AIRCRAFT-ANTENNA PATTERN MEASURING SYSTEM

Directional antenna of special design (on right) is pointed at aircraft under test by modified SCR-584 automatic tracking radar (antenna at left). Antenna provides discrimination against ground-reflected wave, and provides separate outputs for vertically and horizontally polarized field components, making possible direct plotting of aircraft antenna patterns.
The past decade has shown tremendous strides in the adaptation of electronics to the industrial field. The new UTC Commercial Grade Series of transformers was developed to meet the requirement of this field as well as that of the discriminating amateur and public address man.

CG units are conservatively designed with low temperature rise and good insulation factors to assure dependability in continuous service. All coil structures are vacuum impregnated, and cases are poured with special sealing compounds to assure stability under adverse climatic conditions.

The mechanical construction is rugged. Audio units and power units up to 300 V.A. are housed in heavy drawn steel cases with rugged lugs on moisture-proof bakelite, arranged for chassis mounting. Large power and audio components employ cast aluminum shells for minimum weight, and support the laminations in vertical position to occupy minimum chassis space. CG units are finished in light grey enamel and result in unusual professional appearance on equipment in which they are used.

The CG line includes audio components for all applications ranging from low level... humbucking... multiple alloy shielded input transformers to 600 watt Varimatch modulation transformers. Power and filament components range up to those required for a 3,000 volt 1 Amp. plate supply.

For full details on this new line, write for catalogue PS-408.
1948 I.R.E. NATIONAL CONVENTION and Radio Engineering Show

March 22 to 25, 1948

Hotel Commodore • and • Grand Central Palace

More than 12,000 members and visitors attended sessions and exhibits at the National Convention of The Institute of Radio Engineers in March 1947. Once again, this year the favorable facilities of The Hotel Commodore and Grand Central Palace have been obtained. Plan now for these four days devoted to interesting and instructive technical papers—plus entertainment and The Radio Engineering Show. Free to I.R.E. members. Four day registration is $3.00 to non-members.

TECHNICAL PAPERS

128 papers to be presented during the four days, covering twenty-one major topics, in twenty-eight well organized sessions, will reveal the up-to-the-minute pattern of "Radio-Electronic Frontiers" which is the interesting theme of this convention. Topical outline by days will be:


EXHIBITS

165 Exhibitors will present all that is new in radio and electronic equipment, instruments, components and parts, in interesting exhibits on the first three floors of Grand Central Palace, in our greatest "Radio Engineering Show." (About half of the Technical Sessions will be held in improved halls on the Third Floor.) These exhibits are an engineering "must see" and will occupy a third more space than at our last Show.

WOMAN'S PROGRAM

The annual banquet, on Wednesday, March 24, is the social highlight of the I.R.E. year. 1600 feasters will hear a nationally prominent speaker, see two major awards made, be entertained royally.

Four full days of fun! Including "Sightseeing." The popular "Tea at I.R.E." Wednesday, a matinee, choice of "Antony and Cleopatra" or "High Button Shoes" and other exciting events, all planned for ladies!

PRESIDENT'S LUNCHEON

The 1948 President will be honored on Tuesday, March 23, at a "get-together" which has come to be a feature of these annual meetings.

Watch for detailed program in the March issue


Table of contents will be found following page 32A
The Doherty Circuit for AM broadcast transmitters was the first to achieve high efficiency and economy and still retain the following important advantages of linear and grid bias modulated power amplifiers:

1. A simple tube complement — no high-power audio tubes required
2. No modulation transformer required — savings in space and apparatus
3. Freedom from transient or over-modulation surges — can be heavily overmodulated at any audio frequency for long periods without damage
4. Adaptability to large amounts of feedback derived from the final output envelope, resulting in low noise, low harmonic distortion, and low intermodulation distortion over wide variations in tube characteristics and circuit adjustment
5. Negligible carrier shift, assuring full utilization of the assigned carrier power of the station

Gearing tubes to circuits

How a tube acts in a circuit depends, of course, upon the impedances which face it in the circuit. So getting the most out of tubes is a matter of getting the right impedances.

Like pre-Doherty linear amplifiers, the Doherty High Efficiency Amplifier Circuit has two tubes. Unlike them, it has a network which automatically changes impedances to best meet changing needs. Both tubes receive the signal, but — when the carrier alone is on — only one tube is operative. The second tube uses no power. Not until modulation is applied, raising the input voltages on both tubes, does the second tube start up. It then does two things: it contributes more power to meet the added load, and it automatically changes the impedance faced by the first tube so as to throttle it up to full output, too.

For the Broadcaster, this means that the Doherty Circuit consumes only half the power required by old style linear amplifiers — a real triumph in circuit engineering.

It is just one of many Bell Telephone Laboratories developments which have contributed to improved efficiency, greater economy and higher quality in communications.
The 5 KW AM transmitter, like the 1KW and 50 KW, has the famous Doherty Circuit. Eleven years of experience proves this High Efficiency amplifier operates continuously for long periods with no need for retuning.

**ONLY Western Electric**

**AM broadcast transmitters have the Doherty Circuit**

1KW...5KW...50KW

Today the Doherty Circuit is being used by hundreds of broadcast stations—making possible the use of smaller circuit elements, saving space, giving increased stability and greater ease of adjustment, and reducing the outlay for auxiliary equipment.

**Other features**

In Western Electric 1, 5 and 50 KW AM transmitters, you also get two other famous Bell Laboratories developments—stabilized feedback and grid bias modulation. These, together with the Doherty Circuit, are your assurance of superlative performance at rock-bottom operating cost!

**Get full details**

If you’re thinking about a new AM transmitter, remember this: **only Western Electric has the Doherty High Efficiency Circuit**—unmatched today in performance, dependability, and economy! For full details, call your local Graybar Broadcast Representative or write Graybar Electric Co., 420 Lexington Ave., New York 17, N. Y.

*Western Electric*

Manufacturing unit of the Bell System and the nation’s largest producer of communications equipment.

*Quality Counts*
How up-to-the-minute engineering at Sonora Radio uses Centralab Couplate to improve manufacturing efficiency, and reduce servicing.

Sonora engineers take advantage of Couplate’s long life, high efficiency, mechanical strength and resistance to humidity. Result: more dependable performance, simplified production for Sonora Radios.

*Centralab’s revolutionary Printed Electronic Circuit — Industry's newest method for stepping-up manufacturing efficiency!

Yes, and Sonora is just one of the many famous radio manufacturers who are designing Centralab’s revolutionary printed interstage coupling plate into their 1948 sets.

The reason? One look at Couplate’s design and manufacturing advantages gives you the answer. 1) Couplate requires only four soldered connections instead of eight, simplifies wiring and production. 2) Couplate saves space and mass weight, makes possible more compact and dependable finished equipment at lower cost. 3) Couplate improves set performance by lengthening life, gives you a complete “printed” interstage coupling circuit engineered and manufactured by Centralab.

First commercial application of the “printed electronic circuit”, Centralab’s Couplate is a complete interstage coupling circuit which combines into one compact unit the plate load resistor, the grid resistor, the plate by-pass capacitor and the coupling capacitor. For all the facts on how Couplate can simplify your production problems and cut your costs, see Centralab’s local representative, or write for Bulletin 943.

**PROGRESS REPORT ON P.E.C.*

Integral Ceramic Construction: Each Couplate is an integral assembly of Hi-Kap capacitors and resistors closely bonded to a steatite ceramic plate and mutually connected by means of metallic silver paths “printed” on the base plate. Note schematic diagram below.

Chassis courtesy of Sonora Radio and Television Corporation

**ACTUAL SIZE**

Division of GLOBE-UNION INC., Milwaukee

PROCEEDINGS OF THE I.R.E. February, 1948
For Truly Fine
Recording and Reproduction

Professional Recordists Use—
Professional Recordists Recommend—

THE NEWLY EXPANDED LINE of Audiopoints now covers the full range of recording and playback needs. There are Audiopoints that fully meet the requirements of the most exacting professional recordists. There are also Audiopoints which these engineers unhesitatingly recommend to the non-professional and the general public.

RECORDING AUDIOPINOS


Sapphire #202. A fine quality brass shank stylus, ideally suited for those recordists not requiring the super quality of Sapphire Audiopoint #14.

List price $5.25.

Stellite #34. Favorite with many professional and non-professional recordists. Though moderately priced, it is the very best stellite stylus produced.

List price $1.75.

Diamond-Lapped Steel #50. Most practical stylus for home recordists when "first cost" is important. Being diamond-lapped, it cuts a quiet, shiny groove.

List price 3 for $1.00.

PLAYBACK AUDIOPINOS

Sapphire #113. Materials, workmanship and design make this playback point the finest made for original recordings and vinyl transcriptions. For years the outstanding choice of professional recordists.

List price $6.50.

"Red Circle" Sapphire #103. With straight dural shank and fine polished jewel point. Excellent for original recordings, vinyl pressings and phonograph records.

List price $2.00.

"Red Circle" Sapphire #203. Bent dural shank sapphire needle that is tops for phonograph records. For the first time a phonograph needle with a reshaping feature.

List price $2.00.

Steel Transcription Needle #151. The ideal all-purpose transcription needle for original recordings, vinyl pressings and phonograph records. Quality performance is assured since each point undergoes a shadowgraph test.

List price 20 for 25c

Write for new dealer discounts and our folder "Audiopoints."


Audiopoints are a product of the manufacturers of Audiodiscs.

AUDIO DEVICES, INC., 444 Madison Ave., New York 22, N. Y.
Arnold's business is permanent magnets, exclusively—a field to which we have contributed much of the pioneering and development, and in which we have set peak standards for quality and uniformity of product.

Our service to users of permanent magnets starts at the design level and carries on to finish-ground and tested units, ready for your installation. It embraces all Alnico grades and other types of permanent magnet materials—any size or shape—and any magnetic or mechanical requirement, no matter how exacting.

Let us show you the latest developments in permanent magnets, and how Arnold products can step up efficiency and reduce costs in your magnet applications. Call for an Arnold engineer, or check with any Allegheny Ludlum representative.
"FREQUENCY-RATED"
for easy selection and top performance

Now, for the first time, you can select a plate choke for a particular frequency and know that it will give excellent performance at this frequency. The Ohmite line of plate chokes are "frequency-rated"—their frequency characteristics have been accurately predetermined. The chart below gives the operating frequency range for each of the seven sizes.

Ohmite single-layer wound, r.f. plate chokes cover the entire frequency range of 3 to 520 megacycles. These chokes are wound on low power factor plastic or steatite cores, and are insulated and protected by a moistureproof coating. All chokes are rated 1000 ma except the Z-14 and Z-28, which are rated at 600 ma. Further information will be supplied upon request.

**RECOMMENDED OPERATING FREQUENCY RANGES OF OHMITE R.F. PLATE CHOKES**

---

WRITE FOR PLATE CHOKE BULLETIN No. 133.

OHMITE MANUFACTURING COMPANY
4860 Flournoy St.,
Chicago 44, Ill.

Be Right with... OHMITE

RHEOSTATS - RESISTORS - TAP SWITCHES - CHOKEs
The Clinic that Cures Radio Noise

For every evil under the sun, there is a remedy or there is none.

Old Eng. Prov.

For radio noise, the remedy is Filterizing by Tobe ... a complete service that enables you to guarantee that your electrical products will not interfere with radio reception. Filterizing by Tobe covers these three important aspects of every radio noise problem:

R.F. Circuit Design — Engineers with many years experience, thoroughly versed in measurement techniques, and using the latest instruments, determine the radio noise output and r-f characteristics of your product and specify the correct circuit elements to stop radio interference over the desired frequency range.

Electrical Design — The filterizing circuit is checked for effect upon performance of the apparatus being Filterized and all components are selected so that normal performance is obtained after Filterizing; voltage drop, temperature rise, phase relationships — all are held within required limits.

Mechanical Design — The arrangement of circuit elements is co-ordinated with existing space limitations so that radio noise is quelled without need for extensive re-design of the apparatus.

These three design factors, embodied in every Tobe Filterette, are based on exact, scientific knowledge and, when applied by Tobe engineers, enable you to guarantee radio silence for your electrical apparatus. This guarantee, shown by the FILTERIZED label, helps build sales for your product. Ask us for details.

Tobe Deutschmann Corporation • Norwood, Massachusetts
The old saying about mighty oaks and little acorns
sums up the story of El-Menco Capacitors and their record in the
radio and electronic industry. Constantly chosen as components for
the world's finest electrical equipment... El-Menco Capacitors
contribute immeasurably to product performance.

Put the dependability into your product that will establish it as a
leader in its field... put El-Menco Capacitors to work for you!

Send for samples and complete specifications. Foreign Radio and
Electronic Manufacturers communicate direct with our Export Depart-
ment at Willimantic, Conn., for information.

Manufacturers
Our silver mica department is now produ-
cing silvered mica films for all electronic
applications. Send us your specifications.
Here are the 11 new -hp- instruments — developed, announced, and put into production since the war's end. Each fills a definite need. Each is the product of painstaking research and advanced manufacturing methods. Each helps make simpler, easier, the measurement problems of the electronics industry.

Brief specifications appear here. For complete details on these and other -hp- laboratory instruments, write or wire today!

Hewlett-Packard Company
1513 Page Mill Road • Palo Alto, California

PROGRESS REPORT

1. 201B AUDIO OSCILLATOR

Meets every requirement for speed, accuracy, wave-form purity, ease of operation in FM and other fields where high fidelity is most important. Provides 3 watts output into 600 ohm resistive load. Distortion held to 1% or less at 3 watts, 1/2% at 1 watt output. Excels in testing high fidelity amplifiers, speakers, and in comparing frequencies. Output controlled by volume control ahead of amplifier, or attenuator controlling amplifier output. Attenuation approximately linear from 0 db to 40 db.

2. 410A VACUUM TUBE VOLTmeter

This -hp- voltimeter employs a special -hp- diode probe which places a low capacity of approximately 1.3 uuf across circuit under test. Combination of this low capacity and high input resistance results in great measuring accuracy without detuning or danger of loading circuit. Frequency response is 3.1 db throughout the instrument's range. Six voltage ranges provide full-scale sensitivities from 1 to 300 volts. Besides covering frequencies from 20 cps to 700 mc as an a-c voltmeter, this -hp- 410A is a d-c voltmeter with 100 megohms input impedance. It is also a precision ohmmeter for resistances, 0.2 ohms to 500 megohms.

3. 330B DISTORTION ANALYZER

-hp-’s newest and finest distortion measuring instrument. Unusually valuable for the measurement throughout the audio spectrum in broadcast, laboratory or production problems. Measures average value of “total” distortion at any frequency from 20 cps to 20,000 cps. Accurately makes noise measurements as small as 100 microvolts. Linear r-f detector makes possible measurement direct from modulated r-f carrier. As voltmeter, measures voltage level, power output, amplifier gain; or serves as high-gain wide-band stabilized amplifier with maximum gain of 75 db.

THESE -hp- REPRESENTATIVES ARE AT YOUR SERVICE

CHICAGO 6, ILL.: Alfred Crossley, 549 W. Randolph St., State 7444 • HOLLYWOOD 46, CALIF.: Norman B. Neely Enterprises, 7422 Melrose Ave., Whitney 1147
HIGH POINT, N. C.: Bivins & Caldwell, 134 W. Commerce St., High Point 3673 • NEW YORK 7, N. Y.: Burlington Associates Ltd., 11 Park Place, Worth 2-2171
DENVER 10, COLO.: Ronald G. Bowen, 1886 S. Humboldt St., Spruce 9368 • TORONTO 1, CANADA: Atlas Radio Corp., Ltd., 560 King St. West, Waverley 4761
DALLAS 5, TEXAS: Earl W. Lipscomb, 4433 Stanford Street, Logan 6-5097
450A WIDE BAND AMPLIFIER

Here is a new, wide-band instrument for laboratory or production use. Provides exceptional stability at 40 or 20 db gain. Gives freedom from spurious responses. Low phase shift assured by straightforward, resistance-coupled amplifier design, together with inverse feedback. Frequency response flat within 1/2 db between 10 and 1,000,000 cps. Varying tube voltages or aging tubes have no appreciable effect on gain or other characteristics. When used with -hp- 400A Vacuum Tube Voltmeter, increases voltmeter's sensitivity to 100 times. Increases bridge and recorder sensitivity.

710A POWER SUPPLY

Light, compact, inexpensive, this -hp- power supply is an excellent all-around source of d-c power. It replaces batteries for temporary setups, or serves as permanent installation. Output varies approximately 1% with changes in load current to 75 ma or normal line variations. Noise and hum level exceptionally low. Output unusually stable over long periods of time. Instrument also contains auxiliary center-tapped 6.3 volt source providing 5 amperes a-c. Output is continuously variable, 180 to 360 volts, and is practically independent of either line voltage or applied load.

610A UHF SIGNAL GENERATOR

This new -hp- generator is an extremely stable general-use laboratory standard for measurements between 500 and 1350 mc. Throughout those frequencies, it gives accurately known voltages ranging from 0.1 microvolt to 0.1 volt. R-f output may be continuous, amplitude modulated, pulsed or square-wave modulated. Pulse length can be controlled between 2 and 50 microseconds. Pulse rate is variable 60 to 3000 times per second. Instrument is particularly valuable for determining gain or alignment, antenna data, standing wave ratios, signal-to-noise ratios or circuit "Q."

202B LOW FREQUENCY OSCILLATOR

This newest -hp- oscillator gives maximum speed and accuracy for tests between 1/2 and 1000 cps. Particularly designed to test performance of electro-cardiograph and electro-encephalograph equipment, check vibration or stability of mechanical systems, simulate mechanical phenomena, check geophysical equipment. Throughout frequency range provides excellent wave form. Frequency stability within 5%, including initial warm-up drift. Output is 10 volts maximum into 1000 ohm resistive load. Four frequency ranges. Cps read direct on large illuminated dial. Tuning is controlled by direct or 6 to 1 micro-drive vernier.

650A WIDE BAND OSCILLATOR

Continuous frequency coverage 10 cps to 10 mc, is provided in this stable, new -hp- oscillator. Output is flat within 1 db. Voltages available range from 6000 to 3 volts. 94" scale-length, 6 to 1 micro-controlled tuning drive, 50 db output attenuator variable in 10 db steps. Output voltage divider provides 6 ohm internal impedance. -hp- 650A is specially designed for testing television amplifiers, wide-band systems, tuned circuits, receiver alignments, and checking filter transmission characteristics. And, this precision-built -hp- oscillator serves admirably as a power source for bridge measurements or as a signal generator modulator.

616A UHF SIGNAL GENERATOR

Here for the first time is a precision instrument making possible fast, direct output and frequency readings between 1800 to 4000 mc, plus simplified controls and a choice of c.w., pulsed, delayed or limited sweep output. No calibration charts are necessary. R-f output ranging from 0.2 volt to 0.1 microvolt is available. Output continuous, pulsed or frequency modulated at power supply frequency. Wide selection of pulse rates, internal and external synchronization. Stability approximately 0.005% per degree centigrade change of ambient temperature.

-hp- 335B FM MONITOR

This new -hp- 335B is the finest FM monitor ever developed. Requires no attention during operation. Provides continuous measurement of carrier frequency and modulation swing. Approved by F.C.C. for FM broadcast service. Frequency range 88 to 108 mc. Audio output has less than 0.25% residual distortion. Audio output supplied with 75 microsecond de-emphasis circuit, flat within 1/2 db of standard curve, 20 cps to 20 kc. Residual noise and hum in audio output at least 75 db below 100% modulation. Modulation may be monitored at control console or other remote point.

AUDIO SIGNAL GENERATOR -hp- 206A

Here is a source of continuously variable audio frequency having total distortion of less than 0.1%. High stability, frequency stability 0.01%, flat within 0.2 db beyond output meter. Output impedances are 50, 150 and 600 ohms. Instrument provides continuously variable frequency range 20 cps to 20 kc, tunable through 3 bands with a 47" micro-controlled dial. Precision attenuators vary output signal level in 0.1 db steps over 111 db range. Both -hp- 206A generator and -hp- 335B Frequency Modulation Monitor can be supplied in special colors to match transmitter installations.
In Step with Electronic Progress . . .
Modern Hermetically Sealed Instruments

Progressive manufacturers of electronic equipment declare an hermetic seal is as important in a meter as it is in any other product component. That's because meters are just as susceptible to the harmful effects of dust, moisture, corrosive fumes and other destructive factors as resistors, capacitors or transformers.

Therefore, hermetically sealed meters are a "must" in achieving top product performance.

MARION HERMETICS ARE NOT PREMIUM PRICED
Marion glass-to-metal hermetically sealed meters offer you the accuracy, superiority and extended life of an hermetically sealed component at a price no higher than most competitive unsealed instruments. All Marion hermetically sealed instruments are 100% GUARANTEED.

LOOK AT THE FEATURES OF MARION "HERMETICS"

DURABLE
SHIELDED
INTER-CHANGEABLE
MARION "4 for 1" FEATURE

... Unaffected by extremes of heat or cold . . . permanently protected against dust, dirt, moisture . . . instrument malfunction minimized.

... Heavy steel case gives magnetic and electrostatic shielding so important in modern high frequency equipment.

... The Marion case, with its high conductivity plating, eliminates the need for separate shielding and permits interchangeability on any type panel without affecting calibration.

Interchangeable Round and Square Colored Flanges . . . one instrument can thus fill four different needs:
1. Round
2. Round for Steel Panel
3. Rectangular
4. Rectangular for Steel Panel

WRITE FOR FURTHER INFORMATION.
NOW... RF HEATING TUBES DESIGNED and PROCESSED ESPECIALLY FOR RF HEATING PURPOSES

To Machlett Laboratories the tube needs of the RF heating industry have been a challenge—no less than they have been a source of deep concern to the industry itself. The electronic heating industry has now grown to such importance as to require—and merit—the best the electron tube industry can produce...and here the "best" must mean tubes designed and processed especially for its needs, not "hand-me-downs," no matter how high in quality, from communications or other fields.

For this reason...

MACCCHLETT LABORATORIES
are Privileged to Announce

t heir initial step in a planned program

to provide the RF heating industry

for the first time

with a line of tubes designed, processed,

and serviced exclusively

for its use

Machlett Laboratories' announcement several months ago of RF Heating Tube Types ML-5604 and ML-5619 constituted the first tangible recognition by the tube industry of the special requirements of the electronic heating field. These tubes, featuring above all else an unquestioned ability to handle—without penalty to life or performance—the most severe load mismatching and the unusual physical conditions inherent in industrial service, marked the beginning of a new concept of service to this growing industry. Unmatched in mechanical ruggedness, they embody materially heavier sections, sturdier grid, cathode and terminal construction, and principles of tube design and processing which assure better performance and longer life.

These same principles are now embodied in five new tubes—ML-5658, ML-5666, ML-5667, ML-5668 and ML-5669. Thus there is now available—for the first time—for both initial installation and for replacement, for all induction and dielectric heating purposes from 5 to 30 kW, a selection of tubes, each of which is custom-made for the job it has to do.

Machlett RF Heating Tubes will be supplied—where desired—with scientifically-designed terminal connectors affixed to the tubes at the factory. Flexible leads will be permanently attached in lengths to meet equipment manufacturers' requirements.

To the RF Heating Equipment manufacturer these Machlett electron tubes and accessories will provide the first real freedom from "tube worries" and assure user satisfaction. They will contribute to demonstrating the effectiveness and economy of electronic heating. Priced only slightly higher than the standard communication tubes generally sold for this purpose, they will prove lowest in cost through better performance and materially longer life.

Write for complete technical data on this new line of tubes and accessories. A Machlett Application Engineer will gladly visit you at your request.

MACCHLETT LABORATORIES, INC.
Springdale, Connecticut

ML-5619 RF HEATING TRIODE, water cooled with automatic seal jacket, or for forced-air cooling (ML-5604).

- Maximum Input ... 32.5 kW
- Maximum Plate Dissipation (ML-5619) ... 20 kW
- Maximum Plate Dissipation (ML-5604) ... 10 kW

ML-5658 RF HEATING TRIODE

- Maximum Input ... 60 kW
- Maximum Plate Dissipation ... 20 kW
  (Will replace Type 592 without equipment modifications)
- Automatic seal water jacket as shown.

ML-5667 FORCED-AIR COOLED TRIODE, available for water cooling ML-5666, with automatic seal jacket.

- Maximum Input ... 20 kW
- Maximum Plate Dissipation (ML-5667) ... 7.5 kW
- Maximum Plate Dissipation (ML-5666) ... 12.5 kW
  (Will replace Types 599R and 599RA without equipment modifications)

ML-5668 WATER-COOLED RF HEATING TRIODE, available with automatic seal jacket.

- Maximum Input ... 28 kW
- Maximum Plate Dissipation ... 20 kW
  (Will replace Types 592 and 592R for ML-5667 without equipment modifications)
The story’s out . . . Pyrovac, a new Eimac plate material, is now in standard production—at no extra cost.

Pyrovac is truly a milestone in vacuum tube development as the thoriated tungsten filament. Pyrovac plates, like the thoriated tungsten filament, open a new vista for vacuum tube performance.

This new material combines the advantages of tantalum to overloads, molybdenum’s strength, weight and conductivity, and carbon’s ability to dissipate heat . . . with none of the disadvantages of these materials. Tubes with Pyrovac plates are mechanically rugged, require no additional getters and they do not gas even under extreme overloads.

The life span of tubes with Pyrovac plates far exceeds that of tubes incorporating plates of conventional materials. For example, under conditions where a tube gave 3000 hours of service the same tube type with a Pyrovac plate gave 15,000 hours of life, a 400 percent increase!

Pyrovac plates are capable of handling overloads in excess of 1000%. For instance, the 4-65A plate pictured above was radiating 900 watts of heat, a 1280% overload . . . without indication that the eventual life of the tube or its characteristics were affected. We don’t suggest you dissipate 900 watts of heat in your Eimac 4-65A’s (you could probably do it), but this example establishes proof that Pyrovac is a superior plate material destined to become the anode standard of the vacuum tube industry.

Pyrovac plates were first incorporated in the Eimac 4-250A in the early part of 1946 and followed in the 4-125A. As a result there has been universal acceptance of these tubes in all fields of electronic endeavor . . . Further proof of the superiority of this new plate material. In the ensuing period of time all Eimac internal anode type tubes have been converted to Pyrovac plates as rapidly as production facilities would allow.

For your assurance to obtain the most in performance and satisfaction for your vacuum-tube-dollar, insist on Eimac tubes . . . the criterion of good design in any electronic equipment.
THESE SHERRON SCIENTISTS IN THIS ELECTRONICS LABORATORY CAN HELP WITH YOUR TECHNICAL AND INDUSTRIAL PROBLEMS!

Nerve center of the full-scope Sherron operation is the Sherron electronics laboratory.

Here we initiate all the impulses that are eventually translated into design, development and engineering. It is in every way a complete laboratory. Complete in the quality of its facilities... up-to-the-minute equipment and apparatus throughout. Complete, too, in the character of its personnel... physicists, engineers, technicians steeped in the mysteries and mutations of electronics.

As an organizational group, they'll show you some pretty effective trouble-shooting. Just set them loose on any industrial and technical bugaboo that's got you up a tree... Confidential, of course — our laboratory service is for manufacturers only.

DESIGN, RESEARCH, DEVELOPMENT AND ENGINEERING OF "PRECISION ELECTRONICS" EQUIPMENT.

A: Custom Built, Vacuum Tube Test Equipment for receiving, transmitting, Cathode-ray and small power tubes.

B: Television Transmitters and Test Equipment designed and developed to individual specifications.

C: Research and Development in The Field Of:
   1. Instrumentation.
   2. Vacuum Tube Circuit Development.
   3. Control of Measuring Devices.
   4. Electronic Control Equipment.

D: Electron Ballistics

E: Thermionic Emission

F: Electron Optics

SHERRON ELECTRONICS CO.
Division of Sherron Metallic Corporation
1201 FLUSHING AVENUE • BROOKLYN 6, N. Y.
The ALLEN-BRADLEY LINE of RADIO RESISTORS
—not affected by heat, cold, moisture, or age

Bradleyunit resistors are small in size but "taps" in load and life tests. Under continuous 100% load for 1000 hours, the resistance change is less than 5%.

The leads are differentially tempered to prevent sharp bends near the resistor. Leads are easily formed to fit any spot.

Bradleyunits are packed in handy, honeycomb cartons that keep the leads straight. When resistors are kept loose in pans they are hard to pick up. Leads become bent and tangled, and assemblers lose time.

Bradleyunits are made in 3/8-watt and 2-watt sizes in standard R.M.A. values from 10 ohms to 22 megohms. One-watt Bradleyunits are available in values from 2.7 ohms to 22 megohms.

The heart of the Type J Bradleyometer is the solid-molded resistor element. It is a thick ring, molded to provide any resistance-rotation curve. After molding, heat, cold, moisture, or hard use cannot affect it.

The resistor element is molded as a single unit with insulation, terminals, face plate, and threaded bushing in ONE piece. There are no rivets nor welded nor soldered connections. It is rated at 2 watts with a big safety factor; can be furnished with line switch, if desired, and with any shaft extension.

Type J Bradleyometers can be obtained in single, dual, or triple unit constructions. The Type JW Bradleyometer is a watertight unit for special weatherproof control applications.

The handy honeycomb cartons prevent leads from tangling and save time.

SIZES OF UNITS

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Allen-Bradley Co., 114 W. Greenfield Ave., Milwaukee 4, Wis.
Large or small, one or a million, AlSiMag technical ceramics are custom made in the composition with the correct physical characteristics for your application. On request AlSiMag engineers will be glad to help you find the best design and composition for your requirements.

46th YEAR OF CERAMIC LEADERSHIP

AMERICAN LAVA CORPORATION
CHATTANOOGA 5, TENNESSEE
This Nobatron is being used to test battery operated Movietone News cameras. Nobatrons provide a source of DC voltages at high currents previously available only with batteries. The Nobatron maintains a regulation accuracy of 0.25%, ripple voltage (RMS max) of 1% and has a recovery time of 1/5 of a second.

Write today for your copy of the new Sorensen catalog. It contains schematics, curves, application data and a special section on "Principles of Operation."

• Represented in all domestic and foreign principal cities.

Address of Sorensen office in your area furnished on request.

Wherever you use line voltage for precision operations, whether it be in the test laboratory or on the assembly line, a Sorensen unit can provide regulation accuracies to 2/10 of 1% with quick recovery time.

Arrange to have a Sorensen engineer analyze voltage regulation requirements in your plant. He can select one of the standard units or suggest a special design to handle your unusual applications.

Take a look at this Performance!

1. Wide input voltage range: 95 to 125 volts or 190 to 250 volts.
2. Low harmonic distortion: less than 5% in basic models, and 2% in "S" models.
3. Insensitive to input line frequencies between 50 and 60 cycles.
4. Power factor variations from 70% lagging to 90% leading have little effect on regulation accuracy.
5. Recovery time of 0.1 seconds under the most adverse input and load conditions.
6. Regulation accuracies from 0.1% to 0.5% depending upon model chosen.

The FIRST line of standard ELECTRONIC AC Voltage Regulators and Nobatrons

SORENSEN
& COMPANY, INC. • STAMFORD, CONNECTICUT

PROCEEDINGS OF THE I.R.E. February, 1948
Operating Room Gauze Is Not Pure Enough

For This MALLORY CAPACITOR!

The chloride content of the gauze used in making Mallory FP Capacitors is less than one-half of one part per million! To accomplish this, Mallory demands more thorough purification than is required for the gauze used in hospitals!

Purity for Longer Shelf-Life

Due principally to this precaution, Mallory FP Capacitors stubbornly resist deterioration on the shelf or in storage. Cases are on record where Mallory Capacitors have proved ready for use without re-aging after more than six years in storage.

Useful in Television and FM Sets

FP Capacitors are ideal for vertical mounting and contain the famous Mallory "Fabricated Plate" anodes. They give equivalent capacity and voltage in less space. Their pure internal construction and tightly sealed cases make them ideal for tropical use.

Buy Mallory Assured Quality at Regular Price Levels

Yours for the asking!

Send for the Mallory Capacitor Catalog, which contains useful data on all types of Mallory Capacitors—sizes, electrical characteristics, test measurements, mounting hardware.
Problems encountered in the manufacture and erection of home antennas for television and FM receivers are most easily solved by using Revere Aluminum Tube. Note these features:

**Strength.** Revere 61S-T6* Aluminum has high strength for masts. Typical properties are 40,000 p.s.i. yield strength and 45,000 p.s.i. tensile strength.

**Workability.** Revere 61S-T4* Aluminum can be easily bent if desired for the formation of dipoles. Both this and 61S-T6* are easily cut, drilled, and threaded. Typical properties of 61S-T4* are 21,000 p.s.i. yield and 35,000 p.s.i. tensile.

**Lightness.** Aluminum tube, being only about one-third the weight of steel, reduces transportation charges and facilitates installation work.

**Beauty.** Aluminum can be anodized and given almost any desired color. Most people, however, prefer it in its silvery beauty without adornment.

Revere Aluminum Tube is available in practically any size that might be required, and thus each design can be engineered to its own requirements. Revere and any Revere distributor will gladly quote you prices and delivery dates on your requirements. The Revere Technical Advisory Service will cooperate with you on technical matters concerning the use of aluminum tube or any other Revere Metal. Revere supplies the radio industry with many non-ferrous metals and alloys, in such forms as tube and pipe, rod and bar, sheet and plate, extruded shapes and forgings.

---

RCA Television and FM receiving antenna, using Revere Aluminum Tube

*These are new temper designations effective January 1, 1948. Formerly 61S-T6 was designated 61S-T and 61S-T4 was 61S-W.
Accurate performance of your product is limited by the precision of its component parts. It is only through selection of precision components that superior performance can be assured. Hi-Q Ceramic Capacitors, for example, can be held to a minimum tolerance of .25 MMF. Constant surveillance throughout every stage of manufacture ... from raw material to finished product ... is responsible for this uniformly high quality of all Hi-Q components. Specify Hi-Q components ... your assurance of precision performance.

Hi-Q COMPONENTS BETTER 4 WAYS

- Precision: Tested step by step from raw material to finished product. Accuracy guaranteed to your specified tolerance.
- Uniformity: Constancy of quality is maintained over entire production through continuous manufacturing controls.
- Dependability: Satisfaction ... year after year of trouble-free performance. Our Hi-Q makes your product better.
- Space Saving: The smallest BIG VALUE components in the business make possible space saving factors which reduce your production cost ... increase your profits.

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FRANKLINVILLE, N.Y.

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PRECISION standards are set in the laboratory.
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the finest ELECTRICAL CONNECTORS
money can build or buy!

SHELL
High strength aluminum alloy... High resistance to corrosion... with surface finish.

CONTACTS
High current capacity... Low voltage drop.

SCINFLEX ONE-PIECE INSERT
High dielectric strength... High arc resistance.

AND THE SECRET IS SCINFLEX!

Bendix-Scintilla* Electrical Connectors are precision-built to render peak efficiency day-in and day-out even under difficult operating conditions. The use of "Scinflex" dielectric material, a new Bendix-Scintilla development of outstanding stability, makes them vibration-proof, moisture-proof, pressure-tight, and increases flashover and creepage distances. In temperature extremes, from -67° F. to +300° F., performance is remarkable. Dielectric strength is never less than 300 volts per mil.

The contacts, made of the finest materials, carry maximum currents with the lowest voltage drop known to the industry. Bendix-Scintilla Connectors have fewer parts than any other connector on the market—an exclusive feature that means lower maintenance cost and better performance.

*REG. U.S. PAT. OFF.

Write our Sales Department for detailed information.

- Moisture-proof, Pressure-tight
- Radio Quiet
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- Vibration-proof
- Light Weight
- High Arc Resistance
- Easy Assembly and Disassembly
- Less parts than any other Connector

Available in all Standard A.N. Contact Configurations

SCINTILLA MAGNETO
SIDNEY, N. Y.
DIVISION OF
BENDIX SCINTILLA

News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

Automatic Scaling Unit

A new scaling device for use with Geiger-Muller counters in radioactivity research has been announced by Instrument Development Laboratories, 223 West Erie St., Chicago 10, III. Known as Model 163, it incorporates facilities for predetermined count and predetermined time operation, in addition to the basic functions which were found in the older model.

This new scaler operates on impulses from a Geiger-Muller tube and actuates a register once for each group of impulses it receives. Scaling factors of 2, 16, 32, or 64 can be used when desired.

A new switch allows the selection of 10, 100, or 1000 times the selected scaling factor for any predetermined count. The scaler will automatically shut off after this predetermined number of counts has been recorded, up to a maximum of 64,000, and will indicate the time required for these counts if connected to an electric timer.

Mega-Marker

The Kay Electric Co., 34 Marshall St., Newark N. J. has announced the Mega-Marker which is a precision variable marker-oscillator which covers a range of 19 to 29 Mc. for the television i.f. band. For the f.m. i.f. band (10.7 Mc.) a crystal oscillator is incorporated.

Accuracies of 0.02 Mc. may be read off because more than 12 inches of calibrated scale length is provided on the dial.

The Mega-Marker is a valuable accessory for f.m. and television applications of the Mega-Sweep sweeping oscillator, and the Mega-Match for measuring reflected energy.

(Continued on page 38A)
Without CONSTANT VOLTAGE protection, this self-sustaining link in the chain of relay points that chart the nation’s airways, could not successfully perform its safety function.

It is remotely located, at times almost inaccessible to service personnel and solely dependent on local power service. Were it not for a SOLA Constant Voltage Transformer, its delicately engineered electronic and radio equipment would be constantly at the mercy of periodic and unpredictable surges or low voltage levels.

Throughout the entire cross-country system SOLA Constant Voltage Transformers maintain operating voltages at a constant, predetermined level and the nation’s air-men fly their courses with confidence.

If you are building electrically energized equipment to operate at precise voltage levels, remember this: it is more economical to include Constant Voltage protection in your design than to install it later as a remedial measure.

Revised Bulletin KCV-102 available on request. Write for your copy.

31 standard types of SOLA Constant Voltage Transformers available in capacities ranging from 10VA to 15 KVA.

SOLA

Transformers for: Constant Voltage • Cold Cathode Lighting • Airport Lighting • Series Lighting • Fluorescent Lighting • Luminous Tube Signs • Oil Burner Ignition • X-Ray • Power • Controls • Signal Systems • etc. • SOLA ELECTRIC COMPANY, 4633 W. 16th Street, Chicago 50, Illinois

Manufactured under license by: ENDURANCE ELECTRIC CO., Concord West, N. S. W., Australia • ADVANCE COMPONENTS LTD., Walthamstow, E., England • UCOA RADIO, Buenos Aires, Argentina • M. C. B. & VERITABLE ALTER, Courbevoie (Seine), France

PROCEEDINGS OF THE I.R.E. February, 1948 23A
When projection lenses are available, you can project the oscillogram in a well-lighted room with perfect visibility, as in this unretouched photograph. Note open window.

When projection lenses are available, you can project the oscillogram in a well-lighted room with perfect visibility, as in this unretouched photograph. Note open window.

Photographs, projections, high-speed transients are clear if it's a Du Mont Type 247-A Cathode-Ray Oscillograph.

Modified from the Type 247, this new Du Mont Type 247-A is such a startling success that phenomena hitherto totally invisible can now be easily seen. Such modification extends the range of the instrument tremendously in the field of transient studies or high-speed photographic applications.

The modification utilizes the new Type 5RP Cathode-Ray Tube operable at voltages up to 30 KV, producing sufficient brilliance for direct projection, if required.

Other features are: automatic beam blanking; choice of single or continuous sweep; sweep rates available from .5 cps to 50,000 cps; Z-axis amplifier with choice of output polarity; soundly engineered electrical and mechanical design.

Further details on request.

DuMont Precision Electronics & Television

Allen B. DuMont Laboratories, Inc., Passaic, New Jersey • Cable Address: Albeedu, Passaic, N. J., U. S. A.
Aeronautical Radio, Inc., asked the radio communications industry in 1946 for proposals on receivers and instrumentation designed to meet the very difficult specifications demanded by omnidirectional range reception and indication in an airplane. Collins, one of six companies to comply, conducted demonstrations in January, 1947, for ARINC's Radio Equipment Committee and commercial airline engineers, and for the Air Transport Association's Air Navigation Traffic Control Research Group. Collins was one of two companies whose designs were approved.

Up to the time this announcement is written, demonstrations have been made for all domestic and many foreign airlines, and orders have been received for this equipment from American, Chicago & Southern, Northwest, Pan American, United, and Peruvian International. Meanwhile, the omnidirectional radio range system is now being installed on the major United States airways, and it is expected that this system will supplement and ultimately replace the four-quadrant beam range for air navigation.

The Collins equipment includes our 51R 280-channel receiver covering 108-136 mc on a 100 kc channel basis, and the instruments shown above and summarized below. The receiver includes all modern circuit features, and provides extremely high stability and rejection of spurious signals. The engineering model of a companion vhf transmitter is now under test.

Key to illustration above
A. 51R Receiver on Shockmount
B. Control Box
C. Radial Selector
D. Deviation Indicator
E. Radio Magnetic Indicator
F. Accessory Unit (Provides mounting for 2 Radial Converter Indicators, 3 Servo Amp. for R.M.I., and 2 Power Units for 2 51R's. The photograph shows 1 Radial Converter Indicator and 1 Power Unit mounted on the Accessory Unit.)

Collins vhf Airborne Equipment

...for navigational use of the omnidirectional range

Collins Radio Company, Cedar Rapids, Iowa

Proceedings of the I.R.E. February, 1943

Collins radio company, Cedar Rapids, Iowa

11 West 42nd Street, New York 18, N. Y.

458 South Spring Street, Los Angeles 13, California
1948
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K-TRAN

You'll want to use K-TRANS this year
Get an early start!

AUTOMATIC MANUFACTURING CORPORATION
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NEWARK 4, NEW JERSEY
You can
test the paper for density...thickness
...porosity...power factor...chloride content...dielectric constant...dielectric strength.

And then test the foil for thickness...
purity...softness of the anneal...
freedom from oil...cleanliness of surface...absolute smoothness.

And then test the liquid dielectric for
specific gravity...viscosity...power factor...color...acidity...flash point...dielectric strength...dielectric constant...insulation resistance...water content.

And after that, test every single finished capacitor for shorts, grounds, and
opens at overvoltage between terminals and between terminals and case
...and measure the capacitance of every single unit...and then check every single capacitor to see that it has an air-tight, leak-proof hermetic seal.

Or you can
buy General Electric capacitors...which have already passed every one of these tests
...on the materials when they were made.
...and again before they were used.
...and on the capacitors during manufacture.
...and then, finally, on every single capacitor before shipment.

SPECIALTY CAPACITORS
General Electric makes a wide variety of specialty capacitors, all of which must pass similar comprehensive tests. For full information on types, ratings, dimensions, types of mounting, and prices, address the nearest General Electric Apparatus Office or Apparatus Department, General Electric Company, Schenectady 5, N. Y.

GENERAL ELECTRIC
A METER WON'T SHOW WHAT IT DOESN'T FEEL

A STABILINE Automatic Voltage Regulator Type IE limits waveform distortion to 3% therefore...

A meter is not affected by the negligible waveform distortion (3% maximum) of a STABILINE Automatic Voltage Regulator Type IE (Instantaneous Electronic).

Investigations by Weston Electrical Instrument Corp., as to errors due to harmonics in iron-vane a-c ammeters or voltmeters, show that waveform distortion up to 3% in 60 cycle circuits produce negligible errors not recognized in instrument readings. The results are noted in the October 1947 issue of Weston Engineering notes. Since a STABILINE Voltage Regulator Type IE has a maximum waveform distortion less than 3%, it is the ideal equipment to employ for maintaining a constant voltage to electrical apparatus.

However, negligible waveform distortion is just one of the many outstanding features of a STABILINE Automatic Voltage Regulator Type IE. The STABILINE Type IE has no moving parts and is completely electronic in operation. It delivers a constant output voltage regardless of variations in input voltage or load current. The maximum change in output voltage due to any of these variations will not exceed ±0.25 of 1%. For input changes only, the change in output voltage will not exceed ±0.1 of 1%. Speed of correction is in the order of 3 to 6 cycles.

Numerous models are available in attractive black wrinkle-finish cabinets or for relay rack mounting. Complete engineering data is contained in Bulletin 547.

Write The Superior Electric Co., 802 Meadow Street, Bristol, Connecticut

THE SUPERIOR ELECTRIC CO.
BRISTOL, CONNECTICUT

POWERSTAT VARIABLE TRANSFORMERS • VOLTBOX A-C POWER SUPPLY • STABILINE VOLTAGE REGULATORS

PROCEEDINGS OF THE I.R.E. February, 1948
You just can't beat beam power tubes for efficiency. Their low drive requirements mean less space taken up by the driving stages, and a substantial saving in power. Builders and operators of mobile-radio and other communications equipment know this; they choose beam power tubes for a clear, reliable signal with minimum drain on the battery or other source of transmitter supply.

General Electric offers a complete line of beam power (and other) tubes designed to meet the full range of power outputs and frequencies in communications work. If you are a designer or builder of apparatus, G-E tube engineers stand ready to work closely with you in selecting the right tubes for circuits on your drawing-boards.

If you are an operator of police, taxi-cab, or ambulance radio equipment—of a ship-to-shore, airport, or other communications system—same-day, often same-hour replacement service on tubes is available from your nearby G-E tube distributor or dealer.


---

**Ratings (ICAS) for typical operation, Class C plate-modulated**

<table>
<thead>
<tr>
<th>Type</th>
<th>Plate voltage</th>
<th>Plate current</th>
<th>Driving power (approx)</th>
<th>Power output (approx)</th>
<th>Freq. at max ratings</th>
</tr>
</thead>
<tbody>
<tr>
<td>GL-2E26</td>
<td>500 v</td>
<td>54 ma</td>
<td>0.15 w</td>
<td>18 w</td>
<td>125 mc</td>
</tr>
<tr>
<td>GL-807</td>
<td>600 v</td>
<td>100 ma</td>
<td>0.4 w</td>
<td>42.5 w</td>
<td>60 mc</td>
</tr>
<tr>
<td>GL-829-B</td>
<td>600 v</td>
<td>150 ma</td>
<td>0.9 w</td>
<td>70 w</td>
<td>200 mc</td>
</tr>
<tr>
<td>GL-813</td>
<td>2,000 v</td>
<td>200 ma</td>
<td>4.3 w</td>
<td>300 w</td>
<td>30 mc</td>
</tr>
</tbody>
</table>
STACKPOLE
CUP CORES

DELIVER MAXIMUM "Q"
IN MINIMUM SPACE

STACKPOLE iron powder molded cup cores are ideally suited to save valuable space and to make important contributions to high "Q" circuits. Since they are self-shielding, they can be mounted close to the chassis or any other metal part.

Stackpole offers a broad range of shapes and types—and, where required, can produce special cup cores to the most exacting specifications. Standard Stackpole iron powder molding materials include a broad range of design and permeability possibilities for practically any electronic engineering need.

Write for samples. State your specifications and probable quantities required.

IRON CORE HEADQUARTERS

Standard and high-frequency types • Iron sleeve cores
Iron screw cores • Side-molded types • High resistivity types
and many special types, shapes and sizes.

WRITE FOR ENGINEERING BULLETIN RC-78
(Complete Catalog Available Where Required)

STACKPOLE CARBON COMPANY
St. Marys, Pa.

DIMENSIONAL DRAWINGS COVERING
TYPICAL STANDARD STACKPOLE CUP CORES
SWITCHES • IRON CORES

PROCEEDINGS OF THE I.R.E.  February, 1948
RCA SPECIAL RED TUBES

Minimum life – 10,000 hours!

- These new RCA Special Red Tubes are specifically designed for those industrial and commercial applications using small-type tubes but having rigid requirements for reliability and long tube life.

As contrasted with their receiving-tube counterparts, RCA Special Red Tubes feature vastly improved life, stability, uniformity, and resistance to vibration and impact. Their unique structural design makes them capable of withstanding shocks of 100 g for extended periods. Rigid processing and inspection controls provide these tubes with a minimum life of 10,000 hours when they are operated within their specified ratings. Extreme care in manufacturing combined with precision designs account for their unusually close electrical tolerances.

RCA Application Engineers will be pleased to cooperate with you in adapting RCA Special Red Tubes to your equipment. Write RCA, Commercial Engineering, Section BR 52, Harrison, New Jersey.

THE FOUNTAINHEAD OF MODERN TUBE DEVELOPMENT IS RCA

TABLE OF RECEIVING-TYPE COUNTERPARTS

<table>
<thead>
<tr>
<th>Part Number</th>
<th>Counterpart</th>
</tr>
</thead>
<tbody>
<tr>
<td>5691</td>
<td>6SL7GT</td>
</tr>
<tr>
<td>5692</td>
<td>(0.6 A. heater)</td>
</tr>
<tr>
<td>5693</td>
<td>6SN7GT</td>
</tr>
</tbody>
</table>

RCA Special Red Tubes can be used as replacements for their counterparts in equipment where long life, rigid construction, extreme uniformity, and exceptional stability are needed.

SEND FOR FREE BULLETIN—Booklet SRT-1001 provides complete data on RCA Special Red Tubes. For your copy write to RCA, Commercial Engineering, Section BR 40, Harrison, N.J.
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(Including the WAVES AND ELECTRONS Section)  
Published Monthly by  
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Reginald L. Smith-Rose

VICE-PRESIDENT, 1948

Reginald L. Smith-Rose was born in London, England, in 1894. He received his scientific and technical education at the Imperial College of Science, London University, where he obtained his B.Sc. degree with first class honors in physics in 1914, and the diploma of the Imperial College in electrical engineering in 1915. These courses were followed by four years practical experience in the works of Messrs. Siemens Brothers, and Company, Limited, where he was engaged in experimental work on automatic telephone systems and the application of valve amplifiers to line communication.

He was one of the earliest members of the London Wireless Club in 1913. This later became the Radio Society of Great Britain, to which Dr. Smith-Rose was elected an Honorary Member in 1942. He joined the scientific staff of the National Physical Laboratory at Teddington, Middlesex, as a member of the Electricity Department in 1919, and later formed the nucleus of the Wireless Division of that department. He has been associated with the work of the Radio Research Board of the Department of Scientific and Industrial Research, London, since the formation of the Board in 1920, and he has been responsible for conducting extensive investigations in radio direction finding, the electrical properties of soil and sea water, and the propagation of radio waves over the ground and through the lower atmosphere. The results of these investigations have been described in numerous papers published in the Proceedings of the Royal and Physical Societies, the Journal of the Institution of Electrical Engineers, the Wireless Engineer, and in the official reports published by H. M. Stationery Office, England. In the course of this research work, he received the degrees of Doctor of Philosophy and Doctor of Science at London University.

In 1939, Dr. Smith-Rose was appointed superintendent of the Radio Division of the National Physical Laboratory and is responsible for both the Slough and Teddington sections of that division. He is a member of the British National Committee for Scientific Radiotelegraphy, and has attended numerous international conferences, including those of U.R.S.I. and C.C.I.R., in Brussels, Bucharest, Copenhagen, London, Paris, Rome, Venice, and Washington.

Dr. Smith-Rose is a member of the Institution of Electrical Engineers, London, was chairman of the Radio Section in 1943, and is the recipient of five Premiums for original papers read before the Institution. He was awarded the Fellowship of The Institute of Radio Engineers in 1945 "in recognition of his pioneer work in the field of direction finding and radio propagation allied to his leadership of an outstanding radio research group"; and it was during his visit to New York in the preceding year that he was instrumental in arranging a closer co-operation between the British Institution of Electrical Engineers and the I.R.E. He is a member of the Liaison Committee of the two bodies. In August 1947, he was awarded the United States Medal of Freedom with Silver Palm for exceptionally meritorious service in scientific research and development, and for his advice, experience and helpful co-operation among English and American scientists.

Dr. Smith-Rose has just been appointed to a new post as director of radio research in an enlarged organization to be established by the Department of Scientific and Industrial Research, in Great Britain.
The Engineer’s Role in Government

DONALD McNICOL

It has been demonstrated in several instances that engineers are well equipped intellectually to resolve problems of government; local, state, and national. This, because they are trained in resolving engineering problems through the procedures of analyses, blueprints, plans, and estimates. We know, of course, that being equipped to engage in an undertaking may require also knowledge peculiar to the particular undertaking if success is to be attained. There are reasons why in the past not many engineers have looked with favor upon the holding of public office.

The business of politics, which deals with the attainment of and holding of public office, unfortunately has attached to it much that is branded as sordid. Having choice, engineers are averse to being involved in unsavory surroundings. And, as is the experience of the novitiate in most callings, it is necessary for the beginner to serve in a minor capacity, and without money compensation; all of which means that serving the public contains little if any attraction for men whose waking hours appear to be already fully occupied with professional work.

However, there are arriving now new governmental and social concepts that form a background against which, perhaps, engineers’ traditional habits of thought may perforce have to undergo orientation. Engineers may not much longer safely remain on the sidelines while events on the national and international levels relentlessly intrude to confuse the capacities of provincial politicos too often thinking mainly in terms of home-town new postoffices. It may be significant that in the press one comes across declarations such as: “Scientists must quit their ivory towers and assume responsibility or stand convicted in the court of public opinion.”

In a recent address, Professor W. A. Noyes, of the American Chemical Society, said: “Present leaders of political, social and economic thought are not likely to extend to us gold-edged invitations to join them in developing the master plan for the world of tomorrow, other than to assign to us the usual role of supplying strictly scientific advances. This role we reject. Today scientists recognize that they have greater responsibilities than mere discovery, and are determined to see that what they develop for the betterment of mankind shall not be used for its destruction.”

In all of this there is immediate challenge for radio engineers.
The Visibility of Small Echoes on Radar PPI Displays

RUBY PAYNE-SCOTT†

Summary—A theory of visibility on an intensity-modulated display is developed. From it is derived a mathematical formula for visibility on a PPI display, and this formula is confirmed by experimental investigations. It is shown that, under favorable conditions, received signals whose power is 15 db below noise level can be observed. Replacement of a linear detector in the receiver by a square-law detector will, under some conditions, produce a further improvement of 3 db. In the visibility formula all the system variables have been grouped into four parameters, and thus it has been possible to provide nomograms enabling the rapid calculation of the minimum visible signal under any set of conditions.

Introduction

Detection of an object by radar depends ultimately on the ability of an observer to pick out a small change, in brightness or position, of part of the pattern on the screen of a cathode-ray tube. This ability depends on the one hand on physiological and psychological factors, and on the other, on the parameters of the whole radar system, which determine the nature of the change to be detected. In order to design systems of predictable performance or to compute the effect of any proposed change in a given system, we need to know the laws governing visibility.

A general theory of visibility for an isolated echo on an intensity-modulated display, in particular on that type known as a plan-position indicator or PPI, is developed in this paper. By making certain simplifications, this theory is put in a mathematical form enabling the least visible signal under given conditions to be calculated. The predictions of the theory have been checked on an artificial radar system and found to be generally true. Finally, a series of nomograms are provided, from which the least visible signal under any set of conditions can be read off.

Notation

\[ P_{\text{min}} = \text{minimum visible signal, in terms of available signal power at antenna output terminals (watts)} \]
\[ P_s = \text{available noise power, referred to receiver input terminals, i.e., } MKT \Delta f \text{ (watts)} \]
\[ N = \text{receiver noise factor} \]
\[ k = \text{boltzmann's constant (watts seconds}^{-1} \text{ degree}^{-1}) \]
\[ T = \text{ambient temperature (K)} \]
\[ \Delta f = \text{bandwidth at radio frequency, i.e., } (\frac{G_f^2 G_d f}{G_a} \text{where } G_f \text{ is the gain of the amplifier at frequency } f, \text{ and } G_a \text{ the gain at signal frequency (cycles per second).} \]
\[ \tau = \text{pulse duration (microseconds)} \]
\[ r = \text{pulse-repetition frequency (seconds}^{-1} \)]
\[ r_e = \text{repetition frequency beyond which noise background is always uniform for given speed of rotation} \]
\[ \theta_a = \text{antenna beamwidth in direction of scan (radians)} \]
\[ S = \text{antenna speed of rotation (revolutions per second)} \]
\[ s = \text{rate of time-base sweep (millimeters per microsecond)} \]
\[ d = \text{spot diameter along radius (millimeters)} \]
\[ \theta_s = \text{angular spot diameter along arc (radians)} \]
\[ \Phi_s = \text{angle subtended by spot at observer's eye (steradians)} \]
\[ I = \text{average brightness of noise on screen} \]
\[ \Delta I = \text{r.m.s. deviation of noise brightness from } I \]
\[ \delta I = \text{peak increment in brightness due to signal} \]
\[ (\delta I/I)_o = \text{minimum visible value of } \delta I/I \]
\[ (\Delta I/I)_o = \text{minimum visible value of } \Delta I/I \]
\[ V, \Delta V, \delta V = \text{detector output voltages corresponding to } I, \Delta I, \delta I \]
\[ n = \text{number of noise pulses averaged on PPI screen} \]
\[ n_e = \text{value of } n \text{ required to make the noise background uniform} \]
\[ k_1 = i_2 \times V_{11}, \text{where } i_2 \text{ is the beam current of the indicator tube, and } V \text{ the driving voltage on the grid} \]
\[ k_2 = V \times P_{11} \phi, \text{where } P \text{ is the input receiver power and } V \text{ the output voltage from the detector; } 2 \text{ for a linear detector and } 1 \text{ for a square-law detector.} \]
\[ a, b = \text{constants of long-persistence screen; in time } t \text{ after sweep, intensity has decayed by } (1 + at)^{-b}; \text{ for P7 screen, illuminated to about 0.02 effective foot-candles and excited once per second, } a = 0.15 \text{ second}^{-1}, b = 1.2 \]
\[ \alpha = 0 \text{ when } (r_e/d) > 2r \Delta f \text{ or background is uniform, } \frac{r}{d} \text{ otherwise} \]
\[ \beta = 1 \text{ when } r_e/d < 1, \text{ or } r_e/d > 1 \]
\[ \gamma = 1 \text{ when } \theta_a/\theta_s < 1, \text{ or } \theta_a/\theta_s > 1 \]
\[ \epsilon = 0 \text{ for uniform backgrounds, } \frac{1}{2} \text{ for discontinuous background} \]
\[ p = 2/3 \text{ when } \Phi < \Phi_1 \Phi \text{ being solid angle subtended by echo at observer.} \]

The Plan-Position Indicator—A General Theory of Visibility

In a PPI display, the receiver output intensity-modulates a trace that travels out from the center of the cathode-ray-tube screen each time the transmitter
emits a pulse. The trace at the same time rotates in synchronism with the antenna. The screen is made of long-persistence fluorescent material, so that a certain proportion of the brightness produced by the trace at any one bearing persists throughout a revolution of the antenna. Thus the area looked at by the radar is exhibited on the screen as an illuminated map centered on the radar station, any small reflecting object appearing as a bright arc at the appropriate range and bearing. When observing faint echoes, the gain of the receiver is high; so that, in addition to the echoes, there is a background illumination produced by the receiver noise.

Fig. 1 shows graphically how the PPI picture is built up. The wave forms (a) (traced from photographs in a report by Goldstein and Bates)\(^1\) are of single sweeps on a deflection-modulated or class-A display, and may be considered as graphs of the receiver output voltage against time. On each sweep there is one signal pulse, several db above the mean noise level and always occurring at the same time after the start of the sweep. The remaining peaks are due to the receiver noise. This noise originates as a series of impulses (due to Johnson noise in circuit components or shot noise in tubes) which, after passing through the r.f. amplifier, appears as a series of peaks of varying amplitude with characteristic shape. Their shape varies a little with the type of amplifier, but always shows a fast rise and slower fall; its form for an amplifier consisting of five cascaded single-tuned circuits is shown in Fig. 2. The signal pulse also changes its shape on passing through the r.f. amplifier; for a given type of amplifier, the final shape depends only on the product of receiver bandwidth and pulse duration. Fig. 2 also shows the resultant shape of an originally square pulse after passing through five cascaded single-tuned stages. A comparison of the relative shapes of pulse and impulse in Fig. 2 shows that (except when the bandwidth/pulse-duration product is large) the signal and noise pulses are not distinguishable by any difference in shape—a conclusion borne out by the traces in Fig. 1.

The receiver output is next used to intensity-modulate the beam current of the cathode-ray tube (c.r.t.), producing a beam current varying with time as shown in Fig. 1(b). The resulting variation in charge falling on the screen of the c.r.t. gives rise to a proportional variation in the light emitted by the screen. The beam at any instant illuminates a finite area of the screen, having, say, a radial length \(d\) and angular width \(\theta\) (see upper part of Fig. 1(c)). Since the time between sweeps is too short for any appreciable decay in light intensity to occur, the brightness at any point is, to a first approximation, the mean of the brightnesses produced by all the sweeps occurring in an angle \(\pm \frac{1}{2}\theta\), the brightness contributed by each sweep being in turn its average brightness over a distance \(\pm \frac{d}{2}\) on either side of the point. Fig. 1(c) shows the brightness resulting from averaging over all sweeps in an angle \(\theta\), and over a distance \(d\) along the trace; when \(d\) is less than the

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effect is large. A further integrating effect from sweep to sweep is produced by the long persistence of the screen, so that the brightness at a point is built up not only by sweeps occurring in the present revolution but also by sweeps occurring in past revolutions; this effect may be taken into account by increasing by an appropriate factor the number of sweeps integrated in the step from Fig. 1(b) to Fig. 1(c).

It is apparent that in the original receiver output (Fig. 1(a)), it is often very difficult to distinguish the signal pulse from the higher noise pulses, though its power is several decibels above the mean noise power. On the other hand, during integration (Fig. 1(c)) the signal pulse is added at the same position each time, while, owing to the random occurrence of noise peaks, they only coincide at rare intervals, so that the number of high noise peaks diminishes and the possibility of confusing these with the signal pulse correspondingly decreases. The mathematical expression of this fact is the theorem in statistics given in Appendix II. Briefly, this states that, if the individual observations have a mean value \( a \) and a standard deviation \( \sigma \), the means of \( n \) such observations also have a mean value \( a \) but their standard deviation is reduced to \( \sigma / \sqrt{n} \), for any distribution not differing too greatly from a normal distribution. The standard deviation may be taken as a measure of the number of peaks greater than a certain value, so that in the case illustrated, where integration has occurred over 10 sweeps, the number of high peaks should be reduced by more than one-third. In practice, integration may occur over some hundreds of sweeps. The integration over several noise pulses in one sweep, shown in the lower trace of Fig. 1(c), further increases the uniformity of the noise background.

As well as affecting the noise background, the spreading of the beam may affect the signal pulse. This is illustrated in the lower trace of Fig. 1(c), in which a signal pulse shorter than the spot diameter is spread out with a proportional decrease in brightness. A similar effect will occur if the beam width \( \theta_a \) is less than \( \theta_s \), so that a signal pulse only occurs on some of the integrated sweeps; the angular width of the echo will be increased from \( \theta_a \) to \( \theta_s \), with a proportional decrease in brightness.

Fig. 3 shows photographs of two PPI displays, identical except for the amount of background integration. In display (a) the background is still very grainy, while in (b) there is sufficient overlapping of pulses to produce a practically uniform background. This particular display has many defects, but the photographs illustrate the improved visibility of synchronized over random phenomena as integration increases. Not only are small echoes more easily seen on Fig. 3(b) but so are the striations (due to friction in the selsyn drive) and the dark circle (due to a negative kick from the range marker).

It is well known that there is a definite threshold limit to the ability of the eye to distinguish contrast,
recognize a particular bright patch, the signal, against an aggregate of patches of varying brightnesses due to the noise. The theory of visibility developed here is based on accepting this division, setting up criteria of visibility for each type, and then determining mathematically the way in which these criteria and the type of display depend on the system parameters.

The criteria of visibility for the uniform background are, from physiological experiments, known to be the contrast of the echo against the background (δI/I), the area of the echo, and the background brightness. Experiments on visibility under conditions somewhat resembling ours were made by Langmuir and Westendorp. A white screen 1.5 meters square could be illuminated at any brightness from that of moonlight (0.023 effective foot-candles (e.f.c.)) down to zero. This maximum brightness is of the order of that used in a PPI display. In the screen were holes of various areas that could be illuminated to any brightness by flashing lamps on and off. From the data given in their paper we have computed the curve of Fig. 4; in this the contrast (δI/I), important for the following reasons. Langmuir and Westendorp found that decreasing background brightness increased the visibility for a given contrast when they used very small screens; other observers using larger sources and higher background brightness have found the opposite to hold; the size of source and brightness used in PPI displays are about intermediate between these two extremes. In a PPI display the operator is usually allowed to adjust brightness to suit himself, and it is found that the optimum appears to be very flat. It was hence concluded that brightness can be excluded as an important parameter affecting visibility, so long as adequate illumination is available.

The display with a nonuniform background presents the problem of picking out one particular bright patch from a collection usually similar in shape to the one required, a problem apparently not investigated by physiologists, so that we have been forced here to establish our own criteria of visibility. We have assumed that the visibility of the echo (i.e., the reciprocal of the signal power required for detection) is proportional to its brightness relative to that of the unwanted noise peaks, each measured above the mean noise brightness; i.e., that it is proportional to δI/ΔI where ΔI is the standard deviation of the noise. This criterion replaces the contrast δI/I in the case of a uniform background. The other criterion is still taken to be the area of the echo.

A Formula for Visibility

In Appendix I the above theory is applied to produce a mathematical formula for visibility, using simple mathematical expressions as approximations to certain functions which actually are very complex (e.g., the distribution of intensity over a spot or the shape of a pulse on emerging from a receiver). The resulting formula gives the least signal power $P_{min}$ that must be available at the antenna output terminals to produce a visible echo on the display as

$$P_{min} = \left( \frac{k_1}{k_2} \right) \left( \frac{P_n}{\Phi_c} \right) \left( \frac{\tau_s}{d} \right)^{\frac{\delta I}{\Delta I}} \cdot \left( \frac{\Phi_s}{\Phi_c} \right)^{-\delta} \cdot \left( \frac{n}{n_s} \right)^{-\tau} \cdot \left( \frac{\delta I}{\Delta I} \right).$$

where the meaning of the symbols is set out in the section on notation. The significance of the various factors is as follows: $k_1$ and $k_2$ represent the effects of detector law and the grid-bias/beam-current characteristics of the c.r.t.; $P_n$ is the available noise power at the antenna output terminals, i.e., $NKT_\text{A}f$; $(1 - e^{-2\pi \Delta I})^2$ is the decrease in peak amplitude of the pulse produced by the limited bandwidth of the r.f. amplifier; $(rs/d)^{-\delta}$ and $(\theta_s/\theta)^{-\tau}$ represent the reduction in pulse brightness produced by the finite size of the spot and the effect of the echo area; $(n/n_s)^{-\tau}$ represents the smoothing of the noise background due to the superposition of pulses; and $(\delta I/\Delta I)$ is a physical constant of the human eye.

