding entirely those which are outside the field of vision, and mentally excluding those which, while within the field of vision, are not the central object. If visual signals come from a given distant point, light of different colors may be used for simultaneous communications. An individual, by his mental capacity, may concentrate on a particular color, and this concentration is
simikar to the concentration on a particular voice or instrument. As an aid to receiving signals coming in different colors, colored glasses or filters may be used so that the individual sees only the color of that particular frequency which is transmitted by the filter before his eyes. This is really a process of selective tuning, and there is a close similarity between it and the tuning used with a radio receiving set.

There is a further similarity between the selective receiving of visual signals by setting the eyes in a particular direction and the use of aerial coils or "loops" for receiving radio communications. The "field of vision" of the coil aerial is broader than the field of vision in the case of the eye. Nevertheless, it is possible to set the coil so as to completely exclude an interfering station which may be working at practically the same wavelength, or frequency, as the station desired, provided they are in different directions from the receiving point.

At any given point in space, there is a condition resulting from a combination of many sources of radiation. The astronomer may direct his telescope, and, from the radiation at the object glass of his instrument, construct an image of any one of countless thousands of stars or other heavenly bodies. In like manner, but with different equipment, a radio receiving antenna or aerial coil may be set up. From the radiation striking the antenna or coil, a process of focussing and screening brings out the desired communication in code or in spoken words.

It is not likely that sending stations will ever rival in number the heavenly bodies, but the list is increasing and the limit is not in sight.

## General Electric Review

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Manager, M. P. RIClE
Edto Jor. JoN R. HEWETYT

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one of the gauge rooms at the schenectady works of the general electric company sec 110
 when these are assembled in Africal


## WORK TO BE DONE

In a short article entitled " Notes on Wiring" published in this issue, the following most significant figures appear:
Estimated number homes in United States, approximately. . . . . .........
Estimated number homes reached by
electric lines, approximately ......
Estimated number homes wired for electric servica
(ono
13,000,000
7,600,000
Estimated numbrr homes reached by electric service, but not wired.
Estimated numbr homes not reached by electric sarviee, approximat ely.

5, 400,1100

Estimated number homes connected during 1921
$8,000,000$
-00,000
Each of these figures has a special lesson of its own;-21,000,000 homes in the United States.-America is a young country as nations go- and these figures show a national growth which is without parallel in history

If the above figures indicate a marrelous national growth. what can be said of the fact that $13,000.000$ of these $21,000,000$ homes are reached by electric lines: Could any figures testify more eloquently to the fact that those great influences which have been at work, often with much opposition, to build up the industrial enterprises of the country have worked courageously and effectively:

Of the $13.000,000$ homes reached by electric lines slightly over half, or $7 .(600,000)$, are wired. When we think of the age of the electric industry, the country may well be proud of this fact.

There are still $5,400,000$ homes reached by electric serrice and not wired, and still s.000.not homes not within reach of such serrice. In one respect these last figures are the most interesting-they show a wonderful field for enterprise.

We have said enough to show that we appreciate the wonder of what has been done.

But an appreciation of what has been dome is of little value in comparison with an appreciation of what there is to do.

Now let us look at these same figures with a different mental attitude. Of the $21,000,000$ homes in the United States only $7,600,000$ are wired and s,000,000) homes are not even in reach of electric service. Roughly speaking. there are two homes unwired for each home wired. Of the $\overline{7},(600,000)$ homes that are wired, how many use any electrical appliances, excepting a few lamps? These are the things that are really worthy of attention.

How many homes in the United States are still doing family chores in the same silly old fashioned, back aching, nerve racking way as they were done a century ago?

True democracy depends upon giving all an equal opportunity- -Those people who have no opportunity to use what man has done for man in the direction of taking the load off human backs and putting it on the machine have not a fair chance when compared with those who have this opportunity. Electric transmission lines may truly be called the merves of a democratic state.

The electrical engincer has insenterl and developed hundreds of devices for reducing human labor. Why are they not used in every home:

It is a poor home where there is all labor and no leisure and recreation. We are told many alarming stories of the high per cent of our population that hare the minds of thirteen year old children. We all know the effect of environment on crolution.

Are we wrong in building up the electric industry and believing in what it can do for our civilization?

We have only begun.
I. R. H

# Silica Glass or Fused Quartz 

By Elsme Thomason<br>


#### Abstract

Brofesson litho Thomson after giving a few historical notes fells how guart\% is made and recites some of its many valuable qualities. The making of steh large masses of quartz, when compared with what we could doafew gears ago, semens hut lithe show of marvelous. The research work which has led to the se achievements has literally given the world new tools to work with. - Emolor.


The element silicon is perhaps the most abundant of all in the surface layers of the earth and for many miles deep. It occurs only in the oxidized form. It has two oxides, SiO , or monoxide, and $\mathrm{SiO}_{2}$, or dioxide; the former is not found in nature and became known as a laboratory product less than fifty years ago. It was often mistaken for the element itself, and in small specimens sold as such. Researches in the laboratory of the Thomson-Houston Co. in Lynn thirty years ago gave it its true place as monoxide, a dark brown inert powder.

It is, however, with the common oxide $\mathrm{SiO}_{2}$ that we have to deal. This compound is the basis of innumerable minerals, simple and compound silicates which make up a vast variety of the rocks. Industrially they give us the clays, the micas, feldspars, which with the silica itself are so important in ceramics, coarse and fine, and in glass.

Fortunately, silica is found almost chemically pure in rock crystal, and in white veins in rocks, and is abundant even in white sands in an almost pure state. The sands used in making the finer grades of colorless glass are an example. For optical glass the highest grades are used; for plate and window glass a small percentage of iron can be tolerated, and this imparts the green color on edge view. Sand itself is not fusible by any temperatures which were attainable in ordinary combustion furnaces, but in the presence of basic metallic oxides, as soda, potash, lime, alumina, etc.. fusion is readily secured, the product being some variety of glass, possibly. Mixed with clays, hardening takes place on baking at above a red heat, with bricks, tiles, and coarse pottery as a result, the hardening being due to the loss of water from the clay. When feldspar is added to the mixture of silica and clay, there is then, on prolonged firing in a kiln, a fusion more or less complete throughout the mass, and the result is porcelain of a grade depending on the proportions, the purity of the constituents, the fineness of the powders mixed, and the perfection of mixing
and uniformity of drying and burning. These operations may be summed up in the phrase "perfection of working or manipulation." There is generally a subsequent firing for glazing or coating the ware with a more fusible covering which leaves the surface smooth and vitreous like glass, and which ensures non-porosity. It is the cracking or checking of this thin glaze layer which after a time spoils the ware, or, as in certain instances, which secures a surface deemed to denote a highly artistic result. This cracking of the glaze layer probably indicates a condition of strain due to unequal contraction of ware body and glaze on cooling which at last leads to fracture of the latter.

One of the results of feeding a blowpipe with oxygen instead of air was the discovery of the fact that the greatly increased flame temperature rendered it possible to fuse many substances which before had resisted the highest furnace temperatures. Among them was silica, or quartz itself, and more than a half century ago bits of rock crystal so heated were drawn into threads and later used for instrument suspensions, and were found to be almost perfectly elastic; far beyond other known materials in that respect. The instrument indices returned to zero after having been deflected. The quartz fibre untwisted itself completely after twisting through a large angle. It was many years after this that, working with the oxy-hydrogen flame, attempts were made to build up out of fused quartz, tubes or vessels for special uses, and about twenty years ago this had, as in the hands of Shenstone ("Nature," May 6, 1901), become a laboratory art practiced on a limited scale. The process was laborious and necessarily the product was very expensive. The writer foresaw more than twenty years ago that it was desirable to be able to work quartz on a much larger seale, that its properties were such as to give it a high value for a variety of uses. Briefly, its very low, or almost negligible, expansion is perhaps its most remarkable property. Besides this, its high
transparency, not only to rays of the visible spectrum, but to low heat or ultra red rays, as well as to the wlta riolet invisible rays, might give it a minque place in optical and kindred work. Conpled with its low expansion. prisms might be marde of it whose refractive index was independent of ordinary changes of temperature, white astronomical and other mirrors or optical apparatus could be constructed and be practically free from distortion during changes of temperature; a difficulty which was always present in glass mirrors being thus removed.

Morever, it was forescen that the optical working of true surfaces would be greatly facilitated because the work could proceed


Fig. 1. Solid Ingot of Opaque Fused Quartz, Weight 115 Lb .
regardless of the slight heat generated in the polishing process. And again, for the same reason, the question of annealing to aroid strains became of far less importance, almost negligibly so, in fact. Another advantage over glass is that in the case of lenses or prisms, since the material is nearly 100 per cent pure, the formation of striae, due to inequality of composition, is minimized. Again, the low expansion allows the material to be ground or roughed into shape by an ordinary dry carborundum wheel, which, with glass, would cause fracture by heat, unless used with slow speed and great care. This last advantage applies in a general sense to the working of fused quartz into shape by grinding.

Besides the untral possibititus bufore alluded to. the value of fused grart\% in the construction of chemical ressels, and conduits for convering corrosive vapors, even at high temperatures, carly became evident. And further, its properies made it desirable


Fig. 2. (Left) Astronomical Reflector after grinding and polish. ing an $18-\mathrm{ft}$. sadius curvature in the surface. (Right Second Model Astronomical Reflector $11-\mathrm{in}$. dia.
$2^{1}$-in. thick having opaque quartz back-
ing. Transparent quartz facing
to investigate its possible application as an insulator in electrical work

About 1902, the writer began work 10 render it more easy to obtain fused quartz in masses as desired. An electric arc furnace was, constructed at the West Lemn Works of the General Electric Company, and used to


Fig. 3. Clear Fused Quartz Tubes and Rods made in Thomson Research Laboratory of the General Electric Company, River Works, Lynn
meh sand into slats of several inches in diameter. One such slab was worked into the form of a concave telescope mirror and compared with a similar glass mirror for distortion of image under irregular heating. As was expected, the very great superiority of the
quart\% surface ofer the glass was at once manifest. Changes of temperature which would absolutely destroy all definition with the glass mirror left the image formed by the quart\% surface intact. But this was only


Fig. 4. Double Curved Fused Quartz Rod showing transmission of light through rod
a demonstration of what must have been the case as predicted from the relative expansion coefficients.

At the same time, in 1902, in the Works at Lynn, there was another means of working


Fig. 5. Two Clear Fused Quartz Slugs made in the Thomson Research Laboratory, General Electric Company, Lynn, Mass., April 27, 1922
fused silica developed, and this forms the subject of a U. S. patent, Number Tis,286, to Elihu Thomson, "Manipulation of Refractory Materiah," December $\mathbf{2}^{-7}, 1904$. The method itself as found out later, was foreshadowed by

Despret\% in 1819, who passed a voltaic battery current through a small carbon rod bedded in sand, and secured a small fused silica tube surrounding the same, but the Despret\% experiment was anknown to the writer when


Fig. 6. Five Quartz Disks
he began work and lay buried in the literature of the carly years as an isolated experiment.

The writer's plan was to bury in sand a carbon conductor shaped as a mould and to heat it electrically by current, thus causing the sand to fuse where it lay in contact with the mould. This action as continued gave rise to a thicker and thicker fused layer, and when the current was cut off, this layer formed the object required. It might be a tube of fused quartz or a dish, according to the shape


Fig. 7. Samples Clear Fusef Quartz Optical Grade made in Thomson Research Laboratory, General Electric Company, River Works, Lynn
of the carbon mould. The process was found to work well, and was, at the writer's suggestion, practiced by Dr. R. S. Hutton of Owen's College, Manchester, England, and an exhibit of artictes so made was brought before the

Royal Society at the time．Dr．Ilutton credited the writer with the origination of the process．

Lack of facilities and interference by other work and unfavorable conditions postponed any further development for several years，


Fig．8．Lenses（2）and Prisms（3）of Clear Fused Quartz
but the material was used at times for pro－ curing at very low cost tubes of fused quartz as required for laboratory use．

Made from sand or quartz granules，the ware，so to speak，is translucent，not trans－ parent，and this is owing to the innumerable small bubbles enclosed in the mass．For many purposes，they are not to be considered detrimental，and it is easy to imagine that cooking vessels may be produced of such ware， which will not break by sudden heating，or quick cooling even from a red heat，which can be thick enough to stand rough handling，and which can be cleaned，if need be，by burning them off．

Be that as it may，many uses are being found for this coarser variety of fused quartz，


Fig．9．Fused Quartz Applicators（8）and One Quartz Window made for Burdick Cabinet Company， Milton，Wis．
and a consistent line of research has been carried on in producing it and shaping it by moulding，blowing，and grinding．It can readily be produced in masses weighing hundreds of pounds，and though containing
innumerable small bubbles like half melted snow，these do not interfere with the proper－ ties of the guart\％itself，as to low expansiom， cte．，see Fig． 1

It has been noter that the heating of a mass of quart\％throughout occurs with rapislity in


Fig．10．Rectangular Bar of Clear Fused Quartz $4 \times 1{ }^{3} \times \times{ }_{6}^{3}$ in made in Thomson Research Laboracory，General Electric Company，Lynn Works
spite of its low heat conduction，and this fact may probably be the result of the great trans－ parency to low heat rays or radiation，one part of the mass heating its neighbor by trans－ mission of the radiation，so that a mass heated from the outside radiates to the interior in all directions，raising the temperature in spite of the low heat conduction of the material．On account of the low expansion，rapid heating of a mass is possible without fracturing．

It is，of course，desirable that the sand or granular quartz used as a raw material be nearly pure silica．The fused mass is vitreous throughout and impermeable to gases or liquids，and has a surface in certain instances which has a glazed appearance，so that no glazing is called for．On account of the low expansion，also，metals，eren steel，can be


Fig．11．Model No． 1 Fused Quartz Insulator after being taken from the furnace
cast into openings after the material is formed．

Crystalline quartz on being heated expands unevenly in the line of the different axes of the crystal or along the main axis $781 \times 10^{-8}$
for calch deg. C. per mint of length and in the transerse direction to the main axis about $1119 \times 10^{-8}$. In heating, if the aceess of heat is slow, erystobatite crystals form which are changed to tridemite as the temperature is increased.

Particles will begin to fuse together at 1.100 deg. C. in the catse of the purest rock crystal which, however, may contain about $1 / 5$ per cent of impurity acting ats a lhax. Further increase of temperature gives rise to partial fluidity or plastic comdition, and at about


Fig. 12. Ingot of Opaque Fused Quartz weigh ing approximately 100 pounds. Six feet long and six inches in diameter
17.50 deg. C. the silica in the open begins to sublime, but is still viscous like thick molasses. A higher temperature can be reached by fusion under pressure, which holds down the sublimation with little benefit however.

The change from the original crystalline form involves an expansion amounting to about 17 per cent of the volume, and on subsequent cooling to ordinary temperatures, the shrinkage will be about ${ }^{1} / 15$ of one per cent only, a most exceptionable circumstance. Measures of expansion of fused quartz show
that it expands at a slightly increasing rate as the temperature rises, but that on the whole the increase of dimensions is extraordinarily small, or such that with a change of temperature of 1000 deg. C. a meter long rod will expand or contract only about $1 / 2$ a millineter. As a rough expression of the low expansion, it is stated to have about $1 / 17$ that of platinum, the coefficient of expansion being at 200 deg. (C., . $318 \times 10^{-9}$.

At temperatures ranging from about 1100 to 1400 deg. C., and continued for a time, fused quartz undergoes gradual devitrification, a phenomenon which it shares with glass, some varieties of which are extremely susceptible to that action when under prolonged heating. Thoroughly devitrified quartz is white, granular and weak in structure and the property of low expansion which makes the fused product so valuable is entirely lost.

As before pointed out, the vitreous nature and acid resisting quality of fused quartz, even of the coarser or translutent material, coupled with


Fig. 13. First Model Fused Quartz Radio Insulator Complete with Corona Shield. Overall length 48 inches. Creepage distance 31 inches the low expansion and consequent non-liability to fracture under sudden and great temperature changes, has led to the use on a considerable scale of fused quartz conduits and vessels in chemical industry. A single example will suffice. Formerly, the last stages of concentration of sulphuric acid


Fig. 14. Specimen of Cylindrical Grinding of Fused Quartz by a method developed in connection with the radio antenna insular problem
from the state of dilution existing as manufactured in leaden chambers, to the strong acid known as oil of vitriol, was accomplished either by boiling off the water in glass stills, mounted over furnace fires, or in great platinum stills for the purpose. The glass vessels
were slow in operation and very sulpect to breakage, they were large and expensive, and the spilling of acid into the hot furnace was little short of a disaster. The platimum stills. even at the relatively low eost of platinum many years ago, involved a large investment.
 Their use was attended with gradual wear and loss of the precious metal. But its price today is many times what it was formerly. Inthis juncture the fused quartz evaporators worked in cascade accomplish the result without fear of fracture and at low cost of equipment.

By special methods developed in the laboratory of the General Electric Company at Lymn. it is now possible to produce many objects. not only of quartz of the opaque or opalescent character, such as is obtained by fusion of sand. but also to secure comparatively large masses of perfectly clear quartz as obtained from rock crystal, and containing only a few small bubbles widely separated: though progress along present lines will doubtless entirely eliminate them. There are also producible objects, such as disks for astronomical mirrors in which the body or backing is a thick mass of the sand fusion opal material. faced with a clear laver of the fine grade on which the optical surface is produced by grinding, polishing and figuring.

Considerable quantities of clear tubing are demanded for the construction of mercury arc lamps used for sterilization, and for other uses in which emission of ultra violet rays is the important factor. Such is the wonderful transparency of this clear material, that a rod


Fig. 15. Fused Quartz Bushings used in high power rectifier development

Ir tube of it 26 feet long (the longest yet produced will convey, by internal reflection, the light of a match from one end to the other with little apparent loss; and even bent rods convey in this same manner, light and heat "ays through lengths of many feet

Bhocks of the alear maternal of mital quality are mow prowluwd, and there seem to be no especial limit th the size, excepting the scale of operation. Ingets. as they are called, are mon mate of varying we some of the larger of which emmath from on (w foll


Fig. 16. Fused Quartz Pedestals for supporting chemical tanks
cubic inches or more. These, when of high quality, furnish material for prisms and lensen of fused quartz. especially valuable in the construction of instruments dealing with the invisible rars, such as spectrographs for ultra violet rays. Besides, the comstancy of dispersion of the fused quartz, owing to the small effect of temperature changes, is a valuable property in spectrographic work, generally. The refractive index fror the D ray is about 1.46, while the relative dispersion $\mu,-1$ is akin to that of the lighter crown glasses.

The refraction is naturally much lower than that of crystal quartz, which itself being doubly refracting is giren (for the D) line) for the ordinary ray $1.5+423$, and for the extraordinary ray. 1.5.5.3.3 , decreasing with an increase of temperature.

Owing to the transparency to ultra violet rays, rods of clear fused quartz are now being employed to conrey, from a rigorous source. such rays to the carities of the body for treatment of diseased areas. such as in the throat. the nasal carity, the ear. etc., where it would be impossible to place the source itself near the tissue to be treated. Internal reflection is relied upon to confine the bundle of rays which is emitted at the end of the rod; such rod may be bent or shaped to facilitate its use in such cases. Fig. $t$ shows this effect with ordinary light rays.

In the same way, low heat rays (ultra red mav be convever and applied locally. An excellent example of this is seen on heating. by the oxy-hyirngen blowpipe, a rod of clear quartz of say 10 inches in length and about ${ }^{1}{ }^{2}$ Ench diameter. holding it as usual with glass by the fincers some distance away from the heated somt. which may be the center section of the ba:. Care must now be taken
mot to touch the that ands of the bar, or a barn will ressutt, though the temperature there is low. There is, howerer, an intense bundle of heat raysemited at the ends, hed within the bar her internal reflection from its sides.


Fig. 17. Standard Petticoat Type 6-in. Strain Insulator made of fused quartz

The high grade clear fused quartz, in block, rod or tube form, is a very beatiful material, chear, colorless, and probably the most transparent solid in existence. It is the ideal glass. It can be welded when made plastic by heating, as with glass, but with no risk of cracking from sudden heating or cooling, a condition conducive to ease in blowing, drawing, bending or grinding it into various forms.

Tuning forks have been made from it which not only give a note decaying more slowly, but which can be adjusted in pitch without temperature change in adjusting standing in the way of accuracy, as in the case of steel; the variations unavoidably introduced having given rise to serious changes in standard pitch in the past few hundred years.

Thermometers and their tubes made of fused quartz have the merit of needing no correction for expansion, a serious matter in the case of glass where great accuracy is desired. They are not cracked by sudden temperature changes, and stand high temperatures without softening and deformation.

Disks of about a foot in diameter and about 212 in . thick of the coarser quartz faced with clear quartz are a recent triumph of the Lynn laboratory, and open the way to the possibility of relieving the astronomer of some of the trials and difficulties which he has had to endure in the use of glass, so subject to deformation by moderate temperature changes. Fig. 2 is a photograph of such disks.

Indeed, in the production of such disks, a new note has been struck, which may eventually lead to the substitution of fused quartz for glass in all important instruments of the reflecting type. The writer has had this
problem in mind for two decades past, and it is a great gratification to him to have been able to solve it Various means combucive to the best results are under way.

Coming now to the uses of the corarser (or samel melt) (puart\% in eleet rical work, it becomes at once almost obvious that for are chutes it shonkd be ideal as it is not excoriated or fractured by the sudden heat and is an excellent insulator even at high temperatures, vitreous throughont and non-bygroscopic. It can be moukled or formed by grinding into suitably shaped and fitted slabs and supports of metal may be cast into it.

Slabs can be cast with passages for resistance wires to heat them to desired temperatures for any purpose. Clear quartz may, in fact, be so prepared with a heater circuit as to be fitted for use as a window for clear vision in spite of deposits of snow, ice, water, or condensed vapors thereon.

Probably the major uses for the coarser quartz in the electrical industries in the near future will be in forming varions types of insulators some of which are here illustrated.

Reference should properly be made in closing to the special article on "Quartz Glass" prepared by Dr. Arthur L. Day and E. S. Shepherd, of the Geophysical Laboratory of the Carnegie Institution, Washington, D. C., dated April 18, 1906, and published in Science, N.S., Vol. XXIII, No. 591 , pages 670, 671,672 , which discusses the valuable work done in


Fig. 18. Standard 10 -in. Hewlett Type Strain Insulator made of fused quartz
the preparation of fused quartz and the limitations found in the working thereof by the Geophysical Laboratory. The communication is worthy of a careful examination, and does much to clear up some of the doubtful points in regard to this interesting material.

# Studies in the Projection of Light 

Part I

# TYPES OF LIGHT SOURCES AND ANALYSIS OF PARABOLOIDAL REFLECTING SURFACE BY MERIDIAN AND SAGITTAL LINES 

By Frank Beaford




#### Abstract

Artificial light as directly generated is of a "raw" character and must be "refinerf" before it can be most effectively utilized. This manipulation of radiated light is accomplished most readily when the source is the electric lamp, either incandescent or are. How it is accomplished depends primarity on whether the purpuse calls for a more or less diffused light or an intense concentrated beam. Nost of as are familiar to some extent with the production of these 1 wo diametrically opposite effects: howerer, those who are interested in the gathering of light and its projection in the form of a beam will find information of great value in the following article and the others of the series which will appear in our succeeding issues. The present installment explains a most useful and unique scheme of optical analysis as applied to a reflecting parabolode, commonly called a parabolic reflector.-Ebitor.


## Introduction

In the art of illumination many wonderful things are being done. Everyone is familiar with the steady progress made in recent years in the lighting of our homes and streets; and a goodly number of us have seen spectacular wonders that were purely displays of light. Is there an automobile driver who has not given considerable thought to the subject of light, particularly when passing a glaring headlight and wondering just what he is going to hit in the darkness beyond? But it can be said in all seriousness that this particular problem of so projecting light that it will illuminate without glaring is one of the greatest engineering problems of the day, and perhaps by good fortune there may be something on the following pages that in the right hands will contribute to its solution.

It is in the particular field of projecting light to long distances that the art of illumination has reached its highest development. Here we find the largest lamps, the greatest consumption of electrical energy, the greatest collection of automatic devices, and the greatest example of manufacturing optics. In all the wide domain of illumination the lover of superlatives will feel most at home when speaking of the modern high-power searchlight. Here we deal not with illumination at ten feet or a hundred feet, but at thousands of feet, or, as the Army and Nary prefer to say, at thousands of yards. The mirror that is the searchlight may cost orer a thousand dollars before it ever reflects a beam of light. But these figures become commonplace once the subject of candles is brought up. We calmly discuss a small searchlight that gives only ten million candles,
and speak slightingly of a searchlight that gives fifty million candles, whereas another of the same size but of a later generation gives three hundred million candles. Then warming up to the subject we may rclate what happened the night we operated a searchlight of seven hundred million candles. There have even been cases where, carried away by the exhilaration of the moment, we have talked of one billion candles until the dazed audience concluded that a candle must be about as valuable as a Russian ruble.

There are not many branches of art in which the accuracy of workmanship must increase with the size of the product, but this is exactly the case in the manufacture of a searchlight. While this article will not be confined to searchlights of notable size and power, or even to searchlights alone, yet as the ultimate aim of all endeavor is perfection so will the subject continually drift back to the largest because it is the best. The glass in the mirror of the automobile headlight may vary in thickness by several hundredths of an inch without great detriment, but the same variation in the thickness of a sixty-inch searchlight mirror would be fatal. The lamp in the flashlight may be a fraction of an inch removed from the focal point, and who cares? Let the crater of a high-intensity searchlight wander the same distance from the proper position and evervone cares. This same crater, while being held with precision at the focal point, is rotating abott its axis and merrily radiating ten kilowatts of energy. And it must do this in foul weather or fair, on a hearing sea or when pursuing a frightened airplane with its mighty beam clear across the vault of the heavens. Truly,
in the Donnatin of llhmanation, the searehlight is King.

Howerer, as with tomporal kings, all searehlights are not perfect. In testing one of these proud momarehs it was diseovered that several humdred million candles were missing. 'The test was repeated, with the same results. Three hundred millions gone. The King was siek, there was no donbt about that. 'The explanation was not found for many months and in the light of later events it would have been simpler to have doctored up the records than to have doctored up we King.

Much that is found on the following pares of this series of articles is the result of the hunt for the lost three hundred millions, but the bulk of the material is taken from papers presented before the Ilfuminating Engineering Society, from reports submitted to the Amy and Navy at various times, and from other data taken from the files of the department and never before published.

## TYPES OF LIGHT SOURCES

When designing a reflector for some specific effect in illumination, the first necessary information is about the light source; its size, shape, and brilliancy. If it is the intention to use a carbon arc the information is easily expressed by a formula or by a photometric curve with crater dimensions; a high-intensity are is more difficult to define; and the incandescent lamp with its mumerous helical coils in one or more planes is too complicated to be described by mathematics that are simple enough to be understood and used. To avoid these difficulties and reduce theory to practice with some degree of accuracy it is usual to substitute, in the design, some idealized form of light source for the actual source. Thus, the hemispherical or conical crater of the plain carbon are becomes a disk, luminous on one side only and the ineandescent filament becomes either a disk luminous on both sides or a sphere uniformly luminous over its entire surface. The highintensity are on account of a certain dissymmetry in the distribution of brightness is the most difficult one of the three to match with a simpler substitute, but on the other hand the test data on this are are fairly extensive and complete, and the need of a model is mot so urgent. There remains one other type of source that is universal in its usefulness as a starting point of a design
or study, but it is of very limited use when dealing with concrete cases because it exists omly as a mathematical concept, that is, the" "point source."

The nearest approach to an actual point source is furnished by the stars, which never show an apprecialde diameter even when magnified by the most powerful telescope. The area of the star, not being measurable by this means at least, may be considered as zero, which agrees with our idea of a "point" as something that has location but no size. The light received from a star may be measured, and if we divide its total emission of light by its zero area we find that the surface must be infinitely bright. This reduces the matter to an obvious absurdity, and it illustrates some of the peculiar results that may be obtained in lens or mirror design unless the limitations of the useful but deceptive point source are kept constantly in mind.

## ANALYSIS OF PARABOLOIDAL REFLECTING SURFACE

## Point Source

A parabolic curve rotated about its axis generates a surface of revolution that has the useful property of reflecting light originating at its focus into a beam of light that is in general parallel with the axis. If the light source is a mere point then the beam is made up of a bundle of rays each strictly parallel to the axis, and there is neither convergence nor divergence of the light. The beam is thus cylindrical in form and of unvarying intensity at all distances, except as the light is scattered or absorbed by the medium through which it moves. The demonstration of these characteristics has been often made in books on photometry or geometry, and it would not be here repeated if there were not several useful principles of optics involved that are not so well known.

These principles, which will be explained shortly, enable us to analyze any section of a reflecting surface and find out in detail how it acts, what it can do, and what it cannot do. Also, they bring to light some interesting and usefuj properties of the paraboloid and related surfaces that seem to have escaped previous notice.

In the science of applied optics there is a phenomenon known as coma, by virtue of which the image of a point becomes not a point but two straight lines, perpendicular to one another in direction and lying in different planes. There is thus no single plane
that will show an image that resembles the object, and it may be doubted if we are justified in calling either line an image of the gencrating point. Coma, in a camera, gives an imare of a bright source some distance from the axis of the lens as a diffused point of light with a comet-like tail, and sharp definition is not possible in this part of the field. The rules that govern coma, in the simpler cases at least, are in themselves rery simple, and because of this simplicity they are consenient (and powerftu) instruments for the exploration of optical surfaces.

It may fairly be assumed that readers interested in the projection of light are familiar with the general properties of the conic sections, but if they feel any curiosity regarding the derivation of some of the statements here given as conceded facts. they can readily look them up in text books. This assumption will enable us to concentrate more on the principles of the subject in hand and aroid getting lost in a maze of incidental demonstrations.

## Meridian Line

Let us take not a parabolic surface but the parabolic curve itself and see how it acts as a reflector. It may be necessary. in order to form a mental picture, to imagine that the curve has some little width and a flat surface on the concave side so that there will be something to reflect light. From the focal point of the curve draw a straight line at random to some point $P$ on the surface as in Fig. 1,* and call the length of this line $p$, then if $a$ is the angle measured clockwise from the axis up to the line $p$ we have the following equations:

Equation of parabola (in polar coordinates)

$$
\begin{equation*}
p=F \sec ^{2} \frac{a}{2} \tag{1}
\end{equation*}
$$

Radius of curvature at point $P$

$$
\begin{equation*}
R=2 F \sec ^{3} \frac{a}{2} \tag{2}
\end{equation*}
$$

where $F$ is the focal length of the parabola as ordinarily considered in geometry

Let us draw two rave of light parallel to the normal at $P$, Fig. 1, and find what they do after reflection at the two points $P_{1}$ and $P_{2}$ on the curse near $P$. According to a rule of elementary optics the two reflected rays will converge at a point on the normal, half the radius $R$ from the point $P$. This point

[^2] focus of the section of curve $P_{1}, I^{\prime}, I^{\prime}$, and designating this principal focal longth for No sel
\[

$$
\begin{align*}
& f_{11}=\begin{array}{l}
K \\
\because
\end{array} \\
& =I \cdot \sec ^{3} \begin{array}{l}
2 \\
2
\end{array}
\end{align*}
$$
\]



Fig. 1. Focal Properties of a Meridian Line
It will be observed that $f_{0}$ is measured along the normal, and hence does not coincide with what we ordinarily call the focus of the parabolic curve. Also, as the angle a is changed $f_{w}$ will change, so that each section of curve will have a principal axis, or normal, varying in direction and a principal focal length that varies in magnitude.

Consider the points $P_{1}$ and $P_{2}$ to be fixed. and rotate the incident rays counter-clockwise in the plane of the curve to some new position at an angle $e$, keeping the two rays always parallel to one another. The reHected rays will rotate in the opposite dircction through the same angle $\varepsilon$ and the angle of convergence $c$ will remain constant. The distance between the parallel incident rays will decrease by the factor $\cos e$ as they are rotated through the angle $e$, and if the rotation is made equal to 90 deg. the two will coincide in position. When the points $P_{1}$ and $P_{2}$ are fixed then the angle of convergence $c$ of the reflected rays is fixed and independent of the angle of incidence

We have for normal incidence the length

$$
\begin{equation*}
P_{1} P_{2}=\underline{2} f_{0} \tan \frac{c}{2} \tag{4}
\end{equation*}
$$

and at any angle of incidence $e$, we have the length

$$
\begin{equation*}
P_{1} P_{2} \cos c=\underline{2} f_{e} \tan \frac{C}{2} \tag{5}
\end{equation*}
$$

Where $f_{e}$ is the foral lemeth or distanee to the new eomverging point. Leon eompering equations ( 1 ) and (.) wo wet the relation

$$
\begin{equation*}
f_{c}=f_{0} \cos c \tag{6}
\end{equation*}
$$

which shows that ats $\cdot$ is varied the point of eonvergence moves in a eirele that has a


Fig. 2. Foca! Properties of a Sagittal Line
diameter $f_{0}$ and is tangent to the surface at the point of reflection.

If the parallel incident rays, Fig. 1, are rotated until they are parallel to the axis of the parabolic curve, we have

$$
\begin{aligned}
2 \varepsilon & =a \\
\varepsilon & =\frac{a}{2}
\end{aligned}
$$

and

$$
\begin{equation*}
f_{\frac{a}{2}}=f_{0} \cos \frac{a}{2} \tag{7}
\end{equation*}
$$

and also, if we substitute for $f_{0}$ its value in terms of $F$ and sec $\frac{a}{2}$ as found in equation (3), we get

$$
\begin{align*}
f_{\frac{a}{2}} & =F \sec ^{3} \frac{a}{2} \cos \frac{a}{2} \\
& =F \sec ^{2} \frac{a}{2}
\end{align*}
$$

which is the length of the radius vector $p$ as defined by the equation of the parabola itself. The focal point of the entire parabolic curve, therefore, lies on the locus of foci of the element $P_{1} P_{2}$ but it is a secondary or special focus.

A point source of light placed at any point of the circular locus will have such of its light as strikes the parabolic curve at the
point of tangenes to the circle reflected in a parallel beam. The focus of the paraloola acquires its optical importance from the fact that it lies on the common crossing point of all the circular loci that may be drawn at different parts of the parabolic eurve, and therefore it becomes the principal focus of the parabolic curve taken as a whole.

## Sagittal Line

The curvature of a paraboloidal surface is not the same for an elemental line in the surface and in a plane through the axis (the meridian section) as it is for a second line at right angles (known as the sagittal section). This is apparent when we remember what curves are formed by a plane intersecting a paraboloict. If the intersecting plane is perpendicular to the axis the curve of intersection is a circle; if the plane is parallel to the axis the curve is identical with the gencrating parabola, but of course is shifted to one side of the original axis. A plane that is neither parallel nor perpendicular to the axis intercepts the paraboloid in an ellipse and it is evident that the second, or sagittal, line just mentioned is a section of an ellipse. We might solve for this ellipse and thus find the normal and radius of the element in question, but there is a much simpler way of finding its characteristics.

Every normal to points in a surface of revolution intercepts the axis of revolution, and we may define the radius of sagittal curvature at a point $P$, Fig. 2, as being the point of intersection of two adjacent normals such as those erected at $A$ and $B$ on a line in the surface at right angles to the parabolic section. The intersection of the normals is at the axis, and the length of a normal to a point on a parabolic curve is

$$
\begin{equation*}
R^{\prime}=2 F \sec \frac{a}{2} \tag{9}
\end{equation*}
$$

where $a$ is the angle between the axis and the radius vector to the point at which the normal is erected. The principal focal length of the sagittal element is therefore half the length of the normal, or

$$
\begin{equation*}
f_{0}{ }^{\prime}=F \sec \frac{a}{2} \tag{10}
\end{equation*}
$$

By equation (3) the expression for the principal focus in the meridian plane was found to contain $\sec ^{3} \frac{a}{2}$ as a factor; and as $\sec ^{3} \frac{a}{2}$ is always greater than sec $\frac{a}{2}$ when $a$ is less
than 180 deg., the length of $f_{0}$ is always greater than $f_{0}{ }^{\prime}$.

If we imagine the parabolic curve and its axis to lie in the plane of the paper, Fitr. 2. then point A will be above the paper and $B$ will be below it, and parallel planes can be passed through $A$ and $B$ parallel to the plane of the paper and separated by the distance $A B$. Pass a plane perpendicular to the above planes, so that it contains the center of curvature $R^{\prime}$, the principal focal point $f_{0}{ }^{\prime}$ of the line $A B$, and the line $A B$ itself. A pair of rays parallel to the normal and incident at $A$ and $B$ will after reflection intersect at a distance $f_{0}{ }^{\prime}$ as found above, and the reflected rays will lic in the perpendicular plane just erected. It is desired to trace these reflected rays and find their intersection as the parallel incident rass are rotated in their respective planes but kept parallel to one another.

At the points $A$ and $B$ erect lines that are perpendicular to both the incident and reflected rays (one line lies in the horizontal plane through $A$ and the other in the horizontal plane through $B$ ) and at $f_{0}{ }^{\prime}$ erect a common perpendicular to the two reflected rays (this lies in the plane of the paper).

Planes passed through these perpendiculars will pass obliquely between the three parallel planes through $A, P$ and $B$ and the intersection of the two oblique planes will be on the normal through $f_{0}{ }^{\prime}$. As the incident rays are rotated through angle $\mathcal{c}$, the reflected rays will be rotated in an opposite direction through the same angle and as they always lie in the oblique planes their intersection will fall on the intersection of the planes, and the focal length will be

$$
\begin{equation*}
f_{e}^{\prime}=f_{0}^{\prime} \sec e \tag{11}
\end{equation*}
$$

The right-hand member of this equation indicates a straight line as the locus of foci, and in this case the focal length increases with increasing values of $e$. If we rotate the pair of incident rays until they are parallel to the axis of the parabola we have
and

$$
\begin{aligned}
2 e & =a \\
e & =\frac{a}{2}
\end{aligned}
$$

therefore

$$
\begin{equation*}
f_{\frac{a}{2}}^{\prime}=f_{0}^{\prime} \sec \frac{a}{2} \tag{12}
\end{equation*}
$$

and substituting for $f_{0}{ }^{\prime}$ from equation (10) we get the special condition

$$
\begin{equation*}
f_{\frac{a}{2}}=F \sec ^{2} \frac{a}{2} \tag{13}
\end{equation*}
$$

which shows that the locus of foci patses through the focal point of the parabola.

## Element of Surface

So far we have considered the optical properties of lines in the surface of the paraboloid, but what of the surfaces as such?


Fig. 3. Focal Properties of Surface Area at Crossing Point of Meridian and Sagittal Lines

In Fig. 3 the two elemental lines $P_{1} P_{2}$ and $A B$ have been taken to locate and define an element of the reflecting surface. A bundle of incident parallel rays normal to the surface will be reflected into a line focus at $f_{0}{ }^{\prime}$ and into another line focus at $f_{0}$ as defined by equations (10) and (3) and these two line foci will be perpendicular to one another (similar to Sturm's conoid). In Fig. 3, $P_{1}^{\prime} P_{2}^{\prime}$ represent the line image at $f_{0}{ }^{\prime}$ that lies on the straight line locus of $f_{e}{ }^{\prime}$, and hence it is in the plane of the paper. The light, after passing through $P_{1}{ }^{\prime} P_{2}{ }^{\prime}$ forms a second line image $A^{\prime} B^{\prime}$ perpendicular to the plane of the paper and having its center on the circular locus of $f_{e}$. It is evident that as neither $A^{\prime} B^{\prime}$ nor $P_{1}{ }^{\prime} P_{2}{ }^{\prime}$ are common focal points for the two defining lines in the surface of the reflector, neither will do as a location for a source of light to form a parallel beam. If the incident bundle of parallel rays is rotated upward from the axis of the parabola, the focal lines will rotate into lower positions on the straight line and circle, as $P_{1}{ }^{\prime \prime} P_{2}{ }^{\prime \prime}$ and $A^{\prime \prime} B^{\prime \prime}$. Fig. 3. The two lines are now shorter and closer together, and if the upward rotation is continued until the incident light is parallel to the axis of the paraboloid the focal lines will merge into a point at the
crossing point of the circle and the line; that is, at the foeus of the parabolod. Therefore, it is proved that the entire paraboloid will reflect into a parallel beam the light that originates at its focus.


Fig. 4. A Section of a Paraboloidal Surface and the Related Paraboloidal Locus of $\mathrm{F}^{\prime}$

If the incident parallel rays are rotated downward beyond the focus of the paraboloid, Fig. 3, the focal point will separate into two focal lines as before, except that $P_{1}^{\prime \prime \prime} P_{2}^{\prime \prime \prime}$ which has previously been the closer of the two to the reflecting surface now is farther away
at $F^{\prime}$ and this point has identical properties with regard to the element of surface as has point $F$. When light from a point source at $i^{\prime}$, travelling parallel to the axis of the paraboloid, strikes the elemental surface $P_{1} P_{2} A B$ it will be reflected in a beam of parallel rays, and this beam will pass through the focus $F$, so that the two points $F$ and $F^{\prime}$ are optically symmetrical in one respect, but $F^{\prime}$ as a source point is limited to a small area while $F$ is general for the entire surface.

## Use of the $\mathrm{F}^{\prime}$ Point

In Fig. 5 is shown a vertical surface illuminated by a parabolic reflector and a lamp near one of the $F^{\prime}$ positions. This form of beam is ideal for illuminating either a highway or a wall or any rectangular area that must be illuminated from a point well to one side of the center. In the case of a highway the point of the beam, which is the point of greatest intensity, is directed down the highway and the wide section of low intensity is directed on the road immediately in front of the unit.

For wall illumination the unit is set up directly under the section to be illuminated


Fig. 5. The Distribution of Light in a Plane at Right Angles to the Axis of Projection when the lamp is near the paraboloidal focal surface is such that the small section of the beam has a high intensity and the wide section a low intensity
than $A^{\prime \prime \prime} B^{\prime \prime \prime}$ but they are in the plane of the paper and perpendicular to it just as before.

There is one particular condition that has been found useful in practice without the user always realizing fully just what takes place. The two focal line loci meet
and the beam then covers a vertical section of wall. The form of the beam depends upon the position of the light source on the locus of $F^{\prime}$. A short distance from the geometrical focus gives a beam only slightly out of round with the point of maximum intensity shifted


A 24 -in. High-intensity Searchlight with a Beam Power of $80,000,000$ Candles, Used on Destroyers


Incandescent Trolley Headlight


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The Special Dome Door with Its Cushion Support Resists the Shock of Salvo Firing on Battleships. The curvature of the glass is such that it does not interfere with the parallel projection of light


This Large Searchlight May be Turned and Elevated by Electric A Coast Fortification Searcialight of $700,000,000$ Candles. The Remote Control. The Small One, held by the man,
is Directed by Hand
Current is Automatically Maintained Constant and the
Crater in Focus
HEADLIGHT. STUDIO FLOODLIGHT, AND SEARCHLIGHTS FOR VARIOUS TYPES OF PROJECTION
to neate one edge. Thae bean of Pig. is was obtained be moving the latmp abont :3 in. from the focal point of a 1 li-in1, diat. : 3 -in. focal length parabolat.

## Locus of $\mathrm{F}^{\prime}$

From the const ruction of Fig. 3 it is evident that $f$ and $l^{\prime \prime}$ are equally distant from the reflecting element. In Fig. 4 this relation has been used to construct the locus of all points $F^{\prime}$ for the entire reflecting surface.

The rectangular form of equation for the parabola is
and the length of a radtus vector is

$$
\begin{equation*}
p=F+x \tag{14}
\end{equation*}
$$

If the coordinates of the point $P$ are $x$ and $y$, then the coordinates of $F^{\prime}$ are $x+(F+x)$ and $y^{\prime}$, or $2 x+F$ and $y$.
This leads to the equation

$$
\begin{equation*}
y^{2}=2 F(x-F) \tag{16}
\end{equation*}
$$

for the locus of $F^{\prime}$; that is, $F^{\prime}$ moves along a parabola having a focal length of $1 / 2 F$ and having its vertex at the focal point of the reflector.

It was obscrved during the tests of which Fig. $\overline{5}$ is a part that for some positions of the lamp there were four active sections of mirror directing light into the small end of the beam sections where the intensity was greatest. The explanation of these four spots is found in the fact that the points $F$ and $F^{\prime}$ are not isolated positions in space but are merely two points on a closed curve of focal positions that give parallel projections from a given elemental section of the mirror surface.

In Fig. 3 the parallel incident light moves in the plane of the paper and the length of $f_{e}{ }^{\prime}$ becomes greater than $f_{e}$ when either the $F^{F}$ position or the $F^{\prime}$ position has been passed, as at $A^{\prime \prime \prime} B^{\prime \prime \prime}$ and $P_{1}^{\prime \prime \prime} P_{2}^{\prime \prime \prime}$. If now the incident light is rotated in a plane perpendicular to the paper the line $A^{\prime \prime \prime} B^{\prime \prime \prime}$ will move out in a line perpendicular to the paper while $P_{1}{ }^{\prime \prime} P_{2}{ }^{\prime \prime \prime}$ will move in a circular path toward the surface element and $A^{\prime \prime \prime} B^{\prime \prime \prime}$ and $P_{1}^{\prime \prime \prime} P_{2}^{\prime \prime \prime}$ will again come into coincidence.

In Fig. 6a, which is an oblique view of a paraboloidal reflector, $s f_{0}{ }^{\prime} f_{0}$ is the normal to the element $s, s F f_{0} F^{\prime}$ is the circular locus of $f_{e}$, and $F f_{0}{ }^{\prime} F^{\prime}$ is the straight line locus of $f_{e^{\prime}}$ : The two line images $f_{e}$ and $f_{e}{ }^{\prime}$ come into coincidence again at $F^{\prime \prime}$ when the incident parallel light is rotated at right angles to the plane of $s F f_{0} F^{\prime}$ through the angle $g$. Coincidence occurs when

$$
f_{e} \sec g=f_{e}^{\prime} \cos g
$$

$f_{e} \sec g=f_{e}^{\prime} \cos g$
$F \sec ^{3} \frac{a}{2} \cos e \sec g=F \sec \frac{a}{2} \sec e \cos g$

$$
\begin{align*}
& \sec ^{2} \frac{a}{2} \cos ^{2} c=\cos ^{2} g \\
& \sec \frac{a}{2} \cos c=+\cos g \tag{17}
\end{align*}
$$

The locus of equation (17) is a curve on the surface of a eylinder generated by


Figs. 6a and 6b. A Given Elemental Section of a Paraboloid May Be "In Focus" for a Point Source Moved Along the Path of Double Curvature Shown in Projection and Plan. This Path Is Around the Surface of a Cylinder Generated by a Tangent Circle at S Moving Along the Sagittal Tangent
normals to the circular locus of $f_{e}$ and we may consider this locus to be made up of four branches $A, B, C$, and $D$ as marked in Figs. 6a and 6b. The four active areas previously mentioned were on the $A$ branch of one area, the $B$ branch of the second, the $C$ branch of the third, and the $D$ branch of the fourth. The light source was between the paraboloidal surface and the focal paraboloid of Fig. 4, and the separation of the areas was decreased as the source approached the focal paraboloid and finally they merged when this paraboloid was reached. The exploration of this space would be an interesting and perhaps profitable task but cannot be undertaken at present.

# The Cooling of Turbine Generators PART II <br> HEAT TRANSFER IN SURFACE AIR COOLERS 

By. A. R. Smoth<br>



 with Part 15 which will disus "Eennomies of L"sing Surface dir Condersand Heaters in Steath Power Plant.."

Emior.

The extraction of heat from air by means of surface coolers or the addition of heat to air bre means of surface heaters. when dealing with low iomperature differences between the air and the cooling or heating medium, has not been given serious consideration in the past because of the enormous amount of radiating or heating surface required.

Because of the low heat conductivity of air the heat transier, expressed in the common unit, B. i. u. per des. F. per sq. ft. per hr.. is relatively very poor when compared with values obtainable with steam condensers and other heat exchangers dealing with fluids of high conductivities. The following relative values illustrate the low heat transfer obtainable as encountered in everyday practice when dealing with air or gas

Steam to Water Suriace Condenser) - 400 B. t. u.

Water to Water Surface Heat Exchangers) -1.50 B. t. u
Gas to Water Fuel Economizer)-4 B.t.u.
Steam to Air (Ordinary Cast Iron Radiator) -1. B. t. u.
It is obrious from the above comparison that the high resistance operating against heat flow is on the air or the gas side of the surface. It is a well established fact that the heat transier improves as the velocity of the air orer a suriace is increased. If, then. the surface in contact with the air is sreatly enlarged and the air relocity is increased by forced circulation. the heat transfer per square foot of surface in contact with the water can be so materially improted that air coolers and air heaters are real commercial possibilities With the types of coolers considered herein heat transfers as high as s.j B. t. u. per sq. ft. of water surface have been obtained.

## Application

The immediate application of surface coolers is to cool the air from turbine generators. thus making it possible to recirculate the air for the purpose of minimizing dirt deposits
and practically diminating fire hazards, as well as the reclamation of the heat of the generator losses. This field is not necessarily limited to turbine senerators, but may be extended to hydraulic erenerators. motors. transformers, and any kind of electrical machinery where air is used as a heat transporting medium.

A surface cooler may be used as a surface heater where it should find much favor if used to heat the air for combustion for stokers, oil burners and pulverized fuel burners. The heating of the combustion air with stcam extracted from the main turbine presents the same economic possibilities as the heating of the feed water.

If used as steam condensers, suriace conlers will conserve the condensate and make possible condensing operation in localities whore no circulating water is available and space limitation is an important factor

The large amount of surface which can be installed in a small space should in many cases make them well adapted to indirect heating sustems.

## Construction

The design and construction of surface coolers, as now beins manufactured. puts them in the class of other substantial power house apparatus. They should not be confused with automobile radiators but rather compared to surface condensers

The fins are substantially attached to the tubes. The water passages can be cleaned and the foints between the tubes and the headers can be repaired in the same manner as a surface condenser.

Since each conlersection consists of a bundle of tubes the:e are unlimited posifilities as to the

Length of Tubes
Arrangement of Tubes
Air Velocities
Trater Telocities
Number of Water Passes

## Counter and Direct Flow

Direct flow is the term applied to stuch an arrangement of air and water passages that the two pass through in the same direction; while eotunter flow means that they pass in opposite directions, thas bringing the cold water and the cold air at one end of the cooler and the warn water and the warm air at the ather end of the cooler. 'The counter flow



Fig. 1. Curves in Upper Section Show Counter Flow Principle; Lower Section, Direct Flow Principle. Water 85 Deg. F. Air 140 Deg. F.
principle is essential if the air is to be cooled to a temperature close to the entering water temperature or if the water is to be heated to a temperature close to the entering air temperature.

The difference in effect between counter and direct flow depends on the ratio of air and water quantities and the amount of heat transferred. From Fig. 1, illustrating a repre-
per eent of the heat that it wonkl if used for counter llow.

## Heat Transfer

The unit of heat transfer generally used is 13. t. 11. per square foot of surface per hour per degree li. difference in temperature, and this unit will be used throughout this descrip)tion. Also when reference is made to the surface area, it means the square feet of surface exposed to the air, that is, it is a measurement of the fin area as well as the tube surface.

In determining the unit heat transfer the mean temperature difference between the air and the water must be determined. Where the temperature change of both fluids is slight the arithmetic mean temperature can be used without introducing much error. But, where the temperature change of either or both fluids is considerable, then the logarithmic mean is far more accurate.

If the ratio of the terminal temperature difference to the initial temperature difference is 1 to 2 the error is 4 per cent but if the ratio is 1 to 5 , the error is 20 per cent. The conditions dealt with here show ratios sometimes in excess of 1 to .5 which has necessitated the general use of the logarithmic mean temperature as a basis of all heat transfer calculations.

The heat transfer possible depends on the design and construction of the cooler and there may be many unknown factors as well as the following established factors, which have a bearing on the heat transfer:

Arrangement of tubes
Tube spacing
Material of tubes and fins
Depth of fins
Spacing of fins
Thickness of fins
Attachment of fins
Smoothness of surface
Uniformity of water flow.


Fig. 2. Brass Tube with Spirally Wound Copper Fins
sentative condition, it will be observed that the counter flow cooler cools the air to within 15 deg . F. of the incoming water temperature, whereas, the same cooler using direct flow cools it only to within 20 deg. F. Also in the latter case the cooler will remove but is.is

The heat transfer is also greatly affected according to the utilization of the cooler. The factors which have an effect on the heat transfer are as follows:

Air Velocity
Air Distribution

> Water Velocity
> Cleanliness of Surface.

## Physical Conditions

The characteristics of coolers having different kinds of radiating surface may vary quite widely: but the efficiency of heat transfer on the basis of a square foot of radiating surface on the air side does not change as much as might be expeeted, provided there is no decided limitation to the transference of heat from the extremities of the radiating surface back to the tube conducting the water.

Many samples were tested to determine if one kind of surface was more effective than another. Most of the samples were of the finned variety and included fins of different depths, thicknesses. spacings and colors. The trpe selected consisted of a ${ }^{5}$ - in . outside diameter, Number 1s B. W. G. Amiralty brass tube with $1_{4} \mathrm{in}$. deep by 0.012 in. thick copper fins spaced seven to the inch and secured to the tube by flanging and soldering Such a tube is shown in Fig. 2 and data given herein apply to this particular type of radiating surface.

## Effect of Air Velocity on Heat Transfer

The prevailing impression concerning the effect of gas or air velocity on heat transfer has been that the heat transfer varied proportionally to the square root of the gas velocities. It is obrious that no such fixed law can exist because the heat transfer is also affected by the resistance on the water side and therefore unless the relation of internal and external resistances is fixed the effect of air velocity must be a rariable factor.

A general average of the effect of air velocity, as indicated from many tests on these coolers (see Fig. 3), shows a proportionality varying from the 0.5 power to the first power of the air velocity and this with a fixed water velocity. When the air velocity is increased, the resistance to the flow of heat on the air side is reduced but the resistance on the water side is unchanged. Consequently, the effect on the heat transfer depends on the relation of these two resistances. If the water velocity were increased so as to reduce the resistance on the water side commensurate with the reduction of resistance on the air side, the heat transfer probably would be directly proportional to the air velocity:

Some investigators maintain that heat transfer is a function of the frictional resistance rather than the velocity and this is undoubtedly true to some extent because a high resistance to the flow of air generally means a more vigorous agitation and impact
which is conducive whe beter beat transfer. However, resistance does mot neressarily mean frictional resistance but may be loss of veloceity head and severe eddying, which lossent probably have no effect on heat transfer.

## Effect of Water Velocity on Heal Transfer

The effect of water velocity on the heat transfer will depend largely on the medium to or from which the heat is being transmiterd


Fig. 3. Effect of Air Velocity on Heat Transfer. Group A, Curves for shallow cooler. Group B, Curves for deep cooler

A more marked improvement woukd be expected in a steam condenser than in an air cooler because, in the latter case, thermal resistance on the water side is relatively low, compared with the resistance on the air side, and therefore any improvement on the water side will have little effect on the overall results.

In the case of the coolers under consideration, the air surface is six times the water surface, so that the conditions are approaching those met with in steam condenser practice and a reasonable improvement was obtained in the tests. The results are shown in Fig. 4.

If the water velocity in the tubes is below the critical velocity erratic results may be expected. The theoretical critical velocities for ${ }^{5}$,-in. tubes are as follows. For velocities below these values the flow will not be turbulent, and within the zone it may or may not be turbulent depending on whether agitation has or has not been started.

THEORETICAI, CRITICAL VELOCITIES FOR ${ }^{5}$-IN. TUBES


Turbutent liow
Abste.

$3.1 \mathrm{fl} . \mathrm{s}^{\circ} \mathrm{c}$.
$1.1 \mathrm{ft} . \mathrm{sec}$


Fig. 4. Effect of Water Velocity on Heat Transfer

## Effect of Depth of Cooler on Heat Transfer

A careful analysis of many tests covering different kinds of coolers revealed the fact that the depth of cooter had a decided effect


Fig. 5. Relative Effectiveness Factor for Six Types of Surface Cooling Equipment Reduced to 1600 Feet Per Minute Air Velocity and Two Feet Per Second Water Velocity with Estimated Allowance for Tube Design
on the unit heat transfer. By depth is meant the square feet of surface traversed by the air, from the entrance to the exit, per square foot of frontal area or per square foot of free area.

An explatation of this phenomenom has been somght by attribating it to one or more of the following causes; but in every instance some individual test woukd disprove the theory:
(1) That the logarithmie mean temperature might not be a true expression of the temperature difference.
(2) That there may be condensation and re-evaporation of moisture in the air because of the water temperature being below that of the dew point.
(3) That the effect of the viseosity of the water and the viscosity of the air may be appreciable.
(4) That there may be variation of heat transfer with temperature difference:
(.)) That, considering the low temperature differences, there may be a fixed loss or a fixed temperature difference to produce any flow of heat.
(6) That in combining so much surface into one cooler, there may be a material amount of heat conducted from the high to the low temperature side.
(7) That, because of the relatively large drop in temperature of the air in a very short distance and in a very short period of time, the actual air temperature gradient effecting the heat transfer may be quite different from the gradient expected or the one measured by thermometers.


Fig. 6. Illustrating How the Heat Transfer is Affected by Air Velocity and Depth of Cooler for a Constant Water Velocity

This condition has been found by other experimenters to a somewhat lesser extent. The large number of tests made under widely varying conditions were remarkably consistent in all respects and they all indicated a
decided falling off in heat transfors as the depth was increased as indicated in Fig. i. The correet explanation of this condition may be a combination of sereral of the foregong efliects.

## Conclusions

The velocity of air is a very influential factor in beat iransfer, but the effect of water relocity on heat transfer is relatively small providing a turbulent flow is established.

The material used, the physical construction, and character of design are important factors in the heat transfer. The depth of cooler must be taken into consideration in determining the overall performance. It is
unsate to assmane that the mat performance of a small cooler (ath be duphliated in a hatre cooler.

The proper distribution of air and water is. of course essential. Non montion is mante of the possible variation which may reult from poor distribution, because all hest remults are of coolers having apparentlygool airand water distribution.

The determination of cooler depth is dependent on the air velocity For low air velocities the cooler should be shallow and for high air relocities the cooler shoukd he decp. The curves in Fig. if illustrate how the heat transfer is affected by air velocity and depth of cooler for a constant water velocity.

# Notes on Wiring 

By A. K. Baylor<br>Gexeral Electric Compani, New York<br>Chairman Wiring Department of Joint Committee for Business Development

These notes based on figures and arguments issued from time to time by the Wiring Department show the direction in which the Joint Committee for Business Development is working. The figures given prove what boundless possibilities there are in the electrical field and emphasize the fact that we have hardly scratched the surface yet. The engineer is ahead of the business man. The business man must now get busy and make a more extensive use of what the engineer has developed.-Editor.

Among the various branches of work of the Joint Committee for Business Development, the Wiring Department is just now especially active.

It is generally agreed that the development of the domestic demand offers the best immediate prospect of new business for the central station in most communities. The possibilities in this direction are emphasized by the following figures:
Estimated number homes in United States, approximately..............
Estimated number homes reached by
electric lincs approximately electric lines, approximately
$21,000,000$

Estimated number homes wired for electric service.

13,000,000

Estimated number homes reached by electric service, but not wired.

7,600,000

Estimated number homes not reached by electric service, approximately.

5,400,000

Estimated number homes connceted during 1921 .............................. .

Eight years ago the estimated average annual revenue to central stations per residence customer was $\$ 1$ - now it is over $\$ 25$.

It appears reasonable to assume that with the present tendency to make greater use of light and domestic appliances, the comestic revenue within the next five years should be increased to at least $\$ 3.5$ per annum. Also
that the number of houses comnected per annum for the next five years should be at least equal to the record of 1921 , or a total of $3,500,000$ houses connceted during the five year period. Increasing the present average domestic demand from \$2.5 to s.3.5 per anmum and adding $3.500,000$ homes at a 53.5 average per annum would yield a total increase of annual gross from domestic load of nearly 200,000,000.

It is obrious that next to the establishment of the central station itsclf, wiring-the physical connection with the consumerunderlies all central station service and that the central station is primarily interester (with the consumer) in the character and capacity of the connecting lines and the adequacy of outlets.

The central station is the natural nucleus of electrical activity in every community and (neglecting isolated plants) everything electrical in the community is dead and useless except as it is connected to and served by the central station. Therefore in order to get satisfactory and maximum results the jobbers, contractors and dealers must work in co-operation with the central station.

The initiative in connecting new customers or increasing demands on existing connections
should come from the central station, lout, up, to say ten sears ago, the butk of house connections came unsolicited. It is only in more recent years that systematic efforts have been made io attract the domestic consumer and (hecolop the use of current consuming appliances in the home. The results obtained indicate that much more can be done along these lines. In general it has been left to the contractors to solicit as well as execute wiring contracts and as a rule they have competed on a price basis. The public generally is ignorant on the subject and at the same time naturally wants connection and service at a minimum cost.

The consumer can readily obtain information as to the extent and cost of everything he requires in the way of electrical equipment and service except in this all important field of wiring circuits and outlets. Here there are no standards for his guidance.

The inevitable result of these conditions has been that the capacity of lines and number of outlets have been eut down to make possible a low contract price and the myriad outlets from the reservoir of power to the point of application are throttled at the nozzle.

Almost without exception the consumer finds from experience the need of more outlets and the cost of adding them is far greater than would have been the case if proper provision had been made in the original installation. In the meantime the sale of current consuming devices is checked and their use, even when purchased, is restricted sometimes to the zero point by lack of convenience outlets.

It is doubtful if there is a home or place of business anywhere, that is, even in the opinion of the occupant, completely and conveniently wired-a condition which is an object lesson for future wiring business and offers immediate opportunity for development of existing connected load.

With the object of establishing some basis for the guidance of the public in dealing with wiring installations, the Wiring Department of the Joint Committee has been working with the Wiring Committee of the N. E. L. A. who have recommended a so-called "Dinimum Standard" suggesting its adoption by Central Station authorities generally: Through the agency of the Joint Committee this standard will be brought to the attention also of architeets, builders and contractors for their consideration.

Briefly stated, this standard is a minimum of one lighting and one convenience outlet in any one room and an average of three outlets per
room, including lighting and convenience outlets but excluding all switches. In computing this average only parlors, sitting rooms, dining rooms, kitchens, bedrooms, ete., are counted as "rooms." Hallways, stairways, closets, cellars, unfinished atties, ete, are not counted as rooms but lighting and convenience outhets in these areas are included in estimating the minimum arerage of three outlets per room.

With such a standard in vogue the consumer on applying to the central station for information as to wiring his house would not merely be referred to the contractor, but would be advised not to consider anything less than the minimum standard as otherwise he would inevitably be obliged to make additions at a price considerably in excess of what they would cost as a part of the original installation. At the same time information would be given as to value and convenience of adequate outlets. The contractor would give similar adrice and thus the mind of the customer would be set in the right direction.

In the case of new building, the architect would base his recommendations on the minimum standard. The result should be a gradual raising of the standard until the minimum is increased to an average of four outlets per room, then five or more with the increased use of light, of portable lamps and domestic appliances generally, and resultant appreciation of the necessity of convenience outlets.

Statistics show that ten years ago 2 to 4 per cent of the total expended on the average home was applied to the plumbing equipment. This has been gradually increased to from 7 to 12 per cent.

Today the cost of electrical installation in the average home is estimated at about $21 / 2$ per cent. To raise the electrical standards the central station must take the initiative. There is much to be done along educational lines with the public, the architect, the builder and the contractor, but in dealing with the immediate problem of wiring old houses and increasing the outlets in houses already connected the central station must address itself directly to the public. To do this effectively the full co-operation of the contractor must be gained except in the rare cases where central stations have found it necessary to undertake wiring contracts themselves. Will the contractors take advantage of this great opportunity:

A recent article in Electrical Retailing points out that the National Association of Electrical Contractors and Dealers was cre-
ated 22 years ago as an organization of contractors without contemplating the retailing of electrical merehandise. The words "and Dealers" were added only recently when too many got the idea that all contractors should also become chealers. The association was almost swept off its feet by the merchandising movement of the boom years prior to 1921 . The depression of last year and the losses sustained through forced liquidation of inventories caused a reaction. This reaction to the original field of contracting was emphasized at the Buffalo convention of 1921 and in the subsequent activities of the Association has caused a large portion of the members to again direct their attention especially to contracting. This tendency is being augmented by the present widespread interest in wiring under the stimulation of the Joint Committee for Business Development and of the Central Station Interests everywhere.

Those who still continue a retail business should bear in mind that more and better wiring with the provision of adequate outlets must in any case precede a full development of appliance sales.

Coincident with the movement for better wiring conditions have come into general operation financing companies organized to give to the customer, through the contractors. the benefit of time payment terms on wiring installations. This has proved a great stimulant to such business.

In some cases contractors have financed their contracts through local banks but although the ordinary bank interest rates on such cases are low compared with those of the contract financing companies, the bank restrictions are unusually severe and the credit of the contractor in his operating function is limited by these loan obligations.

In many communities central stations have financed these contracts but here also the central station must carry such accounts as a contingent liability and at the same time tie up funds that might be applied to the extension of plant and distribution lines.

There is objection also to central stations entering into a quasi banking business. The most serious objection, however, is that central stations may be forced to take action for recovery against customers delinquent on time payment contract to the detriment of their community goodwill.

It appears better, therefore, for either contractor or central station to turn such business
wer to companies organized and equipped for this special purpose whese rates are reatsmable, and espectally those who becamse of their experience and diversity of operations are in a position to follow the details of collertion efficiently, assume the bulk of the risk of ultimate payment and relieve the dealers on central stations of the necessity of leeing the principals in case of re-jossession proceedings. Such accommodations are atailable in case of old houses being wired for the first time orextension of existing installation and in either case where the owner, whether occupant or landlord, can be dealt with.

With such facilities any contractor of good repute, honest, energetic and competent may secure the capital to turn over any volume of business that he can efficiently supervise.

While the central stations and contractors are at work upon the connecting of old houses and amplifying existing installations, what is to be done to insure that wiring of new houses is of proper capacity and that adequate convenience outlets are provided: Here the aid of the architect and builder must be enlisted.

If the house is being designed and built for the owner's private use it may be almost taken for granted that the mere pointing out of the advantages of modern wiring will insure its adoption.

Where the house is built for sale or to rent the owner is of course primarily interested in the sale or rental price and there is little question that the provision of proper wiring will enhance the demand for any house when the trifling increase in price for sale or rent is considered.

No one would consider it practically ectnomical to omit faucets from bath tubs, sinks or basins because water could be bronght in buckets or through a hose from another point. Why then should the installation of electrical ontlets adequate in number and convenient in location be the exception and not the rule: It should be to the advantage of architects and builders to consider this sulsject carefully.

There are many angles to this important and interesting problem of wiring and if the interested parties-central station, jobber, contractor, electrical dealer, as well as the architect and builder-will study it in their mutual interest the result should be to the direct advantage of all erncerned.

There is no subject more appealing to the general public than electrical service in the home and proper wiring is the foundation of it.

# Control Equipments of the Electrically Propelled Ferry Boats for New York City 

By l. W'. Webl<br>


#### Abstract

It is indect a tribute to the designers of chectric formalsion machinery that virtually the same general scheme of control that has prover so successful on ocean-going merchant ships (such as the leflipse) amt naval bessels (such as the U.S.S. Mary/and) will also fill the exacting requirements peculiar to a ferry loat plying back and forth in conecsted harbor traffic. The principal points of difference result from the double-ended reversible operation that calls for a motor-driven propeller at each end of the boat and for the unequal division of power betwern these two motors. - Enator.


The three New York Municipal ferries now being built at the Staten Island Shipbuilding Corporation l'ards are to be propelled by a 23000 -volt threc-phase $3500-\mathrm{kv}-\mathrm{a}$. turbine-driven alternator and two 2100 -h.p. induction motors. Each induction motor has two separate windings; a high-speed or full-power winding and a low-speed winding. The control is so arranged that the highspeed winding of the stern or propelling motor and the low-speed winding of the bow motor are connected to the alternator. The low-speed winding is so proportioned that the bow motor will develop power just sufficient to overcome the dragging action of the water on the propeller.

The control equipment, a sketch of which is shown in Fig. 1, consists of a group of contactors mounted on the top of the operating panel.

## Control Group

The control group on the top consists of a steel framework on which are mounted nine 2300 -volt line contactors, four 250 -volt field contactors, current and potential transformers for instruments, and two overload relays for the low-speed windings. The contactors are of the air-break type equipped with magnetic blowouts and are operated by means of a master controller and individual solenoids. For emergency operation, however, the contactors may be opened and closed by means of cam shafts actuated by levers on the front of the operating panel. The insulation of the contactors, mechanically and electrically, is of the type successfully used in railway service and consists of vertical steel rods with wrapped insulation upon which are clamped the conducting parts. This method, as proved by past experience, provides flexible insulation of great mechanical and electrical strength.

With all of the contactors above the panel, the high-voltage and heary-current-carrying
parts are well out of reach of the operator. The contactors are faced so that the arc chutes project over the back of the pancl.

## Operating Panel

The operating panel is a structural steel cell faced on the front side by a sheet steel plate upon which are mounted all the meters and levers necessary to control the turbine and electric gear. There are on the front of the panel: the master controller with its single operating lever, speed-control switch lever, generator-field rheostat handwheel, control switch, and three levers for emergency manual operation in addition to the instruments, instrument fuses, etc. There are no live parts on the front of the panel. The four motor ammeters are connected so as to give the current in each winding of both motors. There is one instrument which will indicate the temperature of the generator field and another which will give the temperatures of the generator as well as the motor stators. One other special instrument is the excitation indicator. It is connected to the alternatingcurrent line circuit by means of current and potential transformers and gives an indication as to whether the correct generator excitation is being held to give efficient, stable operation at any frequency. The speed of the generator and motors is given by three millivoltmeters, calibrated in revolutions per minute, and connected to magnetos.

## Connections

The general scheme of connections is shown in Fig. 2. From the sequence of contactor operation, it can be seen that when going in one direction the high-speed winding of No. 1 motor and the low-speed winding of No. 2 motor are used. In the other direction the high-speed winding of No. ? motor and the low-speed winding of No. 1 motor are used. In starting and reversing the boat the high-speed winding of one motor only is


Fig. 1. Outline Drawing showing the Arrangement of the Operating Panel and Control Group
used and always with increased excitation on the alternator. This increased excitation is obtained by contactor No. 13 closing. As double excitation is not needed the resistance indicated as "manoeurring resistance" is used. The transfer resistance shown just
below is to prevent a short circuit on one side of the three-wire exciter when transferring back to normal excitation without opening the field circuit.

As the bow propeller is very hable to become blocked by running into floating
debris, orerlome relass are arranged in the low-spere windings so that in ease this should happen the low-sperd winding contators will le opened.

Athough the ez30-volt alternating-current contactors are copupped with magnetic blowouts capable of opening mader load, the control is arranged so that the fied contactors open first when taking off power. This is accomplished in the electric control by only


Fig. 2. Simplified Diagram of Connections of the Control Equipment
the line contactors being closed on the first position. This means that in turning the lever to the off position the line contactors are still closed in one position after the field contactors open. When using the manual control the two levers are interlocked so that the field lever has to be turned off first.

## Operation

The master controller has four positions either side of the off or stop position. The speed-control switch is a three-position switch which controls the direction of rotation of a small motor on the turbine governor and thereby changes the governor setting. It is spring returned to the off position from the "Increase" postion but a slight star-wheel action will keep it in the "Decrease" position.

To start the boat from rest, after the turbine has been started and the speedcontrol switch placed in the "Decrease" position, the master-controller lever should be pushed or pulled (depending on the
direction it is desired to go) through the first position to the seeond position. On the second position, connections are established to the high-speed winding of the stem motor and inereased excitation put on the alternator. Ifter the motor comes up to a steady speed, the lever should be moved to the third position where the atternator excitation is reduced to normal. Then the lever should be moved to the "Run" position which closes the contactors that connect in the low-speed winding of the bow motor. The speed-control switch may then be manipulated to obtain the desired speed.

To reverse the boat when going at full speed, the speed-controllever should be put over to the "Decrease" position and the controller lever moved to the off position, then to the second position in the opposite direction. The procedure from then on is the same as in starting

If, for any reason, the electric contro] cannot be used, the contactors may be operated manually by the emergency levers on the right of the panel. It will be noted that there are three large levers. The first or left-hand lever is connected to the turbine throttle. The reverse (second) lever handles the high-speed $w$ nding contactors and has a position either side of the off position for obtaining reversal of direction. The other lever operates the field contactors and has two positions besides the off or stop position. In manual operation, the low-speed windings are not used as this is considered emergency operation only.

To start the boat with manual control, the throttle lever should be placed in such a position that the turbine will run between one-quarter and one-third speed. The reverse lever should be placed in either position depending on the direction it is desired to go and then the field lever pulled to the first position which places over-cxcitation on the alternator. After the motor has come up to a steady specd, the field lever should be pulled over to the "Run" position and the throttle lever moved to give the desired speed.

To reverse the boat when going at full speed, first the throttle should be moved to a point where the turbine will run from one-quarter to one-third speed. Next the field lever should be thrown off after which the reverse lever may be put in the opposite direction. This will change the connections so that the high-speed windings of the other (bow) motor will be used. Then the field lever should be pulled on and the same procedure followed as in starting.

There are meelanical interlocks between the electric lever and the mantual levers to prevent both methods of control being used at the same time.

## General

Although there is now in operation a Diesel-electrically propelled ferry on the
west coast, these New lork Municipal ferries will be the first ferry boats to le driven by a turbine-alternator. It is expected that this type of drive will prove to lave increased efficiency and flexibility of control the same as has been shown with the Diesel-electric drive and be far superior to the old direct steam drive.

# Million-volt Testing Set 

## PART II

By A. B. Hendricks, Jr.

Transformer Engneering Department, General Electric Comphisy, Pithaferd, Ahas.
The design and construction of the three $500-\mathrm{kw}$, 578,000 - volt transformers and of the $500-\mathrm{kw}$. insulat ing transformer were given in the Deember, 1929 , issue of the General Ebectric Review in lart I of this article which included also illustrations of single-phase arcs between sharp points spaced 9,11 , and 14 ft . apart and corresponding to the crest voltages of sine potential waves having effective valu s of approximately. $1,000,000,1,200,000$ and $1,509,000$ volts.-EDITOR.

## Three-phase Arcs

Photographs of ares taken with the three main units connected delta- $\mathrm{I}^{\prime}$ with grounded neutral are reproduced in Figs. 19 to 24 inclusive,* the general arrangement being shown in Fig. 19.

The spark gap consisted of sharp pointed brass rods arranged with the points at the cor-

[^3]ners of a horizontal equilateral triangle, measuring nine feet between points on each side. In these tests there was no neutral arcing point, but the arcs seemed to form indifferently in either delta or Y . Doubtless the I formation is always preceded by a single-phase are, but as the arcing voltage between points is closely proportional to distance, at least for high voitages, there is always a strong tendency to form the $\mathrm{I}^{\prime}$ and to the eye it appears


Fig. 19. 1,000,000-volt, 9-ft., Three-phase Spark Gap with Single-phase Are One phase reversed)
instantanconsly. Actually there is a millionvolt electric fied rewolving at 3600 revolntions per minnte.

The lefthand point in Pig. I! was connected to the mint placed in the large tank and excited through the insulating transformer as


Fig. 20. 1,000,000-volt, $9-\mathrm{ft}$. Three-phase Arc showing Both $Y$ and Delta Formations


Fig. 21. Another $1,000,000$-volt, $9-\mathrm{ft}$. Three-phase Arc showing Both Y and Delta Formations
it was inconvenient to change the connections. This inserts additional capacitance and reactance in this leg of the high-vo!tage Y, thus raising the voltage so that there is a slightly greater tendency to arc from this point to either of the others than for an are to form between the other two points.

In the first test there was no means of determining the polarity of this leg except by trial; and, as shown by Fig. 19, it turned out to be reversed, so that only a single-phase are was formed between the other two legs.

Reversal of the connections produced the three-phase Y-delta arc shown in Figs. 20 and 21 . This is somewhat distorted by being seen nearly edge on from a position below the plane of the spark gap. This was really an open delta- $Y$ are as there appears to be no direct are between the two right hand points.

[^4]Since the ares form almost indifferently in any combination, single-phase, open delta, delta or $Y$, and follow each other in rapid succession, the arrangement shown in the illustration is a matter of chance.

In making the three-phase tests there was no resistance in the high-tension circuit other than the high resistances paralleled by the choke coils.

In Figs. 22 to 24 inclusive* the eamera was placed on the floor of the supporting structure shown in Fig. 19, pointing directly upward to the neutral point of the ares, thus showing them in their natural position and about 10 ft . above the camera.

All the arrangements in taking these last photographs were identieal with those of the previous three-phase photographs, but the low-tension voltage was about 10 per cent less, presumably because of different atmospheric conditions. The spacing of the gaps was nine feet as before.

Although less than one million rolts were required to start the arc, the generator excitation was greatly increased by means of the field rheostat at the instant of the first discharge so that the actual arcs were formed at an unknown voltage, but approximating one million.


Fig. 22. 1,000,000-volt, 9 -ft., Three-phase Arc Forming in Open Delta. The two bright spots are incandescent lamps on the ceiling, which were inadvertently turned on before the camera lens was capped

Unless otherwise indicated, all voltages given in the article are effective values of a sine wave having the same crest value as that actually observed. The generator potential wave form was always close to a true sine wave.

Wit hall conditions the same as far as known (except for atmosplieric variations) the lowiension voltage required to produce the are, with a constant distance of nine feet between points, varied as much as i5 per cent from day to day and 5 per cent on the same day.

With two units connected in series for one million solts to ground, the high capacitance Gives an initial discharge resembling a direct lightning stroke which tends to destroy any object under test. This discharge seems to be a rapidly damped oscillation and is usually followed by a 60 -cycle are.

With one or more units in normal comnection, that is with one terminal of the hightension winding dead grounded, the capacitance effects are less marked but still more severe than with testing transformers of smaller size and less inherent capacitance, and the initial discharge is practically always followed by the 60-cycle arc.

Fig. 22 shows two 9-ft.arcs in open delta, the are failing to form on the third side. The two bright spots are incandescent lamps on the ceiling which were inadrertently turned on before the lens was capped. The cover illustration of this issue of the Revien shows a $9-\mathrm{ft}$. delta arc, Fig. 23 shows a $Y$ formation and also one single-phase arc, and Fig. 24 shows a series of $9-\mathrm{ft}$. arcs in both Y and delta.


Fig. 23. 1,000,000-volt, 9 -ft., Three-phase Arc showing $Y$ and also Single-phase Formation

## Three-phase Arcs with Grounded Neutral Sparking Point

Further tests were made with a fourth sharp point placed at the geometric center of the delta and grounded, being supported from above.
'This caused the l' ares to predominate, and to restore equilibrium the motral sparking point was raised about one foot alowe the plane of the delta. The potential of one promet being somewhat higher than that of the others as already explained, it was moved out about


Fig. 24. 1,000,000-volt, 9 -ft., Three-phase Arc showing Y-Delta Formation
six inches in some of the tests. This is the lower right-hand point in the illustrations of three-phase arcs. The curved streak near it


Fig. 25. Repetition of Single-phase Arcs with Y Arcs Tending to Predominate on Two Legs
is a reflection of one of the balls of the $75-\mathrm{cm}$. ball gap, which was near the camera as. shown in Fig. 19 but not comnected to the circuit. No series resistance was used in these tests.

Fig. 2.5 shows single-phase and Y arcs, two legs of the Y tending to predominate. This


Fig. 26


Fig. 27


Fig. 28

Wils an exbilition are repeated many times, the ares holding mintil they had run wo the neutral condluctor* about (; ft.

Fig. 20 shows two legs of the delta and two of the V . The initial discharge of the capacitance (pilot spark) resembles a cotton rope partly untwisted and shows about three oscillations. This effect appears on many of the photographs and justifies the statement that the first discharge is usually oscillatory and rapidly damped. Theory indicates the same thing.

Fig. 27 shows both single-phase and Y ares and Fig. 28 is a good imitation of the Scott connection.

In Fig. 29 one transformer failed to are, but a discharge occurred from the neutral to the middle of one side of the delta. The oscillatory character of the initial discharge is clearly shown.

Fig. 30 shows arcs from neutral to two cornersonly. The grounded neutral sparking point was removed for the next two illustrations.

Fig. 31 gives three single-phase arcs and a Scott connection. Compare with Fig. 28 .

Fig. 32 shows a peculiar formation of great beauty. The arcs are doubtless extremely sensitive to atmospheric conditions, the path of the circuits and the proximity of conductors, especially if grounded, and naturally show infinite variety of form.

## Tests on Line Insulators

In these tests two transformers were connected in series for $1,000,000$ volts to ground. No series resistance was used.


Fig. 29

Fig. 3: shows a fo-cycle aroover to gromat on a string of 20 II ewlett insulators, a distance of about 10 ft . at about $9.00,000$ volts. The are went wide of the insulators, even farther than appears from the illustration.

Effect of Parallel Reactance in Low-Voltage and Series Resistance in High-Voltage Circuit
It has been shown that these transformers take a leading exciting current at a powerfactor of about $2^{-}$per cent which remains. nearly constant through the whole range of voltage.

In a certain test on suspension insulators the generator current was ! $9 . . \bar{i}$ amp. and the field current 16 amp . This is an abnormally low field current, the excitation beiner produced largely by armature reaction of the leading current. The voltage is therefore unstable and at the instant of areover. when the load changes suddenly from leading to a short-circuit lagging current, the generator voltage suffers a large drop. It was thought that the addition of a constant large lagging load in parallel on the low-roltage side would stabilize the voltage since a much higher field excitation would then be required for the same generator voltage.

Accordingly a power limiting reactance (without iron) of 11.5 ohms was connected across the loaded phase and the test repeated. This reduced the generator current from 97.5 to 34.5 amp , and increased the exciting current from 16 to 3.5 amp . The are then held somewhat better. The reactive load stabilizes


Fig. 30


Fig. 31


Fig. 32


Fig. 33
the generator voltage but does not decrasithe destructive effeet of the first discharge.

A resistance of 120,000 olms, consisting of 2s carborundum rods, was then hung from the insulator st ring and connceted in series with it, the reactance being discomected.

The resistances ared over, as well as the insulators, but the are failed to hold.

Finally, the reactance and resistance were tried together, the reactance in parallel with the low side, the resistance in series with the high side. The initial discharge, while arcing over the resistances as before, as well as the insulators, was followed by a heavy 60 -cycle arc around the insulators, the 60 -eycle current also passing through the resistance after the first impulse. No photographs were taken of these last two tests.

In all of these last tests there was little variation in arcing voltage. Apparently the action may be made anything desired by variations in circuit constants and it is a question which condition is most suitable for a given test.

The same transformers will give an impulse test, a 60 -cycle arcover, or a combination of both, but the last is much more severe than the usual tests of past experience.

It should be remembered that the actual voltages are not only greater, but also higher to ground and therefore approach more nearly to abnormal service conditions.

The two transformer units have a combined capacity of 1000 kw . at 6 per cent reactance (plus the insulating transformer) and very high internal capacitance, so that extraordinary effects are just what should be expected.

The three-phase nine-foot point spark gap test was repeated with 23 ohms reactance across each low-voltage winding and it was found that the 60 -cycle ares held better than without reactance, which confirms the singlephase results.

Perhaps the effect of capacitance could be modified and controlled by the use of a water jet or other suitable resistance between line and ground.

## Wave Forms

The two generators are on the same shaft and while each is rated 500 kw . single-phase, it is wound three-phase Y-connected and is good for 750 kw . three-phase.

With the two generators in parallel the normal capacity is thus 1500 kw . or the same as for the three main transformers connected three-phase. These generators were especially designed for a sine voltage wave, and the
variations therefrom are small over a wide range of conditions.

It is often stated as a gencral rule that a leading current distorts the wave form more than in-phase or lagging currents. This may often be true but as a general statement does not hold; it depends on the design of the gencrator.

With the reactance in parallel and 34.5 amp . lagging armature eurrent, the amplitude factor (ratio of erest to effective value) of the voltage wave was 1.399 .

Without the reactance and with 97.5 amp . leading armature current, this factor was 1.395. In both eases the variation from sine shape was thus about 1 per cent. The wave form was nearly perfect with no appreciable ripples, but more symmetrical with leading current.

The reactance of the main transformer is 6 per cent, the errors of the voltmeter coils at full load, zero power-factor leading, is under $1 / 2$ of 1 per cent and of the order of $1 / 10$ of 1 per cent under the conditions of the tests described, while for a single transformer at least there is a difference of only about 1 per cent between voltages determined by the conversion ratio and the voltmeter coil. The values of high voltages given herein are as referred to a ball spark gap which responds to transients of extremely short duration, and the difference between the conversion ratio and gap voltages is as follows, in round numbers at full voltage:

## $71 / 2$ per cent for one transformer. .

$171 / 2$ per cent for two transformers, neutral grounded.
$221 / 2$ per cent for two transformers, one end grounded.

In all cases the ball gap indicates a higher voltage than the conversion ratio or voltmeter coil.

The differences cannot be accounted for by variation of generator wave form (1 per cent), by errors of conversion ( 1 per cent), or voltmeter coil ( $1 / 10$ of 1 per cent), nor by errors of instruments or observation. The cause may be transient voltages which are always present and whose effect seems to increase faster than the voltage and thus reaches a high value with the extreme potentials under consideration, or resonant conditions in some part of the circuit.

In referring to test voltages it is therefore pertinent to ask, what voltage? as it may be the average, effective, crest, or transient value that is meant.

There is also a difference in transients. The point gap does not respond as quickly as the
ball wap and may indicate less than the maximum instantaneous voltage In the present series of tests with point gapos the voltage was
 volts to ground and $9.00,000$ wolts with meut ral grounded which was as high a vollage as the old spark gap would stand, the new lool-cm. gap lecing manfinshed.


Fig. 34. Comparison of Test Results, $1,000,000,1,200,000$, and $1,500,000$ Volts at 108,132 , and 168 inches, with Tentative Straight-line Spark-gap Calibration Curve Through the Origin and $1,000,000$ Volts at 106 inches

The point-gap distance-voltage curve has been determined with some accuracy up to $1.000,000$ volts ( 106 inches) and being close to a straight line through the origin of co-ordinates could be produced to $1,500,000$ as a first approximation at least. This also could be checked by the ratio of ball gap to the conversion voltages of a single unit.

Fig. 34 represents a tentative calibration, a straight line from the origin through 106 inches at $1,000,000$ volts as previously determined by F. W. Peek, Jr. The three plotted points correspond to those of this article at 108,132 and 168 inches ( 9.11 and 14 ft .) for $1,000,000,1,200,000$ and $1,500,000$ volts respectively and are given simply to show that the stated voltages were actually reached and probably exceeded.

The point gap is variable in behavior, the results depending largely on atmospheric conditions, but the curve given is probably correct within $\overline{\text { s }}$ per cent. It does not hold for small spacings below 100,000 yolts.

The transformer terminals act like ball gaps in not showing corona and in response to transients so that the latter set a limit to the voltage that may be obtained. As far as the
transformer proper in ernarimel it could evidently be operated at still hispher biterede vollages if the transents could be suppersed

In one instance, afready referead (o, a dise charge enecurred from the choke esil on the million-volt terminal about in ft due west in an iron pipe on the wall of the buiding. although a sparking point was monnter on the same choke coil nine feet from a grounterd point due cast. The west gap) resembled a point and plane, the cast gap was composed of two points, which may explain the tendency to are to the west.

In one of the three-phase tests with the three units connected in $Y$ with grounded neutral, one of the terminals arced over from cap to sleeve after a vicious series of ! 1 - ft. arcs across the threc-phase point gap at about $1,000,000$ volts. Two of the terminals measure (6.) in. from cap to sleeve, the third or million-rolt terminal mounted in the large open tank measures 12.558 in . This unit was also grounder, but excited through the insulating transformer, the additional reactance and capacitance raising the voltage, though but slightly. However, this terminal arced over, the two shorter ones of about half the length did not!

It has been found that the results may be greatly improved by taking the precaution to keep the generator excitation as high as possible. This is not on account of wave form, which is always good, but to stabilize the generator voltage to give sufficient power to cause a 60 -cycle arc to follow the initial oscillatory discharge. In some of the tests, such as on suspension insulators and high-voltage bushings, the 60 -cycle current failed to follow the initial discharge, the latter being oscillatory and of destructive violence. The simple expedient of changing the generator connection for a lower voltage, which enables much greater exciting current to be used, was sufficient to insure that a bo-cycle are of great volume would invariably follow the first discharge. This also seems to have a tendency to suppress the oscillations and reduce the destructive effects

It is therefore conclusled that with the present testing set at least, high gencrator excitation is of great importance.

Fig. 3.5 shows a threc-phase point-spark gap with $10 \mathrm{ft} .21 / 2 \mathrm{in}$. spacine, arcing in T-formation at over $1,000.000$ wolts with low generator excitation. The crests of the current waves show as fine separate lines. Fig. 36 is of another arc at over a million volts taken under the same conditions except with high


Fig. 35. Three-phase Arc Between Points 10 ft ., $2 \frac{1}{2} \mathrm{in}$. Apart. Generator under-excited, giving arc of little volume
generator excitation. This arc is of much greater volume and appears as a continuous flame.

This is a record of some of the first results obtained with the new testing set representing the first trials which were in the nature of routine acceptance tests. The principal constants and the characteristic curves were measured with care, but no attempt was made to obtain great accuracy in the arcing tests.


Fig. 36. Three-phase Arc Between Points 10 ft ., $21 / 2 \mathrm{in}$. Apart. Generator over-excited, giving arc of great volume

When the $100-\mathrm{cm}$. ball spark gap is put into service it will be possible to extend the spark gap curves with precision to the limit of the apparatus. This is shown in Fig. 37 as it will appear when swung flat against the wall for cleaning and zero adjustment.

It will now be feasible to carry out an unlimited series of tests and researches in a region of high potential yet unexplored, but this must be left for the future to record.


Fig. 37. Diagram of $100-\mathrm{cm}$. Ball Spark-gap Which Will Make Possible the Extension of Spark-gap Curves with Precision to the Limit of the Testing Set Described in this Article

# The Electric Power Industry 

# Part III <br> THE MUNICIPAL ELECTRICIAN AND THE ELECTRIC POWER INDUSTRY 

By Charles P. Steinmetz

Chief Consulting Engineer, General Electric Comidany


#### Abstract

After tracing the early history of electrical power plants to the time when electric power production and supply became a separate industry the author shows the place held by this industry in our modern industrial life and outlines the probable future trend in the growth of large systems. He then discusses the relationship between the electric power industry and the municipality.-Editor.


The rapid development of electric light, railway and power distribution has placed new duties and new responsibilities on the municipal electrician, varying from the operation of a municipal lighting plant, to advising the legislative body on the rules and regulations required to supervise the operation of a private lighting or railway plant. Before discussing these relations, it may be of interest to briefly review the development of the electric power industry. It started with small local electric lighting stations supplying electricity for domestic lighting and street lighting and later also for small distributed power, and still more recently for all kinds of domestic service, as cooking, heating, ventilation, domestic power in the washing machine, vacuum cleaner, ice cream freezer, etc., though this field of domestic electric service is still little developed in most locations. The electric railway came next, again a local electric plant operating the street cars and in the large cities later on the rapid transit system. At the same time the electrification of the industries started and made rapid progress, operating the machinery of factories and mills by electric motors, often in connection with long distance transmission from water power, but often also from local steam electric plants in the factory or mill.

Thus we once had in the same territory three kinds of electric plants, for lighting, for railway, and for industrial power. This was inefficient and uneconomical. The three uses of electricity do not coincide in timethough they partly overlap-and by combining electric power generation for all classes of work, a better load factor of the plant is secured. That is, the machines are more uniformly loaded, thus operating at better efficiency and less machinery is required. The multiplication of reserve machines, of
the operating staff and attendance, etc., is eliminated by consolidating the various small stations into one large station; large and therefore more economical machines become available, etc.

This consolidation was initiated by the development of long distance transmission from water power, by replacing local smaller generating stations by substations from the transmission line. The economies realized herein led to the same development even where steam was the source of power. Two features contributed. First, the development of the modern steam turbine, which reached efficiencies of power production undreamed of in the days of the reciprocating steam engine; but it realized these efficiencies only in the huge units of 10,000 to 50,000 horse power. The second feature is the following: energy or power is the necessity of every industry, and therefore in the days before electrification every factory or mill had its steam engine producing the required power. But power production is an industrial operation just like the production of shoes, or furniture, etc. Now the superior efficiency of modern industrialism is due to the subdivision of work, whereby each industrial operation is carried on by a separate organization. It therefore is not economical to combine two such different industrial operations as the making of furniture and the production of the power used in furniture making; the management of a hotel and the operation of the electric plant supplying light and power to it; the organization most efficient to make furniture will not be efficient to produce power; the efficient management of a hotel will not be efficient in managing an electric plant. This led to the segregation of the power production from the industrial operations using the power, and the concentration
of the power production as a separate industry, the industry of clectric poace production and supply.

There are two fundamental necessities of our civilization: materials and power. The supply of materials has been organized during the last century by the development of railroads, steamship lines, etc., so that now anything produced antwhere in the world is available to us, and even in the necessities of life we draw on far distant countries. Today we see the organization, by the electrical engineer, of the second necessity, power; and just as during the last century the country has been covered by a network of railroads, bringing materials from anywhere to anywhere, so now we see the country being covered by a system or network of electric transmission lines, carrying power.

The development is not yet complete, and there are still numerous gaps, but a number of such electric systems already cover and serve territories of 10,000 to 20,000 square miles, and more, with amounts of energy reaching high into the hundred thousands of horse power. More and more these territorial systems interconnect with each other into still larger systems, closing the gap between them, and rapidly develop towards one unified electric power supply system covering the continent. (Though obviously the different parts of a system may be under different ownership, just as different parts of the railroad system are under different ownership.)

Such a modern territorial system interconnects numerous electric generating stations and many users of electric power: cities, industrial establishments, factories and mills, mines, railroad power substations, etc. Some of the generating stations are water power stations; others are steam turbine stations located at strategic points, such as cities or other large users. Sometimes the system centers around, and is developed from, a big city like Chicago or big water power like Niagara; usually, however, the generating stations and the users of power are fairly distributed over a territory (California, New England, Michigan, Central New York, Southern Atlantic States, etc.).

The electric industry thus has outgrown the limits of the municipality and even of the state, and is rapidly becoming a national industry, just like the railroads are.

In general, therefore, it is not economical any more to generate electricity for some limited service by a local station, but it is preferable to buy the electric power from
the territorial power systems, even where large amounts of power are needed. Thus for instance the elevated railroads of Chicago have shut down their generating stationseach large enough to supply a good sized city-and buy their power from the Commonwealth Edison Company. The large modern electric station built by the N. Y., N. H. and H. R. R. to supply power for its electrified railway service, stands idle and power bought from the New York Edison Company pulls the trains.

Thus with the development of the electric power industry: a complex situation has arisen, with which the municipal electrician has to cope. It is no more merely the question whether a municipal plant would be preferable, or a local private electric lighting company. The situation is further complicated because even most electrical engineers and administrators do not yet realize it.

There are various new possibilities between the municipal lighting plant and the city buying the electric service from a private electric plant just like any other customer.

Furthermorc, new questions arise such as that of the right of transit of high voltage high power circuits over municipal territory to supply power to industries, that of permissible primary distribution voltage, questions of regulation, of reliability of service, etc.

Usually a privately owned public utility corporation supplies the electric service of the municipality. This may operate a local isolated electric generating plant, where the municipality is not yet within reach of a territorial jower supply system. Or the municipality may be served from a substation of a territorial system (through transformers for light and power distribution, converters for railway service). Or, where the local station is sufficiently large and modern, it may be tied into the territorial system, so that the municipality becomes one of the customers, the local plant one of the generating stations of the territorial system.

The territorial power company may then operate the local light and power distribution as a part of the territorial system. Or a separate sub-company may be formed to take care of the local distribution, as is often the case, since the problems of local light and power distribution are sufficiently different from those of territorial bulk power distribution to make a separate management advantageous. Or an independent local company may buy the power in bulk from the territorial system and locally distribute it.

For instance, the company which operated an isolated generating station may, when the municipaity comes within reach of a territorial system, abandon its local station and buy the power from the tertitorial system, but otherwise retain its independence.

Usually, the municipality buys its electricity from the local private station or sul)station. Street lighting is taken care of bya scparate contract, as the long hours and the uniform power demand of street lighting justify a lower rate than for domestic lighting, while on the other hand, the street lights and their method of operation are materially different from domestic lighting, requiring considerable special apparatus (constant current transformers, rectifiers, are lamps, separate circuits, etc.). This has occasionally led to an unfortunate situation resulting in unsatisfactory street lighting by antiquated types of lamp, where the municipality refused to make a contract for more than a year or two, while the street lighting company could not afford the large investment of modernizing the street lighting system without the assurance that the new plant would be in service for a sufficient length of time to return the investment. A possibility is that the municipality does its own street lighting, installing, owning and operating the lamps, the street lighting circuits and the transforming devices, but buying the electric power in bulk from the local or the territorial private corporation (as in Milwaukee, etc.). In general, however, in most municipalities the amount of street lighting is probably too small to economically justify this.

Electricity for indoor lighting of municipal buildings, schools, etc., and for domestic power, as ventilation, would be bought by the city from the public utility corporation at the same rate as by other private customers. Or the city maty get a special rate in view of its peculiar position as the giver of the franchise. Or the city, while paring nominally the same rate as private customers, may effectively get a lower rate, for instance by combining the lighting service of all municipal buildings in one bill, and so getting the lower rate of a large customer; or by charging one uniform power rate for all uses, indoor lighting, power, etc.

Occasionally, municipalities may buy large amounts of power for the operation of a municipal pumping plant, etc., at the low rate of industrial bulk power, and sometimes a still lower rate may be secured if--for
instance be the nse of a remerooir the use of power can be limited whe ont peat: period, that is, discontinued during, ble fow hours of heary load wh the station.

Theoretically, a muncipal plant rammo economically compete with electricity supplied from a territorial system, since crom in large municipalities the electricity demand is so much smaller and so much less diversjfied that the economy of electric power production of the huge morlem territorial system cannot be approached. Practically: howerer under special local conditions a municipal plant may be very successful, espectally as long as no supply from a territorial system is available. I municipal plant has the advantage that a municipality usually (an borrow mones at a lower rate than a private corporation, and as a material part of the cost is the interest on the investment, this results in lower cost. Also, the municipal plant is not intended to make profits. Furthermore, by combination with other municipal activ-ities-as water supply--economies are possible which are not availar le to a local private plant. The formost disadvantage of the municipal plant is the political control of our municipalities. which leads to lack of continuity and often ineffiejency of the management and the operating force of the plant. and continuity and efficiency of management and operating force are most essential in an electric plant and their absence fatal. Where therefore the local conditions are such as to give continuity to the management of the municipa! plant and sufficient independence to train and maintain an efficient operating force, the plant will be successful as long as these conditions pertain.

Industrial power, that is, power in large bulk for the operation of facturies, mills, steel plants, etc., can rarely be supplied from the mumicipal plant, as its size is not large enough to allow sufficiently low rates. When therefore the municipality is reached be a territorial plant, the latter would supply: industrial bulk power and in the interest of the local industries access within the municipality would have to be given to the lines of the territorial plant.

The same economic question arises hetween the municipal plant and the territorial system which arises between a local private generating plant and the territorial system, and which in the latter case has almost always been answered by the local plant tying into the territorial plant as substation or generating station.

The manicipal generating station may be replaced by a manicipal substation of the territorial plant, that is, the monicipality buys the power in louk and distributes it as light and power. ()r, where the nature of the manicipal plan waraants it, it may tic in with the territorial system as combined substation and generating station. In short the municipal corporation takes the same relation to the territorial system as the private local distributing company discussed aloove. Industrial power, and railway power, then may be supplied either directly by the territorial system or by the municipal corporation as its !ocal representative.

Sometimes the development might be carried still further to private operation of the municipal plant. That is, the generating station or substation and the distributing system would be owned by the municipality, but operated by the private territorial company or a sub-company of it.

In general, it must be conceded that the development of the electric power industry from local to national scope leads away from the cconomic desirability of the municipal electric generation and rather towards municipal supervision and control.

The two features of electric supply which are of foremost importance to the public are regulation and reliability.

In lighting, 1 per cent variation of voltage gives about 5 per cent variation of light. A variation of about 2 per cent in light is the lowest which can be detected by the eve when watching for it, and 5 per cent variation is scarcely appreciable unless continuously recurring as flicker. Even an occasional 10 to 15 per cent variation of light (that is, 2 to 3 per cent voltage variation) is only slightly amoying if not too frequent.

Thus unsteadiness or flickering of the light is only objectionable, and inefficiency is due to continuous low voltage; but aside from this, there usually is little difficulty in maintaining good regulation. The free lamp renewal, practiced by the more progressive lighting companies, is a strong inducement to the company to maintain good regulation, as the life of the lamps decreases and the cost of renewal to the station therefore increases with poor voltage regulation.

More unsatisfactory is the situation regarding reliability, that is, continuity of electricity supply, as the meaning of "reliability" is very vague. For instance, a big metropolitan system claims as evidence of reliability that the power has not been off the busbars of
their station for 18 years, while a transmission system claimed as evidence of reliability operation with not more than 1:3 shut downs, cacl for a few minutes, during one year.

It would therefore be very desirable if some authoritative body, such as the National Burean of Standards, would take up the definition of reliability of service, so as to assure that when speaking of reliability (lifferent people mean the same thing.

Obviously, the reliability of operation should be as high as possible. There are limits, however, beyond which the further increase of reliability results in a considerable increase of the cost of electricity by the required reserve plant and the question arises, whether, when and how far the increase of relialility justifies the cost. In a metropolitan city, with thousands of elevators full of people liable to be left hanging between floors by the failure of the electric power, with hundreds of crowded assembly places plunged in darkness with the danger of a panic, the highest reliability of electric service is worth far more than in a smaller municipality, where an occasional short shut down means merely an annoyance to the customers. Thus in the latter case, a few shut downs during the year, of short duration, would be justified, if their elimination or reduction would materially increase the cost of service. Thus it is an economic question, depending on local conditions how far increase of reliability is justified. This obviously assumes that the reliability has already by careful management and supervision been carried as high as possible with the existing plant.

The standard system of distribution for electric light, power and other domestic service, which we find in most municipalities, is an overhead 2300 -volt (approximately) primary distribution to transformers located on the poles, reducing to the secondary threewire distribution system of $115 / 230$ volts. Here 115 volts represents anything between 105 and 130 volts, and 2300 volts the voltage corresponding thereto.

Occasionally three such 2300 -volt primary circuits are combined by having a common return wire, which often is grounded. By making the three circuits of three phases, the common return carries little or no current. This gives the four-wire, three-phase primary distribution, with 2300 volts between outside wires and neutral, and therefore $2300 \times \sqrt{3}=$ 4000 volts between outside wires. It is often called 4000 -volt primary distribution. Its advantage is that a much larger territory
(about three times as large) can be covered from the same station and it therefore finds increasing use in large cities and in extended but sparsely populated territories by reaching more customers from the same substation.

Of bearing on the question whether or what limit should be placed on the voltage permissible in overhead lines in municipa!ities are the primary distribution voltages of 6600 and 13,200 which are being used with increasing frequency in some localities, because it is not economically possible to take a small amount of power from a high voltage transmission line of 60,000 volts and over. The smallest size of wire which can be safely used mechanically in a transformer carries a current which at high transmission voltages represents considerable power and a transformer for less power than this would be practically as large and expensive. Furthermore circuit breakers and lightning protective devices cost almost the same for a small as for a large substation. Thus there is a minimum power below which a substation from a high voltage transmission line is uneconomical. In many cases this power is materially larger than can be distributed at 2300 volts or even at 4000 volts from one substation. Thus either a higher primary distribution voltage is necessary to make it economically feasible to tap a high voltage transmission line or a double transformation and use of an intermediate voltage circuit. The additional losses and the additional cost usually make the latter uneconomical leaving no alternative but the higher primary distribution voltage. This has led to the introduction of 6600 and 13,200 volts as primary distribution voltages in those cases which cannot be economically developed by the lower primary distribution roltages and so justifies their use.

Industrial power supply due to the large bulk power demanded by a single customer also often requires voltage higher than 2300 .

A similar situation arises when changing from a local isolated electric generating plant to a substation of a territorial system. Economically, the substation should be near the center of distribution, that is well within the municipality. But it must be reached by the high voltage transmission line and this
immediately rases the question of the transit of the high voltage transmission lime thromph the municipality. The afternative is at additional substation at the city limits with an intermediate voltage kating from there to the substation in the distribution conter. This means increased cost and dereased efficiency, that is higher pries of electric service.

It seems to follow herefrom that it is economically undesirable to limit the woltage which can be carried through municipalities on overhead lines; that any voltage, no matter how high, must be permitted prorided that the line is designed and built properly and safely for the voltages which it carries. This seems reasonable because a 220,000 -volt transmission line, properly designed and built, is no more dangerous than a $2: 300$-volt line: rather less because contact with the latter kills just as quickly as contact with the former but the chances of coming in contact with the latter are materially greater.

The position recommended here to set no voltage limit but permit overhead lines of any voltage provided they are safely designed and constructed, thongh apparently demanded by industrial progress, has become possible only he the work of the National Bureau of Standards in giving the municipal electrician a definite code and specification of line construction for different voltages.

As regards the question of underground cable versus overhead line: The underground cable is much more expensive than the overhead line, thus increases the cost and thereby more or less indirectly the price of electricity supply. This increase is little where the density of demand is tory great as in the center of the city and the better appearance of the strect then may justify underground distribution. Often by proper city planning the overhead lines or most of them can be kept away from the main streets and located inconspicuously in alleys, ctc., especially in newly developed parts of the city.

To conclude, then, the preceding are genera! considerations which apply generally but in individual cases modification may be necessary for various reasms.

# Protection for Alternating-current Motors 

By 13. WV. JONES<br>


#### Abstract

(imol whimering has atwas dictated that more study and hess guesswork shouh govern the determinafom of the size of motor for a given drive in order that the motor selected be no larger than necessary. Presont emonomic conditons emphasize this policy. As a conseguence, the protection of such a motor is of more importame than formerly. The following artide describes protective devices for multi-phase motors of the imfuction and syndmonous types. Voblor.


There are thee operat ing conditions against which a multi-phase induction or symehronous motor should be protected.
A. Oerloal current, which may result from (oo) heaver a loat on the motor or from abnomal voltage on the power lines.


Fig. 1. Temperature Overload Relay. This shows the relay in the tripped position. For normal running the control cont acts are closed
B. Single-phase power, which may exist when attempting to start the motor or after the motor has started.
(.. Phase reversal, which will cause the motor to rotate in the opposite direction to that intended.

## Protection against Condition A

The device which best protects against overloads is a temperature overload relay. Heretofore, overload relays have usually been of the solenoid type, retarded by some form of dashpot or bellows. The current-time curve of these solenoid relays is similar in shape to that of the current-time curve of an alter-nating-current motor, but generally the relay curve is far below it; i.e., the relay will trip long hefore it is necessary: Also, this type of relay never can take into account the previous history of the load on the motor. The overload may occur white the motor is cold or it may oceur after a long run at rated load, and yet it will require the same time to trip
with the same degree of overload under citherof these two conditions.

Temperature overload relays, one form of which is shown in Fig. 1, will replace the dashpot types on control equipments because the characteristics of the temperature relay correspond very closely to the heating characteristies of the motor. Tests have shown that, if overloads varying from 10 to 500 per cent current are put on the motor, the relay will disconnect the motor from the line when the motor temperature reaches approximately its rater value. This will take place if the overload is put on either a hot or a cold motor.

From a mechanical standpoint, the relay is made to meet the requirements that the average industrial plant requires.

From an application standpoint, the relay is made so that the current at which it will trip can be adjusted over a range of 80 to 120 per cent of its rating. The relay will carry continuously the 120 per cent value.

From the standpoint of its thermal characteristics relative to that of the motor, the


Fig. 2. Open-phase and Phase-reversal Relay with the Steel Yoke and Copper Disc removed to show the construction of che relay
relay very closely approximates that of the motor.

In order that the name "Temperature Overload Relay" may not become meaningless by applying it to a multitude of
devices that possess only a small thermal capacity, it is hoped that steps will be taken to outline some reppirements which a device of this general character must possess before it can be correctly called a "Pemperature Overload Relay."

When these relays are calibrated in the factory they are placed in a room having an ambient temperature of 40 deg . C. and the current values applied until constant conditions exist. In this way the relay is adjusted so that it will (rip) at its indicated
 is greatly redued due 10 the armature om rotating and it will therefore reath a daneerous temperature An (pen-platse relay will give the reguired protection.

Single-phase induction relays and als, multi-phase induction relays have leen built for years. The single-phase relay produces its rotation ly a split-phase action in each magnetic pole by means of a pole-shader, and the multi-p, hase relay produces its rotation by the rotation of a mas.


Fig. 3. The Open-phase and Phase-reversal and the Temperature Overload Relays are shown mounted in an enclosing case to be used as a unit to give full protection to the motor. The tips of both relays are normally closed and connected in series
value in an ambient temperature of 40 deg. C., but at a greater or less current value if the relay is in a lower or higher ambient temperature. Thus the relay is fully able under all ambient temperatures to protect the motor against overloads while the motor is rumning.

## Protection against Conditions B and C

There is one condition against which an overload relay can never protect, and that is when single-phase power is applied to a motor when stationary and the current taken by the motor is about its full-load rating or less. Single-phase power can never start


Fig. 4. The Same Panel as illustrated in Fig. 3. The temperature overload relay has been removed to show its method of mounting
netic field from pole to pole similar to any induction motor.

By making a combination of a single-phase and a multi-phase relay and so comnecting it that the two rotations oppose each other, we have the basis of an open-phase, phasefailure, and phase-reversal relay. If the multi-phase action predominates, the rotating member comes up adrainst a stop and, even when power is removed, will remain there. If series coils are used and one phase to the motor opens, the three-phase rotation ceases but single-phase power continues and will produce the single-phase rotation of the relay in the opposite dircction and cause a latch to be tripped.

The foregoing features may be observed in Fig. 2 which illustrates the relay with its
steel yoke and copper dise remosed. The relay has fome polks and four series coils. Each probe has a pole-shander and is so placed as to prowluce at torque in the copper dise in a counter-clockwise direction. The steed cross, located as shown in ligy :3, also acts as a pote-shader to give a torgue in the same direction as each sladed pole piece and the two develops quite a respectable torque. With single-phase power these forces cause the dise to rotate counter-clockwise and trip) the contact, which is a toggle arrangement.

When multi-phase power is applied, the single-phase torque remains, but there is added a worque produced by the revolving field and this can be in either direction, depending upon the connections. For normal operation these two torques should oppose each other, with the rotating torque predominating. This will bring the copper dise against a stop and produce no further result. Therefore nothing happens when multiphase power is applied or removed; but, should any phase open, then only singlephase power remains and the relay will immediately trip. The relay requires about 60 per cent of its continuous coil rating to trip. This means that if the motor, when
rumning with an open phase requires less than (i) per cent of its rated current, the relay will not 1 rip, but very few laads will allow the motor to draw less than this amount of current and if so no harm can ever result. It is also very apparent that if phase reversal oceurs the relay will trip.

For clevator and hoist service a phase reversal relay is required to protect against a phase reversal condition and against starting the motor if only single-phase power is on the line. Also if a phase fails while the motor is running the relay should not stop the motor because the cage should reach a landing. The relay just described will accomplish these results if shunt instead of series coils are used. However, since this service can be obtained with a smaller and cheaper device this relay is used primarily for the service which it alone can accomplish.

## Combined Protection

The panel shown in Figs. 3 and 4 has been designed to include both the temperature overload and open-phase relays. This combination protects multi-phase alternating-current motors against the three conditions mentioned at the beginning of this article.

## Equations of the Magnetic Circuit

By Frank M. Gentry

Variable permeabilities in magnctic cireuits are troublesome to handle mathematically and we believe that the formula derived by the author should save much time and trouble in ealculating magnetie eireuits involving variable permeabilities.-Editor.

The solution of problems in magnetic circuits involving variable permeabilities, while not a difficult task, is probably one of the most umpleasant in electrical engineering. The present system of solving such problems is the simple but haborious method of trial and error and even then the answers obtained are not of the highest order of precision. While it is admitted that accuracies beyond about three per cent are not desired because of the uncertainties arising from magnetic leakage, it is also generally admitted that the present method of solution is far from being satisfactory and is tolerated only because there is no other simple way of attacking the situation.

The author has been able to derive some empirical equations capable of giving a direct solution to the simple magnetic circuits and, while they are long and formidable looking, yet it has been found that they are quicker to use and give a more accurate result than ordinarily found by trial and error.

The general equation for the flux in any magnetic path is:

$$
\begin{aligned}
& \text { ic path is: } \frac{\frac{4 \pi}{10}(N I)}{\phi=\frac{l_{1}}{\frac{l_{1}}{u_{1} A_{1}}+\ldots \ldots \frac{l_{n}}{u_{2} A_{n} A_{2}}}+\ldots \ldots}{ }^{2}
\end{aligned}
$$

where ( $N I$ ) is the total ampere turns acting, and $l_{n} . u_{n}$ and $A_{n}$ are the length, permeability, and area respectively of the $n^{\text {th }}$ region of the magnetic path. Let us obtain first the equation of a simple annular magnetic circuit consisting of a ferromagnetic material of constant area of cross-section and an air gap. In this case then,

$$
\phi=\frac{0.4 \pi(N I) A}{l_{g}+\frac{l_{s}}{u_{s}}}
$$

since the permeability of air is unity and only slight error is introduced by assuming that the area of the air gap jo equal to the area of the material.

Froclich has shown that the relnetivity of a ferromagnetie substance is essent ially a lincar function of the magnetising fore . Therefore we may write.

$$
\frac{1}{u_{s}}=a\binom{(N /)_{s}}{l_{s}}+b
$$

where $a$ and $b$ are constants depending solely upon the nature of the material.

Now it is evident that the magnetomotive foree required to maintain a given flux is the sum of the magnetomotive forees required to maintain that llux in the various regions, so that.

$$
(\aleph I)=(N /)_{g}+(\aleph /)_{s}
$$

where $(N I)_{g}$ is the ampere turns required for the air gap and $(N /)$, the number required for the rest of the eircuit. Hence,

$$
(N I)_{s}=(X I)-(X I)_{g}=(\Lambda I)-\frac{0.313: 3\rangle \phi l_{g}}{u_{g} A}
$$

and therefore.

$$
(N I)_{\mathrm{s}}=(N I)-\frac{0.313: 3 \phi l_{g}}{A}
$$

since $u_{g}=1$. Combining this with the foregoing equation, we have,

$$
\frac{1}{u_{s}}=\frac{a\left[(N I) A-.31333 \phi l_{g}\right]+A l_{s} b}{A l_{s}}
$$

and upon further substitution,

$$
\phi=\frac{3.193(N I) A}{l_{g}+l_{s}\left\{\begin{array}{c}
a\left[A(N I)-.3133 \phi l_{g}\right]+A l_{s} b \\
A l_{s}
\end{array}\right\}}
$$

which reduces to the quadratic equation,
$\phi^{2}\left[.3133 a l_{s} l_{g}\right]-\phi\left[A l_{s} l_{g}+(N I) A a l_{s}+A b l_{s}{ }^{2}\right]-$

$$
3.193\left(\Upsilon^{5} I\right) A^{2} l_{s}=0
$$

Solving for the ampere turns, we obtain,

$$
(N I)=\frac{\phi\left(.3133 \phi l_{g} a-A l_{s} b-A l_{g}\right)}{\phi a . A-3.193 A^{2}}
$$

and solving for the flux, we find,

$$
\begin{gathered}
\phi=A\left[l_{g}+(N I) a+b l_{s}\right]- \\
\frac{\sqrt{\left[A\left(l_{s}+(N I) a+b l_{s}\right)\right]^{2}-4 A^{2}(N I) a l_{g}}}{0.6266 a l_{g}}
\end{gathered}
$$

Table I gives the values of the constants $a$ and $b$ in the above equations for various materials as determined from the mean of several measurements.

TA1siE1

N:1t.1...

| ( as ( iroll | .1006) S.On | 1112:? ${ }^{\text {a }}$ |
| :---: | :---: | :---: |
| ( 'itst stmel (soft) |  | .1110031 |
| Annealer) sterl (sheret) | . 110100$)^{2} 70$ | (0)002: |
| Cobait (soft) | . 11 (1) (1) $6: 3$ | (10):30) |
| Nickel (09 per cent | .000) $0.5 \pm 1$ | (0)116 |

Placing $l_{g}=0$ in the first formalat, we , whath the equations for a simple masuetio circuit withont an air gap,

$$
(N /)=\begin{gathered}
-\phi l . b \\
\phi u-3.193 .1
\end{gathered} \text { and } \phi=\frac{3.193 .1(X /)}{(X /) a+l . b}
$$

By generalizing the derisation. it has leen found that for a simple magnetie circuit made up of a single substance but with two regions of different length and area.

$$
(\Lambda \rho)=\begin{gathered}
0.313: 3 \phi^{2} a\left(l_{1}+l_{2}\right)-\phi b\left(l_{1} \cdot A_{2}+l_{2} \cdot h_{1}\right) \\
\phi a\left(A_{1}+l_{2}\right)-3.193, A_{1} A_{2}
\end{gathered}
$$

and for the case of two regions of different ferromagnetic substances of equal areas.

$$
(N T)=\frac{0.3133 \phi^{2}\left(a_{1} l_{2}+a_{2} l_{1}\right)-\phi A\left(l_{1} l_{1}+l_{2} b_{2}\right)}{\phi \cdot A\left(a_{1}+a_{2}\right)-3.193 .4^{2}}
$$

and finally for the general case of 1 wor regions with different permeabilities, lengths and areas,
$(N I)=\begin{gathered}0.313: 3 \phi^{2}\left(a_{1} l_{2}+a_{2} l_{1}\right)-\phi\left(l_{1} A_{2} h_{1}+l_{2} \cdot 1_{2} h_{2}\right) \\ \phi\left(a_{1} \cdot A_{2}+a_{2} \cdot h_{1}\right)-3.193 . A_{1} A_{2}\end{gathered}$
These equations are valid only for magnetising forces between ten and two hundred ampere turns per inch because the assumption of a linear reluctivity holds only for that interval. Luekily, however, the values most common in practice fall within these limits. Unfortunately no terms in the above formula ean be neglected because they are usually of the same order. English units are to be usech.

As an example of the application of these formula to problems in the magnetic circuit, if the first equation be applied to problem 31 on page 14.5 of "Hudson's Engineering Electricity," it will be found that the answer works out correcty to less than one and a quarter per cent.

# Gauges 

13y (i. ( C RHILEY




#### Abstract

It is almost superllums to state how important accurate ganges are 10 modern manufacturing operations. Ife are fortanate in having an article from "a man in the shop" who has built up a gatuge system that works su satisfactorily. Mr. Reilley tells his story in his own way and we believe his contribution will be of great valte to others responsible for similar work. After some historical notes he tells about the types of gatges maded and the methods of using them. Fidtor.


All industrial concerns are endeavoring to ohtain two results that are rather difficult to accomplish; i.e., cheaper production and preater acouracy in the manufactured units that go to make up the finished articke. This not only requires modern machine tools and small tool equipment, but a complete gauge system. Is a matter of fact, gauges are the vital part of modern accurate and satisfactory manufacturing methods, the essential results being the ability, not only to work to extremely close limits where necessary, but to be able to duplicate absolutely the various parts at different intervals. sometimes after the lapse of years. In order to accomplish this, it is necessary that a comprehensive gauge system be established, the gauges must be of the utmost refinement, and a method followed to insure the gauges being always in proper condition.

As the mechanical arts advanced and industries were developed for producing machinery for various purposes, naturally the tools used in their production advanced accordingly; not only cutting tools, but measuring tools such as micrometers, verniers, etc. The making of this machinery created complexities that had to be overcome, especially the duplication of parts.

The difficulty of the different interests agreeing on a standard is illustrated by the different standards of serew threads. The Whitworth Standard was accepted in England as long ago as 1841 . This, however, not being metric is not in use on the continent of Europe. The Seller's Standard was introduced in the United States in 1864 and is known as the U. S. Standard, above $1 / 4$ inch. In all countries there are cight threads that have been standardized, out of sixty systematized.

The weights and measures in common use in this country at the time of the Revolution were of English origin, and were in use in England at that time. The principal units were the yard, the avoirdupois pound, the gallon and the bushel. In 1790, a committee of the House of Representatives were requested to prepare a bill for a proper plan
for establishing uniformity in weights and measures, the English standards never having been allopted by the government, but they were being used on account of our not having a standard of our own.

While Congress had been considering the matter, most of the states had independently of each other secured and adopted standards. Standards of the same denominations differed widely, thus causing confusion in the commerce between adjacent states.

In 1828 an act of Congress made the troy pound the standard for coinage. This is the standard from which the avoirdupois pound in common use is derived. The Treasury Department finally adopted a standard, I think in 1830, making the yard 36 inches, the avoirdupois pound 7000 grains, the gallon 231 cubic inches, and the bushel 21.50 cubic inches approximately. The 36 inches adopted for the yard was the distance between the 27 th and 63 rd inches of an 82 -inch brass bar prepared for the coast survey in London. This bar had been brought to America in 1813 , and the 36 -inch space referred to was supposed to be identical with the English standard at 62 deg. F.

In 1866 Congress passed an act legalizing the metric system of weights and measures in the United States. This, however, has never been put into effect $u p$ to the present time.

How the yard measure originated in England in the first place, I am unable to say. The French, however, had a definite reason for the metric system. For example, the meter, which is the measurement of length, equals one ten-millionth part of a meridian quadrant of the earth This in English measure equals 39.37 inches.

One tenth of a meter in cube form filled with water equals one liter, which is equivalent to approximately one of our quarts.

While one tenth meter, or decimeter, in cube form equals one liter in capacity, it also equals one kilogram in weight, which is approximately 2.2 pounds. So the meter has a direct relation to length, capacity, and weight.

Having these standards, looth English and metric to start with, it is then a question of making dupdicates and subdivisions thereof to work from in mantufacturing and commercial pursuits. The gard is suldivided into feet. inches and fractions thereof
the walls of rement binck is mon lhak sen that there is absolutely mon onmtuma: * outside atmospherie comdtions wathed ifor temperature in this rown

All of the master gatuges of the diffoment types are kept in this rom. Fixs 1 and 2 Therefore, in order to have interchangeability and duplication of all parts made to the same nominal dimension. it is necessary to have tools and gauges of proven accurace for use in faloricating the manufactured parts.

In the early stages of machine building, where only a few parts of one kind were made at a time, and each part fitted to the machine or instrument for which it was intended, and made by the same firm, this was not so important Under the present-day conditions, however, where enormous quantities of different articles are constructed and component parts


Fig. 2. Another View of Constant Temperature Room of Standards made at different places, it is absolutely necessary to have ways and means of being sure that all parts are duplicates, and therefore interchangeable.

To accomplish this, gauges recognized for their accuracy by the Cnited States Bureau of Standards, and also the different foreign countries (where the firms do an international business) must be used as master or reference


Fig. 1. Constant Temperature Room of Standards
gauges, duplicates of these gauges to be used as working and checking gauges. This requires a department where the master gauges are kept under the proper temperature. For this purpose we have built a room 21 by 21 feet in the middle of a concrete building with

In addition we have a room 20 by 2.5 feet where are maintained the reference gauges that are used for checking the working gauges. Fig. 3.

The end measuring standards used by the Schenectady Works of the General Electric Company are the Johansson gauges. The set we have consists of 117 pieces, and has a range from 0.0200. inch to 20 inches. This set will give hundreds of thousands of combinations. See Fig. 4.

These gauges are rectangular pieces of Swedish tool steel, hardened, ground and lapped. They stwe four universally recognized mechanical and metallurgical problems; i.e., flat surfaces, paralle] surfaces, and effective heat treatment and seasoning. To make flat surfaces in steel is difficult. Parallel surfaces in steel are also recogmized as a problem in mechanics. Accuracy in producing flat surfaces that are parallel to each other adds to the problem of having these flat and parallel surfaces a distance alart equal to the size which ther represent. These blocks are heat treated and seasoned so that the molecules of the steel are clamed 10 be at rest. Because of this fact, the usual warping and growing of the metal is checked, and when motion is produced by temperature

- langes, the ster not muly expands and contracts miformly, but returns to its normal size.
by using: these hooke in combination with a measuring matchine with a (atpacity tup (o) (o) inches we ato able in produce gatages wi almost ang length within extremely close


Fig. 3. Gauge Inspecting Room
limits. When Mr. Johansson first described his gauges and said ther were within one hundred thousandths of being correct, most people doubted this statement, and those that did not still said there was no occasion for such refinement, while as a matter of fact, it is absolutely necessary that they are within one hundred thousandths of being correct. As an example, when we are required to make a gauge of considerable length, it is sometimes necessary to build up a number of the Johansson blocks in order to obtain the size required. If this occasions the use of thirty of the Johansson blocks, for example, and there was a variation of one hundred thousandths in each block, this would make an accumulated error of three ten thousandths, whiclı would be absolutely out of the question, as at the present time in our Commutator Department there is an allowance of only fire ten thousandths $(0.0005)$ inch between the diameter of the bore of the commutator and the shaft. There is no tolerance to this dimension, as it is necessary that the shaft be five ten thousandths ( 0.0005 ) inch larger than the bore in order to obtain the proper pressure fit. Therefore, if there was an error of three ten thousandths in the gauges used for this work, the proper pressure would not be obtained, and consequently the work would not pass inspection.

11 is very difficult $(6$ conceive what one humbed thousandth really means. Some statistician has figured that if an inch was divided into one homdred thousand parts in the form of playing cards, it would take a person wer seven hours to deal these cards at the ordinary rate, that is about four a second.

In addition to the Johansson gauges, we have a Van Keuren Light Wave Measuring Outfit. This equipment consists of a set of optical glass flats and a source of monochromatic light.

An "Optical Flat" differs from a lens in that it has no magnifying power; but its utility consists solely in that it is a very accurate transparent flat test surface. The "Working Flats," 2 inches in diameter by $5 / 8$ inch in thickness, each have one surface accurately flat. within five millionths of an inch. Only one of these is required for flatness tests, and the two suffice for length measurements or comparisons.
One " Master Flat," $23 / 4$ inches in diameter by ' $\delta$ inch in thickness with one surface accurately flat, within $21 / 2$ millionths of an inch serves to complete the set of optical flats. Thus the two working flats and the master can be proven absolutely by testing them against each other, employing the familiar principle that three surfaces fitting together in all combinations establish or originate flat surfaces. The master flat in addition to its value for reference purposes can be used on larger work than the working flats.

The monochromatic light set is a most practical outfit specially designed for every


Fig. 4. Johansson Gauges in Constant Temperature Room of Standards
day use. It consists of a conveniently constructed, nicely finished oak box. provided with a tungsten filament lamp and a special selenium diffusing glass. This selenium diffusing glass cuts out all of the violet. blue,
green, yelhow and orange wares; and transmits only a very definite red wave of known length, resulting in an equivalent measuring unit of eight dark interference bands to the ten thousandths of an inch or 12.5 millionth. per hand. It can be attached immediately to an alternating or (lirect current lamp) socket.

Interierence bands, or alternate light and dark spaces, can be seen in monochromatic light when an optical flat is placed upon a nearly flat lapped or polished reflecting surface. The illustration, see Fig. 5, shows the character of these interference bands which tell the whole story.

An examination of the bands occurring due to the interference of the light reflected from the upper surface of the two gauge blocks which are wrung on a lower glass flat, with the light reflected from the contacting surface of the upper flat reveals the following facts:

1. The pronounced light space near the observer on each gauge indicates the point of contact.
$\because$. The upper flat is sloping upward toward the rear at the rate of 12.5 millionths of an inch per dark band. At the rear of the right hand gauge there is, therefore, an air space of 5 times 12.5 millionths or $(62.5$ millionths
2. The bands on each gauge curve about 210 of the distance between them, and the center of curvature is on the same side of the bands as the point of contact, thus indicating a convex surface with edges lower than the center by 0.2 times 12.5 millionths or 2.5 millionths.
3. The bands on the left hand gauge occur about $1 / 2$ band lower down on the wedge than those on the right hand gauge, indicating that the left hand gauge is shorter by $1 / 2$ unit or a little more than 6 millionths of an inch.
4. The bands on both gauges although slightly curved are practically parallel. indicating that the upper surfaces of the two gauges, as they are wrung on the lower flat, are parallel within one or two millionths of an inch.

With our present system all manufacturing departments are furnished with necessary gauges pertaining to their class of work. This insures accurate and absolute interchangeability. These gauges are numbered serially. and assigned to the different departmental gauge rooms, where they are given to the workmen. All gauges in use in the factory
 room at keast once a wokk for recalifnatwon,
 week without being chacken)

The acentacy of these gratere is of exterme importance as some of the work is of the


Fig. 5. Interference Bands on Two Flat Gauge Blocks That Are Being Compared for Length and Parallelism
greatest refinement. A case in point is the making of gears for the turbine gear reduction sets for the destroyers for the United States Government. Some of these gears were as large as $i \underline{2}$ inches in diameter, and the gear cutters used for cutting the teeth were made in hob form of the greatest accuracy: These hobs were made of high speed steel and ground all over. On account of the size of these gears, and the accuracy desired, a "snap gauge" or "outside gauge" could not be used for finishing, and we therefore decided to use a steel tape. This tape was ${ }^{3}$ s inch wide by 0.00 inch thick, and was made to the exact length represented by the circumference of the gear. As the pitch line of the gear was determined from the outside diameter, it was necessary that this be of the greatest possible accuracy. due to the fact that the engineers would only allow an accumulative error of three thousandths in the total periphery of the gear after the teeth had been cut. As the 7 -2inch gear had 2 an teeth, this was only a permissible error of approximately one hundred thousandth of an inch between the pitch of the tecth.
＇The kegth of the tape is whtamed in a machine（kesigned sperially for the purpose

First．（ Once end of the sted tipe is inserted in the stot in ckamping block amel elamperl． sco pig． 6. ＇The tape is then passed arombl the stationary head and around the movable

In each instance the thickness of the tape （0．00s inch）mast be eonsidered fate of the diameter of the fit．This thickness，namely， 0．00）inch，equals 0．0．2．）$: 32$ inch in circumfer－ conce，and for the sake of convenionce after the ciremmference of the diameter has been


Fig．6．Tape Measuring Machine
head back to a shot in clamping block ancl hutted to its opposite end．A tension of four pounds is used to straighten out the tape． A pin gauge of the desired length is inserted between the two heads and should check with the desired length of tape when eal－ culated according to the following formula ． Sce Figs 7．S and ！


Fig．7．Position Without Tape


Fig．8．Developed Length of Tape


Fig．9．Length of Pin Gauge
In Fig．7．${ }^{1} \underset{2}{ }$ dia．$\times \boldsymbol{2} \times \pi+($ radius $\times 4)$ $=24.0000^{2}$ inches．

In Fig．S， 24.00002 inches $+0.02 .5132+$ （pin gauge $\times 2$ ）$=$ developed length of tape．

In Fig．9，length of pin gauge

$$
=\text { developed length of tape }-\frac{24.02 .51 .52}{2}
$$

，otained this is added；for example，the actual circumference of 50 inches is 1.57 .0796 ， and with the thickness of the tape added it makes the actual length of the tape 1．57．104．：32 inches．

As a great number of our generators are direct driven by engines or waterwheels made by outside manufacturers both in the Uniter States and abroad，it is necessary to send gauges to these different manufacturers for finishing the shafts upon which our gencrators are mounted，and as the generator spider must go on these shafts at a definite pressure the gauges naturally must be absolutely correct．In the past year we shipper hundreds of gauges to outside builders，a large percentage going to England， France and Switzerland on contracts made by the International General Electric Com－ pany：


Fig．10．Machine for Measuring Thread Gauges Three－wire System

When it is realized that every piece of apparatus made by the General Electric Company can be duplicated at any time，and supply parts furnished or break－downs replaced with full assurance that when the parts are received by the customer they
will fit, the necessity of a comprehensive gauge system can be appreciated.

The gauges which are sent abroad are used on apparatus to be installed in different parts of the world: i.e., in Australia, South Africa, India. ete. I remember a case several years ago. where a Swiss manufacturer made the waterwheels for our generators, of which there were ten in number, all duplicates, of $12.500 \mathrm{~h} . \mathrm{p}$. capacity. These were for a large mining concern in South Africa. These were waterwheel driven generators, and the shaft upon which our rotors were mounted was part of the waterwheel.

We sent the gauges and instructions to the Swiss manufacturers for the making of these shafts and owing to the size there were threc different fits in the armature spiders. The waterwheels were sent to South Africa from Switzerland, and our generators from Schenectady. Therffore the parts to be assembled did not come together until they reached their destination. The respective members fitted perfectly: and the installation proved to be entirely successfui. proving quite conclusively that the gauges exchanged fulfilled all requirements.


Fig. 11. Machine for Checking the Lead of Screw Threads
Our method of determining the accuracy of thread gauges is by what is known as the "Three Wire Method of Measuring Threads. The angle diameter determines the depth of the thread. It is therefore vital to have this angle diameter accurately determined.

The three wire method of measuring threads is the best. Two wires are placed in the threads on one side, close enough toget her
so that they with he cancrad ho • 4 an of and measuring machine, while the hom am
 the two wires. The mathime meature the distance betwern the ont side diame ers of the wires and gives accurate resulta Dofinite diameters of wires are hed for the warmons phtehes. These wires are arenta", willim


In addition (o) measuring the whe vile and angle diameters of all thread sansw. We alow determine the lead or pitch, whan andicator that rexisters within 10.0001 inch. Sw Fif. 11.

We have complete sets of thread gature ion wherkine the working saures Fiz lo and alon


Fig. 12. Cabine: of Reference Thread Gauges
master seth of rauges a be sute rat checkinge gauges are always correct

The number of new saure mate for use in the factory duming the yar amounts to approximately $3: 301$. In addition io this we forward to ontside waterwhee and engine brilders about 1200 sauges yearly: We inspect. on an average, fon sauses each working daw

# High-voltage Thermionic Rectifiers 

<br>


#### Abstract

  applich beqwern the phate and filament of the there-edement tule. At lower powers the high-voltage direct  ohtamahe from such machans, howere it has been necessary w dewopother means for obtaining this supply. The kenoten rectitior has been developed primarily for this purpose in connection with radio telephone and  


Nearly twodecahesage the vacumm tale was first observed topossess the property of a comverter oi direct-current to alternating-current power. This discovery was made with a gascontent receiving tube operat ing with 20 to 40 Solts on the plate and probably delivering less than a milli-watt of alternating-current power. Development of this new converter progressed; and setcral years ago a high-vacuum tube was built wo deliver 2.50 watts of alternatingcurrent power, receiving direct current from a -, (000)-volt generator.

Further increase in power output is made possible by increasing the size of the tube or by operating it at a higher voltage. The latter alternative is preferable as it is in the direction of higher efficiency. Accordingly, a tube was developed to convert onc kilowatt of alternat-ing-current power from a direct-current source of 10,000 volts. Subsequent development has increased the capacity a hundred-fold with an accompanving increase in operating voltage to 15,000 . The development in high-voltage direct-current generators has followed the development of the vacuum tube, but has been less intensive.

Paralleling the development of the vacum tube as a direct-current alternating-current power converter is the development of the vacuum tube as a rectifier or converter of alternating-current power to direct-current power. For every pliotron, or direct-current / alternating-current converter, there is a corresponding kenotron, or alternating-current/ direct-current rectifier, differing in construction only by the removal of the grid or control element. The maximum operating voltage of any particular type of pliotron is determined chiefly by the construction of the tube. Inherent features of operation of the kenotron and pliotron indicate that the kenotron may be operated at a higher voltage than the corresponding pliotron, so that any demand for a new maximum operating voltage. created by development of the new pliotron,
may be met by the use of the corresponding kenotron.

## TYPES OF RECTIFIERS

The usual form of a high-voltage rectifier consists of a suitable step-up transformer and ome or more kenotrons. The rectifier may be single, two, three, or six-phase depending upon the power supply, and in each case the kenotrons may be connected to rectify one or both halves of the alternating-current voltage wave.

In general, full-wave rectifiers are preferable to half-wave rectifiers for the following reasons:
(1) The full-wave rectifier delivers a smoother voltage wave.
(2) The half-wave rectifier operates the step-up transformer with a directcurrent component of flux in the core, with corresponding high iron losses.
(3) The step-up transformer in a halfwave rectifier draws an unsymmetrical current from the line, with large even harmonic components. The accompanying poor regulation is usually objectionable.
(4) In the case of a polyphase rectifier, the resultant even harmonic voltages set up in the line have a phase rotation opposite to that of the fundamental. This is highly objectionable in the case of rotating machinery operating on the line.

The chief advantage of half-wave rectification lies in the smaller number of kenotrons required.

## Single-phase Half-wave Rectifier

Fig. 1A shows diagrammatically a singlephase half-wave rectifier connection, and Fig. 1B the resultant voltage wave with its alter-nating-current and direct-current components. A step-down transformer is used to heat the
filament of the kemotron. When the mexathe tomminat of the rectifier is grommed, as is usually the case in photron circuits. the howroltage winding of this transformer masis be insulated for the full veltage of the step-up transformer to ground. The resistanee $k$ is
 Curves'for Single-phase Half-wave Rectifier

$$
e=E(.637-424 \cos 2 \omega t-.0848
$$

$$
\cos 4 \omega t-.0364 \cos 6 \omega t)
$$



Figs. ${ }^{\circ}$ 2A and 2B. Diagram of Connections and Curves for Single-phase Full-wave Rectifier
for the purpose of regulating the filament temperature. It will be noted that the positive terminal is located at the mid point of the filament winding, instead of on of the filament terminals, because this comnection divides the space-charge current in the kenntron equally between the two leys of the filament. This insures equal temperatures in the two legs. thus increasing the life of the filament.

## Single-phase Full-wave Rectifier

Fig. 2.A shows a single-phase full-ware rectifier connection employing two kenotrons. Fig. 2 B shows the resultant voltage wave with its
 proments It will lx monal that that

 of the tramsemmer is the sallue for the bult


Three phase Half wave Rectifier





Figs. 3A, 3B and 3C. Diagram of Connections and Curves for Three-phase Half wave Rectifier
lines representing the transfomer whage waves. The current wave follows the rectified voltage wate, assuming negligille resistance and reactance in the rectifier. The reason for this lies in the ralue action of the kenotron so that. at any instant, only the kenotron with the highest positive porential on its plate will pass current. Thus, each tube passes current for one third of a cycle. The primary current in the transformer is unsmmmetrical. and in the limiting case of high reactance in the load. assumes the square ware shape shown in Fig. $\therefore \mathrm{C}$. This wave if analyzed is found to have a second harmonic compronent with a magnitude. of sof per cent of the fundamental and a fourth


Figs. 4A and 4B. Diagram of Connections and Curves for Three-phase Full-wave Rectifier

$\left.E_{i}=E 1.827-207 \cos 3 \omega t-.0472 \cos 6 \omega t-.0207 \cos 9 \omega t-.0112 \cos 12 \omega_{t}\right)$ $F_{2}=E\left(.827-.207 \cos \left[300 t+\pi j-.0472 \cos \left[6 \omega \omega^{\prime} t+2 \pi\right]-.0207 \cos \left[3 \omega \omega_{t}+3 \pi\right]\right.\right.$
$=E(.827+207 \cos 5 \omega t-0472 \cos 6 \omega t+.0207 \cos 9 \omega t-0112 \cos 12 \omega t$, $e=E(.827-.0472 \cos 6 \omega t-.0112 \cos 12 \omega t)$ $e_{\text {IPT }}=E\left(.414 \cos 3 \omega_{t}+.0414 \cos 9 \omega_{t}\right)$ Fig. 58
Figs. 5A and 5B. Diagram of Connections and Curves for Three-phase Double-Y Rectifier
harmonic with a magnitude of 2.5 per cent of the fundamental, besides other higher even harmonics of lesser magnitude. As preriously
intieated, these hammines are objectional copecially if the rectifier is a large unit, draning considerable lammonic prower from the linc

It will be noted that Fizs : 3 . shows the filat ments being heated from a there-phase circuit. This is done so that the filament and space(harge currents will add up) equally in all the kenotrons and produce equal filament temperatures. If ath the filaments are lighted from one phase, the phase angle between filament and space-charge current will differ ley 120 dex. in successive tuber, and the sums will not be equal. The resultant unequal filament temperatures shorten the mean filament life. Another method of securing equal filament temperature is to heat the filaments from a single-phase source not synchronous with the three-phase source.

## Three-phase Full-wave Rectifier

Fig. A. shows a three-phase full-wave rectifier and Fig. 4 B the resultant transformer and rectifier voltage waves. The step-up transformer for such a rectifier is wound with mid taps on each of the three phases and these arc joined together to form the negative terminal of the rectifier. It will be noted that the currents drawn from the two sections of each secondary winding are equal and opposite in sign, hence the primary current is symmetrical and contains no even harmonies.

Since each tube passes current only when the voltage on its plate has a higher positive value than on any other plate, it follows that in the three-phase half-wave rectifier each tube passes current for one-third of the cycle, while in the three-phase full-wave rectifier each tube passes current for only one-sixth of a cycle. Thus it follows that three-phase half-wave rectification is preferable to fullwaverectification in that it utilizes the filament


Fig. 6. Diagram of Filter for Suppressing Harmonic Components in the Direct-current Rectified Wave
emission to a much greater extent. On the other hand, full-wave rectification is more decirable on account of its better regulation,
absence of even harmonics in the lime and smaller harmonic components in the rectified voltage wave.

## Three-phase Double-Y Rectifier

The advantages of both full-wave and halfwave polyphase rectifiers may be realized by connecting the high-tension windings of the transformer to form two I's, 1,50 deg. out of phase, as shown in Fig. 5A. Each Y, with it. kenotrons, is a half-wave rectifier delivering voltage waves, $E_{1}$ and $E_{2}$ as shown in Fig. 5B, with the odd multiples of the triple-hamonic component in the two Y's 180 deg. out of phase and the even components in phase. If we connect the neutral points of the two I's through a large reactance, and draw current from the rectifier through the mid-point of the reactance, the odd multiples of the tripleharmonic component will not appear in the rectified voltage wave, since their value is zero at this point but the even-harmonic components will appear. The voltage across the


Fig. 7. Left to right-20-watt 400 -volt Kenotron, 150 -watt 1000 -volt Kenotron, and $2.5-\mathrm{kw}$., 15,000 -volt Kenotron
reactor, or interphase transformer, is the sum of the absolute values of the odd multiples of triple-harmonic frequency voltage due to each Y. The current due to this voltage is the interphase transformer magnetizing current, and circulates through the kenotrons and

Tanshomer windings withont allament in the loarl.

The current wates drawn thonge , we kenotron are nearly spuate, lasting fom ons third of the eycle. Since there are two higho tension windings per phase bassing cument in


Fig. 8. 12.5-kw., 15,000-volt Kenotron, Fig. 9. Water cooled and its parts at left and right

Kenotron; 40 kw ., 15,000 volts
opposite directions, the primary-current wave is symmetrical and contains no cren harmonics. The direct-current component of current delivered by each of the two Y's is one-half of the total direct-current current, so that each tube is required to pass only one-half the maximum value of current required per tube in the ordinary three-phase full-wave rectifier This means that the filament temperature may be lower since less emission is required. and the filament life is accordingty prolonged.

## High-power Rectifiers

The presence of harmonic components in the direct-current rectified wave is frequently undesirable and means are taken to suppress them by using filters such as shown for example in Fig. 6. where $e$ represents the voltage delivered by the rectifier and $\varepsilon_{1}$ is the load voltage due to the filter.

## IN MEMORIAM

Willian Jared (`ard, MWisory Mamager of the Railway Department of the Ceneral Ekedric Company, and for many vears an anthority in the electric railway field, died at his home in New York ('ity on December 12. 192.2, after a fong ithess. Fle was 68 years old and had been connected with the General Electric Company and its predecessor, the Thomson-Houston Company, for 34 years. lhe is survived by his wife and two sons, Harold and William Clark.

He was born in Derby, Comn., on July 20 , 1s.) H , of an old Connecticut family. He left school at the age of $1-1$ years, after two years study at the local high school, and became a clerk in the local post office. In $18 i 9$ he was temporarily appointed postmaster of Birmingham, Conn., and thus became familiar with political conditions to such an extent that he was permanently appointed to the position of postmaster contrary to the recommendations of the Republican political machine then in control. Acting upon the advice of the late William Wallace, pioneer of the are lighting and motor production, and attracted by the possibilities presented by electric traction, Mr. Clark entered the electric field and participated in the commercial expansion of almost every phase of the ThomsonHouston and the General Electric Companies' business throughout the world. In the spring of 1sis he induced the Thomson-Houston Company to purehase the Vandepoele Electric Railway patents, which in his opinion were essential to the fullest development of the industry. He recognized at an early date the value of certain fundamental electrical inventions and was instrumental in bringing these inventions under the control of his Company.

Mr. Clark was a pioneer in the commercial development of electric railways, beginning


WILLIAM JARED CLARK
his connection with this inclustry with a project for the first electrie railway in the world intended for freight traffic. The legislative charter for this line, which was constructed between Derby, his native town, and Ansonia. Conn., was obtained largely through Mr. Clark's efforts.

Shortly after this Mr. Clark, in March, 1s8s, became Railway Sales Agent under General (then Captain) Eugene Griffin, who then was General Manager of the Railway Department of the Thomson-Houston Company. In 1893 he was Manager of the Cincinnati Office for a short time, and took an active interest in the earlier electric railway projects of the middle west. In 1894 he came to Schenectady as General Manager of the Railway Department of the General Electric Company. In this position Mr. Clark played an important part in the commercial exploitation of Sprague's Electric Railway Motor Suspension; Vandepoele's Carbon Commutator Brush; the Pivoted Under-running Trolley; Potter's Series Parallel Control ; Sprague's Multiple Unit Train Control; Curtis Steam Turbine and other inventions. In 1896, he made a valuation of the electric railway and lighting property in Milwaukee. This is said to have been the first extended "Physical Valuation" of a large public utility and the general plan adopted by Mr. Clark has since been frequently followed by other students.

Mr. Clark's next move was the managership of the Foreign Department of the General Electric Company, taking up the duties of this office in 1899.

The universal esteem which was felt toward Mr. Clark by all of the officers of the Company could not be more clearly shown than by quoting the following letter sent out
 Griflin to the entire Cieneral Eleetric oremaization.

In view of the growing volume and importance of our export business, Mr. W, . Clark has been appointed General Manager of the Forejgn Department of the General Electric Company, having been transferred thereto from his present position as General Manager of the Railway Department.

Mr. Clark's connection with this Company dates back to 1888, when he was the first saksman in the Railway Department of the Thomson-Houston Company. Exen before that time he was actively interested in electric railway work. His services have been continuous with the Thomson-Houston Company, from 1888 until that Company was merged into the General Electric Company, and with the latter Company up to the present time. Since $189 t$ he has been General Manager of this important department.

Mr. Clark has been connected longer with electric traction work than any man in the Commercial Department of this or any other electric company in the United States. His indefatigable encrgy. extensive and detailed knowledge of the business, his wide-spread acquaintance with street railway men throughout the United states, and in fact. throughout the world, have gained for him hosts of strong friends, whose good wishes he will take with him from the position he has so long filled with such distinguished abilit $y$, energy, tact and success, to his new field of work, which includes a very large and growing railway business extending over the entire globe.

I know that all the employees of this Company will join with its officers in wishing him, what we all know he will have, every success in his administration of our Foreign business.
lours very truly,
(Signed) Eugene Griffin,

> First Vice-President.

The activities of the General Electric Company at that time were just beginning to take large proportions and Mr. Clark spent a considerable part of his time in Europe and other foreign countries in preparation of facilities for handling foreign business. He was instrumental in reorganizing the British Thomson-Houston Company at the time control was assumed by General Electric interests, and also established the London Office of the General Electric Company:

Mr. Clark's acquaintances among the prominent members of the electrical industry extended to all the capitols of Europe where he was considered an authority on electric railways and electrical manufacturing conditions. In 1908 he was retained as an expert on Cuban affairs for the War Department and made an extensive study of commercial conditions in the Island of Cuba. Acting upon his recommendations, the electrical
 hate simee beerl mathatimed min on
 studies, Mr. (`lark wrote a bomb ammbul  analysis of the situationt, whels is rexachation as an atulhority ont this subjeet  Manager of the Foreign Degartment. . Mr  Manager of the 'raction I opeartment of the Coneral Electric (ompany, when hatl just heen organized to nexotiate for heary steam road etectrification work In this ficle] Nr Clark made many eonfirlential sturlies ate ting directly uncler the instrmetions of Nr. (`. . Coffin, then President of the Company: It this time and since then his hearlquarters have been at the New Vork (oftice of the General Electric Compans.

During practically all of his connection with this industry he has been in close touch with the Federal Government dating back from the time when he was engaged with the Secret Service Branch of the Post Office Department including activities during the Spanish and European wars. The statistics prepared by Mr. Clark covering the corporate relations and interconnections of German Manufacturing Companjes and their allies and subsidiaries in the Cnited States were enormously useful to the Federal Government during the European War. In 192.- the Traction Department was consolidated with the Railway Department at Schenectady and Mr. Clark was given the title of Advisory Manager, which he held at his death.

Mr. Clark throughout his life retained his interest and activity in the Republican political organization, being a member of the National Committee campaigns of $15.00,144$. 1s90, 1904. In 1906 and 1906 he was chairman of the Ways and Means Committee of the National Civic Federation in which connection he financed the extensive investigations then being conducted of municipal ownership in this country and in Europe: He was a member of a large number of National Electrical and Railway Engineering Sucieties including the following:

American Institute of Electrical Engineers
National Electric Light Association
American Electro Chemical Society
New York Electrical Society, and the
American Electric Railway Association.


## LIBRARY SECTION

## Condensed references to some of the more important articles in the

 technical press, as selected by the G-E Main Library, will be listed in this section each month. New books of interest to the industry will also be listed. In special cases, where copy of an article is wanted, which cannot be obtained through regular channels or local libraries, we will suggest other sources on application.Alternators
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## GENERAL

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Fig. 5. Colored Image Obtaned for Normal Inside Pressure and
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Fig. 2. Colored Image when Normal Inside Presscre Alone is


Fig. 3. Colored Image when Both Normal Inside Pressere and
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These illustrations are in connection with an
as Determined by the Photo Elastic Method, using Transparent Celluloid Models. (The Fir numbers are referred to in the text).


## THE CONTROL OF POWER

Mr. Lawrence's article, published in this issue, on the Load Dispatching System of the New York Edison Company should convey to the reader a lesson not actually cited in the text. Forty years ago, as told in our December number, the first Edison station was put into commission. Since that day the power stations built have been legion. They have gradually increased in capacity until today some stations have an installed capacity of over a quarter of a million kilowatts and the individual generating units during this same period have increased from a few kilowatts per unit to the huge Titans of 50,000 kilowatts apiece.

The generation, distribution and control of electric energy has taken an extraordinary amount of scientific and technical knowledge. skill. courage and human energy to bring it to its present perfection.

The public really has no adequate mental conception of what the engineer has done for his country and for civilization by this work. Thirty years ago we pointed with pride to a power station of 2000 kilowatts capacity. Since that time each year has seen an increase in capacity, an extension of the use of electrical energy and an extension of the area covered, until today life in any large city is unthinkable without the distribution of electric energy. Continujty of service from the Public Utility is of more importance to the public than the continuity of any other civic function, yet small appreciation is shown.

A few years ago our small power stations were independent entities serving their own small circles. Today, as Mr. Lawrence describes, many power stations and mumerous substations are interconnected together so that power can be re-routed in case of stress and emergency. The whole system of generating stations can be controlled by one operator from a central point. What this means to the public in the elimination of inconsenient delays is hard to overestimate.

What Mr. Lawrence deariles applies ow one of the largest citics in the world and its enviromments, but there is a seater onneres tion which has more recently hegm ow hear fruit. In many districts we are wrorking wo ward superpower zones where all the gencrating stations, both steam and hylrathle, will have their arteries interomnecterl thagether so that every unit station in this zone can serve any section of the community concord This is a big step in adrance. In the future when these superpower zones themselves have been interconnected we can begin to think that we are really nearing the accomplishment of one of our greatest duties, mamely, on provide the whole country as far as possible with electric energy:

The tying together of these stations and of these zones will entail the comtrol of an almost unthinkable amount of energy and the puttinst into use the machines by the mitlions for both mannfacturing and domestic purposer. The economic life of the country wil! le satiofactory in just such a measure as we dw this work.

The control of such a rast amount of energy would have been impossible a few years ago because in thinking of machines we musi always be mindful of the nature of the machine.

There is nu, greater an mone useful work that the large electrical corporations have done for this country, anl for the world at large, than devising means and ways of controlling these huge amonants of energy efficiently and safely. J. R.H.

# Operating Pilot Board and Load Dispatching System of the New York Edison Company 

By W. H. Lambence<br>


#### Abstract

The anthor describes in considerable detail the load dispatehing pilot board of the New York Edison system. This load dispatehing board enables the whole system, power station, substation, trausmission line, feeders, etc., to be governed from one contral point. It might be described as the master eye of one of the largest and most womderful electric systems in the world.-EDotor.


The load dispatching system, which cent ralizes the control of the operation of the entire system, was inaturater by The New York Elison Company in 190?, shortly after Waterside No. 1, the first of the high-tension alter-nating-current generating stations of the Company, was phaced in service. At that time, the pilot hoard consisted of a drawing board approximately 30 in . by 60 in . on which were indicated all oil switches in the generating stations and sulbstations and the transmission cables. Opened and closed switches and "alive" and "dead" transmission cables were indicated br various colored tags hung on the board.

With the growth of the system, this hoard became inadequate and inefficient. It had been recognized for some time that a pilot board for system operation must function automatically to give instant and correct indications. It should not depend on the human element for the correctness of its indications. Such an automatic board was designed and installed in 1912 in Waterside Station No. 1. The importance of reproducing automatically: before the System Operator, indications of the operation of all oil switches in the generating stations was such that no expense was spared to incorporate on this hoard all the necessar:automatic features. Such automatic indications are extremely valuable during emergencies when the Syistem Operator may see at a glance the existing conditions of the system, the generators which are still connected to the busbars, the feeder switches which have opened and the conncetions which still exist between the various generating stations. From these indications, he is in position. without awaiting reports from generating stations and substations, to act immediately toward the resumption of normal conditions.

The pilot board at the present time is approximately 20 feet long and 9 feet high and is so constructed that it mav be enlarged from time to time to take care of the growth of the system. At the present time, there are represented on the pilot board the four large
generating stations of The New York Edison Company and allied companies: Waterside No. 1, W'aterside No. 2. Sherman Creek, and Hell Gate, the two smallerstations, Kingsbridge and Jersey City; seventy-three substations, and all customers receiving high-tension energy. Fig. 1 shows a general view and Fig. 2 a small section of the pilot board.

The pilot board is mounted on steel framework with hollow metal trimming and consists of several hundred small slate panels, one for each group in the generating stations and one for each substation. The generating stations are indicated on the upper part of the board, the slate panels being arranged horizontally across the pilot board, and the panels representing the substations are mounted vertically on the lower part of the pilot board below the generating stations. The name of each substation is directly above its panel where also is given the total battery capacity of the substation at the one-hour rate. The pilot board as now equipped contains 3302 "bull's eye" telephone lamps and upon the completion of the Hell Gate Station, one half of which is now operating, will contain 3568 lamps.

For each generating station the number of slate panels corresponds to the number of groups of apparatus connected to the station busbars and are numbered correspondingly. A feeder group consists of two oil switches. one for each of the two transmission cables and two selector oil switches which connect the two feeders to either one of two sets of busbars. A generator group consists of the generator oil switch and two selector oil switches which connect the generator to either of the two sets of busbars. The section of buses are separated by white marble panels on which are indicated the bus tie oil switches. On each of the panels, each oil switch of the group, represented is indicated by two "bull's eve" telephone lamps, one red and one green. The lamps indicating the selector switches are placed above and below the group numbers, the ones above indicating the main bus selector switches, the ones below the auxiliary bus


Fig. 1. General View of System Operator's Cffice

selectorswithos. Coard hoders for mombering the apparatus represented are installed on all pancls just above the indicating lamps. The direct transmission cables are represented in :he substations by their respective numbers; bolow each mumber is comnected in parablel ared "bull's eye" lamp and a telephone jack. The group number to which the feeder connects in the generating station is placed just


Fig. 3. View of Distributor showing Multiple Jack Method of Construction at Rear
below the feeder number. The red lamp and telephone jack of each direct feeder are connected to a local circuit operated by a relay which is connected to the secondary of a potential transformer, the primary of which is connected to the feeder cable on the street side of the feeder oil switch at the generating station. So connected, this lamp serves two purposes. First, it indicates when the feeder is "alive" from the generating stations; and second (when not "alive" from the generating stations), it indicates when the feeder is "alive" from substations due to inverted rotary converters, paralleled feeders, or mistakes in switching. Tie cables between substations are represented in the various substations to which they connect by the feeder number below which are red "bull's eye" lamps and telephone jacks. The lamps and jacks of each tie cable are all connected in parallel to one circuit. Connections in substations between direct feeder cables and substation tie cables are indicated by cords which are plugged into the jacks of the cables connected, the cord completing the circuit and lighting the red lamp in each substation to which the tie cable connects.

Lines are drawn on the board to indicate the cables between substations and direct feeder cables which feed more than one substation.

By placing lelow each feeder number the group number to which the feeder connects in the generating station, lines to indicate direct feeders are unnecessary and therefore are omitted. One terminal board is provided for the indicating lamps of each generating station and one for the indicating lamps of all substations, all tamps being permanently connected to their respective terminal boards. Terminal boards are provided for the relay wires, one for each generating station, so that by eross-connecting between the relay terminal board and the indicating lamp terminal board, any relay may be connected to any pair of indicating lamps, thus making it unnecessary at any time to change the wiring or the comnections to the pancls. Current to operate the board is supplied by two $3-\mathrm{kw}$. 30 -volt motor-generator sets (one being reserve) which may be operated from the exciter system, the station lighting system, or from storage batterics. Standard $24-\mathrm{volt}$ telephone lamps and red and green "bull's eye" lamp caps are used throughout.

Special contacts which operate the indicating lamps are installed on the top mechanism of each oil switch in the generating stations. In the Waterside stations, one wire is used between the special contacts of each oil switch and the corresponding indicating lamps on the pilot board, so connected that the green lamp is lighted when the oil switch is open and the red lamp when the switch is closed.

On each end of the board are instrument panels on which the voltmeters and frequency indicators of both systems are mounted. Indicating wattmeters to indicate interchange of energy between generating stations and curve drawing totalizing wattmeters for the two Waterside stations are also provided. On top of the board are totalizing indicating wattmeters indicating the load of each Waterside station.

To receive indications automatically of the operation of switches in the Hell Gate Station, approximately five miles from the pilot board, a 300 -wire cable is used. In the Hell Gate Station these wires terminate in a terminal board where they are cross-connected to the wires leading to the special contacts on the oil switches, one wire being used for each oil switch. The other end of the cable terminates in a terminal board at the pilot board where the wires are cross-connected to polarized relays which operate the red and green lamps on the pilot board. This system is supplied from a $621 / 2$-volt positive and $621 / 2$-volt negative system with neutral and so connected
that negative polarity operates the relays to light the red lamps and positive polarity the green lamps of the corresponding switches at Hell Gate Station. These relays are equipped with auxiliary contacts to give a bell alarm at the pilot board when a syiteh at Hell Gate operates.

A comprehensive system of numbering the transmission cables is employed. Each substation is given a key number of two figures and each generating station a key number of two figures. Each transmission cable is numbered with a number consisting of four figures, the first two figures being the key number of the substation in which the transmission cable terminates, the last two figures being the ker number of the generating station from which the cable originates so that the number of a transmission cable indicates from which generating station the cable originates and at which substation it terminates. Tie cables between substations take the key number of the northerly substation, the last two figures of the number being the key number of tie cables. For instance, the key number of 26th Street substation is 58 , the key numbers of Waterside No. 1 generating station are from 10 to 19 inclusive, and the key numbers of the Hell Gate generating station are from 50 to 59 inclusive. Therefore, feeder number $5 \$ 14$ is a cable from Waterside No. 1 to 26th Street substation and feeder 5856 is from Hell Gate to 26 th Street substation.

To receive indications automatically of the operation of switehes in Sherman Creek Station, approximately ten miles from the pilot board, a distributor system designed and installed by the Western Electric Company is used. See Figs. 3, 4 and 5. Four distributors are installed, two in Sherman Creek Station and two at the pilot board, each pair of distributors taking care of 100 switches and requiring, between Sherman Creek Station and the pilot board, three telephone wires for each 100 switches.

The distributor consists of a fibre disc to the face of which are mounted three sets of insulated segments and corresponding collector rings. The outer and inner rings of these segments are used for the switch indications and the inner ring to keep the distributors in synchronism.

As the circumference of the outer ring is twice that of the inner ring, every other segment of the outer ring is used, there being 50 switches connected to each ring of segments.

All segments and collector rings are traversed by a set of brushes mounted on brush
arms and revolved at approximate of $\quad$ om through a friction clutch and and arran anem of gears. The power to drive the bun onn
 current motor. The speed of this motor is controlled by a centrifugal wovernos which may be aljusted during operation.

The distributors are used in pairs, one located in the Sherman Creck Station, the


Fig. 4. View of the ${ }^{-}$Cabinet showing the Two Distributors and Space for the Reserve
other at the pilot board. They are connected one to the other by three telephone lines, two of which are used to transmit the switeh indications and one to keep the distributors in synchronism. See Fig. 6. Each distributor is a complete unit in itself, all comnections being made by the muttiple jack method of connection so that to change a distributor all that is necessary is to pull it out and push another one in place. A reserve distributor is carried at Sherman Creek and at the pilot board.

The serments of the distributors at Sherthan (reek are conneeter to the special eontacts on the oil switches, one wire being tased for each oil switely. 'The eontact on the oil switeh is practically a single-pole domble-throw switeh, the econter point of which is connecter to the serement of the distributor, the other two points connecterl one to positive polarity and one to negrative polarity. When the oil switel


Fig. 5. Front View of Distributor Used for Obtaining Sherman Creek Switch Indications
is closed negative polarity and when the oil switch is open positive polarity is transmitted to the distributor segment.

The corresponding segments of the distributor at the pilot board are connected to polarized relays which operate the red and green lamps on the pilot board.

To maintain the two distributors in synchronism, there are ten segments on the middle ring separated by insulating material and bridged by the revolving brush to the collector ring, five of the segments of the pilot board distributor are connected to positive polarity and five to negative polarity. The ten segments of the Sherman Creek distributor are connected to ground.

On the periphery of the revolving element which carries the brush arm are five teeth so spaced as to be in alignment with the synchronism segments. Engaging the teeth are two release magnets 180 degrees apart.

The middle collector rings of the two distributors are connected through two polarized line relays in series, one located at the pilot board and one at Sherman Creek.

The release magnets are energized by the operation of the line relays, the right hand one of the pilot board operating with the right hand one of the Sherman Creek distributor and the left hand one of the pilot board distribut or with the left hand one of the Sherman Creek distributor.

As the operating current is suppliced to the pilot board (listributor, this distributor may be callerl the master. As the brushes pass over the synchronizing segments impulses are sent through the two line relays in series, through the brush to the synchronizing segments of the Sherman Creck (listributor.
'The operation of the line relays completes the eirenit through the release magnets and disengatges them from the teeth of the revolving brush clements. The brushes then pass over segments of insulation interrupting the current supply to the line relays and resetting the release magnets to engage the teeth of the revolving brush element.

The distributors are thus synchronized ten times during each revolution and as the teeth on the brush arms are in alignment with the synelironizing segments, the release magnets will be energized before the teeth engage with the release magnets, provided the distributors are in exact synchronism

If, however, the two distributors are not in exact synchronism, and one is slightly ahead of the other, this one will be stopped by the release magnet until the slower one comes into synchronism, when the release magnet will operate, releasing the brush arm and allowing it to continue revolving.

All of the green lamps on the pilot board of switches not in service are capped so that normally no green lamps are exposed lighted, the red lamps of course being lighted for all closed switches. During any emergency when one or more switches in any of the generating stations opens automatically or is opened by switchboard operators, the red lamps corresponding to such switches are extinguished and the green lamps lighted. At the same time, the bell alarm rings, calling the System Operator's attention to the pilot board, where at a glance he is cnabled to see exactly what equipment has been thrown out of service.

It is the function of the System Operator, in his control of the operation of the system, to apportion the load among the several generating stations and keep in reserve at all times sufficient generating equipment, transmission and transforming equipment to take care of any demand which the system may be called upon to meet. No apparatus, therefore, is taken out of service without first obtaining the approval of the System Operator. The system is called upon to meet extraordinary and sudden demands during the summer when thunderstorms oceur. The load during such storms increases rapidly and often exceeds $100,000 \mathrm{kw}$. above normal day load (Fig. S).

The System Operator, further, is charged with the responsibility of protecting all hightension equament that men are engaged in working on against the possil)ility of such equipment becoming "alise," It is his duty to direct that such apparatus, where neeessary, be grounded, oil switehes blocked open. ctc.

A special telephone swithboard is located directly in front of the operating pilot board. From this switchboard radiate direct telephone lines to each sulstation and to cach generating station of the system. In addition
 phone tines keaving the switchan ot : 111
 exchanges. taking different routes through the building and through the streets.

Tor further inerease the efficioney of the system operation and to estal)lish, Juring emergencies, more speedy means of connmunication with the sulstations than is perssible with telephones, a signaling system consisting of standard (jamewedl Fire Darm apparatus is used between the System ()perafor and all of the substations and senerating


Fig. 6. Switch Indicating System Between Sherman Creek Generating Station and System Operator's Pilot Board
to the direct telephone lines, several exchange lines are also connected to the board. The board normally is a two-position board but is so wired that in cases of emergency, by throwing keys, the board may be split into six parts so that six operators may use it at one time if desirable. Extraordinary precautions are taken to maintain this telephone system. "Taking" current may be received from either of two telephone exchanges or from a storage battery located at the switchboard. "Ringing" current may also be obtained from either of two telephone exchanges or from magneto
stations, using for circuits leased lines of The New York Telephone Company. See Fig. 7. The signaling switchboard, which has a capacity of sixteen circuits, ten of which are used at the present time, is located in the System Operalor's Office. This switchloard consists of the master sending device, woltmeters, testing plugs, circuit indicating lamps, balancing resistors, multiple punch recorders, which record on paper tape all signals sent, the circuits over which they are sent and an automatic time stamp which prints on the paper tape the date and time that signals are sent.

Sororal sulastations. tha mamber depondima




 motor-goneratorsctsinstalled in duplicate and
 operalled either frem the station lighting sys-


Fig. 7. Control Switchboard of the Emergency Signal System
tem, the excitation system, or the storage batteries. The equipment is of the closed circuit type so that by means of indicating lamps connected by relays to the circuits, the continnity of each circuit is indicated continuously.

For each signal there is provided a wheel with notches corresponding to the signal number cut into its periphery: To send a signal, the circuit switches of the circuits over which it is desired to send the signal are elosed, the signal wheel placed on the shaft of the sending device and the sending lever pulled. The entire operation requires from .j to 10 seconds. The sending device is equipped with a repeating lever by which signals may be repeated from two to four times as desired. Under the prescont system of operation this lever is set to repeat all signals three times. The substation equipment consists of a 10 -inch electro mechanical gong and a punch recorder mounted on the substation switchboard near the substation switchboard operator. In
order tolest this systenn datily, at time signal1: or ${ }^{\circ}$ lock noon - is sent over all of the circuits and all chocks are set in aterorlanere with this signal. A set of instruments installed in the Executive Offices of the comphany recorels all signals sent by the System Operator and (ratables the executives to keep) in close touch with the operating conditions cluring cmersencies.

The advantages of this system, which under the present method of operation is used during emergency conditions only, may be summarized as follows:

1st: The System Operator is relieved of telephoning instructions to the substations individually as he is enabled to signal the instructions simultaneously to all substations in less than one minute with the result that simultaneous action and cooperation of all substations are obtained.

2nd: The substations, by receiving signals that the disturbance or emergency is general and not local, are enabled at once to adopt the proper course of action.

Brd: Instructions issued by the System Operator are recorded.
tht: Instructions are transmitted accurately, avoiding the liability of misunderstanding telephone instructions. The present code of signals applying to the 2.j-cycle system is as follows:
12 Transfer half of your load on Waterside No. 1 feeders to Waterside No. 2 fueders.
1:3 Transfer half of your load on Waterside No. 2 feeders to Waterside No. 1 feeders.
14 Transfer half of your load on Hell Gate feeders to Waterside No. 1 and Waterside No. 2 feeders.
22 Trouble at Waterside.
23 Indications of trouble-"Stand By."
24 Trouble at Hell Gate.
2.5 All alternating-current supply is interrupted.
26 Indications of approaching storm.
31 Discharge all batteries at the one-hour rate and drop load off Waterside No. 1 feeders.
32 Discharge all batteries at the one-hour rate and drop load off Waterside No. 2 feeders.
33 Discharge all batteries at the one-hour rate and drop load equally off Waterside No. 1 and Waterside No. 2 feeders.
34 Discharge all batteries at the one-hour rate and drop load off Hell Gate feeders.
i3 $1: 3$ Discharge all batteries at the three－ hour rate and drop hate off Waterside No． 1 feeders．
ㅇots：－Ljom recoipt of this signal if discharging at the onc－hour rate piok ap）reduced hattery load on Waterside No． 1 fecolers．
3ㄹ：3 Discharge all batteries at the threc－ hour rate and drop）load off Waterside No． 2 feeders．
Note．－Lpon receipt of this signal if discharging at the one－hour rate piek up reduced battery load on Waterside No．el feeders．
3.33 Discharge all hatteries at the three－ hour rate and drop hoad equally off Waterside No． 1 and Waterside No． 2 feeders．
Note．－Upon receipt of this signal if discharging at the one－hour rate pick up reduced battery load equally on Waterside No． 1 and Waterside No． 2 feeders．
$3: 3+$ Discharge all batteries at the three－ hour rate and drop load off Hell Gate feeders．
Note．－C＇pon receipt of this signal if discharging at the one－hour rate pick up reduced battery load on Hell Gate feeders．


Fig．8．Summer Load Curve showing Effect of Storm． Dotted line is for a normal day

41 Clear all feeders which are not carrying load and promptly notify System Operator when clear．
42 Connect rotaries to start from a＂Stand Still＂and promptiy notify System Operator when ready．
 －t：ar
1：Troublはロバいド
－ 10 Combliomosatsciactors
17 Comations mamal
 voltes a sick


Fig．9．Winter Load Curve
．）．Disconnect all batteries from the d－c． system．
Note．－Reconnect the batteries to system when voltage of system is such that they will not discharge when float－ ing on lowest end cell．
j）：Waterside and Hell Gate will now lower a－c．voltage．
if $f$ Restore d－c．pressure to normal．
61 Interruption probably of short duration， less than is minutes．
62 Interruption probably of fong duration， more than 30 minutes．
63 Interruption of unknown duration．
if 6 Time signal－Correct time is 120 oclock noon．
$67 \quad$ Test signal
7．Cancel last signal．
The storage battery capacity of the Edison direct－current system is today approximately 60.000 kw ．for one hour．By means of this system，the generating stations may obtain relief of 60.000 kw ．in from one to two minutes Which would be impossible if it was necessary to telephone each substation for battery dis－ charges．

The Now lork Edison and allied companies serve the territory within the Boroughs of Manhattan, Bronx and Queens and of Westedester Connty: The direct-current distribution system eovers the Borough of Manhattan south of 18.5 th Street. The alternatingcurrent distribution system covers the balance of the territory mentioned above. To supply Whis territory there are four large high-tension generating stations and several smaller stations having an aggregate installed capacity of t.ti,000 kw. 2. 5 cycle and $233,000 \mathrm{kw}$. 60 cycle, a total installed capacity of $689,000 \mathrm{kw}$. To supply the direct-current distribution sys1 m which lies south of 135 th Street in the Borough of Manhattan, there are thirty-two
rotary converter sulstations and to supply the alternating-current distribution territory there are twenty-seven alternating-current substations. To supply the raiload service which is supplied by the allied companies, there are thirteen direet-current substations and one alternating-eurrent substation.

For the interchange of power with other companies in Greater New York, there are comections between the system of The New York Edison Company and the Interborough Rapid Transit Company, the Brooklyn Edison Company, the Brooklyn Rapid Transit Company, and the Pennsylvania Railroad Company, having an aggregate capacity of approximately $68,000 \mathrm{kw}$.

# Atmospheric Nitrogen Fixation 

## PART I

By Eric A. Lof
Power and Mining Engineering Department, General Electric Company


#### Abstract

The essential need of nitrogen in our modern civilization is now becoming generally recognized. It is a necessary element in plant food and explosives. It is used extensively in the production of celluloid, dyes, many drugs, perfumes, flavorings, ete. In Part I, this month, the author deals with the need for nitrogenous fertilizers, the nitrogen eycle in Nature, Chile saltpeter, by-product ammonia and the arc process of produc. ing nitrogen from the atmosphere. In Part II the cyanamid, cyanide, nitride, Haber and Claude processes will be dealt with. This article originally appeared in the Gas Age-Record.-Edrtor.


The three essential food constituents of living matter are carbohydrates, fats and proteins; the two former chiefly for the production and storage of energy and the latter for building up the body substance. They are alike in the respect that they all contain the three elements carbon, hydrogen and oxygen, but differ in that protein also contains nitrogen, which, therefore, becomes one of the indispensable substances of life.

Nitrogen is a colorless, tasteless and odorless gas, slightly lighter than air. It comprises about four-fifths of the volume of the atmosphere, where it occurs in a free state mechanically mixed with oxygen. In this free state, it is an exceedingly inert element and combines only with difficulty with certain other elements as will be explained later. In combined form, it is found chiefly in certain natural nitrate deposits, and natural manures such as guano also contain large quantities of nitrogen compounds.

## Free Nitrogen

The atmosphere is the inexhaustible source for our nitrogen supply and every bit of nitrogen in plants, animals, and the soil has originated from free atmospheric nitrogen. Arrhenius estimates that no less than $400,000,000$
tons of nitrogen are annually withdrawn from the atmosphere and as nitrogen does not accumulate to any great extent in the soil, this enormous quantity must again be set free as inert nitrogen gas by the decomposition of organic matter and restored to the atmosphere. An immense and endless circulation of nitrogen is therefore continually going on, as shown in the accompanying diagram.

Through the action of electrical discharges of thunderstorms, which continually go on in the atmosphere, appreciable amounts of free nitrogen in the air are converted into oxides of nitrogen which are absorbed by falling rain water and enter the soil in the form of nitric acid. This nitric acid then combines with the bases in the soil, such as potassium, calcium, etc., and forms the corresponding nitrates in which form they are taken up by the plants and metabolized into protein.

Through the action of bacteria in their root nodules, certain legumes, such as peas, beans and clover, also possess the capacity of directly absorbing free nitrogen from the air during their growth and converting it into protein.

It has thus been shown how the nitrogen is supplied to the plants and protein metabolized which serves not only as their own food supply but also as reserve food for the plants' off-
springs. This now becomes animal ford and, for vegetable eating anmats, it is the sole source of the nitrogen for animal protein.

Part of the nitrogen which is not used for maintaining the body sulstance of animals is climinated as urea, and hipporic acid, and from the urea much nitrogen is set free be the action of nitrons acid. This urea and hippuric acid together with deeayed vegetable and animal matter, that is dead protein, is then with the aid of bacteria converted into ammonia. Part of this is by means of oxidizing bacteria converted into nitric acid and nitrate in which form it again is partly assimilated hy the plants. Part of this nitrate is, however, dinitrified by bacteria, one portion reverting into free nitrogen which goes back to the atmosphere, the other being converted into ammonia which fails to oxidize and is volatilized as a gas, which is absorbed by rain and again returned to the soil. Part of the ammonia is also taken up directly by the plants from the soil.

## Need for Fertilizers

The fertility of the soil would thus remain practically unchanged if all the ingredients


Fig. 1. Elementary Diagram of Nature's Nitrogen Cycle
removed in the various farm products were returned to the land where they come from. This is to some extent accomplished by feeding the crops grown on the farm to animals, carefully saving the manure and returning it
 conditions of farming indicater, bome - $1+.{ }^{1}$ as a mole the manture prentuen in the hame far from sulficient tomatutam its fortility and artificial fortilizers must beressorad (u).

It has been estimated that the yearty less of nitrogen from soils maler coltivation jas this


Fig. 2. Inorganic Nitrogen Consumption in United States as given by Nitrate Division of the United States Ord. nance Department. Black portions represent inorganic nitrogen used in agriculture. White portions represent nitrogen used in industries and for explosives
country by grain crops alone amounts to over $2,000,000$ tons per year. Of this, not over three per cent is at present being supplied from organic fertilizer sources, such as tankage, cotton seed, etc., and this supply is constantly diminishing. The remainder must, therefore, come from inorganic materials. It would, of course, not pay to fertilize to the above extent immediately, but it mercly indicates the extent to which nitrogen is needed for fertilizer purposes.

With our constantly increasing population, an increased food supply must be provided and this can mly be assured by increased cultivation and fertilization of the soil. How far behind we lay in this respect as compared with certain European countries, which of necessity have been forced to an intensive use of fertilizer, is shown by the following talale. Prior to the increased use of fentilizer in these

| Country | Pounds <br> Fertilizer used Per Culted Acte | Average yield in bu'sule s PER ACRE, 1905-1913 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Wheat | Rye | Oats | $\begin{aligned} & \text { Pota- } \\ & \text { toes } \end{aligned}$ |
| United States | 37 | 14.6 | 16.0 | 29.5 | 9.5 .0 |
| France | 111 | 20.2 | 16.9 | 30.6 | 130.7 |
| Germany | 207 | 30.4 | 27.4 | 53.6 | 204.8 |
| Great Britain | 244 | 33.4 | 29.1 | 43.5 | 211.7 |
| Belgium. | 495 | 37.0 | 34.7 | 71.5 | 306.0 |

countrics, the productirity of their soil was smimat our own, and the inerease in the food supply, withoul additional labor and at a cost wholly incommensurate with the gatas, has grown in dired propertion to the amomet of fertilizer used.

Besides fertilizers, large amounts of nitrogen are also needed for industrial purposes, and the requirements to meet this demand are also steatily increasing.

Nitrate is one of the main ingredients in high explosives and gun powder, and nitration, that is, the treatment of substances with nitric acid, is the fundamental chemical operation in the production of gun cotton for making smokeless powder, celluloid or other pyroxylin plasties from cotton or paper such as artificial ivory, ete. The dye industry is also to a great extent based on nitration, and numerous drugs, perfumes and flavoring extracts are also being made in this manner from the coal tar bases benzol, toluol and naphthalene.

It is difficult to predict with accuracy to what extent the nitrogen fixation in this country will increase in the future. From statistics presented at a hearing before Congress in 1920, it was estimated that the possible consumption of fixed inorganic nitrogen would be as follows:

|  | 1925 | 1930 |
| :---: | :---: | :---: |
| Agriculture | 190,000 tons | 290,000 tons |
| Industries. | 130,000 tons | 150,000 tons |
| Total | 320,000 tons | 440,000 tons |

To supply this need, it is further estimated that the available production from by-product coke ovens will be:

|  | 1925 | 1930 |
| :---: | :---: | :---: |
| By-product <br> production $\ldots . .$. | 130,000 tons | 160,000 tons |

The difference would then have to be supplied by importation of Chile saltpeter or by increased products from atmospheric nitrogen fixation plants. For this latter purpose, there are now three plants in this country which with certain modifications would be available and with a combined yearly production capacity equivalent to about 45,000 tons of fixed nitrogen per year. At present only one of
these plants is in operation with a yearly output of only a few thousand tons.

From these figures, it is obvious that we will have to continue to rely to a great extent on the importation of Chile saltpeter, unless steps are taken for providing increased facilities for fixation of atmospheric nitrogen. It is the purpose of this article to describe the different proeesses which at present are available for this purpose, but first a brief reference will be made to the other two sources of inorganic nitrogen, viz., Chile saltpeter and by-profluet ammonium suphate.

## CHILE SALTPETER

Chile saltpeter is chemically known as Sodium Nitrate ( $\mathrm{Na} \mathrm{NO}_{3}$ ), the commercial product containing about 95 per cent nitrate of which $151 / 2$ per cent is nitrogen. Like the potash deposits in Germany there are few natural deposits like the saltpeter deposits in Chile on the west coast of South America. These deposits were discovered by Indians about 1809, who, when lighting a fire, noticed that the ground began to ignite in various directions. They attributed this to evil spirits and consulted a priest, who caused the earth to be examined, thus reveating the presence of nitrate of soda.

The nitrate deposits are located at altitudes ranging from 2000 to 6000 feet in the desert regions between the 12 -degree and 26 -degree latitudes, a distance of about 500 miles, and perhaps the driest country in the world, with no vegetation whatever.

The nitrate beds generally form horizontal layers covered by three distinct layers or strata of silica, calcium sulphate and other minerals, the thickness of these layers ranging from two to several feet. The nitrate as mined goes under the name "Caliche," and the deposits vary in thickness from a few inches to four or five feet or more. It is like a cemented gravel, the cementing material being the sodium nitrate and sodium chloride and other salts which accompany it. The caliche treated runs from 14 per cent nitrate up to as high as 30 per cent or more, and it does not as yet pay to mine materials with less than 13 to 14 per cent nitrate.

There are many theories advanced regarding the origin of these natural nitrate deposits. Some think that they are original guano deposits; others ascribe their origin to seaweed, because the caliche contains considerable amounts of iodine and fish skeletons are often found imbedded in the strata. Recent theories are that it has its origin in volcanic actions.

## Preparation of the Nitrate

The production of Chile saltpeter comes under two divisions－the mining of the caliche and the refining．The caliche is extracted from the ground by blasting and hand picking， after which it is loaded in carts or light rail－ road cars and hauled to the refining plants called＂oficinas，＂by mules or small loco－ motives．At the plant it is crushed and leached with boiling water，when due to the different solubility of the nitrate and chloride salts， practically all the nitrate will be dissolved while the other salts if already in solution will be precipitated．The solution is then allowed to cool and due to the solubility characteristics mentioned above the nitrate crystallizes out first while the other salts remain in the solu－ tion which is drained off．The nitrate，now in solid form，is placed in drying pans to allow the remaining water to evaporate and when entirely dry it is packed in bags of about 200 lb ．each and shipped by rail down to the different harbors for export．

Most of the Chile saltpeter is used for ferti－ lizer purposes，the nitrogen contained therein being extremely soluble and readily available as food for plants．The nitrogen in this form is thus directly and immediately a ailable and no further changes are necessary．

Considerable amounts of Chile salt peter are also used for industrial purposes in which case it must be converted in some other form，the starting point as a rule being nitric acid．This conversion is accomplished by treating the sodium nitrate with sulphuric acid，when a violent reaction takes place with the result of the formation of nitric acid which is given off as a gas．This passes into condensers where it is condensed to liquid acid．The reaction takes place according to the formula：

$$
\mathrm{NaNO} \mathrm{NO}_{3}+\mathrm{H}_{2} \mathrm{SO}_{4}=\mathrm{HNO}_{3}+\mathrm{Na} \mathrm{HSO}_{4} .
$$

## Statistics

Chile saltpeter was first exported from Chile in 1830 but the amount was small，only a few thousand tons per year．Then it has， however，constantly increased as seen from

| Year | Total Export <br> in Tons | Export to Uxited states |  |
| :---: | :---: | :---: | :---: |
| Tons <br> Nitrate | Tons <br> Equivalent <br> Nitrogen |  |  |
| 1913 | $3,000,000$ | 700,000 | 110,000 |
| 1914 | $2,700,000$ | 605,000 | 95,000 |
| 1915 | $1,900,000$ | 865,000 | 135,000 |
| 1916 | $2,200,000$ | $1,360,000$ | 214,000 |
| 1917 | $3,600,000$ | $1,680,000$ | 264,000 |
| 1918 | $3,200,000$ | $2,075,000$ | 325,000 |
| 1919 | $1,000,000$ | 450,000 | 90,000 |
| 1920 | $3,000,000$ | $1,430,000$ | 224,000 |

the foregning tabulation，whellathe
export to the L＇nited States and it cerp
nitrogen content．
It is interesting bon mow bow export dropped in 1！日交，when the supply of the（＇en－ tral powers in Europe was colt oft，and bow it since steadily incratased matil the end of the war when it again took a big（lros）．

The proceeds obtained from the expert duty imposed by the Chile（overnment amonnts in about 40 per cent of that combtry＇s vearly revenue．

The question is often asked：How long will the Chile deposits last？There is guite a difference of opinion in regard to this．It is estimated that the contents of the survered areas contained about $300,000.000$ tons of nitrate of which about $50,000,000$ toms have been mined，leaving about $200,000,000$ wins untouched．At the present rate of production this would last about 100 years．It is claimed that the unsurveyed areas are some thinty times larger than the surveyed ones，but un－ doubtedly of a much lower nitrate content， and it is quite safe to assert that the deposits would last another 250 or 300 years．On the other hand，it is almost certain that long lee－ fore that time new artificial nitrogen fixation processes will hare been developed．lo means of which it will be possible to mannafacture nitrogen compounds at a much lower cost than the cost of Chile saltpeter，so that the mining of Chile saltpeter will undoubtedly be very materially curtailed long before these deposits are exhausted．

## BY－PRODUCT AMMONIA

The by－product coke oven industry now occupies a vital place for the supply of nitro－ gen in the form of ammonia．Besides am－ monia，the carbonization of the coal in these ovens gives us many ot her valuable by－prod－ ucts such as benzol，toluol and napht hatene．

It is interesting to watch how these modern be－product coke plants rapidly supersede the

PRO DUKIIONIN゙ UNITED STATES

| Year | By－product Coke |  | Beehive Coke |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Tons | $\begin{gathered} \text { Per } \\ \text { Cont of } \\ \text { Cotal } \end{gathered}$ | Tons | $\begin{aligned} & \text { Pet } \\ & \text { Cent of } \\ & \text { Total } \end{aligned}$ |
| 1901 | 1，180，000 | j | 20，615．000 | 95 |
| 1907 | 5，610，000 | 14 | 35，170，000 | 86 |
| 1913 | 12，715．000 | 28 | 33，585，000 | 72 |
| 1916 | 19，070，000 | 3.5 | 35，465，000 | 65 |
| 1918 | 26，000，000 | 46 | 30，480，000 | 54 |
| 1919 | 25.170 .000 | 56 | 19，650，000 | 44 |
| 1920 | 30，835，000 | 60 | 20，510，000 | 40 |
| 1921 | 19，920，000 | 78 | 5，560，000 | 22 |


Fig. 4. By-product Coke Ovens, showing the Coke Being Removed from an
Oven to the Quenching Car



Fig. 3. Typical Nitrate Beds in Chile


old-fashioned beehive orens, as may be seen from the foregoing tabulation.

A bep-product coke oren is a rather complicated structure, but briefly it consists of a large number of parallel chambers or ovens in which the bituminous coal is heated out of contact with the air. The orens are separated by flues in which part of the gas generated by the distillation is burned to provide the heat necessary for the coking.

It is from the volatile matter in the coal given off that the by-products are obtained The ammonia is thus the result of the union of nitrogen and hydrogen, according to some reaction which is not fully known.

The coal contains from 1 to $1^{1} \underline{2}$ per cent nitrogen, and of this only about 1.5 per cent is recovered in the form of ammonia. This means that we only get about $\bar{i} \mathrm{lb}$. of ammonia per ton of coke. The hot gases from the ovens containing the ammonia are cooled and scrubbed with water to remove the tar. Ther then go to saturators filled with sulphuric acid. and when the gas bubbles through this acid an intimate contact is established between the two and ammonium sulphate is precipitated as a solid salt according to the reaction:

$$
2 \mathrm{NH}_{3}+\mathrm{H}_{2} \mathrm{SO}_{4}=(\mathrm{NH})_{2} \mathrm{SO}_{4}
$$

The ammonium sulphate thus formed in the saturators is then drained and dried in centrifugal driers, after which it is ready for sale. It then contains 24 per cent of ammonia. equivalent to about 20 per cent of nitrogen.

The remainder of the gas, now freed from ammonia, after leaving the saturators may then be further scrubbed with absorbent oils for recovery of other by-products, and if the gas is to be used for municipal purposes it must be further purified by remoring any sulphur that it may contain.

## Production Capacity

The annual productive capacity of the country's existing by-product coke oren plants

| Year | Coke-oven <br> Ammonium Sulphate Production in $\mathrm{C} . \mathrm{S}$. in Tons | Equivalent <br> Nitrogen |
| :---: | :---: | :---: |
| 1910 | 116.000 | 23.000 |
| 1911 | 127.000 | 2.5 .0000 |
| 1912 | 165.000 | 33.0000 |
| 1913 | 195.000 | 39.0001 |
| 1914 | 183,000 | 37.000 |
| 1915 | 250.000 | 50.000 |
| 1916 | 28.0001 | 89.000 |
| 191\% | 3.70 .000 | 74.000 |
| 1918 | 388.000 | TS.001 |
| 1919 | 423.000 | S.5.00) |
| 1920 | 503,000 | 100.0 mm |
| 1921 | 346.000 | 189.010) |


which would correspend (6) a maxmme on
 toms, equisalent to 110.000 toms of combinud nitrogen.

The ammonium sulphate formbution is. however, closely related to the stacl mill hanness, and the recent slate in this industry was clearly reflecterl in the colse production ami nat urally also the ammonium sulphate orthut as shown in the foregrong tabulation.

## THE ARC PROCESS

The principle underlying this process is the possibility of chemically unting part of the free nitrogen and oxygen in the air at such high temperatures which only the electric arc is capable of producing this being around .5000-16000 deg. Fahr.

Air, which is only a mechanical mixture of mitrogen and oxygen, is thus passed through an electric arc furnace when a small part tabout two per cent) of these elements combine chemically and from nitric oxide, $\times O$. This gas. when leaving the furnace, has a temperature of around $1500-1 \mathrm{~s}(0)$ deg. Fahr., and in order to prevent the $N O$ from dissociating or breaking up it must be rapidly cooled to a temperature around 100 deg. Fahr.. which is done in two steps. The hot gas is first passed through ordinary steam boilers. which thus serve as coolers with recovery of heat in the form of steam for use in other parts of the process. The temperature of the gas is lowered to about 300 deg. Fahr. by these boilers. but below this point it becomes necessary to carry out the further cooling in aluminum coolers through which water circulates, without, of course, coming in direct contact with the gas. The reason for this is the fact that nitric oxide at these low temperatures. in the presence of moisture in the gas from water leaking through the tubes begins to oxidize to nitric acid. Which corrodes iron but not aluminum.

From the aiuminum colers the gas mixture is now conveved in an oxidation chamber, a big sheet steel tank lined with fire brick. The purpose of this oxdation tank is to give the gas sufficient time to oxidize the nitric oxide $\therefore 0$ to nitrogen pernide, $\triangle O_{2}$ or $\lambda_{2} O_{4}$, this being desirable for the absorption of the sas which is to follow:

From the oxidation tank the gas is carried through an absompum system consisting of sereral groups of atharption towers usually five towers in series per yroup). These towers are of emomous size the imside being filled

Whth humps of (ghatt\% or other matherials which the acid will mot athack. Water is admitted (1) the tw of the thirl tower and when it trickkes down ofor the quartz blling it meets the asconding gas and is converted into a weak nitron acil. 'This adid is then promped (1) hac (w) of the secomil toner where it is used as the alsmption liquid and similarly the aciol from the second tower is used for absorption in the first tower, thus gradually increasing in strength. After having thus passed the third tower. about so per cent of the $\mathrm{NO}_{2}$ gas has lexem absorbed, and this is about all that can be absorbed by water, the resulting acid from the first tower having a strength of 30 per cent, this being known as weak nitric acid.

The reaction which thus has taken place in the three first towers is as follows:

$$
\because \mathrm{NO}_{2}+\mathrm{H}_{2} \mathrm{O}=2 \mathrm{HNO}_{3}+\mathrm{NO}
$$

The liberated nitric oxide, in the presence of oxrgen and water, is again converted into nitrogen peroxide and nitric acid.

The remaining 20 per cent of the gas leaving the third tower is now so weak that another solution than water must be provided for its absorption. An alkali solution such as soda ash is used for this purpose in towers four and five, the resulting product being a mixture of sodium nitrate and sodium nitrite, which is evaporated and may be used directly as a fertilizer. If only sodium nitrite is desired the gas is passed into a solution of caustic soda.

The weak acid from the first tower is, however, the main product; but as such a weak acid cannot be economically transported, it must be converted into some neutral salt or changed into concentrated acid of 95 per cent strength, which can be shipped in aluminum tank cars. The concentration is accomplished by means of sulphuric acid, which has a greater affinity for the water in the weak nitric acid, thus absorbing it, leaving the nitric acid in concentrated form.

The nentral salt, generally probuced from the weak aced, is calemm nitrate, also known as nitrate of lime or Norway saltpeter. beatuse it is the main moxluct of the large nitrateplants in Norwaty. The caldem nitrate (a $a\left(\mathrm{NO}_{3}\right)_{2}$, is thus produced by treating ordinary limestone with the weak acid, the reaction being as follows:

$$
\mathrm{CaCO} \mathrm{O}_{3}+\stackrel{2}{ } \mathrm{HNO}_{3}=\mathrm{Ca}\left(\mathrm{~N}\left(\mathrm{O}_{3}\right)_{2}+\mathrm{H}_{2} \mathrm{O}+\mathrm{CO}_{2}\right.
$$

The resulting solution is evaporated by the waste heat from the steam boilers before mentioned, and the product is then ready for the market.

This calcium nitrate contains 1:3 per cent of fixed nitrogen, and is, like Chile saltpeter, an excellent fertilizer, although somewhat hygroscopic. It is, as stated, the main product of the large Rjukan nitrate plants in Norway, which have an annual productive capacity of about 200,000 tons of nitrate, equivalent to about 26,000 tons of fixed nitrogen. Over 300,000 electrical horsepower are used for this, generated in magnificent high-head water power plants. The power requirements with this process are thus about 12 h.p. years per ton nitrogen fixed, and from this high rate of consumption it follows that the price of the power must be very low in order to make the process an economic success.

The majority of the furnaces used at Rjukan are of the Birkeland-Eyde type, the latest designs having a capacity of $4000-5000$ h.p. each. There are also some Schoenherr furnaces of $1000 \mathrm{~h} . \mathrm{p}$. capacity each. Numerous other types of furnaces have been proposed and patented, but none except the above-mentioned types have come into any general use. With the exception of the abovementioned large plants in Norway, the process has had a very limited use. One plant of moderate size has been in operation in France, and the activities in this country have so far been confined to two small installations, one in the West and one in the South.

# Stress Distribution in Electric Railway Motor Pinions as Determined by the Photo-elastic Method 

Bỵ l'ath lifranss, Cambridge, Mass.

and A. L. Kimbala, Jr., Research Laboratory, General Electric Company


#### Abstract

This article embodies some results of a general scientific study undertaken for the development of superior electric-railway motor pinions. The particular portion of the work described was performed at the Massitchusetts Institute of Technology, using the General Electric Company's apparatus for stress determination in transparent models by the photo-elastic method. Some of the supplementary mechanical tests were made at Schencetady, and throughout the work close contact was maintaned with the Railway Motor Digartiment and the Research Laboratory at Schencetady. A bricf description and discussion of the photo-elastic method is given in the first part. The stress distribution in, and the causes of ruptures of, given types of gear pinions used in electric-railway motors, as investigated by the photo-elastic method, are afterward reported upon and discussed. This article was presented as a paper at the annual mecting, New York, December 4 to 7, 1922, of the American Society of Mechanical Engineers.


## I. DESCRIPTION OF THE METHOD

## How to Define the State of Stress at any Point of a Solid Body

The state of stress at any point in a solid body is determined when the traction across every plane through the point is known. There exist at any point thrce orthogonal planes across which the traction is purely normal and which are called the planes of principal stress. The normal tractions across those planes are called the principal stresses. The state of stress at any point is completely determined by the direction and the magnitude of the principal stresses at the point under consideration. The principal stresses, given in direction and in magnitude, express in the most general and complete way the elastic state at any given point. The bending moment, the shearing forces, etc., are readily deduced from the direction and the magnitude of the principal stresses. Furthermore, one of the principal stresses always expresses the maximum stress.
2. The notion of principal stress may be illustrated as follows:
3. Consider a spherical element in a solid body. External applied loads will deform this spherical element into an ellipsoidal element (Fig. 1). The axes of this ellipsoid will correspond in direction and in magnitude to the direction and the magnitude of the principal stresses.
4. The orientation and the form of the ellipsoid, and therefore the direction and the magnitude of the principal stresses, will define the state of stress at the point under consideration.

[^5]5. The axes of the ellijsoid represent the largest and the smallest deformation at the point under examination. Correspondingly, the principal strases give the direction and the magnitude of the maximum and the minimum stress.


Fig. 1. Ellipsoidal Element Resulting from Subjecting a Spherical Element to Stress
6. If the three principal stresses vary from point to point in the structure, the problem to be dealt with is a threc-dimensional elastic one. If one of the threc principal stresses vanishes throughout, it is a two-dimensional elastic or plane-stress problem.
7. Corresponding to the three- and twodimensional elastic-stress problems there are also the three- and two-dimensional elasticstrain problems, when the deformations corresponding to the principal stresses are considered. ${ }^{1}$
8. A great number of structural problems (bridge, ship, airplane, plate, dam, etc., construction) are, or their stress analysis may be reduced to, two-dimensional elastic problems.

The Photo-elastic Method of Stress Determination
9. As set forth in Pitr. 1, the state of stress at any point is most completely defined by the direction and the magnitude of the principal st resses. These are, therefore , the elements which we wish to determine for a complete amalysis


Fig. 6. Frame for Comparison Member Designed by E. G. Coker and A. L. Kimball, Jr.
10. The photo-elastic method solves the two-dimensional elastic problems. It primarily takes advantage of the double refracting properties shown by isotropic transparent substances when put under stress. The stresses in the structure may therefore be determined from models made of a homogeneous transparent material, and ordinarily on a reduced scale. The stresses in a steel, cement, or any other structure, homogeneous throughout and obeying Hooke's law of linear proportionality between stress and strain, may be readily deduced from the values obtained by the analysis of the corresponding

[^6]transparent model for the case of two-dimensional elastic problems.
11. If plane polarized light is passed through a stressed specimen of celluloid and afterward through a second nicol prism whose principal section is parallel to the plane of polarization of the original beam of light, only the points where the principal stresses are respectively parallel and perpendicular to the principal sections of the crossed nicols remain dark. This result makes it possible to determine the directions of the principal stresses at any given point. Morever, this information is needed for the measurements which will be lescribed later.
12. If now circularly polarized light be passed through the specimen, by interference of the two component rays, which in the double-refracting specimen have suffered a relative retardation at each point proportional to the difference in magnitude of the two principal stresses, a colored image is obtained. (Figs. 2, 3, 4 and 5.)*
13. By a comparison method, based upon the interposition in the proper direction of a comparison member of constant cross-section, put under uniform tension in a suitable frame (Fig. 6), the value of the difference of the principal stresses at any given point may be read on the dynamometer of the frame.
14. Now, in the two-dimensional elastic problems the transverse deformation, i.e., the deformation along a normal to the plane of the two principal stresses, is proportional to the sum of those two stresses. By means of a lateral extensometer (Fig. 7), we measure this transverse deformation.
15. From the values of the differences and the sums of the principal stresses, the separate values of each of them are computed, thus determining completely the state of stress.
16. A question naturally arising is whether the results obtained on a transparent body such as celluloid hold for structural materials.
17. It is shown by the general discussion of the equations of elastic equilibrium that in the case of strain or plane stress in an isotropic body obeying Hooke's law of linear proportionality between stress and strain, the stress distribution is independent of the moduli of elasticity and consequently of the material of which the body is made. Thus the stress distribution experimentally determined in the case of a celluloid body is the same as it is when the body is made of any other isotropic substances such as iron, steel, etc., obeying Hooke's law, in distribution,
direction, and magnitude. Noreower these conclusions derived from the gemeral theory of elasticity have been cheeked by experiment. ${ }^{2}$

1s. The photo-elasticmethod can beapplied to the great majority of structural problems. not only in taking the place of mathematical computation, but particularly in solving those structural problems where mathematics becomes too involved to be of help. Morcover it has the great advantage of giving the maximum stress at each point throughout the whole structure, and it therefore offers an effective means of inereasing safety and reducing superfluous material.

## II. A STUDY OF THE STRESS DISTRIBUTION IN GEAR PINIONS

19. When accidents occur with gear wheels, besides the metallurgical question, three possible causes of failure suggest themsclves:
a. The gear wheel may not have been properly designed.
b. It may have failed under an excessive load.
c. When the pinion was shrunk hot or forced on to a tapered shaft, an excessive inside radial pressure may have been set up.
20. It is easy to see that the ordinary methods of resistance calculations of gear wheels, based on considering the tooth as a cantilever loaded at its end, would not be expected to give reliable and complete information as to stress distribution, not even for the root section of the tooth which is under consideration.
21. Indeed, the shape of the tooth, the curvature at the root, the ratio of the diameter of the pinion bore to the root and outside diameter, the permanent stresses introduced by the placing of the pinion on the shaft, etc., all affect the stress distribution and the maximum stress. Photo-elastic analysis shows that these factors affect the stresses considerably more than would be expected from present methods of estimating. For standardized pinions the correction coefficients can only partially take account of these factors. For special pinions or for pinions of

[^7]
 not the mily (effertive w:ay lo delermat - 1 stress distribution and (o) lerate (lac matamman stress.
2.2. A detailed ablalysis of the strecs distribution delermined for different gealr jombons


Fig. 7. Lateral Extensometer Designed by P. Heymans
and under different loading conditions is given below.
23. The authors wish first to eall attention to certain interesting points brought out by photo-elastic analysis, which have been checked by tests carried out on steel sections. These are particularly interesting beeause they are unexpected.

24 . Besides the stress distribution in the different sections of the pinions represented by Fig. S, the photo-elastic analysis has given as maximum stress under normal inside ratial pressure and normal torque:
$80,000 \mathrm{lb}$. per sq. in. for tooth form $A$
$-0,3.50 \mathrm{bb}$ per sq. in. for tooth form $B$
$(30,900 \mathrm{bb}$. per sq. in. for tooth form $C$.

Moreover the 12 -tooth pinion shows, besides a smaller maximum stress, a better stress distribution.
2.). For sted pinions the maximmon stress attaned maler momal conditions, although high, appears mot to be excessive. Tooth ( appeard to be a better design under normal comditions.
the inside and outside ratii. The opinion generally expressed is that for the case of the pinion the maximum stress will be intermediate between the maximum values obtained for rings of which the outside diameters are respectively equal to the root diameter of the tonth and to the outside diameter of the pinion, the inside bore being the same.
${ }^{2} 7$. Photo-elastic analysis shows that the gear pinion is ewen weaker than the plain circular ring whose outside diameter is equal to the root diameter of the tooth. The change of external profile, due to the presence of the teeth, although requiring an addition of material, weakens the structure.

2s. Figs. 9 and 10 show the steel specimens after haring been tested by: forcing a tapered plug into the bore; and Table I gives the rupture load applied to the tapered arbor forced into the bore for the different specimens. These confirm the photo-elastic results.
29. Previous to the photo-elastic investigation of the stresses due to radial inside pressure in pinion sections, fracture due to pure radial inside pressure would have been expected to occur through the minimum radial cross-section.
30. From Fig. 2,* representing the color image obtained in the photoelastic analysis, it appears that the regions under the tecth are under higher stress and that the points at the inside boundary right under the teeth are points of maximum stress.
31. Fig. 10 gives the fracture obtained on steel sections. Two of the sections show fractures right through the thickest layer of material, while all of them started at points where the photo-elastic analysis had re.realed maximum stress. The unevenness of the material must account for the deviation of the fracture in one of the cases.
26. The stresses due to shrinking or forcing the pinion on the shaft can only be estimated. The pinion may be assumed to be a plain circular ring, for which case the stresses may be mathematically computed. The stress at any point of the ring as well as the maximum stress in the ring depends upon the lengths of

[^8]32. Can any statement be made as to the causes of the failure by inspection of the shape of the fracture? In the case in which the authors were interested, the photo-elastic analysis determined the best design. As before said, either the placing of the pinion on the shaft, if carelessly done, for instance by pounding the pinion heavily on the tapered
shaft, or excessive torque and hows due to sudden meshing or the taking on of a heary load, will set up) dangerous stresses.

TABLE I

## RUPTURE LOAD ON ARBOR FORCED INTO SPECIMENS TESTED


33. The authors' photo-elastic analysis has shown that the sections of dangerous stresses


Fig. 11. Fatigue Failures of Teeth Produced by Experiment (without Radial Pressure in Bore)
are different for different values of inside radial pressure and applied torque load.
34. The fracture shown in Fig. 11 is of an open V-shape. Photo-elastic analysis shows that the higher the inside radial pressure becomes, for a given torque load, the sharper becomes the $V$-shape of the section of dangerous stresses. (Fig. 12.) If the fracture is due to too high a torque load, the angle of the V will approach 180 deg. Tests on stecl sections have been made with a specially built impact machine.
35. Without inside radial pressure the fracture obtained is a straight line through the root section of the tooth. With increasing pressures the $V$-shaped fracture becomes sharper. For an inside radial pressure exceeding the elastic limit, however, the observation does not hold. The reason for this departure from what the photo-elastic method had predicted is to be found in the fact that beyond the elastic limit the stress-and-strain relation
no longer follows Ifomke's latw ! stresses set up in the steed phum, shrinking proness no longer antapora those set up) in the colluthidmendel.
36. White the that shaje of the break in Fig. 11 is onse limiting case (torgue withont radial shrinking pressure), Fig. It may heormsidered as the other limiting case (rarlials shrinking pressure without torque , showing a $V$-shaped fracture for which the angle of the V has become equal to zero.

37 . It maty be concluded, then, that the inspection of the fracture may be a means of determining the cause of the failure. In this way, possibly, the responsibility may be established between builder and customer as regards pinion mounting


Fig. 12. Fatigue Failures of Teeth Produced by Experiment (with Heavy Radial Pressure in Bore

The Detailed Stress Analysis
38. External Forces Applied to the Pinion When in Service. The pinion is shrunk onto the shaft after having been bored so as to fit the shaft at a temperature of 160 deg. F . above normal room temperature.
39. In normal working conditions, the torque load to which the pinion is subjected corresponds to a tractive force of 500 lb . per inch of face of the tooth, tangent in direction to the pitch circle. The whole torque is supposed to be transmitted by a single contact.
40. Calling respectively $\widehat{\text { or }}$ and $\widehat{\theta \theta}$ the radial and the tangential principal stress in a circular ring, of which the outside diameter equals the root diameter of the teeth, the inside bore being the same as the pinion bore, $(\widehat{r r}-\widehat{\theta \theta})$ $=25.500 \mathrm{lb}$. per sq. in. for $\Delta t=160 \mathrm{deg} . \mathrm{F}$. This value of ( $\widehat{r r}-\hat{\theta \theta}$ ) is the stress value of the color bands obtained in polarized light (isochromatic bands), and will therefore be used
in the stress antalysis of the rellaloid model to seotre the right expemsion pressure before the torque is appled. For ratial pressures hioger than this bomat shrinking pressure, the same characteristic of the $(r r-0 \theta)$ value will be 1 sed.
11. The tangential tractive foree is applied at varying distances from the root of the tooth, depending won the point of eontact. The most mationable conditions arise when this


Fig. 13. Frame Used for Applying Loads to Celluloid Models of Pinions stresses.
1.1. 'The first sets of measurements were made ander normal inside pressure and maximam torguc loatl. Figs. 1.1 represents the lines of principal stress, deduced from the isoclinic bancls. 'The tangents to these lines represent at each point the directions of the principal
45. Fig. "2* gives the colored image when the normal inside pressure alone is applied, whereas Figs. :3* and 4* give the image obtatined when both the normal inside pressure and the maximum torque are applied. An optical measurement on the image shown in Fig. 2* allows one to adjust properly the amount of inside pressure before the torque is applied.
46. The determination of the values of the difference $(p-q)$ of the principal stresses is made on the image shown in Fig. 4.* One of the two principal stresses vanishes at a boundary where no external forces are applied. In this case the optical measurements of the values of $(p-q)$ give directly the values of the tangential stress.
47. Inside of the body the optical measurements are supplemented by measuring the transverse change of
force is applied at the top of a single tooth. Moreover the starting torque load being higher than that realized under normal running conditions, the applied tractive force was brought up from 500 lb . to 1500 lb . per inch of face.
42. Let us for convenience call:
a. The normal inside pressure, the value of $25,500 \mathrm{lb}$. per sq. in. for ( $\widehat{r r}-\widehat{\theta \theta}$ ), corresponding to a shrinking pressure due to a temperature variation of 160 deg . F .
$b$. The maximum torque, the torque corresponding to a tractive load $F$ of 1500 lb . applicd normally to the contour of the tooth (condition of contact) at the top of one pinion tooth.
c. The normal torque, the torque corresponding to a tractive load $F$ of 500 lb . applied under the same conditions as above.
d. Increased inside pressures, the values of ( $\overline{r r}-\widehat{\theta \theta}$ ) exceeding the normal inside pressure, as defined above.
43. The Photo-Elastic Analysis. Fig. 13 represents the frame used for the loading of the models. A tapered expansion ring is used to produce the radial inside pressure. The torque is measured by properly mounted dynamometers.

[^9]thickness, which gives the values of the sum $(p+q)$ of the principal stresses.

TABLE II
VALUES OF THE PRINCIPAL STRESSES ACROSS THE MINIMUM CROSS-SECTION OF THE LOADED TOOTH

| Tenths of Distance <br> $A B$ (Fig. 15$)$ <br> $M$ leasured from $A$ | Lb. per Sq. In. | Lb. per Sq. In. |
| :---: | :---: | :---: |
|  |  |  |
| 0 | 0 | 72,600 |
| 0.1 | 13,850 | 57,300 |
| 0.2 | 10,450 | 49,000 |
| 0.3 | 3,710 | 41,700 |
| 0.4 | $-10,620$ | 25,800 |
| 0.5 | $-20,300$ | 18,700 |
| 0.6 | $-29,000$ | 11,900 |
| 0.7 | $-40,000$ | 9,000 |
| 0.8 | $-51,900$ | $\cdots \cdots$ |
| 0.9 | $-65,700$ | 5,320 |
| $B$ | $-80,000$ | 0 |

48. From the values of the principal stresses at a given point it is easy to obtain the stress on a section in any given direction at that point. Moreover, as said before, the two principal stresses represent respectively the maximum and the minimum stress. Thus the larger of the principal stresses will always
give at each point the maximam stress in direction and magnitude.
49. At the edges where one of the principal stresses has vanished the values of $(p-q)$ and $(p+q)$ must correspond, i.e., the optical determination of $(p-q)$ and the determination of $(p+q)$ must check.
50. Also if we know the total foree acting normally to a given section, the graphical integral of the curve, obtained by plotting the resultant stresses acting normally to this section, must correspond to the total force. In the case of the pinions the data for such a check are not available.
51. Table II gives the values of the principal stresses through the minimum cross-section of the pinion tooth, to which the load is applied. The results given in this table have been plotted in Fig. 15. At each point where measurements have been made the two principal stresses have been plotted in direction and in magnitude, the arrows serving to distinguish between tension and compression. At the points $A$ and $B,(p-q)$ and $(p+q)$ must check: they differ for $A$ by 0.9 per cent and for $B$ by 0.8 per cent.
52. The maximum tension occurs at $A$ and is equal to $72,600 \mathrm{lb}$. per sq. in. The maximum compression occurs at $B$ and is equal to $80,000 \mathrm{lb}$. per sq. in. This difference between the absolute values of these stresses is of course due to the pressure on the inside of the pinion, which affects the tension and the compression stresses differently.
53. Figs. 16 and 17 give the values of the tangential stresses along the edge of the tooth on which the load is applied. The numerical results of Table III have been plotted in Fig. 16, this table giving the tangential stresses at the tension side. Also the numerical results of

TABLE III
VALUES OF THE TANGENTIAL STRESS AT THE BOUNDARY OF THE LOADED TOOTH-TENSION SIDE

| No. of Point in Fig. I6 | Lb. per Sq. In. |
| :---: | :---: |
|  | 41,000 |
| 2 | 54,100 |
| $3(A)$ | $72,30072.750$ |
| 4 | 73,200 |
| 5 | 64,800 |
| 6 | 57,600 |
| 7 | 54,100 |
| 8 | 41,000 |
| 9 | $\cdots \cdots \cdots$ |

[^10]

Fig. 14. Lines of Principal Stress Determined by Polarized Light-Normal Inside Pressure and Maximum Torque Load


Fig. 15. Curves showing the Two Principal Stresses in Direction and Magnitude for Points along the Section $A B$

TABLE IV
VALUES OF THE TANGENTIAL STRESS AT THE BOUNDARY OF THE LOADED TOOTH-COMPRESSION SIDE

$$
\begin{array}{cc}
\text { No. of Point in Fig. } 17 & \text { Lb. per Sq. In. } \\
& \\
1 & 20,500 \\
2 & \pm 1,000 \\
: 3(B) & 79,500 \quad \mathrm{SO} .000^{1} \\
4 & 80,000 \\
. & 82,200 \\
6 & 60,000 \\
\hdashline & 29,000 \\
8 & 0
\end{array}
$$

[^11] table givine: these stresses ont the eompression side. Simen no external load is applied at this
 withe lamsutial stresses up) to the top of the 1004h


Fig. 16. Tangential Stress at Tension Side-Normal Inside Pressure and Maximum Torque

5t. Table V' and Fig. 1s give the numerical and plotted values of the stress difference $(\widehat{r r}-\widehat{\theta \theta})$ along the inside boundary of the pinion, the normal inside pressure and the torque load being applied. A circular ring to which a uniform inside pressure is applied will show concentric isochromatic bands. The deflections of those bands (Fig. 2)* in the case of the pinion show the disturbance due to the presence of the teeth.
55. When the maximum torque is applied, the values obtained for $(\widehat{r r}-\widehat{\theta \theta})$ give the curve of Fig. 18. The colored images as well as the diagrams show that the load applied at the top of one tooth extends its influence as far as the inside boundary of the pinion. The combination of the inside uniform pressure, already disturbed by an irregular outside boundary, with irregularly distributed stresses-tensions in certain parts and compressions in othersdue to the torque load, do not of course give a resultant stress distribution which shows any symmetry with respect to the point of contact. The upper pinion being the driving pinion, it may be seen on the colored image (Fig. 3)* that the stresses vanish rather rapidly in the withdrawing part, but that the penetration extends much farther into the approaching part.
56. It may also be interesting to point out that there is a zone of zero stress inside of the pinion under the root of the tooth when the torque load is applied. This is shown on the diagram of the lines of principal stress (Fig. 14) by the converging of the lines of principal

[^12]stress, as several lines of principal stress can only intersect where the principal stresses vanish.
57. The puestion of enginecring interest was to find the relative influence of the factors which affeet the maximum stress, and the ant hors therefore variced the values of:
a. The inside normal pressure
b. The worque load.

TABLE V
VALUES OF ( $\widehat{r}-\widehat{\theta})$ ALONG THE BOUNDARY OF THE BORE

| No. of Pront in Fis. 18 | Lb. per Sq. In. |
| :---: | :---: |
| 1 | 36,600 |
| $\because$ | 54,100 |
| 3 | :36,600 |
| 4 | 18,100 |
| j | 41,000 |
| 6 | 61,500 |
| 7 | 43,500 |
| 8 | 38,700 |

58. The values of $(\widehat{r r}-\widehat{\theta \theta})$ along the inside boundary when the maximum torque load is applied are given in Table VI and have been plotted in Fig. 19 for the case of reduced inside pressure. The colored image did not show noticeable variation across the minimum cross-section $A B$ and along the outside edges of the main tooth. The influence of the inside


Fig. 17. Tangential Stress at Compression SideNormal Inside Pressure and Maximum Torque
pressure on the above-mentioned limit does not affect materially the regions of maximum stress, due in this case to the torque load.
59. Fig. i* shows the image obtained for normal pressure and reduced torque. Having applied 0.7 of the maximum torque value, the
stresses showed at gememb reduction in the region of high stress. The values of the tangential stresses along the temsion side of the Gonndary of the main woth are given in Table V'll and are photed in Figs 20. This should be comparel with the same diagram (Fig. 16) for TABLE Vi
VALUES OF $(\overparen{r r}-\widehat{\theta \theta})$ ALONG THE BOUNDARY
OF THE BORE (Maximum torque - reduced radial pressure)

No. of Point in Fig. In

$$
\text { Lb. } \begin{aligned}
& (\widehat{r r}-\overparen{\theta \theta}) \\
& \text { per } \mathrm{S}_{1} \text {. In. }
\end{aligned}
$$

37,600
$30,600)$
20,500
14,550
20,500
36,600
54,100
54,100
$+1,000$
20,500
the case where the full load is applied. The maximum tension has dropped from 73,200 lb . per sq. in. (Table II) to $\overline{-7.700 ~ l b}$. per sq. in. (Table VII): i.e., it has been reduced to 0.S of its previous value. The fact that it has dropped only to 0.s, whereas the torque was reduced to $0 . \overline{7}$. is explained by the permanent stress due to the inside radial pressure which had been maintained at its previous value. A reduction of the torque load has as a result a reduction of the maximum stress. We shall see later that this is not always the case.
it will le this internal pressure wha
a prepmaterat influcnce
(i). Pinions have beren examiney whe ,



Fig. 18. Stresses along the Inside of Bore, with Normal Pressure $128,820 \mathrm{lb}$. and Maximum Torque

TABLE VII
VALUES OF THE TANGENTIAL STRESS ALONG THE BOUNDARY OF THE LOADED TOOTH-TENSION SIDE
(Normal inside pressure - reduced torque)

| No. of Penint in Fig. 20 | Lh. per $\mathrm{Sq}_{\mathrm{q}}$. In. |
| :---: | :---: |
|  |  |
| 1 | 30,700 |
| 2 | 51,500 |
| 3 | 58,500 |
| 4 | 57.700 |
| .7 | 56,600 |
| 6 | 51,500 |
| 7 | 38,000 |
| 8 | 19,500 |



Fig. 19. Stresses along the Inside of Bore with Decreased Pressure ( $18,100 \mathrm{lb}$.) and Maximum Torque


Fig. 20. Tangential Stress at Tension Side-Normal Inside Pressure and Rejuced Torque
60. When the inside radial pressure is increased in such proportion that without any torque being applied it produces stresses at the ontside boundary of the gears of a magnitude approaching that due to the torque load,

1b. per sq. in. at the inside boundary with the torque load at its normal value of 500 lb . tractive force per inch of face. The tractive force was afterward brought up to its maximum value of 1.500 lb .
（i）．These kests showed that the torque hate when applied to the pinion subjected to those increassed ralial pressures，affeets only． the distribution of the stresses．It makes the high stresses extem oner a larger area，but it thes mot increase materially the maximum
sections，passing respectively through the points $A$ and $l$ of the minimum cross－section of the main tooth，the prints of maximum lension and compression．
（i）．The values of $(p-q)$ were deduced from the colored image of Fig． $\mathrm{I}^{*}$ Extensom－


Fig．21．Principal Stresses Across Radial Sections of Tooth－
Normal Inside Pressure and Maximum Torque
stress．In these cases the dangerous section is no longer a straight section through the root of the tooth but it follows a V－shaped line，the lower point of which lies toward the inside bore．The sharpness of the angle of the V － shaper fracture at the base of the tooth appears to be due to an excess of radial shrink－
eter measurements of $(p+q)$ were made．As before，the scales of both measurements were determined so that the stresses in the models should represent the stresses in the steel pinion．
（i．）．The maximum torque and the normal inside pressure were applied．Table VIII and Figs． 21 and 22 give the values obtained．Fig．


Fig．22．Principal Stresses in Direction and Magnitude for Same Radial Sections as Those Shown in Fig． 21
ing pressure．In practice this excess is due to the pounding of the pimion onto the tapered shaft past its normal position．
（i3．In this connection a study was made of the stress distribution through two radial
＊See Frontispiece of this issue of the Review．

21 gives the magnitude of the principal stresses along the two sections $A A^{\prime}$ and $B B^{\prime}$ ． Fig． 22 gives a portion of the lines of principal stress taken from Fig．14，and for the same sections $A A^{\prime}$ and $B B^{\prime}$ shows the two principal stresses plotted in direction and in magnitude．

TABLE VIII
VALUES OF THE PRINCIPAL STRESSES ACROSS THE RADIAL SECTIONS PASSING RESPECTIVELY THROUGH THE POINTS $A$ AND $B$ OF THE MINIMUM CROSS-SEC. TION OF THE LOADED TOOTH

Cross-Section $1 B^{\prime}$
Fig. 21 ;
Distance in Inches from Point B

| $0.410(B)$ | 79.900 | 0 |
| :--- | ---: | ---: |
| $0.33-1$ | 5.5000 | 6,000 |
| 0.256 | 39,000 | 15,200 |
| 0.179 | 32,600 | 18,400 |
| 0.102 | 27.100 | 23,500 |

Cross-Section A. $\mathrm{I}^{\prime}$
Fig. 21:
Distance in Inches
from Point A'

|  |  |  |
| :--- | ---: | ---: |
| $0.410(A)$ | 0 | 69,350 |
| 0.334 | 2,350 | 25,400 |
| 0.256 | 2,700 | 10,300 |
| 0.179 | 0 | 0 |
| 0.102 | 11,350 | 3.350 |

66. A good way to visualize the state of stress at a given point is to consider a rectangular element with its sides parallel to the
two principal stress directions at that penat 13y considering such elements along the se tions $A A^{\prime}$ and $B B^{\prime}$ (Fig. 22) from this vell point, one can form a mental pieture of low the section is acted upon by the clastic forces
67. It would require too much space to include in this article a full discussion and tomake a complete report of the results summarized here. The authors trust that the material they have presented will stimulate those interested in this subject to further efforts in the development and use of the photo-clastic methorl.

6S. It seems, finally, almost superfluons to call attention to the comparative ease with which such a stress problem as this can be handled by the photo-elastic method, whereas the use of ordinary engineering methods gives untrustworthy results and the exact mathematical solution based upon the theory of clasticity is impossible.
69. Acknowledgment is due to the Massachusetts Institute of Technology for permission to use in this article certain of the results included in the thesis submitted by Dr. Paul Heymans, University of Ghent, Belgium, as partial fulfillment of the requirements for the degree of Doctor of Science from the Institute.


# Graphs for Calculation of Electron Emission from Tungsten, Thoriated Tungsten, Molybdenum and Tantalum 

By Salol Dushman and Jessie W. Ewald<br>Resharche Laboratory, General Eeectric Company

In the operation of electron tubes such as are used in radio work and related fields, the most important problem is that regarding the maximum electron emission that may be obtained under any given conditions and the efficiency of this emission, that is, the relation between electron current and watts consumed in the cathode. The present article gives eharacteristic emission data and eurves for four different metals, and also certain fundamental relations which should prove of assistance in the design of thermionic devices.-Editor.

## 1. Equation for Electron Emission

The generally accepted equation for electron emission as a function of the temperature is that first enunciated by 0 . W. Richardson. This equation is ordinarily expressed in the form

$$
\begin{equation*}
I=A_{1} \backslash \bar{T}_{\epsilon}^{-b / T} \tag{1}
\end{equation*}
$$

where $I$ denotes the electron emission per unit area at the absolute temperature $T$,* and $A_{1}$ and $b$ are constants for any one substance.

On the basis of the second law of thermodynamics and the assumption that evaporation of electrons from a metal can be considered as thermodynamically equivalent to the evaporation of a monatomic gas, S . Dushman $\dagger$ has recently derived the following relation for the electron emission as a function of the temperature.

$$
\begin{equation*}
I=A T^{2} \epsilon^{-b_{0} / T} \tag{2}
\end{equation*}
$$

where $A$ is a universal constant, and $b_{0}$ is the only specific constant whose value varies with the nature of the emitting surface.

If the electron emission $I$ is expressed in amperes per square centimeter, the constant $A$ has the value 60.2 . Introducing this value into equation (2) and converting to ordinary logarithms, this equation may be written in a form which is more convenient for calculations, thus:

$$
\begin{equation*}
\log I=1.7792+2 \log T-\frac{b_{0}}{2.303 T} \tag{3}
\end{equation*}
$$

Fig. 1 shows a series of graphs of this equation in which $\log I$ is plotted as ordinate against $b_{0}$ at constant value of $T$. It will be

[^13]observed that for two substances at the same value of $T$,
\[

$$
\begin{equation*}
\log I^{\prime}-\log I^{\prime \prime}=\frac{b_{0^{\prime \prime}}-b_{0}{ }^{\prime}}{2.30: 3 T} \tag{4}
\end{equation*}
$$

\]

where $I^{\prime}, b_{0}{ }^{\prime}$ and $I^{\prime \prime}, b_{0}{ }^{\prime \prime}$ refer to each substance respectively. Thus for tungsten, $b_{0}{ }^{\prime \prime}$ $=52,600$, while for thoriated tungsten $b_{0}{ }^{\prime}$ $=34,100 . \ddagger$ According to equation (4) it follows that at $T=1.500$,

$$
\log I^{\prime}-\log I^{\prime \prime}=.5 .356
$$

or

$$
I^{\prime} I^{\prime \prime}=2.27 \times 10^{5}
$$

That is, at $T=1500$, the electron emission from thoriated tungsten is 227,000 times as great as that from pure tungsten.

The plots in Fig. 1 show that as the temperature increases, the value of ratio $I^{\prime} / I^{\prime \prime}$ for any two substances decreases.

Table I gives values of $b_{0}$ for different substances as determined in this laboratory. These values are based on the temperature scale for tungsten as derived by A. G. Worthing and IV. E. Forsythe.§

TABLE I

| Substance |  | $b_{0}$ |
| :---: | :---: | :---: |
| Tungsten |  | 52,600 |
| Molybdenum | 1 | 50,000 |
| Tantalum |  | 46,500 \\| |
| Thorium |  | 34,100 |
| Calcium |  | 26,000 \\| |

## 2. Electron Emission from Tungsten, Thoriated Tungsten, Molybdenum and Tantalum

By means of these values of $b_{0}$, the values of $\log I$ and $I$ at different values of $T$ have been calculated according to equation (3). Table II gives the data for tungsten, thoriated tungsten, molybdenum and tantalum.

While this table gives values at 100 deg. intervals, values of the electron emission at intermediate temperatures may be obtained
with a satisfactory degree of aceuracy by linear interpolation between the nearest tabulated values of loy $I$.

Figs. 2 and 3 give the electron emission for tungsten, plotted on scmi-log paper against the absolute temperature, while Fig. 4 gives simikar data for thoriated tungsten. As the thorium evaporates rapidly at temperatures above 2300 deg. $K$ and emission data below 1.500 deg. $K$ are of no practical interest.
at any temperature $T$ is expre an los the relation
$\log E=3.680\left(\log T-3.3(1)-\frac{1010}{T}+1500\right) \quad \mathrm{S}$
where $E=$ watts $\mathrm{cm} .^{2}$, and ordinary logs are used.

Fig. is gives a graph of this relation on scmi-log paper. From these data and the values of the electron emission, Fig. (; has


Fig. 1. Plot of Equation for Electron Emission
only the data for the interval $1.500-2300$ deg. $K$ are given in the plot.

## 3. Energy Radiated from Tungsten and Efficiency of Emission

From the point of view of the engineer and designer of racuum tubes it is of importance to know the electron emission per watt consumed in heating the cathode. According to A. G. Worthing and W. E. Forsythe* the energy radiated from tungsten

[^14]been plotted to show the electron cmission per watt at any temperature, for tungsten, and Figs. 7 and is for the electron emission and also electron emission per watt at any given value of the watts per cm. ${ }^{2}$ The arrows indicate the scales to be used.

Assuming that the energy radiated from a thoriated tungsten surface is the same as that from pure tungsten, it is possible to calculate similar data for thoriated tungsten. Fig. 9 shows the electron emission per watt as function of $T$, and Fig. 10 shows the electron

TABLE II
ELECTRON EMISSION FROM TUNGSTEN, THORIATED TUNGSTEN, MOLYBDENUM, AND TANTALUM

|  | 11 |  | 'T'\% |  | Mo |  | T/ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Wers h | lan 1 | 1 | $\log 1$ | 1 | 108:1 | 1 | 108:1 | 1 |
| Soo |  |  | 11.08 | $1.20 \times 10^{11}$ |  |  |  |  |
| ! 100 |  |  | !.2:3 | $1.70 \times 10^{-9}$ |  |  |  |  |
| 10101 |  |  | S.: 16 | $9.12 \times 10^{8}$ |  |  |  |  |
| 1100 |  |  | (i. 41$)$ | $2.51 \times 10^{6}$ |  |  |  |  |
| 1200 |  |  | -. 60 | $3.95 \times 10^{5}$ |  |  |  |  |
| 1:300 |  |  | 4.150 | $3.98 \times 10^{-4}$ |  |  |  |  |
| 1400 | 9.76 | $5.75 \times 10^{9}$ | 3.49 | $3.09 \times 10^{-3}$ | S.50 | $3.63 \times 10^{-8}$ | 7.65 | $4.47 \times 10^{-7}$ |
| 1500 | ス.90) | $7.94 \times 10^{8}$ | -3.20 | $1.80 \times 10^{-2}$ | $\overline{7.66}$ | $4.57 \times 10^{-7}$ | 6.67 | $4.68 \times 10^{-6}$ |
| 1600 | 7.91 | S.13×10 $0^{-7}$ | $2.9 \%$ | $8.51 \times 10^{-2}$ | ¢,6\% | $4.17 \times 10^{-6}$ | 5.57 | $3.72 \times 10^{-5}$ |
| 1700 | $\overline{6.80}$ | (i.3) $1 \times 10^{-5}$ | 1.5 .3 | $3.39 \times 10^{-1}$ | 5.47 | $2.95 \times 10^{-5}$ | 4.36 | $2.29 \times 10^{-4}$ |
| 1800 | 5.60 | $3.98 \times 10^{-5}$ | 0.06 | 1.15 | 4.23 | $1.70 \times 10^{-4}$ | -3.08 | $1.20 \times 10^{-3}$ |
| 1900 | 4.33 | $2.14 \times 10^{-1}$ | 0.55 | 3.55 | 4.92 | $8.32 \times 10^{-4}$ | $\overline{3} .71$ | $5.13 \times 10^{-3}$ |
| $\because 000$ | 4.90 | $9.12 \times 10^{-4}$ | 0.98 | 9.55 | 3.54 | $3.31 \times 10^{-3}$ | 2.29 | $1.95 \times 10^{-2}$ |
| 2100 | $\overline{3} .55$ | $3.5 \overline{5} \times 10^{-3}$ | 1.37 | 23.44 | 2.08 | $1.20 \times 10^{-2}$ | $\overline{2.808}$ | $6.43 \times 10^{-2}$ |
| 2200 | 2.07 | $1.17 \times 10^{-2}$ | 1.73 | 5.3 .70 | 2.i) ${ }^{\text {a }}$ | $3.89 \times 10^{-2}$ | $\underline{1.285}$ | $1.93 \times 10^{-1}$ |
| 2300 | $\underline{2.57}$ | $3.71 \times 10^{-2}$ | 2.07 | 117.50 | 1.06 | $1.15 \times 10^{-1}$ | 1.723 | $5.28 \times 10^{-1}$ |
| 2400 | 1.023 | $1.05 \times 10^{-1}$ |  |  | 1. 49 | $3.09 \times 10^{-1}$ | 0.126 | 1.34 |
| 2500 | 1.438 | $2.74 \times 10^{-1}$ |  |  | 1.8! | $7.76 \times 10^{-1}$ | 0.497 | 3.14 |
| $\because 600$ | 1.825 | $1.68 \times 10^{-1}$ |  |  |  |  |  |  |
| 2700 | 0.183 | 1.is |  |  |  |  |  |  |
| $\underline{8800}$ | 0.51 S | 3.30 |  |  |  |  |  |  |

emission and emission per watt as a function of the watts per $\mathrm{cm} .^{2}$

Table III gives ralues of $E$ (watts/cm. ${ }^{2}$ ), and $I E$ (electron emission per watt) at 100 degree intervals for tungsten and thoriated tungsten.

## 4. Lead Loss Correction

In practice the whole of the filament whieh is used as electron emitter is, of course, never at the maximum temperature. The temperature decreases more or less gradually to a very low value as the leads are approached. Consequently only a certain fraction of the total area of the filament is effective in emitting eleetrons. The magnitude of this fraction depends in a complieated manner upon the total length of the filament, the temperature, and the value of $b_{0}$.

Relations have been derived by Dr. I. Langmuin* for calculating the value of the factor $f$ which comnects the obseried electron emission under any given conditions with the emission which would be obtained if the

[^15]whole of the filament were effective. Thus, if $i$ denotes the observed emission from a given

## TABLE III

ENERGY RADIATED FROM TUNGSTEN
Also Efficiency of Electron Emission for Pure
Tungsten and Thoriated Tungsten

| $\stackrel{\text { T }}{\text { Deg. K) }}$ | $\underset{\text { watts/cm? }}{\mathrm{E}}$ | I/E (amps./watt) |  |
| :---: | :---: | :---: | :---: |
|  |  | W | Th. |
| 1000 | 0.570 |  | $1.59 \times 10^{-7}$ |
| 1100 | 1.008 |  | $2.51 \times 10^{-6}$ |
| 1200 | $1.663^{\circ}$ |  | $2.40 \times 10^{-5}$ |
| 1300 | 2.600 |  | $1.51 \times 10^{-4}$ |
| 1400 | $3.89)$ | $1.48 \times 10^{-9}$ | $7.94 \times 10^{-4}$ |
| 1500 | 5.632 | $1.41 \times 10^{-8}$ | $3.24 \times 10^{-3}$ |
| 1600 | 7.889 | $1.02 \times 10^{-7}$ | $1.07 \times 10^{-2}$ |
| 1700 | 10.75 | i. $.89 \times 10^{-7}$ | $3.16 \times 10^{-2}$ |
| 1800 | $14.3!$ | $2.75 \times 10^{-6}$ | $7.94 \times 10^{-2}$ |
| 1900 | 18.82 | $1.15 \times 10^{-5}$ | $1.91 \times 10^{-1}$ |
| 2000 | 24.19 | $3.80 \times 10^{-5}$ | $3.98 \times 10^{-1}$ |
| 2100 | 30.66 | $1.15 \times 10^{-4}$ | $7.58 \times 10^{-1}$ |
| 2200 | 38.30 | $3.09 \times 10^{-4}$ | 1.41 |
| 2300 | 47.30 | $7.94 \times 10^{-4}$ | 2.51 |
| 2400 | 57.77 | $1.82 \times 10^{-3}$ |  |
| 2500 | 69.82 | $3.89 \times 10^{-3}$ |  |
| 2600 | 83.77 | $7.94 \times 10^{-3}$ |  |
| 2700 | 90.74 | $1.51 \times 10^{-2}$ |  |
| 2800 | 117.7 | $2.80 \times 10^{-2}$ |  |

filament and $S$ denotes the total area of the filament, the electron emission per unit area after taking into account the lead loss correction is

$$
\begin{equation*}
I=\frac{i f}{s} \tag{6}
\end{equation*}
$$

The factor $f$ is calculated by means of the relation

$$
\begin{equation*}
f=\frac{\Gamma+\Delta I^{\prime}}{\Gamma+\Delta I-\Delta \Gamma_{H}} \tag{7}
\end{equation*}
$$



Fig. 2. Electron Emission from Tungsten at Lower Temperatures
where $V=$ voltage drop along filament

$$
\Delta V=0.00026(T-400)
$$

and $\Delta V_{H}$ is a function of $b_{0}$ and $T$.
Fig. 11 gives plots of $\Delta V_{H}$ and $\Delta I^{\circ}$ as functions of $T$ for different values of $b_{c}$.
$\Gamma+\Delta \Gamma$ corresponds to the corrected voltage drop along the filament and from this the corrected watts per $\mathrm{cm}^{2}$ of the filament may be derived. In the case of tungsten and thoriated tungsten filaments which are not too short. the temperatures may be calculated fairly accurately from the values of the corrected watts $\mathrm{cm}^{2}$ by means of equation (5) or Table III

[^16]5. Correction for "Schottky Effect"

As equation (2) was derived on the ansmm, tion that the eloceric fied strength at the cathode is zero, while in actual practure a definite anode potential is used, it is neeessary to reduce the values of the observed emission to those which would correspond to the conditions postulated in the theoretical derivation.

It was shown by Wchottky* that if $i^{\prime \prime}$ denotes the electron emission at zero field


Fig. 3. Electron Emission from Tungsten at Higher Temperatures
strength, and $i_{1}$ - denotes the observed emission at an anode voltage $I$, then

$$
\begin{equation*}
i_{1}=i_{0} \epsilon \frac{4.39 \sqrt{k 1}}{T} \tag{ী}
\end{equation*}
$$

where $k$ is a constant whose value depends upon the relative geometrical arrangement of anode and cathode. Thus for a filament of radius $r$ (in cm .) in the axis of a crlindrical anode of radius $R$.

$$
\begin{equation*}
k=\frac{1}{2303 \cdot 3 \log R r} \tag{9}
\end{equation*}
$$

In most cases, the value of $k$ can be obtained much more accurately by measuring the emission (at constant temperature of the cathode) for different values of I


Fig. 4. Electron Emission from Thoriated Tungstea


Fig. 5. Energy Radiated from Tungsten


Fig. 6. Electron Emission per Watt for Tungsten as Function of Temperature


Fig. 7. Efficiency of Emission for Tungsten as Function of Watts per cm.


Fig. 8. Same as Fig. 7 for Larger Values of Watts per $\mathrm{cm}^{2}$.


Fig. 10. Efficiency of Emission for Thoriated Tungsten as Function of Watts per cm :


Fig. 9. Electron Emission per Watt for Thoriated Tungsten as Function of Temperature


Fig. 11. Lead Loss Corrections

If $\log i_{1}$ is plotted against $\sqrt{ } \bar{v}$, a stratight line is obtaned and the value of $\log i_{0}$ may be determined bey extrapolation. The slope of this straight line, $\Delta \log i / \Delta \sqrt{V}$, varies inversely as $T$ and from equation (S) it follows that

$$
\begin{equation*}
2.303 T د \log i / \Delta,^{\prime} \bar{V}=4.39 \sqrt{k} \tag{10}
\end{equation*}
$$

Combining equation ( $(S$ ) with equation (2) it is erident that the electron emission per unit area at any voltage $V$ is given by the relation

$$
\begin{equation*}
I_{V}=60.2 T^{2} \epsilon^{-\frac{l_{0}-4.39 \sqrt{k V}}{T}} \tag{11}
\end{equation*}
$$

Hence if emission data obtained with a given anode voltage are used to calculate the ralue of $b_{0}$, this value is lower than the true calue by the amount $4.39 \sqrt{k V}$.

Table IV gives values of this correction for different cases in which $k$ can be calcu-
lated by means of equation (9), the value of $V$ being taken as 100 volts. These corrections correspond in magnitude to those which may be expected in ordinary thermionic devices.

TABLE IV
DECREASE IN $b_{o}$ AT $V=100$ FOR FILAMENT IN AXIS OF CYLINDRICAL ANODE

| Diameter of <br> Filament | Diameter of <br> Anode | $4.39 \sqrt{100 \mathrm{k}}$ |
| :--- | :--- | :--- |
| $\ldots .001 \mathrm{~cm}$. | 1.00 cm. | 747 |
| 0.005 cm. | 0.50 cm. | 409 |
| 0.005 cm. | 1.00 cm. | 381 |
| 0.01 cm. | 1.00 cm. | 289 |
| 0.1 cm. | $1.00 \mathrm{cn}.$. | 129 |
|  |  |  |

# Studies in the Projection of Light <br> Part II <br> PARABOLIC CYLINDER AND ELLIPSOIDAL REFLECTORS 

By Frank Benford

Pifisicist, Illuminating Engineering Laboratory, General Electric Company


#### Abstract

In Part I of this series, a method of optical analysis employing meridian and sagittal lines was first explained and then applied to a study of the light projecting characteristics of a reflecting paraboloid (parabolic reflector). Students of optics should familiarize themselves with this rather unique scheme of analysis because it readily permits the investigation of complicated problems and is free from the pitfalls that are present when a light source of finite size is considered as a point source. The method is applied in this installment to the analysis of the fan-shaped distribution of light from a parabolic cylinder reflector (parabolic trough). The extraordinary characteristics of this type of reflector are clearly explained. The latter half of the article is devoted to an examination of the ellipsoidal reflector whose light-gathering and projecting properties have always appeared exceptionally attractive theoretically but have been incapable of application to practice except at very low efficiency because of the lack of a suitable light source. This reflector would seem to have a very promising future now that lamps having a highly concentrated filament are becoming available.-Editor.


## PARABOLIC CYLINDER REFLECTOR

In several types of illumination, of which stage illumination is perhaps the most familiar, there is use for a reflector that will give a fartlike beam. There are two fairly simple ways of obtaining this beam formation. One is by the use of a set of cylindrical lenses in front of a parabolic mirror; and the other is by the use of a parabolic cylinder reflector, which is often called a trough reflector. The latter is much the simpler device and is very widely used.

The trough is formed by bending a flat sheet of metal so that it takes a parabolic curve, while at right angles to the curve the elements of the reflector are straight lines. The optical action is unique and is worthy of study: The analysis of the surface
is best made by means of lines similar to the meridian and sagittal lines employed in Part I of this article, but it is first necessary to redefine these surface elements to fit the changed geometrical conditions. In Fig. 7 the line $V_{0} P_{0} E_{0}$ is parabolic in form, while $V_{0} V$, the transverse axis, and $E_{0} E$, the upper edge of the reflector, are straight lines. Let us call any parabolic curve in the surface parallel to $V_{0} P_{0} E_{0}$ a sectional line, and any straight line in the surface parallel to $V_{0} V$ an elemental line. It will be noted that whereas the meridian lines of the paraboloid, previously discussed, all passed through the axis of the surface of revolution. in the case of the parabolic cylinder the sectional lines are parallel and have no crossing points. Also, the elemental lines in the
case of the latter reflector are all straight parallel lines.

Any incident ray as $r_{0}$, Fig. 7, parallel to the axis of projection $V_{0} \lambda_{0}$ will be reflected to the focal point $A$ of the parabolic section V P E. Similarly, parallel rays $r_{1} r_{2}$ in the same sectional plane will converge on the point $A$. Call the angle of convergence $i$ and the distance from the point of reflection to the focal point $p$, then

$$
\begin{equation*}
p \tan \frac{c}{2}=P P_{1} \cos \frac{a}{2}=P P_{2} \cos \frac{a}{2} \tag{1S}
\end{equation*}
$$

where the points $P, P_{1}$ and $P_{2}$ are close together on the sectional line. The incident ray $r_{0}$ lies in the intersection of a horizontal plane (determined by the elemental line $P_{0} P$ and the ray $r_{0}$ which is parallel to the axis $V_{0} X_{0}$ ) and a vertical plane cutting the surface along the parabolic sectional line. After reflection at the point $P$ the ray $r_{0}$ lies in an oblique plane determined by the elemental line $P_{0} P$ and the radius vector $p$. If the ray $r_{0}$ is rotated in the horizontal plane through the angle $e$ the reflected ray will rotate through the same angle $e$ in the oblique plane and pass through point $A_{0}$ of Fig. 7. Similarly, incident rays $r_{1}$ and $r_{2}$ will after reflection converge on $A$, and when rotated each in its own, horizontal plane through the angle $e$ the reflected rays will pass through $A_{0}$ which is thus a conrerging or focal point, providing only that the distance $P_{1} P_{2}$ is extremely small.


Fig. 7. Optical Characteristics of a Sectional Line in a Parabolic Cylinder Reflector

The convergence of the rays is changed by the rotation through the angle $e$. The length of the radius rector from $A$ to $P$ is

$$
p=F \sec ^{2} \frac{a}{2}
$$

while the radius vector from $A_{0}$ w $P^{\prime}$ is

$$
p_{e}=F \sec ^{2} \frac{a}{2} \sec e
$$

therefore

$$
p_{c}=p \sec e
$$



Fig. 8. Optical Characteristics of an Elemental Line in a Parabolic Cylinder Reflector
also

$$
\begin{equation*}
p \tan \frac{c}{2}=p_{c} \tan \frac{d}{2} \tag{20}
\end{equation*}
$$

and we get the relation

$$
\begin{equation*}
c=d \sec e \tag{21}
\end{equation*}
$$

after substituting the small angle $c$ for tan $c$ and angle $d$ for $\tan d$.

It will be shown shortly that the three rays $r_{0}, r_{1}$ and $r_{2}$ must be rotated through slightly different angles in order actually to converge upon the point $A_{0}$. and the latter is therefore not a focal point for the element $P_{1} P P_{2}$. We may place a point source at $A_{0}$ and the reflected rays at $P_{1}, P$ and $P_{2}$ will lie in parallel horizontal planes but the values of $e$ will become smaller as we pass from $P_{1}$ to $P$ and to $P_{2}$.

The physical significance of equation (20) is that a point source of light may be morerl along the line $A A_{0}$ and the reflected rays from various points in $P_{0} P$ will rotate in fixed planes that are parallel; or to take a different riewpoint, a fixed point source will have such of its light as strikes on a given elemental line $P_{\mathrm{c}} P$ reflected at various angles in a single plane. This gives the fan-like beam previously mentioned, but it remains to be seen what the other properties of this fan beam are, and in particular how the angle of spread $e$ is influenced by the proportions of the reflector.

In Fig. s a ray originating at $A_{0}$ and being reflected at the point $P$ is shown as taking the direction $P \quad r_{0}{ }^{\prime}$ after reflection. The angle between $P r_{0}{ }^{\prime}$ and $P r_{0}$, a parallel to the principal axis $T_{0} A_{0}$, is $e$, which we will
call the angle of spreme ll is uscomb to kato how tw eat the corl of the erginder so that the stmo maximumb spocett o will he obtameat frome all points alonis the ends. In Fig. (the trimgle In $P^{\prime} .1$ is shown rotaterf down into the hori\%ntial plane wsing the


Fig. 9. Location of Virtual Image Points in a Parabolic Cylinder Reflector
beus $A_{0} A$ as an axis, and the point $P$ falls on $P^{\prime}$. The length of the radius vector A $P$ is $A V^{\prime}$ (the focal length) plus $X V$, and therefore $I^{\prime} P^{\prime}$ is equal to $\mathrm{I} \mathrm{I}^{\prime}$. The triangle $A_{0} P^{\prime} A$ is shown more clearly in Fig. 9 . If the line $V_{0} l^{\prime}$ is considered to be a plane mirror, then $P^{\prime}$ is the image of $X$, ancl if $\Gamma^{\prime \prime} r_{0}{ }^{\prime \prime}$ is extended backward it will intereept the $l_{0}{ }_{0} f_{0}$ axis at $f_{1}{ }^{\prime}$. The latter point is a common crossing point for all rays reflected in the same horizontal plane, and therefore $A_{0}{ }^{\prime}$ is a virtual image of $A_{0}$. Thus a ray from $A_{0}$ striking the reflector in the same horizontal plane as $P$ will have the same I I distance and hy the construction in dotted lines in Fig . ! it is evident that for any angle $f$, which is different from $\cdot c$, the virtual mage of $A_{0}$ will fall on the same point.

We may thus regard.$_{0}{ }^{\prime}$ as the light souree; and if a total spread of say 50 deg. is desired an are of 50 deg. swung about $A_{0}{ }^{\prime}$ will include the necessary reflecting surface, 2. 5 deg. on each side of the axis, and the ends wilt be formed ber vertical planes cutting the parabolie evelinder.

The end pieces of the crlinder will themselves be parabolic in outline, with the apex of the parabola at the transwerse axis of the refleetor.

Given a parabolic evlinder with a section defined by

$$
Y^{2}=4 F . V^{2}
$$

and at desired sprearl of leam of 2e degrees. the outline of the end pieeres will be the paraboha.

$$
\begin{equation*}
J^{\prime \prime}=1!I^{\prime} \cos c^{\prime} \tag{02}
\end{equation*}
$$

atre the obligute seetion of the reflector where it is joined by the end piece will of erourse hate the same form but the developed form of the retlector end (rlotted curse $I^{\prime \prime} P$. Fig. A) will not be parabolic. The ordinates of the developerl enrve (ligg. l0) will be the developed length of the parabola of equation (20) and the abscissate will be the abscissate of the original sectional line times tan $e$, of

$$
\begin{equation*}
I^{\prime \prime}=I \tan e \tag{2:3}
\end{equation*}
$$

## Distribution of Light from Point Source

The beam from a parabolie cylinder has a highly eharacteristic outline, but its most interesting features are the internal relations between the various parts of the beam. These relations, which must be known if we are to make an intellisent or useful design of a reflector, are somewhat more complex than usttal and the ordinary rules of photometric computation do not apply.

The illumination curves of Fig . 11a were worked out as an illustration of the distribution of light in a parabolie eylinder beam. The intensity of the light from the source at $A_{0}$ falls off as the inverse square of the distance until the refleeting surface is reached. Upon reflection the light is parallel in one direction and spreads according to its dis-


Fig. 10. Development of Parabolic Cylinder Reflector of $200-\mathrm{deg}$. Opening and $80-\mathrm{deg}$. Spread
tance from $A_{0}$ in the perpendicular (horizontal) direction. The decrease in intensity. therefore follows the incerse law but not the ineerse square law. As an example, take the light radiated 60 deg. upward from the axis $(a=100$ der. in Fig. $11 b$ ) and at 30 deg.
to one side of the axis $(c=30)$ deg. Fig. 11a) This light after being reflected seems w come from the virtual mage at $t^{\prime}$ co and there is no divergence in the vertical direction, but in the horizontal direction the divergence is from the point $\mathrm{A}_{0-100}^{\prime}$ of Fig. 11a.

Let $I$ be the intensity of radiation, in candles, given off minformly in all directions. by the point source at $A_{0}$. It any point $\dot{P}$. Fig. 11a and 11 b , the normal illumination is

$$
\begin{equation*}
E_{n}=\frac{I}{p_{e}{ }^{2}} \tag{2}
\end{equation*}
$$

and from equation (19), after substituting the cosines for the secants, the expression for normal illumination at the distance $p_{e}$ is

$$
\begin{equation*}
E_{n}=\frac{I}{F^{2}} \cos ^{4} \frac{a}{2} \cos ^{2} c \tag{2.5}
\end{equation*}
$$

After reflection at the point $P$ the illumination on a normal surface will decrease as the inverse distance, hence at a distance $D$ the illumination $E_{n}{ }^{\prime}$ is in the proportion

$$
\begin{equation*}
\frac{E_{n}{ }^{\prime}}{E_{n}}=\frac{p_{e}}{D} \tag{26}
\end{equation*}
$$

or

$$
E_{n}{ }^{\prime}=E_{n} \frac{p_{e}}{I}
$$

After substituting from (2 -4 ) we get

$$
\begin{equation*}
E_{n}^{\prime}=\frac{I}{p_{e} D} \tag{7}
\end{equation*}
$$

The form of this equation is unique among equations in illuminating engineering in that it contains in the denominator two firstpower variables $p_{e}$ and $D$ instead of the single second power variable $D^{2}$ that occurs when the inverse square law applies.

One striking result of the peculiar formation of the reflected beam is that one camot measure the intensity of radiation in candles. The term "candle" can be applied only to radiation that gives illumination that decreases as the square of the distance. For this particular beam we therefore have radiation that has no name to describe its angular intensity, but the resultant illumination at a given plane may be computed as shown in equation (2) and, of course. expressed in foot-candles.

The illmmination curves of Fig. 11a are along the intersections of horizontal planes (corresponding to $a=0,20,40,60,50$ and 100 deg.) with the crlindrical surface $s$ s generated about the axis $A_{0}^{\prime} A^{\prime}{ }_{1110}$.

The illumination along the rertical lines where the planes for $c=0.10$ deg., etc, cut the cylinder is plotted in Fig. 11 b .

If the illumination on a surface mot promat but making an angle $f$ whith the juctitent light is desired, the equation of sumfan illumination is


Figs. 11 a (upper) and 11b (lower). Normal rllumination by Light Reflected from a Parabolic Cylinder; Plan and End

Elevations of Reflector
The exactness of this equation for the reflector depends upon the closeness of the light source to the ideal "point" conception. and for the usual light sources other features must be taken into consideration. This is mentioned here as a reminder that the "point source" is an excellent starting point for theories of photometry, but the application of these theories to practice must usually be preceded by an expansion of the theories to cover the peculiarities of the source under investigation.

## ELLIPSOIDAL REFLECTOR

## Distribution of Light from Point Source

One of the most interesting jroperties of the ellipse or ellipsoid is the fact that light generated at one focal point is reflected to
the other focal point, and thus the two foci are conjugate in the optical sense as well as in the geometrical sense. This being the case it is at once evident that the ellipsoid is a surface womlerfully adapted for collecting light on all sides of a light source and


Figs. 12a (upper), 12b (middle) and 12c (lower). Three Examples of the Approach of Reflected Light to Parallelism with the Axis of an Ellipsoidal Reflector
projecting it to a common point. For this reason, one might think that the ellipsoid should be frequently encountered in practice whereas there are extremely few actual applications. This form of reflector will without duubt in the future see wide use in the illuminating art, and it is purposed to set down here some of the fundamental optical properties of the surface and show why at the present time its application is so limited.

In Fig. 121) is shown an ellipse with an ellipticity $e$ of 0.812. , or

$$
\begin{equation*}
c=\sin f=\frac{\sqrt{m^{2}-n^{2}}}{m} \tag{29}
\end{equation*}
$$

where $m$ is the semi-major axis $C A$ and $n$ is the semi-minor axis $C \mathscr{C}$.

The point source of light is located at the left focal point $O$, Fig. 12a, and a ray radiated at an angle of 90 deg. from the axis, after reflection at the point $P$, will cross the axis at the conjugate focus at an angle of 10 deg. .54 min . After the second reflection at $P^{\prime}$ the angle at $O$ will be 1 deg. 14 min . This approach of the reflected ray to the major axis continues indefinitely, and ultimately the light will pass back and forth in coincidence with the major axis. It is this feature of an approach to parallelism that makes the ellipsoid seem a useful optical surface, and with the development of manufacturing optics the ellipsoid may find wide service where a moderate concentration of light is desired.

The manner in which the light comes into a path nearly parallel with the axis is shown in Figs. 12a, 12b, and 12c, and also in Table I where the plus $(+)$ sign indicates a path toward the right and the minus ( - ) sign a path toward the left.

The radiation from the source is assumed to be equal in all directions, but after the first reflection the bulk of the light passes through the $O^{\prime}$ focus in the positive direction and only a small part has a backward direction. On the second reflection all the light has a negative direction and the whole quantity of light is thereafter positive and negative in direction of passage.

In the particular ellipse chosen there is 90 per cent of the light reflected with a component to the right, and only 10 per cent with a component to the left. This is a high collecting efficiency for a reflector, and if the ellipsoid is cut off along the section $P_{3} P_{4}$. Fig. 12c, the direct radiation, amounting to 10 per cent, that was turned to the left will now radiate directly out through

TABLE I
Fig. 12a

| Radiation | $b=90^{\circ}$ | $0^{\prime} 0^{\prime \prime}$ |
| :---: | :---: | :---: |
| 1st reflection | $c_{1}=+11^{\circ}$ | $54^{\prime} \quad 0^{\prime \prime}$ |
| Qnd reflection | $b_{2}=-1^{\circ}$ | $14^{\prime} 0^{\prime \prime}$ |
| 3 rd reflection | $c_{2}=+0^{\circ}$ | $7^{\prime} 44^{\prime \prime}$ |
| the reflection | $b_{3}=-0^{\circ}$ | $0^{\prime}+8^{\prime \prime}$ |
| Sth reflection | $c_{3}=+0^{\circ}$ | $0^{\prime} 5^{\prime \prime}$ |
| bith reflection | $b_{4}=-0^{\circ}$ | $0^{\prime} 0.5{ }^{\prime \prime}$ |

Radiation....
lst reflection.
2nd reflection.
3rd reflection.
th reflection.
5th reflection.
bth reflection.

$$
\begin{aligned}
& b=90^{\circ} \quad 0^{\prime} \quad 0^{\prime \prime} \\
& c_{1}=+11^{\circ} 54^{\prime} \quad 0^{\prime \prime} \\
& b_{2}=-1^{\circ} 14^{\prime} 0^{\prime \prime} \\
& c_{2}=+0^{\circ} 7^{\prime} 44^{\prime \prime} \\
& c_{3}=+0^{\circ} \quad 0^{\prime} 5^{\prime \prime} \\
& b_{4}=-0^{\circ} \quad 0^{\prime} 0.5^{\prime \prime}
\end{aligned}
$$

Fig. 12b

$$
\begin{aligned}
& +125^{\circ} 40^{\prime} \quad 0^{\prime \prime} \\
& \begin{array}{cc}
35^{\circ}+0^{\prime} & 0^{\prime \prime} \\
3^{\circ} 90^{\prime} & 0^{\prime \prime}
\end{array} \\
& \text { - } 3^{\circ} 20^{\prime} 0^{\prime \prime} \\
& \begin{array}{l}
+0^{\circ} 20^{\prime} 42^{\prime \prime} \\
-0^{\circ}-8^{\prime \prime}
\end{array} \\
& +\quad 0^{\circ} 0^{\prime} 13^{\prime \prime}
\end{aligned}
$$

Fig. 12c
$\begin{array}{rll}+168^{\circ} & 6^{\prime} & \Omega^{\prime \prime} \\ 90^{\circ} & 0^{\prime} & 0^{\prime \prime}\end{array}$
$-11^{\circ} 54^{\prime} 0^{\prime \prime}$
$+\quad 1^{\circ} 14^{\prime} 0^{\prime \prime}$
$+\quad 0^{\circ} 0^{\prime} 48^{\prime \prime}$
the opening and the entire light from the unit will pass out of the open end of the ellipsoid in a positive direction.

The radius of the circle about the left focus of Fig. 13 represents the intensity of radiation from the light source, and the oral curve about the right focus is the radiation about the image formed on the first reflection. The intensity along the axis in the positive direction is multiplied by nearly a hundred, while in the negative direction the intensity is about one-hundredth.

It might be here remarked that the area of a photometric distribution curve is never a direct measure of the total quantity of light. The quantities of light about the two foci are of course equal if the ellipsoid is complete.

The radius rector (or path of incident ray) at any angle $b$, Fig. 13, is

$$
\begin{equation*}
r=\frac{m\left(1-c^{2}\right)}{1+e \cos b} \tag{30}
\end{equation*}
$$

and the path of the reflected ray to the conjugate focus is
$2 m-r=r^{\prime}$

$$
\begin{equation*}
=\frac{m\left(1-e^{2}\right)}{1+e \cos c} \tag{31}
\end{equation*}
$$



Fig. 13. Distribution of Light about the Source and the Image at the Conjugate Foci of an Ellipsoidal Reflector

The intensifying factor
is the ratio of the square of $r^{\prime}$ and $r$, or

$$
\begin{equation*}
f=\left(\frac{2 m-r}{r}\right)^{2} \tag{32}
\end{equation*}
$$

which may be also given in the form

$$
\begin{equation*}
f=\left(\frac{1+2 e \cos b+e^{2}}{1-e^{2}}\right)^{2} \tag{33}
\end{equation*}
$$

or when both angles are known

$$
\begin{equation*}
f=\left(\frac{1+e \cos b}{1+e \cos c}\right)^{2} \tag{34}
\end{equation*}
$$

The proof of equations (32), (33) and (34) is based on the photometric law that the illumination raries inversely as the square of the distance and directly as the cosine of the angle of incidence. The elemental zone area d.A of Fig. 13 extends around the ellipsoid at a uniform distance of $r$ from the source and its illumination is therefore

$$
\begin{equation*}
E=\frac{I}{r^{2}} \cos i \text { foot-candles } \tag{35}
\end{equation*}
$$

if the intensity $I$ of the source is expressed in candles and the distance $r$ is expressed in feet.

The light reflected from $d A$, assuming the surface to be perfect in both formation and
reflecting power, is concentritted on ( $)^{\prime}$ it a distance $r^{\prime}$. The foregoing law of radiation is independent of the direction of radiation so that while $d A$ is the illuminator and the point $O^{\prime}$ the illuminated, we can again writu

$$
\begin{equation*}
E=\frac{J^{\prime}}{\left(r^{\prime}\right)^{2}} \cos i \tag{35a}
\end{equation*}
$$

where $I^{\prime}$ is the intensity of received radiation and $r^{\prime}$ is the distance from $d A$ to $O^{\prime}$.

Equating (35) and (35a) we get

$$
I^{\prime}=I\binom{r^{\prime}}{\frac{r}{r}}^{2}
$$

which is the equivalent of the equations for the intensifying factor.

It is at this point that the difficulties of a practical application of the ellipsoid begin. The distribution of intensities about the conjugate focus are not widely different from the computed values for any of the usual light sources that suggest themselves, and thus the "point source" and the actual source are thus far in fair agreement. The feature that has been overlooked is the fact that there is an enlargement or reduction of the image at $O^{\prime}$ depending upon the path taken by the light, and this enlarging or area factor is identical with the intensifying factor of equations (32), (33) and (34). The radiation from the image at $O^{\prime}$ is $\left(\frac{2 m-r}{r}\right)^{2}$ times as great because the image has changed its sectional area to that extent. The brilliancy of the image is in every case equal to that of the brilliancy of the source times the coefficient of reflection, and from every angle of view the image at $O^{\prime}$ has a brilliancy

$$
B^{\prime}=K B
$$

where $B$ is the brilliancy of the source and $K$ is the coefficient of reflection of the surface of the ellipsoid.

Distribution of Light from Finite Source
 Was so mommted that the imane at the external forms was in the porer persition to semed light Whomeh the condensing lenses, lantern slide. :and projection bens to the sereen.

Phe dimensions of the ellipsodel were:

$$
\begin{aligned}
& \text { Somi-mator axis. . . . . son in. } \\
& \text { semi-minor axis. . . . . . (o) in } \\
& \text { Ellipticit! . . . . . . . . . } 0 . \text { - }
\end{aligned}
$$

tive to the screen the actual projection efferency of the reflector thus varied from $\because$ per eent in the center to nearly 100 per cent at the rim. It a point directly above the lamp the enlarging ratio in diameters is, from (3is)

$$
\begin{align*}
d & =\frac{1+2 c \cos b+c^{2}}{1-e^{2}}  \tag{39}\\
& =\frac{1+0.61}{1-0.61}=1.1
\end{align*}
$$

The distance from the lamp focus 10 the center of the reflector, which in this case was cut anay tomake room for the limp) base and socket, was, from equation (30)
$r=\frac{\lambda(1-0 .(61)}{1+(1) .5}=1.5 \mathrm{in}$.
and the enlarging ratio $d$, in diameters, is derived from equation (32)

$$
\begin{align*}
d & =\frac{22 m-r}{r}  \tag{3.4}\\
& =a 1.5
\end{align*}
$$

The diameter of the light source was 0.36 in . and this would have made an image diameter of 2.9 in . The enlargement ratio of the condensers, for an image in the center of the objective lens, was 3.5 so that the second image in this plane would have been 10 inches in diameter. The objective had a diameter of only $1 .$, in. and it is very evident that for a central image this optical combination was rery wasteful, the computed efficiency being $0.0^{\circ}$. As a matter of fact, in this particular experiment the lamp, was mosed ahead of the foctus of the ellipse, reducing the enlarging ratio at the conjugate foeus to $\bar{i}$. and the image diameter at the objective to less than so in

Light reflected irom the rim of the reflector formed an imare of about the size of the light source itself ( $r$ and $r^{\prime}$ being equal) and so far as size was concerned this image was ishty efficient in passing through the objee-


Fig. 14. First Example of the Application of an Ellipsoidal Reflector to Lantern-slide Projection


Fig. 15. Second Example of the Application of an Ellipsoidal Reflector to Lantern-slide Projection


Fig. 16. Third Example of the Application of an Ellipsoidal Reflector to Lantern-slide Projection
and this gave an image at the conjugate foens 1.3 .5 in . in diameter, and a second image at the objective 4.7 in . in diameter. The efficiency of this region of the reflector was 10 per cent. As more than half the light collected by the reflector fell in regions haring efficiencies between -2 and 10 per
cent, and less than half was over the latter percentage, it is evident that the net efficiency of the reflector for this particular test and with this particular lamp must have been low.

If we assume that the light from the bare lamp was equally distributed in all directions, the percentage collected by the condensing lens with the lamp in its usual position (the first condenser subtending an angle of 71 deg. from the lamp center) was

$$
f=\frac{1-\cos 35^{\circ} 30^{\prime}}{2}=0.093
$$

The amount of light within any given angle $e$ from the axis of a uniformly radiating source is proportional to the corresponding area of an enclosing sphere of unit radius. Suppose this sphere to be surrounded by an open ended cylinder of radius 1 , so that its center is tangent to the equator of the sphere and its length is equal to its diameter. A plane perpendicular to the common axis cuts equal areas from the sphere and cylinder, and in the latter surface the area is obviously the diameter of the cylinder times the length (from the 0 deg . end) cut off.
Thus

$$
A=2 \pi(1-\cos a)
$$

or, in terms of the entire cylindrical surface

$$
\frac{A}{4 \pi}=\frac{1-\cos a}{2}
$$

The half ellipsoid collected light up to 141 deg. from the axis with a collecting efficiency of

$$
\frac{1-\cos 141 \mathrm{deg} .}{2}=0.823
$$

or $\$ .8$ times the condenser collecting efficiency. Assuming a coefficient of reflection of $0 . S$ for the ellipsoid, and taking 0.12 as being the average projection efficiency for this particular ellipsoid, the total projected light would amount to 0.079 of the initial light of the lamp. This figure of 0.079 is not greatly different from the corresponding figure of 0.093 for the condensing lenses alone. A risual and photographic comparison of the screen illumination showed the two to be nearly equal, and the foregoing rough computations are thus known to be fairly exact.

The apparent outlines of the light reflected from the ellipsoid of Fig. 14 are marked with a dotted line. These outlines do not represent the true edge of the beam, but rather the place where there was visible a marked falling off in intensity. This follows searchlight practice, wherein the edge of the beam is that point of the beam where the intensity
falls to 10 per cent of the maximum, of central, intensity:

A repetition of the experiment with a reflector reaching the plane of the front focal point, Fig. 15, gave only shighty better screen illmmination, as might be expected in view of the small amount of additional light collected (some 1.5 per cent) and the return of this light after two reflections in such a direction as to strike the lamp base or the opening in the rear of the reflector.

A further test was made with the half ellipsoid turned at an angle of 30 deg. with the axis of the projection machine, Fig. 16. The losses were found to be excessive at both condenser and objective, and only one edge of the lantern slide could be projected onto the screen.

The same cllipsoidal reflector that performed so poorly with a lamp having a filament 0.36 in . across the outer coils would be a fairly effective device with the proper lamp. Thus, if we go through the previous computations in the reverse order, we find that with lamp filaments that are now available the reflector should be quite efficient.

We have:
Permissible image at objective, 1.5 in . diameter

Enlargement ratio of condensers 3.;
Permissible image at front focus 0.43 in. diameter

Maximum enlargement ratio of reflector 8.15

Maximum diameter of filament coil 0.0.53 in.
With a filament of 0.0 .5 in . or 0.06 in . outside coil diameter the successive images would thus be within optical bounds and the high collecting efficiency of this ellipsoid would be of great value in increasing the curtain illumination per watt of lamp input. The advantage here is purely a matter of economy, as the ultimate screen illumination is always less with a small source and a reflecting surface than with a large source used directly. Thus with a source of sufficient size used directly at the focal point of the condensers the illumination at the screen is, say, 10 foot-candles, while with a source of the same brilliancy used in connection with an ellipsoidal reflector the maximum attainable illumination will be $S$ foot-candles, but this latter source may be of much smaller size and wattage.

# Electrification of the Massachusetts Cotton Mills, Lindale, Ga. 

By D. W'. PEABODY<br>Amanta Offich, Generme Elechric Combany


#### Abstract

Electrification produces results economically regardless of whether the drives required are one or many and whether the individual power demands are great or small. Among the conspicuous examples may be mentioned the mine hoist, stecl mill, electric railway, machine shop, and textile mill. The following article describes a recent installation of electric drive in the last named industry. The figures of the production conomy thus secured are of inestimable value because they were secured by comparison with the parallel aperation of a similar mill which employs straight mechanical drive.-Editor.


The Massachusetts Cotton Mills at Lindale, Ga., were originally designed and equipped for mechanical drive throughout. They have more than 100,000 ring spindles, 2734 narrow and 460 broad looms, and produce sheeting, shirting, duck, drills, denims, and canton flannel. The mills are divided into three units, which are independent from a power standpoint.

One of these units, known as Mill No. 1, with 35,000 spindles, has recently been changed over from mechanical to electrical drive throughout and the remaining two mills will also be electrified but at present are operating with the original mechanical equipment. This particular installation is of unusual interest in that practically identical mechanically and electrically operated mill equipments are engaged in simultaneous production under conditions which permit of a ready comparison of the operating characteristics and productive efficiency of the two methods of drive.

Originally all three units of these mills were driven by low-speed reciprocating steam engines, operating condensing with steam at 145 lb . and connected to the main driving shafts on the three floors of the mills by rope drive; the various countershafts on each floor being driven by belts from the main shaft. This method of drive involved the use of an enormous amount of belting. The electrification of Mill No. 1 eliminated more than 200 of these belts and incidentally eliminated the loss in power which had previously been involved in the belt slippage. About 25 per cent of the belting consisted of heavy countershaft drives, the remainder being the belts from the countershafts to the machine pulleys. The estimated loss of power amounted to more than 10 per cent of the total primary power.

These conditions, serious as they were from an engineering standpoint, would not have warranted the electrification of the mill if no other benefits were to be derived from electric
drive. It had already been demonstrated, however, in a number of cotton mill installations, that the constant speed characteristics of the electric motor permitted the operation of a large part of the textile mill machinery at higher speeds than could be safely obtained with mechanical drive, and that these speeds could be maintained with absolute uniformity. Therefore, the results to be obtained in the electrification of this mill (in addition to the saving effected in the power cost of production) would be the much more important increase in production secured without any increase of the textile mill machinery.

The changeover was not made until after exhaustive tests had been made with temporary electrical equipment.

The power station equipment (Fig. 1) consists of a $6000-\mathrm{kw} ., 3600-$ r.p.m., 600 -volt, 3phase, 60-cycle steam turbine-generator, operating condensing at present at 190 lb . boiler pressure. This turbine is intended eventually to supply current for all three mills, and when the remainder of the electrical equipment is installed it will then be operated with 100 degrees superheat. There is also a $600-\mathrm{kw}$. turbinegenerator which is utilized to carry the night loads; such as fire pumps and mill, house, and street lighting in the mill village.

The operating economies of the electrified plant begin in the power station. The floor space required by the turbine-generator is less than one-third of that occupied by the original engine (Fig.2), and the higher overall efficiency of the modern steam turbine reduces the boiler capacity required for a given power output and this saving is reflected in the amount of coal used. Even under present conditions, with the generating set operating underloaded, and therefore at relatively low efficiency as compared with full-load operation, there has been secured an actual average saving of about 40 tons of coal per week.

The leads from the main turbine-generator are brought direct to a framework (Fig. 3)


Fig. 1. General View of Power Station showing $6000-\mathrm{kw} .3600-\mathrm{r} . \mathrm{p} . \mathrm{m}$. 600 -volt Turbine-generator Operating Condensing at 190 lb $600-\mathrm{kw}$. Turbine-generator, and Main Switchboard


Fig. 2. Original Engine Drive for Mill No. 1. Superseded
by Turbine shown in Fig. 1

Which contains the matn hosbars, and is
 circuit broakers which are solemoded operated from the main generator panel and eontrolled herelays from the matn switehboard which is loxated on the floor above. This arrangement insures absolute safety to the operator through remote eontrol.
( ${ }^{\text {arrent }}$ is distributed through eight feeder circuits. 'The outgoing feeder wire from the switehboard is all enclosed in metallic conduit, the distribution to the mill being made at 600 volts. The motors used are rated at 550 volts. Current for the lighting circuit is stepped down by transformers outside of the mill to 120 volts and Mazda lamps with standard metallic 'Type RLM reflectors are used throughout (Fig. 4).

The picker room equipment includes nine openor pickers each individually driven by a 10-h.p. motor mounted on the A-frame and provided with three pulleys from which short belts go to the beater shafts.

Ten intermediate single-beater pickers are each equipped with a $7 / 2$-h.p. motor, while the finisher pickers (Fig. 5), of which there are ten, are provided with 5 -h.p. motors. These are all individual drives and the control of each consists of an oil circuit breaker mounted on the A-frame of the picker.

In the changeover of the picker room to electric drive, three countershafts with their main belts, pulleys, and about thirty belts were eliminated. When this room was mechanically driven, the shutdown of one or more machines resulted in no appreciable reduction in the amount of power required, and if only one or two machines were operating the power consumed by the belts and countershafts was practically as great as that involved in the operation of all the machinery.

