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HANDBOOK OF PIEZOELECTRIC CRYSTALS FOR RADIO EQUIPMENT DESIGNERS

John P. Buchanan
Philco Corporation
October 1956


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Sincerely yours


# PIEZOELECTRIC CRYSTALS 

## FOR

## RADIO EQUIPMENT DESIGNERS

This Report Supersedes WADC TR 54248, Dated December 1954

Johe P. Buchaman

## Phileo Corporation



## HANDBOOK

OF
PIEZOELECTRIC CRYSTALS
FOR

# RADIO EQUIPMENT DESIGNERS 

This Report Supersedes WADC TR 54-248, Dated December 1954

John P. Buchanan<br>Philco Corporation

OCTOBER 1956

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This Task No. 43033, titled Handbook of Piezoelectric Crystals for Radio Equipment Designers, ARDC Project 4155 was administered under Mr. V. J. Carpantier as chief of the Specialties Section, Communication Branch of the Communications and Navigation Laboratory, Wright Air Development Center.

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A comprehensive manual of piezoelectric control of radio frequencies is offered. It is directed toward the design of oscillator circuits having optimum operating conditions when employing Military Standard crystal units. Included is a survey of the development of the piezoelectric crystal art; descriptions and characteristics of all crystal elements and mounting methods that have found commercial application; a detailed study of the equivalent circuit characteristics of crystal units; analyses of basic piezoelectric oscillator principles and of the effects of changes in various circuit parameters, using the Pierce oscillator as a reference circuit; analyses and recommended design procedures for all types of piezoelectric oscillator circuits used, or tested for use, in USAF equipments; schematic diagrams and tables giving actual circuit parameters of all available nonclassified piezoelectric oscillators now being used in USAF equipments; descriptions of all crystal units and crystal holders now being used in USAF equipments, containing references and schematics of circuits employing those crystal units recommended for equipments of new design; a brief discussion of crystal ovens and descriptions of ovens currently available for use with Military Standard crystal units; and a comprehensive index to increase the utility of the handbook as a reference manual. Circuit analyses, derivations of equations, and suggestions for design innovations whose sources are not directly acknowledged have originated with the author and so far as is known have not been specifically confirmed in practice.

## PUBLICATION REVIEW

This report has been reviewed and is approved.
FOR THE COMMANDER:


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## SECTION |_GEENERAL INFORMATION

## INTRODUCTION

## PURPOSE AND SCOPE OF MANUAL

1-1. The purpose of this manual is to provide the design and developmental engineer of military electronic equipment with a reference handbook containing background material, circuit theory, and components data related to the application of piezoelectric crystals for the control of radio frequencies.
1-2. This manual is composed of the following sections:

## I. GENERAL INFORMATION

II. CRYSTAL UNITS
III. CRYSTAL HOIDERS
IV. CRYSTAL OVENS

## V. APPENDIXES

1-3. Section I contains a brief historical account of the discovery of the piezoelectric effect and of the application of crystal resonators as frequencycontrol devices, discussions covering the theory and physical properties of piezoelectric crystals, descriptions and performance characteristics of the more important quartz crystal elements, general discussions of the various crystal-unit fabrication processes and types of mounting, detailed discussions of the equivalent electrical parameters and performance characteristics of crystal units, and comprehensive qualitative and mathematical analyses of the various types of crystal oscillators, summarized with recommended design procedures. 1-4. Sections II, III, and IV provide the technical and logistical data, and information concerning the application of the crystal units, crystal holders, and crystal ovens currently recommended for use in equipments of new design.
1-5. The Appendixes contain the acknowledgments; a bibliography; a list of manufacturers associated with the piezoelectric crystal industry; a list of related U. S. Government specifications, standards, and publications; a table of definitions for the abbreviations and symbols used in the Handbook; conversion charts ; and an alphabetical index.

## CONTROL OF RADIO FREQUENCY

1-6. The greatly increased demand for military radio channels, with the consequent crowding of
the radio-frequency spectrum, is, in the final analysis, a problem for the design engineer of fre-quency-control circuits. The problem is essentially one of providing a maximum frequency stability of the carrier at the transmitting station, and a maximum rejection of all but the desired channel at the receiving station. In each instance optimum results are obtained by the use of electromechanical resonators - maximum carrier stability is achieved by the use of crystal master oscillators, and maximum receiver selectivity is achieved by the use of crystal heterodyne oscillators and crystal band-pass filters.
1-7. The design of a constant-frequency generator has been an ideal of radio engineers almost from the beginning of radio science. Although many purely electrical oscillators have been devised which closely approach the ideal, none surpass the performance of the high-quality circuits employing mechanical oscillators. Temperature-controlled oscillators having a sonic-frequency tuning fork as the frequency controlling element and followed by a number of frequency multiplying stages were the first of the radio-frequency generators employing the high precision of mechanical control. The cumbersomeness and expense of the many multiplier stages, however, have made the tuning fork oscillators impracticable insofar as the control of any but sonic frequencies are concerned. Today, precision control of radio frequencies has been made possible through the development of piezoelectric resonators, where the frequency-controlling elements, usually quartz plates, have normal vibrations in the radio-frequency range.

## THE PIEZOELECTRIC EFFECT

1-8. The word piezoelectricity (the first two syllables are pronounced pie-ee") means "pressureelectricity," the prefix piezo- being derived from the Greek word piezein, meaning "to press."
1-9. "Piezoelectricity" was first suggested in 1881 by Hankel as a name for the phenomenon by which certain crystals exhibit electrical polarity when subjected to mechanical pressure.
1-10. That such a phenomenon probably existed seems to have been suggested first by Coulomb in
the latter part of the 18th century. His suggestions prompted Haüy, and later A. C. Bequerel, into undertaking a series of experiments to see if electric effects could be produced purely by mechanical pressure. Although both Haüy and Bequerel reported positive results, there is some doubt as to whether these were not due to contact potentials rather than to piezoelectric properties of the substances investigated-particularly since electrical polarities were reported in crystals that are now known to be non-piezoelectric.
1-11. It is to the Curie brothers, Jacques and Pierre, that the honor goes for having been the first (in 1880) to verify the existence of the piezoelectric effect. (For the initial report of their discovery, see paragraph 1-56.)
1-12. The Curie brothers tested a number of crystals by cutting them into small plates that were then fitted with tin-foil electrodes for connection to an electrometer. When subjected to mechanical pressure, several of the crystals caused the leaves of the electrometer to be deflected. Among those crystals showing electrical polarities were quartz, tourmaline, Rochelle salt, and cane sugar. In the year following these experiments, a prediction by Lippmann that the effect would prove reversible prompted the Curies to further investigations. The results verified Lippmann's prediction by revealing that the application of electric potentials across a piezoelectric crystal would cause deformations in the crystal which would change in sign with a change in electric polarity. Furthermore, it was found that the piezoelectric constant of proportionality between the electrical and mechanical variables was the same for both the direct (pres-sure-to-electric) and the converse effects. In other words, the same polarization at the surface of the electrodes that results from a particular deformation of the crystal can, in turn, if applied from an external source, produce the deformation.
1-13. It should be mentioned that the piezoelectric effect, which occurs only in certain asymmetrical crystals, is not to be confused with electrostricture, a property common to all dielectrics. Although electrostricture is a deformation of a dielectric produced by electric stress, it is unlike the converse piezoelectric effect in that its magnitude varies, not linearly with the electric field, but with the square of the field, and is unaffected by a change in the applied polarity. Electrostricture is the type of deformation a capacitor undergoes on being charged. In piezoelectric crystals this effect is normally small compared with the piezoelectric properties.

## DEVELOPMENT OF PIEZOELECTRIC DEVICES

1-14. From the time of its discovery until World War I, the piezoelectric effect found few practical uses. Those applications it did find appeared in the form of occasional laboratory devices for measuring pressure or electric charges. For the most part, however, little attention was attracted to piezoelectricity outside the crystallographer's study. Nevertheless, during this time considerable theoretical progress was made, due chiefly to the efforts of Lord Kelvin, Duhem, Pockels, and Woldmar Voigt. Voigt's comprehensive Lehrbuch der Kristallphysik, published in 1910, is still considered the reference authority on the mathematical relationships among crystal variables.
1-15. It was after the outbreak of World War I before serious attention was given to the practical application of piezoelectric crystals. During the war Professor Paul Langevin of France initiated experiments with the use of quartz crystal plates as underwater detectors and transmitters of acoustic waves. Although Langevin's immediate purpose was to develop a submarine detecting device, his research became of vital importance to many other developments. Not only did it attract the applied sciences to the possibilities of piezoelectric crystals, but also it initiated the modern science of ultrasonics.
1-16. The detecting apparatus that Langevin eventually devised employed quartz "sandwiches" which were coupled electrically to vacuum-tube circuits, and could be exposed under water where they would vibrate at the frequency of an applied voltage, or at the frequency of an incident acoustic wave. The first function was employed to emit ultrasonic waves, and the second function to receive and reconvert the echo into electrical energy for detection.
1-17. At the same time that Langevin was experimenting with quartz as a supersonic emitter and detector, Dr. A. M. Nicolson, at Bell Telephone Laboratories, was independently investigating the use of Rochelle salt to perform the same functions at sonic frequencies. Indeed, his first application for a patent on a number of piezoelectric acoustic devices, April 1918, preceded by five months Langevin's initial application for a French patent. Employing Rochelle salt instead of quartz, because of its greater piezoelectric sensitivity, Nicolson constructed a number of microphones, loudspeakers, phonograph pickups, and the like. Among the circuits included in his 1918 patent application, was one that later proved of particular interest - an oscillator employing a Rochelle
salt crystal as shown in figure 1-1. With this exception, all the early applications of the piezoelectric crystal involved its use as a simple electromechanical transducer. That is, it was used either to transform mechanical energy in one system to electrical energy in another, or vice versa. Nicolson's oscillator was a distinct innovation in that it employed a piezoelectric crystal as a transformer of electrical energy to mechanical energy and back to electrical energy.
1-18. When Nicolson devised his oscillator, none of the possible functions of a piezoelectric vibrator had previously been investigated or discussed. His patent application offered no description of the crystal's function, although presumably the crystal performed in some way to transfer part of the plate circuit energy to the grid circuit. Evidence that the normal vibrations of the crystal actually controlled the frequency seems to have existed, but no mention was made of this fact. The circuit, however, embodies the combined principles of coupler, filter, and resonator. Obviously the crystal acts as a coupler between the plate and grid circuits; and, inasmuch as the crystal may block the feedback of all plate energy except that at the frequency of the crystal's normal mode of vibration, the crystal may be imagined to perform the function of a filter, even though the over-all operation is that of an oscillator. Finally, if the plate
tap is connected at the bottom of the coil, so that the only feedback is through the plate-to-grid capacitance of the vacuum tube, the crystal may function as a conventional resonator, controlling the frequency as would a tuned grid tank circuitthe complete vacuum-tube circuit being the equivalent of a tuned-plate, tuned-grid oscillator. Thus, to Dr. Nicolson belongs the honor of being the first to employ the piezoelectric crystal purely as a circuit element, in all its principal circuit functions. 1-19. Although Nicolson was the father of the piezoelectric crystal circuit, Professor Walter G. Cady, of Wesleyan University, was its greatest prophet. In 1918 during a series of experiments being conducted to investigate the use of Rochelle salt plates for underwater signaling, Dr. Cady became interested in the electromechanical behavior of crystals vibrating in their normal modes. Out of the resonant properties that he discovered, he came to visualize the great possibilities that the piezoelectric crystal afforded as a resonator of high stability. After experimenting with several circuits, including the first quartz-controlled oscillator, Dr. Cady, in January 1920, not aware that Dr. Nicolson considered his oscillator controlled by the resonance of its crystal, submitted a patent application for the piezoelectric resonator, in which he reported its possibilities as a frequency standard, filter, and coupler, and described the principles


Figure 1-1. The first crystal- (Rochello salt) controlled oscillator. Invented by A. M. Nicolson, 1918
of its operation. Although subsequent litigation concerning the discovery of the piezoelectric-resonator principle was decided in Dr. Nicolson's favor, it is distinctly to Dr. Cady's credit that he was the first to fully grasp the import of the piezoelectric resonator and to publish a public report of its principles and possibilities. His early pioneering in the field and his many later contributions have made Dr, Cady the American dean of piezoelectricity.
1-20. It soon became apparent that quartz crystals were the most stable and practical for use as resonators. Many investigators were attracted to the field, and progress was made both in the design and theory of crystal circuits. Professor G. W. Pierce of Harvard showed that quartz crystal oscillators could be constructed with a single amplifier stage, as Nicolson had already done using Rochelle salt. This marked a considerable improvement over Cady's oscillators, which had consisted of two or more vacuum-tube stages. Of particular note was the analysis by K. S. Van Dyke, in 1925, of the electrodynamic characteristics of a crystal resonator in terms of an equivalent electrical network; for the first time a way was opened to an understanding of the crystal resonator. In 1928, E. M. Terry showed that the frequency of a crystal oscillator was not entirely controlled by the crystal characteristics, but to a small degree was also dependent upon the other circuit constants. F. B. Llewellyn, in 1931, presented a classic analysis of oscillators showing the circuit impedance relationships that are necessary if the frequency is to be independent of variations in the voltage supply and vacuum-tube characteristics. Although the subject matter of this treatise deals with oscillators in general, the principles are applicable to the design of crystal oscillators, if the electrical parameters of the crystal are known.
1-21. The tuned-circuit oscillators of the early transmitters normally operated with heavy and variable loads. Many of the oscillators operated directly into an antenna, and in broadcast transmitters, modulation was performed in the oscillator stage. This resulted in considerable frequency instability, and broadcast reception was often unintelligible because of the frequency difference in radio waves arriving by different paths. It was in the determination of the cause and the correction of such interference that Messrs. R. Bown, D. K. Martin, and R. K. Potter of the Research and Development Department of the American Telephone and Telegraph Company recommended the use of lightly loaded crystal-controlled oscillators followed by amplifiers. Under their supervision, Station WEAF in New York, in 1926, became the first
crystal-controlled broadcasting station.
$1-22$. The principal factor limiting the stability of the early quartz oscillator was the relatively large frequency-temperature coefficient of the crystal, which allowed small changes in the ambient temperature to cause excessive changes in the resonant frequency. The immediate method of obtaining stability, of course, was to mount the crystal in an oven where the temperature could be controlled thermostatically. However, to decrease the temperature coefficient of the crystal, itself, also became the goal of a number of researchers. Because some quartz plates exhibited positive temperature coefficients, whereas others exhibited negative coefficients, according to the orientation of the plate with respect to the axes of the mother crystal, the possibility arose that there should be some shape or median angle of cut which would have a zero coefficient. The first empiricists to enter the field were E. Giebe and A. Scheibe in Germany. In the United States, Mr. W. A. Marrison of Bell Telephone Laboratories turned his attention to the problem of achieving the maximum precision possible in frequency control, and by 1929 had perfected a $100-\mathrm{kc}$ frequency standard using a doughnut-shaped crystal (originally pioneered by Giebe) with a nearly zero temperature coefficient. This success encouraged the Bell Laboratories research staff to launch a concerted investigation into all phases of quartz crystal physics. Out of this program have arisen most of the principal advances in the design and production of quartz crystal units in the United States; although the early pioneering of S. A. Bokovoy and C. F. Baldwin at RCA has also been of notable significance.
1-23. Originally only the Curie, or X-cut, quartz plate was used-a plate in which the thickness dimension is parallel to the crystal's X axis. Later the $Y$ cut, where the thickness dimension is parallel to a Y axis, developed by E. D. Tillyer of the American Optical Co., began to compete with the Curie cut as the frequency-control element in commercial oscillators. By 1934, Messrs. F. R. Lack, G. W. Williard, and I. E. Fair of Bell Telephone Laboratories announced the discovery and development of two types of plates, called the $A T$ and $B T$ cuts, with such small temperature coefficients that they could operate stably under normal conditions without the use of temperature-controlled ovens. Concurrently, Bokovoy and Baldwin at RCA were experimenting with a series of crystals that they named the V cut, and their work, although of a less rigorous theoretical approach, substantially paralleled much of the research that was done at

Bell Laboratories. In 1937, Messrs. G. W. Williard and S. C. Hight announced the development of the CT, DT, ET, and FT cuts; and by 1940 Mr. W. P. Mason had discovered the GT cut, the most stable resonator ever devised. The time-keeping standards at both the Greenwich Observatory and the U. S. Bureau of Standards now use this crystal. Where other cuts exhibit a zero temperature coefficient only at certain temperatures, the GT cut has almost a zero temperature coefficient over a range of $100^{\circ} \mathrm{C}$. Besides the cuts discussed above, a number of others have been investigated which have proved particularly applicable for special uses. Among these are the AC, BC, MT, NT, 5degree $X$, and the -18 -degree $X$ cuts.
1-24. Paralleling the development of the new crystal cuts were the improvements made in the design of crystal holders. The early holders provided no means of "clamping" a crystal, for they were designed originally to accommodate X-cut plates whose favored modes of vibration required that the edges be free to move. Since the crystal in such a holder will slide about if used in equipment subject to mechanical vibrations, a method of clamping was needed before the crystal could be used in vehicular or airborne radio sets. Mr. G. M. Thurston of Bell Telephone Laboratories was led to the solution of this problem when he discovered that a crystal would not be restricted if clamped only at the mechanical nodes of its normal vibrations. The exact positions of these points, where the standing-wave amplitude is zero, depend, of course, on the particular mode of vibration. The low-frequency - 18 -degree X-cut crystal, for instance, can be held by knife-edged clamps running along its center, whereas AT- and BT'-cut crystals can be clamped at their corners. Cantilever and wire supports which resonate at the crystal frequency have been devised for holding crystals at their centers. Although the mounting of crystals requires a far more exacting technique than for-
merly, the crystal holder today provides support and protection sufficient to insure high performance stability, even under the severe conditions of vibration that exist in military aircraft and tanks. 1-25. Unfortunately, the extremely critical nature of the design and production of crystal units has made it impracticable for manufacturers to massproduce units with such exactitude that all the equivalent electrical parameters are standardized with an accuracy comparable to that now achieved in the case of vacuum tubes or other circuit components. However, definite progress has been made in this direction, and, if the need warrants the additional cost, reasonably exact characteristics may be obtained. For several years, each crystal unit had to be tested in a duplicate of the actual circuit in which it was to be used. This procedure was disadvantageous from the points of view of both the radio design engineer and the crystal manufacturer. On the one hand, the radio engineer, knowing little more than the nominal frequency of the crystal unit to be installed in his circuit, could not achieve that degree of perfection in oscillator design which was otherwise theoretically possible. On the other hand, the task of making a given oscillator perform correctly effectively became the responsibility of the crystal manufacturer, since it was necessary for him to fit each crystal unit by trial and error to the particular circuit for which it was intended. In recent years this cut-and-try procedure has been alleviated considerably by the development of standard test sets and by improvements in production techniques that permit more critical specifications. It is hoped that this handbook, by providing a more comprehensive description of the technical characteristics of the crystal units recommended for new design, will contribute in removing the limitations that too often in the past have forced the practical design engineer to approach his crystal circuits philosophically, rather than scientifically.

## PHYSICAL CHARACTERISTICS OF PIEZOELECTRIC CRYSTALS

## descriptions of USEFUL piezoelectric CRYSTALS

1-26. The piezoelectric effect is a property of a non-conducting solid having a crystal lattice that lacks a center of symmetry. Of the 32 classes of symmetry in crystals, 20 are theoretically piezoelectric, and the actual crystals which have been found in this category are numbered in the low hundreds.

1-27. Until the time of World War II only three crystals were commercially employed for their piezoelectric properties - quartz, Rochelle salt, and tourmaline. Today, the number is being increased by the development and application of synthetic crystals. Of these, the principal ones used in frequency selective circuits are ethylene diamine tartrate (EDT), dipotassium tartrate (DKT), and ammonium dihydrogen phosphate (ADP). See figure 1-2.

## Physical Characteristics of Piezoelectric Crystals



Figure 1-2. Commercially used piezoeloctric crystals other than quartz

1-28. Piezoelectricity is still in its infancy, and until more data have been collected and coordinated into a comprehensive atomic theory of the phenomenon, the chemist will have few clues to direct his search for a crystal having the maximum possible piezoelectric effect.

## Tourmaline

1-29. Tourmaline is a semiprecious stone which at one time was called the "Ceylon Magnet." This title seems to have been given it by early 18 th century traders who introduced the stone to Europe, with the story of its strange magnetic property. If placed in hot ashes, tourmaline behaves as if it were electrified-first attracting ashes and then throwing them off. This is the phenomenon of pyroelectricity, closely associated with piezoelectricity, and was possibly the first electrical effect, other than lightning and St. Elmo's fire, ever to be noticed by man. According to the theory proposed by Lord Kelvin, the pyroelectric effect of tourmaline is due to a permanently polarized lattice in the crystal, so that when heated, an unneutralized increase in the dipole moment occurs, proportional to the change in temperature and the coefficient of expansion. It was this pyroelectric theory of permanently polarized crystals that eventually prompted the Curie brothers to test for the piezoelectric effect.
1-30. Tourmaline is unsuitable for wide commercial use because of its expense and the scarcity in the number of large-sized natural crystals. Also, the temperature coefficients are negative for all tested modes of vibrations, which fact rules out the possibility of zero-coefficient cuts.
1-31. Tourmaline does have the advantage of durability and a large thickness-frequency coefficient, so that for a given frequency it permits a more rugged crystal unit than quartz. For this reason it is sometimes used for the control of very high frequencies. However, the chief piezoelectric application of tourmaline is in the measuring of hydrostatic pressures.

## Rochelle Salt

1-32. Rochelle salt ( $\mathrm{NaKC}_{4} \mathrm{H}_{4} \mathrm{O}_{4}-4 \mathrm{H}_{2} \mathrm{O}$ ) is sodium potassium tartrate with four molecules of water of crystallization. The crystals are grown commercially by seeding saturated solutions of the salt and decreasing the temperature of the solutions a few tenths of a degree per day. They were first synthesized in 1672 by Pierre Seignette, an apothecary of La Rochelle, France, and until the time of Nicolson's inventions the salt was used primarily for its
medicinal value. Its exceptionally great piezoelectric effect-a blow with a hammer can generate as much as five thousand volts-has made Rochelle salt the principal crystal for use as a transducer in acoustic devices, such as microphones, loudspeakers, pickups, hearing aids, and the like. As a stable resonator it is far inferior to quartz, not only because of a greater sensitivity to temperature variations, but also because of its tendency to disintegrate during extremes of humidity. If the ambient humidity drops below 35 per cent at room temperature, the water of crystallization will begin to evaporate, leaving a dehydrated powder on the crystal surface. Should the humidity rise above 85 per cent at room temperature, the salt will absorb moisture and begin to dissolve. For these reasons a Rochelle salt crystal should be mounted in a hermetically sealed container, or, if this is not possible, at least coated with wax. In the case of the former, if powders of both the crystalline and dehydrated forms of Rochelle salt are also enclosed within the sealed chamber, the humidity of the chamber will automatically increase or decrease with corresponding changes of temperature, and a stable balance between the crystal and chamber vapor pressures will be maintained. However, at a temperature of $55^{\circ} \mathrm{C}\left(130^{\circ} \mathrm{F}\right)$ the crystal, which is a double salt of tartaric acid, breaks down into sodium tartrate, potassium tartrate, and water. The solution formed will remain a viscous liquid for some time if super-cooled, and, as such, makes an effective glue for binding together plates of the crystal.
1-33. Although Rochelle salt, between the temperatures of $-18^{\circ} \mathrm{C}$ and $+24^{\circ} \mathrm{C}$, has a greater piezoelectric effect than any other crystal, it seems that eventually it will be replaced by other synthetic crystals, in particular, $\mathrm{ADP}\left(\mathrm{NH}_{4} \mathrm{H}_{2} \mathrm{PO}_{4}\right)$, which requires no water of crystallization. Nevertheless, as an electromechanical transducer, Rochelle salt is still the most widely used of the piezoelectric crystals.

## ADP

1-34. ADP $\left(\mathrm{NH}_{4} \mathrm{H}_{2} \mathrm{PO}_{4}\right)$, ammonium dihydrogen phosphate, was discovered and used during World War II as a substitute for Rochelle salt in underwater sound transducers. Like Rochelle salt, ADP crystals can be grown commercially; but unlike Rochelle salt, it requires no water of crystallization, and hence has no dehydration limitations, being able to stand temperatures up to $100^{\circ} \mathrm{C}$ ( $212^{\circ} \mathrm{F}$ ). Also, ADP is more durable mechanically than Rochelle salt.
1-35. Although the crystal's principal application

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has been in submarine-detecting apparatus, its greater stability suggests the probability that it will eventually replace Rochelle salt as the principal transducer in other sonic devices.

## EDT

1-36. EDT $\left(\mathrm{C}_{6} \mathrm{H}_{14} \mathrm{~N}_{2} \mathrm{O}_{6}\right)$, ethylene diamine tartrate, was discovered and developed during World War II as a substitute for quartz in low-frequency filter units. Quartz crystals at this time were in such great demand for the frequency control of military communication equipment, that a shortage developed in the supply of large-sized natural crystals which were needed for cutting filter plates of $11 / 2$ to 2 inches in length. This shortage was acutely felt in the telephone industry, where there exists the chief demand for such plates for use in the band-pass filters of carrier systems. The discovery of EDT was the solution to this problem, for this crystal can be grown to any size desired, and it has the chemical stability (no water of crystallization), low mechanical loss, zero temperature coefficient, and small aging effects that make it a suitable substitute for quartz.
1-37. EDT is not as rugged mechanically, nor does it have quite as high a $Q$ as quartz-although the EDT crystal units operating as filter elements in the 20 - to $180-\mathrm{kc}$ range do have Q's in the neighborhood of 30,000 . Moreover, for use as the frequencycontrol element in high-frequency oscillators, EDT is inferior to quartz because of its greater sensitivity to temperature changes. Even though high-frequency modes of vibration have been found with zero temperature coefficients, the temperature shift to either side of the optimum value must be kept approximately one-fifth that for a comparable quartz plate (BT cut, for example) in order to maintain the same frequency tolerance. Where only a minimum of temperature control might be needed for quartz, EDT will require fairly accurate control. Because of these disadvantages, EDT does not threaten at this time to replace quartz in high-frequency oscillators, but it does have promising possibilities for use in oscillators of the frequency-modulated type. Here, EDT plates have the advantage of a relatively wide gap between their resonant and antiresonant frequencies, thus permitting a large percentage swing of the oscillator frequency. If temperaturecontrolled, the EDT crystal can thus give crystal stability to a frequency-modulated transmitter.

## DKT

1-38. DKT ( $\mathrm{K}_{2} \mathrm{C}_{4} \mathrm{H}_{4} \mathrm{O}_{6}-1 / 2 \mathrm{H}_{2} \mathrm{O}$ ), dipotassium tartrate, is another synthetic crystal which was in-
vestigated at Bell Telephone Laboratories during World War II. The DKT molecule is similar chemically to that of Rochelle salt except that the sodium atom has been replaced by another potassium atom. The crystal, however, differs from Rochelle salt in that it contains only one molecule of water for each two DKT molecules, as compared with a water-to-salt molecular ratio of four-to-one in the Rochelle salt crystal, and it exhibits no tendency to dehydrate below $80^{\circ} \mathrm{C}\left(176^{\circ} \mathrm{F}\right)$. Also, the piezoelectric characteristics of DKT are less like those of Rochelle salt than of quartz. Indeed, in the lower-frequency filter circuits, DKT seems as promising as EDT as a substitute for quartz.
1-39. As compared with EDT, DKT has the advantage of better temperature-frequency characteristics. Zero temperature coefficients are possible where the frequency deviation on either side of the zero point is only one-third that for EDT. However, DKT crystals are more difficult to grow than the EDT crystals, and primarily for this reason the development of a small EDT industry has already been established, whereas the DKT crystals are still in the laboratory stage.

## Raw Puartz

1-40. Quartz is silicon dioxide ( $\mathrm{SiO}_{2}$ ) crystallized in hard, glass-like, six-sided prisms. The normal crystal structure is called alpha quartz; if the temperature is raised above $573^{\circ} \mathrm{C}\left(1063^{\circ} \mathrm{F}\right)$ most of the piezoelectric property is lost with a crystal transformation to beta quartz. At $1750^{\circ} \mathrm{C}$ ( $3182^{\circ} \mathrm{F}$ ) the crystal structure is permanently lost, and the melted quartz assumes the fused amorphous form of silica. The density of alpha quartz at $20^{\circ} \mathrm{C}\left(68^{\circ} \mathrm{F}\right)$ is 2.649 grams per cubic centimeter. The hardness of quartz is rated at 7 on Mohs' scale-a greater hardness than glass or soft steel, but less than hard steel.
1-41. Silicon dioxide is believed to constitute approximately one-tenth of the earth's crust. It occurs in many crystalline forms such as quartz, flint, chalcedony, agate, onyx, etc., and in the fused amorphous state of silica, called "quartz glass." Although quartz is an abundant mineral-sand and sandstone consist largely of quartz granuleslarge crystals of good quality are to be found in only a few areas. The chief source of supply has been Brazil, although large deposits of lower quality are also to be found in Madagascar and in the United States. Progress has been made in growing quartz crystals artificially. Such crystals are now commercially available, although this quartz source is still primarily in the developmental stage. The tremendous pressures required
and the slow rate of growth have, until very recently, prevented quartz manufacture from being commercially feasible. Advances are now being made in growing imperfection-free quartz stones having major dimensions so oriented relative to the principal crystal axes that a desired type of quartz cut can be obtained with minimum waste. The future possibilities of quartz manufacture appear quite promising.
1-42. The large quartz crystals of geological origin are the products of long ages of growth under great pressure. The growing crystal assumes the shape of a hexagonal prism with each end pyramiding to a point. The prismatic faces are designated as $m$ faces, see figure 1-4, and adjacent $m$ faces always intersect at angles of 120 degrees. The opposite $m$ faces of the prism are always parallel, but are rarely of the same dimensions. These faces are not perfectly planar, but are streaked with small horizontal growth lines, or striae. Parallel to the growth lines are the bases of the six end faces -three $r$ and three $z$ faces-which form a hexagonal pyramid, but with only the $r$ faces meeting at the apex. The end faces are quite smooth, with the $r$, or major, faces usually appearing more polished than the z , or minor, faces. Figure 1-3 shows a mother crystal with one of the pyramidal ends missing. Complete crystals are rarely found except in very small sizes. More likely both pyramidal ends will be missing, and frequently crystals are


Figure 1-3. Raw quartz stone
found with all the natural faces broken or eroded away. The largest quartz crystal that has been recorded was found in Brazil. It is described as a crystal of smoky quartz, 7 ft 2 in . long, 11 ft 2 in . in circumference, and weighing more than 5 tons. 1-43. Quartz is enantiomorphous-that is, it occurs in both right-handed and left-handed forms, which are mirror images of each other. The enantiomorphic faces of two ideal alpha-quartz crystals are represented in figure 1-4. The lefthanded and right-handed forms are indicated by the direction in which the small upper x and s faces appear to be pointing. Note that this rule is valid regardless of which end of the crystal is turned up. However, the x and s faces are rarely found, so that the handedness of a crystal is usually determined by noting the optical effects when polarized light is passed through the crystal parallel to the optic (lengthwise) axis.

## IMPERFECTIONS IN QUARTZ

1-44. Pure quartz of structural perfection is a transparent, colorless crystal-such that the early Greek physicists believed it to be a perfected form of ice. Through the centuries quartz has been cut and ground into many ornaments, and was mystically respected in the ancient art of crystal gazing. $1-45$. The presence of impurities can convert quartz into a variety of gem-like colors. Amethyst, agate, and jasper are all quartz crystals colored by impurities. A different form of coloring is that which gives a smoky appearance to quartz. This effect differs in degree from crystal to crystal, and in extreme cases a crystal may be so dark that it cannot be inspected for defects nor for the alignment of axes. However, by heating a smoky crystal from $350^{\circ} \mathrm{C}\left(662^{\circ} \mathrm{F}\right)$ to $500^{\circ} \mathrm{C}\left(932^{\circ} \mathrm{F}\right)$ it becomes


Figure 1-4. Left and right quartz crystals

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quite as clear as the purest stone. Possibly the coloration is due to the dissociation of some of the silicon dioxide molecules, which recombine on heating; in any event, crystals which have been cleared of smokiness, remain clear, and have the same physical properties as the normal colorless crystals. $1-46$. Other than those arising from chemical impurities, there are three types of structural defects to be avoided when cutting blanks from the raw quartz. These are cracks, inclusions, and twinning.

## Cracks

1-47. All raw crystals contain cracks to some extent, particularly near their surfaces, where fractures are easily caused by impacts. Temperature variations and growth conditions are also causes of cracking. The larger cracks are readily visible, but not the separations with dimensions comparable to a wave-length of light. For this reason, any detected crevice should be assumed to extend somewhat beyond its visible length. Raw quartz should be handled with particular care, for the large crystals are more vulnerable to fracturing than are the small finished plates. No finished plate, however, should be permitted to contain a crack.

## Inclusions

1-48. Inclusions are small pockets, often submicroscopic, holding foreign matter which was entrapped during the crystal's period of growth. The trapped material may be a gas, liquid, solid, or any combination thereof. The pockets are often too small to be seen individually, but are readily detected by the shapes and coloring of the clusters
they form. Groups of the smallest-size inclusions have a bluish cast; groups of medium-size inclusions appear as a white frosting; and the larger inclusions are individually visible as small bubbles. Some of the clusters appear as small clouds; others appear as needles, which may be fine or feathery, and which may form parallel rows or spread comet-like from a bubble origin; still other groups are draped in sheets or folds like veils; and, finally, there are those inclusions that arrange themselves in surfaces parallel to the natural crystal faces, outlining former growths, and appearing as crystal phantoms within a crystal. See figure 1-5. Not a great deal is known concerning the effect of inclusions upon the performance of finished plates. However, the fine textured (blue) inclusions are the least objectionable, and the isolated bubbles are more to be tolerated than a veil or phantom. Blue needles are permissible in large, low-frequency plates that are not to be driven at high levels. Nevertheless, any inclusion weakens a crystal, and will not be present in a high-quality, finished plate.

