

**MASTER HANDBOOK  
OF  
ELECTRONIC  
TABLES & FORMULAS**

**3rd Edition**

**BY MARTIN CLIFFORD**



17750



**MASTER HANDBOOK OF  
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FORMULAS** -3rd Edition

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To Kenneth, Paul, and Jerrold

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BY MARTIN CLIFFORD

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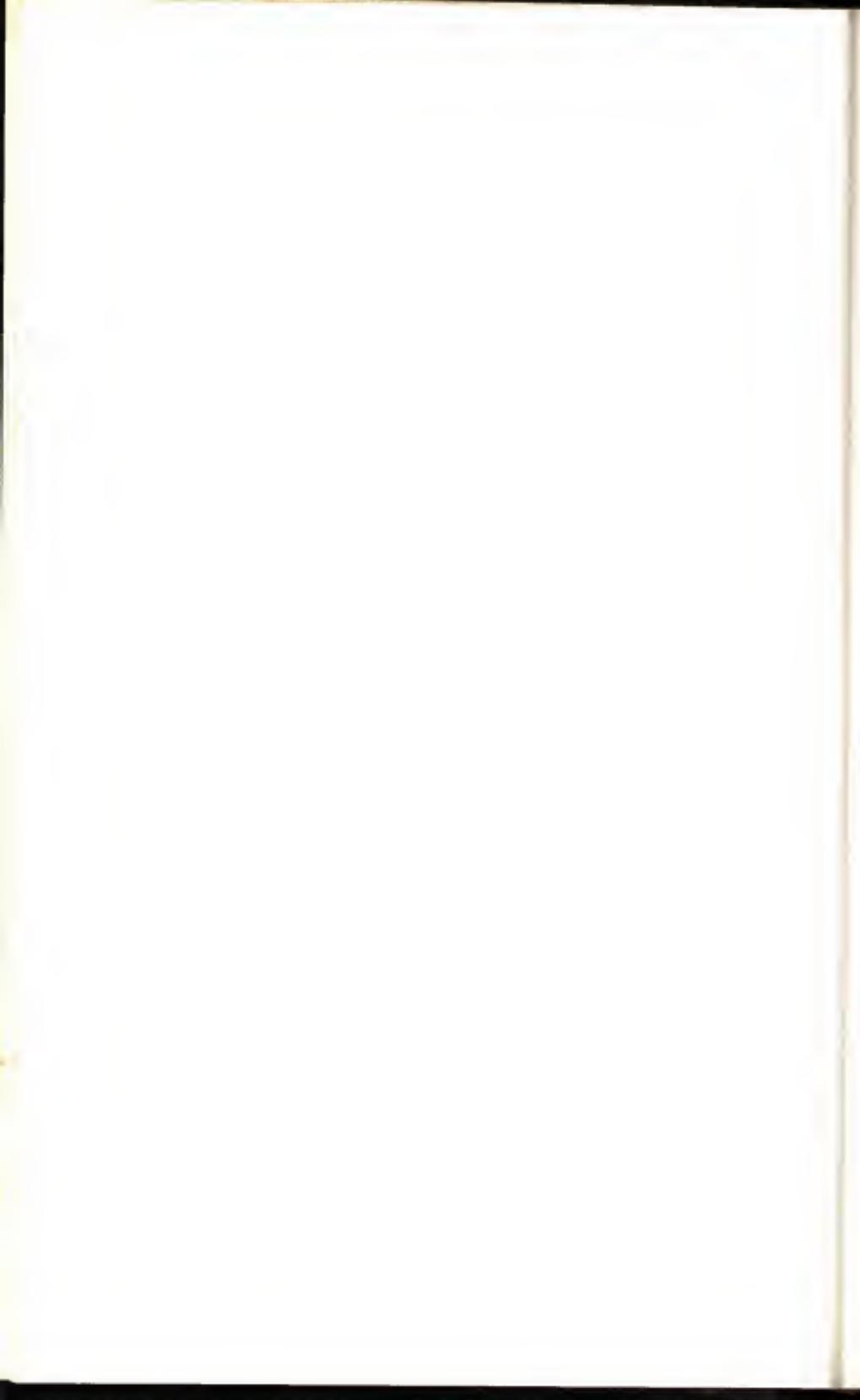
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## **Introduction**

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Problems in electronics can be solved in a number of ways. Possibly the most common method is to use a formula and to plug in or substitute numerical values. This technique calls for some arithmetic dexterity, and, quite often, a good working knowledge of algebraic and trigonometric functions, and sometimes a bit of calculus. Aside from the work involved, the use of a formula has the disadvantage in that it supplies a single solution.

This disadvantage is overcome by the use of nomographs. A nomograph not only gives the desired solution to a problem, but also supplies the user with a fairly good number of alternate possibilities. Thus, nomographs are well-suited for the designer who is not only interested in the solution to a problem, but is confronted with the need for specifying practical and easily-obtained components. The ideal solution to a problem is not always the most practical one.

This book represents still another way of solving electronics problems. It consists of electronics data arranged in tabular form. In a few instances some arithmetic may be needed, but for the most part, if the elements of a problem are known, the answer is supplied immediately by a table.

The tables in this book are based on formulas commonly used in electronics. Many of the tables supply answers with a much higher order of accuracy than is generally needed in the solution of problems in electronics. Also, as in the case of nomographs, the tables supply a number of possible solutions, allowing the user a

choice of practical component values that may be needed for a circuit.

There is a limit to the number of electronics tables that can be prepared. Tables are easily developed when only two variables are involved. Thus, it is simple enough to set up a table for capacitors in series or for resistance vs conductance. For involved formulas it is better to use the formulas directly, or to use nomographs if these are available.

What is the purpose of having a book of tables? Its function is to save time and work. Actually, there is no single best method for problem solving. Those who must solve problems in electronics as part of their educational training or work will find it helpful to be able to have a variety of techniques at their command—solving problems by formulas, solving problems by nomographs, by using a calculator and, with the help of this book, solving problems by tables.

I wish to thank the Digital Equipment Corporation, Maynard, Massachusetts for their kind permission to use their "Powers of Two" table. My thanks also go to my friend Marcus G. Scroggie and to Iliffe Books Ltd. for granting permission to use the "Decibel" table that originally appeared in his *Radio Laboratory Handbook*, and to Dr. Bernhard Fischer and the Macmillan Company for the use of their "Vector Conversion" table.

Martin Clifford

# Chapter 1

## Resistance and Conductance

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### EQUIVALENT RESISTANCE—RESISTORS IN PARALLEL

Whenever two resistors are connected in parallel, the total value of the shunt combination must always be less than that of the value of the smaller unit. From a practical viewpoint, if one of the two parallel resistors has a value that is 10 or more times that of the other resistor, the equivalent value can be taken as being approximately equal to that of the smaller resistor. Use Table 1-1 to find the equivalent resistance of two resistors in parallel.

The tables shown on the following pages can also be used to find the equivalent resistance of three or more resistors in parallel if the problem is handled on a step-by-step basis. First, take any two of the resistors, and, using the Tables, find the equivalent resistance. Consider this equivalent resistance just as though it were a physical unit and combine its value with the remaining resistor, again using the Tables.

Sometimes a design problem involving resistors will yield a value that is not practical—not practical in the sense that a resistor having such a value will be unavailable. In this instance the tables can again be used to advantage. Simply locate the nearest value in the Tables and then move left to get the value of  $R_2$  and upward to get the value of  $R_1$ .  $R_1$  and  $R_2$  will be standard, available resistors, which can be connected in parallel to supply the required resistance.

#### □Example:

What is the equivalent resistance of two resistors in parallel, one having a value of 5.6 ohms and the other a value of 9.1 ohms?

Locate 5.6 at the left, in the column marked R2. Move across and locate the column headed by 9.1. The equivalent resistance is shown to be 3.467 ohms.

**□Example:**

What two resistors in parallel will give an equivalent value of 3 ohms?

The Table shows possible combinations. You could use 3.3 and 33 ohms, or 3.6 and 18 ohms, or 3.9 and 13 ohms.

**□Example:**

What is the equivalent shunt resistance of a 68-ohm resistor and a 27-ohm resistor in parallel?

Locate 6.8 ohms in R1 row. Move the decimal point one place to the right so that 6.8 becomes 68. Locate 2.7 ohms in the R2 column and consider it now as 27 ohms. These two values meet at

**Table 1-1. Equivalent Resistance of Two Resistors in Parallel.**

**R1**

R2	2.7	3.0	3.3	3.6	3.9	4.3	4.7	5.1
2.7	1.350	1.421	1.485	1.543	1.595	1.659	1.715	1.766
3.0	1.421	1.500	1.571	1.636	1.695	1.767	1.831	1.889
3.3	1.485	1.571	1.650	1.722	1.788	1.867	1.939	2.004
3.6	1.543	1.636	1.722	1.800	1.872	1.959	2.039	2.110
3.9	1.595	1.695	1.788	1.872	1.950	2.045	2.131	2.210
4.3	1.659	1.767	1.867	1.959	2.045	2.150	2.246	2.333
4.7	1.715	1.831	1.939	2.039	2.131	2.246	2.350	2.446
5.1	1.766	1.889	2.004	2.110	2.210	2.333	2.446	2.550
5.6	1.822	1.953	2.076	2.191	2.299	2.432	2.555	2.669
6.2	1.881	2.022	2.154	2.278	2.394	2.539	2.673	2.798
6.8	1.933	2.082	2.222	2.354	2.479	2.634	2.779	2.914
7.5	1.986	2.143	2.292	2.432	2.566	2.733	2.889	3.036
8.2	2.031	2.196	2.353	2.502	2.643	2.821	2.988	3.144
9.1	2.082	2.256	2.422	2.580	2.730	2.920	3.099	3.268
10	2.126	2.308	2.481	2.647	2.806	3.007	3.197	3.377
11	2.168	2.351	2.538	2.712	2.879	3.092	3.293	3.484
12	2.204	2.400	2.588	2.769	2.943	3.166	3.377	3.579
13	2.236	2.438	2.632	2.819	3.000	3.231	3.452	3.663
15	2.288	2.500	2.705	2.903	3.095	3.342	3.579	3.806
16	2.310	2.526	2.736	2.939	3.136	3.389	3.633	3.867

Table 1-1. Equivalent Resistance of Two Resistors in Parallel.

	R1							
R2	2.7	3.0	3.3	3.6	3.9	4.3	4.7	5.1
18	2.348	2.571	2.789	3.000	3.205	3.471	3.727	3.974
20	2.379	2.609	2.833	3.051	3.264	3.539	3.806	4.064
22	2.405	2.640	2.870	3.094	3.313	3.597	3.873	4.140
24	2.427	2.667	2.901	3.130	3.355	3.647	3.930	4.206
27	2.455	2.700	2.941	3.176	3.408	3.709	4.003	4.290
30	2.477	2.737	2.973	3.214	3.451	3.761	4.063	4.359
33	2.496	2.750	3.000	3.246	3.488	3.804	4.114	4.417
36	2.512	2.769	3.023	3.273	3.519	3.841	4.157	4.467
39	2.525	2.786	3.043	3.296	3.545	3.873	4.195	4.510
43	2.540	2.804	3.065	3.322	3.576	3.909	4.237	4.559
47	2.553	2.820	3.083	3.344	3.601	3.939	4.273	4.601
51	2.564	2.833	3.099	3.363	3.623	3.966	4.303	4.636
56	2.576	2.847	3.116	3.383	3.646	3.993	4.336	4.674
62	2.587	2.862	3.133	3.402	3.669	4.021	4.369	4.712
68	2.597	2.873	3.147	3.419	3.688	4.044	4.396	4.744
75	2.606	2.885	3.161	3.435	3.707	4.067	4.423	4.775
82	2.614	2.894	3.172	3.449	3.723	4.086	4.445	4.801
91	2.622	2.904	3.185	3.463	3.740	4.106	4.469	4.829
100	2.629	2.913	3.195	3.475	3.754	4.123	4.489	4.853
R2	5.6	6.2	6.8	7.5	8.2	9.1	10.	
2.7	1.822	1.881	1.933	1.986	2.031	2.082	2.126	
3.0	1.953	2.022	2.082	2.143	2.196	2.256	2.308	
3.3	2.076	2.154	2.222	2.292	2.353	2.422	2.481	
3.6	2.191	2.278	2.354	2.432	2.502	2.580	2.647	
3.9	2.299	2.394	2.479	2.566	2.643	2.730	2.806	
4.3	2.432	2.539	2.634	2.733	2.821	2.920	3.007	
4.7	2.555	2.673	2.779	2.889	2.988	3.099	3.197	
5.1	2.669	2.798	2.914	3.036	3.144	3.268	3.377	
5.6	2.800	2.942	3.071	3.206	3.328	3.467	3.590	
6.2	2.942	3.100	3.243	3.394	3.531	3.688	3.827	
6.8	3.071	3.243	3.400	3.566	3.717	3.892	4.048	
7.5	3.206	3.394	3.566	3.750	3.917	4.111	4.286	
8.2	3.328	3.531	3.717	3.917	4.100	4.313	4.505	
9.1	3.467	3.688	3.892	4.111	4.313	4.550	4.764	
10	3.590	3.827	4.048	4.286	4.505	4.764	5.000	

Table 1-1—Equivalent Resistance of Two Resistors in Parallel (cont'd)

	R1							
R2	5.6	6.2	6.8	7.5	8.2	9.1	10.	
11	3.711	3.965	4.202	4.459	4.698	4.980	5.238	
12	3.818	4.088	4.340	4.615	4.871	5.175	5.455	
13	3.914	4.198	4.465	4.756	5.028	5.353	5.652	
15	4.078	4.387	4.679	5.000	5.302	5.664	6.000	
16	4.148	4.468	4.772	5.106	5.421	5.801	6.154	
18	4.271	4.612	4.935	5.294	5.634	6.044	6.429	
20	4.375	4.733	5.075	5.455	5.816	6.254	6.667	
22	4.464	4.837	5.194	5.593	5.974	6.437	6.875	
24	4.541	4.927	5.299	5.714	6.112	6.598	7.059	
27	4.638	5.042	5.432	5.870	6.290	6.806	7.297	
30	4.719	5.138	5.543	6.000	6.440	6.982	7.500	
33	4.788	5.219	5.638	6.111	6.568	7.133	7.674	
36	4.846	5.289	5.720	6.207	6.679	7.264	7.826	
39	4.897	5.350	5.790	6.290	6.775	7.378	7.959	
43	4.955	5.419	5.871	6.386	6.887	7.511	8.113	
47	5.004	5.477	5.941	6.468	6.982	7.624	8.246	
51	5.046	5.528	6.000	6.538	7.064	7.722	8.361	
56	5.091	5.582	6.064	6.614	7.153	7.828	8.485	
62	5.136	5.636	6.128	6.691	7.242	7.935	8.611	
68	5.174	5.682	6.182	6.755	7.318	8.026	8.718	
75	5.211	5.727	6.235	6.818	7.392	8.115	8.824	
82	5.242	5.764	6.279	6.872	7.455	8.191	8.913	
91	5.275	5.805	6.327	6.929	7.522	8.273	9.010	
100	5.303	5.838	6.367	6.977	7.579	8.341	9.091	
R2	11	12	13	15	16	18	20	
2.7	2.168	2.204	2.236	2.288	2.310	2.348	2.379	
3.0	2.357	2.400	2.438	2.500	2.526	2.571	2.609	
3.3	2.538	2.588	2.632	2.705	2.736	2.789	2.833	
3.6	2.712	2.769	2.819	2.903	2.939	3.000	3.051	
3.9	2.879	2.943	3.000	3.095	3.136	3.205	3.264	
4.3	3.092	3.166	3.231	3.342	3.389	3.471	3.539	
4.7	3.293	3.377	3.452	3.579	3.633	3.727	3.806	
5.1	3.484	3.579	3.663	3.806	3.867	3.974	4.064	
5.6	3.711	3.818	3.914	4.078	4.148	4.271	4.375	
6.2	3.965	4.088	4.198	4.387	4.468	4.612	4.733	

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

R2	11	12	13	15	16	18	20
6.8	4.202	4.340	4.465	4.679	4.772	4.935	5.075
7.5	4.459	4.615	4.756	5.000	5.106	5.294	5.455
8.2	4.698	4.871	5.028	5.302	5.421	5.634	5.816
9.1	4.980	5.175	5.353	5.664	5.801	6.044	6.254
10	5.238	5.455	5.652	6.000	6.154	6.429	6.667
11	5.500	5.739	5.958	6.346	6.519	6.828	7.097
12	5.739	6.000	6.240	6.667	6.857	7.200	7.500
13	5.958	6.240	6.500	6.964	7.172	7.548	7.879
15	6.346	6.667	6.964	7.500	7.742	8.182	8.571
16	6.519	6.857	7.172	7.742	8.000	8.471	8.889
18	6.828	7.200	7.548	8.182	8.471	9.000	9.474
20	7.097	7.500	7.879	8.571	8.889	9.474	10.000
22	7.333	7.765	8.171	8.919	9.263	9.900	10.476
24	7.543	8.000	8.432	9.231	9.600	10.286	10.909
27	7.816	8.308	8.775	9.643	10.047	10.800	11.489
30	8.049	8.571	9.070	10.000	10.435	11.250	12.000
33	8.250	8.800	9.326	10.313	10.776	11.647	12.543
36	8.426	9.000	9.551	10.588	11.077	12.000	12.857
39	8.580	9.176	9.750	10.833	11.345	12.316	13.220
43	8.759	9.382	9.982	11.121	11.661	12.689	13.651
47	8.914	9.559	10.183	11.371	11.937	13.015	14.030
51	9.048	9.714	10.359	11.591	12.179	13.304	14.366
56	9.194	9.882	10.551	11.831	12.444	13.622	14.737
62	9.342	10.054	10.747	12.078	12.718	13.950	15.122
68	9.468	10.200	10.914	12.289	12.952	14.233	15.455
75	9.593	10.345	11.080	12.500	13.187	14.516	15.789
82	9.699	10.468	11.221	12.680	13.388	14.760	16.078
91	9.814	10.602	11.375	12.877	13.607	15.028	16.396
100	9.910	10.714	11.504	13.043	13.793	15.254	16.667

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

	R1								
R2	22	24	27	30	33	36	39	43	
2.7	2.405	2.427	2.455	2.477	2.496	2.512	2.525	2.540	
3.0	2.640	2.667	2.700	2.727	2.750	2.769	2.786	2.804	
3.3	2.870	2.901	2.941	2.973	3.000	3.023	3.043	3.065	
3.6	3.094	3.130	3.176	3.214	3.246	3.273	3.296	3.322	
3.9	3.313	3.355	3.408	3.451	3.488	3.519	3.545	3.576	
4.3	3.597	3.647	3.709	3.761	3.804	3.841	3.873	3.909	
4.7	3.873	3.930	4.003	4.063	4.114	4.157	4.195	4.237	
5.1	4.140	4.206	4.290	4.359	4.417	4.467	4.510	4.559	
5.6	4.464	4.541	4.638	4.719	4.788	4.846	4.897	4.955	
6.2	4.837	4.927	5.042	5.138	5.219	5.289	5.350	5.419	
6.8	5.194	5.299	5.432	5.543	5.638	5.720	5.790	5.871	
7.5	5.593	5.714	5.870	6.000	6.111	6.207	6.290	6.386	
8.2	5.974	6.112	6.290	6.440	6.568	6.679	6.775	6.887	
9.1	6.437	6.598	6.806	6.982	7.133	7.264	7.378	7.511	
10	6.875	7.059	7.297	7.500	7.674	7.826	7.959	8.113	
11	7.333	7.543	7.816	8.049	8.250	8.426	8.580	8.759	
12	7.765	8.000	8.308	8.571	8.800	9.000	9.176	9.382	
13	8.171	8.432	8.775	9.070	9.326	9.551	9.750	9.982	
15	8.919	9.231	9.643	10.000	10.313	10.588	10.833	11.121	
16	9.263	9.600	10.047	10.435	10.776	11.077	11.345	11.661	
18	9.900	10.286	10.800	11.250	11.647	12.000	12.316	12.689	
20	10.476	10.909	11.489	12.000	12.543	12.857	13.220	13.651	
22	11.000	11.478	12.122	12.692	13.200	13.655	14.066	14.554	
24	11.478	12.000	12.706	13.333	13.895	14.400	14.857	15.404	
27	12.122	12.706	13.500	14.211	14.850	15.429	15.955	16.586	
30	12.692	13.333	14.211	15.000	15.714	16.364	16.957	17.671	
33	13.200	13.895	14.850	15.714	16.500	17.217	17.875	18.671	
36	13.655	14.400	15.429	16.364	17.217	18.000	18.720	19.595	
39	14.066	14.857	15.955	16.957	17.875	18.720	19.500	20.451	
43	14.554	15.403	16.586	17.671	18.671	19.595	20.451	21.500	

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

	R1									
R2	22	24	27	30	33	36	39	43		
47	14.986	15.887	17.149	18.312	19.388	20.386	21.314	22.456		
51	15.370	16.320	17.654	18.889	20.036	21.103	22.100	23.330		
56	15.795	16.800	18.217	19.535	20.764	21.913	22.989	24.323		
62	16.238	17.302	18.809	20.217	21.537	22.776	23.941	25.390		
68	16.622	17.739	19.326	20.816	22.218	23.538	24.785	26.342		
75	17.010	18.182	19.853	21.423	22.917	24.324	25.658	27.331		
82	17.346	18.566	20.312	21.964	23.530	25.017	26.430	28.208		
91	17.717	18.991	20.822	22.562	24.218	25.795	27.300	29.201		
100	18.033	19.355	21.260	23.077	24.812	26.471	28.058	30.070		
R2	47	51	56	62	68	75	82	91	100	
2.7	2.553	2.564	2.576	2.587	2.597	2.606	2.614	2.622	2.629	
3.0	2.820	2.833	2.847	2.862	2.873	2.885	2.894	2.904	2.913	
3.3	3.083	3.099	3.116	3.133	3.147	3.161	3.172	3.185	3.195	
3.6	3.344	3.363	3.383	3.402	3.419	3.435	3.449	3.463	3.475	
3.9	3.601	3.623	3.646	3.669	3.688	3.707	3.723	3.740	3.754	
4.3	3.939	3.966	3.993	4.021	4.044	4.067	4.086	4.106	4.123	
4.7	4.273	4.303	4.336	4.369	4.396	4.423	4.445	4.469	4.489	
5.1	4.601	4.636	4.674	4.712	4.744	4.775	4.801	4.829	4.853	
5.6	5.004	5.046	5.091	5.136	5.174	5.211	5.242	5.275	5.303	
6.2	5.477	5.528	5.582	5.636	5.682	5.727	5.764	5.805	5.838	
6.8	5.941	6.000	6.064	6.128	6.182	6.235	6.279	6.327	6.367	
7.5	6.468	6.538	6.614	6.691	6.755	6.818	6.872	6.929	6.977	
8.2	6.982	7.064	7.153	7.242	7.318	7.392	7.455	7.522	7.579	
9.1	7.624	7.722	7.828	7.935	8.026	8.115	8.191	8.273	8.341	
10.0	8.246	8.361	8.485	8.611	8.718	8.824	8.913	9.010	9.091	
11	8.914	9.048	9.194	9.342	9.468	9.593	9.699	9.814	9.910	
12	9.559	9.714	9.882	10.054	10.200	10.345	10.468	10.602	10.714	
13	10.183	10.359	10.551	10.747	10.914	11.080	11.221	11.375	11.504	
15	11.371	11.591	11.831	12.078	12.289	12.500	12.680	12.877	13.043	
16	11.937	12.179	12.444	12.718	12.952	13.187	13.388	13.607	13.793	

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

R1										
R2	47	51	56	62	68	75	82	91	100	
18	13.015	13.304	13.622	13.950	14.233	14.516	14.760	15.028	15.254	
20	14.030	14.366	14.737	15.122	15.455	15.789	16.078	16.396	16.667	
22	14.986	15.370	15.795	16.238	16.622	17.010	17.346	17.717	18.033	
24	15.887	16.320	16.800	17.302	17.739	18.182	18.566	18.991	19.355	
27	17.149	17.654	18.217	18.809	19.326	19.853	20.312	20.822	21.260	
30	18.312	18.889	19.535	20.217	20.816	21.423	21.964	22.562	23.077	
33	19.388	20.036	20.764	21.537	22.218	22.917	23.530	24.218	24.812	
36	20.836	21.103	21.913	22.776	23.538	24.324	25.017	25.795	26.471	
39	21.314	22.100	22.989	23.941	24.785	25.658	26.430	27.300	28.058	
43	22.456	23.330	24.323	25.390	26.342	27.331	28.208	29.201	30.070	
47	23.500	24.459	25.553	26.734	27.791	28.893	29.876	30.993	31.973	
51	24.459	25.500	26.692	27.982	29.143	30.357	31.444	32.683	33.775	
56	25.553	26.692	28.000	29.424	30.710	32.061	33.275	34.667	35.897	
62	26.734	27.982	29.424	31.000	32.431	33.942	35.306	36.876	38.272	
68	27.791	29.143	30.710	32.431	34.000	35.664	37.173	38.918	40.476	
75	28.893	30.357	32.061	33.942	35.664	37.500	39.172	41.114	42.857	
82	29.876	31.444	33.275	35.306	37.173	39.172	41.000	43.133	45.055	
91	30.993	32.683	34.667	36.876	38.918	41.114	43.133	45.500	47.644	
100	31.973	33.775	35.897	38.272	40.476	42.857	45.055	47.644	50.000	
R2	10	11	12	13	15	16	18	20	22	
100	9.091	9.910	10.714	11.504	13.043	13.793	15.254	16.667	18.033	
110	9.167	10.000	10.820	11.626	13.200	13.968	15.469	16.923	18.333	
120	9.231	10.076	10.909	11.729	13.333	14.118	15.652	17.143	18.592	
130	9.286	10.142	10.986	11.818	13.448	14.247	15.811	17.333	18.816	
150	9.375	10.248	11.111	11.963	13.636	14.458	16.071	17.647	19.186	
160	9.412	10.292	11.163	12.023	13.714	14.545	16.180	17.778	19.341	
180	9.474	10.366	11.250	12.124	13.846	14.694	16.364	18.000	19.604	
200	9.524	10.427	11.321	12.207	13.953	14.815	16.514	18.182	19.820	
220	9.565	10.476	11.380	12.275	14.043	14.915	16.639	18.333	20.000	
240	9.600	10.518	11.423	12.332	14.118	15.000	16.744	18.462	20.153	

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

	R1									
R2	10	11	12	13	15	16	18	20	22	
270	9.643	10.569	11.489	12.403	14.211	15.105	16.875	18.621	20.342	
300	9.677	10.611	11.538	12.460	14.286	15.190	16.981	18.750	20.497	
330	9.706	10.645	11.579	12.507	14.348	15.260	17.069	18.857	20.625	
360	9.730	10.674	11.613	12.547	14.400	15.319	17.143	18.947	20.733	
390	9.750	10.698	11.642	12.581	14.444	15.369	17.206	19.024	20.825	
430	9.773	10.726	11.674	12.619	14.494	15.426	17.277	19.111	20.929	
470	9.792	10.748	11.701	12.650	14.536	15.473	17.336	19.184	21.016	
510	9.808	10.768	11.724	12.677	14.571	15.513	17.386	19.245	21.090	
560	9.825	10.788	11.748	12.705	14.609	15.556	17.439	19.310	21.168	
620	9.841	10.808	11.772	12.733	14.646	15.597	17.492	19.375	21.246	
680	9.855	10.825	11.792	12.756	14.676	15.632	17.536	19.429	21.311	
750	9.868	10.841	11.811	12.779	14.706	15.666	17.578	19.481	21.373	
820	9.880	10.854	11.827	12.797	14.731	15.694	17.613	19.524	21.425	
910	9.891	10.869	11.844	12.817	14.757	15.724	17.651	19.570	21.481	
1000	9.901	10.880	11.858	12.833	14.778	15.748	17.682	19.608	21.526	
R2	24	27	30	33	36	39	43	47	51	
100	19.355	21.260	23.077	24.812	26.471	28.058	30.070	31.973	33.775	
110	19.701	21.679	23.571	25.385	27.123	28.792	30.915	32.930	34.845	
120	20.000	22.041	24.000	25.882	27.692	29.434	31.656	33.772	35.789	
130	20.260	22.357	24.375	26.319	28.193	30.000	32.312	34.520	36.630	
150	20.690	22.881	25.000	27.049	29.032	30.952	33.420	35.787	38.060	
160	20.870	23.102	25.263	27.358	29.388	31.357	33.892	36.329	38.673	
180	21.176	23.478	25.714	27.887	30.000	32.055	34.709	37.269	39.740	
200	21.429	23.789	26.087	28.326	30.508	32.636	35.391	38.057	40.637	
220	21.639	24.049	26.400	28.696	30.938	33.127	35.970	38.727	41.402	
240	21.818	24.270	26.667	29.011	31.304	33.548	36.466	39.303	42.062	
270	22.041	24.545	27.000	29.406	31.765	34.078	37.093	40.032	42.897	
300	22.222	24.771	27.273	29.730	32.143	34.513	37.609	40.634	43.590	
330	22.373	24.958	27.500	30.000	32.459	34.878	38.043	41.141	44.173	
360	22.500	25.116	27.692	30.229	32.727	35.188	38.412	41.572	44.672	
390	22.609	25.252	27.857	30.426	32.958	35.455	38.730	41.945	45.102	

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

	R1									
R2	24	27	30	33	36	39	43	47	51	
430	22.731	25.405	28.043	30.648	33.219	35.757	39.091	42.369	45.593	
470	22.834	25.533	28.200	30.835	33.439	36.012	39.396	42.727	46.008	
510	22.921	25.642	28.333	30.994	33.626	36.230	39.656	43.034	46.364	
560	23.014	25.758	28.475	31.164	33.826	36.461	39.934	43.361	46.743	
620	23.106	25.873	28.615	31.332	34.024	36.692	40.211	43.688	47.124	
680	23.182	25.969	28.732	31.473	34.190	36.885	40.443	43.961	47.442	
750	23.256	26.062	28.846	31.609	34.351	37.072	40.668	44.228	47.753	
820	23.318	26.139	28.941	31.723	34.486	37.229	40.857	44.452	48.014	
910	23.383	26.222	29.043	31.845	34.630	37.397	41.060	44.692	48.293	
1000	23.438	26.290	29.126	31.946	34.749	37.536	41.227	44.890	48.525	
R2	56	62	68	75	82	91	100			
100	35.897	38.272	40.476	42.857	45.055	47.644	50.000			
110	37.108	39.651	42.022	44.595	46.979	49.801	52.381			
120	38.182	40.879	43.404	46.154	48.713	51.754	55.545			
130	39.140	41.979	44.646	47.561	50.283	53.529	56.522			
150	40.777	43.868	46.789	50.000	53.017	56.639	60.000			
160	41.481	44.685	47.719	51.064	54.215	58.008	61.538			
180	42.712	46.116	49.355	52.941	56.336	60.443	64.286			
200	43.750	47.328	50.746	54.545	58.156	62.543	66.667			
220	44.638	48.369	51.944	55.932	59.735	64.373	68.750			
240	45.405	49.272	52.987	57.143	61.118	65.982	70.588			
270	46.380	50.422	54.320	58.696	62.898	68.061	72.973			
300	47.191	51.381	55.435	60.000	64.398	69.821	75.000			
330	47.876	52.194	56.382	61.111	65.680	71.330	76.744			
360	48.462	52.891	57.196	62.069	66.787	72.639	78.261			
390	48.969	53.496	57.904	62.903	67.754	73.784	79.592			
430	49.547	54.187	58.715	63.861	68.867	75.106	81.132			
470	50.038	54.774	59.405	64.679	69.819	76.239	82.456			
510	50.459	55.280	60.000	65.385	70.642	77.221	83.607			
560	50.909	55.820	60.637	66.142	71.526	78.280	84.848			
620	51.361	56.364	61.279	66.906	72.422	79.353	86.111			

Table 1-1. Equivalent Resistance of Two Resistors in Parallel (cont'd)

R2	56	62	68	75	82	91	100
R1							
680	51.739	56.819	61.818	67.550	73.176	80.259	87.179
750	52.109	57.266	62.347	68.182	73.918	81.153	88.235
820	52.420	57.642	62.793	68.715	74.545	81.910	89.130
910	52.754	58.045	63.272	69.289	75.222	82.727	90.099
1000	53.030	58.380	63.670	69.767	75.786	83.410	90.909

1.93 in the Table. However, this is now 19.3 ohms, since you must again move the decimal point one place to the right.

This problem can also be done directly, in two ways. Locate 68 in the R2 column and then move to the right to find the answer in the 27 column under the general heading of R1. Or, locate 27 in the R2 column and move to the right to find the answer in the 68 column under the general heading of R1.

The values shown in Table 1-1 are median values and do not take tolerances into consideration. Resistor tolerances are usually 10 percent or less, and may be plus or minus. However, Table 1 does supply a practical guide for the quick determination of two resistors in parallel, or for finding parallel resistor combinations which will be equivalent to a desired resistance value.

## RESISTANCE VS CONDUCTANCE

The opposition to the movement of an electrical current can be expressed in terms of resistance (measured in ohms) or in terms of conductance (expressed in siemens). It is often very convenient to be able to move back and forth quickly and easily between resistance and conductance in the solution of electronics problems. This can be readily done since resistance and conductance are reciprocals.

Sometimes, in working with resistances you will find that the values are such that they are not covered by the tables and that using a formula to solve the problem will involve some laborious arithmetic. In that case it may be easier and quicker to work with conductances. To find the total conductance of resistors in parallel simply consider them as conductors and add the values of the individual units. Thus, if you have a number of resistors in parallel, use Table 1-2 to find the equivalent conductance of each resistor. Add the conductances and then use the table once again to find the equivalent resistance.

The symbol for resistance is R; that used for conductance is G. The relationship between the two is expressed as R equals  $1/G$  or G equals  $1/R$ . If you are considering a complete circuit, that is, a circuit consisting of a number of resistors in parallel, then the total resistance of the circuit is the reciprocal of the total conductance.

Conductance can be substituted into the different forms of ohm's law. Thus, for resistance, we would have R equals  $E/I$ . For conductance we would have G equals  $I/E$ .

**□Example:**

What is the conductance of a resistor whose value, as measured, is 64 ohms?

Locate 64 in the column marked ohms. The value of conductance, as shown in the column (siemens) to the right, is 0.0156 siemen.

**□Example:**

What is the resistance of a component whose conductance is 0.0556 siemen.

The value of 0.0556, in the siemens column, corresponds to 18 ohms, as indicated in the ohms column.

**□Example:**

The values of four resistors, measured on a bridge, are 90 ohms, 83, 79, and 71 ohms, respectively. What is the equivalent resistance when these units are connected in parallel?

Using Table 1-2 you will find that the corresponding conductance values are 0.0111, 0.0120, 0.0127, and 0.0141 siemen, respectively. Adding these results in a total conductance of 0.0499 siemen. Using Table 1-2 once again, the closest conductance value is 0.0500 siemen, and, as shown by the table, corresponds to 20 ohms.

**Table 1-2. Resistance (Ohms) vs Conductance (Siemens).**

Ohms	Siemens	Ohms	Siemens	Ohms	Siemens
0.1	10.0000	1.0	1.0000	10	0.1000
0.2	5.0000	2	0.5000	11	0.0909
0.3	3.3333	3	0.3333	12	0.0833
0.4	2.5000	4	0.2500	13	0.0769
0.5	2.0000	5	0.2000	14	0.0714
0.6	1.6667	6	0.1667	15	0.0667
0.7	1.4286	7	0.1429	16	0.0625
0.8	1.2500	8	0.1250	17	0.0588
0.9	1.1111	9	0.1111	18	0.0556

Table 1-2. Resistance (Ohms) vs Conductance (Siemens).

Ohms	Siemens	Ohms	Siemens	Ohms	Siemens
19	0.0526	48	0.0208	74	0.0135
20	0.0500	49	0.0204	75	0.0133
21	0.0476	50	0.0200	76	0.0132
22	0.0455	51	0.0196	77	0.0130
23	0.0435	52	0.0192	78	0.0128
24	0.0417				
25	0.0400	53	0.0189	79	0.0127
26	0.0385	54	0.0185	80	0.0125
27	0.0370	55	0.0182	81	0.0123
28	0.0357	56	0.0179	82	0.0122
29	0.0345	57	0.0175	83	0.0120
30	0.0333				
31	0.0323	58	0.0172	84	0.0119
32	0.0313	59	0.0169	85	0.0118
33	0.0303	60	0.0167	86	0.0116
34	0.0294	61	0.0164	87	0.0115
35	0.0286	62	0.0161	88	0.0114
36	0.0278	63	0.0159		0.0112
37	0.0270			89	
38	0.0263	64	0.0156	90	0.0111
39	0.0256	65	0.0154	91	0.0110
40	0.0250	66	0.0152	92	0.0109
41	0.0244	67	0.0149	93	0.0108
42	0.0238	68	0.0147	94	0.0106
43	0.0233	69	0.0145	95	0.0105
44	0.0227	70	0.0143	96	0.0104
45	0.0222	71	0.0141	97	0.0103
46	0.0217	72	0.0139	98	0.0102
47	0.0213	73	0.0137	99	0.0101
				100	0.0100

### STANDARD EIA VALUES FOR COMPOSITION RESISTORS

Composition resistors are available in values based on the recommendations of the Electronics Industries Association (EIA). These values are shown in Table 1-3.

K means kilo, or multiply by 1000. 120 K equals  $120 \times 1000$ , or 120,000 ohms. Meg means multiply by 1,000,000. 1.8 Meg equals  $1.8 \times 1,000,000$ , or 1,800,000 ohms.

**Table 1-3. Standard EIA Values for Composition Resistors.**

Ohms	Ohms	Ohms	Ohms	Ohms	Ohms
2.7	39	560	8.2K	120K	1.8 Meg
3.0	43	620	9.1K	130K	2.0 Meg
3.3	47	680	10K	150K	2.2 Meg
3.6	51	750	11K	160K	2.4 Meg
3.9	56	820	12K	180K	2.7 Meg
4.3	62	910	13K	200K	3.0 Meg
4.7	68	1K	15K	220K	3.3 Meg
5.1	75	1.1K	16K	240K	3.6 Meg
5.6	82	1.2K	18K	270K	3.9 Meg
6.2	91	1.3K	20K	300K	4.3 Meg
6.8	100	1.5K	22K	330K	4.7 Meg
7.5	110	1.6K	24K	360K	5.1 Meg
8.2	120	1.8K	27K	390K	5.6 Meg
9.1	130	2K	30K	430K	6.2 Meg
10	150	2.2K	33K	470K	6.8 Meg
11	160	2.4K	36K	510K	7.5 Meg
12	180	2.7K	39K	560K	8.2 Meg
13	200	3K	43K	620K	9.1 Meg
15	220	3.3K	47K	680K	10 Meg
16	240	3.6K	51K	750K	11 Meg
18	270	3.9K	56K	820K	12 Meg
20	300	4.3K	62K	910K	13 Meg
22	330	4.7K	68K	1 Meg	15 Meg
24	360	5.1K	75K	1.1 Meg	16 Meg
27	390	5.6K	82K	1.2 Meg	18 Meg
30	430	6.2K	91K	1.3 Meg	20 Meg
33	470	6.8K	100K	1.5 Meg	22 Meg
36	510	7.5K	110K	1.6 Meg	.....

Table 1-4 shows conductance values for standard composition resistors. Column R indicates the resistance values in ohms; column G the corresponding conductance values in siemens. To find the conductance of any number of parallel resistors, add the conductances and then locate the nearest equivalent resistance value. Thus, 10-ohm, 18-ohm, and 30-ohm resistors in parallel have conductances of 0.1 siemen, 0.0556 siemen, and 0.03333 siemen.  $0.1 + 0.0556 + 0.03333 = 0.1889$  siemen. The nearest value in the

G column corresponding to 0.1889 siemen is 0.19608 siemen, equivalent to a standard resistance value of 5.1 ohms.

To find a more accurate value of resistance, divide the sum of the conductances into 1. Thus, 1 divided by 0.1889 equals 5.294 ohms. However, this is not a standard value. The closest standard value is 5.1 ohms.

**Table 1-4. Conductance of Standard EIA Values for Composition Resistors (Resistance, R, in Ohms; Conductance, G, in Siemens).**

R	G	R	G	R	G	R	G
2.7	0.37037	47	0.02128	820	0.001220	15K	0.000066
3.0	0.33333	51	0.01961	910	0.001100	16K	0.000062
3.3	0.30303	56	0.01786	1K	0.001000	18K	0.000055
3.6	0.27778	62	0.01613	1.1K	0.000909	20K	0.000050
3.9	0.25641	68	0.01471	1.2K	0.000833	22K	0.000045
4.3	0.23256	75	0.01333	1.3K	0.000769	24K	0.000041
4.7	0.21277	82	0.01220	1.5K	0.000666	27K	0.000037
5.1	0.19608	91	0.01099	1.6K	0.000625	30K	0.000033
5.6	0.17857	100	0.01000	1.8K	0.000555	33K	0.000030
6.2	0.16129	110	0.00909	2K	0.000500	36K	0.000027
6.8	0.14706	120	0.00833	2.2K	0.000454	39K	0.000025
7.5	0.13333	130	0.00769	2.4K	0.000416	43K	0.000023
8.2	0.12195	150	0.00667	2.7K	0.000370	47K	0.000021
9.1	0.10989	160	0.00625	3K	0.000333	51K	0.000019
10	0.10000	180	0.00556	3.3K	0.000303	56K	0.000017
11	0.09091	200	0.00500	3.6K	0.000277	62K	0.000016
12	0.08333	220	0.00455	3.9K	0.000256	68K	0.000014
13	0.07692	240	0.00417	4.3K	0.000232	75K	0.000013
15	0.06667	270	0.00370	4.7K	0.000212	82K	0.000012
16	0.06250	300	0.00333	5.1K	0.000196	91K	0.000011
18	0.05556	330	0.00303	5.6K	0.000178	100K	0.000010
20	0.05000	360	0.00278	6.2K	0.000161		
22	0.04545	390	0.00256	6.8K	0.000147		
24	0.04167	430	0.00233	7.5K	0.000133		
27	0.03704	470	0.00213	8.2K	0.000121		
30	0.03333	510	0.00196	9.1K	0.000109		
33	0.03030	560	0.00179	10K	0.000100		
36	0.02778	620	0.00161	11K	0.000090		
39	0.02564	680	0.00147	12K	0.000083		
43	0.02326	750	0.00133	13K	0.000077		

## CONDUCTANCE OF METALS

One of the distinguishing characteristics of metals is their ability to conduct electricity. As metals differ in hardness, ductility, density, tensile strength, malleability and melting point, they also differ in inherent conductance of electrical flow. See Table 1-5.

Table 1-5. Relative Conductance of Various Metals.

Substance	Relative conductance (Silver= 100%)
Silver.....	100
Copper.....	98
Gold.....	78
Aluminum.....	61
Tungsten.....	32
Zinc.....	30
Platinum.....	17
Iron.....	16
Lead.....	15
Tin.....	9
Nickel.....	7
Mercury.....	1
Carbon.....	0.05

## RESISTIVITIES OF CONDUCTORS

Yes, metals do conduct electricity, but some do it better than others. Table 1-6 shows how much resistance various conductors exhibit. Silver is the best electrical conductor and presents the least resistance to electrical flow. Although gold is the third best conductor, its rarity makes gold impractical to use as such. Consequently, gold has not been included in Table 1-6.

Table 1-6. Resistivities of Conductors.

Substance	Resistivities of Conductors at 0° C			Round Wires Ohms-Circular mils per foot
	Centimeter cube	Micromhs Inch cube		
Aluminum.....	3.21	1.26		19.3
Carbon.....	4000 to 10,000	1600 to 2800	24,00 to 42,000	
Constantan (Cu 60%, Ni 40%).....	49	19.3		295
Copper.....	1.72	0.68		10.4
Iron.....	12 to 14	4.7 to 5.5		72 to 84
Lead.....	20.8	8.2		125
Manganin (Cu 84%, Ni 4%, Mn 12%).....	43	16.9		258
Mercury.....	95.76	37.6		575
Nichrome (Ni 60%, Cr 12%, Fe 26%, Mn 2%).....	110	43		660
Platinum.....	11.0	4.3		66
Silver.....	1.65	0.65		9.9
Tungsten.....	5.5	2.15		33
Zinc.....	6.1	2.4		36.7

## OHM'S LAW FOR DC

Of all electronic formulas, Ohm's law is probably the best known and the most widely used. Basically set up as  $E = IR$ , it can be used to find an unknown value when the other two are known. It can also be used to determine the power being dissipated. The various arrangements of this law are shown in Table 1-7.

Table 1-7. Ohm's Law Formulas for DC.

Known Values	Formula for Finding Unknown Values of ...			
	I	R	E	P
I & R			$IR$	$I^2R$
I & E		$\frac{E}{I}$		$EI$
I & P		$\frac{P}{I^2}$	$\frac{P}{I}$	
R & E	$\frac{E}{R}$			$\frac{E^2}{R}$
R & P	$\sqrt{\frac{P}{R}}$		$\sqrt{PR}$	
E & P	$\frac{P}{E}$	$\frac{E^2}{P}$		

## Basic Units

The basic units in Ohm's law are the volt, ampere and ohm. Multiples and submultiples of these units are also used in the solution of problems. See Table 1-8.

Table 1-8. Units and Symbols.

Unit	Symbol	Multiple	Value
volt	E	kilovolt (kv)	1000 volts
volt	E	millivolt (mv)	1/1000 volt
volt	E	microvolt ( $\mu v$ )	1/1,000,000 volt
ohm	R	kilohm	1000 ohms
ohm	R	megohm	1,000,000 ohms
ampere	I	milliampere (ma)	1/1000 ampere
ampere	I	microampere ( $\mu a$ )	1/1,000,000 ampere

When large numbers are used in the solution of Ohm's law problems it is more convenient to use exponents. See Table 1-9.

**Table 1-9. Units in Exponential Notation.**

1 volt	= $10^3$ millivolts	= $10^6$ microvolts
1 millivolt	= $10^{-3}$ volt	= $10^3$ microvolts
1 microvolt	= $10^{-6}$ volt	= $10^{-3}$ millivolt
1 ohm	= $10^{-3}$ kilohm	= $10^{-6}$ megohm
1 kilohm	= $10^3$ ohms	= $10^{-3}$ megohm
1 megohm	= $10^6$ ohms	= $10^3$ kilohms
1 ampere	= $10^3$ milliamperes	= $10^6$ microamperes
1 millampere	= $10^{-3}$ ampere	= $10^3$ microamperes
1 microampere	= $10^{-6}$ ampere	= $10^{-3}$ milliamperes

## Power

The basic unit of power is the watt. Large whole numbers or decimals may be involved in the solution of power problems. Using exponents can make the work easier. Power formulas are valid only for linear resistors; that is, resistors which follow Ohm's law. See Table 1-10.

**Table 1-10. Symbols, Multiple and Exponential Values of DC Power.**

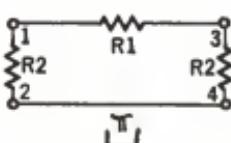
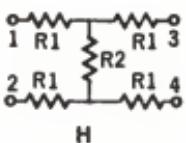
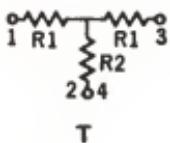
Unit	Symbol	Multiple	Value
watt	P	microwatt	$1/1,000,000$ watt
watt	P	milliwatt	$1/1000$ watt
watt	P	megawatt	$1,000,000$ watts

### In Terms of Exponents

1 watt	= $10^3$ milliwatts	= $10^6$ microwatts
1 milliwatt	= $10^{-3}$ watt	= $10^3$ microwatts
1 microwatt	= $10^{-6}$ watt	= $10^{-3}$ milliwatt

## FIXED ATTENUATORS

The insertion loss of a fixed attenuator network, or pad, is the ratio of the power input to power output, given in dB, and assuming equal impedances for the source and the load. Table 1-11 is for use where these impedances are the same. The values in the table are based on input and output impedances of 600 ohms. Figure 1-1 shows the types of pads for which Table 1-11 may be used.



**Fig. 1-1. Attenuator pads. Design values for these networks are given in Table 1-11.**

□ Example:

A simple pad is required to supply an insertion loss of 40 dB. How many resistors are needed and what is their value?

Table 1-11. Design Values for Attenuator Networks.

Loss, dB	T-PAD		H-PAD		Π PAD	
	R1	R2	R1	R2	R1	R2
0.1	3.58	50204	1.79	50204	7.20	100500
0.2	6.82	26280	3.41	26280	13.70	57380
0.3	10.32	17460	5.16	17460	20.55	34900
0.4	13.79	13068	6.90	13068	27.50	26100
0.5	17.20	10464	8.60	10464	34.40	20920
0.6	20.9	8640	10.45	8640	41.7	17230
0.7	24.2	7428	12.1	7428	48.5	14880
0.8	27.5	6540	13.75	6540	55.05	13100
0.9	31.02	5787	15.51	5787	62.3	11600
1.0	34.5	5208	17.25	5208	68.6	10440
2.0	68.8	2582	34.4	2582	139.4	5232
3.0	102.7	1703	51.3	1703	212.5	3505
4.0	135.8	1249	67.9	1249	287.5	2651
5.0	168.1	987.6	84.1	987.6	364.5	2141
6.0	199.3	803.4	99.7	803.4	447.5	1807
7.0	229.7	685.2	114.8	685.2	537.0	1569
8.0	258.4	567.6	129.2	567.6	634.2	1393
9.0	285.8	487.2	142.9	487.2	738.9	1260
10.0	312.0	421.6	156.0	421.6	854.1	1154
11.0	336.1	367.4	168.1	367.4	979.8	1071
12.0	359.1	321.7	179.5	321.7	1119	1002
13.0	380.5	282.8	190.3	282.8	1273	946.1
14.0	400.4	249.4	200.2	249.4	1443	899.1
15.0	418.8	220.4	209.4	220.4	1632	859.6
16.0	435.8	195.1	217.9	195.1	1847	826.0
17.0	451.5	172.9	225.7	172.9	2083	797.3
18.0	465.8	152.5	232.9	152.5	2344	772.8
19.0	479.0	136.4	239.5	136.4	2670	751.7
20.0	490.4	121.2	245.2	121.2	2970	733.3
22.0	511.7	95.9	255.9	95.9	3753	703.6
24.0	528.8	76.0	264.4	76.0	4737	680.8
26.0	542.7	60.3	271.4	60.3	5985	663.4
28.0	554.1	47.8	277.0	47.8	7550	649.7
30.0	563.0	37.99	281.6	37.99	9500	639.2
32.0	570.6	30.16	285.3	30.16	11930	630.9
34.0	576.5	23.95	288.3	23.95	15000	624.4
36.0	581.1	18.98	290.6	18.98	18960	619.3
38.0	585.1	15.11	292.5	15.11	23820	615.3
40.0	588.1	12.00	294.1	12.00	30000	612.1

Table 1-11. Design Values for Attenuator Networks

Loss, dB	R1	R2	R1	R2
0.1	3.60	100500	3.58	100500
0.2	6.85	57380	6.82	57380
0.3	10.28	34900	10.32	34900
0.4	13.80	26100	13.79	26100
0.5	17.20	20920	17.20	20920
0.6	20.85	17230	20.9	17230
0.7	24.25	14880	24.2	14880
0.8	27.53	13100	27.5	13100
0.9	31.2	11600	31.02	11600
1.0	34.3	10440	34.5	10440
2.0	69.7	5232	68.8	5232
3.0	106.2	3505	102.7	3505
4.0	143.8	2651	135.8	2651
5.0	182.3	2141	168.1	2141
6.0	223.8	1807	199.3	1807
7.0	268.5	1569	229.7	1569
8.0	317.1	1393	258.4	1393
9.0	369.4	1260	285.8	1260
10.0	427.0	1154	312.0	1154
11.0	489.9	1071	336.1	1071
12.0	559.5	1002	359.1	1002
13.0	636.3	946.1	380.5	946.1
14.0	721.5	899.1	400.4	899.1
15.0	816.0	859.6	418.8	859.6
16.0	923.2	826.0	435.8	826.0
17.0	1042	797.3	451.5	797.3
18.0	1172	772.8	465.8	772.8
19.0	1335	751.7	479.0	751.7
20.0	1485	733.3	490.4	733.3
22.0	1877	703.6	511.7	703.6
24.0	2369	680.8	528.8	680.8
26.0	2992	663.4	542.7	663.4
28.0	3775	649.7	554.1	649.7
30.0	4750	639.2	563.2	639.2
32.0	5967	630.9	570.6	630.9
34.0	7500	624.4	576.5	624.4
36.0	9480	619.3	581.1	619.3
38.0	11910	615.3	585.1	615.3
40.0	15000	612.1	588.1	612.1

Table 1-11. Design Values for Attenuator Networks

Loss, dB	R1	R2	R1	R2
0.1	7.2	50000	3.6	50000
0.2	13.8	26086	6.9	26086
0.3	21.0	17143	10.5	17143
0.4	28.2	12766	14.1	12766
0.5	35.4	10169	17.7	10169
0.6	43.2	8333	21.6	8333
0.7	50.4	7143	25.2	7143
0.8	57.6	6250	28.8	6250
0.9	65.4	5504	32.7	5504
1.0	73.2	4918	36.6	4918
2.0	155.4	2316	77.7	2316
3.0	247.8	1452	123.9	1452
4.0	351.0	1025	175.5	1025
5.0	466.8	771.2	233.4	771.2
6.0	597.0	603.0	298.5	603.0
7.0	743.4	484.3	371.7	484.3
8.0	907.2	396.8	453.6	396.8
9.0	1091	329.9	545.5	329.9
10.0	1297	277.5	648.5	277.5
11.0	1529	235.5	764.5	235.5
12.0	1788	201.3	894	201.3
13.0	2080	173.1	1040	173.1
14.0	2407	149.6	1204	149.6
15.0	2773	129.8	1387	129.8
16.0	3186	113.0	1598	113.0
17.0	3648	98.68	1824	98.68
18.0	4166	86.4	2083	86.4
19.0	4748	75.8	2374	75.8
20.0	5400	66.66	2700	66.66
22.0	6954	51.72	3477	51.72
24.0	8910	40.4	4455	40.4
26.0	11370	31.66	5685	31.66
28.0	14472	24.87	7236	24.87
30.0	18372	19.58	9186	19.58
32.0	23286	15.46	11643	15.46
34.0	29472	12.21	14736	12.21
36.0	37260	9.66	18630	9.66
38.0	47058	7.65	23529	7.65
40.0	59400	6.06	29700	6.06

A T-pad can be used to solve this problem. The circuit is a four-terminal network as shown in the corresponding circuit diagram. Locate 40 dB in the left-hand column of Table 11. To the right of this are the values for R<sub>1</sub> and R<sub>2</sub>. R<sub>1</sub> represents two resistors, each having a value of 588.1 ohms. R<sub>2</sub> is shown as 12 ohms. Note that a  $\pi$  pad could also be used to supply the same insertion loss, except that 30,000 ohms is needed for R<sub>1</sub> while R<sub>2</sub> consists of two resistors, each of which is 612.1 ohms. The nearest standard values can be selected from Table 1-3, or series and parallel combinations can be used to obtain the required resistance.

**Example:**

It is necessary to drop the output voltage of a 600-ohm source by 3 dB. What type of pad can do this, and what are the values of the resistors in the attenuator?

Find the number 3 in the column headed Loss, dB. As shown in Table 1-11, a number of different pads can be used to get the same result. For an H pad four resistors (R<sub>1</sub>) will be needed, each having a value of 51.3 ohms. A single resistor (R<sub>2</sub>) of 1703 ohms will complete the network.

## OHM'S LAW FOR AC

When Ohm's law is used for AC circuits containing reactive components the phase angle ( $\Theta$ ) between voltage and current becomes part of the calculations. Table 1-12 is a summary of Ohm's law formulas for AC.

Table 1-12. Power and Ohm's Law Formulas for AC.

Watts	Amperes	Volts	Impedance
$P =$	$I =$	$E =$	$Z =$
$I^2R$	$E/Z$	$IZ$	$E/I$
$EI \cos \theta$	$\frac{P}{E \cos \theta}$	$\frac{P}{I \cos \theta}$	$\frac{E^2 \cos \theta}{P}$
$\frac{E^2 \cos \theta}{Z}$	$\sqrt{\frac{P}{Z \cos \theta}}$	$\sqrt{\frac{PZ}{\cos \theta}}$	$\frac{P}{I^2 \cos \theta}$
$I^2Z \cos \theta$	$\sqrt{\frac{P}{R}}$	$\frac{\sqrt{PR}}{\cos \theta}$	$\frac{R}{\cos \theta}$

## CONDUCTANCE

Conductance, the reciprocal of resistance, can be considered as resistive siemens while susceptance is reactive siemens.

A wire (or any other component) can be either resistive or conductive. While the terms are reciprocals they are two different ways of describing the same thing. See Table 1-13.

Table 1-13. Resistance and Related Symbols

	<i>Symbol</i>		<i>Symbol</i>
Resistance	<i>R</i>	Conductance	<i>G</i>
Reactance	<i>X</i>	Susceptance	<i>B</i>
Impedance	<i>Z</i>	Admittance	<i>Y</i>



## **Chapter 2**

# **Voltage and Current**

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### **PEAK, PEAK-TO-PEAK, AVERAGE, AND RMS (EFFECTIVE) VALUES OF CURRENTS OR VOLTAGES OF SINE WAVES**

The peak value of a sine wave of voltage or current is measured at either 90 degrees or 270 degrees. For this reason peak (or peak-to-peak) values can be considered as instantaneous values. The average of all the instantaneous values over a complete cycle is zero; hence, average is generally understood to be the average of the instantaneous values over a half cycle. The average value is also equal to 2 divided by  $\pi$ . Taking the value of  $\pi$  3.14159265, then the average value of a sine wave of voltage or current is 0.636619, generally rounded off to 0.637, the value used in this book. In some texts, however, you will find the average value given as 0.636. Average value in Table 2-1 is 0.637 times the peak value.

The effective or root-mean-square (rms) value is also a form of instantaneous value averaging. Arithmetically, the effective value is obtained by dividing 1 by the square root of 2. Taking the square root of 2 as equal to 1.414213, then the effective or rms value of a sine wave of voltage or current is equal to  $1/1.414213$ , or 0.707107. In this text, as in other books on electricity and electronics, the rms value is rounded off to 0.707 times the peak value.

The data in Table 2-1 allows rapid movement among peak, peak-to-peak, average, and rms values of currents or voltages of sine waves. Also see Fig. 2-1.

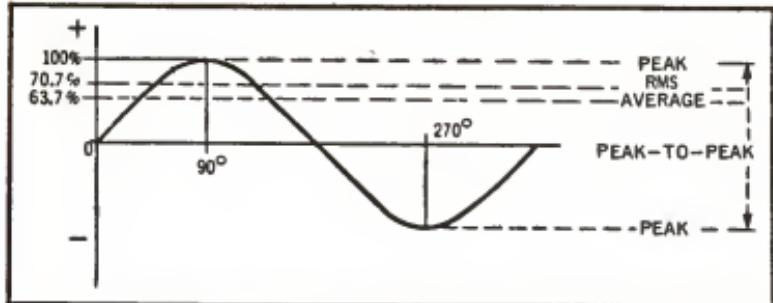


Fig. 2-1. Relationships between peak, peak-to-peak, average and rms values of sine waves of voltage or current.

**□Example:**

What is the peak value of a sine wave current whose effective (rms) value is measured as  $17\frac{1}{2}$  volts?

Locate the nearest value in the rms (effective) column. This is 17.675. Move to the left along the same line and locate 25 as the answer in the column marked peak.

**□Example:**

What is the average value of a voltage sine wave whose peak value is 160 volts?

The maximum peak value shown in Table 2-1 is 120. You can extend the table, however, by multiplying each value by 10. Do this by adding a zero to the right of each whole number. Thus, in the peak column, 16 becomes 160. Move to the right and locate 10.192 in the average column. Multiply this value by 10 by moving the decimal point one place to the right. The average value is 101.92 volts.

Table 2-1. Peak, Peak-to-Peak, Average and rms (effective) Values of Sine Wave Currents or Voltages

Peak	Peak-to-Peak	Average	rms
1	2	0.637	0.707
2	4	1.274	1.414
3	6	1.911	2.121
4	8	2.548	2.828
5	10	3.185	3.535
6	12	3.822	4.242
7	14	4.459	4.949
8	16	5.096	5.656
9	18	5.733	6.363
10	20	6.370	7.070

**Table 2-1. Peak, Peak-to-Peak, Average and rms  
(effective) Values of Sine Wave Currents or Voltages (cont'd).**

<b>Peak</b>	<b>Peak-to-Peak</b>	<b>Average</b>	<b>rms</b>
11	22	7.007	7.777
12	24	7.644	8.484
13	26	8.281	9.191
14	28	8.918	9.898
15	30	9.555	10.605
16	32	10.192	11.312
17	34	10.829	12.019
18	36	11.466	12.726
19	38	12.103	13.433
20	40	12.740	14.140
21	42	13.377	14.847
22	44	14.014	15.554
23	46	14.651	16.261
24	48	15.288	16.968
25	50	15.925	17.675
26	52	16.562	18.382
27	54	17.199	19.089
28	56	17.836	19.796
29	58	18.473	20.503
30	60	19.110	21.210
31	62	19.747	21.917
32	64	20.384	22.624
33	66	21.021	23.331
34	68	21.658	24.038
35	70	22.295	24.745
36	72	22.932	25.452
37	74	23.569	26.159
38	76	24.206	26.866
39	78	24.843	27.573
40	80	25.480	28.280
41	82	26.117	28.987
42	84	26.754	29.694
43	86	27.391	30.401
44	88	28.028	31.108
45	90	28.665	31.815

Table 2-1. Peak, Peak-to-Peak, Average and rms  
(effective) Values of Sine Wave Currents or Voltages (cont'd).

Peak	Peak-to-Peak	Average	rms
46	92	29.302	32.522
47	94	29.939	33.229
48	96	30.576	33.936
49	98	31.213	34.643
50	100	31.850	35.350
51	102	32.487	36.057
52	104	33.124	36.764
53	106	33.761	37.471
54	108	34.398	38.178
55	110	35.035	38.885
56	112	35.672	39.592
57	114	36.309	40.299
58	116	36.946	41.006
59	118	37.583	41.713
60	120	38.220	42.420
61	122	38.857	43.127
62	124	39.494	43.834
63	126	40.131	44.541
64	128	40.768	45.248
65	130	41.405	45.955
66	132	42.042	46.662
67	134	42.679	47.369
68	136	43.316	48.076
69	138	43.953	48.783
70	140	44.590	49.490
71	142	45.227	50.197
72	144	45.864	50.904
73	146	46.501	51.611
74	148	47.138	52.318
75	150	47.775	53.025
76	152	48.412	53.732
77	154	49.049	54.439
78	156	49.686	55.146
79	158	50.323	55.853
80	160	50.960	56.560
81	162	51.597	57.267
82	164	52.234	57.974

**Table 2-1. Peak, Peak-to-Peak, Average and rms  
(effective) Values of Sine Wave Currents or Voltages (cont'd.).**

<b>Peak</b>	<b>Peak-to-Peak</b>	<b>Average</b>	<b>rms</b>
83	166	52.871	58.681
84	168	53.508	59.388
85	170	54.145	60.095
85	172	54.782	60.802
87	174	55.419	61.509
88	176	56.056	62.216
89	178	56.693	62.923
90	180	57.330	63.630
91	182	57.967	64.337
92	184	58.604	65.044
93	186	59.241	65.751
94	188	59.878	66.458
95	190	60.515	67.165
96	192	61.152	67.872
97	194	61.789	68.579
98	196	62.426	69.286
99	198	63.063	69.993
100	200	63.700	70.700
101	202	64.337	71.407
102	204	64.974	72.114
103	206	65.611	72.821
104	208	66.248	73.528
105	210	66.885	74.235
106	212	67.522	74.942
107	214	68.159	75.649
108	216	68.796	76.356
109	218	69.433	77.063
110	220	70.070	77.770
111	222	70.707	78.477
112	224	71.344	79.184
113	226	71.981	79.891
114	228	72.618	80.598
115	230	73.255	81.305
116	232	73.892	82.012
117	234	74.529	82.719
118	236	75.166	83.426
119	238	75.803	84.133
120	240	76.440	84.840

## VALUES OF VOLTAGE OR CURRENT OF SINE WAVES

Peak-to-peak, peak, rms and average values of voltage or current can be calculated from data in Table 2-2.

Table 2-2. Peak-to-Peak (p-p), rms (Effective) and Average AC Values of Sine Waves of Voltage or Current.

Given This Value	Multiply by this value to get			
	Average	rms (Effective)	Peak	p-p
Average	-	1.11	1.57	1.274
rms (Effective)	0.9	-	1.414	2.828
Peak	0.637	0.707	-	2.0
P-P	0.3185	0.3535	0.50	-

### Example:

The rms value of a sine wave is 3.14 volts. What is its peak value?

Locate rms in the left column of Table 2-2. Move across to the peak column. The multiplication factor is 1.414,  $1.414 \times 3.14 = 4.4399$  volts.

## INSTANTANEOUS VALUES OF VOLTAGE OR CURRENT OF SINE WAVES

The instantaneous value of a wave is a function of the phase angle. At 0 degrees, 180 degrees, and 360 degrees the instantaneous value of a sine wave is zero. It is a peak at 90 degrees and 270 degrees. See Fig. 2-2. These are the only values which may be known without the use of a table or formula. The instantaneous value of a sine voltage is  $E = E_{\text{max}} \sin \theta t$  ( $\theta$  equals  $2\pi f$ ) and for a sine current is  $I = I_{\text{max}} \sin \theta t$ . Table 2-3 gives the instantaneous values of either voltage or current through a complete sine wave cycle of 360 degrees for values of voltage ranging from 1 to 10. Other ranges may be obtained by moving the decimal point.

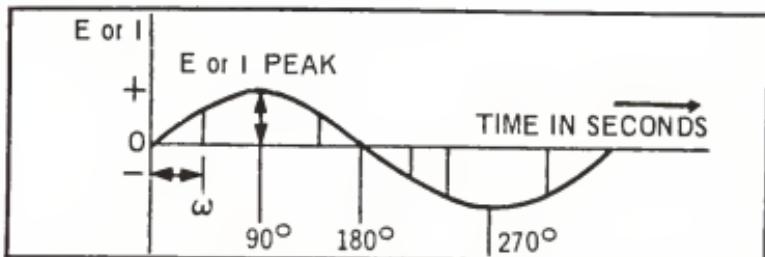


Fig. 2-2. Sine Wave showing various instantaneous values of voltage or current.

The values given in Table 2-3 under the heading of Peak Voltage or Current are those obtained from a table of natural trigonometric functions, and represent sine values. Thus, the sine of 10 degrees equals 0.1736 as shown by locating 10 in the extreme left-hand column and moving to the right and stopping in column 1. Greater accuracy can be obtained by consulting tables of natural trigonometric functions that supply a larger number of decimal places. Thus, a 5-place table would show the sine of 10 degrees as 0.17365. For example, if a sine wave of voltage or current has a peak value of 1 volt, its instantaneous value when the wave reaches 10 degrees is 0.1736 or 0.17365 volt depending on the accuracy you want. For a 2-volt peak, the value would be  $2 \times 0.1736$  or 0.3472. For a 3-volt peak, the value would be  $3 \times 0.1736$  or 0.5208 volt, as shown in the respective columns headed 2 and 3 in Table 2-3. Using this technique, the instantaneous value of any sine wave or voltage can be found.

**□Example:**

What is the instantaneous value of a sine wave at 27 degrees if the peak value of the wave is 138.2 volts?

Locate 27 degrees in the table. Move to the right and in column 1 find 0.4540 volt. This is the instantaneous value at 27 degrees when the peak value is 1 volt. For 138.2 volts, multiply 0.4540 by 138.2. That is,  $0.4540 \times 138.2$  equals 62.7428 volts. A 5-place table of natural trigonometric functions shows the value of 27 degrees as 0.45399.  $0.45399 \times 138.2$  equals 62.741418 volts. Whether this greater accuracy is desirable depends on the work being done. The actual difference is  $62.7428 - 62.741418$  equals 0.001382 volt. Although the example mentions peak in terms of volts, peak can be volts, millivolts, or microvolts, amperes, milliamperes or microamperes.