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An alternative form of this formula is

\[ P_{\text{min}} = \frac{k_1}{k_2} P_n \left( \frac{2r\Delta f}{1 - e^{-2r\Delta f}} \right)^a \left( \frac{\tau_s}{d} \right)^a \left( \frac{\theta_s}{\theta_0} \right)^b \left( \frac{\Phi_s}{\Phi_c} \right)^b \left( \frac{\delta I}{I} \right)_0 \]  

(3)

where \( r \) is the pulse-repetition frequency above which, for a given c.r.t. and antenna speed, the background is always uniform whatever the values of the other system constants, and is given by

\[ r_c = \left( \frac{k_1}{k_2} \right)^2 \left( \frac{I}{\delta I} \right)_0^2 \cdot \frac{2\pi S}{\theta_0} \cdot \frac{1 - (1 + a/S)^{-b}}{1 + (1 + a/S)^{-b}} \]  

(4)

The condition for the background to be uniform is

\[ r > r_c \quad \text{if} \quad \frac{\tau_s}{d} > 2r\Delta f, \]

\[ r \cdot \frac{2\Delta f}{s} > r_c \quad \text{if} \quad \frac{\tau_s}{d} < 2r\Delta f. \]  

(5)

Before discussing this formula in detail, we shall describe the experiments undertaken to check it. At this stage we may observe that, in either form of the equation for visibility, the ratio \( P_{\text{min}}/P_n \) is expressed in terms of only four parameters, other than the multipliers \( k_1 \) and \( k_2 \); \( (\delta I/I)_0 \) is a physical constant independent of the radar system, as is \( \Phi_s \); while for a given type of electron gun \( \Theta_s \) remains constant, the observer moving backward as the diameter of the tube, and hence the spot size, increases in order to keep the whole field in view. The four parameters may be variously chosen, one convenient group being \( \tau\Delta f, \tau_s/d, \theta_s/\theta_0 \) and \( r/r_c \). It is this reduction from the large number of system variables that has permitted the construction of nomograms for calculating the level of signal power required for visibility.

**Experimental Arrangement Used to Test Theory**

Artificial echoes on a normal noise background were produced by the system shown in Fig. 5. The apparatus allowed a wide range of values of system parameters to be arranged in any desired combination. Fading was not simulated.

The receiver consisted of the following:

(a) A standard preamplifier with damping resistors across the tuned circuits, having an over-all bandwidth of about 4 Mc., followed by (b) a special variable-bandwidth preamplifier, with two stages that could be switched to give the required bandwidth, feeding into (c) a standard radio-frequency channel, having 5 stages with an over-all bandwidth of 3.2 Mc., followed by a linear detector, video amplifier, and cathode follower.

All receiver circuits were single-tuned. The heavily damped initial stages were found necessary to ensure that the noise factor of the receiver was not affected by the bandwidth switching. The gain of the output stages was also switched, so that the receiver noise output was constant, and hence the same part of the detector curve was always used. A variable bandwidth in at least two stages was considered necessary to give a fair comparison with actual receivers. Even then the selectivity curves for the various bandwidths were not geometrically similar, as the narrow bandwidths were produced effectively by only the two variable bandwidth stages in cascade, while the wider bandwidths were affected by the later stages of amplification. The video bandwidth could, by switching capacitance, be given values from 0.2 to 2 Mc.

The tube chosen for the display was a 5FP7, used with an orange filter. The high-tension voltage was 6 kilovolts. The tube was magnetically focused, and the values of \( d \) and \( \theta_0 \) were about 0.6 millimeters and 1.1° respectively, at a distance of 1 inch from the center.

The beamwidth of the echo was determined by a cam rotated by the same motor as that driving the sine potentiometers used for the time base. This cam made contact with a stud over a small adjustable angle in each rotation. The bearing angle at which contact was made could be varied.

The whole system was set up in a small darkened cubic. As it has been shown that general illumination of the same order as the trace brightness does not affect visibility and is less tiring for the operators, most of the measurements were made with a low general illumination provided by diffused light from a low-power lamp near the ceiling. The face of the c.r.t. was shielded.

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![Fig. 5—Block diagram of an artificial radar set.](image-url)
by a hood. The observer was seated with his head on a level with the tube and about 15 inches from its face.

To make an observation, the system variables were set to the required values, and the attenuator turned back until the echo was no longer visible. The bearing of the echo was altered to some value unknown to the observer, and he was then asked to turn the attenuator up until he was just certain that he saw the echo. The echo was always placed 1 inch from the center of the tube. Thus the problem was to pick out an echo of known shape and range but unknown bearing; lack of knowledge of bearing precluded guessing. In any one sequence the observations were taken in random order, so that any variations with time in equipment or observer should not have a systematic effect. Readings were taken by three observers—the writer, and two Royal Australian Air Force operators whose experience had been mainly with deflection-modulated (class-A) displays. After a learning period of a few observational hours, the average absolute difference between readings from any two of the observers was less than 1 db and the effects of the various parameters were the same for all observers.

The tube was operated with the grid voltage at cut-off when there was no receiver output, this being the optimum bias. The observer was allowed to set the gain control to the level he preferred; small deviations were not found to affect visibility.

It was necessary to determine the attenuator reading corresponding to the noise level at each bandwidth in order to obtain the ratio \( P_{\text{min}}/P_\infty \). This was achieved by feeding the receiver output to a deflection-modulated display at a high repetition frequency, measuring the height of signal and of signal plus noise for some convenient attenuator setting, and calculating the ratio of signal-to-noise power from the known detector law. This method may give rise to an error of the order of 1 db.

**Comparison of Theory and Experiment**

Using the equipment and procedure described in the preceding section, each of the available parameters was varied through its range of values and the consequent variation in visibility compared with that predicted from (3). Usually only one parameter at a time was varied, but in investigating the effects of pulse length and sweep rate, it was convenient to vary bandwidth at the same time to keep the product \( \tau \Delta f \) constant. Finally, the signal power required for visibility under the best conditions that could be attained was measured.

**Fig. 7** shows typical experimental observations, together with the corresponding theoretical curves, and is discussed in detail below. In this figure, results for the variation in visibility with bandwidth give the value of \( P_{\text{min}} \), the input signal power required, in decibels above an arbitrary level that may vary from one set of curves to the next (but is the same for all the curves of one set). For all other parameters the quantity plotted is the ratio \( P_{\text{min}}/P_\infty \). As mentioned in the previous section, this ratio is not known to better than 1 db. Also, there may be a further slight variation between different curves, because only for the results on ultimate visibility (Fig. 7.7) were the measurements of noise power made at the same time as the observations; at other times values measured perhaps a few days previously were used.

1. **Effect of R.F. Bandwidth (Pulse Duration and Sweep Rate Constant)**

Equation (3) gives, setting \( P_\infty \) equal to \( kT\Delta f \),

\[
P_{\text{min}} \propto \frac{(\tau \Delta f)^{1-\alpha}}{(1 - e^{2\tau \Delta f})^2} \quad \text{for constant } \tau,
\]

\[
P_{\text{min}} \propto \frac{\tau \Delta f}{(1 - e^{2\tau \Delta f})} \quad \text{when the background is uniform}
\]

(6)

\[
\text{otherwise,} \\
P_{\text{min}} \propto \frac{\sqrt{\tau \Delta f}}{(1 - e^{2\tau \Delta f})^2}.
\]

(7)

Graphs of these two functions of \( \tau \Delta f \), expressed in decibels below an arbitrary level, are shown in Fig. 6. The curve for the relative visibility under any given conditions as a function of \( \tau \Delta f \) is then made up from the appropriate parts of these curves. This has been done in Fig. 7.1, in which observations on the experimental system and the corresponding predicted curves are plotted. The agreement is fairly good; some error will be introduced by the previously mentioned variation in shape of the receiver selectivity curve with bandwidth.

The optimum value of \( \tau \Delta f \) varies slightly with the parameters, lying between 0.63 and 1.17, the maxima of the two curves shown in Fig. 6. The optimum is flat, and the loss resulting from making \( \tau \Delta f \) equal to unity is never more than 0.4 db.

The empirical function \( \tau \Delta f \left(1 + \left(1/\tau \Delta f\right)^{3}\right) \), found by Haeff to fit his measurements on deflection-modulated (class-A) displays, is also shown in Fig. 6. It is apparent that it gives the same results as the present

theory if \( P_{\text{min}} \) varies as in (7) for values of \( r\Delta f \) between 0.5 and 10 and as in (6) outside these limits; such displays are the most common, corresponding to a pulse length about equal to the spot diameter and a background discontinuous except for very large bandwidths.

2. Effect of Pulse Duration and Sweep Rate \((r\Delta f \text{ constant})\).

When the length of the pulse on the screen would be less than the pulse diameter,

\[
P_{\text{min}} \propto \frac{(r_s)^{-1}}{\tau}
\]

when the background is uniform or \((rs/d) > 2r\Delta f\); otherwise,

\[
P_{\text{min}} \propto \frac{(r_s)^{-1/2}}{\tau}.
\]

It is apparent that, under all circumstances, the visibility improves with increasing pulse duration; at least uniformly as the pulse duration, and under some circumstances as the square of the pulse duration. This is due to the decreased noise accepted by the narrow bandwidths that can be used with long pulses.

Let us now consider the effect of altering sweep rate, i.e., altering the length of the pulse on the screen, for a given pulse duration.

As long as the pulse length \((r_s)\) would be less than the spot diameter, the visibility improves as the pulse length if the background is uniform or if \(rs/d > 2r\Delta f\), and otherwise improves as the square root of the pulse length.

A little consideration of the conditions when the pulse length is greater than the spot diameter shows that,

For pulse lengths greater than the spot diameter,

\[
P_{\text{min}} \propto \frac{(r_s)^{-\rho}}{\tau}, \quad (8)
\]

when the conditions for (8) obtain, \( \rho \) is usually zero, while when those for (9) obtain, \( \rho \) is usually \( \frac{1}{2} \), so that the visibility is almost independent of pulse length.

In Fig. 7.2 the ratio \( P_{\text{min}}/P_n \) has been plotted against \( rs \). Then

\[
P_{\text{min}}/P_n \propto (r_s)^{-\sigma} \quad \text{for constant} \quad r\Delta f.
\]
and the effect of changing pulse length can be conveniently examined. The experimental points are in conformity with the theory.

3. Effect of Pulse-Repetition Frequency

The theory states that

\[ P_{\text{min}} \propto r^{-1/2} \]

until the background becomes uniform; thereafter \( P_{\text{min}} \) is independent of \( r \).

The frequency at which the change-over occurs is proportional to the length of the average noise pulse \((s/2\Delta f)\) when this is less than the spot diameter; otherwise it is independent of \( \Delta f \) and \( s \). It is, of course, independent of \( r \). It is a function of the antenna speed and the characteristics of the second detector and the indicator tube.

Fig. 7.3 shows that the experimental results confirm the theory. On plotting the change-over frequency against the length of a noise pulse a straight line is obtained; on extrapolating this, the frequency corresponding to a noise pulse one spot diameter in length (i.e., the frequency \( r_s \)) is found to be 6000; we predict that, whatever the other system parameters, as long as the antenna speed remains at 2 revolutions per minute the visibility will always be independent of repetition frequency when this exceeds 6000. Unfortunately, the experimental system could not reach this frequency.

The values of \( n_e \) and \( (\Delta I/I)_{0} \) may be calculated from this critical frequency. Using (36) and (35), we have

\[ n_e = r_s \times \frac{\theta_s}{360} \times \frac{1}{S} \times \frac{1 + (1 + a/S)^{-b}}{1 - (1 + a/S)^{-b}} \quad (\theta_s \text{ in degrees}) \]

\[ = 6000 \times \frac{1.1}{360} \times 30 \times \frac{1.129}{0.871} \]

\[ = 710 \]

and

\[ \left( \frac{\Delta I}{I} \right)_0 = \frac{k_1}{k_2} \frac{1}{\sqrt{n_e}} = \frac{3}{2} \frac{1}{\sqrt{710}} = 0.06. \]

Thus about 700 superimposed pulses are required to make the noise background uniform, and a ratio of brightness deviation to r.m.s. brightness of 6 per cent cannot be detected. The latter figure agrees well with the threshold visible contrast given by Fig. 4.

4. Effect of Antenna Speed

When the background is uniform,

\( P_{\text{min}} \) is independent of \( S \).

When it is discontinuous,

\[ P_{\text{min}} \propto \sqrt{\frac{1 - (1 + a/S)^{-b}}{1 + (1 + a/S)^{-b}}} \quad (\text{see equation 27, Appendix I}) \]

where \( \propto \sqrt{S} \) when \( S \ll a \), independent of \( S \) when \( S \gg a \), \( a \) and \( b \) being constants of the screen material.

For a P7 tube \( a \) is 0.15 seconds\(^{-1}\) and it will be of the same order for other long-persistence screens, so that \( S=a \) for a speed of about 10 revolutions per minute.

The upper curve in Fig. 7.4 shows the above expression and experimental points; owing to build-up, the effect of antenna speed is seen to be small. The lower curve and points show the constancy with uniform backgrounds.

5. Effect of Antenna Beamwidth

\[ P_{\text{min}} \propto \theta_h^{-1} \quad \text{when } \theta_h < \theta_r, \]

\[ P_{\text{min}} \propto \theta_h^{-\sigma} \quad \text{when } \theta_h > \theta_r. \]

The smallest beamwidth that could be obtained (20) was twice \( \theta_s \), so that the behavior for \( \theta_h < \theta_s \) could not be investigated. The experimental observations (Fig. 7.5) agree with the prediction that \( P_{\text{min}} \) is inversely proportional to the 2/3 power of the beamwidth when the pulse first becomes larger than the spot diameter, but show a continuance of this law to much larger beamwidths than anticipated from Fig. 4. This might be expected, as the characteristic arc shape of the echo is of great aid in distinguishing it from noise pulses. The asymptotic values inserted on the margin of the graph (pulse on continuously) show that the 2/3-power law does not continue much further.

It must be remembered that an increase in \( P_{\text{min}} \) with decreasing beamwidth does not necessarily mean a decreased range in the target, as the range varies directly as the square root of aerial gain, as well as inversely as the fourth power of \( P_{\text{min}} \), and the decrease in beamwidth may be accompanied by a more than compensating increase in aerial gain.

6. Effect of Video Bandwidth

This is not taken into account in the theory. The experimental results (Fig. 7.6) show that, over a range of pulse-duration versus video-bandwidth product of 0.4 to 32, the visibility is unaffected by video bandwidth. Similar results have been obtained on deflection-modulated displays.

7. Ultimate Visibility on a PPI Display

From (3) we see that the least value of signal above noise that can be seen on a PPI display is given by

\[ \frac{P_{\text{min}}}{P_n} = \frac{k_3}{k_1} \left( \frac{\delta l}{I} \right) \]

and that this occurs when the background is uniform, neither dimension of the echo is determined by the spot diameter and its total area is at least \( a_r \), and the bandwidth is wide enough not to appreciably limit the power in the pulse. For a pulse of any area greater than the

\[ \delta l \] since \( 1 - e^{-t_{\Delta f}} > 0.98 \) when \( t_{\Delta f} > 2 \), this condition can be readily attained.
spot size, the corresponding equation is

\[ \frac{P_{\text{min}}}{P_n} = \frac{k_2 \delta I}{k_1 I} \]

In Fig. 7.7 is plotted the above equation using values of \( \delta I/I \) from Fig. 4, together with experimental points. The theoretical and experimental curves almost coincide initially, but the experimental curve shows the continued improvement with beamwidth already mentioned. One reason for this divergence may be that the screen brightness chosen by operators (about 0.04 effective foot-candles) is twice that used in the observations from which the theoretical curve was derived. Another reason, previously mentioned, is the greater importance of dimensions along the arc than radial dimensions in distinguishing the echo from noise pulses.

The fact that signals up to 18 db below noise can be seen under favorable conditions is most striking.

Some Other Aspects of the Theory

1. The Effect of Second-Detector Law and Grid-Voltage Versus Beam-Current Characteristic of the Indicator Tube

These occur as \( k_1 \) and \( k_2 \) in (3) and (4), so that

\[ P_{\text{min}} \propto \frac{k_2}{k_1} \left( \frac{k_1}{k_2} \right)^{2r} \]

i.e.,

\[ P_{\text{min}} \propto \frac{k_2}{k_1} \text{ for uniform backgrounds,} \]

but independent of \( k_2 \) and \( k_1 \) with discontinuous backgrounds.

Thus, when once the background is uniform, a system with a square-law detector should have a visibility 3 db better than the same system with a linear detector, while an indicator tube for which \( i_s \propto e_s^2 \) should give a visibility 2 db better than one for which \( i_s \propto e_s \). Attempts to obtain improved visibility by using a square-law detector have been made by various workers and proved unsuccessful; the reason presumably is that the noise backgrounds were always discontinuous—as they are in most practical PPI displays.

Our experimental system did not provide facilities for altering \( k_1 \) or \( k_2 \).

2. Improvement to be Expected from Integrating Systems

As long as the background is still nonuniform (\( n < n_0 \)), an increase in the number of integrated pulses produces improved visibility, but once \( n > n_0 \), further integration gives no improvement. It sometimes may be more convenient to use some integrating system other than the screen of a cathode-ray tube, but the integration will be no more efficient than that obtainable by using high repetition frequencies and low antenna speeds with a PPI display. However, the real advantage of electrical integrating systems lies not in their superior powers of integration or of display (the limit of detectability of a change in a meter reading, for example, is of the same order as that of a change in screen brightness), but in the possibility of removing the d.c. level; if, in such a system, voltages \( V_1, \delta V \), and \( \Delta V \) are obtained corresponding to the \( I, \delta I \), and \( \Delta I \) for the screen, then it is possible to arrange to apply the voltage \( V \) (the mean noise voltage) to bias the system, so that instead of detecting a change \( \delta V \) in a voltage \( V \) we are detecting a change \( \delta V \) in a system whose mean voltage is zero but which suffers random fluctuations of r.m.s. value \( \Delta V \), where \( \Delta V \) can be made as small as desired by increasing the integration time. Any system that could remove the average brightness on a long-persistence screen without affecting the incremental values (e.g., scanning such a screen and biasing the resultant voltages) should be as efficient as a purely electrical integrator.

The above discussion applies, of course, only to postdetector integrators, predetector integrating systems being of quite a different nature.

3. Greater Variability in Results with Discontinuous Backgrounds

As well as increasing the mean signal power required to see an echo, a discontinuous noise background causes the signal power required to vary widely from time to time, in accord with the random occurrence of bright noise pulses. The standard deviation of the mean signal power required for visibility will be inversely proportional to the square root of the number of integrated pulses. This variability was particularly noticeable in the experimental tests at repetition frequencies of about 50 c.p.s., where a large number of observations had to be made to obtain a satisfactory average value.

Display Design, and the Calculation of Losses

1. The Optimum Display

To design a display for optimum visibility, when there are no limitations except those of permissible peak and average power set by the transmitter tube, the foregoing analysis indicates that the procedure should be as follows:

1. Use the maximum available peak power in the pulse.
2. Use as long a pulse duration as possible.
3. Make the over-all bandwidth of the receiver equal to the reciprocal of the pulse duration.
4. Use a time-base sweep to produce a pulse length between one and two spot diameters. (When long ranges are required, this may be achieved by delaying the sweep relative to the transmitter pulse.)
5. Use the highest pulse-repetition frequency that, with the pulse duration chosen, will not necessitate exceeding the permissible tube dissipation.
(6) Make the antenna gain as high as possible.
(7) Having decided on the antenna gain, make the beamwidth in the direction of scan as large as possible, consistent with this gain and requirements of bearing accuracy.
(8) Use as slow a speed of antenna rotation as possible. (This condition is less important than any of the others.)

2. Calculation of Losses

Usually operational requirements make it impossible to fulfill all the above conditions, and it is required to know what losses are thereby incurred. Or, we may want to know what change in visibility occurs when we make some alteration in an existing system. For this purpose, nomograms have been drawn, using (3), to give the value of $P_{\text{min}}/P_*$, the signal power above noise power required for visibility, for any radar system in terms of the system parameters $\tau\Delta f, \tau s/d, \theta_s/\theta_n$, and $r/r_e$.

These nomograms are given in Fig. 10 (a, b, and c); which of the three is to be used in a particular case is determined by criteria that will be given below. Subsidiary nomograms of use in calculation are given in Figs. 8 and 9. Fig. 8 gives $\tau s/d$ in terms of the pulse duration, tube spot diameter, and range and radius of the display on the c.r.t.; Fig. 9, which is a nomogram of equation (4), gives the value of $r_e$ in terms of the angular spot diameter and the antenna speed for tubes with a P7 screen.

In all the nomograms it is assumed that the second detector of the receiver is linear (i.e., $k_2 = 2$) and alternative scales are given for two types of c.r.t., those for which $i_p \propto e_p^2/k_1 = 2$ and those for which $i_p \propto e_p^2/k_1 = 3$. It is also assumed that the echo area remains small enough for $p$ to be $2/3$, and that the ratio $\Phi_s/\Phi_e$ does not vary.

The method of using the nomograms is best illustrated by an example, one of which follows and is worked out in detail in Table I. The form used in this figure has been found convenient, and supplies of blank forms are available from this laboratory. The method of use, obvious from the example, is as follows:

Fig. 8—Calculation of $\tau S/d$. 
(1) Fill in the values of the system variables in the first column.
(2) From these data and the nomograms of Figs. 8 and 9, complete the second column.

(3) Determine from the third column which of Figs. 10(a), (b), or (c) should be used.
(4) Turn to this chart and, using the quantities in the second column marked (1), (2), (3), and (4),

---

**TABLE I**

Example of Use of Nomograms to Calculate Minimum Visible Signal

<table>
<thead>
<tr>
<th>System Variables</th>
<th>Calculations</th>
<th>Choice of Charts</th>
<th>Minimum Visible Signal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pulse duration</td>
<td>From Fig 8,</td>
<td>From Fig. 10(a), minimum</td>
<td></td>
</tr>
<tr>
<td>Receiver bandwidth $\Delta f$</td>
<td>$R = \frac{2\Delta f}{\tau s/d}$</td>
<td>visible signal power</td>
<td></td>
</tr>
<tr>
<td>Antenna beamwidth in direction of scan, $\theta_a$</td>
<td>$\theta_a = 3.5'$</td>
<td>$= +3.3$ + 130.8</td>
<td></td>
</tr>
<tr>
<td>Angular spot diameter of tube $\theta_s$</td>
<td>$\theta_s = 0.6'$</td>
<td>$= +1.34$ db below 1 watt</td>
<td></td>
</tr>
<tr>
<td>Angular spot diameter $\theta_s$</td>
<td>$\theta_s = 0.6'$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Antenna speed of rotation</td>
<td>$\tau_s = 2$ r.p.m.</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Law of tube</td>
<td>$(\text{or } \tau s = \theta_s^2)$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Pulse-repetition frequency $\tau = 500$ pulses/sec.</td>
<td>$r = 500$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Receiver bandwidth $\Delta f$</td>
<td>$\tau s = 10,000$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Receiver noise factor $N$</td>
<td>$\tau s = 0.045$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

---

**Fig. 9**—Calculation of $r_s$ for cathode-ray tubes with P7 screens.
Fig. 10—(a) Minimum visible signal on PPI display. \( R < 1, (r/r_s) > 1, \) or \( R > 1, (r/r_s) X R > 1. \)

Fig. 10—(b) Minimum visible signal on PPI display. \( R < 1 \ (r/r_s) < 1. \)
read off the value of the minimum visible signal power below noise. (Use the scale appropriate to
the type of tube used.)
If the value of the minimum visible signal in terms of
the available signal power in the antenna circuit is
giving for a P7 screen the loss in visibility when the
echo builds up over only a few scans instead of over an
infinite number; e.g., when the target is moving or the
antenna is nodding as it scans.
From it we see that, if in the example of the previous
preferred, add to the above the value of \( P_s \) from the sec-
ond column, obtaining the result in decibels below 1
watt.

**Example**

A system with a PPI display, using a 5FP7 tube, has
a beamwidth of 3.5 degrees (to the 1 \( 4 \)-db points)\(^6\) in
the direction of scan, an antenna speed of 2 r.p.m., a
pulse-repetition frequency of 500 pulses per second, a
pulse duration of 2 microseconds, and a 100-mile sweep
occupying 2\( \frac{1}{2} \) inches on the face of the cathode-ray
tube. The receiver has a noise factor of 13 db and a
bandwidth of 1 Mc. What is the value of the least signal
that can be seen on the display?
This example is worked out in Table I, and the least
visible signal is found to be 134 db below 1 watt avail-
able at the antenna output terminals.

3. **A Nomogram for Obtaining Loss when Echoes are
Returned on Only a Few Scans**

Fig. 11 is a nomogram, based on (37) of Appendix I,
\(^6\) The 14-db points measured for transmission or reception only

Fig. 11—Loss in visibility due to movement of the target, or to change
in antenna elevation between successive scans.

of 0.1 db. The loss is small because there is very little
build-up on the 2-r.p.m. scan. If the original speed had
been not 2 but 60 r.p.m., and still only 2 scans were superposed, the loss would be 54 db, i.e., the build-up is now very important. The nomogram illustrates the behavior mentioned at the end of Appendix I; for speeds greater than 10 r.p.m. \((S>a)\), the visibility depends only on the total time of looking at the target; for speeds less than 4 r.p.m. \((S<a)\), the loss under any circumstance is never more than 1 db.

**ACKNOWLEDGMENT**

This work has been carried out as part of the research program of the Radiophysics, Council for Scientific and Industrial Research, Commonwealth of Australia.

The author would like to acknowledge her indebtedness to the discussion by Andrew and Langford\(^7\) of the problems of deflection-modulated (class-A) displays, and also to many conversations with B. Y. Mills of this laboratory.

**APPENDIX I**

A Mathematical Formula for Visibility

The principles outlined in Section 3 are here applied to derive a mathematical formula for visibility. For some of the factors affecting visibility the exact mathematical expressions are too cumbersome to be useful, while for others they are not exactly known, so that a number of approximations have been made; these are indicated as they occur. As a considerable amount of material is involved, it is presented in note form. First, the various factors involved are set out in their mathematical form, and from these the formula for visibility is developed step by step. The notation is that given in Section 2.

(1) Available Power at Antenna Output:

\[
P_{\text{min}} \quad \text{Peak signal power} = P_{\text{min}}' = G_0 \cdot A^2 \cdot P_{\text{min}}
\]

Mean noise power: \(P_s = NkT\Delta f\).

(2) Output from R.F. Amplifier

Peak signal power: \(P_{\text{min}}' = G_0 \cdot A^2 \cdot P_{\text{min}}\)

where \(G_0\) is the gain at the center of the amplifier pass-band and \(A\) is the reduction in peak voltage of a square pulse caused by the selectivity of the r.f. amplifier. Fig. 12 shows the reduction in peak voltage suffered by a square pulse when passed through an amplifier consisting of 1, 2, 5, or 10 cascaded single-tuned stages. None of the curves diverge greatly from that for one circuit, for which

\[
A = 1 - e^{-2\pi\Delta f t}
\]

and hence we have taken this value for \(A\), so that

\[
P_{\text{min}}' = G_0 \cdot (1 - e^{-2\pi\Delta f t}) \cdot P_{\text{min}}.
\]


Duration of Signal Pulse: Fig. 3 shows that, so long as \(t\Delta f < 0.5\), the pulse duration is not affected significantly by the receiver bandwidth, but that for narrower bandwidths the pulse becomes longer, its duration eventually being inversely proportional to bandwidth. However, in so doing the pulse loses its characteristic shape, and inspection of Fig. 2 shows that, for \(t\Delta f < 0.5\) the signal and noise pulses have almost identical shapes and durations; this effect will offset any improved visibility due to the greater area of the pulse. Hence, we have assumed

\[
\text{duration of output pulse} = \tau.
\]

\[
\text{mean noise power} P_s' = G_0 \cdot NkT\Delta f.
\]

\[
\text{duration of noise pulse} = (1/2\Delta f) \quad \text{(from Fig. 3)}.\]

(3) Output from Detector

Amplitude of Signal and Noise: It has been shown by R. E. Burgess, a member of the staff of the Radio Division of the National Physical Laboratory of England, that

\[
V = 1.25\sqrt{P_s'} \quad \text{for a linear detector}
\]

\[
\Delta V = 0.63\sqrt{P_s'} \quad \text{for a linear detector}
\]

\[
\Delta V = 2P_n' \quad \text{for a square-law detector}
\]

Hence, substituting from (10) and (12),

\[
\frac{\delta V}{\bar{V}} = \frac{(1 - e^{-2\pi\Delta f t})^2}{2 \bar{P_n}} \quad \text{for a linear detector}
\]

\[
\frac{\delta V}{\bar{V}} = \frac{(1 - e^{-2\pi\Delta f t})^2}{k_2 \bar{P_n}} \quad \text{for a square-law detector},
\]

or

\[
\frac{\delta V}{\Delta V} = \frac{(1 - e^{-2\pi\Delta f})^2}{k_2 \bar{P_n}} \quad \text{for either detector}.
\]
Pulse Durations: Still as in equations (11) and (13).

(4) Beam Current in Terms of Receiver Output

\[ i_p \propto V^{k_1} \]  

where

\[ k_1 = 3 \] for magnetically focused tubes of the single-crossover type (e.g., 5FP7, 7BP7).

\[ k_1 = 2 \] for electrostatically focused tubes of the double-crossover type (e.g., 5CP7).

(5) Brightness of Screen for Zero Spot Size and Screen Persistence

\[ I \propto i_p^k \]

where \( k \) is slightly greater than unity when the screen is complete deactivated between sweeps, and slightly less than unity when the screen is allowed to build up with an interval of 1 second between sweeps, so that for the conditions in which we are interested it is sufficient to take

\[ I \propto i_p \]

and hence, from (16),

\[ I \propto V^{k_1} \]  

Hence,

\[ \frac{\delta I}{I} = \frac{\delta V}{I} = k_1 \frac{1}{V} \]

and thus, from (14),

\[ \frac{\delta I}{I} = \frac{k_1}{k_2} \left( 1 - e^{-2\pi f} \right) \frac{P_{min}}{P_n} \]  

(17)

It can be shown that, within wide limits, the value of \( \frac{\delta V}{\Delta V} \) is independent of the detector law, and hence as, according to (17), the change from voltage to brightness is equivalent to multiplying the exponent of the detector law by \( k_1 \), we have

\[ \frac{\delta I}{\Delta I} = \frac{\delta V}{\Delta V} = \left( 1 - e^{-2\pi f} \right) \frac{P_{min}}{P_n} \]  

(18)

from equation (15).

(6) Effect of Spot Size on Screen Picture

1. Area of signal and noise pulses:

signal length = \( \tau \) when \( \tau > d \)

= \( d \) when \( \tau < d \)

Hence, decreasing \( f \) by \( \sqrt{u} \), and using the value of \( \delta I \) given by (22), (19) becomes

\[ \frac{\delta I}{\Delta I} = \left( 1 - e^{-2\pi f} \right) \frac{\tau}{d} \left( \frac{\theta_h}{\theta_s} \right)^m \frac{P_{min}}{P_n} \]  

(23)

(7) Effect of Long Persistence of Screen

Area of pulse: Unaffected (provided target does not move appreciably between successive antenna rotations).

Brightness:

(a) \( \delta I/I \). As stated in Section (5) of this appendix, we may assume that the proportional change in intensity \( \delta I/I \) remains equal to the corresponding change in beam current \( \delta i_p/i_p \), irrespective of the screen persistence and rate of antenna rotation.
(b) $\Delta I/I$ obviously is affected by the screen-persistence, which acts as a further integrating agency smoothing out variations in the noise and thus decreasing $\Delta I/I$; i.e., the effect of screen persistence is to increase $n$, the number of pulses averaged on the PPI screen.

To obtain a value of the factor by which $n$ is increased for long-persistence screens, we shall assume that in each antenna rotation a constant average increment $I'$ of brightness is added, while between each rotation the brightness decays by a factor $(1 + at)^{-b}$, $t$ being the time since the last increment (in this case $1/S$, the time of a rotation), $b$ being a constant of the screen, and $a$ another constant depending on the screen material and the screen brightness. Since past notations whose brightness still appreciably persists are of importance, we are greatly interested only in intensities about the final value $I$, so that it is sufficient to take the value of $a$ appropriate to this final brightness. For the same reason, the assumption of equal average increments from each rotation is reasonable. Then we have

$$I = I' \left[ 1 + (1 + a/S)^{-b} + (1 + a/S)^{-2b} + \cdots \text{to infinity} \right]$$

i.e.,

$$1/\sqrt{1 - (1 + a/S)^{-2b}}$$

Hence the effect of long persistence of the screen causes the ratio $\Delta I/I$ (and hence the ratio $\Delta I/\delta I$) to be multiplied by

$$[1 - (1 + a/S)^{-b}] / \sqrt{1 - (1 + a/S)^{-2b}}$$

i.e.,

$$\sqrt{[1 - (1 + a/S)^{-b}] / [1 + (1 + a/S)^{-b}]}$$

which, as anticipated, is less than unity.

We may express this by saying that the number of integrated pulses is effectively increased from $n_r$ to $n$, where

$$n = n_r \cdot \frac{1 + (1 + a/S)^{-b}}{1 - (1 + a/S)^{-b}}$$

and thus (24) becomes

$$\frac{\delta I}{\delta I} = (1 - e^{-2\tau S}) \cdot \frac{(\tau S)^{\alpha}}{d} \cdot \left(\frac{\theta_k}{\theta_a}\right)^{-\gamma} \cdot \frac{P_{\min}}{P_n}.$$  

(28)

It has been shown by several workers, that the rate of decay of long-persistence screens depends on the past history of the screen. This means that the value of $a$ in (27) is a function of $S$. Since the effect of antenna speed is anyhow small (see Fig. 7.4), it has seemed sufficient to take $a$ as the value appropriate for cyclic excitation at those speeds for which persistence is important. The value given in the notation is for a speed of 1 r.p.m.

(8) Formula for Visibility

(a) Uniform background

From equation (22),

$$P_{\min} = \frac{k_2}{k_1} \cdot \frac{P_n}{(1 - e^{-2\tau S})} \cdot \left(\frac{\tau S}{d}\right)^{\alpha} \cdot \left(\frac{\theta_k}{\theta_a}\right)^{-\gamma} \cdot \frac{\delta I}{I}.$$  

(29)

The variation of $\delta I/I$ with echo area is given by

$$\frac{\delta I}{I} = \left(\frac{\tau S}{d}\right)^{\alpha} \cdot \left(\frac{\theta_k}{\theta_a}\right)^{-\gamma}.$$  

where $\Phi$ is derived from (20), so that

$$\frac{\delta I}{I} = \left(\frac{\tau S}{d}\right)^{\alpha} \cdot \left(\frac{\theta_k}{\theta_a}\right)^{-\gamma}.$$  

(30)

where $u = \rho$ when $\tau > d$

$= 0$ when $\tau < d$

$v = p$ when $\theta > \theta_s$

$= 0$ when $\theta < \theta_s$

$\Phi_s =$ solid angle subtended by spot.

Substituting this in (29), the minimum signal visible on a uniform background is given by

$$P_{\min} = \frac{k_2}{k_1} \cdot \frac{P_n}{(1 - e^{-2\tau S})} \cdot \left(\frac{\tau S}{d}\right)^{\alpha} \cdot \left(\frac{\theta_k}{\theta_a}\right)^{-\gamma} \cdot \left(\frac{\Phi_s}{\Phi_c}\right)^{-\rho} \cdot \left(\frac{\delta I}{I}\right).$$  

(31)

where

$\beta = 1$ when $\tau_s < d, \rho$ when $\tau_s > d$

$\gamma = 1$ when $\theta_s < \theta_s, \rho$ when $\theta_s > \theta_s$

(b) Discontinuous background: The equation corresponding to (29) is (28), i.e.,

$$P_{\min} = \frac{P_n}{(1 - e^{-2\tau S})} \cdot \left(\frac{\tau S}{d}\right)^{\alpha} \cdot \left(\frac{\theta_k}{\theta_a}\right)^{-\gamma} \cdot \frac{1}{\sqrt{n}} \cdot \frac{\delta I}{\Delta I}.$$  

(32)

There is no equation corresponding to (1) giving the numerical values of $\delta I/\Delta I$ required to make a certain bright patch of given area visible. However, we shall assume that the variation with echo area in the value of $\delta I/\Delta I$ required for visibility is of the same form as that with $\delta I/I$, and that when the number $n$ of overlapping noise pulses reaches a certain critical value $n_c$ such that the noise background is just uniform, the values of $P_{\min}$ for uniform and discontinuous backgrounds are identical. The first condition transforms (32) into
where $\beta, \gamma, \rho$, etc., have the same values as in (31). The second condition requires that

$$(\delta I/\Delta I) = \frac{k_2}{k_1} \sqrt{n_r} (\Delta I/I_0),$$

(34)

It is worth noting that this implies that

$$n_r = \left( \frac{k_1}{k_2} \right)^2 \left( \frac{I}{\Delta I} \right)^2,$$

(35)

$(\Delta I/I)_0$ being the highest ratio of the standard deviation of the background brightness to its mean value that produces an apparently uniform background.

(c) A General Formula: Using (34), we can combine (31) and (33) into one formula

$$P_{\text{min}} = \frac{P_n}{(1 - e^{-2\alpha})^2} \left( \frac{\tau_a}{d} \right)^{-\beta} \left( \frac{\theta_a}{\theta} \right)^{-\gamma} \left( \frac{\Phi_t}{\Phi} \right)^{-p}$$

$$\cdot \left( \frac{\Phi_t}{\Phi} \right)^{-p} \left( \frac{\delta I}{I_0} \right)^0$$

where $\epsilon = \frac{1}{2}$ for discontinuous backgrounds

$= 0$ for uniform backgrounds.

The background is uniform when $r > r_e$ if $\tau s/d > 2\alpha \delta f$ or $r \cdot (2\alpha \delta f/s) > r_e$ if $\tau s/d < 2\alpha \delta f$.

Equation (2) can be expressed in a more useful form by defining a critical pulse-repetition frequency $r_e$ given by

$$r_e = n_r \cdot \frac{2\pi S}{\Delta I} \frac{1 - (1 + a/S)^{-b}}{\theta_e} \frac{1 + (1 + a/S)^{-b}}{1 + (1 + a/S)^{-b}}$$

$$= \left( \frac{k_1}{k_2} \right)^2 \left( \frac{I}{\Delta I} \right)^2 \frac{2\pi S}{\theta_e} \frac{1 - (1 + a/S)^{-b}}{1 + (1 + a/S)^{-b}}$$

(36)

using equation (35).

The physical significance of $r_e$ is that it is the pulse-repetition frequency above which, for a given cathode-ray tube and given antenna speed of rotation, the background is always uniform whatever the values of the other system constants.

Then, from (23), (27), and (35),

$$\frac{n}{n_r} = \left( \frac{2\alpha \delta f}{s} \right)^2 \frac{r}{r_e},$$

and

$$\left( \frac{n}{n_r} \right)^{-\epsilon} = \left( \frac{2\alpha \delta f}{s} \right)^{-\alpha} \frac{r}{r_e},$$

$$= \left( 2\alpha \delta f \right)^{-\alpha} \frac{\tau}{d} \left( \frac{r}{r_e} \right)^{-\epsilon},$$

where

$\alpha = 0$ when $(s/2\Delta f) > d$ or the background is uniform = $\frac{1}{\epsilon}$ otherwise.

Then (2) can be written

$$P_{\text{min}} = \frac{k_2}{k_1} \frac{P_n}{(1 - e^{-2\alpha})^2} \left( \frac{\tau_a}{d} \right)^{-\beta} \left( \frac{\theta_a}{\theta} \right)^{-\gamma} \left( \frac{\Phi_t}{\Phi} \right)^{-p} \left( \frac{\delta I}{I_0} \right)^0,$$

(3)

(9) When Echoes are Returned on Only a Few Scans

The target may be moving, or the antenna may alter its elevation between successive rotations (the process of "scanning"), so that, although noise occurs on every scan, a return from the target may occur on only a few scans. Then $I$ and $\Delta I$ are unaltered by $\delta I$ will be reduced.

We shall assume that the simplified picture of build-up processes given in Section (7) of this Appendix can still be used, this time to give the incremental intensity due to an echo. We pointed out in Section (7) that the picture is close to the truth so long as the total light intensity does not vary much, and this is true here as long as $\delta I$ is not too large compared with $I$. Then, if $\delta I_a$ is the value of $\delta I$ when the echo builds up over only $q$ rotations, and $\delta I_w$ the value when it has built up over so many rotations that further build-up has a negligible effect,

$$\delta I_a = 1 + (1 + a/S)^{-b} + (1 + a/S)^{-2b} + \cdots + (1 + a/S)^{-(q-1)b}$$

$$\delta I_w = 1 - (1 + a/S)^{-b},$$

(37)

giving the reduction in visibility.

For $S > a$, the reduction factor is approximately $ab \cdot q/S$; i.e., for high speeds the reduction depends only on the time, $q/S$, during which the antenna looks at the target. When $S < a$, the factor approaches unity; i.e., at very low speeds the number of hits on the target is not important, obviously because build-up hardly enters at these speeds.

APPENDIX II

A Relevant Theorem in Statistics

If $x_1, x_2, \ldots, x_n$ are each distributed normally with means $a_1, a_2, \ldots, a_n$ and standard deviations $\sigma_1, \sigma_2, \ldots, \sigma_n$, then any linear function of the $x$'s, $x_1 + x_2 + \cdots + x_n$ also is normally distributed with a mean $\sum x_i a_i$, and a standard deviation $\sqrt{\sum \sigma_i^2}^2$.

In particular, if the $x$'s are individual observations on a normal population of mean value $a$ and standard deviation $\sigma$, then the means of sets of $n$ such observations form another normal population whose mean is $a$ and whose standard deviation is $\sigma/\sqrt{n}$.

Although these theorems apply exactly only to normal populations, they are adequate for the populations encountered in this paper, for the fairly high values of $n(>10$, and often some hundreds) encountered.
Results of Microwave Propagation Tests on a 40-Mile Overland Path*

A. L. DURKEE†

Summary—This paper gives the results of a series of microwave radio propagation tests over an unobstructed 40-mile overland path. The purpose of the tests was to investigate the transmission characteristics of such a path at centimeter wavelengths over a long period of time. Statistics on the transmission results at wavelengths ranging from 1.25 to 42 cm. are given. The tests extended over a period of about two years.

This paper presents the results of a series of microwave radio propagation tests over an unobstructed 40-mile overland path. The purpose of these tests was to study the characteristics of propagation over such a path at centimeter wavelengths, and to investigate the practicability of using microwaves for radio relaying under conditions calling for a high degree of circuit reliability. The nature of the test program was such as to provide statistical data on the performance of a typical microwave circuit over a long period of time. The program included studies of the variation of transmission characteristics with time of day, season, wavelength, polarization, path length, and path clearance. The tests covered a period of about two years.

The Test Circuit

The transmission path over which the measurements were made extended from New York City to Neshanic, N. J., a distance of 40.1 miles. The New York terminal of the test circuit was located on the roof of the New York Telephone Company building at 140 West Street. The antennas at this location were approximately 500 feet above mean sea level. At Neshanic, the antennas were mounted on top of a 50-foot wooden tower located on a ridge having an elevation of about 550 feet above sea level. A profile of the transmission path is shown in Fig. 1.

Measurements were made on continuous carrier signals transmitted from New York and received at Neshanic. The transmitters employed reflex-oscillator tubes giving output powers up to 100 milliwatts. The receivers were connected to Esterline-Angus recorders which produced continuous records of the transmission variations. In most of the tests, antennas of the parabolic-reflector type, horizontally polarized, were used at both ends of the circuit. Means were provided for measuring the power delivered to the transmitting antennas, and for calibrating the receiver outputs in terms of power delivered by the receiving antennas. The range of calibration of the equipment varied somewhat with the wavelength employed, but except at the shortest wavelength (1.25 cm.) it covered receiver inputs corresponding to received field intensities from about 10 db above to about 20 db below the calculated free-space values.

Scope of the Data and Method of Analysis

Continuous transmission on a wavelength of 6.5 cm. was started late in July, 1943. This circuit was operated until February, 1945, with only a few interruptions, and its performance was taken as a standard against which the results at other wavelengths were compared. In the fall of 1943 a circuit was put into operation on 3.2 cm., and measurements were made at this wavelength until February, 1945. A 10-cm. circuit was operated intermittently from September, 1943, until August, 1944, when it was replaced by a 42-cm. circuit. The latter was kept in operation for about two months. Finally, a series of measurements at 1.25 cm. was made during August and September of 1945. The 3.2-cm. system was used as the comparison circuit during the 1.25-cm. tests.

With continuous graphical recording of the receiver outputs, large amounts of data were accumulated in the course of the tests. Certain sections of particular interest were examined in detail, but the bulk of the record was condensed into a form suitable for statistical analysis.

The reduction process consisted in the tabulation of maximum and minimum received field intensities for each interval of one hour, together with an estimate of the average field for the hour. The ratio of maximum-to-minimum field for a one-hour period, expressed in decibels, was called the fading range for the hour. Similarly,

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the ratio of maximum-to-minimum field for a 24-hour period was called the fading range for that day.

A summary of the data for all of the tests except those at 1.25 cm. is given in Fig. 2. This is a plot of daily fading range for each circuit for each day on which a complete record was obtained. It can be seen that the fading ranges were generally greater on summer days than on winter days. Also, there was a tendency for the fading ranges to be greater at the shorter wavelengths. These trends will be more apparent in later figures. Since the calibration range of the test equipment was limited to about 30 db, this is the maximum value of fading range shown in Fig. 2, although the records indicated that the range exceeded 30 db on some days.

The wavelengths used in the tests were 1.25, 3.2, 6.5, 10, and 42 cm. The 1.25-cm. data are not included in Fig. 2 because the character of the record obtained on that circuit necessitated a somewhat different method of analysis. As a result of the limited amount of transmitter power available and the relatively large atmospheric loss factor at this wavelength, the signal was obscured by the receiver noise a substantial fraction of the time, and a satisfactory value for the daily fading range frequently was unobtainable.

**Diurnal and Seasonal Trends**

Fig. 3 shows the average daily fading range at 6.5-cm. for each month of the year 1944. The greater variability of transmission in the summer than in the winter is clearly evident in this figure. A striking feature is the abrupt rise in the average fading range from April to May. The reduction from May to June may perhaps be accounted for by the fact that complete records on 6.5 cm. were obtained on only 12 days in June, due to special tests and work on the equipment. With respect
to diurnal and seasonal trends, the results at 6.5 cm. are typical of those at the other wavelengths used in the tests.

The diurnal variation of fading at 6.5 cm. for typical summer and winter months is illustrated in Fig. 4. This figure shows average fading range for each hour of the day for the months of August, 1943, and February, 1944. The diurnal trend is much more pronounced in the summer than in the winter. Throughout the summer months, transmission almost invariably was stable for several hours around midday, even on days marked by extreme fading at other hours. The period of greatest fading extended from about midnight to sunrise. After sunrise, the fading range decreased rapidly to a minimum at about 10 A.M.

Another illustration of the seasonal difference in propagation characteristics is given in Fig. 5. This figure shows distribution curves of instantaneous field intensity at 6.5 cm. for two selected days, August 1, 1943, and February 14, 1944, which were the days of greatest fading in the respective summer and winter months. On August 1 the received field was more than 20 db below the free-space value for a total time of about 7 minutes. On February 14, on the other hand, the field never was more than 6 db below free-space.

The curves of Fig. 5 illustrate the difference between relatively severe fading conditions in summer and winter. Many days during the summer showed considerably less field variation than that indicated by curve 1 and, similarly, on most winter days the variability was less than that represented by curve 2. In fact, during the winter there were a number of days on which the maximum variation of received field intensity did not exceed 2 db.

![Fig. 4—Diurnal variation of fading at 6.5 cm. in winter and summer months.](image)

![Fig. 5—Instantaneous field-intensity distributions at 6.5 cm. for a typical summer and a typical winter day. (1) August 1, 1943. (2) February 14, 1944.](image)

**Wavelength Comparisons**

In the discussion of Fig. 2, attention was called to a tendency for the fading range to be somewhat greater at the shorter wavelengths. This effect is shown more clearly in Fig. 6. In this figure, percentage distributions of the hourly fading ranges at 3.2, 6.5, and 10 cm. are plotted for a period of one month, during which the three circuits were operated simultaneously. In the region where the ranges are greater than a few decibels, there is a definite increase in fading range with decreasing wavelength.

For some purposes, field-intensity minima are of more interest than fading ranges. Accordingly, in Fig. 7 are plotted percentage distribution curves of the hourly minima of field intensity for all of the transmission records summarized in Fig. 2. It is evident that the deepest fades occurred at the shortest wavelength, but the over-all spread between the 3.2- and 42-cm. curves is not very great. It should be noted, however, that the 42-cm. data cover only two months at a time of year when fading is severe, while the data for the other wavelengths cover much longer periods of time and a wide range of fading conditions.
A comparison of the records taken on the various circuits revealed several interesting characteristics. In the first place, when there was no fading the received fields at wavelengths from 3.2 to 10 cm. were usually within a few decibels of the calculated free-space values. Secondly, close inspection of the records showed that there was a marked tendency for the fading variations at 3.2, 6.5, and 10 cm. to be synchronous much of the time. It was also found that fading was generally synchronous on two receivers with antennas separated about 25 feet vertically and tuned to the same 6.5-cm. signal. From these observations it was concluded that ground reflections did not play an important part in the propagation of 3- to 10-cm. waves over the New York-Neshanic path.

**Types of Fading**

It was found that the transmission records obtained were of four distinct types, examples of which are shown in Fig. 8. Type 1 represents a condition of stable transmission with very little fading. This condition was quite common in the winter, sometimes lasting for several days at a time. It was comparatively rare in the summer, and when it did occur it seldom continued for more than a few hours. Type 2 consists of a rapid small-amplitude variation superposed on a steady average value or on a slow, irregular variation. It was fairly common in the summer and almost nonexistent in the winter. Type 3 is characterized by comparatively slow variations of irregular amplitude and period. This is the kind of fading most frequently encountered in the summer, and practically the only kind observed in the winter. Type 4 represents the most violent fluctuations experienced on the circuits. It occurred only in the summer and fall, and then only on rare occasions. The duration of these periods of extreme fading ranged from 1 to 5 hours, and they usually occurred between midnight and sunrise.

All four types of fading were encountered at 3.2, 6.5, and 10 cm. In fact, the records for 3 to 10 cm. were generally very much alike, except that the fading was somewhat greater at the shorter wavelengths. At 42 cm., however, the records obtained were noticeably different. The transmission variations, which at times were comparable in magnitude to those at the shorter wavelengths, usually were considerably slower. There was no occurrence of the type-2 rapid scintillation, nor were there any fluctuations as violent as those classified as type 4. On a number of occasions the 42-cm. field was observed to be abnormally high and fairly steady, while the 3.2- and 6.5-cm. circuits were fading considerably. A comparison of 42- and 6.5-cm. records taken during a period of moderately severe fading is shown in Fig. 9.

**Polarization**

Some comparisons of the fading of horizontally and vertically polarized waves were made at 6.5 cm. by setting the polarization of the New York transmitting antenna at 45 degrees and recording the signal at Neshanic on two receivers, one arranged to accept the horizontal component and the other the vertical component. These
tests covered a period of 10 days and included a wide range of fading conditions. After making allowance for minor dissimilarities in the receiver characteristics, no significant differences in the two records could be found.

**Path Length**

About halfway between New York and Neshanic, the transmission path crossed a ridge located in Plainfield, N. J. From the top of a 25-foot tower on this ridge there was an unobstructed view of the New York and Neshanic test sites. A temporary field station was set up at this point in November, 1943, for the purpose of making comparisons of transmission on the over-all 40-mile path and the two 20-mile half sections. The complete setup for these tests consisted of a 6.5-cm. transmitter at New York which was received both at Plainfield and at Neshanic, and another transmitter at Plainfield on a slightly different wavelength which was received on a second receiver at Neshanic. Observations were made during the winter, when transmission was generally stable, but they included several periods of moderate fading which produced some interesting results.

Fig. 10 shows distribution curves of the hourly minima of field intensity for the month of December, 1943. The curves for the two 20-mile sections are very similar, while the one for the over-all path shows a considerably greater range of field minima. In fact, the depth of fading on the 40-mile path was consistently about twice as great, in decibels, as that on either of the two half sections. The similarity of the distributions for the two 20-mile circuits is interesting in view of the different character of the two transmission paths. The New York—
Plainfield path was largely over an industrial and urban area, whereas the Plainfield–Neshanic path crossed a region of woods and fields.

A careful examination of the records for periods of fading revealed no evidence of any correlation between instantaneous variations on the over-all path and those on either of the half sections. When fading occurred, however, all three circuits invariably were affected. There were a few occasions when differences of the order of 30 minutes to an hour were observed in the times at which fading began or ended on the two 20-mile paths, indicating a rather slow movement of the atmospheric conditions responsible for the fading.

**Path Clearance**

In all of the tests described so far, the transmitting antennas at New York were located on the roof of the Telephone Building at 140 West Street. The transmission path from this point to the top of the tower at Neshanic cleared the ground level on the ridge at Plainfield by about 100 feet, assuming no atmospheric refraction. Actually, this 100-foot clearance was reduced somewhat by scattered trees and small buildings on top of the ridge.

The existence of a number of setbacks at different levels on the West Street building made it possible to vary the transmitting antenna height over a wide range, and thus to investigate transmission over the 40-mile path with different amounts of clearance at the midpoint. As a first step, a 6.5-cm. transmitter was installed...
at an elevation of 175 feet at West Street, and comparisons were made with a similar transmitter on the roof. The ridge at Plainfield extended some 60 feet above the straight-line path between the lower transmitter and its receiver at Neshanic. It was found that the received fields on this obstructed path ran 12 to 15 db below the free-space value when the circuit was stable, and fluctuated violently during periods of fading. It was concluded that such paths should be avoided if the objective is to provide a reliable communication circuit. Following the tests at the 175-foot level, the lower transmitter was raised to a height of about 300 feet. From this point the path to Neshanic was very nearly grazing at ground level on the Plainfield ridge, again assuming no refraction. In the absence of fading, the average received field on this grazing path was found to be 3 to 5 db below the free-space value, while the variations during periods of fading were considerably greater than those on the clear path. No evidence of synchronism in the fading on these two circuits was discernible in the records. At times the average field intensity was considerably above the normal steady value on the grazing path when it was below normal on the clear path.

Fig. 11 gives distribution curves of the instantaneous field intensities on the two paths for a 24-hour period characterized by moderately severe fading. These curves illustrate the great variability of transmission on the lower path. It is interesting to note that the maximum field intensity recorded on the grazing path during this day was about 12 db above the free-space value, whereas on the clear path it was only about 7 db above free-space. On the other hand, the fading minima were considerably lower on the grazing path. Distributions of the hourly minima of field intensity on the two circuits during the month of July, 1944, are shown in Fig. 12. Again the data for the grazing path show the greater spread. The desirability of some additional clearance over the grazing condition is evident from these curves.

**Test at 1.25 Centimeters**

Late in July, 1945, the installation of equipment for making tests at 1.25 cm. was completed. Continuous transmission and recording at this wavelength was carried on through August and September. The transmitter power was approximately 25 milliwatts, and the antennas at both ends of the circuit consisted of metal-plate lenses with horn feeds. The receiving equipment was capable of measuring field intensities ranging from about 0 db to about -30 db with respect to the calculated free-space value. For comparison purposes the 3.2-cm. circuit was operated throughout the period of the 1.25-cm. tests.

The performance of the 1.25-cm. circuit was found to be very sensitive to atmospheric conditions. The average path loss varied widely with the water-vapor content of the atmosphere. During rainstorms, even of moderate intensity, the signal was lost completely. In
addition to these relatively slow changes, the received signals were subject to the same types of fading observed in the 3- to 10-cm. range. The maximum instantaneous field intensity at 1.25 cm. during the entire two-month test period was 5 db below the calculated free-space value. Most of the time, however, the fields were 15 db or more below free space. The similarity of the general character of the fading at 1.25 and 3.2 cm. is illustrated by the two sections of record reproduced in Fig. 13.

Fig. 14 summarizes the test results for a period of one week during which the transmission at 1.25 cm. was relatively good. The vertical lines show hourly ranges of received field intensity for both the 1.25- and 3.2-cm. circuits. The large reductions from free-space transmission at 1.25 cm. are typical of the performance at this wavelength. There was no rain during the period in Fig. 13, but on September 25 the relative humidity at New York was very high, ranging between 80 and 100 per cent.
Distribution curves of the hourly maximum and minimum fields at 1.25 cm. for the whole test period are given in Fig. 15. These data show that about 40 per cent of the total hours of transmission had field intensity minima below –30 db, the lower limit of the measurement range. They also show that during 10 per cent of the hours the field never came up to the –30 db level. Although some difficulty was experienced in maintaining the 1.25-cm. equipment in good operating condition, a total of 867 hours of satisfactory transmission record was obtained during the test period of two months.

Meteorological Aspects

It was found that the performance of all of the test circuits was affected considerably by changes in the physical state of the atmosphere over the transmission path. As stated previously, the purpose of these tests was primarily to obtain statistics on the performance of this particular path over a long period of time, rather than to investigate the causes of the transmission variations. Consequently, no attempt was made to include in this test program any extensive meteorological studies, but some of the broader aspects of the relation between transmission variability and local weather conditions were noted.

In general, transmission was steady when the air was well mixed, as in windy or rainy weather. Under these conditions the vertical distributions of temperature and humidity are such as to yield a refractive index which decreases uniformly with height above ground. In such a medium the waves travel along paths which have uniform curvature and which tend to be stable. It was also found, as pointed out in the discussion of Fig. 4, that steady signals almost always were received around midday even on calm days. This may be accounted for by the mixing which normally occurs at this time of day, resulting from convection currents in the lower atmosphere due to the heating of the earth’s surface by the sun.

Severe fading of the received signals frequently occurred when the air was calm and still, a condition favorable to stratification and duct formation. It was shown in Fig. 4 that fading was generally worse at night than during the daytime, particularly in the summer months. On calm nights the cooling of the earth by radiation tends to produce a temperature inversion in the lower atmosphere. Moreover, evaporation from the earth’s surface produces a decrease of moisture content with height which, with the temperature inversion, may result in the formation of a duct. Under these conditions transmission is generally unstable, and may be subject to wide fluctuations. The lower average temperatures and the greatly reduced moisture content of the air during the winter months tend to reduce the severity of fading in the winter as compared with summer.

At the wavelengths above 3.2 cm. used in these tests there was no indication of any appreciable loss due to rainfall over the transmission path. There was some evidence of rain attenuation at 3.2 cm., although no accurate measurements of its magnitude were attempted. At 1.25 cm. a general rainfall of moderate intensity over the path introduced enough loss (15 to 20 db, at least) to obliterate the signal at the receiver.

Conclusion

The results of these tests give further assurance that the use of centimeter waves for communication circuits requiring a high degree of reliability is entirely practicable, provided due allowance is made for the variability of the transmission medium. It was shown that there was a tendency for fading to be somewhat greater at the shorter wavelengths employed in these tests, although the difference was not large enough to be a controlling factor in the choice of an operating wavelength. For continuous, reliable operation day after day in such applications as extensive relay networks, however, wavelengths well above 3 cm. are to be preferred. The usefulness of the shorter wavelengths is affected by rain attenuation and by absorption by certain gases present in the atmosphere (principally water vapor and oxygen). To insure optimum performance, it is desirable to avoid grazing-path conditions and to select transmission paths having ample clearance over intervening obstructions.

Acknowledgment

The tests described represent the co-operative efforts of a number of engineers and assistants of Bell Telephone Laboratories, including members of the Holmdel group. The author expresses appreciation to all who had a part in providing the material for this paper.
Wavelength Lenses*

GILBERT WILKES†

INTRODUCTION

A ROD of dielectric is held in front of a receiver antenna, the received signal increases. When the rod dimensions are properly chosen, a maximum increase is obtainable. Certain laws of this behavior that have been found at the Applied Physics Laboratory of The Johns Hopkins University will be discussed in this paper.

Hertz appears to have been the first experimenter to observe the lens-like action of blocks of pitch on his newly discovered radiation. In the study of dielectric rods, one has constantly to consider their index of refraction, which is a function of their dimensions as well as their orientation with respect to the incident wave. It is also evident that they actually act somewhat like optical lenses as energy concentrators. Finally, the power of these wavelength lenses blends smoothly into that of optical lenses of large aperture. The term "lens" is capable of interpreting satisfactorily this physical behavior, whereas the terms "polyrod antenna" or "dielectric antenna" do not. The term "wavelength lens" for these devices is suggested as more appropriate than "polyrod antenna."

These lenses lie in the transition zone between radio antennas and optical lenses. The writer prefers considering only their relative power, or concentrating action, while others more familiar with radio terms prefer directive gain, as referred to an isotropic oscillator. Both will occur in the following as convenience may require.

A 3-cm. or "X"-band wavelength was used in the experimental work, so as to limit the size of equipment and space requirements.

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FUNDAMENTAL LENS BEHAVIOR

If we take a series of dielectric blocks having a uniform cross section of the order of a wavelength, and place them in front of a receiving horn in such a way as to obtain an increasing length of dielectric or lens in front of the horn, the gain is found to vary periodically with the lens length. If the steps by which the length is increased are made sufficiently small, a second-harmonic variation of small intensity is found superimposed on the fundamental variation. Fig. 1 shows these characteristics for two different lenses. The harmonic is found to correspond to Snell's law for the reflection from thin sheets, and can be eliminated by the use of pointed lenses. It has no practical importance, therefore, but did lead to the determination of a wavelength individual to each lens, which permitted the determination of the velocity at which energy travels through the lens; this, in turn, gives an explanation of the characteristic variation with length of the fundamental gain of lenses.

APPARENT INDEX OF REFRACTION

The harmonic variation of Fig. 1 passes through minima at lengths equal to about 0.4λ. The dielectric constant of lucite is about 2.55, and its index of refraction is 1.6. If the lens behaved according to this index, its wavelength would be 0.635λ, and the minima would occur at every 0.31λ. The discrepancy between this and the observed data exceeds any possible experimental error and the existence of a characteristic wavelength λL must be postulated.1 This wavelength im-
plies characteristic lens velocities \( v_L \) and indices of refraction \( n_L \) that are all interrelated by the same types of equation as the more usual constants for large masses of dielectric.

To visualize lens behavior, it is helpful to realize that there is no critical or cutoff dimension for a bare dielectric rod, and also that the energy traveling in a dielectric rod is mainly concentrated toward the center of the rod. These ideas have been discussed theoretically by many authors, particularly Schelkunoff. The latter gives the general expressions for waves in dielectric wires that substantiate the above statement, and from which at least an approximate form of the expression of the lens index of refraction may be obtained.

The variations of energy observed in Fig. 1 may be explained by Fig. 2, where a plane wave is shown sweeping over a lens. Admitting that the lens has a wavelength \( \lambda_L \), Snell's law for normal incidence gives the transmission through a thin dielectric sheet as

\[
T = 1 - R = 1 - \frac{(r_{12} + r_{33})^2 - 4r_{12}r_{33} \sin^2 \alpha d}{(1 + r_{12}r_{33})^2 - 4r_{12}r_{33} \sin^2 \alpha d}
\]  
\[
(1)
\]

with

\[
r_{jk} = \frac{\sqrt{E_j - \sqrt{E_k}}}{\sqrt{E_j + \sqrt{E_k}}}
\]

\[
(2)
\]

\[
\alpha = \frac{2 \pi}{\lambda_L} \quad \lambda_L = \text{wavelength in lens.}
\]

\[
(3)
\]

If each side of the dielectric is looking at the same impedance, which is only an approximation in the present case, (2) gives

\[
r_{12} = -r_{23} = r
\]

and (1) becomes

\[
T = 1 - \frac{4r^2 \sin^2 \alpha d}{(1 - r^2)^2 + 4r^2 \sin^2 \alpha d}
\]

\[
(4)
\]

which goes through minima for

\[
| \sin \alpha d | = 1 \quad \alpha d = (2K + 1) \frac{\pi}{2}
\]

\[
(5)
\]

or

\[
d = \frac{(2K + 1)\lambda_L}{4} = \frac{\lambda_L}{4}, \frac{3}{4} \lambda_L, \frac{5}{4} \lambda_L.
\]

\[
(6)
\]

The harmonic minima of Fig. 1 therefore define a lens wavelength \( \lambda_L \). This lens wavelength must correspond to an index of refraction \( n_L \) and energy velocity \( v_L \) in the lens:

\[
n_L = \frac{\lambda}{\lambda_L} \quad v_L = \frac{\lambda L}{\lambda} = \frac{c}{n_L}
\]

\[
(7)
\]

where \( v, c, \nu \) are the frequency, velocity, and wavelength of the radiation in free space.

A wave flowing over the dielectric of Fig. 2 will excite displacement currents inside the dielectric. These, in turn, will radiate energy, a large part of which will be totally reflected inside the dielectric. Neglecting losses and external field depletion, this action will continue down the dielectric until the internal and external energies are one-half cycle out of phase, after which the internal energy will feed back into the external field until the two are again in phase, when the process will be repeated.

The transit time of the internal and external energies are, respectively,

\[
t_L = \frac{d}{v_L} \frac{n_L}{c} \quad t = \frac{d}{c}
\]

\[
(8)
\]

The peak gain will occur when these two times differ by an odd number of half periods, or

\[
t_L - t = \frac{(2K + 1)}{2\nu} = \frac{d}{c} (n_L - 1),
\]

\[
(9)
\]

or the first optimum lens length is

\[
d_{\text{max}} = \frac{c}{2\nu(n_L - 1)} = \frac{\lambda}{2(n_L - 1)},
\]

\[
(10)
\]

and so on. This then corresponds to the fundamental variation of energy of Fig. 1.