## Twinning

1-49. Twinning is the intergrowth of two crystal regions having oppositely oriented axes. This abnormality is rarely detectable by a casual visual inspection, and a crystal that appears homogeneous throughout may, indeed, have several twinned areas; in fact, almost all large crystals have twinning to some extent. There are two types of twinning common to quartz-electrical twining and optical twinning. In electrical twinning, only the electrical sense of the crystal axes is reversed, whereas in optical twinning, not only the electrical sense, but the handedness of the crystal


Figure 1-5. Quartz crystal containing inclusions and fractures*
structure is reversed-that is, one area will be right-handed and the other left-handed.
1-50. A finished plate, if it is to have predictable characteristics, must be cut entirely from a region having the same crystal structure; otherwise, the piezoelectric properties of one region will interfere with those of the other. Electrical twins are usually large, so both areas may be used separately for crystal blanks. Optical twinning, on the other hand, is usually confined to pockets, which are normally too small to provide crystal blanks, themselves, so that only the predominant crystal region can be utilized.

## THE AXES OF QUARTZ

1-51. There are several crystallographic conventions by which the reference axes of crystals may be chosen, and much confusion has resulted in the past because of the various preferences of different crystallographers. Insofar as the over-all piezoelectric properties are concerned, the orientations of quartz have been universally measured according to rectangular sets of $\mathrm{X}, \mathrm{Y}$, and Z axes, with the $X Y, X Z$, and $Y Z$ planes determined according to the crystal symmetries. However, even in this case, the choice of positive and negative axial and angular directions for right and left quartz remained more or less a matter of preference until the system proposed by the I.R.E. in 1949 became generally adopted. It is the I.R.E. system that will be followed here. It should be remarked first, however, that a crystal axis is not intended necessarily to coincide with a central point in the crystal, but may represent any straight line parallel to the axial direction. It might also be noted that the different types of crystal faces are designated in this manual by the small letters $\mathrm{m}, \mathrm{r}, \mathrm{s}, \mathrm{x}$, and z , and these should not be confused with the capital letters $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ which denote the axes, nor with the small letters, $x, y, z$, when used to denote dimensions of a crystal in the axial directions.

## 2 Axis

1-52. The Z axis is the lengthwise direction of the quartz prism and is perpendicular to the growth lines of all the $m$ faces. It is an axis of three-fold symmetry, so that there are three sets of XY axes for each crystal (figure 1-6), with the direction of the Z axis common to all three. No piezoelectric effects are directly assiociated with the Z axis, and an electric field applied in this direction produces no piezoelectric deformation in the crystal, nor will a mechanical stress along the Z axis produce a difference of potential. Because the growth lines
are generally missing, optical effects are usually employed to locate the Z azis in raw quartz. (See paragraphs 1-121 to 1-124.) Quartz properties are such that light waves passing through a crystal are effectively divided into two rectilinear components, with one component traveling faster than the other except when the light ray is directed parallel to the Z axis. The optical effects are found to be symmetric about the Z axis, and thus whereas optical instruments may be used to determine this axis, they cannot be used to distinguish an $X$ from a Y axis. For this reason the Z axis is commonly designated as the optic axis. The optical effects associated with the propagation of polarized light parallel to the optic axis not only are used to locate the Z axis in unfaced quartz (crystals, such as river quartz, whose natural faces have been destroyed), but to identify left from right quartz, and to locate twinned regions. Plane polarized light traveling parallel to the optic axis will be rotated in one direction or the other according to whether the crystal is left or right. To an observer looking toward the light source the rotation will be clockwise for right-handed quartz and counterclockwise for left-handed quartz, with the amount of rotation depending upon the wavelength, being greater for blue light (short wavelength) and less for red light (long wavelength). Since the crystal lattice along the optic axis has no properties that distinguish one direction from the other, the choice of the $+Z$ and the $-Z$ reference directions are entirely arbitrary for either right or left crystals.


Figure 1-6. XY plane of quartz showing three sets of rectangular axes: $X_{i} Y_{1} Z, X_{i} Y_{z} Z_{,} X_{,}, Y_{3} Z$ ( $Z$ axis is perpendicular to plane of paper)

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## $Y A x i s$

1-53. The $Y$ axes are chosen at right angles to the $Z$ axis and to the growth lines of the $m$ faces. See figure 1-4. For either left or right quartz, the positive end of a $Y$ axis emerges from an $m$ face that is adjoined by a z face at the end selected as the $+Z$ direction. The $Y$ axes are generally called the mechanical axes in contradistinction to the $X$ axes, which are called the electrical axes. These names originated from the fact that simple compressional and tensional mechanical stresses along either an $X$ axis or a $Y$ axis would cause a polarization of the $X$ axis, but not of the $Y$ axis. The names are somewhat misleading, for polarization in the $Y$ direction is also possible if a crystal undergoes shearing or flexural strains. In practice, the $Y$ axis of a quartz stone is usually determined after the $Z$ and $X$ axes have been located.
$X$ Axis
1-54. The $X$ axes are parallel to the growth lines of the $m$ faces, and to the lines bisecting the 120 degree prism angles. The positive end of an $X$ axis is the direction that forms a right-handed coordinate system (see figure 1-4) with the $Y$ and $Z$ axes. This makes the directional sense of the $X$ axis in right quartz the reverse, rather than the mirror image, of that in left quartz. Thus, in right quartz the negative ends of the $X$ axes emerge from the prism comers that lie between the $x$ faces, whereas, in left quartz the positive ends emerge from these corners.
1-55. In either right or left quartz when the $X$ axis undergoes a tensional strain (stretching), a positive charge appears at the end emerging between the x faces; and when the X axis is compressed, this end becomes negatively charged. The $\mathbf{X}$ axis of raw quartz is usually determined by optical and x-ray methods. See paragraphs 1-126 and 1-127.

## THEORY OF PIEZOELECTRICITY

## Report Announcing Discovery of the Piezoelectric Effect

1-56. The theory of the cause of piezoelectricity stated in the most general terms is substantially the same today as it was at the time of its discovery. The following is the original report by Pierre Curie on the piezoelectric effect, which includes a statement of the theory that led to its discovery. The paper was read at the April 8, 1880, meeting of the societe mineralogique de France, and is recorded in the Bulletin, soc. min. de France, volume 3,1880 .

1-57. "Crystals which have one or more axes whose ends are unlike, that is to say, hemihedral crystals with inclined faces, have a special physical property, that they exhibit two electric poles of opposite names at the ends of those axes when they undergo a change of temperature: this is the phenomenon known as pyroelectricity.
1-58. "We have found a new way to develop electric polarization in crystals of this sort, which consists of subjecting them to different pressures along their hemihedral axes.
1-59. "The effects produced are analogous to those caused by heat: during a compression, the ends of the axis along which we are acting are charged with opposite electricities; when the crystal is brought back to the neutral state and the compression is relieved, the phenomenon occurs again, but with the signs reversed; the end which was positively charged by compression becomes negative when the compression is removed and reciprocally.
1-60. "To make an experiment we cut two faces parallel to each other, and perpendicular to a hemihedral axis, in the substance which we wish to study; we cover these faces with two sheets of tin which are insulated on their outer sides by two sheets of hard rubber; when the whole thing is placed between the jaws of a vise, for example, we can exert pressure on the two cut surfaces, that is to say, along the hemihedral axis itself. To perceive the electrification we used a Thomson electrometer. We may show the difference of potential between the ends by connecting each sheet of tin with two of the sectors of the instrument while the needle is charged with a known sort of electricity. We may also recognize each of the electricities separately; to do this we connect one of the tin sheets with the earth, the other with the needle, and we charge the two pairs of sectors from a battery.
1-61. "Although we have not yet undertaken the study of the laws of this phenomenon, we are able to say that the characteristics which it exhibits are identical with those of pyroelectricity, as they have been described by Gaugain in his beautiful work on tourmaline.
1-62. "We have made a comparative study of the two ways of developing electric polarization in a series of non-conducting substances, hemihedral with inclined faces, which includes almost all those which are known as pyroelectric.
1-63. "The action of heat has been studied by the process indicated by M. Friedel, a process which is very convenient.

1-64. "Our experiments have been made on blende, sodium chlorate, boracite, tourmaline, quartz, calamine, topaz, tartaric acid (right handed), sugar, and Seignette's salt.
1-65. "In all these crystals the effects produced by compression are in the same sense as those produced by cooling; those which result from relieving the pressure are in the same sense as those which come from heating.
1-66. "There is here an evident relation which allows us to refer the phenomena in both cases to the same cause and to bring them under the following statement:
1-67. "Whatever may be the determining cause, whenever a hemihedral crystal with inclined faces, which is also a non-conductor, contracts, electric poles are formed in a certain sense; whenever the crystal expands, the electricities are separated in the opposite sense.
1-68. "If this way of looking at the matter is correct, the effects arising from compression ought to be in the same sense as those resulting from heating in a substance which has a negative coefficient of dilation along the hemihedral axis."

## Asymmetrical Displacement of Charge

1-69. The atomic lattice of piezoelectric crystals is assumed to consist of rows of alternating centers of positive and negative charges so arranged that the structure as a whole has no center of symmetry. When such a lattice undergoes a deformation, a displacement will result between the "centers of gravity" of the positive and negative charges. It is this displacement that results in a net unneutralized dipole moment, the polarity of


Figure 1.7. Effective polarities resulting from sudden displacements of the centers of charge of a neutralixed dipole. (If after displacement, the crystal were maintained indefinitely in the strained position, the effective polarity would evenfually be neutralized by an accumulation of ions at the poles. A sudden return from such a state would thus result in an effective polarization in the unsirained position)
which depends upon the previous equilibrium positions of the positive and negative centers of charge and the direction of the displacement, as indicated in figure $1-7$.
1-70. In the case of a crystal with a center of symmetry, a uniform strain in the crystal will always result in as much displacement of like charges in one direction as in another, and hence there will be no net shift of the centers of opposite charge relative to each other. A distribution of charges having a center of symmetry is illustrated in figure 1-8. Note that the centers of charge, both positive and negative, are at the geometrical center. If a uniform stress-compressional, or shearing-is applied along any axis, it can be seen that the center of either type of charge will at all times remain undisturbed, and thus the net piezoelectric effect will be null.
1-71. Lord Kelvin was the first to propose a molecular model with a charge distribution designed to explain the physical and electrical characteristics of alpha quartz. See figure 1-9. This model was accepted generally by the crystallographers until the theory failed to conform to X-ray tests. When a beam of X -rays enters a crystal, the intersecting atomic planes can be likened to partially silvered mirrors, each passing part of the beam, but reflecting the rest. Since the distance between adjacent parallel planes is on the order of an X-ray wavelength, the waves reflected from adjacent planes will tend to alternately annul and reinforce each other as the angles of incidence vary. The interference pattern on a photographic film will show an array of spots indicating the angles at which the reflected waves from different planes arrive in phase. From such data, with the X-ray wavelength known, it is possible to determine the relative orientation of atomic planes, and hence to reconstruct the arrangement of the atoms in the crystal. The X-ray data on alpha quartz reveals a


Figure 1-8. Example of distribution of charges having a center of symmetry *

## Section 1

Physical Characteristics of Piezoelectric Crystals


Figure 1-9. Kelvin's molecular model of the charge distribution of alpha quartz. The positive direction shown for the $X$ axis corresponds to that of right quartz, for a compression of the erystal along that axis will cause the piezoelectric polarities to coincide in sign with the X-axial directions. For left quartz, the sign of the $Y$, as well as the $X$, axis, must be reversed in order to maintain a right-handed coordinate system *


ARRANGEMENT OF ATONS IN ALPMA QUARTZ, VIEWED ALONG AN $\times$ AXIS

Figure 1-10. Arrangement of atoms in alpha quartz. Plane of paper corresponds to YZ plane in crystal

(B)

Figure 1-11. Equivalent distribution of charges that account for observed piezoelectric effects of alpha quartz. (A) Piezoelectric polarity along $X$ axis of right quartz due to compression along $Y$ axis. (B) Piezoelectric polarity of $Y$ axis of right quartz due to shearing stress, where the resultant strain is equivalent to a compression along the axis designated GH. (Note that in both A and B, the piezoelectric effect is due to a rocking of the axial dipoles, and not to their compression or extension. To achieve the same deformations by the converse effect, equal voltages, but opposite in sign to the polarizations indicated, are applied across the respective axes)*
more complex structure than was once suspected. See figure 1-10. Nevertheless, the early crystal model, as postulated by Lord Kelvin, still can be accepted as an approximation if we treat a single one of his molecules as representing simply the equivalent charge distribution within the lattice, as indicated in figure 1-11.
1-72. Figure 1-11A shows the displacement occurring when a compressional stress is applied along the $Y$ axis, or a tensional stress is applied along the $\mathbf{X}$ axis of a right-handed crystal. Note that the center of positive charge shifts in the negative direction of the $\mathbf{X}$ axis, and that the center of negative charge shifts in the positive direction; however, there is no net displacement along the $Y$ axis. If the direction of the stress is reversed, so also is the effective polarity.
1-73. The polarization of the $Y$ axis due to a shearing strain is illustrated in figure 1-11B. Assume that vectors $A$ and $B$ represent a simple shearing stress applied at right angles to the $Y$ axis. If $A$ and $B$ are equal and opposite forces, there will be no displacement of the center of mass; however, since these forces are not directed in the same straight line, they create a couple which would maintain a rotational acceleration about the center of mass unless opposed by an equal and opposite couple. This counter-couple is represented by vectors C and D. If now, the forces are combined vectorially, they may be represented as a longitudinal tension in the EF direction, or as a longitudinal compression in the GH direction. Consider the charge displacement from the point of view of a GH compression. Note that each of the positive charges is forced to shift slightly in the $+Y$ direction, whereas each of the negative charges is displaced in the $-Y$ direction. The net separation of the centers of charge thus causes the $Y$ axis to become positively polarized at its geometrically positive end, and negatively polarized at its geometrically negative end.
1-74. Since the compression can be further analyzed into two components of equal magnitudeone horizontal, and the other vertical-it can be seen (figure 1-11A) that the polarities which these would induce along the $X$ axis tend to cancel (for reinforcement to occur, one of the rectangular components would need to be tensional and the other compressional), and hence little or no polarization will appear in this direction.

## MODES OF VIBRATION

1-75. If a piezoelectric crystal is suddenly released from a strained position, the inertia and elasticity
of the crystal will tend to maintain a state of mechanical oscillation of constant frequency about one or more nodal points, lines, or planes of equilibrium, and alternating voltages will appear according to the particular mode of vibration. These are called the normal, or free, vibrations of a crystal, as distinct from the forced vibrations due to applied alternating mechanical or electrical forces that may differ in frequency from the crystal's natural resonance. The normal vibrations may, in turn, be of two general types: the freefree and the clamped-free vibrations. Free-free vibrations are those which would occur if a vibrating crystal were floating in empty space, where, regardless of the particular mode, the center of gravity is a nodal point. Clamped-free vibrations are those that would occur if a crystal were clamped at some point, or points, thereby preventing all normal modes except those at which nodes occur at the clamped points. For example, in a freefree vibration the ends of the crystal are free to move; however, if these ends are clamped, the resonant vibrations must be such that the ends become nodes. However, if a crystal is clamped only at those points which would be nodes in a free-free vibration, in the ideal case no interference results, and the resonance is still that of a free-free mode.
1-76. There are three general modes of vibration for which quartz crystal units are commercially designed: extensional, shear, and flexure. Fundamental vibrations of each of these modes are illustrated in figure 1-12. Higher harmonics up to and including the fifth are also widely used. Harmonic vibrations higher than the seventh have special high-frequency applications, but are rarely employed commercialiy.
1-77. A variation of the shear vibration is the torsional mode, which is readily excited in cylindrical crystals; however, except for laboratory


Figure 1-12. Useful fundamental modes of quartz plates. (A) Flexural. (B) Extensional or longitudinal. (C) Face (or length-width) shear. (D) Thickness shear.*

Section
measurements of the properties of solids and liquids this mode is not in general use.

## Frequency of Quartz Vibrations

1-78. The frequencies of the normal mechanical oscillations of a quartz plate may be considered as those at which standing waves will be established by reflection from the crystal boundaries. The positions of the nodes of the standing waves are predetermined by the geometry of the crystal, and by any difference that may exist in the velocities of propagation for the different wave components. The wavelength of a particular mode (but not the wave shape, if the velocity of one component differs from that of another) conforms only to the dimensions of the crystal faces. The frequency is related to the wavelength by the equation:

$$
\begin{equation*}
\mathrm{f}=\frac{\mathbf{v}}{\lambda} \tag{1}
\end{equation*}
$$

where: $v=$ velocity of propagation
$\lambda=$ wavelength
The fundamental equation of the velocity of propagation is:

$$
\begin{equation*}
v=\sqrt{\frac{c}{\rho}} \tag{2}
\end{equation*}
$$

where: $c=$ stiffness factor in the direction of propagation

$$
\rho=\text { density }
$$

or: $\quad \mathrm{v}=\sqrt{\frac{1}{\rho \mathrm{~S}}}$
where: $s=\frac{1}{c}=\begin{aligned} & \text { elastic compliance factor in the di- } \\ & \text { rection of propagation }\end{aligned}$

## Length- (or Width-) Extensional Mode

1-79. The motion of the atoms in an extensional mode is parallel to the direction of propagation. In the case of rectangular plates, stationary waves are established in the length direction by the interference of reflections from the opposite ends, where the wavelength is given by the formula:

$$
\begin{equation*}
\lambda=\frac{2 l}{n} \tag{1}
\end{equation*}
$$

where 1 is the length and $n$ is $s n$ integer ( $1,2,3$, etc.) equal to the harmonic. Thus, the frequency
of a length-extensional mode is:

$$
f=\frac{n v}{2 l}
$$

or, as expressed in terms of a frequency constant:

$$
\mathrm{f}=\frac{\mathrm{nk}_{1}}{\mathrm{l}}
$$

where: $k_{1}=\frac{v}{2}=$ frequency constant

> for length-extensional mode

This formula, as well as the similar formulas for the shear and flexure modes, can be used to indicate the approximate dimensions required for a particular frequency when the appropriate frequency constant is known. Although the velocity of propagation decreases somewhat as the frequency increases, because of an increase in the frictional losses, this decrease is negligible for most purposes, and the same frequency constants that hold for the fundamental are also valid for the first few overtones. However, because of the coupling that exists between the length-extensional mode and other modes, the effective value of $k$ will vary with changes in the $w / 1$ (width/length) ratio. Equation (3) also applies to width-extensional modes except that 1 is replaced by the width, w.

## Thickness-Extensional Mode

1-80. This mode is little used today because of the close coupling that exists between it and the overtones of other modes. It is a mode that can be excited in a crystal whose thickness dimension is parallel to the electrical (X) axis (X-cut crystal) -the vibrations being such that the crystal alternately becomes thicker and thinner. Formerly, when X-cut crystals were widely used, the same crystal was often employed for the control of either a high- or a low-frequency circuit-using the thickness-extensional mode for the former and the length-extensional mode for the latter. Today, however, the more stable thickness-shear mode has almost entirely replaced the thickness-extensional mode in high-frequency circuits. The thicknessextensional frequency is given by the formula:

$$
\mathrm{f}=\frac{\mathrm{nv}}{2 \mathrm{t}}=\frac{n \mathrm{k}_{2}}{\mathrm{t}}
$$

where $v$ is the velocity of propagation in the thickness direction, $n$ is the harmonic ( $n=1,3,5$,-for practical cases, although even harmonics of very small intensities have been observed), and $\mathbf{k}_{z}$ is
the generalized frequency constant. Actually, the effective thickness, $t$, decreases somewhat for the overtones, so that the correct value of $k_{2}$ is slightly greater for the harmonics than for the fundamental.

## Thickness-Shear Mode

1-81. The motion of the atoms in a thickness-shear mode is parallel to the major (length-width) faces of the crystal, whereas the wave propagation is parallel to the thickness dimension. The equation for the fundamental frequency when the thickness is very small compared with the length and width is:

$$
\begin{equation*}
f=\frac{v}{2 t} \tag{1}
\end{equation*}
$$

where: $\mathrm{v}=$ velocity of propagation along thickness dimension

$$
\mathrm{t}=\text { thickness }
$$

or, as expressed in terms of a thickness-shear frequency constant:

$$
\begin{equation*}
f=\frac{k_{3}}{t} \tag{2}
\end{equation*}
$$

The thickness-shear is also called the "highfrequency shear" in contradistinction to the "face," "length-width," or "low-frequency" shear. The overtones of the thickness-shear mode may have components (reversals of phase) in the length and width directions as well as along the thickness. The more general formula for the frequency is:

$$
\begin{equation*}
f=k_{3} \sqrt{\frac{m^{2}}{t^{2}}+\frac{n^{2}}{l^{2}}+\frac{p^{2}}{w^{2}}} \tag{3}
\end{equation*}
$$

where $m, n$, and $p$ are integers representing the harmonic component in the $t, 1$, and $w$ directions, respectively. The above equation applies to an isotropic medium; however, since the elastic constants in quartz are not the same in all directions, the thickness-shear formula has been modified to:

$$
f=k_{3} \sqrt{\frac{m^{2}}{t^{2}}+a_{1} \frac{n^{2}}{1^{2}}+a_{2} \frac{(p-1)^{2}}{w^{2}}}
$$

where $a_{1}$ and $a_{2}$ are constants to be determined empirically. For most applications, $t$ is much smaller than 1 and $w$, and $n=p=1$, so that the formula, $f=\frac{k_{3} m}{t}$, is sufficiently accurate.

## Face-Shear Mode

1-82. The face-shear mode involves a more com-
plex relation among the crystal dimensions. A complication arises from the fact that the wave is effectively divided into two components-one propagated along the length, and the other along the width. Each of these separate components has its own series of possible harmonics, so that the resultant frequencies of the face-shear modes are not necessarily integral multiples of the fundamental. The approximate-frequency equation is:

$$
\begin{equation*}
f=\frac{v}{2} \sqrt{\frac{m^{2}}{l^{2}}+a_{1} \frac{n^{2}}{w^{2}}}=k_{4}^{\prime} \sqrt{\frac{m^{2}}{\mathrm{l}^{2}}+a_{1} \frac{n^{2}}{w^{2}}} \tag{1}
\end{equation*}
$$

where $m$ and $n$ are integers representing the length and width harmonics, respectively. The symbol $a_{1}$ is a constant of proportionality, approximately equal to one, which is inserted when the velocity of propagation along $w$ is not the same as that along 1. If the face of the plate is square, the formula for the fundamental frequency is reduced to approximately :

$$
\begin{equation*}
f=\frac{k_{4}}{w} \tag{2}
\end{equation*}
$$

where: $k_{4}=k_{4}^{\prime} \sqrt{2}$
The fundamental vibration, where $m=n=1$, is shown in figure 1-12C. Note that the shape of the deformation is not that of a parallelogram, as it would be if the plate were slowly compressed along a diagonal. Rather, the vibrational distortion is a dynamic one, and the resultant wave must be in the same phase at all points. Figure 1-13 represents the face-shear mode for $m=6, n=3$. Note that the number of nodes in each row is equal to. m , and the number in each column is equal to $n$.


Figure 1-13. Feco-shoar mode for $m=6, n=3$. Dots indicate nodes *

## Section I

## Length-Width-Fiexural Mode

1-83. The length-width-flexural mode is a bending of the crystal in the length-width plane. Normally, the crystal is so mounted that the ends are free to vibrate in a free-free mode. The formula for the frequency involves the root of a transcendental equation, but expressed in terms of a frequency constant, the equation becomes:

$$
f=\frac{k_{5} w}{l^{2}}
$$

The convenience of a common frequency constant for all practicable harmonics is not realized in the case of length-width flexures, where the "constant" $\mathrm{k}_{5}$ is a function not only of the particular harmonic, but also of 1 and w. However, for long, thin rods ( $\frac{n w}{1}$ less than 0.1 , where $n$ is the harmonic) $k_{5}$ is approximately independent of the dimensions, and fixed values of $k_{5}$ can be assumed for the particular harmonics of different types of cuts. Because of the elastic cross constants in quartz, which relate a field in one direction to a polarization in a perpendicular direction, a flexure may be accompanied by a torsion. To prevent this, the length of a crystal to be operated in a flexural mode should lie somewhere in a $Y Z$ plane.

## Length-Thickness-Flexural Mode

1-84. Length-thickness flexures are used to control frequencies in the audio range. To obtain this mode, two long, thin plates of the same cut are cemented together with the electrical axes opposed, so that, when an alternating voitage is applied across the outer faces, one crystal strip expands as the other contracts, and vice versa-the over-all effect being a flexural vibration. The normal frequency of a free-free length-thickness flexure is given by an equation similar to that for the lengthwidth flexure, except that the thickness, $t$, is substituted for the width, w. Thus:

$$
\begin{equation*}
\mathrm{f}=\mathrm{nk}_{6}\left(\frac{\mathrm{t}}{\mathrm{l}^{2}}\right) \tag{1}
\end{equation*}
$$

## Frequency Range of Normal Modes

1-85. Standard quartz crystal units are designed for frequencies from 400 cycles to 125 megacycles per second. Laboratory devices have employed thickness flexure crystals for the control of frequencies as low as 50 cycles per second, and, by exciting the higher thickness-shear modes, control of frequencies higher than 200 megacycles per second have been realized. At these high frequen-
cies, however, so many interlocking modes are possible that it is difficult to prevent a crystal from jumping from one mode to another during slight variations of temperature, unless a very precise fabrication of the crystal unit has been achieved. The high-frequency limit of the lower harmonics is reached when the dimensions are so small that either the crystal cannot be driven without the risk of shattering, or that the impedances introduced by the mounting become proportionately too large for practicable operation.
1-86. The practical frequency ranges of the different modes are as follows:
Flexure Mode-
Length-thickness: 0.4 to 10 kc
Length-width: 10 to 100 kc
Extensional Mode-
Length: $\mathbf{4 0}$ to $\mathbf{8 5 0} \mathrm{kc}$
Thickness: 500 to $15,000 \mathrm{kc}$
Shear Mode-
Face: 100 to 1800 kc
Thickness (fundamental) : 500 to $20,000 \mathrm{kc}$
Thickness (overtones) : 15,000 to $125,000 \mathrm{kc}$

## ORIENTATION OF CRYSTAL CUTS

## Right-Hamded Coordinate Systom

1-87. With the positive sense of the quartz $X, Y$, and Z axes determined as in paragraphs 1-52, 1-53, and 1-54, the positive sense of rotation about the axes is fixed by the conventions of a right-handed


POSITIVE DIRECTIONS OF ROTATION ANGLES CORRESPOND TO ROTATION OF RIGHT-HANO SCREW WHEN THE SCREW ADVANCES TOWAROS THE POSITIVE ENO OF THE AXIS OF ROTATION.

Figure 1-14. Positive directions of angles of rotation according to conventions of inghthanded coordinate system
coordinate system for both right and left quartz. If one imagines a right-handed screw pointing towards the positive end of an axis of rotation, as represented in figure $1-14$, the direction of an angle of rotation is considered positive if the rotation advances the screw in a positive direction-this corresponds to a clockwise rotation if observed when looking towards the positive end of the axis of rotation. The reverse, or counterclockwise, angles of rotation are taken as negative. The sense of the axes are such that the angles of rotation are positive when the directions of rotation are from $+\mathbf{X}$ to $+\mathbf{Y},+\mathbf{Y}$ to $+\mathbf{Z}$, and $+\mathbf{Z}$ to $+\mathbf{X}$. The axial and rotational conventions permit a particular cut of crystal to have the same rotation symbol for both right and left quartz.

## Rotation Symbels

1-88. To specify the orientation of a piezoid cut, the following system, as recommended by the I. R. E. in 1949 is in general use. The crystal blank to be described is assumed to have a hypothetical initial position, with one corner at the origin of the coordinate system, and the thickness, length, and width lying in the directions of the rectangular axes. There are six possible initial positions, each of which is specified by two letters, the first letter indicating the thickness axis, and the second letter indicating the length axis. These positions are thus designated $x y, x z, y x, y z, z x$, and $z y$. The $x y$ and $y x$ positions are shown in figures $1-15$ and $1-16$, respectively. The starting position is so chosen that the final orientation may be reached with a minimum number of rotations. These rotations are taken successively about axes that parallel the


Pigure $1.15 x y$ initial pesition for designenting orientation of erystal cut
dimensions of the crystal at the time of rotation. Only the first rotational axis will coincide with a rectangular axis; however, the positive direction of any axis of rotation is that defined by the XYZ system for the initial position. A single rotation is sufficient for describing the majority of standard cuts, and three rotations is the maximum in any case. The dimensions and axes of rotation are indicated by the symbols, $t, 1$, and $w$, for thickness, length, and width, respectively. The Greek letters $\phi, \theta$, and $\psi$ designate the first, second, and third angles of rotation, respectively. The following example, illustrated in figure 1-17, is a complete geometrical specification of a crystal plate:

$$
\begin{gathered}
\text { yztwl } 30^{\circ} / 15^{\circ} / 25^{\circ} \\
\mathrm{t}=0.80 \pm 0.01 \mathrm{~mm} \\
\mathrm{l}=40.0 \pm 0.1 \mathrm{~mm} \\
\mathrm{w}=9.00 \pm 0.03 \mathrm{~mm}
\end{gathered}
$$

The lettered combination at the beginning of the specification is called the "rotation symbol." The first two letters, $y z$, of the symbol indicate the initial position, and the next three letters, twl, state the axes of rotation and the order in which the rotations are taken. The three angles, all positive in this case, give the orientation and are listed in the same order as the respective rotations. The dimensions listed are those of the particular plate, and are not to be considered as necessary specifications for that type of cut. For circular plates, the initial position will indicate which directions are to be considered thickness and length, so that the same rotation symbol is used as for rectangular


Flgure 1-16 yx initial pesition for desigmeting orlontation of erytral cut

Section I
Standard Quartz Elements


Figure 1-17 Orientation of eryatal having the rotational specifications yatwl: $30^{\circ} / 15^{\circ} / 25^{\circ}$
plates; in specifying the dimensions, however, 1 and $w$ are replaced by the diameter.

## PIEZOELECTRIC ELEMENTS

1-89. The performance characteristics of a crystal plate are dependent on both the particular cut and
the mode of vibration. For convenience, each "cutmode" combination is considered a separate "piezoelectric element," and the more commonly used elements have been assigned a letter symbol. For example, the thickness-shear mode of the AT cut is designated as element $A$.

## STANDARD QUARTZ ELEMENTS

1-90. The principal quartz elements are given below, with those which have been assigned element
symbols listed first.

| Element Symbol | Name of Cut | Rotation Symbol and Orientation | Mode of Vibration | Frequency Range in KC |
| :---: | :---: | :---: | :---: | :---: |
| A | AT | yxl $35^{\circ} 21^{\prime}$ or $\mathrm{yzw} 35^{\circ} 21^{\prime}$ | thickness-shear | 500 to 125,000 |
| B | BT or YT* | yxl $-49^{\circ} 8^{\prime}$ or yzw $-49^{\circ} 8^{\prime}$ | thickness-shear | 1,000 to 75,000 |
| C | CT | yxl $37^{\circ} 40^{\prime}$ or $\mathrm{yzw} 37^{\circ} 40^{\prime}$ | face-shear | 300 to 1,100 |
| D | DT | yxi $-52^{\circ} 30^{\prime}$ or $\mathrm{yzw}-52^{\circ} 30^{\prime}$ | face-shear | 60 to 500 |
| E | $+5^{\circ} \mathrm{X}$ | xyt $5^{\circ}$ | length-extensional | 50 to 500 |

* The YT cut, which is essentially the same as the BT cut, was developed independently by Yoda in Japan.