**□Example:**

What is the instantaneous value of current at a phase angle of 37 degrees when the peak value is 3 volts?

Locate 37 degrees in the left-hand column of the Table. Move horizontally until the 3-volt column is reached. The required voltage is 1.8054 volts.

**□Example:**

At what phase angles will the instantaneous voltage of a sine wave be 68 percent of its peak value?

Consider peak as 1 or 100 percent. Locate the nearest value to 68 in the column headed by the number 1. This value is 0.6820.

Move to the left of this number and you will see that the phase angle is 43 degrees. Multiples of this value are also given. We have 137 degrees (180 degrees - 43 degrees); 223 degrees (43 degrees + 180 degrees) and 317 degrees (360 degrees - 43 degrees).

**Example:**

What is the instantaneous value of a sine wave of current at a phase angle of 77 degrees when its peak value is 30 mA?

Locate 77 degrees in the left-hand column of the table and move horizontally to the right to intercept 2.9232 in the column headed by the number 3. Multiply 3 by 10 to obtain the peak value specified in the question. However, since 3 was changed to 30 by multiplying it by 10 (or by moving the decimal point one place to the right) the answer must be similarly treated. The value is 29.232 mA.

Table 2-3. Instantaneous Values of Voltage or Current of Sine Waves

Phase Angle (degrees)				Peak Voltage or Current				
	1	2	3	4	5			
0	180	180	360	.0000	.0000	.0000	.0000	.0000
1	179	181	359	.0175	.0350	.0525	.0700	.0875
2	178	182	358	.0349	.0698	.1047	.1396	.1745
3	177	183	357	.0523	.1046	.1569	.2092	.2615
4	176	184	356	.0698	.1396	.2094	.2792	.3490
5	175	185	355	.0872	.1744	.2616	.3488	.4360
6	174	186	354	.1045	.2090	.3135	.4180	.5225
7	173	187	353	.1219	.2438	.3657	.4876	.6095
8	172	188	352	.1392	.2784	.4176	.5568	.6960
9	171	189	351	.1564	.3128	.4692	.6256	.7820
10	170	190	350	.1736	.3472	.5208	.6944	.8680
11	169	191	349	.1908	.3816	.5724	.7632	.9540
12	168	192	348	.2079	.4158	.6237	.8316	1.0395
13	167	193	347	.2250	.4500	.6750	.9000	1.1250
14	166	194	346	.2419	.4838	.7257	.9676	1.0095
15	165	195	345	.2588	.5176	.7764	1.0352	1.2940
16	164	196	344	.2756	.5512	.8268	1.1024	1.3780
17	163	197	343	.2924	.5848	.8772	1.1696	1.4620
18	162	198	342	.3090	.6180	.9270	1.2360	1.5450
19	161	199	341	.3256	.6512	.9768	1.3024	1.6280
20	160	200	340	.3420	.6840	1.0260	1.3680	1.7100

Table 2-3. Instantaneous Values of Voltage or Current of Sine Waves (cont'd)

Phase	Angle (degrees)	Peak Voltage or Current						
		1	2	3	4	5		
21	159	201	339	.3584	.7168	1.0752	1.4336	1.7920
22	158	202	338	.3746	.7492	1.1238	1.4984	1.8730
23	157	203	337	.3907	.7814	1.1721	1.5628	1.9535
24	156	204	336	.4067	.8134	1.2201	1.6268	2.0335
25	155	205	335	.4226	.8452	1.2678	1.6904	2.1130
26	154	206	334	.4384	.8768	1.3152	1.7536	2.1920
27	153	207	333	.4540	.9080	1.3620	1.8160	2.2700
28	152	208	332	.4695	.9390	1.4085	1.8780	2.3475
29	151	209	331	.4848	.9696	1.4544	1.9392	2.4240
30	150	210	330	.5000	1.0000	1.5000	2.0000	2.5000
31	149	211	329	.5150	1.0300	1.5450	2.0600	2.5750
32	148	212	328	.5299	1.0598	1.5897	2.1196	2.6495
33	147	213	327	.5446	1.0892	1.6338	2.1784	2.7320
34	146	214	326	.5592	1.1184	1.6776	2.2368	2.7960
35	145	215	325	.5736	1.1472	1.7208	2.2944	2.8680
36	144	216	324	.5878	1.1756	1.7634	2.3512	2.9390
37	143	217	323	.6018	1.2036	1.8054	2.4072	3.0090
38	142	218	322	.6157	1.2314	1.8471	2.4628	3.0785
39	141	219	321	.6293	1.2586	1.8879	2.5172	3.1465
40	140	220	320	.6428	1.2856	1.9284	2.5712	3.2140
41	139	221	319	.6561	1.3122	1.9683	2.6244	3.2805
42	138	222	318	.6691	1.3382	2.0073	2.6764	3.3455
43	137	223	317	.6820	1.3640	2.0460	2.7280	3.4100
44	136	224	316	.6947	1.3894	2.0841	2.7788	3.4735
45	135	225	315	.7071	1.4142	2.1213	2.8284	3.5355
46	134	226	314	.7193	1.4386	2.1579	2.8772	3.5965
47	133	227	313	.7314	1.4628	2.1942	2.9256	3.6570
48	132	228	312	.7431	1.4862	2.2293	2.9724	3.7155
49	131	229	311	.7547	1.5094	2.2641	3.0188	3.7735
50	130	230	310	.7660	1.5320	2.2980	3.0640	3.8300
51	129	231	309	.7771	1.5542	2.3313	3.1084	3.8855
52	128	232	308	.7880	1.5760	2.3640	3.1520	3.9400
53	127	233	307	.7986	1.5972	2.3958	3.1954	3.9930
54	126	234	306	.8090	1.6180	2.4270	3.2360	4.0450
55	125	235	305	.8192	1.6384	2.4576	3.2768	4.0960

Table 2-3. Instantaneous Values of Voltage or Current of Sine Waves (cont'd)

Phase Angle (degrees)	1	Peak Voltage or Current				5
		2	3	4		
56 124 236 304	.8290	1.6580	2.4870	3.3160	4.1450	
57 123 237 303	.8387	1.6774	2.5161	3.3548	4.1935	
58 122 238 302	.8480	1.6960	2.5440	3.3920	4.2400	
59 121 239 301	.8572	1.7144	2.5716	3.4288	4.2860	
60 120 240 300	.8660	1.7320	2.5980	3.4640	4.3300	
61 119 241 299	.8746	1.7492	2.6238	3.4984	4.3730	
62 118 242 298	.8829	1.7658	2.6487	3.5316	4.4145	
63 117 243 297	.8910	1.7820	2.6730	3.5640	4.4550	
64 116 244 296	.8988	1.7976	2.6964	3.5952	4.4940	
65 115 245 295	.9063	1.8126	2.7189	3.6252	4.5315	
66 114 246 294	.9135	1.8270	2.7405	3.6540	4.5675	
67 113 247 293	.9205	1.8410	2.7615	3.6820	4.6025	
68 112 248 292	.9272	1.8544	2.7816	3.7088	4.6360	
69 111 249 291	.9336	1.8672	2.8008	3.7344	4.6680	
70 110 250 290	.9397	1.8794	2.8191	3.7588	4.6985	
71 109 251 289	.9455	1.8910	2.8365	3.7820	4.7275	
72 108 252 288	.9511	1.9022	2.8533	3.8044	4.7555	
73 107 253 287	.9563	1.9126	2.8689	3.8252	4.7815	
74 106 254 286	.9613	1.9226	2.8839	3.8452	4.8065	
75 105 255 285	.9659	1.9318	2.8977	3.8636	4.8295	
76 104 256 284	.9703	1.9406	2.9109	3.8812	4.8515	
77 103 257 283	.9744	1.9488	2.9232	3.8976	4.8720	
78 102 258 282	.9781	1.9562	2.9343	3.9124	4.8905	
79 101 259 281	.9816	1.9632	2.9448	3.9264	4.9080	
80 100 260 280	.9848	1.9696	2.9544	3.9392	4.9240	
81 99 261 279	.9877	1.9754	2.9631	3.9508	4.9385	
82 98 262 278	.9903	1.9806	2.9709	3.9612	4.9515	
83 97 263 277	.9925	1.9850	2.9775	3.9700	4.9625	
84 96 264 276	.9945	1.9890	2.9835	3.9780	4.9725	
85 95 265 275	.9962	1.9924	2.9886	3.9848	4.9810	
86 94 266 274	.9976	1.9952	2.9928	3.9904	4.9880	
87 93 267 273	.9986	1.9972	2.9958	3.9944	4.9930	
88 92 268 272	.9994	1.9988	2.9982	3.9976	4.9970	
89 91 269 271	.9998	1.9996	2.9994	3.9992	4.9990	
90 90 270 270	1.0000	2.0000	3.0000	4.0000	5.0000	

Table 2-3. Instantaneous Values of Voltage or Current of Sine Waves (cont'd)

Phase Angle (degrees)	Peak Voltage or Current					
	6	7	8	9	10	
0 180 180 360	.0000	.0000	.0000	.0000	.0000	.0000
1 179 181 359	.1050	.1225	.1400	.1575	.1750	
2 178 182 358	.2094	.2443	.2792	.3141	.3490	
3 177 183 357	.3138	.3661	.4184	.4707	.5230	
4 176 184 356	.4188	.4886	.5584	.6282	.6980	
5 175 185 355	.5232	.6104	.6976	.7848	.8720	
6 174 186 354	.6270	.7315	.8360	.9405	1.0450	
7 173 187 353	.7314	.8533	.9752	1.0971	1.2190	
8 172 188 352	.8352	.9744	1.1136	1.2528	1.3920	
9 171 189 351	.9384	1.0948	1.2512	1.4076	1.5640	
10 170 190 350	1.0416	1.2152	1.3888	1.5624	1.7360	
11 169 191 349	1.4448	1.3356	1.5264	1.7172	1.9080	
12 168 192 348	1.2474	1.4553	1.6632	1.8711	2.0790	
13 167 193 347	1.3500	1.5750	1.8000	2.0250	2.2500	
14 166 194 346	1.4514	1.6933	1.9352	2.1771	2.4190	
15 165 195 345	1.5528	1.8116	2.0704	2.3292	2.5880	
16 164 196 344	1.6536	1.9292	2.2048	2.4804	2.7560	
17 163 197 343	1.7544	2.0468	2.3392	2.6316	2.9240	
18 162 198 342	1.8540	2.1630	2.4720	2.7810	3.0900	
19 161 199 341	1.9536	2.2792	2.6048	2.9304	3.2560	
20 160 200 340	2.0520	2.3940	2.7360	3.0780	3.4200	
21 159 201 339	2.1504	2.5088	2.8672	3.2256	3.5840	
22 158 202 338	2.2476	2.6222	2.9968	3.3714	3.7460	
23 157 203 337	2.3442	2.7349	3.1256	3.5163	3.9070	
24 156 204 336	2.4402	2.8469	3.2536	3.6603	4.0670	
25 155 205 335	2.5356	2.9582	3.3808	3.8034	4.2260	
26 154 206 334	2.6304	3.0688	3.5072	3.9456	4.3840	
27 153 207 333	2.7240	3.1790	3.6320	4.0860	4.5400	
28 152 208 332	2.8170	3.2865	3.7560	4.2255	4.6950	
29 151 209 331	2.9088	3.3936	3.8784	4.3632	4.8480	
30 150 210 330	3.0000	3.5000	4.0000	4.5000	5.0000	
31 149 211 329	3.0900	3.6050	4.1200	4.6350	5.1500	
32 148 212 328	3.1794	3.7093	4.2392	4.7691	5.2990	
33 147 213 327	3.2676	3.8122	4.3568	4.9014	5.4460	
34 146 214 326	3.3552	3.9144	4.4736	5.0328	5.5920	
35 145 215 325	3.4416	4.0152	4.5888	5.1634	5.7360	

Table 2-3. Instantaneous Values of Voltages or Currents of Sine Waves (cont'd)

Phase Angle (degrees)	6	Peak Voltage or Current					10
		7	8	9			
36 144 216 324	3.5268	4.1146	4.7004	5.2902	5.8780		
37 143 217 323	3.6108	4.2126	4.8144	5.4162	6.0180		
38 142 218 322	3.6942	4.3099	4.9256	5.5413	6.1570		
39 141 219 321	3.7758	4.4051	5.0344	5.6637	6.2930		
40 140 220 320	3.8568	4.4996	5.1424	5.7852	6.4280		
41 139 221 319	3.9366	4.5927	5.2488	5.9049	6.5610		
42 138 222 318	4.0146	4.6837	5.3528	6.0219	6.6910		
43 137 223 317	4.0920	4.7740	5.4560	6.1380	6.8200		
44 136 224 316	4.1682	4.8629	5.5576	6.2523	6.9470		
45 135 225 315	4.2426	4.9497	5.6568	6.3639	7.0710		
46 134 226 314	4.3158	5.0351	5.7544	6.4737	7.1930		
47 133 227 313	4.3884	5.1198	5.8512	6.5826	7.3140		
48 132 228 312	4.4586	5.2017	5.9448	6.6879	7.4310		
49 131 229 311	4.5282	5.2829	6.0376	6.7923	7.5470		
50 130 230 310	4.5960	5.3620	6.1280	6.8940	7.6600		
51 129 231 309	4.6626	5.4397	6.2168	6.9939	7.7710		
52 128 232 308	4.7280	5.5160	6.3040	7.0920	7.8800		
53 127 233 307	4.7916	5.5902	6.3888	7.1874	7.9860		
54 126 234 306	4.8540	5.6630	6.4720	7.2810	8.0900		
55 125 235 305	4.9152	5.7344	6.5536	7.3728	8.1920		
56 124 236 304	4.9740	5.8030	6.6320	7.4610	8.2900		
57 123 237 303	5.0322	5.8709	6.7096	7.5083	8.3870		
58 122 238 302	5.0880	5.9360	6.7840	7.6320	8.4800		
59 121 239 301	5.1432	6.0004	6.8576	7.7148	8.5720		
60 120 240 300	5.1960	6.0620	6.9280	7.7940	8.6600		
61 119 241 299	5.2476	6.1222	6.9968	7.8714	8.7460		
62 118 242 298	5.2974	6.1803	7.0632	7.9461	8.8290		
63 117 243 297	5.3460	6.2370	7.1280	8.0190	8.9100		
64 116 244 296	5.3928	6.2916	7.1904	8.0892	8.9880		
65 115 245 295	5.4378	6.3441	7.2504	8.1567	9.0630		
66 114 246 294	5.4810	6.3945	7.3080	8.2215	9.1350		
67 113 247 293	5.5230	6.4435	7.3640	8.2845	9.2050		
68 112 248 292	5.5632	6.4904	7.4176	8.3448	9.2720		
69 111 249 291	5.6016	6.5352	7.4688	8.4024	9.3360		
70 110 250 290	5.6382	6.5779	7.5176	8.4573	9.3970		

**Table 2-3. Instantaneous Values of Voltages or Current of Sine Waves (cont'd)**

Phase	Angle (degrees)	Peak Voltage or Current						10
		6	7	8	9			
71	109	251	289	5.6730	6.6185	7.5640	8.5095	9.4550
72	108	252	288	5.7066	6.6577	7.6088	8.5599	9.5110
73	107	253	287	5.7378	6.6941	7.6504	8.6067	9.5630
74	106	254	286	5.7678	6.7291	7.6904	8.6517	9.6120
75	105	255	285	5.7954	6.7613	7.7272	8.6931	9.6590
76	104	256	284	5.8218	6.7921	7.7624	8.7327	9.7030
77	103	257	283	5.8464	6.8208	7.7952	8.7696	9.7440
78	102	258	282	5.8686	6.8467	7.8248	8.8029	9.7810
79	101	259	281	5.8896	6.8712	7.8528	8.8344	9.8160
80	100	260	280	5.9088	6.8936	7.8784	8.8632	9.8480
81	99	261	279	5.9262	6.9139	7.9016	8.8893	9.8770
82	98	262	278	5.9418	6.9321	7.9224	8.9127	9.9030
83	97	263	277	5.9550	6.9475	7.9400	8.9325	9.9250
84	96	264	276	5.9670	6.9615	7.9560	8.9505	9.9450
85	95	265	275	5.9772	6.9734	7.9696	8.9658	9.9620
86	94	266	274	5.9856	6.9832	7.9808	8.9784	9.9760
87	93	267	273	5.9916	6.9902	7.9888	8.9874	9.9860
88	92	268	272	5.9964	6.9958	7.9952	8.9946	9.9940
89	91	269	271	5.9988	6.9986	7.9984	8.9982	9.9980
90	90	270	270	6.0000	7.0000	8.0000	9.0000	10.0000

**PERIOD AND FREQUENCY**

The time required for the completion of one complete cycle by a periodic function, such as a sine wave, is known as its period. The relationship between the period and the frequency of a wave is a reciprocal one and is shown in the formula  $T = 1/f$ . In this formula,  $T$ , the period of the wave, is the time required for the completion of one full cycle;  $f$  is the frequency in hertz (cycles per second).

Table 2-4 permits the rapid conversion between the period of a wave and its frequency. Values not given in the table can be obtained by moving the decimal point. However, since the relationship is an inverse one, the decimal point for frequency and for time will move in opposite directions. Thus, for a frequency of 10 hertz, the time is 0.1 second. For a frequency of 100 hertz, move the decimal point one place to the right, changing 10 to 100. For the corresponding value of time, however, move the decimal point one place to the left. This would change 0.1 second to 0.01 second.

**Table 2-4. Period vs Frequency**

Frequency (Hz)	Time (sec)	Frequency (Hz)	Time (sec)	Frequency (Hz)	Time (sec)
1	1.0000	34	.0294	67	.0149
2	.5000	35	.0286	68	.0147
3	.3333	36	.0278	69	.0145
4	.2500	37	.0270	70	.0143
5	.2000	38	.0263	71	.0141
6	.1667	39	.0256	72	.0139
7	.1429	40	.0250	73	.0137
8	.1250	41	.0244	74	.0135
9	.1111	42	.0238	75	.0133
10	.1000	43	.0233	76	.0132
11	.0909	44	.0227	77	.0130
12	.0833	45	.0222	78	.0128
13	.0769	46	.0217	79	.0127
14	.0714	47	.0213	80	.0125
15	.0667	48	.0208	81	.0123
16	.0625	49	.0204	82	.0122
17	.0588	50	.0200	83	.0120
18	.0556	51	.0196	84	.0119
19	.0526	52	.0192	85	.0118
20	.0500	53	.0189	86	.0116
21	.0476	54	.0185	87	.0115
22	.0455	55	.0182	88	.0114
23	.0435	56	.0179	89	.0112
24	.0417	57	.0175	90	.0111
25	.0400	58	.0172	91	.0110
26	.0385	59	.0169	92	.0109
27	.0370	60	.0167	93	.0108
28	.0357	61	.0164	94	.0106
29	.0345	62	.0161	95	.0105
30	.0333	63	.0159	96	.0104
31	.0323	64	.0156	97	.0103
32	.0312	65	.0154	98	.0102
33	.0303	66	.0152	99	.0101
				100	.0100

**□Example:**

The sine wave input to a power supply is 60 Hz. What is the period of this wave?

Locate 60 in the frequency column. Immediately adjacent you will see it requires 0.0167 second to complete one single cycle of this waveform.

**□Example:**

What is the period of a sine waveform having a frequency of 550 kilohertz?

In Table 2-4 the frequency is given in hertz. In that table 55 can be made to represent 550 kHz by multiplying it by 10,000 or by moving its decimal point four places to the right (550,000). However, as shown in the formula given above, T and f are inverse. Thus, if we move the decimal point to the right for the frequency column, we must move it to the left an equal number of places for the time column. For 55 hertz, the time is 0.0182 second. For 550,000 hertz, the time is 0.00000182 second or 1.82  $\mu$ sec.

**□Example:**

The time of a half wave is 61 microseconds. What is its frequency?

Assuming the problem involves a sine wave, first multiply 61 by 2 to get the time of a full wave.  $2 \times 61$  equals 122. 122 microseconds corresponds to 0.000122 second. The nearest value shown in the table is 0.0122 second, and the frequency for this time value is 82 Hz. We can get 0.000122 by moving the decimal point of 0.0122 two places to the left. The decimal point for the frequency, then, should be moved an equivalent number of places to the right. This would give an answer of 8200 Hz.



## Chapter 3

# Capacitance

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### CAPACITIVE REACTANCE

The reactance of a capacitor, or its opposition to the flow of an alternating current, varies inversely with frequency and with capacitance. Capacitive reactance, expressed in ohms, is based on the ability of a capacitor to store a charge or counter-electromotive force. This emf, acting in opposition to the applied voltage, reduces the amount of current flowing in a circuit, hence produces an effect analogous to that of a resistor. With a resistor, though, the current through it and the voltage across it are in phase. However, the counter end of a capacitor, causes the voltage to lag behind the current. Ideally, the phase angle is 90 degrees, but in practice the phase angle is less than this.

Table 3-1 gives the reactance of capacitors ranging from  $0.0001 \mu\text{F}$  to  $0.0005 \mu\text{F}$  for frequencies ranging from 10 to 5,000 kHz. Table 3-1 is also for capacitors having values from 0.25 to  $3 \mu\text{F}$  and for frequencies from 25 to 20,000 hertz. Both tables can be extended since doubling the frequency will halve the reactance. The same effect can be obtained by doubling the capacitance. Similarly, halving the frequency or capacitance will double the reactance. Naturally, other multiplication or division factors can be used. See also Table 3-2.

#### □Example:

What is the reactance of a  $.01-\mu\text{F}$  capacitor at a frequency of 1000 Hz? What will happen to this reactance if the frequency is increased to 10,000 Hz?

Table 3-1. Capacitive Reactance (Ohms).

Frequency (Hz)	Capacitance ( $\mu$ F)				
	0.25	0.5	1.0	2.0	3.0
25	25,478	12,739	6,369	3,185	2,123
30	21,231	10,616	5,308	2,654	1,769
50	12,739	6,369	3,185	1,593	1,062
60	10,616	5,308	2,654	1,327	885
75	8,492	4,246	2,123	1,062	708
100	6,369	3,185	1,592	796	531
120	5,308	2,654	1,327	664	442
150	4,246	2,123	1,062	531	354
180	3,538	1,769	885	443	295
200	3,185	1,592	796	398	265
250	2,548	1,274	637	319	212
300	2,123	1,062	531	265	177
350	1,820	910	455	228	152
400	1,592	796	398	199	133
450	1,415	708	354	177	118
500	1,274	637	319	159	106
600	1,107	531	265	133	88
700	948	455	228	114	76
800	796	398	199	99	66
900	708	354	177	89	59
1,000	637	318	159	79	53
2,000	319	159	79	39	27
3,000	213	107	53	27	18
4,000	159	79	39	20	14
5,000	127	64	32	16	11
6,000	106	53	27	14	9
7,000	91	46	23	12	8
8,000	80	40	20	10	7
9,000	71	36	18	9	6
10,000	64	32	16	8	5
12,000	53	27	14	7	4.6
14,000	46	23	12	6	4
16,000	40	20	10	5	3.3
18,000	36	18	9	4.5	3
20,000	32	16	8	4	2.6

Table 3-1. Capacitive Reactance (Ohms) (cont'd)

Frequency (kHz)	Capacitance ( $\mu$ F)					
	0.0001	0.00015	0.0002	0.00025	0.0003	0.0005
10	159,236	106,157	79,618	63,694	53,078	31,847
20	79,618	53,079	39,809	31,848	26,539	15,924
30	53,079	35,836	26,539	21,232	17,693	10,616
40	39,809	26,540	19,905	15,924	13,270	7,962
50	31,847	21,230	15,924	12,740	10,616	6,370
60	26,539	17,693	13,270	10,616	8,847	5,308
70	22,748	15,165	11,374	9,098	7,852	4,549
80	19,905	13,270	9,953	7,962	6,635	3,981
90	17,693	11,795	8,847	7,078	5,897	3,539
100	15,924	10,615	7,962	6,370	5,308	3,185
150	10,616	7,077	5,308	4,246	3,539	2,123
200	7,962	5,308	3,981	3,186	2,654	1,593
250	6,369	4,246	3,185	2,548	2,123	1,274
300	5,308	3,538	2,654	2,124	1,770	1,062
350	4,550	3,033	2,275	1,820	1,516	910
400	3,981	2,654	1,991	1,594	1,326	797
450	3,539	2,539	1,769	1,414	1,179	707
500	3,185	2,123	1,592	1,274	1,062	637
550	2,895	1,930	1,448	1,158	965	579
600	2,654	1,769	1,327	1,062	885	531
650	2,450	1,633	1,225	980	816	490
700	2,275	1,516	1,138	910	758	455
750	2,123	1,416	1,062	850	708	425
800	1,991	1,327	896	798	663	399
850	1,873	1,249	937	750	624	375
900	1,769	1,179	885	708	589	354
950	1,676	1,117	938	670	559	335
1,000	1,592	1,062	796	637	530	319
2,000	796	531	398	319	265	159
2,500	637	425	319	255	212	127
3,000	531	354	266	212	177	106
3,500	455	303	228	182	152	91
4,000	398	265	199	159	133	80
4,500	354	254	177	141	118	71
5,000	319	212	159	127	106	64

Table 3-1 shows a frequency of 1000 Hz, but does not have a capacitance value marked 0.01. Locate 1000 in the left-hand column and move horizontally to the right until you reach the number 159 under the heading of  $1.0 \mu\text{F}$ . Change  $1.0 \mu\text{F}$  to 0.01 by dividing it by 100. When we do this, we must multiply 159 by 100. The answer is then 15,900 ohms. If we increase the frequency to 10,000 Hz we will be multiplying the original frequency by a factor of 10. This means the reactance should be divided by a similar factor. The answer will be 15900 divided by 10 or 1590 ohms.

**□Example:**

What is the reactance of a  $0.00015 \mu\text{F}$  capacitor at a frequency of 3,000 kHz?

The Table shows that at this frequency the reactance is 354 ohms.

Table 3-2. Capacitive Reactance At Spot Frequencies

	50 Hz	100 Hz	1kHz	10 kHz	100kHz	1 MHz	10MHz	100MHz
1pF	—	—	—	—	1.6 M	160 k	16 k	1.6 k
10pF	—	—	—	1.6 M	160 k	16 k	1.6 k	160
50 pF	—	—	3.2 M	320 k	32 k	3.2 k	320	32
250 pF	—	6.4 M	640 k	64 k	6.4 k	640	64	6.4
1,000 pF	3.2 M	1.6 M	160 k	16 k	1.6 k	160	16	1.6
2,000 pF	1.6 M	800 k	80 kΩ	8 k	800	80	8	0.8
0.01 $\mu\text{F}$	320 k	160 k	16 k	1.6 k	160	16	1.6	0.16
0.05 $\mu\text{F}$	64 k	32 k	3.2 k	320	32	3.2	0.32	—
0.1 $\mu\text{F}$	32 k	16 k	1.6 k	160	16	1.6	0.16	—
1 $\mu\text{F}$	3.2 k	1.6 k	160	16	1.6	0.16	—	—
2.5 $\mu\text{F}$	1.3 k	640	64	6.4	0.64	—	—	—
5 $\mu\text{F}$	640	320	32	3.2	0.32	—	—	—
10 $\mu\text{F}$	320	160	16	1.6	0.16	—	—	—
30 $\mu\text{F}$	107	53	5.3	0.53	—	—	—	—
100 $\mu\text{F}$	32	16	1.6	0.16	—	—	—	—
1,000 $\mu\text{F}$	3.2	1.6	0.16	—	—	—	—	—

Value above  $10 \text{ M}\Omega$  and below  $0.1 \Omega$  not shown. Values in ohms.

## CAPACITORS IN SERIES

The total capacitance of series capacitors is always less than that of the smallest capacitor in the series network. As a general rule of thumb, if two capacitors are in series, and one has ten or more times the value of the other, the resultant total capacitance can be considered as slightly less than or equal to the value of the smaller capacitor.

Where two series capacitors have equal values, the resultant capacitance is one-half that of either unit. When three capacitors in

Table 3-3. Capacitors in Series

C2	C1				
	1	1.5	2	2.2	3
1	0.50	0.60	0.666	0.69	0.75
1.5	0.60	0.75	0.857	0.89	1.00
2	0.666	0.888	1.00	1.05	1.20
2.2	0.69	0.89	1.05	1.10	1.27
3	0.75	1.00	1.20	1.27	1.50
3.3	0.77	1.03	1.24	1.31	1.57
4	0.80	1.09	1.33	1.42	1.71
4.7	0.82	1.13	1.40	1.49	1.83
5	0.833	1.15	1.43	1.53	1.87
5.6	0.848	1.18	1.47	1.58	1.95
6.8	0.87	1.22	1.54	1.66	2.08
7.5	0.88	1.25	1.58	1.69	2.14
8.2	0.89	1.26	1.60	1.73	2.19
10	0.91	1.30	1.66	1.80	2.31
12	0.923	1.33	1.71	1.85	2.40
15	0.937	1.36	1.76	1.92	2.50
18	0.947	1.38	1.80	1.96	2.57
20	0.952	1.40	1.82	1.98	2.61
22	0.956	1.40	1.83	2.00	2.64
24	0.96	1.41	1.84	2.01	2.66
27	0.964	1.42	1.86	2.03	2.70
30	0.968	1.428	1.87	2.05	2.73
33	0.970	1.43	1.88	2.06	2.75
36	0.973	1.44	1.89	2.07	2.77
39	0.975	1.444	1.90	2.08	2.79
43	0.977	1.449	1.91	2.09	2.80
47	0.979	1.45	1.92	2.10	2.82
51	0.98	1.457	1.924	2.11	2.83
56	0.982	1.461	1.93	2.12	2.84
62	0.984	1.464	1.937	2.124	2.86
68	0.985	1.467	1.94	2.13	2.87
75	0.987	1.47	1.95	2.14	2.88
82	0.988	1.473	1.952	2.142	2.89
91	0.989	1.475	1.957	2.148	2.90
100	0.991	1.478	1.96	2.153	2.91

Table 3-3. Capacitors in Series (cont'd)

C2	3.3	4	4.7	5	5.6
1	0.77	0.80	0.82	0.83	0.84
1.5	1.03	1.09	1.13	1.15	1.18
2	1.24	1.33	1.40	1.43	1.47
2.2	1.31	1.42	1.49	1.53	1.58
3	1.57	1.71	1.83	1.87	1.95
3.3	1.65	1.81	1.94	1.98	2.07
4	1.81	2.00	2.16	2.22	2.33
4.7	1.94	2.16	2.35	2.42	2.55
5	1.99	2.22	2.42	2.50	2.64
5.6	2.07	2.33	2.55	2.64	2.80
6.8	2.22	2.52	2.78	2.88	3.07
7.5	2.29	2.66	2.88	3.00	3.21
8.2	2.35	2.69	2.99	3.10	3.32
10	2.48	2.85	3.19	3.33	3.59
12	2.59	3.00	3.37	3.53	3.82
15	2.72	3.15	3.57	3.75	4.08
18	2.79	3.27	3.72	3.91	4.27
20	2.83	3.33	3.80	4.00	4.37
22	2.87	3.38	3.87	4.07	4.46
24	2.90	3.42	3.92	4.14	4.54
27	2.94	3.48	4.00	4.22	4.63
30	2.97	3.53	4.06	4.28	4.72
33	3.00	3.56	4.11	4.34	4.78
36	3.02	3.60	4.15	4.39	4.84
39	3.04	3.63	4.19	4.43	4.89
43	3.06	3.66	4.23	4.48	4.95
47	3.08	3.68	4.27	4.52	5.00
51	3.09	3.71	4.30	4.55	5.04
56	3.12	3.73	4.33	4.59	5.09
62	3.13	3.75	4.36	4.62	5.13
68	3.14	3.77	4.39	4.65	5.17
75	3.16	3.79	4.42	4.69	5.21
82	3.17	3.81	4.45	4.71	5.24
91	3.18	3.83	4.47	4.74	5.27
100	3.195	3.84	4.49	4.76	5.30

Table 3-3. Capacitors in Series (cont'd)

C2	6.8	7.5	8.2	10	12
1	0.87	0.88	0.89	0.91	0.92
1.5	1.22	1.25	1.26	1.30	1.33
2	1.54	1.58	1.60	1.66	1.71
2.2	1.66	1.69	1.73	1.80	1.86
3	2.08	2.14	2.19	2.31	2.40
3.3	2.22	2.29	2.35	2.48	2.59
4	2.52	2.66	2.69	2.85	3.00
4.7	2.78	2.88	2.99	3.19	3.37
5	2.88	3.00	3.10	3.33	3.53
5.6	3.07	3.21	3.32	3.59	3.82
6.8	3.40	3.56	3.66	4.05	4.34
7.5	3.56	3.75	3.92	4.29	4.61
8.2	3.66	3.92	4.10	4.51	4.87
10	4.05	4.29	4.51	5.00	5.45
12	4.34	4.61	4.87	5.45	6.00
15	4.68	5.00	5.30	6.00	6.66
18	4.93	5.29	5.63	6.43	7.20
20	5.07	5.45	5.81	6.66	7.50
22	5.19	5.59	5.97	6.87	7.77
24	5.29	5.71	6.11	7.06	8.00
27	5.43	5.87	6.29	7.29	8.31
30	5.54	6.00	6.44	7.50	8.57
33	5.64	6.11	6.57	7.67	8.80
36	5.72	6.20	6.67	7.82	9.00
39	5.79	6.29	6.77	7.95	9.18
43	5.87	6.38	6.88	8.11	9.40
47	5.94	6.47	6.98	8.24	9.56
51	6.00	6.53	7.06	8.36	9.71
56	6.06	6.61	7.15	8.48	9.88
62	6.14	6.69	7.24	8.61	10.05
68	6.18	6.75	7.32	8.72	10.20
75	6.23	6.82	7.39	8.82	10.34
82	6.28	6.87	7.45	8.91	10.46
91	6.32	6.93	7.52	9.01	10.60
100	6.37	6.96	7.58	9.09	10.71

Table 3-3. Capacitors in Series (cont'd)

C2	15	18	20	22	24
1	0.937	0.947	0.952	0.956	0.96
1.5	1.36	1.38	1.395	1.40	1.41
2	1.76	1.80	1.82	1.83	1.84
2.2	1.92	1.96	1.98	2.00	2.01
3	2.50	2.57	2.61	2.64	2.66
3.3	2.72	2.79	2.83	2.87	2.90
4	3.15	3.27	3.33	3.38	3.42
4.7	3.57	3.72	3.80	3.87	3.92
5	3.75	3.91	4.00	4.07	4.14
5.6	4.08	4.27	4.37	4.46	4.54
6.8	4.68	4.93	5.07	5.19	5.29
7.5	5.00	5.29	5.45	5.59	5.71
8.2	5.30	5.63	5.81	5.97	6.11
10	6.00	6.43	6.66	6.87	7.06
12	6.66	7.20	7.50	7.77	8.00
15	7.50	8.18	8.57	8.92	9.23
18	8.18	9.00	9.47	9.90	10.29
20	8.57	9.47	10.00	10.43	10.91
22	8.92	9.90	10.48	11.00	11.48
24	9.23	10.29	10.91	11.48	12.00
27	9.64	10.80	11.49	12.12	12.71
30	10.00	11.25	12.00	12.69	13.33
33	10.31	11.65	12.45	13.20	13.89
36	10.59	12.00	12.86	13.66	14.40
39	10.83	12.32	13.22	14.07	14.86
43	11.21	12.69	13.65	14.55	15.40
47	11.37	13.02	14.03	14.93	15.89
51	11.59	13.30	14.37	15.37	16.32
56	11.83	13.62	14.74	15.79	16.80
62	12.08	13.95	15.12	16.24	17.30
68	12.29	14.23	15.45	16.62	17.74
75	12.50	14.52	15.79	17.01	18.18
82	12.68	14.76	16.08	17.35	18.57
91	12.88	15.03	16.40	17.71	18.99
100	13.04	15.25	16.67	18.03	19.35
150	13.64	16.07	17.65	19.19	20.69
180	13.85	16.36	18.00	19.60	21.18
200	13.95	16.51	18.18	19.82	21.43
220	14.04	16.63	18.33	20.00	21.64
250	14.15	16.79	18.52	20.22	21.90

Table 3-3. Capacitors in Series (cont'd)

C2	1	1.5	2	2.2	3
1	0.50	0.60	0.666	0.69	0.75
1.5	0.60	0.75	0.857	0.89	1.00
2	0.666	0.888	1.00	1.05	1.20
2.2	0.69	0.89	1.05	1.10	1.27
3	0.75	1.00	1.20	1.27	1.50
3.3	0.77	1.03	1.24	1.31	1.57
4	0.80	1.09	1.33	1.42	1.71
4.7	0.82	1.13	1.40	1.49	1.83
5	0.833	1.15	1.43	1.53	1.87
5.6	0.848	1.18	1.47	1.58	1.95
6.8	0.87	1.22	1.54	1.66	2.08
7.5	0.88	1.25	1.58	1.69	2.14
8.2	0.89	1.26	1.60	1.73	2.19
10	0.91	1.30	1.66	1.80	2.31
12	0.923	1.33	1.71	1.85	2.40
15	0.937	1.36	1.76	1.92	2.50
18	0.947	1.38	1.80	1.96	2.57
20	0.952	1.40	1.82	1.98	2.61
22	0.956	1.40	1.83	2.00	2.64
24	0.96	1.41	1.84	2.01	2.66
27	0.964	1.42	1.86	2.03	2.70
30	0.968	1.428	1.87	2.05	2.73
33	0.970	1.43	1.88	2.06	2.75
36	0.973	1.44	1.89	2.07	2.77
39	0.975	1.444	1.90	2.08	2.79
43	0.977	1.449	1.91	2.09	2.80
47	0.979	1.45	1.92	2.10	2.82
51	0.98	1.457	1.924	2.11	2.83
56	0.982	1.461	1.93	2.12	2.84
62	0.984	1.464	1.937	2.124	2.86
68	0.985	1.467	1.94	2.13	2.87
75	0.987	1.47	1.95	2.14	2.88
82	0.988	1.473	1.952	2.142	2.89
91	0.989	1.475	1.957	2.148	2.90
100	0.991	1.478	1.96	2.153	2.91

Table 3-3. Capacitors in Series (cont'd)

C2	47	51	56	62	68	75
1	0.979	0.981	0.982	0.984	0.986	0.987
1.5	1.454	1.457	1.461	1.465	1.468	1.471
2	1.918	1.925	1.931	1.938	1.943	1.948
2.2	2.100	2.11	2.12	2.124	2.13	2.142
3	2.82	2.83	2.85	2.86	2.87	2.88
3.3	3.08	3.10	3.12	3.13	3.15	3.16
4	3.68	3.71	3.73	3.75	3.77	3.79
4.7	4.27	4.30	4.34	4.37	4.40	4.42
5	4.52	4.55	4.59	4.62	4.65	4.69
5.6	5.00	5.05	5.09	5.14	5.17	5.21
6.8	5.94	6.00	6.06	6.14	6.18	6.23
7.5	6.47	6.53	6.61	6.69	6.75	6.82
8.2	6.98	7.06	7.15	7.24	7.32	7.39
10	8.24	8.36	8.48	8.61	8.72	8.82
12	9.56	9.71	9.88	10.05	10.20	10.34
15	11.37	11.59	11.83	12.08	12.29	12.50
18	13.02	13.30	13.62	13.95	14.23	14.52
20	14.03	14.37	14.74	15.12	15.45	15.79
22	14.93	15.37	15.79	16.24	16.62	17.01
24	15.89	16.32	16.80	17.30	17.74	18.18
27	17.15	17.65	18.22	18.81	19.33	19.85
30	18.31	18.89	19.54	20.22	20.82	21.42
33	19.39	20.04	20.76	21.54	22.22	22.92
36	20.39	21.10	21.91	22.78	23.54	24.32
39	21.31	22.10	22.99	23.94	24.79	25.66
43	22.46	23.33	24.32	25.39	26.34	27.33
47	23.50	24.46	25.55	26.73	27.79	28.89
51	24.46	25.50	26.69	27.98	29.14	30.36
56	25.55	26.69	28.00	29.42	30.71	32.06
62	26.73	27.98	29.42	31.00	32.43	33.94
68	27.79	29.14	30.71	32.43	34.00	35.66
75	28.89	30.36	32.06	33.94	35.66	37.50
82	29.88	31.44	33.28	35.31	37.17	39.17
91	30.99	32.68	34.67	36.88	38.92	41.11
100	31.97	33.78	35.90	38.27	40.48	42.86

Table 3-3. Capacitors in Series (cont'd)

C2	82	91	100
1	0.988	0.989	0.990
1.5	1.473	1.476	1.478
2	1.952	1.957	1.961
2.2	2.142	2.148	2.153
3	2.89	2.90	2.91
3.3	3.17	3.19	3.20
4	3.81	3.83	3.84
4.7	4.45	4.47	4.49
5	4.71	4.74	4.76
5.6	5.24	5.28	5.30
6.8	6.28	6.32	6.37
7.5	6.87		
8.2	7.45	7.52	7.58
10	8.91	9.01	9.09
12	10.46	10.60	10.71
15	12.68	12.88	13.04
18	14.76	15.03	15.25
20	16.08	16.40	16.67
22	17.35	17.71	18.03
24	18.57	18.99	19.35
27	20.31	20.82	21.26
30	21.96	22.56	23.08
33	23.53	24.22	24.81
36	25.02	25.80	26.47
39	26.43	27.30	28.06
43	28.21	29.20	30.07
47	29.88	30.99	31.97
51	31.44	32.68	33.78
56	33.28	34.67	35.90
62	35.31	36.88	38.27
68	37.17	38.92	40.48
75	39.17	41.11	42.86
82	41.00	43.13	45.06
91	43.13	45.50	47.64
00	45.06	47.64	50.00

series have equal values, the resultant capacitance is one-third that of any of the units.

Table 3-3 gives the resultant capacitance of two capacitors in series. The table can be extended by moving the decimal point in the C1 and C2 columns an equal number of places to the right. The table can also be used for finding the total capacitance of three series capacitors by doing a two-step operation, i.e. determining the value of two capacitors and then combining the result with the remaining capacitor. C1 and C2 must be in similar units of  $\mu\text{F}$  or pF. The answers will then be in  $\mu\text{F}$  or pF.

**□Example:**

What is the capacitance of two series capacitors, having values of 47 pF and 15 pF?

Locate 47 in the C2 column and move horizontally until you reach 11.37 in the C1 column headed by the number 15. The answer is 11.37 pF. You could also have solved this problem by locating 1.5 in the C2 column, and then moving across to reach 4.7 (column C1). The answer would, of course, be 1.13 pF. Moving the decimal point one place to the right supplies an answer of 11.3.

**□Example:**

You have a number of capacitors available, but you do not have one with a capacitance of 6 pF—the value you require. What capacitor combination can you use in series to give you 6 pF?

A value of exactly 6 pF is shown in the table. It can be made by connecting a 10 pF and a 15 pF in series. Another combination which would result in a capacitance fairly close to 6 pF would be 33 pF and 7.5 pF, giving a total capacitance of 6.11 pF. Or you could use a pair of capacitors each having a value of 12 pF.

# Chapter 4

## Inductance

### UNITS OF INDUCTANCE

The basic unit of inductance is the henry. Submultiples are the millihenry and the microhenry. Use Table 4-1 to convert from one unit to another.

### VALUES OF INDUCTANCE CONVERSIONS

When working with formulas involving inductance, it is sometimes necessary to move from the basic unit of inductance to submultiples. Table 4-1 supplies the multiplication factors for making these conversions.

Table 4-1. Inductance Conversions

Given This Value	Multiply by this value to get		
	henrys	millihenrys	microhenrys
henrys	-	$10^3$	$10^6$
millihenrys	$10^{-3}$	-	$10^{-3}$
microhenrys	$10^{-6}$	$10^{-3}$	-

### INDUCTIVE REACTANCE

The reactance of a coil (inductor) varies directly with frequency and with inductance. Like capacitive reactance, coil reac-

tance or inductive reactance is measured in ohms. Inductive reactance is an effect produced by the counter-electromotive force induced across the coil. This voltage, acting in opposition to the applied voltage, reduces the amount of circuit current.

As in the case of capacitors, the coil produces a phase shift. The current lags the voltage and in a hypothetical coil (one containing no resistance) the phase angle would be 90 degrees. In practice, the phase angle is less than 90 degrees.

Table 4-2 supplies the inductive reactance of coils ranging from 10 to 100 millihenrys at frequencies ranging from 1 to 1000 kHz. The table also supplies the reactance of coils from 0.001 henry to 10 henrys from frequencies of 25 Hz to 1000 kHz.

The behavior of an inductor is opposite that of a capacitor. Increasing the frequency or the inductance increases the reactance proportionately, and vice versa. Thus, doubling either the frequency or the inductance will double the reactance. See also Table 4-3.

**□Example:**

What is the reactance of a coil having an inductance of 0.005 henry at a frequency of 1 kHz?

Locate 1000 hertz in the frequency column. Move to the right to the column headed by 0.005. The inductive reactance is 31.40 ohms.

**□Example:**

What is the reactance of a 5-henry choke coil at a frequency of 60 Hz.

Locate 60 Hz in the frequency column and move to the right, finding an inductive reactance of 1884 ohms in the column headed by the number 5. Note that the reactance of this coil at twice the frequency (120 Hz) is 3768 ohms, double its original value.

**□Example:**

What is the reactance of a 1-henry coil at a frequency of 150 Hz?

A frequency of 150 Hz is not listed in the table. Locate 50 Hz, find the corresponding reactance of 314 ohms and multiply this value by 3 to get your answer. You could also get the same result by locating 75 Hz in the Table, finding the reactance of 471 ohms and multiplying this result by 2. In either case the answer is 942 ohms.

Table 4-2. Inductive Reactance (ohms)

Frequency (kHz)	Inductance (millihenrys)				
	10	20	30	40	50
1	62.8	125.6	188.4	251.2	314
2	125.6	251.2	376.8	502.4	628
3	188.4	376.8	565.2	753.6	942
4	251.2	502.4	753.6	1004.8	1256
5	314	628	942	1256	1570
6	376.8	753.6	1130.4	1507.2	1884
7	439.6	879.2	1318.8	1758.4	2198
8	502.4	1004.8	1507.2	2009.6	2512
9	565.2	1130.4	1695.6	2260.8	2826
10	628	1256	1884	2512	3140
20	1256	2512	3768	5024	6280
25	1570	3140	4710	6280	7850
30	1884	3768	5652	7536	9420
40	2512	5024	7536	10048	12560
50	3140	6280	9420	12560	15700
60	3768	7536	11304	15072	18840
70	4396	8792	13188	17584	21980
80	5024	10048	15072	20096	25120
90	5652	11304	16956	22608	28260
100	6280	12560	18840	25120	31400
150	9420	18840	28260	37680	47100
200	12560	25120	37680	50240	62800
250	15700	31400	47100	62800	78500
300	18840	37680	56520	75360	94200
350	21980	43960	65940	87920	109900
400	25120	50240	75360	100480	125600
450	28260	56520	84780	113040	141300
500	31400	62800	94200	125600	157000
550	34540	69080	103620	138160	172700
600	37680	75360	113040	150720	188400
650	40820	81640	122460	163280	204100
700	43960	87920	131880	175840	219800
800	50240	100480	150720	200960	251200
900	56520	113040	168560	226080	282600
1000	62800	125600	188400	251200	314000

Table 4-2. Inductive Reactance (ohms) (cont'd)

Frequency (kHz)	Inductance (millihenrys)				
	60	70	80	90	100
1	376.8	439.6	502.4	565.2	628
2	753.6	879.2	1004.8	1130.4	1256
3	1130.4	1318.8	1507.2	1695.6	1884
4	1507.2	1758.4	2009.6	2260.8	2512
5	1884	2198	2512	2826	3140
6	2260.8	2637.6	3014.4	3391.2	3768
7	2637.6	3077.2	3516.8	3956.4	4396
8	3014.4	3516.8	4019.2	4521.6	5024
9	3391.2	3856.4	4521.6	5086.8	5652
10	3768	4396	5024	5652	6280
20	7536	8792	10048	11304	12560
25	9420	10990	12560	14130	15700
30	11304	13188	15072	16956	18840
40	15072	17584	20096	22608	25120
50	18840	21980	25120	28260	31400
60	22608	26376	30144	33912	37680
70	26376	30772	35168	39564	43960
80	30144	35168	40192	45216	50240
90	33912	38564	45216	50868	56520
100	37680	43960	50240	56520	62800
150	56520	65940	75360	84780	94200
200	75360	87920	100480	113040	125600
250	94200	109900	125600	141300	157000
300	113040	131880	150720	169560	188400
350	131880	153860	175840	197820	219800
400	150720	175840	200960	226080	251200
450	169560	192820	226080	254340	282600
500	188400	219800	251200	282600	314000
550	207240	241780	276320	310860	345400
600	226080	263760	301440	339120	376800
650	244920	285740	326560	367380	408200
700	263760	307720	351680	395640	439600
800	301440	351680	401920	452160	502400
900	339120	385640	452160	508680	565200
1000	376800	439600	502400	565200	628000

Table 4-2. Inductive Reactance (ohms) (cont'd)

Frequency (Hz)	Inductance (henrys)				
	1	2	3	4	5
25	157.0	314.0	471.0	628.0	785
30	188.4	376.8	565.2	753.6	942
35	219.8	439.6	659.4	879.2	1099
40	251.2	502.4	753.6	1004.8	1256
45	282.6	565.2	847.8	1130.4	1413
50	314.0	628.0	942.0	1256.0	1570
55	345.4	690.8	1036.2	1318.6	1727
60	376.8	753.6	1130.4	1507.2	1884
65	408.2	816.4	1224.6	1632.8	2041
70	439.6	879.2	1318.8	1758.4	2198
75	471.0	942.0	1413.0	1884.0	2355
80	502.4	1004.8	1507.2	2009.6	2512
85	533.8	1067.6	1601.4	2135.2	2669
90	565.2	1130.4	1695.6	2260.8	2826
95	596.6	1193.2	1789.8	2386.4	2983
100	628.0	1256.0	1884.0	2512.0	3140
120	753.6	1507.2	2260.8	3014.4	3768
200	1256.0	2512.0	3768.0	5024.0	6280
240	1507.2	3014.4	4521.6	6028.8	7536
250	1570.0	3140.0	4710.0	6280.0	7850
300	1884	3768	5652	7536	9420
350	2198	4396	6594	8792	10990
360	2260	4522	6783	9044	11305
400	2512	5024	7536	10048	12560
450	2826	5652	8478	11304	14130
500	3140	6280	9420	12560	15700
550	3454	6908	10362	13816	17270
600	3768	7536	11304	15072	18840
650	4082	8164	12246	16328	20410
700	4396	8792	13188	17584	21980
750	4710	9420	14130	18840	23550
800	5024	10048	15072	20096	25120
850	5338	10676	16014	21352	26690
900	5652	11304	16956	22608	28260
1000	6280	12560	18840	25120	31400

Table 4-2. Inductive Reactance (ohms) (cont'd)

Frequency (Hz)	Inductance (henrys)				
	.001	.002	.003	.005	.01
25	.1570	.3140	.4710	.785	1.570
30	.1884	.3768	.5652	.942	1.884
40	.2512	.5024	.7536	1.256	2.512
45	.2826	.5652	.8478	1.413	2.826
50	.3140	.6280	.9420	1.570	3.140
55	.3454	.6908	1.0362	1.727	3.454
60	.3768	.7536	1.1304	1.884	3.768
65	.4082	.8164	1.2246	2.041	4.082
70	.4396	.8792	1.3188	2.198	4.396
75	.4710	.9420	1.4130	2.355	4.710
80	.5024	1.0048	1.5072	2.512	5.024
85	.5338	1.0676	1.6014	2.669	5.338
90	.5652	1.1304	1.6956	2.826	5.652
95	.5966	1.1932	1.7898	2.983	5.966
100	.6280	1.2560	1.8840	3.140	6.280
110	.6908	1.3816	2.0724	3.454	6.908
120	.7536	1.5072	2.2608	3.768	7.536
150	.942	1.8840	2.826	4.710	9.420
175	1.099	2.1980	3.297	5.495	10.990
200	1.256	2.5120	3.768	6.280	12.560
250	1.570	3.140	4.710	7.85	15.70
300	1.884	3.768	5.652	9.42	18.84
350	2.198	4.396	6.594	10.99	21.98
400	2.512	5.024	7.536	12.56	25.12
500	3.140	6.280	9.420	15.70	31.40
550	3.454	6.908	10.362	17.27	34.54
600	3.768	7.536	11.304	18.84	37.68
650	4.082	8.164	12.246	20.41	40.82
700	4.396	8.792	13.188	21.98	43.96
750	4.710	9.420	14.130	23.55	47.10
800	5.024	10.048	15.072	25.12	50.24
850	5.338	10.676	16.014	26.69	53.38
900	5.652	11.304	16.956	28.26	56.52
950	5.966	11.932	17.898	29.83	59.66
1000	6.280	12.560	18.840	31.40	62.80

Table 4-2. Inductive Reactance (ohms) (cont'd)

Frequency (Hz)	Inductance (henrys)				
	6	7	8	9	10
25	942.0	1099.0	1256.0	1413.0	1570
30	1130.4	1318.8	1507.2	1695.6	1884
35	1318.8	1538.6	1758.4	1978.2	2198
40	1507.2	1758.4	2009.6	2260.8	2512
45	1695.6	1978.2	2260.8	2543.4	2826
50	1884.0	2198.0	2512.0	2826.0	3140
55	2072.4	2417.8	2763.2	3108.6	3454
60	2260.8	2637.6	3014.4	3391.2	3768
65	2449.2	2857.4	3265.6	3673.8	4082
70	2637.6	3077.2	3516.8	3956.4	4396
75	2826.0	3297.0	3768.0	4239.0	4710
80	3014.4	3516.8	4019.2	4521.6	5024
85	3202.8	3736.6	4270.4	4804.2	5338
90	3391.2	3956.4	4521.6	5086.8	5652
95	3579.6	4176.2	4772.8	5396.4	5966
100	3768.0	4396.0	5024.0	5652.0	6280
120	4521.6	5275.2	6028.8	6782.4	7536
200	7536.0	8792.0	10048.0	11304	12560
240	9043.2	10550.4	12057.6	13565	15072
250	9420.0	10990.0	12460.0	14130	15700
300	11304	13188	15072	16956	18840
350	13188	15386	17584	19782	21980
360	13414	15826	18086	20347	22608
400	15072	17584	20096	22608	25120
450	16956	19782	22608	25434	28260
500	18840	21980	25120	28260	31400
550	20724	24178	27632	31086	34540
600	22608	26376	30124	33912	37680
650	24492	28574	32656	36738	40820
700	26376	30772	35168	39564	43960
750	28260	32970	37680	42390	47100
800	30144	35168	40192	45216	50240
850	32028	37366	42704	48042	53380
900	33912	39564	45216	50868	56520
1000	37680	43960	50240	56520	62800

Table 4-3. Capacitive Reactance At Spot Frequencies

	50 Hz	100 Hz	1 KHz	10 KHz	100 KHz	1 MHz	10 MHz	100 MHz
1 $\mu$ H	—	—	—	—	0.63	6.3	63	630
5 $\mu$ H	—	—	—	0.31	3.1	31	310	3.1 K
10 $\mu$ H	—	—	—	0.63	6.3	63	630	6.3 K
50 $\mu$ H	—	—	0.31	3.1	31	310	3.1 K	31 K
100 $\mu$ H	—	—	0.63	6.3	63	630	6.3 K	63 K
250 $\mu$ H	—	0.16	1.6	16	160	1.6 K	16 K	160 K
1 mH	0.31	0.63	6.3	63	630	6.3 K	63 K	630 K
2.5mH	0.8	1.6	16	160	1.6 K	16 K	160 K	1.6 M
10 mH	3.1	6.3	63	630	6.3 K	63 K	630 K	6.3 M
25 mH	8	16	160	1.6 K	16 K	160 K	1.6 M	—
100mH	31	63	630	6.3 K	63 K	630 K	6.3 M	—
1 H	310	630	6.3 K	63 K	630 K	6.3 M	—	—
5 H	1.5 K	3.1 K	31 K	310 K	3.1 M	—	—	—
10 H	3.1 K	6.3 K	63 K	630 K	6.3 M	—	—	—
100H	31 K	63 K	630 K	6.3 M	—	—	—	—

Values in ohms.

## LC PRODUCT FOR RESONANCE

Table 4-4 shows the relationship between the wavelength in meters, the frequency in kilohertz and the inductance-capacitance product ( $L \times C$ ) required to produce resonance. The inductance is in microhenrys and the capacitance is in microfarads.

In an LC circuit a condition of resonance is reached when the reactive elements are equal—that is, when the inductive and capacitive reactances are identical. When the inductance and the capacitance are both in microunits (microhenrys and microfarads), the resonant frequency will be in kilohertz.

To find the resonant frequency without resorting to formulas, multiply the values of L and C, first converting these to microhenrys and microfarads. Knowing the LC product, find the resonant frequency by using Table 4-4. At the same time the table also supplies the wavelength in meters.

### Example:

What is the wavelength in meters of a circuit when the inductance is 221 uh and the capacitance is 100 pf?

The table requires that the capacitance be in microfarads. 100  $\mu$ F is equivalent to 0.0001  $\mu$ F. Multiply 221 by .0001. The answer will be 0.0221. Locate this value in the  $L \times C$  column in the table. You will find that the frequency in kilohertz is 1071 and the corresponding wavelength is 280 meters.

Table 4-4. LC Product for Resonance

Wave-length (meters)	Frequency (kHz)	L x C	Wave-length (meters)	Frequency (kHz)	L x C
1	300,000	0.0000003	270	1,111	0.0205
2	150,000	0.0000111	280	1,071	0.0221
3	100,000	0.0000018	290	1,034	0.0237
4	75,000	0.0000045	300	1,000	0.0253
5	60,000	0.0000057	310	968	0.0270
6	50,000	0.0000101	320	938	0.0288
7	42,900	0.0000138	330	909	0.0306
8	37,500	0.0000180	340	883	0.0325
9	33,333	0.0000228	350	857	0.0345
10	30,000	0.0000282	360	834	0.0365
20	15,000	0.0001129	370	811	0.0385
30	10,000	0.0002530	380	790	0.0406
40	7,500	0.0004500	390	769	0.0428
50	6,000	0.0007040	400	750	0.0450
60	5,000	0.0010140	410	732	0.0473
70	4,290	0.0013780	420	715	0.0496
80	3.750	0.0018010	430	698	0.0520
90	3,333	0.0022800	440	682	0.0545
100	3,000	0.00282	450	667	0.0570
110	2,727	0.00341	460	652	0.0596
120	2,500	0.00405	470	639	0.0622
130	2,308	0.00476	480	625	0.0649
140	2,143	0.00552	490	612	0.0676
150	2,000	0.00633	500	600	0.0704
160	1,875	0.00721	505	594	0.0718
170	1,764	0.00813	510	588	0.0732
180	1,667	0.00912	515	583	0.0747
190	1,579	0.01015	520	577	0.0761
200	1,500	0.01126	525	572	0.0776
210	1,429	0.01241	530	566	0.0791
220	1,364	0.01362	535	561	0.0806
230	1,304	0.01489	540	556	0.0821
240	1,250	0.01621	545	551	0.0836
250	1,200	0.01759	550	546	0.0852
260	1,154	0.01903	555	541	0.0867

Table 4-4. LC Product for Resonance (cont'd)

Wave-length (meters)	Frequency (kHz)	$L \times C$	Wave-length (meters)	Frequency (kHz)	$L \times C$
560	536	0.0883	735	408	0.1521
565	531	0.0899	740	405	0.1541
570	527	0.0915	745	403	0.1562
575	522	0.0931	750	400	0.1583
580	517	0.0947	755	397	0.1604
585	513	0.0963	760	395	0.1626
590	509	0.0980	765	392	0.1647
595	504	0.0996	770	390	0.1669
600	500	0.1013	775	387	0.1690
605	496	0.1030	780	385	0.1712
610	492	0.1047	785	382	0.1734
615	488	0.1065	790	380	0.1756
620	484	0.1082	795	377	0.1779
625	480	0.1100	800	375	0.1801
630	476	0.1117	805	373	0.1824
635	472	0.1135	810	370	0.1847
640	469	0.1153	815	368	0.1870
645	465	0.1171	820	366	0.1893
650	462	0.1189	825	364	0.1916
655	458	0.1208	830	361	0.1939
660	455	0.1226	835	359	0.1962
665	451	0.1245	840	357	0.1986
670	448	0.1264	845	355	0.201
675	444	0.1283	850	353	0.203
680	441	0.1302	855	351	0.205
685	438	0.1321	860	349	0.208
690	435	0.1340	865	347	0.211
695	432	0.1360	870	345	0.213
700	429	0.1379	875	343	0.216
705	426	0.1399	880	341	0.218
710	423	0.1419	885	339	0.220
715	420	0.1439	890	337	0.223
720	417	0.1459	895	335	0.225
725	414	0.1479	900	333	0.228
730	411	0.1500	905	331	0.231

**Table 4-4. LC Product for Resonance (cont'd)**

Wave-length (meters)	Frequency (kHz)	$L \times C$	Wave-length (meters)	Frequency (kHz)	$L \times C$
910	330	0.233	955	314	0.257
915	328	0.236	960	313	0.260
920	326	0.238	965	311	0.262
925	324	0.241	970	309	0.265
930	323	0.243	975	308	0.268
935	321	0.246	980	306	0.270
940	319	0.249	985	305	0.273
945	317	0.251	990	303	0.276
950	316	0.254	995	302	0.279
			1000	300	0.282

**□Example:**

What is the resonant frequency of a circuit whose capacitance has a value of 250 pF and an inductance of 136  $\mu$ H?

The inductance value can be used as it is, but the capacitance must be changed to microfarads. 250 pF is equivalent to 0.00025  $\mu$ F. The product of 0.00025 and 136 is 0.0340. The table does not list such a value, but it does have a value that is close. The  $L \times C$  column shows this to be 0.0345 with a corresponding frequency in kilohertz of 857. The wavelength is 350 meters.

**□Example:**

You want a circuit that will be resonant at 5 megaHertz. What must be the value of the LC product?

5 megahertz is equal to 5000 kilohertz. The table shows that the LC product is 0.0010140. Any combination of inductance and capacitance producing this product will be resonant at 5 MHz.



## Chapter 5

# Impedance

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The impedance of a series RC, RL, or RLC circuit is the vector sum of the individual reactances and resistance. Table 5-1 supplies the impedance in ohms, when the values of R and X are known. X can represent either inductive or capacitive reactance, or X may be the vector sum of these reactive components when both are present in the circuit.

If you have both types of reactance, subtract one from the other to get the value of X. It makes no difference which reactive component (inductance or capacitance) has the larger reactance. Subtract the value of the smaller reactance from that of the larger to obtain the value of X.

Table 5-1 covers a range of X and of R from 1 ohm to 35 ohms. The table can be extended by moving the decimal point an equal number of places for R, X, and the answer. Thus, if you had a resistor with a value of 30 ohms and a reactance with a value of 90 ohms, you could consider 3 in the R column as 30, and 9 in the X column as 90. The value of impedance would be shown in the table as 9.49 ohms, but moving the decimal point one place to the right gives an impedance of 94.9 ohms. Table 5-2 includes common impedance formulas.

### □Example:

A circuit consists of a 5-ohm resistor, a coil having an inductive reactance of 35 ohms and a capacitor having a capacitive reactance of 21 ohms. What is the impedance of this circuit?