In simple lenses that have no matching device inside the horn or waveguide, the value of optimum length from (10) is always verified. The apparent index of refraction may be obtained either directly from a phase meter or calculated. We note for future reference that the apparent indexes vary with dimensions. Thus, the larger polystyrene lens of Fig. 1 would have an index of 1.5, and the smaller one an index of 1.25. When a lens is extended into a waveguide for matching purposes, the optimum position is influenced slightly by the length in the guide. However, after the best match is obtained, the lens length can be adjusted so as to again verify (10). Referring to Fig. 3, a single piece of dielectric is slid in a waveguide so that one end acts as matching slug and the other as lens. The experimental apparent index of refraction is 1.09, indicating an optimum length of 5.55\( \lambda \). The slug, however, moved the peak gain back to 5.5\( \lambda \). At this point a slight additional gain would have been available by increasing the length of lens by 0.05\( \lambda \) and leaving the matching slug at its original length.

---


The most important characteristic of a wavelength lens is its apparent index of refraction. Reference has already been made to Schelkunoff's treatment of waves in dielectric wires.\(^4\) The equations involved and space does not permit their reproduction here. Suffice it to say that they indicate an approximate form of the transmission constant, and that from this work and our many experimental determinations we have adopted the expression

\[
n_2 - 1 = \left( n - 1 \right) e^{- (\lambda' / \lambda_\text{c})^2}
\]  

in which \(\lambda'\) is a characteristic wavelength akin to the cutoff wavelength of guides. However, it is found experimentally that the dimension of preponderant influence in lenses is the one in the \(E\) plane or "\(a\)" of Fig. 2, while the dimension in the \(H\) plane plays only a minor role that may be neglected.

The expression for \(\lambda'\) is, therefore,

\[
\lambda' = \begin{cases} 
2na & \text{ (rectangular lenses) } \\
\pi a & \text{ (cylinder lenses) } \\
1.84 & \text{ (a = diameter). }
\end{cases}
\]

\(^4\) Equation (11) above is semiempirical. It is found to check closely experimental data on rectangular lenses, and only approximately cylindrical lenses. D. W. Horton, of the University of Texas, has communicated graphical solutions he has worked out for the transcendental expression for waves in cylindrical rods given by Stratton on page 526 of footnote reference 4. These solutions appear to be better for cylindrical lenses than (11), which, however, remains the most accurate expression known for rectangular lenses. The writer also wishes to acknowledge Dr. Horton's kind cooperation in establishing (14) in the following section.

In obtaining (11), dielectric losses, field depletion, and the proximity of metal surfaces were neglected. Reference to Figs. 3 and 4 will show that the apparent index of refraction passes from the true index in the vicinity of the metal mouth to an almost constant value a wavelength away from the mouth, and from this point on it decreases only very slowly. This slow decrease is believed due to field depletion, and will be discussed in the following. A few experimental points are plotted against (11) in Fig. 5.

\[\text{Fig. 5—Experimental verification of } n_2 - 1 = \left( n - 1 \right) e^{- (\lambda / \lambda_\text{c})^2}. \text{ For } \text{rectangular lenses, } \lambda' = 2na. \text{ For cylindrical lenses, } \lambda' = \frac{\pi a}{1.84}.\]

The energy velocities given by (11) explain the operation of the dielectric depolarizer or circular polarizer of Fig. 6. If a flat dielectric plate is mounted at a slant of 45 degrees in front of a crystal, its length can be so adjusted as to transform a plane-polarized wave to circular polarization at the crystal. For example, suppose that a plane wave \(E_1\) normal to the crystal is fed onto this assembly. It will be decomposed into a wave \(E_2\) normal to the dielectric and \(E_3\) parallel to the dielectric. According to (11), the former will not be de-
layed appreciably, while the latter will be strongly retarded. These two waves will have components in the crystal plane equal to half the original amplitude but opposed in space. If the length of the dielectric plate is such that the phase between these two is one-quarter period, the crystal becomes sensitive to their resultant, or 0.7 of the original amplitude or 0.5 of the original energy. This resultant is, then, in reality a circularly polarized wave, rotating counterclockwise in the case of Fig. 6, and the crystal is insensitive to a change in the angle of polarization of the received wave. The device becomes a depolarizer to receive a constant signal with a rolling receiver. It is generally made by flattening the end of the lens sticking into a circular wave guide to resemble a fish tail, by which name it is often called.

Relative Gain

The relative gain of a lens is the optimum energy received on the optical axis of a lens-receiver combination referred to the energy received by the receiver alone. It is the characteristic of practical significance in lens work, and unfortunately the one least reducible to a simple quantitative expression. The relative gain of a lens is affected by the nature of the receiver, the directivity or beam width of the combination, whether the lens intercepts all the received energy or only part of it, and the lens is matched to the receiver, and on field depletion. For short, stubby lenses there does not appear to exist a reliable expression for gain. However, the optimum length can be calculated from (10), and the power of the lens can be determined experimentally without trouble.

For less than wavelength apertures, optimum lenses are always long. Under these conditions all the oscillators along the lens can be considered in phase and their contributions to gain can be added. This results in the simple expression for relative energy:

$$G_{RL} = 1 + \frac{d \max}{\lambda} = 1 + \frac{1}{2(n_L - 1)}, \quad (12)$$

which, it is repeated, is only an approximation on the conservative side for long lenses in which no special matching is used between lens and receiver. Where the dimensions in either plane are such as to influence the beamwidth, the directivity of the lens-receiver combination acts to increase the apparent relative energy on optical axis.

This influence is marked on Fig. 1 and less noticeable on Fig. 4. Where a matching slug is used, as in Fig. 3, the effect of this device is important. In Fig. 4 the end of the lens in the waveguide was made and placed so as to obtain a fixed mismatch between the waveguide and atmosphere. The lens of Fig. 3, identical in all other respects, was intended to afford a variable matching device such that the maximum reflected energy would be 50 per cent of the total. The minima of Fig. 3 lie, therefore, on Fig. 4, and the maxima lie on a line twice as high. The harmonic of Fig. 4 will be recognized as Snell's reflection, and that of Fig. 3 as the characteristic of a matching device which is so great that it hides almost entirely Snell's reflection.

Equation (12) would indicate the possible construction of an infinitely powerful lens by making $n_L$ approach unity. This is very nearly obtained in thin lenses, and the drooping characteristic of Fig. 7 is obtained. The falling off of the relative energy from the straight line indicated by (12) can be analyzed approximately as follows:

Adapting Schelkunoff's treatment for the pattern of an array of sources of amplitude $M$ to the relative gain of a lens, (12) can be written

$$G_R = 1 + \left| \frac{R(d)}{R_0} \right|^2 \quad (13)$$

where

$$R(d) = \int_0^d M \sin (K_L z + \delta) e^{iKz} dz \quad (14)$$

with

$$K_L = \frac{2\pi}{\lambda_L} \quad K = \frac{2\pi}{\lambda} \quad (15)$$

If we suppose $n_L$ to approach unity, then

$$K_L \rightarrow K \quad \delta \rightarrow 0 \quad d \rightarrow \infty,$$

and, neglecting losses, Fig. 7 suggests that

$$M^2 = M_0 e^{-2Km^2} \quad (16)$$

On integrating (14), (13) becomes

$$G_R \rightarrow 1 + \frac{1}{4K^2 m^2} \quad (17)$$

which is finite, although large.

![Fig. 7—Relative gain of a thin lens.](image)

If, in Fig. 7, each increment wavelength gathers an energy fraction $\alpha$ of the preceding one, the total energy is
\[ E = E_0 + \alpha E_0 + \alpha^2 E_0 + \cdots + \alpha^{d/h} E_0 \]
\[ = E_0 \frac{1 - \alpha^{d/h}}{1 - \alpha}, \tag{18} \]
and this equals
\[ 7.5 \quad \text{for} \quad \frac{d}{\lambda} = 10. \]

The values of \( \alpha \) and \( M \) are related by
\[ e^{-2\pi M} = \alpha, \tag{19} \]
and solving, the limit relative energy becomes
\[ G_R \rightarrow 1 + \frac{1}{0.14^2} \simeq 50. \]

The particular lens cross section used in Fig. 7 was 0.2\( \lambda^2 \), so that the maximum energy an ideal lens is capable of gathering appears to be that contained in 10\( \lambda^2 \). The ideal aperture of such a lens would be 3\( \lambda \), and the minimum beam half-power point would be a third of a radian, or 19 degrees, which checks the sharpest patterns obtained with lenses of less than a wavelength aperture.

Equation (12) is the roughest kind of an approximation of the relative energy of a lens. It is of interest, however, as it confirms the experimentally proven fact that more powerful wavelength lenses can be made with dielectric materials of low indexes than with those of high indexes, such as glass. However, as the dielectric constant tends to unity, there must occur a point at which the lens ceases to function. Our experiments have not extended into this region, but only down to F1114 (\( E = 2.1 \)) which gives better lens operation than polystyrene (\( E = 2.5 \)).

**Lens Patterns**

Usable expressions for lens patterns can be derived from metallic-array theory. The computations are, however, too long to repeat here, and only the case of the cylindrical lenses will be discussed, as the expressions obtained can give qualitative information on the directivity of lenses.

The expression for the distant field of a linear array is
\[ E^2 = A^2 F_0^2 F_1^2 F_2^2 \tag{20} \]
where
- \( A \) = function of received energy and aperture
- \( F_0 \) = form factor of aperture
- \( F_1 \) = form factor of single element
- \( F_2 \) = factor of linear array of elements.

If a circular wave guide is filled with a piece of dielectric flush with the end, this dielectric will be the seat of displacement currents that, in the aggregate, resemble the current distribution of a half-wavelength oscillator in the \( E \) plane for which
\[ F_0 = \frac{\cos \frac{\pi}{2} \cos \theta}{\sin \theta}, \tag{21} \]
experimentally checked on graph A of Fig. 8.

As the lens walls are powerful absorbers of energy, its pattern may be compared to that of an orifice in an absorbing screen, and factor \( F_1 \) becomes
\[ F_1 = \frac{2J_1}{\lambda L} \frac{\pi d}{\cos \theta} \frac{\lambda L}{\pi d} \cos \theta \tag{22} \]
experimentally checked on graph B of Fig. 8, for a lens one wavelength long. Side lobes will only occur if \( F_1 \) passes through zero. As long as
\[ \frac{\pi d}{\lambda L} < 3.8 \]
this cannot occur, so that generally lenses of one wavelength are free from side lobes.

The factor
\[ F_2 = \frac{\sin \frac{p}{2} \gamma}{\sin \frac{\gamma}{2}} \tag{23} \]
where \( p \) = number of lens wavelengths in length of lens departs from unity as \( p \) increases from unity. The classical value of \( \gamma \) in (23) is
\[ \gamma = \frac{2\pi l}{\lambda} \cos \psi - \alpha \tag{24} \]

\(^a\) See page 451 of footnote reference 4.
with
\[ l = \text{spacing between oscillators}, \quad \text{one lens wavelength} \]
\[ \psi = \pi / 2 - \theta \]
\[ \alpha = \text{phase lag from one oscillator to next} = 2\pi \].

Equation (11) shows that the wavelength in a lens is an inverse function of the dimension of the \( E \) plane. While this function may be quite complex, satisfactory \( E \) patterns are obtained if
\[ l \sim \frac{1}{\alpha} \sim \lambda_L \sin \theta, \]
and, after simplifying, (23) becomes
\[ F_2 = \frac{\sin \left( \frac{\pi \rho}{n_L} \sin^2 \theta \right)}{\sin \left( \frac{\pi}{n_L} \sin^2 \theta \right)}, \quad (25) \]
which after introduction in (20), is verified in graphs C and D of Fig. 8.

It may be noted that \( \rho \), the number of oscillators in a metallic array, is required to vary by integer lengths, whereas in lenses \( \rho \) can vary continuously and the side lobes represented by \( F_2 \) vary smoothly from one lens length to the next.

The actual patterns are seen to check the above expression closely in the main beam, while the side lobes do not check nearly so well.\(^9\)

**Gain From Patterns**

Returning now to (20), consider only the energy received on the axis, for which
\[ \theta = \frac{\pi}{2} \]
\[ E^2 = A^2 \left( \frac{\sin \left( \frac{\pi \rho}{n_L} \right)}{\sin \left( \frac{\pi}{n_L} \right)} \right)^2. \quad (26) \]

Now consider only optimum lenses for which
\[ \rho_{\text{max}} = \frac{d_{\text{max}}}{\lambda_L} = \frac{n_L}{2(n_L - 1)} \equiv 1. \quad (27) \]

If the equals sign is used,
\[ \rho_{\text{max}} = 1 \]
and the corresponding \( n_L \) is found to be equal to 2, corresponding to short, thick glass lenses for which the lens energy from (26) is equal to the energy of the aperture without the lens. Setting aside this rather inefficient case and letting
\[ 1 < n_L < 2, \]
and replacing in (26) \( \rho \) by \( \rho_{\text{max}} \) drawn from (27),
\[ E^2 = A^2 \left( \frac{\sin \left( \frac{\pi \rho_{\text{max}}}{2} \right)}{\sin \left( \frac{\pi}{2\rho_{\text{max}}} \right)} \right)^2. \]

If only large integer values of \( \rho \) are considered, the expression becomes simply
\[ E^2 = A^2 \left( \frac{2\rho_{\text{max}}}{\pi} \right)^2. \quad (28) \]

To arrive at a qualitative expression of the energy on the axis in the function of aperture "\( a \)" "\( \rho \)" is replaced by its value from (27) and \( n_L \) from (11):
\[ \rho = \frac{n_L}{2(n_L - 1)} = 1 + (n - 1)e^{-\frac{(X/2\pi a)^2}{2}} \]
and introducing
\[ A \sim \frac{a^2}{\lambda^2}, \]
the expression of (28) is seen to assume the form
\[ E^2 \sim B \left( \frac{\lambda}{a} \right)^{2z}, \quad z > 1, \]
which qualitatively expresses the energy of the lens proper on the axis.

In (12), for the relative energy of a receiver-lens combination, the unit represents the signal of the receiver without the lens, which is a function to the fourth power of the aperture. The total signal received by a lens-receiver combination is, qualitatively,
\[ G_{\text{ABS}} = \left( \frac{a}{\lambda} \right)^4 + B \left( \frac{\lambda}{a} \right)^z. \quad (29) \]

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\(^9\) Peter Mallach developed pattern expressions which give good results for small ratios of \( a/\lambda \). They do not seem to apply for \( a/\lambda \leq 1 \), which is usual in this country.
Below this value, the wavelength lens region extends to zero, and the optimum energies are limited by the phase and field depletion discussed previously. Above this value, lenses approach the optical region where the energy is only a function of aperture.

Several experimental values have been plotted on Fig. 9 against the signal received by a square horn of approximately one-square-wavelength effective aperture.

\[ \frac{a}{\lambda} = 1. \]

To arrive at an idea of the directive gains shown on this curve, the ordinates can be multiplied by $4\pi$.

**Acknowledgment**

The writer wishes to acknowledge the co-operation of The Johns Hopkins University and the help of the Applied Physics Laboratory in preparing this note. It is to be hoped that others eventually will arrive at rigorous data were only qualitative information derived from experimental evidence has here been indicated.

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**A Method of Determining and Monitoring Power and Impedance at High Frequencies**

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*Summary—A method and newly developed devices for determining and monitoring power and impedance levels in transmission lines at high frequencies are explained. Practical considerations influencing accurate determination of power and impedance levels are analyzed, and the previous and newly developed methods of monitoring these important quantities under changing conditions of load are compared.

The measurement of power delivered at radio frequencies, as well as the impedance presented by the transmission line over which it is delivered, presents increased difficulties as we go to higher and higher frequencies. The work reported in this paper was directed primarily toward the measurement of power and impedance at the output terminals of radio transmitters operating at frequencies of about 100 megacycles. However, as will be seen, the methods and techniques developed are not necessarily limited to that application or frequency region.

At radio frequencies slight changes in the physical structure of antennas, transmission lines, or networks often cause a substantial change in their impedance. This effect is accentuated as the frequency is increased, and uncertainties regarding impedance values are usually reflected in the accuracy of power measurements. We therefore desire to indicate, with good accuracy, the power being dissipated in a load regardless of any changes, accidental or otherwise, that may occur in the load impedance, and also to indicate the magnitude of a transmission-line mismatch if any should occur during operation. To give such a power indication, it is practically necessary that some form of radio-frequency wattmeter be provided. In addition, some form of impedance indicator or standing-wave detector which can be used under power is essential to fulfill the second desire. Both of these facilities are provided by the circuit arrangements to be described.

Consider Fig. 1(a), where a transmission line with an inductive impedance $L$ in series with the line and a capacitive impedance $C$ across the line is shown. The voltage produced across the inductance $L$ by the line current $I$ causes a small sample current $i_l$ to flow through the resistance $R$ and the crystal rectifier. If the resistance is made large compared with the reactance of the inductance, this sample current is proportional to and in phase quadrature with the line cur-

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current. The voltage $E$ across the transmission line causes another sample current $i_F$ to flow through the capacitance $C$ and the crystal rectifier. If the reactance of the capacitance is made large compared with the impedance of the rectifier, this sample current is proportional to and in phase quadrature with the line voltage. When the line is terminated in a load resistance equal to its characteristic impedance, the sample currents will flow through the rectifier in opposite phase. The capacitance $C$ is then adjusted so that these sample currents are equal in amplitude, which is indicated by zero current through the meter. A change in the transmission-line load impedance will now cause an inequality and generally a phase displacement of the two sample currents. Their resultant, which is no longer zero, flows through the rectifier and provides a meter indication which is related to the magnitude of the impedance change.

The performance of this circuit can also be explained if it is drawn as shown in Fig. 1(b), where it is seen to constitute a Maxwell bridge, the transmission-line input impedance providing one of the resistance arms. When the bridge is balanced, the meter is not, of course, responsive to changes in the generator output. However, changes in the transmission-line input impedance will upset the bridge balance and will cause a meter indication which is related to the magnitude of the impedance change. The conditions for balance with this bridge require that the product of the reactances equal the product of the resistances, i.e.,

$$X_LX_C = RR_s.$$  

A change in frequency causes the reactance of the inductance and the capacitance to change in such manner that their product remains constant, i.e., $RR_s = L/C$. From this it is readily seen that the circuit balance is independent of frequency.

From another point of view, when the circuit of Fig. 1(a) is balanced, it may be said to be unresponsive to energy in a wave traveling from the generator to the load, left to right, while the circuit of Fig. 1(c) is unresponsive to energy in a wave traveling from right to left because this circuit is merely Fig. 1(a) reversed; i.e., the generator and load are interchanged. Each circuit is in effect a "directional coupler"1 responsive only to energy flowing in a particular direction.

We will now consider the application of this circuit to power and impedance monitoring. If the circuit is first balanced, and then the resistance $R$ and rectifier meter transposed as shown in Fig. 1(c), the sample currents $i_F$ and $i_L$ will be equal in amplitude and will add in phase. Their sum will cause a current to flow through the meter which permits it to be calibrated as a wattmeter, the indication being responsive to both line-current and line-voltage variations. If the calibration is carried out with a matched-line termination, the calibration holds with good accuracy for considerable departures from a matched load condition, as compared with the large errors involved when using the customary transmission-line ammeter or voltmeter to measure power absorbed by the load.

The relative accuracies of power monitoring by means of the circuit of Fig. 1(c) and by the ammeter or voltmeter method, as functions of transmission-line standing-wave ratio, are shown in Fig. 2. The ammeter or voltmeter method involves a wide range of uncertainty between curves $A$ and $B$ in Fig. 2(a), depending on the position of the standing wave (phase of the reflection coefficient). The error will lie on a vertical line between curves $A$ and $B$ that intersects the abscissa at a standing-wave ratio corresponding to the mismatch. A derivation of these curves is given in Appendix II.

The inherent error in the combined current and voltage circuit is shown by the curve of Fig. 2(b). A derivation of this curve is given in Appendix II. It will be seen that the error in this case is much smaller than that shown on Fig. 2(a) and does not depend on the position of the standing wave. It is specific for a given standing-wave ratio and always of one sign (positive). We will show later that even this relatively small error can be eliminated from our power measurement. The reason for this error may be explained with the aid of Fig. 1. When a transmission-line mismatch occurs, energy will be reflected back toward the generator, but the meter in Fig. 1(c) will not be cognizant of this reflection because the device is insensitive to energy propagated in the reverse direction. Accordingly, the indication will be in error relative to the power dissipated in the load by the amount of energy reflected from the load. This error, in per cent, is precisely equal to that shown in Fig. 2(b).

Now, if a second circuit is also provided in series with the transmission line, but connected as in Fig. 1(a), it will indicate any energy reflected from the load impedance, and this indication corresponds exactly to the error in the other connection. Hence, by subtracting the power reading afforded by the arrangement of Fig. 1(a) from that afforded by the arrangement of Fig. 1(c), we eliminate the error and have a precise means

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of measuring the power dissipated in the load regardless of its impedance. In addition to measuring the power dissipated in the load by subtracting the reflected from the incident power, the ratio of these two power readings is a measure of the amount by which the transmission line is mistermated by the load impedance. The standing-wave ratio on the transmission line can be computed from the following expression:

$$\text{s.w.r.} = \frac{1 + \sqrt{P_r/P_i}}{1 - \sqrt{P_r/P_i}}.$$  

The two d.c. circuits could be connected in series and poled so that their currents would be subtractive. The meter would then indicate directly the power dissipated in the load. However, to accomplish this it would be necessary for the rectifier to have a linear relation between radio-frequency power and d.c. response. The present application for this device does not appear to justify the extra apparatus and circuit complexities required to obtain this linear characteristic, particularly since the same answer can be obtained by merely throwing a switch and mentally subtracting the readings.

An arrangement of the two radio-frequency circuits in a section of coaxial transmission line, together with the d.c. switching and metering circuits, is shown in Fig. 3. These sampling circuits are arranged back-to-back on a coaxial line and in a shielded enclosure. Each includes a transverse slot cut in the outer conductor of the coaxial line which constitutes an inductive impedance in series with the line, and a circular plate which forms a capacitive impedance to the center conductor. The switch $S_2$ associated with the meter transfers the meter from one sampling circuit to the other, so that the incident and reflected powers can be observed on a single meter. This circuit arrangement also provides for a transmission-line protective device. A relay is connected in series with the d.c. portion of the circuit that samples the reflected wave, so that, if the reflection exceeds a safe operating limit, the relay closes. This relay can be made to de-energize the transmitter or, if preferred, to energize a warning device.

The initial wattmeter calibration is accomplished by first determining the amount of radio-frequency power being delivered to a matched load at the operating frequency. With the desired power being delivered and switches $S_1$ and $S_2$ in position 1, the potentiometer (Pot. 3) is adjusted so that the meter indicates the true power being delivered to the load. Pot. 3 is then sealed and not changed unless an apparatus change or operating-frequency shift is made. Switches $S_1$ and $S_2$ are then thrown to position 2, and Pot. 1 and Pot. 2 adjusted until the meter again indicates the power being delivered, and the relay sensitivity is properly set. This completes the calibration, and switches $S_1$ and $S_2$ are thrown to position 1 for normal operation.

A matched pair of germanium-crystal rectifiers is used in the metering circuit. With this type of rectifier and a d.c. circuit resistance of about 1000 ohms, the characteristics shown in Fig. 4 were obtained. Fig. 4(a) shows the relation of the d.c. current and radio-frequency power, and Fig. 4(b) shows the calibrated meter scale corresponding to this relation. It will be noted that this scale is expanded in the lower power region, which is convenient because we are interested in observing both high and low powers with about the same accuracy.

Convenient devices for use during the initial adjustment of the line load impedance, and for determining the power flow during calibration of the wattmeter, have also been developed and incorporated as a part of this monitor. They consist of the items shown in Fig. 5. Fig. 5(a) is a small Wheatstone bridge arranged so that it can be plugged into the end of a coaxial transmission line. It is connected as shown in the schematic. The ratio arms $R_1$, $R_3$ and the standard arm $R_2$ are high-frequency resistors each equal to the characteristic impedance of the line. (Throughout this paper it is assumed that low-loss lines are used so that the phase angle of the characteristic impedance is negligible.)
through the input jack, and the load impedance at the far end of the transmission line is adjusted for a bridge balance. Owing principally to the compactness of the circuit, it is possible to adjust the input impedance of the line to the desired value with an accuracy better than 5 per cent at frequencies in the region of 100 megacycles and possibly higher.

The power dissipated in the load was measured by the calorimeter method and the calorimeter checked by a known 60-cycle power dissipation. A comparison of the power measurements made with the monitor and the calorimeter showed that they agreed to within 5 per cent for standing-wave ratios up to about 2.5 to 1 and to better than 10 per cent for standing-wave ratios up to 6 to 1. The standing-wave ratio on the line, as measured with the monitor, agreed closely with the values known for standing-wave ratios from unity to about 6 to 1.
to exist from a knowledge of the line terminal impedance.

This monitor has been assembled into a section of coaxial line together with the capacitance voltage divider and a port for the insertion of the small Wheatstone bridge. Photographs of this assembly and the small bridge, as they will be supplied with high-power f.m. transmitters, are shown in Fig. 7 and Fig. 8. Fig. 9—A small bridge, as they will be supplied with high-power sources.

Fig. 9—An internal view of the power and impedance monitor.

is an internal view showing the voltage and current pickups.

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APPENDIX I

Consider a transmission line of characteristic impedance \( Z_0 \) terminated by a load impedance \( Z_L \). If \( Z_L \) does not equal \( Z_0 \), standing waves will appear on the line in which the line voltage (and line current) will vary periodically between maximum and minimum values. The standing-wave ratio (s.w.r.) is defined as follows:

\[
S.W.R. = \frac{E_{\text{max}}}{E_{\text{min}}} = \frac{I_{\text{max}}}{I_{\text{min}}}.
\]

The power in the load \( Z_L \) is given by the expression

\[
P_{\text{load}} = \frac{E_{\text{max}}E_{\text{min}}}{Z_0} = \frac{E_{\text{max}}^2}{Z_0} \times \frac{1}{\text{s.w.r.}} = \frac{E_{\text{min}}^2}{Z_0} \times \text{s.w.r.}
\]

Suppose that the power in the load is calculated from a measurement of line voltage. If the voltage probe is at a voltage maximum, the computed power is

\[
P_{\text{max}} = \frac{E_{\text{max}}^2}{Z_0}.
\]

The error in power determination (relative to the true power in the load) is

\[
\frac{P_{\text{max}} - P_{\text{load}}}{P_{\text{load}}} = \frac{E_{\text{max}}^2}{Z_0} - \frac{E_{\text{min}}^2}{Z_0} \times \frac{1}{\text{s.w.r.}}.
\]

This error, in per cent, is shown by curve \( A \) in Fig. 2(a). When the probe is at a voltage minimum, the computed power is

\[
\frac{P_{\text{min}}}{P_{\text{load}}} = \frac{E_{\text{min}}^2}{Z_0}.
\]

The error in power determination is then

\[
\frac{P_{\text{min}} - P_{\text{load}}}{P_{\text{load}}} = \frac{E_{\text{max}}^2}{Z_0} \times \frac{E_{\text{min}}^2}{Z_0} \times \text{s.w.r.}.
\]

This error, in per cent, is shown by curve \( B \) in Fig. 2(a). A similar analysis, involving the line current rather than voltage, yields identical results.

If the voltage or current probe is not at a maximum or minimum point, the error in power measurement will be less than that shown by curve \( A \) or \( B \) in Fig. 2(a). Accordingly, vertical lines are drawn between curves \( A \) and \( B \) to indicate that the actual error may fall anywhere between limits given by these curves.

APPENDIX II

It has been shown that, when the combined voltage and current circuit is used as a wattmeter, it is sensitive only to energy incident upon the load. Let the incident power be \( P_I \) and the power reflected by the load be \( P_R \). Then

\[
P_{\text{measured}} = P_I,
\]

\[
P_{\text{load}} = P_I - P_R,
\]

The error in power determination (relative to the true power in the load) is

\[
\frac{P_{\text{meas}} - P_{\text{load}}}{P_{\text{load}}} = \frac{P_R}{P_I - P_R} = \frac{1}{P_R} - 1,
\]

and since

\[
P_I = \frac{[\text{s.w.r.} + 1]^2}{\text{s.w.r.} - 1},
\]

\[
P_{\text{meas}} - P_{\text{load}} = \frac{[\text{s.w.r.} - 1]^2}{4 \text{s.w.r.}}.
\]

This error, in per cent, is plotted in Fig. 2(b).
Resistor-Transmission-Line Circuits

PAUL I. RICHARDS†, ASSOCIATE, I.R.E.

Summary—Necessary and sufficient conditions are derived for a function to be the driving-point impedance of a physically realizable network consisting (essentially) of lumped resistors and lossless transmission lines. The circuits so developed are thoroughly practical for pure reactances and in many other special cases, but, in general, ideal transformers are sometimes required. A rigorous correspondence between lumped-constant circuits and line-resistor circuits is established. This correspondence immediately extends the usefulness of a wealth of theorems and techniques.

I. Introduction

Throughout this paper we shall consider networks which are composed of lumped resistors and of lossless transmission lines whose electrical lengths are commensurable. Our goals are (1) to find a method of recognizing physically realizable driving-point impedance functions for such networks, and (2) to construct at least one such circuit having a prescribed driving-point impedance. We shall thus be concerned with an extension of the well-known results of Brune in the field of lumped constants. The word "impedance" will be used throughout only in the sense of "driving-point impedance," unless otherwise stated. Except for the purely reactive circuits, it has, unfortunately, not yet been possible to eliminate ideal transformers in general, so that these, too, must be allowed in the class of circuits to be studied.

As is usual in this type of analysis, we shall find it convenient to introduce a complex frequency variable \( s = \gamma + jw \). The "real-frequency" axis is then the imaginary \( s \) axis, and it is on this line that the truly significant values of the network functions are assumed. The use of the entire complex plane, however, with the consequent extension of the functions involved, enables the use of the powerful methods of the theory of functions of a complex variable.

II. Necessary Conditions

It has been shown that any physical impedance whatever must have a positive real part in the right half-plane, \( \gamma \geq 0 \). Then our first necessary condition is

\[
R \geq 0 \quad \text{in} \quad \gamma \geq 0 \tag{1}
\]

where \( R = \text{real part of} \ Z \).

Since only transmission lines and lumped resistors (and ideal transformers) are involved in the circuit, \( Z \) will be a rational function of factors of the form \( e^{\alpha \gamma} \). Moreover, the restriction that the line electrical lengths be commensurable insures that only terms of the form \( e^{n\alpha \gamma} = (e^{\alpha})^n \) will appear, where \( \alpha \) is an appropriate fundamental phase parameter, and \( n \) is an integer. Hence, our second necessary condition is

\[
Z(s) = \text{rational function of} \ e^{\alpha \gamma}. \tag{2}
\]

III. Change of the Frequency Variable

Let us define a new frequency variable by the equation

\[
S(s) = \tanh (as/2) = \frac{e^{\alpha \gamma} - 1}{e^{\alpha \gamma} + 1} = \Gamma + j\Omega. \tag{3}
\]

We can then solve for \( e^{\alpha \gamma} = (1+S)/(1-S) \); if we substitute this value for \( e^{\alpha \gamma} \) into the impedance function, we obtain from (2)

\[
Z = \text{rational function of} \ S. \tag{4}
\]

Moreover, it is easily verified that the complex function \( S \) has a positive real part \( \Gamma \) whenever \( \gamma \geq 0 \). In other words, (3) maps the right-half of the \( s \) plane into the right-half of the \( S \) plane. Thus, from (1),

\[
R \geq 0 \quad \text{in} \quad \Gamma \geq 0. \tag{5}
\]

Of course, this mapping is not one-to-one, but the multiple-valuedness of the inverse corresponds merely to the periodicity of \( Z \) by (2).

IV. Sufficiency of (1) and (2)

Consider the new variable \( S \) as the independent frequency variable. The conditions (4) and (5) have been shown by Brune to be both necessary and sufficient for \( Z \) to be a physically realizable lumped-constant impedance.

Using Brune's method, let us develop this lumped-constant impedance. This development will, in general, yield a circuit containing inductive tees with one negative element (equivalent to a pair of perfectly coupled coils). These may be replaced, however, with inductances and ideal transformers by means of the equivalences shown in Fig. 1. The lumped circuit will then contain only positive \( L, R, C \), and ideal transformers.

Now replace each inductance \( L \) by the input of a short-circuited line of electrical length \( ac/2 \) (\( c = \) velocity...
of light) and of characteristic impedance \( L \), and replace each capacitance \( C \) by an open-circuited line of electrical length \( ac/2 \) and of characteristic impedance \( 1/C \). The result will be to replace the impedances \( L_2 \) and \( 1/C_s \) by the impedances \( L \tan (as/2) = L S \) and \( 1/C S \). Thus the lumped-constant circuit will go over into a network having exactly the required impedance, and sufficiency of (1) and (2)—or their equivalents, (4) and (5)—has been proved.

\[
\begin{align*}
L_1L_3 + L_2 + L_3L_4 + L_2L_7 &= 0 \\
L_4 &> 0, \quad L_7 < 0
\end{align*}
\]

\[
|Z_L| = \frac{V}{I}
\]

Fig. 1—Equivalents of perfectly coupled coils.

The circuit produced by the above procedure will, in general, involve the eminently impractical ideal transformer. For pure reactances and in other special cases these may be eliminated, as will be discussed later. However, no completely successful general method of elimination has yet been found.

**V. Correspondence With Lumped Circuits**

The last section shows that a completely rigorous correspondence exists between the driving-point impedances of circuits of the type under consideration and those of lumped constants. This immediately makes available a wealth of material. By use of the correspondences

\[
\begin{align*}
S \text{ (lumped nets)} & \quad s \text{ (line-resistor nets)} \\
S = \infty & \quad s = j\pi/a \\
S = 0 & \quad s = 0 \\
j\omega & \quad j \tan (\omega a/2) \\
d\omega & \quad \frac{2}{2 \cos^2 (\omega a/2)}
\end{align*}
\]

many lumped-constant theorems may be "translated" into theorems about line-resistor networks. For example, Bode's well-known "phase-area law" becomes, for line-resistor circuits,

\[
\int_{\omega=0}^{\omega=\omega_c/2} Xd (\log \tan \frac{\omega a}{2}) = \frac{\pi}{2} \left( R \left( \frac{\pi}{a} \right) - R(0) \right) \tag{7}
\]

Again, if the circuit is purely reactive,

\[
\frac{dX}{d\omega} = \frac{a}{4} \left( \frac{X}{\sin \omega a} \right) \tag{8}
\]

This correspondence may also be extended to side-circuit or transfer properties. The appropriate equivalence is shown in Fig. 2. (The line length \( ac \) appears, instead of \( ac/2 \) as before, because transfer properties are only singly periodic in line lengths while input properties are doubly periodic.) The only restriction to be imposed is that the line section must be run in the balanced condition, where the currents in the two conductors are equal and opposite. Thus, for coaxial lines, there must be no current traveling on the outer surface of the shield. With this restriction, any of our line-resistor networks can be replaced by an exactly equivalent lumped circuit. A conventional circuit analyzer may then be used, and the results translated back into terms of the true frequency merely by means of a table of tangents.

**VI. Reactive Circuits**

From the work of Brune and Foster, it is known that the equivalent lumped circuit (and hence the final network) will not contain ideal transformers if the circuit is purely reactive. This removes the greatest practical objection to the method of Section IV, but the circuit...
may not yet be in a form enabling completely shielded construction. This objection may also be removed.

Consider the impedance reduction represented by Fig. 3(a), where

\[
Z' = \frac{Z - SZ_1}{1 - \frac{Z}{Z_1}}
\]

\[Z_1 = (\text{the value of } Z \text{ at } S = 1)\]  \hspace{1cm} (9)

It may be shown that \(Z'\) will again satisfy (1) and (2) or their equivalents, (3) and (4). Moreover, it may also be shown that \(Z'\) is of lower degree than \(Z\). Thus a repetition of (9) will eventually lead to an impedance which is merely a multiple of \(S\) or \(1/S\).

An interesting reciprocity theorem applies to the canonical form of Fig. 3(b). Namely, it is easily seen from (9) that if we are required to realize a new reactance equal to \(R_3/Z\), where \(Z\) is the old reactance and \(R_3\) a (real) constant, then the new canonical circuit can be obtained from that for \(Z\) by (a) reciprocating each characteristic impedance with respect to \(R_3\), and (b) changing the final short- (open-) circuited to an open- (short-) circuited termination.

VII. Eliminating Ideal Transformers

It is known that the procedure of (9) and Fig. 3(a) will always yield a physically realizable \(Z'\) of no higher degree in \(S\) than \(Z\). (A factor \((S-1)\) will always cancel.) Moreover, \(Z'(S)\) will be of lower degree than \(Z(S)\) if, and only if, \(Z(-1) = -Z(1)\).

In view of this fact, if for all \(\omega\)

\[R \geq R_0 = \frac{1}{2}(Z(1) + Z(-1)) \geq 0,
\]

then we may remove a series resistor \(R_0\) and apply (9) to obtain a \(Z'\) of lower degree than \(Z\). If this is not possible, it may be that the same method can be applied to \(Y = 1/Z\) (removal of a shunt conductance). In general, however, both may fail. Occasionally either may succeed after a few applications of (9), but again this will not always happen. Despite the lack of generality, however, these methods are often of considerable assistance.

Any reactance of the type considered can be realized in the canonical form shown in Fig. 3(b).

In actual calculation, \(Z'\) will at first appear to be of higher degree than \(Z\). However, the factor \((S-1)\) will always cancel from numerator and denominator. This cancellation can be performed in a single step by the following device. To obtain a given coefficient in the result, add the corresponding coefficient of the original to the previous coefficient of the result. For example,

\[
\frac{S^7 + 3S^4 - 2S^3 - 2S}{S^4 + 2S^3 - 2S - 1} = \frac{S^4 + 4S^3 + 2S}{S^4 + 3S^3 + 1}.
\]

The rule may be proved by observing the results of the process of synthetic division.

Of course, the canonical form of Fig. 3(b) is not the only shielded circuit which has the prescribed reactance. For instance, a zero of \(Z\) may be removed at any stage in the procedure. The resulting circuit will then have several stubs connected in shunt across the main line. This flexibility may be of considerable assistance in meeting mechanical or other practical requirements.

\[P. \ I. \ Richards, \ "A \ special \ class \ of \ functions \ with \ positive \ real \ part \ in \ a \ half-plane," \ Duke Math. Jour., September, 1947.\]
coupling is inevitable. For example, the circuit of Fig. 4(a) has an input impedance of the minimum-resistance-minimum-reactance type. The first section of its Brune development is shown in Fig. 4(b). While the latter form would require ideal transformers in the line-resistor equivalent, the former goes into the very practical circuit shown in Fig. 5.

![Fig. 5—Line-resistor equivalent of Fig. 4(a).](image)

Thus it appears that there may be hope of eventually finding a general way of eliminating ideal transformers. The principal difficulty appears to be that the presence of an ideal transformer does not affect the mathematical form of the impedance in any easily detectable manner.

VIII. Discussion

The reader has undoubtedly noticed that the present theory derives its simplicity from two postulates defining the class of circuits studied. Without these postulates the simple statements (2) and (4) cannot be made.

The assumption that the lines are lossless is no great bar to practical application. First, these losses are well known to be extremely small and, for a host of practical problems, may be entirely neglected. Second, the following device for including small losses may be carried over from the theory of lumped circuits: Let \( r, l, g, c \) be the series resistance, series inductance, shunt conductance, and shunt capacitance, all per unit length, for a given line. Assume, as a first approximation, that for all lines in the circuit \( g/c = r/l = d \) and that \( d \) has the same value for all the lines. Then the propagation constants and characteristic impedances may be written:

\[
\sqrt{(r + ls)(g + cs)} = (s + d)\sqrt{lc} \\
\sqrt{\frac{r + ls}{g + cs}} = \sqrt{\frac{l}{c}}.
\]

Thus the circuit behavior can be reduced to the lossless case by the familiar device of changing the frequency variable. Note that this change must be made in the (true frequency) \( s \) plane and not in the (equivalent) \( S \) plane.

Our second fundamental postulate requires that the electrical lengths of the lines be commensurable. Although most engineers will feel that this is not a serious practical consideration, it ought to be mentioned that application of the theory to a noncommensurable circuit assumes not only convergence but uniform convergence.\(^6\)

The reader will note immediately that the restriction is an "unnatural" one. In truth, given two actual lines it would be impossible to determine whether their lengths were commensurable; ever-present experimental error would always limit us to a finite range of ratios, within which there would always lie both rational and irrational numbers. The reason why the mathematical theory asks a question which experiment cannot answer lies, of course, in the fact that the simple theory ignores the "smoothing" effect of discontinuity reactances arising at the junction of dissimilar lines. In general, probably no actual physical impedance will be periodic in frequency.

Yet our theory is rooted in an assumption of periodicity. The author feels that this is no serious objection to its physical meaning. A similar situation arises in lumped-circuit theory, where lead inductance, distributed capacitance, and radiation are neglected. This is unimportant for most purposes, but at the same time insures that the impedance function will not be correct for high frequencies. Yet the mathematical theory treats \( Z \) as having physical meaning beyond the frequency of visible light and, indeed, at \( s = \infty \). As usual, a theory both tractable and useful has been achieved by idealizing the physical facts in such a way that there are no heuristic difficulties or internal contradictions. It is felt that the same is true of the present theory.

\(^6\) This was pointed out by P. LeCorbeiller.
Currents Excited on a Conducting Plane by a Parallel Dipole

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Summary—An analysis is made of the distribution of magnetic field and of current on the plane surface of a perfectly conducting infinite sheet due to a driven half-wave dipole parallel to the sheet. The analysis is based on the following assumptions: (a) the axial distribution of the amplitude of the current in the dipole is cosinusoidal with respect to the midpoint; (b) the relative phase of the current in the dipole is constant; and (c) the interaction between currents on the conducting plane and in the dipole does not significantly alter the assumed distribution of the current along the dipole as this is moved relative to the plane. It is found that, independent of the distance of the dipole from the surface, the tangential magnetic field at the plane surface is everywhere perpendicular to the direction specified by the axis of the dipole, while the current in the plane is everywhere parallel to this direction. Expressions are derived for the relative amplitude and phase of the magnetic field and the current in the plane referred to the input current of the dipole. A fairly complete set of graphs is included showing the behavior of these expressions for six different distances \( b \) of the dipole from the surface; namely, \( b = 0.025, 0.05\lambda, 0.125\lambda, 0.25\lambda, 0.5\lambda \), and \( \lambda \). The validity of the initial assumptions when applied to physically possible dipoles is discussed briefly.

I. Theory

In setting up the problem it is noted that the magnetic \( B \) vector amplitude in the space surrounding an isolated dipole has only a \( \theta \) component (Fig. 1):

\[
\mathbf{B} = B_{\theta}\hat{\theta}.
\]  

(1)

Under the assumptions (a) that the length of the dipole is exactly one-half wavelength \( (2h = \lambda/2) \); and (b) that the instantaneous current at any point along the dipole is given by

\[
i = I_m \cos \beta_0 z \cos \omega t = \text{Real part} \left[ I_m \cos \beta_0 z \exp (j\omega t) \right],
\]

\[\beta_0 R \gg 1\]

(2)

In these expressions \( \rho_b \) is the reluctivity of space and equals \( 1/4\pi \times 10^4 \text{meters/ampere} \); \( r \) is the cylindrical radial coordinate of the point \( P \) at which \( B_{\theta} \) is evaluated; \( R_{1h} \) and \( R_{3h} \) are the distances between the extremities of the dipole and \( P ; \beta_0 \) is the phase constant for free space and equals \( 2\pi/\lambda \). The current amplitude in the dipole is cosinusoidally distributed with a maximum value

\[
B_{\theta} \text{ is given by }^{1}
\]

\[
B_{\theta} = \frac{jI_m}{4\pi \rho_b} \left\{ \exp (-j\beta_0 R_{1h}) + \exp (-j\beta_0 R_{3h}) \right\}.
\]  

(3)

**Fig. 1—Intermediate-zone geometry for the half-wave dipole.**

\( a = \text{radius of dipole. } d = \text{distance between input terminals.} \)

\( I_m \) at the center \( (z = 0) \), and the value zero at the extremities \( (z = \pm h = \pm \lambda/4) \). The relative phase of the instantaneous current \( i \) is constant along the conductor and equal to the phase of the instantaneous current at the midpoint. Henceforth the relative phase of current and magnetic field on the conducting surface will be referred to the constant phase of the current in the dipole.

It is important to note that (3) is perfectly general for a half-wave dipole with the assumed current distribution. For a point \( P \) in the radiation zone defined by

\[\beta_0 R \gg 1\]

\[1\text{ An as-yet-unpublished formula due to R. W. P. King. The corresponding expression for half the antenna is given by G. H. Brown, "Directional antennas," Proc. I.R.E., vol. 25, p. 145, Eq. (193); January, 1937. In the Brown formula it is necessary to set } B = 0, G = \pi/2.\]
where \( R \) is the radial distance to \( P \) in spherical coordinates, (3) can be simplified to give the usual approximate expression for the radiation field of a half-wave dipole. In the form given, however, it is valid in the induction and intermediate zones for which \( R \) is too small to satisfy the above inequality. Since the present analysis will inquire into the behavior of the field at points within a few wavelengths of the dipole, the exact expression (3) is required.

The problem can be set up with the aid of Fig. 2. The infinite, perfectly conducting surface is taken to be the \( y-z \) plane, and the half-wave dipole is parallel to the \( z \) axis with its center at the point \((b, 0, 0)\). In calculating the surface density of current on the conducting plane at a point such as \( P(0, y, z) \), the magnetic \( B \) vector is first determined at \( P \). The surface current is then determined from the boundary conditions obeyed by the \( B \) vector at the surface of a perfect conductor. It is assumed that the mutual coupling between the perfectly conducting plane and the dipole does not alter the assumed current distribution along the dipole given by (2) as the distance between the dipole and the plane is varied. A discussion of this assumption, together with those regarding the distribution of current along the dipole, will be given at the end of this paper.

In computing the \( B \) vector at \( P \), use is made of the theory of images, which proves that the combination of the perfectly conducting \( y-z \) plane and the dipole is equivalent at all points in the infinite half-space defined by \( 0 \leq x \leq \infty, y, z \) to the situation actually shown in Fig. 2. Here the infinite surface has been replaced by an image dipole exactly like the actual dipole in physical dimensions and orientation but with its center at the point \((-b, 0, 0)\). Furthermore, the currents at corresponding points in the dipole and its image are equal in amplitude but 180° out of phase.

Thus, for any point \( P(0, y, z) \) in the \( y-z \) plane of Fig. 2, a vector diagram can be drawn similar to that in Fig. 3, where the \( x-y \) plane is shown. The positive \( z \) axis is directed upward from the paper at \( 0 \). Although drawn in the \( x-y \) plane at \((0, y, 0)\) in the figure, the vector diagram actually belongs at the point \((0, y, z)\) at a distance \( z \) above the plane of the paper. The individual \( B \) vectors are oriented correctly to take account of the 180°-out-of-phase relationship of the currents on the antennas. The magnitudes \( B_{\theta_1} \) and \( B_{\theta_2} \) are equal as shown, since the dipoles carry currents of equal magnitude and \( P \) is equidistant from corresponding points on the two dipoles.

It is clear from Fig. 3 that at any point in the \( y-z \) plane the resultant \( B \)-vector amplitude is given by

\[
\begin{align*}
B_x &= B_{\theta_1} + B_{\theta_2} = 0 \\
B_y &= B_{\theta_1} + B_{\theta_2} = 2B_{\theta_1} \\
B_z &= 0.
\end{align*}
\]

(4)

Since \( B_{\theta_1} \) is drawn in the negative \( \theta_1 \) direction in Fig. 3,

\[
B_{\theta_1} = B_{\theta_1} \cos \theta_1 = -B_{\theta_1} \cos \theta_2 = -B_{\theta_1} \frac{b}{r}
\]

(5)

with \( B_{\theta_1} \) as given by (3). Noting from Figs. 2 and 3 that, in (3),

\[
B_{\theta_1} = B_{\theta_1} \sin \theta_1
\]
and using (4) and (5),

\[ B_y = - \frac{j I_m b}{2 \pi \nu_0 (b^2 + y^2)} \left\{ \exp \left[ -j \beta_0 (b^2 + y^2 + (z-h)^2)^{1/2} \right] - \exp \left[ -j \beta_0 (b^2 + y^2 + (z+h)^2)^{1/2} \right] \right\} \]

The instantaneous value of \( B_y \) is then given by

\[ (B_y)^{\text{inst}} = \text{Real part} [B_y \exp (j \omega t)] \]

with the relative amplitude \( A \) and relative phase angle \( \phi \) given by the dimensionless expressions

\[ A = \frac{2 \beta_0}{b^2 + y^2} \cos \left\{ \frac{1}{2} \left[ \beta_0 (b^2 + y^2 + (z-h)^2)^{1/2} - \beta_0 (b^2 + y^2 + (z+h)^2)^{1/2} \right] \right\} \]

\[ \phi = \frac{1}{2} \left[ \beta_0 (b^2 + y^2 + (z-h)^2)^{1/2} + \beta_0 (b^2 + y^2 + (z+h)^2)^{1/2} \right] + \frac{\pi}{2}. \]

Having thus obtained (4) and (9), which define the properties of the vector \( B \) at the perfectly conducting surface \((y-z)\) plane, the boundary condition on the tangential component of the vector \( B \) may be applied in order to determine the surface density of current on the surface. Since the vector \( B \) is wholly tangential to the surface and is directed parallel to the \( y \) axis at all points, the boundary condition can be written in a suitably specialized form as follows:

\[ \nu_0 [-\mathbf{\hat{x}}, (B_y)^{\text{inst}}] = - \mathbf{\hat{l}}^{\text{inst}} \]

where \( \mathbf{\hat{l}}^{\text{inst}} \) is the instantaneous vector density of surface current. Hence,

\[ \mathbf{\hat{l}}^{\text{inst}} = \nu_0 (B_y)^{\text{inst}} [-\mathbf{\hat{x}}, \mathbf{\hat{y}}] = \nu_0 (B_y)^{\text{inst}} \mathbf{\hat{x}} = \mathbf{\hat{l}}^{\text{inst}} \mathbf{\hat{x}} \]

or, with (9),

\[ \mathbf{\hat{l}}^{\text{inst}} = \nu_0 (B_y)^{\text{inst}} = \frac{I_m}{2 \pi \nu_0} A \cos (\omega t - \phi). \]

Thus it has been shown that at all points on the conducting plane the positive directions for \( \mathbf{\hat{B}}^{\text{inst}} \) and \( \mathbf{\hat{l}}^{\text{inst}} \) are respectively the positive \( y \) and \( z \) directions. Furthermore, these two quantities are characterized by the same relative amplitude \( A \) and angle of relative phase \( \phi \) with respect to the current on the dipole.

### II. Graphical Results

In the graphs which follow, the relative amplitude \( A \) and the relative phase angle \( \phi \) of \( \mathbf{B}^{\text{inst}} \) and \( \mathbf{l}^{\text{inst}} \) (see (10) and (11)) have been plotted against \( y \) and \( z \) in terms of the distance of the point \( P \) in wavelengths from the origin. The curves are shown only in the first quadrant of the \( y-z \) plane, since, according to (10) and (11), \( A \) and \( \phi \), and consequently \( B^{\text{inst}} \) and \( l^{\text{inst}} \), are symmetrical in both the \( y \) and \( z \) axes and hence in the origin.

![Fig. 4](image1.png)

Fig. 4—Contours of constant relative amplitude for surface current density and magnetic field on the surface; \( b = 0.125\lambda \).

A somewhat more extensive set of curves was computed for a dipole spaced one-eighth wavelength \((b = 0.125\lambda)\) from the conducting plane than for other spacings. These are shown in Figs. 4 through 7, in addition to being represented in the figures following Fig. 7. Contours of constant relative amplitude and phase (in degrees, 0° to 360°) are shown in Fig. 5.

![Fig. 5](image2.png)

Fig. 5—Contours of constant relative phase for surface current density and magnetic field on the surface; \( b = 0.125\lambda \).
A wave motion along the surface is clearly indicated by these figures. Thus, by means of appropriate contours, Fig. 6 represents instantaneous pictures of this wave motion at two time instants a quarter-period apart; i.e., Fig. 6(a) for $t = 0$, and Fig. 6(b) for $t = T/4$. The contours of constant $I_{\text{inst}}$ and $B_{\text{inst}}$ are shown as solid lines, with small numerals to indicate the relative magnitudes represented by the contours. In addition, the nodal and antinodal (crest) contours are indicated by the dotted and dashed lines, respectively. It is noteworthy that along the loci defining the antinodes the peak absolute value increases from a minimum on the $z$ axis to a maximum on the $y$ axis, these values being indicated by small numerals along the co-ordinate axes. It is for this reason that in three instances in Fig. 6(a) pairs of solid-line contours meet to form cusps whose apexes are located on antinode contours. It might be added that sufficiently close to the origin the variation of peak absolute value along the antinode contours is just the reverse of that described above; i.e., the maximum peak value lies on the $z$ axis, and the minimum on the $y$ axis. (This phenomenon is apparent from an inspection of Fig. 10, which will be described later.)

For $b = 0.125\lambda$, $t = 0$, and $t = T/4$, the expression $A \cos(\omega t - \phi)$ is shown plotted along the $z$ axis in Fig. 7 where the plus and minus signs have the same meaning as before. A curve which forms the envelope of the crests is shown dotted. This curve is simply a plot of $A$ along the $z$ axis; it appears again on Fig. 8 together with five similar curves for other values of $b$. Fig. 9 shows a similar set of curves representing the variation of the relative amplitude along the $y$ axis. As indicated on these two figures, the curves correspond to six different spacings of the dipole from the conducting plane, these spacings lying in the range $\lambda/50 \leq b \leq \lambda$. In comparing the curves it should be noted that the input current amplitude $I_m$ is the same for all curves on Figs. 8 and 9.

It appears that the relative amplitude factor $A$ decreases much more rapidly with distance from the origin along the $y$ axis than along the $z$ axis. In order to compare the curves in Figs. 8 and 9 more accurately in this respect, they are shown replotted in Fig. 10 under the assumption that $I_m$ in the dipole is so adjusted in each case that the amplitude product $I_m A$ in (9) has the same value at the origin on the conducting plane for each value of $b$. It can be seen that while the relative amplitude decreases, at first, most rapidly along the $y$ axis, the rate of decrease also falls off more rapidly. For each pair of curves there is a definite point of intersection which approaches the origin as $b$ increases. The location of a given point of intersection along the distance scale corresponds to the approximate radius of curvature of a nearly circular contour of constant amplitude (cf. Fig. 4) for the given value of $b$. It was mentioned in the dis-

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig6.png}
\caption{Contours of constant, instantaneous surface current density and magnetic field on the surface at (a) $t = 0$, and (b) $t = T/4$; $b = 0.125\lambda$.}
\end{figure}
Fig. 7—Instantaneous surface current density and magnetic field along the z-axis at $t=0$ and $t=T/4$; $b=0.125\lambda$. (The “solid” curve begins near 16; the “dashed” curve near 3.)

Fig. 8—Relative amplitude of surface current density and magnetic field along the z-axis for six values of $b$. 
Fig. 9—Relative amplitude of surface current density and magnetic field along the y-axis for six values of $b$.

Fig. 10—Comparison of the relative amplitudes of surface current density and magnetic field along the y and z axes for six values of $b$. (For each value of $b$ the "dashed" line lies below the "solid" line on the right.)
cussion of Fig. 4 that the contours of constant amplitude are of an approximately elliptical shape, with the major axis oriented along the \( z \) axis for the contours near the origin, and then along the \( y \) axis for the contours further out. Therefore, the nearly circular contour mentioned here represents the transition between these two effects.

The behavior of the relative phase (11) along the \( y \) and \( z \) axes is shown in Figs. 11 and 12. Here again curves are plotted for the same six values of \( b \) mentioned before. However, for clarity, the pairs of curves for only three values of \( b \) are shown on Fig. 11; while on Fig. 12, all six pairs of curves are plotted to an expanded scale which covers only the region within one wavelength of the origin.

It appears that all curves approach each other as the distance from the origin increases. As would be expected, it can be shown quite easily from (11) that all of the curves approach from above the asymptotic line given by

\[
\phi = \frac{2\pi}{\lambda} d + \frac{\pi}{2},
\]

\( d \) being the distance in wavelengths from the origin along either the \( y \) or \( z \) axes. Clearly the curves approach this asymptote the more rapidly, the smaller the value of \( b \).

The fact that the slopes of all curves decrease as the
origin is approached can be attributed to a phase velocity greater than the velocity of light, which increases as the origin is approached, and which becomes theoretically infinite at the origin. This can be shown quite simply in the following way. Referring to either (9) or (14), it is evident that a contour of constant phase behaves in time according to the relation

$$\omega t - \phi = \text{constant.} \quad (16)$$

Differentiating with respect to $t$,

$$\frac{d\phi}{dt} = \omega. \quad (17)$$

If $d\phi/dt$ is evaluated from (11) in terms of $dy/dt$ along the $y$ axis $(z = 0)$, and then in terms of $dz/dt$ along the $z$ axis $(y = 0)$; and if the resulting expressions are substituted in (17), and the latter is solved first for $dy/dt$ and then for $dz/dt$, expressions of the following form are obtained:

$$\frac{(V_\phi)_y}{dy} = c \cdot \frac{(b^2 + y^2 + h^2)^{1/2}}{y} \quad (18)$$

$$\frac{(V_\phi)_z}{dz} = c \cdot \frac{2}{z + h} \frac{z - h}{(b^2 + (z + h)^2)^{1/2} + (b^2 + (z - h)^2)^{1/2}} \quad (19)$$

where $(V_\phi)_y$ and $(V_\phi)_z$ are the phase velocities along the $y$ and $z$ axes, and $c$ is the velocity of light or $\omega/\beta_p$. It is at once evident that, while both expressions approach $c$ asymptotically as $y$ or $z$ becomes large, they are considerably greater than $c$ for sufficiently small values of $y$ or $z$ and become infinite at the origin.

To obtain expressions for the slopes of the curves appearing in Figs. 11 and 12, note that

$$\frac{d\phi}{dy} = \frac{d\phi/dt}{dy/dt} = \frac{\omega}{(V_\phi)_y} \quad (20)$$

and

$$\frac{d\phi}{dz} = \frac{d\phi/dt}{dz/dt} = \frac{\omega}{(V_\phi)_z}. \quad (21)$$

Therefore, as the origin is approached the phase velocity along the $y$ or $z$ axis increases, and the slope of the curve decreases, becoming zero at the origin. It is interesting to note that the $z$-axis curve for the case $b = 0.02\lambda$ has an effectively zero slope almost out to $z = 0.2\lambda$. This is a necessary consequence of (19), for, when $b^2 \ll (z - h)^2$, $(V_\phi)_z$ remains effectively infinite out to a value of $z$ which lies in the range $0 < z < h$ but which no longer satisfies the inequality

$$b^2 \ll (z - h)^2.$$ 

Thus, as $b$ approaches zero, the $z$-axis curve in Figs. 11 and 12 has a sharper and sharper elbow; and the position of this elbow approaches $z = h$. This effect is discussed later from a physical point of view.

It is also evident from Fig. 12 that as $b$ approaches zero the relative phase $\phi$ approaches $\pi$ at the origin. In order to bring out this effect even more clearly, $\phi$ from (11) is plotted as a function of $b$ in Fig. 13 for $y = z = 0$.

![Fig. 13—Relative phase of surface current density and magnetic field at the origin as a function of the distance of the dipole from the conducting plane.](image)

As before, it can be shown that this curve approaches from above the asymptote

$$\phi = \frac{2\pi}{\lambda} b + \frac{\pi}{2}, \quad (22)$$

as $b$ becomes large.

A corresponding plot at the origin of the relative amplitude $A$ as a function of $b$ is not included since such a curve would simply represent an inverse-first-power decrease, as is evident from (10) on setting $y = z = 0$.

The discussion of the graphical results is essentially complete at this point, but a few further remarks will be made on the interesting behavior of the relative amplitude $A$ and relative phase $\phi$ along the $z$ axis in the small interval $-h \leq z \leq +h$, which represents that segment of the $z$ axis directly beneath the dipole. First, since a co-sinusoidal distribution of current in the dipole was originally assumed, it might be expected that, as the distance of separation $b$ becomes smaller and smaller, a plot of the relative amplitude $A$ along the $z$ axis and in the small
range under consideration should approach a cosine curve. That this is the case can be seen from Fig. 14 where a curve, represented by \( \cos \beta \varphi \), is shown together with two of the \( z \)-axis curves of Fig. 10, namely, those for \( b = 0.02 \lambda \) and \( b = 0.125 \lambda \). The distance scale along the axis of abscissas has been expanded ten times in comparison with that on Fig. 10 in order to include only the range of present interest, namely, \( 0 \leq z \leq h = 0.25 \lambda \).

The behavior of the relative phase \( \phi \) along the \( z \) axis in the same range as \( b \) becomes very small has been discussed previously in terms of an essentially infinite phase velocity. To repeat, the phenomenon in question is represented by the effectively horizontal portion of

![Diagram](image)

Fig. 14—The relative amplitudes of surface current density and magnetic field along the \( z \) axis for \( b = 0.02 \lambda \) and \( b = 0.125 \lambda \), as compared with a cosine curve.

the \( z \)-axis curves in Figs. 11 and 12 when \( b \) becomes small.

From a physical viewpoint such an effect is to be expected since it has been assumed that the relative phase of the current along the dipole is constant, and since as \( b \) approaches zero the boundary condition (12) or (13) implies that the current along the \( z \) axis in the range \(-h \leq z \leq +h\) must be at all points oppositely directed to the current at corresponding points along the dipole.

**Conclusion**

In conclusion a few words regarding the initial assumptions are in order. These assumptions were: (a) the dipole is exactly one-half-wavelength long \( (2h = \lambda / 2) \); (b) the distribution of current amplitude along the dipole is sinusoidal with respect to its midpoint; (c) the relative phase of the current along the dipole is constant but not necessarily that of the driving voltage; and (d) the effect of mutual coupling between the dipole and the perfectly conducting plane does not invalidate these assumptions, even for very close spacings. Assumptions (b) and (c) are excellent approximations if it is assumed that the radius \( a \) of the dipole and the distance \( d \) between the input terminals (Fig. 1) are both extremely small compared to the half-length. In fact, even in the case of a physically reasonable dipole, say \( h = 25a \), the distribution of current amplitude is sinusoidal to within approximately \( \pm 3 \) per cent, and the relative phase of the current along the dipole is constant to within approximately \( \pm 3 \) degrees.

In order to discuss (d), let the infinite, perfectly conducting plane be replaced by an actual physical dipole satisfying the image characteristics. That is, consider two parallel half-wave dipoles separated a distance \( 2b \) and driven in phase opposition. For two coupled, parallel, half-wave dipoles, either or both of which may be driven, it has been shown\(^4\) that when the separation distance \( 2b \) is not too small the input self-impedance of either dipole is not appreciably changed from the value it has for an isolated half-wave dipole; and, furthermore, that the mutual impedance computed on the basis of a first-order approximation to the correct current distribution differs negligibly from that computed on the basis of a sinusoidal distribution (with respect to the midpoint). In addition, it has recently been shown\(^7\) that in the event the spacing \( 2b \) becomes small there is a gradual transition to the transmission-line case. This evidence can be interpreted as meaning that, independent of the spacing, the current distribution as assumed under (b) and (c) above is a reasonably good approximation to the actual distribution along either dipole in the presence of the other; hence, that assumption (d) is justified.

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Experimental Determination of Helical-Wave Properties

C. C. CUTLER†, ASSOCIATE, I.R.E.

Summary—The properties of the wave propagated along a helix used in the traveling-wave amplifier are discussed. A description is given of measurements of field strength on the axis, field distribution around the helix, and the velocity of propagation. It is concluded that the actual field in the helix described is slightly weaker than would be predicted from the relations presented by J. R. Pierce for a hypothetical helical surface.

Introduction

RECENT PAPERS† have described a traveling-wave tube in which the circuit consists of a helix through which a beam of electrons is passed. Equations describing the electromagnetic wave on the helix have been developed for an idealized thin helical surface. One might expect the field at a distance from a helix of finite wire size and pitch to be essentially of the form described for the idealized case, but the field would certainly be different in the vicinity of the wire. The quantity of interest in the traveling-wave tube, i.e., the longitudinal electric field for unit power propagated, might be smaller because of the increased field concentration near the wires, or greater because of the space occupied by the wires, within which there can be no field. Also, in using the equations there is a question as to what should be taken as the effective radius of the helix. Consequently, a program was undertaken to determine these factors experimentally.

Measurement of Wave Properties

The velocity of propagation on a copper helix of the size used in the 4000-Mc. traveling-wave amplifier was measured over a range of frequencies from 625 to 8220 Mc. by measuring the wavelength of the standing-wave pattern on a helix terminated by a metal plate.

In order to facilitate measurement of field strengths a scale model of the helix was made, scaling up by approximately a factor of seven, and field measurements were made at a frequency of 560 Mc. This gave a mean helix diameter of 3.38 centimeters, around which it was found possible to make measurements with electric and magnetic probes without greatly distorting the fields. The field configurations were measured using a carefully balanced dipole and a small loop antenna, such as are sketched in Fig. 1. Considerable difficulty was encountered in obtaining a balance in the dipole such that the currents on the coaxial transmission line connecting the probe did not affect the indication, but no such difficulty was experienced with the loop.

To determine the absolute value of the field strength, a waveguide, coaxial transmission line, and a helix were connected in tandem, and the impedance of each carefully matched. The fields were then compared in the three systems with the dipole and loop probes, using a bolometer detector. In order to remove any doubt as to the effect of the coaxial line associated with the probes on the field itself, a tiny gas-discharge tube, about 5 mm. in diameter, was also used to measure the axial electric field.

It was found that the field required to initiate the gas discharge was rather inconsistent but that the field strength at extinction was consistent to within 5 per cent, which was sufficiently accurate for this purpose. The comparisons were made by mounting the tube at the position to be measured, monitoring the power level with a bolometer loosely coupled to the circuit, and varying the power level at the generator. For each obser-
The charge in the tube and then slowly lowered and the level recorded at the moment the discharge ceased.

The theoretical relation between electric or magnetic field and total transmitted power for the transmission systems used is given in Appendix B.