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| Element Symbol | Name of Cut | Rotation Symbol and Orientation | Mode of Vibration | Frequency <br> Range in KC |
| :---: | :---: | :---: | :---: | :---: |
| F | $-18.5^{\circ} \mathrm{X}$ | xyt $-18.5^{\circ}$ | length-extensional | 60 to 300 |
| G | GT | yxit $-51^{\circ} 7.5^{\prime} / 45^{\circ}$ | width-extensional | 100 to 550 |
| H | $5^{\circ} \mathrm{X}$ | yxt $5^{\circ}$ | length-width flexure | 10 to 50 |
| J | Duplex $5^{\circ} \mathrm{X}$ | xyt $5^{\circ}$ (right quartz) and xyt $5^{\circ}$ (left quartz) | length-thickness flexure | 0.4 to 10 |
| M | MT | xytl $0^{\circ}$ to $8.5^{\circ} / \pm 34^{\circ}$ to $\pm 50^{\circ}$ | length-extensional | 50 to 500 |
| N | NT | xytl $0^{\circ}$ to $8.5^{\circ} / \pm 38^{\circ}$ to $\pm 70^{\circ}$ | length-width flexure | 4 to 100 |
| - | AC | yxl $31^{\circ}$ or yzw $31^{\circ}$ | thickness-shear | 1,000 to 15,000 |
| - | BC | yxl $-60^{\circ}$ or yzw $-60^{\circ}$ | thickness-shear | 1,000 to 20,000 |
| - | ET | yxl $66^{\circ} 30^{\prime}$ or $\mathrm{yzw} 66^{\circ} 30^{\prime}$ | combination flexure and face-shear | 600 to 1,800 |
| - | FT | yxl $-57^{\circ}$ or $\mathrm{yzw}-57^{\circ}$ | combination flexure and face-shear | 150 to 1,500 |
| - | v | xzlw or xywl $15^{\circ}$ to $29^{\circ} /-14^{\circ}$ to $-54^{\circ}$ and $13^{\circ}$ to $29^{\circ} / 27^{\circ}$ to $42^{\circ}$ | thickness-shear | $\begin{aligned} & 1,000 \text { to } 20,000 \\ & \text { (fundamental) } \end{aligned}$ |
| - | v | xzlw or xywl $0^{\circ}$ to $30^{\circ} / \pm 45^{\circ}$ to $\pm 70^{\circ}$ | face-shear | 60 to 1,000 |
| - | X | xy | length-extensional | 40 to 350 |
| - | X | xz | width-extensional | 125 to 400 |
| - | X | xy or xz | thickness-extensional | 350 to 20,000 |
| - | Y | yx or yz | thickness-shear | 500 to 20,000 |

of crystals is theoretically possible, where the initial position is a Z cut (thickness parallel to the Z axis) ; however, because the piezoelectric effect

Figure 1-18 Orientation of $X, Y$, and $Z$ cut plates


1-91. The standard quartz elements can be divided into two groups: in the first group belong those crystals which are most conveniently described as being rotated X-cut crystals, and in the second group belong those crystals which are most conveniently described as being rotated Y-cut crystals. The first will hereafter be designated as the $X$ group, and the second as the $Y$ group.
1-92. The $X$ and $Y$ cuts have their thickness dimensions parallel to the X and Y axes, respectively, with the length and width dimensions parallel to the two remaining axes. See figure $1-18$. Thus, in describing a crystal orientation, the X cut is the equivalent of the two initial positions $x y$ and $x z$, and the $Y$ cut is represented by the initial positions $y x$ and $y z$. Belonging to the $X$ and $Y$ groups, then, are those crystals whose rotation symbols begin with the letters $x$ and $y$, respectively. As a general rule, from the $\mathbf{X}$ group, the low-frequency crystal units are obtained, and from the $Y$ group, the medium- and high-frequency units. A third group

Section I

## Standard Quartz Elements

is restricted to the X and Y axes, the electrodes must be placed across one of these axes, which for the $Z$ cut, would be at the edges-not a convenient location. Nor have other cuts, more or less simply oriented relative to a $Z$ cut, been found to have optimum performance characteristics. However, there are experimental $Z$ cuts, such as some of the ring-shaped crystals, which have proven of high quality, even though not practical for general use.

## The X Group

1-93. The principal crystals of the $X$ group are listed below with the frequency ranges for which they have found commercial application:


Figure 1-19. The $X$ group. (The second rotations of the MT, NT, and V cuts are shown only for the pesitive angles) * WADC TR 56-156


## THE X CUT

1-94. The $X$ cut was the original quartz plate investigated by Curie, and thus is sometimes called the "Curie cut." This cut was also the first to be used as a transducer of ultrasonic waves and as the control element of radio-frequency oscillators. However, because of its comparatively large coefficient of temperature, the X-cut plate is now rarely used in radio oscillators. As a transducer of electrical to mechanical vibrations, especially at high frequencies of narrow bandwidth, the $X$ cut has a high electromechanical coupling efficiency, and is still widely used to produce ultrasonic waves in gases, liquids, and solids. These applications are largely for testing purposes, such as the measurement of physical constants and the detection of flaws in metal castings.

## 1-95. CHARACTERISTICS OF X-CUT PLATES IN THICKNESS-EXTENSIONAL MODE

Description of Element: X cut; xy or xz; thick-ness-extensional mode.
Frequency Range: $350-20,000 \mathrm{kc}$ (fundamental vibration) ; lower frequencies when coupled as transducer for generating vibrations in liquids and solids.
Frequency Equation: $f=\frac{n k_{2}}{t}(n=1,3,5, \ldots)$
Frequency Constant: $\mathrm{k}_{2}=2870 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 20 to 25 parts per million per degree centigrade; negative (i.e. for each degree increase or decrease in temperature, the frequency respectively decreases or increases 20 to 25 cycles for each megacycle of the initial frequency-a rise in temperature of $10^{\circ} \mathrm{C}$ would thus cause the frequency of a 5000 -ke crystal to drop 1000 to 1250 cycles per second.)
*Methods of Mounting: Sandwich and unclamped air-gap-for oscillator circuit; transducer mounting depends upon particular type of mechanical load.
Advantages: Mechanical stability, economy of cut, efficiency of conversion of electrical to mechanical energy, and large frequency constant make this piezoelectric element preferred for the radiation of high-frequency acoustic waves when the ratio of the highest to the lowest frequency need not exceed 1.1.
Disadvantages: Large temperature coefficient, tendency to jump from one mode to another, and the difficulty of clamping crystal in a fixed position without greatly damping the

[^0]

Figure 1-20. Frequency constant for length-extensional mode (curve A) of X-cut crystal where the width and length are parallel to the $\mathbf{Z}$ and $Y$ axes, respectively. Curve B is the frequency constant of a face-shear mode coupled to a second fiexural mode, whose interference makes the crystal useless for w/l ratios between 0.2 and 0.3 , unless the thickness approaches the dimensions of the width *
normal vibration prevent this element from being preferred for oscillator control. An electromechanical coupling factor of 0.095 , which is only one-fourth that of the best synthetic crystals, makes this element inefficient as a radiator of a wide band of frequencies.

1-96. CHARACTERISTICS OF X-CUT PLATES IN LENGTH-EXTENSIONAL MODE
Description of Element: X-cut; xy; length-extensional mode.
Frequency Range: 40-350 kc.
Frequency Equation: $f=\frac{\mathrm{nk}_{1}}{1}(\mathrm{n}=1,2,3, \ldots)$
Frequency Constant: Varies with w/l ratio-see figure 1-20.
Temperature Coefficient: Negative**, varies with w/I ratio-see figure 1-21; zero coefficient if $\mathrm{w} / \mathrm{l}=0.272$ and $\mathrm{w}=\mathrm{t}$.
Methods of Mounting: Sandwich, air gap, wire, knife-edge clamp, pressure pins, cantilever clamp; more than one pair of electrodes required for overtones; transducer mounting depends upon particular type of mechanical load.

[^1]

Figure 1-21. Temperature coefficient for length-extensional mode of X-cut erystal, where $w$ is parallel to the $Z$ axis, and $t=0.051$

Advantages: For w/ 1 ratios from 0.35 to 1.0 , the fundamental length-extensional vibration is not strongly coupled to other modes, and hence the resonance is easily excited and of good stability except for drift during temperature variations. Although not preferred over zero-temperature-coefficient cuts, this element, with temperature control, is reliable for use in low-frequency oscillators, and for long, thin bars, for use in filters. H8wever, its most important application is to produce ultrasonic vibration in gases, liquids, and solids, when the ratio of highest to lowest frequency need not exceed 1.1.
Disadvantages: Inefficient as transducer of any but narrow frequency band, since electromechanical coupling is only one-fourth that of the better synthetic crystals. Strong coupling with a flexural mode makes the crystal useless at $w / 1$ ratios between 0.2 and 0.3 (see figure 1-20), and a weak coupling with a shear mode causes the frequency constant to decrease as the $w / 1$ ratio approaches 1.0 . This coupling to other modes interferes with the frequency response of the element when used in filters, unless the w/l ratio is 0.1 or less. Although for long thin bars the temperature coefficient is only about 2 parts per million per degree, this is greater than the minimum obtainable with $5^{\circ} \mathrm{X}$-cut bars.

## 1-97. CHARACTERISTICS OF X-CUT PLATES IN WIDTH-EXTENSIONAL MODE

Description of Element: X-cut; xz; width-extensional mode.
Frequency Range: 125 to 400 kc .
Frequency Equation: $f=\frac{\mathrm{nk}_{1}}{\mathrm{w}}(\mathrm{n}=1,2,3, \ldots)$
Frequency Constant: Varies with w/ I ratio; see


Figure 1-22. Frequency characteristics of X-cut erystal vibrating in width-extensional mode, where the width is parallel to the $Y$ axis. w/l ratios not included between the two outer curves will have interfering modes. $K_{\text {f }}$ is in ke-inches
figure 1-22, which shows the face dimensions that will have a single frequency near the desired resonance. Plates with dimensions not included between the two outer curves will have interfering modes.
Temperature Coefficient: Negative; approximately 10 parts per million per degree centigrade, but varies with w/l ratio.
Methods of Mounting: Sandwich, air gap, wire, knife-edge clamp, pressure pins, cantilever clamp.
Advantages: If cut with dimensions within the single-frequency range shown in figure 1-22, this element can be used in temperature-controlled low-frequency oscillators and narrow-band-pass filters. With the thickness dimension ground for a particular high frequency, the same crystal unit may be used to generate either of two widely separate frequencies.
Disadvantages: Relatively large temperature coefficient prevents this element from being preferred over the low-coefficient cuts.

## THE $5^{\circ} \mathrm{X}$ CUTS

$1-98$. The $5^{\circ} \mathrm{X}$ cut is the orientation that provides a zero temperature coefficient for the lengthwise vibrations of long, thin X bars, as shown in figure 1-23. Thus, this cut is preferred over the nonrotated X cut for use in low-frequency filters and control devices. Its length-extensional, length-width-flexural, and duplex length-thickness-flexural modes are defined as the elements $E, H$, and J , respectively ; the last named element, J, providing the lowest frequencies. However, the $5^{\circ} \mathrm{X}$ elements are also coupled to the other modes, so that for $w / 1$ ratios much greater than 0.1 the frequency spectrum is little improved over that of the lengthextensional mode of the X cut. Furthermore, as the w/l ratio increases, so also does the temperature coefficient. For these reasons the $5^{\circ} \mathrm{X}$ elements are especially advantageous only when the $w / 1$ ratio is 0.1 or less. These long, thin bars are used commercially for the control of low-frequency oscillators and as filters, and are particularly adaptable for use in telephone carrier systems.

## 1-99. CHARACTERISTICS OF ELEMENT E

Description of Element: $5^{\circ} \mathrm{X}$ cut; xyt: $5^{\circ}$; lengthextensional mode.
Frequency Range: 50 to 500 kc .
Frequency Equation: $f=\frac{n k_{1}}{1}(n=1,2,3, \ldots)$
Frequency Constant: Varies with w/1 ratio (see figure 1-24):
Temperature Coefficient: Varies with w/l ratio (see figure 1-25, which holds for temperatures between 45 and 55 degrees centigrade). The


Figure 1-23. Temperature coefficient for length-extensional mode of long, thin X-group bars versus angle of rotation *


Figure 1-24. Frequency consfant versus w/I ratlo for element $E$ *
frequency deviation of representative $\mathbf{E}$ elements of different $w / 1$ ratios is shown in figure 1-26, where the initial frequency is taken at $25^{\circ} \mathrm{C}$.
Note that the temperature coefficient in parts per hundred per degree is the slope of a curve, and varies from positive to zero to negative as the temperature increases.
Methods of Mounting: Wire, knife-edge clamp, pressure pins, cantilever clamp; more than one pair of electrodes required for overtones.
Advantages: The low temperature coefficient and a large ratio of stored mechanical to electrical energy make this element preferred for filter networks. Long, thin bare have only a very


Figure 1-25. Temperature coefficient versus w/l ratio for clemont $E$ at femperatures between $45^{\circ}$ and $55^{\circ} \mathrm{C}$ *


Figure 1-26. Percentage irequency deviation for $E$ elements of various w/l ratios. Initial femperature $=25^{\circ} \mathrm{C}$
weak coupling to other modes and are used for both filter networks and low-frequency oscillators. If a w/l ratio greater than 0.15 is desired, a ratio of approximately 0.39 is optimum insofar as a low temperature coefficient is concerned.
Disadvantages: At w/ ratios between 0.2 and 0.3 the length-extensional mode is so closely coupled to the length-width fiexure that the crystal is useless; as the width is increased the coupling of the length-extensional to the face-shear mode becomes stronger, and the temperature coefficient becomes larger. However, because of the large electro-mechanical coupling of this element, w/l ratios of 0.35 to 0.5 can still be favorably used in filters if a temperature coefficient less than 4 parts per million is not required.
1-100. CHARACTERISTICS OF ELEMENT H
Description of Element: $5^{\circ} \mathrm{X}$ cut; xyt: $5^{\circ}$; lengthwidth flexure mode.
Frequency Range: 10 to 100 kc .


Figure 1-27. Frequency constant varsus w/l ratio for olement $H$


Figure 1-28. Temperature coefficient versus w/l ratio for tement $H^{*}$

Frequency Equation: $f=\mathrm{nk}_{\mathrm{s}} \mathbf{w} / \mathbf{l}^{\mathbf{2}} \quad(\mathrm{n}=1,2,3$, ...)
Frequency Constant: Varies with w/l ratio (see figure 1-27).
Temperature Coefficient: Varies with w/l ratio (see figure 1-28).
Methods of Mounting: Wire, in vacuum; free-free flexures of long, thin bars have nodal points for the fundamental vibration at a distance of $0.224 \times 1$ from the ends; two electrically opposite pairs of electrodes are plated on each side of the YZ faces, with "ears" at the nodal points for soldering to the mounting wires. See figure 1-29. When the polarity of the lower electrodes causes a contraction of the bar, the polarity of the upper electrodes causes an extension, and vice versa-the over-all result being a flexural deformation.
Advantages: For long, thin bars the length-width flexural mode is resonant at much lower frequencies than is the length-extensional mode. This advantage, combined with the favorable electro-mechanical coupling, and reasonably low temperature coefficient, has made this element useful in very-low-frequency filters where only a single frequency is to be selected. When mounted in vacuum, a $Q$ of 30,000 is obtainable.


Flgure 1-29. Element H, showing division of olectrode plating for exciting fundamental mode. Similarly divided dectrodes are on reverse side. The nodal "ears," where the mounting wires are affached, are at a disfance of approximatoly 0.224 times the longth from the ends *


Figure 1-30. Frequency constant versus $\mathbf{t} / \mathrm{l}$ ratio for element $J$


Figure 1-31. Percentage frequency deviation for J. elements. The smaller t/I ratio is representetive of a 1.2-kc element, and the larger i/l ratio is ropresentative of a lo-ke element

Figure 1-32. Frequency constant versus w/l ratio for various resonances of $-18^{\circ} \mathrm{X}$-cut crystal. A is the width-extensional mode. $B$ is the face-shear mode, which, at small w/I ratios, is strongly coupled to D, the second flexural mode. C represents the band between the antiresonamt (upper curve) and the resonant (lower curve) frequencies of the length-extensional mode of eloment F. Note the weak coupling between C and D-8 *

Disadvantages: The ratio of stored mechanical to electrical energy is not as large as that of the length-extensional mode, and because of this, the element does not give as broad a band-pass spectrum. Also, the effect of the shear stresses causes the temperature coefficient to become highly negative as the $w / l$ ratio is increased. Finally, the damping effect of the air is greater for flexural than for other vibrations, so that flexure crystals should be mounted only in evacuated containers.

## 1-101. CHARACTERISTICS OF ELEMENT J

Description of Element: Duplex $5^{\circ} \mathrm{X}$ cut; xyt: $5^{\circ}$ (right quartz), and xyt: $5^{\circ}$ (left quartz); length-thickness flexure mode.
Frequency Range: 0.4 to 10 kc .
Frequency Equation: $\mathrm{f}=\mathrm{nk}_{\mathrm{g}} \mathrm{t} / \mathrm{l}^{\mathbf{2}} \quad(\mathrm{n}=1,2,3$, . . .)
Frequency Constant: Varies with t/l ratio (see figure 1-30).
Temperature Coefficient: Varies with both the $\mathrm{t} / \mathrm{l}$ ratio and the temperature; figure $1-31$ shows the total relative frequency deviation of two elements of different $t / 1$ ratios, the initial frequencies being those at $25^{\circ} \mathrm{C}$. The temperature coefficients in parts per hundred at a given temperature are the slopes of the curves at that point. Note that the temperature at which a zero coefficient is obtained increases as the $t / 1$ ratio decreases. At temperatures below that of a zero-coefficient point, the coefficient is positive ; at temperatures above, it is negative.
Methods of Mounting: Headed-wire, in vacuum; two thin plates are cemented together with polarities opposed so that only one pair of electrodes, plated on opposite YZ faces, are required; the crystal element is supported at the nodal points, which for the fundamental vibration are at a distance $0.224 \times 1$ from each end.
Advantages: Small temperature coefficient and low resonant frequencies (among the lowest obtainable with quartz) make this element useful in providing stable control for sonicfrequency oscillators, and as a component of single-frequency filters.
Disadvantages: Not economical for control of frequencies above 10 kc .

1-102. CHARACTERISTICS OF ELEMENT F
Description of Element: $-18.5^{\circ} \mathrm{X}$ cut; xyt: $-18.5^{\circ}$; length-extensional mode.
Frequency Range: 60 to 300 kc .

Frequency Equation: $f=\frac{\mathbf{n k}_{1}}{\mathrm{l}}(\mathrm{n}=1,2,3, \ldots)$
Frequency Constant: Varies slightly with w/l ratio (see figure 1-32).
Temperature Coefficient: 25 parts per million per degree centigrade-varies very little with changes in the $w / l$ ratio.
Methods of Mounting: Wire, knife-edge clamp, pressure pins, cantilever clamp; more than one pair of electrodes required for overtones.
Advantages: The extremely weak coupling of this element to the face-shear and second flexure modes, represented by curves $B$ and $D$, respectively, in figure 1-32, permits a better frequency spectrum than can be obtained with element E for $\mathrm{w} / \mathrm{l}$ ratios greater than 0.1. For this reason, the $F$ element used to be preferred over the $E$ element as a filter plate, and was the principal quartz element in the channel filters of coaxial telephone systems. This is no longer true because channel filters now use $+5^{\circ} \mathrm{X}$ plates which are smaller and conserve quartz.
Disadvantages: Relatively large temperature coefficient prevents this element from being preferred for oscillator control or as a channel filter if wide variations in temperature are to be expected. Also, the $F$ plate is larger than the $E$ plate of the same frequency and thus consumes more quartz.

## 1-103. CHARACTERISTICS OF ELEMENT M

Description of Element: MT cut; xytl: $0^{\circ}$ to $8.5^{\circ} /$ $\pm 34^{\circ}$ to $\pm 50^{\circ}$; length-extensional mode.
Frequency Range: 50 to 500 kc .
Frequency Equation: $f=\frac{\mathrm{nk}_{1}}{1} \quad(\mathrm{n}=1,2,3, \ldots)$
Frequency Constant: Varies with w/l ratio and angles of rotation (see figure 1-33).
Temperature Coefficient: Varies with $w / 1$ ratio and angles of rotation (see figure 1-34), and with the temperature. The total relative frequency deviation of an $8.5^{\circ} / \pm 34^{\circ} \mathrm{M}$ element, where the initial frequency is taken at $40^{\circ} \mathrm{C}$, is shown in figure 1-35. Note that the temperature coefficient, which is the slope of the curve, changes from positive to negative as the temperature increases, with the zero coefficient occurring at $63^{\circ} \mathrm{C}$.
Methods of Mounting: Wire, knife-edge clamp, pressure pins, cantilever clamp; more than one pair of electrodes required for overtones.
Advantages: The MT crystals were developed in an effort to overcome the large negative temperature coefficients of the X -cut and the $5^{\circ} \mathrm{X}$ -

## Standard Quartz Elemenis

cut length-extensional modes for the larger w/l ratios. See figures 1-21 and 1-25. The unfavorable temperature characteristics are caused by the coupling of the extensional to the face-shear mode, the latter having a high negative temperature coefficient. However, if the crystal is rotated about its length, an orientation will be found where the face-shear mode has a zero temperature coefficient; that is, the coefficient will pass from negative to positive values. The low temperature coefficient of the length dimension will thus be preserved even though the coupling to the shearmode has not, itself, been diminished. The low temperature coefficient makes the M element advantageous for osciliator control in the 50 -to- 100 kc range, and for use in narrow band filters, such as pilot-channel filters in carrier systems, where wide temperature ranges are to be encountered. The $8.5^{\circ} / 34^{\circ}$ rotation with a $w / 1$ ratio of approximately 0.42 provides the greatest electromechanical coupling of the $M$ elements, and hence the broadcast bandpass of the MT cut for use in filters.
Disadvantages: The electromechanical coupling rapidly decreases as the $w / l$ ratio increases, so that at ratios greater than 0.7 the element is too selective for filter use, and of too small a piezoelectric activity to be advantageous for oscillator control. Maximum electromechanical coupling is obtained with $w / l$ ratios of 0.39 to 0.42 ; but for a maximum bandwidth the $E$ element is preferred. Although the interference of the face-shear temperature coefficient is reduced, the coupling to that mode remains relatively strong; so where the temperature varies very little, or where the secondary frequency effects are undesirable, the F element is preferred.

## 1-104. CHARACTERISTICS OF ELEMENT N

Description of Element: NT cut; xytl: $0^{\circ}$ to $8.5^{\circ} /$ $\pm 38^{\circ}$ to $\pm 70^{\circ}$; length-width flexure mode.
Frequency Range: 4 to 100 kc .
Frequency Equation: $f=\frac{\mathrm{nk}_{5} w}{1^{1}}(\mathrm{n}=1,2,3, \ldots)$
Frequency Constant: Varies with w/l ratio (see figure 1-36).
Temperature Coefficient: For w/l ratios of 0.2 to 0.5 , low coefficients are obtained by double rotations of $0^{\circ}$ to $+8.5^{\circ} / \pm 50^{\circ}$. Typical frequency deviation curves are shown in figure 1-37, where the initial temperature is taken at $25^{\circ} \mathrm{C}$. Note that a zero temperature coeff-


Figure 1.33. Frequency constant versus w/I ratlo for $M$ elemonts having low temperature coufficionfs. C is the curve of the most commonly used MT orientation*


Figure 1-34. Temperature coefficiont versus w/I ratio for M oloments *
cient occurs at approximately $10^{\circ} \mathrm{C}$. To produce a zero temperature coefficient at $25^{\circ} \mathrm{C}$ for w/l ratios of 0.05 , the angles of rotation should be as shown in figure 1-38.
Methods of Mounting: Wire, in vacuum; special characteristics are the same as for the $H$ element. See paragraph 1-100.


Figure 1-37. Frequency-temperature characteristics of element N. The larger w/l ratio is typical of 100 -ke elemenis, and the smaller w/l sotio is typical of 16-ke elements

Higure 1-35. Frequency-femperature characteriefics of olement $M$ *

Figure 1.36, Frequency consfant versus $w / l$ ratio for eloment $N$


Figure 1-38. Angles of rotation for N eloment with a w/I ratio of 0.05 which will provide zero temperature coefficient af $25^{\circ} \mathrm{C}$ *

Advantages: The principal advantage of the N element is that the second rotation reduces the temperature coefficient for the flexure vibration of long, thin crystals. This is accomplished by changing the width from near parallelism to the $Z$ axis to near parallelism to the $X$ axis. Theoretically the ideal rotation would be $90^{\circ}$, except that the piezoelectric effect would be reduced to zero. As a compro-
mise, secondary rotations, about the length, effect would be reduced to zero. As a compro-
mise, secondary rotations, about the length, of $39^{\circ}$ to $70^{\circ}$ are made. Besides reducing the flexure-mode temperature coefficient of the long, thin crystals, the rotation also reduces the negative coefficient for the shear modes at the higher $\mathrm{w} / \mathrm{I}$ ratios, as in the case of the M element. Where wide temperature ranges
must be met, this element is preferred for very-low frequency oscillators, and in singlefrequency filter selectors. As the control element of an oscillator, it can maintain the frequency within $\pm 0.0025 \%$ over a normal room-temperature range without temperature control.
Disadvantages: The electromechanical coupling is rather weak, more so for the larger than for the smaller w/l ratio. As a consequence, the bandwidth is too narrow for the element to be used as a band-pass filter of communication channels, and the piezoelectric activity is so low that special circuits are required for its use in oscillators.

## THE V CUT

1-105. The V cut, developed by S. A. Bokovoy and C. F. Baldwin of RCA, is actually an entire series of cuts obtained by a sequence of double rotations of an initial X-cut plate. The first rotation angle, $\phi$, is taken about the $Z$ azis, and the second rotation angle, $\theta$, is taken about the $Y^{\prime}$ axis (the dimension of the crystal that is initially parallel to the $Y$ axis). For each angle $\phi$, there is an angle $\theta$ at which the crystal will have a given temperature coefficient for a particular mode of vibration. Normally, the combination of angles desired is one that will provide a zero temperature coefficient; however, it may be that a small positive or negative coefficient is required to counterbalance an opposite temperature coefficient inherent in the external circuit to which the crystal is to be connected. For this purpose curves of $\theta$ plotted against $\phi$ are shown in figures 1-40 to $1-41$ for small positive and negative temperature coefficients, as well as for a zero temperature coefficient. Other $\phi$ and $\theta$ combinations may be extrapolated to give temperature coefficients differing from the actual values shown. It should be noted that when the rotation about the $Z$ axis is equal to $\pm 30^{\circ}$, the thickness dimension becomes parallel to a $Y$ axis, and hence the crystal is in the position of the $Y$ cut, with the $Y^{\prime}$ axis coinciding with an $X$ axis. Thus, if $\phi= \pm 30^{\circ}$, the V cut is essentially the same as a rotated $Y$ cut, and in this case would embrace practically the entire $Y$ family. On the other hand, if $\phi=0^{\circ}$, the V cut becomes simply a singly rotated $X$ cut-but with rotations about the $Y$ axis, not the $X$ axis as in the case of the $5^{\circ} \mathrm{X}$ and the $-18^{\circ} \mathrm{X}$ cuts. However, when $\phi=0^{\circ}$, the $V$ cut does overlap the MT and NT cuts.

## 1-106. CHARACTERISTICS OF V-CUT PLATES IN THICKNESS-SHEAR MODE

Description of Flement: V cut; xalw or xywl: $15^{\circ}$ to $29^{\circ} /-14^{\circ}$ to $-54^{\circ}$ and $13^{\circ}$ to $29^{\circ} / 27^{\circ}$ to $42^{\circ}$ (see temperature coefficient curves in figure 1-40 for exact $\phi$ and $\theta$ combinations); thickness-shear mode.
Frequency Range: 1000 to $20,000 \mathrm{kc}$ (fundamental) ; higher frequencies on overtones.
Frequency Equation: $f=\frac{k_{s}}{t}$ (fundamental vibration when $t \ll 1$ and $w$ ). Figure $1-39$ shows the frequency constant of the zero-tempera-ture-coefficient series of $V$ cuts as a function of the first rotation angle. The upper curve, designated $k_{3}(+\theta)$, applies to positive angles of $\theta$, the second rotation, whereas the lower
curve, designated $k_{3}(-\theta)$, applies to negative angles of $\theta$.
Temperature Coefficient: Figure 1-40 shows the combinations of $\phi$ with positive values of $\theta$ that provide temperature coefficients of +15 , 0 , and -15 parts per million per degree centigrade, and those combinations of $\phi$ with negative values of $\theta$ that provide temperature coefficients of $+5,0$, and -5 parts per million per degree centigrade.
Methods of Mounting: Sandwich, air gap, clamped air-gap, button.
Advantages: The principal advantage of the $V$ cut is that a given temperature coefficient may be obtained from a large choice of orientations, and with a minimum in trial-and-error procedure. Not only can a series of zerocoefficient plates be obtained, but also plates with coefficients of desired sign and magnitude for annulling the known frequency-tem-


Figure 1-39. Frequency constant versus $\phi$ (angle of rotation about $Z$ axis) for the thicknexs-shear mode of V-cut crystals when $\theta$, the second angle of ratation, is to chosen that a zero temperature coefficient is obfained. The upper and lower curves are for positive and negative valves of 0 , respectively
perature effects of the circuits in which the plates are to be used. The $V$ cut is the only member of the $X$ group that provides a zero temperature coefficient for high-frequency vibrations; and because of the large choice of rotation angles, one or the other of the $V$ orientations will frequently permit the maximum use of an unfaced or badly twinned mother crystal. Because their larger frequency constants permit a thicker and less fragile crystal, the orientations with a negative $\theta$ are preferred for the higher frequencies. Also, small deviations in negative values of $\theta$ produce less variation in the temperature coefficient than do the same deviations in positive values of $\theta$. Hence, the negative orientations of $\theta$ are also generally more dependable for obtaining a desired temperature coefficient. On the other hand, positive values of $\theta$ permit a less bulky crystal for the lower frequencies, a less critical frequency constant, less interference from spurious frequencies, and for accurately determined orientations, a broader temperature deviation for a given deviation in frequency. At $\phi=30^{\circ}$, the values of $\theta=-49^{\circ},+31^{\circ}$, and $+35^{\circ} 31^{\prime}$ are substan-


Figure 1-40. Relations of $\theta$ to $\phi$, for thickness-shear mode of V cut, which provido the temperature coefficlents indicated for each curve
tially the same as the BT, AC, and AT cuts, respectively, of the $Y$ group, as described in paragraphe 1-114, 1-111, and 1-112. The chief use of the thickness-mode $V$ cut is for the control of high-frequency oscillators.
Disadvantages: The possibility of spurious frequencies close to the desired fundamental is the most troublesome limitation of the $V$ cut operating in a thickness-shear mode. As a general rule, the coupling between the desired and the stray modes diminishes as the initial rotation $\phi$ is increased. At values of $\phi$ less than $13^{\circ}$, the interference is too great for stable operation. Because of the relatively poor frequency spectrum, the $V$ cut is not readily adaptable for use in selective networks. With a certain amount of cut-and-try experimentation, the more objectionable modes may be reduced by grinding down the width and length dimensions. For angles of $\phi$ close to $30^{\circ}$ the length and width dimensions most important to avoid are approximately the same as those given in paragraphs 1-112 and 1-114 for the AT and BT cuts, respectively.

## 1-107. CHARACTERISTICS OF V-CUT PLATES IN FACE-SHEAR MODE

Description of Element: V cut; xalw or xywl: $0^{\circ}$ to $30^{\circ} / \pm 45^{\circ}$ to $\pm 70^{\circ}$ (see temperature coefficient curves in figure 1-41 for exact $\phi$ and $\theta$ combinations) ; face-shear mode.
Frequency Range: 60 to 1000 kc .
Frequency Equation: $f=k_{*} / \mathbf{w}$ (fundamental for square plates).
Frequency Constant: Insufficient data exist to plot the curve of $k_{4}$ for all the combinations of $\phi$ and $\theta$ corresponding to this element. However, in the case of the zero-coefficient plates, as the positive value of $\theta$ approaches $37.5^{\circ}, \mathrm{k}_{6}$ approaches $3070 \mathrm{kc}-\mathrm{mm}$, and as the negative value of $\theta$ approaches $-52.5^{\circ}, \mathrm{k}$, approaches $2070 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: Figure 1-41 shows the combinations of $\phi$ and $\theta$ that provide temperature coefficients of $+5,0$, and -5 parts per million per degree centigrade.
Methods of Mounting: Wire, cantilever clamp.
Advantages: The principal advantage is the low temperature coefficient, which makes the element useful for low-frequency oscillators and filters. The large choice of orientation angles is also advantageous for obtaining the maximum number of cuts from a given mother crystal, particularly if the presence of twinning or other defects limit the dimensions in


Figure 1-41. Relations of $\theta$ to $\phi$, for faco-shoai mode of $V$ cut, which provide tomperature coefficients of $0,+5$, and -5 parts, per million per dogree centigrode
the directions at which rough bars would normally be cut. Also, the angles for small predetermined positive and negative coefficients permit a crystal to be cut which can exactly annul the known temperature effects of the external circuit. As indicated in figure 1-41, small deviations in the orientations angles will cause minimum deviations in the temperature coefficient when $\phi=0^{\circ}$ to $15^{\circ}$, and $\theta$ is negative. On the other hand, maximum piezoelectric activity is obtained when $\phi$ is large, and $\theta$ is positive. As a general rule, the positive values of $\theta$ are used for the higher frequencies and the negative values of $\theta$ for the lower frequencies. The zero-temperature cuts for $\phi=30^{\circ}$ are substantially the same as the CT and DT cuts of the Y group. See paragraphs 1-115 and 1-116, respectively.
Disadvantages: Care must be taken that flexure modes are not strongly coupled to the faceshear mode. Such coupling may be reduced by making the plates square, or nearly so. For angles of $\phi$ approaching $30^{\circ}$, the thickness should be approximately within the limits given for the C and D elements in paragraphs 1-115 and 1-116.

## The $Y$ Group

1-108. The principal crystals of the Y group are listed below with the frequency range for which they have found commercial application:

| Name of Cut | Frequency Range in KC |
| :---: | ---: |
| Y | 1000 to 20,000 |
| AC | 1000 to 15,000 |
| AT | 500 to 100,000 |
| BC | 1000 to 20,000 |
| BT | 1000 to |
| CT | 300 to |
| DT | 60 to |
| ET | 600 to |
| FT | 1800 |
| GT | 150 to |
| GT | 1500 |
|  |  |

Figure 1-42 shows the orientations of a yx initial position ( $Y$ cut with the length parallel to the $X$ axis) for the various cuts. In special cases the width may be parallel to the X axis, but this is the exception rather than the rule, unless the plate is square or circular. With the exception of the GT cut, the crystals of the $Y$ group are used in their shear modes-face shear for the low-frequency elements, and thickness shear for the high-frequency elements. The Y cut, itself, has a large positive temperature coefficient; and, because of coupling between the thickness-shear mode and the overtones of the face-shear mode, it also exhibits sharp irregularities in its frequency spectrum. However, by rotation about the $\mathbf{X}$ axis, zero temperature coefficients may be obtained, and the coupling between the shear modes can be greatly diminished. This coupling becomes zero at the angles of the $A C$ and $B C$ cuts, and the frequency constant of the thickness-shear mode has minimum and maximum values, respectively, for these two orientations. Figure 1-43 shows the thicknessshear frequency constant, and figure 1-44 the thickness-shear temperature coefficient, with each plotted as a function of the angle of rotation. For the face-shear mode, the frequency constant and the temperature coefficient are shown in figures 1-45 and 1-46, respectively, plotted as functions of the angles of rotation.