With electric drive it is possible to operate any of the machinery intermittently with only the normal unit consumption of power. With individual motor drive the power consumed is directly proportional to the work produced and the supply of energy to each machine stops when the motor stops.

In the card room segregated group drive (Fig. 6) has been used throughout with the driving motors mounted on the ceiling in an inverted position and utilizing totally-enclosed chain drive to the center of relatively short countershafts. With this arrangement highspeed motors can be used with a corresponding reduction in their physical dimensions and cost, and they can be connected to the countershafts with short centers.

The control for eath group consists of a standard compensator located in a place confenient to the operator, and the subdivision of power application permits economy in the operation of part of the machinery.

Phe shabbers and intermediates are also motor group (lriven and have the same general arrangement as the cards.

The spinning room* was originally equipped with the so-called "bieycle drive," involving the use of long countershafts, with more than 150 large and 300 small pulleys with belts connected to the individual frames. It was an excellent example of mechanical drive and was maintained in good condition by careful alignment of the shafting, frequent inspection, and adjustment of belt tension and adequate lubrication but it was not possible to maintain the front roll speed of the frames at a rate which would give the best production.

In making the changeover to individual electric drive it was not necessary to alter the location of the machines, and the motors were mounted on brackets which utilized the original spinning frame bolt holes. The original spacing of the frame ends, while it was narrow, afforded ample room for the installation of the motors, chain drive, control, conduit wiring, and totally-enclosed protective devices which constitute a compact self-contained and independent power unit for each spinning frame.

The motors used* are $71 / 2$-h.p., 1800 r.p.m. units and are individually controlled by a non-automatic circuit breaker operated by means of a shipper rod. The wiring to the motors is brought up through the floor and all wiring between the motor and the control is enclosed in flexible metallic conduit.

The application of individual drive in this case was due to a realization of the importance of constant speed as compared with the varying speed which was unavoidable in the use of mechanical drive; and the improvement in both the quantity and quality of the output, which result has been very marked.

While it was desired to operate with a front roll speed of 148 r.p.m., to obtain the best production, it was found necessary with the mechanical system to reduce this to 144 r.p.m., and at this speed the average "ends down" was two per cent. After the individual motors were applied to these same frames, it was found possible to increase the front roll speed to 154 r.p.m., and at this increased rate of speed the average "ends down" was somewhat less than one-half of one per cent. In

[^17]

Fig. 5. Pickers with 5-h.p. Picker-type Motors Mounted on A-Frame


Fig. 6. Induction Motors in Card Room with Chain Drive to Countershaft


Fig. 7. Induction Motors Mounted on Ceiling and Driving Weave Room Through Chain-driven Countershafts


Fig. 8. Group of Starting Compensators for Controlling Weave Room Motors
addition to the actual increase in production, there was a definite improvement in the quality of the yam produced.

The spoolers, warpers, and slubbers are all provided with light group drive with small motors monnted inverted on the ceiling and belted to the countershafts.

In the weave room of a new mill it is customary for the loom manufacturer to provide individual motors for each machine as a standard equipment, but in the case of Mill No. 1 it was found that the mechanical changes necessary to provide individual drive in the weave room would involve an expense that was not warranted under the existing conditions, and a system of group drive was therefore adopted. With this change each line of countershafts is provided with its own motor (Fig. 7) thereby eliminating the large main belts which were previously used and permitting the economical operation of separate groups of the machinery on overtime worl.

With the elimination of the main line belts and with the motors driving light groups of looms, the number of interruptions due to belt slip has been greatly reduced and with an increased output there has been a positive improvement in the quality of the loom products.

The motors are mounted on the ceiling with short enclosed chain drives and the control for the various groups of machines is concentrated in groups of compensators installed on angle-iron frames at the sides of the weave room. These compensators (Fig. 8) are each equipped with a switchboard type ammeter and a safety switch.

A thoroughly modern system of illumination has been provided throughout the mill; Mazda lamps with standard metallic type RLM reflectors being used. The most intensified illumination is found in that section of the weave room devoted to colored goods, and in this case (Fig. 4) each loom is provided with a 75 -watt lamp.

While the motors are all operated on $550-$ rolt circuits, special lighting transformers are provided to give 120 volts for the lighting circuits; and the same service is provided for the houses of the mill operatives and streets of the mill village as well as for the churches, school, gymnasium, clubs, theaters, hospitals, and recreation buildings, all of which are maintained by the mills.

Without any increase in the textile mill machinery used, Mill No. 1 has shown an overall increase in production of about 12 per cent for the electric drive as compared with the former mechanical drive.

# Radio Transmitting Sets for the Mexican National Radio System 

By B. R. Cummings<br>Radio Engineering Department, General Electric Company

To the average individual in this country the mention of radio brings to mind only the fascinating interest that is connected with the reception of the entertaining programs which are broadcast daily. For him it would be instructive to learn of the less sensational but more valuable application of radio to commercial communication. For example, the Government of Mexico proposes to cover its territory with a network of radio telegraph stations furnished with the most modern vacuum-tube equipment. This plan calls for the installation of some 42 radio "central stations" and "substations," the first sets for the purpose being described in the following article.-Editor.

The functioning of vacuum-tube transmitters, in general, has been discussed in previous issues of the General Electric ReVIEf** and therefore the present article will be confined to a description of two types of transmitters which have recently been developed and built for installation in Mexico. These will form part of an elaborate radio telegraph communication system in that country.

Their characteristics and ratings were established after a comprehensive study of

[^18]the communication requirements in connection with stations already in service. In the selection of the capacities advantage has been taken of the superior transmission effectiveness of continuous-wave (vacuum-tube) transmitters; and in general capacities have been selected which will insure twice the signal strength that is now obtained from spark transmitters which employ double the power input to the antenna.

The system contemplated involves the erection of forty-two stations, in addition to those already in operation. Of the new stations, four will be so-called "central stations" and will communicate with a
number of smaller "sub-stations." The new central stations will be located at Puerto Morelos, Puerto Mexico, Montercy, and Culiacan. Those already in operation or under construction are located at Mexico City, Tampico, Torreon, and Hermosillo.

With that of spark or arc trancmith (1- :n the latter are almost universall: ratel : terms of "input" to the transmitter on atr converter.

The vacumm-tube sets are built to operate on any wavelength between 800 and $: 300$


Fig. 1. Map of Mexico showing the Location of Stations for the Proposed National Radio Telegraph System

Transmitters of the type described in this article will be installed at the new central stations as follows:

| Station | Capacity | Maximum Com- <br> munication Dis- <br> tance Required |
| :--- | :---: | :---: |
| Puerto Morelos | 2 kw. | 172 miles |
| Puerto Mexico | 2 kw. | 172 miles |
| Monterey | 2 kw. | 202 miles |
| Culiacan | 4 kw. | 280 miles |

The map shown in Fig. 1 illustrates graphically how completely the proposed system covers the Republic of Mexico.

These transmitters are rated at 2 and 4 kw . respectively, putting that amount of power into the antenna circuit. This point should be remembered in comparing their output
meters, when used on an antenna having the characteristics specified in the following paragraphs. By means of wave-change switches any one of four predetermined wavelengths may be selected in minimum time.

These sending equipments are designed to operate on an umbrella-type antenna having two distinct sections. The upper section is used to obtain wavelengths from 1200 to 3000 meters. It has approximately the following characteristics:
Fundamental wavelength. . 700 meters
Capacity. . . . . . . . . . . . . . 0.0027 microfarads
Resistance................ . . 3.9 ohms at 1500 meters 2.4 ohms at 3000 meters

The lower section is used to obtain wavelengths.
from doto to 1200 metors, amd has approximately the following characteristies:
Fimatamental wavenght. Ho meters
Capactiy
0.1000 s 6 microfarads

Ressitatice
11. ohms at boo meters
f. ohms at 1200 meters

Antennas of other forms, having the same characteristios, call be used


Fig. 2. Relay Key


Fig. 3. Operator's Control Cabinet
Provision is made for telegraph transmission either by contintous waves (c.w.) or inter-rupted-continuous waves (i.c.w.) Transfer from one method to the other is made by throwing a single switch, which makes ail necessary changes in the circuit connections.

While continuous-wave transmission has greater transmission effectiveness than inter-rupted-continuous-waye, the latter is provided so that communication can be carried on with ships and shore stations not equipped for the reception of continuous-wave signals. The interrupted-continuous-wave signals can be heard by all stations equipped for spark reception.

The kering system includes a so-called "break-in" relay, whereby the antenna is automatically transferred from the transmitter to the receiver between the dots and
darshes of the transmitter signals. This permits the operator to listen-in while sending. A stand-b) send-receive switel is also included to be used in place of the break-in relay, if desired, or to cover long listening-in perioxls during which the transmitter may be shut down.

The following vacuum tubes are utilized:

| 2 Kw. | 4 Kw. |
| :---: | :---: |
| 2 | 4 |
| 3 | 5 |

The power for operation is to be supplied at 110 or 20 volts, 50 or $(50$ cycles, single phase, alternating current; and at full load the sets will draw approximately \& and 12 kw . respectively from the line. Provision is made in the transmitter for compensating for normal changes in supply voltage, i.e., an increase or decrease of 10 per cent above or below normal.

Control is normally obtained by means of auxiliary equipment constructed for mounting on the operator's table. This equipment consists of a telegraph key with a back con-


Fig. 4. Rectifier Equipment
lact for operating the break-in relay (Fig, ol) and the operatorss signal and control cabinet (Fig. :3) which includes the following:

1. Stop-and-start switch, which ofens and doses the main-line contactor monnted on the rectifier panel.
2. Tumbler swith for controlling the stamd-hesend-recoive switchmonnted in the antemat tuning unit st ructure.
3. Three indicating drops. which indicate plate owerload and kemotron or photron filament wer-voltage respectively.
Each of the three drops actuates a buzzer which indicates 20 the operator that the transmiterer requires attention.

The controls supplied for the operator's table, while sufficient for nomal operation. do not take care of all adjustments for the set. Wave change, power change, signal change, filament voltage atlustment, and line roltage compensation are controlled at the transmitter. Provision is also made for starting and stopping the set (i.e. closing and opening the main-line contactor) from push buttons located on the rectifier and oscillator panels.

The sets are provided with protective equipment which will prevent their being injured in the event they are improperly operated.


Fig. 5. Rectifier Equipment


Fig. 6. Oscillator Equipment


Fig. 7. Oscillator Equipmeat

In case of plate overload a relay actuates, opening the holding coil of the master protective relay and thus cutting all power off the set.

I'rotective relays in the kenotron and pliotron filament circuits actuate the (rops and buzzer in the operator's signal and control cabinet. When over-voltage occurs, the set is automatically shut down. When under-voltage occurs, the relays actuate buzzers located in the rear of the rectifier panel, attracting the operator's attention to this condition.

An interlock is included in the stand-by send-receive relay, which prevents the trans-


Fig. 8. Antenna Tuning Unit
mitter being started when in the "Receive" position.

Switches are provided on the gates of the surrounding railing so that the set is automatically shut down when the gates are opened.

A condenser-discharge switch is included in the rectifier panel which automatically discharges the filter-system condensers when the set is shut down.

Safety gaps are included across the terminals of all condensers in the set to take care of any abnormal surges which may be developed while making initial adjustments.

The low-voltage circuits for the operation of auxiliary equipment and relays are pro-
tected against radio-frequency induction by stuitable condenser systems.

All major power circuits are fused.
The transmitters consist essentially of four oomponent circuits: a rectifying circuit, used to obtain a souree of high-voltage direct current for the plate circuit of the pliotrons; a filter cireuit, which smoothes out the ripple in the rectified alternating current; an oscillator eircuit, which converts the high-voltage dircet-current ontput of the rectifier and filter circuit into radio-frequency current; and a tuning circuit, by which the wavelength of the antenna circuit is adjusted to the wavelength of the transmitter. The trans-


Fig. 9. Antenna Tuning Unit
mitted wavelength is established primarily by the transmitter, to which the antenna is tuned. This practically eliminates any variation in the emitted wavelength due to slight changes in antenna constants.

The foregoing circuits are built in three independent units. A vacuum-tube rectifier panel contains the rectifying and filtering circuits; a vacuum-tube oscillator panel contains the oscillators and auxiliary circuits for converting the direct-current supply into radio-frequency power; and an antenna tuning unit contains the equipment necessary for adjusting the wavelength of the antenna.

The vacuum-tube rectifier for the $4-\mathrm{kw}$. transmitter is illustrated in Figs. 4 and 5.

The rectifiers contain the following component units in both the 2 - and the 4 -kw. sets: High-roltage and filament transformers Rectifier tubes and mountings
Isolating switches
Filter inductance and condensers
Supply-roltage compensator
Power-change switch
Filament-control rheostats
Filament roltmeter
Wattmeter
Plate-circuit ammeter
Line voltmeter
Protective relays

The wave-change switch has frour hank and selects taps on the plate coil, weillation transformer, intermediate circuit comlenst iand the grid coil, thereby adjusting the sw for best operation on each wavelengtl.

The antenna tuning unit, which is the same in the 2- and 4 -kw equipment, is illustrated in ligs. $\delta$ and 9 . It contains a wave-change switch, the break-in relay, an antenna loading inductance, the stand-by send-receive relay, and an antenna-current ammeter.

The weights and dimensions of the complete transmitters are given in Table I.


Fig. 10. Complete Assembly of the Radio Transmission Equipment for a Station

The vacuum-tube oscillator for the $4-\mathrm{kw}$. transmitter is illustrated in Figs. 6 and 7. It contains the following component units:

Pliotron oscillators
Oscillation transformer
Wave-change switch
Equipment for obtaining interrupted-con-tinuous-wave transmission
Signal-change switch
Key relay and keying system.

The development and design of these transmitters was particularly difficult, in that the ratings were higher than those of any other transmitters built up to that time in this country, and there was very little if any standard practice to be guided by. This refers not only to the complete assembly but to a great many of the component units, such as transformers, condensers, filter systems, and the vacuum tubes themselves.

TABLE I

| Units | WEIGHT | WEIGHT | DIMENSIONS IN INCHES, 2 AND 4 kW . |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2 Kw . | 4 Kw 。 | Height | Width | Depth |
| Rectifier. | 2400 | 3000 | 96 | 34 | 70 |
| Oscillator | 1750 | 2000 | 96 | 78 | 64 |
| Antenna Tuning | 825 | 825 | 75 | 50 | 96 |
| Accessories.... | 250 | 250 |  |  |  |

## Cast Iron Welding


#### Abstract

The art of welding cant iron has not progressed with the same rapidity at that of welding other metals Fexamse the many and varme ingredients entering into he eromposition of cast iron each have a great infaence upon the whability．The mormous fied for wedding cast ron constitutes so great an incentive，however，that  following atrticle reports the general considerations that were arvived at and later installonents will detail the timblings with respect to the use of the electric are．EDrbor．


## GENERAL CONSIDERATION

For years it has been common practice in repair defective iron castings in the foundry， by eut ting out the defect，forming a sand mold around it，and then pouring very hot melted iron into the mold and allowing it to overflow and waste，until the surface of the defect is melted，when the mold is allowed to fill，the supply of melted iron is cut off，and the cast－ ing allowed to cool．The process is called ＂burning in．＂In many cases good results are obtained，but frequently there are disadvan－ tages of high cost，cracked castings，and the difficulty of machining the＂burn＂or the metal near it．

Modern methods of repairing cast iron parts are replacing the old practice，with better re－ sults in every way．There are still，however， many matters that need more study：

## Field for Cast Iron Welding

The field for possible applications of cast iron welding is enormous．At present，unlike the welding of steel，the welding of cast iron is confined entirely to repair or salvage work． However，with the further perfection of meth－ ods of making strong，homogeneous，machine－ able welds in cast iron，at a reasonable cost，there is reason to believe that the art of welding may be employed in the fabrication of structures of cast iron，just as it is at this time used in joining cast steel sections．

But in repair work alone，cast iron welding can be extensively used and effect great sar－ ings．Consider the foundry in which the cast－ ings are manufactured；welding can be and is employed to fill up blowholes and gas holes；to build up castings that do not quite meet the required dimensions；and for various other purposes，making useful castings of what would otherwise be scrapped material，saving expense for the foundryman and delay for the purchaser of the castings．

After the castings leave the foundry and go to the machine shop，further defects，remedi－ able by welding，may be uncovered by the machining process．Or the machinist may in－ advertently remove too much metal，which can be replaced by welding．Here are other opportunities for welding to make further sav－
ings of time and money，before the casting even reaches its final destination．

Then，when the iron casting has become a part of an engine，a generator，a boring mill，a punch press，an automohile，a sewing machine， or what not，there is always the chance that some unusual strain to which the machine is subjected，a flaw in the casting，or some other cause，will effect its failure，resulting in loss of use of the machine of which it is a part until it can be replaced or repaired．In the case of large important castings，the time required for obtaining a new one may be a matter of weeks or months and the expense involved very great，especially if the loss of output from the disabled machine is considered．

Here is the great field for cast iron welding， namely，the repair of broken castings．In some cases the possibility of doing the repair without removing the broken part from its operating position alone effects a large saving in time and money．In others，it is the ex－ pense involved in scrapping the broken casting and obtaining a replacement which is the im－ portant item．In still others，time is the all important consideration．In all these cases，if a satisfactory method of welding is available， an economic saving will be effected and any process that can bring about savings of time and money to industry in general deserves earnest and thorough study and investigation in an effort to advance or perfect its use．

## Iron Ore－Pig Iron－Cast Iron

Cast iron，as presented to the welder，is obtained from pig iron，which has been pro－ duced by smelting iron ore in the blast fur－ nace．The molten iron，while in the blast furnace，comes in contact with other elements existing in the ore or fuel and takes them up to an extent depending on the amount present and the conditions under which the furnace is operated

Some of these elements，notably carbon， silicon，sulphur，phosphorus，and manganese， are absorbed by the iron in large amounts and as these amounts vary，so do also the physical properties of the cast iron．It is quite prob－ able that they also affect its weldability to some extent，though this needs further re－
seareh. Carbon is be far the most important element and has the greatest effect, while the others are all of value at times, except sulphur which is alwas injurious cren in small amounts.

The molten iron from the blast furnace, with its content of carbon, silicon, manganese, sulphur, and phosphorus, is cast into pigs, which are shipped to the foundrymen to be made into iron castings.

## Control of Composition and Characteristics of Iron Castings

The foundryman places the pig iron, with possibly some scrap iron or steel and the necessary amount of fuel, usually coke, in a cupola and melts it. When it is in the melted state it can again change its characteristics by absorbing elements with which it comes in contact.

Thus, the foundryman can to a certain extent control the composition of the iron which he taps from the cupola by mixing pig irons and scrap which contain different proportions of these various elements and by using fuels which contain small amounts of injurious elements, such as sulphur. Fluxes are sometimes used with good effect and various elements, such as silicon or manganese, may be added by introducing ferro-alloys, containing high percentages of these materials, into the charge.

The physical properties of the iron casting may also be varied by the method of casting. Thus if a mold is so made as to chill the molten iron quickly, a large proportion of the carbon will remain in the combined state, making a very hard casting.

## Influence of Impurities on the Properties of Cast Iron

Carbon appears in cast iron in two forms, namely, combined and in the free state as graphite, sometimes called graphitic carbon. When in the combined state, it is in the form of iron carbide ( $\mathrm{Fe}_{3} \mathrm{C}$ ), frequently called cementite, a chemical compound of iron and carbon. It is very hard and brittle and has little strength. When free graphite is present, it retains its own characteristics of softness and weakness.

All cast iron contains carbon, usually from 3 to 4 per cent, but the amount of this held in the combined form depends on the rate at which the casting is cooled and also on the amount of other elements, principally silicon, present in the iron. When the iron is molten, practically all the carbon is held as iron carbide. Now if the casting is allowed to cool very slowly, nearly all of the carbon will pass

free flakes of graphite. (on the wher hamal, is the iron is coolerl with extreme raphelity at large proportion of the carlom will remation in the form of iron carbide.

When the carbon is in the free or sraphetice state, it is mixed with the iron in the form of flakes and as neither pure iron nor sraphite is hard or brittle, the result is a relatively soft metal, one which can readily be machined However, the flakes of graphite separate the grains of iron from one another, therebse wakening the metal.

If the carbon is practically all in the combined state, the metal is very hard and brittle and difficult to machine.

Cast irons containing a considerable amount of graphitic carbon are known as gray cast irons because of the appearance of their fracture, which is grayish or blackish and coarsely crystalline. Those containing only combined carbon, and free therefore from graphitic carbon, are called white cast irons from the aspect of their fracture, which is white, brilliant, and highly metallic.

Silicon reduces the solubility of carbon in molten iron, so that pig irons of high silicon content have a low total carbon content. The most important effect of silicon from the standpoint of welding is that it increases the proportion of free to combined carbon, thereby making the metal soft and machineable. Thus, while the presence of silicon may not directly affect the reldability of cast iron, it is of great importance since its introduction in the weld has a strong softening influence. Silicon also helps to eliminate oxides, promote fluidity, and decreases shrinkage and chilling effects.

Sulphur exerts a very bad effect on cast iron and should be kept at a minimum. It tends to cause the carbon to be held in the combined state. This increases the hardness and also the shrinkage since carbon in the combined form occupies less bulk than graphite. It also renders the iron very weak, while at a red heat, unless a sufficient amount of manganese is present. Sulphur also makes the iron solidify more rapidly in cooling from a red heat, thereby often causing blowholes and shrinkage holes or cracks.

Thus sulphur tends to make the iron white, hard, and brittle. Its effects can be partially counteracted by silicon or manganese additions. Silicon will precipitate the carbon as free graphite, even if sulphur is present, while manganese will combine with the sulphur to form manganese sulphide.




Fig. 8. Same as No. 7, but shows structure
more clearly. Magnified 4.30 dia.


Fig. 7. Machine Cast Iron Heated Red Hot
and Quenched in Ice Water. Matrix is martensite with graphite plates showing black. White spots are iron phosphide which the rapid quenching prevented from
becoming phosphide eutectic. Magnified 100 dia.

ig. 5. Hard Close-grained Cast Iron.
Matrix all pearlite. Graphite plates moder-
ate in size. White spots phosphide eutectic. From hydraulic cylinder. Magnified 100 dia.

Fig. 12. Phosphide Eutcctic in Cast Iron
with Pearlite Fringe around it.
Magnified 1200 dia.

Fig. 15. Good Machine Iron. Ferrite around
praphite plates and rest of the matrix
 aṇd number. Magnificd 200 dia.


Fig. 10. Hard Spot in Cast Iron made by just melting surface with torch and allowing
it to cool in air. The rapid cooling has
changed it to chilled iron. Magnified 2 dia.

ig. 14. Another Close-grained Cast Iron
with less graphite than No. 5 and also
less phosphorous. Magnified 100 dia

ig. 13. Chilled Iron Casting. The White
is cementite, the matrix pearlite and there is
some carbon as graphite at the right.
Magnificd 100 dia.

Thosphoms lowers the melting point of cast irm amd makes it hard，britte，and weak．In the amonuts ordinarily present in fomdry iroms，it has no elfeet on the ration of combined th fied cartom，but itself forms a compound with iron and iron carbide，which is hated and hritte，has a low melting peint，and confers these properties on cast iron．If enough sili－ con is present to prevent the formation of iron （anbide，the iron will be softer．but still brittle．

The amoment of phosphorus is usually kept as low as possible，except in castings having very thin sections，where a very fluid iron is necessary to ensure filling all parts of the mold． In such cases，a high phosphorous iron is used because of its fluidity，in spite of its weakness and brittleness．

Manganesc has several effects on cast iron． Its principal one is to combine with the sul－ phur，forming manganese sulphide，which oc－ curs in small gray particles，which，unless seg－ regated，have little effect on the strength of the casting．It also helps to deoxidize the metal．Further，it combines with some of the carbon，making（ $\mathrm{Mln}_{3} \mathrm{C}$ ）manganese carbide． This has the same properties of hardness and brittleness as iron carbide，so that while by combining with sulphur，it softens the iron，it hardens it by combining with the carbon．As neither sulphur nor manganese is uniformly distributed in the metal，it is necessary to have an excess of manganese present，to be sure that all of the sulphur is taken care of．

## General

From the foregoing brief statements，it is evident that the effect of any one element on the properties of cast iron is dependent on the amount of the various other impurities pres－ ent and upon the rate of cooling of the cast－ ing．The effects are in many cases much more complicated than have been indicated． A full discussion of this subject is far beyond the scope of this article．

## Classes of Gray Iron Castings

Since gray iron castings are machineable and in other ways better than white iron for most purposes，the majority of castings pre－ sented to the welder will be of gray iron．For practical purposes，gray iron castings can be divided into three classes：
（1）Machinery castings．
（2）Store plate．
（3）Speciaities，such as structural castings．
Machincry castings，as the name implies，are castings which are made as strong as is com－
patible with having them soft enough to be machineable．It is evident that this class inclucles jrons of widely varying composition， as the foundryman will vary the mixtures according to the size and shape of the castings which be is making as well as the use to which it is to be put．Castings of very heavy cross－ section will be machincable even though they have a low silicon content．This is true be－ cause the heavy section insures a low rate of cooling and much silicon is not needed to cause the precipitation of free graphite．

TYPICAL ANALYSIS OF＂GRAY＂AND ＂WHITE＂CAST IRON

|  | Gray． <br> Per Cent | White． <br> Per，Cent |
| :--- | :---: | :---: |
| Total Carbon | 3.30 | 3.20 |
| Graphitic Carbon | 2.80 | （all combined） |
| Combined Carbon | 0.40 | 3.20 |
| Silicon | 2.50 | 0.80 |
| Manganese | 0.50 | 0.45 |
| Phosphorous | 0.60 | 0.20 |
| Sulphur | 0.10 | 0.15 |

Stove Plate castings are necessarily of thin cross－section and consequently are usually made from iron containing high percentages of silicon and phosphorus．When castings， even though they be of heary section，such as grate bars，are made in a stove plate foundry， they usually are of this same grade of iron．

Structural Castings are made for strength alone．Of course there are exceptions to this statement，such as certain columns and special shapes，which require machining．A casting from a specialty shop，or a structural casting． will use a high percentage of combined carbon．

In Figs．1，2，3，and 4 are illustrated the two extremes，a gray iron in which practically all of the carbon is in the free state，and a white iron in which almost all of the carbon is in the combined form．The greater the proportion of free or graphitic carbon，the darker will be the appearance of the fracture and the grain will be coarser and more open，showing large crystals of iron with intervening flakes of graphite．Filings from such an iron will soil the hands or mark on paper，owing to the presence of the graphite．On the other hand， the fracture of the white iron is light in color and brilliant，and is close grained，with small crystals．Thus，from the appearance of the fracture，it is possible to estimate the propor－ tion of free to combined carbon and thus determine in a measure the characteristics of the iron to be welded．

## Factors Affecting Cast Iron Welds

## Carbon

In making a weld in commereial cast iron, the surfaces which are on be joined must again be melted. These surfaces consist of fron which contains carbon in both the free and combined states. When these surfaces are melted, several things happen. First, both the graphitic and combined carbon go into solution in the molten metal. Second, some of the carbon, silicon, and manganese are bumed out by the heat. while the amounts of sulphur and phosphorus are practically unchanged. Silicon is most casily burned out, so the tendency is to produce a cast iron, in the weld, that will be white when cold, owing


Fig. 17. Cast Iron Gas Welding Rod Heated Bright Red and Quenched in Ice Water. The structure is martensite, but there is enough silicon present to keep some carbon in the form of graphite
to its low stlicon and carbon content. Third, the surface of the molten metal oxidizes, making a slag which in a measure prevents furt her oxidation.

As soon as the welding heat is removed, the melted iron solidifies very quickly, owing to its proximity to the comparatively cold mass from which it has been melted and to its being exposed freely to the air. This sudden cooling causes a large amount of the carbon to be retained in the combined state, resulting in a white, hard, metal in the weld. Of course if the casting has been preheated before welding, the cooling of the added metal will not be so sudden and a softer machineable weld may be secured.

Experience has shown that the grade of cast iron which is most difficult to weld successfully is that which is soft and has an open grain. However, little difficulty is encountered when
the metal is of comparatively thim (mbe-hat inch or less) section.

## Oxidation

When iron is molten, or exen red-lag, it oxidizes very readily if exposed to the air. Thus in welling, the starface of the molten metal beeomes eovered with iron oxide. which may be deposited in the weld by mixing with the molten metal, or be being trapued between two layers of metal added at different times. In either case, the result will be a weak, non-homogeneous weld for the oxide particles segregate and do not form a junction with the adjarent metal.

## Shape of Casting

The shape of castings must also be taken into consideration. A casting comprising both light and heavy parts is subjected to more internal stresses than one of homogeneous cross-sections. These stresses are caused by the different rates of cooling, light sections cooling more rapidly than heary. There are also internal stresses set up at sharp angles.

## $\therefore$ Shrinkage

When in the welding of cast iron, a filler metal of different composition than that of the casting is used, serious consideration must be given to the fact that the co-efficient of expansion and consequently the shrinkage of the metal in the weld may be different than that of the remainder of the casting

The different shrinkages of the two metals will tend to cause one to slide on the nther as they pass from the liquid to the solid state. This shrinkage of course sets up internal strains which the ductility of the welding material must take care of. Altering the carbon content from the combined to the graphitic state helps decrease the shrinkage. If the iron emtains a weakening agent the internal strains set up by shrinkage often cause cracks to appear.

## Summary

From the foregoing, it is evident that the term cast iron is applied to metal of widely varying composition and characteristics. Cast iron always contains in the neighborhoot of :3 per cent of carbon, but this may be in either the combined or graphitic state and it may hold widely varying amounts of ot her elements, as silicon, manganese, sulphur, and phosphorus. Not only the presence of these elements. hut also the rate of cooling of the casting, profoundly affect the physical characteristies and weldability of the metal

## Electrification of the Mexican Railway

The Mexican Railway Company, Letd., is the most recent convert to clectrification and has selected the difficult Orizaba Division for the intial installation. Not only is the capacity of the system limited by the catrabilities uf the present steam equipment, but the operating costs are so high that savings by electrificat bion are expected to pay for the change-over in five or six years of normal traffic.- Ebitor.
()ne of the most interesting electrifications yet undertaken las been initiated by the Mexican Railway Company, Letd., on the single-track line between Mexico City and Vera Cruz. This line, which is 264 miles in lengeth (exclusive of branch lines), was at the time of its construction one of the most
in height from 17,000 to $18,000 \mathrm{ft}$. The contract received by the International General Electric Company covers the electrification of 30 miles of single track, at an estimated cost of between $\$ 2,000,000$ and $\$ 2,500,000$. This is the first main line electrification to be installed in Mexico and the first heavy steam


Passenger Train on Mexican Railway Hauled by Two Double-ended Steam Locomotives Ascending $41 / 2$ Per Cent Grade North of La Bota
difficule engineering problems ever carried through. At its maximum elevation the road reaches an altitude of 5323 ft . above sea level. It is significant that for electrification the initial section between Esperanza and Orizaba has been chosen, which is by far the most difficult division due to heavy curvatures and grades reaching 4.7 per cent ruling and a.maximum of 5.25 per cent.

This section of the road locally called the Maltrata Incline traverses a remarkably scenic country passing under the shadow of Orizaba Peak, which is one of several extinct rolcanoes in the immediate ricinity ranging
road electrification to be initiated in North America since the world war. By changing from steam to electric haulage it is expected that the necessity for double tracking the road will be indefinitely postponed, and that the saving in the operation of the system will be sufficient to repay the entire cost of electrification within five or six years.

The equipment ordered includes ten 1.50ton articulated-type locomotives, which will be used interchangeably for freight and passenger service, and trolley overhead and feeder lines complete for the direct-current supply: Power will be supplied by the Pueblo Tram-


Outline and Dimensions of 150 -ton 3000 -volt Type of Locomotive for the Mexican Railway Company, Ltd.
way Light and Power Co. whose plant is located about five miles from the City of Orizaba. A single substation containing two $3000-\mathrm{kw}$. synchronous-motor-generator sets will supply power to the entire 30 miles.

The locomotives are of particular interest since they will replace double-ended oil-burning steam locomotires, each carrying six driving axles without idle trucks. These steam locomotives are furthermore capable of operating with equal facility in either direction. The electric locomotives will also have six driving axles contained in three double trucks, each equipped with two $1500 / 3000$-volt motors. These motors will be twin geared to the driving wheels and are similar in general to the articulated truck design now operating through the Detroit Tunnel and on the Baltimore and Ohio; Butte, Anaconda and Pacific; and the Chicago, Milwaukee and St. Paul Railways. The three-truck construction with one cab, however, is new and makes possible a single unit of 1.50 tons adhesive weight without exceeding $50,000 \mathrm{lb}$. per axle. The contract provides for three running speeds with an additional arrangement for shunting the fields on light grades or with light trains. Full regenerative control will be provided and the locomotives will be capable of either independent or multiple-unit operation.

In addition to the remarkable mountain scenery, the Mexican Railway passes through a country of unusual historic interest. Between the height of land and the City of Mexico, the little known American pyramids may be seen


Map and Profile of Mexican Railway Between Mexico City and Vera Cruz
and other relics of the former inhabitants of this country. In the fertile Orizaba section, which has a semi-tropical climate, may be found growing wild oranges, bananas, grape fruit. coffee. and other tropical regetation.


150-ton Oil-burning Double-ended Type of Steam Engine Now U'sed on the Crizaba Section, Mexican Railway

## LIBRARY SECTION

Condensed references to some of the more important articles in the technical press, as selected by the G-E Main Library, will be listed in this section each month. New books of interest to the industry will also be listed. In special cases, where copy of an article is wanted, which cannot be obtained through regular channels or local libraries, we will suggest other sources on application.

## Arc Welding

Electric Arc Welding $A_{p p a r a t u s ~ a n d ~ E q u i p m e n t . ~}^{\text {and }}$. (aldwell, J.

(. Ibstract of a paper read before the Institution of Electrical Engineers. 1

## Carrier-current Communication

How "Wired Wireless" Works. Mathorgne, J. A. Tel. Engr., Dec., 1922; v. 26, pp. 19-23.
(Includes bibliography of nime entries.)
Telephony Over Power Lines in Europe. Anderson. Clifford N.
Elec. II \%d., Jan. 6, 1923: v. si, pp. 45-46.
(Short article on methods used.)

## Corrosion

Corrosion as Affecting the Metals Used in the Mechanical Arts. Hatfield, IV. H. Engr., Dec. 15, 1922; v. 13t, pp, 639-643. (Gives results of extensive tests.)

## Current-collecting Devices

New Non-Fouling Trolley Shoe Given Test on London Tramway.
Elec. Trac., Dec., 1922; v. 18, pp. 1061-1062.
(Short description including test results.

## Dielectric Strength

Plysical Nature of the Electrical Breakdown of Solid Dieleetrics. Wagner, Karl Willy.
A.I.E.E. Jour., Dee., 1922; v. 41..pp. 1034-10tt.

## Electric Distribution

Factors in Industrial Plant Distribution. Stevens, Roger B.
Elec. $11 \%$. Dec. 9, 1922; r. 80, pp. 1259-1262.

## Electric Drive-Steel Mills

Improved Rolling Mill Practice Obtained by the Use of Direct Current Notors for Main Roll Drive. Stoltz, G. E.
issoc. Ir. St. Elec. Engrs., Dec., 1922; v. 4, pp. 7.7-799.
Discusses certain principles of steel mill electric drive.)

## Electric Locomotives

Power Characteristics of the Electric Locomotive. Wichert, A. (In German.)
Zeit. des Ier. Deut. Ing., Dec. 2. 1929: v. 66, pp. 1080-1085.
Comparcs operating curves of the electric locomotire and the steam locomotive. Shows that these must be considered from different viewpoints.

## Electric Measurements

Use of Condenser-Type Bushings for Measurement Purposes. Keinath, Gg. (In German.)
Siemens-Zeit., Nov゙., 1:122; r., 2, pp. 606-614.
(Illustrated description of the applications of "Repelit" bushings for high-voltage measurements, etc., in power plants.)

## Electric Meters

Photographic Method of Meter Reading Prevents Disputes with Customers.
Elec. News, Dec. 15. 1922; v. 31, p. 39.
(Special eamera photographs each meter face.)

## Electric Motors

Neutralized Series Conduction Motor on A-C. and D-C. Cireuits. Fynn, Val. A.
A.I.E.E. Jour., Dec., 1922; r. 41, pp. 915-92:3.
(On the theory of operation of small and fractional horse-power motors on either a-c. or d-c.)

## Electric Motors, Induction

Determining the Performance of an Induction Motor without Plotting a Circle Diagram. Smith, G. T.
Elec. Jour., Dec., 1922; r. 19, pp. 485-489.
Torque Components Due to Space Harmonics in Induction Motors. Hansen, K. L.
A.I.E.E. Jour., Dec., 1922; v. 41, pp. 928-932. (Theoretical.)

## Electric Transformers, Instrument Type

Instrument Transformers for Power Circuits-I. Gibbs, J. B.
Power Pl. Engng., Jan. 1, 1923; v. 27, pp. 86-85.
(Principles of construction and operation. Serial.)

## Electric Transmission Lines

Possibilities of Transmission by Underground Cables at 100,000-150,000 V. Taylor, A. M.
Elec'n, Dec. 15, 1922; r. 89. pp. 683-684,
(Abstract of paper before the Institution of Electrical Engineers.)

## Electrical Machinery-Temperature

Relation of Overload to the Inner Temperature of Machines. Semenza, Guido.
A.I.E.E. Jour., Dec., 1924; r. 41, pp. 1031-103:3.

Some Development in Insulating Materials and Processes in Great Britain with Special Reference to Thermal Consideration. Fleming. I . P. M.
A.I.E.E. Jour. Dec., 1922; v. 41, pp. 924-92S.

## Engineering Ethics

A．S．M．E．Adopts Ethics Colk．
Pozer，Dec，26，1922：r．Sti，pp．10：30－1040．
（Gives full text of a code prepared he a joint committe of the mational engine ering societies．Intended ultimately to apply w the entire engineering profession．）

## Excess Voltage

Over－Voltage l＇roblem．Schrottice，F．（In German．）

（Repiort of experiences of the Siemens－ Schuckert Works in the operation of ower－ voltage protective devices．！

## Fatigue of Metals

Fatigue in Metals．Jenkin，C．F．
Engr．，Dec．8．19ㄹㄹ；ゾ．134，pp．612－614．
（Paper hefore the Royal deronautical Society． Gives test results．）

## Flywheels

Electric Mine Hoist with Ward Lennard Control and llgner Balancing System，Hacault，G． （ln French．）
Reiue Gẹn．de l＇Elec．，Dec．2，1022：5．12．pp． $8: 35-8+1$ ．
（Mathematical．Serial．）

## Gears

Epicyclic Reversing Gear for Ljungström Marine Turbines．
Engng．，Dec．8．1922；v．114，pp．699－703． （Illustrated description of the construction of gears manufactured by the lijungstrom Turbine Works，Sweden．

## Hydroelectric Development

Electric Plant Built on a Dam．（In French．）
Génie Círl．Dec．9，1920～～v．81，pp．529－532．
（lllustrated description of the dam and plant built on the Leguer River，near Belle－Isle－ en－Terre，France． 1

## Industries，Electrical

André－Marie Ampère．（In French．）
Revue Gén．de l＇Elec．，Special number．Nor．． 1922；$\because$ 6，pp．1－306．
（Life and works of Ampere．iogether with a number of articles on the present state of the French electrical industry in all its phases．）

## Insulating Oils

On the Use of Oil for Transformers．Mercier，H． （In French．）
Rearue Gin．de l＇Elec．，Dec．2，1922；v．12．pir 858－860．
（Gives hints for maintenance and precau－ tions to be taken in handling transformer oils．Serial．）

## Insulation

Influence of Temperature on Insulating Materials Used in Electrical Machinery．Vannotti． Ernesto．
A．I．E．E．Jour．，Dec．，1922： $\mathfrak{3}$ ．41，pp．933－934．

## Insulators

Pin Insulators on 90．000－Volt Line．Ackerman． Paul．
Elec． $11 \%$ ．．，Dec．30．1922：v．80．pp．1439－144．
（Experiences of the Toronto Power Com－ pany．

Insulators－Testing
Contribution wo the stanly of lusulabor（hame for lligh Trasion systems．Vicl．（it （ln Frenel．
 801－80：3．
（Short article supplementing the atuthor previous paper in the issue of February 2．5． 1922，p．27：3．

## Lightning Protection

Disturbances in Electrical Plamts Due to Light－ ning．
 （＂Statistical data，practical conclusions． theories，propoundel and typical cx－ amples．＂Serial．

## Machinery－Foundations

Erecting Power Machincry Having Cast－Iton Bedplates．Rea，N．I．．
Pozer，Dec．26，1922：••56，pp．1021－102：3．
（Presents practical methods．）

## Lubrication and Lubricants－Testing

Some Recent Rescarches on Lubrication．Stanton． T．E．

（Abstract of a paper before the Institution of Mechanical Encineers．On methods of testing．）

## Measuring Instruments

Elverson Oscilloscope． Engng．．Dec．S． 1922 ： $11+$ ．pp．720－72．
（Describes the construction and use of a device by means of which a rapidly moving mechanism may be made to appear slowed down or stopped．

## Oscillographs

Oscillograph and some of Its l＇ractical Applict－ tions．Borden．Perry A．
 p1． $339-347$.

Poles，Concrete
Method of Building Reinforced Concrete l＇oles． Maréchal．E．In French．
Reaue Gén．de l＇Elec．Dec．23．192ご：v．12，11） 989－992．
（Gives design of a pole which could ．le manufartured in the factory on a quantity production hasis．

## Power Costs

Cost of Power Persfon fay－Rnll．Walker．P．F． Man．Engng．，Dec．．1！2？：V．3，1p，339－3＋2．

On the subject of powe costs im manu－ facturing plants．

Power Factor
Methods for Correcting Power Factor．Hubert E．H
Ind．Engr．．Dec．．1922：$\because$ al．pp）5tif－56t． 80．5－606．
On practical methods of power－factor cor－ rection and on the economic adrantage to be derive？

Radio Communication
Radiophone Insures Service to Customers. Pearson, E. F.
Elec. I'ld., Dec. 2:3, 1922; v. 80, pp. 1395-1396. (Illustrates and describes equipment installed in the Portland, Oregon, offices of the Northwestern Electric Company.)

Scientific Management
Management. A Review of Ten Years' Progress. Alford, L. P'.
Man. Engng., Nov., 1922; v. 3, pp. 277-282.
Statistics-Electric Furnaces
Electric Steel Industry After Ten Years. Cone, Edwin F.
Iron Age, Jan. 4, 1923; v. 111, pp. 80-83.
(Consists essentially of tables of electric furnace installations in the United States and Canada.)

## Steam Boilers

Investigation and Discussion of Slag Formation on Boiler Tubes. Bates, Harry H.
Blast Fur. Eo St. Pl., Dec., 1922; v. 10, pp. 642-646.
(Gives results of tests.)

## Steam Boilers-Testing

Tests of a large Type W Stirling Boiler. Thompson, Paul W.
Mech. Engng., Jan., 1923; v. 45, pp. 25-31, 44.
(Results of extensive tests conducted by the Detroit Edison Company.)

## Steam Plants

Steam Engineering Practice in Modern Central Stations. Keating, T. E.
Elec. Jour., Dec., 1922; v. 19, pp. 490-496.

## Steam Turbines

Check on Steam-Turbine Performance. Phillips, H. M.

Power, Dec. 26, 1922; v. 56, pp. 1012-1014.
(" The nozzle or inlet pressure used to determine relative efficiency, total steam per hour, and power output.")
Dividing Load Between Units. Davison, George R.

Elec. Illd., Dec. 23, 1922; v. 80, pp. 1385-1387.
(Methods of operation of steam turbines.)

## Stokers

Developments in Stoker Practice.
Mech. Engng., Jan., 1923; v. 45, pp. 14-21.
(A group of three articles by Marsh, Bouton, and Lawrence.)
Switches and Switchgear
Enclosed Switches. Jennings, O. S. Elec. Jour., Dec., 1922; v. 19, pp. 496-498. (General considerations as to design and construction.)
Safety Switches. Vanderwaart, P. T.
Assoc. Ir. \& St. Elec. Engrs., Dec., 1922; v. 4, pp. 801-819.
(Discusses the fundamentals of electric safety switch practice.)

## Vibrations

Torsional Oscillations in Propeller Shafts. Thorne, A. T. and Calderwood, J. Engng., Dec. 29, 1922; v. 114, pp. 815-818. ("Notes on torsional oscillations with special' reference to marine reduction gearing.")

## NEW BOOKS

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Berechnen und Entwerfen von Turbinen und Wasserkraft-anlagen. Ed. 3. Holl. 181 pp., 1922, München, R. Oldenbourg.
Dictionary of Applied Physics. Sir Richard Glazebrook, Editor. 5 vol. Vol. 1: Mechanics, Enginecring, Heat. 1067 pp. Vol. 2: Electricity, 1104 pp., 1922, Lond., Macmillan Co.
Diesel Engines for Land and Marine Work. Ed. 5. A. P. Chalkley. 330 pp., 1922, N. Y., D. Van Nostrand Co.
Direct-current Machinery. Harold Pender. 314 pp., 1922, N. Y., John Wiley \& Sons.
Electric Power Plant Engineering. Ed. 3. J. Weingreen. 511 pp., 1922, N. Y., McGraw-Hill Book Co., Inc.
Electric Transients. Carl Edward Magnusson and others. 193 pp., 1922, N. Y., McGraw-Hill Book Co., Inc.
Elektrische Ofen. Oswald Meyer. 133 pp., 1922, Berlin, Vereinigung Wissenschaftlicher Verleger.
Engineering Inspection. E. A. Allcut and C. J. King. 187 pp., 1922, N. Y., D. Van Nostrand Cor.
Flow of Gases in Furnaces. W. E. Groume-Grjimailo: 399 pp., 1923, N. Y., John Wiley \& Sons.
La Force Motrice Electrique dans 1'Industrie. Engéne Marec. 613 pp., 1922, Paris, GauthierVillars et Cie.
Handbook for Electrical Engineers. Ed. 2. Harold Pender and W. A. Del Mar. 2263 pp., 1922, N. Y., John Wiley \& Sons.
Measurement of Gas and Liquids by Orifice Meter. Ed. 2. Henry P. Westcott and J. C. Diehl. 434 pp., 1922, Erie, Pa., Metric Metal Works.
Mechanical Handling and Storing of Material. Ed. 3. George Frederick Zimmer. $80 \pm$ pp., 1922, N. Y., D. Van Nostrand Co.

Production Engineering and Cost Keeping for Machine Shops. William R. Basset and Johnson Heywood. 311 pp., 1922, McGraw-Hill Book Co., Inc.
Steam-engine Principles and Practice. Terrell Croft, Editor. 513 pp., 1922, N. Y., McGraw-Hill Book Co., Inc.
Steam Turbinc; Theory and Practice. William J. Kearton. 456 pp., 1922, N. Y., Sir Isaac Pitman \& Sons.
Telcphony. Samuel G. McMeen and K. B. Miller. 943. pp., 1922, Chicago, American Technical Society.
Theory of Wave Transmission. Ed. 2, rev. George Constantinesco. 209 pp., 1922, Lond., Walter Haddon.

## General Electric Review

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## THIRTY CENTURIES

It should be of interest to the electrical industry that the rays from a 2000 -candlepower $1 / 2$-watt incandescent lamp were the first to shed light in the tomb of Tutankhamen after a darkness of more than 3000 years.

Tutankhamen, with the treasures we are all admiring so much at the moment, was buried several centuries before Thales of Miletus discovered electricity, but it was just about 2500 years after Thales discovered electricity that man made the first incandescent lamp.

Such was the speed of our development.
After the drawn wire tungsten lamp was developed in the Research Laboratory at Schenectady, in a single decade this lamp had become practically speaking the universal standard of the world.

Such is the speed of our development.
Three thousand years seems like a very long time-yet man sometimes lives to the age of 100 years-so it is just the span of thirty old men's lives.

Tutankhamen's chariots should be of interest to the modern engineer-we wonder what the distance between wheels is-how far from 4 feet $81 / 2$ inches?

Two yearshence-in 192.5-we shall celebrate the one hundredth anniversary of the opening of the Stockton and Darlington railroad. From Tutankhamen's chariot to the stage coach of 1825 represents man's progress in passenger transportation for twentr-nine centuries. From Puffing Billy to the giant "steam horses" that haul our modern passe iger trains, at 70 miles an hour, represents man's progress in passenger transportation in the last century. To this thought must be added the progress made from the sailing vessel to the floating palaces of todar, and again, the dirigibles and heavier than air machines that have
flown across the Atlantic. These are only the products of the last few years.

There are few men who really realize the slope of the curve of our modern progress and when one does realize it, they are likely to think with McAndrew, "Leaves me no doot for the machinc; but what about the man."

In talking of transportation, we wish to draw attention to Mr. WV. B. Potter's article published in this issue. Mr. Potter, the Chief Engineer of the Railway Department of the General Electric Company, spent several months in Europe studying traction conditions and we believe that his remarks will be both useful and interesting to a large number of engineers on both sides of the Atlantic.

It is pleasing to find a paper on this subject that does not criticise all that is different from home practice but that rather recognizes that the traction facilities of America and the different European countries have developed to suit the conditions of the individual country and that each has peculiar characteristics and merits of its own.

As we started this editorial with thirty centuries ago in mind, it is rather interesting to invite our readers to speculate on what our transportation will have developed into thirty centuries hence. If ariation shows the same rate of development that so many of our modern marvels have - then time, distance and oceans will have been conquered by the engineer to the point where the world should be in reality one large family and the misunderstandings between nations should disappear. In spite of our modern pace, we can not go backward, we must go forward and the making of our future civilization is one gigantic engineering problem. Fortunately, however small the part may be we can all play a part in this derelopment. J. R. H

## RADIO BROADCASTING

Until the intronductun of ratio broatcatimg, nearly all eleetrieal inventions have beers aceepted slowly by the public. The incambleseont lamp was inventerl by Edison in 1sis!, but torlay only one-thirel of the dwelling houses in the C'nited States are wired for electric lighting. Water powers, Which througl electricity may be advantageonsly utilized with a great resultant saving in our coal resources, have not been thoromghly developed. The superiority of the eleetric locomotive to the steam locomotive has been demonstrated by years of aetual service, but the general adoption of electicity for motive power by our railroads has only just begun. The same conservatism has been shown with regard to nearly every new electrical development except radio broadeasting.

The rate at which this new invention is being grasped by the public is indicated by the number of radio receiving sets being installed. Two years ago there were not more than 50,000 receiving sets in use; today the number probably exceeds one million. In the same time the number of broadcasting stations has increased from ten or twelve to more than six hundred.

The explanation of this unique public interest in a new invention is not found solely in the simplicity of radio reception, although the fact that radio programs are available anywhere to anyone who will buy a receiving set or buy the parts and put one together has much to do with the popularity of radio. However, the really important consideration is that radio broadcasting has presented us with an entirely new form of publicity which immediately takes its place with the telephone, telegrapl, post office, press, pulpit, sehool, and theater. It is the only means of comminicating instantly and simultaneously with large masses of population. One-half of the population of the United States is within the range of the Schenectady station designated by the call letters "WGY," and under favorable circumstances even greater areas are included. On last Christmas Eve a message of greeting from Vice President Calvin Coolidge, broadcast from this station, was received in every state in the Union and at Wailukt, Hawaii, Porto Rico, Liverpool, Puerta Plata, San Domingo, etc.

The newness of radio broadeasting entitles it to charitable consideration. It must be given time to develop and outgrow its youth-
fin awkwardness. Undue regulation at this time may retard its useful growth and thwart its full development.

Radio must already be eredited with many beneficial contributions to the world's prosperity and happiness. It has saved many lives in peril at sea; it provides regular and reliable trans-oceanic communication; through broadcasting it fumnishes music, entertainment, education, and news to hundreds of thousands of homes, and it shortens the tedious hours for invalids and the aged in homes and the injured and sick in hospitals. The daily weather and market reports are invaluable to the great agricultural population, and the evening programs bring music and entertainment to even the most remote districts. When roads are impassable the agriculturist may still keep in touch with the commercial world, and his family can have church services, good music, educational addresses, and a variety of entertainment.

In considering the future of radio, we do not need to draw heavily upon imagination because radio has already shown that fact is stranger than fiction. It seems evident that radio will not supersede other methods of communication and publicity but will supplement them. The great field of broadcasting is the dissemination of messages and entertainment to large masses of population and this suggests two classes of stations: A few high-power stations for broadcasting matter of national importance, and a larger number of smaller stations for the broadcasting of local matter. The President of the United States might address the entire population through a high-power station or through several such stations tied together by telephone lines; the Governor of the State of New York might address the people of that State through a local station. An analogy is found in national magazines for countrywide circulation and in local papers and publications of special interest to certain localities.

It also seems evident that a variety of programs must be simultaneously available. A thousand individuals would not care to read any paper or magazine column by column in exactly the same order and at the same time, and it is unreasonable to suppose that the tens of thousands constituting radio audiences all want just one identical program. Therefore, a variety of wavelengths should be available so that listeners may have a
choice of national news, local news, market and stock reports, concert music, dance music, educational matter, church services, and theatrical productions.

While fancy plays with these alluring thoughts, it is hoped that the power to speak so that thousands or even millions may hear will give rise to a desire to say something worth while and to say it well. Radio broadcasting carries with it a responsibility.

Developed along these lines with the sincere aim to present the best of everything to all the people, radio will have a powerful influence on the press, the pulpit, the school, and the theater. Public taste will be educated and it will demand higher standards. There will be a beneficial evolution of press, pulpit, school, and theater in which the inferior and the mediocre will be eliminated.

Senator Guglielmo Marconi, who has contributed so much to the history of radio, visited Schenectady last summer and spoke to the American people at the broadcasting station widely known as "WGY." His generous appreciation of the progress made in this country and his firm faith in the future of radio are expressed in his address, here quoted in full:
"Of all the embarassing things that may happen to one in this world, one of the worst I know of is to be called upon at very short, or practically no notice, to speak to persons, or as I am in America, I think I should say, to friends, whom I cannot see, and in respect to whom one does not even know how far off or how near they may happen to be located. Assuming, however, that you would like me to speak quite naturally, and as I really feel, I wish to say how very glad I am to be here again amongst the charming, hospitable and appreciative people of this great country, America, whom I have always so sincerely admired and loved.
"Today, I have had the privilage of visiting the Works of the Ceneral Electric Company and have been truls amazed at the progress made by this great organization since the time of $m y$ last visit to Schencetady during the war five years ago. Speaking to persons interested in radio I can truly say that the practical application and study of all branches of this new method of communication is being vigorously investigated by the engineers and scientists of the General Electric Company.
"I am now convinced more than ever that our friends of the General Electric Company are great pioneers, not only in science and engineering applied to industry, but also in numerous branches of other sciences.
"No remarks of mine are necessary to tell you about what is now being done by radio, for in America you already know so much about it yourselves, but I think that broadcasting has come to stay.
"In thousands of homes in this country there are radio telephonic receivers and thousands of intelligent people, young and old, men and women, well able to use them, often able to make them, and in many cases contributing, or striving to contribute, valuable information concerning the problems still unsolved.
"But radio is destined to improve for we are still a long, long way from any kind of finality in this fascinating art. But I think I am safe in saying that if radio has already done so much for the safety of life at sea, for commerce and for commercial and military communication, it is also destined to bring new and, until recently, unforeseen opportunities for healthy recreation and instruction into the lives of millions of human beings."
M. P. Rice.

# Radio Broadcasting Station WGY GENERAL ELECTRIC COMPANY, SCHENECTADY, N. Y. 

By W. R. (i. Baker<br>Radio Engineering Department, General Electric Company


#### Abstract

WVGl* needs no introduction to many of our readers. During the twelve months of its operation some 50,000 letters have been received from its listeners-in scattered across one-third the circumference of the globe. These, together with the public interest which the opening of this broadcasting station aroused and the anticipation with which its daily programs are awaited, all indicate that a semi-technical semi-popular description of the station would be appreciated. The following article was prepared for this purpose at our request. The comprehensiveness of its description and the many illustrations furnish a clear understanding of Broadcasting Station WGI and its engineering operation.-EDitor.


A radio telephone broadcasting station is in many respects similar to a power station. In the power system the energy of waterfalls or fuel is converted into electrical energy by means of electric generators driven by waterwhecels or turbines. As shown in Fig. 1, this


Fig. 1. Diagrammatic Illustration of a Power Distributing System
energy is then carried at a relatively high voltage orer transmission lines to a group of power users, presumably a city. A substation located near the city steps down the voltage to a value suitable for distribution by the feeder system. Additional transformers connected to the feeder system step down the voltage to that still lower value at which it is suitable to supply the consumer with light, heat, and power.

In a radio telephone broadcasting system. Fig. 2. the efforts of the artist, band, or orchestra, are converted into electrical energy. Compared with the waterfalls, this energy is of course infinitesimal. In the case of the power system the energy obtained from the waterfalls is converted into a form suitable for transmission. This also occurs at the broadcasting station with the one important exception that the energy to be broadcast is increased as it is transformed or amplified. After sufficient amplification (or increase of
energy) a final transformation occurs which converts the energy into a form suitable for distribution without the use of metallic conductors. The energy is then introduced into the non-metallic distribution system where it is beyond the control of the broadcasting station and becomes available to every consumer having equipment suitable for its reception. Herein lies the very important difference between the power system and the radio telephone broadcasting system.

We may therefore state that the fundamental function of any radio telephone broadcasting station is to convert the efforts of the artists into electrical energy and to broadcast this energy so that it may be picked up by receiving stations within the range of the transmitting station.

As might be expected there are many different types of radio telephone transmitting equipments. Roughly, we may divide them into two classes: commercial and broadcasting transmitters.

Radio telephone broadcasting transmitters differ in many respects from the commercial type of radio telephone equipment. The


Fig. 2. Diagrammatic Illustration of a Radio Broadcast Distributing System
general requirements of radio telephone transmitters, used for purposes other than broadcasting, are ordinarily determined by commercial traffic conditions. In this case, the limits of both the electrical and mechanical design are rather definitely fixed by economic


Fig. 3. WGY has received authentic reports of the reception of its programs over the range indicated by the arrows



[^19]
Fig. 8. Operator's Control for the Trans-
mitter shown in Fig. 4

Fig. 5. Four such 250 -watt Radiotron Tubes are Used in the Transmitter shown in Fig. 4 as Oseillators for Telegraphy,
and for Telephony Two such Tubes as Oscillators


山

Fig. 7. Extension Station Equipment
for the Transmitier shown in Fig. 4

Fig. 9. Three-unit Motor-generator Set for the Transmitter shown in Fig. 4. It consists of a
motor, a double-current self-excited generater motor, a double-current self-excited generator, and a high-voltage direct-current generator
and operating conditions. On the other hand, the economics of a broadasting station are rather indefinite and the method of operating is determined by factors far removed from those goterning commercial traflic.

It is logeal to expect that a broadeasting station would be somewhat similar to the better class of commercial equipments. There is, howeler, one rery important exception in that the brcadiasting transmitter has been subjected to numerous refinements which, due to toth economic and operating considerations, could not be incorporated in the commercial transmitter. In general, the commercial radio telephone transmitter is required to transmit only that rand of voice frequencies necessary to handle commercial telephony. Transmitters for broadcasting purposes must, however, transmit frequencies over a considerably wider t and, from the deepest tone of orchestral instruments and organs to the high note of the piccolo flute. The commercial transmitter is required to operate both as a telephone and telegraph set over a considerable range of wavelengths. The control equipment is designed to permit the operating personnel to handle commercial traffic with the minimum amount of suitching.

In order to ind:cate the general similarity between a commercial and a brcadcasting telephone transmitter, attention is called to Fig. 4 which shows the type of one-kilowatt radio transmitter built by the General Electric Company for the Radio Corporation of America. This transmitter is designed to provide communication by continuous-mave telegraphy, interrupted-continuous-wave telegraphy, and telephony. In this equipment four 250 -watt radiotrons (UV-204), shown in


Fig. 10. Diagram of the Physical Layout of Broadcasting Station WGY
speech amplifier. The set has a mormal water length range of 300 to sol meters Provision, however, is made so that the watedength range may be modified to coter the band of bow to ?000 meters in which case telephony is avail= able $u_{j}$ ) to 1000 meters and continuous and


Fig. 11. Diagrammatic Layout of the Radio Equipment of WGY
interrupted-ware telegraphy throughout the entire range of wavelengths. Cn the metal panel forming the front of the unit are mounted the various instruments and controls which are required to handle commercial traffic expeditiously.

The extension station equipment and the operator's control are shown in Figs. 7 and 8. The operator's control unit contains switching equipment for starting and stopping the motor-generator. The three-position control switch permits the selection of remote, local, or interphone operation. When in the "Local" position, the operator has complete control of the transmitter. When in the "Remote" position, the send-receive control is transferred to the subscriber's control unit. When in the "Interphone" position, wire telephony is available between the operator and the extension station. The power equipment illustrated in Fig. 9 is a three-unit motor-generator set, consisting of a motor, a double-current self-excited generator, and a high-roltage dircet-current generator.

It is evident that a commercial telephone transmitter such as this must contain the fundamental elements of a brcadcasting transmitter. The service requirements, however, are entirely different,

Fig. 5, are used as oscillators when transmitting continuous waves or interrupted-continuous waves. For telephony, two 250 -watt radiotrons (UV-204) are utilized as oscillators, troo as modulators, and a 50 -w att radiotron (UV-203), shown in Fig. 6, is employed as a
hence it would be expected that the structure of the equipment would vary considerably in details of design. There is also another essential difference between a commercial equipment and a station such as WGY. A commercial equipment is considered satisfactory if it
meetsall the traftierequitements impered upon it. That is, development werk on the particahar installation stops when the equipment has heen mambactured. With the broadeasting

In considering station WGY it is comvenient (o) divide the equipment into three parts; vi\%, studio, control equipment, and power plant.


Fig. 12. Building in Which the Main and Auxiliary Studios and Control Room are Located
The studio consists of rooms prepared and furnisherl especially for broadcasting service.

The control room contains all amplifying and switching equipment.

The power plant includes all equipment necessary for thegencration, modulation, and radiation of the highfrequency power.

In Fig. 10 is shown the general arrangement of the equipment used at WGY. In order to provide suitable space for the main and auxiliary studios it was necessary to locate this portion of the station some 3000 ft . from the power plant. While it is not absolutely necessary to
station, improvements are always under way and the development work is continuous.

The general requirements for a broadcasting station such as WGY are as follows:
(1) The station must be ready to operate at all times. This means that the director of broadcasting may at any time handle a special program if he so desires.
(2) Continuity of service is absolutely necessary. In other words, the equipment must be designed and operated in a manner that will prevent an interruption during a program.
(3) The quality of transmission must be of the highest order.
(4) The transmitter frequency must be maintained constant.
These requirements may be summarized by stating that the best possible service must be arailable at all times.
locate the control room in close proximity to the studio, it was found more convenient to do so in this particular instance.

Attention is called to Fig. 11 as a schematic diagram of the equipment at WGY. Frequent reference to this diagram will be helpful in co-ordinating the various units.


Fig. 13. A Portion of the Main Studio of WGY

## THE STUDIO

The studios are located in the building shown in Fig. 12. A general riew of the man studio is shown in Fig. 13. All microphone and control circuits are carried in lead covered cables laid behind the wall draperies. Connection boxes are arranged near the floor for the microphone outlets. Fig. It shows the amonncer's microphone and control box.

The auniliary studio is of somewhat similar arrangement and differs mainly in that it is considerably smaller. This studio is used chiefly for readings and lectures.

The problem of broadcasting from churches and other places outside the studio has received considerable attention. This is especially necessary when, as in the case of Sunday services, a different church service is broadcast every Sunday. A typical arrangement of pick-up derices is shown in Fig. 16 and illustrates the refinement required in order to transmit every part of the service. These pick-up derices are controlled by a specially designed unit shomn in Fig. 15. This control box contains amplifier equipment sufficient to compensate for line losses, etc. Fig. 17 illustrates schematically how the


Fig. 14. Announcer's Microphone and Control Box on the Phonograph and the Studio Manager's Indicator on the Wall
equipment is linked with the control room at WGY. With this equipment an operator located at the church switches the various pick-up derices in and out of circuit according to the requirements of the church service.
 remote point, it is frequently necesiat" o add additional amplifiers at that locatmon. This requirement of course depends upon the electrical characteristics of the lines between the control rom and the remote print. (ireat


Fig. 15. Portable Control Equipment Used in Broadcasting Church Services, etc.


Fig. 16. Typical Layout of the Microphones for Broadcasting a Church Service


Fig. 17. Diagrammatic Connection of Circuits for Picking up a Church Service, etc.
care is taken in not only obtaining high quality circuits, but in determining the amount of amplification necessary to maintain the speech always above the interference level.

## Pick-up Devices

The pick-up device which is located in the sturlio is one of the most important anits of a station since it is depended upon to transform fathentle the efforts of the artist into a form of energy that can be used by the remander of the equipment. This wnit is receiving an increasing amount of attention. While there are a considerable number of different pick-up devices in use, they may in general be divided into four classes:
(1) Carbon transmitter
(2) Magnetic transmitter
(i) Condenser transmitter
(t) Special types

Two types of microphones in the first class are available and are known as single- and

With this device, individual control of a vocal selection and the accompaniment is readily aceomplished since the vocal selection would be taken care of by a condenser or carbon microphone.

A modification of the magnetic transmitter as used for the piano has been applied to phonograph reproduction, Fig. 19. The transmitter together with a suitable filter has proved quite satisfactory.

One type of condenser microphone is shown in Fig. 20. This pick-up device is probably one of the best types for use in the studio but is sorewhat more difficult to apply outside of the station. The general system employed is either to mount the microphone on a cabinet containing at least the first-stage amplifier or to locate the unit near the end

double-button microphones. A microphone of the latter type is shown in Fig. 1S. Both types have been used considerably at WGY with very fair results.

The magnetic type of pick-up device as used at WGY not only eliminates some disadvantages of the carbon type but provides a means whereby individual control of certain instruments may be readily accomplished. This is particularly true in the case of the piano. Fig. 21 shows the mounting of two pick-up devices on the piano. In this type of device the vibrations of the sounding board are transmitted to a rotatable coil. This coil, which is placed in a strong magnetic field, has induced in it potentials which are impressed on the grid of a special first-stage amplifier.
of the studio so that the amplifers may be located in the control room. The condenser microphone requires from one to two additional stages of amplification and operates with a potential of $\overline{5} 00$ volts between plates.

A new type of pick-up device called the Pallophotophone, Fig. 22, has been used for several types of service. It is dependent for its operation upon the variation of a beam of light. This light is made to fluctuate on and off a light-sensitive cell, the increase or decrease of light causing a corresponding change in the flow of current through the circuit in which the cell is connected. Amplification is obtained in the ordinary way by means of tubes.

The remarkable quality obtained with the device depends upon two main leatures. which are: (1) the special design of the vibrating system, which is extrencely light and responds to vibrations even above the audible range, the amplitude of the mirror moverent being many tines that of the diaphragm upon which the sound waves impinge; (2) the absence of lag in the operation of the special light cell used, which lag is so pronounced in the ordinary selenium cell.

The pallophotophone as used in the studio is mounted upon a pedestal that can be easily moved from place to place, all the main con-
photographed record is passed bieds of the opening at the same specd at which the recond was taken. The variations of light pessing through the opening will correspend to the vibrations produced by the original somud waves, and in this way the reproduction will be the same as if the person talked or sang directly into the device.

In using the reproflucer in broadcasting, the electrical impulses are not again comverted into sound but are impressed directly on the amplifying system. This method eliminates the distortion that would otherwise be present.


Fig. 22. Pallophotophone Pick-up Device


Fig. 21. Two Special Pick-up Devices on a Piano


Fig. 23. Control Cabinet for the Pallophotophone Pick-up Device


Fig. 24. Pallophotophone Recorder and Reproducer
trols (Fig. 2:3) being housed in a suitable cabinet and located in the control room.

The arrangement of the device as shown in Fig. 24 may be used to record and reproduce voice or music. In this case a sensitized film is made to pass at a uniform speed behind a narrow opening across which the beam of light is made to vibrate. In this way a sort of oscillographic record is photographed upon the film.

In order to reproduce speech or music, light is made to pass through the narrow slot or opening, through which the record was made onto the light-sensitive cell, and the

## CONTROL ROOM

In order to understand the function of the control room attention is called to Fig. 2j which shows the amplification system. Nos. 1 to 10 indicate first-stage or microphone amplifiers. The microphone circuits from both the main and auxiliary studios terminate in jacks. Four different ifpes of first-stage amplifiers are provided and are selected according to the pick-up device used. The tubes (CY-202) shown in Fig. 26 are used in all cases and are operated at a plate potential from 3.50 to 400 volts depending upon the type of circuit. The circuits for first-stage
amplifiers are shown in Figs. 27 to :30 inchasive. Each first-stage amplifier has its own output contoo, filament control, and listeming-in jack. . Was asmbly of one gromp of amplifiers is shown in Fig. 3. Certam amplifiers are assigned to various classes of


Fig. 25. Diagrammatic Connection of the Amplifying Circuits in the Control Room


Fig. 26. Five-watt Transmitting Type of Tube Used in the First-stage Amplifiers in the Control Room
service; e.g., each studio has its own announcing amplifier. In addition some of these amplifiers are used exclusively for broadcasting from places other than the studio.

The output circuits of the first-stage amplifiers may be plugged into either one of two second-stage amplifiers. The input circuit of the second-stage units includes a number of jacks connected in multiple thus permitting a number of first-stage amplifiers
(1) He plugged into one secomd-stage unit. The output of the second-stage amplifier may be phaged into cither of two third-stage amplifiers. Both second- and third-stage units use one tule ( $\mathrm{U}^{\prime}$ V-20:3) operated at a plate potential of 600 volts. The circuit diagram of a second-stage amplifier is shown in Fig. 31 and that of a third-stage amplifier in Figg. 32 . Both types of amplifiers use one tube ( $\mathrm{C} V-2(0,3$ ) operating at a plate potential of (60) volts. Fig. 3.5 shows the assembly of a group of second- and third-stage amplifiers with their control equipment.

The output of the third-stage amplifier is plugged into either of two filter units indicated in Fig. 2.) as coupling units. The lines to the power house may be plugged into the particular coupling unit in use.

The input and output jacks of all amplifying equipments are located on the control board as shown in Fig. 33. The lamps at the


Fig. 27. Single-button Microphone and First-stage Amplifier Connections


Fig. 28. Double-button Microphone and First-stage Amplifier Connections


Fig. 29 Push-pull Amplifier Connections
top of this switchboard are a part of the signalling system.

Power for the filaments of all amplifiers is obtained from storage batteries. The plate supply may be obtained either from a directcurrent generator or storage batteries. All
power supplies are in duplicate, usually by providing both a battery and a generator. The battery equipment is illustrated in Fig. 36.

## Timesignal Receiver

The receiving equipment necessary to reradiate the government time signals is located in the control room. This apparatus is shown in Fig. 37 and consists of a trap circuit, tuning unit, and amplifiers.

The equipment might be considered as a special pick-up device for time-signal service. The government time signals are received and amplified until the output is equivalent to that of the ordinary studio pick-up device. The output of the time-signal equipment is


Fig. 30. Condenser Microphone and Connections of Associated Amplifiers


Fig. 31. Second-stage Amplifier at WGY


Fig. 32. Third-stage Amplifier at WGY
connected to a first-stage amplifier used solely for this service.

## POWER HOUSE

The power house is located in the building shown in Fig. 38. The apparatus employed
is comprised in gencral of the followng ("pmph ment, which is provided in cluplicate:
(1) High-voltage direct-current supply consisting of one or more batteries of kenotron rectifiers.
(2) ligh-frequency gencrator utilizing one or more radiotrons as oscillators.
(3) Modulator unit consisting of one or more radiot rons as modulators.


Fig. 33. Çontrol Board for Amplifiers at WGY

## Antenna

Fig. 38 also gives some idea of the antenna employed at WGY. It is of the multipletuned type having two tuning points. An extensive counterpoise system is utilized, a portion of which can be seen in Fig. 39, which also shows the outdoor tuning coil. The second multiple-tuning coil is located in the power house and serves to transfer power to the antenna. The towers are placed 352 ft . apart and are 16.5 ft . high above the building top which is itself 96 ft . abore the ground. The length of the flat top portion of the antenna system is approximately 200 ft .


Fig. 37. Receiving Equipment for Re-radiating Government Time Signals


Fig. 34. Firatare Amplifier at WGY


Fig. 36. Battery Racks in Control Room

## Rectifier Equipment

The directeurrent supply for the plate circuits of the tube equipment used for the generation and modulation of the highfrequency power is obtained from a battery of kenotron rectifiers. The present equipment with its filter is capable of celivering power at 12,000 volts with a ripple of less than one-tenth of one per cent. The sche-
 are comnected through a reactater atal the load commeeted as shown, ble edd multiphes of the triple-hamonic conporent will 1 on appear in the rectifed foltage wave whereas the even hamonie components will apsear. The voltage across the reactor or interphase transformer is the sum of the absolnte values of the triple-harmonic frepuency foltage due


Fig. 38. Broadcasting Towers and Antenna of WGY. The power house of the station is in this building which is located at the center of the Schenectady (N. Y.) Works of the General Electric Company


Fig. 39. A Portion of the Counterpoise and the Outdoor Tuning Coil at WGY
matic circuit diagram is shown in Fig. 40 and the actual construction is indicated in Fig. 42.

In this rectifier the delta-connected primary is supplied from a 3 -phase 220 -volt generator. The high-tension windings of the transformer are connected to form two Y's 180 deg . out of phase. Each Y with its kenotrons is thus a half-wave rectifier delivering voltage waves $E_{1}$ and $E_{2}$ with the odd multiples of the tripleharmonic component in the two Y's 180 deg. out of phase, and the even components in
to each Y . The current due to this voltage is interphase transformer magnetizing current, and circulates through the kenotron and transformer windings without appearing in the load.

The current waves drawn through each kenotron are nearly square lasting for onethird of the cycle. Since there are two hightension windings per phase passing current in opposite directions, the primary current wave is symmetrical and contains no even har-
monics. The direct-current component of current delivered by each of the two Y's is one-half of the total direct current so that each tube is reguired to pass only one-half the maximum value of current reguired per tube in the orlinary thre-phase full-wave


Fig. 40. Diagrammatic Connection of Circuits of the Battery of Kenotron Rectifiers at WGY
rectifier. The tube equipment consists of six kenotrons (UV-21S) one of which is shown in Fig. 43.

## Oscillator and Modulator Units

The oscillator circuit is shown schematically in Fig. 41. It utilizes a tank circuit loosely coupled to the antenna so that the frequency is determined chiefly by the constants of the tank or dummy circuit. The oscillator utilizes one tube (UV-20S) operating at reduced output. This tube is shown in Fig. 4.5 ; and the complete oscillator and modulator assembly is shown in Fig. 46.

The modulator employs five tubes (UT-206) such as shown in
reactance coupled amplifier. Either unit may be used depending upon operating conditions. Both units use tubes (UV-204) operating at a plate potential of 2000 volts.

In addition to the apparatus mentioned, the power house contains the necessary generators and batteries together with an oscillograph, power controls and auxiliary switches.

## OPERATION

In order to understand the duties of the operating personnel and the functioning of the signalling system, it is desirable to trace the operation of the station during the transmission of a program.

The station is manned one-half hour before the program is to start and all clocks are checked from the master clock. The two power men on duty measure the insulation of the tie lines to the control room, check all batteries, and operate the entire equipment into an artificial antenna. The senior power man then throws a switch which operates signal lights in the control room and studio indicating that the power house is ready but that power is not on the antenna. So far as the power house is concerned, the set is in operation and the two operators begin to perform their regular duties. The senior power man supervises the operation of the power equipment, monitors the radio output, and watches the modulation indicators in various parts of the circuit. By means of signal lights he informs the control room whether the modulation should be increased or decreased. In case of emergency he communicates with the control room over the intercommunicating system. The junior power man takes all readings and records them in the $\log$ at the beginning of each selection. In case the selection is a long one the

Fig. 41. Schematic Diagram of Power House Circuits

is that commonly known as the plate method of modulation. This modulation unit also includes an amplifier known as the fourth stage of amplification. The amplifier consists of two units, a push-pull and a Fig. 44. The modulating system
readings are recorded every ten minutes. This finishes the picture insofar as the power house is concerned. These men must keep the station running until directed by the control operator to shut down.




Coming back to the control room we find that the operators have checked all batteries, amplifiers, and pick-up devices and have connected in those required for the program.

In the studio, we find the announcer and his assistant arranging a group of artists. All artists not performing remain in the reception room where a loud-speaking reproducer permits them to hear the other numbers of the concert.

Assume that the artists are placed and the control room has received a signal to this effect. The senior control man throws a key which, operating contactors in the power house, transfers the set from the artificial to the regular antenna. The radiation from the antenna operates a green signal light in the control room and studio. The announcer throws a small key to its "Announce" position which through contactors connects the announce microphone and its set of amplifiers and also lights red warning signals in the studio and control room. While the announcement is being made the control man has grouped the amplifiers and pick-up devices for the first selection. After the announcement has been made, the announcer throws his key to the "Concert" position, automatically disconnecting the announce microphone and connecting in the proper concert amplifiers and pick-up devices.

In the control room the senior operator controls the grouping of the amplifiers and monitors the radio output. The assistant operator takes all readings for each selection, records them in the log, and also checks the output of the amplifiers. A third operator keeps a 600 -meter $\log$ and answers te'ephone calls. This operator also has control of a onekilowatt commercial transmitter adjusted for telegraph operation on 300 or 600 meters. This transmitting equipment is quite similar to the commercial transmitter previously described.

In case the pick-up device has been located incorrectly and the control men cannot compensate by any adjustment of the amplifying equipment, a small electric sign is lighted in the studio. This sign is located where it is not visible to the artist and indicates whether the location is wrong with respect to the soloist or the accompanist. It also indicates the general nature of the trouble. If pcsisible the studio manager then makes the necessary correction in location.

## Studio Operation

A great portion of the success of any broadcasting station depends upon the operation of the studio. The proper placing of the
artist and the relation of the various ind anments of the orchestra, band or (homens, affects the transmission very materialls. Even for the radio phay where a mmoner of piek-up deviecs may be used or where different pick-up devies are used for the various instruments, the broadcasting may be ruined by improper placement of the performers. In cases where a separate pick-up device is used for some instrument such as the piano and where the soloist has an individual pickup, the location is somewhat simplified since the relative intensities may be regulated by the individual controls associated with each pick-up device.

The acoustic properties of the studio also have a decided effect on the placement of the pick-up device, especially for music. Obviously the best method of determining the proper location of the microphone is by actually testing with the artist. This not only assures satisfactory operation during the performance but permits a gradual education of the studio manager in locating the artist and microphone to obtain the best results.

Probably the ideal condition would obtain if the pick-up device could be definitely located and the control equinment used to obtain the dcsired effcct. This could be accomplished if. for example, each instrument in an orchestra had a scparate pick-up device. In general, the individual pick-up jdea has worked out very satisfactorily for a limited class of broadcasting. In this class is the radio show, the musical comedy, and similar performances. The radio show in particular requires the use of individual pick-up devices; for instance, some casts contain from 12 to 15 performers. The use of individual microphones together with a knowledge of the play and the general characteristics of each performer permits a selection and grouping of pick-up devices which gives the most realistic results. This, however, does not stop with the performers but includes the various stage effects such as wind, the ringing of a door or telephone bell, the slamming of a door, the scratching of a match, etc. These effects are very important in order to assist the imagination of the radio theater-goer.

Obriously the operation of the studio is one of the most important and is probably destined to be the most important part of a broadcasting station. While the entire broadcasting equipment may be the best possible, unless the output of the studio is absolutely correct the desired effect on the listener is not obtained.

Trypical studio setting are shown in Figs. 47 to 50 inclusive, and on the coner of this issue of the Revano.

## QUALITY

It has bem indieated that a broadeastinge station is good to just the extent that the output of the piek-11p derice represents the efforts of the artist. This assumes that the batane of the equipment when actated by the output of the piek-up device does not introduce distortion. The distorting effects may be due to either the acceptance or suppression of a particular frequency or band of frequencies. For example, a unit might amplify some frequencies considerably better
fore transmission. The solid line indicates the actuat frepuency characteristic obtained. This characteristic was oltained by substituting a source of power for the pick-up device, hence any distortion due to the pick-up is not considered. It should be noted that the essential frequency band (100 to a000 eyeles) apmoximates very closely the incal characteristic.

## RANGE

Probably the most indefinite factor of a broadcasting station is the range. Not only is the range affected by the usual conditions incident to radio transmission, but in broadcasting it is further complicated by the lack of a common basis of agreement for defining


Fig. 51. Curve Showing the Practically Flat Audio-frequency Characteristic of WGY
than others thus resulting in accentuating those particular frequencies. Distortion may also result from overloading some unit with the result that while faithful reproduction occurs, so long as an impulse does not exceed a certain amplitude, all impulses having amplitudes in excess of this limiting value are decreased proportionately.

While these are but a few of the ways wherein distortion may be introduced, they indicate the care which is required to obtain the high quality of transmission necessary for a broadcasting equipment. The overall frequency characteristic of WGI is shown in Fig. 51. The dotted line represents the condition that should exist for theoretically per-
the term. In commercial work the range generally indicates the distance over which commercial traffic can be handled satisfactorily. With broadcasting the reception of even a small portion of a concert, or just sufficient information whereby the station may be identified, immediately establishes a new record.

It is nevertheless interesting to observe the distances that have been obtained. The map shown in Fig. 3 indicates some of the distant points from which reports of WGY have been received. In each case the report of the reception gave sufficient information to prove definitely that the writer had received an appreciable part of at least one program.

# Observations on Electric Railway Practice 

By. W. B. Potter

Chief Engineer, Rallway Department, General Electric Company


#### Abstract

Mr. Potter recently spent several months in Europe studying railway practice. This paper is based on his observations. He treats his subject very broadly and his comments should be both of interest and use to engineers in this country and abroad. This paper was presented to a double meeting of the Amurican Institute of Electrica! Engineers with part of the members and the speaker assembled at New York City and another group of members gathered at Chicago. Wire connections between the two cities terminating in "loud speakers" made the remarks at either meeting place audible at both. There was also a wire connection to the WEAF broadcasting station in New York, bringing the speech to an unknown number of widely scattered radio listeners. Duplicate sets of lantern slides were shown synchronously at both cities.-Emior.


The development of rail transportation since the day of stage coaches and horse drawn tram cars, has been a process of evolution in which some reminders of the past are still noticeable.

Before the days of steam, the track gauge used for the tram cars of the British coal mines was presumably the origin of the odd dimension of 4 ft . $1 / \frac{1}{2} \mathrm{in}$., which has become so generally accepted as the standard track gauge of the railroads of todar. In Great Britain freight cars are still called "waggons," and many of the older passenger rehicles there and on the continent are a sort of multiple unit stage coach in arrangement and interior fittings. These passenger coaches are much as if several coach bodies were mounted on a flat car, and to carry out the illusion, the exteriors of the separate compartments are sometimes so paneled as to resemble the outlines of a coach. The doors. windows and the interior are as nearly like the old stage as one could imagine. not omitting the looped strap arm rest for those sitting at the ends of the seats.

The modern European passenger cars. although retaining the compartment plan. are usually provided with a corridor throughout and restibuled passage between the cars. These cars are well equipped, comfortable and afford a privacy which we do not enjor without extra price.

Our first electric cars were converted horse-cars, and in keeping with their previous motive power, there was at first a disposition to use much smaller motors than were suitable. About one and one-half horse power was probably a fair arerage for the old horse-car: and where two horses had served. an equipment of two 10 -horse power motors seemed out of proportion despite the improvement in schedule.

While the speed was limited in the horsecar dayts there was progress in other respects. of which one instance is worthy of note. Perhaps some of you may remember the
red glass panel in the monitor of the Stephenson horse-cars that once ran in New York This panel was inscribed with the legend, "This car is equipped with super-springs, contributing to quiet and ease." You may also remember riding in these cars and the comfort derived from reading this sign-it at least had the merit of auto suggestion!

The single truck of the old horse-car was not suitable for the higher speeds and longer car bodies soon called for in electric service. The bogie or double truck motor car so generally used today was a natural adaptation from steam railway practice, and the simplicity of this design was early appreciated as advantageous for electric locomotives. One of the first electric locomotives used in regular serrice in this country was an electrically equipped bogie truck railway express car. The motor car practice of mounting geared motors directly on the axle has been quite generally applied and proven very satisfactory for electric locomotives. In continental Europe the development of the electric locomotive seems largely to have been carried out with the idea of substituting the electric motor for the steam locomotire cylinder and retaining the feature of connecting rod drive.

While there is a similarity in the character of traffic and the conditions under which it is carried on in the European countries. there is a great difference in these respects between Europe and this country. The influence of precedent. experience and indiridual opinion under these quite different conditions. has naturally led to a different riewpoint and to some differences in practice between this country and Europe. There is much to commend and little to criticize in the railway practice and equipment, as it exists in the different countries. Each country has endeavored to provide transportation of a character most suitable for its particular requirements. Occasional risits to any country do not give opportunity of
becoming well informed on this subject compromesively, but exen asmal observations, as in this instance, may serve as an cxense for comment and comparison.

The wright of Buropean froight trains and the maximmon draw-har pull allowed are about one-sparter of what they are in this country. The weight of their passenger

The screw coupler, i.e., two clevises connected by a rod with a right and left hand thread, is used almost miversally. Each draw-har has a hook that is provided with a serew coupler, and in the process of coupling the elevis of one of the couplers is thrown over the hook of the other draw-bar, and the cars in effect are jack-screwed together


Fig. 1. Reproductions from Old Prints Illustrating the Early Days of Steam Railroads in England
trains is about one-half. The permissible weight on driving wheels is about two-thirds and the weight per axle of their cars is about one-half of our usual practice. The low drawbar pull and car weight permit a relatively light mechanical design of rolling stock, and the requirements as to strength are further made easier by the method of car coupling.
by hand. There are two mushroom shaped buffers with faces about one foot in diameter; the right one having a rounded face and the left one a flat face, these are located near the outer end corners of the car. The initial tension on these buffers is about 2000 lb ., and when fully compressed the pressure is approximately $20,000 \mathrm{lb}$. As might be
expected, there is ordinarily no shock when coupling with this kind of a coupler as a slight compression of the buffers is all that is required. With our automatic couplers the shock of coupling is occasionally in the nature of a crash.

Admitting the advantages of the antomatic type of coupler, the use of the screw coupler does permit a much lighter end framing on locomotives and cars. An inquiry as to European experience with automatic couplers brought forth the comment that the couplers were all right, but that the process of coupling wrecked the rolling stock. Allowing for various requirements, the weight of European electric locomotives is from two-thirds to three-quarters the weight of electric locomotives in this country having the same horse power.

The speed of European trains on the average is rather higher than in this country. Many of the European cars have two or three axles, which does not seem to be a wheel arrangement that would provide for smooth running. In many instances these cars have no truck framing, but depend upon the car springs to hold the axles in alignment. These springs are usually about six feet long and semi-eliptical in shape, although so little curved as to be nearly flat. The springs bear directly on the journal boxes and are so resilient that the rertical shock from track joints is very well cushioned. The shorter wheel base two-axle car and many of the three-axle cars have a tendency towards


Fig. 2. Different Plans of Locating Track Joints to Illustrate Effect on Transverse Oscillations of a Car
transverse oscillation. which may be decidedly uncomfortable unless the cars are properly coupled together. The combination of the screw coupler and buffers has more influence in steadying the car and preventing oscillations than might be supposed. When the
coupling is sct up suffeciently to (r,moneses the buffers, the friction loctwen them is sufficient to prevent any relation mosement, so that each car is steadied bey the one (o) wheh it is coupped.


Fig. 3. Outline Drawings of the Latge Two- and Three-axle Cars Used on European Railways; weight 20 to 23 tons; seating 25 to 72 passengers, depenting upon the class; overall wheelbase 28 to 30 ft . The plan shows the arrangement of screw coupler and car buffers

On a fast train made up of similar cars having bogie trucks, there was a noticeable difference in the riding qualities of those cars on which the couplers had been screwed up and certain others so loosely coupled that the buffers did not touch. It is the usual practice to screw up the coupler sufficiently to compress the buffers, but there are exceptions. A remembered instance was a trip on a two axle car of about 14 ft . wheel base which was loosely coupled to the rear end of a passenger train. At a speed of about 5.5 miles the transverse oscillation, or "side slogger" as it has been called, was so bad as to cause some apprehension to the uninitiated. At the first stop the coupling was screwed up, which was all that was necessary to effectually check the "slogging." The frequency of these transverse oscillations appeared to be the natural period of the car body as cstablished by the scheme and pronortions of its flexible supporting structure. The track did not secm to induce any supplemental oscillation.

The method of locating track joints perhaps has more influence on the ruming quality of the rolling stock than is commonly appreciated. The European practice is to lay the track with square joints, i.e.. with the joint of each rail directly opposite. The customary practice in this country is to lay the track with joints spaced diagonally and located
midway betweon the opposite rail. 'The trial run of an clectric locomotive over a track with seflatre joints, which were in poor condition, afforded an execptional opportumity to observe the reaction of a track with this arrangement of joints. 'This locomotivo


Fig. 4. Curves Showing the Relative Train Friction of European and American Passenger Trains. The difference is principally due to the lighter weight of the European cars
had bogie trucks and at about 60 miles an hour there was a very decided vertical vibration, but no tendency whatever toward enforced side oscillation. With diagonally laid joints, in as poor condition, it is questionable whether any locomotive or car could have been run at that speed without something giving way; particularly if the transverse oscillation, which is diagonal in direction relative to the track, had happened to synchronize with a diagonal location of the low joints. Only one railway in Europe was noted where the rails were laid with diagonal joints. The manager remarked that his electric motor cars were subject to so much oscillation that it was his intention to relay this track with square joints.

A comparison of the influence of square and diagonal joints on the running qualities of a motor car was recently observed in this country, over a line having both kinds of joints. On the portion of track having square joints, there was observed a slight steady oscillation of uniform character at the rate of about 1.50 per minute; on the portion of track with diagonal joints the same car did not oscillate with equal steadines̀s and at times had a noticeable swing toward one side or the other. As the car was running at about 60 miles per hour, the natural period of oscillation did not correspond with the location of the diagonal joints. Had the vibration synchronized with the joints, an enforced and in-
ereased oscillation might reasonably have been expecterl. This particular track was in geocel condition throughout.

There is no doubt that track laid with square joints is more difficult to keep up) as the impact on the ballast is more severe when both wheels strike the joints simultaneously. With the less weight per axle customary in European practice, it is much casier to maintain their track, than it would be with our heavier weights per axle.

The writer suggests that it might be possible to secure the advantage of diagonal joints in respect to track maintenance and the steadier running quality of square joints, by laying the track with joints asymmetrically spaced, that is, instead of overlapping a half rail length, to overlap between onequarter and one-third, preferably a length of lap that would not be an even fraction of the rail length.

There was observed on the Great Northern Railway, England, an articulated arrangement of cars into groups, which is a departure from the conventional car with two bogie trucks. This articulation is accomplished by locating a truck midway between each of the several cars in the unit group, so that the number of trucks is only one in excess of the number of cars constituting the group. In the suburban service the trains were composed of two groups each of four cars, thus requiring ten trucks for the eight cars. On the main line the train was made up of a number of individual cars and a five-car articulated group. The reduction in weight as compared with two bogie trucks for each car. was said to be about 10 per cent; it was also stated that the train friction was reduced. A noticeable feature on the main line train at high speed was the smooth running of the group; the riding was exceptionally good and noticeably better than individual cars in the same train.

In the brief reference to electric locomotives, the motor car and steam locomotive were mentioned as prototypes, which have influenced the trend of electric locomotive development. To elaborate, there are at least seven general designs of driving mechanism or methods of motor mounting under which electric locomotives may be classified. These different classes may be briefly described as-axle geared, quill geared, outside geared. axle gearless, quill gearless, direct connected side rod and geared side rod.

Each of these designs, with the exception of the outside gear, is employed in this
country. In England, the axle geared drive has been most generally used, but there has been completed recently a high speed locomotive for the North Eastern Railway equipped with the quill geared drive. The side rod drive does not seem to have met with favor; the following reference to side rod drive is quoted from a paper by Sir Vincent Raven before the North East Coast Institution of Engineers and Shipbuilders, December 16, 1921.

On the Continent, notably in France, Switzerland, Italy, Germany, Austria and Sweden, the connecting rod drive in one form or other is almost universal. Up to the present electrification in these countries has been carried out mainly on the single-phase or three-phase system and Continental Engineers consider that the additional complications caused by the introduction of cranks and coupling rods are more than compensated for by the advantage of having a free hand with the motor design.
connecting rods and inchrded frame will bx subjected to the full strain of driving when the crank is at an angle of about 4.5 degrees. If the two sides are not in even adjustment this angle may be even less.

Aside from centrifugal forces and the shock due to lost motion in the driving mechanism, the stress in the rods, pins and frame of a steam locomotive is limited and may be predetermined from the size of the cylinder and steam pressure. With a motordriven crank the stress is dependent on the crank angle and is affected by the adjustment of the mechanism.

As an extreme illustration, one side of a steam locomotive may be stripped and with the other side on dead center, the throttle may be opened wide without damage to the locomotive. Under the same conditions with a motor-driven crank, the resultant


Fig. 5. Great Northern Railway, England. Two articulated cars showing the intermediate truck midway between the cars. Groups of five cars, similarly articulated, are in regular main-line service


#### Abstract

A large number of designs have been worked out. Some have proved quite satisfactory, others have given rise to a good deal of trouble. In most cases the trouble has been eliminated by strengthening up special parts such as crank pins. Scotch yokes, etc., and by introducing a certain amount of flexibility into the connections between the motors and the crank shafts.


The mechanism of the motor-driven side rod drive needs to be maintained in close adjustment and may reasonably be expected to require more attention and have a higher cost of maintenance than some of the other methods of transmitting power to the drivers.

The transmission of power from a motordriven crank, whether direct connected or geared, introduces strains in the connecting mechanism somewhat different from those which occur in a steam locomotive. With the best adjustment and with operating clearance only in the bearings, the motordriven connecting rods on either side transmit alternately the power through 90 degrees, except for such spring of the parts as may cause the rods to work together for a brief interval. As this transfer of the power from one rod to the other takes place at about 45 degrees from the dead center, the pins.
toggle action would set up enormous stress and undoubtedly wreck some part of the mechanism involved.

There is, further, an irregularity in the angular rotation of the crank, with respect to the driving wheel, which creates a superimposed stress on the driving mechanism, and which may be the cause of very disagreeable vibration, should the natural period of the rotating mass involved happen to synchronize with the nodal points of angular variation. The effect of this irregularity in relative uniformity of rotation of the crank and wheel is more in evidence in some forms of side rod drive than others. The most severe case observed was on a direct connected locomotive with a $V^{r}$ arrangement of connecting rods which ran with but little vibration, except at the critical speed. when a knock developed which sounded as if the crank shaft was broken, or being struck by a steam hammer. As this irregularity is due to the play in the bearings and the spring in the parts. it cannot be entirely eliminated in practical operation, but it may be minimized by maintaining the alignment and close adjustment of the bearings. It is obriously desirable
(o) diminish the shock loy enshioning ats much of the rotating mass as jonsible.

Mr. II. Parouli, chaci electrical engineer of the laris (orleans kalway, in the Reme
 has written of the vilatery characheristics of side rod drive and described the method he emphosed to improve the operation, by the introduction of springs, permitting angular mosement between the mass of the motor armature and the crank shaft.

An attempt will be mate to show graphically on the sereen something of these eharacteristics of side rod drive. To better illustrate the action, the mechanism is asstumed to be inclastic, the pin bearings of
ing axle geared locomotives in their Paris Terminal for more than 20 years and have recently ordered 200 of this type for local passenger and freight service on their main line extension. Over 100 locomotives of similar type are being built for the Midi and the State railways. Locomotives with the same type of drive are also being buitt for the Spanish Northern Railway.

The elcetric locomotives on the Italian railways are mostly of the direct connected side rod type. The workmanship and finish of these locomotives is exceptionally fine, so goorl in fact from our point of view that we might consider it an extravagance. They are well maintained, are giving good service


Fig. 6a. Diagram of Side-Rod Drive showing How Clearance in the Bearings Causes a Division of Load Between the Side Rods and Affects the Relative Angular Position of the Crank and Wheel


Fig. 6b. Curve showing Characteristic of the Change in Angular Position of the Crank with Respect to the Wheel
the rods are shown with exaggerated clearance, and the ordinates of the characteristic curves are greatly out of proportion. In reality, the value of these ordinates is dependent upon the working clearance in the bearings together with the inertia of the rotating masses and whatever may be their actual value, the character of the action calls for its consideration in the design of motor-driven side rod mechanism. Furthermore, the arc of action and the sharp angles of the characteristic curves as shown, would be modified by the spring in the connecting parts.

There appears to be an increasing interest on the Continent in other methods of drive, requiring less attention and maintenance. The Paris Orleans Railway have been operat-


Fig. 6c. Curve showing Characteristic of the Angular Velocity of the Crank with Respect to the Wheel
and many additional locomotives have been built from the same design.

The electrification of the railways in Switzerland has been very well carried out and they may well take pride in their construction and equipment. The Swiss railways have a variety of locomotives which are principally of the geared side rod type. The finish and workmanship of these locomotives is excellent, and they are very fine examples of geared side rod construction.

An interesting departure from side rod drive is a Swiss locomotive having the novel design of an outside geared drive, which is being given a thorough service trial with a number of locomotives. These locomotives have an inside frame the same as a steam locomotive, the motor being carried on the



ig. Swiss Feferal Railwavs. Gca-ct sije-rof
drive. Two moto-s a-e connectet to each of the
jack cranks, Brown, Boveri Co, an: Swiss Locomo.
tive and Machine Works, Winterthur
$\stackrel{0}{\square}$


Fig. Prussian State Railways. Direct-connected
side-rod drive with one motor throdgh a vertical
rod, A.E.G., Berlin
品

g. 7. Italian State Railways. Dircet connectef side-
ro I drive with Scotch yoke. Type originally built by
the Italian Westinhouse Vado Ligure Works and
later by other Italian manufactarers

这
Fig. 11. Swiss Fe teral Raitways. Geare is site-rot drive:


Fig. 14. Swiss Fedcral Railways. Outside geared drive. Built by Brown, Boveri \& Co., Baicn, and
the Swiss Locomotive and Machine Works, Win

Fig. 13. Paris Orlcans Railway. Axcl geared drive.
frame direetly wer the driving whed. The armature pinion is lowated berond the outer face of the driver. The gear case is attached to the lecomotive frame and is a strong structure provited with a pin in the center on which the gear revolves. The gear is


Fig. 16. Swiss Federal Railways. Outside geared drive showing location of gear and pinion with respect to the driving wheels
carried about $: 3 \mathrm{in}$. from the outer face of the driver and within the gear is a system of balanced links, which engage with the two pins projecting from the driving wheel. These links are so designed as to provide for independent movement of the gear and driver in any direction while still maintaining their relative uniformity of rotation. This locomotive runs very smoothly without any characteristic vibration, and the more general use of this type of drive on the Swiss railways may reasonably be expected. These railways have also in trial service a number of locomotives with geared quill drive.

European motive power equipment is generally of more elaborate finish and gives the impression of being better maintained than is customary with us. An instance is recalled of two steam locomotives which were double heading on the London and North Western. One of these locomotives was built in 1897 and the other in 1867 . They were polished and varnished with equal care and had every appearance of being of the same vintage, until one observed the date label, and that the older locomotive had only one pair of drivers while the other had two. As an illustration of the greater attention given to details, it is customary on many of European railways to equip both steam and electric locomotives with a speed indicating and recording instrument. The record obtained is very complete, showing the speed at all times during the run, distance covered,
time of the rum and the location and duration of the stops.

The braking equipment of European trains is (quite different from our almost miversal practice. Their passenger trains are equipped with power lorakes of either the vacuum or pressure type and usually with two brake shoes per wheel. As there are several different braking systems in use, it is necessary in some instances to equip, through cars, which rum over different railways, with more than one system. In the trans-European service to Constantinople, it is said that each car has to be equipped with four different braking systems to conform with the regulations en route.

Power brakes are seldom used on the freight trains and some of the freight cars have no brakes whatever. In many of the freight yards there will be found wooden wedges, which are for the purpose of chocking the wheels to hold the cars in place. The hand brake attachment to the braking system is usually through a screw and nut, instead of the chain and brake staff we commonly use. In some instances the brakes are applied only by a lever extending along side. To handle freight trains on grades, where the brakes are necessary to control the speed, it is customary to provide a brakeman for every four cars. In ordinary freight movements the braking is done entirely with the locomotive.

The sliding contact for current collection from orerhead lines is almost universal on


Fig. 17. Paris Orleans Railway. Locomotive with direct-connected side-rod drive. The motors have torsional springs between the armatures and motor cranks. Built by Cie Electro-Mecanique Le Bourget, and the Swiss Locomotive and Machine Works, Winterthur
the Continent, for both tram cars and locomotives. Two triangular tubes of brass or copper are used for the contact on many of the Italian three-phase locomotives, and triangular blocks of carbon are used on some of the direct current lines; but generally
for tram cars and single-phase locomotives the collector is an aluminum bow of U shaped section with a groove for lubricant.

In locomotive service it is the practice to use two of these bow collectors on cach locomotive, and because of the soft material the pressure against the conductor is limited to about $\& 1 \mathrm{~b}$. With this light pressure, some arcing might reasonably be expected and is observable when collecting from a single wire. In some places two conducting wires with interspaced hangers are used, which is better for current collection than a single wire, as it provides greater flexibility and doubles the collection contacts. Where the double wire construction had been used there was no observable arcing at the collector. While the aluminum bow serves its purpose well for collecting the 100 amperes or more for which it is used, it would not be suitable for collecting current of any great magnitude.

Collectors of this type would by no means serve for the Chicago, Milwaukee \& St. Paul locomotives, on which the current ranges from S00 to 1200 amperes. The collector used with these locomotives has two separate, flat, copper contact surfaces, while the overhead system has double wire conductors with interspaced hangers. This provides four independent contacts in parallel, each of which are $41 / 2 \mathrm{in}$. long, so that theoretically the aggregate contact is a line 18 in . long. The pressure of the collector against the


Fig. 18. Italian State Railways. View of overhead lines of three-phase system, showing long bracket arm construction and bow-shaped supports to facilitate the alignment of the conductors
conductor is about 30 lb . The relatively large amount of current taken by these locomotives is collected with no observable arcing, as the continuity of contact is well insured and the contact surface is of adequate capacity.

Any appreciable arcing at the contact between the collector and comductor is manquestionally mone destructive to both than the wear that oecurs from mechanical friction. Continuits of contact must be maintained, if destructive areing is to be


Fig. 19. Swiss Federal Railways. View of gear and pinion, showing arrangement of equalizing links, which connect at AA with pins projecting from the driver
avoided and the design of the collecting system should be such as will best ensure this continuity.

After investigating the various systems of railway electrification, a number of the European countries have established regulations in favor of a particular system for the electrification of their steam lines.

France. Belgium and Holland have decided in favor of 1.500 rolts direct current. The overhead system of conductors will, presumably, be used in these countries with but few exceptions. There was some discussion in France as to whether 1.000 volts should be the generated or the average voltage of the system. It was finally ruled that 1.500 rolts referred to the generated voltage, but that a maximum tolerance of is per cent would be allowed. There are no electrified railways of importance in Belgium and no projects under immediate consideration. In Holland an initial electrification is being undertaken between Lerden and The Hague, this being a portion of the main line that will ultimately be electrified between Amsterdam and Rotterdam.

England has also decided in favor of 1.500 volts direct current, except in special cases, of which the London, Brighton \& South Coast Railway is an example. This railway
is partially dectrified with single-phase and it is propesed to complete the clectrification with this sistem.

11 is presumable that a lino(o-volt third rail will le enite generally nsed in England. Tho Lanceshive and Vorkshre Railway have been operating over abonst en miles of thard rail at lefon wolts with suceess, for some serem vears. The North Eastern Ralway have bern operating det wolts third rail for something over in years, and have a more recent electrification, with an overhead system at Linoo volts. The London and Sonth Westem Ralway have a boon-volt third rail under consideration. The South Eastern Railway, which runs near the Greenwieh Observatory, are proposing to use two thircl rails with B000 volts potential between them, but with the gencrating and motive power equipment connected in threc-wire relation to the track, so that the voltage between each rail and ground will be only 1.000 volts. The purpose of this double rail arrangement is to eliminate currents in the earth, which might affect the observatorv instruments.

The principal railways in England, some twelve in number, radiating from London, have recently been consolidated into four groups, corresponding to the Northern, Eastern, Southern and Western portions of the country. The purpose of these consolidations is to better co-ordinate the service of the railways in each group, and to direct the transportation of the country more effectively and economically through four general Boards of Directors, instead of through the large number representing the individual railways.

There has been no official decision in Spain as to the system of electrification for their steam railways. There is in operation a short line equipped with the three-phase system. An important elcetrification on the Spanish Northern Railway, over a mountain division in the north of Spain, will soon be in operation with :3000 volts direct current.

Switzerland has standardized the singlephase system at $1 \mathrm{C} 2 / 3$ cycles for their principal electrifications, and this system is being generally extended, although 1500 volts direct current is being used on some of the smaller railwass. For other than single-phase railways, the standardized frequency is 50 cycles.

The Italian electrifications are almost exelusively three-phase, although there are several lines equipped with 600 volts and there is a reecnt installation of 4000 volts direct current. Consideration is being given
to a thorough trial of 3000 volts direct current in the central portion of ltaly, south of the present \%one of threephase operation.

Cermany is contiming the use of singlephase for steam railway electrification, although it was stated that 1.200 volts direct current woukd presumatly be employed for heavy multiple anit and interurban service.

The suljece of clectric railway systems is under discussion in Sweden. The more important existing electrifications are equipped with the single-phase system at $102 / 3$ cycles. As the standard frequency for general purposes is 50 cycles, there appears to have arisen some question as to the expediency of generating and transmitting a particular frequency for the railways only. The more general utilization of natural resources and the better load factor resulting from diversity of use, would seem to indicate an economic advantage in favor of generation at the standard frequency with substation conversion into whatever form of electrical power the railways may require.

The economy in fuel obtained by modern steam power stations and the many available sources of hydraulic power have contributed to stimulate greatly the electrification of the steam railways in Europe. Government endorsement of the projects has also been helpful in financing these enterprises.

Table I, compiled from available records, will give an idea of the extent of railway

TABLE I
STEAM RAILWAY ELECTRIFICATION

|  | Route Miles | No. of <br> + lectric <br> Locomotives |
| :---: | :---: | :---: |
| United States | 1607 | 375 |
| Switzerland. | 661 | 156 |
| Italy. | 650 | 309 |
| France | 602 | 338 |
| Germany. | 550 | 49 |
| Austria. | 340 | 42 |
| Sweden. | 237 | 44 |
| Cuba | 180 | 18 |
| Africa | 174 | 77 |
| Chile. | 154 | 42 |
| England | 129 | 12 |
| Canada. | 49 | 9 |
| Spain. | 48 | 17 |
| Japan. | 39 | 42 |
| Norway | 39 | 37 |
| Mexico. | 30 | 10 |
| Brazil. | 26 | 16 |
| China | 25 | 13 |
| Java. | 25 | 5 |
| Total | 5.565 | 1611 |

chectrifieation throughout the world．It in－ cludes the steam railways which hare been cleetrified or are in process of electriti－ cation，hut not the steam railways on which multiple unit trains are being used exelusively． or electric railways which were not formerly operated by steam．

This is less than 1 per cent of the railway ronte mileage of the work．Conceding the
 of the wordds sorvice of ore sthl ratham－at very large mileage whith ond b be allon－ tageonsly electrified．In the exactution of this great undertaking we have many engitecring and economic pohlems，the solution of when demands the cordial corneration of all who are engaged in the furtherance of ratwat transportation．

# Arc Welding of Cast Iron <br> PART I 

By゙ W．H．Namack


In our last issue a discussion was given of the general considerations that must be taken into acount in the welding of cast iron．The composition of such iron was analyzed with regari to the intluenc．which each of these components have on the weldability．The following article，which is an abstract of the first part oi a paper delivered by the author at the fall meeting of the American Welding Societri，presents further informa－ tion relative to the investigation made by this society to determine the technique of welding cast iron by the carbon arc and by the metallic arc processes，the latter with and without studs．The succeeding installment will detail results of an extensive test which was conducted to notain additional data on the metallic arc well－ ing of cast iron without studs．－Editor．

There are two fundamental methods of arc welding cast iron：riz．，by the carbon arc，and by the metal arc．The latter may be divided into metal are welding with studs and metal arc welding without studs．Each type of welding mentioned will be treated in the order named．

## CARBON ARC WELDING OF CAST IRON

Carbon arc welding is used over a con－ siderable range of application and somewhat resembles the oxyacetylene method．one difference being the way in which the heat is produced．Difficulties are encountered in welding thin sections by the carbon arc process．In welding cast iron with the carbon arc，the casting is sometimes preheated． When this is done，the same precautions must be used（both during heating and cool－ ing）as in the case of gas welding．

Obriously it would be desirable if the weld area could have the same composition and characteristics as the original cast iron． With a riew to approaching this result，the conditions under which the weld is made should preferably be similar to those em－ ployed in making cast iron and the same precautions taken with respect to slow uniform cooling to allow for precipitation of the carbon from the combined state．in
which it exists in the molten case irmo into the graphitic state in the fimished well． The welded part will be machineable ：o the extent to which this result is attamerl． Welds of this kind are possible with the carbon are method，if the precautions sug－ gested in the following paragraphs are followed．

## Preheating

Unless the work is very small and of simple form，it should be preheated in a ＂dull red＂heat to minimize shrinkase stresses．Where the work is complicated． slow heating is necessary Uneven heating may cause warpage and introduction of stresses．

## Manipulation

The arc is applied to the edges to be welded until the iron commences to melt．Then the bottom of the $V$ is melted down，applying during the fusion a little flux or scaling powde： with the heated end of the filler rod．It is important that the two edges to be foned should melt at the same time．Metal from the filler rod should nos be added until the bottom of the $V$ has been filled by metal from the sides．When ready to add metal． the end of the filler rod should be placed in
the methed metal of the welle and the are played on looth the rox and the wed so that the medal rums logether. The rod should be dipperd in the scating powder as often as is necessaty and the lifling in process comtimused. Howerer, ton much scating peowder


Fig. 1. 1llustration of a Single Stud and Its Location Relative to the Hard Zone
should not be added at one time. Only just chongh is neceded to make the metal run frecly: The weld shoukd be made in steps. If too much metal is added in one place it is likely to run into the bottom of the $V$, and unless the welder is experienced and carefut this will cause a "cold shut" and the weld will be defective. As the filling progresses, the operator should satisfy himself that the metal is welded at both sides.

The melting of the filler rod should take place as much as possible in the molten bath in the bevel by plunging in the rod and then playing the are all around. This method should always be used for great thicknesses.

Certain essential manipulations are sometimes difficult to execute. For example, the fluidity of the motal when melted does not permit of making vertical welds. It is therefore desirable to arrange the line of welding as nearly horizontal as practicable, although this is difficult with certain shapes and sizes of pieces to be welded.

The fluidity of molten cast iron makes it necessary in certain work suitably to surround or support the edges to be welded in order to prevent the metal from flowing away.

## Filler Rod and Flux

One adrantage of the carbon are process is that the filler rod can be of cast iron, thus permitting of actually depositing cast iron in the weld. This procedure will, when a suitable flux is used, tend to produce the same general characteristics as those of the base iron. To the extent to which this is effecterl, the subsequent machining of the parts will be practicable.

A good flux can be made of a mixture of equal parts of carlonate of soda and bicar-
bonate of soda. Washing sorla is the name commonly given to a somewhat impure carbonate of soda, while licarbonate of soda is ordinary baking soda. There is no necessity that either shoukd be in a chemically pure state. The action of the carbonates is to combine with the oxygen in the slag. releasing the irom and allowing the oxygen to pass off in the form of cartom monoxide or carbon dioxide.

With cast iron, the oxide formed is lighter than the melted metal and does not flow at quite so low a temperature. The slag which forms on the surface of the iron therefore tends to hold the melted metal in place. Scaling powder should be added by dipping the rod into the powder only when the metal does not flow well and no more should be used than is necessary.

When using a flux in welding cast iron it will be noticed that, as soon as a small portion of the flux is put on the melted iron, the surface of the metal becomes clear and mirror-like, thus making a grood weld possible.

## Annealing

After the weld has been completed, it is desirable that the cooling should be as slow as possible. For articles which have been preheated it is best to replace them in the oven and cover them completely with asbestos or some other non-conductor, so as to avoid local cooling.

Many articles of cast iron, although they have been properly welded, break or crack in cooling, either in the line of welding or elsewhere, owing to a failure to observe such precautions as shall prevent local contraction.

When a coke or charcoal fire has been used for preheating, the piece welded should be completely covered with cinders or charcoal;


Fig. 2. Cross Section of a Studded Joint
refractory bricks or sheets of asbestos should be placed on the sides and underneath, so as to avoid all draughts of cold air, and the article should be left until it is completely cold. Sometimes it is necessary to allow twenty-four hours for cooling.

## METALLIC ARC WELDING OF CAST IRON

Much cast iron are wedling is now done with the metallic are process. In this process an are is drawn between a metal wire electrode and the base metal. the filler metal being supplied be the metting of the electrode. In this respect. the process is exactly the same as that employed in the metallic are welding of steel. Howeres, owing to several circumstances amonest which may be mentioned the high percentage of impurities contained in cast irom, its hrituleness, low strength, and comparatively low melting point, the making of a dependable cast iron weld is very much more difficult with calst fron than with mild steel.

## Penetration

It is extromely diffieult to obtain good fusion of the filler metal with the cast irom. or as it is commonly temed, good" "penetra-


Fig. 3. Procedure in Welding a Studded Joint in Which Squaresection Grooves Have Been Cut to Protect Against Shrinkage Strains
tion." This is particularly true of gray iron. White iron being distinctly easier to weld. The greater difficulty of welding gray cast iron seems to be due partially to the flakes of free graphite present. These tend to separate the filler metal from the
 of irom from each wher

## Carbon Content

In welding cast irom he the metallic atte process, the surfaces whe joinerl ate modted be the heat of the are between the efectonte and the hase material. In gray irnm, these surfaces consist of iron which montams


Fig. 4. Method of Welding a Studded Joint Where the Carbon is in Condition to Produce Good Fesion Between the Casting and the Weld Metal


Fig. 5. Cross Section of a Studded Joint in Which a Strip of Copper or Soft Iron Has Been Inserted
carbon in both the combined and uncombined states. As soon as the heat of the are is removed, the melted iron solidifies very quickly, owing to its proximity to the comparatively cold mass from which it has been melted by the are and further owing to its being exposed to currents of cold air. Naturally this portion of the metal which has been made liquid and has cooled quickly is very hard, and furthermore any uncombined earbon which is brought io the surface also has a deteriorating effect on the weld, since it acts as a separator between the deposited metal assuming that the filler metal is deposited in layers) and the metal which was melted on the surface of the cast iron.

## Oxidation

When iron is brought to a high temperature in the presence of oxygen. as in wetding, oxidation of the metal takes place. When it becomes oxidized the oxide segregates out and being in a granulated state it with, if trapped in the weld, cause a weakness and make it impossible to fuse the added metal io it. This difficulty may be orercome if due care is exercised in remoring this surface oxide by means of a stiff wire brush.

## Shrinkage

As the metal in a weld eowh from the molten state, its voblame dereases comshomably For example, the eontraction of (ast iron in cooling from its melting point (1) orthary foom temperature is appors-


Fig. 6. Gear Repaired with Bare Electrodes Using 150 Amp. Each Weld Reinforced Approximately $\frac{3}{16} \mathrm{in}$. at the Center of the V Groove; Cost $\$ 13.00$
imately one per cent. This amounts to one-eighth of an inch per foot of length. Consequently, if the two parts being welded logrether are not free to move in response to the forces set up by the contraction of the weld metal, very severe stresses will result. As cast iron has practically no ductility, these stresses may break the easting. unless they can be relieved by the stretching of the filler metal.

The situation is complicated by the fact that if steel is used as a filler metal, as is ordinarily the case (i.e., if a steel eleetrode is employed), the shrinkage of the filler metal is from 50 to 100 per cent greater than that of the cast iron itself, since the contraction of steel, during cooling, is from 1. i $^{-}$to 2 per cent. Therefore, there is a tendency for the filler metal to slide over the iron, often resulting in a break at the line between the filler and base metals.

## Shape of Casting

The shape of the casting must also be considered in connection with shrinkage. If a heavy section is heated up by welding and if its expansion, when heated, throws : stress on a lighter section elsewhere in the casting, that lighter portion is liable to fail. Again if a light and heavy section are heaterl equally and then cooled, the lighter section will cool (and consequently contract) faster than the heary section and a break through the lighter section is liable to occur.

## Use of Steel Studs

A very sucecssful method of overcoming trombles due to shrinkage consists in employing stecl studs serewed into the cast iron, the filler metal being welded to them. These studs pass through the brittle layer of iron at the weld and transfer the stresses to the mass of metal back of the weld.

Obriously the use of studding entails considerable expenditure of time and labor, owing to the necessity for drilling and tapping the holes and inserting the studs. It appears, however, to be the consensus of opinion of are welding speeialists that studding should at the present stage of our welding experience be employed when the east iron parts are not free to adjust themselves in response to the contraction stresses set up duringr cooling.


Fig. 7. Cylinder Repaired with Bare Electrodes Using 175 Amp. Quarter-inch studs were used without V-ing out the work

In applying the studding method it is general practice to so chip out the crack to be welded as to form a V. Studs are then inserted in one or more rows, either in the faces of the $V$ or alongside it, or at both these locations. Studs on one side of the
weld are placed opposite the corresponding studs on the other side. If, however, more than one row of studs is used, the studs in adjacent rows on each side are usually: staggered. The stud holes are drilled and tapped with a bottoming tap. The stucls are serewed in tight, completely filling the hole for a depth of about one and one-half to two times the diameter of the stud. It is convenient to use rods threaded for their entire length. These are screwed in tight and are sawed off at a distance of ${ }^{1} \mathrm{~s}$ in. or more above the surface of the work, the precise distance depending upon the size and shape of the weld.

The determination of the size and number of studs to use is a matter of calculation and experience. The combined strength of the studs should be sufficient to develop the full strength of the cast iron. As steel has approximately four times the strength of cast iron, the ratio of the total crosssectional area of the studs on one side of the weld, to the cross-sectional area of the cast iron, should be approximately one to four. The technic of the process is ordinarily better when large studs are employed for large sections and smaller studs for smaller sections.


Fig. 8. Welding a Steel Patch to Repair a Cast Iron Break

The usual welding procedure is to first weld around each stud forming a cone-shaped pad of deposited metal and to then weld from pad to pad until the entire face of each side of the V is covered with steel filler metal. Finally, the space between those faces should
be filled in be welding $\mathrm{It}^{2}$ is sometimes recommended that the filling in betwerg faces be done by boying in beads along the length of the weld, rather than eross-wise, with the idea that this may reduce the comtraction stresses across the welle 'This


Fig. 9. Completion of the Repair Work illustrated in Fig. 8
method is liable to reduce somewhat the tensile strength across the filler motal itself but as its strength is ordinarily much higher than that of the cast irm base. a small reduction is not serious.

## Hardness at Weld

When cast iron is welded he the metallic are process, without preheating, there is usually a layer of extremely hard metal at the junction of the filler and base metal. This is sometimes so hard as to be unmachineable. except by grinding. This hard layer is ascribed principally to the formation of what is known as "white iron."

This white iron is formed when the molten surface laver of east iron is chilled by the cold mass of metal lying back of it. In white iron, which is extremely hard and brittle, the carbon is held in solid solution. In this form the earbon is present as combined carbon.

Furthermore a portion of the steel filler metal. while molten, ahoorbs some of the carbon from the molten east iron, becoming high carbon steel and is also quickly cooled, giving in effect a laver of quenched high carbon steel.

It is suspected that the formation of nitrides in the weld may also be a contributory cause
of the extreme hatoluess hal fat it appears that the extremse hatelacss often experienced is duc to somed hing more than simply the formation of white rats iron. Methods of reseameh (o) determine the trome cause and possible methoule of orereombing this hard-


Fig. 10. Break in Cylinder Block Studded Preparatory to Welding


Fig. 11. Cylinder Block Shown Above After Being Welded

If no furnace is available, a temporary one may be built of fire bricks and the casting heated by a coke or charcoal fire. Care should be exercised to see that all parts of the casting are heated miformly and it is best to heat it rather slowly. For preheating, a temperature of about sor deg. ( . (corresponding to a "dull red" h. i) should be employed. The weld sli ild be inade promptly and the casting allowed to cool down very slowly in the furnace. If the casting has been heated with a charcoal or coke fire it should, while cooling, be covered with ashes and embers.

For annealing after welding, which is desirable if the very best results are wanted, the easting should be heated to a "red heat" (about 850 deg. C.) and then allowed to cool very slowly in the furnace.

## Inserting Copper Strips

When only one side of a weld need be machincable, the following practice is sometimes adopted. The break is V'd out, with the apex of the $V$ on the side that must be soft. Then a strip of copper is laid on the $Y$ and peened in. The steel filler metal is deposited in the $V$ above the strip of copper. The copper filler is of course readily machineable.

## Reversed Polarity

In ordinary metallic are welding of steel, the work is connected to the positive terminal of the welding current supply source and the electrode to the negative. As considerably more heat is generated at
ness are of much importance and have been considered by the Committee

## Preheating and Annealing

The best method of avoiding the hard zone from the standpoint of metallurgical results would seem to consist in preheating the casting before welding, or annealing it after the completion of the we3d. By either preheating or annealing, if properly done, the hard zone can usually be avoided, without prejudice to the quality of the weld. The unfortunate circumstance is that either preheating or annealing is expensive and requires special equipment. It necessitates placing the casting in a furnace or some equivalent process and may result in warping the structure.


Fig. 12. Large Lathe Chuck Repaired with Bare Electrode using 175 amp . Cost $\$ 21.00$
the positive end of an are than at the negative. it has been proposed that in the welding of cast iron the polarity be "reversed, " making the work neyative and decreasing the temperature at the point of application of the are. However even though the local temperature is decreas d, a certain amount of the iron must be nselted in order to obtain a weld and chited iron is bound to result. On the basis of this reasoning "reversed polarity" should not be particularly effective in preventing the hard zone. Nevertheless some welding people of wide experience claim that softer welds are obtained in cast iron welding when "reversed polarity" is employed.

## Special Electrodes

Electrodes of a wide variety of compositions and with various kinds of fluxes and some with flux coverings have been recommended and used for welding cast iron. The Committce is not prepared to say how effective these electrodes are, nor which is best

Nickel electrodes are quite widely used in filling in blowholes in castings, for example, in automobile cylinders. Nickel possesses the advantage of not absorbing carbon from the cast iron. Hardness is thus avoided


Fig. 13. Casting Prepared for Welding by the Studded Joint Method
and a machincable joint is ohamol lhw ever, there is liable to be a small \%one on chilled cast iron around the joint. It wombd appear that nickel should not be emphoved in a weld which will be placed in tension or shear.


Fig. 14. Finished Welding Repair of the Casting Shown in Fig. 13
The Committee found that joints made with a nickel electrode using reversed polarity were not dependable as the filler metal consisted mainly of blowholes and gas pockets.

Phosphor Bronze electrodes are reported to have been employed with some success in producing machincable cast iron welds.

Monel Metal and other copper nickel electrodes are said to give a soft weld in cast iron and one of much strength. Howerer these, electrodes are relatively expensive and it is believed that the deposited metal is apt to contain gas pockets. Consequently where these electrodes are employed, it is general practice to use them only on the first and last lavers, or at places where holes are to be drilled. The remainder of the filling may be done with steel.

# Ten Years of Progress in the Design of Safe Tanks for Large Transformers 

3y W. S. Moons


Mr. Momly thls of the development of the conservator type of transformer. He shows that the use of inert gas torfminate explesions and the "sludging" of the wil was considered and tried ont at an early date. These ideas were later abandoned for the conservator principle which keeps the transformers filled with oif comstantly - Emator.

In the ()etober, 1909, issue of the Review the writer, under the heading "A New Form of Tank for Static Transformers," (leseribed the conservator type of transformer and the results of the three years of experience with this type.


Fig. 1. Original Installation of Transformer Using Inert Gas

The continued practical success of the original construction and refined improvements thereon during the past $31 \frac{1}{2}$ years, applied to a total capacity of over $5,000,000$ kr-a. of such transformers now built, fully justifies the optimistic view taken of the value of this construction.

This extensive use of the construction, and certain recent publications in the technical and daily press regarding a possible alternate form of construction, will make
some remarks regarding the history of this development of interest to many Review reaters.

Early in 1914, the great increase in the demand for large transformers suitable for installation out of doors, without protection


Fig. 2. Installation of $5000-\mathrm{kv}-\mathrm{a}$. 140,000 -volt Single-Phase Transformers with Conservators. Consumers Power Co., Battle Creek, Michigan
from the weather, caused the engineers of the Transformer Department to study very thoroughly the problem of making the tanks of such transformers absolutely weatherproof.

To so make the joints between the cover and tank and the numerous joints necessary between bushings, oil gauges, manhole covers, breathers, etc., reliably weatherproof, was not a simple matter. It was also realized that however well these features might be designed and built trouble from leaky joints might
occur, as most of these joints must be remade a: the time of installation

Efforts were therefore made not only to incorporate simple and reliable methods for making these joints, but to find a construction that would immediately indicate any defect in them. One of the most promising methods appeared to have the air in the top of the transformer under slightly greater pressure than the atmosphere with a suitable indicator to show if any air was escaping. To this thought wos added the idea that
 General Electric Field Engincer. Mr F: I Green (now deceased), costering this combination of transformer, inert pats, and pasmmeter.

Fig. 1 shows, rather poorly, the installation of the $5000 \mathrm{kr}-\mathrm{a}$. transtormer at Providence. R. I., with which this invention was testerl out for some six months in 1911 ;

The method would undoubtedly have been used extensively be the Company from that time on had not a still better methou of


Fig. 3. Installation of Conservator-Type Transformers at the Vacaville Substation of the Pacific Gas \& Electric Co. Single-panase Auto Transformers $0: 16,667-\mathrm{kv}-\mathrm{a}$ output to transform from 200,000 to 100,000 volts
instead of air under slight pressure, an inert gas might be used, thereby avoiding any possibility of an explosire mixture in the tank.

An appropriation to test the practicability of these ideas was obtained early in 1914. and factory tests were so satisfactory that in 1915 two orders were taken, one for 750 $\mathrm{kT}-\mathrm{a}$. transiormers for the Remington Arms Company, and one for $5000 \mathrm{kr}-\mathrm{a}$. units for the Narragansett Electric Company. With the customers' consent it was planned to give this construction a service test on these transformers.

The installations were made in March and May. 1916. $\mathrm{CO}_{2}$ gas was used because it can be so easily purchased almost anywhere and a small "gasometer" was designed and used to maintain the slight internal pressure on this gas. The method was found quite practical, only four or five rechargings per year of the small gasometer being necessary.
accomplishing all the desired results been found, largely as a result of these experiments.

These efforts to reduce the loss of inert gas in these transformers to a minimum led to simple and reliable methods being found to eliminate any leakage; there was no longer. thereiore, any necessity for any gas within the transformer. for such a tank could, with safety, be completely oil filled and kepi under a slight pressure from an elevated reservoir partially oil filled. Thus these experiments with the inert gas led directly to the present "conservator" constructiona simple and safer construction

This construction, as stated in my 1919 article. was first given a service trial in 1916. at Laurinsburg. N. C. The construction has been repeatedly simplified and improved as to details. and today accomplishes all its duties with utmost reliability

# Studies in the Projection of Light PART III <br> CHARACTERISTICS OF A PARABOLIC MIRROR AND SPHERICAL SOURCE OF LIGHT 

By Frank Benford

Physicist, Illuminating Engineering Laboratory, General Electric Company


#### Abstract

In the first installment of this series a description was given of a simple and practical method of optical analysis as applied to the reflection of light from a paraboloid (parabolic reflector). In Part II analysis was made of the reflection of light from parabolic cylinder (parabolic trough) and ellipsoidal reflectors. In the present installment an explanation is given as to why the filament of a projector incandescent lamp can be treated as a spherical source when the lamp is mounted in a reflector of the conventional parabolic proportions. The characteristic formation of the beam is next discussed with reference to the increase of central intensity with distance, the inverse-square region, the testing distance for central intensity, and the width of the crest of the beam.-Emitor.


## The Spherical Source as a Substitute

One of the goals toward which the designers of incandescent lamps are striving is the production of an incandescent filament of spherical form. The goal seems to be far in the future, and can be seen only with the eyes of optimism; but there is a certain physical relation in the incandescent searchlight or floodlight that brings the final result in beam formation even now measurably closer to the desired end. This relation is between the mirror and the light source, and it applies particularly when the mirror is deep in proportion to its diameter.

Concentrated filaments in lamps designed for projection service have several forms. The wire is first wound into a close spiral and this spiral is then bent into loops that are held as close together as seems safe considering the voltage difference between the various parts of the filament. The filament arranged in this manner has but little outward resemblance to a sphere, but we must consider what takes place when it is used in connection with a mirror that partially encloses the lamp. There is a rule of geometrical optics that, while seldom found stated explicitly, might be worded as follows:
"Each section of a simple lens, or mirror, forms an image whose angular size and proportions are identical with the angular size and proportions of the object as viewed from that section." Thus if the source is a ring type filament, which is a more or less complete circle, and the plane of the ring is perpendicular to the axis of the mirror, the beam from the center of the mirror will have an annular form with an open side corresponding to the open side in the filament. A section of mirror to one side of the filament and in its plane will project a narrow vertical
beam; a top section of mirror will project a narrow horizontal beam. These two sections alone, if the remainder of the mirror is covered, will project a beam that has a crossshaped section. But if the entire zone containing these two sections is active in reflecting light, then there will be a multitude of crossing sections that will build up a perfectly round beam that has its greatest intensity in the center and tapers off gradually to a round outline. This beam bears no outward resemblance to the form of the filament, and while it is an extreme case it well illustrates how the mirror may influence the beam formation.

Mirrors used with incandescent lamps are in a great majority of cases of considerable depth, and the resultant beam is composed of a multitude of the filament images that vary in size and proportion, and it is solely due to the resulting blurring out of sharp images that we can in our mathematics substitute a spherical source for the actual source and then by computation arrive at the approximate facts. It will be readily appreciated that a filament that is even roughly spherical in outline will be better represented by the substitute source, and that a shallow mirror which has, so to speak, a single angle of view will give a sharp image for which we can find no satisfactory substitute. However, fortunately for the simple theory of the subject here presented, a great majority of incandescent units have deep reflectors in which the phenomena of multiple images and varying perspective have full sway.

## Increase of Central Intensity with Distance

Every searchlight or floodlight has a critical point on the axis of the beam beyond which we can compute illumination with certainty, and short of which there always
exists much doubt. It is important to know where this point is located, and what is the geometrical structure of the beam up to this point. It may seem somewhat strained to speak of the "geometrical" structure of the beam, but the term is fully justified by experimental facts; and using the simplest kind of geometry the entire beam may be analyzed by anyone willing to take the trouble. The analysis here presented does not cover all the ground, but only that part which seems of prime importance and necessary to know if one is to get the maximum benefit out of the material and equipment now a a ailable.

In Fig. 17. two sections $P_{1}$ and $P_{2}$ of a parabolic mirror are shown reflecting two images of the spherical light source located at the focal point of the mirror. At increasing


Fig. 17. Elemental Images of Spherical Source as Projected by a Parabolic Mirror
distances the two images $A_{1}$ and $A_{2}$, which in this case are circular, will touch as they come into contact with the extended axis of the mirror; and at this point all of the mirror within the zone through $P_{1}$ and $P_{2}$ will be active; that is, it will reflect light through this point of contact. All the area outside of $P_{1}$ and $P_{2}$ will be inactive in reflecting light to the axis at this particular distance $L_{0}$, and the apparent beam strength is therefore

$$
\begin{equation*}
I=\pi B m y^{2} \text { candles } \tag{40}
\end{equation*}
$$

where $B$ is the brilliancy of the source in candles per square inch; $m$ is the coefficient of reflection of the mirror; $y$ is the radius in inches of the outer edge of the active area.

It should be noted that the beam intensity is proportioned to the projected area of the mirror and not to the surface area. Also, the distance $L_{0}$ should be measured from the edge of the active area, and not from the plane
passing through the edge. This latter peint is of small importance because the difference between measurements of $L_{0}$ made from the center and edge is very small and mas be neglected.

The radius $h$ of the image $A_{1}$ is proportional to the radius $r$ of the source, is also proportional to the distance $L_{0}$, and inverscly proportional to the radius vector $p$ from the focal point to the point $P_{1}$ on the mirror. Therefore

$$
\begin{equation*}
h=\frac{12 r L_{01}}{p} \text { inches } \tag{41}
\end{equation*}
$$

where $L_{0}$ is expressed in feet and the other dimensions are in inches.

Rearranging, we have

$$
\begin{equation*}
L_{0}=\frac{h p}{1 \ddot{2} r} \text { feet } \tag{42}
\end{equation*}
$$



Fig. 18. Increase of Central Intensity with Distance from Parabolic Mirror 18 in . in diameter; Spherical Source 0.5 in . in diameter
and at the point of contact of the image $A_{1}$ with the axis, we have

$$
\begin{align*}
h & =y \text { inches } \\
& =2 F \tan \frac{a}{2} \text { inches } \tag{4.3}
\end{align*}
$$

Therefore, in terms of $F, r$ and $a$,

$$
\begin{equation*}
L_{0}=\frac{F^{2} \tan \frac{a}{2} \sec ^{2} \frac{a}{2}}{6 r} \text { feet } \tag{44}
\end{equation*}
$$

or, in terms of $F, r$ and $y$

$$
\begin{equation*}
L_{0}=\frac{y\left(t F^{2}+y^{2}\right)}{t \Delta F r} \text { feet } \tag{45}
\end{equation*}
$$

and in terms of $F$ and $a$ the intensity on the axis is

$$
\begin{equation*}
I=4 \pi B m F^{2} \tan ^{2} \frac{a}{2} \text { candles } \tag{46}
\end{equation*}
$$

or, in terms of $y$

$$
= \pm \pi B m y^{2} \text { candles }
$$

These equations give the desired relations between the axial intensity and the distance
I. 1 . In lig. Is, data from eduations ( 44 ) and (16) are plotted for three mirrors is in. in diameter equipped with a spherical source of 0.25 in . radius. The brilliancy of the source is 10,000 candles per square inch and the coefficient of the mirror is 0.85 .

Nirror A. Fig. 1s, has a focal length of 7.79 in . and a maximum value of 60 degrees for a. For mirror $B$ the dimensions are 4.50 in . and 90 degrees, and for $C$ they are 2.60 in . and 120 degrees.

The three mirrors having equal plane areas give equal maximum intensities, but they approach the maximum in three different manners, and arrive at the maximum at two
along the axis. The filament was a short helix, and in Fig. 21 the turns of wire may be counted and the hole through the helix appears as a black spot in the center of the mirror. 'This inactive area introduces a peculiar feature. The beam increases in strength until at 31 ft , the maximum is reached when the active region reaches the edge of the mirror. At greater distances the inactive center increases and therefore there is no inverse-square region. The dark center does not increase indefinitely but comes to a maximum area as outlined by the diagonals through the hole in the helix. There is thus a rise of intensity to the $L_{0}$ point, then


Figs. 19, 20 and 21. Eighteen-inch Searchlight Mirror Images of Spiral Filament seen from distances of $9.6,13.4$, and 32 feet respectively along the axis
different distances. Equation (44) may be written

$$
\begin{equation*}
L_{0}=\frac{y^{2}}{12 r \sin a} \text { feet } \tag{48}
\end{equation*}
$$

In case the radius $y$ of the mirror is constant and the angle $a$ varies, the lowest value of $L_{0}$ occurs when $\sin a$ is a maximum, that is, at $a=90$ degrees; and for angles equally above and below 90 degrees; for example 60 and 120 degrees, the values of $L_{0}$ are the same.

Equation (44) shows that if the angle $a$ is constant the value of $L_{0}$ varies as the square of the focal length. The focal length of one series of standardized mirrors varies from 7 to 25 in .; and this series alone calls for a variation of 13 to 1 in the testing range, so that this matter of minimum range for full central beam intensity is of considerable importance.

In Figs. 19 to 21 the growth of the active area of a mirror is shown for three points
a slight decrease to a practically constant intensity at a distance several times $L_{0}$. If the diagonals through the helix strike the mirror at radius $y_{1}$, then the limiting central intensity becomes

$$
\begin{equation*}
I=\pi B m\left(y^{2}-y_{1}^{2}\right) \text { candles } \tag{49}
\end{equation*}
$$

## The Inverse-square Region

Let us designate as $L_{0}$ the point on the axis where the beam reaches full intensity. This $L_{0}$ point is of importance because it is one of the limits of a region in the beam where the illumination can be computed by applying the law of inverse squares. The candle intensity within this region is constant and the illumination varies inversely as the square of the distance back to the mirror. It has happened several times to the writer's knowledge that some one has discovered this inverse-square region, or region where the entire mirror is active, and has then been deceived into taking the $L_{0}$ point as the rirtual
origin of light. In Fig. 22 the limiting rays from the center and edges of three 1 S -in mirrors having focii of $7.79,4.50$, and 2.60 in are drawn to show the outline of the entire beam and the outline of the inverse-square region, which is shown shaded. Between the edges of the beam and the edges of the inverse-square region the inversesquare law never holds exactly, but at sufficient distance the disagrecment is small. Mention will be made of this feature later.

## Testing Distance for Central Intensity

When a projector is to be tested for beam intensity there are several preliminary matters to be settled before the test can proceed. Thus, the distance must be sufficient for the beam to come into approximately final form. This is essential for if the examination is not made at the proper distance, the distribution of intensity will depend upon the distance and the addition of this factor will add to the difficulties, which are always numerous enough under the best conditions, and make even a simple comparison of projectors a very uncertain matter. On the other hand, even if space limitations will permit it is not always wise to go to extreme distances on account of the absorption and scattering of light by the atmosphere.

The relations between the minimum distance at which a beam develops full intensity and the dimensions of the mirror and light source were given in equations (44), (45) and (48) in a form that contained the radius $r$ of the source. The angular width of the beam is usually easy to determine in a finished unit, whereas the average effective radius $r$ of a filament is difficult to measure, and it is therefore a great convenience to be able to find the value of $L_{0}$ from the beam width rather than from the filament.

Calling the total angular width of the beam $C$ degrees. we have

$$
\begin{equation*}
L_{0}=\frac{458 \sin a}{C(1+\cos a)^{2}} F \tag{.50}
\end{equation*}
$$

which is plotted in Fig. 23 for rarious beam widths between 10 and 70 deg., and in Fig. 24 for mirror angles up to 140 deg . These values are of course the least distance that can be used,
and where circumstances allow shomld always be exceeded by about in per eent.


Fig. 22. Region of Inverse Squares in Beams of Light Projected by Parabolic Mirrors from Spherical Sources. The shaded section shows the inversesquare region (which has its zero point of linear measurement at the searchlight) within which the illumination follows the law of inverse squares


Fig. 23. Minimum Testing Distance for Central Intensity of a Beam Projected by a Parabolic Mirror from a Spherical Source. Range, angle a from 10 to 70 deg.


Fig. 24. Extension of the Curves shown in Fig. 23, to cover the range of angle $a$ from 70 to 140 deg.

Width of Crest of Beam
If ath observer wallis ateross the width of a beam at some distance from a searehlight, he will olserve that as he first enters the bean only the exnter of the mirror will appear luminoms $d s$ he comes neater to the axis, the lummonts aroa will grow antil at the point where he enters the inverse-square region the entire mirror will appear luminous, and it will remain luminous until the opposite edge of the region is reached.

A plot of the apparent beam canclles along this line of traverse will show a flat crested curve, somewhat resembling a sine curve with the top flattened. The width of the flattened part is proportional to the distance

At some greater distance $L$, measured from the searehlight, the half width is

$$
\begin{equation*}
\frac{11}{2}=\left(1,-L_{-0}\right) \tan \varepsilon \tag{52}
\end{equation*}
$$

The apparent angular width here is $\varepsilon^{\prime}$, giving

$$
\tan \epsilon^{\prime}=\frac{11}{21}
$$

and the crror $E$ catused by using $e^{\prime}$ in place of $e$ is

$$
\begin{align*}
& E=\frac{e^{\prime}-e}{c}=\frac{\frac{11}{2 L}-\frac{11}{2\left(L-L_{0}\right)}}{\frac{11}{2\left(L-L_{0}\right)}}  \tag{.54}\\
& E=\frac{L}{L}
\end{align*}
$$



Figs. 25, 26 and 27. Eighteen-inch Searchlight Mirror Images of Spiral Filament seen from a radius of 145 ft . at points 1 deg. 30 min , 0 deg. 45 min ., and 0 deg .0 min . respectively from the axis
from the beginning of the inverse-square region, as in Fig. 22, but the curve will necessarily be plotted in degrees measured about the searchlight. It is evident that here is a discrepancy that may be diminished but never wholly overcome. The problem is to find what the practical aspect of this difference is, for while at a great distance the angular width would be sensibly equal for either the searchlight or the $L_{0}$ point as a center, the conditions of test and service place a limit on the range of the traverse.

Let the radius of the light source subtend an angle $\varepsilon$ from the edge of the mirror, then the beam from this point, which fixes the boundaries of the inverse-square region, has a divergence $c$ either way from the axis, and we can write

$$
\begin{equation*}
L_{0}=y \cot e \tag{51}
\end{equation*}
$$

for the point where the inverse-square region has zero width.
where $\tan e$ and $\tan e^{\prime}$ have been replaced by the angles $e^{\prime}$ and $e$. If $e^{\prime}$ is to be correct to within 10 per cent then $L$ must be 10 times $L_{0}$; while if $L$ is to be correct to within 1 per cent then $L$ must be 100 times $L_{0}$. This indicates extreme testing ranges; and the tests cannot well be replaced by computations for a complete geometrical analysis is beset with many difficulties, chiefly because solid geometry and solutions by trial and error are necessary. A better and far simpler method will be given when the graphical solution for beam intensity is outlined.

Figs. 25, 26 and 27 show how the active area grows as the beam is entered from the side. The irregular form of the active area, although due in part to optical errors in the mirror, is a clear warning of the difficulty of a strict analysis for intensity in the sides of the beam.

# Full and Semi-automatic Versus Manually Operated Substations for Electric Railways 

By Cassics M. Dayis<br>Rahlway Engineering Department, General Electric Company


#### Abstract

The author compares the relative merits of automatic, semi-automatic and manually operated sulstatuons. He first deals with interurban systems and then with city systems. In each case he considers the pros and cons for these systems of substation operation in considerable detail. This paper was read before the midwinter convention of the Central Electric Railway Association held at Louisville, Ky., on January 18, 1923 . Eintor.


## Introduction

Automatic and semi-automatic substations were introduced primarily as a means of conserving labor. On interurban roads in particular the expense for labor is a large part of the total annual cost of supplying power to the trolley; therefore, anything which will lower this expense is worthy of consideration. That automatic substations have lived up to expectations in this respect cannot be denied and they have given a good account of themselves from an operating point of view.

After the first few equipments were tried out and their success seemed assured, several engineers started a careful study of their application to specific railways. It was soon shown the automatic and the semi-automatic substation offered a new economic means of effecting many improvements in operation in addition to the reduction in labor expense. Schedule speeds might be increased at a minimum expense, improvement in distribution and conversion economics made possible, while additional capacity for new load centers could be provided in a most economical manner, etc.

The many advantages possessed by automatic control become evident when certain fundamental engineering and economic principles are borne in mind. It will be the purpose of this paper to present briefly some of these principles, none of which are new, and to suggest their application in making a comparison between manual and automatic control.

It will be appreciated at the outset that there are several important differences between interurban and city systems. These differences come about primarily because the interurban railway represents essentially a lineally loaded system while the load on a city system is distributed over an extensive area. A single substation on an interurban system usually feeds only a given length of a single route while in the city one substation may feed portions of several routes and the length of feed is indefinite.

It will be well, therefore, to consider the two classes of systems separately, and since the interurban railway represents the simplest problem, this will be considered first.

## Interurban Systems

On the average interurban railway the cost of the labor conserved by the use of automatic control is considerably in excess of the fixed charges on the additional equipment. This applies to both single and two unit substations, although, of course, to a lesser extent in the case of two units. Automatic control for a single unit substation yields a gross return of from 25 to 40 per cent on the investment.

Since the total annual substation operating expense is less for the automatic than for the manual substation, it is possible to strike a new balance between the substation spacing and the amount of feeder conductor. It may be found that a substantial saving in feeder copper can be realized.

This same principle applies in another form to the case where it is necessary to improve the roltage conditions on the trolley. A balance can be struck between the fixed charges on the necessary additional copper and the annual operating expenses of additional automatic substations to accomplish the same result. The result is frequently greatly in favor of the substations. For example, as against $\$ 650,000 \mathrm{in}$ feeders the desired end is obtained on the North Shore Line by the use of automatic substations for about one-quarter this amount. The fixed charges on the substations would come to only about one-third those on the feeder copper.

If estimates indicate automatic substations are more economical than additional fceder copper to accomplish a desired result, then, as an incidental adrantage, the track drop will be reduced and the distribution efficiency increased. Due to the fact that the negative return circuit is usually of considerably greater conductivity than the positive circuit,
it is frepucmity rery expensixe to antrol the track (lop). Froppucnt spacing of athomatio substations, thorefore provickes a means ol hroaking wo this (lrop in at very effective manture. 'The bearing of this principle upon Whe mitigation of chertonlosis is oberous, although its application is of greater momortanter in city service thatron an interurban line.
'fhere are two features in the control itself which monst be borne in mind when considerinse the ecomomies of sulastation location. 'The first of these is the load limiting resistor. It perlomins a three-fold function of replacing the ordinary overload circuit breaker, limiting the output of the substation, and transferring part of the overload to adjacent substations. All these functions are of particular importanee in interurban service. An overzoalous motorman accelerating a heavy train in the vicinity of an automatic substation does not trip the substation breakers and deprive the train of all power for several scconds, but instead a block of resistance is cut in circuit and for the time being reduced voltage is obtained and acceleration continues at a lower rate. Again the bunching of trains and their simultaneous acceleration offer no difficulties in the operation of an antomatic substation. If the load on the substation becomes excessive, one or more blocks of the resistor are cut in and protect the machine. At the same time reduced voltage is available at all the trains enabling them to get under way. When such a condition occurs the adjacent substations assist in supplying. power. The amount of this supply, of course, depends upon the voltage at the load and the resistance between substations. The functioning of the equipment as just outlined actually makes each substation a reserve for its neighbors and thus becomes an important factor in selecting the size of substation equipment. There are some 500 kw . units now in operation which, if under manual control, would be entirely inadequate and would have to be replaced by 750 or 1000 kw . units.

The second feature of the control itself which has a direct bearing upon the economics of operation is that which permits the converting equipment to shut down during periods of light or no load. It is possible to adjust the control so that a given substation is in operation only when a substantial load can be carried. The load factor and conversion efficiency are not only improved but the running-light losses, which amount to from 3 to $\bar{i}$ per cent of the machine capacity, are climinated.

The elimination of labor has a decided effect 11 pon the (lesign of substation buildings. A much ehoaper, and in some cases, a smaller building can be provided. Windows can be practically done away with, space and comveniences for operators maty be absent, and no provision for heating is necessary. In fact the building may be of the simplest and most compact type.

The above statements eover the chief principles encountered in the consideration of automatic versus manual substations. There are various advantages arising from the use of automatic control which may be of more or less value to the operating company depending upon circumstances. It is not proposed to go into these here, however, beyond mentioning that certain modifications of control are possible and that certain portions of the equipment are available to accomplish certain results. For example, the load limiting resistors or reclosing control for feeders may be applied to existing manual substations to advantage. Or, instead of designing a substation to start and stop upon load demand, it may be arranged for time switch or remote control. In other words semi-automatic control may be employed to advantage in some cases although frequently all the possible economics available are not realized.

## City Systems

The conservation of labor by the use of automatic substation control applies in city systems as well as on the interurban line and, in general, similar principles of application are evident. There are certain factors and basic assumptions, however, which require careful consideration in order that a fair comparison with manual control may be made on a metropolitan property.

The problem frequently takes the form of a comparison of a few manual substations versus many automatics. If this is the case the city may be divided into load zones and the comparison simplified such that, in effect, one manual may be compared to three or four automatic substations.

The first basic assumption to be made is that the substation apparatus and d-c. distribution plant per se are equally reliable in operation and therefore no greater reserve equipment is required for one scheme than the other. It may be that one scheme offers certain advantages over the other during times of emergency; but if such be the case they are intangible advantages which must

## 

be capitalized according to the best judgment of the operating deparment.

Since the comparison between the two schemes is an economic one, the next basic assumption is that the same average trolley voltage must be used throughout the discussion. This is important since a change in trolley voltage not only affects the speed of the cars, and with it the platiom expense. but also the distribution losses and total power output of the substations. Furthermore, the trolley roltage assumed affects the amount of feeder conductor required and therefore the capital expense. If it is impossible to assign the same trolley voltage io both schemes then the differences resulting must be estimated and the equivalent capital expense debited to the proper scheme.

Another basic assumption is an equality in both schemes of track and negative return drop. Track drop is difficult to predetermine and also difficult to control. consequently. in practice, it is impossible to adhere to this assumption. In lieu thereof, the advantages and disadrantages of each scheme in this respect must be estimated and a value assigned.

A final basic assumption is that the load on the srstem and the area corered must be alike for both schemes. When dealing with loads expressed in amperes this assumption is intimately associated with the assumption stated above regarding trolley roltage.

The underlying principles in the application of a multiplicity of small substations is that. compared to a single large station. the amount of positive copper required is theoretically in an inverse ratio to the number of substations. This is based on the assumptions previously mentioned.

The limit toward which this principle leads is that number of substations which permits the elimination of all feeder conductor and the entire load is carried by the troller.

In the practical application of this principle it is impossible to realize the theoretical saring in positive conductor due to the many local conditions such as non-uniformity of load distribution, methods of sectionalizing the troller: the use of negative feeders to avoid unnecessary electrolysis hazards proximity of other points of power supply. insurance against interruption of service. local city ordinances building restrictions etc. This principle serves then primarily as a
enterion bey which tu judge how wedl at proposed scheme is laid wht

The next principle is that the mumber on substations in operation can be marle propurtional to the load, mamaming the converam. efficiency at a maximum.

The d-c. distribution efficiencer remain the same regardless of the number of sul, stations. This is due again to the assumption that the same average trolley potential is maintained and that the load is evenly. distributed. Actually the distribution efficiency will be slightily higher since feeders will parallel the trolley wire eren where calculation would indicate the average voltage would be maintained without supporting feeders.

The a-c. distribution system, if laid out for uniform voltage drop, would have the same efficiency regardless of the number of substations. This cannot usually be accomplished and a slightly lower efficiency results in practice which offsets the gain in efficiency mentioned in the preceding paragraph.

The peak load on a city system does not appear simultaneously at all parts of the system but only at a few relatively widely separated localities. It then gradually shifts to other parts of the city. Hence the greater the number of sources of power the shorter will be the feeds to the load peaks and consequently the more efficient will be the d-c. distribution.

Another principle is that the number of substations selected and their locations must be such as to produce the most economical operating results. An aggregate of several small substations cost more than a single substation of the same total capacity. The difference. however is offset by the smaller amount of positive and negative conductor required in the former scheme. By means of automatic control the small stations can be operated with a minimum of labor. they can also be operated with a minimum of light load losses.

A final principle concerns reserve capacity: In a single large manual substation at least one machine. equal in capacity to the largest. must be held in reserve. Thus there is always one idle unit upon which fixed charges must be carried. With a multiplicity of sma!l substations, however, each acts as a reserve for all those surrounding it. Consequently: the loss of a unit in a s nall substation is of little consequence since its load would be picked up by sereral other substations. From this it follows that the reserve in the
case of several small substations is included in the nomal capacity and is always and active reserve caming a deturn on the investment.

The comparison between manual and antomatic control for metropolitan systems is necessarily dose, the more so the denser the traftic. There are also more intangible advantages and disadvantages than are encountered in interurban systems; local
conditions and restrictions also have, at times, almost a determining influence. All these render it difficult to make specific statements which are of value in comection with city sulstations as a class. It is hoped, however, that the general discussion given above will serve to stimulate thought and action on the application of this most recent agent of substation economy.

# Atmospheric Nitrogen Fixation 

PART II

By Eric A. Lof<br>Power and Mining Engineering Department, General Electric Company

In Part I, published in our March issue, the author dealt with many of the general aspects of atmospheric nitrogen fixation and concluded with a description of the arc process. In this issue he deals with the cyanamid, cyanide, nitride, Haber and Claude processes.-Editor.

## THE CYANAMID PROCESS

The cyanamid process is based on the ability of calcium carbide to absorb free nitrogen forming a nitrogen compound known as calcium cyanamid or more generally under its commercial name of simply cyanamid.

The calcium carbide is produced in huge electric electrode furnaces in capacities up to as high as 20,000 electrical horsepower each. The furnaces are kept filled with a mixture of calcined lime and coke, and the electric current passing through the mixture between the electrodes melts the lime to a liquid which then combines with the coke in the interior of the furnace, forming calcium carbide, the reaction being as follows:

$$
\mathrm{CaO}+3 \mathrm{C}=\mathrm{CaC}+\mathrm{CO}
$$

The furnace is tapped every fifteen to twenty minutes into chill cars, the carbide when leaving the furnace having a temperature of about 4000 deg. Fahr.

A supply of pure nitrogen free from oxygen is essential with the cyanamid process. It is obtained by liquefying air under intense cooling and high pressure. Such liquid air machines work under pressures of 500 pounds per square inch, and with cooling by expansion the air is reduced to liquid form at 380 deg. Fahr. below zero. By then allowing this liquid air to warm up slightly, pure nitrogen gas boils off first, leaving the oxygen behind in the liquid. The nitrogen is then pumped to the fixation building.

After the carbide has cooled in the cars, it is crushed and powdered. It is then placed in
cylindrical perforated paper cylinders in the fixation ovens. These are then heated electrically by passing an electric current through a carbon rod which extends through the center of the charge. When the temperature reaches about 2000 deg. Fahr., the nitrogen from the liquid air plant is admitted. The carbide absorbs the nitrogen, forming a new chemical compound, calcium cyanamid. The nitrogen fixation is represented by the equation:

$$
\mathrm{CaC} \mathrm{C}_{2}+\mathrm{N}_{2}=\mathrm{CaCN}+\mathrm{C}
$$

When the absorption is complete, the charge is removed from the oven, allowed to cool, and crushed to a powder. It is then hydrated or treated with a small quantity of water to remove the last traces of carbide and to slake any free lime present. Sometimes it is also treated with a small amount of oil to prevent dusting. It is then known by the trade name "Cyanamid," and has a nitrogen content of about 19 to 21 per cent.

Cyanamid is extensively used as an ingredient in mixed fertilizers, but during the past few years it has also been used to a great extent as a source of nitrogen for making other products such as ammonia, various ammonium compounds, nitric acid, etc. The next step for either of these is the production of ammonia, which is obtained by heating cyanamid with steam under pressure in so-called autoclaves, when the nitrogen is given off as ammonia gas. This gas may be absorbed in water, producing aqua ammonia, which is used in large quantities for refrigeration and for many general chemical purposes. It may also
be used ior producing anhedrous ammonia by drying the gas and compressing it. Such ammonia is also used extensively for refrigeration purposes.

By aborbing the ammonia gas in sulphuric acid, sulphate of ammonia is formed, which is separated out by crystallization in the same manner as previously explained under the heproduct coke oren process

Similarly. by absorbing the ammonia gas in nitric acid. ammonium nitrate is formed, which is used to a large extent in high explosives. The nitric acid required for this product may also be obtained from the ammonia gas by oxidation of the ammonia in the presence of a heated catalyst, usually platinum, according to the following reaction

$$
4 \mathrm{NH}_{3}+5 \mathrm{O}_{2}=4 \mathrm{NO}+6 \mathrm{H}_{2} \mathrm{O}
$$

A mixture of about 10 volumes of ammonia gas and 90 volumes of air is passed over a spongy platinum screen of very fme mesh, heated clectrically to a dull red heat, the temperature with the gas passing over it being about 1000 deg. Fahr. The gas velocity must be very high so as to cut down the time of contact between the gas and the catalyzer to about 1,100 of a second. The efficiency of conversion is quite high, about 90 per cent. and the resulting strength of the nitric oxide gas about $\&$ to 9 per cent, as compared to 22 per cent with the arc process.

The nitric oxide after leaving the catalytic burners is thereafter treated in the same man-
ner as with the are process, that 15, it is passed through oxidation tanks. steam boilers and atuminum coolers and finally the the atorption towers. The alsorption system is. however, much smaller than with the are prowess, due to the much higher concentration of the


Fig. 7. Airplane View of the United States Nitrate Plant No. 2 at Muscle Shoals, Alabama
nitric oxicle and for the same reason the weak acid will have a strength of about 4.5 per cent instead of 30 per cent as with the are process.

There are a large number of clanamid plants throughout the world, their total annual productive capacit being possibly in the neighborhood of 1,2.50.000 tons of cyanamid, equivalent to a fixed nitrogen content of about $2.50,000$ tons. Based on a power requirement corresponding to $21 / 2$ tons of cyanamid per


Fig. 8. General Layout of the United States Nitrate Plant No. 2
clectrical horse power sear, or 2 horsepower years per ton nitrogen fixed as eyanamid, the power for this total output would be no less than onc-half million horsepower years. As compared to the are process the relative power consumption for the cyanamid process per ton fixed nitrogen is only one-sixth of what it is for the are process.

The large government nitrate plant at Muscle Shoals, Ala., built according to the cranamid process, is generally known under the name of United States Nitrate Plant No. ${ }^{2}$. and was built for the Government in 191. for the production of ammonium nitrate for military explosives, the productive capacity of the plant being 110,000 tons of this produet per year. The plant was constructed by the Air Nitrates Corporation, a subsidiary to the American Cyanamid Company, whose process was followed. Incidentally, it might be stated that the plant was completed shortly after the armistice, and onc unit (one-fifth the plant capacity) was thereafter put through a two weeks' complete test operation, which thoroughly demonstrated the technical success of the undertaking.

## THE CYANIDE PROCESS

The fixation of nitrogen in the form of alkali cyanides has not reached any commercial importance, although considerable research work has been done along these lines and a few small plants actually constructed. One of thesc plants was built by the Government during the war at Saltville, Va. Its capacity was very small, only 10 tons of sodium cyanide per day, the plans being to convert this cyanide into the highly poisonous gas, hydrocyanic acid, for the war.

The process of fixation on which the Saltville plant was based is known as the Bucher process, the reaction involved therein being as follows:

$$
\mathrm{Na}_{2} \mathrm{CO}_{3}+4 \mathrm{C}+\mathrm{N}_{2}=2 \mathrm{NaCN}+3 \mathrm{CO}
$$

The raw materials are soda-ash and coke in pulverized form to which iron, also in powdered form, is added, its action, however, being purely catalytic. This material is formed into briquettes, thoroughly dried, and then heated in retorts at a temperature around 1500 deg. Fahr., while nitrogen is passed through the mass. As high as 18 per cent of nitrogen has thus been fixed in the form of cyanide.

When sodium cyanide is once formed it can be converted into ammonia like cyanamid, and the process has the advantage that in this conversion the soda-ash can be recovered and
used over again. The iron can also be repeatedly used.
$\Lambda$ eyanide process has also quite recently been invented in Sweden. $\Lambda$ moderate size plant was built and operated for some time, but is now closed down, and the opinions of specialists seem to be divided as to the commercial success of the process.

The process is of the continuously operated type, the materials being kept in continuous circulation in such a manner that the nitrified portions are decomposed into ammonia leaving a solid residue which is returned to the nitrification building with the addition of some fresh material.

The raw material, consisting of anthracite, sodium carbonate and iron sponge, is formed into small balls in which shape they are fed into the furnaces. These are of the shaft type, the material resting on grates which are intermittently turned in order to facilitate discharging and to avoid baking. The firnaces are further of the electrode type operating on the resistance principle, the balls themselves conducting the electric current from one electrode to the other and become in this way heated to the temperature required for the reaction, which is around 1700 deg . Fahr. The nitrogen under pressure is admitted directly at the bottom of the furnace, and the gases are given off at the top. They contain principally hydrogen and carbon oxide, which is afterward used as fuel gas for the nitrogen ovens and for drying purposes, etc. The bottom of the furnace is connected to an airtight conveying system for transporting the cyanide to the ammonium-sulphate building.

A large surplus quantity of nitrogen is needed for the fixation, and a method has been worked out for its production at a very low cost. The process is chemical, the oxygen of the air being bound by an alkali iron to $\mathrm{Fe}_{2} \mathrm{O}_{3}$, setting the nitrogen free. This ferric oxide is then reduced by the above-mentioned waste gas from the furnaces and the iron used over again. In practice, air is not used in the manufacture of the nitrogen, but the waste gases from the sulphuric acid factory, as these gases contain only a few per cent of oxygen, thus materially reducing the energy required for binding the oxygen.

The cyanide from the furnaces is, as mentioned, conveyed to the ammonia department where ammonium sulphate is produced in the same manner as for cyanamid, with the exception that the sludge left in the autoclaves after proper treatment is used again as raw material for the furnace charge.

The power consumption with this process is claimed to be about $11 / 2$ horsepower years per ton nitrogen fixed as cyanide.

Sodium cranide is also made by fusing cranamid with ordinary salt in an electric furnace. This product is extensively used for case-hardening of steel, for the separation of gold from its ore and for the manufacture of hydrocyanic acid for fumigation of fruit trees. Large quantities of such cyanide is manufactured by the American Cyanamid Company at their Niagara Falls plant.

## THE NITRIDE PROCESS

The fundamental principle underlying this process is the combination of nitrogen with metals, such as aluminum, titanium, lithium, etc., to form nitrides from which ammonia can readily be obtained by decomposition.

The best-developed process of this type is the so-called Serpek process for making aluminum nitride from bauxite (aluminum oxide), coke and nitrogen according to the reaction:

$$
\mathrm{Al}_{2} \mathrm{O}_{3}+3 \mathrm{C}+\mathrm{N}_{2}=2 A \mathrm{~A} \mathrm{~N}+3 \mathrm{CO}
$$

Bauxite mixed with carbon is fed into the upper end of an inclined revolving kiln, the necessary heat for heating the mixture to the required reaction temperature of around $3 \geq 00$ deg. Fahr. being supplied by electric current. Producer gas, containing about 30 per cent $C O$ and 70 per cent $\lambda_{2}$ enters the lower end of the kiln and passes through the same in a direction opposite to that of the descending charge, and in the electrically heated zone, the nitrogen reacts with the alumina-carbon misture and forms aluminum nitride, containing about 26 per cent of fixed nitrogen. The carbon monoxide also formed by the reaction is being used for preheating the charge before it enters the kiln.

Ammonia is then formed by treating the aluminum nitride in autoclaves, this reaction being as follows:

$$
A l \mathrm{~N}+3 \mathrm{H}_{2} \mathrm{O}=\mathrm{Al}(\mathrm{OH})_{3}+\mathrm{NH}_{3}
$$

In addition to the ammonia, a very pure alumina is obtained which can be used for metallic aluminum production. The power required is approximately the same as for the cyanamid process, that is about 2 horsepower years per ton nitrogen fixed as nitride.

Like the cyanide process, the nitride process has not been of any great importance in connection with the nitrogen fixation problem. A few moderate-size plants have been built in this country and abroad, but it can hardly be said that the process has as yet been fully developed.

## THE HABER PROCESS

This process, named after its inventor, l'rof. Fritz Haber of Germany, was introduced there shortly before the war, and was one of the most important factors of insuring (iermany of an ample supply of nitrogen during the war, and this with a much lower power requirement than any of the synthetic processes jureviously described. Germany now possesses two enormous Haber plants at Oppau and at Merseburg. The former, where the verrible explosion occurred in 1921 has a protuctive capacity equivalent to 100,000 tons of fixed nitrogen per year and the Merselurg plant twice this, thus a total of 300.0000 tons nitrogen per year. Two plants, but of comparatively small capacity, have been buitt in this country. One of these was huil he the Government at Sheffield, Ala., during the war, but has never been in actual operation. except what might be termed experimental operation. The other plant was built in 1921 by the Semet-Solvay Company at Syracuse. N. Y. The process of these two plants is a modification of the German Haber process developed by the General Chemical Company, the operating pressure being only about onehalf that which is used in Germany:

The Haber process consists briefly in passing a mixture of one volume of nitrogen and three volumes of hydrogen (the constituents of ammonia) at a pressure of from 100 to 200 atmospheres over a suitable catalyzer at a temperature of some 900-1000 deg. Fahr. The nitrogen and hydrogen will then combine and form ammonia according to the reaction:

$$
\mathrm{N}_{2}+3 \mathrm{H}_{2}=2 N H_{3}
$$

A single passage of the gas misture through the catalytic chamber causes a conversion of about 6 to $S$ per cent (by volume) of the nitro-gen-hydrogen mixture to ammonia, this being recovered either by refrigeration and condensation to anhydrous ammonia or by absorption in water to aqua ammonia. which can again be converted into gaseous form by distillation. The unconverted nitrogen and hydrogen misture, still under the above pressure, is replenished with a fresh gas mixture corresponding to the separated ammonia. after which it is reheated and returned to the cata1rtic chamber, thus repeating the crele.

Besides the mechanical difficulties due to the high pressures at which the process is operated, the solution of the very complicated chemical problems which are involved has required an enormous amount of experimental and research work. It is absolutely essential


Fig. 10. Synchronous Motor-driven Air Compressors in the Liquid air Building



that the two gases, nitrogen and hedrogen be in a very pure state, as even minute quantitios of impurities such as carbon monoxide will be poisonous to the catalytic material and the two gases will refuse to combine or do so at a very reduced rate. It is this preparation and purification of the nitrogen and hydrogen and especially the latter, which comprises the chief items of cost in the Haber process.

The problem of providing a durable and suitable catalyst has also been a difficult one. The reaction when the two gases combine to form ammonia can only take place in the presence of what is known as "catalytic" metals. A catalyst, therefore, is simply a substance which promotes the union of two elements with each other, without itself entering into the combination.

Water is naturally the source from which hydrogen is produced, either chemically or by electrolysis. In the former method, water gas is first generated in a gas producer in the ordinary way by passing steam over incandescent coke. This gas consists of one-half volume of hydrogen, the other one-half being chiefly carbon monoxide, as seen from the following equation:

$$
\mathrm{C}+\mathrm{H}_{2} \mathrm{O}=\mathrm{CO}+\mathrm{H}_{2}
$$

In order to remove this carbon monoxide it is found desirable to convert it into carbon dioxide which can readily be separated by water scrubbing at a pressure of around 25-30 atmospheres. The equation for the reaction is:

$$
\mathrm{CO}+\mathrm{H}_{2}+\mathrm{H}_{2} \mathrm{O}=\mathrm{CO}_{2}+2 \mathrm{H}_{2}
$$

and it is caused by letting an additional quantity of steam react on the gas in a special converter, also with the help of a suitable catalyst. The advantage of this method is obviously that twice the amount of hydrogen is obtained with the same gas producer. The pressure is obtained with no extra cost because the gas must sooner or later, anyhow, be compressed to a still higher pressure as previously stated.

Pure hydrogen can be produced by electrolysis of water but in order that this method shall be commercially feasible, cheap power is essential.

The process used at the Government Synthetic Ammonia Plant at Sheffield, Ala., was a modified water-gas process by which the hydrogen and the nitrogen is produced simultaneously. It is thus possible to directly provide a mixture in the right proportions, if instead of steam, a mixture of air and steam is passed over the incandescent coke in the gas
producer; or in other worls, if instead of water gas, a semi-water gas is produced consisting of five volumes of hydrogen, seven volumes of carbon monoxide, and four volumes of nitrogen. After the seven volumes of carlon monoxide have been converted into seven volumes of carbon dioxide and hydrogen, in the manner previously explained, and the gas freed from carbon dioxide, then it contains evidently twelve volumes of hydrogen and four volumes of nitrogen. or hydrogen and mitrogen in the correct proporions, $3: 1$, for ammonia. The following equations will possibly make this clearer:

$$
\begin{gathered}
\overbrace{5 \mathrm{H}_{2} \mathrm{O}}^{\text {Steam }}+7 \mathrm{C}+\overbrace{4 \mathrm{~N}_{2}+\mathrm{O}_{2}}^{\text {Air }}=5 \mathrm{H}_{2}+7 \mathrm{CO}+4 \mathrm{~N}_{2} \\
7 \mathrm{CO}+7 \mathrm{H}_{2} \mathrm{O}=7 \mathrm{CO}_{2}+7 \mathrm{H}_{2}
\end{gathered}
$$

Adding the hydrogen and nitrogen values from the right-hand side of these two equations we thus get

$$
5 H_{2}+7 H_{2}+4 N_{2}=12 H_{2}+4 N_{2}=8 N H_{3}
$$

In the German Haber plants the hydrogen is produced by the water-gas method and the nitrogen by separate lean-gas producers. Some free nitrogen is also required around the plant for various purposes, especially for adjusting the hydrogen-nitrogen mixture before it enters the synthetic reaction chamber. This nitrogen is made by the liquid-air distillation method. This process could, of course, be used for manufacturing all the nitrogen required but it is a question whether it will be economical unless cheap power can be obtained for driving the refrigerating compressors.

The gases after leaving the respective producers are first thoroughly washed by water separately. The main purification, however, is done after the gases have been mixed, and consists in first washing the gas with water under a pressure of around 25 atmospheres for removing the bulk of the carbon dioxide. After this the gas is brought up to the final process pressure of $100-200$ atmospheres and washed with chemical solutions for removing the final traces of CO and $\mathrm{CO}_{2}$ after which it is passed through the catalytic ammonia reaction chamber. In the Sheffield Plant the gas mixture is brought up to its final pressure of 100 atmospheres in one step and the water scrubbing for removing the carbon dioxide is done at this pressure.

The gases which have been converted to ammonia in the catalytic chamber are removed by means of refrigeration or water absorption and the uncombined gases returned

 "Tow ammonia may be sold as anhydrous or atpua or absorled ins sulphatic acid or phosphorice acid to protuce ammonitum sulphate or ammonimm phosphate the same as with the otler processes, or a portion may be oxidi\%ed and absofferl to form nitric acid in which the remaining portion of the ammonia may be absorferl 10 losm ammoniam nitrate.

In proxlacing hodrogen for synthetic ammomia be the water-gas methorl, it has been shown how large quantities of earbon dioxide have to be climinated in the purification. As in the solvay soda process thousands of tons of carbon dioxide are used each year for which larere quantities of limestone are burned, it follows at once that the two processes can adtantageously be worked together.

The ammonia gas and the carbon dioxide is passed into a brine solution and the products obtained are sodium bicarbonate and ammonium chloride.

$$
\mathrm{NaCl}+\mathrm{H}_{2} \mathrm{O}+\mathrm{CO}_{2}+\mathrm{NH}_{3}=\mathrm{NaHCO}+\mathrm{NH}_{4} \mathrm{Cl}
$$

The solium bicarbonate, $\mathrm{NaHCO} \mathrm{S}_{3}$, is rearlily converted into soda ash, $\mathrm{Na}_{2} \mathrm{CO}_{3}$, by heating when it loses all its water and part of its carbon dioxide gas.

$$
\because \mathrm{VaHCO}_{3}=\mathrm{Na}_{2} \mathrm{CO}_{3}+\mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O}
$$

Soda ash or sodium carbonate is extensively used in the glass, soap, paper, textile and mumerous other industries.

The ammonium chloride, $\mathrm{NH}_{4} \mathrm{Cl}$, after proper concentration and drying, is at once ready for the market. It is claimed, but not substantiated, that ammonium chloride, which is a more concentrated nitrogen product than the sulphate and meets the other requirements also, is equal to the sulphate in fertilizer properties, just as potassium chloride is as available for crops as potassium sulphate.

The power requirements for the Haber process are very low unless the hydrogen should be produced by electrolysis and the nitrogen by liquid-air distillation. The reason for this is, of course, the fact that electricity does not enter into any of the reactions but is chiefly used for motive power.

Where the nitrogen and hydrogen is provided by the gas producer method the power requirements will amount to about $1 / 2$ horse-
power fears per ton nitrogen fixed as ammonia, while if clectrolytic hydrogen and lifuld-air nitrogen is produced the corresponding figure would be around $31 / 2$ horsepower years.

## THE CLAUDE PROCESS

This process, the invention of M. Claude of France, is a modification of the Haber process. It is as yet more or less in the experimental stage, but seems to offer great possibilities. Clamde thus works with a pressure of 900 atmospheres as compared to 200 with the Haber process. By means of this high pressure about 40 per cent ammonia conversion is obtained per catalyzer unit, and the endothermic reaction will raise the temperature of the catalyst to the required temperature of $900-1000$ deg. Fahr. with only a slight preheating, which is readily provided by simply passing the gas through an outer passage in the catalytic chamber. By using three catalyzer units in series, 80 per cent of the gases are converted into ammonia and only 20 per cent needs to be recirculated. The ammonia is readily removed by simply cooling it in a coil submerged in water when practically all the ammonia will liquefy.

The hydrogen and nitrogen may be obtained in the same manner as with the Haber process previously described. It is claimed, however, that the hydrogen from producer gas can be very efficiently purified at this super pressure. The compressed gas is passed through ether at a low temperature when all the gases but the hydrogen are dissolved by the ether. The solvent with the gases in solution is drained off, and when expanding to atmospheric pressure the dissolved gases escape, leaving the solvent ready for re-use.

## THE CASALE PROCESS

This is also a synthetic ammonia process which has been developed in Italy where it is said to be used in one or two plants. It operates at a pressure around 500 atmospheres, or somewhat higher than the Haber process, for which reason a higher ammonia conversion should be expected. It is also claimed that a very satisfactory catalyzer has been found which is less affected by impurities in the hydrogen and nitrogen gases.


## LIBRARY SECTION

Condensed references to some of the more important articles in the technical press，as selected by the G－E Main Library，will be listed in this section each month．New books of interest to the industry will also be listed．In special cases，where copy of an article is wanted，which cannot be obtained through regular channels or local librarics，we will suggest other sources on application．

## Circuit Breakers－Testing

Arrangement for Testing and Adjusting Excess－ Current Relays of Automatio High－ Tension Circuit Breakers．Delenk，A． （In German．）
Siemens－Z．it．，1）ec．，1922；v．2，pp．666－668．
（Brief description of apparatus and methorls．） Condensers，Static

Static Condensers for Power－Factor Correction． Marbury，R．E．
Elec．Jour．，Feb．，1923；ソ．20，1p．49－．51．

## Electric Cables

Apparent Lielectric Strength of Cables，Wise－ man，Robert J
A．I．E．E．Jour．，Fcb．，1923；5．42，pp．16．）－170． （A discussion of two earlier papers by Middle－ ton，Dawes and Daris，and by Simons on the same subject．）

## Electric Conductors

Wind Shielding between Conductors of Telegraph and Telephone Lines．Howe，P．J
A．I．F．E．Jour．，Jan．，1923；v．t2，pp．20－26． Results of an investigation of the effect of wind on telegraph and telephone lines， especially when thes are ice－coated．）

## Electric Control Systems

A－C．Locomotive Control．Dory，Dr．Iran．
Elec．Raiy．Jour．，Feb．3．1923：v．61，pp．199－ 200.

Review of plans used for varying voltage in European single－phase locomotives．）

## Electric Drive－Steel Mills

Improving Rolling Mill Practice．Stoltz，G．E． Iron Age，Feb．8．1923；v．111，pp．411－414．
（Abstract of paper before the Association of Iron \＆Steel Electrical Enginecrs． Discusses use of d－c．for main roll drives．
Electric Furnaces
Electrically Heated Industrial Furnaces．Trinks， IV．
Forg． 8 Heat Treat．，Dec．，1922；v．8，pp．538－ $5+2$.
（Compares efficiency of electrically heated and combustion types．Shows designs of heating elements and furnace construc－ tion．）

## Electric Lighting

Infuence of Daylight Illumination Intensity on Electric Current Used for Lighting Purposes in the District of Columbia． Smirnoff，A．
Illum．Engng．Soc．Trans．，Jan．，1923；v．18， pp．36－4b．
（Tests of the outdoor＂psychological dark－ ness＂which results in electric light being employed in the business district．）

Electric Locomotives
Unicpue Type of Drive for Electric Lonemmosives
 （Illustrated description of the Brown 13nveri ＂individual axle drive＂locomotive used on the Swiss Federal Railways．！

Electric Motors，A－C．
Tariable－Speed Alternating－current Monors with－ out Commutators．Creedy，$F$ ．
Engng．，Jan．19，192：3；․ 11．5，pp．si－91
（Paper before the I．E．E．Serial．same， abstract，in Engineer，January 12．1403， pp．49－50．
Electric Motors，Synchronous
Synchronization of Synchronous Notors on Load．Fraenckel．A．
Brown Boacti Rea＇，Dec．，1920；1．9．［19．こt3－ 2.54.
（Describes the theory of BBC equipment for synchronization．）
Electric Transformers
New Type of Transformer．Designed to Conserve the Oil and Eliminate Explosions．Dann， Walter M．
Elec．Jour．Feb．，1923：r．20，pp，is－．5th
（Description of the Westinghouse＂Incr－ taire＂transformer in which mitrogen occupies the space above the willevel．
Electric Transmission Lines
Cost of Transmission Lines．
Elec．Whld．，Feb．3．1923；v．ה1，11p，271－2：t．
（General and price data on a 7 －mile＂rstem
 Company．
Qualitative Analrsis of Transmission Lines． Goodwin．Jr．，H．

（Method of caleulating transmission lines．
Radiation from Transmission Lines．Nanneback， Charles．
A．I．E．E．Jour．，Feb．．192：3；ィ． 42 pp．（15－10．
（Theoretical study．
Structural Engineering Problems in Transmis－ sion－Line Construction．Nartin，James S．
Engrs．Soc．of 11．Pa．Proc．，Nov．．1922： 1. $38, \mathrm{pp} .309-420$.
（Extensive paper on design of tran mission lines．

Electrical Machinery－Testing
Back－to－Back Tests of Continuous－cursen：Ma－ chines．Smith．C．F
Elec．Rei．（Lond．，Jan．26．1：223：v．12 pp）． $12+126$ ．
Outlines methods of such tests．whin are also called Hopkinson tests．

## Hydroclectric Plants

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Inductive Interference

 Lines．N：ather，Vagen．（ln Corman．）
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（Theroretical（hiseussion．）
Insulators
Reliability and Cost of Conteratry Insulators． Alistin，Arthur（）．
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（Abstract of paper before the $\therefore$ ．Y．Vileceric Railway Association．
Machinery Foundations
Design of Structural Supports for＇Turbo－Gen－ erators．

Ľing Shims Instearl of Wedges for leeveling Bases of Steam Turbines．Barker，Sr．， Edgar C．
Poaer，Jan．（1，1923：v．3̄，pp．is－60．
（Practical methods of turbine erection．）

## Oscillographs

Expansion of（）scillography by the Portable Instrument．I．egg，J．W．
．I．I．E．E．Jour．，Fels．，1923：v．\＆゙，1p1．106－111． （［llustrated description of a portable oscillo－ graph．）
Photometers and Photometry
Direct Reading and Computing Attachment for Sphere Photometers．W＇illis，Ben．S．
Illum，Engng．Soc．Trans．，Jan．，1923；v．18， pp．62－66．
Poles，Wooden
Design of Jlooden Pole Transmission Line． Crawford，Perry 0.
Elec．IVld．，Jan．20．1923；v．81．pp．151－155．
（Results of tests of wood poles．）

## Power－Factor

Power－Factor as It Affects the Consumer． Murphy．L．J．
Elec．Jld．，Jan．13，192＇3；v．S1，pp．97－100．
Railroads－Electrification
Twelve Years＇Experience with Alternating－ current Traction．
Räy．1ge，Feb．10．11923；v，74．pp．381－3Sン．
（Abstract of paper by H．W．H．Richards before the Institution of Civil Engineers． It tells of results obtained with single－ phase operation on an English line．
What Railroads Are Doing with Electric Traction． Ochler，A．G．
Ray．Age，Jan．6．I！23：v．T4．pp．4．5－48．
Summary of recent operating experiences on tmerican and on foreign lines．

## Resistors

Appliettion of Comtol Kesistors．James，11．D． Fifer．Jour．，F（f）．，1！2：3；v，20，pp．57－1；2．

## Steam Turbines

U＇s！of the Blereder Turlsine in［ndustrial Plants． Noore，J． 1.
Poover Pl．Eingng．，Jan．lō，loeg；v．27，pp． $1215-128$.
fShort article showing how the bleeder turbines may be used to advantage．）
Strength of Materials
Siresses in Blectric－ratilway Motor Pinions． Hevomans，Paul and Kimball，Jr．，A．I．
 （Jetermination of their distribution by the photo－clastic methed．）
Substations，Automatic
Automatic s゙ubstations Sucess in St．Paul．Rein－ bold，Robort．
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（lilustrated account of equipment and ex－ periences of the St．Panl Gas Light Com－ pany．）
Towers，Steel
Design of Radio Towers and Masts：Wind－ Pressure Assumptions．EIwell，C．F． Flec＇n，Jan．2t，1923；v．90．pp．88－89．
（ Whstract of paper before the I．E．E．）

## NEW BOOKS

Amcrican Machinist Gear Book．Ed．3．Logue， Charles H．Revised by Reginald Trautschold． $35: 3$ pp．，1922．N．Y．．McGraw－Hil！Book Co．，Inc．
The Dynamo；Its Theory，Design and Manufacture． Ed．6．Vol．1．Hawkins，C．C． 615 pp．，1922， N．Y．，Sir Isaac Pitman \＆Sons．
Elementary Internal－Combustion Engines．Ed． 2. Kershaw，J．W． 211 pp．，1！22，N．Y．，Longmans， Green \＆Co．
Experimental Electrical Engineering and Manual for Electrical Testing．Ed．3．Vol．I．Kara－ petoff，Vladimir． 795 pp．， $1922, ~ N . ~ Y ., ~ J o h n ~$ Wiley \＆Sons．
Incandescent Lighting．Levy，S．I． 129 pp．，1922， N．I．．Sir Isaac Pitman \＆Sons．
Internal－Combustion Engines．Okill，J． 126 pp．．192．2，N．Y．，Sir Isaac Pitman \＆Sons．
Machinery Foundations and Erection．Croft， Terrell． 691 pp．，1923．ス．Y．，McGraw－Hill Book Co．，Inc．
Mechanical Engineering Detail Tables．Ross， John P．197 pp．，1923．N．Y．．Sir Isaac Pitman \＆Sons．
Modern Radio Operation．Smith，J．O． 138 pp．， 192．2，N．Y．，Wireless Press．
Oil Power．North．Sidney H．122 pp．，1922，N．Y．， Sir Isaac Pitman \＆Sons．
Technische Schwingungslehre．Ed．2．Hort， Wilhelm．$\underset{\sim}{2}$ Pp．，1922，Berlin，Julius Springer．

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## SIR JOSEPH JOHN THOMSON VISITS SCHENECTADY

The Research Laboratory and the Schenectady Works were honored on April 6th by the visit of Sir J. J. Thomson, for many years Cavendish Professor at Cambridge and now Master of historic Trinity College. We have entertained many distinguished visitors; including Lord Kelvin, Senator Marconi and Thomas A. Edison, but none more distinguished than "J. J.," as he is lovingly called by the workers in the great laboratory which he directed for so many years with such wonderful skill and inspiration.

Our visitor studied with interest and delight our Research Laboratory, which is largely devoted to work along lines which he himself laid down and largely guided by principles which he himself formulated. He also saw something of the great Schenectady Works, where twenty thousand men are engaged in work which has been made possible principally by his labors and those of his predecessors. Newton, Faraday, Maxwell and Thomson-these four names alone would bring glory enough to any nation. Newton was the founder of modern physics; Faraday's researches made possible the electrical transmission of energy and established the principles on which our own Edison and Elihu Thomson based their historic work; Clerk Maxrell's mathematical researches lie at the foundation of modern electrical knowledge; and I. J. Thomson has for more than a generation led in the development of the principles that these men established and in the broadening and deepening of that knowledge of basic truth which lies at the foundation of our own work and of all modern scientific and technical endeavor.

In particular, he has led us one step nearer to the ultimate-and a long step, a longer step than has been taken for a century, for it
is more than a hundred years ago that his compatriot Dalton demonstrated that matter is made up of molecules and atoms. Thomson has told us how the atom itself is constituted, has shown us that each atom contains positive and negative electricity, the negatives existing as a number of little particles of electricity called electrons. Already this new knowledge has led to practical results of enormous value, and we are very proud of the part which our own Research Laboratory is taking in this work, a part which "J.J." graciously and generously acknowledged in a most inspiring address which he made on the evening of April 7 th at a dinner given in his honor at the Nohawk Club.

It is only as the basic truths of nature are discovered that the application of those truths to the service of humanity becomes possible, and we of the General Electric Company, a concern whose prosperity and whose rery existence are based on science and on the applications of science, are in a peculiarly farorable position to appreciate and to honor the man who has done what J. J. Thomson has done, and to recognize in him not only the greatest living physicist, but a worthy representative of the highest type of those devoted scientists and research workers who have discovered the scientific truths which have made our present prosperity possible.

Albert G. Datis.

Sir Joseph's risit to America is under the auspices of the Franklin Institute. He is to give several lectures during his visit. and we hope through the courtesy of the Franklin Institute to be able to tell our readers something about these lectures in future issues of the Review:

# Electricity Masters Paper Making 

By Robiert II．Rociers




#### Abstract

Thu art of wate makmer has progressed rapidy in reoont years．Mr．Rogers deseribes the equpment 


（＇analla has the lomer of putting into prombetiom the tirst 100 ber cent electric palp and paper mill and it is abreatly tarminge ont＂news＂at the rate of three humdred tons per blay This means that the spruce and balsam from 7.5 arores of forest is spread to 1：301 aroes of mewspaper，which is enotogh for an issue of $2, f(0), 000$ sixterep－page papers．

Every mechanieal recpuirement in this eomplicated industry is met bey eleetrie motors


Fig．1．Diagrammatic Plan of the Paper Mill of the St．Maurice Lumber Co．，and of the Flow of Material from the Log Boom in the River to the Loaded Freight Cars．A cord and one－quarter of wood is converted into a ton of paper every five minutes
（ iil fact for the boilers is delivered to the 1 （0，0）（0）－barrel tanks during the summer by tamkers from down the eoatst．

The Sit．Naturice also furnishes an ideal broiler feed and a clean colorless water that is so necessitry to the production of a bright sheet of paper．Water enters into the proc－ esses in great quantities．The main pumping station at the river bank，Fig．2，has a
 enough to supply a city of $\quad$（0），0） 00 inhabitants． Within the mill there are three great circulating sys－ tems which together with the makenp and interle－ partmental flows aggre－ gate the unbelierable pumping duty of 2.500 tons per ton of paper produced．

The pumps all told have a capacity of 140,000 gal－ lons per minute or $\$ 00,000$ tons per day and every pump is a centrifugal direct connected to a General Electric motor．

Electric power is used at 2200 volts and 550 volts alternating current from the twin $24,000-\mathrm{kw}$ ．trans－ mission lines，and at vari－ ous direct－current voltages from the turbine generators whose exhaust steam is required for drying the
ranging from $1 / 8$ to $2400 \mathrm{~h} . \mathrm{p}$ ．in about 400 units．Ninety four per cent of the $34,000 \mathrm{~h} . \mathrm{p}$ ． connected load is developed by General Elec－ tric units．

The International Paper Company＇s newest mill is at Three Rivers where the St．Maurice river joins the St．Lawrence midway between Montreal and Quebec．Array upstream a timber tract the size of Massachusetts insures them many years supply of logs that can be floated to the mill．From Shawinigan Falls，in the same river，comes the hydro－ electric energy that drives the mill．
paper．The balanced requirements of direct current for adjustable speed work and exhaust steam for drying makes a very fitting arrange－ ment．

There are 522 employees including all supervision and，as the mill is operated by three＂shifts，＂one is impressed more by the absence of employees than by their presence．

One ton of newspaper is represented by one and one－half of the familiar 6 －foot rolls and will print eight thousand 16 －page papers． As being manufactured in this mill，using all
the figures wer a period of ond momth. it

(a) One and one cighth cords of wook
(b) Three and one eight harrels of fued oil.
(c) Seven tons of stean.
(d) Fifteen man-hours of labor.
(c) $1: 3,40$ kw-hr. of hedro-electric emerg?
(f) Five minntes for production.

Reference to Fig. 1, the diagrammatic plan of the mill. will show that the logs are withdrawn from the river. sawed. barked and the excess oxer the daily requirement for the mill is stored in huge piles be stackers during the summer months. The logs are reclamed and passed throngh two independent processes. the sulphite or chemical process and the ground-woot or mechanical process. Twentr-five per cent of the pulp) as it gocs to the paper machine has come from the sulphite process and the remainder is gromat-wont pulp. The diagram shows the connected motor load in each department, the incoming transmission lines and transformer houses, the arrangement of fuel tanks and main boiler house and the railroad connections.

The fall freezeup must find upwarls of 60.000 cords of wood on hand to carry orer the winter production. The cleaner logs are diverted to the sulphite system first going through the chippers which reduce them to small chips which are stored in an elevated chip bin. Bisulphite of lime, prepared in the plant by burning sulphur and passing the resulting gas through towers filled with
limestome and driphing wath of tand chene at hand for thice in the dige ler The huse vertical digesters covery dight lant tak


Fig. 2. General View in Pump and Filter House where there is a Connected Load of 1862 h.p. in Direct-connected Pumps Having a Combined Capacity of 55,800 gal. per min. or Enough to Supply a City of 700,000 People. The weight of all the rotating parts and any unbalanced water thrust in the vertical units is carried on the suspension thrust bearings at the tops of the motors. The pumps are below the low-water level and the control units in the gallery are above the high-water level of the St. Maurice River


Fig. 3. Diagram Showing the Water Content on a 24 -hour Basis Throughout the Various Processes. The ground-wood mill, the sulphite mill, and the machine room each have a circulating system, which, taken together with the make-up and interdepartmental pumping, makes the pumping duty 2500 tons per ton of paper produced. The combined capacity of all the pumps in the mill is 800,000 tons per day

20 cords of chips, about 2.5000 gallons of bisulphite of lime and live steam up to 70 lb . pressure. About 2.50 boiler-horse-power-hours are required per ton of air dry pulp. The process of selective digestion lasts about eight hours and is for the specific purpose of digesting the ligneous and resinous binders without harming the cellulose ( $C_{9} H_{10} O_{5}$ ) fibers that go into the paper. At the end of the "cook," the contents of the digester are blown into a covered concrete "blow pit" which has a perforated bottom through which the waste liquor drains off to the sewer. The steam and gas fumes pass off through high baffled towers called romit stacks which are designed to prevent the escape of pulp. The pulp is now thoroughly washed in

まった Naッ，1！！：

Fig．5．This Lineup of Seven 2400 －h．p．，Synchronous Motors Drive the Grinders which
Daily Reduce to Pulp 250 Cords of four－foot Wood．In their week＇s run the would
drive seven 10,000 －ton cargo ships from New York to the Panama Canal

Fig．7．Six 25－h．p．Wound－rotor Motors Drive 30 Deckers or Pulp Thickeners which
Remove Nine－tenths of the Water from the Pulp．This water is returned to the grind－

Fig．4．One of the Three Stackers and Less than Half of the 22，000－cord Pile that it had Accumulated During the Summer Season．Portable conveyors are sulphite depart－ to the permanent conveyors which connect to dislodge the logs in winter

the blow pits for several hours until practically nothing remains but the silky unbroken fibers of cellulose.

When the stock leaves the digesters it is 92 per cent water and becomes 99 per cent water while being washed in the blow pits. It now goes to a 35,000 gallon stock tank which stores up enough to convert the intermittent discharges from the digesters into a continuous process beyond the tank. Horizontal shaft agitators in this tank keep the contents from settling.

From the tank a steady flow goes through a mixing box, which by the addition of white water from an extracting process further along doubles the volume. A rotary screen of the type called a knotter extracts the coarser clots and fiber bundles and a still further refinement takes place in the improved rotary meshed drum "first" screens which pass only the individual fibers through very narrow slits. The rejected material from the knotters and first screens passes through a "second" screen which returns the valuable portion to the main stream back of the first screens and sends the coarser parts to the wrapping paper department.

The stock now cascades down five steep meshed thickeners into tanks in which revolve partly submerged screen thickener drums.* The excess water falls through the inclined screens or passes to the inside of the drums, while the pulp adhering to the outside of the drums falls over the dams and flows to the soft stock tank below. The thickeners reduce the water flow from 2900 to about 400 gallons per minute which leaves the stock about the consistency of thin porridge. The extracted white water goes to a tank to be worked back into the system in various ways. The screens and thickeners are belt group driven with other miscellaneous machinery.

A sulphite soft stock tank, with a capacity of 45,000 gallons. is equipped with a horizontal shaft agitator to prevent separation. A small addition to this stock comes from two inclined "save alls" which give the white water tank overflow a last screening before it goes to the sewer. Leaving the sulphite pulp at the soft stock tank we will follow the preparation of the ground wood to a similar point.

Interest in the ground-rood department centers about the grinders, for here is the heaviest draft on electric power and the greatest material transformation, all carried on with relentless energy and yet with just

[^20]that skill and delicacy that produces unvaryingly the balance betwern quality and quantity which goes so far to uphold the mill's production record.

Seven General Electric 2400-h.p., 2200 -volt synchronous motors backed by their switehboards, oil switeh cells, starting compensators and exciter motor-generator sets, form the most imposing array of power in the mill.

These synchronous motors, aside from their remarkably high efficiency of 96.2 per cent at full and 90 per cent at three-fourths load, are designed to allow for a strong leading power-factor even at fractional loarls. As their load far outweighs all the induction motors combined, the power-factor for the mill is exceptionally high and is under perfect control.

Wood grinding furnishes an ideal load for synchronous motors as the grinders have light starting load when the pressure is relieved; they have a constant load characteristic regulated by an automatic device and the total load is so great that the power-factor for the whole plant is kept.at unity. It is of interest to note that the induction motor load alone has a power-factor of 72 per cent.

These synchronous motors are started by reduced voltage tap compensators and the power-factor is controlled on the individual motors by their field rheostats. The motors are designed for 72 per cent leading powerfactor at full load.

Each 2400-h.p. motor is direct connected to the end of a shaft that carries two $60-\mathrm{inch}$ diameter by 5 -inch face grindstones thus making twelve stones in all. The seventh set, which will make fourteen stones, is being installed.

The grinders are of the Watrous magazine type, i.e., the wood is fed into vertical chambers that reach to the charging floor where they are kept filled from wood bins that are in turn kept replenished by the conveyor system. The four-foot logs are laid in the magazine parallel to the shaft, making two compact stacks per stone in the magazines with the stone between them at the bottom. The logs that lie alongside the stone on either side are forced against the stone by hydratulic pistons until they are ground away. When the pistons have completed their strokes, they automatically withdraw, allowing more logs to fall into the vacant spaces. when the relentless forward travel of the pistons begins again. The withdrawal of the pistons is accomplished by the low pressure $5(0-1 b$. water system, while the grinding pressure is applied
hy the loto-lh, watter pressure wing, howeror, omly about lion lh, in service
lithout water the wexel wothld burn and the stomes would larst from heat, therefore some beoforaloms per minate of white water is flushod oner tue twolve stones, serving to bring the gronud wood away as pulp which is over ! 9 per cent water. Even so the heat gencrateal coolves a great amonnt of steam. This, howerer, is ejected by an ingenious system which leaves the department unusually dear. Projecting through the side of each magazine is a toothed wheel which is turned as the wood sinks toward the stone, its purpose being to register the cords of wood ground.
the line. Sill more white water is added to the knotter mixing box before the stock goes to the four Improved Sherbrooks rotary sereen knotters. Fiber bundles and other over-large mits are washerl off the upper inside surface of the droms and pass to the wrapper machine system as was the case in the sulphite department.

The stock now flows into long rifflers which are fitted with submerged baffles to arrest sand from the stones and other heavy impurities. Four improved rotary first screens further refine the stock while they discharge undesirables to the second screens for a rescreening. Throughout the process


Fig. 8. Two of the Four 164 -in. Bagley and Sewell Paper Machines make Paper at the Rate of 800 ft . per min. with an Ultimate Speed of 1200 Ft . per Min. Two more similar units are in the next room on the right. The "stuff" is poured on at the extreme foreground and 45 seconds later is reeled up as specification paper at the far end of the room. There is 600 linear feet of paper in process on each machine

Provision is made for burring the stones at regular intervals by means of a built-in hydraulic burring lathe, without interfering with production, and a light burring at three hour intervals is said to give very uniform results. Each stone, consuming about $900 \mathrm{~h} . \mathrm{p}$., grinds 17 tons of air dry pulp per 24 -hour day and the pulp is of such high quality that refining processes usually resorted to are omitted in this mill.

The pulp after leaving the grinders passes through inclined sliver screens having a large area, leaving the slivers on the surface from which they are raked by chain operated scrapers. The coarse residue is burned along with the bark and sawdust.

A tank holding 96,000 gallons receives the raw stock together with the return of useful stock from the second screens further down
so far the water content has varied from 991 to $991 / 2$ per cent as influenced by the addition of white water and extraction to the second screens.

A battery of thirty deckers thickens the stock by removing all but about one-tenth of the water. This is done by rotating meshed drums partly submerged in the stock. The water runs into the drum and aray to the ground-wood white water tank, while the pulp left on the surface is scraped off and passes to the concrete cave-like ground-wood soft stock tank which holds $\$ 90,000$ gallons, equal to 160 tons of stock if it were air dry. A steel tank outside is nearly ready to take 750,000 gallons of stock as an additional reserve. The ground-wood pulp is now advanced to the same relative point as the sulphite pulp.

A stream of pulp from each of the soft stock tanks is automatically regulated to a consistoney of $9 \operatorname{lit}_{2}$ per cent water and brought to the mixing system where they are automatically resulated to mix in the desired ratio. Into the resulting flow is fed a thread of bluing to neutralize the natural yollow color of the pulp, and a trickle of alum water is added for a size. It is now pumped to the machine roon and through the final sereens thence to the mixing boxes where it is literally drowned in a flow of white water which amounts to 60,000 tons per day.

The introduction of this quantity of water which forms the major circulating system of the mill reduces the "stuff" to a consistency of two cups of dry pulp to the barrel, and this dilution is necessary to secure an even felting of the fibers in the early stages of the sheet formation.

It is the function of the four paper machines to form the sheets and remove this water shelter

Fig. 10. View of One of the Paper Machines from the Dry End, Showing Several of the d-c. Units and their Accompanying a-c. Speed Control Units. The paper machine can be operated from 500 to 1200 ft . per min without losing the precise speed relationship between the nine sections

down to a 10 per cemt monsture erontan The four paper machines are cach abomy 350) feet long abd they turas ont oso mates of paper a day as wide as at state reat and at the rate of ba miles per homer.

Fig. 9. The 100 -h.p. Squirrel-cage Motor Which Circulates 35.000 Tons of White Water
per Day from the Pulp Thickeners Back Over the Grindstones. Being located in a
Fig. 9. The 100 -h.p. Squirrel-cage Motor Which Circulates 35.000 Tons of White Water
per Day from the Pulp Thickeners Back Over the Grindstones. Being located in a pit below the ground-wood mill, the motor is protected by a well designed removable


Each machine consists of nine independent precision speed regulated sections driven by the well known General Electric section drive.

The first section, the Fourdrinier "wire"a fine brass wire mesh belt, receives the "stuff" in a stream 13 feet wide and "s of an inch deep. In 50 feet of travel and within three seconds, most of the water has fallen through leaving a very wet sheet of paper which is peeled off the "couch" roll at over Sol feet per minute, passing unsupported over a gap to the second section. In three seconds 200 parts of water to one of pulp has become three parts to one and the watery web is called paper for the first time.

The wonder is that mass production of uniform quality can be carried out at such high speed. for 300 miles of paper has often been run off without so much as a pin hole to mar the sheet. Three gigantic wringers with solid granite rolls and weights on compound levers squeeze the sheet in succession compacting the fibers and removing a little water. Every section must run in linear feet a little faster than its predecessor and more precisely so as the paper dries and becomes less elastic.

The next section is long and high and consists of filty 5 -foot diancter steam heated drums over and budder which the paper passes to expel by heat some 500 tons of water per day all told. The drums are all geared together and weigh nearly foo tons.

The paper comes out containing 10 per cent water- the specified content for comfortable working on the printing presses, but it has a furry surface and is too thick.

The calcinder stack, a pile of ten polished steel rolls, now takes the paper in and ont to the bottom where it emerges bright, smooth and printable.

The reel just beyond the calender rolls up the product into units weighing about $11 / 2$
afternating-eurrent motor-driven direct-current generator in the basement. The trimmings from the sheet and other "broke" resulting from various causes are put through a beater in the basement, which reduces the wet or dry broke to pulp that can be returned to the system at the machine chest.

The commercial rolls are now taken to the finishing room, where they are securely protected by heavy wrapping paper made from the rejections of the sulphite and ground-wood mill.

The General Electric sectionalized drive is operated in the following manner: In the basement below each paper machine there is installed a $500-\mathrm{kw}$. direct-current geared


Fig. 11. The Motors for Each Paper Machine are Driven by a $500-\mathrm{kw}$. Turbine Set with Speed Control Through the Generator Field. The fields of the d-c. motors and their synchronous tie-in units are energized by the exciters on these sets. The turbines are operated at about $8-1 \mathrm{~b}$. back pressure and the exhaust steam carries 88 per cent of its original heat to the dryers
tons. While not affecting the nature of the paper, this unit has also to be intimately tied in as to speed with the other sections. The entire course through the paper machine takes about 45 seconds.

These reels of paper are lifted by means of an electric parallel-motion hoist to stands, from which the paper is run through the slitter, which trims off the edges and slits the paper into two or more parts. The rewinder now rewinds the paper on paper tubes with metal ends that are adapted to the printing presses on which the paper will be used. It is usual to make two $731 / 2$-inch rolls, each weighing about 1400 lb . The rewinder is driven by a $30-\mathrm{h} . \mathrm{p}$. motor with speed control by means of a rheostat in the field of an
turbine generator set. The line voltage determines the rate of production on the paper machines and is 185 volts for 800 feet per minute, with a workable range from 500 to 1200 feet per minute. This voltage is controlled from the machine room by a chain-operated rheostat in the $500-\mathrm{kw}$. generator field. The turbine speed and the exciter voltage are held constant.

The motors driving the various sections have their fields energized by the 125 -volt exciter. They are large, low-speed units designed for about 150 r.p.m. at 245 volts so as to avoid the interposition of gears. The couch roll and calender stack each take a 100 -h.p. motor, while the presses each take a $50-\mathrm{h} . \mathrm{p}$. motor, the dryer two $100-\mathrm{h} . \mathrm{p}$.
motors and the reel a $30-\mathrm{h} . \mathrm{p}$. and the rewinder a $35-\mathrm{h} . \mathrm{p}$. motor, all of the shunt-wound interpole type.

With the exception of the rewinder motor and the second motor on the dryer, each motor is accompanied by a $20-\mathrm{h} . \mathrm{p}$. synchronous motor-or generator, as the case for the moment may be-and these synchronous tie-in units are all connected to a common three-wire three-phase bus to which nothing else is connected. Their fields are energized from the 125 -volt exciter. These synchronous units are belted through cone pulleys to the direct-current motors, with the exception of the first dryer motor. In that case the cone pulleys are dispensed with as the speed of this unit is taken as par and the "stretch and draw" of the other sections are regulated to this base speed.

The effect of these synchronous units tied in as they are is similar to that of a great flywheel which can be neither delayed nor hurried. With all the motors running, any direct-current motor and the section it drives may be adjusted as to speed by moving the belt along on the cone pulleys. If the direct-current motor field strength is right, the synchronous unit will be simply idling, as indicated by its ammeter. Should the directcurrent motor be inclined to run faster, the synchronous unit becomes a generator giving energy to the other similar units which for the time may be performing as motors. This puts a restraining load on the direct-current motor and effectually holds it in line. Conversely, if a direct-current motor is inclined to slow down, its attached synchronous unit would supply aid as a motor again, effectually holding the section in line.

These guide units can aid or hold back up to 40 h.p. each, and by occasional hand adjustment of the direct-current motor-field rheostats these exchanges of loads can be kept near to zero. Little attention is paid to the loads on these units, however, and the meters bear only a center mark and outside limit marks. Any change in the load on one unit affects the other eight by only one-eighth of the change. The belt shifter is brought through to the front of the machine, and the machine tender can change the speed of a section by a fraction of 1 per cent with the assurance that it will hold that place until he makes a further change.
When it is necessary to slow down or stop an individual section, the ordinary drum
controller is resorted to, and its first step disconnects the synchronous unit from the common bus. Thereafter the section is controlled in the ordinary manner. After the section is brought up to normal speed the synchronous unit is tied in by pushing


Fig. 12. The Speed of Each Section of the Paper Machines is Held Adjustably Constant by the Attached Synchronousmotor Guide Unit which may be Generating or Motoring to Hold the d-c. Motor !n Line
a button at the controller. Should the motor-overload circuit breaker open, it also disconnects the guide unit.

After a complete shutdown, as, for instance, to put in a new Fourdrinier wire, all the sections can be restarted, brought up to speed and tied in as fast as the controllers can be handled. The tying in by the synchronous units does not require any special manipulation, as, being belted to their respective sections, they are always so closely in accord that there need be no delay on their account.

In this mill, the only 100 per cent electrified mill in the paper industry, may be found practical applications of electric power in many forms. The pumping of water and stock forms a large percentage of the load, and the combined output of the pumps is about 140,000 gallons per minute. A reference to the chart in Fig. 3 showing the water content in the materials as they pass through the various operations will indicate how important these units are. The grinding of wood on such a wholesale plan by electric motors, while not new, is so well worked out here that it is worthy of considerable study. Only in very recent years has it been considered feasible to grind wood other than by direct application of water power. The hundreds of widely scattered auxiliary units of every conceivable type could certainly not be located so conveniently or operated so economically with any other form of power transmission than electric motor drive. Finally, the sectional motor drive of the paper machines themselves is a very fine development of special industrial engineering and works out very much to the satisfaction of the trade.

# Water Cooled Resistors 

By II. F. Wilson




#### Abstract

The anthor describes the large capacily water resistors designed for use with the electrical equipment 


Vory large capacity resistors are often reguired in starting large machines, such as induction motors ander load and for limiting the load on certain machines in a large network system when short circuits or overloats occur. As a rule the large capacity is only needed for a short time so that a resistor with high thermal capacity is the most desirable. In order to keep the weight and size of such resistors down to reasonable proportions, the resistance units are placed in water. The capacity is further increased if the water is circulated.

The resistance unit used in a resistor of this type must be made of a material which will not corrode in the water or be easily affected by electrolytic action. It must also have a low temperature coefficient and a fairly high specific resistance so that the amount of material necessary will not be excessive. The cross section should be such that the maximum possible surface of metal is exposed to the water.

Of the common medium priced metals, monel metal seems nearest to meet the above specifications. The resistance of this metal is approximately 0.00002 ohm per cubic inch against 0.00000069 ohm for copper. Its temperature coefficient averages approximately 0.002 as compared with 0.00393 for copper.

Two general types of water cooled resistors hare recently been built, one using a continuous circulation of water, and the other using a large tank of water, the amount of water being automatically held between two safe levels.

The water resistor No. 1 is of the first type and is shown in various views in Figs. 1, 2 and 3 . This resistor was designed to be used in the secondary circuits of the induction motors used for driving the Emergency Fleet Corporation cargo boats.

The assembled view of this resistor is shown in Fig. 1. In Fig. 2 it has one side removed showing the assembly of the insulating tubes and terminal plates. Fig. 3 shows the various internal parts of the resistor.

As can be seen from these photographs the resistor consists of three legs, each leg
having a ressistance unit made up) of 12 spirals of monel metal. The total resistance of the unit in the sea water at 20 der. $\mathrm{C}=0.10$ ohm. The three units are installed in three separate water-tight containers built up of tubes of suitable insulating material, each container consisting of two tubes spaced by a metal ring. A tube, which has been used to good advantage for ship work, is one made of treated wooden staves covered with varnish treated paper.

The object of separating the insulating tubes is to secure electrical creepage between the ring castings, to which the high sides of the resistor units are attached, and the top castings, carrying the manifold for the water, as the difference of potential between these two points may be several hundred volts.

The center or ring casting also serves for the outside connection from the resistors to the large contactors which cut the resistance in and out of the circuit.

Pure rubber gaskets are used to prevent water leakage between the ends of the tubes and the various castings, the parts being securely held together by retaining rod bolts. Each unit being capped with a separate casting, the tubes can be properly and tightly seated on the gaskets by the adjustment of the retaining rod nuts.

The twelve spiral resistances are supported by a central standard or post of wood, thoroughly impregnated with moisture-proof material which resists any detrimental action of salt water. The wood is bolted at the lower end to the frame base casting and is supported at the top by the brass ring which spaces the sections of the insulating container.

The individual spirals are prevented from sagging by cross pins made of wood. These cross pins are carried through holes in the standard and are secured by the same screws which fasten the spirals in place. The twelve spirals are connected in series and permanently tied together by copper straps riveted and brazed to the monel metal.

For the cooling system the sea water is pumped through a pipe main into the base casting where it distributes through the three
contanners and resistor anits, discharging through a manifold proxided with three apertures at the lop, the mamifold being comnected to a discharge pipe.

Three hand holes are proxided in the brass easting $t 0$ assist in assembling the resistor


Fig. 1. A Completely Assembled Water Cooled Resistor of the Continuous Water Circulation Type
units as well as to permit of inspection of the interior or removal of sediment which may accumulate. The hand holes are capped with steel plates lined with thin sheet zine, the zinc preventing the wasting away of the steel or iron from electrolytic action between
it and the mondel metal resistor mant of ill hat rather than the iron lxemy allawker! 'Th
 must be renewed.

The eromplete resistor is slemended bes a sheet metal grased to proteret the jumbation


Fig. 2. The Water Cooled Resistor shown in Fig. 1 with the Cover Removed
tubes from injury and to prevent anyone coming in contact with the live parts.

As used with the induction motors, this resistor is only in during starting and reversing, being "shorted" out during normal rumning. The maximum duty required of it,


Fig. 3. Partially Dismantled Resistor of the Type shown in Figs. 1 and 2


Fig. 4. Insulating Tubes for the Type of Resistor shown in Figs. 1 and 2
which ocous during a reversal at full speed, calls for the following eurrents per phase:

2730 amperes for 1.5 seconds.
2r30 amperes decreasing gradually to ㄹ.20 amperes in 10 seconds.
2200 amperes decreasing gradually to 1700 amperes in 4 minutes.
1-00) amperes decreasing gradually to 910 amperes in 7 minutes.


Fig. 5. Curve of Water Temperature for the Type of Resistor shown in Fig. 1 during the reversal of a ship at full speed

The resistance of each leg as stated previously equals approximately 0.10 ohm at 20 deg . C. or 0.12 ohm at 100 deg . C.

A circulation of 100 gallons of sea water per minute is maintained through the resistor while it is in service. A heat run at the above currents was made on one of these resistors and a thermostat placed in the water at the upper end of the middle compariment. The curve in Fig. 5 shows the temperature of the water for the first 60 seconds, the temperature gradually decreasing from this point to the end of the run.

A monel metal coil similar to the ones used in this resistor was tested in a jar of water to obtain the characteristics of the metal. The coil was located 4 inches from the bottom of a 30 -gallon porcelain jar 24 inches deep and 19 inches in diameter. This jar was filled to within 1 inch of the top with water. The resistance of the coil at 20 degrees was 0.007 S ohm and at the boiling point of water 0.01 ohm . The radiating surface was 105 square inches.

Various currents were held until the temperature of the metal became constant which was after the water boiled. The resistance of the coil was read and from this the temperature calculated.

Curve A, Fig. 6, shows the temperature of the metal for various watts per square inch.

For comparison Curve $B$ shows the temperatures obtained in air for various watts per square inch. These curves show that approximately one hundred times the watts radiated in air can be radiated in water. Curve C shows the time necessary for the water to boil for the various loads. The watts per square inch are calculated from the hot resistance.

This type of resistor using monel metal units has proven very satisfactory in service and should have a considerable field wherever large induction motor drive is used.

The second type of resistor, that using a large tank of water, has to date been used for load limiting resistance. The water resistors Nos. 4, 5, 6 and 7 are included in this type.

The first installation of these is in connection with 2.50 -volt, three-wire converters for the Kansas City Light \& Power Company. The water resistors Nos. 4 and 5 are used with a $2250-\mathrm{kw}$. converter and have a capacity of 18,000 amperes, twice the rating of the machine. The resistance of the water resistor No. 4 is 0.00409 ohm and of the water resistor No. 5, 0.00967 ohm .

The water resistors Nos. 6 and 7 are used with a $1.500-\mathrm{kw}$. converter. The water resistor No. 6 is connected in the positive side and has two steps of resistance, 0.00153 ohm in the first step and 0.00593 ohm total. The water resistor No. 7 is connected in the negative side and has 0.00153 ohm in the


Fig. 6. Curve of the Temperature of a Monel Metal Coil at Various Watts per Square Inch in Water and in Air
first step and 0.01303 ohm total. In normal operation all the resistance is "shorted" out by contactors. If the load on one side increases beyond a certain point the first step of resistance on that side is cut in. If a balanced overload occurs the first step on each side
is cut in. If these first steps donot limit the load sufficiently the neutal wite is opened and one of the largersteps cint in. In case of a short circuit at or near the busses all the resistance is cut in and this acts as a load directly across the generater. In the case of


Fig. 7. Water Cooled Resistor of the Tank Type, showing the Main Terminals and Automatic Cutoff
the water resistors Nos. 6 and $\overline{7}$, the current will be limited to 12.000 amperes, twice the normal rating of the machine. These resistors must therefore be capable of carrying this current practically continuously.

The water resistor No. 6 is shown in Figs. 7,8 and 9 . These views show the simple con-


Fig. 9. Interior View of the Resistor shown in Fig. 7
struction of the resistor, it consisting primarily of a steel tank, the resistance unit and the water regulating devices.

The tank is made of steel, the sides being in two parts, welded together and then
welded to the bentom. Insulated lnashars extend throtgh and are fastened to one side.

As shown in Pig. 7 , a syphom regulator is attached to one end. This is adjusted so that fresh water will be admitted when the temperature of the water inside approaches


Fig. 8. The Water Gauge End of the Tank Type of Water Cooled Resistor shown in Fig. 7
the boiling point. The water will continue to flow, running out through the overflow pipe on the other side, until the temperature is reduced to a safe value.

As shown in Fig. S, a safety water column and gauge is mounted on the other end of the tank. The gauge indicates to the station operator the level of the water. If the level


Fig. 10. Resistance Unit Removed from lts Position in the Tank as shown in Fig. 9
becomes too low the float in the water column operates, opening an interlock which opens the line contactors.

An angle iron is welded along the outside upper edge of the tank to which the top is
bolted. I pipe wotlet is provided in the center of the top to allow the steam to ssape.

Fig. ! shows the inside of the tank and Fig. Io the resistance unt remosed from the tank. This unit consists of a wooden support,


Fig. 11. Another Water Cooled Resistor of the Tank Type (similar to that shown in Fig. 7)
the monel metal resistance and the copper busbars which extend from the ends and tap on the monel metal to the large insulated busbar terminals which extend through the side of the tank.

The monel metal resistance is made of strips of metal brazed together to give the length necessary for the resistance. This is bent as shown in the photograph to give 714 convolutions.

The water resistor No. 7 has the same dimensions as the water resistor No. 6 except it is wider and the resistance unit is correspondingly wider, having $151 / 2$ convolutions. The total resistance equals 0.013 ohm with a tap equal to 0.00153 ohm. It has two pipe outlets for the escape of the steam. Fig. 11 shows this resistor.

This resistor holds $\$ 20$ gallons of water when filled up to the overflow pipe. Based on 100 per cent efficiency and assuming the water at 20 deg . C. it requires 21.1 kw . to heat one gallon S 0 deg. or to the boiling point.

Theoretically, therefore, neglecting the thermal (apacity of the tank, $17,300 \mathrm{kw}$. can be dissipated for one minute before the water reaches boiling temperature; and 1.870 kw ., the nomal capacity of the resistor, for $91 / 4$ minutes. Due to the thermal capacity of the tank and other parts of the resistor, an actual heat run at 12,000 amperes ( 1870 kw .) shows that it requires between 11 and 12 minutes to boil the water. In normal operation, however, the sy?phon regulator operates Defore the water boils and cold water is admitted holding the temperature below the boiling point.

It is interesting to compare the size and weight of this resistor with one made of cast iron grid resistors and air cooled, of the same capacity: The water resistor No. 7 weighs 26.50 pounds without water and 9500 pounds when filled with 820 gallons of water. Its volume is 150 cubic feet.

If standard cast iron grid resistors were used, it would require approximately 25,000 pounds of material and 300 cubic feet of space without any supporting frame.

If these resistors were arranged for maximum forced ventilation, the amount would be decreased to approximately 10,000 pounds and 120 cubic feet without supporting frame. The volume including supports with the ventilated grids would be approximately the same as the water cooled resistor, but a blower would be required capable of delivering approximately 15,000 cubic feet of air per minute requiring 11 or 12 horse power. Automatic means for starting this blower when power came on the resistor would have to be provided.

Although the volume and weight (including water) of the water cooled resistor and the ventilated air cooled resistor are approximately the same, when it is noted that the water cooled one requires only 2650 pounds of solid material compared with 10,000 pounds in the air cooled one, the advantages of the former can be appreciated.

It can be seen from the above that for large capacities such as necessitated the design of these resistors, this type of water cooled resistor should be superior to the air cooled one from the standpoint of cost, maintenance, weight, volume and simplicity.

# The $40,000-\mathrm{kv}-\mathrm{a}$. Shawinigan Falls Waterwheel Generator 

By J. Ralph Johnson<br>Contrace Service Deparment, General Eeectric Company

The $40,000-\mathrm{kr}$-a. waterwhed generator which was placed in operation at the Shawinigan Falls Develop. ment, Quebec, Canada, is notable not nnly on account of its size but for its other features of ultra-modern design. The following article describes the design and construction of the machine, and the illustrations show the various stages of its installation. In a forthcoming issue of the REvew we hope to publish a summary of the acceptance tests of this huge waterwheel generator unit whose rotating element alone weighs 20.1 tons.-Editor.

The $40,000-k r-a$. waterwheel generator at the Shawinigan Falls Development of the Shawinigan Water \& Power Co. (Quebec, Canada) has been in operation since October of last year and is the largest machine of this type installed by the General Electric Company to date.

The unit is of the vertical type with direct-connected exciter, and is designed to deliver normally $40,000 \mathrm{kr}-\mathrm{a}$. of three-phase current at 0.50 power-factor, 60 cucles and 11,000 volts, the speed being $133 . \mathrm{i}$ r.p.m. It will also operate on 25 per cent overload ( $44.000 \mathrm{kv}-\mathrm{a}$.) at 0.3 .5 power-factor for two hours without undue heating, and mav, if required, operate continuously at 12,000 volts and full-load current. At full load and unity power-factor the efficiency is 97.5 per cent and the regulation 1.5 per cent.

The rotating parts of the gencrator and turbine are carried by a thrust bearing supported by a deck or bracket which spans the top of the stator frame. The generator and turbine shafts are connected by a solid coupling and there are two guide bearings, one between the thrust bearing and the rotor, the other a lignum ritæ bearing above the waterwheel.

An interesting feature of this installation is that the operating floor is level with the top of the stator frame. This construction gives ample space round the generator on the main floor and provides a convenient means for dealing with the exhaust air from the generator in the annular space beneath this floor, as the air may either be utilized to heat the generator room in winter by opening up steel trap-doors in the floor, or it may in summer be ejected outdoors through windows in the outer wall beneath the main floor.

A point of interest external to the machine is the absence of low-tension switches; the
generator is connected directly to the transformer primary windings through the lowtension bus. Disconnecting links are provided so that the machine may be isolaterd if necessary, and oil circuit breakers are installed between the transformer secondary windings and the high-tension bus for 100,000 -volt service.

## Stator Frame and Core

The stator frame is of cast iron and is divided vertically into four ! 0 -degree sections


Fig. 1. Schematic Diagram of the Armature Winding
in order to facilitate transportation and handling. The outside diameter is 30 ft .4 in . and the height if ft .10 in . The stator core was built up on site in order to avoid the contintous vertical joints which occur in cores which are assembled in the factory and shipped in sections.

## Stator Winding

The armature winding is three-phase, uniformly distributed round the core, and the coils have a fractional pitch. Thus a voltage wave closely approximating a sine wave is obtained and higher harmonics are eliminated. This was confirmed by an oscillogram of the
voltage wate taken after the machine was 1) Operation.

The coils are of the mica insulated type, mica tape having been employed both for the insulation botwoen turns and for coil insulation. Asticker componnd was used between


Fig. 2. Layout of the Work During Construction
the layers of the coil insulation, and all air spaces were eliminated from the coils during the vacuum process of impregnating them with insulating compound. This prevents possible destruction of the mica insulation by ionization and permits the compound to fill completely the interstices of the coils. An outer armor of horn fiber was moulded on the coils thus obviating the use of slot lining. When cold the coils are perfectly solid and it is customary to heat them slightly in order to render them flexible, before inserting or removing them from the slots. Wedges of maple wood secure the coils in the slots.

The copper conductor is suldivided into wires of rectangular section, cotton covered; by this means eddy currents in the copper are considerably reduced and the coil forming process is facilitated.

The phases are effectively distributed round the core as there are four circuits from line to neutral in each phase, giving 12 internal circuits in the winding, the armature reactance being approximately 20 per cent. Six line and six neutral leads are brought out from the machine as shown in Fig. 1; this permits the use of both the differential and the split conductor method of generator protection, since current transformers may be mounted on the two leads of each line. The neutral is grounded through a high resistance and ground relay.

Steel bracing rings attached to brackets on the stator frame are employed for supporting the ends of the coils which are securely tied to the rings with prepared cord. The supporting rings are well insulated with mica and varnished cambric thus providing in addition to insulation a mechanically protective cushion for the coil ends. This method of bracing the coils gives ample strength against the distorting effect of short circuits and allows expansion and contraction of the coils due to temperature changes.

Series connections between adjacent coils are made by means of soldered joints and copper clips, while pole connections are made of flexible conductors similar in section to the stator conductors and connected to the latter by the same type of joint as the series connection. All joints are well insulated with varnished cambric. The phase connections are made to flexible bus rings which run over the top of the end connections, from which they are separated by wooden spacers and to which they are tied for support. The bus rings are also braced against one another by means of wooden spacers and cord.

During the winding of the armature six temperature indicating coils were inserted in pairs of slots that are spaced 120 mechanical degrees apart. Four were placed between coils in the slots and two were placed at the bottom of the slot between the lower coil and the core iron. Armored cables connect the different temperature coils with a protective device on the stator frame which serves to bring any temperature coil to ground potential, by breaking down its insulating disk cut-out, in case the coil exceeds a definite potential which would be unsafe for the instrument or switchboard operator.

## lotor

The rotor spider is made of cast steel and onsists of three wheets each made up of two emi-circular sections bolted together at the ub and linked together at the rim by shrink eys. The rim, arms and hub of eacli section re cast solid. Some manufacturers have aised objection to this type of rotor contruction in large units owing to the difculty of obtaining reliable castings. If, owever, proper care is taken in annealag, testing of samples, and keeping stresses $t$ overspeed within half the elastic limit, ntirely reliable castings can be and have een made. The rotor with the rim cast olid with the spider offers certain advantages ver the laminated rim type. In the former he rim stresses are relieved by the arms, and he rotor balance will not be disturbed while he machine is in operation as might be the ase where a laminated rim "settles" on the hrough-bolts while running.
A one-inch space is left betwcen the wheels $y$ making the hubs slightly wider than the ims; this allows ventilating air to pass along he spider, between the pole pieces, and out hrough the stator ducts. Fans are provided $n$ the upper and lower faces of the rotor im, to draw the cooling air from the pit eneath the generator. Small circular blocks erve to keep the rims separated and suported at intervals, and the three wheels re tied together by vertical bolts through ight arms of each spider.
Fifty-two pole pieces with coils of edgeround copper strip are assembled on the pider by means of V-shaped dovetails and re held securely in position by two taper eys. This fit is designed to withstand tresses due to double normal speed without ny slackening and without exceeding half he elastic limit of the material.
The shaft is made of forged steel and has a olid forged flange which is bolted to the raterwheel shaft flange for coupling. The oupling bolt holes were reamed on site thus asuring proper alignment of the two shafts.
The total weight of the complete rotor is 01 tons and the flywheel effect $\left(W R^{2}\right)$ is $5,034,000 \mathrm{lb} . \mathrm{ft}^{2}$
The kinetic energy stored in the rotating arts is enormous and it would take a coniderable time to bring the machine from ormal speed to rest unless some method of raking were provided. A mechanical braking vstem was therefore installed which serves he double purpose of shutting down the aachine quickly and of holding the rotor
at rest against possible leakage past the waterwheel gates when the Johmson valve is not closed.

Six brakes are mounted on concrete pillow-blocks beneath the muder surface of the rotor rim. Each brake has two cylinders


Fig. 3. Completed Rotor Suspended From Crane by the Lifting Trunnion
with pistons 6 in . in diameter and a shoe is mounted on each pair of pistons. The cylinders are connected to each other and to a tank reservoir containing oil, and normally the tank and interconnecting pipes are full of oil. In order to apply the brakes when the machine is running, air at 7.5 lb . pressure is introduced to the tank by means of a motorman's valve mounted on the operating floor.

The air is introduced and exhansted periodically as the machine slows down, in order to avoid excessive wear of the brake-shoes the pressure is transmitted by the oil to the


Fig．5．Assembling the Rotor Spider



Fig．4．Completed Armature Winding and Three of the Brake Blocks

cylinders, and the hrake-shoes monnted on each pair of pistoms are made to bear on the rotor rim.

The brakes may also be nsed when necessary as jacks to raise the rotor from the thrust bearing for inspection or repair purposes. In this case a hand-operated oil pump is used. This pump is comected to a three-way cock at the bottom of the tank reservoir; the tank is shut off and an oil pressure of about 1.500 lb . is built up in the system by the hand pump. The brakes raise the rotor off the thrust bearing and shims are inserted between the brake shocs and the cylinders so that the rotor will remain raised when the oil pressure is removed.

## Upper Bearing Bracket

The upper bearing bracket is made of cast steel. It consists of tro sections bolted together forming at the center the housing for the upper guide bearing, and the base for the thrust bearing oil bath. The end of each bracket arm rests on top of the stator frame and is provided with a lip in which there are three bolt holes. Two of these are for jack bolts which are used to raise the bracket so that shims may be inserted between the lip and the stator frame for fine vertical adjustment of the rotating parts. The third hole is for the holding-down bolt. In order to insulate the bearings from ground, mica pieces are placed on the stator frame beneath the bearing-bracket shims and insulating washers and bushings are employed on the holding-down bolts. All pipes connected to the bearings have an insulated union so that the possibility of shaft circulating currents, with consequent pitting of the bearings, is eliminated. Cast steel was used in this bracket in preference to cast iron because for a given deflection a much lighter casting may be used thus allowing a more shallow structure, and rendering it possible to lead the drain pipe from the oil pan beneath the upper guide bearing, over the top of the stator frame, instead of employing a rotating pan which has to be drained down through the rotor.

## Bearings

The generator guide bearing is of the standard babbitted type with grooves for distributing the oil, while the waterwheel guide bearing is of the water lubricated lignum vitæ type.

The General Electric spring thrust bearing is used on this machine and is designed to carry a load of 360 tons, this figure including
the hedraulice thrust of I 10 twns. 'lhe Inamme consists essemtally of a spring-4ppmoneal stationary babbiticd phate and a hiobly polished hard wrey cast-iren rotating plate. The stationary plate has radial of aromes and a radial satw-cut which provents any tendence of the plate to dish mader increased temperature It is supporterl on a latre number of helical springs lonsely pinned to a base plate which is dowelled to the machined face of the upper bearine latacket. The flexibility of this support allows the plate to conform to the natural alismment of the shaft thus preventing excessive local pressures in the bearing and allowing the maintenance of an oil film between the bearing surfaces. The rotating plate is

TABLE I

## PRINCIPAL DIMENSIONS AND WEIGHTS OF $40,000 \cdot \mathrm{KV}-\mathrm{A}$. GENERATOR

|  |  |
| :---: | :---: |
| Dial |  |
| Height of stator frame |  |
| Overall height from coupling to top of exciter. |  |
| Maximum height above operating flonr. 13 ft .6 in . |  |
| Weight of shaft. . . . . . . . . . . . . . . . . . . $32,000 \mathrm{lb}$. |  |
| Weight of rotor spider |  |
| Total weight of rotor with shaft . . . . . . 402,000 lb. |  |
| Weight of waterwheel runner |  |
| Hydraulic thrust. . . . . . . |  |
|  |  |

dowelled to a thrust collar which is keyed to the shaft, and a split retaining ring in a circular keyway near the top of the shaft is bolted to the thrust collar. The bearing operates in an oil bath and the heat generated is taken up by the oil as it passes by centrifugal action between the bearing surfaces. Heat is also transmitted to the oil through the metal of the bearing plates. The heat is removed from the oil by the circulating water in a stack of cooling coils immersed in the oil bath. In order to maintain the oil clean it is circulated slowly and filtered. Clean oil is pumped from a filter tank on the ground floor to an upper tank above the level of the machine. From the latter tank the oil is piped to the guide and thrust bearings, thence to a common drain which returns to the filter tank. If by any chance the oil pumps one of which is in reserve) develop trouble and have to be shut down, the generator may still rum if the thrust bearing oil supply line is shut off. as the storage tank can supply the guide bearing for several hours and the cooling coils will maintain the oil in the thrust bearing at normal temperature.

## Excitation

A $2.2(0) \mathrm{k}$ : $2.0(0$-volt exciter, shunt wound, with commotating poles and designed for service with an antomatic boltage regulator is direct connected to the top of the generator shaft. The exciter armature spider is provided with a recessed lower face which fits over the main shaft and is bolted thereto.

The leads from the generator field pass along an arm of the rotor into the shaft and up through a central hole to the slip rings above the exciter.

No rheostat is employed in the generator field, voltage control being effected with the exciter field rheostat. The rheostat losses are thus cut down to a minimum.

# Direct-Current Locomotives for the Imperial Government Railways of Japan 

By A. Bredenberg, Jr.<br>Railway Equipment Engineering Department, General Electric Company


#### Abstract

The United States has been the great proving ground for railway electrification. There are here present a combination of the talent necessary, the manufacturing facilities required, and the reasons for electrification which are: the high cost of maintenance, labor, and fuel for steam operation; the limitations placed on greatly increased tonnage movement by inadequate parallel trackage, heavy grades, or severe climatic conditions; and the smoke nuisance in tunnels and at terminals. All the types of electric systems that showed promise have been tried out on a practical scalc. As the result, the governments of England, France, and Holland have officially accepted the high-voltage direct-current system for their electrification programs; and installations are in operation, or contracted for, in Spain, South Africa, South America, Australasia, Mexico, and Japan. The following article details in particular the control equipments of the locomotives for the initial 1500 -volt directcurrent electrification in Japan.--Editor.


Two direct-current locomotives have recently been completed for the Imperial Government Railways of Japan. The track gauge of this railway system being 42 inches, considerably smaller than is standard in this country, necessitated a very compact design widthwise. This narrower gauge also lends added significance to the locomotive weight, $132,000 \mathrm{lb}$., which is carried entirely on the drivers. The tractive power is furnished by four motors each directly geared to a driving axle. Thus equipped, the locomotives are capable of hauling 670 tons up a one per cent grade at 15 miles per hour.

For the present, the locomotives will operate on the Tokaido line between Tokyo and Yokohama at 1200 volts. Eventually, they are to operate on the extension of this electrification at 1500 rolts direct-current.

While the narrow gauge prevented the use of parts exactly like those in use in this country, where the gauge is $4 \mathrm{ft} . \mathrm{S} / 2 \mathrm{in}$., the design is rery similar to the design of locomotives used successfully on various American railroads.

The running gear consists of two-axle main trucks supporting the superstructure on centerplates. The truck has cast-steel transoms which carry a hollow centerplate and have openings provided with collars at the sides held against the motors in such a manner that
air delivered by a fan in the cab passes down through the centerplate into the hollow transom and thence to the motors.

Equalization of the load on the journals is provided for by semi-elliptic springs and by coil springs in series with the leaf spring which tends to produce an easier riding truck.

The width of the locomotive is determined by a strict clearance line, and by the necessity

TABLE I
PRINCIPAL DATA OF LOCOMOTIVE

| Trolley voltage. | 1500, 1200, or 600 volts |
| :---: | :---: |
| Track gauge | 42 in. |
| Length over bumpers | $37 \mathrm{ft} 2 in.$. |
| Length over cab.. | 29 ft .0 in . |
| Total width. | $9 \mathrm{ft} .41 / 4 \mathrm{in}$. |
| Total. height (Trolleys locked down) | 12 ft .10 in . |
| Total wheel-base. | 26 ft .0 in. |
| Rigid wheel-base | 8 ft .6 in . |
| Diameter wheels | 42 in . |
| Weight locomotive (all on drivers). | $132,000 \mathrm{lb}$. |
| Weight per axle.. | $33,000 \mathrm{lb}$. |
| Number of motors | 4 |
| Tractive effort; one-hour rating ( 1500 volts). . . | 17,800 lb. |
| Tractive effort; continuous rating ( 1500 volts). | 17,300 lb. |
| Starting tractive effort; 25 per cent coefficient of adhesion. | $33,000 \mathrm{lb}$. |

for kecping within such clearance lines on certain specified curves.

The draft and buffing are taken care of by what is known in this country as European type draft gear and buffers; although the details are in accorlance with the Inperial Government Railways' standards. Provision is made for substituting American type draft gear which eventually may be the Japanese standard.

The construction of the platform of structural channels and plates follows the method used in this country:
rolts the moter and resistance commections are commutated so that the sume sperl is olsamerl on 600 volts as (10 1200 volts.

Fig. 4 illustrates the master controller msed. It has two speed combinations with ten steps in the first combination and eight steps in the second. This gives an ample number of operating steps for a locomotive of this size and allows the torque increments between steps to be so proportioned as to obtain smooth acceleration. The first nine steps in the first combination and the first seven steps in the scond combination are resistance steps, i.e.,


Fig. 1. $1500 / 600$-volt Freight Locomotive for Imperial Government Railways of Japan

The cab is of the box type which lends itself best to housing the type of equipment required by the necessity for operation at the same speed on 600 volts as on 1200 volts.

The control equipment for these locomotives is of particular interest as it embodies several new features of design. Outstanding among these features are a new form of high-speed circuit breaker for locomotive service and a new type of electro-pneumatic contactor unit for controlling the motor and resistance circuits.

## Operation

These locomotires are designed to operate on 1500,1200 , or 600 volts. They may be operated either in single unit or with two locomotives in multiple. On 1500 and 1200 volts the same control and motor connections are used, the speeds obtained being approximately proportional to the voltage. On 600
with resistance in series with the motors. The 10 th and 1 Sth steps are running steps with all the accelerating resistance short circuited.

The control voltage for energizing the master control circuits is obtained from the midpoint of a dynamotor with a $2: 1$ voltage ratio. This dynamotor is operated by trolley voltage. Thus with 1500 rolts on the trolley the nominal control voltage is 7.50 volts and with 1200 volts on the trolley it is 600 volts. For operation of the locomotive on 600 rolts, the control circuits are disconnected from the dynamotor and connected directly to the trolley:

On 1.500 or 1200 volts the motors are connected in two groups, each group having two motors connected in series. Thus the motors are operated all four in series in the first combination, and in two multiple groups of tro motors in series in the second combination. On 600 volts the motors in each group are connected in parallel. The motors are
then operater in two series groups of two momors in multiple in the first combination, and all fome motors in moltiple in the seconnl comblinationt.

As a result of these two operating comnections, the same foltarge is applied in the


Fig. 2. Side View of Truck with Motors Assembled
individual motors when operating on the 600volt section of the line as on the 1200 -volt section. Thus the same running speeds are obtained on both voltages.

The change in connections described is aceomplished by means of an air-operated commutating switch. For 600-volt operation this switch changes each two-motor group from the series connection to the multiple comnection. It also divides up the accelerating resistance into several sections and reconneets these sections into a number of series groups, each group having two sections in multiple. By this means approximately the same resistance steps are obtained on 600 volts as on 1200 volts.

When transferring from the first motor combination to the second, the transition is accomplished by means of contactors. In transfer: first, part of the accelerating resistance is cut back in circuit; then, one pair of motors is short circuited while the other pair of motors is maintaining torque on the locomotive. Finally, all four motors are connected in two multiple groups with resistance in the circuit. By this method of transfer, torque is never lost in going from the first to the second combination or from the second to the first. It provides smooth operation of the train during transfer and prevents any jolts or damage to draft gear.

## Current Collection

The locomotive will operate from an overhead trolley wire. Each is equipped with two pantographs similar to those used on the Chicago. Milwaukee and St. Paul Rwy., the

P'anlista Rwy., and others. Each trolley has two independent pans with sliding contacts. The contacts are of copper and are easily rencwed. The ends of the pans are provided with long horns to prevent fouling the overlead if the pan should run off the trolley wire. The operating range is about $61 / 2 \mathrm{ft}$., and throughont the range the pressure on the trolley wire is held approximately constant.

The trolleys are air raised and gravity lowcred. A hand pump is provided for raising the trolleys when there is no air pressure on the locomotive. This pump may be used either to operate the trolleys directly or to pamp air into a trolley rescrvoir from which air pressure may be obtained later for operating the trolleys. This reservoir may cither be pumped up from the hand pump or from the air compressors if the latter are running. A globe valve is connected in the reservoir line which allows air pressure to be maintained in the reservoir for several hours. It will thus rarely be necessary to operate the hand pump.

## Main Circuit Switches

The switches in the main motor circuits consist of:

17 electro-pneumatic contactors
1 reverser
1 main switch
1 motor cutout switch
1 commutating switch.


Fig. 3. End View of Truck with Motors Assembled

## Contactors

Electro-pneumatic contactors are used to make and break the main motor circuits, to transfer the motor connections when passing from one motor combination to another, and to short circuit the starting resistors when accelerating. Figs. 5 and 6 illustrate this contactor.

It will be seen that the elements of the contactor are mounted on an upright insulated rod. This rod is fastened at the top and botton to angle-irons in the locomotive by means of U-bolts. This method of support gives considerable flexibility in mounting the contactors in the locomotive. The operating mechanism of the contactor consists of a maynetically controlled air cylinder which operates a piston and rod that in turn operates the movable contact through an insulator. Both contact tips are alike and are cut from a rolled copper section. The contactor has a narrow are chute with are suppressor plates which together with the blowout coil give a very effective blowout.

The construction of the contactor with the electro-pneumatic operating mechanism, together with the narrow are chute and method of mounting, results in a very compact unit which is comparatively light in weight and requires considerably less room for mounting than previous types of contactors of the same capacity.


Fig. 5. Electro-Pneumatic Contactor

## Reverser

A four-motor electro-pneumatically operated reverser is provided for reversing the traction motors. This device is of a new design that is quite simple in construction. It consists of a series of cylindrical castings which are mounted along an insulated shaft,
this shaft being operated bey the air eylinders. The contacts are made be fingers momented on insulated rods on each side of the main shaft This construction gives a line of reversers for different numbers of motors and of different capacities which hate many parts in common.


Fig. 4. Master Contro'ler with Cover Removed


Fig. 6. Electro-Pneumatic Contactor with Interlock

## Main Switch

A hand-operated knife-blade switch is placed in the circuit ahead of the main motor equipment. It carries the entire traction motor current and is used to isolate the main part of the equipment when it is desired to test out the control anxiliary circuits, etc.

This switch is monnted on an insulated rod similar to those used for the contactors, and can the mounted if desired on the same amgle-iron supports as the contactors.

## Motor Cutout Switch

A hand-operated motor-cutout switch is provided for cutting out one pair of motors in


Fig. 7. Pneumatic Commutating Switch
case one of the motors is damaged. The locomotive can then be operated by the two remaining motors, either in single unit or in multiple with another locomotive. This switch is very simple in construction and consists of a single-pole double-throw knifeblade switch mounted on an insulated rod similar to those used for the contactors and main switch. The switch carries a number of finger type interlocks which commutate the control circuits for operation with motors


Fig. 8. High-speed Circuit Breaker
cut out. It is mounted on the same angle-iron supports as the contactors.

## Commutating Switch

A commutating switch is provided to change the motor, resistance, and auxiliary
circuit connections so that full-speed operation may be obtained on half the normal operating voltage. This switch is air-operated and controlled by hand-operated valves. It is quite similar in construction to the reverser, some of the parts being interchangeable.

The switch, Fig. 7, has contacts for changing the connections of each two-motor group and for dividing up and paralleling the accelerating resistance for operation on low voltage. There are also auxiliary contacts to commutate the compressor and blower connections to run at full speed on half voltage and to change the control voltage connection from the midpoint of the dynamotor to the trolley circuit.

## Protective Apparatus

The protective apparatus for these locomotives consists of the following:

1 high-speed circuit breaker
1 overload relay
1 protective relay
1 lightning arrester
Fuses for auxiliary and control circuits.

## High-speed Circuit Breaker

Short circuit and overload protection is obtained by a high-speed circuit breaker, Figs. $S$ and 9 , which is connected in the main


Fig. 9. High-speed Circuit Breaker Connections
motor circuit directly after the main switch. This is a new form of high-speed circuit breaker for locomotive service. It has several features which make it a distinct improvement over those which have hitherto been applied to electric locomotive service.

In the first place the size and weight for a given capacity have been greatly reduced. It operates on the same principle as those which have previously been described in this magazine;* viz., the armature, operating the movable contact, is held in the closed position magnetically against the tension of strong springs and is released under short circuit or overload by the shifting of the magnetic flux in the holding circuit, due to the action of a bucking bar which carries the entire traction motor current.

Former locomotive high-speed circuit breakers have been closed br a magnetically operated mechanism. This circuit breaker is closed by an electro-pneumatically operated mechanism. Furthermore, the closing mechanism has a trip-free feature. This is obtained by making the movable contact arm separate from the armature and piroting it from the armature arm. Thus in closing, referring to Fig.9, the air-operated closinglever $C$ pushes the armature $A$ against the holding magnet which then holds the armature in against the tension of two strong springs. The closing lever, while closing the armature, at the same time holds the movable contact $B$ open. When the air closing mechanism is released, it in turn releases the contact arm, allowing the contact to close by means of the tension of the springs $D$. With this trip-free feature, if the contacts should close on a short circuit, they would open immediately and would not be required to wait until the closing mechanism was released as the contacts cannot close until the


Fig. 10. Overload Relay
closing mechanism starts to drop back. This is a very important advance in high-speed circuit breaker design.

As in former circuit breakers this one has a strong magnetic blowout with a narrow arc

[^21]chute which will effectively ofon very heavy short-circuit currents.

The tripping point of the circuit breaker is set at the desired value by means of adjustable plugs in the magnetic circuit.

When the circuit breaker opens on short circuit or overload, interlocks open the line


Fig. 11. Protective Relay
contactors. These contactors cannot then be reclosed until the circuit breaker has been reset, which is done on the first point of the master controller.

## Overload Relay

An overload relay is provided for overload protection of the indiridual motor circuits. This relay, Fig. 10, has two series coils either of which will operate the relay contacts. One coil is connected in each two-motor circuit. When the motor current exceeds the setting of the relay, the relay contacts are opened against the compression of the resetting springs. This opens the holding circuit of the high-speed circuit breaker, thus causing it to drop out. Operation cannot then be resumed until the master controller has been turned back to the first notch. The relay contacts automatically reset as soon as the orerload current is remored.

## Protective Relay

When operating from the 600 -volt section of the line with the main and auxiliary circuits in the low-roltage connection, protection is afforded in case the locomotive runs onto the 1.500 or 1200 -rolt section of the line and the operator fails to throw the commutating switch to the high-voltage connection. In this event the high-speed circuit breaker protects the main part of the equipment while a protective relay protects the auxiliary circuits. This relay. Fig. 11, is placed in circuit ahead of all the auxiliaries. It has two coils, an

Wertaing conl aml a tripe coil, and onte sed of contants The contact amband the operating abmature are independently piveted but are
 momatly the melay operates simply as a shome



Fig. 12. Operator's Position Showing Master Controller, Air Valves, Gauges, etc.
opening when voltage is removed. In the high-roltage connection the trip coil is not connected in circuit. In the low-voltage connection the trip coil is connected in series with the operating coil and is calibrated to trip out the trip catch at about 700 volts.

The following sequence of operations results if the locomotive passes from the low-roltage to the high-voltage section of the line and the commutating switch is not thrown to the highroltage position. First, the relay contacts of en when the dead section of the line is reached. Then, when the high-voltage section is reached, the trip coil operates, tripping out the trip catch and preventing the contacts from closing when the operating coil picks up its armature. A small relay is used to short circuit the operating coil in the de-energized position. This slows up the operating coil and allows the trip coil to operate first.

This scheme gives a very effective protection for the auxiliary circuits as the high potential cannot be applied even momentarily to the auxiliary circuits until the commutating switch has been thrown to the high-potential connection.

## Fuses

A cartridge fuse is placed in circuit ahead of all the atuxiliaries including the protective relay. The individual anxilatry motors, the control cirenits, lights, ete., are protected by cartrilge fuses in the auxiliary switehes.

Lightning Arrester
Probection from damage by lightning is scoured by means of an athminum-cell lightning arrester especially o kesigned for railway service This arrester is comnected to the folley circuit ahead of all the apparatus.

## Auxiliaries

The control voltage on 1.000 or 1200 -volt aperation is obtained from a dynamotor with


Compressed air for the air brakes and pnenmatic control apparatus is obtained from two Tint-volt air compressors each having a capacity of 3.5 ( cl 1 ft , jeer min. (On 1500 or 1200


Fig. 13. Apparatus Compartment Showing Location of High-speed Circuit Breaker
volts the two compressors are connected in series, and the lead connecting the compressors is connected to the midpoint of the dynamotor. This balances the load between the two compressors and also provides a means of cutting out one compressor and
sperating with the remaining compressor in ase of emergence.
On low-vitage operation the compressors are each commected directly across the lime hus obtainme full-speed operation on half ohlage.
Forced ventilation for the traction motors s.provided by two blowers. ane for eath pair of motors. These blowers are driven by Totooold motors which are connected in series for 1500 or $12011-$-olt operation and in parallel on 300 rolts


Fig. 14. Apparatus Compartment Showing Location of Contactors, Cutout Switch, Commutating Switch, Reverse:and Resistance Tubes

## Location of Apparatus

An idea of the location of the apparatus in he locomotive cab may be obtained from Figs. 12 to 15 . The cab is of the box type with he apparatus compartments in the center of he locomotive and an operating cab at either nd.
A master controller is located on the left ide of each operating cab and is constructed or operation by the right hand. Directly efore the operator is a gauge panel containing in. ammeter, voltmeter, and air gauges. In me cab is a mercury watthour-meter for measring the power input to the locomotive.

Each operating cal) also contams enclomed hand-operated switches for the anxiliary: onntrol, and light circuits.

There is an aisle connecting the (wo (力) ing calbs on either site of the apparatus compartments. In the center of the apparatus (al) is a compartment containing the accelerating resistors. This compartment extends from the floor to the roof. The air for ventilating the resistors enters throngh openings in the bottom of the compartment and is vented through a ventilator in the roof. (On either side


Fig. 15. Apparatus Compartment Showing Location of Relays and Resis:ance Tubes
of the resistor compartment is a compartment for the control and auxiliary equipment.

The dynamotor, compressors, and blowers are located on the cab floor. The high-speed circuit breaker, contactors, switches, relays, control resistance tubes, etc., are mounted above the motor-operated auxiliaries. This arrangement places the control equipment in a convenient position for inspection or repairs.

From the foregoing description, it may be seen that the principal features of the control equipment for these locomotives are : reduced space occupied. reduced weight, accessibility of parts, and general simplicity:

# 30-kilowatt 15,000-volt Rectifier for the United States Navy 

By A. Schmidt, Jr.<br>Rmbo Enginelering Department, General Electiric Company


#### Abstract

In ant article on "IIigh-voltage Thermionic Rectifiers" in our February, 1923, issuc, the author indicated the remarkable development of the pliotron or vacuum tube converter, with the accompanying demand for power sources up to 15,000 volts direet current to operate these tub es, and then he described the various forms of this type of rectitier. In the following article he describes a specific rectifier of that character developed for the Radio Service of the Navy Departinent to deliver 30 kilowatts at 15,000 volts with a ripple of not more than one-tenth of one per cent.- Ebroor.


The $30-\mathrm{kw}$. vacuum-tube rectifier recently built for the Radio Service of the Navy Department receives threc-phase power at 2.) creles, and delivers two amperes at 7000 to 15,000 volts. The rectifier chosen was of the polyphase type with two Y's 180 deg. out of phase and paralleled with an interphase transformer. Variation of the di-rect-current voltage was securd by tapping the low-tension winding of the transformer. A total of nine taps was needed to supply


Fig. 1. Schematic Circuit Diagram of the $30-\mathrm{kw}$. Rectifier
the necessary voltage range. Twelve kenotrons (UT-2is) were used, two being required in each of the six phases to carry the current. The resultant 1.0 (-cycle ripple is attenuated in a double-mesh filter having a single tuned element, so that the amplitude of the
alternating-current voltage wave in the output is 0.09 of one per cent of the directcurrent voltage. A schematic diagram of connections is shown in Fig. 1.

The filaments are lighted from a $220 / 12-$ volt transformer, having its low-tension winding insulated for the direct-current voltage to ground. The resistance $R$ regulates the filament temperature. This must be held fairly constant; a material increase in temperature greatly shortens the filament life, while a decrease in temperature increases


Fig. 2. Front View of the Rectifier showing Panel and Controls
the space charge loss in the kenotrons. Protective devices are included so that if the temperature should exceed a certain value the set will be shut down, while if it should decrease below a certain value the operator will be warned by an annunciator.

The plate transformer has a rating of 4,5 kr-a.. the primary winding being designed for $40 \mathrm{kr}-\mathrm{a}$. and the secondary winding for $50 \mathrm{kr}-\mathrm{a}$. The higher secondary rating is aecessitated by the fact that the secondary current contains a direct-current component which does not appear in the primary: The orimary winding is designed to have two oarallel sections per phase. Its rating of $40 \mathrm{kv}-\mathrm{a}$ allows for circulating even harmonics n these sections. The transformer draws about $36 \mathrm{kr}-\mathrm{a}$. from the line.
Since there are six phases supplying the enotrons, the resultant ripple will have a requency six times that of the supply, and will have an amplitude equal to 5.7 oer cent of the direct-current voltage. This ripple is reduced by a double-mesh filter, the first mesh being composed of the leakage nductance of the plate and interphase ransformer and the capacity $C_{1}$, the second mesh being composed of the capacity $C_{2}$ and a reactor $L$, which has an inductance of 12 henries, tuned to 150 cycles by the capacity

The condensers $C_{1}$ and $C_{2}$ are of the paper dielectric type.


Fig. 3. Rear View of the Rectifier showing Filter and Reactor

Fig. 2 shows a front riew of the rectifier. Che meters are a line voltmeter, line wattneter. filament voltmeter, and direct-current mmeter. Below the meters, in the center of the panel, is a relay which protects against
changes in filament voltage If the tilanent voltage drops in a peint where the tubes are likely to overheat, a pair of contacts closes and sounds an annunciator which warns the operator. If the filament whage beomes excessively high, a second pair of comtacts


Fig. 4. Performance Curves of the $30-\mathrm{kw}$. Rectifier on the 15,000-volt Tap


Fig. 5. Side View of the Rectifier showing Transformers and Kenotrons
operates on a contactor to shut down the set. On each side of this relay is an overload relay in the main line. Below the relays are switches in the major circuits and a rheostat for adjusting the filament voltage.
＂The taps on the phate tramsformer are hrought out to a set of sockets in the base of the pansel．＇Yte conneretion to any laje is cosed by moans of a three－point phag．A mechamical interlock is provided so that the operator camnot pull ont the plag to change taps white the power is on．The rectifier is stopped and started by two push buttons shown in the center of the panel． These operate on a contactor in the main line．
loig． 3 shows a rear view of the reetifier． The lo kenotrons are mounted over the plate transformer．six on each side．The
smoothing reactor appears in the foreground with its taming condensers just above it．At the left of the fikment transformer is the inter－ phase transformer．The smoothing condens－ ers are monnted in racks above the reactor．

A side view of the rectifier is shown in Fig．$\overline{5}$ ．A protective switch is provided in cach gate so that the opening of either gate shuts down the set．The set cannot be started again until the gate is closed and the start button is pusherl．

The performance curves of the rectifier are illustrated in Fig．\＆

# Charles A．Coffin Foundation 

By W．W．Trench<br>Assistant Secretary，General Electric Company


#### Abstract

In our January issue we made the original announcement of the Coffin Foundation．Mr．Trench， recently appointed Secretary of the Charles $\Lambda$ ．Coffin Foundation，now tells more about the intent of the awards and gives further details concerning certain phases of the Foundation．－Editor．


The Schenectady newspapers recently told the story of a man who had lately been awarded the Distinguished Service Cross for service performed by him while in the front line trenches during the World War．He crawled out under fire into No Man＇s Land and brought to the safety of the American lines a wounded corporal．While performing this arduous and brave task，he was des－ perately wounded．Nothing is so fitting as a reward for couragcous acts of this character， where men go outside their line of duty in order to perform deeds requiring conspicuous courage and fortitude．

The world has never shown quite the same interest in rewards for exceptional devotion to duty in the non－military walks of life，even though there exist such notable prizes as the Nobel Peace Prize and the Carnegie Medals．It is，therefore，of more than ordinary interest that the General Electric Company has created the Charles A．Coffin Foundation for this very purpose－ To reward special achievements which are outside the ordinary line of duty of men and institutions in the electrical industry．The Charles A．Coffin Foundation establishes a monument，living and vital，in honor of the achierements of a man who，during his life， has been and is today above all things a dynamic，vital leader of men．

Mr．Charles A．Coffin who recently retired as Chairman of the Board of Directors of the General Electric Company is himself a wonderful example of a Distinguished Service man，performing his feats in the walks of industry and finance．No problem has seemed too complex for him to solve，no wall of
opposition too mighty for him to surmount； and in overcoming difficulties at every turn， he has found it necessary，in order to promote progress，to do far more than what is ordi－ narily required of a business man．

It is noticeable that the first provision is for the distribution of the income of the Charles A．Coffin Foundation to employees who make the most signal contributions toward the increase of efficiency or progress in the electrical art．The whole spirit pervading the Foundation is this spirit of progress brought about by exceptional efforts outside the line of duty．

As is the case with all prizes where a few men are picked from a large group for special awards，the administration of the Charles A．Coffin Foundation presents many difficul－ ties．There are many men and women in an organization of over 70,000 ，such as the General Electric Company，who are from day to day and from week to week performing extraordinary deeds and making startling inventions or suggestions resulting in the increase of the Company＇s efficiency and the progress of electrical art．One has only to mention a single instance of exceptional service in one department，to have the manager of another department call to mind many parallel instances．Every year the men in the shops of the Company make suggestions for improvement in design of machines and methods of operation，which result in marked progress in the manufacture and greater satisfaction to users of electrical apparatus．

It will be no easy task at the end of this year to choose，from among the best of these
suggestions, the wimner of the special award of a certificate from the Charles A. Coffin Foundation, but there is every reason that the effort should be made to find the men who have made the outstanding achievements and properly honor them.

The first award under the Charles A. Coffin Foundation will not be made among the employees of the Gencral Electric Company. In June, at the ammual convention of the National Electric Light Association, the Charles A. Coffin Medal will be presented to the light and power company in this country which has made distinguished contribution to the development of electric light and power for the convenience of the public and the benefit of the industry.

Intense interest has been shown by leaders in the central station industry in this award and especially in the statement of the factors, which the Committee has announced will be given special consideration. Mr. Frank W. Smith, Chairman of the Charles A. Coffin Prize Committee of the National Electric Light Association, in his interesting letter to the presidents of America's light and power companies, stated that: "Among the factors which will be considered in making the award are the following: The particular initiative, skill and enterprise which have been manifested in popularizing the general use of electrical energy; accomplishments in the development of the efficiency of generation and distribution; the adoption of special plans which have resulted in the largest percentage of increase in new customers; methods adopted of interesting customers in stock ownership; unusual efforts and accomplishments in popularizing and introducing domestic appliances; the extension of service to homes not previously wired and to rural communities."

The Committee has no intention of comparing the standing of various companies but will make its awards purely on the merits of the company's contribution to the progress of the industry.

The real contribution to the electrical industry in the making of the award will undoubtedly come through the emphasis placed by the Foundation on the characteristics of the service rendered by a winning public utility company, which made that company an outstanding leader in the industry.

A similar contribution will be made through competition among the electric railways of the United States for the Charles A. Coffin Medal in the field of electric transportation. What are the accomplishments which should place an electric transportation company in line for this distinguished service award? The

Charles A. Coffin Prize Committer of the American Electric Railway Association, which will decide on the winner of this second medal, has attempted to answer this question in a communication addressed by Mr. C. D). Emmons to electric railway companies within our borders. He states that he and his associates will give special consideration to the following factors:
(1) The particular initiative, skill and enterprise manifested in popularizing electric railway service-more riders and more revenue.
(2) Outstanding success in gaining public good-will.
(3) Economies which have been introduced in operation resulting from original ideas.
(4) Economies in operation viewed as a measure of the extent to which the Company has taken advantage of new developments in operating and maintenance practice and equipment, originating with others.
(5) Improvements in construction practice which have resulted in reduced first cost, reduced maintenance, or greater reliability of service.
(6) Particular success in conducting a safety program and actually reducing the number and seriousness of accidents.
(7) Outstanding accomplishment in development of good relations between management and employees.
(S) Special accomplishment, aside from good management, tending to reduce the cost of new capital.
The encouragement which Mr. Coffin has always given to men engaged in research work has been fittingly remembered by including in the Foundation a provision for a group of Fellowships which will be given to young men desiring to continue research work in the fields of electricity, physics, or physical chemistry. The lure of an immediate paying job to seniors in our colleges and universities takes many a man of great powers in the sphere of research forever out of the realm of research. The Committee of distinguished scientists and educators which is to grant the Fellowships hopes that the Charles A. Coffin Fellorships may save to science in the coming years many valuable men. They feel that eren if only one man of outstanding ability in research work is placed where he can do his best work without worry concerning finances, the Foundation will have more than justified its existence.

# Studies in the Projection of Light 

# PART IV <br> CHARACTERISTIC OF A PARABOLIC MIRROR AND SPHERICAL SOURCE OF LIGHT (Cont'd) 

By Frank benford<br>fobsictar, leluminiting Enginelering Laboratory, General Electric Company


#### Abstract

This mstallment of the series eontinues the subject of lart III in which the characteristic formation of the hean was discussed with reference to the inerease of eentral intensity with distance, the inverse-square region, the testing distance for central intensity, and the width of the crest of the beam. The following discussion includes the width of the beam, the testing distance for width of the beam, the movement of the source, a graphical method for obtaining the characteristics of the beam, and gives 1 wo examples of the enmputation of beam characteristics. Particular attention is called to the charts shown as Figs. 32, 33 and 36 which are very useful in determining the limitations, accuracy, and correction factors for any particular photometric beam test.-Emior.


## Width of Beam

The edge of a searchlight beam is never sharply and definitely outlined, so that in speaking of the beam width it is necessary to define the term "width." As ordinarily constructed a searchlight (or any of its diminutives, the flondlights) has a field of low illumination nearly 180 degrees wide, and it is essential to fix upon some method of distinguishing between the stray light and the beam proper. It is true that with many searchlights, particularly those having carbon arcs, the edge of the beam seen in the air may be sharply defined to the eye, but if we make an attempt actually to measure the beam diameter, say by throwing the beam against a flat target, we find that the sharpness of the edge is largely an illusion. The beam tapers off into the surrounding field of stray light and two observers might have some difficulty in agreeing to within several minutes of arc.

A rule of practice has been adopted by nearly all photometrists, and by use for a number of years has acquired something of the sanctity of age. This rule may bestated: "The width of a projected beam of light is measured between points on a diameter that have an intensity of 10 per cent of the maximum intensity." To this might be added that the diameter is usually but not necessarily horizontal, and that the maximum may or may not be on the axis. This rule sounds rather arbitrary, but experience has shown it to be satisfactory and seldom in serious disagreement with observational data; and, furthermore, in a large number of cases it has been found that beam widths computed from the size of the light source and the mirror dimensions agree with the rule to within the limits of accuracy.

The 10 per cent rule sometimes has the effect of penalizing a searchlight that is kept in sharp focus, and assigning to it a lower light output than would be given with the same searchlight slightly out of focus. As the beam is thrown out of focus the beam expands slowly, but a relatively large change takes place in the central (maximum) intensity. Ten per cent of the reduced maximum carries the cdge out farther than the actual spread, and the additional flux so gained is often a large fraction of the original beam light.

A second "width" is the computed width at a great distance, using either an actual light source or our substitute, the sphere. This is the real maximum beam width and is not to be confused with a spurious maximum obtained at short distance. The third "width" is this width at short range. This latter condition applies to nearly all test conditions, and is therefore of more importance than the limiting width at infinity. This region at comparatively short range which is often, in floodlights particularly, the region of both test and service has some interesting characteristics which will repay investigation.

One of the most confusing features in the discussion of a projected beam of light arises from the inversion that takes place after the light leaves the mirror. The outer rays which form the edge of the beam for some distance from the reflector come from the edge of the reflector, but soon other rays from interior points on the mirror come to the edge of the beam, only to be superseded by light from still more central points, until at infinity the edge rays are from the exact center. It thus happens that the center of the beam at short range is made up in part of the light that will
ultimately be the edge rays, and the edge light close to the mirror becomes the center of the beam at great distances. It is because we are often compelled to test at distances where the final rearrangement of rays is incompletely carried out that attention must be paid to this region of crossing rays. If the searchlight was always to be used at the test


Fig. 28. Crossing Point of Two Rays in a Meridian Plane
range, or if the test could always be made at the working range, there would be little occasion to find the relation between various cross sections of the beam. But different photometric laboratories test at different ranges, and the same unit may be used at ranges varying from 25 to 1000 ft .

Take some point on the mirror, such as $P_{1}$ in Fig. 28, and trace the outer ray to some distance $L_{\ell}$, where the distance from the axis is

$$
\begin{equation*}
\frac{W_{e}}{2}=y_{1}+L_{e} \tan e \tag{55}
\end{equation*}
$$

where $y_{1}$ is the radius of $P_{1}$ and $e$ is the angle between the outer ray and the axis. Also, for any other point $P_{2}$ we can write

$$
\begin{equation*}
\frac{W_{e}}{2}=y_{2}+L_{e} \tan f \tag{56}
\end{equation*}
$$

if we assume that the rays cross at some real point in the beam.

Equating (55) and (56)

$$
\begin{align*}
y_{1}+L_{\epsilon} \tan e & =y_{2}+L_{c} \tan f \\
L & =\frac{y_{2}^{\prime}-y_{1}}{\tan e-\tan f} \tag{57}
\end{align*}
$$

A solution of equation (57) will give the distance to the crossing point of any two rays we choose. If we select two points $P_{1}$ and $P_{2}$ sufficiently close together then the tangents to the spherical source coincide and the intersection of the two rays becomes the image of the common point of tangency. It is permissible to assume that in certain cases at least these image points will be in the absolute boundaries of the beam, originating
as they do from the boundaries of the light source.

We have

$$
\begin{gather*}
y_{1}=2 F \tan \frac{a}{2}  \tag{58}\\
d y_{1}=F \sec ^{2} \frac{a}{2} d a  \tag{59}\\
\tan e=\frac{r}{p_{1}} \\
=\frac{r}{F} \cos ^{2} \frac{a}{2}  \tag{60}\\
d(\tan e)=-\frac{r}{F} \sin \frac{a}{2} \cos \frac{a}{2} d a \tag{61}
\end{gather*}
$$

In the limiting condition when $P_{1}$ and $P_{2}$ are adjacent points

$$
\begin{align*}
L_{e} & =\frac{d y_{1}}{d(\tan e)} \\
& =\frac{F^{2}}{r \sin \frac{a}{2} \cos ^{3} \frac{a}{2}} \text { inches } \tag{62}
\end{align*}
$$

Equation (62) has been plotted in Fig. 29 for a mirror having a focal length of 7.79 in . and a spherical source with a radius of 0.25 in . The ordinates of the curves were computed from equations (55), (58) and (60), giving

$$
\begin{equation*}
\frac{W_{e}}{2}=2 F \tan \frac{a}{2}+L_{e} \frac{r}{F} \cos ^{2} \frac{a}{2} \tag{63}
\end{equation*}
$$

The central point on the mirror gives an image at infinity along the straight line through the origin of co-ordinates. It should be noted that the vertical scale of the curves is 20 times the horizontal scale so that the width of the beam is greatly exaggerated. The image points for $a=20 \mathrm{deg}$. to $a=60 \mathrm{deg}$. are on the upper curve while the image points for $a=60$ deg. to 110 deg. lie on the lower curve as indicated by the plotted dots. As the curve above 60 deg. is within the beam we may call it the imaginary branch. On the left-hand edge of the web two scales are given. One is inches and the other is radii of mirrors having angular openings from 0 to 120 deg. measured from the axis. On account of the compression of the scale in the horizontal direction the curvature of the mirror may be neglected and the mirror surface represented by the straight line used for the base of the stub scale of radii.

A straight line from the radii scale to the same angle on the curve will give the position of the limiting ray from that angle on the mirror. Thus from 60 deg. on the radii scale to 60 deg . on the curve gives the edge of the beam from a $60-$ deg. mirror of focal length
7.79 in . for the first 7.50 in., and the upper section of curve gives the remainder of the beam boundary The beam from a 90 -deg. mirror of the same focal length has a straght initial section 790 in. long and from there on the beam edges are identical with the previous mirror. A 120 -deg. mirror has first

The half width of the beam from the center of the mirror is

$$
\begin{equation*}
\frac{W_{0}}{2}=L_{e} \stackrel{r}{F} \tag{64}
\end{equation*}
$$

The excess linear width $E$ at any finite distance, expressed as a fraction of the linear


Fig. 29. Boundaries of Beam from a Parabolic Mirror ( $F=7.79$ in., $r=0.25 \mathrm{in}$. rad.) The outer curves are asymtotic to the beam boundaries at infinity. The inner curves are asymtotic to the boundaries of the inverse-square region width of the beam from the center, is from cquations (63) and (64):

$$
E=\frac{\frac{W_{e}}{2}-\frac{W_{0}}{2}}{\frac{W_{0}}{2}}=
$$

$$
\frac{12 F \tan \frac{a}{2}+L_{e} \frac{r}{F} \cos ^{2} \frac{a}{2}-L_{e} \frac{r}{F}}{L_{e} \frac{r}{F}}=
$$

$$
2 \sin ^{2} \frac{a}{2} \cos ^{2} \frac{a}{2}-\sin ^{2} \frac{a}{2}
$$

or

$$
\begin{equation*}
E=\sin ^{2} \frac{a}{2} \cos a \tag{65}
\end{equation*}
$$

a straight section 1050 in . long and thereafter the beam is identical with the other two. It is to be noted that above 60 deg . there is a sharp turn in the edge of the beam where the initial straight side crosses the upper branch of the curve. Below 60 deg. the straight line is tangent to the boundary curve at the point of contact and the sharp turn is missing.

The standard searchlight mirror, which has an opening angle $a$ of 60 deg., gives a beam with but little resemblance to an hourglass, and it will be shown later that in this respect the spherical source differs greatly from the disk source which will be taken to represent an arc crater.

The cusp in the curve of images where the two branches of the curve meet is always formed from the $60-\mathrm{deg}$. point on the mirror regardless of the value of $F$ or $r$. The position in space of the cusp does, however, vary with both $F$ and $r$, increasing in distance $L_{e}$ from the mirror as the square of $F$, and inversely as $r$. It is thus evident that the data points on the real and imaginary branches of the boundary in Fig. 29 can be directly applied only to the particular case for which they were computed.

With the information given by the plot of equations (62) and (63) we are now in position to find how any section of beam differs in angular width from adjoining sections or from the limiting width at infinity.

This expression for the excess width shows that the excess is a function of the angle $a$, but the particular distance $L_{e}$ and half width $\frac{W_{e}}{2}$ at which the points lie is also a function of $F$ and $r$. Thus if it is decided that an error (or correction factor) of one per cent in measurements of beam width is allowable, taking the angular width at infinity as the


Fig. 30. Excess Width of Beam from a Parabolic Mirror ( $F=7.79$ in., $r=0.25 \mathrm{in}$. rad.). This width is the excess over the width of the beam from the central part of the mirror
standard, then we can, by trial, solve equation (65) and find $a=11$ deg. 36 min .; and from equation (62) this excess of one per cent in width occurs at 2430 in . or 202 ft .

The numerical value of $E$ is positive for all value of $a$ under 90 deg., at which angle the
maginary branch of the boundary curve rosses the central beam; and beyond 90 deg. he value is negative, so that without having een the curves of Fig. 29 it would be evident hat not all values of $E$ obtained from quation (65) are real.
The excess widths of beams rom three mirrors of focal length .79 in ., having angles of 60,90 , nd 120 deg. are plotted in 'ig. 30. The sharp turn where he straight lines join the comnon curved line marks the juncion of the initial straight ray rith the curred edge of the eam. The sharp upturn at 000 in. shows that only a few eet in that region may take us rom a suitable condition to one hat is not satisfactory for accuate testing.
The imaginary branch of the urve approaches the boundary of the inverse-square region in he same way that the real ranch approaches the outer imiting rays.

## Cesting Distance for Width of Beam

It has been mentioned that for test purposes $t$ is often better to have the data expressed n terms of beam width rather than in the inear dimensions of the filament. There is a eeming contradiction in this, for it has just


Fig. 31. Excess Beam Width from a Parabolic Mirror as a Function of Mirror Angle a
seen demonstrated that the mathematical expression for the edge of the beam is rather omplicated, being given in two parts as a unction of the mirror angle, and the exoression is discontinuous where the edge ray oins the curved boundary. It will be recalled
that the expression for the excess wilth came out as a very simple function of the mirror angle and this suggests that for wating purposes a chart showing the relation of the measured beam width to the excess width will be the simplest to use.


Fig. 32. Charts of Observed and Real Width of Beam from a Parabolic Mirror with a Spherical Light Source

The first step is to replace $r$ and the first power of $F$ in equation (62) by the observed angular width $C$.

$$
\begin{equation*}
L_{e}=\frac{114.6}{C \sin \frac{a}{2} \cos ^{3} \frac{a}{2}} F \tag{66}
\end{equation*}
$$

This equation used in connection with equation ( 65 ) has been used to plot the curves of Fig. 32, where the observed width $\mathrm{I}^{\prime \prime}$, the limiting width $W^{+}$and the excess width $E$ are in the relation

$$
\begin{equation*}
I^{\prime}=\frac{I^{\prime \prime}}{1+E} \tag{67}
\end{equation*}
$$

As an example take a beam of observed angular width of 2 deg. at a test range of 300 times the focal length of the mirror. The chart indicates that the observed width is about 4 per cent greater than the real width and either a greater test distance must be used or the observed width may be reduced by the factor 1.04 . If it is desired to have the direct test data correct to within one per cent, the range required is 575 focal lengths; while if an error of ten per cent is not objectionable only 19.5 focal lengths is required. The latter condition leads to one dangerous possibility and that is the probable existence of an edge ray from the mirror forming the initial straight side of the beam at and beyond the 19.5 focal-length point.

Equation (57) save the range $L$ of the crossing point of two ratys reflected from the mirror at radii $y_{1}$ and $y_{2}$. If we make $y_{1}$ equal to zero, that is the center of the mirror, and $y_{2}$ equal to the radius of the mirror, then the crossing point will be that of the central cone



Fig. 33. Minimum Safe Testing Distance for a Beam from a Parabolic Mirror of Angle a. The otserved width at this distance may be corrected by the reduction factor given in Fig. 32
of rays and the outer cone of rays as point $B$, Fig. 32. This is beyond the junction of the outer ray with the curved edge marked $A$ in Fig. 32, and therefore point $B$ marks a perfectly safe distance for both testing and computing. This point avoids by a considerable margin the sharply upturned branch of the excess-width curves, Fig. 30, that exist for mirrors having an angle a greater than 60 deg. It is hardly necessary to consider mirror angles of much less than 60 deg. because of their rarity, and also because their curve of excess width coincides closely with that of the 60 -deg. mirror except for distances quite close to the cusp point in the edge curve.