**Discussion of Helical-Wave Properties**

From the measurements and the equations in the appendix, the following properties of the wave on a helix may be deduced:

1. It was found that the electromagnetic field clings very closely to the helix. The energy is effectively trapped, or guided, by the circuit and there is no tendency of the helix to radiate; therefore, in many applications it is not necessary to shield the helix. Fig. 2 shows the distribution of the lines of force around the helix. The calculated and measured fields are compared in Fig. 3 and Table I. The form of the field is given satisfactorily by the equations for the cylinder except for variations near the wire. The indicated circumferential electric field is stronger than calculated, probably because of difficulty in obtaining a sufficiently well-balanced dipole to discriminate against other field components. The longitudinal electric field within the helix for a given transmitted power is somewhat weaker than calculated, as indicated in Table I.

It might be expected that the propagation would depart from theory at frequencies where the wavelength approaches the length of a circumference, because the physical helix would then radiate, whereas the hypothetical surface used in the theory would not. This can be seen by considering the contribution of current elements in the circuit to the field at a distance point. In the helix the adjacent current elements are restricted to the wire, and if the circumference is equal to the wavelength they will be in phase and will contribute to give a finite field at a distance, whereas in the hypothetical surface the current elements may be taken as close as desired.

![Fig. 2—Field configurations around a helix.](image)

![Fig. 3—Electric field strength around a helix. The solid lines are theoretical and the points are experimental. The probe was moved between turns, to the right, and directly opposite a turn of wire at the left.](image)

**Table I**

<table>
<thead>
<tr>
<th>Condition</th>
<th>Calculated Value</th>
<th>Measured Value</th>
<th>Difference</th>
<th>Probe</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_x$ center of helix</td>
<td>$E_x$, 9 cm. from guide wall</td>
<td>15.6 db</td>
<td>14 db</td>
<td>-1.6 db</td>
</tr>
<tr>
<td>$E_x$ center of helix</td>
<td>$E_x$ center of guide</td>
<td>12.3 db</td>
<td>8.9 db</td>
<td>-3.4 db</td>
</tr>
<tr>
<td>$H_z$ center of helix</td>
<td>$H_z$ outer wall of guide</td>
<td>17.7 db</td>
<td>18 db</td>
<td>0.3 db</td>
</tr>
<tr>
<td>$H_\theta$ center of helix</td>
<td>$H_\theta$ outer wall of coaxial</td>
<td>5.5 db</td>
<td>5.3 db</td>
<td>-0.2 db</td>
</tr>
</tbody>
</table>

Waveguide dimensions = 1.02 cm × 38.1 cm.
Coaxial: $Z_0 = 100$ ohms, 2.54 cm. i.d. of outside conductor
Helix: Mean radius = 1.69 cm.
Wire diameter = 0.475 cm.

---

spiral in the wrong direction, and, if otherwise unstrained, only a portion of the reflected energy follows the circuit while the remainder is radiated. The reflection properties are illustrated in Fig. 5, which shows the standing wave measured near the intersection of a helix and a plane conducting sheet, at 4000 Mc. The erratic nature of the curve near the end is caused by interference between the guided and the radiated wave. Farther from the termination the curve shows the attenuation of the wave to be 0.18 db per inch, and by extrapolation to the end indicates a loss of about 0.07 db at reflection.

The question might be raised as to whether the waves described are the only ones supportable by a helix. As a result of an extensive study over a wide range of frequencies, exciting conditions, and terminating conditions, no wave other than the one described and an essentially unguided free-space wave was detected. The latter wave may be reduced to a very small amplitude by appropriate launching and care in terminating the spiral waves, or by placing the helix inside a pipe too small to support other waveguide-type modes.

**Conclusion**

These investigations indicate that the spiral-wave solution described gives reasonably accurate results in the case of an actual helix of the proportions used in the...
conducting in the helical direction normal to this. The equations are given here for reference.

**Appendix A**

*Equations for Wave Propagation on a Helix*

Twelve equations are required to define completely the wave guided by a hypothetical helical surface, i.e., a cylindrical surface conducting only in a helical direction making an angle $\Psi$ with a circumference, and non-conducting in the helical direction normal to this. The equations are given here for reference.

**Inside helix:**

$$E_z = B I_0(\gamma r) e^{i(w t - \beta z)}$$  

$$E_r = j B \frac{\beta}{\gamma} \frac{I_1(\gamma r)}{I_0(\gamma r)} e^{i(w t - \beta z)}$$  

$$E_\phi = -B \frac{I_0(\gamma a)}{I_1(\gamma a)} \frac{1}{\cot \psi} I_1(\gamma r) e^{i(w t - \beta z)}$$  

$$H_z = -j B \frac{\beta}{\gamma} \frac{I_0(\gamma a)}{I_1(\gamma a)} \frac{1}{\cot \psi} I_0(\gamma r) e^{i(w t - \beta z)}$$  

$$H_r = B \frac{\beta}{\gamma} \frac{I_0(\gamma a)}{I_1(\gamma a)} \frac{1}{\cot \psi} I_1(\gamma r) e^{i(w t - \beta z)}$$  

$$H_\phi = j B \frac{\beta}{\gamma} \frac{I_1(\gamma r)}{I_0(\gamma r)} e^{i(w t - \beta z)}.$$  

**Outside helix:**

$$E_z = B \frac{I_0(\gamma a)}{K_0(\gamma a)} K_0(\gamma r) e^{i(w t - \beta z)}$$  

$$E_r = j B \frac{\beta}{\gamma} \frac{I_0(\gamma a)}{K_0(\gamma a)} K_1(\gamma r) e^{i(w t - \beta z)}$$  

$$E_\phi = -B \frac{I_0(\gamma a)}{K_1(\gamma a)} \frac{1}{\cot \psi} K_1(\gamma r) e^{i(w t - \beta z)}$$  

$$H_z = j B \frac{\beta}{\gamma} \frac{I_0(\gamma a)}{K_1(\gamma a)} \frac{1}{\cot \psi} K_0(\gamma r) e^{i(w t - \beta z)}$$  

$$H_r = B \frac{\beta}{\gamma} \frac{I_0(\gamma a)}{K_1(\gamma a)} \frac{1}{\cot \psi} K_1(\gamma r) e^{i(w t - \beta z)}$$  

$$H_\phi = -j B \frac{\beta}{\gamma} \frac{I_1(\gamma r)}{K_0(\gamma r)} K_1(\gamma r) e^{i(w t - \beta z)}.$$  

Where $I_0, K_0, I_1,$ and $K_1$ are modified Bessel functions $\eta = 120 \pi$ ohms, $\beta = \omega / v, \beta_0 = \omega / c, \gamma^2 = \beta^2 - \beta_0^2$, $a$ is the radius of the helix, $v$ is the axial velocity, $c$ is the velocity of light, and $\omega$ is the radian frequency.

The factor $\gamma$ may be obtained from the circuit dimensions by the relation

$$\gamma = \beta \frac{1}{\tan \beta z}.$$  

Fig. 1 shows $\beta_0 / \gamma \cot \Psi$ plotted against $\beta a \cot \Psi$ for this expression. Making the approximation of a wave propagating slowly compared with the speed of light, so that $\beta$ and $\gamma$ are nearly equal, and $\beta / \beta_0$ is nearly equal to $\cot \Psi$, the equations may be simplified further.

**Appendix B**

*Formulas Relating Fields to Transmitted Power*

Associated with any transmitted wave, there is a certain transmitted power $P$. At any point in the field of such a wave the quantities $E^2 / P$ and $H^2 / P$, where $E$ and $H$ are any components of the field, are properties only of the geometry of the field. They have dimension of ohm cm.$^{-2}$ and mho cm.$^{-2}$ if $E$ and $H$ are volts per centimeter and amperes per centimeter. These quantities have been evaluated for the transmission systems described in this paper in order to relate the fields in the transmission systems used.

**Equations Relating Field and Power in the Transmission Systems Compared**

*Helical cylinders:* 

$$\frac{E_z^2}{P} = \frac{\gamma^4}{\beta^2} F^2(\gamma a)$$  

$$\frac{H_z^2}{P} = \frac{\gamma^6}{\beta^2 \beta_0^2} \frac{I_0^2(\gamma a)}{I_1(\gamma a)} \frac{1}{\cot^2 \psi} F^2(\gamma a),$$  

where

$$F^2(\gamma a) = \frac{(\gamma a)^2}{240} \left[ (I_1^2 - I_0 I_2) \left( 1 + \frac{I_0 K_1}{I_1 K_0} \right) \right.  

\left. + \left( \frac{I_0}{K_0} \right)^2 (K_0 K_2 - K_1^2) \left( 1 + \frac{I_0 K_1}{K_1 K_0} \right) \right].$$  

*Coaxial line,* at radius $r$ from axis of symmetry of line of characteristic impedance $R$ ohms:

$$\frac{E_z^2}{P} = \frac{\eta^2}{2\pi^2} \frac{1}{r^2 R}$$  

$$\frac{H_z^2}{P} = \frac{1}{2\pi^2} \frac{1}{r^2 R}.$$  

*TE$_{10}$ rectangular wave guide,* cross section $a$ and $b$ with field measured at distance $x$ from side of guide:

$$\frac{E_x^2}{P} = \frac{\lambda g}{\lambda ab} \frac{1}{\sin^2 \frac{\pi x}{a}}$$  

$$\frac{H_x^2}{P} = \frac{\lambda g}{\eta ab} \frac{1}{\cos^2 \frac{\pi x}{a}}.$$
A Tunable Vacuum-Contained Triode Oscillator for Pulse Service*

C. E. FAY†, SENIOR MEMBER, I.R.E., AND J. E. WOLFE‡, SENIOR MEMBER, I.R.E.

Summary—A tunable push-pull triode oscillator is described in which the vacuum-tube components and the entire r.f. portion of the oscillator circuit are contained in an evacuated metallic envelope. A terminal is provided for coaxial output into a 50-ohm transmission line. The oscillator was developed for the frequency range of 390 to 435 Mc. and is tunable by mechanical means continuously through this range. Pulse power of above \( \frac{1}{2} \) megawatt is obtained with pulse voltages of 15 to 17 kilovolts applied.

It seemed to the authors that the best answer to the problem lay in designing an oscillator in which both the tube electrodes and the rest of the oscillatory circuit were inside the vacuum-retaining envelope, as in the magnetrons. One tube employing these general principles has already been described. A the one about to be described here has some additional features which are believed to be of considerable advantage.

INTRODUCTION

The production of high pulse power for radar purposes at frequencies below approximately 600 megacycles was a problem to which considerable of the war effort was devoted. The development of the multicavity magnetron solved the problem of high pulse power very satisfactorily for frequencies higher than this value, but the size of the magnetron and its difficulties at lower frequencies became burdensome, especially when the necessary magnetic field was considered.

The use of conventional triodes in multtube circuits was an obvious expedient which was resorted to in early radar developments because tubes designed particularly for pulse service were not then available. It was found in such cases that circuit difficulties were paramount and that it was difficult to obtain reasonable efficiency at frequencies above about 200 megacycles. Tubes designed for higher power were, of necessity, larger and hence more difficult to operate at high frequencies.

Since so much of the radio-frequency circuit was unavoidably contained within the tube, attention was given to improving the connections to the tube electrodes with the object of reducing the inductance and radio-frequency resistance of the leads. Several tubes have been described which incorporated these improvements. An additional difficulty in obtaining high pulse power is sparkover in the oscillator circuit resulting from the high peak voltages encountered.

The development of this tube, which is known as the 7C22, was undertaken by the Bell Telephone Laboratories, Inc., at the request of and under contract with the Bureau of Ships of the U. S. Navy. It has resulted in an oscillator in packaged form which is very rugged and easy to handle. The specifications called for peak pulse power of approximately \( \frac{1}{2} \) megawatt at a frequency of a little above 400 Mc. from an oscillator tunable over about a 7 per cent frequency range, the pulse length to be at least 5 microseconds and the duty cycle to be 0.001.

In a tube for high peak power it is advantageous to operate at as high a plate voltage as possible in order to keep cathode-emission requirements down. At the time of this development, pulse generators or modulators were available which would deliver up to 20-kv. pulses. It was therefore decided to design for a pulse plate voltage of 15 kv. to 20 kv. This then required that, with a push-pull oscillator, cathode emission of approximately 150 amperes per cathode must be provided. With other than oxide-coated cathodes, this amount of emission would require almost a prohibitive amount of heating power (more than 1.5 kw. per tube). Since oxide cathodes were by this time performing fairly satisfactorily in magnetrons and also in some pulse amplifier or modulator tubes, this type was chosen.

The structure is shown schematically in Fig. 1, and a section drawing is given in Fig. 2. Electrically, it is a push-pull Colpitts-type oscillator operating with "grounded anode." The outer metallic shell is the vacuum-retaining envelope and also the anode terminal. The two sets of vacuum-tube elements are disposed at opposite ends of the cylindrical shell. The grids are mounted on a metallic sleeve concentric with the outer shell, and the cathodes on a smaller sleeve concentric with the grid sleeve. One heater terminal is connected

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† Bell Telephone Laboratories, Inc., New York, N. Y.
‡ Formerly, Bell Telephone Laboratories, Inc.; now, Kansas State College, Manhattan, Kan.

to the cathode sleeve and the other is a rod inside the cathode sleeve and insulated therefrom by ceramic bushings. The heaters are helices of tungsten wire which transfer heat to the cathodes by radiation. The sleeves are supported from each other and from the outer shell by means of ceramic insulators located at the center of the structure, which is at a r.f. voltage node.

Fig. 1—(a) Schematic section of the 7C22 oscillator. (b) Equivalent Circuit of the 7C22 oscillator compared to the conventional Colpitts circuit.

Tuning is accomplished by means of plates attached to sylphon bellows at each end of the structure which may be advanced and withdrawn by rotating a gear. The output is obtained from a coupling loop in the center of the grid-anode space which is connected to a concentric-line terminal. The cathode, heater, and grid terminals are at the center of the structure opposite the output terminal. The structure is cooled by means of air directed through the circular radiating fins appearing adjacent to the anode surfaces.

Mode of Operation

To consider the mode of operation of this device, the schematic shown in Fig. 1(b) represents half the tube broken at the center line. As stated previously, the basic circuit is the Colpitts oscillator, where, in this instance, the capacitances of the circuit are mainly the tube interelectrode capacitances. The short sections of transmission line \( L_{pg} \) and \( L_{ce} \) may be considered to be short-circuited by the center line, and, since these lines are physically short \([<\lambda/4]\), they may be considered as inductances. In the conventional Colpitts oscillator the frequency is given by

\[
f = \frac{1}{2\pi \sqrt{L_{pg} \left( C_{pv} + \frac{C_{pg}C_{pe}}{C_{gc} + C_{pe}} \right)}}
\]

where \( C_{pg} \) is the main capacitance component. The excitation ratio is \( C_{pe}/C_{pv} \), which is the ratio of voltage at the plate to voltage at the grid with reference to the cathode. In the device shown here, \( C_{gc} \) must be considered as divided into two parts in parallel. One part resonates with \( L_{pg} \) at the operating frequency to provide effectively a \( \lambda/4 \) choke between cathode and ground as represented by the center line. The other part is the effective \( L_{pg} \) used in determining the excitation ratio and which appears in the expression for frequency.

Tuning is accomplished by varying \( C_{pe} \) effectively. This is done by advancing or withdrawing the capacitor plate attached to the sylphon bellows at the end of the structure. Actually, this capacitance has in series with it an amount of inductance resulting from the length of the circuit through the bellows and around the cavity to the anode. If this inductive reactance is kept low compared to the capacitive reactance, no difficulty is experienced, the only result being that a somewhat smaller variation of capacitance is required for a given tuning range compared to that required if no series inductance were present. Ordinarily, the Colpitts oscillator may be tuned by varying capacitance between grid and plate without affecting the excitation ratio, \( C_{pe}/C_{gc} \). In this oscillator, however, this is not quite true, since more of the actual \( C_{pe} \) is required to resonate \( L_{pg} \) as the frequency is lowered, and hence less of \( C_{gc} \) is left to act in determining excitation. For the frequency range involved here, however, the effect is not serious, since the excitation ratio can vary considerably with very little effect on the output and efficiency, particularly where self-bias is employed.

In order to provide the required output at the desired plate voltage, it is necessary that the capacitance \( C_{pe} \) have a certain minimum value. The reason for this will be apparent from the following analysis:

In the Colpitts oscillator, the output electrodes of the tube (plate-cathode) are connected across the capacitance \( C_{pe} \). The excitation is obtained from the voltage across the capacitance \( C_{gc} \) (Fig. 1(b)). Since the circuit is resonant at the frequency of oscillation, in the absence of load resistance the voltage across \( C_{gc} \) will be just \( 180^\circ \) out of phase with the voltage across \( C_{pe} \) if the cathode is taken as the reference point. The circulating current \( I_0 \) flowing through \( C_{pe} \) and \( C_{gc} \) will be given by

\[
I_0 = E_{pg} \omega \Phi_{pe}, \quad \text{where } E_{pg} \text{ is the alternating plate voltage and } \omega = 2\pi \times \text{frequency of oscillation}.
\]

If, however, a resistance is introduced into the circuit by loading, usually in the inductive portion, the current through \( C_{gc} \) will differ from that through \( C_{pe} \) by the fundamental component of plate current supplied by the vacuum-tube generator. Prince\(^a\) has shown vector diagrams of these phase relationships. The phase of the voltage appearing across \( C_{pe} \) will differ from the \( 180^\circ \) relationship with that across \( C_{pe} \) by an angle \( \cot^{-1} R_0 \Phi_{pe} \), where \( R_0 \) is the

equivalent load resistance which appears across the output terminals of the tube; e.g.,

\[ R_o = \frac{E_p^2}{\text{power output}}. \]

It was desired that this tube should operate into a 50-ohm coaxial output line with a standing-wave ratio as near unity as possible, and that as little tuning as possible should be required over the frequency range of the tube. The output coupling loop and output terminal are shown in Fig. 3. The inductance of the loop is seen to be shunted by the capacitance between the center conductor and the shell of the lead. By suitably propor-

In the case of the Colpitts oscillator, this departure from 180° phase relationship is in the direction to cause the exciting voltage to lead the plate voltage. This is of advantage in overcoming some of the effects of transit time in a high-frequency oscillator. In the present case, values of \( R_0C_p \) of about 5 seem to be the minimum permissible. This may be considered to be the apparent \( Q \) of the output circuit when viewed across \( C_p \). The actual \( Q \) of the circuit defined as

\[ Q = \frac{2\pi \text{ energy stored}}{\text{energy lost/cycle}} \]

is always greater than this value because there are additional circuit elements storing energy (\( C_{gs}, C_{pp}, C_T \)). In the case of the 7C22 oscillator, the plate-cathode capacitance obtained by exposure of the cathode to anode through the grid was insufficient. Extra plate-cathode capacitance had to be provided in the form of a disk facing the edge of the anode. This disk was mounted from the cathode sleeve and extended as a spoke wheel through slots in the grid sleeve. Then, in order to provide the proper excitation ratio and also to tune the cathode line, additional grid-cathode capacitance in the form of a "hat" at the end of the cathode facing the grid-end disk was necessary. These details are shown in the section drawing in Fig. 2. They also act as heat shields at the ends of the cathode.
tuning this capacitance and inductance, it was found possible to obtain nearly full rated power at all frequencies within the tuning range of the tube when operating into a 50-ohm transmission line with a standing-wave ratio of unity.

CONSTRUCTIONAL DETAILS

A photograph of the 7C22 is shown in Fig. 4, a cut-away model in Fig. 5, and an exploded view showing its parts in Fig. 6. The cathodes of the 7C22 oscillator have a coated area of approximately 40 square centimeters each. They are heated by radiation from a helical filament enclosed by each cathode. Ordinary oxide coating was used on a nickel base roughened to improve adherence.

![Photograph of the 7C22 oscillator.](image)

![Photograph of a cut-away model.](image)

![Exploded view showing the component parts.](image)

TABLE 1

| Cathodes: |  |  
|---|---|---|
| Equipotential oxide-coated |  |  
| Approximate emission per cathode | 150 amperes |  
| Cathode-heating time | 3 minutes |  
| Heater: |  |  
| Tungsten filaments |  |  
| Nominal heater voltage | 9 volts |  
| Nominal heater current | 29.5 amperes |  
| Amplification factor of triode elements | 22 |  
| Capacitances: |  |  
| Approximate total direct capacitances measured at the terminals |  |  
| grid-anode | 53 to 65 µfd. |  
| (depending on setting of tuning gears) |  |  
| grid-cathode | 79 µfd. |  
| anode-cathode | 23 µfd. |  
| Frequency range: |  |  
| Nominal, obtained by adjustment of tuning gears | 390 to 435 Mc. |  

Maximum and Typical Operating Conditions
Plate-Pulsed

<table>
<thead>
<tr>
<th>Maximum Allowable</th>
<th>Typical Operating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plate pulse voltage*</td>
<td>18</td>
</tr>
<tr>
<td>Grid bias† (during pulse)</td>
<td>-3</td>
</tr>
<tr>
<td>Average grid current</td>
<td>8</td>
</tr>
<tr>
<td>Average plate current</td>
<td>90</td>
</tr>
<tr>
<td>Peak plate current</td>
<td>80</td>
</tr>
<tr>
<td>Duty cycle (r.f. pulse length times repetition rate)</td>
<td>0.0012</td>
</tr>
<tr>
<td>Pulse length‡</td>
<td>6</td>
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<tr>
<td>Average plate dissipation</td>
<td>1000</td>
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<tr>
<td>Average power output</td>
<td>550</td>
</tr>
<tr>
<td>Peak power output</td>
<td>550</td>
</tr>
<tr>
<td>Peak power input</td>
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</tr>
<tr>
<td>Peak efficiency</td>
<td>55</td>
</tr>
</tbody>
</table>

* Voltage from plate to cathode at the terminals of the tube.
† Obtained from combination of cathode resistor and grid resistor.
‡ The r.f. pulse length will usually be about 0.2 microsecond shorter than the plate pulse.

The grids are of novel construction, being formed from molybdenum sheets into which slots are punched. The slats remaining are then twisted 90° to the plane of the sheet. The sheet is then formed into cylindrical shape and welded, the slats running parallel to the axis. Diagonal stiffening wires are then welded to the outside surface of the formed grid. The entire grid is gold-plated to inhibit primary emission. This type of grid has several advantages at ultra-high frequencies. Longitudinal slats provide low inductance and low resistance to the heavy r.f. currents that must flow into the grid. Punched construction eliminates many welds and so provides better electrical and thermal conductivity.

The slats, which are 0.008×0.025 inch in cross section, are weakest parallel to the surface of the grid cylinder, so that any tendency to buckle is in this direction rather than perpendicular to the grid surface where close clearances must be maintained. The normal clearance between cathode and grid is 0.050 inch. Between grid and anode it is 0.125 inch.
The grid connecting sleeve and the entire outer envelope including anodes is OFHC copper. The sylphon bellows are monel. All seals to glass are copper seals from the envelope and tungsten seals from lead wires except the output terminal, which is a copper-cup seal. A copper pinch-off exhaust tubulation is used.

**Operation**

The characteristics and ratings of the 7C22 tube are as shown in Table I. A schematic of the typical circuit connection employed is shown in Fig. 7. A noninductive grid resistor of 200 to 400 ohms and a noninductive cathode resistor of 10 to 20 ohms are recommended.

The oscillator is normally adjusted at its low-frequency limit for balance, as indicated by a minimum amount of r.f. voltage on the input leads. The position of each tuning gear is marked at this point. Then, to increase frequency, each gear is rotated in a clockwise direction as viewed from its respective end of the tube. The tube may be inserted in a mounting rack designed to provide a ganged tuning control which rotates the gears simultaneously. Such a mounting is shown in Fig. 8.

The efficiency of the 7C22 remains quite constant at about 55 per cent throughout its frequency range. If the load coupling is left unchanged, the output will be somewhat higher at the low-frequency end of the range because of the higher excitation prevailing there. The variation of frequency as a function of the turns of the tuning gears is shown in Fig. 9. An output-impedance diagram in the form devised by Rieke is shown in Fig. 10. This plot refers to the impedance of the load circuit as seen from the plane of the end of the output terminal of the 7C22. The impedances are given in terms of \( Z_0 = 50 \) ohms. It is seen from this diagram that, if a load of 50 ohms pure resistance is attached, approximately 90 per cent of the peak output will be obtained without need for tuning. Although this diagram applies for only one frequency in the range, the diagrams for other frequencies are very similar.

Since ruggedness was of prime importance, these tubes have been subjected to elaborate shock testing. Development models have withstood shocks of several hundred G's without breaking. A 50-G shock test was specified for the tube. The normal life of the 7C22 tube
as designed is in the vicinity of 500 hours. The end of life in practically all cases occurs when the active area of the cathode has been so reduced by sparking that insufficient emission is available to provide the required output. In no case has grid emission been found to be a limiting factor in pulse service. It was noted that the temperature of the cathodes increased during oscillation. This increase was about 20°C, the desired operating temperature being 800°C to 820°C. Since this increase in temperature is produced by ohmic losses in the cathode and by electron back-bombardment of the cathode, which are r.f. losses, it is a factor in reducing the efficiency of the device.

It is expected that the life of these tubes can be greatly increased by applying knowledge gained in the development of nonsparking cathodes. At the end of the development a tube was made which used a cathode type found advantageous in magnetrons. The life of this tube was about 100 per cent longer than that of previous tubes tested. Extension of this oscillator design to higher and also to lower frequencies seems feasible. The use of relatively high pulse voltages postpones the limitations caused by transit time of electrons, but the sizes of the circuit and electrodes rapidly limit the power as the frequency is increased. At lower frequencies the main limitation would be the increasing length of the device and the resulting inconvenience of handling, plus the economic factor of having the circuit part of the expendable item.

ACKNOWLEDGMENT

As with any development produced by a large organization, many people made valuable contributions in this case. The authors wish, however, to acknowledge particularly the contribution of J. W. West in the mechanical design and assembly techniques which made this device successful.

Correspondence

Angular Frequency Shift*

In the paper by Oatlund, Vallarino, and Silver1 there was described a frequency modulator using a reactance tube in the frequency-determining circuit of the master oscillator. The expression for the angular frequency change was given as

\[ \frac{d\omega}{\omega C} = -\frac{\omega C}{\Delta C}. \]

This is based on the assumption that the actual change in angular frequency, \( \Delta\omega \), is equal to \( \frac{d\omega}{\omega C}/C \); a condition that is only met when \( \Delta C \) approaches zero. At values of \( \Delta C \) other than that zero there will be a discrepancy between the actual frequency shift and the computed value. The actual relation of angular relation of angular frequency shift \( \Delta\omega \) and \( \Delta C \) is

\[ \Delta\omega = (\omega_0 + \Delta\omega) - \omega_0 \]

\[ = \frac{1}{\sqrt{L} \sqrt{C + \Delta C}} - \frac{1}{\sqrt{LC}} \]

\[ = \frac{1}{\sqrt{L} \left( \frac{1}{\sqrt{C + \Delta C}} - \frac{1}{\sqrt{C}} \right)} \]

This shows that, contrary to the authors' statement, the frequency swing is not directly proportional to the change in injected capacitance. While the difference is negligible at small values of frequency swing, it may become large enough to constitute considerable distortion at higher modulation levels. Therefore it is necessary to select the other circuit parameters so that the non-linearity is within the permissible limit of distortion, and not to work on the assumption that the circuit is sufficiently linear for all values of \( \Delta C \).

SHERMAN RIGBY

WGHF (FM)
New York 16, N.Y.
Discussions on

“Generalized Theory of Multitone Amplitude and Frequency Modulation”*

LAWRENCE J. GIACOLETTO

A. S. Gladwin:† The general formula (equation (32) in the paper) for the components of a frequency-modulated wave was first stated, without proof, by Carson and Fry,‡ and the first published proof appears to have been given by Cherry and Rivlin.§ For calculating the amplitudes and phases of the side-frequency components, this formula is satisfactory when no linear relations exist between the modulating frequencies, but when such relations do exist, difficulties arise, as Mr. Giaccoletto has pointed out, because a number (theoretically infinite) of the terms in the general formula have coincident frequencies. When the modulating signal contains more than a few components, the labor involved in calculating the spectra by this method becomes very great. It would appear to be this consideration which has deterred the author from giving theoretical values for the spectra produced by square-wave and sawtooth-wave modulating signals.

When, however, the wave form of the modulating signal is sufficiently simple, e.g., rectangular or triangular, the spectrum may be obtained directly by Fourier analysis.

Let \( f_m(t) \) denote the modulating signal which has a peak value of 1, and let \( \Delta \omega \) be the peak frequency deviation of the modulated carrier in radians/second. Then a frequency-modulated wave can be written as

\[
\cos \left( \omega_c t + \Delta \omega \int f_m(t) \, dt \right)
\]

\[
= R \exp \left\{ \omega_c t + \Delta \omega \int f_m(t) \, dt \right\}
\]

\[
= R \exp j \omega_c t \exp j \Delta \omega \int f_m(t) \, dt
\]

where \( R \) denotes "the real part of."

Let \( f_m(t) \) be periodic with a frequency \( \omega_m \) radians/second. Then \( \int \Delta \omega f_m(t) \, dt \) is also periodic with the same frequency, and may therefore be represented by the complex Fourier series

\[
\sum_{n=-\infty}^{\infty} A_n \exp j n \omega_m t
\]

in which the coefficients \( A_n \) are given by

\[
A_n = \frac{1}{2\pi} \int_{0}^{2\pi} \exp \left( j \Delta \omega \int f_m(t) \, dt \right) \exp (-j n \omega_m t) \, d(\omega_m t)
\]

\[
= \frac{\omega_m}{2\pi} \int_{0}^{2\pi / \omega_m} \exp \left( j \Delta \omega \int f_m(t) \, dt - j n \omega_m t \right) \, dt.
\]

The frequency-modulated wave is then

\[
R \sum_{n=-\infty}^{\infty} A_n \exp j(\omega_c + n \omega_m)t.
\]

The simplest example is that in which \( f_m(t) = \cos \omega_m t \).

Then

\[
A_n = \frac{1}{2\pi} \int_{0}^{2\pi} \exp \left( j \frac{\Delta \omega}{\omega_m} \sin \omega_m t - j n \omega_m t \right) \, d(\omega_m t).
\]

This integral\¶ defines the Bessel function of the first kind of order \( n \) and argument \( \Delta \omega / \omega_m \).

Hence \( A_n = J_n(\Delta \omega / \omega_m) \), and the frequency-modulated wave is

\[
\sum_{n=-\infty}^{\infty} J_n \left( \frac{\Delta \omega}{\omega_m} \right) \cos (\omega_c + n \omega_m)t.
\]

The next simplest case is that for the rectangular modulating signal shown in Fig. 1.

The frequency-modulated wave is, therefore,
\[
\frac{1}{\pi} \frac{\Delta \omega}{\omega_m} \sum_{n=-\infty}^{\infty} \sin \left\{ \pi \alpha \left( \frac{\Delta \omega}{\omega_m} - n \right) \right\} \left( \frac{\Delta \omega}{\omega_m} - n \right) \left( \frac{\Delta \omega}{\omega_m} \alpha + n(1 - \alpha) \right) = \cos (\omega_c + n\omega_m)t.
\]

This expression is indeterminate for values of \( \Delta \omega \) equal to \( n\omega_m \) (\( n \) positive) and \( -n\omega_m(1 - \alpha)/\alpha \) (\( n \) negative), but by finding the limits as \( \Delta \omega \) approaches the critical values it is easy to show that when \( \Delta \omega = n\omega_m \) the component of frequency \( \omega_c + n\omega_m \) is \( \alpha \cos (\omega_c + n\omega_m)t \) and when \( \Delta \omega = -n\omega_m(1 - \alpha)/\alpha \) the component of frequency \( \omega_c + n\omega_m \) is \((-1)^n(1 - \alpha) \cos (\omega_c + n\omega_m)t \).

Thus the components whose frequencies correspond to the maximum and minimum frequencies of the modulated carrier have amplitudes which depend only on the mark-space ratio of the modulating wave, and are independent of the frequency deviation and the modulating frequency.

For a square-wave modulating signal, \( \alpha = \frac{1}{2} \) and (4) becomes
\[
\frac{2}{\pi} \frac{\Delta \omega}{\omega_m} \sum_{n=-\infty}^{\infty} \sin \left\{ \frac{\pi}{2} \left( \frac{\Delta \omega}{\omega_m} - n \right) \right\} \left( \frac{\Delta \omega}{\omega_m} - n \right) \left( \frac{\Delta \omega}{\omega_m} \alpha + n(1 - \alpha) \right) \cos (\omega_c + n\omega_m)t.
\]

The spectrum produced by square-wave modulation was calculated by Van der Pol\(^9\) many years ago with identical results.

A slightly more difficult example is that in which the modulating wave is triangular, as shown in Fig. 2.

---

\[ f_m(t) = -1 + \frac{\omega_m t}{\pi(1 - \alpha)} \]

and

\[ \int f_m(t) dt = \frac{\pi}{3\omega_m} (1 - 2\alpha) - t + \frac{\omega_m t^2}{2\pi(1 - \alpha)}. \]

From

\[ t = \frac{2\pi}{\omega_m} (1 - \alpha) \quad \text{to} \quad t = \frac{2\pi}{\omega_m} \]

\[ f_m(t) = \frac{2 - \alpha}{\alpha} - \frac{\omega_m t}{\pi\alpha} \]

and

\[ \int f_m(t) dt = -\frac{\pi(6 - 7\alpha + 2\alpha^2)}{3\omega_m\alpha} + \frac{2 - \alpha}{\alpha} t - \frac{\omega_m t^2}{2\pi\alpha}. \]

The constants of integration have been chosen to make the integral continuous at \( t = (2\pi/\omega_m)(1 - \alpha) \), and also to make the mean value of the integral over the period equal to zero. Then, from (2),

\[ A_n = \frac{\omega_m}{2\pi} \int_0^{2\pi(1-\alpha)/\omega_m} \exp \left\{ i\Delta\omega \left( \frac{\pi(1 - 2\alpha)}{3\omega_m} - t \right) \right\} dt \]

\[ + \frac{\omega_m}{2\pi} \int_{2\pi/\omega_m}^{2\pi(1-\alpha)/\omega_m} \exp \left\{ i\Delta\omega \left( \frac{\pi(6 - 7\alpha + 2\alpha^2)}{3\omega_m\alpha} - \frac{2 - \alpha}{\alpha} t - \frac{\omega_m t^2}{2\pi\alpha} \right) \right\} dt. \]

If, in the first integral, the substitution

\[ u = \left\{ t - \pi(1 - \alpha) \left( \frac{\eta}{\Delta\omega} + \frac{1}{\omega_m} \right) \right\}) \left( \Delta\omega \omega_m \right)^{1/2} \]

is made, the integral can be written

\[ \frac{1}{2} \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \exp \left\{ -\frac{\omega_m(1 - \alpha)}{\Delta\omega} \pi \right\} \left( \frac{\Delta\omega\omega_m}{\pi^2(1 - \alpha)} \right) \]

\[ + \frac{n^2(1 - \alpha) \omega_m}{2} \Delta\omega \left( \frac{\omega_m}{\omega_m + \eta} \right)^{1/2} \exp \left\{ \frac{\pi u^2/2}{\Delta\omega} \right\} du. \]

The integral may be expressed in terms of Fresnel's integrals \( C(x) \) and \( S(x) \), which are defined as

\[ C(x) = \int_0^x \cos \frac{\pi u^2}{2} du \quad S(x) = \int_0^x \sin \frac{\pi u^2}{2} du. \]

In terms of these functions, (6) becomes

\[ \frac{1}{2} \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \left( \cos \theta_1 - j \sin \theta_1 \right) \left( C(x_1) + C(x_2) + \sin \theta_1 \right) \left( S(x_1) + jS(x_2) \right) \]

in which

\[ \left\{ \begin{array}{l} x_1 = \left( \frac{\Delta\omega}{\omega_m} + \eta \right) \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \\ x_2 = \left( \frac{\Delta\omega}{\omega_m} - \eta \right) \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \\ \theta_1 = \pi \left( \frac{n(1 - \alpha) + 1 + \alpha \Delta\omega}{6\omega_m} + \frac{n^2(1 - \alpha) \omega_m}{2\Delta\omega} \right) \end{array} \right. \]

Similarly, the second integral in (5) can be expressed as

\[ \frac{1}{2} \left( \frac{\omega_m\alpha}{\Delta\omega} \right)^{1/2} \left( \cos \theta_2 + j \sin \theta_2 \right) \left( C(x_3) + C(x_4) - jS(x_3) - jS(x_4) \right) \]

in which

\[ \left\{ \begin{array}{l} x_3 = \left( \frac{\Delta\omega}{\omega_m} + \eta \right) \left( \frac{\omega_m\alpha}{\Delta\omega} \right)^{1/2} \\ x_4 = \left( \frac{\Delta\omega}{\omega_m} - \eta \right) \left( \frac{\omega_m\alpha}{\Delta\omega} \right)^{1/2} \\ \theta_2 = \pi \left( \frac{n\alpha + 1 + \alpha \Delta\omega}{6\omega_m} + \frac{n^2\alpha \omega_m}{2\Delta\omega} \right) \end{array} \right. \]

Substituting the value of \( A_n \) found above into (2), the frequency-modulated wave is

\[ \frac{1}{2} \sum_{n=-\infty}^{\infty} \left[ \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \right] \left( C(x_1) + C(x_2) \right) \left( \cos \theta_1 \right) \left( S(x_1) + S(x_2) \right) \sin \theta_1 \]

\[ + \left( \frac{\omega_m\alpha}{\Delta\omega} \right)^{1/2} \left( C(x_3) + C(x_4) \right) \left( \cos \theta_2 \right) \left( S(x_3) + S(x_4) \right) \sin \theta_2 \]

\[ + \frac{1}{2} \sum_{n=-\infty}^{\infty} \left[ \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \right] \left( C(x_1) + C(x_2) \right) \left( \sin \theta_1 \right) \left( S(x_1) + S(x_2) \right) \cos \theta_1 \]

\[ + \left( \frac{\omega_m\alpha}{\Delta\omega} \right)^{1/2} \left( C(x_3) + C(x_4) \right) \left( \sin \theta_2 \right) \left( S(x_3) + S(x_4) \right) \cos \theta_2 \]

\[ + \frac{1}{2} \sum_{n=-\infty}^{\infty} \left[ \left( \frac{\omega_m(1 - \alpha)}{\Delta\omega} \right)^{1/2} \right] \left( C(x_1) + C(x_2) \right) \left( \sin \theta_1 \right) \left( S(x_1) + S(x_2) \right) \cos \theta_1 \]

\[ - \left( \frac{\omega_m\alpha}{\Delta\omega} \right)^{1/2} \left( C(x_3) + C(x_4) \right) \left( \sin \theta_2 \right) \left( S(x_3) + S(x_4) \right) \cos \theta_2 \]

The amplitudes and phases of the side-frequency components can be evaluated from this formula using...
tables of the Fresnel integrals. For two special cases, namely, \( \alpha = 0 \) and \( \alpha = \frac{1}{2} \), the formula may be considerably simplified.

When \( \alpha = 0 \), Fig. 2 becomes the sawtooth wave form investigated experimentally by Mr. Giacoletto. Equation (7) then reduces to

\[
1 + \frac{(\omega_m)^{1/2}}{2} \sum_{n=-\infty}^{\infty} (C(x_1) + C(x_2))^2 \left[ (\omega_r + n\omega_m)t - \theta_1 + \phi \right]
\]

where

\[
\phi = \tan^{-1} \left( \frac{S(x_1) + S(x_2)}{C(x_1) + C(x_2)} \right).
\]

In the second case \( \alpha = \frac{1}{2} \), and the modulating signal has then a symmetrical triangular wave form. Equation (7) reduces to

\[
\frac{(\omega_m)^{1/2}}{2} \sum_{n=-\infty}^{\infty} \left( (C(x_1) + C(x_2)) \cos \theta_1 \right.
\]

\[
+ (S(x_1) + S(x_2)) \sin \theta_1 \left. \cos (\omega_r + n\omega_m)t \right]
\]

Although only rectangular-wave and triangular-wave modulating signals have been treated, it will be obvious that the spectrum produced by any modulating signal whose wave form is made up of straight lines only can be calculated by similar methods.

When the modulating signal is periodic but the wave form too complicated to allow of a simple analytical solution, the values of the coefficients \( A_n \) may be calculated from (2) by graphical or numerical integration, though for high-order side frequencies the labor is considerable.

If the modulating signal has \( K \) components and if \( 2K \) of the consecutive values of \( A_n \) have been found, it is possible to calculate the next value, and hence all the other values, by means of a recurrence formula. This formula is obtained as follows:

Let

\[
f_m(t) = \sum_{k=1}^{K} \{ a_k \cos k\omega_m t + b_k \sin k\omega_m t \}.
\]

From (2),

\[
A_n = \frac{\omega_m}{2\pi} \int_{-\infty}^{\infty} f_m(t) \exp \left( j\omega \int f_m(t) dt \right) \exp (-jnu_m t) dt.
\]

Integrating by parts,

\[
A_n = \frac{\omega_m}{2\pi} \left. \exp j \left( \omega \int f_m(t) dt - nu_m t \right) \right|_{-\infty}^{\infty} + \frac{\Delta \omega}{2\pi} \int_{-\infty}^{\infty} f_m(t) \exp \left( j\Delta \omega \int f_m(t) dt \right) \exp (-jnu_m t) dt.
\]

The first term is zero, and the second can be written by substituting for \( f_m(t) \) and \( (j\Delta \omega \int f_m(t) dt) \) according to (8) and (1):

\[
A_n = \frac{\Delta \omega}{2\pi} \int_{-\infty}^{\infty} \sum_{k=1}^{K} \{ a_k \cos k\omega_m t + b_k \sin k\omega_m t \}
\]

\[
\cdot \sum_{r=-\infty}^{\infty} A_r \exp ju_{n+k} \exp (-jnu_m t) dt.
\]

(The subscripts in (1) have here been changed from \( n \) to \( r \) in order to avoid confusion with the particular value of \( n \) being considered.)

\[
A_n = \frac{\Delta \omega}{4\pi} \int_{-\infty}^{\infty} \sum_{k=1}^{K} \sum_{r=\infty}^{\infty} \{ A_r (a_k + jb_k) \exp j(r-n-k)\omega_m t
\]

\[
+ A_r (a_k - jb_k) \exp j(r-n+k)\omega_m t \} dt.
\]

Only the terms for which \( r-n-k=0 \) or \( r-n+k=0 \) have a finite value, all others being equal to zero. Hence,

\[
2n \frac{\omega_m}{\Delta \omega} A_n = \sum_{k=1}^{K} \{ (a_k + jb_k) A_{n+k} + (a_k - jb_k) A_{n-k} \}.
\]

This formula may be used to find the coefficient \( A_{n+k} \) in terms of the \( 2K \) preceding coefficients. Like all other devices for extrapolation, the range of this recurrence formula is limited by the accuracy of the primary data.

L. J. Giacoletto. The material presented by Mr. Gladwin should be of value to anyone undertaking the calculation of frequency-modulation spectra. His method of obtaining sideband amplitude and phase can save a considerable amount of labor in those cases amenable to analytical solution. It should be pointed out, however, that in even relatively simple cases the analytic evaluation of the amplitudes of the Fourier series may be difficult. Thus, for a modulating signal composed of a fundamental and a single harmonic, the evaluation of the integral for the amplitudes of the Fourier series (equation (2) above) using known Bessel expansions merely leads to the same solution indicated by my expansion (equation (30) of the original paper). The summing of the resulting two-way series in this case and the extension of the solution for a modulating signal containing \( K \) harmonics would be a valuable contribution to frequency-modulation theory. Of course, the method of graphical or numerical integration indicated by Mr. Gladwin can be applied in any event.

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Contributors to the Proceedings of the I.R.E.

Beverly C. Dunn, Jr.

For a biography and photograph of C. C. Cutler, see page 1328 of the November, 1947, issue of the Proceedings of the I.R.E.

Beverly C. Dunn, Jr. (S'41-A'44) was born on November 16, 1917, in New York, N. Y. In 1940 he received the A.B. degree in mathematics, and in 1942, the M.A. degree in physics, from Harvard University. From 1942 through 1944 he was employed as a Teaching Fellow in the Officers Electronics Training Courses (Pre-Radar), Cruft Laboratory, Harvard University. His duties in this connection included laboratory instruction and lecturing on antennas and ultra-high-frequency circuits. During 1945 he worked as a research assistant in the antenna group at Central Communications Research Laboratory, which operated under contract between NDRC and Harvard University.

Since November, 1945, Mr. Dunn has divided his time between research in the field of electromagnetic radiation at Cruft Laboratory, the work being supported by the Navy and the Signal Corps, and graduate studies toward the Ph.D. degree in physics at Harvard. He is a member of Phi Beta Kappa, Sigma Xi, and the American Physical Society.

Clifford E. Fay (A'26-SM'45) was born on December 2, 1903, at St. Louis, Mo. He received the B.S. degree in electrical engineering from Washington University in 1925, and the M.S. degree in electrical engineering and physics in 1927. Since 1927, he has been a member of the technical staff of the Bell Telephone Laboratories, Inc., where he has been engaged in the development of high-vacuum power tubes.

A. L. Durkee was born in Cambridge, Mass., on August 24, 1905. He was graduated from Harvard University in 1930 with the B.S. degree in engineering, and joined the department of development and research of the American Telephone and Telegraph Co. in July of that year. In 1934 he transferred to the Bell Telephone Laboratories, where his work has been largely on problems associated with the development of transoceanic and other radiotelephone systems. At present he is engaged in studies relating to microwave radio relaying.

Ronold King (A'30-SM'43) was born on September 19, 1905, at Williamstown, Mass. He received the B.A. degree in 1927 and the M.S. degree in 1929 from the University of Rochester, and the Ph.D. degree from the University of Wisconsin in 1932. He was an American-German exchange student at Munich from 1928 to 1929; a White Fellow in physics at Cornell University from 1929 to 1930; and a Fellow in electrical engineering at the University of Wisconsin from 1930 to 1932. He continued at Wisconsin as a research assistant from 1932 to 1934. From 1934 to 1936 he was an instructor in physics at Lafayette College, serving as an assistant professor in 1937.

During 1937 and 1938 Dr. King was a Guggenheim Fellow at Berlin. In 1938 he became instructor in physics and communication engineering at Harvard University, advancing to assistant professor in 1939, and
entered the Radio Research Laboratory, Harvard University, where he held the position of research associate from June, 1943, to September, 1945. His work there concerned mainly the theory and design of distributed-constant filters and wide-band microwave receivers. In the fall of 1945, he entered the graduate school of Harvard University, obtaining the M.A. and Ph.D. degrees in physics in 1946 and 1947, respectively.

Dr. Richards is a member of Sigma Xi, Phi Beta Kappa, and the American Physical Society.

Ruby Payne-Scott was born in Grafton, N.S.W., Australia, on May 28, 1912. Obtaining the M.S. degree from Snyder University in 1936, she was associated with Amalgamated Wireless of Australasia from 1939 to 1941 as a radio engineer. Since 1941, she has been a member of the staff at the Radiophysics Laboratory of the Australian Council for Scientific and Industrial Research. At present she is engaged in carrying out research on radiation from the sun at meter wavelengths.

J. F. Morrison (A’29–M’36–SM’43) was born at Buffalo, N. Y., on March 14, 1906. From 1923 to 1926 he was associated with the Federal Telephone and Telegraph Company, and during 1927, with the American Telephone and Telegraph Company. Mr. Morrison was vice-president and technical director of the Buffalo Broadcasting Corporation from 1927 to 1929. Since 1929 he has been a member of the technical staff of the Bell Telephone Laboratories, assigned to the radio development and research department.

Paul I. Richards (A’45) was born at Orono, Maine, on February 8, 1923. Terminating his undergraduate work at Harvard University after his junior year, he entered the Radio Research Laboratory, Harvard University, where he held the position of research associate from June, 1943, to September, 1945. His work there concerned mainly the theory and design of distributed-constant filters and wide-band microwave receivers. In the fall of 1945, he entered the graduate school of Harvard University, obtaining the M.A. and Ph.D. degrees in physics in 1946 and 1947, respectively.

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J. Edmond Wolfe (S’40–A’41–SM’47) was born on February 21, 1917, at St. John, Kans. He received the B.S. degree in electrical engineering from Kansas State College in 1939, and the M.S. degree in 1940. From 1940 to 1941 he was an assistant in electrical engineering at the Massachusetts Institute of Technology. From 1941 to 1946, he was a member of the technical staff of the Bell Telephone Laboratories, Inc., engaged in the development of high-vacuum power tubes. In 1946, Mr. Wolfe joined the staff of the department of electrical engineering at Kansas State College, where he is now associate professor.

Gilbert Wilkes was born in Denver, Colo., in 1900. He was educated abroad and received a mechanical engineering degree in Paris, France, after World War I, followed by a graduate degree. He returned to Paris after World War II to receive the degree of doctor of engineering from the Sorbonne.

In 1926 he joined the staff of W. S. Barstow and Company, and while there sponsored the design of several steam-power plants in the United States. In 1932 he took out professional licenses in Pennsylvania and New Jersey, and opened offices as a consulting engineer, specializing in steel-mill design. He joined the staff of the Applied Physics Laboratory of the Johns Hopkins University early in 1944, where he has been concerned more particularly with radiation.

Dr. Wilkes has been the originator of several thermodynamic, metallurgical, and radiation devices, and has published several papers on these subjects.

E. L. Younker (S’42–A’45) was born in 1918 at Sidney, Ohio. He received the A.B. degree from Miami University, Ohio, in 1940, and the A.M. degree in physics from the University of Illinois in 1942. From 1942 to 1945 he was a staff member of the M.I.T. Radiation Laboratory. Since 1945 he has been employed as a member of the technical staff of the Bell Telephone Laboratories, at Whipsnay, N. J. Mr. Younker is a member of the American Physical Society.
**Institute News and Radio Notes**

**1948 I.R.E. National Convention News**

By PLANE and by train, by car and by boat, by subway and bus and pedal locomotion, thousands of radio engineers from every corner of North America and from a variety of global points of origin are now initiating plans to attend the 1948 National Convention of The Institute of Radio Engineers, to be held at the Hotel Commodore and Grand Central Palace in New York City, on March 22, 23, 24, and 25.

And wise are they who have begun such early planning. The hotel situation in New York remains acute, and reservations well in advance are advisable for those who seek desirable accommodations. Moreover, advance indications are that the same will apply to those who plan to attend technical sessions, the Radio Engineering Show, the annual banquet, president's luncheon, cocktail party—all of the recognized functions of an I.R.E. Convention, which this year promise to be more heavily attended than ever in the past.

As this is written, the technical papers program for the 1948 Convention has just been completed by Dr. Charles R. Burrows and his hard-working committee. Titles of papers scheduled and dates of presentation will be in the hands of members via a general mailing before these lines are read, and the complete program with summaries of all the papers will appear in the March issue of the PROCEEDINGS.

Ranging from a consideration of technical aspects of public telephone service on railroad trains, through practically every communications, navigation, industrial, and research topic, to health physics problems in atomic energy—the technical program covers the entire gamut of subjects of interest to workers in the radio and electronics and allied fields. Risking repetition, it is decidedly a program which no one in any way associated with these fields can afford to miss.

Further illustrative of the broad range of interests which will be catered to in this Convention is the following list of session titles:

- **Amplifiers**
- **Antennas** (two sessions; one dealing specifically with circular polarization)
- **Broadcasting and Recording**
- **Circuits** (two sessions; one dealing with active and the other with passive elements)
- **Components and Supersonics**
- **Computers** (two sessions; one covering systems and the other components)
- **Electronics** (four sessions; Tube Design and Engineering, Industrial Applications and Electronic Circuits, Tube Manufacture, and New Forms of Tubes)
- **Frequency Modulation Measurements** (two sessions; one dealing specifically with v.h.f., u.h.f., and s.h.f. measurements)
- **Microwaves**
- **Navigation Aids**
- **Nuclear Studies**
- **Propagation**
- **Receivers**
- **Superregeneration**
- **Systems (two sessions)**
- **Television**
- **Transmission (lines and waveguides)**

**Special Technical Sessions Planned**

Two high points of the technical program will be two special sessions; one devoted to "Advances Significant to Electronics," to be held on Wednesday Morning, March 21, and the other on "Nucleonics," scheduled for Tuesday evening, March 23.

Both of these meetings will be symposia, with invited papers from outstanding authorities, and both will be held in the Grand Ballroom of the Commodore, with no conflicting parallel sessions.

The "Nucleonics" symposium, sponsored by a Nuclear Science Symposium working group of the I.R.E. Nuclear Studies Committee, will be under the chairmanship of Dr. L. E. Hafstad, Executive Secretary, Research and Development Board.

The Wednesday morning meeting is expected by the Technical Program Committee to be "broadly stimulating to the electronic profession as a whole by conveying not only the important technical aspects, but also the broad implications of new scientific and technical advances." The Committee's announcement of the session continues:

"The history of progress of special branches of science, and the engineering and industry erected upon them, show that they become increasingly complex as they are subjected to the searching light of concentrated inquiry. This complexity may ultimately become a barrier to their further development unless simplifying influences are introduced.

"These simplifications usually arise from the application of broad philosophical generalizations which make the science more readily intelligible. They remove the barriers to progress by lumping detailed and complex concepts or procedures into relatively simple but more generalized ideas and methods capable of widespread understanding and application. They may appear as generalized theories, methods, or procedures."

"These are the really significant steps in the progress of a science. Their early recognition and widespread proclamation keeps the science healthy, and ensures the rapid growth of the dependent engineering and industrial arts."

Both the technical program and the plans so far disclosed by exhibitors in the Radio Engineering Show amply fulfill the prophecy carried in these pages in the January issue that this will be the greatest and most worthwhile I.R.E. Convention ever held.

Plans for a most interesting program of Women's Activities are progressing, highlighted by a trip to the United Nations by chartered bus on Tuesday, March 23, and tickets to matinee performances of either "Antony and Cleopatra," or "High Button Shoes," now playing in New York. An all-day bus trip to West Point has been arranged for Thursday, March 25, with luncheon at the Thayer Hotel.

A Tea will be held at the I.R.E. Headquarters Building, 1 East 79 Street, on Tuesday afternoon, March 23.

**Largest Radio Show on Record**

As of January 15, 163 leading radio-and-electronic manufacturers have taken 244 exhibit units, totalling 27,109 net square feet of display in the Radio Engineering Show to be held in conjunction with the 1948 Convention. The first and second floors and half of the third floor of Grand Central Palace have been entirely reserved for these exhibits. Two large session halls will occupy the third floor to share with ballrooms at the Hotel Commodore in accommodating 28 sessions for the presentation of approximately 140 technical papers during the convention.

The space taken by exhibitors already exceeds that of the 1947 Radio Engineering Show by 25 per cent. The exhibits will be technical, showing the latest developments in transmitter equipment, components and assemblies, materials and instruments which are the engineering tools and materials of electronics and radio communication.
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I.R.E. People

ALBERT R. HODGES

Albert R. Hodges (A’33-M’39-SM’43) joined Stromberg-Carlson’s patent department toward the latter part of 1947. He will handle patent prosecution and related matters in the radio and electronic field.

Mr. Hodges was born in Ridgewood, N. J., and was educated at Hamilton College and Cornell University. Formerly he was a patent attorney with the Sperry Gyroscope Company, Inc., of Great Neck, N. Y., and with the Airborne Instruments Laboratory (Columbia University Division of War Research) at Mineola, N. Y. He has served in electrical engineering capacities for General Electric, Farnsworth Television and Radio, and for Ralph H. Langley, consulting engineer.

He is a member of the Admissions Committee and the Technical Committee on Radio Receivers of the I.R.E. His booklet on radio receivers, "Better Buymanship," published in 1939, was revised in 1947.

W. A. MARRISON

The British Horological Institute's gold medal for 1947 has been awarded to Warren A. Morrison (A’28-SM’43), a member of the technical staff of the Bell Telephone Laboratories Inc., in recognition of pioneer researches in the development of the quartz crystal clock. The medal is the Institute's highest award. It was presented to Mr. Morrison by Sir Harold Spencer Jones, Astronomer Royal and president of the Institute, at its 89th annual general meeting in London on October 29, 1947.

Mr. Morrison was born in Kingston, Ontario, Canada, on May 21, 1896, and received the B.S. degree from Queens University, Kingston, in 1920, and the M.S. degree from Harvard the following year. During World War I he was a flying mechanic in the Royal Flying Corps. He has been associated with the Bell Laboratories since that time, working largely on problems of frequency standardization and time.

Charles E. Dean

Charles E. Dean (A’29-M’36-SM’43), director of publications of the Hazeltine Electronics Corporation, Little Neck, L. I., was awarded a Certificate of Commendation by the United States Navy for his work and responsibility in the writing and production of the many thorough technical instruction books required for radio equipment designed by the firm.

The certificate awarded Mr. Dean was accompanied by a citation reading in part, "This award is made for your outstanding supervision and unremitting effort.... A standard of excellence of such a high degree was achieved that these books were considered exemplary as to content, format, arrangement and usefulness by both maintenance personnel and instructors in Naval radar schools. These books covered the entire field of radar identification equipment and its interconnection with search radar and beacon equipments."
Major General George L. Van Deusen

On October 16, 1947, following a meeting of the Board of Directors of RCA Institutes, Inc., announcement was made of the election of Major General George L. Van Deusen (SM'46) as president and director of the Institutes.

General Van Deusen received the M.S. degree from Yale University and the B.S. degree from the United States Military Academy at West Point in 1909. During World War I he commanded the 105th Field Signal Battalion, 30th Division, in France and Belgium. From January, 1941, to January, 1945, he served successively as Commanding General, Signal Corps Replacement Center, Commandant, Eastern Signal Corps Schools, and Commanding General, Eastern Signal Corps Training Center at Fort Monmouth, N. J., and was awarded the Distinguished Service Medal. In January, 1945, he became Chief of the Engineering and Technical Service, Office of the Chief Signal Officer, Washington, D. C. General Van Deusen retired from the army with the permanent rank of Colonel on August 31, 1946.

RCA Institutes is a technical school devoted exclusively to instruction in radio and electrical communications and the associated electronic arts. It is stated to be the oldest school of its kind in America.

John M. Cage

John M. Cage (M'41–SM'43) has recently joined the teaching staff of the School of Electrical Engineering, Purdue University, as professor of electrical engineering in charge of electronics. Formerly, he was manager of industrial electronics at the Raytheon Manufacturing Company, where he was in charge of engineering, sales and production of industrial equipment.

Professor Cage is a native of Texas. He received his bachelor's degree at Iowa State College in 1931, and was, for eight years, associated with the General Electric Company, working on electronic research and development. For five years he was on the faculty of the University of Colorado. He is a member of the American Institute of Electrical Engineers.

Newell Arrowsmith Atwood

Commander Newell A. Atwood ('36) United States Navy, reported early in January to the New York Naval Shipyard in

N. A. Atwood

Brooklyn, New York, for duty as Electronics Officer, relieving Captain R. M. Huebl, United States Navy, who will remain as Industrial Engineering Officer.

Commander Atwood was born in Urbana, Ohio, on January 20, 1907, and received the A.B. degree from the University of Michigan in 1932, and the LL.B. degree from the George Washington University Law School. An active radio amateur since 1933, Commander Atwood has used station calls W8KOX and W3KTR. He was a member of the United States Naval Communication Reserve since 1933, and was appointed electronics engineering officer in 1946. During the war years he served with the Naval Research Laboratory, the Bureau of Ships, the Office of Naval Research, and the Norfolk Naval Shipyard. He was awarded the American Defense Medal, the American Theatre Medal, the World War II Victory Medal, the Naval Reserve Medal, and a Letter of Commendation from the Secretary of the Navy. He is a member of Delta Theta Phi Legal Fraternity and a registered patent attorney. From 1926 to 1927 he was connected with the research laboratories of the National Carbon Company, Cleveland, and from 1929 to 1936 he was on the faculty of the University of Michigan. He practiced patent law in Washington, D. C. from 1936 until he took up active navy duty in 1941.

William A. MacDonald

William A. MacDonald (A'19–M'26–SM'43), president of the Hazeltine Electronics Corporation, New York City, was recently presented the President's Certificate of Merit for his distinguished services during World War II. The text of the certificate was as follows: "The President of the United States of America awards this Certificate of Merit to William A. MacDonald for outstanding fidelity and meritorious conduct in the aid of the war effort against the common enemies of the United States and its Allies in World War II." The certificate was accompanied by a letter of transmittal pointing out his outstanding services in the field of electronics which proved to be an invaluable contribution.

Knox McIlwain

Knox McIlwain (A'31–M'40–SM'43), chief consulting engineer of the Hazeltine Electronics Corporation, Little Neck, L. I., was awarded a Certificate of Commendation by the United States Navy for his achievements during World War II. The certificate was accompanied by a citation reading, "This award is made for your outstanding supervision and great personal effort, as a Senior Department Head of the Hazeltine Electronics Corporation, in the design of test equipment which was of vital importance to the efficient and effective operation of Naval radar identification equipment."
Board of Directors

December 10, 1947

Approval of Executive Committee Action of November 11, 1947. The Board of Directors, on recommendation of the Executive Committee, approved Executive Committee actions taken on this date (a copy of which had been mailed to the Board members): (1) That the Board adopt the recommendation of the Executive Committee that a Technical Committee on Audio and Video Techniques be established to cover the standards, equipment, and other matters in that branch of the Institute, and that the Constitution and By-laws be instructed to prepare the necessary by-laws, and that Mr. Lack confer with the Chairman of the Standards Committee and any other interested committees in determination of the scope of the committee. (Unanimously approved.) (2) That the Board adopt the recommendation of the Executive Committee that the appointment of F. B. Llewellyn as the I.R.E., Representative on the ASA Electrical Standards Committee be approved. (Unanimously approved.) (3) That the Board adopt the recommendation of the Executive Committee that the President be authorized to appoint one or more representatives of the I.R.E. on the RMA Spring Meeting Committee, which is handling the Syracuse Transmitter Meeting, and that the I.R.E. absorb, with the RMA the cost of this meeting over and above the income. (Unanimously approved.)

President Baker appointed V. M. Graham, Chairman, E. A. Laport, I.R.E. Representative, and announced M. R. Briggs as RMA Representative.

Student Branch. Mr. Lack moved that the Board approve the petitions for the formation of student branches at the following schools: University of Arkansas (I.R.E. Branch); Wayne University (I.R.E.-AIEE Branch).

Citation. President Baker stated that, since this was the last meeting of the Board of Directors for 1947, he wished to express his appreciation of the fine spirit of cooperation in which the Directors had acted throughout the year. He had greatly enjoyed his association with the Board. At this point, Mr. Pratt arose and suggested that all the Directors arise to express their approval of his motion that the Board recognize the commendable leadership of President W. R. G. Baker during the year 1947, particularly his contacts with other groups and professional organizations, and for his activities in strengthening the fiscal position of the Institute. The Board arose and applauded.

Executive Committee

December 9, 1947

R.M.A. of Canada. Both R. A. Hackbusch, and S. D. Brownlee, executive secretary of the R.M.A. of Canada, have written Editor Goldsmith that the request of the I.R.E. for material from the Canadian R.M.A., for possible inclusion in the "Industrial Engineering Notes" in the Proceedings, has been favorably acted upon by the Board of Directors. The Institute has been placed on the mailing list for receipt of this material. The Editor has established the necessary routine in the Editorial Department to handle these items.

Schools of Recognized Standing. Mr. Lack moved that the President be authorized to appoint a committee to review schools which are not accredited in the Educational Directorate, Part III, of the Office of Education of the Federal Security Agency, in the following two categories: (1) schools now making applications for student branches, or from whom individual student applications are received; (2) schools which have been adopted by the Board in the past but which are not accredited in the Directory, and this committee to come up with a definite recommendation as to whether these schools should be retained, and also a ruling on all new schools. (Unanimously approved.)

I.R.E. Representatives on ASA Committees. Mr. Lack moved that the following be appointed as I.R.E. Representatives on ASA Committees: ASA Sectional Committee C-63, C. C. Chambers; ASA Sectional Committee C-42: A. B. Chamberlain.

Methods of Testing the Sound and Video Sections of Television Receivers. Copies of "Methods of Testing the Sound and Video Sections of Television Receivers" were mailed to the Television Committee and Subcommittee members November 7. At a meeting of the Television Committee held in Rochester November 19 to review this material, a new task group was established under the Television Committee to expedite final drafting of these sections. This group is presently at work and plans to complete the final draft of revisions by the end of December. Mr. Lack stated that it is proposed that this standard will be published no later than May.

ASA Electrical Standards Committee. Mr. Lack moved that the executive committee recommend to the Board that the appointment of F. B. Llewellyn as the I.R.E. Representative on the ASA Electrical Standards Committee be approved. (Unanimously approved.)

Sections Committee Chairman. Mr. S. L. Bailey moved that Alois W. Graf be appointed chairman of the Sections Committee for 1948. (Unanimously approved.)

Admissions Committee Chairman. Mr. Henney moved that George T. Royden be appointed chairman of the Admissions Committee for 1948. (Unanimously approved.)

Public Relations Committee Chairman. Mr. Henney moved that Virgil M. Graham be appointed chairman of the Public Relations Committee for 1948. (Unanimously approved.)

Educational Committee Chairman. Mr. Pratt moved that F. E. Terman be appointed chairman of the Education Committee for 1948. (Unanimously approved.)

Membership Committee Chairman. Mr. Henney moved that Beverly Dudley be appointed chairman of the Membership Committee for 1948. (Unanimously approved.)

President Baker stated that, since this was the last Executive Committee meeting of the year 1947, he wished to thank the Committee for their fine spirit of co-opera-

PROCEEDINGS OF THE I.R.E.

Annual Meeting

The Annual Meeting of The Institute of Radio Engineers will be held on March 22, 1948, at 10:30 A.M. in the Grand Ballroom of the Hotel Commodore, New York City.

I.R.E. Cincinnati Conference

The Cincinnati Section of the Institute of Radio Engineers is sponsoring its second annual Spring Technical Conference on Saturday, April 24, 1947, in Cincinnati, at the Engineering Society Headquarters Building. The Conference will feature television, and a number of prominent speakers are expected to present papers. Among other things there will be demonstrations of television receivers, and components.

Vagaries of Chance?