Table 5-1. Impedance (ohms) for Series R and X

X	1	2	3	4	5	6
1	1.41	2.24	3.16	4.12	5.10	6.08
2	2.24	2.83	3.61	4.47	5.39	6.32
3	3.16	3.61	4.24	5.00	5.83	6.71
4	4.12	4.47	5.00	5.57	6.40	7.21
5	5.10	5.39	5.83	6.40	7.07	7.81
6	6.08	6.32	6.71	7.21	7.81	8.48
7	7.07	7.28	7.62	8.06	8.60	9.22
8	8.06	8.25	8.54	8.94	9.43	10.00
9	9.06	9.22	9.49	9.85	10.29	10.81
10	10.05	10.19	10.44	10.77	11.18	11.66
11	11.04	11.18	11.40	11.70	12.08	12.52
12	12.04	12.16	12.36	12.64	13.00	13.41
13	13.03	13.15	13.34	13.60	13.92	14.31
14	14.03	14.14	14.31	14.56	14.86	15.23
15	15.03	15.13	15.29	15.52	15.81	16.15
16	16.03	16.12	16.28	16.49	16.76	17.09
17	17.03	17.12	17.26	17.46	17.72	18.03
18	18.03	18.11	18.25	18.44	18.68	18.97
19	19.03	19.10	19.24	19.42	19.65	19.92
20	20.02	20.05	20.22	20.40	20.62	20.88
21	21.02	21.10	21.21	21.38	21.59	21.84
22	22.02	22.09	22.20	22.36	22.56	22.80
23	23.02	23.09	23.19	23.35	23.54	23.75
24	24.02	24.08	24.19	24.33	24.52	24.74
25	25.02	25.08	25.18	25.32	25.50	25.71
26	26.02	26.08	26.17	26.31	26.48	26.68
27	27.02	27.07	27.16	27.29	27.46	27.66
28	28.02	28.07	28.16	28.28	28.44	28.64
29	29.02	29.07	29.15	29.27	29.43	29.61
30	30.02	30.07	30.15	30.27	30.41	30.59
31	31.02	31.06	31.14	31.26	31.40	31.58
32	32.01	32.06	32.14	32.24	32.39	32.55
33	33.01	33.06	33.14	33.24	33.38	33.54
34	34.01	34.06	34.14	34.24	34.37	34.53
35	35.01	35.06	35.13	35.23	35.36	35.51

Table 5-1. Impedance (ohms) for Series R and X (cont'd)

X	R					
	7	8	9	10	11	12
1	7.07	8.06	9.06	10.05	11.04	12.04
2	7.28	8.25	9.22	10.19	11.18	12.16
3	7.62	8.54	9.49	10.44	11.40	12.36
4	8.06	8.94	9.85	10.77	11.70	12.64
5	8.60	9.43	10.29	11.18	12.08	13.00
6	9.22	10.00	10.81	11.66	12.52	13.41
7	9.89	10.63	11.40	12.20	13.03	13.89
8	10.63	11.31	12.04	12.80	13.60	14.42
9	11.40	12.04	12.72	13.45	14.21	15.00
10	12.20	12.80	13.45	14.14	14.86	15.62
11	13.03	13.60	14.21	14.86	15.55	16.27
12	13.89	14.42	15.00	15.62	16.27	16.97
13	14.76	15.26	15.81	16.40	17.02	17.69
14	15.65	16.12	16.64	17.20	17.80	18.43
15	16.55	17.00	17.49	18.02	18.60	19.20
16	17.46	17.89	18.36	18.87	19.42	20.00
17	18.38	18.79	19.24	19.72	20.25	20.81
18	19.31	19.70	20.12	20.59	21.10	21.63
19	20.25	20.62	21.02	21.47	21.95	22.47
20	21.19	21.54	21.93	22.36	22.83	23.32
21	22.14	22.47	22.85	23.26	23.71	24.19
22	23.09	23.41	23.77	24.17	24.60	25.06
23	24.04	24.35	24.70	25.08	25.50	25.94
24	25.00	25.30	25.63	26.00	26.40	26.83
25	25.95	25.25	26.57	26.93	27.31	27.73
26	26.93	27.20	27.51	27.86	28.23	28.64
27	27.89	28.16	28.46	28.79	29.15	29.55
28	28.86	29.12	29.41	29.73	30.08	30.46
29	29.83	30.08	30.36	30.68	31.02	31.38
30	30.81	31.05	31.32	31.62	31.96	32.31
31	31.78	31.93	32.25	32.56	32.90	33.24
32	32.75	32.98	33.24	33.52	33.85	34.18
33	33.74	33.96	34.21	34.49	34.79	35.12
34	34.72	34.93	35.17	35.44	35.74	36.06
35	35.70	35.90	36.14	36.40	36.69	37.00

Table 5-1. Impedance (ohms) for Series R and X (cont'd)

	R					
X	13	14	15	16	17	18
1	13.03	14.03	15.03	16.03	17.03	18.03
2	13.15	14.14	15.13	16.12	17.12	18.11
3	13.34	14.31	15.29	16.28	17.26	18.25
4	13.60	14.56	15.52	16.49	17.46	18.44
5	13.92	14.86	15.81	16.76	17.72	18.68
6	14.31	15.23	16.15	17.09	18.03	18.97
7	14.76	15.65	16.55	17.47	18.38	19.31
8	15.26	16.12	17.00	17.89	18.79	19.70
9	15.81	16.64	17.49	18.36	19.24	20.12
10	16.40	17.20	18.02	18.87	19.72	20.59
11	17.02	17.80	18.60	19.42	20.25	21.10
12	17.69	18.43	19.20	20.00	20.81	21.63
13	18.38	19.10	19.84	20.62	21.40	22.20
14	19.10	19.79	20.51	21.26	22.02	22.80
15	19.84	20.51	21.21	21.93	22.67	23.43
16	20.62	21.26	21.93	22.63	23.35	24.08
17	21.40	22.02	22.67	23.35	24.04	24.76
18	22.20	22.80	23.43	24.08	24.76	25.46
19	23.02	23.60	24.20	24.84	25.50	26.17
20	23.85	24.41	25.00	25.61	26.25	26.91
21	24.70	25.24	25.81	26.40	27.02	27.66
22	25.55	26.08	26.63	27.20	27.80	28.43
23	26.42	26.93	27.46	28.02	28.60	29.21
24	27.29	27.78	28.30	28.84	29.41	30.00
25	28.18	28.65	29.15	29.68	30.23	30.81
26	29.07	29.53	30.02	30.53	31.06	31.62
27	29.97	30.41	30.89	31.38	31.91	32.45
28	30.87	31.30	31.77	32.35	32.76	33.29
29	31.78	32.21	32.65	33.12	33.62	34.14
30	32.70	33.11	33.54	34.00	34.48	34.99
31	33.62	34.01	34.44	34.89	35.36	35.85
32	34.54	35.50	35.90	36.33	36.78	37.26
33	35.47	35.85	36.25	36.67	37.12	37.59
34	36.40	36.77	37.16	37.58	38.01	38.47
35	37.34	37.60	38.08	38.48	38.91	39.36

Table 5-1. Impedance (ohms) for Series R and X (cont'd)

X	R					
	19	20	21	22	23	24
1	19.03	20.02	21.02	22.02	23.02	24.02
2	19.10	20.10	21.10	22.09	23.09	24.08
3	19.24	20.22	21.21	22.20	23.19	24.19
4	19.42	20.40	21.38	22.36	23.35	24.33
5	19.65	20.62	21.59	22.56	23.54	24.52
6	19.92	20.88	21.84	22.80	23.77	24.74
7	20.25	21.18	22.14	23.09	24.04	25.00
8	20.62	21.54	22.47	23.41	24.35	25.30
9	21.02	21.93	22.85	23.77	24.70	25.63
10	21.47	22.36	23.26	24.17	25.08	26.00
11	21.95	22.82	23.71	24.60	25.50	26.40
12	22.47	23.32	24.19	25.06	25.94	26.83
13	23.02	23.85	24.70	25.55	26.42	27.29
14	23.60	24.41	25.24	26.08	26.93	27.78
15	24.20	25.00	25.81	26.63	27.46	28.30
16	24.84	25.61	26.40	27.20	28.02	28.84
17	25.50	26.25	27.02	27.80	28.60	29.41
18	26.17	26.91	27.66	28.43	29.21	30.00
19	26.86	27.59	28.32	29.07	29.83	30.61
20	27.59	28.28	29.00	29.73	30.48	31.24
21	28.32	29.00	29.70	30.41	31.14	31.89
22	29.07	29.73	30.41	31.11	31.83	32.56
23	29.83	30.48	31.14	31.83	32.52	33.24
24	30.61	31.24	31.89	32.56	33.24	33.94
25	31.40	32.02	32.55	33.30	33.97	34.74
26	32.20	32.80	33.42	34.06	34.71	35.38
27	33.02	33.60	34.21	34.83	35.47	36.13
28	33.85	34.41	35.01	35.61	36.24	36.88
29	34.67	35.23	35.81	36.40	37.01	37.64
30	35.51	36.06	36.62	37.20	37.80	38.42
31	36.36	36.89	37.44	38.01	38.60	39.21
32	37.22	37.73	38.28	38.83	39.41	40.00
33	38.08	38.59	39.12	39.66	40.22	40.81
34	38.95	39.45	39.96	40.40	41.05	41.62
35	39.82	40.31	40.82	41.34	41.88	42.44

Table 5-1. Impedance (ohms) for Series R and X (cont'd)

X	R					
	25	26	27	28	29	30
1	25.02	26.02	27.02	28.02	29.02	30.02
2	25.08	26.08	27.07	28.07	29.07	30.07
3	25.18	26.17	27.17	28.16	29.15	30.15
4	25.32	26.31	27.29	28.28	29.27	30.27
5	25.50	26.46	27.46	28.44	29.43	30.41
6	25.71	26.68	27.66	28.64	29.61	30.59
7	25.98	26.93	27.89	28.86	29.83	30.81
8	26.25	27.20	28.16	29.12	30.08	31.05
9	26.57	27.51	28.46	29.41	30.36	31.32
10	26.93	27.86	28.79	29.73	30.68	31.62
11	27.31	28.23	29.15	30.08	31.02	31.95
12	27.73	28.64	29.55	30.46	31.38	32.31
13	28.18	29.07	29.97	30.87	31.78	32.60
14	28.65	29.53	30.41	31.30	32.20	33.11
15	29.15	30.02	30.89	31.77	32.64	33.54
16	29.68	30.53	31.38	32.25	33.12	33.80
17	30.23	31.06	31.91	32.76	33.62	34.48
18	30.81	31.62	32.45	33.29	34.13	34.99
19	31.40	32.20	33.02	33.85	34.67	35.51
20	32.02	32.80	33.60	34.41	35.23	36.06
21	32.65	33.42	34.21	35.01	35.81	36.62
22	33.30	34.06	34.83	35.61	36.40	37.20
23	33.97	34.71	35.47	36.24	37.01	37.80
24	34.66	35.38	36.13	36.88	37.64	38.42
25	35.36	36.07	36.70	37.54	38.29	39.05
26	36.07	36.77	37.48	38.21	38.95	39.60
27	36.70	37.48	38.18	38.80	39.62	40.36
28	37.54	38.21	38.71	39.50	40.31	41.04
29	38.29	38.95	39.62	40.31	41.01	41.73
30	39.05	39.60	40.36	41.04	41.73	42.43
31	39.81	40.46	41.11	41.77	42.44	43.14
32	40.61	41.23	41.87	42.52	43.19	43.86
33	41.40	42.01	42.64	43.28	43.93	44.50
34	42.20	42.80	43.42	44.05	44.69	45.34
35	43.01	43.60	44.20	44.82	45.45	46.00

Table 5-1. Impedance (ohms) for Series R and X (cont'd)

X	31	32	33	34	R
1	31.01	32.02	33.02	34.02	35.01
2	31.06	32.06	33.06	34.06	35.06
3	31.14	32.14	33.14	34.13	35.13
4	31.26	32.25	33.24	34.23	35.23
5	31.40	32.39	33.38	34.37	35.36
6	31.57	32.56	33.54	34.53	35.51
7	31.78	32.76	33.74	34.71	35.69
8	32.02	32.99	33.96	34.93	35.90
9	32.28	33.24	34.21	35.17	36.14
10	32.57	33.53	34.48	35.36	36.40
11	32.89	33.85	34.79	35.74	36.69
12	33.24	34.18	35.11	36.06	36.80
13	33.62	34.53	35.48	36.40	37.34
14	34.02	34.93	35.85	36.77	37.60
15	34.44	35.34	36.25	37.16	38.08
16	34.89	35.78	36.67	37.58	38.48
17	35.37	36.24	37.12	38.01	38.90
18	35.85	36.72	37.59	38.47	39.36
19	36.36	37.22	38.08	38.95	39.82
20	36.89	37.74	38.59	39.46	40.31
21	37.44	38.28	39.12	39.96	40.82
22	38.01	38.83	39.66	40.40	41.34
23	38.60	39.41	40.22	41.05	41.88
24	39.21	40.00	40.80	41.63	42.44
25	39.81	40.61	41.40	42.20	43.01
26	40.46	41.23	42.01	42.80	43.60
27	41.11	41.87	42.64	43.42	44.20
28	41.77	42.52	43.28	44.05	44.82
29	42.44	43.19	43.93	44.69	45.45
30	43.14	43.86	44.50	45.34	46.00
31	43.84	44.55	45.28	46.01	46.76
32	44.55	45.26	45.97	46.69	47.42
33	45.28	45.98	46.68	47.38	48.10
34	46.01	46.69	47.38	48.08	48.70
35	46.75	47.42	48.10	48.70	49.40

**Table 5-2. Impedance Formulas**

Diagram	Impedance	Magnitude	Phase Angle	PHASE ANGLE $\phi = \tan^{-1} \frac{X}{R}$	PHASE ANGLE of the Admittance $16 \cdot \text{rad}^{-1} \frac{X}{R}$
				Admittance $Y = \frac{1}{Z} \text{ mhos}$	$\text{mhos}^{-1} \frac{X}{R}$
	$R$	$R$	0	0	$\frac{1}{R}$
	$j\omega L$	$\omega L$	$+\frac{\pi}{2}$	$-\frac{1}{\omega L}$	
	$-\frac{1}{j\omega C}$	$\frac{1}{\omega C}$	$-\frac{\pi}{2}$	$j\omega C$	
	$j\omega(L_1 + L_2 \pm 2M)$	$\omega(L_1 + L_2 \pm 2M)$	$+\frac{\pi}{2}$	$-\frac{1}{\omega(L_1 + L_2 \pm 2M)}$	
	$-j\omega(\frac{1}{C_1} + \frac{1}{C_2})$	$\frac{1}{\omega}(\frac{1}{C_1} + \frac{1}{C_2})$	$-\frac{\pi}{2}$	$j\omega \frac{C_1 C_2}{C_1 + C_2}$	
	$R + j\omega L$	$\sqrt{[R^2 + \omega^2 L^2]}$	$\tan^{-1} \frac{\omega L}{R}$	$\frac{R - j\omega L}{R^2 + \omega^2 L^2}$	
	$R - j\frac{1}{\omega C}$	$\frac{1}{\omega C}(1 + \omega^2 C^2 R^2)^{1/2}$	$-\tan^{-1} \frac{1}{\omega CR}$	$\frac{R + j\frac{1}{\omega C}}{R^2 + \frac{1}{\omega^2 C^2}}$	
	$j\left(\omega L - \frac{1}{\omega C}\right)$	$\left(\omega L - \frac{1}{\omega C}\right)$	$\pm \frac{\pi}{2}$	$\pm \frac{\omega C}{1 - \omega^2 C^2}$	

Table 5-2. Impedance Formulas (cont'd)

Diagram	Impedance	Magnitude	Phase Angle	Admittance
	$R + i\left(\omega L - \frac{1}{\omega C}\right)$	$\left[R + j\omega - \frac{1}{\omega^2 C^2}\right]^{-1}$	$\tan^{-1} \left( \frac{\omega L - \frac{1}{\omega C}}{R} \right)$	$\frac{R-1}{R^2 + (\omega L - \frac{1}{\omega C})^2}$
	$\frac{R_1 R_2}{R_1 + R_2}$	$\frac{R_1 R_2}{R_1 + R_2}$	0	$\left(\frac{1}{R_1} + \frac{1}{R_2}\right)^{-1}$
	$\frac{1}{\omega(C_1 + CR)}$	$\frac{1}{\omega(C_1 + CR)}$	$-\frac{\pi}{2}$	$j(C_1 + CR)$
	$j\omega \left[ \frac{L_1 L_2 - M^2}{L_1 + L_2 \pm 2M} \right]$	$\omega \left[ \frac{L_1 L_2 - M^2}{L_1 + L_2 \pm 2M} \right]$	$+\frac{\pi}{2}$	$-j\frac{1}{\omega} \left[ \frac{L_1 + L_2 \pm 2M}{L_1 L_2 - M^2} \right]$
	$\omega LR \left[ \frac{\omega L + jR}{R^2 + \omega^2 L^2} \right]$	$\frac{\omega LR}{R^2 + \omega^2 L^2}$	$\tan^{-1} \frac{R}{\omega L}$	$\frac{1}{R} - j\frac{1}{\omega L}$
	$\frac{R_1(1-j\omega C)}{1+j\omega C^2 R_1^2}$	$\frac{R_1}{(1+j\omega C^2 R_1^2)^{1/2}}$	$-\tan^{-1} \omega CR$	$\frac{1}{R} + j\omega C$
	$j\frac{\omega L}{1-\omega^2 LC}$	$\frac{j\omega L}{1-\omega^2 LC}$	$\pm \frac{\pi}{2}$	$j \left( \omega C - \frac{1}{\omega L} \right)$
	$\frac{1}{\frac{1}{R} - j\left(\frac{1}{\omega L} + \frac{1}{\omega C}\right)}$	$\left[\frac{1}{R} + \left(\frac{1}{\omega L} + \frac{1}{\omega C}\right)^2\right]^{-1}$	$\tan^{-1} \left( \frac{1}{R} \left( \frac{1}{\omega L} + \frac{1}{\omega C} \right) \right)$	$\frac{1}{R} + j \left( \omega C - \frac{1}{\omega L} \right)$
	$R_1 \frac{(R_1 + R_2) + j\omega^2 L^2 - j\omega R_2}{(R_1 + R_2)^2 + \omega^2 L^2}$	$R_2 \frac{R_1^2 + \omega^2 R_2^2}{(R_1 + R_2)^2 + \omega^2 L^2}$	$\tan^{-1} \frac{\omega^2 R_2^2}{R_1(R_1 + R_2) + \omega^2 L^2}$	$\frac{R_1(R_1 + R_2) + \omega^2 R_2^2 - j\omega R_2}{R_2(R_1 + R_2)^2 + \omega^2 L^2}$

**Table 5-2. Impedance Formulas (cont'd)**

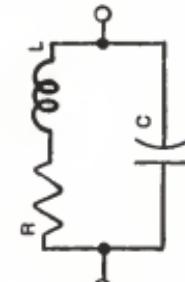
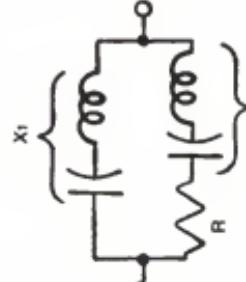
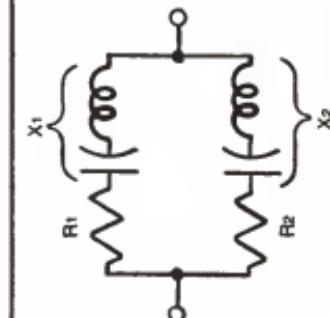
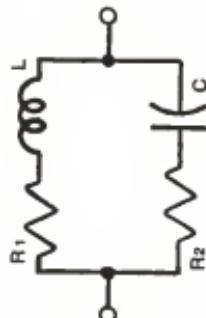
		PHASE ANGLE of the Admittance	
		is = $\tan^{-1} \frac{X}{R}$	
IMPEDANCE $Z = R + jX$ ohms	PHASE ANGLE $\phi = \tan^{-1} \frac{X}{R}$		
MAGNITUDE $Z = \sqrt{R^2 + X^2}$ ohms	ADMITTANCE $Y = \frac{1}{Z}$ mhos		
			
	Impedance	$\frac{R + j\omega [L(1 - \omega^2 LC) - CR^2]}{(1 - \omega^2 LC)^2 + \omega^2 C^2 R^2}$	
	Magnitude	$\sqrt{R^2 + \omega^2 L^2 + \omega^2 C^2 R^2}$	
	Phase Angle	$\tan^{-1} \frac{\omega [L(1 - \omega^2 LC) - CR^2]}{R}$	
	Admittance	$\frac{R - j\omega [L(1 - \omega^2 LC) - CR^2]}{R^2 + \omega^2 L^2}$	
			
	Impedance	$\frac{X_1}{R^2 + (X_1 + X_2)^2}$	
	Magnitude	$\frac{\sqrt{X_1^2 R_2^2 + [R_2^2 + X_2(X_1 + X_2)]^2}}{R_2^2 + (X_1 + X_2)^2}$	
	Phase Angle	$\tan^{-1} \frac{R_2^2 + X_2(X_1 + X_2)}{X_1 R_2}$	
	Admittance	$\frac{R_2 X_1 - j[R_2^2 + X_2^2 + X_1 X_2]}{X_1 (R_2^2 + X_2^2)}$	

Table 5-2. Impedance Formulas (cont'd)

Impedance	$\frac{R_1 R_2 (R_1 + R_2) + \omega^2 L^2 R_2 + \frac{R_1}{\omega C^2}}{(R_1 + R_2)^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} + j \frac{\omega L R_2^2 - \frac{R_1^2}{\omega C} - \frac{L}{C} \left(\omega L - \frac{1}{\omega C}\right)}{(R_1 + R_2)^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$
Magnitude	$\left\{ \frac{\left[ R_1 R_2 (R_1 + R_2) + \omega^2 L^2 R_2 + \frac{R_1}{\omega C^2} \right]^2}{(R_1 + R_2)^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} + \frac{\left[ \omega L R_2^2 - \frac{R_1^2}{\omega C} - \frac{L}{C} \left(\omega L - \frac{1}{\omega C}\right) \right]^2}{(R_1 + R_2)^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} \right\}^{1/2}$
Phase Angle	$\tan^{-1} \left[ \frac{\omega L R_2^2 - \frac{R_1^2}{\omega C} - \frac{L}{C} \left(\omega L - \frac{1}{\omega C}\right)}{R_1 R_2 (R_1 + R_2) + \omega^2 L^2 R_2 + \frac{R_1}{\omega C^2}} \right]$
Admittance	$\frac{R_1 + \omega^2 C^2 R_1 R_2^2 (R_1 + R_2) + \omega^4 L^2 C^2 R_2^2}{(R_1 + \omega^2 L^2) + (1 + \omega^2 C^2 R_2^2)} + j \omega \left[ \frac{CR_2^2 - L + \omega^2 L C (L - CR_2^2)}{(R_1 + \omega^2 L^2) (1 + \omega^2 C^2 R_2^2)} \right]$
Impedance	$\frac{R_1 R_2 (R_1 + R_2) + R_1 X_2^2 + R_2 X_1^2}{(R_1 + R_2)^2 + (X_1 + X_2)^2} + j \frac{R_1^2 X_2 + R_2^2 X_1 + X_1 X_2 (X_1 + X_2)}{(R_1 + R_2)^2 + (X_1 + X_2)^2}$
Magnitude	$\left[ (R_1 R_2 (R_1 + R_2) + R_1 X_2^2 + R_2 X_1^2)^2 + (R_1^2 X_2 + R_2^2 X_1 + X_1 X_2 (X_1 + X_2))^2 \right]^{1/2}$
Phase Angle	$\tan^{-1} \frac{R_1^2 X_2 + R_2^2 X_1 + X_1 X_2 (X_1 + X_2)}{R_1 R_2 (R_1 + R_2) + R_1 X_2^2 + R_2 X_1^2}$
Admittance	$\frac{R_1 (R_2^2 + X_2^2) + R_2 (R_1^2 + X_1^2)}{(R_1^2 + X_1^2) (R_2^2 + X_2^2)} - j \frac{X_1 (R_2^2 + X_2^2) + X_2 (R_1^2 + X_1^2)}{(R_1^2 + X_1^2) (R_2^2 + X_2^2)}$



Subtract the value of the smaller reactance from that of the larger.  $35 - 21$  equals 14 ohms. This is the net reactance and constitutes the value of X. Using this value, locate 14 in the X column. Move horizontally to reach the 5 column (R). The impedance is shown as 14.86 ohms.

**□Example:**

You require an impedance of 30 ohms for an RLC circuit. What values of R and X can you use to obtain this impedance?

The table shows you can get this impedance by using an 18-ohm resistor and a reactance having a value of 24 ohms. This reactance may be a coil having an inductive reactance of this value, or a capacitor, or both components whose net reactance is 24 ohms. Of course you could also use a 24-ohm resistor and a reactance of 18 ohms. There are many other combinations in the table that are very close to this desired 30-ohm impedance.

## **IMPEDANCE AND TURNS RATIO**

Transformers are conveniently used as impedance transformation devices. The impedance of a transformer varies as the square of the turns ratio. These ratios, in steps of 1 to 100, are given in Table 5-3.

**□Example:**

A step-down transformer has a turns ratio of 37 to 1. What is the impedance ratio?

Locate the turns ratio, 37:1. Immediately alongside is the impedance ratio of 1369:1.

**□Example:**

What is the impedance transformation of a step-up-transformer having a turns ration of 1:53?

Table 5-3 shows that the impedance transformation for this turns ratio is 1:2809.

The turns ratio of a transformer is specifically that—a ratio—and gives no indication of the actual number of turns used by the transformer. A transformer having 50 primary turns and 50 secondary turns has a 1:1 ratio. So does a transformer having 5000 primary and 5,000 secondary turns.

To get the ratio, divide the larger number of turns by the smaller. Table 5-3 will then supply the impedance ratio.

Table 5-3. Impedance Ratio and Turns Ratio of a Transformer

<i>Turns Ratio</i>	<i>Impedance Ratio</i>	<i>Turns Ratio</i>	<i>Impedance Ratio</i>
100:1	10,000:1	65:1	4,225:1
99:1	9,801:1	64:1	4,096:1
98:1	9,604:1	63:1	3,969:1
97:1	9,409:1	62:1	3,844:1
96:1	9,216:1	61:1	3,721:1
95:1	9,025:1	60:1	3,600:1
94:1	8,836:1	59:1	3,481:1
93:1	8,649:1	58:1	3,364:1
92:1	8,464:1	57:1	3,249:1
91:1	8,281:1	56:1	3,136:1
90:1	8,100:1	55:1	3,025:1
89:1	7,921:1	54:1	2,916:1
88:1	7,744:1	53:1	2,809:1
87:1	7,569:1	52:1	2,704:1
86:1	7,396:1	51:1	2,601:1
85:1	7,225:1	50:1	2,500:1
84:1	7,056:1	49:1	2,401:1
83:1	6,889:1	48:1	2,304:1
82:1	6,724:1	47:1	2,209:1
81:1	6,571:1	46:1	2,116:1
80:1	6,400:1	45:1	2,025:1
79:1	6,241:1	44:1	1,936:1
78:1	6,084:1	43:1	1,849:1
77:1	5,929:1	42:1	1,764:1
76:1	5,776:1	41:1	1,681:1
75:1	5,625:1	40:1	1,600:1
74:1	5,476:1	39:1	1,521:1
73:1	5,329:1	38:1	1,444:1
72:1	5,184:1	37:1	1,369:1
71:1	5,041:1	36:1	1,296:1
70:1	4,900:1	35:1	1,225:1
69:1	4,761:1	34:1	1,156:1
68:1	4,624:1	33:1	1,089:1
67:1	4,489:1	32:1	1,024:1
66:1	4,356:1	31:1	961:1

Table 5-3. Impedance Ratio and Turns Ratio of a Transformer (cont'd)

<i>Turns Ratio</i>	<i>Impedance Ratio</i>	<i>Turns Ratio</i>	<i>Impedance Ratio</i>
30:1	900:1	1:100	1:10,000
29:1	841:1	1:99	1:9,801
28:1	784:1	1:98	1:9,604
27:1	729:1	1:97	1:9,409
26:1	676:1	1:96	1:9,216
25:1	625:1	1:95	1:9,025
24:1	576:1	1:94	1:8,836
23:1	529:1	1:93	1:8,649
22:1	484:1	1:92	1:8,464
21:1	441:1	1:91	1:8,281
20:1	400:1	1:90	1:8,100
19:1	361:1	1:89	1:7,921
18:1	324:1	1:88	1:7,744
17:1	289:1	1:87	1:7,569
16:1	256:1	1:86	1:7,396
15:1	225:1	1:85	1:7,225
14:1	196:1	1:84	1:7,056
13:1	169:1	1:83	1:6,889
12:1	144:1	1:82	1:6,724
11:1	121:1	1:81	1:6,571
10:1	100:1	1:80	1:6,400
9:1	81:1	1:79	1:6,241
8:1	64:1	1:78	1:6,084
7:1	49:1	1:77	1:5,929
6:1	36:1	1:76	1:5,776
5:1	25:1	1:75	1:5,625
4:1	16:1	1:74	1:5,476
3:1	9:1	1:73	1:5,329
2:1	4:1	1:72	1:5,184
1:1	1:1	1:71	1:5,041
		1:70	1:4,900

Table 5-3. Impedance Ratio and Turns Ratio of a Transformer (cont'd)

<i>Turns Ratio</i>	<i>Impedance Ratio</i>	<i>Turns Ratio</i>	<i>Impedance Ratio</i>
1:69	1:4,761	1:33	1:1,089
1:68	1:4,624	1:32	1:1,024
1:67	1:4,489	1:31	1:961
1:66	1:4,356	1:30	1:900
1:65	1:4,225	1:29	1:841
1:64	1:4,096	1:28	1:784
1:63	1:3,969	1:27	1:729
1:62	1:3,844	1:26	1:676
1:61	1:3,721	1:25	1:625
1:60	1:3,600	1:24	1:576
1:59	1:3,481		
1:58	1:3,364	1:23	1:529
1:57	1:3,249	1:22	1:484
1:56	1:3,136	1:21	1:441
1:55	1:3,025	1:20	1:400
1:54	1:2,916	1:19	1:361
1:53	1:2,809	1:18	1:324
1:52	1:2,704	1:17	1:289
1:51	1:2,601	1:16	1:256
1:50	1:2,500	1:15	1:225
1:49	1:2,401	1:14	1:196
1:48	1:2,304	1:13	1:169
1:47	1:2,209	1:12	1:144
1:46	1:2,116	1:11	1:121
1:45	1:2,025	1:10	1:100
1:44	1:1,936		
1:43	1:1,849	1:9	1: 81
1:42	1:1,764	1:8	1: 64
1:41	1:1,681	1:7	1: 49
1:40	1:1,600	1:6	1: 36
1:39	1:1,521	1:5	1: 25
1:38	1:1,444	1:4	1: 16
1:37	1:1,369	1:3	1: 9
1:36	1:1,296	1:2	1: 4
1:35	1:1,225	1:1	1: 1
1:34	1:1,156		

Example:

A step-down transformer has 2465 primary turns and 85 secondary turns. What is the impedance ratio?

Divide 2465 by 85. This supplies a ratio of 29:1. Table 5-3 shows the impedance ratio is 841:1. If the transformer had 85 primary turns and 2465 secondary turns, the impedance ratio would be 1:841.

## Chapter 6

# Permeability

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### PERMEABILITY

Permeability can be considered the ability of a substance to conduct magnetic lines of force. More technically, permeability is the ratio of flux density in gausses (B) to a magnetizing force, H, in oersteds. The permeability of a vacuum, or air, is considered as unity. See Table 6-1.

Table 6-1. Permeabilities of Magnetic Materials.

Cobalt	170
Iron-cobalt alloy (Co 34%)	13,000
Iron, commercial annealed	6000 to 8000
Nickel	400 to 1000
Permalloy (Ni 78.5%, Fe 21.5%)	over 80,000
Perminvar (Ni 45%, Fe 30%, Co 25%)	2000
Sendust	30,000 to 120,000
Silicon steel (Si 4%)	5000 to 10,000
Steel, cast	1500
Steel, open hearth	3000 to 7000



## **Chapter 7**

# **Power**

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### **WATTS AND HORSEPOWER**

Motors are generally rated in terms of horsepower. But since a motor is an electromechanical device, it also has a rating in watts. The relationship between horsepower (hp) and power in watts is: 1 hp equals 745.7 watts.

Table 7-1 gives the conversion between these two quantities. The table can be extended by moving the decimal point in the same direction, for the same number of places, in both columns. For conversion, see Tables 7-2 and 7-3.

#### **□Example:**

A small motor is rated at one-tenth horsepower. What is its rating in watts.

The closest value to one-tenth horsepower in the table is 0.100575 shown in the right-hand column under the heading hp. The power corresponding to this value is 75 watts.

#### **□Example:**

A motor-generator is rated at one-half kilowatt. What is its equivalent horsepower rating?

One-half kilowatt is 500 watts. Table 7-1 does not list such a value but we can use the number 50 in place of 500. Locate the number 50 in the column headed by watts. Move the decimal point one place to the right and 50 becomes 500. The corresponding value of horsepower is 0.067050 hp. Moving the decimal point of this

Table 7-1. Watts vs Horsepower

Watts	HP	Watts	HP	Watts	HP
1	.001341	34	.045594	67	.089847
2	.002682	35	.046935	68	.091188
3	.004023	36	.048278	69	.092529
4	.005364	37	.049617	70	.093870
5	.006705	38	.050958	71	.095211
6	.008046	39	.052299	72	.096552
7	.009387	40	.053640	73	.097893
8	.010728	41	.054981	74	.099234
9	.012069	42	.056322	75	.100575
10	.013410	43	.057663	76	.101916
11	.014751	44	.059004	77	.103257
12	.016092	45	.060345	78	.104598
13	.017433	46	.061686	79	.105939
14	.018774	47	.063027	80	.107280
15	.020115	48	.064368	81	.108261
16	.021456	49	.065709	82	.109962
17	.022797	50	.067050	83	.111303
18	.024138	51	.068391	84	.112644
19	.025479	52	.069732	85	.113985
20	.026820	53	.071073	86	.115326
21	.028161	54	.072414	87	.116667
22	.029502	55	.073755	88	.118008
23	.030843	56	.075096	89	.119349
24	.032184	57	.076437	90	.120690
25	.033525	58	.077778	91	.122031
26	.034866	59	.079119	92	.123372
27	.036207	60	.080460	93	.124713
28	.037548	61	.081801	94	.126054
29	.038889	62	.083142	95	.127395
30	.040230	63	.084483	96	.128736
31	.041571	64	.085824	97	.130077
32	.042912	65	.087165	98	.131418
33	.044253	66	.088506	99	.132759
				100	.134100

Table 7-2. Horsepower vs Watts

HP	Watts	HP	Watts
.01	7.457	.26	193.882
.02	14.914	.27	201.339
.03	22.371	.28	208.796
.04	29.828	.29	216.253
.05	37.285	.30	223.710
.06	44.742	.31	231.167
.07	52.199	.32	238.624
.08	59.656	.33	246.081
.09	67.113	.34	253.538
.10	74.570	.35	260.995
.11	82.027	.36	268.452
.12	89.484	.37	275.909
.13	96.941	.38	283.366
.14	104.398	.39	290.823
.15	111.855	.40	298.280
.18	119.312	.41	305.737
.17	126.769	.42	313.194
.18	134.226	.43	320.651
.19	141.683	.44	328.108
.20	149.140	.45	335.565
.21	156.597	.46	343.022
.22	164.054	.47	350.479
.23	171.511	.48	357.936
.24	178.968	.49	365.393
.25	186.425	.50	372.850
.51	380.307	.76	556.732
.52	387.764	.77	574.189
.53	395.221	.78	581.646
.54	402.678	.79	589.103
.55	410.135	.80	596.560
.56	417.592	.81	604.017
.57	425.049	.82	611.474
.58	432.506	.83	618.931
.59	439.963	.84	626.388
.60	447.420	.85	633.845
.61	454.877	.86	641.302
.62	462.334	.87	648.759
.63	469.791	.88	656.216
.64	477.248	.89	663.673
.65	484.705	.90	671.130
.66	492.162	.91	678.587
.67	499.619	.92	686.044
.68	507.076	.93	693.501
.69	514.533	.94	700.958
.70	521.990	.95	708.415
.71	529.447	.96	715.872
.72	536.904	.97	723.329
.73	544.361	.98	730.786
.74	551.818	.99	738.243
.75	559.275	1.00	745.700

Table 7-3. Horsepower and Electrical Power Equivalents

Unit	Equivalents
1 H.P.	.745.7 Watts
1 H.P.	.0.746 Kw.
1 H.P.	.33,000 Ft.-Lbs. per Min.
1 H.P.	.550 Ft.-Lbs. per Sec.
1 H.P.	.2,545 B.T.U per Hr.
1 H.P.	.0.175 Lbs. Carbon oxidized per Hr.
1 H.P.	.17 Lbs. Water per Hr. heated from 62-212° F.
1 H.P.	.2.64 Lbs. Water per Hr. evaporated from and at 212°F.
1 Kw.	.1,000 Joules per Sec.
1 Kw.	.1.34 H.P.
1 Kw.	.44,250 Ft. Lbs. per Min.
1 Kw.	.737.3 Ft.-Lbs. per Sec.
1 Kw.	.3,412 B.T.U. per Hr.
1 Kw.	.0.227 Lbs. Carbon oxidized per Hr.
1 Kw.	.22.75 Lbs. Water per Hr. heated from 62-212° F.
1 Kw.	.3.53 Lbs. Water per Hr. evaporated from and at 212°F.

number by one decimal place (to the right) supplies 0.6705 hp. In practice this could be rounded off to 0.7 hp.

**□Example:**

What is the horsepower rating of a 1-kilowatt generator?

1 kilowatt is equal to 1,000 watts. Use Table 7-1 by selecting the number 100 and moving its decimal point one place to the right, thus changing 100 to 1,000. The corresponding value of horsepower is 0.134100, but remember to move the decimal point here as well. The answer is 1.341 hp.

**□Example:**

A fractional hp motor is rated at 0.07 hp. What is its power rating in watts?

There is no value in Table 7-1 that corresponds exactly to 0.07. There are two values, though, which are very close. One of these is 0.069732 and the other 0.071073. Thus, this motor has a rating between 52 and 53 watts. However, if you want a more precise value than this, consult Table 7-2. There, you will see that .07 hp corresponds to 52.199 W.

## **Chapter 8**

# **Decibels**

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### **VOLTAGE AND CURRENT RATIOS VS POWER RATIOS AND DECIBELS**

Table 8-1 supplies voltage or current ratios vs power (watts) ratios for decibels (dB) ranging from 0.1 to 50. A decibel (one-tenth of a bel) is a ratio, a means of comparing the relative strengths of a pair of currents, voltages, or powers. In itself, a decibel is not indicative of any particular amount of power, voltage, or current.

Since the decibel is a comparison unit, and not an absolute value, some reference level must be indicated. A common reference, also called zero level, is 1 milliwatt. Other reference levels can be used, but in any event, the reference should be specified. If 1 milliwatt is the reference, the letter m is added to db, the unit being called the dBm (m for milliwatt). Thus, if an amplifier (assuming equal input and output resistances) has an output of 1 watt, the relationship of the power output to the power input is:

$$dB = 10 \log P_2/P_1$$

or

$$dB = 10 \log 1/1000 = 10 \log 1000 = 30 \text{ db}$$

Instead of using the formula, we could have obtained our answer by consulting Table 8-1. The power ratio is 1000—that is, an output of 1 watt is 1000 times greater than the reference level of 1 milliwatt. Locate 1000 under the heading of power ratio in the table. Move to the left and note a gain of 30 dB.

**□Example:**

The input voltage to an amplifier is 1 volt, and the output is 20 volts. What is the voltage gain of the amplifier in dB?

The ratio of the two voltages is 20. The nearest comparable value in the Table is 19.95. The gain is 26 dB.

**□Example:**

An amplifier is said to have a gain of 20 dB. What is its output in watts?

Locate the number 20 in the dB column in Table 8-1. Move to the right to see that this represents a power ratio of 100. If no power input is given and a reference level of 1 milliwatt is indicated, then the output is 100 milliwatts. If an input power is specified, multiply the input power by 100 to get the value of output power.

Note that the first two columns in Table 8-1 are the reciprocals of the last two columns. It makes no difference whether you divide the output power of an amplifier by the input or vice versa. If you put the larger number in the numerator of the dB power formula the answer will be a whole number and you will work with the two columns at the right in Table 8-1. If you use the smaller power value in the numerator, the answer will be a decimal, as indicated in the first two columns in the Table. In either case, the answer in decibels will be the same. If you have an electronic device with a power ratio of 1 to 1000 or, conversely, 1000 to 1, the gain or loss in dB will be 30 in either case. Some technicians and engineers prefer working with whole numbers and put a minus sign in front of their answer to indicate a loss.

### DECIBELS-NEPERS CONVERSIONS

The neper, like the decibel, is a dimensionless unit. While the decibel is derived from common logarithms (logarithms to the base 10), the neper is used to express the ratio of two power levels using the natural system of logarithms—logarithms to the base e (e equals 2.71828). The formula for finding the number of nepers is:

$$\text{nepers} = \frac{1}{2} \log_e P_2/P_1$$

The relationships between decibels and nepers are as follows:

1 decibel	= 0.1 bel	1 bel	= 10 decibels
1 decibel	= 0.1151 neper	1 neper	= 0.8686 bel
1 bel	= 1.151 nepers	1 neper	= 8.686 decibels

As in the case of decibels, nepers must be used with some reference level if just one value of power, either input or output, is specified.

Table 8-1. Voltage or Current Ratios vs Power Ratios and Decibels

Voltage or Current Ratio	Power Ratio	- dB +	Voltage or Current Ratio	Power Ratio
1.000	1.000	0	1.0000	1.0000
0.989	0.977	0.1	1.0116	1.0233
0.977	0.955	0.2	1.0233	1.0471
0.966	0.933	0.3	1.0351	1.0715
0.955	0.912	0.4	1.0471	1.0965
0.944	0.891	0.5	1.0593	1.1220
0.933	0.871	0.6	1.0715	1.1482
0.923	0.851	0.7	1.0839	1.1749
0.912	0.832	0.8	1.0965	1.2023
0.902	0.813	0.9	1.1092	1.2303
0.891	0.794	1.0	1.1220	1.2589
0.881	0.776	1.1	1.135	1.288
0.871	0.759	1.2	1.1482	1.3183
0.861	0.741	1.3	1.161	1.349
0.851	0.724	1.4	1.175	1.380
0.841	0.708	1.5	1.189	1.413
0.832	0.692	1.6	1.202	1.445
0.822	0.676	1.7	1.216	1.479
0.813	0.661	1.8	1.230	1.514
0.803	0.646	1.9	1.245	1.549
0.749	0.631	2.0	1.2589	1.5849
0.776	0.603	2.2	1.288	1.660
0.759	0.575	2.4	1.318	1.738
0.750	0.562	2.5	1.334	1.778
0.724	0.525	2.8	1.380	1.905
0.708	0.501	3.0	1.4125	1.9953
0.692	0.479	3.2	1.445	2.089
0.676	0.457	3.4	1.479	2.188
0.668	0.447	3.5	1.4962	2.2387
0.661	0.436	3.6	1.514	2.291
0.646	0.417	3.8	1.549	2.399
0.631	0.398	4.0	1.5849	2.5119
0.596	0.355	4.5	1.6788	2.8184
0.562	0.316	5.0	1.7783	3.1623
0.531	0.282	5.5	1.8836	3.5481
0.501	0.251	6.0	1.9953	3.9811
0.473	0.224	6.5	2.113	4.467
0.447	0.200	7.0	2.239	5.012
0.422	0.178	7.5	2.371	5.623
0.398	0.159	8.0	2.512	6.310
0.376	0.141	8.5	2.661	7.079
0.355	0.126	9.0	2.818	7.943
0.335	0.112	9.5	2.985	8.913
0.316	0.100	10	3.162	10.00
0.282	0.0794	11	3.55	12.6
0.251	0.0631	12	3.98	15.9
0.224	0.0501	13	4.47	20.0
0.200	0.0398	14	5.01	25.1
0.178	0.0316	15	5.62	31.6
0.159	0.0251	16	6.31	39.8

Table 8-1. Voltage or Current Ratios vs Power Ratios and Decibels (cont'd)

Voltage or Current Ratio	Power Ratio	- dB +	Voltage or Current Ratio	Power Ratio
0.141	0.0200	17	7.08	50.1
0.126	0.0159	18	7.94	63.1
0.112	0.0126	19	8.91	79.4
0.10000	0.0100	20	10.00	100.0
0.08913	0.0079	21	11.22	125.9
0.07943	0.0063	22	12.59	158.5
0.07079	0.0050	23	14.13	199.5
0.06310	0.00398	24	15.85	251.2
0.05623	0.03162	25	17.78	316.2
0.05012	0.002512	26	19.95	398.1
0.04467	0.001995	27	22.39	501.2
0.03981	0.001585	28	25.12	631.0
0.03548	0.001259	29	28.18	794.3
0.03162	0.001000	30	31.62	1000
0.02818	0.000794	31	35.48	1259
0.02512	0.000631	32	39.81	1585
0.02239	0.000501	33	44.67	1995
0.01995	0.000398	34	50.12	2512
0.01778	0.000316	35	56.23	3162
0.01585	0.000251	36	63.10	3981
0.01413	0.000199	37	70.79	5012
0.01259	0.000158	38	79.43	6310
0.01122	0.000126	39	89.13	7943
0.01000	0.000100	40	100.00	10000
0.00891	0.000079	41	112.2	12590
0.00794	0.000063	42	125.9	15850
0.00708	0.000050	43	141.3	19950
0.00631	0.000040	44	158.5	25120
0.00562	0.000032	45	177.8	31620
0.00501	0.000025	46	199.5	39810
0.00447	0.000020	47	223.9	50120
0.00398	0.000016	48	251.2	63100
0.00355	0.000013	49	281.8	79430
0.00316	0.000010	50	316.2	100000

**Table 8-2. Decibels vs Nepers**  
 (n, nepers; dB, decibels)

dB	n	dB	n	dB	n
1	0.1151	34	3.9134	67	7.7117
2	0.2302	35	4.0285	68	7.8268
3	0.3453	36	4.1436	69	7.9419
4	0.4604	37	4.2587	70	8.0570
5	0.5755	38	4.3738	71	8.1721
6	0.6906	39	4.4889	72	8.2872
7	0.8057	40	4.6040	73	8.4023
8	0.9208	41	4.7191	74	8.5174
9	1.0359	42	4.8342	75	8.6325
10	1.1510	43	4.9493	76	8.7476
11	1.2661	44	5.0644	77	8.8627
12	1.3812	45	5.1795	78	8.9778
13	1.4963	46	5.2946	79	9.0929
14	1.6114	47	5.4097	80	9.2080
15	1.7265	48	5.5248	81	9.3231
16	1.8416	49	5.6399	82	9.4382
17	1.9567	50	5.7550	83	9.5533
18	2.0718	51	5.8701	84	9.6684
19	2.1869	52	5.9852	85	9.7835
20	2.3020	53	6.1003	86	9.8986
21	2.4171	54	6.2154	87	10.0137
22	2.5322	55	6.3305	88	10.1288
23	2.6473	56	6.4456	89	10.2439
24	2.7624	57	6.5607	90	10.3590
25	2.8775	58	6.6758	91	10.4741
26	2.9926	59	6.7909	92	10.5892
27	3.1077	60	6.9060	93	10.7043
28	3.2228	61	7.0211	94	10.8194
29	3.3379	62	7.1362	95	10.9345
30	3.4530	63	7.2513	96	11.0496
31	3.5681	64	7.3664	97	11.1647
32	3.6832	65	7.4815	98	11.2798
33	3.7983	66	7.5966	99	11.3949
				100	11.5100

Table 8-3. Neper vs Decibel Conversion

n	dB	n	dB	n	dB
1	8.686	34	295.324	67	581.962
2	17.372	35	304.010	68	590.648
3	26.058	36	312.696	69	599.334
4	34.744	37	321.382	70	608.020
5	43.430	38	330.068	71	616.706
6	52.116	39	338.754	72	625.392
7	60.802	40	347.440	73	634.078
8	69.488	41	356.126	74	642.764
9	78.174	42	364.812	75	651.450
10	86.860	43	373.498	76	660.136
11	95.546	44	382.184	77	668.822
12	104.232	45	390.870	78	677.508
13	112.918	46	399.556	79	686.194
14	121.604	47	408.242	80	694.880
15	130.290	48	416.928	81	703.556
16	138.976	49	425.614	82	712.252
17	147.662	50	434.300	83	720.938
18	156.348	51	442.986	84	729.624
19	165.034	52	451.672	85	738.310
20	173.720	53	460.358	86	746.996
21	182.406	54	469.044	87	755.682
22	191.092	55	477.730	88	764.368
23	199.778	56	486.416	89	773.054
24	208.464	57	495.102	90	781.740
25	217.150	58	503.788	91	790.426
26	225.836	59	512.474	92	799.112
27	234.522	60	521.160	93	807.798
28	243.208	61	529.846	94	816.484
29	251.894	62	538.532	95	825.170
30	260.580	63	547.218	96	833.856
31	269.266	64	555.904	97	842.542
32	277.952	65	564.590	98	851.228
33	286.638	66	573.276	99	859.914
				100	868.600

Table 8-2 supplies the conversion between decibels and nepers. Table 8-3 gives nepers to decibels.

**□Example:**

An amplifier has a gain of 10 dB. What is its gain in nepers?

Locate the number 10 in the dB column in Table 8-2. To the right of this number you will find 1.1510 nepers.

**□Example:**

Assuming a zero reference level of 1 milliwatt, what is the gain in nepers of an amplifier whose output is 50 milliwatts?

The power ratio in the problem is 50 to 1. Locate the nearest number to this in Table 8-1. This is shown as 50.1. The gain in dB is 17. Now consult Table 8-2. Locate 17 dB in the left-hand column. The number of nepers corresponding to 17 dB is 1.9567.



## Chapter 9

# Sensitivity

### RECEIVER OR TUNER SENSITIVITY

Sensitivity is the ability of a receiver or tuner to respond to signals, previously specified in microvolts ( $\mu\text{V}$ ). These specs have been changed from voltage to power ratings. Sensitivity in microvolts can be converted to dBf by:

$$\text{dBf} = 20 \log (\mu\text{V}/0.55)$$

Where log is log to the base 10 and  $\mu\text{V}$  is microvolts based on a 300-ohm antenna input. Sensitivity is not the same for monaural and stereo so tuners and receivers should include separate dBf figures for each.

#### □Example:

A tuner has an input sensitivity of  $2\ \mu\text{V}$  when set in the stereo mode. What is its sensitivity in dBf?

$$\begin{aligned}\text{dBf} &= 20 \log (\mu\text{V}/0.55) \\ &= 20 \log 2/0.55 \\ &= 20 \log 3.636363 \\ \log 3.636363 &= 0.5599\end{aligned}$$

$$\text{dBf} = (20)(0.5599) = 11.198 \text{ dBf}$$

Instead of doing this work, consult Table 9-1. Locate  $2\ \mu\text{V}$  in the left column. Move directly across to the answer, 11.198 dBf.

#### □Example:

A tuner has an input sensitivity of  $40\ \mu\text{V}$  when set for monaural reception. What is its sensitivity in dBf?

$$\begin{aligned}
 \text{dBf} &= 20 \log (\mu\text{V}/0.55) \\
 &= 20 \log 40/0.55 \\
 &= 20 \log 72.7272 \\
 \log 72.7272 &= 1.8615
 \end{aligned}$$

$$\text{dBf} = (20)(1.8615) = 37.23 \text{ dBf}$$

Using Table 9-1, locate  $40 \mu\text{V}$  in the left column. Move across to the right for an answer of  $37.23 \text{ dBf}$ .

Table 9-1. Microvolts ( $\mu\text{V}$ ) vs. dBf.

$\mu\text{V}$	dBf	$\mu\text{V}$	dBf
1.5	8.71	3.5	16.07
1.6	9.28	3.6	16.3
1.7	9.8	3.7	16.548
1.8	10.3	3.8	16.776
1.9	10.77	3.9	17.012
2.0	11.198	4.0	17.2
2.1	11.6	4.5	18.256
2.2	12.04	5.0	19.17
2.3	12.424	6.0	20.748
2.4	12.8	7.0	22.075
2.5	13.15	8.0	22.984
2.6	13.478	9.0	24.296
2.7	13.804	10.0	25.19
2.8	14.134	30.0	34.74
2.9	14.436	32.0	35.3
3.0	14.74	40.0	37.23
3.1	15.01	50.0	39.17
3.2	15.3	55.0	40.0
3.3	15.7	100.0	45.19
3.4	15.8	1000.0	65.154

## **Chapter 10**

# **Sound And Acoustics**

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### **WAVELENGTHS OF SOUND**

The distance between two successive positive peaks, two successive negative peaks, or between any two corresponding points of a sine wave is known as its wavelength. As mentioned earlier, this is often represented by the letter  $\lambda$ . This description is not only applicable to radio-frequency waves, but also to sound waves. The reference here is not to a complex sound waveform, but to a pure sine wave only.

A sound wave of constant velocity (represented by the letter  $\mu$ ) will travel a distance of one wavelength in a one period interval. This is more concisely stated in the formula  $\mu$  equals  $\lambda/T$ . But the period of a wave has an inverse relationship to the frequency. Thus,  $T$  equals  $1/f$ . By substituting in the formula  $\mu$  equals  $\lambda/T$ , we get  $\mu$  equals  $f\lambda$ . We can rearrange this formula to read  $\lambda$  equals  $\mu/f$ .

The velocity of sound in air at a temperature of 20 degrees C (68 degrees F) is 1130 feet per second. Using this information, we can conveniently set up Table 10-1 which gives the relationship between the frequency of sound in air in hertz and the wavelengths of sound in feet and in inches.

Conversion from feet to meters can be made by using Table 28-4. Conversion from inches to millimeters can be made by using Table 28-6.

Example:

What is the wavelength, in feet, of a 60-hertz sine wave?

Locate the number 60 in the left-hand column of Table 10-1. The corresponding value is shown as 18.83 feet.

Table 10-1. Sound Wavelengths.

(1130 ft/sec, in air, at 20 degrees C; 32 degrees F)

Frequency (Hz)	Wavelength (feet)	Frequency (Hz)	Wavelength (feet)	Frequency (Hz)	Wavelength (feet)
20	56.50	140	8.07	380	2.97
25	45.20	150	7.53	400	2.83
30	37.67	160	7.06	420	2.69
35	32.29	170	6.65	440	2.57
40	28.25	180	6.28	460	2.46
45	25.11	190	5.95	480	2.35
50	22.60	200	5.65	500	2.26
55	20.55	210	5.38	525	2.15
60	18.83	220	5.14	550	2.05
65	17.38	230	4.91	575	1.97
70	16.14	240	4.71	600	1.88
75	15.07	250	4.52	650	1.74
80	14.13	260	4.35	700	1.61
85	13.29	270	4.19	750	1.51
90	12.56	280	4.04	800	1.41
95	11.89	290	3.90	850	1.33
100	11.30	300	3.77	900	1.26
110	10.27	320	3.53	950	1.19
120	9.42	340	3.32	975	1.16
130	8.69	360	3.14	990	1.14

Frequency (Hz)	Wavelength (inches)	Frequency (Hz)	Wavelength (inches)	Frequency (Hz)	Wavelength (inches)
1000	13.56	9000	1.51	16000	0.85
2000	6.78	10000	1.36	17000	0.80
3000	4.52	11000	1.23	18000	0.75
4000	3.39	12000	1.13	19000	0.71
5000	2.71	13000	1.04	20000	0.68
6000	2.26	14000	0.97		
7000	1.94	15000	0.90		
8000	1.70				

**□Example:**

A sound wave has a length of 7 feet. What is its frequency in hertz?

The closest value given in Table 10-1 is 7.06 feet. The frequency of this sound wave, then, is approximately 160 Hz.

**□Example:**

What is the wavelength, in meters, of a wave whose frequency is 75 Hz?

First, locate the wavelength in feet corresponding to a frequency of 75 Hz. Table 10-1 shows that this is 15.07 feet. Consult Table 28-6. The closest value to 15.07 is 15 feet. Move one column and the answer is 4.5720 meters.

## RANGE OF MUSICAL INSTRUMENTS

The fundamental range of musical instruments is limited. At the low-frequency end, few musical instruments can produce tones below 50 Hz. The human voice doesn't go much lower than 70 Hz. At the high-frequency end, all musical instruments and voices are under 5 kHz in fundamental frequency. It is the fundamental frequency that determines the pitch of a tone. See Fig. 10-1.

What you can hear depends on your age, sex, the physical condition of your ears and brain, and prior musical training. While the audio spectrum is assumed to have a range of 20 Hz to 20 kHz, few of us have a hearing capability that goes down to 20 Hz and equally few can hear as high as 20 kHz. The pipe organ, contrabassoon and the harp can reach below 40 Hz. Natural sounds include hardly any low frequencies, and what you may find at such frequencies is noise.

## THE OCTAVE

An octave is a doubling of frequency. From 30 Hz to 60 Hz could be called an octave. We could regard 60 Hz to 120 Hz as another octave. We do not start with 0 Hz for this is actually DC. 32 Hz is often selected as a practical beginning but we can start with 16 Hz as a bottom limit. If we select 16 Hz as our starting point, we can have 10 octaves up to approximately 16 kHz.

The ten octaves in Table 10-2 are of particular interest because they roughly represent the range of human hearing capability. Sounds below 16 Hz and above 16 kHz cannot be heard by most. Consider 16 Hz and 16 kHz as the outermost hearing limits.

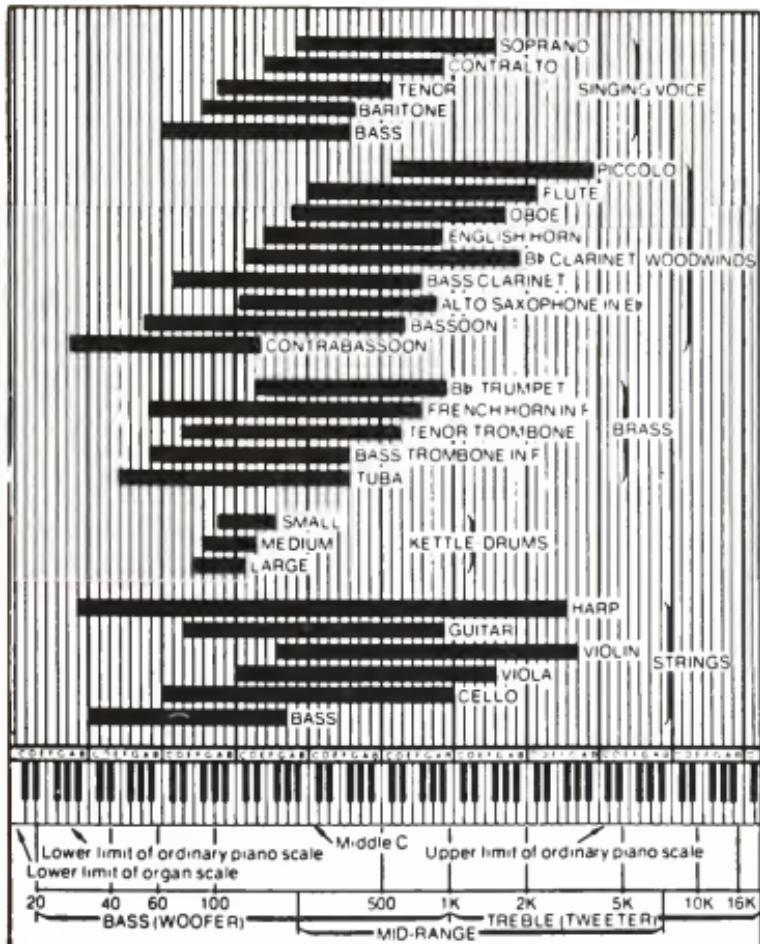


Fig. 10-1. The fundamental range of musical instruments is quite limited. Shown here are the ranges of fundamental components of tones for the principal musical instruments and voices (courtesy of Ziff-Davis Publishing Company, from the January, 1976 issue of Stereo Review).

Table 10-2. Frequency Range in Octaves

Frequency Range, Hz	Octave
16 to 32	first
32 to 64	second
64 to 128	third
128 to 256	fourth
256 to 512	fifth
512 to 1024	sixth
1024 to 2048	seventh
2048 to 4096	eighth
4096 to 8192	ninth
8192 to 16,384	tenth

## FREQUENCY RANGE OF THE PIANO

Letters with a subscript indicate tones below middle C; those with a superscript are tones above middle C. From key A<sub>4</sub> to A<sub>3</sub> is an octave; from A<sub>3</sub> to A<sub>2</sub> is an octave. Starting with key C<sub>3</sub> there are seven octaves to key C<sup>4</sup>. Other frequency ranges are shown in Table 10-4 and 10-5.

Table 10-3. Frequency Range of the Piano

Key	Frequency (Hz)	Key	Frequency (Hz)	Key	Frequency (Hz)
A <sub>4</sub>	27.50	B <sub>1</sub>	246.94	C <sub>3</sub>	2023.00
B <sub>4</sub>	30.87	C	261.63	D <sub>3</sub>	2349.30
C <sub>3</sub>	32.70	D	293.66	E <sub>3</sub>	2637.00
D <sub>3</sub>	36.71	E	329.63	F <sub>3</sub>	2793.80
E <sub>3</sub>	41.20	F	349.23	G <sub>3</sub>	3136.00
F <sub>3</sub>	43.65	G	392.00	A <sub>3</sub>	3520.00
G <sub>3</sub>	49.00	A	440.00	B <sub>3</sub>	3951.10
A <sub>3</sub>	55.00	B	493.88	C <sub>4</sub>	4186.00
F <sub>3</sub>	61.74	C <sub>1</sub>	523.25		
C <sub>2</sub>	65.41	D <sub>1</sub>	587.33		
D <sub>2</sub>	73.42	E <sup>1</sup>	659.26		
E <sub>2</sub>	82.41	F <sub>1</sub>	698.46		
F <sub>2</sub>	87.31	G <sub>1</sub>	783.99		
G <sub>2</sub>	98.00	A <sub>1</sub>	880.00		
A <sub>2</sub>	110.00	B <sub>1</sub>	987.77		
B <sub>2</sub>	123.47	C <sub>2</sub>	1046.50		
C <sub>1</sub>	130.81	D <sub>2</sub>	1174.70		
D <sub>1</sub>	146.83	E <sub>2</sub>	1318.50		
E <sub>1</sub>	164.81	F <sub>2</sub>	1396.90		
F <sub>1</sub>	174.61	G <sub>2</sub>	1568.00		
G <sub>1</sub>	196.00	A <sup>2</sup>	1760.00		
A <sub>1</sub>	220.00	B <sup>2</sup>	1975.50		

Table 10-4. Frequency Range Of Musical Instruments

Instrument	Low Hz	High Hz
Bass clarinet	82.41	493.88
Bass tube	43.65	349.23
Bass viol	41.20	246.94
Bassoon	61.74	493.88
Cello	130.81	698.46
Clarinet	164.81	1567.00
Flute	261.63	3349.30
French horn	110.00	880.00
Trombone	82.41	493.88
Trumpet	164.81	987.77
Oboe	261.63	1568.00
Violin	130.81	1174.70
Violin	196.00	3136.00

**Table 10-5. Frequency Range of Musical Voices**

	Low Hz	High Hz
Alto	130.81	698.46
Baritone	98.00	392.00
Bass	87.31	349.23
Soprano	246.94	1174.70
Tenor	130.81	493.88

## **VELOCITY OF SOUND IN AIR**

Sound velocity can be calculated from:

$$V = 49\sqrt{459.4 + F^\circ} \text{ feet/second}$$

or

$$V = 20.06\sqrt{273 + C^\circ} \text{ meters/second}$$

Where V is the velocity in feet/second or meters/second,  $F^\circ$  is the temperature in degrees Fahrenheit,  $C$  the temperature in degrees Celsius.

The velocity of sound isn't affected by frequency, somewhat slightly by humidity, much more so by temperature, and varies considerably depending on the material (medium) through which it moves. In solid substances, such as brick or steel, the velocity of sound is far greater than in air. In air, the velocity of sound increases by about two feet per second for each increase of one degree Celsius. Refer to Tables 10-6 and 10-7.

**Table 10-6. Velocity of Sound in Air at Various Temperatures**

Deg. F	Speed (ft/second)
32	1087
50	1107
59	1117
68	1127
86	1147

Deg. C	Speed (meters/second)
0	331.32
10	337.42
15	340.47
20	343.51
30	349.61

Table 10-7. Velocity of Sound in Liquids and Solids

Material	Sound Velocity	
	Feet/second	Meters/second
Alcohol	4724	1440
Aluminum	20,407	6220
Brass	14,530	4430
Copper	15,157	4620
Glass	17,716	5400
Lead	7,972	2430
Magnesium	17,487	5330
Mercury	4,790	1460
Nickel	18,372	5600
Polystyrene	8,760	2670
Quartz	18,865	5750
Steel	20,046	6110
Water	4,757	1450

## RELATIVE VOLUME LEVELS OF ORDINARY SOUNDS

The threshold of hearing is zero dB and the threshold of hearing pain is 130 dB. See Fig. 10-2.

## SOUND ABSORPTION

The sound absorption coefficient of materials varies with frequency. Table 10-8 indicates that plywood, a common building material, has a greater sound absorption coefficient at frequencies below 500 Hz, but tends to level off in the region above 2 kHz.

Table 10-8. Sound Absorption Coefficients For 3/16" Plywood

Frequency (Hz)	Sound Absorption Coefficient
125	0.35
250	0.25
500	0.20
1,000	0.15
2,000	0.05
4,000	0.05

The limits of sound absorption coefficients are 0 and 1. 1, or 100 percent, would indicate a substance that absorbed sound completely, and is the goal of construction materials used in anechoic chambers. 0 or 0 percent indicates that the material does not absorb sound at all. This does not necessarily mean total reflectivity. An open window or rather that portion of it that constitutes open space can be regarded as having no reflectivity. In an echo chamber, the

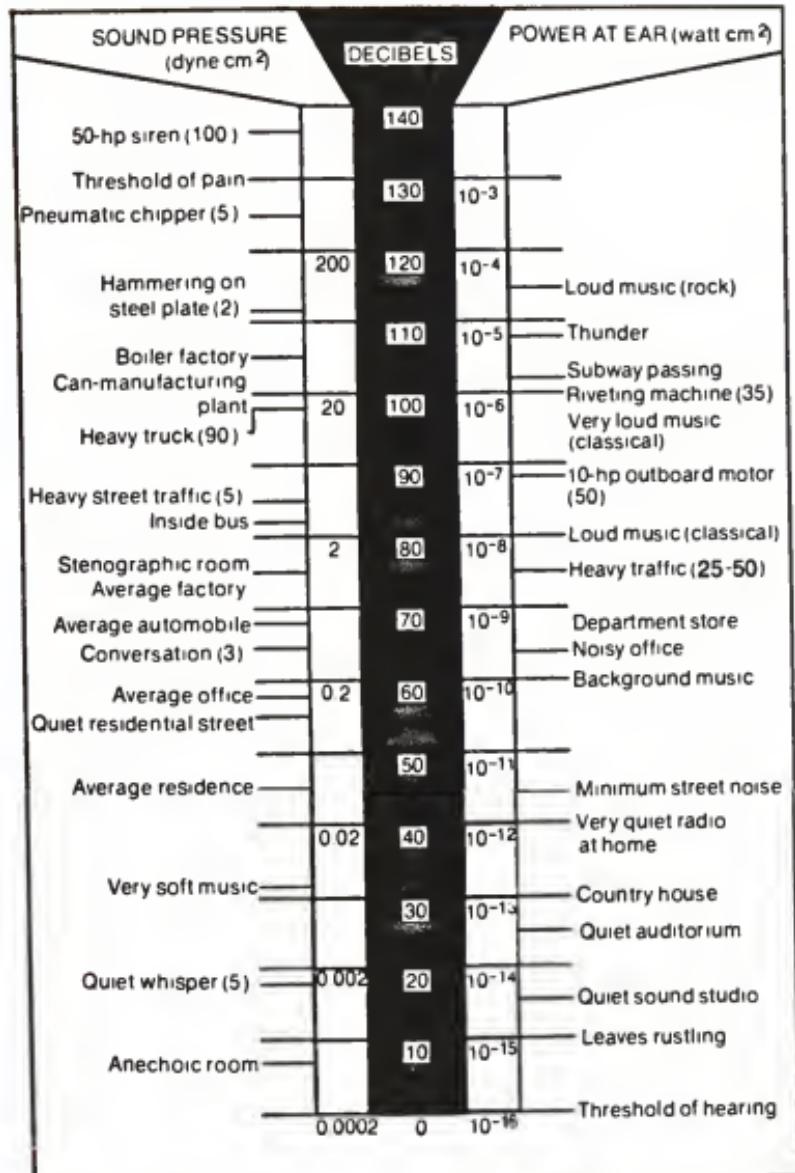


Fig. 10-2. Relative loudness levels of common sounds (courtesy of Ziff-Davis Publishing Company), from the January, 1976 issue of Stereo Review.

surfaces may have extremely high values of reflectivity. How effective a material is for the absorption of sound is indicated by its sound absorption coefficient. A cement floor has an absorption coefficient of 0.015 or 1.5%. This means that sound striking such a floor will

dissipate 1.5% of the sound as heat, or slightly less, depending on how much of the sound will pass through the material. 98.5 percent of the sound will be reflected.

Table 10-9 indicates the effect of frequency on the sound absorption coefficients of various materials. For some materials, the absorption coefficient increases with frequency; with others it decreases; and for some it remains relatively fixed.

Table 10-9. Frequency vs Sound Absorption

Material	Frequency (Hz)				
	125	250	500	1000	2000
Glass window	.12	.25	.18	.12	.07
Lightweight drapes	.35	.25	.18	.12	.07
Heavy drapes	.03	.04	.11	.17	.24
Wood floor	.14	.35	.55	.72	.70
Carpet	.15	.11	.10	.07	.06
(on concrete)	.02	.06	.14	.37	.60
					.65

Absorption coefficients of building materials are often supplied as an overall range without indicating the effect of frequency, as indicated in Table 10-10.

Table 10-10. Sound Absorption Coefficients of Various Materials.

Material	Coefficient Absorption Range
Linoleum on concrete floor	0.03 to 0.08
Upholstered seats	0.05
Ventilating grilles	0.15 to 0.50
Painted brick	0.02 to 0.04
Plaster on brick	0.02 to 0.04
Plaster on lath	0.3 to 0.04
Door	0.3 to 0.05
Window glass	0.3 to 0.05
Thick carpeting	0.15 to 0.5
Heavy curtains	0.2 to 0.8

Reverberation time is a function of room volume and sound absorption. It is directly proportional to the volume of an enclosed space, such as a recording studio or an in-home listening room and inversely proportional to the total amount of sound absorption in that enclosure.

Reverberation time is not the same for all frequencies. The formula for calculating reverberation time, developed by Professor

Wallace C. Sabine in 1895, indicates average reverberation time and does not take frequency into consideration.

$$T_{60} = \frac{0.05V}{S_a}$$

Where  $T_{60}$  is the reverberation time in seconds, V is the volume of the room in cubic feet and  $S_a$  is the total equivalent sound absorption in sabins per square foot of surface material. Reverberation time is how long it takes for reverberant sound to decrease by 60 dB, one millionth of the original sound source intensity.

Table 10-11 shows the sound absorption of seats and an audience at 512 Hz. The absorption is indicated in sabins. Table 10-12 indicates the effect of an audience on reverberation time.

Table 10-11. Sound Absorption of Seats and Audience at 512 Hertz.

	Equivalent Absorption (in sabins)
Audience, seated, units per person, depending on character of seats, etc.	3.0-4.3
Chairs, metal or wood	0.17
Pew cushions	1.45-1.90
Theater and auditorium chairs	
Wood veneer seat and back	0.25
Upholstered in leatherette	1.6
Heavily upholstered in plush or mohair	2.6-3.0
Wood pews	0.4

Table 10-12. Effect of an Audience on Reverberation Time

Audience (number present)	Absorption (sabins)	Reverberation Time (seconds)
0	1,201	7.3
200	2,011	4.3
400	2,821	3.1
600	3,631	2.4
800	4,441	2.0

It takes time for sounds to reach a reflecting surface and then the ears of listeners. Table 10-13 shows the approximate time in seconds for reverberant sound to be heard.