The luminous area of Fig. 25* shows that at a range of 145 ft . the edge of the beam was composed of light from both the center and edge and from an irregular area between. The observed beam width was slightly over 3 deg. and the test range was 220 ft . According to Fig. 32 the observed width was three per cent high. The luminous spot on the left side of Fig. 2.5* was due to an optical error in the front surface of the mirror which

[^22]caused it to seatter the five per cent of light reflected from this surface.

Equation (57) transformed to fit these conditions becomes

$$
L_{1}=\frac{y}{\tan e-\tan f}
$$

and using cquations (58) and (60) to reduce it further, it becomes

$$
\begin{equation*}
L=\frac{4 F^{2}}{r \sin a} \tag{68}
\end{equation*}
$$

Replacing $r$ and the first power of $F$ by the limiting angle (o we have

$$
\begin{equation*}
L=\frac{45 S}{C_{0} \sin a} F \tag{69}
\end{equation*}
$$

To use Fig. 33, which is constructed from equation (69), the observed width of beam is first reduced to the real width $W$ (or in degrees $C_{0}$ ) and with this figure the value of $L$ is found from the plotted curves of Fig. 30. If $L_{e}$ is equal to or greater than $L$ as found from Fig. 33, then the readings on that chart are correct and are not in error through the crossing of an edge ray beyond the test point.

As an example of the use of the two charts in combination, take the case of a mirror of 2.60 in. focal length tested for beam width at 50 ft . radius. The observed beam width is two degrees and the mirror angle is 120 deg. The test distance is 230 focal-lengths and the reduction factor (from Fig. 32) is 1.07 . The


Fig. 34. Diagram Showing the Maximum Distance a Spherical Source can be Axially Displaced without Diminishing the Central Intensity from Mirror $A$. Under these condi tions, Mirrors $B$ and $C$ reflect light to the center of the beam from only the areas bounded by the angle $a$
true beam width is therefore 1.87 deg. Looking up in Fig. 33 a beam width of 1.87 deg. from a $120-d e g$. mirror we find an indicated test distance of 290 focal-lengths or (i:) ft . Therefore the radius of 50 ft . is too
hort for measuring the beam width and ther a greater distance should be used, or ae width should be carefully investigated in ome other way

## lovement of Sourco

It is common practice in the use of inandescent floodlights to move the light purce along the axis from the focal point, nd by thus putting the lamp out of focus the eam is broadened, with a corresponding loss 1 central intensity. If the spreading of the ght is carried too far the center of the beam ill become dark. There will alwass be some ght in the center, but by contrast with the arrounding light it may appear perfectly lack. A beam that stops just short of the lack center is usually soft in outline and free om filament images. Aside from this very ractical feature there is another reason for eing interested in the distribution of light s the lamp is moved. It is possible to move te lamp for some littic distance from the sact focal position without changing the entral intensity, and photometric measureents taken on the axis are thus not a good uide for adjusting the lamp.
There is one case in which we may often e justified in establishing the approximate cal position by means of axial photometric eadings, and that is when testing solely for entral beam intensity. If the mirror is a fair pproximation to the correct shape, and the esting distance is at least the distance $L_{0}$ to oe normal inverse-square region, then the aximum reading obtained may be accepted sthe true central intensity. The smaller mictal eflectors are apt to have zones where the arvature departs markedly from the proper rm, and several of these zones might oncentrate light on a nearby point on the xis but not do it at service distances. 'herefore, the test distance should be at least qual to $L_{0}$, and it seems fair to assume that ny intensity read at that distance can be uplicated at all greater distances.
In Fig. 34 a spherical source is shown moved ther way along the common axis of three hirrors of equal diameter. The beam from re 60 -deg. mirror with the source at $\Omega_{2}$ will aintain its full central intensity at all istances greatly in excess of $L_{0}$ : that is, at istances great enough so that a small angle f convergence will cause the rays to converge in the axis. This follows because the source onceals the focal point from all points on the nirror, and therefore the focal position ppears to be luminous from all points of view. he same is true when the source is at $O_{1}$, for
then a line may be drawn from the somree through the focal peint to every part of the mirror. The "freedom of movement" is therefore

$$
\begin{equation*}
n= \pm \frac{r}{\sin a} \tag{70}
\end{equation*}
$$

or 1.15 F for this 60 d -deg. mirror.
If the mirror extends to 90 dag. the freedom is limited to
$n= \pm r$


Fig. 35. Curves Showing the Effect of Movement of Light Source on the Spread of the Beam from a Floodlight of Proportions Similar to Those of Mirror $C$ in Fig. 34; Curve $A$, with the Light Source at $F$; and Curve $B$, with the Source at $0_{1}$
and the same limit holds for all mirror angles greater than 90 deg. One result of the relation shown by equation (70) is that a shallow mirror is easier to focus for maximum central intensity than is a deep mirror. With the source in either position shown in Fig. 34 the 60 -deg. mirror will give full beam intensity on the axis, the 90 -deg. mirror will give 33 per cent full intensity and the 120-deg. mirror will give only 11 per cent. The active zone for axis illumination is confined to the zone within 60 deg. of the axis, and this zone covers the forconing percentages of the entire projected mirror area.

The two characteristic curves of Fig. 35 illustrate how the beam intensity changes as the light source is moved away from the mirror. The beam width changed from 11 to 21 deg. while the central intensity dropped to 2.3 per cent of its original value. The angle of the marror was nearly 120 deg., the focal length was: in., and the radius of the source was about 0.2.) in

When the source is moved along the axis the rayc from the nuter zune of the mirror
are diverged farthest from their normal path, and they may finally become the edge rays for the entire length of the beam. As has been demonstrated the central point of the mirror gives the edge rays at infinity when the source is in focus. As the source is moved either way from the focus, other zones give off the limiting rays and the beam begins to lose its habit of turning inside out between the mirror and infinity.

The edge rays, with the source out of focus, but still on the axis, may be traced with the aid of the method used to derive equation (62). It is first necessary to find how the angle $\varepsilon$ is influenced by the position of the source. The maximum value of $e$ is not much over ten degrees in any unit that is really projecting light in the ordinary sense of the word. A total beam width of say 30 deg. ( $e=15$ deg.) places the unit in the class of indoor lighting fixtures that may be tested and used at short range, and only in special cases can it be treated as a projector. With this limit in mind the mathematics of the out-of-focus beam may be simplified without a serious loss of accuracy. In Fig. 36 the source is shown moved a distance $S$ toward the reflector. The angle $e$ may be approximated by

$$
\begin{equation*}
\tan e=\frac{T+r_{1}}{p} \tag{72}
\end{equation*}
$$

in which equation

$$
\begin{align*}
& T=S \sin a  \tag{73}\\
& r_{1}=r \frac{p+S \cos a}{p} \tag{74}
\end{align*}
$$

therefore

$$
\begin{gathered}
\tan e=\frac{S}{p} \sin a+\frac{r}{p}+\frac{r S}{p^{2}} \cos a= \\
\frac{S}{F} \sin a \cos ^{2} \frac{a}{2}+\frac{r}{F} \cos ^{2} \frac{a}{2} \mp \frac{r S}{F^{2}} \cos a \cos ^{4}-\frac{a}{2}(75)
\end{gathered}
$$

The edge of the beam was seen to be composed of a series of image points formed by adjacent rays in a meridian plane. The method of deriving equation (62) should therefore apply when the source is out of focus.

$$
\begin{gather*}
L_{e}=\frac{d y}{d(\tan e)} \\
=\frac{F^{2} \sec ^{3} \frac{a}{2}}{S \cos \frac{3 a}{2}+r \sin \frac{a}{2} \pm \frac{r S}{2 F} \sin a \cos \frac{a}{2}(1+3 \cos a)}
\end{gather*}
$$

As we are interested only in the beam width at great distance, we may write

$$
\begin{equation*}
L_{e}=\text { infinity } \tag{77}
\end{equation*}
$$

which in equation ( 76 ) is true only when $a=180$ deg. (which is not a practical limit of mirror construction) or when the denominator is equal to zero.

Therefore, aftuer simplifying by changing several factors from functions of $\frac{a}{2}$ into functions of $a$ and dividing by $\sin a$, we get

$$
\begin{equation*}
S=\frac{-r \sin \frac{a}{2}}{\cos \frac{3 a}{2} \frac{\mp r}{2 F} \sin a \cos \frac{a}{2}(1+3 \cos a)} \tag{78}
\end{equation*}
$$

This equation is plotted in Fig. 36 where the focal length was taken as unity and $r$ was made equal to one-tenth, which is about the proportions of the $120-\mathrm{deg}$. mirror with a halfinch diameter source used in several previous illustrations. The two lower branches show what angle on the mirror gives the ray of maximum divergence for various positions of the light source. The branch to the left is for positions between the focal point and the mirror. Thus the 0.2 focal-length position of the source gives a maximum spread of light from the $50-\mathrm{deg}$. zone on the mirror. A position 0.2 focal lengths bevond the focal point has a higher zone for the ray of maximum spread.

It will be noted in the illustration that the ray of maximum spread never comes from points beyond 60 deg. on the mirror. This indicated that if the mirror angle is over 60 deg . there is always a curved edge to the beam; whereas if the mirror is say 40 deg. wide (equal to angle a) and this particular source is set either 0.14 focal lengths ahead or 0.22 focal lengths back of the focus the beam edge rays at the mirror edge will continue to be edge rays to infinity.

The two upper curves of Fig. 36 are minimum divergences for rays from the periphery of the light source, and these curves therefore are related to the imaginary branch of the locus of edge points with the beam in focus; they locate the zone that gives the inner rays of the hollow beam. Once the proper mirror zone is determined, the computation of angle $e$ is easily carried out.

It has been found in the actual application of the out-of-focus beam that better results are obtained with the lamp moved away from the mirror. The central part of the mirror concentrates its light a little better into the
center of the beam and for equal spreads the center of the beam is stronger. This makes the beam more uniform particularly when it is spread to the point when the center shows signs of becoming dark.

One feature of the spread beam that is of engincering importance is the higher output of a floodlight when the beam is out of focus,


Fig. 36. The Solid Curves Show the Mirror Zones that Give the Maximum Spread of Light from Parabolic Mirror Having a Spherical Source of Radius 0.1, the Mirror Focal Length Displaced Out of Focus Axially. If the center of the beam is dark under these conditions, the dotted curves show the mirror zone that gives the inner boundary of the hollow beam
even if the lamp is moved away, so that less light falls upon the mirror. Thus in Fig. 35 the in-focus beam contained 1930 lumens and when the lamp was moved forward the beam lumens rose to 2090 lumens. The explanation of this parador is found in the stray light between 5.5 and 10.5 deg. that was not included in the concentrated beam. The ten per cent rule is evidently involved in this difference between 1930 and 2090 lumens, for with the integration of light carried to the same upper limits for both beams they should reverse their relative efficiencies.

Another feature of the spread beam is the false value that may be placed on a defective mirror that gains in beam width through surface defects. Unless the added width is kept in mind the mirror may be improperly credited with a higher coefficient than a mirror of good curvature.

## A Graphical Method of Obtaining the Beam Characteristics

It will be recalled that of the several features of the beam that have been investi-

[^23]gated and charted, only one the incerease of central intensity with distance, has been completely covered. The theory of the edge rays, which is in some ways complete, doos not take into accomant the ten per eent rule used in photometry, and the subject of the inverse-square region was left unfinisherd with the promise of future attention. (Of the region between the inverse-square region and the edge, the theories so far developed say nothing. The good and sufficient reason for this omission is that this intermediate region cannot be investigated by considering only what happens in a meridian plane, but we must have recourse to solid geometry. The aththor has started several times to carry out an investigation of this intermediate region, but the mathematical forms encountered at the very beginning left but little hope of an ultimate simplification that would allow an easy application to practice.* The desire for data was prompted by practical needs and a simple solution was therefore desired.

As contrasted to the strictly geometrical solution the optical solution here given is extremely simple and direct, and in its applicability is undoubtedly more general particularly to the special cases of odd shaped sources or defective mirrors.

The image formed by a parabolic mirror is at infinity, but as has been pointed out the image is rather a multiplicity of images of various sizes than a simple image that duplicates the outline of the source. We can build up the composite image by dividing the mirror into a number of concentric zones and then determining separately the image given by each zone. The method is perfectly general and may be applied to any source in focus or out of focus. A summation of the images gives the beam from the entire mirror area. There are only a few equations needed. One is the equation for the plane area of the zones:

$$
\begin{equation*}
A=4 \pi F^{2}\left(\tan ^{2} \frac{n}{2}-\tan ^{2} \frac{m}{2}\right) \text { sq. in } \tag{79}
\end{equation*}
$$

where $F$ is the focal length in inches,
$n$ is the angle to the outer edge of the zone,
$m$ is the angle to the inner edge of the zone, and
$A$ is the plane or projected area of the zone.
The angular size of the image from the zone is determined by the size of the source (radius $=r$ ) and the distance $p$ from the focal point to the center of the zone. We may take an average angle:

$$
\begin{equation*}
a=\frac{n+m}{2} \operatorname{deg} . \tag{.0}
\end{equation*}
$$

as representing the eenter of the zone＇The angular radius b of the image is then obtained from

$$
\begin{align*}
\text { lall } b & =\frac{\prime}{P} \\
& =\frac{\cos ^{2}}{\mu} \quad{ }^{a}  \tag{N}\\
& \text { numberic }
\end{align*}
$$

In seleeting the zones it is well to keep in mind the progressively increasing size of the zones as the angle a（or $n$ and $m$ ）is increased The values in Table 11 are for 10 －des．zones up）to 120 deg．from the axis．

TAELE 11

## ZONE AREAS AND IMAGE WIDTHS

Unity Focal Length and Spherical Light Source of Radius $r=\begin{gathered}F \\ 100\end{gathered}$

| ZONE BOUNDARIES |  | Mid．Zone a | Projecied area |  | Rastius $P$ | image radius |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| From | To |  | Zone | Total |  | Degrees | Per Cent |
| $1)^{\circ}$ | $10^{\circ}$ | $6^{\circ} 40^{\prime}$ | 0．096 | 0．090； | 100.1 | $0^{\circ} 31.25^{\prime}$ | 9\％．6 |
| $10^{\circ}$ | $20^{\circ}$ | $15^{\circ}$ | 0.29 .5 | 0.391 | 1.018 | $10^{\circ} 33: 3.7!9^{\prime}$ | 918． |
| $20^{\circ}$ | $30^{\circ}$ | $25^{\circ}$ | 0.512 | （0．90．3 | $1.0+9$ | $0^{\circ} 332.73^{\prime}$ | （1）．3 |
| $30^{\circ}$ | $40^{\circ}$ | $35^{\circ}$ | 0.760 | 1.665 | 1.100 | $0^{\circ} 31.25^{\prime}$ | 90.9 |
| $40^{\circ}$ | $50^{\circ}$ | $45^{\circ}$ | 1.064 | 2.729 | 1.172 | $0^{\circ}$ 29．3．34＇ | 8．5．3 |
| $50^{\circ}$ | $60^{\circ}$ | $55^{\circ}$ | 1.455 | 4.184 | 1.271 | $00^{\circ} 27.04{ }^{\circ}$ | 78.7 |
| $60^{\circ}$ | $70^{\circ}$ | $65^{\circ}$ | 1．972 | （2．1．59 | 1．40．5 | $00^{\circ} 2+.4{ }^{-1}$ | 71.1 |
| $70^{\circ}$ | $80^{\circ}$ | $75^{\circ}$ | 2.697 | 8.853 | 1.588 | $0^{\circ} 31.65{ }^{\prime}$ | 62.9 |
| $80^{\circ}$ | $90^{\circ}$ | $85^{\circ}$ | 3.713 | 12.566 | 1.839 | $0^{\circ} 18.70^{\prime}$ | S． 4.4 |
| $90^{\circ}$ | $100^{\circ}$ | $95^{\circ}$ | 5.290 | 17.856 | 2.189 | $0^{\circ} 15.71^{\prime}$ | 4.5 .7 |
| $100^{\circ}$ | $110^{\circ}$ | $105^{\circ}$ | 7.794 | 25.650 | 2.699 | $0^{\circ} 12.74^{\prime}$ | 37.0 |
| $110^{\circ}$ | $120^{\circ}$ | $115^{\circ}$ | 12.045 | 37.695 | 3.461 | $0^{\circ} 9.93^{\prime}$ | 2S： |

part hams are compared with the beam from 11 we 120－deg．mirror it will be seen that the onter zones，on account of their greater area， are of prime importance．

If three mirrors of equal radius＇and variable angular widths，such as 60,90 and 120 deg．，are investigaterl，it will be found that they give，as plotted in Fig．38：
（a）Equal central intensitics（cqual areas）
（h）Widest beam from 60－deg．mirror．


Fig．37．Synthetic Method of Arriving at the Distribution of Light in a Beam by Adding the Light from the Different Angular Zones of the Mirror

These data are plotted in Fig．37．The width of the beam from the 0 to 10 －deg． zone is taken as twice 0 deg． 34.25 min ．，and the intensity of the beam is plotted as proportional to the area of the zone．This implies a light source of one candle per square inch brilliancy and a mirror of perfect reflectivity．The image from the second zone， 10 to 20 deg．，is slightly narrower and about four times as intense．The zone images are plotted one on top of another until the 110 －to 120 －deg．zone is added． The resultant figure is a pile of rectangles that must be merged into one another，which we may readily do by drawing a smooth curve through the centers of the vertical steps． This smoothing out could be eliminated by taking small steps，say 1－deg．zones on the mirror，but nothing would be gained thereby．

In Fig． 37 heavy lines are drawn across the beam characteristic denoting the tops of beams from a $60-$ deg．mirror and a $90-$ deg． mirror of equal focal lengths．When these
（c）Narrowest beam from 120－deg．mirror．
（d）Narrowest inverse－square region（flat crest）for $90-\mathrm{deg}$ ．mirror and
（e）Equal width of inverse－square region for $60-$ and $120-\mathrm{deg}$ ．mirrors．

## Computation of Beam Characteristic

Perhaps the first thing to mention in connection with the computation of the beam characteristic is that it applies only to the beam at great distances，and thus gives data that are too often not attainable by test methods．If all tests could be conducted at a range of say 1000 or even 2000 times the focal length of the mirror，then the graphical method just outlined and the geometrical method about to be described would be ideal for checking or even eliminating the actual test work．

This section is placed after the section on a graphical determination of the beam charac－ teristic because the diagrams used to illustrate the methods are the same．

Taking again the mirror with a focal length of unity and a spherical light source of radtius 0.01 , the angular width of the beam is $C$ degrees; $C$ being obtained from the relation

$$
\tan C=\frac{2 r}{F} \text { numeric }
$$

or replacing $\tan C$ by the angle $C$, the half width

Fig. 38. These Curves, Derived from Fig. 37, Show that Three Mirrors of Equal Diameter and Having Angles a Equal to 60,90 and 120 Deg. Give Beams of Equal Central Intensity but Unequal Width

In Fig. 37 this is the point on the characteristic curve where it crosses the axis at zero intensity. At some other point such as ( $C^{\prime}, I$ ) at the top of the $50-$ to $60-$ deg. image, Fig. 37 , the angular half width corresponds to the spread of light reflected from the 60 -deg. point on the mirror. The angle varies inversely as the radius vector $p$, therefore $F$ in equation (83) is replaced by $p$ and

$$
\begin{align*}
& \frac{C^{\prime}}{2}=\frac{57.2 s r}{p} \text { degrees } \\
& =\frac{57.2 s r \cos ^{2} \frac{a}{2}}{F} \text { degrees. } \tag{84}
\end{align*}
$$

The summation of images in Fig. 37 is based on the fact that at sufficient distances the luminous area of the mirror grows in concentric rings from the center outward

[^24]as the wherver moses from the edper of ther beam oward the center The luminous ateat up 10 a degrees is then
\[

$$
\begin{aligned}
\mathrm{A} & =\pi y^{\prime 2} \\
& \left.=4 \pi F^{2} \tan ^{2} \frac{a}{2} \text { square inches } \quad \text { (x.i) }\right)
\end{aligned}
$$
\]

The intensity of light is

$$
\begin{align*}
I & =A B k \\
& =4 \pi B F^{2} k \tan ^{2} \frac{a}{2} \text { canclles } \tag{86}
\end{align*}
$$

Equations ( 8.5 ) and ( N (i) give the characteristic curve of beam intensities of a parabolic mirror and a spherical light source. The brilliancy of the source is one candle per square inch and the coefficient of reflection $k$ is taken as unity in Fig $3 \overline{7}$.

## Testing Distance for Entire Characterist:c

Attention is called to the different manners in which $L$ and $L_{0}$ vary with the angular proportions of the mirror. In Fig. 22* three beams were sketched for the same spherical source with three mirrors of equal diameter but variable angle $a$. The $60-$ deg. mirror requires a "safe" distance $L$ several times $L_{0}$; the 90 -deg. mirror can be measured for beam width at about one and one-third the distance $L_{0}$ necessary for measuring full central intensity; while the beam from the $120-\mathrm{deg}$. mirror can be measured for width at one-third the distance $L_{0}$. It is therefore necessary to investigate each characteristic separately.

The indoor searchlight range of the Illuminating Engineering Laboratory $\dagger$ has a usable length of 150 ft . The measurements of beam flux are made by throwing the beam into a hemispherical photometer 110 in . in diameter. At a distance of 1.50 ft . the hemisphere subtends an angle of 3 deg. 30 min . Smaller angles are obtained by partially closing the iris shutter with which the instrument is provided, and larger angles are obtained by moving the integrator down the track closer to the projector under test. This test equipment is an excellent example of the physical limitations encountered in photometry, and the application of the formulas and charts so far derived for these conditions will show how the theories apply to practice.

Take the case of a floodlight with a diameter of 16 in . and a focal length of 3 in . The lamp filament (the filament of Fig. 39b) is 0.5 in . in average diameter. This unit is provided with a convex glass door of low optical aecuracy:

The computed beam width is 9 deg. 30 min .
The observed beam width is 11 deg. 0 min .

A how optical aconaty for the mait is indieated we the difference between! dege Bo min. and 11 deg. and we may regard the beam ats being 10 deg. wide. This will give us a certain factor of salfor beranse the condition for testing a 10 -heg. beam is momally harder to satisfy than that for an 11-cleg. beam.

Distance to inverse-squatre region by edpattion (1.5) $L_{0}=22 \mathrm{ft}$.

Available distance, $1.50 \mathrm{ft}=L=\left(6 . \mathrm{s} L_{-0}\right.$.
The acouracy of measurement for the width of the inverse-square region is by equation ( $\bar{\sigma}$ ) equal to (0.s.), which seems ample for a low-accuracy unit.

The integrator is set at 52.7 ft . to measure a beam of 10 deg . observed width. This is
macy miren of 7.79 in. focal length is ('puipper with the same lamp) and a precision tower.

The computed beam width is: deg. 41 min. The observed beam width is? deg. tim min. An optical aceuracy of mirror and door levend the limits of the test is indicated.

Distance to inverse-spuare region by equa$1 \mathrm{i}, \mathrm{m}(\mathrm{I}, \mathrm{j}) L_{10}=: 3 \mathrm{fl}$.

Tvailable distance $150 \mathrm{ft} .=L=5 L_{0}$.
Aceuracy of measurement of width of the inverse-sefuare region is $0 . s(0$, which is low for this unit.

The integrator is set at 140 ft . to measure a $3-\mathrm{deg}$. 4.j-min. beam. This is 216 focal lengths. From Fig. 32 an accuracy of width of about two per cent may be expected, which is


Fig. 39. Analysis of the Projection Characteristics of Various Type of Filaments
(a) When the axis of the helix of this filament coincides with the axis of the mirror the beam practically duplicates a spherical source beam
(b) This filament gives a beam greatly resembling that from a spherical source
(c) This filament has almost as good characteristics as that in (b)
(d) The concentration of this filament is only slightly inferior to that of (c)
(e) A filament with as great a spread as this is practically useless for projection purposes

210 focal lengths for this mirror. The curves of Fig. 32 show an accuracy better than one per cent for these conditions, which is more than ample. We may therefore conclude that the dimensions of the indoor range and equipment are sufficient for this unit. If the beam is spread the test conditions are less severe, except for $L_{0}$ which increases if the lamp is displaced toward the mirror.

As a second example, let us investigate the conditions when an $18-\mathrm{in}$. high-accu-
satisfactory. From Fig. 33 a $3-\mathrm{deg}$. 45 -min. beam from a 60 -deg. mirror required 150 focal lengths hence the distance is beyond the straight edge of the beam.

The above data show the conditions to be ample for the determination of maximum intensity and beam width, but it leaves something to be desired in measurements on the shoulders of the beam characteristic which is in that region that for short ranges remains unexplored.

# The Agricultural and Industrial Features of Priest Rapids 

# THE LARGEST POSSIBLE HYDRO-ELECTRIC DEVELOPMENT IN THE UNITED STATES WEST OF NIAGARA FALLS 

By Henry J. Pierce<br>President, Washington Irrigation and Development Company, 71 Broadway, New York City

The author shows the vast possibilities for increased agricultural and industrial enterprises if the largest hydro-electric project in the West is developed. This single development when completed will make an appreciable difference in our national wealth.-Editor.

## The Land

When the pioneers of $1 \$ 40$ travelled toward the Pacific Northwest, some of them remained in the fertile wooded country of Eastern Washington, while others pushed further west and, leaving behind what they deemed a vast useless desert traversed by the Columbia River, crossed the Cascade Mountains and settled in "the American Riviera" lying between the mountains and the ocean.

For the most part, the great Columbia River Valley or, as it is coming to be called, "The Priest Rapids Valley" is in the same primitive condition as when the pioneers crossed it in 1840. Its hundreds of thousands of acres, having but four inches of rain per year, constitute a desert sage brush country, the greater part having a population of less than one person per square mile.

But this vast unproductive area of land, when given water, will become one of the richest agricultural districts in the world. The volcanic ash soil is a veritable treasure in its content of fertilizing material. Given water, it will produce, with its 300 days of sunshine, every crop that can be grown in the temperate zone, such as sugar beets, tobacco, peanuts, soy beans, sweet potatoes, every kind of vegetable, and flax, barley, rye and wheat give wonderfully abundant crops. Corn grows nine feet high. Even Egyptian cotton planted in April comes to full fruition by September. A few green oases already glisten in this desert. Twenty thousand acres planted to apples at Wenatchee yield an annual crop of $\$ 10,000,000$ or over $\$ 500$ per acre, but hundreds of thousands of equally fertile, but now thirsty acres remain to be reclaimed from the desert with water from the mighty Columbia which washes their shores. What a marvelous combination! Water, 300 days of sunshine, and in the rushing rapids of the river latent horse power waiting to be harnessed to lift the water to
the parched land. Water, land, sunshine and power with resultant crops four times as great as is obtained from lands which are copiously watered by rain.

## The Location

As shown by the map on page 292, Priest Rapids is situated almost exactly in the center of the State of Washington. The four principal cities of the Pacific NorthwestPortland, Seattle, Tacoma and Spokanehaving an aggregate population of 800,000 , are each about 150 miles distant. Priest Rapids is located upon the Chicago, Milwaukee \& St. Paul Railroad and with the completion of the projected Wenatchee Southern Railroad will have connection within 60 miles to the North and South with four transcontinental railroads-the Union Pacific, Northern Pacific, Great Northern, and Chicago, Milwaukee \& St. Paul.

## The River

The Columbia, twelfth largest river in the world, second largest in the United States, carries a greater annual volume of water than the Mississippi at Memphis. Its drainage area above Priest Rapids is estimated at 95,000 square miles. The river is navigable from the Pacific Ocean to the foot of Priest Rapids. With the installation of locks and a dam at Priest Rapids, navigation will be extended for a further distance of 130 miles into the interior of the State of Washington, to within 110 miles of the Canadian Border. The Columbia is now navigable for ocean going vessels for 120 miles from its mouth, and for 1000 -ton river steamers and barges from that point to Priest Rapids. Therefore, with one change of bulk, water transportation can be had to and from Priest Rapids and any port of the world.

The Columbia falls 90 feet in nine miles at Priest Rapids. Its flow during the low-water period in the winter averages 50,000 second-
feet，athd daring the stmmater months somme
 twice flo llow of the Niagara River at Niagara Palls．

## The Water Power

Priest Raphels comstmutes the largest pos－ sible hedro－edeetrie devedopment in the l＇mited States west of Niagara Falls its tolal

Secondary Power
The low－water perion west of the Cascade Mountatins ocebrs in the smmmer，which is the high－water period at Priest Rapids． Therefore，it is proposed to build a trans－ mission line 110 miles long from Priest Rapids to comnere with the already inter－connected lines of the power plants located west of the （：ascades，which supply electric energy to


Fig．1．Map of the Territory Involved in the Priest Rapids Development
ultimate capacity is $650,000 \mathrm{~h} . \mathrm{p} .$, of which $400,000 \mathrm{~h} . \mathrm{p}$. is primary power available every day in the year， $100,000 \mathrm{~h} . \mathrm{p}$ ．is secondary power available during the irrigation season from April to October，and $150,000 \mathrm{~h} . \mathrm{p}$ ．is five months＇secondary power available from May to September inclusive．The dam will be 90 feet high and two miles long－－the largest in the world；longer than the Assouan Dam in Egypt．

Seattle，Tacoma and the western portion of the state，and to transmit 150,000 horse power of Priest Rapids secondary power to make up the summer shortage．Sufficient power can be transmitted to Priest Rapids during the winter from west of the Cascades if made necessary by any unusually low－water stage，whereby to stabilize and always keep uniform Priest Rapids $400,000 \mathrm{~h} . \mathrm{p}$. primary power．Thus two uses are provided，agricultural and
transmission, which will absorb all of the 250,000 secondary horse-power to be developed at Priest Rapids. It is most remarkable that this region should itself furnish use for this immense output of secondary power, while not requiring at the outset the primary power.

## Primary Power

All the problems in connection with the Priest Rapids hydro-electric project have been solved except finding uses for sufficient of the 400,000 primary horse-power to justify the beginning of construction. The secondary power can be sold for irrigation and transmission purposes. The necessary lands and Federal and State permits have been acquired.

## Raw Materials

The owners of the pewer projert what a limestone deposit of which it is cestimated there are ten million tons in sight, averaging 98 per cent pure carbonate of lime. They also own 600 acres of high-grade alumina clay which contains 40 per cent alumina and but a small percentage of impurities other than silica. Coal, high-grade iron ore and coke of good metallurgical quality can be delivered at Priest Rapids at a reasonable price. Ninety per cent of the three billion tons of high-grade phosphate rock estimated to exist in the United States is within the states of Idaho, Montana and Wyoming.

Natural gas wells of considerable capacity have been drilled 20 miles from Priest Rapids.


Fig. 2. Foaming Waters of the Columbia River at Whole Chute, Priest Rapids, Washington

The foundations for the dam have been tested and found satisfactory. The engineering plans have been practically completed. and financing has been arranged for. Construction will be begun immediately upon use being found for the primary power. A certain amount of power can be sold for public utility purposes. The railroads will before long undoubtedly require a large amount of the power for electrification of their lines. But industrial use must be found for at least $200.000 \mathrm{~h} . \mathrm{p}$. before development will be justified. Those in charge of the project are using every effort to induce the establishment of manufacturing plants at Priest Rapids which will utilize its cheap power for production of basic materials, and it is believed that these efforts will soon be successful.

The following are among the metallic, non-metallic and other substances which exist within 500 miles of Priest Rapids:

Coal Phosphate Rock
Chromium
Copper
Lead
Manganese
Molybdenum
Gypsum
Kaolin
Silver
Tungsten
Vanadium
Zinc
Leucite
Limestone
Marble Míca

Pyrites
High-grade Iron Ore
Clay, alumina
Clay, china
Clay, fire
Clay, pottery:
Clay, porcelain
Natural Soda
Silica
Sodium Sulphate
Diatomaceous Earth
Feldspar
Fluorspar
Timber products
Alunite

Practically none of the great staples are now being manufactured on the Pacific Coast. The manufacturers who locate at Priest Rapids will have for their export market half the population of the world facing them across the Pacific.

It is hoped that Priest Rapids will be the Niagara Falls of the West, and that its power will be used for a diversity of manufacturing purposes, whether great or small.

Priest Rapids is one of the few great pioncer projects remaining undeveloped in the United States. It will be the second
largest hydro-electric plant in the world, and co-incidentally with its construction great industrial plants will be erected to utilize its power when ready; a city of 30,000 people will be built, and vast acreages of nearby land will be brought ander cultivation, supporting a large agricultural population. Probably over one hundred million dollars will be expended in connection with bringing the Columbia River Valley to life. The time is near when this tremendous work of coordinating the uses and values of water, land, sunshine and water-power will be begun.

# Electric Propulsion for the New San FranciscoOakland Terminal Railway's Ferryboats 

By L. Rask<br>Marine Department, General Electric Company

The author gives a brief but interesting account of the novel features in the equipment of these new ferryboats. Changeable speeds with this arrangement of propellers is an interesting innovation even in ferry-boats.-Editor.

The new ferryboat, Hayward, that operates between San Francisco and Oakland on the Key System, is the first ferryboat in the world to use steam turbine electric drive, with a Ward Leonard system of control for maneuvering. This boat was recently put into operation, and there is a sister ship, San Leandro, that will soon begin to operate on the same route.

These boats are owned by the San FranciscoOakland Terminal Railways and help to carry the passengers of the Southern Pacific Railroad from the Oakland Terminals over the Bay to San Francisco. The boats also carry their share of the large masses of people that daily pass back and forth between San Francisco and Oakland, Berkley and Alameda.

The dimensions of the boat are as follows:
Length over all, 240 ft .
Breadth moulded, 42 ft .
Breadth over guards, 62 ft .7 in .
Depth moulded, 19 ft .6 in .
Depth loaded, 11 ft .6 in .
The speed of the boat is 13 knots.
The boiler plant consists of two Babcock and IVilcos water tube boilers. These boilers have a total heating surface of 5000 sq. ft., and will generate a steam pressure of 225 lb . per square inch. They are equipped with superheaters capable of raising the temperature of the steam 65 deg. F. above
normal. The boilers are fitted with Coen oil burners working under normal draft and are guaranteed to supply steam at 210 lb . per square inch and 50 deg. F. superheat.

The propelling equipment consists of a steam turbine geared to a direct-current generator which furnishes power to the two main motors, one on each propeller shaft, and starting control system for both generator and motors. There are also several electrically operated engine room auxiliaries. Power for these auxiliaries as well as for the general lighting of the boat is obtained from a small generator which is direct connected to the main turbine-driven generator. For port use, and when the main unit is shut down, the auxiliary power is obtained from one of two $35-\mathrm{kw}$. turbine-driven direct-current generators.

The main generator is rated 1000 kw . 500 volts, is shunt wound, and has a considerable overload capacity for short periods. It obtains its excitation from the exciter which is direct connected to it. The main motors are each rated 1200 h.p., 125 r.p.m., 500 volts. They are located at opposite ends of the boat and are direct coupled to the two independent propeller shafts. Under normal operation, one motor drives the stern propeller at 125 r.p.m. and the other motor, the bow propeller, at 100 r.p.m. When the ferryboat makes its return trip the speed relations of the two motors are reversed so that
the stern propeller which formerly was turning 100 r.p.m. now is turning 125 r.p.m., and the former stern propeller which now is the bow propeller is turning 100 r.p.m. The electrical connections are so made that whichever happens to be the bow propeller

This method of driving the propellers is a complete departure from that heretofore used with reciprocating engines when the engine is connected to a continuous shaft through the length of the ship and both propellers are always revolving at the same speed.


Fig. 1. 1100-kw. Curtis Steam Turbine Geared to a $1000-\mathrm{kw}$. Direct-current Generator and a 75 kw . Auxiliary Generator, Ferryboat Hayward


Fig. 2. 1200-h.p., 100/125-r.p.m., 500-volt Shunt-wound Double-armature Propulsion Motor, on Test Blocks, for Ferryboat Hayward. Two of these motors receive power from the generator shown in Fig. 1
driving motor for the time being will automatically take the speed corresponding to that which gives zero slip on the bow propeller, thus increasing the propulsion efficiencr. The stern motor at the same time will automatically take orer the duty of driving the ship at whatever speed is called for from the bridge.

The main control equipment consists of two parts-a panel and a controlling rheostat. The panel carries the switches for the motors, generator and the necessary overload and interlocking device. The controlling rheostat consists of a suitable dial rheostat and resistances for varying the excitation of the main generator, which results in varying the
spered of the fropedling motors. fathe middle of the pathel are two fiek switehes, one for dach motor, mountert horizontally. Bolweron


Fig. 3. Front View of Control Panel for the Propelling Motors and Generator Shown in Figs. 1 and 2


Fig. 4. Main Controlling Rheostat, with Covering Removed
these fwo and 111 it vertical position, is focated the eontrol and excitation switeh Which is so constructed that it most be "pened before the other two switehes can be opencel. This arrangenent insures against accirlental opensing of motor fiekls under load. The two motor field switches are triple-pole, single-thoow, two of the knife blades having the same polarity, one supplying the motor ficld, and the other the holding coil of the motor line contactor. This prevents the cosing of the motor line contactor unless the ficlel switeh is closed.

Increasing or decreasing the revolutions of the propeller, as well as reversing its direction of rotation, are all obtained by means of the potentiometer type of rheostat, Fig. 4, which is connected across the field of the main generator. This rheostat consists of a bank of resistors mounted in a rugged angle iron frame with a dial switch built up on an eloony asbestos base. The whole structure is suitably covered by a sheet metal box covering not shown in the photograph. This rheostat is located in the engine room. Communication between the bridge and the engine room is obtained by means of the usual type of ship's telegraph.

The total weight of the propelling equipment is $212,000 \mathrm{lb}$.

It was on account of the reliable and successful operation and ease of maneuvering obtained with the turbine electric machinery of several large cargo boats, as well as of battleships and coast guard cutters, that the owners lecided to equip these two ferryboats with this form of drive.


Fig. 5. Simplified Diagram of the Main Circuits of the Propelling Machinery of the Ferryboat Hayward


Fig. 6. Complete Diagram of Connections Between the Two Propelling Motors and the Main Generator. Above motor No. 2 are shown the speeding up resistors for the stern or driving motor

# Cooling of Turbine Generators 

# PART III <br> PHYSICAL CONSIDERATIONS AND DESIGN OF SURFACE AIR COOLERS 

By A. R. Surth<br>Construchon Enginhering; Dhpartment, Genfral Electric Company


#### Abstract

The first article of this scries dealing with the various ways of cooling air when re-circulated was published in our issue of December, 1922, and the second part covering heat trar sfer in surface air coolers appeared in our Fehruary, 192:3, number. In this, the third part, the author discusses at considerable length the details of design. This series will be concluded with an article discussing the economies of using surface air coolers and heaters in steam power plants.-Editor.


## Introduction

The introduction of surface air coolers for cooling the air from turbine generators represents such a departure from previous methods that the consensus of opinion of many engineers was that these coolers should not only have a large factor of safety in the amount of cooling surface, but that they should be substantially constructed in order to give reliable service and have a low maintenance cost. The investment cost of a first class cooling system is relatively small, when compared with the cost of the turbine generator, and it is obvious that continuity of service of a turbine generator should not be jeopardized by an apparent trivial saving in the construction of the cooler. These fundamentals were kept in mind in designing the present type of coolers with the result that only high class materials were employed and construction practice long in use for surface condensers was followed as closely as possible so as to eliminate experimental features which might later be found detrimental.

## Tubes

The size tube now used is $5 / 8 \mathrm{in}$. outside diamcter, 18 B.W.G. wall and the material is either Muntz metal or Admiralty metal, as may be required. Three quarters or one inch diameter tubes may be used if the trade requires them but experience will show if there is any advantage in the use of larger tubes. The principal service advantage of larger tubes is that there should be less chance of fouling in cases where ordinary circulating water is used as the cooling medium. To offset this advantage the smaller tube allows the installation of a greater amount of cooling surface in the same space. The length of tubes will depend largely on the size of the generator. The
indications at present are that tubes no longer than 10 ft . will be required. Long tubes are supported at the center so that the unsupported spans are not more than approximately 100 tube diameters.

The tubes are given the same rigid tests as required for surface condenser tubes so that they may be used successfully with salt water, raw water, or condensate. If the circulating water is reasonably good the life of the tubes should be so long as to make the maintenance expense almost nil. With salt water or acidulated water, the maintenance expense may be comparable to surface condenser conditions.

## Fins

In order to get the maximum amount of cooling surface at the minimum expense and in the smallest space, the tubes are wound with copper fins spaced seven to the inch, and having an effective depth of $1 / 4 \mathrm{in}$. The addition of fins increases the external radiating surface of a tube, which is the high resistance side, over six times. The amount of space occupied by these fins is extremely small and they present little interference to the flow of air. The fins are shouldered and soldered to the tube so that the joint presents no measurable drop in temperature or resistance to the flow of heat; furthermore, this substantial attachment makes certain that vibration and handling will not loosen the fin surface. The fins are flat and smooth so that all of the surface is in contact with the air stream and should therefore be swept clean of any dirt which may get into the system.

## Tube Sheets

The tube sheets are made of rolled Muntz metal to obtain a non-porous tube sheet which will prevent water from seeping through
into the air space. Tubes are expanded in the usual manner into the one tube shect and are packed in the other by means of standard condenser ferrules and cotion lace. The packed ends will allow for individual expansion and contraction of tubes which may at


Fig. 1. A Cooler Section 9 Tubes Wide and 24 Tubes Deep. The more usual section will be 20 tubes wide and 12 to 18 tubes deep
times become stopped with foreign matter. If the flow of water in a single tube is shut off, the temperature of this tube will soon reach the temperature of the air and therefore be considerably hotter than the tubes immediately surrounding it.

Defective tubes are eliminated by tests before winding them. Tubes with internal stresses and likely to develop cracks when put in service are protected to a large extent by the tightly wound fins. If a defective tube is found after the cooler is put in service it should be plugged. If the circulating water is of fair quality no further tube trouble would be expected. If the water is so bad
that it readily attacks the tulnes thrat the chances are that most of the tulx:s will fail from dezincification and when this artion becomes acute all of the tubes should be replaced.

When renewing tubes the tube shere using ferrules must be removed. The tules are held in position so that the tube sheet can be replaced withont difficulty after the new tubes are in position. Frequent renewal of individual tubes are not anticipated. If a number of tubes must be renewed and general overhauling of each cooler section is desirable, the removal of one tube sheet and a carcful inspection of the remaining tubes is a desirable procedure.

## Water Boxes

Over each of the two tube sheets is bolted by means of studs and nuts, cast iron water boxes provided with a large inlet and outlet to reduce turbulence, which would tend to effect the distribution of water through the tubes. Partitions are cast integral with the water box so as to form any number of water passes that may be desired. The water boxes are set on rubber gaskets completely sealing the partitions as well as the external joint. The coolers are arranged so that the tube sheets form a part of the air duct which leaves the water boxes accessible so that the tubes can be inspected or cleaned with the least possible inconvenience.

The water boxes are shaped to carry through any entrained air and so far no trouble has been experienced from air binding, although vent cocks are provided for coolers which are to set in a vertical position.

## Number of Water Passes

The plan so far has been to maintain a minimum water velocity through the tubes which would be in excess of the critical velocity. The maximum water velocity naturally depends on the pumping head permissible. The number of water passes depends on the number of tubes in the cooler and on whether condensate of circulating water is used. Eventually, the number of water passes will probably become more or less standard because the conditions under which turbine generators operate are not very different. For the present, however, any number of water passes can be obtained to meet conditions.

The flow of water with respect to the flow of air in so far as temperature difference is concerned is counter-current.

## Ais Pressure Drop

The resistance wo the flow of air through the cooler is dependent on the air velocity and the depth of the cooler, the temperature of the air having only a slight effect on the (drop) in air pressure through the cooker. If a fixed amount of surface is so distributed that the air velocity is low, the depth of the cooler will maturally be reduced but the same amome of surface can be so distributed that
wer amd above that required by the gencrator amd in the ducts is relatively small and may be different for various machines It is, therefore, necessary to know how much of the (otal fan pressure is available for the cooler and the cooler must be proportioned accordingly. (ordinarily, the total drop through the rooler should not exceed 1 in . of water.

Resistance to the flow of air in large air ducts of moderate lengths is almost a negli-


Fig. 2. To show how substantially the Fins are Attached to the Tubes, the fins of the perfect tube on the left were mutilated as shown in the center and were then trued up as shown at the right. No injured or broken joints appeared
the depth is considerably greater, which will result in a higher air velocity. When an approximation of the amount of surface is made, it is obvious that it can be so arranged, providing there is sufficient space, to obtain almost any resistance to air flow that may be desired.

When using the coolers in connection with turbine generators the available air pressure
gible factor. Excessive pressure drops are the result of eddying and loss of velocity heads. In laying out any duct system, and especially those in connection with surface coolers. where all of the available pressure loss should be applied to the cooler, the ducts should be carefully designed and in many cases the ducts can be so designed that the duct loss can almost be neglected.

## Drop in Water Pressure

The loss of head or resistance to the flow of water is also a variable quantity and there is considerable latitude in regulating the total pressure drop. A velocity in the tubes of not less than 2 ft . per second is desired so as to keep the flow above the critical velocity. If a velocity of 5 or 6 ft . a second is attempted, the number of water passes are increased and the frict on head increases very rapidly.

Where the coolers utilize the condensate as a circulating medium then a relatively high velocity, say, of 4 or $41 / 2 \mathrm{ft}$., is desirable when the turbine is operating at full load, so that at partial loads the velocity is more nearly normal. The total pressure drop in the cooler from the inlet to the outlet nozzle usually runs in the neighborhood of 20 ft .

## Method of Cleaning Surface

The coolers should be installed in the air duct so that the water box at either end is accessible. With such an arrangement the water boxes can be removed and tubes cleaned, blown, washed, or turbined in exactly the same manner as the cleaning of a surface condenser. This cleaning process should be entirely unnecessary if condensate is used and unlike the surface condenser problem the small amount of water required by the surface cooler should, in most instances, make it perfectly feasible to filter or screen the water and thus avoid any cleaning process.

One of the purposes of a surface cooler is to insure a clean generator. If the system is sufficiently tight so that there is practically no deposit on the generator, then the external cooling surface of the cooler should also be clean. If the generator surfaces become fouled and clogged then the cooling system is defective. Should the coolers become dirty through any fault of design or operation they can be cleaned by submerging and boiling each section in a tank of water and washing soda.

Should any oil vapor flow into the circulating system it might condense only on the cooler and not on the generator. Although experience so far indicates that the oil vapor does condense even on the warm generator surfaces, any infiltration of oil vapor should be eliminated as far as possible.

## Determination of Leaks

Judging from present experience, trouble from leaky tubes or joints is not anticipated except with air coolers employing salt water
or fresh water combammang deatrathor mat gredients. Some formsison, homever, smald be made to locate an oxeasiomal leak which can not be avoided. It is reenmmmended that pilot holes or sight drams of somue kind for providerl in the air duct in such a location its


Fig. 3. General Construction of a Typical Cooler Section
will indicate the presence of water and if possible indicate which particular section is at fault.

If the duct drainage indicates a serious leak the trouble will probably be found in a bad tube which may be readily located as follows: Remore the two water boxes of the faulty section and then apply water or air under
pressure to cach tube be first plagging one end of the tube and inserting a nozzle which fits the other end of the tube. The nozzle connection should be provided with a gange and a valve so that as soon as the tube is put under static pressure the supply can le shat off and any reduction in pressure on the gange noted.


Fig. 4. Portion of One Water Box Removed to illustrate the uniformity of flow through the various tubes. This test was made to be sure there was no congestion in the water boxes

## General Dimensions

The length of tube can be made to suit conditions. So far no tubes over 10 ft . in length have been proposed, largely because a cooler section having only a light frame might tend to twist and distort if the length is out of proportion to the width and depth. The number of tubes deep, that is, the number of rows of tubes in the direction of the flow of air, will probably vary from 12 to 20 , depending on the requirements. The width of a cooler section is more or less arbitrary. It is preferred to make a complete cooler in several sections for the convenience of handling them and to simplify manufacture. There is nothing to be gained in making a single section for large machines and there are many disadrantages. A common width of section will range from 20 in . to 30 in .

## Arrangement of Cooler Under Generator

The drawing in Fig. 5 will illustrate a common and convenient arrangement which is recommended and which can generally be obtained if the turbine foundation has not been constructed along other lines. The simplicity of air duct not only greatly reduces the cost, but has the important advantages of:

1. Reducing to a minimum the volume of air which would support combustion in case of a fire.
2. Making possible a system where the infiltration of air will be negligible.

It should be observed that with the arrangement shown individual cooler sections can be realily removed for inspection or repairs, white the water boxes are accessible, thus making possible the cleaning of tubes or the maintenance of tight joints possible without entering the air duct.

Arrangements of course are not limited to the one shown in the illustration. Coolers can be set in a horizontal or a vertical position but the arrangement recommended will assure a more uniform distribution of air to the cooler and will make available considerable basement floor area which generally can be used to advantage for many other purposes.

## Advantages of Surface Coolers

In most cases the surface cooler presents a number of economical and operating advantages. To what extent these advantages may be capitalized depends of course upon local conditions. The common advantages are as follows:

1. If the air duct system contains but a small volume of air, no fire extinguisher should be necessary because the oxygen will be rapidly consumed and the fire smothered without requiring the attention of an operator or the operation of any dampers.
2. If the proper precautions are taken to prevent any material infiltration of air, the deposits in the machine or on the cooler should be insignificant. If a clean generator is maintained, the temperature rise of the winding above the incoming air temperature should not increase with age.
3. The volume of water required for cooling the air can be regulated because the flow of water is counter-current with respect to the flow of air. Where water is expensive it is therefore possible to economize on the quantity.
4. The pumping head or the amount of auxiliary power required is extremely low.
5. Where condensate can be employed, either wholly or in part, for the cooling of a generator, some or all of the generator losses are returned to the system in the form of heat.

## General Limitations in Temperature

The surface cooler can be designed to cool the discharged air very close to the entering water temperature. This terminal difference, of course, depends on how much cooling surface is installed. Ordinarily, a terminal temperature difference of 15 deg . F. should be
maintained. A lower temperature difference would be expected with the cooler surface perfectly clean. The ingoing air temperature to the generator should not exceed the standard ambient temperature of 40 deg. C. or 104 deg. F., and it is recommended that this be considered the extreme. Ordinarily the ingoing air temperature should not exceed about 35 deg. C. or 95 deg. F.

If the condensate temperature ever exceeds 85 deg. F., colder circulating water or service water should be substituted, during such periods. The coolers may be constructed in

Therefore, a reliable thermestat wamomace such a condition should affod ample time for an operator to re-estaldish the water sumply or to obtain it from the other source ermnected thereto. The temperature rise of the machine windings during such a perion of course will be sluggish because of the thermal storage of the generator.

## Eliminators

There may be arrangements adopted where the puncture of a tube might release water into the generator. Such a condition can be


Fig. 5. Arrangement of Cooler and Generator Commonly Adopted
two sections, the first section using condensate the year round and the second section using a sufficient amount of cooler water during such periods as may be necessary, to maintain a discharge air temperature within the limits suggested above.

Two sources of water supply are recommended rather than the introduction of dampers to convert the re-circulating system to the open type. In case of the failure of either water supply the air temperature on the discharge side of the cooler will instantly rise to the temperature on the entrance side.
guarded against by the installation of water eliminators which have been developed especially for such a purpose. The introduction of eliminators, however, will introduce additional friction in the air circuit and it is recommended that the coolers be so located as to avoid the necessity of using eliminators. With the cooler sections located below the generator the spouting relocities of the water may prevent it from entering the generator winding even though it is assumed that such a leak derelop at just the right point on the upper row of tubes.

# Arc Welding of Cast Iron 

PART II

By W. H. Namack<br> Smonen, A. W. S.


#### Abstract

The study which the American Welding Society's Northern New York Section Committee on the Electric Are Welding of Cast Iron gave to the problem of preventing the formation of the hard zone, or its removal, and its investigation to determine the relative weldability of varions grades of cast iron led to the performance of a group of carefully conducted tests of seven commercial electrodes on two grades of cast iron at present in wide use. The following article is an abstract of the test results. EDMOR


The problen of welding cast iron by means of the electric are is not a single definite prob)lem which might be solved easily by making a few tests. In fact the Committee has discussed it from every point of view and has found not one but many difficulties which confront the investigator from the start. The variables are many and the control of these variables is in some cases most difficult. The personal clement is probably the greatest variable, but it can be made less dominating by proper selection in carrying out a series of tests although it is yet to be controlled in the practical application of arc welding.

## SPECIAL INVESTIGATION BY THE COMMITTEE

In the course of its investigations, the Committec has considered the following points:
(1) Preparation of the parts to be welded.
(2) Prevention of slag inclusions in the weld metal deposited.
(3) Suitable values of current for the size of electrode employed.
(4) Method of deposition of the filler metal and its effect on the strength and hardness of the weld.
(5) Reversed polarity versus straight polarity.
(6) Effect of long versus short arc.
(7) Effect of speed of welding on the softness of the weld.
( 8 ) Tests of electrodes with a view to ascertaining the most suitable materials, construction, and characteristics for use in welding various grades of cast iron

## Preparation

For the purpose of its investigation the Committee decided that in the preparation of the parts to be welded the single V is better than the double $V$ because in actual service the use of the double V is in most cases practically impossille. A single $V$ was therefore used in all of the Committee tests.

## Slag Inclusions

1t is usually agreed that gray cast iron is the most uncertain grade to weld. The difficulty scems to be due largely to the free carbon present which is called "kish." When welding with bare electrodes this "kish" causes a dark deposit to form on the weld metal. Chemical analysis indicates this deposit to be


Fig. 1. Illustration showing Depth of Heat Penetration and Weld Penetration with Long and Short Arcs
iron silicate or slag, which oftentimes causes a defective weld by lodging in the weld metal and forming what are called "slag inclusions." Two methods suggested to remove this "kish" seemed suitable to the Committee; viz., first, the surface to be welded may be subjected to a slight preliminary melting with the carbon arc, second, a high current value may be used in the welding process although the practicability of its use would depend upon the thickness of the parts to be welded and the skill of the operator. It would seem that the localization of heat has a tendency to create an annealing effect and the Committee
believes that the data incorporated in the test results will tend to show that this proposition to use a high heat value in the welding operation has some worth.

## 1 Current Values

For cast iron welding by the metallic-arc process, the best results with average welding ability and a $1 /$-inch metal electrode on plates up to $\frac{3}{16}$-inch thickness were found to be secured with current up to. 12.5 amp . and for a $\frac{5}{32}$-inch


Fig. 2. Two Similar Examples of the Layout of Test Plates peparatory to cutting

© Opening
Sice View of Plate
Fig. 3. Completion of Plates up to Time of Welding
metal electrode current from 1.35 to 1.9 jmp depending on the thickness of the plate.

## Method of Deposition

The usual method of depositing the weld metal is to apply it in layers or beads lengthwise of the weld. In this way a series of interlocking layers is formed which. if brusher
 should give a clean weld Fumbermore the heat can be kept low and (anの"atuatly the expansion will be small. 'The fepmation of metal be means of a single simal later was. howerer. strongly adrocated and this hater


Fig 4 Layout of Welded Specimen preparatory to Machining the Test Bars

method was employed :o perf amine most o: the Commitice test

Polarity
Some members (ommitict adrocated using reversed foran er educe the heating effect of the ato An hasemetal hut this sug-

ably for some electrodes and for some kinds of cast iron, better results can be obtained with reversed polarity.

## Length of Arc

The Committee decided that an are length not over ${ }^{1}$ anch wotdd give a deeper and more uniform penctration and would insure a stronger weld. In order to test this suggestion samples of long and shore are deposition on both steed and cast iron were analysed with the following result:

The Nitrogen Theory. Three zones were investigated by means of photomicrographs. Sections taken at the top of the bead, at the junction of the filler and base metals, and in


Fig. 6. Diagram of Clamping Apparatus Holding Test Plates preparatory to Welding
the lower dark zone showed traces of nitrogen in the form of dark needles. This nitrogen or "nitride" as it is called was present in both the steel and cast-iron welds. The presence of carbon together with the nitride is the cause of the hardening effect. The hard zone in the steel weld is soft enough to be machineable and gives no trouble. The hard zone in the cast iron was very hard and not machineable.

The four illustrations in Fig. 1 show the depth of penetration and hard zones: for two gray-cast-iron welds (No. 1 and 3) and two steel welds (No. 2 and 4).

[^25]Ciray Cast Iron. Short Arc with bare electrode. Specimen No. 1, Fig. 1, shows that the filler metal is amalgamated nearly to the bottom of the black area and that the black area is somewhat more shallow than in the case of specimen No. ?3.

Ciray Ciast Iron. Long Arc with bare electrode. Specimen No. 3 , Fig. 1. The difference between "heat penctration" and "weld penctration" can be very clearly distinguished in this illustration. There are two hard zones, one at the bottom of the filler layer and the other at the lower edge of the dark area.

Steel. Short arc with bare electrode. Specimen No. 2, Fig. 1. The hard zones are present but are not as troublesome as in the case of


Fig. 7. Photograph of the Set-up, a sketch of which is shown in Fig. 6


Fig. 8. Application of the Filler Metal by what is termed Method No. 2 in the tests
cast iron due to the fact that there is not as much carbon present.

Steel. Long Arc with bare electrode. Specimen No. 4, Fig. 1. The different zones can be clearly distinguished here.

Speed of Welding vs. Softness
As the result of a series of tests the Committee concluded that the speed of welding did affect the softness of the deposited metal, the lower speed in the case of either straight or reversed polarity gave the softer deposit of metal. The hardness tests were made with a Shore Scleroscope and the following hardness numbers are the averages of about 50 readings each.*

| STRAIGHT POLARITY | REVERSED POLARITY |  |
| :--- | :---: | :---: |
| Slow | 33 | 23 |
| Fast | 40 | 36 |

TABLE I
CHEMICAL ANALYSIS OF BASE METAL

B Plate
Per Cent


Total carbon Graphitic carbon Combined carbon Silicon Sulphur Phosphorus
Manganese

G Plate Por Cent
3.15
2.96
0.19
2.28
0.104
0.865
0.55

TABLEE II
KEY TO ELECTRODES USED IN WELDING TEST PLATES

Electrode
13 llates
(i Platrs

6 B and 9 B
16
513
813
1013
$4 \mathrm{~B} \quad 5 \mathrm{C}$
$2 \mathrm{~B} \quad 8 \mathrm{8}$
7 B and 3 B 9C

TABLE III
ELECTRODES AND CHARACTERISTICS
AVERAGE CURRENT 130-150 AMP., 20 VOLTS
The Chemical Analyses Were Made by J. H. Nead of the American Rolling Mills Co. The Characteristics Were Noted When the Test Plates Were Being We!ded

| Electrode | description and analysis of electrodes |  |  |  |  |  |  |  |  | Plate <br> Used | Welding Characteristics |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | C | Mn | Si | S | Ph | Cu | Ni | Cr | Fe |  |  |
| 1 | Bare wire, 5,32 in. by 14 in . |  |  |  |  |  |  |  |  | B | Arc unsteady but not as bad at the start of the weld as at the finish. Deposited metal stays molten over an area of about $1 / 2$ of a square inch and boils while cooling. Hard to hold a short arc for this reason. Black scum formation stops the boiling. Wire varies in workability. |
|  | 0.100 | 0.466 | 0.04 | 0.025 | 0.039 | 0.056 | Trace |  |  |  |  |
| 2 | Bare wire, $5 / 32 \mathrm{in}$. by 14 in . |  |  |  |  |  |  |  |  | B | Large arc flame. Flashy arc with small pool of molten metal which cools quickly. Metal lays solid and deposits quite evenly. This electrode works nearly the same as if on a steel plate. |
|  | 0.010 | 0.012 | Trac | 0.037 | 021 | 062 | rac |  |  |  |  |
| 3 | Coated wire, $5 / 32 \mathrm{in}$. by 14 in . |  |  |  |  |  |  |  |  | B | Arc uneven and sputters. Deposited metal puffs up and solidifies so that, when the arc passes over it after cooling, the deposited metal meltsaway showing a shell-like structure. Metalis deposited unevenly and gas holes appear as the metal cools. Large bright arc flame noticeable. |
|  |  | 1.65 | 0.08 | 0.025 | 0.0212 | 27.27 | 68.25 |  | 2.29 |  |  |
| 4 | Coated wire, $5 / 32 \mathrm{in}$. by 14 in . |  |  |  |  |  |  |  |  | B | Arc steady but sputters similar to a bare commercial electrode on a steel plate. Deposited metal lays evenly and solid but builds up slowly. A black scum forms as the metal cools but the deposited metal appears firm and solid. A smooth working electrode. |
|  | 0.010 | 0.010 | Trac | 0.040 | 0.019 | 0.032 | Trace |  |  |  |  |
| 5 | Coated wire, $1 / 8 \mathrm{in}$. by 18 in . |  |  |  |  |  |  |  |  | B | Steady are similar to bare electrode on steel plate. Deposited metal seems to burn deep into the base metal and arc flame is quite noticeable. Wire burns away very fast. Electrodes were held at the third-points to prevent too rapid melting. No pool of metal to speak of. Black scum is not prominent. |
|  | 0.100 | 0.429 | 0.050 | 0.028 | 0.039 | 0.082 | Trace |  |  |  |  |
| 6 | Alloy wire, $5 / 32 \mathrm{in}$. by . . in. |  |  |  |  |  |  |  |  | B | Reiersed polarity necessary. Sputtering arc. Metal deposits by dropping off in globules and boils and bubbles while cooling. The metal does not spread but bunches up. As metal cools, numerous small gas holes appear and when the arc is passed over it again the surface melts away showing a honeycombed structure. The arc burns into the base metal. Protrusions are numerous. |
|  |  | 4.62 | 0.04 | 0.020 | 0.005 | 0.12 | 94.20 |  | 0.70 |  |  |
| 7 | These electrcdes were not available for these tests. |  |  |  |  |  |  |  |  |  |  |
| 9 | Composite, $5 / 32 \mathrm{in}$. by 14 in . |  |  |  |  |  |  |  |  | B | Smooth steady arc with small flame. Metal solidifies very quickly and the pool of molten metal following the arc is hardiy noticeable. Appearances indicate that the heat generated in the deposited metal is small. Metal deposits where desired and solidifies quickly. A brownish white coating appears on the surface of the finished weld. |
|  |  |  |  |  |  |  |  |  |  | G | The arc characteristics were apparently the same as those already observed for the B plate, except that the arc was more unsteady and somewhat harder to maintain. The deposited metal did not stick as well to the $G$ plate as it did to the B plate. |

## Electrodes

During the progress of its investigations, the Committee found that there were many different kinds of electrodes in use commercially for welding cast iron. It was therefore decided to investigate these as to their respective characteristies when employed in welding cast iron.

As a preliminary project, a program was outhined for investigating seven commercial electroles of the following types: bare wire.
lated) it might come to be accepted as a Standard Method of Procedure for further investigations of this character

## SPECIFICATIONS FOR TESTING COMMERCIAL ELECTRODES

## Size of Plate

The size of plate slaall be 40 by 14 by 1 inch. ( One plate shall be cast for each grade of iron to be tested

TABLE IV

## TIME REQUIRED AND METAL USED IN WELDING TEST PLATES

The weld groove wats $6-1 \mathrm{~m}$. long and $1-\mathrm{m}$. deep, bevelet 90 deg., giving; a volume of 6 ra . in. to top of plate. For electrode numbers sec specifications.

B PLATE
Method as Per Specifications, 150 Amp., 20 Volts

|  |  | Blectiondia |  |  | weıchir |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Electrode Nimber | $\begin{gathered} \text { Size } \\ \text { Inches } \end{gathered}$ | Time Minutes | Number per しか. | $\begin{gathered} \text { Number } \\ \text { Used } \end{gathered}$ | Before. O7. | After. Oz . | Metal <br> Used. Oz . |
| 1 | $\frac{5}{83}$ by 14 | 41 | 14 | 2522/3 | 2915 | 326 | 25.8 |
| 2 | $\frac{5}{32}$ by 14 | 37 | 14 | 22 | 25.1 | 3.4 | 22.1 |
| 3 | $\frac{5}{32}$ by 14 | 41 | 12 | 25 | $33^{1}{ }_{3}$ | 3 | $301 / 3$ |
| 4 | $\frac{5}{32}$ by 14 | 40 | $1: 31 / 4$ | 23 | 27.3 | 4 | 23.3 |
| 5 | $1 / 8$ by 18 | $521 / 4$ | 16 | $26^{\frac{1}{2}}$ | 26.5 | 4 | 22.5 |
| 6 | $\frac{5}{32}$ by .. | 30 |  |  | 40 | 12 | 28.0 |
| 9 | $\frac{5}{32}$ by 14 | 30 | 11 | 17 | 24.7 | 4 | 20.7 |

B AND G PLATES
Method No. 2. 150 Amps., 15 Volts

flux covered, alloy metal, and alloyed flux electrodes.

The Committee's investigations were confined wholly to testing these seven electrodes in accordance with the Specifications for Tests which are given in the following.

After careful deliberation and consideration of the various elements and factors involved, the following program was adopted by the Committee as constituting a basis for a preliminary investigation, and in the belief that (with the many morlifications which would] doubtless be suggested as experience accumu-

## Methoul of Casting

The plates for test shal! be cast flat in a green sand mold.
Chemical Analysis and Tensile Strength of Each Material
These data shall be obtained from the coupon bars cut from the plates as shown by $2-4 \mathrm{G}$, $2-4$ B, etc., in Fig. '2, and compared with the data obtained from the foundry test records.

## Heat Treatment

The plates shall be allowed to cool overnight in the sand of the mold to avoid any

TABLE V
MACHINIST'S REMARKS ON CUTTING THE WELDED PLATES

| Plate | $\begin{aligned} & \text { Electrode } \\ & \text { No. } \end{aligned}$ | Time of Cutting. Hours | Remarks on Cutting |
| :---: | :---: | :---: | :---: |
| 1 G | 1 | $41 / 4$ | Plate cut under difficulties although the wedded portion was mo harder than usual Rather stringy metal in the welded portion cansing saw teeth to cloge espen iatly after cutting the first three test pieces. From the fourth test piece the balance of plate required 1 wo cuts on cach test piece lefore taking the entire thickness. The machine had to be stopped quite frequently to remove chips from the saw teeth, when passing through the weded seetion. |
| 2 G | 2 | $3 \%$ | First four test pieces were cut using same saw as was used in cutting the six test pieces from Plate 5 B. While cutting the fifth test piece, the saw struck a real hard spot which took the entire cutting edge from the saw. A new saw was used to complete the plate. This plate was quite hard in general but was able to cut through the entire thickness of each piece by raising and lowering the table to prevent stopping of saw. |
| 4 G | $\begin{gathered} 2 \\ \text { Method } \\ \text { No. } 2 \end{gathered}$ | 53.4 | Plate was exceedingly hard, requiring the use of three saws and taking two cuts on each test piece. Entire plate was hard not only in welded portion but also through the cast iron. |
| 5 G | 5 | 334 | Plate machined fairly well but metal at junction of filler and base metals was hard. The hard junction and ernst on top of welded section made it necessary to raise and lower the tahle to prevent the saw from stopping. One saw was used on the entire plate. |
| 8 G | 6 | 3 | Plate cut very good. Entire thickness of plate was taken in one eut using same saw as was used on Plate 8 B . The weld section was 10 harder than usual. |
| 9 G | 9 | 3 | Entire plate was cut with one saw taking the entire thickness of the plate in one cut. The welded section had no effect on the saw in the least aside from the effect of the scale and grit. |
| 2 B | 6 | 3 | Plate cut excellently, being cut into test pieces with one saw taking the entire thickness in one cut. Welded section had no effect on the saw aside from the effect of the scale and grit. |
| 3 B | $\begin{gathered} 9 \\ \text { Method } \\ \text { No. } 2 \end{gathered}$ | $82 / 3$ | Entire plate was very, very. exceedingly hard requiring the use of 14 saws before the plate was completed. One saw was totally destroyed as it pulled in two under the strain of the hard welded sections. Plate was raised and lowered repeatedly to allow saw to cut through. |
| 4 B | 5 | $31 / 4$ | Entire plate was machined with same saw as was used on Plate 2 B, taking entire thickness of plate per cut up to last test piece which required two cuts. The welded portion of the whole plate was real hard and probably he hard to turn |
| 5 B | 2 | 33.4 | The first cut was very hard requiring the use of three saws and taking two cuts for the test piece. After securing the first piece a sharp saw was placed on the arbor and the entire plate completed with it. taking the entire thickness of plate at one cut. |
| 6 B | 1 | 3 | Plate machined very nicely. Used same saw that finished last two cuts on Plate 2 G taking entire thickness of plate per cut. In fact this plate machined similar to Plate 7 B although the welded section was much harder. |
| 7 B | 9 | 3 | Plate machined excellently, the entire plate being cut into test pieces with one saw taking the entire thickness of the phate per cut. The welded section did not seem to affect the saw in the least. |
| 8 B | 3 | 3 | A sharp saw was placed on the arbor and the entire plate was machined with it taking the entire thickness of the plate in one eut. Aside from the welded portion being somewhat hard the plate worked inp excellently. |
| 9 B | 1 <br> Method <br> No. 2 | 3 | Plate machined excellently taking the entire thickness of the plate in one cut The welded portion did not seem to be very hard but rather tough. |
| 10 B | 4 | 7 | First cut was extremely hard, requiring five different cuts to go through the plate, practically destroying the saw. The entire plate was quite hard in general, requiring three cuts or more to each test picce also the changing of saws for each piece until the last cut which was made through the entire plate in one cut. |



Fig. 9. Classification of $G$ Iron Test Bars with respect to Machineability and Tensile Strength

1. Along line of weld
2. Perpendicular to axis of test piece
3. Honeycomb structure
4. Coarse granular
5. Crystalline
6. Slag inclusions
7. Blowholes
8. Broke in threads
9. Uneven break


Fig. 10. Classification of $B$ Iron Test Bars with respect to Machineability and Tensile Strength

1. Along line of weld
2. Perpendicular to axis of test piece
3. Honeycomb structure
4. Coarse granular
5. Crystalline
6. Slag inclusions
7. Blowholes
8. Broke in threads
9. Uneven break
chilling action. No heat treatment shall be given to any plate.

## Size of Samples

## For W'clding

Plates shall be laid out as shown in Fig. .2. (Two examples given.)

## For Testing of Parent Metal

The sample test bars shall be prepared according to the specifications of the A.S.T. M.

Method of Welding
Kind, Analysis, and Size of Eledrodes
The following electrodes shatl lee neserl:
(1) Bare wire
(6) Alloy wire
(2) Bare wire
(7) Alloy wire
(3) Coated wire
(h) Alloy wire
(4) Coated wire
(9) Composite (lec:trode
(5) Coated wire

These electrodes shall be $5 / 32$ in. in diameter, and a chemical analysis of each shall be made.


Fig. 11. Classification of B and G Iron Test Bars (welded by Method No. 2
with respect to Machineability and Tensile Strength

1. Along line of weld
2. Perpendicular to axis of test piece
3. Coarse granular
4. Honeycomb structure
5. Crystalline
6. Blowholes
7. Broke in threads
8. Uneven break
from the coupons cut from the plate shown in Fig. 2.

## Preparation of Samples <br> Cutting

Plates shall be marked for identification as shown in Fig. 2, and then cut as shown in Figs. 2 and 3. As an extra precaution, after cutting, the samples shall have the same marking stamped on one short edge of each as is stamped on the surface.

## Beielling

Single bevel, 4.5 deg . to the center, as shown in Fig. 3.

## Current

Preferably 150 amp. in each test. The current actually used shall be recorded.

## Polarity

Straight polarity (work positive and electrode negative) with all electrodes, and also additional samples with reversed polarity on the non-ferrous electrodes.
Clamping
Plates to be clamped as shown in Figs. 6 and 7, and tacked at both ends and the center before the weld is started. These tack melds shall each be a single bead approximately $1 / 2$ in. long.

## Nomber of laters

（ ）he：spiral laser only shath be depusited to lill the groove in eard lest．＇The surface of the deposited material shatl extemd approximately ${ }^{1}$ sin above the surface of the hase material．


Fig．12．Four Welded Specimens，which broke in the threads on the first two tests，turned to one－half inch diameter for the third test

## Cleaning

The surface of the deposited motal shall be kept clear of all scale at all times by brushing with a wire brush．

Just lefore the clamps are removed the wdeder shall stamp an＂S＂on the surface of the phate at the start of the wedt and an＂F＂ at the linish．A record shall be kept of the number stampert on the sample，the type of alodrode nsed，the wedling current，the time reopuited for making the wedt，the are char－ ateristics of eath electrode，and the number， longth，and total weight of electrodes used on cach sample，fogether with the weight of seras ends．

## Testing

The phates shath be laid out to be cut （rosswise of the weld into five bars $7 / 8$ by 1 in ． and two bass＂，by 1 in．，as shown in Fig． 4. Lathe centers shall be drilled so that they will come in the center of the end of each of the $7 x^{2} \mathrm{y} 1 \mathrm{in}$ ．bars．

Then identifying numbers shall be stamped aromed the lathe centers on the $7 / 8$ by 1 in ． bars so that these numbers will appear on each end of each bar after the ends are turned down to 3.1 in ．in diameter，and also on the ends of each of the $3 / 8$ by 1 in ．bars．The identifying numbers shall consist of the num－ ber on the sample plate followed by a numeral， this numeral being（1）for the bar cut from the sample plate at the start of the weld and（7） for the bar cut from the sample plate at the finish of the weld，the intervening bars being numbered consecutively，as shown in Fig． 4.

The sample plates shall then be cut as laid out，and each $7 / 8$ by 1 in ．bar shall be machined


Fig．13．Four Welded Specimens of Fig． 12 after Testing，showing Fractures

## Remarks

After the weld has been completed the clamps shall be left in place until one＇s hand can be held on the weld without discomfort． No artifical cooting shall be applied．
as shown in Fig．．），no machining being done on the ${ }^{3}$ by 1 in ．bars．

The machinist shall keep a record of the characteristics of all of the test specimens as regards machineability of the welded portion．

## Tensilc Strength Tests

Tensile strength tests shall he made on each of the round test hars in accordance with $A$. s. T. M. Standards

## Hardness Tests

Scleroscopic hardness readings shall be taken on the deposited metal, at the junction of the deposited metal and the parent metal, and on the parent metal, on each of the 3, by 1 in . test bars.

## Microscopic and Chemical Analysis

After hardness tests have been completed on the ${ }^{3}$ s by 1 in. test bars, these shall be used to obtain photomicrographs of the junction of the deposited metal and the base metal to
by the leters 13 and (; and their trale names are turbine or cylinder iron, and gray cast iron, respectively. Their chomical analyses are given in Table I.

Two methods of depositing the filler metal were used in these tests, namoly, that as described in the Specifications and another illustrated in Fig. $s$, which will be referred to as Method No. 2. . It will be noted that this latter method allows the operator to deposit steel on the surface of the cast iron better and insures better penetration since the electrode can more easily be held perpendicular to the surface of the base metal while putting on each bead. The procedure is as follows:


Fig. 14. Typical Fractures of Tensile Specimens arranged in groups
determine, if possible, the cause of any cxcessive hardness. No chemical analysis of the deposited metal shall be made unless it is determined, after the various other tests, that such analysis would be desirable on any of the specimens.
Reports
All data collected, with the complete history of each specimen, shall be shown on the final report, together with such conclusions as may be drawn.

## THE COMMITTEE'S TESTS

The Committee selected two different grades of cast iron as base material for the tests. These two grades of iron are identified

The parts $A$ and $B$ are first joined together be bead 1. Then beads 2 and 3 are lad on sn that they do not quite touch. Beads \& and ; are next deposited and then filling $\sigma$ is laid down. More beads are laid on the cast iron and the filling-in process is continuted so that the whole weld is made up of a succession of layers. The advantage claimed for this method is that the deposition of the filler metal by stages has a great tendency to ameal the deposited metal below the particular stage which is being deposited and in this way a softer weld is obtained.

The method referred to in the Specifications consists of depositing the filler metal in one spiral layer after the parts $A$ and $B$ had been

TABLE VI
SUMMARY OF TESTS ON GRAY CAST IRON（G PLATES）

| $\begin{gathered} \text { sumple } \\ \text { No. } \end{gathered}$ | 1：しゃc． trod． Used | Wirld Appear－ ance Before Testing | Machinealility | MMENSH0゙ち |  | （0，11）AT FAMI，URE： |  | （iroup <br> No． | Firacture location | Key to Fracture |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Diam． Inches | Are：i <br> Sq．In． | It． | $\begin{gathered} 1.1) . \\ l^{2}(\mathrm{er} \\ \text { Sil. } \mathrm{In} . \end{gathered}$ |  |  |  |
| 2－16 |  |  |  | 0.5 | （1．19\％ | 4380 | 22400 | Base |  |  |
| 1－11 ${ }^{\text {a }}$ |  |  |  | 0.5 | 0.196 | 33300 | 16850 | $\int$ Metal |  |  |
| 161 | 1 | l＇oor | Medium lard | 0.757 | 0.4501 | 5.305 | 11800 | 1 | al） | 守 |
| 1 Ci | 1 | l＇oor | Medinm lard | 0.747 | 0.4385 | 1725 | 3900 | 5 | a | 乐为号 |
| 10.4 | 1 |  | Medium hard． | Broke（2 | n（ cut） |  |  | 5 | uf | き叁芴 |
| 165 | 1 | I＇oor | Medium hard | $\mid 0.762$ | 10.4560 | 2420 | 53000 | 5 |  | EF ${ }^{\text {Co }}$ |
| 167 | 1 |  | Medium hard． | Broke（4 | th cut） |  |  | 5 | adfg |  |
| 2 Gl | $\stackrel{3}{2}$ | Pair | Soft | 10.75 | 0.442 | 2660 | 6020 | 5 | a |  |
| 2 C 3 | $\stackrel{3}{2}$ |  | Medium liard． | Broke（3） | rd or 4 th | cut）nea | ly $3 / 4 \mathrm{in}$ ． | 5 | ai | ¢ーシ |
| $2 \mathrm{Cl}^{4}$ | 9 | Fair | Very hard | $\mid 0.759$ | 0.4525 | 4925 | 10900 | 5 | a | Eここき |
| 2 G 5 | 2 | l＇oor | Medium hard | 0.754 | 0.4465 | 4750 | 10600 | 2 | ad |  |
| 2G7 | 2 |  | Medium hard． | Broke（3） | rd or 4 th | cut）ab | ut $\frac{5}{16} \mathrm{in}$ ． | 5 | adfg |  |
| 4 G 1 | $2^{*}$ |  | Hardest of all | samples． | Broke | n（l cut） |  | 4 | bj |  |
| 4 G 3 | $2^{*}$ | Good | Hard | ｜ 0.752 | 0.4442 | 5915 | 13300 | 4 | bj |  |
| 4 G 4 | $2^{*}$ | Good | Hard | 0.756 | 0.4489 | 7200 | 17000 | 4 | h | $\cdots$ |
| 4 G 4 | $2^{*}$ | Good | Hard | 0.756 | 0.4489 | 7400 | 16500 | 4 | h |  |
| 4 G 4 | $2^{*}$ | Good | Hard | 0.5655 | 0.2512 | 4440 | 17700 | 4 | abj |  |
| 4 G 5 | $)^{*}$ | Good | Medium hard | 0.754 | 0.4465 | 6130 | 13700 | 4 | bijk | \％ |
| $4 \mathrm{G7}$ | $2^{*}$ | Fair | Medium hard | 0.749 | 0.4406 | 4675 | 10600 | 4 | bj |  |
| $\overline{\mathrm{j}} 1$ | 5 | Fair | Medium hard | 0.75 | 0.442 | 6550 | 14810 | 1 | ab |  |
| 5 G 3 | 5 | Poor | Medium hard | 0.75 | 0.442 | 3410 | 7710 | 1 | ab | ช్ర¢్ర6 |
| 5 G 4 | 5 | V．poor | Hard | 0.75 | 0.442 | 6230 | 14100 | 2 | af |  |
| 5 G 5 | 5 | Poor | Hard | 0.75 | 0.442 | 4950 | 11200 | 1 | ab |  |
| 5 G 7 | 5 |  | Hard．Broke | （last cut） |  |  |  | 1 | $a b$ | 号 |
| SG1 | 6 |  | Undersized． | Not mach | ined |  |  |  |  | －0 |
| 8G3 | 6 |  | Soft．Broke |  |  |  |  | 1 | $a b$ | B＋ |
| 8 G 4 | 6 |  | Soft．Broke（ | （last cut） |  |  |  | 3 | $a b$ | ¢－ |
| 8G5 | 6 | V．poor | Soft | 0.768 | 0.4633 | 4040 | 8700 | 1 | a | \％Э |
| $8 \mathrm{G7}$ | 6 | Poor | Soft | 0.762 | 0.4560 | 3675 | 8100 | 3 | bek |  |
| 9 Gl | 9 | Poor | Medium hard | 0.755 | 0.4477 | 5040 | 11300 | 5 | a | ¢ |
| 9 G 3 | 9 |  | Hard．Broke | （2nd or 3 | rd cut） |  |  | 5 | ai | くが |
| 9 G 4 | 9 |  | Hard．Broke | （1st cut） |  |  |  | 5 | ai |  |
| $9 \mathrm{G5}$ | 9 |  | Medium hard． | Broke | （putting | in cento | mark） | 5 | ai | ¢．잉 |
| $9 \mathrm{G7}$ | 9 | Pioor | Medium hard | 0.762 | 0.4560 | 2735 | 6000 | 5 | a |  |

＊Method No． 2 used．
TABLE VII
SUMMARY OF TESTS ON TURBINE OR CXLINDER IRON（B Plates）


TABLE VII－（Cont＇d）

|  |  | Weld |  | Dime | sions | LOAD A | F－W，Re： |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Sample } \\ & \text { No. } \end{aligned}$ | $\begin{aligned} & \text { Elec- } \\ & \text { trode } \\ & \text { Used } \end{aligned}$ | $\begin{gathered} \text { Appear- } \\ \text { ance } \\ \text { Before } \\ \text { Testing } \end{gathered}$ | M．chinealshy | Diame luches | $\begin{gathered} \text { Area } \\ \text { Sy. In. } \end{gathered}$ | 1．1． |  | $\begin{aligned} & \text { Group } \\ & \text { No. } \end{aligned}$ | $\begin{aligned} & \text { Practure } \\ & \text { Location } \end{aligned}$ |  |
| 3B1 | 9＊ | 1 rair | Hard | 0.7 （i） | 0.4548 | 10755 | 23300 | 1 | 1，j |  |
| 3B3 | $9^{*}$ | Pair | Hard | 0.753 | 0.4453 | 12000 | 26900 | 1 | 11 |  |
| 3B3 | 9）＊ | Fair | Hard | 0.753 | 0.4453 | 11900 | 26700 | 1 | 1 |  |
| 3B3 | $9^{*}$ | Good | Hard | 0.575 | 0.2597 | 7065 | 27200 | $t$ | 1，k |  |
| 3B4 | $9^{*}$ | Faijr | Hari | 0.758 | 0.4513 | 11950 | 26500 | $t$ | 1 |  |
| 3B4 | 9＊ | Fair | Hard | 0.758 | 0.4513 | 11680 | 25900 | 4 | 1 | 令 |
| 3B4 | 9＊ | Good | Hard | 0.570 | 0.2552 | 8540 | 333360 | 4 | $1, \mathrm{j}$ | \％ |
| $3 \mathrm{B5}$ | $9{ }^{*}$ | Fair | Hard | 0.741 | 0.4313 | 9620 | 22：300 | 1 | $1, \mathrm{j}$ |  |
| 3B7 | $9^{*}$ | Good | Medium hard | 0.753 | 0.4453 | 7880 | 17450 | 4 | 1，jk | 说年 |
| $4 \mathrm{B1}$ | 5 | Poor | Hard | 0.755 | 0.4477 | 5765 | 12900 | \％ | 4 | ¢ES |
| 4B3 | 5 | Poor | Medium | 0.750 | 0.442 | 4050 | 9180 | 5 | a |  |
| $4 \mathrm{B4}$ | 5 | Poor | Soft | 0.755 | 0.4477 | 5110 | 11400 | 5 | ， | ESE |
| $4 \mathrm{B5}$ | 5 |  | Hard．Broke | （all but | threaded） |  |  | 5 | afgi |  |
| $4 \mathrm{B7}$ | 5 | V．poor | Medium hard | 0.750 | 0.4475 | 3200 | 7200 | \％ | a |  |
| 5B1 | 2 | Poor | Medium hard | 0.75 | 0.442 | 6250 | 14150 | \％ | ab |  |
| 5B3 | 2 |  | Broke．Nearly | y comple | te |  |  | 5 | a |  |
| 5B4 | 2 |  | Medium．Brok | ke（last | cut） |  |  | 5 | a |  |
| 5B5 | 2 |  | Medium．Brok | ke（2nd | or 3rd cut |  |  | \％ | adf |  |
| 5 B 7 | 2 |  | Hard．Broke | （last cut |  |  |  | 5 | atef | 容 |
| $6 \mathrm{B1}$ | 1 | Poor | Medium hard | 0.749 | 0.4406 | 5540 | 12600 | 5 | a |  |
| 6B3 | 1 | Poor | Medium hard | 0.742 | 0.4324 | 3960 | 9200 | \％ | a |  |
| 6B4 | ， | Poor | Medium hard | 0.752 | 0.4442 | 2130 | 4800 | － |  |  |
| 6B5 | 1 |  | Soft．Broke | 2nd cut） |  |  |  | － | adf | 岂或べへ |
| 6B7 | 1 |  | Undersized．N | Tot mach | ined |  |  |  |  |  |
| $7 \mathrm{B1}$ | 9 | Poor | Medium hard | 0.749 |  | $8850$ | 20100 | 1 |  | Q¢wer |
| 7B3 | 9 |  | Broke（nearly | complete | threaded | d） |  | 5 | adef |  |
| $7 \mathrm{B4}$ | 9 | Poor | Medium hard | 0.741 | 0.4313 | 4850 | 11200 | 2 | a |  |
| 7B5 | 9 |  | Harder than flin | nt．Bro | ke（1st o | r 2 nd |  | 4 |  |  |
| 7B7 | 9 |  | Broke（turning | down la | st cut ap | parently | soft） | 5 | adfg |  |
| 8B1 | 3 | Poor |  |  |  |  | $11600$ |  |  | تِّ |
| 8B3 | 3 |  | Hard．Broke | （2nd or | 3rd cut） | to $\frac{15}{16} \mathrm{in}$ |  | 1 | abdg | E |
| $8 \mathrm{B4} 4$ | 3 |  | Hard．Broke | （1st cut | complete | ）just s | arted | 5 | ik | 烒 |
| $8 \mathrm{B5}$ | 3 |  | Medium．Bro | ke（1st | ut） |  |  | 5 | ik | \％ |
| 8B7 | 3 | Fair | Medium | 0.725 | 0.4128 | 4830 | 11700 | 3 | bik |  |
| 9B1 | $1^{*}$ | Fair | Medium hard | 0.748 | 0.4394 | 8525 | 19400 | 4 | bk | 运运 |
| 9 B 3 | $1^{*}$ | Good | Medium hard | 0.750 | 0.4418 | 7100 | 16100 | 4 | bj |  |
| 9B4 | 1＊ | Good | Medium hard | 0.758 | 0.4513 | 11810 | 26200 | 4 | h |  |
| 9B4 | 1＊ | Good | Medium hard | 0.758 | 0.4513 | 12320 | 27300 | 4 | h | 为或50 |
| 9B4 | 1＊ | Good | Medium hard | 0.575 | 0.2597 | 7230 | 27800 | 4 | bj | －0 ${ }^{\text {cod }}$ |
| $9 \mathrm{B5}$ | $1^{*}$ | Good | Medium hard | 0.75 | 0.442 | 9420 | 21300 | 1 | ab | 등ㅇㅇ |
| 9 B 7 | 1＊ | Fair | Medium hard | 0.748 | 0.4394 | 7820 | 17800 | 1 | ab | く吅ご |
| 10B1 | 4 | Poor | Very hard．Br | roke two | blows on | n edge of | f table | 5 | a | อ3¢9 |
| 10B3 | 4 | Good |  | 0.75 | ｜ $0.442 \mid$ | 5120 | 13400 | 1 | ab |  |
| 10B4 | 4 | Poor | Hard | 0.762 | 0.4560 | 2960 | 5900 | 5 | a |  |
| 10B5 | 4 | Poor | Hard | 0.752 | 0.4442 | 4360 | 9800 | 1 | ab |  |
| 10B7 | 4 | $V$ ．poor | Hard | 0.759 | 0.4525 | 3590 | 7900 | 5 | a |  |

＊Method No． 2 used．
joined by a single bead at the bottom of the groove．This method is claimed to prevent slag inclusions and eliminate hard spots in the weld metal．The results of the tests did not confirm the superiority of this method．

It will be noted from Table II that the number of the electrode used has no connection
at all with the number of the plate which was welded by that particular electrode．

In making the welds，the test plates were set up as shown in Fig．7．During the welding operation the characteristics of the arc were carefully observed．The observations are recorded in Table III．A study of this table

TAlBLE VIII
CHARACTER OF FRACTURE AFTER BREAKING SPECIMENS IN TENSILE TEST
（See l゙is．14）
GROU1 1
Fracture partly through the cast iron at right angles to specimen and then along the line of weld．

| 1 （ ） 1 |  |
| :---: | :---: |
| $\therefore$（i5 | 30 per cont throngh cast iron．Wedd metal surface conarse gramular |
| ，（i） | dio per cent．through cast iron．Balance bally bumed |
| 10135 | 20 per cont through cast iron．Large pigeon har spot at erge of weld metal about $5 / 8 \mathrm{in}$ ．Dy $1 / 4 \mathrm{in}$ ． |
| 7131 | T0 per cont through cast iron．Balance bably burned metal |
| （1） 137 | S0 per cent through cast iron．Burned metat lighter than 7131 |
| i） 131 | 50 per cent through a ast iron．Noout 15 per cont hurned metal．Remainder grayish eolor with pockmarks |
| 10113 | 60 per cent through east iron．Batance dark grayish metal |
| （9）135 | 70 per cent 1 hrongh a ast iron．Dark bown spots in weld metal．Filaw in base metal due to undersized bar before turning |
| $5 \mathrm{G} 5$ | 30 per cent through cast iron．Balance poeknarked，cat＇s paw structure |

GROUP 2
Similar to Group 1 except that break through cast iron was not at right angles to the test specimen but rather parallel to line of weld．


## GROUP 3

Fracture at right angles to test specimen and very irregular on the surface．Break at center of weld．

| 8 | B | Coarse granular and full of gas pockets． | Very purous |
| :--- | :--- | :--- | :--- |
| 8 B | Coarse granular and full of gas pockets． | Very porous |  |
| 8 | C 7 | Coarse granular and full of gas pockets． | Very porous |

## GROUP 4

Fracture at right angles to specimen．Surface quite smooth and regular．An ideal tension fracture．

| 3 B 7 | 90 per cent through east iron．Wedd metal rather fibrous |
| :---: | :---: |
| ${ }^{3} \mathrm{~B} 1$ | 80 per cent through east iron．Fine granular spot between cast iron and well metal |
| 3135 | 50 per cent through cast iron． 50 per cent through weld |
| 9）B 1 | 40 per eent through east iron．Remainder dark bluish metal like slag |
| 9 B 3 | 90 per cent through east iron．Balanee weld metal as before．Double fracture．Second fracture 50 per cent complete nearly along line of weld |
| 4 G 3 | 90 per cent through east iron |
| 4 C5 | Uneven break 50 per cent through cast iron． 50 per cent through weld metal．Alternating layers of light and dark metal |
| 4 G 7 | 90 per eent through east iron similar to specimen ！ 133 |

GROUP 5
Break occurred along the line of weld junction showing various degrees of amalgamation．

| 4 B 4 | Pitted surface showing series of warts like bottom of catts paw．1rregnlar |
| :---: | :---: |
| （i） 31 | Blotched appearance with very meven surface |
| 10 B 4 | litted surface but of lesser degree than $4 \mathrm{B4}$ ．Colors of metal darker |
| 6 B 3 | Blotehed dark gray and light gray．Slag ball pulled out of weld metal size of pea |
| 4 B 1 | Blotehed appearance but somewhat smoother than 4 B 4 |
| 9 G 7 | Similar to＋B4．Large slag inclusion size of pea |
| 4 B 7 | Pitted surface．Series of cold spots like a cat＇s paw．Evidently poor amalgamation |
| 2 G 4 | Irregular surface．Cast iron pulled away to some extent |
| 9 G 1 | Pockmarked surface，somewhat smoother than 4 B 4 and 4 B 7 |
| 6 B 4 | Somewhat smoother than 4 B 4 and 4 B 7 |
| 10 B 7 | Same as 4 B 7 |
| 1 G 5 | Same as 4 B 7 |
| 1 C 3 | Same as 4 B 7 |
| 2 G 1 | Quite smooth surface．Somewhat pockmarked．Some light erystalline sections overlaid by a seum of olive drab color |
| 4 B 3 | Blotched appearance．Light gray，fine grained areas intermingled with dark blue and olive drab． Insufficient fusion |

TABLE VIIt (Continued)
BROKE THROUGH THREADS ON FIRST TWO TESTS


#### Abstract

These specimens broke in the threads on two tests with the results as given previously. The third time, the bals were turnet down to inch diameter over the welded section and tested. The fractures are as described.

THIRD TEST


$\because B 3$
i) 13.1
(1) $13 \cdot 1$

464

Same as Group 4. 20 per cent cast iron shows. Batance is filler metal wheh shmws a large dark area ahout 60 per econ of the entire surface. This is cridently a slag inclusion same as ( F oup 4. 'I hrough cast fon at end of filler metal. Ideal consion fracture Simiar to 9 B 3 , (iroup 1. Frachure through cast iron at cond of well, about 2 per cent of weld metal showing. Second fracture 10 per cont complete across east iron
 showing. Sceond fracture about $\overline{7} 5$ per cent complete, 20 per cent horough cast imon. Balaner along line of weld and then 20 per cent held by filler metal
will show that electrodes No. 4. i, and !aded the best and electrodes No. 3 and 6 acted the worst. The time of welding and amount of electrode material used are noted in Tahle 1 .

After the welling operation had been completed the welds were allowed to cool over night in the clamps to prevent any distortion in the cooling.

While cutting the plates into strips preparatory to turning the strips into standard test bars the machinist made the comments recorded in Table V. It should be noted that the G plates welded with electrorles No. 6 and 9 cut the easiest, with No. in next. As to the B plates those welded with electrodes No. 3, 6 , and 9 , and the plate welded with electrode No. 1 but by Method No. 2 cut the easiest, the two next in order being those welded with electrodes No. 1 and 5.

While turning these bars into test specimens with the lathe, the machinist attempted to classify the bars according to their machineability: The results are recorded in the three charts in Figs. 9, 10, and 11.

Tables VI and VII give the results of the tensile strength tests. For the identifying mumbers of the specimens see Fig. \& and Table 11 . Note that bars No. 2 and 6 of each plate are not recorded in Tables VI and VII. These bars are for hardness and microscopic tests which have not yet been completed.

All of the bars which broke while being machined fractured along the line of weld, except the hardest specimens 4 G 1, j G 7 , and a soft specimen is G $t$ which fractured nearly at right angles to the test piece. All of these specimens except the three mentioned showed a weakness which appeared to be due to poor amalgamation between filler metal and base metal. The fracture showed varring amounts of slag, burned metal, and chilled cast iron.

It will doubtless have been noticed that the majority of the tensile specimens listed in Tables VI and VII are approximately three
fourths of an inch in diameter insteat of onehalf an inch as preseribed in the Committer Specifications. This change to a larger diamcter was arlopted by the Committee when it was found that several of the test hars were breaking in the lathe during the process of turning. The four bars :3 $13: 3,3134,9 \mathrm{~B} / \mathrm{I}$ and $f$ G $f$ broke in the threads on two attempts to test them in the tension machine and were then turned down to approximately one-half inch in diameter across the weld section as shown in Fig. 12. These four bars were tested to fracture as shown in Fig. 13. The fractures are described in Table VIII and the grouping is illustrated in Fig. 14 .

The tables giving the results of the Committee's tests are as follows:
Table I gives the chemical analysis of the grades of iron used.
Table II gives the electrode used with cach plate welded.
Table III gives the observed characteristies of each electrode during the welding operation. Table IV gives the data on the time required and the amount of metal consumed during the welding operation.
Table $V$ gives the remarks on cutting the welded plates as made by the machinist.
Tables VI and VII give a résumé of the history of each test bar.
Table VIII gives the descriptions of the fractures of the test bars.
Table IX gives a brief summary of each welded plate grouped according to the electrode used.

## CONCLUSIONS

From a consideration of the results of these tests, the Committee has reached the following conclusions:
(1) That deposition of the filler metal to fill the weld $V$ in a single spiral laver gives a softer but weaker weld than is afforded by depositing the filler metal in a series of parallel layers.
(2) 'That covering the surface of the cast iron with a laver of eloctroxe material followed by a single spiral layer entirely dilling the groove wouk be likely to give a weld having the desired elandeteris! ies (3) That the tests have shown electroules No. 1, 1, 5 , and 9 to give the best results for the 13 iron tests and eleetrocles No. 2 and of the best results for the (ipron tests. (4) That insofar as the variation of cleetrode strength and the personal equation of the operator may be neglecterd, these tests give an indication of the st rength which may be expected from the Varions electrodes.
(9) 'That the reatiness with which cast irom in general can be welded is more or liss dependent mpon the amount of free (atbon present, i. e., the more free carbon there is in the cast iron, the harder that iron is to weld. In fact some cast iron welling jobs are not successful, and yet no account is taken of the character of the casting, but the welling process is blamed for the failure.
(10) That some so-called cast-iron castings are not really cast iron but rather badly burned iron which cannot be welded. Such jobs should not condemn the cast-iron welding process.

TABLE $1 X$
PREPARATION OF TEST SPECIMENS

| Plate | Electrode Used | Wetmiva |  | Machining |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Time (Minutes) | Metal <br> (Ounces) | Cutting <br> (Hours) | Broke in Lathe Specimen Number See Tables VI \& VII | Remarks <br> Hardness |
| 2 B | 6 | 30 | 28 | 3 | 3,4 and 5 | (S) |
| 8 F | 6 | 32 | 27 | 3 | 3 and 4 | (S) |
| 5 B | 2 | 37 | 23.2 | 334 | $3,4,5$ and 7 | (MH) |
| 2 C | 2 | 47 | 27.5 | 312 | 3 and 7 | ( MH ) |
| 4 G | 2 | 52 | 24 | 531 | $\begin{gathered} 1 \text { (1st cut } \\ \text { V.V.H.) } \end{gathered}$ | (H) |
| 6 B | 1 | 41 | 25.8 | 3 | 5 | (MH) |
| 1 G | 1 | 40 | 22.2 | $41 / 1$ | 4 and 7 | (MH) |
| 9 B | 1 | 39 | 23.4 | 3 | None | (MH) |
| 7 B | 9 | 30 | 20.7 | 3 | 3,5 and 7 | (MH) |
| 9 G | 9 | 33 | 22.9 | 3 | 3,4 and 5 | (MH) |
| 3 B | 9 | 3.5 | 23.8 | $82 / 3$ | None | (VH) |
| 4 B | 5 | . 21 \% | 23.0 | :314 | 5 | (MH) |
| 5 C | 5 | 46 | 21 | $3{ }^{3} 1$ | 7 | (MH) |
| 10 B | 4 | 40 | 23.3 | 7 | 1 | (H) |
| 8B | 3 | 41 | :3) | 3 | 3,4 and 5 | $\begin{gathered} \text { (H.S.) } \\ \text { Hardspots } \end{gathered}$ |

(5) That white the Committee was satisfied with the specifications as drafterl, there are several changes which it now feels should be made before other tests are undertaken along these lines.
(6) That in the are welding of cast irom a short, steady are, not over is inch in length, is essential.
(7) That in order to decrease the importance of the personal variable the automatic are welding machine might be used. (s) That the grades of cast iron used by the Committee can be welded, provided reasonable care is exercised in selecting the proper electrode material which is necessary depending upon the amount of free carbon present. The operator must have had experience sufficient to enable him to control his are properly.
(11) That these tests are insufficient in number to be considered as a finished research, but that they are suggestive of further lines of investigation.
(12) That the standard test bar for cast iron should be larger than that prescribed by the American Bureau of Welding, i. e., the Welding Standard for brittle materials shoukd be similar to the test bar recognized by the American Society for Testing Materials.
This test specimen might be lengthened for welding test specimens for the purpose of a clear section to be turned across the weld.

During the process of the investigations, the Committee has formulated several questions which, as yet, have not been satisfactorily and
conclusively answered. An attempt has been made to outline a program of research and the solution of each point has an important bearing on the final conchisions.
(a) What is the correct method of depositing the filler metal to secure a machineable wekl with maximum strength?
(b) Will preheating the wehding surface with a carbon are help in binding the filler and base metals?
(c) What current is best for obtaining the strongest adhesion between filler and base metals?
(d) Does the phosphor-bronze electrode offer any advantages as an antidote for the hard zone?
(c) What advantages are offered by the use of a niekel electrode?
(f) Doesbrushing the surfaceof eachlayer with a wire brush strengthen the weld?
(g) How much is the hardness dependent on the speed of cooling?
(h) Will silicon soften the filler metal in the weld?
(i) Will hammering cach layer of deposited metal while welding increase the strength of the weld?
(j) What is the best way to apply the filler metal to secure the maximum strength, requisite softness, and minimum contraction?
(k) What kind of electrode and what method of welding contribute to least porosity?


Single-operator Direct-current Arc-welding Apparatus for General Use with Alternating-current Supply


## LIBRARY SECTION

Condensed references to some of the more important articles in the technical press, as selected by the G-E Main Library, will be listed in this section each month. Ncw books of interest to the industry will also be listed. In special cases, where copy of an article is wanted, which cannot be obtained through regular channels or local libraries, we will suggest other sources on application.

Arc Welding
Are Welding of Sted Structures. Mtekibloen. F. 1'. Am. If chl Soc. Jour., Feb., 1923; v. $\ddot{\sim}$, 1p. $\ddot{2}+-52$.
(1)engthy illustrated paper showing numerous apptications of electric welding. Includes reference to some welding methorls and projects.)
Electric Are Welding Apparatus and Equipment. Callwell, J.
J.E.E. Jour., Feb., 1923; v. 61, pp. 2533-277.
(Physical features of the iron are as used for welding ferrous metals. Inclules bibliography of 50 entries.)
Cascade Control
${ }^{(1) p e r a t i o n ~ o f ~ I n d u c t i o n ~ M o h u r s ~ i n ~ C o r s c a d l e . ~}$ Cotton, H.
I.E.E. Jour., Feb., 1923; r. 61, p1, 2xt-293. (Theoretical paper.)
Electric Distribution, Underground
Possibilities of Transmission by Underground Cables at 100,000 to 150,000 Volts. Taylor, A. M.
I.E.E. Jour., Feb., 1923; v. 61, pp. 220-252.
(Extensive paper on design. Includes bibliography of 19 entries.)
Electric Motors-Speed Control
Control of the Speed and Power-factor of Induction Motors. Walker, Miles.
Elec'ı, Mar. 2, 1923; v. 90, pp. 216-219. (Serial.)
Electrical Machinery-Parallel Operation
Operating Alternating-current Generators in Parallel. Brown, Ralph.
Pozier, Mar. 20, 1923; v. 57, pp. 435-437.
(Practical considerations.)
Insulating Oils
Maintaining Dielectric Strength of Transformer Oil.
Elec. Rwy. Jour., Mar. 17, 1923; v. 61, pp.
(Describes centrifugal separator equipment for dehydration. Same, condensed, in Elec. IIld., Mar. 24, 1923, pp. 698-699.)
Metals - Testing
Testing of Materials Used in the Manufacture of Electrical Equipment. Dawson, C.
I.E.E. Jour., Dec., 1922; v. 61, pp. 59-64.

## Nozzles

First Report of the Steam-Nozzles Research Committee.
I.M.E. Proc., Jan., 1923 ; pp. 1-22.
(Report of tests and investigations conducted by a committee of the I.M.E. Includes numcrous foot-note references to other articles on steam nozzles.)

## Power-Factor

Improvement of Power-Factor. Kapp, Gisbert. 1.E.E. Jour., Jan., 1923; v. 61, pp. 89-135.
(With the discussion forms an extensive paper of theoretical nature.)
Relays
New Radial Relay Protection. Ackerman, P. Elec. Wld., Mar. 17, 1923; v. 81, pp. 619-623.
(Excess-current relays with current, time and voltage elements to insure selective operation on radial transmission systems.)
Statistics-Electric Railroads
Statistical Data on Electrified Railroads. Bearce, W. D.

Elec. Trac., Mar., 1923; v. 19, pp. 11:3-116.
(Tabulated and other data on comparative costs of operation of steam and electric railroads.)
Thermometers and Thermometry
How to Use Mercury-in-Glass Thermometers. De Baufre, Wm. L.
Power, Mar. 20, 1923; v. 57, pp. 440-443.
(Suggestions for their use in power plant work.)
Vibrations
Production of Noise and Vibration by Certain Squirrel-Cage Induction Motors. Chapman, F. T.
I.E.E. Jour., Dec., 1922; v. 61, pp. 39-48.
(Mathematical study of causes and remedies.)
Vibration in Small Direct-Connected Units. Phillips, H. M.
Pozier, Mar. 13, 1923; v. 57, pp. 398-400.
(Discusses the subject mainly from the standpoint of correct balancing.)

## NEW BOOKS

Construction and Exploitation des Grandes Réseaux de Transport d'Energie Electrique a Trés Haute Tension. Proceedings of the International Conference, Paris, 1921. 1176 pp., 1922, Paris, l'Union des Syndicate de l'Electricité.
Diesel Engine. Orton, A. 111 pp., 1923, N. Y. Isaac Pitman \& Sons. (Pitman's Technical Primers.)
Electricity in Agriculture. Allen, Arthur H. 117 pp., 1922, N. Y., Isaac Pitman \& Sons. (Pitman's Technical Primers.)
Plastics and Molded Electrical Insulation. Hemming, Emile. 313 pp., 1923, N. Y., Chemical Catalog Co.
Practical Tests for the Electrical Laboratory. Johnson, C. H. and Earle, R. P. 347 pp., 1923, N. Y., D. Van Nostrand Co.

Principle of Relativity with Applications to Physical Science. Whitehead, A. N. 190 pp., 1922, Cambridge, University Press.

## Monthly magazine for engineers




[^26]

## THE TREND OF PROGRESS

The Electrical World published a remarkable issue on January 6th of this year showing the progress of the electrical industry. They noted in that issue three milestones in the industry's history.

1. Fifty billion-50,000,000,000 -kw-hr. generated and distributed in the year 1922.
2. One-billion-dollars- $\$ 1,000,000,000-$ energy sale during 192.2.
3. Five billion dollars- $\$, 5,000,000,000-$ of capital invested in the electric light and power industry.
When the age of the electrical industry is considered, these figures stagger the imagination and it must be remembered that even these figures do not give any idea of the gross size of the industry.

The Electrical 1 'orld shows in a very interesting diagrammatic form that the capitalization of the electrical industry reaches the vast total of thirteen billion one hundred million dollars- $\$ 13,100,000,000$-divided as follows:

$$
\begin{array}{cr}
\text { Light and Power . . . . . . . . } & \$ 5,100,000,000 \\
\text { Electric Railways. . . . } & 5,000,000,000 \\
\text { Telephone and Telegraph. } & 2,000,000000 \\
\text { Electric Manufacturing. . . } & 900,000,000 \\
\text { Electric Merchandising . . } & 100,000,000 \\
\hline \text { Total . . . . . . . . . } \$ 13,100,000,000
\end{array}
$$

The capitalization of the electrical industry thus exceeds that of any other industry in the country with the single exception of the steam railways which are capitalized at $\$ 18,000$,000,000.

We shall soon have to get used to figures of astronomical magnitude in comprehending our industry!

These figures are of more than passing interest-they establish beyond doubt the fact that the electrical industry is the greatest, or one of the greatest. economic assets of the country. To what extent this truth is realized is illustrated by the extraordinary fact that
the country's demand for electrical energy is so great that the kw-hr. consumption in the United States doubles each five years! If we still keep the pace this means that we shall generate and distribute one hundred billion $\mathrm{kw}-\mathrm{hr}$. and probably sell two billion dollars worth of energy in the year 1928!

There scems to be no apparent reason why this pace should slacken because in spite of these enormous figures Switzerland, Canada and Norway still lead the United States in point of kw-hr. consumption per inhabitant. It is true that the total kw-hr. consumption in Switzerland, Canada and Norway combined amount to less than one-fifth of our consumption, but there is no reason why our needs per capita should be less than in any other country.

It is only by the most intelligent, constant and hard work that the engineer is enabled to keep abreast of the industry's needs.

In our present issue we publish a number of articles which show the trend of development in many phases of the industry and it is always well to remember that it is the constant work of the inventor and research engineer that is making our progress possible.

The successful operation of transmission lines at 220,000 volts will open up many new fields of development which were not economically feasible at lower voltages. An overall increase in efficiency in our steam power stations, which can be attained only by paying the most careful attention to every detail of design in the entire plant, brings other uses for electric energy into the field of practical applications. And so the story continues-each advance made in getting more out of the material used in the construction of electrical apparatus -and each invention that enables us to do for one dollar what was considered impossible at two dollars a few years ago-
leading us forward in this spectacular mareh of progress.

There are approximately 4000 indlustrial plants in the United States that eath use mone than 12 million kw-hr. of elect rical energy per year and there are approximately i.j million h.p. of electric motors helping to carry our industrial load. Nearly is million of the 21 million houses in the United States are wired for electrical service. Every kw-hr. put into service in these directions is consolidating and extending the economic soundness of the country's position amongst the nations of the earth-and doing its share in shifting the burden of mechanical labor from human shoulders and placing it on the machine.

Every advance made in the generation, distribution and control of clectric energy is enabling our industry the better to play its part in advancing our civilization. It is in this phase of the work that the engineering developments and the industrial research carried on by large industrial corporations of the country are playing such a useful and prominent part. We often feel that the country at large has little appreciation of the benefits they derive from this constant organized effort to create new, and better old, devices designed to convert more abundantly our natural resources to the useful service of man.
J. R. H.

## CARRIER CURRENT

We publish in this issue an article by Mr. A. P. Austin on Carrier Current which describes the apparatus used and the methorl of operating this system of communication. Owing to the importance of this new means of communication we asked Mr. E. P. Edwards, the Manager of the Radio Department of the General Electric Company, to write some editorial comment on this article. His remarks are given below:
"The importance of communication between the various units of a power transmission system is appreciated fully only by those who are responsible for rendering service to the public through that system.
"Even the smaller systems recognize the practical necessity for rapid, accurate interchange of information. Communication is to a power company what the nervous system is to the human body: Electric light, particularly, is 'eyesight' to the public, therefore, unless the nervous system of the power company is in satisfactory working condition, the public suffers directly and immediately.
"These facts will be better realized by the layman when he learns that many of the financial losses, inconveniences and anoyances occasioned by a cessation of power could be appreciably minimized through adequate and infallible communication facilities.
"In its constant endeav or to serve the public through the power company, the engineers
of the General Electric Company have devised a practical method of communication known as the 'Carrier Current' system, which can either supersede or supplement other methods now generally employed. From actual experience gained through practical operation, it has been conclusively demonstrated that 'Carrier Current' is at least as satisfactory as any other system of communication now in use on transmission systems.
"If the power company proposes to install only one means of communication, 'Carrier Current' should be given first consideration, combining, as it does, many of the advantages of other systems with only a few of their limitations.
"Fundamentally, the carrier system makes possible the superimposing of two currents of different frequencies on the same metallic circuit: one of these currents is that normally carried by the transmission line in supplying power and light to consumers; the other is that produced by the carrier current equipment and is used for communication purposes solely, conveying oral instructions and information to the listener with greater clarity and naturalness than is usually possible through means of older systems.
"As would be expected, the method of generating carrier power and the transfer of this power to the transmission system is decidedly different from the methods employed at commercial frequencies."

# Central Station Developments 

By C. W. Stone<br>Manager Lighting Department, General Electric Company


#### Abstract

Mr. Stone points out the general trend of central station development up to the present time and deals briefly with a few future possibilities. He thinks that public utilities in the future may serve the public by the radio broadcasting of entertainments, etc. His article is concluded with some remarks on public utility investments and on "central control" for large power systems.-EDITOR.


The progress in the development of the central station for the generation and distribution of electrical energy has been so rapid that it is difficult to forecast the future.

There have been some very definite steps in the developments of today with which we are all familiar. I refer particularly to the building of power stations for generating alternating current, and placing these stations at points distant from the immediate load, all of which was made possible by the development of motor-generator sets, rotary converters, high voltage transformers, and switching devices. This method of operation has been so thoroughly developed that the writer feels that future developments will necessarily be confined to refinements in the apparatus used, if the systems are still operated in this manner.

The demand for power has been so great that the development of larger waterwheeldriven generators, and larger steam turbines and generators, has been very rapid. One marked result of such development is that power stations are located in places where water is available. This, of course, always applies to water powers, but it has fast become the determining factor in the location of large steam generating stations.

Electrical energy can be distributed from almost any point with very small losses. Coal can be delivered at almost any location. Water for condensing purposes, however, cannot be obtained for other than relatively small powers except in definite locations. This has resulted in the location of large power houses, in many cases, at long distances from where the power is used. and has brought about many long distance transmission circuits at high roltage with many inter-connections between the systems.

It would appear that in the next decade there will be more and more developments of this nature, and more inter-connections between large systems. Such methods of operation have called for the development of larger and larger transformers, steam turbines, and oil switches. The average
size of transformer is about double what it was five years ago. This applies cqually to large switching devices. Steam turbines of $30,000 \mathrm{kw}$. were comparatively rare five years ago, but today are more generally used than almost any of the smaller size machines. While the $30,000-\mathrm{kw}$. turbine was considered large five years ago, machines of $50,000 \mathrm{kw}$. are in operation and some that are even larger are now being constructed

When the alternating-current system of distribution was first adopted, there was no definite standard of frequency. Many systems were installed at 12.) cycles, and others at 133 cycles. Practically all of the systems employing these frequencies have disappeared. Compromise frequencies were adopted in some cases; hence we have still in operation many systems employing $\quad . \quad$. cycles, a few isolated systems employing 40 cycles, a very few employing $331 / 3$ cycles. and one or two employing 50 cycles. However, 60 -cycle frequency has grown in popularity to such an extent that at least 90 per cent of all systems in this country are now operated at this frequency. The standardization of $60-\mathrm{cyc}$ cle frequency has been of great help to both the operating and the manufacturing company, but it has also been a distinct limitation in the development of apparatus, particularly generating apparatus.

The difficulty of making large high-speed turbine generators for 60 cycles has forced us to build generators of either six or four poles, whereas, if it were possible to use frequencies other than 60 croles-preferably higher frequencies-it is probable that safer generators could be built at a considerable saving in cost.

There seems to be no possibility with the large developments which are already in operation to make ant change in the frequencr used for the generation and distribution of electrical power, unless some new scheme for generation and transmission of power is developed.

The possibilities of the development of merenry are rectifiers, or some of the mans other types of tubes, such as those dereloped for radio communication purposes may be the solution of this problem. If suitable tubes were available direct current could be used for transmitting power over long distances. and with the tubes this direct current could be conserted to alternating eurrent at the frequency of the existing distribution service.

The fundamental part of this problem, of course, is the development of the tubes themselves. It is fortunate, however, for all of us, that, if such tubes are available, there will be almost no fundamental changes to be made in the existing transmission systems, as all of these systems could be operated with direct current at the existing voltages, with less chance of trouble on the transmission systems than is now the case with altemating current; and transmission systems will be capable of transmitting at least twice the power which is now transmitted with alternating currents with the same losses; in other words, a transmission system which is good today for $100,000 \mathrm{kw}$. will be capable of transmitting 200.000 kw . with no greater loss, if direct current is used, with greater safety, and with the resultant economies in the fixed charges.

From the data now available we think that large power distribution at voltages above 220,000 volts with alternating currents will not be undertaken for some time to come. The great danger in the use of potentials higher than 220,000 volts for large powers over long distances is, that we may reach a condition of instability which might become so great as to make such systems inoperative.

The high cost of water power development for generating electrical power when added to the cost of transmission over long distances, has brought about a condition where in many cases it is cheaper to generate power by steam and distribute it than to use water power. This situation reminds one of that suggested by Jules Verne when he describes two men, one working to produce a gun which would fire a projectile through any armor, and the other working to improve the armor to resist penetration by a projectile from any gun. The result was that first one, and then the other, was ahead.

If a tube such as that above referred to can be developed to operate successfully with large amounts of power, and power can be transmitted by means of direct current
at high potentials, it would appear that the water powers would beeome more available, and be greater competitors of the steam plant. I anticipate, therefore, that within the next generation we shall see marked progress in the development of such tubes, with the consequent development of more and more water powers.

The success which has been achieved in the development of automatic operation of sulstations, and substation apparatus, would apparently indicate that automatic operation would be applied more generally, not only to substation apparatus, but to generating apparatus as well, particularly in water power developments. A number of such power houses have been put into operation in the last few years.

The developments in radio communication, particularly in broadcasting, have been of only minor importance to the central station $u_{p}$ p to this time. There are somewhat less than 600 broadcasting stations in this country, each one requiring from 500 to 1500 watts, or less than the flat-iron load of a comparatively small city. Although many storage batteries are in use in receiving apparatus, requiring charging at definite periods, the total energy required is so small as to be practically negligible.

It seems as if it would be possible for the public service companies as represented by the electrical generation and distribution companies to furnish to their consumers service similar to the present broadcasting by radio. A definite charge could be made, which would result in making available for entertainment and educational purposes better programs than can be given by any scheme of radio broadcasting which has yet been suggested. The possibilities in this direction seem to be so great that more and more people will become interested in this class of development, with the natural result that something will be brought out to make it possible for consumers to plug into any lamp socket with special apparatus, and listen to any kind of program they may select.

The use of electrical energy has become so general for practically all industry, it would appear that the demand for such power will continuously increase, thus resulting in stabilizing the entire industry.

I think it is generally considered that public utility investments are the most stable investments which we now have. This indicates two things: first, the industry is on sound foundations, and second, the prop-
erties themselves have been financed and managed with great foresight be those who have been responsible for their development

The movement started several years ago for customer ownership of public utility properties has been of great value, not only to the industry itself, but to all other industries. Many people have invested in such securities who previously had never owned any sceurities whatever. They have thus been taught the value of money and the value of saring.

The development of the large central stations, and the many substations which have to be connected, has resulted in a very complex system, difficult to operate except from one central point. Hence we find that all large systems are now operated by means of a load dispatcher similar to the train dispatcher of the railroads, these load dispatchers having under their supervision the operation of all the stations of the system. As the stations become more complex.
and more extended, the difficultion on "peration of such systems berome greater 'Th.load dispateher can don no nowe than to zive by means of telephone or telegraph, orter. which must be executed by where in times of stress, when the communication lines are interrupted, there are bound io bo interruptions in the service, and it will become more and more necessary to have the load dispatcher in a position where he can himself have control of the operation of all switches, stations, and substations. It would seem as if the problem of distant control of apparatus is one of the most pressing which we have before us.

The possibilities in the development of control by means of so called carrier current devices are great. It has been demonstrated that high frequencies can be super-imposed on the existing transmission circuits without in any way interfering in their operation, and such high frequencies can be used for operating the control devices of the systers.

# Problems and Developments in the Control and Interconnection of Power Systems 

Bỵ H. R. Summerhayes<br>Evgineer Lighting Department, General. Electric Company


#### Abstract

The author describes the problems which have to be met and solved when large power centers are tied together into superpower zones. He discusses the general problem as a whole and considers the control of huge volumes of power under both normal and abnormal conditions. He then deals with some of the more important factors essential to a solution of the problems met.-Editor.


The rapid growth of the large city systems with their huge generating stations, the extension of the power transmission lines of the country and their interconnection into networks, and the increase of voltage which has made it practicable to develop remote sources of hydro-electric power and connect them with existing markets for power. have made prophetic observers predict the establishment of superpower systems in various districts of the North American continent and the ultimate connection of these zones into one grand system.

While there are some parts of the country, notably the Pacific Coast and the Southeastern States, where such predictions have been nearly realized, their fulfillment in other districts has been delayed by less favorable conditions and awaits the urge of economic necessity:

In the meantime there are engineerint problems to be solved. In the important industrial districts the intercomection of already large sources of power and the addition of new sources may cause a concentration of power, in case of short circuit, beyond the capacity of existing protective devices. Operating and load despatching methods must be studied in the light of experience and revised to meet new conditions; the requirements imposed on generating, transforming and switching apparatus must be understood and compared with the limitations of such apparatus.

The designs must be changed where necessary and new apparatus designed and developed to meet the new requirements.

Protective systems must be analyzed and compared. limitations of protective apparatus
investigated, and new protective methods and deviers invented.

Chamateristies of orerhead tramsmission lines at high voltage and of great lenget must be determaned, since our engineers will have to deal with tronk lines cartying large amomes of power for very long distances. Preliminary studies in this fied inclicate that in some projects in the near future, involving the transmission of power in large amounts $t 0$ distances of four or five hundred miles, there are problems calling for new methods of treatment.


Fig. 1. Top of $220-\mathrm{kv}$. Strain Tower
In order to connect the urban power centers with each other and with the interstate transmission systems, underground transmission at higher and higher voltage will be required. Intensive development along these lines is already going on.

Finally, the engineers concerned in this work must keep in touch with new developments in electrical science, such as communication or remote control by radio or carrier currents, the possible uses of power tubes, the phenomena of corona, action of the electrostatic field, etc.

## The General Problem

The general problem is to construct $a$ network extending to all power and light users in the district. which shall act as a reservoir of power, from which electric power may be drawn when and as required, at any point in the district, and the power supply must be of the utmost reliability.

It differs from an hydratlic problem, however. in that it is not possible to store electricity as water can be stored in a reservoir. To store electrical energy, it must be transposed into some other form, as the chemical energy in a storage battery or the mechanical energy of water raised to a reservoir by

Clectrically driven pumps. In actual practice, energy stored to meet the varying demand of an electrical power system is stored in some other form ready to be converted into electricity, as in a coal pile, in the heat energy in the water in a steam boiler, in the potential energy of water in forebay and reservoir.

In an electrical network supplied by a number of steam and hydroelectric plants the variations in demand may be classified as short time and long time. Momentary increases in power demand, within the overload capacity of generators running, are met by the immediate conversion of energy stored in boilers and forebay into electricity. Longer time power demands must be met by starting up more generating units, firing more boilers, etc., thus introducing a time element.

In systems employing a number of generating stations widcly separated, it is the natural and logical practice to meet a local demand by supplying the power from the nearest generating station, or stations, since that involves the least loss in transmission; this policy may be modified by the presence of more efficient generating sources at a distance, or by the requirement of storing at one point and using available stream flow at another point.

On a large system with many generating stations widely separated it is obvious that the control of the system by one load despatcher must produce the best results, and that such control requires a system of communication as reliable as the transmission system itself.

The telephone communication on some systems has already been supplemented by the use of radio and carrier current. It seems quite possible that in the near future radio and carrier current methods will become the main reliance for the load despatcher with the telephone used as an auxiliary. It is not the purpose of this article, however, to consider the means of communication used.

The control of such a system may be considered under two heads:

Control under normal conditions.
Control under abnormal conditions.
In the present state of the art, and for several years to come, such a system will usually consist of:
(A) Steam electric generating stations in large cities and towns.
(B) Steam electric generating stations located for cheap fuel and ample condensing water, at a distance from centers of population.
(C) Hydro-electric generating stations.
(D) Trunk or feeder transmission lines connecting the important generating stations with the important distributing centers and with each other, at 2.20 kilovolts.
(E) Main transmission system, at 110 kilorolts or 66 kilovolts, radiating from the distributing centers, and interconnected into a network.
(F) Distribution lines at various voltages from 33 kv . down to 2300 volts.
(G) Substations on Class D, E, and F lines.

## CONTROL UNDER NORMAL CONDITIONS

## Load Control and Interchange of Power

When a single generating station is supplying power to a load at the terminus of a single line, the conditions are quite simple. the line drop may be readily calculated and the amount of power which can be carried by the line with a certain transmission loss and drop of voltage is easily obtained. When, however, two systems are tied together with the idea of exchanging power in either direction, the problem becomes somewhat more complicated. If a single tie line is used, or multiple lines passing over the same route, the amount of power transferred from one system to the other, the power may be regulated by adjustment of the governors on the prime movers of the two systems. The voltage at the various generating stations, however, may be fixed by local load conditions. The kilowatts transferred over the tie line depend on relative phase angle, which is obtained by adjustment of the governors, but the kv-a. and wattless component depend mainly on the relative voltage.

The sending stations must have a greater voltage than the receiving stations in order that the sending stations may carry the wattless component of the load as well as the watt component. Of course, this requirement may not always be necessary, as for instance, when the receiving station needs power but is short of water. In such a case one or more generators of the receiving station may be operated with just enough water passing through the wheels to take care of the losses and these generators may supply the wattless component. Steam generators are also run in the same way as synchronous condensers. There are cases,
however, where due to loreakiown of the generating equipment the receiving station needs to receive electricity in quantity and quality to carry all of its normal load, that is, it needs to get the wattess component as well as the watt component and at the proper roltage to supply its load. In such a case the sending station must supply the wattless as well as the watt component of


Fig. 2. Medium Capacity Synchronous Condenser, 8 poles, $1500 \mathrm{kv}-\mathrm{a} ., 900$ r.p.m., 4000-2300 volts
the load, and if its roltage cannot be raised the voltage ratio must be varied somewhere along the line, usually in a bank of transformers, or by regulators, so as to force the wattless as well as the watt component over the line.

When power is to be exchanged in either direction, this requirement, which is often overlooked involves the provision of means for varying the voltage over quite a wide range. When station " $A$ " is sending power and station " $B$ " receiving power, the voltage at the " $B$ " end of the line must be lower than at the "A" end and when station "B" is sending power and station "A" receiving power, the voltage at the " $B$ " end must be higher. This applies for ordinary short distance transmission where it would not pay to put in large synchronous condenser capacity so as to transmit always at 100 per cent power-factor.

When two systems are tied together by two or more lines, which because of passing over different routes, or for other reasons. are of different reactance and resistance, and

When the situation is complicated by the tapping off of load at intervals, still other means of regulation must be provided, since in this case it is necessary to see that each line carries its proper share of the load. For one line a greater difference in phase angle may be required than for the other line to make it take its proper share of the load. The total load exchange between the two systems is fixed by the adjustment of govemors at the station, that is to say, by the average difference of phase angle which exists between the stations on one system and that on the other; the relative amounts passing over each line are determined mainly by the relative impedances of the lines and chicfly by the reactance. In order to make each line justify its investment by carrying its proper share of the load and of the wattless. current, it is necessary to have means of controlling the phase angle and the voltage of the two or more lines independently, so that power may pass in either direction, properly divided over the two lines; also, the wattless component should be properly divided.

In order to accomplish the proper distribution of power, current and voltage, several methods are available. The proper use of these methods will depend upon the conditions of the problem, that is to say, the amount of power to be transmitted, differences in voltage and phase angle, line drop voltage, etc. For instance, if the tie is a long distance transmission line, involving a large line investment, it may be necessary for economical reasons to transmit power at 100 per cent power-factor, in which case large synchronous condenser capacity would have to be installed at both ends of the line to take care of the wattless component of the load, since either end may be the receiving end. If, however, the tie is a relatively short line, but possibly of high reactance drop, because of the presence of transformers, reactors, etc., the installation of large synchronous condensers at both ends may not be justified and the situation would be more economically taken care of by the use of regulators, or a wide range of voltage obtained by taps on the transformers.

## Single Line Voltage Control

When the tie between load centers consists of a single line, there is only the voltage problem to be considered and this may be taken care of by taps on the transformers, synchronous boosters or single-phase induc-
tion regulators. The single-phase regulators give a boost or buck of voltage in phase with the applied e.m.f. and are usually cheaper than synchronous boosters. They are also more desirable for other reasons, notably that the regulator is not a continuously running machine, will stand heavier short circuit currents and can be designed for outdoor service.

For high voltages the regulator becomes somewhat cumbersome, since it is limited in voltage by its construction and must, therefore, be supplemented by series and shunt transformers to translate the efforts of the


Fig. 3. Large Capacity Synchronous Condenser (12 poles, $25,000 \mathrm{kv}-\mathrm{a} ., 600$ r.p.m., 11,000 volts) with Connected Exciter and Induction Motor for Starting and Line Charging Purposes
regulator into terms which can be understood by the high voltage circuit. For circuits of large power and voltage, therefore, it seems probable that the regulator will be often supplanted by some form of tap changing device on transformers. It is probable that on most existing tie lines between systems not enough attention has been give to the variation of voltage required by the interchange of power in either direction, and there are many places where this interchange over existing tie lines would be greatly facilitated if proper range of voltage ratio had been provided in the transformers, or if some voltage changing device could be added.

## Multiple Lines Voltage and Phase Angle Control

Coming now to the case where two systems are connected by multiple lines of different reactance and resistance, we have both the problem of proper change of voltage ratio for power in either direction and proper change of phase angle and voltage ratio relatively between the two lines. One solution would be to employ single-phase voltage regulators to take care of the voltage differences in either direction and three-
phase rexulators to take care of the phase angle. Another method would be the use of synchronous boosters with motor-driven devices for adjusting the stator angles. Probably the prettiest solution consists of two three-phase regulators in series in one of the lines, or the equivalent of one three-phase regulator in each tie line. This arrangement


Fig. 4. Large Induction Voltage Regulator of the Water-cooled Outdoor Type
permits the relative adjustment of both voltage and phase angle through a very wide range.

Here again, however, the regulator becomes somewhat cumbersome and expensive when applied to high-roltage systems, on account of the necessary series and shunt transformers and we come again to a transformer tap changing method as the cheapest arrangement, although possibly not quite so convenient in operation as the regulators. By suitable combinations of two transformer windings per phase and two sets of taps, it is possible to adjust both voltage and phase angle independently and thus meet the
requirements of parallel tie lines of dmerent voltage and ractance to divide the loand properly.

Having provided a suitable range in the transformers to take care of voltage adjustments, so as to allow for exchange of power in either direction and for different voltages on parallel lines and having provided suitable combinations of transformer windings to obtain the phase angles required for division of load between lines, we come to consideration of how the transformer taps should be changed. If the load can be thrown off the line while the change is being made. the matter is simple. Only ratio adjusters are nceded. In usual practice, however, and in order to maintain the best condition. it is desirable to have the voltage follow changes in load and consequently the most convenient operating arrangement will be one permitting the changing of taps without interrupting the load. There are several methods of doing this, which are applicable under various conditions. It is impossible to say that one method is the best for all conditions. An arrangement suitable for one set of conditions, such as voltage, current, number of taps, frequency of change desired, would not be the cheapest under other conditions. All of these methods, however, are usually cheaper than regulators, but operate in much coarser steps and are not capable of such fine adjustment. Some of these arrangements are as follows:

First. A transformer may be provided with parallel windings, that is to say, two windings for each phase, with switches arranged so that half of these windings may be cut out, throwing the load on the other half while the taps are being changed. The changed winding is then cut into service in parallel with the other, which is in turn cut out and changed. This method is well adapted to circuits of large power, since on a large transformer the windings may frequently be in multiple anyway, or that provision of multiple windings does not mean a great increase in expense. The taps, however, always mean additional expense. It is obrious that while one winding is cut ont the other winding must carry the entire load, that is to say, double rating of the winding for a short time, but this is not a great objection. It is apparent that after one winding has had its taps changed and is thrown into parallel with the other winding not changed, there will be a circulating current, but this condition is also temporary and
means that the steps must not be too far apart. It is perfectly practicable to make a ${ }^{5}$ per cent change on all ordinary transformers of the usual reactance. The switehing and tap changing devices should be: properly controlled and interlocked for safety and convenience of operation, all three phases being operated at one time.

Sciond. If one winding of a transformer bank is delta connected, instead of using double windings it may be simpler to install switches to open consecutively each side of the delta, leaving the line tied to the remaining two sides of the triangle in open delta. While each side of the delta is open, its taps are changed by the ratio adjuster.


Fig. 5-a. Drum Type Ratio Adjuster Mechanism

Third. The taps of each winding of a transformer bank may be brought out to an insulated switch which operates to change the taps without interrupting the load flowing through the transformer bank. In order to do this, it is necessary while changing taps to short circuit a portion of the transformer winding through a reactor, resistor or auto-transformer. There are quite a variety of schemes of this general nature varying in details. For instance, under certain conditions of current and voltage the switching from tap to tap may be done in air. Under other conditions, under oil. The switching may be done by a drum controller, hand or motor operated, or by contactors operated electrically or from a cam shaft. A few of these schemes have been worked out and some are in actual operation.

Referring to any one of the above three general methods of changing taps, the extra complication in cost involved will usually be found to be well justified by the increased availability of the large tie line investment to carry its proper load and current in either direction and under all conditions.

The use of such devices is independent of the use of symehronous condensers, which may, however, be used to accomplish the same purpose, although put in for other reasons. It is quite possible that in many cases a combination of such voltage changing devices and synchronous condensers will be found advisable.

Another method of causing the load to divide properly in two parallel lines of unequal impedance is that suggested by Mr. John C. Parker of the Brooklyn Edison Company, which employs two series transformers, one in each line, with their secondary windings connected in multiple. Each series transformer is of a size approximately equal


Fig. 5-b. Dial Type Ratio Adjuster Mechanism
to the line current multiplied by half the difference in impedance volts between the two lines. This arrangement functions entirely automatically, but must be short circuited when one line goes out of service. It can be extended to any number of parallel lines.

## Automatic Generating Stations and Substations

In a large power system, containing a number of hydro-electric and steam stations, the diversity of power demand and the large steam reserve will permit the installation on low head streams, where effective water storage would not pay, of hydro-electric plants using a large proportion of the maximum stream flow.

For such plants full automatic operation, or automatic operation supplemented by remote control will be particularly attractive, since a generating station whose output follows $t$ ie steam flow will operate at partial loads for long periods, and it is desirable to keep the cost of attendance as low as possible.

In the full automatic station the starting and stopping, connecting in and disconnect-
ing, load control, voltage control and protection are entirely antomatic: the number of machines in service is usually controlled by rariations in the water level.

When remote control is added it may be used merely to determine the number of machines in service; but if desired may be extended to cover all the automatic functions except protection, and to include switching of lines.

During 1922, a $5000-\mathrm{kr}-\mathrm{a}$., 6600-volt hydroelectric gencrating unit under full automatic control by a time clock or float switch was placed in operation by the New England Power Company.

In New York Sitate, for instance, nearly 70 per cent of the power generated is at -.) cyeles and somewhat less than 30 per cent at 60 eycles, the remainder leemg mostly at 40 eycles. It is, of conrse, expected by engincers that the main super-power stations for this vicinity, as well as for the rest of the country, must be at (if) cyeles and a great deal of the future extension of the present 2.)-cycle systems may be at 60 eycles. The standard European frequency (of) eycles) is in use in Southern California, 30 cycles in parts of Michigan, 40 cyeles in the vicinity of Albany, Schencetady and Troy, with some isolated cases elsewhere. There are a few


Fig. 6. Cam Type Tap Changing Switch for $525-\mathrm{kv}-\mathrm{a}$. Three-phase, 7000. 12,000. 445-volt Transformer

A remote control unit of $11,7.50 \mathrm{kv}-\mathrm{a}$, 13,200 volts was installed on the system of the Washington Water Power Company.

Devices familiar in antomatic telephone and printing telegraph scrvice have been applied to remote station control, utilizing not over four pilot wires, which serve also to bring back indications of the operation of devices in the controlled station.

An application of this method has been made in two of the a-c. switching stations of the Eastern Massachusetts Electric Company. It is well adapted to the control of unattended switching or sectionalizing stations on transmission lines, as well as to stations containing running machinery.

The near future will, no doubt, see carrier current methods applied to similar work.

A notable installation of automatic substations has been made for the Kansas City Power and Light Company where the entire Edison system of $15,000 \mathrm{kw}$. will be supplied from five automatic stations, each containing two 60 -cycle synchronous converters.

## Frequency Changers

In the interconnection of power systems there will be some cases where difference in frequency must be taken into account.
instances where in order to obtain a slight advantage in the cost of frequency changers 021,2 cycles has been adopted, so as to get frequency changers of 37.5 and 750 r.p.m., instead of 300 r.p.m. which is the highest speed available for 60 to 25 cycles transformation. The great bulk of frequency changers in use are of the synchronous type, that is to say, synchronous machines on both ends. In this type when used to tic two systems together the maximum kilowatts transmitted must go through the shaft and is equal to the maximum kilowatt output of the generator. A short circuit on one system, involving a heary output of reactive kr-a., from that end of the frequency changer may not draw very much porier from the other system, since the current to a short circuit is largely reactive and the torque on the machine and output of the motor may be less than full load. This is an advantage in one respect, since a short circuit on one system does not pull down the voltage on the other but becomes a disadvantage when synchronous converters supplied from both systems are operating in parallel in the same substation. In this case it is desirable to have the voltages of both systems droop.

The cascade fom of irequeney comberter, consisting of a symborons machane of 2.0 cyeles, 300 r.p.in., coupled to a botecte induction machine has been developed w meet the requirement of at tie between two systems, wheh will include the feature of direct transomation from one system to amother. In this set the stator of the o.jofele machine is comnected usually through

Fior a tic between two systems of different frequencies, it is sometimes required to focate the frequeney changer at a substation distant from generating stations of either system. To regulate the amount of power passing through a synchronous frequency changer woukd refuire constant communication between the frequeney changer station abl the various generating stations. This


Fig. 7. Ratio Adjuster Type Tap Changing Mechanism for $20,000-\mathrm{kv}-\mathrm{a}$., Three-phase, 44,000 -volt Transformer with Parallel Windings. One revolution of handwheel changes taps one step on both windings, the load being carried by one winding while the other is being changed
a transformer to the collector rings of the rotor of the 60 -cycle induction machine having fourteen poles. Tiventy-five cycles flow through the rotor and 35 cycles is added by rotation, producing 60 cycles in the stator. The 2.j-cycle machine provides excitation for the 60 -crele induction machine, which operates at 100 per cent power-factor as far as the 60 -cycle system is concerned It is even possible to over-excite, so as to have the 25 -cycle machine compensate for poor power-factor of the 60 -cycle system, and if it were not for the fact that the induction machine has to be made larger to carry these wattless currents, there would be some advantage in doing this, since 25 wattless $\mathrm{kv}-\mathrm{a}$., produced in the 25 -cycle machine will become 60 wattless kv-a., in the 60 -cycle system.
difficulty can be overcome by installing an inverted 25 -cycle synchronous converter in series with a 60 -cycle synchronous converter, but the induction set is probably a more stable combination, although there is not much difference in the cost and efficiency.

## VOLTAGE AND POWER-FACTOR

## Generator Regulators

In power stations in large cities supplying current to an alternating-current distributing system through a large number of feeders, with each feeder capacity relatively small compared to the kilowatt capacity of the generators, generator voltage regulators have been seldom used in the past.

On the other hand, in large hydro-electric generating stations, which usually supply power through a few transmission lines of large capacity relative to the capacity of the system, generator voltage regulators are in common use and are really required for good service on account of the large proportion of load which is lost if one line is lost. In a few of the large city stations where the


Fig. 8. Interior View of the 187,000 -volt Oil Circuit Breaker, Tank Removed
load varies in large increments, for example Pittsburgh supplying a steel mill load, and Philadelphia a railroad electrification, generator voltage regulators have been found necessary. They will probably be more extensively used in the future in the large steam stations as interconnection with other systems takes place, since with the regulator the synchronizing power and stability of the system are improved.

## Synchronous Condensers

Synchronous condensers are generally used for the control of power-factor and inter-
linked with this is the comtrol of voltage at substations. On long high voltage transmission lines the line investment is so high that it must be utilized efficiently and a comparatively large investment in synchronous condensers is not only justified by this requirement but necessitated by the fact that without the synchronous condenser the voltage regulation wonld be so bad that the electricity at the receiving end would not be practically useful. On shorter lines, many companies are now getting away with rather poor voltage regulation and inefficient transmission, where it would not take very close figuring to show that the installation of synchronous condensers would be justified. In the case of a transmission network, a conception of the effect of synchronous condensers may be obtained by imagining a tarpaulin spread over a field and supported on various posts which are the generating stations, the canvas sagging to a lower level between the posts, representing lower voltage. At any point where the sagging is too much, another post may be put in by installing a synchronous condenser which boosts the voltage in that neighborhood. By regulating the field of the condenser, the voltage may be held constant with variation of load, that is to say, we have an adjustable post which we can raise up as more water falls on the tarpaulin.

It has been frequently suggested that synchronous boosters could be used to control the voltage of a system. While the synchronous booster may have some field when used in conjunction with a synchronous condenser, that is to say, where voltage control is more important than full power-factor control, the synchronous booster has never been able to compete when used alone with the induction regulator.

As explained in the paragraph under "Load Control" a wide range of transformer taps is necessary on transformers forming a tie between two systems where power is interchanged in either direction, in order that the power-factor of the load exchanged may be properly controlled.

## CONTROL UNDER ABNORMAL CONDITIONS

Abnormal conditions may be considered under two headings:

Excessive currents.
Excessive voltages.

We are able to calentate quite closely the mechanical and thermal effects of excessive currents and are learning how to provide for them in our designs.

Excessive voltages, however, are not so well understood. They are more erratic in their appearance and effeets and a great deal of investigation is necessary before we can be so sure of our factor of safety as we are agrainst excessive currents.

## Excessive Currents

The current existing in a short circuit is the voltage divided by the impedance, very easy to calculate in a simple circuit, excectingly difficult to calculate in a network supplied from several sources of power. The difficulty of such a calculation has led to the use of calculating tables, in which the network with its generators, transformers. lines, etc., can be represented by resistances through which direct current is passed and a short circuit being made at any point, the currents flowing to the short circuit may be measured at all points desired. This method of calculation has proved so useful in studying power systems that no less than sixty important system studies were made on the calculating table of one manufacturer during the period of a year. Several of the large transmission systems, notably the New York Edison Company, Alabama Power Company, New England Power Company. have their own calculating tables.

To make a complete study of the flow of current, including power-factor, single-phase short circuit, etc., would require a much more complicated miniature system, in which three-phase lines could be used and reactance, resistance and capacitance introduced, but for the purposes of determining the proper size of switches and reactors and the setting of relays, most problems can be solved on the miniature system consisting of the directcurrent calculating table.

Haring determined the r.m.s. alternating current flowing at various points, the next step is to calculate the peak current on the first cycle, including the direct-current transient usually present on short circuits. This peak current determines the mechanical shock to the apparatus, which must be designed to stand such currents with suitable factor of safety. There have been many failures of electrical apparatus because it was not well understood that the mechanical strains depend on this peak current.

The designer must then take account of the thermal effects due to the short circuit. A very conservative rule would be to make apparatus connected in series with an underground cable so that it would stand without injury the same overloads of short duration as the cable itself, in case a circuit breaker fails to open immediately.

To apply this same rule to apparatus connected to overhead transmission lines may be beyond good judgment.

When it is realized that the mechanical effects in a large transformer may amount to many tons attraction between the windings, and that the thermal effects due to short circuit currents in circuit breakers have been known to in jure the apparatus in less than half a second, the problem confronting the designer of apparatus connected to a large transmission system may be appreciated. The simple way to avoid these problems would be to segregate systems instead of interconnecting them, but the economics of the situation appear to demand interconnection. The engineer is then forced to use current limiting reactances to cut down the concentration of power at any one point.

Current limiting reactances have been widely used on systems below 15,000 volts and are now coming into use on systems of 2.,, 000 volts. A few have been built for 60,000 volts. As the interconnection of power systems progresses, the current limiting reactors are likely to be widely used on high tension systems, although engineers have so far ingeniously avoided their use by careful placing of transformers, etc.

On a high tension system where the mechanical effects of the peak current on the first cycle may not be important, but where it is desired to limit the current in order to reduce rupturing capacity of circuit breakers, etc., there is available a device known as the saturated core reactor, which under normal conditions up to full load interposes only 10 per cent reactance, but at times of short circuit becomes 35 to 40 per cent. There will probably be a field for this in reducing the cost of high tension circuit breakers at important power centers.

## Automatic Operation

On moderate voltage distribution systems, the use of automatic and remote control substations and of automatic reclosing switches in manual substations, has become
quite common and such stations have proved their worth in service.

In the interconnection of large power systems operators will probably be required in the important switching centers, which may involve a large investment in switching apparatus and possibly in regulating apparatus: but automatic operation, such as automatic reclosing of switches, may soon be introduced in such stations.

In the recent development in oil circuit breakers, involving the elimination of oil throwing, the use of improved test facilities by the manufacturers and important service tests have enabled the designers to obtain more exact knowledge of the operation and basic principles of oil circuit breakers which are now being made safer and more certain in operation and with a better known factor of safètr.

Oil cirsuit breakers have been built for rupturing capacity of one and a half million kw . To form a better picture of what this means call it two million horse power or 1100 million foot pounds per second.

Power may pass through the circuit breaker at this rate from the time the short circuit is established till it is interrupted, say, onefifth of a second or 220 million foot pounds or enough power to lift 110 tons 1000 feet.

After the circuit breaker contacts part, however, the job is done quickly, one cycle on a 60 -cycle circuit being a good time performance.

During this one sixtieth part of a second, there may be absorbed in the circuit breaker about one million foot pounds, enough to lift a ton 500 feet.

## Relays

The general principle in the design of relay systems is to consider the component parts of the system in as small units as possible and arrange the system of relays so that an accident to any part of the system whether a piece of apparatus or a section of line, will.
by the excessive currents flowing, isolate that part of the system without interrupting service on any other parts. This general principle is simple enough, but its application on a power network is often difficult and limited. Service interruptions have, however, been largely done away with by modern relay systems and by grounding the neutral. Grounding the neutral provides a determined flow of current to any fault and simplifies the task of the relay engineer.

## Excessive Voltages

Excessive voltages at fundamental frequency in case of an accident at any point of the system are best prevented by the use of a vibrating regulator. Rheostatic regulators are usually too slow to take care of the sudden voltage rises when a large part of the load is thrown on.

Excessive voltages, due to transient sources, steep wave fronts, inductive effects from lightning, etc., are present on every system and are best taken care of at present by lightning arresters of the electrolytic, or other type, having a large discharge capacity and action within half cycle. Such voltages, however, may be present at various parts of the system, since lightning arresters cannot be located everywhere, and allowance for these voltages has had to be made in the design of apparatus from the experience of the designers. This matter has been mostly empirical and while a great deal of work has been done in the determination of such voltages, a great deal more remains to be done. This is a field towards which many investigators are directing their efforts. Practical experiments on systems during the next few years will result, we hope, in more exact knowledge, not only of the voltages which exist on systems, but their character, duration, and their effect on insulation.

# Large Power Transformers 

By W. S. Moony<br>


#### Abstract

The design and problems of transformers is of vital interest to all responsible for the transmission and distribution of electric power. Mr. Moody has had vast experience, over many years, in designing transformers and in this article he gives our readers data which will enable them to understand the manufacturer's problems as well as help operating engineers to a better understanding of the solution of their problems.-EDITor.


Due to the constant and rapidly increasing demand for electrical energy, largely resulting from the great increase in the cost of coal. generating stations having very large outputs are being built. The use, therefore, of large units for the generation, transmission and distribution of this energy is necessary for the sake of economy, first, in the cost of the apparatus, second, in that the best operating efficiencies may be obtained, and third, in the number of units used.

In the case of the static transformer, which is such an indispensable part of the transmission and distribution equipment, the ques-


Fig. 1. Curve Showing Yearly Increase of Maximum Potential for which Power Transformers Have Been Built
tion of cost becomes more important as the voltage rating becomes higher. In a paper published in 1912, the writer pointed out that since the first attempts in 1892 to transmit power over any considerable distance, the art of transformer building had progressed commercially in voltage limits at a rate of approximately 10,000 volts per year. The writer then predicted that progress in that respect was likely to keep on at about the same rate. Fig. 1 shows the actual progress to date. It will be seen that the prediction has been well confirmed, except for lack of progress during much of the "World War" period. However, this temporary retardation, it should be noted, has been made up.

There is a common misconception that when high voltages, capable of transmitting power economically over 250 to 500 miles, are used, every hamlet along the way can have electric power. The cost of transforming at such high voltages is far too great to make it commercial to supply small customers unless there are enough of them so situated that they can be collected into a unit of service on some much more moderate voltage. Often the demand is so scattered as to require three successive transformations before the individual user is reached.

Fig. 2 shows the relative cost per kv-a. of sclf-cooled transformers of different sizes designed for different voltages. The portion of the curve where the cost per kv-a. takes a


Fig. 2. Relative Costs per Kilovolt-ampere of Transformers of Various Sizes and Voltages
rapid upward turn indicates the minimum size below which it is not usually economical to go, and it will be noted that the higher the voltage the larger is the size at which this occurs. Thus, if for comparison, we compare the points where the curves have a 30 deg. slope upward, we find that this occurs at $1500 \mathrm{kv}-\mathrm{a}$. on the 6600 -rolt line, $3000 \mathrm{kv}-\mathrm{a}$. on the 44,000 -volt line, $4500 \mathrm{kr}-\mathrm{a}$. on the $88,000-$ volt line, and $7500 \mathrm{kv}-\mathrm{a}$. on the 150,000 -volt line. Small units must therefore be avoided by combining the demand at a lower voltage until there is sufficient to use the high voltage without excessive transformer cost.

The lowest economically permissible kv-a. limit becomes higher as the voltage increases because that vital and expensive part of a high-voltage transformer, namely, its insulation, is almost constant in cost regardless of size. The relative cost of the major insulations of 150,000 -volt transformers is shown in Fig. 3 where, it is interesting to note, the cost of the insulation of a $1000-\mathrm{kr}-\mathrm{a}$. transformer is as much as 50 per cent of that of a $10,000-\mathrm{kr}-\mathrm{a}$. transformer. Fig. 4 gives the cost of insulation proper in per cent of the total cost of the transformer. Although these curves alone would be sufficient argument in themselves, there is the further fact to be considered that the insulation proper is only one part of the excess cost entailed by high voltages, and that the excess cost due to larger size of tank, core, coils, clamps and oil necessitated by larger clearances demanded for insulation are also chargeable against the cost of high voltage.


Fig. 3. Relative Cost of the Major Insulation of 150.000 -volt Transformers in Per Cent of that of the $10,000-\mathrm{kv}-\mathrm{a}$. Unit


Fig. 4. Cost of Insulation Proper of 150,000 -volt Transformers in_Per Cent of Total Cost of Transformer

Since large (i.e., power size) transformers have practically the lowest cost at 6600 volts, we will take the cost of the 6600 -volt self-cooled line as a basis and show in Fig. 5 the excess cost of 150,000 volts in various $\mathrm{kv}-\mathrm{a}$. sizes expressed in per cent of the cost of the


Fig. 5. Excess Cost of 150,000 -volt Transformers Above that of 6600 -volt Transformers in Per Cent of Cost of the Latter
corresponding bifoo voht unit. It is interestingr to bote that $1.00,0000$ vehte costs about ös per

 higher at still smaller capacitios.

Minimmon sizes used on any voltage should therefore be well beyond the gone where the cost perkr-a. increases raphidly". 'loansfommers


Fig. 6. Transformer Efficiencies at Various Loads. Single-phase and three-phase lines of 220,000 -volt Transformers
for the highest operating voltages such as 220,000 volts should preferably be above $10,000 \mathrm{kv}-\mathrm{a}$. per phase.

Aside from the advantage in cost in favor of larger sizes there is also an advantage in efficiency in favor of the larger sizes as shown by the efficiency curves for a line of $220,000-$ volt transformers given in Fig. 6.

In the past few years there has been a more rapid growth in the size of self-cooled transformers than in water-cooled transformers. This is largely due to the development of economical and compact means of dissipating the heat from large self-cooled units.

The losses in the coils and core of a transformer vary approximately as the cube of the dimensions, while the radiating surfaces of the coils and core as well as the surface of the containing tank vary as the square of their respective dimensions. As the size of a transformer is increased, it is evident that a point is soon reached where it is necessary to provide additional surface on the tank by means of corrugations or other irregular outlines. The difficulty of obtaining sufficient surface, particularly on the tank, and still maintaining a strong mechanical structure was for years the principal factor in limiting the growth of large self-cooled transformers. This problem has now been satisfactorily solved by the use of tanks with external tubes where shipping clearance
will pemit or separable radiators when the dimensions are loo great to permit shipping the complete unit. Selfeconded transformers of moderate voltage may be shipped comphetely assembled in their tanks, filled with , if, ready for installation in sizes up to about 5000 to $\overline{6} .00 \mathrm{kv}$-a. Larger and higher voltage transformers may require the removal of the rathators for shipment and extreme sizes may recpuite that the transformers be removed from their tanks for shipment.

Fig. 7 shows the relative growth in size of self-cooled and water-conled transformers for the period from 1906 to 1923 . The curves were prepared from the records of transformers louilt by the Gencral Electric Company, but it is believed that they are sufficiently representative to show the general record. It will be noted that up to 1907 the largest selfcooled transformer was $500 \mathrm{kv}-\mathrm{a}$. while the largest water-cooled transformer was 7.500 $k \mathrm{r}-\mathrm{a}$. or fifteen times as large. At the present time the largest self-cooled transformer is $15,000 \mathrm{kv}-\mathrm{a}$. while the largest water-cooled transformer is $25,000 \mathrm{kv}$-a. or only 66 per cent larger. Sclf-cooled transformers can be built cconomically and compactly in even larger sizes when requirements make them desirable.

As both self-cooled and water-cooled transformers may now be built for any desired output, the operating engineer is afforded a free


Fig. 7. Relative Growth in the Size of Self-cooled and Water-cooled Transformers
choice of either of the two types. There will be several factors affecting his choice. If water-cooled transformers are desired, there is required, for a large installation, quite a large supply of water sufficiently pure not to corrode or clog the cooling coils. The extra cost of the water and pumps, if required, must be considered, as well as the possibility of
water freezing in an outdoor transformer in severe climates. A self-cooled transiormer will occupy more floor or ground space and, if indoors, it may sometimes be difficult to provide proper ventilation. However, the self-cooled transformer will normally have higher efficiencies, while the water-cooled unit has the advantage in first cost. Fig. $\delta$ gives the cost of water-cooled transformers expressed as a percentage of the cost of self-cooled transformers. This curve is intended to show merely the trend and should not be used to cover specific cases, as the difference will vary not only with the kv-a. rating but also with the voltage and other special requirements which may have to be fulfilled.

Having decided on the method of cooling, there are certain features which, while important to consider in the choice of any transformer, should be given special consideration when one is to purchase a large unit, and particularly in a unit designed for high voltage. The most important of these features are:

1st. The magnetic core should be rigid and capable of supporting not only itself but also the major insulation and windings against all possible abnormal stresses, as for instance, short circuit forces.

2nd. Windings should consist of cylindrical or disc coils, and for very high-voltage transformers they should be arranged concentrically, not interleaved.

Srd. Major insulations should furnish rigid support to windings and have ample strength to withstand stresses accompanying short circuits.


Fig. 8. Water-cooled Transformer Cost in Per Cent of Self-cooled Transformer Cost

4th. Taps should be avoided, but if they must be used, they should be located as far removed from the line connections as possible and so as not to cause any magnetic unbalancing.
.ith. The tank construction hould be very substantial and such as wedede air.

The following discussion finws how these. features are applied to standard (ieneral Elece tric practice:

First. The magnetic cores should be rigid and capable of supporting louth major insulation and windings.


Fig. 9. Large Transformer Core Ready for Assembly
The necessary support to make the coils rigid and free from vibration, even under great overloads, usually can be best obtained by mounting the supporting insulation directly on the core. An independent structure might of course be used for the purpose, but so doing means extra material and neglect of the great inherent strength of a rigidly assembled core.

This condition is fully met, for example, by the two-legged core as shown in Fig. 9, which is built of straight punchings assembled with alternate lap and butt joints, bolted together and provided with heary steel reinforcing plates. The joints between core leg and yoke are interleaved and secured by structural steel parts. The laminations in both the core legs and yokes have a square notch, so that when assembled a heary insulated bolt of square cross-section fits into it at each corner. Thus the core is practically a one piece unit and together with the clamping structure forms a perfect support for the windings and major insulation which, when circular, can be tightly assembled and effectively ventilated
by means of radially arranged spacing strips The supports at the ends of the coils engage directly with the steel clamping structure, hence there can be no shifting of parts along the core axis, even under the most severe short circuit.

Naturally in the very large transformers the size of the core increases appreciably and if great care were not taken, excessive temperatures of core would result. Data are at hand so that both the intemal and the surfaer temperature of all cores may be accurately predicted. In large units a number of ducts must be puit through the center of the core, not only to keep the surface temperature within proper limits but to provide increased radiation near the center of the core and thus avoid too high an internal temperature.

In extremely large transformers, the cores in some instances consist of two complete concentric structures so that there exists an oil channel across the edges of the laminations in what is ordinarily the center of the core. Since the width of the punchings is thus decreased to less than half the overall dimension, the internal temperature rise is limited to practically as moderate a value as is used in the windings, although the insulations used on laminations and bolts can safely withstand very much higher temperatures indefinitely.

Second. Windings should consist of cylindrical or disc coils. For very high-voltage transformers they should be arranged concentrically, not interleaved.

An inherent mechanical weakness tends to exist in coils for large transformers because of their size, and, in very high-voltage windings, because of the large percentage of space that must be occupied by the insulation and the relatively small size of the conductor. It is, therefore, especially desirable that such coils be of the shape that is inherently the strongest to resist the strains they are called upon to withstand. Cylindrical, or helical, and dise coils wound with rectangular conductors comply with these conditions as the full tensile and beam strength of the conductor are available to resist these forces. Fig. 10 shows a typical low-voltage helical coil.

In general, it is the best practice because of its simplicity to use the interleaved assembly of high- and low-voltage coil groups up to moderate voltages such as 40,000 , where it is desirable to keep the reactance as low as is consistent with the mechanical strength of the structure, and where an unreasonable amount of space is not lost by the repetition of the major insulation between groups. For higher
voltage transformers the concentrie assembly is desirable because of the resulting simplification of major insulation.

In a transformer the primary and secondary currents are always opposed to each other, and therefore, there is always a repulsion between primary and secondary windings. However, the different parts of the primary will attract cach other and the coil group will be compressed. A similar action exists in the secondary. In the interleaved assembly, these forces all act in an axial direction and balance each other except at the ends of the coil stack. Here they are transmitted to the coil supports, which are an integral part of the core clamping structure, by means of spacers which are arranged radially at right angles to the conductors and support each turn at frequent and regular intervals. In the concentric assembly, the repulsion forces are radial, and as the coils are circular in shape, there is no tendency for distortion in this direction. Compressive forces are easily taken care of by the radial spacers between coils. If the high- and low-voltage windings are not symmetrical with respect to their horizontal center line, as when taps are not properly balanced, or when the coils are assembled with slight inaccuracy, a large force results which tends to move the coils along their vertical axis. Substantial coil supports must therefore be provided even with the concentric assembly.

The circular coil assembly has excellent thermal characteristics, as the narrow coil spacers at right angles to the conductors reduce to a fraction of an inch the length of the heat-conducting path from the center of the spacer to the oil, and thus the blanketing effect of the spacer is negligibly small.

Third. Major insulations should furnish rigid support to the windings and have ample strength to withstand stresses accompanying short circuits.

The major insulation is that placed between the high-voltage and low-voltage windings and between the high-voltage winding and grounded core. In the interleaved type, coils are stacked around one or more insulating cylinders surrounding the core leg. The "U" shaped spacers placed about each coil accurately and rigidly space them from the cylinder. Between the highand low-voltage groups insulating collars are assembled as a part of the stack with oil ducts between them and the coils.

The concentric assembly of windings allows a very important simplification of the major insulation, by using a number of concentric cylinders between the core and low-voltage winding and between the low-voltage and high-voltage windings.

These insulating cylinders are highly laminated and are built up on steel forms under high pressure and temperature. Mechanically, they are practically as strong as the coils themselves and will resist temperatures much in excess of the highest oil temperature which it is safe to employ in transformers. They are so installed with longitudinal bracing as to give a continuous line of support from the
therefore, the densitios of magnetio leakage flux less and the forces less. On the wther hand, the increase in phesical size (coil areas), due to increase in voltage, means that the total forces are greater for a given flux density. Therefore, it is quite important to be sure that the coil stacks are not unlalanced by the effect of "buffer" or end turns or by taps or various voltage connections. The forces may be in two dircctions; (a) radial and (b) axial.
(a) In the concentric type the principal mechanical forces are radial and tend to expand the high-voltage and to compress the low-voltage windings.


Fig. 10. Typical Low-voltage Helical Coil for Large Power Transformer. Coil is clamped preparatory to vacuum varnish treatment
outer circumference of the winding to the core. This precludes any morements of parts and closing of oil ducts and yet subdivides the total insulating space into many independent units, so that any foreign material would be unlikely to bridge more than one oil space in any radial direction.

The uniformity and rigidity of these arrangements enables much greater weight to be placed on other important factors of design than is possible in other types, such as the rectangular coil shell type, where they must be subordinated to a complicated and bulky system of rectangular collars, group casings. channel pieces. etc. The complete system is being repeated between each group of highvoltage and low-voltage members and consisting, in total, of hundreds of separate pieces for a transformer of extra-high-voltage.

Fourth. Taps should be aroided, but if used they should be located as far removed from the line connections as possible.

Mechanical considerations become more important with increasing $\mathrm{kv}-\mathrm{a}$. size and moderate voltages due to the higher ampereturns located in a given space. With increasing voltage the spacing must be greater and,

In the interleaved trpe, with all coils properly centered, radial forces are encountered only when portions of a coil section are tapped out. For this reason an endeavor is always made on large units to aroid taps in individual coils. Special tap coils with the requisite number of turns are usually made so that the tapped portions of the winding are complete coils rather than parts of coils and the tap leads are taken from the crossovers between coils. This incidentally makes the problem of insulating the taps easier.
(b) To prevent as far as possible axial unbalancing in the concentric type, the taps are taken from the center of the coil stacks and so balanced that alternate taps are taken out on either side of the center, or in the case of very large transformers the taps are arranged to take equal portions on both sides of the center simultaneously:

Theoretically if the magnetic centers of high- and low-voltage windings coincide no axial forces exist tending to slide the windings with respect to one another. Practically this condition cannot be obtained even when the taps are carefully balanced. Unavoidable variations in manufacture make it necessary
that ample allowance be given in calculating the forees for any reasomable lack of aceuracy in coil assembly

Fifth. The tank construction should be such as to exclude air.

The exclusion of air from the tanks of high voltage transformers is particularly desimable for several reasons.


Fig. 11. Effect of Moisture on Dielectric Strength of Oil
(a) Moisture-Entrapped moisture is perhaps the greatest deleterious agent affecting high-grade insulation. The presence of an exceedingly small amount of moisture will reduce the dielectric strength of solid insulation to a mere fraction of its original value, by


Fig. 12. Diagram Illustrating the Main Features of the Oil Conservator
so changing the distribution of the dielectric stress as to cause a failure in what would ordinarily be a dielectrically strong structure.

The sensitiveness of oil to water has long been known; the effect on the dielectric strength being shown clearly in Fig. 11. Satisfactory transformer oil when received by a customer should stand a test of at least 2.2 kilovolts between one-inch discs spaced ${ }^{1} / 10-\mathrm{in}$. apart, and is unsatisfactory for high-voltage
or large transformers when the dielectric strength is less than 7.5 per cent of this value; that is, when it is below $1651 / 2$ kilovolts. By reference to the curve, it will be noted that oil of the standard strength, that is, 22 kilovolts, should have not more than eight parts of water in one million parts of oil, and that the addition of $101 / 2$ parts of water giving a total of $181 / 2$ parts per million will reduce the dielectric strength to the lowest permissible limit. With increasing capacity and higher


Fig. 13. Large Water-cooled Transformer with Conservator Tank
voltage, the necessity of almost absolute protection of oil against moisture will be appreciated.

Evidently the most completely effective method of protecting against moisture is to have the tank cover and terminals air tight.
(b) Explosion-Due to chemical action in the transformer oil, caused by arcing or static discharges or heavy overloads, combustible gases (mostly hydrogen and light hydrocarbons) are sometimes set free, and in the ordinary tank these gases mix with the air above the oil so that a highly explosive mixture may be formed. This gas may be ignited by sparks of a static or dynamic character occurring along the leads, causing a dangerous explosion. While all General Electric high-
voltage bushings are provided with grounded shields that make this impossible under ordinary circumstances, an abnormally low oil level may expose the lower bushing terminals, thus neutralizing the protection of the shields.
(c) Sludging-Hot oil, even if carefully selected, will very slowly decompose when in contact with oxygen, and a precipitate will be thrown down. This decomposition or shudging, while it does not affect the dielectric strength of the oil, increases the riscosity and thus retards the transfer of heat from the core and coils to the cooling surfaces. Even more deleterious is the fact that the deposit settles on the coil surfaces, in the ducts, and on the cooling coils. This acts as a heat insulator on all surfaces and also will in time clog up the ducts. The result is that the operating temperature gradually increases with consequent acceleration of the sludging.

The oil regularly supplied with General Electric transformers is of such a quality as to practically exclude sludging under normal conditions, yet continued heary service with occasional overloads may eventually produce sludge.

An exhaustive series of tests has demonstrated that when air is not present the oil can be operated continuously with practically no


Fig. 14. Core and Coils of $20,000-\mathrm{kv}-\mathrm{a}$., 220,000-volt Transformer
sludging at a temperature that woske prome disastrous if air were present
(d) Organic Acids-Organic acids are found at the same time as shdere. These acids attack the fibrous insulatins: materials and tend to materially shorten their life. It has been proven by tests that in a transformer


Fig. 15. 20,000-kv-a., 220.000-volt Transformer
from which the air is excluded and the formation of acids prevented, the life of the insulation will be approximately the same as in a transformer not so protected which is operating at a temperature at least 10 deg . C. less.
The exclusion of air is effected by a simple addition to transformer tanks which is now extensively used by the General Elcetric Company. This device is called the Oil Conservator. Fig. 12 shows the arrangement and connections, and Fig. 13 shows the general appearance of this type of tank.

The conservator consists primarily of an anxiliary tank comnected to the top of the main transformer tank by a uitable pipe and mounted somewhat above the level of the oil in the main transformer tank. When the auxiliary tank is supplied with oil the main tank and connecting pipe are completely filled, and the only oil that comes in contact with the air is that in the conservator.

Any mosisture which may combense from, the air in the conservatom will colleet in a sump, from which it may be oreasionally (Iramed. Any gas that mas form in the main tank immeriately esapes into the conservator where there is mo prssibility of ignition There being only ond oit conncetion of


Fig. 16. Connection Diagram of High-voltage Side of 220,000 volt Single-phase Transformer for Y Connection on Grounded Neutral Circuit. Line enters at $L$; slanting lines indicate series connections between core legs. Diagram is schematic only; does not indicate number coils or their spacing
restricted size between the conservator and main tank, there is practically no circulation of oil and the temperature of the oil in the conservator is but slightly warmer than the outside air. Hence sludging of the oil with the accompanying formation of acids is prevented.

This construction has now been tested in service by the General Electric Company for the past seven years, there being installed about 1000 units with an aggregate capacityof $5,000,000 \mathrm{kv}-\mathrm{a}$. The conservator is now furnished with all General Electric transformers designed for pressures of 80,000 volts and above, or for capacities of $2500 \mathrm{kv}-\mathrm{a}$. and larger.

The foregoing features, standard in General Electric construction, are all embodied in the transformers described in the following and which also have several outstanding features.
Figs. 14 and 1.5 show a transformer of record-breaking size, seren of which have been recently built for the Southern California Edison Co. These transformers are water-
(anderi, single-phase, rated $20,000 \mathrm{kv}$-a to transinion from 2en, (0)(0) in 72,000 volts at a) creles. They are similar to previous frsigns for the same voltage, using a twolexged rone with high-and low-roltage windinge assembled concentrically: The high-voltage winding is designed for a permanently groumed nemeral and is so disposed on the core legs that the coils adjacent to the yoke at the ouds of the core legs are at substantially groumd potential. Only one high-voltage bushing is required and the line lead is brought into the winding at the center of the coil stack, with two multiple circuits progressing in both directions to ground at the ends of the stack. This connection, shown diagrammatically in Fig. 16. which usually finds excellent application on extra-high-voltage transformers, effects a considerable saving, since it avoids


Fig. 17. Drawing Illustrating Arrangement of Radiators in Banks for Large Self-cooled Transformers
the necessity of insulating the winding from its supports except for the voltage of one coil, and eliminates the striking distances and creepage surfaces which would be necessary at these points for ungrounded transformers.

Since the transformers weigh nearly 160,000 1b. when filled with oil, a specially designed eight-wheel truck was necessary. The height orer the cover is 16 ft ., and over the highroltage bushing $2 t \mathrm{ft}$. The tank is of an elliptical shape, with axes of 10 and 12 ft .

A notable example of large single-phase self-conled transformers is furnished by seven 60 -cycle $10,41 \overline{\mathrm{ks}}$-a. atto-transformers which will soon be put in service by the Brooklyn Edison Company: These transformers will step up the generator voltage from 13, 800
volts to $2 \overline{2}, 600$ volts. They have a transformer rating of $10,+17 \mathrm{kr}-\mathrm{a}$. but since they are auto-transformers of a one-to-two ratio, each will transform a total of $20,8: 34 \mathrm{kr}-\mathrm{a}$. so that the total output of a bank of three transformers will be $62,502 \mathrm{kr}-\mathrm{a}$. This is probably the largest amount of energy transformed by a single bank of self-cooled transformers.

A novel feature of this design is the arrangement of radiators. The transformer proper is contained in an oval steel plate tank similar to the tanks used for water-cooled transformers. Attached to the top and bottom of this tank are two large rectangular manifolds on which are mounted the radiators in two parallel banks. The radiators and manifolds are supported on structural steel framework and the tank and the banks of radiators are mounted upon a long truck as shown in Fig. 17.

When installed, the transformer proper in its tank will be in a cell and there will be a door or baffle between the transformer tank and the banks of radiators, so that the complete unit may be rolled into the cell similar to a truck type switch, the transformer then being enclosed within its cell and the radiators projected outside and separate from the transformers. This construction, which was dictated largely by local space limitations, will undoubtedly find many applications on very large self-cooled units.

The transformer is provided with a conservator which is mounted above the manifold supporting the radiators and is connected with the outer end of the top manifold. The conservator is provided with the usual sump and breather.

The pressure relief diaphragm, to take care of any excessive pressures that may be generated in the transformer, is mounted on
the elbow leading from the main tank to the top manifold so as to afford a free and unobstructed path for the oil to flow from the main tank to the pressure relief if it is called upon to function.

These transformers are also distinctive in the method of connecting the windings to the underground cables. Contrary to the usual practice of having standard outdoor porcelain bushings, they are designed so that the underground cables will be brought up with their lead covering directly into the transformer cover and connection so made that no live parts are exposed. There are no switches between the transformers and the cables, all the switching being done at the generator end of the cable.

The efficiency of these units is extremely high, being 99.4 per cent at full load, and 99.5 per cent at half load. These high values, which are of course always inherent in any auto-transformer, are further contributed to by the necessarily lower losses of a self-cooled unit over an artificially cooled design.

An example of the high efficiencies obtainable in a large, well designed transformer, even though not self-cooled, and for a low frequency, is furnished by some single-phase, 25 -cycle, $22,000-\mathrm{kv}-\mathrm{a}$. water-cooled transformers now under construction for the Niagara Falls Power Company. These units have guaranteed efficiencies of over 99 per cent. It is also of interest to note that these transformers, although designed for the moderate voltage of $68,500 \mathrm{Y}$. will be the largest singlephase 25 -cycle units which have been built, with respect to kv-a. rating. In physical size, their tanks are about the same as for the $20,000-\mathrm{kv}-\mathrm{a}$., 220,000 -volt transformers preriously mentioned.


# Characteristics and Performance of Conversion Apparatus for Edison Systems 






#### Abstract

The operators of bilimon systems will find in this article information which will be of great value to them concerning the characteristics and performance of converters and motor-generators, particularly with regard to: starting, synchronizing, low-soltage connections, directecurent voltage range, voltage characteristics, load limiting, three-wire operation, enclosing features, effect of alternating-current disturbances, and re-energizing an Eflison system. Editor.


The synehronous converter and the motorgenerator set are the two principal types of conversion apparatus in use in America. The progress in design of each type has kept pace with the general development of electrical apparatus and the requirements of the service. The problems connected with the operation of conversion apparatus have increased greatly with the growth of the direct-current systems, the multiplicity of alternating-current power supply of common and dual frequency, parallel operation of conversion apparatus of the same type and frequency or of different types and frequency, and with the more exacting requirements of the service. The thought given to all phases of this problem by the engineers of the operating and manufacturing companies has resulted in the development of a number of operating schemes with apparatus of special characteristics.

A general description of the more important operating schemes and of machine characteristics, together with results of tests on machines operating under normal and abnormal conditions, is the content of this article.

## STARTING, SYNCHRONIZING, AND LOWVOLTAGE CONNECTIONS <br> Converters

Methods of Starting: Synchronous converters may be started from the direct-current end as direct-current motors, from a direct-connected starting alternating-current motor, from taps on the low-voltage winding in the transformer, or by switching on the high side of the transformer where the high-roltage windings are connected Y in starting and delta in running.

All of the methods, except the last as applied to synchronous converters, are well known and a brief description of the last one is given.

From an economical standpoint, switching on the high-voltage side of the transformer applies to units of approximately 1500 kw . and above at 250 volts. For smaller units where alternating-current starting is required, the low-voltage tap method is usual.

Y-Delta Starting: The advantage of the Y-delta method of starting over the usual
tap method is the elimination of the expensive low-voltage oil switches, or the unwieldy lever switches that are required for low-voltage starting, and the simplification of the low-voltage connections between transformer and converter. Also, it takes full advantage of the $30-$ deg. phase relation between the Y and delta connections.

The time required for the opening of the Y switch and the closing of the delta switch is approximately 0.3 seconds as a minimum, and maybe longer. The time required for the average converter to change its phase position 30 deg. is 0.7 seconds. The time in switching, therefore, can vary between 0.3 and 0.7 sec onds with very little effect on the inrush current in switching from the starting to the running position.

The $I$-delta starting in its simplest form gives 58 per cent starting voltage, but this voltage can be modified either above or below by placing taps in the high-voltage winding or adding an extended winding. Both arrangements have been used, depending on the conditions to be met.

Polarity Insuring: During the period of alternating-current starting, a potential is induced in the shunt-field windings that results in high voltage if the field is open circuited. The field can be divided into a suitable number of circuits to limit to a safe value the roltage across each, or short circuited through a discharge resistance or short circuited on the converter armature. With any of these field connections the converter may lock into step with either polarity. To fix the polarity with certainty, the field should be excited in the proper direction. Twenty per cent of no-load excitation is usually sufficient, and this amount increases the required starting kilovolt-amperes very little. The separate excitation scheme is now in general use. A double-pole double-throw switch with three positions is required. The starting position connects the field to a source of separate excitation, also across a discharge resistance so that the starting position is unchanged if
the separate excitation source fails; the reversing position corrects polarity in the absence of separate excitation; and the running position provides self or separate excitation.

Alternating-current Lou'-ioltage Connections: The transformers are usually connected delta high roltage and diametric low roltage for six-phase converters. The neutral point of each diameter is connected together to supply the neutral of the Edison system. With any scheme of starting, using transformer primary switching, the three neutrals can be permanently connected together and through some suitable disconnecting derice to the system neutral. With low-roltage tap starting the common connection of the neutral to each
and the end of the shaft. For such a tramsformer location the collector ring stands are turned 90 deg. from the usual thp or bottom connection. The collector rings are comnected to the armature in proper phase relation with respect to the transformer terminals, to result in simple short connections with no crossorers.

## Motor-generator Sets

The following methods have been used for starting motor-generator sets: Direct-current starting, compensator starting, Y-delta with or without reactor and series reactor The first two methods are in general use for motorgenerator sets in Edison service. Recently,


Fig. 1. Oscillograms of Starting Test of a $2500-\mathrm{kv}-\mathrm{a}$., 60 -cycle, 13.200 -volt Synchronous Motor, Direct Connected to an $1875-\mathrm{kw}$. 250 -volt Direct-current Generator. Field closed through resistor with 6.1 times resistance of field winding. Starting from line with 10 per cent series reactors
(Left) Intial start. (Right) Synchronizing, showing closing of field circuit on exciter and short circuiting of reactors. Curve A, Motor field current; B, D-C. generator terminal voltage; $C, A-C$. line voltage; $D, A-C$. motor voltage; $E$, A-C. line current (also motor current); and $F$. Speed of set
phase of the transformer must be opened during the starting period.

The loss and reactive drop of the low-voltage connections between transformer and converter are a function of the length of run and the arrangement of the leads. In many 60 -crele installations this loss amounts to more than one per cent in efficiency, and the reactive drop to $\bar{J}$ per cent of the converter roltage.

To reduce both loss and reactance to a minimum the low-roltage connections should be short. Sixty-crcle air-blast transformers can be made of such dimensions as not greatly to exceed the space between collector and base line, and between the magnet frame
principally because of automatic substation application, the $Y$-delta with or without reactor and the series reactor are used. The series reactor is the simplest possible form of starting but has the disadrantage of requiring high starting kilovolt-amperes since the motor current is drawn directly from the alternatingcurrent lines. Its use will necessarily be limited to sets 5 per cent or less in terms of connected generating capacity.

Fig. 1 is an oscillograph record showing the starting period of an $15 \%-\mathrm{kw}$. motor-generator set using series reactor for limiting the starting current. The motor of this set is especially designed for reactor starting. and is furthermore designed to take full adrantage
of the roltage that is impressed on it as it approaches full speed to develop a high torque so that the generator mat deliver approxi－ mately full output before the motor syancho－ nizes．

The next simpler method of starting is the l －delta withont reactor．This method per－


Fig．2．No Load and Full Load Voltage Range of 13,000 －amp．， 225／285－volt，Direct－current，60－cycle Synchronous Booster Converter with 80 Per Cent of Transformer High－tension Winding Connected in $Y$ and Full High－tension Winding Connected in Delta
mits of limiting the starting kilovolt－amperes to approximately 135 per cent（as compared with 250 per cent for series reactor alone），and if the change from $Y$ to delta is made at the proper time the inrush current will not exceed the 135 per cent $\mathrm{kv}-\mathrm{a}$ ．The reactor is some－ times used with the Y－delta starting method if it is desired to operate the machine on the delta connection after an interruption of power，and to resynchronize from low speed on the running connection．

The connections and excitation of the field circuit have a marked effect on the kilovolt－ amperes required at any speed in the starting period，also on the torque developed at any speed．The open circuited field winding gives the lowest starting kilovolt－amperes and the highest starting torque．The speed at which the maximum torque is developed depends on the design of the amortisseur winding，and with low－resistance windings the maximum torque is at approximately 90 per cent speed． By applying excitation to the field with the motor at approximately 9.5 per cent speed，the motor will pull into step a load that it will bring to 9.5 per cent of speed by its induction－ motor－torque characteristic．Automatic de－
vices are anailable to comtrol the field circuit for the most efficient operation．

## DIRECT－CURRENT VOLTAGE RANGE AND VOLTAGE CHARACTERISTICS

## Synchronous Booster Converter

Booster Capacity：Synchronous converters with direct－connected or motor－driven boost－ ers have uswally been designed to give a voltage range on the direct－current end of plus and minus 11 per cent and in no case exceeding 1．）per cent．For a voltage range exceeding this amount it has been usual to use the motor－generator set．Two principal features determine the capacity limit of the direct－ connected synchronous booster．With the synchronous booster consuming a part of the line voltage and lowering the converter volt－ age，the converter operates as a generator in parallel with itself as a converter by an amount equal to the output of the booster as a synchronous motor．The compensat－ ing effect of the alternating current in the converter armature is decreased，which requires an increased excitation on the com－ mutating pole in order to maintain commuta－ tion，but a point is reached where commuta－ tion cannot be successfully maintained．With the booster operating as a synchronous gen－ erator driven by the converter，commutation is effected in the opposite direction，requiring a decrease in excitation on the commutating pole，but the reactions are such that if the


Fig．3．Voltage Regulation of 13,000 －amp．，225／285－volt， Direct－current， 60 －cycle Synchronous Booster Converter
Curve I．With differential booster exciter
Curve II．Self－excited main and booster field rheostats un－ changed
Curve III．Self－excited booster rheostat unchanged，power－ factor held by main field
excitation is properly decreased commutation can be maintained．Another effect，however， comes into the operating characteristic of the machine in the boosting position which results in a tendency for the unit to pulsate if the booster capacity is more than a certain
percentage of the conserter capacity. No trouble has been experienced when the converter operates at neutral or bucking.

A number of tests by operating company showed that pulsation might result under certain conditions of boost. 111 all tests of single-mit operation there was no pulsation under any condition; with units in parallel, however, any condition starting pulsation would result in a gradual building up of the oscillations unless conditions were promptly changed or load entirely removed.

Compensated Booster: The voltage drop across the booster armature winding due to full-load current flowing and without excitation on the booster field is about 66 per cent of the rated booster voltage. A large component of this voltage is due to armature reaction. Compensation by a series winding such as used for compensating direct-current generators would greatly reduce the voltage generated by armature reaction, and in so doing would reduce the core loss of the booster, improve the phase relation between con-

$A_{1} A_{2}-B_{1} B_{2}$ Are Connected To Corresponding Points On Series Commutoting Field

Fig. 4. Diagram of Connections for Synchronous Booster Converter Arranged to Excite Booster Field from the Converter or from a Differential Exciter
verter and booster resulting in greater booster range and lower main field strength to hold unity power-factor at the collector rings. The copper loss of the compensating windings would be offset by the reduction of booster core loss.

A booster with compensationg whathes hats been built and lested in servioe 'The: form of the compensating windings was such that the bars of each pole commected pogether at each side of the pole to form an amortisseur winding. The single winding, therefore served a double purpose.


Fig. 5. Voltage Regulation of $240 / 300$-volt Direct-current Synchronous Booster Converter
Curves at maximum boost, neutral, and maximum buck, all with booster excited from the converter
Curves $A, B$, and $E$ all made with booster excited from differential exciter

The converter with this special booster has been fully tested and a great improvement in stability when boosting was found. Tests


Fig. 6. Relation of Voltage Range to Load, 4200-kw., 25-cycle Field-controlled Converter
were made with and without excitation of the compensating winding and apparently the compensating feature did not noticeably affect stability. Compensation did give the other results expected. The comnections of the converter are rather complicated by the


Fig. 7. Short-circuit Currents of $1200-\mathrm{kw}$., 250-volt, Direct current Generator Driven by Synchronous Motor

Solid curve, with differential series field Dotted curve, with current regulator
addition of compensation, especially if the unit is of the three-wire type. It is preferable, although not necessary, to split the compensating winding for three-wire operation.

For the present, at least, the additional complications in connections appear to more than offset the advantages of compensation. The amortisseur winding feature will, however, be used where a converter is to operate from reduced voltage taps and over the complete booster range on each tap.

Voltage Range and Regulation: The voltage range of a standard 13,000 -amp. 60-cycle 225 285-volt synchronous booster converter at no load and full load and unity power-factor at 100 per cent alter-nating-current voltage, transformer delta connected, and 72 per cent voltage transformer $Y$ connection, including $s 0$ per cent of the winding, is shown in Fig. 2. Some additional voltage range is obtained by powerfactor control.

The inherent voltage regulation of the synchronous booster converter depends on the regulation of the converter itself, which depends principally on the brush position and the strength of the commutating field, the regulation of the transformer and intermediate connections, and the regulation of the supply. On the basis of a constant supply voltage the regulation of the self-excited shunt-wound synchronous booster converter at unity power-factor is
appoximately 2.5 per cent. The regratation with eonstant rheostat setting is approximately 11.0 per cent. The resulation curves for botle conditions are shown in Fig. :3.

Differential Booster Exciter: The voltage of the syonchronous booster can be varied at will and it can be varied athomatically with load in order to increase the inherent regulation of the synchronous booster equipment. This might be acomplished by placing a series differential winding directly on the poles of the booster, but in practice it has been found more eeonomical to use a separate exciter for the booster field winding, and the fields of the exciter arranged with a differential winding. The exciter is designed with sufficient series differential field to give full voltage change of the booster field excitation for 100 per cent change in converter output, that is, with the converter operating at no-load neutral voltage


Fig. 8a. Load Limiting by Differential Series Field, Multipolar 1200-kw., 720-r.p.m., 250-volt, Direct-current Generator with Pole-face Winding

Curve A, Direct current; Curve $B$, Direct-current voltage
Curve $C$, Synchronous motor field current


Fig. 8b
Curve A. Induced voltage generator field; Curve $B$, Alternating-current motor Curve $C$, Alternating-current voltage, motor
the exciter would be operating at zero voltage: adding 100 per cent load to the converter would add 100 per cent excitation to the exciter in the direction to give full excitation for the booster and in the direction to buck the converter voltage.

The differential exciter boes not increase the voltage range of the synchronons booster converter as the available voltage range is determined entirely by the capacity of the booster. It does change the soltage regulation, however, adding to the inherent regulation one-half of the booster range, provided the maximum buck or boost limit is not reached by the load change. The third curve of Fig. 3 shows the voltage regulation of the synchronous booster converter with the differential exciter.

The connections of the differential exciter as a spare to the usual booster and auxiliary
commutating feld rheostat is shown in Fig. . 1. The regulation of the booster converter with differential exciter is given in Fig. i, as chrves AA, BB, and EE which show dearly the limitations, depending on the point of intial operation.

## Field Control Converter

The field control converter has a limited voltage range with plus and minus in per cent as about the economical limit. The inherent regulation of the field control converter is much greater than the synchronous booster converter because of the greater amount of reactance in the circuit. The voltage range curves are shown in Fig. 6. The fied control type is well suited for automatic substation work, also on some of the larger systems where the required voltage range is small.

## Motcr-generator Sets



Fig. 9a. Load Limiting by Counter-Electromotive-Force Regulator, Multipolar 1200-kw., 720-r.p.m., 250-volt, Direct-current Generator with Pole-face Winding

Curve $A$, Direct current; Curve $B$, Direct-current voltage Curve $C$, Synchronous motor field current


Fig. 9b
Curve $A$, Induced voltage generator field; Curve $B$, Alternating-current motor Curve $C$, Alternating-current voltage, motor

A voltage range of 100 per cent is available from the generator prorided a suitable scheme of excitation is used. The shant-wound sepa-rately-excited machine allows 100 per cent voltage range; the self-excited machine allows approximately 25 per cent roltage range unless special construction is used, increasing the voltage range to approximately 50 per cent. The self and separate excitation of the shunt winding, together with differential series excitation provides 100 per cent voltage range, also the constant current characteristic which is not obtained by any other form of excitation. Successful commutation over the complete range of roltage is obtained on the generator of the compensated commutating-pole type.

## LOAD LIMITING

## Synchronous Converters

Load limiting is obtained by decreasing the voltage impressed on the load; and in the case of the synchronous converter the range over which the roltage can be controlled is somewhat limited.

As previously pointed out, it is not desirable to use a direct-connected booster of more than 1.5 per cent capacity. The converter can be operated over a much greater range in voltage if it is operated as a simple converter, which is obtained
be tap changing on the transformer, a separate motoredriven booster set, or some form of induction regulator. The standard $2.0(0-v o l t$ converter will operate successfully at approximately 7.5 volts. Below this voltage it is necessary to make further reduction by inserting in the line leads a resistance which is divided into a suitable number of steps to be cut in and out of circuit by short circuiting devices.

Air cooled resistors are usually used for short time ratings but for time settings exceeding 15 min. the water-cooled resistor becomes the more economical proposition, both from the standpoint of cost and space required.

## Motor-generator Sets

Series resistance has been used in some cases for load limiting in the case of motor-gencrator sets, but for lighting and power work field control gives very satisfactory results.

There are two methods of field control of the generator for load limiting purposes. One is by regulation of the shunt field only, and the other by a differential series winding, the strength of which is varied by a shunting device in combination with a shunt-field excitation of which approximately one-third is furnished by separate excitation and the remainder by self excitation. The shunt winding may consist of two separate windings, one of which connects to the constant source of excitation and the other to the generator terminals, or it may consist of a single winding. In this case a 125 -volt exciter is connected in series with the 250 -volt generator and the shunt-field winding connects across the two in series.

The two methods of control have been carefully tested and there appears certain advantages for the second in that the inherent voltage-current characteristic can be made such that the machine becomes practically a constant-current generator at full-load current. Fig. 7 shows the results of the two methods of field control for load limiting purposes taken on a $1200-\mathrm{kw}$. 2.50 -volt motorgenerator set. Shunt-field control was obtained by the use of a counter-electromo-tive-force regulator with the aid of a contactor shunting a suitable amount of resistance for quickly lowering the voltage to a point where the regulator would take hold and maintain constant current. The time element of this short circuiting contactor was eliminated by energizing the contactor to trip immediately before making the short circuit. While this is not a practical arrangement for service
comditions, it was made a part of this test so as to show the best results that can be oltained from this method of load limiting.

The curves shown in Fig. 7 are taken from the oscillograph records shown in Figs. $S$ and (9. Fig. 8 is the record of load limiting by differential field control. Fig. 9 is the record with a constant-currrent regulator control. The resistance, amounting to 0.0007 ohms, through which the generator was short circuited, was exactly the same in both tests. It is clearly scen by comparing the two oscillograph records that load limiting is effectively obtained by either scheme. The differential field winding is slightly faster as indicated by the direct-current curves, also by the motorinput current curves. The shunt-field voltage is very different in the two cases where 650 volts is the maximum reached with the differential ficld control as against at least 2100 volts with the constant-current regulator control.

A great advantage of the differential field method of control is the absence of all regulating devices, also the current limiting effect of the differential winding that becomes cumulative should the direction of power change. The compensated commutating pole generator may be unstable when operating as a motor at low voltage and at high current. This instability is entirely overcome by the action of the compound winding.

## THREE-WIRE OPERATION

The synchronous converter is easily arranged for three-wire operation, also practically any amount of unbalance can be successfully handled. Observations of machines operating under conditions of 100 per cent unbalance, that is, rated current in one lead and the neutral lead and zero current in the other main lead, show no perceptible difference in the operation of the machine as compared to balanced conditions. In order to successfully commutate such conditions the series commutating field windings must be arranged to include one-half the winding in each side of the line, also the commutation control for the auxiliary commutating field must be so arranged that the excitation of the auxiliary commutating field depends on the output as measured in each of the outside leads.

If the unbalance is 10 per cent or less it is not necessary to split the series commutating field windings, and a number of units for three-wire operation have been so arranged in order to preserve the simplest possible field connections.

In the case of the motor-generator set it may be difficult to provide for three-wire operation, principally because of the complicated field connections that result, and because of the small amount of elearance between field connection strips of opposite polarity. This is particularly true where a compound or a differential-compound machine is used so that there are three windings that must be split and connected in each of the main leads, that is, the series winding, the commutating field winding, and the compensating field winding.

The amount of unbalancing of a system as a whole and at any individual substation is


Fig. 10. Diagram of Connections for Direct-current Balancer Set and Control Auxiliaries
usually small in percentage, and an effort is made by the distribution department to maintain approximately balanced conditions throughout the distribution. Changes are necessary from time to time to accomplish this result.

It should be fully appreciated that in threewire operation the amount of unbalance on the converter or the generator results in the lowering of the total output from the machine. The heating and performance of a machine are based on rated current. If the rated current is not exceeded in the heavier loaded side then the output of the machine is decreased in per cent by half the per cent of
the unbalance. At 2.5 per cent, an anmount usually considered as a maximum for comtinuous operating conditions, $121 / 2$ per cent of the machine capacity is forfeited.

In a system supplied by converters and motor-generator sets it is usually possible to obtam the necessary neutral capacity from the converter, operating all of the motorgenerator sets as two-wire units. In certain cases, however, this has not been possible because of the relative location of the motorgenerator sets and converters.

Balancer Set: A balancer set with special field connections and control has been developed. Each unit of the set is provided with a series winding that has a differential relation when the unit is a generator, and an accumulative relation when the unit is a motor. The poor voltage regulation due to this field connection is compensated for by the automatic control of the shunt fields of each machine to maintain a balanced voltage condition until the capacity of the balancer set is reached, at which point no further change is made in the shunt-field adjustment for voltage balance. Beyond this point the shunt field is automatically adjusted to limit the neutral current which protects the set within certain reasonable limits. A balancer set of this type can be permanently connected to the system and will follow any voltage changes. Fig. 10 shows the simplified wiring diagram and control.

## ENCLOSING FEATURES

Enclosing features for both converters and motor-generator sets are being given more and more consideration because of the special problems in ventilation and in quietness of operation. It is a fairly simple matter to enclose the motor, and this has been standard for a number of years. It is much more difficult to supply suitable enclosures for the commutating machine because it is desirable to have the commutator and brushes visible and accessible. Generators have been enclosed so as to take air from an intake air duct and discharge air at the commutator end, but without any enclosure of the commutator or any means for discharging the air directly into a discharge duct. Synchronous converters are now being built to take air from the room and discharge to a suitable discharge duct, also to take air from an intake duct and discharge to the room. In both cases the arrangement of enclosure is such as to produce quietness of operation. Developments along this line have just started and it is believed that considerable progress will be made during
the next few years (onetness of operation ant rentilation are two of the lige problems in any downtown sulstation

## EFFECT OF ALTERNATING-CURRENT DISTURBANCES

Converters
Pouer Transfer: 'The lowering or raising of the alternatingecurrent voltage to the


Fig. 11. System Connections During Alternating-current Short-circuit Tests, 3900 -kw., $240 / 300$-volt Synchronous Booster Converter with 3-phase 13,200-volt Transformer. Short Circuits made at $A(4500$ V.) and $B(13,200$ V. $)$
$A$, Short-circuit closing O.C.B., 4500 volts; $B$, Short-circuit opening O.C.B.; $C$, Aux. short-circuit opening O.C.B., 13,200 volts; $D$, Converter withstanding short circuit; $E$, Converter floating on line
converter causes a corresponding change in the direct-current voltage and. therefore, during alternating-current disturbances where

Whe altomating-emrent voltage may drop to very low values for periods of time the directcurront vollage tends to drop, and if it is maintained from another source of supply a current will flow from that supply into the alternating-eurrent system, depending upon the difference in voltage of the supply and the alternating-current system. In most systems it is very flesirable to have continuous operation of the synchronous converters and it is, therefore, desirable to meet the conditions produced by alternating-eurrent disturbances without permanently flisconneeting the converter from either the alternatingcurrent or the direct-current system. This problem has been carefully investigated and a series of tests were made to determine the effect of alternating-current disturbances on 6()-cyele synchronous converter operation and what forms of protection are necessary in order to have the machine successfully meet these conditions and continue in operation at the termination of the alternatingeurrent disturbance.

The inherent voltage regulation of the converter is small and therefore a small change in the relation of alternating-current and dircet-current voltage causes the converter to drop its load and invert. The inherent regulation of the booster converter can be increased by bringing into action the voltage range of the booster, and the two in combination permit a much greater change in the relative relation of alternating-current and directcurrent voltages for the same change in load. The effect of both, however, is not sufficient to limit to safe values the amount of reverse current which results from a severe disturb-


Fig. 12. Three-phase 13,200-volt Short Circuit at B, Fig. 11
Curve $A$, Direct current; Curve $B$, Direct-current voltage, converter; Curve $C$, Alternating-current voltage to transformer Curve $D$. Direct-current voltage substation bus; Curve $X$, Short circuit on; Curve $Y$. Current limiting resistor in Curve $Z$, Alternating-current short circuit opened
ance on the alternating-current system such as is due to a short circuit on the primary distribution and where the direct-current voltage is stabilized by storage battery capacity comnected to the system or other conversion apparatus not affected by the alternatingcurrent disturbance.

The system connctions for the tests at Cincinnati are shown in Fig. 11. It was found that a short circuit on the secondary distribution ( 4500 volts) would produce an alternat-ing-current disturbance of sufficient magnitude when one generator ( $31,2.50 \mathrm{kv}-\mathrm{a}$.) was in operation to cause approximately 200 per cent reverse current to flow from the directcurrent system supplied by batteries to the alternating-current system. This disturbance would be less with more alternating-current generator capacity comnected, but each test was taken to cover the worst case. This test clearly indicated that it would not be possible to operate the converter permanently connected to the alternating-current and directcurrent systems when the alternating-current disturbances were of the order produced by a short circuit on the primary distribution. To obtain additional regulation on the converter circuit an air-cooled resistor, short circuited by a breaker, was comnected in the line lead. The action of reverse current opens this circuit breaker shunting the resistor and the resistor remains in circuit until the effect of the disturbance is past, allowing voltage restoration and current flow in the normal direction which closes the breaker across the resistor and the machine is again directly connected to the system delivering load. Fig. 12 is an oscillograph record of these conditions. Fig. 13
is an uscillograph record of a short carenit on a 4.500 -volt feeder

The performance of the sio-cyele conserter is very creditable under the conditions shown


Fig. 14. Estimated Direct Current for 3-phase Short Circuit on Feeder Supplying 3900 -kw. Converter, Fig. 11
in Fig. 12, although there is an instantaneous change in load of almost 2.50 per cent.

Tests indicate that the synchronous converter carrying load in either dircction will operate successfully at about 2.5 per cent


Fig. 13. Three-phase 4500 -volt Short Circuit at $A$, Fig. 11
Curve $A$, Direct current; Curve $B$, Direct-current voltage, converter; Curve $C$. Alterrating-current voltage to transformer Curve $X$, Short circuit on; Curve $Y$. Current limiting resistor in; Curve $Z$, Alternating-current short circuit opened
voltage and at no load at a lower voltage. The Cincimatitests show the results when a short circuit oecurs on a radial feeder that is not supplying the synchronous converter equipment under test. If the feeder supplying that comverter were short circuited then it would be necessary to discomect the unit on the direct-current end and there is no advantage in it remaining connected to the alternatingcurrent end. Fig. It shows the estimated current flow had the alternating-current feeder supplying the converter been short circuited.

In the preceding paragraphs the supply to the direct-current end of the converter was obtained almost entirely from the storage battery that connects to the substation bus.
of the two machines was practically the same; in other words, the presence of high directcurrent load currents made very little difference in the performance of the unit.

The series commutating field strength will follow the load changes but the auxiliary commutating field strength has a considerable time lag due to the time required to move the rheostats. Reducing the time lag to a minimum would change the net results very little because of the inductive relations between the shunt and series windings on the commutating pole. This inductive cffect is shown by the curve of auxiliary field current in Fig. 15. If conditions allowed the apparently correct field currents, the field adjustment would not be correct because of the unbalanced relation


Fig. 15. Currents in Booster and Auxiliary Commutating Fields at Time of Tests, Fig. 13
Curve 1 , Current, auxiliary commutating field; Curve $B$, Current, booster field; Curve $C$, Current to transformer Curve $\mathcal{N}$, Short circuit on; Curve $Y$, Current limiting resıstor in; Curve $Z$, Alternating-current short circuit opened

If no storage battery is connected to the bus then the direct-current supply must come from the system and, therefore, over the resistance drop of the connecting feeders, or must come from other machines in the same station that are fed from a separate source of alternating-current power that is not involved in the disturbance, or from the generator of a motor-generator set (the voltage of which is not directly affected by the alternating-current disturbance even though the motorgenerator is operating from a common source of supply with the converter).

Commutation: To compare the performance of a converter carrying load as against a converter running light when subjected to the same alternating-current disturbance, two similar machines were observed during these tests, one machine loaded and the other running light. The sparking at the commutators
of alternating-current and direct-current component currents in the armature conductors. As an indication of the order of these effects Fig. 16 shows the line current and the commutating field current resulting in connecting and disconnecting load from a converter. Fig. 17 shows the line and field current where the commutating winding is short circuited before the line breaker is opened. The observed flashing at the commutator in the second case was about the same as the first, although a greater load is switched on and off.

If the direct-current bus in the case of these tests had been supplied by a converter of equal size and from a source of supply that was not affected, the amount of reverse current would have probably been of the same general order as that obtained from the battery in this particular case. In other words, the voltage regulation of the $13,000-\mathrm{amp}$. converter is
about the same as shown on the roltagecurrent curve of Fig. 3.

Parallal Operation: From the foregoing it is clear that the same general problem exists where converters are operating in parallel with batteries, or in parallel with converters of the same frequencre and independent power


Fig. 16. Compound-wound $300-\mathrm{kw} ., 1200-\mathrm{r}$. p.m., 750 -volt Converter Short Circuited Through 0.268 Ohms. Transformer Reactance 15.0 Per Cent
Curve A, Current, commutating field; Curve $B$, Alternating current Curve $C$, Direct current


Fig. 17. Compound-wound $300-\mathrm{kw}$., $1200-\mathrm{r} . \mathrm{p} . \mathrm{m} ., 750$-volt Converter Short Circuited Through 0.238 Ohms. Transformer Reactance 15.0 Per Cent. Commutating Field Short Circuited Before Opening Direct-current Breaker
Curve A. Current, commutating field; Curve $B$, Alternating current Curve C. Direct current
supply, or different frequency and power supply, or with motor-generator sets from the same or separate power supply.

Operating experience shows that alternat-ing-current disturbances will cause heary reverse current under any of these conditions. This fact has led operating companies to
provide suitable ties berween the acterat sources of power supply where synchronous converters are operating from each and are paralleled on the direct-current end. If the two supply systems are not tied torether except through the converters, then the converters must of necessity handle the current flowing between the two systems. attempting to maintain the normal roltage relations.

Fig. is shows the comnections of a number of converters in several substations supplied by two generating stations that are not connected together except through the converters on the direct-current end. The connections shown are those existing at the time of a known alternating-current disturbance and the effects on the several machines were noted. No direct-current reverse-current protection is used in this case and the machines are disconnected from the alternating-current end by the operation of inverse time overload relays, and from the direct-current end by the operation of the overspeed switch. It is significant that the only machine showing distress is at the West 41 st Street substation, and this machine is fed by another unit of equal capacity and by a small amount of battery capacity. Fig. 19 shows the connections and capacities involved for another form of alternating-current disturbance, and here again the machine showing the effects of the disturbance was supplied by units of greater capacity connected to the same bus. At West 26 th Street the brushes of the $4200-\mathrm{kw}$. unit were badly burned. This unit was connected to a direct-current bus having a connected battery capacity of 1584 kw ., also three converters of $5.500-\mathrm{kw}$, total capacity not affected by the alternating-current disturbance.

At Crosby Street the brushes of a $4200-\mathrm{kw}$. unit were badly burned Connected to the same bus were $5000-\mathrm{kw}$. total in converter capacity and $4.50-\mathrm{kw}$. in battery capacity. The $4200-\mathrm{kw}$ unit at Van Dam Street against a $2.500-\mathrm{kw}$. unit and 450 kw . battery, a $3.500-\mathrm{kw}$. against a $3500-\mathrm{kw}$. and $17.56-\mathrm{kw}$. battery at W. 41 st Street, and a $4000-\mathrm{kw}$. against a $3.000-\mathrm{kw}$.
and engo-kw. battery did not give any signs of distress in oponing on the alter-bating-current emd beg overload relays. ("omplete data on a number of such cases hate been collected and in each case these general relations existed. It appears, therefore, that a critical condition exists when the capacity of the matelane inverting is just equal to the capacit! of the machine supplying the power
aged mater practically any condition of disturbatice on the alternating-current end.

System Intercomnections: llad the two alter-nating-currentsystems shown in Figs. 18 and 19 been connected together through suitable tie lines, the eonverterswould havebeen protected agatinst alternatingrecurrent disturbances.

The connecting together by tie lines of the alternating-current supply is usually a simple


Fig. 18. Diagram of Connections of Converter Substation Fed from Two Independent Alternating-current Systems
Hell Gate generator lost its excitation. All converters fed from Hell Gate speeded up. Opened d-c. breakers. Brushes on 41 st St. station synchronous converter entirely burned off ( 160 had to be replaced)
to the inverted unit. When the capacity of the inverted unit is greater there is little chance that the machine will be damaged before the inverse time alternating-current overload device clears the unit. On the other hand, if the two capacities are equal trouble may result, and if the capacity of the inverted machine is less trouble may be expected and the amonnt of the damage depends to a large degree on the relative capacities. It should be clearly kept in mind that these conditions exist when certain relay arrangements are selected because of the operating conditions and the requirements that are desired. If reverse-current protection is provided on the direct-current end of the machine it appears that the machine can be successfully disconnected from the line before the unit is dam-
matter where a common frequency is used. If 2.5 - and 60 -cycle frequencies are used, a tie line cannot be employed and some other form of tie is necessary unless the 25 - and 60 -cycle converters are to make the only magnetic tie between the two systems. The synchronoussynchronous form of frequency-changer set is used to tie together systems of different frequency, but this form of tie does not connect the two systems together magnetically and, therefore, this form of tie (while it establishes a frequency tie) does not protect effectively the 2.5 -and 60 -cycle converters that operate in parallel on the direct-current end.

Booster converters are operated at unity power-factor under all conditions, while the field control converter is operated at a powerfactor to give the required voltage. The
shunt field may be under or over excited, and in cases where the direct-current end is not opened on reverse current a protective feature should be added to the field circuit that automatically establishes normal field when the overload alternating-current relay operates or when the oil circuit breaker opens for any cause. The device consists of a short circuit-

In the motor-generator set, it is entirely feasible to provide against a complete interruption of alternating-current power and allow the motor and generator io remain permanently connected to the two systems, and promptly upon the return of alternatingcurrent power to deliver power to the directcurrent system. Figs. Sa and sb on page 417


Fig. 19. Same as Fig. 18 Except for the Following Conditions:
Operator made a dead short circuit at 73 rd St. station on feeder 7354. The Hell Gate end of this feeder opened by overload on W. 26th St. station. The oil switch opened automatically, also d-c. breaker on Crosby Street. Van Dam St., E. 26 St., and W. 41st St. converters unaffected. W. 26th St. and Crosby St. converters had brushes badly burned (practically all had to be replaced)
ing contactor, a holding circuit, and on the rheostat a limit switch that drops the contactor when the rheostat has moved to the desired position.

## Motor-generator Set

In a motor-generator set the alternatingcurrent and direct-current systems are completely isolated and, therefore, a disturbance in alternating-current voltage does not react directly on the direct-current system unless the voltage drops to a point that allows the motor to fall out of step and fail to deliver the necessary power to the generator, or unless the frequency changes sufficiently to cause the motor to act as a generator, returning power to the alternating-current system.
show an oscillograph record of a complete interruption of alternating-current power and the restoration of this power shortly afterward. The input to the motor, the automatic control of the motor field, and the output from the generator are clearly shown. This scheme of operation reduces to a minimum the time required in restoring service on a direct-current system after alternating-current power is available.

## RE-ENERGIZING AN EDISON SYSTEM

In the past the service of practically all the Edison systems of any magnitude has been protected by standby storage battery capacity. The battery served two principal functions; first, to supplement the generating capacity at times of peak load: and, second,
to ated as reserve eapateity in case of an ontage of the sompee of supply.

If an intermption in the source of suppl! is matatained for a time beyond the diseharge capacity of the battery it is disconneeted so that there remains sufficient capacity in the battery for encreizing the system temporarily until the eonversion apparatus can be connected. 'The momentary' overload capacity' of the battery allows for connecting the several substations in succession, which is a difficult problem in the case of conversion apparatus unless the voltage control is sueh that the output of any apparatus connected to the sristem can be controlled within safe limits. The amount of battery capacity in relation to system load varies widely and each operating company has established certain relations.
The problem of re-energizing depends on the capacity of the system, the number and capacity of the substations, the capacity and voltace range of the individual units in the substation, the standby battery capacity, and the distribution of the battery capacity throughout the system. The problem is most difficult in a large system without standby battery capacity because in such a case practically complete voltage control of the conversion apparatus is necessary. As has been pointed out, the voltage range of the synchronous booster converter is limited unless series resistors are used. The amount of system load, however, is a function of the voltage and it is not necessary to provide all of the conversion apparatus with approximately 100 per cent voltage range.

This situation has led to the consideration of a certain percentage of motor-generator capacity properly distributed throughout the system to serve as the first step in re-energizing and to bring the system to a voltage that can be approached by the synchronous booster equipment operating from a reduced voltage connection of the transformer and at maximum buck. At least 2.5 to 30 per cent motorgenerator capacity would be required and it would be necessary to have a number of synchronots converter equipments running and ready to take load as soon as the system voltare was in reach of the converters, so as to reduce to a minimunn the time that the motor-generators would be overloaded. In the average case the load on the Edison system is approximately equally divided between lights and power and it has been generally assumed that the current would vary directly with the voltage instead of at a rate cleter-
mined entirely by the lamp characteristic, and it is on this basis that system requirements have been figured.

A careful study of each system is necessary to determine the best means for re-energizing. On certain systems it may not be economical to use motor-generator sets, and if such a system is not protected by standby batteries and the system load is such that sufficient converter capacity at the minimum obtainable voltage cannot be connected simultaneously to handle the situation, then load limiting resistors become necessary. There is at least one system that is proceeding on this basis at the present time.

On other systems the relation of a single substation capacity to system capacity is such that a sufficient number of converters can be connected simultancously at the minimum voltage. The voltage is gradually increased as other stations connect to the system until maximum boost on the Y connection is reached. The transformer connections are changed, one at a time, allowing a further increase in system voltage until normal conditions are reached. Fig. 2 shows the voltage range obtained by a standard booster converter, and the reduced voltage connection on the transformer is made such that the converter operating from the running connection at minimum voltage can be successfully connected in parallel with the converter operating at maximum voltage and full load from the tap connection. For simplicity, the emergency running connection is also used as the starting connection and the starting characteristic of the converter is made suitable for this voltage. There are at least two companies operating moderate size systems without the standby battery capacity who plan to re-energize their systems by this method.

It is obviously desirable to provide the greatest possible voltage range of the synchronous booster converter, for re-energizing, that is consistent with successful operation under all conditions met with in re-energizing, and at the same time consistent with efficiency of operation under normal conditions. If the alternating-current voltage of the emergency running connection is less than 72 per cent of the rated voltage, then a larger booster is necessary to bridge the voltage gap than is standard for obtaining a 240 - to 300 -volt range. Commutation or stability may become limiting factors. Present experience indicates that the conservative allowable separation of the running and the emergency or starting connection is approximately :3s per cent.

# Alternating-current Generators 

By W. J. Foster<br>Alternating-crrrent Enginering; Department, General Electric Company


#### Abstract

A well balanced, conservative design will give an alternator longer life and higher efficieney. The athor discusses such questions as efficieney, temperature, stability and insulation and shows how these factors shoruld be harmonized to make a satisfactory machine. - Eiditor.


"What is the largest alternator that can be built?" "What is the highest efficiency that can be obtained:" "What should be considered the reasonable life of an alternator?"' "What is it possible to obtain in the way of long life, if designed particularly with reference to it?" These questions are often asked about alternators. While it is not possible to give absolute answers to such questions, some notes throwing light on these subjects may be of interest.

As to the size that is possible at the present time, this depends to a great extent upon the normal operating speed and the over-speed requirement that must be met. Let us confine our thought for the moment to 60 -cycle generators. In the case of steam turbine machines, where the emergency governor is set to trip at 20 per cent over-speed; $40,000 \mathrm{kr}-\mathrm{a}$. at 1800 r.p.m., with possibly $4.000 \mathrm{kv}-\mathrm{a}$. at unity power factor, and $75,000 \mathrm{kr}-\mathrm{a}$. at $1200 \mathrm{r} . \mathrm{p} . \mathrm{m} .$, are being produced, or can be, if desired. In salient pole machines for coupling to waterwheels, where the over-speed is usually from S0 per cent to 100 per cent above normal, $50,000 \mathrm{kr}-\mathrm{a}$. is about the limit for speeds as high as 450 r.p.m. At lower speeds, much higher capacity generators are possible. Assuming that transportation facilities can be provided, and a considerable part of the construction carried out at the plant, $1,50,000-$ $\mathrm{kv}-\mathrm{a}$. generators may be built at the present time at speeds of approximately 100 r.p.m.

## Life of Alternators

In the matter of years of serrice that may be expected, a great deal depends upon the character of the service and the care that is taken with the machine. In the case of steam turbine generators, which are totally enclosed and, consequently, liable to operate at times when not in proper condition, due to the difficulty of inspection, and, furthermore, subjected to considerably higher temperatures in certain parts than other classes of a-c. generators, a certain life may be expected. In the case of salient pole generators of the most advantageous speed and roltage, twice as long life may reasonably be expected. Bỵ
"life" in this connection, is meant the perion from the time that the machine is first put into operation until a burnout or breakdown, that requires either the rewinding or rebuilding of the rotor or stator, occurs.

It is pretty generally agreed that the characteristic of an alternator which is most appreciated is freedom from little operating troubles. Undoubtedly sufficient attention is not often given to such matters as design of bearings and oiling arrangements to prevent the escape of oil, especially in the form of vapor, the design of collector rings for receiving the exciting current, and the design and construction of brush-holder mechanism.

Considerable thought is always given to the important features of the rotor construction. The best constructed rotors at the present time have provision for taking up shrinkages that may occur in the insulating material, either by easy adjustment, or automatically, which is far preferable. With a machine constructed throughout all its parts in accordance with the best principles of mechanical design, there remains the problems of forming up the copper for armature and field and of applying insulation of the proper kind and in the proper manner to secure the greatest possible freedom from trouble and the longest life.

## Insulation

The insulation is of utmost importance. The more difficult problems are met in the insulating of the armature windings. It is the author's opinion that altogether too much emphasis has been laid upon the "looks" of new insulation and its ability to stand high potential test. It should be remembered that there are other qualities of even greater importance than the solidity of the newly formed insulation and the extremely high dielectric strength it possesses. Possibly the methods of testing and the intensity of the tests as now practiced are the best that can be suggested at the present time for the acceptance of new machines, but it is unfortunate that methods of testing insulation have not been established of such nature as to impose tests everywhere throughout that correspond


Fig. 1. $35,300-\mathrm{kv}-\mathrm{a}$., 60 -cycle 13,200 -volt 80 Per Cent Power-factor $1800-\mathrm{r} . \mathrm{p} . \mathrm{m}$. Steam Turbine Generator for Union Gas \& Electric Co., St. Louis. The first machine of this rating has been in operation since January, 1922, in the Calumet Station of the Commonwealth Electric Co., Chicago. Twenty-one have been or are being built in the Schenectady Works
developed that is ton hard and myvichling for coits of wire that camot be perfectly embedded in rigid containers throughout their entirety.

The present high test encourages insulation engineers to concentrate their efforts on the development of materials of the highest possible dielectric strength per unit thickness on the parts of the windings that are embedded in the slot. In order to have a corresponding diclectric strength at points a few inches removed, it is necessary to thicken the insulation materially, especially at the bends. The amount of "padding up" is determined by the weak points that are discovered when the high tests are applied. Who knows how much better, viewed from the standpoint of long life and freedom from trouble, windings might be made and
to the dielectric stresses that occur when the machine is in actual service and passing through its complete cycle of operation. The high potential test now standard is based on consideration of the windings, either as a whole or in sections, as condenser plates. The intensity of the test is measured not by thie dielectric stresses that exist in practice as between turns in the same coil, coils in the same or other phases, but solely on the potential generated at the terminals of the several phases. Granted that there should be a rigid test, one that allows a good margin of safety above what is expected in service, it is obvious that to require too high a test is to court troubles later, due either to the unnecessarily thick insulation or to a type being


Fig. 2. Stator Frame of $65,000-\mathrm{kv}-\mathrm{a} ., 107$-r.p.m., 25 -cycle, 80 Per Cent Power-factor, 12,000 -volt Vertical Generator (on $60-\mathrm{ft}$. Boring Mill) for Niagara Falls Power Co. The immense size of the casting made impossible the taking of a photograph which does not show distortion.
insulated if the present high test were reduced. granted that it is now unnecessarily high? It is significant that some machines are now in use that were built many years aro for certain voltages and reconnected later for higher potentials, usually double potential, or 1.73 times the original, with insulation that no manufacturer would trust to stand the high potential tests now standardized for the higher voltage.

A valuable quality in insulation is repairability. While every effort should be put forth to design and build machines that will not require repairs for a long period, accidents may occur and repairs to the windings be necessary. It is then of great ralue that the insulation be of such character as to remain in close contact with the copper at all points so as to permit the neighboring coils to be bent and distorted while being removed and replaced in making the repairs. Radial slots are still the order of the day. A particularly objectionable type of insulation, when it comes to repairs, is that which, in service. springs away from the copper at the middle of the sides just beyond the ends of the core, or where the coil spans ventilating ducts. This tendency is more pronounced with the deep slots of present day design than with the more shallow slots of former days.

## Stability of Alternators

A characteristic that should be incorporated in practically all a-c. generators is ability to remain in step at sudden overloads incident to disturbed conditions, due to grounding of line, mistakes in switching, etc. This characteristic is designated "stability." The usual way of studying this characteristic is to draw curves showing, first, the rolts and amperes output and, second, the kr-a. output and amperes that the generator will deliver with excitation held constant. Fig. 3 shows typical external characteristics at $\$ 0$ per cent powerfactor (normal excitation) of six generators with short-circuit ratios covering the range 0.9 to 1.5. The short-circuit ratio is obtained by dividing the ampere turns required to give normal volts on open-circuit, bry the ampere turns required to produce normal current on short-circuit. These curves represent actual designs.

Similar curves might be drawn for the same generators at other power-factors, such as 90 per cent or unity. The design should be such that the working point is to the left of the peak of the output curve and slightly removed. It should not be at the crest or to
the riglat. Short-circuit ratios ranging from 1.0 to 1.2 .5 give machines that are quite satisfactory in the matter of stability. A drop in voltage is what occurs when there are disturbances on the system that eall for temporary assistance. A stable generator is one that can carry increased load at reduced voltage without increase of excitation.


Fig. 3. External Characteristic Curves of Salient-pole 80 Per Cent Power-factor 60 -cycle Alternating-current Generators. These curves are based on machines of average reactance of 20 per cent and average degree of saturation

It is desirable in alternators in large systems to have as high reactance as is consistent with such characteristics as stability, in order that the instantaneous rush of current in case of a short-circuit in operation may be kept down. The value of this current is often given in terms of the rated current. This ratio should not be confused with the short-circuit ratio as discussed in connection with stability:

## Economic Voltage

The question is often asked in connection with new installations "What is the best roltage to adopt:" An unqualified answer should not be attempted. It sometimes happens that the high roltage is the best, due to the possibility of obtaining better all-round characteristics in the generator. This is true in the case of two-pole generators of the largest output in steam turbine units. The number of circuits per phase is limited to the number of poles; hence, only two circuits are
possible. In such large machines a single turn generates something in the order of threehundred volts. A good machine canmot be built without having a large number of slots to keep the amperage per slot within certain


Fig. 4. Characteristics of a $31,250-\mathrm{kv}-\mathrm{a}$., 60 -cycle, 13,200 -volt, 80 Per Cent Power-factor $150-\mathrm{r} . \mathrm{p} . \mathrm{m}$. Generator. Designed to meet the usual specifications for a first-class generator where advantage is taken of temperature rises of $50 \mathrm{deg} . \mathrm{C}$. by thermometer and 60 deg. C. by embedded detector
limits. The result is that a very few turns per coil, say one or two, will produce the full voltage. If a much lower voltage were insisted upon, the only way of obtaining it would be to reduce the number of slots greatly and accept


Fig. 5. Characteristics of a $31,250-\mathrm{kv}-\mathrm{a}$., 60 -cycle, 13,200 -volt, 80 Per Cent Power-factor 150 -r.p.m. Generator. Designed for high efficiency where the temperature rises will be much below the allowable 50 deg . C. by thermometer and 60 deg . C. by embedded detector
the additional losses and higher temperatures due to the losses incident to the high amperage per slot. There is also a serious objection to lower voltage machines in the case of these large capacity two-pole generators, due to the difficulty of making connections between coils of such great cross section of copper. As a rule, such limitations in the choice of potential
as the above do not occur in waterwhecldriven generators of the largest capacity. The limitation may occur if certain speeds are insisted upon in connection with large gencrators of any given periodicity; for example, a speed of $12 \cdot 4$ for 60 -cycle generator requires is poles and gives only two choices as to the number of circuits per phase, 2 or 29 . Twentynine circuits would be almost prohibitive, by reason of the complications in connections and the large number of turns per coil; hence, practically the same limitations exist as in a two-pole steam turbine generator when the number of poles is such that the factors are 2 and a prime number of large size, such as 29 .
As a rule, in connection with waterwheeldriven generators of large size, pressure is brought to bear from outside, to use the highest voltage, viz., 13,200 , on account of the saving in cost in the station wiring, switches, etc. Throwing such considerations aside, it is the author's opinion that an intermediate voltage, preferably 6600 , is the best for the largest capacity generators, inasmuch as the clectrical design can be made superior, due to the increased number of slots, the reduced size of the coils and the thinner insulation. It may be expected that the efficiency will be a little higher and the life a little longer. Machines of 6600 volts are seldom subject to any deterioration of insulation on terminal


Fig. 6. Characteristics of a $31,250-\mathrm{kv}-\mathrm{a}$., 60 -cycle, 13,200 -volt 80 Per Cent Power-factor, 1800-r.p.m. Steam Turbine Generator. The windage loss is large. The losses in the steam turbine generator are relatively different from those in a waterwheel generator; see Figs. 4 and 5
coils, due to corona, whereas 13,200 -volt machines in certain localities, especially at higher altitudes, are often subject to a certain amount of damage. Fortunately, it is possible in many cases to escape the objection to switches of great capacity, by running generator leads direct to the low side of step up transformers and by doing the switching on
the high side. Fortunately, such speed as 124 r.p.m. may, as a rule, be avoided, as most waterwheel builders can adapt their designs, without much loss, to a speed of cither 120 r.p.m. or $1281 / 2$, in the case of $60-\mathrm{cycle}$ generators, and thus make it possible to use a number of circuits that will allow a good $6600-$ volt winding to be developed.

## Efficiency

The importance of high efficiency is becoming more generally recognized. At the same time, competition in securing orders has a tendency to make designers go closer to the limits of allowable temperature rise, which tends in most cases to detract from the high efficiency that would otherwise be possible. In most waterwheel-driven generators very high efficiency is a fine investment for the purchaser. He can well afford to pay the higher price. Such high efficiencies almost invariably mean low temperature rise. In-


Fig. 7. Stator of the $20,000-\mathrm{kv}-\mathrm{a} ., 257$-r.p.m., 60-cycle, 11,000volt Horizontal Generator, City of San Francisco Hetch Hetchy Development
stead of going to the limit of 60 deg . C. or 80 deg. C. rise by the embedded detector, it is often the best engineering not to go higher than 40 deg. C. Fig. 4 shows segregated losses and efficiency of a $31,2.50-\mathrm{kr}-\mathrm{a}$., $1.50 \mathrm{r} . \mathrm{p} . \mathrm{m}$. generator, designed, in competition, to meet standard specifications in the matter of tem-
perature rise, while Fig. i) shows segregated losses and efficiency of a generator designed for highest efficiency at greater cost

The two generators have practically the same characteristics in other respects, reactance, stability, flywheel effect, etc. But the more efficient has an armature core of the


Fig. 8. Rotor of the $20,000-\mathrm{kv}$-a., 257-r.p.m., $60-\mathrm{cycle}$, 11,000-volt Horizontal Generator, City of San Francisco, Hetch Hetchy Development
best grade of silicon steel and a greatly increased quantity of copper in both armature and field. It is an easy matter for any user of such machines to calculate the value to him in dollars and cents on the original investment of the higher efficiency generator. He cannot determine accurately the greater value of the low temperature machine that will result, due to its longer life. It is generally agreed that a machine with the lower temperature will have its insulations remain in first-class condition longer than the one with the higher temperature.

Fig. 6 shows a corresponding efficiency curve for a $31,250 \mathrm{kv}-\mathrm{a}$., $1800-\mathrm{r} . \mathrm{p} . \mathrm{m}$. steam turbine generator. It will be seen by referring to this curve sheet, that the greatest loss is the windage ; furthermore, that the load losses are also high. This particular generator had its armature core built up of the best grade of silicon steel so that it does not seem possible at the present time to obtain any reduction in core losses. In like manner, the armature slots are as large as is consistent with lowest aggregate losses, while the rotor contains all the copper possible. Hence, there appears no way of reducing the $I^{2} R$ of either armature or field. These reductions would affect the efficiency but little in comparison with the effect. that might be obtained if it were possible to greatly reduce the windage and the load losses. It now appears possible by certain niceties in design, to considerably reduce the load losses.

# Isolated Phase Arrangement of Switching Equipment 

By 1'. M. Cirrier


and

W. 'T. O'Connell

(Onstriction Engineering Department
This article is the first that we have seen which fully describes the "isolated phase" construction for switching equipment, and which explains the merits of this system. 'The vertical and horizontal construction are discussed imb illustrations shown to emphasize the points made in the text. Attention is called to the fact that, when the phases are isolated, phase to phase short circuits will be eliminated.-EmTor.

The advent of the super-power station with its coneentration of power has necessitated that special consideration be given to the design of its switch house, in order to eliminate the probability of bus short circuits. By locating the three phases of the bus, each with its corresponding switching and protective equipment in compartments isolated from each other by firewalls, and connecting all circuits to the bus through reactors located in the same manner, a logical way of eliminating short circuits between buses has been obtained.*

[^27]While in thisarticle the application of isolated phase switch gear is discussed in its relation to the super-power station it is not the intention to limit its use to stations of large capacities. In general it may be said that its application depends upon the use of reactors, the type of oil circuit breaker used, the number of circuits and local conditions. In every case the choice of design can be made only after careful analysis of the problem.

There are two natural ways in which the phase may be isolated: first, with the corresponding equipment of each phase on the same floor and vertical firewalls between the phases as shown in Fig. 1. This is called horizontal


Fig. 1. Section of Horizontal Isolated Phase Switch House
phase separation. The second way is to locate the equipment for each phase on a separate floor as shown in Fig. 2. This is called vertical phase isolation.


Fig. 2. Section of Vertical Isolated Phase Switch House

Horizontal phase separation inherently requires a greater ground area than the vertical arrangement and as stations are usually located where land is valuable, this factor has considerable influence on the choice. Moreover, the switch operating mechanism for the
horizontal phase separation is more complicated and expensive than that required for vertical phase separation. Horizontal phase separation has several desirable features. For example, similar equipment may be located on the same floor, and the circuits terminate in a cable room directly below the reactors thus making a short run, as shown in Fig. 1.

Vertical phase separation inherently requires a building of considerable height. This is not objectionable from an architectural or constructive standpoint as the adjacent buildings in the group, including turbine room and


Fig. 2a. Plan of Switch House Shown in Fig. 2
boiler house, have considerable height and the switch house can be designed to present a similar external appearance. From the comparisons made of various layouts, it has been found that the rertical phase separation requires less cubical content of building than the horizontal phase separation. The space occupied by oil circuit breakers and reactors is practically the same for both. The saving in building space is therefore in the mechanism and cable rooms. This is evident when one considers that with the horizontal arrangement the operating mechanism must extend over the three phases of the oil circuit breakers, and that the width of the cable room is governed by the width of the circuit breaker rooms. On the other hand, with the vertical arrangement, the operating rods and bell cranks are located on the vertical walls of the mechanism aisles and the cables are dropped from the several floors through conduit located in the wall directly into end bells in the cable room below:

The application of horizontal phase isolat tion to switch honse design may in some cases be fomud advisable and practicable, but in general it may be sat that our experience has shown that fertical separation is less expensive, more flexible and better adapted to


Fig. 3. One-line Diagram
complicated layouts. In this article, we shall therefore confine our discussions primarily to vertical phase separation.

## Examples of Typical Layouts

To illustrate the simplicity of the isolated phase arrangement, as compared to the conventional threc-phase arrangement with the


Fig. 4. Section of Vertical Isolated Phase Switch House
three phases located in adjacent compartments in the same room, and the three phases of the oil circuit breaker mounted as a unit, let us consider several one-line diagrams that are typical of arrangements used by some of the large operating companies.

In Fig. 3 is shown the simplest circuit that should be considered for a large central station, namely, a double bus with selector
oil circuit breakers and reactors on the generator and feeder circuits. In Fig. 4 a plan and section of the vertical isolated phase switch honse, corresponding to this arrangement of equipment is shown.


Fig. 5. One-line Diagram *
In Fig. $\bar{j}$ is shown a one-line diagram of a complicated but very common type of circuit. The feeders have reactors and are grouped with two selector switches for each group of two or more feeders. Each generator circuit has a main oil circuit breaker, two selector oil circuit breakers and a reactor. Thus there are two breakers in series in every circuit. In Fig. ${ }^{6}$ a section of vertical isolated phase switch house corresponding to this arrangement of equipment is shown.

In Fig. 7 is shown a one-line diagram of a more complicated and very flexible and efficient circuit. Each feeder has a single oil circuit breaker and reactor. Four feeders are grouped together on each section of bus. Two


Fig. 4a. Plan of Switch House Shown in Fig. 4
selector oil circuit breakers are provided for each group bus. These breakers are interlocked so that either one, but not both, can be closed, thus connecting the group bus to either of the adjacent generators. Each generator is connected through a reactor and oil circuit breaker to a synchronizing bus and also through another oil circuit breaker to a stub-bus which can be connected to any


Fig. 6. Section of Vertical Isolated Phase Switch House Upper Floor Section AA Lower Floor Section BB
combination of four bus sections. In Fig. 2 a section of a vertical, isolated phase switch house corresponding to this arrangement of equipment is shown.

In Fig. 8 is shown a very complicated diagram of connections. This consists of double ring busses with reactors between the sections


Fig. 7. One-line Diagram
of each bus. Each bus section cath akain be divided by an oil circuit breaker. Each half section will have connected to it one generator, a number of feeders and a comnection to a common transfer bus. The feeders and generators will have both main and selector oil circuit breakers. In Fig. !a section of a vertical, isolated phase switch house corresponding to this arrangement of equipment is shown.

Reviewing the sections of switch houses shown in Figs. 2, 4, 6 and 9, it should be noted how simple the design of station becomes


Fig. 6a. Plan of Switch House Shown in Fig. 6
when vertical isolated phase arrangement of equipment is used, regardless of the complications introduced in the system of connections. The diagram shown in Fig. 3 is quite simple and probably would not find application in the larger stations but it is a typical diagram used by many of the moderately large stations throughout the country. The application of isolated phase to this arrangement is, however,


Fig. 8. One-line Diagram
desimble and warranted for the following reasons:

1. Bus short circuits practically eliminated
2. Short circuit st resses reduced
3. Space occuphod the same or less
4. Connections shertened and crossing of phases climinated
5. Comnections easily changed
6. Structure adapted to any type of oil circuit braker
panies and has the advantage of a fewer number of oil circuit breakers per feeder with only a slightly less reliability of operation. With this combination of switching equipment the advantages of isolated phase arrangement become more evident. A comparison of the arrangements pictured in Figs. 4 and 6 show the same arrangement of building, i.e., a (louble row of circuit breakers per floor, similar location of bus, reactors and operating mech-


Fig. 9. Section of Vertical Isolated Phase Switch House
Upper Floor Section AA-Lower Floor Section BB
7. Arrangement of reactors improved
S. Operating mechanisms removed from proximity to oil circuit breakers
9. Disconnecting switch mechanisms easily mechanically interlocked with mechanism of oil circuit breakers
The diagram shown in Fig. 5 is one that will probably find more general application in large stations as it uses two or less oil circuit breakers per feeder and at the same time has the advantage of two breakers in series. The connection shown in full line on the feeder circuits represents the familiar so called "H" connection which is used extensively by a number of large operating companies. By the addition of the circuits shown in dotted lines, this connection becomes the so-called group bus. This is also used by a number of com-
anisms, and while different types of oil circuit breakers are shown in the two arrangements and dimensions of compartments are different, either breaker is applicable to either arrangement, dimensions changing accordingly.

The designs shown in Figs. 2 and 9 have been included to illustrate that isolated phase arrangements can be applied to the most complicated circuits without introducing features other than an additional row of breakers or a bus or two. It should be noted that the general arrangement of equipment is very similar for all one-line diagrams as illustrated in Figs. 2 to 9 inclusive.

We have not attempted to show designs of switch houses using the conventional threephase arrangement of equipment for one-line
diagrams shown in Figs. 3, 5, 7 and 8 but will leave this for the reader to visualize. The complications involved in obtaining a design that is comparable even for the simple circuit shown in Fig. 3, where reactors are used on all circuits, are sufficient to require a building of the same or even greater dimensions. With circuits such as shown in Figs. 7 and $S$ the complications of buses and connections become so involved that it is quite evident that the isolated phase design will require less space and a simpler structure, and provide better operating conditions.

## Building

The number of circuits installed in the switch house of a large power station warrant that special consideration be given to the building housing this equipment. In general it is found desirable to locate this building


Fig. 9a. Plan of Switch House Shown in Fig. 9
independent of the main power plant. This depends, however, on local conditions and it may be preferable to build it as a section of the power house. In either case an isolated phase design is applicable.

The external appearance of this building, or section of building, should correspond architecturally to the power house. This may govern to some extent its overall dimensions. The building should house not only the main switching equipment, but also the switching and control equipments for the many auxiliary power circuits required for the station service. This latter equipment may take up as much or even more space than the main switch gear.

Isolated phase switch houses introduce no new features in building construction although in their design it would be highly desirable to eliminate all steel work were such construc-
tion feasible. Re-enforced concrete buikdings have some desirable features which those framed with structural steel do not possess.

The location of the different phases on separate floors must necessarily have some effect on the steel framing of the buitding. Sections of this framework form loops around the separate phases causing hysteresis and eddy current losses in themselves. Other sections of the steel work form loops parallel with the buses which result in currents being induced in them.

Troubles from hysteresis may be eliminated to a large extent by installing copper bands around all members of vertical loops at right angles to the busbars. Troubles due to induced currents in the stecl members, which would probably be encountered only in the joints, can be corrected by bonding the latter.

Re-enforcing steel in barricrs and walls in close proximity to conductors should be eliminated as much as possible, and when used must have sufficient cross section to carry, for a limited time, the current that will flow on a short circuit to ground. This rules out the use of wire mesh or metal lath for re-enforcing and calls for stecl rods of appreciable cross section. These rods must be well bonded together and well grounded at as many points as possible.

## Aisles and Cross Aisles

In addition to having the phases located in separate rooms isolated by fire walls it is also desirable to have the main and auxiliary buses and also the several oil circuit breakers on the same circuit in rooms separated by fire walls. The isolation of reactors from circuit breakers may also have some merits; this, however, requires another operating aisle and whether the advantage gained warrants the increase in width of building will depend on the space available for building and the scheme of connections. If bus reactors are used it would not be economical to put them in a separate room from the bus to which they connect. It is therefore questionable whether the isolation of reactors warrants the expense incurred. In Figs. 2, 4, 6 and 9 we have shorn reactors in the same rooms with oil circuit breakers, and this has been found to give a very satisfactory arrangement of equipment and also a minimum width of building.

The location of operating mechanisms for the oil circuit breakers and disconnecting switches in the same compartment as the equipment introduces a hazard and is objectionable. It also necessitates openings in the
floors between phases which permit communication of trouble. It has therefore been found advantageons to arrange the adjacent rows of oil cirenit breakers back to back with an aisle about if ft . wide between the compartment walls and to install in this space all the operating rods, bell cranks, ete. Operating mechanisms for oil circuit breakers and disconnecting switches have been adapted to this arrangement and a very simple and compact arrangement of mechanisms obtained. Operating rods are thus located remote from live parts in a position where they can be readily installed and adjusted without the need of entering oil circuit breaker rooms. The introduction of this aisle has simplified the problem very much and also increased the advantages of isolated phase station design. Conduits for instrument transformer leads can be run in this mechanism aisle and not buried in concrete, thus making them more accessible. The use of armored cable for instrument transformer leads is well adapted to this arrangement and would no doubt simplify the conduit system of the station. This aisle also provides space, isolated from live parts, for air shafts for the ventilating system of the station.

Cross aisles and transverse fire walls should be provided to isolate groups of equipment. The location of these will usually be governed by the number of generators or sections of bus. These cross aisles should be of sufficient width to remove equipment. It is also desirable that elevators and stairways be located at these cross aisles to facilitate access to all floors and also removal of apparatus.

The aisles in the oil circuit breaker rooms should be liberally designed to permit inspection and removal of the equipment. The elimination of hand operated disconnecting switches, however, removes a limitation encountered in the three-phase arrangement and the width of these aisles may be encroached upon without introducing hazards in the operation of the station.

The vertical phase isolation inherently requires a narrow building, so that liberal spacing can be given to the aisles, and may even be found necessary in some cases to obtain correct architectural features for the exterior of the building.

The use of windows in isolated phase switch houses is questionable except at the cross aisles. " They admit light only to the outer aisles and artificial illumination is necessary in all others; furthermore, if windows are installed space must be left in front of them
in which equipment camnot be placed and is therefore of no value. Again the cable ducts are generally rum in these outer walls and windows would interfere with them. Windows are more of a detriment than an aid in the ventilation of the building since stations of this type require an artificial ventilating system, using blowers, either forced or induced, so that the opening of these windows woukl destroy the effectiveness of the ventilating system.

The system of illumination used in the cross aisles, mechanism aisles, etc., can be in accordance with the general practice, but in the oil circuit breaker rooms exposed fixtures should be eliminated and ceilings recessed at the outlets to form reflectors for the lighting units. Moderate sized lamps should be used and the spacing should be such that the compartments are well illuminated in order to facilitate inspection and repair of apparatus.

## Control Room

The control room should be located adjacent to the mechanism floor of the building in order to facilitate access to the operating mechanisms and the disconnecting switch levers. This location also has the advantage of shortening the length of the control circuits to the breaker mechanisms, and the secondary leads to the instrument transformers. As the space above the breakers in the mechanism room is all occupied, and since the control room should have a room below it for terminating conduits, this control room may be conveniently located above the section of building taken up by the station service equipment. If this location is not possible the center section of the building can be carried up two floors above the mechanism floor, and thus room provided for terminating the conduit and installing the control equipment.

## Cable Room

The number of feeder cables radiating from such a switch house as we are considering warrants provision being made for a cable room in which to terminate the connections from the separate phases at the end bells of the three-conductor lead sheath feeder cable. A flexible system of arrangement of feeder cable ducts should be provided so that the cable may terminate at a point in the duct line directly below the breaker to which it connects. By properly designing these runs of conduit the changing over of a cable from
one section of the bus to another, at some future date, may be greatly facilitated.

## Buses

In the conventional three-phase arrangement of buses, where they are in close proximity to each other, the need of enclosing them in concrete compartments is evident. In an isolated phase arrangement, however, the separate phases of the buses are entirely remote from each other and the use of a bus covered with insulation may be considered instead of one run in a compartment. This compartment at best must be opened at every oil circuit breaker so that little advantage is gained, and considerable expense and inconrenience encountered, by its use. All of our high interrupting capacity oil circuit breakers are rented and there should be no throwing of oil which would affect this bus. Attention is called to the ease with which such a bus as shown in Fig. 4 can be installed and inspected. Considerable saving in the cost of bus supports is experienced in the use of isolated phase design, due to the limitation of the possible short circuit current and the elimination of magnetic stress between phases.

## Connections

For circuits carrying heary currents bar connections must necessarily be used; however, where feasible, insulated cable connections with long radius bends are preferable. Due to the liberal spacing obtained the magnetic stresses between adjacent conductors are materially reduced and special extra heary duty supports are not in general required. Only where the circuits form loops or where sharp bends must be made is it necessary to give special consideration to the supports.

## Disconnecting Switches

In all isolated phase arrangements the disconnecting switches used to isolate the oil circtit breakers have been made gang operated from a point remote from the switch aisle (usually the mechanism room) and have been interlocked with the mechanism of the oil circuit breaker in such a manner that they camnot be operated except when the oil circuit breaker is open. While this féature is necessary in isolated phase construction it by 110 means belongs to isolated phase exchisively. It is a feature which should be incorporated in any design where large amounts of power are involved. This is due
to the fact that the uperation of such disconnecting switches should be at a pint remote from the oil cirenit breakers and should be interlocked with the oil circuit breaker mechanism. There are instances on record where, after a heary short circuit in a switch house of conventional three-phase construction, it was twenty minutes before the operators could get into the switch room to operate the disconnecting switehes necessary to resume operation.

The disconnecting switches used to isolate the oil circuit breakers are usually operated in gangs of six, three on each side of the oil circuit breaker. By locating the operating handles on the mechanism room floor they are made remote from the breakers themselves, easily interlocked with the oil circuit breaker mechanism, and usually in a convenient location for operation. Means should be provided to lock the disconnecting switch mechanisms in the open position in order that they shall not be operated, except by the proper person when the equipment is isolated for repairs. The disconnecting switches for isolating the oil circuit breakers are most conveniently mounted on the back wall of the oil circuit breaker compartment. The operating rods for these disconnecting switches are placed in the mechanism aisle.

The disconnecting switches used to isolate the outgoing cables may be made either of isolated phase or of the conventional threephase arrangement since they are on the outgoing side of the reactor. They may be operated either by a remote hand operated mechanism, if it is desired to interlock them with an oil circuit breaker, or they may be operated by levers located adjacent to them. These switches may be operated single-pole or three-pole. It is generally more convenient to locate these disconnecting switches in the cable room.

The disconnecting switches themselves are of two kinds, the lever type, and the brush type. The lever type is the common form of disconnecting switch. The brush type was designed primarily for a special case where it was desired to have the disconnecting switches operated automatically by the oil circuit breaker mechanism, in such a manner that they are closed before the oil circuit breaker is closed and opened with a certain time delay after the oil circuit breaker opens.

Remote operated disconnecting switches do not need to be equipped with safety catches since ther are held chosed by their operating mechanisms.

If it is desimed to ground the equipment for inspection or repairs the disconnecting switches can be made double-throw and one of the elips msed as a grounding elip. In the brush type disconnceting switeh the gromnding contact is made of the wedge and finger type.

## Oil Circuit Breakers

Practically any oil cirenit breaker in which the different phases are located in separate tanks can be adapted to isolated phase arrangement, but it has not yet been thought desirable except on those of higher interrupting capacity.

The following is a list of oil circuit breakers which may be considered for isolated phase designs, with their interrupting capacities in amperes at 15,000 volts.

| Type of Oil Circuit Breaker | Interrupting Capacity |
| :---: | :---: |
| FH-103 |  |
| FH-203 | 10,000 |
| FH-206 | 14,000 |
| FH-209 | 20,000 |
| FHD-17 | 30,000 |
| FHD-21 | 34,500 |
|  | 58,000 |

Type FHK-130 (tank type) oil circuit breakers can also be furnished for the same range of interrupting capacitics in amperes at 15,000 volts.

The Type "FH" oil circuit breakers, namely the FH-103, FH-203, FH-206, FH-209 are similar to the familiar FH-3, FH-6, and FH9 breakers with live pots but are improvements on the latter. These breakers are for cell mounting and although they may be either bottom or back connected, in isolated phase arrangements they are usually back connected. When these breakers are used in a vertical isolated phase design it is necessary to have a paralleling mechanism mounted in the oil circuit breaker compartment over each pole. When this type of breaker is used in a horizontal vertical phase arrangement the paralleling mechanisms may be mounted on the mechanism floor directly above each pole. These breakers may be furnished with the plane of the pots perpendicular to the bus, socalled "parallel pots;" or parallel to the bus, so-called "tandem pots." Since the width of the oil circuit breaker cell is usually determined by that of the reactor cell, the length of the bus generally cannot be decreased by the use of parallel pots and they will cause an increase in the depth of cell which will increase the width of the building. The use of tandem pots greatly simplifies the connections be-
tween the oil eirenit breakers and their disconnecting switches.

The Type FHD oil circuit breakers like the Type Fill breakers open the circuit by an upward movement. 'Theontside pots, however, manlike the 'Yype FH, are dead; the are being broken in an internal explosion chamber which is insulated from the outer pot. The contacts on top of the breaker are alive when the disconnecting switches are closed. These breakers may be mounted fixed in the cell or they may be mounted so that they will be casily removable from the cell in one of two ways. They may have the pots mounted upon a truck, which runs on rails set into the floor of the cell, or have wheels under the top of the switch which run on rails held by brackets mounted on the barrier walls. In either case bolted connections may be made to the oil circuit breakers or they may connect through truck type contacts mounted on the rear wall of the switch compartment. These breakers can be furnished with either "parallel" or "tandem" pots. The pots being dead it is possible to mount the paralleling mechanisms between them, these paralleling mechanisms being mounted on the same member that supports the pots. That is, if the pots are mounted upon a truck, the paralleling mechanism is mounted on the truck; if supported by the top of the switch, the paralleling mechanisms are underhung from the top of the switch.

The Ty.pe FHK-130 oil circuit breakers have a downward break. Each phase has two explosion chambers contained in, but insulated from, a round steel tank. The paralleling mechanism is located within the cover of the tank and each pole is operated by means of a shaft which comes out of a bearing in the side of the housing. These breakers can be mounted fixed in the cell, or upon a truck which runs on rails set into the floor, or on wheels under the top of the breaker which run on tracks supported by brackets on the barrier walls.

The operating rods of the FHD or FHK 130 oil circuit breakers are placed in the mechanism aisle with suitable bell cranks and levers to connect with the paralleling mechanisms. The operating mechanisms are mounted on the mechanism room floor directly above the aisle. These operating mechanisms are the same standard types that would be used in a conventional three-phase arrangement; motor operated mechanisms for the Type FH and FDH breakers and solenoid operated for the FHK-130 type breakers.

Horizontal separation may take, for the same type of oil circuit breaker, a larger mechanism than would be required for vertical separation.

In choosing between these types of oil circuit breakers the first consideration is interrupting capacity, the second is the available space. As stated before, the width of cell is usually dependent upon the width of the reactor cell which leaves only height and depth of cell to be considered. In the following table the approximate inside cell dimension of the various oil circuit breakers are given. These values are for "Tandem" arrangement and take into consideration not only the oil circuit breakers themselves but also the spacing of disconnecting switches, etc., and are given as tentative values only.

| Type | Height | Width | Depth |
| :---: | :---: | :---: | :---: |
| FH-103 and 20.3 | $5 \mathrm{ft} 6 in.$. | 3 ft .0 in. | 2 ft .3 in . |
| FH-206 | 6 ft .0 in . | 3 ft .6 in. | 2 ft .6 in . |
| FH-209 | 6 ft .10 in . | $4 \mathrm{ft} .21 / 2 \mathrm{in}$. | 2 ft .6 in . |
| FHD-17 | 6 ft .6 in . | $4 \mathrm{ft.0} \mathrm{in}$. | 3 ft .0 in . |
| FHD-21 | 7 ft .6 in . | $4 \mathrm{ft.8} \mathrm{in}$. | 3 ft .6 in . |

## Potential Transformers

In the first part of this article we pointed out that electrical isolation was obtained by connecting all circuits to the bus through reactors. The potential transformers are an exception to this; but in order to maintain electrical isolation, they must be connected from bus to ground instead of from bus to bus.

This I connection of potential transformers brings up the question of what connections should be used for metering. This depends upon the possibility of the equivalent of a fourth wire current through grounding at different points. There are two conditions which must be considered:

1st. If there is only one ground on the system and proper provision is made to immediately remove all other grounds as they appear. Ender this condition three transformers may be used with both their primary and secondary windings connected in Y. This provides the equivalent of delta voltage transformation and a two-coil meter can be used. If assurance can be given against the continuance of external grounds this is the better of the two systems.
$2 n d$. If the system is grounded in more than one place there are two connections which may be used depending upon whether one of the grounds is available or not. If it is, two potential transformers connected from
bus to ground may be userl. If not, three potential transformers connected from the three buses to a common point, with their impedances correctly adjusted to make this point a correct neutral for the system, may be used. In these latter cases a four-wire 3 -phase (that is 3 -coil) meter shoukd he used.

The potential transformers should be connected to the bus through resistances and fuses as usual. It may be noted that in all of the arrangements shown potential transformers may be conveniently located between the reactor and the oil circuit breakers.

## Current Transformers

Although by the use of an isolated phase design the currents which flow when short circuits occur are limited by the reactors to a value much less than that which might be obtained with a bus short circuit on a conventional three-phase layout, still, with the size of station which we are considering, these short circuit currents are of considerable magnitude, and the current transformers which must carry them should be of rugged construction. Probably the most rugged and easily installed type of current transformer is the bar type or slip over type either of which consists of a straight primary conductor about which a core carrying the secondary windings is placed. Such a current transformer can be designed with meter accuracy for high ratios but on the lower ratios the accuracy becomes poorer. Current transformers with multiple turn primaries which have meter accuracy on the lower ratios can be made with high mechanical strength but are more expensive and take up more space.

On the "FHK" type of oil circuit breakers it is possible to use bushing type current transformers. These, like the bar type current transformers. can be designed with meter accuracy for the higher ratios but on the lower ratios they are not as accurate as the bar type current transformers.

In a majority of the present existing and proposed isolated phase installations bar type current transformers have been used. If one refers to the arrangements of isolated phase stations shown in Figs. 1, 2, 4, 6, and 9 the convenience with which the current transformers can be installed in the connections between the reactors and the oil circuit breakers is apparent.

## Current Limiting Reactors

Since current limiting reactors are one of the fundamental requisites of isolated phase con-
struction, considerable attention should be given to their design and installation. The reactors should hawe the following characteristies:

High mechanical strength
Non-inflammability
Low loss
Ample electrical clearance between turns; between layers; and from windings to ground.
There seoms to be a growing tendency among central station engineers to request that reactors be furnished with a larger cross section of conductor than has been used in the past. This is probably due partly to the fact that the load factors have increased to such a point that in capitalizing losses a greater initial investment is warranted in order to keep them to a low valuc; and also due to a desire to increase the thermal capacity of the reactor for short circuit conditions. In the past all of our feeder reactors have been designed to withstand for two seconds the current which would be obtained if sustained rated voltage was impressed across their terminals. We believe, however, that the cross section of the conductor used in a reactor should be such that it will carry abnormal current without failure for a greater length of time than the conductor which is connected to it.

In laying out the section of the building in which the reactors are to be placed care should be taken to make certain that it shall be possible to maintain certain definite magnetic clearances between the reactors and any iron work having a cross section greater than can be enclosed in a circle $11 / 2$ inches in diameter. An exception can be made of magnetic material having a cross section of $1 / 4$ inch or less by 12 inches or less.

In a large number of cases the width of the reactor cell (which is dependent upon the diameter of the reactor) is the factor which determines the length of the bus. It is desirable to keep the length of bus to as short a value as possible. There is usually plenty of head room, however, and therefore from the standpoint of building layout it is desirable to use a tall slender reactor. The most efficient design of reactor is ordinarily one in which the diameter is equal or greater than the height. The curves in Fig. 10 show for a typical rating of reactor the variations in height, cost, and watt loss plotted against diameter. These curves show that after a certain point is reached a decrease in diameter is obtained only by a considerable increase in the other
factors. It will be noticed that the ordinate lalues of the second and third points are ncarly equal. This is due to the necessity of using certain standard forms to conform with manufacturing conditions.

In certain cases it is preferable to limit the length of the station by adding slightly to the width. When this is the case it is possible to build the reactors with the planes of the coils vertical instead of horizontal; the latter being the usual construction for "cast in concrete"


Fig. 10. Example of Variation in Height, Watt Loss, and Cost with Change of the Diameter of a Current Limiting Reactor
type of reactors. Under this condition an increase in the diameter of the reactor causes an increase in the height and depth necessary for the reactor cell. Within certain limits, then, the width of the cell may be decreased with an increase of the diameter of the reactor. For example, if such a reactor should be cast with the coils having the same size, number, and spacing as those of the reactor with the larger diameter in the above curves, it would have the following dimensions:

$$
\begin{array}{lcc}
\text { Height } & \text { Width } & \text { Depth } \\
47 \text { inch } & 251 / 2 \text { inch } & 34 / 8-\text { inch }
\end{array}
$$

The losses of course would be the same as those shown on the curve for the $3 t^{5}$ s inch diameter reactor and the cost would be increased by about is per cent.

By balancing the saving in building cost due io the decreased length against the increased cost due to the decrease of diameter of the reactor，or in another case balancing the difference－in cost due to the different shape of building against the change in cost due to a different shape of reactor，an economic bal－ ance may be obtained．There is of course no use in decreasing the size of the reactor cell to a value smaller than the necessary width of the oil circuit breaker cell．

All of the dimensions given have been those of the reactors themselves．In installing re－ actors in cells it is of course necessary to provide proper electrical and magnetic clear－ ance，and unless the reactors are far enough apart（which is not generally the case）braces must be installed，which may further increase the clearance between the reactor and the cell walls．

In isolated phase installations the reactors in the various phases of the same circuit are installed with such a large distance between them that it is not necessary to brace them against thestresses due toa short circuit on any one feeder．If，however，a short circuit involves the same phase of two adjacent feeders at the same time，it is necessary in most cases to brace the reactors．Under such a condition the currents in similar phases of the two adjacent circuits will be in the same direction and the force between the leads connecting to the reactors will be attractive．The reverse is true of the reactors themselves if they are built and connected symmetrically．In this case there will be a repulsive force between the reactors．If all the reactors of one phase are installed in a single straight line，they may be braced against movement along that line by compression type braces．When the reactors of one phase are installed in two adjacent straight lines，there may be a repul－ sive force between corresponding reactors in the two lines，which cannot be checked by a compression type brace．In the latter case strain insulator braces may be used instead of the compression braces．These strain braces should be placed not only between adjacent reactors in the same line but also between the reactors in the two lines．

The leads coming and going to and from the reactors are usually installed with such dis－ tance between them that it is not necessary to brace heavily，against magnetic forces incident to short circuit：except that great care should be exercised in bracing such leads if they cut the field of the reactor transversely．

Ground and Test Buses
The location of ground and test huses will depend somewhat upon the arrangement of equipment and largely upon local conditions． It will be found，however，that these may be incorporated in the isolated phase design much more easily than in a conventional three－ phase design．

## Costs

There scems to be prevalent an opinion that isolated switch house construction requires large buildings，special equipment and in general is very expensive．The designs shown in the fore part of this article indicate that the isolated phase arrangements as there applied should not take up any more space and will probably effect a saving in size of building required for a conventional three－phase arrangement．A large number of compara－ tive studies have been made which show in all instances a saving in cost of building in favor of isolated phase．The amount depends en－ tirely on the type of equipment and arrange－ ment used；in one of the above cases amount－ ing to 15 per cent．

The cost of materials and labor used in the buses and connections show a considerable reduction for isolated phase，this again depend－ ing on the system of connections．

The cost of remote mechanically operated disconnecting switches will be increased 10 to 15 per cent，which is warranted by the improved operating conditions．

To change the mechanism of oil circuit breakers in order to make them suitable for isolated phase arrangement will increase their cost from 5 to 2.5 per cent，depending upon the type of oil circuit breaker used．

The cost of the reactors will be the same unless a special design of reactor has been used to effect a saving in building cost（see curve shown in Fig．10）．

The unit cost of instrument transformers will be approximately the same with a possible advantage for the isolated phase．

A considerable saving can also be made in the conduit system for instrument and control leads．This saving is not only in the first cost but also in maintenance．

The overall cost of an isolated phase switch house may or may not show a saring over the conventional arrangement，depending on the proportional effect of the factors listed above．

## Conclusion

In the foregoing paragraphs it has been shown that isolated phase arrangements pos－ sess many desirable features，which would
justify an increase in cost. These features, howerer desirable, are nevertheless incident to the design. The hasic inlea of isolated phase arrangement is to diminate all bus short circuits from phase to plase. (It is understoon that short circuits from one phase of bus to ground will be linnted by the use of a nentral grounded resistor.)

The climination of phase to phase short circuits is obtained by spacing the buses a considerable distance apart with fire walls between them. All circuits are connected to these buses through reactors which are spaced apart in the same manner as the bus. After a circuit is passect through these reactors it is no longer part of the bus. The only way in which a bus short circuit from phase to phase can occur is as a simultaneous failure of two
reactors on the same circuit or as simultancous faults to ground in two phases. With properly designed reactors the former case is very improbable. Also if the buses are properly insulated and installed, simultaneous failures of two plases to ground are quite improbable. It is admitted that with a well designed conventional three-phase bus properly installed, a phase to phase bus short circuit is an infrequent occurrence; but there is a possibility of its taking place with consequent damage to property, service and possibly life. It is the duty of every engineer responsible for the design and construction of a large power station to investigate such possibilities and eliminate them wherever feasible. In the case of the elimination of bus short circuits we belicve that the answer is "ISOLATED PHASE."

# A Transmission Line Calculator 

By Edith Clarke

Lighting Engineering Department, General Electric Company


#### Abstract

The author shows that the equations met in transmission line problems are capable of solution on a calculator. She has designed such a calculator and describes it and its use in the present article. Two supplements, included in the article, furnish a calculator in paper form together with directions for its assembly and use.-Editor.


Transmission line calculations, as ordinarily performed by means of the wellknown series or hyperbolic formulas, require a great deal of time and labor. In order to reduce the time and labor involved, a transmission line calculator has been developed, a working model of which is given in Supplements I and II. This Calculator may be assembled according to the directions for assembling given on Supplement II and operated according to the directions for use given on Supplement I.

The Transmission Line Calculator is a mechanical device which solves graphically equations which consider the effect of distributed resistance, inductance and capacitance. The effect of leakance is neglected in this Calculator, although it is possible to design a calculator which will include it. Certain assumptions have been made in designing the Calculator for which corrections may be applied where a high degree of precision is desired. Any degree of precision may be obtained with this type of calculator if sufficiently large and free from mechanical defects. The working model of the Calculator given in Supplements I and II, if carefully
assembled, may be used to advantage for preliminary calculations in connection with proposed transmission lines. If mechanically correct, it will give results without appreciable error for lines up to 2.50 miles in length at 60 cycles, 300 miles at 50 cycles, or 600 miles at 25 cycles. For lines 400 miles in length at 60 cycles the error may be about 1 per cent. The error increases with the length of line, but even at the extreme range of the Calculator it will not be more than about 2 per cent for voltage and current values. Since the power at the generator end is obtained from the product of voltage and current, the error in the power may be twice as large as that in voltage or current. It is possible by applying corrections to the calculator given in Supplement I to eliminate all errors, but this is hardly worth while on a paper calculator, mechanically defective. Transmission lines may easily be calculated on the Calculator in less than one-tenth the time ordinarily required for similar calculations made in the customary manner.

To test an assumed transmission line for satisfactory operation, it is customary to start at the receiver end, assuming all condi-
tions as desired at that end, then to calculate by means of suitable equations the conditions at the generator end. The procedure with the Calculator is the same, the only difference being that the Calculator solves the equations graphically by means of movable vectors. In this discussion, the transformers at the ends of the line are not included. Generator end and receiver end refer to the ends of the line on the high-voltage sides of the transformers.

## THEORY OF CALCULATOR

The equations upon which the Calculator is based are as follows:*

$$
\begin{align*}
e_{g} & =e_{r}\left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{24}+\frac{Z^{3} I^{3}}{720}+\ldots\right) \\
& +I_{r} Z\left(1+\frac{Z Y}{6}+\frac{Z^{2} Y^{2}}{120}+\frac{Z^{3} Y^{3}}{5040}+\ldots\right)  \tag{1}\\
I_{g} & =I_{r}\left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{24}+\frac{Z^{3} Y^{3}}{720}+\ldots\right) \\
& +e_{r} Y\left(1+\frac{Z Y}{6}+\frac{Z^{2} Y^{2}}{120}+\frac{Z^{3} Y^{3}}{5040}+\ldots\right) \tag{2}
\end{align*}
$$

The following notation will be used throughout:
$E_{g}=$ Volts between lines at generator end
$E_{r}=$ Volts between lines at receiver end
$K V_{g}=$ Kilovolts between lines at generator end
$K V_{r}=$ Kilovolts between lines at receiver end
$e_{g}=E_{g} / \sqrt{3}=$ volts to neutral at generator end
$e_{r}=E_{r} / \sqrt{3}=$ volts to neutral at receiver end
$I_{g}=$ Amperes line at generator end
$I_{r}=$ Amperes line at receiver end
$K W_{r}=$ Total kilowatts at receiver end
$K V-A_{c}=$ Total $\mathrm{kv}-\mathrm{a}$. of condenser at receiver end
$l=$ Length of line in miles
$f=$ Frequency in cycles per second
$R=$ Resistance per mile of one conductor in ohms
$L=$ Inductance per mile of one conductor in henries
$C=$ Capacitance per mile of one conductor in farads

[^28]$X=2 \pi f L=$ Reactance per mile of one conductor to neatral in ohms
$z=\mathrm{R}+j X=$ Impedance per mile of one conductor to neutral in olims
$Z=l z=l(R+j X)=$ Total impectance of one conductor to neutral in ohms
$y=0+j 2 \pi f C=$ Admittance per mile of one conductor to nettral in mhos (Leakance $=0$ )
$Y=l y=l(j 2 \pi f C)=$ Total admittance of one conductor to neutral in mhos
$(p . f .)_{g}=$ power-factor at generator end
(p.f. $)_{r}=$ power-factor at receiver end
$K=K W_{r} / K V_{r}{ }^{2}=$ Ratio of kilowatts at receiver end to square of kilovolts at receiver end
$K^{\prime}=K V-A_{c} / K V_{r}{ }^{2}=$ Ratio of condenser kilovolt-amperes to square of kilovolts at recciver end
$S / D=$ Ratio of flat spacing between conductors in feet to diameter of conductor in inches

Any desired degree of accuracy may be obtained by using equations (1) and (2) for transmission line calculations, provided a sufficient number of terms of the series are taken. For lines under 200 miles in length with a frequency of 60 cycles per second, two terms of the series ordinarily give results sufficiently accurate, but for longer lines, or higher frequencies, more terms of the series should be used. The Calculator may be used with lines of any length, but when the lines are long and the calculations become laborious, the Calculator is most useful, for the third and higher terms of the series have been taken into considcration in the design of the Calculator whenever it was found necessary to do so.

Equations (1) and (2) may be further simplified and made more convenient for numerical calculations if equation (1) is divided by $c_{r}$, and cquation (2) by $I_{r}$.

$$
\begin{aligned}
& \frac{e_{g}}{e_{r}}=\left(1+\frac{Z \mathrm{Y}}{2}+\frac{Z^{2} \mathrm{I}^{2}}{24}+\ldots\right)+ \\
& \frac{I_{r}}{e_{r}} Z\left(1+\frac{Z \mathrm{Y}}{6}+\frac{Z^{2} \mathrm{I}^{2}}{120}+\ldots\right) \\
& \frac{I_{g}}{I_{r}}=\left(1+\frac{Z \mathrm{Y}}{2}+\frac{Z^{2} \Sigma^{2}}{24}+\ldots\right)+ \\
& \quad \frac{e_{r}}{I_{r}} \mathrm{I}\left(1+\frac{Z Y}{6}+\frac{Z^{2} Y^{2}}{120}+\ldots\right)
\end{aligned}
$$

Since $I_{r}=\frac{K W_{r}}{\sqrt{3} K V_{r}\left(p . f^{\prime}\right)_{r}}$ in magnitude and
makes an angle $\phi$ with $e_{r}$ such that $\cos \phi=$ （p．f．$)_{r}$ ．

$$
\begin{aligned}
& I_{r}=\frac{\text { K } \|_{r}}{13 \text { K } V_{r} e_{r}\left(p . f_{r}\right)_{r}}(\cos \phi \pm j \sin \phi)
\end{aligned}
$$

$$
\begin{aligned}
& I_{r}=\frac{\kappa_{r}^{-1} 10^{-3}}{(p . f .)_{r}^{-}}(\cos \phi \pm j \sin \phi)
\end{aligned}
$$

the positive sign in the $\pm$ ambiguity to be used when the power－factor at the receiver end is leading，and the negrative sign when it is layging．

Equations（1）and（ 2 ）now become：

$$
\begin{align*}
& \frac{c_{g}}{c_{r}}=\frac{E_{g}}{E_{r}}=\left(1+\frac{Z V}{2}+\frac{Z^{2} V^{2}}{2 t}+\ldots\right)+ \\
& \frac{K^{-} 10^{-3} Z}{\left(p \cdot f_{0}\right)_{r}}\left(1+\frac{Z \mathrm{Y}^{-}}{6}+\frac{Z^{2} Y^{2}}{120}+.\right)(\cos \phi \pm j \sin \phi)  \tag{3}\\
& \frac{I_{g}}{I_{r}}=\left(1+\frac{Z \mathrm{I}^{r}}{\underline{2}}+\frac{Z^{2} \mathrm{~V}^{2}}{2 t}+\ldots\right)+ \\
& \frac{(\text { p.f. })_{r} I}{\mathrm{~K} 10^{-3}} \frac{\left(1+\frac{Z \mathrm{I}^{r}}{6}+\frac{Z^{2} \Gamma^{2}}{120}+\ldots\right)}{(\cos \phi \pm j \sin \phi)} \tag{4}
\end{align*}
$$

$E_{g}{ }^{\prime} E_{r}$ is a vector quantity whose magnitude is the ratio of the voltage at the generator end to the roltage at the receiver end and whose slope is the angle by which the voltage at the generator end leads the voltage at the receiver end．
$I_{g} / I_{r}$ is a vector quantity whose magnitude is the ratio of the current at the generator end to the current at the receiver end and whose slope is the angle by which the current at the generator end leads the current at the receiver end．

## Assumptions

The Transmission Line Calculator solves the equations（3）and（4）graphically when the following assumptions are made：

1．The real part of the series

$$
\left(1+\frac{Z Y}{2}+\frac{Z^{2} \Gamma^{2}}{24}+\ldots\right)
$$

is a function of the product of frequency and length of line，and for a given value of this product is independent of the line constants．
2 ．The vector magnitude of the series

$$
\left(1+\frac{Z Y}{6}+\frac{Z^{2} \mathrm{Y}^{2}}{120}+\ldots\right)
$$

is a function of the product of frequency

[^29]and length of line，and for a given value of this product is independent of the line constants．
When the product of frequency in cycles per second and length of line in miles is less than 15,000 （i．e．， 250 miles at 60 cycles or $6(0)$ miles at 25 cycles，$f l=15,000)$ ，the error in the above assumptions is negligible．The error increases as the product，$f l$ ，increases， but it is less than 1 per cent throughout the range of this calculator．

The scries involved in equations（3）and（4） are vector quantities，and may be denoted as follows：

$$
\begin{aligned}
& \left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{24}+\ldots\right)=a=a_{1}+j a_{2} \\
& \left(1+\frac{Z Y}{6}+\frac{Z^{2} Y^{2}}{120}+\ldots\right)=b=b_{1}+j b_{2}
\end{aligned}
$$



Fig．1．Product of Inductance and Capacitance per Mile for Single Conductor

If substitution is made for $Z$ and $Y$ in the series in terms of $R, L, C, f$ and $l$ ，it can be shown that the real parts of these vectors， $a_{1}$ and $b_{1}$ ，are approximately constant for a given product of frequency and length of line．This is due to the fact that the product of $L$ and $C$ is practically constant for high－ voltage transmission lines．The product $L C$ as a function of $S / D$ ，the ratio of the flat spacing between the conductors in feet to the diameter of the conductor in inches，is given in Fig．1．The familiar formulas＊for $L$ and $C$ are given in terms of the ratio of triangular spacing between conductors and radius of the conductor，expressed in the
same units. S' $D$, the ratio of the flat spacing between conductors in feet to the diameter of the conductor in inches, is used here because of its greater convenience. For high-voltage transmission lines, $S^{\prime} D$ lies between 10 and 40. The product $L C$ is approximately constant within this range of $S / D$. If an average value of $S / D$ is assumed, for example, $S / D=20$, and the corresponding value of $L C$ selected, the error in assuming $L C$ constant for all high-voltage transmission lines will be very small. Although $a_{1}$ and $b_{1}$ are not independent of the line constants, they are but little affected by variations in these constants, except for very long lines.
per mile and $S, 1)=20 .(1$ are givem in Table 11 The vector magnitude and slopee, as wodl as the real and imaginary parts of the serics, ate given. These values of a amot $h$ wore used in making the Calculator.

## Equations Solved Graphically by Calculator

The Transmission Line Calculator is designed to solve graphically equations (:3) and (4). The right-hand members of these equations consist of two terms each, both of which are vectors. $E_{g} E_{r}$ and $I_{g} I_{r}$ are likewise vectors. In order that the magnitude and slope of $E_{g} / E_{r}$ and $I_{g} I_{r}$ may be readily determined, the Calculator is provided with a polar coordinate chart. The magni-

TABLE I
$a_{1}$ AND $b_{1}$ FOR VARIOUS LINE CONSTANTS WITH $f l=15,000$ AND 30,000

| $f l$ | $\stackrel{f}{\text { cycles }}$ | $\stackrel{l}{\text { miles }}$ | $\stackrel{\mathrm{R}}{\mathrm{R}}$ | $S / D$ | $a_{1}$ | $b_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15000 | 60 | 250 | 0.2 | 20 | 0.8699 | 0.956 .3 |
| 15000 | 60 | 250 | 0.2 | 10 | 0.8693 | 0.9562 |
| 15000 | 60 | 250 | 0.2 | 40 | 0.8704 | 0.9564 |
| 15000 | (6) | 250 | 0.1 | 20 | 0.8701 | 0.956 .3 |
| 15000 | (6) | 250 | 0.3 | 20 | 0.8697 | 0.9563 |
| 15000 | 50 | 300 | 0.2 | 20 | 0.8698 | 0.9563 |
| 30000 | 60 | 500 | 0.2 | 20 | 0.5116 | 0.8316 |
| 30000 | 60 | 500 | 0.2 | 10 | 0.5089 | 0.83066 |
| 30000 | 60 | 500 | 0.2 | 40 | 0.5137 | 0.832:3 |
| 30000 | 60 | 500 | 0.1 | 20 | 0.5136 | 0.8320 |
| 30000 | 60 | 500 | 0.3 | 20 | 0.5084 | 0.8309 |
| 30000 | 50 | 600 | 0.2 | 20 | 0.5104 | 0.8313 |

If line constants are assumed and these series calculated for various values of $f l$ (the product of frequency and length of line) it will be seen that for lines of such length that only two terms of the series need be used, the real parts, $a_{1}$ and $b_{1}$, of these series are independent of the line constants. That is, for a given product of frequency and length of line, $a_{1}$ and $b_{1}$ are constant no matter what the line constants. For long lines, where the third and even higher terms of the series need be used, $a_{1}$ and $b_{1}$ vary with variations in the line constants, but the variation is not great even for the extreme range of the Calculator. It is possible, therefore, to calculate $a_{1}$ and $b_{1}$ from average line constants for various values of $f l$ and to assume, with but slight error, that these values of $a_{1}$ and $b_{1}$ are constant for a given value of $f l$.

Table I gives $a_{1}$ and $b_{1}$ for various line constants with $f l=15,000$ and 30,000 .

Calculations of $a$ and $b$ for various lengths of line at 50 and 60 cycles with $R=0.2$ ohms
tude of the vector $E_{g} E_{r}$ is the ratio of the voltage at the generator end to the voltage at the receiver end, and the magnitude of the vector $I_{g}{ }^{\prime} I_{r}$ is the ratio of the current at the generator end to the current at the receiver end. Distances from the center of coördinates measured along the radii represent the magnitudes of the vectors $E_{B} E_{r}$ and $I_{g} / I_{r}$. The slope of the vector $E_{g} E_{r}$ is the angle by which $E_{g}$ leads $E_{r}$. With $E_{r}$ as standard phase, the angular displacement from the base line represents the slope of the vector $E_{g}{ }^{\prime} E_{r}$. The slope of the vector $I_{g} I_{r}$ is the angle by which $I_{g}$ leads $I_{r}$. With $I_{r}$ as standard phase, the angular displacement from the base line represents the slope of the vector $I_{g} / I_{r}$.

## Voltage

$E_{g} E_{r}$ is the sum of the two vectors

$$
\left(1+\frac{Z \mathrm{Y}}{2}+\frac{Z^{2} \mathrm{Y}^{2}}{2 t}+\ldots\right)
$$

and
$\frac{K^{K} 10^{3} \%}{\left(p . f_{r}\right)_{r}}\left(1+\frac{Z J^{\circ}}{6}+\frac{\left.Z^{2}\right)^{2}}{120}+.\right)(\cos \phi \pm j \sin \phi)$.