The Chairman of the Admissions Committee of The Institute, George T. Royden, has called attention to a remarkable coincidence, of a type unlikely to occur again for many years. It appears that C. H. Smith of Anchorage, Alaska, and W. N. Smith of Anchorage, Kentucky, were simultaneously admitted as Members of the I.R.E.! The Institute membership will welcome these gentlemen and will, it is believed, be impressed by the occasional strange vagaries of pure chance.

Industrial Engineering Notes

High-Speed Lens Developed

According to an Army announcement late in November, 1947, the fastest known high-speed all-refracting photographic lenses have been developed by Edward K. Kappel, chief of the Photographic Branch at the Squier Signal Laboratory, Fort Monmouth N. J. The relative aperture system of the new lens can be made as large as f/0.6, approaching the theoretical maximum of f/0.5, according to the Signal Corps Engineering Laboratories, and they are used in making photographs under conditions of extremely low light level. It is said that they are particularly suitable for making motion pictures of x-ray fluorescent screens and of cathode-ray tube traces.

The data on which these NOTES are based were selected, by permission, from "Industry Reports," issues of November 21, and 28, and December 5, and 12, 1947, published by the Radio Manufacturers' Association, whose helpful attitude in this matter is here gladly acknowledged.
Institute News and Radio Notes Section

Report on Army's Research Program

A summary of the Army's research and development program for both current and projected, including radio, radar, and electronic projects, was recently released by the Research and Development Division of the General Staff of the United States Army.

The 109-page booklet, entitled "War Department Research and Development Program Fiscal Year 1949," describes the Army's over-all projects for the 1949 fiscal year and briefly discusses anticipated 1950 operations.

Under current projects of applied research in the radio communications field, the Signal Corps referred to its contracts with educational institutions, commercial laboratories, and other government agencies. These include work on electron tubes; propagation studies in frequency ranges potentially suitable for radio relay equipment; research on stable filters, on detectors for f.m. sets, frequency stability and calibration accuracy in receivers, on improving the sensitivity characteristics of receivers, and on the power drain in receivers; work on antennas, and work on reduction of receiver radiation. Projects covering the development of equipment included a series of radio receivers; extremely lightweight and small range miniature v.h.f. radio transmitter-receiver sets; man-pack, short-range v.h.f. radio sets; h.f. man-pack, longer-range radio sets adaptable for vehicular mounting; and a series of l.f., i.f., and h.f. devices for mobile use and adaptable for air transportation, and relay equipment.

The report said that the Signal Corps is continuing radar research on basic theories to obtain data for increasing range, for better resolution and accuracies, for widening the frequency bands over which equipments may operate, and to develop new methods of construction and utilizing equipment. The Signal Corps also is carrying out projects looking toward the development of improved radio direction finders and navigation devices to replace those now in service.

Television studies are underway to indicate the most advantageous utilization of television pictures with the smallest possible frequency band widths. The Signal Corps also is studying methods of developing television equipment for operation under extremely low light conditions.

The Air Forces is working on detection and tracking equipment, u.h.f. communications equipment, and navigation equipment, and is co-operating with the Signal Corps and Navy Department on projects involving tubes and parts.

The research document was issued under the signature of Colonel E. A. Routhead, Chief, Research Group.

Diathermy and Industrial Frequencies Changed

The Radio Administrative Conference held last summer at Atlantic City, N. J., resulted in the first international proposal for use of frequencies by radio devices used for industrial, scientific, and medical purposes. The F.C.C. explained in announcing proposed changes in its rules governing these devices.

Under the proposed amended rules (Public Notice 14395), abandonment of the old frequencies will not be required until July 1, 1952. "However," the F.C.C. said, "it is expected that manufacturers of diathermy equipment who have already obtained type approval of equipment will wish to make the necessary minor changes in such equipment." The frequency band, the center frequency of channel, and the tolerance from the center frequency stipulated in the Atlantic City Radio Regulations are as follows:

<table>
<thead>
<tr>
<th>Assigned Band</th>
<th>Center Frequency</th>
<th>Tolerance from Center Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kilocycles</td>
<td>Kilocycles</td>
<td>Kilocycles</td>
</tr>
<tr>
<td>13,533-13,566</td>
<td>13,550</td>
<td>± 6.78</td>
</tr>
<tr>
<td>26,957-27,282</td>
<td>27,120</td>
<td>± 162</td>
</tr>
<tr>
<td>40,699-40,700</td>
<td>40,698</td>
<td>± 20.34</td>
</tr>
</tbody>
</table>

In general, the changes which apply to diathermy equipment also apply to industrial heating equipment, the F.C.C. pointed out.

F.C.C. Approves Telephone Recorders

On January 15, 1948, the F.C.C. put into effect an order approving the use of a recording device which reproduces telephone conversations. This is subject to an automatic tone warning that notifies all parties so engaged that their conversations are being recorded. The F.C.C. said that this device may be furnished or maintained by anyone, whether or not a telephone company, provided it meets certain characteristics.

Warning On Use Of Surplus Radar Equipment

A quickened interest in the use of radar equipment for training purposes in universities and other educational institutions elicited some comments from the F.C.C. recently. The Commission pointed out the possibility of interference from radar transmitters to the regular radio services, and also the necessity for securing both station and operating licenses. The radar equipments in circulation, the F.C.C. further said, are war-born devices, and not necessarily engineered to operate on frequencies in accordance with the F.C.C. table of frequency allocations. West Virginia University was the first educational institution to receive a grant from the Commission to use radar equipment for the purpose of training students in its theory and operation. This was issued at the end of November, 1947.

Second List Of Inventions Issued By OTS

Inventions for which the Government holds the right to file foreign patent applications, including more than forty electronic patents, were recently described in a second listing issued by the Office of Technical Services, United States Department of Commerce. These are devices, which individual concerns registered abroad for the general benefit of American industry, were valid.

Reports On German Developments

The universal condenser microphone, believed to be the first single-transducer unidirectional microphone to be made, and technical details on other German sound recording and reproducing equipment, are described in three reports released toward the latter part of December, 1947, by the Office of Technical Services. They are: PB-79584, German universal condenser microphone, 25 cents, PB-80572, filter design for communication systems; microfilm or photostat, $1.00, PB-69125, sound recording; reproducing and other electro-acoustic targets; microfilm, $1.00; photostat, $2.00. Four pamphlets were also issued by the OTS on German wartime telephone technology. The reports discuss coaxial cable and associated telephone and television systems, PB-1297; quadded toll cables, PB-1298; and rural telephone service and carrier telephone systems, PB-1299. All these reports and pamphlets may be purchased at the Office of Technical Services, Department of Commerce, Washington 25, D.C.

A report released toward the end of 1947 by the OTS describes the use of special ceramics in German communication equipment. Some of these are: titanium-dioxide thermistors, carbon-film fixed resistors on ceramic forms, and magnetic ceramic materials. The report, PB-79227, mimeographed, is priced at $1.00 and may also be obtained from OTS at the above address.

A new type of cathode-ray tube developed by a German inventor is capable of storing images over long periods of time. It is described in a report on sale by the OTS. The tube was developed with the idea of eliminating flicker in television pictures. Copies of the report (PB-782273) may be obtained by sending a check or money order for 75 cents, payable to the Treasurer of the United States, to the Office of Technical Services, Department of Commerce, Washington 25, D.C.

Another technical research report released by OTS describes new developments in high-current carbon lights. According to this report, the high-current carbon arc is of significant importance "to the future development of more powerful searchlights, better movie studio illumination, and improved motion picture projectors." Report (PB-81644) mimeographed, is priced at $5.75.

Study Of Solar Radio Noise

The National Bureau of Standards announced in December, 1947, that government scientists have initiated a project for the observation and analysis of radio noise generated by the sun, a companion project to cosmic radio noise studies already in progress. They will seek to determine the range of frequencies broadcast from the sun, research the intensities, and the correlation of solar noise with other solar, interstellar, and terrestrial phenomena. This investigation will be conducted at the Bureau's propagation laboratory at Sterling, Virginia.
only if registered before December 31, 1947. Government-owned patents, the OTS said, are made available to American business and industry on a royalty-free, non-exclusive licensing basis.

COMMERCIAL AND COLLEGE LABORATORIES LISTED

The National Bureau of Standards has compiled a list of 220 commercial laboratories, with 30 branches or offices, and 189 college laboratories used for research and testing as well as instruction. The list is arranged both geographically and alphabetically. Miscellaneous Publication M187, entitled Directory of Commercial and College Laboratories, may be obtained from the Superintendent of Documents, Washington 25, D. C., at 30 cents per copy.

I.R.E. ANNUAL AWARDS

The I.R.E.'s 1948 Medal of Honor has been awarded to L.C.F. Horle (A'14–M'23–F'25), chief engineer of the RCA Data Bureau, for his contributions to the radio industry in standardization work, both in peace and war, particularly in the field of electron tubes, and for his guidance of a multiplicity of technical committees into effective action. S. W. Seeley (M'40–SM'43–F'43) will receive the Morris Liebmann Memorial Prize, and W. H. Huggins (S'39–A'44) will receive the Browder J. Thompson Memorial Prize. These awards will be officially conferred upon the recipients at the 1948 I.R.E. National Convention in New York in March.

MOBILE RADIO SERVICES NEEDS

From December 8 to 12, 1947, lengthy technical hearings involving twelve issues relating to the General Mobile Services furnished the six-member Federal Communications Commission with a voluminous record of testimony regarding two-way radio communication. The witnesses represented taxicab organizations, bus companies, telephone operating concerns, and three radio manufacturing companies. The F.C.C. presented 16 exhibits including one showing a total of 617 land stations and 22,720 mobile units licensed in the General Mobile Service, Construction permits for another 607 land stations and 15,150 mobile transmitters have been issued, bringing the total authorizations to 1,224 land stations and 37,870 mobile stations. The F.C.C. has also received applications for 130 land stations and 2,810 mobile units.

Taxicab firms and bus companies are opposed to any allocation plan which requires "bulk" users in the mobile field to subscribe to a common-carrier service. They prefer a choice of service for large radio users and exclusive frequencies assigned to them. An over-all increase in the number of frequencies assigned to the General Mobile service is desired.

Throughout the hearings Commission members indicated that they thought many of the troubles of the taxi concerns could be overcome by closer co-operation and co-ordination between the users of two-way mobile radio equipment.

MEETING OF MARINE SERVICES

The executive committee of the Radio Technical Commission for Marine Services held its regular monthly meeting on December 3, 1947, in the Old State Department Building.

TELEVISION CHANNEL A

THREE-CORNERED BATTLE

All six members of the F.C.C. attended the five-day hearing, November 17 to 21, presided over by Paul A. Walker, acting chairman. Television, f.m., and mobile interests are striving to protect or better their positions in the frequency spectrum. Thirty-six companies and organizations presented their claims.

F.m. interests termed television a "luxury service," and the spokesmen for both the Zenith Radio Corporation and the Stromberg-Carlson Company, J. E. Brown (A'24–M'28–SM'34), and Lee McCanne (A'36–SM'45), respectively, urged the F.C.C. to retain the 44- to 50-Mc. band. Another of the two-score witnesses which represented the various interests believed that eventually television would absorb f.m. because of the added video interest. There were a few suggestions that television should be moved to the higher frequencies at once, but all witnesses were in substantial agreement that sharing of Television Channel No. 1 with the Mobile Services is detrimental to each service, and practically all agreed that the F.C.C. proposal concerning such interference had merits. However, there were a few strong hints and some direct statements addressed to the F.C.C. to the effect that various Government departments and agencies have been assigned more frequencies than are justified by their needs. These Governmentallocations are in reality the responsibility of the Interdepartmental Radio Advisory Commission, on which the F.C.C. has only one vote. Nevertheless, if the F.C.C. decides to abolish sharing of the proposed television channels, it is understood the Government will relinquish its frequencies in the remaining two television channels.

In general the television spokesmen conceded that twelve channels without the sharing requirement would be better than thirteen with that proviso, but that television needs additional frequencies for growth. J. E. Brown said that the 38- to 108-Mc. allocation to f.m. is entirely inadequate, based "on engineering errors and failure to consider the facts involved." Addition of a second f.m. tuning band to a radio receiver, Mr. Brown stated, would not substantially raise its cost to the public. Lee McCanne, vice-president and general manager of Stromberg-Carlson, agreed in this. Zenith has sold about 40 per cent of the industry's total a.m.-f.m. table models. StrombergCarlson produced 11 per cent of the reported industry production, pre-war and post-war, up to October 1, 1947, of 1,220,000 f.m.-a.m. receivers. Mr. McCanne testified that a recent survey of manufacturers showed a total of 635,000 sets capable of receiving the 44- to 50-Mc. band as compared to 585,000 sets capable of receiving the higher.f.m. band only. Edwin H. Armstrong (A'14–F'27) and Everett L. Dillard (A'38), FM Association president, also urged that the F.C.C. assign the lower band permanently to f.m. The FMA asked for this band for wide-area relay purposes only. The proposed channel assignment is the Allen B. DuMont Laboratories, T. T. Goldsmith (Jr. A'38–SM'46) presented detailed technical exhibits showing results of tests revealing television interference from various other services and urged the F.C.C. to give the video in the 52- to 58-Mc. band for further expansion. F. J. Bingley (A'34–M'36–SM'43), of the Philco Corporation, emphasized the fact that "television, like standard broadcasting, is designed to reach the entire American public in their homes and to furnish them with a medium of hour-by-hour education and entertainment." He opposed the F.C.C. proposal and noted that more than twelve channels should be provided to meet, among other things, the problem of the television channels available to smaller communities. Daniel E. Noble (A'25–SM'44–F'47), of Motorola, Inc., presented evidence for RTPB Panel 13 which he described as representing the users of mobile equipment. He characterized the F.C.C. proposal as "inadequate," and suggested that Channel No. 1 be set aside for the exclusive use of the Mobile Services and that the 72- to 76-Mc. band and all unoccupied adjacent channel television bands be made available to mobile equipment users to the extent to which they may be used without interference to other services.

356 F.M. STATIONS ON THE AIR END OF 1947

On December 11, 1947, F.C.C. records showed a total of 356 f.m. stations on the air. New stations are: Reading, Pa. (WEEU–FM); Meriden, Conn. (WWMV–FM); Waterloo, Iowa (KXEL–FM); Roanoke Rapids, N. C. (WGOQ–FM); Shelly, N. C. (WOHS–FM); Shelbyville, Ind. (WSRK); Paterson, N. J. (WWDX); Winston-Salem, N. C. (WSJS–FM); Suffolk, Va. (WLPM–FM); Greenfield, Wisc. (WWCF); San Francisco, Calif. (KQW–FM); Chico, Calif. (KMPC–FM); Belfaire, Ohio (WTRF–FM); Albany, Ore. (KWIL–FM); Cleveland Heights, Ohio (WSRS–FM); Roanoke, Va. (WSLS–FM); San Antonio, Tex. (KONO–FM); Port Huron, Mich. (WTHT–FM); Danbury, Conn. (WLAD–FM); Neenah, Wisc. (WNAM–FM); Poughkeepsie, N. Y. (WVA); Portland, Me. (WGAN–FM), and Roanoke, Va. (WROW–FM).

Three conditional grants for new f.m. stations, and one construction permit for a commercial television station, were issued in November, 1947. They were for Houston, Tex., Burlington, N. C., and Harding College, Memphis, Tenn. The television station is to be erected at Harding College.

EXCISE COLLECTIONS SHOW INCREASED SALES

October sales of radio sets, phonographs, and component parts, reached a new high of $5,513,134.48, in October, 1947. This, as shown by the collection of excise taxes by the United States Bureau of Internal Reve
nue, was an increase of almost 2 million dol-

ars over the September, 1947, sales which
amounted to $3,623,929.13, and more than
a half-million dollars above the October, 1946
sales, amounting to $4,996,294.00.

Tube Sales Show Increase

According to an RMA tabulation, sales of
radio receiving tubes in October, 1947,
totalled 20,343,796, an increase of 3,958,249
over September's. Cumulative sales from
January to October, 1947, inclusive, were
165,884,528.

Set Output Estimated at
Seventeen Million in 1948

A new publication of the Department of
Commerce, which is designed to furnish a
monthly summary of business information
to the trade publications and associations,
estimated recently that radio receiving set
production in 1948 is expected “to approxi-
mate the 1947 volume of about 17 million
units.”

Any loss in the production of standard
a.m. sets, the article states, “is expected
to be offset by a gain in a.m.-f.m. and tele-
vision sets. Total production of sets equipped
to receive f.m. will probably be several
million as a result of increased broadcasting
coverage. The Department estimated that
television reception in 1948 would total around
750,000 and that by the end of this
year nearly 1 million sets will be in use.

Radio-Appliance Sales at New High

The October sales figure of $193,000,000
was up 12 per cent over September and 25
per cent over October, 1946. Sales for the
year through October were up 47 per cent
over the corresponding 1946 period. Sales of
appliance and specialty wholesalers totaled
$16,306,000, a 60 per cent increase over
October, 1946, and 19 per cent over Septem-
ber of this year. Sales for 1947 through Octo-
ber were up 67 per cent over the same 1946
period.

Set Shipments Over 100 Thousand

More than 100,000 receiving sets were
exported during October, 1947, according
to the United States Department of Com-
merce. Foreign shipments of radio equip-
ment in October totalled 4,866,265 units
valued at $9,014,503, compared with
5,468,689 valued at $8,075,631 in September.
Receiving sets exported numbered 107,777
valued at $4,142,437, against 97,768 valued
at $3,514,942 in September.

October Radio, Television Output
Breaks All Industry Records

Radio set production, including television
and f.m.-a.m. receivers, broke all indus-
try records in October, an RMA tabulation of
weekly Haskins & Sells reports for the five
weeks ending October 31 revealed. For the
first time in the industry's history more
than 2,000,000 radio and television receivers
were manufactured by RMA member-com-
panies, in one month. October's record out-
put covered five working weeks, September
29 through October 31, but the average
weekly output was well above that for the
past ten months.

F.m.-a.m. sets produced in October num-
bered 151,244 and were well above the pro-
duction of any other month this year. Tele-
vision receivers manufactured also reached
a new high of 23,693, although the September
reported figure of 32,719 was higher due to
the inclusion of 16,991 sets produced earlier
but not reported. Total radio and television
set production by RMA manufacturers
numbered 2,020,303 in October and brought
the 1947 ten-month total to 14,364,218.
F.m.-a.m. sets for the ten months totalled
830,106, while television receivers for the
same period numbered 125,081. The televi-
sion set production in October represented
an increase of 110 per cent over the average
output for the previous nine months.

October f.m.-a.m. sets included 49,319
table models, 555 converters and tuners, 656
consols, and 100,714 radio-phonograph con-
soles. Television receivers included 13,503
radio table models, 10,181 consoles and ra-
dio-phonograph combinations, and 9 con-
verters.

Sales to manufacturers were 85.84 per
cent of sales in October, 1946, as compared
with the September percentage of 97.7 per
cent. September was 88.99 per cent of
those during the corresponding month last
year and about equal to the September per-
centage of 88.78.

RMA Activities

Toward the latter part of November,
chief engineer of the RMA Data Bureau, was
reappointed for a three-year period as RMA
representative on the Standards Council of
the American Standards Association. Virgil
M. Graham, associate director of the RMA
engineering department, was named alter-
nate.

RMA members received copies of the
RMA Trade Directory and Membership
List at the close of 1947. The directory also
lists division members and includes the
recently adopted and recommended war-
tants for radio parts manufacturers, and the
standard warranty for set manufacturers.
It lists all companies.

RMA director Walter Evans, of Balti-
more, Md., has been appointed a director of
JETBC, representing the National Electrical
Manufacturers Association, according to in-
formation received from NEMA. Mr. Evans
succeeds A. C. Streamer, who has retired from
NEMA activities.

L. C. F. Horle, chief engineer of the
RMA engineering department, recently in-
formed the Atomic Energy Commission,
the Navy Department, and the Army-
Navy Electronic and Electrical Standards
Agency that the RMA Data Bureau, on the
basis of requests of the armed services, is
now prepared "to operate in the field of elec-
tron tube type designation in its special ap-
lication to counter tubes." Provisions now
exist for making available to all makers of
counter tubes the type designation assign-
ment facilities of the Data Bureau.

RMA-I.R.E. Committee
MEETING IN CHICAGO

During the annual RMA mid-winter con-
ference in Chicago there was a joint meeting
of the Executive Committee and Section
Chairmen of the RMA Transmitter Division,
S. P. Taylor, of New York, presided as
chairman at the January 21 meeting. On the
same day the Executive Committee of the
Amplifier and Sound Equipment Division
held a meeting under the chairmanship of
Fred D. Wilson, of Chicago.

RMA-I.R.E. Rochester
FALL MEETINGS

New developments in the radio and elec-
tronic field were under discussion at the
RMA-I.R.E. Rochester Fall Meeting. Mem-
bers of the RMA engineering department,
members of the I.R.E., and some members
of the Canadian RMA attended the three-day
sessions which took place at the Sheraton
Hotel from November 17 through 19, under
the chairmanship of Virgil M. Graham
(A’24-M’27-F’35).

Fred S. Barton (F’35), director of Com-
munications Development for the British
Ministry of Supply and formerly director of
radio engineering for the British Air Com-
munication in Washington, was awarded
the annual citation of the Rochester Fall
Meeting "in recognition of his great accomplish-
ments in bringing about many firm and last-
ing friendships in the radio engineering pro-
fession in the United States, Canada, and
England through his unfailing good humor,
kindliness, and understanding of the other
fellow's point of view." Speaking on the
status of the radio industry in the United
Kingdom, Mr. Barton said that about 25
per cent of the industry's output is now
being exported. He exhibited an automati-
cally manufactured type of receiver which
has recently gone into production in Eng-
land.

E. Finley Carter (A’23-F’36), vice-
-president in charge of engineering of Syl-
vania Electric Products, Inc., spoke on "Engineering Responsibilities in Today's
Economy." He urged engineers to assume a
greater responsibility for the applications,
as well as for the developments, of their engi-
neering skill.

A plea for more simple designs in radio
receivers to enable the maintenance man to
make repairs more easily was made by A. C.
W. Saunders (M’47) of the Saunders Radio
and Electronic School.

RMA Meetings

The following RMA engineering meet-
ings were held:

December 2—Committee on Amplifiers
December 2—Committee on Speakers
December 2—Executive Committee
December 3—Committee on Micro-
phones
December 3—Subcommittee on Ant-
tennas
December 5—Task Group B
December 10—Subcommittee on Point-
to-Point Communication
December 16—Subcommittee on 12-Inch
Bulb Standardization
January 9—Subcommittee on Tube
Sockets
Books

**Elementary Nuclear Theory**, by H. A. Bethe


This slender volume is a set of notes on a series of twenty lectures given by Prof. H. A. Bethe to engineers and scientists of the General Electric Company, covering selected topics in the modern theory of nuclear forces from an empirical point of view. Because of the condensed lecture-note style, the book contains far more meat than its 121 pages of text would imply offhand.

The first section covers the descriptive theory of nuclei. After a brief review of basic facts about nuclei and our knowledge of their size, beta disintegration, nuclear spin and statistics, and the neutrino are described. The main portion of the book is devoted to the quantitative theory of nuclear forces. In this part the deutron is treated at some length since it enjoys in nuclear theories much the same position that the hydrogen atom holds in atomic theory. The topics covered include the physical properties of the proton, neutron, and deutron, the ground state of the deutron, scattering of neutrons by free and bound protons, interaction of the deuteron with radiation, proton-proton scattering, noncentral forces, and saturation of nuclear forces. The meson theory of nuclear forces is given only a very brief treatment, since it is not yet in a form that permits useful predictions. In the third section of the book beta disintegration and the compound nucleus are discussed. A seventeen-page table of nuclear species is given as an appendix.

In selecting his topics Professor Bethe has tried to emphasize the fundamental aspects of the theory; therefore, discussion is centered on the simplest nuclei, and topics such as fission and the theory of complicated nuclei are omitted. The theory of alpha radioactivity is also omitted, since it can be found in many of the standard texts on quantum mechanics.

The book will be of greatest value to those whose knowledge of nuclear physics was acquired some years ago and who wish to bring themselves up to date on the modern theory. For this purpose it has no rival. In addition to its value as an introduction to nuclear physics, a familiarity with the concepts and methods of quantum mechanics is assumed. Professor Bethe's lectures are clear, well-organized, and very much to the point, and the note-takers, Melvin Lax, Conrad Longmire, and Arthur S. Wightman, are to be congratulated on an excellent job.

J. B. H. KUPER
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**Principles and Practice of Electrical Engineering**, by Alexander Gray (Revised by G. A. Wallace)


This is the sixth edition of a work which first appeared in 1914; the fourth revision prepared since the death of Professor Gray in 1921.

The book was written for college students, specializing in branches other than electrical engineering, who desire a working knowledge of the principles and practice of the subject, but who have only a limited time at their disposal. Subsequent editions of the book have held to this object, seeking only to keep the subject matter up to date. In the present edition the m.k.s. system of units is introduced in addition to the use of c.g.s. units, the material on three-phase systems and the transformer have been extended, and new subjects have been included, as, for example, the amplitdye, fluorescent lamps, and vacuum tubes.

The treatment throughout is clear, concise, and interesting, with the employment of a minimum of mathematics. Particularly well done are the chapters on batteries, direct-current machinery, and control of apparatus, alternating-current machinery, and transmission. In the chapters on vacuum tubes are sketched their characteristic curves and their fundamental functions as rectifiers, amplifiers, and oscillators, but no claim is made of a detailed treatment. The emphasis of the book is on power circuits, power apparatus, and low-frequency transmission lines.

The book is copiously illustrated, the pictures of apparatus well chosen for clarifying the treatment in the text. Practical problems and test questions accompany each chapter and a short list of laboratory experiments. The book should be useful for students in general with moderate mathematical equipment. The calculus is used only sparingly.

FREDERICK W. GROVER
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**Sunspots in Action**, by Harlan True Stetson


Few books on the subject of radio, whether technical or nontechnical, give more than a cursory treatment of sunspots. Dr. Stetson, who is himself a radio engineer as well as a distinguished astronomer and a physicist, has helped to fill in this gap over a number of years in several of his books. The latest, "Sunspots in Action," extends his previous discussions and collections into a highly informative and thoroughly readable form a wealth of information covering various aspects of sunspot phenomena. The book brings together what is known about sunspots, including relevant information crossing several fields of science that bear upon the relation of the earth to its cosmic environment.

This volume is written for the intelligent layman and not for the expert, although the expert will find it to be most entertaining reading. Technical language has been held to a minimum, but this is not an indictment against the book from the point of view of the professional radio engineer. The volume contains much information which will prove useful and interesting to the most technical man.

"Sunspots in Action" is not limited to the effects of sunspots on radio communication. Dr. Stetson treats with this phase of sunspot phenomena in some detail but only as a part of a much broader approach. Throughout the book, emphasis is placed on the various effects of cosmic phenomena on the earth's atmosphere and the terrestrial consequences thereof.

The first few chapters deal with the sun, its source of energy, and its radiation. The effects of this radiation and the changes brought about by the appearance of sunspots is then covered. Sunspots themselves are discussed and various methods of predicting their appearance are surveyed. The effects of the other planets on the existence of sunspots and on the earth's atmosphere are brought into the discussion, together with material concerning the northern lights, solar eclipses, cosmic effects, and the earth's magnetism.

In addition to the chapters on sunspots and radio communication and prediction, Dr. Stetson outlines evidence available relating to effects of sunspots on the earth's atmosphere as an ultimate source of weather, on life cycles in plants and animals, and on the possible correlation of sunspots with economic trends. Some of the more plausible hypotheses in these various fields are critically examined.

This book is well worth reading not only for the broader picture of the subject which it presents but also because sunspots may well be proven to have an even more pronounced and direct effect on human life than is definitely known today.

GEORGE M. K. BAKER
RCA Laboratories Division
Radio Corporation of America
Princeton, N. J.
Patent Notes for Engineers

Published (1947) by the Radio Corporation of America, Princeton, N. J. 146 pages +14-page index+vi pages. 6 x 9 inches. Price, $2.50.

This is the first volume in the new engineering book series published by the RCA Review Department of RCA Laboratories Division. While published primarily for the use of RCA divisions and subsidiary companies, the information contained in the volume is of interest to all scientists, engineers, and attorneys concerned with patent matters.

One half of the book is given to the treatment of invention; invention in the popular sense and in the statutory sense, the nature of invention, and invention as a practical matter. Numerous illustrations and examples help to clarify and explain this important subject under each heading and sub-heading.

The remainder of the book presents a perspective of patent prosecution, records of invention, interferences, and ownership and use of patents. Sufficient treatment of each subject is given for a general understanding by the reader without becoming unduly involved in technicalities or the detailed intricacies of these patent matters.

The introduction states that these notes represent a serious effort to bridge the technical gap between engineers, research workers and inventors generally, and their patent attorneys. This small volume is indeed a step in the right direction, narrowing the gap.

No mention is made of patent approval infringement, and such other matters frequently encountered by the engineer and those concerned with production, all of which necessitate co-operation with patent counsel in behalf of the employers' interests.

This omission, however, does not detract from the value of the present work, which has such a complete table of contents and index as to assure the use of the book as a frequent reference manual.

ALFRED W. GRAF
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Men and Volts at War, by John A. Miller


When the axis powers launched the all-out emprise known as World War II, German plans were based largely upon conducting a mechanical war. When the United States joined the Allies opposing the axis, the outcome of the struggle was not long in doubt, because a mechanical war was, in the vernacular, "up our alley." Once American industry was converted to war production, the public was aware of the extent and speed of production largely through announcements of "E" awards to particular manufacturing plants or departments for excellence, or continued excellence, in production of war materials. This book deals with the war production efforts of one American manufacturing company which received a total of seventy-six "E" and "M" awards from the Government: The General Electric Company.

The book deals with research and production contributions made by this company and its subsidiaries to practically all arms of the services, and the author has done an excellent job of presenting in clear and readable text the nature of these contributions and their applications in the war theaters. If there are omissions in the text these are exclusive systems and devices produced by other manufacturers. As an authentic record of what was accomplished by industry during the war period, and what could be accomplished again should the need arise, this book should prove of direct interest to engineers, teachers, officers of the armed services, and the public in general. In the pages of this comprehensive work the reader may, perhaps for the first time, learn the manufacturing and application facts about instrumentality which were war secrets (not written about) during the war years, such as: magnetic-mine defense, degaussing measurements, the bazooka, power trains for the Soviet drive to Berlin, radiolocation in the Battle of Britain, radar countermeasures, radio for combat communication, uranium and atomic energy, and hundreds of other war developments for offense and defense in war operations. These are well organized in twenty readable chapters.

DONALD McNICOL
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Tables of Integrals and Other Mathematical Data (revised edition), by Herbert Bristol Dwight

Published (1947) by The Macmillan Company, 60 Fifth Avenue, New York, N. Y. 207 pages+2-page index+37-page appendix+viii pages. 10 figures. 5 x 8 inches. Price, $3.20.

This compact little volume contains many numerical tables of functions. These include algebraic, trigonometric, logarithmic, exponential, elliptic, hyperbolic, and Bessel functions. A well-organized table of integrals is accompanied by useful algebraic relations and many series often encountered in engineering physics. A usable index adds to the utility of the book.

GEORGE H. BROWN
RCA Laboratories
Princeton, New Jersey

Electronics and Their Application in Industry and Research, edited by Bernard Lovell


This book is the work of about a dozen authors, each one in general contributing a chapter. The editor provided an excellent introduction, particularly the section on electronics and the Second World War.

In his introduction the editor states that he purposely has excluded subjects already dealt with in many other texts and has aimed to include chiefly examples of important advances in the science which have occurred during the past few years. Thus conventional radio engineering aspects are omitted, but such subjects as infrared phototubes, the betatron, servomechanisms, and new applications in medicine and physiology are covered in considerable detail.

The book may be likened to a group of well-prepared papers presented at a meeting of a technical society. It is thus not a textbook, but should be of considerable value to engineers in the field of industrial electronics interested in new developments in England.

W. C. WHITE
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Omission in "TELEVISION—III"

Two sheets listing original publication data for the summaries contained in the appendix of Volume III of "Television," edited by Alfred N. Goldsmith, Arthur F. Van Dyck, Robert S. Burnap, Edward T. Dickey, and George M. K. Baker, have been issued by the publishers. These may be passed in the volume, thus eliminating the omission. They are obtainable by request at the Radio Corporation of America, RCA Laboratories Division, Princeton, N. J.

Notice

The new I.R.E. television standard, "Standards on Television: Methods of Testing Television Transmitters—1947," is now available. The price is $0.75 per copy, including postage to any country.

Orders may be sent to: The Institute of Radio Engineers, Inc., 1 East 79 Street, New York 21, N. Y., with remittance and address to which copies are to be sent.

Calendar of Coming Events

I.R.E. National Convention
March 22-25, 1948
Cincinnati Spring Meeting
April 24, 1948
Syracuse RMA-I.R.E. Spring Meeting
April 20-28, 1948
Chicago I.R.E. Conference
April 17, 1948
New England Radio Engineering Meeting
May 22, 1948
1948 West Coast Convention of the I.R.E.
September 30-October 2, 1948
THE NATIONAL PHYSICAL LABORATORY, TEDDINGTON, MIDDLESEX, ENGLAND

Aerial view of the main part of the Laboratory.

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J. W. McRae

Member of the Board of Editors

J. W. McRae (A'37–F'47) was born on October 25, 1910, in Vancouver, British Columbia. He received the B.S. degree in electrical engineering from the University of British Columbia in 1933, the M.S. degree in 1934 from California Institute of Technology, and the Ph.D. degree from the same institution in 1937. Earlier in the same year, he had joined the Bell Telephone Laboratories, where he engaged in research on transoceanic radio transmitters. His next assignment was in the field of microwave research, which led naturally to work on military projects, including a special microwave oscillator for the National Defense Research Committee and early association with several microwave radar projects.

Early in 1942 he accepted a commission as major in the United States Army Signal Corps and was assigned to the Office of the Chief Signal Officer in Washington, D. C. He remained in Washington for more than two years, engaged in co-ordinating development programs for airborne radar equipment and for radar countermeasures devices. He later received the Legion of Merit for his work on these programs. In June of 1944 he was transferred to the Headquarters of the Signal Corps Engineering Laboratories at Bradley Beach, N. J., as chief of the engineering staff. Some time after this he became deputy director of the Engineering Division and attained the rank of colonel before returning to civilian life at the end of 1945. Once again associated with the Bell Telephone Laboratories, he was appointed director of Radio Projects and Television Research in June of 1946, which made him responsible for work on the New York-to-Boston radio relay project as well as for research on television. With the addition of responsibility for electron-dynamics research in February, 1947, he became director of electronic and television research. He received Honorable Mention for 1943 in the Eta Kappa Nu awards for outstanding young electrical engineers. This was presented to him on January 26, 1948, at the AIEE Winter General Meeting in Pittsburgh, Pa.

Dr. McRae has been a member of the Board of Editors of the Institute since 1946, and was a member of the 1947 I.R.E. Convention Committee. He is now vice-chairman of the New York Section and a member of the Program Committee of the Technical Societies Council of New York. He is also a member of the AIEE and Sigma Xi.
Developments in Radio Sky-Wave Propagation Research and Applications During the War

J. H. DELLINGER†, FELLOW, I.R.E., AND NEWBERN SMITH†, SENIOR MEMBER, I.R.E.

Summary—This paper discusses the work done by the Interservice Radio Propagation Laboratory during World War II. The circumstances leading to the establishment of IRPL are described and the problems which are faced are stated. The measures taken in the solutions of these problems are outlined, and some of the results are presented. Specific services performed by IRPL during the war for the armed forces and commercial companies are recounted.

The influence of the ionized layers of the earth's upper atmosphere, the ionosphere, on radio wave propagation has been recognized ever since the experiments of Breit and Tuve and of Appleton proved its existence. Because of the scarcity of adequate ionospheric data, however, and because relatively few radio men realized its importance, the use of ionospheric data in radio communications before the war was relatively small.

The important part played by radio during the war brought to light the necessity for having adequate radio propagation information. No matter how good the equipment was at the transmitting and receiving ends, satisfactory communication could not be had unless the waves were propagated with sufficient strength to be receivable. Variations in propagation conditions proved to be several orders of magnitude greater than variations in transmitter power or receiver sensitivity. Furthermore, the extreme crowding of the radio-frequency spectrum made necessary full utilization of all available frequencies, and an appropriate selection of frequencies could be made only with the help of radio propagation data. Also, security considerations dictated that the frequencies used should be the best for use and the least likely to be intercepted by the enemy. The design of equipment, especially of antenna systems, was found to depend critically upon a knowledge of radio propagation conditions. In addition, other applications of radio, such as radar and direction finding, involved considerations of propagation regarding range, accuracy, and receivable intensities.

With the widespread use of radio communication by the armed forces, especially in parts of the world where but little experience had been had, the need for improved radio propagation information became apparent early in the war. An aircraft disaster in the European Theater led to the establishment of the British Inter-Services Ionosphere Bureau (ISIB) in 1941, and the exigencies of air force operation in the Southwest Pacific resulted in the formation of the Australian Radio Propagation Committee (ARPC), both instituted to furnish radio propagation data and predictions to their respective armies, navies, and air forces. Correspondingly, in 1942, the Interservice Radio Propagation Laboratory (IRPL) was established in the National Bureau of Standards by order of the U. S. Joint Chiefs of Staff, acting through the Wave Propagation Committee of the U. S. Joint Communications Board, with the functions of (1) centralizing data on radio propagation and related effects, from all available sources, (2) keeping continuous world-wide records of ionosphere characteristics and related solar, geophysical and cosmic data, and (3) preparing the resulting information and furnishing it to the armed forces. This involved maintaining ionospheric observatories, centralizing data from these and other ionospheric observatories operated by other agencies and other countries, performing experimental and research work as necessary to supplement existing sources of data, preparing predictions and forecasts of radio propagation conditions for all parts of the world, issuing charts, tables, handbooks, and bulletins for immediate dissemination to the armed forces, maintaining a "special problem" consulting service to give immediate answers to urgent military problems, and co-operating in this work with other agencies of the United Nations.

The groundwork for the prediction of radio propagation conditions and ranges of useful frequencies had been laid by the previous ionosphere researches of the National Bureau of Standards, some of the results of which were published in the PROCEEDINGS OF THE I.R.E. from 1937 to 1940, under the title, "Characteristics of the Ionosphere at Washington, D. C." During 1941 to 1943, at the request of the National Defense Research Committee, the National Bureau of Standards made a study of the correlation of direction-finder errors with ionospheric conditions, and prepared a "radio transmission handbook" to permit usable frequency calculations.

In meeting the requirement of predicting useful frequencies over any paths anywhere in the world, the IRPL was confronted by five major problems: (1) the obtaining of adequate ionospheric data on a world-wide basis, (2) the development of methods for calculating maximum usable frequency over long paths, (3) the development of methods for calculating sky-wave field intensities, (4) the determination of minimum required field intensities, and (5) the development of methods for forecasting ionosphere storms.

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Fig. 1—Active ionospheric stations reporting data to IRFL in 1945.
Fig. 2—World map showing zones covered by predicted charts.
At the outset, the IRPL was faced with the necessity of obtaining sufficient ionospheric data to permit predictions to be made anywhere in the world. At that time ionospheric observations were being made only at six locations in the world: Washington, D. C.; Slough, England; Huancayo, Peru; Watheroo and Sydney, Australia; and Christchurch, New Zealand. Regular data were available to the IRPL only from the first, third, and fourth of these. Immediate steps were taken to expand the world-wide coverage, with the cooperation of the Carnegie Institution of Washington; the United States Army and Navy; the Canadian Navy and Air Force; the British Admiralty, ISIB, the National Physical Laboratory and the British Broadcasting Corporation; the Australian organization, the ARPC; and the U.S.S.R., with the result that by the end of the war 44 stations were regularly reporting ionospheric observations, as shown in Fig. 1. This network of stations, together with analysis of radio traffic data from a number of communications networks, permitted the continual improvement of world charts of predicted ionosphere characteristics, from the small beginnings in 1941, based on only three stations, to the comprehensive charts now published monthly in the IRPL-D series reports. The knowledge gained from the greatly expanded world-wide ionospheric coverage permitted a much improved delineation of the regular variations of the ionosphere with latitude and local time, so that, for example, the hitherto seemingly anomalous behavior of northern and southern hemisphere stations fell into a consistent world picture.

In the course of their work it became necessary to place radio propagation predictions on a regular, world-wide basis, such that the great mass of data could be handled expeditiously and practical predictions issued regularly.

In order to use the data which were being received from all over the world for prediction purposes, it was necessary not only to understand their geographic, diurnal, and seasonal variations, but also to determine their relationship to relative sunspot numbers. A simple correlation of values of ionosphere characteristics with relative sunspot numbers had been previously found, but during the war trends of the variation of these characteristics with sunspot number were determined for the locations on earth of many of the ionosphere stations. A technique of prediction of ionosphere characteristics at any location, using standard statistical methods, was evolved, involving an estimate of the relative sunspot number for the month of prediction. A nomographic method for doing this type of prediction rapidly was later developed.

As another consequence of the improved world-wide coverage, the so-called "longitude effect" was discovered and put into operational use in 1943. This was the discovery that ionosphere characteristics were not, as previously supposed, the same, at the same local time, for stations at about the same latitude but different longitudes. Instead, they depended to a great extent on the geomagnetic latitudes of the station. Thus the station at Delhi, India, showed quite different characteristics from those observed at Baton Rouge, La.

Following this discovery, the world was divided, for practical operational purposes, into the three zones shown in the map of Fig. 2. In each zone the characteristics are independent of longitude, to a good enough practical approximation.

The second problem faced by the IRPL was the development of a simple rapid method of obtaining the maximum usable frequency (m.u.f.) over any paths in any part of the world. The groundwork for this was laid in 1936 when the "transmission curve" method of scaling ionospheric records was devised, leading to factors which could be applied to critical-frequency data to obtain m.u.f. values. These factors were satisfactory for distances up to 2500 miles, but for greater distances the method of multiple hops proved clumsy and, indeed, quite inadequate in the light of observed radio propagation data.

Consequently, the empirical "two-control point" method was devised (independently at the IRPL and ISIB) for paths longer than 2500 miles, whereby the m.u.f. over such a path is limited by the lower of the 2500-mile m.u.f. at two control points, 1250 miles from each station along the great-circle path connecting the two stations. This procedure gave much better results. As the volume of data increased, it became more and more apparent that normal F2- or E-layer propagation was completely inadequate to account for a considerable part of the observed transmissions, particularly at times when $E_s$ (sporadic $E$) was present. Consequently an extended analysis of $E_s$ occurrence was made, and sufficient regularity was found to make $E_s$ predictions possible, subject to the much wider day-to-day variability than in the case of the normal layers. Considerable further improvement in m.u.f. calculations was then made by including the effects of "sporadic-$E$" ($E_s$) propagation, also on a two-control-point basis.

World charts were prepared giving predictions of maximum usable frequencies, three months in advance. These, are continued in the monthly publication now issued through the Government Printing Office.

The urgent need for knowing distance ranges and lowest useful high frequency (l.u.h.f.) led to the next major problem undertaken by the IRPL—the calculation of sky-wave field intensities. To meet this, the field-intensity-recording program, begun by the National Bureau of Standards early in the last decade, was greatly expanded by installation of recorders at the new United States ionospheric stations. Fig. 3 shows a sample automatic field-intensity record. At the same time, theoretical studies of ionospheric absorption at oblique and vertical incidence were undertaken, in an attempt to obtain a simplified solution to the problem as rapid in operation as the method of calculating m.u.f.

An "equivalence theorem," similar to that used in
calculating m.u.f., was used, employing the observed field-intensity data to supply numerical values to the many uncertain factors in the equation. It was found that the diurnal variation of ionospheric absorption varied to a good approximation, on the average, linearly with the cosine of the zenith angle of the sun, a fact which simplified greatly the integration of ionospheric absorption over a given transmission path; the absorption could then be determined as a function of frequency, distance, and average solar zenith angle over the path.

The determination of sky-wave field intensity did not of itself give the whole story, however, unless information also could be available as to the minimum fields required for radio communication. Thus, the fourth major problem confronting the IRPL was the determination of minimum field intensities necessary to overcome atmospheric radio noise, which was the principal type of noise encountered at sky-wave frequencies. This is still the subject about which least is known in the field of sky-wave communication. Some fragmentary measurements were available, and a beginning on the problem had been made at the ISIB in England. All available data on atmospheric radio noise and required fields were collected, as well as data on thunderstorms, which are the source of atmospheric noise. The result of the analysis was to divide the world into zones corresponding to different grades of noise intensity, taking into account both the generation and the propagation of the noise. Fig. 4 shows one such chart, for November through March. The principal noise-generating centers are in the East Indies, Central and South America, and Africa, with secondary centers in the tropical oceans—the “doldrum belts.” For each noise grade, a set of curves of required intensities was constructed, similar to the one shown in Fig. 5. These were for good 95 per cent intelligible radiotelephone communications, and empirical factors were deduced for other types of service; for example, manual c.w. telegraphy required only 1/7 as great intensities, while four-tone single-side-band six-channel radio teletype might required only 1/14 as great intensities. Much of this work was done with the close collaboration and assistance of the Radio Propagation Unit of the Office of the Chief Signal Officer of the U. S. Army.

For convenience in use, the required field graphs were plotted on nomograms involving frequency and absorption index, so that the l.u.h.f. could be read off directly.

The fifth major problem of the IRPL was the forecasting of ionosphere storms—those abnormalities often associated with geomagnetic storms—which disrupt radio communications, especially in the Arctic. The military importance of the North Atlantic, which reaches into the auroral zone, or zone of maximum disturbance, made it indeed urgent to know when communications were likely to be interrupted. The urgency is apparent when it is realized that aircraft depended largely on radio aids for navigation over the North Atlantic.

Therefore a program was undertaken, in collaboration with the Department of Terrestrial Magnetism, Carnegie Institution of Washington, to study the relations between ionosphere storms and the sun, whose radiations produce the storms. Improved observational techniques, like the Harvard University coronagraph, a device for photographing the extremely active solar corona, contributed to the study. As a result of the analysis, a weekly forecast was issued, which proved to be of some value to the armed services. The world was divided into zones of varying ionospheric disturbance, as shown in Fig. 6, and forecasts were made for each zone.

A different approach, however, led to a considerably
Fig. 4—Map showing atmospheric radio noise zones (November through March).
more accurate service of forecasting disturbances a shorter time in advance. In this, studies of the behavior of radio-d.f. bearings over the North Atlantic path showed that it was possible to issue warnings of radio disturbance a few hours to a half day or more in advance. Consequently a short-time warning service was inaugurated whereby such warnings were telephoned and telegraphed daily to interested agencies. With the lifting of wartime restrictions, this warning service is now being broadcast regularly over WWV, the National Bureau of Standards station at Beltsville, Md., at 20 and 50 minutes past each hour. A group of N's or W's is transmitted, the former meaning "no warning" (quiet conditions expected) and the latter "warning" (disturbed conditions over the North Atlantic expected or in progress).

During the war the IRPL performed many specific services for the armed forces and commercial companies doing war work, involving consultation and advice, on their special problems involving radio wave propagation. Types of problems included the determination of best usable frequencies for specified services, such as point-to-point, short-distance tactical operations, plane-to-ground, high-frequency broadcast, the prediction of ground-wave and sky-wave distance ranges under different conditions, advice as to types of antennas and lowest required radiated power for specified purposes, and frequency allocation. As the techniques promulgated by IRPL became more widely disseminated, many types of problems, especially those in frequency allocation, were eventually solved by the Army and Navy groups in which they originated.

In January, 1944, a two-weeks training course in radio wave propagation was given by IRPL. It was for officers who were to be taught the principles of radio wave propagation and methods of problem solution and then assigned to overseas communication groups, where they could put on a scientific basis the assignment of radio operating frequencies in the field. Others were then to be sent to training units within the United States to organize courses in which additional officers could be instructed in this work. The student body consisted of two groups, the first group consisting of eleven Army Air Forces officers, four officers from the Signal Corps, and three Navy officers, and the second group consisting of fifteen enlisted men and one officer from the Signal Corps, who formed the nucleus of the Radio Propagation Unit of the Signal Corps. The course comprised twenty-five lectures by scientists and others working directly in radio wave propagation, interspersed with problem sessions in which the students were coached in the solution of practical radio wave propagation problems.

As a further aid in determining the proper usage of radio frequencies, three handbooks were issued. The first handbook, "Radio Transmission Handbook—Frequencies 1000 to 30,000 kc.," was issued in January, 1942, giving the basic principles of radio sky-wave propagation, and such computational procedures as were extant at that time, together with preliminary versions of prediction charts and predictions for the winter. A supplement to this handbook was issued June 1, 1942, which gave summer predictions.

On November 15, 1943, the "IRPL Radio Propagation Handbook, Part 1" was issued. This handbook, issued as an IRPL publication, and also as a Navy training manual (TM 11-499) and a Navy publication (DNC-13), gave a descriptive discussion of the behavior of the ionosphere and of the theory behind maximum usable frequencies and lowest useful high frequencies. Prediction charts of maximum usable frequencies and absorption constants were given. Techniques for the determination of m.u.f. and l.u.b.f. over any path at any time were given to the extent that they had been developed at the time. It is impossible to express fully the valuable aid and support received by the IRPL from other agencies. Close and continuous liaison was maintained with the Department of Naval Communications (CNO) and the Radio Propagation Unit of the Army Signal Corps (SPSOL); valuable assistance and suggestions were interchanged with personnel in those departments working with IRPL in the solution of basic problems and applications. Close co-operation was maintained with other branches of the Army and Navy having need of radio propagation data, including the Army Security Agency, the Army Air Forces, other branches of the Signal Corps, the Navy Bureau of Ships, Bureau of Aeronautics, Coast Guard, and other branches of Naval Operations.

Acknowledgment is made to the Department of Terrestrial Magnetism, Carnegie Institution of Washington, for its extremely valuable assistance in operating ionosphere stations and collecting much of the geophysical and solar data upon which the services of the IRPL were based, and to the untiring work of its staff in cooperating in the entire radio propagation program. Acknowledgment is also wholeheartedly given to the full co-operation, from the very beginning, of the radio prop-

Fig. 5—Minimum field intensities required for satisfactory radio-telephone communications in the presence of atmospheric radio noise (noise grade 3).
Fig. 6—World map showing zones of different degrees of ionospheric disturbance.
Alternating-Current Measurements of Magnetic Properties

HORATIO W. LAMSON†, FELLOW, I.R.E.

Summary—Here is presented a critical analysis of various procedures for determining the permeability and core loss of ferromagnetic materials, together with a discussion of the limitations under which such observations are made and the interpretations which should be applied to the data obtained.

INTRODUCTION

It is the purpose of this paper to discuss various methods for the a.c. measurement of the magnetic properties of a specimen of ferromagnetic material and, it is hoped, to clarify certain phases of these techniques about which some misunderstanding has existed. The system of magnetic nomenclature and definitions recently adopted by the American Society for Testing Materials will be used.

Magnetic Condition of the Specimen

It is a well-known, but sometimes ignored, fact that all ferromagnetic materials exhibit the phenomenon of hysteresis and have, in effect, a "memory," so that any present (instaneous) condition is more or less influenced by past events. To obtain significant and reproducible data it is first essential to erase all memory of previous conditions. This preliminary demagnetization may be accomplished by subjecting the specimen to a substantial a.c. magnetization which is then gradually reduced to zero. Thereafter, any applied a.c. magnetization must be removed by a gradual reduction to zero, rather than by interrupting the circuit at some arbitrary time in the cycle.

If any subsequent magnetization is then due to a symmetrically alternating current (having no d.c. component), the specimen will be in a symmetrically cyclically magnetized (SCM) condition, wherein the mean values of both induction and magnetizing force are zero. For either polarity of magnetization, the peak values of each of these parameters will be equal, and are designated as their normal values.

In addition to hysteresis, it is less generally known that some materials exhibit a definite magnetization lag. If, having acquired in them a stabilized variation in B and H, a change is made in the amplitude of the cyclic variation of H, some time (representing a considerable number of cycles) may elapse before a completely stabilized variation and a new maximum value of induction is attained. This magnetization lag appears to be more pronounced for a given increase than for a corresponding decrease in magnetizing force, doubtless due to the effect of retentivity.

When measuring a specimen at different values of cyclic H, it would thus appear desirable to start with the maximum contemplated value and successively reduce this parameter. For incremental measurements, however, the biasing component of H must be increased progressively from an initially demagnetized condition to avoid any retentivity in the biasing H.

It should be remembered that the magnetic properties of some materials may, to a certain degree, be modified by mechanical strains in punching operations on flat laminations, or in the rolling of flat stock into toroidal cores. Subsequent metallurgical treatment may then be necessary to restore the natural magnetic condition of the material. The author is of the opinion, however, that a limited amount of easy and careful shearing may not disturb the specimen as much as is sometimes anticipated (see Appendix E).
INTERPRETATION OF AN IRON-CORED INDUCTOR

A simple iron-cored inductor consists physically of a ferromagnetic core circumscribed \( N \) times by a single conductive winding. This inductor possesses two types of impedance: a reactive component corresponding to energy storage without loss, and a resistive component representing eddy current, hysteresis, and ohmic heat losses. The core is assumed to be homogeneous and to have a uniform cross section \( A \) and a mean length \( \lambda \) for the flux path (c.g.s. units), so that the core reluctance is given by

\[
R = \frac{\lambda}{\mu A}.
\]  

(1)

With this geometric symmetry, the specimen will be subjected to the same values of induction and magnetizing force at all points. This paper deals with the basic concepts of magnetic measurements, thereby assuming that any leakage flux is negligible and that all the flux traverses an iron path and links completely any winding on the inductor.

The specimen core may be constructed of rectilinear strips overlapping at their extremities to form an Epstein square; it may have a shell-type configuration, or it may be toroidal in shape and assembled by stacking annular laminations, by rolling flat stock spiral-wise, or by molding iron-dust mixtures. The author also has used rectangular strips of the specimen material forming a diameter across annular laminations, the latter having sufficiently high permeability and increased cross section to offer negligible reluctance.²

It is a natural and long-established practice to visualize the total impedance \( Z \) of this inductor as the rectilinear sum of its inductive reactance \( \omega L_s \) and its equivalent series resistance \( R_s \), accounting for all losses (see Fig. 1). The parameter \( L_s \) is the equivalent series inductance and \( \phi \) is the phase angle of the inductor having a dissipation factor \( D \). Then the vector impedance value becomes

\[
Z = R_s + j\omega L_s
\]  

(2)

while

\[
D \equiv \cot \phi = \frac{R_s}{\omega L_s}.
\]

(3)

While this representation is mathematically permissible, it does not correspond to certain empirically determined facts concerning the electromagnetic behavior of the inductor.

Consider Fig. 1, which implicitly stipulates that the application of an external a.c. terminal voltage \( E_T \) produces an exciting current \( I_{exc} \) which, circumscribing the core \( N \) times, creates a magnetomotive force which, in turn, produces the flux therein. If \( i \) is the instantaneous value of the exciting current, the instantaneous value of the magnetomotive force is frequently considered to be given by

\[
F = 0.4\pi N i,
\]

(4)

and to be in phase with \( i \). The instantaneous value \( \Phi \) of the flux in the core will be the ratio of \( F \) to the core reluctance. Stipulating that the production of flux by a magnetomotive force is an instantaneous phenomenon, it would apparently follow that \textit{the flux is in phase with the exciting current} (see Fig. 2).

\[ \Phi \]

\[ I_{exc.} \]

\[ 90^\circ \]

\[ E_{ind.} \]

\[ \text{Valid only when} \]

\[ R_s = 0 \]

Fig. 2—Phases in an inductor with no loss.

Another basic law of physics states that the instantaneous voltage induced in a circuit \( e_{ind} \) is proportional to the rate of change of the flux linking this circuit.

\[
e_{ind} = -\frac{N}{10^8} \frac{d\Phi}{dt}.
\]

(5)

If the flux is varying sinusoidally,

\[
\Phi = \Phi_{max} \sin \omega t,
\]

(6)

whence

\[
e_{ind} = -\frac{N\Phi_{max}}{10^8} \cos \omega t.
\]

(7)

Comparing (6) and (7), it follows that \textit{the induced voltage and the flux are in quadrature,} \( e_{ind} \) lagging \( \Phi \) by an angle \( \pi/2 \). Fig. 2 shows these phase relationships at the arbitrary instant when \( e_{ind} \) has a maximum positive value.

Correlation of the italicized statements in the two preceding paragraphs leads to the erroneous conclusion that the induced voltage lags the exciting current by \( \pi/2 \). By applying a secondary winding to the inductor it

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can be demonstrated that the induced voltage lags the exciting current by an angle \( \pi/2 \) plus the hysteretic angle \( \beta \). Consequently, the flux is not in phase with the full exciting current, but lags \( I_{\text{exc}} \) by the angle \( \beta \). These correct phase relationships are indicated in Fig. 3, which

assumes zero copper loss in the inductor winding. In this case, the exciting voltage (always equal in magnitude and opposite in phase to the induced voltage) is the applied terminal voltage and, hence, leads \( I_{\text{exc}} \) by the phase angle \( \phi \). This makes \( \beta \) the complement of \( \phi \) in Fig. 3.

Since the production of flux, per se, represents a storage of energy with no dissipation (disregarding radiation), and since flux must be in phase with that current which produces it, it follows that the exciting current must be the vector sum of two quadrature components; namely, the true magnetizing current \( I_m \) in phase with the flux, and the loss current \( I_l \) which, when squared and multiplied into the proper resistance, gives the power dissipation in the core of the inductor.

The magnetizing current, from which the magnetomotive force and flux may be calculated, is thus but a portion of the exciting current and is given by

\[
I_m = I_{\text{exc}} \cos \beta.
\]

(8)

Likewise, if copper loss can be neglected,

\[
I_m = I_{\text{exc}} \sin \phi.
\]

(9)

It is apparent that the magnetizing current must be produced by an exciting voltage \( E_{\text{exc}} \) equal and opposite to \( E_{\text{ind}} \), and hence leading \( I_m \) by \( \pi/2 \). The voltage \( E_l \) producing the loss current must be in phase with that current. Consequently, both \( I_l \) and \( E_l \) must be coincident in phase with the exciting voltage.

**Parallel Concept Neglecting Copper Loss**

These current and voltage relationships are quite incompatible with the series representation of the impedance components of an inductor (Fig. 1). However, if it is considered that \( E_l \) and \( E_{\text{exc}} \) are not only coincident but also equal in magnitude, and hence may be the same voltage, the representation of the inductor by parallel admittance or impedance components agrees with the known facts (see Fig. 4). The purely reactive path, involving flux energy storage, \( I_m \) in quadrature with \( E_{\text{exc}} \), consists of the equivalent parallel inductance \( L_p \) and carries the magnetizing current; while the purely resistive path, involving core losses, \( I_l \) in phase with \( E_{\text{exc}} \), consists of the equivalent parallel resistance \( R_p \) and carries the loss current. The impedance of this inductor has a vectorial value:

\[
Z = \frac{R_p \omega L_p (\omega L_p + jR_p)}{R_p^2 + \omega^2 L_p^2}.
\]

(10)

**Intercomparison between the impedance values of an inductor evaluated from its series and its parallel components establishes the well-known relationships:**

\[
L_p = L_s \frac{\sin \phi}{\cos \phi} = L_s (1 + \cot^2 \phi) = L_s (1 + D^2)
\]

(11)

\[
R_p = R_s \frac{\cos \phi}{\cos \phi} = R_s (1 + \tan^2 \phi) = R_s (1 + Q^2)
\]

(12)

\[
D = \cot \phi = \frac{R_s}{\omega L_s} = \frac{\omega L_p}{R_p}
\]

(13)

**Parallel Concept with Copper Loss**

When representing the inductor by Fig. 4, the parallel resistance \( R_p \) should correspond, strictly, only to magnetic losses due to hysteresis and eddy currents. Any ohmic losses (copper losses) must be represented by an additional series resistance \( R_e \) which carries the full exciting current (see Fig. 5). The purely reactive impedance \( \omega L' \) is in parallel with the resistance \( R' \), which accounts for the magnetic losses. The vector impedance of this network takes the more elaborate form:

\[
Z = \frac{R_p R'^2 + \omega^2 L'^2 (R_e + R') + j\omega L'R'^2}{R'^2 + \omega^2 L'^2},
\]

(14)

involving both \( R' \) and \( L' \) in its real and imaginary components, but \( R_e \) only in its real component. From (2) and (14),

\[
L' = L_s [1 + (D - D_e)^2]
\]

(15)

\[
R' = (R_e - R_s) \left[ 1 + \left( \frac{1}{(D - D_e)^2} \right) \right]
\]

\[
= \omega L_s \left[ D - D_e + \frac{1}{D - D_e} \right]
\]

(16)
where the "copper-loss" dissipation factor $D_c$ is defined as

$$D_c = \frac{R_c}{\omega L_c}. \quad (17)$$

As long as skin effect in the inductor winding is negligible, $R_c$ may be considered to be the d.c. resistance of the winding. Note that both $L'$ and $R'$ differ from the $L_p$ and $R_p$ values of Fig. 4.

![Diagram of an inductor with both core and copper losses.]

The inclusion of copper losses gives rise to a small copper-loss voltage drop $E_c$ in phase with the exciting current, so that the terminal voltage $E_T$ exceeds the exciting voltage and $\beta$ is less than the complement of $\phi$. Whenever $D_c$ is not a negligible component of $D$, the magnetizing current must be evaluated by (8), or by

$$I_m = \frac{I_{exc}}{\sqrt{1 + (D - D_c)^2}}. \quad (18)$$

The loss current will be

$$I_1 = I_{exc} \sin \beta = \frac{I_{exc}(D - D_c)}{\sqrt{1 + (D - D_c)^2}}. \quad (19)$$

Finally, from the geometry of Fig. 5, the exciting voltage may be computed in terms of the terminal voltage:

$$E_{exc} = \frac{E_T \sin \phi}{\cos \beta} = E_T \sqrt{\frac{1 + (D - D_c)^2}{1 + D^2}}. \quad (20)$$

**Evaluation of Normal Permeability**

Normal permeability, hereinafter symbolized as $\mu$, is defined as the ratio of the normal, or peak, value of the induction (flux density) $B$ to the corresponding normal (peak) value of the magnetizing force $H$, when the magnetic material is in a symmetrically cyclically magnetized (SCM) condition.

$$\mu = \frac{B}{H}. \quad (21)$$

To measure normal permeability, which, as will be shown later, is the most significant of the several "a.c. permeabilities," the normal magnetizing force may be evaluated in terms of the peak magnetizing current, represented by the symbol $I_m$, regardless of the wave form of this current.

$$H = \frac{0.4\pi N \bar{T}_m}{\lambda}. \quad (22)$$

Note that the true magnetizing current, rather than the exciting current, is involved here. If the flux has a cyclic variation which is symmetrical but not necessarily sinusoidal, the normal induction can then be evaluated in terms of the half-period average or the effective (r.m.s.) values of the exciting voltage by the following equation:

$$B = \frac{10^6 E_{exc} \text{ (av.)}}{4NAf} = \frac{10^6 E_{exc} \text{ (r.m.s.)}}{4(ff)NAf}. \quad (23)$$

The third member of (23) is derived from the second member by defining the form factor $(ff)$ of a cyclic variation as the ratio of its effective to its half-period average value.

The normal permeability for any symmetrical variation (SCM condition) is then:

$$\mu = \frac{10^6 E_{exc} \text{ (av.)}}{1.6\pi N^2A\bar{T}_m}. \quad (24)$$

**Normal Permeability With Sinusoidal Parameters**

On the hypotheses that $H$ and $B$ are varying in a sinusoidal manner, the form factor of all cyclic parameters becomes $\pi/2\sqrt{2} = 1.11072$ \ldots. The normal induction can be evaluated in terms of the peak or the r.m.s. value of the exciting voltage:

$$B = \frac{10^6 E_{exc} \sqrt{2}}{\omega NA} = \frac{10^6 \bar{E}_{exc}}{\omega NA}. \quad (25)$$

Then the normal permeability becomes

$$\mu = \frac{10^6 \lambda A_{exc}}{0.4\pi N^3A\omega \bar{T}_m} = \frac{10^6 \lambda L'}{0.4\pi N^2A}, \quad (26)$$

since, by definition, the parallel reactance $\omega L'$ equals the ratio $E_{exc}/I_m$.

Thus normal permeability, for any specified normal induction or normal magnetizing force, may be evaluated in terms of the geometry of the core and a measured value of the parallel inductance $L'$. It should be recalled that most inductance-measuring bridges yield directly the equivalent series inductance (Maxwell, Owen, Hay). Using (15), the normal permeability evaluated in terms of the series inductance becomes

$$\mu = \frac{10^6 \lambda L_e[1 + (D - D_c)^2]}{0.4\pi N^4A}, \quad (27)$$
and demands a knowledge of the dissipation factors of the inductor.

The substantial error which may be introduced by omitting the factor \([1+(D-D_s)^2]\) in (27) and evaluating normal \(\mu\) directly in terms of \(L_s\), using the concepts of Fig. 1, is demonstrated in Appendix A. The effect of neglecting copper loss and assuming that \(D_s\) is negligible at lower frequencies is demonstrated in Appendix B.

If copper loss may be neglected, so that Fig. 4 is valid, it can be demonstrated\(^1\) that normal permeability may be computed in terms of the reactive power \(P_r\), measured in vars, which is taken by the inductor, together with the frequency \(f\), the core volume \(V\) (cubic centimeters), and either the normal induction or the normal magnetizing force:

\[
\mu = \frac{B^2 f V}{0.4 \times 10^f P_r} = \frac{0.4 \times 10^f P_r}{B^2 f V}.
\]

Effects of Harmonic Distortion

Due to the nonlinear character of the d.c. magnetization curve and the phenomenon of magnetic saturation, an inherent distortion exists in the core material, so that, with a generator developing, per se, a pure sinusoidal voltage, the cyclic variations of \(I\) and/or \(B\) will contain odd-harmonic components. Furthermore, the relative distortion in either parameter will be a function of the series resistance of the circuit.

Assuming no copper losses in the winding, if the inductor could be connected directly across the terminals of a resistanceless sinusoidal generator, the exciting voltage applied across the inductance \(L_p\) (Fig. 4) would be sinusoidal. The induced voltage and the flux variation would then have to be sinusoidal and harmonic distortion would exist in the magnetizing current and in \(I\).