Table 10-13. Reverberation Time

Total Distance Traveled (feet)	Distance from Ear to Barrier (feet)	Approximate Time Required (seconds)
11.2	5.6	0.01
22.4	11.2	0.02
33.6	16.8	0.03
44.8	22.4	0.04
56.0	28.0	0.05
63.2	31.6	0.06
78.4	39.2	0.07
89.6	44.8	0.08
100.8	50.4	0.09
112.0	56.0	0.1
224.0	112.0	0.2
336.0	168.0	0.3
448.0	224.0	0.4
560.0	280.0	0.5
632.0	316.0	0.6
784.0	392.0	0.7
896.0	448.0	0.8
1008.0	504.0	0.9
1120.0	560.0	1.0



# Chapter 11

## Recording

### PLAYBACK EQUALIZATION FOR RECORDING TAPES

The point at which treble boost begins is referred to as a time constant. CrO<sub>2</sub> and cobalt-treated ferric tapes have a time constant of 70 microseconds. Ferric oxide tapes have a 120-microsecond time constant. See Table 11-1.

Table 11-1. Time Constants of Magnetic Tapes and Their Equalization

(Time Constants) in Microseconds

Formulation	Bias	Equalization
Ferric Oxide (FeO <sub>2</sub> )	normal	120
Chromium Dioxide (CrO <sub>2</sub> )	high	70
Beridox (Fuji)	high	70
Ferric Oxide/Cobalt	high	70
Ferrichrome (FeCr)	normal	70
Pure Metal	high	70

### TREBLE BOOST

159,154.9431 divided by the time constant in microseconds supplies the treble boost frequency. See Table 11-2.

Table 11-2. Time Constants of Magnetic Tape vs Starting Point of Treble Boost

Time Constant	Treble Boost Frequency (Hz)
10	15,915.4943
15	10,610.3295
20	7,957.7471

Time Constant	Treble Boost Frequency (Hz)
25	8,366.1977
30	5,305.1467
35	4,547.284
40	3,978.8735
45	3,536.7765
50	3,183.0988
55	2,893.7262
60	2,652.5823
65	2,448.5375
70	2,273.462
75	2,122.0659
80	1,989.4367
85	1,872.411
90	1,768.3882
95	1,675.3151
100	1,591.5494

### OPERATING TIME OF MAGNETIC TAPE

The amount of time required by a tape for recording or playback can be calculated by:

$$T \text{ (seconds)} = \frac{\text{tape length (inches)}}{\text{operating speed (inches per second)}}$$

#### □Example:

What is the operating time of a single track tape that is 150 feet long, running at 15 ips (inches per second)?

Convert 150 feet to inches by multiplying by 12, so  $150 \times 12 = 1800$  inches.

$$T = \frac{1800}{15} = 120 \text{ seconds} = 2 \text{ minutes}$$

For two tracks, forward and reverse, operating time would be doubled or 4 minutes. See Table 11-3.

Table 11-3. Tape—Recording or Playback Time.

NO. OF FEET	NO. OF TRACKS	SPEED				15/16 (IPS) (2.375 cm/sec.)
		15 (IPS) (38 cm/sec.)	7½ (IPS) (18 cm/sec.)	3¾ (IPS) (9.5 cm/sec.)	1¼ (IPS) (4.75 cm/sec.)	
4800	1 Track	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.	17 hrs. 4 min.
	2 Tracks	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.	17 hrs. 4 min.	34 hrs. 8 min.
	4 Tracks	4 hrs. 16 min.	8 hrs. 32 min.	17 hrs. 4 min.	34 hrs. 8 min.	68 hrs. 16 min.
3600	1 Track	48 min.	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.	12 hrs. 48 min.
	2 Tracks	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.	12 hrs. 48 min.	25 hrs. 36 min.
	4 Tracks	3 hrs. 12 min.	6 hrs. 24 min.	12 hrs. 48 min.	25 hrs. 36 min.	51 hrs. 12 min.

NO. OF FEET	NO. OF TRACKS	15 (IPS) (38 cm/sec.)	7½ (IPS) (19 cm/sec.)	SPEED 3¾ (IPS) (9.5 cm/sec.)	1¾ (IPS) (4.75 cm/sec.)	15/16 (IPS) (2.375 cm/sec.)
2500	1 Track	33 min.	1 hr. 6 min.	2 hrs. 13 min.	4 hrs. 26 min.	8 hrs. 52 min.
	2 Tracks	1 hr. 6 min.	2 hrs. 12 min.	4 hrs. 26 min.	8 hrs. 52 min.	17 hrs. 44 min.
	4 Tracks	2 hrs. 12 min.	4 hrs. 24 min.	8 hrs. 52 min.	17 hrs. 44 min.	35 hrs. 28 min.
2400	1 Track	32 min.	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.
	2 Tracks	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.	17 hrs. 4 min.
	4 Tracks	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.	17 hrs. 4 min.	34 hrs. 8 min.
1800	1 Track	24 min.	48 min.	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.
	2 Tracks	48 min.	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.	12 hrs. 48 min.
	4 Tracks	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.	12 hrs. 48 min.	25 hrs. 36 min.
1200	1 Track	16 min.	32 min.	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.
	2 Tracks	32 min.	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.
	4 Tracks	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.	17 hrs. 4 min.
900	1 Track	12 min.	24 min.	48 min.	1 hr. 36 min.	3 hrs. 12 min.
	2 Tracks	24 min.	48 min.	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.
	4 Tracks	48 min.	1 hr. 36 min.	3 hrs. 12 min.	6 hrs. 24 min.	12 hrs. 48 min.
600	1 Track	8 min.	16 min.	32 min.	1 hr. 4 min.	2 hrs. 8 min.
	2 Tracks	16 min.	32 min.	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.
	4 Tracks	32 min.	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.	8 hrs. 32 min.
300	1 Track	4 min.	8 min.	16 min.	32 min.	1 hr. 4 min.
	2 Tracks	8 min.	16 min.	32 min.	1 hr. 4 min.	2 hrs. 8 min.
	4 Tracks	16 min.	32 min.	1 hr. 4 min.	2 hrs. 8 min.	4 hrs. 16 min.
225	1 Track	3 min.	6 min.	12 min.	24 min.	48 min.
	2 Tracks	6 min.	12 min.	24 min.	48 min.	1 hr. 36 min.
	4 Tracks	12 min.	24 min.	48 min.	1 hr. 36 min.	3 hrs. 12 min.
150	1 Track	2 min.	4 min.	8 min.	16 min.	32 min.
	2 Tracks	4 min.	8 min.	16 min.	32 min.	1 hr. 4 min.
	4 Tracks	8 min.	16 min.	32 min.	1 hr. 4 min.	2 hrs. 8 min.

## RECORDING AND PLAYBACK SPEEDS

While recording and playback speeds are commonly given in ips (inches per second), these are sometimes supplied in cm/sec (centimeters per second). Table 11-4 shows the relationship between ips and cm/sec.

Table 11-4. Tape Speeds in ips and cm/sec

ips cm/sec	30	15	7-½	3-¾	1-¾	15/16
	76.2	38.1	19.05	9.525	4.7625	2.38125

## TAPE LENGTHS IN FEET AND METERS

Tape lengths are now being supplied in feet and meters. Table 11-5 supplies data on various lengths of tape in the English and metric systems.

Table 11-5. Tape lengths in Feet and Meters

Tape Length, Feet	Tape Length, Meters
100	30.48
150	45.72
200	60.96
210	64.008
300	91.44
400	121.92
420	128.016
450	137.16
500	152.40
600	182.88
700	213.36
800	243.84
900	274.32
1000	304.8
1200	365.76
1500	457.20
1800	548.64
2000	609.60
2400	731.52
3000	914.40
3600	1097.28

### OPEN REEL SIZES

The diameters for the reels used in open reel decks are now measured in inches and centimeters. Table 11-6 supplies diameters of the most commonly used reels in both types of measurements.

Table 11-6. Open Reel Diameters in Inches and Centimeters.

Inches	Centimeters	Actual Diameter (cm)
3	8	7.62
4	10	10.16
5	13	12.70
5-1/4	15	14.605
7	18	17.78
10-1/2	26	26.67

The center column shows the diameters as specified. The column at the right shows the actual diameters.

## **Chapter 12**

# **Television**

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### **TV CHANNELS AND FREQUENCIES**

Table 12-1 supplies the channel width, and the frequencies in megahertz (MHz) of the picture and sound carriers of TV channels. The table cover VHF channels 2 to 13 (channel 1 has not been assigned) and UHF channels 14 to 83.

The bandwidth of each channel is 6 megahertz regardless of frequency. In each instance, the video carrier is 1.25 megahertz above the lower edge of the band while the sound carrier is 0.25 megahertz lower than the high-frequency end of the channel. The separation between carriers, video and sound, is 4.5 megahertz. Worldwide standards are shown in Fig. 12-2.

Picture carrier = sound carrier—4.5 MHz

Picture carrier = low end of TV channel + 1.25 MHz

Lower video sideband = 0.75 MHz

Sound carrier = upper end of TV channel—0.25 MHz

Sound carrier—picture carrier = 4.5 MHz

#### **□Example:**

What is the sound carrier frequency of channel 16?

Locate channel 16 in the left-hand column. Move to the right and under the heading of sound carrier find 487.75 MHz.

**Table 12-1. TV Channels and Frequencies**

(Channel width is 6 MHz; video carrier is 4.5 MHz below sound carrier.)

<b>Channel No.</b>	<b>Frequency Band (MHz)</b>	<b>Video Carrier (MHz)</b>	<b>Sound Carrier (MHz)</b>
(1 not assigned)			
2	54-60	55.25	59.75
3	60-66	61.25	65.75
4	66-72	67.25	71.75
5	76-82	77.25	81.75
6	82-88	83.25	87.75
7	174-180	175.25	179.75
8	180-186	181.25	185.75
9	186-192	187.25	191.75
10	192-198	193.25	197.75
11	198-204	199.25	203.75
12	204-210	205.25	209.75
13	210-216	211.25	215.75
14	470-476	471.25	475.75
15	476-482	477.25	481.75
16	482-488	483.25	487.75
17	488-494	489.25	493.75
18	494-500	495.25	499.75
19	500-506	501.25	505.75
20	506-512	507.25	511.75
21	512-518	513.25	517.75
22	518-524	519.25	523.75
23	524-530	525.25	529.75
24	530-536	531.25	535.75
25	536-542	537.25	541.75
26	542-548	543.25	547.75
27	548-554	549.25	553.75
28	554-560	555.25	559.75
29	560-566	561.25	565.75
30	566-572	567.25	571.75
31	572-578	573.25	577.75
32	578-584	579.25	583.75
33	584-590	585.25	589.75
34	590-596	591.25	595.75
35	596-602	597.25	601.75

Table 12-1. TV Channels and Frequencies (cont'd)

Channel No.	Frequency Band (MHz)	Video Carrier (MHz)	Sound Carrier (MHz)
36	602-608	603.25	607.75
37	608-614	609.25	613.75
38	614-620	615.25	619.75
39	620-626	621.25	625.75
40	626-632	627.25	631.75
41	632-638	633.25	637.75
42	638-644	639.25	643.75
43	644-650	645.25	649.75
44	650-656	651.25	655.75
45	656-662	657.25	661.75
46	662-668	663.25	667.75
47	668-674	669.25	673.75
48	674-680	675.25	679.75
49	680-686	681.25	685.75
50	686-692	687.25	691.75
51	692-698	693.25	697.75
52	698-704	699.25	703.75
53	704-710	705.25	709.75
54	710-716	711.25	715.75
55	716-722	717.25	721.75
56	722-728	723.25	727.75
57	728-734	729.25	733.75
58	734-740	735.25	739.75
59	740-746	741.25	745.75
60	746-752	747.25	751.75
61	752-758	753.25	757.75
62	758-764	759.25	763.75
63	764-770	765.25	769.75
64	770-776	771.25	775.75
65	776-782	777.25	781.75
66	782-788	783.25	787.75
67	788-794	789.25	793.75
68	794-800	795.25	799.75
69	800-806	801.25	805.75
70	806-812	807.25	811.75

**Table 12-1. TV Channels and Frequencies (cont'd)**

Channel No.	Frequency Band (MHz)	Video Carrier (MHz)	Sound Carrier (MHz)
71	812-818	813.25	817.75
72	818-824	819.25	823.75
73	824-830	825.25	829.75
74	830-836	831.25	835.75
75	836-842	837.25	841.75
76	842-848	843.25	847.75
77	848-854	849.25	853.75
78	854-860	855.25	859.75
79	860-866	861.25	865.75
80	866-872	867.25	871.75
81	872-878	873.25	877.75
82	878-884	879.25	883.75
83	884-890	885.25	889.75

Table 12-2. Worldwide Television Standards

COUNTRY	LINES/FIELDS	COLOR	VOLTAGE (V)	FREQUENCY (Hz)
AFGHANISTAN	625/50	PAL	220	50
ALBANIA	625/50	SECAM	220	50
ALGERIA	625/50	PAL	127-220	50
ANDORRA	625/50		220	50
ANGOLA	625/50		220	50
ARGENTINA	625/50	PAL	220	50
AUSTRALIA	625/50	PAL	240	50
AUSTRIA	625/50	PAL	220	50
AZORES	525/60	PAL	220	50
BAHAMAS	525/60	NTSC	120	60
BAHRAIN	625/50	PAL	220	50
BANGLADESH	625/50	PAL		
BARBADOS	625/50	NTSC	120	50
BELGIUM	625/50	PAL	127-220	50
BERMUDA	525/60	NTSC	120	60
BOLIVIA	625/50	PAL	115-230	50
BRAZIL	525/60	PALM	220	60
BULGARIA	625/50	SECAM	220	50
BURUNDI	625/50		220	50
CAMEROON	625/50		127-220	50
CANADA	525/60	NTSC	110-240	60
CANARY IS.	625/50	PAL	127	50
CENTRAL AFRICAN REP.	625/50		220	50
CEYLON	625/50		230	50
CHAD	625/50		220	50
CHILE	525/60	NTSC	220	50
CHINA (PEOPLES REP.)	625/50	PAL	220	50
COLOMBIA	525/60	NTSC	150-240	60
CONGO (PEOPLES REP.)	625/50	SECAM	220	50
COSTA RICA	525/60	NTSC	110	60
CUBA	525/60	NTSC	120	60
CURACAO	525/60	NTSC	120	60
CYPRUS	625/50	PAL	220	50
CZECHOSLOVAKIA	625/50	SECAM	220	50
DAHOMEY	625/50		220	50
DENMARK	625/50	PAL	220	50
DOMINICAN REP.	525/60	NTSC	110	60
ECUADOR	525/60	NTSC	120	60
EGYPT	625/50	SECAM	220	50
EL SALVADOR	525/60	NTSC	110	60
ETHIOPIA	625/50		127	50
FIJI	625/50		240	50
FINLAND	625/50	PAL	220	50
FRANCE	625/50	SECAM	115-230	50
GABON	625/50	SECAM	127-220	50
GAMBIA	625/50			
GERMANY (DEM. REP.)	625/50	SECAM	220	50
GERMANY (FED. REP.)	625/50	PAL	220	50
GHANA	625/50		230	50
GIBRALTAR	625/50		230	50
GREAT BRITAIN	625/50	PAL	127-220	50

Table 12-2 (cont'd).

COUNTRY	LINES/FIELDS	COLOR	VOLTAGE(V)	FREQUENCY (Hz)
GREECE	625/50		110-220	50
GREENLAND	525/60		220	50
GUAM	525/60	NTSC	110	60
GUATEMALA	525/60	NTSC	110-220	60
GUINEA	625/50		127-220	50
GUYANA	625/50	SECAM	127	50
HAITI	625/50	SECAM	115-220	50
HAWAII	525/60	NTSC	117	60
HONDURAS	525/60	NTSC	110-220	60
HONG KONG	625/50	PAL	220	50
HUNGARY	625/50	SECAM	220	50
ICELAND	625/50	PAL	220	50
INDIA	625/50		230	50
INDONESIA	625/50	PAL	110	50
IRAN	625/50	SECAM	220	50
IRAQ	625/50	SECAM	220	50
IRELAND	625/50	PAL	220	50
ISRAEL	625/50	PAL	230	50
ITALY	625/50	PAL	127-220	50
IVORY COAST	625/50	SECAM	220	50
JAMAICA	625/50	PAL	110	50,60
JAPAN	525/60	NTSC	100-200	50,60
JORDAN	625/50	PAL	220	50
KENYA	625/50	PAL	240	50
KOREA (NORTH)	625/50			
KOREA (SOUTH)	525/60	NTSC	100	60
KUWAIT	625/50	PAL	240	50
LEBANON	625/50	SECAM	110-190	50
LIBERIA	625/50	PAL	120	60
LIBYA	625/50	SECAM	120	50
LUXEMBOURG	625/50	SECAM	120-208	50
MALAGASY REP.	625/50		127-220	50
MALAWI	625/50		220	50
MALAYSI	625/50	PA	240	50
MALI	625/50		125	50
MALTA	625/50		240	50
MARTINIQUE	625/50	SECAM	125	50
MAURENTANIA	625/50		220	50
MAURITIUS	625/50	SECAM	220	50
MEXICO	525/60	NTSC	127-220	50,60
MONACO	625/50	SECAM	125	50
MONGOLIA	625/50			
MOROCCO	625/50	SECAM	115	50
MOZAMBIQUE	625/50	PAL	220	50
NETHERLANDS	625/50	PAL	220	50
NETHERLANDS ANTILLES	525/60	NTSC	120-220	50,60
NEW CALEDONIA	625/50	SECAM	220	50
NEW ZEALAND	625/50	PAL	230	50
NICARAGUA	525/60	NTSC	117	60

Table 12-2 (cont'd.).

COUNTRY	LINES/FIELDS	COLOR	VOLTAGE (V)	FREQUENCY (Hz)
NIGER (REP.)	625/50		220	50
NIGERI	625/50	PAL	220	50
NORWAY	625/50	PAL	230	50
OMAN	625/50	PAL	220	50
PAKISTAN	625/50	PAL	220	50
PANAMA	525/60	NTSC	110	60
PARAGUAY	625/50	PAL	220	50
PERU	525/60	NTSC	220	60
PHILIPPINES	525/60	NTSC	115	60
POLAND	625/50	SECAM	220	50
PORTUGAL	625/50		110-220	50
PUERTO RICO	525/60	NTSC	120	60
RHODESIA	625/50	PAL	220	50
RUMANIA	625/50		220	50
RWANDA	625/50		220	50
SAMOA	525/60	NTSC	120	60
SAUDI ARABIA	625/50	SECAM	120-230	50,60
SENEGAL	625/50	SECAM	125	50
SIERRA LEONE	625/50	PAL	230	50
SINGAPORE	625/50	PAL	220	50
SOMALIA (REP.OF)	625/50		220	50
SOUTH AFRICA	625/50	PAL	220	50
SPAIN	625/50	PAL	127-220	50
SPANISH SAHARA	625/50			
ST. KITTS	525/60	NTSC	220	60
SUDAN	625/50	PAL	220	50
SURINAM	525/60	NTSC	115-127	50,60
SWAZILAND	625/50	PAL		
SWEDEN	625/50	PAL	220	50
SWITZERLAND	625/50	PAL	220	50
SYRIA	625/50	SECAM	115-220	50
TAHITI	625/50	SECAM		
TAIWAN	525/60	NTSC	100	60
TANZANIA	625/50	PAL	230	50
THAILAND	625/50	PAL	220	50
TOGOLESE REP.	625/50		127-220	50
TRINIDAD & TOBAGO	525/60	NTSC	117	60
TUNISIA	625/50	SECAM	117-220	50
TURKEY	625/50	PAL	110-220	50
UGANDA	625/50	PAL	220	50
UPPER VOLTA	625/50		220	50
URUGUAY	625/50	PAL	220	50
U.S.A.	525/60	NTSC	110	60
U.S.S.R.	625/50	SECAM	220	50
VENEZUELA	525/60	NTSC	110-220	60
VIETNAM	525/60		120	50
VIRGIN IS.	525/60	NTSC	115	60
YEMEN	625/50		220	50
YUGOSLAVIA	625/50	PAL	220	50
ZAIRE	625/50	SECAM		
ZAMBIA	625/50		230	50



# Chapter 13

## Antennas

### VELOCITY FACTOR

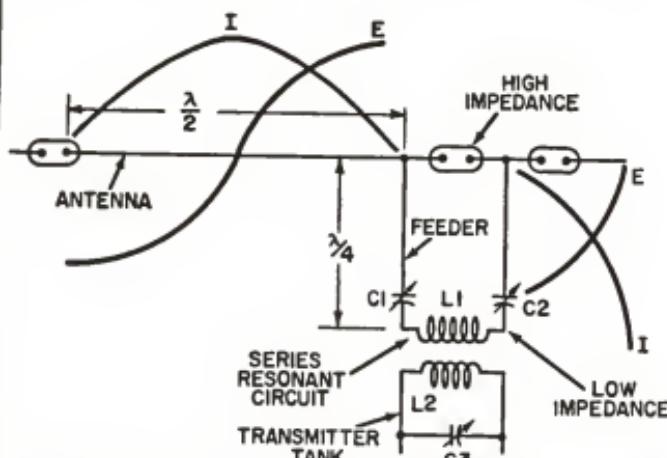
The velocity of a wave along a conductor, such as a transmission line, is not the same as the velocity of that wave in free space. The ratio of the two (actual velocity vs velocity in space) is known as the velocity factor. Obviously, velocity factor must always be less than 1, and, in typical lines varies from 0.6 to 0.97. See Table 13-1.

Table 13-1. Velocity Factors of Transmission Lines

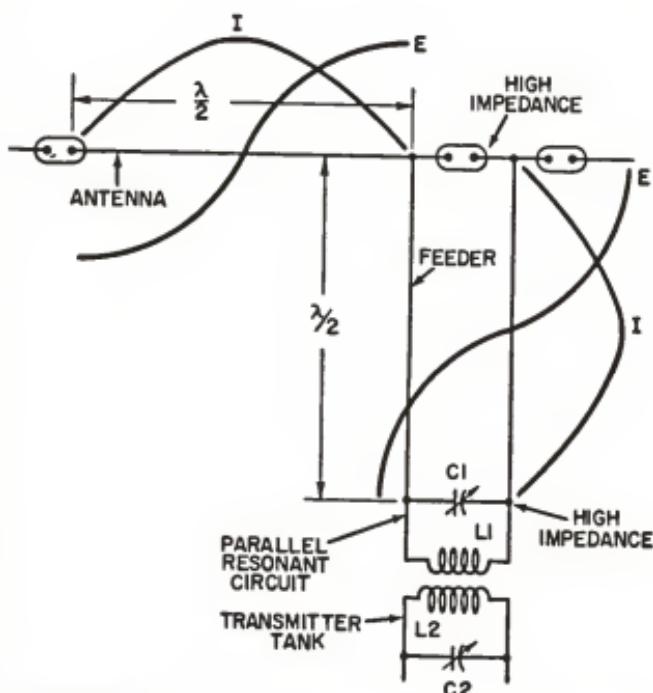
Type of Line	Velocity factor ( <i>V</i> )
Two-wire open line (wire with air dielectric)	0.975
Parallel tubing (air dielectric)	0.95
Coaxial line (air dielectric)	0.85
Coaxial line (solid plastic dielectric)	0.66
Two-wire line (wire with plastic dielectric)	0.68-0.82
Twisted-pair line (rubber dielectric)	0.56-0.65

Table 13-2. Antenna Types

Type of Antenna	Description	Application
<b>PARABOLIC REFLECTOR ANTENNAS</b>	A radiator placed at the focus of a parabola which forms a reflecting surface. Variations in the shape of the parabola provide changes in the shape of the beam produced.	Radar.
<b>COSECANT- SQUARED REFLECTOR</b>	A reflector shaped to produce a beam pattern in which signal strength is proportional to the square of the cosecant of the angle between the horizontal and the line to the target.	Surface search by airborne radar sets
<b>HORN ANTENNAS</b>	Consists of a waveguide with its mouth flared into a horn or tunnel-like shape. The horn usually radiates into a reflector to provide the required beam shape.	Radar Applications.
<b>END-FED HERTZ (Zepp)</b>	Half wavelength voltage-fed radiator fed at one end with tuned, open-wire feeders. See Fig. 13-1.	For receiving and transmitting in the 1.6- to 30-MHz range. Most useful for multi-band operation where space is limited. Use for fixed-station installations.



RESONANT FEED WITH ODD NUMBER OF QUARTER WAVELENGTHS



RESONANT FEED WITH EVEN NUMBER OF QUARTER WAVELENGTHS

Fig. 13-1. Methods of feeding an end-fed half-wave Hertz antenna.

Table 13-2. Antenna Types—(cont'd)

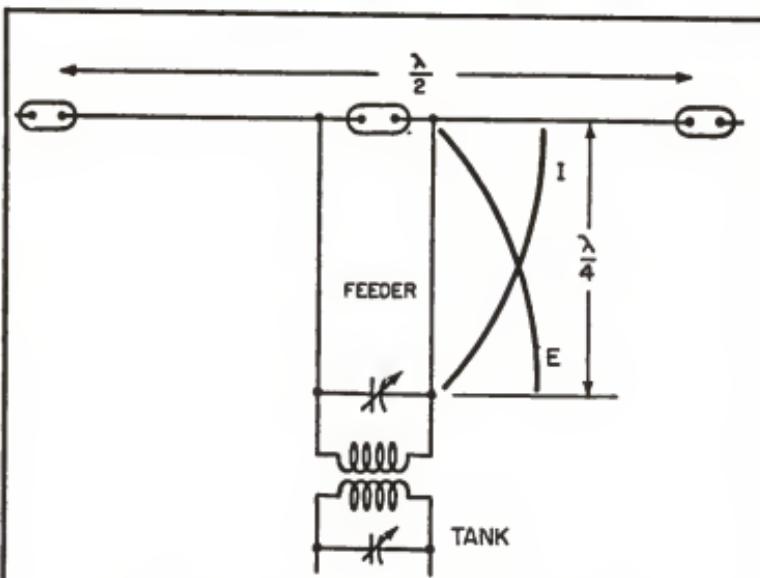
Type of Antenna	Description	Application
<b>CENTER-FED HERTZ (tuned doublet or center-fed Zepp)</b>	A center-fed, half-wave doublet usually employing spaced feeders. Current fed on fundamental and voltage fed on all even harmonics. See Fig. 13-2.	For receiving and transmitting in the 1.6- to 30-MHz range. Can be used on any frequency if the system as a whole can be tuned to that frequency.
<b>FUCHS ANTENNA</b>	Long-wire, voltage-fed radiator an even number of quarter waves long. One end of radiator brought directly to the transmitter or tuning unit without using a transmission line.	For transmitting and receiving on any frequency where simplicity and convenience are desired.
<b>CORNER REFLECTOR</b>	A half-wave radiator with two large metal sheets or screws arranged so their surfaces meet at an angle whose apex lies behind the radiator.	Used in the VHF and UHF ranges to provide directivity in the plane which bisects the angle formed by the reflector.
<b>MARCONI</b>	A vertical radiator approximately one-quarter wavelength long at operating frequency. One end is grounded or worked against ground. May be fed at or near base with low-impedance line. Electrical length may be increased by using loading coil in series with base or near center of radiator or by using capacitive loading at the top. The length, L, in feet can be computed by: $L = \frac{234}{f}$	Widely used for medium- and low-frequency receiving and transmitting where vertical polarization is desirable.

Table 13-2. Antenna Types—(cont'd)

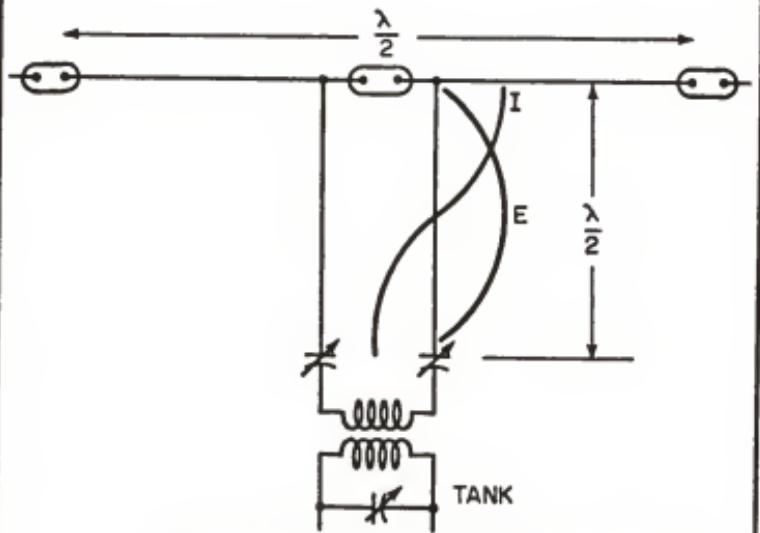
Type of Antenna	Description	Application
	<p>f is in megahertz. L is the overall length, in feet, from the top of the antenna to the point where it connects to ground or counterpoise.</p> <p>The total power dissipated in and radiated from a Marconi antenna can be calculated by:</p> $P_t = I^2 (R_n + R_r)$ <p>I is the antenna current measured at the antenna base, <math>R_r</math> is the radiation resistance and <math>R_g</math> is the ground resistance. The useful radiated power is the difference between the total power consumed and the power lost in the ground resistance. Radiated power, <math>P_r</math> is: <math>P_r = P_t - I^2 \times R_g</math>. See Fig. 13-3.</p>	
<b>PARASITIC ARRAY</b>	Consists of a radiator with a reflector behind and/or one or more directors in front. Produces a unidirectional radiation pattern. May be either vertically or horizontally polarized.	Used to develop high gain in one direction with little or no radiation or pickup in other directions. Used on all frequencies where these characteristics are desired and space is available.
<b>RHOMBIC ANTENNA</b>	A system consisting of four long-wire radiators arranged in the form of a diamond and fed at one end. If the corner opposite the feed point is open, response is bidirectional in a line running through these two corners. If the open end is terminated	Widely used where high gain and directivity is required. Can be used over a wide range of frequencies and is particularly useful when each leg is two or more wavelengths long on lowest frequency. Angle of radiation is lowered and vertical.

Table 13-2. Antenna Types—(cont'd)

Type of Antenna	Description	Application
	with the proper resistance, response is unidirectional in the direction of the terminated end. Gain may vary from 20 to 40 times that of a dipole, depending on the number of wavelengths in each leg.	directivity narrowed by increasing length of legs and/or increasing operating frequency
<b>VERTICAL J</b>	A one-half wavelength vertical radiator fed at the bottom through a quarter-wave matching stub. It is omnidirectional, produces vertical polarization, and can be fed conveniently from a wide range of feed-line impedances.	Practical for use at frequencies above about 7 MHz. Normally used for fixed-frequency applications because of its extreme sensitivity to frequency changes. Efficiency falls off as frequency is raised
<b>COAXIAL ANTENNA (sleeve antenna)</b>	Vertical radiator one-half wavelength long. Upper half consists of a relatively thin radiator and the bottom half a large diameter cylinder. Fed at the center from coaxial cable of 70 to 120 ohms.	Practical for frequencies above about 7 MHz. Normally used for fixed frequency applications. Changes in frequency require that the antenna be retuned by varying length of the two halves of the radiator. Practical for operation up to about 100 MHz.
<b>GROUND-PLANE ANTENNA</b>	Omnidirectional quarter-wave vertical radiator mounted above a horizontal reflecting surface. Its impedance is approximately 36 ohms or less.	Practical for producing vertically polarized waves at frequencies above about 7 MHz and frequently used at frequencies as high as 300 MHz.



ODD NUMBER OF QUARTER-WAVELENGTHS



EVEN NUMBER OF QUARTER-WAVELENGTHS

Fig. 13-2. Methods of feeding a center-fed half-wave Hertz antenna.

Table 13-2. Antenna Types—(cont'd)

Type of Antenna	Description	Application
<b>CROW-FOOT ANTENNA</b>	A low-frequency antenna consisting of comparatively short vertical radiator with a 3-wire V-shaped flat top and a counterpoise having the same shape and size as the flat top. See Fig. 13-4.	Normally used where it is impractical to erect a quarter-wave vertical radiator. Used most frequently for reception and transmission in the 200 to 500 kHz range.
<b>TURNSTILE ANTENNA</b>	An omnidirectional, horizontally polarized antenna consisting of two half-wave radiators mounted at right angles to each other in the same horizontal plane. They are fed with equal currents 90 degrees out of phase. Gain is increased by stacking. Dipoles may be simple, folded, or special broadband types.	Normally used for transmission and reception of FM and television broadcast signals.
<b>SKIN ANTENNAS</b>	Usually consist of an insulated section of the skin of an aircraft. Its radiation pattern varies with frequency, size of the radiating section, and position of the radiator on the aircraft.	Used for VHF and UHF reception and transmission in high-speed aircraft. Often used to replace fixed wire antennas used in the 2 to 2.5 MHz range.
<b>ILAS ANTENNAS</b>	Localizer antennas are of several different types. One type consists of two or more square loops. Glide path is usually produced by two stacked antennas. The lower antenna is usually a horizontal loop bisected by a metal screen and supported about 6 feet off the ground.	Used to enable pilots to locate the airport and to land the plane on the desired runway when weather conditions would prohibit a landing under visual flight reference.

Table 13-2. Antenna types—(cont'd)

Type of Antenna	Description	Application
	The upper antenna is a V-shaped dipole radiator with a parasitic element. Marker beacon antennas may consist of collinear dipoles or arrays.	
<b>OMNI-RANGE (VOR)</b>	Consists of two pairs of square-loop radiators surrounding a single square-loop radiator.	Used to provide navigation signals for aircraft in all directions from the range station.
<b>ADCOCK ANTENNA</b>	Consists of vertical radiators which produce bidirectional vertically polarized radiation.	Used in low-frequency radio ranges and for direction finding.
<b>LOOP ANTENNAS</b>	A loop of wire consisting of one or more turns arranged in the shape of a square, circle, or other convenient form. It produces a bidirectional pattern along the plane of the loop.	Normally used for direction-finding applications, particularly in ships and aircraft.
<b>STUB MAST</b>	A quarter-wave vertical radiator consisting of a metal sheath over a hardwood supporting mast. Fed with 50-ohm line with the outer conductor connected to a large metal ground surface.	Used for wide-band reception and transmission of frequencies above 100 MHz. Normally used in aircraft installations.

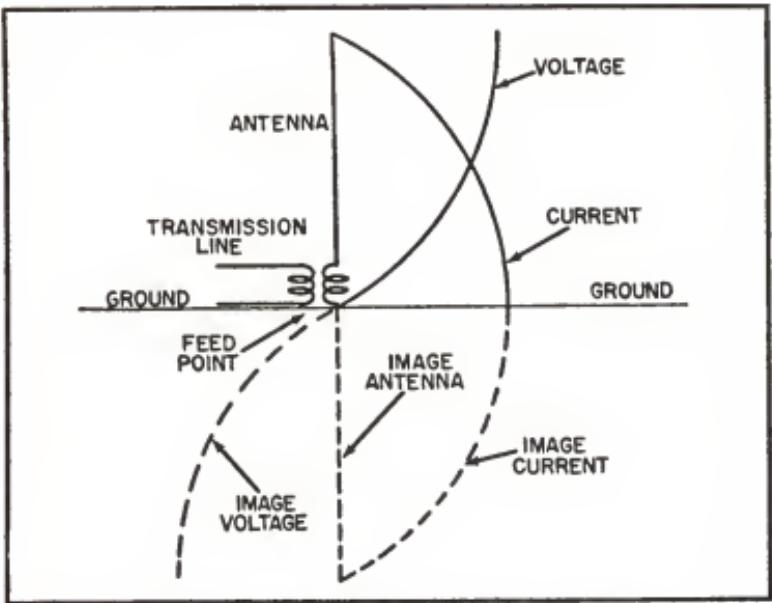


Fig. 13-3. Current and voltage distribution of a Marconi antenna.

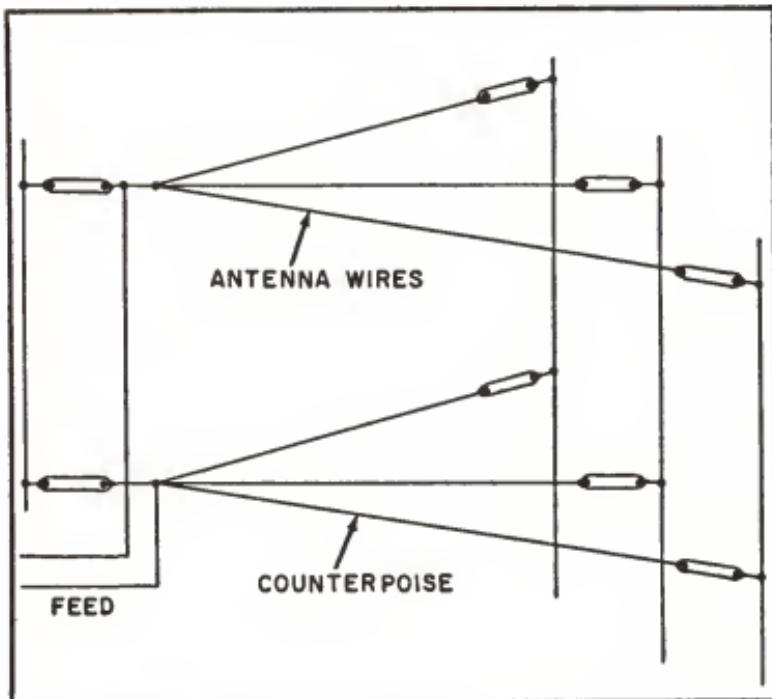


Fig. 13-4. Arrangement of crow-foot antenna.

Table 13-2. Antenna Types—(cont'd)

Type of Antenna	Description	Application
<b>HALF RHOMBIC (inverted V or tilted wire)</b>	A two-wire antenna with the legs in a vertical plane and in the shape of an inverted V. Directivity is in the plane of the legs. Feeding one end and leaving the other open results in bidirectivity. Terminating the free end with a suitable resistor produces unidirectional radiation in the direction of the termination. Gain and angle between legs depend on frequency and the number of wavelengths in each leg.	Used to provide high gain. Used where low angle of radiation is desirable. Usable over a wide frequency range. Bandwidth is greatest for terminated type. Angle of radiation is lowered as leg length and/or operating frequency is increased.
<b>BEVERAGE ANTENNA</b>	A directional long-wire horizontal antenna, two or more wavelengths long. The end nearest the distant receiving station is terminated with a 500-ohm resistor connected to a good counterpoise. The antenna, generally suspended 10 to 20 feet above ground, is non-resonant.	Used for transmitting and receiving vertically polarized waves. Often used for long-wave transoceanic broadcasts. Its input impedance is fairly constant so it can be used over a wide frequency range. Useful for frequencies between 300 kHz and 3 MHz. Highly suitable for use over dry, rocky soil. Never use over salt marshes or water.
<b>FOLDED DIPOLE</b>	A simple center-fed dipole with a second half-wave conductor connected across its ends. Spacing between the conductors is a very small fraction of a wavelength.	Its impedance is higher than that of a simple dipole. Applications same as simple dipole. Often used in parasitic arrays to raise the feedpoint impedance to a value which can be conveniently matched to transmission line.

Table 13-2. Antenna Types—(cont'd)

Type of Antenna	Description	Application
V ANTENNA	<p>Bidirectional antenna made of two long-wire antennas in the form of a V and fed 180 degrees out of phase at its apex. The V antenna is a combination of two long-wire antennas. As the length is increased, more power is concentrated near the axis of the wire.</p> <p>The length of each leg of a V antenna can be found by:</p> $L = \frac{492 (N - 0.05)}{f}$ <p>N is the number of half wavelengths in each leg, and f is the frequency in megaHertz.</p> <p>More gain can be obtained by stacking a second V, one-half wavelength above the first. See Fig. 13-5.</p>	Military and commercial applications.

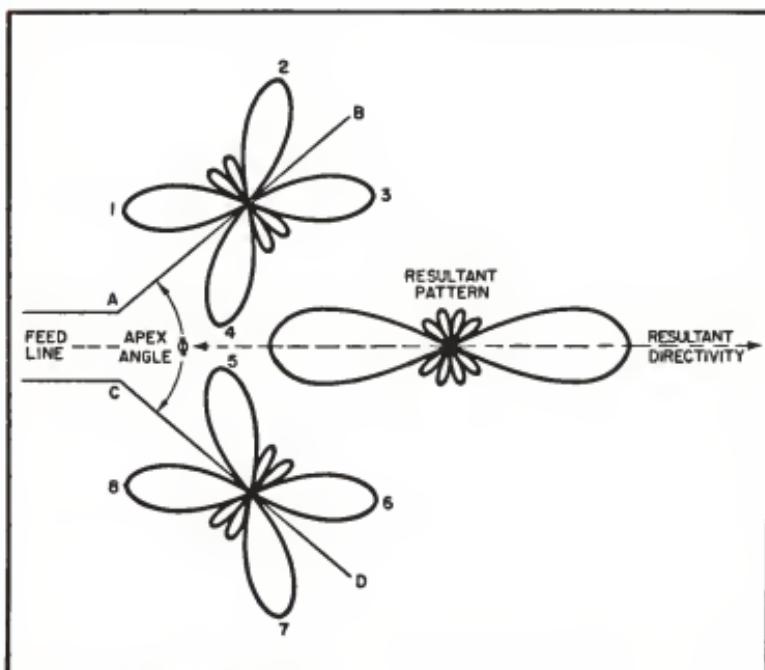


Fig. 13-5. Lobes of a V antenna.

## COAXIAL CABLES

Coaxial cable is a type of transmission line used to connect the CB transceiver to its antenna. The inner conductor of the cables listed in Table 13-3 is copper and so is the outside shield braid. The characteristic impedance is 50 ohms. The cables in this table use a polythelene dielectric.

Table 13-3. Coaxial Cables for CB

RG/U CABLE TYPE	NOMINAL ATTENUATION dB / 100 FT, MHz			
	100	1000	5000	10,000
8/U	1.9	8.0	27.0	100.0
8A/U	1.9	8.0	27.0	100.0
58/U	4.6	17.5	60.0	100.0
58A/U	4.9	24.0	83.0	100.0
59/U	3.4	12.0	42.0	100.0
59A/U	3.4	12.0	42.0	100.0

## CB BASE STATION ANTENNAS

Table 13-4 lists the gain, VSWR, length and typical weight of base station antennas.

Table 13-4. Base Station Antennas for CB

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
hor/vert	hor: 8	1.5:1	108"	26
3-element	vert: 9.75		boom	
half-wave	3.75	1.5:1	216"	10
shunt-fed				
sector	7.75	1.5:1	17.5'	17
phased beam				
vert/hor	hor: 11	1.5:1	22'	
5-element	vert: 12.5		boom	19
vertical	-	-	234"	9
vertical	4	1.4:1	12'	3.5
vertical	11	1.2:1	11.9'	13.5
vertical	3.75	1:1	214"	5
3-element beam	7.5	1:1	120"	15
4-element beam	9	1:1	192"	20
5-element beam	10	1:1	288"	25
6-element dual beam	10.5	1.2:1	216"	30
8-element dual beam	12	1.2:1	216"	45
Universal	0	1.5:1	216"	2
Ground plane	0	1.2:1	216"	5

Table 13-4. Base Station Antennas for CB (cont'd).

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
vertical	-	-	17'3"	-
vertical	1.5	1.5:1	18'	-
vertical	9.2	1.1:1	9' cross boom	16
vertical	12.7	1.1:1	3'1" beam boom 14' cross boom	30
vertical	13.9	1.1:1	12'2" beam boom cross boom	55
vertical	8	1.4:1	20' beam boom	
vertical	9.5	1.1:1	12' boom	7
vertical	unity	1.1:1	18' boom	18
vertical	3	1.1:1	9' ht	3
vertical	3.4	1.1:1	17' ht	6
vertical	3.4	1.1:1	19' 10" ht	8
attic	-	2.1:0	19'10" ht	14
dipole	-	2.1:0	18"	3
vertical	-	2.1:0	36"	6
ground plane	-	2.1:0	18"	3
vertical	-	2.1:0	18"	3
beam	12.3	1.5:1	16"	10
vertical	unity	1.5:1	18'8- ¾" each element	15
vertical	5	1.5:1	9'	4
vertical	6	1.2:1	9'	4
vertical	3.75	1.17:1	19'8"	7
vertical	3.75	1.17:1	210"	10
vertical	10	1.5:1	204"	15
vertical	8	1.6:1	boom 19'8"	11
vertical	-	1.8:1	elements 108"	4
vertical	-	-	element 108" radials	
vertical	-	-	19'	12
vertical	-	-	19'	11
beam	-	-	19'	23
vertical	-	-	17'	8
vertical	-	-	20'	23
vertical	3.7	1.5:1	17'3"	-
beam	8	1.5:1	224-¾"	12.5
beam	8.7	1.5:1	224-¾"	15
beam	9.5	1.5:1	224-¾'	16.5
beam	8	1.5:1	216-½"	14
beam	9.5	1.5:1	224-¾"	20.5
beam and stacking kit	11	1.5:1	224-¾"	29

Table 13-4. Base Station Antennas for CB (cont'd).

Type	Gain (dB)	VSWR	Length	Average Wgt. (bs.)
beam and stacking kit	12	1.5:1	224-3/4"	38
stacking kit	13	1.5:1	224-3/4"	47
conversion kit	-	-	-	10
stacking kit	-	-	-	18
stacking kit	-	-	-	8
vertical	-	1.5:1	235.5"	7.5
vertical	-	1.5:1	245"	7.6
vertical	-	-	19'8"	16
vertical	-	-	19'8"	15
vertical	-	-	19'10-3/4"	8.75
beam	-	-	18'10"	8.5
beam	-	-	boom 14'1"	10.75
gutter lamp	-	-	25"	-
vertical	7.5	1.1:1	-	11
vertical	9	1.1:1	-	16
vertical	10.4	1.1:1	-	22
vertical	-	1.5:1	18'6"	7.5
vertical	3.4	1.1:1	234"	9
vertical	unity	1.4:1	216"	7

**CB MOBILE ANTENNAS**

Antennas for mobile CB transceivers can be trunk mounted, bumper mounted, put on a fender, on the car or truck roof. Table 13-5 supplies comparative data on a number of antennas.

Table 13-5. CB Mobile Antennas

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
whip, base spring	-	1.5:1	108"	6
trunk mount	-	1.5:1	48"	1.5
roof mount	-	1.5:1	44"	1.5
trunk mount	-	1.5:1	48"	2
fender mount	-	1.5:1	44"	1.5
combination CB/AM	-	1.5:1	46"	1.5
roof mount	-	1.5:1	44"	1.5
roof mount	-	1.5:1	46"	1.5
roof mount	-	1.5:1	18"	1.25
gutter mount	-	1.5:1	18"	1.25
magnetic mount	-	1.5:1	-	1.25
trunk mount	-	1.5:1	46"	1.5
gutter mount	-	1.5:1	48"	1.5
vertical	-	-	96'	1.5
vertical	-	-	49"	1.5
vertical	-	-	103"	1.5
CB/AM	-	-	48"	2

Table 13-5. CB Mobile Antennas (cont'd).

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
vertical	-	-	96"	-
vertical	-	-	30"	-
vertical	-	-	48"	-
vertical	1.5	1.5:1	86"	-
vertical	-	1.2:1	-	-
vertical	-	1.1:1	26"	1
vertical	unity	1.1:1	46"	2
vertical	unity	1.1:1	50'	2
vertical	unity	1.1:1	46"	2
vertical	unity	1.1:1	32"	1
vertical	unity	1.1:1	59'	3
vertical	unity	1.1:1	50"	2
vertical	unity	1.1:1	28"	2
vertical	unity	1.1:1	46"	1
vertical	unity	1.1:1	19"	2
vertical	unity	1.1:1	46"	3
vertical	unity	1.1:1	102"	3
vertical	unity	1.1:1	47"	3
vertical	unity	1.1:1	23 7/8"	1.7
vertical	unity	1.1:1	34 5/8"	3.2
vertical	unity	1.1:1	47"	3.1
vertical	-	1.1:1	47"	3.1
vertical	-	2.1:0	18"	3
vertical	-	2.1:0	30"	3
vertical	-	-	30"	1
AM-FM/CB	-	-	50"	1
vertical	-	-	102"	7
vertical	-	1.7:1	39"	2
vertical	-	1.7:1	39"	5
vertical	-	1.8:1	46"	4
vertical	-	1.6:1	102"	3
vertical	-	1:1	20"	3
Gutter vertical	-	-	6'	1.5
vertical	-	-	4'	.5
vertical	-	-	5'	1
vertical	-	-	4'	1
vertical	-	-	6'	1.25
vertical	unity	1.5:1	63"	-
vertical	unity	1.5:1	42"	-
vertical	unity	1.5:1	44 1/2"	-
vertical	unity	1.5:1	45"	-
vertical	-	1.5:1	87"	1.75
vertical	-	1.5:1	45"	2
vertical	-	1.5:1	43 3/4"	1
vertical	-	1.5:1	17"	1
vertical	-	1.5:1	36"	1
vertical	-	1.5:1	100"	3
vertical	-	-	83'	2.75

Table 13-5. CB Mobile Antennas (cont'd)

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
mobile res.			29"	.5
mast	-	-	54"	2.25
mast	-	-	54"	2.5
vertical	-	-	-	1
vertical	-	-	-	.33
vertical	-	-	26 1/2"	1.5
			60 1/2"	
vertical	-	-	26 1/2"	.75
vertical	-	-	60 1/2"	
vertical	-	-	-	.75
vertical	-	-	-	.75
vertical	-	-	-	1
AM/FM/CB			-	1.5
vertical	-	-	-	
roof mount	-	-	30"	.5
gutter clamp	-	-	25"	1
trunk groove	-	-	-	1.25
base loaded	-	-	45 3/4"	3
trans. ant.	-	-	-	-
vertical	-	-	108"	4.5
bumper mount	-	-	108"	5
vertical	-	-	102"	1.5
vertical	-	-	108"	1.5
vertical	-	1.5:1	8'	1
vertical	-	1.5:1	4'	.5
vertical	-	1.5:1	9'	1
vertical	-	1.5:1	36"	1
magnetic mount	4.1	1.1:25	32"	-
vertical	5.2	1.1:25	32"	-
mtch. network	-	-	-	
	6.4	1.1:0	10"	-
vertical	-	1.1:1	35"	.75
vertical	-	1.1:1	36"	1
vertical	-	-	48"	-
vertical	-	-	96"	-
vertical	-	-	-	-
vertical	-	-	38"	-
vertical	-	-	20"	-
vertical	-	-	37"	-
vertical	-	-	19"	-
vertical	-	-	38"	-
vertical	-	-	20"	-
vertical	-	-	3"	4 oz.
vertical	-	-	18"	6 oz.
vertical	4	1.1:1	108"	5
vertical	unity	1.1:1	46"	1.5
vertical	unity	1.1:1	45"	1.75
vertical	unity	1.1:1	18'	1.5
vertical	unity	1.1:1	45"	1.5

Table 13-5. CB Mobile Antennas (cont'd)

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
vertical	unity	1.1:1	46"	1.5
vertical	unity	1.1:1	48"	2
vertical	unity	1.1:1	50"	2
vertical	unity	1.2:1	93"	4
vertical	unity	1.2:1	77"	4

## MARINE ANTENNAS

Marine antennas are described in Table 13-6.

Table 13-6. Marine Antennas

Type	Gain (dB)	VSWR	Length	Average Wgt. (lbs.)
vertical	-	1.5:1	97"	3
vertical	-	-	54"	2
vertical	1.5	1.1:1	19'11"	-
vertical	-	-	6'	4
vertical	1.5	1.5:1	79"	-
vertical	-	1.5:1	96 $\frac{3}{8}$ "	2
vertical	-	1.5:1	12'	7.5
vertical	-	1.5:1	18'6"	9
vertical	4.1	1.125	30"	-
vertical	1.4	1.51	60"	2

# Chapter 14

## Electronics

Table 14-1. Electronic Units, Abbreviations and Symbols

Capacitance	$F$ = farad $\mu F$ = microfarad $pF$ = picofarad	Symbol C
Frequency	$Hz$ = cycles per second $KHz$ = kiloHertz $MHz$ = megaHertz	Symbol f
Inductance	$h$ = henry $mh$ = millihenry $\mu h$ = microhenry	Symbol L
Resistance	$\Omega$ or $\omega$ = ohm $K\omega$ = kilohms $M\omega$ = megohms	Symbol R
Time	$sec$ = second $msec$ = millisecond $\mu sec$ = microsecond $nsec$ = nanosecond	Symbol t
Current	$a$ = ampere $ma$ = milliampere $\mu a$ = microampere	Symbol I or i
Voltage	$v$ = volt $mv$ = millivolt $\mu v$ = microvolt $kv$ = kilovolt	Symbol E or v
Power	$W$ = watt $mW$ = milliwatt $\mu w$ = microwatt $kW$ = kilowatt $MW$ = megawatt	Symbol W

Technical abbreviations appear in electronics text material, in circuit diagrams, in reports and in magazine articles. There is no industry-wide style standard. The best that can be hoped for is that a selected style will be consistent throughout a book, report or article. Abbreviations may be in lower-case, capital letters or some combination of both. Abbreviations may or may not have points (periods). Points are desirable where the abbreviation may be mistaken for a word.

Table 14-2. Table Electronic Abbreviations

Abbreviation	Term
A	
a	alpha, ammeter, ampere, area
A	ammeter, ampere (s)
o	
A	Angstrom unit
abc	automatic base compensation
AC	alternating current or voltage
acc	automatic chroma control
adf	automatic direction finder
adj	adjacent; adjustment
af	audio frequency
afc	automatic frequency control
aft	audio-frequency transformer; automatic fine tuning
agc	automatic gain control
Ah	ampere-hour
alc	automatic level control
AM	amplitude modulation
amp	ampere (s); amplifier
amp-hr	ampere hour
AND	gate
anl	automatic noise limiter
anr	automatic noise reduction
ant	antenna
antilog	antilogarithm
apc	automatic phase control
apl	Automatic program locating device
arm	armature
ASA	American Standards Association
att	attenuator; attenuation
atto	$10^{-18}$
autotrans	autotransformer
aux	auxiliary
av	average
avc	automatic volume control
ave	automatic volume expansion
AWG	American wire gauge
B	
b	bel; beta, magnetic flux density
b or base	base (transistor)
B	magnetic flux density; susceptance
bal	balance

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
bal mod	balanced modulator
balun	balanced-to-unbalanced transformer
batt	battery
bcd	binary coded decimal
bci	broadcast interference
bcl	broadcast listener
bfo	beat-frequency oscillator
bin	binary
bit (s)	binary digit (s)
bo	Barkhausen oscillation
bp	bandpass
bto	blocking-tube oscillator
Btu	British thermal unit
<b>C</b>	
c	centi—(one-hundredth; 10-2); collector (transistor); Celsius (degrees)
c, cap	capacitor (or capacitance)
C	Celsius
calib	calibrate
cath (K on diagram)	cathode
cath foll	cathode follower
CB	citizens' band
cc	cotton covered (wire)
cctv	closed circuit television
ccw	counterclockwise
cemf	counter electromotive force
cent	centering
centi (or c)	10 <sup>2</sup>
c <sub>gk</sub>	grid-cathode capacitance (tube)
c <sub>pp</sub>	grid-plate capacitance (tube)
cgs	centimeter-gram-second
ch	choke
chan	channel
chg	charge
chrome	chromium
cir mil (s)	circular mil(s)
ckt brkr	circuit breaker
cm	centimeters
coax	coaxial cable
colog	cologarithm
com	common
cond	conductor
conn	connection
cont	control
conv	convergence; converter
cos	cosine
cosh	hyperbolic cosine
cot	cotangent
counter emf; cemf	counter electromotive force
cps	cycles per second (Hertz)
c-r	cathode-ray
cro	cathode-ray oscilloscope

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
CrO <sub>2</sub>	chromium dioxide
crt	cathode-ray tube
csc; cosc	cosecant
ct	center tap
cw	clockwise; continuous wave
<b>D</b>	
d	diode; deci—(one-tenth; 10 <sup>-1</sup> ); diameter
dB	decibel
dBf	signal reference to power
dbl <sup>r</sup>	doubler
dbm	decibels referred to 1 milliwatt across 600 ohms
dc	direct current or voltage
dc rest	dc restorer
dcc	double cotton covered (wire)
deci	10 <sup>-1</sup>
defl	deflection
deg	degrees (angle); degrees (temp.)
deka	10 <sup>1</sup>
demod	demodulator
det	detector
dielec	dielectric
diff	differentiator
DIN	Deutsche Industrie Normen (German Industrial Standards)
disch	discharge
discrim	discriminator
dk	deka—(ten; 10 <sup>1</sup> )
dkm	decameters
dm	decimeters
dpdt	double-pole, double-throw (switch)
dpst	double-pole, single-throw (switch)
dsc	double silk covered (wire)
dx	distance
dyn	dynamic
<b>E</b>	
e	emitter (transistor); voltage; electronic charge
ec	enamel covered
eco	electron-coupled oscillator
eff	effective (rms)
ehf	extremely high frequencies (30 GHz to 300 GHz)
EDP	Electronic Data Processing
EIA	Electronic Industries Association
EIAJ	Electronic Industries Association of Japan
elec	electric; electrolytic
elect	electrode
emf	electromotive force (voltage)

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
emu	electromagnetic unit (s)
enam	enameled (wire)
encl	enclosure
ep	extended play
eq	equalization
equiv	equivalent
erase hd	erase head
erf	error function
erp	effective radiated power
esu	electrostatic unit (s)
ev (or eV)	electron volt(s)
ext	external or extension
<b>F</b>	
f	femto ( $10^{-15}$ )
f or freq	frequency
F	Fahrenheit (degrees)
F	farad(s)
fax	facsimile
fa	femtoampere $10^{-15}$ ampere
FCC	Federal Communications Commission
FeCr	ferrichrome
femto	$10^{-15}$
FET	field effect transistor
ff	fast forward
FHR	Fixed Head Recorder
fil (f in diagrams)	filament
fm	frequency modulation
foll	follower (-ing)
fone	headphones; earphones (see also phone)
freq	frequency
FS	Fourier series
<b>G</b>	
G	conductance
g	gram; grid (in diagrams); conductance
gb	gilberts
gca	ground-controlled approach
gdo	grid-dip oscillator
gen	generator
GHz	gigahertz (kilomegahertz)
giga	$10^9$
Gm	Mutual Conductance
gnd	ground
<b>H</b>	
H	magnetic intensity
h	henry (s); hepto or hekto (one hundred; $10^2$ )
ham	radio amateur operator

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
hd	head
hecto	$10^2$
hex	hexadecimal
hf	high frequency (3,000 to 30,000 kHz); high filter
hi fi	High fidelity
hi pot	high potential
hm	hectometers
hor or horiz	horizontal
hp	horsepower
hr	hour
hter (in diagrams)	heater
hv	high voltage
hvr	home video recorder
hy	henry
Hz	Hertz (cycles per second)
 I	
i	current (instantaneous value)
ic	internal connection (in tubes); integrated circuit
icw	interrupted continuous waves
i-f or i.f.	intermediate frequency
i-f or i.f.t.	intermediate-frequency transformer
IHF	Institute of High Fidelity
ils	instrument landing system
im	intermodulation; intermodulation distortion
in	inch; input
int	integrator
ip	plate current
ips	inches per second
 J	
j;J	joule; imaginary number
jb	junction box
jct	junction
 K	
K	numerical constant; dielectric constant; coupling coefficient
k	kilo; thousand; $10^3$
cathode (tube)	
kg	kilogram
kHz	kilohertz
kilo	$10^3$
km	kilometers
kv	kilovolt (s)
kva	kilovolt-ampere
kvar	reactive kilovolt amperes
kw	kilowatt
kwhr	kilowatt-hour

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
L	
L	coil; inductor; inductance; load
LC	Inductance-capacitance
lcd	liquid crystal diode
led	light emitting diode
If	low frequency (30 to 300 kHz)
lin	linearity; linear
lm	limiter
In; loge	Napierian logarithm
log; log <sub>10</sub>	common logarithm
log <sup>-1</sup>	antilogarithm
lp	long playing
ls	limit switch
lsi	large scale integration
LVR	Longitudinal Video Recording
M	
m	million ( $10^6$ ); meter; mutual inductance
$\mu$	micro ( $10^{-6}$ )
$\mu a$	amplification factor; permeability
ma	microampere
mag	milliampere
max	magnetic
md	moving coil
meg	megohm
mega	million; ( $10^6$ )
mem	memory
mev	million electron volts
$\mu f$	microfarad
mf	medium frequencies (300 kHz to 3,000 kHz)
mfb	motional feedback
mh	millihenry (s)
MHz	megahertz
$\mu h$	microhenry (s)
micro	one-millionth; ( $10^{-6}$ )
micromicro	one-millionth of a millionth; ( $10^{-12}$ ) (see also pico)
mike (or mic)	microphone
milli	$10^{-3}$
min	minimum
mks	meter-kilogram-second
$\mu \mu$	micromicro ( $10^{-12}$ ) (same as pico)
$\mu \mu f$	micromicrofarad (same as picofarad)
mm	millimeters; moving magnet
mmf	magnetomotive force
mod	modulation; modulator; modulus
modem	modulator-demodulator
mol	maximum output level
mon	monitor
mono	monophonic; monochrome; monaural

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
mos	metal oxide semiconductor
mosfet	metal oxide semiconductor field effect transistor
most	metal oxide semiconductor transistor
mpx	multiplex
$\mu$ sec	microsecond
msec	millisecond
mpx	multiplex
mult	multiplier
$\mu$ v	microvolt
mv	multivibrator; millivolt
mva	megavolt-ampere
mvb	multivibrator
mvc	manual volume control
$\mu$ v/m	microvolts per meter
$\mu$ w	microwatt
Mw	megawatt
mw	milliwatt
Mwh	megawatt-hour
my	myria; (ten thousand; $10^4$ )
mym	myriameters
<b>N</b>	
n	nano; ( $10^{-9}$ ) number of turns
NAB	National Assoc. of Broadcasters
NAND	gate
nano(n)	$10^{-9}$
nbfm	narrow-band fm
nc	normally-closed (switch or relay); neutralizing capacitor; no connection
ne	neon
neg	negative; minus
net	network
nf	negative feedback
NI	ampere turns
no	normally open (switch or relay)
npn	negative-positive-negative (transistor)
n-type	semiconductor with excess of negative carriers
nvr	no voltage release
<b>O</b>	
OD	outside diameter
omni	omnidirectional
	or gate
o/v	ohms per volt
osc	oscillator
out	output
<b>P</b>	
p	power; pole; plate(on diagrams); pico ( $10^{-12}$ )

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
pa	public address; power amplifier
pb	playback
pc	photocell
pcm	pulse code modulation
pd	potential difference
pent	pentode
perm	permanent
pf	power factor; picofarad (micromicrofarad)
phone (s) (or fone)	headphones; earphones
photo mult	photomultiplier
pico	formerly designated as micromicro ( $10^{-12}$ )
pix	picture
pl	pilot lamp
pil	phase locked loop
pm	permanent magnet (speaker); phase modulation; pulse modulation
pn	diode or transistor junction
pnp	positive-negative-positive (transistor)
pos	positive; plus
pot	potentiometer; potential
pp	peak-to-peak; pushpull
ppl	plan-position indicator (radar)
ppm	parts per million
pps	pulses per second
preamp	preamplifier
prf	pulse repetition frequency
pri	primary
pt	phototube
p-type	semiconductor with excess of positive carriers
pwr	power
Q	
Q	reactance-resistance ratio; transistor; coulomb;
	Q factor; Q signal
quad	quadrature, quadraphonic (quadriphonic)
R	
r	resistance; resistor; radius
rc	resistance-capacitance
r-c	radio control
rdg	recording
rcdr	recorder
rcvr	receiver
rec	record
rect	rectifier
reg	regulator
regen	regeneration
rev	reverse
reverb	reverberation

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
rf	radio frequency
rfc	radio-frequency choke
rft	radio-frequency transformer
rheo	rheostat
r-i	resistance-inductance
r-i-c	resistance-inductance-capacitance
RIAA	Record Industry Association of America
rms	root-mean-square; effective
rpm	revolutions per minute
ry	relay
ry, nc	relay, normally closed
ry, no	relay, normally open
<b>S</b>	
s or sw	switch
scc	single-cotton covered (wire)
sce	single cotton enameled (wire)
scope	oscilloscope
scr	silicon-controlled rectifier
sec	second; secondary; secant
sech	hyperbolic secant
sels	selsyn
sep	separator
sg	screen grid
shf	super-high frequency (3,000 to 300,000 MHz)
sig	signal
sin	sine
sinh	hyperbolic sine
sld	solenoid
s/n	signal-to-noise ratio
sp	single-pole
spdt	single-pole, double-throw
spdtcb	single-pole, double-throw, double-break
spdtncdb	single-pole, double-throw, normally-closed, double break
spdtno	single-pole, double-throw, normally-open
spdtndb	single-pole, double-throw, normally-open, double-break
spec(s)	specifications
spkr	loudspeaker
spl	sound pressure level
spstnc	single-pole, single-throw, normally-closed
spstno	single-pole, single-throw, normally-open
sq	square
ssb	single sideband
ssc	single silk covered (wire)
stereo	stereophonic

Table 14-2. Electronic Abbreviations (cont'd)

Abbreviation	Term
strobe	stroboscope
sup	suppressor
superhet	superheterodyne
sw	switch; short wave
swl	short-wave listener
swr	standing-wave ratio
sync	synchronization; synchronous
T	
t	transformer; trimmer capacitor; tera; ( $10^{12}$ )
tacho	tachometer
tan	tangent
tanh	hyperbolic tangent
teleg	telegraph; telegram
tera	$10^{12}$
term	terminal
thd	total harmonic distortion
TI	ampere turns
TIM	Transient Intermodulation Distortion
tptg	tuned-plate; tuned-grid
tr	transmit-receive; turns ratio; transient response
trans	transformer
trf	tuned-radio frequency
trig	trigger
tsf	telegraphie sans fil (wireless telegraphy)
tv	television
tvil	television interference
U	
uhf	ultra-high frequencies (300 to 3,000 MHz)
UL	Underwriters' Laboratories, Inc.
V	
v	volt(s); transistor; voltmeter
va	voltamperes (apparent power)
vac;vdc	voltage amplifier
var	volts ac, dc
vc	variable; reactive volt-amperes; varistor
vcr	voice coil
vers	video cassette recorder
vert	versed sine
vfo	vertical
vhf	variable frequency oscillator
vid	very high frequencies (30 to 300 MHz)
vif	video
v/m	very low frequencies (below 30 kHz)
vol	volts per meter
vom	volume
vr	volt-ohm-milliammeter; volt-ohmmeter
	voltage regulator (tube)

Table 14-2. Electronic Abbreviations (cont'd)

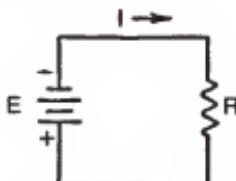
Abbreviations	Term
vt or v	tube
vtf	vertical tracking force
vtvm	vacuum-tube voltmeter
vu	volume unit
W	
w	watt (s)
whr	watt-hour
wrms	weighted rms
WVDC	working volts, DC
X	
x	reactance
X <sub>c</sub>	capacitive reactance
X <sub>L</sub>	inductive reactance
xformer	transformer
xmit	transmitter
xmission	transmission
xtal	crystal
Y	
Y	admittance
Z	
z	impedance; characteristic impedance

Table 14-3. Electronic Formulas

**DC CIRCUITS**

$$\begin{aligned} I &= E/R = P/E = \sqrt{P/R} \\ R &= E/I = P/I^2 = E^2/P \\ E &= IR = P/I = \sqrt{PR} \\ P &= EI = E^2/R = I^2R \end{aligned}$$

**DESCRIPTION**  
Ohm's law  
R is in ohms; I in  
amperes; E in volts and  
P in watts



**Resistors in Series**

$$R_{\text{t}} = R_1 + R_2 + R_3 \dots$$

Resistance, R, is in  
ohms, or identical  
multiples

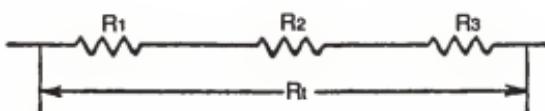


Table 14-3. Electronic Formulas (cont'd)

Two Resistors in Parallel

$$R_t = \frac{R_1 \times R_2}{R_1 + R_2}$$

$$\frac{1}{R_t} = \frac{1}{R_1} + \frac{1}{R_2}$$

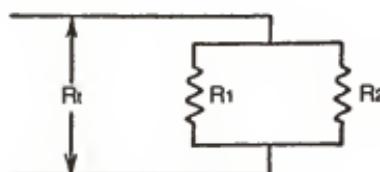
$$R_t = \frac{R_1}{2} \text{ or } \frac{R_2}{2}$$

(when both resistors are identical)  
 Three or more Resistors in Parallel

$$\frac{1}{R_t} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots$$

$$R_t = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

$$R_t = \frac{R_1}{1 + R_1/R_2 + R_1/R_3 + R_1/R_4}$$



Conductances in Parallel

$$G_t = G_1 + G_2 + G_3 \dots$$

$$E = I/G$$

$$I = E/G$$

$$R = 1/g$$

G in mhos  
 Ohm's law for conductance  
 E is in volts, I in amperes  
 conductance, G, in mhos

Two Conductances in Parallel

$$IR_1 = \frac{I_t \times G_1}{G_2 + G_2}$$

$$IR_2 = \frac{I_t \times G_2}{G_2 + G_2}$$

$$G = \frac{1}{R}$$

$$\frac{1}{G}$$

G in mhos  
 R in ohms

Resistance of a Conductor

$$R = K \frac{L}{D^2}$$

R is ohms; K is  
 resistance of a mil-foot  
 (specific resistance);  
 L is length in feet and  
 D is diameter in mils

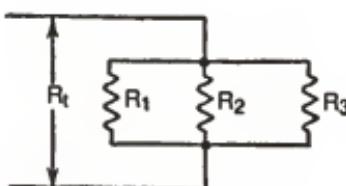
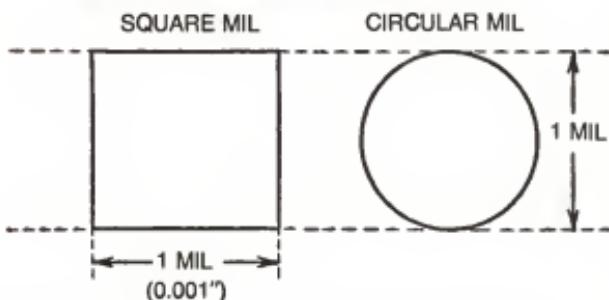


Table 14-3 Electronic Formulas (cont'd)



**Heating Effect of a Current**

$$H = 0.057168 \times R$$

$$F = (C \times 9/5) + 32$$

$$C = (F - 32) \times 59$$

H is heat in calories/sec;  
R is resistance in ohms

F is temperature in degrees Fahrenheit  
C is temperature in degrees Celsius (formerly Centigrade)

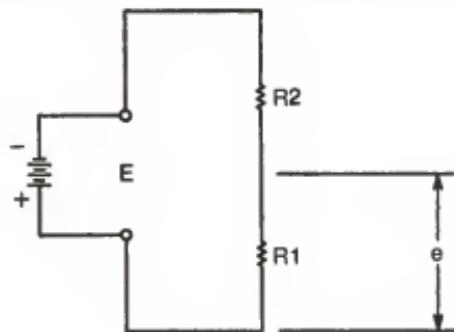
$$\eta = P_o/P_i$$

n is efficiency  
P<sub>o</sub> is output power  
P<sub>i</sub> is input power  
multiply answer by 100 to obtain efficiency in terms of percentage rather than a decimal

**Voltage Drop**

$$e = E \times \frac{R_1}{R_1 + R_2}$$

E is the DC source voltage  
R<sup>1</sup> and R<sup>2</sup> are series resistors  
e is voltage across R<sup>1</sup>



**Horsepower**

$$1 \text{ HP} = 746 \text{ watts} = 550 \text{ ft lbs/sec}$$

$$1 \text{ watt} = 1/746 \text{ HP} = 0.00134 \text{ HP} \quad \text{HP is horsepower}$$

$$kW = \frac{\text{HP} \times 746}{10^3}$$

**Table 14-3. Electronic Formulas (cont'd)**

**Shunt Law**

$$I_1 \times R_1 = I_2 \times R_2$$

$I_1$  and  $I_2$  are currents in amperes

$$I_1 = \frac{I_2 \times R_2}{R_1}$$

$R_1$  and  $R_2$  are resistance in ohms.

$$I_2 = \frac{I_1 \times R_1}{R_2}$$

$$R_1 = \frac{I_2 \times R_2}{I_1}$$

$$R_2 = \frac{I_1 \times R_1}{I_2}$$

**Kirchhoff's Law for Current**

$$I_1 + I_2 + I_3 = 0$$

The sum of the currents flowing toward a junction is zero.