The Calculator adds these two vectors.
For short lines when the first vector reduces to $\left(1+\frac{Z Y}{2}\right)$ we must add vecto-

TABLE II
VALUES OF a AND $b$ WHICH WERE USED FOR THE TRANSMISSION CALCULATOR
$R=0.2$ ohms per mile and $S / D=20.9$

| Length of line Miles | $\begin{aligned} a= & \left(1+\frac{\% 1}{2}+\frac{71^{2}}{24}\right. \\ & \left.+\frac{71^{3}}{720}+\ldots\right) \end{aligned}$ | $\begin{aligned} b= & \left(1+\frac{Z Y}{6}+\frac{Z^{2} 1^{2}}{120}\right. \\ & \left.+\frac{Z^{3} Y^{3}}{5040}+\ldots\right) \end{aligned}$ | Length of Line Miles | $\begin{aligned} a= & \left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{24}\right. \\ & \left.+\frac{Z^{3} Y^{3}}{720}+\ldots\right) \end{aligned}$ | $\begin{aligned} b= & \left(1+\frac{Z Y}{6}+\frac{Z^{2} Y^{2}}{120}\right. \\ & \left.+\frac{Z^{2} Y^{3}}{5010}+\ldots\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 60 Cycles |  |  |  |  |  |
| 50 | $\begin{aligned} & 0.9947+j 0.00131 \\ & 0.9947 \quad 00^{\circ} 5^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9982+j 0.000+4 \\ & 0.9982 \\ & 0.90^{\circ} 2 \prime \end{aligned}$ | 400 | $\begin{aligned} & 0.6779+j 0.0745 \\ & 0.6820 \end{aligned}$ | $\begin{aligned} & 0.8903+j 0.0260 \\ & 0.8907 \end{aligned} 1^{\circ} 40^{\prime}$ |
| 100 | $\begin{aligned} & 0.9788+j 0.00519 \\ & 0.9788 \\ & 0.0 \\ & 0.18^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9929+30.00174 \\ & 0.9929 \quad 10^{\circ} 6^{\prime} \end{aligned}$ | 450 | $\begin{aligned} & 0.5981+j 0.0914 \\ & 0.6050 \quad / 8^{\circ}+1^{\prime} \end{aligned}$ | $\begin{aligned} & 0.8624+j 0.03226 \\ & 0.8360 \\ & 12^{\circ} 99^{\prime} \end{aligned}$ |
| 150 | $\begin{aligned} & 0.9526+j 0.01157 \\ & 0.9527 \quad 0^{\circ}+2^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9841+j 0.003882 \\ & 0.9841 \quad 10^{\circ} 1 t^{\prime} \end{aligned}$ | 500 | $\begin{aligned} & 0.5118+j 0.1088 \\ & 0.52: 32 \quad 11^{\circ} 20^{\prime} \end{aligned}$ | $\begin{aligned} & 0.8 .319+j 0.0389 \\ & 0.8327 \\ & !2^{\circ} 4^{\prime} \end{aligned}$ |
| 200 | $\begin{aligned} & 0.9162+j 0020.3 \\ & 0.916 t \quad 1^{\circ} 16^{\prime} \\ & \hline \end{aligned}$ | $\begin{aligned} & 0.9719+j 0.00685 \\ & 0.9719 \quad 0^{\circ} 24^{\prime} \end{aligned}$ | 550 | $\begin{aligned} & 0.4197+j 0.1264 \\ & 0.4383 \quad 16^{\circ}+6^{\prime} \end{aligned}$ | $\begin{aligned} & 0.7984+j 0.0462 \\ & 0.7997 \quad 33^{\circ} 18^{\prime} \end{aligned}$ |
| 250 | $\begin{aligned} & 0.8700+j 0.0312 \\ & 0.8706 \end{aligned}$ | $\begin{aligned} & 0.95683+j 0.01060 \\ & 0.9564 \end{aligned}$ | 600 | $\begin{aligned} & 0.3228+j 0.1438 \\ & 0.3534 \quad 24^{\circ} 1^{\prime} \end{aligned}$ | $\begin{aligned} & 0.7629+j 0.0536 \\ & 0.7647 \\ & \hline 4^{\circ} 1^{\prime} \end{aligned}$ |
| 300 | $\begin{aligned} & 0.8145+j 0.04+1 \\ & 0.81 .57 \\ & 3^{\circ} 6^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9374+j 001508 \\ & 0.9375 \quad 10^{\circ} 55^{\prime} \end{aligned}$ | 650 | $\begin{aligned} & 0.2 \because 20+j 0.1606 \\ & 0.2740 \\ & 135^{\circ} 53^{\prime} \end{aligned}$ | $\begin{aligned} & 0.7252+j 0.0612 \\ & 0.7278 \quad 14^{\circ} 50^{\prime} \end{aligned}$ |
| 350 | $\begin{aligned} & 0.7502+j 0.0586 \\ & 0.7525 \\ & 4^{\circ} 2.21 \end{aligned}$ | $\begin{aligned} & 0.9154+j 0.0202 .4 \\ & 0.9156 \end{aligned} / 1^{\circ} 16^{\prime}$ |  |  |  |

50 Cycles

| 50 | $\begin{aligned} & 0.9963+j 0.00109 \\ & 0.9963+0^{\circ} t^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9988+j 0.000363 \\ & 0.9988 \quad 10^{\circ} 2^{\prime} \end{aligned}$ | 450 | $\begin{aligned} & 0.7146+j 0.0799 \\ & 0.7191 \quad / 6^{\circ} 23^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9031+j 0.0277 \\ & 0.9035 \\ & 1^{\circ} 45^{\prime} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | $\begin{aligned} & 0.08 .33+j 0.004 .34 \\ & 0.9853 \\ & 0.0015^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9951+j 0.00145 \\ & 0.9951+0^{\circ} 5^{\prime} \end{aligned}$ | 500 | $\begin{aligned} & 0.6514+j 0.09625 \\ & 0.6585 \\ & \hline 8^{\circ} 24^{\prime} \end{aligned}$ | $\begin{aligned} & 0.8812+j 0.03368 \\ & 0.8818 \underline{2^{\circ} 11^{\prime}} \end{aligned}$ |
| 150 | $\begin{aligned} & 0.9670+j 0.00970 \\ & 0.9670 \end{aligned}$ | $\begin{aligned} & 0.9890+j 0.00325 \\ & 0.9890 \quad 0^{\circ} 11^{\prime} \\ & \hline \end{aligned}$ | 5.50 | $\begin{aligned} & 0.5832+j 0.1134 \\ & 0.59+1 \\ & 11^{\circ} 0^{\prime} \end{aligned}$ | $\begin{gathered} 0.8571+j 0.04021 \\ 0.8580 \\ 2^{\circ}+1^{\prime} \end{gathered}$ |
| 200 | $\begin{aligned} & 0.9+1 . \overline{5}+j 0.01 .710 \\ & 0.9+17 \\ & \hline 1^{\circ} 2^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9804+j 0.00574 \\ & 0.9804 \quad 0^{\circ} 20^{\prime} \end{aligned}$ | 600 | $\begin{aligned} & 0.5104+j 0.1311 \\ & 0.5270 \\ & 14^{\circ} 24^{\prime} \end{aligned}$ | $\begin{aligned} & 0.8313+j 0.04706 \\ & 0.8326 \end{aligned}$ |
| 250 | $\begin{aligned} & 0.9091+j 0.0264 \\ & 0.9095 \\ & 1^{\circ} 40^{\prime} \end{aligned}$ | $\begin{aligned} & 0.9695+j 0.00891 \\ & 0.9695 \end{aligned} 0^{\circ} 32^{\prime}$ | 650 | $\begin{aligned} & 0.4336+j 0.1489 \\ & 0.4584 \\ & 18^{\circ} 57 \end{aligned}$ | $\begin{aligned} & 0.8037+j 0.0542 \\ & 0.8055 \quad 13^{\circ} 48^{\prime} \end{aligned}$ |
| 300 | $\begin{array}{r} 0.8699+j 0.0375 \\ 0.8707 \\ 2028 \end{array}$ | $\begin{aligned} & 0.9563+j 0.01273 \\ & 0.9564+0^{\circ} 46^{\prime} \end{aligned}$ | 700 | $\begin{aligned} & 0.3532+j 0.1666 \\ & 0.3905 \\ & \hline 25^{\circ} 15^{\prime} \end{aligned}$ | $\begin{aligned} & 0.7744+j 0.0616 \\ & 0.7768 \quad 4^{\circ} 33^{\prime} \\ & \hline \end{aligned}$ |
| 350 | $\begin{array}{r} 0.8242+j 0.0503 \\ 0.8257 \\ 3^{\circ} 299^{\prime} \end{array}$ | $\begin{aligned} & 0.9408+j 0.01716 \\ & 0.9410 \end{aligned} 1^{\circ} 3^{\prime} 6$ | 750 | $\begin{aligned} & 0.2698+j 0.1840 \\ & 0.3266 \\ & \hline 34^{\circ} 18^{\prime} \end{aligned}$ | $\begin{aligned} & 0.7+36+j 0.0692 \\ & 0.7+68 \quad 15^{\circ} 19^{\prime} \\ & \hline \end{aligned}$ |
| 400 | $\begin{aligned} & 0.7523+j 0.0645 \\ & \left(1.7750 \quad 4^{\circ}+6^{\prime}\right. \end{aligned}$ | $\begin{aligned} & 0.9230+j 0.02216 \\ & 0.9233 \\ & \hline 1^{\circ} 23^{\prime} \\ & \hline \end{aligned}$ |  |  |  |

rially 1 and $\frac{Z I}{2}$. On the polar coordinate chart, we locate 1 ; it is at the point $P$. In order to add $\frac{Z I}{2}$ to 1 , we must apply at the point $P$ a vector which has the same slope $Z Y$ as
2 The slope of $Z$ is determined by the ratio of the reactance, $\lambda$, to the resistance, $R$; the slope of $Y$ is 90 deg . when the leakance is neglected. The slope of $Z Y$ is therefore the slope of $Z+90 \mathrm{deg}$.* In order to represent graphically $\frac{Z Y}{2}$ with its proper slope, a movable vector, Vector No. 1 of the Cal-- culator, is pivoted at point $P$ and set with a slope of $Z+90 \mathrm{deg}$. This is accomplished by considering $P$ the origin of rectangular coordinates. If the abscissas to the left of $P$ correspond to $-X$, and the ordinates to $R$, and the center line of Vector No. 1 is set over the point $(-\lambda, R)$, Yector No. 1 will be perpendicular to $Z$. The distance from $P$ to the point $(-X, R)$ will be $\sqrt{R^{2}+Y^{2}}=z$. If Vector No. 1 is graduated to the same scale as $X$ and $R$, the magnitude of $z$ can be read directly on Vector No. 1 over the


Fig. 2. Inductive Reactance per Mile for Single Conductor for 50 and 60 Cycles
point ( $-\mathrm{I}, \mathrm{R}$ ). The same scale must be chosen for $R, . X$ and $z$, but this scale need not be the same as the other scales of the calculator. To the left of the polar coorrdinate chart on Supplement I is another chart which is provided with equally spaced hori-

[^30]zontal lines corresponding to varons values of " $R=$ Resistance per mile in ohms" and unequally spaced vertical lines corresponding to various values of $S / D$, one set for . 50 cycles and one for fio cyeles. Since $X$ is uniquely determined for a given value of


Fig. 3. Capacity Susceptance per Mile to Neutral for 50 and 60 Cycles
$S / D$ and a given frequency, these vertical lines have been graduated in terms of $S_{i} D$ rather than $X$. Since $X$ is not needed directly, it is not given in the Calculator. $X$ and $Y$ as functions of $S_{,}^{\prime} D$ are given in Figs. 2 and 3. Knowing $S / D$ and $R$ for a given line, a point is located on the $S, D, R$ Chart whose horizontal distance from $P$ is. V and whose rertical distance above the zero axis is $R$. Vector No. 1 is swung about $P$ until its " $z$ Scale" is over this point. The slope of Vector No. 1 is the slope of $Z+90$ deg. and Vector No. 1 is parallel to $Z \mathrm{I}$. On Fig. 4 $O S$ is the vector representing the series

$$
\left(1+\frac{Z Y^{Y}}{2}+\frac{Z^{2} I^{2}}{2 t}+\ldots\right)
$$

$O T$ represents the real part, $a_{1}$, and $T S$ the imaginary part, $a_{2}$. It has been pointed out that $a_{1}$ is practically constant for a given frequency and length of line; the distance $O T$, for a given frequency and length of line, is therefore known. Vertical lines marked "Length of Line-Miles" have been drawn

On the Calculator to represent $a_{1}$ for various lengths of line at Trefuencies of 50 and 60 cycles. The intersection of Vector No. I with one of these vertical lines, or lines produced, will locate Scorresponding to any desired freguency and length of line. There is no error in this method of locating $S$ when the lines are of such length that two terms only of the series need be used, but as the length of the line increases, the error in this methor of locating $S$ increases. For long lines it is fomm that although OT represents $a_{1}$ to a high degree of accuracy, $T S$ is greater than $a_{2}$. This error in $a_{2}$ may be calculated from a series, the first term of which is $R \frac{x^{2} y^{2}}{2-1}$, and applied as a correction to $E_{g}$ Fir and $I_{g} / I_{p}$ in the form of a vector, of length equal to the error, extending vertically downward. The error in the calculated $E_{g} / E_{r}$ and $I_{g}$, $I_{r}$ caused by this methorl of representing the series

$$
\left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{2 t}+\ldots\right)
$$

will be negligible for a $2.50-\mathrm{mile}$ line at 60 cycles, or a 600-mile line at 2.) eycles; it will be less than 1 per cent for lines of 400 miles or less in length and a frequency of 60 cycles. For the extreme range of the Calculator, the error may be in the neighborhood of 2 per cent. It is probably not worth while to correct for this error when using the paper calculator given in Supplement I, but it may be worth while to remember that the error tends to make the calculated values too high, rather than too low.

After the end point, $S$ of the vector representing the series

$$
\left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{24}+\ldots\right)
$$

is located, the second term of the right-hand member of equation ( $: 3$ ) is added vectorially. Vector No. 2 must represent this second term in magnitude and slope. Vector No. 2, therefore, must slide along Vector No. 1 until its pivot is over the intersection of Vector No. 1 with the vertical line, or line produced, of the "Length of Line-Miles" scale corresponding to the given frequency and length of line. The magnitude of this term may be expressed very simply as

$$
\frac{K Q z}{(p . f .)_{r}}
$$

if $Z$ is replaced by its equal, $z l$, and

$$
10^{-3 l}\left(1+\frac{Z \mathrm{~V}}{6}+\frac{Z^{2} \mathrm{~V}^{2}}{120} \cdots\right)
$$

is replaced by $Q$ in magnitude and $\theta$ in slope. From an inspection of Table II which gives

$$
\left(1+\frac{Z Y^{\prime}}{6}+\frac{Z^{2} Y^{2}}{120} \ldots\right)
$$

for various lengths of line at frequencies of 50 and 60 cycles for average line constants, it is apparent that the magnitude of this vector is but little greater than its real part, and, since the real part is constant for a given frequency and length of line, the magnitude of the vector is determined when the frequency and length of line are known. The " $Q$ Tafle" of the Calculator gives the magnitude of this series multiplied by $10^{-3} l$ for various lengths of line at 50 and 60 cycles. The error in assuming $Q$ constant for a given frequency and length of line is negligible throughout the range of the Calculator. The slope, $\theta$, of the series varies directly


Fig. 4. Vector Representation of the Transmission Line Calculator
with $R$; it varies also with $C$, as may be seen if the series is expanded in terms of the line constants, but since the angle in all cases is small, the error in assuming that $\theta$ varies directly as $R$, but is independent of the other line constants, is not serious. The " $\theta$ Table" on the Calculator gives this angle for various lengths of line for 50 and 60 cyc es with $R=1 \mathrm{ohm}$ per mile. When only approximate results are desired, $\theta$ may be disregarded entirely. When great precision is desired, the angles in the " $\theta$ Table" should be corrected for variations in capacitance, as well as for variations in resistance.

At unity power-factor, the factor ( $\cos$ $\phi \pm j \sin \phi$ ) is equal to one, and if $\theta$, the slope of the vector representing the series

$$
\left(1+\frac{Z \mathrm{~J}}{6}+\frac{Z^{2} V^{2}}{120}+\ldots\right)
$$

is disregarded for the present, but applied as a correction to the slope of Vector No. 2 later, the second term of the right-hand member of equation (3) may be represented by a vector whose magnitude is $K Q z$ and
whose slope is the slope of $\%$. If Vector No. 2 is placed perpendicular to Vector No. 1 it will have the same slope as $Z_{\text {. since Vect or }}$ No. 1 is perpendicular to $\%$. For any powerfactor other than unity. Vector No. 2 must be tumed from its unity power-factor position, through an angle $\delta$, such that $\cos \delta=$ $(p . f .)_{r}$. The circular head of Vector No. 2 is graduated in terms of power-factor, so that Vector No, 2 may be given the slope corresponding to any given power-factor at the receiver end. After Vector No. 2 has been given the slope corresponding to the given power-factor, the slope of the series

$$
\left(1+\frac{Z 1}{6}+\frac{Z^{2} I^{2}}{120}+\ldots\right)
$$

should be taken into consideration if the line is long enough to necessitate doing so. This is done by turning Vector No. 2 through an angle $\theta$ corresponding to the slope of the


Fig. 5. Example of Vector Quantities used in Determining Generator Power-factor
series. The magnitude of the vector measured along Vector No. 2 will be

$$
\frac{K Q z}{(p \cdot f \cdot)_{r}}
$$

Where $K=K W^{\prime} K V^{2}$, Q, corresponding to the given frequency and length of line, is taken from the " $Q$ Table" and $z$, the impedance per mile in ohms, is read on Vector No. 1.

$$
\frac{K Q z}{(p . f .)_{r}}
$$

is calculated on the slide rule and this quantity laid off along Vector No. 2 by means of the scale on Vector No. 2. Directly under the point

$$
\frac{K Q z}{(p . f .)_{r}}
$$

of Vector No. 2, $E_{g} E_{r}$ is located and its magnitude and slope read by means of the polar coördinates.

## Current

Equation (t) may be treated in the same way as equation (3). The first term of the right-hand member is the same as in equation (3). For unity power-factor, the second
term will have the slope of $b^{\prime}$, if the smatl angle of the series

$$
\left(1+\frac{75}{6}+\frac{Z 3}{120}+\ldots\right)
$$

is neglected for the present and applied as a correction later. When Vector No. 2 represents this second term for unity powerfactor, it must have the slope of ${ }^{\prime}$. hat ${ }^{\prime}$ is a pure imaginary with a slopee of 90 deg., therefore, to give Vector No. "2 the proper slope, it must make an angle of 90 ders. with the base line. Disc No. 3 is pivoted about the same center as Vector No. 22 and is graduated in terms of power-factor at the receiver; it should be set with its unity power-factor line in a vertical position. Disc No. 3 is held in this position and Vector No. 2 is rotated under it and given a slope corresponding to the power-factor at the receiver end by making Vector No. " coincident with the proper power-factor line of Disc No. 3. The slope of V'ector No. 2 may now be corrected for the small angle $\theta$ of the series

$$
\left(1+\frac{Z \zeta}{6}+\frac{Z^{2} \zeta^{2}}{120}+\ldots\right)
$$

If $I$ is replaced by its equal, $y l$, and

$$
10^{-3 l}\left(1+\frac{Z \mathrm{Y}}{6}+\frac{Z^{2} y^{2}}{120}+\ldots\right)
$$

by $Q$, the magnitude of the second member of the right-hand side of equation (4) will be

$$
\frac{y Q(p . f .)_{r}}{K}
$$

where $y$, the capacity susceptance per mile in micro-mhos, is taken from the " $y$ curves," $Q$. corresponding to the given frequency and length of line, is taken from the " $Q$ Table," and $K=K W / K V{ }_{r}^{2}$.

$$
\frac{y Q(p \cdot f \cdot)_{r}}{K}
$$

is calculated on the slide rule and its value laid off along Vector No. ㄴ by means of the scale on Vector No. 2. Directly under the point

$$
\frac{y Q(p . f .)_{r}}{h^{\prime}}
$$

of Vector No. 2, $I_{g} I_{r}$ is located and its magnitude and slope read by means of the polar coordinates.

## Power-factor

The power-factor at the senerator end of the line is calculated from the phase differences between $E_{g}$ and $E_{r}$, between $I_{g}$ and $I_{r}$ and between $I_{r}$ and $E_{r}$. With $E_{r}$
as standard phase, an inspection of Fig. 5) shows:

$$
(p, f)_{k}=\operatorname{Cos} \phi_{g}
$$

$$
=\operatorname{Cos}\left(\text { angle } I_{r} l_{g}-\text { angle } I_{g} / E_{r} \pm \zeta_{r}\right) \text {. }
$$

$\phi$ is positive when ( $\left.p . f_{\mathrm{f}}\right)_{r}$ is leading, and negative when it is lagging. If the angle in the parenthesis comes out positive, the generator power-factor is leading; if negative, it is lagging.

## Power

The power at the generator end of the line is calculated from the following equation:
$K W_{g}^{\prime} K^{\prime} W_{r}=\left(E_{g} / E_{r}\right)\left(I_{g}^{\prime} I_{r}\right)(p . f .)_{g}^{\prime}(p . f .)_{r}$.
Since the conditions at the receiver end are known, $E_{g}, I_{g}$ and $K W_{g}$ are easily calculated from $E_{g} / E_{r}, I_{g} / I_{r}$ and $K W_{g} / K W_{r}$.

## No Load

With no load at the receiver end, $K=0$ and equation (3) becomes:

$$
\begin{equation*}
E_{B /} / E_{r}=\left(1+\frac{Z Y}{2}+\frac{Z^{2} Y^{2}}{2 t}+\ldots\right) \tag{5}
\end{equation*}
$$

The end point of the vector representing the series

$$
\left(1+\frac{Z Y}{2}+\frac{Z^{2} I^{2}}{2 t}+\ldots\right)
$$

is located as above in finding $E_{g} / E_{r}$ and $I_{g} / I_{r}$ with a load on the line. The end point of the vector is at the pivot of Vector No. 2. $E_{g} / E_{r}$ may be read by means of the polar coorrdinates on the Base Chart directly under this pivot when Vectors No. 1 and No. 2 are made of some transparent material; but when they are opaque, like the ones given in this article, Vector No. 1 should be replaced by a straight edge and $E_{g} / E_{r}$ read, on the Base Chart, at its intersection with the vertical line, or line produced, of the "Length of Line-Miles" scale corresponding to the given frequency and length of line.

## Condenser at Receiver End

When a synchronous condenser is used at the recciver end to furnish a lagging current at no load, and thus to prevent the receiver voltage from rising too high,

$$
\begin{aligned}
& I_{r}=-j \frac{K V-A_{c}}{\sqrt{3} V_{r}} \\
& \frac{I_{r}}{e_{r}}=-j \frac{K V A_{c}}{K V_{r}^{2}} 10^{-3}=-j K^{-1} 10^{-3}
\end{aligned}
$$

where $\mathrm{Kl}^{\circ}-A_{c}=$ total $\mathrm{kv}-\mathrm{a}$. of the condenser and

$$
K^{\prime \prime}=\frac{K F \cdot A}{K V^{2}}
$$

Equation (3) now becomes:

$$
\begin{array}{r}
\quad E_{g}^{\prime} E_{r}=\left(1+\frac{Z Y^{\prime}}{2}+\frac{Z^{2} V^{\prime \prime}}{24}+\ldots\right) \\
-j K^{-1} 10^{3} Z\left(1+\frac{Z Y}{6}+\frac{Z Z^{2} Y^{2}}{120}+\ldots\right) \tag{6}
\end{array}
$$

When equation (6) is compared with equation (3) it is seen that the second term in the right-hand member of equation (fi) has a slope which is 90 deg. less than the slope of the corresponding term in equation (3) when the power-factor at the receiver end is unity. To represent this second term


Fig. 6. Transmission Line Calculator Assembled
of equation (6) Vector No. 2 must be turned through an angle of 90 deg . in a negative direction from its position at unity power-factor. Vector No. 2 will then make an angle of 180 deg. with Vector No. 1. The magnitude of this term is $K^{\prime} Q z$ when $Z$ is replaced by $z l$ and

$$
10^{-3 l}\left(1+\frac{Z \mathrm{Y}}{6}+\frac{Z^{2} V^{2}}{120}+\ldots\right)
$$

by Q. It may be calculated on the slide rule and this quantity laid off along Vector No.2. Directly under the point $K^{\prime \prime} Q z$ of Vector No. 2, $E_{g} / E_{r}$ is located and its magnitude and slope read by means of the polar coordinates.

## Charging Current

The charging current at no load is obtained from equation (2) by substituting zero for $I_{r}$.

$$
I_{g}=e_{r} I\left(1+\frac{Z Y}{6}+\frac{Z^{2} Y^{2}}{120}+\ldots\right)
$$

If $I$ is replaced by $y l$ and

$$
10^{-3}\left(1+\frac{Z Y}{6}+\frac{Z^{2} V^{2}}{120}+\ldots\right)
$$

## DIRECTIONS FOR USE

I. For 50 and 60 cycles.

Diride flat spacing between conductors in feet by diameter conductor in inches, obtaining $S / D$. For $\triangle$ spacing use
$S(1,2 b D)$ Vector No, 1 pivots about point $P$. Bring it to rest so that " $s$ Scale" is over the intersection of $R$, located on "R $=$ Resistance per mile-ohms" scale, and $S / D$ at the given until its pirot is over the intersection of Vector No. 1 with the certical line (or line produced) of the "Length of Line-Miles" scale corresponding to the given frequency and length of line ector...o. 1 and pivot of Vector No. 2 remain in these positions throughout the calculations
A. Iollage. $E_{g} E_{r}=\mathrm{Ra}$
oltage at receiver end. Ratio of voltage at generator end to 1. 11'ith Load. Swing Vector No. 2 about its pivot until the viven power-factor is coincident with the center line of Vector
No. 1. Correct slope of Vector No. 2 by placing zero of
Ro Scale: of Disc No. 3 coincident with Vector No. 2, then holding Disc No. 3 fixed, turn Vector No. 2 under it counter-clockwise through an angle $R \theta$, where $R=$ resistance per mile in ohms and
$\theta$ corresponding to the given frequency and length of line is taken corresponding to the given frequency and length of line, is taken is read on " $z$ Scale" of Vector No. 1. Q at given frequency and length of line is taken from the "Q Table." ( $p . f.)_{r}=$ power-
factor at receiver end. $K=K V_{r} / K V_{r}{ }^{2} . K H_{r}=$ total kw. at factor at receiver end. $K=K W_{r}^{r} / K V_{r}^{2} . K H_{r}^{\prime}=$ total kw . at
receiver end. $K V_{r}^{\prime}=\mathrm{kv}$. between lines at receiver end. By seceiver end. $K r=k V$. between lines at receiver end. By
means of the polar ccordinates of the Base Chart, read the magnitude and angle of $E_{g} / E_{r}$ directly under the point on Vector $\mathrm{NO}_{3}$ 2, Whose distance from the pivot is $\Sigma Q K /(p . f$. . r. directly under the pivot of Vector No. 2 . arectly under the prot of Vector No. 2.
3. No Load-Condenser Taking Lagging
No. 2 about its pivot until zero power-factor line is coincident with Vector No. 1 (Vector No. 2 extending towards the right).
With a slide rule, $\begin{array}{ll}\text { With a slide } \\ K ⿰ 丬 & \text { rule, obtain } z Q K^{\prime} \text {. Where } K^{\prime}=K I^{\prime}-A_{c} / K \mathrm{I}^{2} r^{2}, \\ \mathrm{C}=\text { total } \mathrm{kv}-\mathrm{a} \text {. of Condenser. Read } E_{g} / E_{r} \text { on the Base }\end{array}$ Chart directly under the point on Vector No. 2 whose distances from the pirot is $z Q K^{\prime}$. current at receiver end.

1. With Load. Place Disc No. 3 with the "Power-factor Scale" upward and unity power-factor line vertical. Swing Vector No. 2 about its pivot until it coincides with the given porer-factor on Disc No. 3 . Correct slope of Vector No. ${ }^{2}$.
by angle $R \theta$ as above. With a slide rule, obtain $y Q(p . f .)_{r} / K$. $y$ corresponding to the calculated $S / D$ and the given frequency
is obtained from the " $y$ curves." $Q_{1}$ (p.f.)r and $K$ as above By means of the polar coordinates of the Base Chart, read the magnitude and angle of $I_{g} / I_{r}$ directly under the point o
Vector No. 2, whose distance from the pivot is $y Q(p . f$.$) . / K$.
2. No Load-Charging Current:

Where $K V_{r}=\mathrm{kv}$, $I_{g}=\frac{K-\frac{1 r}{3}}{13}, v_{\text {. }}$
Q as above. $=$ Sv. hetwee

$$
\begin{gathered}
I_{r}=\frac{K Y_{g}}{\sqrt{3} Q z .} \\
I_{g}=\frac{K I_{g}}{\sqrt{3} Q z .}\left(E_{g} / E_{r} \text { at no load }\right)
\end{gathered}
$$

$K V_{g}=\mathrm{kv}$. between lines at the generator end, $Q, z$ and ( $E_{g} / E_{r}$ at no load) as above.
C. Generator power-factor $=(p . f)_{\text {. }}$ g.
With $E_{r}$ as standard phase, an inspection of Fig. $5^{*}$ shows: $(\phi . f .)_{g}=\cos \phi_{g}=\cos \left(\right.$ angle $I_{g} / I_{r}$-angle $\left.E_{g} / E_{r} \pm \phi_{r}\right)$ sho If the angle in the parenthesis comes out positive, the generator power-factor is leading; if negative, it is lagging.
power-factor is leading; if negative, it is lagging.
D. Power. $K W_{g} / K W_{r}=$ Ratio of power at receiver end.
II. $\begin{gathered}K W_{g} / K W_{r}=\left(E_{g} / E_{r}\right) \\ \text { For any frequency: } \\ \left(I_{g} / I_{r}\right)(p . f .)_{g} /(p . f .)_{r} .\end{gathered}$

For any frequencies, $f$, other than 50 or 60 cycles, find a new Resistance $R^{\prime}=R \frac{50}{f}$ and a new length of line, $l^{\prime}=l \frac{f}{50}$; then with these new values proceed as above for a 50 -cycle line.
*Adpears in G. E. Revizw, June, 1923, page 387.


## TRANSMISSION LINE CALCULATOR

 DIRECTIONS FOR ASSEMBLINGIf this working model of the Transmission Line Calculator is carefully assembled, it may be used to advantage in preliminary calculations to obtain the voltage, current, power-factor and power at the generator end of a transmission line when the voltage, load and power-factor at the receiver end are known. If mechanically correct, it will give results without appreciable error for lines up to 250 miles in length at 60 cycles 300 miles at 50 cycles or 600 miles at 25 cycles For lines 400 miles in length at 60 cycles th error may be about 1 per cent. The error increases with the length of line, but even at the extreme range of the Calculator it will not be more than about 2 per cent for voltage and current values. Since the power at the generator end is obtained from the product of voltage and current, the error in the power may be twice as large as that in voltage or current. In general, the values calculated on the Transmission Line Cal culator are high rather than low

Cut out the three parts given on this sheet For a more substantial calculator, paste them, and also the Base Chart of Supplement I (entire shcet) on cardboard. Cut out the narrow crossed hatched band of Vector No. 1 then fold along the dotted line. Pivot Vector No. 1 at point $P$ of the Base Chart, with point $P$ of the Vector above point $P$ of the Base Chart. A thumb tack will do very well as a pivot if the point of the tack is cut off after it is in place and a metal washer soldered on. This pivot at point $P$ must be flat so that the pivot of Vector No. 2 may slide over it for short-line settings. Place the center $P^{\prime}$, of Disc No. 3 over the center, $P^{\prime}$, of the circular head of Vector No. 2. This common center, $P^{\prime}$, must be made to slide along the center line of Vector No. 1 in the groove cut out for that purpose, and Disc No. 3 and Vector No. 2 must be free to rotate about it. A second thumb tack will do for this pivot and sliding point. Place the thumb tack in the groove of Vcctor No. 1, with its point upward. Glue the under and upper parts of Vector No. 1 together in such a manner that the thumb tack is not impeded when sliding in the groove. Force the point of the thumb tack through the center, $P^{\prime}$, of the circular head of Vector No. 2 and the center, $P^{\prime}$, of Disc No. 3. A second metal washer may be soldered on to keep Vector No. 2 and Disc No. 3 in place The Calculator is now ready for use Directions for use are given on the Base Chart of Supplement 1 .

A Transmission Line Calculator
By Edith Clarke


Disc No. 3


by $C$.
$I_{s}=\frac{K^{\prime \prime} r}{\sqrt{3}} y . Q$. Where $y$, the capacity susceptance per mile in micro-mhos, corresponding to $S D$ and given frequency, is taken from the " $y$ Curves," and $Q$ corresponding to given frequency and length of line, is taken from the " $Q$ Table."

## Short Circuit at Receiver End

For short circuit at the receiver end, from equation (1) and (2) by substituting zero for $c_{r}$

$$
\begin{aligned}
& c_{g}=I_{r} Z\left(1+\frac{Z \mathrm{I}^{2}}{6}+\frac{Z^{2} 1^{2}}{120}+\ldots\right) \\
& I_{g}=I_{r}\left(1+\frac{Z I^{2}}{2}+\frac{Z^{2} I^{2}}{24}+\ldots\right)
\end{aligned}
$$

TABLE III
FOUR ASSUMED TRANSMISSION LINESAND CONDITIONS AT THE RECEIVER ENDS

| Conditions | Line 1 | Line 2 | Line 3 | Line 4 |
| :---: | :---: | :---: | :---: | :---: |
| $f$ (cycles) | 60 | 2.5 | 50 | 60 |
| $l$ (miles) | 125 | 3300 | 750 | 150 |
| Materia! | Copper | Aluminum steel core | Aluminum steel core | Aluminum steel core |
| Size | No. 00 | $510,000 \mathrm{~cm}$. | $950,000 \mathrm{~cm}$. | $605,000 \mathrm{~cm}$. |
| $D$ (inches) | 0.420 | 0.855 | 1.194 | Split conductor, 9 wires. |
| $S$ (feet) | 10 | 21 | 22 | Assume: $\mathrm{X}=0.495$ ohms/mile $y=8.58$ micromhos/mile |
| $R$ (ohms 'mile) | 0.4108 | 0.1704 | 0.0916 | $\begin{gathered} 1 / 3(0.144) \\ =0.048 \end{gathered}$ |
|  |  | $200$ | 220 | $250$ |
| $K 11^{\prime},(k z .)$ | 20,000 | 80.000 | 115.000 | $400,000$ |
| $p . f$. of load | 0.75 lag | 0.75 lag | 0.80 lag | 0.85 lag |
| $(p . f .) \text {, }$ | 0.98 lag | 0.98 lag | 0.95 lag | 1.00 |
| $\left(k z^{\prime}-a .\right)$ | 13,600 | 54,300 | 124.000 | 248,000 |

from which it follows that

$$
\begin{aligned}
& I_{r}=\frac{e_{g}}{Z\left(1+\frac{Z \mathrm{Y}}{6}+\frac{Z^{2} I^{\prime 2}}{120}+.\right)}=\frac{K V_{g}}{1 \overline{3} z Q} \\
& \begin{aligned}
I_{g} I_{r} & =\left(1+\frac{Z \mathrm{Y}}{2}+\frac{Z^{2} Y^{2}}{2 t}+\ldots\right) \\
& =E_{g} / E_{r} \text { at no load } \\
I_{g} & =\frac{K V_{g}}{\sqrt{3} z Q}\left(E_{g}^{\prime} E_{r} \text { at no load }\right)
\end{aligned}
\end{aligned}
$$

## Split Conductor

Lines of the split conductor type proposed by Mr. Percy Thomas* can be solved on the Calculator when $I$ and $y$ are known. $z=\sqrt{\prime}^{\prime} \overline{R^{2}+X^{2}}$ is calculated, and Vector No. 1

[^31]is given the proper slope by making it the hypotenuse of a triangle having sides, -1 and $R$, laid off to any convenient scate. The procedure is then the same as with any other three-phase transmission line.

## Frequency

The Calculator given in Supplement I is designed for transmission lines with frequencies of 50 and 60 cycles , but it can be used for lines of any frequency. A new resistance, $R^{\prime}=R \frac{.50}{f}$, and a new length of line, $l^{\prime}=l \frac{f}{50}$, are calculated; then the line is treated as though it were a 50 -cycle line having a resistance of $R^{\prime}$ and a length of $l^{\prime}$.

The above statement is apparent from equations (3) and (4), if the following substitutions are made for $Z$ and $Y$ :

$$
\begin{aligned}
& Z=l==l(R+j \mathrm{~J})=f l\left(\frac{R}{f}+j 2 \pi L\right) \\
& I=l y=l(+j y)=f l(+j 2 \pi C)
\end{aligned}
$$

Since $L$ and $C$ are uniquely determined for a given value of $S / D$, the number of independent variables on the right-hand sides of equations (3) and (4) may be reduced to five. They are $f l, R / f, S / D, K$ and ( $p . f)_{r}$. Two lines of different length, frequency, resistance, spacing between conductors and size of conductors, operated at different voltages and delivering different amounts of power will have the same drop in voltage from the generator end to the receiver end and the same per cent power loss if $f l, R_{/} f, S^{\prime} D, K^{\prime}$ and (p.f.) $)_{r}$ are the same in the two cases. Two such lines are given below:

1. 3-phase, 60 -cycle, 12.5 -mile line of No. 00 copper, flat spacing between conductors of 10 feet, $K \mathrm{~F}_{r}=100 \mathrm{kr}$., $\mathrm{KII}_{r}=$ $25,000 \mathrm{kw}$., (p.f. $)_{r}=0.90$ lagging.
2. phase, 3-2.5-cycle, 300-mile line of 510,000 c.m. steel re-enforced aluminum, flat spacing between conductors of 21 ft ., $\mathrm{K}^{\prime} \mathrm{V}_{r}=200 \mathrm{kv} . \mathrm{KII}_{r}=100,000 \mathrm{kw}$., $(p . f)_{r}$ $=0.90$ lagging.

|  | Case 1 | Case 2 |
| :--- | :--- | :--- |
| $f l$ | $60 \times 12.5=7.500$ | $2.5 \times 300=7.500$ |
| $R f$ | $0.11 \quad 60=.00653$ | $0.172 .5=0.006 .50$ |
| $S / D$ | $100.42=2.3 .5$ | $-210.58 .5=2.3 .7$ |
| $K$ | $2.5,000100^{2}=2.5$ | $100,000 \div 00^{2}=2.5$ |
| $($ p.f. $)$, | 0.90 lagging | 0.90 lagging. |

For these two lines. $E_{g} E_{r}, I_{g} I_{r}$ and $\mathrm{KH}_{3} \mathrm{KIH}_{r}$ will be the same.

## Twenty-five Cycles

It was not found neoessary to design the Calculator for a frequence of 2.5 cycles, since it is such a simple matler to calculate a 25-cycle line on the bo-eycle calculator. The resistance used must be twice the given resistance and the length of line one-half the given length, but otherwise, the procedure is the same as though the frequency were 50 cycles instearl of 25 eycles.

## EXAMPLES

In order to illustrate the use of the Calculator, four high-voltage transmission lines
will be selected and the conditions at the receiver ends assumed. Following the directions given on Supplement I, conditions at the generator ends of these lines will be calculated on the Calculator, and each step of the procedure, as well as the final results, will be given.

The assumed transmission lines and conditions at the receiver ends are given in Table III.

The calculations of conditions at the generator ends of the assumed transmission lines by means of the Transmission Line Calculator, following the directions given on Supplement I, are given in Table IV.

TABLE IV
CALCULATED CONDITIONS AT GENERATOR ENDS OF THE ASSUMED TRANSMISSION LINES BY MEANS OF THE TRANSMISSION LINE CALCULATOR

| Conditions | Line 1 | Line 2 | Line 3 | Line 4 |
| :--- | :---: | :---: | :---: | :---: |
| $S$ (feet) | 10 | 21 | 22 | Assumed |
| $D$ (inches) | 0.420 | 0.88 .5 | 1.194 | value of |
| $S / D$ | 2.3 .8 | 2.3 .7 | 18.4 | $\mathrm{~N}=0.495$ |
| $f$ (cycles) | 60 | 2.50 |  |  |
| $R$ (ohms/mile) | 0.4104 | 0.1704 | 0.0916 | 0.048 |
| $R^{\prime}=R \frac{50}{f}$ | $\ldots$. | 0.341 | $\ldots$. | $\ldots$. |

Vector No. 1 is set for $S^{\prime} D$ and $R$. ( $R^{\prime}$ for 25 cycles). For Line 4. Vector No. 1 is given slope $R /-N$.

| $z$ (from '"s |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Scale" of Vec- | 0.925 | 0.770 | 0.670 | $=\overline{R^{2}+र^{3}}$ |
|  |  |  |  | $=0.49{ }^{-}$ |
| (miles) | 125 | 300 | 750 | 150 |
| $l^{\prime}=l \frac{f}{\bar{L} O}$ |  | 150 | ... | . . . |

Pivot of Vector No. 2 is moved along Vector No. 1 and set for $l$. ( $l^{\prime}$ for 25 cycles.)

| VOLTAGE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (p.f. $)_{r}$ | 0.98 lag | 0.98 lag | 0.95 lead | 1.00 |
| Vector No. 2 is rotated about its pivot and set for (p.f.), |  |  |  |  |
|  |  |  |  |  |
| Table ${ }^{\text {² }}$ ) | 0.8 | 1.0 | 26.6 | Neglect |
| $R \theta$ (degrees) | 0.33 | 0.34 | 2.44 | Neglect |
| Slope of Vector No. 2 is corrected by rotating it counter-clock wise through the angle $R \theta$. |  |  |  |  |
| $Q$ (from ' ${ }^{\text {a }}$ Q |  |  |  |  |
| Table"') | 0.1234 | 0.1484 | 0.560 | 0.1476 |
| K ${ }^{*}$ ( $k w$. | 20.000 | 80.000 | 115.000 | 400,000 |
| K1 ${ }^{\text {r }}$ (kp.) | 100 | 200 | 220 | 250 |
| $K=K W_{r} / K V^{\prime}, 2$ | 2.0 | 2.0 | 2.38 | 6.40 |
| $\mathrm{KQ} \mathrm{z} /(\mathrm{p} . f$.$) )$ | 0.233 | 0.233 | 0.940 | 0.470 |
| H'ith Load:-K ()$z /(p . f$.$) - is laid off along Vector No. 2, an$ $E g{ }^{\prime} E r$ is read on Base Chart under this point. |  |  |  |  |
|  |  |  |  |  |
| Eg/Er (Magni-1 |  |  |  |  |
| tude) | 1.125 | 1.125 | 1.015 | 1.103 |
|  |  |  |  |  |
|  | 112.5 | 225 | 223 | 276 |
| No Load; No Condenser: $-E \mathrm{~g} / E_{r}$ is read under pivot of Vector |  |  |  |  |
| No. 2. |  |  |  |  |
| $\begin{aligned} & E g E_{r} \\ & K^{\prime} g^{\prime}= \\ & K V_{r}(E g / E r) \end{aligned}$ | 0.967 | 0.967 | 0.29 | 0.953 |
|  | 96.7 | 193.4 | 63.7 | 238.0 |
| No Load; Condenser Taking Lagging Current: |  |  |  |  |
| $K \mathrm{~V}-\mathrm{A}$ clagging ${ }^{\text {a }}$ |  |  |  |  |
| 75 per cent of leading $\mathrm{kv}-\mathrm{a}$. | 10,200 | 40,800 | 93,000 | 186,000 |
| $K^{\prime}=K \-A,{ }^{\prime}$ |  |  |  |  |
| K $\mathrm{V}^{\prime 2}$, | 1.02 | 1.02 | 1.925 | 2.97 |
| $\mathrm{K}^{\prime} \mathrm{Qz}$ | 0.1167 | 0.1167 | 0.723 | 0.218 |


| Conditions | Line 1 | Line 2 | Line 3 | Line 4 |
| :--- | :--- | :--- | :--- | :--- |

VOLTAGE-Continued
Vector No. 2 is rotated about its pivot and set for p.f. $=0$ $K^{\prime} O z$ is laid off along Vector No. 2 and $E_{g} / E_{r}$ is read on Base Chart under this point.


With Load:-y $Q(p, f.) \cdot / K$ is laid off along Vector No. 2 and $1 \mathrm{~g} / I_{r}$ is read on Base Chart under this point.

| $\underset{\text { tude) }}{I g / I r} \text { (magni- }$ | 0.959 | 0.959 | 1.180 | 0.974 |
| :---: | :---: | :---: | :---: | :---: |
| Ig. $/ I_{r}$ (angle ${ }^{\circ}$ ) | 19.3 | 19.3 | 62.6 | 12.0 |
| $r_{r}=\ldots i_{r}$ | 117.8 | 235.6 | 317.5 | 923.0 |
|  | 113 | 226 | 375 | 900 |

Charging Current; Open Circuit:

| $I g=\frac{K V r}{\sqrt{3}}$ y $Q$ | 36.5 | 73.0 | 316.0 | 183.0 |
| :---: | :---: | :---: | :---: | :---: |
| GENERATOR POWER-FACTOR |  |  |  |  |
| $\phi,=\cos ^{-1}(p . f$.$) ,$ | $-11.5$ | -11.5 | $+18.2$ | 0 |
| $\begin{aligned} & \phi g=(\text { angle } I g / \\ & I_{r}-\text { angle } E g / \\ & \left.E_{r} \pm \phi r-\right) \end{aligned}$ | -2.5 | -2.5 | -5.2 | -13.3 |
| ( $\mathrm{p} . \mathrm{f}.) \mathrm{g}=\cos \phi_{h}$ | 0.999 lag | 0.999 lag | 0.996 lag | 0.973 lag |
| POWER |  |  |  |  |
| $\mathrm{KWg} / \mathrm{KH} \cdot=$ |  |  |  |  |
| $\left(\frac{E g}{E_{r}}\right)\left(\frac{I g}{I_{r}}\right)$ |  |  |  |  |
| (p.f.)g | 1.10 | 1.10 | 1.26 | 1.045 |
| $\begin{aligned} & \overline{(p \cdot f .) r} \\ & K H^{\prime}=K H, \times \\ & \left(K H_{g} K H^{\prime} r\right) \end{aligned}$ | 22,000 | 88.000 | 145,000 | 418,000 |

# Alternating-current Secondary Networks 

By D. K. Blake<br>Lhomting Exgineering lepartment, General Electric Compiny


#### Abstract

Great attention has been patd to every detail of power station and substation equipment and also to the details of transmission lines, but in the past such minute study has not beengiven to the distribution system. The author takes up this study and treats it in detail in a way that should be of interest to those respensibhe for the distribution of electric energy. Enitor.


During the past few years, the engineers of central station companies have given more attention to their alternating-current distributing system than previously. It is being recognized that, since the investment in the distribution system is a very large part of the total investment, large economies are possible. Changes and expansions based upon economic studies by different engincers have produced şurprising economies. Some of the results usually obtained are less primary copper; fewer but larger transformers, with the consequent increase in load factor and efficiency; decrease in core loss per kr-a.; less investment per kr-a.; and less investment in lightning arresters, where they are used at each transformer location; and smaller difference between substation watthour meters and consumers' watthour meters.

One company, upon investigating a certain section of its distribution ssstem containing approximately 3000 transformers, found that the average size of transformers was approximately $12 \mathrm{kr}-\mathrm{a}$. with a transformer load factor of 11 per cent. Improvements made in the system brought the average size up to approximately $26 \mathrm{kr}-\mathrm{a}$. with a load factor of approximately is per cent.

The distribution systems which now exist in most American cities consist of direct current substations supplying an Edison threewire network for the business section, and transformer substations supplying 23300 -rolt or 4000 Y -rolt, three-phase radial feeders with distribution transformers, for other sections. For lighting loads, the secondaries of the distribution transformers supply approximately 115230 volt, three-wire mains, which usuall: are not interconnected, as shown in Fig. 1. For power loads, three-phase banks are installed for low roltage motors. The expanding business sections make it necessary to extend the Edison network, or carry part of the business section on a-c. feeders. The investment and energy losses in substation equipment and low voltage feeders make it uneconomical and undesirable to extend the Edison network. Some companies have installed a-c. secondary networks in place of extending the Edison
network. Many other companies are now considering the use of secondary networks to prevent extending the Edison network. One company in a large eastern city and a few smather companies are considering replacing their Edison system with a-c. secondary networks. Secondary net works on existing singlephase, three-wire, secondary distributing systems are formed by connecting the secondary mains of each transformer on the same phase together, as shown by the dotted lines in Fig. 1.


Fig. 1. Typical Three phase Feeder
There are several factors which make the secondary network more economical and desirable than the method of supplying groups of consumers from a single transformer. With a network it is possible to reduce the total transformer kr-a. capacity installed and increase the transformer load factor due to the diversity of loads between transformers. Large size transformers may be used which have a lower cost per $\mathrm{kr}-\mathrm{a}$. than small transformers. These two factors reduce the transformer investment and installation costs. Large size transformers also have a lower core loss per $\mathrm{kv}-\mathrm{a}$. and a higher efficiency than small ones. The ability to supply customers from two or more directions and the diversity
between customers reduces the secondary copper losses, and improves the voltage regulation and also assists in giving continuous service which results in inereased wattage consumption on resistance loads with increased revemue. Reductions are also possible in primary


Fig. 2. Transformers in Network Protected with Fuses
copper losses and investment, particularly where the three-phase four-wire primary system is used with the same neutral wire for the primary and secondary. With a well designed secondary network the difference between the consumers' watthour meters and the feeder watthour meters is a minimum. Increase in loads may be taken care of with greater ease and economy. The number of points of inspection on a secondary network


Fig. 3. The Alternating-current Network Protector
are a minimum whieh is quite an adrantage, particularly in case of trouble.

The successful design and operation of secondary networks presents many interesting and complex problems. Chief among these are the short circuit protection of primary mains and transformers, the division of loads between transformers, supplying motor loads and the choice of the trpe of system to use.

Fuses have been used to a large extent for short circuit protection of transformers. The methods generally used are shown in Fig. 2. The primary fuses are selected for operation on short circuits and the secondary fuses are selected to operate after the primary fuse. The transformers should not be fused for overload protection since the losing of one transformer, due to overload, shifts the overload to adjacent transformers which also may be overloaded, thereby blowing their fuses. This action in scheme (a) may proceed until all


Fig. 4. Assembly of Core and Coils of a 50-kv-a. Subway Transformer Equipped with Network Protector; Highvoltage Side
transformer fuses on the network are blown. Overloads usually occur at or near peak load on the network. Therefore, it is a very serious matter to have an interruption at this time. It requires considerable effort and time to restore an interrupted network protected with fuses. The scheme shown at (b) protects the secondary mains also. In a network of any size it is unnecessary to have short circuit protection on secondary mains, since it has been found that any short circuit will burn itself clear as in a d-c. network. Fairly good results have been obtained with fuses, but the best of them do not meet the requirements of most engineers.

Some companies are now using the a-c. network protector, which is shown in Fig. 3. The coils $\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}$ and E are wound on the same iron core. The arrows indicate the flow
of current with the transformer carrying load. The ampere turns of $B$ and $C$ are equal and their sum is equal and opposite to the ampere turns of A. They, therefore, have no magnetic effect on the iron core. In coils D and E the current enters at the center and divides equally. Since the turns are wound in the same direction in each coil, the ampere turns of one half neutralize the ampere turns of the other half. Under normal conditions, the core is not excited and no voltage is generated in coils $D$ and $E$. If a breakdown or short circuit should occur in the transformer the current through B and C will be reversed. Under this condition the ampere turns of $A$, B and C act in the same direction and produce a magnetic flux in the iron core. The flux in the core induces a voltage in coils D and E . The voltages across these coils are short circuited through the fuse links. The large currents which circulate through $1-2-3$ and $4-5-6$ blow the fuses almost instantaneously, thereby disconnecting the secondary of the transformer from the network. The primary fuses blow practically simultaneously with the


Fig. 5. $50-\mathrm{kv} \cdot \mathrm{a}$. Transformer Equipped with Network Protector, Complete

Assembly, Low-voltage Side
secondary fuses. The secondary fuses are designed so as not to operate under load conditions. The signal lamp is lighted when the fuse, across which it is connected, blows. This gives a reliable indication of the transformer disconnected from the network.

The network protector is mow math as a part of the transformer, which simplifies the wiring and installation, as shown in Fig. 4 The coils are assembled about the middele leg of a three legged core which is firmly mounterl in clamps and supported under the oil at about the same place inside the transformer tank that the lead supports ordinarily come. To


Fig. 6. $50-\mathrm{kv}-\mathrm{a}$. Transformer Equipped with Network Protector View of Cover and Fuse Board
eliminate possible damage which might result from the explosion of the fuse links over the oil, they are placed in a separate compartment formed in the transformer cover, as shown in Figs. 5. 6, 7 and s. The fuse links are located so that the blowing of one link will


Fig. 7. Model of Network Protector, Cover Removed Showing Leads
ensure the blowing of the other. The signal lamp provided is located inside the fuse chamber behind the bull's eve, as shown in Figs. 6 and 7 , so that in dark manholes or at night there can be no doubt as to the transformer disconnected. The fuse chamber is arranged for a conduit connection so that additional
signal hamps may be connected and located on lamp posts above the street level or on joles, or carricd to some convenient place where patrolmen can notice immediately any transfomer which may be cut off from the network. On networks large transformer units are used with relatively few sizes. The


Fig. 8. Model of Network Protector, Cover Removed Showing Connections
protector, therefore, has been standardized for 50,75 and $100-\mathrm{kv}-\mathrm{a}$, 2300 to $115 / 230$-volt, 60 -cycle transformers for either pole or subway operation. It can be developed for higher voltage circuits or for polyphase transformers and networks. The vertical terminal board is standard for transformers of 50, 75 and $100 \mathrm{kv}-\mathrm{a}$. in the pole type and for 75 and $100 \mathrm{kv}-\mathrm{a}$. in the subway type. On subway transformers, the principal object in using the vertical terminal board on the larger sizes is to enable a man to work in the fuse chamber more conveniently. The low ceilings in many manholes would make this difficult with the larger sizes of transformers. The layout of a 2400 -volt, two-phase primary, $120 / 240$-volt, single-phase, three-wire secondary underground network, using network protectors, is shown in Fig. 9.

The United Electric Light and Power Company of New York City are now using a reverse energy device which permits the use of a network supplied by multiple feeders, as shown in Fig. 11, instead of having a small network for each radial feeder, as shown in Fig. 10. The device consists of an air circuit breaker, no-voltage relay, reverse energy relay and reactive shunt, all of which are mounted on a panel. A diagram of connections is shown in Fig. 12. Normally the circuit
breaker is closed with the transformer supplying current to the network. The breaker is held closed by means of a latch. The current flowing through the reverse energy relay holds the lower contacts of the relay closed. When power flows from the network to the transformer, the reverse energy relay opens its lower and closes its upper contacts. The closing of the upper contacts shunts the novoltage relay coil, thereby tripping the breaker. With no voltage applied to the primary of the step-down transformer, the upper contacts of the reverse energy relay remain closed because of the current which flows through the difference of potential coils. The circuit of the difference of potential coils is completed through the secondary of the transformer. The small current which flows does not have an appreciable magnetizing effect on the transformer. When approximately normal voltage is applied to the primary, the voltage opposes the network voltage applied to the difference of potential coils, with the result that the lower contacts of the relay


Fig. 9. Alternating-current Network Using Network Protectors


Fig. 10. Networks on Radial Feeders


Fig. 11. Multiple Operation of Primary Feeders
shunt the resistor which permits full secondary voltage to be applied to the no-voltage relay. The closing of the contacts of the novoltage relay energizes the closing coil of the air circuit breaker which closes the breaker, thereby connecting the transformer to the network.

By referring to Fig. 11, it will be seen that if a fault should occur in the transformers or primary mains and feeders, the device $A$ will clear the transfomers of the fecter in trouble from the network and the feeder breaker at the substation bus will open. The other feeders will carry the network load without an interruption to service. When the fault is repaired the breaker at the substation is closed and the air circuit breakers automatically close, connecting the transformers to the network. During periods of light load the circuit breakers of one or more feeders may be opened, in which case the exciting eurrent supplied to the transformers from the network is sufficient to trip the breakers and disconnect the transformers from the network. This permits removing a feeder for repairs and a saving in core loss with the consequent increase in the light load efficiency of the net-


Fig. 12. Air Circuit Breaker with Reverse-current Trip
work. The operation of the device on the exciting current of the transformer is accomplished by the reactive shunt. The shunt consists of one turn of copper around an iron core. The core becomes saturated at low values of current with the result that at normal load current, the ordinary 5 ampere relay coil is not overheated. The device is arranged for basement or vault mounting. It is protected from water by means of a bell which fits over the derice and is sealed at the bottom. In case the seal should break, the water is prevented from covering the apparatus by the compression of the air in the bell. The load densities on the networks range from 100 kw . per block to 400 kw . per block. The net-
works are supplied from two or more sul)stations with no less than a whal of right primary feeders. The transformers jer feerles range from 5 to 20 transformers.

Oil circuit breakers with reverse power relays are being used to some extent. Mr. M. T. Crawford, in the Electrical II orld of


Fig. 13. Protection of Transformers Connected to Secondary Networks with Oil Circuit Breakers and Reverse-power Relays


Fig. 14. Differential Protection of Transformers
December 23, 1922, describes a scheme used by the Puget Sound Power and Light Company in Seattle. A diagram of connections is shown in Fig. 13. In case of transformer trouble the reverse power relay trips the secondary oil circuit breaker and the primary fuses blow. In ease of primary feeder or main trouble the substation oil circuit breaker and the secondary oil circuit breakers of the transformers, connected to the phases of the feeder in trouble, will open. The load on the secondary network will be carried by the other feeder or feeders. Any number of feeders or transformers per feeder may be used. In sections where the power load is dense, small power secondary networks supplied from the same primary feeders are formed.

The use of oil circuit breakers connected in the primary and secondary circuits of the transformers, as shown in Fig. 14, is under consideration by several companies. Current transformers in the primary and secondary will have their secondaries connected in series with trip coils connected aeross the current transformers to give differential protection. The breakers will open automatically only when trouble oceurs in the transformers. Circuit breakers for this purpose are being
developed with the two-pole breaker for the 2500-volt primary, two-pole braker for the $2: 3(0)$-volt secondary, and current 1 mansformers assembled in one init for use in valults. The mechanism will be arranged so that hoth breakers will trip simultancously on automatic operation, hat either the primary or secondary


Fig. 15. Automatic Throw-over Circuit Breakers
breaker may be opened or closed by hand independently of the other.

Practically all applications of oil circuit breakers to distribution networks are limited to districts with very high load densities. Several schemes using oil circuit brcakers with relays have been suggested for downtown business sections. A scheme for automatically transferring transformers from one feeder when its voltage fails to a good feeder is shown in Fig. 15. If the station oil circuit breakers of feeder No. 1 should open, then the transformer oil circuit breakers, which are normally closed, will open, and the breakers normally open will close and connect the transformers to feeder No. 2. The control circuits of the breakers are shown in Fig. 16. The potential relay with time delay opening is connected to the line side of the oil circuit breaker No. 1 through a potential transformer. Under normal operating conditions, the upper contacts of the potential relay are closed. When the voltage of feeder No. 1 falls below its adjustment, the lower contacts close. Oil circuit breaker No. 1 is then tripped by its trip coil. The opening of No. 1 breaker closes its auxiliary switch (b) which completes the operating motor circuit of breaker No. 2, thereby closing breaker No. 2. Feeder No. 2 then carries the transformers of feeder No. 1. When voltage is restored to feeder No. 1, the potential relay closes its upper contacts which trip circuit breaker No. 2. The opening of circuit breaker No. 2 completes the operating motor circuit of breaker No. 1, thereby restoring the transformers to their original feeder. If the transformers on each feeder are connected to form a network, the network protector may be used to clear the transformer, or an oil circuit breaker may be installed in the secondary
with current transformers in the primary and secondary differentially connected to trip all three breakers in case of transformer failure. If the networks are tied together, as shown by the dotted lines in Fig. 15, a complete interruption to both feeders may result in case of a fault on one feeder, unless the potential relay has an inverse time characteristic sufficient to let the feeder with the lower voltage clear first. If the line breakers are equipped with reverse power relays instead of the voltage relay, both feeders could be tied together at each transformer. In case of trouble on any one feeder, the reverse power relays would clear the transformers from that feeder. Service on the network will be maintained by the other feeder. Transformer trouble as in the previous case would be cleared by network protectors or differential protection. The network may be supplied by more than two feeders if required.

A network supplied by loop feeders is shown in Fig. 17. The feeders may be protected by inverse time limit overload relays at the station with reverse power relays at the breaker connecting the feeder to the mains, or pilot wire protection. With the breakers in the mains equipped with reverse power relays, it is necessary to give alternate breakers graded


Fig. 16. Control Circuits for Automatic Throw-over Oil Circuit Breakers
current and time settings to prevent improper relay operation. The settings would be graded as shown by the numbers below the breakers. With the pilot wire protection, no grading is necessary, since the breakers can only trip in case of trouble on the main in which they are connected. Under normal
conditions, the secondary current of the current transformers circulates through the pilot wires. When a fault occurs in the main, the secondary current of each current transformer is forced through the relay equipment connected to it. The relays trip the breakers at each end, thereby clearing the fault from the system. The pilot wires should be run in a separate cable and duct. A multi-conductor cable can be used containing pilot wires for several feeders and other purposes. The presence of pilot wires in moderate or high voltage cables greatly increases the insulation stresses and interferes with the making of good joints. The insulation of the cable should be increased to take care of the increased stresses. The extra insulation reduces the maximum conductor size obtainable in multi-conductor cables because of the diameter of the cable being limited. A faulty transformer is removed from the system by the network protector or the differential connection of relays to trip a secondary breaker and the two breakers in the mains.

Where a-c. secondary networks are to be used in the downtown business sections of very large cities, it is desirable to use a higher primary voltage than 2300 volts or 4000 volts, because of the high load density. With 11,000 volts or 13,000 volts about one third as many feeders will be required because of the greater capacity per feeder. Large vaults spaced a few hundred feet apart will be required to ventilate the large transformers and to contain the protective equipment. Where the transformers must be installed in vaults which are not large enough to radiate the heat through the earth by natural radiation, other


Fig. 17. Loop Feeders Supplying a Network
means of ventilation must be provided. The use of oil circuit breakers in vaults presents several difficult problems. The opening into the vault and the space available limit the overall dimensions of the breaker, thereby

[^32]limiting the interrupting capacity obtamalife Means must he provided to conduct away the gases from the oil circuit breaker which may be generated when the breakers open under short circuit.

The cost of the vaults with the equipment and the difficulty of obtaining proper locations


Fig. 18. Substations Feeding Directly Into Network with Low-voltage Feeders
for vaults may, in some cases, make the scheme shown in Fig. 18 preferable. The network is supplied by a few substations containing large transformers of the power class. A large number of low voltage feeders connect each substation to the network. The transmission cables are protected with balanced connection of relays and the tie cables with reverse power relays. The transformers have standard differential relay protection. The feeders and mains would burn a fault clear as in a d-c. network. This scheme is practically the same as the Edison system, except that the converting equipment is replaced by the transformers. There are two important factors which make this scheme more economical than the Edison system, namely, the higher efficiency of transformation than conversion and the lower cost per kw. of the a-c. substation which in some cases, is about 65 per cent of the d-c. substation cost. *Similar schemes with three-phase, four-wire networks are in use in Europe and Australia. The roltage to neutral is about 200 rolts and between phases 346 volts.

The successful operation of a secondary network depends fundamentally on the proper division of load between the distribution transformers. Standard distribution transformers connected to a network, spaced several hundred feet apart, will not share their
loads acoording to their rating．If two transfomers of equal rating are connected， as shown in Jig．19，with the load concen－ trated at or beyomid tamsommer No． 1 ，amose the entire load will be carried be No． 1 trans－ former．This is becathse the imperdance of the secondary main is large compared with the imperdace of the transformers．If the load is concent rated at the middle of the secondary main，then of course the load will be diviked equally between the transformers．


Fig．19．Concentrated Load Connected to Network
If a transformer in a network is damaged by an overload，it will be cleared from the net－ work by its protective equipment．The load carried by the transformer will then be trans－ ferred to the other transformers in the network．If standard transformers which have low reactance are used the adjacent transformers will carry the load of the faulty transformer．If the location of the faulty transformer is equi－distant from the adjacent transformers then they will divide the addi－ tional load approximately according to their rating，otherwise，the nearest transformer will take most of the load．The extra load carried by the adjacent transformers may be suffi－ cient to burn out one or more transformers which will be cleared by their protective equipment．This action may proceed until the service to the entire network is interrupted． It is evident then，that some method must be used to force the transformers to divide the load according to their rating in addition to any protective device used to clear a damaged traisformer from the network．

By increasing the reactance of both trans－ formers in Fig．19，transformer No． 2 will carry a larger proportion of the total load as shown by the curves in Fig．20．The secondary mains are assumed to be 250 feet long for single－phase and 500 feet for three－phase with 40 wire mounted on 8 －inch secondary brackets．The transformers are assumed to be one 75 kv －a．transformer for a single－phase network and three $50 \mathrm{kv}-\mathrm{a}$ ．transformers for a three－phase network．If the impedance of the transformers is increased to 10 per cent， transformer No． 2 will carry $40 \mathrm{kv}-\mathrm{a}$ ．when No． 1 is carrying $7.5 \mathrm{kv}-\mathrm{a}$ ．in case of single－
phase，or 5．5 kr －a．when No． 1 is carrying 150 kr－a．in case of three－phase．A better division of load will be obtained in underground networks using multi－conductor cable due to the lower reactance of the eable．Since the loads on a network are not usually concen－ trated at the transformer but distributed along the mains，a better division of load will be obtained than that shown by the curves． The use of high reactance in series with the transformers will，therefore，greatly relieve the transformers adjacent to the damaged one by distributing a large part of its load over the transformers beyond the fault．This should prevent to a great extent the trouble experi－ enced on networks after the loss of one or more transformers．The impedance of the transformers may be increased by external reactance connected in series with the trans－ former or by designing transformers with inherent high reactance for network operation． The latter has a much lower cost than the former．

Standard distribution transformers have approximately 1.5 per cent resistance drop and 4 per cent reactance drop．The following is a comparison of the regulation of transform－


Fig．20．Division of Load Between Transformers of Like Design
ers with 4 per cent reactance and 10 per cent reactance：


It will be necessary to compensate for the extra regulation by means of the feeder regulators which，in some cases，may have to
be increased in size. The curves show that not much is to be gained by increasing the impedance above 10 per cent for single-phase networks and 15 per cent for three-phase networks. The increased regulation may not permit the use of 15 per cent reactance.

Reactors may be connected in the secondary mains, instead of in series with the transformers, as shown in Fig. 21 . Under normal conditions only a small current is carried by the reactor since most of the load on each section is supplied by its own transformer. If the distances between transformers are equal and the loads uniformly distributed, the load on section No. 5 will be supplied equally from transformers Nos. 2, 4, 6 and 8 without the use of reactors in case of the loss of transformer No. 5. Since the distances are not always equal, nor the loads uniformly distributed, the load will not be divided equally between the transformers. If the reactance of the mains between transformer No. $\overline{5}$ and No. $\mathcal{S}$ is 10 per cent and between No. 5 and No. 6 is 15 per cent, then the short main will carry 50 per cent more current than the long main when supplying load to section No. 5. If the reactors are rated at 25 per cent then the total reactance in the short main will be 35 per cent and the long main 40 per cent. Then the short main will only carry 11.4 per cent


Fig. 21. Reactors Connected in Network Mains
more current than the long main. The reactor therefore need only be designed for one quarter of the current rating of a transformer. The reactive drop with this current would then be 6.25 per cent. In case of a short circuit on any section, the reactors will maintain voltage on the adjoining sections.

There is at present under investigation a network system designed to compel an even division of load among the transformers, in spite of the usual uneven and irregular distribution of load on the secondary network. Reference to Fig. 22 will show the proposed arrangement, which consists of series balanc-
ing coils placed in the feeder at each transformer of the network, and so designed that they compel each transformer to take its proper share of the load regardless of where the load is located. The primary main between transformers 'Tt and $T 5$ carries the current of To and T(6 while the main T\%-T(; carries the current of T 6 only. If the transformers are of the same rating the turns of the auto-transformer E shoukl be proportioned so that twice as many turns will be connected in the main T.)-T( F as in T4-T\%.


Fig. 22. Schematic Arrangement of Balanced Alternatingcurrent Network

The numbers below the auto-transformer indicate the relative turns while the numbers above indicate the relative currents. The auto-transformers may consist of one coil in series with the feeder and one in series with the individual transformer, or of two coils in the feeder magnetically apposed and with the transformer connection brought off at a tap in the proper position.

This system will tend to avoid the difficulty commonly experienced with networks, that a heavy overload or short circuit will blow the fuses of adjacent transformers and extend the trouble to the entire network, by removing the transformers progressively from the line as the load is thrown on them. The transformers will all share an overload and the transformers adjacent to the ove, load will not take an undue proportion of it. In case of a short circuit, more energy will be supplied from the network as a whole, with the possibility of more rapidly burning off the fault.

It is evident that, since the current can flow in one direction only, loop primary circuits or feeders multipled on the primary side at other points than Tl cannot be used. Any number of feeders may be used with their transformers feeding into a common secondary network as shown in Fig. 23. A balance coil is connected in the mains at A to divide the load on each branch of the feeders.

A defeetive tramsfomer on such a network may be removed from the system by simple fuses, since the remainter of the network will feed in sufficient current to blow the primary and secondary fuses on a defective unit without howing the fuses of the adjacent trans-


Fig. 23. Balanced Alternating-current Network with Multiple Feeders
formers. When one transformer has been removed from the system, however, the bałancing coils are no longer properly adjusted for their positions in the circuit, and an even distribution of load is no longer obtained. This condition may require special provision in the arrangement of the transformers or in protective apparatus. This feature and the desirable capacity in the balancing coils are being carefully studied. The capacity, of course, will be determined as a compromise between the cost of the apparatus and the extent to which it is desired to maintain an even division of load under extremely heary overloads or short circuits.

The balancing coils under uniform distribution of load on the network do no work, and have no effect on the system except to introduce a negligible IR drop. When the load is unbalanced, however, the difference in drop between transformers supplying the load is taken up by the auto transformer, which under this condition develops a voltage across its terminals which is in such relation to the
voltages within the feeder as to compel an approximately correct division of the currents. The balancing coil must be designed for the maximum voltage which would be required muder unbalanced conditions.

The advantage expected from this system, in addition to those mentioned previously, are that it will permit a saving in transformer capacity over that ordinarily required to provide a margin for uneven distribution and local overtoads. It should also tend to reduce copper losses by providing multiple paths for the supply of the load.

For the successful operation of feeders with induction regulators in parallel some modification may be necessary in the regulator control equipment. If both regulators are compensated to hold approximately normal voltage at the point 13, Fig. 24, an increase in load may cause regułator No. 1 to increase its voltage before No. 2. If the reactance of the line is high with respect to the resistance a circulating current will flow which will be lagging almost 90 deg. the voltage of No. 1 regulator and leading almost 90 deg. the voltage of No. 2 regulator. The lagging current will cause regulator No. 1 to boost the voltage and the leading current through No. 2 will cause it to buck the voltage, both of which cause an increase in circulating current. This may progress until No. 1 regulator runs to full boost and No. 2 to full buck position. In this case the regulators are set to compensate for the entire reactance of the circuit. If the compensators are set to compensate to the


Fig. 24. Parallel Operation of Feeders with Induction Regulators
point A for No. 1 feeder and the point C for No. 2 feeder then the portion A to C is not compensated for. In this case it will take a greater circulating current to run the regulators to the full buck and full boost position. Since the value of the circulating current
depends on the position of the regulators, it is obrious that the regulators will not take their limit positions, but will become stable at some intermediate point. This point will depend on the ratio of the reactance of the main between $A$ and $C$ to the reactance of the rest of the circuit.

The connections for the parallel operation of single-phase regulators is shown in Fig. ...5. The current transformers connected in parallel are used with the line drop compensators to compensate for line drop. The current transformers connected in series are used to prevent circulating currents in the feeders. The reactance X may be a line drop compensator using both resistance and reactance where the resistance is appreciable. When a feeder is removed its current transformer used to prevent circulating currents should be short circuited by means of an auxiliary switch on the oil circuit breaker.

Most networks now in use are single-phase three-wire. Where the primary feeders are polyphase, the loads are balanced between the phases as nearly as possible with each phase


Fig. 25. Connections for Parallel Operation of Singlephase Regulators
supplying one or more small networks. This type of network will have many applications, particularly in residence sections with increasing appliance loads. Small single-phase motors used on appliances are supplied from the network, but any power loads within the district are supplied by separate transformers from the primary. The networks shown in Fig. 9 are supplied br a two-phase primary.

In some blocks the whases are run patallel w cach other to supply two-phase motors

In districts with high load densities, it is desirable to have a common polyphase secondary network. This will permit supplying power and lighting foads from the same mains similar to an Edison system. Some


Fig. 26. Polyphase Secondary Networks
companies who have two-phase primary distribution are considering the two-phase fivewire system and the three-phase four-wire system shown in Fig. 26. The two-phase five-wire system can supply standard voltages for motors and lamps from the same mains. If the two-phase primaries are supplied from a three-phase source by T-comnected transformers, there is a 6.7 per cent loss in transformer capacity. Two-phase motors may not be obtained as easily as three-phase motors. When used, a four-pole circuit breaker is required.

With a standard voltage to neutral to supply lighting load, in a three-phase fourwire network, the phase voltages will be below the standard motor voltage. With $12 . j$ volts to neutral the phase voltage is 216 volts. At the motor terminals the voltage may be as low as 205 or 200 volts. Standard motors are designed for emergency operation on 10 per cent above or below normal voltage. Where the motor load is a small part of the total load supplied by the network, auto-transformers may be installed to step up the motor voltage. This requires a separation of the lighting circuits from the motor circuits on the customer's premises. For the same voltage to neutral, this system requires approximately ( 5.5 per cent more copper than the two phase fire-wire system. The primaries may be also three-phase four-wire which permits a higher transmission voltage using standard single-phase transformers where the existing srstem is three-wirt. The $\mathrm{Y}^{\prime}-\mathrm{I}^{\prime}$ connection of
the transformers with this system shonld cause no more telephone interference due to thited hamonies than does the common practice of using single-phase transformers connected to three-phase or single-phase feeders. Mr. William (`. L. Eglin in his article, "The Future Distribution System," in the Electrical 11 orld, December 17. 192:3, gives the relative investment as 1.000 for the three-


Fig. 27. Diagram of Connections of Voltage Stabilizer for Alternating-current Circuits
phase four-wire and 0.97 .5 for the two-phase five-wire. The relative losses are given as 1.000 for the former and 1.045 for the latter.

It will be necessary to limit the size of motor connected to the network and also avoid connecting motors which start and stop frequently, due to the low power-factor starting current. The starting current produces a drop in the transformers, mains and service lines which causes the lamps to flicker. Motors which are not large enough to cause a voltage variation on the mains may cause quite a drop in the service lines. To eliminate the instantaneous variation in voltage caused by starting the motor, a voltage stabilizer, shown in Fig. 27, may be used. This is essentially a reactive transformer having a primary through which the motor current flows, and a secondary which is connected in series with the lamp load and boosts the lamp voltage by an amount proportional to the voltage drop caused by the starting current of the motor. This of course requires the separation of the lighting and motor circuits. The stabilizer is provided with an adjustable air gap which permits adjusting the yoltage induced in the coil connected in series with the lighting circuit within certain limits.

A-c. equipments for printing presses and elevators up to 540 ft . per minute have been developed and are giving satisfactory operation. For the present higher speed elevator equipments must be d-c. Rotary converters or motor-generator sets on customer's premises, or a skeleton d-c. system can be used to supply printing press and elevator loads where
a-c. will not be feasible or permitted. Motors which camot be supplied from the secondary network, due to their size and character of load, may be supplied from the primary mains. If the motor loads are dense enough, a separate network may be formed for power at a higher voltage than the lighting network.

The design of an a-c. secondary network requires an intensive economic study. Among the important factors which affect the successful and economical operation in addition to those already discussed are the size of conductor, spacing and size of transformers and the voltage drop in the mains. A paper entitled "Economic Study of Secondary Distribution" by Messrs. P. O. Reyneau and Howard P. Seelye, in the A.I.E.E. Transactions Part II, 1920, cover these points thoroughly. The same authors discuss the same factors, in addition to other factors of vital importance, in a book on "Economics of Electrical Distribution," published by the McGraw-Hill Company: The equations used


Fig. 28. Curves Showing the Annual Charges on Single-phase Transformers in Place, 15 to $100 \mathrm{Kv}-\mathrm{a} ., 2300$ volts Primary
will be mentioned here for the purpose of calling attention to their application. No attempt will be made to explain their derivation or all of the assumptions on which they are based.

The annual charges on transformers per 1000 ft . for overhead construction are expressed in an equation:

$$
\begin{equation*}
Y_{L}=\frac{1000}{S}\left(K_{1}+K_{2} T\right)=\frac{1000}{S}\left(K_{1}+K_{2} \frac{L_{D} S}{1000}\right) \tag{1}
\end{equation*}
$$

The constants in this equation may be approximated by plotting the transformer size against the cotal annual charges of the transformer with protective equipment in place, as shown in Fig. 노. The annual charges per 1000 ft . on single-phase three-wire secondary mains in place are expressed in an equation:

$$
\begin{align*}
& I_{L}=\frac{\left(i_{L}\right.}{100}\left(3000 \omega C_{C u}+C_{S R}\right) \\
& +60.83 S^{2}\left(\frac{L^{2} D \rho t C_{C 2}}{1 E^{2} \cos ^{2} \theta}\right) \tag{2}
\end{align*}
$$

By adding equation (1) and (2) the total annual charges per 1000 ft . on transformer equipment and secondary mains are obtained. $\mathrm{I}^{-}=\mathrm{I}_{T}+\mathrm{I}_{L}$

$$
\begin{gather*}
Y=\frac{1000}{S}\left(K_{1}+K_{1000}^{I_{-D} S}\right)+ \\
\frac{G_{L}}{100}\left(3000 \omega C_{c u}+C_{s R}\right)+60 . s_{3} S^{2}\left(\frac{L^{2}{ }_{D} \rho t C_{e 2}}{A E^{2} \operatorname{Cos}^{2} \theta}\right) \tag{3}
\end{gather*}
$$



Fig. 29. Curves Showing the Most Economical Conductor Size

From this equation the most economical conductor, transformer size and spacing, and voltage drop may be determined. By making substitutions for certain of the symbols the equation may be differentiated with respect to the factor for which it is desired to determine the most economical condition. If Y is differentiated with respect to A and equated to zero an equation:


Fig. 30. Curves Showing the Most Economical Transformer Spacing
is obtained which gives the most economical size conductor. If Y is differentiated with respect to $S$ and equated to zero an equation:

$$
\begin{equation*}
\operatorname{Sec}=2.02\left[\frac{K_{1} E^{2} \operatorname{Cos}^{2} \theta}{\rho t C_{e 2}}\right]^{1 / 3} \frac{A^{1 / 3}}{L_{D} D^{2 / 3}} \tag{5}
\end{equation*}
$$



Fig. 31. Curves Showing the Most Economical Voltage Drop
is "obtained which gives the most economical transformer spacing. Since the load is assumed uniformly distributed and the transformer just large enough to carry the load, the most economical transformer size may be obtained from the equation:

$$
\begin{equation*}
T e c=L_{D} \frac{S_{e c}}{1000} \tag{6}
\end{equation*}
$$



Fig. 32. Curves Showing the Comparative Economy of Various Wire Sizes in Secondary Installations with Transformers


Fig. 33. Small Indoor or OutdoorëSubstations Supplied by Loop Feeders

The equation:

$$
\begin{equation*}
S=\frac{E}{17.32} \sqrt{\frac{A V}{B L_{D}}} \tag{I}
\end{equation*}
$$

sher mer most economical voltage drop). With a given load density and conductor size the transformer size and spacing may be determined from Fig. 30. If the conductor and transformer size are given the spacing may be determined. If the transformer size and spacing are given the conductor size may be determined. The curve in Fig. 32 shows the comparative economy with various wire sizes and also the difference between a threcphase four-wire network and a single-phase three-wire network, including only the secondary mains and transformer equipment. The equations and curves indicate ideal conditions which cannot be obtained in practice. They indicate the limitations and are a valuable guide. In making an actual layout several other types of curves based on the equations are very useful. An estimate was made considering local factors in a certain city and it was found that the three-phase four-wire worked out slightly more economical than the single-phase three-wire.

Messrs. Gear and Williams in their book on "Electrical Central Station Distributing Systems," published by D. Van Nostrand Company, give the equation:

$$
Y=\frac{a}{R}+b C^{2} R+c C^{2} R
$$

which gives the total annual charges of an electric circuit. By differentiating with respect to R and equating to zero the equation:

$$
C R=\sqrt{\frac{a}{b+c}}
$$

is obtained. Where it is customary to adopt either a standard feeder load or a standard
gives the spacing for a voltage drop V. If this is substituted for $S$ in equation (3) and then Y is differentiated with respect to V and equated to zero an equation:
$V^{\prime} e c=1223\left[\frac{\operatorname{Cos}^{2} \theta}{E \rho t C_{e 2}}\right]^{2 / 3} \frac{B K_{1}^{2 / 3}}{A^{1 / 3} L_{D}^{1 / 3}}$
is obtained which gives the most economical voltage drop.

These equations with some modifications were used to compare the economy of a three-phase four-wire network with a single-phase threewire network. The curves of the equations are plotted in Figs. 29, 30,


Fig. 34. Indoor Automatic Reclosing Equipment


Fig. 35. Automatic Reclosing Outdoor Equipment with Oil Switch
wire size, the most economical size wire for maximum load may be obtained. A modification of Kelvin s law to determine wire size


Fig. 36. Automatic Reclosing Equipment in Outdoor Switch House
is given by Mr. (ilen Smith in the Electracal If orld, December 17, 192?.

The advent of remote control and automatic reclosing equipments will permit anethods of distribution which before, with some


Fig. 37. High-voltage Feeders Supplying Distribution Transformers and Customers' Substations
exceptions, were not permissible. Where new load centers are rapidly developing they may be supplied by small indoor or outdoor substations, instead of a large manually controlled substation, as shown in Fig. 33. The low voltage feeders may be remote controlled from the substations or equipped with automatic reclosing equipments illustrated in Figs. 34, 3.5 and 36. The breakers of the reclosing


Fig. 38. Outdoor Automatic Reclosing Equipment for 33,000-volt Feeder


Fig, :37. The branch feeders may be profeeted with alutomatic reclosing eguipments or for circuits below $1.5,000$ volts with the pole mounted breakers illustrated in Fig. 39 and 11. The feeders may be equipped with automatic reclosing equipments and the transformers with fuses or oil circuit breakers set so as to operate at a higher current and time setting than the feecler breakers. In some cases low


Fig. 41. Three Manually Operated Oil Circuit Breakers Installed on Transmission Line
voltage feeders to supply small power and light users may be located at the customer's substations. Where automatic or remote control is not desired outdoor switch houses with oil circuit breakers similar to Fig. 40 may be used. These are particularly useful at small outdoor substations tapped to a high voltage transmission line or feeder.

Acknowledgment is made to Mr. C. G. Jeter and Mr. E. D. Treanor of Pittsfield, for information furnished on the network protector and auto-transformer scheme for balancing load on a-c. secondary networks.
Fig. 40. Outdoor Switch House, Three-phase, Four-circuit, Showing Front and Doors Open on Two Circuits

# Applying the Results of High-voltage Research to Practice 

By F. W. Peek, Jr.<br>Pittafielid Works, General Electric Company


#### Abstract

The value of research work in solving our "field problems" in high-voltage transmission is ably shown in this article. The testing laboratory where so many notable results have been accomplished is briefly described and the construction of a million-volt transmission line considered. The use of the insulation shichl is shown in our illustrations.-EDitor.


While it is probably true that research work should be carried on in a systematic way regardless of apparent immediate practical application, nevertheless the research worker will have a much broader aspect if the possibility of application is kept in mind. It is also true that practical application is never more apparent than in the laboratory demonstration. The pure physicist who looks with disfavor upon the consideration of practical application should remember that he would soon be without tools if the results of his work were not practically applied. When theory and practice disagree it generally means that theory is wrong in not including all of the variables. The most difficult part of a research is, in fact, the proper application of the result to practice.

It is the purpose of this paper to discuss the methods and apparatus used in highvoltage research.

In this connection, a brief description of the "High-voltage Engineering Laboratory" at the Pittsfield Works will probably be of interest.* This laboratory is equipped with the apparatus necessary to carry on the problems of pure and applied research as well as the more immediate developmental problems. The first essential of such a laboratory is plenty of free space. A single example will make this apparent. During a recent investigation sparks over eighteen feet in length were obtained. Fig. 1 gives a view of the "million-volt" corner of this laboratory. A good idea of the size is obtained by noting the visitors in the gallery observing the nine-foot, 60 -cycle arc. Fig. 2 shows a view in the opposite direction. At the time this picture was taken a full size section of a 220 kv . transmission tower was erected in order to study the effect of the tower on the behavior of the insulator shield.

It is possible to make this whole laboratory dark in a few minutes. A smaller dark room

[^33]is available for tests up to 300 kv . as shown in Fig. . $\overline{ }$. The whole building is of substantial brick construction and kept at practically constant temperature inside.

A great variety of apparatus is available for use in both pure and practical researches.


Fig. 1. Million-volt Corner of the High-voltage Engineering Laboratory Showing Lightning Generator and Million-volt Transformers

In fact, almost any condition that can occur in practice can be simulated. A partial list may be of interest and is as follows:

A million and a half volts single-phase; a million volts to ground and a million volts three-phase (root mean square) at commercial frequencies; damped and undamped high frequency oscillation; high voltage d-c.; arcing grounds; two million volts, lightning, etc. Apparatus is also available for studying the effects of such weather conditions as heat and cold, and rain and dew formation on insulators. Special measuring instruments
are also available 15 an example, spheres 100 cms. ( 40 inchl in diameter are necessary to measure the very high voltages

Sone investigations are started purely from theoretical reasoning and others from sug-


Fig. 2. Section of Full-size $220-\mathrm{kv}$. Tower Erected in the Laboratory to Study the Effect of the Tower on the Behavior of the Insulator Shield
gestions received in practice. Quite often a practical result is obtained from work started on a theoretical basis while the truth of a theory often is established from the work started from a practical suggestion.

A short description of some specific investigations taken at random may give a better idea of how this work is carried out.

The lightning generator, shown in Fig. 1, will produce voltages of approximately two million. This is perhaps higher than lightning roltages that are usually induced on transmission lines. These voltages are of a known wave shape and duration. The wave front is under control and is rery steep. In fact, it may be made so steep that the voltage starting at zero or line voltage may increase at the rate of 50 million million volts per

[^34]second. The rate that the energy is dissipated in the are is generally in the order of millions of horse power. The duration of such discharges is conveniently measured in micro seconds (one micro second $=$ one millionth of a second).

The development of this impulse or lightning generator resulted from observations matle on a transmission line in 1913. Some switch bushings with a 60 cycle arc-over voltage of about 100 kv . were "protected" be a low gap lightning arrester set to spark over at about 2.5 kv . (30 cycle. Lightning always sparked over the bushing. It took the horn such a long time to discharge that the rapidly increasing lightning voltage rose to over 100 kv . and discharged over the bushing which was of a design with very little time lay. Although the lag is generally less than a millionth of a second, a lightning voltage, increasing at the rate of millions of kilovolts per second, can become quite high in this time.

In order to study this phenomena an impulse or lightning generator was developed that gave a very high voltage, a wave shape under control and of definite value. ${ }^{1}$ The phenomena observed in practice were repeated in the laboratory. The result was that spheres were added to the arrester gap and the discharge voltage was probably reduced to about one quarter. The difference between successful and unsuccessful operation here


Fig. 3. Another corner of the High-voltage Engineering Laboratory
was a slight change in the electrodes. The sphere has very little lag because the field is practically uniform and the break occurs in the gaps everywhere simultaneously. With the needle or the horn the field is irregular and
a sphere of corona must be formed before arc-over can occur. This takes time. The modern bushing on the other hand is clesigned to have a very high lightning spark-over roltage. In this investigation, much data of theoretical interest was obtained and the term " impulse ratio" added to our " engineering" vocabulary.

The original generator which was designed for 200 kv . has been added to from time to time as available exciting roltages have increased. Approximately two million volts is now available with a discharge rate of millions of kw.

In order to apply the laboratory results to practice it is necessary to know just what occurs in practice. This information is obtained by making measurements on actual lines. In one investigation the voltage, current and "frequency" of lightning induced on transmission lines were actually measured.

Other transient or "predatory" voltages that occur on transmission lines are surges, or highly damped oscillations, caused by arcing grounds or switching. Undamped oscillations have never been observed. Nor would these be expected since even if they were started they would soon be damped out by the losses.

The insulator shield shown in the tower in Fig. 2 is a development recently brought to


Fig. 4. Original Sphere Horn Arrester Gap
${ }^{a}$ practical stage for $200-\mathrm{kv}$. transmission. Unlike the sphere lightning arrester gap this device was first started from the theoretical

[^35]or mathematical end.2. It is generally well known that, when an insulator string is mot shielded, 25 to 30 per eent of the (i0) exele voltage appears across the units of the line end. This is obriously not dessrable. With


Fig. 5. Small Dark Room with Office Above. This dark room is equipped for tests up to 300 kv . to ground
the shield, each unit takes its share of the roltage. The shield also prevents corona on the line conductor and the insulator units. Another very important use of the shield is to prevent the arc from cascading and the following dynamic destroving the string.

The lightning investigation has been of great help in tying-in research with practice. The shield was designed so that lightning and such oscillations as appear on transmission lines cleared the string. The results are shown in Figs. 7. S. and !.* It will be noted that even during rain, lightning clears the insulators. Incidentally. Figs (i and 7 show by far the highest voltage and the greatest energy ever produced in a lightning stroke in the laboratory. Lightning voltages of such magnitude rarely occur on transmission lines, for it is very seldom that lightning sparks over a sevenunit string.

The shiedd does not lower the lightning are over voltage of the string. It would obviously be wrong to use a type of shield in practice because it gave a spectacular performance with radio frequency in the laboratory. There is continual danger of falling into error in this way.

Athough it is probably not generally known, a similar slield is used most effectively

It is alwatys well to make a model "set-up" of apparatus before practical application is made on an extensive scale because it is not always jossible to foresee all of the variables that maty enter into a combination. It is also a fact that some phenomena, unimportant in certain stages, may suddenly become of commanding importance, as, for instance, the corona when the loss jumps from zero to


Fig. 6. A 1,500,000-volt Lightning Stroke between Points


Fig. 7. Spark-over of Shielded Insulator String; dry, 60 cycles


Fig. 8. Spark-over of Shielded Insulator String; single lightning stroke, $1,200,000$ volts, dry


Fig. 9. Spark-over of Shielded Insulator String; single lightning stroke $1,200,000$ volts, during heavy rain


Fig. 10. Spark-over of NonShielded Insulator String: single lightning stroke $1,200,000$ volts, dry
high values with a slight change above a critical voltage.

In the preliminary stages of the 220 kv . development, in addition to the insulator tests in a full size tower, a model three-phase line was operated at full voltage. The fact of principal interest that developed was the triple harmonic caused by corona. ${ }^{4}$ A study was also made of the propagation of lightning along this model transmission line.

In the laboratory it is often necessary to improvise apparatus to get results in a hurry. In fact the first million volts were obtained (September 13,1921 ) by putting two standard testing transformers in series. Only the addition of a bushing and other slight insulation changes were necessary to obtain over a million volts from these two ten-year-
old transformers. ${ }^{5}$ The test was made hurriedly to sce if existing laws of corona and spark-over held at the very high voltages. This was fonnd to be so. The present permanent equipment, which can be seen in Fig. 1, was specially designed for the jurpose of general laboratory use and has been adequately described. ${ }^{6}$ There are, of course, many uses for a million volts in the laboratory from the standpoint of pure researeh. It may not be out of place to comelude this article with a discussion as to just what are the possible uses of a million volts in jractical transmission.

The conductor would probably be about $61 / 2$ inches in diameter. If it is assumed that this is a hollow tube with copper equivalent

[^36]to a one-inch diameter rexl, it is prositle wh transmit three million kilowatts a thrnsand miles with abont 12 per cent loss and a million volts at each end. If fire-inch tubes were used there would be very little lose in fair weather but during a rainstorm the loss would be of the order of 1000 kw . per mile. An approximate idea of the size of a $1000-\mathrm{kr}$. tower eompared with a 220 -kv. (ower is slown in Fig. 11

The striking fact that these figures bring out is the large amonnt of power necessary to make such a line economically desiratle. They also emphasize the enormonts size of the apparatus units necessary: If present practice were followed $1,000,000-\mathrm{kw}$. transformer units would be necessary. This would probably mean erecting in the field. The problem of size and transportation becomes greater than the problem of voltage. ${ }^{7}$ However, it is only a little over ten years ago that the $200-\mathrm{kv}$. line was in a similar laboratory stage as the $1.000,000$-volt line discussed above.


Fig. 11. Comparison of $1,000,000$-volt and 220,000 -volt
Transmission Towers

# Resynchronizing Characteristics of Synchronous Motors 

By O. E. Smitay




#### Abstract

The resynchonizing of synchronous motors under heary bad is a new engineering accomplishment. Sucessful results were obtained only be redesigning cortain features of the motor and by originating several new anxiliary devices. The author diseusses factors for successful operation, torque characteristies and tests under operating conditions. He then shows the results of interruption in power supply and concludes his article with some remarks on general operating characteristics.- EDITor.


The usual applications of synchronous motors have been for purposes where in case of failure of power supply the motor could be allowed to shut down, and then started up in the usual way after the return of the voltage to normal. Recently, however, there has been a tendency toward automatic operation, and more attention is also being paid to minimizing interruptions, so that a motor and control which will allow the motor to remain connected to the line, either directly or through a protective reactance. is very desirable. These motors may be used to great advantage where momentary interruption of output is allowable, but where it is essential that normal operation should be restored as quickly as possible.

There are two classes of service for which these motors have been used.

The first class is for motor-generator sets which are connected to an Edison directcurrent system with storage battery reserve. The minimizing of the time of interruption of power supply is quite important, and a considerably smaller battery reserve will be allowable, if the motor-generator set will pick up the load immediately after the return of the main a-c. power.

The second class is for frequency converters which are operating singly or in parallel. but where there are no other generators operating in parallel with the generator units of the sets. The usual interruption of power is caused by a short circuit on the system supplying power to the motors of these sets, which will cause the roltage to drop to values ranging from zero to practically normal at the motor terminals. The motor voltage may be less than the breakout voltage corresponding to the excitation and load on the set, and if the duration of the voltage drop exceeds from ${ }^{1}+$ to ${ }^{1} / 2$ second with from one-half to normal load, the motor will usually drop out of step. When the trouble clears, the roltage almost immediately comes up to a value between 60 and

100 per cent normal, depending on the relative size of the motor and the system, and the line drop, and it is very desirable to have a motor that will pull into step without having to go through the usual starting procedure.

## Factors for Successtul Operation

The successful operation of a synchronous motor for resynchronizing after an interruption in power supply is dependent on two factors: the inherent design of the motor, and the functioning of the control equipment.

It is usually quite practicable to design the motor with sufficient torque at speeds close to synchronism to enable it to pull into step with a considerable percentage of load; but the current input at lower speeds may in some cases be objectionably high from the operating standpoint, as well as requiring considerable extra bracing of the coils to prevent distortion. It is, therefore, usually advisable to provide control equipment to change the connections of the motor (usually delta to Y); to throw over on a compensator; or to insert protective reactance in the circuit, when the speed drops below a certain predetermined value. depending on the design of the motor and operating conditions. The voltage of the power supply is quite likely to return after an interruption at a value somewhat lower than normal, and it is advisable to have a device for automatically reducing the load of the motor until it pulls in. This reduction in load may be accomplished, in the case of a motor-generator set or frequency converter, by inserting resistance in the field of the generator until the motor pulls in.

The torque of a synchronous motor, when operating at sub-synchronous speed, is considerably reduced by field excitation, and, therefore, some means should usually be provided for removing this field excitation. The torque near synchronism may be increased by the proper value of external
resistance in the fick. and the fied circuit may be arranged so that the field discharge resistor is connected in when the excitation voltage is removed. This lends itself to simplicity of control, as the discharge of the field is taken by the discharge resistor without other complication of control. The removal of the excitation and the use of a resistor in the field circuit has the additional advantage in the case of interruption of power in that the current surge, when the voltage returns, is rery much less than if the excitation is left on. Motors with direct-connected exciters are sometimes arranged so that the field is left connected across the exciter, and if the speed drops far enough, the exciter loses its roltage and consequently the excita-


Fig. 1. Torque and Stator Current Curves of a $6000-\mathrm{kv}$-a 25 -cycle 11,000-volt 300 -r.p.m. Synchronous Motor with Field Circuit Open
tion is removed from the motor field. This method of operation does not give nearly as good pull-in torque as closing the field on the discharge resistor, but is somewhat simpler in control, and mar be used if the lower value of pull-in torque is all that is required. This connection, however, introduces the danger that the exciter may not drop far enough in speed to remove the excitation, and there will be a very high surge of current when the voltage returns, especially if the voltage returns at full value instantaneously, as would be the case if the switch were closed on the motor.

There are not vet much data available as to the relative values of torque at 95 per cent speed, which is approximately the speed
from which the motor will pull in with forld applied for these various mothods of when wo but the tests now available indicate the following values, based on the worgue with the field open circuited as 100 per cent


Fig. 2. Torque and Stator Current Curves of a $1600-\mathrm{kv}-\mathrm{a}$. 60 -cycle 6600 -volt 720 -r.p.m. Synchronous Motor
Curse $A$. Field circuit open; Curve $B$. Field circuit closed through exciter, with normal setting of main and exciter field rheostats


Fig. 3. Torque and Stator Current Curves of a $1400-\mathrm{kv}-\mathrm{a}$. 60 -cycle 13,8006900 -volt 720 -r.p.m. Synchronous Motor
Curve $A$, Field circuit open; Curve $B$, Field circuit chosed through resistor with 6.2 times resistance of field winding

With the field short circuited or, with various values of field current up to so per cent normal excitation $=70$ per cent torque.

Field with discharge resistor $=120$ per cent torque.

Torque Characteristac Curves
A matulber of torque corves of symehromons
 beren lakern by the＂．Vecelerations＂＊methox， athel a fow representative casesatergivern．These curves were taken at reduced voltage and cor－

Figs．$: 3$ for a 1 foolokvoi．，（io－cyele motor shows very clearly the increase in torgue near syblaronism，due to the use of a proper resistor in the ficle circutt．The＂Aecelera－ tion＂method of testing is mot absolutely atcemate in this case as the motor aceolerates


Fig．4．Oscillograms of Starting Test of a $2500-\mathrm{kv}-\mathrm{a}$ ． 60 －cycle 13，200－volt Synchronous Motor，Direct Connected to an 1875 － kw．250－volt Direct－current Generator．Field closed through resistor with 6.1 times resistance of field winding．Start－ ing from tine with 10 fer cent series reactors
（Lefl）Initial start．（Right）Synchronizing，showing closing of field circuit on exciter，and short circuiting of reactors
Curve A，Motor ficld current；$B$ ，D－c．generator terminal voltage；（．A－c．line voltage；$D, A-c$ ．motor voltage；$E, A-c$ ． line current（also motor current）；and $F$ ，Speed of set．
rected to full voltage，assuming the torque varies directly as the square of the voltage，and the starting current varies directly as the voltage．

Fig． 1 is the curve for a $6000-\mathrm{kr}-\mathrm{a} ., 2.2$－ cycle motor with field circuit open．This curve shows the usual characteristics of the low resistance amortisseur winding；com－ paratively low starting torque，high peak in the torque curve near synchronism，and quite high starting current with full voltage．

Fig．． 2 for a 1600 －kr－a．，6（0－cycle motor gives a comparison of the performance with open field and with field closed on the exciter which was set for normal operating conditions．The curve for the latter condition is not exactly correct near synchronism，as the torque， due to the field excitation，does not vary as assumed above；but the curve is very nearly correct through most of the range．It may be seen that the torque is quite materially reduced with the field connected across the exciter，and also that the current is increased． The torque efficiency，that is，the torque in synchronous kw ．divided by the kr－a． input，is very much less with the exciter connected in than with the field open．

[^37]very quickly near synchronism，which intro－ duces crrors in the torque curve．A number of curves were taken for various values of resistance in the field，and they were very


Fig．5．Starting Characteristics of Synchronous Motor from Oscillograms，parts of which are shown in Fig． 4
consistent in indicating the peak in the curves so that there is no question that the use of a resistor in the field materially increases the torque near synchronism．The curve given in Fig ． 3 is the average curve as indi－ cated by several tests．

Tests Under Operating Conditions
The behavior under actual operating con－ ditions of a motor－gencrator set with motor designed for resynchronizing was tested in co－operation with the L＇mon（oas \＆Electric

 exciter．
 When the line is encreszed frem the mann


Fig．6a．Oscillograms of Resynchronizing Test from 84 Per Cent Speed． 2500 －kv－a． 60 －cycle 13，200－volt synchronous motor direct connected to $1875-\mathrm{kw}$ ． 250 －volt direct－current generator．Field closed through resistor with 6.1 times resistance of field wind ing．Motor connected to line through 10 per cent series reactors
 also motor current）：and $F$ ．D－c．generator line current


Fig．6b．Continuation of Oscillograms in Fig．6a

Company at Cincimmati．Ohio，and several oscillograms taken during these tests are given to show the results secured．

The motor－generator set consists of an 1ヵラ－5－kw．．2．う（i－rolt，d－c．generator，direct connected to a 2．50（）－kr－a．．（）．ラ．）－p－f．，13，2（1）－
generating statiom．When the set reaches a speed correspondine to almma（1．j per cent of the system sperer，a slip relay actuates the control，closing the monor field circuit across the armature of the exciter，and this in turn operates the chosing mechaniom of
the reactor short circuiting switehes. The d-c. generator is atutomatically paralleled with the d-c. system and picks up its load without attention of an operator.

A complete description of this substation is to be given in the N.E.L.A. report for 1922, by the Direct-current Substation Committee.

## Starting Test

Fig. 4 is an oscillogram, showing the initial and synchronizing period of a regular starting test. The motor is started by throwing


Fig. 7. Oscillograms of Resynchronizing Test from 90 Per Cent Speed. 2500-kv-a. 60 -cycle 13,200 -volt synchronous motor direct connected to $1875-\mathrm{kw}$. 250 -volt direct-current generator. Field closed through resistor with 6.1 times resistance of field winding. Motor connected to line through 10 per cent series reactors
Curve $A$, Exciter voltage; $B$, Motor field current; $C, A-c$. line voltage; $D$. D-c. generator terminal voltage; $E, A-c$. line current (also motor current); and $F$, D-c. line current
neeted to the bus. This gives a time of approximately $3: 3$ seconds after energizing the a-c. lines for the set to be operating at its required output.

## Resynchronizing Tests

These tests were made by operating the set at loads between 60 and 100 per cent and opening the a-c. main lines. The set then dropped to between 90 and 93 per cent speed with the d-c. machine operating as a motor. The speed was further reduced to a value of from i.) to !) per cent by cutting out the resistance in a temporary rheostat in the ficld of the d-c. generator. The permanent rheostat is arranged to begin cutting in resistance as soon as the power returns, which reduces the load until the motor synchronizes, after which the rheostat adjusts the field to hold the proper value of load. This reduction in field enables the sct to synchronize under practically any conditions of initial load or a-c. power supply.

Fig. 6 is an oscillogram of a test resynchronizing from st per cent speed. The generator load rises to about 110 per cent, after which it is reduced to $\$ 4$ per cent at the time the motor pulls in. The motor was in step with the field on and reactor short circuited in approximately 10 seconds after the return of the a-c. voltage. The line
normal voltage on directly through protective reactors, having approximately 10 per cent reactance. The values of line voltage, motor voltage, stator current (also line current) and time, are plotted against synchronous speed. Refer to Fig. 5 for these curves.

A similar starting test, including the complete cycle, was also taken, and the set came up to speed, the exciter built up, the motor field was applied, the reactor short circuited, and the motor synchronized in 18 seconds. The d-c. generator built up to normal voltage and was connected to the d-c. bus about 10 seconds later. The generator load was then adjusted automatically to its proper value for holding voltage at the center of distribution. This load adjustment was completed in $\bar{i}$ seconds after the generator was con-
current to pull in was approximately $21 / 2$ times the normal rated current of the motor.

Fig. 7 shows a similar test resynchronizing from 90 per cent speed. The motor came into step very quickly in this case with the $\mathrm{d}-\mathrm{c}$. load rising to 76 per cent when the motor reached synchronous speed. The set was up to synchronous speed with field applied and reactor short circuited in about 2.7 seconds after return of the a-c. voltage. The maximum peak value of current was about 2.7 times the maximum value of the normal current wave.

## Interruption of Power Supply

The tests described above were more severe than actual operating conditions, as the speed of the set was reduced considerably below its usual value under normal operation.

A test was made operating at normal load, opening the power supply for a few seconds, and then reclosing the a-c. switeh. IVig. \& is an oscillogram of this test. The power was off $3 . S$ seconds during which time the speed dropped to about 90 per cent, the mot or field opened on to the lischarge resistor and the reactor short circuiting switches opened. The set came up to the speed which operated the slip relayy, and the motor field closed 2.6 seconds after the return of the a-c. voltage; the reactor was short circuited about ${ }^{1}$ í second later. The (1-c. generator rheostat then started to adjust the load and in 7 seconds the load was back to normal. The total time from the return of the a-c. voltage until the set was in normal operation was slightly under 10 seconds.

## GENERAL OPERATING CHARACTERISTICS

There are a number of different designs of motors for resynchronizing service. The three usual ones may be classified as follows:

1. Standard stator windings with low reactance amortisseur winding.
2. Special stator winding for $Y$ connection, when starting, and delta connection for running, with low reactance amortisseur winding.
3. Standard stator winding with high reactance amortisseur winding.
These motors will, of course, all have low resistance amortisseur windings, and the stator reactance is not subject to much change, as it depends principally on the voltage and design characteristics of the motor, which cannot be easily modified.

Motors classed as No. 1 arre uscel For servire when the speed will not drop bedow apporoximately 90 per cent, as in the case of motergenerator sets with storage baltery reserve


Fig. 8a. Oscillograms of Interruption of Power Supply and Resynchronizing Test. 2500-kv-a. 60 -cycle 13,200 -volt synchronous motor direct connected to $1875-\mathrm{kw} .250$-volt direct-current generator. Field closed through resistor with 6.1 times resistance of field winding. Motor connected to line through 10 per cent series reactors
Curve A, Exciter voltage; $B$, Motor field current; $C$, A-c. motor voltage; $D, D-c$ generator terminal voltage; $E$, A-c. line current (also motor current) ; and $F$, D-c. line current


Fig. 8b. Continuation of Oscillograms in Fig. 8a
on the d-c. system. These motors may be started by reduced voltage from compensators. This design will give the best torque efficiency (starting torque in synchronous kw. divided by kr-a. input). and consequently
the most desirable starting characteristics. It should be noted that a low resistance annortisseur winding, which is necessary for a resynchronizing motor, does not have nearly as good torque efficiency at starting as a motor with the usual high resistance winding designed for starting duty only, and consequently the kv-a. input for starting on the former class of machines is materially higher than for the latter class.

The use of a compensator may be eliminated for motors of class No. 2, and this class usually gives very satisfactory operation. The low resistance amortisseur winding gives quite low initial starting torque, and it is, therefore, usually necessary to design for low rotor reactance to insure starting on the Y connection. The control for this type of motor may be arranged to change over from I to delta at a speed from $S 0$ to 95 per cent, and also to change back in case the speed drops down to 5 per cent less than the value at which the change-over was made for increasing speed.

Motors of class No. 3 may be used when the motor is rather small in comparison with the system, and the higher starting current is not objectionable. Simplicity of control may be obtained by starting directly from the line through reactors which are short circuited when the motor comes up to from 80 to 95 per cent speed. The motor for this service being designed for higher reactance in the rotor, does not take as high initial starting current as motors of class No. 1, although the pull-in torque is slightly less than for the latter type.

Referring to Fig. 5 it is evident that the stator current is fairly constant as the motor comes up to speed, and does not begin to fall off materially until about 90 per cent speed is reached. It is, therefore, essential that the connection should not be changed from Y to delta until the motor is very nearly up to speed or there will be a considerably greater rush of current when the change-over is made than was obtained for the initial starting period.

The value of torque at which the motor can be pulled in is usually determined by the allowable current input that may be taken from the line. The 25 -cycle motor, for which curves are given in Fig. 1, would pull in at nearly two times normal torque with full voltage applied, but the current required would vary from five times normal at 85 per cent speed down to $31 / 2$ times normal
at 95 per cent speed. This current would be excessive, and a change of connections or the use of reactors would be desirable. The 60cycle motor, Fig. 2, would take less than 3 times normal current from 85 per cent speed up, but the pull-in torque is only about 85 per cent normal. However, there will usually be quite a considerable line drop for these values of current, and, therefore, the motor may remain connected to the line after disturbances of one or two seconds duration without taking an excessive amount of current to pull back into step. Protective reactors, that may be inserted in the circuit in case the speed falls below a certain value, may sometimes be necessary if the motor is connected to buses close to large generating apparatus. The torque at which the motor will pull in successfully under ordinary operation will be from 40 to 100 per cent of normal, and it is usually not necessary to go above these values.

Reference to the torque curve $B$, Fig. 3, shows that the maximum peak of the torque curve is rather sharp and close to synchronism. In case the load comes up too quickly during the synchronizing period, or the voltage is low, it may sometimes happen that the load exceeds the peak of the curve, and then the motor behaves exactly like an overloaded induction motor and drops down in speed to a point where the slope of the curve between load and speed is greater than that of the torque curve of the motor. A motor-generator set with selfexcited d-c. generator and straight resistance load not operating in parallel with other generators will drop down in speed to approximately 70 per cent of synchronism.

The application of resynchronizing motors to frequency converters has not been as widely extended as it should be, as with these motors and proper control it should be possible to maintain operation on the generators with only a short time of interruption in many cases where there is now a complete shut-down on the system. The usual short circuit disturbance is just about sufficient to drop the machines out of step, but the speed does not have time to decrease very far before the short circuit is cleared and the voltage returns on the motor lines. The use of a resynchronizing motor, and a reduction in load by automatic decrease of generator excitation until the set is in synchronism, should enable these machines to recover the load within a few seconds after the return of voltage on the motor lines.

# Status of 220,000 -volt Transmission 

By G. F. Brown<br>Lheminci Engnemerng Department, General Electric Cumpans

The importance of an increase in transmission voltage, brought to commercial practice, is apparent when we realize the new fields of development it opens up. Our article describes the present status of 220,000 -volt transmission giving a list of the installations now made and being made. The author discusses the apparatus, the use of lightning arresters and line insulation and then gives some notes on corona, line charging and regula-tion.-Editor.

For more than ten years there has been no substantial increase in the maximum voltage of power transmission. But the problems of transmitting at greatly increased voltage have received a great deal of attention in the last half of this period.

During the present summer it is expected that California will break another record, and the transmission of power at 220,000 volts will become an accomplished fact. Successful operation at this coltage will doubtless give impetus to other large projects, now under consideration, for which such a transmission voltage is essential.

The first extensive studies of 220.000 -volt transmission were published in 1919.* The major power companies of California at this time were also studying the problem, being faced with the early necessity of transmitting very large blocks of power over distances of more than 200 miles. Their requirements were apparently outside the economic field of existing transmission voltages, on account of the excessive number of circuits required and the consequent high investment per kw. for transmission.

A capacity of 100,000 to $150,000 \mathrm{kw}$. per circuit fitted in well with their development programs, and was about double the circuit capacity with existing voltages. For these loads a transmission voltage of the order of 200,000 volts was required, and 220,000 was selected as the nearest voltage corresponding to the established practices of standardization.

It was felt that the problems of construction and operation at this voltage were not too far outside past experience. The manufacturers were prepared to build apparatus for this voltage on a commercial basis.

Estimates of cost showed that the investment for transmission would be 30 to 50 per

[^38]cent below that required if the existing voltages were retained.

Having decided upon 220,000-volt transmission the power companies of California moved rapidly. Extensive investigations were undertaken by Mr. F. G. Baumt for the Pacific Gas \& Electric Company. The Southern California Edison Company assigned Mr. R. J. C. Wood $\ddagger$ and Mr. H. Michener to the investigation of their problems. Orders were placed for 220,000 -volt apparatus as follows:

Southern California Edison Company

| Date | Station | 220,000 -volt Apparatus |
| :---: | :---: | :---: |
| June, 1920_... Big Creek No. 8 Transformers and |  |  |
| Circuit Breakers. |  |  |

## Pacific Gas and Electric Company

Sept., 1920 .. Pit River No. 1. Transformers
Jan., 1921 ... Vaca Substation. Transformers ....
July, 1921... Pit No. 1 and
Vaca Sub..... Oil Circuit Breakers

The total transforming capacity installed at present, for 220,000 -volt operation, is:

Pacific Gas \& Electric Company, 200,000 kv-a.

Southern California Edison Co., 523,500 $\mathrm{kv}-\mathrm{a}$.

These figures include both step-up and stepdown units, but do not include spare capacity. In addition there are 36 oil circuit breakers on these 220,000 -volt circuits.

Fig. 1 shows Big. Creck No. \& Stationthe first 220,000 -volt hydro-electric station, and Fig. 2 shows the Vaca Substation-the first substation constructed for 220,000 -volt operation.


Fig. 1. Big Creek No. 8 Generating Station of the Southern California Edison Company

## PROBLEMS OF 220,000 -VOLT TRANSMISSION

Apparatus
The General Electric Company had been for some time prior to this engaged in a study of the design of apparatus for 220,000 -volt service.

In the design of power transformers it was found that it would be very desirable to change the then existing practice of building transformers good for ungrounded operation. While it is entirely practicable to extend this practice to 220,000 volts, such designs were very expensive in comparison with similar transformers designed for permanently grounded operation. This reduction in cost is of the order of 3.5 per cent and is entirely due to the elimination of the heary insulation at the ends of the windings and the consequent saving in space. No reduction is made in the turn and coil insulation, the insulation of buffer coils and coils throughout the stack being to the same specifications as that used for transformers designcd for ungrounded operation.

In all of the transformers built by the General Electric Company for this service, the high-tension lead is brought to the middle of the coil stacks and progresses both ways through the winding to ground. This is shown diagrammatically in Fig. 16, page 346 , and physically in Fig. 14, page 345 . This idea of having the high-voltage terminal in the center of the stack was first put forward by Mr. W. J. Wooldridge of the General Electric Company in 1906 and patent was issued the succeeding year.

Fig. 14, page 345 , shows the core and coils of the $20,000-\mathrm{kr}-\mathrm{a}$. $220,000 / 72,000$-volt transformers for the Laguna Bell substation of the Southern California Edison Company. Fig. 15, page 345 , is of the complete transformer. There are seven of these units


Fig. 2. Vaca Substation of the Pacific Gas \& Electric Company
installed, two banks of three, and one spare, each bank having an output of $60,000 \mathrm{kw}$. Fig. 3 shows the seven auto-transformers at the Vaca Substation of the Pacific Gas and Electric Company; these are also arranged in two banks and a spare; stepping down from 200,000 to 110,000 volts; output per bank is $50,000 \mathrm{kw}$. Fig. 4 shows the bank of $220,000-$ volt transformers installed in Big Creek No. 8 Power Station of the Southern California Edison Company. The capacity of this bank is $25,000 \mathrm{kv}-\mathrm{a}$.

The oil circuit breakers, except as to size, insulation and clearance, are similar to the latest design for lower voltages. It does not appear that the interrupting duty on these breakers for some time to come will exceed that which many breakers are doing at lower voltages on the more concentrated systems in the East.

The oil circuit breakers supplied by the General Electric Company are of the explosion chamber type. Fig. 5 is the completely assembled breaker. Fig. 6 is a riew of the cover with bushings, explosion chambers and insulation and separator mounted.

## Lightning Arresters

No lightning arresters have been installed, neither has extra insulation been employed on the apparatus, as advocated by some engineers. Some engineers seem to have reached the conclusions that an operating voltage of 220,000 is of the order of induced lightning


Fig. 3. Seven 200,000 -volt Auto-transformers at the Vaca Substation of the Pacific Gas \& Electric Company
disturbance; that arresters are of little use in case of direct stroke; and that the solidly grounded neutral at all points reduces surges due to switching. Operating experience should yield useful information with due allowance for climatic and geographical conditions.


Fig. 4. Three 8333-kv-a. 220,000-volt Transformers Installed in Big Creek No. 8 Hydro-electric Station

## Line Insulation

At the outset it was known that, due to uneven distribution of voltage over long strings of insulators, the unit next the line carried about 30 per cent of the total stress, and that this percentage was practically constant for strings of any number of units above five. Increasing the number of units would not lessen the duty on the insulator next the line, which at 220,000 volts was beyond that set by good practice.

Professor Harris J. Ryan* and F. W. Peek, Jr., $\dagger$ pointed out several ways of correcting this uneven distribution, and lowering the duty on the line unit. Of the means suggested the two most promising were
a. Grading of insulators by use of units of different size at the line end.
b. Use of static shields.

The Pacific Gas \& Electric Company have solved the problem along the lines of the first named method (see Figs. 7 and S) while the Southern California Edison Company are using shield rings on strings of standard 10 -inch units throughout (see Figs. 9 and 10). Extensive studies have also been made of the shield-

[^39]ing effects of the towers and location of shiclds for the purpose of minimizing the cascading of ares ower insulator strings at times of fashovers.


Fig. 5. Complete Oil Circuit Breaker, One of Eight that will Handle the 220,000 -volt Circuits at the Laguna Bell Substation of the Southern California Edison Company


Fig. 6. Single Unit Oil Circuit Breaker Removed from Tank. These breakers are installed at the Laguna Bell Substation

## Corona

Extensive field tests were conducted by the Southern California Edison Company on a 27 -mile section of the line with voltages up to


Fig. 7. Straight Line Tower on the 220,000 -volt Pit River Line of the Pacific Gas 8 a Electric Company

280,000 . The results are in accord with Peek's formula. Complete calculation for the Big Creek lines show negligible corona loss; none below 4000 ft . altitude. Under most extreme


Fig. 8. Transposition Structure of the 220,000 -volt Pit River Line of the Pacific Gas \& Electric Company
assumptions as to storm conditions the corona loss is about $\because$ - per cent.

## Line Charging

In the matter of line charging it has been necessary to abandon past practice of building each generator large enough to pick up and control an unloaded circuit. Each of these California systems will require 40,000 to $50,000 \mathrm{kv}-\mathrm{a}$. to charge a single circuit. It would require a 60,000 to $70,000 \mathrm{kv}-\mathrm{a}$. generator of normal design to do this under normal operating conditions and still retain control of the voltage. This is about twice the size that other conditions have heretofore dictated for these developments.

## Regulation

Synchronous condensers are installed at the receiving ends of these lines, in sufficient amount to maintain constant voltage from no load to full load.

## Existing Plant and Equipment

The problem of raising existing stations on the Big Creek system from 150,000 to 220,000


Fig. 9. Anchor Tower on 220,000-volt Big Creek Line of the Southern California Edison Company
volts has been soferd by installing at eato of these stations two banks of auto-t ransformers: one bank in each circuit. These hanks are installed as an integral part of the line withorut


Fig. 10. Tie-down Tower on 220,000 -volt Big Creek Line
switching equipment of any kind. Each bank is good for the entire output of the station: that is, under normal conditions they will operate at half load, which is the point of maximum efficiency. This plan showed the lowest cost, and high efficiency. It has the very decided advantages of simplicity and full use of existing equipment without change.

These projects have had the closest atter1tion of all concerned, and operation will be begun with assurance that everything physically possible, that could contribute to their success, has been done.

# Carrier Current Communication Over High-voltage Transmission Lines 

By E. Austin<br>Radio Enginelering Department, General Electric Company


#### Abstract

Carricr current telephony is sort of a first cousin to wireless communication. It is likely to find extensive application on a! large power systems and in the public utility field, and as there has been little publication on the subject, we believe the author's comprehensive and practical treatment will be appreciated.-Editor.


When telephone communication is desired between stations on a power transmission system, there are three ways in which it can be provided. The most common method in use today is to erect a telephone line between all stations on the system, and use regular wire telephony.

The second method is the application of radio telephony which requires no interconnecting wires for successful operation.

The third method utilizes the existing power circuits to carry the communication, and is known as carrier current telephony.

The relative merits of the first two methods are fairly well known, whereas very little has been published to date on the third or carrier method. Therefore, the outstanding question is "What are the features of carrier telephony which make it especially well adapted to this class of communication?"

In considering this question, it is advantageous to outline, in a general way, how carrier current telephony is accomplished.

First: There is provided a source of relatively high frequency alternating current of constant amplitude. This is usually produced by a pliotron in conjunction with an oscillating circuit. The high frequency current thus generated is known as the carrier.

Second: Suitable means are provided for controlling the amplitude of this carrier. It is moulded into an electric current varying in accordance with the sound waves set up by the voice. This action is commonly called modulation.

Third: This modulated carrier current is transferred to the overhead transmission lines which serve as the conducting channel. It is superimposed directly on the current normally carried by these lines, thus obviating the necessity of a separate communication circuit. A single wire, one or two tower lengths, is usually used for this purpose. This is called the coupling wire.

Fourth: The carrier current thus transferred to the power lines is guided by them to the distant receiving stations, instead of being broadcast in all directions as with radio.

Fifth: The current arriving at these receiving stations is drained from the power conductors by a coupling wire. Suitable circuits, selective to the carrier frequency only, are used in order to suppress the lower frequency power current.

Sixth: The received carrier energy is converted into sound waves of the same character as those produced by the speaker.

The first, second and third are accomplished at the transmitting station, the fifth and sixth at the receiving stations. The fourth, however, is provided by the existing power circuits connecting the various stations on the system.

Thus, carrier telephony combines the chicf advantage of each of the other two methods, without the corresponding disadvantage of either. Namely, the advantage of radio-that a special circuit is not required -is combined with the advantage of wire telephony, that directive transmission is obtained.

There are a number of other important features of the carrier system. The quality, for example, is in most cases better than that obtained on the wire line. When unusual precautions are taken with the wire lines such as use of a separate pole line, frequent transpositions and drainage, then the quality obtained during normal operation is about the same with either type. Actual tests have shown, however, that even on a system where all precautions were taken the carrier was many times superior during cases of short-circuit and grounding of the power conductors. Since it is during the time of trouble that communication is most needed, this advantage of carrier is obvious.

The quality obtained with radio and carrier are practically the same.

The hazard of accidental contact with the high-voltage line is many times greater with the wire telephone than with the carrier, except in cases where the telephone wires are on a separate pole line. The coupling wire used at each end is only a fraction of a mile in length, whereas the telephone line must
extend throughout the entire distance. The coupling wire is usually somewhat closer to the $h-v$. lines than the telephone circuit, thus increasing somewhat the probability of accidental contact with the li-v. linc. This possibility is reduced considerably by using the same conductor and spacing as cmployed for the li-v. lines. In this way the chance of contact between coupling wirc and line is made as small as that of contact between lines. The same general form of protection is used on both the wire line and coupling wire, so that they are equally capable of withstanding accidental contact.

Some further advantages of carrier over radio telephony for this class of communication are brought about by the directiveness of carrier transmission. A radio station transmits almost uniformly in all directions whereas the carrier is confined to the $h-v$. lines. This results in far greater power being received at the distant point for a given input at the transmitter, or conversely the same received energy for a lower transmitted power. For this reason, reliable calling or ringing can be provided far more economically with carrier than with straight radio, thus eliminating the need for an operator on watch, twenty-four hours each day.

Privacy to the extent of the system and very little interference to external communication circuits are two direct results of the carrier's confinement to the $\mathrm{h}-\mathrm{v}$. lines. This also makes it possible to operate the carrier stations without a license or licensed operator. The costly towers required for a radio antenna are not required for the carrier system since the coupling wire is suspended directly from the existing transmission line towers.

From the foregoing, it is obvious that carrier telephony is very well adapted to communication between power stations over power transmission lines.


Fig. 1. A Fundamental Transmission System

## Technical Features

In order that the operation of carrier telephone equipments under actual service conditions be better understood, it is desirable that some of the technical features be considered.

Fig. 1 represents a simple power transmission system. $L$ is the transmission line between the generator station and the loarl. $T_{1}$ and $T_{2}$ are transformers connecting the power apparatus to the line. $T$ and $R$ represent the points between which carrier


Fig. 2. Variation of Received Voltage with Distance $E_{T}=$ Transmitted voltage $\quad E_{R}=$ Received voltage
communication is desired. For simplicity, only one transmitter $T$ and one receiver $R$ will be considered.

Any voltage $E_{T}$ impressed on the line at $T$ will result in a voltage at $R$. This voltage represented by $E_{R}$ will be less than the impressed voltage. The value of $E_{R}$ can be determined, if the circuit constants are known. Neglecting, for the present, the effect of the power transformers $T_{1}$ and $T_{2}$ and assuming that the proper terminal impedances are provided at $T$ and $R$, then $E_{T}$ will cause a voltage $E_{R}$ at the receiving station, which is governed by the following relation:

$$
\begin{equation*}
E_{R}=E_{T} e^{-a L} \tag{1}
\end{equation*}
$$

where $L$ is the length of line, and $a$ is the attenuation constant determined by the resistance, leakage, capacitance and inductance of the linc.

In the case of a uniform line of constant attenuation, the voltage received varies with distance in the manner shown in Fig. 2.

Another interesting curve is plotted in Fig. 3. This shows the variation in impressed voltage with increasing distance for a given received voltage. The attenuation is assumed to be constant, as in Fig. 2. This curve shows quite clearly that the impressed voltage required varies at a greater rate than the distance. This factor is of considerable importance when considering extensions to existing carrier systems.

Uniform lines properly terminated are seldom, if ever, met when applying carrier to existing power transmission lines. This is primarily due to the effect of shunt transformers, intermediate taps, and the difficulty of coupling to the $h-v$. line with a carrier


Fig. 3. Variation of Required Impressed Voltage with Distance for a Given Signal Strength
$E_{T}=$ Transmitted voltage $\quad E_{R}=$ Received voltage
circuit of the proper impedance to fit each particular line.

The equivalent circuit of a simple system is shown in Fig. 4. $T$ and $R$ represent the carrier stations. $Z_{1}$ and $Z_{2}$ represent the impedances of the power transformers at the carrier frequencies. These transformers are represented with one side grounded. This represents the general case since practically all transmission systems are grounded, either directly through an impedance or by capacity effects. The value of these impedances varies with the load on the lowvoltage windings of the transformer. For the simple arrangement shown, the impedance of the high-voltage side varies approximately as the square of the voltage ratio of the transformer. Thus, if the impedance of the lowvoltage side is 100 ohms and the voltage step-1p is in the ratio of 1 to 10 , then the effective impedance is approximately $10^{2} \times 100$, or 10,000 ohms.

Since the type, capacity and load vary considerably from station to station and from time to time it is obvious that fixed relations cannot be established. Actual measurements on certain transformers have indicated that, in the majority of cases, the impedance of the transformer at the frequency used is relatively high compared with the rest of the elements under consideration. The energy which the transformers absorb from the circuit will then be relatively small.

The impedance of $\mathrm{h}-\mathrm{v}$. lines varies considerably with the number of circuits, arrangements on the towers, etc. As in other cases, the impedance of the output and input circuits should be matched for the maximum energy transfer. Accordingly, the most desirable conditions will exist when both the carrier transmitter and receiver circuits $Z_{T}$ and $Z_{R}$, respectively, have an impedance equal to the characteristic impedance of the lines. Furthermore, it would be advisable that the impedance of all transformers and other power apparatus on the line be of such a high value that they would act essentially as an open circuit to the carrier current.

We have just shown that the impedance of the power transformers is relatively high compared with the line impedance. Regardless of the relative values, neither can be altered appreciably without the use of costly and rather undesirable apparatus.

The problem then becomes one of designing a coupling arrangement which will most efficiently impress carrier on the $\mathrm{h}-\mathrm{v}$. line at the transmitting station and absorb carrier from the $h-v$. line at the receiving station. Any arrangement which will provide for an efficient transfer of energy between the line and coupling wire will serve equally well at the transmitting or receiving stations.

Coupling through instrument transformers, power transformers, high-tension condensers and paralleling wires have all suggested themselves. These methods have been tested. The best method to be used is determined by the operating conditions at the power station, and the cost of the equipment required.


Fig. 4. Equivalent Circuit of a Simple Transmission System
Fig. 5 shows a typical arrangement of the circuits at a power station. $A, B$ and $C$ are the three incoming phases of the h-v. line. $S, S_{1}$ and $S_{2}$ are air break disconnecting switches which permit grounding of the lines when disconnecting from the station bus. Current transformers, C.T., are shown in each of
the three lines. The neutral of the transformer is shown metallically grounded. Actual conditions will vary somewhat from these outlined, but will not alter the general method of operation which is under consideration at this time.

Normal operation is with the switches $S, S_{1}$ and $S_{2}$ closed. However, in cases of trouble on the lines, they are disconnected and frequently the lines are grounded. Thus, two widely different sets of conditions must be met.

In the first case, the lines are ungrounded and connected to the power transformer windings. These windings offer a relatively high impedance to the carrier current. When the switches are opened and the lines grounded, the impedance offered to the carrier is relatively small. This impedance is only that offered by the lines between the point of grounding and the station ground.

Fig. 6 shows the equivalent circuit. Since the conditions on the three lines are similar, only one line is shown. The lines are represented by units of series and shunt impedances, which determine the characteristic impedance of the line, $Z_{0}$.

During normal operation, the switch $S$ is in the lower position connecting the transformer winding $Z_{1}$ in parallel with the carrier equipment, represented by $E_{T}$. As previously pointed out, the impedance $Z_{1}$ is usually relatively large compared with $Z_{0}$.

When the switch is in the other position the impedance $Z_{1}$ is reduced to zero. The only impedance offered by this circuit is


Fig. 5. Circuit Arrangement at Power Station
that cfthe line between point $A$ back through switch $S$ to ground. This impedance is usually very low compared with $Z_{0}$, so that the line and carrier are effectively short circuited.

Two solutions are obrious. The voltage can be introduced in series with the line by
opening switch $S_{4}$, thus feeding from carrier generator Es. This is quite satisfactory for operation with grounded lines, but las the disadvantage previously mentioned, that Es must be sufficiently high to work through impedance $Z_{1}$ of the transformer when in circuit.


Fig. 6. Equivalent Circuit of Power Station Arrangement
The other solution is to apply the voltage in shunt as with $E_{T}$ only at a point $B$ sufficiently far out on the line so that the impedance of the ground path is increased to a value comparable with $Z_{0}$.

Since any method of coupling employed must be satisfactory under both normal and abnormal conditions in the station, it is obvious that the second solution is the one to be used.

The problem of impressing the carrier voltage on the line at any point is quite involved. Any apparatus directly connected to the $\mathrm{h}-\mathrm{v}$. line must be insulated to withstand not less than two or three times the operating voltage of the line. The cost of such equipment as condensers or transformers is so high for lines above 33,000 volts that it is seldom economical to use them. Furthermore the disadvantage arising when the lines are grounded from coupling at a point within the station also influences the decision not to use direct coupling equipment.

The use of a parallel coupling wire solves both of these difficulties. It is relatively inexpensive, since it need only be insulated for low voltage, and can usually be constructed from material available at the power station. It can be made sufficiently long so that part of the carrier energy is impressed on the line at quite a distance from the point of grounding, thus grounding the lines in the station is made relatively ineffective.

The chief disadvantage of this method of coupling is low efficiency. This can best be seen by reference to Fig. 7. The capacitance of the coupling wire to ground is represented by $E C_{2}$, of the coupling wire to the $h-v$. line by $E C_{1}$, and the $h_{i}-r$. line to ground by $E C$. ER represents the effective resistance of the circuit. $E_{T}$ and $I_{T}$ are the carrier voltage and current into the coupling wire.
$I_{1}$ represents the portion of the current induced in the h-v. line which loaks back into the station, while $I_{2}$ is the eurrent on the h-v. line actually passing the end of the coupling wire toward the receiving station.

The voltage $E_{T}$ caluses a current $I_{T}$ to flow which divides inversely in proportion


Fig. 7. Equivalent Circuit of Coupling to Line
to the impedances offered by the capacitance $E C_{1}$ and $E C_{2}$. Since $E C$ is large in comparison with $E C_{1}$, it can be neglected for the present.

The current passing through $E C_{1}$ into the $h-\mathrm{r}$. line represents useful energy, whereas that absorbed by the coupling wire capacitance to ground is lost, dissipating itself in the resistance of the circuit.

An example of a typical coupling wire will show the low efficiency effect quite clearly. A coupling wire 1000 ft . long, and 40 ft . above the ground and 10 ft . from a single $h-v$. line has an electrostatic capacitance of approximately 0.002 microfarads to ground and 0.0009 microfarads to the overhead wire. Thus the current divides, approximately 55 per cent passing to ground directly and only 45 per cent being transferred to the line.

In practice there are usually three or more conductors in the $\mathrm{h}-\mathrm{v}$. line so that this ratio is somewhat improved.

The maximum efficiency will obtain when the impedance of the carrier circuit equals the effective impedance of the carrier equipment. This condition can only be approached with this method of coupling. Increasing the length of the coupling wire decreases the impedance between it and the line. However, at the same time it results in an increase in the capacitance between the coupling wire and ground. Thus more energy is required from the carrier generator to charge the coupling wire to the same potential. It is obvious that a limit will be reached beyond which it is not advantageous to extend this wire.

Experience has indicated that a good average length for the coupling wire is approximately 1000 to 2000 ft . This length has also been sufficient to reduce to a workable value the effect of grounding the lines at the station.

The factors governing the crection of coupling wires to provide the maximum (fficiency may be summarized as follows:

1. The wire should be kept as far above the ground as possible.
2 . The distance between the coupling wire and all lines should be made as small as possible consistent with safety. The usual spacing is that used between phases of the line.
2. The coupling wire should be at least 1000 ft . long.
3. The coupling wire should be brought to the carricr equipment by the most direct path. The uncoupled portion or lead-in tends to increase $E C_{2}$, Fig. 7. without increasing $E C_{1}$, thus lowering the efficiency.

As previously stated, any arrangement used to transfer energy to the line will serve well to absorb energy from it. Accordingly the factors summarized above apply to the erection of a coupling wire for reception as well as for transmission.

Fig. 8 shows a typical coupling arrangement with its protective equipment. The coupling wire is connected through the lead-in to a high-voltage low-current fuse, $F$. This point is connected to the ground through a horn gap, a drainage coil and the carrier equipment.

The impedance of the drainage coil $L_{1}$ is very low at the power frequency, but extremely high at carrier frequencies. It will, therefore, drain off the static charge that accumulates on the coupling wire without absorbing power from the carrier equipment.


Fig. 8. Schematic Diagram of Coupling Equipment with Protective Apparatus

In the case of momentary contact between the $\mathrm{h}-\mathrm{v}$. line and the coupling wire, the choke $L_{1}$ will pass enough current to blow the fuse $F$. In case of a steep wave front the voltage across $L_{1}$ might rise very rapidly: The horn gap $K$ will discharge to ground, until
the fuse has time to blow, thus limiting the voltage across the carrier equipment.

The chance of contact with the $h-v$. line is very slight as pointed ont in the introduction. However, this protective equipment is supplied as additional insurance against possible damage.

In practice simple systems such as the one thus far considered are very seldom, if ever, met. For example, there are usually a number of transformers tied on at intermediate points along the line. The effect of these transformers is the same as previously outlined for the terminal transformers. Unless they are of large power capacity and have heavy secondary loads, the carrier loss is smali. A rough approximation of the effect has been established. Every intervening transformer station is considered as the equiralent of 10 miles of line added to the actual distance. A line 40 miles long with three intervening transformer stations would then be said to have an equivalent length of 70 miles.

It is also obvious that more power will be required for communication over a given distance if the line divides or branches off at an intermediate point. The energy arriving at this point not only divides in inverse proportion to the impedances of the two circuits, but also some of the energy is reflected due to the change in the constants of the line at that point.

The equivalent of a tie-in in miles of line depends largely upon local conditions. The usual figure used is from 10 to 25 miles depending on the extent of the system.

Another form of loss which must be considered is the effect of one carrier receiver on another. This condition is illustrated in Fig. 9. In this case 1,2 and 3 are carrier stations coupled to the line. When Station 1 is calling Station 3, the intermediate Station 2


Fig. 9. Schematic Diagram of Three-station Communication System
will absorb some of the carrier. The usual procedure is to lessen the coupling to the line at Station No. 2. This is possible due to the shorter distance involved. The coupling is reduced to a value consistent with successful operation from Station No. 2,
and at the same time minimizing the offert produced on communication hetwern the two extremes.

A closed metallic path is not required for successful carrier communication. The inn-


Fig. 10. SChematic Circuit of Gap-bridging Equipment
pedance offered to the carricr in passing from the coupling wire to the line is relatively low, while to audio frequency telephone current it would be practically infinite.

However, for a given carrier voltage impressed at the transmitting station, the received voltage will be determined to a large extent by the impedance offered by the intervening path. Thus, if the impedance is high, due to breaks in the lines, open switches, intervening transformers, etc., the received voltage will be appreciably less than in the case of a direct unbroken circuit.

Tests have been made which indicate that all lines except one can be disconnected and grounded not only at the terminals, but also at an intermediate point without interfering with carrier communication. It is also known that five out of six lines can be opened at an intermediate point with the same result as before.

It is obvious from the foregoing that definite assurance cannot be given regarding the operation of carrier through breaks in the line. The only statement which can be made is that if the break is of such a character that the normal carrier frequency path is not completely opened or made too high in impedance then communication will still be possible.

There is another gap met on transmission systems known as the predetermined type such as open switches, step-up transformers, frequency changers, etc. This gap is definitely located and its magnitude known.

A method has been developed for bridging gaps in this class. Fig. 10 shows the most common method in use. $L$ and $L_{1}$ are h-v. lines separated from each other by switch $S$. $C$ and $C_{1}$ are wires erected parallel to $L$ and $L_{1}$ respectively. The exposure in each case is in the order of $2000 \mathrm{ft} . L_{2}$ is a tuning inductance which is adjusted to neutralize the capacitance of the coupling wires. In this way the impedance across
switch $S$, which was practically infinite, can be reduced to a much lower value due to the presence of this series tuned circuit between the two lines.

Successful operation has been obtained between stations on independent lines crossing each other at right angles, when coupled together through this form of gap bridging equipment. This method is equally applicable to bridging the other forms of predetermined gaps mentioned above.

Another obstacle is met in carricr transmission when high-tension cables rather than aerial lines are used to carry power between stations desiring carrier communication. High efficiencies cannot be obtained because of the tremendous increase in power required to
radio telephony. The circuits used, although modified to fit the somewhat special conditions of carrier service, are essentially those used in radio equipments. The most essential difference is the ringing feature incorporated in the carrier equipments. This is very seldom furnished with radio equipments.

Fig. 11 shows the transmitter-receiver cabinct supplied with the 50 -watt simplex carrier current telephone and calling equipment. This equipment is rated for communication over 85 equivalent miles.

This cabinet is divided into two compartments. The receiving apparatus is mounted in the compartment on the right and the transmitting apparatus on the left.

The receiver is further subdivided into the tuned coupler in the top section, the three vacuum tube units in the center section and the calling and control apparatus at the bottom.

The transmitter compartment contains the generating and modulating units and their accessories. A small panel is provided across the bottom of this compartment to mount switches, fuses and controls. Power for the transmitter is supplied from a motor generator operated from the station supply. The receiver is supplied from a 6 -volt storage battery. These units are shown in Fig. 12 along with a spare storage battery and charging equipment.

The three units shown in Fig. 13 are located conveniently to the station
charge the cable to the required potential. Carrier communication is possible over short lengths of cable if specially designed equipment is used.

Not over two or three per cent of the total number of power companies actively interested in carrier have presented conditions involving high-tension cables.

The influence of the power circuits and apparatus has been outlined briefly above. The effects may be summarized as follows: The more intricate and complex a power transmission system, the greater the power required for successful communication. Accordingly, all conditions must be known in detail before outlining a carrier communication system.

## Carrier Equipment

The equipment required for carrier telephony is similar to that used for commercial
attendant. They are the operator's desk stand, and control unit, a terminal box, and the calling bell.

The control unit on the side of the desk stand contains a three-position key, selfrestoring to the neutral position. When in the neutral position this key controls circuits which place the carrier equipment in the receiving condition so that the station attendant can hear the speech from the remote transmitter.

When this key is held in the lower or talk position, the apparatus is automatically re-connected for transmission. This method of operation is known as simplex in comparison with the duplex method which does away with this control.

The upper position is used in sending out calling impulses. Code combinations are used to select stations when there are more than two on the same system.

A lead covered cable is also melucled with this operator's control equipment to connect it with the transmitter-receiver cabinet. Experience has indicated that the distance between the transmitter-receiver cabinet and operator's control is seldom, if ever, in excess of 250 ft . Accordingly, the circuits were proportioned for distances up to 250 ft . Special provision is then made for distances in cxcess of this.


Fig. 12. Fifty-watt Carrier Current Telephone Equipment; Rectifier, Storage Batteries, and Motor-generator

Fig. 14 shows schematically the circuit used in the carrier transmitter for telephony. The functions of the coupling wire and its protective units $F, K$ and $L_{1}$ have been given.

Switch $S$ serves to connect the coupling equipment to either the transmitter or receiver. Condenser $C$ and the oscillation transformer $L_{2}$ in conjunction with the coupling wire determine the frequency of the carrier current generated by the oscillator. $C_{1}$ and $R$ are grid leak (resistor and condenser) providing the proper grid bias potential


Fig. 13. Fifty-watt Carrier Current Telephone Equipment; Desk Telenhere, Terminal Box and Calling Bell
for the oscirfator. $C_{2}$ is a condenser blocking the 1000 -volt d-c. from the output system.

Two 50 -watt pliotrons are used, one as an oscillator, the other as a modulator.

Inductance $L_{3}$ and condenser $C_{3}$ are adjusted to parallel resonance at the carrier frequency. A very high impedance is offered to this carrier, thus preventing its absorption in the modulator and generator circuits.

This trap eircuit is so designed, buwerer, that it does not suppress to any appreciable extent the audio frequency variations catused by the modulating system.
$L_{4}$ is the customary plate reactor used with this method of modulation. $E$ is a biasing


Fig. 14. Circuit Used for Telephony, 50 -watt Transmitter
potential impressed on the grid of the modulator tube to hold it on the proper portion of the characteristic curve. $T$ is a microphone transformer stepping up the voltage variations produced by the microphone $M$ and impressing them on the grid of the modulator tube. This circuit operates in the same manner as in radio transmitters so is quite generally known.

The circuit used for calling is the same: except that only the portion shown in Fig. 15 is effective. It will be noticed that control is no longer accomplished by the modu-


Fig. 15. Circuit Used for Calling, 50-watt Transmitter
lator. In its stead a contact is introduced in the grid leak circuit to control the output of the carrier generator. These contacts are operated by the three-position key at the desk stand when in the call position.

The receiver circuit used for telephony is shown schematically in Fig. 16. This is a typical tuned coupler, detector amplifier connection.
$C_{5}$ and $I_{6}$ are the primary tuning capacitance and inductance used to resonate the coupling wire to the incoming carrier frequency. Coil $L_{6}$ is coupled to this primary circuit and is also resonated to the carrier frequency by condenser $C_{6} . \quad R_{1}$ and $C_{4}$ are the usual grid leak resistance and condenser.

PR-1-13 pliotrons are used both for the detector and amplifier. The filaments are energized from a 6 -volt battery. One quarter


Fig. 16. Receiver Circuit Used for Telephony
ampere is required from the battery for each tube. The plate is supplied from a 44 -volt battery of dry cells.

The output of the detector tube is supplied to the amplifier through an intervalve transformer $T_{1}$. This tube further amplifies the signal which is reproduced by the telephone receiver through a step down transformer $T_{2}$.

The circuits are so arranged that this amplifier may be cut out if not required. Also a second stage of amplification normally used for calling only can be introduced for telephony when required.

The circuit used for calling is shown in Fig. 17. Three tubes are normally used: the first two as carrier amplifiers, the last as a rectifier. Transformer coupling is used


Fig. 17. Receiver Circuit Used for Calling
throughout. The grid of the rectifier tube is normally held at the rectification point on its characteristic by a biasing potential. The pulsating unidirectional output of the last tube is passed through a sensitive polarized relay, $R_{2}$.

The contacts of the relay close a local circuit energizing a second relay, $R_{3}$, which controls the call bell $B$.

Suitable switching arrangements are provided to make these circuit changes automatically. There are four conditions in all:

!Fig. 18. Circuit Used for Telephony, 250-watt Transmitter
Stand-by, Receive, Call and Talk. The first obtains when the receiver is on the hook, and the three-way key is in the neutral or receive position. This is the condition required for the reception of calls. Lifting the receiver from the hook starts the power apparatus and connects the equipment to receive telephony. The other two conditions have previously been described. When the communication has been completed, hanging the receiver back on the hook will automatically shut down the equipment and restore it to stand-by.

When communication and calling is desired over a greater range than 85 equivalent miles, a higher power equipment is used. The next standard size is a 250 -watt equipment, rated at 260 equivalent miles.


Fig. 19. Receiver Circuit Used in 250 -watt Equipment
Since this equipment is somewhat larger than the 50 -watt equipment, regular switchboard design is used. The transmitter and receiver are mounted on separate panel structures.

The transmitter circuit differs from that in the 50 -watt equipment in one major
respect. The carrier generator in the 50 -watt equipment is self-excited. In the 250 -watt equipment a separate 50 -watt master oscillator is used to excite the larger tube which then operates as a power amplifier. The circuit is shown in detail in Fig. 18. It will also be noticed that a fourth tube has been introduced. A PR-2-B pliotron is used to amplify the feeble roice currents set up by the microphone. This amplification is required in the higher power equipment in order that complete control of the carrier be obtained. Also a differential transformer has been substituted for the tuned trap used in the 50 -watt transmitter.

The receiver circuit used with the 250 -watt equipment is shown in Fig. 19. Three tubes are used at all times, thus somewhat simplifying the switching. Two tubes are used as carrier amplifiers and the third as a rectifier. The same combination and arrangement of tubes are used for receiving both call, signals and telephony. The only changes required when changing from one to the other are: the adjustment of the tuner, the bias potential on the grid of the rectifier and transfer of the output from the relay circuit to the telephone transformer and vice versa.

Some cases have come up where control of the carrier equipment was desired from two separate places. In order to meet this need the operator's controi equipment was designed for parallel operation from a second point. The number of extension stations may be increased to three or four, providing the total distance from any one station back to the transmitter-receiver cabinet does not exceed 250 feet.

When control is desired over much longer distances, a remote control unit must be employed. Equipment has been developed especially for this purpose. This equipment consists of suitable control and amplifying equipment to permit control of the standard carrier equipment from a point several miles from the transmitter-receiver cabinet. Four ungrounded conductors are required between the transmitter-receiver cabinet and the point of control.

Several extensions can also be added at the remote point if desired.

## Installations

Within the next few months a total of fiftyfive 50 -watt and sixteen 2.50 -watt installations will be completed. Several installations of the 50 -watt equipment have been made to date.

Fig. 20 illustrates one installation. This and another similar ofowatt equipment, although not the first installed, have been in daily operation over a $70,000-\mathrm{volt}$ line 40 miles long, for several months.

Fig. 21 shows the first commercial installation of the 50 -watt carrier equipment. This


Fig. 20. Fifty-watt Carrier Installation in Substation
equipment has been in operation with a similar one twelve miles away on a 44,000 -volt line. This installation was made during the latter part of November.

Prior to that time an experimental installation was placed in operation over a local power line. The standard 50 -watt equipments were used for communication over 27 miles of 33,000 -volt line. This circuit is composed of two sections of independent lines tied together by gap bridging apparatus at a point 17 miles from one carrier station.

Considerable experience has been obtained from the installations now in service. The engineering and operating personnel of the Various power companies have become familiar with their equipments and the operation of carrier in general. The result is that they have started to outline involved operating requirements which their experience with the simpler system has indicated can be met by more elaborate carrier systems.

## FUTURE CARRIER SYSTEMS

## Selective Ringing

Extension of the carrier systems to inchede several stations on one power transmission line has created a demand for selective ringing. The present method of code selection although satisfactory for a limited number of stations beeomes inconvenient when many stations are added. A selective ringing attachment to the existing equipments will shortly be available. The value of making this equipment in attachment form is obvious, since existing systems can be so equipped when extended to a point where code selection is undesirable.

## Duplex

Up to the present time, all commercial installations have been made for simplex operation. This was the more economical and least involved method. Much has been said regarding the inconvenience of simplex operation as compared with duplex.

The consensus of opinion obtained from the operators and dispatchers who have used the equipment is almost entirely favorable to simplex operation.

The one real objection to the method now in use for providing simplex is that the opcrator's hand is required at intervals to operate the control key between talking and listcning periods. This may be overcome by the use of a foot operated switch now available for the purpose.

The other objection raised at times appears to be of no consequence to the operators who are actually using the equipment. That is the inability to interrupt the speaker. This feature appears unnecessary when handling the usual class of communication on power transmission systems.

As is well known, the problem of duplex operation consists of preventing the local transmitter from paralyzing the local receiver to an extent that it is no longer responsive to signals from the remote transmitting station. Any number of methods have been proposed, each having its merits and demerits. Experience has indicated that, among other precautions, it is usually necessary to operate the equipment at two frequencies in order to differentiate between the local and remote signats.

The equipment required for such service, although more involved than for simplex, is not really the limiting factor.

Considering the problem broadly, the useful frequency range for carrier trans-
mission is probably between 12,000 and 100,000 eyeles. Certain portions of this range are now in use for high-power radio telegraph and existing carrier systems. If the remaining ranges were all available for duplexing one power company's systems the


Fig. 21. First Commercial Installation of 50 -watt Carrier Equipment
problem would be solved. This, however, is not the case.

The ever increasing trend of power companies to interconnect their systems changes the aspect of the situation considerably. Several instances have come up where four and five interconnected companies are or shortly will be equipped with carrier communication systems, each to operate without interference to the others.

This is just the beginning of the interconnection of power systems. In order to
provide for the conditions which will have to be met on the mammoth networks of the future, it is necessary that the frequency bands be very carefully chosen and assigned. The groups of four and five interconnected systems now under consideration require a considerable portion of the arailable frequency range for simplex operation. Any attempt to employ duplex by means of frequency selection would further reduce
the range available for extension on the (amsmunication system.

The frequency range is sufficiently brat if the individual bands are properly assigned and are not used unnecessarily. For theses reasons, it is believed that the advantages of duplex over simplex in the majority of cases is not sufficient to warrant jeopardizing the expected usefulness of carrier communication to the power companies

# Frequency Converter Ties Between Large Power Systems 

By J. WV. Dodge<br>Lighting Exgneering Department, General Electric Company


#### Abstract

With the adrent of the "superpower zone" some means must be used of making powcr of various frequencies available over large areas; this lends added importance to the various types of frequency changers. The author describes the rarious types of frequency changers, discusses their relative merits and their fields of application.-Editor.


The expansion of power systems throughout the country is leading to the tying together of a great many of these systems, forming large interconnected systems similar to the proposed "Superpower System" covering the territory from Boston to Washington. Due to the variety of frequencies used, it is often desirable to tie two systems of different frequencies together, and this has led to the development of several types of frequency converters to meet special requirements.

Each type of frequency converter has a rather definite and well defined field of application, and it is the purpose of the present article to describe the available types of frequency converters and their application to power systems.

## Types of Frequency Converters

For convenience let us use the following terms in discussion of different types of sets:

1. A synchronous set we will consider as consisting of a synchronous motor driving a synchronous generator.

[^40]2. An induction motor sct we will consider as an induction motor driving a synchronous generator.
3. A speed regulating induction motor set we will consider as a wound rotor induction motor with Scherbius speed control, driving a synchronous generator.
4. An induction-synchronous set will consist of an induction type frequency converter direct connected to a synchronous machine. In other words, it is a wound rotor induction machine operated at a definite slip (determined by the speed of the synchronous machine) so that the higher frequency system is connected to the stator circuit, and the lower frequency system is connected to the rotor circuit of the induction machine and also to the synchronous machine. This type of set is entirely synchronous in operation, although it makes use of an induction machine.
5. A synchronous conierter type set will consist of two synchronous converters operated in series, converting a-c. to d-c. and then back to a-c. of another frequency.

Any of the above mentioned sets are reversible, that is, they may be used for power flow in either direction. Parallel operation* will not be discussed, as it has little bearing on the subject at hand.

Synchronous Sets
The frequency conterter, consisting of two syonchronous machines, is the most eommon and familiar lype for large power use. It gives a power tie betweon the two systems which it conmeets and forms a rigid


Fig. 1. A $10,000-\mathrm{kw}$. 450 -r.p.m. Synchronous Type Frequency Converter Consisting of a $12,000-\mathrm{kv}-\mathrm{a} .30$-cycle Machine Direct Connected to a $\mathbf{1 6 , 0 0 0 - k v - a}$. 60 -cycle Machine. A $60-\mathrm{kw}$. direct-connected exciter is provided for each machine
frequency tic. The ratio of frequencies of the two systems must remain the same as long as this type of set comects the two together. Any variation in this ratio will overload the set and cause it to pull out of step. Synchronous machines of this class are normally designed for at least 50 per cent momentary overload before the pull out point is reached. This means that momentary fluctuation in frequency ratio may occur and still maintain synchronous operation of the set, provided this fluctuation in frequency does not load the set above the pull out point,


Fig. 2. A $5000-\mathrm{kw}$. 300 -r.p.m. Synchronous Frequency Converter, 25 to 60 Cycles, with Direct-connected Exciters
and provided the frequency change is of very short duration.
Synchronous sets may be provided with low resistance amortisseur windings which

[^41]will make them self-synchronizing, so that in the event of an overload which pulls the set out of step, the machine which is operating as a motor will pull back into synchronism as soon as the load is sufficiently decreased (and with excitation removed). This feature is covered in detail by another article in this issue of the Review, by Mr. O. E. Shirley.

The synchronous frequency converter does not form a voltage tie between systems. The only effect upon the voltage of cither system is that of adding one gencrator (or synchronous motor) of the rating of the set, to each sustem. It may help to maintain voltage by the addition of a certain amount of $k v-a$., but gives no voltage tie between systems. Figs. 1, 2 and 3 show synchronous sets suitable. for use on large power systems.

## Induction Motor Sets

Sets consisting of an induction motor (either squirrel cage or wound rotor) driving


Fig. 3. A 2000-kw. 750-r.p.m. Synchronous Frequency Converter, 25 to $62 \frac{1}{2}$ Cycles, Showing Semi-enclosed Construction and Stator Shifting Device
a synchronous generator are very similar in operation to the synchronous type of set, except that the frequency ratio varies slightly with load on the set, due to the slip of the induction motor. This does not allow the use of exactly synchronous speed on both systems, and this fact, together with the lower power-factor and efficiency of the induction, as compared with synchronous, sets leads to the choice of the latter in the great majority of cases.

## Speed Regulating Induction Motor Sets

The Scherbius type of speed control for operating induction motors* above and below synchronism has been used for several years where large variable speed induction motors are required. This method of speed control has recently been considered for frequency converters in order to obtain a
set which can be operated between two systems where the frequency ratio may vary between such wide limits as to make the operation of a synchronous set impractical.

The principal elements and connections of such a set are shown in Fig. 4. The equipment consists of the main frequency converter set and an auxiliary speed regulating set. The frequency converter is made up of an ordinary synchronous generator and its exciter, a wound rotor induction motor, and an ohmic drop exciter. The speed regulating set consists of a squirrel cage induction motor and a polyphase commutator motor with shunt field excitation, called the regulating motor. This regulating motor is connected across the slip rings of the main induction motor to be controlled, its counter


Fig. 4. Simplified Diagram of Connections for Speedregulating Induction-motor Type Frequency Converter
electromotive force opposing the voltage across the slip rings. By varying the excitation of the regulating motor, the slip ring voltage opposing its counter electromotive force may be varied, thereby changing the speed of the main motor. Because of the shunt excitation of the regulating motor, its counter electromotive force, and therefore the speed of the main motor, remains practically constant throughout the entire range of loads for any given setting of the control.

The ohmic drop exciter mentioned above is a device mounted on the shaft of the main set and used as an automatic source of constant voltage at exact slip ring frequency for the control of the shunt field on the regulating motor. This is shown in Figs. 5 and 6 mounted on the end of the induction motor shaft, and consists of a single primary winding connected to a commutator exactly similar to a di-c. armature, and has collector rings tapped off at 120
electrical deg. intervals (for 3 -phase). The secondary is a smooth laminated ring without windings. The theory of operation is explained in the article referred to at the bottom of page 436 , by Mr. J. I. Hull. Figy. 7 shows a typical speed regulating set.


Fig. 5. Ohmic Drop Exciter Mounted on the Shaft of a 2500-h.p. 240-r.p.m. Induction Motor
For motor operation below synchronism or induction-generator operation above synchronism the energy which is taken from the slip rings drives the regulating set causing the squirrel cage induction motor to act as an induction generator and return this energy to the a-c. line, so that the slip energy of the secondary circuit is all returned to the primary line, except for a small loss in putting this power through the speed regulating


Fig. 6. 2500-h.p. 240 -r.p.m. Wound-rotor Induction Motor with Ohmic Drop Exciter
motor-generator set. With the main motor operating as a motor above synchronism or as a generator below synchronism the power flow through the regulating set is reversed.

The variation in speed required for a frequency converter is small, probably never
exceeding of per cent above and below synchronous speed, as mo large power system womld operate more than 5 per cent above or below normal frequency.

The rating of the regulating set depends upon the speed range required. If $S$ (max), $S$ min), and $S(\mathrm{~s})$ represent the maximum, minimum, and synchronous speeds of the main motor, and $K w(s)$ be the kw. output of the frequency converter at $S(s)$, then the rating of the regulating set required will be approximately as follows [if the synchronous speed is half way between $S(\max )$ and $S(\min )]$ $K w($ reg. set $)=1 / 2 K w(\mathrm{~s}) \times \frac{S(\max )-S(\min )}{S(\mathrm{~s})}$

As an example, consider a $10,000-\mathrm{kw}$., $300-\mathrm{r} . \mathrm{p} . \mathrm{m}$. frequency converter with a speed range of 3 per cent above and below synchronism. The approximate size of the regulating set required will be:

$$
\begin{aligned}
K w(\text { reg. set }) & =1 / 2 \times 10,000 \frac{309-291}{300} \\
& =300 \mathrm{kw} .
\end{aligned}
$$

This shows that the regulating set is comparatively a very small unit where small regulation is required, and therefore, would not greatly increase the cost of the frequency converter.

Speed control on the main unit is obtained by adjusting the excitation of the regulating motor shunt field. This is accomplished in a very simple way, and gives a smooth change in speed over the entire range, and does not require any contactor panels or other additional control equipment, other than that described above.

The power-factor of the main induction motor can be controlled by the regulating set so that it is rarely necessary to operate at a lagging power-factor. The equipment would normally be designed to give approximately unity power-factor at synchronous speed and full load. The power-factor is not adjustable at synchronous speed, and varies somewhat with changes in load. When operating above or below synchronism, the power-factor is adjustable and varies with the load on the motor, similar to the operation of a synchronous motor.

It is evident that the principal objections to the induction motor drive have been removed by the addition of the speed regulating set, since it allows the operation of both connected systems at exactly synchronous speed, and the power-factor of the induction machine has been increased to unity or better for the majority of operating conditions.

In addition to correcting the power-factor and speed, it gives a speed control which adds the following distinctly new features:

1. It allows the set to be operated between systems of varying frequency.
2. It allows the control of load on the set by regulating the slip on the induction machine, that is, control of load at the set rather than at the governors of the prime movers on the two systems connected by the set.

## Induction-synchronous Sets

For convenience, let us consider an induc-tion-synchronous type of frequency converter for connecting between a $25-$ and a $60-$ cyele system. Fig. 8 is a simplified diagram of such a set, consisting of:

1. A wound rotor induction motor having a 60 -cycle stator and a 2 .5-cycle rotor (induction frequency converter).


Fig. 7. Double-range Scherbius Speed-regulating Set for Use with a 2500-h.p. Induction Motor
2. A $25-\mathrm{cyc}$ le synchronous generator.
3. A direct-connected exciter for exciting the synchronous generator.
4. An induction starting motor.
3. A transformer for stepping up the voltage of the induction motor rotor to 25 -cycle line voltage.
A transformer is usually required between the 25 -cycle bus and the induction motor rotor because it is difficult to build a high voltage rotor for this machine.

The synchronous machine is a 10-pole, 25 -cycle, $300-$ r.p.m. generator. The $60 / 25-$ cycle induction unit is wound for 14 poles, which at 60 cycles would have a synchronous speed of 514 r.p.m. By holding the rotor speed down to 300 r.p.m. with the synchronous generator, we obtain a slip of 214 r.p.m. in the induction machine, which gives 25 cycles at the collector rings of the rotor.

The stator of the induction machine is connected to the 60 -cycle line, and the rotor
of the induction machine and the stator of the synchronous machine are both connected to the 25 -cycle line as shown in Pig. 8 .

With this type of a set, consider the 60cycle machine as a motor and the set generating 25 -cycle power. The induction machine will then deliver power both mechanically through the shaft to the 25 -cycle generator and electrically through the collector rings to the 25 -cycle line.

Neglecting losses, this power will be divided as follows:

1. Power through the shaft $=\frac{300}{514} \times$ (the $60-$ cycle input to the stator.)


Fig. 8. Simplified Diagram of Connections for an Inductionsynchronous Type Frequency Converter
2. The electrical power output through the collector rings $=\frac{214}{514} \times$ (the 60-cycle input to the stator).
Applying this to a set of $35,000-\mathrm{kr}$. rating, we have:
Mechanical power output through the shaft

$$
=\frac{300}{514} \times 35,000=20,400 \mathrm{kw} .
$$

Electrical power output through the collector rings $=\frac{214}{514} \times 35,000=14,600 \mathrm{kw}$.

The induction machine furnishes an electromagnetic tie between the 25 - and 60 -cycle systems, similar to a transformer tie between two parts of a system of one frequency. In other words, this machine forms a voltage tie between systems in addition to being a frequency and power tie, and any variation or disturbances of voltage on one system will be transmitted to the other system through this tie in a manner similar to that obtained through a transformer tie.

The effectiveness of this voltage tie is dependent upon the reactance oi the circuit
through the induction machine between the two systems. It is also dependent upen the ratio of frequencies of the $t w o$ systems

If both systems were of the same frequency, the induction motor rotor would be stationary and straight transformer relations would exist. However, if the frequency of the rotor circuit is reduced, the rotor speed increases proportionally and the induced rotor voltage (and therefore the rotor $\mathrm{kv}-\mathrm{a}$.) is proportionally decreased. That is, with a $60 / 25$-cycle machine with $35,000-\mathrm{kr}-\mathrm{a}$. input to the stator, the equivalent output of the rotor would be $\frac{2.5}{60} \times 35,000=14,600 \mathrm{kv}-\mathrm{a}$.

A $35,000-\mathrm{kw}$. frequency converter has a reactance of approximately 17 per cent between the two systems to which it would be connected. This reactance is based on the rating of the circuits, that is, 35,000 $\mathrm{kv}-\mathrm{a}$. on the 60 -cycle side and $14,600 \mathrm{kv}-\mathrm{a}$. on the 25 -cycle side. If reactors are used between the machines and the busses, as shown in Fig. 8, this reactance between systems is increased.

With this in mind, let us consider the effect produced with this induction machine tying two systems together when short circuit conditions occur on either system. If a short circuit occurred on the 60 -cycle bus and the 25 -cycle bus voltage was maintained, a flow of current would occur from the 25 -cycle system to the 60 -cycle system through the induction machine. Assuming the reactance to be 22 per cent between busses, as shown in Fig. S, the kv-a. input to the 60 -cycle system would be approximately $\frac{35,000}{0.22}=160,000 \mathrm{kv}-\mathrm{a}$. at short circuit. The kr-a. taken from the 2.j-cycle system under this condition would be $\frac{14,600}{0.22}$ $=66,000 \mathrm{kr}-\mathrm{a}$. (neglecting input to the synchronous machine, which will be comparatively small, being only the power component).

Now consider a short circuit on the 2.5cycle system with 60 -cycle bus roltage maintained. The kv-a. input to the $25-$ cycle system from the induction motor rotor would then be $66,000 \mathrm{kv}-\mathrm{a}$. and the input from the 25 -cycle synchronous machine would be $5 \times 25,000=125,000 \mathrm{kv}-\mathrm{a}$. (the reactance of the 2.5 -cycle machine being approximately 20 per cent). This makes a total of 191.000 kT -a input to the 2.5 -crele system on short circuit. The kr-a. taken
from the 60 -cycle hus would be $\frac{35,000}{0.22}=$ $160,000 \mathrm{kr}-\mathrm{a}$.

From the above, it is plain that such a set will tend to maintain voltage on one system at the expense of the other whenever trouble occurs which reduces voltage on either system. This may be very advantageous in some large systems where it is important to maintain service at a reduced voltage during trouble periods, rather than to drop off entirely. On the other hand, this type of set spreads the effect of the trouble over the two systems, pulling down voltage on both when trouble occurs on either one. In this respect, the induction set differs from a synchronous set.
synchronous machine for about 0.85 p -f. lagging load (as a generator) and exciting the induction machine from the 25 -cycle machine. The power-factor of the 60 -cycle side of the set can be adjusted by changing the ratio of the transformer in the 25 -cycle rotor circuit of the induction machine and the power-factor of the 25 -cycle side can be controlled by adjusting the field excitation of the synchronous machine.

In gencral, it is desirable to use current limiting reactors in the lines to the two systems, as it increases the synchronizing power between the two machines of the set, but, as previously stated, the effectiveness of the voltage tie between systems depends upon keeping this reactance down to a minimum. This requires a compromise.

TABLE I
INDUCTION-SYNCHRONOUS FREQUENCY CONVERTERS

| cycles |  | poles |  | R. P. M. |  |  | comparative kw. rating req'd |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Motor (Ind.) | $\begin{gathered} \text { Gen. } \\ (\text { Syn. }) \end{gathered}$ | Motor <br> (Ind.) | $\begin{gathered} \text { Gren. } \\ \text { (Syn.) } \end{gathered}$ | Shaft <br> Speed | Motor Slip | Syn. of Motor of Motor | Induction Motor Stator Per Cent | Induction Motor Rotor Per Cent |  |
| 60 | 25 | 14 | 10 | 300 | 214 | 514 | 100 | 41.7 | 58.3 |
| $621 / 2$ | 25 | 6 | 4 | 750 | 500 | 1250 | 100 | 40 | 60 |
| 6212 | 25 | 12 | 8 | 375 | 250 | 625 | 100 | 40 | 60 |
| 60 | 40 | 2 | 4 | 1200 | 2400 | 3600 | 100 | $662 / 3$ | $331 / 3$ |
| 60 | 40 | 4 | 8 | 600 | 1200 | 1800 | 100 | $662 / 3$ | $331 / 3$ |
| 60 | 40 | 6 | 12 | 400 | 800 | 1200 | 100 | $662 / 3$ | $331 / 3$ |
| 50 | 25 | 4 | 4 | 750 | 750 | 1500 | 100 | 50 | 50 |
| 50 | 25 | 8 | 8 | 375 | 375 | 750 | 100 | 50 | 50 |
| 60 | $331 / 3$ | 8 | 10 | 400 | 500 | 900 | 100 | 55.6 | 44.4 |
| 60 | 30 | 6 | 6 | 600 | 600 | 1200 | 100 | 50 | 50 |
| 60 | 30 | 8 | 8 | 450 | 450 | 900 | 100 | 50 | 50 |
| 60 | 50 | 4 | 20 | 300 | 1500 | 1800 | 100 | $831 / 3$ | 162/3 |
| 60 | 50 | 2 | 10 | 600 | 3000 | 3600 | 100 | $831 / 3$ | $162 / 3$ |

Table I shows some of the common combinations of frequencies, and the number of poles, speed, and comparative rating of the different parts of the sets, which nay be used for induction-synchronous frequency converters. (Ratings given do not take into account the efficiency or power-factor of the set.)

In case of a short circuit on either side of a synchronous set, the unit on the affected system simply acts as any synchronous generator, adding a certain amount of kv-a. to the system. The other system is not affected, except that the load of the set is dropped. In other words, there is no wattless $\mathrm{kv}-\mathrm{a}$. exchange between the two systems with a synchronous set, and there is an exchange of wattless $\mathrm{kv}-\mathrm{a}$. through the induction set. The need for this kind of a tie between systems should be the primary reason for using the induction-synchronous type of set in preference to a synchronous set.

The induction-synchronous set is normally designed for $1.0 \mathrm{p}-\mathrm{f}$. input and output at full load with power flowing in either direction. This is accomplished by designing the

Table I gives some of the combinations of poles which may be used for inductionsynchronous sets, also the speeds and comparative sizes of the different parts of the sets. It will be noted that the larger the frequency ratio, the nearer the ratings of the motor and generator come together, while for small frequency ratios the comparative size of the synchronous machine becomes smaller. For instance, with the $60 / 25-$ cycle ratio, the synchronous machine is 58.3 per cent of the total rating of the set while with the $60 / 50$-cycle ratio its rating becomes only $16 \frac{2}{3}$ per cent of the total. The actual kv-a. ratings of machines designed for such sets would vary somewhat from the figures given in Table I, due to consideration of efficiency (or losses) and
power-factor. If a transformer is used for the rotor circuit of the induction unit, its kv-a. rating would be the same as that of the rotor.

The synchronous speed of the induction machine becomes very high, as compared with the normal speed of the set, when a close frequency ratio is used, such as $50 / 60$ cycles. This makes it impractical to design a set to stand a runaway speed equal to the synchronous speed of the induction unit, and since there is danger of the set reaching this high speed if the lower frequency circuit becomes disconnected from the collector of the induction machine, it is very important that reliable over-speed protection be provided for opening the a-c. supply circuit to the induction unit stator in case of over speed. This feature is not so important for the sets in which the higher frequency machine has a lower synchronous speed, but such protection should always be provided on this type of set.

## Synchronous Converter Type

The use of synchronous converters operating in series for frequency conversion gives a tie between systems which is extremely flexible and in some respects is very similar to both the induction motor set with Scherbius speed control, and to the inductionsynchronous type set. It allows the operation of the two systems through a wide range of frequency ratio, allows control of load at the converter, and also gives a voltage tie between systems. This type of conversion apparatus, however, has not received very much favorable consideration for commercial purposes because the cost and maintenance charges are very much in excess of the cost of other types of frequency converters, and the efficiency of such equipment is usually found to be from one to three (or more) per cent below that of synchronous type frequency converters.

## Field of Application for Various Types of Frequency Converters

The synchronous type of set is properly applied as a tie between power systems where a power and frequency tie are necessary and where no voltage tie is desired. It is limited to use between systems operating at constant ratios of frequency, and the load over such a set must be controlled by adjustment of governors on the prime movers of the connected systems. It has the advantage of simplicity of construction and operation, over all other types of sets. It is inherently
adaptable to rugged and simple design, with a minimum of auxiliary parts. It involvers no new or untried types of construction. Its efficiency is probably as good or better than any other type of set (for any given rating), it can be designed to give any desired power-factor on either machine, and the power-factor is easily adjustable by field control. Either machine may be used as a synchronous condenser on its system, when the set is not in use as a tie between the two systems.

The induction motor set is rather infrequently used as a tie between large power systems due to its poor efficiency and powerfactor as compared with a synchronous set. It also has the handicap of frequency variation with the load, and of course, the induction motor can not be utilized as a synchronous condenser when the set is not in use as a tie.

The speed regulating induction motor type frequency converter, however, adds a unique operating advantage. This is the characteristic of adjustable frequency ratio on the set, to compensate for varying conditions on the systems connected by the set and the advantage of control of power flow through the set, at the set itself.

An induction motor has a certain inherent speed regulation. In other words, the slip changes with changes in load on the motor. This very important difference between an induction and a synchronous motor makes the induction motor set flexible to slight changes in frequency, simply changing the load on the set where a syinchronous set would be forced out of step. The speed regulating set makes it possible to bring the load back to normal after such changes in frequency.

In the past it has been considered impractical to tie certain systems together with synchronous sets because the frequency of one or both systems was so unstable as to cause a synchronous set of reasonable size to trip out frequently on overload, due to these changes in frequency. Such systems are usually those covering large areas geographically and having various size generating plants located at widely separated points, tied together by high-voltage transmission lines. They are mostly hydro-electric plants, and on such systems the voltage and frequency regulation are necessarily large compared with systems consisting of large steamelectric generating plants concentrated in small areas, where very close voltage and frequency regulation are obtained.

It is in tying the former type of system to a system of different frequency that demands a speed regulating type of set. As the frequency ratio varies between systems, the slip of the induction motor can be varied to hohl practically constant load on the set. If the frequency changes are slow this adjustment could be manual, while on systems where frequency changes are rapid, an automatic control woukd be necessary. This could be operated from a contact-making watmeter arranged to hold constant load on the set. Any changes in load on the set would operate the contact-making wattmeter which in turn would operate the control of the shunt excitation of the speed regulating motor of the Scherbius control set, and raise or lower the speed of the main set as the load demanded. This type of set is, therefore, well adapted to automatic or semi-automatic control.

On systems covering large areas it should be quite an advantage to have the control of load on the frequency converter located at the set. Otherwise the system operator must keep informed as to the load on the set, and instruct his various station operators to change their governor settings to adjust for changes in load on the set.

The speed regulating type of frequency converter has the disadvantage of being more complicated than the synchronous sets, and will usually be found to have a little lower efficiency. The power-factor can usually be maintained at unity or better on the induction machine so that the synchronous motor has little advantage in this respect.

While the frequency converter is a new field for the Scherbius type of control, a great deal of experience has been obtained on this control for steel mill main roll drives where the fitness for the work and the thorough reliability of the Scherbius system of control have been demonstrated by years of very successful operation under the most extreme speed and load conditions.

## Need for Voltage Tie Between Systems

The majority of our large metropolitan districts in this country are each served by systems of two or more frequencies. Where Edison systems (d-c.) are used and supplied from the a-c. systems through conversion apparatus, the early practice was in many cases to use 25 -cycle a-c. power, due to the superior performance of 25 -cycle synchronous converters. More recently, the tendency has been to increase the 60 -cycle
system in preference to the 2.5 -cycle, because with the conversion equipment now available the advantage of the lower frequency no longer exists.

We therefore find large cities supplied by both 25 - and 60 -cycle systems covering the same territory, and feeding the same general load. Sooner or later it usually becomes very desirable, for best economy, to use synchronous converters of both frequencies in the same substations operating on the same d-c. bus, as shown in Fig. 9.

This has been tried in several cases, and it was found difficult to operate the 25- and 60 -cycle rotary converters in parallel due to different voltage regulation on the two systems. It was also found that at times of voltage disturbance (such as short circuits) on one system, the converters on that system would invert and trip out on overspeed, with a heavy flow of current from the other a-c. system through the converters and $\mathrm{d}-\mathrm{c}$. bus to the a-c. system where the disturbance occurs. This usually results in severe burning of the brush gear and commutator of the inverted converters.

Similar experience has resulted from the parallel operation of rotary converters fed from separate isolated generating stations of the same frequency. This trouble was largely overcome by the use of suitable cable ties between the two a-c. generating stations of like frequency. These cables tend to equalize the voltage between the sources of a-c. supply and prevent the damage to rotary converters in case they invert at times of short circuit on the a-c. system.

The induction-synchronous type of frequency converter provides a tie between systems of different frequency which simulates the cable tie between stations of the same frequency as mentioned above. As explained earlier in this article, this type of set provides a voltage tie in addition to the frequency and power tie. The inductionsynchronous type of set is being developed particularly for use in connection with Edison systems where it will make practical the operation of 25 - and 60 -cycle converters in parallel.

These systems are in many cases of very large capacity, and in order to provide a suitable link, sets of large size are necessary. Modern large city systems are using steam turbine generators of from $20,000-\mathrm{kw}$. , to $50,000-\mathrm{kw}$. sizes, and it is considered good practice to use a frequency converter, for such a tie, of the same size as the largest
generating units. This allows a reduction in standby generating equipment. It is not good practice to operate with a standby generating capacity of less than that of the largest generator on the system. This means that with 25 - and 60 -cycle systems operating separately, each using units of $35,000-\mathrm{kw}$. capacity, there should be one generator unit of this size on each system for standby service. If these two systems are tied together by a frequency converter of $35,000-\mathrm{kw}$. capacity, one standby generator for the two systems would be sufficient, since it could be used to supply load on either system in case of a generator or turbine failure.


Fig. 9. Diagram Showing the Application of an Inductionsynchronous Type Frequency Converter to a Typical Edison System Having Generating Systems of Both 25 and 60 Cycles

The cost of a frequency converter of this size would be approximately 50 to 60 per cent of the cost of a turbine alternator set. This of course neglects the boiler capacity and other auxiliary equipment necessary with the steam turbine.

The efficiency of a $35,000-\mathrm{kw}$. frequency converter of either the synchronous or the induction-synchronous type would be approximately 94 to 95 per cent at full load.

Many large urban systems are now spending large sums of money to obtain continuity of service on their a-c. systems, as even a rery short interruption must be avoided if possible. It is preferable to take a dip in voltage at a time of trouble on the system rather than to let the voltage fall to zero and this is usually possible if the system is laid out
with this in mind, making proper use of current limiting reactors. The use of om induction-synchronous frequency converter may be of considerable aid in holding (up) voltage on interconnected systems of different frequencies, as it forms a voltage tie: between the two, and will tend to hold up voltage on one system by feeding in $\mathrm{kv}-\mathrm{a}$. from the other during periods of voltage disturbance.

The cost of an induction-synchronous type set for $60 / 25$-cycle systems (including the transformer for the 25 -cycle rotor circuit) is about the same as the cost of a synchronous set. For systems where the frequencies are more nearly the same, the size of the synchronous machine becomes smaller in proportion to the rating of the set and, therefore, the cost of such sets should be somewhat less than for a synchronous set. The induc-tion-synchronous set involves a somewhat more complicated rotor construction than a synchronous machine.

It is possible to utilize the set as a condenser for either system during times of light load on the set. If reactive $\mathrm{kv}-\mathrm{a}$. is required on the low frequency system, simply use the synchronous unit as a condenser. If the higher frequency system requires reactive kv-a., it may be obtained through the induction machine from the synchronous unit, or from the lower frequency system. The peculiar thing about this is that you can take out from the induction machine more kv-a. than you put in. Consider a $60 / 25$-cycle set, with the induction machine operating at 25 -cycle slip. For each $25-\mathrm{kr}-\mathrm{a}$. input to the rotor, you obtain $60-\mathrm{kv}-\mathrm{a}$. output from the stator (neglecting impedance drop in the machine) so that it is possible to obtain considerable reactive $\mathrm{kv}-\mathrm{a}$. at 60 cycles, with a comparatively small amount taken from the $2 \overline{5}$-cycle machine or line. This flow of reactive kv-a. through the induction unit is controlled by the ratio of the transformer in the rotor circuit, or by a change of 25 - or 60 -cycle bus voltage. It is evident that the usefulness of the inductionsynchronous type of set is nearly as great as a synchronous set as a source of synchronous condenser capacity, during times of light load on the set.

This type of set adds the voltage tie between systems, which is considered absolutely essential in certain cases, such as the problem involving parallel operation of synchronous converters of two frequencies, which was outlined above.

Frequency converters may now be obtained in practically any size required, as their design and construction involves no greater difficulties than are met in the building of any large generating equipment. Sets of $35,000-\mathrm{kw}$. capacity are now in process of


Fig. 10. A $12,000-\mathrm{kw}$. 500 -r.p.m. 25/50-cycle Frequency Converter with Direct Connected Exciters and Stator Shifting Device
construction and there is no reason why such sets should not be built of larger capacities to keep pace with the requirements of large power systems.


Fig. 11. Rotor of a $15,000-\mathrm{kv}-\mathrm{a}$. 500 -r.p.m. 50 -cycle Generator

## Mechanical Features

It is the general practice to build large sets, such as $10,000 \mathrm{kv}-\mathrm{a}$. and above, with four bearings and to provide sheet-steel air deflectors on the machines, making them either semi or totally enclosed. Figs. 1 and 10 show the arrangement of bearings and enclosing features in common use on large
synchronous sets. Figs. 11 and 12 show the rotor construction used on large synchronous machines. The simplicity and ruggedness of construction used are self-evident.

## Accessories

In addition to the two main units of a frequency converter, it is often found desirable to add exciters, induction starting motors, phase (stator) shifting devices for paralleling scts, and forced oil lubricating systems for use during starting.

It is very desirable to have an individual exciter for each synchronous machine, as this allows power-factor control by exciter ficld rhcostat, and eliminates the necessity for a main generator field rheostat. By the use of induction starting motors and high pressure lubrication of main bearings during starting, the kv-a. taken from the line for


Fig. 12. Rotor of a $10,000-\mathrm{kv}-\mathrm{a}$. 720 -r.p.m. 60 -cycle Generator
starting may be reduced to $1 / 3$ or $1 / 2$ that required for starting one of the synchronous machines with a starting compensator.

If one of the main units is a wound rotor induction machine it is possible to use this machine for starting the set (with a suitable resistor in the secondary circuit) and very good starting characteristics are obtained in this way.

If sets are to operate in parallel it is a great advantage to have a motor-operated phase shifting device on one machine of each set, as this allows the absolute control of load division between sets, and enables the operator to add or remove sets from the line without any sudden olts to the system (other than starting kv-a. required). This phase shifting device is especially desirable on large sets, and the cost is a comparatively small item.

# Development of Automatic Control 

By H. C. Hoyt<br>Lighting Department, General Electric Company


#### Abstract

The author writes yery interestingly on the development of automatic control for electric stations. There is a lot of information in this contribution which has not appeared in other articles on the subject. A short review of this nature will be profitable reading for many of our subscribers.-Editor.


There is possibly no more striking illustration of the emancipation of the electrical industry from purely manual operation, than in the contrast between past and present central station boiler rooms. When one recalls the inferno of the dark, narrow, coal cluttered firing aisles of a few years ago and the crews of half stripped sweating fircmen who labored there in a blackness, more intensified than relieved by the glare of open furnace doors, and compares that scene with the light, well ventilated stations of today in which human labor has been all but eliminated, one can appreciate the benefits of automatic appliances.

While less spectacular in appearance, the change resulting from automatic control of substations and hydro-electric generating stations, is, in reality, far more complete. Regular shifts of operators-water tenders, oilers, etc.-are still required in even the most modern boiler room, while the automatic station normally needs only an occasional inspection for cleaning and adjustment.

Labor saving devices are always popular. Undoubtedly a number of operators had developed more or less ingenious arrangements amounting to automatic control of portions of electrical equipment for their own convenience, before the development was seriously undertaken by the manufacturers of electrical apparatus. Little record of these individual experiments is available, so that any history of the development of automatic equipment must, of necessity, be confined to published data of the larger manufacturing companies.

So far as these records go, the beginning of automatic operation is found in the Rowena Street Station of the Detroit Edison Company where, in 1912, was installed a remotely controlled automatically operated synchronous converter for serving a lighting and power load. There is little doubt that this was the first development in which the attempt at automatic control of a complete electrical unit, as distinguished from one of the various functions of this unit, was undertaken.

While this automatic equipment at Detroit proved entirely successful and was followed by additional units for the same Company,
the next installation of automatic equipment in point of time, was for very different service and consisted of the automatic control for a railway type converter on the lines of the Elgin and Belvedere Railroad at Union, Ill., in 1914. This installation should perhaps be classed as the first completely automatic installation in the sense that it was started, connected to the line and shut down entirely without assistance from an operator. This equipment followed the plan, which has subsequently become almost universal practice for this service, of starting the converter on low voltage, connecting it to the line and shutting down on underload. So successful was the operation of this installation, that automatic equipment was rapidly purchased for all the other substations on the system, and shortly its application was started on the lines of the Des Moines (Iowa) City Railway Company.

The inherent adrantages of the automatic equipment to railway systems, and particularly to interurban lines on which the service is rather infrequent, led to a very rapid expansion of the application to this particular class of service. Here the success of the automatic control was so well proven and the various items in this equipment so fully developed, that the expansion of this control to other types of apparatus was the natural and logical result.

In 1917 automatic control for a $3000-\mathrm{kv}-\mathrm{a}$. sunchronous condenser was installed at the Hazel Green Substation of the Interstate Light \& Power Company, for the improvement of power-factor and regulation on a line serving the lead mines of this district. This equipment performed so successfully during the years of unusual activities in the lead mining industry, that it seems strange the demand for automatic control of synchronous condensers, since this initial installation, has not been greater. Inherently the control of this equipment is of the most simple type and the ability to locate condensers at the load end of transmission lines, where often there is no occasion for installation of other substation equipment requiring an attendant, would seem to make this class
of service an icheal one for automatic operation.

It is believel the first hyrlro-electric station tostart and beswitched on the line, due entirely to the load requirements of the system, was the one placed in operation by the Iowa Railway


Fig. 1. Automatic Control Equipment for Waterwheel-driven Generator. The generating equipment transmits its power to a mill and is started by energizing the transmission line through the closing of a manually operated switch at the mill. Generator oil circuit breaker of the automatic solenoid operated type is shown mounted on separate channel iron framework.

Light and Power Company at Cedar Rapids, Iowa, in 1917. This equipment has been so fully described and reviewed in the technical press that mention of it only is sufficient at this time.

The installation at Cedar Rapids was quickly followed by others for a similar class of service, notably among the earlier developments being that of the Blue River Power Company at Seward, Neb., and Station No. 2 of the Ontario (California) Power Company. An interesting feature in connection with the Blue River Development is that, so far as is known, this was the first instance in which a drop in frequency on the system was used as the indication for this station to automatically come into service.

Probably the most notable example of applying automatic control to city lighting service, is that of the Kansas City Power \& Light Company. Due to a re-organization, the lighting service of the entire city was changed from a frequency of 25 to 60 cycles. This necessitated the furnishing of new
conversion equipment throughout for the Edison 3-wire district in the business section of the city. It is most unusual for such a complete reconstruction of an entire Edison System to be undertaken, and before proceeding with final plans, an exhaustive study was undertaken as to the best method to adopt. It was finally decided that for reasons of cconomy and reliability of service, a plurality of automatic substations scattered throughout the district would best meet the requirements. A total of ten synchronous converters arranged in five substations of two units each were therefore ordered. These stations are interconnected through the Edison network and the automatic equipment is so arranged that one unit in any particular station will start in response to the load demand in its immediate neighborhood, followed by the second unit when needed.

Aside from the reliability secured through the prompt and positive operation of this automatic equipment, ability to pick up load after an entire shut-down of the Edison System is furnished by the use of watercooled cushioning resistors which are automatically placed in series with the load so as to limit the output of each individual converter to its normal full load current, until


Fig. 2. Motor-generator Set Consisting of $1875-\mathrm{kw}$. 250 -volt Generator, 13,200 -volt Synchronous Motor, and Directconnected Exciter for Separate Excitation of Motor and Generator Fields. Solenoid operated air circuit breaker for short circuiting generator differential field winding is shown mounted on a separate framework. The set supplies power to an Edison three-wire network.
such a time as the system voltage can be raised to approximately normal. Cushioning resistors of the air-cooled type had been used in railway service for a considerable time prior to this, but it is believed Kansas City was the first installation of water-cooled
resistors having sufficient capacity to enable the converters to function successfully under abnormal conditions 11 p to the point where the heating of the converter required its shutdown.
Application of antomatic control to motorgenerator sets of both symchronous and induction types, naturally followed the successful operation of the converter and synchronous condenser equipment. Adoption of synchronous motor-generator sets especially has come into favor, not only because of the greater stability of this motor, enabling it to "hang-on" during minor fluctuations in the a-c. supply which would trip out a converter, but also becanse of the possibilities of power-factor correction inherent in this type of motor.

The conviction had also been reached that to facilitate picking up load on an Edison system after a complete shut-down, the presence of a certain proportion of the machine equipment, approximately one-third, in synchronous motor-generator sets would prove of great assistance. Also, the development of the differentially wound generator which


Fig. 3. Automatic Control Equipment for $1000-\mathrm{kw}$. 240 -volt 2-wire Synchronous Motor-generator Set Having Differential Series Field Winding on Generator. Sequence of operation secured by motor-driven drum controller. Solenoid operated line circuit breaker and differential field short circuiting breaker are shown mounted separately.
accomplished the same results as the synchronous converter and load limiting resistor, has further established the value of this class of conversion apparatus.

The advantages of electrically operated reclosing circuit breakers of either the direct or
alternating-current type were recognized at an early date. The development of these tecleniing equipments was allong the lines of solenoid operation for a number of years. This was the logical form of procedure for the direct current breakers, but for a c. operation the solemod


Fig. 4. Automatic Control for Alternating-current Reclosing Feeder Equipments Showing Motor Operated Oil Circuit Breaker Mechanisms Mounted on Front of Panels.
is inherently a far from satisfactory feature, and for that reason the motor operated oil circuit breaker, particularly in its latest form of centrifugal mechanism operated by a 1 -h.p. motor, has won a well deserved popularity.

The logical development of a-c. reclosing breakers has been the complete antomatic control of transformer substations; an installation offering many points of unusual interest is that of Substation " $R$ " of the Kansas City Power \& Light Company. Here, through the medium of motor operated drum controllers, this station is not only brought into service when the supply feeders from the power house are energized, but the equipment is so designed that normally one of the three step-down transformers supplying this substation first picks up the load and supplies all outgoing feeders. As the load demand increases a second transformer is automatically connected to the supply mains and serves a portion of the outgoing feeders. In case of accident, a third or spare transformer automatically comes into service and picks up the load of one of the regular units which may be temporarily disabled. So
suceessful has this equipment proven, that additions to the present station are not only contemplated, but other stations of a similar design are now being actively considered.

The use of operation counters on various devices in the automatic equipment carly became a common practice in order that some record might be kept of the performance of the equipment. In line with this custom there was developed an operation recording instrument consisting of a number of pens suspended over a clock-driven roll of paper. Each of these pens can be connected to some particular device of the automatic equipment whose operation it is desired to recorl. The
purcly control purposes, was probably that installed by the Northern States Power Company of Minneapolis in their Highbridge and Stillwater Stations. A similar installation was also tried out on the lines of the Des Moines City Railway Company and its subsidiaries at practically the same date. Recently the demand for more complete information in the load despatcher's office as to the functioning of automatic equipment, led to the development of a supervisory system giving complete indication and control of the operation of all circuit breakers or auxiliary apparatus in a distant automatically operated station. One of the earliest in-


Fig. 5. Automatic Control for Alternating-current Reclosing Feeders. The equipment controls a total of 3 three-phase power circuits and 6 single-phase lighting circuits. Motor operated timing devices and interlocks are provided so that only one breaker can close at a time, thus reducing size of storage battery required. Small lever switches shown on the panels permit transfer of operation from automatic to manual control for purpose of inspection or test
sequence of these operations is indicated on the moving paper chart, not only as to the individual device, but the relation, in point of time, of this device to others of the automatic equipment. In this way a complete history of the operation of the equipment as a whole is made available for future study and for use in properly adjusting the various devices.

The desire on the part of operating officials for some form of supervisory control over automatic equipment in their various stations, is probably only natural in view of the importance attached to continuity in service. One of the earliest installations of a supervisory control over telephone wires for
stallations of this latter system was placed in service on the lines of the Malden (Mass.) Electric Company about a year ago.

Among the many items which have been developed to meet certain functions desirable in automatic control, may be mentioned the thermal relay, having heating characteristics similar to that of the apparatus which it is designed to protect and which will operate to disconnect the piece of apparatus in case danger from overheating is threatened. Flashing relays, so-called, connected between frame of a converter and ground to immediately disconnect the converter from both the a-c. and d-c. lines in case of flashover or accidental ground, have done much to
render antomatic control of this class of apparatus successful. There have been developed stalling relays to disconnect the apparatus from the circuit if, for any reason, the cyele of operations in starting and connecting a machine to the line is not completed. In this connection protection is also given against starting or operation of 3 -phase rotating machinery under single-phase conditions. For direct-current feeders, relays have been developed which will permit "feeling out" of the line to insure its being clear from a ground or other trouble before its circuit breaker is closed.

In deciding the question of the advantages of automatic versus manual control, a great many features must be considered and individual merits of each case be accurately determined. There might be little excuse for installation of automatic control in one large Edison 3-wire station serving a territory of high load density. On the other hand, there is scarcely a case in which automatic substations could not advantageously be added to serve outlying territories supplied by either direct or alternating current.

For the central station whose business is selling electrical energy, any reduction in cost of generating or distributing this product is of the utmost importance.

For electric railways, whether urban, interurban or trunk lines, whose business is selling transportation, the cost of electrical energy is of great importance, but the raising of the average voltage, due to the more frequent spacing of automatic substations, will result in faster schedules and longer trains, both of which contribute directly to the revenue obtainable from a given amount of equipment, while decreased maintenance and repair charges and platform expense offer attractive possibilities in economy.

For industrial plants selling a manufactured product where electrical energy is but one of the items entering into the expense of manufacture, the saving in cost of this energy would probably be of far less importance than the avoidance of plant shut-down duc to failure of the power supply.

It is a common idea that the advantage of automatic equipment lies solely in the saving of operators' wages. This is often the largest individual item of saving but is rarely the sole consideration.

Reliability of service in itself may often be of sufficient value to overshadow the item of operators' wages. The man who can and does think quickly and accurately in
emergencies, who ads whont hestatan or expensive mistakes, is too valuable an individual to be wasted on an operating job. The results of errors on the part of less skillful operators may be highly expensive

Automatic equipment substitutes. in phace of the operators nswally availathe, the skill


Fig. 6. Alternating-current Reclosing Feeder Equipment showing Motor Operated Oil Circuit Breaker, Mechanism, and Metering Equipment Mounted in Small Weatherproof House.
and reliability of the highest class of engineering talent employed in the design and functioning of automatic control.

Quick restoration of service after a shutdown is an item which might well be capitalized in the good will of customers if for no more tangible reason. Automatic equipment permits the reclosing of a breaker almost instantly and operating experience has proven that the large majority of outages are caused by troubles of an instantaneous nature only. Automatic equipment, however, will permit the reclosing of breakers up to a total of three times in case the fault still exists and finally lock out the circuit until the trouble has been located and cleared.

The above are but a few of the most obvious adrantages secured by using antomatic control and, in general, will apply to all classes of service. Particular advantages will accrue in many individual cases. The values to be assigned such itcms as improved power factor and reliability of service are largely local. The considerations governing antomatic hydro-electric developments are quite
distinct in many respects from those covering the location of substations. But the published data available covering results obtained in actual service by automatic equipment, often over long periods of time, speak for themselves. At Cedar Rapids in one year's operation of the automatic hydro-clectric station $6,580,000 \mathrm{kw}$.hr. were generated at a total operating and maintenance charge of $\$ 42.80$. The Butte Electric Railway Company
operated its $500-\mathrm{kw}$. automatic converter station for three years at an average annual cost of $\$ 270.00$. The Tennessec Electric Power Company has in one of its substations an automatic reclosing feeder equipment which recently functioned eleven times during an early morning storm, and so successfully that the only record of these interruptions was that shown by the operation counter installed on the breaker.

# Devices for Leveling Large Machines 

By N. L. Rea<br>Contract Service Department, General Electric Company


#### Abstract

The "lining up" of machincs has bceome an increasingly difficult problem with each increase in size. Machines have reached such large proportions now that special instruments have been designed to meet the requirements. The author describes these instruments and their use.-Editor.


In the early days of the industry when a $30-\mathrm{kw}$. generator was a giant and a $50 \cdot \mathrm{kw}$. required half the factory force to load on the car, the problem of erecting was simple. A spirit level, a plumb bob and a hank of silk fish line composed all the special equipment necessary. Practically all the machines were belt-driven which simplified the erecting problem.

As the size of the machines increased and direct connection became common, the spirit level had to be supplemented by straight edges. The span of the bases soon increased to such an extent that the length and cost of the straight edges became prohibitive.

We then turned to the surveyor's level, and for a time this served fairly well, but we found that the average instrument man got cold feet when we talked of sixty-fourths; and thousanths were beyond his wildest dreams. The increasing size and speed of equipment called for increased accuracy in leveling and we laid our problem before one of the best instrument makers who gave us a 22 -inch engineer's, or Wye, level fitted with an especially accurate and sensitive level vial. This solved the problem as far as the instrument was concerned but left us with the standard survevor's target.

We soon found this was not altogether suitable for our purpose and started experimenting on a satisfactory substitute. The "blind spot" back of the cross hairs is appreciable at a distance and may be several times wider than the finest mark on the target.

Some of our erectors overcame this by having two parallel lines drawn on the
target, with enough space between these lines so that the cross hair would not completely cover this space. The target was used by making the cross hair lie midway between the two lines.

One of the first of these targets was made of a silver plate blackened with sulphur smoke and with two parallel lines drawn across it with a dividing engine. This plate was fastened on a regular surveyor's target with the head of an inside micrometer below it, arranged to slide the plate on the target and to measure the movement in thousandths. This arrangement was not altogether satisfactory. The lines tarnished quickly, the lacquer blurred them and caused reflection from the surface of the plate which was confusing to the instrument man.

Several other schemes were tried and through a process of elimination we developed the arrangement shown in Fig. 1.

This consists of a standard 24 -inch combination square with a special target arranged to slide on the blade. The smaller bar of the target can be clamped in any position. The target proper is a sliding fit on the blade and is pulled towards the other member by a coil spring. The measuring head of an inside micrometer is mounted between the two parts and any movement of the sliding target can be read in thousandths of an inch.

The two sides of the target face are of white celluloid with three parallel lines across them. These lines are cut with a dividing engine and are blackened; they are a sixty-fourth of an inch apart. The inside edges of the celluloid are also notched between the lines as shown.

This target gives readings that cheek within two or three thousandths but has several disadvantages. An electric hand lamp is necessary to illuminate the target. This lamp must be carefully shaded and held so that the instrument man does not get any direct or reflected light. The light must be kept in the same relative position as a change of angle in the illumination apparently changes the reading.

In use the target and cross hairs appear somewhat as shown in the sketch in Fig. 1. For clearness; only a portion of the instru-


Fig. 1. Photographs of the Two Sides of a Sliding-target Leveling Device and a Sketch showing the Appearance of the Target when Viewed Through the Telescope
ment crosshair is shown, it being superposed midway between the top and bottom lines of the left-hand set of target lines.

Lighting difficulties caused us to continue our experiments and as a result we developed the outfit shown in Fig. 2. This consists of a "V" block arranged to clamp the measuring head of an inside micrometer. The target proper consists of a steel ring arranged for mounting on the end of the measuring rod of the micrometer, any length of rod can be used to suit local conditions as we are usually interested only in the variation of height
from point to point and this is reat an the micrometer.

The steel ring is provided with two cress hairs of 0.003 steel wire that are at right angles to each other and 45 deg. from the axis of the measuring rod.

A sheet of white paper is held at the hack of the target at the proper angle to catch the best light. This white background throws the cross hairs of both the target and Wye level in silhonettc. This gives clear, sharp readings without errors from lighting changes or eye strain from reflected light.


Fig. 2. Latest Improved Form of Leveling Target for Use in Conjunction with a Telescope

The eye automatically bisects the angle of the target cross hairs with those of the instrument and a thousandth of an inch shows as an appreciable amount.

The base shown and the micrometer are standard equipment and might be varied to suit local conditions and special requirements. We have considered making the base a little longer and mounting a small round type level as a check on the staff being always plumb.

The steel ring and the cross wires are the important things in the equipment.

# Development in Power Production 

By () Jumiciran




#### Abstract

The conomical production of power is of vital comern to evervone- the kilowattho irs generated and distributed in this combtry in 1922 reached the lum - lotat of fifty billion-this figure is likely to double each five years! With such figures in mind the gain made by each increase in efficiency is apparent. The author tells us how we are obtaning better conomies now thin formerly and the possililities of still further economies in future jower production.- Emotor.


The great expansion in power production during the past year promises to be exceederd in 1923 and 1924. This expansion has created a demand for turbine units of larger individual capacity. A company that only a year or two ago considered a $10,000-\mathrm{kw}$. unit the largest that could efficiently be utilized, now finds that $15,000 \mathrm{kw}$. is the proper size, and those previously using $20,000-\mathrm{kw}$. units are now installing $30,000-\mathrm{kw}$. wnits. Large systems are installing 50,000 - and $60,000-\mathrm{kw}$. units. This tendency is only one example of how rapidly the power business is growing.

In planning new stations great attention is given to securing the highest economy compatible with reliable design and reasonable first cost. These studies include a carefu? analysis of the number of heat units required to deliver a kilowatt to the switchboard with various types and arrangements of apparatus. How effective the various arrangements proposed will be in practice, of course, cannot be accurately predicted. The conditions under which the stations are to operate vary considerably and those operating most continuously will always have an advantage in the eeonomical production of power, but it is safe to say that the changes ineorporated in the new stations will lead to material improvements in economy, and without doubt a kilowatt wilt be produced in these stations for less coal than in any station now in operation.

The use of steam for converting heat into power has been considered wasteful in compariSill with gas engines, but for large capacities the probability that the steam cycle will be superseded is far removed. However, it is well recognized that the steam eycle has inherently theoretical possibilities elosely approaching the efficiency of oil or gas engines when worked to its limit. What this limit is in practice will depend greatly upon the ingenuity of handling materials already developed and possibly upon future researeh work.

It is only a few years ago that the steam pressure was $1,0 \mathrm{H}$... from this there has been a steady rise to $200 \mathrm{1b}$., 2.00 1b., 300 lb . A
considerable number of new stations are being planned for 3.50 lb . pressure with superheat to bring the total temperature of the steam to about 700 deg. F. At the present time there are three large stations, for which steam conditions of $500-1 \mathrm{~b}$. gauge with superheat. giving a total temperature of 72.5 to 750 dey. F. have been selected. The steam will be reheated up to the original temperature after it has gone through a portion of the turbine, thereby adding a considerable amount of heat to each pound of steam. At the present time $300,000 \mathrm{kw}$. capacity to be operated under these steam conditions is under contract, 200,000 kw . of which is on order with the General Eleetric Company.

Due to the great expansion of power companies in general and various intereonnections of transmission lines, there has recently developed a demand for a special type of turbine which has been termed "Base Load Machine." As the name implies, the machine is to carry continuously a certain portion of the load, and the stations in the outlying districts of the systems are to take care of the load variations. It is obvious that with base load machines high economy is exceedingly important. Such machines are designed with only one governing valve, as they are intended to run as nearly as possible at full capacity. The governor, so to speak. will only be used as an emergeney device to check the speed of the machine in case the load is suddenly removed. For emergeney operation, to take care of drop in steam pressure or loss of vacuum, a hand operated by-pass is provided.

We may in the near future see large central stations located at the most favorable points for coal and water as well as distribution. These stations will supply other companies with power, such companies themselves producing power in large quantities, and these stations will be designed with the object of obtaining a kilowatt for the lowest number of heat units.

New stations are being designed with much greater attention to details than formerly, in
order to obain high efficiency as well as greater reliability. We all realize that these two conditions must go toget her.

Stations that are now being projected are a distinct advance upon anything that has heretofore been done and will undoubtedly produce a kilowatt with a considerable saving in coal. The Operating Company is vitally interested in how much coal it is necessary to burn to produce a kilowatt at the switchboard, but as the turbine is only one part of the operation, it is of course necessary to give as much attention to all the apparatus as to the turbine itself. If one per cent unnecessary loss has taken place in the boiler, in the piping or in the auxiliaries, it is just as important as if this per cent were lost in the turbinc. We who manufacture turbines are continuously studying our end of it in order to produce high efficiency in the turbine and the generator. However, in the turbine itself we have not very much farther to go, that is, any material improvement in coonomy, in all probability, will not come from any radical changes or improvements in the turbine. Therefore, the advancement must be in the conditions under which the turbine operates, also improvements of all the other apparatus in the station and especially in the steam cycle so that the working range is increased. It is in this direction that much progress is possible before the ultimate is reached.

Stations now being planned have a number of new features all tending to improve the economy as follows:

First: Higher steam pressure and temperature, thereby increasing the temperature range so that we, so to speak, are starting at a higher level; the lower level is fixed by the condensing water.

Second: Reheating. This arrangement is to take the steam out of the turbine after it has done a certain amount of work, send it through a superheater, thereby adding more heat to it, and then finally expand it through the lower portion of the machine, or a separate turbine, down to the condenser pressure. The idea back of this arrangement is to put as many B.t.u.'s as possible into each pound of steam, thereby reducing the quantity of steam per kilowatt, which also reduces the quantity which must be condensed. In addition, it has the advantage of delaying the dew point in the turbine quite considerably, thereby improving the efficiency, as the efficiency of the turbine is quite sensitive to moisture. The reason for this is that it requires work to accelerate the moisture in the steam to the
high steam velocity that is required in hurbines. This work must be furnished loy tho steam itself.

Third: Blecding for leating feed water.
It has long been known that extracting steam from the main unit for heating the feed water after the steam has gone through a certain portion of the machine will improve the station economy, but it is only recently that this plan has been extensively adopted. The main advantage is the reduction in the quantity of heat rejected to the condenser, and the more this loss can be reduced the higher the efficiency will be, other conditions being the same.

The difference between the steam going through the throttle and the steam discharged into the condenser represents what is absorbed in the feed water, and the greater this difference is the higher the economy. Theoretically, there should be a number of these extraction points, that is, in the extreme case one for each stage. This would lead to too great mechanical complication and we have provided only three extraction points in our large units. The theoretical requirement for high efficiency with extraction is that the water be heated $u p$ to the saturated temperature of the steam. This suggests the use of air preheaters for the boilers, that is, heating the incoming air to the boilers by the stack gases. It is probable that in the near future considerable advancement in this direction will be made. and when so made the minimum amount of heat will be rejected to the condenser, and thereby still greater benefit will be obtained from bleeding.

Fourth: The use of motor-driven auxiliaries.

It is only a comparatively short time ago that station operators considered it essential for safe operation to have practically all of the auxiliary apparatus steam driven, using high pressure steam with very little consideration to economy. In some cases, there was practically no drop in temperature between the steam going in at one end and coming out of such auxiliary turbines. The exhaust steam from such apparatus was either used to heat the feed water or was put back into the main unit. It is obvious that this was very wasteful. Many of these auxiliaries are now driven by motors with power from the main unit. It is probable that in the near future nearly all the auxiliaries will be driven electrically with two-fold gain in economy: First. higher economy of the auxiliary itself; second, greater extraction from the main unit.

One arrangement that has been proposed is to attach a separate low voltage alternator of suitable size to the main unit as a source of power for the anxiliaries. This arrangement, no doubt, has considerable advantage in comparison with taking power from the main busbars or from separate units called house turbines.

All the above mentioned arrangements are for new stations where the selection of the units can be made to conform to all the requirements, but there are numerous places where this cannot be done, and for such cases it has been proposed to install a high pressure boiler, using a special turbine, which, in turn, discharges the steam into the present steam mains and thence to the turbines, thereby obtaining an increased economy and increased output, without scrapping all existing apparatus. For such conditions we have proposed a standard boiler of a capacity of approximately 110.000 lb . per hour, and a turbine generator set for each boiler, the turbine acting simply as a pressure reducing valve which develops power. Such units are actually being built by us to utilize steam pressure of 1000 lb . to 1200 lb. maximum, with superheat giving a total temperature of 700 to 750 deg . F. in one station, the steam being discharged into existing mains at about 250 lb ., and in another at about 350 lb . We anticipate considerable gain in economy with this arrangement, although the economy can never be as great as when the whole station is designed for high temperature and high pressure conditions.

With the increase in temperatures, the design must properly provide for the free expansion of the parts that come in contact with the high pressure steam, otherwise distortions take place which interfere with the safe operation of the unit. In new designs a most careful study has been made of this problem, in order to provide turbines perfectly safe to operate at the present temperatures and also higher temperatures in case they are called upon to do so.

Special attention has been given to the design of high pressure steam joints, particularly to the joints of the turbine shell to minimize all steam leaks, and bolts are made of high grade, heat treated steel. It is, however, practically impossible to design steam joints which can withstand the strains caused by water coming into the turbine, especially at the high temperatures now used; and, therefore, special care should be given to the design of the steam mains, and also to the operation of the boilers.

The material used in the diaphragms and turbine casings of our large turbines is steel. Even in the low pressure end where cast iron could safcly be used, stecl has been adopted in order to avoid additional bolting and chances of leakage. The only principal part of the turbine where cast iron is now used is the exhaust casing. By properly attaching the steel shell to the exhaust hood, the strains are materially reduced.

A number of surface air coolers are now under construction for use with turbine generators. These coolers will maintain clean generators inasmuch as they operate on a closed system, using the air over and over again. In addition, they give the advantage of reduced fire risks, on account of the limited amount of oxygen in the cooling system. Where the vacuum is sufficiently low the condensate may be used to cool the air, thereby recovering the major part of the generator loss.

Some stations are arranged to heat the incoming air to the boilers by extracting steam from the main unit. This arrangement acts exactly as heating the feed water by extracted steam and tends to increase the efficiency of the main units and reduces the heat discharged to the condenser.

Another very important point in the economic production of power is the utilization of the by-products in the coal before burning the coal in the furnace. Economic conditions in the near future may be such that this question must be given serious consideration.

The above is a short description of the present tendencies in the design of power stations. It would be natural for you to ask what possibilities there are in still further reducing the amount of coal necessary to produce a kilowatt.

Some years ago in discussing this subject with a well known engineer, it was stated that a kilowatt could be produced for as low as 12,000 heat units, and it is perfectly within the range of possibilities that even this figure may be bettered. At the time of making this statement we were very far away from the realization of such economy, much farther that we are today, but I still think that this figure can be obtained in practice. In order to obtain such results, it may be necessary to increase the steam pressure from 550 lb . to 1200 lb., or perhaps higher. The possible gain in economy by raising the pressure from 550 lb . to 1200 lb ., keeping the initial temperature constant, is 10 per cent with extraction, and 7 per cent without extraction.

When the high pressure portion of the turbine is separate from the low pressure portion, high steam pressures in turbines can safely be used, as the parts exposed to the high pressure are small. Further advancement of course will be dependent upon
actual trial of the forward steps being taken at the present time, but it is certain that these developments, radical as they are, will only lead to still further developments in the economic profluction of power.

# The High Capacity Current Interrupting Testing Station of the General Electric Company 

By C. E. Merris<br>Switchboard Engineering Department, General Electric Company


#### Abstract

Until the last year or two the development of oil circuit breakers to keep pace with the ever-increasing generator capacity of large systems had been hindered by the lack of satisfactory testing facilities of sufficient magnitude. The testing station described in this article was built to remove this handicap and has already demonstrated its worth.-Editor.


A comprehensive program for investigating the behavior of current interrupting apparatus under various conditions has resulted in the erection of a thoroughly modern and unique testing station at Schenectady with all equipment necessary to test to destruction high interrupting capacity apparatus.

This station has been in operation approximately one and one half years and already has given answer to many problems that could have been solved in no other way. The result has been the improvement in several forms of interrupting devices, either by a change in construction or the addition of some new means to improve the behavior of the individual device when subjected to interrupting duty. For example, the value of the separating chambers with the latest type of baffle as used in the type H breaker, and the explosion chamber in the tank type breakers, has been proved conclusively by means of this testing plant.

As short circuits or dangerous overloads on power lines cannot be entirely avoided there must be means provided to remove them quickly from the system. Whether the removal is done safely or disastrously depends largely upon the operation of the oil circuit breaker.

Due to the many variable problems involved, the building of a dependable oil circuit breaker is inherently difficult. However, it is not now so baffling a problem as it was before the testing equipment herein described was available in a specially designed station where many factors could be kept constant during the investigation of one variable.

Inside the oil vessel actions take place which can not be observed and which for a long time could not be measured. Thus, the path taken by the arc, the general form of the gas "bubble," the length of the arc under various conditions, the pressures generated, the speed of the moving parts at all stages of the stroke, the proper oil level, the scientific venting of the gas to prevent oil throwing and many other phenomena were practically unknown or very insufficiently investigated. The solution of these problems depended very largely on finding out certain empirica! data which could be obtained only by a large number of tests under a given set of conditions on a system large enough to stress high capacity breakers to failure. At the same time, this system had to be flexible so that the conditions were under control, thereby permitting the change of one variable at a time.

## Handicaps to Testing

Heretofore high capacity short circuits could be obtained only on the systems of large power or central station companies. The progress of testing breakers on these lines was slow and somewhat uncertain for the following reasons:

Short circuits on commercial systems which would stress the larger breakers to their capacity were believed to be hazardous to equipment and very objectionable to customers having synchronous apparatus which would very often be thrown out of step during short circuit tests.

There was great expense involved in sending apparatus, instruments, operators, and engineers to distant cities where they might have to remain for months awaiting favorable opportunities to make

Fig. 1. Diagram Showing the Essential Features in the System of Connections Used in the Testing Station
tests at such times as suited the convenience of the power or central station company.

There was almost an entire lack of control of conditions of voltage, current, power-factor, etc.

Progress was slow in the cut and try met hod of investigating samples buit to incorporate improvements indicated as desirable from the preceding tests. Oftentimes conditions changed so that the power companies could not permit succeeding tests for a year or two and sometimes they were averse 10 having any further short circuit tests made at all. This delay often detracted greatly from the value of the data obtained and greatly impeded progressive development.

Evidently a high capacity testing station was the only satisfactory means by which existing problems could be solved and pace kept with future development. Aecordingly a $26,700-k \geqslant-a$. station was built and deroter exclusively to interrupting capacity tests.

## Station Apparatus

A specially built alternator ( $26,600 \mathrm{kr}-\mathrm{a}$. 300 r.p.m., 25 cycles, 13.200762066003510 volts with two coils per phase and all coil terminals brought out to convenient switches) feeds power through two large capacity oil circuit breakers to a "bomb-proof" testing compartment in which the test breaker is set up. One breaker acts as a generator protective breaker while the other is used as a closing switch to energize the bus leading into the testing compartment. In a high voltage testing yard, equipment has been installed adjoining the "bomb-proof" so that by throwing disconnecting switches three high voltage transformers can be energized and made available for testing. Four oscillographs, with an adjoining developing room. form part of the permanent station equipment. Other oscillographs may be readily connected when desired. A diagram of the connections of the station is shown in Fig. 1.

A 3 -phase 16 -pole $1500-\mathrm{h} . \mathrm{p} .300-\mathrm{r}$. p.m. 5.50volt induction motor. coupled directly to the alternator shaft, is connected through a 1.5,000 -volt oil circuit breaker to an open delta transformer bank. 12.000 .50 rolts, which is connected through another oil circuit breaker to the 12.000 -volt distribution bus of the works.

In the motor lines are two current transformers to operate inverse time limit overload relays with comparatively long time delay settings. These are provided for emergency short circuit protection and function to trip the breaker in the event of heary sustained overloads in the motor winding.

The motor is started by means of a group of grid resistors and large contactors. Acceler-
ating, or lock-out, relays on the (omtar wor coils make the outfit "fool-proof" and yet the. motor can be run bedow full speced if ide ired by stopping the controller handle at any one of the six different notches.

In the exciter set a direct-current (i-pule $1.50-\mathrm{kw} .1200-\mathrm{r} . \mathrm{p} . \mathrm{m} .2 .50,23.5-\mathrm{volt}$ comperundwound generator is direct connected to a 22.)h.p. $1200-\mathrm{r} . \mathrm{p} . \mathrm{mI}$. $\mathrm{sin}(0$-volt induction motor


Fig. 2. Diagram Showing System of Connections for a Threephase Test Employing Three Oscillographs
connected through a 15.000 -volt oil circuit breaker to the $12,000,50$-volt transformers.

The exciter armature is connected through a solenoid operated field switch to the alternator field. Field discharge resistance is provided in parallel with this field switch. Grid resistors located in the pit beneath the alternator, for use in series with the alternator field, are connected to a contactor on a control panel and are readily available when desired. Forced lubrication and water cooling systems are provided for the alternator bearings.

## Generator

The $26.700-\mathrm{kr}-\mathrm{a}$. $2.5-\mathrm{crcle}$ alternator is especially braced both in the frame and the windings to withstand the enormous strains thrown upon it. The rotor, including the motor rotating parts, weighs approximately 1.50 tons. This gives a flywheel effect of approximately ( $\mathrm{IV}^{2}$ ) 3.000 .1000 lb . it

Two coils per platse with all terminals bronght ont to convenient disconnecting switches afford a combination of series, multiple, $I$ or delta connections whereby four test bus voltages at full excitation are availahle'; viz., 13,200 , 7620 , 6600 , and SS10.


Fig. 3. Testing Generator, $26,700-\mathrm{kv}-\mathrm{a}$., 300 r.p.m., 25 Cycles 13,200/7620/6600/3810 Volts

## Reactors

Between the generator coil switches just referred to and the protective 15,000 -volt 2000 amp. oil circuit breaker is a set of reactors, two in series per line, with taps brought out to another set of disconnecting switches. There are nine taps per pair of reactors affording reactance steps at intervals between 0 and 6.1 ohms.

## Current Measurement

Current is measured by oscillographs connected to special shunts located in the test bus just ahead of the point of grounding. In order to get these shunts near the oscillograph, which are of necessity located in the control room, the test bus is carried back from the "bomb-proof," through the shunts and grounded. Approximately 40 ft . of twisted pair leads are required to run from each shunt to its corresponding oscillograph. The shunts are arranged so that their axes lie in the planes of an imaginary cube, i.e., with the three axes mutually at right angles. This arrangement practically eliminates errors due to inductive effects of one shunt upon another. Shunts are used because they are considered more accurate than current transformers for recording transient phenomena.

## Voltage Mcasurements

Gencrally, voltage is measured by the use of potential transformers cannected in the circuit at the desired points. Twisted pair leads run to the oscillograph tables.

In some cases where transient phenomena are being studied closely it has been found desirable to use high resistances, across a small portion of which an oscillograph shunt is connected to give a potentiometer effect. Sphere gaps are used in some classes of investigations where high voltage impulses are expected.

## Pressure in Test Breaker

Special apparatus has been developed to record the pressure at all times during the drawing of the are in the test breaker. This recording device is very sensitive to rapid changes in pressure and has proven extremely valuable in studying the phenomena taking place inside the breaker.

## Speed of Test Breaker

The speed recorder used has proved very valuable in studying the performance of breakers in action.


Fig. 4. High Voltage Equipment of Testing Station

## Control

With the driving motor and exciter set running, the control of the protective breaker, closing breaker, exciter field, alternator field, and test breaker is centered at the control
board in the operating room. Furthermore, by tripping the direct-current control breakers at the control board all oil circuit breakers in the station can be tripped out in an emergency. Several interlocks are provided to insure the proper sequence of operation of the important breakers in the event of failure of one control circuit. Thousands of short circuits have been interrupted with no instance of the protective breaker failing to clear the trouble.

The short circuit is actually thrown on by closing a knife switch on the oscillographer's table. Thus there is close coordination between the opening of the shutters and the operation of the test breaker. With the skilled operators employed, it is seldom indeed that an oscillographic record is missed.

## Cars

Steel cars are provided on which the test breakers are mounted, adjusted, run into the "bomb-proof" for test, and then returned to the assembly floor. This arrangement permits the crew to get the breaker ready during the time that its predecessor is actually being tested.


Fig. 5. Test Breaker Ready to be put into Testing Compartment

## Oil Handling Equipment

Storage tanks for both new and used oil, together with a pumping and filtering system, are being installed. This equipment will per-
mit the rapid handling of oil and assure propere dielectric strength.

## Power Available

There are not many power systems in the country which have an available capacity under short circuit conditions excceding 600,-


Fig. 6. Three Oscillographs on one Driving Shaft Used in the Control Room
$000 \mathrm{kv}-\mathrm{a}$. at 13,200 volts. This is equivalent to $200,000 \mathrm{kv}-\mathrm{a}$. at 7630 volts per phase on a Y-connected grounded system which is the connection ordinarily in use. The short circuit capacity of the generator in the testing station considerably exceeds this capacity so that breakers at that roltage can be tested at their full rated interrupting capacity. If the breaker is of a type that permits of testing its breaks individually, then by testing a single break a capacity much in excess of 200,000 kv-a. per phase can be obtained.

## Conclusion

During its comparatively brief existence. the high capacity testing station has developed considerably beyond the original plans. It very soon became apparent that such an equipment was vital to the design of dependable oil circuit breakers and other circuit interrupting devices. The old order of things was no longer adequate. Advanced designs of generating, transmitting, and converting apparatus of super-power systems representing millions of dollars in investments had to be guarded by scientifically designed breakers. The data had to be obtained. This testing station is producing it. By close co-ordination of the testing, designing and factory organizations, very superior breakers scientifically constructed are being built and will continue to be developed -superpower breakers for superpower systems.

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## COFFIN FOUNDATION AWARDS

In our January issue of this year we announced the founding of the Charles A . Coffin Foundation - and on this occasion we have the pleasure of announcing the first award. It should be recalled that this Foundation was established as an expression of appreciation of Mr. Coffin's great work, not only for the General Electric Company, but for the entire electrical industry.

The first award was made to the Southern California Edison Company in recognition of its notable contribution during 1922 to the development of the electric light and power industry in its territory.

The award was presented on the evening of June 7th at the Public Policy meeting of the National Electric Light Association and was received on behalf of the Southern California Edison Company by Mr. J. B. Miller, President of the Company: The certificate of award bears the following inscription:

## Charles A. Coffin Foundation Established by

General Electric Company
For the advancement of the Electrical Art Awards
The Charles A. Coffin Medal To the
Southern California Edison Company Califorvia
In recognition of its distinguished contribution to the
development of electric light and power for the
convenience of the public and the benefit of the industry during the year 1922 .
After the certificate of award had been presented a check for $\$ 1000$ was handed to Mr. Miller to be turned over to the employees' benefit or similar fund.

Finally, a beautiful gold medal which had been struck for the occasion was presented to
the Southern California Edison Company. This medal is a striking piece of work-on the obverse side appears a portrait of the man whose name and work it was sought to perpetuate with the inscription Charles A. Coffin Medal 1923, and on the reverse side the following is inscribed:
"For distinguished contribution to the development of electric light and power for the convenience of the public and the benefit of the industryawarded to the Southern California Edison Company, California, 1922."

We reproduce the obverse side of this medal as the cover of our magazine this month.

The presentation was made by Frank $\mathbb{W}$. Smith, President of the National Electric Light Association and Chairman of the Charles A. Coffin Prize Committee. The other members of this committee are Nartin J. Insull and Dr. S. TV. Stratton.

The committee reports that is companies responded to the invitation to submit presentations of their accomplishments and that it was no easy task to come to an unanimous opinion as homorary mention might well be accorded several of the splendid presentations.

The following day, June Sth, the Charles A. Coffin Fellowship and Research Committee, consisting of Dr. Frank B. Jewett, Dr. Charles F. Scott and Dr. John C. Merriam, announced the award of seven fellowships, totalling 8.5000. These awards went to Edwin Lawrence Rose, of Pasadena. Cal.; Ralph A. Beebe, of Monson. Mass: ( feorge Lynn, of Lawrence, Kansas: William L. Fink, of Detroit; Elmer V. Hutchinson, of Cleveland. Ohio; Henry N. Beets, of Grand Rapids, Mich.; and Alfred Lemard Dixon, Champaign, Ill. All the recipients are college graduates engaged in research work and are planning research work in the fields of electricity, phrsics and physical chemistry.

# The Electrical Plant of Transocean Radio Telegraphy 

By E. F. W. Alexanderson, A. E. Reoch and C. H Taylor

All of the Radio Corporation of America


#### Abstract

Radio experts and amateurs alike will be interested in this instructive paper which gives an account of the equipment and of the methods used by the Radio Corporation of America in its transoceanic radio business. This paper is to be read at the midsummer convention of the A.I.E.E. which is held this year at Swampscott, Mass., June 26 to June 29.-Editor.


At the beginning of 1920 the United States Government removed the war restriction on commercial radio service, and the Navy Department restored to the Radio Corporation of America those stations which were built and equipped in 1914 by the Marconi Wircless Telegraph Company of America for transocean scrvice.

In addition to the agreements previously entered into with countries in Europe for transocean radio service, the Corporation faced the situation arising out of the Great War, in which practically every European country demanded direct radio communication with the United States.

The need for the provision of modern facilities for carrying on radio communication with those countries with which agreements had already been made, was imperative, and hardly less imperative was the need for the expansion of our facilities to meet the new situation.

The radio equipment in all of the installations restored to the Corporation was of obsolete type and based on the use of damped waves, except in the case of the New Brunswick station. At that station the Navy Department had instructed the General Electric Company to install high-frequency alternator equipment and to modify the antenna circuit to meet the requirements of their system. Accordingly, an alternator equipment was installed which was able to supply to the antenna circuit 200 kilowatts at the high frequency to which the antenna circuit is tuned. The antenna at this station had been erected as an inverted L, approximately a mile long and 550 feet wide. This was changed to the multiple-tuned type by adding five tuned down leads, equally spaced along the length of the antenna, and connecting them through a balanced distribution system to the ground and counterpoise wires. This installation has been described by technical papers read in 1920 and 1921.

Operation of the system of the Radio Corporation started with two transmitting stations-at New Brunswick, New Jersey, and at Marion, Massachusetts. Each of these transmitting stations had its corresponding receiving station at Belmar, New Jersey, and at Chatham, Massachusetts, respectively. New Brunswick was used for communication with England, and Marion for communication with Norway. The telegraphic operation of the English circuit was centered in Belmar, and the operation of the Norwegian circuit was centered in Chatham. Messages to England or Norway were telegraphed to Belmar and Chatham respectively, where they were copied and transmitted over the radio circuit via New Brunswick and Marion. Similarly, messages from England and Norway were received in Belmar or Chatham, were copied by hand, and re-telegraphed to New York. This process involved several relays of telegraph operators with the consequent high expense and possible delays and errors.

With the present system of operation, the Radio Corporation has six transmitters on the Atlantic coast, two in Tuckerton, one in New Brunswick, one in Marion, and two in the Radio Central station on Long Island. All these transmitters are controlled directly from the traffic office in New York City.

Only one receiving station is needed for all incoming messages. This receiving station is located at Riverhead, Long Island. It has a single antenna of a new and special type, which will be described later. This antenna intercepts the waves from all European transmitting stations. The receiving apparatus, also of a new type, separates this conglomeration of ether waves which come in over the receiving antenna, into separate messages which are automatically relayed over telephone wires so that all messages are received and copied in the same traffic office in New York.

The transmitting station on Long Islandknown as "Radio Central"-and the receiving station at Riverhead, Long Island, represent the modern system of the Radio Corporation. The stations at New Brunswick, Marion, and Tuckerton are adaptations of the modern transmitting apparatus developed by the General Electric Company and antemnas built before the war. The characteristic features of the transmitting system are: The high-frequency alternator, the multipletuned antenna, the speed or wavelength regulator, and the magnetic amplifier.

In the Riverhead receiving station the method of centralization has been carried to its logical conclusion by concentration of all radio apparatus in the one station, and concentration of all reception in New York. The advantage of such concentration is obvious. New receiving circuits for communication with any new station in Europe can be added at a negligible cost by installing a new set of receiving apparatus on some of the shelves provided for that purpose in the Riverhead receiving station.

The Radio Central transmitting station has been planned in such a way that the cost of additional transmitting units will be a minimum. The choice of the site of the Radio Central transmitting station was carefully considered, looking forward to a growth of international radio communication which would require as much as twelve transmitters in this new station. Two of these twelve transmitters are already completed.

The principal considerations in selecting the site for the Radio Central station were:

1. The site must be within a reasonable distance from New York-the center of traffic.
2. A large tract of land of a desirable nature must be available, at a moderate cost.
3. A good power supply must be within easy reach.
4. There must be direct and reliable wire line communication with New York City.

The site selected on Long Island fulfilled these requirements in an ideal way, but another desideratum which, in the past, had been the deciding factor in selecting sites for transmitting stations, was not fulfilled in the Long Island location-a natural low ground resistance. The Long Island ground consists of quartz sand of extraordinarily high resistance. The decision, therefore, regarding the selection of this site was a grave responsibility for the engineers of the Radio Corporation. It meant a radical departure from the generally
accepted theories. It implied that practical operation rather than technical considerations was to be the controlling factor. The engineers thus undertook to remedy loy new developments in the technique what nature had failed to provide-a good ground. Much progress had already been made to reduce ground resistance by multiple tuning and ground equalizers, but this experience had been gained in stations like New Brunswick, Marion, and Tuckerton, where the natural ground resistance was low. However, we had sufficient faith in the further possibilities of development of improved grounding methods to take the responsibility for starting the construction of the new station while investigation was going on to find a solution for the grounding problem. The development work of the new ground system required as much time as the completion of the rest of the station, but by the time the station was ready to go into service the ground system was also ready and proved to be successful beyond the most sanguine expectations.

The Radio Central transmitting station of the Radio Corporation of America is the first of our stations that has been planned and designed from the beginning to meet modern requirements, the other stations having been made to conform to modern practice by modification of equipment installed in earlier times. The Radio Central type of station is being duplicated in Poland and Sweden. This station has been frequently described and while its 400 ft . steel towers with 150 ft . cross arms are quite well known, little has been published regarding the technical performance of the plant.

## Radiation

The transmission value of the transmitting station is expressed by the product of the effective height-usually given in metersand the charging current of the antenna cir-cuit-given in amperes. In deciding upon the value of meter amperes that would be required at our Long Island station, we took advantage of the experience gained from work done with the signals transmitted from the Nauen station in Germany and the Carnarvon station in England. As a result of the preliminary work in this connection, a figure of 50,000 meter amperes was decided upon and the antenna circuit was designed to give this value with full power on one transmitting unit.

As this figure of 50,000 meter amperes is made up of two factors, effective height of and current in the antenna circuit, the values
assigned to each of these factors must be so chosen that the cost of the antenna, cost of power equipment, and cost of operation and maintenance will result in the most economical investment. In order to determine the most economical height of antenna, it was necessary to check carefully the varying effects of capacity, effective height, wave length, voltage and current. The result of
lig. 2 shows the calculated cost for antenna structures at different heights for two typical stations of 50,000 and 100,000 meter amperes radiation.

The antenna voltage limitations which had been experienced at our older stations necessitated an investigation of the insulators that should be used in connection with these antennas. This work has been described in a


Fig. 1. Principal Dimensions and Other Data of the Types of Antenna Used in the Atlantic Shore Stations of the Radio Corporation
these investigations showed that if the first cost of the transmitting station be plotted against the height of the towers for a given value of meter amperes at a given wavelength, a curve is obtained showing a distinct minimum. This minimum is not sharp but shows that there is a minimum cost of station for the given meter ampere value over a small range in the height of the towers.

Fig. 1 gives for comparison the principal dimensions, effective height, and resistance of the four types of antenna used in the Atlantic shore stations of the Radio Corporation. The effective heights are determined by measurements of radiation.
paper read by Mr. W. W. Brown on March 7 th last, before the Institute of Radio Engineers, and this shows that by careful design and arrangement of parts, we have been able to raise the working voltage of our antennas from around 60,000 to 150,000 . In a recent test of the insulators actually installed and operating at our Radio Central station at a voltage of approximately 120,000 , it was found that the voltage distribution over the double insulator unit, by means of which the wires are suspended from the bridge arm of the towers, is roughly 45 per cent and 55 per cent. the insulator nearer the tower having the smaller proportion of the voltage.

## Power

The power to operate the station is generated in the Long Island Lighting Company's plant at Northport. L. I.. and carried by a threephase network at 22,000 volts, a distance of 30 miles to the radio station. At the radio station, the power is transformed to 23300 , twophase, to drive the induction type motors connected through step-up gears to the highfrequency alternators.

## Antenna

The suspension of the antenna wires followed current transmission line practice. The wires run the full length of the antenna;


Fig. 2. Curves of Cost of Antenna Structures of Different Heights ( $A$ for 50,000 meter amperes radiation; $B$ for 100,000 )
standard transmission line clamps are fastened to the wire at each tower suspension point. These are shackled to the insulators suspended from the tower bridge arm. As the working voltage at which this antenna would operate. was higher than that used at our other transoceanic stations, the design of this circuit was carefully considered with respect to corona losses. The operation of this antenna at 135.000 volts showed that the corona limit was not reached on any portion of the circuit, although there is not a very great reserve where the inner wires, unshielded by the suspension insulators, pass across the face of the steel tower.

The antenna consists of 12 parallel wires $\frac{5}{16} \mathrm{in}$. diameter $\bar{i} 500$ feet long and spaced on an average about 14 feet apart forming an approximately horizontal plane about 1.50 feet wide. The wires are stretched from dead end structures close to the building to the first tower cross arm, then from cross arm to cross
arm in a straight line w the sixth werer. then again to a dead end structure at the groum level at the far end.

The self-supporting type of tower was selected for use with this antenna. It is equipped with a bridge arm, its length 150 ft . over-all-fixed to the top of the tower. The insulators carrying the antenna wires are suspended from the lower face of this bridge. Many reasons entered into the decision to use this type of tower, three of which may be mentioned here. One consideration was the average height of the antenna wires. With a group of similar antenna wires, equally loaded, suspended on a springstay between two towers, the height above ground of the point of suspension of a wire decreases as the distance between this point and the nearest tower is increased. With a similar group of wires suspended from the bridge arm of a tower, there is no similar variation.

Another engineering consideration was the variation in antenna constants caused by high winds. The suspension of the group of antenna wires from a springstay slung between the tops of two masts or towers, has been used at our New Brunswick, Marion, and similar stations. It has been found that whenever there is a high wind blowing across the antenna wires, the springstay assumes a new position varying with the strength and direction of the wind. With gusty winds of high velocity, this change of position is continuously occurring. There is, in addition. the variation in the position of the antenna wires due to the cross wind on the wire span between the springstays. The result of these changes in position of the wires is that the constants of the antenna circuit change, and detune the antenna from the alternator which is operated at an accurately regulated wavelength. The resulting fluctuations in radiation have been so great at times as to seriously impair the commercial effectiveness of this station. Now, with a fixed point of suspension, such as the tower bridge arm, the only variations in position of the wires are those due to the wind on the wire span between the towers. Those due to the variation in the position of the springstay are not present.

The antenna circuits at all of our stations are equipped with variometers to correct for these changes and our experience is that the variations are less severe with Radio Central type of antenna than with that of New Brunswick.

As Long Island is well within that zone of the Cnited States in which sleet and glare
formation must be expected on all structures exposed to the weather during the winter months, provision has been made to melt such ice as may form around the antenna wires. The heating current for sleet melting is supplied from the power house, at 60 cycles, through special transformers and reactances. The antenna wires are connected together at the far end of the circuit. By opening switches at the power house end of this circuit, the wires can be discomnected from the radio frequency feeder circuit and the 60 cycle power circuit can be connected. If the several downleads were connected directly to the antenna wires throughout their length the path of the heating current would be short circuited. Two satisfactory methods have been used to avoid such short circuit. One method consists in dividing the wires into four groups and connecting only the wires belonging to one group at each of the four intermediate points. At both ends, all wires are connected. The other method consists of making the connection of each wire through a specially designed condenser.

The inductors used at each downlead of the multiple tuned antennas are installed without any protection from the weather. This type of installation has proved satisfactory except at some locations close to the sea where the spray from the sea water deposits salt on the insulators.

The standard outdoor coil is shown in Fig. 3. Fig. 4 shows coils housed in frame structures lined with copper.

At stations where more than one antenna circuit is installed, attention must be given to the disposition of the several antennas and of their individual feed circuits in order to minimize their mutual interaction. In enlarging or remodelling an existing station, it is not always expedient to attempt to bring all antenna circuits to the close proximity of the power house. This is particularly true of a station where the original antenna circuit is of umbrella design and where a second antenna circuit is to be installed, which can be operated simultaneously with the first and on a long wavelength differing from that of the first by only a few per cent. Such a situation confronted us at our Tuckerton station. The space immediately surrounding the power house was occupied by the umbrella antenna, which was in continuous commercial use. The new antenna could be erected on some vacant land just beyond the boundary of the space occupied by the umbrella antenna provided this antenna circuit could be fed
with power at radio frequency from the power plant. The study of a transmission line that would be suitable for supplying to this antenna from the power plant, 200 kw ., at frequencies of around 18,000 per sec. with little loss on the line, disclosed that this was quite practical. The antenna has been erected, this high-frequency line has been installed and the circuit has been operated very satisfactorily now for over a year. The power delivered to the antenna circuit is 92 per cent of the power supplied to the line.


Fig. 3. Standard Outdoor Inductor Coil for Multiple Tuned Antennas

The success of this type of antenna feed circuit will have a profound effect upon the design of stations operating two or more antenna circuits simultaneously.

## Grounding System

The first decision to be made in the development of the ground system was whether it should be of the buried wire type, or the type known as "counterpoise" or "earth's green." The New Brunswick station has a ground system combining counterpoise and buried wires. Experience had shown that while the counterpoise type might be ideal, from a theoretical point of view, it would be undesirable from the point of view of practical maintenance.

A counterpoise consists of a network of wires mounted on poles. These wires carry fairly high potential and the failure of any one wire will cause interruption of service until the fault is located and repaired. The overhead system of wires is also undesirable because it is an obstruction, making the maintenance of the overhead antenna wiring


Fig. 4. Coil Similar to That of Fig. 3, but Housed in a Frame Structure Lined with Copper
difficult and expensive. Theoretical considerations indicated that a buried wire system"would be as effective as an insulated counterpoise provided that its dimensions and design were carefully planned with reference to the character of the soil.

To determine the basic factors for the design of a buried ground system, measurements were made of wave propagation on wires of different lengths buried in the Long Island soil. As a result it was found that the velocity of wave propagation on a wire in this soil is about one-tenth of the velocity of wires suspended in the air. It was found, furthermore, that the resistance of the wire is a function of the wavelength. With ircreasing
length of the wire, the conductivity increases as a linear function $u_{p}$ to a length of onequarter wavelength, where it reaches a maximum, after which it becomes a periodic function of the wavelength and the length of the wire. The results of these measurements showed that the maximum length of wire which could be used effectively must be something less than one-quarter wavelength of the wave propagation in the buried wire.

Measurements of wave propagation in the buried wires indicated that while lengths as great as 1200 feet could be used economically in the Long Island soil, it was furthermore determined, through calculations of the electric field distribution around the antenna, that 76 per cent of the clectric lines of force radiating from the antenna would be collected by these ground wires if they were made 1000 feet long. One thousand feet on each side of the center line of the antenna was therefore considered sufficient; the result is that the Long Island antenna, in effect, stands on a plate of copper 2000 feet wide and 3 miles long, and therefore the functioning of this antenna is made independent of the resistance of the soil.

The combined antenna and ground system offers a total equivalent resistance to the antenna currents of only 40 hundredths of an ohm, made up as follows:

| Radiation resistance at 16,500 meters |  |
| :---: | :---: |
| Ground resistance | ms |
| Tuning coil resistance | .15 ohms |
| Conductor resistance | 0.05 ohms |
| Insulator and | . 0 |

Total.
0.40 ohms

The unit is operated with 200 kw . in the antenna, and the antenna current is 700 amperes, resulting in a radiation of 60,000 meter amperes.

A special plow was constructed by which the wires could be laid cheaply. The plow carried a coil of wire. It had a blade which introduced the wire in the ground at a depth of twenty inches. The plow was drawn by two Ford tractors.

The ground network consists of wires each 2000 feet long buried in the ground a depth of 15 to 20 inches in lines at right angles to the line of the antenna with the center point of the ground wire under the center line of the antenna. The ground wires are spaced 10 feet apart and as the antenna is 7500 feet long there are therefore 750 such wires making the total length of buried wire approximately
$1,500,000$ fect. The gromed wires are conneeted to a heavy matergromed bus which runs in the ground inater the center line of the antemat There is also an acrial bus feeder which is comected to the buried bus through induction reactances in such a manner as to make all pathis to ground of equal reactance, resulting in ergual distribution of the antemat current (1) all sections of the ground system.

## Constancy of Wavelengths

A factor of great importance is that of maintaining the frequency or wavelength radiated absolutely constant for reasons that will be referred to later. In radio stations using high-frequency generators of the alter-
therely eliminated. Speed fluctuations due to changes in the power supply are not so easily disposed of however. A portion of the generator output is utilized to energize a tuned circuit of low resistance adjusted to have a natural period slightly different from the frepuency at which the generator is maintained so that if the alternator frequency varies only a few hundreths of one per cent in one direction, there will be a large increase in the current in this resonant circuit, or if the variation is in the other direction, there will be a correspondingly large decrease. A portion of the eurrent in this resonant circuit is rectified and we are thus provided with a direct current which varies up or down practi-


Fig. 5. Section of Speed Control Ammeter Chart of the New Brunswick Station


Fig. 6. Section of Speed Control Ammeter Chart of the Radio Central
nator type the speed of the alternator determines the frequency of the waves radiated. In many other forms of transmitters the frequency is affected by the antenna constants if not actually controlled by the antenna, with the result that as the antenna wires are blown about by wind, and ground and insulators are affected by dry, wet or frosty weather, changes in frequency will constantly occur. In the case of the alternator the problem resolves itself into maintaining the driving motor at constant speed regardless of voltage or frequency fluctuations in the power supply or the telegraph load fluctuations to which it is subjected by the alternator. This is accomplished by a system of relays operated in synchronism with the telegraph key by means of which the voltage applied to the motor terminals and the resistance in series with the wound rotor is varied so that the motor torque is always just equal to the load to which it is applied. Tendency to change speed on account of the telegraph load is
cally instantaneously with the slightest change in the alternator frequency. This direct current is made to control the voltage supplied to the motor terminals reducing the voltage to counterbalance a tendency towards increase in speed and vice versa. In order that there may be a visual indication of what is going on, a recording ammeter is inserted in the rectified current circuit; a fine straight line on the ammeter chart indicates a constant frequency, a thick line indicates small and continuous variations of frequency, and so forth. Under usual conditions of operation, irregularities of the ammeter chart line can be included within two parallel lines $1 / 8 \mathrm{in}$. apart representing maximum frequency variations not exceeding one in 5000 or 4 cycles per second, or 3 meters when operating at 20,000 cycles and 15,000 meters.

Fig. 5 is a section of speed control ammeter chart from the New Brunswick station; the irregularities in this chart are due to various adjustments being made while in operation.

Fig. 6 is a section from a speed control ammeter chart for one of the transmitters at the Radio Central Station.

Fig. 7 is the corresponding section of the wattmeter chart of the same transmitter.

## Receiving System

The centralized recciving ss-stem is located at Riverhead, Long Island. The antenna is of a new type which gives uni-directional reception. This system is so oriented as to receive signals from the over-ocean transmitter and annul signals from all other directions, including the powerful home transmitter nearby.

- The antenna consists of two copper wires strung on ordinary poles like a telephone line. and extending over a distance of mine miles ( 15,000 meters). This antenna feeds a num-
loops, and the other by Alexanderson describing a system of open wires halanced against each other.

In this development the eontrolling idea is a mental picture which we now have of the nature of the disturbance which we wish to suppress. We call it "static" because it was assumed, in the past, that it was of the nature of static electricity. The hypothesis which is the basis of our modern work is, however, different. We imagine the ether as a disturbed ocean with waves of every length rolling in from all directions. These waves are of the same nature as the signal waves. Those disturbing waves which are of different wavelength from our signals can be shut out by the same means as we use for shutting out other signals, that is, by tuning. But the disturb-


Fig. 7. Section of Wattmeter Chart of the Radio Central
ber of separate receiving circuits of different wavelengths without the slightest mutual interference or weakening of the signals.

Important as it is, from the point of view of centralization, to be able to receive an indefinite number of signals from the same antenna, the greatest importance in the use of this new receiving system is its remarkable properties of suppressing atmospheric disturbances or the so-called "static" which hitherto has been the bane of radio communication. The attainment of these results is not an accident; it is the result of development work covering a number of years. The "wave antenna" as now used in Riverhead is the practical answer to the receiving problem of today. The principle of directive reception has almost unlimited possibilities, and, by economic laws, the receiving system should be developed along these lines until its cost begins to equal the transmitting system. Then will the total cost of a complete circuit, transmitter and receiver reach its ultimate minimum. However, this economic balance is far from reached as yet. The principles of reception by long antennas were laid down in two papers presented to the A.I.E.E. in 1919, one by Weagant describing a system of balanced long
ing waves which have the same wavelength as our signal and are in all respects of the same nature, pass through our tuning system like the signal. We must therefore find some basis for discrimination other than wavelength.

If we can construct a receiver which is sensitive only to waves coming from one direction, then we can shut out waves from all other directions, even if they have the same wavelength. This idea started us on the work of directive reception. Theoretically, there is no limit to the improvement attainable in this direction. We might build a receiving antenna focussed on one transmitting station in Europe, but such receiving antenna would cover a very large area.

A complete theoretical analysis of the wave antenna has been given in a recent paper this year before the A I.E.E. by Messrs. Beverage, Rice and Kellogg. For those who wish only to understand the characteristics of our modern receiving system, in order to make use of it, the following popular explanation may be of some guidance.

Imagine the antenna to be a long, narrow lake, and that the wind is the incoming signal, and further that a cork floating on the waves of water that beat against the shore is the
detector. If the observer stands at one end of the lake, he will observe waves beating against his shore only when the wind blows lengthwise to the lake and from the end opposite to this location. When, on the other hand, the wind blows from his end of the lake, the beating waves appear at the opposite end, while his shore is calm. This, at least, would be the ease if the lake has smooth sand beaches on which the waves could spend their energy without reflection. But, if the lake ends have steep rocky shores, the water waves will be reflected back and forth and thereby make the surface of the whole lake rough. The wares, which indicate the "signal wind," would thus appear at both ends of the lake, regardless of the longitudinal direction of the wind. This reflection must be avoided. The wave antenna is therefore made with ends corresponding to the sandy beach. The antenna terminates in a resistance which is carefully adjusted to absorb all save encrgy and reflect none. The practical advantages of the use of the wave antenna are the elimination of about 90 per cent of the extraneous disturbances known as static.

A valuable practical feature of the form in which the wave antenna has been developed is the method of reflecting the signal so that the "surge resistance" which absorbs the static can be located in the receiving building. This is accomplished by erecting a two-wire line and making the same two wires function both as an antenna and as a transmission line for radio frequency waves. The two wires in parallel act as the antenna. At the far end of the line they are connected together through the primary winding of a special transformer. One end of the secondary of this transformer is connected to the middle point of the primary winding; the other end is connected to ground. The secondary winding feeds the current back into the two wires in series as a transmission line and a second transformer at the front end of the line couples the transmission line to the receiving set. The midpoint of the transformer winding connected to the lines is grounded through the "surge resistance." By this connection, the windings on the two halves of the transformer are opposed for currents flowing over the two wires in parallel; that is, for the antenna effect, and produce no effect upon the receiver.

The resultant reception characteristic curve shows that reception residuals of static of a few per cent may occur in certain directions in the back area of the diagram. The residuals are practically negligible in most cases, but when there is very strong interference or strong sharply directional static in their
general direction, an appreciable improvement may be obtained by balancing the residuals to absolute zero for some particular direction in the back area. This is illustrated by Fig. 8 .

The final balancing of static and interference is accomplished by the use of an artificial line. This line is fed by currents coming from only the same direction as the undesirable residuals. The phase of these currents may be made anything desired with respect to the phase of the residuals in the secondary of the transformer to which the surge resistance is


Fig. 8. Directive Curve of Wave Antenn ${ }^{2}$
connected. By making the intensity of the voltage on the artificial line the same as the residual voltage intensity, and by making the phase displacement 180 degrees, the residual currents are readily balanced for any particular direction in the back area.

With this antenna system, extremely satisfactory multiplex reception is being carried out at Riverhead. Six sets of receiving equipment are normally coupled to this one antenna system, and the signals on six transoceaniccircuits are separated by tuning, and copied simultaneously, each independent of the electrical operation of the other sets.

For the purpose, the antenna output transformer is built with several secondaries and the artificial lines are made up to accommodate a number of receiver sets. Many precautions are necessary in the design and.
arrangement of the receiving equipment to eliminate cross talk and "beat note" interference between the different sets. With this end in view, an equipment for reception of long waves has been completely remodelled.

In the first place, all of the different elements in each receiving set must be thoroughly shielded. The tuning inductances are all balanced pairs of coils placed in an inner shielding of copper to eliminate the losses in the iron casing of the outer shicld. In spite of the shielding, cross talk and beat note interference occurred until suitable chokes and
complete unit on a shelf and the shelves are arranged in three tiers on the racks. The Riverhead station is equipped with three racks making space for the accommodation of nine receiving sets.

Fig. 9 gives the general view of the receiving equipment.

The signals received from the wave antenna are strong; so usually a total of four stages of amplification is sufficient to bring the intensity of normal European signals up to a strength that is rather uncomfortable to the ear.

Since all the local long wave stations, except Marion, are cither


Fig. 9. General View of the Receiving Equipment at the Riverhead Station behind or in the case of Rocky Point, at right angles, to the direction from which the European signals come, directive reception alone lowers the intensity of the local stations so much that tuning can easily eliminate their interference. Interference as strong, for instance, as that from Marion, can be eliminated when the wavelength differs by not less than 3 per cent. For interference of considerably less intensity than that from Marion, as for instance, that from stations in Europe, or from a local station, reduced by directive reception, a 2 per cent difference in wavelength is sufficient.
filters were placed in both the positive filament and positive plate leads of all coupling tubes, amplifiers, detectors, and oscillators.

The receiving apparatus is arranged in line with the antenna input panel at one end and the audio-frequency output panel at the other end. The intervening units are placed in correct sequence so that the signal currents pass in progressive order along the line through all the various unitsfrom input to output panel without looping back over this same path.

The elements of a set are mounted on a sub-panel which is placed in an iron box, the front door of which may be opened. All adjustments of tuning and filament control which are likely to be made frequently on a set tuned to a fixed wavelength can readily be made without opening the front door of the iron boxes because such control handles are mounted on the outer doors in such a manner as to engage with the controls on the sub-panel when the iron door is closed.

These receivers are set up on racks holding three sets per rack. Each set is arranged as a

For wavelength difference of 2 per cent and less the constancy of frequency of the transmitting station becomes of very great importance. Extremely good frequency regulation at the transmitting station will allow the use of filter circuits by means of which interference on wavelengths differing less than 2 per cent from that of the desired signal can be eliminated.

The receiving station at Riverhead, L. I., is about 70 miles east of New York and the next phase of the problem was the automatic transfer of the radio signals to the central control office in New York City in order to eliminate the double handling of traffic, the slowing up of the circuit, and the other delays inseparable from the older system. The requirements of this circuit were studied and then the American Tel. \& Tel. Co. was requested to provide a suitable tone circuit from Riverhead to our Broad Street office, New York City. For a period of several months experiments were conducted over this temporary line, during which it was demon-
strated that it was feasible to send these tone signals over a $7(1)$ mile cirenit without detriment to the readability of the signals. Contimotos commeretal operation over a single tone circuit was started about July I, 1921. Subserfucntly additional tone circuits were built for the commsercial operation and control of Riverluad station in this manner.

## Central Operating Room

The operating room at the city offices is the place where the written message is converted to the dot and dash of the Morse code. The continental cole is used in radio as in all other international telegraphic communication. During the last lew years a great change has taken place in the transmission of the message. Whereas formerly the mantally operated telegraph key was used almost universally for speeds of transmission of 40 words per minute or less, this has been entirely displaced by the machine transmitter. The advantages of machine transmission over hand transmission are (1) that the operator is required to work a typewriter keyboard only and need not necessarily be a skilled telegraphist; (2) that one operator can transmit messages in this manner at rates $u p$, to 100 words per minute. whereas the best that can be done by hand is 35 or 40 words per minute; (3) that all characters are perfectly formed and do not vary with the different operators, and (4) the machine is tireless and has no lost time. The telegraphic manipulation is actually accomplished by first punching the message on a paper tape and subsequently passing the punched paper tape through the mechanical transmitter which is an automatically operated telegraph kes.

The transmitter sends telegraph impulses over the control wires between the city office and the transmitting station and operates the relay system at that station.

In order that a check can be kept on the performance of the automatic transmitter, the control wires, and the relay system of the transmitting station, a radio receiving set is provided at the city office which makes audible or visible to the operator the actual signal being transmitted into the ether. This receiver is a very simple piece of apparatus, since the reception of the signal from the nearby hand power transmitter is not at all difficult, although of course, as there are so many transmitters operating in one locality with only small wavelength separation, very efficient tuning equipment must be provided.

The reception of a message at the city office requires a reversal of the above process. The signal as received at the receiving station is in the form of audio frequency current, the
frequency of which is variable as desired, these signal currents are transferred to the city office by telephone wires. At the city office it is necessary to further amplify the currents before they are introduced into the telephone or the recorder. It is possible to use aural reception at speeds up) to 35 or 40 words per minute. Better speeds can be secured at times by a combination of aural and recorder reception. At speeds over 40 words per minute tape reception must be used exclusively. It is possible for some tape readers to copy as fast as 60 words per minute but generally for speeds over 40 words per minute, the work is divided up among an increased number of operators; 40 to 70 words per minute two operators; 70 to 100 words per minute three operators, and so forth. The development of the tape recorder used for transoceanic radio reception was ably described in a paper presented to the Inst. of Radio Engineers by J. Weinberger in 1921.

The electrical equipment of the operating room of a city office, handling a large number of circuits, requires careful planning. In the city office of the Radio Corporation of America at $6 \pm$ Broad Street, New York City, there are at present in continuous operation,

6 transoceanic receivers
( 6 load Monitor receivers
6 automatic transmitters
and over 30 land wires. To these will soon be added a number of new services.

Power supplies of different types are provided for the various electrical and mechanical devices and measures have been taken to prevent inductive interference effects between instruments.

## Wavelength Distribution

The economical wavelength for communication over a certain distance can be selected by the practical rule that the economic range of a station for reliable communication is about 500 to 1000 times the wavelength. If too short a wave is selected the signals will be weak in daytime and strong but variable at night. This variation is most noticeable during the period when darkness exists over the area between the communicating stations. In some parts of the world it is possible to use short waves to advantage because the absorption is comparatively lower than on long waves and variations are unimportant but generally speaking for distances over 3000 miles the reliability of wavelengths of over 11,000 meters is so much greater than that of shorter waves. Long waves have therefore been universally adopted for long distance communication.

It can now be readily seen that since the ability to receive distinct signals depends on the separation of different frequencies there is a definite limit to the number of "channels" of communication between stations that can be sct up.

If the wavelengths between 11,000 and 22,000 meters are divided into 2 per cent bands there are 3.5 "channels." If into 1 per cent bands, there are 70 " channels." Except to such extent as directional reception will permit the number of one way channels open for such long distance commmnication is limited to the number of these bands.

If we suppose our plans to be based on the use of 1 per cent bands, it is evidently necessary first that each transmitter shall cause no radiation outside of the 1 per cent band allotted to it and furthermore shall maintain its actual radiation frequency exactly on the center of such band; and second that each receiver shall be capable of separation of currents from those differing only 1 per cent in frequence. The above requirements imposed upon the transmitter have already been proved practicable. But the realization of the full possibilities of radio communication requires that all transmitters of antiquated type which take undue space in the ether be replaced.

There are, however, other difficulties that cannot be so easily overcome. For instance, while it is quite possible for the receiving station to separate currents of frequencies differing 1 per cent if the voltages induced at the station at the different frequencies are equal, it is not an easy matter to separate the currents when the voltage induced in one case is 1000 times the voltage induced in the other. This is the situation where in the case of a transatlantic circuit the receiving station in America receives from Europe on 15,000 meters and the transmitting station in America sends to Europe at the same time on 15,150 meters. In such cases, as described above, it is necessary to increase the separation between frequencies to 3 per cent and in order that such large separation may not be too numerous a rule has been established by precedence and informal agreement, that all the transmitters in one locality shall transmit on wavelengths close together. We have such a case in the concentration of American transmitters between 16,000 and 17,500 meters. In this band of wavelengths there are operating at present the following stations:

15,900 meters Tuckerton No. 1 Transmitter
16,300 meters Kahuku No. 1 Transmitter
16,465 meters Radio Central No. 1 Transmitter
 16.97 .5 meters Kahuku No. 2'Transmitum
16.97.5 meters Amapolis Compernsatmpy Wave Ate
17.14. meters Amapolis Sigmalling Wrave Are
1T, 000 meters Radio Central No. 2 Transmitter
It is planned to operate transmitters in Siveden, Poland and Argentina in the near future on wavelengths 15,000 meters w 19.000.

The French Government station at Lyons operates at 15,500 meters and there are a number of additional European and American transmitters operating between that wavelength and 11,000 meters, while other (iovernment and Commercial stations in France are at present operating at wavelengths from 19,000 to 22,000 meters.

The congestion of the ether is therefore not a mere matter of looking into the future, but a real present-day problem. The necessity for traffic regulation at least suffices to prevent reckless driving so to speak, is just as apparent as the undesirability of hidebound regulations until such time as the limit of possible improvements in technique have been more definitely determined.

Such is the present situation in the long distance radio ether. The congestion is due to the necessity for the use of the longer waves for long distance work and the fact that all high-power stations are broadcast stations; much improvement is possible in existing practice but radically new methods of operation must also be considered, such for example as directional radiation on shorter waves. With the realization of such possibilities the situation will take on a new aspect.

## Project of New Communications

Sufficient statistics are now available by means of which the technical and financial possibilities of new circuits of communication can be accurately predetermined.

Fig. 10 shows the daily. monthly and yearly reception curves for a typical transatlantic circuit. The ordinates of these curves show the capacity of the circuit at the different times of the day and year respectively. By the capacity of the circuit we mean the practically possible speed of reception in fiveletter code words per minute. The capacity of the circuit is a function of the strength of the signal and the intensity of the disturbance. The intensity of the signal is measured in absolute units of microvolts per meter. Fig. 11 shows a typical daily curve of variation of signal strength.

Experience has shown that under any given condition of atmospheric disturbance, there is a direct proportionality between the strength of the signal measured in microvolts per meter and the traffic capacity of the cir-


Fig. 10. Daily, Monthly, and Yearly Reception Curves for a Typical Transatlantic Circuit


Fig. 11. TypicallDaily Variation of Signal Strength and Disturbances Measured on a Simple Vertical Antenna
cuit measured in words per minute. The proportionality defined above is almost exact between the limits of oral reception ranging from 5 to 40 words per minute and it can be
considered as substantially correct up to the highest speeds that are used. This simple relation between strength of signal and words per minute has given us a practical method of measuring the intensity of atmospheric disturbances.

As an actual standard method of measurement an artificial signal is introduced into the recciving system and regulated so that the capacity of the receiver is 20 words per minute. The number of microvolts per meter which must be introduced to permit reception at 20 words per minute is thus a direct measure of the intensity of disturbance.

If a transmitting station is to be designed for a new geographic location, measurements of disturbances are taken in that location. The results of these measurements, which may be taken over a large part of a year, show what strength of signal will be needed during the different months of the year to carry a desired traffic. Fig. 12 shows a typical chart of this kind. Comparison between this chart and the known typical yearly chart for a transatlantic circuit gives a direct indication of the capacity of the new circuit in terms of the circuit in operation. The chart for the projected circuit shows the capacity of a 50,000 -meter ampere and of a $100,000-$ meter ampere transmitting station.


Fig. 12. Typical Yearly Readability Chart
A: East-West Circuit
B: North-South Circuit; 100,000 m.a.
C: North-South Circuit; 50,000 m.a.
Thus it can be stated that guess work has been eliminated from the developments of radio communication, and that sound foundations, both technically and financially, can be laid for all future expansions of our system.

# Testing Transformers for Central Stations 

By A. B. Hendricks, Jr.<br>Transformer Engineering Department, General Electric Company


#### Abstract

Tests of the dielectric strength of electrical equipment are as essential in its maintenance as in its manufacture. Such tests to be reliable, however, should be made with apparatus designed for the purpose. Ton much is at stake to warrant an operating company placing reliance on makeshift paraphernalia, even though there may not daily be occasion to make such tests. For those who are concerned with the subject, the following article will be of great assistance. It calls attention to the necessary qualifications for reliable insulation testing and describes the various equipments standardized for this purpose and for high-current testing.-Enitor.


The routine and special tests of apparatus and cables commonly carried out at central stations require testing transformers and auxiliary devices of a wide range of capacities and characteristics. Standardization of testing apparatus is desirable, alike from the standpoint of the maker and user, but so far has appeared almost impossible. The legitimate requirements show large variations, but the great number of special sizes and styles that have been furnished central stations reflect the ill-considered fancies and lack of foresight of engineers and operators and result in an excessive amount of special designing with consequent slow delivery and high cost. It is intended here to discuss the desirable characteristics of such apparatus and to describe representative testing sets, with a plea for the elimination of freak designs as well as those differing slightly from standard. The statements are necessarily of a general character because of the special nature of the problem.

## General

The service requirements and characteristics of testing transformers differ widely from those of the usual trepes designed for power and lighting and are met by a distinct form, although there are similarities in fundamental structure. Many of the salient features of large power transformers were first developed and used in testing transformers. The special features are:
(a) High voltage.
(b) Low kilowatt capacity.
(c) Low reactance.
(d) Short time rating.
(e) Small size and weight.
(f) Means for varying and measuring voltage over a wide range.
(g) Ability to withstand short circuits and high-frequency oscillations.
The general form and many of the parts have been standardized and some parts such as terminals are made in quantities and carried in stock.

The standard frequency is 60 cycles, but 50 cycles is used for most sets for foreign countries. Many designs are made so they may be used at either frequency.

Standard ratings run from $3 \mathrm{kv}-\mathrm{a}$. at 30,000 volts to $500 \mathrm{kv}-\mathrm{a}$. at 500,000 volts with a large variety of intermediate ratings and special designs.

The high-voltage current is usually 0.1 to 0.5 or 1.0 amp . except for alternating-current cable testing where it may be of the order of $3 \tilde{\mathrm{amp}}$. at 30,000 or 60,000 volts representing 1000 to $2000 \mathrm{kv}-\mathrm{a}$.

The reactance is about five per cent. This is the result of a large core and few turns in the winding, giving a substantial construction, voltage stability on the usual leading current, great accuracy of the voltmeter coil, and high power in the test circuit. It tends to small size but great weight, and for portable outfits a smaller core and higher reactance are sometimes necessary.

High-voltage tests seldom last longer than 1 to 30 minutes. The time ratings are usually from 1 to 4 hours for a $50-\mathrm{deg}$. C. temperature rise, but may vary from less than 1 second to continuous operation. At the higher voltages the limit is set by dielectric losses and danger of insulation failure rather than by the actual temperature of the winding.

Voltage variation may be obtained by field control and series-parallel connections of the generator (which is considered the best method) or by induction regulator, tap transformer, or series-parallel connections of the high-voltage transformer.

Sometimes a larger power generator is available, with field control. In this case some means of limiting the power and quickly opening the circuit is necessary, or a breakdown of the material or apparatus under test may be disastrous.

A separate generator of about the same rating as the transformer makes an ideal arrangement, but it is also the most expensive.

Perfect wave form under all conditions of load, power-factor, and excitation is the indispensable characteristic and is best
attamed hy a groncrator with a revolving field of eylindrical form having a distributed winding in słots, rescmbling at onntinuous-current armature. A mumber of short-circuited fied coits or, bettor still, a complete short-circuited spuirrel cage in the same stots compensates for ammature reaction and prevents wave distortion. Such a machine efminates many corrections and uncertanties in testing and is well worth its higher cost.

The driving motor may be of a capacity onc-half to one-third that of the generator as the power-factor of the load is always low. Direct comnected induction, synchronous, or direct-current motors are all satisfactory but the last gives exact speeds, variable over a considerable range which is sometimes desirable.

High speeds (1200 to 1800 r.p.m.) tend to small size, low cost, close regulation, and grood wave form.

High excitation, that is, at or above normal, gives stability of voltage and wave form and high power in the discharge circuit.

Unsatisfactory results follow an attempt to use a generator at normal current and low excitation. Distortion of wave form is accompanied by low power in the high-voltage circuit, and when arcing over or puncturing insulation a destructive high-frequency oscillation is set up, which may not be followed by a dynamic arc because of a sudden drop in voltage. If the voltage can be maintained sufficiently to form a dynamic arc, the oscillations are largely suppressed, as the are short circuits the transformer. This applies more particularly to the testing sets of high power and voltage when used in tests such as those on line insulators, high-voltage terminals, and switches.

Transient oscillations lead to erratic results in testing, and are a disturbing factor to be avoided as far as possible.

It should be obvious that the best results are to be attained with any apparatus when operated at or near its normal rating, but many engineers do not seem to realize this. It is recommended that transformers be not used at less than one-fifth of normal voltage. This is an arbitrary figure, representing nothing but a compromise. At lower ratios the voltage becomes unstable, 5 per cent normal reactance representing 25 per cent at onefifth voltage and this is particularly undesirable with leading loads.

Series-parallel transformer windings are often used on both sides of testing transformers, but complicate the construction and
increase the size and cost. Double primaries and secondaries are practicable but to be awoided at voltages over $1.50,(0)(0)$

Fontr primary (low-voltage) windings are sonnctimes used to give four voltage ratios; 100 , 50 , $331 / 3$, and 2.5 per cent of maximum rating. It is lecter to use four circuits on the generator giving the ratios $100,75,50$, and $22^{\circ}$ per cent as the 75 per cent ratio is more useful than the $3: 31 / 3$ per cent.

Induction regulators are employed for voltage variation more often than other devices and are generally made for the full range from zero to maximum. 'This means that the transformer must be wound for double the line voltage, since the regulator cloubles the voltage; a point often overlooked.

The fear is sometimes expressed that with leading loads the series impedance of the regulator may give resonance difficulties, either with the fundamental frequency or the harmonics. The value of the impedance is too low for such effects, and no trouble from this source has been reported.

Sometimes the voltage is controlled by generator field and induction regulator, but this represents an unnecessary duplication of function. Series-parallel armature windings of the generator insure operation at or near normal excitation and render additional devices unnecessary. The regulator impedance and exciting current would be likely to affect the wave form more than a small variation of generator excitation.

For cable testing there is some excuse for series-parallel high-voltage windings on the transformer, as these may be required to give large current at fractional voltage. In this case all the high-voltage leads are brought out to terminals on the cover and internal connection boards are never used. This is really a simpler, more compact construction, and more convenient in use.

## Generator Testing

Ordinary testing transformers of medium capacity and about 30,000 volts suffice for high-potential tests of generator armatures and fields, except in large sizes. The kilovoltampere capacity required in the transformer varies so widely with the rating of the generator that no rule for determining it has been made. Medium and large size alternators for either steam or water turbines require from 25 to $100 \mathrm{kv}-\mathrm{a}$. or more at 60 cycles and voltages up to 30,000 .

Low-speed water turbine alternators take the largest charging current of any. Table I
gives results of actual tests on representative armatures.

For ordinary generator armatures up to $1000 \mathrm{kr}-\mathrm{a}$. . the charging current is of the order of $1 / 4$ to ${ }^{1} 2$ amp. These figures apply to tests from one phase to the other two and core.

## Cable Testing

High-voltage cables many miles in length take a charging current, and require a kilo-volt-ampere capacity in the testing transformer much greater than might be supposed (sometimes ruming into the thousands at double voltage and nomal frequency).

The charging currents for threcerore cables vary with the nature of the connections, approximately as follows:

Test between 3 cores and sheath $=100$ per cent current

Test between 1 core and (2 cores and sheath $=5.5$ per cent current

Test 3 -phase (per core) $=38$ per cent.
The charging current is proportional to frequency and voltage and this has led to the suggestion to reduce the cost of the testing apparatus by reducing the frequency. This is fallacious because the cost per kilovolt-ampere increases as the frequency decreases. In

TABLE I

| Kr-a. | Speed | voltage |  | Frequency | Trans. Kvoa. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Rated | Test |  |  |
| 7000 | 90 | 13200 | 27400 | 36 | 422 |
| 33333 | 1800 | 14000 | 29000 | 60 | 100 |
| 700 | 900 | 13200 | 27400 | 60 | 50 |
| 1400 | 720 | 6600 | 14200 | 60 | 34 |
| 187 | 138.5 | 4000 | 9000 | 60 | 25 |

While the formulas for calculating cable constants are well known, they are given in a variety of inconvenient and confusing forms in the reference books and are therefore inserted here in the form which has been found most useful.

The electrostatic capacitance of a singlecore cable is:

$$
C=\frac{K}{59 \log _{e} \frac{R}{r}} \text { microfarads per } 1000 \mathrm{ft}
$$

$K=$ Specific capacity of insulation
= (approx.) 3 for paper, 4 for varnished cloth, 5 for rubber
$R=$ Inner radius of sheath
$r=$ Radius of conductor
The charging current is:
$I=0.377 C E$ at 60 cycles
$I=$ Amperes (effective)
$C=$ Microfarads
$E=$ Kilovolts (effective)
The maximum voltage gradient is:
$G=\frac{E}{r \log _{e} \frac{R}{r}}$
$E=$ Applied voltage
$G=$ Voltage gradient in same units as $E, R$, and $r$.
There is no simple expression for capacitance, or maximum stress in a three-core cable.
general, nothing is to be gained by reducing the frequency below 50 or 60 cycles, and these values are recommended.

Cable testing sets are usually built singlephase although three-phase sets are occasionally used for the sake of speed in testing threecore feeder cables.

Since the load is practically at zero powerfactor 90 -deg. leading current, the terminal voltage will be increased by the reactance of the transformer and regulator or generator. This may be compensated in the rating of the generator, transformer, and single-phase regulator, but not in a 100 per cent raise and lower three-phase regulator. The reason is that voltage variation is by simple addition and subtraction in a single-phase regulator, but by phase rotation in a three-phase regulator.

In the latter case, if the primary and secondary voltages are made unequal the test voltage cannot be reduced to zero by the regulator alone.

## Balancing the charging current by parallel inductance

The leading charging current of the cable may be balanced by the lagging exciting current of an inductance connected in parallel with the cable thus reducing the kilovoltampere capacity required in the generator. regulator and transformer. The two currents
being nearly in opposition, the resultant is small and in practice the kilovolt-ampere capacity of the supply circuit and apparatus is reduced to 20 per cent or less of the kilovoltamperes represented by the cable charging current.

An inductance for cable testing resembles an ordinary testing transformer but has a series of small air gaps in the middle leg of the core, a high-voltage winding with taps, and no low-voltage winding. The standard ratios of kilovolt-ampere capacities are:

Inductance; 100 per cent cable load, with taps down to 40 per cent.
Transformer: 20 per cent load.
Regulator; 10 per cent load.
Gencrator; 20 per cent load.
This combination gives 0 to 100 per cent capacity, literally it gives 120 per cent, but the inductance is always made 100 per cent and the 20 per cent transformer capacity, which really adds to it, covers any lack of balance which may exist.

## Air-gaps in Transformer Core

Transformers are often made with air-gaps in the core, proportioned for 50 per cent exciting current; the high-voltage winding being of 100 per cent capacity, the low-voltage of 50 per cent, regulator 25 per cent, and generator 50 per cent.

The currents in the low- and high-voltage windings, throughout the range of operation, are then approximately as follows:

| high voltage |  | Low voltage |  |
| :---: | :---: | :---: | :---: |
| Amp. <br> Per Cent | Phase | Amp. <br> Per Cent | Phase |
| 50 <br> 100 | Lead | 50 | Lag |

Such a transformer will carry full-load current on the high-voltage side, only when it is leading. It will carry no lagging high-voltage current without overloading the lowvoltage circuit.

The input to the transformer with 50 per cent exciting current is 50 per cent of the load, with the balancing inductance it may be 20 per cent or even less.

Danger of resonance has been suggested in connection with the inductance, forgetting it is intended for current resonance and being in parallel with the cable can do no harm.

## Cable Testing by direct current

A high-voltage three-phase cable 10 miles in length may require a capacity in the testing
apparatus of the order of 10,000 to 15,000 $\mathrm{kv}-\mathrm{a}$. at 60 cycles.

Recluction of frequency is of no assistance in this problem, but with a direct-current testing set the case takes a new aspect. It has been found possible to maintain 1.5 miles of 33,000 -volt cable at 100,000 volts, directcurrent, with a steady input of 50 watts.

The hot-cathode rectifier or kenotron has been applied for this purpose and a number of these outfits are now being used by central stations.

Direct-current testing sets for 100 and 200 kv. are practically standardized. These are composed of the following main parts:

A high-voltage testing transformer is used with induction regulator for voltage control. Transformers vary in capacity from 5 to 50 $\mathrm{kv}-\mathrm{a}$. and 44,000 to 88,000 volts. A 60 -cycle 220 -volt source is the most suitable for all excepting the largest sizes when 440 or 2300 volts may be used. Supply voltages above 440 increase the cost and decrease the safety in handling.

The kenotrons used are standard 250-milliampere tubes with a 50,000 -volt direct-current rating. For sets of 50,000 volts or less a single tube is used. For higher voltage sets, two or more tubes in series are used so as to limit the voltage across each tube to a safe value. The filaments of the tubes are supplied from individual filament transformers insulated for the maximum voltage at which the tube operates. Rectification of one-half of the wave is generally used but the sets are often supplied with a second set of kenotrons to rectify the other half of the wave for testing three-core cables.

A power limiting reactance for protecting the kenotrons in case of cable failure and during fault reduction is usually placed in the low-voltage supply circuit.

A small capacity ( 2.5 to $10 \mathrm{kv}-\mathrm{a}$.) transformer of moderate voltage ( 2.5 to 10 kv .) is frequently used for completing the burning down of failures to a low-resistance ground.

With larger sets a switchboard is used, mounting crest voltmeters for indicating the direct-current test voltages and ammeters for reading the values of direct current in the various circuits.