Total lack of flux distortion would demand an impossible circuit of zero series resistance. On the other hand, if the series resistance of the circuit is made very large compared with the reactance of the inductor, the generator would be working into an essentially resistive load, so that both the exciting and magnetizing currents, and hence \(I\), would be practically sinusoidal. Distortion would then exist in both the induced voltage and the cyclic variation of flux.

The existence of flux distortion may, in many cases, be demonstrated by examination of the terminal voltage of the inductor with a cathode-ray oscillograph or, more precisely, with a harmonic analyzer. It is not universally recognized, however, that, if the resistance of the sinusoidal generator is low, an examination of the terminal voltage of the inductor may not show the existing flux distortion which is introduced by the internal copper-loss resistance \(R_s\) (Fig. 5). An infallible procedure for observing true flux distortion would be the examination of the open-circuit voltage induced in a secondary winding on the inductor core. An approximate evaluation of the distortion existing in \(I\) may be obtained by analyzing the exciting current, i.e., the voltage drop across a resistor in series with the inductor. To maintain the initial conditions, this resistance must be negligible compared to the reactance of the inductor, unless it is purposely made large to ensure a small distortion in \(I\).

External circuit resistance thus increases flux distortion while reducing the distortion of magnetizing force. The presence of a nominal amount of circuit resistance gives harmonic distortion of both \(B\) and \(H\), and yields somewhat ambiguous data which are a function of the measuring circuit external to the inductor. It would be desirable to have one of these parameters as free from distortion as possible. The question thus arises, should a.c. magnetic measurements be standardized at sinusoidal \(B\) or at sinusoidal \(H\)? The answer is somewhat determined by the method of measurement and the contemplated use of the specimen material. An empirical comparison between sinusoidal \(B\) and sinusoidal \(H\) measurements is given in Appendix A.

In the various meter methods of measurement the circuit resistance, using a low-resistance generator such as a 60-cycle power line, may be kept small, thus permitting a good approximation to sinusoidal \(B\) if copper losses are small.

Whenever the generator has a significant amount of resistance, and in most bridge methods of measurement which insert an appreciable amount of resistance into the circuit between the generator and the inductor, sinusoidal \(B\) is impossible. It would then appear desirable to go the whole distance and to standardize on conditions yielding sinusoidal \(I\). This was done in a magnetic test set developed by the authors\(^2\) by inserting considerable resistance in series between the generator and the bridge, with a corresponding increase in the e.m.f. of the generator to obtain a specific normal \(I\). Sinusoidal currents are thus ensured. If a selective null-balance detector, responsive to the fundamental component of the voltage induced in the inductor, is then employed, the conditions for bridge balance will correspond to sinusoidal values of both \(I\) and \(B\). This will permit normal \(\mu\), referred to the fundamental components, to be evaluated in terms of the measured inductance by (27).

Regardless of any distortion in \(I\), its normal value may be computed in terms of the peak value of the magnetizing current by the use of (22). When using non-selective measuring instruments it should be noted that, if appreciable distortion exists in the flux, (23) rather than (25) must be used for evaluating normal induction.

Normal \(\mu\) Determined From the A. C. Hysteresis Loop

It is common practice to plot the a. c. hysteresis loop of a magnetic specimen by using as ordinates values of \(B\) obtained from the induced voltage, and as abscissae values of a pseudo-\(I\) computed from the exciting cur-

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\(^1\) An analysis first brought to the author’s attention in an unpublished memorandum from S. L. Burgwin to J. P. Barton, dated February, 1942.

\(^2\) No analysis of methods of measurement has been made in this paper, but a comprehensive discussion of the subject is available in a note by the authors in the March, 1942, issue of The Electrical Engineering.
rent. This technique will be illustrated by some 60-cycle data taken at a small induction by Burgwin upon an Epstein inductor having a HiPernik core and using a d. c. voltmeter together with a synchronous commutator to obtain values of $B$ and $H$ at successive phases around the loop.

The pseudo-$H$ values measured by using a low-resistance, air-core mutual inductor in series with the specimen inductor were closely sinusoidal. Core losses are nonexistent in this mutual inductor, so that its value of $R'$ becomes infinite and its hysteretic angle is zero. Consequently, the entire exciting current is producing flux, and the open-circuit secondary voltage may be calibrated in terms of the exciting current. It should be emphasized, however, that whenever such a mutual inductor is used, the current values obtained must be corrected by (8) before evaluating the normal magnetizing force in the specimen inductor from (22).

The $B$ data (exciting voltage) were given a small correction to obtain the fundamental sinusoidal component which was given by

$$B = 682 \sin \omega t + 693 \cos \omega t.$$  \hfill (29)

The hysteretic angle was, therefore,

$$\beta = \cot^{-1} \left( \frac{682}{693} \right) = 45^\circ 28', \tag{30}$$

and the normal induction

$$B = \frac{682}{\cos \beta} = \frac{693}{\sin \beta} = 972 \text{ gausses.} \tag{31}$$

In Fig. 6, loop $A$ is a duplication of Burgwin's data showing a semilooop corresponding to positive values of induction. Burgwin also gave the d. c. hysteresis loop $C$

![Image of hysteresis loop](image)

for the same specimen carried to the same maximum induction value. For loop $C$ the abscissa values are, of course, true d. c. values of $H$. For loop $A$, however, the abscissae give pseudo-$H$ values calculated in terms of exciting current. This loop shows six significant values as follows:

- $H_{\text{max}} = 0.0550$ oersteds, maximum value of pseudo-$H$
- $H_1 = 0.0392$ oersteds, pseudo-$H$ corresponding to $B = 0$
- $H_2 = 0.0386$ oersteds, pseudo-$H$ corresponding to $B_{\text{max}}$
- $B_{\text{max}} = 972$ gausses, maximum value of $B$, i.e., normal $B$
- $B_1 = 693$ gausses, induction corresponding to pseudo-$H = 0$
- $B_2 = 682$ gausses, induction corresponding to $H_{\text{max}}$.

Time sequence around this loop is counterclockwise and, since both components are sinusoidal, it can be shown that

$$\sin \beta = \frac{H_1}{H_{\text{max}}} = \frac{B_1}{B_{\text{max}}} \tag{32}$$

$$\cos \beta = \frac{H_2}{H_{\text{max}}} = \frac{B_2}{B_{\text{max}}} \tag{33}$$

$$\tan \beta = \frac{H_1}{H_2} = \frac{B_1}{B_2}. \tag{34}$$

The maximum $H$ for the loop $C$ is seen to be 0.0300 gausses; consequently, the d. c. permeability of the specimen has a value of 32,400, given by the slope of the radius $G$ in gausses per oersted. Three different a. c. permeabilities may be defined from loop $A$.

The slope of the radius $K$ gives

$$\mu_K = \frac{B_{\text{max}}}{H_{\text{max}}} = 25,200. \tag{35}$$

The slope of the line $M$ gives

$$\mu_M = \frac{B_{\text{max}}}{H_{\text{max}}} = 17,670. \tag{36}$$

The line $M$ is not the major axis of the ellipse unless $B_{\text{max}}$ and $H_{\text{max}}$ are scaled to be equal distances on the diagram.

The slope of the radius $N$ gives

$$\mu_N = \frac{B_{\text{max}}}{H_{\text{max}}} = 12,395. \tag{37}$$

These permeabilities have the relation

$$\mu_{\text{a.e.}} > \mu_K > \mu_M > \mu_N, \tag{38}$$

and it can be shown from the above equations that $\mu_M$ is the geometric mean of $\mu_K$ and $\mu_N$.

The loop $A$ encloses an area proportional to the total core loss because it is evaluated in terms of exciting current, which leads the flux and the true magnetizing current by the angle $\beta$.

If, for each induction value, the phase of the corresponding pseudo-$H$ value is retarded by the angle $\beta$, the loop $A$ degenerates into the line $M$, enclosing no

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4 This relation was pointed out by S. L. Burgwin.
area. Line $M$ has the same $H_{\text{max}}$ value as loop $A$, but has been made coincident in time with $B_{\text{max}}$ (normal $B$). However, the magnitude of $H_{\text{max}}$ is determined by the exciting current, so that, to determine the true path of $B$ versus $H$ variation, the abscissa value of each point on line $M$ must be reduced by $\cos \beta$ (compare (8)). The true path is, therefore, line $K$, so that $H_2$ is the true normal $H$ for the given normal $B$, and $\mu_K$ (slope of line $K$) is, in fact, the normal permeability of the specimen.

This same result may be achieved by first reducing the abscissa of each point of loop $A$ by $\cos \beta$, giving loop $D$. Then when, for each $B$ value of loop $D$, the corresponding $H$ value is retarded by the angle $\beta$, this loop degenerates into the line of operation $K$ which encloses no area, since the loss component of the exciting current has been removed.

Assuming a negligible value of copper loss, the significance of $\mu_N$ may be seen by taking the ratio of (35) to (37) and substituting from (33) to obtain

$$\mu_N = \mu_K \cos^2 \beta = \mu_K \sin^2 \phi. \quad (39)$$

The normal permeability $\mu_K$ has been shown in (24) to be computable directly from the parallel inductance $L'$. Likewise, from (11) and (15), $\mu_N$ may be considered to be the permeability computed directly from the series inductance omitting the factor $[1 + (D - D_x)^2]$ in (27).

The only significance which can be attached to the $\mu_M$ value is its definition (36) as the ratio of the normal induction to the maximum value of pseudo-$H$ evaluated in terms of the full exciting current. It follows that a second evaluation of $\mu_M$ is given by

$$\mu_M = \mu_K \cos \beta = \frac{B_2}{H_2}. \quad (40)$$

It is apparent that the normal $H_2$ required to produce the dynamic cycle of induction exceeds the maximum static value of $H$ required to produce the same maximum induction (total flux) in the d.c. loop $C$. It may be considered that the shielding effect of eddy currents in the core reduces the actual interior induction, so that to produce a given total flux more magnetizing current would be required. The departure of normal $\mu$ below $\mu_{d.e.s.}$, or, graphically, the angle between lines $G$ and $K$, would thus increase with the frequency and the lamination thickness of a given material. Data supporting this hypothesis is suggested by R. F. Field.

The foregoing data show close agreement between the values $H_1$ and $H_2$ and again between $B_1$ and $B_2$. This is only because, for loop $A$, the hysteretic angle was close to $45^\circ$. In Fig. 7 a pseudo-$H$ loop has been constructed for the same normal $B$, but having increased core loss, resulting in the angle $\beta$ becoming $55^\circ$. The significant values for this loop, which degenerates into the same line $K$ when corrected for phase displacement and into terms of magnetizing current, are as follows:

\begin{align*}
H_{\text{max}} &= 0.0672 \text{ oersteds} \\
H_1 &= 0.0551 \text{ oersteds} \\
H_2 &= 0.0386 \text{ oersteds, as before (normal $H$)} \\
B_{\text{max}} &= 972 \text{ gauss, as before (normal $B$)} \\
B_1 &= 796 \text{ gauss} \\
B_2 &= 558 \text{ gauss}.
\end{align*}

These data yield:

| $\mu_K$ | 25,200, as before (normal $\mu$) |
| $\mu_M$ | 14,460 |
| $\mu_N$ | 8,290 |

Note that, here, $\mu_N$ (series inductance) is less than one-third of $\mu_K$ (parallel inductance).

For any of these sinusoidal pseudo-$H$ loops, normal permeability may be evaluated from (33). A precise value of $H_2$ is difficult to observe, since the loop is horizontal at its summit. It will be useful to note that, from the geometry of any of these sinusoidal loops, the radius $K$ bisects each horizontal chord of the loop, while the radius $N$ bisects each vertical chord of the loop. The radius $K$ (normal $\mu$) may thus be located more accurately as the bisection of the horizontal chord having an ordinate value $B_1$, and the radius $N$ as the bisection of the vertical chord having the abscissa value $H_1$.

It should be noted that, had harmonic distortion existed in $H$ and/or $B$, correcting the observed loop for phase displacement and true $H$ magnitude would have degenerated it into a curved line, in reality the initial d.c. magnetization curve displaced horizontally by eddy-current shielding. The slope of the straight line $K$ drawn to its extremity would then determine normal $\mu$.

**Measurement of Core Loss**

The core-loss power $P_e$, jointly due to hysteresis and eddy-current losses may be measured in various ways. Using a wattmeter reading $P$ and an r.m.s. ammeter to measure the exciting current,

$$P_e = P - I_{eeq}^2 R_e. \quad (41)$$
The copper-loss correction term in (41) may be avoided if the voltage coil of the wattmeter, together with an r.m.s. voltmeter reading $E$, are connected in parallel to constitute a resistive load $r$ across a secondary winding on the inductor. The wattmeter will respond to the product of the in-phase parameters $E_{exc}$ and the currents through the resistances $R'$ and $r$, so that

$$P_c = \gamma \left( P - \frac{E^2}{r} \right)$$  \hspace{1cm} (42)

where $\gamma$ is the reciprocal of the turns ratio.

In bridge measurements the r.m.s. values of the exciting current or the terminal voltage may be obtained by using (16), (19), and (20):

$$P_c = I_1^2 R' = I_{exc}^2 \omega I_0 (D - D_e) = I_{exc}^2 (R_s - R_e)$$  \hspace{1cm} (43)

$$P_c = \frac{E_{exc}^2}{R} = \frac{E^2}{\omega L_s (1 + D^2)}$$  \hspace{1cm} (44)

or, in terms of the apparent power,

$$P_c = E_T I_{exc} \left( \frac{D - D_e}{\omega L_s} \right) = E_T I_{exc} \cos \phi - I_{exc}^2 R_e.$$  \hspace{1cm} (45)

Equations (44) and (45) stipulate sinusoidal flux. However, it will be demonstrated in Appendix D that, in the presence of flux distortion, the use of a tuned voltmeter to measure $E_T$ or $E_{exc}$ (across a secondary winding) will give $P_c$ values from (44) which check those obtained from (43).

**Composition of Core Loss**

When the specimen material is in a SCM condition, the existing core loss $P_c$ is composed of two additive components: hysteresis power $P_h$, and eddy-current power $P_e$. By means of the following analysis it is possible to separate the measured core loss into these two components, provided that the total dissipation factor $D$ and the copper-loss dissipation factor $D_e$ are known.

The hysteresis power is directly proportional to the frequency and is given by

$$P_h = \eta f B^4 \times 10^{-7},$$  \hspace{1cm} (46)

which involves the coefficient $\eta$ and the Steinmetz exponent $\epsilon$, both of which are not too well known and by no means constant functions of the normal induction.

The eddy-current power is directly proportional to the square of the frequency and is given by

$$P_e = \frac{\pi^2 B^4 \delta^2 V}{6 \times 10^{16} \rho}$$  \hspace{1cm} (47)

where $\delta$ is the lamination thickness, and $\rho$ is the resistivity of the specimen material (c.g.s. units).

In Fig. 5 consider the resistor $R'$ to be replaced by two parallel components $R_h$ and $R_e$ which, if divided into $E_{exc}^2$, would yield, respectively, the values $P_h$ and $P_e$. The hysteresis and eddy-current dissipation factors may be defined as

$$D_h = \frac{\omega L'}{K_h} = 2^{(1+\epsilon/2)} \eta \mu B^{(\epsilon-2)}$$  \hspace{1cm} (48)

$$D_e = \frac{\omega L'}{K_e} = \frac{2\pi^2 \delta^2 \mu}{3\rho \times 10^6}.$$  \hspace{1cm} (49)

The following relation is shown to exist:

$$D = D_e + D_h + D_e.$$  \hspace{1cm} (50)

If these values are plotted versus frequency on log-log paper and no eddy-current shielding (constant inductance) is assumed, $D_h$ will be a horizontal line; $D_e$ will be a straight line with a negative unity slope, assuming a constant $R_e$ value; and $D_e$ will be a straight line having a positive unity slope. The total $D$ will be a hyperbolic curve asymptotic to $D_e$ and $D_h$ and having a vertical axis. Thus, $D$ will have a minimum value at that frequency which makes $D_e$ equal to $D_h$ and will be the reciprocal of the familiar $Q$ versus frequency curve. $D_e$ thus predominates at low frequencies and $D_h$ at high frequencies.

Without trying to compute $D_h$, $D_e$ may be evaluated from (49). Then, using (50), the ratio

$$\frac{D_e + D_h}{D - D_e} = \frac{P_e}{P_e + P_h}$$  \hspace{1cm} (51)

will give the fractional part of the total core loss $P_e$ which is due to eddy currents. Consequently,

$$P_e = \frac{D_e P_e}{D - D_e},$$  \hspace{1cm} (52)

and, finally,

$$P_h = P_e - P_e.$$  \hspace{1cm} (53)

Empirical data illustrating this procedure are given in Appendix C.

**A.S.T.M. Testing Methods**

The A.S.T.M. has compiled a useful series of standardized testing procedures for the measurement of $\mu$ and $P_e$, which embody the principles that have been discussed. Lack of space prevents a further detailed analysis of these procedures herein. The reader should remember that their validity depends upon certain limitations; namely, (1) that $H$ must be evaluated in terms of true magnetizing current; (2) that a bridge-measured $\mu$ must be computed in terms of $L'$; and (3) that, if flux distortion exists, $B$ must be obtained from (21) rather than from (23). It will be shown in Appendix D, however, that in the presence of flux distortion, values of $\mu$ determined by (25) and, independently, by (19) will agree within observational errors, provided that instruments tuned to the fundamental frequency are used.


ACKNOWLEDGMENT

The author wishes to thank S. L. Burgwin of the Westinghouse Electric Corporation for permission to use his valuable hysteresis-loop data. He is also indebted to his colleague, R. F. Field, for many helpful suggestions in the preparation of this paper.

APPENDIX A

SINUSOIDAL H VERSUS SINUSOIDAL B
ERROR IN USING FIG. 1

The following appendices give data taken upon a 25-cm. Epstein square loaded with 29-gauge Wheeling VII 72 silicon steel. Measurements were made with an Owen bridge using a harmonic analyzer as a null detector. This instrument also served as a tuned voltmeter for current and voltage measurements. Unless otherwise noted, the bridge was excited at a frequency of 60 cycles.

In order to ascertain the differences existing between measurements made under conditions of sinusoidal \( H \) and, again, under conditions of sinusoidal \( B \), the data depicted in Figs. 8 and 9 were obtained. The tuned voltmeter permitted normal \( B \) values to be evaluated from (25), while normal \( H \) was obtained from (22) and normal \( \mu \) values were computed from (27).

![Fig. 8—Sinusoidal \( B \) versus sinusoidal \( H \) data.](image)

In the first run the generator resistance was made sufficiently high (20 kilohms) to ensure sinusoidal \( H \). In Fig. 8 the curves \( \mu_1 \), \( B_1 \), and \( d_1 \) show the variations of \( \mu \), \( B \), and the simultaneous percentage distortion in \( B \) versus normal \( H \). In the second run the generator resistance was essentially a 10-ohm bridge arm, resulting in closely sinusoidal \( B \) conditions, and yielded the corresponding curves \( \mu_2 \), \( B_2 \), and \( d_2 \), the latter giving the simultaneous distortion in \( H \).

Fig. 9 shows the core-loss values \( P_1 \) (sinusoidal \( H \)) and \( P_4 \) (sinusoidal \( B \)) computed from either (43) or (44).

From the foregoing data it will be seen that the distinction between sinusoidal \( H \) and sinusoidal \( B \) measurements was not measurable below an \( H \) of 0.15; that it was most pronounced in the region of \( \mu_{\text{max}} \), and finally became less significant at higher induction values. Maximum differences of about 8 per cent in \( \mu \) and \( B \) and about 5 per cent in \( P_e \) were observed.

The inductor had a dissipation factor which varied between 0.4 and 0.8. Accordingly, if the erroneous assumptions of Fig. 1 are used and the permeability is computed directly in terms of series inductance and the geometry of the Epstein square, while a pseudo-\( H \) is evaluated in terms of the full exciting current, the curves \( \mu_3 \) (sinusoidal \( H \)) and \( \mu_4 \) (sinusoidal \( B \)) in Fig. 8 are obtained. The substantial departure between these curves and those depicting the true values \( \mu_1 \) and \( \mu_2 \) is apparent.

APPENDIX B

DATA SUPPORTING THE HYPOTHESIS OF EDDY-CURRENT SHIELDING; EFFECT OF COPPER LOSS

The following typical data (Table I) taken from the U. S. Steel Technical Bulletin No. 2 for their Motor Grade (2% per cent silicon) show the decrease in normal \( \mu \) with increasing sheet thickness for specific values of normal \( H \).

<table>
<thead>
<tr>
<th>Gauge</th>
<th>( H = 0.4 )</th>
<th>( H = 1.05 )</th>
<th>( H = 4.0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>29</td>
<td>2750</td>
<td>6100</td>
<td>3000</td>
</tr>
<tr>
<td>26</td>
<td>2200</td>
<td>5780</td>
<td>2890</td>
</tr>
<tr>
<td>24</td>
<td>2100</td>
<td>5400</td>
<td>2810</td>
</tr>
</tbody>
</table>

To investigate the effect of frequency variation, the author made the Owen-bridge determinations of normal \( \mu \) upon the 25-cm. Epstein, while maintaining a con-
and core loss using tuned and untuned voltmeters in the presence of $B$ and $H$ distortion, the Owen-bridge data were taken upon the Epstein square as shown in Table IV. Values of normal $\mu$ were then computed from (27) and values of $R'$ from (16). Simultaneous values of $J_{sec}$ were obtained with a voltmeter across a 100-ohm resistive arm of the bridge carrying $I_{sec}$, whence the magnetizing current was computed from (18) and normal $H$ from (22). Simultaneous values of $E_{sec}$ were obtained from the voltage induced in the secondary winding and the turns ratio, whence normal $B$ was computed from (25).

Each of these two voltage measurements was made with two different instruments, a tuned voltmeter (harmonic analyzer) tuned to the fundamental frequency, and an untuned vacuum-tube voltmeter. A harmonic analysis of $J_{sec}(H)$ and of $E_{sec}(B)$ was likewise made. From the data a second (independent) value of normal permeability $\mu_A$ was computed as the $B/H$ ratio obtained with the tuned voltmeter, and a third value $\mu_B$ as the $B/H$ ratio obtained with the untuned voltmeter. Using the tuned voltmeter readings, core-loss power was evaluated in two independent ways, $P_1$ from (43) and $P_2$ from (44).

### APPENDIX C

**AN ANALYSIS OF CORE LOSS INTO $P_A$ AND $P_*$**

Using the data given in Appendix B and equations (17) and (49) through (53), together with the measured data $R_e = 1.81$ ohms, $\delta = 0.0384$ cm., and $\rho = 66.7 \times 10^{-4}$ ohm-cm., the following data were computed as shown in Table III.

### TABLE III

<table>
<thead>
<tr>
<th>$f$ (c.p.s.)</th>
<th>$P_*$ (mw.)</th>
<th>$P_\lambda$ (mw.)</th>
<th>$P_\mu f$</th>
<th>$P_\mu /f$</th>
<th>$P_\mu /P_\lambda$</th>
<th>$P_\mu /P_*$</th>
</tr>
</thead>
<tbody>
<tr>
<td>33.3</td>
<td>0.006</td>
<td>0.139</td>
<td>54x10^-7</td>
<td>417x10^-4</td>
<td>0.043</td>
<td>0.96</td>
</tr>
<tr>
<td>50</td>
<td>0.014</td>
<td>0.201</td>
<td>56</td>
<td>402</td>
<td>0.063</td>
<td>0.94</td>
</tr>
<tr>
<td>75</td>
<td>0.022</td>
<td>0.264</td>
<td>55</td>
<td>418</td>
<td>0.078</td>
<td>0.92</td>
</tr>
<tr>
<td>100</td>
<td>0.032</td>
<td>0.318</td>
<td>57</td>
<td>424</td>
<td>0.091</td>
<td>0.91</td>
</tr>
<tr>
<td>150</td>
<td>0.056</td>
<td>0.421</td>
<td>56</td>
<td>421</td>
<td>0.117</td>
<td>0.88</td>
</tr>
<tr>
<td>200</td>
<td>0.126</td>
<td>0.657</td>
<td>56</td>
<td>425</td>
<td>0.165</td>
<td>0.83</td>
</tr>
<tr>
<td>250</td>
<td>0.225</td>
<td>0.865</td>
<td>56</td>
<td>423</td>
<td>0.206</td>
<td>0.79</td>
</tr>
<tr>
<td>300</td>
<td>0.350</td>
<td>1.08</td>
<td>56</td>
<td>432</td>
<td>0.244</td>
<td>0.76</td>
</tr>
<tr>
<td>400</td>
<td>0.50</td>
<td>1.32</td>
<td>56</td>
<td>440</td>
<td>0.276</td>
<td>0.72</td>
</tr>
<tr>
<td></td>
<td>0.89</td>
<td>1.78</td>
<td>56</td>
<td>445</td>
<td>0.335</td>
<td>0.66</td>
</tr>
</tbody>
</table>

At the frequency of 63.5 c.p.s. the $D_i$ and $D_\lambda$ values were closely identical, while $D$ had its minimum value.

The constancy of the two ratios $P_\mu f$ and $P_\mu /f$ attests the validity of this analysis and of (50), even though the theoretically linear graphs of $D_i$, $D_\lambda$, and $D_\mu$ may have small curvatures due to the slow variation of inductance with frequency.

### APPENDIX D

**INTERCOMPARISON OF METHODS**

To compare the methods of measuring permeability and core loss using tuned and untuned voltmeters in the presence of $B$ and $H$ distortion, the Owen-bridge data were taken upon the Epstein square as shown in Table IV. Values of normal $\mu$ were then computed from (27) and values of $R'$ from (16). Simultaneous values of $J_{sec}$ were obtained with a voltmeter across a 100-ohm resistive arm of the bridge carrying $I_{sec}$, whence the magnetizing current was computed from (18) and normal $H$ from (22). Simultaneous values of $E_{sec}$ were obtained from the voltage induced in the secondary winding and the turns ratio, whence normal $B$ was computed from (25).

Each of these two voltage measurements was made with two different instruments, a tuned voltmeter (harmonic analyzer) tuned to the fundamental frequency, and an untuned vacuum-tube voltmeter. A harmonic analysis of $J_{sec}(H)$ and of $E_{sec}(B)$ was likewise made. From the data a second (independent) value of normal permeability $\mu_A$ was computed as the $B/H$ ratio obtained with the tuned voltmeter, and a third value $\mu_B$ as the $B/H$ ratio obtained with the untuned voltmeter. Using the tuned voltmeter readings, core-loss power was evaluated in two independent ways, $P_1$ from (43) and $P_2$ from (44).

### TABLE IV

<table>
<thead>
<tr>
<th>$H$ in $f$</th>
<th>Distortion</th>
<th>$\mu$</th>
<th>$\mu_A$</th>
<th>$\mu_B$</th>
<th>$P_1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.37</td>
<td>37.5</td>
<td>5.410</td>
<td>0.980</td>
<td>1.482</td>
<td>0.973</td>
</tr>
<tr>
<td>1.74</td>
<td>34.7</td>
<td>6.600</td>
<td>0.974</td>
<td>1.373</td>
<td>0.909</td>
</tr>
<tr>
<td>1.323</td>
<td>29.6</td>
<td>7.990</td>
<td>0.977</td>
<td>1.305</td>
<td>0.929</td>
</tr>
<tr>
<td>1.000</td>
<td>25.5</td>
<td>9.320</td>
<td>0.977</td>
<td>1.212</td>
<td>0.967</td>
</tr>
<tr>
<td>0.756</td>
<td>21.0</td>
<td>10.800</td>
<td>1.008</td>
<td>1.156</td>
<td>1.043</td>
</tr>
<tr>
<td>0.576</td>
<td>19.7</td>
<td>11.800</td>
<td>1.045</td>
<td>1.090</td>
<td>1.096</td>
</tr>
<tr>
<td>0.431</td>
<td>17.8</td>
<td>12.200</td>
<td>1.002</td>
<td>1.038</td>
<td>1.007</td>
</tr>
<tr>
<td>0.341</td>
<td>15.7</td>
<td>11.630</td>
<td>1.008</td>
<td>1.010</td>
<td>1.012</td>
</tr>
<tr>
<td>0.272</td>
<td>13.9</td>
<td>9.570</td>
<td>1.040</td>
<td>1.009</td>
<td>1.075</td>
</tr>
<tr>
<td>0.203</td>
<td>12.0</td>
<td>6.190</td>
<td>0.995</td>
<td>0.988</td>
<td>0.988</td>
</tr>
<tr>
<td>0.149</td>
<td>10.1</td>
<td>2.410</td>
<td>1.024</td>
<td>0.990</td>
<td>1.060</td>
</tr>
</tbody>
</table>

Recalling that the accuracy of the $\mu_A$, $\mu_B$, $P_1$, and $P_2$ values depends upon the precision of voltmeter readings, the close equality between the two independent values $\mu$ and $\mu_A$ and between $P_1$ and $P_2$ is evident. The value of $\mu_B$ ($B/H$ ratio obtained with an untuned voltmeter) progressively diminishes from the true $\mu$ value as the distortion in $B$ increases, demonstrating that (25) is valid only for sinusoidal components and that, with flux distortion, (23) must be used.

### APPENDIX E

**EFFECT OF SHEARING ON NORMAL $\mu$ AND CORE LOSS**

The 3-cm. strips were then removed from the Epstein square and each sliced longitudinally to give three strips each one cm. wide. Each of two pieces was thus subjected to a shearing strain along one of its edges, while the third piece was subjected to shearing strains along both of its edges. The same iron was then replaced in the
Epstein square and a duplicate test run was made. By interpolation, the percentage changes in normal $\mu$ and core loss for specific values of $H$, and again for specific values of $B$, were determined as shown in Table V.

<table>
<thead>
<tr>
<th>$H$ (oersteds)</th>
<th>Original $\mu$</th>
<th>Per Cent Change in $\mu$</th>
<th>Original $P_e$ (watts)</th>
<th>Per Cent Change in $P_e$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.20</td>
<td>6,050</td>
<td>+ 0.7</td>
<td>0.175</td>
<td>0.0</td>
</tr>
<tr>
<td>0.30</td>
<td>10,580</td>
<td>− 1.7</td>
<td>0.355</td>
<td>− 2.8</td>
</tr>
<tr>
<td>0.40</td>
<td>12,070</td>
<td>− 3.3</td>
<td>0.52</td>
<td>− 6.8</td>
</tr>
<tr>
<td>0.50</td>
<td>12,150</td>
<td>− 4.3</td>
<td>0.87</td>
<td>− 11.5</td>
</tr>
<tr>
<td>0.75</td>
<td>10,700</td>
<td>− 8.1</td>
<td>1.13</td>
<td>− 8.9</td>
</tr>
<tr>
<td>1.00</td>
<td>9,320</td>
<td>− 4.9</td>
<td>1.57</td>
<td>− 8.3</td>
</tr>
<tr>
<td>1.50</td>
<td>7,570</td>
<td>− 4.2</td>
<td>1.96</td>
<td>− 8.2</td>
</tr>
<tr>
<td>2.00</td>
<td>6,120</td>
<td>− 3.4</td>
<td>2.33</td>
<td>− 8.2</td>
</tr>
<tr>
<td>2.50</td>
<td>5,170</td>
<td>− 2.9</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The effect of shearing strains is seen to be: a reduction in $\mu$ (except at low induction), a reduction in core loss for specific values of $H$, and an increase in core loss for specific values of $B$. For specific values of $H$ a maximum fractional change in both $\mu$ and $P_e$ occurs at an $H$ value which is somewhat in excess of that corresponding to $\mu_{\text{max}}$. For specific values of $B$, the effect of shearing upon $\mu$ and $P_e$ increases progressively with rising values of induction.

**APPENDIX F**

The author has used with success a method of measuring $\mu$ which involves a direct determination of the angles $\phi$ or $\beta$ by means of a cathode-ray oscillographic (see Fig. 10). A suitable resistance $R$ is placed in series with the specimen inductor and shunted by a peak-reading voltmeter, so that the ratio $\varepsilon_{\text{m}}/R$ gives the value of the exciting current. The adjustable high-resistance voltage divider $P$ draws no appreciable current through $R$. The source generator $E_t$ through a transformer feeds a phase-shifting network consisting of two equal fixed capacitors $C$ and two equal adjustable resistors $r$. With low input and high output impedances, the output voltage of this network is essentially constant and has a phase displacement $\alpha$ from the input voltage given by

$$\tan \alpha = \frac{2\omega C}{1 - r\omega^2 C^2}. \quad (54)$$

Joint adjustment of the two $r$ resistors thus varies the phase of the reference voltage $E_{\text{ref}}$ (output of the amplifier $A_1$) which is applied to the horizontal deflectors of the c.r.o. By means of the switch $B-H$ either the voltage drop across $R$ or a suitable portion of the terminal voltage may be applied through the amplifier $A_4$ to the vertical deflectors.

If copper loss may be considered negligible, the exciting voltage may be taken to be the terminal voltage read on the high-impedance voltmeter $E_f$. The operating procedure is as follows: With the switch open, adjust the gain of the amplifier $A_1$ to give an appropriate length of the vertical sweep on the screen. Close the switch to the $H$ position and adjust the phase network to reduce the elliptical pattern on the screen into a line with, say, a positive slope. The phase of the reference voltage $E_{\text{ref}}$ having a relative displacement $\alpha_H$ has thus been matched to the phase of the exciting current. The most accurate determination of this matching may be made if the slope of the line is made approximately $45^\circ$ by an appropriate gain adjustment of the amplifier $A_3$. Any distortion in $H$ will introduce curvature into the line, in which case the center portion should be closed. Leaving the amplifier $A_3$ unchanged, throw the switch to the $B$ position and readjust the phase network to provide a new relative displacement $\alpha_B$ which will match the phase of $E_{\text{ref}}$ with the terminal voltage of the inductor, resulting in a line with a positive slope which may be approximated to $45^\circ$ by adjustment of the potentiometer $P$. The phase angle $\phi$ of the inductor will then be the algebraic difference between the two relative displacements $\alpha_H$ and $\alpha_B$.

Normal magnetizing force may then be computed by substituting (9) into (22). For measurements with sinusoidal $B$ (small $R$ values), the voltmeter $E_f$ must read peak values. Substituting $E_T$ for $E_{\text{ess}}$ in (25) gives the normal induction, whence the normal permeability becomes

$$\mu = \frac{10^3 \lambda R}{0.4 \pi N^2 l \omega \sin \phi \left( \frac{E_f}{E_R} \right)}. \quad (55)$$

For measurements with sinusoidal $H$ (large $R$ values) the voltmeter $E_T$ must read average values and normal induction obtained from (28). In this case normal permeability is given by

$$\mu = \frac{10^3 \lambda R}{0.8 N^2 A \omega \sin \phi \left( \frac{E_T \text{ (av.)}}{E_R} \right)}. \quad (56)$$
Copper losses could be taken into account in this method by substituting the factor \( \cos \beta \) for \( \sin \phi \) in (55) and (56) and substituting (8) into (22). The angle \( \beta \) can be measured by connecting the \( B \) contact of the switch across an appropriate number of secondary turns on the inductor. The observed displacement \( \alpha_{B} \) would then be the angle between \( E_{ac} \) and the induced voltage. It follows that the algebraic difference between the two relative displacements \( \alpha_{H} \) and \( \alpha_{B} \) will be the angle between \( E_{ind} \) and \( I_{sec} \), and hence will equal \( \beta \) plus \( \pi/2 \). The voltmeter reading \( E_{F} \) would be replaced by \( E' \) across the secondary winding, as indicated in the lower portion of Fig. 10, so that its peak or its average reading divided by the turns ratio would give the exciting voltages to replace the corresponding terminal voltages in (55) or (56).

**APPENDIX G**

**Units of Magnetic Measurement**

There are currently three systems of magnetic units in use. Since some confusion exists in the interpretation of these systems and the relationships between them, the following summary was considered desirable.

The A.S.T.M. specifications embody the nonrationalized c.g.s. electromagnetic system of units (used in this paper) in which magnetomotive force \( F \), measured in gilberts, is given by 0.4π times the ampere-turns circumscribing the flux path, and the unit of reluctance \( R \), sometimes called the "magnetic ohm," is the reluctance across a centimeter cube of free space. Magnetic flux \( \Phi \), measured in maxwells or "lines," is then the ratio \( F/R \). In a symmetrical and homogeneous flux path the magnetizing force \( H \), measured in oersteds, is the ratio \( F/\lambda \); while the induction \( B \), measured in gausses, is the ratio \( \Phi/\lambda \). In this system permeability \( \mu \) is the ratio \( B/H \) evaluated in gausses per oersted, and has a value of unity in free space.

In the practical nonrationalized m.k.s. electromagnetic system, \( F \) is measured in pragilberts and given by 4π times the ampere-turns, so that a pragilbert is in reality a decigilbert. The unnamed unit of reluctance may be defined as 10−4 m.k.s. magnetic ohms. Flux is measured in webers, one weber being 106 m.k.s. maxwell. \( H \) is measured in praeoersteds (pragilberts per meter), so that a praeoersted is a milliweber. \( B \) is measured in a unit (webers per square meter) which equals 10 kilogausses. Hence, in this system the permeability of free space has a value of 10−7.

In the rationalized m.k.s. electromagnetic system \( F \) is measured directly in ampere-turns, while the units of \( \Phi \) and \( B \) remain the same as in the nonrationalized m.k.s. system. Consequently, the rationalized m.k.s. units of \( F, R, \) and \( H \) are each larger than the corresponding nonrationalized m.k.s. units by the factor 4π and the permeability of free space becomes 4π×10−7. The conversion tables shown in Table VI may be used.

<table>
<thead>
<tr>
<th>TABLE VI</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Converting c.g.s. into nonrationalized m.k.s. values</td>
</tr>
<tr>
<td>To convert</td>
</tr>
<tr>
<td>( F ) in gilberts</td>
</tr>
<tr>
<td>( R ) in magnetic ohms</td>
</tr>
<tr>
<td>( \Phi ) in maxwells</td>
</tr>
<tr>
<td>( H ) in oersteds</td>
</tr>
<tr>
<td>( B ) in gausses</td>
</tr>
<tr>
<td>( \mu ) c.g.s.</td>
</tr>
</tbody>
</table>

| II. Converting c.g.s. into rationalized m.k.s. values |
| To convert | multiply by |
| \( F \) in gilberts | \( F \) in ampere-turns | 10/4π |
| \( R \) in magnetic ohms | \( R \) in m.k.s.-\( R \) units | 10−3 |
| \( \Phi \) in maxwells | \( \Phi \) in webers | 10−3 |
| \( H \) in oersteds | \( H \) in ampere-turns/meter | 10−3 |
| \( B \) in gausses | \( B \) in webers/square meter | 10−4 |
| \( \mu \) c.g.s. | \( \mu \) m.k.s.-\( R \) | 4π×10−7 |

| III. Converting nonrationalized m.k.s. into rationalized m.k.s. values |
| To convert | divide by |
| \( F \) in pragilberts | \( F \) in ampere-turns | 4π |
| \( R \) in m.k.s. (\( N \)-\( R \)) | \( R \) in m.k.s.-\( R \) units | 4π |
| \( \Phi \) in webers | \( \Phi \) in webers | 1 |
| \( H \) in praeoersteds | \( H \) in ampere-turns/meter | 4π |
| \( B \) in webers/square meter | \( B \) in webers/square meter | 1 |
| \( \mu \) m.k.s. (\( N \)-\( R \)) | \( \mu \) m.k.s.-\( R \) | 1/4π |

**The Degenerative Positive-Bias Multivibrator**

**SIDNEY BERTRAM†, SENIOR MEMBER, I.R.E.**

Summary—The operation of a multivibrator with positive grid supply and cathode degeneration is described. It is shown that, for suitable circuit parameters, the frequency of the multivibrator is very nearly a linear function of the applied grid voltage. Since the grid voltage can be controlled with relatively simple auxiliary circuits, the positive-bias multivibrator becomes a useful variable-frequency source.

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describe the operation of a multivibrator operating with positive grid return and cathode degeneration, and to show that it is possible to choose the circuit constants so as to make the grid-voltage versus frequency relationship extremely linear over a frequency range of well over an octave. This inherent linearity should make the multivibrator adaptable to a wide variety of applications.

The multivibrator shown in Fig. 1 consists of a two-stage resistance-coupled amplifier with the output coupled back to the input so that the circuit is regenerative. The mode of operation is easily seen.

Suppose the multivibrator has just been turned on and is not yet oscillating. Any disturbance during the warm-up period would then be amplified regeneratively until it started the oscillation. Thus, if the plate current of tube \( T_2 \) is momentarily increased, it would start the following chain of reactions: (a) the plate voltage of \( T_2 \) would decrease; (b) the grid of \( T_1 \) would become more negative; (c) the plate current of \( T_1 \) would decrease, allowing the plate voltage to increase; (d) the grid of \( T_2 \) would become more positive; and (e) the plate current of \( T_2 \) would increase, adding to the original change that started the reaction.

If the over-all gain around the loop is greater than unity, the system is unstable; in this case the reaction will progress at a rapid rate until tube \( T_1 \) is cut off, so that its plate is at substantially the voltage of the supply, while \( T_2 \) has its grid positive with respect to its cathode and considerable drop across its plate load (time \( A \) in Fig. 2). The voltage on the grid of \( T_1 \) now rises as the coupling capacitor charges, approaching the voltage of the grid supply \( E_c \) asymptotically. When the grid of \( T_1 \) nears the cutoff voltage, \( T_1 \) starts to conduct (\( B \) in Fig. 2), so that its plate becomes increasingly negative. This reduces the voltage on the grid of \( T_2 \), causing its plate to become increasingly positive and thus accelerating the already rising voltage on the grid of \( T_1 \). When \( T_1 \) becomes sufficiently conducting to make the combined gain of \( T_1, T_2 \) greater than unity, the circuit "flips over"; i.e., the two tubes change places, the grid of \( T_1 \) becoming positive with respect to its cathode while the grid of \( T_2 \) is driven below the cutoff voltage. The operation is then repeated, the grid of \( T_2 \) rising exponentially until \( T_2 \) becomes conducting, when a second flip-over occurs, etc.

The above analysis has neglected the small but observable effect of grid current on the operation of a multivibrator. When the multivibrator flips over, the grid of the tube, becoming conducting, goes positive with respect to its cathode. This prevents the plate voltage of the opposite tube from immediately reaching the plate-supply voltage (being restrained by the grid current). As the coupling capacitor charges, the grid voltage of the conducting tube decreases, allowing its plate voltage to increase; this change in plate voltage is carried over to the grid of the nonconducting tube, modifying the rate of rise of its grid voltage. In a multivibrator it is important that \( R_e \) be large compared to \( R_L \) (grid-circuit time constant large compared to plate-circuit time constant), so that the grid current will decrease to a low value, compared to its maximum value immediately following a flip-over, before the next flip-over occurs; otherwise, the grid current will affect the stability of the multivibrator. Another factor that affects the multivibrator operation is the input capacitance of the tubes, which reduces the signal to the grids; this is particularly true at high frequencies where the coupling capacitance is small.
The period of the multivibrator is dependent upon the amplitude of the oscillations, the resistance-capacitance combination in the grid circuit, and the voltage to which the grids are returned. The half-period is very nearly the time necessary for the grid to change from its highly negative voltage following the flip-over to the cutoff voltage. The period will be increased by (a) increasing the amplitude of oscillations by increasing the plate load resistance or decreasing the cathode resistance; (b) increasing either the resistance or capacitance in the grid circuit, thus decreasing the rate at which the capacitor charges; and (c) decreasing the grid-return voltage \( E_r \), thus decreasing the rate at which the capacitor charges.

The voltage versus frequency relationship of a multivibrator is fairly linear (except at very low or very high grid-supply voltages) for any circuit values. The relationship has an inflection point, and it is possible to choose the circuit parameters so that the point of inflection is at the center of the desired operating range of \( E_v \). In designing a multivibrator, it is convenient to adjust the cathode resistance \( R_k \) to obtain the desired linearity; the grid-circuit parameters \((R_v, C)\) can then be adjusted to give the desired operating range.\(^3\) When this adjustment is properly made it is found that the grid-voltage versus frequency relationship is quite linear. Thus, in Fig. 3 the curve is slightly concave downwards for \( R_k = 0 \), very linear for \( R_k = 1000 \) ohms, and concave up for \( R_k = 2000 \) ohms. It is not possible to show the degree of linearity obtainable on the curve.

In making the measurements, the frequency was set at harmonics of a low-frequency standard (5000 c.p.s.) by varying the grid-return voltage, and the voltage then read on a three-decade potentiometer. A change in \( \beta \) from 0.3 to 0.7 resulted in a change in frequency from 37 to 70 kilocycles with a departure from linearity of less than ±200 c.p.s. It is particularly significant that this linear operation is essentially independent of the tubes used, so long as their characteristics fall within normal limits. Thus, once a suitable set of values is obtained, the results can be duplicated with only ordinary care in choosing the elements.

Since the grid return is a high-impedance circuit, the voltage can be varied dynamically, if desired, using low-power circuits. Here the high degree of linearity obtainable makes the positive-bias multivibrator very useful as a frequency-modulated source.

**APPENDIX**

The frequency of a multivibrator can be approximated in terms of the constants of Figs. 1 and 2. When a grid is rising exponentially from its maximum negative value (taken at time \( t = 0 \)), its instantaneous voltage can be expressed as

\[
e_v = \left[ E_e - (E_e - E_{in})e^{(t/t_{m}C_e)} \right]
\]

where \( C_e = C + C_{in} \) is the effective capacitance in the discharge circuit. The circuit will flip over when \( e_v \) reaches the cutoff value \( E_{vo} = -(E_e/\mu) \); the value of \( t \) for this cutoff condition is the half-period of the multivibrator, and thus determines the frequency. The voltage \( E_{vo} \) is found as follows:\(^3\):

\[
E_{vo} = E_v - (E_b - E_{in}) \left( \frac{C}{C + C_{in}} \right)
\]

where

\[
E_v = \frac{R_k E_b}{R_p + R_L + R_k}
\]

and

\[
(E_b - E_{in}) = \frac{R_L E_b}{R_p + R_L + R_k}.
\]

The frequency of a multivibrator can now be written

\[
f = \frac{1}{2R_x C_e \log\mu (\beta - \gamma)/\mu \beta + 1} \tag{1}
\]

where

\[
\beta = \frac{E_e}{E_b} \quad \text{and} \quad \gamma = \frac{E_{vo}}{E_b}.
\]

\(^3\) In calculating \( C_e \), the input capacitance is \( C_e = C_{ph} + C_{sp} + C_n \), the plate voltage being constant in the discharge period. In calculating \( E_v \), the voltage transferred from the plate to the other grid is reduced by the input capacitance; for this condition, \( C_{ex} \approx C_{ph} + 2C_{sp} + C_n \), because the plate voltage moves positively about the same amount that the grid moves negatively.
In deriving the frequency equation, the following simplifying approximations have been made. It is assumed that, before a flip-over occurs, an equilibrium condition is reached in which the grid of the conducting tube is at the same voltage as its cathode; the plate current is then determined by the intersection of the load line for the combined plate and cathode loads with the zero-bias plate current. The effective amplification factor is determined by the grid voltage at the effective cutoff point—the point where the over-all gain is just unity. Actually, a very good approximation is obtained if the values for $\mu$ and $R_p$ given in the tube manuals are used.

The frequency equation (1) is cumbersome and not readily interpreted. It can be transformed as follows: Let $\beta_0$ be the center of the operating range of $\beta$ and $x$ the deviation from the center, i.e., $\beta = \beta_0 + x$; then, if the additional substitutions $a = 1/\beta_0 - \gamma$ and $b = \mu/1 + \mu\beta_0$ are made, (1) becomes

$$ f = \frac{1}{2R_C(s) \log \frac{b}{a} + \log \frac{1 + ax}{1 + bx}}. $$

It is expedient at this point to expand the second logarithmic expression (involving $x$) in a power series; thus

$$ \log \left( \frac{1 + ax}{1 + bx} \right) \approx (a - b)x \left[ 1 - \left( \frac{a + b}{2} \right)x \right. $$

$$ + \left( \frac{a^3 - b^3}{3} \right)x^3 \left[ \left( \frac{a^4 - b^4}{4} \right)x^4 + \cdots \right] $$

$$ = (a - b)x \left[ 1 - \left( \frac{a + b}{2} \right)x \right. $$

$$ + \left( \frac{a^2 + ab + b^2}{3} \right)x^2 \left[ \left( \frac{a^3 + a^2b + ab^2 + b^3}{4} \right)x^3 + \cdots \right]. $$

If $a$ is not too different from $b$, then

$$ \frac{a^2 + ab + b^2}{3} \approx \left( \frac{a + b}{2} \right)^2, $$

and, in general,

$$ a^n + a^{n-1}b + a^{n-2}b^2 + \cdots + b^n \approx \left( \frac{a + b}{2} \right)^n. $$

Thus, the above series is approximated by the new series

$$ \log \left( \frac{1 + ax}{1 + bx} \right) \approx (a - b)x \left[ 1 - \left( \frac{a + b}{2} \right)x \right. $$

$$ + \left( \frac{a + b}{2} \right)^2 x^2 - \left( \frac{a + b}{2} \right)^3 x^3 + \cdots \right] $$

$$ \approx \frac{(a - b)x}{1 + \left( \frac{a + b}{2} \right)x}. $$

In terms of this approximation the frequency equation becomes

$$ f \approx \frac{1}{2R_C(s) \log \frac{b}{a} + \log \left( \frac{a + b}{2} \right) \frac{b}{a} \left( \frac{a - b}{a + b} \right)} $$

$$ \left[ 1 + \left( \frac{a + b}{2} \right)x \right] \beta. $$

It is possible to adjust the circuit parameters so that the coefficient of $x$ in the denominator vanishes. Thus, if $(a + b/2) \log b/a - b - a$, the denominator is constant and the frequency becomes a linear function of the grid-return voltage $\beta = E_c/E_b$. Under these conditions the frequency equation takes the simplified form

$$ f \approx \frac{1 - \left( \frac{a + b}{2} \right) \beta_c}{2R_C(s) \log \frac{b}{a} + \frac{a + b}{4R_C(s) \log \frac{b}{a}} \beta} $$

$$ \frac{1 + \left( \frac{a + b}{2} \right)x \beta}{\beta_c} + \frac{a + b}{4R_C(s) \log \frac{b}{a}} \beta $$

$$ \frac{R_K - R_L}{R_p + R_L + R_K} \frac{C}{C + C_i}, $$

$$ \gamma = \frac{R_K - R_L}{R_p + R_L + R_K} \frac{C}{C + C_i} \cdot $$

For a multivibrator employing two 6J5 tubes, with $R_L = 5000$ ohms, $R_K = 1000$ ohms, $R_p = 270,000$ ohms, and $C = 100$ $\mu$fd. (also, from tube manuals, $R_p = 7700$ ohms, $\mu = 20$, and including 5 $\mu$fd. of stray capacitance, $C_i = 22$ $\mu$fd.), (5) reduces to

$$ f \approx \left( 11 + 888 \right) \times 10^3 \text{ c.p.s.} $$

where $\beta_0$ has been taken at $\beta = 0.5$.

The three experimental curves of Fig. 3 illustrate the effect of varying the cathode degeneration. With zero resistance the frequency characteristic is very slightly concave downwards; with 1000 ohms the characteristic is extremely linear over a range of about two octaves. With larger values of cathode resistance the frequency characteristic is concave upwards. The dotted line is the straight-line frequency variation of (6).
A Variable-Radio-Frequency-Follower System*

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Summary—This paper deals with a new follow-up or servo system for amplification of mechanical forces and remote positioning. The system described makes use of variable radio frequencies representative of the respective positions of system leader and follower. Two parallel-resonant circuits are provided, one of which is the frequency-determining circuit of an oscillator, while the other is the balance-frequency-determining circuit of a balanced-frequency discriminator. One of the circuits can be tuned by the leader, while the other is tuned by the follower; or, one of the circuits can be tuned by both leader and follower. System balance is reached when both circuits are tuned to the same frequency. Of the possible variety of system modifications, four significant types are described with their particular applications. The system provides for low-frequency keying of the radio-frequency signal before application to the frequency discriminator, in order to obtain a low-frequency-discriminator output signal of one phase or opposite phase, depending upon the direction of system unbalance. For system balance no discriminator output signal is produced. The low-frequency signal is used to control a two-phase induction motor driving the follower.

System design considerations and performance data are given. Wide-band frequency-discriminator tuning is discussed with respect to constant system sensitivity. Experimental and production models are described.

In the past few years much development work has been done in the field of follow-up or servo systems for use either solely for amplification of mechanical forces or for remote positioning and metering. The multitude of different systems, their requirements and applications, and their limitations, is too great for even a brief discussion in this paper. It may be sufficient to say that all of these systems include a circuit arrangement which can be unbalanced by a leader movement to produce an unbalance or error signal, which is amplified and used to control a power device or motor to move a follower to restore the balance of the circuit arrangement.

Depending upon the circuit arrangement, the unbalance signal usually consists of a d.c. signal of variable amplitude and polarity or a low-frequency a.c. signal of variable amplitude and phase. Some systems are applicable to wire transmission only, while some are applicable to wireless transmission.

The present system makes use of variable radio frequencies representative of the respective positions of leader and follower. For remote transmission, particularly, the use of a variable frequency has the advantage that the frequency of a transmitted signal of single frequency is not affected by changes in the characteristics of the transmission path, and therefore eliminates the need for transmission of an additional reference signal.

Furthermore, a system of this type can easily be designed for a multiplicity of receivers, any of which can be switched on and off without affecting the operation of the operating receivers.

Basically, the system comprises two separate tuned circuits which are tuned to the same frequency when the system is balanced. There are two species of this system. In the first, the balance frequency remains constant, and the detuning of one of the tuned circuits causes a follow-up action to restore its tuning to the original balance frequency. In the second species, a detuning of one of the tuned circuits is followed by a corresponding detuning of the second circuit. When both circuits are tuned to the same frequency the system is balanced. Obviously, in this species there exists a range of balance frequencies.

Fig. 1 shows four types of the system, all including a radio-frequency oscillator, a keying stage, a frequency discriminator, a voltage amplifier, a phase-sensitive power amplifier, and a two-phase induction motor. Keying is effected in phase and synchronism with the power amplifier and motor-energizing voltage.

Types (a), (b), and (c) operate at a fixed balance frequency determined by the fixed discriminator tuning. Types (a) and (b) are for amplification of mechanical forces alone, while type (c) can be used for short-distance remote transmission.

In type (d), both oscillator and discriminator are tuned, and the balance frequency varies over a relatively wide range. This system is unlimited in distance and can be used for wire and wireless transmission.

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In types (b), (c), and (d), the follower movement can be made to be practically any desired function of the leader movement, depending on the shape of the cam of type (b) and the shape of the capacitor plates of types (c) and (d). Inductive tuning can be used in place of capacitive tuning and has been used in types (b) and (d).

It may be noted that in the first three types the feedback loop extends around the entire system between motor and oscillator. In type (d), the feedback loop extends around a portion of the system only, between motor and discriminator.

Fig. 2 shows the discriminator characteristics typical of a conventional discriminator, such as used in frequency-modulation receivers and for automatic frequency control.

Such a discriminator delivers no output signal in the absence of an input signal as well as for an input signal of the frequency to which the discriminator is tuned. This is the system balance frequency \( f_0 \), at which no discriminator output signal is desired. For keyed radiofrequency signals of frequencies above and below \( f_0 \), a series of positive or negative pulses is obtained, containing a keying-frequency signal component of one phase or the other depending upon the direction of system unbalance.

Lines A and B indicate the discriminator output signal magnitudes at which the limiting action of the subsequent voltage amplifier takes place. Therefore, the shape of the discriminator characteristic above A and below B is of no consequence to the operation of the system.

A free choice of operating frequencies is governed by the following factors: The percentage change of frequency over the operating range should be as great as feasible in order to minimize the effects of frequency drifts. Such drifts can be caused by changes in temperature, relative humidity, and the like, and by supply-line variations.

The tuning elements should be of small physical size, and for remote positioning systems their total variation should be large as compared with their manufacturing tolerances.

The most-preferred compromise between these requirements was found to be a range of operating frequencies between 350 and 500 kc.

Fig. 3 shows a schematic circuit diagram of a torque amplifier and a typical damping system for step excursions. The torque amplifier proper is of the system type (a), and operates on a fixed balance frequency of 450 kc.

Leader and follower are parts of the same oscillator-tuning capacitor, the leader consisting of a small vane between two follower plates. The frequency excursion from the balance position to total vane and plate engagement and disengagement was about 50 kc. in an experimental model. Maximum and minimum capacitances were 48 and 17 \( \mu \)fd., respectively. Full motor torque and maximum follower speed was obtained for a leader movement of \( \frac{1}{4} \) degree rotation, or 0.1 per cent of maximum rotation. This vane movement corresponds to a capacitance change of less than 0.1 \( \mu \)fd., and produces a discriminator output signal of 2 volts peak to peak. The maximum permissible leader speed for the model, excluding the damping circuit, was 1 revolution in 7.4 seconds.

For higher speeds a damping circuit is provided including a buffer amplifier (B.A.) with a third resonant circuit tuned to the balance frequency. The magnitude of the signal across this circuit changes rapidly in the vicinity of system balance. This signal is rectified and differentiated to produce positive pulses on balance approach and negative pulses on departure from balance. The positive pulses are selected and used to actuate a control tube to inject a reverse-phase voltage into the system. This voltage is derived from the motor and is proportional to motor speed. With this arrangement, sudden braking of the motor is accomplished just
before balance is reached. Upon motor-speed reduction the feedback voltage diminishes and the gain of the control tube is reduced as the positive pulse decays until the negative-feedback damping circuit is inactivated when system balance is reached.

Fig. 4 shows a schematic circuit of a remote transmission system of the system type (d). The oscillator is tuned by the leader, while the discriminator secondary circuit is tuned by the follower. System balance is reached when both circuits are tuned to the same frequency. Keying is accomplished by applying a power-line-frequency voltage of, say, 60 cycles to the screen grid of the keyed amplifier. A trimmer capacitor in the discriminator secondary circuit is provided for zero adjustment, while a variable-inductance coil is provided for span adjustment. If leader and follower capacitors have straight-line-capacitance characteristics, zero adjustment is possible without changing span, while a span adjustment requires zero readjustment.

Fig. 5 illustrates the problem of obtaining constant sensitivity; that is, a constant discriminator output signal per unit-leader movement over the entire span, for straight-line-capacitance leader and follower capacitors for linear transmission. For such capacitors the frequency variation per unit-capacitance change is not linear, but varies as the cube of the ratio of the particular operating frequency to the maximum operating frequency, as shown by curve $\beta$. Also, the discriminator sensitivity—that is, the output signal per kilocycle frequency deviation—changes over the range of operating frequencies because of the fixed tuning of its primary circuit, and causes, therefore, the amplitude variation of its primary voltage as illustrated by curve $\gamma$. Fortunately, these two effects can be opposed, and by proper tuning and loading of the discriminator primary this curve can be so shaped that the system sensitivity $S = \beta \times \gamma$, and the discriminator output voltage per unit-leader movement can be made sufficiently constant over the operating range, as shown by curve $S$. In a particular case, the discriminator primary was tuned to 325 kc. and loaded with a resistance of 7500 ohms, for an operating range from 370 to 460 kc.

Fig. 6 shows a model of a torque amplifier (of type (a))
of Fig. 1) with a leader vane and two associated semi-
circular plates driven by the motor pinion, visible to
the left. This model uses the circuit substantially as
shown in Fig. 3, and the design and performance data
given in connection with that figure pertain to this
model.

Fig. 7 shows a model including a rate-of-flow meter
with a force amplifier of system type (b), and an inte-
grating flow meter with a torque amplifier of system
type (a). The circuits in both cases are substantially as
shown in Fig. 3.

Fig. 7—Model with force amplifier (type (b)) and torque
amplifier (type (a))

The rate-of-flow meter comprises a differential-bel-
lows arrangement with the movable capacitor plate
rigidly attached to the bellows diaphragm. This plate
is also attached by means of a spring to a cam-operated
lever, so that the movable plate is always returned to
the same relative position with respect to the fixed
capacitor plate by increasing or decreasing the spring
tension. By this action, the bellows diaphragm is also
always returned to the same position, thus reducing
bellows travel to a minimum in order to eliminate
hysteresis effects. The cam is provided for extracting
the square-root relation between the rate-of-flow and
the differential-bellows pressure. The pointer is coupled
to the cam, so that the angular cam position is indi-
cated on the scale.

The integrating flow meter comprises a constant-
speed turntable and a radially movable friction wheel
contacting the turntable at a radius depending upon the
rate-of-flow. Since such an arrangement should not be
mechanically loaded, the friction wheel shaft is pro-
vided with a leader vane, which is followed by a motor-
driven follower plate, forming a capacitor in co-opera-
tion with the leader vane. The number of follower revo-
lutions is counted to indicate flow.

The electronic equipment for the rate-of-flow and flow
meters is seen at the top of the case.

Fig. 8 and 9 show the transmitter and receiver,
respectively, of a remote plotting system, in which
movements of the transmitter writing stylus are faith-
fully followed by the receiver recording pen. This sys-
tem is of type (d) of Fig. 1, and uses two circuits, sub-
stantially as shown in Fig. 4, for the two co-ordinates.

Fig. 8—Remote-plotting-system transmitter.

Fig. 8 shows the stylus arm with the writing stylus.
The writing stylus is equipped with a pressure contact
for actuation of the recorder pen at the receiver. This
arm is mounted in gimbal joints and is coupled to the
rotors of two capacitors by way of correction cams,
provided to extract the tangent relations between the
position of the stylus point and the angle of the stylus
arm. The transmitter head includes the gimbal joints,
correction cams, oscillator-tuning capacitors, and asso-
ciated oscillators. The oscillators are keyed alternately,
so that only a single channel is required for transmitting
both co-ordinate-system signals.

Fig. 9 shows a receiver with the door open. This door,
equipped with a window 18X18 inches, carries the
transparent chart paper, on the back of which pen re-
cordings are made. This feature eliminates the obstruc-
tion of the record by the pen and its supporting and
acting mechanism.
To the right, the follower capacitors and their drive motors are visible. The pen carriage is supported by the cross bars, guided and driven by the drive motors by way of a rack-and-pinion arrangement and cable drive. The pen carriage also carries the pen-actuating relay, energized whenever the pressure contact at the transmitter stylus is closed.

The two receiver-amplifier units are alternately keyed in phase and synchronism with the transmitter oscillator keying, so that only corresponding transmitter oscillators and receiver amplifiers are operated at any time.

This system is connected as a wired radio system and operates over a frequency range of 370 to 460 kc, with a pen speed of 12 inches per second. A typical warm-up drift, for which the system is not compensated, is about 0.2 per cent of full-scale travel. Pen movements due to temperature and supply-voltage changes are inconsequential. The system accuracy, including all tolerances, was found to be about 0.3 per cent, on the average, while the repeatability was about 0.03 per cent or better.

In a typical system one to six receivers are selectively or simultaneously connected to one transmitter. Failure of one receiver does not affect the operation of the other connected receivers.

Apparatus of the remote positioning type has been used successfully for production checking of coil inductances with the aid of high- and low-limit coils. Small tolerances can be spread over a large-scale portion for ease of reading and accurate checking. Another possible application of this system is the constant-frequency regulation of oscillators, such as the oscillator of a frequency-modulation transmitter.

The broad idea of using the frequency of a signal for remote transmission of the variation of a condition is not new, and various other systems based on this idea have been proposed. In concluding this paper, a brief comparison of the present system with others is presented.

Systems have been suggested in which an unkeyed radio-frequency signal is applied to a discriminator, to which a low-frequency keying voltage is also applied. In order to maintain a usable wave shape of the discriminator output signal for efficient motor drive, the applied keying voltage must be considerably greater than the applied radio-frequency signal. This makes for low discriminator sensitivity and makes the system highly susceptible to slight discriminator unbalances. This is a disadvantage which is not present in the new system.

In another system a steady low-frequency component due to the discriminator keying voltage is present even for system balance, and considerably reduces the efficiency of the amplifier between discriminator and motor.

Certain proposed audio-frequency systems use frequency indicators as output devices. Since these arrangements have very low-torque output, they are not, per se, suitable for remote power positioning.

Some proposed systems use a radio-frequency or superaudible signal, the frequency of which is varied over a narrow range and then heterodyned to produce a variable audio frequency. In such systems any error due to undesired frequency drift is extremely serious, because the system error is determined by the ratio of frequency error to the operating-frequency range, which, in other words, is simply the noise-to-signal ratio. Consequently, the narrower the range, the greater the system error caused by deviations from the desired frequency.

To safeguard against such errors and to ensure a high degree of stability, a relatively wide frequency range was chosen in the new system.

For narrow-band transmission of the signals of the new system, by wire or wireless, it is feasible to narrow the frequency band by frequency division before direct transmission or modulation on a carrier, and to expand the frequency band after reception by frequency multiplication. In this way, the high quality of performance can be retained in spite of narrow-band transmission.
New Techniques in Glass-to-Metal Sealing*
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Summary—The new techniques in glass-to-metal sealing described in the paper include accurate and controlled oxidation of the metal, and the powder-glassing method of making seals. The accompanying experimental data refer to Kovar, since most of the laboratory work has been on glass-to-Kovar seals.

Data are presented for Kovar oxidized at a number of controlled temperatures and varying times. Excellent adherence of glass to Kovar is obtained with a weight gain of about 0.0003 to 0.0007 grams per square centimeter regardless of temperature of oxidation. Without preoxidation, any tendency for peeling or flaking shows up readily on cooling to room temperature. This condition is undesirable, since it indicates subsequent poor glass-to-metal adherence.

The powder-glassing method of making seals consists of grinding the glass, suspending the powdered glass in a suitable liquid, applying it to the prepared metal, and fusing to form a thin glass layer. The glass tube or bulb is subsequently joined to this layer as a glass-to-glass seal. Several examples of applications are given, one of them pertaining to multisection blanks employing butt seals.

Hypotheses on the function of H2 baking of Kovar, the adherence of glass to Kovar, and the nature of the oxidation process of Kovar are presented.

Prior to oxidation the Kovar is baked in a wet hydrogen atmosphere at 1100°C for 15 to 30 minutes, in order to eliminate possible bubbling at the glass-metal interface during sealing.

Experiments on oxidation were carried out in an electrically heated oven at controlled temperatures and varying times. Curves for weight gain per unit area versus time were thus obtained for a number of constant temperatures, as shown in Fig. 1. A range of values is indicated, since such variations occurred with changes in H2 baking, cleanliness of pieces, standing prior to oxidation, etc.