## THE Y CUT

1-109. The $Y$ cut was introduced commercially in the late 1920's, at which time its principal advantage was that it could be clamped at its edges, whereas the X cut would not oscillate if the edge movement were even slightly restricted. The use of a $Y$ cut, vibrating in a shear-mode, was originally suggested by E. D. Tillyer of the American Optical Company, to whom a U. S. patent was


Figure 1-42. Rotation angles of $Y$ cut about $X$ axis which provide the principal members of the $Y$ group. The GT cut is the only member having a second rotation ( $\pm 45^{\circ}$ about the $Y^{\prime}$ axis). The $+X$ sign indicates that the posilive end of the $X$ axis points toword the observer
issued in 1933. For this reason, the $Y$ cut is sometimes called the Tillyer cut. For several years this crystal was used extensively in commercial and military transmitters mounted in mobile equipment, and also in commercial broadcast transmitters where the $Y$ cut's readily excited oscillations permitted the use of crystal ascillators with low plate voltages. However, due to the strong coupling between the thickness-shear and the overtones of the face-shear and flexure modes, the $Y$ cut's frequency spectrum is very poor. Also, small irregularities in the dimensions of the crystal readily produce abrupt changes in the frequency.

A typical frequency-temperature curve of a Y-cut crystal is shown in figure 1-47. Today, the Y cut has been almost entirely replaced by the rotated cuts having small temperature coefficients, and the $Y$ cut's only major application now is that of transducer for generating shear vibrations in solids.

## 1-110. CHARACTERISTICS OF Y-CUT PLATES IN THICKNESS-SHEAR MODE

Description of Element: Y cut; yx or yz ; thick-ness-shear mode.
Frequency Range: 500 to $20,000 \mathrm{kc}$; much lower


Figure 1-43. Frequency constant versus angle of rotation about $X$ axis for thickness-shear elements of $Y$ greup. (Values shown for Y, BT, and BC cuts are smaller than the average) *


Figure 1-44. Temperature coefficient versus angle of rotation about $X$ axis for thicknose-shear elements of $Y$ group ${ }^{*}$


Figure 1-45. Frequency censtant versut angle of roterthon chow $X$ axis for ferce-shoar dements of $Y$ group
frequencies when bonded to solids for use as transducer.
Frequency Equation: $f=\frac{\mathbf{k}_{\mathbf{3}}}{\mathbf{t}}$ (fundamental vibration).
Frequency Constant: $\mathbf{k}_{\mathbf{z}}=1981 \mathrm{kc}-\mathrm{mm}$ (average value).
Temperature Coefficient: Varies with dimensions of crystal and with temperature but is usually between 75 and 125 parts per million per degree centigrade, and is positive, with an average value of 86 parts per million per degree centigrade.
Methods of Mounting: Sandwich ; air gap, clamped air gap; bonded to solids when used as transducer.
Advantages: Ratio of stored mechanical to electrical energy is larger than that of any other


Figure 1-47. Tomperature-frequency choracteristic: typical of the Y-cut, thicknese-shear clement. The frequancy jumps are most apt to occur whon small discrepancies are prosent in the thickness-dimension


Figure 1-46. Tomperoture coeficient versus angle of rotation about $X$ axis for face-shear dements of the $Y$ group
quartz element; this large ratio, combined with the quartz crystal's superior strength, makes the $Y$ cut desirable as a generator of shear vibrations in solids for the purpose of measuring or testing the solids' physical properties. This element is the easiest of all quartz cuts to excite into vibration, and thus requires the lowest voltages for operation. Large temperature coefficient makes element useful as a sensitive detector of variations in temperature.
Disadvantages: Large temperature coefficient, discontinuities of resonant frequencies, and poor frequency spectrum make this element a secondary choice for use in either oscillator or filter circuits. Special $Y$ cuts, such as the block- and doughnut-shaped crystals in figure $1-48$, vibrate in a combination mode composed of coupled shear and flexure modes, and have zero temperature coefficients at certain temperatures. However, because of the prevalence of spurious frequencies, the large volume of quartz used per cut, and the difficulties of mounting, these crystals have little practical use.


Figure 1-48. Y-cuf block and doughnut-shaped crystals which con provide zero temperature coefficients for certain combination modes

## 1-111. CHARACTERISTICS OF AC-CUT PLATES IN THICKNESS-SHEAR MODE

Description of Element: AC cut; yxl : $31^{\circ}$; length-thickness-shear mode.
Frequency Range: 1000 to $\mathbf{1 5 , 0 0 0} \mathrm{kc}$ (fundamental vibration).
Frequency Equation: $f=\frac{k_{8}}{t}$ (fundamental vibration when $t \ll 1$ and $w$ ).
Frequency Constant: $\mathrm{k}_{3}=1656 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 20 parts per million per degree centigrade; positive.
Methods of Mounting: Sandwich, air gap, clamped air gap, button.
Advantages: This element vibrates in a very pure length-thickness mode with an excellent frequency spectrum. It has the lowest frequency constant of all the quartz thickness modes and thus permits a smaller thickness, and hence a more economical cut, for use at the low end of the high-frequency spectrum. For a given temperature, the electrical parameters of an AC crystal unit can be predetermined with an accuracy equal to, or greater than, that of the more commonly used AT units.
Disadvantages: The principal disadvantages of the $A C$ cut is its relatively large temperature coefficient; because of this the element has found little commercisi use, and the low-coefficient AT cut, with an orientation close enough to that of the AC for the coupling between the shear modes to be small, is generally preferred.

## 1-112. CHARACTERISTICS OF ELEMENT A

Description of Element: AT cut; yxl: $35^{\circ} 21^{\prime}$; length-thickness-shear modes; or, yzw: $35^{\circ}$ 21'; width-thickness-shear mode.

Frequency Range: 500 to 1000 kc (special cuts) ; 1000 to $15,000 \mathrm{kc}$ (fundamental vibration) ; 10,000 to $100,000 \mathrm{kc}$ (overtone modes).

## Frequency Equation:

$f=k_{3} / t$ (fundamental vibration when $t \ll 1$ and $w$ )

$$
f=k_{s} \sqrt{\frac{m^{2}}{t^{2}}+a_{1} \frac{n^{2}}{l^{2}}+a_{2} \frac{(p-1)^{2}}{w^{2}}}
$$

where $m, n$, and $p$ are integers.
Frequency Constant: $\mathrm{k}_{\mathrm{s}}=1660 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 0.0 at $25^{\circ} \mathrm{C}$; figure $1-49$ shows the total relative frequency deviation for the normal maximum, minimum, and average angles of this element; the temperature coefficient at each point on a curve is the slope at that point in parts per hundred. At $\phi=35^{\circ} 15^{\prime}$, the temperature coefficient will vanish at $45^{\circ} \mathrm{C}$, changing from negative to positive as the tempersture increases. Optimum orientations for zero coefficients at other temperatures are given below:

| Deg. $C$ | $\phi$ |
| :--- | :--- |
| 20 | $35^{\circ} 18^{\prime}$ |
| 20 | $35^{\circ} 27^{\prime}$ (overtones) |
| 75 | $35^{\circ} 31^{\prime}$ |
| 75 | $35^{\circ} 33^{\prime}$ (overtones) |
| 85 | $35^{\circ} 83^{\prime}$ |
| 85 | $35^{\circ} 36^{\prime}$ (overtones) |
| 100 | $35^{\circ} 36^{\prime}$ |
| 190 (max.) | $36^{\circ} 26^{\prime}$ |

Methods of Mounting: Sandwich, air gap, clamped air gap, button.
Advantages: The excellent temperature-frequency characteristics make this element preferred for high-frequency oscillator control wherever wide variations of temperature are to be encountered; it is particularly applicable


Figure 1-49. Temperature-frequency characteristics of element $A$
for aircraft radio equipment where sharp changes in temperature may be frequent, but where the added weight of constant-temperature ovens is undesirable. The angle of orientation is sufficiently close to that of the AC cut for the coupling between the shear modes to be weak, so that the resonant frequency can be isolated from that of other modes, except for certain dimensions of $w$ and 1 . The A element also shares the low frequency constant of the AC element, and this is preferred for frequencies at the low end of the highfrequency spectrum. However, because of its superior temperature-frequency and piezoelectric characteristics as compared with the BT characteristics, the A element may well be preferred for the control of frequencies in the vhf range, even though the BT cut has the larger frequency constant.
Disadvantages: Because of the large thickness dimensions that would be required, the A element is generally not economical for the generation of frequencies below 1000 kc , although special circular cuts have been used at frequencies as low as 500 kc . In its normal highfrequency range, the most troublesome problem is to find the proper length and width dimensions which will permit the desired frequency to be widely separated from other modes. Although the orientation of the AT cut is close to that of the AC cut, there still exists a fair amount of coupling to the faceshear modes, and to the extensional and flexural modes along the X axis. Sufficient information is not available to avoid a certain amount of trial and error in grinding and finishing an AT blank to provide an optimum frequency spectrum at a desired frequency; however, there are certain $X$ and $Z$ ' (the dimension parallel to the $Z$ axis before rotation) values that can be avoided by use of the frequency equations which hold approximately for the less complex of the unwanted modes. The following equations give the face dimensions of an AT cut which will produce unwanted resonances at the same frequency, $f$, as the thickness-shear mode.
For extensional modes along X:

$$
X=\frac{2438 n}{f}(n=1,3,5, \ldots)
$$

For flexure modes along $\mathbf{X}$ :

$$
X=\frac{1338.4 n}{f}(n=2,4,6, \ldots)
$$

For shear modes along $X$ :

$$
X=\frac{2542.0 n}{f}(n=1,3,5, \ldots)
$$

For shear modes along $Z^{\prime}$ :

$$
Z^{\prime}=\frac{2540.0 n}{f}(n=1,3,5, \ldots)
$$

With $f$ expressed in $k c, X$ and $Z$ are given in mm . Either $\mathbf{X}$ or $\mathrm{Z}^{\prime}$ may be the length, with the other dimension being the width. It has been found that the unwanted modes are somewhat restricted by giving the plate a convex contour, and also by the use of circular plates. The convex contour is possible for all but the very thin plates that are used at frequencies above $15,000 \mathrm{kc}$. A 1000 -kc crystal may have a contour of 3 to 5 microns. The equations above hold for flat plates, and be- come increasingly in error as the contour is increased.

1-113. CHARACTERISTICS OF BC-CUT PLATES IN THICKNESS-SHEAR MODE
Description of Element: BC cut; yxl: $-60^{\circ}$; length-thickness-shear mode.
Frequency Range: 1000 to $20,000 \mathrm{kc}$ (fundamental vibration).
Frequency Equation: $f=\frac{\mathbf{k}_{\mathbf{s}}}{\mathrm{t}}$ (fundamental vibration when $t \ll 1$ and $w)$.
Frequency Constant: $\mathrm{k}_{\mathrm{s}}=2611 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 20 parts per million per degree centigrade; negative.
Methods of Mounting: Sandwich, air gap, clamped air gap, button.
Advantages: The advantages and disadvantages of the $B C$ cut are similar to those of the $A C$ cut, except that the BC thickness-shear frequency constant is the highest obtainable for a rotated $Y$ cut. A BC cut may thus have a greater thickness for the same frequency, and hence be less likely to be shattered from overdrive or mechanical shock-a distinct advantage at the higher fundamental frequencies where very thin crystals are used. Since the BC orientation is the negative angle of rotation which provides zero coupling between the shear modes, the element vibrates in a very pure length-thickness mode with an excellent frequency spectrum. For a given tempersture, the electrical parameters of a BC crystal unit can be predetermined with an accuracy equal to or greater than that of the more commonly used BT units.
Disadvantages: As in the AC cut, the principal disadvantage of a BC cut is its relatively large
temperature coefficient. Because of this, the element is not widely used, and the zero-coefficient BT cut, with an orientation sufficiently near to that of the BC cut to have a weak coupling between the shear modes, is used instead. An added disadvantage is that the magnitude of the rotation away from the $Y$ axis is approximately double that for the AC cuts. For this reason the piezoelectric coefficient is smaller for the BC than for the AC or AT cuts, and, hence, somewhat higher voltages are required to maintain oscillations.

## 1-114. CHARACTERISTICS OF ELEMENT B

Description of Element: BT cut; yxl: $-49^{\circ} 8^{\prime}$; length-thickness-shear mode; or, $\mathrm{yzw}:-49^{\circ} 8^{\prime}$; length-width-shear mode.
Frequency Range: 1000 to $20,000 \mathrm{kc}$ (fundamental vibration).
15,000 to $75,000 \mathrm{kc}$ (overtone modes).
Frequency Equation:
$f=k_{3} / t$ (fundamental vibration when $t \ll l$ and $w$ )

$$
f=k_{3} \sqrt{\frac{m^{2}}{t^{2}}+a_{1} \frac{n^{2}}{l^{2}}+a_{2} \frac{(p-1)^{2}}{w^{2}}}
$$

where $m, n$, and $p$ are integers.
Frequency Constant: $\mathrm{k}_{3}=2560 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 0.0 at $25^{\circ} \mathrm{C}$; figure 1-50
shows the total relative frequency deviation for the normal maximum, minimum, and average angles of this element; the temperature coefficient in parts per hundred per degree centigrade at each point on a curve is the slope at that point. Zero coefficients are obtained at $20^{\circ} \mathrm{C}$ and $75^{\circ} \mathrm{C}$ when $\phi$ is $-49^{\circ} 16^{\prime}$ and $-47^{\circ} 22^{\prime}$, respectively.
Methods of Mounting: Sandwich, air gap, clamped air gap, button.
Advantages: The temperature-frequency characteristics make this element useful for highfrequency oscillator control where the temperature is not expected to vary too widely from the mean value. It is particularly applicable for use in radio equipment which is to operate at the high end of the high-frequency spectrum. Most of the high-frequency crystal oscillators employ either the BT or the AT cut, with the B element, because of its larger frequency constant, often preferred at frequencies from 10 to $20,000 \mathrm{kc}$. Since the orientation angle is near that of the BC cut, the shear modes are not too strongly coupled together; and, when ground to proper dimensions, the $B$ element exhibits a reasonably satisfactory frequency spectrum.
Disadvantages: Like the $A$ element, the $B$ element is not suitable for use at the lower frequencies because of the large thickness dimensions


Figure 1-50. Temperature-frequency characteristics of element B
that would be required. Because of its greater angle of rotation from the $Y$ axis, the BT has a smaller piezoelectric coefficient than the AT cut, and hence requires a higher voltage to maintain oscillations. Also, the temperature coefficient of the BT cut increases more rapidly than that of the AT cut when the temperature varies to either side of the zero point. Moreover, zero temperature coefficients cannot be obtained at as widely separated temperatures, as can be done with the AT cut by slightly varying the orientation angle. This limitation, however, becomes an advantage inasmuch as it reduces the percentage error when cutting a crystal to provide a given tem-perature-frequeney characteristic. The greatest problem in preparing a $B$ element is to avoid those length and width dimensions that cause the frequencies of unwanted modes to approach the frequency of the desired mode. As in the case of the AT cut, a BT blank with a good frequency spectrum will require a certain amount of trial and error in the finishing process. For the simpler modes of lower order, the following equations give the face dimensions of a BT cut which produce unwanted resonances of the same frequency, $f$, as that of the thickness-shear mode.
For flexure modes along $X$ :

$$
X=\frac{1810 n}{f}(n=2,4,6, \ldots)
$$

For shear modes along $X$ :

$$
X=\frac{1635.14 \mathrm{n}}{\mathrm{f}}(\mathrm{n}=1,3,5, \ldots)
$$

For shear modes along Z':

$$
Z^{\prime}=\frac{1664.5 n}{f}(n=1,3,5, \ldots)
$$

With $f$ expressed in kc, $X$ and $Z$ are given in millimeters. ( $Z^{\prime}$ is the dimension of the rotated $Y$ cut that originally was parallel to the $Z$ axis.) Either $X$ or $Z^{\prime}$ may be the length, with the other dimension being the width. As in the case of the $A$ element, a convex contour of a plate will aid in restricting unwanted modes. At 1000 ke the contour may be as great as 5 microns; the thin, 20,000 -ke plates, however, must be flat. The equations above hold only for flat plates, but are approximately correct if the contour is very small.

## 1-115. CHARACTERISTICS OF ELEMENT C

Description of Element: CT cut; yxl or yzw : $37^{\circ}$ to $38^{\circ}$; face-shear mode.
Frequency Range: 300 to 1100 kc .
Frequency Equation: $\mathrm{f}=\mathrm{k}_{4} / \mathrm{w}$ (fundamental of square plate).
$f=k_{i}^{\prime} \sqrt{\frac{m^{2}}{l^{2}}+a_{1} \frac{n^{2}}{w^{2}}}\binom{m=1,2,3, \ldots}{.n=1,2,3, \ldots}$
Frequency Constant: $\mathbf{k}_{4}=3070 \mathrm{kc}-\mathrm{mm}$. (Square plates are preferred since they have fewer secondary frequencies.)
Temperature Coefficient: 0.0 at $25^{\circ} \mathrm{C}$ for rotation angle of $37^{\circ} 40^{\circ}$. Figure 1-51 shows the total relative frequency deviation with temperature for maximum, minimum, and average angles of rotation for a nominal cut of $37^{\circ} 40^{\prime}$; the initial temperature is taken at $25^{\circ} \mathrm{C}$. The slope of a curve at any point is the temperature coefficient in parts per hundred per degree centigrade at that point. Note that as the rotation angle is increased, the zero coefficient is shifted to a higher temperature;


Figure 1-51. Temperature-frequency characteristics of element $C$
the same is true when the $\frac{Z^{\prime}}{X}$ ratio is increased. For square plates, zero coefficients can be obtained at higher temperatures ( $50^{\circ} \mathrm{C}$ to $200^{\circ} \mathrm{C}$ ) by rotation angles from $38^{\circ} 20^{\circ}$ to $41^{\circ} 50^{\prime}$, respectively.
Methods of Mounting: Wire, cantilever clamp.
Advantages: The CT cut is essentially a BT cut rotated approximately $90^{\circ}$ so that the face shear of the $C$ element corresponds to the thickness shear of the $B$ element. This orientation provides a zero-temperature-coefficient shear mode for generating low frequencies, without requiring a crystal of large thickness dimension. The frequency characteristics of the $C$ element, as compared with the $D$ element, are roughly analogous to those of the $B$ with the $A$ element, except that the former pair vibrate at low frequencies, and the latter at high frequencies. The C element has the higher frequency constant, so is generally preferred over the $D$ element at the high end of the low-frequency range. The $C$ element is widely used both for low-frequency oscillator control and in filters, and does not require constant temperatures control under normal operating conditions. One of its principal applications has been as the control element in frequency-modulated oscillators.
Disadvantages: Because of its larger frequency constant, the $C$ element must be cut with larger face dimensions than the $D$ element to provide the same frequency of vibration. Thus, for the generation of very low frequencies the smaller DT cut is the more economical to use. Care must be taken that flexure modes are not strongly coupled to the face-shear mode. To prevent a coincidence of resonance
between the two modes, the following thicknesses have been used:

| Frequency Range in KC | Thickness in Mils |
| :---: | :---: |
| 370 to 428 | 18.5 to 19.9 |
| 428 to 475 | 16.0 to 17.5 |
| 475 to 540 | 18.5 to 19.9 |
| 730 to 875 | 12.0 to 14.0 |
| 875 to 1040 | 16.0 to 17.5 |

## 1-116. CHARACTERISTICS OF ELEMENT D

Description of Element: DT cut; yxl or yzw: $-52^{\circ}$ to $-53^{\circ}$; face-shear mode.
Frequency Range: 60 to 500 kc .
Frequency Equation: $f=k_{k} / \mathbf{w}$ (fundamental of square plate).

$$
f=k_{i}^{\prime} \sqrt{\frac{m^{2}}{1^{2}}+a_{1} \frac{n^{2}}{w^{2}}} \quad(m=1,2,3, \ldots)
$$

Frequency Constant: $\mathrm{k}_{4}=2070 \mathrm{kc}$-mm. (Square plates are preferred since they. have fewer secondary frequencies.)
Temperature Coefficient: 0.0 at $25^{\circ} \mathrm{C}$ for rotation angle of $-52^{\circ} 30^{\prime}$. Figure 1-52 shows the total relative frequency deviation with temperature for maximum, minimum, and average angles of rotation for a nominal cut of $-52^{\circ} 30^{\prime}$, where the initial temperature is taken at $25^{\circ} \mathrm{C}$. The slope of a curve at any point is the temperature coefficient in parts per hundred per degree centigrade at that point. Note that as the rotation angle is increased, the zero coefficient is shifted to $a$ higher temperature. The upper limit for a zero coefficient is approximately $200^{\circ} \mathrm{C}$, when $\phi=-54^{\circ}$.
Methods of Mounting: Wire, cantilever clamp.


Figure 1-52. Temperature-frequency characteristics of element D

Advantages: The DT cut is essentially an AT cut rotated approximately $90^{\circ}$ so that the face shear of the D element corresponds to the thickness shear of the A element. This orientation provides a zero-temperature-coefficient shear mode for generating low frequencies, without requiring a crystal of large thickness dimension. Because the frequency constant is less than that of element $C$, the face dimensions of element $D$ are smaller for a given frequency, and hence the DT is the more economical cut for use at very low frequencies. Like the C element, the D element is widely used in both oscillators and filters, and does not require constant temperature control under normal operating conditions.
Disadvantages: At frequencies above 500 kc , the impedance effects introduced by the mounting become excessive, since the contact surfaces between the crystal and the supporting wires become rather large compared with the area of the crystal faces. Hence, the C is preferred over the $D$ element in the $500-1000 \mathrm{kc}$ range, since the higher frequency constant of the former permits a larger crystal face. To avoid strong coupling of the face-shear mode with flexure modes, certain thicknesses must be avoided. For most frequencies, however, a thickness of approximately 17 mils is satisfactory.

## 1-117. CHARACTERISTICS OF ET-CUT plates in combination mode

Deseription of Element: ET cut, with $\frac{w}{1}$ ratio approximately equal to 1.0 ; yxl or yzw : $66^{\circ} 30^{\prime}$; combination of coupled modes with second flexural vibration appearing to dominate a face-shear harmonic.
Frequency Range: 600 to 1800 kc .
Frequency Equation: $\mathbf{f}=\mathbf{k} / \mathbf{w}$ (square plate). $f=\frac{2 k}{1+w}$ (nearly square plate).
Frequency Constant: $\mathbf{k}=5350 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 0.0 at $75^{\circ} \mathrm{C}$; see figure 1-53 for total relative frequency deviation.
Methods of Mounting: Wire; preferably mounted in vacuum.
Advantages: Besides its zero temperature coefficient, the principal advantage of the ET cut is its high frequency constant, which is almost 1.8 times that of the C element. This permits an effective extension of the frequency range for this type of piate and mounting. Optimum performance is obtained at temperatures near


Figure 1-53. Temperature-frequancy characteristic: of ET-cut plate vibrating in combination mode *
$75^{\circ} \mathrm{C}$, so that the element is particularly advantageous where crystal ovens are used.
Disadvantages: Stability and general performance are inferior to those that can usually be obtained by using, according to the particular frequency, either an $A$ or a $C$ element.

## 1-118. CHARACTERISTICS OF FT-CUT PLATES IN COMBINATION MODE

Description of Element: FT cut, with w/ ratio approximately equal to 1.0 ; yxl or yzw : $-57^{\circ}$; combination of coupled modes with second flexural vibration appearing to dominate a face-shear harmonic.
Frequency Range: 150 to 1500 kc .
Frequency Equation: $\mathrm{f}=\frac{\mathrm{k}}{\mathrm{w}}$ (square plate); $f=\frac{2 k}{1+w}$ (nearly square plate).
Frequency Constant: $\mathrm{k}=4710 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: 0.0 at $75^{\circ} \mathrm{C}$; see figure 1-54 for total relative frequency deviation.
Methods of Mounting: Wire; preferably mounted in vacuum.
Advantages: The advantages of the FT cut are approximately the same as that of the ET, except that the FT has a lower frequency constant. The FT is related to the ET in approximately the same way that the DT is


Figure 1-54. Temperature-frequency characteristics of FT-cut plate vibrating in combination mode *
related to the CT. However, the frequency constants of the ET and FT are approximately twice that of the low-frequency shear elements, so that these cuts can be made in practical sizes for twice the frequencies obtainable from the CT and DT crystals. Like the ET, the FT cut is particularly suited for use in ovens at temperatures between $70^{\circ}$ and $80^{\circ} \mathrm{C}$.



Figure 1-55. Temperature-frequency characteristica of element $G^{*}$

Disadvantages: Stability and general performance are inferior to those that can usually be obtained by using, according to the particular frequency, either an $\mathrm{A}, \mathrm{C}$, or a D element.

## 1-119. CHARACTERISTICS OF ELEMENT G

Description of Element: GT cut, with ratio $\frac{W}{1}=$ 0.859 ; yxlt: $51^{\circ} 7.5^{\prime} / 45^{\circ}$; width-extensional mode.
Frequency Range: 100 to 550 kc .
Frequency Equation: $\mathbf{k}_{1} / \mathbf{w}$ (fundamental).
Frequency Constant: $\mathbf{k}_{1}=3870 \mathrm{kc}-\mathrm{mm}$.
Temperature Coefficient: Very nearly zero over the range from $-25^{\circ}$ to $+75^{\circ}$. Figure 1-55 shows the total relative frequency deviation from the initial frequency at $0^{\circ} \mathrm{C}$. Note that

(B)

Figure 1.56. (A) Diagram illuatrating the equivalence between a face-shear mode and the lengthe and width-extensional modes of a rectangular plate which has been cut diagonally with respect to the face-shear oloment. (B) w/I ratio vs rotation angle, $\phi$, of element $G$ providing zero temporature coefficient *
for a span of $100^{\circ} \mathrm{C}$ the frequency does not vary more than one part in a million from the center frequency. The midpoint of the flat portion of the curve can be shifted from $25^{\circ} \mathrm{C}$ to $50^{\circ} \mathrm{C}$ by increasing the initial orientation angle from $51^{\circ} 7.5^{\prime}$ to $51^{\circ} 30^{\prime}$; the zero coefficient range will thus extend from $0^{\circ} \mathrm{C}$ to $100^{\circ} \mathrm{C}$. A temperature variation of $\pm 15^{\circ} \mathrm{C}$ on either side of the midpoint will not change the frequency more than 0.1 part in a million.
Methode of Mounting: Wire, knife-edge clamp, pressure pins, cantilever clamp.
Advantages: The GT cut provides the greatest frequency stability that has yet been obtained from a quartz plate. Where other quartz elements have zero temperature coefficients at only one temperature, the $G$ element will not vary more than one part in a million over a range of $100^{\circ} \mathrm{C}$. This element was originally suggested by the fact that a face-shear mode consists of two extensional modes coupled totogether. When a face-shear element is rotated $45^{\circ}$ the vibrations lose their shear effect and appear as two extensional modes-one along the width, and the other along the length. See figure 1-56(A). Since all pure extensional modes must have a negative or zero temperature coefficient, a positive coefficient of a faceshear mode must be due to the coupling between its two extensional components. If the cut of a face-shear crystal having a positive coefficient has been rotated $45^{\circ}$, the coupling between the extensional modes can be reduced by grinding down one edge so that one of the modes will increase in frequency. As the frequencies become more widely separated, the extensional modes will approach their true
negative temperature coefficients. At some ratio of width to length a zero coefficient will be obtained. The GT cut is properly a $\pm 45^{\circ}$ rotation of any positive-coefficient face-shear crystal in the Y group. Although the most satisfactory cut is the one described above, a number of other GT cuts have been investigated where the initial angle of rotation, $\phi$, has had negative as well as positive values. Figure 1-56(B) shows the w/l ratios for both positive and negative angles that will provide a zero temperature coefficient. For negative values of $\phi$, the dominant mode is the one of lower frequency, whereas for positive angles of $\phi$, the higher-frequency mode is dominant. The $G$ element is used for the control of oscillators where the most precise accuracy is required, such as in the frequency standards of loran navigational systems, the time standards at the U.S. Bureau of Standards and at Greenwich Observatory, and in both fixed and portable frequency standards of general use. Other than in frequency and time standards, the GT cut is employed in filters that are designed for use under very exacting phase conditions.
Disadvantages: The principal disadvantage of a GT cut is its expense. To obtain optimum temperature-frequency characteristics requires pains-taking labor in cutting and grinding to the exact orientation and dimensions. Furthermore, the excellence of a particular cut will be of little advantage unless the mounting and the external circuit are also of superior design. For these reasons a G element is not particularly practical except when the utmost frequency precision is mandatory.

## FABRICATION OF CRYSTAL UNITS

1-120. The production stages during the fabrication of a crystal unit may differ somewhat from one manufacturer to the next because of variations in the instruments, techniques, and the type of mounting employed. However, the general procedure is fundamentally the same throughout the industry-first, the inspection and cutting of the raw quartz; next the lapping and etching of the diced blanks; and finally, the mounting and testing of the crystal unit in its holder.

INITIAL INSPICTION OF RAW PUARTZ
1-121. The manufacture of a crystal unit begins
with the inspection of the raw quartz for impurities, cracks, and inclusions. For this purpose, the arc lamp of the inspectoscope shown in figure 1-57 is used.
1-122. The inspectoscope tank is filled with a clear, colorless oil mixture having an index of refraction approximately the same as the average in quartz (1.52 to 1.56). Such a medium for transmitting the light to and from the raw crystal, or "stone," is necessary in order to see the interior, for otherwise reflections and refractions at the rough surface will not only create an excessive glare, but will diminish the intensity of light penetrating beyond.


Figure 1-57. Polariscope-inspecfoscope. Used for examining raw quartz

The lamp incorporates a high-powered (500- to 1000 -watt) projection system of white light, and inspection of the stone is performed by direct observation. The usable parts of the stone are marked; or if too many imperfections are present, the stone is discarded.

## INSPECTION FOR OPTIC AXIS AND OPTICAL TWINNING

1-123. If a stone has retained some of its natural faces, the optic (Z) axis may be readily located by direct observation. In the usual case, however, it is necessary to use the plane-polarized light system that is provided by the inspectoscope. The light from a mercury or incandescent lamp is plane polarized by a polaroid plate placed between the lamp and the tank. On the opposite side of the tank is a second polaroid plate with its transmission axis perpendicular to that of the first, so that if a stone is not in the tank to rotate the polarity of the light, the rays will be stopped at the second plate. Light that does filter through, however, is reflected upward by a mirror, and the pattern may be observed through the glass cover shown in figure 1-57. When a stone is piaced in the tank and oriented so that its optic axis is parallel to the rays, the polarity of the rays will be rotated and a bright
image will be reflected from the mirror. If white light is used, a pattern of concentric rainbow colors will appear; and if monochromatic light is used, a pattern of concentric rings of light and darkness will appear. The optic axis will be exactly parallel with the light rays when the stone is in the position that yields the fewest and broadest bands. If optical twinning is present, it will be revealed by a fine-toothed pattern cutting across the rings, as indicated in figure 1-58. The twinning areas are more clearly indicated when white light is used, and when viewed slightly off the optic axis. On the other hand, monochromatic light produces ring patterns of maximum clarity for the determination of the optic axis itself. Flat surfaces are ground on opposite sides of the stone, parallel to the optic axis; and, with the stone resting on one of the flat surfaces at the bottom of the inspectoscope tank, a line is drawn on the upper surface to indicate the approximate Z-axis direction.

## USE OF CONOSCOPE POR EXAGT DETERMINATION OF OPTIC AXIS

1-124. After the approximate optic ( $Z$ ) axis is determined, the stone is cemented to a glass plate, and a small-end-section of the crystal is sliced off with a diamond saw, leaving a flat surface approxi-

mately perpendicular to the optic axis. The stone is then mounted on an adjustable orienting jig, which is placed against the reference edge in a conoscope tank. The conoscope (see figure 1-59) provides a polarized light system with which the optic axis may be accurately located by observing a concentric ring system. The principle of the conoscope is similar to that of the polarizing system of the inspectoscope, except that a converging lens system and a vernier system are provided that permit the optic axis to be determined with an accuracy of one degree. The handedness of the crystal is readily determined by rotating the second polaroid plate, or analyzer, of the conoscope. The quartz is right or left according to whether the concentric rings appear to expand or contract for a given direction of analyzer rotation. When the $\mathbf{Z}$ axis is accurately determined, each end is trimmed to form plane surfaces ("windows") exactly perpendicular to the $Z$ direction.