The question which first arises is: What is the ratio of direct to alternating voltage for the same test results? There is not, and in the nature of the case there cannot be, a definite an iwer to this question. The first assumption would be that the direct voltage should be the same as the crest value of the
alternating voltage for the test desired, but in practice the ratio has been found much greater than this, except n some ideal cases where the maximum value alone was the determining factor such as in using a sphere-gap.

Present practice favors a direct voltage of over two times (in some cases 2.4 times) the effective alternating test voltage in cable tests. Conditions vary so much that no definite rule can be given for general application, but the type of cable insulation and other


Fig. 1. 200 -kv-a., $75,000 / 150,000$-volt Transformer
factors (such as the temperature of the cable at the time of test) must be taken into account. It has been found that the direct voltage must be higher than was originally expected.

Roughly, in short-time tests the dielectric strength of solid insulating materials varies more or less as the square root of the thickness for alternating voltage and more or less directly as the thickness for direct voltage, which means that the direct-current testing set must give very high voltage when used for breakdown on the best type of cable for 33,000 volts or more working pressure.

The direct-current set is lighter, less expensive, and requires less power for operation than the alternating-current set, but is more complicated and delicate in construction and operation, requires about the same space and
does not give exactly the same test as alternating current. For long high-capacity cable, it is the only available and practical means for making tests.

In operation the voltage is brought up gradually so as to prevent a rush of current. When the cable is fully charged the load will be small since the current is limited to the leakage loss current.

## Transformer Design

A high-voltage testing transformer of typical design is shown in Fig. 1 as it appears when taken from its tank. This is one of a set of three built for three-phase tests in a cable factory, but gives a good idea of the construction of the whole series of sizes and styles.

## Core and Tank

The core is of the vertical three-legged type, all windings being on the middle leg, which is cruciform in cross-section and composed of three widths of plates. The core clamps are steel channels held by throughbolts insulated with fiber tubes and washers. The core is suspended from the steel plate cover by hangers made from steel channels or I beams. The hangers are made as short as possible, the length being determined by the distance needed for the terminals.

The tank is round, made of steel plate, with electrically welded side seams and flanged steel plate base, riveted and welded. A steel angle band is riveted around the rim of the tank, the rivet heads being welded on the inside and serves for bolting on the cover. A large number of hardened head cap screws and nuts are used for the bolts. The rim of the tank projects slightly above the angle band and is machined for a soft gasket, together with the under side of the cover at this point, to make an oil-tight joint. A single large eye-bolt is placed at the center of the cover for handling by a crane.

## Winding and Insulation

The primary or low-voltage winding forms a thin cylinder surrounding the middle leg of the core and insulated therefrom by a cylinder of shellac-paper. The secondary or high-voltage winding consists of a series of disk coils of several turns per layer, wound on foundation rings of shellac-paper and insulated by one or more wraps of black varnished cloth tape. Paper ribbon is used for layer insulation. All the coils are dried in vacuum, impregnated with rarnish, and baked before
applying the outside tape. The major insulation between primary and secondary is formed of a series of concentric cylinders of shellac-paper interleaved with cylinders of back varnishod cloth. The eloth projects at the ends where it is split and turned over to form flanges, interleaved with the moukded presshoard shields composing the main insulation between high-voltage winding and core.

This particular transformer is wound in two 75,000 -volt sections and one terminal of one section is brought out to a film cutout on the cover, for connection through an ammeter to ground, while there are one 150,000 -volt and two 75,000 -volt terminals.

A voltmeter coil reading direct in kilovolts is placed between, but thoroughly insulated from, the two high-voltage sections and connected to a terminal board on the cover and also to ground. A protective choke coil, made of bare aluminum wire wound on a treated wood frame, is supported from the 150,000 -volt terminal.

Pressboard collars and coil spacers insulate the high-voltage coils from each other and allow oil circulation. The main high-voltage coils are wound as single sections and connected alternately at the inner and outer edges.

Several coils at each end of each section are reinforced, the line coil being of heavily insulated copper strip, wound one turn per layer.

## Voltmeter Coil

A coil of few turns, so placed as to embrace the same flux as the average turn of the highvoltage winding, will indicate the high voltage with great accuracy regardless of load or power-factor. The ratio of turns with the high-voltage winding is usually 1 to 1000 or 2000, thus reading direct in kilovolts or half kilovolts.

The usual impression seems to be that this coil will not be correct at low power-factors, but it should be obvious that there is at least one location in which the resultant flux linkage (main flux plus the leakage flux added vectorially) will be the same per turn of the voltmeter coil as for the average turn of the whole high-voltage winding so that it must read correctly, neglecting second order differences, which are negligible.

These differences, such as the resistance of the voltmeter coil and high-voltage winding and the distributed nature of the reactance, are extremely small. Tests show that the
voltmeter coil indicates the induced high voltage with a greater accuracy than any other practicable methorl, that the difference between the induced and terminal voltage may be kept below $1 / 2$ of 1 per cent, and that even the wave form is reproduced with great fidelity: Either the effective or crest value of the voltage may be read on suitable instruments, but it is not claimed that transients maty be so measured. For these a ball sparkgap is universally used and connected through a resistance of $1 / 2$ to 1 ohm per volt, directly across the high-voltage circuit.

## Terminals

The high-voltage terminals were expressly designed for testing transformers and represent a distinct and original type. Relatively small size and high arcing voltage are essential for this work where extreme high voltage is coupled with low kilovolt-ampere capacity.

The terminals are of the semi-solid type. A steel tube is heavily insulated with shellac paper forming the core of the terminal. This is wrapped with black varnished cloth which is formed into flanges much as in the transformer itself.

The insulated core is inserted in a metal ground sleeve forming the supporting flange, and completed by the addition of the outer $\mathrm{c} v$ linder of shellac-paper and the hollow cast aluminum alloy cap. The whole is then given a vacuum treatment and filled with "vaseline" (petrolatum).

The central steel tube ends some distance from the lower end of the terminal and connection to the windings is made through a heavily taped connecting rod. The insulation thus extends from the cap clear into the windings so that the lower end of the terminal may be short and placed close to grounded metal.

The large radius cap permits close grouping and the final result of the design is that terminals of very high arcing voltage may be placed close together and close to the core or tank without danger of arc-over. Fig. 2 shows where the terminals are placed at the edge of the cover and close together. The arcing voltage is about 200,000 for the small terminal and 300,000 for the large one. When arc-over occurs, as in testing the terminal, it is not preceded by corona or sparking and the arc goes wide of the terminal, hence does no damage.

The terminal boards for the low-voltage winding, voltmeter coil, and grounded end of the high-voltage winding are of fiber with nickel plated brass unions.

## General Characteristics

Round tanks are standard for single-phase and are relatively short, the depth varying from one to one and onc-third diameters. Extra radiating surface when needed is j)rovided by the addition of ontside tubes.

All testing transformers are shipped oilfilled, and are made as nearly air and oil tight as possible by gaskets at every opening in the cover and close spacing of all bolts. The design is compact and it is seldom necessary to remove the terminals for shipment


Fig. 2. $150-\mathrm{kv}-\mathrm{a}$., $75,000 / 150,000$-volt Transformer
though all of the vaseline-filled type are designed for easy removal, without disturbing the internal connections.

The high-voltage coil stack is clamped and centered by set screws at each end passing through the flanges of the core channels. In the larger sizes additional support is given by cast iron or steel brackets held by the main core bolts.

Flux densities are moderate, to avoid wave distortion from the effect of harmonics in the exciting current acting through armature reaction in the generator. Ordinary generators may give good wave form at zero load but show bad distortion on small load if the exciting current contains a large proportion of third and fifth harmonics.

The internal capacitance of testing tramsformers of 100,000 volts and higher is so preat and the magnetizing current so low that the exciting current is usually leating at all wht ages.

The high-voltage conductor is seldom less than 0.010 in . in diameter, which is goond ion 0.1 amp .

It is difficult to wind large diancter conils with fine wire which is liable to mechanical injury and open circuits and is not suitable for the thick conductor insulation required for high dielectric strength between turns. Wire 0.010 in . in diameter might be userl up to 150,000 volts, but larger wire would be used for higher voltages regardless of current capacity, for facility of winding and handling, mechanical strength, and better insulation possibilities.

The ability to put many turns in small space is of little advantage because it leads to a concentration of voltage too great to be safe, since the volts per turn is high. This requires subdivision of the winding into many narrow coils of little mechanical strength. At the higher voltages, the capacitance of the transformer itself plus that of the apparatus under test may take a charging current exceeding 1 amp . and in general, to allow for this, the current capacity should increase with the voltage at the rate of at least 0.1 amp. per 100,000 volts.

Since the current capacity of the high-voltage winding may exceed the normal rating and is preferably made high, a great increase in rating may mean little more than a large low-voltage conductor, which signifies little, and a higher reactance, which may be important. A $300-\mathrm{kv}-\mathrm{a} .300,000$-volt transformer is practically identical with a $150-\mathrm{kv}-\mathrm{a}$. unit except for the reactance which may be double.

Grounding the middle point of the highvoltage winding halves the voltage stresses from winding to ground and reduces the size, weight, reactance, and cost. Grounding one end permits tapering the insulation from maximum to zero and eliminates one highvoltage terminal.

Full insulation with two high-voltage terminals represents the most inefficient and expensive construction and is seldom necessary.

The ratios of cost for the three forms are about:

Center grounded; 66 to 75 per cent
End grounded; 100 per cent
Ungrounded; 125 to 133 per cent.

## Preferred Standard Ratings

Frequeney; 60 or 50
Kilovolts; 30, 50, 100, 150, 200, 250, 300, 350
Amperes; ro, 1/4, 1/2, or 1
Supply voltage; 220,1150 , or 2300
If an induction regulator is used the transformer low voltage rating must be double the supply voltage.


Fig. 3. Standard, Oil Testing Set

Testing transformers and auxiliary apparatus exhibit refinements in design, construction, and finish not usually associated with this class of equipment. Reliability is the most important requisite, but great care is taken to obtain simplicity, compactness, close regulation, low flux densities, good mechanical construction, and attractive appearance.

## REPRESENTATIVE SIZES AND TYPES OF TESTING SETS

High-voltage, Alternating-current Sets for General Testing
The frontispiece of this issue of the Review shows a general view of a series of sizes of testing transformers and auxiliary apparatus
set up in the shop in which they were built. It includes the following:
:3-kv-a. 30,000 -volt oil testing set
5-kv-a. 50,000-volt Portable set
$10-\mathrm{kv}-\mathrm{a}$. 100,000 -volt Laboratory transformer
7.5-kv-a. 75,000-volt Precipitator transformer
$10-\mathrm{kv}-\mathrm{a}$. 100,000-volt Precipitator transformer
$150-\mathrm{kv}-\mathrm{a}$. 300,000 -volt Insulator testing transformer
$61 / 4,121 / 2$, and $25-\mathrm{cm}$. ball spark-gaps.

## Oil and Insulation Testing Set

Fig. 3 represents a thoroughly standardized 60 -cycle set, made in quantity and considered indispensable in all electrical installations of any magnitude. It consists of a $3-\mathrm{kv}-\mathrm{a}$. 30,000 -volt transformer, a $1-\mathrm{kv}-\mathrm{a}$. induction regulator, giving the full range of voltage from zero to 30,000 , and a standard oil testing spark-gap, removably mounted on the highvoltage terminals.

The high-voltage winding is entirely insulated so that tests may be made either with or without a ground connection.

A voltmeter coil gives accurate indications of the high voltage, which may also be determined approximately from a graduated dial


Fig. 4. Oil Testing Spark-gap and Stand
on the regulator shaft, when the low-voltage is known, and the load small, as in oil testing.

The whole outfit weighs about 500 lb . and is mounted on casters. It is not limited to oil testing, but the voltage, capacity, and reactance are suitable for a wide range of testing and experimental work about a power station, on generators, motors, other transformers, insulating material, rubber gloves, and so on.

The current capacity is not sufficient for testing cables except in short lengths.

## Oil Testing Spark-gap

The oil testing spark-gap is shown in Fig. 4 mounted as a separate unit, which is sometimes convenient when operated from a transformer other than the standard oil testing transformer.

Fig. 5 shows the spark-gap alone. It is made in identical halves, each consisting of three pieces of simple symmetrical form and massive proportions. The body is turned from the highest grade of hard rubber plate and threaded to receive the adjustable studs forming the electrodes; flat, square-edged disks, 1 in. in diameter. Both studs and micrometer locking nuts have index marks. The pitch of the thread is 20 per inch and gap settings may be made from zero to 0.25 in . in steps of 0.05 in ., the standard setting being 0.100 in . or two turns of the screw. The setting is determined by the index marks, no gauge being necessary.

This form of spark-gap is the result of long evolution and has been adopted as standard by the leading transformer manufacturers of the United States. It is anticipated that it will soon be officially adopted by the American Society for Testing Materials and possibly abroad also. It conforms to the requirements of the National Electric Light Association and the American Institute of Electrical Engineers.

The best form of spark-gap has been the subject of much discussion and elaborate comparative tests. It is generally admitted that the present standard combines the greatest


Fig. 5. Oil Testing Spark-gap
number of desirable features and is the best in accuracy, sensitiveness, simplicity, reliability, and consistency of results.

## 5-ki-a., 50,000-volt Set

The next most popular size is shown in Fig. 6 mounted on a ball-bearing truck with regulator and circuit breaker. One end of the high-voltage winding is connected to the tank and but one high-voltage terminal is required.

This is the usual arrangement for central station work where the apparatus under test is grounded.

A film cutout at the ground terminal permits the insertion of an ammeter directly in the high-voltage circuit.


Fig. 6. 5 -kv-a., 50,000 -volt Portable Testing Set

## 10-kv-a., 100,000-iolt Set

The unit shown in Fig. 7 has the middle point of the high-roltage winding grounded, which reduces the size and cost and permits the use of small treated wood terminals. It is especially suited for laboratory work or portable testing sets when small weight is an object and the apparatus or material under test may be insulated from ground.

## $7.5 \mathrm{kv}-\mathrm{a} ., 75,000-\mathrm{volt}$ Set

Fig. 8 shows an interior view of a unit originally built for operating a Cottrell precipitator, but it is essentially the same as a testing transformer, except that there is no voltmeter coil and the high-voltage winding is entirely insulated.

## 75-ki-a., 100,000-iolt Set

Fig. 9 is of a unit of the same type, built for continuous operation with a tubular tank, oil gauge, and thermometer. The exterior is shown in Fig. 10.

An interior view of a lypical testing transformer of medimm size is shown in Fig. 11. One end of the high-voltage winding is grounded through a film cutout. 'The domed cast-iron cover is sometimes used but it is suitable only for a (lefinite mumber and size of terminals. Steel plate corers must be used for special designs.
"Jhe exobiting primary has thesamenumber of taras as the main primary and is permanently commected in parallel with it. The exciting secondatry has the same number of turns as the primary, but is located adjacent to the line end of the main secondary and the two have a common connection to the high-voltage terminal. The other end of the exciting secondary connectsto an additional insulated conductor run-


## 150-ki-a., 250,000-iolt Set

Several units, Fig. 12, may be connected in series for the higher voltages by the use of extra primary and secondary windings in each unit for exciting the next in the series. This scheme is known as the "chain connection" and is illustrated in Fig. 13. Fig. 14 shows one of the units, which externally can hardly be distinguished from an ordinary design.

Previous designs for series connection and excitation have given poor results because of excessive reactance, voltage instability, and low power in the high-voltage circuit. The present method overcomes these disadrantages in the following manner:

Each unit has, in addition to the main primary low-voltage and secondary highroltage winding, additional primary and secondary exciting windings.
ning through the high-voltage terminal. The lower end of the main high-voltage winding is connected to the tank through a film cutout.

The primary and secondary exciting windings are separated by the main high-voltage insulation, but are in close inductive relationship, so that the next unit in the series may be excited through windings of low reactance.

All the units are identical but the second and following units must be placed on insulating supports since the tanks are at successively higher voltages to ground.

The load on the exciting windings decreases through the series toward the high-voltage line, and the exciting windings of the last unit are not used.

Special features, not clearly shown, insure low reactance and protection from high-voltage transients.

This is a flexible and economical arrangement, enabling the use of a few comparatively small, low-voltage units for obtaining very high voltages, with one end or the center of the series connected to ground, as well as a three-phase connection with grounded neutral.

It is applicable particularly to testing sets of high voltage and low capacity.

300,000 -volt units are used in series with the neutral point grounded for obtaining $\mathrm{f} 0(0,0) 00$ volts for tests on strings of suspension insulators.

Voltages over 300,000 volts are more easily obtained by the use of several 250,000 -volt units in "chain conncetion" as already described. This has the advantage that operations may be begun with one 250,000 -volt


## 150-kv-a., 300,000-volt Set

The unit shown in Figs. 1.5 and 16 is of a popular size and type, much used for tests on line insulators and experimental work. One end of the high-voltage winding is grounded so that but one high-voltage terminal is required. The tank is 65 in . in diameter and 84 in . high over the cover.

The voltmeter coil is of the so-called differential form, wound partly inside and partly outside of the high-voltage winding. The errors of the two parts are of opposite sign and made to neutralize as nearly as possible.

## j00,000 Volts and Higher

Central stations seldom require voltages above 300,000 volts, although sometimes two

[^42]unit and the capacity of the testing set may later be increased by the addition of one or more 250,000 -volt units to obtain three-phase combinations or voltages to ground up to 1,000,000.

The voltage to ground of any combination may be doubled by duplication of the apparatus so that eight 2.50 .000 -volt units could be operated in series with neutral grounded to give $2,000,000$ volts between lines.

So far no reference has been made to the $1,000,000$-volt, three-phase outfit of the Pittsfield Works of the General Electric Company as this was fully described in the Journal of the A.I.E.E. for October and November, 1922, and the General Electfic Review of December, 1922, and February, 1923*. However, it may be of interest to add some of the latest results obtained with this outfit.


Fig. 13. "Chain Connection" for $1,000,000$ Volts to Ground


Fig. 14. Exterior of Transformer Shown in Fig. 12


Fig. 15. $150-\mathrm{kv}-\mathrm{a} ., 300,000$-volt Transformer


Fig. 16. Exterior of Transformer Shown in Fig. 15

Fig. 18. Same Arc as Shown in Fig. 17, but Photographed through a Lens made of
Quartz produced in the Thomson Research Laboratory of the General
Electric Company

Fig. 20. Same Arc as Shown in Fig. 19, but Phetographeal thonath

Fig. 19. Fourteen foot, One-and one half Million-volt Are, through Glass Lens

Photographs of Arc and Corona taken with Glass and Quartz Lecnses
Fig. 17 shows a nine-foot million-volt are to ground between points as taken with a glass lens: and Fig. 18 shows the same are taken through a quartz lens.

The glass lens, being opaque to ultra-violet rays, shuts off much of the corona but, being highly corrected, gives sharp defination. The quartz lens is transparent to ultra-violet rays, but being a simple lens cannot be corrected as with glass and gives a blurred effect.

Since quartz has uniform optical constants, it is not possible to combine several grades to


Fig. 21. 800,000-volt Corona, through Glass Lens
neutralize the principal aberrations as is done with glass. Even so, a quartz lens is something like five times as fast as glass and transmits perhaps a thousand times as much ultraviolet light, extending the effective spectrum over double the range of visible light.

The quartz lens was made from fused quartz produced by the Thomson Research Laboratory of the General Electric Company at West Lynn.*

Fig. 19 represents a fourteen-foot arc between points at about $1,500,000$ volts, taken with a glass lens. Fig. 20 is the same arc taken with the quartz lens. There is a great difference in the amount of corona shown on the choke coils mounted on the million-volt terminal.

[^43]The difference between glass and quart\% is brought out in a still more striking manner by comparative photographs taken on a pinwheel, mounted on ball bearings on the top of the $1,000,000$-volt terminal. The wheel is three feet in diameter, consisting of four aluminum wires with the ends bent tangent to the circumference of the wheel and pointed. When voltage is applied the wheel revolves at considerable speed from the reaction of the discharge from the points.

Fig. 21 shows the corona as taken through a glass lens from a point 23 ft . directly above the wheel which revolves in a horizontal


Fig. 22. 800,000-volt Corona, through Quartz Lens
plane. The exposure was 15 seconds and the voltage 800,000 .

Fig. 22 is of a photograph taken under the same conditions except that a quartz lens was used. The width of the band of corona is about five times as great as with the glass lens.

Fig. 23 shows a photograph of 900,000 -volt corona taken through a quartz lens with the same exposure.

At low voltages the difference in the appearance of the photographs taken through glass and quartz lenses is considerable; but it was supposed that the difference would be much greater at the higher voltages and this is horne out by the photographs. which indicate that it is necessary to use a quartz lens in taking photographs of arc and corona phenomena if the whole effect is desired.

Fig. 24 is of 500,000 -volt corona, taken through a quartz lens with an exposure of five minutes.

Alternating-current Cable Testing Sets
200-ki-a., 10,000-volt Set
Of relatively high capacity and low voltage, the unit shown in Fig. 25 is built in the interleaved disk coil type and is compact and of great simplicity.

## 40-kv-a., 26,400-volt Set

A portable set with induction regulator and switchboard all mounted on a truck with ball-


Fig. 23. 900,000-volt Corona, through Quartz Lens
bearing rubber-tired wheels is shown in Fig. 26. The transformer has a high-voltage winding in four sections with eight terminals.

## 132-kv-a., 24,000-volt Set

An unusually elaborate set with two ballbearing reels, each carrying 100 ft . of $24,000-$ volt cable, is illustrated in Fig. 27.

600-ki-a., 30,000-iolt, 3-phase Set
The transformer shown in Fig. 28 is operated by a three-phase induction regulator. The series-parallel high-voltage windings require 12 high-voltage terminals.

## 2100-ki-a., 60,000-iolt Set

The high-voltage winding of the unit shown in Fig. 29 is in two sections for series-
parallel connection, one end being grounded through a film cutout. The conductor is of flat strip wound one turn per layer, the same as in a large power transformer. The core has air gaps for 50 per cent exciting current.

300-kv-a., 66,000-volt, Transformer with 1000-ki-a. Balancing Inductance
These two units, Figs. 30 and 32, are intended to be used together. The interior construction of the inductance resembles that of a transformer except that it has taps on the high-voltage winding and there is no low.


Fig. 24. 800,000-volt Corona, through Quartz Lens (5-minute exposure)
voltage winding. The core has air gaps as previously described.

## 125-ki-a., 30,000-iolt Transformer with r00-$k_{i}-$ a. Balancing Inductance

Fig. 31 is of a complete outfit in three units, each mounted on a roller-bearing truck. The inductance carries a ball spark-gap with series high resistance and an ammeter is mounted on an insulating post for direct insertion in the high-voltage line.

## 60-ki-a., 100,000-volt Set

The tank of the unit in Fig. 34 contains the main $60-\mathrm{kv}-\mathrm{a}$. transformer and three filament transformers for heating the cathodes of four kenotrons mounted on the high-voltage terminals. The induction regulator, power

limiting reactance, and threc-pancl switchboard are combined as a separate unit.

## 100,000-iolt Filament Transformer

The illustration in Fig. 33 is from a drawing showing the cross-section of a standard design, insulated for 100,000 volts effective and intended for heating the filament of a keno-
tron in a direct-current cable testing sed Tho tank is 15 in . in dianeter and the kenotron is mounted directly on the terminal in a vertical position.

Fig. 35 shows an outfit for an impulse generator for lightning arrester tests and includes a 100.0000 -volt transformer with four filament transformers and kenotrons


Fig. 31. $125-\mathrm{kv}-\mathrm{a} ., 30,000$-volt Transformer, $700-\mathrm{kv}-\mathrm{a}$. Balancing Inductance and $62.5-\mathrm{kv}-\mathrm{a}$. Induction Regulator


Fig. 32. 1600-kv-a., 66,000 -volt Balancing Inductance


Fig. 33. 1/2-kv-a. Filament Transformer Insulated for 100,000 Volts


Fig. 34. 60-kv-a., 100,000-volt Directcurrent Cable Testing Set


Fig．35． $10-\mathrm{kv}-\mathrm{a}, 200,000$－volt Direct－current Set for Testing Lightning Arresters

## Auxiliary Apparatus

Ball spark－gaps for moasuring the voltage have been standardizer in sizes using $\left({ }^{1}{ }^{1}\right.$ ． 1212.2 .5 and $.0(0-\mathrm{cm}$ ．balls and suitable for 100． 200,300 ，and 500 kv ．respectively．A $50-\mathrm{cm}$ ．Lap of the suspended type is shown in Fig．3i．This is now made with removable leas so that it may be suspended from insula－ tors or stool on the floor as in Fig． 37 ．

Protective choke coils with parallel resist－ ances are mounted on the terminals for the
higher voltages．A conl 37 in ，in diameter for BH，（HO volts is shown in Fig．3s．

In testing a large number of small devices， 11］，to 10.000 volts，it is eonvenient to employ insulaterl handles for the high－voltage leads， but the methorl is dengerous moless suitalble precatutions are taken．


Fig．39．10，000－volt Safety Test Handles

Fig．3：represents a pair of safety test handles showing great refinement of design and thoroughly safeguarded．

The cables have a complete outer sheath of fine braided wires which are connected together and grounded through the bronze chain shown attached to the ground clamp near the transformer terminal end．Each handle has a thumb－operated plunger switch with 10 breaks directly in the high－voltage circuit．This is normally held open by a spring and cannot be left closed．There is a complete grounded sheath between the operator and the high－ voltage conductor，so that only the hardened tool－steel points are dangerous．



Figs. 40, 41 and 42. 250-kv-a., Air-blast High-current Transformer

## High-current Testing

High current at low roltage is often required for tests on instruments, switches, husbars and other purposes.

Figs. 40, 41, +2 show a $2.50-\mathrm{kv}-\mathrm{a}$ air-blast transformer with self-contained fan suitable for continuous operation. The low-voltage coils consist of 12 single turns, each sawed from sheet copper and without joints. One of these is shown in Fig. It and the complete low-roltage winding in Figs $4: 3$ and 45.

The low-roltage coil may be connected in all series-parallel combinations giving from 132 volts 1900 amp . to 11 volts 22.500 amp . The changes are made by loosening the terminal yoke and shifting the bent connecting straps.

Several other sizes of the same style have been made and used for welding, resistance
furnaces, and testing. The alvantages of this type are the simple compact and economical construction, the great range of arailable ratios and ease of changing connections.

## Conclusion

The examples given are of the more usual sizes and types of testing transformers, and those more or less standardized; but numerous and varied as they are, they represent but a small part of the endless variety that has been made and is constantly being increased. It would be tedious and take ton much space even to illustrate the whole series of special designs, but enough has been presented to guide those who may be interested in such devices, but are unfamiliar with the course of development of a highly specialized branch of engineering.


Fig. 43. Complete Low-voltage Winding of High-current Transformer


Fig. 45. Complete Low-voltage Winding of High-current Transforme

# Sir Joseph J. Thomson's Address Before the Schenectady Research Laboratory 


#### Abstract

Sir Joseph J. Thomson's visit to Schenectady was noted in our May issue, on which oceasion we pub)lished a photograph taken in the Research Laboratory of him and others. We now publish the brief address lemade to the Research staff at Schenectaly on the afternoon of April 6,1923 . - EDitore.


Dr. Coolidge:
I am going to dispense with any introduction today, because our distinguished visitor can talk to us only about half an hour. He needs no introduction to us. There is no man in the world who less needs an introduction to the men and women here than Sir Joseph Thomson. Sir Joseph, the floor is yours.

## Sir Joseph Thomson:

Ladies and gentlemen, I feel very acutely that the proper attitude of any visitor to this Laboratory is that of a learner, rather than a speaker. I have learned this morning very many interesting things that I did not know before, and I should like to have spent all my time learning, rather than in attempting to offer you something that I feel is not worthy of the occasion. But I thought perhaps it might interest you if I spoke first for a minute or two upon the efforts that we are making in England to imitate that movement of which you were the pioneers, and are the leaders, of the application of research to industry.

In my country there are difficulties about that, which do not exist here. In many of our industries there are not the important concerns that are capitalized to the extent of the very large firms in America. The backbone of the industry are firms, say, with a capitalization of some 200,000 to 500,000 pounds. Now it is clear that when the industry consists of units of that kind, the number of individual firms who can establish research laboratories on a scale that would promise important results cannot be very many. So the Government came in, and they established a body, of which I am a member, and placed very considerable sums of money at our disposal, and we go to the leading members of the industry and we say, "Won't you combine, and form a research laboratory for the whole industry? If you will do that, your Government will meet you and will pay pound for pound." Well, that has been a sufficient inducement for research laboratories to be established, and I think in between 2.5 and 30 different industries. We do not take any active share after these laboratories are
started, in their management. We leave it entirely to the industry, and we say this-"It is up to you now that the thing has been started, to make it a success. We give you this grant for five years and then we shall come in and make a carcful investigation of what you have done; and if you have done well, help will be continucd if you need it."

Circumstances have not been very fortunate for the start, because when we started we started in a boom, and they could not get men. This was followed by a slump, and they could not get money. So we have had exceptional difficulties to contend with, but I think many of them, or a majority of them, have made good, and I imagine that they have become permanent institutions in our country.

Then again, we had to supply them with trained research workers. There were not enough men in the country, trained in research work, to man these laboratories, so that what we do now is, we say to the Universities, "If any of your graduates, or people who have just graduated, seem to you to be promising, promise to make good research workers, if they get the opportunities, then we will consider providing them with funds for two years' training in research under some Professor whom we approve." In that way we have been able to get a considerable number of men to be trained and to be available, either for these research laboratories, or for posts in Universities.

We have no lien upon their services afterward. If they choose, they are perfectly free after they have received these schoolarships for two years, perfectly free to do as they please. I think that movement has been successful now. We have almost a competent supply of properly-trained workers. This has only been going on for a short time, but it is, as II said, an attempt to keep up what has been successful in this country-the establishment of research laboratories in close connection with industries.

Well, that is a matter of organization. I won't say anything more about that, but I will try to speak about one or two things
which have been happening in the Cavendish Laboratory recently, although $I$ fear it is a poor showing, compared with the very interesting things which I saw this morning. But one thing that may interest you is the work of a young Russian who had escaped from the country and who came to us, and who has developed an old idea into a form which seems to me to promise very remarkable applications. I don't know if any of you have read Plante's original papers on the storage cell, but he in those papers describes a number of very interesting and simple experiments. He used to take two strips of ordinary lead and separate them by canvas, put them in a bucket, charge them up and then discharge. and get immense currents for a short time.

Well, that is the principle which Mr. Capietza has worked upon-the idea that if you used unprepared plates-plates of pure lead-they discharge with enormous rapidity, and so he builds up a storage cell. When it is completed it is not bigger than about the size of a cigar box. He has put a tremendous amount of work into it, so as to have the plates very near to each other, so that there is practically no internal resistance in this cell. Well, that cell is charged up until it is loaded, and then it is short-circuited and discharged. The time of discharge is only something less than $1 / 700$ th part of a second, and so you get the whole of the charge you put in discharged in this extremely short time. The result is that for a short time you get enormous magnetic fields, running up to several hundred thousand Gauss.

That little thing, about as big as a cigar box, will melt when it discharges, a copper rod about as thick as my finger. Well, I think that would probably have very important applications. It seems that the French military people have had something of the kind in their minds for a gun. You see you get a tremendous concentration of energy in this way in a small space; and I think the French have been proceeding on these lines and had this gun in their minds; but I do not know that anything has been done quite so convenient for physical purposes as this battery which Mr. Capietza has made, which is still in its early stages. The line on which he is working is by very careful workmanship to reduce the distances between the plates as much as possible, and have a rery small internal resistance of the cell.

His view is that it is likely to have a very extensive application to producing Roentgen ray photographs for a doctor, to have this
little thing which he charges at the nearest electric light station connected with an especially wound transformer or induction coil; and all that he would have todo wond be to turn a handle. I don't know whether this will materialize or not, but it is evident to anybody who is interested in experiments on electrons or positive rays or anything of that kind, that the power to produce fied of this enormous magnitude is of great importance, especially when it can be done in such a simple way.

I ought to say that it would take very considerable labor and expense to make this battery, so as to get into it the workmanship good enough to produce the best results; but the body to which I have alluded before have taken it up and are financing it, and we hope to get it in a state in which it will be applicable for laboratories and can be applied to any case when we have to produce a very large magnetic field. When you come to think of it, generally when you want a very strong magnetic field you don't want it very long. You want it to deflect things moving very rapidly. Well if they move rapidly they don't stay long in a magnetic field, so that the strong magnetic field is only required for an infinitesimal time, and a little thing of this kind will furnish it.

In some experiments I have been doing myself. on the positive rays, I have been trying to get to the stage when you can do with a single flash for the positive rays, instead of producing a continuous discharge through the gas, and instead of using an induction coil, which keeps a discharge continuously going through the gas, to just use one flash. There is a great advantage in working with one flash instead of with a continuous discharge, because all kinds of complicated compounds are produced by the discharge itself. You see a great number of lines on your photograph which you have every reason to believe are compounds formed in consequence of a discharge passing through the gas. And so it is a matter of interest to try to get the conditions such that one flash would give you a photograph.

Well, a great deal depends upon properly designing the coil. I was sorry to find when I came to consider the question of design, that the best coil would be a rery expensive instrument. But there is one point, that you can do something with ordinary coils-and that is that you must, to get the best results, reach a certain rapidity in breaking the circuit. After you get that, you don't get any

Wencefit. So 1 set to work to try to get the break to work last enomgh to give the lost results. I testad this by Lord Rayleigh's devise I lom't know whe ther you have evor emplosed it here. Vou break the eirenit by simply farms a butlet from a revolver throtagh a finc wire 'That gives a very sharp break. ambl look that metherl for testing whether I got my break up to the required stamelard. It is mot convonient in a laboratory to fire these revolvers and loreak these wires and When 1 got a mechanical break to do as well, I was very drad to employ that, instead of indtulging in this shooting.

Well with that arrangement, I have not got it yet to the stage when I could get a photograph with one llash. I am sure it cottld be done by designing an induction coil of the right size, but what I have done I think is equivalent to it. I have a stream of the pure gas I an investigating flowing through the thing. I take one discharge and then I let it go on and flow for a time, and leave five or ten minutes between each flash, and so give the gas that is in the tube time to get washed out between the two; and I can get photographs with about eight flashes. Now these photographs are very interesting, entirely different (when I say entirely different, they look entirely different) from the photographs you get when you allow discharge to pass through continuously. For example, I took one with Benzine vapor flowing through the tube, and it gave an unusual spectrum. There was the atom of Hydrogen; there was the atom of Carbon; there was the molecule of Carbon; there was a compound of three atoms of Carbon, $C_{3}$. There was $C_{4}$, and there was $C_{5}$, and that was all. If I had taken a continuous discharge, I would have got probably fifty or sixty or more lines of all kinds of compounds of Carbon with Hydrogen; but when you take the flash and just deal with the molecules of the gas put into the tube, you get much simpler results, and results which are much more easily interpreted.

Then again, I tried to test views about chemical compounds, by means of these positive rays. You know that the Oxygen atom has 6 electrons in the outer layer. Nitrogen has 5. Now if you take a positively electrified Oxygen atom, which has lost an eleetron, it has 5 outside. Therefore, the positively electrified Oxygen atom would have an outer layer very similar to the neutral Nitrogen atom. Now when a neutral Nitrogen atom combines, you get a compound with three atoms of Hydrogen; and I wanted to see
whether if you take the positively electrified ()xygen atom, which has five electrons, and therefore room for three more, whether you would get at compostand contaiming three If yheren atoms to one (oxygen. Ifell, trying this experiment, I did. There is a line on the phate corresponding with a molectular weight of l!. It is a very common line, whenever you spark through a mixture of ()xygen and llydrogen. Well then, I thought I would try to go one better.

You can get Oxygen atoms which have lost two electrons-that is, carrying a double charge. In that case you see you only have four electrons left, and they ought to correspond to neutral Carbon atoms. Neutral Carbon atoms can link up with four Hyclrogens, and I wanted to see whether the doubly positively electrified Oxygen atom could link up with four Hydrogens, too. Well, on giving a loner exposure, I found evidence of a line for which $\mathrm{M} / \mathrm{e}$ was equal to 10 . You see the charge is doubled, so $\mathrm{M} / \mathrm{e}$ being equal to 10 meant that MI was equal to 20 , or about 16 plus 4 , so that corresponds to a compound of Oxygen with four Hydrogens. There was no Neon in the tube, and no line for which M/e equals 20 . The only line seen was M/e equals 10. And so you see the essence of this proof is that you only get the 4 Hydrogens when you have taken '2 electrons out of the Oxygen, so that it is only the doubly-charged ones that will exist in the combination represented by the compound $\mathrm{OH}_{4}$.

Then there is another test-suppose you take an atom like Neon. Neon has eight electrons, and therefore does not combine with hydrogen; but suppose you pick out oneyou can get positively electrified Neon atoms with the greatest ease, and these are the Neon atoms that have lost one electron and have seven left. They are like neutral Fluorine atoms and might be expected to combine, therefore, with one atom of Hydrogen. Mr. Aston, who has worked a great deal with Neon, has several plates in which there is a line corresponding to $M$ equals 21-that is, 20 plus 1 , of which the only interpretation seems to be that it is this compound of Neon and Hydrogen. I think there is a lot of interesting work to be done on these inert elements.

I do not believe that inert atoms are inert if you electrified them. If you knock off some of their electrons, I think it quite possible to find lots of compounds of the inert gases with the others. Most of them, of course, would be electrified and not of much use to you, because
an electrified molecule cannot exist in a free state. But it is quite possible that you might get some one that is not eleetrified. The line on which I am trying to work is-suppose you have Neon positively electrified. its atom has, say, seven electrons. And then lake the Oxygen negatively electrified atom- you can get Oxygen electrons negatively electrifiedthis will have seven electrons. Then yon will have the Ncon with seven and the Oxygen with seven also. They will be ahmost like two Fluorine atoms and possibly they may combine. I don't know whether the will or not. I haven't got it yet, but I hope to have another try at it.

Then I have been trying toapply the method of positive rays to determine the nature of any charged atom-whether it occurs with the positive ray or not. For example. what was in my mind was to get some method that will tell you if there are any ions when chemical combination is going on at low pressure. or in combustions, to have some way of applying the method to gases where the ionization was not produced by electrical discharge.

It seems an casy enough thing-one sees how to start. anyhow. You let these combinations, whatever they are, go on in vessels raised to rery high potential, and have a little hole in the ressel and a stream of gas flowing through. Just in front of that you have a perforated tube at a low potential, corresponding to the perforated cathode of the positive ray tube, and you get enough fall of potential to make the ions go along the narrow tube, so as to move in a definite direction.

Well, there came to be a good many practical difficulties in this work. I could not get it to work with photographic plates. We got no traces of lines on the plates. I got, however, results when I replaced the plates by a Faraday cylinder. I only had it working
two or thre days lefore I laft ('ambridee, and I only applied it to tect whether the thing: was working or not. I took the positise column in a diseharge at high pressure and squirted out the gas from that and cxamine it, and found that in the pesitive cotum there are, as far as I can see, no negatively electrified ions. There are clectrons, of course, hut I could not detect amy megatively electrified ions.

I don't want to lay too much stress upon that, because, as I said, I only got the methood to work two or three days before experimenting with it. It is possible that a more careful study of experiments might reveal the existence of some of these negative ions, but I think they are rery small in comparison with the positive. But when we get the thing working it will be capable of a great many applications, to determine the nature of the carriers of positive electricity under all kinds of circumstances. I think if we once get this thing properly schemed and arranged that it will be capable of attacking a good many questions of considerable interest, and I think now it has got to the stage where there is no doubt that it will work.

Well, I am afraid that I have detained you longer than the half hour. but I cannot sit down without expressing my very profound admiration for the work that is being done here. It seems to me there is greater density of interesting things in this building than in any other building with which I am acquainted; and I am very grateful to you for giving me an opportunity of seeing them.

## Dr. Coolidge:

I cannot possibly express to you, Sir Joseph, the love and admiration we all feel for you, but I can thank you as I do, most heartily, for giving us this chance to see you and hear you. TVe hope that you will come again, and come many times.

# Power Developments in Japan 

By W. W. Lewis<br>

Japan has in $7(0)$ yars changed from a fadal state to one of the World Powers. Her influence is extendng. She is trying to maintain what was good in the "old order of things" and at the same time to adopl the most useful features of occidental civilization. Her industries are increasing. Mr. Lewis recently made an extended visit to Japan and tells of her clectrical developments.-EDtor.

The leaders of Japan have a fascinating problem. Theirs is the problem of superimposing on the old Oriental civilization the most useful features of the modern Occidental civilization. This has resulted so far in retaining largely their own morle of living,

Japan has heretofore been free, such as conflicts between labor and capital, a congestion of population in the large cities, and a breaking down of the present family system. It is sure to change the political life of the country as the workers become self-conscious and


Fig. 1. Map of Japan, showing the Principal Transmission Lines in the Tokyo, Nagoya-Osaka, and Kyushu Districts
habits of thought, religion, and system of ethics, and of adopting the mechanical facilities of Western nations. In time the mode of living of a large part of the population is bound to be affected, as Japan gradually changes under the stimulus of its mechanical and electrical development from an agricultural to an industrial nation. This transformation is inevitable and unescapable owing to Japan's resources in water power and lack of other natural resources, its geographical position and the necessity of competing with other industrial nations. Nevertheless, such a transformation will bring with it many evils known to Western nations and from which
demand a share in the government. The influence of the industrial era together with that of other Western innovations, such as the movies and the dance, will in time affect the character of the people, and it is only to be hoped that they do not lose too many of the characteristics which at present differentiate them from other peoples, that is the politeness, courtesy, and the general charm of their home life.

One of the Western facilities which was adopted first in a small way has now grown to tremendous proportions, that is the electrical industry: About one out of every three houses in the Kingdom uses electric light
(although the per capita consumption is not large) and the small home industries use eleetric power to a large extent. Large industries, such as shipyards, steel plants, collieries, spinning mills, breweries, bakeries, etc., make extensive use of electricity and the industrial operations are being rapidly extended in all directions as more and more power becomes available.

## Topography and Climate

The topography and climate of Japan are such that immense water-power resources are available. On the main island, named Hondo, mountains run through the country from one end to the other. In the central part are the Japanese Alps, with numerous peaks having altitudes of 5000 to 12.000 ft ., and in some cases covered with perpetual snow. The rainfall and snowfall in these momntains are copious and the rivers numerous. The distance from the source of the rivers to the sea is in most cases short, so that the drop is quite rapid. This results in a large number of sites for small or moderate size power plant developments. The run-off varies of course throughout the year, being smallest in the winter months. As a rule, there is no great amount of storage capacity, so that the hydroelectric developments will naturally be accompanied by considerable steam development for standby service.

## Power Available

There are three principal industrial districts on the island of Hondo; namely, the Tokyo district comprising Tokyo, Yokohama, and vicinity; the Nagoya district; and the Osaka district comprising Osaka, Kobe, Kyoto, and vicinity. The two latter districts are already tied together in a common power network, and according to plans under contemplation the Tokyo district will be connected to the others in the near future. Unfortunately, the frequency in the Tokyo district is 50 cycles while that in the others is 60 cycles, and this will present an obstacle in the way of free interchange of power between these districts. The island of Kyushu to the south also has a well developed power and industrial district, and in Taiwan (or Formosa) a large power project is being developed. It is difficult to obtain accurate or complete data on the power possibilities in any country and Japan is no exception. However, the following data are from reliable sources and as far as they go are believed to be quite authentic.

Aceording to statistics prepared liy the 1)epartment of Communications of the Japanese Government, there is available in the whole of Japan about $10,000,000 \mathrm{kw}$. of hyolroelectric power. Of this amount about $\mathrm{T}, \mathrm{O}(\mathrm{of}, \mathrm{O}(\mathrm{of}) \mathrm{kw}$. is to be found on the main island (Homdo). It is estimated that about $1,500,000 \mathrm{kw}$. of this power is not economically capable of development. This leaves $5,500,000 \mathrm{kw}$. that can be economically developed. Of this amount about $4,6.00,000 \mathrm{kw}$. is distributed on the rivers of Central Japan, within transmission distance to the Tokyo, Nagoya, and Osaka districts. This power is divided as shown in Table I. Of these rivers, the last named 11 with an aggregate capacity of $2,900,000 \mathrm{kw}$. are considered to have the most economical sites for power development, and of these rivers all except the Kurobe, Kumano and Yodo are either in operation or in some stage of development.

| TABLE I |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| POWER AVAILABLE ON THE RIVERS OF |  |  |  |  |
| CENTRAL JAPAN |  |  |  |  |

In Tables II, III and IV are given a list of the principal hydroelectric power systems in operation and under construction, from data compiled by the Department of Communications in November, 1922. The output in these three districts may be summarized as follows:

| Tokyo District | 241,500 kw. |
| :---: | :---: |
| Nagoya and Osaka Districts | 197,500 kw. |
| Kyushu District. | 62,200 kw. |
|  | $501,200 \mathrm{kw}$. |

This is less than ten per cent of the power available. These figures change from month to month as new projects are begun, but they are sufficiently close to give an idea of the present stage of development. In Taiwan (Formosa) there is a development under way by the Taiwan Electric Power Company involving at present about $110,000 \mathrm{~km}$. The intensive manner in which the rivers are being developed is illustrated by the installed and

TABLE II
TOKYO DISTRICT


TABLE III
NAGOYA AND OSAKA DISTRICTS

| Name of Company and Length of Transmission | Operation <br> Started | POWER STATIONS |  | Output in Kw . |  | SUbstations |  | Transmission Voltage |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Name | $\begin{aligned} & \text { Elev. } \\ & \text { in Ft. } \end{aligned}$ |  |  | Name | E |  |  |
| *Toyamaken |  | Shomeigarva | $3160$ | $\begin{aligned} & \text { No. 1, } \\ & \text { No. 2, } \end{aligned}$ | $\begin{aligned} & 4,000 \\ & 1,900 \end{aligned}$ | Fushiki | 165 | 44,000 | 60 |
| *Tateyama Hydro Electric Co. |  | Shirahagi Nakamura | 3070 |  | $\begin{aligned} & 1,400 \\ & 3,000 \end{aligned}$ | Fushiki | 165 | 22,000 | 60 |
| * Azumi Denki K.K. |  | Saigava | 23.0 |  | 2,400 | Matsumoto | 1930 | 22,000 | 50 |
| Ina Denki K.K. | Tuly 21, 1913 | Otagiri | 3820 |  | 1,350 | Ono | 3300 | 22,000 | 50 |
| Tenryugawa Hydro Electric Co. | $\text { May } 31,1921$ | Toyone | 2.50 |  | 3,450 | Hamamatsu | 132 | 33,000 | 50 |
| Tolagi Hydro Co. | $\begin{aligned} & \text { Feb. } 28,1921 \\ & \text { July } 13,1922 \end{aligned}$ | Shimomura Oshiyama | 20.30 |  | $\begin{aligned} & 4,200 \\ & 2,500 \end{aligned}$ | Toyohashi Okazaki | 316 | $\begin{aligned} & 33,000 \\ & 77,000 \end{aligned}$ | $\begin{aligned} & 60 \\ & 60 \end{aligned}$ |

[^44]TABLE III (Continued)

## NAGOYA AND OSAKA DISTRICTS



## KYUSHU DISTRICT



[^45]propesed plants of the Daido Electric Power Co. on the Kiso River. Aceording to the plans, 16 phants will utilize a total head of 3.46 .4 ft . in a distance of about io miles.

During the present year there will be five systems in operation at 154,000 volts; namely, the Shinvetsu, Keihin, Nippon, Daido, and Tawan Electrie Power Companies. In the future it may eren be necessary to go to 20,000 volts for some of the large power developments contemplated.


Fig. 2. Synchronous Condenser Rated 25,000 kv-a., 600 r.p.m., 11,000 Volts, for Nippon Electric Power Co.

The pioneer high-tension system is that of the Inawashiro Hydroelectric Co., which began operation at 115,000 volts in 1914. Aside from this, and the Gumma Electric Power Company which will operate at 110,000 volts, 66,000 and 77,000 volts are the most prevalent and popular.

## Where Power is Used

The power supply or the three principal districts (which it is estimated require about 70 per cent of all the power demand on the main island) was in Junc, 1922, approximately as given in Table V.

TABLE V

|  | Steam $\mathrm{K} \mathbf{w}$. Power | Vater Power Kw. | Total Present Supply Kw. |
| :---: | :---: | :---: | :---: |
| Tokyo District | 15,000 | 200,000 | 215,000 |
| Nagoya District. | 10,000 | 60,000 | 70,000 |
| Osaki District... | 130,000 | 50,000 | 180,000 |
|  | 155,000 | 310,000 | 465,000 |

According to statistics prepared by the government, the annual rate of increase of power demand since 1911 is about as shown in Table VI. Using this rate of increase of

TABLE VI

power demand, the total requirements for five years and ten years hence may be found in Table VII and Fig. 3.

TABLE VII

|  | $\begin{aligned} & \text { Present } \\ & \text { Supp,ly } \\ & \text { Kw. } \end{aligned}$ | Total Requircment at End of Five Years $K w$. | Total Regirementat Eind of Ten Years |
| :---: | :---: | :---: | :---: |
| Tokyo District. | 215,000 | 315,000 | 415,000 |
| Nagoya District.. | 70,000 | 120,000 | 170,000 |
| Osaka District | 180,000 | 280,000 | 380,000 |
| Total requirement | 465,000 | 715,000 | 965,000 |
| Total increase |  | 250,000 | 500,000 |

Assuming that this is 70 per cent of the total requirement on the main island, the total for the main island ten years hence will be $1,375,000 \mathrm{kw}$. Assuming that the total for the main island is 67 per cent of the total for all Japan, the requirement for the whole of Japan will be $2,050,000 \mathrm{kw}$. At the present time approximately 67 per cent of the power is furnished hydroelectrically. In the future, this figure will probably be nearer 80 per cent, that is, in the neighborhood of $1,600,000 \mathrm{kw}$. will be developed hydroelectrically at the end of ten years.

A start has been made on the electrification of the Japanese Government Railways, the first section to be electrified being that from Tokyo to Kobe, a distance of 374 miles.


Fig. 3. Power Demand Curve for the Three Largest Divisions in Japan

Based on operating experience in the United States, S. T. Dodd has estimated that to electrify all the main lines of Japan, of which there are about 7,000 route miles and 10,000 track miles will require about $135,000 \mathrm{kw}$. operating 24 hours per day, or allowing for a daily load-factor of 50 per cent, about 270,000 kw. of power plant capacity will be required. This electrification will be completed within ten years and the power required should be
added to the figure of $2,0,00,000 \mathrm{kw}$ ．required at the end of ten years for industrial load，and would bring the grand total of power demand to about $2,300,000 \mathrm{kw}$ ，or a three－fold in－ crease over the total power now available．

It is interesting to compare these figures with similar figures for the United States．It is estimated that here there was in 1917 about $20,000,000 \mathrm{kw}$ ．of installed generating capac－ ity．There was available for development about $45,000,000 \mathrm{kw}$ ．of water power，of which about 20 per cent or $9,000,000 \mathrm{kw}$ ．had been developed．There are about 265，000 route miles of steam railway or about 400,000 track miles，and to electrify this railroad would require about $5,500,000 \mathrm{kw}$ ．on a 24 － hour basis or about $11,000,000 \mathrm{kw}$ ．assuming a 50 per cent load－factor．

## Construction Work

The construction of the power plants and transmission lines follows closely that of American practice．The buildings themselves are often ornate and an architectural addition to the surroundings．The masonry work in connection with the dams，canals，etc．，is of a very high class and installed in a permanent manner．

Excavation work as a rule is done by primi－ tive hand methods．Dirt and stones are removed in rope basketssuspended from poles， each carried by two men．Hods carried on the


Fig．4．View of the Shizumo Power Plant of the Daido Electric Power Company on the Kiso River
back and wheelbarrows are often used．Men and women take part in this work and in some cases Koreans are used extensively．A few of the companies now use steam shovels and light gauge construction railroads and these labor saving methods will no doubt come more into use as labor conditions become worse．The Japanese laborer is hard working
and patient hat likes to do things in his own way：Coming from a line of individualists， workers in metal，wood，poreclain，ete．，he has not yet learned to work in groups or to take orders from a foreman．He is also very sensi－ tive to reprimand．The result is that work proceeds with surprising slowness and with an unnecessarily large number of men，according


Fig．5．Method of Excavating by Means of Rope Baskets
to our standards．In spite of this some very reasonable costs are reported for some of the developments．For example，the Daido Com－ pany report approximate costs based on about


Fig．6．Modern Method of Excavating by Means of Steam Shovels；Shinetsu Electric Power Company
$167,000 \mathrm{kw}$ ．of generating capacity in opera－ tion or under construction as follows：

| Generating stations | \＄170 per kw． |
| :---: | :---: |
| Substations． | 38 per kr |
| Transmission lines | 64 per kv |

That is，a total of $165,000 \mathrm{kw}$ ．in generating capacity， $264,000 \mathrm{kw}$ in substation capacity， and 350 miles of double－circuit $7 \mathrm{~T}-\mathrm{and} 154-\mathrm{kv}$ ．
transmission line were hail for appoximately
 it amothe way for the transmission line, 3 and miles of dontile-cirenit line were buith at an arerage cost of sal.010) per mile. These figmese compate fanmably with eosts obtamed for simiar work in the lonited states

The inderieney of the Japanese labor is offse somewhat he its cheapness. Rights-of-way we would also expect to be more reasomable than in the L'nited States. Machinery costs are somewhat greater. Taken altogether, these factors tend to make the cost in the two countries about equal.

## Operation and Government Regulation

The systems are manned by native operators who seem to bequite efficient and capable. Much the same methods are used as in the Cnited States. The native costume is discarded by the operators in favor of foreign clothes, which are more suitable for working around machinery.

There is a rapid trend toward the interconnection and amalgamation of power systems serving the same territory, and the various problems arising from such interconnection are being solved in a very business-like manner.

In Japan all the water-power rights belong to the Government, regardless of whether the banks of the river are owned by the Government. Licenses for water-power development are given by the Governors of the Prefectures (corresponding to our State Governors) with the approval of both the Ministers of Communications and Home Affairs.

The administration and regulation of electrical developments is carried out by the Ministry of Communications in accordance with the Electric Enterprises Law, as follows:
(a) The Power Company applies for a license to the Ministry of Communications, accompanying its application with documents describing the object, the supply area, the general plan of the enterprise, etc.
(b) After obtaining the license the promoter submits plans of the technical construction with a precise description of all the structures pertaining to the development, such as dams, buildings, transmission lines, etc, to the Ministry of Communications. These plans must be approved by the Minister before proceeding with the work.
(c) On completion of the electrical installation, the equipment and lines are inspected and sometimes tested by the Government engineers before operation may be commenced. During operation also the installation is often inspected by the Government engineers.
(d) Regulations for electrical installations are issued by the Ministry of Communications. Those for overhead lines, for example, cover construction,

Chatance from gromat, sats, distance from adjaternt lmidings, highways, ralways, famways, other oserbeal powar homes, and communcation circuits, (-16: Ohars in smimar delatil (o) or the constraction of datms, buildings, installation of spare equipment, (-l

After installation the insulation strength of werhead power lines is subjected (6) the following test:

Operating Voltage
Trest Voltage ble ween Line and Cround for Ten Minutes

13chow 50,000 voles
Donve bo,000 volts
1.i) times the maximum operating voltage.
Max. operating voltage plus $2 \overline{5}, 000$ volts.

For lead-covered cables the foregoing tests are made between each core of the cable and between each core and ground.

Where the neutral point of Y-connected generators or transformers is grounded through a resistance, the test voltages may be reduced as follows:
Operating Voltage

The telephone and telegraph systems of the country are owned by the Government and controlled by the Department of Communications. The proximity of power lines and communication circuits has influenced the whole course of operation of the power systems in Japan. The principal point of concern seems to be not so much the interference with speech as the building up of a voltage on the communication circuit which may be dangerous to men working on these circuits. On this account, although there is no absolute ruling on the subject, it is generally considered that the short-circuit current on a system shall be limited to such a value as not to induce on a neighboring communication circuit a voltage in excess of 300 ; and as a practical interpretation of this ruling, power companies have been in the habit of inserting sufficient resistance in the grounded neutral to limit the shortcircuit current to about 1.5 times the rating of one bank of transformers in the station. It is obvious upon consideration that 1.5 times the rating of a transformer bank will give greatly different values of current depending
on the size of the transformer bank, and also that a certan current in one case maty induce more voltage on communication circuits than a similar amount of current in another case, depending on the proximity of the communication circuit and the length of the parallel. In some cases, therefore, 100 amp. in the ground would have as much effect as 150 amp . in another case. For this reason it seems that some other rule than the present one should be established so that those power companies which are more or less immune from interference should be allowed to increase their ground current, as it is apparent that as much ground current as possible should be allowed to flow in order to facilitate positive and rapid relaying.

Grounding the neutral is done with a twofold purpose, namely, to reduce voltage stress and to produce more positive conditions for relay operation than possible on an isolated neutral system. If too high a resistance is used in the neutral, neither of these objects will be accomplished, and probably also telephone interference will not be eliminated. When there is an arc over an insulator, a charging current passes from the two ungrounded conductors to ground and back through the arc, the current in the ungrounded conductors being increased to about 130 per cent of the normal charging current and the current in the grounded conductor to about 200 per cent of the normal charging current. These currents lead their respective voltages. Now sufficient current must pass through the grounded neutral and the arc to counterbalance the leading current and make it predominately lagging, in order to eliminate the danger of arcing grounds and to permit the relays to operate. If sufficient current does not flow to accomplish this, then the circuit will not be cleared and the arc may become of the nature of an arcing or oscillating ground, with consequent liability of damage to insulation and interference with communication circuits. Thus if the neutral resistance allows only 50 amp . to flow and the charging current in case of a line ground is 200 amp ., then the system is obviously in the class of an isolated neutral system.

It would seem that less trouble would be caused if sufficient current were permitted to pass through the neutral to permit positive and rapid relaying, and this is borne out by the operating experience of many power companies. A number of years' experience with isolated neutral proved conclusively that the extent and disastrous results of transmission
line trouble was vers largely date w armag grounds on these systems. Where is anmakerable evidence to show that the chice canso of permanent damage is due to the heat of the are breaking the porcelan dises, hut that a fair amount o time, say sereral secontls, is required for the damage to ocerwr. It is not uncommon to have an are oceur over a string of insulators due to lightning or other catuse, and when tripped off quickly, say in less than one second, to cause no plysical damage whatever. The line trijss out, is put lack into service immediately, and operation is resumed. This of course is not possible with an isolated neutral system, as a secondary breakdown must occur to cause a short circuit: and in the meantime the original are has been maintained a considerable length of time, and the system subjected to overvolage strain

On systems where the neutral is grounded without resistance, relaying is a comparatively simple matter and relays have been designed to take care of practically all known cases and combinations of lines. Such relaying has proved positive and reliable.

When the system is grounded through high resistance the situation becomes very difficult and none of the usual relays or relay sehemes will operate. This will be readily appreciated from a study of Figs. 7 to 14 .

Fig. 7 illustrates a system consisting of a generating station and a substation connected by two transmission lines. The high-tension neutral of the generating station transformers is grounded without resistance. The normal load current of each of the lines is assumed to be 300 amp . Now with a ground on one conductor at the substation end 2.200 amp. flows into the ground. It is calculated from the constants of the assumed system that the generating station gives 400 amp. and that the remaining 1800 amp . is contributed by generators and other synchronous apparatus at the substation end. The current distributes as shown in Fig. 7a. It is evident that at the substation end, overload, reverse-power, balanced-reverse-power, or balanced-current relays would operate to clear the circuit in trouble and that afterwards the generating station end could be cleared by similar relays.

Likewise for a ground at the generating station end, 3200 amp . flows into the ground, of which 2000 amp . Comes from the generator end and 1200 amp . from the substation end, as shown in Fig. 7b. As in the previous case the line in trouble could be cleared by the proper use of overload, reverse-power. balanced-reverse-power, or balanced-current


Fig.I7a. Two-circuit Transmission System with Neutral at Generating Station Grounded without Resistance. Con ductor of one circuit grounded at substation end. Ground current 2200 amp . Current unbalance between the two circuits $1700-500=1200 \mathrm{amp}$


Fig. 7b. Same System and Conditions as in Fig. 7a Except that Conductor is Grounded at Generating Station End. Ground Current 3200 Amp., and Current Unbalance $2800-400=2400$ Amp.
relays. The initial overload in these cases is from six to nine times and the unbalance between the lines from four to six times the normal load of one line.

In Fig. $S$ is shown the condition with a line ground at the substation end and with sufficient resistance in the neutral ground to limit the short-circuit current to 150 amp . Fig. Sa shows the normal load current, Fig. Sb the distribution of short-circuit current, and Fig. Sc the distribution of line charging current. This latter current was also present (somewhat reduced) in the case of Fig. 7, but in that case it could be neglected as it did not form an appreciable part of the total current.

Now it will be seen from Fig. $S$ that neither the short-circuit current nor the charging current nor their combination is sufficient to operate the ordinary overload, reverse-power, balanced-reverse-power, or balanced-current relays. In order to operate such relays, the overload or unbalance should in no event be less than 600 amp , that is, two times the load current of one line.

Fig. 9 shows the current distribution for a line ground at the generating station end. The conclusions from this case are the same as
from that of Fig. s, namely, that there is insufficient current or unbalance of current to operate the ordinary relays.

In Fig. 10 the condition of Fig, 9 is reproduced with the object of showing in detail how the currents pass through balanced-current relays. In this relay the two outside coils tend to hold down the moving mechanism. When the difference between the currents becomes sufficiently great, the middle coil will overcome the weaker of the two outside coils and cause the contact mechanism to be operated on the side to trip the breaker carrying the heavier current. The vector diagram at the left shows how these currents combine in the three coils. For example, in one outside coil 20 amp . short-circuit current combines with 40 amp . charging current to give about 45 amp . total; in the other outside coil 130 amp . short-circuit current and 270 amp. charging current combine to give about 284 amp . total; in the middle coil 150 amp . short-circuit current and 230 amp . charging current combine to give about 275 amp . total.


Fig. 8a. Two-circuit Transmission System with Neutral at Generating Station Grounded Through Resistance. Load current shown


Fig. 8b. Same System as in Fig. 8a but with Conductor of One Circuit Grounded at Substation End. Short-circuit components of current shown, of which the unbalanced current is $115-35=80 \mathrm{amp}$.


Fig. 8c. Same System as in Fig. 8b except that Charging Components of Current are Shown. No unbalance in these currents

If one line tripped at the substat ion end the full 600 amp . load current would presumably be thrown on the other line temporarily. In this case there would be ( 600 amp. through one outside and the middle coil of the relay, and zero amp. through the other outside coil. In order to prevent tripping the switch of the good line at the generating station end, it would be necessary to have the relay set for a difference greater than 600 amp . It is therefore necessary with this relay, and other similar relays, to have it set so it will not operate on a current less than two times the load current, which renders it useless for ordinary line-to-ground short circuits with the current limited by high resistance.

A so-called ground relay operating on the unbalanced current in the three conductors of one line is sometimes used. This may be set for comparatively small currents. Fig. 11 shows the use of this relay for the case of a line ground at the substation end. It will be noted that there is no difference in the currents in the relays of the good and bad lines, and therefore there would be no discrimination. Both lines would go out if the relays


Fig. 9a. Two-circuit System with Neutral at Generating Station Grounded Through Resistance. Load current shown


Fig. 9b. Same System as in Fig. 9a but with Conductor of One Circuit Grounded at Generating Station End. Shortcircuit components of current shown, of which the unbalanced current is $130-20=110 \mathrm{amp}$.


Fig. 9c. Same System as in Fig. 9b Except that Charging Components of Current are Shown, in Which the Unbalance is $270-40=230 \mathrm{amp}$.


Fig. 10. Application of Balanced Relays to the System Under the Conditions Given in Figs. 9b and 9c, Showing the Effect of Line Ground on the Currents Through the Relay of One Phase Only


Fig. 11a. Application of Ground Relays to the System Under the Conditions Given in Fig. 8b, Showing the Division of Short-circuited Current Through the Relays


Fig. 11b. Application of Ground Relays to the System Under the Conditions Given in Fig. 8c, Showing the Division of the Charging Current Through the Relays
were set low enough. The case of a line ground at the generating station end is illustrated in Fig. 12. Here it is probable that the faulty line would go out due to shortcircuit current and the good line due to charging current. For line grounds between the generating and substation ends there would be equally objectionable combinations of current. It is evident that this relay should not be used on such a srstem.

A special balanced relay has been developed and promises to solve to a large extent the relay problem on such systems. This relay has a current element and a reverse power or directional element. The current element is
atenated be the difterence of eurrent in the wo lines，and the potential coil of the direc－ tional clement is actuated by a potential in phase with the ground current，by taking a protion of the voltage drop across the ground－ ing resistor as shown in F 名g．13．The current flows through the relay in one direction for a ground on line 2, Fig．13a，and in the other


Fig．12a．Application of Ground Relays to the System Under the Conditions Given in Fig．9b．Showing the Division of Short－circuit Current Through the Relays


Fig．12b．Application of Ground Relays to the System Under the Conditions Given in Fig．9c，Showing the Division of the Charging Current Through the Relays
direction for a ground on line 1，Fig．13b， while the potential is in the same direction in both cases．In this sketch the full lines with arrows represent short－circuit currents and the dotted lines with arrows represent charg－ ing currents．The vector diagram at the left shows the direction of the short－circuit and charging currents and their resultant，and the direction of the voltage drop $E_{r}$ ，and its pro－ jection $E_{p}$ on the resultant current．In the case of Fig．13a the voltage $E_{p}$ and resultant current are in phase，and in the case of Fig． 13 b they are 180 deg ．out of phase．The relay has two sets of contacts，one set of which will be closed in the case illustrated in Fig．13a and the other set in the case illustrated in Fig． 13 b ，thus tripping the switch of the line in trouble．The current element of the relay provides a minimum operating point and time delay．Under one－line operation the relay would tend to trip the oil circuit breaker on the line which produced a flow of power
outward from the bus．Normal current with one line in operation would not cause the relay to act as there would be no potential， this potential existing only when current flows through the ground resistance．Inverse time limit overload relays are provided to take care of line－to－line short circuits or bus short cir－ cuits，there being in this case no discrimina－ tion between the two lines．Such short circuits，however，would probably be so rare as to justify the risk of losing both lines．Other means could be provided to take care of line－ to－line short circuits in a discriminating man－ ner such as the use of balanced－current relays in addition to the special balanced relay and in some cases this may be desirable．


Fig．13a．Application of Special Balanced Relay to the System Under the Conditions Given in Figs．9b and 9c，Showing the Effect of a Ground，on a Conductor of Line 2，upon the Currents Through the Relay of One Phase Only．Potential for relay is obtained from a portion of the neutral resistance


Fig．13b．Same System and Conditions as in Fig．13a Except the Ground is on a Conductor of Line 1

At the substation end of the line or at switching stations where the neutral is not ordinarily grounded，potential for the special balanced relay is more difficult to obtain．

This may be done，however，as illustrated in Fig． 14 by the use of three potential trans－ formers connected $Y$ with grounded neutral on the high－tension side and open delta on the low－tension side．The delta is closed through
the potential coil of the relay. In the calse of a line ground a voltage will be produced across the relay coil in phase with the voltage produced at the grounded end of the line be the current passing through the resistor. Another method, for the sulstation end, is to place resistance in the neut ral at this end of the line also and tap off this resistance with potential transformers, the same as at the generating station end.

Even with the type of relay just described, the more ground eurrent allowed to flow the more positively will the relay operate and the more leeway will there be in setting the current elements, the overload relays, etc. So from all standpoints it is desirable to reduce the neutral resistance as much as possible, thereby rendering the whole relay problem much simpler and more flexible.

An effort has been made by the Department of Communications to protect communication circuits from power lines by the introduction of a balancing transformer in the communication circuit as shown in Fig. 15.


Fig. 14. Method of Obtaining Potential for the Relay Used in Figs. 13a and 13b at the Substation End, where the Neutral Resistance is not Available


Fig. 15. Proposed Balancing Coil for Eliminating Interference on Communication Circuits

It is claimed that this has given good results as far as cutting down the inductive interference is concerned, but that such a transformer impairs the efficiency of the telephone transmission. Efforts have also been made by the Electrotechnical Laboratory of the Department of Communications to develop sensitive low-voltage arresters to take care of over-voltage on the telephone circuits.

In the Lated states menther the wephome nor the power systems are operated be the Government. Both of themexist sild be side and stand on their own feer bere the telephone commonication is probally the best


Fig. 16. Power Plant No. 1 of the Inawashiro Hydroelectric Company
and most advanced of any country in the world. The telephone company has a large staff of very able and efficient technicians, and the telephone interests are well protected by these representatives. The result is that there is very little trouble from interference, and when such trouble does arise it is remedied by joint action between the telephone and power company engineers.

From the writer's observation of the Japanese telephone system it seems to be rather out of date and inefficient. Perhaps the remedy for the interference complained of by the Department of Communications is not in hampering the operation of the power systems but in modernizing and placing in first-class condition the communication circuits.

## Conclusion

In 70 years time, Japan has made a marvelous transformation from an isolated feudal state to one of the most powerful and influential countries in the world. Accompanying this transformation has been a change in occupation from agriculture and home industries to the large mechanically operated industries of the modern western world. Mechanically speaking, Japan is therefore only about 70 years old and it is natural that the mechanical sense has not yet been fully developed among the people. Considering the great strides that have been made and the thoroughness with which modern methods are adopted and put into practice, we may expect within the next few vears a wonderful development along industrial and mechanical lines

# Low-power Radio Telephone and Telegraph Transmitter 

By I. F. Byrnes<br>Radol Enginetering; 1)epariment, General. Electric Company


#### Abstract

The articles we have so far published on radio tedephone and telegraph transmitters have described highpower commorial outfis. The low-power out fit described in the following article is of compact size, substamtial construction and is conveniently oporated. It ably fills the widespread need for a telephone and lelegraph transmitter to cover moderate distances. - Ebolor.


A previous article* has indieated the equip)ment available for commercial radio telephony and telegraphy. The transmitter described in the present article is designed for service on yachts or small vessels where only relatively short distance transmission is required, but this equipment also has possibilities as an amateur transmitter.
ing into the transmitter the modulated antenna input rises to instantaneous peak values of 30 to 40 watts. Power for the radio transmitter proper may be obtained either from a kenotron reetifier that uses four 20watt kenotrons (UV 216) or from a motorgenerator. The rectifier operates from a $110-$ volt 60 -cyele lighting circuit.


Fig. 1. Front View of Rectifier and Radio Transmitter


Fig. 2. Rear View of Rectifier and Radio Transmitter

Its normal rating as a continuous-wave telegraph transmitter is 20 watts input into the antenna. This requires the use of four 5 -watt radiotrons (UV 202) operating as oscillators. For telephony two of these tubes function as oscillators and the other two as modulators, thus giving an antenna input of 10 watts when not modulating. When speak-

[^46]Front and rear views of a complete equipment are shown in Figs. 1 and 2. The unit on the left is the kenotron rectifier $\dagger$ while the unit on the right is the radio transmitter. $\ddagger$ A standard desk-type microphone and a telegraph key are also part of the equipment. The small size of the kenotron and transmitter units is apparent when they are compared with the desk microphone. In the design of the entire equipment particular attention has been directed to make it substantial and safe to operate. Rigid busbar
wiring connects the component parts in each unit. All controls on the front of the panel may be operated without danger to the operator or equipment. Interconnections are made from the rear with the result that the units present a neat appearance when installed.


Fig. 3. Schematic Diagram of Kenotron Rectifier


Fig. 4. Complete Diagram of Kenotron Rectifier
A vacuum-tube radio transmitter requires a low-voltage source of direct-current or alternating-current for the tube filaments, while the plate circuit must be operated on direct-current at a potential of several hundred volts. Both of these conditions are fulfilled by the kenotron unit. The schematic circuit arrangement of the rectifier is shown in Fig. 3 and the actual connection diagram in Fig. 4. Referring to the schematic diagram it will be seen that the transformer is wound
with three secondaries. Trwo of these deliver power to the kenotron and radiotron filaments while the center winding connects to the plates of the kenotrons. The taps on the primary of the transformer permit the filament voltage to be maintained at 7.5 volts over a range of line voltage from 102.5 to 115 . The plate winding delivers a potential of 1100 volts between outer leads or in) volts between the mid-tap and either leg.


Fig. 5. Oscillogram of Rectifier Output Wave without Filter


Fig. 6. Oscillogram of Rectifier Output Wave with Filter
The arrangement of tubes in Fig. 3 constitutes a single-phase full-wave rectifier, two of the kenotrons operating in parallel from each leg of the 1100 -volt winding. Due to the unilateral conductivity of the tubes, current passes only when the plate or anode is positive. Thus the plate winding delivers current first through one leg and then through the other, making the mid-tap on the kenotron filament winding the positive side and the mid-tap on the plate winding the negative side of the resultant direct-current output. If no filter or smoothing circuit were used the output current would appear as shown in the oscillogram in Fig. 5. The frequency of the pulsations is twice the frequency of the power supply because both halves of the cycle are rectified.

Fon telephony, a plate supply that pulsates as in loig is is masuitalde becatase such variat tions will caluse atripple whose ampliturde apporamimates (he signal produed by the voice and this ripple will be heard at the receiving station. 'Therefore a lilter cireroit is used to smooth out the reetified pulsations. This filter consists of a combination mesh amd tumed circout amd is made atp of conclensers and a reactor. The reactor and condenser in parallel (Fir. :3) are tumed to the ripple fre(fucney and, being in series with the direetcurrent line, offer a very high impedance to


Fig. 7. Rectifier Characteristic Curves
the alternating-current component in the rectified wave. The condensers, on the other hand, that are comnected across the line serve to store energy when the rectifier output is rising and then deliver it to the load as the kenotron roltage falls. It is evident that the condensers cannot discharge back into the tubes due to the valve action of the latter. The final shape of the output current of the rectifier is shown in Fig. 6. The ripple present is generally of the order of three per cent or less and does not introduce any appreciable interference for either telephony or telegraphy:

The characteristics of the kenotron rectifier are plotted in Fig. 7. These characteristics were obtained by placing different resistance
loalls arross the high-voltage gutput of the rectifier. The overall efficiency was computed as the ratio of kenotron output watts plas radiotron filanent watts over the total primary input to the transformer. The actual overall rectification efficiency of the kenotrons


Fig. 8. Schematic Diagram of Radio Transmitter


Fig. 9. Complete Diagram of Radio Transmitter
themselves is not high in low-power equipments due to the fact that the energy expended in heating the rectifier filaments often equals or exceeds the plate output. It will be seen that the load voltage falls very rapidly as the load resistance is decreased.

This is caused mainly her space charge drop in the kenotrons themselves. The regulation improves as the ratio of load resistance to plate resistance increases, exeept at zero load when the output voltage equals the peak value of the kenotron plate voltage. This latter condition occurs because the smoothing condensers, at zero load, remain charged at the maximum voltage that is impressed upon them. Referring to Fig. 7, the area between the dotted lines represents the normal operating conditions. In other words, the radio transmitter acts as a resistance load on the kenotron plate output with an average value of about 4000 ohms.


Fig. 10. Oscillogram showing Envelope of Antenna Current with Telephone Modulation

The fundamental circuit of the radio transmitter appears in Fig. S, and a complete circuit diagram of the unit is shown in Fig. 9. In considering the operation of the transmitter, reference will be made to the fundamental diagram. The radio transmitter has two main functions to perform. For telegraphy the radiotrons (UV 202) must convert their direct-current plate supply into alternating current at radio freouency. The signal switch is arranged to permit all four tubes to operate as oscillators for continuous-wave telegraphy. In order to telephone, two of the tubes are connected as oscillators while the other two act as modulators, or speech control tubes for the oscillators. Before considering the modulating circuits the operation of the transmitter oscillating circuits will be described.

It is a well-known fact that a three-electrode vacuum tube will oscillate or generate alter-nating-current power if the grid circuit is coupled, in proper phase, to the output circuit. This coupling is obtained in the transmitter by means of an oscillation transformer. The oscillation transformer consists of a
copper strip helical enil withatual inductance of about ( 6 ) mierohenties. When the line switch on the kenotron unit is alosed and the telegraph key is depressed, direct current flows from the rectifier through the morlulating reactor and the radio choke to the plates of the oscillators. The circuit is closed through the oscillator tubes to the negative side of the rectifier circuit through the mid-tap of the filament transformer winding and the bias resistor. The first inrush of current through the oscillator tubes sets up a momentary impulse in the circuit which includes the turns on the oscillation transformer $B$ (or $C$ ) and $D$. This in turn induces feeble oscillations in the antenna circuit of a frequency determined by the inductance and capacitance of the antenna system and the inductance between the turns $A$ and $D$. The grid-filament circuit of the oscillators, being connected to the lower end of the oscillation transformer, has induced in it oscillations of the same frequency as those in the antenna. This causes the current in the plate circuit to follow the grid potential variations until the oscillations in the system reach a maximum amplitude determined by the tube and circuit constants. The condenser, in series with the alternating-current plate circuit, serves to prevent the direct-current circuit from passing to ground through the oscillation transformer and at the same time acts as a low-impedance path for the radio frequency. The alternat-ing-current potential impressed on the grids of the tubes is rectified during the positive half of the cycle and sends current through the grid leak. The IR drop across the grid leak determines the negative bias voltage on the oscillators.

A 5 -watt radiotron (UV 202) operates most efficiently as an oscillator under average conditions when the alternating-current plate potential is 190 volts and the alternatingcurrent grid potential is 120 yolts. These voltages are determined mainly by the reactive drop across the plate and grid sections of the oscillation transformer. Since more antenna current is obtained on continuouswave than on telephone operation, the drop per turn is greater. Provision is made therefore to change the plate tap by means of the signal switch when shifting from continuouswave to telephone operation or vice versa. The grid turns do not carry antenna current and are less critical to variations in this current. For this reason the grid tap is not changed by the signal switch. The condenser shunted around the grid turns serves to tune

He grid cirenit and enables the requasite grid voltage to be established without the ase of excessive indactance on the oscillation transformer Aradio choke eoil is connected in the positive side of the plate circuit in order to provent the plate alternating-current component from passing back into the rectifier. The by-pass condensers, connected from the neatral to each leg of the filament circuit, are used to furmish a low-imperlance path to the grid and plate alternating-current components.


Fig. 11. External Connections of Complete Equipment

The method used in keying the transformers for continuous-wave telegraphy is of interest. Heretofore, it has been customary to open the grid leak with the key or to open the plate circuit directly in order to stop oscillations. The first method is liable to give incomplete control as oscillations may not cease entirely when the grid leak is opened. The second arrangement is productive of injurious sparking at the key contacts even in low-power transmitters. Referring to Fig. 8, it will be seen that when the key is opened the grid leak connects to the negative side of the plate circuit. This side of the plate circuit is also disconnected from the radiotron filaments. Under these conditions no oscillations can take place. When the set is keyed the grid charges up negatively each time the key opens, and since this reduces the plate current to nearly zero no sparking occurs, notwithstanding the fact that the platecircuit is opened by the same contacts.

Telephone control is arcomplished in this transmitter by means of the familiar plate modulation system. If a curve is ploted between antenna current and oscillator plate potential, approximately a lincar characteristic will be obtainerl. Hence if the speech were made to vary the plate potential, the antenna current would be molded or modulated in proportion to the amplitude and frequency of the voice vibrations. The microphone transmitter is connected in series with the primary of a microphone transformer and a 6 -volt battery. Current variations in the primary set up a potential in the secondary which is impressed between the grid and filament of the modulator tubes. The bias resistor is used in order to maintain a fixed negative potential on the modulator grids so that these tubes will operate on the straight portion of their characteristic curve. The IR drop across this resistor is determined by the direct-current plate component. As the modulator grid potential is varied, the plate current varies which must pass through the modulating reactor. An audio-frequency voltage is thus built up across the reactor and aids or opposes the normal plate potential. The resultant envelope of the antenna current is shown in the oscillogram in Fig. 10. This oscillogram indicates that the antenna current is varied from zero to about twice its nonmodulated value, corresponding to practically 100 per cent modulation.


Fig. 12. Curve showing Effect of Antenna Resistance on Output

In addition to telephony and continuouswave telegraphy, it is possible to obtain interrupted-continuous-wave telegraphy by the use of a motor-driven chopper. The chopper is used to interrupt a circuit at audiofrequencies and in practice is connected in place of the microphone as in Fig. 11. Then, with the signal switch in the telephone position and the key in series with the chopper, it is possible to modulate the transmitter output each time the key is depressed. Motor-driven choppers are generally used to interrupt the circuit about 1000 times a second.

The effect of antenna resistance on the output of the transmitter is plotied in Fig. 12. This curve was obtained with four oscillators under continuons-wave conditions at 200 meters. Since the average antenna seldom has a resistance as low as 4 ohms at 200 meters, it is evident that the transmitter will deliver rated ont put over a considerable range of antenna resistance. When used with the average small antemna, the equipment will cover a wavelength range from 180 to 320 meters. On short waves, most of the tuming is accomplished with the variable series antenna condenser. When transmitting on
the longer watelengths, this combencer may be short circuited and the taps on the wesillation transformer alljusted to ohtain the desired wavelength.

For installations where only direct-current power is available, a small motor-zemerator set is used to replace the kenotron rectifier. In this case the plate supply is ontained from the generator and the filaments are heated loy a transformer whose primary is supplied from the slip) rings on the motor windings. Lnder average conditions, using alternating-current supply, the total primary input to the kemotron rectifier is about 300 watts.

# Summary of High Tension Underground Transmission Practice and Development 

By G. B. Shanklin<br>Lighting Engineering; Department, General Electric Company


#### Abstract

Underground cable practice in America is receiving more attention that it merits now than it has in the past. The author afler discussing the advances made in the art and giving certain data concerning the three- and single-conductor cables installed in America compares the development with that in Europe. He then compares the relative merits of three-conductor and single-conductor cables and discusses joints, dielectric strength, internal ionization and heating of cables.-Editor.


Until recent years cable practice was looked upon by most engineers as a separate branch of electrical engineering obscured in a maze of "trade secrets." The geometrical cross section of cables offered an attractive problem to the theoretician and mathematical formulas dealing with electrostatic and magnetic properties were deduced years before the engineering problems had made much progress. There was at that time a wide gap between the theoretical and practical cable activities, but gradually this gap has been filled until today the whole field of cable engineering rests on a fairly solid foundation, with a majority of electrical engineers having some knowledge of its fundamental principles and varied details.

## Cable Committees

The more general this knowledge becomes the greater the progress will be, for cable practice and development more than any other phase of the electrical arts is dependent upon co-operative effort.

Committee work in England and America has been a vital progressive factor, not only due to direct contributions in the field of research and development but, more important, to the co-ordination and shaping of independent developments. Co-ordination of accepted standards of practice has also made Committee work indispensable.

The chief contributing Committees in the United States have been the Transmission and Distribution Committee of the A.I.E.E.. and the Underground Systems Committee of the N..E.L.A., whose "Specifications for Paper Insulated Cables" have accomplished a great deal. The annual reports covering their activities are accepted standards of reference. There is a joint Sub-Committee on Cable Research of these two organizations which is pursuing a very broad research program. The Insulation Committee of the National Research Council is now laying out a program covering the fundamental characteristics of gaseous, liquid and solid insulation. As soon as this work is actively under way it will prove
of valuable assistance to cable work. There is also the Sectional Commitere on Insulated Wires and Cables, of the American Engineering Standards Commitue, which is at work on the eollation and distribution of usoful data and informations.

Advancement
There has been a devided increase in standards of high voltage madergromed cable prace ice during the past few years. The manufacture and operation of cables is now more of an exact science, with the many varied factors better maderstood and under mueh better control. That there is still unlimited room for improvement does not detract from tirese accomplishments.

In reviewing this adrancement, the one ontstanding feature las been the inclusion of a dielectric loss clause in cable specifications. It has resulted in a closer study by both the manufacturer and operator, with a consequent reduction in dielectric loss and increase in quality of insulation on the one hand and a better understanding of loading and heating conditions on the other.

Previous to these specifications the quality of insulation was such that the dielectric power-factor at 100 deg. C. varied anywhere from 1.5 to .50 per cent. The A.I.E.E. Standardization Rules allow a maximum operating temperature of 5.5 deg. C.-E, where E represents line kilovolts. With such high dielectric losses as mentioned above, the critical temperature at which accumulative heating and failure occurred was too near the allowable operating temperature. The margin of safety was so narrow that frequently it was over stepped, particularly so with the higher voltage cables at points along the line called "hot spots" where, due to congestion of cables, sources of external heat, etc., the ability to dissipate heat from the ducts was inadequate.

The cable furnished today shows a powerfacto of from 1.5 to 12 per cent at 100 deg . C. with the majority of cables running considerably lower than the $1 \geq$ per cent maximum. This reduction has meant a corresponding increase in quality of insulating material, not only from a dielectric loss standpoint, but from all standpoints. The dielectric strength has been improved and the paper wrappings are more compact and more thoroughly filled than heretofore. Instead of the critical temperature at which accumulative heating starts being too near the allowable operating temperature of 5.5 deg. C.-E, it is now so far above that the question of revising this rule
frequently comes up. It is clamed that the maximum operating temperature should now be based on the physical deterionation of the paper or the effects of expansion and contraction, depending upon which is found to be the limiting feature.

A good deal of work has already been done in and attempt whermine the temperature limit of paper cable insulation. The results were published in the A.I.E.E. Journal, Pobrnary and March, 1921, and resulted in general disagreement. Some engineers felt that this work, logether with accumulated experience, warranted an increase in temperature limit, while perhaps even a larger number were opposed to this increase. Since then the Cable Research Committee has started an additional series of tests and it is hoped that the question will eventually be settled.

## Increase of Operating Voltage

The general trend of cable development is towards higher voltages. Cable lines representing very considerable increase in operating soltage are now actually in service both here and abroad with other lines under construction, while additional installations are being seriously considered. There can be no question regarding the economic need of these developments. The concentration of huge central station loads and the distances to which they must be transmitted practically demands higher voltages.

Three-conductor Cable: One of the large Central Station Companies in the Middle West has had several miles of $33-\mathrm{ky}$., threeconductor cable in operation during the past year. They are so pleased with the results that plans are now under way for $44-\mathrm{kv}$. operation. A smaller amount of $33-\mathrm{kv}$. cable has been in operation in Los Angeles since June. 1921, and a more extensive installation of similar cable is planned.

The above are the only important installations of three-conductor cable above $25-\mathrm{kv}$. rating in America. In Europe, however, such installations are becoming quite common. The first was of $30-\mathrm{kv}$. rating, installed in Berlin about 1912. Since then several installations of $33-\mathrm{kv}$. cable have been made in England and elsewhere. There is a recent .) ()-kv, three-conductor installation in Holland. It has not ret been placed in operation at full voltage and there remains some doubt whether a voltage of 50 kv . will eventually be used.

Rumors have emanated from England concerning a three-conductor "super-cable"
rated at dif kr ．and these rumbers hate leen strengthened bey an adrertisement of one of the responsible cable companies offering to quote on cable of this rating．I short length has been installed at a river erossing lout at the present time this cable should le lowed upon as purely experimental．

Single－condator（ $a b l e:$ There has been parallel progress in the development of single－ conductor cable．One of the first installations， a single－phase bo－kw．line with micl－point grounded，was made in（emmany in 1911. After considerable 1 rouble its use was discon－ timued in 1917．＇The next important installa－ tion was mate at Barcelona by an Italian Company in 1914．It represented about nine miles of $50-k v$ cable and its operation has been very successful．The st．Gotthard $60-\mathrm{kr}$ ．single－phase line in Switzerland（1920） was next，although in the meantime several short lines in the nature of ties and river crossings，rated from 40 kv ． 1060 kv ．，were installed in Europe and America．The St Gotthard line has，according to reports，aler given trouble and at least part of the cable is to be replaced by a more conservative design．

 phase，so－cyele lines form ble bew（iombe－ villiers Stationsupplying the sulmong of l＇atio These lines total die kin in lemplh atm were put in operation af fex monnthe aty 11 is manderstood that certain trombles of a remedi－ able natare were encountered ambl the veltame
 increased in stepstothe original（if）kv．Son arti－ cle（leseribing this instatlation appeared in the Reate（ioneral de l＇Electricite，Nareh ：1！iz：

There are two interesting installations of single－conductor cable now in prosress here in America．An Eastern company is mstalling a t．o－kv．，3－phase line several miles in lengeth． Another large company in 1 he Great Lakes section is installing four（ifi－kv．，B－phatse lines from eight to fourteen miles in lenerth．

In the Anntal Report of the Transmission and Distribution Committee of the A．1．EE． for 1022 ，there appeared a tabubated list of high voltage cable installations，together with data on insulation thickness，etc．This table is so comprehensive and valualne that we take the liberty of reproducing it in this article as Table I．

TABLE I
DATA ON HIGH－VOLTAGE CABLES
From 1922 Report of Transmission and Distribution Committee of A．I．E．E．

| Location | Date | Normal operating voltage | Size of Conductor cm． | Thickness of Insulation |  | Maximum dielectric between conductors kr ．per cm． | Stress to sheath |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Conductor | Belt |  |  |
|  |  |  |  | Inches | Inches |  |  |
| 1 Chicago． | 1921 | $3: 3,000$ | 350.000 | 0.297 | 0.11 | 29.4 | 26.7 |
| 2 St．Paul． | 1900 | 25,000 | 66，400 | 0.281 | 0．125 | 32.8 | ご． |
| 3 Manchester． | 192］ | 33，000 | 382.000 | 0.25 | 0.25 | 32.3 | －2 心 |
| $\pm$ Birmingham． | 1921 | 33.000 | 25．5，000 | 0.25 | 0．2．） | 34.6 | $\because 4.4$ |
| －English Cable | 1921 | 33.000 | 95.500 | 0.25 | 0.15 | 41.5 | ：3：3．6 |
| 6 Normandy． | 1914 | 33，000 | 79.000 | 0.216 | 0.216 | 47.3 | ：33．4 |
| 7 Paris．．． | 19.21 | 60.000 | $29.5,000^{*}$ | 0.53 X |  | ．． | ＋11． 5 |
| 8 Erith（England | 1921 | 33.000 | 320，000 | 0.25 | 0.2 .5 | ：3：3．6 | $2: 3.4$ |
| 9 Rome．．．．．．． | 1913 | 30,000 | 39.500 | 0.473 | $\dagger$ | 17.7 |  |
| 10 Florence | 1916 | 40,000 | $148.000^{*}$ | 1.18 | ．．． | 22.3 |  |
| 11 Turin． | 1916 | 38．000 | 138．000＊ | 0.67 |  | 28.7 |  |
| 12 Turin． | 1917 | 38，000 | 99，000＊ | 0.646 |  | 31.1 |  |
| 13 Rome | 1919 | 30,000 | 49.400 | 0.630 | I | $3 \mathrm{SC.7}$ |  |
| 14 Naples． | 1919 | 32.000 | 237．000 | 0.5911 | i | 30.6 |  |
| 15 Rome． | 1920 | 30.000 | 59.000 | 0.5 .52 | $\dagger$ | 33.6 |  |
| 16 Barcelona． | 1914 | 50，000 | $99.000^{*}$ | 0.5 .8 |  | 4.5 .1 |  |
| 17 Clyde Valley． |  | 33,000 | 237,000 | 0.512 | $\dagger$ | 34.4 |  |

Sources of information：
1，3，5， 7 Private sources．
2 Transactions A．I．E．E．．Vol．XVII， 1900.
4 London Electriral Reaiew．April 22．1921，Page 528.
6 M ．Delon at N．F．L．A．Convention，1921，discussion on Underground Systems Report．
\＆Electrical Times（London）．Sept．29， 1921.
9 to 17 from Mr．Guido Semenza，Milan．Italy．
No． 1 has sector shaped conductors；all other are round．
Dielectric stresses calculated according to Davis \＆Simon（Journal A．I．E．E．，］anuary，1421
＊Single－conductor cables．All others are three－conductor．
$\dagger$ Not giver．

## Experimental Cable Lines

An solve．simgle－conductor cable line is being installed in Italy．No definite detailed information is avalable concerning this line Dut it is understood to be relatively short in length and，although it will transmit power， is more in the nature of an experiment．Cer－ tain unique features are understood to be incorporated in the cable design，including a liquid oil filler．It is probable that new departures from established cable practice will have to be followed to take care of con－ traction and expansion and to prevent migra－ tion and leakage of the oil．If these problems can be met in a practical way it will mean a big step forward in operating voltage．The use of a thin liquid filler would prevent voids which are produced in the present type of cable by handling and by contraction and ex－ pansion during operation．These voids neces－ sarily limit the voltage stress．

One of the operating companies here in America has laid out a co－operative plan to install a $132-\mathrm{kv}$ ．， 3 －phase experimental line of single－conductor cable not over one mile in length and consisting of various types of cable．This experiment should prove very valuable．

## Comparison of Cable Developments in Europe and America

In comparing the preceding lists of cable installations in Europe and America，one can－ not help but notice that the trail is always blazed in Europe．Without detracting in the slightest from the credit due European engi－ neers it might be stated that this does not mean that American practice is too conserva－ tive nor that we are backward in develop－ ment．It is a perfectly normal situation largely due to the different conditions which surround cable practice in Europe and this country．The chief difference is the use of buried cable in Europe and cable drawn into ducts here．The concentration of load is so great and conditions change so rapidly that American operators are practically forced to sacrifice the advantages of buried cable in the interests of the more imperative demands of accessibility．

Buried cable lends itself exceptionally well to extra high voltage operation．It is not subjected to strain and severe bending during installation，there is plenty of room for joint－ ing，it dissipates the heat better than cable in ducts，and cable diameter is not limited by duct size．European cable is less heavily loaded， due to the fact that load congestion is not
nearly so great，and runs considerably cooler than American cable．All of which leads to assurance of a more compact cable with fewer and smaller voids．The above compari－ son also accounts for the somewhat thinner insulation and，consequently，higher voltage stressing followed in European practice．

Comparison of Three－conductor and Single－conduc－ tor Cable
$\Lambda$ few years ago there was a good deal of uneasiness regarding tangential stressing in three－conductor cable．Scetions near a fault were frequently found with the central tri－ angle and adjoining paper wrappings badly charred．It was at first assumed that the strength in this section was too low and the stress too high in proportion to the rest of the cross section．Later developments would indicate，however，that three－conductor design is not so badly unbalanced and that the trouble was mainly due to poor grade material and heavy loading．

Paper cable insulation is inherently weaker in a lateral direction than in a direction per－ pendicular to the wrappings，due to the fact that the surfaces are smooth and do not lie in absolutely intimate contact．The barrier effect offered by the fibers is consequently less in a lateral direction．Based on this reason－ ing，lateral stressing is a weak point in three－ conductor design but，now that high grade materials are available and loading conditions better appreciated，it is an open question whether it will be the limiting feature in future increase of operating voltage．As the voltage increases the difficulty of making three－conductor splices of reasonable size will increase rapidly．Even today it offers a serious problem，due to the complicated structure．Overall diameter of cable might also have some influence．Cables of $33-\mathrm{kv}$ ．and $44-\mathrm{kv}$ ．rating are already nearly as large as present practice is willing to accept， $66-\mathrm{kv}$ ． three－conductor cable would be of almost prohibitive size for duct operation．

This cable is favored in England because of the necessity of using steel armor on buried cable．Magnetic armor cannot be used on single－conductor cable due to high induced sheath losses．

By the time we reach such voltages as con－ sidered above the three－conductor cable must compete with the single－conductor type， with its absence of lateral stressing，compact construction，small diameter，simplicity of joints and end bells and lesser cost．Instead of having the full line voltage under a common
sheath there is only the yoltage to gromud. By taking simple precantions, short circuits between phases can be eliminated and the hazard to apparatus thereloy reduced. At these voltages the induced sheath losses will be small, provided magnetic armor is not used, something in the order of 1.5 to 30 per cent of the copper loss at 60 cycles. There is not a corresponding increase in temperature rise and reduction in carrying capacity, however, as the sheath loss does not have to be conducted through the insulation. The reduction in carrying capacity would be not more than 4 per cent.

## Cable Joints

The problems connected with cable jointing have not received the same helpful co-operative attention that other and no more important problems have. Cable joints are largely hand made. This involves a certain amount of personal element and the problems are usually accepted as individual to each operating company.

When the ratio between the number of joint failures and total length of joints in any given line is compared with the corresponding ratio for the cable proper, the results are often surprising and indicate very clearly that the factor of safety in joints is seldom comparable.

For operating voltages up to about 1.5 kv . almost any kind of joint is satisfactory, provided the dimensions are reasonable and the degree of filling and grade of materials and workmanship are reasonably good. As the voltage increases, more attention must be paid to fundamental principles, the design dimensions and dielectric stress field more scientifically proportioned, the grade and types of material more carefully chosen, and the process selected to give the best assurance that moisture and voids will be reduced to a minimum.

In the above respects much could be contributed by engineers who have developed high tension bushings. The principles are identical, although the conditions are somewhat different, being altogether in favor of bushings. For a given ralue of voltage, say 66 kv ., single-conductor cable joint design is more difficult than bushing design. Threeconductor design is correspondingly more difficult. One reason for this is the relatively high stressing of cables. This is all very well over the cable length, proper, but at the ends where

[^47]the joints must be placel it introndues an undesirable factor. If it wern practiable during the process of manufacture, th flare out the ends of cables be increased thicknese of insulation, many of the joint problems wothld be eliminated.

Most of the high voltage joints in this country are filled with soft or even liquirl, compounds. The defects of hard compound fillers for high voltage work are generally recognized. The lateral weakness of paper wrappings, a very important factor in cable joints, is also recognized and various methods are used to overcome this.

There is a very decided lack of satisfactory methods of testing and comparing joints during investigative work. Dielectric strength tests of either long or short duration tell only part of the story. Dielectric loss and high roltage direct-current tests are being studied to determine their value. Nicrophone listening devices for detection of internal discharge have proved helpful.

End bells have been purposely left out of this discussion. Their problems parallel joint problems closely and being somewhat easier are best served by centering attention on joints.

## Dielectric Strength

Three important rules have been estabr lished concerning dielectric strength of paper cables:

1st. The paper and compound must be free of all impurities. especially moisture.
$2 n d$. All interstices between and around the cellulose fibers and throughout the cable cross section must be completely filled with compound, leaving no voids or air spaces.
grd. The cellulose fibers act as very effective barriers and the largest possible number should be interposed along the dielectric path.
The pyro-electric, or conduction, theory of breakdown as developed by Dr. Wagner ${ }^{1}$ and others is generally accepted as agreeing closely with observations.

Additional light has been thrown on dielectric strength by Mr. Wiseman's² recent paper and the discussion which followed. Instead of assuming that dielectric strength is a function of maximum, minimum, or average stress, he tends to show that it is best expressed by an empirical formula similar to that for corona in air A formula of this nature is more in line with Dr. Wagner's conduction breakdown theory, and with observed facts.

The Coblo Reseated Commitue is apparently Working twands the cataldishment of a defi-
 age as detemman he standard dielectric strengh tests, and operating voltage Acoording lopresem information this ration shouk be somewhere hetwernitamil it wotal seem logioal to alsu estahhish a ratio between breakdown voltase and standard high potential accoptance and installation tests. This would give the best assuraner that cable was not in jurchl laring these tests.

Dielectric strength lests are becoming increasingly diffictlt. requiring extremely high voltage test erguipment and special end beels.

## Internal Ionization

The consensus of opinion seems to be that ionization will beeome of more importance as voltage rating increases and, that with the present voltage ratings and thicknesses of insulation, there is little to fear from this cause. Referring to the data in Table I, it will be seen that cables are now operating at stresses from 30 to 4 ik . per cm., somewhat higher than the values now derived from ionization tests in the laboratory on short lengths.

Ionization has been investigated for a number of years with little success in placing the results upon a qualitative working basis. Apparently, laboratory tests are of no use as a guide to operating performance. Systematic field tests would be necessary: Certain principles, such as complete filling and avoidance of contraction and expansion troubles, have been emphasized, however, by this work.

## Heating of Cables

The Second Report, on the "Heating of Buried Cables," was recently presented before the I.E.E. by the British Research Association. It is a very remarkable and valuable report, representing a tremendous amount of work and a complete summary of present knov:ledge on the heating of cables. Among the more interesting results are the following:

TABLE II

## Temperature Limits for Paper Cables Buried Cable

German-in deg. C. (ambient soil 25 deg. C.)

French - io deg. C. (ambient soil 10 deg. C.)

British - (i.) fleg. C. (ambient soil 15 deg. C.)
(to 11,000 volts only, presumably lower temperature for higher voltages)

## Cables in Ducts

British ion deg. ( C (ambient soil 1.5小er (`.)

$$
(10,11,000) \text { volts only) }
$$

American-sis deg. ("E (where E is line kilomolts)

In the aloove table the british limit the temperature for duct operation to a lower value due to peossible abrasion of sheath from contration and expansion.
'Thermal resistivity of soil :3t(0) to (0) for dilferent degrees of moisture content.

Thermal resistivity of paper cables 60 arerage up to 2200 volts and jor average up 10 11,000 volts.

Example of grouping two equally loaded cables (buriced):

| Distance between axis inches | Reduction permissible <br> current (ratio) |
| :---: | :---: |
| 4 | 0.76 |
| 8 | 0.82 |
| $1 \underline{2}$ | 0.86 |

Three-conductor . 0.1 .5 -sq. in., 11,0000 -volt cable, 2.20 amperes (dielectric loss negligible):

ONE CABLE

| Iemp. rise | $\frac{\text { Buried }}{25 \text { deg. C. }}$ | $\frac{\text { In air }}{31 \text { deg. C. }}$ | $\frac{\text { In duct }}{36 \text { deg. C. }}$ |
| :---: | :---: | :---: | :---: |

Ratio of temperature rise of one three-conductor, 0.2 -sq. in. cable buried and in air for average soil conditions $(\mathrm{G}=120)$ :

|  | $\frac{3300 \text { Volt }}{1.13}$ | $\frac{11.000 \text { Volt }}{1.09}$ | $\frac{22.000 \text { Volt }}{1.04}$ |
| :---: | :---: | :---: | :---: |
| Ratio | 1.3 |  |  |

Ratio of temperature rise, three-conductor cable, in cluct and in air, for average soil conditions, 0.98 to 0.94 for different size cable.

In reference to above paragraph the British findings would indicate that this ratio is not affected by soil conditions, because of the greater influence exerted by the layer of air surrounding the cable. This does not agree with experience in this country, where moisture in the soil has been proved to have a decided cooling effect

The British Report contains some very valuable loading tables for all conditions and types of cables. American practice in ducts now strictly avoids grouping excessive numbers of cable, and aims towards exposing at least one side of each duct to the earth. Grouping low and high voltage cables in the same duct bank is avoided as far as possible, and where it must be done the high voltage cables are placed in the most farorable
outside ducts. Artificial conoling ley fored rentilation, soaking of soil with monsture, etc., is employed where comstitions malse it necessary.

Operating and manufacturing companies in this country have individually contributed a great deal towards this problem of heating. but the work was not properly organzed and the individual efferts did not enordinate. The Cable Researeh Committee is undertaking a serious program along these lines. If they are given whole hearted support much can be aceomplished.

A great deal more information is meeded on grouping of cables. themal resistivity and capacity, heating due to fluctuating loads, best methods of cooling, effects of contraction and expansion, etc.

## Short Circuit Heating

Heating of cables from short circuit current has not received the attention it deserves. Reactors are used to limit short circuit more in the interest of transfomers and station apparatus.

English writers state that they do not experience contraction and expansion troubles in cable because ther limit the loading temperature to a safe value. They lose sight of the fact that one or two short circuits, lasting only a few seconds, might undo years of conservatism of loading temperature.

The whole question is, what temperatures are reached in cables under shorl circuit: One of the manufacturing companies has started work on this problem. Indications are that short circuit 33 times normal for a period of five seconds (not an uncommon condition) will cause, for a short duration of time, copper temperatures several times that allowed by limiting rules.

[^48]

 the other hatad it might prow it ver impontant factor. 1ts pessibitition are peintal onat constructively, will matirit of pessimion.

## Testing Cable with High Direct current Voltage

One of the ontstanding cable dewormpnemt of the past peas was described in a paterer presented before the linstitute by Nessm Phelps and Tanzer ${ }^{3}$ By wase of the kenotren as a sontere of high potential direct current they have developed a romtine test which scries to detect incipient faults in cable lines. Insulation resistance versus time (absorpetion) curves are taken periodically and tronble detected bey peculiarities in the shape of these curves. They have been very successful in detecting and weeding out incipient trouble in 6.0-kw. and l:3.2-kr. three-conductor cable lines with direct-current test vollages, respectively, of 9.0 kr . and 1.50 kr .

This method is being tried out on other cable systems up to 33 -kw rating with promising results. The experiments are not yet far enough adranced to say that this method is universally applicable. The principle is correct and it is hoped, in time, that it will be the means of reducing all cable short circuits to a negligible figure.

Direct-current voltage is also a useful substitute for alternating-current voltage in high potential testing of long cable lines.

The ratio between direct-current and alter-nating-current test voltage has been the source of much study: At the present time, at least one of the cable companies is accepting a ratio for paper insulated cables of 2.4 at 2.5 deg. C. with a reduction of 0.010 in ratio for each deg. C. increase in temperature. The Institute is working towards the adoption of Standard Rules covering direct-current testing.

## LIBRARY SECTION

Condensed references to some of the more important articles in the technical press, as selected by the G-E Main Library, will be listed in this section each month. New books of interest to the industry will also be listed. In special cases, where copy of an article is wanted, which cannot be obtained through regular channels or local libraries, we will suggest other sources on application.

Alternators
Some Problems in High-Speed Alternators, and Their Solution. Kosen, J.
I.E.E. Jour., Apr., 1923; v. 61, pp. 439-476.

Balancing
Balancing of Turbo-Alternator Rotors. Bellisson, J. (In French.)

Reiue Gén. de l'Elec., Apr. 28, 1923; v. 13, pp. 693-702.
(Presents a method for which a great saving in time is claimed.)
Carrier-current Communication
Baltimore-Holtwood Carrier Current Giving Excellent Scrrice.
Elec. 11'ld., May 12, 1923; v̌. 81, pp. 1077-1081. (An account of tests conducted on a 40 -mile length of the Pennsylvania Water $\mathcal{\&}$ Power Company's lines.)
Electric Cables
Cable Geometry and the Calculation of CurrentCarrying Capacity. Simons, Donald M.
A.I.E.E. Jour., May, 1923; v. 42, pp. 525-539. (Design calculations for underground cables.)

## Electric Furnaces

Some Problems in Electric Furnace Operation. Andreae, F. V.
A.I.E.E. Jour., May, 1923; v. 42, pp. 49s-509.
(Mathematical discussion of the design of threc-phase furnaces.)

## Electric Locomotives

Fuel Consumption of Oil Burning Locomotives. Babcock. A. H.
Rizy. Mech. Engr., May, 1923; v. 97, pp. 265267.
(Paper before the A.I.E.E. Methods used and results obtained in a test on the Southern Pacific Railroad to determine the relative efficiency of oil burning and electric locomotives. Serial.)
Electric Transmission Lines-Towers
Double-Circuit Tower Construction. Sharp, H. L.

Eiec. Mld., May 19, 1923; v. 81, pp. 1133-1135.
(Design, erection and cost information on towers for a 110,000 -volt line constructed by the Niagara, Lockport \& Ontario I'ower Company.)
Hydroelectric Plants, Automatic
Full-Antomatic Hydro-Electric Station. Collins, E. B.

Elec. Ifld., May 19, 1923; v. 81, pp. 1143-1147. (Description of a $5000-\mathrm{kv}$ a. plant installed by the New England Power Company at Searsburg, Vt.)

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Neutral Grounding Reactor. Lewis, W. W. A.I.E.E. Jour., May, 1923; v. 42, pp. 467-484. (Discusses tests made on the Peterson coil installation on the Alabama Power Company's system.)

## Ship Propulsion, Electric

Electric Propulsion of Ships. Johnson, R. S.
Shiphuilder, May, 1923; v. 28, pp. 360-366.
(Abstract of paper before the Liverpool Engincering Society.)

## Steam Plants

Benson Super-Pressure Plant, Swain, P. W. Power, May 22, 1923; v. 57, pp. 796-801.
(Describes an experimental boiler installation for a pressure of 3200 lbs., which is being erected in the Rugby plant of the English Electric Company, Ltd.)
Problems in Steam Plant Operation. Quinn, E. A. Jour. Elce. \&e IVest. Ind., May 15, 1923; v. 50, pp. 370-377.
(From a report of the Prime Movers Committee of the Pacific Coast Electrical Association.)
Steam Turbines-Governing
Steam-Turbine Governors and Valve Gears; Adjusting Speed and Speed Regulation. Thompson, Eustis H.
Power, May 22, 1923; v. 57, pp. 790-795.
Substations, Automatic
Discussion of Application and Economics of Automatic Railways Substations. Bale, L. D.
A.J.E.E. Jour., May, 1923; v. 42, pp. 439-444.

Maintenance of Voltage on a D-C. Distribution System by Means of a Fully Automatic Substation. Robinson, P. J.
I.E.E. Jour., Apr., 1923; v. 61, pp. 417-438.
(Describes an installation in Liverpool, England, used to operate a three-wire system.)

## Switches and Switchgear

Automatic Switch-Reclosing Apparatus. Middlemiss, G. H.
Elec. Illd., May 19, 1923; v. 81, pp. 1150-1152. (Illustrated description of apparatus developed by the Alabama Power Company.)

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Four Lectures on Relativity and Space. Steinmetz, Charles P. 126 pp., 1923, N. Y., McGrawHill Book Co., Inc.
Industrial Furnaces. Vol. 1. Trinks, Willibald. 319 pp., 1923, N. Y., John Wiley \& Sons.
Printing Telegrapl Systems and Mechanisms. Harrison, H. H. $435 \mathrm{pp} ., 1923, \mathrm{~N} . \mathrm{Y} .$, Longmans, Green \& Co.
X-Rays. Ed. 4. Kaye, G. W. C. 320 pp., 1923, N. Y., Longmans, Green $\&$ Co.

## General Electric Review

A MON゙THLV MAGAZINヒE FOR EN゚GIN゙EER

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# Frontispiece：Turbine－generator Equipped with Surface Air Cooler 

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Cargo Winches for Merchant Ships
By C. H. Giroux

Studies in the Projection of Light．Part V
Bỵ Frank Benford
Bỵ Bassett Jones
1可萑
*
$18,750-\mathrm{kv}$-a. Turbine-generator Installed in the Amsterdam Steam Plant of the Adirondack Power and Light Corporation. In this issue we conclude


## NATURE'S LAWS

A twentieth-century engineer would feel somewhat bewildered if suddenly transplanted back into a pre-Newtonian world. If he were asked to perform the simplest calculation in mechanics, such as today a high school boy would, we hope, do with ease, his embarrassment would be complete. It is quite hard and requires a good deal of imagination to put ourselses in the position of this embarrassed engineer. Let him attempt the solution of any common everyday problem which requires an elementary knowedge of mechanical laws and metaphorically speaking he would flounder about like a flat fish out of water.

Newton, among his many other notable contributions to our knowledge of the natural laws which govern the world we live in, and, indeed, the universe, propounded the laws of motion. This single contribution to our knowledge gave new light to thousands of minds and enalled them to do new work for the benefit of mankind of which they were utterly incapable before

The progress that the world makes, owing to the work of one such genius, is incalculable, but there were many men in Newton's time who did not realize that his genius had given the world a new epoch.

We have tried to make our readers see how bewildered an engineer today would be if he had not the knowledge that Newton gave the world, and we feel that it is time for engineers to realize that they will be sadly bewildered in the near future if they do not have at least some understanding of the work that Sir Joseph John Thomson has
done in recent years. If we perceive things correctly, Sir Joseph John Thomson has shown the orderliness of Nature's laws down to the very minutest of all things. He has done more than given us knowledge of one law in giving its knowledge of the structure of the atom - he has given us knowledge of the structure of all things and opened up a host of new reahms for man's imagination and skill to work in.

The fruit that his work and the work of others, stimulated by his great lead, will bear in the next ten, twenty or thirty years is absolutely impossible to contemplate. But there is little doubt that with nur large industrial research laboratories of today, whose function it is to take this new knowledge in the realm of science and turn it to practical everyday use in the realm of commerce, we shall be using this new knowhedge extensively in everyday engineering practice in the very near future.

It is for this reason that we see the imperative necessity of the engincer trying to understand the work that J. J. Thomson, Rutherford. Bragg and others have done and why we feel there is no apology needed for publishing in our pares the scientific theories that are destined 10 govern future engineering practice.

It is with these thoughts in mind that we asked the Editor of the Journal of the Franklin Institute for permission to putblish the lectures recently given in America by Sir Joseph John Thomson on the Electron in Chemistry. We fublish the first of these lectures in this issue. J. R. H.

# The Electron in Chemistry 

PART I<br>By Sur Josprif John Thomson<br>


#### Abstract

Sur doseph John Thomson gave a serics of lectures before the Franklin Institute，April 9 to 183，192．3，on the Bectron in（hemistry．Bedieving that these lectures are of great value to the entire scientific and engi－ merting profession in showing what the scientist is doing todiry to stimulate enginerering developments in the future，we asked the Editor of the Journal of the Franklin Institute for permission to reprint these lectures in the Rにいたw．We wish to acknowledge with gratitude the granting of this permission．Our present con－ thinuton appeared in the May issue of the Journal of the Franklin Institute．Formor．


I ought to explain why it is that I，who am a physicist and not a chemist，hate chosen chemistry as the subject of these lectures． I have done so because I believe that the introduction of the idea of the electron will meak down，and indeed has already done so 10 some extent the barrier of ignorance which has divided the study of the properties of matter into two distinct sciences，physies and chemistry．The properties of matter which are of primary importance to the chemist are those which relate to the power of atoms to unite together to form new combinations， new componuds．The ability to do this and the type of compound formed vary enor－ mously from one chemical element to another． Until recently the conception formed by the pliysicist of the atom afforded no clue to this variation in the chemical properties of the atom and gave therefore but little guidance to the chemist in what he regarded，and quite rightly：as the most important part of his work．The chemist wants to know much more about the difference between an atom of hydrogen and one of oxygen than that the atom of hydrogen is a small particle of one kind of matter and the atom of oxygen a heavier particle of another kind of matter． This lack of knowledge led to a proposal made by a distinguished chemist at the beginning of this century to give up the atomic theory and base chemistry on statis－ tical and thermodynamical considerations．

The chemist wants to know the reason why the behavior of an atom of hydrogen is so different from that of one of oxygen．This must depend upon the differences in the constitution of the two atoms themselves． Thus to explain the difference between the chemical properties of different atoms we have to go a stage further than the atomic theory．Just as some of the physical prop－ erties of matter in bulk had required for their explanation the conception that matter is not continuous but has a structure of finite and measurable fineness，so no progress could
be made towards the explanation of their chemical properties until we gave up the idea that the atom was indivisible，continuous and uniform，and assigned to atoms as well as to solids and liquids a structure of their own． The discovery of the electron in 1897 was the first direct evidence of such a structure．It was shown that these electrons came from all types of atoms，and that whatever the source there was only one kind of electron，which has a mass only about $1 / 1700$ that of an atom of hydrogen and carries a charge of negative clectricity numerically equal to the positive charge associated with an atom of hydrogen in the electrolysis of solutions．

Thus an invariable electron was proved to be a constituent of all atoms．Means were then devised to measure the number of elec－ trons in the atoms of the different chemical elements．It was found that this number was finite and varied from element to ele－ ment，and that the number of electrons in the atom of an element was equal to the atomic number of the clement：The atomic number of an element being its place in the list when the clements are arranged in the order of their atomic weights．As the atomic number is roughly proportional to the atomic weight the proportion between the mass of the electron and the total mass of an atom is，except for hydrogen，much the same for all atoms．The electrons，however，only account for about $1 / 3400$ of the whole mass， for most purposes a negligible fraction．

The greater part of the mass is accounted for by the positively electrified part of the atom．The electrons are all negatively elec－ trified and as the normal atom is electrically neutral，there must be within it a positive charge to balance the negative one on the electrons．This positive charge，as experi－ ments on positive rays show，is attached to a mass equal to the mass of the atom．Thus the carrier of the positive charge，unlike that of the negative，varies from element to ele－ ment．As the mass of the positive charge is
always an integral multiple of a mit, it is natural to suppose that this mass is made up of a number of units bound together. The number of such units is equal to the atomic weight and the number of electrons approximately half that number, if each unit of mass carries the atomic charge of positive electricity, the quantity of positive electricity would be too large unless these positive units were associated with about half this number of electrons. Thus, in addition to the stateture conferred by the electrons, the positively electrified parts have themselves a structure, it is the structure conferred by the electrons which is responsible for the chemical properties of the atom. The structure of the positive core is concerned with radioactive transformations.
rounded be electrons: The number of alectrons increasing from one in the atom of hydrogen to a handred or mone in the beatrion elements. The positioe charge of the whter and the negative charges on the efoetmons will produce a fiek of electrical foree which will be determinable when the pesition of the electrons can be specified. Thus the forte exerted by the atom and therefore its chemical properties will depend 10 on the configuration of the electrons and to determine this is one of the most important problems in the electron theory of chemistry

This problem is that of determininer the way the electrons will arrange themselves under the action of their mutual repulsions and the forces exerted upon them by the positive charge.


Fig. 1

As up to the present nothing has been discovered that cannot be resolved into electrons and positively electrified particles, it is natural to frame a theory of the structure of the atom on the supposition that it is built up of these two ingredients. It should be borne in mind, however, that our means of detecting the existence of electrically charged bodies far surpass those for detecting uncharged ones, and if there were any uncharged constituents of the atom, they would in any case probably have escaped detection. We know, however, even supposing that such constituents do exist. their mass must be negligible compared with that of the positive parts, for these parts account for well within a fraction of a per cent of the whole mass of the atom.

## Arrangement of Electrons in the Atom

Confining ourselves then to the consideration of things whose existence has been demonstrated we regard the atom as made up of a massive positively electrified center sur-
.In the first place we observe that if these forces were to vary strictly as the inverse square of the distance we know by Earnshaw's theorem that no stable configuration in which the electrons are at rest or oscillating about positions of equilibrium is possible, the electrons must describe orbits, and further ther must describe different orbits: for such a system as that in Saturn's rings where several units follow each other round the same orbit is not possible when the units. as the electrons would do, repel each other instead of attracting one another like the constituents of Saturn's rings. When there are several electrons in the atom the orbits described by the electrons would be of great complexity, and the mental picture convered by this multitude of orbits would be too blurred and complicated to be of much assistance in helping us to get readily a clear idea of what is going on in chemical processes.

I have therefore adopted the plan of supposing that the law of force between the positive part and the electrons is, at the
distances with which we have to deal in the atom, not strictly that of the inverse square, but a more complex one which changes from att raction to repulsion as the distance between the positive charge and the electron dimmishes. This bypothesis leads to a simple mental pieture of the structure of the atom and its consequences are in close agreement with the facts of chemistry. I suppose that the repulsive foree between two clectrons is always inversely proportional to the square of that distance. With regard to this point I may point ont that we have no direct evidenee as to what may be the law of foree between electrical charges at distances comparable to $10^{-8} \mathrm{~cm}$. . which is a distance we have reason to believe is comparable with that which separates the positive charge from the electron in the atom. The direct experimental verification of this law has been of course made at incomparably greater distances, while the direct experiments, such as those on the scattering of the alpha particles, only give information as to the law at distances very small compared with $10^{-8} \mathrm{~cm}$.

I shall assume that the law of force between a positive charge and an electron is expressed by the equation

$$
\begin{equation*}
F=\frac{E c}{r^{2}}\left(1-\frac{c}{r}\right) \tag{1}
\end{equation*}
$$

where $F$ is the attraction between the charges, $E, e$, the positive and negative charges on the core and electrons, respectively, $r$ the distance between them and $c$ is a constant varying from one kind of atom to another, it is the distance at which the force changes from attraction to repulsion and is of the order of $10^{-5} \mathrm{~cm}$.

We may remark in passing that the introduction of some new physical law, involving directly or indirectly a length of this order, is necessary for any theory of the structure of atoms. We could not form a theory at all if all we knew about the action of electric charges was that they repelled or attracted inversely as the square of the distance, for this would put at our disposal only two quantities, the mass of an electron and its charge, and so could not furnish the three units of space, mass and time required for any physical theory. The discovery of the induction of currents or what is equivalent, the magnetic effect due to electric charges, introduced another fundamental unit, the relocity of light; the unit of length to which this system leads is the radius of the electron, about $10^{-13} \mathrm{~cm}$., a quantity of quite
different order from $10^{-8}$ em., which corresponds to atomic dimensions. The size of atoms being what it is, is a proof that there is some law of physies not recognized in the older science which is all-important in connection with the theory of the atom and must form the hasis of that theory.

If the law of foree is that just given, then a number of electrons can be in stable equilibrium around a positive charge without necessarily describing orbits around it.

## Onc Elcctron Atom

Thus, for example, if there is one electron it will be in stable equilibrium at a distance $c_{1}$ from the positive charge.

## Two Elcctron Atom

If there are two electrons they will be in equilibrium with the positive charge midway between them, $r$ the distance of either electron from the positive charge is given by the equation

$$
\begin{equation*}
\frac{E_{c}}{r^{2}}\left(1-\frac{c_{2}}{r}\right)=\frac{c^{2}}{4 r^{2}} \tag{2}
\end{equation*}
$$

When the positive charge and the two electrons form an electrically neutral system $E=2 e$, so that $c_{2} / r=7 / 8$ or $r=1.14 c_{2}$.

## Three Electron Atom

When there are three electrons, they will be in equilibrium at the corner of an equilateral triangle with the positive charge at the center. $r$, the distance of any clectron from the center, is given by the equation

$$
\begin{equation*}
\frac{E c}{r^{2}}\left(1-\frac{c_{3}}{r}\right)=\frac{\dot{2}}{3 r^{2}} \cos 30 \tag{3}
\end{equation*}
$$

When the system is electrically neutral $E=3 e$, so that $r=1.26 c_{3}$.
Four Elcctron Atom
The most symmetrical arrangement of four electrons is when they are at the corners of a regular tetrahedron. The distance of the electrons from the center when the atom is neutral is equal to $1.29 c_{4}$. The tetrahedron may be regarded as the ends of two equal lines at right angles to each other and also to the line joining their middle points.

## Five Electron Atom

Five electrons are in equilibrium when arranged so that three are at the corners of an equilateral triangle, the other two at the ends of a line passing through the center of the triangle and at right angles to its plane; the line is bisected by the plane of the triangle. The distance of the electrons in the triangle from the center is $1.34 c_{5}$, that of the other two $1.37 c_{5}$.

## Six Electron Atom

Six electrons are in equilibrium when at the comers of a regular octahedron. For some purposes it is convenient to regard the octahedron as two equilateral triangles at right angles to the line joining their centers, one triangle being twisted relatively to the other so that the projection of their corners on a parallel plane forms a regular hexagon. The distance of the electrons from the center is $1.38 c_{6}$.

## Scuen Elcctron Atom

Seven electrons arrange themselves so that five are at the corners of a regular pentagon while the two others are at the ends of a line through the center at right angles to the plane

In Table I, I give the results of a calculation of the positive charge $E$ required to keep $n$ electrons in stable equilibrium. The first line refers to the two-dimensional problem, when the electrons are arranged at equal intervals round the circumference of a circle with a positive charge at the center; the second line refers to the three-dimensional problem when the electrons are at the corners of a polyhedron.

These numbers are for a law of force botween the positive charge and the electron represented by $\frac{E e}{r^{2}}\left(1-\frac{c}{r}\right)$. If the part of the force which does not vary inversely as the square of the distance varies inversely as some higher power than the cube, then the

TABLE I

| Two-dimensional Problem |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & n=1 \\ & E \mid e>0 \end{aligned}$ | $\stackrel{2}{2}$ | $\begin{gathered} 3 \\ 1.58 \end{gathered}$ | 4 3.10 | 5 4.76 | 6 7.32 | 14.2 | 10 24.48 | 12 38.9 | 14 58 | 16 83 | $\stackrel{8}{115}$ |
| Three-dimensional Problem |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & n=1 \\ & E / e>0 \end{aligned}$ |  |  | 3 1.58 |  |  | 6 4.8 |  |  | 12 |  | $\begin{array}{r} 20 \\ 30 \end{array}$ |

of the pentagon and which is bisected by that plane. The distance of the electrons in the pentagon from the center is $1.4 c_{7}$, that of the other two $1.37 c_{7}$.

## Eight Electron Atom

Eight electrons arrange themselves at the corners of a twisted cube, a figure obtained by taking two squares, placing them parallel to each other and at right angles to the line joining their centers, and twisting them relatively to each other so that the projection of their corners on a parallel plane forms a regular octagon.
Configuration when the Number of Electrons is Greater than Eight
The following considerations show, however, that there must come a stage when it will no longer be possible to have all the electrons at the corners of a regular polyhedron.

To keep the electrons in stable equilibrium in spite of their mutual repulsion requires a finite positive charge and the greater the number of electrons and therefore the smaller the angular distance between an electron and its nearest neighbor, the greater the positive charge must be.
number of electrons which a given positive charge can keep in stable equilibrium will be increased.

Confining ourselves for the moment to the case when the force is represented by

$$
F=\frac{E e}{r^{2}}\left(1-\frac{c}{r}\right)
$$

we see from the second table that when the number of electrons is not greater than eight, the electrons can be kept in equilibrium by a positive charge equal to the sum of the negative charges on the electrons, which is the greatest positive charge which can occur in a neutral atom. So that when the number of electrons is not greater than eight, a neutral atom can have these electrons arranged symmetrically at the same distance from the center at the corners of a regular polyhedron. When, however, the number exceeds eight this is no longer possible. For we see from the table that to keep, say, nine electrons in stable equilibrium would require a positive charge more than $y_{e}$. where $c$ is the charge on an electron, but in a neutral molecule $9 c$ is the maximum positive charge a vailable when there are nine electrons in the atom. Thus the regular progression in the arrangement breaks down when the electrons
amonmt to eight and a new arrangement must come into foree. Let us suppose that there are nine electrons; then these nine camot atl be arranged at the same distance from the eenter, for this arrangement would be mastable since a positive chatge of nine is insufficient to keep nine electrons in stable equilibrimm. The charge ge could, however, keep cight electrons in stable equilibrimm at the same distance from the center, leaving one to go outside. The distance of the eight clectrons from the central charge would be $1.3 \mathrm{~S} c_{9}$, that of the single electron would be $9 c_{9}$. So that the single electron would be a long way out from the center of the atom.

If there are ten electrons, these can be arranged so that eight form a laver round the
of nine to keep them in equilibrium. We can, however, get a system which will be in stable equilibrium if the electrons proceed to form a third shell; thas, if there are seventeen electrons, we could have an inner shell of eight, then another shell of eight and then an electron a long way outside. If we had eighteen electrons we should get two shells of eight and two electrons outside, and so on, until with 24 electrons we shall have filled $u_{p}$ the third shell and have to begin again.

Let us now arrange the lighter elements in the order of the number of electrons they contain, and place underncath the symbol for the element the number of electrons in the outer layer of the atom. The number of free electrons in the atom has been taken as two

TABLE II

|  | Li | Bc | Bo | C | N | O | F | Ne | Na | Mg | Al | Si | P | S | Cl | A | K |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of frec elec- <br> trons in the atom... | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| Number of clectrons in <br> the outer layer.... | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |

center and two go outside, the distance of the cight from the center would be $1.33 c_{10}$, that of the two outlying ones would be $5.7 c_{10}$.

Eleven electrons can be arranged with an imner layer of eight and an outer one of three, the distance of the inner one from the center would be $1.3 c_{11}$, that of the outer one 4.62.5 $c_{11}$.

Twelve electrons might be arranged with an inner layer of eight, radius $1.26 c_{12}$ and an outer layer of four, radius $3.9 c_{12}$.

Thirteen electrons, with an inner laver of cight, radius $1.2 .2 c_{13}$ and an outer layer of five, mean radius 3.5? $c_{13}$.

Fourteen electrons, with an inner layer of eight, radius $1.22 c_{14}$; and an outer layer of six, radius $3.22 c_{14}$.

Fifteen electrons, with an inner layer of eight, radius $1.2 c_{15}$; an outer layer of seven, mean radius $3.1 c_{15}$.

Sixteen electrons, with an inner layer of eight, radius $1.18 \mathrm{c}_{16}$; an outer layer of eight, radius $2.9 \varepsilon_{16}$.

We have now got eight electrons on the outer layer and there is not accommodation for any more; for since the atom is neutral the excess of positive over negative electricity in the system consisting of the central charge and the inner layer is equal to the charge on the electrons in the outer layer, thus if there were nine electrons in the outer layer there would be only an effective positive charge
less than the atomic number of the element, since two electrons always seem to cluster round the center core and form a system by themselves.

## The Periodic Law

Thus, if we arrange the elements in the order of the number of electrons in the atom, which we have seen is the same as the order of the atomic weights, there will be a periodicity in the number of electrons in the outer layer. It will increase from one to eight, then drop again to one; increase again to eight, drop to one, and so on. Thus, as far as properties depending upon the outer layer are concerned, the elements will show a periodicity in their properties similar to that expressed by Mendeleef's periodic law in chemistry.

We shall show later on that the valency is a property depending on the number of electrons in the outer layer, the electropositive valency being proportional to that number, so that this type of atom would explain the periodic law.

## Variation of the Number of Elements in a Period

We have supposed that when the positive charge and therefore the number of electrons in the atom is increased by unity, the additional electron goes to the outer layer. This
need not, however, necessarily be the case. When the positive charge is increased, the number of electrons which it can hold in stable equilibrium on a spherical layer with its center at the atom increases also; thus a large positive charge at the center could hold more than eight electrons in the inner layer, and so the additional electron might, instead of going to the outside, find accommodation on one of the imner layers. Thus, since the valency depends on the number of electrons
rhodium group, the crowd of elements known as the rare earths, and the platimum group, which fulfill this condition.

## Allotropic Forms

There is in general more than one way in which the electrons can be arranged in stable equilibrium and though one particular arrangement may have the absolute minimum potential energy, yet calculation shows that in some cases the difference in potential

## TABLE III

POTENTIAL ENERGY OF ATOMS WITH THREE TO EIGHT ELECTRONS

in the outer layer, if the additional electron was trapped in an inner layer, two consecutive elements, though they would have different atomic weights, would have the same valency. When there are a large number of electrons in the atom arranged in many layers it may require the addition of several electrons to the atom before there is any increase in the number in the outer layer and thus there might be a considerable number of adjacent elements with different atomic weights but with very similar chemical properties. There are groups of elements such as iron, nickel and cobalt group, the
energy between this configuration and some other one is exceedingly small and changes in the surroundings change the balance in favor of one or the other. If these configurations have different numbers of electrons in the outer layer, then they would correspond to forms with different valencies, and thus we may look in this direction for an explanation of the variable valencies shown by some elements. The shall return to this point later on.

Table III, calculated by Miss Woodward, gives in the third column the potential energy corresponding to the various arrangements
of the clectrons in atoms containing from three to eight electrons. The second column contains the distances of the electrons from the center of the atom. Thus the figures corresponding to the arrangement of seven clectrons in a double triangular pyramid with two electrons outside on the axis of the pyramid, indicate that the electrons on the triangular base are at a distance 1.244 c from the center; those at the vortex of the inner pyramid at the distance 1.191 c while the outer electrons are at a distance 4.316 c .

A simple example of the small difference in the potential energy between different configurations is afforded by an atom containing five electrons. We have described one such configuration when the five electrons were approximately at the same distance from the center. There is, however, as we see from the table, another arrangement where four electrons are at the corners of a regular tetrahedron with its center at the positive charge, while the fifth electron is a long way outside the tetrahedron. The mean distance of the electrons on the tetrahedron from the center is approximately $1.22 c_{5}$; where $c_{5}$ is the value of $c$ for the fifth electron atom, while that of the outside electron is approximately $5 c_{5}$, i.e., more than four times greater. The potential energy of the second configuration is only about two per cent greater than the first, thus there would be no great tendency for the second configuration to pass back to the other. The properties of the two configurations would, however, be quite different, in the second configuration we have a single electron far away from the others; this, as we have seen; is also the case with the alkali metals; in this configuration the five electron atom might be expected to show some of the properties of a monovalent element, in the other it would be pentavalent.

## Active Nitrogen

As nitrogen has an atom with five disposable electrons, it seems possible that the active form of nitrogen discovered by the present Lord Rayleigh may have this configuration. This active form is produced by passing an electric discharge through nitrogen and it is clear that if an atom were first ionized by the detachment of an electron the conditions would be favorable for the production of the configuration under consideration. For when the first electron is detached the remaining four will naturally arrange themselves in a tetrahedron round the
center, thus the nucleus of the configuration is already there and an additional electron at some distance from the center would be more likely to take up a position outside than to force itself into the tetrahedron. As the second form has, like the alkali metals, a single electron at a great distance from the center, we should expect that like them it would be attacked vigorously by halogens, and that as the outlying electron would require little work to detach it, this form of nitrogen would be easily ionized; both these properties are characteristic of Lord Rayleigh's active nitrogen.

We see that besides the two forms for the fifth electron atom there are forms for the sixth and seventh electron atoms which differ little in their potential energy in which two electrons are separated from the rest (e.g., oxygen and fluorine). These would tend to be formed if the atoms were ionized so as to lose two electrons and then regain these electrons. As the number of atoms which lose two electrons when the electric discharge passes through a gas is small compared with the number which only lose one, we should not expect these modifications of oxygen and fluorine to be produced so freely as those of nitrogen.

## Experimental Evidence as to the Configuration of Electrons in the Atom

We may hope when our sources of Röntgen radiation are more powerful to be able to obtain evidence of this by observing the interference effects produced when Röntgen rays pass through large numbers of neutral atoms. If the orientation of these atoms is a random one we can easily show that the interference of the rays scattered by the electrons will give rise to a series of rings. There will be a separate ring for every different distance between pairs of electrons in the atom. Thus if there were only two electrons there would only be one ring whose radius is proportional to the distance between the two electrons; again in an equilateral triangle there would only be one ring, for the distance between any two electrons is equal to a side of the triangle. If four electrons were at the corners of a regular tetrahedron there would again be only one ring for the distance between any two electrons is equal to a side of the tetrahedron. If, however, the four electrons were at the corners of a square there would be two rings, the radius of one being proportional to a side of the square, that of the other to its diagonal. Arrangement at the
corners of a regular octahedron would also give two rings, the radits of one being proportional to the side of the octahedron, the other to the distance between two opposite corners. A cubical arrangement of electrons would, however, give three rings, the radius of one proportional to a side of the cube, that of the second to a diagonal of a face and that of the third to the diagonal of the cube. Evidence of this kind is not, however, available at present.

As we shall see later on, the coefficient of diamagnetism gives on Langevin's theory of diamagnetism, the moment of inertia of the electrons about a line through the center of the atom, this can be made to yield a certain amount of information about the disposition of the electrons, especially if we know from other sources the distance of the outer layer of electrons from the center of the atom.

## Evidence Afforded by Positive Rays

More definite information can be got from evidence afforded by the positive rays. Let us first take the case of positively charged atoms. Their positive charge is due to their having lost electrons from the outer layer, now on this theory there is only one electron in the outer layer of the atom of hydrogen and in those of the alkali metals, so that these atoms should not be able to lose more than one electron and therefore should be unable to gain more than one unit of positive charge.

It is remarkable that these are the only atoms which in the positive ray spectra have not been observed with more than one positive charge. On the other hand, other light atoms have more than one electron and thus gain double or treble positive charges.

All such atoms when detected in the positive ray spectrum have been observed with double positive charges and in some cases such as carbon, nitrogen, oxygen with three or four, while as many as seven positive charges have been found in the atom of mercury.

Further confirmation of the views we have been discussing about the relation between the number of electrons and the property of the atom is afforded by the study of the occurrence of negatively electrified atoms in a gas through which an electric discharge is passing. By the method of the positive rays we are able to detect negatively as well as positively electrified atoms, and we find in this way that some atoms readily acquire a negative charge while others never do so. On the view we are considering, eight is the
maximum number of electrons which cath exist in the outer layer; as the atom of nem already possesses this mumber it camont, accommodate another electron and su camint receive a negative charge. (on the other hand, the atom with a similar number of electrons in the outer layer has, as a reference to Table II shows, a superfluity of stability and can therefore accommodate another electron and thus acquire a negative charge. The superfluity of stability is not, however, great enough for them to accommodate two electrons so that we should not expect to find any atoms with a double negative charge.

In the experiments with positive rays the atom of neon which has eight electrons in the outer layer has never been observed with a negative charge, while negative charges are common on atoms of hydrogen, chlorine, carbon and oxygen. No atoms have been observed carrying two negative charges.

It is remarkable that though carbon and oxygen, the neighbors on cither side of nitrogen, readily acquire negative charges, nitrogen itself is very rarely observed with a negative charge. It was thought for a long time that the nitrogen atom never carried a negative charge, recently, however, I have observed in more intense discharges a faint line on the positive ray photograph corresponding to the negatively charged nitrogen atom, it is, however, very feeble in comparison with the adjacent lines due to negatively charged carbon and oxygen, respectively. A calculation of the work required to remove the additional electron from a negatively charged nitrogen atom shows that it is very small in comparison with that required to remove the additional electrons from negatively charged atoms of carbon or oxygen, so that a negatively charged nitrogen atom would easily lose its charge and so be difficult to detect.

Again the only negatively electrified atoms we can observe by the positive ray method are those which have previously been positively charged, i.e., those which at one time have lost an electron. If such atoms, when they regain electrons, are in the condition we have ascribed to "active nitrogen" the electrons they regain will be far out from the center of the atom and so would be very easily detached. Thus very few of those atoms could be expected to retain the electrons necessary to give them a negative charge.

There are some other interesting results which follow at once from the view we have taken of the constitution of the atom. The
first we shall consider is the ehange in the chemical properties produced by electrifying the atom. Let us take the oxyen atom as an example, it has six eleetrons in the ofter layer, and we may anticipate the results to be given in the next chapter bey sang that its valency is determined by the number of electrons in this layer. When the oxygen atom is positively electrified it has lost one or more electrons. If it is clectrified so that it carries one mait of positive charge, the unit of charge being that carried hy an electron, it must have lost one electron, so that the atom will only have five electrons in the outer layer, the same number as there are in a neutral atom of mitrogen. Thus, if the valency depends on the number of elect rons in the outer layer, the valency of oxygen carrying a unit charge of electricity ought to be the same as that of a neutral atom of nitrogen, i.c., it ought to form the compound $\mathrm{OH}_{3}$, a compound having the molecular weight 19. This is confirmed by observation with the positive rays, when liydrogen and oxygen are present in the tube, a line corresponding to this molecular weight is frequently observed. Again, if the oxygen atom carries a double positive charge, and obscrvations on the positive rays show that oxygen atoms with this charge are frequent when the electric discharge passes through gases, the atom must have lost two electrons and will be left with only four in the outer layer, the same number as in the outer layer of a neutral atom of carbon; hence the doubly charged oxygen atom ought to have the same valency as neutral carbon, and thus form the compound $\left(\mathrm{OH}_{4}\right)++$. This compound would carry a double charge and the ratio of $m / e$ would be 10. I have found ${ }^{1}$ in the positive ray, spectrum lines having this value of $e / m$ when both oxygen and hydrogen were in the discharge tube.

Again the atoms of the inert gases which have eight electrons in the outer layer, would, if they acquired one unit of positive charge, have lost an electron and would only contain seven electrons in the outer layer. This is the number in the outer layer of a neutral halogen atom. The positively electrified atoms of the inert gases could thus like the neutral atoms of the halogens combine with one atom of hydrogen and thus the compound NeH would be possible if it carried a unit charge of positive electricity.

The molecular weight of this would be 21 and a line corresponding to a carrier with this

[^49]molecular weight has been observed by Aston. The neon atom can, as observations on the positive rays show, lose two electrons, in this state it could combine with two atoms of hydrogen, or one of oxygen, the first of these molecules woukd have the value $m c=11$, and the second $m / c=15$; the first could not be distinguished from the isotope of neon atomic weight 22 with a double charge, and the line due to the second would be identical with that due to water, so that the positive rays could not afford convincing evidence of the existence of these compounds. If we turn to negatively electrified atoms, a negative electrified chlorine atom would have eight electrons in the outer layer, it would resemble the neutral atom of an inert gas and so would not be able to enter into chemical combination. It would seem as if it ought not to be very difficult to determine this point by direct experiment.

The negatively electrified chlorine atom has the same number of electrons as a neutral atom of argon, both having eight in the outer layer. It might therefore be expected to resemble argon not merely in its chemical properties, but also in the nature of its spectrum. The spectra would not be identical for the positive charge binding the electrons together would be greater for argon than for chlorine. The similarity in the arrangement of the electrons might be expected to lead to similarities in the spectra of negatively electrified chlorine atoms and neutral argon atoms. Again, a positively electrified potassium atom has lost an electron and so would contain the same number of electrons as a negatively electrified chlorine atom or a neutral argon one. Thus we should expect the spectrum of positively electrified potassium atoms to show similarities both with that of negatively electrified chlorine atoms and with neutral argon atoms. Professor Zeeman and Mr. Dik ${ }^{2}$ have compared the red spectrum of argon, which is the one due to the neutral atom, with the spectrum due to positively electrified potassium atom and have found some exceedingly interesting points of resemblance. It is easier to observe the spectra due to positively electrified atoms than those due to negatively electrified ones, for in the latter case we should have to observe the spectrum they give out on receiving the negative charge, any attempt to stimulate them to luminescence afterwards would probably result in their destruction.

Similarly positively electrified oxygen atoms might be expected to give spectra resembling
those of neutral nitrogen atoms and positively electrified nitrogen atoms show similarities with neutral carbon atoms.

## The Size of Atoms

By the radius of an atom we mean the distance of the electron in the onter layer from the center of the atom. Let $E$ be the central positive charge and

$$
\begin{equation*}
\frac{E e}{r^{2}}-\frac{c^{2} C}{r^{3}} \tag{4}
\end{equation*}
$$

the attraction between this charge and an electron at a distance $r, c$ is the charge on the electron and $c C=c E$ where $c$ is the quantity introduced in the expression for the same force [formula (1)], $c$ is the distance at which
layer is greatest for the light efemems and diminishes rapidly at first and then wory slowly to the end of the perised. When we. pass from neon, the last element in this period, to sodium, the first in the uext, 1 hn w is a large increase in the ratius. The sortium atom will have a larger radins than the lithium one, the ratio of the two will dejemel on the ratio of $a$ to $b$, if $a$ were zero the radij would be equal.

The increase in the radius which ocems at sodium is followed by a continually diminishing radius until we reach argon; when we pass to potassium, the first elemont in the next period, there is again an increass. The radii of atoms in the same group like

TABLE IV

| Element | N | E/e | $S_{u}$ | $r$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Hydrogen. | 1 | 1 | 0 | CII | $a+b$ |
| Lithium. . | ¢ | 1 | 0 | CLi | $7 a+b$ |
| Beryllium. | 9 | 2 | 1 | $4{ }^{4} \mathrm{CBe} / 7$ | $5.14 a+.57 b$ |
| Boron. . . . | 11 | 3 | 2.3 | $4 C_{B 0} / 9.7$ | $4.522+.412 b$ |
| Carbon. | 12 | 4 | 3.66 | $4 C C / 12.3$ | $3.88 a+.322 b$ |
| Nitrogen. | 14 | 5 | 5.2 | $4 C .5 / 14.8$ | $3.78 a+.2706$ |
| Oxygen. | 16 | 6 | 6.68 | $4 \mathrm{Co} / 17.3$ | $3.69 a+.23 b$ |
| Fluorine | 19 | ' | 8.08 | $4 C F / 19.9$ | $3.8 a+.21 b$ |
| Neon. | 20 | 8 | 10.1 | ${ }_{4} \mathrm{CN}_{\mathrm{C}} / 21.9$ | $3.634+.182$ |
| Sodium. | 23 | 1 | 0 | C. ${ }^{\text {a }}$ | 23. $a+b$ |

the force between the positive charge and the electron changes from attraction to repulsion.

Then for the equilibrium of an electron on the outer layer we have

$$
\begin{equation*}
\frac{E e}{r^{2}}-\frac{C e^{2}}{r^{3}}=\frac{S_{n}}{4 r^{2}} e^{2} \tag{5}
\end{equation*}
$$

where $S_{n}=\Sigma \frac{1}{\sin \theta}, 2 \theta$ being the angle subtended at the center of the atom by a pair of electrons and $\Sigma \frac{1}{\sin \theta}$ means that the sum of the values of $1 / \sin \theta$ for each pair of electrons is to be taken. We get from this equation

$$
\begin{equation*}
r=\frac{C}{\frac{E}{e}-\frac{S_{n}}{4}} \tag{6}
\end{equation*}
$$

The ralues of $r$ for the lighter elements are given in the third column of Table IV. The fourth column is the value of $r$ on the assumption that $C$ is a linear function of the atomic weight, given by the equation $C=a N+b$, where $N$ is the atomic weight and $a$ and $b$ constants.

Thus, taking the elements from lithium to neon, we see that the radius of the outer

[^50]ithium, sodium, potassium, or fluorine, bromine and iodine increase with the atomic weight of the element.

The relation between the radius of the atom and the atomic weight is such that the minima radii occur at the ends of the perions and, as in Lothar Meyer's well-known graph, which has been reproduced in almost every text-book of chemistry, not at the mildle. Recent experiments have shown, however, that this graph does not accurately represent the relation. Gervaise le $\mathrm{Bas}^{3}$, says:

1. "There is a periodic relation between the atomic volume and the atomic weight of the elements."
2. "There is a tendency for the atomic volume to diminish in each series as the atoms increase in weight, the smallest occurs in group 7. ."
3. "There is a general increase in tio atomic volumes of each group from series one onwards, that is in the direction of increasing atomic weight."

This is in entire agreement with the results we have just found. The same thing is beautifully shown by the experiments of IV. L. Bragg ${ }^{4}$ which give a curve (Fig. 1) for
the atomic ratlii which in the period from lithium to noon agrees mumerically very well with those deduced from the Table IV given above, especially if $b$ is small compared with a. The formula we have given wonk, anless a were very small compared with $b$, make the incrase in atomic volume from lithium to sodiam too great. According to Bragg the value of the solium atom is only about 1.2 times that of the lithium one. While if the formula could be streteled from one period (0) another the increase would be much greater unless a were very small compared with $b$. We shall see later on that the law of the inverse cube only holds within a limited range of $r$ and that bevond a certain distance the force seems to vary as the simple law of the inverse square. An effect of this kind would prevent any large increase in the radius of the atom as we passed from one period to another, and we should expect to find, as is the case, that the agreement between theory and experiment is most marked for the lighter and smaller atom.

## Ionizing Potential

Another quantity which has been the subject of a great many experiments is what is known as the ionizing potential. This is the work required to detach an electron from the atom, expressed as the fall of the charge on an electron through this potential. We may remark that the work required to detach the electron must depend upon the way in which it is done, so that the ionizing potential is not a perfectly definite quantity. Thus to take two extreme cases, we may suppose the electron removed so suddenly that the other electrons have no time to change their position before it is out of their range of action, or to take the other extreme we may remove it so slowly that the electrons are always in their position of equilibrium corresponding to the position of the electron which is being ejected. In the first case the work required to move the electron away from the central positive charge is

$$
\frac{E e}{r}-\frac{1}{2} \frac{C e^{2}}{r^{2}}
$$

and the work done by the other electrons in ejecting it is $e^{2} / r_{12}+e^{2} / r_{13}+e^{2} / r_{14}$. . . where $r_{12}, r_{13}, r_{14}$ are the distances of the ejected electrons from the other electrons indicated by the suffixes $2,3,4$. Now $r_{12}=2 r \sin \theta_{12}$ where $2 \theta_{12}$ is the angle between the radii from the center to the first and second electrons, and $r$ is the distance of an electron from the center, hence

$$
\begin{gather*}
r_{12}^{r_{12}}+\frac{c^{2}}{r_{13}}+\cdots=\frac{1}{2 r}\left(\frac{1}{\sin \delta_{12}}+\frac{1}{\sin \delta_{13}}+\frac{1}{\sin \delta_{11}} \cdots\right) \\
=\frac{1}{2 r} \cdot r_{1 \prime} \tag{7}
\end{gather*}
$$

The work required to remove the electron is thus

$$
\begin{equation*}
\frac{E c}{r}-\frac{1}{2} \frac{C c^{2}}{r^{2}}-\frac{1}{2 r} S_{n} \tag{8}
\end{equation*}
$$

but from the equation of equilibrium

$$
\begin{equation*}
\frac{E c}{r^{2}}-\frac{c^{2} C}{r^{3}}=\frac{e^{2} S n}{4 r^{2}} ; \tag{9}
\end{equation*}
$$

hence if $V$ is the ionizing potential, $V e$, since it is equal to the work required to remove the electron, is given by the equation

$$
\begin{equation*}
V e=\frac{E e}{2 r}-\frac{3}{8} \frac{e^{2} S_{n}}{r}, \tag{10}
\end{equation*}
$$

if $n$ is the number of electrons $E=n e$ and

$$
\begin{equation*}
V=\frac{c^{2}}{2 r}\left(1-\frac{3}{4} S_{n}\right) \tag{11}
\end{equation*}
$$

Next take the case when the electron is removed so slowly that the system of electrons is always in equilibrium. The work required is the difference between the potential energy of the atom in its original state when it contains $n$ electrons and in its final state when it contains $(n-1)$ electrons. The value of the former is

$$
\begin{equation*}
\frac{1}{2} \frac{n e^{2}}{r}\left(n-\frac{S_{n}}{4}\right) \tag{12}
\end{equation*}
$$

that of the latter

$$
\begin{equation*}
\frac{1}{2} \frac{(n-1) e^{2}}{r_{1}}\left(n-\frac{S_{n-1}}{4}\right) \tag{13}
\end{equation*}
$$

where $r_{1}$ is the radius of the atom when one electron has been removed.

For the equilibrium of the electrons in this state we have

$$
\begin{equation*}
\frac{E e}{r_{1}^{2}}-\frac{e^{2} C}{r_{1}^{3}}=\frac{e^{2} S_{n-1}}{4 r_{1}^{2}} \tag{14}
\end{equation*}
$$

from the equilibrium of the atom in its original state we have

$$
\begin{equation*}
\frac{E e}{r^{2}}-\frac{e^{2} C}{r^{3}}=\frac{e^{2} S_{n}}{4 r^{2}} \tag{15}
\end{equation*}
$$

hence

$$
\begin{equation*}
\frac{1}{r_{1}}=\frac{1}{r}-\frac{\left(1=\frac{S_{n-1}}{4 n}\right)}{1-\frac{S_{n}}{4 n}} \tag{16}
\end{equation*}
$$

and the difference between the potential energies is

$$
\begin{equation*}
\frac{1}{2} \frac{c^{2}}{r}\left\{n\left(n-\frac{\dot{s}_{n}}{4}\right)-(n-1) \frac{\left(n-\stackrel{s}{n-1}_{4}^{4}\right)}{n-\frac{s_{n}}{4}}\right\} \tag{17}
\end{equation*}
$$

if $V_{2}$ is the ionizing potential for slow ionization. In caleulating these ionizing potentials we have assumed that the law of force between the positive charge and the electron was expressed by $\frac{E c}{r^{2}}-\frac{c^{2} C}{r^{3}}$ at all distances. There is evidence, howerer, that the repulsive term varying inversely as the cube of the distance has only a limited range of action and that bevond this range the force varies strictly as the inverse square of the distance. If we suppose that the range of the repulsive force $\rho C e, E$, then the work done in taking an electron from a distance $r$ to an infinite distance will be

$$
\begin{align*}
& \int_{r}^{\sim} \frac{E \varepsilon}{r^{2}} d r-\int_{r}^{\rho} \frac{e^{2} C}{\rho^{3}} d r \\
& \quad=\frac{E \varepsilon}{r}-\frac{1}{2} e^{2} \frac{C}{r^{2}}+\frac{1}{2} \frac{E^{2}}{\rho^{2} C} \tag{18}
\end{align*}
$$

In calculating the ionizing potential, we have neglected the last term and so have underestimated its value. Neglecting this correction, the ionizing potentials for the elements whose outer layers contain 1, 2, 3, $4,5,6,7, \delta$ electrons, respectively, are given in Table $V . r_{1}$ is the radius of the outer layer of the one electron atom, $r_{2}$ that of the two electron atom and so on. The third column gives the potential in volts when the values of $r_{1}$ and $r_{2}$, given by W. L. Bragg (loc. cit.) are substituted in column 2. These values apply to the ionization of the atom and not of the molecule. In experiments on the ionizing potential it is the value for the molecule and not for the atom which is in general determined.

## Specific Inductive Capacity

Further information about the atom is afforded by the study of the specific inductive capacity of the gas. We shall proceed to find the value of the specific inductive capacity of atoms containing different numbers of electrons.

The case of the one electron atom is exceptional because such an atom in its undis${ }^{5}$ Phil. Mag., 27, p. 75\%.
turber state has a finite clect meal monnent; it will therefore tend to set in an elecetrie field and this will give rise to a term in the specifie inductive capacity independent of the displacement of the electrons inside the atom by the electric field; this 10 mm will vary

TABLE V

| Number of Electrons in Outer Layer | Ionizing Potential for Quick Ionizaton |  |
| :---: | :---: | :---: |
| 1 | ${ }^{1} 2 e^{2} / r_{1}$ | 4.8 Jithium |
| 2 | .625 $e^{2} / r_{2}$ | 8.1 Beryllium |
| 3 | (1i:3:3 $e^{2 / r} r_{3}$ |  |
| 4 | .ii3 $e^{2} / r_{4}$ | 11.8 Carbon |
| 5 | .54 $c^{2 / r_{5}}$ | 12 Nitrogen |
| 6 | .i2 $e^{2} / r_{6}$ | 12 Oxygen |
| 7 | . 5 e $e^{2 / r_{7}}$ | 10.5 Fluorine |
| 8 |  |  |

rapidly with the temperature. ${ }^{5}$ In addition to this effect due to the setting of the atoms there will be an effect due to the displacement of the electrons relative to the central core under the action of the electric field; this effect will be present in atoms containing more than one electron. The effect due to setting is absent when the normal atom has no finite electrical moment.

## Two Electron Atom

If $a$ is the distance of cither of the electrons from the center of the normal atom, $X$ the external electric force, then if this force is in the direction of the line joining the electrons, the displacement $\delta x$ of either of the electrons in the direction of the force is given by the equation

$$
\begin{equation*}
c \delta x=\frac{4}{5} a^{3} . \tag{19}
\end{equation*}
$$

This displacement of the electron relative to the positive charge endows the atom with an electric moment $2 c \delta x$, and if $N$ is the number of atoms per cubic centimeter, the electric moment per cubic centimeter is

$$
\begin{equation*}
N \frac{S}{5} a^{3} X \tag{20}
\end{equation*}
$$

hence if $K_{1}$ is the specific inductive capacity of these atoms

$$
\begin{equation*}
K_{1}-1=4 \pi N \frac{S}{5} a^{3} \tag{21}
\end{equation*}
$$

If the electric force acts at right angles to the line joining the electrons, then

$$
\begin{equation*}
e \delta x=4 a^{3} X \tag{22}
\end{equation*}
$$

and $K_{2}$, the specific inductive capacity for
atoms oricutaterl this was, is givern by the ("qualtion

$$
\begin{equation*}
K_{2}-1=1 \pi N^{2} \times d^{3} \tag{2:3}
\end{equation*}
$$

If the atoms in the gas ate maformly orientated. the specific induetive capracity $\Sigma^{\prime}$ of the assemblage will be given by the equation
$\mathrm{Ol}^{\circ}$

$$
K=\frac{\grave{L}_{1}+2 \check{K}_{2}}{3}
$$

$$
\begin{equation*}
K-1=4 \pi N u^{3} \times \frac{\AA \times 11}{15} \tag{24}
\end{equation*}
$$

the refratetivity of an element in the first periond to the corresponding element in the secomd and third periods is the same for all fhe dements. We have seen that for members of the same family the ratio of the values of $K-1$ is equal to the ratio of the volumes of the elements. So from these experiments we arrive at the interesting deduction that, on passing from one period to the next, the volumes of all the atoms are increased in the same proportion.

TABLE VI
Specific Inductive C'apacity of Atoms with Two to Eight Electrons

| No. of Electrons | Arrangement | $K$ | Mean Value of $K$ |
| :---: | :---: | :---: | :---: |
| § | Cube. | $1+4 \pi r^{3} N .4^{\prime} 338$ | $1+4 \pi r^{3} N \cdot 4^{\prime} 3: 38$ |
| 8 | Twisted cube force perpendicular to sq. face. | $1+4 \pi r^{3} N .4^{\prime} 27$ |  |
| 7 | Onc layer force perpendicular to plane of pentagon. | $1+4 \pi N a^{3} \cdot 3^{\prime} 605$ | $1+4 \pi a \quad N .4^{\prime} 29$ |
| 7 | One layer force parallel to plane of pentagon. | $1+4 \pi N a^{3} \cdot 4^{\prime} 634$ |  |
| 6 | One layer. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . | $1+4 \pi N r^{3} \cdot 4^{\prime} 269$ | $1+4 \pi r^{3} N .4^{\prime} 269$ |
| 5 | One layer force perpendicular to plane of triangle.... | $1+4 \pi a^{3} N \cdot 4^{\prime} 655$ | $1+4 \pi a^{3} N .4^{\prime} 236$ |
| 5 | One layer force parallel to plane of triangle......... | $1+4 \pi a^{3} N \cdot 4^{\prime} 027$ |  |
| $t$ | Tetrahedron . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . | $1+4 \pi N r^{3} .3^{\prime} 9$ | $1+4 \pi N r^{3} .3^{\prime} 9$ |
| 3 | Triangle force perpendicular to plane of triangle.... | $1+4 \pi N r^{3} .5^{\prime} 203$ | $1+4 \pi N r^{3} .4^{\prime} 39$ |
| 3 | Triangle force parallel to planc of triangle. . . . . . . . . | $1+4 \pi N r^{3} .3^{\prime} 981$ |  |
| ? | Force perpendicular to line of electrons. | $1+4 \pi N r^{3} .8$ | $1+4 \pi N r^{3} \cdot 5^{\prime} 87$ |
| $\because$ | Force parallel to line of clectrons. . . . . . . . . . . . . . . . . | $1+4 \pi N r^{3} \cdot 1^{\prime} 6$ |  |

The value of the specific inductive capacities for gases whose atoms contain from two to eight electrons is given in Table VI, which has been calculated by Miss Woodward.

It will be noticed that if $K$ is the specific inductive capacity of a gas in the atomic condition, $K$ is equal to $g a^{3}$, where $a$ is the distance of the outer electrons from the center of the atom, $g$ is a quantity depending on the number of electrons in the outer layer. For elements belonging to the same family the number of electrons in the outer layer and therefore $g$ is constant, so that the ratio of specific inductive capacities of two members of one family should be the same as the ratio of the volumes of the atoms. Cuthbertson has pointed out that there are some remarkably simple relations between the refractivitices and therefore between the values of $k$ - -1 , for consecutive elements in the same family. This is shown by Table VII given hy Cuthbertson and Prideaux. ${ }^{6}$

Thus for these four families the ratio of

[^51]Some confirmation of this is furnished by the determinations by W. L. Bragg ${ }^{7}$ of the diameters of the atom of the various elements, these were made by measuring by the Rönt-gen-ray method the distance between the metal and the negative element in a series of

TABLE VII

| Element | Refractivities | Approximate Ratio |
| :---: | :---: | :---: |
| Helium. | 72.0 | 1/2 |
| Neon. | 137.4 | 1 |
| Argon | 56.8 | 4 |
| Krypton. | 85.0 | 6 |
| Schon.. | 137.8 | 10 |
| Fluorine . | 195 | 1 |
| Chlorine. | 768 | 4 |
| Bromine. | 1125 | 6 |
| Iodine. | 1920 | 8 |
| Nitrogen. | 297 | 1 |
| Phosphorus:. | 1197 | 4 |
| Oxygen. | 270 | 1 |
| Sulphur.... | 1101 | 4 |

salts. $I_{11}$ these the atoms of the negative elements are probably negatively eharged and are not in the state of neutral atoms. For the electronegative elements the diameters are as follows:
$\AA$ is $10^{-3} \mathrm{~cm}$.
$\mathrm{F}=1.35 \mathrm{~A}$
$O=1.30 \AA$
$C=1.54 K$
$\mathrm{Cl}=2.10 \mathrm{~A}$
$S=2.05$ i
$\mathrm{Si}=2.35 \mathrm{I}$
$\mathrm{Br}=2.38 \mathrm{~S}$
$\mathrm{Se}=2.35 \mathrm{~d}$

For the ratio of the diameters, we have
$\mathrm{Cl} / \mathrm{F}=1.55$
$\mathrm{Br} / \mathrm{F}=1.76$
I/F $=2.07$
$\mathrm{S} / \mathrm{O}=1.57$
$\mathrm{Se} / \mathrm{O}=1.8$

For these elements, which are all alecter negative ones, there seems thas stme exidence from direct macasuremonts that the ratio of the diameters of the atoms of corresponding elements in two periods is ernstant. It does not, howerer, apply w the electropositive elements like the alkali metals. Thus, for example

```
Na/Li=1.185 K/Li =1.38 RO/Li=1.K
Mg/13c=1.24 Ca1 /Be=-1.5 Sr/13e-1.7 Bat/Be 1.8
```

Thus the increase in the size of the atoms of corresponding metals in different periods is not nearly so large as in that of the atoms of corresponding electronegative elements.
(To be contunued)

# Radio Broadcast Central <br> wJy and wJZ, NEW York city 

By I. F. Byrnes and H. R. Butler<br>Radio Evgineering Department, General Electric Compani


#### Abstract

We feel fortunate at being able to present in the following pages so complete a description of the latest and undoubtedly the best equipped of broadcasting stations, termed "Broadcast Central" and operating under the call letters WJY and WJZ. This radio source of simultaneous classical and popular entertainment in reality functions as two independent stations in each of which there are sets of duplicate cquipment, one being a reserve. In other words, the entire equipment would furnish the "makings" for four stations. Although it has been in service but a short time, and its duplex function an innovation, the operation of Broadcast Central has been phenomenally successful.-Editor.


On May 15th, this year, radio listeners in the eastern part of the United States were able to act as silent participants at the opening of the newest and latest broadcasting station situated at Aeolian Hall, New York City. The equipment at "Broadcast Central," as the new station has been termed, is operated by the Radio Corporation and embodies several new features to insure the highest quality of reproduction and continuity of service.

In the first place the location of Radio Broadcast Central is ideal in that it is at the heart of New York City, which is the center of some of America's best music and art. Excellent concerts and recitals are continually being held in Aeolian Hall itself and provision has been made to broadcast these programs. In addition, special wire lines run to the more important theaters and hotels so that outside programs are readily transmitted by the station.

## Two-channel Operation

One of the chief features that is prominent at Broadcast Central is the "two-channel" operation or simultaneous transmission of
two programs on separate wavelengths. One channel operates on a wavelength of $40 \%$ meters with the call letters WJY and is used to broadcast popular music, lectures, etc. It has been appropriately called the "jazz" channel. The second channel transmits on a wavelength of 45.5 meters and uses the call letters WJZ, replacing the station formerly located at Newark. The WJZ channel is used for the transmission of operatic and all classical music. Both studios are located on the sixth floor of the Aeolian building, while the transmitting equipment is housed in a special room built on the roof.

## Description of Equipment Studio

In describing the transmitting equipment it should be remembered that technically the two channels are identical, so that only one will be described. The apparatus comprising this equipment may be divided into three groups; viz., that contained in (1) the studio. (2) the control room, and (3) the transmitter room.

As may be seen in Figs. 1 and 2, each studio itself is a medium sized room which has been
acoustically deadened by draperies and especially prepared walls to prevent olijectionable echoes that might be pieked up by the sensitive microphones.
portable podestal which can be properly located with respect to the performers by the studio director. 'There are also two mierophones on the announcer's desk, which


Fig. 1. The Classical Studio, WJZ


Fig. 2. The Popular Studio, WJY

The microphones used in "picking up" the music or speech of the various artists are two in number, and are mounted side by side on a
are used only for making announcements regarding the program. Only one "announce" or one "concert" microphone is
ordinarily used at a time; the control room operator having the power to choose which anmounce and which concert microphone shall be used.

The change from announce microphone to concert microphone is, however, at the disposal of the amouncer or studio director by virtue of the "director's control box." Fig. 3, which is fastened to the desk near the announce microphone. This unit contains a threc-way telephone key and a greencapped signal light. The three positions of the key are marked "Off," "Amounce," and "Concert," and in each position the proper relays are operated in the control room to comnect the tone generator, the announce microphone, or the concert microphone, respectively, to the amplifying equipment. This operation will be more fully described later.

The key is also utilized to operate a signal system which indicates whenever any transmission is taking place from the studio. Whenever the key is not in its "off " position. a contact is closed which lights two small red signal lamps, one of which is in the control
with the transmission of the program is warned of the fact that the studin is in operation, and interruption is reduced to a minimum.

The green signal light in the studio control bex is for the purpose of informing the studio


Fig. 3. Director's Control Box
director or announcer that the station is in operation and all apparatus in readiness for the program. The method for operating this signal will be described later.


Fig. 4. Microphone Amplifier Rack
room, and the other in the transmitter room. Also another contact is closed which, through a relay, effects the illumination of a redlettered sign in the studio reading "Silent," and a similar sign in the reception room reading "Caution." Thus everyone connected

## Control Room

Passing now to the control room, we have three main units: (1) the microphone amplifier rack. (2) the oscillograph, and (3) the timesignal receiver. The microphone amplifier rack is shown in Fig. 4. It is an angle-iron
framework having nine sections, into which removable mints of uniform size may be bolted. The units used in this ratek are four "microphone amplifiers," two "line ampliliers." a microphone control pancl, a filament control pancl, and a chopper unit.

Each microphone amplifier contains the apparatus for controlling the current which will flow through any microphone connected to it, an amplifying tube (UV-202), microphone transformer for transferring the
neeted to one of the four microphones situated in the studio. At the bottom of this panel hang four telephone plugs, each one being connected to the input of one of the four microphone amplifiers. Thus by properly manipulating these plugs, any microphone may be connected to whatever amplifier it is to operate. It should also be noted that there are several spare jacks on the panel to accommodate any additional microphones which may be installed.


Fig. 5. Simplified Connection Diagram of One Channel at Broadcast Central
output of the microphone to the input of the amplifying tube, and a variable-resistance shunt across the primaries of the transformers whereby the volume obtained from the amplifier may be regulated.

The method of connecting the various microphones to the amplifiers provides maximum flexibility by means of the microphone control panel seen at the lower left-hand corner of the rack. On this panel are four telephone jacks, each one of which is con-

Having conducted our program in electrical form to the input of the first amplifier, we come next to the filament control panel whose function is to determine which of the four amplifiers shall be connected to the succeeding apparatus. The simplified schematic wiring diagram shown in Fig. 5 will assist in following the various amplifier circuits.

The first puint to be noted is that the output of all the five-watt amplifiers (UV-202)
is connected to a common wire which goes directly to the "speech amplifiers" located in the transmiter room. Thus the only operation necessary to place any one amplifier in operation is to light the filament of the respective amplifier tube. In the filament control panel are four telephone jacks each one of which forms one sile of the filament circuit of one of the four amplifiers. Below the panel are two pairs of telephone plugs, each pair being comected to an individual relay which, when closed, will place filament potential on the plugs connected to it. These two relays are known as the "announce" and "concert" relays, and are operated by the corresponding position of the studio director's control key. To make clearer the functions of the rarious control units, we shall follow through the operations necessary for placing the microphone amplifiers in readiness for a zoncert.

The control room operator decides that he will use, for instance, announce microphone No. 1, and concert microphone No. 2. Also he decides that he will use microphone amplifier No. 1 for announce purposes, and amplifier No. 3 for concert purposes. First he goes to the microphone control panel and inserts the plug labeled "No. 1 " into the jack "Announce No. 1," and also the plug "No. 3" into the jack "Concert No. ?." This connects announce microphone No. 1 which is on the studio director's table to the input of amplificr No. 1 and also connects concert microphone No. 2, which is on the microphone stand in the studio, to the input of amplifier No. 3. The operator adjusts the current in the two microphones and goes to the filament control panel. Here he inserts one of the plugs connected to the announce relay into jack "No. 1," and also one of the plugs connected to the concert relay into jack "No. 3." Now as soon as the studio director moves his key to the announce position, the amounce relay is operated thereby lighting the filament in amplifier No. 1, and causing sounds picked up by announce microphone No. 1 to operate the set. Again, when the studio key is moved to the concert position, the announce relay drops out while the concert relay comes in, lighting the filament of amplifier No. 3 and placing concert microphone No. 2 in,readiness for the artist or performer.

Another feature not previously mentioned is performed by the studio control key when in the "off" position. Two relays are operated simultaneously in the chopper unit,
which unit contains, as sughested hey its name. a chopper or tone-whed driven liy a smatl direct-curcent motor. One of the relays starts the motor and the other commerts the brushes of the chopper whee directly from the plate circuits of the microphome amplifiers, to ground. Since there are 16 insulated segments on the tone-wheel, which revolves at 1800 r.p.m., the effect of this device is to make and break current through the microphone amplifier plate resistance 4 o times a second, thereby modulating the transmitter with a 480 -cycle note. A variable resistance is shunted around the tone-wheel to control the amount of fluctuation of current and consequently the intensity of the tone produced. This arrangement was designed so that, if desired, the station could be given a distinguishing tone, enabling it to be easily tuned in when not actually broadcasting a selection. The tone may be easily eliminated by opening the motor supply.

The two line amplifiers are in the two upper compartments of the right-hand row, and consist of an amplifying tube (UV-202), a rheostat for controlling the intensity of amplification, and a transformer for coupling a telephone line or other source of signal to the input of the tube. Thus concerts or speeches from distant points can be transmitted over land line to the broadcasting station and then radiated in the usual manner.

Before leaving the microphone amplifier rack, mention should be made of a few other units to be found on the filament control panel. A jack labeled "Studio Output" is in series with the common output of the rack. thus enabling the operator to assure himself that his part of the apparatus is functioning properly. Also there is a jack labeled "Radio" which furnishes the operator with the output of a crystal receiving set for the purpose of observing the quality of the radio transmission.

Of the four signal lights seen at the top of the panel, one is the red signal previously mentioned, one a green signal in series with that of the studio control box, and the other two are white signal lights used for signalling between the control room and transmitter room.

In order to enable the operator to make the proper adjustments of the amplifiers, means must be provided for determining at all times how much the antenna current is being modulated. This is sometimes done merely by listening to the signal intensity with a receiving set, or by noting the fluctuation of
current to the modulator tubes, or by measuring the voltage across the modulation reactor. These methools are, however, only comparattive and approximate, and give little idea of the actaal pereentage of modulation. For these reasons an oscillograph is furnished in the control room. ('This is the unit on the left in Pig. . .) A rectified portion of the antema current is supplied from the transmitter room by a vacuum-tube rectifier, to the vibrator of the oscillograph, thereby giving a continuous picture of the output of the station on a motor-driven mirror. The


Fig. 6. Speech Amplifier Rack
light for the oscillograph is furnished by a specially developed high-current incandescent lamp, supplied through a transformer from the 88 -volt 30 -cycle winding of an exciter in the transmitter room. Current for the mirror motor and magnetic field is supplied from the lighting mains at 115 volts direct current.

The only remaining unit situated in the control room is the time-signal receiver. In order to transmit the naval observatory time signals, which are broadcast from station NAA at twelve o'clock noon and ten o'clock night on a wavelength of 2500 meters, means have been provided for re-radiating these signals at the normal broadcasting wave. For this purpose a receiving set is supplied which contains, in addition to the tuning, detector, and amplifier system necessary for picking up NAA's signals, a double-
trap circuit which prevents energy from the WJ\% and WJY antemas from being picked up) and fed back into the input thereby causing howling. The output of this receiver is fed into one of the line amplifiers previously mentioned, and thus N $\Lambda$ 's natural tone is again sent out in the same manner as a concert or speech from some outside source.

## Transmitter Room

We shall now pass from the control room up to the transmitter room. This is in a special building erected on the roof of the Acolian building, and situated midway between two $120-\mathrm{ft}$. structural-steel towers which are located at each end of the roof about 175 ft . apart. Within this building is housed all the power equipment of the station including motor-generator, batteries, speech amplifiers, and the transmitting units themselves.

Still following our entertainment as it passes through the various groups of apparatus, we come now to the speech amplifier rack. This unit, Fig. 6, follows in its mechanical construction the general form of the microphone amplifier rack in the control room as it also is divided into nine small compartments, each containing an individual unit. In this case, however, the whole lower row of units, consisting of two resistancecoupled amplifiers and a reactance-coupled power amplifier, is an exact duplicate of the upper row, while the middle row contains the coupling unit on the left, the input unit in the middle, and the output unit on the right.

In explaining the operation of this unit it will be remembered that the plates of all the amplifying tubes in the control room are connected to a common point. From this point a specially shielded line runs up to one contact of each of two relays in the coupling unit. Since these relays, called amplifierinput relays, merely determine which of the two duplicate rows of amplifiers the speech current will enter, we shall follow only the lower route. The other contact of the relay corresponding to the lower bank is connected to an 80,000 -ohm resistor and also to a $0.5-$ microfarad condenser. These form a plate resistance and coupling condenser for the microphone-amplifier tubes below. Thus the output of the microphone amplifier is really the other terminal of the coupling condenser which goes directly to the input of the lower left-hand speech amplifier, and also to the sleeve side of a two-circuit telephone jack
mounted in the coupling unit and marked "Two Stages." The speech amplifier just mentioned is, like the microphone amplifier, of the resistance-coupled type, but uses a $50-$ watt pliotron, $100,000-$ ohm grid leak, $40,000-$ ohm plate resistance, and 0.5-microfarad coupling condenser. The output of this amplifier is led back to the compling unit and connected to the slecve side of another telephone jack marked "Three stages." The third jack shown is marked "Amounce," and the sleeve side of this jack is connected to the secondary of a microphone transformer whose primary is connected to a desk-stand microphone on the operator's desk. So it is seen that the sleeve side of each of these jacks normally carrics an audio-frequency voltage from an individual source. These voltages are utilized by means of a telephone pluy whose sleeve side is connected to the input of a sccond speech amplifier which is an cxact duplicate of the first, and occupies the center position in the lower row of units. The output of this unit is connected directly to the imput of the unit immediately on its right. which is a reactancecoupled amplifier. Since this is the last stage of amplification before the modulator grids, it must handle considerable power with good regulation, for which purpose reactance instead of resistance is used in both the plate and grid circuits of the 50 -watt tube. On account of the low ohmic resistance of the plate reactance, a negative bias of about 30 volts is fed through the grid reactance to prevent excessive plate current, and to provide linear amplification. The output from this last stage is obtained through a 0.5microfarad coupling condenser as in the previous stages.

Now the purpose and marking of the three jacks in the coupling unit may be easily understood. If the plug carrying the input circuit of the second speech-amplifier stage is plugged into "Three Stages," all three stages are in operation in cascade. If it is plugged into "Two Stages," the output of the coupling unit, or microphone amplifier, passes directly to the second stage thereby eliminating the first resistance stage. If the plug is inserted in "Amnounce," the output of the operator's microphone is connected to the last two stages, and the transmitter may be modulated from the transmitter room independently of the studio.

On returning to the output of the reactance amplifier it should be noted that an exactly similar path may be traced through the
upper row of amplifiers, using the tip connections of the telephone phig and jacks mentioned. Thus the out put of the reactance amplifier passes through an amplifierorntput relay to a bus common to fonur relays. These consist of the two amplifierentutut relays and two transmitter-input relays whereby either set, or bank, of amplifiers may be connected to either transmitter as desired in a manner to be described later.

Grid bias for the modulator tubes is normally supplied by a 4.j-volt dry battery connected through a high reactance to the output of


Fig. 7. Transmitting Panel
whichever reactance amplifier is being used. These reactors are located in the respective reactance stages themselves.

The four relays mentioned, together with two more known as biasing relays, make up the output unit. Jacks for listening to the outputs of the four resistance stages are also located on this panel.

The input unit contains only four relays for supplying plate and filament voltages to either one or both of the two amplifier banks.

Having passed through the speech amplifiers, we come now to the transmitter proper shown in Fig. 7. This unit utilizes two 250watt oscillator tubes and two 250 -watt
 means of power relays, with 11 volts alternating cument for filaments, and $2 \theta(\theta)$ volts direct curemt for plates. The primary oscillating circuit is mot conductively compled to the antema, but consists of an elgewisewound copper strip inductance and a highefficiency mica condenser. The hartley oscillating circuit is used and movable clips on the inductance provide for adjusting the wavelength as well as the plate and grid roltages for best operation. Placed in inductive relation to this primary inductance is a simitar inductance coil connected through an antema relay to the antema post of the
ratiating frepuency. This is very essential for stealy reception.

While considering the oscillating circuit, mention should be made of the operation of the green power-indicating signal lamps previously mentioned as being located in the control room and studio. Whenever the transmitter is oscillating properly, a current of from 30 to 60 milliamperes flows in the gricl leak cirenit. A portion of this energy is used to operate a small relay, which in turn lights the two green signal lamps in series. In orfer that this signal may not be lighted when the set is oscillating into the tank and not supplying energy to the antemna, a spare


Fig. 8. Interior of the Transmitter Room
transmitter. The low-potential end of the coil is connected through a variometer to the counterpoise terminal of the transmitter, which terminal becomes ground if no counterpoise is used. Adjustable taps on this coil, in conjunction with the variometer, allow the antenna to be tuned to the frequencr of the primary or tank circuit, under which conditions maximum energy is supplied to the antenna from the tank. The advantage of this circuit is that, due to the relatively loose primary to secondary coupling and the fairly high circulating energy in the tank, slight changes in antenna constants caused by swinging do not appreciably change the
contact on the antenna relay is also included in the lamp circuit, allowing illumination only when the antema is actually connected and radiating energy.

The modulation system used is the wellknown plate system whereby the voicefrequency voltages impressed upon the modulator grids by the speech amplifier cause corresponding voice-frequency voltages of much greater intensity upon the oscillator plates, which changes of voltage in turn cause audio-frequency variations in the amplitude of the radio-frequency output. Thus the weak sound waves acting upon the microphone diaphragm in the studio are
reproduced in form, with very little distortion, in the powerful variations of radiated energy emanating from the antema system to be intercepted by thousands of ratio recciving sets which reproduce more or less perfectly, the orginal somud waves.

Several more units accessory to the operation of this whole system remain to be described. The filter pancl, Figs. sand 9, is situated between the two transmitersand contains two resistance and capacity filters which cut down and smooth the output of one commutator of each 2000 -rolt gencrator to supply the proper plate voltage to the microphone and speceh-amplifier tubes. A separate filter is prowided for the generator belonging
with the corresponding lamp in the filanemt control pand in the control roonn.

Four telophone jacks are shown Tho lower left-hand jack is labeled "Stullo (hotput" and is in series with the correspondines jack in the filament control mint in the control rom. The upper left-hand jack allows supervision of the input to the modulator tubes by means of a high series resistance eomnected to the modulator grid circuit of whichever transmitter is being used. The jack on the lower right gives an indication of the radio output of the channel by means of a simple crystal receiver. Thus complete supervision of operation may be had, step by step, throughout the equipment.


Fig. 9. Another View of the Interior of the Transmitter Room
to each of the two transmitters, and the two required voltages are supplied from the proper filter by two pairs of relays, known as filter relays, whose operation is described later. The filter panel is also used to mount the filament voltmeters and rheostats of the two transmitters.

The heart of the whole transmitter room apparatus is the operator's control box. Figs. 10 and 11. This unit contains all the various jacks, signals, and switches that are necessary for supervision and for operation of the various relays previously mentioned. Of the three signal lights seen at the top of the unit, two are white and one red, and each is in series

The last jack shown is for plugging in the desk stand microphone for announcing or testing purposes, as has been described.

The top row of switches on the control unit is in comnection with the transmitter alone. The push-button type on the left operates the automatic starter of the motorgenerator set belonging to the left-hand transmitter. The right-hand push button belongs correspondingly to the right-hand transmitter. The center switch of this row is a single-pole double-throw tumbler switch. Thrown to the left, it operates the antenna relay and transmitter input relay of the lefthand set, and also the two filter relays cor-


Fig. 10. Operator's Control Box
responding to the filter used with the lefthand generator. In this manner the lefthand set is connected to the antenna and to the amplifier output, and is ready for operation as soon as the high-voltage field relay and the filament lighting relay are closed. These latter operations are taken care of by the vertical single-pole single-throw tumbler switch on the left. Also that filter is connected in which it is sure to receive power from the generator in use. Throwing the middle switch to the right and throwing up the right-hand tumbler switch perform exactly the same operations for the right-hand transmitter.

Since power is supplied to a transmitter on the operation of the corresponding vertical switch alone, regardless of the position of the middle horizontal switch, it is seen that


Fig. 11. Interior of Operator's Control Box
the set may be caused to oscillate into the tank circuit without feeding energy to the antenna. This is often desirable, but it is also evident that under these conditions the transmitter input relay for this set is open, hence the modulator grids do not receive their normal bias. This is taken care of by the bias relay which places negative 125 volts from the motor-generator on the modulator grids of the set not in actual operation.

The lower row of switches in the control box pertain to the amplifiers only. The two outside vertical tumbler switches are labeled "Power No. 1" and "Power No. 2" and operate the proper relays in the input unit to supply plate and filament current to the lower and upper banks of amplifiers respectively. The center horizontal tumbler switch, corresponding to the transmitter changeover


Fig. 13. Interior of Oscillograph Rectifier
switch abose phaces either one of the amplifier banks in circuit. Thus if thrown to the left, the amplifier input relay in the input unit belonging to the lower amplifier bank, and also the amplifier output relay in the output unit belonging to this same bank are closed. When thrown to the right, the corresponding relays for the upper bank are closed.

The extreme flexibility of the whole equipment may now be seen as there is a complete duplication throughout of every important part of apparatus necessary for the transmission of a program. Also, changeover from one piece of apparatus to another is made very easy and rapid by use of concentrated controls which uperate remote relays.

A small though important piece of apparatus which is used in connection with the oscillograph is the oscillograph rectifier, Figs. 12 and 13. This unit is mounted on the wall of the transmitter room near the antenna leadout. A small edgewise-wound inductance which is mounted in inductive relation to a single loop in the antenna lead is tuned by a variable condenser within the rectifier. A portion of the high-frequency current set up in this tuned circuit is sent through a rectifier tube (UV-217) and the resulting rectified current, whose pulsations are an exact copy of the audio-frequency variations in the radiated wave, is passed through the vibrator of the oscillograph in the control room below for visual observation of the final output of the whole equipment.

The three-unit motor-generator set used with the transmitters is shown in Fig. 14. The middle machine is the mutor which operates on 12.5 volts direct current from the building main. The right-hand machine is a combined alternating current and direct current generator furnishing 125 volts direct current for the high-voltage generator field and grid bias, and is volts alternating current for filament lighting and the oscillograph lamp. A voltage regulator keeps the alter-
nating-current voltage of this machme constant, thus insuring constant filament temperature when onee adjusted The left-hand machine is the high-voltage generator which has a 1000 -volt commutator at eath end thas giving 1000 volts for the amplifer plate filter and 2000 volts for the transmitior


Fig. 15. Roof of Aeolian Hall showing the Antennas
The only unit which is common to the two channels is the battery charging panel. Two 480 -amp.-hr. 12 -volt lead batteries are supplied with each channel for filament lighting and signalling. A single motor-generator is used for charging, and by a system of doublethrow switches any of the four batteries may be placed on charge or discharge thereby providing absolute continuity of service if desired. The biasing batteries for the modulator tubes and reactance amplifiers are mounted in the rear of this pancl.


Fig. 14. Three-unit Motor-generator Set

In concluding the physical description of the installation, mention shomd be made of the antemas, or radiating system, wheh are shown in Fige 15 and also on the cover of this issute As already mentioned, two 120 - ft . towers are located about 17.5 ft . apart on the roof with the transmitter romm midnaly between them.
 ft. long from which the four antema wires are suspended. The total span between the two towers is broken mp by ropes and insulators to form two separate four-wire antennas, one on each side of the transmitter room. The antema on the 4 ned Street side of the building is 55 ft . long, and a four-wire down lead deseends from this to the two tramsmitters used for the elassical chamel which operates on 45.5 meters. The antema on the $4 . \mathrm{rd}$ Street side is 4.5 ft . long and a
fedsle output of the mierophone can be offectively utilized.

The following equations give approximately the vollage amplification per stage that is obtained in the amplifying equipment.

The first stage or microphone amplifier uses a radiotron (UV-202) with 80,000 ohms resistance in the plate circuit, Fig. 5 .

We may express the uscful amplification factor of this type of resistance amplifier by

$$
u^{\prime}=\frac{u R_{L}}{R_{p}+R_{L}}
$$

Where $u^{\prime}=$ useful voltage amplification.
$u=$ amplification constant of tube.
$R_{L}=$ external or series plate resistance.
$R_{p}=$ internal plate-filament resistance of tube.


Fig. 16. Portable Control Equipment for Broadcasting from Outside Sources
similar down-lead makes connection with the transmitters of the channel which operate on 40.5 meters.

## Audio Amplifier Design

The microphones or "pick-up" devices used in broadcast work are designed to give, as nearly as possible, a uniform response for all frequencies in the audible range. This means that a range of approximately 30 to 5000 cycles must be covered. It also follows that the amplifier and associated circuits must cover this frequency range if highquality transmission is to be obtained.

In order to modulate completely the output of one of the transmitters at Broadcast Central, the audio voltage applied to the oscillators must be about 2000 volts. The output of a high-quality microphone is very small due principally to the highly damped diaphragm and seldom exceeds a few millivolts. It is therefore evident that considerable amplification is necessary before the

Solving for $u^{\prime}$ in the case of tube employed we have

$$
u^{\prime}=\frac{7.5 \times 80,000}{7000+80,000}=6.5 \text { approx. }
$$

In other words, the voltage developed across $R_{L}$ and applied to the grid of the second stage is 6.8 times the voltage delivered by the microphone transformer secondary.

The second and third stage audio amplifiers are located in the transmitter room and use radiotrons of a different type (UV-211). The amplification constant of this type tube is 12 and a series plate resistance of 40,000 ohms is used. At the low-plate voltage available for this tube a plate resistance of about 5000 ohms is obtained.

Therefore $u^{\prime}$ for the second and third stages is

$$
u^{\prime}=\frac{12 \times 40,000}{5000+40,000}=10 \text { approx. }
$$

The last stage amplifier also uses the same type and size of radiotron tube but is designed
as a reactance amplifier since it must supply some power to the modulator grid circuit． The useful voltage amplification，$u^{\prime}$ ，as obtained in this last stage is nearly the theoretical value of 12 over the essential audio－frequence band．
Summing up，the total voltage amplifica－ tion possible with all four stages is

$$
6.8 \times 10 \times 10 \times 12=\therefore 160
$$

In practice it is seldom necessary to use four stages，so that under average conditions the amplifier control plug on the speech amplifier bank is placed in the＂Two Stages＂


Fig．17．Outside Private Cable System of Broadcast Central
position which disconnects one of the resist－ ance amplifiers（じ「－211）．

## Design of Radio Circuits

Two radiotrons（L＇V－20t－A）are operated in parallel as power oscillators in each trans－ mitter at Broadcast Central．Instcad of using a direct coupled circuit as in many radio transmitters the tubes are connected to a primary or＂tank＂circuit which is in turn coupled to the antenna．This arrange－ ment of the oscillators is shown in Fig． 5.

There are three important advantages gained by using a tank circuit coupled to the antenna．

1．The frequency of the oscillations is determined almost entirely by the constants of the tank circuit．Then should the antenna characteristics vary due to swinging，etc．，the emitted frequency remains practically con－ stant，making zero－beat reception more reli－ able for the distant listener．

2．Harmonic radiation is reducert to a negligible degree due to the sedective prop－ erties of the coupled circuit

3．With two－channel operations as carricd out at Broadeast Central，reaction of one antenna on the other does not cause＂cross talk．＂If power from one antemna enters the antenna system of the other channel the undesired freguency does not reach the tube circuits and consequently does not affect the modulation of that particular channel．

The following values represent a typical operating condition for one of the trans－ mitters．Reference will be made to the oscillator circuit as shown in Fig．is．

Wavelength 400 meters（ 7.50 kilocycles）．
Antenna current 7 amp ．
Antenna capacitance 0.000 S microfarad．
Tank current 9 amp．
Tank capacitance 0.0008 microfarad．
Under these conditions approximately 16 turns are required on the tank incluctance． The alternating voltage required for the plate circuit of the oscillators is developed across turns $B$ and $C$ ．The alternating grid voltage is determined by the drop across turns $C$ and $D$ ．At 7.50 kilocycles，the 16 turns on the tank inductance have a reactance of about 26.5 ohms．This gives a reactive drop of 238.5 volts with 9 amp ．tank current．Assum－ ing equal potential distribution across the used turns on the coil，the drop per turn is $\frac{238.5}{16}=149$ volts．Since 10 turns are used in the plate circuit between points $B$ and $C$ ， the alternating plate voltage is 1490 ．Three grid turns are used between points $C$ and $D$ giving a resultant alternating grid voltage of 447．Due to the potential distribution not being uniform toward the lower end of the coil，the grid voltage is somewhat lower than this value．

The circulating kilovolt－amperes in the tank circuit may be expressed by $I^{2} X$ where $X$ represents the reactance of the tank capacitance or inductance at the operating frequency．In this case the tank $\mathrm{kr}^{-\mathrm{a}}=$ $\frac{9^{2} \times 265}{1000}=21.46$ ．The antenna $k T-a$. may be expressed in the same manner and are equivalent to $\frac{7^{2} \times 26.5}{1000}=13$ approximately．It is therefore evident that the antenna $\mathrm{kv}-\mathrm{a}$ ． under these conditions are about 60 per cent of the tank $\mathrm{kr}-\mathrm{a}$ ．This ratio gives good sta－ bility and frequency holding characteristics． In general，the tank kv－a．must at least equal the antenna $\mathrm{kv}-\mathrm{a}$ ．for reliable operation．

# Cooling of Turbine Generators 

## PART IV

# UTILIZATION OF HEAT IN STEAM-ELECTRIC POWER PLANTS 

By A. R. Simen<br>


#### Abstract

This series of articles was started in our issue of Docember, late , when the author dealt in Part I with the various ways of cooling air when recirculated. Part 11 was published in our February issue and covered the heat transfer in surface air coolers, and in our May issue we published Part 111 which diseussed the details of design. In this, the fourth and concluding articte of the series, the author discusses the utilization of heat in steam-electric power houses, dealing in great detail with the heating of air for combustion and other features of heat utilization.- Enitor.


The purpose of this article is to present the general problem of steam-electric power plant economies with respect to temperature exchanges in a manner which may be readily understood or even visualized. No radical departures from prevailing practices in modern plants are proposed except the heating of the furnace air as a means of still further improving the overall plant efficiency.

The common methods now employed for heating the boiler feed water may be classified as follows:

1. Fuel economizers.
2. Exhaust steam from steam-lriven auxiliaries.
3. Extraction steam from the main turbine.
In some instances all of these methods may be used in series. The same means may be utilized for the heating of the air to the boiler furnaces with almost equal advantages. These, similarly classified, will be termed as follows:
4. Gas air pre-heaters (air economizers).
5. Steam air pre-heaters (using exhaust steam from steam-driven auxiliaries).
6. Steam air pre-heaters (using extraction steam from the main turbines).
The two major heat losses in a steam-electric power plant are in the gases leaving the stacks and in the circulating water leaving the condensers. It is obvious that if a relatively small percentage of this heat can be returned to the boilers or furnaces as a substitute for some of the fuel a gain will be effected. The problem, therefore, is to revert all of this heat possible to either the boiler or the furnace with the least complication and the highest efficiency. For many years there has been an intensive endeavor to reduce the temperature
of the stack gases and to reduce the weight of the gas by proper combustion so as to minimize this loss. The waste of heat in the condensing water is far in excess of the stack loss and it is only recently that any concerted effort has been made to reduce this waste. It should be borne in mind that every pound of steam that can be kept out of the condenser should result in a thermal advantage, besides reducing the size of the condenser and the congestion of steam in the latter stages of the turbine which generally exists due to the rapid expansion of steam at high vacua.

## Fuel Economizers

This name is not sufficiently descriptive because any piece of apparatus in the power plant which improves the efficiency is a "fuel economizer." A more proper name would be "waste gas water heater." Inasmuch as both the boiler and the economizer use the same gas (the economizer is now generally installed as a unit with the boiler) they should really be considered as a two-stage boiler because the only purpose of the economizer is to obtain a greater temperature difference between the gas and the water by dividing the unit into two stages so as to segregate the low temperature water from the water in the boiler which is at steaming temperature or thereabouts.

Possibly the greatest handicap to the economizer in the past was that the boiler manufacturer recommended and standardized boilers which took out so much heat from the gas that there was little work for the economizer to do, with the result that there were relatively few economizer installations and it was often difficult to justify the investment in economizers, except where the price of fuel was high and the load factor very good. The second handicap was that the installation of an economizer introduced considerable resist-
ance to the flow of gas as well as lowering its temperature which generally necessitated the use of induced draft fans.

The operation of boilers at several times their rated capacities materially increases the draft loss and if induced draft fans are to be installed anyway, the addition of a fuel economizer is advantageous aside from the improved efficiency inasmuch as the fans can be reduced in size because of the higher pressure that must be produced and the smaller gas volume that is handlect.

There is another possibility, and that is a reduction in draft loss through the boiler and through the coonomizer to such an extent as to make it possible to operate at high boiler ratings with reasonably high stacks and without induced draft fans. Excessive draft loss is largely the result of eddying, and simple baffles. properly arranged for more uniform gas velocities and as few turns as possible will undoubtedly greatly reduce the draft loss without affecting the performance.

With higher steam pressures, the water circulated in a boiler is of higher temperature and the use of fuel economizers becomes more and more advantageous. Furthermore, it is now more generally appreciated that with any predetermined exit gas temperature the division of heating surface between boiler and economizer should be carefully proportioned in order that each may do its proper share of the work.

There has prevailed amongst many operating engineers an impression that the feed water should not be heated by exhaust steam when fuel economizers are employed for the purpose of making a better showing for the economizer. This impression is wrong for the reason that the economic adrantage of heating water with exhaust steam is then deliberately discarded for the sake of a different form of economy. Furthermore, from a practical standpoint it is essential to have the feed water enter the economizer at a temperature above the dew point of the gases to avoid sweating and the consequent accumulation of soot which can not be readily removed. The dew point of a gas will wary with the character of the fuel. There was an old rule that the water should be 120 deg. F., or higher, when coal was used and 140 dea. F., or higher, when oil was used. These limits are gradually being raised and some now recommend as high as 170 deg . F. for certain grades of coal.

It is obvious from the foregoing that the boiler feed water should first be heated by exhaust or extraction steam to a temperature
higher than the dew point of the gases passing through the comomizer for pratical reasons and may be heated still hother for economical reasons. The cost of equipment to heat water with exhaust or extraction steam is not so expensive as the equipment necessary to heat it with the flue gas. On the other hand, the temperature removed from the flue gas is a complete gain; whereas, the heat extracted from the low pressure steam is but a partial gain. Furthermore, the economic value of extraction steam becomes less as the temperature of the water increases because at the higher temperatures there is less work done by the steam in passing through the turbine. A balance must therefore be struck between the work that the economizer is to do and that which is to be done by the steam water heater. This division will vary materially for different steam pressures and different local considerations. However, there is a distinct field for gas heating and for steam heating of the feed water in every properly balanced power plant.

## High Boilers

By the term "high boiler" is meant a boiler provided with more heating surface over which the gas travels so as to lower the flue gas temperature to a minimum. Such a boiler has a more uniform efficiency throughout its range of operation but when operated at its rated capacity may show but a slight improvement in economy over the standard boiler. The simplicity of a high boiler, if natural draft can be employed, as against the boilerwith economizers and induced draft fans, will in many cases favor the former. As the steam pressure is increased, the load factor improved, and the cost of fuel raised, the economizer installation will then have the advantage. It is therefore apparent that there is also quite a distinct field of service for each of these two designs.

## Exhaust Steam from Steam-driven Auxiliaries

This is by far the most common method of heating the feed water and besides its economic value, it served in the past to drop out some of the impurities in the water and minimized expansion and contraction stresses in the boiler. There existed, however, a somewhat prevalent idea that the efficiency or the water rate of such auxiliaries which exhausted into the feed water heater was of no moment. This is an erroneous impression because there is a definite amount of water which may be heated and there is a limiting temperature to which it may be heated, consequently there
is a fixerd amomat of heat which may be utilized and the less offecont the atwiliaries, the fewer the nomber of anxiliaries which may be exhatsted into the heater.

The necessity of asing effecient anxiliaries or obtaining the most by-prodnct power possible is now gencratly appreciated and the result is that most of the larger power plants are resorting to motor-driven anxiliaries and extracting the steam for heating the feed water from the main turbine where the lowest possible water rate per kilowatt may be obtained.

## Extraction Steam from the Main Turbine

Aside from the simplicity, from both an installation and an operating standpoint, of electrically driven auxiliaries in a power plant, the plan of heating the feed water by extraction steam is conducive to a perfect heat balance and makes possible the production of the greatest number of by-product kilowatthours.

A kilowatt-hour produced as a by-prochuct will have a fixed net steam consumption or net water rate regardless of the gross or apparent water rate because all of the steam exhausted from the machine is absorbed in the system as heat and therefore the net steam consumption is the heat in the kilowatthour plus the additional heat consumed in producing the mechanical and electrical losses of the machine; for example:

A kilowatt-hour contains 3412 B.t.u. If the machine has a mechanical and electrical efficiency of 90 per cent, then the total heat abstracted is 3750 B.t.u. which is equivalent to a net water rate of 3.87 lb . from and at 212 deg. If a turbine has a condensing water rate of 13 lb . from and at 212 deg., then the saving in pounds of steam per kilowatt-hour is 9.13 for every kilowatt-hour that can be produced as a by-product.

With a fixed amount of heat which may be absorbed by the feed water the greatest number of kilowatt-hours can be produced as a by-product by extracting steam from one of the latter stages where the lowest gross water rate prevails. But an extremely low gross water rate is accompanied by a low temperature, which naturally limits the amount of heat which may be put into the feed water. 'This condition is illustrated by the curves in Fig. 1, which show for a particular turbine that the greatest economy for singlestage extraction would be at the fourth stage, which is at a pressure of about $\$ \mathrm{lb}$. gauge.
'This naturally will vary with different turbines, steam pressures, superheat, and other conditions.

The more ceonomical method, of course, is to resort to series heating from clifferent stages and the number of stages that should be employer depends so much on conditions that no general recommendations can be made. If the feed water were heated from each stage in succession, the resulting economy would be as shown by curve "BB" in Fig. 1. But the improvement over two- or three-stage heating would gencrally not be worth the complication and therefore the most economical condition, from an overall standpoint, would lie somewhere between curves "AA" and "BB."

## Collection of Heat from Various Sources

The most natural thing to do is to collect unavoidable heat wastes in a plant such as: transformer losses, bearing losses. generator losses, drips, etc. The heat of the generator losses has in the past been wasted, except for a few isolated cases where this air has been discharged to the boiler room for combustion purposes and in many plants where the warm air was used in winter to assist in the heating of the turbine room. By using surface coolers for the generators it is possible to utilize most of the heat of the generator losses by circulating the condensate through the coolers. While the generator losses are a considerable factor when expressed as kilowatts, when converted into heat they are not of great magnitude and if the boiler feed water is heated by this means it must necessarily replace an equivalent amount of heating by extraction steam which is also an efficient process. Therefore, the absorption of the generator losses as heat can not be credited on an energy basis, but must be credited on a heat basis; comparing it with the saving in extraction steam to do the same work. The absorption of this heat, however, back into the system is often an important factor because otherwise it is a complete loss.

## Heating of Air for Combustion

It is difficult to understand why we have always considered it economical and advisable to heat the feed water before it was fed to a boiler but never considered it advisable to heat the air fed to a furnace. Only in the last two or three years has this subject been given any particular attention, although pre-heating of air for combustion purposes has been used
for many years in marine work in the form of the "Howden System" The ammont of byproduct electric encrgy which may be produced by heating the combustion air is almost as great as can be producel be heating the feed water, and the same statements can be made with reference to the reduction of the flue gas temperature by means of gas air preheaters as for gas water heaters or fuel economizers. Many engineers are still skeptical as to the resultant efficiency and fear that some difficulties may be encountered by introducing hot air, particularly with the stokers. Such disadrantages as have been suggested are discussed in the following paragraphs.


Fig. 1. Curves showing the Relative Economy of Single. stage Extraction and Multiple Extraction in Turbine Operation

## Heat from Eoiler Room

In the boiler room of small plants sufficient air for combustion can be taken from the building and this air may be relatively warm. In some cases it has helped to ventilate the boiler room; in others, it has produced air stagnation and was found objectionable. In the larger and more modern boiler rooms the amount of air used for combustion is so great that if it is not taken from outside the boiler room it is uncomfortably cold in winter and pipes are often frozen. Every provision is made for bringing fuel into a plant, but sufficient care is not always exercised in providing for the air. Fifteen to eighteen pounds of air is usually burned per pound of coal. which means that there must be delivered to the furnaces 200 to 250 cu . ft . of air for every pound of coal that is consumed. This most properly should be provided from ontside the building and the ventilation of the boiler room can better be taken care of independently. Arrangements may be made whereby air for combustion is taken partly from the boiler
form tor assist ventilation lan 110 wiat balk
 temperatures.

## Efficiency of Pre-heating Combustion Air

If the combustion of coal is thomsht of in lems of "burning air" rather thath "burning coal," the process is simple to mularstamd. and it is just as proper to talk of bumbing air on oxygen as of burning coal because there is usel fifteen to eighteen times as much air as coml by weight. Ssife from the radiant heat which is transmitted directly from the ineandescent fire to the boiler heating surface, the great bulk of the heat produced by the union of the carbon and the oxygen is transmitted to the nitrogen and thence to the heating surface. In other words, the intense heat which would have been formed in the combination of $\mathrm{CO}_{2}$ is diluted by the presence of nitrogen and the furnace gases kept within limits which may be handled with available materials. On one side of the stoker the air for combustion is delivered at a temperature ranging from 0 deg. F . to 90 deg. F . In the combustion chamber the temperatures may range from 2000 deg. to 2500 deg. F. If the combustion air enters the stoker at a higher temperature, then there is so much less coal that must be burned to increase the total gas temperature to the same point. On the other hand, if the amount of coal is reduced, then likewise the amount of air must be reduced so as to hold the same percentage $\mathrm{CO}_{2}$ in the gases. Therefore, if the boiler is to do the same work with less coal and less air, the furnace temperature must be slightly hotter.

If it is conceded that the furnace temperature is slightly hotter and that the ratio of air to coal has not been increased then the stack losses remain unchanged and all of the heat that was put in the combustion air must represent a true gain and does not have to be multiplied by the boiler and furnace efficiency to obtain the net gain.

## Increase in Furnace Temperature

At the present time furnaces are being worked to a temperature almost to the limit of the deformation temperature of the refractory materials and in many cases berond the fusing temperature of the ash, and the general opinion is that if the furnace temperature is raised, the maintenance of the furnace might become excessive. This is largely a matter of speculation because it is a question if a high furnace maintenance is not due more to the radiant heat than it is to the temperature of
the sases. It therefore rematios to be seen if there would be any increase in furnate maintenance due to the employment of hot combustion air within reasonable limits. Fumace maintenance is very much aggravated when beilers are foreed bevond the ratings. With a fixed amonut of heating surface and a fixed quantity of heat to be applied to the combustion air the air temperature will be lower as the boiler rating is inereased. Also refractory materials are being made to withstand higher temperatures than formerly and it is possible that more improvements will be made in the futime

However, if it is found that an increase in the temperature of combustion air shows an increase in furnace maintenance it is possible to allow a slightly higher ratio of air to coal and therchy reduce the $\mathrm{CO}_{2}$ percentage in the gas and still show an improvement in efficiency, depending on how much the ratio of air to coal has been changed. On the other hand, some plants are working with a $\mathrm{CO}_{2}$ percentage so high that at times some CO is produced which loss may more than offset the gain of the high $\mathrm{CO}_{2}$. If the combustion air is heated and the $\mathrm{CO}_{2}$ percentage lowered slightly, the operation is getting away from the danger line of the production of CO , and an improvement in conomy may be effected in this manner alone. A number of plants are now being designed to use heated combustion air in some form or another and the results obtained will probably be available shortly.

## Effect of Hot Air on Stokers

While most stokers depend on the cold air to hold down the temperature of the metal parts, the general opinion is that hot combustion air will not be detrimental to stokers, at least up to temperatures of 2.50 or 300 deg. F .

## Warm Combustion Air for other Fuels

What has been said in connection with burning of coal applies equally well to other fuels, such as fuel oil, gas, and pulverized coal. With such fuels warm combustion air will undoubtedly improve combustion and may possibly permit the use of smaller combustion chambers. For liquid, gaseous and pulverized fuels warm combustion air has already been employed by passing it through or around the hot furnace walls with good success.

## Gas Air Pre-heaters

The combustion air may be heated from the waste gases from the boiler or even from the
fuel comomizer. This construction has been used in Europe and is being contemplated in a few cases in this country. The gas air preheater has some advantages, when compared with the fuel economizer.
liirst: There are no high pressures to be dealt with and therefore thin steel tubes or plates or other forms may be used and need not be replaced until they are literally worn out.

Second: While the heat has to be transmitted from a gas to a surface and then from a surface to the air the unit heat transfer per square foot per degree difference is not materially different from a fuel economizer and the cost per square foot of surface should be considerably cheaper.

The gas air pre-heater also has some disadvantages, in that it is not always convenient to pass the air, which enters the stoker at the bottom of the boiler, by the gas which usually leaves at the top of the boiler. These two gases must be brought together some way and this introduces a limitation in the design of the boiler room. The gas air pre-heater is also subject to corrosion on the gas side, the same as a fuel economizer, and must take air at a temperature just as hot as the fuel economizer must take the water. Otherwise, the soot deposit at the cold end will make operation impracticable.

## Steam Air Pre-heaters using Exhaust Steam from Auxiliaries

Inasmuch as a gas air pre-heater should accept air at a temperature in excess of 150 deg. F. to avoid sweating, then the air must be pre-heated by means of steam in the same manner as the pre-heating of water to an economizer. In winter if this air is at 0 deg. F., there is 1.50 deg. which must be put into the air. It is therefore essential that some form of steam air pre-heater be provided and this device can be made very simple, compact, and relatively inexpensive because the problems met with are comparatively easy. In the first place the resistance to the flow of heat on the steam side is very low, the steam being the best conductor in transmitting heat from it to a surface. On the air side there is no soot or dirt problem aside from the ordinary dust and impurities in the atmosphere which should go right on through the ordinary steam air pre-heater. Inasmuch as the air is being heated and not cooled, there is no dew point to be considered and therefore no tendency for the dirt entrained with the air to become moist and adhere to the heating surfaces.

These desimable comditions permit the use of fimed tubes similar to those used for generator air conlers.

In a plant using steam-driten auxiliaries and where the heat hatance is imperfect as is the case in most plants, any execes steam may be readity abserthed whout complication to operation by introducing steam air preheaters.

## Steam Air Pre-heaters using Extraction Steam

As the tide is rapidly changing from separatelydriven steam axiliaries to motor-driven ausiliaries and the heating of the feed water accomplished he extraction steam, so the heating of the combustion air should be accomplished by extraction steam. Furthermore, the air can best be heated in stages in a manner similar to the heating of the feed water. This stage heating would be counterflow and the low temperature of the air usuatly dealt with permits using steam from the latter stages of the turbine where the gross water rate would be lowest.

If steam is extracted from a turbine for heating the feed water to the maximum temperature practical and also for heating the air to the maximum temperature practicable, then the flow of steam to the condenser is reduced to a minimum and the same turbine should show a greater improvement for a high vacuum condition than if operating straight condensing. Atso the same condenser should show a better vacuum with the same water temperature because of the reduced steam flow or a smaller condenser may be used to accomplish the same result.

## Physical Consideration of Surface Heaters

In the past it was found to be cumbersome to heat the air because of the large amount of heating surface required. With the finned
 space oreupied is rery small suls hatome can be installed in exist ing air duch in many plants because the fromtal area of a heatein need be expmatent to at duet area having: at maximum air velocity of 1006 of a minute If the duct area is such that the maximman air
 uponly to double the area. The depeth of the heater may be from 1in to e. inches, depending on the amount of surface required.

The heating sections connected wa stage on the main turbine which operates at a pressure below atmosphere can be drained by means of racuum traps and a vacuum pump, in a manner simitar to any vacum heating system in a buidding. This equipment is relatively inexpensive and simple to operate. The section using steam from a turbine stage at a pressure above atmosphere can be dripped back through traps to any receiving tank.

The installation of a surface air heater does not alter the design of the plant to any extent. It does not determine how the gases shall be taken away from the boilers, nor whether economizers should or should not be installed.

## Operation of Steam Air Heaters

The steam air heaters can be paralleled with the water heater. The temperature of the air learing the heaters will float with the temperature corresponding to the pressure in the particular stage of the turbine at any load. No regulation is necessary. If the steam is shut off from a heater section the air goes to the boiler cold, no harm resulting. If the air is shut off from a heater section the steam will not condense and there will be no flow from the main turbine. Thus, it will be seen that the regulation is inherently automatic.

# The Development of Current Limiting Reactors and Their Shunting Resistors 

By F. II. Kiersteab




#### Abstract

The wisdom of using current-litniting reactors seems to be well recognized. The athor lays much emphasis on the value of shunted resistance as a means of dampening out disturbances. This contribution has been written in the light of much experience and should give some of our operating friends useful data. EDtror.


In the early days of alternating-current generation and distribution, one of the diflicult problems for the designer of apparatus was to reduce the reactance to a minimum. This practice continued until the size of generators had so increased that the shortcircuit current of a generator, with the accompanying magnetic forces, was so great as to chistort the armature coils, resulting in a general failure of the generator. It was therefore necessary to add external reactance to the generator circuits, in the form of current limiting reactors, in order to limit the current during short circuits and thus prevent the self-destruction of generators. This was only a transition period, however, and for a number of years generators have been built with sufficient internal reactance to enable them to withstand short circuit without injury. This transitory use of reactors for the protection of generators was the forerunner of a permanent demand for current limiting reactors in bus and feeder circuits.

As the use of electricity grew, more generators were connected to the same busbar and consequently the energy that flowed into a short circuit on the busbars or connected feeders was enormous. As a resutt, great injury was done to the circuits by the large magnetic forces, and the very rapid rise in temperature. Furthermore, the duty required of the circuit breakers in interrupting the current was beyond their capacity. It therefore has become necessary, in large systems, to separate the busbars into two or more sections connected together through reactors, in order to limit the flow of current to a value that the circuit can safely stand and the switches will interrupt. This practice of sectionalizing busbars with reactors is a permanent one which, it is believed, will grow in proportion to the growth in capacity of generating stations. The basis for this expected growth lies in the fact that it is not
economical to increase the reactance of each generator connected to the busbars sufficiently to protect the bus circuit and switches.

Bus reactors give sufficient protection to small stations, but they by no means solve the problem of short circuits in big systems where the kv-a. capacity per section is large. This problem is three-fold. First, a short cireuit on a feeder connected to a system protected with bus reactors alone results in very high temperature rises and great magnetic forces. Second, very expensive feeder switches are required to open the circuit. Third, the bus section voltage drops to zero, and the generators fall out of step. The complete solution of the problem therefore requires the use of reactors in the feeders which, in the case of a short circuit on a feeder, reduce the current that flows and enable the bus section voltage to be maintained at a high percentage of normal value. The dangers due to high temperatures and great forces are thus eliminated, less expensive switches are required, and the generators remain in step.

In large cities where two or more generating stations are tied together by lines operating at the generated voltage, it is necessary to insert reactors in the connecting lines which perform the same function as bus reactors. Of course in those cases in which the stations are tied together by lines operating at different voltages from the generated voltage, the transformers insert sufficient reactance for safe operation and reactors are not required.

The first reactors were used in 1911 as generator reactors, and then to a large extent in the nature of an experiment, but today they are as much a part of a modern station equipment as the switches themselves. Fig. 1 shows a typical outdoor instatlation.

In past years when the systems were small the capacity of a station was doubled without consideration of its effect upon the short-
circuit current, but now no operator will increase his capacity e. per cont without a careful consideration of its offect upon the operation of the station under short-cireuit conditions. Tolay the control of short-circuit currents by current limiting reactors is a fundamental consideration in the equipment of a power station
short circuits was easily calculated, but the real problem to determine was how high transient voltages might rise. There weregroot reasons to believe that they might be very high, and rery high factors of safety were used in the insulation of reactors. In spite of this, some reactors in large stations failed in operation in a manner which seemed to


Fig. 1. A Typical Outdoor Installation of Reactors

The long experience in the manufacture and operation of reactors has cleared away the difficulties in their design. In the early days the designer did not know the magnitude of the magnetic forces within a reactor, and had only a hazy idea of their direction. Now their magnitude and direction are accurately calculated. Eddy losses also caused the designer considerable concern in those early days, for the reason that reactors were then built in which the total losses were three times the $I^{2} R$ loss. In modern reactors the total losses are very little more than the $I^{2} R$ loss. The next really serious problem that the designer had to solve was the magnitude of voltage across the reactor and the distribution of this roltage between its turns and lavers. The voltage across the reactor under simple
indicate that the voltage stresses on the reactor were higher than had been anticipated.

About this time, the General Electric Company put into operation at the Schenectady Works a large generator of approximately $27.000 \mathrm{kr}-\mathrm{a}$. continuous capacity and capable of developing nearly $300,000 \mathrm{kv}-\mathrm{a}$. instantaneously. With this generator we made short circuit tests on reactors which proved beyond doubt that most of the failures, which we had heretofore attributed to high voltages, had been due to high magnetic forces. This proved to be a great advance in the art, as it cleared away the apprehension of high voltages and gave very definite data on the magnitude of the short-circuit forces. We are now able to
calculate acemately the magnetic fore on the weakest pertion of the conductor and to determine the strength of that portion of the conductor so that we know the factor of salety we are using.

The past twelve years of experience in the design of reactors has led to the belief that aside from the case of a direct lightning stroke, voltages on a system seldom reach a value capable of causing a flashover of our reactors.

Operators have frequently been apprehensive that a short circuit on their system will be maintained for a long enough time to raise the temperature of the reactor so high that it will either fail at that time or will be so badly damaged that it will fail during the next short circuit. This very point was the determining influence in the adoption of the present fireproof reactor. Large currents have been hold in these concrete reactors until the conductor melted and it was found that the reactor continued to operate up to the melting point of the conductor which leads to the conclusion that these reactors will operate satisfactorily during short-circuit periods up to the melting point of the conductor. On the other hand, the General Electric Company's fixed policy of conservatism has been maintained and reactors are guaranteed for temperatures at short circuit up to 350 deg. C. only. In all the years of manufacture of these reactors no failures due to overheating, caused by long continued short-circuit currents, have ever been brought to notice, and this experience indicates that the apprehension of operators on this score is not justified. On the other hand, up to a certain limit the net cost of a reactor with a large conductor is not so much more than one of small conductor, for the reason that the saving in the operation cost due to the reduced losses partially compensates for the increased cost of investment. For instance, if for an increased price which would entail an increased investment cost (including depreciation) of $\$ .50 .00$, a saving in operation cost due to the reduced losses of $\$ .50 .00$ is made, it would, by all means, be the better policy to buy the higher priced reactors, and gain the additional advantage of reduced temperature rise under short circuit.

Almost from the start of the electrical industry, engineers have recognized the important part that the resistance of a circuit plays in the limitation and reduction of transient voltages. The word resistance is used here broadly to include both the series
resistance and shunting resistance of a circuit. Every transiont is damped out solely by the energy absorbed due to the resistance of the eirenit. If a circuit could be made without resistance, over-voltages would not be transitory, but would be permanent. The great advantage in having over-voltages die out rapidly is, of course, apparent and the first thought from the standpoint of protection is to increase the energy absorbed in the circuit so as to


Fig. 2. Current-limiting Reastor with Shunt Resistor Placed Side by Side
increase the rapidity with which over-voltages die away. On the other hand the efficient use of electricity requires the reduction of losses to a minimum. The problem, therefore, is to find a means of absorbing the destructive energy due to a disturbance without absorbing the useful energy that is being generated. A resistor shunting a reactor has this property. During the normal operation of the system, the voltage across the reactor and therefore across the resistor (since it shunts the reactor) is only a few per cent of the circuit voltage; and the energy absorbed by the resistor, which varies directly as the square of the voltage, is small. On the other hand, high-voltage disturbances generally occur at high frequencies and, because the frequency is high, the voltage built up across the reactor, and therefore across the resistor, is high. The energy thus absorbed, which is destructive in its nature, is large. Thus we see that resistors which shunt reactors are
selective in their operation, absorbing large quantities of dangerons energy and very little useful energy. The General Electric Company were carly to realize the great protection from high voltages afforded by resistors shunting reactors and purchased the Campos Patents which cover the use of resistors shunting reactors for this purpose. Figs. 2 and 3 illustrate the standard construction of this type.


Fig. 3. Current-limiting Reactor with Shunt Resistor Assembled in the Proper Position
In modern power stations in which all the feeders which radiate from the busbars are equipped with current limiting reactors any steep wave front disturbance which originates in the station due to switching, etc., is trapped in the station by the reactors and therefore expends its energy in raising the busbar voltage instead of dissipating itself into the feeders which it would do if it were not for the feeder reactors. On the other hand any steep wave front disturbance coming in towards the station from one of the feeders, strikes the reactor and is reflected into the line where it dissipates itself.

If then each reactor is shunted by a resistor of high resistance compared with the surge impedance of the feeder, a steep wave front disturbance coming in from the feeder will still be largely reflected into the line and that which passes through will be largely absorbed by the resistor, while a disturbance originating inside the station will find a comparatively free passage, through the many resistors shunting the reactors, out into the feeders where it is dissipated.

In every pewer station thare are combinationsof inductance and capacity in series which may cause an increase in voltage due to restonance if comparatively low voltages having the proper freguency are impressed across them. There are also points in these stations corresponding to each of these combinations of capacity and inductance at which, if a short circuit or a switching operation occurs, oscillations will result at a frequency which will resenate with its corresponding combinations. While such potential dangers of high resonant voltages exist, the circuits of a modern system are so complex, that such resonating combinations are not recognized and camot be eliminated. Such rises in voltage, however, will not be high if the damping is great, that is, if the energy absorption is great. The most effective manner of increasing the damping of these oscillations without increasing the losses, under normal conditions, is to shunt each reactor in the station with a resistor.

Summarizing, it has been shown that resistors which shunt reactors protect a system in two ways. First, by their unidirectional action of by-passing disturbances originating inside the station, but reflecting disturbances coming in towards the station, from a line. Second, by absorbing highfrequency energy and thus increasing the rate of damping-out of such disturbances.

In an article published in the July, 1921, issue of the General Electric Review, by Messrs. G. Faccioli and H. G. Brinton, the authors have reviewed the action of the reactor shunted by a resistor and have shown the properties of such an energy absorber for minimizing the danger of high-frequenc: oscillations.

In the 1921 report of the Electrical Apparatus Committee of the National Electric Light Association, Dr. Charles P. Steinmetz and Messrs. G. Faccioli and F. W. Peek have very clearly stated why resistors shunting reactors are desirable.

The European practice has been for some time to shunt reactors with resistors. Professor $\mathbb{W}$. Peterson of Darmstadt, the well known inventor of the Peterson grounding choke coil, has written a paper for the Elektrotechnische Zeitschrift, published February 20,1913 , in which he very strongly advises the shunting of all reactors with resistors.

It has been very difficult to obtain actual tests on a system with and without the reactors shunted by resistors under conditions such that high voltage should appear, due to
the matmaral mathingomess of mathaters of Whotric spsoms 10 subject heir plants to the hatards of a homedklown maring the tests. Such tests, howeror, haw been recently mathe an ome vory large system. Fig. it shows the diagrath of eomincetions. '1he fests comsisted of switehing the primary of the tramsformer on and off the hashars of the gemerating station with the seemelary open circuited

${ }^{\text {' Fig. 4. Diagram of Connections Used in Switching Test. }}$ Trans.ormers Switched Out of the Circuit

It will be noted that reactors are locat between the primary of the transformer and the circuit breakers comecting the transformer to the busbars. These switching tests were made with and without the reactors shunted by resistors. Measurements by means of sphere gaps were made of the voltages between the lines connecting the transformer to the reactors and also from these lines to ground.

The sphere gaps used were limited in range to the measurement of a maximum of $33_{4}$ times normal voltage. With the sphere set for this voltage arcing of spheres occurred, indicating that the transient voltages were of higher value than the voltage for which the spheres were set. Out of a large number of switching operations the number of spleregap arc-overs as a percentage of the total possible number of are-overs has been determined for different setting of the spheres. This percentage of arc-overs has been plotted in Fig. 5 , against the number of times normal voltage for which the spheres were set. The extrap-

[^52]wated portion of the carre which is dotted indicates that no aro-over woukd ocour at a setting of the sphare gaps for 3 ? $)$ times normal volage. With the resistor shanting the reactor similar ratlings were taken. In this case, the time allotted for making the test had expired before a determination had been made of the minimum distance apart, at which 110 sparking would take place, and therefore, these readings are ploted in the same manner as the first reathing. The expropolated portion of the curve indicates that no are-over would occur at a setting of the sphere gaps for 2.f times normal voltage. This shows that shunting the reactors with resistors lowered the voltage that the transformer had to withstand to less than 70 per cent of the value without the resistor.


Fig. 5. Voltages Measured When Switcining a Transiormer Out of the Circuit

A large number of laboratory tests have been made in which operating conditions were duplicated as nearly as possible to determine the effectiveness of resistors shunting reactors in preventing high voltage from being built up, due to resonance.* In these tests voltages as high as ten times the generated voltage were built up between a line and ground due to resonance, but when the resistor was shunted across the reactor, this was reduced to less than double that of the generated voltage.

# Edison Mazda Lamps in Lighthouse Service 

By L. C. Porter

Commerchal. Engineerin, Debartment, Emison Lamp Works, Gentrai. Elecaric Chmpany
There are no lights in all the world of more importance than those in our lighthoust s. Failure not possibly but probably means death to many. The author tells how electric lights are now replacing older forms in our lighthouses. The successes of the tests already made are best told by the fact that clectric ontfits for twelve of the principal districts have been ordered.- Enoltor.

At present, the majority of illuminants used as aids to narigation, be the United States Lighthouse Service are oil wick lamps. In addition to these, there are a number of incandescent oil vapor lamps, and some oil gas lamps using mantles. Acetylene gas is the illuminant used in the next largest quantity, then come incandescent electric lamps, and electric arc lamps.


Fig. 1. Cil Post Lantern used in Lighthouse Service
There are several reasons why electric lamps have not come into general use for this class of service. Most of the lights are located along the coast, rivers and lakes, at"points where electric current is not available. Absolute reliability is a factor of prime importance in lighthouse service, and the tendency of electric power lines and lamps to fail occasionally has been a serious detriment to their use in this class of work. The relatively high cost of power from batteries, and lack of suitable low-voltage electric flashing mechanisms have also retarded the use of electric lamps in lighthouse service.

[^53]During the past few years, however, conditions have been changing rapidly. Great advances have been made in the reliability and efficiency of electric lamps. The rapid increase in labor costs have made the use of oil lamps, which require frequent cleaning, trimming and filling, very expensive. The


Fig. 2. Vertical Distribution Curves of Light from an Cil Post Lantern, with $200-\mathrm{mm}$. Pressed Lens, taken 90 deg . apart-narrow and broad sile o? flame. (A) Efgewise. (B) Flatwise. High flame used, perhaps higher than would te possible in practical use
acetylene lamps are operater from large, heary tanks of compressed gas. Large boats and several men are needed to remove these tanks and ship them back to the factory for refilling.

In a number of cases these difficulties have been overcome by the use of electric lamps which have been applicd very successfully to some of the larger lights located where electric power of commercial lighting voltages is available.*
'The solntion of the small light problem, howiver, has mot heen so easy, and no small amomut of researeh has been expended on it. In determining what was neecsabry in the way of an ineandeseent lamp to replace the ai and atedyleme harners, photometric tests were comblacted on topical umits. Vertical dist ribution curves were made (111 a 10ew oil post kantern with a 200 mm . lens. This lamp is ilhustrated in Fig. 1.


Fig. 3. One-half Foot Acetylene Burner and $200-\mathrm{mm}$. Lens for Lighthouse Service

The curves are shown in Fig. 2., where A represents the edgewise and $B$ the flatwise distribution. These show a maximum beam candle-power of 32 on the axis, and a spread of about 20 deg.

Next, a typical 200 mm . lens equipped with a ${ }^{1}{ }_{2}$-ft. acetylene burner lantern was tested, see Fig. 3. In this case a horizontal curve was taken as well as the vertical curve, see Figs. 4 and 5. These curves indicated a maximum beam candle-power on the axis of 56 , and a spread of about is deg.

As both of these equipments were new, and adjusted to get the maximum light from the source, it was felt that any incandescent lamp which would give equal beam candl-power would be more effective in service, as it is well known that the average candle-power of oil lamps, under service conditions, falls considerably below their intial rating.

Experience in replacing oil signals by electric signals in railroad service had also shown that the characteristic color and steadiness of the electric light is such as to make a more effective signal at an actually lower candle-power of light source than maintains with the oil flame. Distribution curves made with a 10 -volt, 0.5 -ampere,

Marda lamp, see Fige 6, with the $2000-\mathrm{mm}$. lens, showed a maximum candle-power on the axis of 40 , with a spread of about 4 deg., see Fig. 7. A study was made of the distances at which beams of different spread woukd strike the water from different mounting heights, see Fig. S. From these data it


Fig. 4. Horizontal Distribution Curve of Light from One-half Foot Acetylene Gas Lantern with $200-\mathrm{mm}$. Buoy Lens


Fig. 5. Vertical Distribution Curve of Light from One-half Foot Acetylene Gas Lantern with $200-\mathrm{mm}$. Buoy Lens. Flame perpendicular to screen
seems apparent that the spreat from an electric lamp will be ample to take care of the requirement. There is sufficiont stray light in the lens to give a good indication when a ship is close to the light, but below the main beam.


Fig. 6. Ten-volt, One-half-ampere Edison Mazda Lamp for Lighthouse Service

- While this work was under way, Mr. A. IV. Tupper of the Lighthouse Department at Washington, was busy designing and dereloping an electric flashing device. This little flasher is a rery ingenious device, having but two moring parts. It consumes


Fig. 7. Vertical Distribution Curves from Electric Lantern with 10 -volt, ${ }^{1}{ }_{2}$-amp. Mazda Lamp and $200-\mathrm{mm}$. Buoy Lens. Curves taken 90 deg. apart
only 24 watthours of energy per year, and can be set to give single, double, triple or quadruple groups of flashes at any desired rate between 20 and 60 per minute.

The adrantage of using a flasher is twofold. First, it reduces the battery energy consumption rery materially over that required for a steady burning light. Second,
the desired chamacteristics of omann thashing lights can be mamamed, and latily, a flashing light is more comspicuons matn a steadily buming light.


Fig. 8. Curves to determine:
(1) The distance from a light at which the bottoms of beams of various spreads and mounting heights will strike the water
(2) The height above the water of the top of the beams of various spreads and mounting heights at various distances from the light
(3) The distance from lights of various spreads and mounting heights at which the bridge of a ship passes out of the beam DIRECTIONS FOR USE
Case 1. To determine the distance from the light at which the bottom of beams of various spreads and mounting heights will strike the water.

Instance: 100 -ft. post and lantern having .5 dcg. beam spread.
Directions: Follow out on the horizontal line of $100-\mathrm{ft}$. height above the water until it intersects the diagonal o deg. line. From this point or intersection follow the vertical line down to the scale giving "Distance from Light." The intersection of the vertical line with this scale will give the distance in feet that the verticaline with this scale will give the distance in ineet thead and lower edge of the beam of light having a. ideg. bean spre
originating 100 ft . above the water will strike the water.
riginating 100 ft . above the water will strike the water.
Sote: For lantern mounted at heights other than 100 it and having beams of other than 5 deg. spread, substitute the required height and beam spread respectively in the above directions.

Case 2 . To determine the height of the top of the team above the water at various distances from the light and various mounting heights.

Instance: $3000-\mathrm{ft}$. distance, 3 deg. beams, $40-\mathrm{ft}$. mounting height.

Directions: From the scale at 3000 ft .follow a vertical line until it intersects the diagonal 3 deg. line. At this point of intersection follow the horizontal line to the right to the scale showing height above water and read the intersection in feet - -80 ft . The height of the mounting post or 40 ft . added to this amount80 ft .-will give the height of the top of the 3 deg. beam mounted on a $40-\mathrm{ft}$. post at a distance of 3000 ft . from the light which is 120 ft .

Note: For beams other than 3 deg. spread, distances other than 3000 ft . and mounting height other than 40 ft . substitute the required beam distance and mounting height in the above directions.

Case 3. To determine the distance from the light mounted on posts of various heights, at which a ship bridge of various heights will pass out of the beam.
4. Where the height of the bridge is greater than that of the post.
Instance: $50-\mathrm{ft}$ bridge, $20-\mathrm{ft}$. mounting post, 2 deg. beam.
Directions: Find the difference between the height of the bridge and mounting height $50-20=30 \mathrm{ft}$. Follow the $30-\mathrm{ft}$. line until it intersects the 2 deg, beam. Directly below this toint read the distance in feet-1700 ft. -at which the bridge will pass out of the beam.

Note: For other bridge height, mounting heights and beam spreads. substitute in the above directions.
$B$. Where the height of the bradge is less than the height of the mounting post.
Instance: - -ft . bridge and ho-ft. mounting post. Beam spread of 6 deg.
Directions: Find the difference bet ween the height of mounting post and height of bridge, $(1)-20=60 \mathrm{ft}$. Follow the $60-\mathrm{ft}$. Ine out until it intersects the diagonal fideg, lone. Read the distance directly beneath this point- 1120 ft . Which is the distance at which the bridge passes out of the beam.
Note: For other bridge height, mounting heights and bea spread substitute in the abose directions.

Incilentally, the use of this same litule thasher with primary hatteries makes practical eloctric highway orossing beacons throughont the country, in places where deotrie power semvere is mot avalable.

Whike this work was under way, the Edison Primary Battery Company was cooperating with the Lighthouse Department in the development of stitable batteries for operating the lamps and thashers, see Pig. 9. Tests were made to determine the effect of very low temperature on the voltage mantenance of the battery, to make sure that it would function properly in Alaska.

Tests were also conducted with a lamp and flasher to determine the effect on the voltage curve of intermittent hurning service. These tests showed that either the 500 - or $1000-$ ampere-hour cells will function satisfactorily even if exposed to zero temperature, using a $1 / 4$-ampere load. If, however, $1 / 2$ - or 1 -amperc lamps are to be used, some protection should be afforded the cells, such as placing them in a battery box buried in the ground.

The incandescent lamps used are designed to outlast the life of the battery with a factor of safety, and the practice is recommended of renewing the lamps at the time the battery is renewed. Incandescent lamps, however, are not absolutely infallible. Occasionally, a lamp will burn out before its allotted time. To guard against this contingency, Mr. Tupper designed a relay which, in case one lamp fails, will automatically light a second lamp in a lens placed just above the first one. In this manner practically infallible service is assured.

In order to secure further economy in battery energy, and to increase the length of renewal period, the American Gas Accumulator Company has developed an electric sun valve, see Fig. 10, similar to the one which has been in use for many vears on gas outfits. This device automatically opens the circuit and thus extinguishes the lamp with the approach of daylight, and lights it again on the approach of darkness.

One of the questions raised in connection with the substitution of electric for gas and oil lamps, was that of ice and sleet. It was felt that possibly the greater heat of the flame sources would keep the lens freer of ice than would the electric lamp at points just below freezing. This is probably true. However, tests were conducted on an electric outfit, 10 -volt, 12 -ampere lamp and 200 mm . Fresnel lens, free from ice, and then the same outfit covered with a $1 / 4-\mathrm{in}$. coating
of rongh ice. This was found to increase the spread of the beam slightly, and to reduce its maximum candle-power on the axis about jof per cent. The average candlepower throughout the beam, however, was reduced only $1+2$ per cent.

After all this preliminary research was completed, an actual installation was made


Fig. 9. Five-hundred Ampere-hour Edison Primary Battery
at the 3rd Lighthouse District at Tompkinsville, Staten Island, N. Y. An electric outfit using a 10 -volt, $1 / 2$-ampere Edison Mazda lamp was installed alongside a gas outfit having a $1 / 2-\mathrm{ft}$. acetylene burner and an oil post lantern. The electric outfit has been in successful operation now for nearly a year. Reports made by the Technical Assistant at the depot, on the effectiveness of this light, read in part as follows:
"In the evening the three lights were observed from the upper deck of the municipal ferry, from locations on the viaduct leading to the ferry station at St. George, from locations on the terrace, at the depot, and from various locations on the depot docks. The evening was rainy and the visibility below normal. On the trip from Manhattan to Staten Island the electric lantern was first observed when the ferry was about opposite Robbins Reef Light. The acetylene lantern was not seen for several minutes, or until in fact the ferry had almost reached the slip. As observed from the riaduct,
the electric lantern appeared more than twice as bright as the acetylene lantern， and from the terrace the ciectric lantern was still ummistakably brighter．From positions on the docks there was not much choice between the two lights，but whenever there was any difference，it was in favor of the light given by the electric lantern．


Fig．10．Electric Sun Valve of the American Gas Accumulator Company
＂On the following evening，July 19th，the writer observed the three lights from the upper deck of the Brooklyn ferry，and also from various elevations on the depot coal tower．In going across toward Brooklyn the acetylene light gradually disappeared from view，while the electric light was still plainly visible．On returning from Brooklyn，the electric light was picked up first，and by a comparison with the location of other lights on the shore，the writer is fairly certain that the electric lantern was observed as soon as it came within the range of vision from behind the cotton docks．The acetylene lantern was not observed until the ferry was more than half way across the Narrows． From all points when the two lights were visible，the electric lantern was much the brighter．On account of the post lantern being a fixed light，the writer was not able to distinguish it from the other shore lights． so that it was not possible to compare it
with the flashing lights at any distance． Observations made from the viaduct seem to indicate that the intensity of its light lay in between the other two．（in the occasion of this trip，observations wate also made with marine glasses，and it was foumd that in this case the advantage of the electric lantern was not nearly as marked，its short flash giving more difficulty when the glasses were used．It is also believed that the greater visibility of the electric lantern is not so much due to a greater candle－power，as the laboratory tests made by the Edison Lamp， Works indicated that it did not have a greater candle－power，but that this increased visibility is due to the fact that we have a smaller source of higher intrinsic brilliancy． The observations made from the coal tower indicated that at that short distance，when appreciably below the level of the lantern， both lights were about equal；when viewerl approximately on the level of the two lanterns the advantage was decidedty in favor of the electric lantern．When viewed from eleva－ tions considerably above the lanterns，the acetylene lantern was the brighter．
＂On the evenings of July 20th，21st，and 24 th the writer made further observations of these lanterns from the deck of the munici－ pal ferries．On one occasion when visibility was good，the electric lantern was first picked up while the ferry was about opposite the Statue of Liberty，whereas the acetylene lantern could not be observed until the ferry was nearly opposite Robbins Reef Light． On another occasion of lower visibility the electric lantern was first picked up when the ferry was eleven minutes from the Manhattan shore，whereas the acetylene lantern was not discerned until six minutes later．The total trip occupied about twenty－two minutes． Observations were also made on trips when the ferry was bound toward Manhattan．In these cases the acetylene lantern was always lost from view long before the electric lantern．＂

Electric installations have been ordered for each of the 12 principal districts．These， undoubtedly：will be followed by many more， thus establishing the entrance of the Mazda lamp into another field－that of guarding human life and property on the water．

The advantages of the electric outfit are marked．Greater reliability is assured．It not infrequently happens that other illumi－ nants，particularly those on buoys，are extin－ guished by being pushed down under the water either by boats or ice．The electric lamp will not be extinguished by such submersion．

The ele et rie ond lit does mot need to be visited exery fow days be a temder It will operate abont a year withat attention, thas bringing about a lage reduction in operating cost. The sil hamps cost about sis.on per month, per light, for maintenanee labor, in addition to burning one guart of oil a day, costing
 selected, high yrark kerosene oil is used), as well as the expense of chimners, burners, cte.

The acetylene lamps refuire a large lightbouse tender and erew costing about sisot.00 a daty to hardle the rencwals of the heary gas tanks, whereas the simple battery ad lamp renewals ean be handled by one or two men in a motor boat at a cost of about sa30.00 per day. The electric outfit will cost about $\$ 18.00$ per year for batteries, and about $\$ 1.00$ for lamps.

In addition 10 this saving and greater reliability, a more effective light is obtained.

# Cargo Winches for Merchant Ships 

By C. H. Giroux<br>Electrical Engineer, U. S. Engineer Dept., Washington, D. C.

This comprehensive article on cargo winches for merchant ships deals with all the important considerations which enter into an intelligent selection of equipment.-Editor.

When selecting equipment for a merchant vessel, the first consideration is always the class of service for which the ship is fitted. Although not always recognized, this applies fully as much to the deck winches as to any other machinery.

On a passenger ship the winches are used only for putting supplies aboard, or for handling baggage, and then for comparatively short periods of time. Obviously duty of this character does not demand a winch of the same capability as one used for loading and unloading a freight vessel. On the other hand, noise may be a very vital factor on the passenger vessel, and of little consideration on the freighter.

There are similar conditions which must be observed when supplying equipment for tankers, barges, yachts and other types of vessels.

Considerations too numerous to mention all have a bearing on this subject, but the most important may be cited as the trade in which a vessel is employed, the methods used in the different world ports, the facilities for delivering and disposing of cargo and possibly the most important of all is the character of the commodities carried.

It would not be wise to fit a ship with deck machinery suitable for a certain trade, if at a later date it would be called upon to run in another trade, such that this machinery would be inadequate. It is seldom known at the outset in what trade a cargo vessel will be
called upon to operate during its life, and it is therefore usually necessary to fit it with machinery which will meet the most severe requirement for a ship of its class. Occasionally we find ships designed for a special purpose, such as refrigerating ships, and here we may take full advantage of the peculiarities of this service when selecting the equipment.

The financial success of a freight vessel depends to a considerable extent upon the rapidity with which the cargo is loaded or discharged. The application of proper winches to ships of this class handling general cargo in all ports of the world, is, therefore, a very important matter and worthy of considerable study by both the manufacturer of the winches and by the shipbuilder.

The remainder of this article will be confined to this application, assuming that if the same principles are followed, there will be little likelihood that inadequate equipment will be supplied where the duty is comparatively light and much easier to determine.

There are many factors affecting the duty imposed upon a general cargo winch, of which the following are the most important:

1. Design of vessel
2. Kind and weight of cargo
3. Number of stevedores working
4. Facilities for disposing of cargo
5. System of handling
6. W$e a t h e r ~ c o n d i t i o n s . ~$

The features in the design of the ressel which influence the operation of the cargo winch are briefly-depth of holds, heighth above the water line, distance from center line to side of ship, size of hatehes, arrangement of booms and winches.

The first three dimensions determine the time during which the load is hoisted, lowered, and transferred to or from the wharf. Assuming that the time for hooking, whooking and preparing loads is fairly constant for a given cargo, the duty on the winch is directly proportional to the distance traversed between the wharf and ship's hold.

The size of the hatches has a decided effect on the dispatch with which certain kinds of cargo can be handled. For example, it is very difficult to load lumber into a ship having small hatches, considerable time being consumed in getting the load into position for lowering. On some ships very large hatches are provided, so that two pairs of winches for each can be used, one pair discharging to the wharf, and the other to lighters.

The arrangement of winches and booms should always be so that the lines will spool properly on the drums, and that the lines will not be in the stevedores' way, else considerable time may be wasted.

When the weight, dimensions and character of the loads handled are uniform, the duty cycle to be performed by the winches can be quite accurately determined, and a design made which will do the required work in the least possible time and with the greatest efficiency: However, the cargo winches on a general cargo vessel may be called upon to handle any one of over twenty-five hundred commodities put up in various ways. This means that such a winch should be so designed that it will attain its greatest efficiency when handling the average cargo, but it must also have capacity and speed control for successfully manipulating loads of minimum and maximum bulk and weight.

This would appear to be an almost impossible task when considering, for the first time, the enormous variety of commodities. However, the mere fact that these articles have to be shipped and handled at a reasonable cost has compelled the manufacturers to send out their products in more or less uniform packages. These packages are usually grouped in slings, etc., so that the average winch load is between 1500 and 2000 lb . Less than two per cent of the commodities, when packed for shipment by water, weigh 6000 lb . or over. These heavier loads are usually grouped in
one hatch so that it is not a difficult matter to rig additional falls for handling them. The consequent low speed is not a serious handicap because these loads are such a small percentage of the total cargo and also because these heavy packages are handled slowly and carefully by the stevedores.

From the above, it would appear that a winch having a maximum capacity of 6000011 , or over, and capable of reaching its maximum cargo handling efficiency at approximately 2000 ll ., fully meets the load requirements for general cargo work.

Assuming that the winches are able to transfer cargo somewhat faster than the stevedores can prepare the loads and stow them on the wharf, or in the ship's hold, the tomage attained will vary directly with the number of gangs employed in this work. There is, however, a limit to the number of men which can work without interference with each other.

The usual practice is to station four gangs, one at each comer of the hatch, and to distribute the loads to them in rotation. This arrangement may be varied according to the size of the hatches, kind of cargo, etc. The winch must, however, be capable of keeping ahead of the maximum number of stevedores which may be used.

The facilities for preparing hook loads, or for disposing of cargo on the wharf is a very important factor, affecting the tonnage handled, and consequently the dut $y$ imposed on the winch. Here again we must assume the most favorable conditions, so that the winch will not be blamed for delay. We can allow only a reasonable length of time for hooking, or unhooking the load and assume that the hook will be in motion the remainder of the time.

The system employed in handling a load, especially the method of transferring it between the center of the ship's hatch and the wharf, influences the duty imposed on the winch. The greatest tonnage rate can be obtained by selecting the method most suitable to the cargo. With some methods, one winch does considerably more of the work than its mate, and must not fail under this unequal distribution of labor.

Because of the fact that certain laborious duties in the handling of cargo must be done manually, the weather conditions have a decided effect on tonnage rates. It is reasonable that a man will do considerably more work in a moderate temperature than when it is either extremely hot or cold. The statement is often made that electrical winches on ships running into tropical ports must have motors of extra
capacity because of the high intital temperature Beratuse of the shower working of the (argo be the steredores, it maty be well assumbed that if the winch hats tomage eapacits to meet all other reguiments, it will perform sucerssfully under tronsal conditions.

Most of the abose conditions have been established hy many years of experience in shipping and as long as existing methods are used, the ship's winches must meet these requirements.

The following chatacteristics have an inportant bearing on the ability of a winch to handle cargo under the conditions outlined above:

1. Reliability
2. Mechanical efficiency
3. Maximum load which the winch can hoist
4. Rope speed at average load and at no load
5. Thermal capacity.

Unless every part of the entire system of cargo handling machinery is thoroughly reliable, it has no place on a vessel of the kind we are discussing. A failure of one winch will usually mean that operations in one hold of the vessel cease, and a continued delay will mean that the vessel will have to stay in port an extra day or more. The value of a ship's time may be several thousand dollars a day, and the loss due to failure of the winches is out of all proportion to the cost of repairs or to the first cost of the apparatus.

The mechanical efficiency of the various parts of the winch affect the maximum load capacity, the rope speed, and if motor driven, the thermal capacity. The efficiency of the varions parts should therefore be made as high as possible consistent with reliability giving proper regard to weight, space and first cost.

When considered alone, it would seem that the maximum load capacity of a winch should be great enough to enable the winch to lift any piece of freight which it is likely to encounter. This would mean either that the motive power would have to be abnormallylarge, or that the rope speed would be abnormally slow. Both of these factors are of such great importance that the maximum load capacity is of secondary consideration. As explained above, a winch having a maximum
(apacity of (0000 ib or over should be satisfactory for general carge work. This does not mean that the winch shouk only have capacity for exerting this pull momentarily, but must be capable of handling these loads continumusly at a good tomage rate.

The question of rope speed for general cargo winches is of greatest importance, and is the subject of a great diversity of opinion. Theoretically the ropee speed should be just high enough so that the hook will always be


Fig. 1. S. S. Steel Ranger Receiving Barrels of Ammonium Chloride. Three barrels ( 810 lb .) per draft. Tonnage rate 24 tons per hour


Fig. 2. Theoretical Effect on Cycle shown in Fig. 1 of Increasing Rope Speed Hoisting to Correspond with that of Electric Winch Geared for 250 ft . per min. with 2000-1b. Load. Tonnage rate 26 tons per hour


Fig. 3. S. S. Steel Ranger Receiving Steel Plates from Lighter. Average tonnage rate 13.25 tons per hour
at the point of loading at the exact moment that the load is ready. In this way the maximum tonnage output would be obtained with maximum efficiency: Howerer, this ideal can not be attained in practice, and the rope speed must be chosen so that the load will never be waiting for the hook on account of the time consumed in completing the cycle.

This cycle always consists of four distinct elements: hoisting the load, lowering the load, hoisting the light hook, lowering the light hook. It is therefore evident that the rope speeds lowering loaded and light and the speed
hoisting the light hook are just as important as the speed of hoisting the lowd, although the latter is uswally the only one speedifed by the purchaser. This practice has arisen through the use of steam winches where these speeds only are limited by the safe engine speed With electrical winches, howerer, further attention should be paid to these speeds as they may vary great ly depending on the motor characteristies and method of control.

Observations taken on a large number of vessels loading and discharging in various


Fig. 4. Load-speed Curves of Electric Cargo Winch with $35-\mathrm{h} . \mathrm{p} .30-\mathrm{min}$. Series-wound Motor
ports indicate that a rope speed of 250 ft . per minute when hoisting the average load is sufficient. Little or no time can be saved by providing a higher speed than this, and the first cost of the apparatus and the power consumption increase rapidly with an increase of speed.

Fig. 1 illustrates a typical cycle of operation where the loading and unloading of the hook is done rery quickly. Here the rope speed in hoisting from the pier was necessarily slow on account of interference with the pier shed. The rope speeds used in the operation were not the maximum of which the winches were capable, and thus gearing for higher speeds would not increase the tomage rate.

Fig. 2 illustrates the theoretical effect of increasing the rope speed in hoisting, assuming that interference with the pier shed could be
aroded. The tomager rate wond then be increased it per cemt.

Fig. 3 is a good illustration of the winch performance when handling unwidly loads, The winch is idle a great perecontage of the time while drafts are leing prepared and stowed. The rope speed here is of litule comsequence, as one or two seconds reduction in rumning time would only mean a longer wait at the destination.

Fig. 4 shows calculated values of rope speeds, both hoisting and lowering, of a cargo winch equipped with a $3.5-\mathrm{h} . \mathrm{p}$ ). Series wound motor and well designed dynamic braking control.

The facility with which the operator can perform the rarious operations has some effect on the amount of cargo handled. A few seconds delay on each operation will amount to many hours during the loading or unloading of a ship. The winch builder who provides a control which is easy and simple to handle will get the good will of the stevedore and this may not only influence the tonnage rate, but also may have a far reaching effect on the use or abuse which the equipment will receive.

Experience has proved that the greatest rapidity with the Burtoning system can be obtained where one man operates both winches. This is because he can anticipate subsequent movements, and therefore can stop or start each winch at exactly the right moment.

In order to take advantage of this condition, controllers for cargo winches should be arranged so that one man can operate two winches with ease. This can best be accomplished by a design having horizontal levers, one for each hand. The upward direction should hoist, and the downward direction should lower the load.

With electric winches overload protection for the motors should be provided so that in case the controller handles are moved too rapidly, the equipment will not be injured. These protective devices should be arranged to reset automatically when the controller handle is moved to the off position. The overload setting should always be under the superrision of the ship's electrician and should be proof against tampering by unauthorized persons

With electric winches, the cargo landling capacity is limited by the ability of the motor to dissipate the heat generated in the windings bearings, etc. For instance, we may have 1 wo motors with exactly the same characteristics and geared for the same speed at

He same average load. One of these motors may be rated at 3.5 h.p. for 30 minutes and the other 3.5 h.j. for in mimutes. If we should operate these two motors on the same duty evele for an extended period of time, we might find that the 30 -minnte rated motor would never exeed a sale ultimate temperature, whike the 15 -minute rated motor would in time reach a temperature which would be injurious to the insulation.

Thus, it will be seen that the horse-power rating is not sufficient to determine whether


Fig. 5. Cargo Handling Capacity of Deck Winch Using $35-\mathrm{h} . \mathrm{p} .30-\mathrm{min}$. Series-wound Motor. Tonnage rates are maximum obtainable on continuousduty with 55 deg . C. rise on motor on following duty
Duty Cycle-Burtoning system used for unloading ship Curves are for inboard winch
Hoist from hold 40 ft
Transfer to dock 38 ft .
Lower to dock 30 ft .
Return light hook to bottom of hold
the motor will perform the required duty. The time rating must always be considered, or preferably, the characteristics of the motor should be analyzed with reference to the most severe duty cycle likely to be encountered in the handling of cargo. With steam winches, the thermal capacity does not enter; but with electric motors, it is important. A good rule to follow is to fix as the maximum load, that which the motor can hoist continuously for five minutes.

Referring again to Fig. 4 , we find that with the gearing selected, the motor will exert its normal horse power at 1000 lb ., but will be able to hoist sood lla, at its five-minute rating. The maximum capacity of this winch should, therefore, be limited to so(0) 1b.

The gearing which is selected for an electric winch has a decided effect on the thermal capacity as may be seen from Fig. ©.

Curve " $\Lambda$ " is the load-speed curve of a winch geared to handle $2000-\mathrm{Hb}$. loads at a speed of 2.50 ft . per minute, and curve " $B$ " is the corresponding tonnage rate curve when performing a definite duty cycle. The rates given are the maximum which can be obtained on this cycle of operations without exceeding the allowable temperature rise on the motor.

It will be noted that the maximum tonnage rate on curve " $B$ " occurs at 4000 lb ., which means that the winch is operating at its maximum overall efficiency at this load.

By changing the gear ratio so that the rope speed at 2000 lb . is 18.5 ft . per minute as shown on curve "C," we get tonnage rates as shown on curve "D." Here the maximum rate occurs at 6500 lb .

This shows that a decrease in rope speed has the effect of increasing the tonnage rates at heavy loads, but decreases them on light loads.

Inasmuch as we are most interested in average loads of about 2000 lb . for general cargo work, it would at first appear that we should select a gear ratio which would give the maximum rate at this load. However, a further increase in rope speeds beyond those shown in curve "A" results in rest periods with light loads, which are too short for hooking and unhooking most kinds of cargo. The result is that the winch remains idle for longer periods and consequently the tonnage is not materially increased.

The above results show the desirability of selecting a gear ratio which will give the highest tonnage rate with the least expenditure of energy and the consequent minimum size of electrical equipment. This can be done only by carefully comparing the duty to be performed with the motor characteristics.

# Studies in the Projection of Light 

PART V

METHODS OF COMPUTING FLOODLIGHTING

By l₹ra̦k Besford




#### Abstract

The problem of floodighting a buikimg or other object is be no means as simple as it might appear. The number of flondights necesary, ther locations, intensities and direction of leams are collectively dequendent on the size of the objeci, its enlor, perspective, and the distance bet ween cach foodlight and the surface it illuminater and the angle with whicheach beam meets the surface. All those factors must le properly correlated to secure satisfactry results. The flux and the single-unt methows of computation are first explained in the following artiele and their shoricoming, pointed out. An improved method, that employing spherical irojection, is then cescrited and applied to the solution of two typical problems. - Editor.


## Nature of Floodlighting Problem

The gains in lamp efficiencr during recent years have made it practical to illuminate large areas of wall or ground by beams of light profected for considerable distances There is a strons tendencr toward larger and larger units: and while the general efficiency is thus raised, and the possible applications much extended. the large size of the indiridual floodlight sometimes increases the difficulty of obtaining the proper distribution of light. Ii often happens that due to limited current capacity, or more often to limited funds. the strictest economy of projection is desired. and a close examination of engineering details is necessary. In making this examination certain problems in solid geometry arise, and the ordinary methods of perspective drawing do not always yield simple and accurate data. In many cases plain perspective becomes hopelessly involved. and the spec:al type of perspective drawing which will shonly be described is intended to simplify and shorten the design work so that a promps solution can be made of eren the more dificuit cases.

Floodighting might be divided into three classes:
(1) Spectacular illumination for expositions. faiss, and conrentions, where the competition from street lights and sims may make it necessary to have high average illumination in order to secure effectiveness.
12 Sisn lighting, which is oiten simplified by dack suroundings.
3 Sinctiy utilitarian floodighting. such as Oluminating a factory fence line of the deck of a ship during loading of wnioading
Not only does each type of floodlighting require different treatment. but each indiridual case is apt to have certain peculiar
features that require special attention. Note is made of these distinctions because the name "floodlighting" suggests a large quantity of light that simply floods the jiluminated object more or less regardless of size. distance, or the angle of view.

A number of years ago, when preliminary work was being done for an international exposition. a building facade some 140 ft long by 60 ft . high was illuminated by a small group of lighting units placed about il ft from the building. To an observer standing near the source of light the illumination appeared to be of high uniformity: but an exploration over the face of the building with a photometer showed variations in illumination of ten to one. But if the observer went several hundred feet from the building the variations not only became risible but actually objectionable. The difference here was entirely in the eve of the observer. In the first case he could not see the entire facade in a single slance. and in the brief part of a second necessary to look from one comer to another. the impression of brightness would fade. and, to the casual observer certainly the illumination would seem uniform. At a greater distance the entire facade could be included in a single glance and the high and low areas of iltumination became distinct. Thus in this particular case the point of view the observer becomes of the utmost improtance. for in spectacular lighting things are what they seem. and if the eve is satisfied then computations are vain and phometry is an idie thing.

In the present instaiment atiention will be confined to incandescent hoodlichts with plain glass dorss. Thewe are various lens doors made ior dicuersint the beam in one or more directions and by the use of these doors the beam may be made to assume
different cross sections. Are lights have also seen wide and sucorssful use als foodlights for facalde illumination, and when equipped with diverging door strips the resultant beam is ideal in mane respects. Discussion of these optical devices will be reserved until more attention cat be giver to several interesting optical eharacterist ies of the dispersed beam.

## The Flux Method of Computing Floodlighting

The simpler cases of floodlighting may be solved by mental arithmetic. Thas if an arear of 1000 sq . ft . is to be illmminated to 6 ft -cl., three floorlights giving 2000 lumens each will be sufficient. This elemental way of arriving at results is certainly rapid enough, but there are often unsuspected elements of danger in it. Plans so made will be successful:
(a) If the beams of light can be so overlapped that no dark spots will remain,
(b) If the beams can be distributed so that the near and far sections are of equal apparent brightness, and
(c) If the beams can be arranged so that the light will not be unduly wasted around the edges of the surface.
Items (a) and (b) will be recognized as opposing characteristics, for if the beams are placed close enough together to secure continuous illumination there may not be enough beams to cover the entire surface; and if the distribution can be made to satisfy both (a) and (b) then the loss around the edges of the illuminated area may be so great as to lower the average illumination below the desired level. There are a variety of floodlighting units of various beam diameters and volumes of light that are available and intelligent choice of both number and types of units usually requires more data than are given by the method just outlined.

## Method of Computing Floodlighting by Single Units

When only a few beams are to be used it is often best to investigate the individual action of each beam, finding what area is covered and how the illumination varies from point to point in the beam. Perhaps the most common case that arises is the attempt to illuminate a large poster board with a single floodlight placed rather close to one end. This is a type of installation that is not to be recommended, but it frequently cannot be aroided, and to make the best of cireumstances the field of illumination should be at least outlined if not fully explored.

The following symbols are used in the ecpuations for the area illuminated by a single thoorlight:
$2 b=$ total angular width of beam
$a=$ angle at which axis of beam strikes surface
$D=$ distance between the point where the axis strikes the surface and the foot of the normal
$L=$ length of illuminated area
$11^{\prime}=$ width of illuminated area
$P=$ perpendicular distance to illuminated surface
$H=$ length of axis of beam (mirror to surface)
$c=$ the ellipticity of the illuminated area
The angular width of the beam, $2 b$, the perpendicular distance $P$, and the angle of inclination are ordinarily known, and the others can readily be derived by the aid of the following equations:

$$
\begin{align*}
& H=P \sec a \\
& D=P \tan a  \tag{88}\\
& L=P[\tan (a+b)-\tan (a-b)] \tag{89}
\end{align*}
$$

The ellipticity of the illuminated area is

$$
\begin{equation*}
e=\frac{\sin a}{\cos b} \tag{90}
\end{equation*}
$$

If the entire beam is received on the surface then $e$ is less than unity and the area is elliptical in form. If the beam is projected almost in line with the surface so that the outer ray is parallel to the plane of the surface, then $a+b=90$ deg. and $e=1$, that is, the illuminated area is a parabola stretching to infinity, but the usefully illuminated area is concentrated near the vertex of the parabola, and the farther sections of the parabola are without engineering significance.

When the outer ray diverges out from the plane of the surface then the illuminated area is a hyperbola and the useful light may fall to a low percentage of the total projected light. It is seldom that we deal with any except the elliptical area.

The width of the ellipse is

$$
\begin{equation*}
W=L \sqrt{1-e^{2}} \tag{91}
\end{equation*}
$$

and the area is

$$
\begin{equation*}
A=\frac{\pi}{4} W L \tag{92}
\end{equation*}
$$

Even when the entire beam is incident upon the surface, the area covered cannot always be considered as illuminated on account of the large variation between the intensity at different points. As an example, in Fig. 40 is given the illuminations at the ends of the elliptical areas illuminated by the same floodlight at various angles. The
illumination at the point where the axis of the beam strikes the surface is taken as 100 per cent in eacla case. When the beam is incident at near the normal the illumination curve resembles the beam-candle curve, that is, the illumination falls off to 10 per cent at the point where the edge rays of 10 per cent the central intensity strike. At high angles of incidence the near ends of the


Fig. 40. Diagram Showing the Size and Shape of the Spot of Light Projected on a Surface from Various Angles by a Conical Beam 11 Deg. Wide
ellipse is much brighter than the far ends, and the brightest part of the illuminated area is near the point where the axis strikes, but slightly closer to the near end of the ellipse. Taking the typical case of a beam 11 deg. wide incident at an angle of 60 deg., the near end of the ellipse has a brightness of 15.7 per cent of the axial intensity while the far end has an intensity of only 6.1 per cent. These variations have the effect of making the effectively illuminated area come slightly back from the computed outline, and therefore in applying a beam to some particular area it is best to overshoot slightly.

This particular floodlight gives almost the best uniformity of any on account of its narrow width. A wider beam at even low angles of axial incidence will give greater variation in illumination, and if the spread
amomints to for or de deg the frodight camot be used economically excent when nearly normal to the surface.

## The Spherical Projection Chart Mcthod

In making plans for floodlighting any considerable area, the illuminating engineer is as often as not embarrassed by the number of variables entering the problem. If only a limited number of lighting stations are available, the variables are reduced in number but there still remain the choice of lighting units, the number required, and the focal adjustment of each. When the number of floodlights reach a total of 50 or 100 , it becomes a serious problem to make an adequate preliminary layout of the proposed illumination for each floodlight must be treated as an individual, otherwise the engineer may find himself in the unhappy position of having plenty of light but not being able to distribute it properly.

The usual orthographic scheme of projection is useless for floodlight plans of any great size. Actually each individual beam illuminates an individual elliptical area, and each ellipse has its own major and minor axis, its own ellipticity and its own orientation. Orthographic drawings would of course represent each ellipse faithfully but this very faithfulness defeats the purpose.

Perspective drawings (or a photograph) come one step closer to usefulness, for if the point of view (or the camera) is at the lighting station then each floodlight beam is represented by a circle, but the diameter of each circle depends upon the angle at which the leam strikes the projection p!ane of the drawing. In general each beam will be represented by a circle of different size, but a group of circles even if to different scales will be vastly more tractable than a similar group of ellipses. As an illustration, the three circles $A, B$, and $C$ in Fig. 41 show the area illuminated by beams of equal diameter. The diameter varies as the distance to the plane of projection and as a result the beam to the top of the tower has a circle diameter three times as great as the beam to the adjacent comer. In order better to compare the three they are drawn separated from the drawing as $A^{\prime}, B^{\prime}$, and $C^{\prime}$.

A spherical surface with the lighting station as a center would make an ideal surface on which to make the layout, for then each beam would trace a circle of a diameter directly proportioned to its angular width and the variable scale of the plane
perspective drawing wodd be eliminated. of combe a spherical drawing surface is hardly a practical allair. but there are a number of wass of representing a spherical surface on a flat surface.

Occasionally a map of the world is seem in which half of the contire surface is present and which has parallets of longitude conferging topoints at the north and south poles.


Fig. 41. Plain Perspective Drawing of a Building. Circles $A, B$, and $C$ indicate the size of the spot of light that would be cast on those portions of the building by a floodlight of fixed spread. This variation in scale makes the perspective type of drawing difficult to use for making preliminary layouts

On these maps the lines of latitude make a half-hearted attempt to curve about the poles and this represents an effort on the part of the cartographer to lessen the formdistortion of the countries lying near the boundaries of the map. This curving of the latitude lines restores the outlying lands to recognizable form, but it changes the area scale, which is in our present case the very thing we are trying to avoid. By leaving the lines of altitude run parallel to the equator the areas are correct in size but distorted in outline.

We usually need less than a hemisphere for projection purposes and we are at liberty to make our drawing in the center of the web where distortion is least. In Fig. 42 the spacing of the lines of longitude is proportional to the cosine of the altitude. Thus
at altitude for deg., where the cosine is (0.5 the distance betwern the lines of latitude is half the distance at the equator.

The distortion is zero on this chart at the center and along the vertical and horizontal axes, but where the longitude lines depart much from the vertical the circular section of a beam would be plotted as an ellipse as illustrated in the upper left comer of Fig. 42. The seale of the drawing remains unaltered, say 10 deg. to 1 in., but a distortion takes place in the horizontal directions. It is therefore best to keep the drawing as near the center of the web as possible by shifting to right or left, but the vertical position must be left in the position it takes according to the vertical scale of degrees.

The semi-circular web in the center of the chart is used to plot the ground plan of the structure to be illuminated, placing the building in its proper relation to the lighting station which has a fixed position at the center of curvature of the concentric circles. If more than one lighting station is used, the layout must be repeated for each. Radial lines from the lighting station through the corners and other selected points of the ground plan and extended to the stub scale of degrees will give the angular relations between the vertical planes passing through the points. Both the stub scale on the ground plan web and the horizontal degree scale on the projection web proper are left unmarked, so that the projection can better be located near the center of the projection chart.

Two angles are sufficient to locate definitely any point on a sphere just as a point on the surface of the earth is fully located by its longitude and latitude. The ground plan is laid out to one of the two linear scales extending to the right and left of the lighting station, giving the scale some convenient value at the points marked $A$ and $B$. The curves at the bottom of the chart are then also given a corresponding value where marked $A$ and $B$. These sets of curves are simply tangent curves plotted to the vertical degree scale down the center. Thus a line through a point 300 ft . from the lighting station and 300 ft . high obviously has an elevation of 4.5 deg. regardless of its direction in azimuth from the point of sight. The point may be anywhere on a semi-circle 300 ft . from the center of the ground plan web, and a perpendicular dropped from the end of the semi-circle will intersect the 300 ft . tangent curve on a level with 4.5 deg. on the stub scale of degrees. The latter scale is
(as) $\underbrace{+}$ (

I
$\qquad$



Fig. 42. Spherical Projection Chart Applicable to any Floodlighting Calculation; Here Applied to the Solution of the Problem Described in the Article
"xamery duplicated by the scale on the projection wers, and the point can now be photed. It shouk be poted that 4.) dex. elevation is the same height regatedless of azimuth (fongitude) which is the rariation from map pactice previously noter
of the different sections. In the particular example chasen the end elevation, 12.5 ft . longe and 112.5 ft. high, is divided into two (i2. 5 - ft . sections, and the front facade, :00 ft. long hy 112.5 ft . high, is divided inte five fio-ft. sections. These sections are ketered from $A$ to $(;$ for reference.

TABLE 111
COMPUTATION OF FACADE ILLUMINATION

| 1 Nu |  |  | $\underset{B y}{\text { Mumimation }}$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. Useal | $\begin{aligned} & \text { Tumal } \\ & \text { Rated } \\ & \text { 1.14mens } \end{aligned}$ | $\begin{aligned} & 0 \eta \\ & \text { Section } \end{aligned}$ |  | A | B | ${ }^{\prime}$ | 1) | E | F | G |
| 12 | 24.000 | A | Proj.* | 2.046 | 0.428 |  |  |  |  |  |
| ${ }^{\text {i }}$ | 12,000 | B | Direct $\dagger$ Proj. | 0.172 | 1.200 | $\begin{aligned} & 0.276 \\ & 0.176 \end{aligned}$ | 0.144 | 0.072 | 0.036 | 0.024 |
|  |  |  | Direct |  |  |  | 0.072 | 0.036 | 0.018 | 0.012 |
| 18 | :36,000 | G | Proj. |  |  |  |  |  | 1.066 | 2.132 |
| s | 16,000 | F | Direct Proj. | 0.054 | 0.144 | 0.414 | 0.216 | 0.108 0.712 | 1.424 | 0.238 |
|  | 16,00 |  | Direct | 0.024 | 0.064 | 0.184 | 0.096 |  |  |  |
| 8 | 16,000 | E | Proj. |  |  |  | 0.950 | 1.424 |  |  |
|  |  |  | Direct | 0.024 | 0.064 | 0.184 |  |  | 0.024 | 0.016 |
| 4 | 8,000 | U | Proj. Direct | 0.012 | 0.032 | 0.480 | 0.59 .4 | 0.024 | 0.012 | 0.008 |
| $\because$ | 6,000 | C | Proj. |  | 0.228 | 0.740 | 0.246 |  |  |  |
|  |  |  | Direct | 0.006 |  |  |  | 0.012 | 0.006 | 0.004 |
| 58 | 118.000 |  |  | 2.338 | 2.160 | 2.454 | 2.318 | 2.388 | 2.586 | 2.434 |

*Proj. $=$ Projected Light. $\dagger$ Direct $=$ Direct Light.

## SUMMARY OF TABLE III

> Average illumination from beams.. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . $2.00 \mathrm{ft}-\mathrm{cd}$. Average illumination from direct light . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . $0.38 \mathrm{ft}-\mathrm{cd}$. Average illumination from beams and direct light. . . . . . . . . . . . . . . . . . . . . $2.38 \mathrm{ft}-\mathrm{cd}$. Average illumination from rated lumens . . . . . . . . . . . . . . . . . . . . . . . . . . . . $2.47 \mathrm{ft}-\mathrm{cd}$.

The summary of Table III shows how important is the direct light, which amounts in this case to 19 per cent of the beam light and almost compensates for the light lost at the ends of the building.

Facade Lighting as Computed by the Chart Method
In giving an example of facade lighting the purpose is to illustrate the use of the chart and not particularly to show a model example of illumination. To bring out some of the peculiar problems encountered let us taine rather an extreme case of large areas, high angles of incidence and low average illumination. Let us assume that the building of Fis. 4.3 is to be illuminated on two facades from a single lighting station at the point of sight, and that an average illumination of $2.5 \mathrm{ft}-\mathrm{cl}$. will be sufficient.

The first step in making the lighting plan is to draw the outline of the building on the spherical projection chart, using the lighting station as the point of view. Each facade is divided into a number of vertical sections, so that the drawing will indicate the areas

The second step is to compute the illumination from a single bare lamp along a line through the centers of these sections. This is done because there is a quantity of light radiated directly from the lamp that will illuminate the building, and this light is particularly useful on account of its perfect freedom from images, such as are found in the projected beam. In the units to be employed, a 500 -watt lamp is used and the direct light from the lamp may be taken as 500 candles. This makes a generous allowance for losses in the door of the floodlight and for possible interference due to crowding of the units.

On the basis of 500 candles per unit the illumination in the centers of the sections from $A$ to $G$ are, in foot-candles, 0.003, $0.005,0.023,0.012,0.006,0.003$, and 0.002 . These values may seem small but if each
illumination is maltiplied by the number of lamps they will in the agregate amount to a considerable fraction of the whole illumination.

The third step is to begin on the more distant sections and assign to each a number of beams that will bring the illamination nearly $u_{p}$ to the desired level. Thus 12 beams applied to section 1 (four to each circle in the illustration) with an estimated covering efficiency of $0 . f$ will give this


Fig. 43. The Building of Fig. 41 Redrawn in Spherical Projection. The circles on Sections $A, E, F$. and $G$ represent areas covered by $11-\mathrm{deg}$. beams; the circles on Section $D$ are for beams from the same type of unit spread to maximum diameter; while those on Section $B$ have an intermediate size. The large circle centered on Section $C$ is from a different type of floodlight giving an extremely wide beam. The computation of facade illumination by the spherical projection method requires the simultaneous preparation of a drawing of this character and a table of values such as given in Table III
section 14,400 lumens, which distributed over the 7040 sq . ft. of the panel will give an illumination of $2.046 \mathrm{ft}-\mathrm{cd}$.; and the section of the beams that overlap onto section $B$ will give an average of $0.428 \mathrm{ft-cd}$. The covering efficiency is estimated from the fraction of the beam section that falls within the bounds of section $A$, making allowance for the greater intensity of light in the center of the beam. These values are given on the first line of Table III. On the second line is given the direct light falling on the other sections from $C$ to $G$. It will be noted that section $C$ receives over a quarter of a footcandle of direct light from units that do not bear directly upon it. All the beams on section $A$ are at maximum concentration of 11 deg. total width, and even then there is a considerable loss of light above and to the side of the section.

The fourth step) is to assign leams to section $B$, which in spherical projection is secm (1) be of double the angular area. It wrubl seem wise in this case to spreal the beams to atmout 15 deg. and thas take advantage of the greater softeress of outline.

Step fiee is to illuminate section is at the opposite end of the building with is leams of 11-deg. width and a covering efficiemey of 0.4 .

Step six is to assign eight concentrated beams in section $F$, and adding to each column of Table 111 the proper amount of leam and direct light.

Step seven is to assign eight beams w section $E$, keeping the beams well in toward the near side of the section so that $E$ will not reccive too much light. This precaution is called for because a summation of the light already tabulated shows section $E$ to have an average of $0.9 \mathrm{ft}-\mathrm{cd}$. and most of this illumination is on the far side.

Step eight is to direct four spread beams onto the near ends of section $D$, as this section is also unequally illuminated by light from the beams on section $E$.

Step nine is to direct two beams from another type of floodlight onto section ( This section had received nearly two footcandles from units bearing on the other sections, and the small amount of additional light could not be properly distributed with the floodlight usect on the previous sections. These wide angle reflectors give 3000 lumens with the same lamp, as will be noted from the rated lumens given in the tabulation.

## Sign Lighting Computed by the Chart Method

It is sometimes difficult to plan illumination for surfaces that are irregular or broken in outline, particularly if of large area and a number of lighting units are required. For this type of work the spherical projection chart is a great help as it removes any doubt that may exist as to the angular dimension of the surface. Recently, recommendations were made for the illumination of a sign. Fig. 4t, madeup of three capital letters, each iff ft. high and $s \mathrm{ft}$. across each section of the letter. The total area is about $\mathbf{6 0 0 0 (}) \mathrm{sq}$. ft. and preliminary experimental work by the designing engincers has shown that from 10 to 15 foot-candles wrould be most satisfactory: The three letters of the sign stand close to one another; but as each letter in Figs. 4. and $t 6$ is drawn in spherical projection as seen from a different point of view, they are shown separated in the latter illustrations.

The letter $f$, drawn in spherieal projection, as in Fig. Fin, showed that with the beam of the selected floodtight drawn down to the narrowest angle the loss of light around the adges of the letter would be over two-thirds


Fig. 44. Plan and Elevation of Two Buildings on One of Which is Mounted an Advertising Sign with Letters 56 Ft. High Floodlighted from Stations at the Base of the Sign and on the Top of the Other Building
of the total light. Without the chart it would have been a matter of some difficulty to have computed the approximate average illumination.


Fig. 45. Spherical Projection of the Letters as Viewed and Lighted from the Stations on the Building Top Across the Street

There were two locations available for locating the lighting units, one across the street from which the entire sign except the lower part of the $A$ and $B$ could be reached, and a station close to the foot of these letters for the remaining section. The $A$ and $B$ as seen from the edge of the supporting frame are shown in Fig. 46, where each letter is viewed from a station as indicated by the arrows in Fig. 44. In the recommendations three sizes of beam from the same unit were called for, as it was found that neither the concentrated nor the fully spread beam would be suitable in all cases.


Fig. 46. Spherical Projection of the Letters $A$ and $B$ as Viewed and Lighted from the Stations at the Base of the Sign

The covering efficiency for the entire sign is estimated to be less than 70 per cent, that is 30 per cent of the light is lost around the sides of the letters.