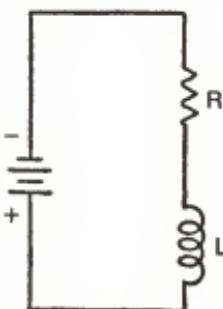
**Kirchhoff's Voltage Law**

$$E_1 + E_2 + E_3 = 0$$

The sum of the voltage drops in a closed loop is equal to zero.

**Time Constant for Series RL**

$$t = L/R$$

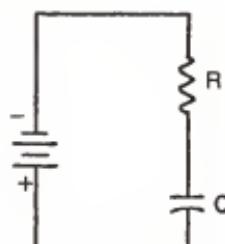


$t$  is the time (in seconds) for current to reach 63.2% of peak;  $L$  is in henrys and  $R$  is in ohms.

**Time Constant for Series RC**

$t$  is the time (in seconds) for the voltage across the capacitor to reach 63.2% of peak;  $R$  is in ohms and  $C$  is in farads

$$t = R \times C$$



**Table 14-3. Electronic Formulas (cont'd)**

**Meters (Measuring Instruments)**

$$I_s + R_s = I_m \times R_m$$

$I_s$  is shunt current;  $I_m$  is meter current; both must be in same current units.  $R_s$  is meter resistance both must be in same resistance units

**Meter Multiplier Resistance**

$$R = (R_m (n - 1))$$

$R$  is value of multiplier resistance;  $R_m$  is meter resistance and  $n$  is the multiplication factor

**Meter Sensitivity**

$$M_s = \frac{R_m + R_1}{E}$$

$M_s$  is meter sensitivity in ohms per volt;  $R_m$  is meter resistance and  $R_1$  is multiplier resistance.  $E$  is full scale reading in volts.

**Wheatstone Bridge**

$$R_r = \frac{R_3 \times R_2}{R_1}$$

$R_r$  is unknown resistance value;  $R_1$ ,  $R_2$  and  $R_3$  are bridge resistance elements

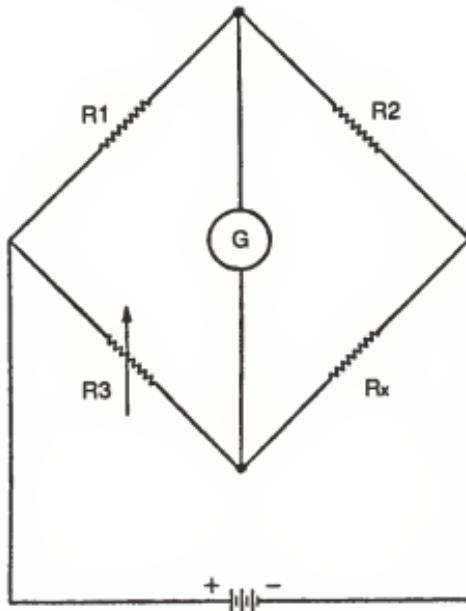
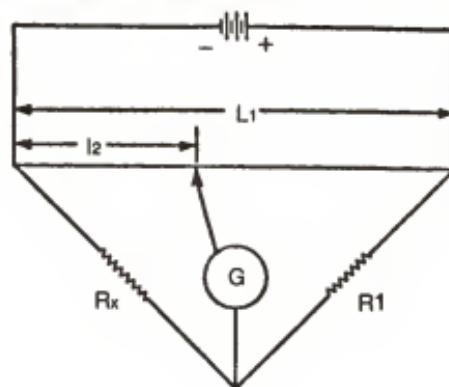


Table 14-3. Electronic Formulas (cont'd)

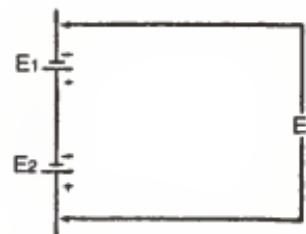
**Slide-Wire Bridge**

$$R_f = \frac{L_2}{L_1 - L_2} \times R_1$$



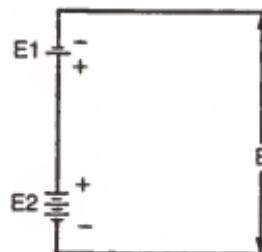
**Voltages In Series-Aiding**

$$E_t = E_1 + E_2$$



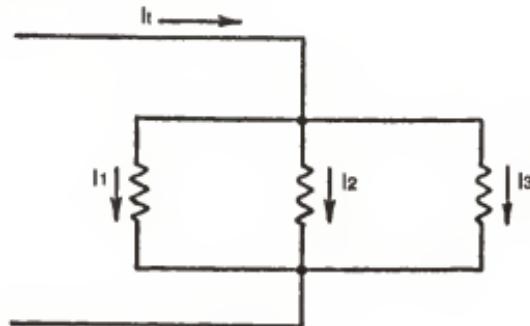
**Voltages In Series-Opposing**

$$E_t = E_2 - E_1$$



**Line and Branch Currents**

$$I_t = I_1 + I_2 + I_3$$



**Table 14-3. Electronic Formulas (cont'd)**

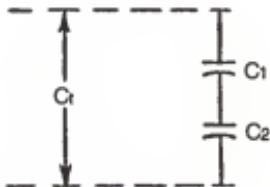
### AC CIRCUITS

Capacitors in Series

$$C_1 = \frac{C_1 \times C_2}{C_1 + C_2}$$

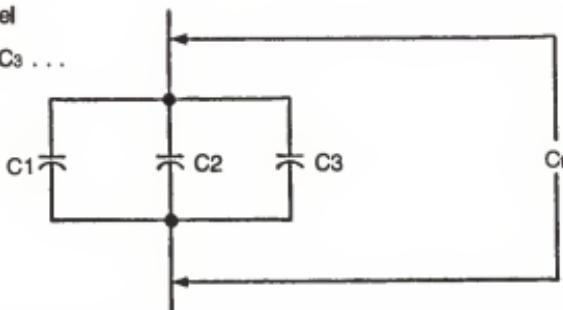
All capacitance units must be in farads or in identical submultiples

$$\frac{1}{C_1} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \dots$$



Capacitors in Parallel

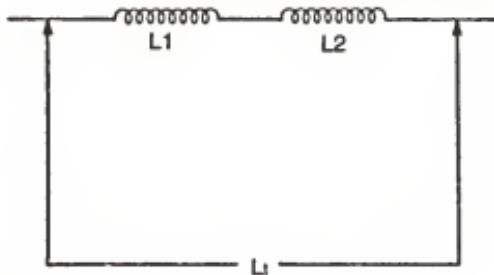
$$C_1 = C_1 + C_2 + C_3 \dots$$



Inductors in Series (no coupling)

$$L_t = L_1 + L_2$$

All inductance units must be in henrys or identical submultiples



Inductors in Series-Aiding

$$L_t = L_1 + L_2 + 2M$$

$m$  is mutual inductance, in henrys

**Table 14-3. Electronic Formulas (cont'd)**

**Inductors in Series-Opposing**

$$L_1 = L_1 + L_2 - 2M$$

**Inductors in Parallel (no coupling)**

$$L_1 = \frac{L_1 \times L_2}{L_1 + L_2}$$

**Frequency-Wavelength of Sine Wave**

$$\lambda = 3 \times 10^8 / f$$

$\lambda$  is wavelength in meters  
f is frequency in kHz

**Period of a Sine Wave**

$$t = 1/f$$

t is time in seconds; f is frequency in Hz

**Sine Wave Voltages or Currents**

$$E_{av} = 0.637 \times E_{peak}$$

$$E_{av} = 1.274 \times E_{peak-to-peak}$$

$$E_{av} = E_{peak}/1.57$$

$$E_{peak} = 0.5E_{peak-to-peak}$$

$$E_{av} = 0.3185 E_{peak-to-peak}$$

$$E_{eff} = \frac{E_{peak}}{\sqrt{2}} = \frac{E_{peak}}{1.414} = 0.707E_{peak}$$

**Susceptance**

$$B = \frac{X}{R^2 + X^2}$$

B is susceptance in mhos  
R = resistive ohms  
X = reactive ohms

$$B = 1/X$$

B = susceptance in mhos  
X = reactive ohms

**Power in AC Circuit**

$$P = E \times I$$

P is apparent power in watts:  
E is voltage in volts and I is current in amperes

True Power:  $P = EI \cos \phi = EI \times pf$   
 $pf = P/EI = \cos \phi$   
 $\cos \phi = \text{true power/apparent power}$

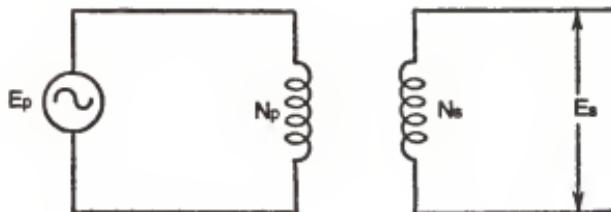
pf = power factor

Table 14-3. Electronic Formulas (cont'd)

Transformers

$$\frac{E_p}{E_s} = \frac{N_p}{N_s}$$

$E_p$  is voltage across primary winding  
 $E_s$  is voltage across secondary  
 $N_p$  = number of primary turns  
 $N_s$  = number of secondary turns



$$\frac{I_p}{I_s} = \frac{N_s}{N_p}$$

$I_p$  = primary current  
 $I_s$  = secondary current  
 voltages and currents must be in basic units or similar multiples

$$Tr = \sqrt{\frac{Z_s}{Z_p}} = \frac{N_s}{N_p}$$

$Tr$  = turns ratio:  $Z_s$  and  $Z_p$  are secondary and primary impedances in ohms;  $N_p$  = primary turns;  $N_s$  = secondary turns

Capacitive Reactance

$$X_C = \frac{1}{2\pi f C}$$

$\pi = 3.14159$  approximately  
 $f$  is frequency in Hz;  $C$  is capacitance in farads  
 $L$  is inductance in henrys

Inductance Reactance

$$X_L = 2\pi f L$$

Ohm's Law for AC

$$E_C = I \times X_C$$

$$E_L = I \times X_L$$

$$E_R = I \times R$$

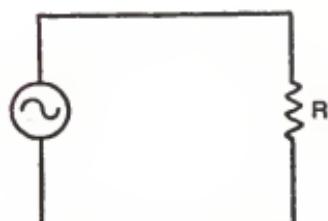


Table 14-3. Electronic Formulas (cont'd)

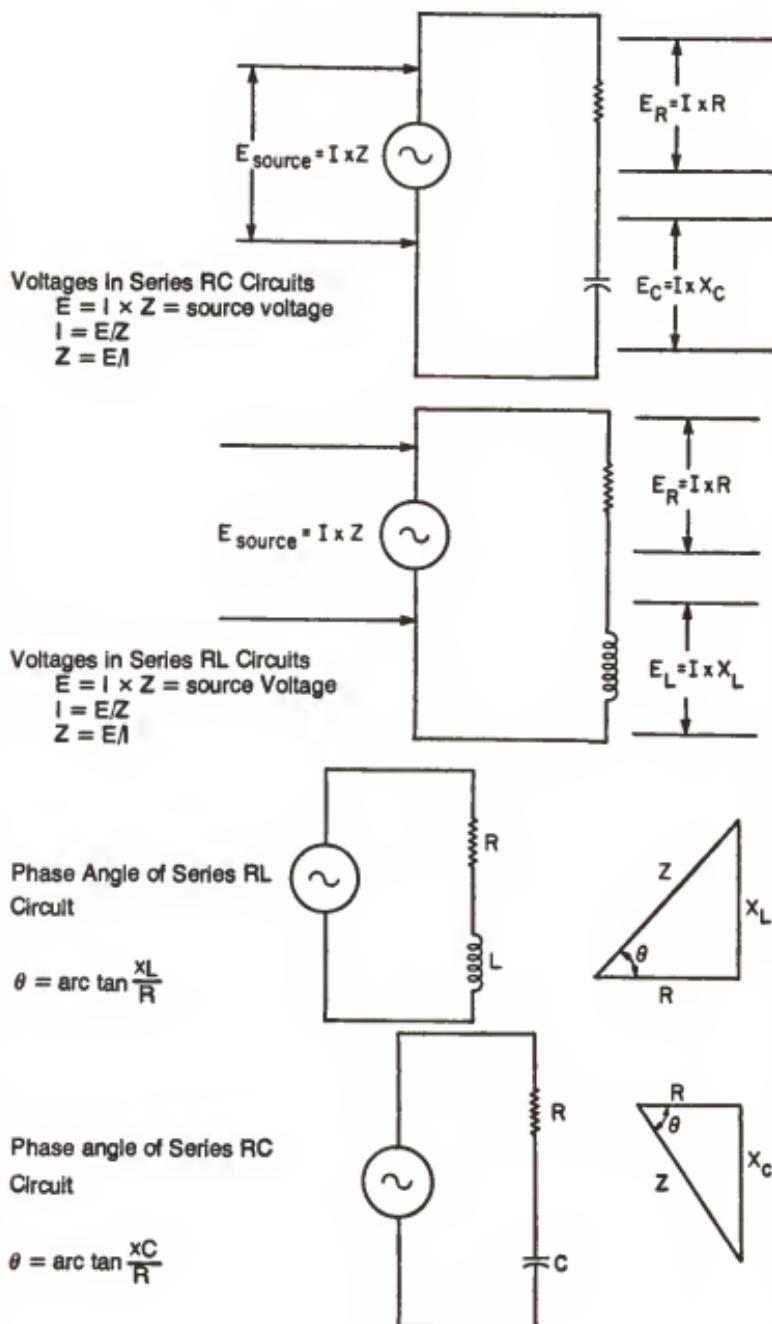
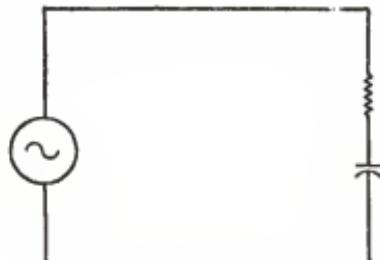


Table 14-3. Electronic Formulas (cont'd)

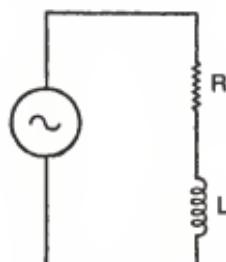
Impedance of R Circuit

$$Z = R$$



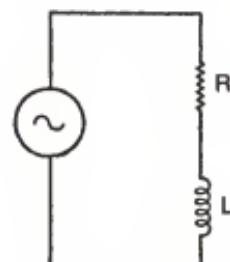
Impedance of Series RC Circuit

$$Z = \sqrt{R^2 + X_c^2}$$



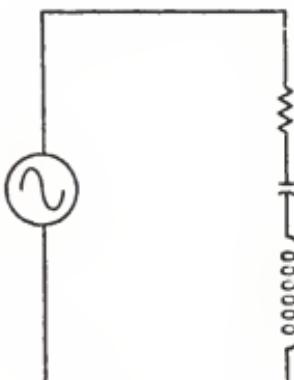
Impedance of Series RL Circuit

$$Z = \sqrt{R^2 + X_L^2}$$



Impedance of Series RLC Circuit

$$Z = \sqrt{R^2 + (X_L - X_c)^2}$$



Impedance of Parallel RL Circuit

$$Z = \frac{RX_L}{\sqrt{R^2 + X_L^2}}$$

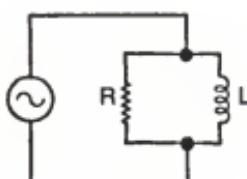
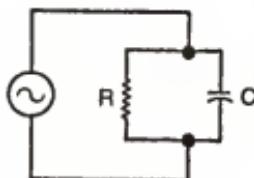


Table 14-3. Electronic Formulas (cont'd)

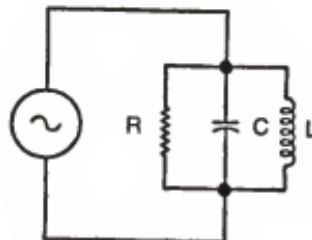
**Impedance of Parallel RC Circuit**

$$Z = \frac{RX_c}{\sqrt{R^2 + X_c^2}}$$



**Impedance of Parallel RLC Circuit**

$$Z = \frac{RX_L X_C}{\sqrt{X_L^2 X_C^2 + R^2(X_L - X_C)^2}}$$



**Impedance**

At resonance:  $X_L = X_C$

**Resonant Frequency**

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$f_0$  is the frequency in hertz.  
L is in henrys; C in farads

**Series Resonance**

$$\begin{aligned} Z \text{ (at any frequency)} &= R + j(X_L - X_C) \\ Z \text{ (at resonance)} &= R \end{aligned}$$

**Parallel Resonance**

$$\begin{aligned} Z_{\max} \text{ (at resonance)} &= \frac{X_L X_C}{R} = \frac{X_L^2}{R} \\ (X_L = X_C) &= QX_L = \frac{L}{RC} \end{aligned}$$

**Impedance and Phase Angle of Series RL Shunted by C**

$$Z = X_C \sqrt{\frac{R^2 X_L^2}{R^2 + (X_L - X_C)^2}}$$

$$\phi = \arctan \frac{X_L (X_C - X_L) - R^2}{R X_C}$$

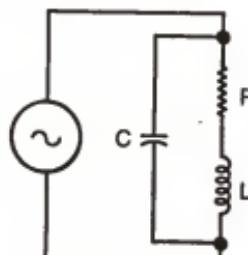


Table 14-3. Electronic Formulas (cont'd)

**Bandwidth**

$$\Delta = \frac{f_0}{Q} = \frac{R}{2\pi L}$$

**Tube Characteristics**

$$\mu = \frac{\Delta e_p}{\Delta e_\mu} \quad (\text{i}_p \text{ constant}) \qquad \mu \text{ is amplification factor}$$

$$g_m = g_m \times r_p \qquad g_m \text{ is grid-plate transconductance} \\ r_p \text{ is AC plate resistance}$$

$$r_p = \frac{\Delta e_p}{\Delta i_p} \quad (e_g \text{ constant})$$

$$g_m = \frac{\Delta i_p}{\Delta e_g} \quad (e_p \text{ constant})$$

**Transistor Characteristics**

$$\alpha = \frac{\Delta i_c}{\Delta i_e} \qquad \alpha \text{ is current gain; } i_c \text{ is} \\ \text{collector current; } i_e \text{ is emitter current}$$

**Resistance Gain**

$$r_g = \frac{r_o}{n} \qquad r_g \text{ is resistance gain; } r_o \text{ is} \\ \text{output resistance; } r_i \text{ is input resistance}$$

**Voltage Gain**

$$v_g = \frac{e_o}{e} = \frac{i_c r_o}{i_e r_i} = \alpha \frac{r_o}{r_i} \qquad e_o \text{ is output voltage} \\ e_i \text{ is input voltage}$$

**Power Gain**

$$P_g = \alpha^2 \frac{r_o}{r_i}$$

**Base Current Amplification Factor**

$$\beta = \frac{\Delta i_c}{\Delta i_b} \qquad i_c \text{ is collector current} \\ \beta \text{ is base current amplification factor}$$

Table 14-3. Electronic Formulas (cont'd)

Decibels (power ration)

$$dB = 10 \log P_2/P_1$$

Decibels (current and voltage ratio)

$$dB = 20 \log \frac{I_2 \sqrt{R_2}}{I_1 \sqrt{R_1}}$$

log to base 10

$$dB = 20 \log \frac{E_2 \sqrt{R_1}}{E_1 \sqrt{R_2}}$$

When Reference Level is 1 milliwatt

$$dB_m = 10 \log P/0.001$$

P is in watts

$$dB_f = 20 \log (\mu V/0.55)$$



# Chapter 15

## Transistors

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### TRANSISTOR ALPHA AND BETA

The current amplification factor of a transistor can be expressed in terms of either alpha ( $\alpha$ ) or beta ( $\beta$ ). The ratio between a change in collector current for a change in emitter current is called alpha, and since alpha is less than unity, you will find it given as a decimal.

When we change emitter current we not only change collector current but base current as well. The ratio of a change in collector current to a change in base current is also used as a measure of the amplification of a transistor and is represented by beta.

The relationship between alpha and beta is shown in these formulas:

$$\beta = \alpha / 1 - \alpha$$

or

$$\alpha = 1 - 1 / [\beta + 1]$$

Because alpha is a decimal it sometimes makes a problem awkward to handle. For this reason it is sometimes more convenient to give current amplification as beta. Since beta is always in whole numbers it becomes convenient when comparing the current gains of different transistors.

Table 15-1 supplies common values of alpha and corresponding values for beta. The range of alpha is from 0.5 to 0.9964; that of beta is from 1 to 270.

□Example:

The current gain (alpha) of a transistor is 0.9730. What is its current gain in terms of beta?

Table 15-1. Alpha vs Beta.

$\beta$	$\alpha$	$\beta$	$\alpha$	$\beta$	$\alpha$
1	0.5000	40	0.9756	79	0.9875
2	0.6666	41	0.9762	80	0.9877
3	0.7500	42	0.9767	81	0.9878
4	0.8000	43	0.9773	82	0.9880
5	0.8333	44	0.9778	83	0.9881
6	0.8571	45	0.9782	84	0.9882
7	0.8750	46	0.9786	85	0.9884
8	0.8889	47	0.9792	86	0.9885
9	0.9000	48	0.9796	87	0.9886
10	0.9091	49	0.9800	88	0.9888
11	0.9167	50	0.9804	89	0.9889
12	0.9231	51	0.9808	90	0.9890
13	0.9286	52	0.9811	91	0.9891
14	0.9333	53	0.9815	92	0.9892
15	0.9375	54	0.9818	93	0.9894
16	0.9412	55	0.9821	94	0.9895
17	0.9444	56	0.9825	95	0.9896
18	0.9474	57	0.9828	96	0.9897
19	0.9500	58	0.9831	97	0.9898
20	0.9524	59	0.9833	98	0.9899
21	0.9545	60	0.9836	99	0.9900
22	0.9565	61	0.9839	100	0.9901
23	0.9583	62	0.9841	110	0.9909
24	0.9600	63	0.9844	120	0.9917
25	0.9615	64	0.9846	125	0.9921
26	0.9630	65	0.9848	130	0.9931
27	0.9643	66	0.9851	140	0.9932
28	0.9655	67	0.9853	150	0.9933
29	0.9667	68	0.9855	160	0.9938
30	0.9677	69	0.9857	170	0.9942
31	0.9688	70	0.9859	180	0.9945
32	0.9697	71	0.9861	190	0.9948
33	0.9706	72	0.9863	200	0.9952
34	0.9714	73	0.9865	210	0.9954
35	0.9722	74	0.9867	220	0.9956
36	0.9730	75	0.9868	230	0.9958
37	0.9737	76	0.9870	240	0.9960
38	0.9744	77	0.9872	250	0.9962
39	0.9750	78	0.9873	260	0.9963
				270	0.9964

Table 15-1 shows that an alpha of 0.9730 corresponds to a beta of 36.

**□Example:**

What is the alpha of a transistor if its beta value is 76?

Locate 76 in the column marked beta. To the right find the value of beta in terms of alpha, 0.9870.

## TRANSISTOR TESTING

Transistors can be checked with ohmmeters that have low voltage and low current. Some meters use voltages of 10 volts or more on the high resistance scales and have no current limiting resistor on the low scale, hence such instruments can damage transistors. The method used in Table 15-2 does not indicate the quality of the transistor, simply whether it is good or bad. If the transistor is connected into the circuit, at least two of its three leads must be disconnected. The base is shorted to either of the other elements for the last four tests.

Table 15-2. Method for Testing Transistors

Meter	Connection	(polarity)	Resistance ( $\times 100$ scale)	
Emitter	Base	Collector	PNP type	NPN type
positive negative	negative positive	(none) (none)	low high	high low
(none) (none)	positive negative	negative positive	high low	low high
negative positive	(none) (none)	positive negative	high mid	mid high
positive positive	to emitter to collector	negative negative	high low	
negative negative	to emitter to collector	positive positive		high low

## INTERNAL INPUT AND OUTPUT RESISTANCES OF A TRANSISTOR

There is no isolation between the input and output circuits of a transistor. These are related through their respective resistances, as indicated in Table 15-3.

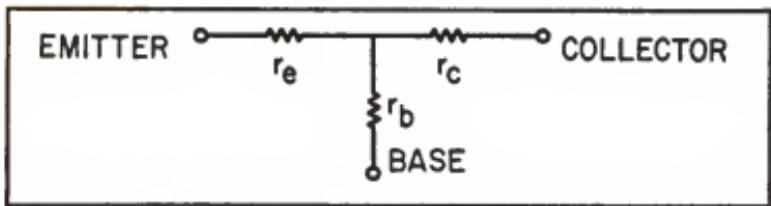


Fig. 15-1. Transistor resistance diagram.

Table 15-3. Transistor Resistances

Circuit	Input resistance	Output resistance
Common base	$r_e + r_b$	$r_c + r_b$
Common emitter	$r_b + r_e$	$r_e + r_c$
Common collector	$r_b + r_c$	$r_e + r_c$

# Chapter 16

## Digital Logic

### LOGIC GATES

Gates are used in a wide variety of electronic equipment. In logic circuits, 1 can represent a closed circuit condition; 0 an open circuit. A closed circuit, or 1, is sometimes called a *true* condition; an open circuit is called false. Figures 16-1 through 16-6 shows basic diagrams, logic symbols and truth tables. Truth tables indicate operating conditions.

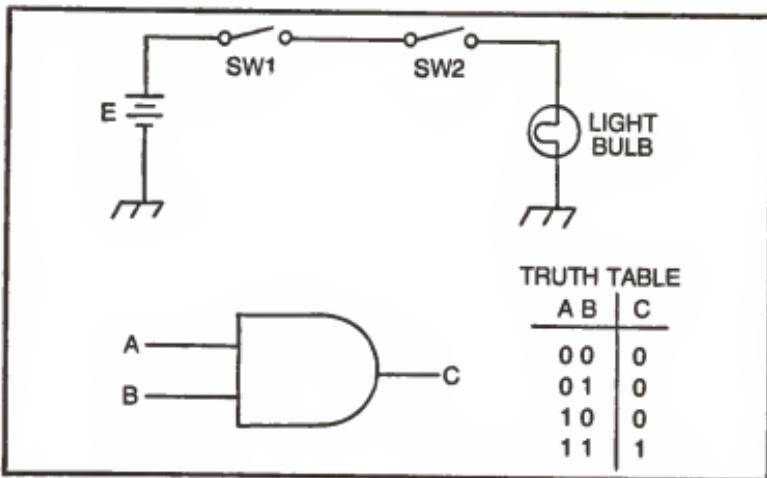


Fig. 16-1. AND gate and its truth table. SW1 and SW2 must be closed for the light bulb to be on.

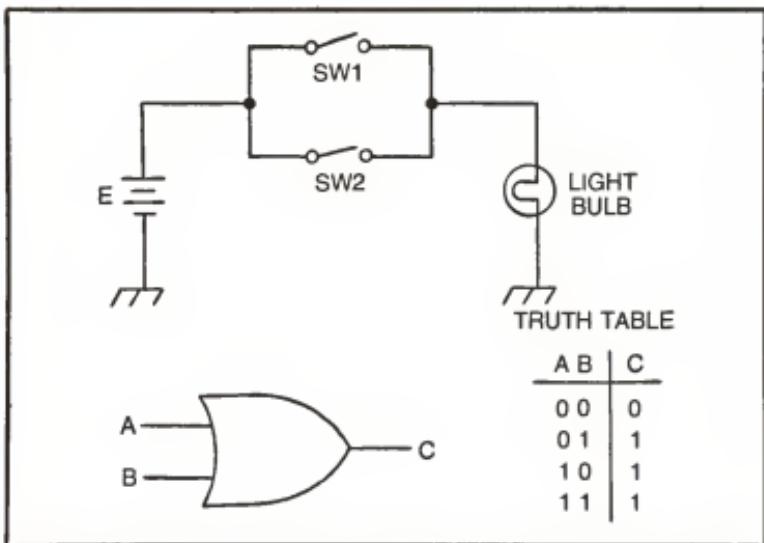


Fig. 16-2. OR gate and its truth table. Either SW1 or SW2 must be closed for the light bulb to be on.

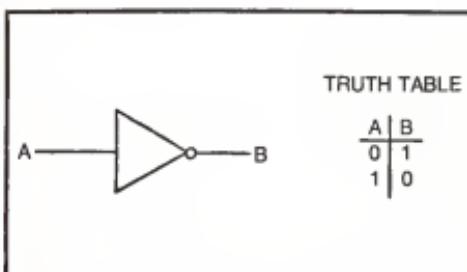


Fig. 16-3.  
Inverter circuit is often used with gates. This circuit changes output from plus to minus, or from minus to plus. The small circle indicates the inversion function. Without it the diagram is that of an ordinary non-inverting amplifier.

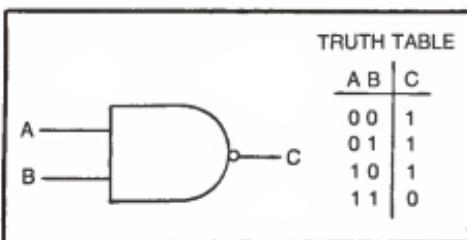


Fig. 16-4.  
NAND gate and its truth table. Same as AND gate but note small circle to indicate inversion of signal.

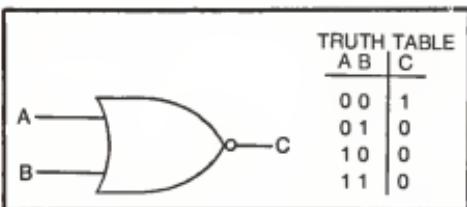


Fig. 16-5.  
NOR gate and its truth table. This is a negative OR gate

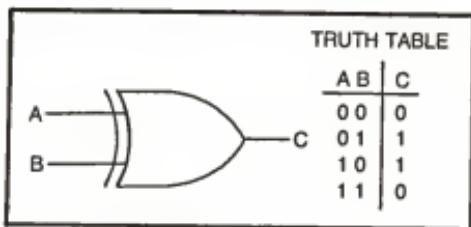


Fig. 16-6.  
Exclusive OR gate. This circuit produces output when inputs are not identical.

## LOGIC DIAGRAMS

The chart in Table 16-1 shows some possible arrangements of AND and OR gates. The small circle attached to the symbol indicates signal inversion. Inversion can be arranged for one input, both inputs, or for the output.

Table 16-1. Logic Diagrams

GATES		TRUTH TABLES		
AND	OR	A	B	C
		0	0	0
		0	1	0
		1	0	0
		1	1	1
		0	0	1
		0	1	0
		1	0	1
		1	1	0
		0	0	0
		0	1	1
		1	0	0
		1	1	0
		0	0	0
		0	1	0
		1	0	1
		0	0	1
		0	1	1
		1	0	0
		1	1	1

## BOOLEAN ALGEBRA

In Boolean algebra, letters are used to represent switches. Boolean algebra is used for the design of switching circuits or logic

gates. A plus symbol is used in place of the work OR. The AND symbol is a dot placed between two letters ( $A \cdot B$ ). Note the dot is moved up a bit so as not to confuse it with a decimal point. The dot symbol for AND is sometimes omitted and the two letters are written immediately adjacent to each other ( $A \cdot B$  is the same as  $AB$ ). The NOT function is shown by a line above a letter or by a prime mark as in  $\bar{A}$  or  $A'$ . See Tables 16-2 and 16-3.

**Table 16-2. Boolean Algebra Definitions.**

**Definitions**

a, b, c, etc.....	Symbols used in symbolic logic
$a + b$ or $ab$ .....	Read as: a or b
$a + b$ .....	Read as: not a
$a'$ or $a$ .....	Read as: not a
1.....	"True" or "on"
0.....	"False" or "Off"
$\bar{A} =$ .....	Read as "not not" A
$\bar{A}B$ .....	Read as "not A AND not B"
$A + B$ .....	Read as "not A OR not B"

**Table 16-3. Theorems in Boolean Algebra.**

$A + A = A$	$A + AB = A$
$A \cdot A = A$	$A(A+B) = A$
$A + 1 = 1$	$\bar{A} + B = \bar{A}B$
$A \cdot 1 = A$	$\bar{A}B = \bar{A} + \bar{B}$
$A + 0 = A$	$A(\bar{A}+B) = AB$
$A \cdot 0 = 0$	$A + \bar{A}B = A + B$
$A + \bar{A} = 1$	$\bar{A} + AB = \bar{A} + B$
$A \cdot \bar{A} = 0$	$\bar{A} + A\bar{B} = \bar{A} + \bar{B}$
$\bar{\bar{A}} = A$	

### BOOLEAN EXPRESSIONS FOR GATING CIRCUITS

Logic circuits can be described in Boolean functions. Figure 16-7 shows various gates and their equivalent Boolean expressions and truth tables.



A	B	AB
0	0	0
0	1	0
1	0	0
1	1	1

AND GATE



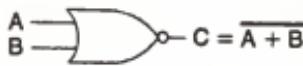
A	B	A + B
0	0	0
0	1	1
1	0	1
1	1	1

OR GATE



A	B	AB̄
0	0	1
0	1	1
1	0	1
1	1	0

NAND GATE



A	B	A + B̄
0	0	1
0	1	0
1	0	0
1	1	0

NOR GATE



A	Ā
0	1
1	0

INVERTER AMPLIFIER

Fig. 16-7. Boolean Logic.



## Chapter 17

# Wire

### GAUGE

The cross sectional area of wire approximately doubles for every three gauge numbers. At the same time the current carrying capacity is doubled. Every wire size becomes 12.3 percent greater in diameter as the wire gauge number is decreased by one. Wire gauges are based on this computation:

Wire gauge diameter (mils)  $\times$  1.123 = diameter of next larger size.

#### □Example:

Gauge 22 wire has a diameter of 25.347 mils

25.347  $\times$  1.123 = 28.464681 mils = diameter of No. 21 wire

Table 17-1. Diameter in mils and area in circular mils of bare copper wire. AWG (American Wire Gauge) or B & S (Browne and Sharpe) Measured at 20 degrees C.

AWG	Diameter, mils, d	Area, circular mils, $d^2$	Ohms per 1000 ft. at 20°C., or 68°F.	1000 ft.
0000	460.00	211,600	0.04901	640.5
000	409.64	167,805	0.06180	508.0
00	364.80	133,079	0.07793	402.8
0	324.86	105,534	0.09827	319.5
1	289.30	83,694	0.1239	253.3
2	257.63	66,373	0.1563	200.9
3	229.42	52,634	0.1970	159.3
4	204.31	41,743	0.2485	126.4
5	181.94	33,102	0.3133	100.2
6	162.02	26,250	0.3951	79.46
7	144.28	20,817	0.4982	63.02

Table 17-1. Diameter in Mils and Area in Circular Mils of Bare Copper Wire. AWG (American Wire Gauge) or B&S (Browne and Sharpe). Measured at 20 degrees C (cont'd)

AWG	Diameter, mils, d	Area, circular mils, $d^2$	Ohms per 1000 ft. at 20°C., or 68°F.	1000 ft.
8	129.49	16,768	0.6282	49.98
9	114.43	13,094	0.7921	39.63
10	101.89	10,382	0.9989	31.43
11	90.742	8,234.1	1.260	24.93
12	80.808	6,529.9	1.588	19.77
13	71.961	5,178.4	2.003	15.68
14	64.084	4,106.8	2.525	12.43
15	57.068	3,256.8	3.184	9.858
16	50.820	2,582.7	4.016	7.818
17	45.257	2,048.2	5.064	6.200
18	40.303	1,624.3	6.385	4.917
19	35.890	1,288.1	8.051	3.899
20	31.961	1,021.5	10.15	3.092
21	28.465	810.10	12.80	2.452
22	25.347	642.47	16.14	1.945
23	22.571	509.45	20.36	1.542
24	20.100	404.01	25.67	1.223
25	17.900	320.41	32.37	0.9699
26	15.940	254.08	40.81	0.7692
27	14.195	201.50	51.47	0.6100
28	12.641	159.79	64.90	0.4837
29	11.257	126.72	81.83	0.3836
30	10.025	100.50	103.2	0.3042
31	8.928	79.71	130.1	0.2413
32	7.950	63.20	164.1	0.1913
33	7.080	50.13	206.9	0.1517
34	6.305	39.75	260.9	0.1203
35	5.615	31.53	329.0	0.0954
36	5.000	25.00	414.8	0.0757
37	4.453	19.83	523.1	0.0600
38	3.965	15.72	659.6	0.0476
39	3.531	12.47	831.8	0.0377
40	3.145	9.89	1049	0.0299

## FUSING CURRENTS

Table 17-2 gives the fusing currents in amperes for five commonly used types of wires. The current  $I$  in amperes at which a wire will melt can be calculated from  $I = Kd^{3/2}$ , where  $d$  is the wire diameter in inches and  $K$  is a constant that depends on the metal concerned. A wide variety of factors influence the rate of heat loss and these figures must be considered as approximations.

## CIRCULAR MIL AREA AND SQUARE MIL AREA

The cross-sectional area of a wire can be stated in square mils or circular mils. The cross-sectional area of a square wire given in square mils is equal to the square of any side, while the cross-

Table 17-2. Fusing Currents of Wires

<b>AWG B &amp; S gauge</b>	<b>d in inches</b>	<b>copper <math>K =</math> 10,244</b>	<b>alum- inum <math>K =</math> 7585</b>	<b>german silver <math>K =</math> 5230</b>	<b>iron <math>K =</math> 3148</b>	<b>tin <math>K =</math> 1642</b>
40	0.0031	1.77	1.31	0.90	0.54	0.28
38	0.0039	2.50	1.85	1.27	0.77	0.40
36	0.0050	3.62	2.68	1.85	1.11	0.58
34	0.0063	5.12	3.79	2.61	1.57	0.82
32	0.0079	7.19	5.32	3.67	2.21	1.15
30	0.0100	10.2	7.58	5.23	3.15	1.64
28	0.0126	14.4	10.7	7.39	4.45	2.32
26	0.0159	20.5	15.2	10.5	6.31	3.29
24	0.0201	29.2	21.6	14.9	8.97	4.68
22	0.0253	41.2	30.5	21.0	12.7	6.61
20	0.0319	58.4	43.2	29.8	17.9	9.36
19	0.0359	69.7	51.6	35.5	21.4	11.2
18	0.0403	82.9	61.4	42.3	25.5	13.3
17	0.0452	98.4	72.9	50.2	30.2	15.8
16	0.0508	117	86.8	59.9	36.0	18.8
15	0.0571	140	103	71.4	43.0	22.4
14	0.0641	166	123	84.9	51.1	26.6
13	0.0719	197	146	101	60.7	31.7
12	0.0808	235	174	120	72.3	37.7
11	0.0907	280	207	143	86.0	44.9
10	0.1019	333	247	170	102	53.4
9	0.1144	396	293	202	122	63.5
8	0.1285	472	349	241	145	75.6
7	0.1443	561	416	287	173	90.0
6	0.1620	668	495	341	205	107

sectional area of a circular wire given in circular mils is equal to the square of the diameter.

A circular wire having a diameter of 1 mil will have an area of 1 circular mil. A square wire having a side of 1 mil will have an area of 1 square mil. However, an area of 1 circular mil is somewhat smaller than an area of 1 square mil, as indicated in Fig. 17-1.

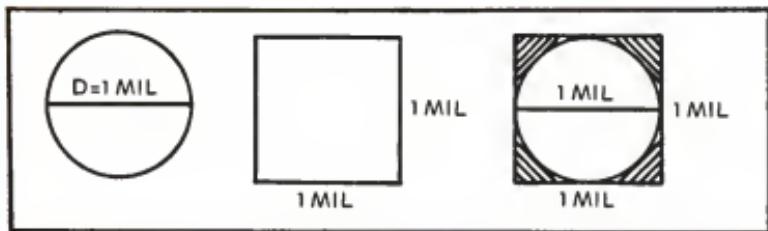


Fig. 17-1. Relationship of circular and square mil area. The shaded area in the lower drawing indicates the large cross-sectional area of the square wire.

$$\text{Square mils} = \text{circular mils} \times 0.7854$$

$$\text{Circular mils} = \text{square mils}/0.7854$$

Tables 17-3 and 17-4 supply conversion data for circular and square wires.

Table 17-3. Circular Mil Area vs. Square Mil Area.

Circular Mils	Square Mils	Cir. Mils	Sq. Mils	Cir. Mils	Sq. Mils
1	0.7854	11	8.6394	21	16.4934
2	1.5708	12	9.4248	22	17.2788
3	2.3562	13	10.2102	23	18.0642
4	3.1416	14	10.9956	24	18.8496
5	3.9270	15	11.7810	25	19.6350
6	4.7124	16	12.5664	26	20.4204
7	5.4978	17	13.3518	27	21.2058
8	6.2832	18	14.1372	28	21.9912
9	7.0686	19	14.9226	29	22.7766
10	7.8540	20	15.7080	30	23.5620
31	24.3474	56	43.9824	76	59.6904
32	25.1328	57	44.7678	77	60.4758
33	25.9182	58	45.5532	78	61.2612
34	26.7036	59	46.3386	79	62.0466
35	27.4890	60	47.1240	80	62.8320
36	28.2744	61	47.9094	81	63.6174
37	29.0598	62	48.6948	82	64.4028
38	29.8452	63	49.4802	83	65.1882
39	30.6306	64	50.2656	84	65.9736
40	31.4160	65	51.0510	85	66.7590

Table 17-3. Circular Mil Area vs Square Mil Area (cont'd)

Cir. Mils	Sq. Mils	Cir. Mils	Sq. Mils	Cir. Mils	Sq. Mils
41	32.2014	66	51.8364	86	67.5444
42	32.9868	67	52.6218	87	68.3298
43	33.7722	68	53.4072	88	69.1152
44	34.5576	69	54.1926	89	69.9006
45	35.3430	70	54.9780	90	70.6860
46	36.1284	71	55.7634	91	71.4714
47	36.9138	72	56.5488	92	72.2568
48	37.6992	73	57.3342	93	73.0422
49	38.4846	74	58.1196	94	73.8276
50	39.2700	75	58.9050	95	74.6130
51	40.0554			96	75.3984
52	40.8408			97	76.1838
53	41.6262			98	76.9692
54	42.4116			99	77.7546
55	43.1970			100	78.5400

Table 17-4. Square Mil Area vs. Circular Mil Area.

Square Mils	Circular Mils	Sq. Mils	Cir. Mils	Sq. Mils	Cir. Mils
1	1.273	6	7.638	11	14.003
2	2.546	7	8.911	12	15.276
3	3.819	8	10.184	13	16.549
4	5.092	9	11.457	14	17.822
5	6.366	10	12.730	15	19.095
16	20.368	46	58.558	76	96.748
17	21.641	47	59.831	77	98.021
18	22.914	48	61.104	78	99.294
19	24.187	49	62.377	79	100.567
20	25.460	50	63.650	80	101.840
21	26.733	51	64.923	81	103.113
22	28.006	52	66.196	82	104.386
23	29.279	53	67.469	83	105.659
24	30.552	54	68.472	84	106.932
25	31.825	55	70.015	85	108.205

Table 17-4. Square Mil Area vs Circular Mil Area (cont'd)

Sq. Mils	Cir. Mils	Sq. Mils	Cir. Mils	Sq. Mils	Cir. Mils
26	33.098	56	71.288	86	109.478
27	34.371	57	72.561	87	110.751
28	35.644	58	73.834	88	112.024
29	36.917	59	75.107	89	113.297
30	38.190	60	76.380	90	114.570
31	39.463	61	77.653	91	115.843
32	40.736	62	78.926	92	117.116
33	42.009	63	80.199	93	118.389
34	43.282	64	81.472	94	119.662
35	44.555	65	82.745	95	120.935
36	45.828	66	84.018	96	122.208
37	47.101	67	85.291	97	123.481
38	48.374	68	86.564	98	124.754
39	49.647	69	87.837	99	126.027
40	50.920	70	89.110	100	127.300
41	52.193	71	90.383		
42	53.466	72	91.656		
43	54.739	73	92.929		
44	56.012	74	94.202		
45	57.285	75	95.475		

## Chapter 18

### Color Codes

---

Resistors may be identified by using the color code recommended by the Electronics Industries Association (EIA). Each color indicates a number. See Table 18-1.

Table 18-1. The Basic Color Code

Black	0	Green	5
Brown	1	Blue	6
Red	2	Violet	7
Orange	3	Gray	8
Yellow	4	White	9

These colors are used to indicate the values of resistors and they are also used to represent tolerance. Thus, brown is a tolerance of plus or minus 1 percent, red is plus or minus 2 percent, orange is plus or minus 3 percent and yellow is plus or minus 4 percent. However, gold is used for plus or minus 5 percent and silver for plus or minus 10 percent. Absence of color means plus or minus 20 percent.

#### RESISTORS

The value of a resistor in ohms is coded by rings of color placed at one end. The first color is the first significant figure or digit of the resistance value. The second color is the second significant figure or digit of the resistance value. The third color, known as the decimal

multiplier, represents the number of zeros which follow the first two digits. Resistors having a tolerance of plus or minus 20 percent have only three bands of color. A fourth color, if used, is the tolerance. This fourth color is either silver or gold. Table 18-2 lists the resistor color code.

**□Example:**

What is the value of a resistor that is color coded yellow, violet and orange?

The first color, yellow, is 4. The second color, violet, is 7. The final color, orange, is 3 and represents three zeros. The resistance is 47,000 ohms.

Table 18-2. Color Code for Resistors

Color	First	Second	Multiplier	Tolerance ( $\pm$ )
	Digit	Digit		
Black	—	0	1	—
Brown	1	1	10	1%
Red	2	2	100	2%
Orange	3	3	1,000	3%
Yellow	4	4	10,000	4%
Green	5	5	100,000	
Blue	6	6	1,000,000	
Violet	7	7	10,000,000	
Gray	8	8	100,000,000	
White	9	9	1,000,000,000	
Silver				10%
Gold				5%
No color				20%

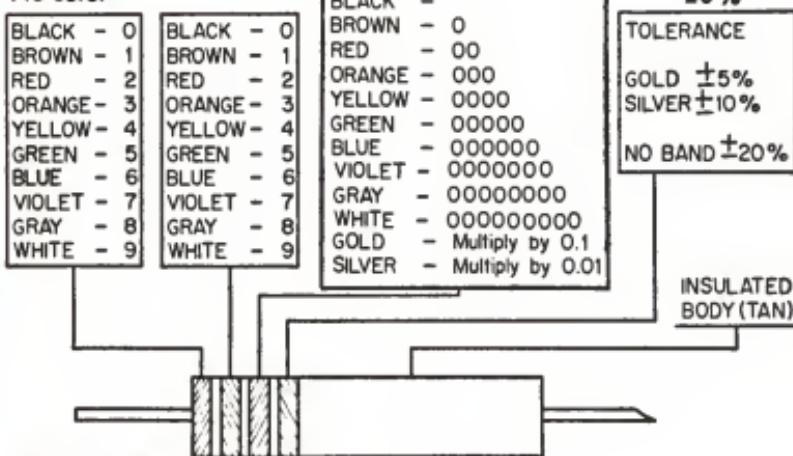


Fig. 18-1. Resistor markings.

## DIODES

Crystal diodes might be marked according to the EIA color code given in Table 18-1. The color bands start from the cathode

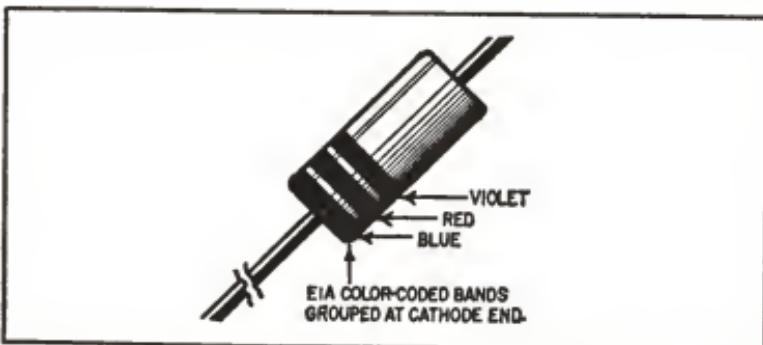


Fig. 18-2. Crystal diodes are marked according to the same basic color code used for resistors.

Table 18-3. Color Code for Power Transformers

Primary	Secondary		
	Rectifier	Filament Windings	Color
Primary (no taps)	—	—	Black
Primary (tapped);			
Camman	—	—	Black
Tap No. 1	—	—	Black-yellow
Tap No. 2	—	—	Black-orange
Finish	—	—	Black-red
—	Plate center tap	—	Red Red-yellow
—	Filament center tap	—	Yellow Yellow-blue
—		Filament No. 1 Center tap	Green Green-yellow
—		Filament No. 2 Center tap	Brown Brown-yellow
—		Filament No. 3 Center tap	Slate Slate-yellow

end and represent the digits following the 1N prefix. For example, the diode in the drawing is a 1N627. (Other manufacturers use other number and letter combinations in place of 1N.)

## ELECTROLYTIC CAPACITORS

Electrolytic capacitors are marked showing the rated capacitance in microfarads, the rated DC working voltage, and terminal identification. The data are generally printed or stamped directly on the case of the capacitor.

## POWER TRANSFORMERS

Table 18-3 supplies the color code for power transformers. A bare wire (if used) represents the connection to the Faraday shield (electrostatic screen) between the primary and secondary windings. This wire should be grounded.

## **Chapter 19**

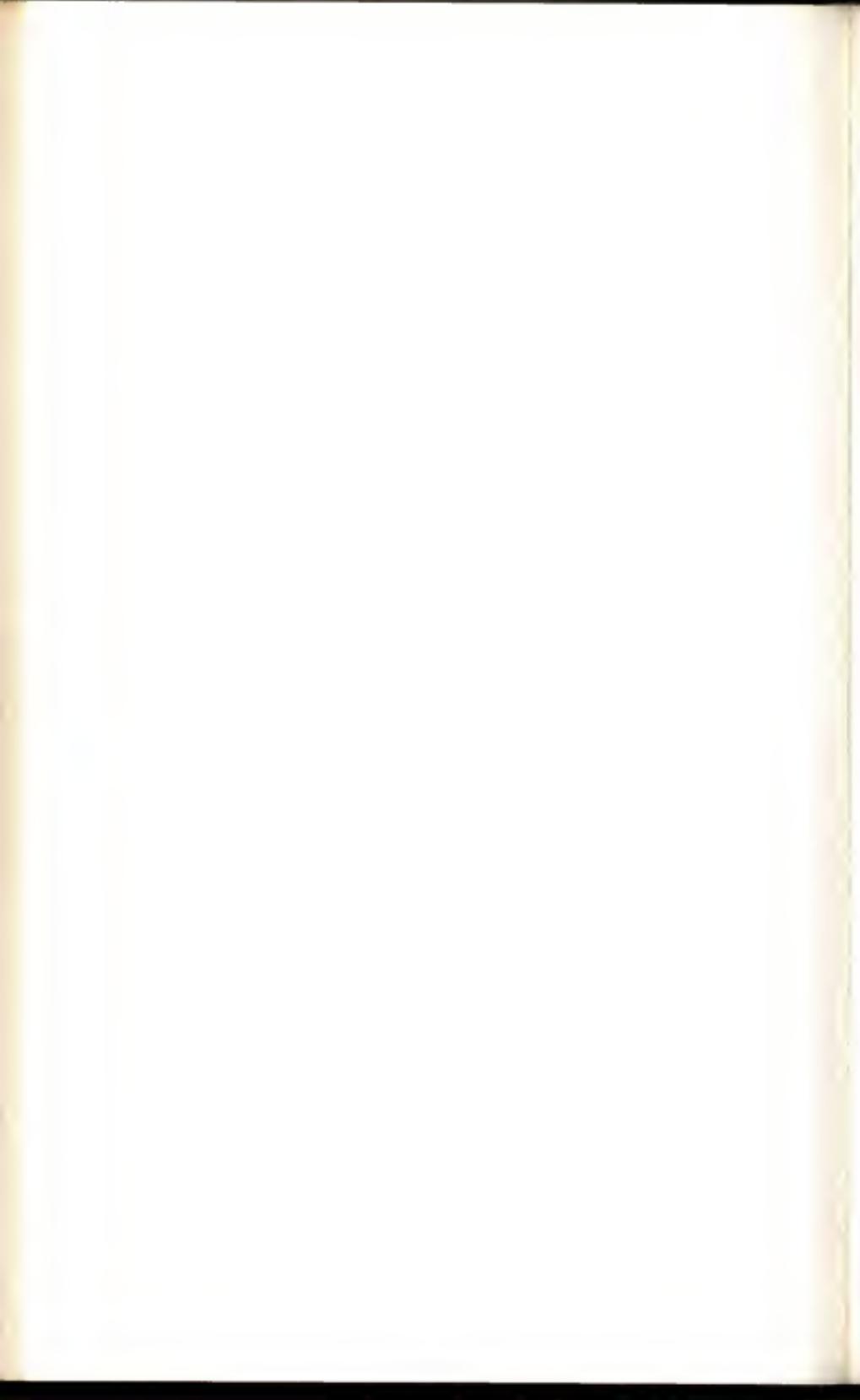
# **Heat and Energy**

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Table 19-1 shows the relationship between heat and its equivalent in work or energy.

**Table 19-1. Heat vs Energy**

<b>Amount of heat</b>	<b>Equivalent amount of work or energy</b>
1 calorie	4.186 joules
1 B.t.u.	778 foot-pounds
0.239 calorie	1 joule



## Chapter 20

# Thermocouples

### THERMOCOUPLES

A thermocouple consists of two dissimilar metals with one at a higher temperature than the other. A voltage is produced under these circumstances, with the amount of current generated proportional to the temperature difference. Table 20-1 shows voltages produced by thermocouple materials with the cold junction kept at 0°C. In Table 20-1 the column at the extreme left shows one element of the thermocouple; the other element is either platinum-rhodium or copper-constantan.

Table 20-1. Potentials of Thermocouples

Substance	Point	Degrees	Degrees	EMF in millivolts	
		Celsius	Fahrenheit	Platinum-rhodium couple	Copper-constantan couple
Tin	melting	231.9	449.0	1.706	11.009
Cadmium	melting	320.9	609.6	2.503	16.083
Zinc	melting	419.4	786.9	3.430	
Sulphur	boiling	444.5	920.1	3.672	
Aluminum	melting	658.7	1217.6	5.827	
Silver	melting	960.2	1760.3	9.111	
Copper	melting	1082.8	1981.0	10.534	
Nickel	melting	1452.6	2646.6	14.973	
Platinum	melting	1755	3191	18.608	



# Chapter 21

## Chemical Properties

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Table 21-1. Metallic Elements.

Number of Symbol	Color	Atomic Weight	Specific Gravity or Density	Specific Heat	Melting-point (°Celsius)	Coefficient of Linear Expansion
Aluminum.....	Tin-white	27.1	2.67	0.2140	657	0.0000231
Antimony.....	Bluish-white	120.2	6.71-6.86	0.0508	630	0.0000105
Arsenic.....	Steel-grey	75.0	5.72	0.081	450	0.0000055
Banum.....	Pinkish-grey	137.4	3.8	0.068	850	—
Beryllium.....	Gl	Silver-white	9.1	1.9	0.5820	—
Bismuth.....	Bi	Pinkish-white	208.0	9.823	0.0305	268
Bromine.....	Br	—	79.6	—	—	—
Cadmium.....	Cd	Tin-white	112.4	8.546-8.667	0.0548	322
Caesium.....	Cs	Silver-white	132.8	1.9	0.048	27
Calcium.....	Ca	Yellow	40.1	1.578	0.1700	800
Cerium.....	Ce	Grey	140.2	7.64	0.0448	623
Chromium.....	Cr	Grey	52.0	6.81-7.3	0.1200	—
Cobalt.....	Co	Greyish-white	59.0	8.5-8.7	0.1070	1,700
Columbium.....	Cb	(see Niobium)				0.0000123
Copper.....	Cu	Red	63.6	8.92-8.95	0.0952	1,100
Erbium.....	E	—	166.0	—	—	0.0000167
Gadolinium.....	Gd	—	156.0	—	—	—
Gallium.....	Ga	Bluish-white	69.9	5.9	0.079	30
Germanium.....	Ge	Bluish-white	72.5	5.5	0.074	900
Gold.....	Au	Yellow	197.2	19.265	0.0324	1,065
Indium.....	In	White	114.8	7.42	0.0570	176
Indium.....	Ir	Steel-white	193.1	22.38	0.0326	2,250
Iron.....	Fe	Silver-white	55.9	7.84	0.1140	1,550
Lanthanum.....	La	Grey	139.0	6.163	0.0449	826
Lead.....	Pb	Bluish-white	207.1	11.254-11.38	0.0314	328
Lithium.....	Li	Silver-white	7.02	0.589-0.598	0.9410	180
Magnesium.....	Mg	silver-white	24.3	1.75	0.2500	632
Manganese.....	Mn	Reddish-grey	55.0	8.0	0.1220	1,245
Mercury.....	Hg	Bluish-white	200.0	13.594	0.0319	-40
Molybdenum.....	Mo	Silver-white	96.0	8.6	0.0722	2,450
Neodymium.....	Nd	—	143.6	7.0	—	840
Nickel.....	Ni	—	58.7	8.9	0.1080	1,450

Table 21-1. Metallic Elements.

Number of Symbol	Color	Atomic Weight	Specific Gravity or Density	Specific Heat	Melting-point (°Celsius)	Coefficient of Linear Expansion
Niobium.....	Nb	Steel-grey	93.5	12.1	0.071	1,950
Osmium.....	Os	Bluish-white	190.9	22.5	0.0311	2,500 0.0000065
Palladium.....	Pd	Tin-white	106.7	11.4	0.0593	1,549 0.0000117
Platinum.....	Pt	—	195.2	21.5	0.0324	1,780 0.0000089
Potassium.....	K	Silver-white	39.10	0.875	0.1660	60 0.0000841
Praseodymium.....	Pr	—	140.5	8.5	—	940 —
Radium.....	Ra	—	225.0	—	—	—
Rhodium.....	Rh	Tin-white	102.9	12.1	0.0580	2,000 0.0000085
Rubidium.....	Rb	Silver-white	85.5	1.52	0.077	38.5 —
Ruthenium.....	Ru	—	101.7	12.261	0.0611	2,400 0.0000096
Samarium.....	Sm	—	150.3	7.7	—	1,350 —
Scandium.....	Sc	—	44.1	—	—	—
Silver.....	Ag	White	107.9	10.4-10.57	0.0560	962 0.0000192
Sodium.....	Na	Silver-white	23.0	0.98	0.293	96 0.000071
Strontium.....	Sr	Yellow	87.8	2.5	—	800 —
Tantalum.....	Ta	Black	181.6	16.8	0.0385	2,910 0.0000079
Tellurium.....	Te	—	127.5	8.25	0.049	452 0.0000167
Terbium.....	Tb	—	160	—	—	—
Thallium.....	Tl	Bluish-white	204.0	11.8	0.0335	303 0.0000302
Thorium.....	Th	Grey	232.4	11.2	0.0278	1,690 —
Thulium.....	Tm	—	171	—	—	—
Tin.....	Sn	White	119.0	7.293	0.0559	232 0.0000203
Titanium.....	Ti	Dark grey	48.1	3.8	0.13	1,800 —
Tungsten.....	W	Light grey	184.0	19.129	0.0334	3,000 —
Uranium.....	U	Greyish-white	238.5	18.33	0.0277	1,500 —
Vanadium.....	V	Whitish-grey	51.1	5.9	0.125	1,680 —
Ytterbium.....	Yb	—	173.0	—	—	—
Yttrium.....	Yt	Grey	89.0	3.80	—	—
Zinc.....	Zn	Bluish-white	65.4	7.1	0.0935	419 0.0000274
Zirconium.....	Zr	Grey	90.8	4.15	0.0662	1,300 —

Table 21-2. Densities of solids and liquids in cubic centimeters and cubic feet.

Aluminum.....	2.58 g. per cub. cm.	1.61.1 lb. per cub. ft.
Copper.....	8.9 g. per cub. cm.	555.4 lb. per cub. ft.
Gold.....	19.3 g. per cub. cm.	1,205.0 lb. per cub. ft.
Ice.....	0.9167 g. per cub. cm.	57.2 lb. per cub. ft.
Iron.....	7.87 g. per cub. cm.	491.3 lb. per cub. ft.
Lead.....	11.0 g. per cub. cm.	686.7 lb. per cub. ft.
Mercury.....	13.596 g. per cub. cm.	848.7 lb. per cub. ft.
Nickel.....	8.80 g. per cub. cm.	549.4 lb. per cub. ft.
Platinum.....	21.50 g. per cub. cm.	1,342.2 lb. per cub. ft.
Sea Water.....	1.025 g. per cub. cm.	64.0 lb. per cub. ft.
Silver.....	10.5 g. per cub. cm.	655.5 lb. per cub. ft.
Tin.....	7.18 g. per cub. cm.	448. lb. per cub. ft.
Tungsten.....	18.6 g. per cub. cm.	1,161.2 lb. per cub. ft.
Uranium.....	18.7 g. per cub. cm.	1,167.4 lb. per cub. ft.
Water.....	1.000 g. per cub. cm.	62.4 lb. per cub. ft.
Zinc.....	7.19 g. per cub. cm.	448.6 lb. per cub. ft.

Table 21-3.

## CRYSTAL DATA

## Crystals and their Symbols

Bornite	$3\text{Cu}_2\text{S}_3\text{Fe}_2\text{S}_3$
Carborundum	SiC
Cassiterite (tinstone)	$\text{SnO}_2$
Copper pyrites	$\text{Cu}_2\text{S}_2\text{FeS}_2$
Galena	PbS
Graphite	C
Hertzite	PbS
Iron Pyrites	$\text{FeS}_2$
Malachite	$\text{CuCo}_2\text{CuH}_2\text{O}$
Molybdenite	$\text{MoS}_2$
Silicon	Si
Tellurium	Te
Zincite	$\text{ZnO}$

## Crystal Combinations

Carborundum with Steel

Iron Pyrites with Silicon

Galena with Tellurium

Tellurium with Zincite

Carborundum with Silicon

Copper Pyrites with

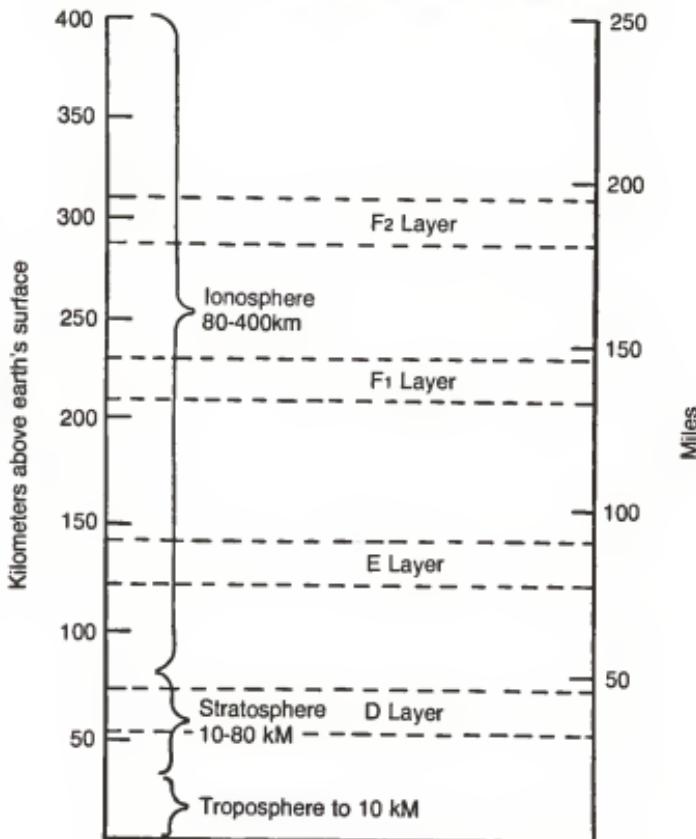
Tellurium



## Chapter 22

# Atmospheric Layers

Table 22-1. Troposphere, Stratosphere and Ionosphere





## Chapter 23

# Lissajous Patterns

### LISSAJOUS PATTERNS

An oscilloscope can provide Lissajous figures for calibrating an unknown against a known frequency. Figure 23-1 shows patterns indicating the frequency ratio of horizontal to vertical input sine waves. Count the number of loops across the top and down the side.