## SECTIONING THE STONE

1-125. There are three general methods of cutting the stone to obtain crystal blanks of desired orientation: the direct-wafering, X-block, and Z-section-Y-bar methods. In direct wafering, shown in figure 1-60, wafers are sliced directly from the stone at the desired orientation, and the blanks are diced from the wafer. The X-block method, as indicated in figure 1-61, is similar to that of direct

Figure 1-58. Polarized-light view of pyramidal cap indicating optical twinning *


Figure 1-59. Conoscope. Used for locating accurately the optic axis and for defermining the handedness of quartz stones *

wafering, except that, before being sliced into oriented wafers, the stone is cut into one or more blocks with place surfaces at each end of the Z axis; and at the ends of one of the X axes; each surface is accurately cut at right angles to the axis it terminates. It is from these " X " blocks that the properly oriented wafers are cut and then diced into blanks. The third method of cutting proceeds as indicated in figure 1-62. The stone is aliced into Z sections (cross-sectional slabs with plane faces perpendicular to the $Z$ axis) ; the $Z$ sections are cut into $\mathbf{Y}$ bars (bars with the length parallel to the $\mathbf{Y}$ axis) ; and crystal blanks are sliced at the desired

Figure 1-60. Direct-wofering method of cutting crystal blanks
mother duartz sectioned
into 2 日locks

$x$ Elock cut from 2 Block

figure 1-61. X-block method of cutting wafers from unfoced stone. Wafors, on boing diced, provide crystal blanks of the proper oriontation
orientation from the $Y$ bar. Of the three methods of cutting, the X-block method is the one most commonly used, and will be the one assumed in the following paragraphs.

## DETERMINATION OF X AXIS

1-126. A reasonably accurate method for a preliminary determination of the $\mathbf{X}$ axis of an unfaced quartz is by observing the cleavage lines of a thin Z section when it fractures after being heated and dropped into cold water. The intersections of the fractures with the XY plane of the Z section are normally parallel to an $X$ axis. A more useful procedure, however, is to first etch a Z block (block or section with Z windows, before X windows have been cut) in a bath of $30 \%$ hydrofluoric acid, and determine the approximate $\mathbf{X}$ axis with a pin-hole oriascope, shown in figure 1-63. The oriascope provides a pin-point source of ordinary light which will cause a triangular image to appear on the upper XY window when the lower window of the $Z$ block is placed over the pin hole. The sides of the triangle are approximately parallel to the X axes, and matching windows and a template are provided to aid in marking the crystal.
$1-127$. With the X axis approximately located by


Figure 1-62. Z-section-Y-bar method of cutting properly oriented crystal blanks
the cleavage or oriascope methods, an exact orientation is determined by use of X-ray apparatus. The Z block is cemented to a glass plate, which in turn is placed on an adjustable orienting jig that can later be transferred to a saw. As indicated in


Figure 1-63. Pinhole oriascope with matching and marking arms tor use on 2 sections *
WADC TR 56-156


Figure 1-64. X-ray determination of $X$ axis in $Z$ block. $M$ is horizontal bisector of angle that ray must make if reflected beam is to enter ionization chamber. $\theta$, the Bragg angle of X-ray refection for copperanode $K_{a}$ radiation, is predetermined according to the particular atomic plane to be identified. For plane that is parallel to an $m$ face, and hence to an $X$ axis, $\theta=10^{\circ} 38^{\prime}$. With positions of $X$-ray source and ionization chamber fixed, rotation of $Z$ block about $Z$ axis will cause maximum curreni to flow through ionization chamber when an $X$ axis becomes perpendicular to $M$


Figure 1-65. Reflection pafferns of twinned $\mathbf{Z}$ section, showing both types of twinning. The section is predominantly right quartz, but is fairly evenly divided by the electrical twins $a$ and $b$. The small regions of optical twinning of one electrical sense are shown in C, and those of the opposite sense are shown in D. The $X$-axis polarities indicated apply only to the respective bright regions. The regions marked $f$ contain flaws *
figure 1-64, an X-ray beam is directed toward the crystal's vertical surface, which deflects part of the beam into the window of an ionization chamber, causing a current to flow that has an amplitude proportional to the intensity of the rays entering the chamber. X-rays of constant wavelength are propagated in a narrow pencil from a properly filtered source, which consists of a special highvoltage cathode-ray tube having a copper anode. The X-rays are emitted by virtue of the highenergy electrons' striking the copper target, and a thin nickel plate is inserted in the X-ray path to eliminate unwanted wavelengths. The atomic planes of the crystal lattice effectively serve as reflecting surfaces, except that interference between the reflected rays from adjacent parallel planes eliminates all angles of reflection except those that permit the path lengths of coinciding rays to differ by an integral number of wavelengths. The above condition is satisfied when the distance between the atomic planes is related to the wavelength and the angle of incidence of the $X$ rays in a manner that can be expressed by Bragg's law:

$$
\mathrm{n} \lambda=2 \mathrm{~d} \sin \theta
$$

where: $\mathrm{n}=1,2,3, \ldots$.

$$
\begin{aligned}
\lambda= & \text { wavelength of } \mathrm{X} \text { rays } \\
\mathrm{d}= & \text { distance between parallel atomic } \\
& \text { planes } \\
\theta= & \text { angle of incidence of } \mathrm{X} \text { rays with } \\
& \text { atomic plane }
\end{aligned}
$$

The ionization chamber is a gas-filled metallic cylinder having an electrode which is maintained at a voltage relative to the cylinder. $X$ rays entering the chamber will ionize the gas, permitting a current to flow through the external circuit. With $\theta$ predetermined for a particular atomic plane, the exact direction of the plane, and hence of the crystal's orientation, can thus be determined by rotating the Z block for a maximum reading on the ammeter.

## CUTTING X BLOCK

1-128. When the $X$ direction has been precisely determined, the mounting jig is locked in position and transferred to a diarnond saw, where windows are cut perpendicular to, and at each end of, the $X$ axis-thereby forming an $\mathbf{X}$ block. After the alignment of the windows is rechecked with the X-ray apparatus, the $\mathbf{X}$ block is cleaned, and then etched in $48 \%$ hydroflouric acid or a saturated solution of ammonium difluoride.

Section I

## DETERMINATION OF TWINNING

1-129. Electrical and optical twinning boundaries can be observed directly by shining a spot lamp upon the etched $Z$ windows of the $X$ block. The light should be directed at approximately a 30degree angle with the surface being examined, with the line of sight of the observer perpendicular to the surface. As the block is rotated about the axis perpendicular to the surface, there will be four particular orientations, each corresponding to a reflection of maximum brightness from the etched area of one of the four possible twins-right-hand quartz of either electrical sense, and left-hand quartz of either electrical sense. See figure 1-65. Normally a crystal is predominantly right or left, so that optical twinning usually appears only in small scattered regions. Electrical twinning, however, normally divides a crystal into large regions of opposite electrical sense. The polarities of the various twinned areas can be readily determined by noting the angles of rotation at which maximum brightness is observed. The axial polarities of an X block may also be determined by examining the $\mathbf{X}$ windows with the aid of a pin-hole oriascope having matching and marking arms designed especially for X sections. The images observed will differ according to the electrical sense of the particular area-also, according to whether hydrofluoric acid or ammonium difluoride was used in etching. By a proper interpretation of the patterns,
the axial directions of the twinned regions can be suitably marked. If there is an excessive amount of scattered twinning, the block must be discarded; otherwise, the observation permits a proper orientation for cutting slabs, so that optimum use of the quartz is possible.

## PREPARATION OF WAFERS

1-130. The mounting jig, adjusted to the correct orientation, is transferred to a saw, and the $X$ block is sliced into slabs of sufficient thickness for finishing. See figure 1-66. After being cleaned and etched, the slabs are inspected and marked for twinning, and the unusable portions are cut away by a diamond saw. Each slab is cemented to a holder and mounted in a jig for a final X-ray determination of the orientation. The adjusted slab holders are transferred to the jig of a lapping machine, and the slabs are lapped on one surface, using an abrasive of 400-grain carborundum, until the lapped faces have the desired orientation. The slabs are then cemented to a large plate with the corrected faces down, and the uncorrected faces are lapped until parallel with the bottom faces. The "wafers," as the slabs are now called, are next cemented to a glass-topped steel plate for dicing.

## PREPARATION OF CRYSTAL BLANKS

1-131. The wafers are diced to the approximate crystal blank size with a dicing saw, as shown in


Figure 1-66. Diamond saw for cutting wafers from $X$ block

Section 1


Figure 1-67. (A) Dicing saw. (B) Diced wofor. (C) Nest of lapping machine. (D) Lapping machine
figure 1-67. The dice are then transferred to the nest of a lapping machine, where they are lapped to a thickness equivalent to several kilocycles below the desired frequency. The lapping proceeds in three stages: rough, semifinishing, and finishing. However, the rough stage is accomplished prior to dicing, if the slabs are first lapped to wafers as described in paragraph 1-130. The semifinishing is done with 600 -grain carborundum or equivalent, and the finshing requires 1000 - to 1200 -grain abrasive. Each of the last two stages should completely remove the surface left by the preceding stage. (Where extreme care is required, as when finishing thin harmonic mode plates, 3000 mesh aluminum oxide mixed with water, cosmetic talc and powdered white rouge provides high-precision results, with the ultimate operating dependability greatly increased if the final lapping is followed by


Figure 1-68. Loaf of erystal dice, all blanks oriented in the same direction in preparation for edge grinding by edging machine *
a brief semi-polishing with a mixture of water, rouge, and small amounts of rust preventative and wetting agent.) In the case of high-frequency blanks, the final lapping should bring the blanks within 25 to 50 kilocycles of the desired frequency. Next, a stack of 25 to 100 dice are clamped into a loaf, with all the blanks oriented in the same direction. See figure 1-68. Two exposed edges are then ground parallel to locating surfaces by an edging machine. The loaf is then reversed and the two remaining edges are ground to square the blanks. Finally, the blanks are etched to the proper frequency. For high-frequency crystals, a frequency tolerance of $\pm 0.002$ percent will require that the finished blanks be etched to within $\pm 0.00001$ millimeter of the ideal thickness. After cleaning, the crystal blanks are ready for mounting.

## METHODS OF MOUNTING CRYSTAL BLANKS IN CRYSTAL HOLDERS

1-132. In the past, some confusion has resulted among radio engineers because of a mixed usage of the terms crystal holder and crystal unit by manufacturers in describing and naming their products. However, it is now generally agreed that the term crystal holder is to be used only in reference to the mounting and housing assembly, whereas the term crystal unit is to designate a complete assembly-that is, a crystal holder containing a mounted crystal plate.
1-133. Crystal holders have been variously classified by different specialists in the field, and in the
absence of a standard nomenclature, a certain amount of overlapping has resulted among the different classifications. The procedure to be followed here is to treat each particular method of mounting as a separate category. The holders to be discussed are described according to the following types of mounting: gravity-sandwich, pressuresandwich, gravity-air-gap, corner-clamped-air-gap, nodal-clamped-air-gap, dielectric-sandwich, plated-dielectric-sandwich, button-sandwich, knife-edgeclamp, pressure-pin, cantilever-clamp, solder-conewire, headed-wire, and edge-clamped. Only two general classifications of mounting, wire and pressure, are specified for Military Standard crystal units currently recommended for use in equipments of new design. The wire-mounted crystals are cemented directly to supporting wires. The pressure-mounted crystals are clamped in place by frictional contact with electrodes or other supporting elements. The wire mounts include the solder-cone-wire, the headed-wire, and the ce-mented-lead types, the latter being a particular kind of edge-clamped support cemented to the crystal. The pressure mounts include all other types listed above except the gravity-sandwich and the gravity-air-gap.

## Gravity Sandwich

1-134. A "crystal sandwich" is simply a crystal plate sandwiched between two flat electrodes. In the simple gravity type of holder the crystal plate is placed on one electrode, with the second electrode resting on top and connecting to the external circuit through a flexible wire. See figure 1-69. A small clearance is provided around the sides to permit the crystal to vibrate freely. The clearance must not be too large, however, else the crystal will slide around in the holder, and may become chipped, or, at least, cause the electrical constants of the crystal unit to vary. The electrodes must be perfectly plane and made of noncorrosive metal, such as stainless steel, brass, or titanium. Brass is inferior to the other two metals, and titanium is largely a future possibility. The top electrode is considerably lighter than the bottom electrode, and is usually specifically dimensioned to fit a par-


Figure 1-69. Gravity sandwich
ticular crystal size. If the top electrode is too heavy, the impedance it introduces will be excessive, preventing the crystal from vibrating near its normal mode; on the other hand, if the top electrode is too light, firm contact will not be made with the crystal, and the operation of the crystal unit will be unstable. The edges of the crystal are slightly rounded to insure that they are free of burrs. Both the crystal and the electrodes must be perfectly clean, and the entire unit must be mounted in a hermetically sealed chamber. Normally, the grid terminal of the unit connects to the flexible wire of the top electrode, and the ground or cathode terminal to the bottom electrode. 1-135. The gravity holder was at one time widely used, but has now been largely replaced by holders that can maintain the crystal in a relatively fixed position if subjected to external vibration, such as might be encountered in vehicular or aircraft equipment. Occasionally, even when mounted in vibration-free equipment, a gravity crystal unit may fail to operate because one edge of the crystal has become closely pressed against one of the sides of the chamber. However, a light tap of the holder is usually sufficient to start oscillations. Compared with the holders in which flat inflexible electrodes are pressed against the crystal, the activity of the gravity holder is generally superior, and requires less voltage to maintain a state of oscillation.

## Pressure Sandwich

1-136. In holders of the pressure-sandwich type, the crystal is held more or less firmly between two flat electrodes under the pressure of a spring. In a typical assembly, the electrodes, which normally are of identical size and shape, are in turn sandwiched between two very thin contact plates. The contact plates connect to two metal prongs that serve as electrical terminals and plugs for mounting the crystal holder in a socket. An insulating washer is placed over one of the contact plates, a coil spring is placed over the washer, and a neoprene gasket is placed between the spring and the cover to provide hermetic sealing. Except for the glass spacers, the pressure holder described above is very similar to the air-gap holder shown in figure 1-70.
1-137. Although the activity of a pressure-type crystal sandwich normally is not as great as that of the gravity type, it is much preferred because of its greater ruggedness and less critical requirements concerning the orientation and vibration of the equipment in which it is to be mounted. Another advantage of the pressure holder is its relative simplicity of design-fewer of its compo-


Figure 1-70. Methods, old and new, for mounting crystal units. (A) Construction of early model crystal unit employing the gravity air-gap type of mounting, now largely outmoded. The crystal holder shown is the type FT-243. (B) Solder-cone wire mount for v-l-f length-flexure crystal. (Courtesy HEEMCO). (C) Recently developed techniques for mounting shock-proof, 1 -mc, A elements in the miniature HC-6/U metal holder to meet the specifications for 1-mc CR-18/U crystal units: a. Reeves-Hoffman flexible nylon mount. b. Hupp loose-slotfed edge-clamped mount. c. Bliley molded nylon bumper mount. d. RCA edge-clamping spring mount. (Courtesy McCoy Electronics.)
nents require separate and exact dimensions for each particular frequency than is true of the majority of holders. If the holder is constructed so that the spring pressure may be adjusted, very slight variations in the frequency are possible; the activity, however, will decrease proportionally as the pressure is increased. Although the pressure holder is widely used and is less expensive than most of the other types of holders, it has the disadvantage of low activity and comparatively large damping of the oscillations. Thus, crystal units of this construction are not as sharply selective, nor as electrically predictable, as crystal units of more critical design.

## Gravity Air-Gep Mounting

1-138. A gravity air-gap crystal unit is essentially a gravity sandwich, but with an air space separating the crystal from the upper electrode. The air gap may be variable or fixed. In the variable type, the frequency can be adjusted slightly by raising or lowering the upper electrode, by means of a screw. The fixed air gap, however, is more commonly used. As shown in figure 1-70, the fixed gap is maintained by glass or other insulating spacers placed between the electrodes. It is important that the thickness of the air gap not be an even quarterwavelength of the acoustic vibrations which the crystal will generate in the air. Otherwise, the air waves, on refiection from the upper electrode, will return to the crystal 180 degrees out of phase with the normal vibrations, thereby introducing a high impedance and greatly reducing the activity. Maximum activity is obtained when the air gap is an odd quarter-wavelength in thickness. The exact dimension, however, is not particularly critical in the case of shear modes, and a variation of $\pm 1 / 8$ wavelength will cause little change in the amplitude of the vibrations. The quarter-wavelength formula is $\frac{\lambda}{4}=\frac{v}{4 f}$, where $v$ is the sound velocity in air, and $f$ is in cycles per second. At room temperature and pressure, $v=330,000 \mathrm{~mm} / \mathrm{sec}=$ $12,992,000 \mathrm{mils} / \mathrm{sec}$. The gap thickness should not exceed 3 mils, else the piezoelectric coupling will be too weak to maintain oscillations at reasonable voltages. Where it is necessary to have as large a piezoelectric coupling as possible, the air gap must be reduced to the minimum of $1 / 6$ wavelength.
1-139. The advantage of the air-gap mounting is that it shares the simplicity of design of the sandwich holders, but eliminates the damping effect caused by the frictional contact of the upper electrode with the crystal. The presence of the air gap also effectively inserts in the crystal circuit a
series capacitance equal to that between the upper electrode and the crystal face, thereby increasing the ratio of the stored electrical to the stored mechanical energy, and thus decreasing the electromechanical coupling. The reduction of the frictional losses (i.e., the effective electrical resistance) and the electromechanical coupling serves to give the crystal unit a higher $Q$, and thus to make it more selective and stable, and less affected by small variations on the external circuit. However, with the decrease in electromechanical coupling, the tendency of the crystal to vibrate is reduced; and also reduced is the bandwidth for use in filters. On the credit side, the gravity-air-gap mounting is particularly convenient for the preliminary testing of crystals at the time they are being ground, and it has also been widely used in fixed-plant equipment with thickness-mode crystals operating at frequencies between 200 and 1500 kc . The principal disadvantages of the gravity-air-gap holder are the loose mounting of the crystal, the reduced piezoelectric coupling, and the possibility that a momentary overdrive will cause arcing across the air gap, or a corons discharge, thereby damaging the crystal and electrode surfaces, or even puncturing the crystal completely.

## Cormer-Clamped, Alr-Gap Mounting

1-140. The principal features of the cornerclamped, air-gap mounting are indicated in figure 1-71. Note that air gaps exist at both the major faces of the crystal, except at the corners where the electrode risers, or lands, clamp the crystal in position. If the length of a thickness-shear plate, such as an AT or BT cut, is not less than twenty times the thickness, a firm pressure may be applied at the corners without greatly reducing the activity. The same precaution for avoiding an air column with dimensions approaching a multiple of a half-wavelength is necessary for the clamped as for the unclamped holder. The lands at the corners normally provide a gap of 0.5 to 2 mils.
1-141. The corner-clamped, air-gap method is widely used for mounting high-frequency thick-ness-shear crystals. Its operating characteristics


Figure 1-71. Typical corner-clamped, air-gap method of mounting erystals *

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## Fabrication of Crystal Units

are similar to those of the unclamped holder; and, in addition, it has the important advantage of clamping the crystal in a fixed position, thus permitting its use in aircraft and vehicular equipment. However, the clamping at the corners introduces an excessive amount of impedance when used for the lower-frequency, thickness-shear crystals where the $1 / t$ ratio is less than 20 ; hence, this type of mounting is generally confined. to crystals with frequencies above 1500 kc .

## Nodal-Clamped, Air-Gap Mownfing

1-142. The principal features of the nodal-clamped, air-gap mounting are indicated in figure 1-72. This method may be used for mounting low-frequency piezoelectric elements vibrating in an extensional mode and having a nodal area at the center of the crystal. Each electrode has two risers for clamping the crystal at each end of its nodal axis, and thus provides a secure mounting with a minimum of damping from direct contact between the crystal and the electrodes. A general advantage of any "zone-type" clamping, such as the nodal or corner methods where particular areas of a crystal are subjected to pressure, is that spurious frequencies requiring free vibrations in the clamped zones will be suppressed.

## Dielectric Sandwich

1-143. This type of holder is essentially a crystal sandwich with a "lettuce" of high dielectric material inserted between the crystal and the electrodes. The sandwich and air-gap holders previously described do not permit a crystal to operate


Figure 1-72. Typical nodal-clamped, alm-gap mothod of mounting erystals

figure 1-73. Pressure type of dielectric andwich for mounting erytals
near its elastic limit, for otherwise arcing would occur between the electrodes and the crystal. Low drive levels are particularly necessary at frequencies above 4000 kc , for the likelihood of corona discharge or arcing increases with the frequency. Even if the arcing is insufficient to puncture the crystal, its presence will cause either wet or dry oxides to form on the crystal and the electrodes, thereby reducing the activity and greatly shortening the crystal's useful lifetime, if not preventing its operation entirely. Many factors contribute to the possibility of a breakdown: type of holder, presence of sharp edges, smoothness and parallelism of crystal and electrode faces, type of cut, airgap dimensions, d-c and r-f voltages, frequency, and the like. However, since the arcing in all cases is the direct result of ionization of the air between the electrodes and the crystal, this danger may be removed if the more vulnerable air spaces are filled with an elastic cushion that has little tendency to ionize. It is necessary that the material have a dielectric constant much higher than that of air, and preferably higher than that of the crystal, and that it have low dielectric losses at the operating frequency; otherwise the special advantages of the particular types of mounting with which dielectric material is used would be destroyed by an increase in damping. The dielectric fller may consist of insulating sheets cut to fit a particular mounting, or it may be costed over the electrode faces. In either case, a material of high dielectric constant will permit a cryatal to be driven near its elastic limit without the danger of corona effects, and with much less restraint of the normal vibrations than occurs when the crystal is in direct contact with the electrode faces. Suitable dielectric materials are mica, thin sheets of glass or fused quartz or other ceramics, "Cellophane," nonsul-


Figure 1-74. Confer-pressure type of diolectric sandwich for mounting erystals
furous rubber sheeting, cellulose esters and ethers, varnishes, lacquers, vitreous enamels, metallic oxides, rubber coatings applied by electro-deposition, rubber containing resin and other fillings, or fused coatings of natural or synthetic resins. The sheets or coatings should be from 1 to 5 mils in thickness, but care should be taken that the thickness of the insulating material does not approach a multiple of a half-wavelength of the acoustic waves that will be generated. In any event, the addition of the dielectric material will tend to raise the impedance and frequency slightly, so that in extreme cases it may be necessary to grind the crystal to a frequency lower than that at which it is to operate.
1-144. Figures 1-73 to 1-77 indicate different methods in which the dielectric fillers may be used in mounting a crystal. Figure 1-73 illustrates a pressure type of mounting with two sheets of dielectric material-mica, for instance-inserted between each electrode and crystal. Note that the mica extends beyond the edges of both electrodes. This feature is important, for although in a welldesigned pressure sandwich no air spaces exist between the crystal and electrode faces, so that ionization and arcing do not occur at the major surfaces, corona discharges can and do occur at the edges, particularly if the sides of the chamber are close in, as is usual, causing the alternating field around the edges to be more intense. However, with the insulating sheet of high dielectric constant overlapping the electrode edges, the intensity of the electric field will be greatly diminished. That part of the dielectric directly between the crystal and the relatively inelastic electrode, acts as an elastic cushion, and thus serves much the same function as an air gap, but without increasing the possibility of corona or arcing effects.
1-145. Figure 1-74 shows a top and a side view of a center-pressure type of mounting, where two circular electrodes of small cross section are separated from the crystal faces by insulating sheets
of high dielectric constant. Again, it is important that the insulation extend well beyond the edges of the electrodes. This arrangement increases the length of the shortest possible arcing path, and, in so doing, diminishes the chance of the occurrence of a discharge.
1-146. Figure 1-75 illustrates two methods by which a corner-clamped air-gap holder can be converted into a dielectric sandwich while still retaining the principal advantages of the air-gap mounting. Figure 1-75A shows an insulating sheet cut to the dimensions of the air gap, and figure 1-75B shows a corner view of the assembled sandwich. Figure 1-75C is a side view of a similar sandwich,


Figure 1-75. Two methods (B and C) by which a corner-clamped, air-gap holder can be converted into a dielectric sandwich. Figure A shows a diolectric shoet cut to the dimensions of the air gap


Figure 1-76. Diefectric sheet cut to fill air gap of nodal-clamped mounting
but with two additional insulating sheets inserted to cushion the crystal entirely from direct contact with the electrode risers.
1-147. Figure 1-76 illustrates the cut of an insulating sheet for converting a nodal-clamped, airgap mounting into a dielectric sandwich. Two niches in the edges of the sheet are cut to fit the two risers of an electrode. When assembled, the sandwich is similar to the corner-clamped model of figure 1-75B; or, if additional rectangular sheets are inserted next to the crystal, the assembly will resemble the arrangement in $1-75 \mathrm{C}$. With either method, maximum rigidity is obtained for the nodal mounting with a minimum in damping.
1-148. Figure 1-77 is a cross-sectional view of a gravity type air-gap mounting with the electrodes coated with an insulating material of high dielectric constant. It is characteristic of air-gap holders that the smaller the thickness of the air gap, the higher the r-f voltage that can be applied before arcing occurs between the crystal and electrode faces. When the electrodes make perfect contact with the crystal, not only are the opposing surfaces theoretically at the same potential, but no ionizable substance lies between them in which an arc can form. However, the introduction of an air gap not only inherently reduces the electromechanical coupling of a crystal unit, but also effectively lowers the voltage that can be practicably applied. To remove the latter restriction without diminishing the advantages the air gap provides, the arrangement shown in figure 1-77 can be used. Note that the coating covers the edges of the elec-trodes-an important consideration since it is at the points of sharpest curvature that ionization is most likely to arise.
1-149. The use of insulating sheets and coatings of high dielectric constant permits a crystal to be operated near its elastic limit without the danger


Figure 1-77. Cross-sectional view of gravity-air-gap mounting with electrode surfaces protected by eoating of high-dielectric material
of arcing, and hence this type of crystal unit can be operated at higher drive levels than would otherwise be possible. The dielectric sandwich would be advantageous in filter circuits where high amplitude signals are to be encountered; or in small portable transmitters where several amplifier stages are not possible, and the excitation level must be as high as possible; or in any radio transmitter designed to be keyed in the oscillator stage where it is important that the oscillations built to peak amplitude in a minimum number of cycles. The insertion of the dielectric sheets also improves the stability and selectivity of the sandwich-type holders, inasmuch as they eliminate direct contact between the crystal and the relatively inelastic electrodes. The principal disadvantages of the dielectric sandwich are the reduced piezoelectric coupling caused by the separation of the electrodes from the crystal, and the damping effect of the frictional and small dielectric losses which are slightly greater than those of the air-provided the crystal is operated well below its elastic limit.

## Ploted-Dielectric Sandwich

1-150. This type of mounting is essentially the same as the previously described dielectric sandwich except that a thin layer of conducting material is interposed between the dielectric sheets and the electrodes, or between the dielectric sheets and the crystal, or both. The conductive surfaces may be strips of metal foil not more than 1 mil in thickness, or they may be plated, painted, or sprayed directly on the insulating material. Suitable conducting substances are copper, nickel, silver, gold, platinum, and their alloys. The conducting layer may be coated on one or both major surfaces of the insulating sheet, or it may completely cover the edges as well as the major surfaces, thus effectively converting the sheet into a highly compliant metal plate.
1-151. Figure 1-78A illustrates the corner-clamped-air-gap mounting using dielectric plates having conducting films on both major surfaces. The two

figure 1-78. (A) Air-gup mounting using didectric sheets hoving conducting fims on each major surface. (B) Air-gap mounting using dielectric sheots having a conducting Alm on major surioce in contact whh electrode. (C) Dieloctric sundwich in which leaves of metal foll are inserted betwoen dielectric and erystal
films that are in direct contact with the electrode risers prevent the establishment of differences of potential across the air gaps, and hence obviate the possibility of arcing or corona discharges in these spaces. Figure 1-78B illustrates the nodal-clamped, air-gap mounting using dielectric plates having a conducting film on only one surface. In the case of air-gap mountings, if only one conducting surface is to be interposed between a crystal and each electrode, it is preferable that this surface make contact with the electrode rather than the crystal, so that possible electric fields will be "shorted" around the air gap. Figure 1-78C illustrates a dielectric sandwich mounting in which leaves of metal foil are inserted between the dielectric plates and the crystal. The metal foil, being very thin and flexible, snugly fits the crystal surface and interferes but little with the crystal's vibrations. On the other hand, its presence insures a uniform potential at all points on the crystal's surface, thus protecting the surface from the effects of excessive electric stresses.
1-152. The plated-dielectric sandwich combines the advantages of the plain dielectric sandwich with improvements in the frequency stability, crystal life, frequency spectrum, and piezoelectric coupling. The improvement in frequency stability is greatest in the case of the air-gap crystal units, for the danger of arcing or corona discharge in an air gap is removed without the insertion of a dielectric sheet to fill the gap. Since the damping effect of the air is less than that of the insulating material, the use of conducting film permits a
closer approach to the high selectivity of the pure air-gap mounting for crystals which are to be driven near their elastic limit. The insertion of a metallic film next to the crystal surface serves to reduce possible electrical stresses at the surface which might indirectly aid the production of small fractures, or cause ionization and chemical effects that would lead to a weathering of the crystal's face. The insurance of a uniform potential at all points on the surface of the crystal also improves the frequency spectrum, particularly at very high frequencies, where many possible overtone modes can vibrate at frequencies close to that of the desired mode. However, the majority of the unwanted modes will have changes of phase and differences in amplitude along the major plane of the crystal, so that the resulting eddy currents that they induce in the conducting surfaces will aid in damping them out. Where the interfering modes might otherwise lead to a frequency drift or jump, the damping effect will be reflected principally as an increase in the effective electrical resistance and as a decrease in activity. Finally, closer piezoelectric coupling is achieved if the entire insulating material is given a metallic coating. The dielectric sheet thus effectively becomes an extension of the electrodes, and the close coupling of the simple sandwich mounting is approached, but without the heavy damping caused by friction between the crystal and solid metal.

## Button Mounts

1-153. The ceramic button crystal mount represents the ultimate in crystal-holder design yet to be reached via the sandwich and air-gap evolutionary chain. Originally, the button electrode was developed as an all-metal modification of the cor-ner-clamped, air-gap type. As illustrated in figure 1-79A, the all-metal electrode is provided with conventional lands at the corners, but the effective center area has been reduced by surrounding the center with a relatively deep circular groove. The effect is to reduce the shunt capacitance across the crystal while retaining a central area of sufficient size for adequate excitation; the reduction in shunt capacitance is particularly desirable if the crystal is to be operated in the v-h-f range. Also, since the principal excitation is confined to a central circular area, the likelihood of spurious modes is somewhat reduced, because the vibrating part of the crystal tends to exhibit the properties of a circular plate. The superior frequency spectrum of the circular plate is probably even more closely approached by using electrodes having solid ringshaped lands that completely surround the circular

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Figure 1.79. Buffon electrodes and methods of mounting
air gap at the center. See figure 1-79B. However, it is by combining the advantages of the button mounting with those of the plated-dielectric sandwich and circular quartz plates that optimum performance is obtained for thickness-shear modes at very high frequencies. Figure 1-79C shows the principal parts and the complete assembly of Crystal Holder HC-10/U. The shunt capacitance is held to a minimum, first, by the use of ceramic supporting plates in place of all-metal electrodes, and second, by the use of a coaxial electrode system in place of the conventional method where the crystal leads parallel each other through the base assembly. The ceramic-button electrodes are usually very thin metallic platings that cover a small circular area at the center of each ceramic plate. Although the lands may be provided by forming thickened sections at the rim of the ceramic disks, usually they are obtained by plating metal risers on the surface of the ceramic; these plated risers are not connected electrically to the center metallic section. The air-gap thickness is normally between three and five microns. A noteh in each ceramic button permits an extension of the electrode plating to the opposite side, so that contact with the crystal leads can be made with a minimum of increase in electrode capacitance. This type of crys-
tal holder is unequalled in performance when used with harmonic-mode crystals in the very-high-frequency range. It should be noted, however, that one of the original advantages of the plated-dielectric sandwich mounting is not fully realized in the case of ceramic-button electrodes - namely, the protection against arcing or corona discharges. For this reason, the ceramic-button crystal units will not withstand as high a drive level as might otherwise be possible. On the other hand, the thin air gap that can be obtained, the presence of a highdielectric material almost flush with the edges of the plated electrodes, and the firm mechanical support by which the crystal is held and cushioned against shock make this unit more durable under high drive levels than conventional air-gap holders. One of the more important advantages of the ceramic-button is the reduction of spurious modes through the use of circular quartz plates and small electrodes. The small electrode dimensions serve to concentrate the activity at the center of the crystal, where the crystal is most likely to be of uniform thickness; thus, sudden frequency jumps are prevented, for these seem to be due primarily to abrupt shifting of the center of activity between areas having slightly different average thicknesses.