The floodlights on the supporting frame were directed at the letters at a large angle of incidence so as to spread the beams out to cover larger areas, and even with this help some of the lights had to be thrown out of focus to the maximum degree, as illustrated by the larger circles on the foot of the letters $A$ and $B$, Fig. 46.
(To be continued)

## PREVIOUS INSTALLMENTS OF THIS SERIES OF ARTICLES

Part I. Types of Light Sources and Analysis of Paraboloidal Reflecting Surface by Meridian and Sagittal Lines (February, 1923, p. 75).

Part II. Parabolic Cylinder and Ellipsoidal Reflectors (March, 1923, p. 160).
Parts III and IV. Characteristics of a Parabolic Mirror and Spherical Source of Light (April and May, 1923. pp. 230 and 290).

# The Probable Number of Stops Made by An Elevator 

By Bassett Jones<br>Consluting Evgineer, New York City


#### Abstract

It is always hard to determine the number of elevators required to give satisfactory service in large buiddings. It is also hard to determine the duty eycle of the motor. The number of elevators refuirefl, and the duty cycle of the motors, are functions of the number of stops. The author applies the thenry , probabilities to determine the probable number of stops.-EDitor.


## General

In determining the number of passenger elevators required in a building, and in determining the arrangement of these elevators in banks, or groups of cars serving different groups of floors, the rational method is to treat the problem as one of traffic handling on the basis that "the passenger is the standard antomotive package that stacks itself in one tier.

Let $P$ be the total number of passengers arriving on the ground floor in the period $Q$. The value of $P$ may be determined either from a definite knowledge of the total population and their working schedules, or, such definite knowledge lacking, from a more general knowledge of population densities in rarious types of buildings used for various purposes, and from the corresponding records of traffic flow.

One phase of the subject, called the problem of arrival traffic, is concerned with moving the $P$ passengers from the ground floor in the time $Q$, and for this purpose, to use the most economical number and best arrangement of elevators coupled with service of suitable character.

The round trip time of each elevator having a given time-velocity characteristic is determined by the distance it must travel, the number of passengers it carries and the number of stops it must make. The first two elements are direct functions of the arrangement of the building and of the interval or time between departures.

Generally the interval is determined by the service required. It sets the available loading

[^54]time, and therefore the maximum number of passengers that the car will be required to carry and, so, the rated car load and its size.

The round trip time is the time between the moment a car leaves the ground floor until, having completed its trip, the car again reaches the ground floor, waits at the ground floor during the interval time and the moment it leaves on the next succeeding trip. The round trip time is composed of (1) running time. or the total time the car is normally in motion between stops and is a direct function of the relocity-time data for the type of equipment adopted. (2) standing time, or the total time the car is standing at floors including the interval, and (3) lost time, or the time consumed by false stops if any, the time consumed by limit slowdowns, and the synchronizing time, or the time allowed for maintaining the schedule when an abnormal number of stops occur, or for other reasons. Each of these must be separately computed, for each depends on a different set of factors, although all three are a function of the number of stops made.

Dividing the round trip time by the interval gives the number of cars required to maintain the schedule of operation, and to handle the traffic.

## Object

The object of this article is to explain a method based on the theory of probabilities, for determining the number of stops. The method of probabilities is merely the only known intelligent method of guessing. The only criterion of its legitimacy is the test of experience, and in this regard, it has proved to be quite satisfactory:

The application of the theory of probabilities to any class of data requires that, to a certain degree, the data be of random events.* In the case of elevator operation the assumption is that in all buildings the ordinary
movement of the population, in so far as it afieets the elevators, can be considered as randon. This is erpuivalent to assmming that all thoors are equally weighted. That is, that there is no antecedent reason why any one passenger shoukd wish toget off at any one floor, or that any partioular number of passengers should wish to get off at any particular floor.


Fig. 1
Method
Assume that $\lambda$ passengers enter an elevato: car at the ground floor, and that this car serves $u$ floors. The question is at how many of the $n$ floors will the car stop to discharge passengers, and what is the probable number of passengers discharged at any floor.

Each passenger has a choice of $n$ floors. Therefore the probability that he will wish to get off at any particular floor is $1 / n$. The probability that he will not so wish is $1-1^{\prime} n=\frac{n-1}{n}$. The probability that all of the $N$ passengers will wish to get off at any particular floor is $\left(\frac{1}{n}\right)^{N}$. The probability that none of them will so wish is $\left(\frac{n-1}{n}\right)^{r}$.

In general, the expansion of the point binomial

$$
\begin{align*}
& \frac{n-1}{n}+\frac{1}{n}=\left(\frac{n-1}{n}\right)^{N}+N\left(\frac{n-1}{n}\right)^{N-1} \cdot \frac{1}{n}+ \\
& \cdots+{ }^{N} C_{r}\left(\frac{n-1}{n}\right)^{x-r}\left(\frac{1}{n}\right)^{r}+\ldots+\left(\frac{1}{n}\right)^{x} \tag{1}
\end{align*}
$$

gives:
1st term: The probability that none of the passengers will wish to get off at any one floor.

2nd term: The probability that one passenger will wish to get off at any one floor, and that the remaining $(N-1)$ passengers will not so wish.
$(r+1)^{t h}$ term: The probability that $r$ passengers will wish to get off at any one floor and that the remaining $(N-r)$ passengers will not so wish.
$(\lambda+1)^{t h}$ term: The probability that all the $N^{+}$passengers will wish to get off at any one floor.
The values of the terms in this expansion for a few usual values of $N$ and $n$ are shown graphically in Figs. 1 and 2. Since frequency of occurrence is synonymous with probability, these graphs may be looked upon as representing the probable frequency with which any number of passengers will leave the car at any stop, also as showing the probable distribution of the $N$ passengers among the total number of stops made.

This statement results from the assumption that $\Lambda$, which corresponds to the number of trials is sufficiently large. In any particular case of elevatoring we are not so much concerned with individual round trips of a single car as with all the round trips made by all the cars in a bank during a given traffic period. In other words we are primarily


Fig. 2
concerned with the mean round trip for the whole bank. Thus, the terms in (1) may be taken to represent the mean conditions for several cars each making two or more round trips. In the usual high class office building case the upper quartile of the arrival traffic distribution curve, on which the elevator equipment is based, shows that from 200 to 2.50 passengers will be handled by each bank during the maximum $\overline{\mathrm{D}}$-minute period, involving a total of about 15 round trips.

From (1), the frequency with which no passengers will wish to leave the car at any of the $n$ floors is given by the term

$$
\begin{equation*}
P_{0}=\left(\frac{n-1}{n}\right)^{n} \tag{2}
\end{equation*}
$$

This term determines the probable number of floors at which the car will not stop. If $S$ be the probable number of stops made,

$$
\begin{equation*}
S=n\left(1-P_{0}\right)=n\left\{1-\left(\frac{n-1}{n}\right)\right. \tag{3}
\end{equation*}
$$

Values of $S$ for various values of $N$ and $n$ are plotted in Fig. 3.


Fig. 3
The problem can be visualized readily by means of a dice analogy. For simplicity assume the usual cubical dice, but of which five faces are blank and the remaining face given some identifying mark. Let there be 1 dice, of $n=6$ faces. Each dice represents a passenger. Each face of the dice represents a landing. The marked face of the dice represents the passenger's intention to get off at some one of the six landings.

If a dice be thrown, the probability that the marked face comes up is 16 . The probability that it does not come up is 56 . If $N$ dice representing $\lambda$ passengers be thrown simultaneously the probability that any number of marked faces from zero to $N^{t}$ come up simultaneously is given by some term, in the expansion of

$$
\left\{5,6+\frac{1}{6}\right\}^{x}
$$

If a throw be made for each landing, that is, six throws of the $N^{*}$ dice, the probable result will in each case be the same, and the relative value of each term represents the probability that the number of passengers represented by each such term will wish to leave the car at any landing. The most probable distritrip.
bution of the $\lambda$ passengers ammen the six landings will be in proportion to the values
 Of these, the first term (.) (i) ${ }^{N}$ is associated with zero passengers and therefore it is proportional to the number out of the total landings at which the car will not stop). On the same scale the cotal number of landings is proportional to 1.0. Therefore $\left\{1-(5,6)^{N}\right\}$ is proportional to the number of landings at which the car does stop. This number of landings is $6 ; 1-(5)(6)^{N}$, and is the value of $S$ for this case.

For ease in obtaining numerical valwes the formula (1) may be written,

$$
\begin{align*}
& \left.\frac{n-1}{n}+\frac{1}{n}\right\}^{N}=\frac{1}{n} x(n-1) x+N(n-1, N-1 \\
& \quad+\ldots+N C_{r}(n-1, x-r+\ldots+1\} \tag{11}
\end{align*}
$$

The expression in the right-hand bracket is the expansion of $\{(n-1)$ $+1^{x}=n^{x}$ which is the total number of ways in which the passengers may leave the car. Eliminating the term $(n-1)^{n}$, which is the total number of ways in which the passengers do not leave the car, the sum of the remaining terms is $n^{3}-(n-1)^{3}$, which is the total number of ways in which the passengers actually leave the car.

The most probable number of stops, $S$. defined by (3) may be called the normal stops. and defines the normal round

## Probable Variations from Normal

But we must also determine the probable variations from the normal stops, since the net effect of such variations may be to increase the round trip time in a sufficient number of round trips to slow down the service.

Let us take a case. Assume $N=12, n=10$, then, from (2).

$$
P_{0}-\left(\frac{n-1}{n}\right)^{x}=\left\{\frac{9}{10}\right\}^{12}=0.2 \Omega 2
$$

and from (3),

$$
S-n \cdot 1-\frac{(n-1)^{x}}{n}:=10 \times 0.72=7.2
$$

or, the value of $S$ can be obtained directly from Fig. 3 .

The question then is, what is the probable frequency of round trips in which $S^{\prime}=S \pm X$ stops will occur?

This (puestion is equivalent to asking maler what comditions maty the liest tomin the expansions of $\binom{n-1}{n}+\frac{1}{n}$, or the term $\left({ }^{n-1}\right)^{n}$ - We yreater or less than the value whathed when $X=12$, and $n=10$. on what is the same thing. when is; $\left.1=\binom{n-1}{n}^{v}\right\}$ less or greater than the value obtained for $\lambda^{\prime}=12, n=10$. ()hriously, when either.$V^{\prime}$ or $n$ are less or greater than the values given. But $n$ cannot change, therefore the variation must be equivalent to a deerease or 10 an increase in N, which is a probable cause of variation in . C

Therefore we must find the value of $N$ which, for a fixed value of $n$, gives the desired change in S.

From (3)

$$
\begin{equation*}
\lambda=\frac{\log (1-S n)}{\log \left(\frac{n-1}{n}\right)} \tag{4}
\end{equation*}
$$

Giving any value $S^{\prime}$ to $S$, for any given value of $n$, from ( $t$ ) the probable value $\lambda^{\prime \prime}$ of $N$ can be determined. From this the corresponding value of $P_{0}$ or $P_{0}{ }^{\prime}$ can be found from (2).

The relative values of $P_{0}$ and $P_{0}^{\prime}$ corresponding respectively to $N$ and $N^{\prime \prime}$ are then measures of the relative frequency with which $S$ and $S^{\prime}$ stops may occur and therefore, of the relative frequency of the round trips involving $S$ stops and of the round trips involving $S^{\prime}$ stops.

The value of $P_{0}{ }^{1}$ is the probability that no passengers will wish to leave the car at any floor in a round trip involving $S^{\prime}$ stops, where $S^{\prime}=S \pm \lambda$. If we put

$$
\begin{equation*}
P_{0}^{\prime} P_{0}=I^{1}, \tag{.5a}
\end{equation*}
$$

when $S^{\prime}>S$, and

$$
\begin{equation*}
P_{0} P_{0}^{\prime}=u^{\prime} \tag{5b}
\end{equation*}
$$

when $S^{1}<S$. In either case, put

$$
\begin{equation*}
P_{0}=w, \tag{6}
\end{equation*}
$$

then $w$ is proportional to the number of normal round trips involving the normal number of stops and $w^{1}$ is proportional to the number of round trips involving $S^{1}=S \pm S$ stops.

The use of (t) can be aroided by using the relations given by (3), namely,

$$
S=n\left(1-P_{0}\right),
$$

and

$$
S^{1}=n\left(1-P_{0}{ }^{1}\right)
$$

Then

$$
\begin{equation*}
\Gamma_{0}=1-S / n \tag{7a}
\end{equation*}
$$

and

$$
\begin{equation*}
I_{n}^{\prime}=1-S^{1} / n \tag{7b}
\end{equation*}
$$

Therefore, when

$$
\begin{align*}
& S^{\prime}>S \\
& u^{\prime \prime}=\frac{1-S^{\prime} \cdot n}{1-S}=\frac{n-S^{1}}{n-S}
\end{align*}
$$

and when $S^{1}<5$,

$$
w^{\prime}=\frac{n-5}{n-5}
$$



If any value of $N$ and $n$ be given, the value of $S$ is found from the graph in Fig. 3 and the corresponding value of $P_{0}$ from the appropriate graph in Figs. 1 and 2. Then by (8a) or (sb) the values of $w^{1}$ may be determined for $S^{1}=S \pm x$.

The value of $w^{1}$ for various values of $\Lambda$ and $n$ are shown graphically in Fig. 4. These graphs show that:

1. The probable frequency of variations from the normal round trip increases as the ratio $r=N n$ decreases; that is, for any given number of passengers $\lambda$ per car, the probability of variations from the normal increases as the number of floors served, $n$, increases.
2. Except for a very limited range both in the value of $r$ and in the value of $x$ in $S^{1}=$ $S \pm x$, it is more probable that the value of $S^{1}$ will be less than the normal than it will be greater than the normal. In other words, only in a few cases is it likely that any material number of round trips will occur involving a number of stops in excess of the normal. Therefore, except in a few cases, ample precautions against delay will be taken if the normal round trip time be used to determine the proper number of cars.

These conclusions also follow both from experience and from obvious general considerations. They may be summed up by saying that in nearly every case the actual average number of stops during any traffic period will be less than the most probable number of stops calculated on the basis of random traffic. The actual traffic is more likely to depart from its assumed random character in a negative direction than in a positive direction.

Having thus determined the normal number of stops, dividing the hoist by the number of stops less one, ( $S-1$ ), gives the average distance the car travels start to stop, from which, and from the velocity-time data for the type of hoisting engine being considered, the normal running time can be determined with some reasonable degree of accuracy.

## Non-random Arrival Traffic

If, due to unequal weighing of the floors, the traffic is not random, say, because a specially prompt arrival occurs on one group of floors, because the bank serves groups of floors having markedly different areas, or because certain groups of floors have markedly different population densities, divide the floors served by the bank into the necessary groups $n_{1}, n_{2}$, etc., and divide the passengers per car into proportional groups $N_{1}, N_{2}$, etc. Then determine the value of $S$ for each such group. and add together the results. Such conditions will be of importance only in rare cases.

## Transient Traffic

The maximum number of stops may not occur during the arrival period, but during the noon period when people are simultaneously arriving and departing. The rate of passenger flow may be less than the rate of passenger flow during the arrival period, but the cars make stops in both directions of motion. Again there may be some departure traffic during the maximum arrival traffic; all of which depends on the working habits of the population.

This simultaneous arrival and departure traffic during the noon hour or at other periods may be called "transient traffic." In such cases, let $N_{1}$ be the number of passengers entering the car at the ground floor, and let $\Lambda_{2}$ be the number of passengers leaving the car on its arrival at the ground foor. Then $S_{1}$ is determined as the most probable number of stops on the up motion, and $S_{2}$ is determined as the most probable number of
stops on the down motion. Their sum is the most probable number of stops in the round trip.

## Comparison with Experience

For a long period it has been the custom, based on observed stops, to assume that during the morning arrival traffic peak the cars would stop at 0.8 of the floors on the up motion while delivering the passengers loaded on the ground floor. It is interesting to note how much of the data presented in Fig. 3, averages $S=0.8 \mathrm{n}$. This figure will approximate to a very large range of usual cases. Purely arbitrary allowances have been made for an abnormal number of stops, which allowances experience has proved were as likely to be insufficient as to be too liberal. In such cases the wrong value of $S$ was used. As shown above, if the proper value of normal stops, $S$, be used, ordinarily no such allowance will be necessary.

A comparison of the computed number of stops with the actual number of stops was recently made in four large office buildings. The average number of passengers both entering and leaving the cars at the ground floor and the average number of stops made by the cars during the arrival period were determined by count. The data as to number of passengers and number of floors served was taken into the curves of Fig. 3. The results varied from the count by tenths of a stop. In one case the variation amounted to sorewhat over one stop.

Furthermore, it has been a very general custom to estimate the number of elevators of some arbitrary size required on the basis of some entirely empirical ratio to total rentable floor area. The above discussion shows why such a method is likely to give wrong results unless the ratios compared are from identical buildings used for identical purposes and occupied by the same class of tenancy. So far as the method discussed above is concerned, the rentable area enters in only when other and more accurate determinations of population are not available.
Application to the Determination of Power Input
Having thus determined the probable average, or normal number of stops, and their time distribution, an average duty cycle can be set up and the probable time distribution of input to the hoisting engines established by the method given in "Resultant Duty "Cycles," Geveral Electric Review, Vol. XXV, No. 7, p. 40.5 (see footnote page 58.3 ).

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Alloys, Magnetic
Magmet Steels. Kayser, J. Ferdimand. Ele'n, May 25, 192:3; 1.90, [11. $557-558$.

## Alternators

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## FRANKLIN S. TERRY

Vice-President General Electric Company


## THEORY AND PRACTICE IN THE PROJECTION OF LIGHT

One of the pet phrases of technical literature is "reducing theory to practice," the implication being that theory is upon an elevated plane and requires considerable reducing to bring it down to the level of its humble co-partner. There are cases where theory is indeed greatly superior to practice, but this is not always so. It more often happens that greater intelligence and skill are required to make a thing than to theorize about it. This is largely due to the common fault theories have of being incomplete, and when we attempt to complete them we encounter the other difficult task of "reducing practice to theory."

Something along this line has occurred in the science and practice of projecting light. The theoretical optician, with perhaps more than a touch of smug content, looked down upon the struggles of the practical worker and did not realize that practice was well in advance of theory and was indeed being hindered by the lagging member of the team. If a reason is sought for this state of affairs we need look no farther than that beautiful matheratical concept known as the "point source" of light. Its beauty is its curse; and so long as the theory of projection concerned itself with only this concept, it arrived nowhere. Once the idea of a finite light source is introduced the subject immediately becomes com-plicated-and neglected. The practical experimenter not being aware of the troubles he is breeding for the mathematician goes ahead on a trial and error basis and. while the errors make almost the same sad total as the trials, still he makes progress and arrives at results.

Why does a high-intensity are give five times the beam intensity with only half again the light of a low-intensity arc? Can a mirror be formed so as to concentrate light on a distant point? How wide is the beam for a $60-\mathrm{in}$. mirror at five miles? Why should a monoplane filament be used with a shallow mirror and a spherical shaped filament with
a deep one? Should a large mirror be more accurately formed than a small one: Has the depth of the crater any influence upon the choice of mirror angle:

These are samples of practical and important questions on which the literature of the subject is almost silent. for the classical "point source" of the text books sheds very little light that is of direct service to the experimenter, and if he has often stumbled the blame is not entirely his.

Beginning with our February issue we printed the first of a series of articles on "Studies in the Projection of Light" in which the author has outlined the theory of projection as applied to light sources in everyday service. Mir. Benford has had years of experience in designing projection equipment. but by far the greater part of his work has been in the testing of both experimental and standard devices intended for a wide variety of service. A proper test can hardly be run without snme little study of the inward workings of the beam, and from these enforced studies has arisen what is probably the most complete mathematical surver of the theory of projection that has so far been published.

There are few branches of engineering that are more in the public mind or that seem to have a better future ahead than this branch of illuminating engineering. The automotile headlight alone is the subject of considerable legislation and police requlation (with a different set of laws and rules for each locality) ; and it does not take much of a seer to predict that when we travel in our individual airplanes we shall be in need of all the knowledge that can be sained by a most earnest co-operation of theory and practice. Today there is a battle on between the bombing plane and the defending gun aided at night by a beam of light. Victory for the defending forces depends largely upon how we combine all our resources in the design and construction of the searchlight.

# Staging the Unseen 

<br>R


#### Abstract

   out such at lochmate of practice as will wathe a varicty of worthy progratms to be arranged and then broadeast with a ratism whim imathation makes ome forget the sonse of sight is not being employed as well. The  


I vast audione sits before a curtaim that is newer raised. Whather the program be one of education of amusement, music or dramatic art, the listeming car must be so satisfied that the maseing eve is forgotten. Perhaps it would to more accurate to say that he simend alone the mind must be led io visuatize the stage and its characters. Above the proscenium are inscribed three letters, " ${ }^{1 /}$ (i Y"."

In the Studio the watchworl is ever "Responsibility." The transmitting apparatus -from microphone to antenna-is merciless in the accuracy with which it spreads aboroad erery syllable and note exactly as they come from the lips of the speaker or singer. In fact, it registers and makes evident tonal defeets that would not be perceived by one who has not had studio experience.

Here, then, is a new set of conditions that must be considered in the production of music, addresses, plays, operettas, and the many specialties that find a place on broadcast programs. On the actual stage or concert platform, where flesh-and-blood personality reaches out across the footlights, the play or song is carricd over with a score of aids that make a convincing and delightful ensemble. In the broadcasting studio, however, the voice is, so to speak, dissected out of its customary surroundings and held up in cold blood for critical inspection-and even then it must suggest the warmth and verve of a performance that is visibly presented.

In is staging of the unseen, the studio management is keenly sensitive to the presence of an unseen audience. The fancy cannot help drawing a picture of unnmmbered men, women, and children, gathered in circling ranks, silent, unapplanding, but critical with a concentrated attention that hardly any other form of entertainment receives. The pure force of an invisible audience, greater than any that has been assembled, impresses one with the responsibility of broadcasting far more than would the physical presence of a great ascembly. Imagination? Yes; but a perform-
ance that is to appeal to the listeners' imagination must also be conceived in an maginative spirit-and the sense of responsibility is none the less real.

There is one person, however, who must not feel an undue pressure of responsibility unless he or she be a seasoned artist whose certitude is proof against the most unusual conditions. That person is the performer. From the moment that an applicant for radio honors makes contact with the studio management, every effort is put forth to relieve the singer, or speaker or instrumentalist-as the case may be-from any anxiety peculiar to a hidden stage and an unseen audience.

In justice to those who shall histen and in true kindness to the applicant, the first process must be one of elimination. Radio aspirants are almost as numerous as candidates for motion-picture fame. They apply by letter and in person. They are of course in quite a different class from recognized artists whose services are engaged by the Studio through established channels.

The Studio is ever hopeful of discovering hidden ability among the many who seek to put their names on its programs. The hope is not always vain. No one is refused a hearing. Whether it be a modest performer on the saxophone or a soprano who offers nothing less ambitious than "Vissi d'arte," the same courteous hearing is given.

If the voice or the instrumental ability be of such a calibre as to justify further consideration, the next step is to select numbers that will display it to the best advantage. If ever the studio directorate had need for tact it is in separating a clever amateur from some pet number that has literally been "done to death"-and the pet numbers are always the same. The weekly scries of programs could be filled with vain repetitions of the "Polonaise Militaire," "Humoresque," "Melody in G," "Road to Mandalay," "May Morning," and a half dozen other "war horses" that are so miversally ridden to a fall unless the rider


Fig. 1. Senator Guglielmo Marconi Broadeasting from WGY




Fig. 5. The WGY Players in Action Scene from "The Great Divide "
be that fine type of artist who can do simple things superlatively well.

Another problem is the vocalist who can sing a ballad well but who is convinced that the radio audience will prefer a sketchy attempt at some famous operatic aria. In the end, a selection suited to the woice and skill of the performer is suggested and insisted on with such arguments as will persuade without wounding the pride; and another item is built into a program that is being prepared for a date three or four weeks in advance.

Day by day this preliminary process goes on. Not only must the individual be carefully considered but also the nature of the whole program, the balancing of it with other and dissimilar offerings, the pleasing of every taste within the scope of a few concerts, and the observance of public holidays and national and local occasions. All of these things are variously shaped stones that must be fitted into a mosaic pattern that a critical public shall pronounce good.

The Studio has a nucleus of professional musicians, the WGY orchestra, about whose work are grouped the performers selected week by week to participate in the programs. As experienced members of the staff, the musicians in this orchestra have achieved a sense of responsibility which but adds to the artistic finish of their performance. Not so, however, with those who are making their first appearance behind the unraised curta $n$. Here-for we are now entering the studio proper on the evening of a performanceeverything is planned to forestall the nervousness that may arise at the thought of a vast viewless audience or be evoked by the very real lonesomeness of the position.

A singer of songs, a tiny mechanism, and half a continent ready to listen! Be the voice ever so good, the music ever so well learned, there is enough of the bizarre in the situation to add an extra beat to the stoutest heart and lend a little quiver to the steadiest nerve. Facing an audience that stretches away for a thousand miles-and yet isolated! No wonder that the studio staff steps in and shifts as much as possible of the musician's responsibility to its own shoulders.

To this end, the unseen stage might well be the music room in the singer's own home. To be sure. the walls must of necessity be covered with soft fabric. The acoustics of broadcasting demand this. But the rich gray folds that hang from ceiling to floor are in themselves a home-like furnishing. There is nothing of the stage in the artistic lights or in the deep rugs
that cover the foom. The commentalle chairs, the piano, and in fact all the cogy charm of the room has been phanned torifiet any feeling of strangeness.

Best of all, there is no uncouth instrument staring the musician in the face, ready of announce to the word any deviation from pitch or shurred pronunication. Instead there is a "homey" appearing floor lamp - at least it looks like a floor lamp-near which the performer stands. Suppose a microphone is concealed beneath the dainty shade; suppose it is our contact with a continent! It makes no impression on our minds as it falls quietly into place with its surroundings, and we shall sing and play with the same confidence as within our home walls!

There is one departure from the normal, and that adds to the interest of the experience without cramping the musician's freedom. In an adjacent control room, an unseen operator listens to every note as it comes from the broadcasting antenna. Under his hand are tiny switches which flash electric signals to the studio director. "Louder,""Softer,""Stand Nearer"' if the singer or player needs any such instruction, the word, in letters of light, appears in sight of the director, who holds out a card, similarly inscribed, within the performer's vision. It does not disconcert; rather it is an assurance of friendly co-operation.

Thus from the first interview with an applicant to the moment when his last note rings true in a hundred thousand receiring sets, the Studio has felt and honored the responsibility with which it was charged.

So much for the initiation of one candidate into the Unseen Order of Radio Performers. The next degree is marked by more elaborate work. Would the brilliant Gilbert and Sullivan have countenanced an invisible presentation of "The Mikado," or "Pinafore," or "The Pirates of Penzance": We entertain the opinion that they would, if they could have been present at a WGY rendering of these immortal creations.

It is all there-thanks to two microphones, a careful stage director, and an alert company of singers. The orchestra remains at one strategic point-but the caste! Such silent comings and goings as were never in the original instructions of IV. S. Gilbert! Such stealthy approach to a microphone for the purpose of a solo! Such forming and dissolving of ensemble groups at another microphone! Preliminary explanations are made by the announcer, but it is in the hands of the performers to thrust the rollick and glow of
the eomie operat deep into the imatgination of the atudience．
＇Those who hater heard these radio rendi－ tions assure 1ss that they not only hear the stamp）of the foot，they can aetwally see the flashing eyes and donbled fists as the linafore chomes bursts into the sublime swagrer of ＂A British＇「ar．＂They can follow every grimaee of the dejected Ko－Ko as he groans over the＂caricature of a face＂and they iteh to join the dance of the＂maidens from the shipping＂whose steps they can farly see through the unraised curtain．

The Studio has taken another step forward in its staging of the mseen．It is the father of the Radio Drama．Through its lowered cur－ tain was projected the first entire play ever broadeast．It was a bold venture．Conld a three－act play be acted by radio？The venture was made，and radio drama has become one of the Studio＇s most popular offerings．

Comedies of the better class are atternated with dramatic presentations，and are equally well received．One night each week is given i1p to the play．The orchestra is in attend－ ance for overture，entr＇acte，and incidental music，and of course the announcer performs the function of an annotated program．

The listener hears more than voices． Telphone bells ring，doors slam，wind storms rage，rain patters，the noise of moving chairs and of revolvers is heard．From these elc－ ments and from the preliminary explanations of the ammouncer，the drama is built before the cyes of the audience as well as in its ears．Nor are the actors to be classed as amateurs．They are men and women well seasoned in stage－ craft，and with records of success in their vocation．They have brought these qualifica－ tions to the creation of a new dramatic art； they have entered into this spirit of creation with an enthusiasm and a wealth of personal resource that have uncovered remarkable possibilities in the projection of motion and scene through the medium of sound．

Not all the programs broadcast from the Studio are carried out there．It has reached across whole states and transmitted to its audience interesting public events at the very moment they oceurred．Its listeners have heard from New Haven the eheering at a Harvard－Yale football game and have received word of each play as it occurred； all of this has come directiy from the fietd． They also participated in the world＇s series haseball sames at New York in 1122，and they have sat at distant banquet tables where famonts speakers delivered messages of great
import．These miracles were performed by atid of long－distance telephone wires installed at the field or in the dining hall and equipped with microphones that speeded every sound direct to the transmission apparatus of the Studio．

In so far as seriousness of purpose and effectiveness of aceomplishment are con－ cerned，WGY has struck its richest chord in the regular broadeasting of Sunday services direct from the churches in which they are held．Here，for the time，the studio aban－ dons all suggestions of the stage and of entertainment and enters the larger room of human hearts．In a spirit of reverence and helpfulness，it takes its place among the influences that uplift men＇s souls as no purely cultural endeavor can．

Its mission is to the sick，the isolated，and the infirm－to all whom circumstances pre－ vent from joining in a common worship．And yet it is a common worship to which they are invited．Each listener to hymn and anthem， sermon and prayer，knows and feels that he or she is joining hands with thousands as in spirit they kneel before one altar and unite their aspiration and devotion．Let a single letter bear evidence．It is taken from a great number of similar import and is from an aged， blind woman living on Cape Cod．
> ＂I am writing you a few lines this beautiful morning to tell you how much I enjoyed your good sermon Sunday afternoon，also the singing of＇Just as I Am．＇The prayer went to my heart．I heard every word of the sermon and singing．I could hear just as plain as though you were in my room．I have been stone blind over 12 years，have not seen one ray of light．I take care of a crippled husband who is over 80 ，and cannot walk a step alone．Some－ times the way seems dark，but my dear Heavenly Father gives me strength every day．It is one of the most wonderful inventions to know that I can sit here way down on old Cap Cod，and hear such lovely sermons and singing．God bless the man that invented it！＂

In different vein，but not without its own touch of pathos，is the story of a woman nearly seventy－five years old who has been unable to attend church in five years．Since the Studio began its Sunday broadcasting， this good lacly dresses in her best when service time approaches，places her chair by the radio set，and attends the service．When the collection is announced，she puts her offering on a plate by her side and，next day，formards it to the pastor of the church whose service she has heard．

In its comprehensive embrace，WGY co－ operates with Government welfare agencies． The State Board of Health has broadcast a


Fig. O. Harp Solos Prove Delightful Music for Broadcasting. Floorlamp" microphone in foreground


Fig 11. M. Charles Kanony, Leading Baritone of the French Grand Opera Company


Fig. 10. Charles Wakefield Cadman, Well known American Composer with Princess Tsianina, Mezzo-Soprano


Fig. 12. Jackie Coogan Filming a Few Words for the Radio World


Fig. 13. WGY Broadcasting the Harvard-Yale Football Game from New Haven, Conn.


Fig. 15. Two Kinds of Waves Join Hands
long series of messages on the prevention of disease and on the many obscure factors that are of importance to public health. The Highway Commission gives weekty reports on the condition of New York State roads. Intimate afternoon talks are broudeast for the bencfit of homekecpers who will gain by authoritative advice from experts in domestic economy. Twice a dary, a complete report of the New York Stock Exchange is given, and every evening the day's produce market is reviewed for the information of growers who are engaged in sending farm and dairy products to centers of consumption.

We have spoken of the Studio's "unapplauding" audience. Let us modify the phrase. The artists who fill programs do receive an applause that is far more earnest than any clapping of hands. Every day, hundreds of letters are received that do not merely congraiulate 1 VGY on its offerings, they are also expressions of thanks. They chat with the studio management as with those who have entered their homes, cheered their sick and brought courage to the sorely tried. They make special mention of the melody or the word that has flown across the many miles with comfort on its wings. They ask for this or that selection as one would ask it of a friendly artist and guest. These letters are the real reward of work. They are evidences of gratitude that urge the worker to still better serrice-for WGY in its large aspect is a personal as well as a public service.

This article would be incomplete without reference to a special contribution which the Studio makes to general welfare-a contribution depending on its ability to speak in one
breath to excry town and hamlet on the continent. A man or whan has mesteriously disappeared; a child has been stolen and may have been carried far away. 11 ow can a nation be instantly put on the look-out? WGY is ready at a moment's motice to bramlcast deseriptions and, on occasion, offers of reward. Time and again it has performed this service, and in several instances has been the means of rescue.

This is the most dramatic scene that can be enacted in a broadeasting studio. A ery for help from those whose dear one is lost - the quick response - the turn of a switch - a few words spoken quietly into the microphone and heard wherever there is an ear to listen-a thousand communities put on the alert-and all within perhaps five minutes.

Where is there a stronger or stranger "situation" in fiction: Where is there a kindlier or more efficient service to home and public than this that is offered by the Studio?

It has been said that every man is the richer for what he gives in a spirit of good will. This truth has its expression in the broadeasting studio. More than one performer, who has shown traces of nervousness as the crucial moment approached, has been told a story of the gratitude expressed by a crippled child or an invalid whose life has been made brighter by WGY. In the interest and pathos of the story, the singer has taken on new courage. With the picture of that eager little listener before the mind's eye a new ferror and inspiration have gone into the music-a spirit that has, in equal measure, enriched the program and the soul from whose very depths the song has come.


# Electrical Development in Australasia 

13Y゙(i. (i. (`REE<br>


#### Abstract

   


The traveler to Australia or New Zabamd. who has not primed himself with knowledge of the "Iskand continent" is likely to hate a number of surprises in store for him at the end of his 10,000 -mile voyage across the Pacific Ocean.

There he will find no erude civilization such as might be imagined to exist in a country that has only been settled for a matter of 100 years, and has only a population of seren million to cover an area greater than that of the United States and Great Britain combined.

The electrical development of a country's urban centers might be a misleading guide to its degree of civilization, but it would certainly provide an estimate of the progressiveness, energy and initiative of its people.

Judged on this basis Australasia ranks high. Not only is the proportion of houses reached by electric service fifth among the nations of the world, but there is now in operation in Melbourne the largest suburban railway electrification in existence, and a similar project is now under construction at Sydney.

It is probably correct to state that the people of Australia and New Zealand have more faith in the ability of electricity to solve their labor and transportation problems than any other nation, and they are backing that faith with all their resources, natural and financial.

## Systems of Supply

Fifty-cycle, three-phase current has been adopted as standard except for railway work. Even in that field, the New South Wales Government Railways have decided to introduce 50 -cycle turbines into their 25 -cycle power house at Sydney, for the electrification of the Sydney suburban railways, so that no extensions will be made to the 25 -cycle system.

Service voltages are far from uniform and an example of the onerous burden imposed on the industry is afforded by the diversity of incandescent lamp stocks. The larger
importing houses must carry in stock about (in) different lamps to meet adequately the demands of the trade.

The Institution of Engineers and the Bureau of Science and Industry of the Ferleral Government are working actively for standardization with satisfactory results.

Practically all new alternating-current developments will distribute to consumers at 2.3) volts single-phase, and 400 volts threephase, the " Y " and delta voltages, respectively, of three-phase transformers, which are commonly used.

## Distribution Systems

This high scrvice voltage is associated with a distinctive scheme of distribution. Paper insulated lead covered cables operating usually at 6600 volts are laid directly in the ground and run from the generating station or main substations to small brick transformer houses containing comparatively large distribution transformers of capacity up to 300 or even $500 \mathrm{kv}-\mathrm{a}$. From there, the $230 / 400$-volt supply is led to the consumer's premises. This question of distribution is one which is exercising the mind of American engineers today and there is no question of its importance.

Other nations have profited by the pioneer work of American engineers in the central station field. The consumer's voltage of 110 to 120 common to all the United States was undoubtedly chosen to meet the initial difficulties of carbon lamp manufacture. A high service voltage is a necessity in Australia where apartment houses are hardly known and practically the entire population is housed in "one-family" houses with a garden. For example, the metropolitan area of Melbourne is greater than that of New York or Paris, but the population is only 800,000 .

In consequence, the distributing costs are usually greater than the generating costs. the ratio being approximately $60: 40$, while in comparable American utilities, it will be found that the relation between distributing and generating costs is reversed, being more nearly $40: 60$.

Electrical Apparatus in Australia
It is only within the last few fears that Sustralia has moned serionsly to the manufacture of her requirements in eleetrical expapment. In placing orders in the past. the various publice utilities (they are nearly all owned hy states or momicipalities) hate been particularly free from prejulice, and Atsetralia has offered a market for the electrical mannfacturers of all nations. As a


Fig. 1. Seven $3000-\mathrm{kw}$. Synchronous Converters in the Substation of the Electrolytic Zinc Company of Australasia
result, competition has been keen and the visiting engineer finds there electrical apparatus of American, British, German, Swedish and Swiss manufacture, the first two, of course, predominating.

In operating, American and British practice is followed exclusively, the latter being particularly in evidence where the influence of British consulting engineers has been felt.

Australian engineers have not manifested any marked indication of following their lead in such details as split conductor distribution (underground and overhead) and truck type switchgear, although the latter is becoming popular in America.

The enormous size of Australia compared to its population alters the whole aspect of commerce within the country. Although Australia has more railroad mileage per inhabitant than any other country, transportation to inland points is expensive. The unfortunate adoption of different gauges by the various state railroads aggravates this condition. As a result when steam coal is, say, $\$ 5$ per ton in Sydney, it will be $\$ 20$ in Broken Hill, the well-known lead and silver mining center in the same state. Water in Broken Hill costs $\$ 1.25$ per 1000 gallons.
 pay substantial promiums for high effergeney in their power equipmente It is tunt ontmate, under these eonditions, that eard minn has establishod its ewn pewer station. A Lhere are ten important mines gromped elowly, with a total prak load of about 24.t世日 kw, the conditions are iteal for entrat station service. It should be noterl, in pasints. that the generating stations of the larger mines are models of goot engincering both in clesign and operation, while much ingenuity and originality has been exercised by the local engineers in the application of power in the mines and on the surface. To cite one example, the first application of centralized motor control on a big scale was made at "The Itill." The summers there are hot and exceedingly dusty, ambient temperatures of 11.) deg. not being uncommon, so that the duty of the hundreds of motors ranging in size from $\frac{1}{2}$ h.p. to $800 \mathrm{~h} . \mathrm{p}$. is unusually severe.

It is significant that General Electric equipment is used almost exclusively

## Power and Light Supply-Municipal Ownership

With very few exceptions, the retailing of electricity is in the hands of the municipal authorities. The generation of power is undertaken except where there is already in existence a nearby source owned by a larger municipality, private undertaking or the state, from which an efficient supply can be purchased.

## State Control and Ownership

Until recent years the State Governments took little part in the electrical development of the country. Each state had its "Electric Light Act" which regulated the industry in a small degree, chiefly from the standpoint of safety to the public. Today, however, all the state bodies in Australasia are engaged to some degree in the business of electrical supply: The picturesque island state of Tasmania has received a remarkable amount of publicity as a result of the vigorous policy of the Government in developing the hydroelectric resources of the state. As a result, a number of industries have been attracted to Tasmania, which for many years had seemed to have reached almost its complete development as an agricultural. and later, as a mining state.

At the Waddamanna power station, there are seven $70.50-\mathrm{kr}-\mathrm{a}$. General Electric alternators driven by Boving impulse wheels
wanker aterat of lown foet The voltage is
 milesto Ilobart．

In this，the caprital cit！at an historic and beatulfully sitated lown of（i0），000 imbab）－ itamts，the entire statiom ontput is ab）－ sorbere．


Fig．2．Split Conductor Transmission Line，Victorian Railways． Each circuit is composed of six $\frac{7}{16}$－in．copper conductors

The largest customer of the Government is the Electrolytic Zinc Company with a capacity of over 120 tons of zine per day． At these works，the complete electrical equip－ ment was supplied by the Australian General Electric Company and consists of seven $3000-k w$ ．synchronots converters by the British Thomson－Houston Company．The d－c． roltage is induction regulator controlled between .00 and 600 volts．

The switchgear was also built ly the British Company，while the transformers are of General Electric manufacture．

The Victorian State Government has for years maintained a very progressive attitude toward electrical development．The elec－ trification of the Melbourne suburban rail－ way lines is the largest undertaking of its kind and provides the suburban dweller with transportation facilities which are not approached by any other metropolis．The possibilities of electrification were first brought to the attention of the Victorian Railway Commissioners in 1596 by Mr．A．W．Jones who was then the representative in Australia of the General Electric Company．

It was mot antil l！日le that contracts were pated and after serions delays due to the war，operation was begun in I！n！g．

Blectrification from an overhearl trolley at 1.500 volts has been applied to 33.5 single track miles．The system was deseribed in what in the Ceneral Elemotric Review for August，1！20．Some of the features of the power plant equipment are of particular interest．

There are six gencrating units totaling $70,000 \mathrm{kw}$ ．in capacity：Each alternator is permanently connected to its transformer bank and differential relay protection is provided across the combined alternator－ transformer unit．

The generator voltage is 33300 ，the distri－ bution voltage 20,000 ，and the frequency 2．）cyeles．The main point of interest is probably the adoption of split conductor protection throughout the system，this practice being adopted on the overhead transmission lines as well as on the extensive cable network （see Fig．2）．All transmission circuits are so protected with the exception of two workshop feeders which are not split but are protected by pilot cables．


Fig．3．Draw－out Type Switchgear with Buses Enclosed in Compound－filled Compartments．This type of switchgear is used in some of the Victorian Railway Substations

In lieu of lightning arresters，each over－ head feeder is carried through two or three hundred feet of underground cable before entering the station．Feeder switches are of the split conductor type，the contacts being arranged so that the split conductors of each phase are connected together only when the switch is closed．By this means，faults at the
distant end of a feeder will be cleared without the addition of end reactors. Other advantages such as convenience for lesting are held to assist in justifying the extra expenditure involved in providing all singlepole circuit breaker units with three terminal bushings.

Of the substation equipment, the British Thomson-Houston Company supplied four $4500-\mathrm{kw}$. and cight $1000-\mathrm{kw}$. synchronous converters (the latter with automatic control) in which novel means have been adopted to prevent commutator flash-over due to d-c. short circuits.

The commutator is made the same diameter as the armature, and fan blades are fitted to the armature periphery, so that a strong air current flows outward axially across the face of the commutator in combination with a magnetic blow-out from the brush-holders. The hot gases from the brushes under short circuit conditions are thus prevented from reaching the adjacent brush-holder and establishing the highly destructive commutator flash-over. This type of construction is shown in Fig. 4.

The entire work of electrification was carried out to the plans and designs of Messrs. Merz and McLellan, consulting engineers of London, and under the direct supervision of their Melbourne office.

It is notable that the first car equipments exported by the General Electric Company, almost 30 years ago, were shipped to Melboume.

## The State Electricity Commission of Victoria

In 1919 the Victorian Government formed an Electricity Commission consisting of four members who are appointed by the Government. With the exception of the Chairman who devotes his entire time to his official duties, the appointments are honorary, the Commissioners receiving only a nominal fee for each meeting that they attend.

The powers of this commission are very wide. Not only does it act in the supervisory capacity of the Public Service Commissions of the United States, but at present it is engaged in the opening up of the Brown Coal Fields at Morwell, the construction of two $50,000-\mathrm{kw}$. power stations with 115 -mile transmission line to Melbourne, terminal station, and substations. When power is available from this source, the Commission will sell power principally to municipalities and other retailers, but in some cases the Commission may sell direct to the consumers where expedient.

In 1! 2 I , after inviting and reariving tembers from the leading American and Emopean manufacturers, the (ommission ontraster) the General Electrie Company with contracts for all transformers, switchgear, ete, required in connection with the Morwell scheme. amounting in all to st. 50000000 .


Fig. 4. Fan on Armature and Magnetic Blowout in Brushholder for Prevention of Flash-over on 4500 kw ., 1500 -volt B.T.H. Synchronous Converter

In New South Wales, the State Government owns and operates all railways, steam and electric. The most important electric undertaking of the State is the power supply for the Sydney Tramways. The metropolitan population is 900,000 . The famed beauty of Sydney and its harbor is a measure of the precipitous grades and tortuous curves over which the tramways must operate. Two steam stations, one at Ultimo and a more modern station at White Bay, have a combined installed capacity of 50.000 kilowatts (2.5 eycles), which will be increased shortly by the addition of (two) $20.000-\mathrm{kw}$. turbine-generators ( 50 creles).

Figs. 5, 6, and 7 illustrate the White Bay station exterior, control room and switch gallery. This station, since its inception, has received much attention from Australian engineers and in many respects is regarded as a model.

The distribution system has reerently been improver he the adrlition of several antomatic substations.

A local pest that gave trouble in Sydney distribntion systems in the pest is the white ant. Is is well known, this insect lives on Wool amd shums the darlight, so that a wool pole mall berome a hollow shell and eollapse Withont wamangr. White ants will also attack


Fig. 5. White Bay Power House, New South Wales Government Tramways, with Venturi Type Smoke Stacks for Induced Draft
cables unless elaborate precantions are taken. Lead covering has no terrors for them, and the only effective protection appears to be that adopted in Sydney.

The lead corered cables are laid in troughing constructed of timber which has been vacuum dried and then impregnated moder pressure with arsenic.


Fig. 6. Control Room of the White Bay Power House

After the cables are laid, the troughing is filled with bitumen to which arsenic has been added.

There is no recorded case of cable breakdown caused by white ants where these precautions were taken.

The Public Works Department of the (iovernment is also interested in the greneration and distribution of electrie power, So far the larger power projects that have been planned by the department have not been carried out owing to consideration of finance.

Phere is every indieation, however, that the (Bovermment of New South Wales intends to take a very active part in the electrical development of the state. The Government has recently contracted to supply the Municipal Council of Sydney with the future requirements beyond the capacity of its existing station:


Fig. 7. Switch Gallery of the White Bay Power House. Cell doors are of wood and glass

## New Zealand Government, Public Works Department

This Government, like that of Tasmania, has shown great activity in developing the water-power with which Nature has lavishly endowed New Zealand. The first Government venture in this direction was commenced about ten ycars ago at Lake Coleridge in the South Island. This development of 12,000 kw. has been of great benefit to the territory served, which contains the rich pastoral lands known as the Canterbury Plains. The Government has made its electric service particularly attractive to the many dairy farms in the district, where agricultural labor is always scarce and expensive.

In consequence, the use of electric power is universal throughout these farms and hand milking is alnost unknown. The ability to flood all the out-buildings with light has eliminated much of the early morning discomfort of dairy farming.

In the South Iskand the transmission network voltage will probably remain at dif,000. This has been adopted at Lake Coleridge and also at the $14,000-\mathrm{kw}$. plant now being built at Lake Monowai in the extreme south.

Between these two plants lies the City of Dunedin’s development at Waipori Falls from which the city has enjoyed the benefits of hydro-electricity for many years.

It will probably be sometime in the future before the South Island systems are linked up into one system.

In the North Island (sce Fig. S) the most important development at present is that at Mangahao where a hydro-electric development of $24.000 \mathrm{~h} . \mathrm{p}$. is now in construction and will be in operation very soon. This will immediately supply Wellington, the capital city, and the surroming country. The next development will be at Arapuni Rapids where $96.000 \mathrm{~h} . \mathrm{p}$. will be developed to supply Auckland in the north. The third is at Lake Waikaremoana which will add $40.000 \mathrm{~h} . \mathrm{p}$. to the system. These lydro-electric plants when completed and connected together will enable the North Island to be covered with a reticulation of 110,000 -volt lines, 1100 miles in length.

## Conclusion

The foregoing remarks on Australasia's electrical development will serve to indicate that the utilization of the available resources has been by no means neglected. In accordance with the settled policy of these countries on the question of public ownership, prirate enterprise is not encouraged. On the utilization of electricity for large public works such as railway electrification, the various political bodies responsible, their technical advisers, and the general public are all well-informed-the public more so than in other countries. This may be due to the press, which wields tremendous ${ }^{\circ}$ power in the Antipodes. At least one Australian daily newspaper reserves space regularly for the treatment of engineering questions in a manner that appeals to the majority of readers and the articles printed are nearly: always illustrated.

For the same reason they are no more backward than the countries of the Northern Hemisphere in the domestic use of electric power.

The big field for development ties in mannfacturing industry the big pewer onnsumer in ally country The mainstaty of these southern comntries has been, and for some time to come will be, the proslucts of farm and mine; but it did not require the lessent


Fig. 8. Map of North Island, New Zealand, showing Trans. mission Network. Map prepared by Hydro-electric Branch of Public Works, New Zealand
of the War and its aftermath to teach them that no nation can maintain a high standard of living and survive without the magic aid of power applied freely to manufacturing processes, thus maintaining a balanced economic structure.

While this review of electrical development deals with the subject mainly from the engineering standpoint, mention must be made of the pioneer work done in Australia by the various associations of contractors and dealers. Many of these are actively engaged in valuable educational work which must have a profound effect on the rate of electrical progress.

# Some Fundamentals in Protecting Against Lightning 

By E. E. Burcier<br>Chenfal. Enghmeringi Laboratory, Generah, Electric Company

To give adequate protection against lightning an arrester must have certain fundamental qualities. To design a set of tests which will determine in what degree a given type of arrester possesses these essential qualities has taker years of study. The aththor discusses the fundamentals which should be considered in the commercial testing of lightning arresters. These conclusions were based on experiments made in the Gemeral Enginecring Laboratory in Febrnary, 1923.-EDitor.

Fors some time past the American Institute of Ekeetrical Engrineers has felt the need of revising its standards in regard to lightning arrester tests, so that definite recommendations could be made as to the tests required and the mamner of making them. It is also desirable that such tests represent service conditions as far as possible.
knowledge of lightning arrester performance has been increased, and it is hoped that in the near future a method of test will be devised whereby the true characteristics of lightning arresters can be determined before placing them in service. Many of the characteristics that a lightning arrester should have, and various de-


Fig. 1. (Left) 500-amp., 120,000-volt Discharge from Lightning Generator Between $6.25-\mathrm{cm}$. Spheres
Fig. 2. (Center) Aluminum-type Lightning Arrester and Insulator as Arranged for Test with Lightning Generacor
Fig. 3. (Right) Resistance-type Li bhtning Arrester Composed of Five Water Tubes and a Series Gap as Arranged for Test with the Generator

For many years Dr. C. P. Steinmetz has been making a study of lightning, and the transient phenomena which result from it on transmission and distribution circuits. Comparatively recently he has been able to design and build apparatus which is capable of reproducing the same effects as actual lightning. This apparatus was first described in the General Electric Review, November, 1921. With this apparatus our

[^55]scriptions of arresters and tests have been given in earlier issues of the General Electric Review.*

During the present year the American Institute of Electrical Engineers' Protective Device Sub-Committee on Lightning Arresters held their meeting at Schenectady, and in the General Engineering Laboratory of the General Electric Company witnessed a series of tests which demonstrated a few of the fundamental characteristics which should be considered in lightning protection. The tests that were made before this committee will now be described.

## Tests

The tests are divided into a number of groups, with each group demonstrating some particular fundamental.

Preliminary tests were made to show the observers that the discharge from the lightning generator had all the external characteristics of real lightning. Several short lengths of tree branch were split into pieces by the discharge, the same effect having often been observed after an electric storm when trees have been found split down the conter or the


Fig. 4. Diagram of Connections, showing Lightning Arrester and Insulator Connected in Discharge Circuit of Lightning Generator
bark stripped off by a lightning bolt. Then the bright flash and sharp report simulated in miniature real lightning when it discharges from cloud to ground at close range.

The first group of tests were made to show the power, energy and voltage of the testing circuit. A 15,000 -volt standard pin-type insulator was connected in the path of the discharge and the ease with which it arced over the edges showed that the voltage was sufficient for test purposes on apparatus haring insulation of equal strength. The energy of the impulse was demonstrated when a short length of 5 -ampere fuse wire was placed in the discharge circuit and, after several discharges, was heated just enough to separate the wire in one or two places. The current that is discharged in the above test has been measured at approximately 5000 amperes.

Thus the energy as measured hey the heat produced must be very small. This test atso shows that lightning arresters, which are protected in service against damage from low frequency discharges by series fuses, are capable of discharging a large amount of current for the duration of a lightning discharge without damaging or blowing the fuse.

The second group of tests were made to demonstrate the importance of the discharge rate in lightning arrester design. The discharge rate of a lightning arrester is briefly defined as the rate at which the released charge on the line due to lightning is dis-


Fig. 5. $125-\mathrm{kv}$. High-frequency Cscillator with Sphere-gap Voltmeter
charged to ground. This discharge rate is measured in amperes at some reference potential such as two times normal line potential. The tests were made to show that the higher the discharge rate of an arrester the better protection it gives, and also that this discharge rate is largely affected by the impedance of the discharge path. A 2300 -volt aluminum cell arrester having a high discharge rate was shown protecting a $15,000-$ rolt insulator which had been previously arced over. A power supply of $400 \mathrm{kr}-\mathrm{a}$. at 2300 rolts, 60 creles, was connected to the arrester and the insulator while the impulses or discharges were passing through the circuit. The insulator was protected without any signs of distress or interruption of the power supply. Next, an arrester composed of a water tube resistance and a horn gap in series was used
to replate the atumbimm arrester. 'This armester had a very bow discharge ralle and was (atoable of discharging approximately 17 amperes at the test voltage usod. Whern impulses were passed throtgh this circoit, the insulator areed over and short cirented the



Fig. 6. Diagram of Connections, showing Lightning Arrester Arranged to Protect Gap with Long and Short Connections


Fig. 7. Varnished Cambric Insulation Punctured by 0.75 -amp. Current from 200,000 -cycle Oscillator
supply was protected against damage by a fuse which quickly opened the circuit. The tests were then repeated using resistances which would give 2, 3 and 5 times the discharge rate or 34,51 and 85 amperes respectively. In each of these tests the arrester failed to protect the insulator.

To demonstrate further how resistance will affect the discharge rate of an arrester, tests
were mate to measure the voltage areross the ahminum cell arrester, first alone, and then with $2.5,50$ and 100 ohmes in series. The voltage of the arrester alone gave about 20.8 kiv, and the arrester and resistance in series gave 50,56 and 66 kv . respectively, showing that the discharge rate was deereased by the resistance and the additional voltage was due 10 the backing up of the discharge. From these tests it can be concluded that an arrester, which has high series internal resistance, must have a low discharge rate, or, in other words, have a low degree of protection.

The third group of tests were made to demonstrate how test results will differ with the method of test used. Voltage measurements were made on an aluminum arrester having a high discharge rate and the resistance arrester having a low discharge rate by two different methods of test. The first method, the same as used in some of the previous tests, was that of using a high voltage, steep wave front impulse of high current and high power for a short duration of time. The second method was to use a high voltage, high frequency oscillation of low current and low power for a comparatively long duration of time. The impulse generator and oscillator were set for the same test voltage, 85 kv . The impulse generator was capable of discharging 5000 amperes at this voltage and the $200,000-$ cycle oscillator about 0.75 amperes. The


Fig. 8. Varnished Cambric Insulation Punctured by 5000 -amp. Discharge from Lightning Generator
voltage values given below clearly show that in testing arresters care must be used in choosing a method of test so that true indications of protection will be given. $\begin{array}{ll}\text { Impulse } & \\ \text { Generator } & \text { Oscillator } \\ 20.8 \mathrm{kv} . & 10.4 \mathrm{kv} .\end{array}$ Aluminum Arrester. . . . . . . . . . . 20.8 kv . 10.4 kv . Resistance Arrester, greater than 70.0 kv . 26.4 kv .

The fourth group of tests were made to demonstrate the importance of installing
lightming arresters close to the apparatus to be protected. The almminum arrester was shown protecting a small air gap between spheres with the connecting wires between gap and arrester about two foet kong. The second test showed the same arrester failing to protect the same gap with fifteen or more fect of connecting wire between the arrester and the gap. When the gap) was increased to five times its initial value, the arrester protected it.

The last group of tests were made to demonstrate what different results might be expected on the breakdown of insulation when taken with non-oscillatory transients of steep wave front and transients of undamped oscillations. Several thicknesses of mica and
varnished cambric, 15 indres spuate were punctured by the discharge from the impulse generator which tore the insulation ats themgh some solid substance had beem shon thenoth it. There was no sign of homing due whe the discharge and the breakdown was instantaneous. The same thicknesses of insulation were then punctured using the high frequency oscillator at the same test voltare The voltage was applied for several minutes lefore breakdown occurred. Corona formed on the surface around the electrodes and the insulation became heated and carbonized before breakdown occurred. The breakdown formed a small carbonized hole in the insulation which later caught fire.

# The Solution of Electric Power Transmission Problems in the Laboratory by Miniature Circuits 

By O. R. Schurig<br>General Engineering Laboratory, General Electric Company


#### Abstract

In our June, 192.3, issue we published an article by F. W. Pcek, Jr., on "Applying the Results of High. voltage Research to Practice." Our present contribution shows how miniature circuits are employed to solve transmission problems. Long lines present special problems and the author shows how these are handled. He deals with "smooth" and "lumpy" miniature lines and with complete transmission system networks. He gives the procedure of solving a typical network problem.-Editor.


## Foreword

It is the object of this article to outline the established processes by which transmission circuits in operation, or to be constructed, may be reproduced on a small scale in the laboratory. Thus, theoretically calculated phenomena may be confirmed experimentally in a simple manner. Moreover, miniature systems afford a number of practical advantages in the experimental solution of specific circuit problems

## PROBLEMS ON LONG LINES

The most elementary conception of an electric circuit involves the assumption that all parts of the same conductor carry one and the same current at any one time. If the current be alternating and of constant effective value, it varies uniformly between definite constant limits in a continuously recurring cycle. Its variation is then a function of time, but at any one instant the

[^56]current is the same at all points of an insulated conductor. Should this conductor, however, be that of a long aerial high-voltage transmission line, several hundred miles long, the instantaneous currents measured at widely remote points of this line would no longer be the same, because of the capacity charging current required to charge the line; i.e., there is a continuous drain of current from the line, mile after mile. Furthermore, the time required for the current and potential to advance over a long line becomes an appreciable factor in the electrical behavior of the line. Consequently, on long lines, voltage and current vary not only with time but also with distance along the line. Both time and distance, then, determine the magnitudes and phases of current and voltage.

Ohm's law and Kirchhoff's law still hold. but must be applied to an infinitesimal length of line. This procedure results in differential equations-not of the simplest kind-for the solution of transmission-line behavior.* Thus, if it is desired to determine
the voltage and emorent in the steary state at the gencrator end of a long line for given values of vollate current and power-lactor at the recoiver end, the calculations maty be made ber the well-known hyperbolic formulas or be the exponential formmas. * The calculation of transicot phenomena, such as those caused by swatching oferations, lightning, areing gromols, ete., is more complicated than that of steaty-state phenomena. 'Thus, a demand was created for the experimental solution of long-line problems both of the transient and of the steardestate variety.
determined by the well-known formulas for resistance, inductance and capacity of aerial condmenors.

An cheotrically equivalent model of this line would therefore require for each hundred miles the following constants per conductor: resistance 16.3 ohms, inductive reactance (at (i0) cycles) si.3 ohms, cajacity 1.36 mierofarads. To be an exact replica of the $200-\mathrm{kr}$. line in question (to the extent of correctly representing the behavior of the full-size line at all frequencies for transient as well as stistained phenomena), the miniature line

TABLE 1

## LINE CONSTANTS, FOR 60-CYCLE, 200-KV., 3-PHASE AERIAL LINE OF 350,000 CIR.-MIL COPPER CABLES, EQUILATERAL SPACING 20 FT.

```
Resistance
Inductance
Inductive reactance (at \(60 \mathrm{cyc} . / \mathrm{sec}\).)
Capacity
Capacity susceptance
```

$r=0.163$ ohms per mile per conductor
$L=0.002237$ henry per mile per conductor
$2 \pi f L=0.843$ ohm per mile per conductor
$C=0.0136 \times 10^{-6}$ farad per mile per conductor to neutral
$2 \pi f C=5.13 \times 10^{-6}$ mhos per mile per conductor to neutral

The leakage conductance over insulators, etc., is negligible in comparison with the capacity susceptance and will therefore be considered equal to zero.

## MINIATURE REPRESENTATION OF LONG LINES

Since experiments on active, real lines are not often practical, and since it is generally desirable to determine the electrical behavior of a line before it is built, miniature laboratory models of full-size lines have come into existence. Their use is not new. They have aided materially in the acceptance by engineers of the theory of transmission-line calculations.

## "Smooth" Type of Miniature Line

Miniature laboratory transmission-line models-also called "artificial lines"-do not involve poles, towers, or cross-arms, but consist of mits of resistance, inductance, capacity, and leakance, designed so as to represent, in rue proportion, the constants of a full-size line. Let it be desired, for example, to reproduce in miniature a 60cycle, 200,000 -volt, 3 -phase line, having copper cables of $350,000 \mathrm{cir}$. mils cross section, with 20 ft . spacing between conductors arranged equilaterally. The constants of this line are given in Table I, as

[^57]must be of the "smooth" type, i.e., one having uniformly distributed resistance, reactance, and capacity. Such models have been built. One $\dagger$ consists of turns of wire in a single laver wound over glass tubes having a lining of metal foil fitted against the inner wall of the glass. $i$ nother type of smooth artificial line $\ddagger$ employs coils of several layers of uniformly wound wire; the uniformly distributed capacity is obtained by the use of metal foil wrapped over each layer of wire. A three-phase miniature circuit requires three similar elements, one for each phase, the metal foil terminals for the three elements being joined together to form the neutral of the three-phase system.

## "Lumpy" Types of Miniature Line

While the smooth type of miniature line is particularly suited for the experimental study of transient phenomena involving high frequencies well above 60 cycles per second, the special construction for strictly uniform distribution of line constants is not necessary for low-frequency problems; in other words, a simpler construction of miniature circuit elements, in the form of separate units of resistance, of reactance and of capacity, is permissible. This type of miniature line, called "lumpy," is more common than the smooth type. Lumpy artificial lines
may be made to represent one conductor to neutral, or all three pliases, of a threcphase line.

In the use of a lumpy artificial line caution must be exercised on account of the fact that such a line of fixed constants does not represent, at all frequencies, the true equiralent of one and the same full-size line. Two questions, therefore, arise: (1) how is the correct magnitude of the lumps to be determined at any one frequency, and (2) what is the proper manner of connecting the resistance, inductance and capacity mits of the miniature circuit?

The second question will be answered first: each phase, to neutral, may be represented either as in Fig. 1 (T-linc) ${ }^{\text {* }}$ or as in Fig. 2 ( $\pi$-line).* For a uniform transmission line, the elements of cither arrangement are symmetrical. A long line may be represented by a number of equal $T$ or $\pi$ sections with the resistance and inductance units connected


Fig. 1. Circuit Diagram of Miniature T-Line, representing One Phase (to Neutral) of a Three-phase Transmission Line
in series with $A B$, and with the free terminal of each capacity unit connected to a common "neutral" point. The various sections so joined together represent, then, equally long sections of the transmission line, and observations of coltage, current and power at the section junctions $A$ and $B$ of the miniature line indicate the correct behavior of the corresponding points of the full-size line. Observations taken at points other than the section junctions or terminals of the miniature line are not representative of actual-line conditions. The adrantage of employing sereral sections each equivalent to a short length of line are the following: (1) opportunity is offered for making observations at a number of equally spaced points throughout a long line; (2) practical equivalence of miniature and actual lines is obtained over a wider range of frequencies.

[^58]Lumpy Miniature Circuits at Different

## Frequencies

At low frequencies and for sections representing short lengths of line the magnitude of the lumps is obtained directly, without correction, from the constants of the full-size line. Thus, the 60 -cyele, $200,0(0)$-volt line considered in Table İ, may be reproduced in 10 -mile $\pi$-sections derived as in Table II

If, however, the equivalent length of a section is increased, or if the frequency is materially raised, the lumpy-line constants must no longer be made exactly proportional


Fig. 2. Circuit Diagram of Miniature $\pi$-line, representing One Phase (to Neutral) of a Three-phase Transmission Line
to the smooth-line constants, but must be obtained as follows, in the case of a $\pi$-line, (see Fig. 2) :

$$
\begin{gather*}
Z_{2}=l z\left[\frac{\sinh \theta}{\theta}\right]=l z k_{l}  \tag{1}\\
Y_{2}=\frac{l y}{2}\left[\frac{\tanh \left(\frac{\theta}{2}\right)}{\left(\frac{\theta}{2}\right)}\right]=\frac{l y}{2} k_{c} \tag{2}
\end{gather*}
$$

The symbols are defined_as follows:
(1) actual-line data:
$l=$ length of section in miles.
$z=r+j \omega L=$ line impedance, ohms per
mile per conductor.
$y^{\prime}=g+j \omega C=$ admittance. mhos per mile
per conductor to neutral.
$\theta=l \sqrt{z y}=$ total hyperbolic line angle per
conductor, for section $l$ miles long.
$\omega=\underline{\bullet} \pi f$.
$f=$ frequency, cycles per second.
$j=\sqrt{-1}$.
(2) ( 2 (quivakent $\pi$-line data, representing a scotion $l$ miles long:
 chement (sec ligk. : $)$ ).
$)_{n}=i_{2}+i \omega x_{2}$ mhos admittance of each capracit! clemest of $\pi$ line.
( $2=$ malos leakage eonductance associater with each caparity element; when $g$. the leakare conductance per condmetor to neutral for the actual line, is of negligibly small magniturle (as in the case of well insulated lines in clyy weather), (in atso is small in comparison with the capacity susceptance $j \omega \mathrm{Cu}$.
$k_{i}$ and $k_{i}$ are the equivalent $\pi$-line correction factors,* shown by the square brackets of equations (1) and (2), respectively; $k_{l}$ may be called the line-clement correction factor and $k_{c}$ the condenser-element correction factor, for an equivalent $\pi$ circuit.

$$
\begin{aligned}
& \theta=l,^{\prime} z y^{\prime}= \\
& 20\left(0, ~ 0.5 .59699^{\circ} 1 \times .5: 3 \times 10^{6} / 900^{2}\right. \\
& =0.420 / 4.6 \\
& Z_{2}=\operatorname{lz} \frac{\sinh \theta}{\theta}= \\
& 200 \times 0.5 .59890^{\circ} 1 \times \frac{\sinh 0.120 / 81 .{ }^{\circ} 6}{0.120 / 51 .{ }^{\circ} 6} \\
& =167.0 / 79.901 \mathrm{~ms} \\
& \text { or } \\
& Z_{2}=30.15+j 164.1 \text { ohms. } \\
& \text { Similarly, from equation (2) } \\
& y_{2}=\frac{l y}{2} \cdot \frac{\tanh \left(\frac{\theta}{2}\right)}{\left(\frac{\theta}{2}\right)} \\
& =\frac{.200 \times 5.13 \times 10^{-6} / 90^{\circ} \tanh 0.210 / 84.6^{\circ}}{9} \\
& =521 \times 10^{-6} / 899^{\circ} 8 \mathrm{mhos} .
\end{aligned}
$$

TABLE II
 Length

Resistance
Inductance
Capacity to neutral
1.63 ohms
0.0224 henry
$0.136 \times 10^{-6}$ farad

## Example of Miniature Line Equivalent to a

## Power Line

For the $200-\mathrm{kr}$. line considered in Tables I and II, a strictly equivalent miniature $\pi$-section representing 200 miles of line, for steady-state conditions, is determined as follors from the line data of Table I (leakage conductance is neglected):

Two cases are considered: (1) for the fundamental frequency ( 60 cycles per second) and ( -2$)$ for the third-harmonic frequency (1s0 cyeles per second).

Case 1. $f=60$ cycles per second
$l=200$ miles.
$z=r+j \omega L=0.163+j 0.843=0.859 \quad 79 .^{\circ} 1$
ohms per mile.
$y=g+j \omega C=o+j 5.13 \times 10^{-6}=$
.). $13 \times 10^{-6} / 90^{\circ}$ mhos per mile.

[^59]Equivalent "Lumped" Constants of Miniature $\pi$ - -in , 10 -mile Section, for 60 Cycles. The Symbols Refer to Fig. 2
$R_{2}=163$ ohms
$L_{2}=0.022+$ henry
$C_{2}=0.068 \times 10^{-6}$ farad for each capacity element

Or

$$
\mathrm{I}_{2}=(1 . \mathrm{s}+j .521) \times 10^{-6} \mathrm{mhos}
$$

Case ‥ $f=180$ cycles per second.
$l=200$ miles.
$z=0.16: 3+j 2.529=2.53 .3 / 86^{\circ}$ ohms per mile.
$y=o+j 15.39 \times 10^{-6}=1.5 .39 \times 10^{-6} 90^{2}$ mhos per mile.

$$
\theta=200,2.533 \times 80^{\circ} \times 15.39 \times 10^{-6} 90^{2}
$$

$=1.25 \mathrm{Ss}^{\circ}$
$Z_{2}=200 \times 2.533 / 86^{\circ} \frac{\sinh 1.2 .5 / 85^{\circ}}{1.2 .5 / 88^{\circ}}$
$=506.6^{\circ} 86^{\circ} \times 0.760 / 1 .^{\circ} 2=38.5 \cdot / 87^{\circ} 2$ ohms
or

$$
Z_{2}=1 ৯ .9+j 384 . \mathrm{ohms}
$$

and

$$
\begin{aligned}
Y_{2} & =\frac{200 \times 15.39 \times 10^{-6} 90^{\circ}}{2} \frac{\tanh 0.62 .5 / 88^{\circ}}{0.62 .5 / 88^{\circ}} \\
& =1539 \times 10^{-6} / 90 \times 1.15 .5 \cdot \frac{0.6}{0.6} \\
& =1778 \times 10^{-6} \angle 89 .^{\circ} 4 \\
& =(19+j 177 S) \times 10^{-6} \text { mhos. }
\end{aligned}
$$

The results of the two cases may be summarized as follows in Table III:

In order, then, to represent correctly (as to terminal conditions) the given $200-\mathrm{kv}$. actual line of 200 miles, for its 60 -cycle steady-state behavior, the equivalent one-section $\pi$-line must have the constants indicated in the 60 -cycle column of Table III. In order, however, to represent the identical full-size line, for its 180 -cycle steady-state behavior, the $\pi$-line constants in the last column of Table III must be employed. It is seen that the values of resistance, reactance, and
electric power systems, however, generally have a network of lines. Thus, a great many of their problems involve simultanerns consideration of the transmission network torgether with the station apparatus, and require for experimental solution in the laboratory a miniature transmission network with miniature station apparatus. This kind of miniature system may have either fixed circuit constants and fixed system connections -for representation of one system only*or it may have adjustable circuit constants and variable system connections. The "Short-

TABLE III
COMPARISON OF SMOOTH-LINE AND EQUIVALENT $\pi$-LINE CONSTANTS FOR 60-CYCLE AND FOR 180-CYCLE FREQUENCIES


* Values per conductor to neutral.
$\dagger$ Half the total capacity is used here because the value of $Y_{2}=\frac{l y}{2} k_{c}$ from equation (2) reduces to $\frac{l y}{2}$ when $k_{c}=1$.
$\ddagger$ Leakage conductance associated with capacity.
capacity for an equivalent lumpy line differ appreciably from the nominal values for the uniformly distributed (or "smooth") type of line, under the conditions chosen in the abore example. The difference between nominal and equivalent values is seen to be small at 60 crcles, but is considerable at 180 cycles.


## MINIATURE REPRESENTATION OF COMPLETE TRANSMISSION SYSTEM NETWORKS

The trpe of miniature circuit discussed in the foregoing is used primarily for the solution of long-line problems and for confirming the theory of such lines. Large modern

[^60]circuit Calculating Table" $\dagger$ is of the latter type. Though based on an approximation, it serves for the quick experimental solution of a wide variety of short-circuit problems, but is limited to the determination of threephase short-circuit currents.

The experimental solution of nnt1nerous problems pertaining to singie-phase short circuits and to normal current flow (due to loads) in complex networks calls for a polyphase miniature system. A system of this kind is available in the General Engineering Laboratory at Schenectady. It inchudes synchronous machines and transformers for two generating stations (or substations), adjustable line units of resistance, inductance and capacity for eight three-phase lines (with loads), and switching arrangements for making any desired circuit connections. The switchboard for the entire miniature system and the table for measuring


Fig. 3. Miniature Electric Power Transmission System. View of Switchboard and Instrument Table
instruments are pictured in Fig. 3. The current rating of the equipment is from $\overline{5}$ to 20 amperes, thus permitting the use of standard portable meters. A full description of this miniature system, together with a discussion of some of the problems for which it is suited, is given in a paper prepared for the June, 1923, Convention of the A.I.E.E.


Fig. 4. One-line Diagram of Three-phase System with Full-size Circuit Data

## PROCEDURE IN SOLVING A TYPICAL NETWORK PROBLEM

In the following example the problem of determination of normal current flow (due to loads) in a network will be considered. The object of this example is to show how the full-size circuit is converted into its equivalent miniature circuit for experimental solution.

A one-line diagram of the three-phase circuit to be represented in miniature is that of Fig. 4. Since the circuit constants and the loads in this 3 -phase, ( 00 -cycle system are balanced, it may be reproduced in miniature as a one-conductor circuit to neutral. Moreover, the series-connected circuit elements may be joined together into a single-circuit element, by the addition of impedances; and finally, all of the circuit constants are expressed in terms of one common reference $\mathrm{kv}-\mathrm{a}$. and voltage. After these transforma-


Fig. 5. One-line Diagrammatic Representation of Circuit of Fig. 4 for Calculation of Current Division
tions have been made, the circuit of Fig. 5 is obtained. The corresponding full-size circuit data are those of Table IV, column 2. The value of $z_{0}$, for example, is obtained as follows: From Fig. 4, $z_{0}$ represents the sum of two 10 per cent reactances (at $62,500 \mathrm{kv}-\mathrm{a}$. base). From the formula
Per cent reactance $=$

$$
\frac{(\text { ohms reactance }) \times(3 \phi \mathrm{kv}-\mathrm{a} . \text { basis })}{10(\mathrm{kv} . \text { reference line voltage })^{2}}
$$

the value of $z_{0}$ in ohms then is

$$
z_{0}=\frac{10 \times 20 \times 27.6^{2}}{62,500}=2.44 \mathrm{ohms}
$$

Since the cable lengths are not over 5 miles, capacity charging currents may be neglected. The full-size circuit load data appear in the lower part of column 2 in Table IV. For the
single-conductor-to-neutral miniature representation of this system, convenient miniature values are:

200 volts line-to-neutral voltage.
7.0 amperes line current corresponding to 130.3 full-size line current.
$4.2 \mathrm{kr}-\mathrm{a}$ equivalent 3 -phase minature kv-a. corresponding to 62,500 full-size system kv-a.
The determination of the minature system impedance values will be illustrated in the

Obrionsty, the reciproxal values of the above factors serve for the combersom of the minature test data to the ororespondings actual system datat. Witle the miniature circuit comnerted as in Figr, is and arljusted for the circuit constants of 'lable $\mathbb{N}$ ', collumn 3, the preparations are complete for test readings of any desired mononwn currents, such as $I_{G 1}, I_{A}, I_{B}, I_{0}$ and $I_{1}$. With the atel of voltage and watt readings the relative current phases are easily determinerl.

TABLE IV
FULL-SIZE AND MINIATURE LINE DATA FOR CIRCUIT OF FIG. 4, REPRESENTED DIAGRAMMATICALLY IN FIG. 5

| 1 | Full-size Circuit $\stackrel{2}{D^{2}}$ ata at 27.600 Volts Reference Line Voltage | Equivalent Miniature Circuit Data at 346.4 Volts Reference Line Voltage |
| :---: | :---: | :---: |
| $\begin{aligned} & \left.z_{0} \text { (reactance only }\right) \\ & R_{A^{*}}^{*} \\ & X_{1}^{* *} \\ & z_{1} \text { (reactance only } \end{aligned}$ | 2.44 ohms <br> 1.66 ohms 7.20 ohms 15.28 ohms | 5.72 ohms <br> 3.87 ohms <br> 16.8 ohms <br> 35.6 ohms |
| Line Current for 62.500 Kv -a. | 130.) Amp. | 7.0 Amp. |
| Load at $I_{L 1}$ Current $I_{L 1}{ }^{+}$ Load at $I_{12}$. Current $I_{12}^{\dagger}+$ <br> Load at $I_{P 3}$ Current $I_{l, 3} \ddagger$ Load at $I_{1 / 4}$ Current $I_{/ 4}+$ | $32.100 \mathrm{kv}-\mathrm{a}, 0.7 \mathrm{p}-\mathrm{f} . \dagger$ 670 amp . <br> $50,000 \mathrm{kv}-\mathrm{a}, 0.90 \mathrm{p}-\mathrm{f} . \dagger$ 1045 amp . <br> $8,050 \mathrm{kv}-\mathrm{a}, 0.76 \mathrm{p}-\mathrm{f} . \dagger$ 168 amp . <br> $10,000 \mathrm{kv}-\mathrm{a} ., 0.95 \mathrm{p}-\mathrm{f} . \dagger$ 209 amp . | 3.6 amp <br> . .6 amp . <br> 0.90 amp. <br> 1.12 amp. |
| Current at $I_{G 2} \ddagger$ | $840 \mathrm{amp} .0 .80 \mathrm{p}-\mathrm{f} . \ddagger$ | 4.50 amp. |

[^61]case of $z_{0}$. Since the per cent drop through $z_{0}$ must be 20 per cent for both miniature and actual systems, the equivalent miniature value of $z_{0}$ is found as follows:
Miniature $z_{0}=\frac{10 \times 20 \times(0.2 \sqrt{ } 3)^{2}}{4.2}=5.72$ ohms. Thus the reduction factors from actual circuit to equivalent miniature circuit data are:

Factors based on $2 \overline{2}, 600$ volts reference line voltage. Multiply full-size system values by these factors to get miniature-system ralues.

| Yolts | $\frac{1}{79.7}$ |
| :--- | :---: |
| Amperes | $\frac{1}{186.5}$ |
| Ohms | 2.34 |

## Solution by Calculation

The equations for the mathematical calculation of load-current flow in the network of Fig. . will be presented in the following to show the procedure in this (relatively simple) case. From this figure, the equations of the circuit are:

$$
\begin{align*}
& I_{A}+I_{0}+I_{L 1}=I_{L 1}+I_{L 2}+I_{L 3}+I_{L 4}-I_{G 2}  \tag{3}\\
& I_{A} z_{A}+I_{1} z_{1}=I_{0} z_{0}+I_{B} z_{B}  \tag{4}\\
& I_{A}+I_{B}=I_{L 3}+I_{L 4}  \tag{.5}\\
& I_{B}+I_{1}=I_{L 4} \tag{6}
\end{align*}
$$

From these equations the currents $I_{A}, I_{B}$, $I_{0}, \quad I_{1}$ may be solved if the impedances $z_{A}, z_{B}, \quad z_{0}, \quad z_{1}$, the load currents $I_{L 1}, I_{L 2}$, $\tilde{I}_{L 3}, I_{L \mathrm{k}}$, and generator current $I_{G_{2}}$ are given.

From（i）

$$
\begin{equation*}
I_{I}=I_{14}-I_{1} \tag{T}
\end{equation*}
$$

$$
\begin{gathered}
\text { From (i) and (.i) } \\
I_{.1}=I_{l .3}+I_{1}
\end{gathered}
$$

## Advantages of Experimental Solution

＇The aldeantages of the experimental solu－ ton are the following：
（1）Lesis time is consumed in olstaining answors
（2）The results are casily checked by rearlings of instruments．
（3）Vroblems may le solved for which （ablenlations are not practical．
（1）A varicty of circuit conditions may be solved with one experimental set－up）．

The last－mentioned factor is of great importance for a miniature system with adjustable circuit constants．In dealing，for instance，with a problem of normal－current division in a system，successive solutions for a variety of load conditions may quickly be obtained experimentally by adjustments of a rheostat or of a reactor，while solution by calculation requires computing，with new values for each load condition，the entire set of vector equations，or practically repeating the complete graphical solution．

In the solution of short－circuit－current problems，the advantages of the experimental procedure are even more pronounced，when the current flow for a variety of short－circuit locations in a network is to be determined． The reason will be seen when it is considered that each location of short circuit requires a new set of simultaneous equations for the mathematical solution．

# Record Breaking Current Collection Tests at Erie 

By W. D. Bearce<br>

The casual observer of our ordinary street trolley car seldom stops to think it is truly womberfal that sufficient current can be collected be a whe rolling on a wire. How much contact surface is theret Whan would design a switel with the same limited surface contact? To collect current for such service as the lowe
 high as from $\mathbf{D O O O}$ to 6000 amperes has recontly been demonstrated in a series of remarkable tests carifed out at the Erje Works of the General Electric Company. The author describes these tests and the werbead construction and equipment used. Dompor.

A series of current collection tests was made before a group of prominent railroad men and engineers at Erie during the week of July 16. These tests were particularly important because of the remarkable case with which currents of from . 5000 to 6000 amperes were collected at speeds approximating ( 60 miles per hour with a complete absence of sparking. The occasion of this public exhibition was the demonstration, under actual
and .000 kw. for a 3000 -ton train hatuled be two units $u_{p}$ a 2 per cent grade. The current for these locomotives is obtained at different points through a collector on each engine, and is in any case less than one-third the amonnt collected during the Erie tests. Heary freight service at low speeds is being planned on the Tirginian Railway, consisting of 8000 -tom trains up a 2.2 per cent grade. This service would require approximately $10,000 \mathrm{kw}$.


Fig. 1. The Test Train Consisting of a Locomotive, a Gondola Carrying a Second Pantograph and Loading Rheostats, and an Observation Coach
operating conditions, of the collection of heary currents from a single pantograph, if desired, at practically any operating speed. It was remarked during this demonstration that the amount of current collected from a single pantograph is far bevond the requirements of any single-minit electric locomotive for many years to come.

It is interesting to note that .5000 amperes represents 7.500 kw at 1.500 volts or $1.5,000 \mathrm{kw}$. at 3000 volts. Heary freight locomotive service. such as is handled by the C., MI. \& St. P. Railway requires a maximum of between 4000
and would employ two or probably four collectors.

It is further of interest to make a comparison between the amount of energy collected from this type of orerhead line construction with the well known trolley wheel collector as used in the heavier interurban service. With this latter equipment, the current ranges from about sol amperes during acceleration down to 300 to 500 amperes at rumning speeds.

For successful current collection it is essential that the contacts between the work-
ing combluctor and the colleotor be maintamed. Smy irrogularity in the comtand that maty
 at the combate is a mone sroater fater in the deterioration of the contate wire and collewtor thats the meehanical wear due 10 the shiding friction. The topx of ofertuad comstruction deroloped at Erie is desigued to comply with


Fig. 2. Connection Diagram showing the Wiring of the Locomotive and Gondola
these essential characteristics and has demonstrated the possibility of collecting an amount of current far in excess of that necessary to handle the heaviest trains.

It should be noted that in all of these tests. the type of pantograph used is a duplicate of that now in operation on the C., M. \& St. P. locomotives. The improvement in the capacity of the collecting equipment is due to the flexible type of overhead construction developed by General Electric engineers at the time the initial 3000 -volt equipment was installed on the C., M. \& St. P. Railway and consisting of loop hangers with a twin trolley supported from alternate points. This design is unusually flexible and represents a vast improvement over anything previously used.

In order to demonstrate to interested visitors the remarkable qualities of this type
of construction, a series of tests wats marle using a special train, wheld is deseribed hereafter. ley means of which the amount of curfent fowing from the toolley wire the the loenmotive could be regulated form the engine (ath) The tests were run on three consecutive days, and the program was pratedically identical during eath of these exhibitions. After prominary inspection during the afternoon, the heary current collection tests were started each day at about $5: 00 \mathrm{p} . \mathrm{m}$. The first test consisted of a run made at 4000 amperes and 1.000 volts, reaching speeds of from i0 to (if) miles per hour with one pantograph. A second run was made under the same conditions after the visitors hard been distributed to the several observation towers along the track. The second test was made a! the same current but at reduced voltage to afford a comparison between operation at 1500 and s.00 volts. This test was also repeated for the benefit of observers located along the track. On account of the limited capacity of the power station. the higher current tests were all made at 8,50 volts.

The third test was made at 5000 amperes 8.50 volts running at about 30 miles per hour with two pantographs. The object of this test was to show successful operation at moderate speeds. The final test on the regular program was made at 5000 amperes 8.50 volts at speeds between 50 and 60 miles per hour using two pantographs. This was repeated a sufficient number of times to allow observers located on the several towers to witness operation both from the train and from any one of the towers. At the request of some of the visiting engineers an extra run was made at 5000 amperes 850 volts high speed using only one pantograph. The actual speed obtained during this run was. 58 miles per hour while drawing a current of 5400 amperes.

In all of these tests visitors noted a complete absence of sparking at the pantograph and no difference whatever could be observed between operation at 1,500 and 8.50 volts. The tests indicate that the amount of current which can be collected is practically independent of the trolley voltage when contact is maintained between the collector and the working conductor. A further special test was made at the request of some of the visiting railroad men to show the effect of lowering the pantograph under load with the train at standstill. This test was performed directly in front of the substation and the standard relay protection interrupted the $5000-\mathrm{amp}$. $850-$ volt load before the pantograph could leave
the wire．A second test was made with the relay discomected and the are formed was quickly extinguished as the collector dropped from the wire．At this time it was explained that in case of a reduction in the air pressure． which holds the pantograph against the wire． protection to the locomotive is afforded by a relay which opens the lime switches thus eliminating the possibility of arcing from this cause．

## Sieel Structures

The steel supporting structures begin about 600 ft ．west of the substation with latticed column bridges extending up to bridge へo． 13 ． Bridges No． 14 to 1 in inclusive are Bethlehem column bridges．The structures from No． 19 to 23 are latticed chamel bracket poles；from

Working Conductor
 to 3.4 ，the working comductors andencts of two No． 0000 erooved hard－drawn copper wites hanging side be side．From brideres No 16 to 21 two No．000000 copper wires are used．

## Type of Suspension

Droppers from the primary messenger sup－ port the secondary messenger at points 1.5 it ． apart．The working conductors are supported from the secondary messenger by clips spaced 1.5 ft ．apart on each wire．

## Observation Towers

To witness current collection tests conven－ iently，observation towers had been erected to a height of approximately the top of the

Fig．3．A Close－up View of the Trolley Wire Suspension Used in the Tests

No． $2 t$ to 28 inclusive， $10-\mathrm{in}$ ．Bethlehem bracket poles：from No． 29 to 33 inclusive． 9 －in．Bethlehem bracket poles．Bridge No．3t is of the latticed column type used for an anchor．The steel structures are spaced 300 ft ． throughout．All of the steel structural work was supplied by the Archbo！d Brady Co．， Syracuse．N．I．

## Primary Messenger

The primary messenger consists of a $5 / 6 \mathrm{in}$ ． i－strand high－strength steel cable，from structure No． 1 to 34 ．

## Secondary Messenger

The secondary messenger is a 1.000 .000 circular mil stranded copper cable between bridges $\times 10.1$ and 15 ．and a 750,000 circular mil stranded copper cable from bridges No．1．5 io 34.
pantograph．Tower No． 1 is located between bridges No． 9 and 10 on the center of a reverse curve so that current collection can be observed on the curves approaching and leaving as well as on the connecting tangent． Tower No． 2 is located between bridges No． $1 t$ and 1.5 on tangent level track．Towers No． 3. 4．and ．）are located farther east at intervals of about 1200 ft ．

## Substation

The substation in building No． 60 contains two synchronous moto：－gererator sets with switching equipment suitable for connecting these units to supply any trolley potential from 600 to 3000 volts．One of these sets has a rated capacity of 1000 kw ．and consists of two $500-\mathrm{kw}$ ． 1.5003000 －rolt generators direct connected to a symchronous motor．The second unit is of simila：construction but with


Fig. 4. The Overhead Trolley Suspended from Latticed Side Bracket Poles


Fig. 6. A Tangent Section of the Tracks on whic. 1 the Tests were Run


Fig. 5. The Overhead Suspension on a Curve in Front of the Substation


Fig. 7. One of the Several Cbservation Towers from which the Action of the Suspension was Conveniently Viewed
two $750-\mathrm{kw}$ : generators. Full capacity can be obtained with both series and parallel connections, and lower voltages can be obtained by adjusting the rheostats in the generator fields. Both of these sets are designed to operate at three times normal load for short periods, and a total of 6000 kw . can be obtained, the limit of the power supply: All generators are protected by high-speed circuit breakers and the switching equipment and the meters and voltage control are especially arranged to facilitate testing.

The substation is located approximately nine-tenths of a mile from the west end of the track. Building No. 60 also serves the purpose of a shop and contains four tracks for the entire length. Pits underneath these tracks facilitate inspection and repairs to equipment.

## Locomotive Scales

On one of these tracks there is also an elaborate weighing equipment* for determining the weight per axle of locomotives under test. There are a total of cight scales which can be moved to accommodate different wheel spacing so that simultaneous weights can be taken on all of the axles of a locomotive. Each scale has a capacity of $80,000 \mathrm{lb}$. and the entire set occupies a pit 78 ft . long. By means of air pressure the entire locomotive can be lifted at once or any axle separately. The distance which the wheels are lifted to bring the weight onto the scale is about $3 / 4 \mathrm{in}$.

## Test Train

For the current collection tests, a special train had been prepared consisting of a 110-ton gearless locomotive arranged for operation on $750 / 1.500$ volts followed by a gondola furnished by the New York Central R. R. in which were installed sufficient iron grid rheostats to obtain necessary current for the special tests. By means of remote controlled contactors, sections of these grids could be inserted or removed so as to draw whatever current might be called for under each particular test. Behind the gondola was an observation car also furnished by the New York Central R. R. Co. in which were fitted up instruments for indicating the amount of current being collected and the speed at which

[^62]the train was raming. The lecomotive is equipped with four bipolar motors with pony guiding axkes at the from and reat of each two-axle driving truck. On acoome of the short length of the calb, the second pantograph was mounted on the gondola to simulate operating conditions. The normal pressure of the pantograph against the e prolley wire was between 30 and 8.9 lb .

Among the visitors who witnessed these tests were consulting engineers from the various parts of the comontry and representatives from many steam railroads. The following railroads were represented:

Ashtabula Rapid Transit Co.<br>Baltimore \& Ohio R. R.<br>Boston \& Maine R. R.<br>B., A. \& R. P. R.<br>Buffalo \& Lake Erie Traction Co.<br>Canadian National Rys.<br>Chesapeake \& Ohio Ry.<br>Chicago Surface Lines<br>Cleveland Union Terminals Co.<br>Delaware \& Hudson R. R.<br>Delaware, Lackawanna \& Western R. R. Interborough Rapid Transit Co.<br>Illinois Central R. R.<br>Lehigh Valley R. R.<br>Long Island R. R.<br>Michigan Central R. R.<br>New York Central R. R.<br>New York, New Haven \& Hartford R. K.<br>Norfolk \& Western Ry.<br>Pennsylvania R. R.<br>Southern Pacific Co.<br>Third Ave. Railway<br>United Rys. \& Electric Co.. Baltimore<br>Virginian Railway:

The following consulting engineering firms were also represented:

Murray \& Flood, N. Y.
Sterens \& Wood Co., N. Y.
Stone \& Webster. Boston
Archbold Brady, Syracuse
W. D. Spengler, Inc., Cleveland

Jackson \& Moreland, Boston
Sargent \& Lundy, Chicago
IIcClellan \& Junkersfeld, N. Y. Gibbs \& Hill, N. Y.
Other companies represented ineluded:
The R. D. Nuttall Co., Pittsburgh The Ohio Brass Co., Mansfield, Ohio Shields Electric Co., N. Y. American Locomotive Co., Schenectady Bridgeport Brass Co., Bridgeport, Conn. Erie Lighting Co., Erie. Pa.
Dept. of Street Railways, Ashtabula The Board of Estimate, Xew Fork City McGraw-Hill Con, New York City

# Studies in the Projection of Light 

PART VI

# THE PARABOLIC MIRROR AND DISK SOURCE OF LIGHT 

By Frank Blanford<br>


#### Abstract

larts III and IV of this series analyzed the projection characteristics of a parabolic mirror with a spherical source of light, in which latter classification fall the usual bunched types of concentrated incandeseent lamp filament. The present article deals similarly with the combination of a parabolie mirror and disk source of light, which latter is regarded as a direct andytical substitute for the plain carbon are and for the special concentrated incandescent lamp filament the members of which are all mounted in one plane. The formulas and curves furnish a convenient and accurate means of determining the increase of central intensity with distance, the inverse-square region, the testing distance for central intensity, the width of crest of beam, and the width of beam. The treatment of the parabolic mirror with a high-intensity are as source of light is reserved for a later article.-Emitor.


## THE DISK AS A SUBSTITUTE FOR THE CRATER OF THE ARC

The crater which is the source of light in all of the more common ares usually has a depth from one-quarter to one-half its diameter; but, providing the crater is luminous from edge to edge, we are in no wise interested in the depth because the crater is the exaet optical equivalent of a flat surface or disk of equal brightness and diameter. The disk thus becomes an idealized source that is in many eases a very close optical counterpart to the actual crater and has the great virtue of being simple to visualize and to treat in a mathematical manner.

It is one of the commonplaces of popular science that carbon when used as a positive electrode comes to a fixed and invariable brilliancy of some $\$ 4,000$ candles per square inch of crater surface. The general acceptance of this figure as the ultimate in brilliancy of a solid body, such as an electrode, had the effect of stopping for many years the development of the newer types of are now coming into general use, and, strangely enough, it acted to prevent the complete development of the pure carbon are itself. Carbon comes to its greatest brilliancy at 3800 deg. A, but the attainment of this temperature depends upon current density, electrode resistance, and the diameter of the electrode; so that we may. and often do, have what seems to be a normal crater without attaining the best results. A classical example of this was the 200 -amp. arc (now happily defunct) that gave only one-quarter the theoretical brilliancy and failed to function properly in other ways. One characteristic of this carbon was the formation of an extremely deep crater. The active area of are contact would center on the core of the electrode
and give its best brilliancy (perhaps 30,000 ed. per sq. in.) for a few seconds, then the are would become conical and hollow, and make contact around the rim of the crater with a brillianey of half the best value. This are is mentioned, not because it is of direct practical interest, but because these characteristics are present to some degree in every pure carbon arc. Thus, instead of the carbon crater being of uniform brilliancy from edge to edge, there is always a tendency for either the core or the rim to average a little brighter than the remainder, and we must thus distinguish between the different parts of the crater.

Therc is some cvidence that in a plain carbon electrode of good design the central brillianey exceeds slightly the limits set by the boiling point of carbon. Two possibilities here suggest themselves. One is the reflection trom wall to wall of the crater, thus adding to the radiation brilliancy. It is hardly likely that much could be gained in this way if carbon retains its normal reflection properties at high temperature. The other possibility is that the gas in the crater becomes superheated and being transparent adds its own brillianey without interfering with the radiation of light from the erater walls. Regardless of the accuracy of this explanation it is a fact that has been noted many times that the center of the projected beam is appreciably stronger than points nearby, whereas the theory of a uniform crater calls for a certain region in the center of the beam where the beam strength is uniform. These variations from absolute uniformity are important to remember in the present discussion of the disk source because while there is a general agreement between theory and test results, there are
some diserepancies that can hardly be overlooked or ignored. But when these differences are eonsidered from all points of view and one set of ohservations are brought into concordance with the general theory, the other test data usually fall directly into line and the geometrical theory here outlined seems to be entirely adequate.

The so-called "high-intensity" or graseous are is not only some six times more brilliant than the pure carbon are, but it has an entirely different crater brilliancy characteristic. In this are, the main source of light is the heated gas given off by the core and the brilliancy from any angle of riow is influenced by the depth of gas as measured in that direction. The edge intensity is only one-sixth the central intensity for here the gas depth is small and the carbon surface is the main source of light.

The pure carbon arc has a crater brilliancy greatly in excess of the brilliancy of the outside walls of the crater, and as a result the beam is fairly sharply and definitely outlined, but the carbon walls of the high-intensity crater are almost as brilliant outside as inside and the beam boundaries are correspondingly hazy. Not only is there thus a lack of a definite boundary at the crater rim, but the luminous gas from the


Fig. 47. A Monoplane Fitament used for Projection by Condensers in the Motion-picture Industry but Adaptable for Projection by a Mirror
crater spills over the sides and further obliterates any trace of a sharp edge to the light source. These features would seem to make it impracticable to attempt to formulate some simplified substitute for the high-intensity crater such as the uniform
disk for the carton are and the splumical source used in place of the concentrated incandescent filament.

An extension of the theory of the disk luminous on one side only to a disk luminous on both sides will bring many of the high-


Fig. 48. A Monoplane Filament Particularly Designed for Projection Purposes. The coils being in multiple can be spaced very close together as the potential difference between adjacent coils is practically zero
current incandescent filaments of the monoplane type, Figs. 47 and 48 , under the same general theory of the disk.

It will be shown later that the p.ain carbon crater may be considered as the general case, and by suitable changes the theory may be extended to the high-intensity arc through the medium of graphical methods. For the present, we can summarize the use of the disk source as a substitute by saying that it is physically a good substitute for the pure carbon arc and for the monoplane incandescent filament; but the high-intensity crater must be treated as a special case whic'1 is best handled by applying graphical methods and it seems wise to reserve the high-intensity arc for a separate installment of this series of articles.

The geometrical analysis is always confined to a meridian plane, and if we are considering an incandescent filament, which ordinarily has a rectangular form, the analysis can be carried out in a number of planes, say the two axes of the figure and one diagonal. If it is desired to investigate mathematically the working conditions of a given test, the least farorable condition can usually be discovered and used as a criterion for the entire test

Increase of Central Intensity with Distance

 the latler foresturters when vewod form at point unt omt the axis and lowommes clliplical in whline ( alling the matum ands 1 and


Fig. 49. Diagram lllustrating how the Rays from the r edge of the Crater Cross the Axis, providing they are reffected from a point on the mirror back of the focal plane, and rays for the $-r$ edge cross the axis when reflected from points in front of the foral plane
the minor axis $B$, then at angle $a$ from the perpendicular to the center of the ellipse, we have

$$
\begin{equation*}
\frac{B}{A}=\cos a \tag{93}
\end{equation*}
$$

In Fig. 49 the crater of radius $r$ as seen from the point $P$ is an ellipse of semi-major axis $r$ and semi-minor axis $r \cos a$, and the image of the elemental beam from $P$ has these same proportions with the minor axis set in a radial direction to the axis of the beam. The image touches the axis at a distance $L_{0}$ such that

$$
\frac{L_{0}}{y}=\frac{P}{r \cos a}
$$

and substituting for $y$ and $p$ their values in terms of $F$ and angle $a$.

$$
\begin{equation*}
L_{0}=\frac{2 F^{2}}{r} \times \frac{\tan \frac{a}{2} \sec ^{2} \frac{a}{2}}{\cos \alpha} \text { inches } \tag{94}
\end{equation*}
$$

Two other forms of this equation are sometimes useful:

$$
\begin{align*}
L_{0}= & \frac{\underline{2} y^{2}}{r \sin 2_{a}} \text { inches }  \tag{0.5}\\
\text { and } \quad L_{0}= & =\left(F+\frac{y^{2}}{4 F}\right)^{2}  \tag{96}\\
& \left(F-\frac{y^{2}}{4 F}\right)^{\text {inches }}
\end{align*}
$$

As an example, take the case of the three 15-in. mirrors of focal lengths $7.7!9 \mathrm{in.}$,
inn.. and 2. ©in. What have been mised in previous illathalions, and bet us assume the erater (w) have a ratius of 0.2.5 in. These three mimors have angles of 80 deg, 90 deg. and 120 dag. The begimning of the inversespuate region, computad hy any of the three
 minter and infisity for the !ef- and 120bege mirrors. Three points about these figures are of interest. The are with a (it)-deg. mirror takes twice the range of the conespemding spherical somere to attain full central intensity; the are with a $90-$-deg. mirror gives a bean that (in theory at least) never attans full axial intensity at finite distances; and the negative sign found when solving for the 120-deg. mirror indicates a crossing point for the critical ray back of the mirror. This "virtual" point is meaningless for another reason. The 120 -deg. mirror has a $9(1)-(\mathrm{leg}$. zone, and therefore it comes under the condition noted above of not having an inversc-square region. The assumption is here made that the source can radiate light to the $120-\mathrm{deg}$. zone, which is the case when dealing with incandescent lamps with the monoplane filament (see Figs 47 and 45) that entitles them to come under the head of disk radiators.

The beam intensity on the axis is proportional to the area of the mirror that is luminous, and equation (46) is used regardless of the source being a disk or a sphere.

$$
\begin{equation*}
I=4 \pi B m F^{2} \tan ^{2} \frac{a}{2} \text { candles } \tag{+1;}
\end{equation*}
$$



Fig. 50. The Rates of Increase of Beam Intensity for Three Mirrors of Equal Diameters but Different Focal Lengths. Of the three, only the $60-\mathrm{deg}$. mirror gives a beam that reaches the permanent condition which gives the inverse-square region along the axis. The radius of the source is 0.25 in .

Taking, merely as an example that can be readily compared with the similar one used for the spherical source, a brilliancy $B$ of 10,000 candles per square inch, and a
mirror coefficient $m$ of $0 . s .9$, the rates of increase are worked out in Fig. j) for three mirrors with a disk radius of 0.25 in. The beam from the 90 -deg. mirror increases rather slowly in intensity along the axis, so that at 720 in . it is only slightly over hald as intense as the beam from the $60-\mathrm{deg}$. mirror. If we imagine the disk to be without thickness then the $90-\mathrm{deg}$. curve comes tangent to the limiting value of the $60-\mathrm{deg}$. curve at infinity. The $1: 0-$ deg. mirror reveals an interesting phenomenon. The first section of the curve, Fig. 50, has a limiting value of 0.72 million candles, because
area in the center of the mirror has an angle a of is deg. and the mirror beyond this angle is dark. At 720 in . a bright zone has appeared near the edge of the mirror bounded by angles of 106 deg. and 11 N deg. as determined by the upper curve in the illustration. The central active zone has grown to s:3 deg. as found by the lower curve. At 1080 in. the central zone extends to 8.5 deg . and the outer zone begins at 97.5 deg. and goes to the edge of the mirror.

Returning to Fig. 50 the first section of the 120 -deg. mirror curve is continuous up to 680 in., where a sudden increase in inten-


Fig. 51. The manner in which the discontinuous rise of central intensity occurs with a deep mirror and a double disk source is illustrated by the bright zones in these three views of a 120 -deg. mirror. The light in the center bright zone comes from the side of the disk facing the mirror, and at short distances the opposite side of the disk does not project light to the axis. As the distance along the axis is increased the beam intensity is suddenly increased due to the appearance of a bright zone on the outer part of the mirror which reflects light from the side of the disk facing outward along the beam. The dark zone between the two active areas decreases as the distance along the axis is increased, but even for an ideal disk of zero thickness the dark zone will never entirely disappear
with a disk luminous on the side next to the mirror, the active mirror area would be limited to 90 deg. from the axis, or to onethird of the mirror area. If the disk is equally luminous on the reverse side, an entirely different method of increase is introduced.

The three views of the $120-$ deg. mirror in Fig. 31 illustrate how the luminous area grows as the observer goes out along the axis of the beam. These views were drawn from the curves of Fig. 52 in which the data were computed by equations (94) and (46). At 360 in . the boundary of the luminous
sity marks the abrupt introduction of the luminous outer zone. The rapid rise of the second section of the curve is broken at 750 in. by this zone reaching the mirror edge, and the slower rise from there on is due to the slow contraction of the dark zone illustrated by the third mirror in Fig. 51. This zone gradually decreases but never entirely disappears.

If equation (94) is plotted as in Fig. 52, it will be found that $L_{0}$ reaches infinity when a reaches 90 deg. Above 90 deg., $L_{0}$ decreases to a minimum at 111 deg .30 min . and then increases to infinity at 150 deg . The min-
imum point at 111 deg. 30 min. is independent of either the focal length or the radius of the disk source. The first derivative of (9-4) when placed equal to zero gives

$$
\begin{equation*}
\cos a=-2 \sin \frac{a}{2} \frac{a}{2} \sin \frac{3 a}{2} \tag{!7}
\end{equation*}
$$



Fig. 52. The plot of the distances at which rays from the various mirror zones first cross the axis of the $\mathbf{1 2 0} \mathbf{- d e g}$. mirror of Fig. 50 shows that at short range there is a single zone added for each increase of distance, but beyond 680 in . three zones are introduced into the luminous area by each increase of $L_{0}$. These zones are on the edge of the central active zone of the middle view in Fig. 51, and on the inner and outer edges of the outer active zone
for a minimum value for $L_{0}$ at the above angle.

Three curves for three searchlights are given in Fig. 53. These curves were computed a number of years ago to see if test conditions on the outdoor searchlight range (2300 ft. to test station) were suitable for a series of tests on $60-\mathrm{in}$. searchlights. This distance was found to be more than sufficient for the plain carbon electrodes having crater diameters of $0.5 \pm \mathrm{in}$. and 0.81 in and just barely sufficient for the high-intensity electrode. The center of the high-intensity electrode is much brighter than the edge and light from this central portion must reach the axis to give the beam its full central intensity. This arc will be investigated in detail when the graphical methods of computing are explained.

## The Inverse-square Region

When a disk source luminous on one or both sides is employed and the mirror angle is less than 90 deg., there is a flat crest to the beam and a region where the law of inverse squares may be used to compute the illumination. But if the mirror subtends an angle greater than 90 deg. from the axis the beam will never reach full intensity
because all light reflected from the 90 -deg. \%one will be parallel to the axis and will not reach it. This, of course, is a theoretical point but it is of considerable importance in l)ringing out the highly practical fact that an are with a 90 -deg. mirror requires a much greater testing range than any combination previously considered.

A monoplane filament with a mirror of over 90 deg. gives a beam whose intensity rises in a discontinuous manner, as illustrated in Fig. 50, but the approach to the final maximum is probably greatly accelcrated by the fact that the filament has considerable thickness along the axis. As a result, there is an inverse-square region at distances only slightly in excess of the second turning point in the curve. As a rule, in testing, the inverse-square region is readily mapped out by walking across the beam at the test distance and observing the angular range over which the entire mirror is active. The results obtained in this way will be influenced by the optical errors in the reflector and other factors, such as the thickness of the filament along the axis and the accuracy of focusing. The theoretical data are therefore only a first approximation to the facts.

The fact that tests on the plain carbon arc do not always show an appreciable flat crest does not necessarily indicate an absence of an inverse-square region, which may be present but concealed by the lack of perfect uniformity of the crater brilliancy.


Fig. 53. Curves showing that a $60-\mathrm{deg}$. mirror with different arcs requires different minimum distances for measuring the full central intensity. Curve $A$ shows a plain carbon crater of 0.81 in . dia. with a $60-\mathrm{in}$. standard mirror requires 400 ft .; a plain carbon crater of 0.54 in . dia. requires 600 ft ., as in Curve $C$; but a high-intensity arc of equal diameter, Curve $B$, requires nearly 2000 ft .

## Testing Distance for Central Intensity

As a rule those light sources that are classed as disk-formed are readily measured for diameter with considerable accuracy. Thus the crater of the high-intensity arc is
consistently within a few tenths of a millimeter of the average value and the monoplame incandescent filament has definite boundaries. The conditions are thus favorable for computing the varions beam characteristies from the dimensions of the source except in the case of certain plain carbon ares that often have ollique craters of irregular outline. This circumstance of greater ease of accurate measurement is fortunate because of the greater (and sometimes inconvenient) distances required for are testing. We are thus in a position to base onr computations on either source dimensions or on the beam width.

Using the observed beam width to compute the testing distance, we get

$$
\begin{equation*}
L_{0}=\frac{45 S \tan a}{C_{0}(1+\cos a)^{2}} F \tag{98}
\end{equation*}
$$

This expression differs from equation (50) which is the expression for $L_{0}$ with a spherical source by having $\tan a$ in the numerator in place of $\sin a$. Therefore $L_{0}$ becomes infinite when $a=90 \mathrm{deg}$. and in the curves of Fig. Jt no greater angle is considered.

## Width of Crest of Beam

When the light source is uniformly bright across a diameter the beam has a "crest" or central region in which the intensity is uniform. In nearly every actual searchlight, the crest is not perfectly flat on account of variations in the brightness of the light source. An exploration of the beam from


Fig. 54. When the beam diameter is known these curves will indicate the least distance, in focal lengths, at which the central intensity comes to its full maximum value
a plain carbon arc gives a definite trace of the edges of the crest, but the intensity on the axis is higher than at these edges. An incandescent filament shows the same departure from theory to about the same degree, which is, of course, due in a large degree to
the higher temperature of the eentral part of the filament.

The beam of the high-intensity are is most intense in the center and falls off rapidly to either side of the axis so that the plotted curve shows no trace of a flat crest.

The expression for the error $E$ in measuring the crest width has real practical significance even in the case where the crest is not apparent, and equation (.54) is a useful suide in selecting test conditions, as will be seen later in investigating the beam formation of a (0)-in. high-intensity searchlight at short 2300 ft .) range.
The crest comes to full width only at infinity, and the error at finite distances is

$$
\begin{equation*}
\left.E=\frac{L_{0}}{L} \text { (numeric }\right) \tag{.54}
\end{equation*}
$$

which indicates that to get fairly correct data on the intensities near the axis the test distance should when possible be five or more times greater than $s_{0}$ as computed by equation (94).

## Width of Beam

The "width" of beam from a disk source is subject to the same classification as in the spherical source beam. There is the width, at great distances, of angle $C_{0}$, and the width $C$ at short distances, and in addition the width according to the 10 -per-cent rule.

The limiting angular width $C_{0}$ is derived from the spread of light from the center of the mirror.

$$
\begin{equation*}
\tan \frac{C_{0}}{2}=\frac{r}{F} \tag{999}
\end{equation*}
$$

So long as $C_{0}$ is not over 10 deg., we may use the relation

$$
\begin{equation*}
C_{0}=\frac{114.56 r}{F} \operatorname{deg} . \tag{100}
\end{equation*}
$$

as a working approximation.
The curved boundary or envelope of the beam is determined by considering where two rays from an edge of the disk and reflected from adjacent points in a meridian plane meet in the beam. In Fig. i. 5 two rays from the lower edge of the disk meet at a distance $L_{e}$ along the axis and at a distance $\frac{\Pi_{e}}{2}$ from the axis.

$$
\begin{gather*}
y_{1}+L_{e} \tan \varepsilon=y_{2}+L_{e} \tan f \\
L_{e}=\frac{y_{2}-y_{1}}{\tan \varepsilon-\tan f} \text { inches } \tag{.57}
\end{gather*}
$$

Taking $y_{1}$ and $y_{2}$ close together so that the difference between them becomes the differential $d y$, then

$$
\begin{equation*}
L_{e}=\frac{d y}{d(\tan \varepsilon)} \text { inches } \tag{101}
\end{equation*}
$$

Where

$$
\begin{equation*}
d y=l \cdot \sec \left(\frac{10}{\square} d u\right. \tag{0!1}
\end{equation*}
$$



$$
=-\frac{r}{I} \cdot \cos \frac{a}{2} \sin _{2}^{3} \frac{3}{2} d a
$$



Fig. 55. The width of the beam at any distance is determined by some particular zone within 45 deg . of the axis of the mirror, as shown by the heavy curve; and the region between 45 and 90 deg. (the dotted curve) gives the outline to the inverse-square region. The other mirror zones do not contribute to these important boundaries

Combining (102) and (103) we get for negative (downward) values of $r$ :

$$
\begin{equation*}
L_{e}=\frac{F^{2}}{r \cos ^{3} \frac{a}{2} \sin \frac{3 a}{2}} \text { inches } \tag{103}
\end{equation*}
$$

for the distance to the point where the line image of the edge of the disk occurs. The radius of this image from the axis is

$$
\begin{equation*}
\frac{W_{e}}{\dddot{\prime}}=y_{1}+L_{e} \tan \varepsilon \tag{.5.5}
\end{equation*}
$$

The ralue of tan $c$ in terms of $F, a$, and $r$ is

$$
\begin{equation*}
\tan e=\frac{r \cos a}{F \sec ^{2} \frac{a}{2}} \tag{104}
\end{equation*}
$$

and equation $(55)$ reduces to

$$
\frac{W_{e}}{2}=2 F \tan \frac{a}{2}+L_{e} \frac{r \cos a \cos ^{2} \frac{a}{2}}{F}
$$

If this equation is further reduced to eliminate $L_{e}$, we get the interesting form
$\frac{11_{e}}{2}=\mathrm{F}\left(2 \tan \frac{a}{2} \mp \frac{\cos a}{\cos \frac{a}{2} \sin \frac{3 a}{2}}\right)$ inches.
It will be noticed that the radius $r$ does not occur in this equation and therefore the width of beam as determined from each section of mirror is independent of the size of the source. What happens is that the image from say the $60-\mathrm{deg}$. point on the mirror is at a distance 1.7321 F from the
axis, lat it is closer to the mirror for a large source than for a smatl one. 'Therefore, all loams from mirrors of equal angles a are of the same form, and one set of width curves will do for all by simply making the proper change of coördinates.
liquation (10ti) has been solved and plotted in l’ig. 5. for all angles up to 180 deg . There are four branches to the curve, two for the (o) of the source, $+r$ in Fig. 5 . , and two for the bottom, $-r$. Not all of these branches are involver in the determination of the beam outline. The ordinates are in terms wf the focal length; thus at mirror angle 10 deg. the upper curve has an ordinate of $+4 \%$ where the + sign signifies distance up from the axis and the $-r$ with which the curve is marked indicates that the lower edge of the source furnishes the light for this boundary. Angle $a$ is always measured upward from the axis. The $-r$ branch goes from plus infinity at 0 deg. to minus infinity (below the axis) at 120 deg. The other part of this $-r$ curve comes from plus infinity at 120 deg. to a minimum at 1330 deg. and then returns to plus infinity.

The curve for the upper edge of the source at $+r$ comes from minus infinity at 0 deg. and crosses the $-r$ curve at 90 deg. and then goes to plus infinity. The second section of the $+r$ curve rises from minus infinity at 120 deg. to zero at 135 deg. and then goes to minus infinity at 180 deg.

It is shown in Fig. 56 that only a part of the $-r$ curve between 0 deg. and 45 deg . is directly connected with the outline of the


Fig. 56. The relation between the beam width $W_{e}$ and the distance $L_{e}$ at which the images from various mirror zones occur is plotted to show that zones zero to 45 deg. furnish the edge rays of the beam and all other images fall within the beam
beam. Points from 4.5 to 90 deg. on the $-r$ curve plus the $+r$ curve from 90 to 120 deg. are used only in connection with the initial straight section of beam before the surved boundaries are encountered.

In Fig. if the outline of a beam from a mirror of 7.79 in . focal length with a disk somree of 0.25 in. radius is given by the heary solid lines. On the left of the illustration a seale of degrees is laid out. A staight line from any angle on either the heary solid line or the heary dotted line gives the initial straight section of beam edge, and beyond the crossing point the straight line forms the tangent line (tangent at infinity) for the inverse-square region.

If the mirror angle is over 90 deg. there is no inverse-square region and a line through the proper point of the light dotted section of the $+r$ curve is uscful only in determining the straight edge of the beam from the mirror out to the curved edge.

At the center of the mirror the linear width of reflected beam is

$$
\begin{equation*}
\frac{11_{0}^{\circ}}{\underline{2}}=L_{c} \frac{r}{F} \text { inches } \tag{64}
\end{equation*}
$$

and at some outer zone at angle $a$, the width is
$\frac{W_{c}}{\underline{2}}=2 F \tan \frac{a}{2}+L_{i} \frac{r \cos a \cos ^{2} \frac{a}{2}}{F}$ inches
The excess width of $\frac{\mathbb{W}_{e}}{\underline{2}}$ over $\frac{\mathbb{W}_{0}}{\underline{2}}$ is
$E=\cos ^{2} \frac{a}{2}\left(2 \sin \frac{a}{2} \sin \frac{3 a}{2}+\cos a\right)-1$ (numeric)
and from the absence of both $F$ and $r$ the excess is quite evidently dependent only upon the angle $a$. The distance along the axis at which the measured excess corre-


Fig. 57. The beam width at extreme ranges is determined solely by the exact center of the mirror, but at working ranges other zones of the mirror produce a beam of greater width. At short range, rays from the edge of the mirror form temporary false beam edges that are greatly in excess of the true beam width
sponding to angle $a$ occurs is dependent upon $F^{2}$ and $r$ as may be seen in equation (102) for $L_{e}$. The excess width is a maximum (20.9 per cent) at 45 deg. and in this it

[^63]differs from the beam from the spherical source which has a maximum of to. per cent at do deg.

One visible effect of the fow angle at which the maximum oceurs is the sharp spintle or neck in the beam from an are lamp. The mir-


Fig. 58. The excess of beam width at finite distances over the final beam width is solely a function of the angle of the mirror zones; the value of the excess is not influenced by the relative size of the source, although the distance at which some particular excess width occurs is dependent upon the ratio of $r$ to $F$
rors used with ares nearly ahways have an angle of 60 deg . and the initial edge ray of the beam intersects the curved boundary at an appreciable angle as illustrated in an exaggerated manner in Fig. $\boldsymbol{\pi}$.

The errors arising from computing or testing the beam of a 7.79 in . focus mirror at ranges so short as to encounter the initial straight boundary from the edge of the mirror are shown by the branches from the heary curye in Fig. $5 \overline{7}$. For this particular case distances under 1000 in . are evidently best avoided.

The general relation between the excess width and mirror angle is given in Fig. 58. The data of this curve can be applied to any case by solving for $L_{e}$ independently, using the proper values for focal length, radius of source, and mirror angle $a$. The data so obtained, when plotted, give a curve similar to that of Fig. 57. A comparison of this curve with Fig. 30* shows that while the disk source reaches higher errors for given regions on the mirror, the errors at any given range along the axis of the beam is about half. Thus at 1000 in . the spherical source gives an excess beam width of 6 per cent, while the disk source at the same distance gives an excess of only 2 per cent. We can therefore conclude that, in general, the arc searchlight can be tested for beam width at considerably shorter distances than the corresponding spherical shaped incandescent filament.

# The Electron in Chemistry <br> PART II (A) 

By Sir Joserh John 'Thomson<br>Masher of Trinity Coliege, Cambridge, England

In our August issue we published the first of this series of lectures. The second lecture, published in full in the June issuc of the Journal of the lranklin Institute, is solong that we divide it. Accordingly in this issue we print Part 1 ( $\Lambda$ ) dealing with The Combination of Atoms to Form Molecules; Four-electron Atoms, Combination of Different Elements, Chemical Compounds; Polar Molecules; Physical Test for Polar Molecules and - Irrangement of Electrons in Octets. In our October issue we purpose printing Part II (B) which will include Disposition of the Electrons in Typical Compounds; Connection Between Chemical Constitution and Chemical Properties; Residual Affinity, Molecular Compounds, Werner's Co-ordination Numbers and Electrolytic Dissociation.-EDITOR.

The Combination of Atoms to Form Molecules
We shall begin by considering molecules in the gascous state, where each molecule is separated so far from its neighbors that it may be regarded as an individual and not as mercly forming a brick in a much larger structure. Indeed, the term molecule when applied to the solid state is quite ambiguous without further definition; for example, from many points of view we can consider quite legitimately the whole of a large crystal as forming a single molecule. It is natural to expect that when the atoms are crowded together as in a solid, where each atom may come under the influence of a large number of neighbors, the arrangement of the electrons relatively to the atom may differ substantially from that in a gaseous molecule.

Let us begin with the simplest case, that of the union of two similar atoms each containing one electron. We see that if the atoms and electrons are arranged as in Fig. 2, where $A$ and $B$ are the atoms and $\alpha$ and $\beta$ the electrons, the mutual repulsion of the electrons may be balanced by the attraction of the positive charges on the electrons; and the mutual repulsions of the similarly electrified atoms by the attractions of the electrons. Thus we may regard the electrons in the atom as acting like hooks by which one atom gets coupled up with another. As the atoms are held together by the attraction of the pair of electrons $\alpha, \beta$, the presence of two electrons between the atoms may be taken as the physical interpretation of what is called a bond by chemists. In this example and in general, two electrons go to each bond. There are, however, cases such as that of a positively electrified molecule of hydrogen (so frequently detected in positive-ray photographs) where a single electron is able to bind two atoms together. The arrangement being that represented in Fig. 3.

The dimensions and shape of the parallelogram represented in Fig. 2 will depend on the
law of force between two positive charges at atomic distances as well as upon that between a positive charge and an electron. If $e^{2} \phi\left(\frac{C}{r}\right)$ is the attraction between a positive charge $e$ and an electron with equal charge


Fig. 2
separated by a distance $r$ and $e^{2} \psi\left(\frac{c^{1}}{r}\right)$ the repulsion between two positive charges at a distance $r$, then if $A \alpha=r$ and $\angle A \alpha \beta=\delta$, we have for equilibrium

$$
\begin{align*}
& 2^{2} e \phi\left(\frac{c}{r}\right) \cos \delta=\frac{e^{2}}{4 r^{2} \cos ^{2} \delta}  \tag{25}\\
& 2 e^{2} \phi\left(\frac{c}{r}\right) \sin \delta=e^{2} \psi\left(\frac{c^{1}}{2 r \sin \delta}\right)
\end{align*}
$$

Though the distance of an electron from its atom will obviously be not quite the same in the molecule as in the atom, we should expect that the differences would not be very large. For if they were, work would have to be done at some stage in the act of combination comparable with that required to ionize an atom, as this work is much greater than the equivalent of the heat developed by the union of the atoms to form a molecule we could not expect atoms under these conditions to combine to form molecules except in the presence of a very efficient catalyst.

Let us now pass to the case where each of the atoms contains two efectrons. if only onte pair of electrons is used up in miting the atoms, the arrangement would be that represented in Fig. f, where the Greck letters represent the electron. In the language of chemists this wouk be expressed by saying that the atoms were united by a single bond and the molecule would be expressed by the formula - A- $B-$. The electrons $\alpha^{\prime}$ and $\beta^{\prime}$ Would enable this molecule to link up with other molecules so that it would not be saturated. If, howeter, all four electrons are used in coupling up the atom, they will be at the corners of a square bisecting $A B$ at right angles.

The system of four electrons instead of two between the positively electrificd atoms may be regarded as the physical equivalent of what the chemists call a double bond. Inasmuch as the equilibrium of four electrons in one plane, when their displacements are not confined to that plane, requires very strong restoring forces to make it stable, we should not expect the double bond to be permanent when the positive charges which exert the restoring force are as small as in this case, where their sum is only equal to the sum of the charges on the four electrons.

For the union of two tri-electron atoms, if all the electrons were used to couple up the atoms, there would be a hexagonal ring of electrons in a plane bisecting $A B$ at right angles; as this ring requires a greater positive charge than that of three units on each side to keep it in stable equilibrium it would be


Fig. 3


Fig. 4
unstable. The most probable arrangement of the electrons is the octahedral one shown in Fig. 5 with four electrons between the atoms and two on the line $A B$; this would be represented symbolically by the formula $-A=B-$. The end electrons would enable it to bind other
atoms so that the molecule world not be saturated.

## Four-electron Atoms

These may form a molecule in which the electrons are as represented in fiy, (; font


Fig. 5




Fig. 6
electrons are between $A B$ and the other four form two pairs bevond the extremities of the line $A B$.

A peculiarity of the arrangement in Fig. 6 is that the molecule has four free electrons the same as the original atom, thus other atoms can be coupled up with the molecule, and we might have a chain of atoms, each atom being at the center of a parallelipiped of eight electrons. We can show that a long chain of such atoms would be unstable, but it is evident that the four-electron atom is one peculiarly suited for forming complexes containing several atoms. The carbon atom has four electrons in its outer layer and thus carbon atoms would have a great tendency to unite with each other. It is this tendency that is responsible for the Science of Organic Chemistry. I may point out in passing that we can obtain from the study of positive rays direct evidence of the coalescence of carbon atoms. For on a positive-ray photograph of benzene I found lines corresponding to $\mathrm{C}_{1}$. $\mathrm{C}_{2}, \mathrm{C}_{3}, \mathrm{C}_{4}, \mathrm{C}_{5}$, where $\mathrm{C}_{1}$ represents a carbon atom; $\mathrm{C}_{2}$, a carbon molecule; $\breve{C}_{3}$, a carbon triplet, and so on.

The form we have suggested for the electrons in the molecule of atoms of this type is represented symbolically by the formula
 diverlectron atoms we hate to int ronduce new ansulerations. Wra bato sern that eight is the maximum numbur of ofotmons which can be in stahle expilibrime in a single laver mater the ation of pestive edarges whose aggresate




Fig. 7
camot excecd the total charges carried by the clectrons. With a five-clectron atom we have ten electrons in the molecule, while the aggregate positive charge, in the molecule, is also ten, which is not sufficient to keep the ten electrons in stable equilibrium if spread over a single layer. A simple way of arranging the electrons is shown in Fig. 7. Mielway between the positive charges are six electrons which keep the atoms together, four of them at the corners of a square forming the normal double bond, while two others are inside the square.

The remaining four electrons are arranged in pairs beyond the atoms $A, B$, respectively. Thus we have cight electrons surrounding two atoms and two electrons. The arrangement is somewhat like that suggested for the carbon molecule with the addition of two electrons near the center of the molecule.

When each of the atoms contains six electrons the arrangement is as follows: There are four electrons forming the normal double bond between the atoms, and two other sets of four, one set beyond $A$, the other beyond $B$. Thus each of the two atoms may be regarded as being inside an octet of electrons, the two octets having four electrons in common. When each of the atoms contains seven electrons, we have fourteen electrons at our disposal. These may be arranged so that two of them form a single bond between the atoms while the remainder complete two octets with two electrons common to both, as is represented in Fig. S. This, though a very symmetrical arrangement, is not the only conceivable one. For when the positive charges are large, as they are in this case, they might hold four or even more electrons in stable equilibrium, even though the electrons were very close together. Thus suppose there
were a double instead of a single bond between Whe atoms, this would aceoment for four clecwons, leaving ten to be distributed outside. If these were distributed symmetrically, there would le five aromol each atom, so that cach atom would 1 e the center of a layer contaiming nine clectenss, four coming from the double lond and five from those left over after the domble bomal has been provided for. Now nine electrons comk not he in equilibrium if equally distributed under a central charge of seven, lut if four of them are held elose together in stable equilibrium under two positive charges, it is possible that there may be room for the other five to be so far apart that they can be kept in stable equilibrium by a positive charge of seven units.

It will be noticed that the molecules formed by the mion of two atoms, each of which contains less than five electrons, have free cketrons which are available for linking up with other molecules. The one-electron atoms could form chains as in Fig. 9. Thus the process of aggregation is not exhausted by the formation of the molecule; these molecules will form further aggregations and thus tend to get into the solid or liquid state. On the other hand, the molecules formed by atoms with five or more electrons form saturated systems and will not tend to aggregate further. This agrees with the properties of the elements; for $\mathrm{Li}, \mathrm{Be}, \mathrm{Bo}$, and C , whose atoms contain less than five electrons, are solids, while $\mathrm{N}, \mathrm{O}, \mathrm{F}$ and Ne , whose atoms contain five or more electrons, are gases.

From the consideration of the arrangements of the electrons in different molecules. we see


Fig. 8
that for the atoms containing four and five electrons we can regard the electrons in the molecule as roughly distributed over a single layer not very far from spherical; when, however, we reach the six-electron atom the
dectrons in the molectule form two cells, and a surface wheh would contain them all would have to be very elongated We set some confimation of this result from the stady of the seattering of polarized light by gases. The theory of such seatering shows that the light scattered bey a single electron in a direction at right angles of the incident beam is completely polarized and can be extmguished by a Nicol prism. The same thing is true when the light is scattered by a perfectly symmetrical body such as a sphere. If the scattering body is not perfectly symmetrical, if, for example, it is elliptical instead of spherical, the scattered light is never completely polarized and therefore cannot be entirely quenched by a Nicol. The ratio of the minimum to the maximum intensity of the light seen through a Nicol would be zero for a spherical body, but would be finite for an ellipsoid and would increase with the ellipticity: The value of this ratio mar be taken as an indication of the deriation of the scatiering body from sphericity. The scattering of light by molecules is due to the electrons in the molecules: we should expect that an arrangement of electrons in one shell would approach more closely to the spherical arrangement than an arrangement in two cells, and that two cells would approximate to the spherical more closely than three. Thus the ratio of the minimum to the maximum intensity of the scattered light should increase with the number of cells. Lord Rayleighs has determined the value of this ratio for several gases with the results given in the following table:

| Gas | Ratio Expressed as a Percentage |
| :---: | :---: |
| Argon. | 0.46 |
| H)drogen | 3.83 |
| Nitrogen | 4.06 |
| Oxygen | 9.4 |
| Carbon Dioxide | 11.7 |
| Nitrons Oxide.. | 15.4 |

We see how small this ratio is for the symmetrical distribution of electrons round


Fig. 9
the argon atom. A striking feature of the table is the great jump between nitrogen and oxygen. We have seen that the passage from nitrogen corresponds to the transition from an arrangement of the electrons in one cell to

[^64]
 and nitrous wide requite hare oll - buthedr
 than those in the rexeren monerule


Fig. 10

## Combination of Different Elements, Chemical Compounds

We may apply considerations similar in those we used to explain the formation of molecules of an element by the union of two similar atoms to the union of $t w o$ different atoms to form the molecule of a comprind

Let us consider, for example, the union of a seven-electron atom with a one-electron atom. Suppose that $A$ is the center of the first atom. $B$, that of the second, see Fig. 10 .

Let $\alpha$ be an electron in the first atomn. 3 one in the second. Then if $B$ and $\beta$ place themselves somewhat as in the figure, the attractions the two electrons exert on $A, B$ may keep these together in swite of their mutual repulsions, while the electrons are kept in equilibrium by the attraction upn them of the atoms $A$ and $B$. The addition of $\beta$ to the seven electrons already round $A$ will raise the number in the outer layer of $A$ to eight. Now suppose we attempt to attach another atom $\beta^{\prime}$ to $A$, this would introduce another electron into the outer layer round $A$, raising the number in this layer to nine. We have seen. however, that nine electrons in one laver cannot be kept in stable equilibrium by a positive charge of nine units; in this case nine units are all we have at our disposal and two of these are outside the layer. The outside ones will make the arrangement of electrons more stable than it would be in their absence. They will not, however. increase the stability more than they would if they were inside, and even in that case they could not make the arrangement stable. Thus $A$ cannot hold a second atom of the type $B$, so that the compound $A B_{2}$ is impossible and that represented by $A B$ is saturated. Thus, if $B$ with
its one eleetron is laken ats the type of a monovankent atom, like hyedrogen, A with its seven electrons would also be monovalent, and would in this respect ate like flnorine. 'The electrons in the molecute $/ 1 /{ }^{\circ}$ would form a laver round the eenter of the flatorine atom


Fig. 11
with the positive part of the hydrogen atom outside. Let us now suppose that $A$ is a six instead of a seven-electron atom and let an atom of $B$ get attached to it in the way we have supposed. This will raise the number of electrons in the layer round $A$ to seven, so another atom can be attached before the number of electrons in the outer layer is raised to eight and the limit of stability reached. Thus $A$ could form the unsaturated compound $A B$ and the saturated one, $A B_{2}$, but $A$ could not combine with more than two atoms of $B$. Thus $A$ with its six electrons would behave like the atom of a divalent element, say oxygen.

In a similar way we see that if $A$ contained five electrons it would form the unsaturated compounds $A B$ and $A B_{2}$ and the saturated one $A B_{3}$. Thus $A$ would behave like a trivalent element, nitrogen.

In this way we see that when $A$ acts as the center round which the layer of electrons is arranged, it behaves like an element whose valency is equal to ( 8 -number of electrons in the outer layer of the atom $A$ ).

There is, however, another way in which the atoms might combine, in this $A$, instead of receiving electrons from other atoms, might give up its electrons to help to form a layer round another atom. Take, for example, a two-electron atom $B$, by using one of its electrons it can attachitself to a seven-electron atom and still have one electron free. It can use this free electron to bind itself to another seven-electron atom and thus form the compound $B F_{2}$, where $F$ represents an atom of such an element as fluorine. Thus in this

[^65]type of compound the atom with its two dectrons would behave like a divalent element. A threc-electron atom would be able to bind three atoms of fluorine and so on. In this type of compound the atom under consideration is acting, so to speak, as a giver and not as a receiver of electrons. The valency of the atom when acting in this way is equal to the number of its electrons. The electron theory thus, as I pointed out long ago, ${ }^{9}$ leads in a very natural manner to an explanation of valency and it suggests conclusions very similar to those advanced by Abegg and Bödlander, ${ }^{10}$ who ascribed to each clement two valencies according as it was combined with a more electronegative or more electropositive element. The sum of the two valencies always being eight. We have in some of the elements notable examples of two valencies; take nitrogen as an example, whose atoms contain five electrons in the outer layer. If this combines with hydrogen, three atoms of hydrogen will saturate it, as they will bring the number of electrons in the layer round the nitrogen up to eight, the limiting number, thus in the compound $\mathrm{NH}_{3}$, the nitrogen behaves as a trivalent element. But suppose that instead of combining with a hydrogen atom it combines with a chlorine one, which we assume to have seven electrons in the outer layer. One of the electrons from the nitrogen atom might join the layer round the chlorine one, bringing the number of electrons in the latter up to eight, and leaving four in the nitrogen atom. These four electrons can link up with four hydrogen atoms which will bring the number of electrons in the layer round the nitrogen atom up to eight, the limiting number. We thus get the compound $\mathrm{NH}_{4} \mathrm{Cl}$. The arrangement of the electrons being as represented in Fig. 11. As the chlorine nucleus has a positive charge of seven and is surrounded by a layer containing eight electrons, the atom Cl in this compound has a unit negative charge. Since there is a positive charge of five on the nitrogen nucelus and one of four on the four hydrogen atoms, there are nine positive charges on the system $\mathrm{NH}_{4}$, which contains eight electrons; there is thus a balance of one positive charge on the system represented by $\mathrm{NH}_{4}$, so that $\mathrm{NH}_{4} \mathrm{Cl}$ would, when electrolyzed, give $\mathrm{NH}_{4}$ and Cl as ions.

Again each of the five electrons of the nitrogen atom might go off to complete the tale of eight electrons round each of five chlorine atoms forming the compound $\mathrm{NCl}_{5}$; though this substance does not seem to have
been prepared, the corresponding compound $\mathrm{PCl}_{5}$ is well known. The oxygen atom containing six electrons might attach itself to six atoms of chlorine and so be apparently hexavalent, as sulphur is in the remarkable compounds SF $\mathrm{F}_{6}$ discovered by Moissan.

Carbon having four electrons in the outer layer has the same valency $4=S-4$, whether it is acting in either of the above-mentioned ways, hence the compounds $\mathrm{CH}_{4}, \mathrm{CCl}_{4}$. The kind of union between atoms which we have been considering requires two electrons to effect the bond, hence since we cannot have more than eight electrons round a central atom, four is the maximum number of atoms which can be bound by a single atom. There are in fact very few exceptions to this rule, the most conspicuous are the chlorides of some of the elements which have very variable valencies, such as $\mathrm{UrCl}_{5}, \mathrm{WCl}_{5}, \mathrm{MoCl}_{5}$, which will be considered later.

Thus the considerations we have been discussing give a physical basis for the theory of valency in the extended form given by Abegg. The electron theory, however, is much more general than the laws of valency and points to the existence of compounds which are not in accordance with these laws. The electron theory states that any distribution of atoms and electrons in stable equilibrium is a possible compound and will be saturated provided that each electronegative atom is surrounded by a layer containing eight electrons.

Let us consider, as an example, carbon monoxide. CO ; this according to valency laws, is an unsaturated compound, the gas is, however, remarkably inert and only liquefied with great difficulty, so that its physical properties give no support to the view that it is a highly unsaturated gas. In CO there are ten electrons to be arranged the same as in $\mathrm{N}_{2}$, and we may therefore expect that a similar arrangement to that represented in Fig. $\overline{7}$ would furnish a stable and permanent molecule. As the positive charge on the carbon is not the same as that on the oxygen, the cell will not be so symmetrical as that of the nitrogen molecule. It is interesting to note that, as Langmuir has pointed out, some of the physical properties of CO are very similar to those of $\mathrm{N}_{2}$. If this is the constitution of the molecule of CO, it explains why we do not get $\mathrm{CH}_{2}$ as a saturated substance, as the ordinary valency theory would lead us to expect. There are only six available electrons in $\mathrm{CH}_{2}$ and these are insufficient to produce a completely saturated layer. It is
important to point out that we distinguish between the molecule of carlon monoxide and that of the carbonyl radicle ( ${ }^{\circ}()$.

In the latter we suppose that two out of the four electrons of the carbon atom have gone to unite it with the oxygen and to make up


Fig. 12


Fig. 13
the eight electrons required to form the layer round the oxygen atom, while the other two are free to join up with other electrons. Thus while the molecule of CO is represented by Fig. 7, that of the carbonyl radicle is represented by Fig. 12.

Another molecule which may have a somewhat similar constitution to that of CO is NO, Fig. 13. The molecule contains eleven electrons, if we take eight of these to form the outer layer we are left with three, these by taking up positions between the atoms of nitrogen and oxygen inside the outer layer may help to keep these atoms together. The molecule of nitrogen monoxide is not the only form in which the combination NO occurs; it can also exist as the radicle NO, and just as we suppose the carbonyl radicle to have a different configuration from that of the molecule CO, so we suppose that the radicle NO has a configuration in which eight electrons form a cell round the oxygen, the nitrogen atom is surrounded by a layer of seven electrons made up of the three electrons left over after two have been supplied to the oxygen octet; the other four form part of the layer round the oxygen atom. The layer
foumd the nit poxen rexpires amother electron to siturate it and will thus atet like a monalent atom. 'The there electrons left oxer from the live nitrogen ebectrons after two have been used to sattrate the eell round the oxygen atome might he used to hind three hydrogen ions and thus it is possible that mader certain efromstances this raticle might be trivalent

Nitrogen monoxide is an example of the rate type of molectule where the number of electrons in the molectule is odd. Other examples of this type are $\mathrm{NO}_{2}$ and $\mathrm{ClO}_{2}$. If we suppose that for stable substances an octet of electrons is formed round each of the heavier atoms in the molecule, then if the number of electrons is odd, some of these octets must have an odd number of electrons, either one or three, in common. If we suppose the octets are eubes, they could not have three electrons in common, though they could have one, the two cubes having a corner in common. If, however, the clectrons are arranged in twisted cubes instead of the ordinary cubes, two octets might have $1,2,3$ or 4 electrons in common, since twisted cubes have triangular as well as square faces and thus we might have molecules containing an odd number of electrons with a less exiguous connection between the atoms than that furnished by a sincle corner common to two octets. The three-electron contact would account for the existence of a saturated compound with the formula $\mathrm{ClO}_{2}$. We have here nineteen electrons and these might be accommodated in three octets if there was one double contact and one triple one.

Another problem in which the triple contact might come in, is the well-worn one of the benzene ring. In benzene $\mathrm{C}_{6} \mathrm{H}_{6}$ we have thirty electrons which have to be arranged in octets round six carbon atoms. The simplest and most symmetrical way of doing this is to have the six cells in contact round a ring with a three-fold contact between each two. As two opposite triangular faces of the twisted cube are inclined to each other, this could be done without introducing much strain into the system. Models have been made by two of my students on this principle of a benzene ring and also of a naphthalene one. With this arrangement we have complete symmetry, and it is analogous to the Armstrong and Bayer or central theory of the benzene ring. The configuration corresponding to Kekules' conception of the constitution of the benzene ring would consist of three sets of pairs of cells, the cells in one pair having four-fold
contact with each other, but only double conlact with a ecell in a neighboring patir.

The three-contact view leads to restilts with regarel to the constitution of additional compormats of benzene and the halogens which are in harmony with experience.
'The process which we have just been deseribing loy which two atoms $A, B$ are united into a molecule $A B$, of a compound maty be regraded as consisting in one or more of the


Fig. 14
electrons in the outer layer of $A$ becoming a member of the outer layer of $B$. This is equivalent to one of the electrons in the outer layer of $B$ becoming a member of the outer layer of $A$. Thus each atom lends electrons to the other to enable it to fill up its outer layer; the atoms share their electrons for this purpose and the electrons which they have in common tend to hold the two atoms together. I think it is desirable to emphasize this aspect of the question, to regard the union of the two electrons as a sharing of their electrons rather than as the robbery of one atom of the electron belonging to another. I doubt if there is any very large change produced in gaseous compounds by chemical combination in the distance of an electron from the center of the atom to which it originally belonged. I do not mean that the distance remains unaltered, but only that there is no such change in distance as would warrant our saying that the electron was bound to $B$ before combination and was free afterwards. To tear electrons from an atom requires a much larger amount of work than to separate a molecule into uncharged atoms, and though there may be a redistribution of the electric charges on the molecule, there is nothing which can fairly be described as ionization. Thus to take a specific example we regard the constitution of a molecule of HF as consisting of a unit positive charge H outside an outer layer of eight electrons surrounding the fluorine atom with its positive charge of seven units, and though we may legitimately describe the molecule as consisting of a positively charged hydrogen atom and a negatively charged fluorine one, it does not follow, if the
molecule were dissociated by a rise in temperature that the product of dissociation would be a positively charged hedrogen atom and a megatively charged fluorine one. It would take much less energy to detach the positive hedrogen atom plus an electron than the positively charged hydrogen atom alone, so that the probable result of the dissociation would be a neutral hydrogen atom and a neutral thumbe one. This would not neces-


Fig. 15
sarily be the case if the dissociation were effected by a high-speed positive ray with an energy corresponding to many thousand volts, for then the hydrogen atom could receive energy far more than sufficient to detach it from the negative electron. 'he result to which we have been led that dissociation would yield neutral atoms is in accordance with experience, for we do not find that chemical changes in gases produced by a rise in temperature are accompanied by a rise in electrical conductivity unless the gases are in contact with hot metals, and in this case the increase in conductivity may be explained by thermionic effects. The absence of electrical conductivity in several cases of chemical action at moderate temperatures was investigated by Bloch, ${ }^{11}$ who showed that the dissociation of arseniuretted hydrogen which takes place at low temperatures is not accompanied by any increase in the electrical conductivity: He also showed that many chemical actions which go on at low temperatures such as the oxidation of nitric oxide, the action of chlorine on arsenic, the oxidation of ether vapors, have little or no effect on the conductivity.

## Polar Molecules

Though in the gaseous molecule we have not ionization in the sense that the atoms of the molecules are free to move in opposite directions under the action of an external electric force, yet the disposition of the electric charges may be such that the molecules would tend to set in a definite direction under

[^66]the action of such an electric force. The center of the positive charges does mot always coincide with that of the negrative ones. so the molectule may have a definite electric moment. It is only in some type of molecoles that this electric moment has a finite value. Thus in the symmetrical molecule formed loy the union of two atoms of the same kind the centers of the positive and negative electric charges coincide and the molecule has no electrical moment. Whereas in a molecule like HCl , where the positive charge is outside the octet as in Fig. 14, the molecule has evidently a finite electric moment.

In other compounds such as $\mathrm{CO}_{2}$, of which the arrangement is that in Fig. 15, there is complete symmetry. Thus, as I pointed out some years ago, ${ }^{12}$ molecules may be divided into two types: (a) Pólar, those having a finite electric moment; (b) Non-polar, those for which the electrical moment vanishes.

These two types will have very different properties. If the molecule has a finite electrical moment, it will give rise to an electric field whose intensity will vary inversely as the cube of the distance, while if the electric moment vanishes the force due to the molecule will vary inversely as some higher power of the distance and will thus die away much more rapidly than the forces due to a polar molecule; the latter will have a more extensive stray field and will attract and be attracted by a much larger number of other molecules.

## Physical Test for Polar Molecules

We shall first describe a test based on physical principles by which we cari separate the polar from the non-polar molecule and then see whether the molecules so separated show marked difference in their chemical properties.

The physical method for determining whether the molecule has a finite moment or not is the determination of the specific inductive capacity of the substance formed by the molecules, and if possible when the substance is in the gaseous state. The molecule with a finite moment will tend to set in a definite direction under the electric field, and this setting will contribute to the specific inductive capacity of the gas, hence such molecules will tend to give an abnormally high value to the specific inductive capacity: Again, since this setting of the molecule involves the rotation of the molecule as a whole, these will move so sluggishly that they will not be affected by vibrations as rapidly as those of light wave: in the visible spectrum.

Hence these molecules will not affect the refractive index in the visible spectrum while they will affect the specifie inductive capacity. We should expect, therefore, that the sul)stances formed by such molecules would depart widely from Maxwell's law that the spuare of the refractive index is equal to the specific inductive capacity. Again, since the setting of the molecules under the electric field will be hampered by the collisions with other molecules and as these collisions are more mumerous and vigorous at high temperatures than at low, the specific inductive capacities of these substances will be affected by temperature and will diminish as the temperature increases. Bädeker ${ }^{13}$ has deter-

TABLE I

| Compounds Which Have a Finite Electrical Moment |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{O}$ | $\mathrm{CH}_{3} \mathrm{OH}$ | $\mathrm{SO}_{2}$ | $\mathrm{CH}_{3} \mathrm{Cl}$ |  |
| $\mathrm{NH}_{3}$ | $\mathrm{CH}_{2} \mathrm{OH}$ | HCl | $\mathrm{CHCl}_{3}($ slight $)$ |  |

mined the specific inductive capacities of many gases at varying temperatures, and it appears from his results that some of these gases, such, for example, as $\mathrm{H}_{2} \mathrm{O}, \mathrm{NH}_{3}$, $\mathrm{HCl}, \mathrm{CH}_{3} \mathrm{OH}$, exhilit all these characteristics, they have specific inductive capacities which are much greater than the square of the refractive index and which diminish as the temperature increases.

Taking this as the criterion, we can find whether the molecules have or have not finite electrical moments and in the following tables, derived from measurements made by Bädeker and other observers, of the specific inductive capacity of gases, various compounds are placed in one or other of two classes.

This list shows that the physical test we have applied separates the substances into two types which have great differences in their chemical properties. In the first type we have substances like water and alcohol which are good ionizers of salts or acids dissolved in them.

The substances in the first table are also those which, like water, ammonia, and alcohol, are conspicuous in forming complex compounds with other salts, such as the hydrates, alcoholates, ammoniates. Another property which differentiates the substances in Table I from those in Table II is that of giving electrification by bubbling. When air or other gases bubble through some liquids, e.g., water, alcohol, acetone, the gas when it emerges is found to be ionized, i.e., mixed with positive and negative ions. Little, if any,

[^67]clectrification is found when a gas bubbles through a liquid like paraffin oil or benzene. This is shown very clearly by the experiments of Bloch. ${ }^{14}$ Liquids of the first type show electrification by bubbling, those of the second do not.

Motecules which contain the hydroxyl radicle OH , such as $\mathrm{H}_{2} \mathrm{O}, \mathrm{CH}_{3} \mathrm{OH}, \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$, are usually polar; other organic radicles, such as $\mathrm{COOH}, \mathrm{CO}, \mathrm{CN}, \mathrm{NO}_{2}$, also make the molecules of which they form a part polar. As the attraction of polar molecules extends over a much wider field than that of nonpolar ones, we can understand why, though the hydrogen in saturated non-polar molecules such as $\mathrm{CH}_{4}, \mathrm{C}_{2} \mathrm{H}_{6}$ is not oxydized by weak

TABLE II
Compounds Which Have Not a Finite Electrical Moment

| $\mathrm{H}_{2}$ | $\mathrm{CO}_{2}$ | He | $\mathrm{C}_{6} \mathrm{H}_{6}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{O}_{2}$ | $\mathrm{CS}_{2}$ | $\mathrm{Cl}_{2}$ | $\mathrm{CH}_{4}$ |
| $\mathrm{~N}_{2}$ | $\mathrm{CCl}_{4}$ | CO | $\mathrm{N}_{2} \mathrm{O}$ |

solutions of sulphuric acid or bichromate of potash, the hydrogen in polar molecules such as $\mathrm{CHO}_{3} \mathrm{H}, \mathrm{CH}_{2} \mathrm{O}$ (formaldehyde), CHOOH , is oxydized under the same conditions.

The fact that the polar molecule must be unsymmetrical gives us some information about the configuration of the electrons. One of the most interesting cases is that of water, which is conspicuous above all molecules for the possession of an electrical moment. Our first impression is that the structure of the water molecule should be that represented by Fig. 16, where the two hydrogen atoms are symmetrically placed with respect to the center of the oxygen atom and the electrons are symmetrically distributed round the line joining the hydrogen atoms. This, however, cannot be right, for it would correspond to a molecule having no electrical moment. If the octet of electrons round the oxygen atom were situated at the corners of a cube, then there could be no question that a symmetrical arrangement of the hydrogen atoms with these atoms, respectively, attached to two electrons at the opposite ends of a diameter would be the position of equilibrium and this would correspond to a system having no electrical moment. If, however, the electrons were arranged at the corners of a twisted cube, no two electrons would be at opposite extremities of a diameter. Thus, if the positive atoms were attached to two electrons the system would be unsymmetrical and would have an electrical moment. Thus the electrical and chemical properties support the view that the electrons in the octet are at the corners of a twisted cube. The symmetrical
position for the hydrogen atoms would, with the twisted cube, be when the positive hydrogen atoms are on the axis through the center at right angles to the square faces. On this axis the positive atoms camot be at a clistance from the nearest electron less than half the diagonal of a square face. This distance is greater than would be necessary if the hydrogen atoms were placed close to the corners of the octet. This increase of distance


Fig. 16
would correspond to an increase of potential energy which might make the arrangement unstable. If would appear from these considerations that there may be more than one form of water. Thus the two hydrogens might be joined (a) to two electrons on the same square face or (b) one of the hydrogens might be joined to an electron on one square face and the other hydrogen to an electron on the other. Similar considerations would apply to the hydroxides of the alkali metals, but we should hardly expect the want of symmetry in these to be as pronounced as in hydrogen for the reason that the radius of say an atom of sodium is greater than that of one of hydrogen, so that these atoms might be able to get into the symmetrical positions without their distance from the nearest electron being increased much beyond that between the atom and electron in the uncombined atom. The effect of increased size may be illustrated by comparing water with methyl ether, which may be regarded as water in which the hydrogen atoms are replaced by the larger $\mathrm{CH}_{3}$ group. The specific inductive capacity of methyl ether and its dissociating power are very much smaller than those of water.

As another instance of the aid which considerations like these may give in determining the structure of the molecule, we may take the case of $\mathrm{SO}_{2}$. The determination of its specific inductive capacity shows that it has a finite electrical moment. It is therefore more likely to be represented by one of the unsymmetrical formulas $\mathrm{S}=\mathrm{O}-\mathrm{O}, \mathrm{O}=\mathrm{S}-\mathrm{O}$, S
than by the more symmetrical one $\mathrm{O}-\mathrm{O}$.

A molecule of a gas with a large electrentatio moment may itself promete combination between two gases, neither of which has molecules with a finite moment. Let us consider the effeet of a mokecule of this kind on the molecules of a gas near it. The intense electric fiekl round this molectile will dray towards it the molecules round it; it will act as a nucelus round which the molecules of the other gas will condense. The nucleus will thus bring these molecules nearer together than they otherwise would be, and if like chlorine and hydrogen they can combine, the presence of the nucleus will assist combination. It seems possible that part of the action of water vapor in chemical combination may arise in this way, the interacting molecules crowding together so as to get into the strongest part of the electric field round the water molecules and thus getting into positions which are favorable for chemical combination.

In some cases the product of the chemical action will be active molecules with large moment. This will happen in the case of hydrogen and oxygen, or with hydrogen and chlorine. since the molecules of water and hydrochloric acid have a finite electrostatic moment. Here chemical combination promoted by the water vapor produces a fresh supply of active molecules and thus of nuclei which promote the combination. There will evidently be a tendency for mixtures of this type to become explosive. It is the intense electric field round a molecule with a finite electrostatic moment which causes the other molecules to condense round it. If, instead of a molecule with its electrostatic doublet, we had a charged ion, we should have a still more intense electric field and therefore might expect to get still greater condensation and more intense chemical action. The study of the conduction of electricity through gases gives us evidence of the existence of this condensation, as the ions in gases behave more like clusters than single molecules or atoms. It may be asked why is it that while molecules possessing finite electric moments are able to promote so markedly chemical action, yet the speed of these actions is not noticeably greater in ionized than in nonionized gases, though in the former the ions must produce intense electrical fields? The answer to the question is, that in any ordinary type of ionization the number of charged ions is very small indeed compared with the number of molecules of a foreign constituent of the gas, even when the constituent is present as the merest traces. Take, for example, the case
of water vapor, if the partial pressure of the Water vapor wore only ho millionth of ath
 $10^{13}$ moleonles of water vapur per cubic centimeter. W'ith such ionizing agrents as Rombgen rays, it is exocptionally strong


Fig. 17
ionization when there are $10^{10}$ ions per cubic centimeter, so that even with the amount of water vapor mentioned above, which it would be very difficult to avoid, even with the most careful drying, there would be about 2800 times as many molecules as there are ions in an intensely ionized gas. In cases where there are an exceptionally large number of ions present as, for example, in the negative glow in a discharge tube, all kinds of chemical actions seem to go on with great facility.

We shall sce later on how these polar molecules are able to bring about dissociation of salts in liquids as well as promote chemical action.

It can be shown ${ }^{15}$ that if $M$ is the electrostatic moment of a molecule, i.e.. the product of one of the charges in to the distance between the charges in an electric doublet which would produce the same electrostatic effect as the polar molecule; then $K$, the specific inductive capacity of the gas at the absolute temperature $T$ and at a constant density corresponding to that at 760 mm . pressure and $0^{\circ} \mathrm{C}$., is given by the equations

$$
\begin{equation*}
K=a+\frac{. S 8 M^{2} \times 10^{36}}{T} \tag{26}
\end{equation*}
$$

where $a$ is independent of the temperature. Hence measurement of $K$ at two different temperatures would give us $M$.

Appiying this formula to the results of Bädeker's experiments, I find that for water

$$
\begin{equation*}
M=2.1 \times 10^{-18} \tag{27}
\end{equation*}
$$

for ammonia

$$
\begin{equation*}
M=1.5 \times 10^{-18} \tag{2S}
\end{equation*}
$$

It is probable that determinations of $K$, and thereby of $M$, at different temperatures for different gases, would give us valuable information as to the lack of symmetry in the molecules of the gas.

[^68]
## Arrangement of Electrons in Octets

We have secen that when a shell of eleremons surrounds a positive charge equal to the total charge on the electrons so that the system as a whole is clectrically neutral, eight is the naximmm mumber of electrons which (an be in stable equilibrimen on the shell. If some of the positive charge be taken from the inside of the shell and placed outsirle in symmetrical positions so as not to destroy the approach to sphericity of the shell of electrons, we can prove that though this transformation will increase the radlus of the shell, it will not in general increase the stability, and that eight will still be the maximum number of electrons which can, consistent with stability, be on the shell.

Thus confining our attention to systems such as those formed by collections of atoms where there is no excess of one kind of electricity over the other, cight will be the maximum number of electrons that can be inchuded on a single spherical surface, while, if there are less than eight, the system will not be saturated. It follows from this that any system of clectrons and atoms which is stable and saturated must consist of a number of cells of electrons, each cell containing eight electrons and having a charged atom inside. It does not follow that all configurations which can be built up in this way are possible, for though each cell might be stable if all the electrons and positive charges outside it were fixed, yet an aggregate of such cells need not be stable if all the electrons and atoms can move quite freely. Thus we cannot be sure that all distribution of electrons into octets represents a possible compound-as a matter of fact. we know that many do not. Thus to take a system of octets like that shown in Fis. 17, which represents a line of cubes placed face to face, each cube containing a positive charge


Fig. 18
equal to four. This is an electrically neutral system, and corresponds to a long line of carbon atoms. This system turns out on mathematical investigation to be unstable and therefore a long chain of carbon atoms cannot exist, but would break up into shorter
(hains. cath containing $\because=3$ on 1 atoms; this is in acoord with chemical experience. (On the wher hand. lones chains of the radicle $\mathrm{CH}_{2}$ exist in many orvanic compondes. 1 have found that the analogons system consisting of a row of doubly charged positive atoms, cath of which is at the center of a tetrahedron of electrons as in Fifr 1ヶ, is stable. Take, as another example. a long row of enbes placed cdge to edge as in Fig. 19, cach cube containing a positive charge 6 , this would form an electrically neutral system and would orrespond to a long chain of oxygen atoms. The mathematical thenry, however, shows that this arrangement is unstable and this is confirmed by experience as compounds which contain even rery short chains of oxygen atoms are highly explosive.

This dirision into octets may be regarded as a kind of entrance examination which every candidate for recognition as a formula representing the structure has to pass, and not as being necessarily either the ight or even a possible formula. It is a necessary condition which every formula must fulfil, bu it is not sufficient to ensure the stability of the compound. It was just the same on the old theory of valency; all kinds of compounds could be imagined which would satisfy the ralency condition, but only a small fraction of these have been detected. In fact, chemistry is something more than freehand drawing.

If we wish to find any arrangement of octets which can represent a molecule consisting of specified atoms, we have to solve the following


Fig. 19


Fig. 20
problem. The number of electrons at our disposal is known because we know the atoms of which the molecule consists; we know the number of cells because there is to be one round each of the atoms which in a free state have four or more electrons in the outer layer.

Thus we know the number of a...- repuriterl and the mumber of chectome at ond hateral: we have wose if it is persible warmate the electrons in rectets. if the ondet-were - gharate




Fig. 21
we make an octet share an edge with another, we save two electrons: if it shares a triangular face, we save three; if it shares a square face. we save four. We have to try to find contacts between the octets of such a kind that the saring of electrons will equal the difference between eight times the number of cells required and the number of electrons at our disposal. Thus to take an example. suppose we want the arrangement for two oxygen atoms; here two cells are required and there are twelve electrons at our disposal: we have therefore to save four electrons by the contact between the two cells; to do this the octets must have a square face in common, so that the only possible arrangement is that represented in Fig. 20.

Suppose, however, we have three oxygen atoms to arrange in a molecule; hence we require three cells and we have eighteen electrons at our disposal; hence we have to save $3 \times 8-18=6$ electrons by the contacts. We may do this in two ways: In one represented in Fig. 21, we have three line contacts, at each of which two electrons are saved. In the other, we have that represented in Fig. 22. where we have one line contact, saving two, and a face contact saving four. The first arrangement is represented by $\angle \mathrm{O} \searrow \mathrm{O}$, the second by $\mathrm{O}=\mathrm{O}-\mathrm{O}$; which are two possible
formulas for w\%one fifotharepossible, there manst be two kinds of ozone; the first of these being quite symmetrical would represent a molecosle without a resultant electric moment, the second we should expeet to involve a finite monment. . Is we can detere the existence of


Fig. 22
electrostatic moments by experiment on specific inductive capacity, we may hope to find out whether or not there are two kinds of ozone and, if there is only one, which is the formula which represents its constitution.

For $\mathrm{CO}_{2}$ we require three cells, and we have $4+2 \times 6=16$ electrons. We have, therefore, to sare $3 \times 8-16=8$ electrons by the contacts; if the atoms are in a line there are only two of these, hence we have to save four at each contact, so that the configuration will be that represented in Fig. 23. This configuration can also be regarded as a quadruply charged carbon atom placed midway between two oxygen atoms surrounded by octets of electrons, each of these systems carrying a charge -2 , the molecule being represented by $\mathrm{O}=\mathrm{C}=\underset{-2}{\mathrm{O}}$. We may point out that we might have another configuration for the same distribution of electric charges, viz., that represented by Fig. 24 ; here the oxygen atoms carry the same charge as before, but they present an edge of the octet to the carbon atom instead of the full face. In this case we see that the layer of
clectrons nearest the carbon atom only contans four elcetrons, in that represented in Fig. $2: 3$ it contains eight. Thus this layer is saturated with the arrangement of Fig. $2: 3$, but not with that of Fig. 2d. Thus if the clectrons in $\mathrm{CO}_{2}$ were arranged as in rig. 24, the molecule would not be saturated ; it could aceommodate, for example, two molecules of water if these were arranged so that the water octet presented an edge to the carbon. While if they were arranged so that each of the water octets presented a point to the carbon atom instead of an edge, it could accommodate four molecules of water. If the oxygen atom also turned a corner to the carbon atom instead of an edge, there would be accommodation for six molecules of water. We thus see that where there are contacts such as those in Fig. 2?3, which are represented by double bonds


Fig. 23


Fig. 24
between the atoms, we can, by alternating the orientation of the cells, make room for other neutral molecules or radicles. The whole number of systems nearest to the central atorn must not, however, exceed eight.
(To be continued)

# Dielectric Strength Ratio Between Alternating and Direct Voltages 

By J. L. R. Hayden and W. N. Eddy<br>Consclting Engineering Department, General Electric Company


#### Abstract

Until the present stage was reached in the general trend toward higher operating vollages and longer distances of transmission, alternating voltage has served well as a universal agent for testing the delectric strength of the insulation. The great lengths of modern high-voltage cable, however, apparently mark the limit of usefulness of alternating voltage for testing the insulation strength of equipment of high electrostatic capacity. Attention is therefore being directed toward the application of direct voltage for this purpose, made possible by the development of the kenotron tube rectifier. This latter method possesses several decided advantages, but its immediate adoption has been delayed by a lack of knowledge as to what value of direct voltage for test is equivalent to the alternating voltage of operation. The following article, delivered as a paper at the recent Annual Convention of the A. I. E. E., reports an extensive investigation made to determine the dielectric strength ratio, or rather ratios, for various insulating materials.-Editor.


As the operation of electrical apparatus and circuits depends on their insulation, the maintenance and test of insulation is of foremost importance.
Insulation testing, even of direct-current apparatus, is usually done by alternating voltage, since high alternating voltages are easily obtained by the alternating-current transformer.

Two serious disadvantages arose in the use of alternating high potential testing: First, in apparatus of considerable capacitance such as underground cables, the charging current at the high test voltage is excessive, requiring uneconomically large and expensive transformers. Second, in other apparatus, corona and other dielectric losses incident to the abnormally high alternating test voltage (of three and a half and more times the normal operating voltage), may permanently damage the insulation.

With the development of the kenotron vacuum tube as rectifier, high direct voltages became available. As there is no permanent charging current with direct voltage, a kenotron rectifier of a few kilowatts capacity could replace a testing transformer of many hundred kilowatts. In the absence of the intensive corona and the high dielectric losses incident to an alternating field, damage of apparatus by the high testing voltage was less to be feared with direct voltage testing.

At first it was expected that the striking distance with direct voltage would be equal to that of the maximum value of the alternating voltage, and tests made with air as dielectric corroborated this. However, engineers familiar with high-voltage direct-current transmission claimed that apparatus could stand materially higher direct voltages than alternating voltages. When high direct voltages became more available, tests made with
them showed that some solid insulation, such as that of cables, stand a higher direct roltage than alternating voltage, and it was hoped then that a constant ratio between the disruptive strength of direct and of alternating voltage could be found, by which the one could be expressed in terms of equality with the other. A series of tests made abroad on cables gave 2.5 as the average ratio between the direct voltage and the (effective or root-mean-square) alternating voltage which has the same disruptive effect.

Further tests made by various engineers here and abroad gave inconsistent results and different ratios between the disruptive effect of direct and alternating voltage, so that now no fixed ratio between direct and alternating voltage can be universally applied.

As the result of severa! years experimental investigation we have come to the conclusion, and expect to show in the following that:

1. The disruptive effect on insulation of a direct voltage in general is different from that of an alternating voltage of a peak value equal to the direct voltage.
2. The puncture or disruptive effect of the alternating voltage (peak value) may be greater, and sometimes very much greater, than that of the direct voltage of equal value, but it may also be less. That is, the ratio: " Direct voltage divided by the peak value of the alternating voltage which gives the same disruptive effect," which we may call " dielec-tric-strength ratio," varies from values less than unity, when the direct voltage stress is more severe, to values much above unity, when the alternating voltage stress is more severe.
3. In air, the dielectric-strength ratio is probably unity.
4. In solid insulation, the dielectricstrength ratio depends on the mechanical,
phesical, and thermal eonditions of the matorial, amd in general, seems to tend fowarls mity, the more lomogeneous the material is.
. $\quad$ In one and the same material, the dielectric-strength ration may vary considerahly with temperature, thickness, rate of voltage application, ete.
5. In generat, it seems that the mechanism of failure of insulation under high alternating voltage stress is materially different in some features from that under high direct voltage stress, and no miniversal and constant dielec-tric-strength ratio can therefore be expected, but dependent on the feature which dominates in the failure different values must result.

The dielectric-strength ratio has been defined in previous literature in two ways, cither as the ratio: Direct voltage divided by effective or root-mean-square value of alternating voltage (in which case air would have the ratio $\sqrt{2}=1.41$ ) or otherwise the ratio: Direct voltage divided by the peak value of alternating voltage, which gives to air the convenient ratio 1 . We use herein, and recommend for general acceptance, the latter definition, as more rational. It gives the value 1 to air, and in general the values tend toward 1, and it gives the value 1 , if the nature of the alternating voltage puncture is the same as that of the direct voltage puncture, since a direct voltage and an alternating voltage with the same peak value should be equivalent.

Although the values given in the following tables are the averages and abstracted from thousands of individual tests, made under the greatest possible precautions, so that the experimental errors are small, they are not so consistent as to draw final conclusions from single recorded values (though these values usually are averages of 10 or 25 tests), and the conclusions are drawn from the general trend of groups of individual values. The reason for variations in results is the inherently erratic nature of disruptive tests. Dielectric tests made with air can be duplicated within two to three per cent, but in liquids like oil erratic variations occur between successive tests made with all precautions, amounting to $\because 0$ per cent to 30 per cent and more. ${ }^{1}$ In solid insulation, the phenomenon of dielectric disruption apparently is still more complex, and the individual test results therefore are still more erratic, so that acceptable conclu-

[^69]sions can be drawn only from the comparison of the arerages of very numerous tests.

The results of this investigation seem inevitably to lead to the conclusion that the diclectric rupture under high-voltage stress is a far more complex phenomenon than is usually assumed. Puncture is not due to a mere effect of electrostatic stress, or a mere leating effect, or any specifie leterioration effect, ete., but it results from a number of different effects combined in different degrees. While it is somewhat disappointing no miversal " diclectric-strength ratio" can be determined, which is applicable to all conditions and all apparatus, we believe that dielectric-strength ratios can be derived for definite classes of insulation under definite operating conditions, and that the determination and study of the dielectric-strength ratio will give us an additional and powerful tool in the study of insulation failure and its causes.

## METHODS OF TEST AND APPARATUS

The principal source of high, direct voltage used in the tests was the kenotron. This is a two-element vacuum tube containing a filament cathode supported within a cylindrical plate as anode. The filament is kept incandescent by means of either a transformer or a storage battery. In operation the kenotron acts simply as a unidirectional conductor. passing through only the half waves of one polarity. Figs. 1, 2 and 3 show some of the principal circuits used for kenotron rectification. Fig. 1 is the simplest connection. In this the kenotron is in series with the supply transformer and a condenser storing the rectified voltage. This gives a direct current every second half cycle the vacuum becomes conducting. The principal advantage of such a connection is its simplicity, and if the load is small compared with the condenser capacity, the voltage is quite steady. Fig. 2 shows the bridge type of connection. This has the advantage of passing through both half waves in such a way that they produce the same polarity on the receiving circuit. Fig. 3 shows the full-wave or double-half-wave type which has the principal advantage of requiring an alternating voltage source of only approximately one-third of the direct voltage. The purpose of the condenser is to smooth out the pulsations of the direct voltage. It is readily seen that the half-wave connection, Fig. 1 , requires more capacitance than a full-wave connection, either Fig. 2 or Fig. 3. The cajacitance required for satisfactory smoothing is dependent on the load. In testing long cables
no capacitance additional to that of the cable is required. But laboratory tests on short lengths of cable or other test pieces of low electrostatic eapacity necessitate the use of the condensers shown. On account of the swall direct current conducted by any type of insulation the roltage fluctuation of such a rectifier can be reduced below 2 per cent without the necessary condensers becoming large.

Both the altenating and the direct-roltage data were taken on the same transformer. The direct roltage was obtained by means of the full-ware kenotron connection, Fig. 3, using sufficient capacitance in parallel with the sample to reduce the ripples in the voltage wave to less than 2 per cent under the conditions of tests. In taking all spark voltage values special attention was given to the rate of increasing the roltage. keeping this rate as nearly the same as possible at the value noted in the data.
without then taking an equal number on direct voltage or vice versa so ats to give the closest possible comparion Each value given in the tabulations is usually the averane of 10 to 25 tests. Practically all of the wests were repeated at different times 1 dife difent operators and under different experimental conditions.

## RESULTS OF TESTS

## A. Oil, Petrolatum and Cable Paper

A series of tests were made on the materials entering the insulation of high-potential cables, such as petrolatum and cable paper, and the results of these tests are given in


Fig. 3. Full-wave Kenotron Rectifier Connection Requiring an Alternating Voltage of but One-third the Direct Voltage

The various types of insulation were tested in various forms and shapes and with various electrodes but care was always taken to have no sharp corners or edges on the electrodes. All roltage readings were taken on the low side of the supply transformer and the high-tension voltage, whether alternating or direct, was obtained from a calibration curve which had been made against a sphere gap in parallel with the sample or an equivalent load. All direct-roltage data below 3000 rolts were taken on a special direct-current generator with field control, the roltage being read br an indicating roltmeter in series with multiplying resistance. Whenever possible both alternating and direct roltage punctures were taken on the same sample of insulation. For instance. if the sheet of insulation under test was large enough for 10 puncture tests, 5 would be taken on altemating and 5 on direct roltage. At no time were more than $j$ punctures taken on alternating voltage

Table I. In the same table are also siven the results with transil oil No. 6, as of similar character to petrolatum but far more fluid. Oil and petrolatum were tested between 2.54 cm . spheres, but cable paper was tested between 5 cm . plates. The alternating voltage values are the maximum of the voltage wave.

The table gives the tested materials: Transil oil No. 6 alone, petrolatum alone. manila paper of 0.2 mm . thickness in air dry condition alone, and the same paper impresnated with petrolatum. The table also gives the length of the gap betwreen the spheres for oil and petrolatum, and the number of larers of cable paper used. Then it gives the approximate rate of voltage increase in per-cent-per-second of the puncture voltage. Then follow the values of direct voltage in kilorolts. and of alternating voltage, peak values for the four temperatures 2.5 .50 .75. and 100 der. C.. and finally in the four last columns, the values of the "dielectric-strensth
ratio" derived by dividing the diene voltage be the alternating voltare. As seem, values are eiven for there rates of increase in terms of the pencture voltage as follows: 20, $\overline{5}$, and 0.1 per eent rise of this voltage per second. Each of the mumerical values given in Table 1 is the axerage of a minimum of 10 to 25 olservations, but in many cases as many as a hundred repetitions were made.
a. Oil. The table shows incidentally that the dielectric strength of oil, with direct voltagy is well as with alternating voltage,

A Comparison of Ratios at Different Temperatures. The combined averages of all the rations at 25 and 50 der. C . is $K=0.900$; but the combined averages of all the ratios at 75 and 100 deg. $C$. is $R=0.947$. This change shows that the dielectric-strength ratio increases with increasing temperature or, as we may say, becomes more normal at higher temperatures by approaching closer to the value of unity.

Ratios at Different Gap-Lengths. The average ratio for the short oil gap is $K=0.975$; the

TABLE I
OIL, PETROLATUM AND CABLE PAPER

| Material | Elec. trodes | Length of git $p$ mm. | Rate of voltage rise per cent per sec. | Direct voltage kv. |  |  |  | Alternating voltage kv . |  |  |  | Dielectric-strength ratio |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 25 deg . | 50 acg . | 75 deg . | 100 deg . | 25 deg. | 50 deg. | 75 deg. | 100 deg. | 25 deg . | 50 deg. | 75 deg . | 100 deg . |
| $\begin{aligned} & \text { Transil oil } \\ & \underset{N o}{ }{ }^{2} \mathrm{n} \end{aligned}$ | $\frac{2.54 \mathrm{~cm}}{\text { spheres }}$ | 2 4 2 4 | 5 5 2 2 2 | 30.5 45.8 20.7 36.7 | $\frac{28.8}{37.5}$ | 27.6 36.2 20.5 37.0 | 19.9 34.0 | 32.9 53.9 25.4 49.0 | 27.2 45.0 | 27.0 40.4 19.5 42.9 | 25.3 37.7 | 0.927 0.864 0.815 $(.755)$ | 1.059 0.83 | 1.022 0.896 1.051 0.862 | (0.785) 0.902 |
| Petrulatum | 2.54 cm . spheres | 2 | 5 | 15.1 <br> 27.6 | 15.6 | 17.8 34.8 | 15.1 28.2 | 15.9 28.9 | 22.7 | 18.4 35.9 | 15.9 29.6 | $\begin{aligned} & 0.950 \\ & 0.955 \end{aligned}$ | ( .687) | 0.967 0.969 | $\begin{aligned} & 0.950 \\ & 0.953 \end{aligned}$ |
|  |  | No. of layers |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Cable Paper 0.2 mm . thick air | $\begin{aligned} & 5 \mathrm{~cm} . \\ & \text { plates } \end{aligned}$ | 4 | 20 | 4.3 | 3.4 | 3.6 | 3.2 | 2.4 | 2.5 | 2.3 | 2.2 | 1.790 | 1.360 | 1.565 | 1.445 |
|  |  | 8 | 20 | 9.0 | 8.4 | 7.7 | 7.0 | 7.0 | 6.6 | 5.5 | 5.5 | 1.286 | 1.273 | 1.400 | 1.273 |
|  |  | 16 | 20 | 17.3 | 12.8 | 12.7 | 13.1 | 16.1 | 12.0 | 11.6 | 9.7 | 1.075 | 1.067 | 1.095 | (1.340) |
|  |  | 32 | 20 | 33.1 | 26.6 | 24.5 | 26.5 | 30.5 | 28.0 | 28.0 | 28.0 | 1.085 | 0.950 | 0.875 | 0.946 |
|  |  | 4 | 5 | 5.4 | 4.84 | 5.47 | 4.4 | 4.19 | 4.15 | 4.25 | 4.33 | 1.290 | 1.176 | 1.287 | 1.016 |
|  |  | 8 | 5 | 7.6 | 7.5 | 8.7 | 9.0 | 7.39 | 7.32 | 8.97 | 8.72 | 1.028 | 1.025 | 0.969 | 1.032 |
|  |  | 16 | 5 | 14.0 | 13.0 | 15.2 | 15.2 | 12.8 | 12.9 | 13.6 | 15.3 | 1.094 | 1.078 | 1.117 | 0.993 |
|  |  | 3: | 5 | 22.5 | 13.1 | 15.3 | 20.3 | 18.7 | 13.2 | 15.6 | 20.7 | 1.203 | 0.992 | 0.981 | 0.981 |
|  |  | 4 | 0.1 | 5.3 | 4.7 | 4.5 | 4.0 | 4.5 | 4.1 | 4.2 | 4.0 | 1.178 | 1.147 | 1.072 | 1.000 |
|  |  | 8 | 0.1 | 9.2 | 9.4 | 7.8 | 8.3 | 8.8 | 7.8 | 7.8 | 7.8 | 1.045 | 1.205 | 1.000 | 1.064 |
|  |  | 16 | 0.1 | 15.5 | 13.6 | 12.7 | 13.5 | 16.3 | 14.7 | 14.0 | 14.3 | 0.951 | 0.925 | 0.907 | 0.944 |
|  |  | 32 | 0.1 | 27.5 | 25.5 | 24.3 | 22.5 | 31.5 | 29.7 | 28.9 | 28.3 | 0.873 | 0.858 | 0.841 | 0.774 |
| Cable Paper 0.2 mm . thick. impregnated with petrolatum | . cm . plates |  |  |  |  |  |  |  |  |  |  | 2.470 |  |  |  |
|  |  | 2 | 20 | 18.3 | 19.0 | 15.0 | 15.1 | 6.6 | 10.6 | 8.7 | ${ }^{7} 8$ | 2.775 | 1.793 | 1.725 | 1.940 |
|  |  | 4 | 20 | 31.0 | 41.5 | 39.3 | 29.5 | 15.8 | 25.3 | 24.6 | 20.3 | 1.960 | 1.635 | 1.605 | 1.453 |
|  |  | 1 | 5 | 9.4 | 8.0 | 6.7 | 7.5 | 7.0 | 6.5 | 5.6 | 6.5 | 1.343 | 1.232 | 1.197 | 1.154 |
|  |  | 2 | 5 | 36.0 | 22.8 | 17.7 | 22.4 | 18.2 | 15.9 | 14.3 | 13.6 | 1.980 | 1.435 | 1.238 | 1.650 |
|  |  |  | 0.1 |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | $\frac{2}{4}$ | 0.1 | 16.2 | 14.4 36.5 | 13.8 34.0 | 14.7 | ${ }^{7} .0$ | ${ }_{20}^{7.3}$ | 88.0 | 8.5 | 2.314 1.900 | 1.975 1.795 | 1.725 | 1.735 1.253 |
|  |  | 4 | 0.1 | 29.5 | 36.5 |  | 25.6 | 10.0 | 20.3 | 21.7 | 20.0 | 1.900 | 1.795 | 1.570 | 1.253 |

decreases somewhat with increasing temperature, but not to any great extent.

As would be expected from the erratic behavior of oil, the values of the dielectricstrength ratio of the oil, given in the last four columns, differ from each other more than any possible error of observation. However, in general the data show fairly conclusively a dielectric-strength ratio somewhat below unity, specifically a general average of $R=$ 0.923. In other words, this ratio of 92 per cent indicates that oil has a greater dielectric strength under alternating than under direct roltage, by about $\$$ per cent.
average ratio for the long gap is 0.871 . This difference shows conclusively that the dielectric strength ratio of oil seems to become more abnormal, that is, differs more from unity, with increasing length of oil gap. This conclusion, however, requires further corroboration.

Ratios as Affected by Rate of Increase of Voltage. For the slower rate of increase of voltage, 2 per cent per second, the ratio averages $R=0.909$; for the faster rate of 5 per cent per second it averages $R=0.929$. The conclusions drawn from this small change of 2 per cent also require further corroboration.
b. Petrolatum. Petrolatum is stated to be an amorphous hydrocarbon, essentially of the paraffin series. At room temperature it has the consistency of vaseline, and as a closety related hydrocarbon it shows the same general characteristics as transil oil.

As seen from Table I, the dielectric strength of petrolatum, under direct or alternating voltage, does not appreciably change with the temperature, between 2.5 and 100 deg. C., nor is there appreciable change in the dielectricstrength ratio.

The averages of the dielectric-strength ratio, taken from the table:

| At: | 2.5 deg. | 75 deg. | 100 deg. C. |
| :--- | :---: | :---: | :---: |
| $R=$ | 0.952 | 0.968 | 0.952 |

Thus the ratio is essentially constant.
Again as regards variation in gap-length:
At: $\quad 2 \mathrm{~mm}$. 4mm. length of gap between spheres:
$R=0.9 .560 .9 .59$ respectively, which is also essentially constant over this small range of gap.

The average of all values of dielectricstrength ratio for petrolatum is: $R=0.957$. Therefrom it is evident petrolatum shares with oil the characteristic that its dielectric strength is less for direct voltage than for alternating voltage, but the difference is not so great.

If the abnormal behavior of oil were due to differences in the mechanical motion produced in the ingredients of its unhomogeneous structure by the continuous dielectric field, the resultant concentration of the weaker ingredients might account for its lesser strength under the continuous direct voltage than under the alternating voltage stress, and the far more viscous petrolatum would show still less the effect of any movement and concentration-as is, in fact, the case.
c. Dry Cinimpregnated Cable Paper. Incidentally tests with direct and alternating voltage show no definite difference in effect on the dielectric strength of cable paper, within the range of temperature and rate of voltage rise used in the tests. But there is a very pronounced effect on the dielectric-strength ratio, as seen from the three sets of values in the last four columns of the table which tabulate 45 results, each the average of a number of tests. Ratios are given for the three general factors; riz., for temperatures from 25 to 100 deg. C., for thickness from 4 to 32 layers of 0.2 mm . paper, and for rates of roltage rise from 0.1 of 1 per cent per second to 20 per cent per second. Although individual values may fall somerwat out of
line, there is a very pronomaced gromping of the results. The highest values of dieloetricstrength ratio oceur at the lowest comperature, at the lowest thickness and at the highest rate of voltage rise (shown in the table at the top left-hand corner). On the contrary, the lowest values of the ratio occur at the highest temperature, the thickest insulation, and the slowest rate of voltage rise (shown at the bottom right-hand corner). It is interesting to note that with dry paper, unlike oil, the ratio extends to both sides of unity. There are some values materially above 1 , and there are also values below 1 .

To get the general trend of variation of the ratio, with each separate feature, we average all the values for the same temperature, or for the same thickness, or for the same rate of voltage rise, and thus get the effect of one variable, segregated from the effect of the others. This grouping of data gives the following results:

Temperature, Thickness, and Rate Data for Dry L'nimpregnated Cable Paper.
Temperature: 25 deg .50 deg .75 deg .100 deg. Average ratio: $R=1.158 \quad 1.088 \quad 1.0921 .057$ There is a consistent decrease of ratio with increasing temperature.

| Thickness: |  | 4 | 8 | 16 | 32 layers |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Average ratio: | $R=$ | 1.277 | 1.133 | 1.027 | 0.947 |

There is a consistent decrease of ratio with increasing thickness, from values considerably above 1 to values below 1 .
Rate of volt-
age rise: $\quad 20$ per cent 5 per cent 0.1 of 1 per cent per sec.
Average ratio:

$$
\mathrm{R}=\begin{array}{llll} 
& 1.231 & 1.079 & 0.987
\end{array}
$$

There is a consistent decrease of ratio with decreasing rate of roltage application, down to values below unity.

The total average of all the values of the dielectric-strength ratio of cable paper is slightly above unity: $R=1.100$. In other words, dry cable paper shows a slightly lesser dielectric strength for alternating than for direct voltage. Conversely stated, unimpregnated paper requires, on an average, a 10 per cent higher direct voltage than the peak alternating voltage to puncture the same thickness of paper under otherwise identical conditions.

Since a laminated structure, consisting of a number of layers of unimpregnated cable paper, thus shows also a small deviation from the normal dielectric-strength ratio but opposite to that of either oil or petrolatum, it is of interest to consider the combination of
both: i.e. (able patper impregnated with the iasulat mas hydrocarbon.
d. Cibhli l'uper lmpresmated with l'etroletam. If matreatod cable paper (with a diclec-tric-strength ratio slightly above maty; viz. 1. 1001 ) is inmproghated wilh petrolat mom (which alome bas a ration shaghty below unity, vi\%, $0.95)^{6}$ wight expeet as a result of the combination of the two a ratio close to mity. ()n the contrary, the tests of imprecrated paper show consistently very high ratios, much hisher indered than dry paper, and give an average ratio $K=1.773$.

This result is vory startling and its significance on insulation strength and failure is still far from being understood. The phenomenon of extra high ratio has, however, been checked and corroborated with data on several other materials of similar character.

Significant also is another factor, the enormots increase of dielectric strength due simply to impregnation of the paper.

To get the general trend of the variation of the dielectric-strength ratio with the three controllable variables, viz., temperature, thickness, and rate of voltage application, the tabulated data are again grouped for the purpose of comparison.

Temperature, Thickness, and Rate Data for Cable Paper Impregnated with Petrolatum.
Temperature: 25 deg .50 deg .75 deg .100 deg . Average ratio: $R=2.038 \quad 1.644 \quad 1.510 \quad 1.531$
Thus the ratio consistently decreases with increasing temperature.

| Thickness | 2 | 4 layers |
| :--- | :---: | :---: |
| Average ratio: $R=$ | 1.857 | 1.646 |

Thus the ratio decreases with increasing thickness.
Rate of volt-
age rise: $\quad 20$ per cent 5 jer cent 0.1 of 1 per cent per sec.
Average

$$
\text { ratio: } R=1.861 \quad 1.576 \quad 1.783
$$

Thus the general trend is apparently that the ratio decreases with increasing slowness of voltage application, although the slowest rate shows a partial recovery.

This last group of data illustrates the difficulty of the investigation of the action of solid insulating material and emphasizes the complexity and limited knowledge of the phenomena occurring in insulating materials under clectric stress. The values averaged in the middle figure ( 1.576 at 5 per cent rate) were taken some weeks before the other two sets of tests, and while apparently the same materials were uscd and treated in the same manner and the general trend of variation is
the same, at considerable difference oreurs in the mumerica! values.

It is interesting to note that the ratio of direct voltage to peak alternating voltage of petrohatum-impregnated cable paper, $K=$ 1.773, in the comparison of direct voltage with the root-mean-sguare value results in the ratio $\sqrt{2}(K=1.773)=2.50) 1$. This value is the same as has been proposed as the results of extensive tests made abroad on cables.

## B. Mica and Glass

Table It gives data on some inorganic insulation, such as mica and its compositions, and also glass. The table gives the name of

TABLE II
MICA, GLASS AND PARAFFIN

| Material | Electrodes | $\begin{gathered} \text { Gap } \\ \text { cm. } \\ \text { length } \end{gathered}$ | No. of layers | Direct | Alternating | Dielec. str'gth ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | kv . per mm. |  |  |  |
| Clear Mica, 0.12 to 0.18 mm . thick. . |  |  |  | 100.5 | 98.0 | 1.025 |
| Pasted Mica, 0.32 to 0.3 .7 mm . thick. |  |  |  | 60.5 kv . | $\begin{gathered} 48.6 \\ \text { kv. } \end{gathered}$ | 1.24 .5 |
| Mica Tape on Brass Tube. |  |  | 2 | 14.05 | 8.55 | 1.64 |
|  |  |  | 4 | 34.9 | 21.9 | 1.59 |
|  |  |  | 8 | 70.7 | 45.1 | 1.57 |
| Mica Tape without sticking compound |  |  | 2 | 12.7 | 7.3 | 1.74 |
|  |  |  | 4 | 21.5 | 12.7 | 1.69 |
|  |  |  | 8 | 65.4 | 27.5 | (2.42) |
| Mica Tape with sticking compound |  |  | 2 | 24.5 | 9.6 | 2.55 |
|  |  |  | 4 | 48.1 | 20.2 | 2.38 |
|  | diam. |  |  | k 7 . pe | mm . |  |
| Glass Tubing 0.7 to 0.85 mm . thick. . . | $2.54$ |  |  | 68.0 | 46.3 | 1.469 |
| Powdered Glass.... | 2.54 | 1.90 |  | ${ }_{37}{ }^{\text {kv. }}$ | kv 44.5 | 0.832 |
|  | cm. | 2.54 |  | 51.9 | 53.8 | 0.965 |
|  | spher |  |  |  |  |  |
| Powdered Glass made into paste with No. 6 transil oil. . | 2.54 | 0.63 |  | 56.8 | 61.6 | 0.922 |
|  | cm . <br> spheres | 0.95 |  | 71.2 | 73.8 | 0.965 |
| Cast Paraffin 0.9 to 2.2 mm , thick .. . |  |  |  | kv. pe | mm |  |
|  |  |  |  | 17.4 | 16.8 | 1.036 |

the material, the data on sizes of electrodes, and either the gap length or number of layers; there are also the voltages of the tests using either direct or alternating voltage, and their ratio; i.e., the dielectric-strength ratio of these materials. Here, as in the preceding table, each numerical value is the average of a number of tests, usually 10 or 25 . For some of the materials, such as clear and pasted mica, glass, etc., the dielectric-strength is given in kilovolts per millimeter, so as to
compatio :he arerages of the difieremt tests made wht stightly different thicknesses of maternal

The Mheictric-Strength Rutio of Mica in Seacral Foms. Clear micagives a dielectricstrensth ratio very little ahose mity, that is. in pure mica the dielectric-stmenth is pactically the same for altemating as for direct voltage Possibly this low value of ratio indicates very low dialeetric losese Builtup or" pasted" mica, however already shows a materially lesser strength for altemating than for direct voltage, a ratio of $1.24 . \bar{\circ}$. Mica tape shows still much higher ratios and mica tape put thecther with some organic sticker shows

The Didetria-Straneth Kitho of bilues and Parafin. (ilase was latal, in the formon thin walled glas mbes. with meremry at immer
 Somewhat agamst wixectation, alan, as the average of a number of tests, grate a high ratio. vize. 1 the9. That it to say ylass ic dielectrically much stomger againct direct than against alternating voltage Whether this high ratio indicates a lack of homosencity of the structure of the glass-as a collomidal solution-we cannot yet judge.

The glass of the tubes was powdered and the powdered glass in air was tested between 2.54 cm . spheres Next. the powdered glass

TABLE III

## VARNISHED CAMBRIC AND PARAFFINED PAPER

| Materai, | Elec. <br> :roces | $\begin{aligned} & \text { No of } \\ & \text { iayers } \end{aligned}$ | $\begin{aligned} & \text { Rate of } \\ & \text { volt- } \\ & \text { 3ge rise } \\ & \text { heer cent } \\ & \text { per sec. } \end{aligned}$ | Direct volage kv. |  |  |  | Alternatmy whlage kv. |  |  |  | Drecueru-btumath ratio |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 25 deg . | 50 dcg . | $\therefore \mathrm{A}$ ce | 00 d | 25 deg | 30 ders | Fis der | 00 d | 2.5 dc | 30 des | $\therefore \mathrm{Fc}$ | 100 deg . |
| ```Black var- nished cam- bric 0.3 mm. (a=- phaitum base)``` | $\begin{aligned} & 5 \mathrm{~cm} \\ & { }_{5}^{2} \mathrm{lates} \end{aligned}$ | $\begin{aligned} & 1 \\ & 2 \\ & 2 \end{aligned}$ | $\frac{!}{9}$ | $\frac{21.8}{40.2}$ | 15.1 | 16.0 | 14.5 | $\begin{aligned} & 17.4 \\ & 29.4 \end{aligned}$ | 15.9 | 1.86 | 14.7 | $\begin{aligned} & 1.2 .3 \\ & 1.3654 \end{aligned}$ | 1.130 | 1.029 | 2.014 |
| Yellow var- |  | 1 2 4 | \% | $\begin{aligned} & 11.9 \\ & 19.3 \\ & 31.3 \end{aligned}$ | $\begin{aligned} & 14.2 \\ & 23.5 \\ & 43.1 \end{aligned}$ | $\begin{aligned} & 13.6 \\ & 21.0 \\ & 39.4 \end{aligned}$ | $\begin{aligned} & 12.0 \\ & 19.2 \\ & 30.8 \end{aligned}$ | $\begin{aligned} & 11.1 \\ & 17.3 \\ & 26.5 \end{aligned}$ | $\begin{aligned} & 19.6 \\ & 22.4 \\ & 41.1 \end{aligned}$ | $\begin{aligned} & 11.5 \\ & 22.2 \\ & 32.4 \end{aligned}$ | $\begin{aligned} & 11.7 \\ & 19.4 \\ & 25.6 \end{aligned}$ | $\begin{aligned} & 1.072 \\ & 1.116 \\ & 1.176 \end{aligned}$ | $\begin{aligned} & 1.127 \\ & 1.062 \\ & 1.049 \end{aligned}$ | $\begin{aligned} & 1.148 \\ & 1.0 .54 \\ & 1.215 \end{aligned}$ | $\begin{aligned} & 1.026 \\ & 0.9696 \\ & 1.074 \end{aligned}$ |
| nished cam 0.2 mm . dinseed oi? base |  | 1 2 4 | 5 5 9 | 3.9 .4 | 20.1 36.0 | 14.0 27.6 43.5 | 9.5 21.8 | ${ }_{2}^{14.4}$ | 1.5 .0 27.1 | $\begin{array}{r} 9.2 \\ 29.7 \\ \hline 22.2 \end{array}$ | $\begin{aligned} & 10.2 \\ & 22.0 \end{aligned}$ | 1.347 1.29 .3 | $\begin{aligned} & 1.340 \\ & 1.329 \end{aligned}$ | $\begin{aligned} & 1.525 \\ & 1.216 \\ & 1.031 \end{aligned}$ | $\begin{aligned} & 0.932 \\ & 0.990 \end{aligned}$ |
|  |  | 12 | $\frac{2}{2}$ | $\begin{aligned} & 21.2 \\ & 38.8 \end{aligned}$ | ${ }^{18.0}$ | $\begin{aligned} & 11.5 \\ & 22.5 \end{aligned}$ |  | 14.4 24.2 | $\begin{aligned} & 13.9 \\ & 23.5 \end{aligned}$ | $\begin{array}{r} 9.8 \\ 22.4 \end{array}$ |  | $\begin{aligned} & 1.472 \\ & 1.600 \end{aligned}$ | $\begin{aligned} & 1.295 \\ & 1.350 \end{aligned}$ | $\begin{aligned} & 1.173 \\ & 1.005 \end{aligned}$ |  |
| Cable Paper 0.2 mm . impreg. mated rith paraxin |  | $\underline{1}$ | 5 | $\begin{aligned} & 20.1 \\ & 32.3 \end{aligned}$ |  |  |  | $\begin{aligned} & 1.4 .0 \\ & 22.4 \end{aligned}$ |  |  |  | $\begin{aligned} & 1.437 \\ & 1.442 \end{aligned}$ |  |  |  |

very high values. Acomparison is made in the following averages:


Therefore the combination of two different materials in a laminated structure. here as in the preceding Section A for impregnated paper seems to raise the ratio. The ratio increases with the increase in the difference between the materials.

Apparently there is also a slight decrease of ratio with increasing thickness of the insulation. such as observed in the preceding studies.
was mixed with No. 6 transil oil to form a paste, and this paste tested between 2.54 cm . spheres. Both the glass powder with the spaces between the particles filled with air. and that with the spaces filled with oil, show a dielectric-strength ratio slightly below unity (total arerage 0.921 ). That is. glass in solid form has a much greater dielectric strength for direct than for alternating voltage; as powder, however, its dielectric strength is less for direct than for alternating voltage. The explanation of this difference is still unknown.

In the same table have been added the averages of a number of tests made on thin cast disks of paraffin. They show a ratio close to unity, riz.. 1.036. This result seems reasonable.

## C. Varnished Cambric and Paraffined Paper

Table ill gives data on two kinds of insulat ing cloth black and yellow varnished cambric, and cable paper impregnated with paraffin. Cable paper inpregnated with paralfingives ingeneral the same characterist ic as cable paper impregnated with pet rolat 1 m , as might be expected, i.e., a high value of the ratio.

The data on both kinds of varnished eloth seem to show a decrease of dielectric strength with increasing temperature, and also a decrease of the dielectric-strength ratio with increasing temperature and possibly also with increasing thickness. Thus, grouping the average values as was done in previous cases, the results are as follows:

Tomperature and Thickness Data for V'ellow Varmished Cloth.
 Average Ratio: $R=1.297 \quad 1.222 \quad 1.171 \quad 1.003$ Thickness: $1 \quad 2 \quad 3$ layers Average Ratio: $R=\begin{array}{llll}1.231 & 1.193 & 1.080\end{array}$
The whal average is $R=1.18 t$.
The similarity of the change of the ratio in varnished cloth, with that in impregnated paper, raises the question whether it is not a general characteristic of compound laminated structures to have a high dielectric-strength ratio at low temperatures, low thicknesses, and high rates of voltage rise, and conversely to have this ratio decrease with increasing temperature, increasing thickness, and increasing slowness of voltage application.

# Periodic Inspection, Cleaning, and Testing of Alternating-current Generators 


#### Abstract

Offhand, it would appear as if those in charge of electrical machinery would realize that regular and efficient inspection and cleaning are essential to the satisfactory performance of the equipment. A recent survey of the field, however, revealed an astonishing lack of appreciation of the importance of this branch of maintenance work and also a wide divergence in its mode of conduct.

Because the lack of proper care in operation almost always results in expensive repairs, the precautionary measures and other instructive information in this article should be found to be of value.-Editor.


There is a great divergence of practice among operating companies in regard to the periodic inspection, cleaning, and testing of alternating-current generating equipment The following suggestions are made in the hope that they may serve as a basis for more uniform practice in these important items of maintenance.

## Inspecting

One of the fundamentals of successful operation of electrical generating equipment is frequent, thorough, and systematic inspection. Such inspection will often give warning of approaching trouble and thus allow the operator to take precautions that will prevent a serious breakdown and consequent damage to the generating equipment.

It is the practice of some operating companies to inspect all generators each day. This is an excellent precaution and highly recommended. It is understood that operating conditions may not permit such frequent inspections, but nothing should interfere with the thorough inspection of each machine as soon as it is shut down. No definite rule can be laid down, but the principle should be recognized that frequent inspections are vital
to the proper maintenance of all generating equipment. All inspections should be thorough. While a casual inspection is perhaps better than none, the value of an inspection depends on the care used in making it.

The inspection should always include the armature windings and field coils of the main generator in so far as they are visible and accessible, the armature, field coils, and commutator of the exciter (if there is one), the collector rings, all brushes and brush-holders, bolts, nuts, dowels and all other mechanical and electrical parts and fittings. Lubricating oils are injurious to insulations and also to concrete foundations, and all bearings and oiling systems should be examined for oil throwing and leaks. In the case of steam turbines, the turbine itself so far as possible, and the valves, valve gear, governor, throttle, and other parts should be included.

Haphazard inspection by anyone in the plant cannot be considered systematic. A definite routine of inspection should be standardized and every part should be taken up in order. Station superintendents should compile a list of all parts subject to inspection, and insist that inspectors use this list, checking off each item as it is examined. The inspector
should be thoroughly familiar with what to look for and shoukt be drilled in his work so as to guard as much as possible against the omission of any part

## Cleaning

All goncrating equipment will acoumulate dust and dirt in the course of time; even the use of air washers does not altogether eliminate this trouble. This dust and dirt lodges in the air ducts and on the ends of the windings, interfering with the free circulation of the cooling air and the radiation of heat from the windings, and at the same time increases the fire hazarl.

The life of generating equipment may be prolonged by frequently blowing out the dirt with compressed air. In large turbinegenerators this is a difficult matter, if indeed it is possible. owing to the design of the generator frame and end bells. On other types of machines. however, such as waterwheel generators, the air ducts and windings are more exposed and are accessible to this form of cleaning. If possible, the compressed air should be used every day but, before doing so, care should be taken to make sure that the air stream is free from water. If it is not conrenient to shut down a machine, such blowing out as is possible can be done while the machine is ruming.

All generating equipment should be thoroughiy cleaned once a year or more, if operating conditions are such as to require it. Special attention must be given to machines operating in localities where the air is contaminated with dust, lint, coal dirt, cement dust, and the like. Under such conditions, arrangements should be made for a thorough cleaning at frequent intervals. To insure that this periodic cleaning be thorough, the end bell covers and similar parts should be taken off to expose fully the end turns of the windings and the air ducts. The revolving field should also be removed, so that it can be cleaned and examined, and at the same time permit the cleaning and inspection of the inside of the armature.

Loose dirt can be removed by wiping, brushing, the use of compressed air, bellows, or by some form of vacuum cleaner. Should dirt and dust be lodged with oil, it may be remored with gasoline, benzine, or carbon tetrachloride. In using any of these, limit the quantity to that required for the purpose in hand. Too much liquid is liable to flush the dirt into inaccessible places. After using any of these solvents, all the surfaces to
which they have been applied shonuld be carefully and thooroughly dried Care should be exercised when using yasoline or benkine because of their inflammable properties. Special attention should be given to ventilation, not only because of the danere of explosion but also because the fumes of all three are injurious to the workman, particularly if working in a pit where fumes are likely to collect. In using gasoline, care should be taken to obtain a good quality, since a poor quality is liable to leave a coating of oil or other substance on the windings and in inaccessible places, which will cause the rapid accumulation of dirt and dust. Test all gasoline by allowing a small quantity to cvaporate in a porcelain dish. If the quality is good, no residue or odor will remain. After cleaning and before re-assembling the parts, spray the exposed windings with a high grade of airdrying insulating varnish. While the machine is disassembled, all electrical parts and connections and all mechanical parts should be carefully examined and such tests applied as may be considered advisable.

## Testing

No definite rules can be established for testing generating equipment which has been in operation for any length of time. The permissible test depends particularly on the age of the machine, on the character of the service to which it has been subjected, and on the type of insulation used on the windings. All insulation deteriorates with age and use. particularly where organic material forms a large part of the total. An old machine or one that has been subjected to severe operating conditions will not stand, nor should it be subjected to, the same test that might be applied with safety to a comparatively new machine.

There comes a time in the life of all equipment when the deterioration reaches the point of breakdown and, when this occurs, expensive repairs are usually the result. For the purpose of enabling operators to determine the approach of this time, various tests have been derised and are now in use.

The ordinary so-called megger is frequently used to measure the resistance of insulation. The results obtained are difficult to interpret owing to the many varying factors that must be considered and for which due allowance must be made in the results. The voltage of the megger is usually low compared to that of the machine being measured and this also tends to limit the accuracy of the measurcment. Despite these objections, however, the
megger is very widely used among openators and some clains are made of great bencfits from the use of this device.

The combination of high voltage (at last as high as that of the machine in test) and direet current gives the most effective results. This combination is best obtained by the kenotron measuring set. With this set, the true leakage current is measured and the readings are not influenced by the detrimenta! effects of the alternating-current voltage supplied loy the small generators of the megger and similar instruments. If insulation tests are to be relied upon to give warning of coming trouble, the kenotron is recommended as giving the most accurate and reliable results.

There frequently arises the question of applying a high potential test, or what might be called a generated overvoltage test (running the generator at overvoltage byincreasing the excitation or speed, or both) to determine the condition of the insulation. The answer must take into account the various insulating materials used, the age of the machine, and the operating conditions, particularly regarding overloading and periodic examination and cleaning. General approval in the abstract, at least, will be accorded the statement that "the insulation of all generating equipment should be maintained in such condition as to withstand safely the application of a 50 per cent overvoltage test." Whether such conditions can be maintained and whether such a test is desirable are questions difficult to answer. Not until operating conditions are standardized and operators' ideas on this subject correlated, can a satisfactory answer be obtained. The following tests have been used successfully under various operating conditions and will no doubt be of interest.

After the generators have been carefully examined and thoroughty cleaned, they have been run on open circuit with sufficient excitation to raise the terminal voltage about 25 per cent above normal for five minutes. After that lest, the voltage has been reduced to normal and the several terminals grounded in succession. In making this test, arrangements must be made to break the field current instantly in case of failure.

This test is more searehing than the application of an equivalent alternating-current potential from a testing transformer. The latter or so-called high potential test is usually made between the windings and ground, whereas the generated voltage test described is in reality a test from turn to turn, from coil to coil, and from phase to phase.

A test frequently used on the windings of revolving fields is to subject them to two or three times normal exciting voltage, applied between one terminal and the shaft. The test should be applied while the field is running at normal speed and may be made with either direct or alternating current as may be most convenient.

High potential tests using a testing transformer vary widely among different operators. Tests are required on armatures ranging from 10 to 60 fer cent over normal and are applied for periods of time varying from one to 30 minutes. On revolving fields, voltages up to six times normal are applied for widely varying periods.

When attempting either the generated voltage or the familiar high potential test, the windings should be exposed as much as possible so that any failure can be seen immediately and the test voltage instantly removed.

LIBRARY SECTION
Condensedreferences to some of the more important articles in the tech． nical press，as selected by the G－E Main Libsary，will be listed in this section each month．New books of interest to the industry will also be histed．In special cases，where copy of an article is wamted which can－ not be olstained through regular channels or local libraries，we will sug． pest other sources on application．

## Arc Welding

Applications of Arc Wrelding to Ship Construction． Ewertz，E．H．
Mar．Engng．，July，1923；••2s，pp．420－424，440．
（A review of the subject in general，prepared under the auspices of the American Bureau of Welding．Serial．）

## Car Lighting

Principles of Car Lighting by Electricity．Stuart， Chas．II．T．
Rwy．Elec．Engr．．July，1923；v．14，pp．199－20．5．
（＂A comprehensive description of the parts and operation of the USL．Type C equip－ ment and the l．R．R．type．＂）

## Carrier－Current Communication

Emergency Communication hy Guided Radio Telephone．D＇Alton，l：K．
Bul．of Hyd．Pr．Comm．of Ont．，June，1923；•• $10,1 \mathrm{p}, 1 \times 3-102$

## Cars，Electric

Single－phase．Type Ce $4-6$ Motor Cars of the Swiss Federal Railways．（In German．）
Schweiz．Bau．，July 7,1923 ；v．82，pp．13－16．
（11lustrated description．Serial．）

## Condensers，Static

Use of Static Condensers for the Improvement of Power－factor．Mever，G．IV．（In German． Trua，July 1，1923；ゾ．4，pp．243－247．
（Advantages，mechanical and electrical de－ sign，etc．）

## Corrosion

Rapid Corrosion of Condenser Tubes．Bengough， Guy D．，and May，R．
Engr．，July 6，1923：́．136，pp．T－10．

## Electric Cables

Current Loading of Cables．Melsom，S．WV．
Beama．July，1923：v．13，1pp．30－36．
（Author is connected with the National Physical Laboratory in England．Serial．

## Electric Current Rectifiers

Mercury Vapor Rectifiers for Street Railway Systems．Odermatt．A．（In French．
Ind．des Tram．，June，1923：v．17，pp．197－216．
（Estensive，illustrated report presented be－ fore the Congrès International de Tram－ ways，at Brussels，October，1922．）

## Electric Distribution

Sources of Power for Three－wire Direct－current Systems．Hancock，M．S．
Elec．Jour．，July，1923：v．20，pp．267－269．
（Discusses three ways of supplying power to a three－wire system．）

## Electric Drive Paper Mills

Electric Drive for Sectional Paper Machines． Cordes，O．©
Elec．Jour．，July，1923；ソ． 20 pp．236－241．
Electric Drive Power Plant Auxiliaries
Alternating－current Versus Direct－current Motors for Stoker Drive．Douglas，W．E．，and Bates，Harry H．
Power，July 3，1923；v．58，pp．8－9．

## Electric Heating，Industrial

Application of Electricity for Heating Purposes． Zeulmann．Edgar．（In German．）
Zeit．des Ter．Deut．Ing．，June 23，1923；•．67， 1 1 ．617－622．
（Illustrated review of industrial electric heat－ ing processes．）

Electric Locomotives
Service Records of Electric Locomotives and Motor Cars．
Elec．Trac．，July，1923；๙．19．pp．347－349
（A enllection of operating experiences on seven electrified lines．）

Electric Measurements
Measurement of a Single－phase Load at a Low Power－factor．Dorjikov，A．
Elec．Jour．，July，1923；v．20，pp．258－261．

## Electric Meters

New Development in Alternating－current Instru－ ments．NacGahan，Paul．
Elec．Jour．，July，1923；r․ 20，pp．252－257．
Discusses the design of a new and complete line of instruments operating on the dyna－ mometer principle．

Electric Motors，Induction
Starting Torque and Current of Squirrel－cage Induction Motors．Wall，T．F．
Elec．Rez．Lond．July 13，1923；ソ．93，pp． $4-46$

Electric Motors，Railroad
Selecting a Railway Motor for a Given Cycle of Duty．Gurdon，IV．G．
Elec．Rwy．Jour．，July 14，1923；v．62．pp．62－64．
Abstract of paper before the Canadian Electric Railway Association．）

Electric Motors，Synchronous
Autosynchronous Motors．Lindstrom，A． Elec＇n．July 6，1923；v．91；pp． $4-$ \％．
＇Serial．

## Electric Transformers

Care and Gperation of lower Transformers from the Stampoint of Those in Charge of Their Installation and Mantenance.
Ind, Eingr., July, 1923; v. 81, pp. 318-355.
(Recommendations of Electric Power Club.)
Ratio Regulating Traps of Transformers. Bunct, 1'. (In French.)
Ketur (ićn. de l'lilec., July 7, 192:3; v. 14, pp. 17-27.
(Disensses mechanical and clectrical difficalties oceasioned by (ransformer taps.)

## Electric Transmission Lines

Spacing and Wire Stresses of Catenary Supporting Structures. McGee, P. A.
Elec. Jour., July, 1923; v. 20, pp. 248-252.
(With reference to wind load effect.)
Underground Transmission at 44 Kv . Dennis, R. E., and Searing, H. R.

Elec. II'ld., July 1f, 1923; v. S2, 11p. 6.7-69.
Electrical Machinery-Parallel Operation
Parallel Operation of Direct-current Generators. Hancock, Scott.
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Cooling of Turbo-generators. Luke, George E. Elec. W'/d., July 14, 1923; v. 82, pp. 70-72.
Electricity-Applications-Domestic
Domestic Refrigerating Machine.
Ice Eo Refrig., July, 1923; v. 65, pp. 1-7.
(Discusses relative operating costs of mechanical and ice refrigeration. Gives list of manufacturers with illustrations and descriptions of their products. Serial.)

## Feed Water Heaters

Effect of Feedwater Heating on Plant Economy. Bell, G. G.
Mech. Engng., July, 1923; v. 45, pp. 417-420, 429.

## Frequency Changers

Reduction of the Frequency of Alternating Currents by Means of Lamps with Cathode Emission. Blusson. (In French.)
Revue Gén. de l'Elec., July 7, 1923; v. 14, pp. 7-16.
(Summary of theories of a frequency changer involving mercury vapor arc principles. Serial.)

## Heat Transmission

Laws of Heat Transfer.
Engng., July 6, 1923; v. 116, pp. 1-3.
(Serial.)
Hydro-electric Development
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Mech. Engng., July, 1923; v. 45, pp. 410-416.
(Present and projected developments; also data on the Queenston-Chippawa plant.)

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Electric Traction Interference with Telegraph Circuits. Thorrowgood, W. J.
Rwy. Gaz., July 6, 1923; v. 39, pp. 19-20.
(Short account of a system used on the Italian State Railways for preventing inductive interference.)

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Desirable Duplication and Safeguarding in the Electrical Equipment of a Gencrating Station. Sims, William F'.
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Disturbing Effects of the Electric Ignition Systems of Internal Combustion Engines Upon Radio Reception Aboard Aeroplanes. Kulebakin, V. S. (In German.)
Elek. Zeit., June 7, 192:3; v. 44, pp. 537-541.
(Describes ordinary ignition systems for aviation engines, discussing their ill effect upon radio reception and remedies therefor.)
Ready Reckoner for Wave-length, Inductance and Capacity. Hobbs, E. J.
Wireless Wld. © Radio Rev., July 14, 1923; v. 12, pp. 472-476.

## Radio Stations

Electrical Plant of Transocean Radio Telegraphy. Alexanderson, E. F. W., and others.
A.I.E.E. Jour., July, 1923; v. 42, pp. 693-703.
(An account of the equipment and of methods used by the Radio Corporation of America in its transoceanic radio business.)

## Railroads-Electrification

Electric Train Operation on the German Federal Railroad and on Lines in Neighboring Countries. Wechmann, W. (In German.)
Verkehrs. Woche, June 11, 1923; v. 17, pp. 178-181.
(Describes and compares the more important electrified railroads in Germany, Austria, Switzerland, Sweden and Norway. SeriaI.)
Electrification of Foreign Railways. I. Switzerland. Smith, S. Parker.
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(This initial installment, including maps and tables of locomotive dimensions and construction, gives details of Switzerland's progress.)
N. \& W. Electrification a Good Investment.

Elec. Rwy. Jour., July 14, 1923; v. 62, pp. 45-46.
(Brief article in which are given the opinions of N. D. Maher, President of the Norfolk \& Western Railway.)

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Analysis of Claims of the Electric Drive Over the Geared Drive Shaw, J. C.
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Standardized Insulator Tests.
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Remote Control of High Pressura Stam lanme 1) ean, Peter l'ayne.
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Rwy. Age, July 21, 192:3; v. 75, pp. 103-106.
(Report of tests on the Indiana Equipment Corporation's automatic train control equipment.)

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Hydro-electric Possibilities of Quebec. Smith, Julian C.
Mech. Engng., July, 1923; v. 45, pp. 407-409, 429.
("The potential and actual hydro-electric development of the Province of Quebec and its probable rate of growth in the future." Discussion on 1. 416.)

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Electric Cranes and Hauling Machines. Chilton, F. E. 114 pp., 1923, N. Y., Isaac Pitman \& Sons. (Pitman's technical primers.)
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Mechanical Testing. Vol. 2: Testing of Prime Movers, Machines, Structures and Engincering Apparatus. Batson, R. G., and Hyde, J. H. 446 pp., 1923, N. Y., E. P. Dutton \& Co.
Sampling and Analysis of Coal, Coke and By-products; Methods of the U. S. Steel Corporation. Ed. 2. 184 pp., 1923, Pittsburgh, Carnegic Steel Co.

## BOOK REVIEW

Atlas of the U. S. A. Electric Power Industry. By Frank G. Baum. $11 \times 17$ in., 34 plates. McGraw-Hill Book Co., New York and London. 1923.

In this admirable work the author gives us in graphic form complete figures of the electric power industry, power resources, and power demand of the United States. Based on the wealth of data either compiled from various sources or obtained by surveys in the field, the author suggests a comprehensive plan of developing our latent power resources and of the economical utilization of the developed power supply. According to this plan, the water power sources are to be developed and used as far as practicable, and the country divided into twelve regional power districts all of which would be inter-connected. Each regional district would be under the control of one company and this regional company would wholesale the power to
smaller units for distribution. The power would be transmitted by what the author calls a constantvoltage transmission system, the voltage control being accomplished by means of synchronous condensers located every 100 or 200 miles along the transmission lines. The details of this system are given in Part II of the Itlas as well as in a recent paper read before the American Institute of Electrical Engineers. (See A.I.E.E. Journal, Vol. 40, pages 643-65, of August, 1921.) Mr. Baum has made a valuable contribution to the economics of the electric power industry and his work will command the attention of the financier, the engineer, the statistician and others who have an interest in power development in the United States.


Ready for Service-The set may be supplied from lighting circuits of 110 volts, 50 to 140 cycles.

To keep the same factors of safety in oil-insulated apparatus as were put there by the designer, it is necessary to maintain a high dielectric value of the insulating oil. Only a little moisture in the oil may reduce these normal safety factors as much as $50 \%$. The only safeguard is regular testing of the oil.

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Entered as second-class matter, March 26, 1912, at the post-office at Schenectady, N. Y., under the Act of March, 1879.
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# GENERAL ELECTRIC REVIEW 

## IRON AND STEEL

On the occasion of the annual convention of the Association of Iron and Steel Electrical Engineers, which is to 10 hele this rear at Buffalo, N. Y'. on September 2tth to 29 h, we derote our carrent issue to articles which we hope will be of both interest and use to the stecl industry

Since a very remote period iron has played an all important part in developing civilization. First the Stone Age, then the Bronze Age and then and now the Iron Age. The Iron Age started thousands of years before the birth of Christ and still exists today. From the days of primitive man to the present time iron has ruled the destinies of individuals and of nations.

Tlere must be some fundamental reasons for this.

These reasons are so well put in an article in the Encyclopædia Britannica that we quote the following paragraph from this source:
"Iron, the most abundant and the cheapest of the heavy metals, the strongest and most magnetic of known substances, is perhaps also the most indispensable of all save the air we breathe and the water we drink. For one kind of meat we could substitute another: wool could be replaced by cotton, silk or fur; were our common silicate glass gone, we could probably perfect and cheapen some other of the transparent solids; but even if the earth could be made to yicld any substitute for the forty or fifty million tons of iron which we use each year for rails, wire, machinery, and structural purposes of many kinds, we could not replace either the steel of our cutting tools or the iron of our magnets. the basis of all commercial electricity. This usefulness iron owes in part, indeed, to its abundance, through which it has led us in the last few thousands of rears to adapt cur ways to its; but still in chief part first to the single qualities in which it excels, such as its strength, its magnetism, and the property which it alone has of being made at will extremely hard by sudden cooling and soft and extremely pliable by slow cooling; second, to the special combinations of useful properties in which it excels, such as its strength with its ready welding and shaping both hot and cold; and
third, to the great variety of its properties. It is a very Jroteus. It is extremely hard in our files and razors, and extremely soft in our horse-shoe nails, which in some conntries the smith rejects unless he can bend them on his forehead; with iron we cut and shape iron. It is extremely magnetic and almost nonmagnetic; as brittle as glass and almost as pliable and ductile as copper; extremely springy, and springless and dearl; wonderfully strong, and very weak; conducting heat and electricity easily, and again offering great resistance to their passage: here welding readily, there incapable of welding; here very infusible, there melting with relative ease. The coincidence that so indispensable a thing should also be so abundant, that an ironneeding man should be set on an iron-cored globe, certainly suggests design. The indispensableness of such abundant things as air, water and light is readily explained by saying that their very abundance has evolved a creature dependent on them. But the indispensable qualities of iron did not shape man's evolution, because its great usefulness did not arise until historic times, or even, as in case of magnetism, until modern times."

The above paragraph seems to give ample reason why the iron and steel industry of America is the premier industry. Today this industry is capitalized at more than mine billion dollars $(\$ 9,000,000,000)$.

But we are living in a Machine Age as well as an Iron Age and in an Electrical Age as well as a Machine Age; and a point which is of interest to us all is the fact that the steel industry and the electrical industry are the big twin sisters of the great American industrial family:

The steel industry employs over five million (5,000,000) horse power of electric motors and its annual consumption of electric energy exceeds eight billion is,000.000,000) kilowatthours.

As each year passes we shall use more and more electrical machines and appliances in the steel industry and more steel in the electrical industry. And so these inseparable giants.the children of man's imagination, energy and work, are destined still to rule man and the civilization he is building. I. R. H.

# "Motorizing" the 33-inch Structural Mill at the Homestead Steel Works 

By S.S. Wades

Comer Electrical Engineer, Carneghe Stebl Company


#### Abstract

This very valuable articte shows the results obtaned by just substituting an electric motor for a steam engine on a 33 -ind stractural sted mill at the 1 Homested Steel Works. A study of the summary of these results is very instructive. EDrom.

Although electric motor-driven rolling mills are now becoming quite common and attract little attention, an account of the "motorization" of the $3: 3$-inch structural mill at the Homestead Steel Works will be of interest on mill no change in the roll train, shoes, housings, bearings, or methods of lining up and down was made, nor were the roll sections changed in any way until after the motor had been installed and run.




Fig. 1. Structural Steel Mill Similar to that Described in this Artic!e
account of the unique feature that the installation of the motor was the only change made in the equipment.

It has been almost universally the case that the engineering department of a plant has in mind a number of changes, more or less drastic, to be made in the mill itself to improve its performance, which changes are made at the same time the motor is installed so that it is necessary to adjust the resulting benefits among several applicants each justly claiming a certain credit. With the 33 -inch structural

## Mill

This mill was installed in 1892 and is of the three-high, continuous running type, similar to that shown in Fig. 1, rolling up to 12 -inch beams and 15 -inch channels with such other standard and special structural shapes as fall within its capacity.

It consists of one roughing and one finishing stand normally carrying six passes in the roughing and four in the finishing rolls. The rolls are of 33 -inch theoretical centers, have 20 -inch diameter necks, and are 74 inches
between bearings. They are made of standard material such as gray east iron or steel.

The mill was designed to take reheated blomens or cogged shapes up to $9 \frac{1}{2}$ inches by 11 inches. The bloom is received from the heating furnace and is handled on each side of the mill by electrically-driven travelling pass tables, which move parallel to the mill, receiving the out-coming piece and returning it to the proper pass until it finally is delivered to the cooling beds. The cooling beds were of ample capacity for the mill when run by the steam engine.
near the mill or be a master switel inside the motor room. While it would hatre been desirable to direct connect the motor and raise the speed of the mill to A.3.3 it was thought best not to experment along this line at the start so a reduction gear with a ratio of 20 to 16 was introduced between the motor and the mill pinions.

The motor was started on its regular working program during June, 1921, and has continued without interruption to the present time, the only repairs being the renewal of contact tips on certain parts of the control

## Engine

The engine was built by the Southwork Foundry $\mathbb{\&}$ Nachine Co. and was of the well-known PorterAllen tepec horizontal simple engine, with $\overline{5}$-inch cylinder and 66 -inchstroke. and with a 24 -foot, $1: 0,000$ pound flywheel. It was designed to work under a steam pressure of 12.5 pounds and atmospheric exhaust with a speed of (6.) r.p.m.

## Motor

Tine motor selected to replace this engine was a $40010-12$ p. . 2.5 -cycle. 3 -phase, (6if00-volt machine with a symehronous speed of \&3.3. illustrated in Fig. 2. The efficiency is calculated to be (14.5 per cent with a power-factor of $\$ 1$ per cent
and a speed of $S_{2}$ r.p.m. at full load. It will deliver 4000 h.p. continuously with a rise of 3.5 deg. C. above the surrounding air. and $6000 \mathrm{~h} . \mathrm{p}$. with a 50 degree rise. and is capable of exerting a maximum ruming torque of approximately 700,000 $\mathrm{lb}-\mathrm{ft}$. corresponding to $10,500 \mathrm{~h} . \mathrm{p}$. It is provided with a cast steel flywheel 19 feet in diameter, with 16 -inch face, weighing 170.000 pounds and the combined stored energy of the rotor and flywheel is approximately 18,400 h.p.-sec. An extra section of resistance
 is installed which is cut into the rotor circuit by means of a notch-back relay and contactor. if the load on the motor exceeds approximately 150 per cent normal torque. The motor can be started. stopped or rerersed by means of push buttons mounted


Fig. 2. 4000-h.p., 25-cycle, 3-phase, 6600 -volt Induction Motor for Driving the 33 -inch Mill
system due to the severe strain put on them in "wedging up" the rolls in the process of " lining" where it is necessary to successively start and stop the mill for a morement of only a few inches on the surface of the rolls.

## Results

It was noticed almost immediately that, whereas the engine used to slow down and drag on the long finishing passes, the motor held up to speed and that the finished piece was delivered to the cooling beds much hotter than before. This led to cutting the ingot into two blooms instead of into three blooms per ingot as was the former practice. further increase in weight being precluded by lack of room in the mill, as designed, to care for the extra length of the fimished piece

The trouble which had alwars been experienced in variation in weight of section


Fig. 3


sometimes amounting to several per cent was entirely eliminated, even with the 50 per cent incrase in length due to using two cuts instead of three cuts to the ingot. The only difficulty encomenterd due to the ehange was that the cooling beds prowed to be inadequate to care for the inereased tomnage which could now be handled, so placing the limit on the output of the mill.

It was feared that the great reserve power of the motor would cause serious trouble in case of a piece being "cobbled," and that an increase in roll breakage would result, but


Fig. 7. Curve Drawing Instrument Chart showing the Fluctuating Character of the Load
this has not proved to be the case, the result being fewer cobbles and a considerable decrease in roll breakage. This is probably due to the uniformity of speed the motor maintains and the ample power provided, which eliminates slow rolling and serious loss of temperature during the process.

One very noticeable advantage of the motor over any other method of driving a rolling mill is the intimate knowledge it provides the operators and roll designers regarding the power required for each pass, by means of continuous chart-drawing instruments. The flow of plastic steel under pressure is governed by so many things that the power may vary over wide limits, for reductions of area which are practically equal, especially when structural shapes are being rolled. It is possible to distribute this work over the passes to the best advantage for the mill and the finished product if the work done in each pass is known.

## Charts

Fig. 7 shows a reproduction of a chart taken at 12 inches per minute with a swing of the
pen equal to one half inch per 1000 kw . In this curve and those following, the wavy shape at the top and bottom is probably due to the sensitiveness of the instrument and the vibration of the ground caused by the running of the mill. The high saw-tooth form of the curve for changes from friction load to frill load and back appears to be due to lack of dead beatness in the instrument allowing the pen to over swing in both directions.

Figs. 3, 4, 5 and 6 are reproductions of a chart taken at 18 inches per minute with a swing of 1 inch per 1000 kw . The speed curves at the bottom are of interest only as showing the drop in speed under load, which allows the flywheel to function. The speed curve is omitted for the finishing passes as there is hardly any noticeable decrease of speed under the power demands at this point. The curve has been spread toallowbetteropportunity for study and a picture of the section resulting and the data for the pass are shown above the curve. In these chart curves the time is shown in five second blocks evenly divided into single seconds which is near enough for all practical purposes. These chart curves form a basis for some very interesting study and need no discussion in this article.

## Summary

As no change was made other than the installation of the motor in place of the steam engine, the electrification of this mill may be credited with the following:

1. More convenient operation due to push button control for starting, stopping and reversing.
2. Cheaper operation due to less attendance, and practically no repairs.
3. Greater tonnage and fewer pieces to handle due to the reserve power inherent in the electric motor.
4. Fewer cobbles and reduced roll breakage.
5. More uniform sections with less difference in weight of finished piece, due to quicker finishing.
6. Assistance to roll designer derived from recording chart.

# Reliability of Power, a Necessity in the Steel Industry 

By F.O. Schnure<br>Electrical Enginier, Sparrows Pont Plant, Betmenem Steel Co.


#### Abstract

In emphasizing the importance of a continuous power supply in steel mills the athor follows the steel through the mills and shows what would happen at each step if power failed. He then describes the system adopted to insure continuous power supply at all times. This contribution is written by a practical stecl man in the light of long cxperience and will be useful to all interested in the business of manufacturing stect.


- EDHIOR.

An uninterrupted flow of electrical energy is vitally important if the various operations in a stecl plant are to function successfully: An interruption of power means chiefly loss of production, but even momentary interruptions may mean serious loss of plant equipment and extraordinary hazards to the workmen. In discussing the situation, it seems adrisable to follow the raw material through the plant. noting the necessity of continuous power flow as we go. Then we may discuss the power house, transmission system, motorized equipment and their relation to the continuity of power.

The pumping station if motorized presents the most important problem. The blast furnaces, coke orens, open hearths and mills all depend on this station for cooling water for their stacks. doors, valves, rolls, etc. Steam standbr equipment. for use in case of power failure is not satisfactory unless installed in adequate capacity to maintain the standard water pressure, othervise the upper parts of the blast fumnace suffer. Booster pumps, either steam or electrically driven, from other sources of electrical supply, at certain strategic points relieve the situation somewhat, but are not a definite insurance against burnouts, as pump men for starting this equipment are not always instantly available.

The ore wharf and field is not seriously affected br power interruption provided braking on trollevs is done by air or hand, and the lowering of buckets by the use of dynamic circuits. However, when power fails because of faulty contactor operation, it is possible to drop a bucket in a ship or car and do serious damage. Track clamps should be set by gravity, so that a combination of high winds and loss of power would not allow the traverse motion of the bridge to get beyond control. A prolonged interruption of power may mean a considerable loss of product throughout the plant if the bridges are not able to keep the blast furnaces stocked, and in
holding up the unloading lof ships or cars may mean the accumulation of considerable demurrage.

A power interruption in the coke ovens affects principally the by-product plant, so that any revenue such as obtained from the sale of illuminating gas may be lost. If this gas is used as a fuel in other operations of this plant, these operations will also be delayed. Cooling water is also very important in this plant, and where these pumps are driven electrically, the situation could become very critical. An interruption of any length would of course limit the production of coke, which would in turn limit the output of pig iron at the blast furnaces.

At the blast furnaces, a momentary interruption of porwer, stopping the flow of cooling water through the stack plates and valves, may cause damage to the equipment amounting to thousands of dollars. In the blowing engine department, failure of power on the motors driving the gas washers would shut down the blast furnaces, by stopping the flow of gas to the blowing engines. An interruption of power on the pumps circulating the cooling water for the gas engines will cause hot cylinders and exhaust headers. and require an immediate shutdorn of these units. Untimely re-entrance of water into the cy-linders and headers may cause cracks that will require considerable time and expense to repair. When power fails the most dangerous place in the plant is in this gas engine department, as failure of the engines to function normally releases live CO to the atmosphere in quantities that makes work in restricted areas extremely hazardous.

In the open hearth, a slight interruption of power affecting the cooling water will warp the coolers on the doors and burners and if not causing instant failure will affect the metal, so that in a ferr dars it mar become necessary to change i. per cent of all such equipment subjected to this loss of water. This loss of equipment is not serious of itself,
hat affects production which may mean sereal humdred dollars per furnace per hour. The secondary situation in the open hearth lies in loss of direct-current power to operate the cranes, mixers and tilting furnaces. It is very often possible when power fats while pouring a ladle of metal to move the line of ingots be a locomotive and save any loss of product or serious inconvenience. When the boded ladle is being raised to the porring pesition, and the power fails, the situation is not quite so simple. If of long duration, heary sculls result requiring expensive handling and re-melting. If the power fails white the mixer is in the "down" position, and the operator is unable to raise it, a very nasty spill occurs which means a considerable amount of money to clean up. The same situation prevails in respect to the tilting furnace.

In the rolling mills, there is the possibility of burning out valve coolers, furnace door frames and bearings when cooling water fails. Power failures which eatch soaking pit eranes and furnace chargers, with the ram in the pit or furnace, may be the cause of castings warping and the wiring burning up. In continuous mills driven by large induction motors, a partial failure of voltage causing the control to trip or contactors to drop out may cause stickers in the mills, which require from one to three hours to clear up. In addition the hot steel warps and cracks the chilled rolls so that roll depreciation may be very high. On sheet bar mills, an interruption of a few seconds on the pinch rolls, delivering the sheet bar to the bar piler, may mean cobbling the entire ingot. It is important that some mills have a constant voltage as well as uninterrupted supply of power.

Having reviewed the things which may happen to cause loss of production and equipment, both of which entail considerable expense, we can now pass to the power house to study ways and means of preventing these failures.

The power supply for stcel plants may be derived from gas-engine-driven generators, steam turbines or central station power or combinations of two or all; and it is worth while to make a study of the reliability of each source of energy. Gas-engine-driven generators unless installed in sufficient number and operated below their rating have very little overload capacity, and may easily stail under grounds or heavy overload unless proper relay protection is afforded. Gas engines may also fail because of gas trouble in the
furnaces, from low fuel value of the gats and from overspeed and ignition trouble.

Steam turbines are probably the most reliable provided the boilers are equipped wo burn fucl oil or coal in case of blast furnace gas failure.

Central station power is usually on a par with stam turbines, when the central station system does not cover too much territory or overload its transmission system and generating stations. When the central station extends over considerable territory, lightning disturbances in the form of surges are apt to be reflected over the entire system, in the same way cable failures cause voltage variations, which are disastrous to continuous mills employing large motors on their main drives.

There are, however, few steel plants which employ only one of the above systems, usually a steel plant has either gas engine or steam turbine equipment and uses central station power to make up what they cannot produce themselves. Thus it means the steel plant has all its own trouble to guard against plus the reflection from the central station. It is important then that some relay connections between the two systems be employed, so that in case of failure of the one the service on the other would not be seriously affected.

The Sparrows Point plant is operated by six $4000-\mathrm{kw}$. gas-engine-driven units augmented by feeders totaling $20,000 \mathrm{kw}$. from a central station. The plant has a maximum demand of from 25 to $3 \overline{5}, 000 \mathrm{kw}$. With no total outage during the past six months we have had 24 disturbances where the voltage dropped below 75 per cent of normal, four of which originated in our plant. One was caused by a locomotive crane grounding the lines, one by a 1000 h.p. motor grounding, one by a $1400 \mathrm{~h} . \mathrm{p}$. starting compensator failing and one by a circuit blown down by a storm. Of the central station disturbances, five were slight surges, three were outages from overload, and twelve were surges of sufficient intensity to trip either a low voltage or reverse current relay. In addition to this our plant system was separated from the central station system nine times in order to avoid surges due to storms and lightning disturbances. In the power house, the rital load consisting of the power house auxiliaries and the central pumping station, making a total load of 5000 kw . is placed on the house bus along with two generators. The remainder of the plant load is placed on the main bus with the other generators and the central station power.

The bus tie comnects the two and has relay protection consisting of low roltage and a predetemined amount of reverse power from the house bus to the main bus. It has been demonstrated that a reflection from a surge from the central station system, or about our own plant, will cause this bus tie to open under either low roltage or rush of current from house or main bus and leave the vital plant load to be served by two generators. This protection has proven very satisfactory functioning without a failure during the last year. As an extra precaution in case of this relay failing, it is the practice of our operators, in the face of an approaching storm, to open the bus tie and run with these auxiliaries as a two engine load.

Power interruptions from the power house may also come from overloading the central station feeders and to prevent this occurring. an overload relay has been installed on the central station system, so that when the load on this circuit reaches about 90 per cent of its tripping value, the relay functions, opening the control circuit of power on the approach tables in one of our mills thus stopping the flow of steel. This, in the course of a fraction of a minute, automatically cuts off 3000 kw . load and if required, 30 seconds later 4000 kw . and in about three minutes 3000 kw . more when the mill is running empty. In case further relief is required, push buttons operated from the power house open the circuit breakers on the main motors in other mills and provide means for the operator to lighten the plant load without tripping the circuits and losing the auxiliaries, before the central station power reaches a point where it might open from overload.

The transmission system presents a very important link in the chain which our electrical department forges in order to maintain continuity of service. In our plant, rather than maintain a multiplicity of circuits from the power house to the various mills, a double loop system has been installed, which virtually extends the power house bus to the various mills and substations. This system has been very satisfactory, being substantially built of the best equipment, and enough cable capacity has been installed so that no trouble can possibly arise from overload. At
cach load point, this double loop consisting of one million circular mil cable per phase, enters the switching fowers and passes through two oil switches, as a part of the transmission system. The mill feeders conneet to the loops between these ril switches and relay protection is so afforled that when trouble occurs on any section, the system will automatically clear itself.

After three years operation of these (6600volt circuits, we have had but three failures on this system, two being caused by lightning flashing over the entrance bushings, both occurring before the ground wire was installed and one by a rat grounding a disconnecting switch. Another double feeder passing over the coke plant to the main pumping station, although well insulated, got in trouble so often from dirt, gas and loose sheathing blown from conveyors by high winds that a single circuit consisting of a thrce-conductor cable well insulated by cambric and armored by a steel tape was installed. This installation has proven very satisfactory.

All the protection incorporated in the power house and transmission system is not of much value unless the distribution system permits of flexible operation. In this plant, the secondary circuits of 550 -voit alternating current and 250 -volt dircet current practically follow the 6600 -volt loop so that in any mill or substation this service can come from the low voltage loops. Besides permitting of urgent repairs without shutting down any mill equipment it allows taking motor-generators and iransformer banks out of service and laying off substation operatois during inactive periods.

The electrical department's responsibility i.2 maintaining power on any service does not end with maintaining roitage at the point of consumption. Power is of no value unless converted into work through motors and switching equipment well maintained. In the first place all equipment should be of rugged construction, in the second it should be well cared for and in the third, suitable spares should be carried for emergency replacements.

If all three ideas work hand in hand from the power house though the transmission system to the motorized equipment the steel plant should have reliable power.

# Direct-current Power Generation for Steel Plant Loads 

By Ernest Pragist<br>Power and Mining Enginemring Department, General blemerte Company


#### Abstract

The sedection of a system to provide an adequate amount of direct-current power for operating steel mill auxinaries often presents a diffent problem to solve. The author analyzes the pros and cons of the various methods awablabe and makes recommendations to suit different necds.-Enotor.


As each new plant is designed the most suitable method of obtaining an adeguate source of contintous current power for operat ing the numerous auxiliary drives throughout the plant has to be determined. Nuch has been written on this subject, but it might be well to present again the characteristics of the several systems of deriving this form of power. The following discussion will approach the subject primarily from the point of view of the steel plant electrical engineer, will concern itself largely with apparatus suitable for use in such industries and will deal with the operating characteristics of the types of machines involved rather than with the problems of their design and manufacture.

## Characteristics of Steel Mill Loads

It is not possible to set forth in detail and with accuracy the characteristics of stecl plant loads in a form that will be applicable to all. One can only speak in generalities, in terms of tendencies and those plants representative of a large and influential group. The steel mills, as do all other classes of industrial establishments, vary greatly one from another in size, modernity, principle of operation, and administrative policy. Further variables are introduced by location, the raw materials used, products manufactured and the like. With a realization of these limitations in mind it may be said that in general relatively large amounts of electrical power are used in their manufacturing processes and in the form of both a-c. and d-c. energy, the former predominating in quantity. The greater part of the a-c. power is usually consumed by a relatively few large motor installations and in some cases electro-thermal applications. On the other hand the d-c. power is used to actuate a proportionally large number of relatively small auxiliary drives. This classification excludes from the d-c. group such applications as reversing blooming mill drives, etc., which are d-c. operated. These may more truly be classed with the a-c. loads.for they are in variably operated as a unit with and supplied with power from
a special a-c./(1-ce motor-yenerator set which in turn is fed from the phant a-c. power source. So, we have to deal with two forms of electrical power, a-c. and d-c., and it is evident that we must consider them in their interdependence if a true apprassal of the merits of the apparatus best suited for the generation of either is to be arrivel at.

As a rule the points of power usage are distributcd over a relatively large area and the generating capacity confined to a single point. The locations of the drives are determined by the layout of the mills which in turn are so arranged as to permit a frec and easy flow of raw materials and those in process throughout the plant. The locations of the loads usually have only a secondary influence in determining the selection of the generating site or sites. The controlling influences are the sources of fuel and water supply as electrical energy can be more satisfactorily transported than either. For economic reasons, where possible, power is generated in any given plant at a single point. This applies to those plants which generate their own power. In those cases where power is purchased, the locations of the principal loads can influence to a greater extent the placing of the primary substation and the distribution from it.

The electrical characteristics of the a-c. loads of representative plants are very typical. They are of twenty-four hour duration each day fluctuating greatly with unusually high momentary recurring peaks and of low powerfactor. The operating potential is generally either 2300 or 6600 volts with a few exceptions as high as 13,200 volts. The voltage selection is determined by the minimum which efficient transmission permits and the maximum for which induction motors of economic design and good electrical characteristics can be built. Three-phase operation at either 25 or 60 cycles is almost universal.

The d-c. load is in operation also twentyfour hours a day. It is of a fluctuating nature but the fluctuations are not as great as in the case of the a-c. load, due to the effect of the diversity factor of the numerous small loads.

The generating voltage for this class of load has been standardized. It is 250 volts.

Continnity of service is essential. An interruption in the power supply might result, not only in a loss of production, as in some industries, but as well in the loss or deterioration of materials in the process of manufacture, the failure of apparatus and a serious hazard to the lives of employees.

## Sources of D-c. Power

There are several sources from which d-c. power may be derived.
(a) Through direct generation, namely by driving d-c.generators by prime movers.
(b) Through a-c. generation and a-c./d-c. conversion using for the conversion:
(1) Motor-generator sets either induction or synchronous motor driven.
(2) Synchronous converters with transformers.
(3) Mercury arc rectifiers.

As a rule the derivation of $\mathrm{d}-\mathrm{c}$. power through direct generation is not economically desirable. For its efficient production in this manner large capacity units located at a single point must be employed. When this is done, the distribution of the output at its low voltage presents a problem for which a satisfactory solution does not seem possible. To divide the generating capacity into numerous relatively small machines located near the load centers, thereby overcoming the difficulties of distribution, presents a more numerous group of problems. In such a case the efficiency of generation will be decidedly decreased and its cost increased. Together with these disadvantages are coupled the problems of getting steam or fuel and water to and from the prime movers, plus those of an operating nature which must necessarily ensue. It must be concluded that, excepting some peculiarly special cases, the direct generation of $\mathrm{d}-\mathrm{c}$. power is accompanied with such difficulties as must always act as serious detriments to its selection as a means of securing this form of energy. The limited number of this class of installation throughout the country confirms this conclusion.

Where the required d-c. power is obtained through a method of a-c./d-c. conversion, the whole plant's electrical demand may be produced in a single a-c. generating station consisting of a relatively few large capacity

[^70]high ceonomy machines. This represents a type of generating station in which the highest generating efficiency can be obtained with a minimum investment and operating cost. The conversion capacity may be composed of relatively small units located near the load centers and fed with a-c. power from the central a-c. source at a voltage which will produce a negligible loss in the transmission system. The d-c. distribution losses may thus be inexpensively reduced to a reasonable minimum. It is this possibility which has brought this method of obtaining the d-c. power requirements of steel plants into almost universal use as against that of direct generation.

The two most common methods of conversion are through the use of motor-gencrator sets and synchronous converters with transformers. These will be considered at length later.

A third method is based on the employment of mercury are rectifiers. Our interest in these for steel mill work is more academic than practical. In their present form their characteristics are such as to limit their field of economic application to those high voltage ( 600 volts and above) d-c. uses where high efficiency at both light and heavy loads is essential. Electrical losses in a rectifier vary with the current rectified and are substantially independent of the voltage. Hence their efficiency at low voltages is not so different from that of motor-generators and converters, but increases rapidly with an increase in voltage, surpassing that of this class of apparatus at the higher voltages. When considered with their transformers, the a-c. input to the transformers used with rectifiers is of high power-factor, roughly 95 per cent. As their price at present is greater than that of either motor-generators or converters, their efficiency not materially greater and their power-factor lower, when designed for service at the potentials usually met with in the class of service under consideration, there has been no incentive to consider them seriously for installation in steel plants as yet.

## Motor-generator Sets versus Synchronous Converters*

For the practical business of a-c. d-c. conversion in steel plants the choice of system becomes a selection between synchronous converters with transformers and motor-generator sets or more specifically, synchronous motor-generator sets. The induction motordriven set may at once be eliminated from
consideration due to its lower power-factor and the fact that the induction motor possesses no peenliar characteristics which better adapt it to generator drive than does the synchronous motor.

In making a comparison between motorgenerators and converters, no consideration need be given to such questions as relative heating, commutation, overload capacity, etc. These are strictly machine design problems. Both classes of apparatus can be built to meet the same requirements in these respects. Obviously, a true comparison must be based on the assumption that these characteristics are alike in both classes of equipments.

The synchronous converter as, commercially designed is inherently a unity power-factor
apparatus with the motor-generator having a slight alvantage if any.

Maintenance likewise shonld not differ greatly. Here, too, engineers are inclined to fawor the motor-generator set slightly due to the converter requiring two sets of brushes. On the other hand, the converter with transformers should be less liable to electrical break-down of insulation as a result of abnormal voltages impressed on it by such phenomena as lighting. This is due to the ability of the apparatus designer to inexpensively angment the insulation at vulnerable points. It is accomplished by increasing the insulation on the end turns of the transformer primary windings, the ends of which are connected to the incoming lines and so


Fig. 1. Motor-generator Set. Generator Rating 1500 kw., 514 r.p.m., 250 volts. Motor Rating 2100 kv -a., 514 r.p.m., 6600 volts
machine. Operation under loads approaching rated output at power-factors varying more than a few per cent from unity will result in serious local heating within the armature and poor commutation with its accompanying detrimental effects. The synchronous motor may without difficulty be constructed for operation at any power-factor with a decreasing cost per kv-a. of rated input for an increase in input. As power-factor correction is so desirable in most installations, it is almost universal practice to design the motors of synchronous motor-generator sets for 80 to 85 per cent leading power-factor operation. Where system power-factor correction is felt necessary, the motor-generator set is decidedly superior to the converter.

As regards simplicity of operation, there is little difference between the two classes of
must withstand the shock due to high voltage and frequency, particularly where the lines are exposed to severe lightning disturbances. The synchronous motor armature winding does not lend itself to such a simple precautionary measure.

Flexibility of voltage control is superior in the case of the motor-generator set to that of the converter. The d-c. potential of a motor-generator set can be controlled and varied at will irrespective of voltage conditions on the driving a-c. system. In the case of the ordinary converter it is a function of the a-c. voltage and varies directly with it. There is a slight compounding possible where compound converters are operated with high reactance transformers due to the possibility of varying the potential drop through the transformers and over the lines by changing
the power-factor of the imput to the converters within the limited range possible. It is usual to so adjust the compound and shumt field excitations that full load operation is at unity power-factor or slightly leading, and at low loads lagging, thus reducing the potential drop over the a-c. circuit and up to the converter rings to a minimum at full load and increasing it to a maximum at light loads. thereby approaching or in some special cases possibly slightly excceding flat compounding. Through the introduction of a synchronous booster or induction regulator the control of the arerage $d-c$. roltage becomes possible but at the penalty of additional cost and a decrease in efficiency:

Wherever converters are used, there is an electrical connection between the a-c. and d-c. systems. Disturbances on one are reflected in the other. Change in frequency affects the roltage of the motor-generator; while change in primary a-c. voltage is transformed through the converter. In the case of motorgenerator set conversion there is no electrical connection between the two systems. The only tie is mechanical through the shafts of the sfis. and so there is no possibility of reflection from one system to the other of momentary abnormal electrical voltage and current variations from the normal which are constantly occurring in the class of service under consideration. It is this dependence of d-c. voltage upon that of the a-c. source which makes it uindesirable to attempt to parallel on the d-c. side converters with generators, except in special cases where the a-c. source of supply is known to be substantially free from voltage fluctuations.

In some few cases it is felt desirable to be able to meet emergencies through an inversion in the operation of the conversion apparatus, namely through conversion from d-c. to a-c. Here the synchronous machine will be capable of carrying a load having a power-factor at least as low as the power-factor rating of the synchronous machine when operating as a motor and equal to the rated output of the d-c. machine less the set losses. The converter under such a condition is at a disadrantage due to its inability to carry loads approaching its capacity at power-factors varying materially from unity.

Where the a-c. voltages do not exceed those usually met with in steel plant practice, in which case it is assumed that the synchronous motor may be built for operation at the system $a-c$. voltage. there is not a great difference in price between the two classes of equipment.

Synchronous motor-generator sets with ermplete a-c. and d-c. control will cost substantially the same as converter outfits, including transformers, a-c. and d-c contsol and the bus material between the ransformers and converter collector rings in the case of the smaller sizes ( 100 to 17.5 kw . capaiity). As the size is increased the converter equipment becomes proportionately less costly, reaching in the case of the larger


Fig. 2. Synchronous Converter, Rated at 1500 kw ., 514 r.p.m., 250 volts
machines, a value of to to 90 per cent of that of the motor-generator set with switchboard. These ratios are based on an a-c. potential of 2300 rolts in the smaller sizes and 6600 volts in the larger ones, also 2.50 volts d-c. throughout. An increase in a-c. potential will lower the ratio slightly in the larger sizes and to a greater extent in the smaller ones as the increase in cost of transformers with an increase in voltage is less than in the case of synchronous motors. So, where the smaller medium a-c. voltage equipments are concerned, price need not be considered in determining their selection, but in the large ones, where a difference exists between the two, favoring the converter, it must necessarily be taken into account and act as one of the factors influencing choice.

The synchronous converter along with its complementary apparatus has a higher efficience than the motor-generator set throughout the whole range of sizes. the ratio of efficiencies varying from, roughly, 94 to 96 per cent in the smaller sizes to 96 to 97 per cent in the larger.

The floor space required by large converters with transformers is mily 5 or 6 per cent greater than that required by motorgenerator sets but in the case of the smaller sizes this will be increased as much as 30 to 40 per cent.

The relative weights of the two classes of equipment are sulstantially the same except in the smaller sizes where the converter with transformers is slightly heavier.


Fig. 3. Relative Price Per Kw. of Capacity Expressed in Per Cent for Motor-generator Sets and Synchronous Converters with Transformers
Curve A Motor-generator Sets with Complete Switchboard
Curve $B$ Synchronous Converters with Transformers, Complete Switchboard and Alternatingcurrent Bus Material between Transformer and Converter


Fig. 5. Relative Floor Space Per Kw. of Capacity Expressed in Per Cent for Motor-generator Sets and Synchronous Converters with Transformers
Curve $A$ Motor-generator Sets
Curve $B$ Synchronous Converters and Transformers
So that the reader may better visualize certain of the more important relations between the two classes of equipment a number of curves have been included. Fig. 3 shows the relative price per kw. of capacity for motor-generator sets and synchronous converters with transformers; Fig. 4, the relative efficiencies; Fig. 5, the relative floor space required; and Fig. 6, the relative weights. These curves are based on apparatus having a continuous rating as defined by the A. I. E. E.
and designed to operate from a three-phase source, $6(0)$-cycle, $2: 300$-volt in the smaller, and (i60) -volt in the larger sizes, and to deliver 250 -volt d-c. power. The power-factor of the motor in the case of the motor-generator sets is taken as s.) per cent. In (letermining the curves the characteristics of numerous equipments were plotted and a curve drawn through the mean of these values. $\Lambda$ s one might naturally expect certain designs have


Fig. 4. Relative Efficiencies Expressed in Per Cent for Motor-generator Sets and Synchronous Converters with Transformers
Curve A Motor-generator Sets
Curve $B$ Synchronous Converters with Transformers. The Losses included are those of the Converter, Transformer and Alternating-current Bus between the Transformers and Converter


Fig. 6. Relative Weights Per Kw. of Capacity Expressed in Per Cent for Motor-generator Sets and Synchronous Converters with Transformers
Curve $A$ Motor-generator Sets
Curve $B$ Synchronous Converters and Transformers
values which fall well off the curve; however, there were enough varied designs to define the curves fairly well as shown. Although the actual values for 2.5 -cycle apparatus and that having a nominal rating will differ somewhat from those of the machines which form the basis of the curves, namely an increase in price, weights and dimensions, the relative values as shown in the curves are fairly representative of this class of apparatus as well.

## Summary

It is usually more desirable to generate the whole power requirement of a steel plant in the form of a-c. enerys and convert sufficient of it to meet the d-c. need than to produce the $a-c$. and $d-c$ power independently. Of the several possible methods of conversion those employing motor-generator sets and synchronous converters with transformers are the only ones which. in the present derelopment of the art, warrant serious consideration.

It is essential to maintain continuity of power service on both the a-c. and d-c. sestems. Substantially constant d-c. potential is desirable. The a-c. load is a greatly fluctuating one of low power-factor. Where blast furnace gas and waste fivel is burned the cost of power production is relatirely low. Comparing these characteristics of the loads with those of motor-generator sets and converters, it appears that in all of its major character-
istics with the exception of price and effietency the motor-generator set is superior to the converter, and where the cost of power is low as is often the case, the difference in efficiencies is discounted to a great extent. This leaves the decision to be drawn largely from a comparison between the difierence in cost of the two classes of apparatus, which favers the convioter equipment. and the value placed on the power-factor corrective capacity of the motor-renerator set, its flexibility and its ability to maintain an electrical segregation of the a-c. and d-c. systems. From the ratio of the installed capacity in synchronous motor-generator sets to that in synchronous converters now operating in steel plants one is led to conclude that most steel plant engineers appraise the more adrantageous operating characteristics of the former higher than the lower price and better efficiencies of the latter for steel plant loads.

# Switching Apparatus in Steel Mills 

Bỵ G. H. Jump<br>Engineer, Buffalo Office, General Electric Company


#### Abstract

The author notes and points out the similarity and difference between city and steel mill porer equipments. He then discusses the layout of power supply circuits for steel mills and gives many useful details regarding switching equipment.-EdIIOR.


Electricity in the iron and steel industry has adranced from the position of a necessary, but minor, auxiliary to that of a major element in plant operation. In the modern steel plant nearly every mechanical power requirement, from the handling of coal and ore to the loading of the finished product, is supplied by electric motors receiving energy through the plant distribution system from one or more main generating sources. It follows that. with the exception of the power supply itself, no element of the plant equipment is more rital or deserves more careful consideration than the primary distribution system with its switching and protective derices.

In steel mills having electric main roll drives the requifements of the distribution system are similar in many respects to those met with in central station practice. especially with regard to the amount of power to be handled and the high degree of reliability necessary: Since it is quite natural and proper to utilize as far as possible the methods of switching and protection adopted as a result of central station experience, consideration should be given to the similarities and differences in the
general requirements of the two classes of service. in order that the experience in the one may be applied intelligently to the other. In both steel mill and city distribution reliability of service is of the highest importance. In both cases power is usually received from at least two principal sources, the area to be served is of such an extert as to require a number of distribution substations connected with the power sources by a loop or network, and the magnitude of the load will demand several circuits in parallel from power stations to substations. The points of dissimiarity exist principally in the nature of the load itself. The steel plant normally operates at full capacity continuously from the beginning to the end of the week thus taking a fairly constant average load throughout the 24 hours of each working day. in contrast with the widely rarying day and night loads ordinarily encountered on city systems. Steel mill main roll drives, however, constitute large units of load which may be rapidly fluctuating, causing peaks and valleys of short duration in the plant load curre. Furthermore. the steel plant distribution system must
supply a considerable proportion of its capacity through conversion apparatus to directcorrent load which may alse be subject to fluctuation. Aside from the character of the load another factor which directly affects switching expipment is that the arerage transmission distance in the sted plant is ustally less than in city systems of corresponding capacity the result being that the impedance of the distribution circuits is lower and the current which can llow into a short cirenit at any point on the system will be greater.

The general conclusions which can be drawn from the consideration of these points of comparison are: that switching equipment used in steel plant service should be especially liberal in capacity since the "peak load" periods are six days long instead of a few hours, that devices used for protective service against line failures must be proof against operation under load fluctuations, but sensitive and rapid in case a fault develops, that particular consideration should be given to the question of short circuit values and the selection of apparatus suitable to meet them, and finally that switching equipment in common with most other stecl plant apparatus offers the opportunity for inspection and overhauling every seven days even though it maybe subjected to continuous heavy duty throughout a six-day week. The last consideration will often make advisable less duplication of apparatus and consequently greater simplicity than is common in central station practice, the tendency being toward fewer but heavier switches and simpler but more carefully safeguarded construction. From the economic standpoint the distribution system in central station work is one of the principal items in the cost of operation while the steel plant system is a tool which represents a comparatively small item in the cost of the finished product, but a tool which if seriously damaged may entail many times its cost in loss of production. Consequently there are few cases in steel mill service where the best in switching apparatus and construction is not justified even though a somewhat greater expenditure may be necessary.

The foundation for the design of a switching equipment is of course the connection scheme. While it is not the intention of the present discussion to consider the general layout of distribution circuits, it may be said that the usual substation or switching point will have two or more power supply circuits connecting it with the power stations or with other switching points, and also a certain number of
fecters supplying the load in the vicinity. To meet such conditions a number of different switching schemes are available as indicated in Fise. 1. Although many further modifications are possible, the arrangements shown will serve for comparison. With the seheme shown in Fig. 1-A load is simply tapped off from either or both of two circuits which are


Fig. 1. Connection Diagram Illustrating Various Switching Arrangements
controlled by switches in other stations. Simplicity and low cost are secured at some sacrifice in protecting continuity of service, although this sacrifice is not great if only one feeder circuit is to be taken off. The scheme in Fig. 1-B uses a single bus with one oil circuit breaker in each circuit and permits isolating automatically any circuit which develops a fault, without interrupting service on the others. In Fig. 1-C a second bus is added with selector disconnecting switches allowing access to either bus without dropping load. The load may also be carried in two groups if desired and may supply the circuits in each group separately. A double bus is also provided in the arrangement shown in Fig. 1-D but with two breakers per circuit so that any breaker may be isolated for inspection or repair at any time. Easy access to the oil circuit breakers is accomplished by Fig. 1-E with a smaller number of breakers and a single bus. Double blade disconnecting switches on the feeders are used to connect two or more circuits to one breaker for temporary operation, thus allowing any breaker to be taken out of service without interrupting the load.

The selection of a connection scheme must of necessity depend on the particular conditions involved, and it is possible to point out only a few general considerations. Simplicity is an important factor in any installation and particularly in steel mill work on account of the reduced possibility of confusion in operating and because more careful maintenance can usually be secured where a smaller amount of equipment is involved. From the standpoint of simplicity alone we might use the arrangement show in Fig. 1-13, but the element of flexibility must also be taken into account to determine whether or not the conditions justify a more elaborate scheme. Flexibility as provided by double buses, duplicate oil switches, and various other expedients serves two main purposes; to meet the requirements of changing load conditions and to allow access to parts of the equipment at all times for maintenance purposes and for making extensions. These features are often of great value, but in a great many cases they will prove to be of less importance in the steel mill system than in the city distribution system because there is less change in the load conditions, less necessity of changes and extensions in the equipment, and because the weekly light load period can be more easily taken advantage of. Reliability of relay protective schemes can be more easily secured with single bus arrangements and simple connections. Consequently the more elaborate connection schemes should be adopted only when circumstances definitely demand their use and when proper consideration has been given to the disadvantages as well as the advantages involved.

The oil circuit breakers constitute the most important item of the station control equipment and the reliability of the plant power is greatly dependent on their successful operation. They must be capable of interrupting the maximum amount of short circuit current which can be fed into the circuits which they protect and to this end it is highly important that a careful survey of the distribution system be made to determine the value of this maximum current. Liberal allowance should be made for further growth in the quantity of synchronous apparatus connected to the system and in the number and size of circuits required to carry the load. The methods of calculating short circuit current after having determined the future system characteristics are well known. On loop systems or networks frequently used in steel mill practice the calculating table is of great assistance in simplifying the calculations.

The interrupting capacity requirements of a large plant usually demand breakers of a heavy type which for case and certainty of operation should be electrically rather than manually controlled, and conseduently a thoroughly reliable direct current supply: preferably at 12.5 volts, is required for oil circuit breaker operation. A storage battery is by far the most satisfactory methorl of obtaining such a supply and the advantages of its use to obtain reliability fully justify the cost and the small amount of maintenance required.

In steel mill service the manner in which switching apparatus is installed is especially important. The possibility of insulator flashovers and the breakdown of insulation is greater than in most other classes of service due to accumulation of conducting dust and presence of moisture and corrosive gases. To prevent arcs which form in this manner from communicating to other apparatus and causing, serious damage is one of the principal considerations in the design of the switching structure. Another is to protect operators and others as far as possible from accidental contact with live parts. To design for these results it is first necessary to have sufficient space so that the structure may be designed with proper clearances. Too often the switching apparatus is made to occupy the space which is left when everything else has been provided for, the result being a switch room which is a menace to the power supply as well as to persons who enter it. The second requisite is to protect the live parts of the equipment, either by enclosing in compartments or by suit. able insulation, so that the conducting gases produced by an are will be prevented from causing additional breakdowns. Experience has proved beyond question the effectiveness of masonry cells and barriers in preventing the spread of arcs, and if the switch and bus compartments are equipped with doors which serve to enclose live parts completely greater safety from accidental contact is secured as well as greater probability of confining trouble to one point in the structure Even though the doors may be blown off the compartment where the trouble starts it is unlikely that the doors of other compartments will be disturbed. In general the use of cell and compartment construction will be fully justified for any important switching equipment in steel mill service.

The actual design of switch structures involves an almost infinite variation in detail depending on the type of breakers used, the
manmer in which the various circuits are to conter and leare the building, the character of the building const ruction and the space available and many other factors. It is, therefore, difficult to preseribe a definite structure design which will fit more than a small percentage of cases and any appreciable amonnt of standardization appars to be impossible. It is obviously desirable, however, and often possible to standardize to some extent the farious structures, installed in one plant, and in selecting a design for a particular location it is well to consider the feasibility for using the same gencral scheme for future work at other probable switching points. However, the best procedure is to work out the arrangement for each substation based on the conditions existing, and to obtain such uniformity as is possible without sacrifice of safety or reliability. The following are some of the points which it is well to bear in mind in designing the structure.

Each phase should be in a separate compartment, where it is necessary to have copper exposed as, for example, in the case of disconnecting switches. Busses and connections, if completely insulated and protected from mechanical injury, may be run on post insulators with all phases in one compartment or entirely in the open and still provide a very safe construction.

Connections should be as direct as possible and should be adequately supported against magnetic stresses resulting from short circuit. Loops which tend to increase the short circuit stresses should be avoided. Connections may be run in walls or floors by use of fiber ducts imbedded in the concrete and properly insulated cable. This often proves a very useful expedient and at the same time gives good protection to the leads.

Oil circuit breakers, disconnecting switches, current transformers and insulators should be so placed that they are readily accessible for inspection as well as quick repair or replacement. A device in an awkward location seldom receives proper attention and causes loss of time if replacement becomes necessary. Deep and narrow compartments are undesirable for this reason.

The possibility of opening disconnecting switches by mistake on circuits carrying load is always a serious danger to operators. A liberal operating aisle may prove a worth
while investment if an accident of this sort occurs and in addition the stracture can often be arranged to minimize the chances of confusing one circuit with another.

If the switching equipment is to perform efficiently its function of safeguarding the power service it must have as an auxiliary a carefully applied and well maintained protective relay equipment. For the best protection the relays must so function as to trip those breakers and only those necessary to isolate a faulty circuit from the rest of the system. Also, the fault must be cleared with minimum delay to lessen the disturbance to the rest of the system and the possibility of synchronous machines falling out of step. On individual fceder circuits the requirements are met by ordinary over-current relays having adjustable time delay which may be set to prevent tripping under normal load fluctuations. For power supply circuits between stations it is usually necessary to trip the breaker at each end of the faulty line in order to clear the trouble. In most cases two or more circuits are operated in parallel making it possible to use balanced current or balanced power relays which depend for their operation on a difference or reversal of power flow over one circuit of the paralleled group. They are, therefore, practically unaffected by overload or short circuit disturbances except on that particular circuit where the trouble exists. The circuit in trouble, however, is tripped out with minimum delay since it is not necessary to depend on long time settings to secure the desired selective action. Reliable relay schemes and devices are available to meet practically every protective requirement and their proper application is a matter of vital importance in steel mill service.

Finally, it is impossible to over-emphasize the value of good appearance. The quality of service secured from electrical as well as other types of equipment is, in the final analysis, greatly dependent on the human element. Switching apparatus installed in a well lighted room, protected from mill dirt, and constructed with the best grade of workmanship, immediately becomes a matter of pride to the individuals responsible for its operation, and the careful attention to details which constitutes good maintenance is difficult to secure unless such an attitude of mind exists.

# Adjustable Speed Main Roll Drives 

By A. K. Bushman<br>Power and Mining; Enginebring Debartment, General Ehectric Company


#### Abstract

There are various methods of obtaining the adjustable speed eontrol of the main rolls used in the manufacture of sted. The author considers the advantages and disadvantages of each, first dealing with the directcurrent methods awalable, incluthy motor fied control, Ward Leonard control and a combination Ward Leonard and motor fiek control. After some general comments covering direct-eurrent mothods as a whole he passes on to consider and discuss the pros and cons of the alternating-current systems which are available and includes under this heading the Kraemer system, Scherbius system and a polyphase brush-shifting, alternatingcurrent motor with shunt characteristics. His contribution is concluded with some general remarks comparing the relative merits of the alternating-current and direct-current systems.-EDitok.


Perhaps no questions in regard to main roll drives in steel mills cause more perplexity than those which arise due to the need for adjustable speed. The object of this article is to present the advantages and the disadvantages of the various types of adjustable speed equipment as they are considered by the electrical manufacturer when preparing recommendations for a proposed installation.

In every case the drive must be fitted to the load, therefore, the first duty of the engineer is to analyze the working conditions carefully and to determine the power required at the different speeds. These are then plotted as points on cross section paper, horse power against speed, and the motor rating must be sufficient to include every point. This rating, due to the inherent characteristics of electric motors which usually fall under one of the three classes, will be constant torque, constant horse power, or a combination of the two. Constant torque is represented by a straight line drawn from the origin (zero speed and zero horse power) at any angle to the axis. Constant horse power of course, is a straight line drawn parallel to the speed axis.

Fig. 1 is typical of the third class. In this case the proposed operating schedule requires constant torque from 220 to 550 r.p.m. and constant horse power from 550 to 750 r.p.m. The low speed of 220 r.p.m. in this particular case is necessary for mill adjustment and is not required for actual production. If the points above $550 \mathrm{r} . \mathrm{p} . \mathrm{m}$. Were not required the motor could be rated at constant torque up to 410 r.p.m. and at constant horse power from 410 to 550 r.p.m.

The principal types of adjustable speed drive available are: direct current with motor field control; direct current with generator field control (Ward Leonard); a combination of motor field control and Ward Leonard control; Kraemer system; Scherbius system, which is built for operation below synchronism only (single range), or for operation both
above and below synchronism (double range). For smaller drives there is also available a three-phase brush shifting motor with shunt characteristics, that is, the motor speed remains practically constant regardless of load. The equipments as applied to main roll drive will be considered in the order given.


Fig. 1. Curve Showing Estimated Power to Roll Round and Flat Bars. Motor Rating 220/550, 550 h.p., 220/550/750 r.p.m.

## Direct Current-Motor Field Control

This consists of a direct-current motor, usually shunt wound, running from a constant potential bus, suitable equipment being provided for starting the motor. Speed adjustment is obtained by means of a rheostat in the motor field. This was the first adjustable speed electric drive devised and for years was the only recourse where constant speed was not satisfactory. It is still highly favored on account of its simplicity and has been used in several notable installations, such as indiridual drive of stands of a continuous strip mill, etc., on account of its adaptability to special control systems. The motor is inherently constant horse power over its speed range and if constant torque is required the motor is oversize at its low speed by approximately the ratio of maximum to minimum speed.

In cost this motor with its control is cheaper than any other adjustable speed drive but. except in the rare cases where direct current is available without conversion from alternating current, the cost of its proportion of the
motor-gencrator or synchronous converter and transformer equipment must also be charged abainst the drive. This charge will often make some ofther expipment competitive on a cost basis.

The efficiency of the installation is low. 'To he sure the motor may be gatranted 92 per cent or better at full kod but the effieiency of the conversion equipment will not average hetter than 90 per cent. Then, too, it is uswal to use a $2: 30$ (0)-volt motor with a 2.50 -volt generator to allow for bus drop, thus the transmission efficiency is 92 per cent. Multiplying the above assumed values, the overall efficiency is 76 per cent. Under ideal conditions this may be bettered by several per cent,
since the maximum speed is limited principally by commutation and stability. By using a liberal design, compensating windings, ete., successful motors have been built with a speed ratio as high as 5) or 6 to 1 , but in large sizes the range is usually kept below 3 to 1 , and 2 to $l$ is a common figure.

## Direct Current - Ward Leonard Control

This equipment consists of a direct-eurrent motor, usually shunt wound, receiving its power from a generator which is also usually shunt wound. The motor operates with its field excited at a constant value and its speed and direction of rotation are controlled by the strength and polarity of the generator field.


Fig. 2. Motor Room of the 14 -inch Hot Strip Mill, Trumbull Steel Company, Containing Two 2300 -kw., 600-volt, Direct-current Generators Direct Connected to 2300 -volt, Synchronous Motors, $150-\mathrm{kw}$. Exciter, Four $800-\mathrm{h} . \mathrm{p}$, and Two $1250-\mathrm{h} . \mathrm{p}$. Direct-current Motors
but an average installation will not be far from this figure.

Another disadvantage of obtaining adjustable speed by motor field control is that it necessitates an uneconomical use of material at the higher speeds. For example, assume a motor rated 1500 h.p., $200 / 400$ r.p.m., 600 volts. This motor will have to be somewhat more liberally designed than a $1500-\mathrm{h} . \mathrm{p}$. . $200-$ r.p.m. 600 -volt machine in order to insure stability and good commutation at 400 r.p.m. From this same mass of material a $3000-\mathrm{h} . \mathrm{p}$., $400-$ r.p.m. motor could be built, but it is impossible to rate this machine $1500 / 3000 \mathrm{~h} . \mathrm{p}$., $200 / 400$ r.p.m. at constant voltage.

No definite figures can be given in regard to speed range obtainable by this method

Evidently the motor is inherently constant torque and, therefore, the material of which it is built is used economically. For example, the rating of a motor of the same physical size as that considered under the heading of Motor Field Control would be $1500 / 3000$ h.p., $200 / 400$ r.p.m., $300 / 600$ volts. In this case, however, the power set is working at full capacity only when the motor is running at top speed which may be but a small part of the time.

Since the motor output and also its voltage are proportional to its speed it is evident t at the motor requires the same current for rated load at any speed and, therefore, the overall efficiency is very low at the low speeds, but is good at high speeds. Assume for example,
the same efliciencies as in the previous example. At $400 \mathrm{r} . \mathrm{p} . \mathrm{m}$. the motor efficiency is 92 per cent and the set efficiency is 90 per cent, the hus loss should be small, say 2 per cent, for the motor and its generator will probably be placed near together. The overall efficiency is therefore is per cont. At 000 r.p.m. The $I$ R losses are the same as for $3000 \mathrm{~h} . \mathrm{p}$. but are twice the percentage of the motor output which is only $1.500 \mathrm{~h} . \mathrm{p}$. at this speed. The motor field loss is also the same, the machine driving the gencrator is running at half load and hence at reduced efficiency and only the motor core loss and friction and the generator core and field losses are reduced in proportion to the load. The efficiencies of this equipment would probably be about as follows: motor 86 per cent, set 85 per cent, transmission 96 per cent, overall just over 90 per cent. At lower specds the overall efficiency is correspondingly decreased. Obviously this type of drive is entirely unsuited for a constant horse power equipiment since neither the main motor nor the generator would ever be used efficiently.

Ward Leonard drives have many advantages to offset their poor efficiency at low speeds. The control is extremely simple and reliable. There is no limit to the speed range for by using forced rentilation of the main motor the speed may be reduced to zero with no diminution of torque. Also, weakening the generator field to reduce the speed causes the motor to regenerate and not only gives a most effective brake for a quick stop, but the stored energy in the motor armature is returned to the line instead of being wasted. When starting, no series resistance is used and the power drawn from the line is only that necessary to accelerate the armature instead of about double this amount as is required when starting from a constant potential bus. When the motor is started and stopped very frequently as on reversing mill drives, this saving of power on each start and stop is a very important item.

In large sizes Ward Leonard equipments are little if any more expensive than a constant speed direct-current motor of the same maximum horse power and speed with control and switchboard and its proportionate share of the direct-current generating equipment. etc. In small sizes, however, the Ward Leonard drive becomes much more expensive on account of the higher cost of several small generators than one large one, also, the separate exciter required for voltage control is a larger percentage of the whole drive.

## Direct Current Combination Ward Leonard and Motor Field Control

Many mills require a combination of constant torguc and constant horse power. In these cases, Ward leomard comtol is used over the constant torque part of the range and motor field control is used for the upper part of the speed range. The high torque passes must be rolled with full field on the motor in order to keep the size and cost of the equip)ment at a minimum, since the current required to give a certain motor torque is inversely proportional to the strength of the motor field, or, in other words, the torque per ampere of a two to one speed motor by field control is half as much at top speed as at full fickl speed. Using a combination of voltage control and motor field control, where the horse power required at various speeds will allow it, effects a marked saving in generator cost over using voltage control for the whole speed range and a large saving in motor cost over using field control alone. Naturally the combination retains the advantages and disadrantages of both components.

## General Comment on Direct-current Adjustable Speed Drives

Direct-current equipment of the types under consideration possess a great adrantage over their alternating-current competitors in that they are well known, had been used successfully for years before alternating-current adjustable speed drives were invented and every one who has had any electrical experience feels that he understands them thoroughly. This feeling in some cases may or may not be justified but it is of great importance nevertheless. Other things being equal or nearly so, the engincer of limited experience will usually prefer direct current.

On the other hand, direct current has two great disadrantages. First, in the great majority of cases it is much less efficient than a corresponding alternating-current drive, due to the losses which are incurred when converting alternating current to direct current; second, it has to carry all its power on two commutators and it is well known that a commutator is always a potential source of trouble. It must be kept clean and free from oil. It must be kept smooth and free from ridges. The brushes must more freely in their boxes and the spring pressure be kept at the proper value. In spite of all care, a short circuit on the bus or a heavy overload or some object dropped on the commutator causes a flash over with the usual results of roughened
surface, burned brush rigeing, ete, often necessitating a shotdown 1.0 grind and slot the commatator. 'These two disadvantages of direct-cument drives were the cause of a persistem effort to develop all afternatingcurrent adjustable speed drive and so far two


Fig. 3. Steel Mill Induction Motor Kraemer Single Range Control, Rated 1400/1400 h.p., 600/405 r.p.m.
successful systems have been developed. While neither system eliminates commutators entirely their size and the power they handle has been greatly reduced and in most cases a large increase in efficiency has been secured.

## Kraemer System

This well known system consists of a synchronous converter running from the slip rings of the main induction motor and delivering direct current to a motor direct connected to the main motor shaft. This apparatus can regulate only below the synchronous speed of the induction motor but its range is unlimited except by economic considerations.

The drive utilizes equipment which is used for other purposes and with which every engineer is acquainted. It should be noted, however, that these familiar machines are used in an entirely new way which introduces difficultics not encountered in their ordinary operation. For example, the direct-current motor direct connected to the main induction motor is operated at maximum speed at minimum voltage and minimum field, and when running at lowest speed it has to generate its highest voltage. The speed of the direct-current motor is fixed by the induction motor and not by the direct-current voltage and motor field except as these factors affect the induction motor. It is evident, therefore, that the direct-current motor is in no sense a "standard" motor.