The excellent adherence of the glass to Kovar is obtained with a weight gain of about 0.0003 to 0.0007 grams per square centimeter regardless of temperature of oxidation, i.e., approximately 17 minutes at 800°C, 3 minutes at 900°C, 1 minute at 1000°C, or ¾ minute at 1100°C.

Fig. 1—Oxidation of Kovar. Time-rate curves are shown. Area inside V-shaped dotted curve indicates conditions under which greatest tendency for oxide flaking exists.

If the piece is underoxidized, the strength of the seal is poor but it is still vacuum tight. If it is overoxidized, the strength is good but the seal may be a leak because the glass is unable to penetrate the oxide layer completely, thus leaving a continuous porous path through which gases can seep into the tube.

INTRODUCTION

In making glass-to-metal seals the usual technique consists of cleaning the metal, oxidizing it the proper amount in order to develop a strong, vacuum-tight seal, and sealing the glass to the metal while it is still hot. Consequently, in seals made on the glass lathe, success is entirely dependent upon the skill and judgment of the operator. This is especially true on large and intricate seals. He must decide whether he is oxidizing sufficiently and, also, whether a firmly adhering oxide layer has been obtained.

The development of the powder-glassing method at the Research Department of the Westinghouse Lamp division enables the making of seals on a controlled basis. The new techniques in glass-to-metal sealing to be described include accurate and controlled oxidation of the metal, and the application of the glass in a powdered state that is fused to form a thin glass layer to which the glass tube or bulb is subsequently joined as a glass-to-glass seal.

OXIDATION OF METAL

Since most of the laboratory work has been on glass-to-Kovar seals, references to specific data will be on Kovar, an iron-nickel-cobalt alloy developed at Westinghouse.

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† Westinghouse Electric Corporation, Bloomfield, N. J.

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Prior to oxidation the Kovar is baked in a wet hydrogen atmosphere at 1100°C for 15 to 30 minutes, in order to eliminate possible bubbling at the glass-metal interface during sealing.

Experiments on oxidation were carried out in an electrically heated oven at controlled temperatures and varying times. Curves for weight gain per unit area versus time were thus obtained for a number of constant temperatures, as shown in Fig. 1. A range of values is indicated, since such variations occurred with changes in H2 baking, cleanliness of pieces, standing prior to oxidation, etc.

The excellent adherence of the glass to Kovar is obtained with a weight gain of about 0.0003 to 0.0007 grams per square centimeter regardless of temperature of oxidation, i.e., approximately 17 minutes at 800°C, 3 minutes at 900°C, 1 minute at 1000°C, or ¾ minute at 1100°C.

Fig. 1—Oxidation of Kovar. Time-rate curves are shown. Area inside V-shaped dotted curve indicates conditions under which greatest tendency for oxide flaking exists.

If the piece is underoxidized, the strength of the seal is poor but it is still vacuum tight. If it is overoxidized, the strength is good but the seal may be a leak because the glass is unable to penetrate the oxide layer completely, thus leaving a continuous porous path through which gases can seep into the tube.
With the preoxidation of Kovar any tendency for peeling or flaking shows up on cooling to room temperature. Statistical recording has shown that this tendency exists more strongly under certain conditions of temperature and time, as indicated in Fig. 1 by the area inside the V-shaped dotted line. Flaking is emphasized by improper or lack of H₂ baking, dirty Kovar, and other factors.

Pieces with flaking or peeling oxide layers should be eliminated immediately, since poor oxide adherence also results in poor glass adherence. Such a tendency may be missed with the usual glassing technique, wherein the glass is sealed to the oxidized metal while the latter is still hot.

**Powder-Glassing Method of Making Seals**

Grinding of glass, in any form, to pass through a 200-mesh sieve constitutes the first step in the preparation of the glass for use in the powder-glassing method of making seals. A porcelain-ball mill is used to avoid contamination by iron. The composition of the ground glass is the same as normally used for sealing to a given metal; for instance, Corning 7052 or 704 for Kovar.

The powdered glass is suspended in a suitable liquid such as water or alcohol. With alcohol, which has been used most extensively at Westinghouse, a few drops of LiNO₃ solution or NH₄OH keep the glass particles from settling out into a hard mass, thus enabling the suspension to be easily dispersed after standing. The best ratio of liquid to solid is determined by careful experimentation.

The powdered-glass suspension is then applied to the oxidized Kovar surface by spraying. The pressure of the spray is controlled by the viscosity of the suspension and the shape of the piece. Pressures ranging from 10 to 40 pounds have been employed.

If the powdered glass is to be applied by, dipping or slushing, the suspension is adjusted to the proper viscosity and mobility to obtain the necessary thickness of coating. In either case, the glass is restricted to the desired areas by proper masking prior to application, or by brushing afterwards.

The dried powdered-glass coating is then fused in an electrically heated oven. 7052 and 704 glasses produce a smooth coating by firing at 1000°C for 6 minutes. The powdered glass can also be fused by fires or by induction heating of the metal. Kovar-glass seals are fired in air, since the rate of oxidation of the Kovar is slow in relation to the rate of fusion of the glass. For seals with copper, however, if oxidation during fusion is undesirable, the firing would have to be carried out in a neutral atmosphere, since the rate of oxidation of the metal is faster than the rate of fusion of the glass. The fired pieces are removed from the heat and allowed to cool in air without any annealing. These powder-glassed parts are now ready for tube assembly and can be stored indefinitely.

The thickness of the fused-glass coating is not critical but has ranged mostly from 4 to 6 mils. The thinner coatings are generally preferred, since there is less tendency for pulling away from edges. Considerable amounts of bubbles, seen with low-power magnification, are present. However, these can be ignored, since no detrimental effects have been noticed because of their presence.

Afterwards, the sealing of the tube or bulb to the powder-glassed parts becomes simply a glass-to-glass seal. Nothing is gained in temperature, since just as much heat and "working" are necessary to make the glass-to-glass seal. The advantage lies in the fact that the seals are now protected and extended heating will not affect them, allowing the operator to work on the seals without any time limitations, which is very important in some cases.

**Hypotheses**

*Hydrogen Baking*

Wet-hydrogen baking, for instance, in the time allotted should remove any carbon in the surface of the Kovar at either 900 or 1100°C, but the temperature also controls the grain size of the Kovar, as shown in Fig. 2. Variations in time also alter the grain size, but not as effectively. The whole temperature range is used in baking but the large-grain-size structure is desirable, since the oxide, and the glass in turn, then have been found on an average to adhere more firmly to the metal surface.
Adherence

The adherence of glass to metal can be attributed to both ionic bonds and physical roughness of the metal. The ionic bond is the oxygen bond resulting in an affinity between the metal and glass, manifested as wetting of the former by the latter. Firing in air without any noticeable preoxidation is sufficient to cause this wetting action. Some adherence because of this wetting alone is evidenced by glassing untreated polished Kovar, but this adherence is weak.

The desirable function of oxidation is to roughen the metal surface by action on the grains, as well as along grain boundaries. The degree of roughness is related to the severity of oxidation, and hence the need for a minimum thickness of oxide to develop the adherence strength of the glass. The maximum thickness of this type of oxide is restricted by the ability of the molten glass to penetrate, but not necessarily dissolve completely, the oxide layer at sealing temperature, primarily because of vacuum-tightness considerations. Final adherence strength is thus realized because of the mechanical clinging of the glass or oxide to the roughened metal surface. A good finished seal, however, does not have nor does it need a continuous oxide layer at the interface.

The preference for large grain texture is due to the resulting decrease of grain boundaries. Oxide ridges are formed at boundaries because the volume of oxide is greater than the volume of a corresponding amount of metal, and more metal surface is available there for oxidation. These ridges are not as completely penetrated by the glass as the oxide on the grain surface, with a subsequent loss of some strength, since the glass develops its chief mechanical adherence by direct contact with the roughened metal surface.

Oxidations

Photomicrographs of cross sections of two Kovar-to-glass seals are shown in Fig. 3, in which the Kovar had been preoxidized at 1000°C for 1 minute to produce the normal amount of oxidation, and also for 10 minutes.

An observation of considerable interest is the presence of a new metallic layer in the surface of the Kovar, with an average thickness of about 10 microns in the normal seal. X-ray studies of the layer indicate the same structure as that for the alloy Kovar but with a condensed crystal lattice because of less iron. In turn, X-ray examinations and chemical analyses of the oxide layer indicate that it is primarily FeO. Therefore, in the oxidation of Kovar, iron diffuses preferentially, forming an oxide layer composed primarily of iron oxide and a new alloy layer at the surface consisting mostly of nickel and cobalt.

Applications

The use of the powder-glassing techniques can be referred to several specific examples. Part of the liquid air trap in the mass spectrometer consists of a special Kovar cylinder brazed to a heavy copper tube. Glass-to-metal seals are required on each end of the part. Prior to the use of the new methods, usual scaling techniques resulted in a shrinkage of about 40 per cent. The powdered-glass method allowed the making of successful seals with no shrinkage. Fig. 4 shows the powderglassed portions of the cylinder to which subsequent seals were made.

Similar experiences prevailed in the making of multisection blanks employing butt seals. Such butt seals were normally found impossible to make on a glass lathe, since the opposite side of a Kovar ring was oxidizing while the glass blower was making a seal. By first powder-glassing the rings on both sides this difficulty was eliminated, since the glass coating protected the seal interface during subsequent heat applications. Consequently, good multisection butt seals with controlled oxidation resulted, and such blanks became pos-
Contributors to Waves and Electrons Section

Sidney Bertram (A'36–SM'47) was born at Winnipeg, Canada, on July 7, 1913. He attended the Los Angeles City College from 1930 to 1933. From 1934 to 1936 he was an instructor at the Radio Institute of California, leaving to enter the California Institute of Technology where he received the B.S. degree in engineering in 1938. Later Mr. Bertram was employed as a research engineer by the International Geophysics Company. In 1939 he entered the Ohio State University, receiving the Master's degree in electrical engineering in 1941. From 1941 to 1942 he was engaged in war research under the O.S.U. Research Foundation. In 1942 he joined the staff of the University of California, Division of War Research, where he was engaged in the development of underwater-sound-ranging equipment. In 1945 Mr. Bertram joined the staff of the Physical Research Unit of the Boeing Aircraft Company and in 1946 he returned to the Ohio State University as an assistant professor in electrical engineering. He is a member of Sigma Xi, Tau Beta Pi, and Eta Kappa Nu.

J. H. Dellinger (F'23) was born on July 3, 1886, at Cleveland, Ohio. He attended Western Reserve University from 1903 to 1907, received the A.B. degree from George Washington University in 1908, the Ph.D. degree from Princeton University in 1913, and the D.Sc. degree from George Washington University in 1932.

Dr. Dellinger has been on the staff of the National Bureau of Standards as physicist since 1907, and from 1928 to 1929 was chief engineer of the Federal Radio Commission, on loan from the Bureau. He has been a representative of the United States Government at numerous international radio conferences since 1921, and of the Department of Commerce on the Interdepartment Radio Advisory Committee since 1922.

Dr. Dellinger was vice-president of The Institute of Radio Engineers in 1924, and president in 1925. He has been vice-president of the International Scientific Radio Union since 1934, and chairman of the Radio Technical Commission for Aeronautics since 1941.
Contributors to Waves and Electrons Section

Horatio Wellington Lamson (A'15-M'27-F'33) was born on January 2, 1893, at Somerville, Mass. He received the S.B. degree in physics in 1915 from Massachusetts Institute of Technology, and the A.M. degree in physics in 1917 from Harvard University.

Mr. Lamson was a member of the United States Naval Reserve Force during World War I and assistant to G. W. Pierce in the development of antisubmarine devices. Subsequently he became a physicist in the United States Navy Department. Since 1921 he has been a research engineer with the General Radio Company.

Mr. Lamson is a Fellow of the Acoustical Society of America and a member of the American Institute of Electrical Engineers.

Newbern Smith

Newbern Smith (A'41-SM'46) was born on January 21, 1909, at Philadelphia, Pa. He was graduated from the University of Pennsylvania, Moore School of Electrical Engineering, with the degrees of B.S. in 1930 and M.S. in 1931, in electrical engineering; and of Ph.D. in physics in 1935.

Since 1935 Dr. Smith has been a physicist at the National Bureau of Standards. During the war he was Assistant Chief of the Interservice Radio Propagation Laboratory which was set up by the U. S. Joint Chiefs of Staff to meet Army-Navy needs for radio propagation information. He has participated in several international radio propagation conferences.

R. F. Wild (A'37) was born in New York, N. Y., on August 27, 1910. He received the M.S. degree in communications engineering from the Berlin Institute of Technology in 1935, and then joined the research group of Farnsworth Television, Inc., at Philadelphia, Pa. He remained there until 1939 when the company was reorganized under the name of Farnsworth Television and Radio Corporation and moved to Fort Wayne, Ind. He was connected with the new organization in the capacity of research consultant and patent engineer until the end of 1941, and then joined the patent department of Zenith Radio Corporation, Chicago.

Since the latter part of 1942, Mr. Wild has been senior electronic research engineer for the Brown Instrument Company of Philadelphia. In this capacity he has supervised the design and development of special electronic equipment to be used with precision measuring instruments. He is now employed in the applied physics section of the experimental station, E. I. DePont de Nemours and Company, Inc., Wilmington, Del.
Acoustics and Audio Frequencies

Aerials and Transmission Lines

Circuits and Circuit Elements

General Physics

Geophysical and Extraterrestrial Phenomena

Location and Aids to Navigation

Materials and Subsidiary Techniques

Mathematics

Measurements and Test Gear

Other Applications of Radio and Electronics

Propagation of Waves

Reception

Stations and Communication Systems

Subsidiary Apparatus

Television and Phototelegraphy

Transmission

Vacuum Tubes and Thermonuclear

Miscellaneous

534.214:534.844


534.219

Abstraction of Supersonic Waves in Liquids—S. B. Gurevich. (Compt. Rend. Acad. Sci. (U.R.S.S.), vol. 40, no. 1, pp. 17–20; 1947.) In Russian. Formulas derived by Stokes (1) and Mandelstam and Levontovich (2) are discussed and a more general formula (7) is proposed.

534.219.0:546.212

A Pulse Method for the Measurement of Ultrasonic Absorption in Liquids: Results for Water—J. M. M. Pinkston. (Nature (London), vol. 160, pp. 129–139; July 26, 1947.) Measurements were made at frequencies between 7.37 and 66.1 Mc, using a quartz crystal as a transducer. The pulse recurrence frequency was 250 c.p.s. and the pulse length variable from 2 to 40 microseconds. The values obtained for the amplitude absorption coefficient are higher than those given by the theory of Stokes.

534.219.0:621.317.757

Electronic Indicator for Low Audio Frequencies—A. E. Hastings. (Proc. I.R.E., vol. 35, pp. 821–827; August, 1947.) For analysing a periodic complex wave form. The components within the frequency band 1 c.p.s. to 1 kc are displayed on four parallel linear scales traced on a c.r.t. Only a rough measurement of the amplitudes of the frequency components was desired, but the frequency scales can be set up, without frequency calibration and within an accuracy of 3 per cent from design equations developed in this paper. The performance and limitations of the instrument are described.

534.62

A New Sound-Absorbing Device of High Efficiency and the Construction of a Sound-Damped Room—E. Meyer, G. Buchmann, and A. Schoch. (Akus. Zeit., vol. 5, pp. 352–364; December, 1940.) Measurements of the absorption by conical shapes of various shapes led to the use of cones of 1 meter overall length for the lining of a sound-absorbing chamber. The cones were constructed by hand from slagg wool, with a bitumen binder, and had a parallel section 15 centimeters long, the mouth being 15 centimeters. About 23,000 of these cones were used, fixed to the walls and roof by hooks and pins, and with points inwards, giving a clear space of 6 centimeters by 7 meters. Results of tests carried out in the completed room are shown graphically and discussed.

534.756

Investigations on the Theory of Hearing—H. Jürgen. (Akus. Zeit., vol. 5, pp. 268–283; September, 1940.) Mathematical treatment of the propagation of sound in an elastic tube filled with a viscous incompressible fluid is used to draw conclusions as to the hydrodynamic processes which take place in the ear. The results are in agreement with the phenomena occurring in an electrical network analogous to the elastic tube and are compatible with the resonance theory of hearing.

534.756.1

Transient Reception and the Degree of Resonance of the Human Ear—R. J. Pumphrey and T. Gold. (Nature (London), vol. 160, pp. 124–125; July 26, 1947.) Experiments have been conducted which support the Helmholtz theory of pitch discrimination based on high-Q resonators of the ear. Q values of 200 to 350 at 10 kc falling to about 50 at 1 kc were obtained.

534.851:621.395.66

Experimental Volume Expander and Scratch Suppressor—McProud. (Skef 46.)

534.86:534.322.1

Frequency Range Preference for Speech and Music—J. E. Olson. (Electronics, vol. 20, pp. 80–81; August, 1947.) Tests with live performers heard through a removable acoustic low-pass filter cutting off at 5 kc, showed that 69 per cent of the listeners preferred the full acoustic range in contrast to accepted results on reproduced programs. Reasons are suggested. See also 3007 of 1947 (Webster and McPeak) and 3765 of January.

534.86:534.322.1

Psycho-Acoustical Aspects of Listener Preference Tests—C. J. LeBel. (Audio Eng., vol. 31, pp. 9–12, 48; August 1, 1947.) A detailed and critical analysis of various attempts to discover whether listeners prefer reproduction systems to have a full or a restricted a.f. range. The economic aspects of possible improvements in the quality of reproduction are also considered. See also 3765 of January (Olsen) and 10 above.

534.861.1/2

Microphone Placement for Studio Liveness—(Tele-Tech, vol. 6, pp. 44–45, 103; July, 1947.)

621.395.623.7

Loudspeaker Damping—F. Langford-Smith, G. N. Patchett, P. J. Walker, C. J. Mitchell, and E. J. James. (Wireless World, vol. 53, pp. 309 and 343–344; August and September, 1947.) The electromagnetic damping of a loudspeaker is limited by the equivalent series impedance of the loudspeaker itself, but at resonant points, the efficiency considerably exceeds its mean value, and the equivalent impedance is thus reduced.

621.395.623.8

The Distribution of Acoustic Power—L. Chretien. (T.S.F. Pour Tous, vol. 23, pp. 158–160 and 180–182; July, August, and September, 1947.) Practical circuits for feeding a number of similar or different loudspeakers. See also 3317 and 3770 of January.

621.395.623.8


621.395.625.2


621.395.625.2

1: Comparison of disk recording with alternative systems, and discussion of standardization of disk and groove dimensions, cutting, and turntable speeds, the magnitudes of stylus amplitudes, velocities, and accelerations, the use of radius compensation, and the choice of the theoretically highest fidelity.

2: Discussion of turntable drive, design and mounting of the cutting head, methods of making cue marks and of removing swarf while recording.

Section 3: Description of a high-fidelity disk-recording equipment developed for the B.B.C., and of its performance.

621.392.029.64 Two Coaxial Dielectrics—S. A. Frankel. (Tele-Teach, vol. 6, pp. 56–57; September, 1947.) Discussion of German war-time development of magnetic tape recording, and American post-war improvements.

621.396.67 Automatic Gain Control and Limiting Amplifier—Jurek and Guenther. (See 69.)

AERIALS AND TRANSMISSION LINES

621.392.029.64 TMz Mode in Circular Wave Guides with Two Coaxial Dielectrics—S. Frankel. (Jour. Appl. Phys., vol. 18, pp. 650–653; July, 1947.) "Field components for a transversive magnetic wave in a wave guide with two coaxial dielectrics are computed. A typical example is given to show the calculation of guide dimensions to reduce phase velocity to a preassigned value."

621.392.029.64 Properties of Ridge Wave Guide—S. B. Cohn. (Proc. I.R.E., vol. 35, pp. 783–788; August, 1947.) The calculation, experimentally, giving cutoff frequency and impedance are presented for rectangular wave-guides having a rectangular ridge projecting inward from one or both wide sides. The guide has a lower cutoff frequency and impedance and greater higher-mode separation than a plain rectangular waveguide of the same width and height. A number of applications are suggested.

621.396.67 Effect of Feed on Pattern of Wire Antennas

—D. C. Cleekner. (Electronics, vol. 20, pp. 103–105; August, 1947.) Measured polar diagrams for cuts through wires of lengths between one-half, 3, and 3A are given, showing how the feed point affects the number, orientation, and magnitude of the lobes.

621.396.67 A Tentative Investigation of a Complex System of Tower Radiators for Radio Broadcast Stations—H. M. Rushchuk, and M. M. Pruzhanski. (Radioisotopika (Moscow), vol. 2, pp. 22–33; July and August, 1947. In Russian.) In designing a radiating system having four self-supporting towers at the corners of a square, and intended for both directional and non-directional broadcasting, experiments were conducted with a model using brass lattice towers 250 centimeters high, erected on a ground system of galvanized iron sheets. The radiators were fed through single conductor feeders from two u.s.w. oscillators covering a wavelength range from 3 to 9 meters. Measurements were made of the input impedance of the radiators, of the phase velocity of e.m.w. waves along them, and of the directivity coefficient of the system for various operating conditions. Experimental curves so obtained are shown and the conclusions reached regarding the operation of the proposed system are enumerated.

621.396.67 Fourier Equations in Aerial Theory: Part 3—Operations with Fourier Transformers—Ramsay. (See 155.)

621.396.67:621.396.621 In a Big Aerial Whirl While?—M. G. Scroggie. (Wireless World, vol. 53, pp. 314–318; September 1947.) Discussion showing the many advantages of good outdoor aerials.


621.396.67:621.397.5 Performance Characteristics of the WABD TV Antenna System—G. E. Hamilton. (Communications, vol. 27, pp. 16–18, 43; July, 1947.) The advantages of the 3-bay superturbulent batwing aerial system are discussed. The performance specifications are listed and compared with actual results. An earlier article on the installation and testing of this system was noted in 3432 of 1947 (Denke).


621.396.67:621.397.9 Microwave Antenna Beam Evaluator—II. LeCaine and M. Katchky. (Electronics, vol. 20, pp. 116–120; August, 1947.) Apparatus for automatic tracing of polar diagrams of microwave aerials to an accuracy within 1 per cent. Square law detectors are used at the transmitter, whose aerial is rotated, and at the receiver. A self-balancing system using motor-driven ganged potentiometers gives the traced diagram a linear scale and eliminates errors due to varying transmitting power and eventual interference.

621.396.67:621.397.9 Calculation of the Current for Frame Receiving Aerials—J. Müller-Strobol and J. Patry. (Schweiz. Arch. Angew. Wiss. Tech., vol. 13, pp. 193–202; July, 1947.) An approximate solution for currents in frame aerials of N turns is based on the theory of Hallen, assuming that the wire radius is small compared with the coil radius and that the coil radius is small compared with the wavelength of the incoming radio waves.

621.396.67:621.397.9 Note on Circular Loop Antennas with Non-Uniform Current Distribution—G. Glenn. (Jour. Appl. Phys., vol. 18, pp. 638–644; July, 1947.) The radiation patterns, power gain, and radiation resistance are calculated for a closed loop of radius \(\frac{2\pi}{m}\) with a hyperbolic current distribution. The effective attenuation constant of the equivalent transmission line is deduced from the radiated power. The theory agrees closely with experiment.


CIRCUITS AND CIRCUIT ELEMENTS

518.5 Electronic Computing Circuits of the ENIAC—Burs. (See 158.)

518.5:612.318 Use of Magnetic Amplifiers in Computing Circuits—Beyer. (See 159.)


621.396.72:1:621.385.39 Shunt Tube Control for Thyatron Rectifiers—J. A. Potter. (Bell Lab. Rec., vol. 25, pp. 273–276; July, 1947.) The inherent delay in thyatron rectifiers using fixed-value, steep-fronted voltage variations by changes of grid bias is overcome by connecting the anode circuit of a tube across the load. The grid bias of this tube is controlled by a regulating circuit so that small current changes pass through the tube without flowing through the thyatron, which reacts only to the average load.

621.396.8:621.317.33 Method for Determining the Time-Constant of Resistors at Low Frequency—Ney. (See 166.)


621.319.4 Significance of Watt-Second Ratings of D.C. Capacitors—J. D. Stacy. (Communications, vol. 27, pp. 24–25; August, 1947.) When the life and the high-temperature performance of capacitors are to be considered, watt-second rating gives a better criterion than voltage and capacitance rating.


621.392.518.5 Machine Computing of Networks—Dunstan. (See 160.)

621.392.1 Transforms—Obvious and Otherwise—"Cathode Ray." (Wireless World, vol. 53, pp. 388–390; October, 1947.) An elementary explanation of the way in which various tuned
and untuned coupling networks do, in fact, act as transformers, as was stated in the article abstracted in 2919 of 1947 (Moxon).

621.305:66:534:851

Experimental Volume Expander and Speech Amplifier—C. G. McProud. (Radio Eng., vol. 31, pp. 13-15; Aug., 1947.) A number of familiar circuits are combined into one unit. Block and circuit diagrams are given and component values stated. The unit is preceded by a 2-stage preamplifier.

621.306:611:3

Variation of an RC Parallel-T Null Network—H. S. McQuaugh. (Tele-Tech, vol. 6, pp. 48-51; Aug., 1947.) *When used in the negative feedback loop of an amplifier, this network produces either a frequency-selective amplifier or an oscillator, depending on the choice of circuit parameters. An unsymmetrical null network is shown which provides greater activity than is possible with the conventional network under the same conditions of amplification.* See also 1464 of 1946 (Hastings).

621.306:611:4:518:4

Charts for Resonant Frequencies of Cavities—A. R. Bracewell. (Proc. I.R.E., vol. 35, pp. 830-841; Aug., 1947.) Six abaxes are given which may be used for designing cylindrical resonant cavities whose cross sections are circles, concentric circles, squares, or rectangles. The equations involved, the method of use, and the special advantages of each abace are described, together with the method of construction. The effects of small deformations or of wavelength changes are considered.

621.306:615

RC Oscillator Control—B. J. Solley. (Wireless World, vol. 53, pp. 321-322; Sept., 1947.) A network is described, by which the frequency of a RC oscillator may be adjusted over a wide range, using a single potentiometer control. A frequency range of 4 to 1 may be obtained with only 1 db variation in amplitude, and a range of 25 to 1 if greater amplitude variation is permissible.

621.306:615:029:3


621.306:615:029:5:63

Wide Range Sweeping Oscillator—Engineering Staff, Kay Electric Co. (Electronics, vol. 20, pp. 112-115; Aug., 1947.) A 50-kc. to 500-Mc. beat-frequency oscillator with sawtooth frequency modulation variable up to 40 Mc. Two 3-centimeter klystron oscillators are used, one being varied in frequency by a panel control of cavity resonator shape and modulated in frequency by variation of the repeller (electrostatic potential). The two klystron frequencies are measured by a precision absorption wavemeter, the difference giving the beat frequency.

621.306:615:14

U.S. Oscillators—E. P. Korchugina (Radiotehnika (Moscow), vol. 2, pp. 34-43; Jul., and Aug., 1947.) In Russian. The effects of interelectrode capacitances and of the inductance of the leads on the operation of the oscillators are investigated theoretically. Suitable calculating circuits are discussed and design methods indicated.

621.306:615:14

High Power U.S.W. Valve Oscillators—A. M. Kugushev and D. I. Karpovski. (Radio-tehnika (Moscow), vol. 2, pp. 48-54; July and August, 1947. In Russian.) The use of transmission lines with distributed constants as tuning elements for high-power demountable tubes is considered and experiments are described with such tubes operating on wavelengths from 2 to 3.5 meters and with outputs from 8 to 50 kw.


Ultra High Frequency Modulation on Wave-Guides—H. Gutton and J. A. Orutsi. (Jour. Brit. I. R. E., vol. 7, pp. 205-210; October, 1947. Discussion, pp. 210-211.) A description of a method of modulating a master klystron oscillator combined with a v.m. amplifier tube. The energy produced is fed to the radiator by a waveguide across which is connected a magnetron working in a cutoff condition and such that variations of anode voltage vary its impedance. By means of a transformer between the klystron and the guide, the impedance across the guide can be made to vary from zero to infinity, thus enabling 100 per cent modulation to be obtained.

Application to a 100-kw television transmitter for a wavelength of 21.5 centimeters and up to 20 Mc. modulation frequency is described briefly.

For a fuller account see Onde Elettr., vol. 27, pp. 307-312; August and September, 1947.

621.306:615:18

Cathode-Coupled Half-Slot Multivibrator—R. K. F. Scal. (Electronics, vol. 20, pp. 150, 158; September, 1947.) Describes a double-triode common-cathode RC trigger circuit with two stable states operated alternately by successive negative pulses applied across the cathode-bias resistor; the output from either anode, therefore, occurs at half the repetition frequency of the initiating pulses, and is square-wave in form. Successive frequency division can be obtained by connecting units in tandem with differentiating RC coupling circuits.

621.306:619:23+621.306:645

A 120-Watt Modulator and Speech Amplifier—C. A. Chambers. (QST, vol. 31, pp. 13-18; August, 1947.) A compact 3-stage amplifier-modulator, using Type 807 tubes in class AB2 and having overall feedback. Full circuit and construction details are given.

621.306:621+621.306:59

British Printed and Sprayed Circuits—(See 238.)

621.306:621


621.306:622:71

Ratio Detector for F.M. Signals—(See 248.)

621.306:645

Amplifier with Variable Bandwidth—F. Juster. (Toute a Radio, vol. 14, pp. 258-260; September, 1947.) A design giving (a) very large bandwidth with low sensitivity, (b) medium bandwidth with medium sensitivity, or (c) small bandwidth with high sensitivity. The changes are effected by varying the anode resistance of each tube.

621.306:645

Harmonic-Amplifier Design—H. Brown. (Proc. I.R.E., vol. 35, pp. 771-777; August, 1947.) Two methods are presented for calculating the ideal performance of harmonic-amplifier stages as used in frequency multiplication. The first gives approximate results while the second, a graphical method, is exact. Performance may be adversely affected by degenerative effects introduced by the grid-anoode capacitance and by inductance in the cathode circuit common to both grid and anode circuits. Circuit arrangements for overcoming these degenerative effects are discussed theoretically and applications are indicated.

621.306:645:518:3


621.306:645:518:4

Gain Chart for Cathode Followers—G. Houck. (Tele-Tech, vol. 6, pp. 54-55; August, 1947.)

621.306:645:621.317:755


621.306:645:621.317:755


621.306:645:621.317:755

Multi-Purpose Audio Amplifier—M. P. Johnson. (Audio Eng., vol. 31, pp. 20-23, 39; August 1, 1947.) "Combines high gain, unusually high fidelity, and an expander-compressor circuit. It can be easily built from readily obtainable components. Full circuit and constructional details are given.

621.306:645:029:3

Level-Governing Audio Amplifier—(Tele-Tech, vol. 6, pp. 67-69, 96; August, 1947.) Design of a program-operated amplifier which will automatically minimize overmodulation of the radio transmitter. A control circuit reduces amplifier gain when the input exceeds a predetermined value. See also 1189 of 1942 (Black and Norman).


Automatic Gain Control and Limiting Amplifier—W. M. Jurek and J. H. Guenther. (Electronics, vol. 20, pp. 94-97; September, 1947.) Describes in detail a full-wave audio program amplifier, installed between the studio audio apparatus and the transmitter, for maintaining a high peak modulation depth without danger of over-
loading and with minimum reduction of dy-
namic range. For another account see Com-
munications, vol. 27, pp. 18, 37; August, 1947.

2.94

namic range. For another account see Com-
munications, vol. 27, pp. 18, 37; August, 1947.

2.94

namic range. For another account see Com-
munications, vol. 27, pp. 18, 37; August, 1947.

2.94

namic range. For another account see Com-
munications, vol. 27, pp. 18, 37; August, 1947.

2.94

namic range. For another account see Com-
munications, vol. 27, pp. 18, 37; August, 1947.
Abstracts and References

523.53: 551.510.535 92

523.53: 551.510.535 93
Meteorites, Comets, and Meteoric Ionization—A. C. B. Lovell. (Nature (London), vol. 160, pp. 76-78; July 19, 1947.) Notes on a conference held at Manchester University under the auspices of the Physical Society. See also 92 above.

523.7 94
The Sun a Regular Variable Star—C. G. Abbot. (Science, vol. 105, p. 632; June 20, 1947.) Summary of National Academy of Sciences' paper. The solar constant of radiation for the years 1924 to 1944 has a regular periodicity of 6.6456 days. Statistical studies show fluctuations of temperature of identical average period and average range 5°F.

523.72: 523.854: 621.396.822 95
Emission of Radio-Waves by the Galaxy and the Sun—J. S. H. Shklovsky. (Nature (London), vol. 159, pp. 752-753; May 31, 1947.) Henney's and Keenan's theory of long-wave radio emission (Astrophys. Jour., vol. 91, pp. 625 ff.; 1940) is extended to take account of the absorption due to free electrons. In order to correlate the theory with observations on the emission from the sun, it is necessary to assume that the electron temperature of the outer corona is about 3500°.

The occasional intense solar emission in the range 7 to 30 meters may be due to excitation of the cold earth corona in the flow of charged corpuscles through the corona with a velocity greater than that of sound. This would give a magnetic storm about one day after the anomalous radio emission.

523.72: 621.396.822: 020.62 96
Relation between the Intensity of Solar Radiation on 175 Mc/s and 80 Mc/s—M. Kyle and D. D. Vonberg. (Nature (London), vol. 160, pp. 157-159; August 2, 1947.) Simultaneous observations at the two frequencies were made simultaneously, May 18, 1947, by the technique described in 89 of 1947. Short-lived bursts having an intensity up to five times the mean value and lasting from 1 to 20 seconds occur with frequencies but at irregular times; bursts having intensities 20 to 100 times the mean value can persist for many minutes and are usually observed on both frequencies. The day-to-day variation of intensity on the two frequencies is also investigated. See also 3508 of 1947 (Appleton and Hey).

523.74 97
A Short-Lived Solar Phenomenon in High Latitude—A. D. Thackray. (Nature (London), vol. 160, pp. 439-440; September 27, 1947.) An intensely dark absorption flocculus was observed in the region with heliographic coordinates 6°W, 61°S from 09h 46.00 GMT onwards on June 15, 1947. It appears to be similar to the dark flocculi in regions surrounding sunspots and flares, and there is evidence that it was associated with increased radio noise on 175 Mc.

523.74: 98
Influence of Solar Activity by Radio—J. F. H. S. (Nature (London), vol. 160, p. 293; August 30, 1947.) The daily sunspot (relative) numbers given by the Swiss Federal Observatory, Zurich are broadcast monthly in the short-wave service of the Swiss Broadcasting Corporation. Dates, times, wavelengths, and languages of the transmissions are detailed.

523.74: 551.515.535 99
On the Forecasting of Sunspots—M. Mayou. (Compt. Rend. Acad. Sci. (Paris), vol. 224, pp. 1699-1701; June 16, 1947.) A method making use of 1884 to 1946 data to derive formulas giving the probable Wolf-Wolfer numbers for each month for one and two years in advance. The numbers for 1948 approximate to those of Gleissberg (1830 of 1946 and back references) and of Waldmeier (2560 of 1946).

523.854: 551.812: 537.591 100

So long as the condition of weak magnetic coupling among the stars of a galaxy still obtains, stellar dipole moments are still oriented at random and the resultant field of the galaxy almost vanishes.

537.591 101

538.712 103

551.308 104

551.510.535 105
On the F3 Layer in the Ionosphere—Ya. L. A'pert. (Compt. Rend. Acad. Sci. (U.S.R.S.S.), vol. 55, no. 1, pp. 25-26; 1947. In Russian.) As a result of recent ionosphere investigations, it is suggested that the three- and four-tailed characteristics of ionosphere reflection records (Figs. 1 and 2) are due to double refraction of the ray taking place in the main and F3 layer in semitransparent sporadic ionized clouds appearing in this layer.

551.510.535: 525.624 106
Atmospheric Tides in the Ionosphere: Part 2—Lunar Tidal Variations in the F Region near the Magnetic Equator—D. F. Martyn. (Proc. Roy. Soc. A., vol. 199, pp. 273-288; July 8, 1947.) Examination of the data for the heights and critical frequencies of the F regions over three years at Huancayo, Peru, shows the existence of certain tides in all latitudes except 67°S. The lunar variation in the F3 region depends on solar time in both phase and amplitude and at certain epochs attain very large amplitudes, up to 60 kilometers for 27 per cent of f<sub>0</sub>.

The theory of these variations given in part I of this paper (2421 of 1947) is extended.

551.530.515: 621.396.11 107
The Ionosphere—J. H. Dellinger. (Sci. Mon., vol. 65, pp. 115-126; August, 1947.) A general survey of ionosphere characteristics such as layer height, ionization density, energy absorption, and radio noise, and their significance. World-wide observations have extended knowledge of these phenomena, thus allowing reliable predictions to be made of radio propagation conditions.

551.510.535: 621.396.11 108
A Frequency Prediction Service for Southern Africa—Hewitt, Hewitt, and Wadding. (See 292.)

551.524.4 109
The Daily Course of Temperature in the Troposphere—E. S. Seleznjova. (Bull. Acad. Sci. (U.R.S.S.), str. geogr. geophys., vol. 9, no. 2, pp. 82-88; 1945. In Russian with English summary.) The daily oscillations of temperature in the lower layers of the troposphere appear to be influenced by the earth's surface, and not of the report of the 1947 International Meeting on Marine Radio Aids to Navigation. Performance standards are laid down for radio equipment and radar for position-finding within ranges of reliable fixed targets, either natural or artificial. Compulsory fitting of radar and frequency standardization is not yet contemplated. Development of a new standard long-range radar, and its possible implications for other types of devices for better identification of shore features and small ships is recommended. Medium-frequency d.f. services, though not fully satisfying standard requirements, should be continued. Deco services should be expanded, and for long range, standard lorans should be adopted. Medium-range aids should have priority over long-range, but marine requirements should be considered when setting up long-range aircraft aids. For short-range communication, 2-way 150-Mc./sec. intercommunication is recommended. Main components of equipment should be standardized.

621.396.933 111
International Recommendations for Marine Electronic Aids—E. Electronics in the Antartic—Bailey. (See 258.)

621.396.932 112
International Recommendations for Marine Electronic Aids—E. Electronics in the Antartic—Bailey. (See 258.)

621.396.933 111

621.396.932: 621.396.96 113

621.396.933: 621.396.96 114
Radar System for Airport Traffic and Navigation Control: Part 1—F. J. Kilty. (TeleTech, vol. 6, pp. 40-44; 104; August, 1947.) Description of a fixed ground radar system, based on a long-wave Navy G.C.A., for airport surveillance, height finding, traffic control, and instrument approach under all conditions of visibility. The height-finder, azimuth, and eleva-
tion systems operate at frequencies near 9000 Mc., and the search system at 2900 Mc. Two-way communication with aircraft is provided in the 2 to 9 Mc. and 100 to 156 Mc. bands.

621.396:323:621.396.96 115
Airborne Radar—(S.A.E. J., vol. 55, pp. 27–31; August, 1947.) Based on a paper entitled "American Airlines’ Evaluation of Airborne Radar," I read before the S.A.E. Mid-Continent Section. The APS-10 radar, with the aerial modified to give a pencil beam, provides a simple and effective method of collision prevention under blinding conditions. A number of photographs are given of actual PPI displays obtained during flight tests.

621.396:96:621.318:572 116

621.396:96:621.396.619:23:778 117
Photographing Pulse Wave Shapes of Radar Modulators—Markus. (See 288.)

621.396.96 118

MATERIALS AND SUBSIDIARY TECHNIQUES

533.5:621.3.021.53 119
The Effect of Heat Treatment in Different Atmospheres on the Stress in Tungsten-to-Glass Seals—A. F. Dearing. (Jour. Soc. of Photo-Techn., vol. 30, pp. 217–238; August to October, 1946.) A study of the relations between the heating time and temperature, in air or in hydrogen, and the longitudinal stress at the glass-metal boundary of single-wire "oxide" or "oxide-free" seals.

533.5:621.3.021.53 120
Metal-Ceramic Vacuum Seals—N. T. Williams. (Rev. Sci. Instr., vol. 18, pp. 394–397; June, 1947.) A complete account of processes using ALSMat (32460 of 1947). Mixtures of Mo and carbonyl-iron powders are fired on to the ceramic at 1400°C in a H-N atmosphere and to the surface thus obtained a Ni powder is sintered on for brazing. An alloy consisting of 50 per cent Fe, 50 per cent Ni is used for outside seals and an alloy of 42 per cent Ni, 50 per cent Cr, 2 per cent Fe for inside seals.

533.5:621.3.021.53 121
Ceramic-Metal Seals—M. Kuhner. (Le Vide (Paris), 11 pp., January, 1947; Reprint.) Discusses the advantages of using ceramics instead of glass in the construction of u.h.f. tubes and describes processes for direct ceramic-metal seals without a glass intermediate.

533.5:621.315.016 122

533.7:621.386 123
546.289: 621.315.59: 536.48
140 Theory of Low Temperature Semiconduct-
istor Resistivity—V. A. Johnson and K. Lark-
orovitz. (Phys. Rev., vol. 72, p. 531; Septem-
ber 15, 1947.)

546.841: 621.385.203.216
141 Thermionic Properties of Thoria—D. A.
White. (Nature (London), vol. 160, pp. 129-
130; July 4, 1947.) A coating of thorium 0.1
mm. thick was sprayed on to a Ta strip and
incorporated in a diode. A saturated emission
of 2.5 A per centimeter² was obtained under
d.c. conditions at 1900°K. 10 A per centimeter²
under d.c. conditions and 30 A per centimeter²
under pulsed conditions were obtained at 2100°K
without flashover. A thorium cathode was also
made in tubular form by extrusion and sinter-
ing. The emission fell rapidly on continued
operation and the cathode was sensitive to ther-
mal shock.

549.514.51: 548.24
142 Artificial Electrical Twinning in Quartz
Cryystals—T. M. S. Kettle. (J. Inst. Elec. En-
gineers, vol. 35, pp. 789–790; August, 1947.) For another
account see 1463 of 1947.

549.514.51: 621.306.611.21
143 FT-241 Frequency Control (Quartz Cryst-
als) by Transistor.—I. E. Fair. (Bell. Lab. Res., vol. 25,
p. 293–298; August, 1947.) Construction of a
unit for 200 to 1040 kc. using CT- or DT-cut
quartz plates, which are much smaller than A.
T. quartz plates for a given frequency. Vibration
in face shear and not thickness shear is used and
a technique is developed for mounting the plates
on small wires soldered at the nodal points.

549.514.51: 621.306.611.21: 621.386.001.18
144 A Method for the Determination of Crystal
Cut by Applying the Reflection of X-Rays from
a Known Lattice Plane—V. Pettrilka and J.
Benčík. (Phil. Mag., vol. 37, pp. 399–410;
June, 1946.) The method uses a Seemann elec-
tron diffraction spectrometer. The required in-
formation is derived from measurements on
a single photograph.

621.315.62: 621.537.32
145 High Altitude Flashover and Corona Cor-
September, 1947.) "The design principles that
were followed in order to ensure that the integra-
tion of the electronic computer is presented,
and the basic types of computing circuits are
analyzed. . . . The Eniac performs the opera-
tions of addition, subtraction, multiplication,
division, square-rooting, and the looking up of
function values automatically. The units which
perform these operations, the units which take
numerical data into and out of the machine,
and those which control the overall operation
are described. The technique of combining the
electronic circuits to perform these func-
tions is illustrated by three typical computing
circuits: the addition circuit, a programming
circuit, and the multiplication circuit." See also
2481 of 1947 (Wilkes) and 3952 of January
(Iartree).

510.05
153 The Quarterly Journal of Mechanics
and Applied Mathematics—(Nature) (London),
vol. 160, p. 427; September 27, 1947.) A new peri-
odical beginning publication in April, 1948.

517.512.2: 518.8
154 Graphical Methods for Evaluating Fourier
Integrals—W. J. Cunningham. (J. Appl.
methods are described, all involving an analysis of
the function considered into the sum of sim-
pierical functions whose transforms have been
obtained. The method for the analytic solu-
tion is too complicated or the data take the
form of curves of obtained experimentally.

517.512.2: 621.306.67
155 Fourier Transforms in Aerial Theory: Part
3—Operations with Fourier Transforms—J. F.
Ramsay. (Joum. IRE, vol. 35, p. 41–58;
April to June, 1947.) Continuation of 3561 of
1947. Discussion of elementary operations with
Fourier transforms, namely: (a) change of sign of
the independent variable, (b) interchange of
function, (c) identity of function; self-reciprocal
transforms, (d) the Gaussian and Rayleigh
transforms, (e) even and odd functions, (f) real
and imaginary parts of complex functions, (g)
the displacement theorem, (h) multiplication
by a constant, (i) change of scale, (j) addition
and subtraction, (k) differentiation of trans-
forms and the transform of a product.

517.93: 531
156 Introduction to Non-Linear Mechanics:
Parts I–4 —N. Minorsky. (United States Navy;
David W. Taylor Model Basin, Reports 534,
546, 538, and 564.) These reports review the
progress up to approximately 1940 in obtaining
solutions to many kinds of nonlinear differen-
tial equations. Numerous examples are given,
many of which are of an electrical nature. Much
of the work is a presentation of material which
has hitherto existed only in Russian books and
papers. Part 1 is concerned with solutions by
topological methods of qualitative integration,
while part 2 gives an outline of the three prin-
ciples of analytical methods that are used by
Pol and Kryloff-Bogoliuboff. In part 3 there
is a discussion of the complicated phenomena of
nonlinear resonance, with its numerous ramifi-
cations, such as internal and external super-
harmonic resonance, entrainment of frequency,
and parametric excitation. Finally, part 4 con-
tains a study of the developments of Mandel-
brat, Chizinik, and Luchakow in the theory of
relaxation oscillations for large values of the
parameter μ which appears in the basic quasi-
linear equation

\[ x'' + \mu x' = x \]

All analytical approaches to a solution of this
equation assume that μ is very small, whereas
for oscillations such as those conformed to by
van der Pol's differential equation, μ is large.

518.5
157 Electrical Analogue Computing: Part 3—
Functional Transformation—D. J. Mynall.
(Electronic Eng., London), vol. 19, pp. 259–
262; August, 1947.) Electromechanical and
electronic devices are described for causing one
quantity to vary as a predetermined function of
another. The system is similar to that used for
multiplication, but some of the potentiometers or
variable resistors involved are nonlinear.

518.5
158 Electronic Computing Circuits of the ENIAC—
767; August, 1947.) "The design principles that
were followed in order to ensure that the integra-
tion of the electronic computer is presented,
and the basic types of computing circuits are
analyzed. . . . The Eniac performs the opera-
tions of addition, subtraction, multiplication,
division, square-rooting, and the looking up of
function values automatically. The units which
perform these operations, the units which take
numerical data into and out of the machine,
and those which control the overall operation
are described. The technique of combining the
electronic circuits to perform these func-
tions is illustrated by three typical computing
circuits: the addition circuit, a programming
circuit, and the multiplication circuit." See also
2481 of 1947 (Wilkes) and 3952 of January
(Iartree).
MEASUREMENTS AND TEST GEAR

621.172: 621.396: 621.001.4 163

Chassis Testing on a Quantity Basis—A. H. Beattie. (Murphy News, vol. 22, pp. 188–191; August, 1947.) A high-quality laboratory receiver incorporating 24 individual crystal-controlled oscillators, which provide suitable signals for all chassis testing. Each oscillator is calibrated to give complete flexibility and permitting the use of low signal levels in the feeders.

621.311 164

A Method for the Measurement of Small Direct Currents—E. J. Harris. (Electronic Engineer's News, vol. 22, p. 19; February 26, 1947.) The small e.m.f. to be measured is interrupted at 50 c.p.s. and applied, in opposition to a variable known e.m.f., to the primary of a transformer. The secondary output, giving complete flexibility and permitting the use of low signal levels in the feeders.

621.332: 537:533:7 105


621.333: 621.316:8 166

Method for Determining the Time Constant of Resistors at Low Frequency—G. Ney. (Comp. Rend. Acad. Sci. (Paris), vol. 225, pp. 227–228; July 28, 1947.) A semisubstitution method, using a Schering bridge, gives the self-inductance and distributed capacitance of a resistor and hence its time constant. Measurements on numerous metalized resistors show that the distributed capacitance is practically negligible and Ohm's law is followed up to frequencies of many hundreds of kc. Measurements on resistors of 1 to 100,000 ohms show, in general, errors in determining the time constant of order of 10⁻⁴ seconds.

621.334 167

Conductivity of Metallic Surfaces at Micro-wave Frequencies—E. Maxwell. (Journ. Appl. Phys., vol. 18, pp. 629–638; July, 1947.) Two methods of measurement which have been used are described. The first involves the measurement of the standing-wave ratio, and the frequency loss, in a shorted waveguide; the second involves the measurement of the conductivity of the resonant cavity. The results for a number of metals are given. Deviation from d.c. conductivity are ascribed to surface roughness.

621.335 168


621.336 169

Connection Errors in Capacitance Measurements—R. F. Field. (Gen. Radi. Exp., vol. 21, pp. 1–4; May, 1947.) Stray capacitance errors are largely eliminated by use of a small diameter for connection to the high potential terminal, the wire being curved so as to increase its average distance from earthy conductors. Correlation of the methods is aided by observing the effect of varying the initial separation of the end of the wire and the terminal.

621.336 + 621.376 170

Royal Observational Standard Frequency Transmissions—(R.S.B. Bull., vol. 23, p. 24; August, 1947.) Brief details are given of the 2-Mc. standards transmitted from Aiber. The accuracy is better than 1 in 10⁸.

621.337-6: 621.311:5 171

WWV Standard Frequency Broadcasts—W. W. George. (F M and Tele., vol. 7, pp. 25–27, 44; June, 1947.) Details of the various transmissions, with photographs of some of the equipment.

621.344-7: 621.311:5 172


621.346-7: 621.311:5 173

Resonant Cavities for Dielectric Measurements—C. N. Works. (Journ. Appl. Phys., vol. 18, pp. 605–612; July, 1947.) The susceptance variation method of measuring dielectric constant and dissipation factor, widely used in the frequency range of a few centimeters to frequencies up to 1000 Mc. Fixed and variable length re-entrant resonant cavities are described; the specimens are in the form of small disks. Design principles are discussed and formulas given for calculating the required dielectric properties. Good agreement is found with values measured by other methods. Some results for typical dielectrics are shown graphically.

621.375:621.382:029:63 174

A Coaxial Load for Ultra-High-Frequency Calorimeter Wattmeters—W. R. Rambo, W. J. Ewing, and V. M. Mathias. (Phys. Rev., vol. 71, pp. 159–162; August, 1947.) Design considerations and description of a broad-band wave load for operation in the frequency band 1000 to 3000 Mc. at input levels within ±15% of full scale. The magnetic force is measured by placing it in a small winding with a high permeability core very close to the surface of the test specimen.

621.374 175

A Method of Measuring Magnetic Permeability for Weak Fields and a Wide Range of Frequencies—J. Epstein. (Comp. Rend. Acad. Sci. (Paris), vol. 225, pp. 532–537; September 29, 1947.) An account of the method used at the Sorbonne and at the Laboratoire National de l'Electricité. A constant magnetic field coil previously described (797 of 1947) can be used for frequencies up to 12 Mc. In the most favorable case a new coil extends the range to 25 Mc. and two others now under construction should enable measurements to be made to 100 Mc. Preliminary results are quoted for powdered-iron cores of low μ and relatively large cross section and for permalloy strip.

621.370 176


621.371-2: 621.374 177

A Cathode-Ray B-H Trace—J. Zamay. (Rev. Gen. Radi. Exp., vol. 66, pp. 175–179; September, 1947.) Two coils are used to pickup voltages from the test sample in a magnetic circuit and apply them by means of an electric circuit to the vertical (flux density B) and the horizontal (magnetic intensity H) sets of deflecting plates of the c.r. tube. The B coil encloses the sample, the H coil is inside it. The magnetic properties are deduced from photographs of the c.r. traces. See also 2247 of 1946 (Long and McMullen).

621.373 178

Apparatus for Measuring Power Loss in Small Ferromagnetic Samples Subject to an Alternating Magnetic Field—K. H. Stewart. (Journ. Sci. Instr., vol. 24, pp. 159–162; June, 1947.) For samples about 15 centimeters by 1 centimeter by 0.03 centimeter. Includes a Bmax meter and a wattmeter in which the a.c. quantities to be measured are balanced. Also p.d. quantities, thus allowing all readings to be made on d.c. meters.

621.377 179

Electrical and Acoustical Instruments shown at the Physical Society's Exhibition [at the American Institute of Electrical Engineers meeting]—J. V. L. Eberly. (Phys. Rev., vol. 24, pp. 148–151; June, 1947.) An account of a few of the exhibits, including the following:—(a) A spectrum analyzer for the output of a klystron, using a cavity resonator which is vibrated by a loudspeaker unit, causing the resonance frequency to vary harmonically. The output from the wavemeter is applied to the output of the p.c.o., whose square wave is fed to the a.c. source operating the loudspeaker. (b) A complete test set for radio installations. (c) A standard frequency generator capable of producing substantially pure frequencies of any integral number of kc. from 2 kc. to 10 Mc. with an accuracy of 3 parts in 10⁴, (d) Counting and pulse circuits. (e) Moving-coil meters, including a d.c. instrument of 100,000 ohms per volt resistance. (f) A supersonic flaw detector. (g) An electroencephalograph with an 8-pen recorder. (h) Magnetic varicimeters with a third scale which can be adjusted from 10⁻⁴ gauss per division upwards, the usual value being 3X10⁻⁴ gauss per division. See also 3581 of 1947 and back references.

621.373 180

A Wide-Frequency-Range Capacitance Bridge—R. F. Field and I. G. Easton. (Gen. Radi. Exp., vol. 21, pp. 1–7; April, 1947.) The RCA capacitance bridge Type 716-C is a Schering bridge circuit adapted for capacitance measurements up to 1000 pF over the frequency range 30 c.p.s. to 300 kc., and up to 1 pF at 1 kc. 621.373 181

A V.H.F. Bridge for Impedance Measurements between 20–140 Mc./s.—R. A. Soderman. (Communications, vol. 21, pp. 26–27; August, 1947.) Summary of a New England Radio Engineers meeting paper. For measurements on lumped-parameter circuits, or on distributed-parameter circuits using coaxial transmission lines, a modified 716-C bridge circuit is used, whereby both the resistive and the reactive components of the unknown impedance are measured in terms of inductive and capacitive reactance.

621.373 182

Abstracts and References

299

J. Martin, (Touise la Radio, vol. 14, pp. 253–256; September, 1947.) Full circuit details and layout of an instrument using in the fixed-frequency oscillator, frequencies 2000, 2004, 2006, and 1998 kc, any one of which may be selected. The variable-frequency oscillator also uses a quartz crystal, whose frequency is varied between 999 and 1000 kc by altering the crystal air-gap. Frequency doubling gives a range from 1998 to 2000 kc, so that, when combined with the fixed-frequency oscillator, frequencies from 0 to 10,000 c.p.s. is covered in 5 steps. Distortion is low and stability excellent.

621.379.79:621.396.813

Distortion Meter—R. Besson. (Touise la Radio, vol. 14, pp. 242–244; September, 1947.) Circuit details and layout of an instrument comprising supply unit, amplifier, tube voltmeter, and a simple type of T-filter using a single inductance with a number of capacitors selected by a switch.

621.379.79:621.392.001.4

Virtual Oscilloscope and Provision Receivers. M. H. Krondorf. (Radio News, vol. 38, pp. 64–65, 122; August, 1947.) Method of using an f.m. signal generator, in conjunction with an auxiliary c.r. tube for aligning the various stages.

621.379.791

Design and Construction of a Universal Meter—A. V. Howland. (R.S.G.B. Bull., vol. 23, pp. 22–24; August, 1947.) The circuit diagram and component values are given for a universal meter to measure a.c. and d.c. voltages, d.c. current, and resistance, using a 0–1-milliampere moving coil meter and a 1-milliampere bridge-connected instrument rectifier. A buzzer is incorporated for continuity testing.

621.379.794

Competition and Characteristics of Evaporated Nickel Bolometers—B. H. Billings, E. E. Barr, and W. L. Hyde. (Rev. Sci. Instr., vol. 18, pp. 429–435; June, 1947.) The bolometers described are approximately 200 A thick and are evaporated on to a nickel-thermocouple about 1000 A thick, which is supported on a glass base with a sand-blasted groove below the bolometer. A thermostatted bolometer has a time constant of 0.004 second and a threshold of 3.3 by 10⁻⁴ watts for radiation modulated at 30 c.p.s., the bandwidth being 100 c.p.s.

631.377.75:621.376.361

Measuring Speed with WWV—J. C. Coe. (Electronics, vol. 20, pp. 90–93; August, 1947.) The a.f. output of a variable-reluctance tachometer generator is 30,000 r.p.m. is compared with the output of a variable-frequency oscillator, which is calibrated by means of harmonics of the standard 440-c.p.s. signal broadcast by station WWV.

539.16:08


551.508.1:621.396.9

The Kew Radio Sonde—E. G. Dymond. (Proc. Phys. Soc., vol. 59, pp. 645–666; July 1, 1947.) A radio transmitter of frequency 26 to 30 Mc. is modulated by an audio oscillator, whose frequency is controlled in turn by temperature, pressure, and humidity units. The modulated output and the values of these three quantities in the neighborhood of the balloon carrying the transmitter. A detailed description is given of the apparatus, and its accuracy is discussed. See also 4263 of 1938 (Thomae).

621.318

Applications of Magnetic Amplifiers—W. E. Greene. (Electronics, vol. 20, pp. 124–128; September, 1947.) The magnetic amplifier, a saturable core type, is described in which the current in an auxiliary winding controls that in the main winding by varying the permeability of the high-μ core, was first used in 1916. It was superseded by the electronic amplifier until the Germans, employing high-μ cores and Se rectifiers, used it for servomechanism amplifiers during the war. The mechanical strength and low ohmic drop make the amplifier suitable for many post-war applications. Research is proceeding to overcome the slowness of response at very low frequencies, an inherent fault, and to produce better core materials. By using feedback, power gains of 10^5 have already been obtained.

621.319.330.027.3

The Imperial College High-Voltage Generator—W. B. Mann and L. G. Grimmet. (Proc. Phys. Soc., vol. 59; July 1, 1947.) "The design and construction of two pressure-insulated electrostatic generators similar to those of Van de Graaff and Trump are described briefly. Voltage tests with one of the generators with mixtures of nitrogen and freon under pressure have shown it to be capable of producing voltages in excess of two million."

621.319.43:621.371.79:531.718.4+531.787.9

A Variable Capacitor for Measurements of Pressure and Mechanical Displacements; A Theoretical Analysis and Its Experimental Evaluation—J. C. Lilly, V. Legallais, and R. Cherry. (Jouir. Appl. Phys., vol. 18, pp. 613–628; January 172.) The capacitor consists of a fixed plane electrode and a parallel diaphragm, which is clamped at the edges. Small displacements, volume changes, or pressure differences, acting upon the diaphragm, are deduced by electrical measurement of the resulting change in capacitance.

621.365.5.001.8+621.365.92.001.8


621.365.93:621.377.37+621.301.15

Dielectric Loss at High Frequency—Whitehead. (See 172.)

621.38:629.13.054

Precision Balancing at Mass-Manufacturing Speed—S. Bousky. (Electronics, vol. 20, pp. 95–104; September, 1947.) The periphery of a gyro rotor is stamped with a series of numbers; unbalance at any point is indicated when a stroboscopic lamp illuminates the correspondingly numbered surface. Full constructional details and operational procedure are given. A rotor can be balanced to within 5X10⁻⁶ oz-inches in 2 minutes.

621.38:390.001.8:629.13

Electronics and Aeronautical Research—(Engineering (London), vol. 164, p. 91; July 25, 1947.) An account of equipment on view at an exhibition arranged by the Instrumentation Department, R. A. E., Farnborough, including various types of acceleration and pressure pick-up, multichannel recording equipment, 4-way c.r. equipment, 600-way static strain recording equipment, transmitting and statistical accelerometer, and an electronic torque-meter. See also Engineer (London), vol. 184, pp. 85, 87; July 25, 1947.
An Electron Accelerator with an Air-Cored Field—H. Hill, Nature (London), vol. 159, pp. 774–775; June 7, 1947.) The electric field, produced by a pulsed 25-centimeter magnetron, having recurrence frequency 100 per second pulse width, and peak power 300 kilowatts, is fed to dees by a Lecher wire system. The dees are 2 centimeters deep, have a radius of 3 centimeters and contain a tungsten filament 4 inches in diameter. The focusing field is 425 gauss and the dynamic field 300 gauss at the peak of a sinusoidal 250-kc. oscillation. Absorption curves show that the inclusion of a dynamic field results in an increased X-ray yield of harder radiation.

An Acceleration of Charged Particles to Very High Energies—M. L. Oliphant, J. S. Gooden, and G. S. Hide. (Proc. Phys. Soc., vol. 59, pp. 666–677; July 1, 1947.) A synchrotron is being built at Birmingham University to accelerate protons to 1000 Mev. The advantages of the technique and the design of the magnet and its excitation are described in detail. Electron energies up to 300 to 400 Mev are possible, higher energies being prevented by radiation loss. For proton energies above 10^9 e.v., the cost of this method would be prohibitive. For theory see 209 below.


A Memory Tube—Haefl. (See 326.)

The Design and Construction of an Electron Microscope—M. E. Haine, Engineering (London), vol. 164, pp. 20–24; July 4, 1947.) Long summary (J. H. S. Measurements Section) paper giving details of the Metropolitan-Vickers Type EM2 electron microscope. The general construction, the procedure for aligning the microscope, the magnetic lenses, and the operating and photographic techniques are described in detail. The instrument is continuously pumped, uses an accelerating voltage of 25–50 kv. and gives a magnification of 10,000 diameters.


A New Electron Microscope with Continuously Variable Magnification—J. B. le Poole. (Phil. Tech. Rev., vol. 13, pp. 33–35; April, 1947.) An electron microscope constructed at Delft in 1944 is fully described and compared with previous models. Its resolving power is 25 A and its magnification is continuously variable from 1000 to 8000 diameters. Various applications are mentioned.


A Space-Charge Lens for the Focusing of Ion Beams—D. Gabor. (Nature (London), vol. 169, pp. 89–90; July 19, 1947.) Suggested a sign for a powerful concentrating lens for positive ions, particularly those of extreme energy. Meana are described for maintaining a suitable space-charge inside a hollow cylinder using electrons derived from an auxiliary ring-shaped cathode. The focal length of the lens is expected to increase only linearly with the energy of the ion beam, and the design should yield lenses of relatively short focal length to be made.


X-Ray Tube with Very Bright Line Focus—M. Pottevin. (Compt. Rend. Acad. Sci. (Paris), vol. 224 pp 1709–1711; June 16, 1947.) Details of a tube with curved filament located in a groove cut across the face of a semicircularly concentrated piece. The apparent brightness is 30 k./mm.² when the apparent dimensions of the focus are those of a square of side 0.1 mm.

Metal Locator with Remote Field Source—Beams Jour, vol. 54, p. 271; August, 1947.) Describes a unit for use in the ER.A Mine Locator No. 7. The magnetic field is generated by a cable fed by a.c. and laid on the ground in a large loop, instead of by the search unit. Therefore, its operating range is not limited by the magnetic properties of the ground.


Air-Borne Magnetometers—E. P. Felch, L. G. Purrett, W. J. Means, L. H. Kneubuhm, T. S. Schmitt, and A. J. Tinkham. (Elect. Eng., vol. 66, pp. 680–685; July, 1947.) An inductor with an open core of highly permeable and easily saturable material, such as permalloy, is connected in the unknown field, with a superposed sinusoidal magnetomotive force large enough to saturate the core. The time variation of the core flux induces an e.m.f. in a coil surrounding the core; this e.m.f. is fed into an electronic circuit and there analyzed. The sensitivity increases with the length of the core, but is limited by the highest impedance which can be maintained at the grid of the first tube with satisfactory stability. With a 1.5-inch length, the sensitivity exceeds 10 microvolts/μ (1μ 10^-6 oersted). The detector is a direct current potentiometer, and the sensitivity is controlled by the controlling action, through servomotors, of two auxiliary inductors. The apparatus records variations in the sum of the squares of the outputs of all three inductors, hence giving the variations of the unknown field. See also 3245 of 1947 (Shackleton).


Electronic Developments [Book Review]—R. G. Britton. George Newnes, London, 206 pp., 7s. 6d. (Electronic Eng. (London), vol. 19, p. 268; August, 1947.) *This book will be of value even to those already acquainted with many applications of electronic science, and a well-balanced survey of such an important subject is something new in more than one sense."

PROPAGATION OF WAVES


The Field of a Microwave Dipole Antenna in the Vicinity of the Horizon—C. L. Pekeris. (Jour. Appl. Phys., vol. 18, pp. 667–680; July, 1947.) Three cases are treated in which the transmitter or receiver is either on the ground or elevated. For very short waves, the field at points on the horizon approaches that of the direct wave diffracted by a straight edge at the point of tangency. The results are compared graphically with the exact theory of van der Pol and Bremer (2249 of 1939 and back references). When both transmitter and receiver are on the ground, the potential can be expressed as the sum of a surface wave for a flat earth and an integral depending upon the earth radius, these two terms tending to cancel at large distances.

The Structure of an Electromagnetic Field in the Vicinity of the Horizon of the Earth—C. L. Pekeris. (Phil. Mag., vol. 37, pp. 311–317; May, 1946.) *A detailed mathematical and numerical study of the field structure at and near a line focus of a cylindrical electromagnetic wave train possessing any finite amount of cylindrical aberration of the first order."

A Method for Calculating Electric Field Strength in the Interference Region—H. E. Newell, Jr. (Phil. Mag., vol. 35, p. 777; August, 1947.) Brief summary only. For an interference region, over a spherical earth, which has an effective radius equal to four-thirds of the radius of the earth, the field strength is limited by the great number of graticular steps involved, but the procedure has given "very useful working estimates."