## Plated Crystals

1-154. Since 1940 the designers of crystal units have increasingly favored the use of electrodes in the form of extremely thin metal films deposited directly on the crystal. Coatings of silver and gold have been successfully applied by spraying and baking, but in general the most advantageous method is by evaporating the metal in a vacuum and allowing it to condense on the exposed surfaces of the crystal. Sputtering processes are being used increasingly, particularly for base plating; where the crystal is plated in vacuum by ionic bombardment from high-voltage negative electrodes composed of the desired plating metal. Electroplating of crystals also finds application. The noble metals, gold and silver, are the elements most commonly used in plating crystals because of their resistance to oxidation, their relative ease of plating, and the strength of their soldered junctions. Other metals that are used in plating are nickel and copper. Aluminum plating is preferred if a crystal is to be held in position by pressure pins or knife-edge clamps. This is because aluminum is more durable to frictional wear, and because its lesser density permits an electrode of lighter weight. However, aluminum is the more difficult to apply, has a tendency to oxidize, and its soldered connections are not as strong as those of
silver or gold. For these reasons, silver is more widely used if the crystal is to be soldered between wire supports, and gold is used if the wire-supported unit requires maximum stability and resistance to aging. Aluminum coatings are commonly applied at 1 milligram per square inch, which is equivalent to a thickness of approximately 0.0225 mil; silver is applied at 4 milligrams per square inch, a thickness of approximately 0.0232 mil ; and gold is applied at 3 milligrams per square inch, a thickness of approximately 0.0114 mil. The actual plating procedure may be divided into two or more steps involving more than one plating process. As an example, the Signal Corps Engineering Report E-1108 by J. M. Roman recommends as many as three different plating stages during the fabrication of low-resistance, 50 -me harmonic-mode crystal units of the CR-23/U type. The base plating is accomplished by a sputtering machine in which a group of crystal blanks are mounted in a rectangular metallic mask midway between two gold electrodes, which are $51 / 2$ inches square and $61 / 4$ inches apart. A bell jar is placed over the electrode assembly and is evacuated to 0.05 to 0.02 millimeters of mercury. 2200 volts dc are applied between the crystal mask and the electrodes; first for 30 minutes at 100 ma with the mask negative in order to clean the crystals by ionic bombardment, and next, for 37 minutes at 100 ma with the electrodes negative for the actual gold plating operation. A second sputtering machine is used to clean the crystal mask of the gold deposited upon it during the plating procedure. This latter operation requires an hour at 100 ma . After being mechanically mounted on HC-6/U bases between 9 -mil, edge-clamping spring wires, the crystals are given a preliminary performance test. If a crystal is more than 0.1 per cent off its nominal frequency it is subjected to an additional plating process. This time it is plated electrolytically with nickel. The electroplating of $50-\mathrm{mc}$ crystals proceeds at a rate of 0.9 ma, which is equivalent to a harmonic frequency change of 100 kc per minute. The electrolytic solution consists of chemically pure nickel ammonium sulphate, boric acid, ammonium chloride, and water in a weight ratio, respectively, of $75 / 15 / 15 / 1000$. After mounting, testing, and electrically bonding the plated crystal electrodes to the supporting wires with silver cement, the crystals are given a final spot plating with gold in an evaporation type plater to bring them to their specified frequency. This final plating process is accomplished in vacuum while the crystal is connected in a test oscillator circuit. 1-155. The advantages of using metal-film elec-
trodes are several fold: maximum piezoelectric coupling is achieved; the possibility of arcing between the electrodes and the crystal is reduced to a minimum; variations of frequency due to a shift of the position of the crystal relative to the electrodes are eliminated; frictional losses and wear due to inelastic contact between the crystal and the electrodes are removed; the metallic film aids in protecting the crystal from erosion; the film is readily adaptable for various types of nodal mounting, and is easily divided into several electrodes for use in exciting particular harmonic modes. All in all, the plated crystal is the most practical for obtaining optimum crystal performance at low and fundamental-mode high frequencies. The metal-film electrodes, however, have certain disadvantages: the metal has a tendency to absorb moisture, thereby causing the frequency to change; when clamp supports are used, friction at the clamped points will eventually wear away the metal coating; and generally, the mounting techniques are more critical for plated crystals.

## Pressure-Pin Mounting

1-156. Pressure-pin holders (see figure 1-80) are used to support low-frequency (up to 200 kc ), electrode-plated crystals, particularly those crystals used in telephone filters. Each crystal is clamped at the center of a nodal zone by one or more pairs of opposing pins. For crystal plates one-half inch square and smaller, the diameter of the pins is approximately 10 mils, and the clamping force varies from one to two pounds; for larger plates, pins of larger dimensions exerting somewhat greater clamping forces are used. It is important that the plated electrode be of aluminum, for the greater hardness of aluminum is required to resist the wear at the points of contact with the pins. Normally, these holders are designed for mounting a complete set of filter crystals within


Figure 1-80. Pressure-pin mounting, with provisions for supporting four platod filter crystals *
a single hermetically sealed container. The holder shown in figure 1-80 mounts four crystal elements. The pressure is applied by the springs mounted at the ends, and the pins serve as electrical connections as well as mechanical supports. For greater mechanical stability, slight niches may be made in the quartz at the clamped points.
1-157. The pressure-pin holder has the advantages and disadvantages of the plated electrodes, and is used primarily for low- and medium-frequency filter crystals. It is particularly applicable for use with face-shear elements, since these have but one practicable nodal spot for clamping. The chief limitation of the pressure-pin mounting is the mechanical impedance it introduces. If the diameter of the pin is made too small, the crystal will tend to rotate about its axis of support; however, the larger the diameter is made, the more the clamping area will extend beyond the nodal point. To obtain optimum performance with this type of mechanical support, a resonant-cantilever design for pressure pins was invented by J. M. Wolfskill of the Bliley Electric Company (U.S. Patent $2,240,453,1941$ ). This step was quite significant, not only in its own right, but because it provided a forerunner of the resonant-wire type of mounting. The following discussion is based on an analysis of the cantilever clamp by R. A. Sykes (Bibliography No. 741).

## The Cantilever Clamp

$\mathbf{1 - 1 5 8}$. The cantilever clamp is a pressure-pin support designed to resonate at or near the crystal frequency. Figure 1-81 illustrates a pin mounted as a cantilever, and figure $1-82$ indicates the motion of the cantilever as a quarter-wavelength bar with a node at the fixed base and a loop at the point of contact with the crystal. It is important that even quarter-wavelengths be avoided, else the mechanical energy returning to the crystal will


Figure 1-81. Cantilever clamp for providing a resonant-pin support for the crystal *


Figure 1-82. Resonant motion of cantilever pin when its length is equal to one-quarter wave-length of clamp-free flexural vibration. Note that the effective free end of the pin is that end supporting the crystal (not shown) *
oppose its motion, thereby greatly increasing the impedance and lowering the activity. The length of a cantilever pin that will present a loop to the crystal can be determined approximately from the frequency formula of a clamp-free rod in flexural vibrations:

$$
f=\frac{\mathrm{m}^{2} \mathrm{dv}}{8 \pi \mathrm{l}^{2}}
$$

where: $m=1.875$ for the 1 st node of vibration of the rod (pin)

$$
\begin{aligned}
& \mathrm{m}=\left(\mathrm{n}-\frac{1}{2}\right) \text { for } \mathrm{n}=2,3, \ldots \\
& \mathrm{~d}=\text { diameter of pin } \\
& \mathrm{v}=\text { velocity of propagation along pin } \\
& \mathrm{l}=\text { length of pin }
\end{aligned}
$$

For phosphor-bronze pins, $v=3.6 \times 10^{5} \mathrm{~cm} / \mathrm{sec}$; therefore, to support a 100 -ke crystal, pins 1 mm in diameter should be 2.25 mm long to resonate in the mode indicated in figure 1-82. To resonate as a three-quarter-wavelength rod, $n=2$, and $1=5.67$ mm for a pin of $1-\mathrm{mm}$ diameter. The pin should be rounded at the end, as shown in figure 1-81, so that firm contact is made without the risk of having all the clamping force concentrated momentarily at a sharp point.
1-159. A properly designed cantilever clamp should extend the useful range of the pressure-pin type of mounting to somewhat higher frequencies, and this has proved to be true in actual practice; however, at the present time no data is available concerning its frequency application above 350 kc . Theoretically, a pair of pins could be used at any of their clamp-free harmonic modes, and thus pins of the same design need not be restricted to use at a single frequency. The principal promise of the cantilever clamp, however, is that it can provide a firm mechanical support while presenting a minimum of interference to the normal vibration of the crystal.

## Knife-Edged Clamp

$1-160$. The knife-edged clamp is similar to the pressure-pin method of mounting, except that the


Figure 1-83. Knife-edge clamp support for two crystal plates. Each crystal has two pairs of plated electrodes, and is so mounted that each pressure blade makes electrical contact with a different electrode. This arrangement effectively provides four crystal elements for use in a balanced filter circuit*
clamping prongs are blade-shaped, as indicated in figure 1-83. The dimensions of the clamping points are, on the average, about 35 mils in length, and 10 to 15 mils in width. These blades are used with crystal elements that have a nodal axis parallel to the plane of the major faces, and care must be taken to make certain that the blades are centered along the nodal line. Pressure is applied by phos-phor-bronze springs, with the blades serving as electrical connections as well as mechanical supports for the crystal. The holder shown in figure 1.83 mounts two crystals, but, because the plated metal films are divided to provide two electrode pairs for each crystal, the equivalent of four crystal plates is effectively available for use in a balanced flter circuit.
1-161. The advantages of the knife-edge clamp are essentially the same as those of the pressure-pin mounting, except that the greater surface of contact between the crystal and the clamp permits a firmer mechanical support. However, the knifeedge clamp is limited to use with those crystal elements that have well-defined nodal lines. Its most important application has been as a mounting for the $-18^{\circ}$ X-cut filter crystal, a crystal that can vibrate in a very pure length-extensional mode, and which has a nodal axis at the center parallel to the width dimension. The knife-edge clamp is generally useful only at frequencies below 120 kc .

## Wire Mounting

1-162. Wire-mounted crystal units are of two kinds: those that employ wire supports designed to resonate at the crystal frequency in a manner
similar to that described in paragraph 1-158 for cantilever clamps, and those that clamp the crystal at the edges by non-resonant spring wire. This latter type of wire support is the cemented-lead mount, which is classified here as an edgeclamped mount. The wire mounting provides a firm but Hexible support that serves to cushion the crystal from external vibration and shock. In addition, it can combine the advantages of the metal-film electrode with the low impedance of resonant supports, and can be used to mount any of the crystal elements, both high- and low-frequency plates, vibrating in extensional, shear, or flexural modes. Hecause of these advantages, the wire-type mounting is generally favored for crystal units used in military equipment.
1-163. There are two principal types of resonant wire mounts, the solder-cone and the headed-wire. In general, the solder-cone support is restricted to relatively small crystal plates-for example, to frequencies above 300 kc for C elements. The headed-wire type is more suited to larger plates.

## Solder-Cone Wire Support

1-164. A diagram of the solder-cone type of wire mounting is shown in figure 1-84, and a mounted crystal is shown in figure $1-85$. The crystal to be mounted is first spotted with small silver footings, 40 to 90 mils in diameter, at the nodal points where the wires are to be attached. Next, the electrodes are plated on the crystal by an evaporation or other process. Silver is generally used, although gold may be preferred where resistance to corrosion is paramount. Aluminum has not been widely used in wire-mounted units, because of the weak junction it makes with the solder. However, recent experiments indicate that an aluminum junction with a solder of indium (a rare, fusible metal, chemically similar to aluminum) is quite strong, so that eventually greater application may be found for aluminum-plated crystals. The mounting wires are normally of phosphor bronze, because of its high tensile strength and resistance to fatigue. A eutectic tin-lead solder is used that would normally be an alloy of approximately 63 percent tin and 37 percent lead by weight; however, to prevent an excessive diffusion of silver molecules from the silver spot into the solder during the soldering operation, the solder should contain 0.1 percent silver if the soldering is performed by hot-air blast, or a $59.5-34.5-6$ percent tin-lead-silver combination if performed by hot iron. A solder cone in the shape of a bell (see figure 1-84) has been found to provide the best performance characteristics, and is the type of cone that

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Figure 1-84. Solder-cone resonant-wire support. The solder ball "tunes" the wire to the crystal frequency if it is placed at a distance equal to an odd multiple of a quarter wavelength ( $I_{1}, I_{2}$, etc.) from the peak of the solder cone*
is least likely to rupture at the peak to form a "crater." For small crystals, the part of the wire enclosed by the cone may be straight, but for larger crystals sufficient anchorage requires that the end of the wire form a small hook. The wire is tuned to resonance by fixing the position of a solder ball at an odd quarter-wavelength from the peak of the cone; the solder ball serves as a "clamped" point for reflecting the wave energy back to the crystal. The "free" end of the wire is effectively at the point where it enters the solder cone. The distances $l_{1}, l_{2}$, and $l_{3}$ indicated in figure 1-84 mark "free lengths" of wire that will be resonant at the given wavelength. Note that each of the lengths defines a distance from the "free" end of the wire to a node where the solder ball should be placed.


Figure 1-85. Solder-cone wire mounting of face-shear element

1-165. Theoretically, the resonant lengths $1_{1}, 1_{2}$, $I_{3}, \ldots$ obey the same clamp-free frequency equation that is given for the cantilever clamp in paragraph 1-158. Experiment, however, has demonstrated that somewhat longer lengths are required for optimum performance. Normally, the free length of the wire is made a quarter-wave section, $l_{1}$, in the frequency range of 20 to 250 kc , and a three-quarter-wave section, $l_{2}$, in the range of 250 to 1000 kc . For phosphor-bronze wire, the empirical formulas for these distances are:

$$
\begin{aligned}
& 1_{1}=5.42 \sqrt{\frac{d}{f}} \text { inches } \\
& \mathrm{l}_{2}=12.4 \sqrt{\frac{\mathrm{~d}}{\mathrm{f}}} \text { inches }
\end{aligned}
$$

where: $\mathrm{d}=$ diameter of wire in inches (usually $0.0035,0.005,0.0063$, or 0.008 in .).

$$
\mathbf{f}=\text { frequency in } \mathrm{kc} \text {. }
$$

1-166. After soldering to the crystal, the supporting wires are bent to make them serve as springs. One, two, or three bends are carefully spaced and directed so that the displacement per unit force will be the same for all directions. The ends of the wires are then soldered without tension to metal rods, or "straights," which in turn are welded to eyelets staked in a mica or bakelite base. In mounting small crystal plates, the straights are little more than short, metal stubs, but larger crystals are mounted in "cages" having a mica roof as well as a mica base. Figure 1-86 shows the cage assembly of a $40-\mathrm{kc}$ length-width flexure crystal. The cage is formed by two mica plates at each end, and four straights. Besides providing for the proper mounting of the straights, the mica plates also serve as "bumpers" for the crystal. The inner and outer plates limit the horizontal and vertical
displacements respectively, thereby protecting the unit from wire or crystal damage in the event of severe shock or vibration. The spacing between bumper and crystal is normally between 25 and 30 mils. Where the operating frequency is below 3 kc , the wavelength is usually sufficiently long for the entire wire to be cut to a resonant length, so that the soldered junction at the straight can serve as the nodal terminal. However, the optimum free length of wire becomes increasingly critical as the frequency is raised. Solder balls are used to establish resonance, but at low frequencies small metal disks are threaded on the wire to provide greater mass while permitting a precise adjustment to the correct position; after adjustment, the disks are loaded at the back with the correct amount of solder. Better control is obtained at the higher frequencies without the disk. The solder weights range from approximately 80 milligrams for 8 -mil wire, for large crystals, to 6 milligrams for $3.5-\mathrm{mil}$ wire, for small crystals.
1-167. The principal disadvantages of the soldercone wire support arise from the effects of the solder cone upon the electrical characteristics of the crystal. To provide a junction of given mechanical strength, a certain quantity of solder is required. The solder, however, considerably increases the effective resistance of the crystal circuit as the temperature becomes high; if a high


Figure 1-86. Cage assambly for soldercone wire mounting of low-frequency length-width fexure erystal *
crystal $Q$ at high operating temperatures is required, the solder cone must be small, and, consequently, the crystal unit cannot be as rugged mechanically as would otherwise be possible. Conversely, if the crystal unit is to withstand severe mechanical vibrations and high operating temperatures, the solder cone must be of maximum size, so that the $Q$ and frequency stability will necessarily be at a minimum. Furthermore, as the volume of solder is increased appreciably, the tem-perature-frequency characteristics of the crystal may be considerably changed. Normally, the tendency will be for the zero temperature coefficient to shift to a lower temperature; in extreme cases, the zero point may be lost altogether. The tempera-ture-frequency effects of hooked wire are generally more pronounced than those of straight wire, when equal volumes of solder are used. Another consideration is the difficulty experienced in making two cones of the same dimensions.

## Headed-Wire Support

1-168. The headed-wire support (see figure 1-87) was developed to obviate the disadvantages of the solder cone, while preserving all the advantages of the wire type of mounting. The head of the wire, which resembles that of a common pin, has a diameter of approximately 22 mils for 6 -mil wire. It is pretinned, and a small globule of solder is left at the end for sweating to the crystal; the volume of solder varies from 1000 to 7000 cubic mils, according to the size of the crystal. Phos-phor-bronze wire is used, and all other mounting details are substantially the same as those for the solder-cone type of support.
1-169. The headed-wire is superior to the soldercone mounting, because it provides a greater and more uniformly distributed mechanical support with a smaller quantity of solder; in the case of low-frequency crystals, the $Q$ is improved by as much as twenty-five percent. Furthermore, the
distance $d$ (figure 1-87) is a constant for all crystal units of the same design, so that the resonant free length of the wire can be predetermined accurately, thus permitting smaller tolerance in the rated characteristics. An additional advantage is that the headed wire diminishes the mechanical coupling between the vibrating systems represented by the crystal and the wires. Standing waves are caused, not only by reflections between solder ball and crystal, but also to a certain extent by reffections from one solder ball, through the crystal, to the solder ball on the opposite side. By reducing the coupling between crystal and wires, the impedance effects due to the interfering through-waves are reduced, and a purer frequency spectrum is possible. Headed wire may be used to replace any other type of low- and medium-frequency crystal mounting, and a well-designed headed-wire crystal unit will generally surpass the other types in all-round performance. However, at the higher frequencies a clamped air-gap holder is still to be preferred for greater activity and frequency stability, and at low frequencies, ultimately the cantilever clamp may prove superior for general use.

## Edge-Clamped Mounts

1-170. Two variations of the edge-clamped type of mounting are illustrated in figure 1-88. The mount


Figure 1-88. Edge-clamped systems of mounting. (A) Mounting for low-frequency cryatals. (B) Cementedlead mounting for high-irequency crystals
shown in (A) has been used with low-frequency crystals vibrating in extensional or flexure modes; the mount in (B), known as the cemented-lead mount, is widely used as an alternate to air-gap holders in mounting high frequency, thicknessshear elements. Although edge-clamped mounts have been successfully used in the production of high-activity crystal units for both high- and lowfrequency applications, this type of mounting when used with low-frequency crystals, is probably somewhat inferior to well-constructed headed-wire or resonant-pin supports. However, a special feature of the edge-clamped mounting system is the method of dimensioning the electrodes (a method also adaptable for use with resonant pins), by which optimum performance characteristics can be obtained with high-frequency crystals. Plated electrodes (or metal foil cemented to the crystal) are used, but, as shown in figure 1-88(B), the crystal faces are only partially plated, and the plating on opposite faces is extended to opposite edges only, so that the effective electrode area is concentrated within a small circular region at the center of the crystal. By this means the capacitance is kept small, and the principal activity is confined to the central region, where the crystal is most likely to be of uniform thickness. Both of these factors are advantageous in improving the frequency stability. Also by reducing the activity in the vicinity of the edges, much of the damping due to the impedances of the supporting structure is obviated. Mechanical support and electrical connection is supplied by tinned, high-quality spring piano wire, which is clamped and cemented to the crystal at the edge where electrical contact can be made with the lead-outs from the electrodes. The cementing is used principally for the purpose of insuring good electrical connection, and not for supplying mechanical support, which should be provided by spring-wire clamps. The base ends of the spring wire are coiled around and soldered or welded to the base stubs. Although the supporting wires are not designed to be resonant elements of the crystal unit, they do provide the protection against shock and external vibration afforded by the other types of wire mounting. As compared with the performance of fundamental-mode, thickness-shear crystals, such as elements $A$ and $B$, that are mounted in corner-clamped air-gap holders, the performance of the same elements, when wiremounted, will generally be superior. In addition, the wire mounting permits the use of smaller crystal holders. The elimination of the air gap reduces the likelihood of arcing, but this does not mean that the wire-mounted units can be operated
at higher voltages than the conventional air-gap crystal units. This is because the wire-mounted crystal is more isolated thermally and tends to become hotter. The advantages of the cemented-lead over the ceramic-button mounting system are less pronounced than the advantages over the other air-gap systems. For operation at frequencies from 1 to 10 mc , the wire-supported crystal usually has the better operating characteristics. As the frequency increases, however, the metal plating of the wire-mounted element becomes an increasingly greater factor in damping the oscillations; and in the upper very-high-frequency range, above 100 me, non-plated crystals that are pressure-mounted between ceramic buttons are definitely to be preferred. Even in the fundamental frequency range, the ceramic-button mounts, which provide the better mechanical protection, may be used with good effect, and optimum performance characteristics for given operating conditions might better be achieved by combining the merits of wiremounted edge clamps with those of plated dielectric buttons.

## HOUSING OF CRYSTAL UNITS

1-171. The principal function of the housing is to provide a hermetically sealed, moisture-resistant container. Plastic housings of sandwich, air-gap, and clamp-type holders are normally sealed with neoprene gaskets. Natural rubber is not recommended, as the sulphur used in processing the rubber will ultimately contaminate other parts of the holder. Wire-mounted units are readily adaptable for housing in metal or glass tubes, employing standard radio parts; however, small, two-pin holders are generally preferred. Before sealing, a crystal unit is exposed to high temperature in an evacuated oven, in order to drive off adsorbed gasses. The sealing itself is usually performed in dry air, although certain crystals, particularly the flexure-elements, are sealed in vacuum. Optimum performance is obtained when a crystal is mounted in an evacuated container, since the damping effect of the air is eliminated.
1-172. If metal, rather than glass, housing is employed, it is difficult and expensive to seal a crystal unit so perfectly that not even minute leaks will develop due to stresses on the pins and the glasssealing of the eyelets. For this reason most crystal units are sealed in dry air, so that if very small leaks are present, the crystal characteristics will not be appreciably affected for a long period of time. Leakage is minimized if the base is rigidly protected against deformation, and if the glass
sealing fills the entire eyelet cavity uniformly. However, if a crystal is to be mounted in vacuum, a glass housing is to be preferred.

## AGING OF CRYSTAL UNITS

1-173. "Aging" is a general term applying to any cumulative process which contributes to the deterioration of a crystal unit and which results in a gradual change in its operating characteristics. There are, of course, many interrelated factors involved in aging-minute leakage through the container, adsorption of moisture, corrosion of the electrodes, ionization of the air within the container, wire fatigue, frictional wear, spurious electrolytic processes, small irreversible alterations in the crystal lattice, outgassing of the materials composing the unit, over-drive, presence of foreign matter, various thermal effects, pin strain due to socket stresses, and erosion of the surface of the crystal. However, if a crystal unit is well designed and carefully constructed, the rated operating characteristics may well outlast the equipment in which the crystal is used.
1-174. Usually the first effects of aging can be traced to changes at the surface of the crystal. These changes may be due directly or indirectly to almost any combination of the factors mentioned in paragraph 1-173, and their occurrence can be avoided or greatly diminished only if proper precautions and techniques are employed during manufacture, and if low driving voltages are employed during operation. To produce a crystal unit of long life, the final stages of production require particular precautions. These concern the finishing processes of lapping, etching, cleaning, mounting, heat cycling, and protecting against moisture.

## Lapping to Reduce Aging

1-175. Whether a crystal is being ground with abrasives which are cemented or imbedded in a grinding disk, or lapped with loose abrasives under a lapping disk, the cutting proceeds by virtue of the small fractures and chips which result when the hard, sharp edges of the abrasive particles are rubbed against the surface of the crystal. Commercial crystals are usually produced by lapping with loose abrasives, instead of grinding by "grindstones," except in the initial cutting stages and the final edging process, where diamond saws are commonly used. Each succeeding lapping stage employs a finer grade of abrasive, and must completely remove the surface left by the preceding stage. The final lapping requires very fine abrasive particles, such as 1000 - to 1200 -grain carborundum, and should preferably be performed in a

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mixture of abrasive, castile soap, and water. To reduce aging, soap and water are preferred as the coolant in the finishing stage, rather than kerosene or other oils, although kerosene permits a faster cutting rate for the same abrasive and lapping speed. Apparently, the residue of fractures remaining after a soap-water-abrasive lapping does not penetrate as deeply as that remaining after a kerosene-abrasive lapping. Regardless of how fine the abrasive, small fractures and cracks will be left in the surface of the crystal after the final lapping, and in time these cracks will spread, absorb moisture, and ultimately result in a weathering of the surface. Additional care must be taken to ensure


Figure 1-89. Minimum change in frequency that AT and BT plates must undergo due to etching, if the etching is to be sufficient to remove all surface cracks and fissions ramaining from the final lapping stage. Note that, as the crystal becomes thinner, a given change in the thickness dimension means a greater change in the frequency. The frequency change for a BT cut is less than that for an AT cut of the same initial frequency, since the larger frequency constant of the BT cut permits a thicker plate
that the crystal is not finished with slight concavities in the surfaces, or with one end lapped down more than the other, making the crystal wedge-shaped. Although optimum performance is to be obtained with perfectly planar surfaces, greater insurance against unwanted non-parallelisms is gained if the lapping is controlled to give the plates a symmetrical convex contour of approximately 5 microns for lower-frequency crystals, and approximately $10^{7} / \mathrm{f}$ (cycles) microns for crystals above 3 mc .

## Etching to Reduce Aging

1-176. After the final lapping stage, the crystal is normally given an etching bath to remove all foreign particles. An eight-minute bath in forty-seven percent hydrofluoric acid is sufficient for the average crystal, and will permit a firm contact between the crystal and its electrode coating. An etching time of at least thirty minutes is necessary, however, if a minimum aging and a maximum $Q$, stability, and drive level are desired. The longer etching period is required to ensure that the deeper fissions in the surface caused by the final lapping are thoroughly removed. However, the deep etch is difficult to control, and particular care must be exercised if the desired dimensions of the crystal are to be achieved. It is customary to divide the deep-etching process into two, or more, steps: (1) to etch the crystal to within 1 kc of the desired frequency; and (2) in the succeeding steps, to bring the crystal within its tolerance limits. Figure 1-89 indicates the degree of etching required to prevent aging in AT and BT cuts.

## Cleanliness to Reduce Aging

1-177. The protection of a crystal from foreign matter and moisture is of paramount importance if the crystal is to operate with stability and long life. Only minute traces of dirt, dust, or fingerprints on a crystal will cause the performance to be erratic. Cleanliness is necessary throughout the final production period, but particular emphasis is required during the stages immediately prior to sealing. Before and after etching, each crystal blank should be scrubbed thoroughly in soap, or trisodium phosphate, and water with a soft brush; rinsed in 0.5 percent ammonium hydroxide solution, and again washed thoroughly in running water; dried in an oven heated to 100 degrees centigrade, or in a warm, clean, air stream; washed again in distilled carbon tetrachloride or other solvent; rinsed in hot distilled water; and finally, carefully dried in an oven. The electrodes and holder must be similarly cleaned, and neoprene
tweezers should be used in handling the parts during the final assembly. If the crystal is to be metalplated, the complete mounting must be cleaned again before sealing. A hot spray of distilled trichloroethylene for one-half minute is sufficient. The plated crystal will normally require a small amount of edge-grinding with fine emery paper to bring the mounted unit to the proper frequency. This step unfortunately weakens the aging resistance of the treated surfaces at a stage when further etching is no longer feasible for commercial crystals. However, before testing and sealing, a retouched crystal unit should be thoroughly washed and scrubbed, with every precaution taken to ensure that no foreign matter remains on the crystal or mounting. Where the facilities are available, cleaning can be performed by exciting the bath with supersonic acoustic waves, which can clean the crystal by shaking all loose fragments off its surface. In fact, a supersonic bath can be quite as effective as an etching bath in reducing aging.

## Mounting to Reduce Aging

1-178. As a general rule, any deviation in the mounting which causes an increase in the frictional losses will shorten the useful life of a crystal unit. Thus, in the nodal types of mounting, small deviations from the nodal point in the position at which a crystal is held will shorten the life of the crystal. Wire-mounted crystals require additional precautions during fabrication to avoid local changes or stresses at the surface of the crystal. Particular care must be taken to avoid electrical "twinning," which will occur if the temperature is raised above the inversion point, $573^{\circ} \mathrm{C}$, and then lowered again; or twinning may be induced at a much lower temperature if a sharp temperature gradient is present in the crystal. These precautions are necessary during the baking of the silver spots, the division of the electrode coating by electric stylus, and the soldering operation. In baking the silver spots, the temperature should be kept forty to fifty degrees centrigrade below the inversion point, and care must be taken to make certain that the crystals are heated uniformly. Some twinning is inevitable when using an electric stylus to divide an electrode coating; however, if straight-line division is required, the twinning may be avoided by using an abrasive tool or sand blasting in place of the stylus. To avoid thermal stresses during the soldering operation, a heated support should be provided for heating the crystal uniformly to a temperature of approximately $100^{\circ} \mathrm{C}$. Twinning, regardless of its cause, primarily affects the steady-state electrical characteristics of
a crystal element, and only indirectly contributes to gradual changes in the performance of the crystal. At least, no statistical data has been collected to show a correlation between twinning and aging; nevertheless, a series of small twinned spots at the surface is likely to make the area more susceptible to erosion. Readjustments of the crystal lattice at the twinning boundaries after long periods of electrical, mechanical, and thermal stresses might be expected; but if these are due to occur, they can probably be made to take place by a process of artificial aging before the crystal is placed into operation. Twinning, however, raises the inductance and effective resistance of an element, and hence, decreases its activity for a given operating voltage. Since the ultimate requirement of a higher operating voltage can lead to a shortening of the life of the crystal unit, an undue amount of twinning indirectly becomes a factor in the aging. Twinning will also raise or lower the frequency, according to the particular type of element. If the twinning is introduced during the final stages, this may require a substantial amount of edge-grinding during the final frequency-adjustment stage, and more of the etched surface may need to be removed than otherwise. Thus, although "heat" twinning is considered primarily in connection with its immediate effect upon the characteristics of the crystal, it should also be avoided as an indirect factor in aging. A more direct factor in shortening the life of a wire-mounted crystal unit is a nonuniformity in the soldexed junction, which is more likely to occur in a solder-cone than in a headed-wire support. When the stresses are unevenly distributed, the soldered junction itself will tend to age; and even if mechanical breakage does not occur, the changes in the electrical characteristics will lead to poor performance and instability. Special care must be taken to make certain that the silver spots are of uniform density. The containers of liquid silver should be agitated for several hours immediately prior to application. Also, the critical nature of the soldering operation requires the aid of a machine and accessories of special design.

## Heat Cycling to Reduce Aging

1-179. A newly mounted crystal will normally appear to age more rapidly than one that has been in operation for a long period of time. This effect is not due to an actual deterioration of the crystal unit, but merely to an initial adjustment of the crystal, particularly at its surface, to its operating environment and changes in temperature. The stabilization period can be reduced to one of very

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## Electrical Parameters of Crystal Units

short duration by subjecting the crystal unit to a series of slow heating and cooling cycles varying between $24^{\circ} \mathrm{C}$ and $116^{\circ} \mathrm{C}$. Metal-plated elements are frequently heat-cycled during the final fre-quency-adjustment period, and again after sealing. In a series of tests at the Hunt Corporation, it was found that negative aging (frequency decreases with time) is generally due to insufficient cleaning of the crystal unit. When this was remedied, it was found that the crystal units would then age positively. The cause of the positive aging was traced to the outgassing of the metal plating of the crystal, and its elimination has been achieved by pre-aging the plated crystal for 3 minutes in a $300^{\circ} \mathrm{C}$ oven. After a sufficient period of artificial aging, a properly fabricated and operated crystal unit will maintain its final tempera-ture-frequency characteristics indefinitely.

## Low Relative Humidity to Reduce Aging

1-180. A low relative humidity is of paramount importance if excessive aging is to be prevented. Even if a crystal is perfectly mounted and clean, an ambient relative humidity higher than 40 percent will sharply increase the insulation resistance, and will greatly accelerate the weathering of the
surface of the crystal and the corrosion of the electrodes. For optimum performance and long life, every precaution must be taken to ensure that the interior of the sealed crystal unit is as free as possible from moisture. Prior to sealing, all components of the crystal unit should be heated in vacuum to drive off absorbed water vapor and other gases; and if the sealing is performed in air, the atmosphere should not have a relative humidity higher than 5 percent.

## Low Drive Level to Reduce Aging

1-181. As a general rule, the lower the drive level, the longer will be the useful life of a crystal unit. This is true because the cumulative effects of almost all of the previously discussed aging factors are considerably more pronounced when the crystal is operated at high drive levels. Also, the higher operating voltages greatly increase the tendency toward corona discharge and other ionization effects, and the vibrations of greater amplitude are more likely to result in crystal or wire fatigue. To ensure maximum lifetime, a piezoelectric resonator should be driven at the lowest practicable level consistent with the circuit requirements.