The synchronous converter also operates peculiarly for its speed is constantly changing, whereas the converter, as commonly known, runs at constant speed. This changing speed of the converter is the weak point of the system for a converter has low synchronizing torque-its torque being merely sufficient to supply friction and windage losses which, of course, are constant at constant speed. Assume, for example, a Kracmer set running light at is per cent below synchronism. The slip of the set from no-load to full-load will be approximately 5 per cent, therefore when the load is suddenly thrown on the main motor the frequency on the synchronous converter is doubted and the converter speed must be doubled. If the frequency increases too fast the converter will fall out of step and stop, leaving the main motor running non-regulating and the converter standing still with alternating current impressed on the slip rings from the induction motor sccondary, with direct current impressed on its commutator from the direct-current motor and with very heavy currents circulating. To insure against this it is often necessary to install a flywheel on the mill solely to reduce the rate of change of load so that the converter will have time to change its speed without exceeding its synchronizing torque. The cost of the fiy-


Fig. 4. Steel Mill Induction Motor Rated 5500/4400/ 3400 h.p., 170 136 105 r.p.m., 6600 -volt, Scherbius Double Range Speed Control Driving the 20 -inch Hot Strip Mill at the Gary Plant of the Illinois Steel Co.
wheel under these conditions must, of course, be charged against the Kraemer equipment, as must also the power required to drive the wheel, since the flywheel would not be necessary with another type of adjustable speed drive.

Another disadvantage of the converter is that it will not rum at very low frequencies and hence there is a gap in the speed range between the non-regulating speed and the highest regulating speed. For the same reason the converter camot be used to give power-factor corrcetion when operating near synchronism. Also, there must be supplied a source of direct current to excite the field of the direct-current motor and of the synchronous converter; thus, continnous operation depends upon the continuity of both an alternating-current and a direct-current system.

This drive having the direct-current motor direct connected to the main motor requires much more room at the mill than would be necessary for the induction motor alone and in case of trouble with the direct-current motor repairs cannot be made while operating non-regulating unless the machines are uncoupled

The Kraemer system has many advantages, and many successful installations testify to its practicability: In common with all the systems described it has its own field in which it is pre-eminent. Its overall efficiency is better than that of direct current and the size of the commutators required are greatly reduced since only the slip energy is carried on two commutators instead of all the energy as is the case with direct current. In addition there is the commutator of the exciter which is of small capacity compared to the main motor.


Fig. 5. Scherbius Double Range Speed Regulating Set for use with the 5500 h.p. Motor shown in Fig. 4

This system is especially suited for drives having large speed ranges when the main motor speed is such as to give an economical design for the direct connected direct-current motor and when constant horse power is
required throughont the speed range. Under these conditions the Kratemer drive will prove cheapest in first cost. It should be noted, however, that in case of trouble with the regulating equipment so that the main motor has to be operated non-regulating, the speed


Fig. 6. Ohmic Drop Exciter $1.6-\mathrm{kv}-\mathrm{a}$. Mounted on Shaft of 600/600/600 h.p., $469375 / 281$ r.p.m., Steel Mill Induction Motor. Scherbius Double Range Control
will be the maximum of which the drive is capable, and, therefore, only a small per cent of the usual sizes of product can be rolled.

## Scherbius System

Although a more recent development than the Kraemer there are more installations of this system in the Lnited States than all other adjustable speed alternating-current drives combined, not including small brush shifting alternating-current motors. The apparatus consists of a main induction motor and a regulating set which in turn is composed of a perfectly standard type induction motor direct connected to a three-phase commutator type regulating machine. The double range system also includes a small machine known as an ohmic drop exciter direct comnected to the main motor.

This system labors under two disadrantages: First, the speed range is limited by the fact that it is undesirable from a design standpoint to handle more than 1.5 to 1 c cucles on the regulating machine. This means that on a 60 -cycle equipment the range is limited to approximately To per cent synchronous speed as a minimum and 130 per cent as a maximum which gives a speed ratio slightly less than 2 to 1 . On 2.5 cycles a 3 to 1 range is easily obtained. Secondly, engineers who have not
hadexperience with the scherbiusdrive feel that it is complicated and involves machines with which they are totally unfamiliar. It cannot be denied that the vector diagrams and design calculations are highly complicated, but the operator is no more concerned with these than with similar and equally complicated calculations involved in the design of an ordinary induction motor. In both cases the results of these calculations are built into thoroughly reliable machines which require only simple and easily understood adjustments and care. The fundamental principles involved are the same as for the Kracmer system and the machines themselves are as easily understood.

The regulating machine is exactly like a modern direct-current generator except it is wound for three phases instead of one. In fact a one line diagram of the two machines is identical. Both are driven at practically constant speed and both generate a voltage which is a function of the shunt field strength. Both have an interpole field and a compensating (pole face) winding to insure good commutation at all loads. The only point of difference is that the direct-current generator is excited with direct current and the regulating machine is excited with alternating current from the main induction motor secondary, and, therefore, generates alternating current of the same frequency as its excitation. In experimental work a directcurrent generator coming through the factory in regular production, by making a few changes, has been used to regulate the speed of an induction motor. The generator was later changed back to a straight direct-current machine.

The small olimic drop exciter is nothing more or less than the armature of a synchronous converter with a ring of sheet iron punchings without windings replacing the usual stationary field. This little machine is pressed on the main motor shaft and receives line frequency on its rings through a potential transformer and so gives slip frequency on its commutator. The only other apparatus involved is a contactor panel and two or three transformers which are used in place of rheostats since all circuits are alternating current

The Scherbius drive reduces the number and size of the necessary commutators to a minimum since the slip energy is handled on but one commutator as against two in the Kraemer. It should, also, be noted that for similar speed ranges the slip energy is much less for double range apparatus than for the

Kraemer. For example, in an equipment giving a speed ratio of 1.67 to 1 the slip energy of the Scherbius drive at maximum regulation is 25 per cent of the primary power while it is 40 per cent under the same conditions with the Kraemer. The commutator of the ohmic drop exciter is smaller than that of the exciter required for the other system and in addition is for very much lower voltageusually about 20 volts.

Operation both above and below synchronism is an extremely valuable feature which can be obtained with good commutation on the auxiliary machine only in the Scherbius system. Double range operation not only greatly reduces the capacity of the regulating apparatus for a given speed range, but in case it is desirable or necessary to run non-regulating, the motor speed is about midway of the range and therefore practically all regular sizes and shapes of product can be rolled. Also, the maximum efficiency is obtained at this average speed at which the mill operates a large part of the time, instead of at maximum speed as in all single range equipments.

There are no synchronous machines in this drive and, therefore, no danger of any part of the apparatus falling out of step. Also, 110 direct current is required for excitation or any other purpose and so there is no dependence on any source of power other than the main alter-nating-current line. There are no gaps in the speed range, any speed from maximum to minimum being obtained by operation of a single control handle, and there is no diminution of overload capacity at any point in the range. When running at synchronous speed the regulating equipment may be used to maintain high power-factor which is very desirable when the power contract carries a clause penalizing low power-factor. The system may be built for constant torque, constant horse power or constant torque below synchronism and constant horse power above, thus it is suitable for practically any combination of speeds and horse power which may be required.

From the foregoing brief outline of Scherbius characteristics the reasons for its use in the majority of adjustable speed alternatingcurrent installations will be evident. The exceptionally large number of repeat orders are evidence of its reliability.

## Polyphase Brush Shifting Alternating-current Motor with Shunt Characteristics

This motor involves the same principles as the Scherbius double range system but in
small sizes it is possible to eliminate the regulating set, contactor panel, transformers, etc., and obtain complete control by means of two sets of brushes whose relative position on the commutat or is altered by means of a hand or motor operated brush shifting mechanism. Thi: motor has characteristics practically identical with the double range Scherbius equyment and fills a long felt want for an adjustable speed alternating-current drive
systems cannot be compared except in relation to a particular set of conditions, therefore, which system is preferable must be determined for each proposed installation and, unfortunately perhaps, camnot be settled once for all. The electrical manufacturer who builds all types chooses the drive for the mill in question just as a workman chooses the proper tool for the work in hand from a well fitted bench. It is only when a complete line


Fig. 7. Scherbius Speed Regulating Sets and Adjustable Speed Induction Motors for Hoop Mill Drive. Finishing Mill Motor in Foreground Rated 180015001200 h.p.,

240, 200 , 160 r.p.m., 2300 -volt, 3 -phase, 60 cycles
where the power required is too small to make Scherbius or Kraemer apparatus feasible on account of the high initial cost of very small installations.

The output of this machine is limited to a sertain maximum per pole and it is, therefore, necessary to use low speeds to obtain high 13tinss. Motors are now being built from 2.5 h p. up to $600 \mathrm{~h} . \mathrm{p}$. with speed ranges up to 3 to 1.

## Alternating Current vs. Direct Current

There has been a great deal of discussion of the relative merits of alternating-current and direct-current drive and each has its ardent supporters. Similarly Kraemer iss. Scherbius has been argued pro and con. A broad view of the subject, howerer, will show that such
is not a vailable from which to choose that it is necessary to try to compare adjustable speed drives as such.

Since alternating-current systems were developed to overcome certain universally recognized defects in direct-current apparatus, it is safe to say that in general alternating current is preferable to direct current if equal results can be obtained. Past this point generalization is dangerous in the extreme. As an example, it may be interesting to note that the same manufacturer recently sold two $4500-$ h.p. mill motors; one was the largest single unit direct-current motor ever built in the United States and the other was the largest Kraemerdrive. Such apparently contradictory recommendations are but the natural result of fitting the drive to the mill conditions.

# Flywheels for Steel Mill Drives 

By 1. A. Lmansky<br>Powle ind Mining Engenering Department, Genteral Electrac Company


#### Abstract

The athor has written a very complete treatise on the use of fly wheds for sted mill drives. He takes into consideration the character of the rolling mill load; the energy of flywhels; characteristies of induction motors; the influene on duty erch; the effect on motor size; cost of operating flywheds; their application and misapplication and steam and efeelrie drives. After covering this part of the subject very completely, under the heading of "Plywhed Calculations," by the aid of mumerous but simple formulae and examples he shows how to calculate the total stored energy; the energy avalable for regulation, and the acecleration and retardation of flywheds. He then shows numerous means of varying the secondary resistance; diseusses direct-current drives, and concludes his contribution with some remarks on the mechanical arrangement.-EDITok.


## Introduction

Flywheels have been known to engincers much longer than electric motors; but the combination of these two devices is hardly twenty years old. Although the fundamental theory of this combination was developed at onee, there still exist today many conflicting views and confused ideas about the use of flywheels for electric drives-even among those that are using them.

For instance, one steel mill superintendent, brought $u_{p}$ in the steam engine days, insists on having all his electric drives equipped with flywheels "In order to reduce the variations of speed with the load;" on the other hand, it is well. known that if we have two elec-trically-driven mills, both equally well designed, but one for flywheel operation and the other for operation without, the former drive should show a greater speed variation than the latter.

The problem before us lies on the borderline between meehanical and electrical engineering, touching both sides. This possibly explains why many practical engineers of either profession are sometimes reluctant to look up their old handbooks, flavoring of mathematics, and prefer to be guided by the "Rule of Thumb."

This fact serves as the excuse for writing this article. Nothing basically new is told in it, but a few old established facts are looked into from a possibly different angle. An attempt is made to consider the problem not merely in a formal way but rather from the standpoint of common sense. Mathematics are not excluded from the discussion, because this science is but systematized common sense; but whenever applied, it is intended as a supplement to the plain reasoning, and not as a means to conceal the lack of physical conception.

## GENERAL CONSIDERATION

Character of Rolling Mill Load
Fig. 1 shows schematically an inductionmotor driving a three-high (i.e., non-reversing) mill; it may be, for instance, a plate mill drive, like the one illustrated in Fig. 2. A slab will be passed between the lower and the middle rolls, and then passed backward between the two upper ones. A number of such passes will be required before the slab is rolled down to a thin plate.

When the metal is in the rolls it is being deformed and elongated and the power required to accomplish this is quite large. During the intervals of time when the slab


Fig. 1. Layout of a Three-high Non-reversing Rolling Mill Driven by an Induction Motor Equipped with a Flywheel
is being transferred from the two lower rolls to the two upper ones, and vice versa, there is no load on the mill except the comparatively small friction load.

Fig. 3 shows a load diagram for a large plate mill. This load, or duty cycle, is none too good for any kind of drive; the load peaks are of a "violent" character, high in value and of short duration. But such is the nature of the rolling work, over which we have but little control; if for instance, the rolling schedule should be maintained and the mill requires $13,300 \mathrm{~h} . \mathrm{p}$. during the first pass, this amount of power should be delivered to the rolls, otherwise the metal will not be put through the mill.

Now, all plate mills are equipped with flywheels. It is admitted that they help the motor considerably in carrying the high peak loads; numerous tests have proven this point. But how is this help extended? How is it that this great rotating mass reduces the amount of power that the motor draws from the line?

## Flywheel Energy

Any rotating mass, or more generally, any moving body possesses a certain amount of energy. It requires an outside effort to bring it up to speed, but once this is done, the energy that was spent for doing it is not lost; it is "stored" in the rotating flywheel, ready"

Without allowing the flywhed to slow down its stored energy is of ano use for our purpose. Imagine the mill being driven ly a sufficiently large synchronous motor. This machine will run at strictly constant speere of will not run at all; and the power input to such a drive will be the same regardless of whether the drive is, or is not, equipped with a flywheel.

## Induction Motors

But our plate mill is driven by an induction motor. We know the inherent characteristic of this machine: the sreater the load imposed the more is the drop in speed, or "slip." Expressed in per cent of the no-load speed (practically the same as the synchronous


Fig. 2. 4000-h.p., 83-r.p.m., 6600-volt Induction Motor Driving a 110-in. Plate Mill
to be liberated and used at will. A wheel of given dimensions and weight possesses a strictly definite amount of such stored energy at any definite speed; this amount is proportional to the square of the speed and we shall show later how to calculate it. But first of all we must understand how to use up, if necessary, a part of that stored energy.

There is but one way of doing it: to let the flywheel slow down. When its speed is reduced, the amount of stored energy is manifestly less; but where is the balance: It was given out as mechanical work at the shaft; in our case it did part of the work of deforming the metal, and the electrical motor made up only the balance of the total work required for the rolling during the pass.
speed) the slip may be assumed proportional to the load, other conditions being equal. Thus if a $1000-\mathrm{h} . \mathrm{p} .600-\mathrm{r} . \mathrm{p} . \mathrm{m}$. (synch.) induction motor runs with a slip of 3 per cent, i.e., at 5 S2 r.p.m. at full load, it will have a slip of only 1.5 per cent ( $591 \mathrm{r} . \mathrm{pm}$.) at $500-\mathrm{h} . \mathrm{p}$. load, and so on.

There is another way of looking at this fact: when an induction motor with a fixed permanent resistance runs with a certain slip, it carries but one, and only this one, definite load. "Tell us the slip and you thus tell the load."

Another factor affecting the slip is the amount of resistance in the rotor circuit. We express it in per cent and say: the motor has 3 , or 5 , or 10 per cent secondary resistance.

The meming of this is: the resistance is such that the motor rums at its full load with is, or $\overline{5}$, or 10 per eront slip. Fore instance, the 1000-1.p. motor refored to above had a $\therefore$ per cent secondary resistance. Assume that we double the ammont of the secondary resistance: the fall hat slip will be 6 pere cent and We shall have a 6 per eent resistance.*

We must keop these hasie facts in mind White discussing the nse of thywheds in conjunction with induction motors.

## Influence on Duty Cycle

Let us seleet, for instance, pass No. 4 , of that duty cyele which is represented by Fig. 3. and see more closely (on Fig. 4) what will take place during that periorl.

The mill is driven by a $3.500-\mathrm{h} . \mathrm{p}$. motor with 5 per cent resistance. Just before the metal entered the rolls, the motor was rumning light overcoming only the mill friction
beeomes smaller and smaller, and therefore the whed does not have then to slow down at the same rate as it did in the begiming.

This performance is well illustrated in Fig. 4: the gradually increasing motor output is shown by the curve AB; the area under it (OARF) gives the amount of work (in h.p.-sec.) done by the motor during that pass. The shaded arca $A(D) B$ stands for the energy given out (in h.p.-sec.) by the flywhect. The motor slip is illustrated by the curve $A^{\prime} B^{\prime}$ in the lower part of the diagram; this curve is proportional to the motor load curve $A B$.

At the end of the pass under consideration (which lasted for 0.9.) seconds) the motor output increased from the original $300 \mathrm{~h} . \mathrm{p}$. to $4.50 \mathrm{~h} . \mathrm{p}$., and the slip from 0.43 per cent to 6.43 per cent. After the metal leaves the rolls at the end of the pass the remaining external load amounts to only 300 h.p.


Fig. 3. Calculated Duty Cycle of a Large Plate Mill. Curve (a) shows the total power required for rolling; Curve (b) indicates the motor output if assisted by a large flywheel
of $300 \mathrm{~h} . \mathrm{p}$.; the corresponding slip is therefore $5 \times \frac{300}{3500}=0.43$ per cent. As soon as the rolling begins the load imposed on the mill rises instantly to $-200 \mathrm{~h} . \mathrm{p}$. ; but the motor cannot assume this whole load, until its slip reaches the value of $5 \times \frac{7.200}{3.000}=10.3$ per cent-a long way off the 0.4:3 per cent that existed at the beginning of the pass. For that reason the load is at first carried almost entirely by the flywheel, which of course slows down inasmuch as it gives out its stored energy. But the more the flywheel and the motor connected to it slow down, the larger becomes the motor slip and proportionally larger becomes the motor's share of the total load. The flywheel's share, on the other hand,

[^71](friction) whereas the motor slip at that instant is such that the motor develops 4.500 h.p. This excess capacity developed by the motor causes the flywheel to accelerate. The fact that the drive speeds up makes the motor slip smaller. and smaller (see line $B^{\prime} E^{\prime}$ ) and therefore the motor output decreases in the course of time (see line $B E$ ). At the end of the interval between the passes the drive may have regained practically the initial speed, corresponding to $300 \mathrm{~h} . \mathrm{p}$. friction load. During this second period the motor obriously develops more power than is necessary to carry the small friction load; the excess of work done by the motor is used to speed up the flywheel, i.e., this work tends to replenish the stored energy partly spent during the previous pass. This is represented by the shaded area $B E F$ in Fig. $t$.

Fig. 3 and also Fig. 4 illustrate very convincingly the effect produced by the flyweel
on the duty cycle: The load "peaks" are greatly reduced and the "valleys" are filled. The power house will be the first part of the steel plant to appreciate such an improvement; or, if the power is purchased the reduction of the maximum demand from 13,300 h.p. to $5500 \mathrm{~h} . \mathrm{p}$. may mean a net saving of a great many dollars per month.

## Effect on the Size of Motor

But this is not the only adrantage of the flywheel. Let us examine the original duty cycle, assuming that no flywheel is furnished. What size motor should be used to drive this mill?

There are two factors that decide this question: the heating of the machine and the


Fig. 4. Effect of the Flywheel on the Motor Load and Speed
maximum torque that it is capable of developing. The heating produced by the original duty cycle, Fig. 3, is considerably more than that corresponding to the average load; this is easily understood when one recalls that the heating is proportional to the square of the load; manifestly the aierage heating load or the root wean square of the duty cycle is ahways higher than the average load and increases rapidly with an increase of the peaks. Thus in our case, the r.m.s. is $4000 \mathrm{~h} . \mathrm{p}$., whereas with a flywheel the r.m.s. of the duty crele is only $2800 \mathrm{~h} . \mathrm{p}$. The arerage load is close to $2.500 \mathrm{~h} . \mathrm{p}$. in either case.

But it will not be feasible to drive the mill even with a $4000-\mathrm{h}$.p. motor without using a flywheel. Every motor has only a limited maximum overload capacity, even for an instantaneous load; in the case of an induc-
tion motor if the lowd exeecels a definite value for each machine, the latter will stall. This stalling or "breaking-down" load is usually around 2.50 per cent of the normal for mill motors. In case of direct-current motors the limit is usually set by the commutation and the 250 per cent value is very seldom execeded.

Assuming 250 per cent as the maximum permissible load, and knowing that the maximum peak of duty cecle, see Fig. 3, is 13,300 h.p., it may be casily seen that no motor smaller than -500 h.p. can be used for driving this mill. It would be safer to install a motor of at least 6000 h .p. to take care of occasional greater overloads. With the use of a flywheel the peak load was reduced from $133,300 \mathrm{~h} . \mathrm{p}$. to $5(600 \mathrm{~h} . \mathrm{p} . ;$ the selected 33000 h .p. motor is capable of developing $9000 \mathrm{~h} . \mathrm{p}$. momentarily:

In other words. the flywheel has permitterd us in this case to reduce the motor size; the drive is not "overmotored;" the aterage power-factor is thercfore higher.

This is the second big factor in favor of the flywheel application.

## Cost of Flywheel Operation

The reader must have noticed that the flywheel has reduced the peak load, but that the average load is not reduced. Obviously, the flywhel does not generate poüer-it only redistributes it. When its speed drops from say, 100 per cent to A.) per cent, the whecl gives out so much energy, but it takes just that amount to bring the speed back to its orjginal value. As long as the speed remains within that range, the flywheel energy will only circulate back and forth, but the amount of power drawn from the line and registered by the watthour meter will not be reduced.

The flywheel is not like a bank that pays interest on the deposited money; it may be rather compared to a broker, retaining commission for each operation-buying or selling alike. And we should now look into the nature of this "commission" to determine under what conditions we are justified in paying it.

In the first place a heavy flywheel needs large bearings, and this increases the friction losses; together with the windage these losses are present whether the mill is rolling steel or is rumning light. These losses are piling up and present an appreciable item in the monthly bill.

Then, the heary wheel itself costs moner: An extra ton of weight means so many more dollars in the first cost. Large bearings are expensive and the cost of their maintenance and of the oil is higher.
'loses consitherations limit as in groing too far in seleoting a heary flywhed.

But we know that it smaller wheed is capable of giving out as much emorgy as a large one provided it is allowed a respectively srabler sperd reduction.

What is the maximmon fermissible redurtions of speed?

The steel mill operators will be the first to protest against poor speed regulation of the mill drise ()ther conditions being equal, the grabater the speed reduction the lower will be the arerage speed, and the lower the speed the smaller will be the tonnage rolled. We should not go beyond 15 per cent in speed recrulation in order to maintain good rolling conditions.

The electrical department will be the next to object to an excessive reduction in speed. They know that the larger is the motor slip the more are the secondary, or the so-called rheostat, losses of the motor. For instance, when the power transmitted to the rotor is $1000 \mathrm{~h} . \mathrm{p}$. , and the slip is 10 per cent, only $900 \mathrm{~h} . \mathrm{p}$. are developed as mechanical power on the motor shaft-the other $100 \mathrm{~h} . \mathrm{p}$. go as waste heat, dissipated in the secondary resistance. By increasing the average slip by, say $\bar{j}$ per cent, we decrease the motor efficiency by a like amount. The kw-hr. per ton of steel rolled will go up-and so will the power bill. The increased power consumption per ton means that the average demand will be somewhat higher if the same tonnage is obtained-or if the average demand will be the same, the mill tomnage will be reduced.

This is the "commission" which is paid for the flywheel assistance. We should be certain always that we gain not less than we pay for.

## Application and Misapplication of Flywheels

A good example of a duty cycle where flywheels do not pay for themselves is shown in Fig. 5; it represents rolling on a continuous mill. Due to the sustained load, the flywheel would not reduce the peak; the r.m.s. values are practically the same-the motor size eannot be reduced, and then the question may rightly be asked: What is the use of going to the expense of installing a flywheel on such a mill and having the increased secondary and friction losses, when, on the other hand, no benefit may be derived from its operation?

This question is usually answered in the negative, and hardly any continuous mills or rod mills are equipped with flywheels.

There are certain classes of mills the duty of which always require flywheels; such, for
example, as the plate and sheet mills, :3-high boomers and the like. But there are other mills that do not lend themselves to any hard and fast rules. 'lake for instance a piercing mill of a tube plant: the duty is severe; only one piece is in the mill at a time and the high load peaks alternate with the light friction load; one is apt to conclude that this would be an ideal application for flywheels. However, the majority of piereing mills are not equipped with wheels, and rightly so.

When the billet to be piereed is short, the whole operation takes only 2,3 , or 4 seconds and the flywheel will very materially assist the motor; piercing mills doing this kind of work should be and usually are flywheelequipped. But when the piereing of one billet lasts for 20 or 30 seconds the flywheel will be all "used up" after, say i. or (i seconds, and for the rest of the period the line input will


Fig. 5. Typical Duty Cycle of a Continuous Mill. Flywheels are of little use for such duty
be about the same as if no wheel were used, unless, of course, we make a flywheel of noncommercial size and weight. Therefore most of the piercing mills run without flywheels.

Thus we see the importance not only of the magnitude of the load peak, but also of its duration. The same flywheel obviously does nuch more good in case (a), Fig. 6, than in case (b), although the first peak is much higher than the second one. This explains very well why it is a mistake to speak of a certain flywheel as capable of "elipping" say, 1000 h.p. off the peak load; such a definition means nothing at all unless the duration of the peak is given.

What determines the capacity of the flywheel is the total amount of stored energy, or that part of it which the wheel is capable of giving out within a certain range of speed; the energy, shown by the shaded area in Fig. 4 is expressed in horse power seconds and not in horse power, and it is thus that the capacity of the flywheel should also be expressed.

The only proper way of deciding whether a mill should have a flywheel or not-is to

Study the duty cyele. If the peakes are only 1.5) per cent, or less, of the momal, and are sustamed, then the chances are that the use of a flywher will not be a paying proposition.

The smaller the drive the less important obriously is the question of a reduction of peaks. On the other hand, the more limited the generating capacity of the steel mill power plant of the higher the maximum demand rates of the power company, the more adrantagenus becomes the applications of flyheels.

## Steam and Electric Drives

Only a few words are necessary to point out how difterent are the reasons for equipping steam engines and electric drives with flywheek.

A reciprocating steam engine has not, and cannot have, an inherently uniform crank


Fig. 6. Influence of the Duration of Pass on the Effect Produced by the Flywheel
effort; obviously, the torque produced by a steam engine varies quite appreciably during one revolution, depending on the position of the pistons. A single cylinder engine could not pass the dead centers if not assisted by the stored energy of the rotating masses. On this account, even with a perfectly uniform load, the steam engine would vary its speed during one revolution, if not furnished with a flywheel of proper capacity. Thus, in this case, the flywheel is needed primarily to correct the inherently poor speed regulation of the drive, and only secondarily for the load equalization.

With electric drive the problem is entirely different. The torque produced by the motor is uniform; there are no dead centers; the motor speed regulation is so good that it is necessary to increase it artificially in order to utilize the flywheel; thus the latter is not needed for correcting some inherent deficiencies of the drive, but for the single purpose of equalizing the load.

## FLYWHEEL CALCULATIONS

After the general purpese of flywheed applications to mill drives hats been made reasonably clear, it may be worth while to show briefly by a few concrote examples how the various fly whed calculations can be made.

## Total Stored Energy

Assume a large flywheel having a $\|^{1} R^{2}=$ $15,000,000 \mathrm{ll}-\mathrm{ft} .^{2}$ (i.e., an effect of $\left.\mathrm{F}, 0,000,000\right)$ 1 b . at 1 ft . radius or of $3,750,000 \mathrm{lb}$. at 2 ft . radius, etc.) and a wheel speed of 8.3 r.p.m. What is the total amount of energy stored in the wheel?

The energy ( $E$ ) possessed by any body of weight II lb . moving with a velocity of $V \mathrm{ft}$. per sec. is

$$
\begin{equation*}
E=\frac{U^{1} \times V^{2}}{32.16 \times 2} \mathrm{ft}-11 \tag{1}
\end{equation*}
$$

$(32.16 \mathrm{ft}$. per sec. is the rate of gravity acceleration). The rotating fiywheei with a given $\| R^{2}$ and running at $n$ r.p.m. may be considered as a body with weight II moving with the same velocity as the end of its radius of gyration $R$; this velocity in ft . per sec.

$$
\begin{equation*}
Y=\frac{2 \pi R \times(\mathrm{r} . \mathrm{p} . \mathrm{m} .)}{60} \tag{2}
\end{equation*}
$$

Substituting this value in (1), obtain

$$
\begin{align*}
E= & \frac{1 W^{2} \times(2 \pi R)^{2} \times(\text { r.p.m. })^{2}}{2 \times 32.16 \times(60)^{2}}= \\
& \frac{\pi R^{2} \times(\text { r.p.m. })^{2}}{5865} \mathrm{ft}-1 \mathrm{~b} . \tag{3}
\end{align*}
$$

In the example

$$
E=\frac{15,000,000 \times 1.3^{2}}{.58(5.5}=17, .500,000 \mathrm{ft}-1 \mathrm{~b}
$$

This energy is strictly equal to the amount of work which was required to bring the flywheel from rest to the speed of $n$ r.p.m.

As

$$
\begin{align*}
& 1 \mathrm{~h} . \mathrm{p} .-\mathrm{sec}=5.50 \mathrm{ft-1h} .  \tag{4}\\
& \begin{aligned}
E & =\frac{11 R^{2} \times(\mathrm{r} . \mathrm{p} . \mathrm{m} .)^{2}}{3.226,000} \mathrm{~h} . \mathrm{p} .-\mathrm{sec} . \\
& =31,900 \mathrm{~h} . \mathrm{p} .-\mathrm{sec} .
\end{aligned} \tag{.}
\end{align*}
$$

We note that these formulas express the well known facts: the stored energy is proportional to the $1 R^{2}$ of the wheel and to the second power of its speed.

## Amount of Energy Available for Regulation

The energy as calculated above is the total amount stored in the wheel at a certain speed. How much of this amount may be used for load equalization in case the flywheel is installed at the mill drive?

We with assume that a speed variation of more than io per cent is not permissible, $i$ e., in this case the whed speod will vary from A3 r.p.11. (max.) to 70.5 r.p.m. (min.). $\Lambda t$ 7().5 r.p.m. the stored eneryy will be, as per equation (.) :

$$
E_{2}=\frac{15,000,000 \times 70.5^{2}}{3.2: 30,000}=22,950 \mathrm{~h} . \mathrm{p} . \mathrm{sec} .
$$

Thus the energy given out is:

$$
31.900-2.950=89.00 \text { h.p. }-\mathrm{sec} .
$$

or approximately $2 \mathrm{~S}_{\mathrm{p}}$ per cent of the total.
Thus it is evident that the per cent of energy given out is not directly proportional to the per cent of speed reduction. On this account it is advisable to give the general relation between the two ralues.

Suppose that the flywhed ${ }^{1 /} R^{2}$ drops its speed from $n_{1}$ r.p.m. to $n_{2}$ r.p.m. The speed reduction (s) expressed as a fraction of the maximum operating speed $\left(n_{1}\right)$ is:

$$
\begin{equation*}
s=\frac{n_{1}-n_{2}}{n_{1}} \tag{6}
\end{equation*}
$$

or, the minimum speed is:

$$
n_{2}=n_{1} \times(1-s)
$$

Now, the total amounts of stored energy at wheel speeds of $n_{1}$ and $n_{2}$ r.p.m. are:

$$
E_{1}=\frac{\| R^{2} \times n_{1}^{2}}{3,226,000} \text { h.p.-sec. }
$$

and

$$
E_{2}=\frac{\Pi^{2} R^{2} \times n_{2}^{2}}{3,226,000} \text { h.p.-sec. }
$$

respectively.
Hence the energy given out comprises the following portion of the total:

$$
\begin{equation*}
\frac{E_{1}-E_{2}}{E_{1}}=\frac{n_{1}^{2}-n_{2}^{2}}{n_{1}^{2}} \tag{8}
\end{equation*}
$$

Transposing:

$$
\begin{gather*}
\frac{E_{1}-E_{2}}{E_{1}}=\frac{n_{1}-n_{2}}{n_{1}} \times \frac{n_{1}+n_{2}}{n_{1}}=s \times \frac{n_{1}+n_{1}(1-s)}{n_{1}}= \\
s \times(2-s)=2 s-s^{2} \tag{9}
\end{gather*}
$$

Giving $s$ (speed reduction) various values from 0 to 1 (or from 0 to 100 per cent) we may calculate the corresponding portions of the total energy given out. These calculations are shown in Fig. 7. For instance, if the speed reduction is 12 per cent $(s=0.12)$ the flywheel gives out approximately 20. 5 per cent of the total energy available at the maximum speed. It is worth noting that at the beginning of retardation for one per cent drop in speed more energy is given out than when the wheel was previously retarded. At 50 per cent speed reduction, three quarters of the total energy is already used up.

Acceleration and Retardation of the Flywheel Example 1

Assume that the wheel should be accelcrated at a uniform rate from $n_{2}$ r.p.m. to $n_{1}$ r.p.m. in $t$ seconds. Hence the rate of acceleration will be

$$
\begin{equation*}
a=\frac{n_{1}-n_{2}}{t} \text { r.p.m. per sec. } \tag{10}
\end{equation*}
$$

If the inertia of the wheel is $W R^{2} 1 \mathrm{~b}-\mathrm{ft} .^{2}$ then there will be required during this period an uniform accelerating torque

$$
\begin{equation*}
T_{a}=\frac{\Pi R^{2} \times a}{30 \mathrm{~s}} \mathrm{Hb-ft} . \tag{11}
\end{equation*}
$$

For instance, if the same wheel, as was considered above ( $\mathrm{II}^{\prime} \mathrm{R}^{2}=1.5,000,000 \mathrm{lb-ft} .^{2}$ ),


Fig. 7. Energy Given Out by a Flywheel at Various Reductions of Speed in Per Cent of the Total Energy at Maximum Speed
is to be brought from rest ( $n_{2}=0$ ) to $n_{1}=83$ r.p.m. in 10 seconds, then the required torque

$$
T_{a}=\frac{15,000,000}{30 S} \times \frac{\varsigma 3}{10}=405,000 \mathrm{lb}-\mathrm{ft} .
$$

If the flywheel must be brought to this speed by an 8.3 -r.p.m. motor, the latter will have to develop during the acceleration a torque (in addition to the friction torque) which corresponds to a

$$
\frac{405,000 \times 83}{52.50}=6440 \text { h.p. load. }
$$

## Example 2

Assume now that the same flywheel, as considered in Example 1, runs at 83 r.p.m. and its speed is then reduced to $50 \mathrm{r} . \mathrm{p} . \mathrm{m}$. at a uniform rate, in 3 seconds.

When it is slowing down the flywheel gives out some of its energy. Therefore no torque is required to drive it but, on the contrary,
the whee itself develops a torgue. What does this torque amount to:

The rate of acceleration is

$$
a=\frac{50-53}{3}=-\frac{3: 3}{3}=-11 \text { r.p.m. sec. }
$$

( 6 is nerative and we therefore call! it "retardation"). L'se the same formula (11), as before and determine

$$
\begin{equation*}
T=\frac{15,000,000 \times 11}{305}=535,000 \mathrm{lb}-\mathrm{ft} . \tag{11a}
\end{equation*}
$$

## Induction Motor Characteristics

The majority of all mills equipped with flywheels are driven by induction motors. For this reason little need be said to remind the reader of some fundamental characteristics of these machines, in order to make the discussion clearer.


Fig. 8. Slip-torque Characteristic of Induction Motors

Fig. $S$ shows the speed-torque curve $(O B C)$ of an induction motor with a fixed resistance in its secondary. Starting at small values (point $O$ ) the slip at first increases proportionally to the torque; then the curve bends over until, at point $B$, the torque begins to decrease with the increasing slip. Torque $T_{B}$ is the breaking-down torque of the motor. We have previously mentioned that it is usually about two and one half times the normal torque ( $T_{n}$ ) for mill motors. If the load exceeds $T_{B}$-the motor will stall.

Within the operating range the speedtorque or the slip-torque curve is very nearly a straight line; this is especially true in our
case, when flywheres are usell for the express purpose of reducing the maximum leat on motors. This fact explatins why we assume in our reasoning that the motor torgue is proportional to its slip.

If, for instance, our motor has an instantaneous value of slip) $-s$ (Fig. h) then it develops at that instant the corgue

$$
\begin{equation*}
T=\frac{T_{n}}{s_{n}} \times s \tag{12}
\end{equation*}
$$

where $T_{n}$ and $s_{n}$ are the nomal torque and slip.

If the secondary resistance is changed, another curve (for instance $O B^{1}$ ) will represent the slip-torque relation. However, the value of the breaking down torque $T_{B}$ will not be affected by this change.

Assume now that an induction motor, having a synchronous speed of $n_{s}=600 \mathrm{r} . \mathrm{p} . \mathrm{m}$. runs with a slip $s=0.0 .5$, and develops a torque $T=8750 \mathrm{lb}-\mathrm{ft}$. With a slip of 5 per cent, the motor speed is

$$
\begin{align*}
u & =n_{s}(1-s)  \tag{13}\\
& =600(1-0.05)=570 \mathrm{r} . \mathrm{p} . \mathrm{m} .
\end{align*}
$$

The horse power $P$, developed at the motor shaft is,

$$
\begin{align*}
P & =\frac{T \times n}{52.50}  \tag{14}\\
& =\frac{8.50 \times .570}{52.50}=9.50 \mathrm{~h} . \mathrm{p} .
\end{align*}
$$

But this $P$ is only the mechanical power developed by the motor at its shaft; it is less than the power input from the line, as measured by the watmeter (we will call it $P_{0}$ ) because part of this input will be lost as copper loss and core loss in the stator of the machine; the remaining balance ( $P_{\mathrm{s}}$ ) is then transmitted magnetically through the air-gap to the rotor. For a given line input $P_{2}$ the power $P_{s}$ has a definite value.

But even the power transmitted to the rotor ( $P_{s}$ ) is not entirely converted into mechanical power at the shaft. When the motor runs with a slip there exist secondary losses, which are approximately proportional to the slip; with. say, i per cent slip, 5 per cent of the power $P_{s}^{-}$may be assumed as lost on that account.

The secondary losses are partly in the rotor winding and iron, but with an external permanent resistance the bulk of these losses is outside the motor and may be charged to the use of this resistor.

After the secondary losses are subtracted from $P^{\prime}$ s the balance is the mechanial power at the motor shaft $(P)$ :

$$
\begin{align*}
& P=(1-s) \times P  \tag{1.5}\\
& P_{s}=\frac{P}{1-s}=\frac{0.00}{0.95}=1000 \mathrm{~h} . \mathrm{p} . \tag{16}
\end{align*}
$$

The secondary losses

$$
P_{r}=P_{s}^{*} \times 0.0 .5=50 \mathrm{~h} . \mathrm{p}
$$

Thus the power $P_{s}$ is the sum of the shaft output and of the secondary bosses. It is clear from (14) and (1.5) that

$$
\begin{equation*}
P_{s}=\frac{T \times n_{s}}{i 2.50} \tag{17}
\end{equation*}
$$

The value $n_{s}$ (synehronous speed) is at constant; therefore the torque $T$ and the power $P_{s}$ are always proportional to each other, regardless of the actual (mechanical) speed. For that reason $P_{s}$ is quite frequently (but not accurately') called "the h.ptorque;" this means, that $P_{s}$ is the horse power that the motor would develop delivering the torque $T$, but running at synchronous speed. More properly it should be called the "equivalent h.p.," because it is the measure of the heating load imposed on the machine, regardless of whether it runs with a small or large slip.

Starting from rest, and drawing normal current from the line the motor at first does not develop any power at the shaft (because the speed is zero) but the secondary losses are high (see Fig. 9). With the increased speed (the torque remaining constant) the losses are being reduced and the mechanical power increases. The "equivalent h.p." $P_{s}$ is constant throughout this period, as also is the line input.

If the motor is rumning and we introduce more resistance in the secondary, maintaining constant line input, we shall observe that the speed $n$ and the mechanical (shaft) power $P$, see (13) and (1.5), both decrease in the same proportion; this means, of course, that the torque $T$ is not changed.

Assume that we increase, in the above example, the motor slip to 10 per cent; then

$$
\begin{aligned}
P_{s} & =1000 \mathrm{~h} . \mathrm{p} ., \text { as before } \\
n & =600 \times .90=450 \mathrm{r} . \mathrm{p} . \mathrm{m} . \\
P & =1000 \times 0.9=\frac{900}{540} \mathrm{~h} . \mathrm{p} .=5750 \mathrm{lb}-\mathrm{ft} .
\end{aligned}
$$

which is the old value.
This is a very important conclusion; it means for instance, that when an induction motor drives a mill without any flywheel and is called upon to develop a certain torque (for instance when taking a certain draft on a
certain bithet) mothing is gained by increasing the secondary resistance; as long as the torque requirements are the same, the increased resistance only means lower speed, proportionally smatler mechanical horse power and respectively higher secondary losses; but the total power and therefore the line input will be the same as mentioned previously. It is clear enough now that a drive without a flywhed does not have to have any external permanent resistance; the speed regulation dees not need to be as large as with a flywheel.

## Motor Load Curves

We have shown in Figs. 3 and 4 the influence of the flywheet on the motor load, and have explained in a general way why the motor load is represented by the curves of the given shape. It is necessary now to show how these curves are actually calculated.

Assume a mill being driven by an induction motor of $P$ horse power and $n$ - r.p.m. (syn-


Fig. 9. Relative Proportion of Mechanical Power and Secondary Losses of an Induction Motor at Various Values of Slip
chronous speed). The mill is running light and the motor is developing only the friction torque $T_{0}$. Then the metal enters the rolls and this imposes a combined torque $T_{1}$. (See Fig. 10.) The torque developed by the motor ( $T$ ) will gradually increase, as we know, along some curve $\dot{A} B$.

What is this motor torque after, say, $t$ seconds?

At any instant the external torque $T_{1}$ is counter balanced by two torques:
$T=$ Motor torque to be determined.
$T_{f w}=$ Torque developed by the retarding flywheel.
In other words:

$$
\begin{equation*}
T_{1}=T+T_{f w} \tag{18}
\end{equation*}
$$

If the motor develops the torque $T$, it means that the slip at that instant is, see (12),

$$
\begin{equation*}
s=s_{n} \times \frac{T}{T_{n}} \tag{19}
\end{equation*}
$$

or

$$
T=\stackrel{T_{n}}{S_{n}^{n}} \times s
$$

The worque delivered be the slowing-down flywhed of known flywhed effect (IV $R^{2}$ in $1 b-\mathrm{ft} .{ }^{2}$ ) depends exclusively on the rate (a) in r.p.m. per see. at which it retards; we have shown previonsly in one example how to calculate it. (See 11-a).

It equals

$$
\begin{equation*}
T_{j z w}=\frac{11 R^{2} \times a}{30 s} \tag{21}
\end{equation*}
$$

What is the rate of retardation $a$ ? So far all that we know about it is, that it is not a constant value throughout the entire period; this makes it necessary to consider its instantaneous value at any selected instant, and not merely the arerage. When the time $(t)$

In this equation onlys and $t$ are unknown and variable; the other quantities have a definite and constant value throughout the period under consideration. We must determine from (2.0) how the slip $s$ changes with time $t$, and if we know the slip it is the same as if we knew the motor torgue $T$

Now, the equation (2.i) (ammot be solved with elementary mathomatics. It is a socalled lincar differential equation and it would be outside the scopee of this article to show how it is solved. W'e shall therefore write the answer directly:

$$
\begin{equation*}
T=T_{1}-\frac{T_{1}-T_{0}}{c^{A t}}\left({ }^{*}\right) \tag{26}
\end{equation*}
$$

where

$$
\begin{equation*}
A=\frac{308 \times T_{n}}{\| R^{2} \times n_{s} \times s_{n}} \tag{27}
\end{equation*}
$$



Fig. 10. Study of Flywheel and Motor Performance
increases slightly by a very small quantity (dt), see Fig. 10, the slip increases also by a verysmall quantity (ds) ; the respective change of speed is obviously

$$
\begin{equation*}
\dot{n}_{s} \times d s \tag{22}
\end{equation*}
$$

If the speed changes thus in $(d t)$ seconds, it means that the rate of acceleration is

$$
\begin{equation*}
a=n_{s} \times \frac{d s}{d t} \tag{23}
\end{equation*}
$$

and therefore the torque developed by the flywheel. see (21). is

$$
\begin{equation*}
T_{\text {fiu }}=\frac{\Pi R^{2} \times n_{s}}{30 \mathrm{~S}} \times \frac{d s}{d t} \tag{24}
\end{equation*}
$$

Hence, see (1s), (20), (24);

$$
\begin{equation*}
\frac{\Pi R^{2} \times n_{s}}{30 s} \times \frac{d s}{d t}+\frac{T_{n}}{s_{n}} \times s=T_{1} \tag{25}
\end{equation*}
$$

[^72]The expression (26) is the so-called formula of Gasche, used since 1910 for flywheel calculations. The value of $A$ is a constant for a given motor and flywheel, provided the secondary resistance is permanent (otherwise the value of normal slip $s_{n}$ will change). We shall call A the "motor-flywheel constant;" once determined it will be used throughout the calculations for the same drive.

## Example 1

A short example will illustrate this method and will show how simple are its applications.

Let:
Motor rating, $3.500 \mathrm{~h} . \mathrm{p}$.
Synchronous speed, $n_{s}=8.3 .3$ r.p.m.
Synchronous torque.

$$
T_{n}=.52 .50 \times \frac{3.000}{83.3}=2.21 .000 \mathrm{lb}-\mathrm{ft}
$$

Nornal slip (with 5 per cent resistance) $s_{n}=0.05$.
Flywhere cfect, $11 K^{2}=15,000,000 \mathrm{lb}-\mathrm{ft} .^{2}$
Thus the motor-flywhed constant is, per (27):

$$
A=\frac{305 \times 2.01,000}{1.5,000,0000 \times 3.3 .3 \times 0.0 .5}=1.1
$$

We shall see how this drive will behave during the pass shown in fig. 10 .

The initial motor load at the begimning of the pass depends, of course, on the previous conditions; when the rolling just begins after a considerable time interval, the initial load equals the friction load; in a more general case, the initial load may be higher. In this example we shall assume that when the pass begins the motor did not regain as yet its
in Fig. 10; for the 2nd Period, the "external" torque $T_{1}=$ friction torque $;$ the "initial" torque $T_{0}=$ torgue at point $B$; the time is, of course, measured from point $F$.

Orclinarily it is not necessary to calculate as many points as was done in the tabulation. It is most important of all to find the motor load at the end of the periods ( $B$ and $C$ ) and for quick calculations this is sufficient. The next period will start from $C$, with initial torque $T_{0}=29,900 \mathrm{lb}-\mathrm{ft}$., and by calculating, two points similar to $B$ and $C$ for each pass a fairly complete picture of the performance will be determined.

## Example 2

Assume now another case: how to determine the size of the flywheel, if the motor peak load is to be limited to a predetermined value?

TABLE I

no-load speed and that it was developing about $400 \mathrm{~h} . \mathrm{p}$., or

$$
T_{0}=25 ; 000 \mathrm{lb}-\mathrm{ft} .
$$

The external load imposed on the mill including friction is

$$
T_{1}=475,000 \mathrm{lb}-\mathrm{ft}
$$

(equivalent to $7530 \mathrm{~h} . \mathrm{p}$. at $83.3 \mathrm{r} . \mathrm{p} . \mathrm{m}$.).
The calculations made in accordance with (26) are tabulated in Table I, and plotted in Fig. 10.

The values of $\varepsilon^{A t}$ were read from the curve Fig. 11, plotted on semi-logarithmic paper, against respective values of $A t$.

The and Period, as included in Table I, covers the time when the metal is out of the rolls and when the motor is regaining its speed. Exactly the same formula (26) is used for this part of the calculations as for the 1 st Pcriod. The definitions are shown

We shall consider the same mill and motor as before. The external load (Fig. 12) is $T_{1}=400,000 \mathrm{lb}-\mathrm{ft}$.; it lasts for 2.1 sec .; the initial motor torque is $T_{0}=2.5,000 \mathrm{lb}-\mathrm{ft}$. How big should the flywheel be to limit the motor load to, say, 1.50 per cent normal?

The maximum motor load during this period will occur at the end of the pass, that is, after $t=2.1 \mathrm{sec}$. Its value should not be more than

$$
T=1.5 \times 221,000=331,500 \mathrm{lb}-\mathrm{ft} .
$$

Substitute these values in (26), and deter$\operatorname{mine} e^{A t}$ :
$e^{A t}=\frac{T_{1}-T_{0}}{T_{1}-T}=\frac{400,000-25,000}{400,000-331,500}=\frac{375,000}{68,500}=5.5$ From curve, Fig. 11, we shall find that for $e^{A t}=5.5$,

$$
A t=1.72
$$

and therefore, for $t=0.1$

$$
A=\frac{1.72}{2.1}=0 . \mathrm{s} 2
$$

Substitute this value in expression (27) to determine the flywheel effect $W^{\prime \prime} \mathrm{K}^{2}$ :

$$
\begin{gathered}
11 R^{2}=\frac{30 \mathrm{~s} \times T_{n}}{A \times n_{\mathrm{s}} \times s_{n}}=\frac{305 \times 2.21,000}{0.5 .2 \times 5.3 .3 \times 0.05}= \\
20,000,000 \mathrm{lb}-\mathrm{ft} .^{2}
\end{gathered}
$$

## means of varying the secondary RESISTANCE

## Effect of Secondary Resistance on Load Curves

We have heretofore assumed that the motor secondary resistance is j per cent. What will be the effect on the load curves if we increase this resistance to any other value, say, 10 per cent?


Fig. 11. Curve Giving Values of $e^{-/ /}$for Different Valu

This value is of course, the theoretical minimum that should be used under these circumstances. It is interesting to compare the two examples. Whereas in Example 1 the external load is higher, and the flywheel is smaller, still the maximum motor load is only $285,000 \mathrm{lb}-\mathrm{ft}$. or 128 per cent normal, as against 150 per cent in Example 2. The obvious reason for this is, that the duration of the pass was increased from 0.8 sec . to 2.1 sec .


Fig. 12. Case Considered in Example 2
It will be shown in the following how to obtain the same reduction of load peaks with a smaller wheel.

Before making the calculations, let us reason as follows:

With a larger secondary resistance the motor acquires a more pronounced drooping speed characteristic; thus the flywheel delivers more work, and the motor's share of the load is smaller. In other words, the motor more readily "yiclds" to the load and "relies" in a greater degree on the flywheel to carry it.

This reasoning is fully sustained by the following example:

The same motor and flywheel are considered as in Example 1. The initial motor load $T_{0}=30,000 \mathrm{lb}-\mathrm{ft}$., the imposed external load $T_{1}=425,000 \mathrm{lb}-\mathrm{ft}$., the duration of pass $t=2.5 \mathrm{sec}$. Similar calculations, as shown in Table I, were made both for $\bar{j}$ per cent and 10 per cent resistance and plotted in Fig. 13. It is obrious how the change of resistance affects the calculations: with 10 per cent resistance the normal slip is: $s_{n}=$ 0.10 instead of $s_{n}=0.05$ and therefore the "flywheel constant" A (see 27) is one half of its former value. Therefore the quantities $A t, e^{A t}$, and finally $T$ will be the same for 10 per cent resistance as for 5 per cent, but at the time $2 t$ instead of $t$. Hence the simple rule for re-plotting the motor load curve
from "is per cent" 10 " 10 per cent:" double the abscssate: $(B=2 \times(A)$ as shown in Fig. 1:3; repeat this for sereral points, and this will determine the " 10 per cent" curve during the rolling period. If the secondary resistance is not doubled, but changed in some other ratio, then the abseissae shoukd be changed in that same proportion.

The increased resistance reduced the maximum peak from $392,2001 \mathrm{lb}$-ft. (equivalent to $(6200 \mathrm{~h} . \mathrm{p}$.$) to 32 \mathrm{t}, 000 \mathrm{lb}-\mathrm{ft}$. ( $5140 \mathrm{~h} . \mathrm{p}$. .) or from 17 per cent to 146 per cent of normal. The average slip) values are ( 6.5 per cent and 9.7 per cent respectively. On the other hand, with the doubled resistance, the maximum slip is 14.6 per cent instead of the former s.s.i per eent; this means that the flywheel has spent (see Fig. 7) 27 per cent of its total stored encrgy instead of only 17 per cent ; the motor is "lazy," especially at the beginning of the pass, when it carries for nearly 1.2.) seconds (out of the total 2.5 seconds) less than its rated torque. With a 5 per cent resistance the motor load reaches its normal value in a fraction of a second $(0.6 \mathrm{sec}$.$) and this accounts for the fact that$ less encrgy is extracted from the flywheel, i.e., more of it is left for use during the next passes. The rheostat losses are calculated and plotted in Fig. 13; they amount, for one pass to $0.306 \mathrm{kw}-\mathrm{hr}$. with 5 per cent resistance and to $0.446 \mathrm{kw}-\mathrm{hr}$. with 10 per cent resistance. Thus we arrive at an obvious conclusion: it is desired to have a small resistance at the beginning of the pass, in order to let the motor do the work, to keep the average rolling speed high and the secondary losses low. But when the gradually increasing load reaches a certain value, say, 150 per cent, normal, it is desired to increase the resistance in order to prevent the load from exceeding that value.

## Notching-back Method

This desired end is obtained very simply by the use of a so-called "notching-back" relay, which acts as follows:

The regulating resistance in the rotor circuit is subdivided in two parts, each of them amounting to, say, 5 per cent. The first block of resistance always remains in the circuit-hence its name-"permanent resistance." The second part is normally short circuited by a contactor; but when the motor load exceeds the predetermined value, a "notching-back" relay causes that contactor to trip, thus throwing the additional
secomdary, and colting down the motor boad to one half at that instant.

Fig. 1:3 illustrates this performance. At point $K$ the motor load reached 1.50 per cent of normal, its slip is $\mathbf{7} . \mathrm{i}$ per cent; the notchingback relay inserts another if per eent in the circuit, makings a total of 10 per cent. Now (in) induction motor, with 10 per cent resistance, running at $7 . \overline{\text { in }}$ per cent slip camot carry more than three quarters of its normal load, and therefore the load drops instantly to point $L$, which is 7 is per cent of normal (or one half of the loarl $K$ ). From point $L$ the


Fig. 13. Motor Load, Slip, and Secondary Losses for Different Values of the Permanent Resistance and Also with the Notching-back Control
motor load builds up as per line $L M$, which is nothing else but the previously plotted " 10 per cent" line $P Q$, only moved to the right over the distance $P L$. At the end of the pass the load is $297,000 \mathrm{lb}-\mathrm{ft}$. ( $4710 \mathrm{~h} . \mathrm{p}$.) or 134 per cent normal. The maximum slip (at point $M$ ) is 13.4 per cent, the stored energy given out is 25 per cent. The average slip during rolling is 7.6 per cent. The secondary losses for this pass are only 0.365 kw -hr.

## General Electric Notching-back Control

A good example of an effective notchingback equipment is shown in Fig. 14

The mill motor is shown diagrammatically, with reversing switeles in the primary and with a part of the secondary control. The permanent resistance $t$ is always in circuit; the notching-hack resistance $B$ is normally short circuited by the contactor ( $C$, but the latter trips out at heary loads, actuated by the nothing-hack relay $D$. The three-phase coil of this relay is energized by the voltage drop across the permanent resistance $A$ (when the contactor ( is closed, the potential at points $L_{1}, I_{-2}, L_{-3}$ is the same as at points $K_{1}$, $K_{2}, K_{2}$ ). In other words, the magnetic flux of the notching-back relay is proportional to the secondary eurrent of the motor, i.e., to


Fig. 14. Wiring Diagram of the General Electric Notchingback Control as Applied for Steel Mill Drives. The insert shows schematically the new notching-back relay
the kw. load and not to the $\mathrm{kv}-\mathrm{a}$. input to the machine.

When the relay is not energized, its contact 1 is closed; this energizes the relaying contactor $M$. which keeps the notchingback contactor $C$ closed; the contactor $\lambda$ is at that time open not only because it is mechanically interlocked with $M$, but also because both ends of the coil $N$ have the same potential.

When the motor load reaches the predetermined ralue, the relay $D$ picks up, the contact 1 breaks and the relay armature moves from 1 to 2 . Quick as this movement is, we may distinguish the following separate phases of it:

The opening of the comtact $I$ does mot cause in itself the tripping of the motchingback contactor; the erils of the (wo relaving contactors, $M$ and $A$, are then connected in series across the lines, but while the eontactor $M$ is closed, and its imperlance is high, the contactor $N$ is still ogen and has therefore a lower imperdance; for this reasom the total line voltage is not divided evenly between the two coils: the voltage across the coil $1 /$ may be more than !o per cont of the wal which causes the contactor if to stay elosed and $\lambda$ to stay open. After the relay armature completes its travel, the contact ¿ closes, full voltage is then appled to $\lambda$, and the latter closes; the contactor $M$ is tripped; this, in turn, trips the notching-lack contactor, throwing additional resistance in the rotor and immediately cuts down the motor load and the secondary current in proper proportion. Although the secondary current is thus reduced, the relay coils are energized from the voltage across a larger resistor, and therefore the relay will stay closed.

After the load decreases below the set value, the voltage drop across $H_{1}-L_{1}, H_{2}-L_{2}$, $H_{3}-L_{3}$ becomes insufficient to hold the relay armature. The contact ? opens and after the 1 closes the contactors $i l$ and $N$ return to their original positions; the contactor $C$ cuts out again the notching-back resistor.

Sometimes the load fluctuates close to the relay setting and the armature would pick up and would just make and break the contact 1 without traveling all the way across the air gap to make the contact 2 ; such oscillations will not be reflected, howerer, on the notching-back contactor as is clear from the description of the system. This is the main reason for employing the small relaying contactors $M$ and $N$. The tips of the contactor $\lambda$ do not carry any current and it is employed merely to provide for the proper functioning of $M$.

The relay setting may be adjusted within wide limits by changing the tension of its spring, by varying the distance between tips and also by adjusting the resistance $R_{1}-R_{2}-$ $R_{3}$. It is customary to set it to trip the notching-back contactor at about 150 per cent load, and to close the latter again when the load goes down to about 7.5 per cent. The closing of the notching-back contactor will cause the instantaneous value of the load to double (if resistance $B$ equals $A$ ) and it will then decrease gradually.

It is perfectly feasible to have the notchingback resistor subdivided into several sections,
cach short-circuited by a seprarate contactor and controlled by a separate relay. 'The latter should be set at gradually inereasing values, so that the secondary resistance is increased with the load in several smaller steps. Practice has shown, however, that such


Fig. 15. Elementary Diagram of a Liquid Slip Regulator
a refinement is very seldom needed, and the one-step notching-back equipment, as described, meets the steel mill requirements quite satisfactorily.

## Liquid Slip Regulators

There is another device for regulating the secondary resistance with the load in order to smooth out the peaks. This apparatus (see Fig. 15) known as a liquid slip regulator, consists of a tank $A$, with three insulating pots $B$. In each pot, mounted on an insulating bushing $I$, is located a stationary electrode $E_{1}$; each of these electrodes is connected to one of the slip rings of the motor. Three movable electrodes $E_{2}$, one in each pot, tied together by a cross-bar $C_{0}$ are suspended to the lever arms $D$. These arms are mounted on the shaft of the so-called "torque motor" $T M$, which is an induction motor with its primary winding connected in series with the main motor lines. The tank is filled with a weak solution of sodium-bicarbonate; the columns of the liquid between the electrodes $E_{1}$ and $E_{2}$ act as the secondary resistance in each phase, with the cross-bar? serving as the Y-point. Cooling coils are immersed in the tank and water is circulated through them in order to remove the heat produced by the secondary current. The suspended electrodes $E_{2}$ are partly balanced by the counterweight $W$, but the latter in itself is not sufficient to raise the electrodes, which normally occupy the lowest position corresponding to the minimum resistance in the rotor circuit.

When however, the load increases and execeds a predetermined value, the torque of the motor $T M$, added to the torque produced by the counterweight $W$, raises the electrorles $E_{2}$, thus inserting more resistance in the secondary. By making the counterweight IV heavier, the current value at which the regulator begins its action is reduced, and vice versa. The slip regulator tends to so adjust the secondary resistance as to limit the input to the motor, throwing the balance of the load on the flywhecl. During the interval between the passes the slip regulator reduces the secondary resistance and brings the mill gradually to speed.

The same apparatus is intended for "starting duty" of the motor: the naximum resistance, as determined by the maximum distance between $E_{1}$ and $E_{2}$ should be high enough to limit the starting current to a sufficiently low value. This determines the strength of the electrolyte in the tank; it is not feasible, however, to weaken the solution


Fig. 16. Liquid Slip Regulator
too much in order to obtain a higher maximum resistance, as by doing so the minimum resistance (when the blades are close together) is also increased, which is of course objectionable. This feature limits the maximum resistance of the regulator.

When the flywhed drive should be quickly stopped, the driving induction motor is "plugged," i.e., the phase rotation is reversed and a counter-torpue is thus produced. In such cases in order to limit the current to the same value as at starting, the secondary resistance should be made twice as great: inasmuch as the existing liquid slip regulators cannot give this increased amount of resistance, it is necessary to add an external irongrid resistor (so-called plugging resistor) normally short circuited by a contactor, but inserted in the circuit when phagring. A liquid slip regulator is shown in Fig. 16.

Slip regulators are universally used in conjunction with flyweel motor-generator sets, such as are employed in large mine hoists and in reversing steel mills. The load equalization obtained in such cases through the use of a slip regulator is very efficient as witnessed by the many actual tests as shown in Fig. 17. The question then naturally arises: why not apply this effective device to the induction motor mill drives equipped with flywheels. instead of using the resistorcontactor control.

This topic was quite a live one of late, various steel mill engincers and electrical manufacturers discussing the comparative merits of the two devices. Unfortunately some of these discussions were conducted on, what may be called, purely partisan lines,

Slip Regulators vs. Magnctic Control
Assuming that the slip regnlator is mathe sensitive enough it should reduce the loand peaks somewhat more spertacularly than the notching-lack control previously described. The curve 1 in Fig. is is the same loarl


Fig. 18. Comparison Between Performance of a Notching-back Control and that of an Ideal Liquid Slip Regulator
curve which has been plotted in Fig. 13; the curve 2 shows what could be the result of the application of a slip regulator to the same part of the duty cycle.


Fig. 17. Load Equalization Obtained on a Large Mine Hoist Equipped with a Flywhee! Motor-generator Set and a Liquid Slip Regulator as shown in Fig. 16
and as such did not clear the issue. But this problem, as is the case with many others. can and would be answered correctly if prejudices and beforehand-made-conclusions are set aside and the subject looked into from an engineering standpoint.

It is to be noted, in the first place, that when the electrodes of the slip regulator are as close together as possible there still remains a quite substantial minimum resistance in the rotor circuit. Manifestly the upper and lower electrodes cannot be brought into
dired eontace with ead othor as this would eatise them to "freeze." 'The neeressity of using spacors brings the minimum resistanore to a value which is rery sedfom less that (i) or of per eent : in other words, Ane motor has a if or 7 per eent permanent resistance which cammon be made smaller as rearlily as when seric! resistors are used. 'The reduction of the minimum resistance by strengthening the cectoolyte is not feasible, as was pointed ont previonsly
'Thus, when the loarl is mposed on the mill. the line input will build up gradually, see curve ? ( $\mathrm{Fj} \mathrm{g}_{\mathrm{g}}$ ls) as it would with any motor

The reduction of peaks is olviously in faver of the slip regralator provided it funcfons as was assumber. What is the possible result of reduction of peaks, in this case from l.io) per ernt to le. per ernt: It will not affect the motor rating or the maximum worfue requirements. It may be of some importance for a small power plant, supplying current to one or two mills, which comprise the londk of the loat. Such a case is conceriable although it is cncountered rather as an exception than as a rule. If other lhings like first cost and maintenance are (equal, and the slip) regulator is marle sensitive


Fig. 19. General View of a Large Reversing Blooming Mill; the Mill Motor is shown in the Foreground and the Flywheel Motor-generator Set Behind it; the Liquid Slip Regulator is Located to the Right of the Flywheel Set
having, say, 6 per cent resistance. When the load reaches the setting of the regulator, see point $A$, the latter will start to move the blades apart. We shall assume that this regulator is very quick-acting and that it will, from this instant on, maintain a constant input, equal to say 125 per cent of the motor rating or any other value depending on amount of counterweight W . During the time between the passes the regulator will bring the electrodes together tending to maintain constant input. At point $B$ the blades are close together and after this point the load will drop off as with any motor having 6 per cent permanent resistance.
enough for steel mill duty, then it would be preferred. Unfortunately a small installation is never a good place to install a slip regulator, as will be explained in the following paragraphs.

But first of all we should analyze whether the slip regulator will meet our expectations.

We have assumed that the slip regulator is so sensitive that its movements follow very closely the rapid fluctuation of the load. There is an inherent limit to this sensitiveness. Essentially, the electrode mechanism of the regulator consists of parts that should be sufficiently rigid to work properly; in other words its weight is far from negligible. This
heary mechanism should be moved quickly first in one, then in the other direction, in order to follow the fluctuations of load. The motive power is the torque motor TM. Fig. 15), or to be exact, the excess value of its torque when the current exceeds the predetermined amount. This excess torque should move the electrole mechanism, and it is clear to anyone that with a limited motive force and with a definite weight to be accelerated, the clectrodes cannot be moved faster than the fundamental laws of mechanics permit. This limits the minimum time in which the electrodes can cover a certain travel, even if they were moving in the air. But as a matter of fact. the electrodes must travel through the liquid and the resistance which the latter offers to this travel is proportional to the second, if not to a higher,


Fig. 20. Elementary Duty Cycle of a Reversing Mill; the Horse Power Curve shows that the load builds up gradually, which fact assists the slip regulator to equalize the load
power of the relocity: This resistance may. be very appreciably reduced by proper design of the moving parts and this is done of course as far as feasible: but the point is that a certain amount of "dashpot action " should be left in the regulator as otherwise a worse trouble will derelop, namely, the hunting or "overshooting" of the mechanism. In other words. the resistance of the liquid will be and should always be present in any slip regulator, regardless of the make or details of design. This feature inherently prevents this apparatus from following rapid and violent fluctuations of load. as take place in steel mills, while its application is entirely satisfactory when the load varies more smoo hly:

For instance. in mine hoist practice the fastest hoist does not make more than three trips in one minute: this means that the slip regulator has 20 seconds in which to move
the electrockes apart and then to bomg then together. For such serviee the ship, regulators are mexcellerl, as winessed by the praphine record, Fig. 17 l3ut in stecl mills the loarl may come on and ges off not once. Int a dozen times during a periond of 20 secromls and it is impossible to expect the same respencireness from the slip regulator. The perfectly straight line $A B$ (Fig. I $)$ is never enconntered or approached in steel mill practice.

In several articles and papers writem on this subject graphic records were reprotuced showing how much better the performance of the liquid slip regulators is in steed mill practice than the notching-lack control, in the sense of relucing the maximum frower demand. Unfortunately, the authors of these papers do not alware state what was the minimum resistance of the slip regulators used during the teste. It is obrious that by making this resictance high (weaken the solution of the electrolyte) the peaks are reduced even though the slip regrilator mav not operate as such; this merely corresponds to a large permanent resistance which. as we know, is rery effective not on'y in reducing the peaks but also in reducing the averase rolling speed and in boosting the secondary losses. It is recommended that when examining such graphic records that we should also examine the corresponding charts recording the mill speed.

The reversing mills comprise a class in themselves. These mills, driven by directcurrent motors are furnished with power from a special motor-generator set; the set is driven by a slip-ring induction motor. and is equipped with a heary flywheel mounted on its shaft. The line input is equalized by adjusting the secondary resistance of the induction motor which enables the flywheel to play its part. A good general view of such a reversing drive is given in Fig. 19. There is. however, a very definite difference between the power requirements of a reversins mill and those of a non-reversing one. When a piece of metal of a uniform cross-section passes through the rolls, the torque required by the mill to deform the metal is the same at the beginning as at the end of the pass (neglecting the effect of the cooling during one pass). The non-reversing mills are running at constant speed and therefore not only the torque but also the total horse power requirements of the mill rises instantly to the full value at the instant the steel enters the rolls. This explains why such mill duty cycles are represented by rectangular diagrams. In
the reversing mills the entering spece is always less than the rolling speed; thus while the rolling torgue requirements rematin the same, the horse power demand for rolling rises gradually with the increase of mill speed white metal is in the rolls. Fig. UO shows how the horse power load builds up gradually during the first part of the pass. This character of the loatd reflects directly and favorably on the slip regulator, as the latter has a better chance to adjust itself to the change of the load.

There is another factor assisting the slip) regulators in such cases:

The first cost of reversing mill equipments is considerably higher than for induction motor drives; the cost of the flywhed with bearings
it may be in other steel mill cases. The practice fully sustains this conclusion.

We have already pointed ont that any of the existing slip regulators have a certain ratio of maximum to minimum resistance which cannot be exceeded; this means that in order to limit the plugging peaks an outside grid resistor should be furnished. If it is not supplied it simply means that the plugging features are not taken care of. To plug the motor with only a slip regulator in the circuit means not only a (louble peak on the line, but also double voltage on the slip regulator itself.

Comparing the two methods of slip regulation (liquid regulator and magnetic control), other points are to be considered in addition


Fig. 21. Typical Location of Flywheel for Geared Mill Drives. The other flywheel identical to the one shown in the picture is mounted on the opposite side of the pinion shaft
is a much smaller part of the whole cost in the former case, and it is more commercially feasible to build a flywheel of a larger capacity for mounting on the motor-generator set than for mounting on the drive itself. For instance, a $2500-\mathrm{h} . \mathrm{p}$. reversing drive has a flywheel with $130,000 \mathrm{~h} . \mathrm{p}$. sec. total stored encrgy, whereas one of the largest sheared plate mills, driven by a $5000-\mathrm{h} . \mathrm{p}$. motor has a wheel of only $63,500 \mathrm{~h} . \mathrm{p} . \mathrm{sec}$. The larger the capacity of the flywheel the more is the load equalization obtained on the permanent (minimum) part of the slip regulator resistance, and the easier becomes the duty of the electrode mechanism.

Summing up, the load equalization as encountered in the reversing mills may be more readily solved by the slip regulator than
to the operating characteristics of either apparatus.

The slip regulator is a very simple device in principle; the fact that it eliminates the contactor panel, with the necessary relays and wiring, at times appeals to operators, who think that an inexperienced man will handle it much more easily than the magnetic control. As a matter of fact the contrary is nearer the truth.

There are too many incidental things that may render the slip regulator inoperative unless it is under good care. After regular intervals of time it should be overhauled to clean the dirt accumulating in the tank, etc.; the mill electrician that does this work cannot be expected to reassemble the regulator as thoroughly as it is done at the factory, not
having the same facilities. The three electrodes are frequently not re-set in proper aligmment and then they may begin to rub against the tubes $B$; the resultant friction makes the regulator absolutely inoperative: if, on heary overloads, the torque motor overcomes the friction and pulls the electrodes apart, they will oftentimes stay in the raised position even after the load goes off. At the next peak load the motor, having such large secondary resistance, will slow down excessively; the operator then chooses the "easy ray." and reduces the counterweights, to make sure that the electrodes shall not move; the purpose of the regulator is annulled, it is used merely as a starting box and as a block of permanent resistance. Many a slip regulator of various makes may be seen around the steel mills in such inoperative condition.

By installing a slip regulator too much reliance is put on the ability of the operator to keep it in good shape. In large and expensive installations, like reversing mills, a good experienced electrician is usually available and it is reasonable to expect that the slip regulator will receive the necessary care. But less elaborate equipments should be made fool-proof; a well made magnetic control, once installed, will work for years without much attention, except renewal of the contactor tips. If any fault develops in the control, it may readily be located and corrected, because all parts are accessible; repairs, if any, may be made in a fraction of the time required for overhauling of the slip regulator.

Of the slip regulators and magnetic-control either cne may be made as good and as efficient in its own class as the present engineering art permits. The problem is not which of the two devices is better, but which is more suited for the particular application.

## Direct-current Drives

In exceptional cases, when direct current motors are used for driving non-reversing mills equipped with flywheels, the required speed regulation is accomplished very simply and economically.

The motor is furnished with a compound wound field so proportioned that the speed will drop with the load to the amount neces-
sary for making use of the stored energy of the flywhed. No control devices are needed to take care of this performance.

There are no electrical losses incidental to the flywheel operation, like the secondary losses in the case of induction motor drives.

Assuming that the drop in speed is directly proportional to the load the calculations may be made in the same general manner as was done for the induction motors.

## Mechanical Arrangement

When a mill is driven by a direct-connected electric motor, the flywheel is naturally mounted on the same shaft. In case of a geared or belted drive the question may rise as to what is the best location for the flywheel: on the low speed mill shaft or on the high speed motor shaft.

It is quite evident that with the first arrangement the high load peaks will be absorbed by the flywheel and they will not be therefore transmitted through the gears. This makes the gear service easier and sometimes a smaller and less expensive gear unit may be used.

However. the same flywheel will have four times greater capacity if its speed (in r.p.m.) is doubled; for the same capacity the wheel designed for high speed shaft mounting will have smaller weight.

Low speed wheels are usually made of cast iron or of cast steel. It is impossible to be certain that such a large casting is of uniform structure; it is not safe to exceed the rim speed of, say, $S 000$ to $10,000 \mathrm{ft}$. per minute.

High speed wheels are either made of cast steel or of boiler plates riveted together. In the latter case the uniformity of material is assured; rim speeds may safely go as high as $21,000 \mathrm{ft}$. per min. or even higher. Fewer pounds per h.p.-sec. stored energy is thus necessary.

This makes the flywheel designed for mounting on the high speed shaft less expensive than the low speed wheel, even though the gear unit should be made stronger and higher in cost. It is very customary to have the high speed flywheel divided in two units. each of half capacity and mount them overhung on the high speed pinion shaft, as shown in Fig. 21. With this arrangement the total cost of the bearings is reduced.

# The Electron in Chemistry <br> PART IIB 

By Sir Joseph John Thomson<br>

The first of this serics of lectures was published in our Jugust issuc. Last month we published the first part of the second lecture which we conchade in our present mumber. This, Part HB, deats with the Disposition of the Electrons in Typieal Componnds; Comnection Between Chemical Constitution and Chemical Propertics; Residual Affinty; Moleerlar Compounds; Werners Co-ordination Numbers and Electrolytic Dissociation. Emror.

Disposition of the Electrons in Typical Compounds
Chlorides.-Monochlorides, type HCl . We have here a positive eharge outsicle the octet. The compound has a finite electrostatic moment. The region round the hydrogen atom is comparatively free from electrons, thus molecules of water could be held in stable equilibrium round the hydrogen ion, so that substances with this composition should be hygroseopic.

Bichlorides, type CaCle. A double positive charge between two octets; the molecule is non-polar. If each of the octets presents a face to the calcium atom, there will be eight electrons on a sphere round this atom; with this configuration there is no room for other molecules. If the chlorine octets swing round so as to present an edge instead of a face to the calcium atom, there will only be four electrons on the laver next to this atom. Thus there would be room for two water molecules if the water octets came edge formost, or for four if they came point foremost. While if the chlorine octets were also point foremost to the calcium atom, there would be room for six molecules of water. We should expect these chlorides to be very hygroscopic.

An interesting fact about the halides is that we find chlorides such as tungsten hexachloride, $\mathrm{WCl}_{6}$, and molybdenum pentachloride, $\mathrm{MoCl}_{5}$, sulphur hexafluoride, $\mathrm{SF}_{6}$, in which there are more than four atoms of chlorine or fluorine combined with one atom of another element. Now if each octet is to present an edge to the central atom, it will furnish two electrons to the layer round the central atom and as the number of electrons in this layer cannot exceed eight, it follows that there cannot be more than four atoms of one kind combined with one of another, a rule to which there are a few exceptions, such as these we are considering. We may explain the existence of these in two ways-one is to suppose that only four of the chlorine atoms are in the inner zone, that the other two are in the outer zone. In this case two chlorine octets carrying a negative charge would be easily detached,
so that the compound should be a good electrolyte. The other supposition is that all the chlorine octets are in the inner zone, but only two of them present an edge to the central atom, the other four only presenting a corner. The difference between the two is roughly that, on the first supposition, two chlorine octets are loosely and four firmly held, while on the second two are firmly and four loosely held.

Oxides.--The points previously raised in connection with water apply to the oxides of the univalent elements generally.

Oxides of divalent elements of the type CaO . Here we have the core of the calcium atom outside the oxygen octet. If this octet presents an edge towards the calcium atom, there will be room for three more octets, each presenting an edge, so that we can easily understand why this substance dissolves easily in water. It is not necessary that the octets which go to complete the tale round the calcium atom should be those of water molecules, they may be the octets of other CaO molecules. The fact that the octet of one molecule of CaO can also find its way into the inner zone surrounding other Ca atoms will have a great effect in binding the different molecules together and thereby account for the very high melting points of the oxides. The arrangement in two dimensions when molecules of CaO mutually saturate each other is shown in Fig. 25. The arrow between Ca and O indicates that two electrons have gone from this particular calcium atom to complete the octet round the oxygen atom. The octets are supposed to present their edges to the calcium atom.

Sesquioxides, type $\mathrm{B}_{2} \mathrm{O}_{3}$. The most symmetrical arrangement for oxides of this type would seem to be one where the three oxygen octets have their centers at the corners of an equivalent triangle, while the cores of the two boron atoms are symmetrically placed on an axis at right angles to this triangle and passing through its center.

Carbonates. $-\mathrm{M}_{2} \mathrm{CO}_{3}$. We have here three oxygen octets surrounding a central carbon
atom. If the inner zone round this atom is to be saturated with electrons, one of the octets must tum a face, while the other two octets present edges towards the carbon atom. If the octet turning its face to the carbon twists round and turns an edge, there will be room for another octet in the inner zone: thus the molecule can lake up water or bind itself to other molecules of the carbonate. There would seem to be the possibility of two isomers. in one both the metal atoms are attached to the octets which present edges to the carbon: in the other, one metal atom is attached to the octet presenting a face and the other to one of those presentingr an edge.
.Vitrates- $\mathrm{MNO}_{3}$. The arrangement is the same as for the carbonates, except that the central atom is mitrogen. with a positive charge of five and not carbon with a charge of four, and there is only one metal atom instead


Fig. 25
of two to put outside the octets. There is the possibility of two isomers as hefore.
 oxvgen octets surrounding a central sulphur atom. These must hare edges and not faces turned towards this atom. As all the four octets are turned the same way and are similar there will be no isomers.

Perchlorates. $-\mathrm{MClO}_{4}$. The same as the preceding. except that the central atom is chlorine and not sulphur, and there is only one metal atom to place outside the octets.

Sulphites.- $\mathrm{I}_{2} \mathrm{SO}_{3}$. These from our point of riew differ from the carbonates and nitrates because after providing for the electrons to furnish the three oxygen octets, there are still two electrons to provide for. The most symmetrical way would be to arrange them as in Fig. 26, i. 6. with one of the $I I$ atoms connected directly up with the sulphur and not indirectly through an oxygen octet. This would put the metal atom in the inner zone,
from which we should not expect it to be detached in electrolysis: thus if $\ /$ were hydrogen, this arrangement wonld correspond to a monobasic acjel. $\mathbb{I}_{2} \mathrm{SO}_{3}$ is, howeter, dibasic and therefore has probably both the II atoms commected lirectly with the oxigen


Fig. 26
and not with the sulphur. In this case we see that there are two electrons which have no direct connection with any but the sulphur atom. and which would be available for attaching to the $\mathrm{M}_{2} \mathrm{SO}_{3}$ molecule the positire part of any polar molecule or to complete the octet of an oxygen atom and thus form the sulphate.

Chlorates. $-\mathrm{MClO}_{3}$. Here we have the same number of electrons as in the sulphites, but the fact that the chlorates very readily give up oxygen while the sulphites take it up suggests a different grouping of the electrons. The arrangement given in Fig. $\mathbf{2}^{-7}$. where one of the oxygen atoms is bound to another oxvgen atom and not directly to the chlorine. would represent a molecule which would readily part with oxygen.

This arrangement of two oxygen octets with an edge in common is one that occurs in connection with the molecules of exception-

ally intense oxidizing agents. and we have already met with it when considering the form of the molecule of ozone. In hydrogen peroxide $\mathrm{H}_{2} \mathrm{O}_{2}$ there are two possible forms. one represented by Fig. 2S: (a) In which both hydrogen atoms are attached to the same
axyen octet, and the other (h) when one hedrogen atom is attacherl to ons oxyen octed and the other to the other. In both cases we have two oxygen octets eomeded together by an edre. The first one woukd peossess at finite electrical moment, the second one would not, so that the forms conld be distinguisherd by measuring the specific capacity of $\mathrm{H}_{2}()_{2}$ in the gasconsstate.

Nitrites. $-\mathrm{HNO}_{2}$. The nitrites resemble the sulphites in having two cleetrons which are not in direct connection with any but the central atom. There are two oxygen octets and two electrons $E$, as in Fig. 29. If the hydrogen ion took up the position (HI), it would be bound by these electrons, the hydrogen would be in the first zone and the substance would not be an acid. If the hydrogen is attached to one of the oxygen octets, the substance will be an acid, and the two electrons will be free to complete the octet round a neutral atom of oxygen, link it
get formicateid, a sulstance with pronounced acid properties. We know the general character of the distribution of electrons in the two coases, can we see why the difference in the distribution shoukd make the difference between an acid and a feeble hase? We shall suppose that the acid character of a substance containing the hydroxyl radicle OH depends on the case with which the hydrogen ion H can be detached from the oxygen. We have therefore to see what is the difference between the foree on the hydrogen ion in $\mathrm{CH}_{3} \mathrm{OH}$ and CHIO.OHI. The arrangement of the electrons in methyl alcohol is represented in a general way by the continuous lines in Fig. 30, where for the sake of avoiding confusion in the drawing, the tetrahedral arrangement of the $\mathrm{H}_{3}$, OH atoms round the central carbon atom has been replaced by an arrangement in one plane. We have the octet round the carbon atom; the size of this does not vary much from one compound to another. We may thus regard

(a)

(b)

Fig. 28
up with the nitrogen, and convert the nitrite into a nitrate.

## Connection Between Chemical Constitution and Chemical Properties

If we know the distribution of the electrons and positive charges in a molecule, the behavior of the molecule under specified physical conditions can be calculated from the forces exerted on each other by the electric charges. The exact calculation in most cases would be a process of considerable length, but we can get without an appreciable amount of mathematics a general idea of the nature of the change in properties likely to be produced by changes in the composition of the molecule. The clearest way of illustrating the point in question is to take an example. Methyl alcohol $\mathrm{CH}_{3} \mathrm{OH}$ is a substance without any tinge of acid properties; in fact, it is basic, if anything. When, however, two of the hydrogen atoms are replaced by an oxygen one we
this octet as occupying much the same position in the formic acid as in the methyl alcohol. Consider the difference when we replace two of the hydrogens $\mathrm{H}_{2}, \mathrm{H}_{3}$ by an atom of oxygen. We take away the positive charges $\mathrm{H}_{2} \mathrm{H}_{3}$, and replace them by a positive charge 6 at the center $S$ of the oxygen octet, and four negative electrons at the corners $E, F$ of the face of this octet. Thus the difference between the forces on the atom $\mathrm{H}_{1}$ in the hydroxyl radicle in the methyl alcohol and formic acid is the difference between the force exerted by the positive charge 6 at $S$, by the four electrons on the face $E F$ of the octet, and that exerted by the two positive charges $\mathrm{H}_{2} \mathrm{H}_{2}$, which can be represented approximately by a positive charge 2 at $S$. Subtracting this from the charge 6 due to the oxygen, we see that the change due to substituting the oxygen for the two hydrogens can, as far as the forces are concerned, be represented by a plus charge 4 at $S$ and a charge on the whole
amounting to -4 carried by four electrons at the corners of the square face of the octet. If we replace these by a charge -1 at $G$, the center of the square face, then the force on $\mathrm{H}_{1}$, in the formic acid molecule will equal the force on $H_{1}$ in the molecule of methyl akohol plus the force due to the doublet with a positive charge 4 at $S$ and a negative one -4 at $G$. The effect of the doublet is, as will be seen from the figure, to repel $\mathrm{H}_{1}$ away from O . It will thus tend to detach $\mathrm{H}_{1}$ from the molecule, i.c., to make the molecule act like an acid.

As a further example let us consider whether replacing a hydrogen atom in such a compound as formic acid by a chlorine one would increase or diminish the acid properties of the molecule.

Suppose that Fig. 31 represents the distribution of the electrons in a molecule of formic acid. If the hydrogen $\mathrm{H}_{4}$ were replaced by chlorine, the change as far as the electrical forces are concerned will be that the charge


Fig. 29
+1 at $H_{4}$ will be replaced by a charge +7 carried by the chlorine atom, and that six other electrons will be introduced which, with the two along the edge $E$, will make up the octet round the chlorine atom. To calculate the effect of these six electrons, we take the four along the edges $F$ and $G$; these are at the corners of a rectangle whose center is at $S$, the center of the chlorine atom. If these electrons act as if they were concentrated at the center of figure $S$, they will have the effect of reducing the positive charge at the center of the chlorine atom from 7 to 3 . Now take the two electrons at the edge $L$; these with two of the three charges at the center of the chlorine atom will form an electrical doublet whose moment is $2 e \times L S$ with its positive part turned towards the center of the molecule, the remaining positive charge at $S$ will represent the positive charge on the hydrogen atom before it was replaced by chlorine. Thus the
difference in the forces due the the repacement of hydrogen by chlorine is represented by the electrical double 2e $L$ S. and this as we see from the figure will tend to drive off the hydrogen in the hydroxyl radicle- thus the substitution of chlorine for hydrogen tends (1)


Fig. 30
increase the acidity of the molecule. This is very strikingly shown by monochlor, dichlor and trichlor acetic acids, which are much stronger acids than acetic acid itself.

It follows from the investigation we have just given that if in a hydrocarbon such as $\mathrm{CH}_{4}$ we substitute for one of the hydrogen atoms $E$, the atom of an electronegative element such as chlorine, the change in the electric forces can be represented by the introduction of an electrostatic doublet at $E$


Fig. 31
with its axis along CE and the positive part of the doublet turned towards C. The molecule of $\mathrm{CH}_{4}$ before the substitution of the chlorine atom was non-polar, i.e., the molecule had no electrostatic moment, the substitution of the chlorine for the hydrogen introduces a
timite cheretrastatie moment and thas makes the molecule polar．

The positive part of the domblet at $E$ is tumed towards（ ，bence the foree it pro－ dutees at $F^{\circ},(B, I f$ ，the other eorners of the tetrahedron whose center is at the carbon atom，will tend to attract megatively and repel positively ehatred atoms Hence if a molerote of © ${ }^{\circ} \mathrm{H}_{3}$（｀l were placed moter sued conditions that there were positively and negatively charged atoms in its neighborhood， the eoncentration of the nestative atoms round $F,(i, I l$ would be greater than it would be for the molecule C $\mathrm{H}_{4}$ before the hydrogen at $E$ had been replaced by the electronegative chlorine．Thus the sulstitution of the atom of an electronexative element for one of the hydrocen atoms round the carbon will tend to promote the substitution of clect ronegative atoms for the remaining hydrogen atoms．If two of the hydrogen atoms are replaced by an atom of oxygen，this will for the same reason promote the substitution of electronegative atoms for the other two hydrogen atoms．We have illustrations of this effect in the follow－ ing examples for which I am indebted to Mr． W．IH．Mills．

Ethyl chloride＋chlorine（ 1 molecule）in the liquid state under the influence of ultra－violet light，

$$
\mathrm{CH}_{3} \cdot \mathrm{CH}_{2} \mathrm{Cl} \rightarrow \underset{i 0 \text { per cent }}{\mathrm{CH}_{3} \cdot \mathrm{CHCl}_{2}}+\underset{10 \text { per cent }}{\mathrm{CH}_{2} \mathrm{Cl}_{2} \mathrm{CH}_{2} \mathrm{Cl}}
$$

Ethrl bromide heated with bromine in sealed tube，

$$
\mathrm{CH}_{3} . \mathrm{CH}_{2} \mathrm{Br} \rightarrow \mathrm{CH}_{3} . \mathrm{CHBr}_{2}
$$

Chlorine on boiling toluene $\left(\mathrm{C}_{4} \mathrm{H}_{5} . \mathrm{CH}_{3}\right)$ in sunlight gives successively

$$
\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{2} \mathrm{Cl}, \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHCl}_{2}, \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CCl}_{2}
$$

We see from these examples that there is a tendency for a new hydrogen atom to go into that part of the molecule which is already halogenated．

In the presence of catalysts such as ferric bromide，the halogen atoms in the higher members of the series go to the carbon atom adjacent to the one already brominated．

Another illustration of this effect is the well－ known fact that when an organic compound is oxidized the carbon atom attacked is the one which already is attached to oxygen．

I pass on now to consider a problem which I can best explain by stating a particular case． Why is it that in a compound such as methyl alcohol $\mathrm{H}_{3} \mathrm{C} . \mathrm{OH}$ the only atom of hydrogen which is replaceable by a monovalent metal is the one in the hydroxyl radicle？Or to take another aspect of the same problem，why
cath the hydrogens in marsh gats not be replaced by the monovalent positive elements， while they can be replaced by the monovalent negative one like（｀l，Br，I？Let us consider what are the conditions for the existence of Cl1s．We have an oetet of electrons round the carbon atoms．The carbon atom which only carries a charge of four units could not by itself keep eight electrons in stable equilib－ rimm．It is enabled to（lo this by the stabiliz－ ing effect of the positive charges which are on the hydrogen atoms．This stabilizing effect will depend on the distance of the positive eharge．on the hydrogen from the nearest electron in the octet，a distance which we should expect to be not greatly different from the radius of the hydrogen atom．Consider now the effect of replacing the hydrogen atom by one of an alkali metal；the radius of the atom of the alkali metal is very considerably greater than that of the hydrogen atom．The control over the electron in the metal is much less than that on the electron in the hydrogen atom．This is shown by the fact that the ionizing potential for the hydrogen atom is much greater than that for the metal one，thus we should expect the stabilizing effect of the positive part of the metal atom to be very considerably less than that of the hydrogen atom．Thus while the stabilizing effect of the hydrogen atom may be great enough to make the octet of electrons round the carbon atom stable，that of the metal atom may not be able to do so，in which case the metallic com－ pound could not exist．

In this view the atoms of the monovalent metals are not efficient stabilizers of an octet of electrons，and we should expect that in the compounds they form，the octet should be of a kind that requires little help from the positive charge on the metal atom to make it stable．

Let us consider a few types of the salts formed by these monovalent metals．Let us begin with the chlorides，here we have an octet of electrons round the chlorine atom and the positive charge outside．Now experi－ ments with positive rays show that a neutral chlorine atom，having seven electrons in the outer layer readily takes up a negative charge，i．e．，acquires another electron．Thus an octet of electrons round a chlorine atom is stable even without the assistance of an external positive charge，and thus a metal atom outside an octet round a chlorine atom will be a system where the octet is very stable． Hence we should expect that all these alkali metals would，as in fact they do，form chlorides readily．Now let us turn to the hydroxides．

The neutral hydroxyl radicle has seven electrons arranged round the oxygen atom. Now again experiments with positive rays show that the hydroyxl radicle very often occurs with a negative charge and in this state there must be an octet of electrons round the oxygen atom. Thus such an octet with the hydrogen atom outside is stable by itself even without assistance from the positive part of a metallic atom. Thus when it gets this assistance the octet will be very stable, so that we should expect, as in fact is the case, that the hydroxides of the alkali metals would be formed very readily.

Now let us turn to the oxides, here we have an octet round the oxygen atom and the positive part of two metallic atoms outside. As lines corresponding to negatively electrified oxygen atoms are to be seen on nearly every positice-ray photograph, a system of seven clectrons round the oxygen atom must be a stable system. In the case of the metallic oxides we have two positive charges to make the system stable when another electron is added. We have scen from the case of hydroxyl that a single hydrogen atom is able to bring about this stability, so that as two metal atoms are available the metal atoms would have to be very inferior to the hydrogen one as stabilizers if the octet were not fairly stable.

Now let us consider why it is that, while we cannot replace by a metal one of the hydrogen atoms directly connected with the carbon atom in a hydrocarbon, we can replace the hydrogen in a hydroxyl group linked up to the carbon. Let us take methyl alcohol as an example, where we may suppose the electrons are arranged as in the diagram. We see that from its position the hydrogen in the hydroxyl group has little to do with the stability of the octet round the carbon atom; it is the stability of that round the oxygen atom with which it is concerned. Now an octet round an oxygen atom is a very different thing as far as stability is concerned from one round a carbon atom. We have seen that seven electrons can be in stable equilibrium round an oxygen atom without any help from systems outside and that a single positively charged hydrogen atom outside is sufficient to make the octet stable. If the hydrogen in the hydroxyl is replaced by a metallic atom, then to keep the octet round the oxygen atom stable we have not only the positive part of the atom of the metal, but also that of the carbon atom with its attached e'ectrons and positive hydrogen atoms. Thus the conditions are much more
favorable for the stability of this oetet than they are for that round the carbon atom, and thus it may be possible to replace the hydrogen in the hydroxyl lint not that in the rest of the atom. The positive rays afford evidence that to make the octet of electrons round the carbon stable in a compound $\mathrm{Cll}_{3} \mathrm{X}$, where X is a monovalent element, assistance is required from X . For if it were not, the system got by remoring the positive part of X would be stable, but this system is just the radicle $\mathrm{CH}_{3}$ with a negative charge. Now the line corresponding to this radicle occurs frequently in positive rays, but always with a positive charge; while other radicles, such as OH , are found with negative as well as with positive charges. This is an indication that the stability of the octet round the carbon atom depends upon the presence of X . On the other hand, if the residue after taking away an atom of hydrogen from a hydrocarbon is stable even after receiving a negative charge we should expect that the hydrogen atom might be replaced by an atom of the metal, for the molecule is stable after the hydrogen has been removed and the octet does not depend on the positive charge for its stability: Now on many positive-ray photographs I have observed a line corresponding to a molecule with a negative charge, whose molecular weight is 25 , when hydrocarbons were in the discharge tube. The molecular weight indicates that the molecule is $\mathrm{C}_{2} \mathrm{H}$, i.e., acetylene minus an atom of hydrogen, if this is so the hydrogen in acetylene might be replaced by a metal: The compound $\mathrm{C}_{2} \mathrm{Cu}_{2}$ which is of this type is well known.

Though we have seen the stability of the oxides indicates that the octet round the oxygen atom can be stabilized by the presence outside it of the positive parts of metallic atoms, there are indications that this octet is not so stable as those in the chlorides and hydroxides. The main evidence is that many oxides and sulphides when in the solid state are conductors of electricity, especially at high temperatures, and that, as the researches of Königsberger and Horton show, this conductivity is not electrolstic, but resembles that through metals. There are some chlorides which conduct in the solid state, but as far as I am aware their conductivity is always electrolytic. The conductivity of metals can, as we shall see, be explained as due to electrons which move freely about in certain directions through the solid. So that the non-electrolytic conductivity of these oxides and sulphides indicates that some
dectrons have pot free i.e., that some of the oclets round the oxygen and subphur atoms have broken up. 'This breaking up increases very rapidly with the temperature. Another piece of evidence to the same effect is the very intense thermionic emission by oxides such as those of calcium, strontium and barimm, an emission which, as llorton has shown, is far more intense than that from the metals themselves at the same temperature. On our viow this is clue to the breaking up of the octets round the oxygen atoms. The smaller the charge on the neutral atom, the more will the stability of the octet round it depend on the positive charges outside. Thus as nitrogen has only a charge of 5 while oxygen has one of 6 , we should expect the octet round nitrogen in a metallic compound to be more easily broken up than that round oxygen in metallic oxides. It would be interesting to test from this point of view the properties of iripotassiumamide, $\mathrm{NK}_{3}$.

## Residual Affinity, Molecular Compounds, Werners Co-ordination Numbers

We have regarded the molccule of a chemical compound as made up of atoms some of which have lost electrons, while others have gained them, so that the former are positively, the latter negatively, electrified; the forces between the electrical charges on the atoms and electrons binding the atoms together in such a way as to form a stable system. The number of electrons which an atom can gain or lose depends upon the nature of the atom. The number it can lose is equal to the number of electrons in the outer layer, and varies from one to eight according as the element belongs to one or other of the Mendeleefian groups; the number it can receive is 8 minus the number in the outer layer.

If the transference of electrons has proceeded to its limit, i.e., if every positively charged atom has received the maximum positive charge of electricity it can acquire and every negatively charged one its maximum charge of negative electricity, there must be simple relations between the number of different kinds of atoms in a neutral molecule. Thus, for example, if we have two kinds of atoms, e.g., calcium and chlorine, since the neutral calcium atom has two electrons in its outer layer and the neutral chloride seven, the calcium atom can lose two electrons while the chlorine atom can only gain one. We see therefore that when the transference of electrons has gone as far as possible, each
calcium atom will have given up its electrons to two chlorine atoms neither more nor less and thus for each calcium atom positively charged there must be two chlorine ones with negative charges, thus the composition of the molecule would be represented by the symbol $\mathrm{CaCl}_{2}$. And we can show easily that when the transference of electrons has proceeded to the limit the proportion between the numbers of the various kinds of atoms in the molecule will be the same as that deduced from the ordinary principles of valency.
In such a molccule as $\mathrm{CaCl}_{2}$ the transference of electrons has reached its limit, and as far as this property is concerned the molecule may be regarded as "saturated." Unfortunately there has been a tendency to regard this "saturation" as applying to quite a different thing. Some chemists have supposed not merely that the calcium atom when it had charged two chlorine atoms had exhausted its power of charging up any more atoms negatively, which is true, but they implied, which is not true, that the doubly charged calcium atom camot by its attraction hold more than two atoms in stable equilibrium. It is important to distinguish between the maximum positive charge the atom can acquire and the maximum number of negatively electrified systems which the maximum charge can hold in stable equilibrium in a single layer around it. The table given in the first chapter shows that when the attractive force between the positive charge and a negative one is represented by $\frac{a}{r^{2}}=\frac{b}{r^{n}}$, the number of negative charges which a positive charge can hold in stable equilibrium in a single layer is, when the positive charge does not exceed a limit determined by the value of $n$, greater than the number of units of positive charge on the central system. This is confirmed by the fact that the positive-ray method reveals the existence of negatively charged atoms, for example, the atoms of hydrogen, carbon, oxygen, chlorine are frequently found to be negatively charged, and a negatively charged atom must have more electrons than the number of units of positive charge. Thus, though a calcium atom could not itself charge negatively more than two chlorine atoms, yet if a third chlorine atom, negatively electrified by some external agent, were brought near the calcium atom, it would hold it in stable equilibrium and form the system Ca Cl Cl Cl .
This system would, however, be negatively charged and so could not be expected to
remain free under normal conditions; it might, however, be found in electrolytes or charged gases. There may, however, be electrically neutral compounds in which the calcium atom is surrounded by more than two systems. Let us suppose that instead of bringing up a negatively electrified chlorine atom to the $\mathrm{CaCl}_{2}$, we bring up a molecule which possesses considerable electrical moment. i.c., one in which the positive and negative parts are separated by a considerable distance, such for example, as a molecule of water $\mathrm{H}_{+}(\mathrm{OH})$. The negative end of this would place itself closer to the calcium than the positive one and we should get a system such as that represented in Fig. 3 . 2 .

Ca


Fig. 32
This srstem as a whole is electricall neutral and so could exist under normal conditions; it would be held together by forces of just the same trye as those which hold the atoms together in $\mathrm{CaCl}_{2}$, yet from the ordinary chemical point of view the latter is a valency compound while the former is not.

It must be noticed, however, that though the number of sristems that can exist round the central atom may be greater than the positive charge on that atom, theory indicates that there is a sharp limit to this number, so that the possible compounds of this type would be determined by definite rules.

We can get some information about the number of atoms or molecules which can be grouped in stable equilibrium about a central system $S$ by applying the conditions for stability which we have already used when considering the stability of arrangements of electrons in the atom. Let us suppose that the atoms grouped around $S$ are the centers of octets of electrons, the electrons in these octets which are nearest to $S$ will furnish a layer of electrons round $S$ and for stability the number of electrons in this laver must not
exceed eight. The number of electrons an octet will supply to this layer will depend upon the orientation of the octet If () is the center of the octet, then if 50 passes through an electron, i.e., if the octet presents a corner to $S$, it will supply one electron to this layer. If $S O$ bisects at right angles the line joining two electrons on the octet. i.e., if the octet presents an edge to $S$, two electrons will be supplied; while if $S O$ is at right angles to a face of the octet, i.e., if the octet presents a face to $S$, four electrons will be supplied When all the octets present corners to $S$ the maximum number around $S$ will be eight. Considering the exiguous character of this connection between $S$ and the octets, we should not expect this arrangement to have any very great stability. If each octet presents an edge to $S$, the maximum number of octets will be four, while if each presents a face to $S$, the maximum number will be two. Thus the number of systems which can be held in stable equilibrium in the first zone round $S$, which following Werner we shall call the coordination number of $S$, may vary from 2 to $S$. Werner finds that an appreciable number of elements have a maximum coordination number four, a few have eight, the number for the majority is, however, six, which would correspond to four of the octets presenting a corncr, and two an edge to $S$.

The coordination number is never less than the valency and is generally greater. The somewhat vague notion implied by the use of the term "Residual Affinity." which appears frequently in chemical literature, is an attempt to give expression to the facts implied by a difference between the valency and the coordination number. The consequences of this difference are of the first importance. Let us see, for example, how it would facilitate the aggregation of molecules. Let us take as an example formaldehyde $\mathrm{COH}_{2}$, a substance which is saturated for valency purposes, but is not coordinately saturated. Thus if $A$ (Fig. 33) represents a molecule of formaldehyde, then if the coordination number of carbon is four. A can hold another negatively electrified oxygen atom in its shell; this may form a part of another formaldehyde molecule $B$, and thus $A$ and $B$ may be held together in the way indicated in Fig. 3.3. As $B$ is not coordinately satisfied. it may link up with the oxrgen from a third molecule $C$; in this way aggregates of the formaldehyde molecule would be formed readily.

We can apply to the union of molecules considerations quite analogous to those we
applided the combination of atoms. Thas. for example, we can pieture two moleenles of Li (! joined together by an arrangement like Fige :3. which is smilar to that binding two atoms of lithium together, the electrons in the latter being replaced by negatively electrified atoms in the chlorite. Indeed, if the coordination mumber were always eight, the molecular componmds would run guite parallel with the atomic ones, c.g. whe atoms would be arranded in octets in the molecular compounds just as the electrons are arranged in octets in the atomic ones. Since eight is the maximum mumber of electrons which can be arranged in one layer round a central atom, eight is the coordination mumber of an atom with respect to electrons; hence when the coordination number in molecular compounds is eight, we see that the molecular compounds will run parallel to the atomic ones. Let us apply this result to a particular case. We saw that when the atoms of an element contain few electrons, so few that these are not sufficient in a diatomic molecule to make up the total of cight, the molecules have a great attraction for each other, so that the element under normal conditions is in the solid state, e.g., $\mathrm{Li}, \mathrm{Be}, \mathrm{Bo}$, C. When, however, there are sufficient electrons in the atom for the atoms in a diatomic molecule to make up, by sharing electrons, one or more octets, the molecules have but little attraction for each other, and the element is gaseous, e.g., $\mathrm{N}_{2}, \mathrm{O}_{2}, \mathrm{~F}_{2}, \mathrm{Ne}$. Considerations of exactly the same character will apply to the molecular compounds formed, for example, by the chlorides. A chloride like NaCl , which contains only one chlorine atom, is analogous to an atom containing only one electron; a chloride like $\mathrm{BeCl}_{2}$. which contains two chlorine atoms to an atom containing two e'ectrons and so on. The molecules formed by atoms which contain less than five electrons exert great attractions on each other and condense into the solid state, while those containing five or more electrons are much more volatile and for the elements in the first period are gaseous. The result we have just obtained shows that we may apply to the chlorides the same reasoning as we applied to the atoms. Hence we should expect those chlorides which contain only a small number of chlorine atoms to be solids; while those containing more than a certain number of chlorine atoms should be much more volatile. The following table of the boiling points of the different chlorides and fluorides shows that this is the case to a very marked extent.

The mumber of halogen atoms corresponding to a volatile or non-volatile substance will depend upon the coordination number of the element with which the halogen atoms are combined. The smaller the coordination number of the clement, the smaller the number of chlorine atoms required to make the chloride volatile As the coordination number varies from element to element, the connection between volatility and the number of chlorine atoms cannot be expected to be as clear cut as that between the volatility of an element and the number of electrons in the atom, when the coordination number of an atom with respect to an electron is always cight. The non-volatility of some of the chlorides such as $\mathrm{WCl}_{5}, \mathrm{WCl}_{6}$ is, I think, due to the c lorine atoms being in two laycrs, so that the number in the outer layer, which determines the volatility, is less than the number of chlorine atoms in the compound.

Compounds Containing One IIalogen Atom

| $\quad$ Name | Formula | Melting <br> Point |
| :--- | ---: | :---: |
| Boiling <br> Point |  |  |
| Sodium chloride | NaCl | 776 |
| Silver chloride | AgCl | 450 |
| Sodium fluoride | NaF | above 902 |


| $\quad$ Compounds Containing | Two Halogen | Atoms |  |
| :--- | :--- | :--- | :--- |
| alcium chloride | $\mathrm{CaCl}_{2}$ | 720 |  |
| Iagnesium chloride | $\mathrm{MgCl}_{2}$ | 708 |  |
| trontium fluoride | $\mathrm{SrF}_{2}$ | above | 902 |
| alcium fluoride | $\mathrm{CaF}_{2}$ | above 902 |  |
| tannous chloride | $\mathrm{SnCl}_{2}$ | 250 | 620 |

Compounds Containing Three Halogen Atoms

| Antimony trichloride | $\mathrm{SbCl}_{3}$ | 73 | 223 |
| :--- | :--- | :--- | ---: |
| Bismuth trichloride | $\mathrm{BCCl}_{3}$ | 230 | 430 |
| Boron trichloride | $\mathrm{BCl}_{3}$ | liquid | 18 |


| Boron trichloride | $\mathrm{BCl}_{3}$ | liquid |
| :--- | :--- | :--- |
| 18 |  |  |

Compounds Containing Four Halogen Atoms

| Silicon tetrachloride | $\mathrm{SiCl}_{4}$ | liquid 50 |
| :--- | :--- | :--- |
| Stannic chloride | $\mathrm{SnCl}_{4}$ | liquid 114 |
| Titanium tetrachloride | $\mathrm{TiCl}_{4}$ | liquid 135 |
| Silicon tetrafluoride | $\mathrm{SiF}_{4}$ | gas |

Compounds Containing Five Halogen Atoms

| ny pentachloride | $\mathrm{SbCl}_{5}$ | gas |
| :---: | :---: | :---: |
| Molybdenum pentachloride | $\mathrm{MoCl}_{5}$ | 194 |

$\begin{array}{lllll}\text { Tungsten pentachloride } & \mathrm{WCl}_{5} & 248 & 278\end{array}$

| Compounds Containing |  |  |  |
| :--- | :--- | :--- | :--- |
| Six Halogen Atoms |  |  |  |
| Sulphur hexafluoride | $\mathrm{SF}_{6}$ | gas |  |
| Tungsten hexachloride | $\mathrm{WCl}_{6}$ | 275 | 346 |

Another example of the analogy in physical properties for similar proportions between the number of electrons in the atom and the number of chlorine atoms in a chloride is afforded by the consideration of the electrical properties of the elements and of chemical compounds.

When there are less than four electrons in the outer layer of an atom of an element, the element is a metal and a good conductor of electricity, the conductivity arising from the movement of the electrons: when there are more than four electrons in the outer layer the element is a bad conductor of electricity. The electrical conductivity of fused chlorides may be compared with that of the metals, the negatively electrified chlorine atoms taking the place of the electrons and making the conduction electrolytic. Chlorides containing a small number of chlorine atoms are good conductors when fused, while the higher chlorides like $\mathrm{SnCl}_{4}, \mathrm{CCl}_{4}$ insulate, although they are in the liquid state.

The thermionic properties of metals find, too, a parallel in those of the chlorides. A metal contains lattices of positively electrified atoms and electrons, the solid chlorides, lattices of the atoms of the metal and of negatively electrified chlorine atoms, and the work required to eject a chlorine atom from the salt would be of the same order as that required to eject an electron from the metal. Again, the proportion between the number of atoms and electrons in the metal would be the same as that between the number of metal atoms and of chlorine atoms in its chloride. Hence we should expect from thermodynamic considerations that at temperatures at which the thermionic emission of electrons from the metal is considerable, there should be an


Fig. 33
emission of negatively electrified chlorine atoms from the salt. Such an emission does in fact take place. ${ }^{16}$ When salts are first heated considerable currents' are carried by the chlorine atoms and no electrons can be

[^73]detected. The effects produced he prolonged heating are very complicated, more so even than those occurring on the emission of electrons from hot metals. This is what we might expect, as the tearing away of the chlorine atoms would produce a more fund-

mental change in the surface than the emossion of electrons from a metal. After prolonged heating electrons, as well as chlorine atoms, are given off. suggesting that the tearing away of the chlorine atoms has produce an excess of metal atoms at the surface.

When the coordination numbers of the metals occurring in double salts are not all equal, the arrangement of the electronegative atoms round the atom of the metal will not be in octets, but one which provides a laver of negative atoms round each atom equal to the coordination number of that atom.

Before leaving the consideration of the coordination number we must raise the question whether a doubly charged atom like oxygen ought to count as two towards the coordination number as it does towards the valency: If we take the view before discussed, the oxygen atom for coordination purposes ought to count as one and not as two. On that view the limits to the coordination mumbet depend on the octets round the central atom. An octet with a double charge, such as that associated with an oxygen ion, can be orientated so as not to bring more electrons into the layer next the central atom than an octet with a single charge like that associated with a chlorine ion, thus the oxygen need not count for more than the chlorine.

## Electrolytic Dissociation

When the coordination number of the central atom is greater than its valency, the
molecule can combine with polar molecoles such as $\mathrm{H}_{2} \mathrm{O}, \mathrm{NH}_{3}$ to form new compounds in which the atoms in the original mokente are driven further apart, and are therefore able to rearrange themselves with the expenditure of much less energy than would have been necessary if these compounds had not been formed. Positively and negatively charged atoms may in this way be thrust so far apart and the connection between them made so shight that they move in opposite directions. under the action of an electric field, and are thus resolved into ions

This is well illustrated he the well-known example given by Werner of the ammoniates of platinic chloride. If the coordination number of platinum is six, then in $\mathrm{PtCl}_{4}$ there is room for two polar molecules in the first layer round the platinum atom without that layer becoming unstable. The chlorine atoms are in direct comection with a platinum atom and so cannot be detached easily from it. Thus the compound $\mathrm{PtCl}_{4}\left(\mathrm{NH}_{3}\right)_{2}$ is not an clectrolyte. If, however, more molecules of $\mathrm{NH}_{3}$ are added, since 6 is the maximum number of constituents which can be in one layer round the positive charge, the constituents in the inner layer must break up into two groups, one group forming a layer of six next the platinum, the remainder forming an outer layer at some distance from the inner one. The process is very closely analogous to that described in Part I when new layers of electrons were formed when the number of electrons in the atom exceeds the number which can be held in stable equilibrium in one layer by the central positive charge.

Thus if four molecules of ammonia are added to the platinic chloride, there must be two constituents in the outer layer; if these are

[^74]chlorine atoms carrying a negative charge they will tee easily detached and form negative chorine atoms and the compound will be, as Werner showed it is, an clectrolyte, with ions $\mathrm{Pt}\left(\mathrm{l}_{2}\left(\mathrm{NH}_{3}\right)_{2}\right.$ and ClCl . The work required to separate the ions comes from the loss of potential energy due to the approach of the polar molecules to the central system, and not from thermal agitation. The reasons in favor of this view of electrolytic dissociation are in my opinion very strong. I have already pointel out that to ionize a molecule isolated from otber molecules would require an amount of energy comparable with the "ionizing potential" of one of its atoms, a quantity varying from one element to another, but comparable with 10 volts. As the average kinctic energy of a molecule at $0^{\circ} \mathrm{C}$. due to thermal agitation is, when measured on the same scale, only about $1 / 30$ of a volt, it will be seen that there is little likelihood of the ionization being due to thermal agitation.

On this view of electrolytic dissociation the ions in the solution are not simple atoms or radicles, but combinations of these with polar molecules. These molecules not only dissociate the original molecule, but after dissociation they tend to keep the ions apart. They surround the charge on the central atom with an oppositely charged laver and thus diminish its attraction on other systems. Thus, for example, in an aqueous solution of $\mathrm{CaCl}_{2}$ the positively electrified part of the calcium atom would have next to it the negative ends of polar water molecules, and the attraction between it and an oppositely charged chlorine atom would be diminished. The researches of Mr. Washburn furnish direct experimental evidence of the hydration of ions. ${ }^{17}$
(To be Continued)



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（1）escribes the properties of a new alloy for electrical work．）

## Amplifiers，Vacuum Tube

Experimental Investigations of High－frequeney Amplifier Tibles．Bley，．（In Ger nan．）
 （Considers the various factors that influence the performance of high－frequeney tubes．）

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Reducing Substation Cost and Insulator Hazard by Stee］Buses．
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## Electric Distribution

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（Includes methods of overhead and under－ ground construction as used by the Hydro－ clectric Power Commission of Ontario．）
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（Gives two approximate formulas，derived from a series of 16 tests，for calculating the heat transfer from tank to atmosphere．）
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## General Electric Review

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The Casting of Plate Glass. From a pot, manipulated by the teeming crane, molten glass is poured on the casting table in front of the 13 -ton roller while this is being rolled to the right. The complete process of manufacture and electricity's part therein is described on page 746

## General Electric Review

## MUTUAL"HELPFULNESS

We are very pleased to be able to publish in this issute an address recently given by Mr. E. W. Rice, Jr. It is descriptive of a visit he and Dr. W. R. Whitney paid to Europe together.

Our pleasure in publishing this address lies largely in the fact that it reads differently from most accounts of foreign visits that we have seen. It is simple observation made by an analytical mind long trained in science, engincering and business. There is no point to be made-nothing to prove or nothing to disapprove-and there is no political or diplomatic slant. Above all it shows a keen grasp of realities and a great appreciation and sympathy for the work of others.

Our reason for calling particular attention to this address is because we have an abiding faith in the good to come from a better understanding between those with mutual interests in different lands. And also we firmly believe in the good to be accomplished by international co-operation in the solution of our problems-be they scientific, engineering, social, or diplomatic.

Such visits by the right types of minds lead to a better understanding, and the wrorld has just gone through, and has not yet recovered from, a ghastly nightmare because the people did not understand.

With these thoughts in mind let us get another set of thoughts from a few eloquent but brief paragraphs of Carlyle quoted by John Ruskin in his essay on War.

What, speaking in quite unofficial language, is the net purport and upshot of war? To my own knowledge, for cxample, there dwell and toil, in the British rillage of Dumdrudge, usually some five hundred souls. From these. by certain "natural enemies" of the French, there are successively selected, during the French war, say thirty ablebodied men. Dumdrudge, at her own expense, has suckled and nursed them; she has, not without difficulty and sorrow, fed them up to manhood, and even lrained them to crafts, so that one can weave, another build, another hammer, and the weakest can stand under thirty stone avoirdupois. Nevertheless, amid much weeping and swearing, they are selected; all dressed in red; and shipped away, at the public charge, some two thousand miles, or say only to the south of Spain; and fed there till wanted.

And now to that same spot in the south of Spain are thirty similar French artisans, from a French Dumdrulge, in like manner wending; till at length, after infinite effort, the two parties come into actual juxtaposition: and Thirty stands fronting Thirty, each with a gun in his hand.

Straightway the word "Fire!" is given, and the blow the sonls nat of one another, and in place of sixty brisk useful eraftsmen, the world has sixty dead carcasses, which it must bury, and anon sheal tears for. Hat these men any quarrel? Busy as the devil is, mot the smallest. They lived far enough apart; were the entirest strangers; nay, in so wide a universe, there was eren, unconsciousiy, by commerce, some mutual helpfulness between themHow then? Simpleton, their governors had fallen out; and instead of shooting one another, had the cunning to make these poor blockheads shoot.
-Sartor Resartus.
Some may think that this is a strangesul, ject for editorial comment in a technical magazine. but our purpose is to be useful. We think it is worthwhile pointing out that the American engineer who can be thrilled by the honor of sitting in Clerk Maxwell's chair and of being shown the room where Davey, Faraday, Maxwell, Tyndall, Thomson, Kelvin, Rutherford and Dewar worked-all men who helped to lay the scientific foundations upon which Amcrican industry is built-has understanding; and also, has the type of mind that will appreciate "in so wide a iniverse, there was even, unconsciously, by commerce, some mutual helpfulness between them.'

Mutual helpfulness is the thing that all scientists and engineers in all lands can and should strive for

Antual helpfuhness should exist between the artisans of all nations.

The League of Nations is not an entife success-the politicians and the diplomat: have, at least in part, failech. Can't the engineer help?

The engincering and commerial interests of different countries can and should have mutual interests and they can understand each other better if they visit one another. And if while visiting ome another they appreciate the work the other fellow has done. and give of their knowtedge as well as take. and confine criticisms io the constructive class, mutual helpfulness will then be so great that in the futuro it will be harder than in the past to find some poor knave to give the word "Fire" and harder still to find thirty poor fools to wey the order; unless the quarrel is theirs and their fight is for a righteous cause.

We thank Mr. Ricc for the seed he has sown.

- I. R. H


# A Visit to Europe 

<br>


#### Abstract

   


1）t．Whatney amel I saled foom Xew York




 hatd hoon matle whicd womld be of interest and valuc to the（ieneral Vile entre（ompany

In Engrand．We did bot lame of startling new engine eriner develoments，but the pros－ ress eosmed to have eontinued along well defined lines besed apeon the experienere abd practice of the past．There had been at comtinuted increase in the size of gencrating apparatus．and a roond start mate wowarls stations of harger capateit：with latre gencra－ tor mits．and designed to eronemate and sell electricity on a much larerer soake than had heretofore prevailed．But in no case did we learn of stations whose power units would seem large judered by common American practice．In the new enterprises and exten－ stons，the gencration and（listribution was of ot eveles，alternatiner emrent and largely by゙ ：$\quad$ ， 0 （o）－volt．undereround cable．

1 will say bridly that wo wore interested in the latest design of 13 ．$T$－II ．rotary converters whieh were shown to the in operations，and which are so satisfactory in eost and per－ formance as to secure for the B．T－H．Co．the largest share of such business．They were interesting to us as differing in certain detaits of design．such as starting methods，blowout for commutator，ete．，which may be useful 10 us in America．

There also seemed to be a demand in England for the motor converter．A number have been made and sold by the B．T－H There is no demand as yet in this country． although the device has been known to us for many years

The Curtis turbine has been successfully developed in Engłand，under the able en－ gincering leadership of Mr ．Samuelson，and has sriven such a splendid account of itself． even in competition with the Parsons turbine in its own home，that the business has greatly increased and larger facilities for
marhincry and toris have been fommed neeses－ sary and ate be ine provided．

Some of the latest developments in switch－ ing appatratus wore of interest，especially the ase of an inculating eompound for pro－ tection of the bushars and the corresponding switches，transformers and instruments，and wher switchboard deviees and arrangements worked out to eo－operate with this new sys－ tem．The advantages over present methods were satid to be a sreat saving in the space reepuired for substation buiklings，etc．，as well as grater use of standardized parts． This resulted in great saving to the customer as well as to the manufacturer，although the price of the switchbord apparatus purchased he the enstomer was naturally much greater than for the air insulated type．I found that our switchboard engineers here were familiar with this new adrance．Apparently． however，we have not put out any such apparatus in America．I believe that the advantages of this method of insulation are sueh that the swstem will be used to con－ siderable extent in this country，and that we should push our own derelopment as rapidly as possible．

I will say nothing more at present about B．T－H．cngineering developments，but will take up our investigations in the research field．

While in London，Dr．Whitney and I． together or separately，saw most of the leading scientific men engaged in electrical or physical researeh，such as Dr．Donnan，the very able and energetic head of the Chemistry Department at University College，an old friend and brother student of Dr．Whit－ nev＇s at Leipsic：Professor Aston，of Caven－ dish Laboratory．Cambridge，whose original work in the discoveries in isotopes have been so fruitful and remarkable．He called upon us on the way to Stockholm where he was to receive the Nobel prize which had been awarded to him． He is fine，modest and enthusiastic；has visited Schenectady． and is therefore personally known to many of our research workers．Incidentally，I be－ lieve that he is a good golfer and has a
brother who manufactures a very superior type of elub Professor O Wichardson. of Kings College Labotatory of Phesies, who made carly and notable investigations into the laws governing the dischared of electricte. through racua: Sir William Braser who is chiefly known through his remarkable work with the X-ray spectra, covering the structure and pesition of the atoms in erestals: Profeson Coker, who is head of the Mechanical Engineering Department at the Coniversity College, who spent some time in schencetady, and whose work in connection with the pictorial illustration of the strains in mechanical work has been made useful to us in many directions. His machine and beautiful methods have been described in the Geveral. Electric Reven:

We alon ristical the National Phersice Laboratory at Buthey Park. (The work of this (foremment lnstitution is in many respects similar to the Bureau of Standards in Wathmeton

The new Research Laboratory of the General Electric Company. Ltd., at Wembley. is the lates word in this line haring been completed but recently after a careful study by Director Patturson of research laboratories and organizations in other parts of the world. inchuding schonectady. The buildings and facilities are must excellent. Director Patterson is ambitiou in make this laboratory the leater in such work in England. If he is as successitu in obtaining a group; of scientific workers as he has been in the physcal layont, he will be in line to realize his ambition.

On Dectmber 11. we took an early train to Cambridye for a visit to the Cavendish Laboratory by appointment with its Director. Sir Emest Rutherford. Rutherford needs no int:oduction to a group of engineers or scientinic men. His investigation into the nature of radimm and its disintegration products and alpha ray, his theory of the atom, his brilliant experimental investigations his broad and fruitful theories and his writings have all combined to make him justly famous not only in England but throughout the world.

Linder his leadership there is now gathered at Cambridge a sroup of talented and earnest workers many about as well known as himself, such as Professor Aston. C. T. R Wilson. and others. He is a worthy successor to Sir Joseph Thomson. who. by the way, is now Master of Trinity College. Cambridge.
but still retains latmotary romms at Cavemdish.

Neither Whitney mor I will wer forme the two days we spent at (ambridge. Kutherford comducted us about his laboratory introduced us to his assistants. and showed us a number of his most interesting experiments.

One experiment esperially delighted us. C. T. R Wilom had shown some yeare ag that be admitums some iomizing particles into a chamber contaming air saturated with mosisture, and at the same time expanding the air, the track of an alpha particle through the air of the chamber was marle risible because of the water drops iommed around the inns produced by the 1 artice on its journer: Rutheriord showed us such an apparatus and the ionization produced be the alpha particles was such that the paths of the different alpha particler were ceary defmed as separate straisht line radiatine from the radium. Some of the lines. after passing straight as an arrow for an inch or more. wrould bend sharply at an ande. This bending occurred when the alpha particle struck the nucleus of an atom and was deflected. Rutherford repeated the experiment for us a number of times and left no doubt in our minds that we were actually looking at the path of an alpha particle (nucleus of a helium atom) driving with a speed of 20.1001 miles or more a second through the gas. and knocking off electrons from the atoms of gas on the way: to finally collide with the mucleus of an atom.

We had read of this experment many times and had seen the resulting photographs. but the sight of the actual erent produced a much more vivid and satisfactory impression of the reality of the phenomenon. Dr. Whitney has arranged to purchase or make one of the Wilson condensation chambers so that we may all have the pleasure of seeing this wonderfu! phenomenon in our laboratory at Schenectady:

Sir Ernest went with us to call upon Sir Joseph Thomson. Master of Trinity who invited us to dinner at Trinity Hall and to his rooms in the evening. where we had a most delightful time listening to the entertaining conversation of J. I. Thomson and Rutheriord. Sir Joseph. by the way is a successor to Clerk Maxwell and occupies Maxwells room at Trinity College. We were both invited to sit in Maxwell's old arm chair. a privilege which we both gladly. accepted.
( )ur thomghts maturally turned to the memory of that gemins Maxwell, whose mathematical and theoretical writingselucidated the great Faradaydexperimental researches, whose equations demonstrated the identity of light waves and electro-magnetic waves, and therefore that light itself was an clectro-matgetic phenomenon. The plysical demonstration of this wonderful prophecy had to wait for many yearsuntil that incomparable experimenter Ilertz made the actual demonstration. We could only wish that Maxwell could have lived to enjoy sceing the fulfiment of his prophecies and to see the great advances in his field made by his successors, Sir Joseph Thomson, Rutherford and others.

We were delighted that J. J. Thomson was able to visit our Research Laboratory at Schenectady at a later date and that Coolidge, Langmuir and others, in the absence of Dr. Whitney, were able to show Sir Joseph matters of interest and to return in some degree the courtesies extended to Whitney and mysclf while in Cambridge.

We were also gratified that our Directors approved our suggestion, made soon after our return home, to give a small fund to Rutherford for the advance of his scientific investigations. We believe this contribution by the General Electric Company will prove a good investment.

Upon returning to London, we made a visit to Sir James Dewar at the Royal Institution. Dewar met us and conducted us all over the rooms of the Institution. He showed us the library filled with invaluable scientific books and literature, the laboratories of Davy and Faraday, the room where Davy, Faraday, Maxwell, Tyndall, Sir Joseph Thomson, Kelvin, Rutherford, and Dewar himself had lectured, and which Dewar had just refurnished at his own expense-all sacred ground to scientific men. He talked to us of his friend, Lord Kelvin, and of Kamerlingh Onnes. He took us down to his own laboratory and showed us his latest apparatus for experimenting with oil films, about which he lectured a few weeks later before the Royal Institution. The oil was contained in a glass cell and arranged so that the thickness of the soap bubble film could be delicately varied by regulated air pressure. He projected on the screen a picture with all the beautiful tints of the rainbow, which he called "The Dance of the Molecules," and it filled us with longing to know and see more, and to linger in the presence of his strong and fascinating personality.

As we listened to the brilliant conversation of this enthosiastic and witty Scotehman, be was so full of vigor and vitality that it was difficult to realize that he was past so years, and easy to believe he would live for many years to advance the cause of science and humanity. We were greatly shocked to hear of his cleath a few weeks later.

Dewar is chiefly known to the world as one who investigated liquid oxygen, hydrogen, helium and other gases, but particularly as the inventor of the Dewar vacuum flask, which unfortunately is known to the world as the "thermos" bottle. He gave this to the world as a free gift. With much gusto, and in his inimitable manner and brogue, he told us of how his friend Kelvin had called him "an awful fool" because he had not patented his ideas, pointing out that if he had patented the vacuum flask he would easily have made a great fortune. Dewar said he tried Kelvin's plan on his next invention, the use of charcoal for absorbing gases, with the net result that he made an out-ofpocket expenditure of five thousand pounds in lawyers' fees, and had nothing but trouble for his pains. It is a shame that this wonderful invention of the vacuum flask which has done so much for the comfort of millions of people should have yielded nothing to its inventor and that even his name is not connected with it in the public mind. I wish we would all make an effort to speak of the thermos bottle as the Dewar bottle or flask.

From London we went to Paris, and took a few weeks' vacation, during which we incidentally explored the Grimaldi caves on the shore of the Mediterranean near the boundary of France and Italy. Some thirty years ago there were discovered in these caves the remains of prehistoric man along with the remains of the mastodon, the sabre tooth tiger, the cave bear and other extinct animals which lived one or two hundred thousand years ago.

We returned to Paris and resumed our work. We visited the University of Paris, at the Sorbonne, meeting the physicist Fabry of the Institute Optique, Prof. Langevin at the College of France, Professors Abraham, Bloch and DuFraisse at the Physical Department of the University of Paris, Prof. Perrin at the Laboratory of Physics, at the Sorbonne, etc.

We spent some time with Prof. Moureu, head of the Chemical Department in his laboratory at the College of France, and he
showed us some interesting new insulating material and chemical substances.

We visited the Gaumont factory and laboratory where we saw talking and colored movies or "cinemas" as they are called in France.

After making several indirect efforts to meet Madame Curic without success, we decided to do it "American Style," took a taxi to the Radium Institute and sent in our cards. We were immediately and most graciously received by Madame Curie. Dr. Whitney led the conversation, as it was in French, but after a short time Madame Curie began, with an apology for her" "poor" English, to converse in most excellent idiomatic English, much to my satisfaction, as my understanding of spoken French is painfully limited. For some strange reason I always could understand the French spoken by the Doctor better than that spoken by a Frenchman.

We found Madame Curie an unassuming, intelligent woman, full of enthusiasm for her work, and well posted as to the progress of science in other fields. She is, as you know, the co-discoverer with her husband of radium. She has a fine set of rooms with several assistants at her disposal in the new buildings of the Radium Institute.

The Radium Institute is well provided with clinics and a full line of apparatus for the therapeutic treatment of cancer, etc., by radium as well as by X-ray. This portion 0 : the work is under the direction of Prof. Regaud, biological expert, assisted by a number of young and intelligent scientific workers. Careful investigations are in process and we may hopefully look forward to discoveries which will prove a boon to suffering humanity.

Dr. Whitney found that Madame Curie was desirous of help on X-ray work and Dr. Regaud wished us to assist with new tubes of highest possible voltage, and arrangements were made that this should be done through Mr. Pilon, of the French X-ray Company. In return, the results of experimental work with X-rays at the Institute will be supplied us.

Time will not permit, and I should only weary you if I told of our visits to the Belin laboratory near Paris, where we saw Belin's method of sending copies of photographs, pictures and autographed letters by wireless, or of a visit to the Eiffel Tower wireless station operated by the French Government, containing considerable obsolete apparatus.

This is not intended as a criticism, as the condition is probably due to a lack of funds necessary to keep pace with the rapidly advancing technique of the new att.

On our visit to St. Assize, the big wireless transmission station of the French Wireless Company, we were shown apparatus of more modern character, quite similar to that used by our Radio Corporation here in America. We had the pleasure of listening to signals from home-Rocky Point, Long Island.

The French Wireless Company is doing a regular commercial business with the United States, England, Algiers, Syria, Constantinople, the Near East, etc., and works in cooperation with the Radio Corporation of America. Manager Girardeau is young and progressive, and may be trusted to keep his system up-to-date.

We were most favorably impressed by Gaumont, who is the leader in France in the production of moving picture films and apparatus. He has a large factory and laboratory in the suburbs, and operates a large theater in Paris. We visited his factory and laboratory several times and were shown a good colored movie and a good talking movie.

After some weeks in Paris, of which I have given a most fragmentary sketch, we decided to go to Switzerland, partly for a rest and partly to see some things scientific, and also because that was a good way to get to Germany.

After a short holiday at Lake Lugano and Como, Dr. Whitney left me for Germany. While at Lugano we called on C. E. L. Brown, the founder of Brown-Boveri \&Co., well known to you gentlemen as one of the pioneers in alternating-current power transmission. He engineered and supplied the apparatus for the famous 3 -phase power transmission from Lauffen to Frankfort at the Frankfort exhibition in Germany, in 1891. It was a great pleasure to renew our acquaintance of many years with Brown, who is interested in all things worth while, a good friend to America, and of a most inspiring personality.

Next day we took the electric train for Zurich. We started by riding on the locomotive from Lugano, up the St. Gotthard Pass, and through the famous tunnel. It was a thrilling ride through beautiful scenery. We stopped on the way at Bellinzona and carefully examined the various locomotives in the repair shops of the railroad company located at that place. It is the practice to
 kilometors of operation
'The locomotives were mate by brownBoseri and (orlikens, and have bexal fally described in considerable detail bes the teednical press O Onr rabluay emgineers ate fally famitiar with their comstractions. Noont IO

- Gocomotives are beed on the St. (iotthard Division which mans from ( hatasso to \%arich a total kongh of about :300 kilometers, and mostly two tracks . 111 of these bocomotives are singte-phase, $16 z_{3}$ croles, operating from werhead lines at loboot volts with maximum speeds varying from (i.) to !o kilometers an hour and weighing from 90 to 11.5 tons.

Some fol kilometers of main line rablwas. hate already been electrifed, and by lose it is expected that 1.000 kilometers will be elecrified out of a lotal railway mileage in all switzerland of 30000 kilometers.

Power for the St. Cothard Division, above mentioned, is supplied from two hydroeleetric stations containing $1\left(i z_{3}\right.$-cyele, singlephase apparatus, one located at the south end of the tumnel and the other at the north end. The total installed kilowatts are about T0,000 with a transmission voltage of 60,0000 with grounded neutral. Serious telephone and telegraph troubles were avoided by moving the wires away from the railway route, or placing them in lead covered cables buried in the right of way.

At Zurich, we visited the plants of BrownBoveri. Oerliken, and Escher-Wyss, with a side trip to Winterthur to see the incandescent lamp factory operated by Dr. Remane, who is well known to our ineandescent lamp people. We saw at both Brown-Boveri and Oerliken large numbers of electric locomotives of the type already mentioned being manufactured, and they also had an order for freight locomotives for the French Railway system. Brown-Boveri were manufacturing mercury rectifiers on a large scale, and, we were told, had sold at least $200,000 \mathrm{kw}$. with something like $100,000 \mathrm{kw}$. in operation.

Dr. Zoelly, head of Escher-Wyss, showed us all through his works and we saw there his latest designs of waterwheel turbines, steam turbines and electric refrigerating apparatus. We were particularly interested in the very well equipped hydraulic laboratory fitted out to test the efficiency of waterwheels under actual operating conditions. We also spent an interesting hour with Prof. Stodola, the great European authority on steam turbines, at the Polytechnic Institute.

At Manstricht, Mollamd, we attended at Scientifice (onvention which is held at regular intervals in Holland, to whioh physiodsts, chemists, docors, biologists, ete., from Ilolland, Devgium, Scandinavia and parts of Cermany eome together to discuss problems of mutual interest. There we met quite a number of the rescareh engineers of the Philips Lamp Works of Eindhosen, Ilodand. and also had the pleasure of meeting Dr. Coster, eorlisconcerer with Hevescy of the clement "hafnitm," Hafnium is one of the dements, number $\bar{i} 2$ in the Periodie Series of the efements, whose existence was predieted by Moscley. It is a sort of glorified zireonimin. It was rather astonishing to hear Coster state that this hitherto unknown element existed in sufficient quantity in his estimation to represent at least a hundred thousandth part of the crust of the earth. Dr. Nernst, whom we afterward met in (iermany, stated that if he had had hafnium the Nernst slower incandescent lamp might still be a commercial illuminant.

At Eindhoven we spent some time visiting Mr. Philips and his researeh men, and the works and laboratory. Philips is most progressive and has started a research laboratory under the charge of Dr. Holst, assisted by a group of able young scientists. We were most favorably impressed with the character of these men and the quality of their work. We saw under construction a large group of buildings of most excellent design which were to be devoted exclusively to research work.

From Eindhoven we went to Leyden, and there met Kamerleigh Onnes at his Cryogenic Laboratories at the University of Levden. Onnes is an enthusiastic youngster of 70 or more years, well known as the liquefier of helium and for his inrestigations into the conductivity of materials at the extraordinarily low temperature of 1 or 2 degrees absolute. In his laboratory he has succeeded in producing temperatures that are estimated to be colder than that of interplanetary space, and has shown that if a current of electricity is merely started even in a lead wire at such low temperatures, it will go on circulating for many hours, because at such low temperatures all conductors of electricity become practically perfect conductors. Onnes speaks of them as "super" conductors.

From Leyden we took the night train for Berlin, arriving there in the morning on time and without any unpleasant adventures.
()ur visit to Germany is a story by itself. If 1 attempted to go into detaits it would take more time than we have at our disposal.

1 may say briefly that we maturally saw first our ohl friends of the A.E.C., and many whers.

Dr. Deutsch, the head of the Allegemeine Co, sate us a lancheon. After a preliminary discussion we were told of the general business situation in Cermany, and we obtained the impression that all hands were quite discouraged. Nevertheless the factories seemed to be full and the workmen occupied. So far as we could notice in walking about the shops and streets, the people seemed to be contented, happy and well fed as before the war. We noticed a scarcity of atitomobiles and yet one coukd not safely cross Unter den Linden without "watching his step."

We risited the various factories of the A.E.G. and did not notice any great changes over ten years ago in turbines, large generators, motors, and similar lines. We did see some matters of interest as different from our own practice in switchboards and transformers.

We visited the works of Siemens \& Halske. A.E.G.'s great German competitor, where we met the Managing Director, his associates, and some of the engineers. We also visited the works of Bergman who makes cables. turbines, motors, locomotives and other lines generally competitive with A.E.G. and to a lesser extent, with Siemens and Halske.

Bergman, as some of you know, was an old associate of Edison, and a friend of ours. He was extremely anxious and proud to show us his factory. We were particularly interested to note that he had large orders for locomotives to be supplied to the State lines in Bavaria. These locomotives were about 2000 h.p. and operated by singlephase, alternating current, $162 / 3$ cycles. They were in general very similar to the Swiss locomotives already mentioned.

Out of the window of Bergman's office, we saw a super-power line which we were told was operating at 100,000 volts as part of a system for bringing electricity from brown coal mines about so miles from Berlin. This installation, which utilizes immense deposits of brown coal which exist in this part of Germany, has been described in the technical press. We were interested to see that these power lines have been put right through what is practically the most populous part of Berlin. This was done during the war, but it is probable they will remain permanently.

The incandeseent lamp business in Germany was formerly handted by three large companies. - .E. $(\dot{\text { i }}$, Siemens \& llalske, and the ()sram Co. These are now combined into one large company which the three parent companies control. Bergman and some others have been licensed to manufacture drawn tungsten lamps. Dr. Whitney hat visited the lamp factorics before my arrival, and I did not find time to repeat these visits.

At the time we were in Berlin, the mark was worth about 20,000 to the dollar and had been held fairly stable for some months. A few days after we left it declined to 30,000 to the dollar, and has since been traveling downward until it has reached the present fantastic figure of millions of marks to the dollar. We thought 20,000 was bad enough. as this meant that 1,000 marks were only equal to an American nickel in value.

We were told that the working people, through increases of wages and other means were then obtaining wages equivalent to about 8. Si) $^{\text {per cent of the gold value before the }}$ war. The farmers were getting as much or more than before the war; the managing class about 50 per cent, hut the professional and scientific and research workers were apparently receiving not much over 10 to 20 per cent, and all the savings invested in mortgages, bonds, etc., of course were valucless. There seemed, therefore, to be a real danger that the scientific and research work of Germany, especially in the Universities and outside of the large industrial corporations was suffering and likely to disappear. This, we all realized, would be a great loss to the world, and Dr. Whitney was especially anxious that something shoutd be done to show our desire to assist pure scientific work.

As a result of meetings with Prof. Nernst. the great German chemist, inventor of the Nernst lamp, and present Director of the Techniches Reichsanstalt, and after conferences with the leading men in the A.E.C. and Siemens-Halske, we arranged to place a small fund at the disposal of Dr. Nernst for specific scientific investigations in which we were interested. The results of this research, if successfut, would be useful to the electrical industry in general and to the General Electric Compans as the world's largest manufacturer.

The problem which Dr. Nernst has agreed to mudertake is the investigation of the electric phenomena preceding and accompanying the breakdown of insulators. This
is a problem on which our own Dr. Steinmetz has been at work, but it is a case where competition is useful.

We also arranged for the assistance of pure electro-physical research in Germany for one year under a Committer consist ing of the eminent and well-known scientists Max Planck, Prof. llaber, Drs. Nernst, Latue, and Franke.

The money is to be used for the purchase of apparatus and material, and must not be used to relieve the Govermment of its duty of properly maintaining any laboratory. It is also to be used for the remmeration of co-workers and assistants. It is not to be used for the solution of problems of direct industrial use, such as specific technical processes.

We visited the Kaiser Wilhelm Institute, under the direction of Dr. Haber. It is a well equipped government institution for research in physics, chemistry and biology, the Reichsanstalt, as mentioned above, and a number of Government wireless laboratories scattered about Berlin, the wircless laboratory of the Telcfunken Co., etc.

We came out of Germany by night train which took us directly through the Ruhr territory which had then been occupied by the French for about four months. We could see nothing unusual from the train, although the cities as we passed were more or less deserted, but a large number of people seemed to be working in the fields. The country itself never appeared more beautiful.

Shortly after our trip to Germany we took the steamer from England for home, having been away about five months. Needless to say we were glad to get back to our friends and our regular work.

In conclusion I would say that we found in every country that we visited many men earnestly engaged on researches in chemistry, physics, biology, electronics and allied fields. We were welcomed everywhere in the most friendly spirit and were eagerly shown the latest research. Of course we were equally glad to tell of any similar work in America. There was great satisfaction, even joy, in such mutual exchanges of experiences and opinion.

We were impressed by the willingness of such men to co-operate with American workers in advancing the knowledge of nature's laws. There was no holding back, no rescrvations, but an evident desire to share new facts, new theories, new knowledge.

While retaining proper pride in the advancements of their brother nationals, the spirit of scientific service seemed to eradicate national prejudices and to forget political boundaries.

Our fresh realization that such men in every country were marshalled together to conquer our great enemies, ignorance and prejudice, inspires us with confidence in a happy and useful future-if only those who are blind may be made to see.


# Positive Ion Currents in the Positive Column of the Mercury Arc 

By. Dr. Irving Lancimunk


#### Abstract

Negatively chatged electrodes in the path of a mercury are take up a current which is found to be infependent of the impressed voltage Dr. langmuir, starting with this phenomenon, arrives at a theory which not only explains this fact but which also gres a new conception of the nature of the mercury arc. A short prelim.nary note describing this theory has just appeared in Science and we hope to publish subsequent papers on this stabject in the REvTEW.-EDITOK.


When a mercury are passes through a tube of uniform diameter, as in the side arms of a mercury rectifier or in a mercury vapor lamp, the tube is filled with a uniform glow whose intensity depends on the current density and the mercury vapor pressure. Practically the whole of the discharge, except in close proximity to the two electrodes, is of the type usually referred to as the positive column.

If an auxiliary electrode of small size is placed in the path of the discharge and connected to an electrometer or potentiometer, it is found that it acquires a definite potential, which in accordance with common practice we may provisionally assume to be that of the gas surrounding it, and, for convenience, we will refer to as zero potential. If the electrode be charged positively to one or two rolts, a relatively large current of electrons flows to it from the gas, so that it becomes an anode sharing the current with the main anode. If the electrode be negatively charged, the current to it reverses in direction, but only a relatively small current flows, which increases, in general, slowly, if at all, when the negative voltage is raised to several hundred volts, thus behaving as if it were a saturation current. This current must result from a flow of positive ions to the electrode (out of the gas) or an emission of electrons from the electrode (or from both phenomena). Such electron emission might conceivably be photo-electric emission caused by the intense ultraviolet radiation or it might result from the impact of positive ions against the electrode (delta rays).

Numerous experiments in this laboratory, especially with caesium ions from a genode* have proved that positive ions impacting on a surface with velocities up to 300 volts do not cause appreciable electron emission; but the following direct experiments have proved that positive ion bombardment and photo-electric effect cause only very little electron emission

[^75]from an auxiliary electrode in a mereury are under the foregoing conditions.

A $\overline{\text { amp amp mercury are was made to pass }}$ through a 1 -in. tube from a cathode compartment into a 5 -in. spherical glass bulb which was provided with several electrodes. one of these serving as the main anode. Reaching into this bulb was a graphite anode, A, 14 inch in diameter, surrounded by and entirely enclosed within a cylindrical grid, $B$, made of $10-\mathrm{mil}$ molybdenum wires with $30-\mathrm{mil}$ spacing. When $A$ and $B$ were connected together and charged negatively, a current of 17 milliamperes flowed, which increased only about 10 per cent when the voltage was changed from 10 to 125

With B at -20 volts electrons flow readily to A if this electrode is charged positively, a current of an ampere being obtained with only a few volts. But a negative potential of 40 volts or more on $B$ keeps electrons from passing through the grid, so that practically no current flows to A even if several hundred rolts (positive) be applied to this electrode. More careful measurement, however, shows that the current to A is not zero. For example, with -60 volts on $B$ and +60 volts on $A$, a current of 0.094 milliamperes of electrons flowed to A while the current to B was 17 milliamperes: the same as that previously observed to $A+B$ when these were both negative. The current to A is probably due to electrons which are emitted photoelectrically from B and which are then drawn over to $\bar{A}$ by the strong accelerating field between these electrodes. This conclusion is confirmed by the fact that the current to A remains almost absolutely constant when the voltage on B is changed from -60 to -120 , or the voltage on A is changed from +60 to several hundred or even thousands of volts. $\dagger$

More than half of all the electrons emitted from $B$ should pass to $A$ when $A$ is strongly positive. The fact that the current flowing to B was 180 times that flowing to A proves definitely that the current to negatively charged electrodes is carried by positive ions.

It lirst sight it appears improbable that a pesitive ion current from an ioni\%ed gas should be independent of the matage. The explatation. however, is very simple. Consider, for example, a mafommy ionized gas in whim there are swatms of ele tons and ions mowing in random directions with redocities corresponding to a fall through a petential of saty once volt. Assume that each unit of volume contains equal numbers of positive and negative charges (a comdition that must aluats be approximately fulfiled in the positive eolumm). Them through each spotare cm. of an imaginary plane surface there flows a certain enrrent of dectrons corresponding to a current density $l$. Similarly there is : current density of positive ions which we may denote by $I_{+}$. The ratio between $I$ and $I_{+}$is thus the same as the ratio of the velocities of the ions, which is the invers: ratio of the square roots of the masses of the charged particles. Since the mercury ion is $200 \times 1$ ists times heavier than the electron we see that $I_{-}$is bos times as great as $I_{+}$.

Instead of an imaginary plane, let us now consicler the case of an electrode having a plane surface If this electrode is electrically insulated and is originally at zero potential (same potential as the surrounding gas), it at first takes up 60 s times as many electrons as positive ions, and thus becomes more and more negatively charged, until the number of electrons it receives no longer exceeds the number of positive ions. Under the conditions we have assumed, with electrons having a velocity corresponding to 1 volt, the electrode cannot acquire a negative voltage greater than 1 volt, for if it did it could not receive any electrons at all, although it would continue to receive positive ions.

Let us now assume that the plane electrode be charged to a negative potential of 100 volts. Electrons will therefore be prevented from approaching close to the electrode, whereas positive ions will be drawn towards it. There will therefore be a layer of gas near the electrode where there are positive ions, but no electrons, and in this region there will therefore be a positive ion space charge. The outer edge of this sheath of ions will have a potential of -1 and the positive ions pass through this outer cdge with a relocity corresponding to $2 \boldsymbol{2}$ volts.

Pure electron discharges are well known in which the current is limited by space charge. Between parallel plane electrodes, separated

[^76]be the distance $a$, the maximan current density $l$ that catn flow with the difference of poremtial I'betwem the electroces is given by

Where e is the charge of the electron and $m$ is its mass. If $1^{\prime}$ is expressed in volts, $x$ in centimeters, and $I$ in amperes per square centimeter, this equation becomes

$$
\begin{equation*}
I=2.3 \because 3 \times 10^{4} 1^{23}= \tag{2}
\end{equation*}
$$

Equation (1) is applicable also to currents carried wholly by positive ions if we substitute in the equation the mass of the positive ion in place of the mass of the electron. With mereury ions, therefore, the currents given by the space charge equation are fios times smaller than in the case of corresponding clectron currents.

We can now calculate the thickness of the sheath of positive ions in case of any given current density and voltage. For example, let us assume that a plane electrode, charged to a negative potential of 10 volts, takes up a positive ion current of 10 milliamperes per $\mathrm{cm} .{ }^{2}$ By substituting these values of $I$ and $V^{\prime}$ in to the modified equation ( 2 ) , we find $x$ equals 0.020 cm . () 1 the other hand, if the voltage of the electrode were 100 volts, $x$ would be 0.003 .3 .5 cm

The thickness of the sheath with current densities of the order of milliamperes per square centimeter. such as those observed in mercury arcs, is therefore extremely small; in fact. very small compared with the mean free path of the electrons and ions ( 1 to .5 cm .). Whether the voltage on the electrode is 10 volts or 100 volts, all the electrons that reach the outer edge of the sheath are reflected back into the ionized gas and all the positive ions that reach this edge of the sheath more towards the electrode and are absorbed by it. The potential of the electrode has no effect on the potential distribution in the ionized gas beyond the edge of the sheath, and since the displacement of the edge of the sheath by changing the potential from 10 to 100 volts is entirely negligible compared to the dimensions of the discharge tube, it is clear that the number of positive ions that reach the edge of the sheath is also independent of the potential on the electrode.

Thus, the current density of positive ions flowing to a plane electrode measures directly the positive ion current density in the discharge which we have denoted by $I_{+}$.

Schottky* has observed currents up to 70 amperes flowing to the iron case of a
boto-amp, mereury are redifier, and he fond that these currents were absolutely independem of the negative voltage applied to the case. The current densities obtained ranged from I to 10 milliamperes per cm. ${ }^{2}$ Schottive attributed these currents to photo-cleetric effeet and has developed a theory of the positive column of the mercury are totally different from that here described. All of the experimental facts observed by Schottky, however, are in agrement with the present theory of positive ion currents. The remarkable constaney of the currents, which constituted the main reasen that Schottky considered them to be photo-electric, is seen, in fact to follow of necessity if the currents are positive ion currents.

A crucial test of the theory is alforded by the behavior of small, cylindrical electrodes. such as wires. introduced into the path of the discharge. With planc elcetrodes, the increasing thickness of the sheath with increasing voltage does not change the effective area over which the positive ions are collected; but. in the case of small celindrical electrodes, the increasing thickness of the sheath may cause a very appreciable increase in the effective collecting area.

For example, consider a small wire at a certain negative roltage in an ionized gas. The diameter of the sheath may be twice the diameter of the wire itself, and the collecting area, therefore, is the area of the outside of the sheath, for all positive ions which reach the edge of the sheath must fall into the electrode. If the negative voltage of the wire is increased. the thickness of the sheath increases, and. at a certain voltage, the sheath will have a diameter say three times that of the wire. The current to the wire thus increases with the voltage in proportion to the diameter of the sheath.

This theory can be tested quantitatively. because it is possible to calculate the diameter of the positive ion sheath by means of the space charge equations. The current $i$ of positive mercury ions flowing between concentric crlinders is given by the equation

$$
\begin{equation*}
\frac{i}{L}=\frac{1+659 \times 10^{-6}}{605} \frac{1^{32}}{r \beta^{2}} \tag{3}
\end{equation*}
$$

where $r$ is the radius and $L$ the length of the electrode which collects the positive ions, and $\beta$ is a function of $a r, a$ being the radius of the sheath. The function $\beta$ has previously been calculated and tabulated* for the case that the charged particles move from an inner to an outer cylinder. For the inverted case of

[^77]motion inwarls from the outer colinder. the same method of caleulation mas be used Tables of this function of for the inverted case will appear in a fortherming number of the Physical Reaiew. Detemmations of the positive ion currents hate been made whts cylindrical electrodes of several different diameters and with varions intensities of ionization in the meroury vaper. Talle 1. H. III and IN give a few topical results.

The first column gives the negative whate on the electrode. The seeond column amtains the observed current in milliamperes. The third column gives the current densit at the surface of the electrode as observed. The fourth column gives the value of $\beta$ which is calculated from equation (3) by substituting in it the values of 1 (column 1) and $i$ (column 2 ). toget her with $L$. the length of the evlindrical electrode, and $r$. the radius of the electrode as given at the head of each table.

TABLE I
5-ampere Arc in 5 -in. Spherical Bulb. Mercury Vapor Pressure, 0.016 mm . Cylindrical Collecting Electrode: $r=0.95 \mathrm{~cm} . ; \mathrm{L}=5.7 \mathrm{~cm}$.

| $\stackrel{\mathrm{r}^{-}}{\text {olts }}$ | $\begin{aligned} & \quad i \\ & \mathrm{I}, 11 \mathrm{l} /- \\ & \mathrm{amp} . \end{aligned}$ | ! <br> M1illi- <br> amp. <br> per <br> (m. ${ }^{2}$ | $\beta$ | $11 r$ | $\begin{gathered} I \\ \mathrm{I}, \mathrm{illi}- \\ \mathrm{amp} \\ \text { per } \\ \mathrm{cm} . \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | 11.4 | 0.3.50 | (0.028:3 | 1.0.2. ${ }^{\text {d }}$ | (1). $3+10$ |
| 3.$)$ | ] $2 . .5$ | 0.368 | 0.0497 | 1.0 .09 | 10.3 .50 |
| 102 | 13.0 | 11.382 | 0.10 c | 1.110 | 10.347 |

TABLE II
4.4-ampere Arc in 5-in. Spherical Bulb. Mercury Vapor Pressure, 0.027 mm . Graphite Collecting Electrode: $\mathrm{r}=0.32 \mathrm{~cm} . ; \mathrm{L}=3.2 \mathrm{~cm}$.

| $1^{\prime}$ | Mi"liamp. | I | $\beta$ | ${ }^{4} r$ | ${ }_{\text {I }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3.8 | 0.60 | 0.19 .44 | (1.0.5.) | 1.0515 | (1.0.0! |
| 13.7 | 0.65 | $0.10{ }^{2}$ | (1.1:37 | 1.139 | 0.0895 |
| 28.6 | 0.72 | 10.11:3 | (1.2.26 | $1.2: 31$ | 1).092 |
| 58.5 | 0.75 | 0.122 | (0.374 | 1.388 | 0.088 |
| 127.2 | 0.92 | 1.148 | (1.614 | 1.6 .50 | 11.08917 |

TABLE III
9-ampere Arc in Tube 3.2 cm . Diameter. Collecting Electrode: $r=0.0038 \mathrm{~cm} .: \mathrm{L}=1.59 \mathrm{~cm}$.

| 1 | Nilis. amp. | I | $\checkmark$ | $4{ }^{1}$ | I. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 3.00 | -8. 9 | 0.132 | 1.134 | 69.6 |
| S | 3.30 | 86.9 | 0.264 | 1.271 | 68.4 |
| 18 | 3.70 | 97.3 | 0.459 | 1.480 | 65.7 |
| $\because 8$ | +.20 | 110.5 | 0.597 | 1.6 .31 | 67.7 |
| 33 | 5.00 | 131.5 | 0.884 | 1.958 | 67.2 |
| 78 | 5.58 | 147.0 | 1.120 | 2.237 | 65.7 |

TABLE IV
Discharge in Tube with Hot Tungsten Cathode. Voltage of Anode, 50; Current 10 Anode, 0.010 Ampere. Collecting Electrode: $r=0.0063 \mathrm{~cm}$; $\mathrm{L}=1.9 \mathrm{~cm}$. Mercury Vapor Pressure, 0.012 mm .

| 1 | $\begin{aligned} & \quad i \\ & \text { мicro. } \\ & a m p . \end{aligned}$ | $\stackrel{J}{1}$ <br> M1llinแ!!. jer ( 111. ? | H | 16/1 | $I_{+}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 36.2 | 0.15:3 | 2.59 | 1.1)! | 0.118 |
| $\because()$ | ¢1.0 | O. (is) | 3.57 | ¢.(ii) | 0.120 |
| : ${ }^{(1)}$ | (01.0) | 0.81.1 | -1.42 | 7.0 :3 | 0.116 |
| 1() | (i7.5) | 0.9000 | ¢. 21 | 8.40 | 0. $10 \%$ |
| (6) | Silo | 1.068 | 6.19 | 10.8 | 0.099 |
| SO | S.8.0 | 1.175 | 7.97 | 1:3.2 | 0.08:) |
| 100 | 96.0 | 1.280 | 8.69 | 15.3 | 0.08 .4 |
| 120 | 102.0 | 1.36 | 9.66 | 17.5 | 0.078 |

Column 5 contains the value of a/r calculated from the function $\beta$ (column 4) by means of the tables that are to appear in the Physical Revicu. Column ( j gives the positive ion current density at the outsidesurface of the sheath. This is calculated from the current density on the electrode itself (column 3) by dividing the latter figure by $a / r$ (column 5$)$, since the ratios of the current densities at the outer and inner edges of the sheath must be inversely proportional to the respective radii.

An inspection of these tables shows that the current density varies with the voltage in exactly the manner predicted by the theory. Thus with a large diameter electrode, as in Table I, the variation of $i$ with voltage is slight, since the diameter of the sheath is relatively only slightly greater than that of the electrode. But with small electrodes, the variation in current with voltage mav be very considerable, as, for example, in Table IV, where the current increased 17.5 -fold when the voltage was raised from 10 to 120 .

The variation of the current with the voltage is, moreover, not a question merely of the diameter of the electrode, but depends upon the relation between this diameter and the intensity of the ionization. Thus, if $I_{+}$ is very small, the diameter of the sheath will be large, whereas if $I_{+}$is large, the sheath diameter will be smaller. With a cylindrical electrode of given diameter, the variation of the current with voltage is greater when $I_{+}$is small than when $I_{+}$is large. The experimental data are seen to be in agreement with this, as shown by comparison with Tables III and IV.

According to the theory outlined above, the values of $I_{+}$should be independent of the voltage. That this comes out to be the case is conclusive proof of the correctness of the theory.

Whith wires of such small diameter, or with such low intensities of imization that a/r is bery large (for example, more than about 5 ) Ho value of $I_{+}$is found to decrease somewhat with increasing voltage This variation of 1/ does not indicate any fature of the general theory as outlined, but is, in fact, to be expected, because of assumptions made in the derivation of the function $\beta(a / r)$. In this derivation it was assumed that the charged particles moving from an outer cylinder to an imner cylinder move exclusively in radial directions. When the ratio between the outer and inner cylinders is not very great, this assumption is well fulfilled under ordinary conditions, but, when the ratio between the diameters is large, even very small tangential velocities of the particles passing through the outer edge of the sheath cause them to form orbits about the small inner cylinder instead of striking it directly. The space charge effects are thus exaggerated and the resulting current becomes less than that calculated on the assumption that the motions are exclusively radial. These effects have been observed experimentally with pure electron discharges, and it is therefore not surprising that the same kind of effect should be observed, and should cause similar discrepancies, in the case of positive ion discharges.

The glass walls of a mercury are tube should become negatively charged by taking up electrons in exactly the same way as an insulated electrode. All positive ions which move towards the glass walls should therefore strike the walls and be absorbed, and an equal number of electrons should thus pass to the walls to neutralize these positive charges. Since the electron current density $I_{-}$must be several hundred times $I_{+}$, all but one out of several hundred electrons which move towards the walls must be elastically reflected.

A rather similar state of affairs also exists in the interior of the arc path, for, in general, electrons make elastic collisions with mercury atoms, whereas mercury ions, being of the same mass as mercury atoms, must lose on the average about one quarter of their energy on each collision. Since the mean free path in the ordinary mercury are tube is comparable with the diameter of the tube, each positive ion must reach the wall of the tube and be absorbed before it has made more than a very few collisions with mercury atoms. Under normal conditions it also follows that very few mercury ions move in a tube in a direction against that of the potential gradient.

The electrons, on the other hand, because of their clastic collisions with the mercury atoms and with the walls, must move in very crooked, or random paths, so that there must be nearly as many electrons moving against the potential gradient as moving with it

Stark* determined the current flowing between two small exploring electrodes in the path of a 3 -amp. mercury are in a tube 2.3 cm . in diameter. The first two columns of the following Table $V$ ' contain the data giving the current as a function of the voltage, this voltage being measured with respect to a third electrode carrying no current.
table V
3.1-ampere Arc in Tube 2.3 cm . Diameter. Collecting Electrode: $r=0.02 \mathrm{~cm} . ; \mathrm{L}=0.30 \mathrm{~cm}$.

| $1{ }^{\circ}$ | $\mathrm{Milll}_{i}^{i}$ $\mathrm{amp}$ | I | $\beta$ | $a^{\prime} / r$ | $I_{+}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.0 | 1.35 | 35.9 | 0.0463 | 1.046 | 34.4 |
| 6.0 | 1.42 | 37.8 | 0.0612 | 1.062 | 35.6 |
| 8.6 | 1.47 | 39.1 | 0.0787 | 1.079 | 36.2 |

It is seen that the currents vary with the voltage in the way expected from this theory, and these data indicate that the value of $\dot{I}_{+}$ in an ordinary mercury are is of the order of 35 milliamperes per $\mathrm{cm} .^{2}$ Thus, through a given cross-section of the tube, about 20.75 amperes of electrons flow in the direction of the potential gradient, and about 20 amperes in the opposite direction, the observed current of 0.75 amperes per $\mathrm{cm}^{2}$ being the difference between these two.

The presence of such large numbers of electrons with random motions explains why it is that a glow from an arc spreads into a

[^78]side amm a comsiderable distance, even if om current flows into the side arm.

The positive ions which strike the glase walls combinc with electrons, and must generate on the walls an anount of hoal which may be large compared to that carriod to the wells by the mercury atoms (simtherSchulze has attempted on calculate the temperature of the mercury vapor in a mercury are by measuring the heat which flows to the walls. Consiflering that the ionizing voltage of merary is 10.4 volts. whereas the energy of thermal agitation at room temperature corresponds to 0.0 .3 wolt it is clear that relatively few positive jons might cause considerable heating of the walls. As a matter of fact, the heating of the walls observed by Gunther-Schulze in typical instances corresponds to positive ion current densities of $10-20$ milliamperes per cm * striking the walls, which is of the same order of magnitude as that observed on negatively charged electrodes in the are.

Considerations similar to those outlined in this article have led to a new theory of the mechanism of the cathode spot, by which the thickness of the cathode layer is about equal to the mean free path of the electrons in the vapor above the cathode spot and is also determined by positive ion space charge, the positive ion current being of the order of magnitude of half the total current. The potential gradient at the surface of the mercury is thus found to be so great that it is probable that the electrons escape from it by being pulled out of the relatively cold metal by the intense electric field, in accordance with a theory suggested by Schottky. This theory will be described in more detail in a sul,sequent issue of this magazine.

# The Don Pedro Project of the Turlock Irrigation District 

13y R. WV. SHOMAKにK

St perintendent, Ele: 1 ricu. Depariment


#### Abstract

'The anthor who was responsible for the electrie design and construction and also for the organization of the electrical department deseribes the most interesting features of the Turlock irrigation district. Data which will be useful to all interested in irrigation projects are given. Eintor.


The Turlock Imrigation District was organized in ksis. under a law which had just been enacted by the California Legislature. giving the people the right to bond their lands for the purpose of developing a water supply for irrigation purposes.

The District comprises $1 \times \mathbf{x}, 000$ acres, lying between the Tholumne and Mereed Rivers. and extending from the foothills of the Sierra Nevala monntains to as far west as the San Joaguin River. The soil within this area is what is known as a sandy loam and is very porous, with the result that any rainfall very rapidly drains away, leaving the soil too dry for agricultural purposes. Without irrigation, practically nothing can be raised excepting


Fig. 1. Don Pedro Dam, North End,
Aug. 10, 1922
grain, and even with this crop a failure results unless the rainfall comes within welldefined limits. With irrigation, such crops as alfalfa, beans, corn, fruit, and grapes, grow very luxuriantly.

The first development of the District consisted of the construction of what is known as the La Cirange Dam, which is of the overflow type, and is approximately 127 feet high. It is used for the purpose of raising the water in the Tuolumne River high enough to enter a system of canals which have been gradually extended until at the present time there are $2.5)$ miles of main canals and 800 miles of secondary canals throughout the District. The flow in the Tuolumne River is extremely


Fig. 2. Generator Rotor on Power House Tramway, Jan. 8, 1923
varable an areage over 20 years showing a maximum of fos, 000 acre feet run off in the month of May, falling to $2 x, 000$ in September. The areage runoff for the month of July is 1sob,oot acre fect, but this falls to $3 \mathrm{sen}, 00$ in August.

The high water during the early summer is caused by the rapidly melting snow in the mountains and is usually all grone by the end of July. The physical chatacteristics of the water shed area prechude the retention of moisture to any extent: hence the sudden falling off of the river flow with the melting of the snow.

Is the agricultural season in the District extends through september, it is apparent that a need for additional water supply during
a dam at this point for the additional stomage of water, but it was mot matil the year of $1!921$ that conditions had shaped themsidves so that actual construction was logem

On August 23 , 192 1 , the first concrete was poured in the toe wall of the Don Pedro Dam; the last concrete in the structure being poured Mareh 15, 192:3. In this interval, there were placed in the dam 2st, (0) (ub) yards of orncrete, and $2 x, 500$ cubic yards of rock excavated in the dam site, also 1.30 , (o) cub io yards excavated in the spillway. The work of placing the concrete was, of course, interrupted by high water during the high water season of 1921 and 1922 , so that not much progress was made until March, 1!22. It then became necessary to conduct the work so that the dam


Fig. 2. Lowering 28 -ton Generator Rotor to Power House, Jan. 8, 1923
the months of August and September was soon felt. An attempt was made to overcome this difficulty by constructing a reservoir in the foothills, having a capacity of 48,000 acre feet. With the growth of the District, this storage became inadequate, and it was necessary to look to more satisfactory methods of increasing the water supply to the farms.

Fortunately, there existed in the mountains a short distance above the diversion dam a peculiar formation where two canyons branched out from the main river just above a very narrow gorge in solid rock formation. The early gold miners had noticed this locality, and it had taken the name of one of the early Argonauts and was known as the Don Pedro Dam site. The District had for many years contemplated the construction of
would be finished in time for the high water period in 1923.

The capacity of the dam proper is 260,000 acre feet, which can be increased to $2 x 9,000$ by raising a set of gates in the spillway, increasing the height of the water level 9 ft . The total height of the dam from the river bed is $2 S: 3$ feet; the length at the top 1000 feet, and the length at the base. is feet; while the respective thicknesses are 16 feet and 177 feet. The dam is of the solid gravity type, but is also constructed as an arch, with a radius of 674 feet.

With this amount of water in storage at a head varying from 130 to 2.50 feet, there exists of course an excellent opportunity to develop a considerable amount of power. The District, therefore, constructed a power house


Fig. 4. Detail View of the Switchboard Equipment, also shown in Fig. 6
Fig. 5. $5000-\mathrm{kv} \cdot \mathrm{a}$. Waterwheel Generator and Transformers


Fig. 7. Oil Circuit Breakers and Instrument Transformers
with an initial installation of three 5000 kv-a. machines of the vertical type, direct connected to turbines designed to operate with a head varying from 100 ft . to 240 ft . These machines are able to generate full capacity with a head of above 160 ft . With an efficiency of not less than si3 per cent thronghout the entire range. The greatest efficiency of 90.1 occurs at a head of 120 feet and the minimum cfficience at the maximum head of 240 feet; under which cond tion of course the efficiency is of least importance.

Provision was made in the construction of the dam for the future installation of two more units. The maximum amount of power that could be generated at Don Pedro is somewhere in the neighborhood of $60,000 \mathrm{kw}$.. but this would be arailable only over a part of the year. The probable maximum economic development will be in the neighborhood of $35,000 \mathrm{kw}$. It is not possible to estimate accurately what this maximum development will be, owing to the fact that the irrigation requirements, which must be given precedence on the water delivery, are somewhat of an unknown quantity, for the reason that prior to the construction of the dam the farmer had a tendency to use more water on his land than he knew was good for it in an effort to increase the length of the irrigation season. It is probable that the effect of the dam will be to increase the irrigation season without a corresponding increase in acre feet of water applied to the lands.

The amount of water available for power during the low period of the river is of course dependent on how much water is withdrawn from storage between the end of the high water period and the end of the irrigation season.

Furthermore, it will be possible to develop a large pumping load in sections of the district which have an elevation too great to receive the benefits of gravity irrigation, which load will be coincident in time with the demand for water; hence, for these reasons, the ultimate development is, at this time. uncertain.

As the laws affecting irrigation districts have been modified so as to permit such districts to go into the generation, distribution and sale of electric power, where such power can be generated in conjunction with their hydraulic development, the people of the Turlock District by an overwhelming popular vote decided to distribute the power to themselves rather than sell it wholesale to the power companies.

As the City of Tarlock does not colow terminal freight rates, the probability of developing a large manufacturing load is rather remote; so the marke for the bon Pedro power seems to lie in the development of the use of electrical energy in the home and on the farms. The most obvious outlet along these lines is, of course, the use of the electric range and water heater.

It would be hard to imagine a more promising field for this development, as the cost of fuel is very high; wood selling for $\$ 27.00$ a Califormia cord and coal at $\$ 18.00$ a ton. The climatic conditions are also favorable to this, as the winters are not excessively cold, the thermometer rarely going as low as 32 deg. F., and the summers are quite hot.

The District is therefore proceeding along the lines indicated in developing the use of electrical energy, and in so doing, it has adopted a "Readiness to Serve" system of rates as being the most logical method of encouraging the use of electrical energy under the conditions existing within the District.

It must be borne in mind that the dam was erected and that the cost was justified from the standpoint of water storage and development, and as water must be passed through the dam for from seven to eight months a year, the cost of power within that time can be the only actual cost of operation of the power plant, fixed charges of course included. It is probable that under all conditions, water will have to be wasted through the irrigation outlets, hence the cost to the District of maintaining the consumer during these months will be practically independent of the amount of electrical energy that he uses. The cost of carrying a consumer will be entirely in the cost of transporting the energy to him, and it is for these reasons that the Readiness to Serve method of rate making is the fairest to both parties. To accomplish this, a rate with a relatively high service charge coupled with a relatively low energy charge has been developed to meet the local conditions.

In addition to the use of power for lighting, cooking, etc., there exists within the District a very unique and serious problem, which can be most advantageously solved by the use of pumps using electric power. This is the drainage problem, and is caused by the fact that the continual use of water on the lands of higher elevation in sufficient quantities to meet the agricultural requirements results in the gradual flow of this water down towards the lands of less elevation, with the result that

Whese lathets beoonte bow wer for satishatory development In many areas within tho District this fow has catased the water plathe to rise so high that some sections are absolately matit for agriculture and have to be withdrawn fom the taxable areas, thereby entling afl the revernte of the Distriet at its sonece - Itempts have beed made tomere this problem he the construction of what were known as drathage canals, which were deep canals cut inte areas that wore becoming flooded; but these ditehes did not prove to be an entirely sat isfactory solution of the problem.

The District hat installed in the affeeted lands quite a number of turbine jumps, driven by vertical electric motors, which receive their power from the Don Pedro System. Although these pumps have only been in operation a few months, there has been in their localities a marked lowering of the water plane, even to the extent of drying up some small lakes which existed near the location of some of the pumps.

It is contemplated that eventually there will be over one hundred of these pumps, and it is expected that the use of 3.500 acres of land will be reclaimed by this method; also, what is more important, that there will be no further increase in lands withdrawn from taxation on accomnt of high water plane. The water pumped from these wells is diverted into the irrigating ditches, where it can be used over again for further irrigation.

It is quite probable, in the future, that many farmers will prefer to pump their water electrically, rather than make use of the free water supplied by the District's canals; for the reason that by having a pump they will be able to have the water exactly when their crops require it. The gravity water is only
available at certain perioxls, as cach trace of land must lake the water in tarn. In this conneretion, it is interesting to note that from (10) 1020 times as much water can be furnished he pumping electrically as can be supplied through the canals, for the reason that the loss from evaporation and seeprage between the dam and the mitimate consumer is in the neighborhood of $\overline{\text { of }}$ per eent when supplying water to the land through the canal system. As this is approximately the orer-all efficiency between the power plant and the electrically operated pump, the total water supplied is in proportion to the ratio existing between the height the water has to be pumped and the head of the water on the generator turbines.

As the average head at the dam will be in the neighborhood of over two hundred feet, and the average pumping head is between ten and twenty feet, the reason for the above ratios is apparent.

The use of electrically driven pumps would make it unnecessary to devote several thousand acres of land to canals as at present. While it is not probable, however, that the District will ever reach a point where the canals will not be used at least to some extent, yet from the requests for power for pumping that have been receiverl to date, it is apparent that many farmers are going to make use of the more expensive method of electric pumping, which they can use at any time, rather than depending on the ditch water, which can be used only on schedule.

The dam was constructed under the direction of Mr. R. V. Meikle, Chief Engineer of the Turlock Irrigation District, with Mr. A. J. Wiley, of Boise, Idaho, as Consulting Engineer.

# Review of the Lamp Report of the National Electric Light Association 

By (ieorge F. Morrison<br>Vice-preshent, General. Electra Company


#### Abstract

On several previous occasions we have reviewed the Lamp Committers report of the National Electru Light Association, which is always an interesting document. The review of this year's report shows that we are still progressing rapilly in the direction of standardizing and of giving the customer more light for it dollar.-Emitor.


The Lamp) Committe of the National Electric light Association each year, since 1908. has submitted a report to its anmual comeention containing a great deal of interesting data regatding the developments of electric illuminants during the previous year. The latest report, giving data on the progress in 1922. contains a voluminous amount of statistics on incandesont lamps during the sixteen years, $190-1920$ inclusive.

Total Incandescent Lamp Sales, 1907-1922
In 1907, the total sales of incandescent lamps (excluding miniature lamps) in the United States amounted to about sixty-five million lamps. The tungsten filament lamp had just appeared on the market and the tantalum lamp the previous year, their sales however then being a negligible proportion of the total. In 1922 , the total sales were 20.3 million lamps, over three times that of $190^{-}$

This increase in lamp sales, however, does not fullv indicate the growth of the use of light. During the sixteen-year period, the demand for the carbon filament lamp decreased until it is now practically a negligible item and the tungsten filament lamp now constitutes orer $9 x^{1}{ }_{2} 2$ per cent of the total demand. The candle-power of the average size of tungsten filament lamp sold in 1922 is nearly four times that of the average carbon filament lamp of 1907 , so that the aggregate candle-potver of the lamps sold in 1922 is about twelve times that of 1907 . This is diagrammatically shown in Fig. 1.

The tantalum lamp never became a large factor and disappeared from the market in 191:3 oring to the greatly superior efficiency of the tungsten filament lamp, even though the latter was a comparatively fragile lamp until the introduction of drawn tungsten wire for its filament in 1911. An improved carbon filament lamp. known as the metallized carbon or Gem lamp, was first marketed in 190.5. This lamp was largely used by central stations as a free renewal lamp. Its
sales increased until it reached a maximum proportion of about half of all the carbon filament lamps sold, then falling off and tisappearing from the market in 191s

## Average Watts and Efficiency

The average wattage of the lamps soll decreased slightly during the first six years of the sixteen year periocl, from about 53 to th and then gradually increased on practically in in 1929.2 The decrease was due to the replacement of earbon with tungsten filament lamps of slightly less wattage although of much higher candlepower. The later increase was the to the gradually increasing use of the gas-filled tungsten filament lamps which appeared in 1913, and which conld at first be made only: in the very high wattage sizes. It is the writer's belief that this shifting in the average wattage does not indicate a similar change in the amount of current used he the average central station consumer. The consumer not only has used a higher average candlepower lamp but has been burning it for longer periods, so that the average sales of current per customer has probably increased appreciably since 1907 .

The efficiency of an incandescent lamp used to be expressed in "watts per candle." This term is unfortunate as an increase in efficiency would be indicated by a decrease in watts per candle. Furthermore, the candlepower of a lamp usually meant its "mean horizontal" candle-power, which is the average candle-power a lamp gives in a horizontal plane. The "mean spherical" candle-power, which is the average candle-power a lamp gives in all directions. is a better measure of the total light it gives because the ratio between the mean horizontal and mean spherical is different in different lamps. This ratio depends on the shape of the filament and is somewhat different for the different sizes of tungsten filament lamps which have ratios very different from that of the carbon lamp

In order to get away from the incomplete term＂candle－power，＂the term＂hamen＂ was atopted．One mean spherical candle－ power is equivalent to practically 12．क力 lumens，and the ofd 16 e－p．lamp gave patac－ tically 160 lumens．A corresponding change was made in the torm expressing efficiency， a reciprocal expression＂lamens per watt＂ being used，so that an increase in efficiency is shown ly an increase in lumens per watt．

The increase in candle－power and watts of the arerage lamps sold in 1907 and 1922 has alreaty been stated，so the efficiency of these lamps，expressed in the modern term of lumens per watt，has increased from less than $31 / 2$ to over $111 / 2$ ，an increase of nearly two hundred and fifty per cent．

## Voltage of Lamps

There are several groups of voltages for which tungsten filament lamps are regularly made．In many cascs lamps can be had，if desired，for each individual voltage within the range of that group．In addition，lamps are made for use on street series circuits which are rated in amperes instead of volts．

## 115－volt Group

The most popular voltage is the so－called 115 －volt group which covers over SS per cent of the total demand．Originally lamps were regularly made in this group for each individual voltage between 100 and 130 ， and a demand for such individual voltage lamps was fostered．This was necessary in the carbon lamp days as it was impossible to predetermine the exact voltage of every carbon lamp made．With the development of the drawn tungsten wire filament in 1911 it became possible to predetermine exactly the voltage of such lamps and a movement was started to eliminate the demand for many of the voltages between 100 and 130 as the use of carbon lamps decreased．

One voltage would，of course，be an ideal situation not only from the lamp manufac－ turers＇standpoint but also from that of the consumer as he would then be able to get better delivery than is possible with a mul－ tiplicity of voltages to be supplied．The 115 －volt lamp is now considered the standard， but 110 －and 120 －volt lamps are known as recognized departures from the ideal stand－ ard．These three voltages in 1913，when voltage standardization was first started， constituted less than half of the $100-130$－volt group．In 1922 they constituted considerably over 90 per cent．This percentage will in－
erease，as the lamp report shows that nearly 97 per cent of the total population in the United states that is served with current is supplied at one of these three voltages， nearly half of which is 11.5 volts．

The increase in the demand for the standard wolages during the years 191：3 to 1922 inclusive is shown in the diagram，Fig． 2. Excluding the present j per cent demand for $12 \overline{5}$－volt lamps，about one－half of the re－ maining $31 / 2$ per cent demand for odd voltages


Fig．1．Incandescent Lamp Sales，1907－1922
is for the 112 －volt lamp．While this is a small percentage of the total，it means，how－ ever，that over two million 112 －volt lamps were sold in 1922.

The lamp report again calls attention to the fact that the use of 112 －volt lamps should be discouraged．In practically all cases their use is a continuation of the old practice of burning 112 －volt lamps on $110-$ volt circuits．This practice was adopted in the early days of the tungsten filament lamp to compensate in lamp life for the fragility it then had．With the present sturdy drawn wire filament this practice is no longer
warranted, as it entails a sacrifice of candlepower, wattage and efficiency.

## Other Voltage Groups

The 230 -volt group in 1922 constituted 4 per cent of the total. This percentage is less than in former years and indicates that lighting installations on 230 -volt circuits, usually power circuits, are being changed over to 115 -volt lighting circuits. Such a change is most desirable, as not only are the 115 -volt types of lamps more readily available on account of their large demand, but they are lower in price and more efficient than 230 -volt lamps. Practically all the demand in the 230 -volt group is for the four voltages: $220,230,240$ and 250.

The 30 - and 60 -volt groups constitute about $31 / 2$ per cent of the total, most of the demand being in the 30 -volt group. Lamps of these voltages are generally used in gas-engine driven electric plants for rural homes beyond the reach of central station circuits and for illumination in railroad coaches and Pullman cars that have a storage battery which is usually kept charged by a generator driven by a belt from the car axle.

There is a so-called street railway voltage group which constitutes two per cent of the total lamp demand. These lamps are similar to the 115 -volt group, but are designed for series burning, each size of lamp, irrespective of its voltage, being made for a given amperage. They are supplied for use, five in series, on $525,550,575,600,625$ and 650 volts.

The remaining miscellaneous voltage groups cover less than one per cent of the total demand. They include such lamps as $111 / 2-$ volt sign lamps, which are burned on transformers reducing the 115 -volt alternatingcurrent circuit to one-tenth of this pressure, and 275 -volt lamps used in mine lighting service.

## Street Series Group

About $11 / 2$ per cent of the lamps sold are in this group. This does not indicate the proportion of lamps used for street lighting as many lamps of the 115 -volt group are used on multiple street lighting circuits.

The standard series circuit for incandescent lamps is 6.6 amperes and probably 70 per cent of the lamps in this group are burned on this circuit. This is because the efficiency of 6.6 -ampere lamps of the ordinary sizes is
greater than those made for other currents. These 6.6 -ampere lamps constitute 60 of the 70 per cont. The high candle-power sizes, which constitute over 10 per cent of the group, are more efficient if made for 20 amperes, so these lamps are usually operated on compensators to permit their use on 6.6-ampere circuits.

The other series lamps are 4 amperes covering 9 per cent, $51 / 2$ amperes covering less than 8 per cent and $71 / 2$ amperes covering 12 per cent of the demand in the street scries group. It should be noted that the so-called $4-, 51 / 2$ - and 6.6 -ampere luminous or magnetite arc rectifier circuits supply a current whose mean effective heating value is different from the figures given. For this reason special lamps are made for use on these circuits, being labeled the nominal amperes of the circuit, but actually made for the heating value of the current. For example, the 4ampere lamp for General Electric rectifier circuits is actually made for 4.2. amperes though labeled "4 Amp. G.E. Rect." The 4 -ampere lamp for usc on Westinghouse rectifier circuits is actually made for 4.1 amperes though labeled " 4 Amp. West. Rect." In addition, these series lamps for use on rectifier circuits are designed to operate at a poorer efficiency than regular series lamps operated on constant current transformers in order to compensate for the great surges in current which occur on rectifier circuits. For this reason the vacuum tungsten filament lamp is recommended unless a surge arrester is used, as the filament in the gasfilled lamp operates closer to its melting temperature than the filament in a vacuum lamp.

There has been a considerable increase in the size of the average street series lamp used during the past sixteen years. Within a short time, about two years after the tungsten filament series lamp appeared in 1907, the carbon and Gem series lamps previously used were withdrawn from the market. In 1907 the average candle-power was 32 , which, converted to the present lumen rating, becomes practically 320 lumens. This gradually increased to 600 lumens in 1913 when the gas-filled tungsten filament series lamps appeared. This made it possible to make such an efficient high candle-power incandescent street lighting lamp that they soon replaced the carbon arc lamps previously used. This demand greatly increased the average size of the lamps sold, the average lumens rising to over 1600 in 1917. In

1!2!2 it was wor 1700, the changes being illustrated in ligg :3.

The smallest street series lamp regularly listed is foo lomens, the lamps being made in bight sizes un) (o and including 2.),000 lemens. Therestill is a demand, aggregating


Fig. 2. Standard Voltages, 1913-1922
about $121 \%$ per cent of the serics group, for lamps of less than 600 lumens. The lamp report again refers to the undesirability of using such small sizes, as lamps producing less than (i00 lumens are inadequate and unceonomical under ordinary street lighting conditions, urging the substitution of larger sizes in place of the great number of small sizes mow in use.

## Demand of Lamps by Types and Sizes

While a little over 20 per cent of the total number of lamps sold in 1022 were of the gas-filled type, their aggregate wattage was over 44 per cent and aggregate candlepower over is per cent of the total. This is on account of their general average wattage being higher and efficiency greater than that of the racuum type of lamps. This means that nearly half the current sold for lighting purposes and over half the light used is by means of the gas-filled lamp whose demand is one-fifth of the total number purehased.

The most popular of the gas-filled lamps are the $\overline{5} \cdot \mathrm{~F}$ - and 100 -watt sizes, the demand for each of which is about $6 \frac{1}{2}$ per cent of the grand total of all lamps. The most popular of the racuum lamps is the 40 -watt, whose demand is 19.3 per cent; next comes the 2.)-watt having a demand of 18.6 per cent; then the $\mathbf{5})$-watt, constituting 1.5 .5 per cent
of the total demand for all lamps. The so watt lamp has been increasing in popularity each year since it was put on the market.

There are now six sizes of vacuum lamps regularly made for standard lighting service, 10, $15,2.5,40,50$ and (30 watts. In addition there is another 10 -watt lamp supplied in a small butb generally used for sign lighting. It seems unnecessary to have so many different sizes for standard lighting purposes, so it is hoped that the recommendation suggester awhile ago, that the demand be concentrated on but three sizes, 15, 25 and .0 watts, can be accomplished in the near future. If a 10 -watt lamp is desired, this lamp in the small bulb can be used. The demand for larger sizes is now well cared for by the $75-, 100-, 150-, 200-, 300-500-, 750-$ and i 000 -watt gas-filled lamps.

The above mentioned lamps cover a great majority of the total demand, but when it is remembered that they are regularly supplied in three voltages, some of them all frosted or colored, usually the smaller sizes for decorative purposes and some bowl enameled, usually the larger sizes for industrial lighting, the total number of individually different lamps becomes very great, amounting to about a hundred items. In addition, there are various sizes of lamps for sign lighting, country home, projection, floodlighting, mine lighting, street railway, train lighting, street series and 230 -volt services so that the number of individually different lamps regularly listed in lamp manufacturers' catalogues


Fig. 3. Average Lumens of Street Series Lamps, 1907-1922
aggregate over five hundred items. Furthermore there are a lot of special lamps, regularly used by individual purchasers for some device or special service of theirs, that increases the number of items to more than one thousand.

## Lamp Developments

"Sprased" colors hate heen devoloped Which ate very satisfactory The coloring material is sprayed on clear lamps, is weatherproof and does not fade. These lampes are muc! loss expensive than those with mathral colored ylass bullos, which usually have to be made 10 order, and more grompt delivery can be mate as the sprated eolor can be
 with typical rellectors lhis is mot the (are and ath all frosted lampl gives much lownor amel more desirable restalts in all cäses

## Pric: Changes

On April 1. 192.2. a readtuctment on pricen was made on Mazod lamps N.azo. IS lamps were reduced about lol 2 per remt amel \azas


Fig. 4. Price Chart of Mazda Lamps
quickly appliad to the clear lemps in stock. There are four colors supplich which are a standard shade of red. blue. green and yellow
"All frosted" lamps are now being supplied where frosted lamps are ordered. At few years ago "bow frosted" hamps were alen quite commonly used, but in the desire to standardize on but one finish the use of bow frosting is now discourased. The bowl frosted lamp has been used in the past because of the belief that a considerable amount of light would be lost by the use of

C lamps about i) per cent ()n ()ethier 1. 192?. Mazda C lamps were further reducerd about 20 per cent and on Nay 1, 1!2: $\%$ both Mazna B and © lamps were aqain reduced. averaging about in per cont. The prices of Mazda B lamps are now below the prewar level of 1914 and the jrices of Mazda C lamps are the lowest in the history of the industry:

Fig. 4 shows the dates of introducturn of the more important sizes of Mazda lampe in the 11.5 -volt group, their original list prices and changes to date.

# Glass and Electricity 

By I. $A$. Connor

General. Electric Combany, pittsburgin, Pa.


#### Abstract

There is a great ficld for electricity in the glass industry. From the very early days the glass industry has been conservative and even at present, in most glass factories, manual operation predominates. The anthor describes the different processes in making plate glass and the application of electric motors to these processes.-limtor.


The art of making glass is one of the oldest in the work. Men have slaved in developing the industry for six thousand years in order that you might see the world through your plate glass window or find yourself reflected llawlessly in your mirror. Someone has said that the invention of glass was an accident into which a group of Phoenician merchants stumbled while cooking on the sand in the dim days of antiquity. According to history the Phoenicians beached their galleys on the coast of Palestinc. When they had built their camp fires and tried to set up their cooking pots to prepare a meal they failed to find any stone in that desert country, so the pots were set up on cubes of soda from their cargo. The heat of the fires melted the soda and fluxed it with the sand and to their amazement they beheld a clear fluid forming as a result of the fluxing-glass.

Now here is where science tells us something: it says that to produce a fluxing of sand and soda a heat of 2600 deg . F. would have been necessary and that cooking fires didn't get that hot even in hot Palestine. You say you found glass in the Temples of the Fourth Dynasty, 4000 years B.C., eh? Where did those Egyptians get their 2600 deg. F.? Quite unable to answer, a deep blush of humiliation mantles the brow of history.

Getting down to more modern times it is stated that the first glass factory in the United States was built in the woods near Jamestown, Va., in 1608, and that the chief product was glass beads. Afterwards in many places bead factories sprang up proving a cheap and profitable kind of mint, as great profit was made by trading with the Indians and it is stated that one was established near Hanover Square, in New Amsterdam, to give the Dutch burghers a chance to recoup their fallen fortunes after paying $\$ 24.00$ for Manhattan Island.

The plate glass industry, as we know it today, has changed very little in principle since about 1690 when it was first established.

[^79]Stepping into the present this article is primarily to describe the plant of the American Plate Glass Co., at James City, Pennsylvania.*

This is a very modern plate glass factory and every power requirement in this complete industry is met by electric motors ranging in size from one to $400 \mathrm{~h} . \mathrm{p}$. in approximately 135 units, 97 per cent of the $10,652 \mathrm{~h} . \mathrm{p}$. connected load is developed by G-E motors. All of the alternating-current motors are 550 volt, 3 -phase, 60 -cycle, except those in the pump house, some distance away, which are 2200 -volt, 3 -phase. The direct-current motors are 125 -volt.

Plate glass is made from a mixture consisting of pure silica sand, soda ash, limestone, salt cake with small quantities of arsenic and charcoal and a proportion of cullet or scrap glass being remelted with the batch. The mixture is then placed in clay pots and melted in gas fired furnaces. Modern gas fired furnaces will usually accommodate twenty pots, and eight such furnaces are in use at this plant.

In making glass the mixture is first dumped into batch wagons which haul it to filling machines which are placed near the furnaces. The filling machine is in the form of a bin which moves along on wheels and is propelled by a small motor. In front of each furnace an operator opens a gate in the filling machine which allows some of the mixture to fall into a ladle and this, in turn, enters through the furnace door and delivers its charge to clay pots. The pots in the furnace are already heated to approximately 2000 deg . F. and after the mixture has melted down they are refilled several times in order to make up for shrinkage in the batch. The pots, with the mixture, are then subjected to a temperature of approximately 2600 deg. for from 14 to 15 hr ., during which the melting and fusing process goes on. Just before the pots are ready to be taken out, the temperature is reduced to approximately 2000 deg. F. At this temperature the batch is suitable for casting. All temperatures are regulated by recording pyrometers. When ready for cast-
ing, the pots are removed from the furnace be special tongs carried on an overhead traveling crane and are delivered to the teeming crane which grasps them in jaws; they are held tight by a hand-operated "screw-down."

Considerable care is required in making the clay pots, and as there is no machine that will mould them successfully it is necessary that this be done by hand. Clay is the only practical material as the pots must stand a temperature of approximately 2700 deg. F . Up to a few years ago the only practical way


Fig. 1. Motor-driven Mechanism for Slowly Pushing Glass Melting Pots Through a Preheating Kiln
of making a smooth velvety surface free of air pockets was by tramping the clay with bare feet. In these modern times a pug-mill driven by an electric motor does this work. Twelve to sixteen weeks are required for moulding and drying the pots and after all this tedious work the pots are good for not more than 20 trips to the melting furnace. Each pot is 43 inches in diameter by 31 inches deep and holds 1800 lb . of glass. The pots are dried slowly and then preheated in a furnace kiln and pushed through this kiln by means of the motor-operated mechanism shown in Fig. 1.

The filled pot after being taken from the furnace and while still in the clutches of the teeming crane has the bottom cleanerl by letting it rest slightly on revolving steel brushes which knock off all loose pieces and the sides are also thoroughly blown off in order to remove any foreign substances or matter which might fall on the casting table.

After the molten glass has been skimmed by means of copper tools, which are worked around the top in order to remove any impurities, the pot, still in the jaws of the tceming crane, is taken to the opposite side of the $131 / 2 \mathrm{ft}$. by 22 ft . flat surface steel casting table. The top of this table has already been covered with a very thin layer of fine sand to prevent sticking and chilling,: the contents being poured or "teemed" in front of a huge knurled cast iron roller. At the same time the teeming crane is given a direct forward movement and the contents poured along in front of the roller. The roller, which is 26 inches in diameter by 15 ft . long and weighs approximately 13 tons, is then started in motion, being pulled by a chain connected to a motor. Crane type direct-current motors are used on the special four-motor teeming crane.

A good view of the teeming crane, the casting table and a portion of the molten plate glass while the roller is being passed over it can be seen in Fig. 4. The roller at the end of its travel mounts on wedges placed on either side which raises it slightly above the glass and allows the plate to pass under it. After the plate glass has cooled for a few seconds it is then pushed from the table into the first annealing oven. These pushers or stowing tools operate in regular successive movements and push the plate glass, after certain intervals of time, into five separate ovens which have a graded downward temperature, the first being 1200 deg . F. From the fifth oven the glass is pushed on to conveying rods into a 300 ft . leer, and still through gradually reducing temperatures moves along the leer until it comes out at the other end, $31{ }_{2}$ hours afterward, annealed and cooled to approximately 190 deg. F. While the glass is in the leer it is carried along on leer rods in steps of approximately 15 ft ., the operation being by semi-automatic motor control. The interior of the leer is lighted by arc lamps. When the glass leaves the leer it is then trimmed and examined in order that pieces having large defects such as "stones" may not be put through the expensive process of grinding and polishing. Ḅ̣ means of
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'The ammaling leor amd also sexoral of the

 tahle (which is 2s ft . $\mathrm{f}_{\mathrm{i}} \mathrm{in}$. in diameter and werglis apmoximately 1.5 toms) two grinding rumbers or disess ome of large diameter Weightag itons, and one of smatler diamcter weighing is toms, are bowered on the plate glass. The mater surfaces of these rumbers are corered with bricks like blocks of east iron, eath block weighing apporimately I:3 11). when new. The two manners revolve in the same clicection as the table and varying grades of sand and water are then plated mpon the glass.

These rumners receive their motion entirely from the friction prodnced between them and the plate glass and are not revolved by any external sounce of power. Due to the roughness of the glass at the beginming of the grinding process the table revolves at about 1.5 r.p.m. and after this period (approximately five minutes),


Fig. 3. Load Curve on a Motor Driving a Grinding Table Such as Shown in Fig. 2; Full Scale is 400 Kw .
glass were designed by J. W. Cruikshank, Plate Glass Engineer of Pittsburgh.

The plate is laid on the grinding tables in ghass stucco, a mixture of grpsum and lime. which is quiek drying. This composition holds the glass on the talle, but in order to further avoid accidents due to centrifugal force, wooden pegs are also placed around the miter edges of the plates to prevent slippage.
it is inereased to the full speed of $2(6$ r.p.m. Fig. ㄹ shows the table revolving with the two rumners fairly distinguishable on top. The motor shown at the right of this photosraph supplies the mixture of sand and water by means of a centrifugal pump. The grinding process is finished by use of different grades of emery being placed upon the plate glass. This emery is ground and pulverized


F:g. 4. Teemang Crane. Casting Table and Roller


Fig. 6. Polishing Table, 400-h.p. Slip-ring Induction Motors


Fig. 5. Grinding Table. : 00 h.p. Stip-ring Induction Motor


Fig. 7. Po'ishing Rouge Mixing Tanks with
Mctor driven Agitators
in a ball mill which is operated by a fo-h.p. motor. The huge grinding tables are each driven by a 300 -h.p. slip-ring induction motor ruming at $51 / 4$ r.p.m. synchronous speed. A typical load curve on one of these grinder motors is shown in Fig. 3, the full scale being 400 kw . One of these motors is shown in Fig. 5.

Approximately one hour is required for grinding each side of the glass and after the plate has been ground to a perfect plane on one side and being left on the same table, it is then taken to the middle yard, where the plaster joints between the plates are raked
ring induction motor operating at $514 \mathrm{r} . \mathrm{p} . \mathrm{m}$. synchronous speed. Several of these motors are shown in Fig. 6.

A typical load curve on one of these polishing motors is shown in Fig. 8, the full scale being 400 kw .

The red rouge for polishing is constantly agitated and is mixed in oblong tanks which permit of a thorough mixing and three such agitators are driven by a $71 / 2$-h.p., 720 -r.p.m. induction motor as shown in Fig. 7 .

All of the seven grinding and eight polishing machines are rope driven as shown in the photographs, except one polishing machine


Fig. 8. Load Curve on a Motor Driving a Polishing Machine; Full Scale is 400 Kw .
out, any broken plates removed, unbroken plates substituted, new plaster run in between all the joints, and the plate and the table are then taken to one of the polishing machines. Each polishing machine is equipped with four runners, and attached to each runner is a number of circular blocks approximately 18 inches in diameter and to the under side of each a felt pad is attached. These felt blocks bear against the surface of the glass. Red rouge or roasted sulphate of iron held in suspension by wate1 is then applied for polishing. The polishing tables revolve at approximately 22 r.p.m.

After an hour and twenty minutes of this and a repetition of the whole process for the opposite side of the plate all that man has been able to learn in sixty centuries to make a perfect plate glass has been done. Each polishing table is driven by a $400-\mathrm{h} . \mathrm{p}$. slip-
which is chain driven as will be seen in Fig. 9 . The American System of rope drive is used and has given very satisfactory results.

After the glass has been given a fine polish it is washed off and taken to the cutting tables, where it is handled by a special type crane as seen in Fig. 10, which was designed particularly for this class of service. The plate glass is then carefully examined, all defects noted, and cut into the proper sizes and placed in the wareroom from whence it is packed and shipped.

Each grinder and polisher motor is controlled individually from a point just in the rear of the grinder and polisher machines. After years of experience it was decided that this was the logical place as it gives each operator instant control of each machine. The control consists of a hand operated master switch and an automatic control panel




Fig. 13. Motor-driven Hydraulic Triplex Pumps for Raising and Lowering the Fieavy Grinder Disks


Fig. 15. Synchronous Motor-generator Set for Supplying Direct
which provides for low speed for a few minutes at start until full speed is desired.

Quantities of air for raising sand to the grinder tables and for use in the casting hall in blowing off the casting table and opening furnace doors, etc., are supplied by motordriven air compressors, one of which is shown in Fig. 11. A similar motor-driven air compressor for the same purpose is shown in Fig. 1 .

In addition to these drives, alternating-corrent motors are used to operate the fire pump, plaster pumps, plaster mixers, carpenter shop, polisher agitators, centrifugal pumps for sand graders, centrifugral pump for emery graders, emery grinders, sand hoist, coal crusher, coal conveyor, casting room pumps, casting room fan, gas producers, machine shop and motor-generator sets.


Fig. 17. Section of a Curve-drawing Kilowattmeter Chart Showing the Typical Load of the Plant.


Fig. 18. Section of a Curve-drawing Power-factor Chart Showing the Power-factor of the Plant

The heary circular iron runner discs, over each grinding machine, require approximately 600 lb . of water pressure for raising and lowering them on the glass grinding tables, and this pressure is supplied by an hydraulic accumulator which in turn is supplied with water through motor-driven triplex pumps as seen in Fig. 13. One of these pumps is driven by a ?-h.n. squirrel-cage motor, and the other by a $\overline{\text { o }}$ (0-h.p. squirrel-cage motor.

Great quantities of water are required in a glass factory particularly for the grinding tables and for washing off the glass and the floors. This is supplied by three 100-h.p., 4. ()-r.p.m. slip-ring induction motors driving triplex pumps, one of which is noted in Fig. 14.

The entire direct-current motor load of the plant is taken care of by one 125-k.w., $1200-$ r.p.m., 12.j-rolt compound wound synchronous motor-generator set shown in Fig. 15, although a $125-\mathrm{kw}$. induction motor-generator set is held in reserve. Direct current is used. for the motors on the two transfer cars which handle the grinding and polishing tables, the power house and casting room crane's the teeming crane, the special wareroom cretas and the two main leer motors.

A 28 -panel switchboard controls the different circuits throughout the plant. An $\mathrm{e}_{1}$. view of this board is seen in Fig. 15. In order to show at a glance just how the plant is operating, the incoming line panel is equipped
with voltmeter, ammeter, kilowathour meter, fregucucy meter, power-fater meter, curve-lrawing kilowattmeter and chrve-drawing power-factor meter. 'The companys, at presemt, purchases its power, athough in ease of emergency they are prepared to start 11 , their private gencrating plant and generate a large portion of their requirements. A donble hus system with double-throw switches permits the operation of any motor cirenit cither with purchased power or from their private sencrating plant.
'The gencrating plant consists of three Tsl-kv-a. 150-r.p.m., and three $500-k v-a .$, 1s(0-r.p.m., ( 000 -volt, 3 -phase, (60-cycte General Electric gas engine driven generators. The power is purchased from the Keystone Power Corporation and is transmitted at 44,000 volts, 3 -phase, through two lines from the main generating station at Ridgway. A $6000-k v-a$. bank of transformers steps the voltage down to 550 . The glass plant is in operation 24 hours a day, except Sundays, and the load over the entire period is well represented by the load curve taken from the curve-drawing kilowattmeter, as indicated in Fig. 17.

About two years ago the power-factor of this plant varied between 70 and 80 per cent.

Since power is purchased on a basis which provides a penally for low power-factor, it Was decided to prat in a 1500-kv-ia., 900-r.p.m. D.0)-volt synchronous condenser for corrective purposes and since then the power-factor avorages more than 9.j per cent, as indicated by the power-factor curve in Fig. 1s. The synchronous condenser with its direct conneeterl exciter is shown in Vig. 16 .

The condenser has proven to be a very profitable investment and has been paying karge dividends by maintaining a high powerfactor.

This plant has recently been purchased by the Durant interests, it being the first independent plate glass factory to change hands in several years, and we believe that their decision to take over this plant rather than any other of the independent glass factories, was due largely to the completeness with which it was electrified. The present 60 -cycle equipment has been in operation for about three years, although they had operated their plant for approximately ten years previously by 25 -cycle motors of various makes.

This plant has probably the most complete modern equipment of any of the plate glass manufacturing concerns to-day and the quality of the glass produced is unexcelled.


# The Origin of Ions in the Unsustained Glow Discharge 

By Prof. K. T. Compton<br>Palmer Physical Lab., Princeton University

and

T. E. Foulke

Research Division, Edison Lamp Works


#### Abstract

This is our first contribution from the new Research Division which was established at Harrison a few months ago. The article shows that there are sufficient residual ions present in any gas to start a discharge when a sufficiently high voltage is applied. Attention is drawn to the application of the Einthoven galvanometer for registering minute currents for very short intervals of time.-Editor.


## Introduction

In the unsustained discharge using a cold cathode it is of interest and importance to know the origin of the initial ions. It is known that electric fields which are strong enough to produce a spark or glow discharge in a gas are quite incapable of extracting ions from the metal clectrodes or of causing the formation of ions from molecules.

To account for sparking in a gas Townsend developed a theory in which any free electrons present in the gas may be multiplied by collisions with gas molecules. The theory postulates that the energy at impact, due to velocity gained in the applied field, must be great enough to cause ionization of the molecules. With sufficient voltage between the electrodes, both electrons and positive ions may ionize at collisions until the current density becomes great enough for the discharge to occur.

The general belief is held that a few ions are continually being formed everywhere in the earth's atmosphere, and that the number of ions formed will equal the number lost by recombination over a sufficiently long interval of time. If the original ions are produced in the gas in a haphazard fashion, as would be expected if due to penetrating radiation arising from the minute traces of radioactive material found everywhere in the earth, the discharge might not occur immediately after the application of the voltage, but would occur whenever ions happened to be formed in a location favorable for building up the discharge current. The ions if generated too close to the anode would not ionize sufficiently to reach sparking density. The spark or discharge would occur, however, as soon as a pair of ions are formed far enough away from the anode to multiply to the critical value.

The less favorable the location of the original ions, the greater would be the voltage necessary to start the discharge. Thus we should expect that the average interval of time between application of the voltage and setting in of the discharge would be increased by
reducing the frequency with which the original ions are produced and also by reducing the voltage toward the minimum value capable of producing the discharge.

The number of pairs of ions formed per cubic centimeter in air at normal pressure is only five or six per second. Thus it seems possible to measure the variable time-lag between the application of voltage and starting in of current that reaches the discharge value. Furthermore, if the original ions are produced from radiation originating in the earth, it should be possible to cut the time-lag by placing radium near the discharge tube or to increase the time-lag by shielding the tube from the earth's radiation.

## Experiments

The discharge tube consisted of concentric cylinders of nickel in mercury vapor, the vapor pressure of which was controlled by placing the tube in an oven. The working temperature of the vapor was determined by adjustment so as to give the minimum spark potential with the smaller cylinder as anode. The temperature used was 190 deg. C., corresponding to 19 mm . pressure. The voltage required to start the discharge was 264 at the above pressure. However, 300 volts was used in the experiments to insure occurrence of the discharge within a few seconds after the application of voltage.

The time-lag between the application of voltage and the starting of the discharge was measured by means of a string oscillograph designed by Prof. Trowbridge of Princeton University and made available for this work. It consisted of two separate elements recording simultaneously on a continuous photographic film, which was delivered from the camera, automatically developed, and fixed. Time coordinates are lined across this film at 0.01 -second intervals by the shadows cast by spokes of a rotating wheel, driven and controlled by a standard tuning fork. One string was connected with suitable resistances to serve as a voltmeter and the other with a
shunt to serve as an ammeter, so that they registered on the film the instant of application of the voltage and the instant of setting in of the discharge.

This oscillograph made it not only possible to record the time-lay but due to ease and speed of operation allowed a large number of oscillograms to the taken, which is necessary to obtain even fair averages.

## Results

Ircliminary results showed a wide variation in the time-lag, thus confirming carlier views on the formation of ions. To show the approach to this state of haphazard formation of ions the following procedure was followed: The gas was put into an ionized condition by rumning the discharge for a definite time of 15 seconds; the roltage was then cut off for a definite time interval and applied again. The time-lag between the application of the voltage and the starting of the current was measured after various intervals of time between the cutting off and application of the voltage. If this time interval is short, say 0.2 second, the time-lag is never over 0.001 second (which was the limit of detectability). This time-lag increases with the time interval, rapidly at first and finally becomes quite erratic but with a constant average value near 0.7 second under the experimental conditions used.

For the shorter intervals of time, residual ions from the preceding discharge evidently accounted for the quick starting of the discharge when the voltage was reapplied, but with the longer intervals of time the ions present are evidently not residual ions but are being produced at a constant rate by some external source.

A few of the oscillograms are given in Fig. 1 and the results are plotted in Fig. 2. The average values are plotted in curve $A$ and the limits of observation are given in $A^{\prime}$ and $A^{\prime \prime}$, for the time-lag against the interval of time between cut off of voltage and reapplication.

## Effect of Radium

The next set of observations was made with radium near the tube. The time-lag never exceeded about 0.01 second and was usually only 0.003 second for the longest time interval.

While it is evident that the presence of the radium decreased the time-lag, by increasing the number and frequency of formation of initial ions, this by no means points to the nature of the source of the original ions. However, it appeared to be a simple matter to determine if they are of radioactive origin,


Time Interval 0.10 Suec.


Time Intcrval 5.0 Sec .


Time Interval 10.0 Sec.


Time Interval 20.0 Sec.


Time Interval 40.0 Sec.
Fig. 1. Oscillograms showing Time-lag Between Voltage and Current in Discharge. The vertical tines are located at $0.01-\mathrm{sec}$. intervals
by shielding the discharge tube with lead, which was expected to cause the time-lay to increase.

## Effect of Shielding

The tube was placed in a jacket of lead 0.6 .3 cm. thick. The temperature of the furnace was varied to get the same pressure conditions for minimum discharge voltage. Under these conditions it was found the minimum discharge voltage was 120 volts higher than the previous


Fiz. 2. Relation Between Interval During which Discharge was Discontinued and Resulting Time-lag Between Applied

Voltage and Current
test voltage: or, in other words, the minimum voltage had increased from 264 to 420 volts. The temperature (and corresponding pressure) was varied above and below the minimum point as it was thought that the tube might have developed a leak, but it was soon found that the low discharge voltage could only be
obtained immediately after the higher voltage was applied. On waiting one or two minutes after the voltage was cut off, only the high voltage would start the discharge. 'Time-lag measurements were not made because they are not comparable with data given previously. The shield was then removed and the discharge was found to occur at 264 volts as in the experiments mentioned already. The results justified the belief that the time-lag was increased by the shielding lead to longer than one-half hour.

This last experiment, in which the starting voltage was increased by shielding, suggested that the starting voltage might be lowered by the presence of the radium. This experiment showed, however, that the lowering was less than two volts.

## Conclusions

These experiments lead to the following conclusions:
(1) The essential number of original ions in a discharge tube of the type studied are due to the radiation from the radioactive elements in the earth. The reasons for believing this are these: (a) By shielding the tube with lead the number of ions generated can be reduced to a value insufficient to start the discharge. (b) The discharge can be aided by exposing the tube to a source of radioactive emanations.
(2) The results obtained on the time-lag are in agreement with the view that the ions are formed due to the earth's radiation and that the multiplication to discharge value can readily be explained by means of Townsend's theory.

In conclusion, the writers wish to thank Prof. Trowbridge for his ready co-operation and to Mr. C. C. Van Voorhis for his assistance in making the observations.


# Electric Drive in the Printing of Newspapers 

By Carl, F. Scott<br>Bloomfield Works, General Electric Company


#### Abstract

A description of the complete process of newsprint paper manufacture on an enormous scale by a 100 per cent electrified plant appeared in our last May issue. The following article outlines the application of electricity to the next plase in the production of the finished newspaper, that is, the actual printing. The early part of the article is devoted to a detailed but brief historical review of the development of the modern types of newspaper printing presses. The remainder describes the load characteristics of a press, the manner in which the electric drive is arranged to fulfill the requirements completely, and the control equipment employed.-Ediror.


## Historical Development of the Newspaper Printing Press

Pause for a moment and picture a modern metropolis without newspapers. Then if you feel as most people do, that you can't do without them, consider briefly the wonderful organization and equipment that has made possible the gathering and dissemination of news.

We will in this article outline some essential features of the mechanical and electrical equipment of the publishing office, whose life blood is the incoming news flashes and advertising contracts, and whose nerves of motion are the electric control. Between 200,000 and 300,000 h.p. produce through the newspaper press $31,000,000$ daily papers in the United States from 2350 establishments. A quarter of a million people and half a billion of capital are employed in the publishing trades.

Besides daily papers, 17,000 different periodicals find readers in this country. It is with the daily newspapers, however, that we have to deal here.

Printing from blocks was known in China in the early part of the Christian era. 1 Paper was made there, from the inner bark of the mulberry tree.

The Arabians learned the art of making paper from the Chinese. They were known to have made paper from cotton about the year 1000.

Printing from blocks for ornamentation of fabrics came into England in the 12th century.

The making of paper from rags was also introduced in England in the 12th century.

Playing cards were printed in the 14th century.

Paper made from rags replaced vellum or sheepskin in the 15 th century about the time that movable types were invented by Coster of Haarlem, Holland; and put into practical use by Gutenberg, a German who is regarded as the father of printing. Gutenberg built presses in 1455.

In 147.5 , William Caxton, the first printer in England, translated and printed in English a
book which had been printed in Bruges or Cologne somewhere between 1471 and 1474.

Books printed before the year 1500 are known to collectors as "Incunabula" and are very valuable.

One of the first newspapers was the NotizerScritte, issucd by the Venctian Government in 1566. It could be read upon payment of a gazetta, a small coin. From this comes our word "gazette."

The first English newspaper was the London Weekly News, issued in 1622. The first French paper was the Gazette de France, and started in 1631.

The first newspaper printed in America was Public Occasions, issued in Boston in 1690. The Colonial Government suppressed it after the first issue. Printing had been suppressed in New York two years before by royal authority.

The first English daily was the London Daily Courrant, started in 1702. In 1703, came the first penny paper, the Orange Postman.

The first American daily was the Pennsylvania Packet, later known as the General Advertiser, which was started in 1784.

The next year saw the inception of the London Times, by John Walter, father of an illustrious line of publishers.

In 1797, there was started the Commercial Advertizer, now the New York Globe, the oldest paper in America that still runs.

The New York Evening Post was next and started in 1801.

It was the growing industrial and commercial life of the 19 th century which expanded journalism beyond the purely literary and political character it maintained in the early two-page and four-page sheets. These changes, especially in America, were hastened by the development of four factors: cheap paper, improved printing machinery, machine composition, and stereotyping.

All these early newspapers were single sheets or given one fold, making four pages. They were of course all printed on hand


Fig. 1. Straight-line Octuple Press. Capacity 36,000 , 32 -page papers per hour. The press has 4 decks, 4 pages wide, 54 plates. This machine is typical of large decked type presses in common use in metropolitan offices from about 1900 to 1915
presses, like those made familiar to all readers of "Franklin's Autobiography:" There had been considerable mechanical ingenuity displayed in these hand presses which were first crude affairs of wood, but by the end of the 1Sth century were of iron and even adapted
to be run by horse power. No press took over a fraction of a horse power in those days and this was two-armed or four-legged power.

Printing presses were not run by steam power till $1 \$ 14$, and not by electric power till the latter 80 's.


Fig. 2. Unit-type Low-pattern Sextuple Press. Capacity $36,000,24$-page papers per hour. Typical of present day construction. Presses are built in this form with many units in a straight row, and arranged for several combinations of units. One large press room has 25 units in a single row. The controller shown in Fig. 9 operates twelve units, equivalent to four presses like that shown above, and arranged to run as five sextuples, or as three octuples, or as two decuples and one quad

A great monetus was given to printing by the development of the paper－making machine by Fourdrinice in 1,806 ，which made elieap paper possible．It is a remarkable tribute to this genius that the Fourdrinier machine，

Napier，the inventor of grippers for carrying the sheets around the eylincler．It was im－ ported in 182.5 ，for the National Intelligencer of Washington，and was often called the Napier Cripper．


Fig．3．Multi－unit Double Quadruple Combination Octuple Press．First built in 1910. This press has two drives which operate independently or in parallel
though greatly improved over the original， is stitl the standard of modern paper making and still earries the inventor＇s name．This can be said of few other machines of so early an origin．

The hand press could turn out 200 copies an hour．

Something approaching speed came with the invention and development of the flat－bed cylinder press．The invention of this machine is attributed to F．Koenig，a German，in 1812 and 1813．He built a continuously revolving cylinder press for the London Times in 1814．This press was started Nov．29，1814，

Robert Hoe，a Scotchman，born in 1784， came to America in 1803 ，and by 1825 had become a manufacturer of printing presses． He bought the rights to the＂Washington＂ hand press from Rust and Turney，and his firm turned out in all over 6000 of them．

In 1827 and 1828，Hoe copied and improved on the Napier press，and began the production of a long series of flat－bed cylinder presses： the single large cylinder，the single small cylin－ der，the double cylinder，and others．Hoe died in 18.32 but his son continued his work．

These early flat－bed cylinder presses reached a speed of 2000 per hour，limited by the speed


Fig．4．Sixteen－page Tubular Plate Press．The plate cylinders are $7 \frac{1}{2}$ inches in diameter，and the plate surrounds the cylinder．Capacity 25,000 to $30,000,16$－page papers per hour
the first press to be run by steam power．The speed is variously given at $\$ 00$ to 1100 impressions per hour．

The first flat－bed cylinder press used in America was one built by the Frenchman
with which the sheets could be fed by a boy： They were printed on one side，and a second run was required for printing on the other side．

We read in the history of the New York $S_{u m}$ ，which was started by Benjamin H．Day
on Sept. 3, 1s:33, that he had to begin the venture with a hand press at 200 sheets an hour. Cylinder presses were too few and too costly.

In those days, it took eight hours to run off an cdition, and at that there were only four pages to the sheet. To increase the output, the double-cylinder machine with two fecders was developed. By 1843, the circulation of the New lork Sun was 35,000 and we read that it employed two Hoe-Napier doublecrlinder machines, with a combined capacity of 4000 copies per hour, printed on both sides.

The necessity for still greater production resulted in the development by Hoe of the type-revolving press in 1846, which largely supplanted other forms up to the introduction of the rotary web press in the carly 70 's.

In 1571. Hoe brought out the first rotary web machine of that manufacture. The date of 1573 or 1874 , however, is given to "Web No. 1 " which is said to be still in use though somewhat modified. This Hoe press was described as "rery compact." It was 20 ft . long, 6 ft . wide and 7 ft . high. The speed was 12,000 per hour.

The first Hoe web press, like all the early rotaries was a 2 -page wide, single-roll machine, turning ont two 4-page papers per revolution, or one s-page. The first Hoe had a "gathering and delivering cylinder," the forerunner of the modern folder.

In 1872, Walter Scott, a Scotch pressman who came to America in 1869 and was employed by the (hicagoInter-Ocean, invented a press which was adopted by his employers. Scott's first presses were built in Chicago by H. Hart and later by C. Potter,


Fig. 5. Direct-current Double Motor Drive, $100 \mathrm{~h} . \mathrm{p}$.
Jr. The manufacture was then moved to Plainfield, Ň. J., where the present factory was built in 1884.

Scott, who was a prolific inventor, put the first folder on a Bullock Rotary, perhaps the
first successful rotary web, press, built first in 1865. He invented the angle-bar first used for bringing the webs up to the folder, before the days of the triangular former. The anglebar also made the 4 -page wide press possible.


Fig. 6. Alternating-current Double Motor Drive, 40 h.p.
Hoe's first 4-page wide or "double" press came out in 1874.

The triangular former, which was one of the important elements that made the modern high-speed newspaper press possible, was introduced in 1881.

In 1885, the Goss Printing Press Co. was founded in Chicago and its first presses were 2 -page wide, 4 - and 8 -page machines.

In 1887, Hoe built for the New York Herald the first quadruple press, or 2 -unit, 4-page wide machine, called a quad because it had four times the capacity of the early single press, or twice that of the double press. Its capacity was 24,00016 -page papers per hour, using 32-plates. Like the double supplement, the rolls were at floor level and at right angles.

A book printed in England in 1888, "Modern Printing Machinery," describes no newspaper presses of more than one roll. The Hoe press described is the 1875 model.

In 1888 electric light had come in. It reduced the temperature of press rooms considerably as well as giving better light. In 1857 electric motors were first being used on newspaper presses. In 1922, a Sprague motor was running a press at the Boston Globe which it ran first in 1887.

The first sextuple, or 3 -roll, 4 -page wide, 48page press was built in 1889-1890. It had a capacity of 24,00024 -page papers per hour.

Scott's first color press came out in 1892 and Hoe's in 1893.

The first octuple, or 4 -roll, 4 -page wide, 64page press was made in 1895.

1907-190 saw the high-speed rotary camless folder and the first high-speed presses, 300 r.p.m. of the cylinders, 36,000 papers per
hour. By 1910, presses of this speed leegan to be generally installed.

In 1909, the Duplex Printing Press Co. brought ont its tulbular plate press. The essential difference between this press and the semi-cylindrical plate press heretofore built


Fig. 7. D-c. Controller for Drive Shown in Fig. 5
was in the plate cylinders. The plates surround the cylinder, one plate around instead of two around. The cylinder is $71 / 4 \mathrm{in}$. in diameter outside, instead of $141 / 2$ in., so the same size newspaper may be printed one newspaper per revolution instead of two. Thus for the same surface speed of the web the revolutions of the tubular plate cylinders will be twice that of the semi-cylindrical plate press.

About 1915, H. A. Wise Wood, inventor of the Autoplate, built a press to run at 72,000 per hour, 1200 cylinder revolutions per minute.

The early presses, taking more than one roll, were usually of the decked type. Modern presses are almost all of the low pattern type, taking more floor space, but making all parts accessible from the floor. This results in reduced labor in plating and dressing the press, shortens the time of make ready, and makes shorter and easier the job of clearing a press after a web break.

## The Power Requirements of a Newspaper Press

The power applied by the motor is used to:
(1) Overcome gear and bearing friction.
(2) Rotate the plate cylinders, impression
cylinders, and inking cylinders, the two former being pressed together under the impression.
(3) Keep the web in motion under the tension supplied by the brakes on the roll spindles and by the rollers over which it passes.
(4) Rotate the folding mechanism, drive the cutting knives and folding blades, and overcome gear, bearing and cam friction in the folder.
(5) Overcome the friction of the web on the rollers.
(6) Overcome the friction of the ink distributing rollers and the drag of the ink.
(7) Accelerate the rotating masses.

The combined resistance of these several elements, excluding accelcration, produces a characteristic curve in which the torque increases slightly with the speed. The horse power therefore increases somewhat faster than in direct ratio to the speed increase, but slower than in the ratio of the square of the speed.

Most large presses are arranged so that their separate units can be disconnected. For example, a 5 -unit, 40 -page press may at times be operated as a 3 -unit, 24 -page machine, and again as a 4 -unit, 32 -page machine. With one or two entire units disconnected, the load on the motor is greatly reduced. Provision for such operation must be made in the control system to secure smooth acceleration and proper speed control under all conditions.

One of the most important elements in press control is uniform acceleration and deceleration. Any jerks or sudden changes in speed will break the web. A broken web is always a source of delay, and time is the essential element in newspaper production. Also it may damage the rollers and blankets and perhaps spring the spindles if the paper clogs up.

The gear, bearing, and roller friction are a very large part of the total resistance. While running, these are greatly reduced by the oil films which form between the gear teeth and between journals and bearings. At standstill, the film usually does not exist. To put it another way, static friction is much higher than running friction. This applies to rollers, inking devices, and folders, as well as to gears and bearings. Cold oil and cold ink add to the static friction.

Consequently, it takes much more torque to start the press than to run it; from 150 to 300 per cent of the running torque. If this torque were applied without some way of restraining it as soon as the static friction were overcome, it would be available for acceleration to an extent that would jerk the
whole machine, break the web, and perhaps strip the gears.

Furthermore, it is necessary to give the press a low, steady speed of the web (about 40 ft . per min.) for threading it in. It is also necessary to turn the cylinders over very slowly for putting on plates. In the carly presses, from 1873 to about 1885, threading-in was accomplished by "barring-over" the press by hand, with the power off.

Later various forms of mechanical slow motion came to be employed. Presses were driven by belt, usually at one printing speed. The most usual form of mechanical slow motion consisted of a set of back-gears, with a ratio of $20: 1$, or more, associated with the loose pulley of a pair of tight and loose pulleys. The belt ran continuously on the loose pulley, and power was applied for starting the press on slow motion by means of a clutch which brought the back-gears into engagement. The press was brought up to printing speed by shifting the belt to the tight pulley. A man was usually stationed at the belt shifter, for in case of emergency the only way to stop was to signal to the man, who would throw off the belt and apply a hand brake interlocked with the belt shifter.

The modern slow motion most commonly used consists of a separate motor called the starting motor, mounted on the same base with the main motor and connected to the shaft of the main motor through doublereduction spur gearing and overrunning clutch. The gearing has a total ratio of about $30: 1$. On starting the press, the starting motor only is connected to the circuit, turning the press at a speed of about 10 cylinder revolutions per minute. When ready to go on speed, the main motor is connected to the circuit through the control, and its shaft runs faster than it had been driven by the starting motor. This causes the clutch to overrun, the clutch pawls disengaging from the ratchet teeth by centrifugal force and severing all mechanical connection between the main and the starting motors. Shortly thereafter the starting motor is electrically disconnected at the control. The starting motor is usually about one tenth the horse power of the main motor.

A conspicuous advantage of the two-motor drive is that the threading speed is substantially constant regardless of the load; whereas with a single-speed motor drive with the speed reduced to a sufficiently low value by resistance or other means, it is extremely
difficult to keep this speed uniform if the load varies through any considerable range.

At least four other distinctive types of slow motion, all dispensing with the starting motor, have been emplosed with electric drive in the past 20 years and some have shown


Fig. 8. A-c. Controller for Drive Shown in Fig. 6
merit which may lead to their reintroduction. These are:

Direct-current motor with $3: 1$ or $4: 1$ field control and with armature shunted for threading speed.
Direct-current motor with separate motorgenerator set to supply a low voltage for use in giving a low speed to the main motor; the "teaser" system.
Alternating-current or direct-current motor with double-reduction back gearing and mechanically operated friction clutch.
Alternating-current or direct-current motor with double-reduction gearing, spur or internal, and magnetically operated clutch.
However, at this time the two-motor drive is nearly universal in this country.

The basic requirements of a newspaper press drive and control are as follows:

Reliability. Delay due to breakdowns are more costly in the press room of a daily paper than in almost any other line of manufacture. The loss of an edition may mean the rebating of thousands of dollars on advertising contracts. The motors must not fail. The control must not get out of order.

Proper liuntioning. Even if the equipment does not hail or break down due to electrical or meehanical troubles, delay and expense may come from meven acceleration, jerks or other improper operation. A paper break may tie up the press for a considerable time. Failute to run evenly at high speeds may force reduced speed and delay production. Improperly adjusted brakes may cause too quick a stop, or a stop not quick and smooth cnough. Jerky starting or stopping may in

First Cost. This comes last because, while first cost counts, no publisher can afford any other equipment than the best. On the other hand, the introduction of too many and too complicated relays and other devices in the control for protection, etc., may increase the cost beyond their worth, because these very devices may be unreliable and result in more trouble by their presence than by their absence. The simplest is often the safest and most reliable.


Fig. 9. Controller for Four Drives Operating a 12 -unit Press
time cause crystallizing and fracture of gear teeth on the press.

Safety. Perhaps this should be first on the list. Men are of greater value than machines. All modern electrical equipment, however, gives great regard to protection of operators from injury. A press drive and control requires, in addition to the usual protection, devices to prevent improper and unexpected starting, lock-out of the control while working on the press, warning signal at starting, quick stopping in emergencies, and automatic stopping on breaking of the web.

Economy of Operation. In a small newspaper office, whose edition can be run off in an hour or two, power consumption does not assume the importance it does in a big metropolitan daily with a series of editions which keep the presses running a large part of the day. Saving in paper waste by proper control is usually more important than small savings in power consumption.

## Controllers for Newspaper Presses

The driving and control equipment for a newspaper press include the following:
(1) The main driving motor.
(2) The starting motor.
(3) The reduction gearing between the two.
(4) The over-running clutch for disengaging the starting motor when the main motor takes hold.
(5) The base, pedestal, shaft, bearings, couplings, or other parts needed for the assembly of parts (1), (2), (3) and (4).
(6) The chain drive or gear drive between the main motor and press shaft.
(7) The controller which includes:
(A) The main circuit disconnecting device, fused switch or circuit breaker, integral with the panel or separately mounted.
(B) The contactors or magnetic switches for connecting or disconnécting the starting motor and main motor.
(C) The accelerating and retarding means: consisting of a series of stationary contacts for cutting out or cutting in resistances, as a contactmaking arm or cross head is moved successively over these segments under the action of a pilot motor, solenoid, or gravity restrained by a dashpot. The contacts so established may act on resistance direct or may scrveas pilot circuits for operating elec-tro-magneticswitches to establish such resistance connections. Included in the accelerating means are the resistances which may be mounted on the back of the panel in the case of directcurrent field resistances, or separately in frames mounted near the panel and connected thereto by asbestos-covered wires.
(D) The stopping means: including dynamic braking for direct current; solenoid brakes and "torque-motor" brakes for alternating current; and separate brakes on the press itself, which have been of four types, viz.: disc brakes on extensions of the press cylinders; shoe or band brakes on extensions of the impression cylinder shafts operated by torque motors mounted below the press or by compressed air through cylinder and pistons direct connected to the brake band; and band brakes acting under the influence of solenoids on brake wheels secured to the vertical shafts driving the press units.
(E) Protective devices, including:

Overload protection.
Under-voltage protection.
Protection against accidental starting. Safety lock-out for the pressman working on the press.
Warning signal before starting.
Locking against increase in speed after a certain maximum has been reached. Adjustable setting of maximum permissible speed.
Prevention against too rapid acceleration or retardation.
Automatic return of controller to "off" position after starting.
Prevention against connecting in main motor unless starting motor has started and come up to speed.

Device for stopping the motor and setting the brakes when the web breaks.
Protection against overtravel of the switch arm, and hence the attainment of a greater speed than desired for any given condition, quality of paper, etc.
( 8 ) The push-button stations, located about the press, for inching, jogging, starting, lowspeed, accelerating, slowdown, stopping, safety lock-out, and warning signal. The minimum number of buttons in any one station for a full automatic control system would appear to be four, and it should be unnecessary to resort to more than seven for the most complicated


Fig. 10. Push-button Station for Newspaper Press Control system.

The push-button stations and the wires connecting them up are an extremely important part of the system. The push-button mechanisms themselves must be very substantial as they are in constant use under none too dainty handling.

There are from four to nine wires in the conduits leading to the push-buttons. If any of these wires becomes grounded, or opencircuited, or if a short circuit develops between wires, the system may be temporarily inoperative. Hence, it is best to use none but the very highest grade of multiple conductor cable, thoroughly insulated, and well protected mechanically. If run in flexible conduit, the cable must be lead covered. Great care must be taken to prevent abrasion in pulling the wires in, and making connections. Great care must also be taken to prevent oil getting into the cable. Oil may run down the press frame, soak into the push-button station, and so into the wiring; or it may run into junction boxes below the press if the latter are not oil tight. Filling them with paraffin is a good precaution.

It is customary to provide an emergency push-button station, with an entirely independent wiring system direct from the controller, for use in case a failure occurs in the main system.

# The Electron in Chemistry <br> PART III 

By Sir Josbph John Thomson<br>Master of Trinity College, Cambridge, England


#### Abstract

The first of this serics of lectures appeared in our August issuc. The present lecture deals with the Mechanism of Chemical Combination; Formation of the Double Layer; Active Molecules; Thicles' Theory of Partial Valencies; Kete-enol Change; Production of Light by Chemical Change and on Homologous Elements and Variable Valency. These lectures are reprinted by permission from the Journal of the Franklin Institute.-Edrror.


## The Mechanism of Chemical Combination

Let us in the first place consider chemical combinations between gases. That something more than collisions between the molecules of the reacting gases is required is clcar, from the fact that gases like hydrogen and oxygen, hydrogen and chlorine (in the dark), which can form very stable compounds, can be mixed without any appreciable amount of chemical combination taking place at moderate temperatures. The test is a very severe one since at atmospheric pressure each molecule of oxygen in a mixture of hydrogen and oxygen would in one second collide with many million hydrogen molecules, so that even if only one collision in a million were to result in combination the rate of combination would be very great. A mixture of hydrogen and oxygen in the proportion of two molecules of hydrogen to one of oxygen can be stable, (a) when the gases are uncombined, and (b) when they are combined and the mixture exists as water vapor. The large evolution of heat observed in the transit from (a) to (b) shows that (b) has much less potential energy than (a). The fact that the gases can exist side by side without combination shows that the phase of high potential energy does not spontaneously pass to one of lower. We have many examples of this in ordinary mechanics. Thus the water in a mountain lake has more potential energy than it would have if it ran down into the valley, it does not do so because before it could get away work would have to be supplied to raise it above the level of the height immediately surrounding it. If a syphon is put into the lake this work is forthcoming and the water will run out. To enable a system to pass to a state of smaller potential energy may require the expenditure of a certain amount of energy and if this is not forthcoming the change will not take place. Thus, if a preliminary to the combination of hydrogen and oxygen were the dissociation of the molecules of these gases into atoms, the
gases would not combine unless the very considerable amount of energy required for this initial stage were available. Now in the mixture of two pure gases the energy available is that due to the thermal agitation of the molecule; this at $0^{\circ} \mathrm{C}$. is only about $1 / 30$ of a volt per molecule, and is small compared with the changes in energy occurring in chemical processes which on the same scale would be represented by several volts. Thus we might expect that unless some source of energy besides that due to thermal agitation were available, the combination would not take place. In the case we have just been considering, that of the dissociation of electrolytes in solution, the main part of the energy required to separate the ions in the electrolyte came not from thermal agitation, but from that derived from the falling in of polar molecules, i.e., from the energy of chemical separation of the polar molecule and the molecule of the electrolyte.

The effect of water vapor, whose molecule is strongly polar, on the combination of gases is well known. Thus, H. B. Baker showed that very carefully dried HCl and $\mathrm{NH}_{3}$ would not combine, that the combination of $\mathrm{H}_{2}$ and $\mathrm{Cl}_{2}$ went on exceedingly slowly, even in strong sunlight, when the gases were carefully dried, while H. B. Dixon showed that electric sparks might be passed through a mixture of dry CO and $\mathrm{O}_{2}$ without combination taking place. He also showed that other substances besides water vapor render possible the combination between CO and O , and it is probable that all polar molecules possess this property to a greater or less extent. Baker found that the effect of water vapor was not confined to combination if extended also to dissociation, for while ordinary ammonium chloride is dissociated to a very considerable extent when the temperature is raised to three or four hundred degrees centigrade, no dissociation occurs at these temperatures if the salt is very carefully dried.

When polar molecules, such as those of water or ammonia, are present, they may combine with the other molecules, forming aggregates in which, as in the case discussed in a previous lecture, there is a kind of incipient ionization, the atoms being more widely separated than in the normal molecule. The aggregate has a finite electrical moment and thus exerts much greater forces on neighboring molecules than the normal molecule. Let us represent these aggregates by $\mathrm{A}\left(\mathrm{H}_{2} \mathrm{O}\right)_{n}$, $\mathrm{B}\left(\mathrm{H}_{2} \mathrm{O}\right)_{m}$ when A and B represent molecules of the reacting gases. When two of these come together the work required to separate them may be so much greater than that required to separate $A B$ that though $A$ and $B$ cannot by collision form a potent aggregate $\mathrm{A}\left(\mathrm{H}_{2} \mathrm{O}\right)_{n}$ and $\mathrm{B}\left(\mathrm{H}_{2} \mathrm{O}\right)_{m}$ are able to do so. After the aggregate has been formed the atoms loosened by the action of the polar molecules rearrange themselves so as to produce the sustem with the minimum potential energy. If, as the result of this rearrangement, the water is set free, it will be available for producing a further supply of the complex molecules. Even if only a small percentage of the molecules are in the complex state the rate of combination might be considerable, as the number of collisions made by a molecule under ordinary circumstances is so large. Thus to take the combination of gaseous HCl and $\mathrm{NH}_{3}$ to form $\mathrm{HN}_{4} \mathrm{Cl}$ as an example. If even only one molecule in a hundred thousand were in the complex state and if the combination only occurs when a complex molecule of HCl collides with a complex one of $\mathrm{NH}_{3}$, these collisions will still be so numerous that something like one per cent of the HCl and $\mathrm{NH}_{3}$ will combine per second. We see from this that to avoid appreciable combination the gases must be exceedingly dry, and that traces of water too small to be detected by other means might produce very marked effects on chemical combination.

On this view of chemical combination the rearrangement of the atoms takes place inside a complex formed with the polar molecules, thus no ions need get free. There is very strong evidence against the necessity for the existence of free ions in gaseous combinations; free ions make a gas a conductor of electricity and the conductivity due to free ions can be detected when the number of free ions is much less than one-million-millionth of the number of molecules. Many cases of chemical combination have been tested for electrical

[^80]conductivity without any trace of it being detected. Thus L. Bloch showed that many chemical actions which go on at moderate temperatures, such as the oxidation of nitric oxide, the action of chlorine on arsenic, the oxidation of ether vapor and so on, have no effect on the electric conductivity of the gases. I found, too, that even when the combination was as vigorous as that between hydrogen and chlorine in the light, no effect whatever was produced on the electrical conductivity of the mixture. Again dissociation at moderate temperatures such as that of nickel carbonyl at about $100^{\circ} \mathrm{C}$. into nickel and carbon monoxide, or in the dissociation of arseniuretted hydrogen, is quite without effect on the conductivity. This is in accordance with the consequences of the theory.

There are, however, some cases in which free gaseous ions are produced by dissociation or chemical action. Thus Kalendyk ${ }^{19}$ found that the vapor of potassium iodide was a conductor of electricity at temperatures above $300^{\circ} \mathrm{C}$. if damp, but not when dry; this is a good example of the effect of water vapor. Another case investigated by Bloch (loc. cit.) is the oxidation of $\mathrm{P}_{2} \mathrm{O}_{3}$ to $\mathrm{P}_{2} \mathrm{O}_{5}$, which is also accompanied by an increase in electrical conductivity.

The efficacy of polar molecules is on this view due to their large electrostatic moment, which causes them to be strongly attracted by other molecules. Any systems, such as free electrons or gaseous ions, which give rise to strong electric fields, might be expected to promote chemical combination by processes similar to those which occur with water molecules.

Again, if the reacting gases were condensed on the surface of a piece of metal, or on the surface even of a non-metal or liquid, particularly if these substances were of special types, the molecules would find themselves in the presence of agents of the kind we are considering. At the surface of a metal there are mobile electrons, while the molecules at any surface can only be coordinately saturated in very exceptional cases. For when a new surface is produced by fracture some of the atoms which helped to "satisfy" the molecules left behind have been torn away, so that the molecules on the surface must be unsaturated and able to bind other atoms or molecules. The energy derived by the approach of a molecule to the unsatisfied molecules at the surface of the solid or liquid may be used to separate the atoms in the approaching
molecule，in just the same way as the energy due to the approach of a polar molecule helped to separate them．Thas the molecules of a gat condensed in a layer on a surface will be exposed to influences very similar in character to those to which they wonld $b x$ ． exposed when combined with water molecules， and we may expeet to find that the connection between these atoms gets so loose that these are able to rearange themsclves and form new compounds．

The layers condensed on a surface will in many respects be in a more favorable con－ dition for entering into chemical combination than the free molecules of the gas，even if these are supplied plentifully with water molecules． For the molecules in the surface layor will be crowded together and kept in close contact； they will thus be in a situation particularly favorable for the rearrangement of theiraton：s．

The effect of metal surfaces in promoting chemical combination is shown by the com－ bination of hydrogen and oxygen produced by platinum black，by the synthesis of ammonia in the Haber process，by the effect rioduced by metals when in the colloidal state，by the Sabatier－Senderens method，wher many changes in organic compounds are priduced by passing them along with hydrogen over finely divided nickel or certain other metals at a high temperature．Another instance is the effect produced by the walls of the vessel in which the reacting gases are contained；many examples of this are given by Van t＇Hoff in his studies on chemical dynamics．

It is possible that water in addition to the effect it produces by the individual molecules may produce an additional effect by forming small drops，which in the aggregate might have a very large surface，on which the gases might condense．

We can get some very direct evidence as to the conditions at the surface of separation of gases，liquids and solids by the study of the very interesting cases of electrifications pro－ duced by the bubbling of gases through liquids，by the splashing of liquids against solid surf ${ }^{n}$ ces，and the motion under an elec－ tric field of bubbles of air and colloidal particles through liquids When gases bubble through certain liquids of which water is a conspicuous example，the gases after they emerge from the liquid are found to be electrified．The liquids which give rise to this electrification are those which possess con－ siderable electrical moments $i e$ ，they are those which，as we have seen，have the property of forming complex compounds with
compounds which are already electrically saturated．The amount，and even the sign of the electrification produced by bubbling，is very sensitive to small changes in the com－ position of the liquid．Thus air bubbling through pure water emerges with a negative charge，but if a small quantity of HCl or $\mathrm{H}_{2} \mathrm{SO}_{4}$ be added to the water，the electrifica－ tion of the air becomes positive．The electrifi－ cation is dependent upon the breaking of the liquicl film when the air bubble escapes from the fluid．No electrification is produced by blowing a current of air along a water surface or by stretching，without breaking，a liquid film．A similar dependence upon the com－ position of the liquid is shown by the motion through a fluid of small particles or air bubbles under an electric field，a phenomenon which is sometimes called cataphoresis．The addition of acids and salts，especially if these contain elements of high valency，produces a great effect on the velocity with which the bubble moves through a liquid under a constant clectric field．Cataphoresis is more amenable to mathematical treatment than electrification by bubbling and the mathematical theory has been worked out by v．Helmholtz and Lamb on the supposition that there is a double layer of electricity，one layer being positive and the other negative，at the surface between the bubble and the liquid，and that one layer is attached to the liquid，the other to the bubble or colloidal particle．If $v$ is the velocity of a particle under an electric force $\mathrm{X}, \eta$ the coefficient of viscosity of the liquid， $\sigma$ the surface density of the electric charge on either layer，$d$ the distance between the layers， then according to $v$ ．Helmholtz

$$
\begin{equation*}
v=\sigma d X / \eta \tag{29}
\end{equation*}
$$

so that the measurement of the velocity would at once give us the potential difference at the surface．Lamb has given very strong reasons for thinking that this relation is not sufficiently general and is based upon supposi－ tions which are not likely to be valid when，as in this case，we are dealing with distances which are of the order of atomic distances； he finds instead of（29）the cquation

$$
\begin{equation*}
v=\sigma l X / \eta \tag{30}
\end{equation*}
$$

where $l$ is a length dependent on the liquid and on the nature of the particle．As $l$ is not known，we cannot claim that the use of the v．Helmholtz formula gives more than the order of the surface density；in some cases， however，where it has been possible to measure the potential difference between the particle and water，this has been in fair agreement with
the value deduced by Helmholtz's equation. It will be noticed that according to either formula the velocity of the particle is independent of its size, provided $\sigma d$ and $\sigma l$ are unaltered. This has been verified by several observers, among others by Burton ${ }^{20}$ and McTaggart. ${ }^{21}$ - In water, air bubbles and some solid particles move as if the negative charge were on the particle, and it is remarkable that, in spite of great variations in the character of the particle, the changes in the potential difference are comparatively small. This is shown in the following table taken from Burton. ${ }^{22}$ The potential difference $\phi$ has been calculated from the $v$. Helmholtz equation assuming

$$
\phi=4 \pi \sigma d / K
$$

where $K$ is the specific inductive capacity of water

| Substance | Potential Difference in Volts Deduced by Helmholtz's Equation |
| :---: | :---: |
| Lycopodium. | -. 035 |
| Quartz | -. 042 |
| Air bubbles. | -. 056 |
| Arsenious sulphide | -. 031 |
| Prussian blue. | -. 056 |
| Gold (Bredig). | -. 030 |
| Platinum (Bredig). | -. 028 -.034 |
| Silver (Bredig) | -. 033 |
| Mercury (Bredig) | -. 035 |
| Bismuth (Bredig) | +. 015 |

We see from this list that for many substances the difference of potential between the two layers is about $1 / 30$ of a volt; this is very nearly the potential difference through which an electron must fall at room temperatures to acquire an amount of energy equal to that possessed by a molecule of gas from its thermal agitation. Thus a charged atom at the double layer would possess by thermal agitation an amount of energy comparable with that required to detach it from the double laver. We should expect that a limit to the potential difference between the two layers must be imposed by the necessity of one layer being able to move freely relatively to the other. If, for example, the double layer were formed by positively and negatively charged atoms in the same molecule it could not produce cataphoresis unless some source of energy sufficient to dissociate the positive from the negative parts were forthcoming. If this energy has to come from thermal agita-

[^81]tion, the positive and negative parts must have been driven so far apart that the energy required to separate them is of the order of the mean kinetic energy of a molecule due to thermal agitation, which at $0^{\circ} \mathrm{C}$. is aloout $1 / 30$ of a volt. The energy required to detach a charge from the double layer is proportional to the potential difference between the layers. Thus the energy available from thermal agitation may be a most important factor in determining the value of the potential difference in the effective double layer.

## The Formation of the Double Layer

Polar molecules, such as those of water, have, as we have seen, the power of forming molecular compounds in which oppositively charged atoms are separated and put into a condition in which they can be easily detached from each other. These compounds are of two types, in the first symbolized by such a case as $\left[\mathrm{Me} .4 \mathrm{H}_{2} \mathrm{O} \cdot(\mathrm{OH})_{2}\right] \mathrm{H}_{2}$, the effect of the formation of the complex compound is to give a charge of negative electricity to the substance with which the water is in contact and to put two positively charged atoms into a condition in which they can easily be detached fron, the substance. The formation of a comi" and of this type would produce a doul, le layer with the positive part in the water and the negative on the substance. This is the type of double layer formed at the surface of colloidal particles of platinum, gold, silver, quartz or air bubbles. The other type of complex compound is that symbolized by $\left[\mathrm{Ca} .4 \mathrm{H}_{2} \mathrm{O}_{1}\right] \mathrm{Cl}_{2}$, here the water molecules drive out the negative constituent from the original compound and give to the system surrounding the central atom a positive charge. If a substance of this kind were formed there would again be a double layer, but in this case the negative part of it would be in the water, the positive on the substance in contact with the water. This is the type of double laver formed at the surface of colloidal particles of ferric hydroxide.

The case of a gas bubble in water is an interesting one in which the evidence on some points is somewhat conflicting. IcTaggart found that the velocity of bubbles of hydrogen was the same as that of oxygen bubbles indicating that the potential difference was independent of the nature of the gas, and that the gas did not take part in any chemical reaction. Alty, who has recently been making experiments on this point in the Cavendish Laboratory, finds that considerable variation in the relocity of the bubbles is produced in
some cases by changing the gras. 'The view that oxygen may take part in chemical reactions with water is supported by the observation frequently recorded but first made, I think, by Bellucei, ${ }^{23}$ that the air in the neighborbood of waterfalls, where there is a great deal of splashing, contains abnormally large (fuantities of ozone. Under the action of the water molecules ozone may be formed and negatively electrified ozone form the coating in the gas of the double layer.

We should expect that there would be a double layer at a surface separating water from its own vapor. Hardy and Langmuir have pointed out that the molecules at a liquid water surface are polarized, i.e., the number of molectles which have their positive ends at the top is not the same as the number with the negative end. Thus, suppose the majority of molecules had the negative ends, i.c., the oxygen atom, at the top, the oxygen atoms are not coordinately saturated and may combine with the molecules of water vapor to form comporinds of the type $\left[\mathrm{O} . \mathrm{H}_{x}\right](\mathrm{OH})_{x}$ : This would give rise to a double layer with the positive half in the water, the negative one in the bubble. Experiments are in progress at the Cavendish Laboratory to see whether any evidence can be obtained of a double layer when water is in contact with nothing but water vapor.

The formation of the double layer gives a supply of positive and negative ions at the surface of an air bubble in water. Just before the bubble emerges from the water this surface has a considerable area. It is reduced to very small dimensions after the bubble emerges. Thus the emergence of the bubble involves a considerable and very abrupt contraction of the surface and of the double layer associated with it. The double layer will be violently distorted and it does not seem surprising that some of the ions in the layer on one side should not have time to combine with those on the other before they are carried away by the air. Only a very small fraction of the ions in the double layer get liberated when air bubbles through water. Assuming v. Helmholtz's formula, we can calculate from the velocity of the bubble the quantity of electricity per unit area of each layer. Assuming that the distance between the layers is $10^{-8} \mathrm{~cm}$., McTaggart (loc. cit.) found that this density was $4 \times 10^{-5}$ coulombs per square centimeter. If all the water molecules had been polarized, i.e., if all the

[^82]Oll ions of the water molecules were next the surface and if the distance between two molecules of water on the surface were the same as that in the interior, i.e., $3.09 \times 10^{-8}$ cm., the density would be about $1.7 \times 10^{-4}$ coulombs per square centimeter, about four times greater. On one layer of a bubble 7.8 mm . in diameter the charge on either layer would be $7.6 \times 10^{-5}$ coulombs. Simpson ${ }^{24}$ found that when a drop of this size struck against a plate the amount of electricity set free was $2.8 \times 10^{-12}$ coulombs, i.e., only about one thirty-millionth of the charge on the layer. We conclude from this that only an exccedingly small fraction of the water molecule at the surface of an air bubble or drop of water is ionized by the bursting of the bubble or the splashing of the drop.

When air bubbles through water sone ions become free, there are other types of experiments when, though there is a separation of positive and negative electrification, few if any ions get free. The Armstrong hydro-electric machine is a case in point. Here small drops


Fig. 35
of water are carried by a jet of steam through a tube with great velocity. In their passage through the tube the drops strike against the sides and the tube becomes negatively, the drops positively, electrified. Here the separation of the positive and negative electrification is the principal effect and not the liberation of free ions. We have supposed that at the surface of a drop of water there is a double layer, the negative part, OH ions, in the air and the positive part, H ions, in the water. When the drop strikes against the tube the OH ions combine with the material of the wall of the tube forming those molecular compounds we have been considering in this chapter. When the drop rebounds from the wall of the tube it will tend to take the $\mathrm{H}_{+}$ions away with it, while the walls of the tube will hold the $\mathrm{OH}_{-}$ions. The ions will be separated by the kinetic energy of the drops. The ions will not, however, get free; the positive ones will be on the water drops and the negative ones on the walls of the tube. This is a particular case of
electrification by friction, and it is evident that the formation of double lavers must be of vital importance in that phenomenon.

## Active Molecules

We have hitherto considered the way in which chemical combination was promoted by polar molecules and by active surfaces, the energy necessary for the preliminary separation of the atoms in the reacting molecules before their final readjustment to form the molecules of the new compound coming from the potential energy of separation of the polar molecules and of the reacting molecules before combination. We have seen that the kinetic energy of themal agitation is inadequate for this purpose. Though the influence of polar molecules on chemical combination is undoubtedly very great, the evidence does not, I think, warrant the conclusion that all chemical combinations are dependent upon their agency. The combustion of carbon


Fig. 36
bisulphide, of cyanogen and of certain hydrocarbons in oxygen appears to be unaffected by the presence of traces of moisture. ${ }^{25}$ The question arises, what is the mechanism by which the combination can be brought about, when the energy arising from polar molecules is not available, and when that due to thermal agitation is too small to split up the molecules of the reacting gases into atoms? The electron theory indicates a way in which certain molecules could be put into a chemically active state without separation into atoms by an expenditure of energy much less than would be required for that purpose. Consider, for example, a molecule of oxygen, its neutrality is attained by the arrangement of its electrons into two octets, to obtain these two the utmost economy in construction must be observed and the octets have to have four electrons in common. Let the electrons in the molecule be

[^83]displaced so that the cells surrounding the atoms have no longer four electrons in common, suppose, for example, that they have only two in common, then since there are only twelve electrons avaibable there can only be seven electrons in cach cell, and each atom will be surronnded be only seven electrons instead of by ciglit. Now the cell of seven electrons is not saturated and will be chemically active, though it will not be so unsaturated as the free oxygen atom which is only surrounded by six electrons. To move the electrons so as to change the arrangement of electrons from that corresponding to the inactive state represented by Fig. 35 to that of the active state represented by Fig. 36 would require far less energy than to separate the atoms, so that the necessary amount may be derivable from thermal agitation at temperatures far below that required to separate the atoms.

I think this conception of the active molecule has an important bearing on the combination of explosive mixtures such as those of oxygen and hydrogen; these gases explode at temperatures as low as $600^{\circ} \mathrm{C}$. where the energy of thermal agitation is quite insufficient to split the oxygen molecules up into atoms. Indeed, direct experiments on the relation between temperature and pressure have shown that there is no appreciable dissociation of the molecules of oxygen at $1700^{\circ} \mathrm{C}$. If, however, the work required to make the molecule active in the manner described was that corresponding to thermal agitation at a lower temperature, say $600^{\circ} \mathrm{C}$., then if in any region of a mixture of the explosive gases the temperature reaches this value, the oxygen molecules will become active and combine with the hydrogen, the heat developed by the combination will raise the temperature still further and the hot molecules will travel out with energy sufficient to make the molecules of oxygen against which they strike active. This will lead to further combination and a further development of heat and combination will spread throughout the mixture.

As there is no dissociation of the molecules into atoms, the process of making the oxygen molecules active will not change the pressure in pure oxygen.

There is direct experimental proof that the molecule of oxygen can be put into the active state. When we use the method of positive rays we find that oxygen is one of the few molecules, as distinct from atoms, that can occur with a negative charge. If the oxygen
molectule conkl only ocenr with its electrons arranged as Fig. $\mathbf{3 i n}^{3}$, it could not receive a negative charge, because there is no room for an electron in the octets. It could, however, receive such a charge if the electrons were arranged as in Fig. 36 because there is room for an clectron on each of the septets.


Fig. 37
The fact that a particular atom or molecule can be negatively charged shows that it can be in stable equilibrium after receiving an additional electron, so that in the neutral state it is unsaturated and chemically active.

The arguments we have used about the oxygen molecule will apply to any arrangement of electrons where there are two octets with four electrons in common. This arrangement occurs when we have two atoms connected by a double bond-it occurs, for example, in carbon compounds whenever there is a double bond between two carbon atoms, $\mathrm{C}=\mathrm{C}$, it so occurs in the combination $\mathrm{C}=\mathrm{O}$, though not in $\mathrm{C}-\mathrm{O}-\mathrm{H}$.

## Thieles' Theory of Partial Valencies

This conception of the active molecule leads in many cases to the same results as Thieles' theory of partial valencies. Thus to take the case which led to the theory. It was found that a compound where the carbon atoms are arranged according to the scheme -
$\mathrm{C}=\mathrm{C}-\mathrm{C}=\mathrm{C}$, where two double bonds are separated by a single one, when it forms additional compounds does so by adding the new atoms to the carbons at the ends of the chain. On our view the distribution of the electrons in the compound is represented in Fig. 37.

There are four octets, $1,2,3,4 ; 1$ and 2 and also 3 and 4 have four electrons in common, 2 and 3 only two. Suppose all the carbon atoms get put into the active condition. The octets with four electrons in common will become septets with two electrons in common and the system will be a chain of four septets (Fig. 38), where the septets are represented by triangles, each having two electrons in common with its nearest neighbor. To make this change in which all the carbon atoms have
been made active requires the expenditure of a certain amount of energy; an expenditure of a smatler amount will be sufficient to make a part of them active. To find the change which will require the least energy, we notiee that if any adjacent pair of septets were to revert to a system with four electrons in common, the new system woukd have less potential energy than that shown in Fig. 38, and would require less energy to be expended to derive it from the original system.

The work required for this change woukd be the work required to convert the system (Fig. 37) into the system (Fig. 38), minus the loss of potential energy when an adjacent pair of septets reverts to two octets with four electrons in common. Thus the system which will require the minimum work will be the one when the pair which reverts is the one for which the loss of potential energy on reversion to octets is greatest. This pair will be the one which is most symmetrically placed, i.e., the central pair. Thus the active configuration which requires the least expenditure of work is that represented in Fig. 39, where the end cells are septets and active. As these cells are active, additions will take place at them, and the central carbons will be connected by a double bond.

## Keto-enol Change

The same reasoning will apply where the double bond is between a carbon and an oxygen atom (Fig. 40). Thus in the compound $\mathrm{O}=\mathrm{C}-\mathrm{C}-\mathrm{H}$, the distribution of electrons is that represented in the figure, if the two octets with four electrons in common are made active, the active oxygen units with the neighboring atom of H , the hydrogen coming away from


Fig. 38
$\mathrm{C}_{2}$ with its electron; this completes the octet round $O$, leaving septets round $C_{1}$ and $C_{2}$ with two electrons in common; these revert to the more stable arrangement of the same number of electrons, viz., two octets with four electrons in common, and we have thus the compound
$\mathrm{OH}-\mathrm{C}=\mathrm{C}$
this is known as the keto-enol change. It only takes place when one of the atoms attached to $C_{2}$ is that of an electronegative element; the reason for this follows from the same considerations as those previously given to explain the effect of introducing electronegative groups into hydrocarbons.

The same principles will apply to a smaller extent when two octets have only two electrens in common, for if the electrons were displaced so that the cells had only one electron in common, one of the atoms would become active and could enter into chomical combination. Thus if the electrons in a chlorine molecule get displaced so that the cells have only one electron in common instead of two, one of the cells will become active and can combine with hydrogen. The energy required to displace the electrons need not come from the energy of thermal agitation, it might come from light if that were absorbed by the molecules.

## Production of Light by Chemical Change

Many chemical reactions involve an increase or a decrease in the number of electrons grouped round some of the atoms; thus, for example, if an atom of hydrogen combines with one of chlorine to form HCl . after combination the chlorine atom is surrounded by eight electrons, whereas before it was surrounded br only seven, thus the reaction has resulted in an electron falling into the later round the chlorine atom; this atom may be regarded as coming from the hrdrogen atom. On the other hand, when HCl dissociates into H and Cl the chlorine ion loses an electron. While the hydrogen ion gains one. We shall use the term oxidation for the process by which the atom of an electronegative element gains an electron and becomes negatively charged since ordinary oxidation is


Fig. 39
a process of this kind, and reduction for the process by which a positively electrified ion of an electropositive element receives an electron and becomes neutral.

Thus, in oxidations an electron falls into the zone round the atom of an electronegative element; in reductions an electron falls into
the zone round the atom of atn electropositive one. From the study of the luminous effects in the discharge of electricity through wases we are led to the conclusion that the capture of an electron by an atom results in the emission of light, and from the quantum therery it would follow that the frequency of the light


Fig. 40
would be proportional to the potential energy lost when the electron falls into the atom, or what is equivalent, to the work required to remore an electron from the negatively electrified constituent of the compound in the case of oxidation or from the neutral atom in that of reduction. Thus we should expect that both oxidation and reduction would be accompanied by the emission of light; it may be that the rate at which the chemical processes go on is so slow that the energy in the light is not sufficient to make it apparent. or again, that the wave-length of the light is not within the range of the risible spectrum. The production of light br chemical action is a well-known phenomenon. In addition to the conspicuous cases of flames where the temperature is high, there are many examples of luminosity occurring at moderate temperatures; the luminosity of phosphorus when oxygen passes orer it is one example; then there is the luminosity of sulphur when heated to about $300^{\circ} \mathrm{C}$. in the presence of oxygen, the light given out by the glowworm and by the animalculae which cause the phosphorescence of the sea. Linneman found that fresh surfaces of sodium or potassium are luminous in the dark until they get corered by a coat of oxide. This production of light is. I think the cause of the emission of electrons in the dark from the alloy of sodium and potassium when exposed to rarious gases which I observed many years ago and which has been investigated rery fully by Haber. If chemical action went on between the gases and the NaK alloy.
light womk be given ont, and as the alloy is very photedededic, clectrons would be given out he the surface of the alloy. The seat of the light is at the surface of the alloy so that, although the light might not be intense emough to be visible at molar distances, yet at the atomic distances which separate it from the alloy its intensity might be sufficient to produce very considerable effects. Again, since in oxidations the origin of the light is in the electronegative elements, we should not expect to find in light due to oxidation the spectrum of the electropositive element. It has long been considered remarkable that the spectrum of hydrogen is not visible in flames or in light produced by chemical means, though it is so easily produced by the electric discharge. This is just what we should expect if the chemical reactions were of the type of oxidations; to have a chance of getting the hydrogen spectrum the process should be a reduction. Thus, for example, in the partial dissociation of hydrodic acid, when there is cquilibrium between the formation of HI and its dissociation into H and 1, the combination would give rise to the spectrum of HI with the iodine as the source of light, the dissociation might give the hydrogen spectrum. It is to be noted that the spectrum of a molecule may vary with the atom in that molecule which is excited. Thus to take as an example $\mathrm{COCl}_{2}$, the spectrum emitted due to the fall of an electron into the oxygen atom would not be the same as that due to the fall of one into the chlorine atom. We have in considering the type of light emitted to consider not merely the atom into which the electron falls, but also the method in which it falls. Thus to take a case in which we have very vigorous reduction going on, that of the liberation of hydrogen from the cathode when strong currents pass through acidulated water. Since the hydrogen atoms which come off are neutral, the hydrogen ions which were positively electrified must each have received an electron and so might be expected to have given out light. I am not aware, however, that anyone has observed any luminosity in the neighborhood of the cathode during the electrolysis of acidulated water. Nor need we, I think, expect it; we have already seen reasons for thinking that hydrogen ions in water have attached to them a number of water molecules, the negative ends of these molecules being turned towards the hydrogen ion. The effect of these negative charges is to diminish very materially the attraction of the hydrogen ion
on the negative electron, so that when the clectron falls into the ion it will do so with very much less cnergy that it would in the absence of the water molecules; as the energy is so much less, the intensity of the light and also its frequency will be greatly diminished, so that not only will the light be feeble, but also probably far away, on the red side of the visible spectrum.

## On Homologous Elements and Variable Valency

Homologous Elements.-The valency of an clement depends according to these views on the number of electrons in the outer layer rather than upon the total number of electrons in the atom. We have supposed that the electrons in the atom are arranged in a finite number of layers, the members of each layer being approximately at the same distance from the center of the atom. As we pass from the atom of one element to that of the element next in order of atomic weight, we have to provide for the accommodation of one more clectron in the atom. If the additional electron joins those in the outer layer it will give rise to an atom of an element of different valency and with very pronounced difference in chemical properties. If, however, the electron finds accommodation in one of the layers below the surface, the element corresponding to this atom will have the same valency as the first and will resemble it in chemical properties more or less closely according as the layer on which the new electron settles is near to or far from the center of the atom. Thus we might have a graduated series of elements differing in atomic weight; the properties of some-those with the additional electrons in the layers close to the center differing so little from those of some element of smaller atomic weight in the series that the two might with propriety be regarded as isotopes. The difference in propertics will increase though the valency remains unaltered, as the electrons find a place in layers nearer the surface until finally we come to the element where the additional electron has got to the outer layer; here there is a change in the valency and a marked alteration in the chemical properties. We are thus led to expect the existence of groups of elements possessing very similar properties; in some cases the chemical properties might be so similar that the elements would not be separable by chemical means and would be classed as isotopes; in others the differences would be large enough to enable the elements to be isolated by chemical processes. Exam-
ples of such groups are the iron, nickel and cobalt group, the ruthenium, rhodium and palladium group, the large group of the rare carths and the iridium platinum group. Inside these groups, increase in atomic weight is not accompanied by change of valency; outside them, it is.

In considering the way in which a definite number of electrons will arrange themselves round a central charge, there are two influences of predominating importance: The first of these is the tendency of the electrons to get as close to the central charge as is consistent with the stability of the layer, i.e., to have as many electrons in the innermost layer as the central charge can hold in stable equilibrium, and then as many in the second layer as the central charge when surrounded by the first layer can hold in stable equilibrium, and so on. This disposition will make the potential energy due to the forces between the positive nucleus and the electrons as small as possible. The potential energy due to the forces between the electrons has next to be considered. This will diminish as the distances between the electrons increase and will tend to make the electrons in the various layers arrange themselves so that their figures are similar, or at any rate have the same kind of symmetry about the center. This latter tendency would, if it prevailed, cause a new electron if added to an atom already containing a number of electrons either to go to the outer layer, or if that were full, to make the beginning of a new outer layer. The tendency to get as close as possible to the center would, on the whole, make for the retention of the electron by one of the inner layers.

We should expect that we could not go on increasing the number of electrons without reaching a stage where a new electron would stay in the inner layers. If so, its influence on the chemical properties would be very slight and the new element would be very similar to the old. The addition of an electron to one of the inner layers would alter the nature of its symmetry round the center and make it different from that of the other layers; as the different layers like to have the same kind of symmetry, when one layer has got a new electron the other will try to get one, too, so that when once the absorption of electrons by the inner layers has begun it will continue as the next few electrons are added to the atom. When each layer has received an electron, we may expect the next electron to come to the surface, giving rise to an element whose properties are markedly different from those
of the clements which just preceded it. Thus the homologous elements might be expected to occur in groups and inasmuch as in the elements inside the group some of the layers have one lind of symmetry and others a different one, the distribution of electrons inside the atom of elements in a homologrous group is irregular and does not possess the uniformity or regularity possessed by elements outside the group where the electrons in the inner layers have adjusted themselves so as to produce a high degree of symmetry.

Varying Valcncy.-We have been considering eases where different elements have very similar chemical properties, although they contain different numbers of electrons, where, in fact, we have variations in the number of electrons in the atom without much alteration in the chemical properties. The question naturally arises whether we might not have also variation in the chemical properties without alteration in the number of electrons, and whether the existence of some elements which have more than one kind of valency is not a case in point. Ferrous and ferric iron have different properties, so have cuprous and cupric copper. As the elements can pass backwards and forwards between the -ous and the -ic states, if these states correspond to two different configurations of the same number of electrons, these configurations must be such that by suitable chemical or physical processes they can pass from one form to the other. We have already seen that there are frequently more ways than one of arranging in stable equilibrium a given number of electrons round a central positive core. If these arrangements are to explain the difference between the ous and -ic states of the elements, they must differ in the arrangement of the outer layer (a) because unless they did so there would not be sufficient difference in the chemical properties in the two states, and (b) because if the difference was only in the inner layers we could not affect these sufficiently by ordinary chemical operations to cause one configuration to pass into the other.

We should expect, I think, to find forms of the same kind of atom differing in their outer layers in those elements which are either in a group of homologous elements or in their immediate neighborhood. For in the atoms of such elements an electron hesitates, as it were, whether to go to the surface or to stay in one of the inner layers, i.e., it hesitates between two different configurations. It is reasonable to suppose that by suitable
inthences at the surface the electron might be induced to take one conse or the other and thus confer one valency or another on the atom of which it is an occupant. Now it is remarkable that many of the elements which are most conspicuous for the variability of their valency are either in the homologous groups or in their immediate neighborhood. Take, for example, chromium and manganese, which are the next neighbors of the iron groups, each of these shows great variations in valency in its different compounds, then molybdenum, the next neighbor to the ruthenium, rhodium and palladium group forms the series of chlorides $\mathrm{MoCl}_{2}, \mathrm{MoCl}_{3}$, $\mathrm{MoCl}_{4}$, and $\mathrm{MoCl}_{5}$; again tungsten, the next neighbor to the platinum and iridium group, forms the four chlorides $\mathrm{WCl}_{2}, \mathrm{WCl}_{4}, \mathrm{WCl}_{5}$ and $\mathrm{WCl}_{6}$, and nearly, if not quite, all of the elements in the homologous groups themselves form more than one series of salts. The electrons in the outer layers of elements of this type seem to be in a peculiarly sensitive condition and can move from one layer to another without much expenditure of energy.

The number of electrons which can be held in stable equilibrium in a single layer by a positive charge increases with the charge. Thus, though an inner layer of eight might be as many as the positive charge possessed by the lighter elements could stabilize, yet the heavier elements with their large positive charges might be able to stabilize more than this number. We should thus expect that at some stage in the list of elements the number of electrons in the inner layers would increase, that while when we pass from one element to the next and the number of electrons in the atom increases the additional electron stays in the inner layer instead of going to the one on the outside of the atom. When this process begins the change from atom to atom will not be the addition of an electron to the outer layer, but a reorganization of the distribution of electrons in the interior of the atom. The properties of the elements indicate that this process begins soon after passing calcium. To illustrate the point. I will take the series of elements beginning with titanium and consider the arrangement of electrons in it and the neighboring elements. I do not lay any stress on the actual numbers of electrons assigned to the inner layers; the determination of these would require much further investigation, both theoretical and experimental.

Titanium.-The distribution of electrons, if it followed the same course as in the lighter
dements, would be represented by $2,8,8,4$, the figures representing the number of electrons in the different layers starting from the inside; the four electrons in the outer layer would make the element quadrivalent. The existence of the tet rachloride $\mathrm{TiCl}_{4}$ shows that this distribution is one which occurs in nature. In addition to the tetrachloride there are the chlorides $\mathrm{TiCl}_{3}, \mathrm{TiCl}_{2}$, showing that forms of the titanium atom exist in which there are respectively one and two more electrons in the inside than in quadrivalent titanium, the distribution of electrons in the tautomeric forms may be represented by $2,9,8,3$, and $2,10,8,2$, respectively.

Vanadium.-If the electrons had followed the normal course, the arrangement of the electrons would be represented by $2,8,8,5$, and the element would be pentavalent. Vanadium is said to, form a pentafluoride $\mathrm{VF}_{5}$, so that this configuration would seem to exist. Vanadium forms chlorides $\mathrm{VCl}_{4}$, $\mathrm{VCl}_{3}, \mathrm{VCl}_{2}$, in which the inner layers of the atom must contain respectively one, two and three electrons more than the preceding. casc; thus we have atoms in which the arrangements are $2,9,8,4 ; 2,10,8,3 ; 2,10,9,2$, respectively.

Chromium. - If the electrons followed the normal course the arrangement would be $2,8,8,6$, and the element would be hexavalent; the compound $\mathrm{CrF}_{6}$ shows that this type exists. Chromium forms the chlorides $\mathrm{CrCl}_{3}, \mathrm{CrCl}_{2}$, so that in addition there are atoms of the type $2,11,8,3 ; 2,12,8,2$, respectively.

Manganese.-The normal arrangement would be 2, $8,8,7$. The fluoride $\mathrm{MnF}_{7}$ shows that this type exists. There are in addition the fluorides $\mathrm{MnF}_{4}, \mathrm{MnF}_{3}, \mathrm{MnF}_{2}$, corresponding to atoms of the type $2,11,8,4 ; 2,12,8,3$; $2,12,9,2$.

Iron, Nickel and Cobalt.-From the similarity of these elements we infer that the distribution of electrons only differs in the inner layer. Their halogen compounds are all of the type $\mathrm{FeCl}_{2}$ or $\mathrm{FeCl}_{3}$; suggesting the following distribution of electrons:

| Fe | $2,12,10,2.2,12,9,3$ |
| :---: | :---: |
| Ni | $2,13,10,2.2,13,9,3$ |
| Co | 2, 14, 10, 2. 2, 14, 9, 3 |

Copper.-The halogen compounds are of the type $\mathrm{CuCl}, \mathrm{CuCl}_{2}$, indicating atoms with one or two electrons, respectively, in the outer layer, corresponding to distribution of electrons represented by $2,14,12,1 ; 2,14,11,2$.

The normal process by which, when we pass from one element to the next in order of
atomic weight, the new electron goes to the outer layer seems to be resumed after passing copper, thus we have zine with two electrons in the outer layers; gallium with three; germanium with four; arsenic with five; selenium with six; bromine with seven, and krypton with cight.

Thus we see that as we proceed up the list of elements we may expect to meet with a batch of elements in whose atoms the electrons change from one tautomeric distribution to another with but little expenditure of energy. In this batel the ordinary progress of valency with atomic weight is interrupted, and the valencies are variable. On passing through the batch the regular sequence is resumed, the series goes on and ends with eight electrons on the outer laver, while the next scries begins with one in that layer.

Paramagnetism.-One very conspicuous feature of the elements from titanium to copper is that they are strongly paramagnetic. The quality of paramagnetism would on several theories depend on a want of symmetry in the arrangement of the electrons in the atom. This would be the case for example, in Parson's theory of the ring electron; it would also follow from the law connecting electrostatic and magnetic force which I suggested some time ago. ${ }^{26}$

If want of symmetry in the distribution of electrons is essential for paramagnetism, we can understand why it is confined to elements such as those we are considering, where the arrangement of the electrons in the inside of the atom may change, not merely from element to element, but even in a particular element under different external conditions. Outside such a group of elements the arrangement of the inner electrons does not change from element to element, it is very stable, and thus has probably a high degree of symmetry. It would. from this point of riew, be interesting to test the magnetic qualities of compounds like $\mathrm{Cr}_{6} \mathrm{~F}$ and $\mathrm{MnF}_{7}$, in which the readjustment of the inner clectrons has not taken place.

The researches of G. Wiedemann, Quincke, Townsend, Pascal, Weiss, Kamerlingh Onnes and others on the relation between magnetic properties and chemical composition have brought to light a great number of very striking phenomena, which are very diverse and in some cases anomalous, their very diversity, however, renders them all the more suggestive.

For salts in solution, and the same seems to be true for salts in the dry state, especially

[^84]if these contain water of erystallization, the value of $k$, the coefficient of magnetization, i.e., the quotient of the induced magnetization by the magnetic force, depends upon whether the metal is in the -ous or -ic state, but does not depend upon the acid radicle with which it is combined. Thus if a solution contains a definite amount of ferric iron the value of $k$ will be determinate. it does not matter whether the dissolved salt is ferric chloride, ferric sulphate or ferric nitrate. The same is true for the ferrous salts; again the value of $k$ depends only on the quantity of ferrous iron, but the value of $k$ for the same weight of iron will depend upon whether the iron is in the ferrous or ferric state. Thus if $W$ is the weight of iron in a cubic centimeter-
\[

$$
\begin{aligned}
& 10^{7} k=2660 W^{-}-.7 \text { for ferric salts. } \\
& 10^{7} k=2060 \mathrm{~W}-7.7 \text { for ferrous salts. }
\end{aligned}
$$
\]

In such salts as ferrocyanide of potassium where the iron appears on the negatively electrified part of the molecule, thus ${ }^{+} \mathrm{K}_{4} \overline{\mathrm{Fe}}$ $\mathrm{CN}_{6}$ ), the compound is not paramagnetic at all, but slightly diamagnetic. The ferrocyanide $\mathrm{K}_{3}\left(\mathrm{FeCN}_{6}\right)$ is slightly paramagnetic, although the paramagnetism is very small in comparison with that of the ferrous or ferric salts. Similar results are shown by the magnetic metals $\mathrm{Cr}, \mathrm{Mn}, \mathrm{Ni}, \mathrm{Co}$. Copper itself is diamagnetic as are also the cuprous salts; the cupric salts, however. are magnetic. The oxides and sulphides of the magnetic elements show large variations in their magnet ic properties, thus magnetite $\mathrm{Fe}_{3} \mathrm{O}_{4}$, which is regarded as a compound of FeO and $\mathrm{Fe}_{2} \mathrm{O}_{3}$, is much more magnetic than either of them, and a similar statement is true for the corresponding sulphur compouncis. Again variation in the temperature may produce great changes in the magnetic properties of an element, thus four types of iron, $\alpha, \beta, \gamma, \delta$, have been detected by Osmond and other workers; these pass from one into the other when the temperature passes through definite stages, and each of these types of iron has characteristic magnetic properties. In discussing the meaning of these results we must remember that on the view that paramagnetic properties are due to the setting of magnets, or their equivalents, under the action of a magnetic force: the magnetization, unless the field is intense enough to produce saturation (a state of things which is not attained with solutions), will depend upon two quite distinct things: (a) The resultant of the moments of the magnets; (b) the restoring force which tends to keep the magnets in the position of equilib-
rium. A substance may have a small coefficient of magnetization either because it contans few magnets or because the restoring force is very great so that a given extemal fiek produces but a small displacement of the magnets. Thus the difference between the coclicients of magnetization of ferrous and ferric iron may be due either to the difference of the magnetic moments of the magnets in the atom in the two states or to a difference in the restoring force. If it is due to a difference in the magnetic moments the intensity of magnetization when the ferrous iron is saturated will not be the same as when the ferric iron is saturated, whereas if it is due entirely to the difference in the restoring force the saturation magnetization will be the same in the two cases. We can distinguish between these effects by Weiss' Theory of Magnetons as the number of magnetons is proportional to the magnetic moment. The result of the application of this theory is that the number of magnetons per atom of iron in ferrous sulphate is 27 , in ferric it is 29 . As the coefficient of magnetization differs more widely than these numbers, it follows that the restoring forces must be different in the ferrous and ferric salts. In the iron in potassium ferrocyanide Weiss finds that there are only ten magnetons. The difference between the number of magnetons in the trivalent and divalent condition is more pronounced in chromium and cobalt than it is for iron, thus for trivalent chromium the number of magnetons is 19 , for divalent 25 , in trivalent cobalt the number is 17 , in divalent between 24 and 26 ; thus in both these metals the number of magnetons in the trivalent condition is less than in the divalent, whereas in iron the trivalent form is slightly richer in magnetons than the divalent. A very striking case of the variation of the number of magnetons with chemical composition is that of the oxides and sulphides of vanadium. Wedekind and Horst ${ }^{27}$ give the following values for $k$ the coefficient of magnetization and $n$ the number of magnetons in various compounds of vanadium.

|  | $k \times 10^{6}$ | $n$ |
| :---: | :---: | :---: |
| VO | 50.06 | 13.9 |
| $\mathrm{V}_{2} \mathrm{O}_{3}$ | 13.88 | 10.92 |
| $\mathrm{VO}_{2}$ | 3.73 | 4.19 |
| $\mathrm{V}_{2} \mathrm{O}_{5}$ | 0.86 | 2.99 |
| VS | 7.22 | 5.86 |
| $\mathrm{V}_{2} \mathrm{~S}_{3}$ | 8.95 | 10.00 |
| $\mathrm{V}_{2} \mathrm{~S}_{5}$ | 12.55 | 11.90 |
| VOCl | 27.16 | 13.18 |
| VN | 4.13 | 3.92 |

Thus the effect of oxygen is of the opposite character to that of sulphur, an increase in the oxygen content decreases, while an increase in sulphur content increases the number of magnetons.