Circularly Polarized Waves Give Better F.M. Service Area Coverage—T. B. Friedman. (Tel–Tech., vol. 6, pp. 26–30, 102; August, 1947.) A discussion of the theory and practical applications of circularly polarized radiation, and its advantages in certain cases of f.m. reception.
621.360:11:551.510.535
Some Observations of the Maximum Frequency of Radio Communication over Distances of 1000 km and 2400 km—W. J. G. Beynon. (Proc. Phys. Soc., vol. 59, pp. 521–534; July 1, 1947. Discussion, p. 535.) The maximum usable frequencies for radio transmission from short-wave broadcasting stations near Berlin and Moscow were observed from at Slough of the field strength variations from dawn to dusk and from sunrise to sunset. The results were compared with theoretical values deduced from vertical-incidence ionospheric measurements at Slough and at Bourghead (Scotland). Certain ionospheric conditions at the midpoint of the trajectory had a notable effect on the maximum usable frequency. It is concluded that the main source of the discrepancy lies in the inadequate knowledge of ionospheric conditions at the midpoint of the trajectory.

621.360:11:551.510.535
A Frequency Prediction Service for Southern Africa—F. J. Hewitt, J. Hewitt, and T. L. Wadley. (Trans. S. Afr. Inst. Elect. Eng., vol. 38, part 2, July, 1947. Discussion, pp. 193–197.) A discussion of existing facilities and the proposed short-term predictions of ionospheric disturbances. The nature of the observed data and the prediction methods are described. As local data over a number of years do not exist, back data from Australian records are used, suitably modified according to present observations in South Africa. A new design of recorder uses a double superheterodyne receiver-transmitter. The frequency is swept from a few hundred kilocycles to 20 Mc, in one step; and the only moving part is the rotor of the main sweeping oscillator. Automatic frequency calibration is provided. The complete sweep takes 15 seconds and the display on a long afterglow r.c.r. tube is suitable for visual or fully automatic photographic recording.

621.360:11:551.510.535
How Daytime Skywave Reflections Affect Cleared Channels—(Tele-Tech, vol. 6, pp. 45–47; August, 1947.) Report on a conference organized at which evidence was produced suggesting that daytime sky-wave reflections could cause interference in the 550 to 1600 kc. band. Little information was available at the time.

621.360:61:215.396.913
F.M. Receiver Design for Rail Radio Service—Martin. (See 309.)

621.360:61:215.029.6
Transmitter-Receiver, 280–330 Mc./s.—Dieutegard. (See 308.)

621.360:61:215.029.6
Heterodyning and Modulation—C. W. Mitchell. (Wireless World, vol. 53, p. 359, October, 1947.) A simplified method of additive and multiplicative mixing, indicating that the required frequency change and modulation are multiplicative processes, irrespective of the method employed

621.360:610:215.029.6
F.M. Receiver Design for Rail Radio Service—Martin. (See 309.)

621.360:610:215.029.6
F.M. Receiver Design for Rail Radio Service—Martin. (See 309.)

621.360:610:215.029.6
Harvey Double Superheterodyne F.M. Receiver—B. J. Cosman and A. W. Richardson. (F.M. and Tele., vol. 7, pp. 21–24, 52; June, 1947.) Circuit details and description of a commercial receiver covering the frequency range 85 to 115 Mc. with a bandwidth of 250 kc. Another similar aerial input and the i.f. frequencies are 10.7 Mc. and 4.6 Mc., the latter being crystal controlled. Audio amplifier response is linear from 20 to 15,000 c.p.s.

621.360:610:215.029.6
Simple Converter-Preselector—F. C. Jones (CQ, vol. 3, pp. 31–34, 70; June, 1947.) "A unit to give broadcast band, 15- and 6-meter coverage, as well as preselection on other bands, for a receiver with limited tuning range.

621.360:610:215.029.6
Ratio Detector for F.M. Signals—(Tele-Tech, vol. 6, pp. 46–49; July, 1947.) Modifications to the balanced discriminator circuit for conversion from i.f. to a.m. are described which make it independent of input amplitude variations due to fading, to multipath reflections, to selective effects in the r.f. stages or to unbalances in the detector itself. See also 3643 of 1947 (Seeley and Avins)."
302 PROCEEDINGS OF THE I.R.E.—Waves and Electrons Section

621.396.283 253 Ignition Interference: Part I. Its Nature, Magnitude and Measurement—W. Nethercot. (Wireless Eng., vol. 25, pp. 352–357; October, 1947.) A comprehensive account of unpublished reports by the Electrical Research Association on the mechanism of the ignition spark and the field strength to which apparatus, such as telephone and length of the ignition leads, are discussed. See also 402 of January (Turney).

621.396.282 254 Curing Interference to Television Reception—M. Seybold. (QST, vol. 31, pp. 19–23, 110; August, 1947.) A detailed account of methods of harmonic suppression applied to a 14-Mc. transmitter to improve a neighbor's television reception. Full-power transmitter operation was subsequently possible.

621.396.288:621.396.1 255 Installations for Improved Broadcast Reception by a Cortney Van Shooten. (Philips Tech. Rev., vol. 9, pp. 55–63; 1947.) A method of diversity reception is used to eliminate selective fading. Three identical sets of receiving equipment are situated about 2 kilometers apart. Voltages $E_1$, $E_2$, and $E_3$, which increase with the signal strength, are fed from each of the receivers to the corresponding tubes $V_1$, $V_2$, and $V_3$. A three-tube switching circuit of the Eccles-Jordan type, of which a diagram is given. If $E_3$ is the greatest of the voltages, the switching circuit is only stable with $V_3$ carrying a high anode current and $V_1$ and $V_2$ carrying practically no anode current. Interference from other transmitters on neighboring frequencies is counteracted by using directive frame aerials. The freedom from disturbance thus obtained enables the bandwidth of the receiving set to be increased, thus improving the quality of the reproduction.


STATIONS AND COMMUNICATION SYSTEMS

621.395.43:621.392.099.64 257 The Exploitation of Micro-Waves for Trunk Wave-Guide Multi-Channel Communications—H. M. Barlow. (Journ. Brit. I.R.E., vol. 7, pp. 251–257; October, 1947. Discussion, pp. 257–258.) The use of the H$_0$ waves in a cylindrical waveguide at 40,000 Mc is suggested. Attenuation would be about 6 db per mile, making repeaters at 8-mile intervals necessary when using a 1.5-inch diameter copper waveguide. The repeaters would be located 2000 ft above the ground, and after amplification, this signal to re- modulate a new carrier on 40,000 Mc. Thousand of speech channels on a single waveguide may be possible.

The waveguide might also be used as a 132-kv., 50-c.p.s. power line.

621.395.43:621.396.619.16 258 Pulse Code Modulation Method for Multi-Channel Telephony—R. R. Batchelor. (Tele- Tech, vol. 67, pp. 28–33; July, 1947.) Description of a system of modulation in which the variations of amplitude of the speech wave control the amplitude of short pulses at a sampling rate that will give at least two pulses per cycle at the highest audio frequency, but many more at the lowest. The pulse amplitude variations are transmitted over the system by a special five-digit code permitting the handling of 32 levels instead of 2. Details of the method are described. The system is stated to be distortionless and free from cumulative noise effects on long circuits. For another account of this system, see S. Black, see Bell Lab. Rec., vol. 25, pp. 265–269; July, 1947.


621.396.65 262 Mobile V.H.F. Radio Telephone (—Electro, vol. 139, p. 117; July 11, 1947.) A description of a single-unit unit-receiver having a maximum current consumption of 10 amperes from a 12-volt heavy duty battery and output of 6 watts on any limited frequency band in the v.h.f. range. Either a.m. or f.m. can be used. The equipment weighs 16 and two thirds pounds, and its overall dimensions are 9 and three quarter inches by 7 and three quarter inches by 8 inches.

621.396.65 263 A Frequency-Modulated Multi-Channel V.H.F. Radio Link—E. S. Teitscher. (Electronics, vol. 2, pp. 256–258; August, 1947.) A f.m. adaptor is used in place of the ordinary modulator, in order to obtain a higher degree of linearity and reduce cross talk between the channels.


621.396.65:621.397.5 265 Television Extensions—(See 297.)
train and a radio station for the purpose of a broadcast from the train to a ship at sea. A phase-modulated duplex system working on frequencies in the region of 100 Mc was used and contact was maintained for distances up to 15 miles from the radio station.

621,306,021,020,62 274

621,306,931,026,93 275
Telecontrol of Aerodrome Ground Station Receivers—J. E. Benson and W. A. Cobleek. (Proc. I.R.E. (Australia), vol. 8, pp. 8-15; June, 1947.) A general discussion of radio communication services for civil aviation was given by Newstead (3425 of 1946). A crystal locked 3-channel telecontrolled receiver installation operating in the 0.3-, 3-, and 6-Mc. frequency bands is described. The outputs from the receivers are conveyed over three independent telephone lines which also serve for the d.c. potentials used for switching from c.w. to speech, and for switching on and off the power supply and preset test oscillator.

SUBSIDIARY APPARATUS
621,526,021,453,14 276
Automatic Frequency Control of Micro-wave Oscillators—V. G. Rideout. (Proc. I.R.E., vol. 35, pp. 767-771; August, 1947.) A technique applicable to any type of tunable microwave oscillator is described. In this method, a servomechanism is used which includes a waveguide discriminator circuit, a mercury-contact relay which vibrates at 60 c.p.s., and a set of relays to confine the output energy in 60-c.p.s. square waves, a 60-c.p.s. amplifier and a small 2-phase induction motor. A stability of 1 part in 30,000 is obtainable.

621,314,58 277
A D.C. Mains-Operated Vibratory Inverter—E. E. Cornelius. (Proc. I.R.E. (Australia), vol. 8, pp. 16-18; June, 1947.) Using the piezoelectric effect in quartz, a constant-frequency a.c. output is obtained by the application of the piezoelectric effect to a crystal. The power factor control is described for the number of primary turn pairs. The effect of frequency is indicated. Types of iron circuit and inductor are covered. The efficiencies of various types are shown to be 63 to 80 per cent over the operating range of load resistance. The interference-free unit has been constructed on this principle, to operate from 220-volt a.c. mains and to provide 500 watts of a.c. energy at 250 volts. The conversion efficiency is 65 to 80 per cent and the output voltage is 500 volts.

621,317,722,107,68 278

621,318,572 279

621,318,572:021,598 280
R.F. Operated Remote Control Relay—D. G. Fink. (Electronics, vol. 20, pp. 114-116; September, 1947.) The relay, which consumes no stand-by power, responds directly to the current in the grid circuit. It closes on 8 in. of the 10 mv. r.f. signal and can be operated by a tuned circuit and crystal, and actuates a power relay. It can be used at unattended stations or as a carrier-failure alarm.

621,396,68 281
The Characteristics of Power Supplies for Radio Transmitters—W. E. Pennett. (Marconi Rev., vol. 10, pp. 33-40; April to June, 1947.) The use of constant voltage supplies for the transmitter is discussed. The voltage regulation obtained is indicated. Types of iron circuit and inductor are covered. The efficiencies of various types are shown to be 63 to 80 per cent over the operating range of load resistance. The interference-free unit has been constructed on this principle, to operate from 220-volt a.c. mains and to provide 500 watts of a.c. energy at 250 volts. The conversion efficiency is 65 to 80 per cent and the output voltage is 500 volts.

621,396,68:021,314,222 282
The Theory and Practice of Constant Voltage Transformers and Power Supplies: Part 1—R. H. Burdick. (Marconi Rev., vol. 10, pp. 59-71; April to June, 1947.) The reasons for using constant voltage transformers are discussed. The type of transformer is described. A method for the stabilization of transformer output is described and a series capacitor scheme is outlined. For constant voltage operation, the product \( V_{\text{in}} \cdot H_{\text{min}} \) is constant. For the stabilized condition, the secondary voltage is independent of the number of primary turns. The effect of frequency is indicated. Types of iron circuit and inductor are covered. The efficiencies of various types are shown to be 63 to 80 per cent over the operating range of load resistance. The interference-free unit has been constructed on this principle, to operate from 220-volt a.c. mains and to provide 500 watts of a.c. energy at 250 volts. The conversion efficiency is 65 to 80 per cent and the output voltage is 500 volts.

621,396,68:021,316,722 283
Low-Voltage [high current] Regulated Power Supplies—F. W. Smith, Jr., and M. C. Thiex. (Electronics, vol. 27, pp. 72-75; July, 1947.) Voltage regulation obtained by feeding the output voltage back through a d.c. amplifier to control a saturable reactor in the a.c. input circuit. Characteristics of a 6-volt, 14-ampere supply are given.

621,396,68:021,316,722:4 284
Design of Regulated Power Source—L. L. Helterline, Jr. (Tele-Tech, vol. 6, pp. 63-65, 107, July, 1947.) A description of the Sorensen Nobatron regulated d.c. supply device. A bridge circuit incorporating a mains-heated, temperature-limited diode in one arm is used, and voltage variation of the a.c. supply causes changes typical of changes in the input to the rectifier. By limiting the input to the rectifier, 0.5 per cent regulation and 1 per cent ripple voltage are claimed.

621,396,68:021,316,722:4 285
Voltage-Regulated Power Supplies—L. Mautner. (Electronics, vol. 27, pp. 894-910; September, 1947.) The basic series-type regulator circuit is analyzed; it can be regarded as a cathode follower. Methods of obtaining low internal impedance and low output ripple are discussed. Various typical reference-voltage connections and the necessity for a stable feedback amplifier are considered. Five circuits for specific applications are given, together with calculated performance data. See also 4046 of January (Koons and Dilatash).

621,396,682:021,397,62 286
R.F. Operated Remote Control Relay—D. G. Fink. (Electronics, vol. 19, p. 245; 1947.) The line-scan sawtooth wave form is applied to the control grid of the tube. The signal is amplified off of the anode current at flyback causing a coil in the anode circuit to ring. The high oscillator voltage generated is rectified by a diode whose heater current is provided by a small coil coupled magnetically to the ringing coil.

621,396,69 287
Maintenance Mats for B.B.C.—(Engin. News, (London), vol. 184, p. 110; August 1, 1947.) A description of a transportable mats which may be quickly erected near permanent mats for use while maintenance work is done on the main installation. They are triangular, parallel sided, 300 feet high and insulated for 70 k.v. a.m.s. There are also light weight 4 and one-quarter tons including fittings.

778:621,396,619,23:021,396,96 288
Photographing Pulse Wave Shapes of Radar Modulators—J. W. Marks. (Tele-Tech, vol. 6, pp. 60-62; 103; July, 1947.) Single modulations from the required shape of the output pulse of radar modulators may cause serious loss of power, double moding, misfiring, and frequency modulation of the associated transmitter. In production testing, the pulse wave shape is photographed for comparison with a standard to diagnose possible sources of trouble. Equipment for this purpose is described.

TELEVISION AND PHOTO TELEGRAPHY
621,397,73 289
Facsimile is Ready for Home Use—M. B. Sleeper. (FM and Tele., vol. 7, pp. 19-20, 55; June, 1947.) Acrophone is now commercially practicable, and transmission standards are required. A definition of 103 lines per inch and a paper speed of 3.43 inches per minute have been agreed upon and a paper speed of 4.1 and 8.2 inches per minute is proposed. Standardizers using a width of 8.2 inches are expensive and require a flat frequency response range beyond that of the average f.m. set. Once a pulse facsimile picture has been instituted, its use will spread rapidly.

621,397,26 290
V.H.F. Link for Press Photos—(Electronics, vol. 20, pp. 100-102; August, 1947.) A mobile equipment for picture transmission scanning at 90 lines per minute and using an 1800-c.p.s.a.m. tone for the picture gradations. Transmission time for a 5-inch by 7-inch photograph is about six minutes.

621,397,331,2 291
Improvements in Electronic Television Cameras—P. Hémondinger. (T.S.F. pour Tous, vol. 23, pp. 163-165 and 191-193; July, August, and September, 1947.) Descriptions of the iconscoop or emitter, the super-emitter or the orthicon and the image orthicon and their mode of operation; also of the iconscoop of Barthélémy and a method of modulation resembling somewhat the super-emitter type method used in radio receivers.

621,397,335 292
Image Generator Frequency Stability and TV Remote Pickups—W. J. Pooh. (Communications, vol. 27, pp. 14-39; July, 1947.) Locking the synchronizing generator to the power-supply system has advantages where power-supply frequency variation is small.

Abstracts and References
303
The generator can also be locked to a crystal oscillator; in this case, wire or radio links may be needed for maintaining a close relationship between vertical blanking signals. Pulse timing and amplitude during switching are also considered.

621.397.5 The Verdict of the F.C.C.—(Télégr. Franç., Supplement Électronique, p. 17; June, 1947.) (a) No color television for 5 years. (b) Immediately start of black-and-white television on the present line standard. (c) It is laboratory practice to invite continuing research in order to achieve an absolutely flawless color television system.

621.397.5 The French [line] Standard—(Télégr. Franç., Supplement Électronique, p. 17; June, 1947.) The Comité Mixte de Télévision, at the session of May 28, 1947, has decided (a) to maintain for 10 years the present line standard for the Paris district and (b) to put into service in about 2 years a high-definition standard of about 1000 lines.

621.397.5:535.88 A New Television Projection System—W. E. Bradley and E. Traub. (Electronics, vol. 20, pp. 84-89; September, 1947.) Combination of a S.C.C. oscillograph, with a new fluorescent phosphor, directional viewing screen, and key-stone projection, produces an image 15 inch by 20 inch picture of exceptional brightness and contrast.

621.397.5:535.88:532.62 Theoretical Studies of the Use of Quasi-Insulating Ediphors for Large-Screen Television Projection—H. Thiemann. (Schweiz. Arch. Angew. Wiss. Tech., vol. 13, pp. 147-154, 175-182, 210-217, and 239-252; May to August, 1947.) A continuation of previous work (3080 of 1941 and 1736 of 1942). The term ediphor is applied to a thin layer of a viscous fluid whose surface deformation can be used for television projection. The wiping out of the surface charge on the ediphor with the help of secondary emission is fully discussed and a general theory is presented of the electro-hydrodynamical problems associated with the deformation of the surface of liquid ediphors of finite thickness. Picture production methods are described and stability conditions considered. See also 554 of 1947.

621.397.5:621.396.05 Television Extensions—(Elect. Times, vol. 111, p. 675; June 12, 1947.) A brief general description of the 1000-Mc. link, now under construction to carry normal 405-line, 50-frame per second signals from the Alexandra Palace to the relay station in Birmingham. Three successive optical paths will be used, one of 20 miles and two of 40 miles, with 80-foot towers at the intermediate stations. For another account see Elect. Rev. (London), vol. 140, p. 984; June 13, 1947.

621.397.5:621.396.05 F.C.C. Studies TV Relays for Inter-City Network Systems—(Tele-Tech, vol. 6, pp. 34-37; August, 1947.) Report of conference organized by the F.C.C. Several links are already in operation, and the system between New York, Philadelphia, Pittsburgh, and Washington is practically complete. The New York-Chicago link of 900 miles will use 35 repeaters, and an aerial system operating uniformly over the band 3700 to 4200 Mc.

621.397.5:621.396.82:3:551.594.21 Televisión y thunderstorms—III. (See 232.)

621.397.62 The R.C.A. Television Receiver—Type 300—M. Chavvière. (Radio Frang., pp. 12-17; July, 1947.) An account of some of the principal features, with a complete circuit diagram. 13 stations having frequencies between 44 and 216 Mc. can be received.


621.397.62 Build Your Own Television Receiver—L. S. Wecker and T. Gootée. (Radio News, vol. 38, pp. 45-48; August, 1947.) The construction and adjustment of a receiver covering all channels from 44 to 88 Mc., which can be built from the components and chassis of a war-surplus oscilloscope, Type BC-412, with a Type 5FP4 c.r. tube.


621.397.62:621.314.67 Pulsed Rectifiers for Television Receivers—Maloff. (See 311.)

621.397.62:601.4:621.317.79 Visual Alignment of Television Receivers—Kronenberg. (See 192.)

TRANSMISSION

621.396.61:621.396.41 An Inexpensive Rig for Local Duplex Operation—D. D. Ralston. (QST, vol. 31, pp. 52-53; August, 1947.) Low-power equipment for R/T on 11 meter.

621.396.61:621.029.6 Transmitter-Receiver, 280-330 Mc./s.—Diegertag. (QST, vol. 31, pp. 246-251; September, 1947.) Three distinct units are included: (a) the oscillator-detector, (b) the amplifier-modulator and (c) the supply unit. A current gain of 10 is obtained by the use of Type 955 and the use of a common source and is tuned and weighted by Lecher lines with a variable bridge, the whole system being enclosed in a metal tube, with suitable coupling for the double aerial. Aerial and circuit details are given.

621.396.931:621.396.61:621 F.M. Receiver Design for Rail Radio Service—D. W. Martin. (Communications, vol. 27, pp. 14-17; August, 1947.) Circuit details of a F.M. receiver-transmitter for use in the band 152 to 162 Mc. The receiver has a modified single superheterodyne circuit using half-frequency mixing to reduce reraidation and spurious responses. Special cone-wound coils are used in the temperature-compensated i.f. transformers. Figures are shown for sensitivity and selectivity.

621.396.537.533.8 Vacuum Tubes and Thermionics—Present State of Knowledge of Secondary Electron Emission from Solid—Palluel. (See 89.)

621.396.147:621.397.62 Pulsed Rectifiers for Television Receivers—I. G. Maloff. (Electronica, vol. 20, pp. 110-111; August, 1947.) "Brief analysis of pulsed cascade rectifiers used in television receivers indicates that no component is subjected to potentials substantially higher than those encountered per section. In a doubler, this voltage is about half the output voltage from the rectifier."
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(Continued on page 55A)
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The dependability and performance of these VHF communication and navigation systems spells increased safety in flight, more efficient aircraft operation. Specify A.R.C. for your next installation.

ENGINEER, SENIOR
Fine opportunity with a large midwestern radio corporation. Must have a minimum of three years' experience in loud-speaker design and materials used in manufacturing. College education in electronics or equivalent. In replying state age, education, experience, and salary requirements. Box 508.

ELECTRONIC ENGINEERS WANTED
Engineers experienced in the development and design of electronic equipment.

Opportunity for advancement with long-established and growing company. Laboratories and plant situated in pleasant, open surroundings on Long Island within half hour of New York City.

Also openings for Junior Engineers.

Write details of education and experience to Personnel Office HAZELTINE ELECTRONICS CORPORATION Little Neck, L.I., N.Y.
Positions Wanted By Armed Forces Veterans

In order to give a reasonably equal opportunity to all applicants, and to avoid overcrowding of the corresponding column, the following rules have been adopted:

The Institute publishes free of charge notices of positions wanted by I.R.E. members who are now in the Service or have received an honorable discharge. Such notices should not have more than five lines. They may be inserted only after a lapse of one month or more following a previous insertion and the maximum number of insertions is three per year. The Institute necessarily reserves the right to decline any announcement without assignment of reason.

JUNIOR ENGINEER

TECHNICAL EDITOR
Former AAF officer with four years experience in writing and editing technical project reports and summaries, budget defense, press releases, technical papers, etc. Assigned during this period to Radiation Laboratory, M.I.T. and Aircraft Radio Laboratory, Wright Field. Additional experience as sales engineer (2 years), radio and radar technician (2 years), and two years of college credits towards E.E. degree. Box 131W.

ELECTRONIC ENGINEER
B.E.E. Ohio State University, June 1948. Two years as electronics technician, U. S. Navy. Would like position in research or development. Victory New York or Cleveland. Box 136W.

ELECTRICAL ENGINEER

RADIO ENGINEER
B.E.E. from N.Y.U. 1947; Graduate work B.S. in physics from C.C.N.Y. 1943. Signal Corps radio and repeater man telephone experience. Desires design and development work in radio, industrial electronics or communications. Box 137W.

ELECTRONICS ENGINEER
B.E.E. Drexel Institute, 1936. 11 years experience in radio transmitter design, electronic control circuits, bridge, oscillators... (Continued on page 54A)
A marked increase in service life and performance of brush contacts is made possible by using minute quantities of an appropriate precious metal alloy for the actual contact. The photograph above shows brush arms and contacts used in a variety of typical applications. Note the small amount of precious metal needed to assure superior service.

Ney also offers industrial users a wide range of precious metal alloys for many specialized applications as well as gold solders and fine resistance wires (bare or enameled). Details on request.

Positions Wanted

(Continued from page 53A)

tor, amplifier and null detector design. Investigation of foreign electronic equipment. Also new short wave therapy circuits. Box 123W.

ELECTRONIC ENGINEER—PHYSICIST

Electronic Engineer—Physicist. Graduated Princeton University. Wide research experience. Circuits, aircraft-servo-mechanisms, microwave plumbing, antennas. Able to take full charge of project from design specifications through preliminary manufacture. Prefer small aggressive company with aircraft connections. Box 141W.

ENGINEER

Engineer, 25 years old desires personnel or contact position where three years as a Signal Corps officers followed by two years of electronic laboratory and factory experience will pay dividends. Married and will locate anywhere. Box 142W.

DESIGN AND DEVELOPMENT ENGINEER

Design and development engineer—Extensive experience FM and VHF, broadcast equipment and audio, some microwave. Both theoretical and practical background. Registered Professional Engineer. Employed but good reason for desiring change. Box 143W.

PHYSICISTS ENGINEERS

The establishment of a new section in our research laboratory requires the services of Junior and Senior Electronic Engineers, Servo Engineer and Physicists.

An excellent opportunity to grow with this expanding group and receive responsibility commensurate with your ability.

EMPLOYMENT SECTION

Bendix Aviation Corporation
Research Laboratories
4855 Fourth Avenue
Detroit, Michigan

Write or phone (Hartford 2-4271) our Research Department

THE J. M. NEY COMPANY 171 ELM STREET, HARTFORD 1, CONN.
SPECIALISTS IN PRECIOUS METAL METALLURGY SINCE 1812

NEW! RH-7-C
SUCCESSOR TO RH-243

An adaptation of the famous RH-7 crystal unit, RH-7C offers such advantages as:

- Smaller Size (1" x ¾ x 11/32", more than ½ smaller than RH-243)
- Smaller Weight (Less than ½ the weight of RH-243)
- Improved Accuracy (can be made to ±0.005% over a temperature range of -55° C to +90° C).
- Greater Frequency Range (3-15 mc Fundamental and 15-75 mc Harmonic Mode, compared to RH-243's 3100-10,000 kc.)
- True Hermetic Seal
- The Greater Stability of Wire Mounting
- Completely Interchangeable with RH-243

REEVES-HOFFMAN CORPORATION
SALES OFFICE: 215 EAST 91 STREET, NEW YORK 28, N. Y.
PLANT: 321 CHERRY STREET, CARLISLE, PA.
HIGH FIDELITY EV-635 MICROPHONE USES "XL" PLUG

Electro-Voice has equipped the new EV-635 High Fidelity Dynamic Microphone for studio and remote broadcasting, with the Cannon Type XL-3-11 Plug—a quality plug for a quality microphone.

Shown at left is the new XL-3-36 Wall Receptacle (pin insert) engaged with an XL-3-11 Plug. XL-3-36 is priced at $5.65 List; and XL-3-35 (socket insert) $4.95 List.

For a practical, low cost but high quality connector series having three 15-amp. contacts, choose the "XL". Four plug types and six receptacles with 3 adapter receptacles are available. Min. flashover voltage 1500 Volts.

Above are the two zinc plugs (Left) XL-8-12, List $1.20 and (right) XL-8-11, List $1.25.

No other small electric connector has all the features of the XL, including the safety latch lock.

XL Connectors are available from more than 250 radio supply houses throughout the U.S.A.


CANNON ELECTRIC Development Company
3209 HUMBOLDT ST., LOS ANGELES 31, CALIF. IN CANADA & BRITISH EMPIRE: CANNON ELECTRIC CO., LTD., TORONTO 13, ONT. WORLD EXPORT (Excepting British Empire): FRAZAR & HANSEN, 301 CLAY ST., SAN FRANCISCO

News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 49A)

Tetrode Type 4-400A

A new 400-watt Eimac tetrode, known as type 4-400A, has been announced by Eitel-McCullough, Inc., 189 San Mateo Ave., San Bruno, Calif.

This new tetrode is ruggedly designed, physically small, and of compact structure. Design features which contribute to its stability, long tube life, and economy of operation, are the short low-inductance leads, processed nonemitting grids, thorian-tungsten filament, and plate of new Eimac material, Pyrovac.

The 4-400A is radiation-cooled, and is suggested for use in the special Eimac socket and air duct. According to the manufacturer, two of these tetrodes conservatively operated will provide over 1 kw. output power at 4000 plate volts on the 88-108-Mc. f.m. band.

Permanent-Magnet Speakers

A standard line of permanent-magnet speakers for general replacement and sound-systems work has been announced by the Tube Department, Radio Corporation of America, Harrison, N. J.

Engineered to RMA standards, these speakers feature high-quality cones for rattle-free response, rugged dustproof and rust-resistant mechanical construction, powerful Alnico magnets, and moisture-proof centering. The line includes a controlled-resonance 12-inch speaker, a 4-inch and a 5-inch speaker, a 4-by-6-inch elliptical speaker, and a 2-by-3-inch elliptical speaker.

Complete specifications and descriptions of the speakers are included in Catalog Sheet 2F384R, available from RCA tube distributors or from the Renewal Sales Section, Tube Department, Harrison, N. J.

(Continued on page 56A)
The versatility of Taylor Laminated Plastics makes possible the fabrication of parts with structural, mechanical, and electrical properties to fit almost any engineering problem involving the mass-production of small, accurately-sized parts.

The three parts illustrated above, for example, selected at random from thousands of such parts being turned out daily in the modern Taylor plant, involve two different types of Phenol Fibre and one of Vulcanized Fibre. No. 1 is a switch back machined from Phenol Fibre and having excellent moisture-resistance and electrical properties. No. 2 is an end lamina for a fractional horsepower motor, punched and formed from Vulcanized Fibre. No. 3 is a coil bar support for a secret electronic device which is sawed, milled, and drilled from Phenol Fibre having especially good insulating qualities and mechanical strength.

If your production problem involves great quantities of parts with light weight, great strength, and special insulating or dielectric qualities, let our engineers tell you what Taylor can do for you.

**Write us TODAY!**

**TAYLOR LAMINATED PLASTICS**

**LAMINATED PLASTICS:** PHENOL FIBRE • VULCANIZED FIBRE • Sheets, Rods, Tubes, and Fabricated Parts

**NORRISTOWN, PENNSYLVANIA • OFFICES IN PRINCIPAL CITIES • PACIFIC COAST PLANT: LA VERNE, CALIFORNIA**

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**News—New Products**

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 55A)

**H & K Frequency-Shift Receiver Terminal**

The Type A-4601 Dual-Diversity Receiver Terminal has been added to the line of frequency-shift equipment now being produced by the Communications Equipment Division of Heintz & Kaufman, Ltd., 50 Drumm St., San Francisco, Calif.

This unit accepts a frequency-shifted signal from two communications receivers and converts it either to tone, neutral, or polar d.c. keyed in accordance with telegraphic intelligence. The recording device may be radiotype, teletype, or a high-speed telegraph tape recorder.

A crystal oscillator and b.f.o. unit provides stable high-frequency and beat-frequency injection voltages to both receivers. The audio response from each receiver is thus identical in frequency.

The input filters have a range of 1850 to 3250 cycles. The response is down 70 db at 1700 cycles, and 60 db at 3400 cycles. A frequency shift between 600 and 900 cycles may be used.

The A-4601 permits an improvement of 11 db in signal-to-noise ratio over make-break systems by virtue of using frequency shift alone, according to the manufacturer. Further gains are obtained under circuit conditions where noise and atmospherics are high. The gain of the H & K dual-diversity system over a single-channel make-break system approaches 22 db. Another advantage of the frequency-shift system is that it makes high-speed keying possible with no loss of selectivity.

The complete terminal is mounted in two relay racks each measuring 6 feet by 19 inches. It is designed for 110-125-volt operation, 60 cycles, and has a power requirement of approximately 150 watts.

**Interesting Abstract**

• • • The Electronic Engineering Co. of California has recently been organized by Burgess Dempster and R. B. Bonney with Headquarters at 2008 West Seventh St., Los Angeles 5, Calif. They are doing general electronic consulting and are also available to represent eastern firms who require technical representation in California. Mr. Dempster was formerly with the Magnavox Company and the Crosley Corp., and Mr. Bonney was previously with R. C. A. and Crosley Corp.

(Continued on page 57A)
New Geiger-Mueller Counter

A new Geiger-Mueller counter, Model D11, has been announced by Instrument Development Laboratories, 223 West Erie St., Chicago 10, Ill. This new counter was designed for use with recording instruments, and is all glass with a window thickness of 25 milligrams per square centimeter. Over-all dimensions of the counter are 8 x 4 inches, with an active length of 3 inches. Cathode material may be specified as copper or silver, and the central wire is made of 0.004-inch polished tungsten.

Interference Filters

A new series of heavy-duty radio-interference filters for wiring screens, screened rooms, and industrial equipment is now available from Solar Manufacturing Corp., 1445 Hudson Blvd., North Bergen, N. J.

Type EB series Elim-O-Stat filters are furnished in standard Underwriters'-approved heavy cadmium-plated-steel surface cabinets. Type EB filter assemblies have a noise elimination range of from 150 kc to 250 Mc., covering all frequencies used for radio communication and entertainment, as well as commercial television.

Descriptive literature is available upon letterhead request.

(Continued on page 58A)

NOTICE

Information for our News and New Products section is warmly welcomed. News releases should be addressed to Mrs. Harriet P. Watkins, Industry Research Division, Proceedings of I.R.E., Room 707, 303 West 42nd St., New York 18, N. Y. Photographs, and electromagnets if not over 2' wide, are helpful. Stories should pertain to products of interest specifically to radio engineers.
**News—New Products**

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 57 A)

**New Voltmeter**

A recent addition to the line of measurement instruments manufactured by the Electronic Measurements Corp., 423 Broome St., New York, N. Y., is the Model 120 Voltmeter illustrated below.

The manufacturer claims that this model gives wide resistance range (0.2 ohm to 300 megohms) and high a.c. voltage sensitivity (10,000 ohms per volt).

Other features include an a.c.-voltage frequency range of 30 cycles to 1 Mc; special precision voltage multipliers, accurate to 1 per cent; and a rectifier battery replaceable without soldering iron. No external source of power is required for a.c. voltage measurements.

**Miniature Precision Resistors**

The Shallcross Manufacturing Co., of Collingdale, Pa., has announced four new small-size Akra-Ohm precision resistors which afford interesting possibilities for designers of miniature equipment where the need is for small, close-tolerance units. Type 136, the smallest Akra-Ohm resistor yet produced by this manufacturer, has a maximum wattage rating of 0.25 and is only 1 5/32 inches long by 3/8 inch in diameter. Maximum resistance of this unit is 150,000 ohms. Standard tolerance is 1 per cent although closer tolerances can be furnished on special order, as can special impregnation for operation under highly humid conditions.

Types 137, 133, and 134 are 2-, 3-, and 4-section units with 3, 4, and 5 leads respectively and with 0.25 watts maximum load per section. Maximum resistance of 550,000 ohms is available in Type 133.

We will be grateful if you will mention PROCEEDINGS of the I.R.E. when writing to our advertisers.

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**... and now the NEW Precision**

**Electronamic Test Master**

**SERIES 10-20**

Combination Tube PERFORMANCE Tester, Battery Tester and 34 range AC-DC Circuit Tester


*A tube tested for just one characteristic does not necessarily reveal overall performance capabilities. In the Precision Electronamic Tube Tester, the tube is electro-dynamically swept over a complete Path of Operation, on a sinusoidal time base which is automatically integrated by the meter in direct terms of Replace-Weak-Good.

Affords highest practical order of obsolescence insurance thru use of the Precision 12 station Master Lever Element Selector System.

**THE SERIES 10-20 TEST MASTER**

is particularly engineered for general-purpose industrial and electronic maintenance, service and installation. Tests all modern standard receiving and low power transmitting tubes; including facilities up to twelve individual element prongs; dual-capped H.F. amplifiers, 5 & 7 pin ecm types, Novel 7 pin tubes, etc.

**CIRCUIT TESTING FEATURES**

34 self-contained ranges, to 3000 volts, 10 megohms; 12 amperes, +600. +400 microamperes, 4% meter • All standard functions at only two L.P. jacks • Push-button range selection.

**MODEL 10-20-P** in portable hardwood case (Illustrated) $109.10

Also available in counter and panel mount models. All models include test leads and ohmmeter batteries.

"Precision" Master Electronamic Test Instruments are on display at all leading radio equipment distributors. Write for the Precision 1948 catalog fully describing the Electronamic Tube performance testing circuit.

**PRECISION APPARATUS CO., Inc.**

92-27 Horace Harding Blvd.
Elmhurst 12, N. Y.

Export Division: 458 Broadway, N.Y. C., U.S.A.
Cables: MORHANEX
News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

Pulse Generator

A new instrument, designated as Model 471 Pulse Generator, is now being manufactured by The Electrodyne Co., 899 Boylston St., Boston 15, Mass.

The output consists of rectangular-shaped voltage pulses, and the pulse is internally triggered for continuous operation from ½ to 1000 c.p.s. Provision is made for the use of an external triggering device which can be the type 208 oscilloscope or any source of positive pulses of at least 20 volts. There is also a position provided for generating a single pulse every time the switch is depressed.

Continuously variable pulse duration is available from 25 to 950 microseconds. The maximum output obtainable into a 10,000 ohm load is 50 volts, and 5- and 1-volt ranges are provided. The output impedance of the 50-volt range is approximately 1500 ohms. Remaining relatively constant regardless of output-control setting. Approximate output impedances of the 5-volt and 1-volt ranges are 250 and 50 ohms respectively.

A three-step range switch and a single fine control provide ample spread adjustment for each of the pulse-frequency, pulse-duration, and amplitude ranges. Accuracy of each range is ±2 per cent of maximum value.

Cueing Attenuators

New and improved cueing attenuators have been designed by the Shallcross Manufacturing Co., Collingdale, Pa.

These new units, which feature a special switching mechanism to transfer attenuator input to a pair of separate output terminals for cueing purposes, facilitate program switching and fading-in "on cue" without any increase in the diameter of the attenuator.

Any standard Shallcross ladder, bridged T, straight T, or potentiometer may be equipped for cueing action, including units as small as 1½ inch in diameter. All controls are available with mounting by means of a single-hole ⅜-inch-32-thread bushing or two 6-32 or 8-32 screws on 1-inch or ⅛-inch centers (except 1-inch diameter units).

(Continued on page 60A)
How Large Is a Big Coil?

We don't know, but we do know that from less than ½ inch in diameter on up to a 2-foot inductor like the larger one shown here, the organization of electronic specialists at Barker and Williamson is set to give your requirements prompt, intelligent attention.

Engineering and production facilities at B&W are ample to take care of a myriad of varying coil requirements — big or little, a few at a time or a production run!

Write Department PR 28 concerning your requirements.

BARKER & WILLIAMSON, INC.
237 Fairfield Ave., Upper Darby, Pa.

New Microphones in Crystal, Dynamic, and Carbon Types


Designed for complete adaptability, the "Century" is available in a choice of three generating elements: crystal, dynamic, or carbon. It can be used in any position, and mobile communication models are fitted with a hook for dash mounting. This new microphone is made of die-cast metal and finished in lustrous gray-brown. The dimensions are 3 x 2 x 1 inch.

An optional slide-to-talk shorting switch is available on all three types, and an optional slide-to-talk relay control switch and hang-up hook available on the dynamic and carbon types, all at slight extra cost. A new reeling Desk Stand Model 415 and other accessories are also available for use with the "Century." For complete information write to the manufacturer for Bulletin No. 137.

Radio Frequency Plate Chokes

Six new r.f. chokes have been developed by Ohmite Manufacturing Co., 4954, Flournoy St., Chicago, Ill., to cover the higher radio frequencies now in use by amateurs, police, communications facilities, and various other services. These new chokes are described in Bulletin 133 issued by the manufacturer.

Recent Catalogs

- • • • On Model 61, direct reading v.h.f.-u.h.f. wattmeter, by Bird Electronic Corp., 1800 East 38th St., Cleveland 14, Ohio.
- • • • On rack-and-panel-type connectors for radio and instrument applications, Bulletin No. D.P.547, by Cannon Electric Development Co., 3209 Humboldt St., Los Angeles, Calif.
- • • • On electrical and scientific instruments developed by James G. Biddle Co., 1316 Arch St., Philadelphia 7, Pa., the Biddle Instrument News, published on an average of four times each year. Write to the manufacturer, Dept. B-46, if you wish to receive future issues.
- • • • On microwave equipment, a reference manual and catalog, by DeMornay-Budd, Inc., 475 Grand Concourse, New York 51, N. Y. Copies will be sent free to all legitimate individuals and firms in the electronic and allied fields if requests are sent to DeMornay-Budd on firm stationery.
- • • • On custom-built oscilloscope recorders, issued by The Electrodyne Co., 899 Boylston St., Boston 15, Mass. Request for free copy should be made to the manufacturer on business letterhead.
- • • • On resistors, an attractively illustrated file catalog issued by Instrument Resistors Co., 25 Amity St., Little Falls, N. J. If interested, also ask manufacturer for leaflets on two new units not listed in catalog, Type WLA (one watt) and Type WLAs/8 (one-half watt).
News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

New Voltbox A.C. Power Supplies

The illustration shows one of the new models recently announced by Superior Electric Co., 607 Laurel St., Bristol, Conn., as an addition to its line of power supplies. The two new units are designated as types UC1M and UC2M, and in appearance both are alike.

These new models offer features of lightness, pleasing appearance, and flexibility. Contained in the cast-aluminum case are a Powerstat variable transformer; an easily read voltmeter, accurate to 2 per cent; three output receptacles and a set of Superior binding posts; an “on-off” switch and “line-load” switch; renewable fuse; and a six-foot cord with plug.

For type UC1M the input is 115 volts, 50 to 63 cycles, one phase, and the output is 0–135 volts, 7.5 amperes; for type UC2M the input is 230 volts, 50 to 60 cycles, one phase, and the output is 0–270 volts, 3.0 amperes.

For users who already have a Superior Powerstat variable transformer type 116 or 216 in their possession, but require the features of the new Voltboxes, the Voltbase is available. For further information regarding these products and their uses, write to the manufacturer.

Tubular Capacitors

A complete line of phenolic-molded paper tubular capacitors, developed after four years of intensive research, has been announced by Sprague Electric Co., North Adams, Mass.

Features of the new units include the facts that they are highly heat- and moisture-resistant, are noninflammable, are conservatively rated for operation from -40°C to +85°C, and are mechanically rugged, according to the manufacturer.

Write to the Sprague Electric Co. for Bulletin 210 containing complete details on the new capacitors.

(Continued on page 62A)
NOW! SELF-CONTAINED, EXPERIMENTAL
SCHOOL & INDUSTRIAL LAB EQUIPMENT

Kepco Laboratory Multiple Power Supply Model 103, available separately.

Kepco Electronic Instruction Panel Model 104, available separately.

Now you can perform electronic experiments simply, easily with the Kepco Electronic Instruction Panel. Here is a teaching aid that graphically illustrates vacuum tube principles — enables all students to grasp fundamentals in the laboratory.

Extremely versatile, the Kepco Electronic Instruction panel covers a wide range of tubes, comes with a pocket of 23 keyed interchangeable circuit charts, 3 master charts and 12 blank key sheets for additional experiments. Panel contains 3 octal tube sockets, 18 binding posts. By placing a keyed circuit diagram on the panel and wiring the circuit, students determine tube and circuit characteristics.

For a basic electronic instructional aid that vastly simplifies the teacher’s task, it’s the Kepco Electronic Instruction Panel!

WRITE FOR FULL INFORMATION TODAY!

Kepco - LABORATORIES
142-45 Roosevelt Avenue
Flushing, New York

STANDARD SIGNAL GENERATOR Model 80
CARRIER FREQUENCY RANGE: 2 to 400 megacycles.
OUTPUT: 0.1 to 100,000 microvolts. 50 ohms output impedance.
MODULATION: A.M. 0 to 30% at 400 or 1000 cycles internal. Jack for external audio modulation.
Video modulation jack for connection of external pulse generator.
POWER SUPPLY: 117 volts, 50-60 cycles.
DIMENSIONS: Width 19”, Height 10½”, Depth 9½”.
WEIGHT: Approximately 35 lbs. Suitable connection cables and matching pads can be supplied on order.

News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 61A)

Model S-7 Frequency Meter

A frequency meter especially designed for measurements in the 72-76 and 152-162 Mc. band is announced by Browning Laboratories, Inc., 750 Main St., Winchester, Mass.

Designated as Model S-7, the new meter features accuracy in either band of 0.005 per cent, or 0.0025 per cent where minor precautions are taken, rendering measurements of control station and satellite transmitters possible in the above-mentioned bands. The meter is housed in a rugged steel cabinet and has an engraved aluminum panel. Finishes are black throughout. A whip antenna mounted at the side of the cabinet furnishes coupling to the transmitter and may be telescoped to form a convenient carrying handle. Charts supplied with the instrument show deviation from assigned frequency. This instrument is available in single or two specified frequencies in either or both bands. It operates from 117 volts a.c. or d.c. and consumes approximately 50 watts. The weight is 15 pounds and the dimensions are 13½ inches by 7½ inches by 6½ inches.

New Miniature Electron Tube

The Tube Department, Radio Corporation of America, Harrison, N. J., has announced availability of the RCA-6BH6 sharp-cutoff miniature pentode intended primarily for service in mobile equipment where heater-current drain is an important consideration, and in a.c.-d.c.a.m. and f.m. receivers. In the latter, it is especially useful as a limiter or as a driver for a ratio detector. Features of the 6BH6 are its high transconductance, its low grid-plate capacitance, and its 6-volt, 150-milliampere heater.
News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

Volt-Ohm-Mil-Ammeter

The Triplet Electrical Instrument Co., of Bluffton, Ohio, announce the availability of a new Combination Tube Tester—Volt-Ohm-Mil-Ammeter, designated as Model 3480.

This instrument was designed as a combination tester for conclusive tube testing and complete voltage, current and resistance analyses. The tube tester has a fully balanced, multipurpose test circuit for emission, short- and open-element tests. This unit tests all receiving-type tubes, gaseous rectifiers, resistor and ballast tube continuity, and pilot lamps. A speed-roll tube chart, conveniently located simplifies testing. The volt-ohm-mil-ammeter provides a.c.-d.c. voltage ranges 0 to 1200 at 10,000 ohms/volt for d.c. and 200 ohms/volt for a.c.; d.c. ma. 0 to 120; d.c. amp.: 0-12; ohms: 0-1000-100,000; megohms: 0-1-50; output: capacitor in series with a.c. volts.

(Continued on page 64A)
EVERY Pickering Cartridge which leaves our laboratory has been carefully tested for the following characteristics, the allowable limits for which are shown:

- **Frequency Response**: ±2 db, 40-10,000 cps
- **Waveform Distortion**: 1 per cent maximum
- **Output Level**: 70 millivolts, ±2 db
- **Tracking Pressure**: 15 grams max. at 40 and 10,000 cps

IN ADDITION, optical inspection of the stylus polish and shape, mechanical inspection of the moving parts, and electrical inspection of the pickup coil has been made on each unit.

REGULAR sampling tests reveal absolute stability, amazing ruggedness, and complete insensitivity to the effects of temperature and humidity.

NO OTHER PICKUP CAN QUITE MATCH THIS PERFORMANCE

Available with diamond or sapphire stylus from all principal distributors

---

**New Tube Type GL-5674**

A new "split-anode" electrometer tube, which the manufacturer claims will measure reliably current as low as a milliamp of a billionth of an amper, has been made available by the Tube Division, Electronics Dept., of General Electric Co., Schenectady, N. Y.

This new tube is expected to prove of value in nuclear, medical, and industrial research which involves the measurement of minute currents. It is a two-tubes-in-one device in which the electrodes (control grid and plate) are cut in two and connected so as to function as a pair. Measurement is then the differential response between the two halves of the tube. Since sporadic effects influence both parts alike, the difference between the two responses is independent of incidental fluctuations.

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**Recent Catalogs**

- On radio and electronic equipment, a new 48-page supplement to the regular catalog by Allied Radio Corp., 833 West Jackson Blvd., Chicago 7, Ill. The new supplement No. 114 as well as the regular master catalog No. 112 can be obtained from Allied Radio Corp.
- On their complete line of stock molded plastic knobs control handles, instrument knobs, etc., an illustrated catalog issued by Rogan Brothers, 2500 West Irving Park Blvd., Chicago 18, Ill.

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**News—New Products**

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 61A)
News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

Recent Catalogs

• • • On capacitors and radio noise filters, a complete new 1948 catalog is now available from Solar Capacitor Sales Corp., 1445 Hudson Blvd., North Bergen, N. J. Ask for Catalog SC-2.

• • • On a newly designed Tru-Sonic Model P-52FR Co-Spiral Speaker and other items in the Tru-Sonic line, by the Stephens Manufacturing Corp., 10416 National Blvd., Los Angeles 34, Calif. Write for Bulletin #109.

• • • On Model SC-9A Lead-Shielded Sample Changer and Preamplifier, by Tracerlab, Inc., 55 Oliver St., Boston, Mass. This equipment is fully described in issue number 7 of Tracerlog, which is available upon request to Tracerlab, Inc.

Type 116 Polar Recorder

The commercial availability of a polar recorder has been announced by Airborne Instruments Laboratory, Inc., 160 Old Country Road, Mineola, N. Y.

Originally designed to plot aircraft-antenna radiation patterns, this recorder charts voltage on either a linear or a logarithmic scale as radial distance against angular position. Identified as A.I.L. Type 116, the device will be custom built to each customer's specific requirements. Provision of a permanent ink record (readily reproducible), rapid writing speed coupled with low pen overshoot, and preciseness of angular positioning are the recorder's outstanding features. It appears to be readily adaptable to any measurement task recordable in terms of polar co-ordinates, and can be provided in either portable or rack-mounted form. Complete descriptive material is available from the Laboratory.

(Continued on page 66A)
**NEWS—NEW PRODUCTS**

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 654)

**New Postwar Bridge**

The postwar models of the Wheatstone bridges offered by Industrial Instruments, Inc., 17 Pollock Ave., Jersey City 5, N. J., are produced along the same sturdy lines as the previous models but are more conveniently operated. Distinctive bar knobs, used in the place of the former fluted round knobs, are easier to hold and manipulate. Also, the knobs are continuously rotatable.

**New Tubular Trimmer Design**

Types 531 and 532 Tubular trimmers which are announced by Erie Resistor Corp., 640 West 12 St., Erie, Pa., have low minimum capacitance, high ratio of tuning range, require very little space, and are economically priced. The capacity range is 1-8 μfd.; the power factor is 0.1 per cent of maximum; and rated voltage is 350 volts d.c. The dimensions are approximately 1-inch diameter by 1½-inch long at maximum capacitance. Capacitance is varied by changing position of plunger inside high-temperature thermoplastic di-electric tube. Absence of peaks and valleys in capacitance change curve and relative smoothness of capacitance change makes for accurate alignments of sets without over-shooting.

Trimmers are mounted by a standard cadmium-plated clip nut which is the ground terminal. Erie Type 531 is for panels 0.015 to 0.039 inch thick; Erie Type 532 is for panels 0.040 to 0.065 inch thick.

**Interesting Abstracts**

• • *International Instruments, Inc., New Haven, Conn., a new organization formed from the Instrument Division of the M B Manufacturing Company, of the same city, announces that the company is well established in the production of a specialized line of midget meters and allied equipment.*

• • *A new industry service, announced as the Resistor Analysis Council, by International Resistance Co., at 401 No. Broad St., Philadelphia, Pa., is being headed by Wm. H. Knowles, Jr. Interested engineers and designers may have the resistor requirements of their products analyzed by sending as much pertinent data as is available to the Resistor Analysis Council.*

• • • *The firm of Don C. Wallace and William H. Wallace is now fully established in new offices in the Bendix Bldg., 1206 Maple Ave., Los Angeles 15, Calif. As manufacturers' representatives, this firm will continue to represent eastern factories in the western territory.*

• • • *Continuing promotion of f.m. and television, Westinghouse Electric Corp., with headquarters at 306 Fouth Ave., Pittsburgh 30, Pa., plans to expand facilities of the Sunbury, Pa., plant to handle and control production of television receivers, according to an announcement made by Walter C. Evans, vice president.*

---

**Specify**

**MYCALEX**

**LOW LOSS INSULATION**

Where high mechanical and electrical specifications must be met.

**MYCALEX 410**

**(MOLDED MYCALEX)**

makes a positive seal with metals . . . resists arcing, moisture and high temperatures.

27 years of leadership in solving the most exciting high frequency insulating problems.

**MYCALEX CORPORATION OF AMERICA**

"Owners of 'MYCALEX' Patents"

Plant and General Offices: Clifton, N.J.

Executive Offices: 30 Rockefeller Plaza

New York 20, N.Y.

---

**New Microphone Models**

Two new floor-stand microphones designed by Shaeffer of Hollywood have been announced by Universal Microphone Co., Centinela at Warren Lane, Inglewood, Calif.

The Model ST-3 is a modern, three-legged stand designed with a low center of gravity for added stability, and with rubber cushioned feet to minimize floor noises and to absorb vibrations. Sturdily built to withstand abuse, its extended height is 72 inches and its closed height is 40 inches.

Model ST-R is the same as ST-3 except for a heavier, round base. Prompt delivery is promised on both models.
News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

1.6-Mc. Interval Timer Counter Chronograph

For applications which require an accurate time interval measurement, the new Model 450 Interval Timer manufactured by the Potter Instrument Co., Inc., 136-56 Roosevelt Ave., Flushing, N. Y., will measure intervals in steps of 0.625 microsecond. The instrument will register, directly, intervals up to 1 second. Longer periods can be recorded by using an external counter to record the number of times the cycle is repeated.

Model 450 is actuated by positive pulses which can be easily derived from detectors such as photoelectric equipment and closing contacts. The time base included in the instrument consists of a 1.6-Mc, crystal oscillator. The oscillator, electronic switch, and counter decades are made up as individual units which plug into the chassis. Indication is by means of neon indicator glow lamps.

(Continued on page 68A)

Program for Ladies

at the
1948 I.R.E.
National
Convention
4
FULL
Days of
Fun

See details in your Program Letter, and this issue.

Bring "The Wife"!

Your Most Complete Source of Supply for
RADIO and ELECTRONIC
EQUIPMENT • COMPONENTS • ACCESSORIES

No matter what your need — whether Tubes, Components, Test Equipment, Receivers, Transmitters, or Public Address, you can save time and SAVE MONEY by shopping "Newark" first! As one of the largest distributors of radio and electronic components in America, we've got what you want — IN STOCK!

You'll like dealing with "Newark" because —

• Our tremendous stocks of standard brand merchandise always on hand insure speedy shipment of your order.
• Our highly specialized and competent personnel will know what you're talking about.
• Our Special Order Department performs miracles in getting those hard-to-find items that nobody else has!

Two centrally located warehouses — New York and Chicago — at your service!

Designed for
YOUR APPLICATION

PANADAPTOR

Whether your application of spectrum analysis requires high resolution of signals closely adjacent in frequency or extra broad spectrum scanning, there is a standard model Panadaptor to simplify and speed up your job.

Standardized input frequencies enable operation with most receivers.

<table>
<thead>
<tr>
<th>MODEL SA-3 TYPES</th>
<th>MODEL SA-6 TYPES</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum Scanning Width</td>
<td>T-50 T-100 T-200 T-1000 T-1000 T-6000</td>
</tr>
<tr>
<td>50KC 100KC 200KC 1MC 1.6MC 6MC</td>
<td></td>
</tr>
<tr>
<td>Input Center Frequency</td>
<td>455KC 455KC 455KC 5.25KC 10.2KC 30MC</td>
</tr>
<tr>
<td>Resolution at Maximum Scanning Width</td>
<td>2.5KC 3.4KC 4.4KC 11KC 11KC 25KC</td>
</tr>
<tr>
<td>Resolution at 20% of Maximum Scanning Width</td>
<td>1.5KC 2.7KC 4KC 9KC 7.5KC 22KC</td>
</tr>
</tbody>
</table>

Investigate these APPLICATIONS OF PANADAPTOR

• Frequency Monitoring
• Oscillator performance analysis
• FM and AM studies

WRITE NOW for recommendations, detailed specifications, prices and delivery time.
D.C. Power Supplies

A new line of hermetically sealed high-voltage, low-current d.c. power supplies has been announced by the Condeenser Products Co., 1375 No. Branch St., Chicago 22, Ill.

The HiVolt PS-1 and PS-2 Supplies, both of which transform 118 volts a.c., 60 cycles, to 2,400 volts d.c., are now in production. The PS-1 is designed to charge Picotronic capacitors for use in electronic photoflash and spectrograph analysis equipment. The PS-2 is intended for use in radiation counters, oscilloscopes, and television receivers. The manufacturer states that HiVolt 4,000-volt and 10,000-volt supplies will be announced at an early date.

New Graphic Recorder

The Servo-Tek Products Co., 247 Crooks Ave., Clifton, N. J., has announced a new type of position recorder which is declared to be capable of recording almost any mechanical motion or position. It is known as the "Servograph," a graphic recorder utilizing a 10-inch circular chart with an inking pen which is motivated from a remote point by war-proven synchro, or self-synchronous motors.

It is claimed that accuracy is better than 1 per cent for 360-degree transmitter rotation. Models are available for operation from a source of 115 volts at a frequency of either 60 or 400 cycles. Full mechanical clock drives and synchronous 115-volt 60-cycle electric drives are available for chart speeds of 12 hours, 24 hours, or 7 days. Multiple recording may be obtained by the use of two pens for two independent simultaneous recordings.

Electron-Tube Socket

To meet the requirements of manufacturers of electronic equipment, the new molded-bakelite sockets, designated as No. 146-116, have been developed by the American Phenolic Corp., 1830 So. Fifty-fourth Ave., Chicago 50, Ill.

Signal Generator

The Triplet Electrical Instrument Co., Bluffton, Ohio, announces a new f.m.-a.m. signal generator, known as Model 3433, with frequency coverage from 100 kc. to 120 Mc. in 10 fundamental bands, plus an additional 50 Mc. from a fixed oscillator, giving fundamental coverage to 170 Mc.

This signal generator features constant deviation by using a fixed-frequency re-antennae-modulated oscillator; an output meter for measuring relative r.f. output; double-copper-plated steel shielding, greatly minimizing r.f. leakage; coaxial-cable output lead; ladder attenuator; high-r.f.-output voltage output jack; high a.f. output available; air trimmer capacitor and permeability-adjusted oscillator coils; voltage-regulated power supply; heterodyne detector; and external a.m. modulation.

The case measures 15 11/32 inches by 11 1/32 inches by 8 1/4 inches. Power Source: 115 volt, 50 to 60 cycles a.c.

The design of these sockets is based upon the electrical and structural requirements of all tube types requiring the RMA super-jumbo tube base, as well as industrial 411 and 412 tube bases which have the same pin arrangement but with smaller shell diameter. Socket contacts are of high-conductivity material and of a unique cloverleaf design presenting four lines of contact to the tube pin. Repeated tests are claimed to indicate a contact resistance of considerably less than 0.001 ohm may be expected at current levels as high as 25 amperes.
News—New Products

These manufacturers have invited PROCEEDINGS readers to write for literature and further technical information. Please mention your I.R.E. affiliation.

(Continued from page 68A)

KW Television Transmitter

Development of General Electric Television transmitters, Type TT-6-A and TT-6-B, with a 5-kw. visual transmitter and a 24-kw. aural transmitter for operation on television channels 1 through 13, has been announced by the Transmitter Division, Electronics Dept., General Electric Co., Electronics Park, Syracuse, N. Y.

Low-level plate modulation features the electrical design and affords advantages which include: low-power modulator; linear modulation characteristic; high percentage-modulation capability; stable grounded-grid linear amplifiers; elimination of vestigial-sideband filter unit.

Physically, both the high-band transmitter (TT-6-B) and the low-band transmitter (TT-6-A) are arranged in three adjacent cubicals and occupy a space 16 feet long, 3 feet deep and 7 feet high. The aural transmitter, which incorporates the phasitron modulator employed in all General Electric’s postwar f.m. broadcast transmitters, is contained in one cubical, with the visual transmitter occupying the other two cubicals.

P.M. Speakers

Correction

The type L-301 and L-401 speakers now being produced by the William J. Murdock Co., 158 Carter St., Chelsea 50, Mass., which were publicized on page 48-A of the December, 1947, issue of the PROCEEDINGS, should have been designated therein as permanent-magnet speakers.

Don’t be a Park Bench Sitter!

There are going to be plenty of rooms if you act fast on your reservations. See form in the invitation letter.

1948 I.R.E. National Convention
March 22-25, New York City
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Attention

Associate Members!

Many Associate Members can qualify for higher membership grades and should certainly do so. Members are urged to keep membership grades up in pace with their present development.

An Associate over 24 years of age who is occupied as a radio engineer or scientist, and is in this active practice three years may qualify for Member Grade.

An Associate who has taught college radio or allied subjects for three years may qualify.

Some may possibly qualify for Senior Grade. But transfers can be made only upon your application. For fuller details request transfer application-form in writing or by using the coupon below.

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New York 21, N.Y. 2-48

Please send me the Transfer Application Membership-Form.

Name ..................................
Address ................................
Place ..................................
State ..................................
P resent Grade .........................

PROCEEDINGS OF THE I.R.E. February, 1948
This seven-tower directional array was designed to protect several stations operating on the same frequency. Six towers are used during the night and the seventh, with two night pattern towers, give excellent daytime coverage. Due to the location it was necessary to place gravel fills through the ice to a depth of over 30 ft. before pile foundations could be driven to solid ground. Towers are Blaw-Knox Type CN, base insulated 225 ft. high.

BLAW-KNOX DIVISION of Blaw-Knox Company
2037 FARMERS BANK BUILDING
PITTSBURGH 22, PA.
Not long ago, a radio beam flashed across the New York sky—and "carried" more than 7000 surgeons into an operating room...

Impossible? It was done by television, when RCA demonstrated—to a congress of surgeons—how effective this medium can be in teaching surgery.

In a New York hospital, above an operating table, a supersensitive RCA Image Orthicon television camera televised a series of operations. Lighting was normal. Images were transmitted on a narrow, line-of-sight beam... As the pictures were seen the operating surgeons were heard explaining their techniques...

The beam was picked up at a midtown hotel—carried to RCA Victor television receivers. And on the video screens, visiting surgeons followed each delicate step of surgical procedure. Action was sharp and clear. Each surgeon was as "close-up" as if he were actually beside the operating table.

Said a prominent surgeon: "Television as a way of teaching surgery surpasses anything we have ever had... I never imagined it could be so effective until I actually saw it..."

Use of television in many fields—and surgical education is only one—grows naturally from advanced scientific thinking at RCA Laboratories. Progressive research is part of every instrument bearing the names RCA or RCA Victor.

When in Radio City, New York, be sure to see the radio and electronic wonders at RCA Exhibition Hall, 36 West 49th St. Free admission. Radio Corporation of America, RCA Building, New York 20, N. Y.
C.D.'s new "Vikan" impregnated tubular capacitor—Type GT "Grey Tiger"—has won wide industry acclaim. "Remarkable durability"—the unanimous decision after many rigid laboratory tests. Write for samples today. Cornell-Dubilier Electric Corporation, Dept. M2, South Plainfield, New Jersey. Other plants in New Bedford, Worcester and Brookline, Massachusetts; and Providence, Rhode Island.

- new "Vikan" impregnation assures extra long life at high operating temperatures,
- new moisture seal and tube impregnation designed to withstand temperatures to 100°C,
- high insulation resistance: at 25°C. above 10,000 megohms per unit or 2,000 megohms per mfd.
- low power factor; averages .35% at 1,000 cycles,
- eliminates need for stocking high and low temperature units,
- excellent capacity stability over wide temperature range,
- excellent electrical stability over life of unit,
- available in all commercial capacity and voltage ratings for maximum flexibility,
- one line to meet all your production requirements—whether for high or low temperature and humidity applications.

"GREY TIGER" Capacitor and DC Voltage Ranges

<table>
<thead>
<tr>
<th>Capacity Mfd.</th>
<th>100 Volts</th>
<th>200 Volts</th>
<th>400 Volts</th>
<th>600 Volts</th>
<th>1,000 Volts</th>
<th>1,400 Volts</th>
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</tr>
</tbody>
</table>

CORNELL-DUBILIER ELECTRIC CORPORATION, Department M2
SOUTH PLAINFIELD, NEW JERSEY

GENTLEMEN: Please send Bulletin Number NB116 describing type GT tubulars. Catalog Number 195A. 

Name: ___________________________ Title: ___________________________
Firm: ___________________________ Address: ___________________________
for

Smooth VOLTAGE CONTROL

- THE VARIAC* — the original continuously-adjustable autotransformer — is the ideal device for controlling any a-c operated equipment. VARIACS not only supply perfectly stepless control of voltage from zero, but also supply output voltages 17% above line voltage. VARIACS are correctly designed for many years of trouble-free operation. Data below are for single-phase operation. Polyphase assemblies are available.

SINGLE-PHASE DATA

<table>
<thead>
<tr>
<th>LINE VOLTAGE</th>
<th>RATED AMPS.</th>
<th>MAX. AMPS.</th>
<th>OUTPUT VOLTAGE</th>
<th>KVA</th>
<th>CASE</th>
<th>TYPE</th>
<th>PRICE</th>
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<tbody>
<tr>
<td>115</td>
<td>1</td>
<td>1.5</td>
<td>0-115</td>
<td>.170</td>
<td>(1)</td>
<td>200-B</td>
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<td>115</td>
<td>5</td>
<td>7.5</td>
<td>0-115</td>
<td>.862</td>
<td>(2)</td>
<td>V-5</td>
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<td>2.3</td>
<td>(3)</td>
<td>V-20M</td>
<td>55.00</td>
</tr>
</tbody>
</table>

*The trade name VARIAC is registered at the U. S. Patent Office. VARIACS are patented under U. S. Patent No. 2,009,013 and are manufactured and sold only by General Radio Company or its authorized agents.

(1) Unmounted model.
(2) Protective case around windings.
(3) Protective case, terminal cover, line switch, convenience outlet and 6-foot line cord.
(4) Protective case, terminal cover and BX outlet.
(5) Two gang assembly — requires type 50-P1 Choke — $10.00

GENERAL RADIO COMPANY

Cambridge 39, Massachusetts

90 West St., New York 6
920 S. Michigan Ave., Chicago 5
950 N. Highland Ave., Los Angeles 38