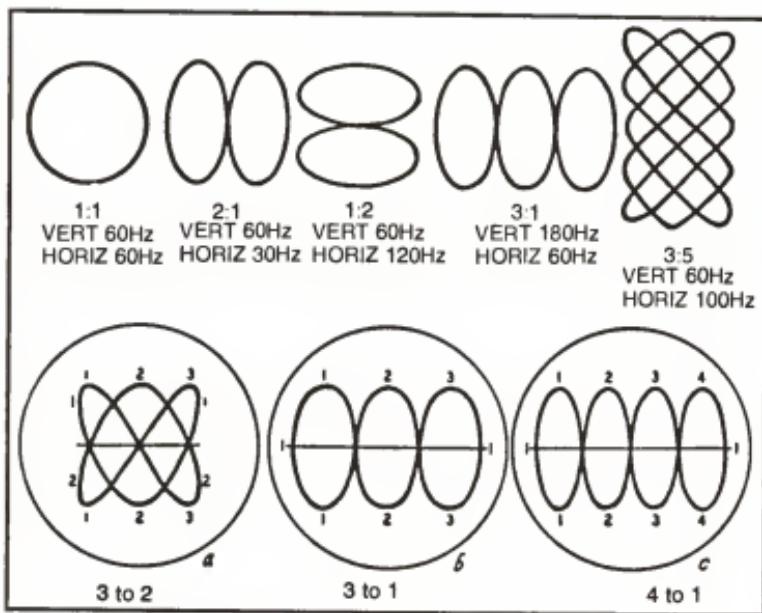


Fig. 23-1. Lissajous figures



## Chapter 24

# Citizens Band and Amateur Radio

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**Table 24-1. TV Channels and Amateur and Citizens Band Harmonics**

Channel	Freq. Range	Picture Carrier Freq.	Harmonics				
			CB	40 meters	20 meters	15 meters	10 meters
TV I-F	41-47	42	—	—	42-43	42-43	—
2	54-60	65.25	63.9-54.8 (2nd)	66-58.4 (8th)	56-57.3 (4th)	—	56-58.4 (2nd)
3	60-66	61.25	—	63-65.7 (9th)	—	63-64.35 (3rd)	—
4	66-72	67.25	—	70-73 (10th)	70-72 (5th)	—	—
5	76-82	77.25	60.9-62.2 (3rd)	—	—	—	—
6	82-88	63.25	62-62.2 (3rd)	—	84-85.4 (8th)	84-85.8 (4th)	84-85.1 (3rd)

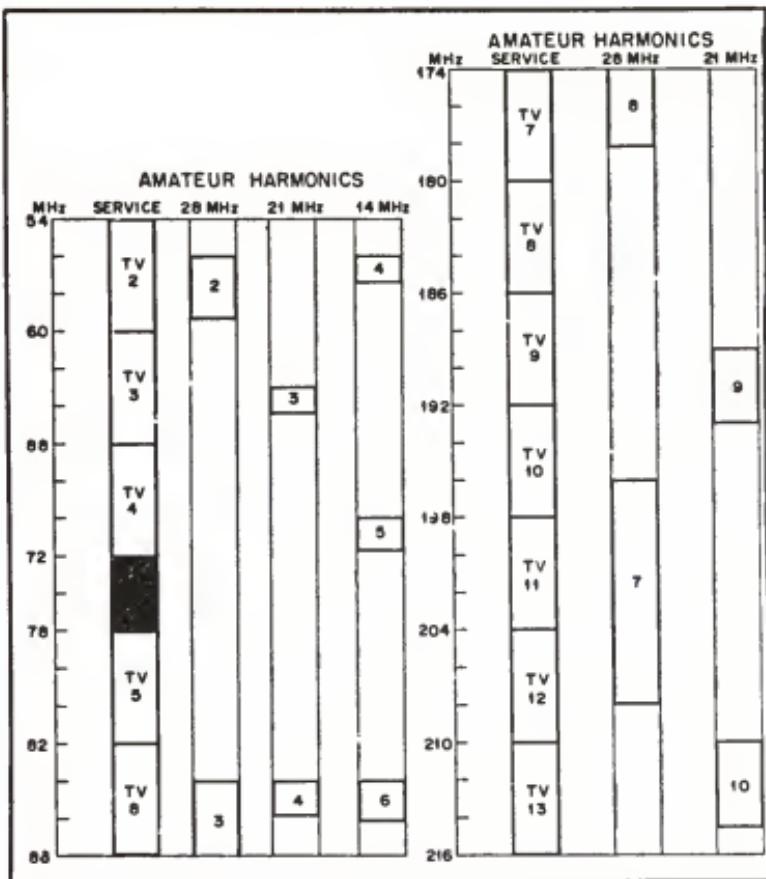


Fig. 24-1. The relationship of amateur-band harmonics to the vhf TV channels. (courtesy of American Radio Relay League Inc.).

Table 24-2. Harmonic Relationship—Amateur VHF Bands and UHF TV Channels

Amateur Band	Harmonic Freq.	Fundamental Channel			Amateur Band	Harmonic Freq.	Fundamental Channel		
		Range	Affected	Channel			Range	Affected	Channel
144 MHz	4th	144.0-144.5	31	220 MHz	3rd	220.00-220.67	45		
		144.5-146.0	32			220.67-222.87	46		
		146.0-147.5	33			222.67-224.67	47		
		147.5-148.0	34			224.67-225.00	48		
5th		144.0-144.4	55		4th	220-221	82		
		144.4-145.6	56			221.0-222.5	83		
		145.6-146.8	57						
		146.6-148.0	58	420 MHz		420-421	75		
6th		144.00-144.33	79			421-424	78		
		144.33-145.33	80			424-427	77		
		145.33-147.33	81			427-430	78		
		147.33-148.00	82			430-433	79		
						433-436	80		

## Chapter 25

# Vectors

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### VECTOR CONVERSION

Table 25-1 can be used to change the form of vector quantities from j-notation to polar notation, or from polar to j-notation. The first column is the ratio of reactance, X, to resistance, R. The second column is the phase angle of the polar vector and is the angle whose tangent is  $X/R$ . The third column, Z, is the absolute magnitude of the vector in terms of X.

#### □Example:

The impedance of a circuit, expressed in polar form, is  $Z$  equals  $3000-j4000$ . What is the absolute magnitude of the impedance and the phase angle?

3000 represents the resistance R; 4000 is the reactance X. The ratio  $X/R$  is  $4000/3000$  equals 1.3333. The closest value of  $X/R$  in Table 25-1 is 1.3319. Immediately to the right is the phase angle of 53.1 degrees. However, because the reactance is negative and is given as  $-j4000$ , the phase angle is also negative and is -53.1 degrees. The value for Z in the column directly to the right of the phase angle is 1.2505X. Since X is 4000, Z equals  $1.2505 \times 4000$ , 5002 ohms. The answer, then, is that Z is 5002 ohms and the phase angle is -53.1 degrees.

#### □Example:

Take the example just given and work it backward. Suppose we are told that the circuit impedance is 5000 ohms (5002 rounded

Table 25-1. Vector Conversion

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.00000	0.0	Z = R	0.06116	3.5	16.380 X
.00175	.1	572.96 X	.06291	3.6	15.926 X
.00349	.2	286.48 X	.06467	3.7	15.496 X
.00524	.3	190.98 X	.06642	3.8	15.089 X
.00698	.4	143.24 X	.06817	3.9	14.702 X
0.00873	0.5	114.59 X	0.06993	4.0	14.335 X
0.01047	0.6	95.495 X	0.07168	4.1	13.986 X
.01222	0.7	81.853 X	.07344	4.2	13.654 X
.01396	0.8	71.622 X	.07519	4.3	13.337 X
.01571	0.9	63.664 X	.07694	4.4	13.034 X
.01746	1.0	57.299 X	0.07870	4.5	12.745 X
0.01920	1.1	52.090 X			
0.02095	1.2	47.750 X	0.08046	4.6	12.469 X
.02269	1.3	44.077 X	.08221	4.7	12.204 X
.02444	1.4	40.930 X	.08397	4.8	11.950 X
.02618	1.5	38.201 X	.08573	4.9	11.707 X
.02793	1.6	35.814 X	.08749	5.0	11.474 X
0.02968	1.7	33.708 X	0.08925	5.1	11.249 X
0.03143	1.8	31.836 X	0.09101	5.2	11.033 X
.03317	1.9	30.161 X	.09277	5.3	10.826 X
.03492	2.0	28.654 X	.09453	5.4	10.626 X
.03667	2.1	27.290 X	.09629	5.5	10.433 X
0.03842	2.2	26.050 X	.09805	5.6	10.248 X
0.04016	2.3	24.918 X	0.09981	5.7	10.068 X
.04191	2.4	23.880 X	0.10158	5.8	9.8955 X
.04366	2.5	22.925 X	.10344	5.9	9.7283 X
.04541	2.6	22.044 X	.10510	6.0	9.5668 X
.04716	2.7	21.228 X	.10687	6.1	9.4105 X
0.04891	2.8	20.471 X	0.10863	6.2	9.2593 X
0.05066	2.9	19.766 X	0.11040	6.3	9.1129 X
.05241	3.0	19.107 X	.11217	6.4	8.9711 X
.05416	3.1	18.491 X	.11394	6.5	8.8337 X
.05591	3.2	17.914 X	.11570	6.6	8.7004 X
.05766	3.3	17.372 X	.11747	6.7	8.5711 X
0.05941	3.4	16.861 X	0.11924	6.8	8.4457 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.12107	6.9	8.3238 X	0.18173	10.3	5.5928 X
.12278	7.0	8.2055 X	.18353	10.4	5.5396 X
.12456	7.1	8.0905 X	.18534	10.5	5.4874 X
.12663	7.2	7.9787 X	.18714	10.6	5.4362 X
.12810	7.3	7.8700 X	0.18895	10.7	5.3860 X
0.12988	7.4	7.7642 X	0.19076	10.8	5.3367 X
0.13165	7.5	7.6613 X	.19257	10.9	5.2883 X
.13343	7.6	7.5611 X	.19438	11.0	5.2408 X
.13521	7.7	7.4634 X	.19619	11.1	5.1942 X
.13698	7.8	7.3683 X	.19800	11.2	5.1484 X
0.13876	7.9	7.2756 X	0.19982	11.3	5.1034 X
0.14054	8.0	7.1853 X	0.20163	11.4	5.0593 X
.14232	8.1	7.0972 X	.20345	11.5	5.0158 X
.14410	8.2	7.0112 X	.20527	11.6	5.9732 X
.14588	8.3	6.9273 X	.20709	11.7	5.9313 X
.14767	8.4	6.8454 X	0.20891	11.8	5.8901 X
0.14945	8.5	6.7755 X			
0.15124	8.6	6.6874 X	0.21073	11.9	5.8496 X
.15302	8.7	6.6111 X	.21256	12.0	4.8097 X
.15481	8.8	6.5365 X	.21438	12.1	4.7706 X
.15660	8.9	6.4637 X	.21621	12.2	4.7320 X
0.15838	9.0	6.3924 X	.21803	12.3	4.6942 X
0.16017	9.1	6.3228 X	0.21986	12.4	4.6569 X
.16196	9.2	6.2546 X	0.22169	12.5	4.6201 X
.16376	9.3	6.1880 X	.22353	12.6	4.5841 X
.16555	9.4	6.1227 X	.22536	12.7	4.5486 X
.16734	9.5	6.0588 X	.22719	12.8	4.5137 X
0.16914	9.6	5.9963 X	0.22903	12.9	4.4793 X
0.17093	9.7	5.9351 X	0.23087	13.0	4.4454 X
.17273	9.8	5.8751 X	.23270	13.1	4.4121 X
.17453	9.9	5.8163 X	.23455	13.2	4.3792 X
.17633	10.0	5.7588 X	.23693	13.3	4.3469 X
.17813	10.1	5.7023 X	0.23823	13.4	4.3150 X
0.17993	10.2	5.6470 X			

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.24008	13.5	4.2836 X	0.30001	16.7	3.4799 X
.24192	13.6	4.2527 X	.30192	16.8	3.4598 X
.24377	13.7	4.2223 X	.30382	16.9	3.4399 X
.24562	13.8	4.1923 X	.30573	17.0	3.4203 X
.24747	13.9	4.1627 X	.30764	17.1	3.4009 X
0.24933	14.0	4.1336 X	0.30995	17.2	3.3817 X
0.25118	14.1	4.1048 X	0.31146	17.3	3.3627 X
.25304	14.2	4.0765 X	.31338	17.4	3.3440 X
.25490	14.3	4.0486 X	.31530	17.5	3.3255 X
.25676	14.4	4.0211 X	.31722	17.6	3.3072 X
0.25862	14.5	3.9939 X	0.31914	17.7	3.2891 X
0.26048	14.6	3.9672 X	0.32106	17.8	3.2712 X
.26234	14.7	3.9408 X	.32299	17.9	3.2535 X
.26421	14.8	3.9147 X	.32492	18.0	3.2361 X
.26608	14.9	3.8890 X	.32685	18.1	3.2188 X
.26795	15.0	3.8637 X	0.32878	18.2	3.2017 X
0.26982	15.1	3.8387 X			
0.27169	15.2	3.8140 X	0.33072	18.3	3.1848 X
.27357	15.3	3.7897 X	.33265	18.4	3.1681 X
.27554	15.4	3.7657 X	.33459	18.5	3.1515 X
.27732	15.5	3.7420 X	.33654	18.6	3.1352 X
0.27920	15.6	3.7186 X	0.33848	18.7	3.1190 X
0.28109	15.7	3.6955 X	0.34043	18.8	3.1030 X
.28297	15.8	3.6727 X	.34238	18.9	3.0872 X
.28486	15.9	3.6502 X	.34433	19.0	3.0715 X
.28674	16.0	3.6279 X	.34628	19.1	3.0561 X
0.28863	16.1	3.6060 X	0.34824	19.2	3.0407 X
0.29053	16.2	3.5843 X	0.35019	19.3	3.0256 X
.29242	16.3	3.5629 X	.35215	19.4	3.0106 X
.29432	16.4	3.5418 X	.35412	19.5	2.9957 X
.29621	16.5	3.5209 X	.35608	19.6	2.9810 X
0.29811	16.6	3.5003 X	0.35805	19.7	2.9665 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.36002	19.8	2.9521 X	0.42036	22.8	2.5805 X
.36199	19.9	2.9379 X	.42242	22.9	2.5699 X
.36397	20.0	2.9238 X	.42447	23.0	2.5593 X
.36595	20.1	2.9098 X	.42654	23.1	2.5488 X
.36793	20.2	2.8960 X	0.42860	23.2	2.5384 X
0.36991	20.3	2.8824 X			
0.37190	20.4	2.8688 X	0.43067	23.3	2.5281 X
.37388	20.5	2.8554 X	.43274	23.4	2.5179 X
.37587	20.6	2.8422 X	.43481	23.5	2.5078 X
.37787	20.7	2.8290 X	.43689	23.6	2.4978 X
0.37986	20.8	2.8160 X	0.43897	23.7	2.4879 X
0.38186	20.9	2.8032 X	0.44105	23.8	2.4780 X
.38386	21.0	2.7904 X	.44314	23.9	2.4683 X
.38587	21.1	2.7778 X	.44523	24.0	2.4586 X
.38787	21.2	2.7653 X	.44732	24.1	2.4490 X
0.38988	21.3	2.7529 X	0.44942	24.2	2.4395 X
0.39189	21.4	2.7406 X	0.45152	24.3	2.4300 X
.39391	21.5	2.7285 X	.45362	24.4	2.4207 X
.39593	21.6	2.7165 X	.45573	24.5	2.4114 X
.39795	21.7	2.7045 X	.45783	24.6	2.4022 X
0.39997	21.8	2.6927 X	0.45995	24.7	2.3931 X
0.40200	21.9	2.6810 X	0.46206	24.8	2.3841 X
.40403	22.0	2.6695 X	.46418	24.9	2.3751 X
.40606	22.1	2.6580 X	.46631	25.0	2.3662 X
0.40809	22.2	2.6466 X	0.46843	25.1	2.3574 X
0.41013	22.3	2.6353 X	0.47056	25.2	2.3486 X
.41217	22.4	2.6242 X	.47270	25.3	2.3399 X
.41421	22.5	2.6131 X	.47483	25.4	2.3313 X
.41626	22.6	2.6022 X	.47697	25.5	2.3228 X
0.41831	22.7	2.5913 X	0.47912	25.6	2.3143 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.48127	25.7	2.3059 X	0.55203	28.9	2.0692 X
.48342	25.8	2.2976 X	.55431	29.0	2.0627 X
.48557	25.9	2.2894 X	.55659	29.1	2.0562 X
.48773	26.0	2.2812 X	0.55888	29.2	2.0498 X
0.48989	26.1	2.2730 X			
0.49206	26.2	2.2650 X	0.56117	29.3	2.0434 X
.49423	26.3	2.2570 X	.56347	29.4	2.0370 X
.49640	26.4	2.2490 X	.56577	29.5	2.0308 X
0.49858	26.5	2.2411 X	0.56808	29.6	2.0245 X
0.50076	26.6	2.2333 X	0.57039	29.7	2.0183 X
.50295	26.7	2.2256 X	.57270	29.8	2.0122 X
.50514	26.8	2.2179 X	.57502	29.9	2.0061 X
.50733	26.9	2.2103 X	.57735	30.0	2.0000 X
0.50952	27.0	2.2027 X	0.57968	30.1	1.9940 X
0.51172	27.1	2.1952 X	0.58201	30.2	1.9880 X
.51393	27.2	2.1877 X	.58435	30.3	1.9820 X
.51614	27.3	2.1803 X	.58670	30.4	1.9761 X
0.51835	27.4	2.1730 X	0.58904	30.5	1.9703 X
0.52057	27.5	2.1657 X	0.59140	30.6	1.9645 X
.52279	27.6	2.1584 X	.59376	30.7	1.9587 X
.52501	27.7	2.1513 X	.59612	30.8	1.9530 X
.52724	27.8	2.1441 X	0.59849	30.9	1.9473 X
0.52947	27.9	2.1371 X			
0.53171	28.0	2.1300 X	0.60086	31.0	1.9416 X
.53395	28.1	2.1231 X	.60324	31.1	1.9360 X
.53619	28.2	2.1162 X	.60562	31.2	1.9304 X
0.53844	28.3	2.1093 X	0.60801	31.3	1.9248 X
0.54070	28.4	2.1025 X	0.61040	31.4	1.9193 X
.54295	28.5	2.0957 X	.61280	31.5	1.9139 X
.54522	28.6	2.0890 X	.61520	31.6	1.9084 X
.54748	28.7	2.0824 X	0.61761	31.7	1.9030 X
0.54975	28.8	2.0757 X			

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.62003	31.8	1.8977 X	0.69243	34.7	1.7566 X
.62244	31.9	1.8924 X	.69502	34.8	1.7522 X
.62487	32.0	1.8871 X	0.69761	34.9	1.7478 X
.62730	32.1	1.8818 X			
0.62973	32.2	1.8766 X			
0.63217	32.3	1.8714 X	0.70021	35.0	1.7434 X
.63462	32.4	1.8663 X	.70281	35.1	1.7391 X
.63707	32.5	1.8611 X	.70542	35.2	1.7348 X
0.63953	32.6	1.8561 X	0.70804	35.3	1.7305 X
0.64199	32.7	1.8510 X	0.71066	35.4	1.7263 X
.64466	32.8	1.8460 X	.71329	35.5	1.7220 X
.64693	32.9	1.8410 X	.71593	35.6	1.7178 X
0.64941	33.0	1.8361 X	0.71857	35.7	1.7137 X
0.65189	33.1	1.8311 X	0.72122	35.8	1.7095 X
.65438	33.2	1.8263 X	.72388	35.9	1.7054 X
.65688	33.3	1.8214 X	.72654	36.0	1.7013 X
0.65938	33.4	1.8166 X	0.72921	36.1	1.6972 X
0.66188	33.5	1.8118 X	0.73189	36.2	1.6932 X
.66440	33.6	1.8070 X	.73457	36.3	1.6891 X
.66692	33.7	1.8023 X	.73726	36.4	1.6851 X
0.66944	33.8	1.7976 X	0.73996	36.5	1.6812 X
0.67197	33.9	1.7929 X	0.74266	36.6	1.6772 X
.67451	34.0	1.7883 X	.74538	36.7	1.6733 X
.67705	34.1	1.7837 X	0.74809	36.8	1.6694 X
0.67160	34.2	1.7791 X			
0.68215	34.3	1.7745 X	0.75082	36.9	1.6655 X
.68471	34.4	1.7700 X	.75355	37.0	1.6616 X
.68728	34.5	1.7655 X	.75629	37.1	1.6578 X
0.68985	34.6	1.7610 X	0.75904	37.2	1.6540 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.76179	37.3	1.6502 X	0.85107	40.4	1.5429 X
.76546	37.4	1.6464 X	.85408	40.5	1.5398 X
0.76733	37.5	1.6427 X	0.85710	40.6	1.5366 X
0.77010	37.6	1.6389 X	0.86013	40.7	1.5335 X
.77289	37.7	1.6352 X	.86318	40.8	1.5304 X
.77568	37.8	1.6316 X	.86623	40.9	1.5273 X
0.77848	37.9	1.6279 X	0.86929	41.0	1.5242 X
0.78128	38.0	1.6243 X	0.87235	41.1	1.5212 X
.78410	38.1	1.6206 X	.87543	41.2	1.5182 X
.78692	38.2	1.6170 X	0.87852	41.3	1.5151 X
0.78975	38.3	1.6135 X			
0.79259	38.4	1.6099 X	0.88162	41.4	1.5121 X
.79543	38.5	1.6064 X	.88472	41.5	1.5092 X
0.79829	38.6	1.6029 X	0.88784	41.6	1.5062 X
0.80115	38.7	1.5994 X	0.89097	41.7	1.5032 X
.80402	38.8	1.5959 X	.89410	41.8	1.5003 X
.80690	38.9	1.5924 X	0.89725	41.9	1.4974 X
0.80978	39.0	1.5890 X			
0.81268	39.1	1.5856 X	0.90040	42.0	1.4945 X
.81558	39.2	1.5822 X	.90357	42.1	1.4916 X
0.81849	39.3	1.5788 X	.90674	42.2	1.4887 X
			0.90993	42.3	1.4858 X
0.82141	39.4	1.5755 X	0.91312	42.4	1.4830 X
.82434	39.5	1.5721 X	.91633	42.5	1.4802 X
0.82727	39.6	1.5688 X	0.91955	42.6	1.4774 X
0.83022	39.7	1.5655 X	0.92277	42.7	1.4746 X
.83317	39.8	1.5622 X	.92601	42.8	1.4718 X
.83613	39.9	1.5590 X	0.92926	42.9	1.4690 X
0.83910	40.0	1.5557 X			
0.84208	40.1	1.5525 X	0.93251	43.0	1.4663 X
.84506	40.2	1.5493 X	.93578	43.1	1.4635 X
0.84806	40.3	1.5461 X	0.93906	43.2	1.4608 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
0.94235	43.3	1.4581 X	1.0538	46.5	1.3786 X
.94565	43.4	1.4554 X	1.0575	46.6	1.3763 X
0.94896	43.5	1.4527 X	1.0612	46.7	1.3740 X
0.95229	43.6	1.4501 X	1.0649	46.8	1.3718 X
.95562	43.7	1.4474 X	1.0686	46.9	1.3695 X
0.95896	43.8	1.4448 X	1.0724	47.0	1.3673 X
0.96232	43.9	1.4422 X	1.0761	47.1	1.3651 X
.96569	44.0	1.4395 X	1.0799	47.2	1.3629 X
0.96907	44.1	1.4370 X	1.0837	47.3	1.3607 X
0.97246	44.2	1.4344 X	1.0875	47.4	1.3585 X
.97586	44.3	1.4318 X	1.0913	47.5	1.3563 X
0.97927	44.4	1.4292 X	1.0951	47.6	1.3542 X
0.98270	44.5	1.4267 X	1.0990	47.7	1.3520 X
.98613	44.6	1.4242 X	1.1028	47.8	1.3499 X
0.98958	44.7	1.4217 X	1.1067	47.9	1.3477 X
0.99304	44.8	1.4192 X	1.1106	48.0	1.3456 X
0.99651	44.9	1.4167 X	1.1145	48.1	1.3435 X
1.0000	45.0	1.4142 X	1.1184	48.2	1.3414 X
1.0035	45.1	1.4117 X	1.1224	48.3	1.3393 X
1.0070	45.2	1.4093 X	1.1263	48.4	1.3372 X
1.0105	45.3	1.4069 X	1.1303	48.5	1.3352 X
1.0141	45.4	1.4040 X	1.1343	48.6	1.3331 X
1.0176	45.5	1.4020 X	1.1383	48.7	1.3311 X
1.0212	45.6	1.3996 X	1.1423	48.8	1.3290 X
1.0247	45.7	1.3972 X	1.1463	48.9	1.3270 X
1.0283	45.8	1.3949 X	1.1504	49.0	1.3250 X
1.0319	45.9	1.3925 X	1.1544	49.1	1.3230 X
1.0355	46.0	1.3902 X	1.1585	49.2	1.3210 X
1.0391	46.1	1.3878 X	1.1626	49.3	1.3190 X
1.0428	46.2	1.3855 X	1.1667	49.4	1.3170 X
1.0464	46.3	1.3832 X	1.1708	49.5	1.3151 X
1.0501	46.4	1.3809 X	1.1750	49.6	1.3131 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
1.1791	49.7	1.3112 X	1.3367	53.2	1.2488 X
1.1833	49.8	1.3092 X	1.3416	53.3	1.2472 X
1.1875	49.9	1.3073 X	1.3465	53.4	1.2456 X
1.1917	50.0	1.3054 X	1.3514	53.5	1.2440 X
1.1960	50.1	1.3035 X	1.3564	53.6	1.2424 X
1.2002	50.2	1.3016 X	1.3613	53.7	1.2408 X
1.2045	50.3	1.2997 X	1.3663	53.8	1.2392 X
1.2088	50.4	1.2978 X	1.3713	53.9	1.2376 X
1.2131	50.5	1.2960 X	1.3764	54.0	1.2361 X
1.2174	50.6	1.2941 X	1.3814	54.1	1.2345 X
1.2218	50.7	1.2922 X	1.3865	54.2	1.2329 X
1.2261	50.8	1.2904 X	1.3916	54.3	1.2314 X
1.2305	50.9	1.2886 X	1.3968	54.4	1.2298 X
1.2349	51.0	1.2867 X	1.4019	54.5	1.2283 X
1.2393	51.1	1.2849 X	1.4071	54.6	1.2268 X
1.2437	51.2	1.2831 X	1.4123	54.7	1.2253 X
1.2482	51.3	1.2813 X	1.4176	54.8	1.2238 X
1.2527	51.4	1.2795 X	1.4228	54.9	1.2223 X
1.2572	51.5	1.2778 X	1.4281	55.0	1.2208 X
1.2617	51.6	1.2760 X	1.4335	55.1	1.2193 X
1.2662	51.7	1.2742 X	1.4388	55.2	1.2178 X
1.2708	51.8	1.2725 X	1.4442	55.3	1.2163 X
1.2753	51.9	1.2707 X	1.4496	55.4	1.2149 X
1.2799	52.0	1.2690 X	1.4550	55.5	1.2134 X
1.2845	52.1	1.2673 X	1.4605	55.6	1.2119 X
1.2892	52.2	1.2656 X	1.4659	55.7	1.2105 X
1.2938	52.3	1.2639 X	1.4714	55.8	1.2091 X
1.2985	52.4	1.2622 X	1.4770	55.9	1.2076 X
1.3032	52.5	1.2605 X	1.4826	56.0	1.2062 X
1.3079	52.6	1.2588 X	1.4881	56.1	1.2048 X
1.3127	52.7	1.2571 X	1.4938	56.2	1.2034 X
1.3174	52.8	1.2554 X	1.4994	56.3	1.2020 X
1.3222	52.9	1.2538 X	1.5051	56.4	1.2006 X
1.3270	53.0	1.2521 X	1.5108	56.5	1.1992 X
1.3319	53.1	1.2505 X	1.5166	56.6	1.1978 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
1.5223	56.7	1.1964 X	1.7461	60.2	1.1524 X
1.5282	56.8	1.1951 X	1.7532	60.3	1.1512 X
1.5340	56.9	1.1937 X	1.7603	60.4	1.1501 X
1.5399	57.0	1.1924 X	1.7675	60.5	1.1489 X
1.5458	57.1	1.1910 X	1.7747	60.6	1.1478 X
1.5517	57.2	1.1897 X	1.7820	60.7	1.1467 X
1.5577	57.3	1.1883 X	1.7893	60.8	1.1456 X
1.5636	57.4	1.1870 X	1.7966	60.9	1.1445 X
1.5697	57.5	1.1857 X	1.8040	61.0	1.1433 X
1.5757	57.6	1.1844 X	1.8115	61.1	1.1422 X
1.5818	57.7	1.1831 X	1.8190	61.2	1.1411 X
1.5880	57.8	1.1818 X	1.8265	61.3	1.1401 X
1.5941	57.9	1.1805 X	1.8341	61.4	1.1390 X
1.6003	58.0	1.1792 X	1.8418	61.5	1.1379 X
1.6006	58.1	1.1779 X	1.8495	61.6	1.1368 X
1.6128	58.2	1.1766 X	1.8572	61.7	1.1357 X
1.6191	58.3	1.1753 X	1.8650	61.8	1.1347 X
1.6255	58.4	1.1741 X	1.8728	61.9	1.1336 X
1.6318	58.5	1.1728 X	1.8807	62.0	1.1326 X
1.6383	58.6	1.1716 X	1.8887	62.1	1.1315 X
1.6447	58.7	1.1703 X	1.8967	62.2	1.1305 X
1.6512	58.8	1.1691 X	1.9047	62.3	1.1294 X
1.6577	58.9	1.1678 X	1.9128	62.4	1.1284 X
1.6643	59.0	1.1666 X	1.9210	62.5	1.1274 X
1.6709	59.1	1.1654 X	1.9292	62.6	1.1264 X
1.6775	59.2	1.1642 X	1.9375	62.7	1.1253 X
1.6842	59.3	1.1630 X	1.9458	62.8	1.1243 X
1.6909	59.4	1.1618 X	1.9542	62.9	1.1233 X
1.6977	59.5	1.1606 X	1.9626	63.0	1.1223 X
1.7044	59.6	1.1594 X	1.9711	63.1	1.1213 X
1.7113	59.7	1.1582 X	1.9797	63.2	1.1203 X
1.7182	59.8	1.1570 X	1.9883	63.3	1.1193 X
1.7251	59.9	1.1559 X	1.9969	63.4	1.1184 X
1.7320	60.0	1.1547 X	2.0057	63.5	1.1174 X
1.7390	60.1	1.1535 X	2.0145	63.6	1.1164 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
2.0233	63.7	1.1155 X	2.3789	67.2	1.0647 X
2.0323	63.8	1.1145 X	2.3906	67.3	1.0840 X
2.0412	63.9	1.1135 X	2.4023	67.4	1.0832 X
2.0503	64.0	1.1126 X	2.4142	67.5	1.0824 X
2.0594	64.1	1.1116 X	2.4262	67.6	1.0816 X
2.0686	64.2	1.1107 X	2.4382	67.7	1.0808 X
2.0778	64.3	1.1098 X	2.4504	67.8	1.0801 X
2.0872	64.4	1.1088 X	2.4627	67.9	1.0793 X
2.0965	64.5	1.1079 X	2.4751	68.0	1.0785 X
2.1060	64.6	1.1070 X	2.4876	68.1	1.0778 X
2.1115	64.7	1.1061 X	2.5002	68.2	1.0770 X
2.1251	64.8	1.1052 X	2.5129	68.3	1.0763 X
2.1348	64.9	1.1043 X	2.5257	68.4	1.0755 X
2.1445	65.0	1.1034 X	2.5386	68.5	1.0748 X
2.1543	65.1	1.1025 X	2.5517	68.6	1.0740 X
2.1642	65.2	1.1016 X	2.5649	68.7	1.0733 X
2.1741	65.3	1.1007 X	2.5781	68.8	1.0726 X
2.1842	65.4	1.0998 X	2.5916	68.9	1.0719 X
2.1943	65.5	1.0989 X	2.6051	69.0	1.0711 X
2.2045	65.6	1.0981 X	2.6187	69.1	1.0704 X
2.2147	65.7	1.0972 X	2.6325	69.2	1.0697 X
2.2251	65.8	1.0963 X	2.6464	69.3	1.0690 X
2.2355	65.9	1.0955 X	2.6604	69.4	1.0683 X
2.2460	66.0	1.0946 X	2.6746	69.5	1.0676 X
2.2566	66.1	1.0938 X	2.6889	69.6	1.0669 X
2.2673	66.2	1.0929 X	2.7033	69.7	1.0662 X
2.2781	66.3	1.0921 X	2.7179	69.8	1.0655 X
2.2889	66.4	1.0913 X	2.7326	69.9	1.0648 X
2.2998	66.5	1.0904 X	2.7475	70.0	1.0642 X
2.3109	66.6	1.0896 X	2.7625	70.1	1.0635 X
2.3220	66.7	1.0888 X	2.7776	70.2	1.0628 X
2.3332	66.8	1.0880 X	2.7929	70.3	1.0622 X
2.3445	66.9	1.0872 X	2.8083	70.4	1.0615 X
2.3558	67.0	1.0864 X	2.8239	70.5	1.0608 X
2.3673	67.1	1.0855 X	2.8396	70.6	1.0602 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
2.8555	70.7	1.0595 X	3.5339	74.2	1.0393 X
2.8716	70.8	1.0589 X	3.5576	74.3	1.0387 X
2.8878	70.9	1.0582 X	3.5816	74.4	1.0382 X
2.9042	71.0	1.0576 X	3.6059	74.5	1.0377 X
2.9208	71.1	1.0570 X	3.6305	74.6	1.0372 X
2.9375	71.2	1.0563 X	3.6554	74.7	1.0367 X
2.9544	71.3	1.0557 X	3.6806	74.8	1.0362 X
2.9714	71.4	1.0551 X	3.7062	74.9	1.0358 X
2.9887	71.5	1.0545 X	3.7320	75.0	1.0353 X
3.0061	71.6	1.0539 X	3.7583	75.1	1.0348 X
3.0237	71.7	1.0533 X	3.7848	75.2	1.0343 X
3.0415	71.8	1.0527 X	3.8118	75.3	1.0338 X
3.0595	71.9	1.0521 X	3.8390	75.4	1.0334 X
3.0777	72.0	1.0515 X	3.8667	75.5	1.0329 X
3.0960	72.1	1.0509 X	3.8947	75.6	1.0324 X
3.1146	72.2	1.0503 X	3.9231	75.7	1.0320 X
3.1334	72.3	1.0497 X	3.9520	75.8	1.0315 X
3.1524	72.4	1.0491 X	3.9812	75.9	1.0311 X
3.1716	72.5	1.0485 X	4.0108	76.0	1.0306 X
3.1910	72.6	1.0479 X	4.0408	76.1	1.0302 X
3.2106	72.7	1.0474 X	4.0713	76.2	1.0297 X
3.2305	72.8	1.0468 X	4.1022	76.3	1.0293 X
3.2505	72.9	1.0462 X	4.1335	76.4	1.0288 X
3.2708	73.0	1.0457 X	4.1653	76.5	1.0284 X
3.2914	73.1	1.0451 X	4.1976	76.6	1.0280 X
3.3121	73.2	1.0466 X	4.2303	76.7	1.0276 X
3.3332	73.3	1.0440 X	4.2635	76.8	1.0271 X
3.3544	73.4	1.0435 X	4.2972	76.9	1.0267 X
3.3759	73.5	1.0429 X	4.3315	77.0	1.0263 X
3.3977	73.6	1.0424 X	4.3662	77.1	1.0259 X
3.4197	73.7	1.0419 X	4.4015	77.2	1.0225 X
3.4420	73.8	1.0413 X	4.4373	77.3	1.0251 X
3.4646	73.9	1.0408 X	4.4737	77.4	1.0247 X
3.4874	74.0	1.0403 X	4.5107	77.5	1.0243 X
3.5105	74.1	1.0398 X	4.5483	77.6	1.0239 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
4.5864	77.7	1.0235 X	6.4596	81.2	1.0119 X
4.6252	77.8	1.0231 X	6.5350	81.3	1.0116 X
4.6646	77.9	1.0227 X	6.6122	81.4	1.0114 X
4.7046	78.0	1.0223 X	6.6911	81.5	1.0111 X
4.7453	78.1	1.0220 X	6.7720	81.6	1.0108 X
4.7867	78.2	1.0216 X	6.8547	81.7	1.0106 X
4.8288	78.3	1.0212 X	6.9395	81.8	1.0103 X
4.8716	78.4	1.0208 X	7.0264	81.9	1.0101 X
4.9151	78.5	1.0205 X	7.1154	82.0	1.0098 X
4.9594	78.6	1.0201 X	7.2066	82.1	1.0096 X
5.0045	78.7	1.0198 X	7.3002	82.2	1.0093 X
5.0504	78.8	1.0194 X	7.3961	82.3	1.0091 X
5.0970	78.9	1.0191 X	7.4946	82.4	1.0089 X
5.1445	79.0	1.0187 X	7.5957	82.5	1.0086 X
5.1929	79.1	1.0184 X	7.6996	82.6	1.0084 X
5.2422	79.2	1.0180 X	7.8062	82.7	1.0082 X
5.2923	79.3	1.0177 X	7.9158	82.8	1.0079 X
5.3434	79.4	1.0174 X	8.0285	82.9	1.0077 X
5.3955	79.5	1.0170 X	8.1443	83.0	1.0075 X
5.4486	79.6	1.0167 X	8.2635	83.1	1.0073 X
5.5026	79.7	1.0164 X	8.3862	83.2	1.0071 X
5.5578	79.8	1.0160 X	8.5126	83.3	1.0069 X
5.6140	79.9	1.0157 X	8.6427	83.4	1.0067 X
5.6713	80.0	1.0154 X	8.7769	83.5	1.0065 X
5.7297	80.1	1.0151 X	8.9152	83.6	1.0063 X
5.7894	80.2	1.0148 X	9.0579	83.7	1.0061 X
5.8502	80.3	1.0145 X	9.2051	83.8	1.0059 X
5.9123	80.4	1.0142 X	9.3572	83.9	1.0057 X
5.9758	80.5	1.0139 X	9.5144	84.0	1.0055 X
6.0405	80.6	1.0136 X	9.6768	84.1	1.0053 X
6.1066	80.7	1.0133 X	9.8448	84.2	1.0051 X
6.1742	80.8	1.0130 X	10.019	84.3	1.0050 X
6.2432	80.9	1.0127 X	10.199	84.4	1.0048 X
6.3137	81.0	1.0125 X	10.385	84.5	1.0046 X
6.3859	81.1	1.0122 X	10.579	84.6	1.0044 X

Table 25-1. Vector Conversion (cont'd)

$\frac{X}{R}$	$\theta$ degrees	Z	$\frac{X}{R}$	$\theta$ degrees	Z
10.780	84.7	1.0043 X	22.022	87.4	1.0010 X
10.988	84.8	1.0041 X	23.904	87.5	1.0009 X
11.205	84.9	1.0040 X	23.859	87.6	1.0009 X
11.430	85.0	1.0038 X	24.898	87.7	1.0008 X
11.664	85.1	1.0037 X	26.031	87.8	1.0007 X
11.909	85.2	1.0035 X	27.271	87.9	1.0007 X
12.163	85.3	1.0034 X	28.636	88.0	1.0006 X
12.429	85.4	1.0032 X	30.145	88.1	1.0005 X
12.706	85.5	1.0031 X	31.820	88.2	1.0005 X
12.996	85.6	1.0029 X	33.693	88.3	1.0004 X
13.229	85.7	1.0028 X	35.800	88.4	1.0004 X
13.617	85.8	1.0027 X	38.188	88.5	1.0003 X
13.951	85.9	1.0026 X	40.917	88.6	1.0003 X
14.301	86.0	1.0024 X	44.066	88.7	1.0002 X
14.668	86.1	1.0023 X	47.739	88.8	1.0002 X
15.056	86.2	1.0022 X	52.081	88.9	1.0002 X
15.464	86.3	1.0021 X	57.290	89.0	1.0001 X
15.894	86.4	1.0020 X	63.657	89.1	1.0001 X
16.350	86.5	1.0019 X	71.615	89.2	1.0001 X
16.832	86.6	1.0018 X	81.847	89.3	1.0001 X
17.343	86.7	1.0017 X	95.489	89.4	1.0000 X
17.886	86.8	1.0016 X	114.59	89.5	1.0000 X
18.464	86.9	1.0015 X	143.24	89.6	1.0000 X
19.081	87.0	1.0014 X	190.98	89.7	1.0000 X
19.740	87.1	1.0013 X	286.48	89.8	1.0000 X
20.446	87.2	1.0012 X	572.96	89.9	1.0000 X
21.205	87.3	1.0011 X	R = 0	90.0	1.0000 X

off to 5000) and the phase angle is  $-53.1$  degrees. How could we express this in  $j$ -notation?

Start with the phase angle. In the third column  $1.25X$  equals  $Z$ . But  $Z$  equals 5000 ohms. Since  $1.25X$  equals 5000, then  $X$  equals  $5000/1.25$ , or 4,000 ohms. Now move back to the first column. Here  $X/R$  equals 1.3319. Thus,  $4000/R$  equals 1.3319. Solving for  $R$  we get  $R$  equals 3000 ohms. And, since we know that the phase angle is negative, we also know that our  $j$  term will also be negative. Our answer, then, is  $3000-j4000$ .

**□Example:**

What is the impedance of a circuit whose resistance,  $R$ , is 1000 ohms and whose reactance,  $X$ , is 775 ohms?

The ratio,  $X/R$  is  $775/1000$  or 0.775. Locating the nearest equivalent number in the first column of Table 25-1 gives 0.77568. To the right of this number, the phase angle is 37.8 degrees and, continuing to the right,  $Z$  equals  $1.6316X$ . Thus, the impedance,  $Z$  equals  $1.6316 \times 775$ , or 1264.49 ohms.

## Chapter 26

# Time Constants

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### RC TIME CONSTANTS

RC networks are used in a variety of applications, including differentiating and integrating networks; emphasis and de-emphasis circuits; time delay elements in radio control receivers; oscillators; electronic switches and light flashers.

The time required to charge or discharge a capacitor depends on the amount of capacitance and the value of the associated resistor. The formula for the charge or discharge of a capacitor through a resistor is  $T = R \times C$  in which the resistance is in ohms and the capacitance is in farads. The time,  $T$ , is the time in seconds for the capacitor to charge to 63 percent of its maximum, or for the charge on the capacitor to drop to 37 percent of its maximum. Multiples are shown in Table 26-1.

Table 26-2 supplies the time constants for a capacitance range of 0.1 to 1  $\mu\text{F}$  and from 0.1 to 10 seconds. Note that increasing the value of  $R$  or  $C$  will increase the time constant proportionately.

Although the formula for RC time constants requires basic units, multiples can be used if conversions are made in accordance with Table 26-1.

#### □ Example:

How long will it take to charge a capacitor having a value of 0.2  $\mu\text{F}$  through a 500K resistor?

Locate 0.2 in the capacitance column in Table 26-2. Immediately beneath this value locate 500K. Move to the left and you will see that it will take 0.1 second.

Table 26-1. Multiples of Units for Time Constants

Where R is in	C is in	L is in	T is in
ohms	farads	henrys	seconds
ohms	$\mu$ f	$\mu$ h	$\mu$ sec
kilohms	$\mu$ f	henrys	msec
kilohms	—	mh	$\mu$ sec
megohms	$\mu$ f	—	seconds
megohms	pf	henrys	$\mu$ sec

( $\mu$  sec = microseconds; m sec = milliseconds;  $\mu$ F = microfarads; pF = picofarads;  $\mu$ H = micro henrys; mH = millihenrys)

#### □Example:

What combination of resistance and capacitance can be used to obtain a one-second time constant?

Locate one second in the *time in seconds* column. If you will now move to the right you will see that a number of possible combinations are available—10 megohms and 0.1  $\mu$ F; 5 megohms and 0.2  $\mu$ F; 3.3 megohms and 0.3  $\mu$ F, etc.

Time constants can be had for values other than those shown in the left-hand column of Table 26-2. Thus if the value of capacitance is reduced by half or if the value of resistance is similarly reduced (but not both at the same time) the value of the time constant is also lowered by half.

#### □Example:

What is the time constant for a value of capacitance of .05  $\mu$ F and a resistance of 1 megohm?

There is no column headed by .05  $\mu$ F but there is a column marked 0.1. Divide this by 2 and you will have .05  $\mu$ F. Move down from 0.1 (now considered as .05) until you reach 1.0 megohm, the given value of resistance. Move directly to the left and you will see a time constant of 0.1 second. Divide this by 2 and the time constant for the values of R and C that were given will be .05 second. To get a time constant of .05 second either reduce the resistance 1.0 megohm to 500K ohms or the capacitance to .05 microfarads. If we reduce both R and C by 50 percent, the value of the time constant becomes one-fourth of the value given in Table 26-2. Thus, for a value of 500K ohms and a capacitance of .05  $\mu$ F the time constant is .025 second.

Table 26-2. RC Time Constants

Time (sec)	Capacitance (microfarads)				
	0.1	0.2	0.3	0.4	0.5
0.1	1.0M	500K	333K	250K	200K
0.15	1.5M	750K	500K	375K	300K
0.2	2.0M	1.00M	666K	500K	400K
0.25	2.5M	1.25M	833K	625K	500K
0.3	3.0M	1.50M	1.00M	750K	600K
0.35	3.5M	1.75M	1.17M	875K	700K
0.4	4.0M	2.00M	1.33M	1.00M	800K
0.45	4.5M	2.25M	1.50M	1.13M	900K
0.5	5.0M	2.50M	1.67M	1.25M	1.0M
0.55	5.5M	2.75M	1.83M	1.38M	1.1M
0.6	6.0M	3.00M	2.00M	1.50M	1.2M
0.65	6.5M	3.25M	2.17M	1.63M	1.3M
0.7	7.0M	3.50M	2.33M	1.75M	1.4M
0.75	7.5M	3.75M	2.50M	1.88M	1.5M
0.8	8.0M	4.00M	2.67M	2.00M	1.6M
0.85	8.5M	4.25M	2.83M	2.13M	1.7M
0.9	9.0M	4.50M	3.00M	2.25M	1.8M
0.95	9.5M	4.75M	3.17M	2.38M	1.9M
1.0	10.0M	5.00M	3.33M	2.50M	2.0M
1.5	15.0M	7.50M	5.00M	3.75M	3.0M
2.0	20.0M	10.00M	6.66M	5.00M	4.0M
2.5	25.0M	12.50M	8.33M	6.25M	5.0M
3.0	30.0M	15.00M	10.00M	7.50M	6.0M
3.5	35.0M	17.50M	11.66M	8.75M	7.0M
4.0	40.0M	20.00M	13.33M	10.00M	8.0M
4.5	45.0M	22.50M	15.00M	11.25M	9.0M
5.0	50.0M	25.00M	16.67M	12.50M	10.0M
5.5	55.0M	27.50M	18.33M	13.75M	11.0M
6.0	60.0M	30.00M	20.00M	15.00M	12.0M
6.5	65.0M	32.50M	21.67M	16.25M	13.0M
7.0	70.0M	35.00M	23.33M	17.50M	14.0M
7.5	75.0M	37.50M	25.00M	18.75M	15.0M
8.0	80.0M	40.00M	26.67M	20.00M	16.0M
9.0	90.0M	45.00M	30.00M	22.50M	18.0M
10.0	100.0M	50.00M	33.33M	25.00M	20.0M

K = kilohms

M = megohms

Table 26-2. RC Time Constants (cont'd)

Time (sec)	Capacitance (microfarads)				
	0.6	0.7	0.8	0.9	1.0
0.1	166K	143K	125K	111K	100K
0.15	250K	214K	188K	167K	150K
0.2	333K	286K	250K	222K	200K
0.25	417K	357K	313K	278K	250K
0.3	500K	429K	375K	333K	300K
0.35	583K	500K	438K	389K	350K
0.4	666K	571K	500K	444K	400K
0.45	750K	643K	563K	500K	450K
0.5	833K	714K	625K	555K	500K
0.55	917K	786K	688K	611K	550K
0.6	1.00M	857K	750K	666K	600K
0.65	1.08M	929K	813K	722K	650K
0.7	1.17M	1.00M	875K	778K	700K
0.75	1.25M	1.07M	938K	833K	750K
0.8	1.33M	1.14M	1.00M	889K	800K
0.85	1.42M	1.21M	1.06M	944K	850K
0.9	1.50M	1.29M	1.13M	1.00M	900K
0.95	1.58M	1.36M	1.19M	1.06M	950K
1.0	1.67M	1.43M	1.25M	1.11M	1.0M
1.5	2.50M	2.14M	1.88M	1.67M	1.5M
2.0	3.33M	2.86M	2.50M	2.22M	2.0M
2.5	4.17M	3.57M	3.13M	2.78M	2.5M
3.0	5.00M	4.29M	3.75M	3.33M	3.0M
3.5	5.83M	5.00M	4.38M	3.89M	3.5M
4.0	6.66M	5.71M	5.00M	4.44M	4.0M
4.5	7.50M	6.43M	5.63M	5.00M	4.5M
5.0	8.33M	7.14M	6.25M	5.55M	5.0M
5.5	9.17M	7.86M	6.88M	6.11M	5.5M
6.0	10.00M	8.57M	7.50M	6.66M	6.0M
6.5	10.83M	9.29M	8.13M	7.22M	6.5M
7.0	11.67M	10.00M	8.75M	7.78M	7.0M
7.5	12.50M	10.71M	9.38M	8.33M	7.5M
8.0	13.33M	11.43M	10.00M	8.89M	8.0M
9.0	15.00M	12.86M	11.25M	10.00M	9.0M
10.0	16.66M	14.28M	12.50M	11.11M	10.0M

K = kilohms

M = megohms

## RL TIME CONSTANTS

RL circuits—circuits consisting of a resistor in series with an inductor—are used in timing circuits or in relays where the relay must make or break at predetermined times. The time constant of an RL circuit is based on the formula  $T = L/R$ , where  $T$  is the time in seconds,  $L$  is the inductance in henrys, and  $R$  is the resistance in ohms. The time in seconds is that required for the current to reach 63 percent of its maximum value, or to fall to 37 percent of its maximum. Time constants of RL circuits are in Table 26-3.

The resistance of the coil wire wound must be considered when calculating the time constant. This resistance is regarded as acting in series with the coil. Thus, if the resistance of a coil is 10 ohms and a 100-ohm series resistor is required for an RL circuit, a value close to 90 ohms should be used. As a rule of thumb, if the resistance of the coil is 10 percent or more of the required resistance, it should be taken into consideration. In the case just mentioned, subtracting the 10 ohms of the coil from 100 ohms shows that a 90-ohm resistor would be required. If the value of the external resistor is in the order of kilohms, a coil whose resistance is just a few ohms would not seriously affect the time constant.

### □Example:

A relay coil whose internal resistance is negligible, and whose inductance is 0.05 henry, will make (contacts will close) when the current through the coil reaches 63 percent of its peak. What value of series resistor is needed to have the relay close 0.008 second after the circuit is on?

Note that Table 26-3 does not include a time of 0.008 second nor an inductance of 0.05 henry. However, it is easy to extend the table by moving the decimal point. Change 0.008 to 8 by moving its decimal point three places to the right. The inductance, 0.05 henry, will then become 50. Locate the number 8 in the time column. Move across to the right to reach the 50 column. The answer is 6.3 ohms. The decimal point does not need to be moved in the answer. The reason for this is based on the time-constant formula,  $T = L/R$ . Equal increases or decreases in  $L$  and  $R$  will have no effect on the time constant.

### □Example:

An RL circuit has an inductance of 30 henrys and a resistance of 42.9 ohms. What is its time constant?

Locate the column marked with the number 30 at the top. Move down in this column until you reach the number 42.9. Then

Table 26-3. RL Time Constants

Time (sec)	Inductance (henrys)				
	10	20	30	40	50
0.1	100.0	200.0	300.0	400.0	500.0
0.15	66.7	133.3	200.0	266.7	333.3
0.2	50.0	100.0	150.0	200.0	250.0
0.25	40.0	80.0	120.0	160.0	200.0
0.3	33.3	66.7	100.0	133.3	166.7
0.35	28.6	57.1	86.6	114.3	142.9
0.4	25.0	50.0	75.0	100.0	125.0
0.45	22.2	44.4	66.7	88.9	111.1
0.5	20.0	40.0	60.0	80.0	100.0
0.55	18.2	36.4	54.5	72.7	90.9
0.6	16.7	33.3	50.0	66.7	83.3
0.65	15.4	30.8	46.2	61.5	76.9
0.7	14.3	28.6	42.9	57.1	71.4
0.75	13.3	26.7	40.0	53.3	66.7
0.8	12.5	25.0	37.5	50.0	62.5
0.85	11.8	23.5	35.3	47.1	58.8
0.9	11.1	22.2	33.3	44.4	55.5
0.95	10.5	21.1	31.6	42.1	52.6
1.0	10.0	20.0	30.0	40.0	50.0
1.5	6.7	13.3	20.0	26.7	33.3
2.0	5.0	10.0	15.0	20.0	25.0
2.5	4.0	8.0	12.0	16.0	20.0
3.0	3.3	6.7	10.0	13.3	16.7
3.5	2.9	5.7	8.7	11.4	14.3
4.0	2.5	5.0	7.5	10.0	12.5
4.5	2.2	4.4	6.7	8.9	11.1
5.0	2.0	4.0	6.0	8.0	10.0
5.5	1.8	3.6	5.5	7.3	9.1
6.0	1.7	3.3	5.0	6.7	8.3
6.5	1.5	3.1	4.6	6.2	7.7
7.0	1.4	2.9	4.3	5.7	7.1
7.5	1.3	2.7	4.0	5.3	6.7
8.0	1.2	2.5	3.8	5.0	6.3
9.0	1.1	2.2	3.3	4.4	5.5
10.0	1.0	2.0	3.0	4.0	5.0

All resistance values in ohms

Table 26-3. RL Time Constants (cont'd)

Time (sec)	Inductance (henrys)				
	60	70	80	90	100
0.1	600.0	700.0	800.0	900.0	1000.0
0.15	400.0	466.7	533.3	600.0	666.7
0.2	300.0	350.0	400.0	450.0	500.0
0.25	240.0	280.0	320.0	360.0	400.0
0.3	200.0	233.3	266.6	300.0	333.3
0.35	171.4	200.0	228.6	257.1	285.7
0.4	150.0	175.0	200.0	225.0	250.0
0.45	133.3	155.6	177.8	200.0	222.2
0.5	120.0	140.0	160.0	180.0	200.0
0.55	109.1	127.3	145.5	163.6	181.8
0.6	100.0	116.7	133.3	150.0	166.7
0.65	92.3	107.7	123.1	138.5	153.8
0.7	85.7	100.0	114.3	128.7	142.9
0.75	80.0	93.3	106.7	120.0	133.3
0.8	75.0	87.5	100.0	112.5	125.0
0.85	70.6	82.3	94.1	105.9	117.6
0.9	66.6	77.8	88.9	100.0	111.1
0.95	63.2	73.7	84.2	94.7	105.3
1.0	60.0	70.0	80.0	90.0	100.0
1.5	40.0	46.7	53.3	60.0	66.7
2.0	30.0	35.0	40.0	45.0	50.0
2.5	24.0	28.0	32.0	36.0	40.0
3.0	20.0	23.3	26.7	30.0	33.3
3.5	17.1	20.0	22.9	25.7	28.6
4.0	15.0	17.5	20.0	22.5	25.0
4.5	13.3	15.6	17.8	20.0	22.2
5.0	12.0	14.0	16.0	18.0	20.0
5.5	10.9	12.7	14.6	16.4	18.2
6.0	10.0	11.7	13.3	15.0	16.7
6.5	9.2	10.8	12.3	13.9	15.4
7.0	8.6	10.0	11.4	12.9	14.3
7.5	8.0	9.3	10.7	12.0	13.3
8.0	7.5	8.8	10.0	11.3	12.5
9.0	6.7	7.8	8.9	10.0	11.1
10.0	6.0	7.0	8.0	9.0	10.0

All resistance values in ohms

move to the left to the time (sec) column and you will find the time constant of this circuit is 0.7 second.

If you were to do this problem by using the formula,  $T = L/R$ , you would have  $T = 30/42.9 = 0.6993$  second. The difference between the two answers is  $0.7 - 0.6993 = 0.0007$  second, an extremely small percentage of error.

## Chapter 27

### Angular Velocity

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In an AC generator, the rotating armature produces a voltage sine wave. We can represent the armature by a rotating vector  $r$ . The angle through which this vector sweeps is usually indicated by the Greek letter  $\Theta$ . The instantaneous values of the voltage produced are maximum when the phase angle,  $\Theta$ , is 90 degrees or  $270^\circ$  and zero when that phase angle is 0 degrees or 180 degrees.

The radius vector  $r$  rotates about the origin, 0, and is taken to rotate in a counterclockwise direction. The angular velocity in radians per second of this rotating vector is the rate at which the angle,  $\Theta$ , is produced by its rotation. Angular velocity is conveniently represented by  $\omega$  or  $2\pi f$  (radians per second) in which  $2\pi$  is a constant and is equal to 6.28. The frequency  $f$  is in Hertz.

Angular velocity appears in formulas involving instantaneous values of sine waves of voltage or current ( $e$  equals  $E_{max} \sin \omega t$ ) and in formulas involving inductive reactance ( $X_L$  equals  $2\pi fL$ ) and capacitive reactance ( $X_C$  equals 1 divided by  $2\pi fC$ ).

The solution of problems involving angular velocity is simplified by Table 27-1. Here we have angular velocity corresponding to particular values of frequency.

Table 27-1 can be used for values of frequency other than those indicated by moving the decimal point. To find  $\omega$  at a frequency of 4 kHz, find 40 in the  $f$  column. To change 40 Hz to 4 kHz multiply 40 by 100. This means we must also multiply the value of 251.20 (which is the value of  $\omega$  for 40) by 100. The answer is 25,120. To get megahertz values, multiply both  $f$  and  $\omega$  by 1,000,000.

□ Example:

What is the angular velocity of a generator, whose armature rotates at 1800 revolutions per minute?

Divide 1800 revolutions by 60 (60 seconds equals 1 minute) to obtain the number of revolutions per second. 1800/60 equals 30 revolutions per second. In 30 revolutions the armature generates 30 complete sinewave cycles. The frequency, then, is 30. Locate 30 in the frequency (f) column of Table 27-1. The corresponding angular velocity is found to the right in the  $\omega$  column. The answer is 188.4 radians per second.

Table 27-1. Angular Velocity (Radians per Second)

f (Hz)	$\omega$	f (Hz)	$\omega$	f (Hz)	$\omega$
10	62.8	40	251.20	70	439.60
11	69.08	41	257.48	71	445.88
12	75.36	42	263.76	72	452.16
13	81.64	43	270.04	73	458.44
14	87.92	44	276.32	74	464.72
15	94.20	45	282.60	75	471.00
16	100.48	46	288.88	76	477.28
17	106.76	47	295.16	77	483.56
18	113.04	48	301.44	78	489.84
19	119.32	49	307.72	79	496.12
20	125.60	50	314.00	80	502.40
21	131.88	51	320.28	81	508.68
22	138.16	52	326.56	82	514.96
23	144.44	53	332.84	83	521.24
24	150.72	54	339.12	84	527.52
25	157.00	55	345.40	85	533.80
26	163.28	56	351.68	86	540.08
27	169.56	57	357.96	87	546.36
28	175.84	58	364.24	88	552.64
29	182.12	59	370.52	89	558.92
30	188.40	60	376.80	90	565.20
31	194.68	61	383.08	91	571.48
32	200.96	62	389.36	92	577.76
33	207.24	63	395.64	93	584.04
34	213.52	64	401.92	94	590.32
35	219.80	65	408.20	95	596.60
36	226.08	66	414.48	96	602.88
37	232.36	67	420.76	97	609.16
38	238.64	68	427.04	98	615.44
39	244.92	69	433.32	99	621.72
				100	628.00

## **Chapter 28**

# **Conversions**

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### **FREQUENCY-WAVELENGTH CONVERSION (KHZ TO METERS)**

The relationship between the frequency of a wave ( $f$ ) in hertz or cycles per second and its wavelength, in meters, is supplied by the formula  $\lambda$  equals  $300,000,000/f$ . The number 300,000,000 in the numerator of the formula is the velocity of light (and of radio waves) in space, and is a constant.  $\lambda$  is the wavelength in meters.

The velocity of light is in meters per second. Although it is frequently rounded off to 300,000,000, its more probable value is 299,820,000 meters per second, the value used in Table 28-1. When the frequency is in hertz, wavelength in meters equals  $299,820,000/f$ . When the frequency is in kilohertz, wavelength in meters equals  $299,820/f$ . When the frequency is in megahertz, wavelength in meters equals  $299.82/f$ .

Wavelength and frequency have an inverse relationship. As frequency increases, wavelength decreases. Conversely, a decrease in frequency means an increase in wavelength. In terms of formulas:  $\lambda$  equals  $299,820,000$  divided by  $f$ , or  $f$  equals  $299,820,000$  divided by  $\lambda$ . Consequently, the columns indicated in Table 28-2 are interchangeable. Thus, the first line in the first column indicates that a wavelength of 10 meters is equivalent to a frequency of 29,982 kilohertz, or 10 kilohertz corresponds to a wavelength of 29.982 meters.

Table 28-1 supplies the abbreviations and descriptions of waves whose frequency extends from 30 kilohertz to 300,000 MHz.

Table 28-2 gives conversion data between frequency in kilohertz and wavelength in meters. The columns shown in Table 28-2 are interchangeable and cover the range from 1 kilohertz or meters to 10,000 kilohertz or meters.

**Table 28-1. Frequency Bands**

Frequency	Description	Abbreviation
Below 30 kHz	very-low frequency	VLF
30 to 300 kHz	low frequency	LF
300 to 3,000 kHz	medium frequency	MF
3,000 to 30,000 kHz	high frequency	HF
30 to 300 MHz	very-high frequency	VHF
300 to 3,000 MHz	ultra-high frequency	UHF
3,000 to 30,000 MHz	super-high frequency	SHF
30,000 to 300,000 MHz (30 GHz to 300 GHz)	extremely-high frequency	EHF

**□Example:**

A radio wave has a frequency of 500 kiloHertz. What is its wavelength in meters?

Find the number 500 in Table 28-2. Move horizontally and you will see the corresponding wavelength of 599.6 meters.

**Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz**

kHz	m	kHz	m	kHz	m	kHz	m
1	299.820	80	3,748	240	1,249	400	749.6
2	149,910	90	3,331	250	1,199	410	731.7
3	99,940	100	2,998	260	1,153	420	714.3
4	74,955	110	2,726	270	1,110	430	697.7
5	59,964	120	2,499	280	1,071	440	681.4
6	49,970	130	2,306	290	1,034	450	666.7
7	42,831	140	2,142	300	999.4	460	652.2
8	37,478	150	1,999	310	967.7	470	638.3
9	33,313	160	1,874	320	937.5	480	624.6
10	29,982	170	1,764	330	908.1	490	612.2
20	14,991	180	1,666	340	882.4	500	599.6
30	9,994	190	1,578	350	859.1	510	588.2
40	7,495	200	1,499	360	833.3	520	576.9
50	5,996	210	1,428	370	810.8	530	565.7
60	4,997	220	1,363	380	789.5	540	555.6
70	4,283	230	1,304	390	769.2	550	545.4

Table 28-2. Kilohertz (kHz) to Meters (m), or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
560	535.7	910	329.5	1,260	238.0
570	526.3	920	325.9	1,270	236.1
580	517.2	930	322.4	1,280	234.2
590	508.5	940	319.0	1,290	232.4
600	499.7	950	315.6	1,300	230.6
610	491.8	960	312.3	1,310	228.9
620	483.7	970	309.1	1,320	227.1
630	476.2	980	305.9	1,330	225.4
640	468.7	990	302.8	1,340	223.7
650	461.5	1,000	299.8	1,350	222.1
660	454.5	1,010	296.9	1,360	220.5
670	447.8	1,020	293.9	1,370	218.8
680	441.2	1,030	291.1	1,380	217.3
690	434.8	1,040	288.3	1,390	215.7
700	428.6	1,050	285.5	1,400	214.2
710	422.5	1,060	282.8	1,410	212.6
720	416.7	1,070	280.2	1,420	211.1
730	410.7	1,080	277.6	1,430	209.7
740	405.4	1,090	275.1	1,440	208.2
750	399.8	1,100	272.6	1,450	206.8
760	394.7	1,110	270.1	1,460	205.4
770	389.6	1,120	267.7	1,470	204.0
780	384.6	1,130	265.3	1,480	202.6
790	379.8	1,140	263.0	1,490	201.2
800	374.8	1,150	260.7	1,500	199.9
810	370.4	1,160	258.5	1,510	198.6
820	365.9	1,170	256.3	1,520	197.2
830	361.4	1,180	254.1	1,530	196.0
840	357.1	1,190	251.9	1,540	194.7
850	352.9	1,200	249.9	1,550	193.4
860	348.8	1,210	247.8	1,560	192.2
870	344.8	1,220	245.8	1,570	191.0
880	340.9	1,230	243.8	1,580	189.8
890	337.1	1,240	241.8	1,590	188.6
900	333.3	1,250	239.9	1,600	187.4

Table 28-2. Kilohertz (kHz) to Meters (m), or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
1,610	186.2	1,910	157.0	2,210	135.7
1,620	185.1	1,920	156.2	2,220	135.1
1,630	183.9	1,930	155.3	2,230	134.4
1,640	182.8	1,940	154.5	2,240	133.8
1,650	181.7	1,950	153.8	2,250	133.3
1,660	180.6	1,960	153.0	2,260	132.7
1,670	179.5	1,970	152.2	2,270	132.1
1,680	178.5	1,980	151.4	2,280	131.5
1,690	177.4	1,990	150.7	2,290	130.9
1,700	176.4	2,000	149.9	2,300	130.4
1,710	175.3	2,010	149.2	2,310	129.8
1,720	174.3	2,020	148.4	2,320	129.2
1,730	173.3	2,030	147.7	2,330	128.7
1,740	172.3	2,040	147.0	2,340	128.1
1,750	171.3	2,050	146.3	2,350	127.6
1,760	170.4	2,060	145.5	2,360	127.0
1,770	169.4	2,070	144.8	2,370	126.5
1,780	168.4	2,080	144.1	2,380	126.0
1,790	167.5	2,090	143.5	2,390	125.4
1,800	166.6	2,100	142.8	2,400	124.9
1,810	165.6	2,110	142.1	2,410	124.4
1,820	164.7	2,120	141.4	2,420	123.9
1,830	163.8	2,130	140.8	2,430	123.4
1,840	162.9	2,140	140.1	2,440	122.9
1,850	162.1	2,150	139.5	2,450	122.4
1,860	161.2	2,160	138.8	2,460	121.9
1,870	160.3	2,170	138.2	2,470	121.4
1,880	159.5	2,180	137.5	2,480	120.9
1,890	158.6	2,190	136.9	2,490	120.4
1,900	157.8	2,200	136.3	2,500	119.9

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
2,510	119.5	2,810	106.7	3,110	96.41
2,520	119.0	2,820	106.3	3,120	96.10
2,530	118.5	2,830	105.9	3,130	95.79
2,540	118.0	2,840	105.6	3,140	95.48
2,550	117.6	2,850	105.2	3,150	95.18
2,560	117.1	2,860	104.8	3,160	94.88
2,570	116.7	2,870	104.5	3,170	94.58
2,580	116.2	2,880	104.1	3,180	94.28
2,590	115.8	2,890	103.7	3,190	93.99
2,600	115.3	2,900	103.4	3,200	93.69
2,610	114.9	2,910	103.0	3,210	93.40
2,620	114.4	2,920	102.7	3,220	93.11
2,630	114.0	2,930	102.3	3,230	92.82
2,640	113.6	2,940	102.0	3,240	92.54
2,650	113.1	2,950	101.6	3,250	92.25
2,660	112.7	2,960	101.3	3,260	91.97
2,670	112.3	2,970	100.9	3,270	91.69
2,680	111.9	2,980	100.6	3,280	91.41
2,690	111.5	2,990	100.3	3,290	91.13
2,700	111.0	3,000	99.94	3,300	90.86
2,710	110.6	3,010	99.61	3,310	90.58
2,720	110.2	3,020	99.28	3,320	90.31
2,730	109.8	3,030	98.95	3,330	90.04
2,740	109.4	3,040	98.63	3,340	89.77
2,750	109.0	3,050	98.30	3,350	89.50
2,760	108.6	3,060	97.98	3,360	89.23
2,770	108.2	3,070	97.66	3,370	88.97
2,780	107.8	3,080	97.34	3,380	88.70
2,790	107.5	3,090	97.03	3,390	88.44
2,800	107.1	3,100	96.72	3,400	88.18

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
3,410	87.92	3,710	80.81	4,010	74.77
3,420	87.67	3,720	80.60	4,020	74.58
3,430	87.41	3,730	80.38	4,030	74.40
3,440	87.16	3,740	80.17	4,040	74.21
3,450	86.90	3,750	79.95	4,050	74.03
3,460	86.65	3,760	79.74	4,060	73.85
3,470	86.40	3,770	79.53	4,070	73.67
3,480	86.16	3,780	79.32	4,080	73.49
3,490	85.91	3,790	79.11	4,090	73.31
3,500	85.66	3,800	78.90	4,100	73.13
3,510	85.42	3,810	78.69	4,110	72.95
3,520	85.18	3,820	78.49	4,120	72.77
3,530	84.93	3,830	78.28	4,130	72.60
3,540	84.69	3,840	78.08	4,140	72.42
3,550	84.46	3,850	77.88	4,150	72.25
3,560	84.22	3,860	77.67	4,160	72.07
3,570	83.98	3,870	77.47	4,170	71.90
3,580	83.75	3,880	77.27	4,180	71.73
3,590	83.52	3,890	77.07	4,190	71.56
3,600	83.28	3,900	76.88	4,200	71.39
3,610	83.05	3,910	76.68	4,210	71.22
3,620	82.82	3,920	76.48	4,220	71.05
3,630	82.60	3,930	76.29	4,230	70.88
3,640	82.37	3,940	76.10	4,240	70.71
3,650	82.14	3,950	75.90	4,250	70.55
3,660	81.92	3,960	75.51	4,260	70.38
3,670	81.69	3,970	75.52	4,270	70.22
3,680	81.47	3,980	75.33	4,280	70.05
3,690	81.25	3,990	75.14	4,290	69.89
3,700	81.03	4,000	74.96	4,300	69.73

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
4,310	69.56	4,610	65.04	4,910	61.06
4,320	69.40	4,620	64.90	4,920	60.94
4,330	69.24	4,630	64.76	4,930	60.82
4,340	69.08	4,640	64.62	4,940	60.69
4,350	68.92	4,650	64.48	4,950	60.57
4,360	68.77	4,660	64.34	4,960	60.45
4,370	68.61	4,670	64.20	4,970	60.33
4,380	68.45	4,680	64.06	4,980	60.20
4,390	68.30	4,690	63.93	4,990	60.08
4,400	68.14	4,700	63.79	5,000	59.96
4,410	67.99	4,710	63.66	5,010	59.84
4,420	67.83	4,720	63.52	5,020	59.73
4,430	67.68	4,730	63.39	5,030	59.61
4,440	67.53	4,740	63.25	5,040	59.49
4,450	67.38	4,750	63.12	5,050	59.37
4,460	67.22	4,760	62.99	5,060	59.25
4,470	67.07	4,770	62.86	5,070	59.14
4,480	66.92	4,780	62.72	5,080	59.02
4,490	66.78	4,790	62.59	5,090	58.90
4,500	66.63	4,800	62.46	5,100	58.79
4,510	66.48	4,810	62.33	5,110	58.67
4,520	66.33	4,820	62.20	5,120	58.56
4,530	66.19	4,830	62.07	5,130	58.44
4,540	66.04	4,840	61.95	5,140	58.33
4,550	65.89	4,850	61.82	5,150	58.22
4,560	65.75	4,860	61.69	5,160	58.10
4,570	65.61	4,870	61.56	5,170	57.99
4,580	65.46	4,880	61.44	5,180	57.88
4,590	65.32	4,890	61.31	5,190	57.77
4,600	65.18	4,900	61.19	5,200	57.66

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
5,210	57.55	5,510	54.41	5,810	51.60
5,220	57.44	5,520	54.32	5,820	52.52
5,230	57.33	5,530	54.22	5,830	51.43
5,240	57.22	5,540	54.12	5,840	51.34
5,250	57.11	5,550	54.02	5,850	51.25
5,260	57.00	5,560	53.92	5,860	51.16
5,270	56.89	5,570	53.83	5,870	51.08
5,280	56.78	5,580	53.73	5,880	50.99
5,290	56.68	5,590	53.64	5,890	50.90
5,300	56.57	5,600	53.54	5,900	50.82
5,310	56.46	5,610	53.44	5,910	50.73
5,320	56.36	5,620	53.35	5,920	50.65
5,330	56.25	5,630	53.25	5,930	50.56
5,340	56.15	5,640	53.16	5,940	50.47
5,350	56.04	5,650	53.07	5,950	50.39
5,360	55.94	5,660	52.97	5,960	50.31
5,370	55.83	5,670	52.88	5,970	50.22
5,380	55.73	5,680	52.79	5,980	50.14
5,390	55.63	5,690	52.69	5,990	50.05
5,400	55.52	5,700	52.60	6,000	49.97
5,410	55.42	5,710	52.51	6,010	49.89
5,420	55.32	5,720	52.42	6,020	49.80
5,430	55.22	5,730	52.32	6,030	49.72
5,440	55.11	5,740	52.23	6,040	49.64
5,450	55.01	5,750	52.14	6,050	49.56
5,460	54.91	5,760	52.05	6,060	49.48
5,470	54.81	5,770	51.96	6,070	49.39
5,480	54.71	5,780	51.87	6,080	49.31
5,490	54.61	5,790	51.78	6,090	49.23
5,500	54.51	5,800	51.69	6,100	49.15

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
6,110	49.07	6,410	46.77	6,710	44.68
6,120	48.99	6,420	46.70	6,720	44.62
6,130	48.91	6,430	46.63	6,730	44.55
6,140	48.83	6,440	46.56	6,740	44.48
6,150	48.75	6,450	46.48	6,750	44.42
6,160	48.67	6,460	46.41	6,760	44.35
6,170	48.59	6,470	46.34	6,770	44.29
6,180	48.51	6,480	46.27	6,780	44.22
6,190	48.44	6,490	46.20	6,790	44.16
6,200	48.36	6,500	46.13	6,800	44.09
6,210	48.28	6,510	46.06	6,810	44.03
6,220	48.20	6,520	45.98	6,820	43.96
6,230	48.13	6,530	45.91	6,830	43.90
6,240	48.05	6,540	45.84	6,840	43.83
6,250	47.97	6,550	45.77	6,850	43.77
6,260	47.89	6,560	45.70	6,860	43.71
6,270	47.82	6,570	45.63	6,870	43.64
6,280	47.74	6,580	45.57	6,880	43.58
6,290	47.67	6,590	45.50	6,890	43.52
6,300	47.59	6,600	45.43	6,900	43.45
6,310	47.52	6,610	45.36	6,910	43.39
6,320	47.44	6,620	45.29	6,920	43.33
6,330	47.36	6,630	45.22	6,930	43.26
6,340	47.29	6,640	45.15	6,940	43.20
6,350	47.22	6,650	45.09	6,950	43.14
6,360	47.14	6,660	45.02	6,960	43.08
6,370	47.07	6,670	44.95	6,970	43.02
6,380	46.99	6,680	44.88	6,980	42.95
6,390	46.92	6,690	44.82	6,990	42.89
6,400	46.85	6,700	44.75	7,000	42.83

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
7,010	42.77	7,310	41.02	7,610	39.40
7,020	42.71	7,320	40.96	7,620	39.35
7,030	42.65	7,330	40.90	7,630	39.29
7,040	42.59	7,340	40.85	7,640	39.24
7,050	42.53	7,350	40.79	7,650	39.19
7,060	42.47	7,360	40.74	7,660	39.14
7,070	42.41	7,370	40.68	7,670	39.09
7,080	42.35	7,380	40.63	7,680	39.04
7,090	42.29	7,390	40.57	7,690	38.99
7,100	42.23	7,400	40.52	7,700	38.94
7,110	42.17	7,410	40.46	7,710	38.89
7,120	42.11	7,420	40.41	7,720	38.84
7,130	42.05	7,430	40.35	7,730	38.79
7,140	41.99	7,440	40.30	7,740	38.74
7,150	41.93	7,450	40.24	7,750	38.69
7,160	41.87	7,460	40.10	7,760	38.64
7,170	41.82	7,470	40.14	7,770	38.59
7,180	41.76	7,480	40.08	7,780	38.54
7,190	41.70	7,490	40.03	7,790	38.49
7,200	41.64	7,500	39.98	7,800	38.44
7,210	41.58	7,510	39.92	7,810	38.39
7,220	41.53	7,520	39.87	7,820	38.34
7,230	41.47	7,530	39.82	7,830	38.29
7,240	41.41	7,540	39.76	7,840	38.24
7,250	41.35	7,550	39.71	7,850	38.19
7,260	41.30	7,560	39.66	7,860	38.15
7,270	41.24	7,570	39.61	7,870	38.10
7,280	41.18	7,580	39.55	7,880	38.05
7,290	41.13	7,590	39.50	7,890	38.00
7,300	41.07	7,600	39.45	7,900	37.95

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
7,910	37.90	8,210	36.52	8,510	35.23
7,920	37.86	8,220	36.47	8,520	35.19
7,930	37.81	8,230	36.43	8,530	35.15
7,940	37.76	8,240	36.39	8,540	35.11
7,950	37.71	8,250	36.34	8,550	35.07
7,960	37.67	8,260	36.30	8,560	35.03
7,970	37.62	8,270	36.25	8,570	34.98
7,980	37.57	8,280	36.21	8,580	34.94
7,990	37.52	8,290	36.17	8,590	34.90
8,000	37.48	8,300	36.12	8,600	34.86
8,010	37.43	8,310	36.08	8,610	34.82
8,020	37.38	8,320	36.04	8,620	34.78
8,030	37.34	8,330	35.99	8,630	34.74
8,040	37.29	8,340	35.95	8,640	34.70
8,050	37.24	8,350	35.91	8,650	34.66
8,060	37.20	8,360	35.86	8,660	34.62
8,070	37.15	8,370	35.82	8,670	34.58
8,080	37.11	8,380	35.78	8,680	34.54
8,090	37.06	8,390	35.74	8,690	34.50
8,100	37.01	8,400	35.69	8,700	34.46
8,110	36.97	8,410	35.65	8,710	34.42
8,120	36.92	8,420	35.61	8,720	34.38
8,130	36.88	8,430	35.57	8,730	34.34
8,140	36.83	8,440	35.52	8,740	34.30
8,150	36.79	8,450	35.48	8,750	34.27
8,160	36.74	8,460	35.44	8,760	34.23
8,170	36.70	8,470	35.40	8,770	34.19
8,180	36.65	8,480	35.36	8,780	34.15
8,190	36.61	8,490	35.31	8,790	34.11
8,200	36.56	8,500	35.27	8,800	34.07

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
8,810	34.03	9,110	32.91	9,410	31.86
8,820	33.99	9,120	32.88	9,420	31.83
8,830	33.95	9,130	32.84	9,430	31.79
8,840	33.92	9,140	32.80	9,440	31.76
8,850	33.88	9,150	32.77	9,450	31.73
8,860	33.84	9,160	32.73	9,460	31.69
8,870	33.80	9,170	32.70	9,470	31.66
8,880	33.76	9,180	32.66	9,480	31.63
8,890	33.73	9,190	32.62	9,490	31.59
8,900	33.69	9,200	32.59	9,500	31.56
8,910	33.65	9,210	32.55	9,510	31.53
8,920	33.61	9,220	32.52	9,520	31.49
8,930	33.57	9,230	32.48	9,530	31.46
8,940	33.54	9,240	32.45	9,540	31.43
8,950	33.50	9,250	32.41	9,550	31.39
8,960	33.46	9,260	32.38	9,560	31.36
8,970	33.42	9,270	32.34	9,570	31.33
8,980	33.39	9,280	32.31	9,580	31.30
8,990	33.35	9,290	32.27	9,590	31.26
9,000	33.31	9,300	32.24	9,600	31.23
9,010	33.28	9,310	32.20	9,610	31.20
9,020	33.24	9,320	32.17	9,620	31.17
9,030	33.20	9,330	32.14	9,630	31.13
9,040	33.17	9,340	32.10	9,640	31.10
9,050	33.13	9,350	32.07	9,650	31.07
9,060	33.09	9,360	32.03	9,660	31.04
9,070	33.06	9,370	32.00	9,670	31.01
9,080	33.02	9,380	31.96	9,680	30.97
9,090	32.98	9,390	31.93	9,690	30.94
9,100	32.95	9,400	31.90	9,700	30.91

Table 28-2. Kilohertz (kHz) to Meters (m) or Meters to Kilohertz (cont'd)

kHz	m	kHz	m	kHz	m
9,710	30.88	9,810	30.56	9,910	30.25
9,720	30.85	9,820	30.53	9,920	30.22
9,730	30.81	9,830	30.50	9,930	30.19
9,740	30.78	9,840	30.47	9,940	30.16
9,750	30.75	9,850	30.44	9,950	30.13
9,760	30.72	9,860	30.41	9,960	30.10
9,770	30.69	9,870	30.38	9,970	30.07
9,780	30.66	9,880	30.35	9,980	30.04
9,790	30.63	9,890	30.32	9,990	30.01
9,800	30.59	9,900	30.28	10,000	29.98

□Example:

One of the bands of a short-wave receiver covers the range from 3000 kHz to 5000 kHz. What wavelength range does this include?

Table 28-2 shows that 3000 kHz corresponds to 99.94 meters and that 5000 kHz corresponds to 59.96 meters. Thus, this particular band is from approximately 60 to 100 meters.

□Example:

What is the length, in feet, of a wave having a frequency of 4280 kilohertz?

Locate this frequency (4280 kHz) in the kHz column. You will note it corresponds to a wavelength of 70.05 meters. However, the problem calls for the answer in feet. Consult Table 28-3 and you will see that 70 meters is 229.66 feet.

### CONVERSION—METERS TO FEET

The distance from the start to the finish of a single cycle of a wave, called the wavelength, is usually specified in meters. Table 28-3 supplies data on the conversion of meters to feet. The Table can easily be extended by moving the decimal point. Move the decimal point an equal number of places in the same direction in both columns. Thus, a wavelength of 18 meters corresponds to 59.055 feet. And 180 meters corresponds to 590.4 feet, etc. Use Table 28-4 for converting feet to meters.

□Example:

What is the length, in feet, of a wave that is 36 meters long? Table 28-3 shows that 36m equals 118.08 ft. (36 x 3.28.)

Example:

What is the frequency of a wave whose wavelength is 20 feet?

Table 28-3 shows 19.68 feet equals 6 meters. For greater accuracy, using Table 28-4 (1 foot equals 0.3048006 meter), 20 ft. x 0.3048 equals 6.096 meters. Table 28-2 shows 6 meters equals 49,970 kHz. For greater accuracy, use the formula

$$f = 299,820,000/\lambda$$

$$= \frac{299,820,000}{6.09}$$

$$= 49,231,527 \text{ Hz}$$

$$= 49,231 \text{ kHz}$$

The conversion factor in Table 28-3 is based on 1 meter = 3.2808 feet.

Table 28-3. Meters to Feet

Meters	Feet	Meters	Feet	Meters	Feet	Meters	Feet
1	3.2808	26	85.302	51	167.32	76	249.34
2	6.5617	27	88.583	52	170.60	75	256.62
3	9.8425	28	91.863	53	173.88	78	255.90
4	13.123	29	95.144	54	177.16	79	259.19
5	16.404	30	98.425	55	180.45	80	262.47
6	19.685	31	101.71	56	183.73	81	265.75
7	22.966	32	104.99	57	187.01	82	269.03
8	26.247	33	108.27	58	190.29	83	272.31
9	29.527	34	111.55	59	193.57	84	275.59
10	32.808	35	114.83	60	196.85	85	278.87
11	36.089	36	118.11	61	200.13	66	282.15
12	39.370	37	121.39	62	203.41	87	285.43
13	42.651	38	124.67	63	206.69	88	288.71
14	45.932	39	127.95	64	209.97	89	291.99
15	49.212	40	131.23	65	213.25	90	295.27
16	52.493	41	134.51	66	216.53	91	298.56
17	55.774	42	137.80	67	219.82	92	301.84
18	59.055	43	141.08	68	223.10	93	305.12
19	62.336	44	144.36	69	226.38	94	308.40
20	65.617	45	147.64	70	229.66	95	311.68
21	68.897	46	150.92	71	232.94	96	314.96
22	72.178	47	154.20	72	236.22	97	318.23
23	75.459	48	157.48	73	239.50	98	321.52
24	78.740	49	160.76	74	242.78	99	324.80
25	82.021	50	164.04	75	246.06	100	328.08

The conversion factor in Table 28-4 is based on 1 foot = 0.3048 meter.

Table 28-4. Feet to Meters

Feet	Meters	Feet	Meters	Feet	Meter	Feet	Meters
1	0.3048	26	7.9248	51	15.545	76	23.165
2	0.6096	27	8.2296	52	15.850	77	23.470
3	0.91440	28	8.5344	53	16.154	78	23.774
4	1.2192	29	8.8392	54	16.459	79	24.079
5	1.5240	30	9.1440	55	16.764	80	24.384
6	1.8288	31	9.4488	56	17.069	81	24.689
7	2.1336	32	9.7536	57	17.374	82	24.994
8	2.4384	33	10.058	58	17.678	83	25.298
9	2.7432	34	10.363	59	17.983	84	25.603
10	3.0480	35	10.668	60	18.288	85	25.908
11	3.3528	36	10.973	61	18.593	86	26.213
12	3.6576	37	11.278	62	18.898	87	26.518
13	3.9624	38	11.582	63	19.202	88	26.822
14	4.2672	39	11.887	64	19.507	89	27.127
15	4.5720	40	12.192	65	19.812	90	27.432
16	4.8768	41	12.497	66	20.117	91	27.737
17	5.1816	42	12.802	67	20.422	92	28.042
18	5.4864	43	13.106	68	20.726	93	28.346
19	5.7912	44	13.411	69	21.031	94	28.651
20	6.0960	45	13.716	70	21.336	95	28.956
21	6.4008	46	14.021	71	21.641	96	29.261
22	6.7056	47	14.326	72	21.946	97	29.566
23	7.0104	48	14.630	73	22.250	98	29.870
24	7.3152	49	14.935	74	22.555	99	30.175
25	7.6200	50	15.240	75	22.860	100	30.480

### FREQUENCY TO WAVELENGTH CONVERSION FOR VERY HIGH FREQUENCIES

At very high frequencies certain components, such as the elements of receiving or transmitting antennas, become small enough to be measured easily. Knowing the frequency at which such elements work and using data such as that contained in Table 28-5 makes it easy to convert frequency into lengths in meters or centimeters.

In Table 28-5,  $\lambda$  represents the wavelength in centimeters or meters; MHz is the frequency in megahertz.

#### □Example:

What is the frequency of a wave whose length is 10 cm?

Using Table 28-5 find the number 10 under the heading of cm. As you move to the right you will note this is also listed as 0.1 meter or one-tenth of a meter. Continue moving to the right and locate the answer in the MHz column—3000 MHz.

**□Example:**

What is the wavelength of a wave whose frequency is 25 MHz?

In the MHz column you will see 25.0. Move to the left and you will see that the corresponding wavelength is 12 meters.

Table 28-5. Wavelength to Frequency (VHF and UHF)

cm	$\frac{\lambda}{m}$	MHz	$\frac{\lambda}{m}$	MHz	$\frac{\lambda}{m}$	MHz
10	0.1	3,000	1.1	273	2.1	143
20	0.2	1,500	1.2	250	2.2	136
30	0.3	1,000	1.3	231	2.3	130
40	0.4	750	1.4	214	2.4	125
50	0.5	600	1.5	200	2.5	120
60	0.6	500	1.6	188	2.6	115
70	0.7	429	1.7	176	2.7	111
80	0.8	375	1.8	167	2.8	107
90	0.9	333	1.9	158	2.9	103
	1.0	300	2.0	150	3.0	100
$\frac{\lambda}{m}$	MHz	$\frac{\lambda}{m}$	MHz	$\frac{\lambda}{m}$	MHz	
3.1	96.8	6.1	49.2	9.1	33.0	
3.2	93.8	6.2	48.4	9.2	32.6	
3.3	90.9	6.3	47.6	9.3	32.3	
3.4	88.2	6.4	46.9	9.4	31.9	
3.5	85.7	6.5	46.2	9.5	31.6	
3.6	83.3	6.6	45.5	9.6	31.3	
3.7	81.1	6.7	44.8	9.7	30.9	
3.8	78.9	6.8	44.1	9.8	30.6	
3.9	76.9	6.9	43.5	9.9	30.3	
4.0	75.0	7.0	42.9	10.0	30.0	
4.1	73.2	7.1	42.3	10.1	29.7	
4.2	71.4	7.2	41.7	10.2	29.4	
4.3	69.8	7.3	41.1	10.3	29.1	
4.4	68.2	7.4	40.5	10.4	28.8	
4.5	66.7	7.5	40.0	10.5	28.6	

Table 28-5. Wavelength to Frequency (VHF and UHF) (cont'd)

$\frac{\lambda}{m}$	MHz	$\frac{\lambda}{m}$	MHz	$\frac{\lambda}{m}$	MHz
4.6	65.2	7.6	39.5	10.6	28.3
4.7	63.8	7.7	39.0	10.7	28.0
4.8	62.5	7.8	38.5	10.8	27.8
4.9	61.2	7.9	38.0	10.9	27.5
5.0	60.0	8.0	37.5	11.0	27.3
5.1	58.8	8.1	37.0	11.1	27.0
5.2	57.7	8.2	36.6	11.2	26.8
5.3	56.6	8.3	36.1	11.3	26.5
5.4	55.6	8.4	35.7	11.4	26.3
5.5	54.5	8.5	35.3	11.5	26.1
5.6	53.6	8.6	34.9	11.6	25.9
5.7	52.6	8.7	34.5	11.7	25.6
5.8	51.7	8.8	34.1	11.8	25.4
5.9	50.8	8.9	33.7	11.9	25.2
6.0	50.0	9.0	33.3	12.0	25.0

### CONVERSION—INCHES TO MILLIMETERS AND MILLIMETERS TO INCHES

Table 28-6 supplies a convenient way of converting decimal inches to millimeters. Use Table 28-7 for converting millimeters to decimal inches. The range of both tables can easily be extended by moving the decimal point an equal number of places in the same direction, for both columns.

#### □Example:

What is the length in millimeters of a wave whose length is 0.280 inch?

Locate 0.280 in the inches column in Table 28-6. The answer, 7.112 millimeters, is shown in the column immediately to the right.

#### □Example:

A wave is approximately 33 millimeters long. What is its length in inches?

Locate 3.302 in the millimeters column in Table 3-6. By moving the decimal point one place to the right, you will have 33.02 millimeters. The corresponding distance in inches is 0.130, but we must move the decimal point one place to the right. The answer is 1.30 inches.

Table 28-6. Decimal Inches to Millimeters

1 inch = 25.40 millimeters					
Inches	Milli-meters	Inches	Milli-meters	Inches	Milli-meters
0.001	0.0254	0.290	7.37	0.660	16.76
0.002	0.0508	0.300	7.62	0.670	17.02
0.003	0.0762	0.310	7.87	0.680	17.27
0.004	0.1016	0.320	8.13	0.690	17.53
0.005	0.1270	0.330	8.38	0.700	17.78
0.006	0.1524	0.340	8.64	0.710	18.03
0.007	0.1778	0.350	8.89	0.720	18.29
0.008	0.2032	0.360	9.14	0.730	18.54
0.009	0.2286	0.370	9.40	0.740	18.80
0.010	0.2540	0.380	9.65	0.750	19.05
0.020	0.5080	0.390	9.91	0.760	19.30
0.030	0.7620	0.400	10.16	0.770	19.56
0.040	1.016	0.410	10.41	0.780	19.81
0.050	1.270	0.420	10.67	0.790	20.07
0.060	1.524	0.430	10.92	0.800	20.32
0.070	1.778	0.440	11.18	0.810	20.57
0.080	2.032	0.450	11.43	0.820	20.83
0.090	2.286	0.460	11.68	0.830	21.08
0.100	2.540	0.470	11.94	0.840	21.34
0.110	2.794	0.480	12.19	0.850	21.59
0.120	3.048	0.490	12.45	0.860	21.84
0.130	3.302	0.500	12.70	0.870	22.10
0.140	3.556	0.510	12.95	0.880	22.35
0.150	3.810	0.520	13.21	0.890	22.61
0.160	4.064	0.530	13.46	0.900	22.86
0.170	4.318	0.540	13.72	0.910	23.11
0.180	4.572	0.550	13.97	0.920	23.37
0.190	4.826	0.560	14.22	0.930	23.62
0.200	5.080	0.570	14.48	0.940	23.88
0.210	5.334	0.580	14.73	0.950	24.13
0.220	5.588	0.590	14.99	0.960	24.38
0.230	5.842	0.600	15.24	0.970	24.64
0.240	6.096	0.610	15.49	0.980	24.89
0.250	6.350	0.620	15.75	0.990	25.15
0.260	6.604	0.630	16.00	1.000	25.40
0.270	6.858	0.640	16.26	....	....
0.280	7.112	0.650	16.51	....	....

Table 28-7. Millimeters to Decimal Inches

millimeters	inches	millimeters	inches
1 millimeter = 0.0393700 inch			
0.01	0.0003937	0.36	0.014148
0.02	0.000786	0.37	0.014541
0.03	0.001179	0.38	0.014934
0.04	0.001572	0.39	0.015327
0.05	0.001965	0.40	0.015720
0.06	0.002358	0.41	0.016113
0.07	0.002751	0.42	0.016506
0.18	0.003144	0.43	0.016899
0.09	0.003537	0.44	0.017292
0.10	0.003937	0.45	0.017685
0.11	0.004323	0.46	0.018078
0.12	0.004716	0.47	0.018471
0.13	0.005109	0.48	0.018864
0.14	0.005502	0.49	0.019257
0.15	0.005895	0.50	0.019650
0.16	0.006288	0.51	0.020043
0.17	0.006681	0.52	0.020436
0.18	0.007074	0.53	0.020829
0.19	0.007467	0.54	0.021222
0.20	0.007860	0.55	0.021615
0.21	0.008253	0.56	0.022008
0.22	0.008646	0.57	0.022401
0.23	0.009039	0.58	0.022794
0.24	0.009432	0.59	0.023187
0.25	0.009825	0.60	0.023580
0.26	0.010218	0.61	0.023973
0.27	0.010611	0.62	0.024366
0.28	0.011004	0.63	0.024759
0.29	0.011397	0.64	0.025152
0.30	0.011790	0.65	0.0255450
0.31	0.012183	0.66	0.025938
0.32	0.012576	0.67	0.026331
0.33	0.012969	0.68	0.026724
0.34	0.013362	0.69	0.027117
0.35	0.013755	0.70	0.027510

Table 28-7. Millimeters to Decimal Inches (cont'd)

millimeters	inches	millimeters	inches
0.71	0.027903	0.86	0.033798
0.72	0.028296	0.87	0.034191
0.73	0.028689	0.88	0.034584
0.74	0.029082	0.89	0.034977
0.75	0.029475	0.90	0.035370
0.76	0.029868	0.91	0.035763
0.77	0.030261	0.92	0.036156
0.78	0.030654	0.93	0.036549
0.79	0.031047	0.94	0.036942
0.80	0.031440	0.95	0.037335
0.81	0.031833	0.96	0.039370
0.82	0.032226	0.97	0.037728
0.83	0.032619	0.98	0.038121
0.84	0.033012	0.99	0.038514
0.85	0.033405	1.00	0.038907

□Example:

A wave has a length of 0.92 millimeter. What is the corresponding length in inches?

Using Table 28-7 locate 0.92 in the millimeters column. The length in inches is 0.036156. (See also Table 3-12).

## FREQUENCY CONVERSIONS

Three common measures of frequency are used in electronics. To convert from one to the other, see Table 28-8.

Table 28-8. Frequency Conversion

Multiply by this value to get

Given This Value	Multiply by this value to get		
	hertz	kilohertz	megahertz
hertz	—	$10^{-3}$	$10^{-6}$
kilohertz	$10^3$	—	$10^{-3}$
megahertz	$10^6$	$10^3$	—

## DIELECTRIC CONSTANTS

The material placed between the plates of a capacitor is its dielectric. All dielectrics are compared to a reference, air, which has a dielectric constant ( $k$ ) of 1. The capacitance of a capacitor is directly proportional to the dielectric constant. Values of these constants are only approximate since there can be considerable variations in the qualities of the materials used as dielectrics. See Table 28-9.

Table 28-9. Dielectric Constants ( $k$ )

Dielectric Material	$k$
Air, dry	1.0
Cellulose acetate	6.0
Formica	4.6
Glass, window	4.2 to 8.0
Hard rubber	2.0
Lucite	2.5
Mica	2.5 to 6.0
Nylon	3.4 to 22.4
Paper	2.0
Polystyrene	2.5
Porcelain	5.5 to 6.0
Pure water	81.0
Pyrex	4.5
Quartz	5.0
Rubber	2.0 to 3.0
Teflon	2.1
Varnished cambric	4.0

## CAPACITANCE CONVERSIONS

Electronic formulas involving capacitance sometimes require changing capacitance units to some multiple or submultiple. Table 28-10 supplies the multiplication factors for making these conversions.

Table 28-10. Capacitance Conversions

Given This Value	Multiply by this value to get		
	farads	microfarads	picofarads
farads	—	$10^6$	$10^{12}$
microfarads	$10^{-6}$	—	$10^6$
picofarads	$10^{-12}$	$10^{-6}$	—

## MEASURING SYSTEMS

Two measuring systems are in common use—the English and the metric. The advantage of the metric system is that it is decimal, and so it is easy to move from basic metric units to multiples or submultiples. The meter and the gram are bases for the metric system. Commonly used abbreviations are m for meters, mm for millimeters, cm for centimeters, dm for decimeters, dkm for decameters, hm for hectometers, km for kilometers, and mym for myriameters. The micron is represented by  $\mu$  (Greek letter mu). Table 28-11 shows the relationships between English measure and metric equivalents.

Table 28-11. English Units to Metric Units

1 micron	=	0.001 millimeter
1 micron	=	0.000001 meter
1 millimeter	=	0.0393700 inch
1 millimeter	=	0.00328 foot
1 centimeter	=	10 millimeters
1 centimeter	=	0.393700 inch
1 centimeter	=	0.032808 foot
1 centimeter	=	0.01093611 yard
1 meter	=	39.3700 inches
1 meter	=	3.280833333 feet
1 meter	=	1.09361 yards
1 decimeter	=	10 centimeters
1 decimeter	=	3.937 inches
1 meter	=	10 decimeters
1 meter	=	100 centimeters
1 meter	=	1,000 millimeters
1 decameter	=	10 meters
1 decameter	=	393.7 inches
1 hectometer	=	10 decameters
1 hectometer	=	328 feet, 1 inch
1 kilometer	=	10 hectometers
1 kilometer	=	0.62137 mile
1 myriameter	=	10 kilometers
1 myriameter	=	6.2137 miles
1 inch	=	25.40005 millimeters
1 inch	=	2.540005 centimeters
1 inch	=	0.02540005 meter
1 foot	=	304.8006 millimeters
1 foot	=	30.48006 centimeters

Table 28-11. English Units of Measure and Metric Equivalents (cont'd)

1 foot	= 0.3048006 meter
1 yard	= 0.9144 meter
1 mile	= 1.609 kilometers

### AREA

1 sq. inch	= 6.452 sq. cm.
1 sq. foot	= 0.0929 sq. meter
1 sq. yard	= 0.84 sq. meter
1 sq. mile	= 2.589 sq. kilometers
1 sq. millimeter	= 0.00155 sq. in.
1 sq. centimeter	= 0.1550 sq. in.
1 sq. meter	= 1.196 sq. yd.
1 sq. kilometer	= 0.3861 sq. mi.

### VOLUME

1 cu. in.	= 16.3872 cu. centimeters
1 cu. ft.	= 0.02832 cu. meter
1 cu. yd.	= 0.7646 cu. meter
1 liquid qt.	= 0.9464 liter
1 liquid gal.	= 3.785 liters
1 dry qt.	= 1.101 liters
1 cu. centimeter	= 0.06102 cu. in.
1 cubic meter	= 1.308 cu. yds.
1 milliliter	= 0.03381 liq. oz.
1 liter	= 1.057 liq. qts.
1 liter	= 0.9081 dry qt.

### WEIGHT

1 grain	= 0.0648 gram
1 oz. (avoird.)	= 28.35 grams
1 oz. (troy)	= 31.10 grains
1 lb. (avoird.)	= 0.4536 kilogram
1 lb. (troy)	= 0.3732 kilogram
1 ton (short)	= 0.9072 metric ton
1 gram	= 15.43 grains (troy)
1 gram	= 0.03215 oz. (troy)
1 gram	= 0.03527 oz. (avoird.)
1 kilog.	= 2.205 lbs. (avoird.)
1 kilog.	= 2.679 lbs. (troy)
1 metric ton	= 1.102 tons (short)

## PROPER (COMMON) FRACTIONS AND MILLIMETRIC EQUIVALENTS

Fractions are the usual form when measurements are made with a foot rule or yardstick. Table 28-12 shows the metric equivalents in millimeters and also decimal equivalents for fractions of an inch, from 1/64 inch to 1 inch, in 1/64-inch steps.

When the conversion involves a whole number plus a fraction, use a factor of 25.40005 millimeters for each inch. Based on Table 28-11. See also Table 28-6.

### □Example:

Convert 2-17/64 inches to millimeters.

Two inches equals  $2 \times 25.40005$  millimeters, or 50.8001 millimeters. Table 28-12 shows that 17/64 inch equals 6.746875 millimeters. 50.8001 millimeters + 6.746875 millimeters equals 57.546975 mm.

Table 28-12. Fractional and Decimal Inches and Millimeter Equivalents

(1 inch = 25.40005 millimeters)

FRACTION	INCHES	DECIMAL	MILLIMETERS
1/64		0.015625	0.396875
1/32		0.031250	0.793750
3/64		0.046875	1.190625
1/16		0.062500	1.587500
5/64		0.078125	1.984375
3/32		0.093750	2.381250
7/64		0.109375	2.778125
1/8		0.125000	3.175000
9/64		0.140625	3.571875
5/32		0.156250	3.968750
11/64		0.171875	4.365625
3/16		0.187500	4.762500
13/64		0.203125	5.159375
7/32		0.218750	5.556250
15/64		0.234375	5.953125
1/4		0.250000	6.350000
17/64		0.265625	6.746875
9/32		0.281250	7.143750
19/64		0.296875	7.540625
5/16		0.312500	7.937500
21/64		0.328125	8.334375
11/32		0.343750	8.731250

Table 28-12. Fractional and Decimal Inches and Millimeter Equivalents (cont'd)  
 (1 inch = 25.40005 millimeters)

FRACTION	INCHES	MILLIMETERS
	DECIMAL	
23/64	0.359375	9.128125
3/8	0.375000	9.525000
25/64	0.390625	9.921875
13/32	0.406250	10.318750
27/64	0.421875	10.715625
7/16	0.437500	11.112500
29/64	0.453125	11.509375
15/32	0.468750	11.906250
31/64	0.484375	12.303125
1/2	0.500000	12.700000
33/64	0.515625	13.096875
17/32	0.531250	13.493750
35/64	0.546875	13.890625
9/16	0.562500	14.287500
37/64	0.578125	14.684375
19/32	0.593750	15.081250
39/64	0.609375	15.478125
5/8	0.625000	15.875000
41/64	0.640625	16.271875
21/32	0.656250	16.668750
43/64	0.671875	17.065625
11/16	0.687500	17.462500
45/64	0.703125	17.859375
23/32	0.718750	18.256250
47/64	0.734375	18.653125
3/4	0.750000	19.050000
49/64	0.765625	19.446875
25/32	0.781250	19.843750
51/64	0.796875	20.240625
13/16	0.812500	20.637500
53/64	0.828125	21.034375
27/32	0.843750	21.431250
55/64	0.859375	21.828125
7/8	0.875000	22.225000
57/64	0.890625	22.621875
29/32	0.906250	23.018750
59/64	0.921875	23.415625
15/16	0.937500	23.812500
61/64	0.953125	24.209375
31/32	0.968750	24.606250
63/64	0.984375	25.003125
1	1.000000	25.400050

## TEMPERATURE CONVERSIONS

Components used in electronics, including wire, can have a positive temperature coefficient, with resistance increasing as temperature rises, or a negative temperature coefficient, with resistance varying inversely with temperature. Some components are specifically designed to have a zero temperature coefficient, with resistance not affected by temperature changes.

While resistance is often specified in degrees Fahrenheit, the use of the Celsius temperature scale (formerly known as Centigrade) is becoming more acceptable in electrical and electronic applications. The following tables aren't complete for all possible values of F degrees and C degrees but are intended for the more common values encountered in electrical and electronic applications.

Tables 28-13 and 28-14 are based on the formulas:  $C = (F - 32) \times 5/9$  and  $F = (C \times 9/5) + 32$ .

All Celsius and Fahrenheit temperatures in Table 28-13 and Table 28-14 are plus unless otherwise indicated.

Table 28-13. Degrees Celsius to Degrees Fahrenheit

C degrees	F degrees	C degrees	F degrees	C degrees	F degrees
-100	-148	5	41	105	221
-95	-139	10	50	110	230
-90	-130	15	59	115	239
-85	-121	20	68	120	248
-80	-112	25	77	125	257
-75	-103	30	86	130	266
-70	-94	35	93	135	275
-65	-85	40	104	140	284
-60	-76	45	113	145	293
-55	-67	50	122	150	302
-50	-58				
-45	-49	55	131	155	311
-40	-40	60	140	160	320
-35	-31	65	149	165	329
-30	-22	70	158	170	338
-25	-13	75	167	175	347
-20	-4	80	176	180	356
-15	5	85	185	185	365
-10	14	90	194	190	374
-5	23	95	203	195	383
0	32	100	212	200	392

Table 28-14. Degrees Fahrenheit to Degrees Celsius

F degrees	C degrees	F degrees	C degrees
-100	-73	90	32
-90	-68	95	35
-80	-62	100	38
-70	-57	105	41
-60	-51	110	43
-50	-46	115	46
-40	-40	120	49
-30	-34	125	52
-20	-29	130	54
-10	-23	135	57
-5	-21	140	60
0	-18	145	63
5	-15	150	66
10	-12	155	68
		160	71
15	-9	165	74
20	-7	170	77
25	-4	175	79
30	-1	180	82
35	1.7	185	85
40	4	190	88
45	7	195	91
50	10	200	93
55	13		
60	16		
65	18		
70	21		
75	24		
80	27		
85	29		

## ELECTRONIC UNITS

Formulas in electronics use basic units—units such as the volt, ohm, ampere, farad, and henry. However, problems invariably supply information in terms of multiples or submultiples of these units. Thus, before any solution can be attempted, it is often necessary to convert multiples or submultiples to basic units.

Quite frequently the numbers used in formulas will be very large whole numbers or large decimals. In either case, it is highly advantageous to be able to use powers of ten and to be familiar with the rules for dividing and multiplying numbers using exponents. Table 28-15 shows the method of expressing small and large numbers using powers of ten.

Table 28-15. Powers of 10

$10^0 = 1$	$10^0 = 1$
$10^1 = 10$	$10^{-1} = .1$
$10^2 = 100$	$10^{-2} = .01$
$10^3 = 1,000$	$10^{-3} = .001$
$10^4 = 10,000$	$10^{-4} = .0001$
$10^5 = 100,000$	$10^{-5} = .00001$
$10^6 = 1,000,000$	$10^{-6} = .000001$
$10^7 = 10,000,000$	$10^{-7} = .0000001$
$10^8 = 100,000,000$	$10^{-8} = .00000001$
$10^9 = 1,000,000,000$	$10^{-9} = .000000001$
$10^{10} = 10,000,000,000$	$10^{-10} = .0000000001$
$10^{11} = 100,000,000,000$	$10^{-11} = .00000000001$
$10^{12} = 1,000,000,000,000$	$10^{-12} = .000000000001$

### SYMBOLS AND PREFIXES FOR POWERS OF 10

Numbers have names. The prefixes given in Table 28-16 are helpful in identifying particular values of powers of 10. Thus, a gigahertz (prefix giga) corresponds to  $10^9$ .

Table 28-16. Powers of 10, Symbols, and Prefixes

Power of ten	Prefix	Symbol
$10^{-12}$	tera	T
$10^{-9}$	giga	G
$10^{-6}$	mega	M
$10^{-3}$	kilo	k
$10^2$	hecto or hekto	h
$10^1$	deka	dk
$10^{-1}$	deci	d
$10^{-2}$	centi	c
$10^{-3}$	milli	m
$10^{-6}$	micro	$\mu$
$10^{-9}$	nano	n
$10^{-12}$	pico (micromicro)	p
$10^{-15}$	femto	f
$10^{-18}$	atto	a

Table 28-17 supplies data on the conversion of electronic units from one form to another. Most of the conversion factors are supplied as powers of 10.

Table 28-17. Electronic Units

Multiply	By	To Convert To
ampere turns	1.257	gilberts
amperes	$10^{12}$	micromicroampères
amperes	$10^6$	microampères
amperes	$10^3$	milliamperes
centimeters	10	millimeters
degrees	60	minutes
farads	$10^{12}$	picoфarads (micromicrofarads)
farads	$10^6$	microfarads
farads	$10^3$	millifarads
gauss	1	lines per square centimeter
gauss	6.452	lines per square inch
henrys	$10^6$	microhenrys
henrys	$10^3$	millihenrys
Hertz	$10^{-6}$	megahertz
Hertz	$10^{-3}$	kilohertz
Hertz	$10^9$	gigahertz (kilomegahertz)
horsepower	.7457	kilowatts
horsepower	745.7	watts
joules	1	watt-seconds
joules	10	
kilohertz	$10^3$	hertz
kilohertz	$10^{-3}$	megahertz
kilohertz	$10^6$	gigahertz
kilovolt-amperes	$10^3$	volt-amperes
kilovolts	$10^3$	volts
kilowatt-hours	$3.6 \times 10^6$	joules
kilowatts	$10^3$	watts
kilowatts	1.341	horsepower
lines per square centimeter	1	gausses
lines per square centimeter	6.452	lines per square inch
megahertz	$10^6$	hertz
megahertz	$10^3$	kilohertz

Table 28-17. Electronic Units (cont'd)

Multiply	By	To Convert To
megawatts	$10^{-6}$	watts
megahms	$10^6$	ohms
meters	$10^2$	centimeters
meters	3.281	feet
meters	39.37	inches
meters	$10^3$	millimeters
mhos	$10^6$	micramhos
mhos	$10^3$	millimhos
micraamperes	$10^{-6}$	amperes
micraamperes	$10^{-3}$	milliamperes
microfarads	$10^{-6}$	farads
microfarads	$10^6$	picafarads (micramicrofarads)
micrahrenrys	$10^{-6}$	henrys
micrahrenrys	$10^{-3}$	millihenrys
micromhos	$10^{-6}$	mhos
micramicraamperes	$10^6$	micraamperes
micromicrofarads (picofarads)	$10^{-12}$	farads
micramicra-ahms	$10^{-12}$	ahms
micravolts	$10^{-3}$	millivolts
micravolts	$10^{-6}$	volts
micrawatts	$10^{-6}$	watts
micrawatts	$10^{-3}$	milliwatts
milliamperes	$10^{-3}$	amperes
milliamperes	$10^3$	micraamperes
millihenrys	$10^{-3}$	henrys
millimeters	$10^{-3}$	meters
millimeters	$10^{-1}$	centimeters
millimhos	$10^{-3}$	mhos
millivolts	$10^{-3}$	volts
millivolts	$10^3$	microvolts
millivolts	$10^{-6}$	kilivolts
milliwatts	$10^{-3}$	watts
milliwatts	$10^3$	micrawatts
milliwatts	$10^{-9}$	megawatts
mils	$10^{-3}$	inches
minutes	60	seconds
minutes	1/60	degrees

Table 28-17. Electronic Units (cont'd)

Multiply	By	To Convert To
ohms	$10^{-3}$	kilohms
ohms	$10^{-6}$	megohms
picofarads		
radians	57.3	degrees
seconds	1/3600	degrees
seconds	$10^3$	milliseconds
seconds	$10^6$	microseconds
seconds	1/60	minutes
square centimeters	$1,973 \times 10^2$	circular mils
square inches	$1,273 \times 10^3$	circular mils
square mils	1.273	circular mils
volt-amperes	1/1,000	kilovolt-amperes
volts	$10^6$	microvolts
volts	$10^3$	millivolts
volts	$10^{-3}$	kilovolts
watt-hours	$36 \times 10^2$	joules
watt-seconds	1	joules
watts	$10^6$	microwatts
watts	$10^3$	milliwatts
watts	$10^{-3}$	kilowatts
watts	$10^{-6}$	megawatts

While it is more convenient to handle electronic conversions using powers of 10, such conversions can also be made using whole numbers. Table 28-18 shows the conversion relationships for current, resistance, voltage, power, capacitance inductance, and frequency.

Table 28-18. Electronic Unit Multiples and Submultiples

**CURRENT**

Microamperes	milliamperes $\times 1,000$
Microamperes	amperes $\times 1,000,000$
Milliamperes	amperes $\times 1,000$
Milliamperes	microamperes/1,000
Ampères	microamperes/1,000,000
Ampères	milliamperes/1,000

**RESISTANCE**

Ohms	kilohms $\times 1,000$
Ohms	megohms $\times 1,000,000$
Kilohms	ohms $/ 1,000$
Kilohms	megohms $\times 1,000$
Megohms	ohms $/ 1,000,000$
Megohms	kilohms $/ 1,000$

**Table 28-18. Electronic Unit Multiples and Submultiples (cont'd)**

**VOLTAGE**

Volts      kilovolts  $\times 1,000$   
Volts      megavolts  $\times 1,000,000$   
Kilivolts    volts/1,000  
Kilivolts    megavolts  $\times 1,000$   
Megavolts   volts/1,000,000  
Megavolts   kilovolts/1,000  
Millivolts   volts  $\times 1,000$   
Millivolts   microvolts/1,000  
Microvolts   volts  $\times 1,000,000$   
Microvolts   millivolts  $\times 1,000$

**POWER**

Watts = milliwatts/1,000  
Watts = microwatts/1,000,000  
Watts = kilowatts  $\times 1,000$   
Watts = megawatts  $\times 1,000,000$   
Kilowatts = watts/1,000  
Kilowatts = megawatts  $\times 1,000$   
Megawatts = kilowatts/1,000  
Megawatts = watts/1,000,000  
Milliwatts = watts  $\times 1,000$   
Milliwatts = microwatts/1,000  
Microwatts = milliwatts  $\times 1,000$   
Microwatts = watts  $\times 1,000,000$

**CAPACITANCE**

Microfarads = farads  $\times 1,000,000$   
Picofarads = farads  $\times 1,000,000,000,000$   
Microfarads = picofarads/1,000,000  
Picofarads = microfarads  $\times 1,000,000$   
Farads = microfarads/1,000,000  
Farads = picofarads/1,000,000,000,000

**INDUCTANCE**

Microhenrys = henrys  $\times 1,000,000$   
Microhenrys = millihenrys  $\times 1,000$   
Millihenrys = henrys  $\times 1,000$   
Millihenrys = microhenrys/1,000  
Henrys = millihenrys/1,000  
Henrys = microhenrys/1,000,000

**FREQUENCY**

Hertz (Hz) = cycles per second (cps)  
Hertz = millihertz  $\times 1,000$   
Hertz = megahertz  $\times 1,000,000$   
Millihertz = hertz/1,000  
Millihertz = megahertz  $\times 1,000$   
Megahertz = hertz/1,000,000  
Megahertz = millihertz/1,000

Table 28-19. Conversion factors for electronic multiples and submultiples.

TO CONVERT THESE TO THESE, MULTIPLY BY THE FIGURES BELOW  
 → Pico— → Pico—

Name—	Micr—	Milli—	Centi—	Deci—	Units	Deka—	Hecto—	Kilo—	Myria—	Meg—a—	Giga—	Tera—
Pico—	0.001	$10^{-4}$	$10^{-3}$	$10^{-2}$	$10^{-11}$	$10^{-12}$	$10^{-13}$	$10^{-14}$	$10^{-15}$	$10^{-16}$	$10^{-17}$	$10^{-18}$
Nano—	1000	0.001	$10^{-4}$	$10^{-3}$	$10^{-2}$	$10^{-9}$	$10^{-10}$	$10^{-11}$	$10^{-12}$	$10^{-13}$	$10^{-14}$	$10^{-15}$
Micro—	$10^6$	1000	0.001	0.0001	$10^{-3}$	$10^{-4}$	$10^{-7}$	$10^4$	$10^9$	$10^{10}$	$10^{13}$	$10^{16}$
Milli—	$10^6$	1000	0.1	0.01	0.001	0.0001	$10^{-3}$	$10^{-4}$	$10^{-7}$	$10^{-8}$	$10^{-11}$	$10^{-15}$
Centi—	$10^{10}$	10,000	10	0.1	0.01	0.001	0.0001	$10^{-1}$	$10^{-4}$	$10^{-6}$	$10^{-11}$	$10^{-14}$
Deci—	$10^{11}$	$10^4$	$10^3$	100	10	0.1	0.01	0.001	0.0001	$10^{-2}$	$10^{-7}$	$10^{-10}$
Units	$10^{12}$	$10^6$	$10^3$	1000	100	10	0.1	0.01	0.001	0.0001	$10^{-4}$	$10^{-12}$
Deka—	$10^{13}$	$10^6$	$10^7$	10,000	1000	100	10	0.1	0.001	0.0001	$10^{-1}$	$10^{-11}$
Hecto—	$10^{14}$	$10^7$	$10^8$	100,000	10,000	1000	100	10	0.1	0.001	0.0001	$10^{-1}$
Kilo—	$10^{15}$	$10^{12}$	$10^9$	10 <sup>3</sup>	10,000	1000	100	10	0.1	0.001	0.0001	$10^{-4}$
Myria—	$10^{16}$	$10^{13}$	$10^9$	$10^7$	$10^6$	10,000	1000	100	10	0.01	0.0001	$10^{-10}$
Meg—a—	$10^{18}$	$10^{13}$	$10^{12}$	$10^9$	$10^8$	$10^9$	$10^9$	10 <sup>3</sup>	10,000	1000	100	$10^{-4}$
Giga—	$10^{21}$	$10^{14}$	$10^{13}$	$10^{12}$	$10^{11}$	$10^9$	$10^9$	$10^7$	$10^6$	10 <sup>3</sup>	1000	0.001
Tera—	$10^{24}$	$10^{14}$	$10^4$	$10^{13}$	$10^4$	$10^3$	$10^2$	$10^1$	$10^0$	$10^4$	$10^6$	1000

Table 28-20. Physical Conversion Factors.

To Change			To Change Back		
Units	Multiplied by	Yields	Units	Multiplied by	Yields
<b>LENGTH</b>			<b>LENGTH</b>		
Mils	.0254	Mm.	Mm.	39.37	Mils
Mils	.001	In.	In.	1,000.	Mils
Mm.	.03937	In.	In.	25.4	Mm.
Cm.	.3937	In.	In.	2.54	Cm.
Cm.	.03281	Ft.	Ft.	30.48	Cm.
In.	.0254	M.	M.	39.37	In.
Ft.	.3048	M.	M.	3.2808	Ft.
Yds.	.9144	M.	M.	1.0936	Yds.
Kilometer	.6214	Miles	Miles	1.6093	Kilometer
<b>AREA</b>			<b>AREA</b>		
Cir. Mils	.0000007854	Sq. In.	Sq. In.	1,273,240.	Cir. Mils
Cir. Mils	.7854	Sq. Mils	Sq. Mils	1.2732	Cir. Mils
Cir. Mils	.0005066	Sq. Mm.	Sq. Mm.	1,973.51	Cir. Mils
Sq. Mm.	.00155	Sq. In.	Sq. In.	645.16	Sq. Mm.
Sq. Mils	.000001	Sq. In.	Sq. In.	1,000,000.	Sq. Mils
Sq. Cm.	.155	Sq. In.	Sq. In.	6,4516	Sq. Cm.
Sq. Ft.	.0929	Sq. M.	Sq. M.	10.764	Sq. Ft.
<b>VOLUME</b>			<b>VOLUME</b>		
Cu. In.	.01639	Liters	Liters	61.023	Cu. In.
Cu. In.	.004329	Gals.	Gals.	231.	Cu. In.
Liters	.26417	Gals.	Gals.	3.7854	Liters
Cu. Cm.	.06102	Cu. In.	Cu. In.	16.387	Cu. Cm.
Cu. Cm.	.000264	Gal.	Gal.	3,785.4	Cu. Cm.
<b>POWER</b>			<b>POWER</b>		
Ft.-Lbs. per Min.	.0000303	H.P.	H.P.	33,000.	Ft.-Lbs. per Min.
Ft.-Lbs. per Sec.	.001818	H.P.	H.P.	550.	Ft. Lbs. per Min.
Ft.-Lbs. per Min.	.0226	Watts	Watts	44.25	Ft. Lbs. per Min.
Ft.-Lbs. per Sec.	1.356	Watts	Watts	.7373	Ft.-Lbs. per Sec.
Watts	.001341	H.P.	H.P.	746.	Watts
B.T.U. per Hr.	.000393	H.P.	H.P.	2,545.	B.T.U. per Hr.

Table 28-20. Physical Conversion Factors (cont'd.).

To Change		ENERGY		To Change Back	
Multiply	by	To Get	Multiply	by	To Get
Ergs	.0000001	Joules	Joules	10,000,000.	Ergs
Joules	.2388	Gram-Calories	Gram-Calories	4.186	Joules
Joules	.10198	Kg.-M.	Kg.-M.	9.8117	Joules
Joules	.7375	Ft.-Lbs.	Ft.-Lbs.	1.356	Joules
Ft.-Lbs.	.1383	Kg.-M.	Kg.-M.	7.233	Ft.-Lbs.
Gram-Calories	.003968	B.T.U.	B.T.U.	252.	Gram-Calories
Joules	.000947	B.T.U.	B.T.U.	1,055.	Joules
Ft.-Lbs.	.001285	B.T.U.	B.T.U.	778.	Ft.-Lbs.
B.T.U.	.293	Watt-Hrs.	Watt-Hrs.	3.416	B.T.U.

WEIGHTS		WEIGHTS	
Lbs. (Avdp.)	.4536	Kgs.	Kgs.
Oz. (Avdp.)	.0625	Lbs. (Avdp.)	Lbs. (Avdp.)
Oz. (Troy)	.0833	Lbs. (Troy)	Lbs. (Troy)
Oz. (Avdp.)	.9115	Oz. (Troy)	Oz. (Troy)
Lbs. (Troy)	.82286	Lbs. (Avdp.)	Lbs. (Avdp.)
Oz. (Avdp.)	.0759	Lbs. (Troy)	Lbs. (Troy)
Oz. (Troy)	.0686	Lbs. (Avdp.)	Lbs. (Avdp.)
Grains	.00209	Oz. (Troy)	Oz. (Troy)
Grains	.002285	Oz. (Avdp.)	Oz. (Avdp.)
Milligrams	.005	Carats	Carats

MISCELLANEOUS		MISCELLANEOUS	
Ohms per		Ohms per	Ohms per
Ft.	.3048	Meter	Meter
Ohms per		Ohms per	Ohms per
Kilometer	.3048	1000 Ft.	1000 Ft.
Ohms per		Ohms per	Ohms per
Kilometer	9144	1000 Yds.	1000 Yds.
Kg. per		Lbs. per	Lbs. per
Kilometer	.6719	1000 Ft.	1000 Ft.
Lbs. per		Kg. per	Kg. per
1000 Yds.	4960	Kilometer	Kilometer



## Chapter 29

# Numbers

### BINARY NUMBER SYSTEM

The decimal system using digits ranging from 0 through 9 for all number applications is just one of a large array of number systems. Other number systems (including the decimal) such as the binary and hexadecimal, find applications in computer technology.

The binary system uses two digits: 0 and 1. As in the case of the decimal system, the value of the number depends on its horizontal position. Thus, in a decimal number such as 875, the digit 8 has a true value of 800, 7 has a value of 70 and 5 has a value of 5;  $800 + 70 + 5$  equals 875. The binary system is based on powers of two (Table 29-3) similar to powers of 10.

Table 29-3 supplies powers of two up to  $2^{10}$  and  $2^{-6}$ . To find the value of  $2^{15}$ , as an example, move down the center column headed by the letter n, stopping at the number 15. Move to the left and the value of  $2^{15}$  is given as 32,768. To find the value of  $2^{-6}$ , move down the center or n column and stop at the number 6. Look to the right and the value of  $2^{-6}$  is supplied as 0.015625.

Binary numbers, as in the case of decimal numbers, are generally arranged horizontally. The first binary number at the right has a value of  $2^0$ , the adjacent binary a value of  $2^1$ , etc. Thus, a number such as binary 1011 would have an equivalent decimal value of:

$$(1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (1 \times 2^0)$$

$$8 + 0 + 2 + 1 \text{ equals } 11$$

Table 29-1. Numerical Prefixes

Number	Greek prefix	Latin prefix
$\frac{1}{2}$	hemi-	semi-
1	mono- or mon-	uni-
$1\frac{1}{2}$	---	sesqui-
2	di-	bi-; duo-
3	tri-	tri- or ter-
4	tetro- or tetr-	quadr- or quadr-
5	penta- or pent-	quinque- or quinqua-
6	hexa- or hex-	sexi- or sex-
7	hepto- or hept-	septi- or sept-
8	octo- or oct- or octo-	octo-
9	enneo- or enne-	nona-; novem-
10	deco- or dec-	decem-
11	hendeco- or hendec-	undeca- or undec-
12	dodeca- or dodec-	duodec-
13	trideco- or tridec-	tredec-
14	tetradeco- or tetradec-	quatuordec-
15	pentadeco- or pentadec-	quindec-
16	hexadeco- or hexadec-	sextadec-
17	heptadeco- or heptadec-	septendec-
18	octadeco- or octadec-	octadec-
19	nonadeco- or nonadec-	novemdec-
20	eicoso- or eicos-	viginti-
21	heneicoso- or heneicos-	
22	docoso- or docos-	
23	tricosa- or tricos-	
24	tetracosa- or tetracos-	
25	pentacosa- or pentacos-	
26	hexacosa- or hexacos-	
27	heptacosa- or heptocos-	
28	octacosa- or octacos-	
29	nonacosa- or nonocos-	
30	triaconta- or tricont-	triginti-
31	hentriaconta- or hentriacont-	
32	dotriaconta- or dotriacont-	
40	tetraconta- or tetrocont-	quadrigint-
50	pentaconta- or pentacont-	quinquagint-
60	hexaconta- or hexocont-	sexagint-

Hence, binary 1011 is equivalent to decimal 11. To emphasize the number system, the subscript 2 is sometimes used to identify binary numbers while 10 is used as a subscript for decimal numbers. In the example given:  $1011_2$  equals  $11_{10}$ .

Table 29-4 lists the binary equivalents of decimal numbers ranging from 0 to 100.

□Example:

What is the binary equivalent of 27?

In Table 29-4, locate 27 in the left-hand column. Move directly across to the right and the binary equivalent is 00011011. The three zeros at the left of the binary can be omitted since they add nothing to the value of the number. Accordingly, decimal 27 equals binary 11011. Binary 11011 can be set up as:

$$\begin{array}{r} 1 & 1 & 0 & 1 & 1 \\ 2^4 & + & 2^3 & + & 2^2 & + & 2^1 & + & 2^0 \\ 16 & + & 8 & + & 0 & + & 2 & + & 1 \end{array} \text{ equals } 27$$

$11011_2$  equals  $27_{10}$ . The subscripts 2 and 10 have no effect on the values of the numbers and are just used for identification.

Table 29-2. NUMERICAL DATA

1 cubic foot of water at $4^\circ \text{ C}$ (weight).....	62.43 lb
1 foot of water at $4^\circ \text{ C}$ (pressure).....	0.4335 lb/in <sup>2</sup>
Velocity of light in vacuum, c.....	$186,280 \text{ mi/sec} = 2.998 \times 10^{10} \text{ cm/sec}$
Velocity of sound in dry air at $20^\circ \text{ C}$ , 76 cm Hg.....	1127 ft/sec
Degree of longitude at equator.....	.69.173 miles
Acceleration due to gravity at sea-level, 40° Latitude, g.....	32.1578 ft/sec <sup>2</sup>
$\sqrt{g}$ .....	8.020
1 inch of mercury at $4^\circ \text{ C}$ .....	1.132 ft water = 0.4908 lb/in <sup>2</sup>
Base of natural logs e.....	2.718
1 radian.....	$180^\circ \div \pi = 57.3^\circ$
360 degrees.....	2 $\pi$ radians
$\pi$ .....	3.1416
Sine 1°.....	0.00029089
Arc 1°.....	0.01745 radian
Side of square.....	$0.707 \times (\text{diagonal of square})$

Table 29-3. Powers of Two

$2^n$	$n$	$-n$
1	0	1.0
2	1	0.5
4	2	0.25
8	3	0.125
16	4	0.062 5
32	5	0.031 25
64	6	0.015 625
128	7	0.007 812 5
256	8	0.003 906 25
512	9	0.001 953 125
1 024	10	0.000 976 562 5
2 048	11	0.000 488 281 25
4 096	12	0.000 244 140 625
8 192	13	0.000 122 070 312 5
16 384	14	0.000 061 035 156 25
32 768	15	0.000 030 517 578 125
65 536	16	0.000 015 258 789 062 5
131 072	17	0.000 007 629 394 531 25
262 144	18	0.000 003 814 697 265 625
524 288	19	0.000 001 907 348 632 812 5
1 048 576	20	0.000 000 953 674 316 406 25
2 097 152	21	0.000 000 476 837 158 203 125
4 194 304	22	0.000 000 238 418 579 101 562 5
8 388 608	23	0.000 000 119 209 289 550 781 25
16 777 216	24	0.000 000 059 604 644 775 390 625
33 554 432	25	0.000 000 029 802 322 387 695 312 5
67 108 864	26	0.000 000 014 901 161 193 847 656 25
134 217 728	27	0.000 000 007 450 580 596 923 828 125
268 435 456	28	0.000 000 003 725 290 298 461 914 062 5
536 870 912	29	0.000 000 001 862 645 149 230 957 031 25
1 073 741 824	30	0.000 000 000 931 322 574 615 478 515 625
2 147 483 648	31	0.000 000 000 465 661 287 307 739 257 812 5
4 294 967 296	32	0.000 000 000 232 830 643 653 869 628 906 25
8 589 934 592	33	0.000 000 000 116 415 321 826 934 814 453 125
17 179 869 184	34	0.000 000 000 058 207 660 913 467 407 226 562 5
34 359 738 368	35	0.000 000 000 029 103 830 456 733 703 613 281 25
68 719 476 736	36	0.000 000 000 014 551 915 228 366 851 806 640 625
137 438 953 472	37	0.000 000 000 007 275 957 614 183 425 903 320 312 5
274 877 906 944	38	0.000 000 000 003 637 978 807 091 712 951 660 156 25
549 755 813 888	39	0.000 000 000 001 818 989 403 545 856 475 830 078 125
1 099 511 627 776	40	0.000 000 000 000 909 494 701 772 928 237 915 039 062 5
2 199 023 255 552	41	0.000 000 000 000 454 747 350 886 464 118 957 519 531 25
4 398 046 511 104	42	0.000 000 000 000 227 373 675 443 232 059 478 759 765 625
8 796 093 022 208	43	0.000 000 000 000 113 686 837 721 616 029 739 379 882 812
17 592 186 044 416	44	0.000 000 000 000 056 843 418 860 808 014 869 689 941 406
35 184 372 088 832	45	0.000 000 000 000 028 421 709 430 404 007 434 844 970 703
70 368 744 177 664	46	0.000 000 000 000 014 210 854 715 202 003 717 422 485 351
140 737 488 355 328	47	0.000 000 000 000 007 105 427 357 601 001 858 711 242 675
281 474 976 710 656	48	0.000 000 000 000 003 552 713 678 800 500 929 355 621 337
562 949 953 421 312	49	0.000 000 000 000 001 776 356 839 400 250 464 677 810 668
1 125 899 906 842 624	50	0.000 000 000 000 000 888 178 419 700 125 232 338 905 334
2 251 799 813 685 248	51	0.000 000 000 000 000 444 089 209 850 062 616 169 452 667
4 503 599 627 370 496	52	0.000 000 000 000 000 222 044 604 925 031 308 084 726 333
9 007 199 254 740 992	53	0.000 000 000 000 000 111 022 302 462 515 654 042 363 166
18 014 398 509 481 984	54	0.000 000 000 000 000 055 511 151 231 257 827 021 181 583
36 028 797 018 963 968	55	0.000 000 000 000 000 027 755 575 615 628 913 510 590 791
72 057 594 037 927 936	56	0.000 000 000 000 000 013 877 787 807 814 456 755 295 395
144 115 188 075 855 872	57	0.000 000 000 000 000 006 938 893 903 907 228 377 647 697
288 230 376 151 711 744	58	0.000 000 000 000 000 003 469 446 951 953 614 188 823 848
576 460 752 303 423 488	59	0.000 000 000 000 000 001 734 723 475 976 807 094 411 924
1 152 921 504 606 846 976	60	0.000 000 000 000 000 000 867 361 737 988 403 547 205 962

Table 29-4. Decimal Integers to Pure Binaries

DEC. INTEGER	BINARY	DEC. INTEGER	BINARY	DEC. INTEGER	BINARY
00	00000000	33	00100001	67	01000011
01	00000001	34	00100010	68	01000100
02	00000010	35	00100011	69	01000101
03	00000011	36	00100100	70	01000110
04	00000100	37	00100101	71	01000111
05	00000101	38	00100110	72	01001000
06	00000110	39	00100111	73	01001001
07	00000111	40	00101000	74	01001010
08	00001000	41	00101001	75	01001011
09	00001001	42	00101010	76	01001100
10	00001010	43	00101011	77	01001101
11	00001011	44	00101100	78	01001110
12	00001100	45	00101101	79	01001111
13	00001101	46	00101110	80	01010000
14	00001110	47	00100111	81	01010001
15	00001111	48	00110000	82	01010010
16	00010000	49	00110001	83	01010011
17	00010001	50	00110010	84	01010100
18	00010010	51	00110011	85	01010101
19	00010011	52	00110100	86	01010110
20	00010100	53	00110101	87	01010111
21	00010101	54	00110110	88	01011000
22	00010110	55	00110111	89	01011001
23	00010111	56	00111000	90	01011010
24	00011000	57	00111001	91	01011011
25	00011001	58	00111010	92	01011100
26	00011010	59	00111011	93	01011101
27	00011011	60	00111100	94	01011110
28	00011100	61	00111101	95	01011111
29	00011101	62	00111110	96	01100000
30	00011110	63	00111111	97	01100001
31	00011111	64	01000000	98	01100010
32	00100000	65	01000001	99	01100011
		66	01000010	100	01100100

## BINARY-CODED DECIMALS

Binary numbers can be arranged in groups of four to correspond to decimal digits. A decimal number such as 5, for example, can be represented by binary 0101. Decimal 55 would then be 0101 0101. A setup of this kind is known as a binary-coded decimal, abbreviated as BCD. Note the difference between binary-coded decimals and pure binary numbers shown earlier in Table 29-4. A decimal number such as 82 in pure binary form would be 1010010, while decimal 82 in BCD notation would be 1000 0010.