Let us now proceed to sce how the magnetic properties of the salts of the magnetic metals are consistent with the following assumptions:

1. That the paramagnetism of these substances arises from the atoms of the paramagnctic element. Fe. Cr. Mn.
2. That the magnetic properties of these atoms arisc from a want of symmetry in the distribution of the electrons in the inner layers.
3. That the distribution of these electrons and therefore the symmetry of their arrangement can be affected by intense electric forces arising from atoms with their electrons in the neighborhood of the atom of the magnetic element, and that such forces may also affect the restoring force of the electrons in the atom, i.e., the force with which the system of electrons resists any displacement from their position of equilibrium.

We shall take in the first place the very large diminution in magnetic properties which takes place when the atom of the magnetic element is a constituent of a complex salt such as $\mathrm{K}_{4}\left(\mathrm{FeCN}_{6}\right)$ ferrocyanide of potassium. We may point out that this diminution may take place when the magnetic element occurs in a complex with the positive charge and not merely when as in $\mathrm{K}_{4}\left(\mathrm{FeCN}_{6}\right)$; the iron is a member of the negatively electrified group. Thus Feytis ${ }^{28}$ has shown that the following cobalt salts are diamagnetic- $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right) 6\right] \mathrm{Cl}_{3}$, $\left[\mathrm{Co}\left(\mathrm{N}_{3}\right) 5 \mathrm{Cl}^{2} \mathrm{Cl}_{2}, \quad\left[\mathrm{Co}\left(\mathrm{N}_{3}\right) 4 \mathrm{Cl}_{2}\right] \mathrm{Cl}\right.$ and $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{H}_{2} \mathrm{O}\right] \mathrm{Cl}_{3}$; though in all of these the cobalt atom occurs in the positively electrified portion of the complex molecule.

What is the condition of the atom of the metal in a complex salt? Let us take potassium ferrocyanide as an example, for similar considerations will apply to all the complex salts. In potassium ferrocyanide the iron atom has lost two electrons and is surrounded by 6 CN radicles, all of which are negatively electrified. Considerations of symmetry suggest that these negatively electrified radicles are at the corners of an octahedron and the iron atom at the center. The cyanogen radicles are, using Werner's notation, in the first zone with the atom of iron and are much more closely attached to it than are the atoms of potassium which are in the outer zone. Thus by the close proximity of the negatively
charged cyanogens, the atom of iron is exposed to an intense and very symmetrical field of force, and this would (1) give rise to a very strong, restoring force; this, if there were no change in the magnetic moments, would until saturation is approached reduce the magnetization. (2) From its symmetry this field tends to make the arrangement of the electrons inside the iron atom more symmetrical and thus reduces the magnetic moment. Both effects occur, the magnetization at ordinary temperature is reduced so much that it is not able to overcome the diamagnetism which iron, like all systems containing electrons, possesses; the number of magnetons is, according to Weiss, reduced to ten, which is only about one-third of the number in an atom of ferric iron. Let us now consider simple salts either in solution or which contain water of crystallization. Since these are electrolytes, the negative constituents of the molecule, such as $\mathrm{Cl}, \mathrm{SO}_{4}, \mathrm{NO}_{3}$, will not be in the inner zone with the iron or other magnetic molecule, but in the outer zone. Thus these negative constituents will exert but little influence on the iron atom, and thus its state and magnetic properties will be but little affected by the change of $\mathrm{SO}_{4}$ for $\mathrm{Cl}_{2}$ and so on. The molecules in the zone nearest to the iron atoms are water molecules; these are probably arranged symmetrically around the iron atom and it is also probable that there are six molecules of water in the inner zone. We may picture the atom of iron as at the center of an octahedron with the water molecules at its corners. As far as the geometrical arrangements are concerned, they are very similar to those of the ferrocyanide with water molecules in place of negatively charged eyanogen radicles. As the water molecules are as a whole uncharged, while the cyanogen ones are negatively charged, we should have expected the field of force to be much stronger with the cyanogen atoms than with the water mole-
cules, so that in the simple salt both the restoring force and the tendency to make the distribution of clectrons symmetrical would be less than in the complex salt. Thus both the magnetization and the mumber of matsnetons would be larger for the simple salt than for the complex one. In the salt where iron is trivalent, the iron atom will have lost three electrons; while in the divalent ones, it will only have lost two. Thus there is a difference in the number of electrons in the atoms; this might of itself be supposed to affect the magnetization. In addition to this, since the charge on the trivalent atom of iron is greater than that on the divalent, its attraction on the water molecules will be greater, these will be drawn closer into the atom and will be more favorably situated for influencing the arrangement of the electrons in the atom of iron.

In the case of the oxides the conditions are more complicated, we should expect as a general result that in these compounds the closer the connection between the iron and the atoms with which it was combined the lower would be the magnetization and that anything which tended to loosen these bonds would increase the magnetization. A loosening of these bonds would, however, increase the chemical activity of the iron by rendering it easier for it to enter into other combinations, thus we should expect to find correlation between chemical activity and magnetization, a connection which is brought to light very clearly by the experiments of Pascal. From this point of view we can understand a remarkable result obtained long ago by $G$. Wiedemann, viz., that the magnetic qualities of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ were increased by mixing with it $\mathrm{Al}_{2} \mathrm{O}_{3}$; the substances are isomorphous and may combine and form a compound in which the iron is not so firmly bound to other atoms as in $\mathrm{Fe}_{2} \mathrm{O}_{3}$.
(To be continued)

# Studies in the Projection of Light 

Part VII

# PARABOLIC MIRROR AND DISK SOURCE OF LIGHT (Cont'd) 

By FRANK BENFORI<br>


#### Abstract

$1_{11}$ this discussion of the characteristies of searchlight beams for ares and monoplane incandescent lamps, certain interesting rolations between the beam formation and mirror deformation are pointed out. These fotures have fombl practical application as has also the shop test methol for determining the focal position of the light subrec. Some test data on the measurement of beam widths are also given and it is shown that, with care in the testing, the measured width will come remarkably close to the computed value. The degree in wheth the beam formation can be controlled by moving the light source is discussed and curves are given by the help of which a complete analysis of any particular case can be carried out without going to the expense of an actual trial. A graphical method of determining the distribution of light is developed, and this method (like the one shown in Part lV) gives us information about those regions of the beam that have not been determined by the purely analytical methods previously employed. In the next article of the series, a variation of this method will be used to determine beam characteristics at relatively short range. It is in this particular case that analytical methods fail on account of their complexity and the relative simplicity of the graphical method makes it a useful working tool.-EDITOR.


## Testing Distance for Width of Beam

At distances which are adequate for a proper analysis of a searchlight beam, the beam width is, within certain limits, independent of the position of the are with respect to the focal point. The reason for this is the narrowness of the bundles of rays given off by the edge zones of the mirror. These rays must be swung through a considerable angle before they appear as edge rays and thus appreciably increase the diameter of the beam. It is therefore to be expected that measurements of beam diameter can be made with considerable accuracy even in the types of searchlights that have no mark or mechanism for locating the focal point.

As an indication of what may be expected from a $60-\mathrm{in}$. pure carbon arc searchlight without "focus finders" or other mechanical aids to correct focusing, reference may be made to the data points given in Fig. 59, where each point represents a reading of angular beam diameter at a radius of 2300 ft . plotted against the crater diameter measured after the carbons had cooled off. These data were collected during the development of a 200 -amp. electrode, and some of the earlier samples had rather poor operating characteristics, which increased greatly the difficulty of the photometry and added to the uncertainty of estimating the real diameter of oblique and uneven craters. These factors undoubtedly increased the scattering of the points, but if an average is taken of all points this average will be found to agree to within a few minutes of arc with the computed width, which should fall on the straight line in the diagram. The good agreement here is not the result of highly accurate focusing,
for in these tests the searchlight operator and trainer between them kept the are in focus by observing the general formation of the beam, more particularly in the central parts. If the beam width at this distance had been easily influenced by the adjustment of the electrodes, the difference between observed and computed widths would probably bs much greater.

The beam width, being almost wholly a function of the crater and mirror dimensions, and only in a slight degree dependent upon the focal adjustment, is an excellent datum point from which to compute the other beam characteristics. To obtain the testing distance for measuring the width of beam we can, therefore, most conveniently use the formula

$$
\begin{equation*}
L_{e}=\frac{114.6}{C \sin \frac{3 a}{2} \cos ^{3} \frac{a}{2}} F \text { inches } \tag{108}
\end{equation*}
$$

where $C$ is the observed width of beam in degrees, $F$ is the tocal length in inches, and $a$ is the angle from the axis to the edge of the mirror. The observed beam width $C$ at the range $L_{e}$ has an excess $E$ over the true beam width which may be computed by equation (107) or read from the curves of Fig. 60. There are certain test conditions under which the straight section between the mirror and true curved boundary may be encountered, and to guard against this happening it is often wise to determine the least safe testing distance in the same manner as was outlined for the spherical source. These safe distances are plotted in Fig. 61, and if used as a check on the curves of Fig. 60 they will insure the reality of the data of these latter curves.

The solid section of each curre of Fig. (i) may be used for are searchlights, in which the mirror must necessarily be limited to a useful are of $!!(0$ deg. from the axis. The dotted section is, therefore, useful only for monoplane incandescent lamps or similar light sources

The minimmon safe distance occurs for the ras from the edge of a mirror of fis deg. angle from the


Fig. 59. The crater diameter of a plane carbon arc is constantly undergoing changes during the burning of the electrode and while a single comparison of measured and computed beam diameter may fail to be consistent, as illustrated by the distance of some of the points from the computed line, a number of determinations even under adverse conditions will give an accurate average


Fig. 60. When it is necessary to make a beam test at relatively short range the measured beam width will exceed the true width by the factors given in this diagram, which should always be consulted first to make sure that the test deals with the true curved edge of the beam
to this plane. It may be thomght that determining the maximum width of the beam from the minimum width of the clemental image is perhaps not a logical proecess, and the real maximum beam width might be determined by some section of the elemental beam that extends farther from its own axis.

No analytic proof is here offered for the correctness of the solution in the meridian plane, but in Fig. 62 a number of elemental heam sections are drawn accurately to scale to illustrate how they overlap, and how the greatest distance from the axis of the beam is reached by the end of the minor axis of some particular elemental beam. The particular case chosen is that of a disk source of a radius of one per cent of the focal length, and the section through the beam is taken at the beginning of the curved edge boundary as determined by equation (10S) when the angle $a$ has the value 4.5 deg.

The circle A. Fig. 62, is a section of the elemental image from the center of the mirror. Ellipse $B$ is from the 30 -deg. point on the mirror, and it is removed from the center of the beam by the radial distance of that point. Ellipse $C$, shown dotted, is from the 45 -deg. point but it is overlapped very slightly by the elliptical beam from the $60-\mathrm{deg}$. point on the mirror. This overlap is due to the (i0-deg. beam forming what has been called the initial straight edge, which has been shown previously to be slightly outside the nodal point of the curved edge. The circle $E$ is drawn tangent to the outer end of the minor axis of the $60-\mathrm{deg}$. beam and it includes within it all of the elemental beams. The same would quite cridently be true if we had stopped at the $4.5-\mathrm{deg}$, or the 30-deg. point
axis. This does not differ much from the standard Army and Nayy mirror, which varies between 60 deg . and 65 deg . depending upon size.

A question might properly be raised as to the validity of the solution given for edge ravs when dealing with a disk source. The elemental images are (except for the one from the exact center of the mirror) elliptical in section with the small axis in the meridian plane in which all the computing has been done, and with the long axis at right angles

## Determination of Focal Position by Measuring the Beam Width at Short Range

The exchange of rays between the center and edge of the beam leads to the submergence of the initial edge rays and at relatively short range they are well within the boundaries, but before this occurs there are two uses at least to which we may put these rays from the edge of the mirror. The manufacturing processes of producing parabolic
mirrors has been redueed to a quantity basis， hat still there are variations of foeal length great enough to hate a serious effect on the beam．Some kind of test for focal length is therefore required，and about the most acourate and convenient nethod makes use of these edge rays．


Fig．61．When the mirror angle is greater than 45 deg．，the edge ray intersects the curved edge o the beam at a relatively sharp angle and measure－ ments of beam width at a range short of this point of intersection cannot be corrected by the data of Fig．60．The curves of Fig． 61 may be used to make certain that only the curved edge of the beam is involved in the width measure－ ment

As an example，let us take the case of a $60-\mathrm{in}$ ．mirror supposedly of 25 in ．focal length but actually of 25.25 in ．focal length．This is greater variation than is ordinarily found， but as will be demonstrated it indicates the order of accuracy of the test even when the original assumption of focal length is greatly in error．Also，in the following computations the value of $F$ is used just as if it were known， but the error in the final results from using $F$ ，the erroneous value，is not large enough to be of importance．

From equation（103）the beginning of the curved part of the beam edge begins at 3140 in．for a 0.54 －in．diameter crater and a focal length of 25 in．The curve of Fig． 60 also indicates that for this beam of 1 deg． 14 min ． width some 12.5 focal lengths，or 312.5 in ．will
be the distance of the beginning of the curved edge．Taking some distance considerably less than this，say 1200 in ．so as to be certain of dealing only with the particular edge rays we want，the computed width of the beam $W_{e}$ e is from equation（5．5）and（104），using $a=30 \mathrm{~d} \mathrm{cg} .$,

$$
\frac{W_{e}}{2}=34.0 . \overline{5} \text { inches. }
$$

If a target having a cirele of 34.0 .5 in ．radius drawn upon it is erected at 1200 in．from the searchlight and the beam is directed upon it， the beam radius when the are is at the 25 －in． position will be about 44.45 in．radius．When the are is moved forward to bring the beam diameter down to the diameter of the circle， the relative rates of motion will be some 41.6 to one，that is，a movement of one inch along the axis gives a movement of 41.6 in．across the target．This ratio is not quite exact （F not being known exactly），but if the crater is advanced until the beam has the diameter of the circle，the focal point will be deter－ mined to within a few hundredths of an inch． The mirror angle instead of being 60 deg．as assumed is exactly 61 deg． 22 min．，and if the value is used in connection with the true focal length of 25.2 .5 in ．，the diameter of the circle should be 34.55 in ．The difference between


Fig．62．The location of the $0,35,45$ ，and $60-\mathrm{deg}$ ． elemental images within the beam limits of a $60-\mathrm{deg}$ ．mirror beam shows the end of the minor axis of the $60-\mathrm{deg}$ ．（ellipse $D$ ）image lies at the beam limits．For images from greater mirror angles，this will no longer be true
this value and the 34.05 －in．circle is 0.50 in ． and dividing by the ratio 41.6 the result 0.01 in ．indicates the degree of approach to the true foeal point．The error in the final determination is only one twenty－fifth of the original error made in assuming the focal length to be 25 in ．The method is thus
accurate enough for shop practice, and on account of its simplicity it is to be preferred to other more complicated methods such as mechanical measurements on the mirror or photometric explorations of the beam.

Truing the Mirror Ring by Observing the Beam Formation at Short Range
It sometimes happens that a searchlight mirror, monnted in a searchlight, becones deformed due to stresses set up in shipping or by rough usage. This deformation is ordinarily not visible either in the mirror or in the beam, and while there is a great loss of central intensity the condition of the mirror may entirely escape attention. If the beam is directed normally against a wall at short range, sar at 100 ft . as in the previous section, the beam outline will be observed to deviate from a circle. If now the normal diameter of bean for that range is computed and a circle is accordingly drawn on the wall, the extent of the deformation can be accurately determined and proper steps taken for its correction. The edges of the mirror may be forced forward or backward slightly at various points by adjusting the


Fig. 63. The sensitiveness of the beam to focal adjustment is illustrated by the drop in central intensity when the beam is spread from 2 to 3 deg . in total width. At the same time there is a considerable increase in the light in the beam proper
packing or applying force to the mirror ring, and it is a comparatively simple operation to make the beam a true circle. With the outer zone of the mirror in true alignment there is not much possibility of the more central parts having any deformation that was not there before mounting.

## Movement of Source

The practice of throwing the are out of focus to widen the beam is not so common as it is in incandescent service, but there are occasions when a spread are beam is useful. There is a considerable difference in the reactance of the beam to a movement of the are, but if we consider the physical surroundings of the crater these differences are readily understood.


Fig. 64. The region surrounding the crater that contributes light to the beam is always a circle providing the crater is circular. This circle has a fixed diameter equal to the maximum diameter of the beam, and hence covers a greater region as the beam is expanded

The trpical incandescent lamp used for proiection purposes has a rather definite outline and, aside from the image formed by the bulb which may not exactly coincide with the filament, the intensity of the source is zero at points just outside of the filament. In the case of the arc there is no definite outline to the source, for while there is a very sharp and distinct drop in brilliancy at the edge of the crater, still the light radiated from the regions surrounding the crater may amount to a considerable part of the total radiation. To enumerate, there are the glowing outside walls of the positive electrode, the hot tip of the negative electrode, the violet arc stream between electrodes, and the flame above the crater. Which often attains considerable size and brilliancy.

As the crater is mored away from the focal point the first result is a rather sudden
deconase in central hemm intensity as ilhastrated by curves A and $B$ of Fig. (i:3. 'This dererase makes the point where the intensity falls 10 bo per cent of the new maximum move ontward from the axis, amd the additional light so inchaded raises the measured beam flux. 'Thus in the curves of ligg. (6:) the sharply


Fig. 65. This diagram illustrates how the light source may be moved either way along the axis without changing the central beam intensity providing the mirror does not extend to 90 deg. from the axis. If the mirror contains a 90 -deg. zone, any movement away from the focal point will cause a loss of intensity in the center of the beam
focused beam had 7.5.390 lumens against $9+400$ lumens in the 5 -deg. beam.

The three sketches of Fig. 64 are intended to illustrate the manner in which the region surrounding the focal point contributes light to the beam. The beam diameter is really fixed, for a focused arc, by the light from the center of the mirror. Let us say that the crater subtends an are of 2 deg. from this position, so that sketch $A$ of Fig. 64 will correspond to curve A of Fig. 63. Measuring from a point near the rim of the mirror a - -deg. circle will exceed the crater in size and will include a certain amount of light from the side of the electrode, and from the arc stream and the positive flame.

When the crater is thrown out of focus the circle surrounding the area of useful light expands in the same proportion as the beam boundaries and more light from the surrounding regions is included as will be seen from the sketches corresponding to curves $B$ and $C$.

It is not necessary to advance the crater toward the mirror in order to secure this increase of flux, for practically the same results are obtained by drawing it back from the mirror. In this case the arc stream and the tip of the negative contribute more and the sides of the positive less.

Returning again to the idealized crater or disk source, Fig. 65 , the distance through which
it can le moved along the axis without decreasing the central beam intensity is

$$
\begin{equation*}
n= \pm r \cot a \tag{109}
\end{equation*}
$$

where a, the mirror angle, is never more than (0) deg. Where the mirror contains a $90-\mathrm{deg}$. \%one, the disk must remain coincident with the focal plane regardless of any movement allowed by other zones.

In Fig. 66 the angle of spread $e$ is given approximately by

$$
\begin{array}{r}
\tan c=\frac{(S \sin a \mp r \cos a)}{p}= \\
\frac{(S \sin a \neq r \cos a)(1+\cos a)}{2 F} \tag{110}
\end{array}
$$

This spread is for any selected angle $u$, but there will be some particular angle or angles that will give a maximum spread.

Applying the method used to derive equation (62) for the spherical source, we have

$$
\begin{gather*}
L_{e}=\frac{d y}{d(\tan e)}= \\
2 F^{2} \sec ^{2} \frac{a}{2}  \tag{111}\\
\frac{S(\cos a+\cos 2 a) \pm r \sin a(1+2 \cos a)}{i} \tag{inches}
\end{gather*}
$$



Fig. 66. The ray of maximum divergence originates on the edge of the crater that is farthest removed from the focal point, but the point on the mirror at which reflection takes place must be solved for as it varies with the relative size of the movements along the axis as compared with the radius $r$ of the source
and as we are interested only in the limiting width when $L_{e}$ is infinity, the denominator of (111) may be set equal to zero, giving the relations between the zone $a$ that gives the maximum spread and $S$ and $r$.

$$
\begin{equation*}
s= \pm r \sin a \frac{1+2 \cos a}{\cos a+\cos 2 a} \text { inches } \tag{112}
\end{equation*}
$$

This equation does not contain the focal length as a direct factor and, therefore the relative size of $r$ to $F$ does not change the zone at which the maximum divergence occurs. This is not the exact fact of the case, but is a result of the simplified expression used for the angle $\varepsilon$. The results are sufficiently close for practical use, as it has been found in the case of the spherical source that a relatively wide mirror zone gives the same angle of spread as elosely as can be measured, and an accurate determination of angle $a$ is not necessary.

Equation (112) is plotted in Fig. 67 which must be used with the foregoing limitation in mind; that is, the source must not be large, say not over 0.1 F , and the morement $S$ must not be over 0.3 F . These limits are well beyond ordinary practice.

The curves of Fig. 67 may be used in connection with equation (110) to compute the maximum spread of a searchlight when the lamp is moved to the limit of its travel. The following question was recently asked: How wide is the beam from a 24 -in. mirror of $1 . \mathrm{in}$. focal length when the lamp is moved 2.5 in. toward the mirror, or $1 .)$.in . away from the mirror? The radius of the crater is 0.27 in .

We are dealing with an are and it is obriously only angles on the mirror of less than 90 deg. that have any significance. For the position toward the mirror the ratio of $S$ to $r$ is 9.26 . The curve in the lower left corner of Fig. 67, when produced, indicates a mirror angle of some 55 deg . This particular mirror extends only to 43 deg., so the maximum spread will be found in the rays reflected from the extreme edge of the mirror.

Substituting numerical values in equation (110), the half width is found to be 6 deg. 30 min . or a total width of 13 deg . for the position toward the mirror and $\delta$ deg. total width for the position away from the mirror. Without the use of Fig. 67 it would be necessary to explore the mirror, either graphically or analytically, or perhaps run a test in order to arrive at the angle of maximum spread.

## First Graphical Method of Obtaining the Beam Characteristics <br> Circular Elemental Images

The graphical determination of the arc beam depends on a simplification of the ele-
mental images in order to arrive at a working method. This simplification does not adversely influence the ultimate accuracy of the results and it does make it possible to reduce a difficult problem to simple terms. This particular method has been used by the author for eight years and has yidded excellent results in the buikding up, of the searchlight beam from the brilliancy data of the crater. The synthetic beams so computed have been an excellent check on the beam tests and where disagreements have appeared there has always been found some physical explanation in either the searchlight or the test. As will be explained more


Fig. 67. There are two mirror zones, one below 60 deg . and the other above 60 deg., that give the ray of maximum divergence when the disk source is displaced from the focal position
in detail later this circular elemental image gives its best results for mirrors of less than 90 deg . angle. Deeper mirrors require that attention be given to some of the details that are omitted in developing the circular image.

From the center of the mirror the crater appears circular and the projected elemental beam is also circular and of the same angular width as the crater. From a point in the $60-$ deg. zone of the mirror, the crater appears to be elliptical in form with a minor axis half the length of the major axis. The projected beam has the same proportions and is also reduced in all dimensions inversely as the length of the line from mirror to focal point. The solid angle subtended by the crater as viewed from the $60-\mathrm{deg}$. point is only 0.28 of the solid angle from the center, and the projected beam suffers the same reduction in size.

If the light is reflected from a small section of mirror in the 60 -deg. zone directly above
or below the are, the projected elliptical beam will have its major axis horizontal; a mirror section on either side of the mirror will give a beam with a vertical major axis; and intermediate mirror points will give intermediate directions to this axis. At sufficiont distances these elliptical sectioned beans will overlap as in Fig. (is where six such beams are superimposed. The eentral area which is


Fig. 68. Diagram showing how the elliptical shaped elemental beams from the edge of the mirror overlap, giving a central circular region of full intensity
covered by all six beams is a circle having a diameter equal to the minor axis, and going outward on a radial line the number of beams on successive points will be found to be 5,4 . 3,2 , and 1 , reaching zero at the outer circle of radius equal to the major axis.

The difficulty of exactly summing an infinite number of such ellipses corresponding to the infinite number of points around the circumference of a mirror zone is fairly obvious, but ordinarily there is small need for such a solution for we may represent any
single ellipse by a circle of equal area, as in Fig. (69, and the infinite number of circular beams will immediately add to a single beam of edpual diameter and the proper intensity. The summation of the circular beams from the varions mirror zones can then be carried out in a mamer similar to the method employed for the spherical light source. The only difference between the two sources is that the elemental beam diameter of the disk source is reduced by the square root of the cosine of the mirror angle $a$; and in terms of the focal length $F$ and the radius $r$ of the source, the elemental beam width is

$$
\begin{equation*}
C_{\text {are. }}=\frac{57.28 r}{F}(1+\cos a) \sqrt{\cos a} \tag{113}
\end{equation*}
$$

The intensity of the beam is determined by the brightness $B$ of the source, the cocfficient $k$ of the mirror, and the projected area of the zone, as given by equation (79).


Fig. 69. Diagram showing how the ellipses are reduced to equivalent circles for making the graphical solution for the beam

The summation of zone images is illustrated in Fig. 70, where the rectangular areas represent zonal beams, the dimensions of which are given in Table IV. The narrower zonal

TABLE IV
ZONE AREAS AND IMAGE WIDTHS
Unity Focal Length and Disk Light Source of Radius $r=\frac{F}{100}$

| zone boundaries |  | Mid Zone a | Projected Area |  | Radius $p$ | $\sqrt{\cos a}$ | image radius |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| From | To |  |  | Total |  |  | Degrees | Per Cent |
| $0^{\circ}$ | $10^{\circ}$ | $6^{\circ} 40^{\prime}$ | 0.096 | 0.096 | 1.004 | 0.996 | $0^{\circ} 34.1^{\prime}$ | 99.0 |
| $10^{\circ}$ | $20^{\circ}$ | $15^{\circ}$ | 0.295 | 0.391 | 1.018 | 0.983 | $0^{\circ} 33.2^{\prime}$ | 96.7 |
| $20^{\circ}$ | $30^{\circ}$ | $25^{\circ}$ | 0.512 | 0.903 | 1.049 | 0.952 | $0^{\circ} 31.2^{\prime}$ | 90.7 |
| $30^{\circ}$ | $40^{\circ}$ | $35^{\circ}$ | 0.762 | 1.665 | 1.100 | 0.905 | $0^{\circ} 28.3{ }^{\prime}$ | 82.3 |
| $40^{\circ}$ | $50^{\circ}$ | $45^{\circ}$ | 1.064 | 2.729 | 1.172 | 0.841 | $0^{\circ} 24.7^{\prime}$ | 71.8 |
| $50^{\circ}$ | $60^{\circ}$ | $55^{\circ}$ | 1.455 | 4.184 | 1.271 | 0.757 | $0^{\circ} 20.5^{\prime}$ | 59.6 |
| $60^{\circ}$ | $70^{\circ}$ | $65^{\circ}$ | 1.972 | 6.156 | 1.405 | 0.650 | $0^{\circ} 15.9^{\prime}$ | 46.3 |
| $70^{\circ}$ | $80^{\circ}$ | $75^{\circ}$ | 2.697 | $8.85: 3$ | 1.588 | 0.509 | $0^{\circ} 111.0^{\prime}$ | 32.0 |
| $80^{\circ}$ | $90^{\circ}$ | $85^{\circ}$ | 3.713 | 12.566 | 1.839 | 0.295 | $0^{\circ} 5.5{ }^{\prime}$ | 16.0 |
| $90^{\circ}$ | $100^{\circ}$ | $95^{\circ}$ | 5.290 | 17.856 | 2.189 | 0.295 | $0^{\circ} 4.6^{\prime}$ | 13.5 |
| $100^{\circ}$ | $110^{\circ}$ | $105^{\circ}$ | 7.794 | 25.650 | 2.699 | 0.509 | $0^{\circ} 6.5{ }^{\prime}$ | 18.8 |
| $110^{\circ}$ | $120^{\circ}$ | $115^{\circ}$ | 12.045 | 37.695 | 3.461 | 0.650 | $0^{\circ} 6.5^{\prime}$ | 18.8 |

beams come from around the $90-$ dey. position on the mirror and the beams from higher angles are wider. The two upper zonal beams in the illustration are scen to overlap the beams from the $80-$ to $90-$ and $90-$ to $100-$ deg. zones. In making the graphical summation the overlapping parts are brought down to make contact with the rectangles below. When this has been done the images pile up


Fig. 70. The zonal images from a disk source are widest for the 0 -deg. zone and for a zone slightly above 90 deg. The $90-$ deg. zone gives a minimum width and a second minimum may occur if the mirror angle extends to beyond 120 deg . To the left of the center line the rectangles representing the intensities and widths of the zonal images are piled on top of one another so that some of the upper ones overhang smaller ones below. On the right, the overhanging parts are slipped down to make contact with the rectangles below
as on the right of Fig. 70, and the characteristic curve can now be drawn through the middle of the steps formed by the rectangles.

The peak of the curve is known to be a point when the mirror contains a $90-\mathrm{deg}$. zone as it has already been pointed out that such a mirror does not have an inverse-square region or a crest on the beam. If the mirror stops short of 90 deg. the width of crest can be found by the equations developed when discussing the inverse-square region of the disk source beam.

The dotted curves give the beam characteristics of the same mirror ( $F$ constant) reduced to 90 deg. and 60 deg.

In Fig. 71 are drawn the beams from three mirrors of equal diameter and variable focal
length and having disk sources of 0.01 the focal length of the 120 -deg. mirror. These characteristic curves were derived directly from Fig. 70 by increasing the peak intensities to a common value as called for by the common projected area of the threc mirrors and reducing the widths inversely as the focal lengths.

The general relations here exhibited are the same as found for the spherical source,


Fig. 71. Three mirrors of equal diameter but different focal length give equal central intensities but different beam widths. The sharp point to two of the characteristic curves indicates the presence of the 90 -deg. zone in the mirror.
but the differences between the three are somewhat increased. The wide angle mirror gives a wide beam, but the distribution of light is such that its usefulness is rather limited. It might be used, for example, for lighting a group of statuary in which the central figure is to be brought out with especial prominence, but for searching or illuminating difficult targets the wide zone of low intensity around the edges makes it distinctly inferior to the clean-cut beam from the narrow angle mirror. It is for this reason that so many incandescent lamps of the monoplane type have shallow mirrors rather than deep ones, and it is only in the case where volume of light is more important than uniformity that the deep mirror is to be desired.
(To be continued)


## LIBRARY SECTION

Condensed references to some of the more important articles in the technical press, as selected by the G-E Main Library, will be listed in this section each month. New books of interest to the industry will also be listed. In special cases, where copy of an article is wanted which cannot be obtained through regular channels or local libraries, we will sug. gest other sources on application.

## Alternators

Waterwheel Generators and Synchronous Condensers for Long Transmission Lines. Smith, M. W.
A.I.E.E. Jour., Sept., 1923; v. 42, pp. 894-903.
(lllustrated paper on design and operation of such machincry.)

## Ball Bearings

Approach of Flat Elastic Plates Under Load when Separated by a Ball of Similar Material. Goodman, John.
Engng., Aug. 24, 1923; v. 116, pp. 244-246.
(Results of tests to determine the load-carrying capacity of balls.)
Brakes, Dynamic
Compound Characteristics in Regenerative Braking with Direct-current Traction. Say, M. G. and Frampton, H. G.
I.E.E. Jour., Aug., 1923; v. 61, pp. 863-868.
("Deals with a particular form of regenerative braking for d-c. trains, effected by application of a differential compound field excitation to the traction motors.")

## Condensers, Steam

Testing Jet Condensers. Long, L. Power, Aug. 21, 1923; v. 58, pp. 293-296.

## Eddy Currents

Eddy Currents in Iron Masses. Rosenberg, E. Elec'n, Aug. 24, 1923; v. 91, pp. 188-191.
(On the theory of eddy currents.)

## Electric Control Systems

System of Coal and Ore Bridge Traverse Control for Protection Against Wind and Skewage Hazards of Skew Type Direct-current Bridges. Canney, P. R.
Assoc. Ir. \& St. Elec. Engrs., Sept., 1923; v. 5, pp. 425-447.
Electric Drive-Foundries
Complete Electrification of the Foundry Industry. Egan, Leonard W.
Assoc. Ir. \& St. Elec. Engrs., Sept., 1923; v. 5, pp. 381-424.
(Considers drive of various kinds of foundry machinery, electric welding, electric melting furnaces and core ovens, electric cranes, etc.)
Electric Drive-Hoisting and Conveying
Single Bucket Blast Furnace Skip Hoist Characteristics. Cummins, A. C. and Leavitt, A. R.

Assoc. Ir. \&o St. Elec. Engrs., Sept., 1923; v. 5, pp. 449-466.
(Discuisses the following types of equipment: single-motor d.c., double-motor d.c., singlemotor a.c., Ward-Leonard a.c. or d.c.)

Electric Drive-Power Plant Auxiliaries
Drive of Power Station Auxiliaries. Breach, L. and Midgley, $H$.
I.F.E. Jour., Aug., 1923; v. 61, pp). 829-862.
(Deals with seven alternative schemes for supply of power to auxiliaries.)

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Motor Operater Centrifugal Pumps in Steel Plants. Cornwell, B. $\Lambda$.
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(Selection of equipment, operating costs, etc.)

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Adjustable-speed Motors for Driving Non-reversing Rolling-mill Trains. Bauer, Hellmut. (In German.)
Elek. Zeit., Aug. 9, 1923; v. 44, pp. 753-757.
(Pays special attention to three-phase induction motors.)
Reversing Mill Drive at Messrs. Cammell Laird \& Co.'s Penistone Works.
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Capacities of Electric Melting Furnaces. Brooke, Frank W.
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(Short article on selection of correct furnace.)
Electric Furnace Phenomena. Moore, Edward T. Assoc. Ir. © St. Elec. Engrs., Sept., 1923; v. 5, pp. 529-582.
(Results of extensive tests.)

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Some Experiments Illustrating the Electrical Properties of Neon Lamps. Coursey, Philip R.
Wireless Wld. \& Radio Revi, Aug. 22, 1923; v. 12, pp. 700-704.

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Art of Sealing Base Metals Through Glass. Houskeeper, William G.
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(Describes different methods of making successful seals between glass and base metals.)

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Wave Meter as a Substitute for the Oscillograph. (In German.)
Elek. Zeit., Aug. 9, 1923; v. 44, pp. 757-758.
Electric Motors-Starting Devices
Method of Starting Two-phase Motors. Hill, Norman B.
Elec'n, Aug. 31, 1923; v. 91, pp. 212-213.

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Relative Air Density in High-voltage Testing. Doyle, E. D.
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A.J.E.E. Jour., Sept., 1923; v. 42, pp. 891-893. (Short paper dealing with design methods.)

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Making Iron from Ore by a New Electrolytic Process. Kreutzberg, E. C.
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(Description of the plant and processes of the Milford Electrolytic Iron Co., Milford, Conn.)

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Aligning a Frequency Changer Set.
Power, Aug. 21, 1923; v. 58, pp. 298-299.

## Grounding

Present Day Practices in Grounding of Transmission Systems.
A.I.E.E. Jour., Sept., 1923; v. 42, pp. 928-946.
(First report of the Sub-committee on Grounding of Systems of the Protective Devices Committee of the A.I.E.E.)

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Design of Inductances for High-frequency Circuits. Fortescue, C. L.
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(Methods of testing iron and steel for physical and mechanical properties.)

## Insulating Oils

Purifying Transformer Oils.
Elec. IVld., Aug. 18, 1923; v. 82, pp. 338-339.
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How to Get Uniformly (iond Results with Fisulat ing Varnishes. Stringham, ․ W'
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Electrical Loud Speakers. Nyman, A.
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(The first of a series of articles on distortion. This installment treats of distortion in high frequency circuits.)

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| International Paper Company |  |  | 213.5 | Dryden Paper Company, Limited | 1400 2500 | 29 25 |
| (Sherman Island Development) | 1 | 10000 | 66 | Spruce Falls Company, Limited ${ }_{\text {East Kootenay Power Company }}$ 2, | 2500 7500 | 25 190 |
| Adirondack Power \& Light Corp. <br> (Spier Falls Development) | 1 | 9000 | 66 80 | East Kootenay Power Company Northern Ontario Light \& Power Co. | 7500 3300 | 190 305 |
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| Great Northern Paper Company (Anson Plant) | 4 | 1500 | 20 | Montreal Light. Heat \& Power Cons. <br> (Cedars Plant) | 1500 | 30 |
| Western New York Utilities Co. | 1 | 3160 | 79 | Price Bros. \& Company, Limited I | 11000 | 72 |
| Washington Water Power Co. |  |  |  | Howard Smith Paper Mills, Limited 2 | 350 | 8 |
| P (Long Lake Station) | 1 | 22500 | 168 | Hydro-Electric Power Commission of Ontario |  |  |
| Pennsylvania Water \& Power Co. |  |  |  | (Queenston Chippewa Development) 3 | 58000 | 294 |
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CHARLES PROTEUS STEINMETZ
1865-1923
His life was a service to mankind;
His death, a sorrow to the world


## STEINMETZ

By the time our readers receive this copy of the Review the sad news of Steinmetz's death will be a month old and most of them will have read some of the splendid tributes that have been paid to his great genius. Almost every paper in the land, and many of our foremost men, as well as our foreign contemporaries. have done him homage and we feel that it is a peculiarly hard task to add a fitting tribute.

So, recognizing our own inability to do the justice we should wish to the memory of this great man, we reproduce elsewhere in this issue an address delivered by Mr. E. W. Rice, Jr., at a memorial service held in Schenectady, on the evening of October 31st. Of the many tributes we have read there is none more authoritative or more fitting than this.

On the day of Steinmetz's death Mr. Martin P. Rice prepared a hurried address which he broadcast from WGY in the evening. We also reproduce this on account of the many pleasing personal touches.
As our readers know, Steinmetz was a great friend of the Review and made many notable contributions to our columns, and, therefore, his loss will be an especially sad blow to us. But, at the same time as we mourn his death, we wish to rejoice at his life's work and to emphasize the fact that his achievements are destined to live forever as a perpetual tribute to his genius and as a lasting benefit to mankind.

Steinmetz was a peculiarly fortunate man in living such a useful life, because his strength lay in a great intellect, capable of clear and logical reasoning, with a natural bent for pure mathematics. His usefulness was based on his derotion of these high gifts to the solution of some of the most difficult problems confronting the electrical engineer. Had he been a rich man, and could he have followed his own bent in his own country, there is little doubt that he would
have applied these gifts to the pursuit of pure mathematics. Had he done this it is possible that he might have lived and died almost unknown or, at least, known only to a few intellectuals and instead of the splendid contributions he has left us these might have been confined to a few papers, left on the dusty shelves of some museum or in the archives of some scientific societies, on such abstruse subjects as Poly-Dimensional Space and the Fallacy of Ether. Such papers have their value in stimulating the imagination of those who can read them, and, by a process of mental gymnastics, of exercising the mind of the writer, but they could never be compared with the contributions we have received from Steinmetz' brain.

The whole world knows the parable of the sower and how easy it is for some seed to fall on stony ground. And the world owes much to the fact that this giant mind in a frail body found a congenial soil in which to grow and flourish. It was indeed fortunate that this young immigrant of 1889 was not turned back at the gates of his land of promise and opportunity, and it is equally fortunate that he found, in his first place of employment, those who recognized his ability and guided his talents into fruitful channels. His coming into the organization of the General Electric Company at so early a date was a benefit alike to him, to the country, and to the wide world.

Steinmetz himself considered as his most useful work
(1) His investigations on magnetism.
(2) The development of his symbolic method of alternating-current calculations (complex quantities).
(3) His general theory of electrical transients.

Concerning his investigations on magnetism the whole scientific and engineering world
knows his famoms Law of llysteresis, amd man! know of some of his other notable masestigations in this direotion, but few, Who were not intimately familiar with contomporary engincering. ean know or appreciate what this work did for the world electrical. Aow had learned how to build dymamo-eleetric machines, transfommers, ofe, but they only knew bow to buikd them bỵ a cut and try method. Their knowledge was qualitative and not quantitative, and as Kelvin said "anyohing becomes a science only when we can measure it." Stemmety laught us how to ealculate the magnetio cirouit and thas at once gave us the useful, efficient electrical machine. We know no words that can exagrerate the importance of this work to a then infant industry, and the far-reaching benefits it has conferred on the general public will remain largely unknown by them.

It is still harder to form an adequate conception of the value of his Symbolic Method of Calculating Alternating Currents. Most mon. who had attompted to calculate alter-nating-current phenomena became confused. It would harlly be an exaggeration to say that Steinmetz did for alternating-current calculations what the immortal genius of Newton had done for mechanical laws three centurics earlier-he brought order out of chaos. He put a tool into the hands of other men which enabled them to work successfully in a field which hitherto had been too strewin with rocks to plant.

His symbolic method so simplified the treatment of many complicated phenomena that its use soon spread. First it became generally used in America, and then the whole world adopted it. He advanced the progress of civilization by this contribution to our knowledge. To what degree this work brought forth useful fruit will always be unknown, but will probably always be underestimated. When the work of one genius enables an unnumbered host to do more fruitful work the result is something like a snowball rolling down hill; it gets bigger and bigger. Who can determine how long it will roll: Who can determine how great it will become?

It was largely by the results of this work of Steinmetz that the path was made clear for transmitting large alternating-current powers over long distances. These accomplishments stimulated his dream that some day the country would be covered with a veritable network of high tension transmission lines, which would transport electric energy to
cever corner of the land in the same way as our railways eonvey materials.

With the growth of transmission lines, "our ohl encony, lightning" (using his words) beeame a terror to the electrical engineer. Steinmet\% with characteristic energy sturlied the phenomena of lightning and propoumeled his General Theory of Electrical 'Transients. In brief, he founcl that it was not the actual stroke of lightning that did the most damage, but the great brief surge, or transient, as he termed it, which was prodlaced by the machines in circuit, when they get out of control due to the lightning stroke. With this knowledge he tackled the problem of protecting transmission lines and machines against lightning and its attendant transients, and the modern lightning arrester is largely the result of his work.

The name of Steinmetz could be conjured with, and as is only natural it was the spectacular elements in some of his undertakings that fired the imagination of the public, rather than the true significance of the work.

His lightning generator thrilled a continent and he was heralded as the wizard of Schenectady, who had outdone Jove in making lightning bolts. But his lightning generator was no instrument of destruction; its purpose was to teach us means and ways of making apparatus to protect against lightning.

The great work that Steinmetz was so busy on during the last few years of his life and up to the time of his death, was a study of the mechanism of electric breakdowns in air, oil and solids. He himself thought that the importance of this would outrank most of his other work. He was trying to determine just what happens at the instant of a breakdown when the insulation fails; and his lightning generator was the instrument he was using to create the high powered transients he needed for experimental purposes in the design of lightning-proof, and transientproof apparatus.

Steinmetz was above all things a mathematical genius, and Steinmetz the mathematician was greater than either Steinmetz the inventor or the author. But he has some 200 patents to his credit, which might well make many other inventors envious; while his books on electrical subjects are the textbooks of the world.

As a teacher it is hard to place himonly because it is difficult to reach the height. His life would still have been well spent had it been devoted to teaching. His clearness
of vision and precision of thought were brought out to the nth degree when explaining complicated problems to minds less brilliant than his own. WVe know no one who conk explam a problem in as few words as Steimmet\%. His value as a teacher will never be eomputed. He taught others the fundamentals of mechanical as well as electrical engincering, and again his pupils taught yet others, and so on. He took a keen interest in education in general. He was a power in educating others and at the same time a power among educators. If we take a seed and dropl it in the ground and then take all it produces and plant again, and so on, for a period of years, who can estimate the value of the original seed? So it is with the value of Steinmelz' work as a teacher-we cannot estimate it.

As a lecturer he had few equals. The English language was not his own, but his clearness of expression, his conversational delivery, and his charm of manner endeared him to his audience. The public came to learn and coming leamed to love.

Had we the wit and wisdom we would try to tell you something of the Man, Stein-metz-as well as touching on him as the mathematician, scientist, engineer, inventor, teacher and lecturer, but we feel that we must leave this to a more ready pen.

However, we have many pleasant recollections of the Man. We remember some years ago dropping in oneevening to have a chat with "The Doctor." He took us to his conservatory which was filled with cacti and strange creatures, and we remember now the interest with which he talked on the struggle for life in the desert. We had seen the cactus growing in its own native wildness in the deserts of New Mexico, Arizona and California; and had met the Gila monster in its own home, in that most uncharitable of all spots, the Apache Trail. So we could appreciate his interest in the great struggle to surrive, and how such ugly things as the poison of the rattlesnake and of the Gila monster, and the spinie of the cactus were necessary weapons to protect life in such a seemingly unfair fight.

And, as we looked at the Doctor, we could but realize that, with all his brilliancy, there must have been a great barren space in his own life. As the little cripple boy of Breslau and as the young man, he must have realized, as his mind unfolded.
that many ehapters in a complete life must forever be closed to hims. 'The jonftul spirit of gouth, which he maintamer io such an extraordinary degree all thronght life eonld find nos outlet in athletic sports, and the handicap that was phaced upon him from the start prevented a lower of chilitren froms marrying and having a family of his own.

Many minds less noble than the Doctor's would have cultivated the poison of the serpent and the spine of the cactus in such a struggle. But not he. And herem lies the greatest triumph of his life. He chose love instead of renom as a weapon. He turnerl his barren spot into an oasis and planted it with flowers. And like the blossoms of the cacti in the desert, the flowers he planted were more beautiful than the lily and more fragrant than the rose; because they grew where only God knew flowers could grow. To the man in a desert one bloom, unfolding its petals to heaven, is more precious than unnumbered roses in a garden. In the one place you expect flowers, in the other thorns.

The Doctor adopted a son who lived and raised his family in the Doctor's home and his son's children were as his children.

It was a character that could thus turn defeat into victory and build a home of love upon a quicksand that made Steinmetz one of the unique figures in history. The public who did not and could not understand his work regarded him as their idol. He was respected and lored by more than one continent. He added lustre to the fame of the town he lived in and honor to the country he adopted.

In the fulness of his greatness he loved chil-dren-and children loved him-and so on the day of his funeral every school in Schenectady was closed. We, and the children, can't bear think of him as gone; so will ever remember his work as living rather than him as dead.

To Charles Proteus Steinmetz, the great mathematician and multigifted genius, we render homage and proclaim that his work will live forever, as a flaming beacon to light the paths of men and guide their feet.

But to Steinmetz- the Friend of Childrenthe lover of animals and birds and flowers -the congenial comrade, calling him by the name the little children called him, we blow a kiss into the air and call out "Good Bye.' 'Daddy' Steinmetz. God bless you."
J. R. H.

# Charles Proteus Steinmetz 

# HIS SCIENTIFIC ATTAINMENTS AND THEIR MEANING TO THE WORLD 

By E. W. Rice, Jr.<br>Honorarl Cimarman of the lboard, Genieral Electric Company


#### Abstract

Among the most pleasing tributes Schenectady paid to Charles Proteus Steinmetz was a memorial service held on the evening of October 29th. On this occasion Mr. Rice, a lifelong friend and associate, read the principal address. As Mr. Rice was one of the first to recognize the genius of our illustrious citizen and was largely responsible for his coming to the General Electric Company, we publish this address in full for the benefit of our readers, feeling that it is the most authoritative tribute we have read.-EDitor.


The whole word, through its orators and writers, has expressed so beautifully and so well its appreciation of Charles Proteus Steinmetz, that if I attempted to express what is in my heart, it would be but to repeat what has already been said much better by others. However, as his devoted friend and intimate associate for one-third of a century, as one who recognized his great talents when he was unknown, and surrounded him with a favorable environment for the development of his genius, I regard it as a privilege to publicly endorse all that has been said of his usefulness, his commanding genius, his inspiring personality. This cheerful, patient, kindly spirit, this zealous student of nature and lover of humanity, was your friend and my friend.

I have been asked to speak of his scientific attainments and their meaning to the world. To do this properly would be to cover much of the history of the electrical industry during the past 30 years. I must confine myself to sketching such features as seem of most importance, and possibly of greatest interest.

Thirty years ago I first met Steinmetz.
The General Electric Company had been recently formed by the union of the Edison Company and the Thomson-Houston Company, which brought into one enterprise the results of the work of Edison, Elihu Thomson, and many other early pioneers in the fields of arc and incandescent lighting, electric traction, and industrial motor application.

Rudolph Eickemeyer of Yonkers had developed some interesting designs for electric traction purposes, and certain novel and econonical forms of windings for armatures of electrical machines. I was then in charge of the manufacturing and engineering of our Company and my views were sought as to the desirability of acquiring Eickemeyer's work. I remember giving hearty approval, with the understanding that we should thereby secure the services for our Company of a young engineer named Steinmetz. I had read
articles by him which impressed me with his originality and intellectual power, and believed that he would prove a valuable addition to our engincering force.

I shall never forget our first meeting at Eickemeyer's workshop in Yonkers. I was startled, and somewhat disappointed by the strange sight of a small, frail body surmounted by a large head, with long hair hanging to the shoulders, clothed in an old cardigan jacket, cigar in mouth, sitting crosslegged on a laboratory work table. My disappointment was but momentary, and completely disappeared when he began to talk. I instantly felt the strange power of his piercing but kindly eyes, and as he continued, his enthusiasm, his earnestness, his clear conceptions and marvelous grasp of engineering problems convinced me that we had indeed made a great find. It needed no prophetic insight to realize that here was a great man, one who spoke with the authority of accurate and profound knowledge, and one who, if given the opportunity, was destined to render great service to our industry.

I was delighted when, without a moment's hesitation, he accepted my suggestion that he come with us.

Steinmetz had already made his first important contribution to electrical science in investigations of magnetism, and especially in formulating and determining the laws governing the losses in iron subjected to varying magnetic induction. He showed that the hysteresis varied as the 1.6 power of the density of magnetic flux. This made possible for the first time the exact predetermination of the so-called iron losses in the armatures of electric motors and generators and in the transformers and other electrical apparatus employing iron. As a result, the quality of our electrical machinery was improved, and the weight and costs reduced. It is difficult at this date to realize the fundamental importance of this one contribution to the orderly and definite progress of the electrical industry.

During most of the first decade of the commercial application of electricity to light and power which may be said to cover the period between 1sso and 1890 , direct current only was used. This was the basis of the Edison system, the Thomson-Houston are system, the Vanderpool and Sprague railway motor systems. The laws governing the flow of direct current were simple and easily understood, and could be treated by mathematics of the most elementary character.

About the time Stemmetz came with the General Electric Company in 1893, the use of alternating current for lighting, power, and other purposes was just begiming to be of demonstrated commercial valuc. Adrance in the commercial use of alternating current was hindered by the extreme difficulty of understanding the technical nature of its action and of the various phenomena connected therewith. The engineer who had been working with direct current found it difficult to understand, and therefore to correctly design alternating-current apparatus. While the problems of the direct-current apparatus and clectric circuits could be treated by the simplest mathematics such as ordinary arithmetic, the alternating current, involving such phenomena as reactance, capacity, leading and lagging currents, phase displacements. etc., could apparently only be solved by higher mathematics involving the use of calculus - methods which were not generally familiar to the engineers of those days. Even skilled mathematicians familiar with such methods made slow and difficult progress in the solution of the problems which arose daily:

Steinmetz took hold of this situation with characteristic energy, and soon brought order out of chaos. He abolished the mystery and obscurity surrounding alternating-current apparatus and soon taught our engineers how to design such machines with as much ease and certainty as those employing the old familiar direct current.

He had already made the discovery that alternating-current problems could be attacked and solved with success by the use of what was known as complex quantities. By the use of this system he not only was able to solve these problems himself, but to teach our engineers to do the same work by methods almost as simple as ordinary arithmetic and algebra. Steinmetz himself always regarded this as one of his greatest contributions and called it the development of the "Symbolic Method of Alternating-current Calculations."

This method was found to be so powerful, aceurate and rapid that its use was not confined to the enginecrs of our Company, but rapidly spread throughout the world. He preferred to use this mathematical met hod in the treatment of all the problems of alternating-current engincering which arose and advocated its use before the American Society of Electrical Engineers in mumerous papers, and emborlied it in the textbooks of which he was author.

Not only did the adoption of these mathematical methods open the door to many to do useful design work who otherwise could not have done so, but it enormously increased the speed with which definite and accurate calculations and designs could be made. It furnished the engineer with a powerful tool which multiplied his power with just as much certainty as the machinc tool improves and multiplies the usefulness of the ordinary workman.

It was fortunate indeed for our Company and for the electrical industry that Steinmetz became associated with us at the critical time when the alternating-current development had just started. It is not too much to say that his genius and creative ability, not only in his own personal work, but in adrocating and obtaining the general use of a simple mathematical system (for treatment of alter-nating-current problems) was largely responsible for the rapid progress made in the commercial introduction of alternating-current apparatus.

Steinmetz's practical inventions literally cover the entire field of electrical applications: generators, motors, transformers, lightning arresters, lighting, heating and electrochemical operations. Of these many inventions. which were set forth in some 200 patents, perhaps the most important are the induction regulator, the method of phase transformation, as from two-phase to threephase, and the metallic electrode arc lamp.

His experimental work in are lighting led to the production of the magnetite arc. The practical advantage of this type of lamp is found in the extreme length of time which the metallic electrode will burn without recharging-these electrodes burning 200 hours contrasted with a life of 70 hours in the carbon are used before his time. The efficiency also of this type of lamp, especially in small units of illumination was of great commercial value.

He deroted much time to the development of the mercury arc and by his masterly
mothonk did much to improse this interesting and important type of illumination. 'These and many other of his inventions have found permantent and extensive ase in the industry.

During the last ten years when alternatingcorront power transmission fines of great lemgth, carrying large amounts of energy. have spread ath over the comatry, to use his own worts - "an old enemy became more and more formidable-hightning, and for many years the great problem which pertaned to the suceessful development of electrical engincering was that of protection from lightning. Before this could be undertaken with reasonable hope of success we must know a great deal more about lightning and centered phenomena. This led to the investigation of transient phenomena. It was soon found that while lightning might have been the eriminal which started the trouble in the electrical system, the damage and destruction was not done by lightning, but by the electric machine power back of the circuit which was let loose and got out of control by the disturbance initiated by lightning." He goes on to say that "the study of the phenomena produced by lightning effects could in general be grouped under the name of 'transients' because, unlike the direct and alternating currents which flow continuously, these disturbances last a limited time only."

The study of this problem led him to produce his famous "lightning" generator of which so much has been told in the public press. In the hands of Steinmetz and his assistants such progress has been made that the nature of the phenomenon has been so elucidated that as a result it is possible to proceed with confidence in the further development of the large high powered transmission systems, making possible Steinmetz's vision that the day was rapidly approaching when the electrical engineer would supply the world's requirements of energy over transmission lines which would cover the country with a network similar to that of the railways, the one taking care of the distribution and supply of energy, and the other carrying the materials.

Steinmetz was an ardent believer in the value of education. He not only found time to aid the educational work of Schenectady, but became President of the National Association of Corporation Schools, and lecturer at Union College. In a masterly address, upon retiring as President of the A.I.E.E. in 1902, he stated that "all future progress in science and engineering depends upon the young
gencration, and to insure unbroken atvance it is of preeminent importance that the coming greneration enters the field properly litted for the work."
llis personal example, his spoken words, and his writings have had a powerfol and beneficial influence upon the development of education, especially technical edincation in this country.
'That I have not overstated the value of Steinmetz's work in the carly period is indicated by the message of an eminent electrical engincer, Prof. Harris J. Ryan. President of the American Institute of Electrical Engineers, who says: "Through a period of years Dr. Steinmetz stood almost alone as the one electrical engineer in the world capable of defining and solving the many perplexing problems encountered for the understanding and improvement of the transformer, induction motor, alternator and polyphase high voltage system, the modern fundamental implements of the electrical engineer."

That the value of Steinmetz's services was not limited to the General Electric organization is well known, but it pleases us to have the testimony to that effect by President Herr of the Westinghouse Electric and Manufacturing Company, who states: 'He has been such an outstanding figure in engineering work for so many years and is so well known to the public that his death will be a great loss not only to the profession but to people generally."

Cne of our largest customers offers the following tribute:
"He was untiring in his devotion to the development of the electrical industry and in his passing the industry has suffered an irreparable loss."

From far Japan comes the following comprehensive and beautiful encomium: "He spent his life serving humanity."

A representative of the greatest electrical manufacturing company in Germany offers the following tribute:
"It will always remain one of the highest merits of your Company that he found here the congenial environment and support necessary for a genius like his to develop to the fullest benefit of mankind."

Edison says:
"I regret very much to learn of the death of Charles P. Steinmetz. The world has lost one of its greatest practical mathematicians, and the electrical industry will miss one of its shining lights."

Professor Elihu Thomson, one of our country's greatest sciontists and electrical engineers, a man whom all the world delights to homor. sends this tribute:
"In the death of Dr. Steinmetz, the science of electrical enginecring has lost a great keader, whose talents were most exceptional. Nearly a thirl of a century has passed since he displayed a faculty amounting to genius in the application of mathematical methods to the solution of difficult problems in electrical work, and throughout the subsequent period this special work of his has been followed up unremittingty His mumerous books and papers, his lectures and discussions will in themselves constitute an imperishable monument for all time. His long connection with the General Electric Company gave him the needed opportunity to put into extensive practice his ifleas, and the resulting value to the industry itself cannot be measured or estimated. The whole science of transient phenomena in electric circuits is virtually his: and he had the quatities of the patient teacher and expositor to those seeking information as students or listeners to his discourses. Only those who have followed his career. so full and so fruitful. can know the racancy created by his absence from among us.

I must now bring to a close this inadequate sketch of the contributions of this remarkable man to the development of the electrical science and industry: During his short life he rendered services of the most conspicuous character and inestimable value.

He was the athon of many origimal seientific papers and of a large number of electrical books which have been the acerepted standards in colleges, laboratories and workshops everywhere.

He was a prolifie insentor, a skilled mathematician, a traned engineer, and an inspiring teacher. Our gencration has produced men who have equatted or excelled him in some one of these fiedes, but no one has arisen who, to such a superlative degree, combined the qualities of inventor, mathematician, engineer and teacher.

He possessed a marvelous insight into scientific phenomena, and unequalled ability to explain in simple language the most difficult and abstruse problems.

Countless electrical engineers now occupying positions of great importance in our Company and elsewhere in the work gladly give testimony of their debt to him.

He was patient, sympathetic, cheerful, and ever willing to share his great gifts with all those who sought his counsel.

He loved children and they loved him. A neighbor and his wife were mourning his loss in the presence of their children, when the father exclaimed with deep emotion, "and he was my friend." His little son of seven years looked up from his play and said, "He was my friend too, daddy."

We, his fellow citizens, friends and associates, join the great world in mourning his loss, but may our grief be tempered by the memory of his great achievements which make his name the smonym of high scrvice to humanity:


# Dr. Charles Proteus Steinmetz 

By Martin P. Rice<br>Manager Publacation Departamen, Cimenab, Electric Combany


#### Abstract

We shall hear and read much abont Steinmetz as the great mathematician, engineer and inventor but not so much about him as the man; and it is the human side of this qreat genius that makes such a strong appeal to us. Mr. M. J. Rice wrote a hurried tribute on the day of Stemmetz's death and broadcast it over WGV' in the evening. We publish this quickly prepared tribute because of its many human touches.-linitor.


Some years ago Dr. (harles Protens Stemmet\% was warned of a valvular tronble of the heart, but it made little difference in the energy which he devoted to his favorite sturlies and investigations. Last night he was reading a scientifie work on the physies of the air. This morning we learned the sad news of his death.

A large part of the world recognized him as an outstanding genius in the realm of electrical engineering and mathematics-a worker of spectacular wonders- the superman of an electrical age.

To a few, however, it was given to know him as a friend and companion of winsome charm-intensely human in his fine appreciation of Nature-happy in the fellowship of children-loving to animals, and trustful of his fellowmen.

In the scientific world he was a recognized master of mathematical calculation and theory as well as a genius in the practical application of abstract principles to the design of electrical machinery. A creator of complex formulae, he possessed the rare gift of translating them into phrases which could be understood even by young students of electrical engineering.

Dr. Steinmetz was no recluse. Where another man of like attainments might have preferred to remain in the isolation of a laboratory, he went forth to meet menpartly through his many published text books and treatises, and partly through a personal interest in public affairs. The master of scientific attainment was also a daring publicist and participant in matters of economic interest.

Let me briefly review the career of one who reached the shores of America almost penniless and without knowledge of the English language and who, at the end of five years was actively engaged in the design of the General Electric Company's apparatus and in its scientific research. More than this he had appeared before the American Institute of Electrical Engineers and had propounded principles that fairly astonished that learned body.
1)r. Steinmetz was born at Breslat, Germany, April 9, 186.5 . He studied mathematics, physics and kindred subjects at the University of Breslat. It is curious to relate of this great mathematician that in his younger years he experienced the greaiest difficulty in learning the multiplication tables.

Ever an ardent student of public affairsever refusing to be bound by tradition or authority, he espoused the cause of Socialism while at the University and so fell under the ban of the German government. He was forced to leave the University and to flec the country to avoid arrest because of his convictions. In Switzerland he found a refuge where he continued his studies and made a scanty living by writing and teaching.

Herc he heard the call of America-a summons that has reached the ears of many a great man with its promise of intellectual freedom and of opportunities for scientific recognition. An American student at the Polytechnic at Zurich, who had formed a close friendship with the eager German and who was compelled to return to America, persuaded Dr. Steinmetz to accompany him to the Land of Promise-first by emigrant train and then in the steerage of an ocean liner. Thus there arrived at Castle Garden in New York the scientist whose death is now being mourned, whose loss to the world of electrical science is now being deplored not only by those competent to appreciate his contribution to the development of electricity but by the multitude who took pride in the accomplishments of his unusual genius.

Within two weeks the man who had narrowly escaped rejection at the hands of the immigration officials was devoting his talents to the improvement of electric street cars in the employ of Rudolph Eickemeyer at Yonkers, N. Y. This was one of the most important creative fields in the electrical industry at that time, and the unknown immigrant at once showed his mastery of electrical theory and practice. Soon he was writing on electrical subjects-more especially the laws of magnetism-with an authority and vision
that compelled attention among America's foremost electrical engineers.

When the comparatively small Eickemever business was purchased be the General Electric Company in 1sion, Dr. Steinmetz was recognized as the most precious part of the transaction and was established at the Lymn Works. He was soon transferred to Schenectady and became a fixed star in the electrical firmament. As a consulting engineer of the General Electric Company his knowledge of electrical phenomena and the mathematical laws governing them were of invaluable service. Other engineers discussed their problems with him and invariably profited by his wisdom and inspiration.

Meanwhile special honors awaited the mind that had been expelled from Germany. President Eliot of Harvard Lniversity, in conferring the degree of Master of Arts on Dr. Steinmetz in the year 1902, said: "I confer this degrec upon you as the foremost electrical engineer in the United States, and therefore the world." In 1903 he received the degree of Doctor of Philosophy from Union College at Schenectady with which he has since been connected as Professor of Electrophysics. He has been President of the American Institute of Electrical Engineers, of the Illuminating Engineering Society, and of the National Association of Corporation Schools. and has received recognition in many foreign lands.

Dr. Steinmetz accounted as one of the most important of his accomplishments his investigations in the field of magnetism. Before he addressed himself to this important part of electrical theory, much apparatus had been built in the hope that it would operate economically or to quote Dr. Steinmetz's orn words: "The designer of electrical apparatus simply built it, then tested it, and when the loss was too high and the efficiency too low, or the machine too hot, he tried again. This obviously was not a satisfactory way."

Steinmetz's famous paper which astonished the American Institute of Electrical Engineers
in 1s92, established basie principles that afford data for all future design.

Dr. Stemmetz's investigations into the theory of direct and alternating current were so far ahead of the knowledge of his time that when his views were developed by him before the International Electrical Congress held at Chicago in 189:3, many of his hearers were unable to follow him and it was only after several years that his investigations took printed form. Thirty years ago Steimmetz stood almost alone in his knowledge that has since been embodied in accepted engineering practice.

The third of the fields of investigation which Dr. Steinmetz adjudged the most important in his life work was the study of the phenomena of lightning. The world knows of his artificially developed lightning bolts, but the world does not know of the painstaking study which he bestowed on the protection of electrical apparatus not only from natural lightning but from the disturbances which it set up in electric circuits and machinery.

These accomplishments may not mean very much to the lay mind, but to the electrical engineer and manufacturer they have marked epochs in the development of the industry.

The unassuming figure without hat or overcoat. that was so well known about the streets of Schenectady, was literally a world power. To him every country looked for authoritative dicta on all matters of electricity. The man who welcomed friends to his summer camp with an almost boyish glee, whose kindly soul went forth in the fondling of a favorite dog, whose life and likings were the most simple-this man was an international figure, a criant in his profession, a conservator of the world's natural resources, and a friend to every user of electricity.

We mourn his passing, but we are deeply grateful for the wealth of knowledge that he has contributed to the world's progress, and we treasure as a choice possession the memory of an earnest, simple man who devoted his transcendent mind and talents to the service of his fellow men.

# Charles A Coffin Medal Railway Award 

By R. D. Ow上<br>


#### Abstract

ln recont yoars we have heard more of criticisms than of praise concerning our electric railways; but many of our roads have been by no means lax in making improvernents. The clectrie railway industry has been through hard times owing to the changed conomic status cansed by the war, but the fact that some roads have made as mach progress and as many improvements as have been achieved in any part of the electrical onductry is well bronght out by some of the speakers at the recent convention of the American Electric Railway Association hed at Athatic ('ity. The hriof submithed by the North Shore line in competition for the ('harles A. Coffin Medal is an coguent tribute to what a progressive policy can do in tarning apparent failure 


The Chicago. North Shore and Xilwankee Railroad hats been awarded The Charles A. Coffin Medal for "its distinguished contribution durng the past year to the development of electrical transportation for the comrenience of the pultic and the benefit of the industry." This was the first award to an clectric railway by the Charles $A$. Coffin Foundation, established by the General Electric Company in honor of its founder.

There are four classes of annual awards made by the Foundation for the encouragement of those in various branches of the industry, and it was the hope, now thoroughly justified, that the railway award would be an inspiration to railway managements by marking the progress from year to year toward better service to the public and high standards of operation.

Indeed, C. D. Emmons, former president of the American Electric Railway Association, who announced the award at the annual convention of the Association at Atlantic City, October 11, said that alone it justified the existence of the Foundation because of its service in bringing before the industry the record of electric railway accomplishments. He saw in it the means of stimulating initiative by giving recognition and honor to great achievements.

The Chicago, North Shore and Milwankee Railroad won the prize this year because of its outstanding work in giving and selling service to the public. There were many close contenders for the award, but the attainments of the North Shore Line, as it is called, were so great that there was no doubt in the minds of the prize committee as to where the award should go. The accomplishments of other railways was something of which the industry might well be proud, and Mr. Emmons said that their contributions would be published so that they might be known generally throughout the industry. Seventeen roads sent in briefs in support of their claims to recognition, and they presented
impressive evidence of the desire of electric lines w give service.

The conmittee which made the award was made up, of C. D. Emmons, president of the United Railways \& Electric Co., of Baltimore; J. II. MeGraw of the MeGraw-1Iill Co., New Fork; and Brition I. Budd, president of the North Shore Line. When it was found that the decision was narrowing down to a small group) of which the North Shore Line was one, Mr. Budd withdrew from the committee. J. (3. Barry and A. H. Jackson, vice-presidents of the General Electric Company, acted in an advisory capacity.

The announcement was made in the Greck Temple on the Million Dollar Pier, where the Association held its mectings. The room was well filled when Mr. Budd went up to the platform to receive the medal from Mr . Emmons and to hear an appreciation of his services and the high standing attained by the North Shore Line. Many things which had been talked about for years, said Mr. Emmons, had been carried to fruition on the North Shore Line, the committee being particularly impressed by the work in gaining good will and selling service.

Mr. Budd was smiling with gratification as he took the medal and the certificate which accompanied it, and expressed his appreciation and thanks for the recognition given his line. Whatever had been done, he said, had been done by the concerted effort of directors, officers and employees.
"We have teamed as one in the common purpose of endeavoring to give service and win the approval of the public," he said.

It was a striking coincidence that Mr. Budd was also elected President of the Association to succeed Mr. Emmons. He has long been one of the outstanding figures in electric railway operation. He is one of the few men in the country who understands thoroughly interurban, street railway and rapid transit operation.

He has been associated with transportation ever since he left school, when he took a
position with the survering department of a steam railroad in (Ohio. In 1s903, during the World's latir at Chicago, he was associated with the Intramual Ratway. When the Oteropolitan Elevated was started in Chicago, he foresaw the city's tansportation derelopment, and obtained a position in 1s9.0 as elerk in the storehouse. His adrance was rapid and in 1910 be became president of the company. When all the elevated lines in Chicago were consolidated in 1911 he was chosen president of the combined system. When the Chieago, North Shore and Milwaukee Railroad was reorganized in 1916 he was selected as the man to straighten out the tangled affairs of that rundown and dilapidated property. How well he did his work is evidenced by the award.

The medal was accompanied by $\$ 1000$ for the Employees Mlutual Benefit Fund of the North Shore Lines. It was accepted by Louis Homans, president of the fund, on behalf of the emplosees, who said that it would not only be a substantial contribution to their fund. but would inspire the employees to greater effort in making the North Shore Line a synony for courteous and efficient service.

The accomplishments of the line were summarized in the brief presented in its behalf in the following words:
"From a railroad patronized only as a necessity when other means of travel were not readily arailable, it has become the most talked about electric railroad in the country,' and is patronized by thousands of travelers in preference to any other means of transportation in the territory through which it runs.
"How was this accomplished:
"The answer may be epitomized in a single sentence: By giving service and telling the public its story:"

The equipment was in a rundown condition after ten years in the hands of receivers, only such work as was needed to keep the cars running had been done. Service was worse than poor. This was all changed. A frequent local serrice was begun, and fast non-stop trains making a mile a minute were run between Milwaukee and Chicago. Trains were run eren when the patronage did not at first justify them. The policy of additional
service withomt wating for requests from patrons was heold wemsistently. The best types of cats were provided. some of them luxurions observation parter cars. They were wedl heated and vemilated.

This service was then sold w the publie. Every courtesy and assistance was offered to shippers. Newspaper advertisements, attractive posters, bulletion batrds and motion pictures were used to carry the message of service. Every emplosee was mate a salesman of service, and their courtesy is the result of pride in their road. So many things were done to obtain the good will of the communities, through which the road ram, that the things done became "news" which the newspapers were glad to publish.

Economy in operation was sought, but mot at the expense of the public. Automatic substations were used extensively, and the power system improved in every possible way. Power consumption was reduced by hetter equipment and whough the co-operation of employecs. Labor saving devices were used wherever possible.

Improved construction played a big part in wiming public good will. Handsome stations were erected, roadbeds made as smooth as possible by rock ballast and heavy rails, wonden platforms were eliminated, even the grade crossings were made smooth so that motorists would not be bumper when they crossed the line. Accident prevention work was done among employees and the public was educated by lectures, posters and other means. First aid drill teams were organized among the employees.

The relations between the emplovees and the manarement have been carefully cultivated. They have been made to fed that the road is their road and to have a pride in its operation. The financial problems of public utilities have been put clearly before them. Financial assistance was given to students, public speaking classes were encouraged. Americanization work was undertaken with the idea of making better citizens. Home building was encouraged. Employees were not discharged because they did not fit in a job: they were shifted until it was found what work they could do well. Suggestions from employees were sought and rewarded.

# The Sherman Island Hydro-electric Development of the International Paper Company 

13y B. R. Connele,<br>Indmotrial Enginelering Department General blectric Company

and

lby W. T. O'Connell.<br>Construction Engenerking Departmext General Electric Company

The construction of aydro-electric phant at Sherman tsland in the Hudson River presented an unusually diffeult problem, as described in the following article, and great credit is che the engineers for the ingenious features of design which have made possible this development. The output of the station will be distributed throughout the extensive system of the Adirondack l'ower and Light Corporation, which is tied in with the New England lower Co. on the cast, the United Hudson Gas and Electric Co. on the south, and the Utica (ias and Electric Co. on the west, all of which will benefit by this further conservation of the waters of the Adirondacks.-Dintor.

Civil, mechanical, and electrical engineering put into form by high-class craftsmanship in many trades has created the Sherman Island Hydro-electric Plant of the International Paper Co.

Four of the five ultimate units of this $50,000-\mathrm{h} . \mathrm{p}$. development on the Hudson River a few miles west of Glens Falls, N. Y., were recently put into operation. The power is transmitted to the main trunk system of the Adirondack Power and Light.Corporation, purchaser of the entire output.

This unusual generating station is located where the Hudson River emerges from the mountains at the edge of the great plain of glacial fill east of the Luzerne Range. Fig. 1 shows the location, general plan, and contours. The pond extends back to the tailrace of the Spier Falls plant of the Adirondack Power and Light Corp. and the tailrace discharges to the pool of the Barge Canal feeder dam at the western edge of Glens Falls. The maximun flow is about $117,000 \mathrm{sec}-\mathrm{ft}$. and the plant is designed for $7600 \mathrm{sec}-\mathrm{ft}$. at 66 ft . head. The installation of the fifth $9000-\mathrm{kw}$. unit will await flow regulating developments along the head waters and tributary streams.

The general design was made by A. H. White, chief engineer of the International Paper Co. and in general charge of the work. H. de B. Parsons was consulting engineer and designer of the main dam. The construction work was done by the Parklap Construction Corporation. The waterwheels were built by the I. P. Morris Dept. of Wm. Cramp and Sons. The entire electrical equipment and electrical layout was furnished by the General Electric Company.

## Dam

The river at this point flows between the granite and sandstone shoulders of Luzerne and Palmertown Mountains and over a boulder and gravel fill 550 ft . wide and of unknown depth. The banks on either side east of the dam site are of gravel and fine sand.

There are four structures to the dam and they are: (from south to north) the spillway, the main dam, the wing dam, and the head gates.

## Spillway

The spillway is a horscshoe-shaped gravitytype dam on solid rock, all upstream from the main dam and 175 ft . wide at the opening of the horseshoe. Fig. 3, a view from the south end of the main dam, shows the larger part of the 864 ft . of weir which is at elevation 350.5 ft . and 11.5 ft . below the crest of the main dam. With the pond level 2 ft . below the crest of the main dam 100,000 sec-ft. can be discharged by the weir. Sluiceways provided for construction use are retained for possible lowering or draining the pool.

## Main Dam

The main dam is of special interest as it is of the hold-down type built entirely upon the boulder and gravel river bed. It is 551 ft . long with its crest at elevation 362 ft . The walkway is 70 ft . above the bottom of the great longitudinal ribs under the slab. Fig. 2 shows its general appearance though its height is partly concealed by the $20-\mathrm{ft}$. sand fill on the slab.

This dam is made up of arches across the upstream sloping sides of some 30 buttresses which in turn rest on a slab 104 ft . wide and 3 ft . thick. The buttresses are 3.5 ft . thick and are spaced 15.5 ft . face to face. The slope is in two pitches, the lower two-thirds being 5 to 12 with arches 24 in. thick and the upper third 12 to 12 with arches 18 in. thick. The floor slab is reinforced and insured against slippage by three longitudinal ribs 9 ft ., 10 ft ., and 6 ft . deep. An apron 50 ft . wide and 2 ft . thick extends downstream from the slab. The slab and apron are covered by 20 ft . of sand for additional weight. Fig. 4 shows the massive concrete work in the upper portions of the dam.

Seepage under the dam is minimized by two interlocking steel piling barriers driven
5.5 ft. deep and sealed into the upstream edge of the slab. 'The pond botwom for some distance upstream was cosered with fine sand to stop) the interstices of the bottom. Oxerturning is prevented by the broathess of the base and the shope of the upstream side which puts about in ft. of static head on the upstream toe.

Wing Dam
The wing dam is of solk concrete on rock commecting the main dam with the headgate
and 10 ft . from face to fate . The eight openings (1) the power (anal are (ontrolled be eight reinfored eomerete gates 20 fl. high, 10 ft. wide, and is in. thick. These gates are in three sections with a 11-in. opening between the upper two for filling the ramal. Jach section is protected at the ermers by angle iron and each complete gate weighs about 20 tons.

The concrete structure is tropucel by a steel hoist rumway leg. ft. lomg (mn which is mounted a $2 . \mathrm{F}$-tom motor-operaterl hoost for


Fig. 1. Location of the Sherman Island Hydro-electric Plant on the Hudson River, four miles west of Glens Falls, N. Y. The numbered arrows indicate the locations where the corresponding photographs were taken. Illustration based on a U. S. Geographical Survey map)
structure, and tapering off as a reinforcement into the river side wall of the power canal. It is 171 ft . long and of the same type as the spillway

## Head Gates

The headgate structure is a buttressedtype dam for 35 ft . head bedded in the solid granite mountain shoulder. The buttresses are 40 ft . from front to back at the bottom
handling the gates. A sluice with hand-operated gate provides for the passage of logs to mills downstream. A small house protects the water level transmitting instruments which are over the float well.

Fig. 5. which is a photograph taken overlooking the head gates, shows the upstream side of the arches of the main dam, and part of the weir may be seen at the far end of the dam.

## Power Canal

The river bed has at drop of about 19 ft . from the dam to the head of the Barge Canal fooder pool, a distance of over two-thirels of at mile. This additional drop detemineal the location of the power house and neressitated the construction of $3.3 / 1 \mathrm{ft}$. of canal in the same and gravel north bank of the river.

The canal bottom is 32 ft . wide at elevation 321 ft . and the top edges of the concrete sides are 12 s ft , apart at 3.5 ft . elevation. The bottom and about 40 ft . up the sides are of 6 -in. reinforced concrete while the upper 1 s th of sides are 9 -in. thick.

The down-st ream end is enlarged to form a forebay with the lining sealed to the forebay dam to prevent leakage and undereutting. Tests show that the canal leakage is negligible.

## Forebay Dam

The forebay dam is a buttressed structure over 300 ft . long built on a slab in the sand and gravel river bank. A sheet-steel pile cutoff near the forebay side prevents under seepage. The buttresses are 3.5 ft. thick, 10 ft . face to face. Fifteen inter-buttress spaces are closed by Broome Caterpillar type gates which are handled by a like number of Maine Electric Hoists housed in a brick and stcel superstructure. The hoists are operated by 15 -h.p. motors having local individual control and also remote control in groups of three from the power-house. Hand-operated gates open to a $\log$ and ice sluice of timber construction leading to the river east of the power house.

Water passes from the forebay under a skimmer apron wall through trash racks and gates to the penstocks. Over the trash racks is a concrete trash trough which can be flushed to the $\log$ chute. The construction of the forebay dam and comnected structures is shown in cross-section in Fig. 1.

## Penstocks

The penstocks are of novel construction being of reinforced concrete with walls 2 ft . thick enclosing 1.5 passages 10 ft . by 10 ft . is in. aggregating over 1500 sq. ft. The penstocks are cast in groups of three, each group leading to a single turbine scroll casing. The penstock length of 240 ft . is divided into transwerse sections so that there are 20 1-erforated blocks in the penstock structure. The sections nearest the power house are thickened on the upper side to form an aboveground deck for the outdoor transformer and switching station. The penstocks drop 3.5 ft. from the forebay dam to the turbine scrolls.

## Power Stalion

In Figs. 6 and 7 are shown the elevation and plan of the power station. The substructure of the power station, 80 ft . by 220 ft ., consists of a huge concrete block 50 ft . deep containing the five moulded-in-concrete turbine scroll casings and draft tubes. The superstructure is of steel and brick construction and houses the generators, low-tension switch gear, operating board, etc. The bearing material is entirely of sand confined in ten rectangular columns by interlocking steel piling. Settlement stopped during the process of the construction work and there has been no signs of its recurring.

The superstructure carries a 50 -ton Shaw crane which serves the main floor as well as a standard-gauge track that enters the west end of the station. Ventilation is provided by a double row of monitor sash 180 ft . long in the roof. This is motor operated with remote control from the floor. A two-story extension along the head gate side is provided for housing the 6600 -volt bus structure and miscellaneous auxiliary equipment on the first floor; and offices, main switchboard control room, and circuit breaker gallery on the second floor. The control room projects into the station proper giving a good view of the main floor. Stairways to the main floor are provided at both ends of this projection.

## Waterwheels and Governors

The number and size of units to be installed are generally determined by the hydraulic conditions. However, the character of the load, as well as the maximum and minimum stream flow, and the possibilities of future storage developments have to be taken into account to insure operation at the highest efficiency. Only by the careful weighing of all the factors is it possible to utilize to best advantage the water available. After a study of all these factors for this particular plant it was decided to supply four units initially with five units for the complete development.

These waterwheel units are each rated at $10,000 \mathrm{~h} . \mathrm{p}$. when operating at a speed of 150 r.p.m. and under a net effective head of 66 ft . The turbine is set with a concrete casing, and a cast-ron speed ring and pit liner which serves not only as a support for the turbine itself but to transfer the load of the generator to the power house foundation.

The design of the draft tubes is of the Moody spreading type which has been shown by recent tests to have a very high efficiency.


Fig. 3. Spillway from South End of Main Dam. Its great length 864 ft
prevents floodwater overtopping the dam


Fig. 5. Headgates and Gate Horst Overlooking the Pond. A portion of the dam
and spillway may he seen through the host runway

Bach waterwhed mat is controlled by a gevernor which is oil operated and beld driven from the main shaft. Tliese are of the 1. P. Norris double-floating lever type, such as has beon instathed at a manler of reeent plants in this combtry.

The governor pumps and accumblators are momenten on the generator floor near the downstram wall. The pamps are each driven by a ${ }^{3} 0$-h.p. induction motor; three such units are supplicd. one being a spare for the present.

## Generators and Exciters

The present installation consists of four vertical-type generators which are threcphase 60-eycle machines and have a continuous rating of $9000 \mathrm{kv}-\mathrm{a}$. ( 7200 kw . at 0.8

Tomperature coils are also installed in the armature windings and connected to the indicating temperature meters on the benchboard. The armature frame is made up of $\mathfrak{i}$ wo sections having a total weight of approximately 67,000 1h., the outsidediameter of the machines being Is ft. 2 in . The total height of the mit from the face of the coupling to the upper end of the shaft is approximately $19 \mathrm{ft} .91 / 2 \mathrm{in}$.

The rotor is made up of two sections, each consisting of a solid cast-steel wheel mounted on the shaft, one above the other into which the field poles are dovetailed. The total weight of the rotor including the shaft is $92,500 \mathrm{lb}$. and it has a flywhecl effect (WR ${ }^{2}$ ) of approximately $2,900,000 \mathrm{lb}$.-ft. It is designed to withstand a maximum runaway speed of twice normal with an ample margin of safety.


Courtesy of Engineering News Record
Fig. 6. Cross-sectional Elevation through Forebay Dam, Penstocks, Outdoor Station, and Power House
p.f.), 150 r.p.m., 6600 volts, and are furnished with direct-connected exciters. Fig. 8 shows the generators and their exciters.

The generators are designed with an inherent reactance of approximately 27 per cent to limit the current of each machine under instantaneous short-circuit conditions to $31 / 2$ or 4 times full-load current.

The armature winding consists of formwound coils with both ends of the phase windings brought out so that current transformers can be inserted inside the Y connection for differential protection of the generators. A station neutral bus is provided to which the nentral of each generator can be connected through a solenoid-operated oil circuit breaker. These switches are remote controlled from the benchboard.

A heavy bracket-arm type of construction as shown in Fig. 8 supports the thrust bearings, which are of the General Electric spring plate type, mounted on the thrust deck, formed by the bracket arms, and between the generator and exciter. These bearings each carry a total load of approximately $200,000 \mathrm{lb}$. including all rotating parts of the generator, waterwheel, and water thrust. Cooling coils are provided in the thrust bearing housings supplied with water from the station header that is tapped from the penstocks as mentioned later. Two guide bearings are also supplied with each machine, one located just below the thrust bearing and one below the rotor.

The oiling system of these generators is of the unit type, that is, each machine has an
independent system consisting of individual Richardson-Phemix filter and Brown \& Sharpe gear pump) for cirenlating the oil to the thrust and guide bearings. This system makes a considerable saving in cost of station oil piping. The pumps are gear driven from the main shaft and with the filters are located in the generator pit.

Six brakes are provided for shutting down the unit. These are of the plunger type and are air operated from the station air system
supplied by a motor-driven compressor. These brakes alsus serve as combined jacks for lifting the rotating clements to allow for dismantling the madhane when mecessary. When applied as jacks, wil is used from a special hatdeoperated ligh-pressure oil pump, supplied for this purpose.

Generator-fied rheostats are omitted and voltage control is obtaned through the exciter fied theostats, thus eliminating the losses of the generator-fied rheostats.


Fig. 7. Plan of the Headgate House, Outdoor Station, and Power House

```
1. Generator (Future)
Generators
Generators
Governor
Field switch panel
Storage battery room
Toilet room
Store room
Air compressor
Series lighting transformer
Lighting transformers
Station service transformers
Conduit room
Station service switchboard
```

Generator (Future)
Generators
Governor
Field switch panel
Storage battery room
Store room Air compressor
Series ighting transiormer
Station service transformers
Station service switchboard

| 14. Transformer oil cooling equipment |  |
| :--- | :--- |
| 15. | $6600-v$ bus compartments |
| 16. Governor oil pumps |  |
| 17. | Air compressor |
| 18. Accumulators |  |
| 19. | Motor-driven exciter |
| 20. | Heater cowis |
| 21. | Bench board |
| 22. | Voltage regulators |
| 23. | Battery charging set |
| 24. | Water-level recorders |
| 25. | $6600-v$. oil circuit breakers |
| 26. | Main transformers |

27. Transformer transfer car 25. High-tension oil circuit breakers 29. Lightning arresters
28. Transmission lines
29. Disconnecting switches
30. Gate hoists

Gate hoists
Trash trough gates
Ice and log chutt
Transformer pit
Starting compensators
Starting compen
Lighting panel
Lighting panel
Machine shop
38. Machine shop

- Arr for lentilation of the fenerators is takers into the generator pits, from over the
 the mathone he the rotor fans and discharged into the gencrator room thonugh dacts in the stilor.
liatrh direet eommeoter exciter is raterl
 are shmot womad amd are mounted direetly above the hrast bearing. 'They are not operatcol in pattallel and eatch is eontrolled bs an individual voltage regulator.

A spate exciter of the same cathacity hats

bitiono volls delta commected. 'Where are severn matis of ontdoor eonstruction rated
 mait leoing a spare. After a careful sturly of various framsformer arrangements it was Aecider to rase two banks, eatel consisting of three single-phase mits with one as a spare, as being the most eeonomical layout and alloantageous arrangement from an operatinge standpoint.

The transfomers are of the core-type construction with concentric-(lise helical wimdings. Two 2 ! 2 per cent full capacity taps aloove and below normal voltage are provided


Fig. 8. Interior of Power House Showing Four $9000-\mathrm{kv}-\mathrm{a}$. 150 -r.p.m. 6600 -volt Generators with Direct-connected Exciters. The projecting part of the gallery shows the location of the operating room
r.p.m. squirrel-cage induction motor operating off the 5.50 -rolt bus. By means of a transfer bus this exeiter ean be thrown on any field through the double-throw generator-field switehes which are mounted on separate panels on the floor near the main generator thus making the exciter main leads as short as possible.

## Main Transformers

The voltage is to be stepped up from 6600 to 114,500 volts for transmission. The transformers will be star comnected on the high-tension side with dead grounded neutral but for a few months will be operated at
in the high-tension winding. Conservators are a feature of these units as shown in Figs. 9 and 13 , which also show the spare transformer.

The tanks are of reinforced boiler plate construction and are equipped with alarm type thermometers. Each transformer is furnished with trucks. A transfer truck of standard gauge is provided so that the transformers can be run into the generator room under the main station crane for dismantling if nccessary.

Instead of being of the usual water-cooled type, these transformers are of the forced oil type, the oil being circulated through an
external cooling system. This system was used as trouble fad been encountered in other locations above this plant due to pitting and corroding of watter cooling coils from impurities in the river water. For each transformer bank there is supplied a motordriven centrifugal pump, for cireulating the oil and a Griseom Russell multi-whind type oil cooler, with a third complete mit provided as a spare. The pumps and cooler are capable of handling los gal. of oil per minute, and are located in a separate room under the main
 water into the wil in the event of a lakk in the oil cooler, it is cssemtial that the oil pressume in the coover is kepe at a higher value than the water. Pressure gatuges were therefore hoated on the ingoing water line of the conlers, and (on the outgoing oil lince. Thermometer wells were located in the ingoing and outgoing oil and water lines to the coolers in order to enable the operator we cherk wi, the efficioncy of the cooler, and to be assured that the system was operating satisfactorily:


Fig. 9. View of the Outdoor Transformer and Switching Station from Forebay Dam. The transmission lines lead off to the right. The concrete deck is a part of the penstock formation
operating gallery near the center of the building.

The use of one cooling equipment consisting of cooler and pump for each bank of three transformers made it necessary that in the design of this piping system an equal distribution of circulating oil should be assured in the three transformers. To meet this requirement an attempt was made to equalize the velocity of the oil at the inlets of the three transformers. This was accomplished by increasing the size of the pipe line between the first, second, and third transformers. Equalizing of flow was also obtained by means of a regulating globe valve in the inlet line to

The three cooling equipments have been piped up to a combination of headers so that the spare cooler can be used with either bank of transformers or in the event of only one transformes bank operating any one of the cooling equipments can be used. An oil storage tank is provided in the space beneath the slal of the outdoor substation and valves inserted in pipe lines so that the oil from any transformer can be drained to this tank if desired. A comnection from this tank is also taken into the pump room so that oil can be pumped from this tank through the filter press into the oil cooling system. The filter press is also comected to a header in
the pump romen in order that sif from either equipment ean be tiltered. These heakers were tapped off the hot and cold oit liness so that the filter can operato in paralle with either cooler. Cooling water for the multiwhirl conders is supplical from a (i-in. header Whide taps pernstocks No. $2,: 3$ and I. Shutoff valves are provided in each penstock so that a constant supply of cooling water is assured. A dosed 10 -in. drain pipe leads from the pump) rom to the tailrace for discharge of the cooling water.

## Switching Equipment

The electrical control of the entire station, inchding the main generators, outloor equip)ment and headgate motors, is centralized in the control gallery which is located on the batcons in the central part of the station. The main control switchboard is of the benchboard type and of natural black slate. There are three sections, the two end sections each containing the control of two generators and one outgoing high-tension linc. The central section contains the control of one gencrator, station auxiliary equipment, and space for a future outgoing line. Figs. 11 and 12 show general views of this control board.

The bench section contains a mimic bus showing the main connections of the station and the control switches for the remote control of oil circuit breakers and field switches which are motor or solenoid operated, synchronizing and potential receptacles, etc. The indicating instruments are of the horizontal edgewise type and are mounted on the vertical section above the bench.

On the sub-bases are mounted the control equipments for the temperature indicators of the generators and transformers, and the rheostat controls for the exciter field and regulator adjusting rheostats.

In the rear of the bench section is a vertical section, the interspace being enclosed by grill work with a door in each end. On these rear vertical panels are mounted the recording and curve drawing meters, relay equipment, and testing or calibrating terminals.

At each end of the main board are mounted the voltage regulators on individual pedestals. An individual automatic voltage regulator is supplied for each direct-connected exciter and another regulator of different type for the spare motor-driven exciter set. In the rear of the control gallery is mounted a vertical panel for controlling the storage battery and its charging set.

On the rear wall there is mounted a small panel containing control switches and signal
lights for the unit operation of the three hadd gate motors for each main unit in emergencies. This control is comnected in parallel with that at the head gate house, where each motor is individually controlled by push buttons operating contactors. An individual light on this panel indicates when each gate is in the full open or closed position.
ligg. 10 is a one-line diagram showing the main connections of the entire station.

The (6if)(0)-volt oil circuit breakers for each gencrator, transformer, station service, and Dus tie are of the $1 ., 000$-volt motor operated


Fig. 10. One-line Diagram of the Power Station and Outdoor Station Circuits
$H$ type equipped with stuffing boxes and separating chambers. The generator circuits are non-automatic except for differential protection against internal failure, the station service circuits being automatic with timelimit overload relays. The main transformers are protected by differential relays.

The five high-tension oil circuit breakers are of the high interrupting capacity, tank type, equipped with explosion chambers. One is installed between each transformer and the high-tension bus, one in each outgoing line, and one serves as a bus-tie switch as will be seen from Fig. 10.

The two outgoing lines are each rated $45,000 \mathrm{kw}$. capacity and are protected by balanced reverse power relays with overload relays.


Fig. 11. Front View of Main Control Switchboard


Fig. 13. One Bank of 7500-kv-a. 6600-66000 114500-volt Transformers Equipped with Conservators. These units are truck mounted and a transfer car serves to bring them under the power station crane


Fig. 12. Back View of Main Control Switchboard


Fig. 14. High-tension Circuit Breakers and Disconnecting Switches. The nature of the forebay and power house site is shown by the bank in
the background

Lew-tonson Oil Circuit Breaker and Bus Structure
'「16 hus and oil cirenit breaker exll structures are in separate compartments to the left of the control gatlery. The buts cells are (an) the generator foor level and the wil ciremit breaker exlls on the gallery level.
'The bus structure was constructed of hatr-burned pressed brick, light tan in eolor. Concrete skabs were used for all horizontal sections in the bus strueture and sobpstone shabs in the cirewit loreaker strueture

In the design of the bus strueture the main lonses were loeated in compartments in the front of the strueture so that thes are aceessible for inspeetion and cleaning, and the connections to the oil eireuit breaker were taken off at the back of the eompartments.

All conduits for control and instrument transformer leads are ran concealed in the gallery floor from the benchboard to the oil circuit breakers and instrument transformer compartments. In the compartments, howerer, they are necessarily rum in the open and are located close to the front of the compartments clear of all live parts and accessible for installing the cables. At the oil circuit breakers, conduits are run exposed up the back of the rear wall.

Strips of 1 by $1 /-\mathrm{in}$. copper straps are run throughout the length of the bus structure and circuit breaker cells for the grounding of bases of disconnecting switches, the casings of current and potential transformers and operating mechanisms of the oil circuit breakers. The bases of bus supports however were not grounded. The secondary windings of both the current and potential transformers were grounded at the transformers only, and not at the switchboard, and in everv case a ground wire was carried to the switchboard with the other conductors in the circuit.

For groups of instrument transformers consisting of two current transformers and two potential transformers, two independent ground wires were taken to the switchboard for each equijment. This was necessary in order that the voltage drop in a common wire from two current transformers would not introduce an error in the potential transformer circuit. Where three current transformers were used the use of separate ground wires was not necessary.

The arrangement of buses one above the other and the mounting of the supports on the horizontal slabs of compartments eliminated all cantilever forces in supports, due to magnetic stresses at time of short circuit. Thus the moderate duty bu: support was satisfactory for this installation.

The low-tension oil circuit breakers are of the improved design provided with gravel chambers and gas vents. These vents are all piperd to a : z -in. header extending the full longth of the row of oil circuit breakers and supported from the ceiling above. The vents from the three sets of pots in each oil circuit breaker are connected to a 1 -in. header in the eell and these $1-\mathrm{in}$. pipes are connected io the main header. Gases generated in the breakers at the time of opening under stvere short circuits will be discharged through this header outside the building so that no danger will be encountered from gases in the switching room.

## Auxiliary Equipment, Lighting, Etc.

The entire station auxiliary equipment is operated off the main generator bus, through a step-down transformer bank, rather than from an independent supply as power will always be available through the trans nission lines for starting up the plant initially or after a complete shut-down. This gives a simpler operating arrangement and is more economical than providing a small waterwheel for supplying the auxiliary power.

This station auxiliary service is supplied by three $100-\mathrm{kr}-\mathrm{a}$. $6600-575-\mathrm{volt}$ transformers, and three $15-\mathrm{kv}-\mathrm{a}$. $57.5-115 / 230$-volt transformers supply the station lighting. A $.5-\mathrm{kw}$. 575 -volt, $6.6-\mathrm{amp}$. series lighting transformer is also provided for the lighting of the head gates and grounds around the operators' cottages which are located along the pond above the main dam on the north bank of the river.

To insure the transformer oil being in proper condition, a 3 -kv-a. oil-testing transformer equipment and an oil filter press and drying equipment of 30 gal . per min. capacity are also included in the station equipment.

The control for the 5.50 -volt auxiliary circuits in the station, including the series lighting equipment and a machine shop, is laken from an auxiliary switchboard located directly under the operating galler: on the generator floor level. This board consists of six double-circuit panels equipped with automatic oil circuit breakers.

Operating current for the solenoid and motor operated oil circuit breakers, rheostats, emergency lighting, etc., is supplied by a 60 -cell Exide storage battery. A $43 / 4-\mathrm{kw}$. induction motor-driven charging set is supplied for charging and is operated continuously with the battery floating. The emergency lighting is thrown from the alternating-current circuit to the battery
circuit by an antomatic throw-oner switeh on the battery control panel.

Ample light is provided by day from mumerous large windows on three sides and monitors in the roof of the generator room. These windows and monitors are also arranged to provide for natural ventilation of the building.

The three lighting transformers supply power for lighting the generator station, outdoor station, and head gate house. The general illumination of the station is furnished by 200 -watt units mounted in angle reflectors on each of the building columns 21 ft . from the floor. These lamps are controlled by four circuits from the main panel box and are connected so that alternate lamps are on each circuit to allow controlling the quantity of light to suit the requirements. An additional row of 200 -watt units with reflectors are installed in the roof trusses, alternate lamps being connected on the emergency lighting srstem to provide general illumination around the machines in case of trouble on the alter-nating-current system. The control room is lighted by six 200 -watt units with improved glass-steel reflectors, which type has been designed for locations where semi-indirect lighting is desired but where no reflecting surfaces are available. The bus and circuit breaker rooms and other similar rooms are lighted by $\bar{j}$-watt units. The lighting of the outdoor yard is by floodlights, two 500 -watt units being located on poles at each side of the yard.

A complete water-level indicating equipment is installed showing the water levels at the canal head gates, the gate house, and the tailrace. These are remote operated and the meters are located at one side of the switchboard operating gallery.

## FEATURES IN STATION DESIGN

The transformers, high-tension oil circuit breakers, and lightning arresters are located in an outdoor station adjacent to the generating station on a concrete slab over the penstocks on the northeast side of the building, Fig. 9. The location of the outdoor equipment in this space was pertinent in the design for the following reasons:
(1) To facilitate the handling of equipment it was desirable that the outdoor station yard level be located at the same elevation as the main floor of the station so that a transfer track could be installed by means of which transformers could be taken into the station on the transfer car and the station crane used for dismantling of this equipment.
(2) The location of the substation at this point simplified the piping of the oil cooling
sytem for transformers ; and as at is desimable to have the promping equipment for this system located in the station, where it is under olservation of the flow operater. Whis location gave a very flexible and combact arrangement.
(3) Severe climatic conditions in this section of the country also made it desirable that the outdoor station be lowated as close as feasible to the generating station to assure frequent inspection and also to facilitate the operation of disconnecting switches during the winter season.

## Steel Structure

In the design of this structure S-in. H sections were used for columns in the lower tier and 6 -in. H sections in the upper tier. Deck framing was made up of channels and I beams. Angles were used for bracing throughout. Light sections requiring the use of latticing were avoided inasmuch as the use of heavier rolled sections reduced shop and maintenance charges. Furthermore, this type of structure presents a smaller number of exposed sides so that painting insures a good weather resisting surface and is very easily renewed. All shop connections were riveted and the field connections bolted.

Outgoing line anchorages were designed for a load of 3000 lb . per phase and other strain connections for 2000 lb . Tensile stresses were limited to $20,000 \mathrm{lb}$. per sq. in. For the main compression members the ratio of slenderness was limited to 1.50 , and for secondary members to lso.

## High-tension Connections

In designing the high-tension connections the use of disc-type insulators in a strain position was avoided as far as possible. The main buses are made up of $2^{1} 2^{-}$in. dia. standard galvanized iron pipe, and supported by strings of s-unit Hewlett insulators spaced 2.) ft apart. This size pipe was not necessary to obtain sufficient current capacity: but was used to permit a wider spacing of supporting insulators without undue sagging of buses under an ice load of ${ }^{1} 2$-in. thickness. This wide spacing of insulators made a considerable reduction in the number of insulators required and also in the amount of the steel work.

Connections from the oil circuit breakers to the buses and transformers were made with $1-\mathrm{in}$. standard iron pipe size copper tubing. The size of these connections was determined by length of span rather than current capacity. Machine cast bronze alloy connectors
of the bedted type were used for making eonnections between the several lengths of pipe.

The gencral diveetion of outgeoing lines from this station wats at right angles to the natural direction 10 fonform with the arrangement of equipment in the substation, and as space was not available between the substation and gateloouse to permit the use of turning towers, it was necessary to obtain this change in direction within the substation structure itself. This was aceomplishoed hy introlucing two vertieal stub buses in an upper seetion of the tower directly ower the line oil cireuit breakers. This proved to be a very satisfactory arrangement and allowed the transmission lines to enter the structure in the same relative vertical positions as on the line and at the same time occupy a minimum width of structure. The two transmission lines were terminated in the upper tier of the structure in the same bay as required for the transformers on the lower ticr.

## Lightning Arresters and Choke Coils

The choke coils are located in the vertical stub buses and connections to lightning arresters are taken off the stub buses at points corresponding as closely as feasible to taps from the line so that the path to the lightning arrester is as direct as possible.

Two sets of disconnecting clamps are provided at the lightning arresters, one set will be used for disconnecting the arrester from the line for inspection. The second set of disconnecting clamps has been provided for grounding the transmission lines at the station, and when clamped to the line above the strings of insulators, connects the line through flexible connections to the ground bus on the arrester framework.

## Disconnecting Switches

In the design of the station, the space available was limited and the width of the structure was a determining factor. Advantage was therefore taken of the improved heary-duty built-up type post insulator which permitted the mounting of disconnecting switches with the insulators in the horizontal position. The introduction of this feature in the design resulted in a very simple arrangement of equipment and reduced the ground area to $\overline{5}$ per cent of that required if disconnecting switches had been mounted in the underhung position.

## Oil Circuit Breakers

The spacing between columns in the outdoor structure is governed by the space
required for the oil eircuit breakers and transformers. It is the usual practice to space columns at oil eircuit breakers sufficiently far apart to allow space at the end of the breaker for inserting an emergency handle at the solenoid for hand operation. In this design an appreciable saving was mate in the length of bay by turning the soleneid operating mechanisms 90 deg. so that the emergency handle cotthl be operated at the side of the breaker where there was alreaty space provided for the transferring of main transformers. This feature reduced the length of the bays at the oil circuit breakers from 30 to 2.5 ft . with a corresponding saving in steel work.

## Spacing of Conductors

Minimum spacing of 5 ft .4 in . between live parts and 4 ft .8 in . between live parts and ground were maintained throughout this design. The spacing in most cases, however, exceeded these values due to space requirements for the apparatus so that throughout the design very liberal spacings were obtained without increasing the size of the structure.

## Grounding System

As the outdoor station was constructed on a concrete slab a good grounding medium in the immediate vicinity of the grounding apparatus was not assured. A $4^{\prime} 0$ bare copper cable was therefore buried in concrete throughout the switch yard, and at each end of the substation cables it was run to the tailrace where copper ground plates 2 ft . square by $1 / 8 \mathrm{in}$. thick were buried in moist earth well below the minimum tail-water level and imbedded in charcoal to assure a good connection to ground.

Casings of all apparatus and columns of steel towers were connected to this ground system. In addition to these points of grounding, ground connections were also attached to the steel piling which formed a box work about the entire station.

Separate ground circuits were run from the lightning arresters to separate ground plates near the tailrace, and in addition to these a series of iron pipes were driven into the earth to a depth of s to 10 ft . beyond the edge of the concrete penstocks.

## Auxiliary Transformer and Battery Room

Following the general practice of locating transformers in a room isolated from the remainder of the equipment in the station, a special transformer room has been provided
in which are located the station service, station lighting, serics lighting, and testing transfomers. The battery charging set and air compressor equipment have also been located in this room.

In addition to limiting the fire hazard, the locating of all this secondary equipment $n$ one room, isolated from the remainder of the station, improves the appearance of the station and localizes this equipment.

In the design of the battery room the usual precautions were taken. The cells were mounted on two impregnated wood frame supports in two rows, two tiers high, along the sides of the room, and a special floor covering of acid-proof tile set in bitumastic compound was provided and drained by an acid-proof drain pipe. The walls and exposed steel work and conduits were painted with asphalt paint, and the lighting unit installed in a gas-proof fixture and controlled from a switch located outside the room close to the door opening into the battery room.

To insure proper ventilation a wooden louvre was installed in the space provided for a window.

Weatherproof covering was used on all conductors entering the battery room, and all openings in conduits were closed with an asphaltum compound.

All exposed copper was well coated'with vaseline to prevent corrosion from the acid fumes.

## Power and Control Cables

The main leads from the generators to the low-tension oil circuit breakers were made up of one $1,500,000$-cir. mil single-conductor ropecore varnished-cambric-insulated cable per phase, insulated for 8500 volts. In place of the usual weatherproof braid covering used on single-conductor cables carring alternating current, a special rubber hose jacket was provided thus assuring better protection against moisture. Over this rubber jacket a tape impregnated with compound was
wrapper to protect the rubber jacket from mechanical injury, and also to exclute air from the rubber, thus prolonging its life.

The low-tension transformer comections were made up, of two $2,000,00(0)$-cir. mil ropecore single-conductor cables per phase, the same insulation and covering being used as on the generator cables.

All control and low-tension power cables in the station were provided with weatherproof covering while all cables keaving the buikding either to the outdoor sulstation or to the head gate house were provided with lead covering. Bare copper cables were used for the ground system throughout.

Threc-inch drive-joint fiber conduits were used for the generator and transformer leads, and hot-dip galvanized-iron conduit for all low-tension power circuits and control.

## TRANSMISSION LINE

The Adirondack Power \& Light Corporation's two transmission lines lead from the side of the outdoor structure in a southwest direction over Palmertown Mountain running to the high-tension buses at its Spier Falls Station. This line is four miles in length and consists of one double-circuit tower line, the towers being of the square, rigid type and galvanized. The conductors are in a vertical plane spaced 9.5 ft . apart and consist of 4,0 stranded copper supported by eight insulators in suspension and nine in strain. The distance between lines at the top and bottom wires is 17 ft . and at the middle wires 20 ft . The insulators are the Locke No. 580010 -in. cemented type. A $3 / 8$-in. steel-core copperclad ground wire is installed and a private telephone line is strung on the main towers.

From the Spier Falls bus the lines will be connected by a 114,500 -volt line to the main system of the Adirondack Power \& Light Corporation and its new outdoor main distributing substation near Rotterdam just west of Schenectady.

# Studies in the Projection of Light 

# PART VIII <br> PARABOLIC MIRROR AND DISK SOURCE OF LIGHT (Concluded) 

By. Prank Benforb




#### Abstract

The charatorichice of a parabolo maror amb sherical source of lizht were deseribed in our April and May isubes. The tratment of the same tye of mirror and a disk souree of light was begun in the September number, combund in the Nowember, and is comelnded beow with a second graphical method whereby greater accuracy san be obtained and the amblysis for beam characteristic may be mode at any desired distance between the searehlight and the plane of amalyeis. The methol is moveover perfectly general in its applieability, and by ohvious changes the solution might be applicd to light sources of syuare or rectangular form. With this graphical method ats a stamdard, the usefulness of certain equations previously developed is shown to be limited in some dircetions. The fimal paragraphe deal with the sedection of the best testing distances, which is one of the main goals of these studies. In a fortheoming issue the methods here developed will be applied to concrete examples of searchlight design, and the data of the high-intensity anc will be used exelusively.-Ebror.


## Second Graphical Method of Obtaining the Beam Characteristic

## Elliptical Elemental Image

In a previous section,* the beam from a double-disk source was built up for a mirror having a generating angle of 120 deg. ; but in the introduction of that description, note was made of the conditions under whieh the method of circular elemental images was lacking in accuracy. It is now proposed to go into the details of a similar method based on elliptical elemental images. This method, while not so simple as the previous one, is perfectly general in its application and may be used to determine beam intensities from odd shaped sources, from defective mirrors, or to obtain the distribution of light in the beam at short range.

The maximum dimension of the elemental image from a section of a mirror, at an angle $a$ from the axis, is

$$
\begin{equation*}
C_{\text {max. }}=\frac{57.2 S r}{F}(1+\cos a) \text { deg. } \tag{114}
\end{equation*}
$$

The minor axis is equal to the major axis foreshortened by the angle $a$, or

$$
\begin{equation*}
C_{m i n}=\frac{57.28 r}{F}(1+\cos a) \cos a \mathrm{deg} . \tag{115}
\end{equation*}
$$

and, as already derived, the average diameter of the elliptical beam is

$$
\begin{equation*}
C_{\text {are. }}=\frac{5 \overline{2} .2 \delta r}{F}(1+\cos a) \sqrt{\cos a} \mathrm{deg} . \tag{113}
\end{equation*}
$$

These three diameters, maximum, minimum, and the average that gives a circle of equal area, are plotted in Fig. 72. The average falls to zero at 90 deg. for although the image has considerable length, the width is zero; that is, it is the image of a line of zero area. The maximum corresponds exactly to the diameter of the image from a spherical source.

[^85]The curves are for the particular case of $r=0.01 \mathrm{~F}$ but the application to any other diameter of source is readily made by multiplying by the proper factor, as the beam width is directly proportional to the relation between $r$ and $F$


Fig. 72. The angular axial dimensions of the elemental beam images are plotted for ( $A$ ) the major axis, ( $C$ ) the minor axis, and ( $B$ ) the diameter of the circle of equivalent area. The ordinates are for the particular case where $r=0.01 F$

Taking an elemental image in its true elliptical form, the beam from a given mirror zone is derived graphically as illustrated in Fig. 74 . The angle $a$ is taken as 5.5 deg. so this ellipse represents the average fro $n$ a mirror zone centering about 5.5 deg. The width of the zone is largely a matter of choice, but in this region of the mirror a total width of 10 deg. is not too great for reasonable accuraey. It is assumed that the beam is being investigated at ranges suffieiently great that the distance between the axis of the beam (and mirror) and the axis of the elemental beam may be neglected.

The half ellipse in Fix. it was computed from equations (ill) and (11.i). and the height of the zonal mage was computed by equation (T! (r) fom the plane area of the mirror zones. The assumption is made that the brilliancy


Fig. 73. The elemental images are here drawn to scale, and by their changing size and ellipticity they illustrate the relation between mirror angle and the form of the elemental parts of the beam
of the source and the coefficient of the mirror are both unity, and the immediately following figures are computed uniformly on this basis.

The multitude of elemental clliptical images from a complete mirror zone


Fig. 74. The half ellipse below the horizontal axis is the elemental image from the $55-\mathrm{deg}$. point on the mirror, and the curve above the axis is the zonal image found by adding all the elemental images in the complete zone
overlap in the center to give a zonal image of full intensity over a circle of a diameter equal to the minor axis of the ellipse. This formation was illustrated in Fig. 6s and the central circle there corresponds to the flat crest of the zonal image of Fig. it. The outer di-

Fig. 75. The summation of all the zonal images gives the curve, shown by the solid line, for a $120-\mathrm{deg}$. mirror and a double-disk source of radius one-hundredth the focal length. The same mirror stopped down to 90 deg. and 60 deg. gives the beams shown by the dotted curves
ancter of the \%mal image is fixed bey the major axis. An internediate perint is foumd be noting what part of a concentrie aircle is inclucted in the edlipse and making the image intensity in this propertionat the same ratlius. In Fige it the long axis of the ellipse is taken as the zero line and radial lines are drawn at
 min.. so that these lines mark out ares of 2.5 , 50 , and in per cemt of the go dees. in the quadrant. Contimuing the circles from the intersection of the radials with the ellipse until they reach the base of the zonal imade, the perpendicular can then becrected to the proper proportional height to give points of $2.5,50$, and 7. per cent intensity of the zonal maximum.

This method may fairly be called exact, and providing the drawing is done carefully the results will have a degree of correctness that can hardly be hoped for in photometric measurements. The results of the graphical method using elliptical images is therefore regarded in the following pages as being the standard of accuracy

In Fig. 7.5, a beam from a 120 -deg. mirror is built up of such zonal images and the beams from a $90-$ deg. and a CO-deg. mirror are indicated by dotted lines. The beams are direct summations of the zonal beams with one minor exception. The width of the crest of the 60 -deg. beam is determined by the 60deg. position and not by the .in-deg. position in the middle of the zone. The erest is therefore slightly narrower than the narrow part of the $50-$ to $6(t)-\mathrm{deg}$. zonal image.

If the mirror contains a 90 -deg. zone, the beam must come to a point and the narrow crest indicated by the narrowest zonal width must be eliminated.

This illustration will be used later in making a comparison of the sereral methods for deriving the beam characteristics.

## A Curve Method of Deriving the Beam Characteristic

There is another way of using the data of equations (113). (114), and (11.5) that yields quick results, but as sereral items are left to the skill of the computer there is too much
"ruke of thumb" for it to be entirely reliable. In Fig. Cl , the total plane area of a mirror of anity focal length is ploted for angles ap to 120 deg. In Fig. 77 , curve $A$ is obtamed loy combining the elemental beam widthe as plotted in curve $A, F i g$. 22 , with the curve of mirror areas. Thus at mirror angle 60 deg., the maximum angular total width from Fig. 72 is $0 . s 6$ deg. (25.s min. radius) and the mirror area or beam intensity is 4.2 according to Fig. 76 . These data plot as shown he the circle on curve A, Fig. 77. Similarly, curve $B$ is derived from the curve of average width in Fig. 7 , and curve $C$ is derived from the curve of minimum width, and this curve determines the width of the crest.

If we use only the curve for the average diameter of the zonal image, the summation of curve $B$ will give a beam formation identical to that found by adding the zonal images in Fig. 70. The curve so obtained is in fair agreement with the curve from the elliptical images up to mirror angles of 70 or 80 deg.; but when the mirror is 90 deg . or over, the upper part is too square across the top and the sides of the upper part of the curve are too nearly vertical. This can be in part corrected by taking into consideration the long and short axes of the elemental ellipses, but before the curves for maximum and minimum width can be used certain features must be investigated a little further.

Curve $B$ in Fig. 77 which corresponds to equation (113) shows a maximum width between 100 and 120 deg. By differentiating (113), a maximum is found for an angle $a$ such that

$$
\cos a=-0.33333
$$

which indicates a maximum image width at $a=109 \mathrm{deg} .2 \mathrm{~min}$.
This angle can now be taken as marking out separate sections of the mirror which must be treated independently. There are thus ihree sections to a mirror extending beyond 109 deg .28 min . These sections are 0 deg. to 90 deg, then 109 deg. 28 min . back to 90 deg. and from 109 deg. 28 min . on to the limiting mirror angle. The inversion of angles in the second section was made on account of the beam from the $90-\mathrm{deg}$. zone furnishing the point. The three inner ellipses of Fig. 73 illustrate how the $90-\mathrm{deg}$. to $100-\mathrm{deg}$. zone furnished both the extreme edge light and the narrow beams that make up the central short peak of the total beam. The points of the first two beams thus join at 90 deg. on the curves as plotted in Fig. 77, and the bases
of sections two and three join at the intensity level of the 109-deg. zone.

Consider first the 0-to 90 -deg. section. The beam characteristic curve must conform in general to the curve of average widths, and come tangent to the curve of minimum widths at the upper part of the beams. In Fig. 77 , the dotted curve $E$ is plotted from the curve obtained with elliptical images and it is seen that this curve agrees with the foregroing condition.


Fig. 76. The area of a mirror of unity focal length projected on the focal plane is given by this curve. The relatively great importance of the outer zones is illustrated by the rapid progressive rise of the curve

The curve for a 60-deg. mirror is also derived in the same way and shows that a curve drawn tangent to the flat crest and also tangent to the average curve will satisfy the points taken from the accurately determined curve of Fig. 75. The question now is how to draw this doubly tangent curve without previously knowing its point of tangency. This is one feature where a "rule of thumb" must be used.

The second section of the mirror gives a beam of a maximum radius of 17 min . as determined by curve $A$ at the $90-\mathrm{deg}$. level. This same zone of the mirror also furnishes the beam of minimum spread for here the image is a line whose length is greater than
any of the images from higher angles. (See Fir. 73.) Hence curve $A$ has its maximum widh at 90 deg. and curve $C$ has its minimum width at the same angle. The doted curve $F$ which represents the beam from this section is tangent to the horizontal line at the $109-\mathrm{deg}$. level at a point determined by the A curve at the $90-$ deg. level, doubly tangent to curve $B$ at an intermediate point, and tangent to curve ( at the $9(i-d e g$. level. Likewise, the section of mirror between 109 and


Fig. 77. Curve $A$-The maximum dimensions of the elemental images give a characteristic identical with that of a spherical source
$B$-The characteristic derived from the average diameter of the image
$C$ - The characteristic derived from the mini mum diameter of the elemental image
$D$-Beam from a 60 -deg. mirror
$E$-Beam from a $90-\mathrm{deg}$. mirror. Derived from curves $B$ and $C$
$F$-Beam from mirror section from 90 to 109 deg .
$G$-Beam from mirror section from 109 to 120 deg .
$H$ - Beam from a 120 -deg. mirror from summation of $E, F$ and $G$

120 deg. has a characteristic $G$ tangent to the 109-deg. level, doubly tangent to $B$, and tangent at the upper end of $C$.

The summation of the three beams, $E, F$. and $G$, gives the solid curve $H$ on the left of Fig. 77. The crosses on this curve are from Fig. 75 and show that with the section beams
drawn as in the illustration, the agrement with the exact curve is complete.

With a little practice in drawing the dotted curves, it is probally possible to get the beam characteristic of any depth of mirror with a fair degree of aceuracy, and this method, in spite of the open gaps in the data, is therefore of some use as a first approximation.

## Characteristic at Short Range

If we think of the beam of light from an are searchlight in terms of the elemental images of which it is composed, the reason for the change in shape of the intensity curve at various ranges becomes at once apparent. The final beam formation is completed only when the distance between the centers of the extreme edre beams becomes negligible in comparison with the total beam width. At lesser ranges, there is a spurious width in nearly all parts of the beam and by a simple extension of the method for getting the zonal image from the elliptical elemental image, the beam characteristic at any range may be computed graphically: This will complete the study of the beam from a disk source as it gives us information about that section of the sides of the beam that was left untouched by the geometrical investigation and was covered for a special case by the last few sections on graphical construction.

As a starting point, let us investigate the distribution of light in a beam from a source of radius 0.01 in a mirror of unity focal length at the point where the curved edge of the beam begins for a 4.5 -deg. mirror. It is worth pointing out that with this angle the inversesquare region begins at exactly the same distance. This range therefore, has considerable importance as one might be tempted to try to analyze the beam from a ti-deg. mirror at a point where the full central intensity is first realized and where the excess width may be computed.

For an angle $a$ of 4.5 deg., we have

$$
L_{o}=137 \text { focal lengths }
$$

The center of each zonal beam is computed by equation (43) and the major and minor axes (the latter always on a radial line with the searchlight axis) are computed by equations (114) and (115).

In Figs. is to 89 inclusive, the zonal images are computed for each 10 -deg. zone up to 120 deg. It might have been advisable to have used narrower zones for angles beyond 90 deg. but for purposes of exposition the loss in accuracy of construction is not of great importance.


$$
\begin{aligned}
& \text { Fig. 86. The elemental } 1 \text { mage } \\
& \text { f.om } 85 \text { deg. is almost a straight } \\
& \text { line, and the maximum beam } \\
& \text { width is determined by points } \\
& \text { near the end of the major axis }
\end{aligned}
$$



the $35-\mathrm{deg}$. elemental image
at a distance $y$ from the
axis


Fig. 85. Zonal image from 70.
Fi
see only one-fifth of
luminous at one time


Fig. 84. The opening in the center
of the
image is half the diameter of the
image and the intensity is less
image and the intensity is less
than a quarter the full intensity Fig. 83. The zonal image from the
$50-\mathrm{deg}$. to $60-\mathrm{deg}$. zone is annular
in form and of about one-third full
intensity, as indicated by the
height of the image as compared
to the line abovethe horizontal axis



Fig. 87. The elemental image from 95 deg.
gives a weak annular beam of large radius
and small thickness

The cemter of the elliptical elemental image. Fig. st, is displated by the radial distance $y$ which is constant at all distances along the beam. The actual linear dimension of the image at 137 focal lengths and the relation between center of image and center of beam are plotted to scale in the ilhustration, and a series of crenly spaced semicireles are drawn concentrically about the beam axis. The proportion of each semicircle included within the ellipse is measured and this proportion is used as a factor to reduce the height of the zonal image immediately above the construction semicircles. Except for the separation of the two axes and the use of evenly spaced semicircles in place of evenly spaced radial lines, the method is the same as previously used for finding the zonal images from the elliptical beams.

The images from the zones beyond 50 deg., Fig. S3, ctc., are annular in form, and attention is called to the great reduction of intensity in these annular images below the intensity of the normal concentrated zonal image. In the particular case of the $90-$ to $100-\mathrm{deg}$. image, the reduction is to one eleventh, and the $110-$ to $120-\mathrm{deg}$. image is reduced to one twentyfifth.

In Fig. 90, the twelve zonal images are assembled for adding. The addition of the first six gives the characteristic shown by the dotted line. Later, a comparison of this curve and the corresponding curve of Fig. 75 will be made for the purpose of showing the precise effects of distance upon the beam formation. The beam intensities at double the distance, that is 27.5 focal lengths, is given


Fig. 90. Zonal images arranged for summation for beam formation at 137 F . The dotted curve is the beam from the 0 -deg. to $60-\mathrm{deg}$. sections. The solid curve to where it first approaches the horizontal axis is the 0 -deg. to $90-\mathrm{deg}$. beam. The outer sections of the solid curve are the annular beam from the $90-$ deg. to $120-$ deg. mirror section
in Fig. 91 along with the zonal images. The elliptical images of Figs. 78 to $\$ 9$ were used after reducing the distance between axes to half in every case. A doubling of the range makes each image twice as wide, and therefore the constant distance between axes is in
propertion reduced to one half. The graphical solution mast of anurse be repeated in cach case.


Fig. 91. At a range of $275 F$, the 0 -deg. to $60-\mathrm{deg}$. section gives a beam of nearly normal appearance. The 60 -deg. to 90 -deg. section adds to the shoulder of this beam, and the $90-\mathrm{deg}$. to $120-\mathrm{deg}$. section adds to the ower parts only, giving the solid curve for the characteristic of a 120 -deg. mirror

A further doubling of the distance to 5.50 focal lengths gives the characteristic of Fig. 92 , and at 1100 focal lengths the curves are as in Fig. 93. The progressive closing in of


Fig. 92. Beams from 60-deg., 90-deg. and 120 -deg. mirrors at 550 F range
the annular zonal images results in greater central intensities and a narrowing of the upper part of the beam. The triple maxima
at the longer ranges is an interesting feature that has appeared a momber of times in am incipiont form in the testing of bo-in. searehlights at esen for


Fig. 9.3. Beam formation at 1100 $F$. The $60-\mathrm{deg}$. mirror gives a beam of almost normal form but the wider mirrors give beams that are characteristic of this range only

The manner in which a beam changes in form at increasing range is illustrated in Figs. 94.95 , and 96 where the characteristic curves of beam intensities are plotted for three mir-


Fig. 94. The progressive change of beam formation at 137 F , $275 F, 550 F, 1100 F$ and infinity are here illustrated for a 60-deg. mirror
rors of 60 deg., 90 deg., and 120 deg., respectively, and of equal focal lengths. The beam from the $60-\mathrm{deg}$. mirror comes fairly rapidly into final form (which is here taken from Fig.
7.j) and the range of 1100 focal lengthe gives a curve that can barely be distinguished from the final form at extreme distances.

At short range, the crest of the 60 - -leg. beam is either missing in its full intensity or reduced in width. The erest gets wider as the range inereases, but never exceeds the final width. The elge of the beam, at the point of zoro intensity, first exceeds the final width but quickly decreases to about its final value; but keeps always on the outer side of that point. There is a region near the top of the curves where the heam is first too narrow, then too wide, so that in this region there is ahwass a reasonable doubt as to the direction of error in a test, unless of course we solve that particular combination of source and mirror in a manner similar to the particular case of Fig. ! $)$.

The beam from the 90 -deg. mirror comes to its final form very slowly, and here the last point to come into practical agreement is the central point of the beam. This is a result of the shape of the image given by the !(0)-deg.


Fig. 95. A 90-deg, mirror gives a beam characteristic that is sharply pointed but the test distance must greatly exceed $1100 F$ as shown by the upper dotted curve compared with the solid curve for infinity. The lower dotted curve is for a range of 137 F , and the three above it are for distances of $275 F, 550 F$ and $1100 F$
zone, and if reference is made to the curves of Fig. 50 (showing the increase for a different combination of source and mirror) it will be seen that no further finite increase of range


Fig．96．The progressive alteration in the distribution of light in the beam is illustrated by this series of curves．For each doubling of the test range the central intensity is increased by a constant amount．After one or two further doublings of the distance there will be a sudden increase and then a slower increase for additional ranges．The changing rate of increase is due to the introduction of an active outer zone on the mirror as was illustrated for the spherical source
will bring the comtal intensity up to its full maximum

The two very pronombed peaks on the
 able to the sambe geometrical relations that gave the outer \％once of light in the mirror of Fig．is．The light from this active outer \％one is still confined wo the outer part of the beam at the greatest range hore considered，and very greatly increased ranges must be used to make these ammar zones join on the axis． The data of the 120 －dege mirror of Firs．． 0 and isl were for a beam of a source of radius 0.0960 Fo white we are here considermeng a sonrce of radius 0．0］$F$ ．＇The equivalent of the 1100 focal－kength distance for the larger source is 1100 divided bey 9.62 （the ratio of beam widths）and multiplied by 2．（i）（the ratio of foeal lengths）．This gives 2etrin．on the 120 －deg．Curve of Fig．iot．This is less than half the distance where light from the outer zones of the mirror reaches the axis and where the sharp rise in intensity takes place：and accordingly no further marked increase in the central heights of the curves of Fig． 96 can be expected short of a range of 2．500 focal lengths；and a reasonably close approach to the final maximum does not occur until the range is between $50(0)$ and （60）0）focal lengths．

## Computation of Beam Characteristic

It was shown in the description of the ＂Curve Method of Deriving the Beam Char－ acteristic，＂page $2=1$ ，that at best only a part of the beam characteristic curve followed the curve for the average width of the zonal image．Any formulas based on the same images must have the same limitations，and we get by our computations the curves of Fig． 71 and not those of Fig．it．As has been mentioned several times，the accuracy of the curve from the average zonal image is good for mirrors of 60 deg ．or less but there is a great loss of accuracy when the mirror con－ tains a 90 －deg．zone．

The mirror must first be considered as made up of three sections，and to atoid confusion，let the mirror angle in the 0－deg．to 90 －deg． section be designated by $a_{1}$ ，the angle in the section from 109 deg． 2.2 min ．to 90 deg．be denoted by $a_{2}$ ，and mirror angles higher than 109 deg ． 2 min ．be denoted by $a_{3}$ ．

Equations for points on the three sectional beams are therefore

$$
\begin{gather*}
C_{a: \epsilon .}=\frac{5 \overline{5} \cdot 2 \backslash r}{F}\left(1+\cos a_{1}\right) \sqrt{\cos a_{1}} \text { deg. }  \tag{116}\\
I_{a_{1}}=4 \pi B k \tan ^{2} \frac{a_{1}}{2} \text { candles }
\end{gather*}
$$

for the lirst secelion, and
for the second seetion. The value 2 in the brateket is the square of the tangent of one latf 109 deg. 2N min. The third section has the equation

$$
\begin{align*}
& C_{a r e}=\frac{5 \overline{-} \cdot 2 S r}{\pi}\left(1+\cos a_{3}\right) \^{\prime} \cos a_{3} \ln \operatorname{cog} . \\
& I_{a_{3}}=4 \pi B k^{2}\left(1: 11^{2} \frac{\left(I_{3}\right.}{2}-2\right) \text { canclles } \tag{11K}
\end{align*}
$$

In using these equations, it is necessary to plot the individual sectional heams becanse the values of $I_{a_{1}}, I_{a_{2}}$, and $I_{a_{3}}$ cannot be added unless they fall at the same angle in the beam, that is, $C_{\text {are }}$ must have a common value. They can have a common value only if a trial solution is made for equal values of $C_{\text {are. (which is a long operation) }}$ or if the curves of Fig. 73 are used to pick out equal values.

## Testing Distance for Entire Characteristic

In dealing with arc scarchlights of the larger sizes, the required testing distance sometimes extends into thousands of feet and a new factor enters. This is the absorption of light by the atmosphere. If the absorption were uniform in all parts of the beam, we could measure the quantity of light at short range and again at long range and correct the characteristic curve at long range by a constant factor to compensate for the loss in the atmosphere. The actual problem is not so simple because it has been found that there is a progressive alteration in beam formation that is in addition to the orderly geometrical phenomenon already discussed. This additional change arises from the selective absorption and scattering of light by the atmosphere combined with a change in color composition between the center and the edge of the beam. As a rule, the edges of the beam are richer in blue and violet light, and these are the colors that are most quickly absorbed by the atmosphere. The result is a narrowing of the beam that might possibly deceive the experimenter into thinking that the searchlight was in some manner improperly focused.

Two views may be taken of the practical importance of this phenomenon. We may take the view that if service conditions require long ranges then the test should be
taken at the service distance. The difficulty here is that the phenomenon of narrowing and otherwise changing is apendent both in nature and degree upon the precise condition of the atmosphere. We know, of course, that the atmosphere goes through all kinds of variations in its transmitting properties and therefore we could not after all hope to have the test and service conditions agree.

The other way of looking at the matter is to find the beam formation under conditions where the influence of the atmosphere is a mininum and thus climinate one unknown quantity. This requires a short test distance and we must therefore establish a minimum distance that will give data of satisfactory accuracy:

Take first the case of a plain carbon arc with a $60-\mathrm{deg}$. mirror. If reference is made to the characteristic curves of Fig. 94 the greatest deviation of intensity and width is seen to occur near the shoulders of the curves where the inverse-square region joins the sloping sides. This is directly related to the width of the inverse-square region itself, and equation (54) should therefore be our guide in all cases where we are free to choose the testing range. In Fig. 94, the short range curve that best agrees with the curve for an infinite distance is at a distance of nearly $4 L_{o}$ from the searchlight. In Fig. 94, the upper finite range curve is at 1100 focal lengths while $4 L_{o}$ for this $60-$ deg. mirror gives 1200 focal lengths.

It would not do to attempt to make a fixed rule for all projectors for the reason that in many cases $L_{o}$ is infinite, and we must therefore look for other data on which to form an estimate in the particular case of mirrors extending to 90 deg. In Fig. 95, the beams are all considerably below the theoretical maximum, but it must be remembered that the sharp point to the limiting curve is based on a mirror accuracy that belongs in the realm of the optics of astronomy and is never encountered in searchlight practice. A moderate scattering of light in the center of the beam will increase the intensity of the adjacent points and thus mirror defects wilh tend even at extreme testing distances to give the upper triple-peaked beam of Fig. 95, and this wider beam will of course not be so sensitive to change in range. Just as an arbitrary rule, we may therefore take $L_{e}$ for our base of computation and make the testing range $4 L_{e}$ when $L_{e}$ is computed for the $90-\mathrm{deg}$. zone of the mirror. For the 90-deg. mirror of Fig. 95,
this would call for a testing distance of 1600 focal lengths.

A mirror of wider angle than 90 deg. maturally requires a greater range than one of gust io deg. hat this additional distance will perhaps not be great and at a maximum biLe would seem to be sufficient. The peak
of the jeleal come greathe excerds the best short rampe corve of Fig. . $\mathrm{l}_{\mathrm{i}}$, but in any actual case the great eoncemtation of energy in the center of the leam camm lo mathaned and the working range for this miror is brought within more reasonalle limits.
(scries be be watimuled)

# The Mounting of Diamonds by the Casting Method 

By Howard Miller<br>Hean of Testing Laboratory, Fort Waye Works of General Electric Company

The importance of correct setting of diamonds used for truing abrasive wheels cannot be over emphasized, for incorrect setting probably is responsible for more loss of stones than any other cause. A correct setting of any stone incolves two major factors. First, the stone must be so placed that the best cutting point is available for use, included in which operation is a proper orientation of the stone to minimize shattering. Sccond, the stone with the exception of the small point exposed for use should be securely anchored.

Many schemes have been developed for mounting diamonds and it goes without saying that there are a number of successful methods in everyday use. However, all of them require expert knowledge gained only after long experience. This is always true of the correct placing of the stone which constitutes the greatest problem in setting. The mechanical operation of anchoring the stone is also important; and it is the purpose of this article to describe an anchoring method which it is felt will be of interest to everyone using diamonds for the purpose under consideration.

It is evident that the most secure mounting is that in which the diamond is entirely surrounded by a relatively hard and tough material, impervious to the heat generated during the truing process. This of course requires pouring or tamping around the diamond a material having a sufficient degree of fluidity to conform to the contour of the stone, and has usually been done either by molten metal or mercury amalgams. The use of molten metal, especially the operation known as brazing where brass is used, subjects the diamond to a more or less high temperature with the possibility of doing harm to the stone unless great skill and care is used.

The use of lower melting point alloys is therefore to be recommended.

In the method about to be described, the diamond is properly held by supporting wires and placed in the bottom of a split mold similar to a bullet mold. The stone and mold are then slowly heated to about 3.50 deg. F. The mold is then poured full of molten alloy which has previously been melted in the small electric furnace shown in Fig. 1. This alloy, familiar to the trade as Sampson Metal, is a mixture of
Zinc. . . . . . . . . . . . . . . . . . . . . . . . . . 90 per cent
Copper.. . . . . . . . . . . . . . . 5 per cent
Aluminum . . . . . . . . . . . . . . . 5 per cent

It has a melting point of about 6.50 deg. $F$.. and a Brinell hardness of about 7s. Thus its relatively low melting point permits casting at temperatures that will not hurt the stone and at the same time the material is sufficiently strong and hard to hold the diamond properly.

In developing a suitable alloy; a number of different varieties were made the subject of experiment, especially those of the aluminum series. This series was first suggested because aluminum has a somewhat lower melting point than brass. It was soon found that stones set in pure aluminum loosened and chattered after being used a short time; and on cutting open the nib, it was seen that air pockets had developed at the rear of the diamond which resulted in its becoming loosened. This was mainly attributed to the diamond having floated slightly when the aluminum was poured into the nib. The diamond was then anchored securely in the bottom of the bullet mold by means of copper wire. Better results were obtained but still the diamond would loosen slightly, due
apharently to the chatacteristic softhess of pure almmintmo. A copper harelened aluminum wats then tried amd the results were much better. Howerer, the melting and peotring chanacteristios of the almminmm alloys are somewhat critical, especially in such smatl castings as these. Efforts were hen directed
work. Fig. $\because \quad$ shows sections of diamond setlings made with this alloy. It will be noted that the diamond is firmly embedded in the nib.

The furnace shown in Fig. I is built uj) of fire brick and refractory cement so eonstructed as to hold a small graphite erucible. Two


Fig. 1. Electric Arc Furnace Supplied with Energy from the Standard Compensarc in the Foreground. The combination is here employed for melting the alloys in which abrasive diamonds are mounted
to the zinc series. The best results were obtained by the use of the zinc-copperaluminum mentioned; and it is believed that the relative ease with which this alloy can be melted and poured together with a fair degree of hardness, recommends it for this class of
carbons are inserted through the refractory wall, one from each side, and by means of a standard Compensarc an arc is drawn between the crucible and the electrodes which quickly melts the metal in the crucible. This type of furnace has been found very convenient for
melting small guantides of allose both in an experimental way and for limited production. It provides a clean, ready somere of heat: and as the current is casile controlled, the heat can also be controlled so that once the metal is melted it can be kept molten at ane temper-
are ham controlled, and in stant the furnace it is mily necessmy (o bing them in cemtact with the coucible and draw them away slighteg. It is pussible wome a chatge of the alloy in about 1.5 min., after which the cursent can be regulated to maintan the proper


Fig. 2. Sections of several diamond mountings produced by the method described in this article
ature desired by controlling the current. The life of the crucible is very good and the expense of renewal is nominal. It has been found that about a five-eighth inch diameter white flame cored carbon for one electrode and an extremely hard carbon for the other gives the best operating results. The carbons
pouring temperature. The convenience of a melting furnace of this type can be appreciated in connection with work such as the setting of diamonds where its use is only intermittent. It always is ready for use, will melt a charge very quickly, and when the work has been done it is only necessary to pull a switch.

# The Temperature and Brightness of Tungsten Lamps 

By IV．E．Forsythe<br>


#### Abstract

Ifter some general remarks on the brightness and temperature of incandescent lamp filaments the athor Wescruces the three different ways of measuring the brightness of tungsten．Valuable data are given in the four tables in the article．－EnITOR．


Tungsten lamps are now manufactured in a great varicty of sizes and types and the different sizes and types are not all operated at the same temperature In gen－ eral the higher wattage lamps are operated at higher temperatures．As a result of meas－ urements made in Nela Research Laboratory for various purposes over a period of several years，considerable data have been accumu－ lated on the temperature and brightness of tungsten lamps．

The filament of a vacuum tungsten lamp unless it is a miniature lamp is practically all at the same temperature and thus at the same brightness．There is，it is true，a portion of the filament near the leads and supports where the temperature is lower than the main part of the firament．That the integral effect of this difference in temperature is not very marked is seen when the color temperature of such a lamp is measured first as a whole and then with the ends screened so as to cut off the light from the cooled portion．For an ordi－ nary vacuum lamp the difference in color tem－ perature for the ends screened and the ends unscreened is only about 9 deg．for 2500 deg． K ，the color temperature corresponding to about 10 lumens per watt．This，however， is not the case for a miniature vacuum lamp or gas－filled lamp where the temperature of the filament is not as uniform．

The energy loss from the heated filament of a gas－filled lamp，due to the surrounding gas，has been shown＊to depend upon the diameter of the filament，being relatively much smaller for the larger filaments．To get the effect of a large diameter with a small wire the filament of a gas－filled lamp is coiled in the form of a helix．This has been found to have about the same effect in reducing the gas loss as would result from a filament of the same diameter as the coil．

There are two reasons why the higher wattage gas－filled lamps have a higher efficiency than the smaller lamp of this type． In the first place the larger filaments can

[^86]be wound in larger helices and still be strong enongh to keep their shape throughout their life．Also the larger wire can be operated at a higher temperature，since a small amount of evaporation from the surface does not affect the resistance of the large filament as much as it does the smaller one．

In this article，whenever the temperature of a lamp is given it is to be understood that the maximum temperature of the filament is meant．The values given，in general， represent the average of a number of measure－ ments on a number of different lamps．

The temperatures given in this article are on the scale adopted by the General Electric Company for use in its laboratories．$\dagger$ This temperature scale is based upon the assump－ tion of Wien＇s equation with $c_{2}$ taken as $143.50 \mu \mathrm{deg}$ ．and upon the melting point of gold taken as 1336 deg．K．（deg．C．＋273）． On this scale the melting point of palladium has been found to be $182 \$$ deg．K．For con－ venience in the calibration of optical pyrom－ eters，a black body held at the melting point of palladium is used as a point of reference．

When measuring the temperature of a lamp filament it is necessary to use some form of optical or radiation pyrometer．If the temperature of the filament is not uniform or if for some reason the temperature of only a small portion of it is desired，the disappearing filament optical pyrometer is the best type to use．

Practically all solid substances when heated to a sufficiently high temperature begin to glow，giving off at first a very deep red light of low intensity．As the temperature is raised the intensity of the light increases rery rapidly and at the same time the color changes first to lighter red，then to an orange， etc．，tending to approach white at higher temperatures．Although the brightness of any source that is heated depends upon its temperature，all substances are not equally bright at the same temperature．Black objects that absorb practically all the radia－ tion they receive when cold are，when at a high temperature，brighter than other
objects that reflect a large portion of the light they receive when cold. Thus one should not expeet a bright metal like tungsten to emit as much light per unit area at a high temperature as carbon which is black at ordinary temperatures. The amount of light emitted per unit area is not, however, the sole measure of efficiency. 'This depends upon how the substance radiates both in the risible and infra-red portion of the spectrum.

The standard of radiation is the "black body" that theoretically absorbs all the radiation that it receires. It has been shown that the black body radiates so that the following equation, for values of the product $\lambda T$ less than 3000 , represents the relation between the temperature and the intensity of the energy radiated for a particular wavelength interval

$$
\left[E_{\lambda}=c_{1} \lambda^{-\bar{s}} e^{-\frac{C_{2}}{\lambda T}}\right]
$$

where $E_{\wedge}$ is the energy intensity, $\lambda$ the wavelength expressed in $\mu$, and $T$ the temperature in degrees Kelvin, $C_{1}$ and $C_{2}$ being constants. For the visible spectrum, where the longest wavelength is in general less than $0.8 \mu$, $T$, the temperature can have a very high value and still the product $\lambda T$ be less than 3000 . Thus this equation is satisfactory to use for this region of wavelengths for as high temperatures as are ordinarily dealt with. A cavity with walls at a uniform temperature containing a small opening for observation approximates very closely the ideal black body:

All other bodies, when the radiation is due to thermal causes alone, are less bright than the black body at the same temperature, not only for the total radiation but for the different wavelengths. This is expressed in the form of an equation as follows:

$$
\left[E_{\lambda}^{\prime}=\epsilon_{\lambda}^{\prime} c_{1} \lambda^{-5} e^{-\frac{C_{2}}{\lambda T}}\right]
$$

where $E_{\lambda}^{\prime}$ is the energy intensity for the wavelength interval with center at $\lambda$ and $\epsilon_{\lambda}$, which has a value less than unity, is the emissive power of the substance studied. The emissive power depends not only upon the substance studied but may vary with both the wavelength and temperature. From this equation it is very evident that if the emissive power is known for any wavelength the temperature can be determined from a measurement of the energy intensity for the same wavelength interval. Worthing,* by making a black body of a tungsten tube with

[^87]a small radial hole for olservation and monnting this in a lamp bulb, so as to heat it electrically, was able to dotermine the emissiow power of tumgsten for different wavelengths and different tomperatures. He measured the true temperature from observations through the small hole and the relative brightness of the black body and tungsten at the same temperature by ofservations through the hole for the black body and on the outside of the tube for the tungsten brightness.

The temperatures of the various lamp filaments were measured using a disappearing filament optical pyrometer having as the monochromatic screen a red glass. This glass transmits enough light so that accurate measurements can be readily made for temperatures as low as that of melting gold ( 1336 deg. K.) and is sufficiently monochromatic so that photometric balances can be made accurately even when there is a temperature difference of 1500 deg. C. or more between the source and the pyrometer filament.

An optical pyrometer gives the relative brightnesses of the surfaces compared. If the temperature of a particular substance is determined from its brightness as if it were a black body, too low a value for the temperature will be obtained, since, as was mentioned above, no known radiator is as bright as the black body when at the same temperature. Such temperatures are called brightness temperatures and will in general be different for different wavelength intervals. Thus when a brightness temperature of say 1.500 deg. K . for $\lambda=0.66 .5 \mu$ is given, it means that the substance as studied has the brightness of a black body at 1500 deg. K. for $\lambda=0.665 \mu$.

The brightness temperatures of tungsten obtained by the use of the optical pyrometer were reduced to true temperatures by making use of the emissive powers of tungsten that have been determined by Worthing by the method outlined above. The true temperature and brightness temperature are related as follows:

$$
\frac{1}{T}-\frac{1}{S}=\frac{\log \epsilon_{\lambda} \cdot \lambda}{C_{2} \log e} .
$$

where $T$ is the true temperature and $S$ and $\epsilon_{\lambda}$ the brightness temperature and the emissive power corresponding to the wavelength $\lambda$.

The temperature and brightness of the filaments of some of the lamps with bulbs
that ate bot transpatent was determined either be measurememts on the lamps before they were made non-tamsparent or bey having filanents of the same kind monnted in char bathes abl operated at the same voltage in the clear buth as in the other bulb. If the filaments had exactly the same dimensions they should be operated so as to be at the same resistance rather than at the same voltage for the same temperature. For the filaments that were studied the arerage of the results on the resistance for the same voltage were higher in the elear bulbs than in the other bulbs, which is contrary to what might be expected. The brightness temperature of some of the lamps with blue bulbs was measured using a blue glass as the monochromatic sereen of the optical pyrometer. These brightness temperatures were then reduced to true temperatures using the known data on tungsten.

TABLE I
TEMPERATURE AND BRIGHTNESS OF VACUUM LAMPS

| Lamp | Lumens per Watt | Tempera. ture ${ }^{\circ} \mathrm{K}$. | Brightness Candies $\mathrm{cm}^{2}$ |
| :---: | :---: | :---: | :---: |
| 50 -watt carbon | 3.3 | 2115 | 55 |
| 50-watt gem | 4.0 | 2180 | 78 |
| 50 -watt tantalum | 4.9 | 2160 | 53 |
| 10-watt tungsten | 7.7 | 2355 | 128 |
| 25-watt tungsten. | 9.8 | 2450 | 191 |
| 40-watt tungsten. | 10.3 | 2475 | 212 |
| 60-watt tungsten. | 10.3 | 2475 | 212 |

Knowing the temperature of the tungsten filament it is of course possible from the known data to get its brightness in candles per square centimeters. When the brightness of a light source is spoken of, in general, what is meant is the maximum brightness. The inside of the coil of a gas-filled lamp is much brighter than the outside. This is due to the fact that the brightness of the inside of a particular coil is made up of the regular radiation from the inside of that coil and radiation from the inside of other coils that seem to come from this coil by repeated reflections. The brightnesses of the filaments of the different types of lamps as well as the brightness of the inside of the coils for the large lamps were measured. The outside brightness of the bulb for some of the frosted and sprayed lamps was measured.

These brightnesses were measured by one or more of three different methods. The

[^88]first was the direet method where the candlepower of a filament of known length and cross section or a definite area of the bulb was measured and from such data the brightness caleulated. The seeond method was to measure the brightness of the different sources with a disappearing filament optical pyrometer used as a brightness photometer.* In this case the glass used as a monochromatic sereen was one that had an effective wavekength about equal to the Crova wavelength for a particular temperature interval and changed about the same amount as does the Crova wavelength for different temperature intervals. The Crova wavelength is defined as the wavelength for which the monochromatic change in brightness for a particular temperature interval is the same as the brightness change for the entire visible spectrum. Thus it is possible to measure relative brightnesses using the Crova

TABLE II
BRIGHTNESS OF TUNGSTEN AT VARIOUS TEMPERATURES

| Temperature | Lumens per Watt | Brightness |
| :---: | :---: | :---: |
| 1800 | 1.2 |  |
| 1900 | 1.9 | 10.2 |
| 2000 | 2.7 | 20.2 |
| 2100 | 3.8 | 35.8 |
| 2200 | 5.3 | 61.7 |
| 2300 | 6.9 | 105.0 |
| 2400 | 8.9 | 155.0 |
| 2500 | 11.2 | 234.0 |
| 2600 | 13.6 | 343.0 |
| 2700 | 16.9 | 482.0 |
| 2800 | 19.8 | 679.0 |
|  |  | - |

wavelength, without having trouble due to color difference. Since it was impossible to get a glass that would give exactly the Crova wavelength, corrections had to be made where the difference in wavelength became large. Knowing the effective wavelength of the glass, the Crova wavelength and the color temperature of the source, such corrections could readily be made.

The third method, applicable only to filaments of uniform temperature, was to measure the color and brightness temperatures and making use of the known brightness of the black body to compute the brightness of the filament thus measured. The color temperature of a source is defined as the temperature at which it is necessary to operate a black body so that the light from the black body will have the same integral color as that from the source studied. This
means in general that the stmures studied and the back bow hate the same dist ribution of encrgy in the visible spectrom. In general. however, when operating at the same color the hack bedy will be brighter than other sources, that is, each ordinate of the curve representing the energy of the source studied will be some fraction (l ド) of the corresponding ordinate of the black body. Thus the brightness $B$, of the somere studied is given hy

$$
B=\frac{B_{B B}}{K}
$$

where $B_{B B}$ is the brightness of the black body at a temperature the same as the color

For some of the brightasesses it was onty pessible to use the secomed metherf, that is the optical perometer (alibrated as a phomencter.

The relation between the eflacience of an ordinary vacumm tumsten lamp as a light sonter and also its brightness in candles per square exatimeter and temperature is given in Table 1. The temperatures and brightnesses were measured far enough away from a lead or support so ats mot tobe affeeted We the cooling dae to conduction of the leads. If the values of the efticiency given were corrected for end losses, they would be about eight per cent higher.* At a temperature of 24.0 deg. K the tungsten lamp has an efficience of about 10 lumens per watt and

TABLE 111
TEMPERATURE AND BRIGHTNESS OF VARIOUS GAS-FILLED TUNGSTEN LAMPS

| Lamp | Lumens per Watt | $\begin{gathered} \text { Temperature } \\ \stackrel{\mathrm{K} .}{ } \end{gathered}$ | $\begin{gathered} \text { Color } \\ \text { Temperature } \\ \text { K } \end{gathered}$ | Brightness of Flament Candle. m |
| :---: | :---: | :---: | :---: | :---: |
| Regular Gas-filled Lamps |  |  |  |  |
| 50-watt | 10.0 | 2685 | 2670 | 462 |
| T-5-wat | 11.8 | 2735 | 270.5 | 546 |
| 100-wat | 12.9 | 2760 | 2741 | $39 \%$ |
| 200 -wat | 15.2 | 2840 | 2810 | 788 |
| 300-watt | 16.3 | 28.5) | 2x:30 | 802 |
| 500-watt | 18.1 | 29331 | 29.20 | 1000 |
| 1000-watt | 20.0 | 3990 | 2!80 | 119.0 |
| 2000 -watt | 21.2 | 3020 | 3000 | 1295 |
| Special Lamps |  |  |  |  |
| 1000-watt stereopticon | 24.2 | 3185 | 3175 | 2018 |
| 900 -watt movic | 27.3 | 3290 | 3200 | 26.36 |
| 10 kw . | 31.0 | 3350 | :3300 | 303.34 |
| 30 kw . | 31.0 | 3:350 | :33011 | $30: 34$ |
| Daylite Lamps |  | - |  |  |
| 200-watt | 10.0 | 2860 |  |  |
| 500 -watt | 11.2 | 2960 |  |  |
| Photographic |  |  |  |  |
| 750-watt |  | 3065 |  |  |
| 1500-watt |  | 310.5 |  |  |

temperature of the source studied, and $K$ is given by the following equation:

$$
\log K=\frac{C_{2} \log e}{\lambda}\left(\frac{1}{T_{C}}-\frac{1}{S}\right)
$$

where $T_{c}$ is the color temperature of the source studied and $S$ the brightness temperature corresponding to wavelength $\lambda$.

The three methods outlined above have been used in a determination of the brightness of tungsten as a function of temperature. The values thus obtained agreed within experimental error. The brightnesses given in this article were measured by two of the above methods, whenever it was possible.

[^89]a life of about one thousand hours. As the temperature is increased the life is decreased very rapidly until at about 2800 deg. K. the life would only be about seventy hours.

In Table II the efficiency of some of the vacuum tungsten lamps is given. For comparison data are included on carbon and tantalum lamps. These lamps are all operated at such an efficiency that the life will be one thousand hours. The 60 -watt tungsten lamp that was in use a few years ago operated at about $7 . \mathrm{s}$ lumens per watt for a life of one thousand hours. A comparison of this value with that given in the table will show that the efficiency has been increased about thirty per cent. This increase
hats 1 een hromght about ber more refined and better eontrolled gromesses of mantulacture.

Ln 'Table $1\|\|$ some data are given on the cffeconey, temperature and brightness of some of the present day gras-filled lamps. 'The bamps listed in the first part of the table are some of the regrular clear gas-filled lamps. They are operated at such a temperature that they have a life of one thousand hours. In column four are given the color temperatures of some of these lamps. 'The color temperature is abont twenty to thirty degrees lower than the true temperature. 'This is because the color temperature is for the whole lamp while the true temperature refers to the hottest part of the filament. A comparison
while that of the $30-\mathrm{kw}$. lamp is about 7 hy 11 cm . It is interesting to note that the 10-kw. lamp has an intensity of about 40,0000 candles in a direction jerpendicular to the coils while the $30-\mathrm{kw}$. has an intensity of about 100,000 candles in the same direction. This means that the $10-\mathrm{kw}$. lamp wouk give the same illamination at a distance of two fect from the plane of the coils as is received from the sun in mid-summer. The $30-\mathrm{kw}$. lamp would give this same illumination at a distance of about $31 / 2$ feet from the plane of its coils. Since the temperature of the lamp is much lower than the sun the amount of heat received from the lamps at this distance is much greater than from the sun.
table iv
BRIGHTNESS OF FILAMENTS AND BULBS OF SOME TUNGSTEN LAMPS TOGETHER WITH
THE BRIGHTNESS OF SOME OTHER SOURCES FOR COMPARISON

| Lamp | Brightness Measured at | $\begin{gathered} \text { Brightness } \\ \text { Candles } \\ \mathrm{cm}^{2} \end{gathered}$ |
| :---: | :---: | :---: |
| Kerosene flame. | Flat wick | 1.2 |
| 4-watt per candle carbon lamp | Filament | 55.0 |
| 40 -watt vacuum tungsten lamp. | Filament | 212.0 |
| 40 -watt vacuum tungsten lamp. | Bulb frosted | 2.5 |
| 40 -watt golden Mazda. | Bulb | 2.0 |
| 50 -watt White Mazda. | Filament | 408.0 |
| 50 -watt White Mazda. | Bulb | 1.3 |
| 75 -watt White Mlazda sprayed. | Filament | 546.0 |
| 75 -watt White Mazda sprayed. | Bulb | 2.1 |
| 2000-watt gas-filled Mazda.... | Filament | 1295.0 |
| 2000 -watt gas-filled Mazda | Between coil | 3000.0 |
| 2000-watt gas-filled Mazda | Bulb frosted | 130.0 |
| Sun as observed at earth's surface |  | 165,000.0 |
| Clear sky, average............. |  | 0.4 |

with Table II will show how much it has been possible to increase the efficiency by raising the temperature and still maintain the one thousand hours' life by the introduction of an atmosphere of an inert gas. The lamps on which data are given in the second part of the table are for special purposes. They are operated at a temperature that will give either the desired brightness or efficiency. In general they do not have as long a life as the regular lamps. The $10-$ and $30-\mathrm{kw}$. lamps are some special lamps that were designed and constructed by the Lamp Development Laboratory of the National Lamp Works for some special studio motion picture work. These lamps are constructed with four coils in the same plane. The plane covered by the coil of the $10-\mathrm{kw}$. lamp is about 4 by 5 cm .,

The temperatures in the third part of the table are for some of the lamps with blue bulbs called daylite and photographic lamps. The daylite lamps are operated at a temperature somewhat higher than the corresponding sizes in the clear bulbs so that their life is seven hundred and fifty hours. The photographic lamps are operated at a slightly higher temperature than the daylite lamps in order to increase their intensity in the blue end of the spectrum.

In Table IV are given data on the brightness of the bulbs and filaments of some of the tungsten lamps with some other sources included for purposes of comparison. The data show how much the maximum brightness of the different lamps is reduced by frosting or spraying the bulb.

# Ten Years of Voltage Standardization 

By M. D. Cooper

Enginembing Department, Nathonal. Lamp Works of Genferal Eleftrb Company


#### Abstract

The advent of the drawn-wire tungsten lamp enabled the manufacturer to make lamps of predetermined standard voltages. The author shows the result of ten years' work on the standardization of voltages in the lamp industry.-Editok.


That any industry to be successful must fulfill certain definite obligations with respect to the use of its products, is axiomatic. Fortunately, soon after the introduction of the drawn-wire tungsten filament lamp about 13 years ago it was recognized that the standardization of circuit voltage, which of course would lead to a standardization of lamp demand, was one of the most important problems confronting the lighting industry.

It is generally understood that the wide spread in central station voltages in the early days was due to the inability of manufacturers to make lamps to a specified voltage. As new stations were placed in operation they selected such odd voltages as would best utilize the manufacturers' product. Most of these voltages fell within the $100-130$ volt range. With the coming of the drawn-wire tungsten lamp, and improved methods of manufacture whereby lamps could be made accurately to a predetermined voltage, the whole order of things was changed and the work of standardizing was actively started.

The problem with which central stations were confronted was not one to be solved in a day. It involved a thorough engineering study and analysis of every phase of lighting and power practice-the generation and distribution of energy, as well as the electrical characteristics of all the many forms of current consuming apparatus using the service. The immensity of the problem is indicated by the fact that in many cases central station operating voltages had to be changed as much as 10 volts one way or the other in order to establish any basis of standardization. It had to be shown conclusively that readjustments of this magnitude were justified from the purely economic standpoint.

Although progress in voltage standardization has of necessity been slow, much has been accomplished in the last decade. Of greater importance, however, is the increasing evidence that the idea is fundamentally sound. Standardization of voltages is just as logical and just as desirable as standardization of lamp bases and of lamp types, both of which have contributed in no small part to the
tremendous growth of the lighting load in this country. Only recently, lamp engineers have made an intimate study of the lighting development of several leading foreign countries. This study clearly revealed the fact that the lack of standardization both in operating voltages and in types of lamps had been a serious hindrance to the development of the foreign lighting business. The effect of higher prices, slower deliveries, and the general inconvenience attending the use of any non-standardized product was plainly evident. The lamp consumption of seven of the leading foreign countries is less than twothirds of a lamp per capita per year as compared to a figure of about two lamps per capita in the United States,-a disparity which is in itself conclusive evidence that foreign peonies have not had full opportunity to use light economically.

In order to facilitate the work of voltage standardization, lamp manufacturers have for a number of years distributed as a guide to lamp supply a record of the operating voltages of individual central stations in this country. In Table I these figures are compiled and an interesting analysis of conditions is shown. The first three lines of this table show the number of communities and the corresponding total population in which the electric service is so closely regulated as to require only one lamp voltage for the entire community, and in which the voltage is a standard voltage, that is, 110,115 or 120 volts. From the standpoint of public lamp supply, these communities are the only ones which may be called completely standardized and, even here, there is a possibility that small isolated plants in these communities may require a lamp voltage differing from the standard of the central stations. It will be noted, however, that 91.5 per cent of the total number of communities are served under this condition of one standard central station voltage for the entire community; this corresponds to 83.5 per cent of the total population within reach of electrical service.

A further study of this summary indicates that future efforts must be directed not only
toward converting odd and high voltages (20) 0 -2(0) volts) to one of the three standard voltages but also toward the wnifuation of service voltages in commmities where more than one voltage is now used. The difficulty encountered in handling a stock of lamps of various voltages and in distributing the proper lamps to specified districts of a commonity, through the regular commercial channels, can be readily understood. It is also well recognized that the purchaser cannot be expected to differentiate between lamps which look exactly alike but which nevertheless will render vastly different degrees of satisfaction on his circuit. The solution of this distribution problem lies in unification of voltages.

Although the percentage of communities in which unification of service voltage at a single standard has not been accomplished is small (about 10 per cent of the total), the customers adverscly affected by this non-unification represent nearly 20 per cent of the total population to which electric service is available. To effect this unification, changes of 5 volts in many cases and of 10 volts in a few cases will be required.

To summarize, it is significant that from the standpoint of standardization only and without regard to complete unification, 95.2 per cent of the communities, representing 96.7 per cent of the electrical population, is served at one or


Fig. 1. Ten Years of Voltage Standardization
more of the three standard voltages; these figures compare with 74.1 per cent and 71.8 per cent respectively only four years ago.

One of the handicaps of the early voltage standardization movement was the lack of

TABLE I
AN ANALYSIS OF CENTRAL STATION PRACTICE BY LAMP VOLTAGES

| Lamp Voltage Recommended by Central Station | Numbe: of Communities |  | $\begin{gathered} \text { Per Cent of } \\ \text { Total } \end{gathered}$ |  | Population of Communities <br> (1920 Census) |  | $\begin{aligned} & \text { Per Cent of } \\ & \text { Total } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 110 volts only | 6,976 |  | 47.7 |  | 21,360,400 |  | 33.9 |  |
| 115 volts only | 5,221 |  | 35.6 |  | 24,282,400 |  | 38.4 |  |
| 120 volts only | 1,198 |  | 8.2 |  | 7,147,600 |  | 11.2 |  |
| Total, one standard voltage only |  | 13,395 |  | 91.5 |  | 52,790,400 |  | 83.5 |
| More than one standard voltage, one station. | 434 |  | 3.0 |  | 1,405,100 |  | 2.2 |  |
| More than one standard voltage, more than one station. | 106 |  | 0.7 |  | 6,961,100 |  | 11.0 |  |
| Total, standard voltage(s) only.. |  | 13,935 |  | 95.2 |  | 61,156,600 |  | 96.7 |
| 112 volts only | 11.8 |  | 0.8 |  | 333,500 |  | 0.5 |  |
| 125 volts only | 88 |  | 0.6 |  | 189,100 |  | 0.3 |  |
| Other voltage below 130 volts | 162 |  | 1.1 |  | 667,100 |  | 1.1 |  |
| 200 volts or higher. . . . . . . . . . . | 259 |  | 1.8 |  | 250,500 |  | 0.4 |  |
| Standard and odd voltages, one station | 59 |  | 0.4 |  | 337,000 |  | 0.5 |  |
| Standard and odd voltages, more than one station. | 17 |  | 0.1 |  | 318,000 |  | 0.5 |  |
| Grand Total |  | 14,638 |  | 100.0 |  | 63,251,800 |  | 100.0 |

information which would indicate in some degree the ultimate standard toward which central station practice was tending. It was in view of this sitmation, ogether with the fact that in some cases wide readjustments in central station voltages were physically and commercially impracticable (some stations were unable to raise their voltage above 110 volts owing to the limitations of their equipments while others could not greatly decrease their voltage without considerable increase in line copper) that the three voltage centers, I 10 , 115 , and 120 volts, were selected for lighting service. Fig. 1 is therefore of interest in this connection, charting as it does the course of lamp demand in the $100-130$ volt class for the past ten years. The chart is of historic
interest in that it shows the tremendous progress made in eliminating odd voltages; in the ten-gear period represented, the demand for lamps of odd voltages has decreased from over 5) per cent of the total demand in 1918 to less than 10 per cent in 192!2. Of greater practical value, however, is the establishment of the trend toward a single voltage standard. Although 110 volts gave considerable evidence of becoming the predominant standard, the 115-volt demand has been making steady inroads into the $110-$ and 120 -volt classes and now exceeds either of the other two standards by at least $1: 3$ per cent. When all things are considered there is every reason to believe that 11\% volts will become the ultimate standard for lighting service.

# A New Type of Overload Protective Relay 

By A. B. Campbell<br>Fort Wayne Works of General Electric Company


#### Abstract

The author describes some new types of temperature or thermal overload relays. After some instructive remarks on the gencral principles involved he deseribes the construction and then the operation. In conclusion, he lists the more important features of the device described.-Emitor.


During recent years the problem of overload protection for electrical machines has been demanding more attention because stricter requirements are now placed on devices performing this service.

In studying this problem it is found that the greatest overall economy in operation results when the equipment is worked at its maximum rated capacity, provided always that interruptions due to accidental overloads under this condition are of rare occurrence. Overload protective relays, therefore, should allow maximum usefulness of equipment and yet give positive protection against all dangerous overloads.

The type of relay described in this article is designed to fulfill these requirements and is based on the thermal principle of protection, involving operation by machine temperatures. Since this factor alone, in the great majority of cases, determines whether or not a given overload is dangerous to the equipment, this method of operating the protective device is fundamentally correct in principle. The actual temperature, at any instant, of a piece of electrical equipment under load includes a time measurement as well as a load measurement and therefore depends to a great extent on the condition of load previous to the measurement as well as on the ambient temperature surrounding the machine and on
many other factors. The thermal protective relay takes all of these variable factors into account and operates to remove load from the equipment when the temperature of the machine reaches a predetermined value, usually between 90 and 100 deg. C.

The same results as are obtained by this type of control could be accomplished by temperature indicators located at various places in the machine, but to be practical in the sense of general application to all sizes of machines the device must be entirely external to the machine and yet must indicate machine temperatures reliably. The method used in thermal relays to obtain this result is to build the relay so that it has a time-load temperature characteristic exactly duplicating that of the machine which it is desired to protect; in other words, the relay is built to have the same thermal time lag for all loads as the machine. The relay is then subjected to the same load as the machine by being connected in series with it, and therefore its temperature follows exactly the rariations of the machine temperature. C'pon reaching the ultimate operating temperature, regardless of the time required, the device functions to operate the control contacts, disconnecting the equipment from the load.

Variations in ambient temperature affect the relay as well as the machine, so that
assuming the device to be adjusted to operate momatly in am ambiont of 40 deg. C. with a 50 deg. C. rise, it will allow the equipment to carry greater than mormal loads for all ambients less than 40 deg. C. and less than mormal loads for all ambients above 40 deg. C., ahwas limiting the ultimate temperature to a predetermined value. With this adjustment it would be impossible to operate the machine at any load in an ambient of 90 deg . C., if this wats selected as the maximum operating temperature.

Nachine temperature in this connection refers to the temperature of the machine and the time-load characteristic refers to a curve experimentally determined showing the time required for the machine to reach a predetermined ultimate temperature for various overloads under a constant set of conclitions.

## General Construction and Operation

In actual construction the relay consists of three principal elements functioning together as follows:

1. A strip of thermostatic metal of fixed size and resistance, which responds to the relay temperature;
2. A heat storage volume having definite thermal constants determined by its size, shape, and material;
3. A heating unit of fixed resistance mounted in a space provided in the heat storage block.
The thermostatic metal strip performs two functions: first, it is the actuating means and operates the contacts by virtue of its property to assume a definite position for a predetermined temperature of the relay; and second, it is constructed so that it is part of the load circuit. Its constants, resistance and heat storage volume are so proportioned that it forms the high speed element of the relay, largely determining the shape of the high overload portion of the time-load characteristic. The high speed element predominates at the high overload portion of the curve, while its effect becomes less pronounced on decreasing overloads until at the critical value the shape is determined by the constants of the heat storage blocks. These two actions merge smoothly together on changing overloads and form the complete characteristic.

The heat storage volume of definite capacity gives the relay the required time lag at low overloads and its constants, size, specific heat, heat conductivity, and ratio of volume to radiating surface, determine the slope of
the lower portion of the time load temperature chamacteristic.

The heating unit supplies heat to the thermal storage volume at a rate dependent upon the load on the machine, the ratio of resistances of the heating unit and thermostatie strip determining the shape of the timeload temperature characteristic, as will be shown later.

An assembled view of a single-element device is shown in Fig. 1. In this view the thermostatic metal strip is seen mounted in intimate thermal contact to the heat storage blocks which are electrically insulated as a convenient means of electrically separating the ends of the strip. The circuit through the


Fig. 1. Single-element, Thermal Type of Overload Protective Relay
device is through both heater and strip in series, the heater being located in the round longitudinal hole through the centers of the blocks.

In the single element device the simplest form of contact arrangement is shown; i.e., a single contact at the end of the thermostatic metal strip touches a stationary but adjustable contact in the base at the contacting temperature ( 90 deg. C.). This arrangement can be made either circuit closing or opening simply by reversing the direction of deflection of the thermostatic metal strip, i.e., having it move toward or away from the stationary contact on increasing temperature. The adjustment of the stationary contact provides a means of changing the contacting temperature.

The simple contact arrangcment shown in Fig. 1 is not used as a direct line control, but is
used for making or breaking an alarm circuit or a circuit controlling the operation of an auxiliary relay which in turn controls the main line. This latter construction is used in two thermal twe of protective relays, which are provided with an anxiliary relay within the case allowing an antomatic resetting feature. In the simpler forms of relays having push button or other hand reset mechanisms, the thermostatic metal strip) is used as a mechanical latch holding a pair of spring mounted contacts closed under


Fig. 2. Thermal Time-Load Characteristic Curves of the Relay for the two limiting ratios of heater resistance to strip resistance and for an intermediate value
normal operating conditions and allowing them to open at the predetermined temperature of operation on overloads.

In operation the device functions as follows: On all loads some heat is developed in the device, but on normal loads the thermostatic metal strip does not reach its operating temperature. On low overloads the temperature of the whole device is gradually raised to the operating temperature by heat developed in the heating coil and transmitted to the strip through the thermal storage blocks. Under this condition the rate of heat generation in
the strip itself by the load current is lower than the rate of heat absorption by the blocks, hence the strip) follows the block temperature; on high overtoads, however, the rate of heat gencration in the strij) is greater than the rate of absorption by the blocks, so that the strip, builds up temperature within itsclf and since its heat storage volume is relatively small, its operating temperature is reached in a very short time. This is analagous in what actually happens in a piece of electrical apparatus under load; low overloads gradually raise the temperature of the whole mass while high overloads generate heat in the windings so much faster than it can be alsorled by the frame that they reach a dangerous temperature in a very short time. Permitting the analogy to be carried a little farther, it may be said that the windings in the machine are duplicated in the relay by the thermostatic metal strip while the machine frame is representer by the thermal storage blocks.

## Duplication of Thermal Time-Load Characteristics

As was indicated above, the thermal relay operates on a time-load characteristic which is a duplicate of the characteristic curve of the machine being protected

The characteristic curve of this relay is the resultant of two thermal characteristics; one adjusted by proper lagging to give the required time on relatively low overloads, and the other adjusted for proper times on high overloads. After these two clements have been adjusted for the proper values, they are combined thermally and the resultant curve is the characteristic desired.

The method by which this is accomplished is shown clearly in Fig. 2. Two curves are plotted in this illustration showing the shift in the time-load characteristic between the two extremes of the value of the ratio of heater resistance to strip resistance; in one case, $\mathrm{R}=$ infinity, where the thermostatic metal strip was omitted from the circuit entirely, and in the other case $\mathrm{R}=$ zero, where the thermostatic metal strip was the only part of the device in the circuit. Any time load characteristic falling between these two extremes may be duplicated simply by determining the proper ratio of resistances of these two elements. The curve in Fig. 2 marked $\mathrm{R}=10.7$ is plotted from data taken on a relay having a ratio of heater resistance to strip resistance of 10.7.

Characteristics not included between these two limiting curves will lie between two similar curves plotted from data on a similar
deviee having different time-lag characteristies due twathange ind dimensions or material of the thermal starage reservoir. The new eharacterist ics may then be duplicated as just shown.

By the use of these various modifications it is therefore peossible to dupliente any actual thermal time-load characteristies of chetrical equipment.

Since the ontput of some direct-current machinery is limited by commutation difficulties beyond eertain loads rather than exeessive temperature rise, it has been neessary to further modify the design to obtain a time-load characteristic which would give complete protection to the equipment. For rotary converters, temperature rise limits the lengt th of time the machine may carry loads up to about 170 per cent while beyond this point the time is limited by commutation. The thermal relay for rotaries, therefore, has a characteristic which is a combination of two curves; one a duplicate of the thermal characteristic of the machine for all loads below 170 per cent, and the other a thermal inverse-time characteristic of very steep slope which is intended to remove the machine from service after very short intervals for all loads over 170 per cent, this curve giving much shorter times for these loads than would be required only by temperature rise considerations. Under operating conditions ( 40 deg . C. ambient temperature and 90 per cent continuous load) this relay requires 2 hours to trip at 1.50 per cent load, while at 200 per cent load it will trip in 2.j) minutes, giving a ratio in times of $4: 1$. Under the same operating conditions another variation of the thermal relay, used for fractional h.p. motor protection, gives times to trip for the loads mentioned above of 1 minute and 0.6 minute respectively, or a ratio of only 1.67:1. These two examples illustrate the possibility of thermal characteristic curve duplication by thermal relays over extreme conditions.

The theory and design of the relays described in this article are the result of research and development directed by Mr. Chester I. Hall of the Fort Wayne Works, and many devices embodying these principles are in actual service in connection with automatic generating and substation equipment, and many industrial motor applications. A special device for application to domestic motor appliances has also found extensive use.

Throughout this discussion it has been assumed that the heating and cooling characteristics are practically identical, as they are in the case of a transformer, and under this condition the temperature of the relay is always the same as that of the machine even though the machine may be performing special duty cycles such as rolling mill loads, cte., where the peak load in each cycle is of very high value.

The motor equipment of electric locomotives presents a more complicated problem because of the fact that the equipment may be subjected to different rates of cooling, depending on whether the cooling takes place when the locomotive is stationary or coasting. In the latter case the forced ventilation results in rapid cooling which must be duplicated in the relay by special ventilation in order that the relay may follow the motor temperature variations.

The use of thermal overload protection properly designed for a given installation results in many advantages which are not obtainable by any other means. The more important features are given below:

The equipment is protected from overheating for any and all conditions of load.

The maximum overload ability of the machine is utilized without danger.

The capacity of the equipment is automatically varied between proper limits for changes in ambient temperature.

Interruptions of service due to overloads are reduced to a minimum and maximum possible intervals are allowed for carrying overloads over temporary peaks.

Thermal relays are self-protective and are not harmed by overloads when properly installed because of the fact that they trip at a predetermined temperature.

Thermal relays are applicable to either alternating current or direct current without modification.

These devices are particularly useful in induction motor operation since they may be set to trip on small overloads and yet allow sufficient time for starting even though the motor may require several times full load current under this condition.

The application of this new principle to overload protective relays is fundamentally correct and it is anticipated that thermal protection will find a wide field of usefulness.

# The Electron in Chemistry <br> PART IV 

By Sir Joseph John Thomson<br>


#### Abstract

In this, the concluding article of this series, the author deals with ()xyern; Viamagnetism; Electron Theory of Solids; Divalent Elements; Trivalent Noms; Tetravalent Element; Hexagonal Sistem; Compressibility of the Metals; The Energy and Compressibility of Divalent Elements; The Comprescibility of atrivalent Element; Surface Tension; Communication of Charge from Cascous lons to the lilectrodes; intermetallic Compounds and Mixed Crystals and Intermetallic Compounds. We again acknowledge rur indebtedness to the Journal of the Franklin Institute for permission to reprint this remarkable series of artules. -- Emolor.


## Oxygen

The most fascinating of all magnetic bodies is to my mind oxygen. Here we have one of the simplest of atoms; its atom contains only eight electrons, it is a gas, and therefore in the simplest of all phesical states, and yet it alone of all gases is paramagnetic and quite strongly so. Another remarkable thing about it is that innumerable as are the compounds of oxygen there is only one, NO, into which oxygen carries its magnetic properties. This would seem to suggest that the magnetic quality does not arise from some quality int rinsic to the atom. but from some specialty in the arrangement of the colligating electrons in those molecules where it exhibits its magnetic character. The oxygen molecule itself is the most conspicuous example: the arrangement of the electrons may be represented symbolically as two cubes having a face in common. this face being at right angles to the line joining the atoms. If the system were rotating about this line there would be an odd number of square faces in rotation. A rotating square with its electrons would act like a current and thus behave like a magneton. Now suppose that the rotation of electrons must be such that adjacent squares rotate in opposite directions, and it is erident that if we start one from rest in one direction. the adjacent one will start in the opposite direction. Suppose then that the electrons in the planes of the squares were rotating so that the rotation in one plane is opposite to that in the adjacent plane, then two of these planes will be rotating in one direction and the third in the opposite, the resulting magnetic effect will be the same as if only one plane rotated, and this will produce a magnet of finite moment.

It might be thought that if this arrangement of electrons were all that is required to produce paramagnetism, a considerable number of gases would be paramagnetic, whereas
so far as is known only two possess this property. The consideration of the arrangement of the electrons in gaseous compounds shows, however, that the configuration of $\mathrm{O}_{2}$ is almost unique in this respect. Consider the arrangement of electrons in some compounds of oxygen, e.g., in water where it is in combination with two monovalent atoms, the electrons are arranged in an octet which has two sets of four electrons in parallel planes, if adjacent sets rotate in opposite directions, the total magnetic effect will be zero. The same is true for a compound like CaO , or for one like CO , where there are four such sets. We see that whenever the oxygen atom occurs, as it always does in valency compounds, with two additional electrons forming an octet, the effect. of one face of the octet will always balance that of the other. In a neutral atom of oxygen the electrons would be arranged at the corners of an octahedron; if this were to rotate about one of its axes, the four electrons at right angles to the axis would form an unbalanced system and this would have magnetic properties. The magnetic properties of NO , if we take the arrangement of the electrons to be as that given in the first lecture, would arise from the rotation of the three electrons inside the octet, those on the octet itself would not contribute to the magnetic properties. In the compound $\mathrm{C}_{2} \mathrm{H}_{4}$ we have a similar arrangement of electrons to those in $\mathrm{O}_{2}$, but in $\mathrm{C}_{2} \mathrm{H}_{4}$ all the massive positive charges are not as they are in $\mathrm{O}_{2}$ on a straight line. The result of this is that if the two octets rotate, say about the line joining the two carbon atoms they would either have to carry the hydrogen atoms with them, in which case the moment of inertia would be enormously increased, or else move the electrons relative to the hydrogen atoms: the forces between the positive charges and the electrons would resist this motion, and tend to stop the rotation. In the oxygen
molerule the clectrons can rotate while the positive parts are at rest. If the eomponands
 electrons wonld be as in $\mathrm{O}_{2}$, and on the views we have been expressing we should expert that these compounds would be magnetic.

## Diamagnetism

The diamagnetic properties of chemical compounds will furnish, I think, many searching tests of any theory of the distribution of electrons among the atoms of the compound. According to the theory of diamagnetism given by Langevin, ${ }^{29}$ the contribution of an aton to $k$, the coefficient of diamagnetism, is equal to $\frac{1}{4} \frac{c^{2}}{m} \check{m} r^{2}$, where $m\left\llcorner{ }^{2} r^{2}\right.$ represents the moment of inertia of the electrons in the atom about an axis through their centre of figure. The distribution of electrons is supposed to be quite symmetrical so that the moments about all axes are equal, $c$ is the charge and $m$ the mass of an electron.

If $n$ is the number of atoms per unit volume, $k$, the coefficient of magnetization is given by the equation

$$
\begin{equation*}
k=\frac{1}{4} n \frac{e^{2}}{m} \check{y} r^{2} \tag{32}
\end{equation*}
$$

If $M$ is the molecular weight of the system, $\Delta$ the density of the substance, $N$ the number of hydrogen atoms in a gram of hydrogen

$$
\begin{equation*}
n=\frac{\triangle}{M} N \tag{33}
\end{equation*}
$$

hence

$$
\begin{equation*}
\frac{k M}{\triangle}=\frac{1}{4} \frac{e^{2}}{m} N \Sigma r^{2} \tag{34}
\end{equation*}
$$

Thus $k M / \triangle$, which is called the atomic diamagnetic coefficient and is denoted by $X_{a}$, is proportional to $\Sigma r^{2}$, and when $X$ is known $\check{-} r^{2}$ can be calculated. We pass on to consider, what, for our purpose, is the most important application of diamagnetism -the connection between the diamagnetic coefficient of a compound, and those of its constituents.

Pascal ${ }^{30}$ has made a series of most valuable experiments on this point, chiefly on organic compounds. He finds that the connection between $X_{m}$, the diamagnetic constant of a compound $A_{x} B_{y} C_{z}$ and $X_{a}, X_{b}, X_{c}$, the constants for its constituents, is expressed by the relation

$$
\begin{equation*}
X_{m}=x X_{a}+y X_{b}+z X_{c}+\lambda \tag{35}
\end{equation*}
$$

where $\lambda$ is a quantity, generally small compared with $X_{a}, X_{b}, X_{c}$, which depends on

[^90]${ }^{30}$ Annales de Chimie et de Physique [8], 25, p. 289.
the "bonding" of the atoms. 'Thus, for example, when oxygen is one of the constituents of the molecule, the value of $\lambda$, when the oxygen is connected by two linkages with a carbon atom, is not the same as when the oxygen is connected by one link with a carbon and by another to a hydrogen atom; thus, for example, the contributions of the two oxygen atoms in formic acid HCO.OH are different.

Pascal was dealing with valency compounds; in these, on the electron theory, the atom of any particular element will be associated with the same number of electrons whatever may be the compound in which it occurs; thus, for example, the electronegative elements $\mathrm{O}, \mathrm{S}, \mathrm{F}, \mathrm{Cl}$, will always be surrounded by an octet of electrons; the outer layers of the electropositive elements will have been transferred to the electronegative ones to make up their octets. An interesting point arises here in connection with the hydrogen atom and to a less extent with metal atoms. In a compound of hydrogen with an electronegative element, the electron associated with the hydrogen atom has gone to make up the octet round the negative ion, as, for example, in HCl . Thus the hydrogen atom in such a compound is but a positive core, it has no electrons associated with it, and hence on the electron theory of diamagnetism would not contribute anything to the diamagnetic coefficient. Pascal, however, in deducing the coefficient for any compound, assigns to hydrogen a constant value. This is to some extent a matter of bookkeeping, the electrons transferred from the hydrogen to the chlorine will increase the contribution of the chlorine atom to the diamagnetic coefficient. If we like we may transfer this increase to the credit of the hydrogen atom and regard the hydrogen atom as making a contribution to the diamagnetic coefficient, though it does this not by acting itself as the centre of one of the molecular currents, which account for diamagnetism, but by furnishing an electron which increases the molecular currents in some other atom. We should, however, expect that the amount of the increase would depend upon the kind of atom to which the electron is transferred, that it would increase with the radius of this atom and thus be greater for bromine than for fluorine or chlorine.

We shall now consider what relation would be indicated on the theory we are considering between the diamagnetism of a compound
and of its constituents. On the view that. at any mate, in valency componds there is a transference of electrons from one atom to another, the atoms in the compond are not in the same state as when they were free and uncombined. The atoms of the electronegative elements such as oxygen or chlorine have gained electrons, while those of the electropositive elements have lost them. The coefficient of diamagnetism is proportional to the sum of the moments of inertia of the electrons about an axis throught their centre of figure parallel to the magnetic force. It the transference of the electrons involves a change in this moment the coefficient of diamagnetism will be altered by chemical combination, i.c., the additive law will not hold.

Suppose that in the free state the distances of the electrons from the centres of the atoms of the elements $A$ and $B$ are $r_{a}$ and $r_{b}$, respectively, and that the electrons are symmetrically distributed. Then if there are $\alpha$ electrons on $A, \beta$ on $B$ the coefficient of diamagnetism is proportional to

$$
\begin{equation*}
\frac{2}{3} \alpha r_{a}^{2}+\frac{2}{3} \beta r_{b}^{2} \tag{36}
\end{equation*}
$$

If as the result of chemical combination $\alpha$ atoms are transferred from $A$ to $B$, if $R_{b}$ is now the distance of the electrons on the $B$ atoms from its centre the coefficient of diamagnetism is now

$$
\begin{equation*}
\frac{2}{3}(\alpha+\beta) R_{b}^{2} \tag{37}
\end{equation*}
$$

This may be written in the form

$$
\begin{align*}
& \frac{2}{3} \alpha r_{a}^{2}+\frac{2}{3} \beta r_{b}^{2}+\frac{2}{3} \alpha \\
& \quad\left(R_{b}{ }^{2}-r_{a}^{2}\right)+\frac{2}{3} \beta\left(R_{b}^{2}-r_{b}^{2}\right) \tag{3§}
\end{align*}
$$

the sum of the first and second terms is the value given by the additive law, the remaining terms represent corrections which must be applied to obtain the diamagnetic coefficient of the compound. If $X_{A B}$ represents this coefficient, we see

$$
\begin{equation*}
X_{A B}=X_{A}+X_{B}+\alpha \lambda_{A B}+\frac{2}{3} \beta\left(R_{b}^{2}-r_{b}^{2}\right) \tag{39}
\end{equation*}
$$

when $\lambda_{A B}=\frac{2}{3}\left(R_{b}{ }^{2}-r_{a}{ }^{2}\right)$ and is a function which involves the dimensions of each of the atoms at the ends of the bond binding them together. The term $\frac{2}{3} \beta\left(R_{b}{ }^{2}-r_{b}{ }^{2}\right)$ depends
only upon the atom $b$, hence the equation may be written as

$$
\begin{equation*}
X_{A B}=X_{A}+X_{B}^{\prime}+\alpha \lambda_{1 B} \tag{40}
\end{equation*}
$$

where $X^{\prime \prime}{ }_{b}$ depends only upon the properties of the $B$ atom
$A_{p}$ plying the same reasoning to the most general case, we see that $X$ the value for the compound $A_{x} B_{y} C_{z}$ will be given by an equation of the form $X=x X(A)+y\left(B^{\prime}\right)+z X$ (C) $+こ \lambda_{A B}$.
$A$ term has to be introduced into $\Sigma \lambda_{A B}$ for each electron transferred, i.c., for each valency bond in the compound. Thus we may regard the diamagnetic coefficient of a compound as consisting of a series of terms, one set depending on the atoms in such a way that each atom contributes a definite amount depending only upon the atom; the second set of terms depending on the valency bonds, each bond contributing a term, the value of which depends upon the dimensions of the atoms at the ends of the bond. There may be a term in this set even when the atoms at the ends of the bond are the same; for example, when we have single or double bonds between two carbon atoms: For from the expression for $\lambda$ we see that they would not ranish unless the radius of the octet round the carbon atoms in the compound $\mathrm{C}-\mathrm{C}$ was equal to the distance of an electron in a free carbon atom from the centre. As the radius of the octet, round the carbon atoms when there is a double bond $C=C$ is not the same as when there is only a single bond, the value of $\lambda$ for a double bond is not necessarily twice that for a single one.

Pascal found that a double bond produced a very appreciable diminution in the diamagnetism, the magnitude of the effect of the double bond was about equal in magnitude, though opposite in sign to that due to a single carbon atom. The effect of a triple bond was much smaller than that of a double one.

Pascal's researches on the diamagnetism of compounds show that what we have called the $\lambda$ terms are not in general large compared with the atomic ones, yet these terms undoubtedly exist. He shows, for example, that the contribution of oxygen to the diamagnetic coefficient is not the same, when as in $\mathrm{CH}_{3} \mathrm{OH}$ the oxygen is linked by one bond to the carbon and by another to the hydrogen as it is in CH.O.OH, where one of the oxygen atoms is linked by two bonds to the carbon atom; he shows, too, that the contributions of
doubly amd singly linked carbon atoms atr different: the shows in fine that to calculate the diamargentio confficiont of a comporand we must take into aceoment the comstitution and configuation as well as the ehemical composition.

In addition to the effeets protuced be the bonding of the atoms, there are others, though protably not so important, arising from what may be called the compressibility of the cell of electrons surrounding the atoms. Thus, for example, it is probable that the distance of the electrons from the eentre of the chlorine atoms in 11C1 is not quite the same as in $\mathrm{CCl}_{1}$, where the four chlorine atoms may compress each other by their mutual repulsions. A change in the dimensions of the atom would give rise to a change in the diamagnetic coefficient.

The corrections due to the $\lambda$ terms amount in some cases to as much as 30 per cent, though it is exceptional for them to be as large as this.

From the equation

$$
\begin{equation*}
X_{a}=-\frac{1}{4} \frac{c^{2}}{m} N \Sigma r^{2} \tag{+1}
\end{equation*}
$$

we can, if we know the value of $\mathrm{X}_{a}$, deduce the distance of the electrons from the centre of the atom. For if the distribution of the electrons in the outer layer is symmetrical about the centre

$$
\begin{equation*}
\Sigma r^{2}=\frac{2}{3} n R^{2} \tag{42}
\end{equation*}
$$

where $n$ is the number of electrons in the outer layer and $R$ the distance of these from the centre of the atom; hence

$$
\begin{equation*}
X_{a}=-\frac{1}{6} \frac{c^{2}}{m} N n R^{2} \tag{43}
\end{equation*}
$$

or since $e / m=1.87 \times 10^{7} ; \quad e=1.6 \times 10^{-20}$; $N=6.16 \times 10^{23}$

$$
\begin{equation*}
\Lambda_{a}=-3.06 \times 10^{10} \times R^{2} \times n \tag{44}
\end{equation*}
$$

Pascal ${ }^{31}$ gives the following values for $-10^{6} . \mathrm{X}_{a}$.

| H | 2.93 | Al | 13.2 | As | 43 | Te | 37.5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: |
| Li | 4.20 | Si | 20.0 | Sc | 23 | I | 44.6 |
| Bc | 8.55 | P | 26.3 | Br | 30.5 | Cs | 41.0 |
| B | 7.30 | S | 15 | Rb | 27.2 | Ba | 38.2 |
| C | 6.80 | Cl | 20.1 | Sr | 24.5 | An | 45.8 |
| N | 5.57 | K | 18.5 | Ag | 31 | Hg 11 | 33.4 |
| O | 4.61 | Ca | 15.0 | Cd | 20 | Pt | 40.3 |
| F | 5.95 | Cu | 18 | $\mathrm{In}>$ | 15 | Pb | 45.8 |
| Na | 9.2 | Lu | 13.5 | Sniv | 30.3 | Bi | 192 |
| Mg | 10.1 | Ga | 16.8 | Sbiii | 74.0 |  |  |

From these values of $X_{a}$ we find from the preceding equation the following values for

[^91]the diameters of fully charged electronegative atoms. The values foumb by W. L. Braggas are given for comparison.

| Element |  Constant | Values Foound by Browt |
| :---: | :---: | :---: |
| () | $1.02 \times 10^{\circ}$ | $1.30 \times 10^{-8}$ |
| 1 | $1.05 \times 10^{-8}$ | $1.35 \times 10^{-4}$ |
| 心 | $1.84 \times 10{ }^{6}$ | $2.05 \times 10^{-8}$ |
| ( ${ }^{1}$ | $2.0 \times 10^{-8}$ | $2.10 \times 10^{-8}$ |
| So | $2.203 \times 10^{-4}$ | $2.35 \times 10^{-8}$ |
| Br | $2.40 \times 10^{-4}$ | $2.38 \times 10^{-8}$ |
| '1'c | $2.8 \times 10^{4}$ | $2.69 \times 10)^{-8}$ |
| I | $3.0 \times 10^{5}$ | $2.80 \times 10^{-8}$ |

The agreement between the values of the diameters found from the diamagnetic coefficient and those found by Bragg is fairly chose. It is interesting to note that there is nothing exceptional in the value of the strongly paramagnetic element oxygen; from this we conclude that the oxygen atom when it has two additional electrons is not paramagnetic.

When the diamagnetic substance is in a solid state a somewhat different treatment is required. If it is a metal, the electrons will be arranged in lattices and along these lattices the electrons may be free to move. If these lattices form a simple cubical system, then it can be shown that the effect of the electrons on the lattices in a plane at right angles to the magnetic force is to produce per unit area of this plane a magnetic moment equal to $-\frac{1}{16} \frac{H e^{2}}{m}$, when $H$ is the magnetic force, if $d$ is the distance between two parallel lattice planes the moment due to the electrons in unit volume is $-\frac{1}{16} \frac{H e^{2}}{m d}$, hence the coefficient of diamagnetism is equal to $\frac{1}{16} \frac{e^{2}}{m d}$.

Since the radius of an electron is of the order $e^{2}, m$, we see that the volume coefficient of diamagnetism is of the order of the ratio of the radius of the electron to the distance between adjacent atoms.

Since the volume coefficient of diamagnetism varies as $l ; d$, and the atomic volume varies as $d^{3}$, we see that for metals of the same valency the diamagnetic coefficient should vary inversely as the cube root of the atomic volume.

## Electron Theory of Solids

We shall now proceed to examine how atoms can be bound together not merely in twos or threes to form molecules, but in large numbers so as to form solids. We shall consider how such a collection of atoms is
held together and calculate some of its phesical properties. We begin with the case when the atoms are all of one kind and when the solid is a crystal, so that it may be regarded as made up of units whieh are repetitions of each other. These units will be built up of atoms and electrons and the proportion between the number of atoms and the number of electrons will depend upon the valence of the element. Thus for the alkali metals there will be as many atoms as electrons, for the alkaline earths there will be two electrons for each atom, for trivalent metals like aluminum there will be three electrons for each atom and so on. Since the units completely fill space, they must be of the shape of one of the solids into which space may be divided, i.c., the units must be parallelipeda, hexagonal prisms, rhombic dodecahedra or cubo-octahedra.

Let us take the case where the units are cubical. When a number of cubes are built up into a solid each comer of a cube will be the meeting place of eight cubes. Thus, if for purposes of calculation, we take the cube as our unit, and proceed to find the effect of one cube and take the sum of these effects for all the cubes into which the solid is divided, the effect due to an atom or electron at a corner will be counted eight times over. We may compensate for this by assigning to an atom or electron at the corner oneeighth of its normal charge. An atom or electron at the center of the face of a cube would be common to two cubes and so must be assigned half its normal charge, while an atom or electron at the middle point of a side of a cube will form a part of four cubes and so must be given one-quarter the normal charge.

Thus suppose the atom is at the centre of a cubical layer of electrons, then if the electrons are at the corners of the cube, both electrons and atoms will be arranged in simple cubical lattices, there will be as many electrons as atoms, the unit cell will be a cube with one-eighth of an electron at each corner and an atom at its centre. Suppose the electrons are at the middle points of the faces of the cube as well as at the corners, there will be four electrons for each atom so that the arrangement will be a possible one for a quadrivalent element. The symmetry of the arrangement shows that it corresponds to a crystal in the regular system. The cell in this case will be a cube with one-eighth of an electron at each corner and half an electron at the centre of each face.

Another quite symmetrical arrangement is when there is ann electem at the conner of each cube and one at the middle point of each of its twelve sides; as each side is shared by forn cubes the twelve electrons at the middle of the sides will only furnish three electrons to the cell, the one-cighth of an electron at each of the corners will contribute another, so that this arrangement would again be representative of an element in which there are four electrons per atom. The cell in this case will be a cube with one-cighth of an electron at each corner, one-quarter of an electron at the middle point of each side and an atom with a charge four at the centre.

The arrangement of the atoms in each of the preceding eases is that of a simple cubical lattice, the experiments of Sir William and Prof. W. L. Bragg on crystal structures have shown that one of the most frequent arrangements of the atoms is that of face-centred cubes. Here the atoms are at the corners and the centres of the faces of the cubes. If such a cube is taken as the unit cell, one-eighth of an atom must be placed at each corner and half an atom at the centre of each face: This makes each cell contain four atoms. If the atom is one of a monovalent element like lithium, the cell must contain four electrons. These electrons can be arranged with cubical symmetry in two ways-

1. By putting one-quarter of an electron at the middle point of each edge and one at the centre of the cube. This gives an arrangement where each atom has six electrons and each electron six atoms for its nearest neighbors. The atoms and electrons are arranged alternately at equal intervals along the lines of a simple cubical lattice.

This arrangement corresponds to that formed by Sir William and Prof. W. L. Bragg for the chlorides of the alkali metals.
2. Put one electron at the centre of four out of the eight cubes into which the unit cube is divided by planes bisecting the sides at right angles. The four cubes are to be chosen as follows: Take any one and put an electron at its centre, then electrons are to be put at the centres of the three cubes which have an edge but not a face in common with the cube originally chosen. When the cells are put together the same rule must be observed, any two small cubes which have a face in common must have an electron at the centre of one but not at the centre of the other. The four electrons in each cell
are at the conners of a regular tet mabedron． The distribution of the atoms and electrons is equisalent to one where each atom is at the centre of a regular tetrathedron of electrons and each electron at the centre of a regular teraberatron of atoms．

## Divalent Elements

If the atoms in the face－centred eell belong （1）a divalent element，since there are four atoms in the cell there must be eight electrons．

Two wats in which this may be done are as follows：

1．Fitl up the four small cubes which were left empty on scheme 2 for the monovalent elements．Each atom will now have eight electrons as its nearest neighbors，the elec－ trons being at the corners of a cube with the atom at its centre．The cubes surround－ ing two adjacent atoms have an edge in common and not a face as in the simple cubical arrangement for monovalent atoms．

2 ．Take the scheme 2 for four of the elec－ trons and in addition place a quarter of an electron at the middle point of each of the twelve sides of the large cube and another electron at its centre．

## Trivalent Atoms

When the atoms in the face－centred cube are trivalent there must be twelve electrons in the unit．We can find accommodation for these if we put one at the centre of each of eight small cubes into which the unit cube is divided，a quarter of one at the middle points of each of the twelve edges of the unit cube and another at the centre of this cube．This arrangement is equivalent to putting the atoms at the centres and the electrons at the corners of a series of rhombic dodecahedra filling space．

## Tetravalent Element

The arrangement of the atoms in the diamond has been worked out by the Braggs． It is that shown in Fig．41．The unit contains eight atoms distributed as follows：One－ eighth at each of the corners of the unit， this accounts for one；one－half at the centre of each of the faces，this accounts for three； and four more at the centres of four of the eight cubes into which the unit cube is divided by planes bisecting the sides at right angles．The cubes to be occupied by the atoms are chosen by the same rule as that given for the arrangement of the clectrons for the centre－faced arrangement for the monovalent element．As the unit
contains eight carbon atoms and carbon is quadrivalent，there must be thirty－two elec－ trons in the unit；these may be arranged as follows：
（a）At the middle points of the sides of the cubical unit；this aceounts for three．
（b）At the centre of each of the faces of the eight small cubes；this accounts for twenty－ four．
（c）At the eentres of the four small cules not occtupied by the carbon atoms；this accounts for four．
（d）One at the centre of the large cube．
Röntgen－ray analysis has shown that for some elements the atoms are arranged at the


Fig． 41
corners and the centre of a cube．Taking this cube as the unit it contains two atoms； if the element is monovalent，it must contain two electrons．We cannot place these electrons so as to get complete cubical symmetry for one such unit；if，however，we group eight such units together，we get a larger cubical unit containing sixteen atoms， and it is possible to arrange sixteen electrons in this larger unit so as to get cubical sym－ metry．Thus we might put pairs of electrons along the diagonals of the eight cubes which go to make up the larger unit．

If the atom were a divalent one we should have to accommodate four electrons in the original unit．This may be done by putting them at the centres of four out of the eight cubes into which the unit may be divided．

## Hexagonal System

We have hitherto confined ourselves to the consideration of crystals in which the unit was a cube and the arrangement both of atoms and electrons completely symmetrical， so that the crystals would belong to the regular system．If our unit were a hexagonal prism，if，for instance，the electrons were at
the conners and the atoms at the centres of hexagonal prisms, then since each corner is common to six prisms, we must, when calculating the electrical forces due to the unit, give to each electron at the comer one-sixth of its normal charge, the twelve electrons at the comers are thus equivalent to two electrons, so that the unit contains two electrons for each atom and would thus correspond to a divalent element.

The arrangement of electrons and atoms in the systems we have described have such regularity that the calculation of the properties of such an aggregate is casier than that of the properties of an aggregate of a small number of atoms in an individual molecule. For the electrons in one part of a molecule, for example, those at the ends of the two octets which form the oxygen molecule, are exposed to forces which are different from those acting on the electrons between the two oxygen atoms. The greater regularity in the arrangement of the electrons in the crystal more than compensates, as far as the mathematical difficulties are concerned, for the necessity of taking into account the effect of a much larger number of electrons and atoms than is necessary for the molecule.

I have in a paper published in the Philosophical Magazinc (53, p. T21) calculated some of the propertics of crystals when the atoms and electrons are arranged according to some of the schemes we have just been discussing. I shall describe the results of these investigations, beginning with the simplest case, where the atoms and electrons are both arranged in simple cubical lattices, where each atom may be regarded as the centre of a cubc formed by eight electrons.

In the paper referred to, the stability of the system is investigated, and it is shown that if $2 d$ is the distance between two atoms the arrangement will be stable, provided $d$ is less than $c / 1.69$ where $c$ is the distance at which the force exerted by the positive nucleus on an electron changes from attraction to repulsion. As the distance between an atom and the nearest electron is $\sqrt{3 d}$. i.e., $1.72 d$, we see that for the equilibrium to be stable, the shortest distance between an atom and an electron in the solid cannot exceed by more than a very small amount the distance of the electron from the centre of the atom when the element is in the gaseous state.

The system of electrons and atoms in the metal will have a very large number of

[^92]periods of vibration, depending on the way the electrons are displaced relatively to cach other and to the atoms; the highest frequeney of these vibrations is when the electrons are not displaced relatively to each other, but only with respect to the atoms; this corresponds to the displacement which would be produced by light whose wavelength is long compared with the distance between two atoms. I find that this maximum frequency $p$, is given by the equation
\[

$$
\begin{equation*}
m p^{2}=.384 c c^{2} / d^{4} \tag{4,5}
\end{equation*}
$$

\]

where $m$ is the mass and $e$ the charge on an electron.

If $M$ is the mass of an atom and $\triangle$ the density of the solid, then since $S d^{3}$ is the volume of a cell, $1 / d^{3}$ is the number of cells in a cubic centimetre, hence

$$
\begin{equation*}
\frac{M}{S d^{3}}=\triangle \tag{46}
\end{equation*}
$$

so that cquation (45) may be written as

$$
\begin{equation*}
m p^{2}=.38+c^{2} \frac{S \triangle}{M} \frac{c}{d} \tag{7}
\end{equation*}
$$

This type of vibration is the one that would be excited by waves such as those of risible or ultra-violet light whose wavelength is large compared with the distance between the atoms in the solid. We might therefore expect cvidence of it in the behavior of monovalent metals when acted upon by light, the cffect produced upon such metals would be greatest when the frequency of the incident light was that given by equation (4.5). An interesting case when the action of light on a metal is a maximum for light of a particular wavelength is what is known as the selective photoelectric effect. ${ }^{33}$ This has been measured by Pohl and Pringsheim, ${ }^{34}$ and in the following table, I give the comparison of the wavelength $\lambda$ for which the selective photoelectric effect is a maximum for the monovalent metals sodium, potassium and rubidium as determined by Pohl and Pringsheim with the wavelengths calculated by equation (45) where $c / d$ has been given the value 1.7 , i.e., on the supposition that the shortest distance between the atom and the electron in the metal is the same as that in the gas.

| Metal | $\Delta$ | $11 / 1.64 \times 10^{-24}$ | $\lambda$ Calculated | $\lambda$ Observed |
| :--- | :---: | :---: | :---: | :---: |
| Sodium... | .971 | 23 | $323 \pm$ | 3400 |
| Potassium. .862 | 39 | 4457 | 4400 |  |
| Rubidium. 1.532 | 85.45 | 4940 | 4800 |  |

It will be noticed that the agreement between the observed and calculated values is satisfactory.

11 is interesting to compare the freduency of this sepe of vibation of the electrons in the solid, with $P$ ', that of the vibation of the cheotrom in a gaserots atom, the latter eam easily be prowed to be given be the equation

$$
\begin{equation*}
m l^{n}=c^{2} c^{3} \tag{1A}
\end{equation*}
$$

so we see from (1) if $1 . \quad \pi=c$ and $p$ is 1 he frequency in the metal

$$
\begin{equation*}
P=1 . N P \tag{1!}
\end{equation*}
$$

thas the frequener in the metal is a lithe less than twiee that in the gas, the values for the wavelength of the vibations in the gaseons atom deduced from the table just given are for sodium isto, and for potassium 7900)

The slowest vibations of the efectrons are when the displacement of adjacent elec(rons are in opposite directions. Thus sup)pose one of the lines of the electron lattiee is vertical, then the slowest wibration of the electrons is when the electrons in any one line have all equal vertical displacements and the displacements of the electrons in the six vertical lines which are its nearest neightors are equal in magnitude, but opposite in direction, to that in the line under consideration.

## Compressibility of the Meta's

We can calculate the potential encrgy due to the forces between the atoms and the electrons. I have given the calculations in a paper in the Philosophical Magazine (43. 1). FO1) and have shown that if the metal is supposed to be made up of cubical cells with an atom at the centre and one-eighth of an electron at each of its eight corners, each cell corresponding to an atom with its electron, the potential energy per cell is

$$
\begin{equation*}
-1.8 \cdot 5 \cdot \frac{\varepsilon^{2}}{2 d} \tag{.50}
\end{equation*}
$$

when $2 d$ is a side of the cube. Thus, if there are $\Lambda$ cells per unit volume, the potential energy per unit vohume is

$$
\begin{equation*}
-1.82 .5 \frac{\varepsilon^{2}}{2 d} 1 \tag{.51}
\end{equation*}
$$

Now $N=1 \& d^{3}$, and if as before $M$ is the mass of an atom and $\triangle$ the density of the metal

$$
\begin{equation*}
N M=\triangle \tag{52}
\end{equation*}
$$

hence the potential energy per unit volume is equal to

$$
\begin{equation*}
-1.825 \varepsilon^{2}\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \tag{53}
\end{equation*}
$$

It is shown also that the work required to compress the cells so that the distance
betwern two atoms is reduced from $2 d$ to $\because(d-\Delta d)$ is equal to

$$
\begin{equation*}
1 . N 2 \cdot=r^{-1}\binom{\triangle d}{d}^{2} \tag{54}
\end{equation*}
$$

If $d 1^{\prime}$ is the diminution in a volume $I^{\prime}$ due to this diminution in $d$

$$
\begin{equation*}
\frac{d r}{1}=3 \frac{\Delta d}{d} \tag{5.5}
\end{equation*}
$$

hence the work required to compress the cetts in mait volume is equal to

But if $k$ is the butk modulus, then this work is equal to

$$
\begin{equation*}
2_{2}^{1} k\left(\frac{d V}{V}\right)^{2} \tag{.57}
\end{equation*}
$$

hence

$$
\begin{equation*}
k=\frac{3,65}{9} c^{2}\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \tag{.5'}
\end{equation*}
$$

The "compressibility" of the substance is equal to $1 k$.

We owe to Professor Richarts invaluable determinations of the compressibility of the various elements. The following table contains the results of the comparison of his values of the compressibility with those calculated from equation (.)s).

| Metal | $\triangle 1$ | $111.64 \times 10^{-}$ | $k$ Calculated | $k$ Observed |
| :---: | :---: | :---: | :---: | :---: |
| Lithium | . 334 | 7 | . $1+\times 10^{12}$ | . $114 \times 10^{12}$ |
| Sodium. . | . 971 | 23 | . $068 \times 10^{12}$ | . $065 \times 10^{12}$ |
| Potassium | .862 | 37 | . $03 \times 10^{12}$ | . $032 \times 10^{12}$ |
| Rubidium. | 1.532 | 8i.) | $.022 \times 10^{12}$ | . $025 \times 1()^{12}$ |
| Carsium . | 1.87 | 132 | . $016 \times 10^{12}$ | $.016 \times 10^{12}$ |

Thus the results given by equation (58) are in close agreement with experiment.

If the atoms are in the gaseous state, the work required to change the radius of an atom from $r$ to $r-\Delta r$ is equal to $\frac{1}{2} \frac{e^{2}}{c}\left(\frac{\Delta r}{r}\right)^{2}$.
Thus to produce the same percentage changes (4.5) in the sum of the volume of the atoms when in the gaseous state and (47) in the volume of the same number of atoms in the solid state requires the expenditure of amounts of work which are in the proportion of $\frac{1}{c}$ to $\frac{1.8 \cdot 2}{d}$, or if $1 . \bar{\tau} d=c$, of 1 to 3.1 . Thus the compressibility of the atoms in the solid state is about one-third of that in the gaseous.

The potential energy of a cell in the solid is equal to $-\frac{1.82 .5 \varepsilon^{2}}{2 d}$ or, since $\frac{1}{(2 d)^{3}}=\Delta / M$, to
$-c^{2} 1$.N. $2 .\binom{\triangle}{M}^{\prime}$; if $W^{\prime}$ is the atomic weight of the element

$$
\begin{equation*}
M=1.64 \times 10^{2} \times M^{\prime} \tag{.59}
\end{equation*}
$$

hence the potential energy of the metal per cell is equal to

$$
\begin{equation*}
-c^{2} 1 . \overline{5} \times 10\left(\frac{\triangle}{M^{\prime}}\right) \tag{0}
\end{equation*}
$$

This is equal to the energy acquired loy the charge on an electron falling through a potential difference of

$$
\begin{equation*}
21.2 .5 \times\binom{\triangle}{M^{\prime}}^{\frac{1}{2}} \text { volts. } \tag{61}
\end{equation*}
$$

The values for the various alkaline metals are

$$
\begin{aligned}
& \mathrm{Li}=9.2 \text { rolts } \\
& \mathrm{Na}=7.3 \\
& \mathrm{~K}=(6.36 \\
& \mathrm{Rb}=5.52 \\
& \mathrm{Cs}=5.100
\end{aligned}
$$

The work which must be done in pull the cell from the metal and convert it into an atom of a monatomic gas is the difference between the potential energy in the cell and the potential energy of the gascous atom; the latter when expressed in rolts is for a monoralent element equal to the ionizing potential.

The potential energy per cell is equal to $-1 \frac{1}{2}\left(u_{1}+u_{2}\right)$ where $\tilde{u}_{1}$ is the work required to remove a single electron from the metal and $u$ that required to remore a single atom. We have calculated $w_{1}+a^{\prime}$, but not $w_{1}$ and $u_{2}$ indiridually: If the repulsion between the positive parts of two atoms was proportional to the inverse square of the distance, then $w_{1}^{\prime}$ would be equal to $w_{2}$, but if the repulsion is equal to $\frac{c^{2}}{r^{2}}\left(1-\frac{c p}{r}\right)$, then $w^{2}$ will be greater than $w_{1}^{\prime}$, and $w_{1}^{\prime}$ will be less than $\frac{1}{2}\left(w_{1}+w_{2}\right)$. Let $w_{1}=\frac{\beta}{2}\left(w_{1}+w_{2}\right)$ where $\beta$ is a fraction, then the work required to remore any electron from the alkali metals will be $\beta$ times the values given in the preceding tables. The contact difference of potential between two metals is equal to the difference in the amounts of work required to remove an electron from the two metals, thus the contact difference of potential between sodium and potassium would be $\beta(7.3-6.36)=.92 \beta$ volts. The value found by experiment is .4 volt, hence $\beta=.44$, so that $x_{1}^{\prime}=.44$ (potential energy per cell).

This gives the following values for the work required to tean an chectron from the alkali metals.

$$
\begin{aligned}
& \mathrm{Le}=4.0-\mathrm{n} \text { m } \mathrm{s} \\
& \mathrm{Na}=3.2 \\
& \mathrm{~K}=2.51 \\
& \mathrm{RW}=2.42 \\
& \mathrm{Cs}=2.24
\end{aligned}
$$

The work reguired to tear an electrom from sodium was estimated be Richardson from thermionic data as 2.6 volts, and from the photoelectric effect as 2.1 volts. The values given in the table represent the work required to remove an electron from the body of the metal; the atoms in the surface layers of the metal differ in energy from those in the interior, and an electron can escape from them with less expenditure of energy. As the values given in the table are less than half the amount of work required to remove both an electron and the positive part of an atom from the metal, the work required to remove an atom is greater than that required to remove an electron, so that when the metal is heated, the number of positive ions which come off will be small compared with the number of electrons.

The values given on page sts for the compressibility are for a distribution of atoms and electrons such that the atoms are at the centres of cubes and the electrons at the corners.

When the atoms and electrons are arranged so that atoms and electrons occur alternately at equal intervals along the lines of a cubical lattice, we can show that the electrostatic potential energy for a volume of the metal containing $N$ electrons and $N$ atoms is

$$
\begin{equation*}
-1.7 \frac{N c^{2}}{d} \tag{62}
\end{equation*}
$$

where $d$ is the shortest distance between an atom and ann electron. If these $\Lambda$ atoms and electrons make up unit volume, then if $\Delta$ is the density of the metal and $M$ the mass of an atom, since a cube with side $2 d$ contains four atoms

$$
\begin{gather*}
\frac{4 M}{S d^{3}}=\triangle: M M=\Delta  \tag{6:3}\\
\frac{1}{d}=\left(\frac{2 \triangle}{M}\right)^{\frac{1}{3}}
\end{gather*}
$$

hence the electrostatic energy per unit rolume is

$$
\begin{align*}
& -1.1 \checkmark \varepsilon_{2} 2 \frac{1}{3}\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \\
& =-2.2 \varepsilon_{2}\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \tag{64}
\end{align*}
$$

It follows from this that the bulk moxlulus is

$$
\begin{equation*}
9\binom{\triangle}{1 /} \tag{6.0}
\end{equation*}
$$

this is not very mach more than half the value $\frac{3.6}{6}\binom{\Delta}{W}$ corresponding to the other (istribution which we saw anreed very well with the experiment results; hence we conclude that the atoms and electrons cammot in the alkali metal be arranged so as to oceur alternately at equal intervals along the lines of a cubical lattice.

For the arrangement where the atoms are arranged in face-centred cules with electrons at the centres of four out of the eight smaller cubes into which the face-centred cube is divided, I find that the elcetrostatic potential energy for a volume containing $N$ atoms and $\lambda$ clectrons is

$$
\begin{equation*}
-3.50\left(\frac{\triangle}{M}\right)^{\frac{4}{3}} \tag{66}
\end{equation*}
$$

so that $k$, the bulk modnlus. is equal to

$$
\begin{equation*}
\frac{-3.50}{9} c_{2}\left(\frac{\triangle}{M}\right)^{\frac{4}{3}} \tag{67}
\end{equation*}
$$

this differs by less than 5 per cent from the value given by equation ( 58 ), and would agree within the errors of experiments with the values found by Richards.

When the arrangement of the atoms of a monovalent element is that of the bodycentred cube and the electrons are placed two by two along the diagonals of eight such cubes taken as a single unit, Miss Woodward finds

$$
\begin{equation*}
k=\frac{3.2}{9} e_{2}\left(\frac{\triangle}{M}\right)^{\frac{4}{3}} \tag{6S}
\end{equation*}
$$

This would give values for $k$ appreciably smaller than those found by experiment. The arrangement of the electrons was assumed to be as follows: Two electrons were placed inside each cube on a diagonal, one on one side of the centre, the other on the other, midway between the centre of the cube and the ends of the diagonal. The diagonals along which the electrons are placed are chosen so that in a cube built up of eight such small cubes no two of the diagonals in any four whose centres are in one plane are parallel or intersect. The diagonals in two cubes which have a corner but neither an edge nor a face in common are to be parallel. This arrangement is equivalent to arranging the atoms and electrons alternately at equal intervals along lines whose directions are parallel to the four diagonals of the cube.

The Encrgy and Compressibility of Divalent Elements
We shall further test the electron theory of solids by calculating the compressibility of a divalent element. Calcium crystallizes in the regular system and the arrangement of the atoms has been shown by X-ray analysis to be that of the face-centred cube. Taking such a cube as the unit, it contains four calcium atoms; since calcium is divalent, if there are four atoms there must be eight clectrons. The most symmetrical way of arranging these is to place one at the centre of each of the cight small cubes in to which the unit cube is divided by planes bisecting its sides at right angles.

Taking this arrangement, I find that the electrostatic potential energy of a calcium atom is, if $2 d$ is a side of the unit cube,

$$
\begin{equation*}
-\frac{e^{2}}{d} 5.33 \tag{69}
\end{equation*}
$$

while that of an elcetron is equal to

$$
\begin{equation*}
-\frac{e^{2}}{d} 1 . S \tag{70}
\end{equation*}
$$

Hence the electrostatic potential energy of one atom and two electrons is

$$
\begin{equation*}
-\frac{e^{2}}{d} 8.93 \tag{71}
\end{equation*}
$$

The total actual potential energy, i.e., the potential energy when we take into account the effect of the forces varying inversely as the cube of the distance is one-half of this, i.e.

$$
\begin{equation*}
-\frac{e^{2}}{d} 4.46 \tag{72}
\end{equation*}
$$

Since the cube whose volume is $S d^{3}$ contains four atoms

$$
\begin{equation*}
\frac{4 M}{8 d^{3}}=\triangle \tag{73}
\end{equation*}
$$

where $M$ is the mass of an atom and $\triangle$ the density of the metal; hence the energy per unit volume is equal to

$$
\begin{equation*}
-e^{2} 5.61 \times\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \tag{74}
\end{equation*}
$$

The bulk modulus $k$ is equal to

$$
\begin{equation*}
e^{2} \frac{11.2}{9}\left(\frac{\triangle}{M}\right)^{\frac{t}{3}} \tag{75}
\end{equation*}
$$

for calcium $\triangle=1.55$ and $M=40 \times 1.64$ $\times 10^{-24}$, hence $k$ for calcium $=.192 \times 10^{12}$. The compressibility which is the reciprocal of $k$ is $5.2 \times 10^{-12}$; the value found by Richards is $5.5 \times 10^{-12}$, so that the agreement between the observed and calculated values is quite satisfactory.

The potential energy for an atom and two electrons is that corresponting to the fall of an electron throngh twonty-two volts.

## The Compressibility of a Trivalent Element

Aluminum is a trivalent chement crestallizing in the regular system. The arrangement of the atom has been shown to be that of a face-centred cube. Taking this cube as the unit it contains four atoms; it must, therefore, since aluminnm is trivakent, contain twelve electrons. If we place electrons at the middle points of the sides, at the centres of each of the cight cubes into which the unit cube is divided be bisecting planes and one at the centre of the cube, we get a symmetrical distribution of these 1 welve electrons. This distribution is the same as if each atom were placed at the centre of a rhombic dodecahedron and the electrons at the corners of the dodecahedron. Since four planes meet at some of the corners while only three meet at others, we see that the electrons will be divided into two groups.

For this arrangement I find that the electrostatic potential energy of the atom, with its triple charge of electricity, is equal to

$$
\begin{equation*}
-e^{2} \frac{10.6}{d} \tag{76}
\end{equation*}
$$

where $2 d$ is the side of the face-centred cube and $c$ the charge on an electron.

For an electron at a corner of the dodecahedron where four planes meet, the potential energy is

$$
\begin{equation*}
-c^{2} \frac{0 . \overline{0}}{d} \tag{71}
\end{equation*}
$$

and for an electron at a corner where three planes meet

$$
\begin{equation*}
-c^{2} \frac{1.75}{d} \tag{7ু}
\end{equation*}
$$

Each atom is associated with one electron of the first type and two of the second, hence the electrostatic potential energy of this system is $-c^{2} \frac{1+2.5}{d}$ and the total potential energ! - $\varepsilon^{2} \frac{-12}{d}$.

Now

$$
\begin{equation*}
\frac{1}{d}=\left(\frac{2 \triangle}{M}\right)^{\frac{1}{x}} \tag{79}
\end{equation*}
$$

hence $k$ the bulk modulus is given by the equation

$$
\begin{equation*}
k=\frac{17 . S^{2}}{9} c^{2}\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \tag{>0}
\end{equation*}
$$

 hence $k=10.4 \times 10^{2}$, the ralue found be experiment is is $\times 10^{12}$.

## Compressibility of the Diamond

In the diamond we hate a quatrivalent chement erystallizing in the regular system. The arangement of the carbon atoms in the diamond has been shown be Sir IV. H. Brage and brof. Wr. L. Brages whe given by the following scheme. The atoms ocempe
(a) the corners of a cube;
(b) the centres of its faces;
(c) fonir of the centres of the eight cubes into which the large cube is divided by planes bisecting its sides at right angles.
We shall take this cube as our unit: it contains eight carbon atoms. Since carbon is qualrivalent, it must contain thirty-two clectrons; these electrons will be situated
(a) at the middle points of the edges of the cubical unit; this accounts for three;
(b) at the centres of each of the faces of the eight small cubes; this accounts for twent y -four;
(c) at the centres of the four small cubes not occupied by the carbon atoms; this accounts for four;
(d) one at the centre of the large cube.

Making use of this unit, we can calculate the electrostatic potential energy due to the charges on the atoms and electrons. Let $E$ be the charge on a carbon atom, $c$ that on an electron.

The electrostatic potential energy of a carbon atom

$$
\frac{1}{2} E\left(\frac{\ddot{y} c}{r^{\prime}}-\frac{\check{Z} E}{r^{\prime}}\right)
$$

I find to be equal to

$$
\frac{1}{2} \frac{E}{d}(149.346 c-35.13 E)
$$

where $2 d$ is the side of a unit cube. Since $E=t e$, this reduces to

$$
\begin{equation*}
17.65 \frac{e^{2}}{d} \tag{ऽ.3}
\end{equation*}
$$

The electrostatic potential energy of an electron I find to be

$$
\begin{gather*}
\frac{1}{2} \frac{e}{d}\left\{\frac{E}{4} 149.346-147.54 e\right\}  \tag{54}\\
=\frac{1}{2} \frac{c^{2}}{d} 1.75
\end{gather*}
$$

Hence the edectrostatic potential energy for the atom and its four associated electroms is $\quad 21.15^{c^{2}} d$

Since there are erght atoms in the cube whene odge is $2 d$, if $\Delta$ is the density of the damond and $I /$ the mass of a carbon atom,

$$
\begin{align*}
& \therefore d /  \tag{..i}\\
& \therefore d^{3}
\end{align*}=\triangle
$$

or

$$
\begin{equation*}
{ }_{d}^{1}=\left(\frac{\triangle}{l /}\right)^{\frac{1}{3}} \tag{Nis}
\end{equation*}
$$

Thus the electrostatic potential energy per one atom and form electrons is

$$
\begin{equation*}
21.1 .5 c^{2}\binom{\triangle}{11} \tag{n7}
\end{equation*}
$$

and the energy per unit volume is

$$
\begin{equation*}
21.1 .5 \epsilon^{2}\left(\frac{\triangle}{M}\right)^{\frac{1}{3}} \tag{S.S'}
\end{equation*}
$$

Hence $k$, the bulk modulus of the diamond, is given by the equation

$$
k=\frac{21.15}{9} c^{2}\left(\frac{\triangle}{M}\right)
$$

for the diamond $\triangle=3.52, \quad M=12 \times 1.64 \times$ $10^{-24}$; hence $k=.5 .6 \times 10^{12}, 1 k=.178 \times 10^{-12}$.

This value for $1 k$ is much less than that, $.5 \times 10^{-12}$, found by Richards. It is, however, in close agreement with $.16 \times 10^{-12}$, the value recently found by Adams. ${ }^{35}$

The properties of solids formed by elements whose atoms have more than four disposable electrons are quite different from those of solids formed by the elements with one, two or three disposable electrons. The latter are, with the exception of boron, metallic and good conductors of electricity and heat. The former, for instance sulphur and phosphorus, are insulators. Not only do they insulate in the solid state, but they do so after they are fused. They differ in this respect from solid salts which, though they may insulate when in the solid state, generally conduct when melted. This suggests that in the salts there are positively and negatively electrified systems which are fixed when the substance is in the solid state, but can move about when it is liquefied. In such elements as sulphur or phosphorus there does not seem to be any evidence of existence of anything but neutral systems; in other words, the solid may be regarded as built up of units, each of which contains as much positive as negative electricity. It is

[^93]noteworthy that, according to the Electron Theory of Chemical Combination, two similar atoms, if they have each more than four disposable electrons, like the atoms of sulphur and phosphorus, can combine and form a saturated molecule, which is electrically nentrat.

Thus we are led to distinguish three types of solicls:
(a) A type where the atoms are arranged in lattices, and the electrons in other lattices coordinated with the atomic ones. In this type each electron has no closer connection with a particular atom than it has with several others. Thus, for example, when the electrons form a simple cubsical latice with the atoms at the centres of the cubes, each electron has eight atoms as equally near neighbors; so that an electron is not bound to a particular atom. This type includes the metals; it also includes boron and carbon in the form of diamond, which are insulators.
(b) A type represented by the salts; here the atoms are again arranged in lattices, but each electron has much closer relation with one particular atom than it has with any other. Thus to take the case of NaCl , where the Braggs have shown the atoms to be arranged according to the following scheme:

$$
\begin{array}{llll}
\mathrm{Na} & \mathrm{Cl} & \mathrm{Na} & \mathrm{Cl} \\
\mathrm{Cl} & \mathrm{Na} & \mathrm{Cl} & \mathrm{Na} \\
\mathrm{Na} & \mathrm{Cl} & \mathrm{Na} & \mathrm{Cl}
\end{array}
$$

We suppose that each sodium atom has lost an electron, while each chlorine atom has gained one; thus each chlorine atom has eight electrons around it, and each electron is much more closely bound to one particular chlorine atom than to any other. It is so closely associated that it is not dissociated from its partner in either the solid or liquid state of the substance. Thus the chlorine system always has a negative charge, the sodium one a positive. These atoms do not move when the substance is in a solid state, though they may do so when it is liquefied.

If the distance of the electrons from the chlorine atoms were to increase until it was not far from half the distance between the sodium and chlorine nuclei, this type would approximate to type (a).
(c) A type where the lattices are built up of units which are not electrified; such units are probably molecules containing two or more atoms, though in certain cases they may be single atoms. The characteristic of the type is that each unit has sufficient elec-
trons bound to it to make it clectricalls. neutral. and that cach electom remains attached to a particular atom. Thus where an electric force acts on the system there is no tendency to make the mit move in one direction rather than the opposite, so that the substance camon conduct electricity.

There is something anomatons abont the compressibility of silieon: the arransement of its atoms as determined he X-ray analysis is the same as that of the diamond. white its atomic rolume is 2.7 times greater. Wo might therefore expect that its compressibility would 1 e (2.5) or : $:$ - times that of the diamond. Its compressibility, however. as determined loy Richards, is only $16 \times 10^{22}$. which is practically the same as the revised value for the diamond. In silicon, however, there are $t$ wo layers of electons so that when the four electrons in the outer laver have been distributed to form the lattice. a layer of eight will remain surrounding the positive part of the atom. The compression of the silicon may involve not merely the closer approach of the positive parts of the silicon atoms, but also a closer approach to the central atom of the layer of cight electrons which surround it. The work required to do this would tond to make the compressibility less than for a substance like carbon, which after its outer layer has been distributed. has no imner layer left to compress.

The case may be compared with that of a chloride of an alkali metal, say LiCl. In the lattice formed by the atoms each chlorine atom is surrounded be a layer of eight electrons. The compressibility of the salt has been determined by Richards and it is much less than the ralue calculated on the supposition that the chlorine ion with its octet of electrons round a positive charge of seven units can be treated as a negative charge of one unit at the centre of the chlorine atom. The compression of the octet round the chlorine atom has also to be taken into account. Miss Woodward has done this recently and finds that the calculated values are in fair agreement with those determined by experiment.

A similar argument applies to the elements copper, silver and gold, which are far less compressible after allowing for the difference in the atomic volume than they would be if they followed the same law as the other monovalent elements, the alkali metals. The heavier alkali metals have also inner layers. but the atomic volume of these is so great that the compression of these layers does not
come nearly so much into play as in prold and silcer. Which have much smaller atomic volumes.
T.DBLE V'lll

Potential linurgy fer 1 tom with Its . Assoriated bilertrons.
Monoialent Eilements

FaCe-CENTRED C(CbE:
Electrons at midhle points of edgees

Electrons at centres of four cometit-
vent сиъес . . . . . . . . . . . . . . . $\frac{3.5 r^{2}}{!}\binom{\triangle}{I I}$
Bons-Centred Cube
Dizalent Elements
Fice-centren Cube:
Electrons at centres of cight constit -
uent culues................. $\frac{11: 2 e^{2}}{9}\binom{C}{I I}^{\frac{1}{3}}$
Electrons at centres of edges iturl
four constituent chbes.......... $\frac{7.75 e^{2}}{9}\left(\frac{L}{M}\right)^{\frac{4}{3}}$
Tritalent Elements
F.tce-centred Clbe:

Electrons at middle proints of cerges and centre of culbe and at centres
of four constituent cubes. . . . . $\frac{18 e^{2}}{9}\left(\frac{\square}{M}\right)^{\frac{1}{3}}$
Quadriadent Elements
Face-centrej Ctbe and at:
Centres of four constituent cubes. Elecirons, conlres of edges, centres of faces of constituent cubes

$$
\begin{aligned}
& \text { and at centres of four of these } \\
& \text { cubes. . . . . . . . . . . . . . . . . } \frac{21.1 . j e^{2}}{9}\left(\frac{\triangle}{11}\right)^{\frac{1}{3}}
\end{aligned}
$$

We mar sum up the results of the preceding investigation of the compressibility of solids as follows:

The compressibility is equal to $C\left(\frac{\triangle}{I I}\right)^{\frac{1}{3}}$, where $C$ is a quantity depending on the valencr of the element and the form in which it crystallizes: $\triangle$ is the density of the solid and $M$ the mass of an atom of the element.

The potential energy of an atom with its associated electrons is equal to

$$
\begin{equation*}
-\frac{4.5}{c}\left(\frac{\triangle}{\overline{I I}}\right)^{\frac{1}{x}} \tag{90}
\end{equation*}
$$

Table VIII contains a summary of the preceding results.

## Surface Tension

The preceding expression represents the energy of an atom in the mass of the metal,
for ond on the surface it reguites modification. 'Thus if $l$ ' is ath atom or electron part of its potential energs depends on the atoms and deotrons above a borizontal Hane thromph $P$. If the metal is broken so that this plane beomes a surface of the metal, the atoms amd electrons above $P$ will 160 lenger affect the potential energy so that this will be changerl. We cam find an approximation to the amonat of this change in the following way: let us take a crystal of a monovalent element and suppose that the atoms and electrons are arranged in the plane of the surface according to the scheme when the atoms are at the corners and centres of the faces of a culbe and the electrons at the middle points of the sides and the centre of the eube. This is the more convenient arrangement to take, since the atoms are present in equal numbers in the plane, so that the total electric charge 1 pon it is zero. With this arrangement I find that the contribution of the atoms and electrons above $P$ to the potential energy of the system consisting of $P$ and an electron is $-.07 .5 \frac{e^{2}}{d}$, where $d$ is the distance between an atom and the nearest electron. We saw that in this case for an atom and electron in the interior the energy is $-1.77 \frac{e^{2}}{d}$. Thus the potential energy $S$ of the atom and electron in the surfaces exceeds $I$, the potential energy in the interior by $\frac{.075}{1.77} I=0.42 I$. The surface tension arises from the excess of the potential energy of the atoms in the surface over those in the interior and is equal to the excess for one atom multiplied by the number of atoms in unit area of the surface. Let us apply this to find the surface tension of sodium. The energy of an atom of sodium not on the surface is equal to that gained by an electron falling through 7.2 volts, i.e., $7.2 \times 1.6 \times 10^{-12}$ ergs. The distance between two sodium atoms is equal to $3.37 \times 10^{-8}$, hence the number of sodium atoms per square centimetre is $10^{16} / 11.35$. Thus the surface tension of sodium is

$$
\begin{gather*}
.042 \times 7.2 \times 1.6 \times 10^{4} 11.35  \tag{91}\\
=4.32 \mathrm{ergs} / \mathrm{cm} .^{2}
\end{gather*}
$$

The value given in the tables for molten sodium is 500 , so that the calculated and the observed value are of the same order of magnitude. The calculation is only a rough approximation as we have neglected the effect of temperature and supposed that
the distance botween the soditm atoms is the same on the surface as in the interior. The increase in the potential energy at a surface will depend upon the orientation of the surface. Thus if the face of the sodium is a plane paratlel to the diagonal plane of the cube instead of the plane parallel to one of its faces, I find that the potential energy of an atom and electron at the surface will be greater than if they were in the interior by . 067 I instead of $.042: 3 I$ as in the former case. In this plane the number of atoms per unit area is only $1 / \sqrt{2}$ that in the former case, thus the surface tension in this plane will be to that in a plane parallel to a face of the cube in the proportion of 47.3 to 42. The atoms in this plane having greater potential energy than those in a plane paralled to the faces of the cube will develop a greater amount of heat when they enter into chemical combination. I find that for a gram molecule of sodium the difference would be about 10,000 calories. Thus chemical action would be more likely to go on at these faces than at the natural cleavage faces of the crystal; the photoelectric emission of electrons would also be greater.

## Communication of a Charge from Gaseous Ions to the Electrodes

The preceding values have an important bearing on the transmission of electric charges from gaseous ions to metallic electrodes.

Consider first the case of a positively charged ion. If this is to give up the charge to the electrode and escape as an uncharged atom or molecule, an electron must come from the metal, and be received by the ion. Let the work required to abstract the electron from the metal be $V_{m}$ and let the ionizing potential of the gas be $V_{g}$, there the work required to discharge the ion is $V_{m}-V_{g}$. If $V_{m}$ is greater than $V_{g}$ it will require an expenditure of work to discharge the ion, the ion will not give up its charge, i.e., there will be no continuous current through the gas unless the external potential difference is greater than $V_{m}-V_{g}$.

Now take the case of a negatively electrified ion giving up its charge to the anode; here an electron has to be taken from the ion and given up to the anode; to remove the electron requires an amount of energy equal to $V_{1}$, where $V_{1}$ is the work required to move an electron from the negatively charged ion, it will be less than the ionizing potential. On the other hand, work equal to $V_{m}$ is gained when the electron goes into the metal
thas to effect the transfermene work equal to $\mathrm{V}_{1}-\mathrm{V}^{\prime} \mathrm{m}$ must be donce, so there must be an extemal potential difference wrater than $V_{i}-V_{m}$ to keep up the current.

It would seem as if experiments on the potential required to fffert the passage of electricity from the gas to the metal ought to give us the means of finding $V_{k}$ and $I_{i}$. quantities which are of fundancontal importance in the energetics of chemical combination. To illustrate the kind of effects we are considering, let we take the case of ionized mercury vapor, the ionizing potential of mercury vapor is about 10 volts; I cannot find any direct measurements of the work required to extract an electron from liquid mercury, but inasmuch as mercury gives off electrons when exposed to light whose warelength is not less than 2000 , it can not be greater than about five volts: thus $V_{m}$ is much less than $V_{g}$; thus a positively charged mercury atom could give up its charge to a liquid surface of mercury without the aid of an external potential difference. Unless, however, the work required to extract an electron from a negatively electrificd mercury atom is less than half that required to extract it from a neutral one, $\Gamma_{1}$ would be greater than $\mathrm{V}_{m}$ and it would require an external electromotive force to make negatively electrified mercury atoms give up their charge to a mercury surface. Both the gas and the electrode can be raried in these experiments; thus if the gas were a strongly electronegative one, like chlorine, we should expect $V_{1}$ to be greater than $V_{m}$ for a metal like sodium for which Richardson's value is 2.6 volts; if so, it would require an external electric force to make negative chlorine ions discharge to sodium and get free. The chlorine ion would cling to the sodium and combine with it, thus with chlorine ions and an electropositive metal as electrode, the anode would be more likely to be attacked by the chlorine than the cathode. To liberate the electron from the chlorine and get a neutral chlorine atom would require a potential difference at the anode equal to $V_{1}-V_{m}$. At the cathode a positively electrified chlorine atom might not merely get neutralized by receiving one electron, but if $V_{1}$ were greater than $V_{m}$, work would be gained by the chlorine atom receiving a second electron from the meta. When an electron falls into an atom, light is emitted; the frequency of the light depending on the amount of loss of potential energy caused by the falling in of the atom, or what
is the stanc thing. We the work required to eject the eleetren again. This work where a pesitively charged chlorme atom receives one electom and beomes nemtral is meatured by the ionizing potential of the chlorine atom: when a netutal atom receives an additional electron it is measumed by $\mathrm{l}_{\mathrm{l}}$. Thus, whenever, at the sumface, say of an alkali metal, the transference of clectrons from the metal to, say, chlorine atoms, is going on, light will be emitted; this light will fall upon the metal, and as these metals give large photoelectric effects, it may cause them to emit electrons. As the light is emitted quite close to the surface of the metal it is quite likely that the intensity at the surface may be sufficient to protuce measurable effects though the intensity of the light may be much too faint to be detected at distances large compared with the radius of an atom.

## Intermetallic Compounds

The expression we have found for the potential energy of a solid has an important application to the theory of intermetallic compounds and alloys. Take the case of $t$ wo metals, $A$ and $\bar{B}$, when they are apart they consist of lattices of atoms and electrons, and as we liave seen may be regarded as built up of units, each unit containing a certain number of atoms, together with the appropriate number of electrons. Thus if the metal were monovalent there would be as many electrons as atoms; if it were divalent there would be twice as many, and so on. Suppose now that the metals were mixed under conditions which permitted free movement of the atoms and electrons. Then in the mixture in addition to the units consisting wholly of $A$ or of $B$ atoms, we may have units containing both $A$ and $B$ atoms. Thus to take a definite case, let $A$ be sodium and $B$ potassium, the unit might be a cube of side $2 d$, built up of eight cubes; at the centres of these, atoms of sodium and potassium might be placed alternate $y$, the electrons would be at the corners, the centres of the faces and the centres of the edges, and at the centre of the large cube. Such a unit would certainly be formed at low temperatures if its potential energy were less than that due to four units of sodium and four of potassium when these metals were separated. Again we might have a cubical unit with the potassium atoms at the corners and the sodium atoms at the centres of the faces, in this unit there would be three sodium to one potassium atom. There are many other
possible units with different proportions of sodium and potassium atoms. Whether such units will be formed or not is a question of the redation between the potential energy of such a mit and the potential energy of the atoms it contans when arranged so that the units contain only one kind of atom. The point I wish to emplasize is that the conditions which determine the formation of these metallic compounds are of quite a different kind from those which determine the formation of gaseous compounds containing one or more electronegative constituents. With these it is the valeney conditions, such as may be expressed by the formation of octets, which govern the type of admissible compound; with the metals, on the other hand, the formation or not of a compound is determined by the potential energy possessed. by a unit of the lattice system formed by the compound. As this potential energy depends on the number of electrons as well as upon the number of atoms in the unit, and as the number of electrons depends upon the valencies of the atoms, valency will have an influence upon the type of compound, but of a different character to that exerted in compounds between metals and electronegative elements. From these considerations we should expect that the structure of intermetallic compounds would not conform to the condition of valency as ordinarily understood. We find, for example, many stable compounds in which two atoms of a bivalent metal are combined with one atom of a univalent one, e.g., $\mathrm{NaCd}_{2}, \mathrm{KHg}_{2}$, CuMg., a proportion inconsistent with the usual conception of valency, but one which would be satisfied by a very simple form of unit cell. Thus if the divalent atoms were at the corners of a hexagonal prism and the monoralent atom at the centre, while the electrons were placed at the centres of side faces of the prism and two along the axis on either side of the monovalent atom, we have a unit containing two divalent atoms, one monovalent atom and five electrons.

## Mixed Crystals and Intermetallic Compounds

Metallurgists distinguish between two types of combination between metals. The one type called intermetallic compounds consists of alloys of a composition at which on a graph representing the relation between percentage composition and some physical property, such as electrical conductivity, shows a well-marked maximum or minimum. These points in general correspond to alloys
in Which the proposition between the numbers of atoms of the two metals are expressed by simple ratios. Alloys of other composition represented by the regions between the maxima and minima are supposed to be in a state which is sometimes described as mixed crystals and sometimes as solid solutions.

Let us consider the question of the combination of two metals $A$ and $B$ from the point of view of the electron theory of solids. There are several possibilities, the alloy might be a mechanical mixture of $A$ and $B$; by this we mean that the atoms of $A$ and $B$ are respectively arranged in their own space lattices, and that there are no composite space lattices made up of atoms of $A$ and $B$ arranged in regular sequence. Another alternative is that the atoms should be arranged in composite space lattices, the atoms along the lines of the lattices consisting partly of $A$ atoms and partly of $B$. Here there are again several possibilities, for with a fixed proportion between the number of $A$ atoms and the number of $B$ there are many different composite lattices possible. Thus, for example, if there are three $A$ atoms for one of $B$, we might in two dimensional lattices hare the spacings

## I.

a a a a a a a a a
$\mathrm{ab} a \mathrm{~b} a \mathrm{~b} \mathrm{a} b \mathrm{a}$
a a a a a a a a a
a babababa
or
II.
a a aba a a ba a aba a a $a b a a \operatorname{aba} a \mathrm{a} b \mathrm{a} a \mathrm{a} b \mathrm{a}$ a a a b a a aba a aba a a or

## III.

$a \mathrm{aba} a \mathrm{~b} a \mathrm{ab} \mathrm{a} a \mathrm{~b} a \mathrm{a} \mathrm{b}$ a a a a a ba a a a aba a a a a ba abaaba abaab
Thus the alloy might consist either of one kind of lattice or a mechanical mixture of a number of different kinds. If the atoms have been in a condition in which they could diffuse freely, e.g., if the alloy were stirred for a long time when the melt was liquid, the arrangement would be that corresponding to minimum potential energy, remembering that when there is a mechanical mixture of different phases we must take into account the energy due to surface tension. When there is a well-marked minimum in the poten-
tial energy for one arrangement of the atoms. we should expect that the allor would be homogeneous and represented by a single lattice corresponding to this arrangement. If, on the other hand, there are several arrangements which differ but little from each other in potential energy we might expect to find all these arrangements present in the alloy in proportions which would vary with the temperature. When the alloy is homogencous and the arrangement of atoms and electrons capable of being represented by a single lattice, it corresponds in my view to an intermetallic compound. When, however, there are several different arrangements mised together, it corresponds to a solid solution.

When the atoms of $A$ and $B$ carry the same charge of electricity, then if $A$ is greatly in excess we should expect the $B$ atoms to occupy positions along a space lattice that differed but little from that for pure A. When, however, the number of the $B$ atoms increase beyond a certain proportion, there will probably be large modifications in the space lattice for the mixture and possibly the formation of one of quite a different character. The probability of a new type of space lattice will be much increased if $B$ and A carry different electrical charges, i.e., have different valencies.

Let us consider from this point of view the changes we might expect in the properties of a mixture of two metals, $A, B$, starting from pure $A$ and ending with pure $B$.

When $A$ is greatly in excess, the formation of those compounds which contain a comparatively large proportion of $A$ in comparison with $B$ will, in accordance with the principles of mass action, be promoted, and the mixture will consist of free $A$, little or no free $B$, and a number of compounds, the majority of which contain an excess of $A$ over $B$. As the proportion of $B$ increases the amount of free $A$ diminishes and the proportion between the amounts of different types of compounds changes, the change being mainly at the expense of those which contan a large number of $A$ atoms. When the mixture is such that the proportion between $A$ and $B$ is that of a possible compound, if that compound is one which has markedly less potential energy than its constituents, the whole mass of metal at low temperatures at any rate may practically consist of this compound. It need not, however, do so in all cases; there may be a

[^94]certain amount of dissociation of the compound depending upon the temperature Again, if there is another compound with very small potential energy, some of it is pretty sure to be formed, so that the mixture may not be quite homogencous even when the proportions are those of a possible compound. When the mixture consists almost entirely of one compound, its constitution is identical in many respects with that of a simple metal. All the units of which it is built up are of one kind, and that kind an arrangement of atoms and electrons, which when the units are united give, as in the cases of metals, a system of lattices for atoms and electrons. Any general property possessed by all metals would, we should expect, be possessed by this compound. In particular the conduction of electricity through the compound would take place by the same mechanism as through metals. Now one peculiarity of the conduction of electricity through metals is that the temperature coefficient of the electrical resistance is much the same for all metals, hence we should expect that the temperature cocfficient of an intermetallic compound would be about that of the pure metals. There seems to be very considerable cvidence ${ }^{36}$ that this is approximately true.

The temperature coefficient of the electrical resistance when the mixture of the two metals contains several compounds is often very much smaller than that for pure metals; in fact, it is even sometimes of opposite sign. When there are several different components the effect of a rise in temperature will be an increase in the dissociation and hence an alteration in the proportion of the amount of different compounds present in the alloy. The more complicated compounds will be split up by the rise in temperature and the proportion of simpler ones increased. As the lattices formed by the complex compounds are more intricate than those of the simpler ones, we should expect their electrical resistance to be greater so that when some of these are split up owing to the rise in temperature there will be a tendency to reduce the resistance. Thus in a mixture of this kind there is, in addition to the normal effect which makes the resistance increase, an effect tending to make the resistance fall when the temperature rises; this will diminish the temperature coefficient of the resistance.

Let us now consider the changes in the elastic properties produced by the formation
of these intermetallie compounds. We have seen that in the solid state the potential conergy of an atom and its associated electoms is cepual to

$$
\begin{equation*}
-1.5 \frac{N_{1}}{k_{1}} \tag{92}
\end{equation*}
$$

When $k, 1$ is the bulk modulus and $N_{A}$ the number of atoms in unit volume for the element $A$, since $N_{A}=\triangle_{A} / M_{1}$ where $\triangle_{A}$ is the density of $A$ and $M_{A}$ the mass of its atom, the potential energy per atom may be written as

$$
\begin{equation*}
-4.5 k_{A} \frac{M_{A}}{\triangle_{A}} \tag{93}
\end{equation*}
$$

Thus the potential energy of $n$ atoms of a metal $A$ and $m$ of a metal $B$ before they combine is equal to

$$
\begin{equation*}
-4.5\left(k_{A} \frac{n M_{A}}{\triangle_{B}^{\prime}}+k_{B} \frac{m M_{B}}{\triangle_{B}}\right) \tag{94}
\end{equation*}
$$

If these unite to form the compound $A_{n} B_{m}$, the potential energy per molecule of this compound is

$$
\begin{equation*}
-4.5 \frac{k_{n m}}{\triangle_{n m}}\left(n M_{A}+m M_{B}\right) \tag{95}
\end{equation*}
$$

Where $k_{n m}$ is the bulk modulus of the compound and $\Delta_{n m}$ its density, thus by the formation of the compound, the diminution of potential energy per molecule of the compound formed is

$$
\begin{equation*}
4.5\left\{\frac{k_{m n}}{\triangle_{m n}}\left(n M_{A}+n M_{B}\right)-\left(\frac{n k_{A} M_{A}}{\triangle_{A}}+\frac{m k_{B} M_{B}}{\triangle_{B}}\right)\right\} \tag{96}
\end{equation*}
$$

and this must be equal to the heat of formation per molecule of the compound at zero absolute temperature. Thus from the compressibilities of the compound and those of its
constituents we can calculate the heat of formation of the compound.

Again

$$
\begin{equation*}
\frac{n k_{A} M_{A}}{\triangle_{A}}+m_{{ }_{B} M_{B}}^{\triangle_{B}}=K\left(\frac{n M_{A}}{\triangle_{A}}+\frac{m M_{B}}{\triangle_{B}}\right) \tag{97}
\end{equation*}
$$

:and

$$
\begin{equation*}
\frac{n M_{A}}{\triangle A}+\frac{m M_{B}}{\triangle_{B}}=\frac{n M_{A}+m M_{b}}{\triangle} \tag{98}
\end{equation*}
$$

Where $K$ is the bulk modulus and $\triangle$ the density of the mixture, calculated on the assumption that $A$ and $B$ exert no influence on each other, hence the diminution in potential encrgy due to the formation of the compound may be written in the form

$$
\begin{equation*}
4.5\left(n M_{A}+m M_{B}\right)\left\{\frac{k_{m n}}{\triangle_{m n}}-\frac{K}{\triangle}\right\} \tag{99}
\end{equation*}
$$

Now the compound will not be formed unless the potential energy diminishes, hence

$$
\frac{k_{m n}}{\triangle m n}-\frac{K}{\triangle}
$$

must be positive, or if, as is generally the case, $\Delta_{m n}$ is very nearly equal to $\triangle, k_{m n}$ must be greater than $K$; in other words, the compound must be less compressible than a mechanical mixture of the metals. It is a general rule that the "hardness" of an alloy is greater than we should expect from its composition, and though hardness is not the same thing as the reciprocal of the compressibility yet some of the tests used to measure the hardness, e.g., the indentation produced by a loaded ball, seem almost more a test of compressibility, the result that combination diminishes the compressibility seems to be indicated.


## LIBRARY SECTION

Condensed references to some of the more important articles in the tech. nical press, as selected by the G-E Main Labrary, will be listed in this section each month. New books of interest 10 the industry will also be listed. In special cases, where copy of an article is wanted which cannot be obtained through regular channcls or local libraries, we will sug. gest other sourees on application.
Busbars
Heavy Altemating-cument Buses for Pumaces and Synchronous Converters. Yardles, J. L. Mick.
Blast Fur. \&e St. Pl., Sept., 1923; v. 11, pp. 492-494.
(Discusses diffeculties due to magnetic effects. Serial.)
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Radio Has Been Adopted for Emergeney Communication. D'Alton, F. K.
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(General description of the "guiderl wave" system of the Hydrnelectric Power Commission of Ontario.
Telephoning Over Power Lines.
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(Brief account of the installation on the lines of the Consumers Power Co., Michigan.)

## Cars, Electric

New Forms of Transportation. Potter, WV. B.. and Andrews, H. L.
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("How buses and trackless trolleys should be used in order that transportation shall be most economical.")
Trolley Buses and Flexible Vehicles for Street Railway Service. Kennedy, Tilliam P.
Soc. Auto. Engrs. Jour., Sept., 1923; v. 13, pp. 179-195.
(Survers the field of application of the trolley bus and describes and illustrates several European and American types.)
Circuit Breakers
High-tensinn Oil Circuit Breakers. Delling, W. (In German.)
Elektro-Jour., Aug.-Sept., 1923; r. 3, pp. 174179.
(1llustrated description of breakers and explanation of their operating characteristics.)
Incorporating Series Trip Coil Inside Circuit Breakers.
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## Coal Storage

Storage of Bituminous Coal.
Power, Sept. 25, 1923; v. 58, 1pp. 513-514.

## Condensers, Static

Dieleetric Stresses in Static Contensers for Powerfactor Correction. Marbury, R. DE., ind Atherton, A. 1.
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Why Use Weatherprof Linc Wire? Lindsay, s. C.

Elec. 1Fld., Scp: 22, 1923; v. S2, pp. 609-610.
(Bricf article including a summary of tests on 42 samples of weatherproof line wire.)

## Electric Control Systems

Electrical Control for a 110 Strip Mill at the West Leechburg Steel Company. Wohlgemuth, ⒈ J.
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Foot Control for Main Reversing Mill Motors. Wright, R. H.
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(A companion article entitled: "Foot Control at Steelton' follows on pp. 321-322.)
Supervisory Sustems for Remote Control. Stewart, C. E. and Field, J. C.
Elec. Illd., Sept. 29, 1923; r. 82, pp. f.7.j-6.99.
(Illustrated description of apparatits and methods for remote control of power networks.)

## Electric Distribution

Underfloor Duct System.
Elec. 117d., Sept. 22, 1923; v. 82, pp. 59.-59S. (Describes the underfloor system of distribution for large buildings.)

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Choosing Proper Type of Motor. Johnson, C. N. Iron Tr., Sept. 20, 1923; v. 73, pp. 812-813.
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Motor Drive and Control Requirements for Paper-mill Beaters. Cordes, O. C.
Elec. Hld., Sept. 22, 1923; r. S2, pp. 611-612.

## Electric Drive Pumps

Kevolutionizing：Minc J＇unpring witls ．Intomat－ ically l＇amod，Sitartod and．（＇ontrolled （＇onirilugal P＇umps．Coaly，lidgar．

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Electric Drive－Steel Mills
Direet－rommeded Induction Motors vos．Cearcel Molors for Rolling Iron and Stcel．Barn－ looldt，11．I．
Elé．Jour．，Supt．， $1923 ;$ r．20，pp．31t－317．
Ekectic Drive for（ind－rollerl Steel Strip Reels． Maloney，James，and 1）can，D．W．
Elec．Jour．，S＇心ut．，1923；ど．こ0，1p．320－329．
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（Describes a regulator for motors lriving wire reels in a steed mill．）

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Facts Abont Electric Heating．Whelen，M．P． Elec．News，Sept．15，1923；v．32，pp．78－80．
（＂Results of special researeh on the applica－ tion of elcetrical heating systems to （wellings．＂）
Electric Meters
Meter for Recording Transformer Losses．（In German．）
Elektro－Jour．，Aug．－Sept．，1923；‥ 3，pp． $179-$ 180.
（Describes a three－phase meter for use in determining transformer and line losses in high－tension installations．）
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Calibration of Test Meters．Knowlton，A．E． Elec．ITld．，Sept．29，1923；v．82，pp．645－647．
（Describes equipment and methods used in the laboratory maintained by the Public Utilities Commission of Connecticut，at Yale University．）
Electric Motors，Induction
Operation of Induction Motors with External EMF＇s Impressed on the Rotor Circuit． Cotton， H ．
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Causes and Prevention of Explosions in Power Transformers．Eschholz，O．H． Elec．IVld．，Sept．1，1923；v．82，pp．423－425．
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How to Check Instrument Transformer and Meter Connections．Todd，Victor H． Power，Sept．11，1923；v．58，pn．413－415．

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Interannection Progress in Ohio at 132，000 Volts．Snider，George E．，and Spracklen， E．E．
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Temperature Rise in Copper Conductors on Nomentary Iligh Current Densities． Gittins，G．E．
Met．－Vick．Gas．，Aug．，1923；v．T，110．329－330．
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Producing Synthetic Gray Iron in the Electric Furnace．Willson，Edwin L．
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（Results of experiments conducted by the Hartford Electric Light Co．，and the Con－ nceticut Elcetric Steel Co．）

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Development of the Modern Gear．Phillips W．H．
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Continuous－current Generator for High Voltage． Bergman，S．R．
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Recording Hydraulic－turbine Governor Operation with an Oscillograph．
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Detailed Estimate of the Cost of Davis Bridge Development．
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Accurate Methods of Migning Steam TurbinesUsing Sound to Increase Sensitiveness of Measurements. Barker, Sr., Edgar G. Power, Oct. 2, 1923; ․ 58, pp. 526-527.

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Care of Power Transformers. Brown, Ra!ph. Power, Oct. 2, 1923; ․ 58, pp. $32-524$.

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Why You Can Measure the Area of an Indicator Diagram by a Planimeter.
Power, Oct. 2,1923 ; v. 5s, pp. int-52.5.
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Study of Power-station Efficiencies. Marshall, C. 11 .

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(Short article summarizing the essentials of test procedure.)

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Protective Features of Current Limiting Reactors. Knotts, C. L.
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Exhanst Stem Turned to Profit.
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Surver of the Milwathec Market on Household Appliances. The Milwaukee Journal. 333 pp., 1923. Milwatkee. The Milwatuee Journal.

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[^0]:    * A variometer of this type is illustrated on the cover of this ssue of the Review.

[^1]:    * A photograph of this illumination is shomn as the Frontispiece of this issue of the Review.

[^2]:    * In this illustration, as well as in Figs. 2, 3, 4, 6a, and 6b, the symbols $f_{3}, f_{j}, f e, f_{e^{\prime}}, R, R^{\prime}, F, F^{\prime}$, and $F^{\prime \prime}$ are used to designate both locations and lengths. Whether a location or a length $1 s$ being referred to is explained in each instance in the text.

[^3]:    * The cover illustration of this issue of the REview is to be considered as included in this group.

[^4]:    * The cover illustration of this issue of the Review is to be considered as included in this group.

[^5]:    ${ }^{1}$ A complete theory of stress and strain may be found in the "Treatise on the Mathematical Theory of Elasticity," by A. E. H, Love, 3d ed., chapters i-iv.

[^6]:    * See Frontispiece of this issue of the Review.

[^7]:    ${ }^{1}$ Except, however, if the body is multiply connected and the resultant applied forces do not vanish separately over each boundary. In this particular case the correction coefficients for passing from one isotropic substance to another may be experimentally determined. ("On Stresses in Multiply-connected Plates." by L. N. G. Filon, British Assn. Report, 19.21 .
    ${ }^{2}$ "Photo-elastic Measurements of the Stress Distribution in Tension Members Used in the Testing of Materials," by E. G. Coker, Excerpt Proc. Inst. C. E. (London),-vol. ccvii, part lI. p. 8.
    "Photo-elastic and Strain Measurements of the Effects of Circular Holes on the Distribution of Stress in Tension Members," by E. G. Coker, Trans. Inst. Engrs. \& Shipbuilders in Scotland, vol. lxiii, part I. p. 33.
    -La Photo-elasticimétrie, ses principes, ses méthodes et ses applications," by Paul Heymans. Bull. Soc. Belge Ing. et Ind. Aug., 19르, pp. 147-154, 16j-167. 189-199.

[^8]:    * See Frontispiece of this issue of the Review.

[^9]:    * See Frontispiece of this issue of the Review.

[^10]:    ${ }^{1}$ Value obtained by taking $1 / 2[(p+q)+(p-q)]$, the other values being $(p-q)$ measurements.

[^11]:    ${ }^{1}$ Value obtained by taking $1 / 2[(p+q+(p-q]$, the other values being $(p-q)$ measurements.

[^12]:    * See Frontispiece of this issue of the Review.

[^13]:    * Temperatures on this scale are also denoted as Deg. $K$. (Kelvin).
    $\dagger$ A brief account of this derivation was published in Phys. Rev. 20, 109 (1922). A much more comprehensive paper will appear shortly in the same Journal.
    $\ddagger$ The experimental data on which these values are based will be discussed in a paper by S. Dushman, H. N. Rowe and C. A. Kidner, which will appear shortly in the Physical Review.
    § Phys. Rev. 18, 144 (1921).
    $\|$ These values are to be regarded as only first approximations to the real values.

[^14]:    * loc. cit.

[^15]:    * I. Langmuir. Trans. Far. Society 1r. Part 3. 1921

    Formulie for the end-loss correction have also been derived by A. G. Worthing (Journ. Franklin Inst. 19\%. 597 (1922). But these relations apparently do not agree as well with actual data as Langmuir's relations.

[^16]:    * Physikal. Zs. 15. si2 1914

[^17]:    * See cover illustration of this issue of the Review.

[^18]:    * "Radio Communication," by W. R. G. Baker, September, 1922;.p. 535.
    "Commercial Radio Telephone and Telegraph Transmitting Equipment," by W. R. G. Baker and B. R. Cummings, October, 1922, p. 603, and November, 1922, p. 666.

[^19]:    Fig. 6. Three Views of the 50 -watt Radio-
    tron Used as a Speech Ampilifier in

[^20]:    * See illustration on the cover of this issue of the Review.

[^21]:    *..Nem Type of High-speed Circuit Breaker,' by J. F. Trit?e, General Electric Review. April. 1920.

[^22]:    * See Part III of this series, G. E. Review, April. 1923.

[^23]:    * The mathematical investigation has been carried out and published by F . Henning, in the Elektrote-knisch Zeitscinrif:, Val. 41, 49 and 50. Dec. 9 and 16, 1920. pp. $973-976$ and $10061005^{\circ}$. In the illustrations of the theory the difficult middle distance is a voided.

[^24]:    * See Part III of this Series G.E. Rewnew, April, 1923.
    $\dagger$ Information concerning this range and its photometer is given in the article " Some Feature; of the High-intensity Motion Picture Arc." G.E. Review, Sept., 1922. p. 555.

[^25]:    * These should be regarder as of the nature of a hasty pre liminary test which should be followed by a thoroughly careful and comprehensive research.

[^26]:    Static head 2103. This station is of special inte n
    0
    $\vdots$
    0
    0
    0
    0
    1
    $\vdots$
    $\vdots$
    0
    0
    0
    0
    0
    0
    0
    

[^27]:    * This design was first proposed by B. G. Jamieson, of the Commonwealth Edison Co.

[^28]:    * See "Engineering Mathematics," page 206, by C. P. Steinmetz.

[^29]:    ＊$L=\left(0.7411 \log _{10} s / r+0.08047\right) 10^{-3}$ henries．
    $C=\frac{0.0388 .3}{\log _{10} s / r} 10^{-\pi}$ farads．Where $s$ is a verage spacing between conductors in inches，and $r$ is radius of the conductor in inches．

[^30]:    *For a concise treatment of the multiplication of plane vectors see "Artificial Electric Lines," page 117, by A. E. Kennelly.

[^31]:    * Transactions of the A.I.E.E., June $29,1909$.

[^32]:    *"Review of Distribution Practice." by H. R. Summerhayes, G.E. Review, March, 1914, and "The Dublin, Ireland. Threephase Four-wire Distribution System," by Gilbert Archer, G. E. Review, June, 1914.

[^33]:    * This laboratory was completed in July, 1914. At that early date a $750-\mathrm{kv}$. transformer was available.

[^34]:    ${ }^{1}$ Peek, F. W.. Jr... ${ }^{\text {. The Effect of Transient Voltages on }}$ Dielectrics."'Part"I. Transactions.A.I.E.E., 1915, Vol. 34, p. 185\%; Part II, A.I.E.E., 1919. Vol. 38, p. 1137. ' 'Lightning," General Electric Review, July. 1916.

[^35]:    ${ }^{2}$ Ryan, Harfis J. \& Henline. "Unit Duties on Long Suspension Insulators ". A.I.E.E.: July, 1920 .

    Peek. F. W..., JT. Electrical Characteristics of the Suspension Insulator.' Part I. A.I.E.E. 1912. Page $90^{-}$; Part II, A.I.E.E., 1920. Vol. 39. p. 1685; Electrical World Feb., 1920. * The author was ably assisted by Mr. W. L. Lloyd in obtaining these data.

[^36]:    ${ }^{5}$ Peek, F. W.., Jr., "Tests at $1 .(100.000)$ Volts," Electrical World, Dec. 31,1921 .
    ${ }^{6}$ Hendricks, A. B., "A Million Volt Testing Set," A.I.E.E. Oct., 1922.
    "Peek, F. W.. Jr.. "High Voltage Power Transmission." Proceedings AmericanSozietyot CivilEngineors, November, 1920.

[^37]:    ＊＂Synchronous Motor Starting Torque Characteristics，＂by O，E．Shirley，General Electric Review，October， 1921.

[^38]:    *"Problems of $220-\mathrm{kv}$. Transmission, " by A. E. Silver. Transactions A.I.E.E., Vol. 38 (1919), p. 1037.
    $\dagger$ "Voltage Regulation and Insulation for Large Power Long Distance Transmission Systems," by F. G. Baum, Transactions A.I.E.E., Vol, 40 (1921), p. 1017.
    $\ddagger$ "'220-kv. Transmission, " by R. J. C. Wood, Journal A.I.E.E., July, 1922, p. 471.

[^39]:    *"Unit Voltage Duties in Long Suspension Insulators." by Harris J. Ryan and Henry H. Henline, Transactions A.I.E.E., Vot. 39 (1920), p. 1669.
    $\dagger$ "Electrical Characteristics of the Suspension Insulator," by F. W. Peek, Jr., Transactions A.I.E.E., Vol. 39 (1920), p. 1685.

[^40]:    * See "Parallel Operation and Synchronizing of Frequency Converters," by O. E. Shirley, G.E. Review, February, 1920, page 136.

[^41]:    *See "'Speed and Power-factor Control of Large Induction Motors," by J. I. Hull. G.E. Review, July, 1920, page 630.

[^42]:    * Reprints of the G. E. Review article are at present avááabie by application for Reprint X-692.

[^43]:    *See article on "Silica Glass or Fused Quartz," by Elihu Thomson, G. E. Review, February, 1923.

[^44]:    * Plants under construction.

[^45]:    * Plants under construction.

[^46]:    *"Commercial Radio Telephone and Telegraph Transmitting Equipment." by W. R. G. Baker and B. R. Cummings, General Electric Review, October, 1922 , p. 603, and November, p. 666.
    † Model ET 3620.
    $\ddagger$ Model ET :3619.

[^47]:    ${ }^{1}$ "Physical Nature of Electrical Breakdown of Solid Dielectrics," K. W. Wagner, Journal A.I.E.E., December. 1922.
    ${ }^{2}$ "The Apparent Dielectric Strength of Cables," R. J. Wiseman. Journal A.I.E.E., February, 1923.

[^48]:    ${ }^{3}$ "A New Method for the Routine Testing of High Voltage Cable," by H. S. Phelps and E. D. Tanzer, Journal A.I.E.E., March, 1923.

[^49]:    ${ }^{1}$ Proc. Roy. Soc., 101, p. 290.
    ${ }^{2}$ Proc. Amsterdam Akademie, 25, pt. 3 and 4.

[^50]:    ${ }^{3 "}$ Molecular Volumes of Liquid Chemical Compounds," p. 237. 'Phil. Mag., 40. p. 169, 1920.

[^51]:    Phil. Trans., A, 20.i, p. 319.
    Phil. Mag., 40. p. 169.

[^52]:    * Published in a paper on "Voltage Stresses in Reactors," by F. H. Kierstcad and R. Meeker in the Transactions of the A.I E.E., 1920.

[^53]:    *"Lighthouses and Light Yessels." by Capt. S. G. Hibben. tlluminating Engineering Society's Transactions, Marc'i. 19, 3. Vol. XV'II, No. 3. p. 2+1-272.

[^54]:    *In a previous article published in the Geveral Electric REview, Yol. XXV. No. 7. p. 405 , the writer assumed that in a very wide class of motor-drives. the starting and stopping of all the motors in a group could be considered as random events, and that the theory of probabilities applied to events, and that the theory of probabilities appled to such cases furnished a method for determining the average group. An error in the necessary preliminary discussion of duty cycles led to error in the resulting group r.m.s. input, negligible in most cases. The error did not affect the legitimacy of the method, nor did it affect the average input to the group, or the time distribution of input to the group.

[^55]:    *See General Electric Review, November: 1920. "Performance and Life Tests on the Oxide Film Lightning Arrester," by N. A. Lougee. See also General Electric Review. December, 1921 . "Types of Lightning Arresters," by J. L. R. Hayden and N. A. Lougee.

[^56]:    * See C. P. Steinmetz's "Transient Electric Phenomena," Section 4.

[^57]:    * See A. E. Kennelly's "Hyperbolic Functions Applied to Electrical Engineering Problems." McGraw, 1916; Chap. 7 . p. 85; and C. P. Steinmetz's "Transient Electric Phenomena." $\dagger$ J. H. Cunningham, A.I.E.E. Trans., 1911, Vol. 30, Part 1, p. 245.

    TV Designed by M. I. Pupin; Trans. A.I.E.E., March, 1899; Yol. 16, p. 93.

[^58]:    * This nomenclature and the diagrammatic representation shown in Figs. 1 and 2 are those employed on p. 88, Figs. 47 and 48 of A. E. Kennelly's "Hyperbolic Functions Applied to Electrical Engineering Problems," McGraw, 1916.

[^59]:    * For the equivalent T-line, the same correction factors apply. but change places with each other; i.e., for the T-line, the factor involving the hyperbolic tangent of half the line angle is used for each of the series line elements, while the factor involving the hyperbolic sine of the line angle is used for the capacity element of the T-line (see A. E. Kennelly s "Hyperbolic Functions Applied to Electrical Engineering Problems, McGraw, 1916, pp. 31-33).

[^60]:    * A complete miniature system with substantially fixed circuit constants is described by G. H. Gray. Trans. A.I.E.E., circuit constants is d
    1917, p. 789 . Vol. 36. H. The original short circuit calculating table, due to Messrs. Electric Review, Oct. 1916. p. 901.

[^61]:    * $R_{A}$ and $X_{A}$ comprise reactor, transformer and cable; each cable is 5 miles long. The total per cent values referred to 10,000 kra. base are: Per cent $R_{-A}=2.18$ per cent; Per cent $X_{A}=9.42$ per cent.
    † Lagging.
    ${ }_{+}^{+}$At normal reference line voltage, for balanced loads.

[^62]:    * See G. E. Review, Dec., 1916, p. 1119.

[^63]:    *See Part IV of this series, Geveral Electric Review, May, 1923.

[^64]:    ${ }^{5}$ Proc. Roy. Soc., 98, p. 57

[^65]:    ${ }^{9}$ Phil. Mag. [6]. 27, p. 757 (1914)
    ${ }^{10}$ Zeit. Anorg. Chem., 20. p. 453 (1899); 30, p. 330 (1904)

[^66]:    ${ }^{11}$ A nn. de Chimie et de Physique. 22, pp. 370, 441; 23. p. 2s.
    2Phil. Mog., 2个, p. 7.7 (1914)

[^67]:    ${ }^{13}$ Zeit. für Physik. Chem.. 36. p. 305
    ${ }^{14}$ Ann. de Chimie et de Physique, 23, p. 28 (1911)

[^68]:    ${ }_{15}$ Phil. Mag., 27, p. 763 (1914)

[^69]:    1"Three Thousand Tests on the Dielectric Strength of Oil," by Hayden and Eddy, presented before Convention of A.I.E.E. at Niagara Falls, June 26-30, 1922.

[^70]:    * For a further discussion of this subject with particular reference to motor-generator sets and synchronous converters for railway and d-c. lighting service see " 60 Cycle Converting Apparatus," by J. L. Burnham, General Electric Review, May, 1920. p. 392.

[^71]:    * Induction motors of the sizes ursed for steel mill drives have a normal slip of 1 to 2 per cent; when larger slip is required an external resistance should be added in the secondary circuit.

[^72]:    $\left(^{*}\right) \varepsilon=2.715$, is the base of natural logarithms.

[^73]:    ${ }^{16}$ Richardson, "Emission of Electricity from Hot Bodies."

[^74]:    17 Te hnology Quarterly, 21, p. 288 (1908).

[^75]:    * Langmuir and Kingdon, Science, 57, 58 (1923).
    $\dagger$ The merculy vapor pressure in this experiment was 0.0025 mm . so that very fer ions were formed by collision by electrons passing between electrodes A and B .

[^76]:    * Hissenschaflliche Veroeffenllichungen des Siemens-Konzern. II. p. 252 (1922).

[^77]:    * Langmuir. Physical Re:iesi. 2. 450 (1913) and Physik. Zeit., 15. 345 (1914.)

[^78]:    * Retschinsky and Schaposchnikoff, Annalen d. Physik, 18 , 212-251 (1905).

[^79]:    * The writer wishes to acknowledge the courtesy and assistance extended him in obtaining photographs and_information by the American Plate Glass_Co.

[^80]:    ${ }^{10}$ A nnales de Chimie et de Physique, 22, pp. 370, 441; 23. p. 28.
    19 Proc. Roy. Soc., A90, p. 638, 1914.

[^81]:    20 "Physical Properties of Colloids," 2nd Edition, p. 136. ${ }^{21}$ Phil. Mag., 27, p. 297 (1914).
    2 " Physical Properties of Colloids," p. 135.

[^82]:    ${ }^{23}$ Ber. Deutschen Chem. Gesell., 8, p. 905 (1875).
    ${ }^{24}$ Phil. Trans., 209A, p. 379 (1909).

[^83]:    ${ }^{25}$ H. B. Baker, Proc. Manchester Phil. Soc., 53, No. 16.

[^84]:    ${ }^{26}$ Phil. Mag. 37. p. 419.

[^85]:    * G. E. Review, Nov., 1923, p. 785

[^86]:    ＊Langmuir：Jour．A．I．E．E．，Nx，p．1910． 1913.
    ＋Hyde，G－E Review，ふx，p．S19， 1917.

[^87]:    *Phys. Reziezt, N. S. ス, p. 377, 1921.

[^88]:    *Jour. of Franklin Institute, 1923.

[^89]:    *Worthing: Jour. Franklin Inst. 194, p. 608, 1922.

[^90]:    ${ }^{29}$ Annales de Chimie ct de Physique [81, 5, 70 (1905).

[^91]:    ${ }^{31}$ Comptes Rendus, 158, p. 1895.
    ${ }^{32}$ Phil. Mag., 40, p. 169.

[^92]:    ${ }^{33}$ Hughes: "Photoelectricity." Chap. 5.
    ${ }^{34}$ [erh. d. Deutsch, Phys. Gesell., 13, p. 474 (1911).

[^93]:    ${ }^{35} 1 \mathrm{~F}$ ashington A cad. Sic., 11, p. 4.5 (1921).

[^94]:    :6"Desch. Intermetallic Compounds," p. 52.