## ELECTRICAL PARAMETERS OF CRYSTAL UNITS

## EquIVALENT CIRCUIT OF CRYSTAL UNIT

1-182. A crystal unit may be represented by the equivalent electrical circuit shown in figure 1-90. $\mathrm{R}_{1}$ represents the terminal-to-terminal r-f insulation resistance of the crystal unit. $\mathrm{C}_{\mathrm{L}}, \mathrm{L}_{\mathrm{L}}$, and $\mathrm{R}_{\mathrm{L}}$ represent, respectively, the distributed capacitance, inductance, and resistance of the electrical leads and terminals of the mounted crystal. $\mathrm{C}_{\mathrm{L}}$, in addition, includes the capacitance across any elec-
trode parts that extend beyond the quartz. $\mathrm{C}_{\mathrm{H}}$ and $\mathrm{C}_{\mathrm{H} 2}$ represent the distributed capacitance of the crystal circuit to the holder $H . C_{A}$ represents the capacitance between the electrodes and the crystal faces when they are separated by an air gap or other dielectric. If a dielectric exists on both sides of the crystal, $\mathrm{C}_{\mathrm{A}}$ would equal the total capacitance of the two capacitances in series. Thus, if the airgap capacitances on the opposite sides of the crystal were equal, as would normally be the case, $\mathrm{C}_{A}$


Figure 1-90. Equivalent circuit of erystal unit
would be equal to one-half the value of either one. $C_{4}$ is the electrostatic capacitance across the quartz plate, where the quartz serves as the dielectric. The series LCR branches represent the piezoelectric properties of the crystal as they appear to the external circuit when the crystal is undergoing mechanical vibrations. For this reason, these values are called the "motional-arm" (also, "seriesarm") parameters, in contradistinction to the parameters such as $C_{e}$ that are not of piezoelectric origin.
1-183. The motional-arm values of $L$ are closely associated with the mass of the crystal, those of C are closely associated with the elasticity of the crystal, and the motional-arm values of $R$ indicate the tendency of the crystal to dissipate heat during vibration. Each of the motional-arm branches is associated with a different mode or harmonic of vibration, and the normal frequency of each of the modes coincides with the series-resonant frequency of the respective LCR branch. It will be assumed that the branch indicated by $L_{1}, C_{1}$, and $R_{1}$ represents the equivalent circuit of the desired mode, and that all of the higher subscript branches $L_{k}$, $\mathrm{C}_{\mathrm{k}}, \mathrm{R}_{\mathrm{k}}$, represent unwanted modes.
1-184. Since a crystal unit is normally intended for use only within a very narrow frequency range centered at a specified nominal frequency, the equivalent circuit may be greatly simplified to that shown in figure 1-91. If the crystal is mounted so that the electrodes are in direct contact with the crystal faces, $C_{A}$ will not be effective, and the values of $L, C$, and $R$ in figure 1-91 will normally be approximately the same as those of $L_{1}, C_{1}$, and $R_{1}$ in figure 1-90, and $C_{0}$ will approximately equal $\mathrm{C}_{\mathrm{e}}+\mathrm{C}_{\mathrm{L}}+\frac{\mathrm{C}_{\mathrm{H}_{1}} \mathrm{C}_{\mathrm{H} 2}}{\mathrm{C}_{\mathrm{H}_{1}}+\mathrm{C}_{\mathrm{Hz}}}$. For these assumptions to


Figure 1-91. Simplified equivalont circuit of erystal unit

Section I
Electrical Parameters of Crystal Units
tal, is to reduce the effective $Q$ of the crystal unit. For all practical purposes this effect is negligible when the crystal is being operated at, or very near, the resonant frequency of the series arm. Under these conditions the electrical impedance of the crystal is so small by comparison that $R_{I}$ can be ignored. On the other hand, as the frequency rises above the resonant point, the impedance increases sharply, and the greater the impedance becomes, the greater is the effect of a given $\mathrm{R}_{\mathrm{r}}$. Insofar as the equivalent circuit of figure 1.91 is concerned, the effect will be to increase the value of $R$. The extent of this increase will depend upon how large the effective reactance of the crystal becomes, relative to $\mathrm{R}_{\mathrm{I}}$. For the sake of simplification, most of the discussion given later concerning the equivalent circuit assumes that the increase in $R$ due to $R_{I}$ is negligible, or at least, is constant, regardless of the frequency, an assumption that can produce reasonably accurate results in the case of well-fabricated crystal units. The leakage resistance of military crystal units has a specified minimum d-c value of 500 megohms. As long as this minimum d-c value is maintained, $R_{1}$ at low frequencies will be comparable to this value. However, if an accumulation of moisture, dirt, or the like seriously reduces the d-c insulation resistance below the allowed minimum, the off-resonance characteristics will undergo a noticeable change. For instance, low-frequency filter crystals may have impedances at antiresonance in the neighborhood of 50 to 100 megohms. If $\mathrm{R}_{\mathrm{I}}$ decreases below 500 megohms, the equivalent $R$ of the motional arm will increase markedly. In the case of high-frequency crystal units, the effeceive dielectric losses may become relatively large, particularly when plastic holders are used, so that, at off-resonant frequencies, $\mathrm{R}_{\mathrm{I}}$ can become a significant parameter of the over-all effective resistance. However, for high-frequency crystal units employing modern methods of mounting and construction, $\mathrm{R}_{1}$ can generally be ignored. In the very-high-frequency range, crystal units are almost always operated at series resonance, so that, even if $R_{1}$ were on the order of 100,000 ohms, as might easily be the case, the effect would still be relatively minor. However, where the shunt resistance cannot be ignored, a more concrete analysis of its effect is to let $R_{1}$, in figure 1-90, represent only the d-c leakage resistance, and to account for the r-f dielectric losses by inserting other equivalent resistances in series with the various shunt capacitances. In the simplified equivalent circuit in figure $1-91$, the $d-c$ leakage resistance could still be ignored, but nonnegligible r-f shunt losses could be interpreted as
being due to a single resistance in series with the shunt capacitance, $\mathrm{C}_{0}$. The Q of the equivalent shunt arm will effectively equal the $Q$ of the crystal unit when the unit is operated at frequencies well removed from resonance. The crystal units that are mounted in metal or glass holders of the type described in Section 11, and are recommended for use in equipments of new design, can be expected to have shunt-arm Q's greater than 1000 at all frequencies within their specified range. This assurance, however, cannot be given for the crystal units mounted in plastic holders, particularly the old-style phenolic holder, or for those employing all-metal sandwich or air-gap electrodes. However, the lower Q's of the older types of crystal holders are not entirely due to greater dielectric losses and larger values of shunt capacitance. An equally important factor is the effective inductance of the circuit effectively in series with the shunt capacitances. For example, a corner-clamped air-gap mounting, such as that provided in a DC-31 crystal unit, has an effective shunt-arm $Q$ of approximately 80 or 180 at 30 mc , depending upon whether the clamping pressure is applied by a coiled or a flat spring, respectively. Apparently, the reactance and resistance of a coil spring can be quite detrimental to the quality of a crystal holder at very high frequencies, since it can cause not only an effective increase in the shunt capacitance, but also an increase in the effective dielectric losses. These losses would become prohibitive if the inductance of the spring and its stray capacitance should approach the properties of a series-resonant arm shunting the crystal. However, except in such abnormal cases, and in cases where the insulation is weakened by extremes in humidity and temperature, the shunt resistance will have a negligible effect upon the performance of a crystal circuit.

## EFFECT OF DISTRIBUTED INDUCTANCE

1-187. The effective self-inductance of the crystal leads, $\mathrm{L}_{\mathrm{k}}$, is normally not sufficient to seriously affect the crystal parameters, except in the case of very high operating frequencies where it is necessary to operate the crystal at series resonance. At resonance, the reactance of the crystal unit will be zero, so that the crystal, in combination with its shunt capacitance, must have a net equivalent series $\mathrm{X}_{\mathrm{C}}$ equal in magnitude to the $\mathrm{X}_{\mathrm{LL}}$ of the distributed inductance. This means that the resonant frequency will be slightly lower than would be the case if there were no distributed inductance. The net effect on the equivalent circuit of figure 1-91 is that the LC product is increased very slightly (lower resonant frequency), and that $\mathrm{C}_{\text {。 }}$
is increased to a greater extent. If the distributed inductance is completely negligible, the resonant frequency of the crystal will be slightly higher than the normal resonant frequency of the series arm, because of the reactive component of current through $C_{0}$. However, the distributed $X_{L}$ of the lower-frequency crystal units may be sufficient to approximately cancel the reactance due to the true $\mathrm{C}_{0}$. Under these conditions, the resonant frequency of the crystal unit as a whole would coincide with the natural vibration frequency of the crystal-an ideal operating state. In the case of the higherfrequency crystal units, the distributed inductive reactance may be sufficient to lower the frequency below the natural resonance point by several cycles. If the crystal unit were being operated at series resonance in a capacitance-bridge circuit, for example, such an effect would lead to frequency jumps with slight changes in the tuning adjustments. Under such conditions it would be desirable to add a capacitance in series with the crystal, with a reactance just sufficient to cancel the unwanted $\mathrm{X}_{\mathrm{LL}}$. The distributed inductance, $\mathrm{L}_{\mathrm{L}}$, of the lower-frequency crystals, and of practically any crystal unit which is to be operated above series resonance, has only a minor effect. The maximum effect will always be at very high frequencies near series resonance. In analyzing the behavior of a crystal unit where the distributed $X_{\mathrm{La}}$ cannot be neglected, the simplest approach is to consider $\mathbf{X}_{\mathrm{L}}$ as a separate fixed reactance in series with the crystal unit. From this point of view, as long as $\mathrm{X}_{\mathrm{LL}}$ is very small, as compared with $\mathrm{X}_{\text {cos }}$ it can be seen that $L_{L}$ will not seriously affect the rate at which the net crystal reactance will change with frequency, and, therefore, will not influence the stabilizing effect of the crystal on the frequency. Crystal oscillators can operate successfully up to frequencies as high as 200 mc . However, crystalcontrol of the frequency can be stable only when the impedance at series resonance is much smaller than the reactance of the effective shunt capacitance $\mathrm{C}_{0}$. The larger the value of $\mathrm{X}_{\mathrm{L}}$, the smaller this ratio will be. Thus, the higher the frequency, the greater the importance of keeping the crystal leads as short as possible, not only to reduce $L_{L}$, but also to reduce the distributed capacitance and the r-f resistance of the wires. The small coaxialelectrode type of mounting, such as the HC-10/U, is the most satisfactory for achieving a minimum effective $C_{0}$, and hence, a maximum frequency stability in the very-high-frequency range. It should be remembered, however, that since the distributed $X_{L L}$ will increase with the frequency, the effective $C_{0}$ will also increase with the frequency,
so that a measurement of $\mathrm{C}_{0}$ at a frequency far lower than that of resonance will not alone give a reliable indication of the effective parameter near the operating frequency.

## EFFECT OF DISTRIBUTED CAPACITANCE

1-188. The effect of the distributed capacitance on the parameters of the simplified equivalent circuit is merely to increase the value of $\mathrm{C}_{0}$. However, it should be noted that the amount of the increase will depend somewhat upon how the crystal unit is connected in the external circuit. For example, assume that the holder and terminal 1 in figure $1-90$ are grounded. $\mathrm{C}_{\mathrm{H}_{1}}$, which would otherwise be in series with $\mathrm{C}_{\mathrm{H} 2}$, is now effectively short-circuited, so that the total shunt capacitance $\mathrm{C}_{6}$ is increased. If $\mathrm{C}_{\mathrm{H} 1}$ were assumed to be equal to $\mathrm{C}_{\mathrm{H} 2}$, the amount of the increase due to grounding terminal 1 and the holder would equal $\mathrm{C}_{\mathrm{H}_{1}} / 2$. On the other hand, grounding the holder can result in an effective decrease in $\mathrm{C}_{0}$. Assume, for instance, that a crystal unit is connected in a circuit equivalent to that shown in figure 1-93. With the metal holder ungrounded, $\mathrm{C}_{\mathrm{H}_{1}}$ and $\mathrm{C}_{\mathrm{H}_{2}}$ are effectively connected in series, so that, if $\mathrm{C}_{\mathrm{H}_{1}}=\mathrm{C}_{\mathrm{H} 2}$, the total capacitance of the series combination is $\mathrm{C}_{\mathrm{H}_{1}} / 2$. If switch $S$ is closed, thereby grounding the holder, the effective total $\mathrm{C}_{0}$ becomes larger or smaller, depending upon the point of view of the observer. Since $\mathrm{C}_{\mathrm{H}_{1}}$ is no longer in series with $\mathrm{C}_{\mathrm{H} 2}$, but, instead, is shunted across the entire circuit, whereas $\mathrm{C}_{\mathrm{H}}$ is shunted across the load $Z$, the total capacitance facing the generator is increased (assuming that $Z$ is the reactance of a capacitor). When $S$ is closed, the current through $\mathrm{M}_{\mathrm{i}}$ increases; however, the current through $\mathbf{M}_{2}$ decreases. An observer at $M_{1}$ would say that grounding the holder increased $C_{0}$, whereas an observer at $M_{z}$ would say that $C_{0}$ has decreased. At frequencies well removed from the nearest resonant frequency of the motional arms, the branch impedances are so


Figure 1-93. Circuit diagram indicating the effect that grounding a metal holder may have on shunt capacitance
high that the crystal unit behaves essentially as a capacitor of value $\mathrm{C}_{0}$. It can be seen that if a measurement were being made of the change in $C_{0}$ due to the grounding of the holder, it would be important to know exactly how the measurements were made. For example, low-frequency crystal units mounted in the $\mathrm{HC}-13 / \mathrm{U}$ have been reported as having $0.8 \mu \mu \mathrm{f}$ less shunt capacitance, and mediumfrequency crystal units mounted in the HC-6/U holder have been described as having $0.5 \mu \mu \mathrm{f}$ less shunt capacitance with the holder grounded. However, it should be noted that crystal units so specified are intended primarily for use in circuits where the crystal operates in a series-resonant rather than a parallel-resonant circuit. Even so, the grounded holder alters the entire circuit, not simply $C_{6}$. Thus, in the circuit of figure $1-93$, suppose that it is necessary for the current through $Z$ to be in phase with the generator voltage. If the circuit is properly adjusted with an ungrounded holder, grounding the holder will detune the circuit by effectively decreasing $C_{o}$, on the one hand, and on the other, by shunting the load with $\mathrm{C}_{\mathrm{H} 2}$. The over-all effect cannot be predicted simply by specifying an effective change in $C_{o}$, since the end result will depend upon the impedance characteristics of the entire circuit. If the frequency of a crystal oscillator is being measured by beating its output with the output of a frequency standard, it is common practice to touch the crystal holder with the hand in order to determine whether the crystal unit which is touched is operating at a frequency above or below that of the standard oscillator. The oscillator frequency will be higher or lower than that of the standard according to whether the hand capacitance causes the beat frequency to fall or to rise, respectively, provided that the effective $C_{0}$ is actually increased by the touch of the hand, as is invariably assumed. Before this assumption is made with complete assurance, however, the response of the circuit to a grounded holder should be known.

## EFFECT OF DISTRIBUTED RESISTANCE

1-189. $\mathrm{R}_{\mathrm{L}}$ is assumed to include only the ohmic resistance of the electrical leads and the reflected resistance due to eddy currents in the holder and ground connections. At normal frequencies $R_{L}$ is quite small, as compared with $R_{1}$; even the smallsized supporting wires of wire-mounted crystals have r-f resistances that are measurable in tenths of an ohm. As in the case of the other distributed parameters, the effect of $\mathrm{R}_{\mathrm{L}}$ upon the equivalent circuit of figure 1-91 becomes more pronounced at the higher frequencies. To a first approximation
$R$ is simply $R_{1}+R_{L}$. However, at frequencies above 10 mc , the $r$-f resistance of the leads increases directly as the square root of the frequency, so that, in the v-h-f range $R_{L}$ may be greater than one ohm. $\mathrm{R}_{\mathrm{L}}$ will also increase somewhat if the holder is grounded, as the increased eddy-current losses in the shielding will be reflected as additional resistance losses in the crystal circuit. At normal frequencies, however, the effect of $R_{L}$ is of minor importance; and even at frequencies above 100 mc , its consideration is secondary to the effects of the distributed capacitance.

## RULE-OF-THUME EQUATIONS FOR ESTIMATING PARAMETERS

1-190. The crystal parameters for a given frequency vary rather widely from one crystal unit to the next. Even crystal units of similar dimensions and fabrication made by the same manufacturer may show significant differences between corresponding parameters. These differences arise from the sensitivity of the quartz plate to slight changes in its angle of cut, surface state, electrode area, soldered connections, and the like. The parameter with the greatest percentage variation is $R$, and it is not uncommon for the larger values of R to be from 300 to 900 percent greater than the minimum values. The most predictable parameter is $\mathrm{C}_{e}$, since it is primarily a linear function of the electrode area, the thickness of the quartz dielectric, and the dielectric constant, all of which are reasonably constant for a given fabrication technique, although variations may be expected in crystal units of the same nominal frequency and type of mounting, when made by different manufacturers. For the same manufacturer, nominal frequency, and type of crystal unit, however, $C_{e}$ rarely varies by more than $\pm 5 \%$ of its nominal value. With a reasonably constant $C_{4}$ as a starting point, approximate values for the major parameters $L, C, R$, and $C_{0}$ may be predicted for the principal types of crystal elements and holders. First, $\mathrm{C}_{\mathrm{e}}$ is computed from the known values of plate area, dielectric thickness, and dielectric constant. Next, $C$ can be found, since it is theoretically equal to $\mathrm{C}_{\mathrm{e}}$ times a constant of proportionality. L can next be computed, since the LC product must conform to the nominal frequency. Next, an approximate range of the values of $R$ may be estimated from the empirical values of the crystal quality factor, $Q$. Since $Q$ is the ratio $X_{L} / R$ (or $\left.-X_{C} / R\right), R$ is thus equal to $X_{L} / Q$. Finally, $C_{0}$ can be estimated by simply adding to $\mathrm{C}_{e}$ the approximate total distributed capacitance common to the particular type of holder and mounting.

## Estimating $\mathrm{C}_{\mathrm{e}}$, Static Capacitance of Crystal

1-191. Although the dielectric constant of quartz varies somewhat according to the angle of cut, the following formula will be approximately correct for plated electrodes:

$$
\mathrm{C}_{\mathrm{\theta}}=0.402 \mathrm{~A} / \mathrm{t} \mu \mu \mathrm{f}
$$

where $A$ is the effective electrode area in square centimeters, and $t$ is the thickness in centimeters. 1-192. In the case of partially plated $A$ elements, where $t$ is a function of the nominal frequency and the harmonic, equation 1-191 (1) may be expressed as:

$$
\begin{equation*}
\mathrm{C}_{\mathrm{e}}=2.42 \mathrm{Af} / \mathrm{n} \mu \mu \mathrm{f} \tag{1}
\end{equation*}
$$

where $f$ is the nominal frequency in $\mathrm{mc} / \mathrm{sec}$, and $n$, an odd integer, is the harmonic of the thicknessshear vibration. Although the quartz plates range from 1 to more than 2 sq cm in plate area, the electrode area normally covers only a fraction of the total quartz surface. The RTMA Standards Committee on Quartz Crystals has recommended the following approximate electrode areas for the fundamental frequencies of this type of crystal unit.

| Frequency in me/sec | Electrode Area $\pm 10 \%$ |
| :---: | :---: |
| $(\mathrm{n}=1)$ | $(\mathrm{sq} \mathrm{cm})$ |
| $1-2$ | 0.504 |
| $2-5$ | 0.385 |
| $5-9$ | 0.283 |
| $9-15$ | 0.159 |
| $15-20$ | 0.126 |

For the overtone modes, where $n$ is greater than 1 , the electrode area will be the same as that of the fundamental mode of frequency equal to $f / n$. The harmonics for various ranges of $f$ are as follows:

$$
\begin{aligned}
& \mathbf{f}=10-45 \mathrm{mc} ; \mathrm{n}=3 \\
& \mathrm{f}=45-75 \mathrm{mc} ; \mathrm{n}=5 \\
& \mathrm{f}=75-105 \mathrm{mc} ; \mathrm{n}=7
\end{aligned}
$$

1-193. In the case of crystals vibrating in a faceshear mode, it is the electrode area $A$ that is a function of the frequency. For fully plated $C$ elements, equation 1-191 (1) may be expressed as:

$$
C_{e}=0.038 / t f^{2} \mu \mu f
$$

where $t$ has an average value of 0.05 cm , and $f$ ( $\mathrm{mc} / \mathrm{sec}$ ) lies between 0.3 and $1 \mathrm{mc} / \mathrm{sec}$.
1-194. For fully plated $D$ elements, equation 1-191 (1) may be expressed as:

$$
\mathrm{C}_{\mathrm{e}}=0.0172 / \mathrm{tf}^{2} \mu \mu \mathrm{f}
$$



Figure 1-94. Cr versus frequency for typical wiremounted $N$ elements
where $t$ has an average value of 0.05 cm , and f ( $\mathrm{mc} / \mathrm{sec}$ ) lies between 0.2 and $0.5 \mathrm{mc} / \mathrm{sec}$.
1-195. For a typical wire-mounted $J$ element, equation 1-191 (1) may be expressed as :

$$
C_{e}=k / f \mu \mu f
$$

where: $\mathrm{k}=38$ for $\mathrm{f}=1.2$ to $2.5 \mathrm{kc} / \mathrm{sec}$

$$
\begin{array}{ll}
=45 & =2.5 \text { to } 4.0 \mathrm{kc} / \mathrm{sec} \\
=58 & =4.0 \text { to } 6.6 \mathrm{kc} / \mathrm{sec} \\
=77 & =6.6 \text { to } 10.0 \mathrm{kc} / \mathrm{sec}
\end{array}
$$

Note that $f$ in this case is to be expressed in kc/sec. 1-196. Typical values of $\mathrm{C}_{\mathrm{c}}$ for an N element are shown in figure 1-94.

## Estimating C, Equivalent Motional-Arm Capacifance

1-197. After $\mathrm{C}_{\mathrm{n}}$ is known, an approximate value for $C$ at the fundamental frequency can be readily obtained from the following equation:

$$
\begin{equation*}
\mathrm{C}=\mathrm{C}_{\mathrm{e}} / \mathrm{r}_{\mathrm{e}} \tag{1}
\end{equation*}
$$



Figure 1-95. Approximate values of the ratio of capacitances, $r_{n}=\frac{C_{c}}{C}$, for various plated crysfal elements

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## Electrical Parameters of Crystal Units

where $r_{e}$ is simply the ratio of the electrostatic capacitance $C_{e}$ to the motional capacitance $C$, with $\mathrm{C}_{\mathrm{e}}$ and C expressed in the same units. The values of $r_{e}$ for the more important elements are given in figure 1-95. For the odd harmonics ( $n$ ) of the thickness-shear modes:

$$
\begin{equation*}
\mathrm{C}=\mathrm{C}_{\mathrm{E}} / \mathrm{r}_{\mathrm{e}} \mathrm{n}^{2} \quad 1-197 \tag{2}
\end{equation*}
$$

## Estimating L, Equivalent Motional-Arm Inductance

1-198. Since $X_{L}$ is equal to $X_{c}$ at the series-resonant frequency of the motional arm, $L$ is found quite simply, once $f$ and $c$ are known. Thus:

$$
L=\frac{1}{4 \pi^{2} f^{2} C} \text { henries }
$$

Remember, however, that $f$ is expressed in cycles/ sec, and $C$ in farads.

## Estimating R, Equivalent Mofional-Arm Resistance

1-199. A theoretical equation for $R$ would not be practical, since this parameter is much too sensitive to slight variations during the fabrication process and to changes in the crystal drive. An approximate estimate is gained from observations of the value of $Q$ for the various frequency ranges. Thus:

$$
\begin{equation*}
R=\frac{2 \pi f L}{Q} \text { ohms } \tag{1}
\end{equation*}
$$

where $f$ is in cycles/sec, and $L$ is in henries. The values of Q will range from 10,000 to 200,000 , and in exceptional cases will have much higher values. Generally, the higher Q's are to be found at the higher frequencies. For face-shear elements, the average $Q$ is approximately 30,000 , with most values falling between 10,000 and 40,000 . Thick-ness-shear elements will have average Q's of approximately 75,000 , and most of the values will lie between 35,000 and 100,000 .
$1-200$. The $Q$ is not a dependable parameter, and will vary from frequency to frequency, and from manufacturer to manufacturer, for the same type of crystal unit. For example, when' expressed as $Q=-X_{c} / R=\frac{1}{2 \pi \mathrm{fCR}}$, it can be seen that $Q$ is inversely proportional to C , and thus might be considerably increased by simply reducing the area of the electrodes. On the other hand, the resistance, $R$, is at least limited in practice by military specifications. For this reason, the typical


Figure 1.96. Typital curves of the serios-arm resistance of plated erystals versus frequency. Actual series-arm resistances will vary between $R / 3$ and $3 R$, where $R$ is the value shown, excapt when $R$ is less than 10 ohms, in which case the minimum resistance will be approximately one-half the value indicated. Values indicated are average for fundamental modes and approximately $1 / 2$ the average for overtone modes
values of $R$ versus $f$, shown in figure 1-96, are more likely to be found in randomly selected crystal units than is a given value of $Q$. The values of $R$ indicated in figure 1-96 are merely typical, however, and a small percentage of actual Military Standard crystal units will have series-arm resistances as small as one-third, or as large as three times the amounts showh.

## Estimating Cot $_{0}$ Total Static Shunt Capacitance

1-201. The equation for $C_{0}$ is

$$
C_{o}=C_{e}+C_{d}
$$

where $C_{d}$ is the total distributed capacitance of the crystal leads and terminals. Approximate values of $\mathrm{C}_{\mathrm{d}}$ for plated crystals in ungrounded holders are given below:

| Crystal Holder | $C_{d}(\mu \mu f)$ |
| :---: | :---: |
| $\mathrm{HC}-6 / \mathrm{U}$ | 0.7 |
| $\mathrm{HC}-10 / \mathrm{U}$ | 0.3 |
| $\mathrm{HC}-13 / \mathrm{U}$ | 1.0 |
| $\mathrm{HC}-15 / \mathrm{U}$ | 1.5 |

## IMPEDANCE CHARACTERISTICS VERSUS FREQUENCY

1-202. The superiority of the quartz crystal as a frequency stabilizer lies in the fact that a small change in the frequency will cause a much larger change in the impedance of the equivalent circuit than can be obtained with conventional inductorcapacitor networks. Where an ordinary r-f tank coil would have an inductance measured in microhenries, and an effective $Q$ of 10 to 250 , the equivalent circuit in figure 1-91 will have an inductance measured in henries and a Q of 10,000 to 250,000 or more. C, of course, is extremely small, since its reactance must equal $\mathrm{X}_{\mathrm{L}}$ at resonance, and is commonly expressed in milli- $f$ f (thousandths of a micromicrofarad). $R$ is expressed in ohms, and although at low frequencies it may have values higher than 3000 ohms, depending upon the particular crystal element and method of mounting, the more common values lie between 10 and 100 ohms. $C_{0}$ normally lies between 3.5 and $14 \mu \mu$ f, although much larger values are encountered where electrodes of large surface area are employed. Among the smaller holders, such as types $\mathrm{HC}-6 / \mathrm{U}$ and $\mathrm{HC}-10 / \mathrm{U}$, values of 5 to $6 \mu \mu \mathrm{f}$ are quite common.

1-203.

$$
\text { Since } X_{\mathrm{L}}=2 \pi \mathrm{fL}
$$

$$
\text { and } X_{C}=\frac{-1}{2 \pi \mathrm{fC}}
$$

then, the rates at which $X_{L}$ and $X_{C}$ change with frequency will be, respectively:

$$
\begin{gathered}
\frac{d X_{\mathrm{L}}}{d f}=2 \pi L \\
\frac{d X_{C}}{d f}=\frac{1}{2 \pi f^{2} C}
\end{gathered}
$$

Note that both of these derivatives indicate a positive change in reactance with an increase in frequency. However, it should be remembered that $\mathbf{X}_{c}$ is negative, so that a positive change in $\mathbf{X}_{0}$ means that its magnitude becomes smaller as the frequency increases. On the other hand, the reactance of the inductance increases by an amount $2 \pi \mathrm{~L}$ for each additional cycle per second. At the series-resonant frequency of the series arm, the total reactance

$$
\mathbf{X}_{\mathrm{L}}+\mathbf{X}_{\mathbf{C}}=0
$$

or

$$
2 \pi f_{3} L=\frac{1}{2 \pi f_{3} C}
$$

or

$$
2 \pi L=\frac{1}{2 \pi f_{s}{ }^{2} C}
$$

However, note that this last equation not only implies that the two reactances have equal magnitudes at the series-resonant frequency, $f_{\text {, }}$, but also, that $f_{s}$ is the one frequency at which both reactances will change with frequency at the same rate. Therefore, for small changes in frequency near series resonance:

$$
\Delta \mathbf{X}_{\mathrm{I}}=\Delta \mathbf{X}_{\mathrm{C}}
$$

And since the total change in the reactance of the series arm is

$$
\Delta \mathbf{X}_{\mathrm{s}}=\Delta \mathbf{X}_{\mathrm{L}}+\Delta \mathbf{X}_{\mathrm{C}}
$$

then

$$
\Delta X_{\mathrm{s}}=2 \Delta \mathrm{X}_{\mathrm{l}}=4 \pi \mathrm{~L} \Delta \mathrm{f}
$$

If $f_{s}$ is taken as the reference frequency, so that $\Delta f=f-f_{s}$, then, since $X_{s}=0$ at resonance, the total reactance of the series arm, $X_{s}$, will be equal to $\Delta X_{8}$. That is :

$$
\begin{equation*}
X_{s}=4 \pi L \Delta f \tag{1}
\end{equation*}
$$

Thus, for all frequencies near $f_{n}$, the equivalent circuit of a crystal unit may be represented as shown in figure 1-97, where $X_{C o}$ and $R$ may be assumed


Figure 1-97. Impedance diagram of equivalent circuil of crystal unit

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Figure 1-98. Equivalent circuit of crystal unit when represented as an effective reactance in series with an effective resistance. The ganged arrows indicate that $X_{e}$ and $R_{r}$ will vary together with changes in the frequency, as indicated by the approximate formulas given as functions of $\Delta f$. ( $X_{\varepsilon_{v}}$ is negative.)
to be constant, but with $X_{\text {u }}$ a variable that changes linearly with $\Delta f$, and has the same sign as $\Delta f$. 1-204. The series-parallel circuit of figure 1-97 may be reduced to an equivalent circuit of $X_{\text {e }}$ and $R_{e}$ in series, as shown in figure 1-98. It should be remembered, however, that $X_{c_{0}}$ is negative, whereas $X_{e}$ is either negative or positive, according to the sign of $\Delta f$. The values of $R_{e}$ and $X_{e}$, expressed as functions of $\Delta f$, are not exact, but are close approximations, well within the accuracy of the normal test procedure, except when the numerstors reduce to zero. Note, however, that with $\Delta f=0$, the approximate expressions equate $X$. to 0 , and $R_{e}$ to $R$. This is equivalent to assuming
that $X_{C_{o}}$ is infinite by comparison with $R$, so that at series resonance of the motional arm the crystal unit as a whole behaves as a pure resistance equal to R. Although this is a close approximation, it is not exact. For $X_{e}$ actually to be zero, the term ( $\mathrm{R}^{2}+\mathrm{X}_{*}{ }^{2}+\mathrm{X}_{\mathrm{co}_{0}} \mathrm{X}_{\mathrm{s}}$ ) must be zero. There are two frequencies at which this will occur. One is called the resonant frequency of the crystal unit, $f_{r}$, and the other is called the parallel-resonant, or antiresonant frequency, $f_{k}$.

## RESONANT FREQUENCY OF CRYSTAL UNIT

1-205. First, it should be remembered that $f_{r}$, the resonant frequency of the crystal unit, is almost, but not exactly, identical with $f_{n}$, the series-resonant frequency of the motional arm. If there were no shunt capacitance, $C_{o}$, then $f_{r}$ would indeed be the same as $f_{n}$; but, as it is, $C_{0}$ introduces a reactive component to the current which must be cancelled by a reactive component of opposite phase through the motional arm, if the crystal unit is to appear as a pure resistance. These conditions are illustrated (not to scale) in the vector diagram of the currents through the two arms of the crystal unit, shown in figure 1-99. *Note that the frequency at which the crystal unit has the lowest impedance (maximum current) is $f_{n}$. Since $X_{n}=0$ at this frequency, the equivalent circuit of figure 1-98, according to

* This sentence applies only to the relative impedances suggested by the current vectors in figure 1-99. It can be shown that the true minimum impedance of the crystal unit occurs at a frequency, $f_{m}$, that is es far below $f_{n}$ as $f_{x}$ is above $f_{n}$.