Table 29-5 lists BCD equivalents of decimal numbers ranging from 0 to 100.

Table 29-5. Decimal to Binary-Coded Decimal (BCD) Notation

DECIMAL	BCD		DECIMAL	BCD	
00	0000	0000	27	0010	0111
01	0000	0001	28	0010	1000
02	0000	0010	29	0010	1001
03	0000	0011	30	0011	0000
04	0000	0100	31	0011	0001
05	0000	0101	32	0011	0010
06	0000	0110	33	0011	0011
07	0000	0111	34	0011	0100
08	0000	1000	35	0011	0101
09	0000	1001	36	0011	1001
10	0001	0000	37	0011	0111
11	0001	0001	38	0011	1000
12	0001	0010	39	0011	1001
13	0001	0011	40	0100	0000
14	0001	0100	41	0100	0001
15	0001	0101	42	0100	0010
16	0001	0110	43	0100	0011
17	0001	0111	44	0100	0100
18	0001	1000	45	0100	0101
19	0001	1001	46	0100	0110
20	0010	0000	47	0100	0111
21	0010	0001	48	0100	1000
22	0010	0010	49	0100	1001
23	0010	0011	50	0101	0000
24	0010	0100	51	0101	0001
25	0010	0101	52	0101	0010
26	0010	0110			

Table 29-5. Decimal to Binary-Coded Decimal (BCD) Notation (cont'd)

DECIMAL	BCD	DECIMAL	BCD
53	0101 0011	77	0111 0111
54	0101 0100	78	0111 1000
55	0101 0101	79	0111 1001
56	0101 0110	80	1000 0000
57	0101 0111	81	1000 0001
58	0101 1000	82	1000 0010
59	0101 1001	83	1000 0011
60	0110 0000	84	1000 0100
61	0110 0001	85	1000 0101
62	0110 0010	86	1000 0110
63	0110 0011	87	1000 0111
64	0110 0100	88	1000 1000
65	0110 0101	89	1000 1001
66	0110 0110	90	1001 0000
67	0110 0111	91	1001 0001
68	0110 1000	92	1001 0010
69	0110 1001	93	1001 0011
70	0111 0000	94	1001 0100
71	0111 0001	95	1001 0101
72	0111 0010	96	1001 0110
73	0111 0011	97	1001 0111
74	0111 0100	98	1001 1000
75	0111 0101	99	1001 1001
76	0111 0110	100	0001 0000

## THE HEXADECIMAL SYSTEM

This number system uses digits 0 through 9 and letters A to F for its number applications. As in the case of the binary and decimal systems, the value of a hexadecimal number depends on its horizontal position. Hexadecimal numbers are based on powers of 16, as shown in Table 29-6.

Hexadecimal numbers, as in the case of binary and decimal numbers, are usually arranged horizontally. The first hexadecimal number at the right has a value of  $16^0$ , the adjacent hexadecimal number a value of  $16^1$ , etc.

In the hexadecimal system, the letter A corresponds to decimal 10, B to decimal 11, C to 12, D to 13, E to 14, and F to 15.

Table 29-6. Powers of 16

$16^0$	=	1	$16^{-1}$	=	0.0625
$16^1$	=	16	$16^{-2}$	=	0.003906
$16^2$	=	256	$16^{-3}$	=	0.000244
$16^3$	=	4,096	$16^{-4}$	=	0.000015
$16^4$	=	65,536			
$16^5$	=	1,048,576			
$16^6$	=	16,777,216			
$16^7$	=	268,435,456			
$16^8$	=	4,294,967,296			
$16^9$	=	68,719,476,736			
$16^{10}$	=	1,099,511,627,776			

$$\begin{array}{rcc}
 & 4 & \\
 & F & \\
 = & (4 \times 16^2) + (15 \times 16^1) + (3 \times 16^0) & \\
 = & (4 \times 256) + (15 \times 16) + (3 \times 1) & \\
 = & 1,024 + 240 + 3 & \\
 & & = 1,267
 \end{array}$$

Hexadecimal 4F3 equals decimal 1267.

Table 29-7 lists hexadecimal equivalents for decimal numbers from 0 to 100.

Table 29-7. Decimal to Hexadecimal Conversions

DECIMAL	HEXADECIMAL	DECIMAL	HEXADECIMAL
0	0	16	10
1	1	17	11
2	2	18	12
3	3	19	13
4	4	20	14
5	5	21	15
6	6	22	16
7	7	23	17
8	8	24	18
9	9	25	19
10	A	26	1A
11	B	27	1B
12	C	28	1C
13	D	29	1D
14	E	30	1E
15	F	31	1F

Table 29-7. Decimal to Hexadecimal Conversions (cont'd)

**DECIMAL HEXADECIMAL DECIMAL HEXADECIMAL**

32	20	69	45
33	21	70	46
34	22	71	47
35	23	72	48
36	24	73	49
37	25	74	4A
38	26	75	4B
39	27	76	4C
40	28	77	4D
41	29	78	4E
42	2A	79	4F
43	2B	80	50
44	2C	81	51
45	2D		
46	2E	82	52
47	2F	83	53
48	30	84	54
49	31	85	55
50	32		
51	33	86	56
52	34	87	57
53	35	88	58
54	36	89	59
55	37	90	5A
56	38	91	5B
57	39	92	5C
58	3A	93	5D
59	3B	94	5E
60	3C	95	5F
61	3D	96	60
62	3E	97	61
63	3F	98	62
64	40	99	63
65	41		
66	42	100	64
67	43		
68	44		

**HEXADECIMAL TO DECIMAL CONVERSIONS**

Every hexadecimal number consists of two parts: a coefficient or multiplier and some value of 16 raised to a power. Thus, hexadecimal 5A is the same as  $(5 \times 16^1) + (10 \times 16^0)$ . In this hexadecimal number 5 is a coefficient, and so is A. (A equals decimal 10.) In a

hexadecimal number such as 234, these digits have a decimal value of  $(2 \times 16^2) + (3 \times 16^1) + (4 \times 16^0)$ . Each of the numbers, 2, 3, and 4, are coefficients which are used to multiply various powers of 16. Since 234 looks like a decimal number, it can be identified as a hexadecimal number by using the subscript 16. Hence, 234 is more correctly written as  $234_{16}$ .

Table 29-8 is a convenient way of obtaining decimal equivalents of hexadecimal numbers, but some addition is involved.

□Example:

What is the decimal equivalent of 5FA4?

In Table 29-8, the first column at the left represents all possible coefficients or multipliers.

In converting 5FA4 to a decimal number, work with each part of this hexadecimal a digit at a time, starting at the right-hand side. The first right-hand digit of 5FA4 is 4. In Table 29-8, locate the number 4 in the left-hand column. Move completely across to  $16^0$  and the value of 4 is indicated as 4.

The next number of 5FA4 to consider is A. Find A in the left-hand column of Table 29-8. Move horizontally, but stop at the second or  $16^1$  column for you are now working with the second digit of the hex number. The value of A is 160.

The third digit of 5FA4 is F in the left-hand column of Table 29-8 and move to the third column, or the  $16^2$  column. The decimal value is 3840. Finally, find the decimal equivalent of the fourth digit in 5FA4. This is the number 5. Locate 5 in the left-hand column. Move across to the right and stop in the fourth column—the  $16^3$  column. The decimal equivalent here is 20,480.

$$\begin{array}{r} 4 \\ 160 \\ 3,840 \\ 20,480 \\ \hline 24,484 \end{array}$$

Hexadecimal 5FA4 equals decimal 24484. This can also be written as  $5FA4_{16}$  equals  $24,484_{10}$ .

Table 29-10 lists powers of numbers from 1 to 100, and from the third power to the eighth power, inclusive.

Table 29-8. Hexadecimal to Decimal Integer Conversions

	$16^7$	$16^6$	$16^5$	$16^4$	$16^3$	$16^2$	$16^1$	$16^0$
	X00000000	X000000	X00000	X0000	X000	X00	X0	X
1	268,435,456	16,777,216	1,048,576	65,536	4,096	256	16	1
2	536,870,912	33,554,432	2,097,152	131,072	8,192	512	32	2
3	805,306,368	50,331,648	3,145,728	196,608	12,288	768	48	3
4	1,073,741,824	67,108,864	4,194,304	262,144	16,384	1,024	64	4
5	1,342,177,280	83,886,080	5,242,880	327,680	20,480	1,280	80	5
6	1,610,612,736	100,663,296	6,291,456	393,216	24,576	1,536	96	6
7	1,879,048,192	117,440,512	7,340,032	458,752	28,672	1,792	112	7
8	2,147,483,648	134,217,728	8,388,608	524,288	32,768	2,048	128	8
9	2,415,919,104	150,994,944	9,437,184	589,824	36,864	2,304	144	9
A	2,684,354,560	167,772,160	10,485,760	655,360	40,960	2,560	160	10
B	2,952,790,016	184,549,376	11,534,336	720,896	45,056	2,816	176	11
C	3,221,225,472	201,326,592	12,582,912	786,432	49,152	3,072	192	12
D	3,489,660,928	218,103,808	13,631,488	851,968	53,248	3,328	208	13
E	3,758,096,384	234,881,024	14,680,064	917,504	57,344	3,584	224	14
F	4,026,531,840	251,658,240	15,728,640	983,040	61,440	3,840	240	15

Table 29-9. Counting in Different Number Systems

DECIMAL	DUODECIMAL	OCTAL	BINARY
t	t	e	s
o	w	i	x
e	e	g	e
n	l	h	t
e	l	o	o
s	e	n	ne
s	s	s	s
0	0	0	0
1	1	1	1
2	2	2	10
3	3	3	11
4	4	4	100
5	5	5	101
6	6	6	110
7	7	7	111
8	8	10	1000
9	9	11	1001
10	A	12	1010
11	B	13	1011
12	10	14	1100
13	11	15	1101
14	12	16	1110
15	13	17	1111
16	14	20	10000
17	15	21	10001
18	16	22	10010
19	17	23	10011
.20	18	24	10100
21	19	25	10101
22	1A	26	10110
23	1B	27	10111
24	20	30	11000

□Example:

What is the value of  $9^6$ ?

Locate 9 in the left-hand column. Move to the right to the column headed by  $n^6$ . The value of  $9^6$  is given as 531,441.

□Example:

What is the value of  $23^7$ ?

Locate 23 in the left-hand column. Move to the right to the column headed by  $n^7$ . The number shown here is 3.404825. However, this number must be multiplied by  $10^9$  as indicated in the column heading. Hence,  $23^7$  equals  $3.404825 \times 10^9$ . To get the final answer, move the decimal point 9 places to the right.  $3.404825 \times 10^9$  equals 3,404,825,000.

## SQUARE ROOTS OF NUMBERS

Table 29-11 lists the square roots of numbers from 1 to 100.

□Example:

What is the square root of 19?

Table 29-10. Powers of Numbers

$n$	$n^3$	$n^4$	$n^5$	$n^6$	$n^7$	$n^8$
1	1	1	1	1	1	1
2	8	16	32	64	128	256
3	27	81	243	729	2187	6561
4	64	256	1024	4096	16384	65536
5	125	625	3125	15625	78125	390625
6	216	1296	7776	46656	279936	1679616
7	343	2401	16807	117649	823543	5764801
8	512	4096	32768	262144	2097152	16777216
9	729	6561	59049	531441	4782969	43046721
10	1000	10000	100000	1000000	10000000	$\times 10^8$
11	1331	14641	161051	1771561	19487171	2.143589
12	1728	20736	248832	2985984	35831808	4.299817
13	2197	28561	371293	4826809	62748517	8.157307
14	2794	38416	537824	7529536	105413504	14.757891
15	3375	50625	759375	11390625	170859375	25.628906
16	4096	65536	1048576	16777216	268435456	42.949673
17	4913	83521	1419857	24137569	410338673	69.757574
18	5832	104976	1889568	34012224	612220032	110.199606
19	6859	130321	2476099	47045881	893871739	169.835630
20	8000	160000	3200000	64000000	$\times 10^9$	$\times 10^{10}$
21	9261	194481	4084101	85766121	1.801089	3.782286
22	10648	234256	5153632	113379904	2.494358	5.487587
23	12167	279841	6436343	148035889	3.404825	7.831099
24	13824	331776	7962624	191102976	4.586471	11.007531
25	15625	390625	9765625	244140625	6.103516	15.258789
26	17576	456976	11881376	308915776	8.031810	20.882706
27	19683	531441	14348907	387420489	10.460353	28.242954
28	21952	614656	17210368	481890304	13.492929	37.780200
29	24389	707281	20511149	594823321	17.249876	50.024641
30	27000	810000	24300000	$\times 10^8$	$\times 10^{10}$	$\times 10^{11}$
31	29791	923521	28629151	8.875037	2.751261	8.528910
32	32768	1048576	33554432	10.737418	3.435974	10.995116
33	35937	1185921	39135393	12.914680	4.261844	14.064086
34	39304	1336336	45435424	15.448044	5.252335	17.857939

Table 29-10. Powers of Numbers (cont'd)

$n$	$n^3$	$n^4$	$n^5$	$n^6$	$n^7$	$n^8$
35	42875	1500625	52521875	18.382656	6.433930	22.518754
36	46656	1679616	60466176	21.767823	7.836416	28.211099
37	50653	1874161	69343957	25.657264	9.493188	35.124795
38	54872	2085136	79235168	30.109364	11.441558	43.477921
39	59319	2313441	90224199	35.187438	13.723101	53.520093

			$\times 10^9$	$\times 10^{10}$	$\times 10^{12}$
40	64000	2560000	102400000	4.096000	16.384000
41	68921	2825761	115856201	4.750104	19.475427
42	74088	3111696	130691232	5.489032	23.053933
43	79507	3418801	147008443	6.321363	27.181861
44	85184	3748096	164916224	7.256314	31.927781
45	91125	4100625	184528125	8.303766	37.366945
46	97336	4477456	205962976	9.474297	43.581766
47	103823	4879681	229345007	10.779215	50.662312
48	110592	5308416	254803968	12.230590	58.706834
49	117649	5764801	282475249	13.841287	67.822307
					33.232931

			$\times 10^9$	$\times 10^{11}$	$\times 10^{13}$
50	125000	6250000	312500000	15.625000	7.812500
51	132651	6765201	345025251	17.596288	8.974107
52	140608	7311616	380204032	19.770610	10.280717
53	148877	7890481	418195493	22.164361	11.747111
54	157464	8503056	459165024	24.794911	13.389252
55	166375	9150625	503284375	27.680641	15.224352
56	175616	9834496	550731776	30.840979	17.270948
57	185193	10556001	601692057	34.296447	19.548975
58	195112	11316496	656356768	38.068693	22.079842
59	205379	12117361	714924299	42.180534	24.886515
					14.683044

			$\times 10^8$	$\times 10^{10}$	$\times 10^{11}$	$\times 10^{13}$
60	216000	12960000	7.776000	4.665600	27.993600	16.796160
61	226981	13845841	8.445963	5.152037	31.427428	19.170731
62	238328	14776336	9.161328	5.680024	35.216146	21.834011
63	250047	15752961	9.924365	6.252350	39.389806	24.815578
64	262114	16777216	10.737418	6.871948	43.980465	28.147498
65	274625	17850625	11.602906	7.541889	49.022279	31.864481
66	287496	18974736	12.523326	8.265395	54.551607	36.004061
67	300763	20151121	13.501251	9.045838	60.607116	40.606768

Table 29-10. Powers of Numbers (cont'd)

$n$	$n^1$	$n^4$	$n^5$	$n^6$	$n^7$	$n^8$
68	314432	21381376	14.539336	9.886748	67.229888	45.716324
69	328509	22667121	15.640313	10.791816	74.463533	51.379837
				$\times 10^8$	$\times 10^{10}$	$\times 10^{12}$
70	343000	24010000	16.807000	11.764900	8.235430	5.764801
71	357911	25411681	18.042294	12.810028	9.095120	6.457535
72	373248	26873856	19.349176	13.931407	10.030613	7.222041
73	389017	28398241	20.730716	15.133423	11.047399	8.064601
74	405224	29986576	22.190066	16.420649	12.151280	8.991947
75	421875	31640625	23.730469	17.797852	13.348389	10.011292
76	438976	33362176	25.355254	19.269993	14.645195	11.130348
77	456533	35153041	27.067842	20.842238	16.048523	12.357363
78	474552	37015056	28.871744	22.519960	17.565569	13.701144
79	493039	38950081	30.770564	24.308746	19.203909	15.171088
				$\times 10^8$	$\times 10^{10}$	$\times 10^{12}$
80	512000	40960000	32.768000	26.214400	20.971520	16.777216
81	531441	43046721	34.867844	28.242954	22.876792	18.530202
82	551368	45212176	37.073984	30.400667	24.928547	20.441409
83	571787	47458321	39.390406	32.694037	27.136051	22.522922
84	592704	49787136	41.821194	35.129803	29.509035	24.787589
85	614125	52200625	44.370531	37.714952	32.057709	27.249053
86	636056	54700816	47.042702	40.456724	34.792782	29.921793
87	658503	57289761	49.842092	43.362620	37.725479	32.821167
88	681472	59969536	52.773192	46.440409	40.867560	35.963452
89	704969	62742241	55.840594	49.698129	44.231335	39.365888
				$\times 10^9$	$\times 10^{11}$	$\times 10^{13}$
90	729000	65610000	5.904900	5.314410	4.782969	4.304672
91	753571	68574961	6.240321	5.678693	5.167610	4.702525
92	778688	71639296	6.590815	6.063550	5.578466	5.132189
93	804357	74805201	6.956884	6.469902	6.017009	5.595818
94	830584	78074896	7.339040	6.898698	6.484776	6.095689
95	857375	81450625	7.737809	7.350919	6.983373	6.634204
96	884736	84934656	8.153727	7.827578	7.514475	7.213896
97	912673	88529281	8.587340	8.329720	8.079828	7.837434
98	941192	92236816	9.039208	8.858424	8.681255	8.507630
99	970299	96059601	9.509900	9.414801	9.320653	9.227447
100	10000000	1000000000	10.000000	10.000000	10.000000	10.000000

Find 19 in the column headed by the letter n (abbreviation for number). The square root of 19 appears immediately to the right in the column identified by  $\sqrt{n}$ . The square root of 19 is 4.3589.

Table 29-11. Square Roots Of Numbers

n	$\sqrt{n}$	n	$\sqrt{n}$	n	$\sqrt{n}$	n	$\sqrt{n}$
1	1.0000	26	5.0990	51	7.1414	76	8.7178
2	1.4142	27	5.1962	52	7.2111	77	8.7750
3	1.7321	28	5.2915	53	7.2801	78	8.8318
4	2.0000	29	5.3852	54	7.3485	79	8.8882
5	2.2361	30	5.4772	55	7.4162	80	8.9443
6	2.4495	31	5.5678	56	7.4833	81	9.0000
7	2.6458	32	5.6569	57	7.5498	82	9.0554
8	2.8284	33	5.7446	58	7.6158	83	9.1104
9	3.0000	34	5.8310	59	7.6811	84	9.1652
10	3.1623	35	5.9161	60	7.7460	85	9.2195
11	3.3166	36	6.0000	61	7.8102	86	9.2736
12	3.4641	37	6.0828	62	7.8740	87	9.3274
13	3.6056	38	6.1644	63	7.9373	88	9.3808
14	3.7417	39	6.2450	64	8.0000	89	9.4340
15	3.8730	40	6.3246	65	8.0623	90	9.4868
16	4.0000	41	6.4031	66	8.1240	91	9.5394
17	4.1231	42	6.4807	67	8.1854	92	9.5917
18	4.2426	43	6.5574	68	8.2462	93	9.6437
19	4.3589	44	6.6332	69	8.3066	94	9.6954
20	4.4721	45	6.7082	70	8.3666	95	9.7468
21	4.5826	46	6.7823	71	8.4261	96	9.7980
22	4.6904	47	6.8557	72	8.4853	97	9.8490
23	4.7958	48	6.9282	73	8.5440	98	9.8995
24	4.8990	49	7.0000	74	8.6023	99	9.9499
25	5.0000	50	7.0711	75	8.6603	100	10.0000

### CUBE ROOTS OF NUMBERS

Table 29-12 can be used to find the cube roots of numbers ranging from 1 to 10,000.

#### □Example:

What is the cube root of 16?

Locate 16 in the column headed by the letter n. Move to the right to the column identified by  $\sqrt[3]{n}$ . The cube root of 16 is 2.519842.

Two additional columns are marked  $\sqrt[3]{10n}$  and  $\sqrt[3]{100n}$ . These are used for extending the values in the n column. Thus, if n is 18, then 10n is  $10 \times 18$  equals 180, and 100n is  $100 \times 18$  equals 1800. Consequently, 18 in the n column can represent 18, 180 or 1800.

**□Example:**

What is the cube root of 3100?

Locate 31 in the n column. 3100, however, is  $31 \times 100$ , and so the answer will be found in the  $\sqrt[3]{100n}$  column. Move horizontally to this column and the answer is given as 14.58100. The last two zeros of this number do not contribute to its value and so can be omitted.  $\sqrt[3]{3100}$  equals 14.581.

Table 29-12. Cube Roots of Numbers

n	$\sqrt[3]{n}$	$\sqrt[3]{10n}$	$\sqrt[3]{100n}$
1	1.000000	2.154435	4.641589
2	1.259921	2.714418	5.848035
3	1.442250	3.107233	6.694330
4	1.587401	3.419952	7.368063
5	1.709976	3.684031	7.937005
6	1.817121	3.914868	8.434327
7	1.912931	4.121285	8.879040
8	2.000000	4.308869	9.283178
9	2.080084	4.481405	9.654894
10	2.154435	4.641589	10.000000
11	2.223980	4.791420	10.32280
12	2.289428	4.932424	10.62659
13	2.351335	5.065797	10.91393
14	2.410142	5.192494	11.18689
15	2.466212	5.313293	11.44714
16	2.519842	5.428835	11.69607
17	2.571282	5.539658	11.93483
18	2.620741	5.646216	12.16440
19	2.668402	5.748897	12.38562
20	2.714418	5.848035	12.59921

Table 29-12. Cube Roots of Numbers (cont'd)

<i>n</i>	$\sqrt[3]{n}$	$\sqrt[3]{10n}$	$\sqrt[3]{100n}$
21	2.758924	5.943922	12.80579
22	2.802039	6.036811	13.00591
23	2.843867	6.126926	13.20006
24	2.884499	6.214465	13.38866
25	2.924018	6.299605	13.57209
26	2.962496	6.382504	13.75069
27	3.000000	6.463304	13.92477
28	3.036589	6.542133	14.09460
29	3.072317	6.619106	14.26043
30	3.107233	6.694330	14.42250
31	3.141381	6.767899	14.58100
32	3.174802	6.839904	14.73613
33	3.207534	6.910423	14.88806
34	3.239612	6.979532	15.03695
35	3.271066	7.047299	15.18294
36	3.301927	7.113787	15.32619
37	3.332222	7.179054	15.46680
38	3.361975	7.243156	15.60491
39	3.391211	7.306144	15.74061
40	3.419952	7.368063	15.87401
41	3.448217	7.428959	16.00521
42	3.476027	7.488872	16.13429
43	3.503398	7.547842	16.26133
44	3.530348	7.605905	16.38643
45	3.556893	7.663094	16.50964
46	3.583048	7.719443	16.63103
47	3.608826	7.774980	16.75069
48	3.634241	7.829735	16.86865
49	3.659306	7.883735	16.98499
50	3.684031	7.937005	17.09976
51	3.708430	7.989570	17.21301
52	3.732511	8.041452	17.32478
53	3.756286	8.092672	17.43513
54	3.779763	8.143253	17.54411
55	3.802952	8.193213	17.65174

Table 29-12. Cube Roots of Numbers (cont'd)

$n$	$\sqrt[3]{n}$	$\sqrt[3]{10n}$	$\sqrt[3]{100n}$
56	3.825862	8.242571	17.75808
57	3.848501	8.291344	17.86316
58	3.870877	8.339551	17.96702
59	3.892996	8.387207	18.06969
60	3.914868	8.434327	18.17121
61	3.936497	8.480926	18.27160
62	3.957892	8.527019	18.37091
63	3.979057	8.572619	18.46915
64	4.000000	8.617739	18.56636
65	4.020726	8.662391	18.66256
66	4.041240	8.706588	18.75777
67	4.061548	8.750340	18.85204
68	4.081655	8.793659	18.94536
69	4.101566	8.836556	19.03778
70	4.121285	8.879040	19.12931
71	4.140818	8.921121	19.21997
72	4.160168	8.962809	19.30979
73	4.179339	9.004113	19.39877
74	4.198336	9.045042	19.48695
75	4.217163	9.085603	19.57434
76	4.235824	9.125805	19.66095
77	4.254321	9.165656	19.74681
78	4.272659	9.205164	19.83192
79	4.290840	9.244335	19.91632
80	4.308869	9.283178	20.00000
81	4.326749	9.321698	20.08299
82	4.344481	9.359902	20.16530
83	4.362071	9.397796	20.24694
84	4.379519	9.435388	20.32793
85	4.396830	9.472682	20.40828
86	4.414005	9.509685	20.48800
87	4.431048	9.546403	20.56710
88	4.447960	9.582840	20.64560
89	4.464745	9.619002	20.72351
90	4.481405	9.654894	20.80084
91	4.497941	9.690521	20.87759
92	4.514357	9.725888	20.95379

Table 29-12. Cube Roots of Numbers (cont'd)

$n$	$\sqrt[3]{n}$	$\sqrt[3]{10n}$	$\sqrt[3]{100n}$
93	4.530655	9.761000	21.02944
94	4.546836	9.795861	21.10454
95	4.562903	9.830476	21.17912
96	4.578857	9.864848	21.25317
97	4.594701	9.899893	21.32671
98	4.610436	9.932884	21.39975
99	4.626065	9.966555	21.47229
100	4.641589	10.00000	21.54435

## NUMBERS AND RECIPROCALS

The reciprocal of a number is the inverse of that number, or the number divided into 1. The reciprocal of 5 is 1/5; the reciprocal of 87 is 1/87. Table 29-13 supplies reciprocals of numbers ranging from 0.1 to 100.

### □Example:

What is the reciprocal of 27?

Locate 27 in the  $n$  column. Move to the right and in the column headed by  $1/n$  the answer is given as 0.0370.

Table 29-13 can be extended by moving the decimal point as required.

### □Example:

What is the reciprocal of 160?

160 does not appear directly in the table. Instead, locate 16 in the  $n$  column and change it to 160. In the  $1/n$  column, the corresponding reciprocal value for 16 is 0.0625. Add another zero directly after the decimal point (equivalent to dividing the reciprocal by 10) and the answer becomes 0.000625.

To find the reciprocal of 1600, divide the answer in the  $1/n$  column (corresponding to 16) by 100, or insert two zeros after the decimal point. Hence the reciprocal of 1600 is 0.000625.

Table 29-13. Numbers and Reciprocals

<i>n</i>	1/ <i>n</i>	<i>n</i>	1/ <i>n</i>	<i>n</i>	1/ <i>n</i>
0.1	10.0000	28	.0357	65	.0154
0.2	5.0000	29	.0345	66	.0152
0.3	3.3333	30	.0333	67	.0149
0.4	2.5000	31	.0323	68	.0147
0.5	2.0000	32	.0313	69	.0145
0.6	1.6666	33	.0303	70	.0143
0.7	1.4286	34	.0294	71	.0141
0.8	1.2500	35	.0286	72	.0139
0.9	1.1111	36	.0278	73	.0137
		37	.0270	74	.0135
1	1.0000	38	.0263	75	.0133
2	.5000	39	.0256	76	.0132
3	.3333	40	.0250	77	.0130
4	.2500	41	.0244	78	.0128
5	.2000	42	.0238	79	.0127
6	.1667	43	.0233	80	.0125
7	.1429	44	.0227	81	.0123
8	.1250	45	.0222	82	.0122
9	.1111	46	.0217	83	.0120
10	.1000	47	.0213	84	.0119
11	.0909	48	.0208	85	.0118
12	.0833	49	.0204	86	.0116
13	.0769	50	.0200	87	.0115
14	.0714	51	.0196	88	.0114
15	.0667	52	.0192	89	.0112
16	.0625	53	.0189	90	.0111
17	.0588	54	.0185	91	.0110
18	.0555	55	.0182	92	.0109
19	.0526	56	.0179	93	.0108
20	.0500	57	.0175	94	.0106
21	.0476	58	.0172	95	.0105
22	.0455	59	.0169	96	.0104
23	.0435	60	.0167	97	.0103
24	.0417	61	.0164	98	.0102
25	.0400	62	.0161	99	.0101
26	.0385	63	.0159	100	.0100
27	.0370	64	.0156		



## Chapter 30

# Mathematics

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### SQUARE VS CIRCULAR AREA

It is sometimes necessary to convert from square to circular area, or from circular to square area. Square area is equal to circular area when the side of the square is equal to 0.88623 multiplied by the diameter of the circle. Conversely, the areas are equal when the diameter of the circle equals 1.12838 multiplied by the side of the square.

#### □Example:

A circle has a diameter of 2 inches. What is the length of any side of a square so that the area of the square is the same as the area of the circle?

The length of any side of the square is equal to the diameter of the circle multiplied by 0.88623. Therefore,  $2 \times 0.88623$  equals 1.77246 inches. The area of the square is  $1.77246 \times 1.77246$ , or 3.1416 square inches. The area of the circle is  $\pi r^2$ . The radius equals one-half the diameter  $\frac{1}{2} \times 2$ , or 1. The area of the circle is equal to  $\pi r^2$  equals  $3.1416 \times 1^2$  equals 3.1416. Thus, a circle with a diameter of 2 inches has the same area as a square, each of whose sides has a length of 1.77246 inches.

Table 30-1 supplies the circumference and area of circles having diameters ranging from 1/32 inch to 100 inches.

Table 30-1. Circumference and Area of Circles

Diameter	Circumference	Area
1/32	0.09817	0.0007
1/16	0.19635	0.0030
3/32	0.29452	0.0069
3/16	0.58904	0.0276
7/32	0.68722	0.0375
9/32	0.88357	0.0621
11/32	1.07992	0.0928
13/32	1.27627	0.1296
9/16	1.76715	0.2485
19/32	1.86532	0.2768
21/32	2.06167	0.3382
11/16	2.15984	0.3712
23/32	2.25802	0.4057
25/32	2.45437	0.4793
27/32	2.65072	0.5591
29/32	2.84707	0.6450
1	3.142	0.7854
2	6.283	3.1416
3	9.425	7.0686
4	12.566	12.5664
5	15.708	19.6350
6	18.850	28.2743
7	21.991	38.4845
8	25.133	50.2655
9	28.274	63.6173
10	31.416	78.5398
11	34.558	95.0332
12	37.699	113.097
13	40.841	132.732
14	43.982	153.938
15	47.124	176.715
16	50.265	201.062
17	53.407	226.980
18	56.549	254.469
19	59.690	283.529
20	62.832	314.159

Table 30-1. Circumference and Area of Circles (cont'd)

Diameter	Circumference	Area
21	65.973	346.361
22	69.115	380.133
23	72.257	415.476
24	75.398	452.389
25	78.540	490.874
26	81.681	530.929
27	84.823	572.555
28	87.965	615.752
29	91.106	660.520
30	94.248	706.858
31	97.389	754.768
32	100.531	804.248
33	103.673	855.299
34	106.814	907.920
35	109.956	962.113
36	113.097	1,017.88
37	116.239	1,075.21
38	119.381	1,134.11
38	122.522	1,194.59
40	125.66	1,256.64
41	128.81	1,320.25
42	131.95	1,385.44
43	135.09	1,452.20
44	138.23	1,520.53
45	141.37	1,590.43
46	144.51	1,661.90
47	147.65	1,734.94
48	150.80	1,809.56
49	153.94	1,885.74
50	157.08	1,963.50
51	160.22	2,042.82
52	163.36	2,123.72
53	166.50	2,206.18
54	169.65	2,290.22
55	172.79	2,375.83

Table 30-1. Circumference and Area of Circles (cont'd)

Diameter	Circumference	Area
56	175.93	2,463.01
57	179.07	2,551.76
58	182.21	2,642.08
59	185.35	2,733.97
60	188.50	2,827.43
61	191.64	2,922.47
62	194.78	3,019.07
63	197.92	3,117.25
64	201.06	3,216.99
65	204.20	3,318.31
66	207.35	3,421.19
67	210.49	3,525.65
68	213.63	3,631.68
69	216.77	3,739.28
70	219.91	3,848.45
71	223.05	3,959.19
72	226.19	4,071.50
73	229.34	4,185.39
74	232.48	4,300.84
75	235.62	4,417.86
76	238.76	4,536.46
77	241.90	4,656.63
78	245.04	4,778.36
79	248.19	4,901.67
80	251.33	5,026.55
81	254.47	5,153.00
82	257.61	5,281.02
83	260.75	5,410.61
84	263.89	5,541.77
85	267.04	5,674.50
86	270.18	5,808.80
87	273.32	5,944.68
88	276.46	6,082.12
89	279.60	6,221.14
90	282.74	6,361.73

Table 30-1. Circumference and Area of Circles (cont'd)

Diameter	Circumference	Area
91	285.88	6,503.88
92	289.03	6,647.61
93	292.17	6,792.91
94	295.31	6,939.78
95	298.45	7,088.22
96	301.59	7,238.23
97	304.73	7,389.81
98	307.88	7,542.96
99	311.02	7,697.69
100	314.16	7,853.98

## FUNCTIONS OF ANGLES

Table 30-2 supplies the trigonometric functions of the angle included between the base and the hypotenuse of a right-angle triangle, designated as angle A in the Fig. 30-1. The sine (sin) of the angle is the ratio of the altitude to the hypotenuse; that is, the altitude divided by the length of the hypotenuse. The cosine (cos) is the base divided by the hypotenuse. The tangent (tan) is the altitude divided by the base while the cotangent (cot) is the base divided by the altitude. The sec (secant) is the ratio of the hypotenuse to the base while the csc (cosecant) is the ratio of the hypotenuse to the altitude.

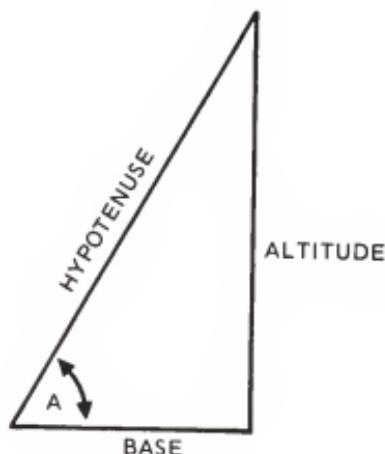


Fig. 30-1. Right triangle.

Table 30-2. Angles and Their Functions

Angle A	sin A	cos A	tan A	cot A	sec A	csc A
0°	0	1	0	∞	1	∞
30°	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$	$\sqrt{3}$	$2\sqrt{3}/3$	2
45°	$\sqrt{2}/2$	$\sqrt{2}/2$	1	1	$\sqrt{2}$	$\sqrt{2}$
60°	$\sqrt{3}/2$	1/2	$\sqrt{3}$	$\sqrt{3}/3$	2	$2\sqrt{3}/3$
90°	1	0	∞	0	∞	1
120°	$\sqrt{3}/2$	-1/2	$\sqrt{3}$	$-\sqrt{3}/3$	-2	$2\sqrt{3}/3$
180°	0	-1	0	∞	-1	∞
270°	-1	0	∞	0	∞	-1
360°	0	1	0	∞	1	0

Table 30-3. The Ratio Tan X/R and Corresponding Values of Phase Angle, Θ.

Phase Angle (in degrees)	Ratio	Phase Angle (in degrees)	Ratio	Phase Angle (in degrees)	Ratio
0	0.0000	30	0.5774	60	1.7321
1	0.0175	31	0.6009	61	1.8040
2	0.0349	32	0.6249	62	1.8807
3	0.0524	33	0.6494	63	1.9626
4	0.0699	34	0.6745	64	2.0503
5	0.0875	35	0.7002	65	2.1445
6	0.1051	36	0.7265	66	2.2460
7	0.1228	37	0.7536	67	2.3559
8	0.1405	38	0.7813	68	2.4751
9	0.1584	39	0.8098	69	2.6051
10	0.1763	40	0.8391	70	2.7475
11	0.1944	41	0.8693	71	2.9042
12	0.2126	42	0.9004	72	3.0777
13	0.2309	43	0.9325	73	3.2709
14	0.2493	44	0.9657	74	3.4874
15	0.2679	45	1.0000	75	3.7321
16	0.2867	46	1.0355	76	4.0108
17	0.3057	47	1.0724	77	4.3315
18	0.3249	48	1.1106	78	4.7046
19	0.3443	49	1.1504	79	5.1446
20	0.3640	50	1.1918	80	5.6713
21	0.3839	51	1.2349	81	6.3138
22	0.4040	52	1.2799	82	7.1154
23	0.4245	53	1.3270	83	8.1443
24	0.4452	54	1.3764	84	9.5144
25	0.4663	55	1.4281	85	11.43
26	0.4877	56	1.4826	86	14.30
27	0.5095	57	1.5399	87	19.08
28	0.5317	58	1.6003	88	28.64
29	0.5543	59	1.6643	89	57.29

Table 30-4. Trigonometric Functions

Degrees	Sine	Tangent	Cotangent	Cosine	
0	.0000	.0000	.....	1.0000	90
1	.0175	.0175	57.29	.9998	89
2	.0349	.0349	28.636	.9994	83
3	.0523	.0524	19.081	.9996	87
4	.0698	.0699	14.301	.9976	86
5	.0872	.0875	11.430	.9962	85
6	.1045	.1051	9.5144	.9945	84
7	.1219	.1228	8.1443	.9925	83
8	.1392	.1405	7.1154	.9903	82
9	.1564	.1584	6.3138	.9877	81
10	.1736	.1763	5.6713	.9848	80
11	.1908	.1944	5.1446	.9816	79
12	.2079	.2126	4.7046	.9781	78
13	.2250	.2309	4.3315	.9744	77
14	.2419	.2493	4.0108	.9703	76
15	.2588	.2679	3.7321	.9659	75
16	.2756	.2867	3.4874	.9613	74
17	.2924	.3057	3.2709	.9563	73
18	.3090	.3249	3.0777	.9511	72
19	.3256	.3443	2.9042	.9455	71
20	.3420	.3640	2.7475	.9397	70
21	.3584	.3839	2.6051	.9336	69
22	.3746	.4040	2.4751	.9272	68
23	.3907	.4245	2.3559	.9205	67
24	.4067	.4452	2.2460	.9135	66
25	.4226	.4663	2.1445	.9063	65
26	.4384	.4877	2.0503	.8988	64
27	.4540	.5095	1.9626	.8910	63
28	.4695	.5317	1.8807	.8829	62
29	.4848	.5543	1.8040	.8746	61
30	.5000	.5774	1.7321	.8660	60
31	.5150	.6009	1.6643	.8572	59
32	.5299	.6249	1.6003	.8480	58
33	.5446	.6494	1.5399	.8387	57
34	.5592	.6745	1.4826	.8290	56
35	.5736	.7002	1.4281	.8192	55
36	.5878	.7265	1.3764	.8090	54
37	.6018	.7536	1.3270	.7986	53
38	.6157	.7813	1.2799	.7880	52
39	.6293	.8098	1.2349	.7771	51
40	.6428	.8391	1.1918	.7660	50
41	.6561	.8693	1.1504	.7547	49
42	.6691	.9004	1.1106	.7431	48
43	.6820	.9325	1.0724	.7314	47
44	.6947	.9657	1.0355	.7193	46
45	.7071	1.0000	1.0000	.7071	45

## VALUES OF $\pi$

Various values of  $\pi$  appear regularly in calculations involving electronic problems. This constant is used for finding values of inductive reactance, capacitive reactance, frequency, and in problems involving resonance. Table 30-5 supplies coefficients, powers, roots, and logs of  $\pi$ .

Table 30-5. Coefficients, Powers, Roots, and Logs of  $\pi$

1 $\pi = 3.14159265$	6 $\pi = 18.84955592$
2 $\pi = 6.28318531$	7 $\pi = 21.99114857$
3 $\pi = 9.42477796$	8 $\pi = 25.13274122$
4 $\pi = 12.56637061$	9 $\pi = 28.27433387$
5 $\pi = 15.70796327$	10 $\pi = 31.41592652$
$\sqrt{\pi} = 0.31830989$	$4/\pi = 1.27323954$
$1/2\pi = 0.15915494$	$\pi^2 = 9.86960440$
$1/3\pi = 0.106103$	$\sqrt{\pi} = 1.77245385$
$\pi/2 = 1.57079633$	$1/\pi^2 = 0.10132118$
$\pi/3 = 1.04719755$	$1/\sqrt{\pi} = 0.56418958$
$\pi/4 = 0.78539816$	$\sqrt{3/\pi} = 0.97720502$
$\pi/5 = 0.62831853$	$\sqrt{4/\pi} = 1.12837917$
$\pi/6 = 0.52359878$	$3/\sqrt{\pi} = 1.46459189$
$\pi/7 = 0.44879895$	$\log \pi = 0.4971499$
$\pi/8 = 0.39269908$	$\log 2\pi = 0.7981799$
$\pi/9 = 0.34906585$	$\log 4\pi = 1.0992099$
$\pi/10 = 0.314159265$	$\log \pi^2 = 0.9942997$
$4\pi/3 = 4.18879020$	$\log \sqrt{\pi} = 0.248$
$3/\pi = 0.954929666$	

## MATHEMATICAL SYMBOLS

Electronics is a science which relies on mathematics for the solution of problems. Consequently, the symbols used in mathematics have become an integral part of textbooks having electronics as their subject matter. Table 30-6 lists those mathematical symbols most often found associated with electronics.

Table 30-6. Mathematical Symbols

Symbol	Name or Meaning	Description
0, 1, 2, 3, 4, etc.	Whole numbers	Cardinal (Arabic) numbers used in mathematics. Arithmetic numbers.
No.; no.; #	Abbreviation	Symbol that may precede a number.

Table 30-6. Mathematical Symbols (cont'd)

Symbol	Name or Meaning	Description
I; II; III; IV; V I; II; III; IV; V	Roman numerals	Have limited use—introductory pages of books; watches; building cornerstones, etc.
2-1/2; 3-1/8; 4-1/9	Mixed Numbers	Consist of a whole number and a proper fraction.
1/2; 3/4; 4/7	Proper fractions	Numerator is always smaller in value than the denominator.
5/2; 4/3; 9/5	Improper fractions	Numerator is always larger in value than the denominator.
+	Plus sign	Positive; plus; addition. May be used to indicate direction.
-	Minus sign	Negative; minus; subtraction. May be used to indicate direction.
±	Plus-minus	Positive or negative; plus or minus; addition or subtraction.
〒	Minus-plus	Negative or positive; minus or plus; subtraction or addition.
a; x; y; z; etc.	Literal numbers	Letters used as a symbol for a number.
25/100; 4/10; 6589/1000	Decimal fractions	Fractions having 10, 100, 1000, etc. in the denominator.
1.657; 0.354 0.25	Decimal point	Point used in decimal fractions when denominator is omitted. Also known as the radix point. The number to the right of the decimal point is the decimal fraction. In some countries a comma is used in place of the decimal point. In the U.S. the decimal point is put at the bottom; in England at the center or higher. In other number systems, such as the binary, it is known as the binary point. In the hexadecimal system it is called the hexadecimal point. The term decimal point refers only to the use of the radix point in the decimal system.

Table 30-6. Mathematical Symbols (cont'd)

Symbol	Name or Meaning	Description
$\infty$	Infinity	An indefinitely great number or amount.
$\times$	Multiply by	Multiplication. A form of repeated addition.
$x \cdot y$	Dot between letters means multiplication	$x$ is multiplied by $y$ .
$(x) (y)$	Adjacent parentheses means multiplication	$x$ is multiplied by $y$ .
$x + y$	Straight line with dot above and below means division	$x$ is divided by $y$ .
$x/y$	Slant line indicates division	$x$ is divided by $y$ . Also, ratio of $x$ to $y$ .
$\frac{x}{y}$	Horizontal line means division	$x$ is divided by $y$ . Also, ratio of $x$ to $y$ .
$x : y$	Dots indicate division or ratio	$x$ is divided by $y$ ; the ratio of $x$ to $y$ .
= or ::	Equals signs	Signs representing equality between two quantities; is equal to.
=	Identity sign	Sign representing Identity between quantities.
$\approx$	Approximation sign	Quantities separated by this sign are approximately equal. Congruent.
$\neq$	Inequality sign	Quantities separated by this sign are not equal.
<	Inequality	Is less than.
<<	Inequality	Is much less than.
>	Inequality	Is greater than.
>>	Inequality	Is much greater than.
$\geq$	Inequality or equality	Is equal to or Is greater than.
$\leq$	Inequality or equality	Is equal to or Is less than.

Table 30-6. Mathematical Symbols (cont'd)

Symbol	Name or Meaning	Description
∴	Therefore	Symbol used in geometry and logic.
= or $\rightarrow$ or $\lim$	Approaches as a limit	Variable approaches a constant, but never reaches it.
$\perp$	Perpendicular. Normal	Lines which form right angles.
	Parallel	Lines which are parallel to each other.
$\angle$	Angle. Also positive angle	The angle formed by two lines.
$\angle s$	Angles	Two or more angles.
$\lceil - \rceil$	Negative angle	An angle whose sine, tangent, cosecant and cotangent are negative.
$\Delta$	Change. Increase or decrease. Increment	Capital Greek letter delta. A similar symbol is used to represent triangles in trigonometry.
$\sqrt{ }$	Square root	Quantity raised to the one-half power.
$n\sqrt{ }$	nth root	Quantity raised to the nth power.
sin	Sine of included base angle	Ratio of altitude to hypotenuse in a right-angle triangle
cos	Cosine of included base angle	Ratio of base to altitude in a right-angle triangle.
tan	Tangent of included base angle	Ratio of altitude to the base in a right-angle triangle.
cot	Cotangent of included base angle	Ratio of base to altitude in a right-angle triangle.
sec	Secant of included base angle	Ratio of hypotenuse to base in a right-angle triangle.
csc	Cosecant of included base angle	Ratio of hypotenuse to altitude in a right-angle triangle.

Table 30-7. Common Logarithms

N	0	1	2	3	4	5	6	7	8	9
10	0000	0043	0086	0128	0170	0212	0253	0294	0334	0374
11	0414	0453	0492	0531	0569	0607	0645	0682	0719	0755
12	0792	0828	0864	0899	0934	0969	1004	1038	1072	1106
13	1139	1173	1206	1239	1271	1303	1335	1367	1399	1430
14	1461	1492	1523	1553	1584	1614	1644	1673	1703	1732
15	1761	1790	1818	1847	1875	1903	1931	1959	1987	2014
16	2041	2068	2095	2122	2148	2175	2201	2227	2253	2279
17	2304	2330	2355	2380	2405	2430	2455	2480	2504	2529
18	2553	2577	2601	2625	2648	2672	2695	2718	2742	2765
19	2788	2810	2833	2856	2878	2900	2923	2945	2967	2989
20	3010	3032	3054	3075	3096	3118	3139	3160	3181	3201
21	3222	3243	3263	3284	3304	3324	3345	3365	3385	3404
22	3424	3444	3464	3483	3502	3522	3541	3560	3579	3598
23	3617	3636	3655	3674	3692	3711	3729	3747	3766	3784
24	3802	3820	3838	3856	3874	3892	3909	3927	3945	3962
25	3979	3997	4014	4031	4048	4065	4082	4099	4116	4133
26	4150	4166	4183	4200	4216	4232	4249	4265	4281	4298
27	4314	4330	4346	4362	4378	4393	4409	4425	4440	4456
28	4472	4487	4502	4518	4533	4548	4564	4579	4594	4609
29	4624	4639	4654	4669	4683	4698	4713	4728	4742	4757
30	4771	4786	4800	4814	4829	4843	4857	4871	4886	4900
31	4914	4928	4942	4955	4969	4983	4997	5011	5024	5038
32	5051	5065	5079	5092	5105	5119	5132	5145	5159	5172
33	5185	5198	5211	5224	5237	5250	5263	5276	5289	5302
34	5315	5328	5340	5353	5366	5378	5391	5403	5416	5428
35	5441	5453	5465	5478	5490	5502	5514	5527	5539	5551
36	5563	5575	5587	5599	5611	5623	5635	5647	5658	5670
37	5682	5694	5705	5717	5729	5740	5752	5763	5775	5786
38	5798	5809	5821	5832	5843	5855	5866	5877	5888	5899
39	5911	5922	5933	5944	5955	5966	5977	5988	5999	6010
40	6021	6031	6042	6053	6064	6075	6085	6096	6107	6117
41	6128	6138	6149	6160	6170	6180	6191	6201	6212	6222
42	6232	6243	6253	6263	6274	6284	6294	6304	6314	6325
43	6335	6345	6355	6365	6375	6385	6395	6405	6415	6425
44	6435	6444	6454	6464	6474	6484	6493	6503	6513	6522
45	6532	6542	6551	6561	6571	6580	6590	6599	6609	6618
46	6628	6637	6646	6656	6665	6675	6684	6693	6702	6712
47	6721	6730	6739	6749	6758	6767	6776	6785	6794	6803
48	6812	6821	6830	6839	6848	6857	6866	6875	6884	6893
49	6902	6911	6920	6928	6937	6946	6955	6964	6972	6981
50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067
51	7076	7084	7093	7101	7110	7118	7126	7135	7143	7152
52	7160	7168	7177	7185	7193	7202	7210	7218	7226	7235
53	7243	7251	7259	7267	7275	7284	7292	7300	7308	7316
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396

Table 30-7. Common Logarithms

N	0	1	2	3	4	5	6	7	8	9
55	7404	7412	7419	7427	7435	7443	7451	7459	7466	7474
56	7482	7490	7497	7505	7513	7520	7528	7536	7543	7551
57	7559	7566	7574	7582	7589	7597	7604	7612	7619	7627
58	7634	7642	7649	7657	7664	7672	7679	7686	7694	7701
59	7709	7716	7723	7731	7738	7745	7752	7760	7767	7774
60	7782	7789	7796	7803	7810	7818	7825	7832	7839	7846
61	7853	7860	7868	7875	7882	7889	7896	7903	7910	7917
62	7924	7931	7938	7945	7952	7959	7966	7973	7980	7987
63	7993	8000	8007	8014	8021	8028	8035	8041	8048	8055
64	8062	8069	8075	8082	8089	8096	8102	8109	8116	8122
65	8129	8136	8142	8149	8156	8162	8169	8176	8182	8189
66	8195	8202	8209	8215	8222	8228	8235	8241	8248	8254
67	8261	8267	8274	8280	8287	8293	8299	8306	8312	8319
68	8325	8331	8338	8344	8351	8357	8363	8370	8376	8382
69	8388	8395	8401	8407	8414	8420	8426	8432	8439	8445
70	8451	8457	8463	8470	8476	8482	8488	8494	8500	8506
71	8513	8519	8525	8531	8537	8543	8549	8555	8561	8567
72	8573	8579	8585	8591	8597	8603	8609	8615	8621	8627
73	8633	8639	8645	8651	8657	8663	8669	8675	8681	8686
74	8692	8698	8704	8710	8716	8722	8727	8733	8739	8745
75	8751	8456	8762	8768	8774	8779	8785	8791	8797	8802
76	8808	8814	8820	8825	8831	8837	8842	8848	8854	8859
77	8865	8871	8876	8882	8887	8893	8899	8904	8910	8915
78	8921	8927	8932	8938	8943	8949	8954	8960	8965	8971
79	8976	8982	8987	8993	8998	9004	9009	9015	9020	9025
80	9031	9036	9042	9047	9053	9058	9063	9069	9074	9079
81	9085	9090	9096	9101	9106	9112	9117	9122	9128	9133
82	9138	9143	9149	9154	9159	9165	9170	9175	9180	9186
83	9191	9196	9201	9206	9212	9217	9222	9227	9232	9238
84	9243	9248	9253	9258	9263	9269	9274	9279	9284	9289
85	9294	9299	9304	9309	9315	9320	9325	9330	9335	9340
86	9345	9350	9355	9360	9365	9370	9375	9380	9385	9390
87	9395	9400	9405	9410	9415	9420	9425	9430	9435	9440
88	9445	9450	9455	9460	9465	9469	9474	9479	9484	9489
89	9494	9499	9504	9509	9513	9518	9523	9528	9533	9538
90	9542	9547	9552	9557	9562	9566	9571	9576	9581	9586
91	9590	9595	9600	9605	9609	9614	9619	9624	9628	9633
92	9638	9643	9647	9652	9657	9661	9666	9671	9675	9680
93	9685	9689	9694	9699	9703	9708	9713	9717	9722	9727
94	9731	9736	9741	9745	9750	9754	9759	9763	9768	9773
95	9777	9782	9786	9791	9795	9800	9805	9809	9814	9818
96	9823	9827	9832	9836	9841	9845	9850	9854	9859	9863
97	9868	9872	9877	9881	9886	9890	9894	9899	9903	9908
98	9912	9917	9921	9926	9930	9934	9939	9943	9948	9952
99	9956	9961	9965	9969	9974	9978	9983	9987	9991	9996



## Chapter 31

# Symbols, Codes and Alphabets

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Table 31-1. US American Standard Code for Information Interchange (courtesy of American Radio Relay League Inc.).

The U.S. American Standard Code for Information Interchange (USACII or ASCII) is an 8-unit code as shown here, used largely with computers.

NUL	Null, or all zeros	DC1	Device control 1
SOH	Start of heading	DC2	Device control 2
STX	Start of test	DC3	Device Control 3
ETX	End of text	DC4	Device Control 4
EOT	End of transmission	NAK	Negative acknowledge
ENQ	Enquiry	SYN	Synchronous idle
ACK	Acknowledge	ETB	End of transmission block
BEL	Bell, or alarm	CAN	Cancel
BS	Backspace	EM	End of medium
HT	Horizontal tabulation	SUB	Substitute
LF	Line feed	ESC	Escape
VT	Vertical tabulation	FS	File separator
FF	Form feed	GS	Group separator
CR	Carriage return	RS	Record separator
SO	Shift out	US	Unit separator
SI	Shift in	SP	Space
DLE	Data link escape	DEL	Delete

* INSERT APPROPRIATE DESIGNATIONS #	A - AMMETER V - VOLTMETER mA - MILLIAMMETER etc. METERS	SINGLE CELL OR MOTOR	ASSEMBLY OR MODULE	CRYSTAL QUARTZ HEADSET
	EARTH GROUNDS	MULTICELL BATTERIES	FUSE	ANTENNA
CONTACTS	PHONE JACK	PHONE JACK	SHIELDED WIRE	SHIELDING
	MULTIPLE, MOBILE	MIC. JACK	SHIELDED MULTICOMPONENT CABLE	ENCLOSURE
CONNECTIONS	CONTACT PLUG	MIC. JACK	GENERAL	OTHER
	MALE	MALE		INVERTER LOGIC
COAXIAL RECEPTACLE	PHONE PLUG	PHONE PLUG		OR GATE
	MALE	MALE		CRYSTAL QUARTZ
FEMALE	230 V	230 V		HAND KEY
	115 V	115 V		
CONNECTORS	MALE	MALE		
	MALE	MALE		
COMMONS CONNECTIONS	MALE	MALE		
	MALE	MALE		
COAXIAL PLUG	MALE	MALE		
	MALE	MALE		
FEMALE	MALE	MALE		
	MALE	MALE		
DUAL-GATE MOSFET	N-CHANNEL	N-CHANNEL	PNP	LINEAR INTEGRATED CIRCUITS
	P-CHANNEL	P-CHANNEL	NPN	
HEMI FET	N-CHANNEL	N-CHANNEL	BIPOLAR	
	P-CHANNEL	P-CHANNEL	JUNCTION FET	
PILOT LAMPS	N-CHANNEL	N-CHANNEL	MOSFET	
	P-CHANNEL	P-CHANNEL		

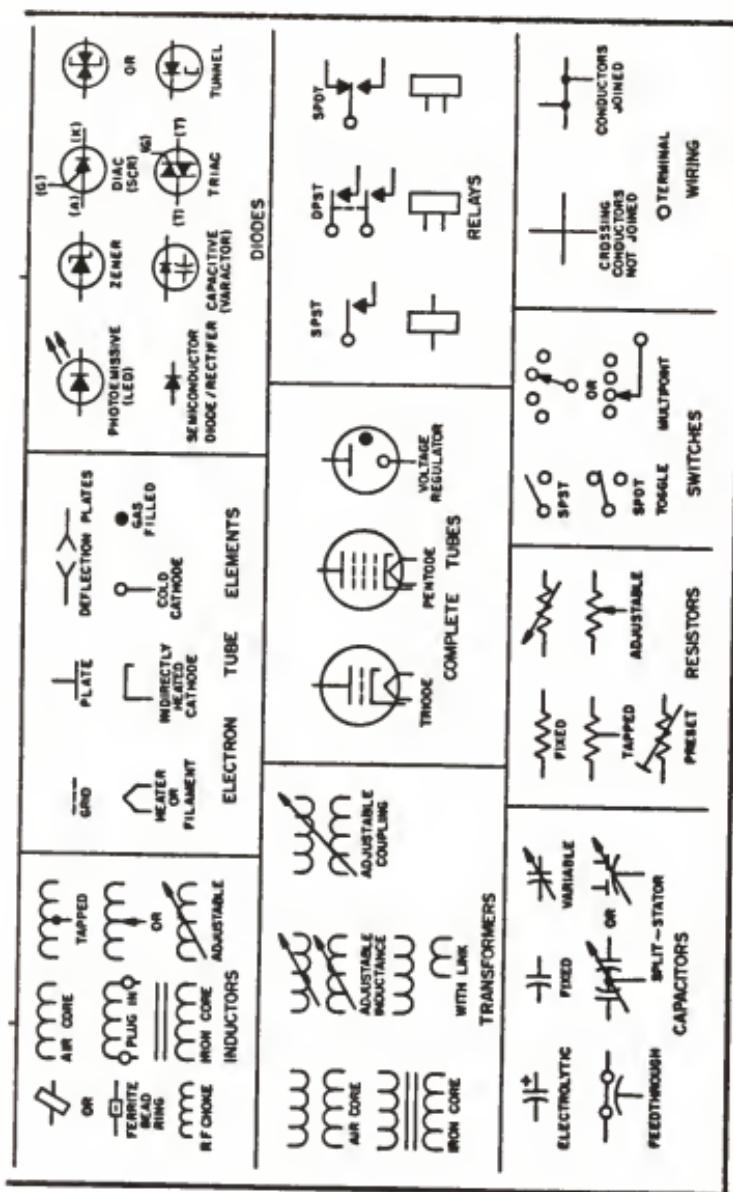
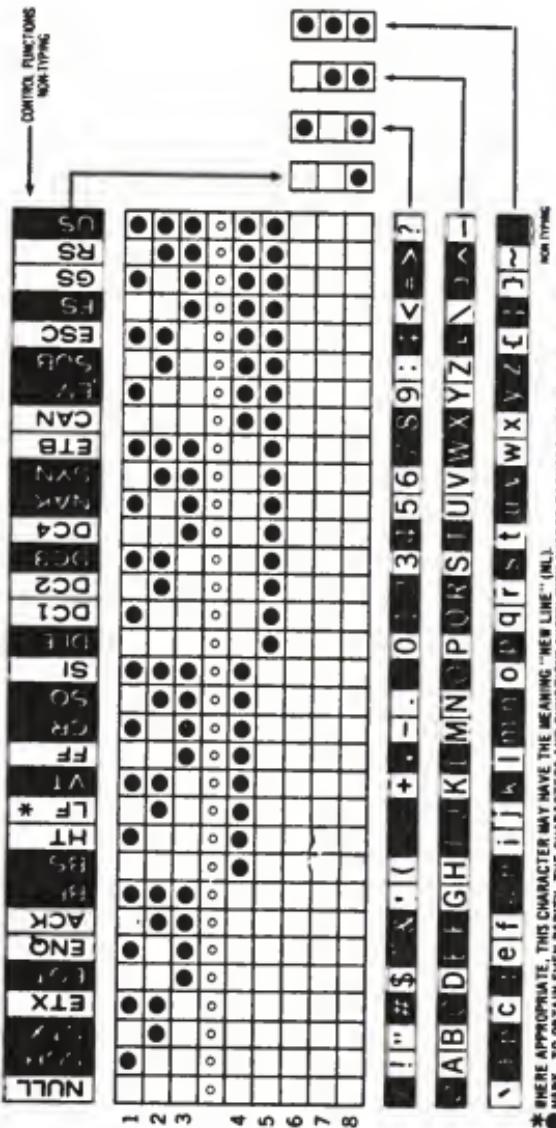


Fig. 31-1. Commonly used electronic schematic diagrams (courtesy of American Radio Relay League Inc.).

American Standard Code for Information Interchange (ASCII)



WHERE APPROPRIATE, THIS CHARACTER MAY HAVE THE MEANING "NEW LINE" (NL).  
MARK TO OBTAIN EVEN PARITY, THE CHARACTERS AND FUNCTIONS SHOWN WITH SHADED BACKGROUNDS HAVE 8N BIT MARKing.  
UPON RECEIVING CODE COMBINATIONS FOR "THROUGH", MONOCASE EQUIPMENT SUCH AS MODELS 30 AND 35 POINT RESPECTIVE CHARACTERS @ THROUGH ^.

Fig. 31-2. American Standard Code for Information Interchange (ASCII) chart (courtesy of American Radio Relay League Inc.).

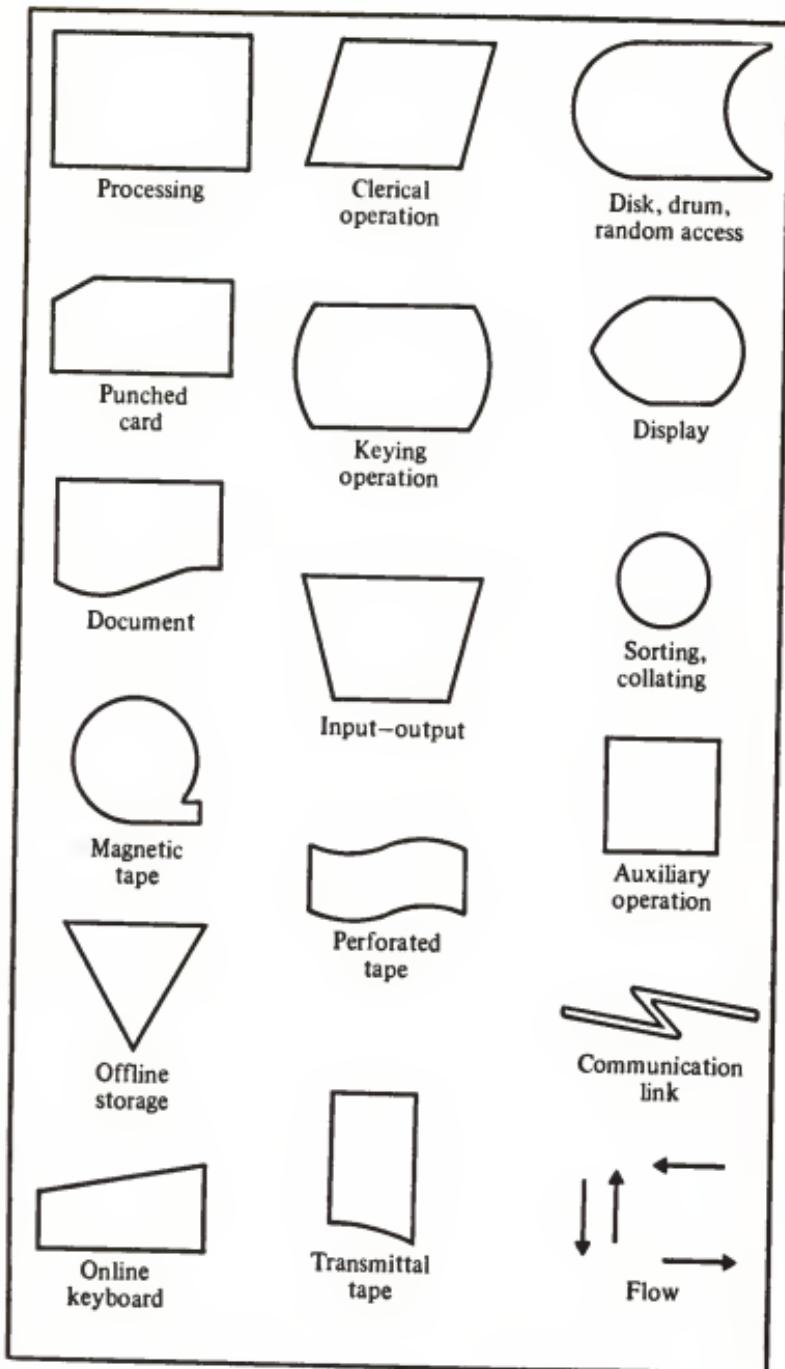


Fig. 31-3. System Flowchart Symbols

Table 31-2. International Morse Code

A	— — — —	Period	— — — — —
B	— — — — —	Comma	— — — — — —
C	— — — — — —	Colon	— — — — — — —
D	— — — — — —	Question mark, or request for repetition of a transmission	— — — — — — — —
E	—	not understood	— — — — — ?
F	— — — —	Apostrophe	— — — — — ’
G	— — — — —	Dash or hyphen	— — — — — — —
H	— — — — — —	Fraction bar	— — — — — — /
I	— —	Parenthesis (before and after words) ()	— — — — — — — —
J	— — — — —	Underscore (before and after words or part of sentence)	— — — — — — — —
K	— — — — —	Equal sign	— — — — =
L	— — — — —	Understood	— — — — —
M	— — — — —	Error	— — — — — —
N	— — — — — —	Cross or end-of-telegram or end- of-transmission signal	— — — — — — —
O	— — — — — —	Invitation to transmit	— — — — — — —
P	— — — — — —	Wait	— — — — — — —
Q	— — — — — —	End of work	— — — — — — —
R	— — — — — —	Starting signal (beginning every transmission)	— — — — — — —
S	— — — — —	Separation signal for transmission of fractional numbers (between the ordinary fraction and the whole number to be trans- mitted) and for groups con- sisting of figures and letters (between the figure-groups and the letter-groups)	— — — — — — — —
T	—		
U	— — — —		
V	— — — — —		
W	— — — — — —		
X	— — — — — —		
Y	— — — — — —		
Z	— — — — — —		
Ä (German)	— — — — —		
Å or Å (Spanish-Scandi- navian)	— — — — — —		
CH German-Spanish	— — — — — — —		
É (French)	— — — — —		
Ñ (Spanish)	— — — — — — —		
Ö (German)	— — — — — — —		
Ü (German)	— — — — — — —		
1	— — — — —		
2	— — — — — —		
3	— — — — — — —		
4	— — — — — — —		
5	— — — — — — — —		
6	— — — — — — — —		
7	— — — — — — — —		
8	— — — — — — — —		
9	— — — — — — — —		
0	— — — — — — — —		

## PHONETIC ALPHABET

To avoid a misunderstanding when words must be spelled or when call letters must be clearly identified, words are used in place of each of the letters. Syllables in italics are emphasized. See Table 31-3.

### □Example:

W2CDV would be spoken as W2 Charlie Delta Victor.

Table 31-3. Phonetic Alphabet.

Letter	Code Word	Pronunciation
A	Alfa	AL FAH
B	Bravo	BRAH VOH
C	Charlie	CHAR LEE
D	Delta	DELL TAH
E	Echo	ECK OH
F	Foxtrot	FOKS TROT
G	Golf	GOLF
H	Hotel	HOH TELL
I	India	IN DEE AH
J	Juliett	JEW LEE ETT
K	Kilo	KEY LOH
L	Lima	LEE MAH
M	Mike	MIKE
N	November	NO VEM BER
O	Oscar	OSS CAH
P	Papa	PAH PAH
Q	Quebec	KEH BECK
R	Romeo	ROW ME OH
S	Sierra	SEE AIR RAH
T	Tango	TANG GO
U	Uniform	YOU NEE FORM
V	Victor	VIK TAH
W	Whiskey	WISS KEY
X	X-ray	ECKS RAY
Y	Yankee	YANG KEY
Z	Zulu	ZOO LOO

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