Figure 1-99. Phasor representation (greatly exaggerated) of current through arms of crystal unit af the series-resonant frequencies, $f_{r}$ and $f_{s}$. Distributed inductance of the crystal leads is assumed to be negligible
equations 1 and 2, becomes
and

$$
\begin{aligned}
& \mathbf{X}_{\mathrm{e}}=\mathbf{X}_{\mathrm{Co}}\left(\frac{\mathrm{R}^{2}}{\mathrm{R}^{2}+\mathrm{X}_{\mathrm{Co}_{0}^{2}}}\right) \\
& \mathbf{R}_{\mathrm{e}}=\mathbf{R}\left(\frac{\mathbf{X}_{\mathrm{Co}_{0}}^{2}}{\mathrm{R}^{2}+\mathrm{X}_{\mathrm{Co}_{0}^{2}}}\right)
\end{aligned}
$$

Except at the very high frequencies, $X_{C o}$ is much larger than $R$, so that $R_{e} \approx R$, and $X_{e}$ is so small that it may well be more than annulled by the distributed inductance of the external wiring. Even at frequencies in the neighborhood of $100 \mathrm{mc}, \mathrm{X}_{\mathrm{Co}}$ will have a magnitude in the vicinity of 400 ohms , or approximately 10 times or more than that of $R$, so that $R_{e}$ will equal $R$ within $\pm 1$ percent. The true frequency at which a "series-resonant" crystal circuit is intended to operate, however, is $f_{r}$, where all the reactive components of crystal current cancel. Actually, the term "series-resonance" is somewhat misleading, for the conditions of crystal resonance are those of a parallel, and not a series circuit. It should be understood that when we speak of series-mode circuits and oscillators, the operating frequency is generally assumed to be $f_{r}$. 1-206. By equation 1, figure 1-98, in order for $X_{\text {. }}$ to be zero, the frequency must be such that:

$$
\mathbf{R}^{2}=-\left(\mathbf{X}_{\mathrm{s}}^{2}+\mathrm{X}_{\mathrm{Co}} \mathrm{X}_{\mathrm{s}}\right)
$$

Since $X_{C_{0}}$ is negative, this equality can only exist when $X_{n}$ is positive, i.e., $X_{n}$ is inductive, and $f>f_{s}$. At frequencies very close to $f_{k}, X_{C o} \gg X_{k}$, so that $X_{n}{ }^{2}$ may be considered negligible. Thus, $f_{r}$ will be the frequency at which

$$
\mathbf{R}^{2}=-\mathbf{X}_{\mathrm{Co}} \mathrm{X}_{\mathrm{s}}=-4 \pi \mathrm{~L} \mathrm{X}_{\mathrm{Co}} \Delta \mathrm{f}_{\mathrm{r}}
$$

where $\Delta f_{r}=f_{r}-f_{s}$
Since $X_{C o}$ is negative,

$$
\begin{equation*}
\Delta f_{r}=\frac{-\mathrm{R}^{2}}{4 \pi \mathrm{LX}} \tag{1}
\end{equation*}
$$

1-207. As a concrete example, assume that a partially plated A element, mounted in an HC-6/U holder according to RTMA recommendations, operates at resonance in its fundamental mode at a nominal frequency of 10 mc . Approximately, what value of $\Delta f_{r}$ could be expected? Referring to paragraph 1-192, we find that $A=0.159 \mathrm{sq} \mathrm{cm}$. On substitution in equation 1-192(1) :

$$
C_{0}=2.42 \times 0.159 \times 10=3.85 \mu \mu f
$$

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According to figure $1-95, r_{0}=250$. Thus, by equation 1-197 (1):

$$
C=\frac{3.85}{250}=1.54 \times 10^{-2} \mu \mu \mathrm{f}
$$

By equation 1-198 (1):

$$
\begin{aligned}
\mathrm{L} & =\frac{10^{14}}{4 \times 3.14^{2} \times 10^{14} \times 1.54} \\
& =1.65 \times 10^{-2} \text { henries }
\end{aligned}
$$

According to paragraph 1-201:

$$
\mathrm{C}_{o}=3.85+0.7=4.55 \mu \mu \mathrm{f}
$$

So that

$$
\begin{aligned}
X_{C_{0}} & =\frac{-1}{2 \pi f_{\mathrm{r}} C_{o}}=\frac{-10^{12}}{6.28 \times 10^{7} \times 4.55} \\
& =-3.5 \times 10^{3} \Omega
\end{aligned}
$$

From figure 1-96, a typical value of $R$ is found to be $8 \Omega$. On substitution of the foregoing values of $R, L$, and $X_{r_{0}}$ in equation 1-206(1), we find that:

$$
\begin{aligned}
\Delta f_{r} & =\frac{8^{2} \times 10^{-1}}{4 \times 3.14 \times 1.65 \times 3.5} \\
& =0.088 \mathrm{cycle} / \mathrm{sec}
\end{aligned}
$$

With such an extremely small difference between the two resonant frequencies of the crystal unit (less than 1 part of $10^{\circ}$ ), for all practical purposes it can be assumed that $f_{n}=f_{r}$. Indeed, it would be academic to seek to distinguish between them. Remember, however, that the discussion has only concerned the equivalent circuit, in which the effects of the distributed inductance have been assumed to be reflected in a lower series-arm frequency, and a larger $C_{o}$. If the parameters in the example above are assumed to be the "true" values, so that the inductance of the leads must be represented separately, then a slightly more realistic interpretation will be possible. Assume, for instance, the $L_{L}=10^{-8}$ henries. Then

$$
X_{L L}=2 \pi L_{1} f_{s}=0.628
$$

In order for $X_{e}$ to cancel this reactance, then, by equation 1 in figure 1-98:

$$
-4 \pi \mathrm{~L} \Delta \mathrm{f}_{\mathrm{F}}=0.628
$$

or

$$
\Delta f_{r}=\frac{-0.628}{4 \pi \times 1.65 \times 10^{-2}}=3 \text { cycles } / \mathrm{sec}
$$

## Electrical Parameters of Crystal Units

The inductance of the external connections could easily increase this value of $\Delta f_{r}$ ten-fold, so that for optimum frequency stability, an external series capacitance would be necessary. It is important to note the negligible effect that a small change in $R$ or $C_{0}$ will have on the frequency of a crystal unit at series resonance. In equation 1-206(1), as applied to the $10-\mathrm{me}$ crystal unit, even if $R$ should triple in value, the frequency would not change by more than 1 part in $10^{7}$. Although the power transferred through the crystal would be diminished, as would the $Q$, and hence, the effectiveness of the crystal as a frequency stabilizer, a reasonable increase in $R$ will not, in itself, cause the frequency of a series-resonant crystal oscillator to drift.

## ANTIRESONANT FREQUENCY OF CRYSTAL UNIT

1-208. Returning again to equation 1 of figure 1-98, it can be seen that the term ( $\mathrm{R}^{2}+\mathrm{X}_{0}{ }^{2}+\mathrm{X}_{\mathrm{C}_{0}} \mathbf{X}_{4}$ ) can also be zero at some higher frequency than $f_{r}$, namely, when $X_{s}=X_{\omega_{0}}$ ( $R^{2}$ being negligible). This would represent the high-impedance, parallel-resonant state of the equivalent circuit in figure 1-97. Letting $\Delta f_{n}=f_{m}-f_{n}$ then, at $f_{n}$ the antiresonant frequency

$$
X_{\mathrm{sa}}=4 \pi L \Delta f_{n}=\left|X_{C o}\right|
$$

so that

$$
\begin{equation*}
\Delta f_{\mathrm{a}}=\frac{\left|\mathrm{X}_{\mathrm{C}_{0}}\right|}{4 \pi \mathrm{~L}} \tag{1}
\end{equation*}
$$

On substitution of the typical values of $X_{C o}$ and $L$ that were found for the $10-\mathrm{mc}$ crystal unit:

$$
\Delta f_{\mathrm{t}}=\frac{3.5 \times 10^{3}}{4 \times 3.14 \times 1.65 \times 10^{-2}}=16.9 \mathrm{kc} / \mathrm{sec}
$$

For a 10 -me crystal, this value of $f_{a}$ represents a 0.169 percent frequency range in which the crystal may be used as a frequency-control device. At all frequencies within its range, except at $f_{r}$ and $f_{a}$, the unit will appear to the external circuit as an inductive reactance, $X_{e}$, in series with a resistance, $R_{e}$. There is a very simple relation between the fractional frequency range, $\frac{\Delta f_{a}}{f}$, and the ratio of the capacitances, $r=\frac{C_{0}}{C}$, that can be derived from equation 1. Thus:

$$
\Delta f_{\mathrm{s}}=\frac{1}{4 \pi \mathrm{~L} 2 \pi \mathrm{fC}_{6}}
$$

so

$$
\Delta f_{a} / f=\frac{1}{2 \omega^{2} L C_{0}}
$$

where $\omega=2 \pi$ f. Now,

$$
\omega^{2}=1 / \mathrm{LC}
$$

so, on substitution:

$$
\begin{equation*}
\Delta f_{s} / f=C / 2 C_{0}=1 / 2 r \tag{2}
\end{equation*}
$$

In the case of plated crystals, $r$ is usually somewhat less than that predicted by theory. Where it should be slightly greater than the values of $r_{e}$ in figure 1-95, since $C_{0}>C_{e}$, it is usually somewhat less. However, as a practical rule-of-thumb, it can be assumed that $r=r_{e}$, but only in those cases where $C_{0} \approx C_{e}$. The ratio of capacitances, $r$, is quite an important parameter of the crystal unit in its own right, not only as an indication of the maximum percentage width of the frequency band in which a particular crystal element can operate, but, as will be discussed later, as a measure of the electromechanical coupling, and also, because of its relation to the frequency stability.

## IMPEDANCE CURVES OF CRYSTAL UNIT

1-209. Figure 1-100 shows the typical characteristics of the equivalent impedance circuit of figure $1-98$, but with the frequency scale greatly expanded near the resonance point of the crystal. At frequencies sufficiently removed from resonance, both above and below $f_{r}$, where the motional impedance is large compared with $\mathrm{X}_{\mathrm{Co}}$, the $\mathrm{X}_{\mathrm{e}}$ curve is essentially the same as the reactance curve of a capacitance equal to $C_{0} . X_{e}$ is inductive only between its two zero points, $f_{5}$ and $f_{a}$. Note that $R_{s}$


Figure 1-100. Impedance sharacteristics versus frequency of crystal unit. Neither the frequency nor the impedances are drawn to scale
rises sharply to a maximum at $f_{a}$, where it is equal to the parallel-resonant impedance of the equivalent circuit of figure 1-97. Since $R$ is much smaller than $X_{C o}$, at antiresonance

$$
\mathbf{R}_{e}=\mathrm{Z}_{\mathrm{e}}=\left(\mathbf{X}_{\mathrm{C}_{0}}\right)^{2} / \mathbf{R}
$$

In the case of the particular 10 -me crystal unit where $X_{C a}=-3.5 \times 10^{3} \Omega$, and $R=8 \Omega, R_{\mathrm{e}}$ at antiresonance will be approximately 1.5 megohms. $\mathbf{Z}_{e}\left(=\sqrt{\left.R_{e}{ }^{2}+X_{e}{ }^{2}\right)}\right.$ at most frequencies is simply equal to $X_{e r}$. Only in the immediate regions of $f_{r}$ and $f_{a}$, where $X_{e}$ becomes negligible, is the magnitude of $\mathrm{Z}_{\mathrm{e}}$ affected greatly by $\mathrm{R}_{\mathrm{e}}$. The impedances, of course, are not drawn to scale. For example, if $\mathrm{Z}_{e}$ at antiresonance were drawn to the scale used for $Z_{e}$ at resonance, the curve could extend more than a mile above the horizontal axis.

## PARALLEL-RESONANT FREQUENCY, $\boldsymbol{f}_{\mathrm{p}}$, OF CRYSTAL CIRCUIT

1-210. Although an oscillator may depend upon a crystal operating at its series-resonant frequency, it is not practicable for a crystal unit to control an oscillator at the antiresonant frequency, $f_{a}$. The crystal will either be operated to pass a maximum current (series-resonant circuit), or to develop a maximum voltage (parallel-resonant circuit) at some proper phase and frequency. It would seem that these latter conditions could best be met by operating the crystal unit at its antiresonant frequency, for it is in this region that the effective impedance is most sensitive to small changes in the frequency. However, another circuit, such as the input of a vacuum tube, will necessarily be


Figure 1-101. Equivalent parallel-resonant circuit of erystal unit ( $X_{r p,} R_{c} p$ ) shunted by load ( $X_{1}, R_{i}$ ). Normafly $\boldsymbol{f}_{r}<\boldsymbol{f}_{p}<\boldsymbol{f}_{a}$ so that $X_{r p}$ is inductive and $X_{r}$ is capacitive
shunted across the crystal. The shunt, or load circuit into which the crystal operates will have a much lower impedance than that of the crystal at antiresonance, so that the total impedance will be relatively insensitive to small frequency variations in the region of $f_{a}$. In determining the actual frequency stability, the entire circuit must be considered as a whole. The operating frequency may be considered as the resonant frequency, $f_{p}$, of an equivalent parallel circuit, as shown in figure 1-101. $X_{e p}$ and $R_{e p}$ are simply the reactance and resistance of the equivalent circuit of the crystal unit at $f_{p}$, and $X_{x}$ and $R_{x}$ are the equivalent shunt reactance and resistance, respectively. Since $X_{0}$ is more frequency-sensitive above series resonance than below, there is normally no advantage in using a crystal in circuits that require $X_{e}$ to be capacitive. Thus, in practice, $f_{5}$, will be some intermediate frequency between $f_{r}$ and $f_{s}$, so that $X_{e p}$ is always inductive and $X_{x}$ is always capacitive. The distinction made between "parallel resonance" and "antiresonance" in this discussion is somewhat arbitrary, and it is not uncommon to use the term "antiresonant" to describe any parallel-resonant crystal unit.

## Effects of Changes in Shunt Capacitance on $\boldsymbol{f}_{\mathrm{p}}$

1-211. In discussing $\Delta f_{r}$, the difference between the motional and the effective resonant frequency, it was found that

$$
\Delta f_{\mathrm{r}}=\left|\frac{\mathrm{R}^{2}}{4 \pi \mathrm{~L} \mathrm{X}_{\mathrm{Co}}}\right|
$$

That this quantity is normally insignificant is fortunate, for it varies directly with the square of $R$, a parameter quite likely to change during operation. On the other hand, it was later found that

$$
\Delta f_{a}=\left|\frac{X_{\mathrm{Co}}}{4 \pi \mathrm{~L}}\right|
$$

could amount to more than 0.1 percent difference in frequency. In this case, since, $\Delta f_{a}$ is relatively large, it is also quite fortunate that, to a first approximation, the antiresonant frequency of a given crystal unit is independent of operational changes in R. However, it is not the antiresonant frequency of the crystal unit itself, but rather, the actual parallel-resonant frequency at which the crystal unit will operate that is of primary interest. Let $f_{p}-f_{n}=\Delta f_{p}$. Now, it can be imagined that $\Delta f_{p}$ is simply the $\Delta f_{a}$ of a crystal unit whose shunt capacitance $C_{0}$ has been increased by an


Figure 1-102. Equivalent parallel-resonant tank circuit, in which the motional impedance of the crystal unit is the inductive arm of the tank, and the total shunt impedance is the capacitive arm
amount $C_{x}$ and which has an effective resistance added to the shunt arm equal to $R_{x}\left(\frac{C_{x}}{C_{s}+C_{x}}\right)^{2}$. This last assumption can be made without introducing an appreciable error as long as $R_{x}$ is small compared with $\mathrm{X}_{\mathrm{x}}$. The multiplying factor is needed, since only a fraction, $\left(\frac{C_{x}}{C_{o}+C_{x}}\right)$, of the total equivalent tank current will flow through $\mathrm{R}_{\mathbf{x}}$. The equivalent tank circuit is shown in figure 1-102, where $C_{T}$ and $R_{T}$ are the values of the shunt parameters. Now, since $\Delta f_{\mathrm{p}}$ is equivalent to the
$\Delta f_{s}$ of a crystal unit that has $C_{0}=C_{r}, \Delta f_{p}$ will be expressed by the same general formula that holds for $\Delta f_{\text {a. }}$. Thus, $\Delta f_{p}=\left|\frac{X_{T_{p}}}{4 \pi L}\right|$. Also, since $\mathrm{X}_{\mathrm{T}}=-1 / 2 \pi \mathrm{fC}_{T}$, it can be seen that $\Delta \mathrm{f}_{\mathrm{p}}$, will be inversely proportional to the total shunt capacitance. Although $\mathrm{C}_{0}$, itself, is the most stable of all the crystal parameters, the stability of the effective external capacitance $C_{s}$ will depend upon the over-all design of the oscillator circuit. The crystal unit may be considered a device that determines the limits within which the frequency may be varied; that is, $f_{p}$ must lie somewhere between $f_{r}$ and $f_{k}$. However, it is primarily the parameters of the external circuit in conjunction with the equivalent $\mathrm{L}, \mathrm{C}$, and $\mathrm{C}_{0}$ of the crystal that fix the exact frequency; and although the stability of the crystal parameters is fundamentally a problem for the crystal manufacturer, the stability of the effective $\mathrm{C}_{\mathrm{T}}$ is largely the concern of the radio designer.
1-212. Figure 1-103(A) shows the reactance curve of $\mathrm{X}_{n}$ versus frequency, and figure 1-103(B) shows the reactance curve of $X_{T}$ versus $C_{T}$. The values of $X_{n}$ are those of the $10-\mathrm{mc}$ crystal unit which has previously been taken as an example, and where $L$ is assumed to be $1.65 \times 10^{-8}$ henry. Note that the variations in $X_{T}$ with frequency have been neglected, and $f$ is simply assumed to equal the nominal frequency of 10 mc , insofar as the capacitive arm is concerned. Since $X_{n}$ and $X_{r}$ are drawn to the same scale, a horizontal line drawn through


Figure 1-103. Reactance curves of: (A) $X_{s}$ versus $\Delta f_{i}(B)-X_{t}$ versus $C_{t}$
both curves will intersect points of equal but opposite reactances. These points of intersection will, in turn, indicate the value of $\Delta f$ required for a given $C_{T}$, if the two arms are to be resonant. For example, at $\mathrm{C}_{\mathrm{T}}=7.69 \mu \mu \mathrm{f}, \mathrm{X}_{\mathrm{T}}=-2000 \Omega$; so that in order for $X_{,}$, to be $2000 \Omega, \Delta f_{p}$ must equal 9.65 kc . Likewise, a $\mathrm{C}_{\mathrm{T}}$ of $40 \mu_{\mu} \mathrm{f}$ will mean approximately a $\Delta f_{p}$ of 2 kc . Now it so happens that the part of $\mathrm{C}_{\mathbf{T}}$ represented by $\mathrm{C}_{\boldsymbol{x}}$ will have a component that tends to vary with changes in the plate voltage applied to the vacuum tube, changes in the temperature or the tuning, changes in the coupling and neutralizing adjustments, and any changes in the vacuum-tube characteristics or other circuit parameters due to other causes. Such a change in $X_{x}$ will cause not only a change in the resonant frequency, but also a change in the amplitude of the oscillations. If a given change in $\mathrm{C}_{\mathrm{x}}$ is to have a minimum effect upon the frequency and power expenditure of the oscillator, then $\mathrm{C}_{\mathrm{T}}$ must be as large as possible without seriously reducing the stabilizing effect of the crystal. In other words, $C_{T}$ should have a value where the slope of the $\mathrm{X}_{\mathrm{T}}-\mathrm{vs}-\mathrm{C}_{\mathrm{T}}$ curve is not steep. For the 10 -mc crystal of figure 1-103, maximum stability would be obtained with $\mathrm{C}_{\mathrm{T}}$ between 36 and $40 \mu \mu \mathrm{f}$. With $\mathrm{C}_{0}$ equal to $4.55 \mu \mu$, this would mean a load capacitance, $\mathrm{C}_{\mathrm{x}}$, between 32 and $36 \mu \mu \mathrm{f}$. As much of $\mathrm{C}_{\mathrm{x}}$ as is possible should be supplied by a fixed or adjustable capacitor connected directly across the crystal unit or in some other part of the circuit, so that its effective capacitance with respect to the crystal terminals will remain constant, and not be affected by changes in the tube characteristics. This would reduce the variable part of $\mathrm{C}_{\mathrm{x}}$ to a minimum. $\mathrm{C}_{\mathrm{T}}$, however, should not be made so large that $X_{T}$ will approach the magnitude of $R$, otherwise the crystal will not only lose some of its stabilizing effectiveness, but will require an excessive drive level to maintain oscillations.

## Stablizing Effect of Crystal on $\boldsymbol{F}_{\mathrm{D}}$

1-213. Although $\mathrm{C}_{\mathrm{T}}$, plays an important role in the final determination of the frequency, it is the crystal itself that must be primarily responsible for the stability of the frequency-that is, if the use of a crystal is to be justified. For this reason, care should be taken to make certain that the apparent Q. of the crystal series arm $\left(\frac{X_{0}}{R}\right)$ is as large as 10 , if possible, and preferably much larger during operation. Otherwise, the series-arm impedance will not respond with maximum sensitivity to changes in $\mathrm{C}_{\mathrm{T}}$. However, since $\mathrm{X}_{\mathrm{T}}$, and hence $\mathrm{X}_{\mathrm{a}}$, must be kept small to reduce the effects of a
change in $\mathrm{C}_{\mathrm{T}}$, it might appear at first thought that a conventional coil could serve quite as well as a crystal. The reason why this is not true is that the frequency stability is dependent upon the magnitude of the change in reactance for a given change in frequency, and not primarily upon the total magnitude of the reactance. It will be recalled that, in the conventional $L_{-}$C circuit, the instantaneous rate of change of $\mathrm{X}_{\mathrm{I}}$ with frequency is

$$
\frac{\mathrm{dX}_{\mathrm{L}}}{\mathrm{df}}=2 \pi \mathrm{~L}
$$

and that, at resonance

$$
\frac{\mathrm{d} \mathrm{X}_{\mathrm{L}}}{\mathrm{df}}=\frac{\mathrm{d} \mathrm{X}_{\mathrm{C}}}{\mathrm{df}}
$$

In the parallel-resonant crystal circuit, however, these equalities do not hold, for $X_{u}=4 \pi \Delta f L$, and not $2 \pi \mathrm{fL}$. Thus, $\frac{\mathrm{dX}}{\mathrm{df}}=4 \pi \mathrm{~L}$, where L of the crystal is greater than $L_{c}$ of a coil of the same reactance by a factor of $f / 2 \Delta f$. Since at resonance, the rate of change of $\mathrm{X}_{\mathrm{T}}$ would equal that of $\mathrm{X}_{\mathrm{L}}$, it follows that $4 \pi \mathrm{~L}$, the change in the motional reactance with frequency, will be $f_{v} / \Delta f_{p}$ times as great as the change in $X_{T}$ with frequency. Consequently, the stabilizing effect of the crystal is much greater than that of the shunt reactance, so that, for all practical purposes, the crystal can "automatically" annul the effect of small changes in $\mathrm{C}_{\mathrm{T}}$, but not vice versa. It can be seen that, even with $X_{n}$ relatively small, the stabilizing effect of the crystal for a fixed change in $X_{T}$ is not diminished, provided, of course, that $X_{s}$ is sufficiently large, as compared with $R$, so that the total impedance of the series arm is essentially equal to, and varies linearly with, $X_{4 .}$ (See paragraphs 1-238 to 1-245.)

## Effect on Parallel Crystal Circuit Due to Variations in Resistance

1-214. As long as the apparent $Q$ of the parallel. resonant circuit $\left(\frac{X_{k}}{R+R_{T}}\right)$ is at least as great as 10 , a change in either $R$ or $R_{T}$ will not, in itself, have a large effect upon $f_{p}$. However, depending upon the design of the particular circuit, a change in the resistance may indirectly affect the frequency by causing a change in $\mathrm{C}_{\mathrm{T}}$, since, to a certain extent, the effective $C_{T}$ will be a function of the other circuit parameters. The most critical effect due to changes in the resistance parameters is the effect on the power required for excitation of the oscillator in order to obtain a given output. The impedance, $Z_{p}$, of the parallel circuit at reso-
nance will be approximately $\frac{X_{\Delta p}{ }^{2}}{R+R_{T}}$. An increase in the total resistance of 100 percent would thus decrease $\mathrm{Z}_{\mathrm{F}}$ by one half. If, for example, the output of the oscillator depended directly upon the r-f voltage across $Z_{y}$ (i.e., across the crystal), a decrease in $Z_{p}$ by one half would require twice as much power in the crystal circuit to maintain the output at the same level as before. A part of $\mathrm{R}_{\mathrm{T}}$ will be the result of reflected resistance losses in the output circuit. An increase in the load will thus be reflected as an increase in $\mathrm{R}_{\mathrm{T}}$. This is unfortunate, for if the load should increase it would be desirable to have an increase in $Z_{y}$, to raise the exeitation voltage automatically, or at least to keep it constant. As it is, the effect is to decrease the excitation, unless special circuits, such as the TriTet, are employed to increase the feedback directly. If a principal component of the losses in $\mathrm{R}_{\mathrm{T}}$ are due to the losses in the grid circuit, and if the oscillator design is such that the grid current is not linear with the excitation voltage, but rises at a much greater rate, then $\mathrm{R}_{\mathrm{T}}$ can rapidly increase or decrease with the excitation voltage, and $\mathrm{Z}_{\mathrm{P}}$ will vary inversely. Under these conditions, $\mathrm{Z}_{\mathrm{P}}$ will always change in a direction that will tend to annul any change in the excitation voltage. The greater that part of $R_{T}$ reflecting the grid losses, as compared with that part reflecting the output losses, the greater will be the amplitude stabilizing effect for counteracting changes in the plate voltage or the effective load resistances. Another characteristic of a crystal circuit in which $R_{T}$ varies automatically is that the effect resulting from a variation in R is minimized. Assume, for example, that the desired output at a constant load will require a certain effective value of $\mathrm{Z}_{\mathrm{P}}$. If, for some reason, $R$ should change, thereby changing the excitation voltage, $R_{T}$ would tend to change by an equivalent amount in the opposite direction, thus maintaining $\mathrm{Z}_{\mathrm{p}}$, and hence the output, essentially constant. However, a change in $R$ or $R_{T}$ will almost certainly be accompanied by a change in the crystal power losses, thereby causing a frequency drift if the particular crystal unit is frequency-sensitive to the drive level. At this point, however, the important items to note are: (1) $\mathrm{X}_{\mathrm{T}}$, and hence $\mathrm{X}_{\mathrm{ap}}$ preferably should not be smaller than $10\left(R+R_{T}\right)$, or the maximum stabilizing effect of the crystal will not be realized; (2) the direct effect of a change in ( $R+R_{T}$ ) is to change $Z_{p}$; (3) the effects of a change in $Z_{p}$ primarily will involve changes in the excitation voltage, in the power expended in the crystal circuit, as well as that delivered to the load, and in the equivalent value of
$\mathrm{C}_{\mathrm{r}}$, thereby also changing the frequency; (4) if changes in either R or $\mathrm{R}_{\mathrm{T}}$ are such that the power expended in the crystal unit itself is caused to vary, then a significant change in the frequency characteristics of the crystal may result; and (5) for maximum frequency stability, the oscillator should be lightly loaded, and the drive level of the crystal should be as small as is practicable.

## Effect on Parallel Crystal Circuits Due to Variations in Motional-Arm C or L.

1-215. Crystal circuits operated at the resonant frequency of the crystal units may be only slightly affected by variations in C or L from one crystal unit to the next, or even during the operation of a particular unit, provided that the effective LC product remains constant, so that the frequency does not change. In the parallel-resonant circuit, however, even if $f_{g}$ is the same, a different $C$ and $L$ means a change in $\Delta f_{p}$. For a given $C_{T}$ and nominal frequency, $X_{T_{p}}$, and hence, $X_{\mathrm{a}}$, must remain approximately constant, so that $\Delta f_{p}$, equal to $X_{4 p} / 4 \pi \mathrm{I}_{\text {, }}$, will tend to vary inversely with L . The exact value of $L$ for a given crystal unit will depend upon the effective electrode area, the orientation of the cut, the thickness of the crystal, whether twinning is present in the quartz, and the degree to which spurious modes are coupled to the desired mode. Insofar, as the variations in L from one crystal unit to the next are concerned, no problem arises unless it is necessary to adjust $f_{p}$ to an exact value; in which case the problem of the design engineer is to ensure that $\mathrm{C}_{\mathrm{r}}$ will be sufficiently adjustable so that the desired $f_{p}$ may be obtained with any reasonable value of $L$. Since such adjustments must be provided for anyway, in order to allow for different values of $f_{\mathrm{s}}$, no new problems are introduced, except that a greater deviation in $\Delta f_{p}$ must be met than otherwise. Unless spurious modes are closely coupled to the desired mode, the variations in L that might occur during the operation of a particular crystal unit will be too small to affect the magnitude of $\Delta f_{p}$, as long as $X_{T_{p}}$ remains constant. However, the operational variations of $L$ and/or $C$ may be such that $f$, will change, in which case $f_{p}$ will also change. Such a deviation in frequency, i.e., in the equivalent LC product, would occur during changes in temperature or drive level, or because of fatigue or other aging effects. Minimum variations in $L$ and $C$ are obtained by the use of low temperature-coefficient crystals and constant-temperature ovens, and by ensuring that the drive level will remain both low and constant. In any event, a reasonable operational variation in $f_{p}$ can be compensated for by an adjustment in $C_{\pi}$.

## Minimum Value of $\Delta f_{p}$

1-216. Returning to equation 1 in figure 1-98, let it be imagined that $X_{e}$ represents the effective reactance of the motional arm of a crystal unit in parallel with a total capacitance $\mathrm{C}_{\mathrm{T}}$, instead of simply the $\mathrm{C}_{8}$ of the crystal unit, itself. Furthermore, assume that $R_{T}$ is negligible. As before, the condition of resonance is that $X_{e}$ be zero, which will occur only when

$$
\mathrm{R}^{2}+\mathrm{X}_{\mathrm{a}}{ }^{2}+\mathrm{X}_{\mathrm{a}} \mathrm{X}_{\mathrm{T}}=0
$$

(Note that $\mathrm{X}_{T}$ now replaces $\mathrm{X}_{\mathrm{Co}}$ ) Now $\mathrm{X}_{\mathrm{n}}=4 \pi \mathrm{~L} \Delta \mathrm{f}$, and on substitution in the preceding equation and rearranging, it is found that

$$
(\Delta f)^{2}+\frac{\mathrm{X}_{\mathrm{T}}}{4 \pi \mathrm{~L}} \Delta f+\frac{\mathrm{R}^{2}}{16 \pi^{2} \mathrm{~L}^{2}}=0
$$

Note that this is simply a quadratic equation of the type $A X^{2}+B X+C=0$, so by the quadratic formula

$$
\Delta f=\frac{-\frac{X_{T}}{4 \pi \mathrm{~L}} \pm \sqrt{\frac{\mathrm{X}_{\mathrm{T}}^{2}-4 \mathrm{R}^{2}}{16 \pi^{2} \mathrm{~L}^{2}}}}{2}
$$

The $\pm$ term indicates that there are two possible solutions for $\Delta f$ at which resonance will occur. One of these is equivalent to $\Delta f_{r}$ (but with $C_{0}$ replaced by $\mathrm{C}_{\mathrm{T}}$ ), and the other is equivalent to $\Delta \mathrm{f}_{\mathrm{p}}$. For these solutions of $\Delta f$ to be real, $X_{T^{2}}$ must be greater than $4 R^{2}$; otherwise, the expression under the radical sign becomes negative, and $\Delta f$ will be imaginary. However, in the special case where $\mathrm{X}_{\mathrm{T}}{ }^{2}-4 \mathrm{R}^{2}=0$, there is only one solution for $\Delta f$. In other words,

$$
\Delta f_{r}=\Delta f_{\mathrm{p}}=\frac{-\mathrm{X}_{\mathrm{T}}}{8 \pi \mathrm{~L}}
$$

This represents the minimum value obtainable for $\Delta f_{p}$; or, from the point of view of series resonance, it may be considered the maximum value obtainable for $\Delta f_{r}$. The important point to note is that neither parallel nor series resonance is possible unless $X_{T}{ }^{1}$ is equal to, or greater than, $4 R^{2}$. At the minimum $\Delta f_{n}$,

$$
\mathrm{X}_{\mathrm{T}}{ }^{2}=4 \mathrm{R}^{2}
$$

or

$$
\left|X_{\mathrm{T}} / \mathrm{R}\right|=\mathrm{X}_{\mathrm{0}} / \mathrm{R}=2
$$

It should be remembered that all the resistance has been assumed to be in the motional arm, and so
has the effect of limiting the maximum component of lagging current for a given voltage; but parallel resonance could be achieved at any frequency between $f_{n}$ and $f_{s}$ if $R_{T}$ were equal to $R$. However, since $\mathrm{C}_{0}$ limits the minimum amplitude of leading current, $\mathrm{R}_{\mathrm{r}}$ cannot be made equal to R for all values of $f_{1}$, and there will still be a minimum $f_{p}$ greater than $\mathrm{f}_{\mathrm{s}}$. (A minimum which can be shown to be identical with the natural $f_{r}$ of the crystal unit.) With $\mathrm{R}_{\mathrm{r}}$ assumed to be negligible, the ratio of reactance to resistance equal to 2 represents the minimum apparent $Q_{n}$ of the parallel crystal circuit, if resonance is to be obtained. As stated previously, if the full stabilizing properties of the crystal are to be in use, $Q_{n}$ should be at least 10. However, if the power delivered to the crystal circuit is sufficient, oscillations can be maintained as long as the apparent $Q_{n}$ does not fall below 2. This occurs at the frequency at which the amplitude of the lagging component of current through the series arm is the maximum obtainable.

## TYPICAL OPERATING CHARACTERISTICS OF CRYSTAL UNIT

1-217. Figure 1-104 shows the effective impedance characteristics of the 10 -mc crystal unit which has been assumed to have the following parameters:

$$
\begin{aligned}
\mathrm{L} & =1.65 \times 10^{-2} \text { henry } \\
\mathrm{C} & =1.54 \times 10^{-2} \mu \mu \mathrm{f} \\
\mathrm{R} & =8 \text { ohms } \\
\mathrm{C}_{o} & =4.55 \mu \mu \mathrm{f}
\end{aligned}
$$

$\mathrm{X}_{\mathrm{e}}, \mathrm{R}_{\mathrm{e}}$, and $\mathrm{Z}_{\mathrm{r}}$ are given by equations 1,2 , and 3 , respectively, in figure 1-98; $\mathrm{X}_{\mathrm{co}}$ is assumed to be equal to $-3.5 \times 10^{3}$ ohms for all values of $\Delta f$. Note that the normal operating range covers only about one fourth of the total range between $f_{r}$ and $f_{s}$. Of course, if $\mathrm{C}_{0}$ were greater than the value assumed, $\Delta f_{z}$ would be smaller and the normal operating range would be a larger percentage of the total. As explained previously, $\mathrm{C}_{\mathrm{T}}\left(=\mathrm{C}_{0}+\mathrm{C}_{\mathrm{s}}\right)$ must be relatively large, so that small variations in $\mathrm{C}_{\mathrm{x}}$ will not greatly affect the frequency, and it is this consideration that limits the practical operating range to low values of $\Delta f$. At parallel resonance, $X_{e}$ must approximately equal $-X_{x}$, for the same reason that $X_{k}$ must equal - $\mathbf{X}_{\mathrm{T}}$. Standard military high-frequency crystal units are normally tested with a value of $\mathrm{C}_{\mathrm{x}}=32 \mu \mu \mathrm{f}$. At 10 mc , a capacitance of $32 \mu \mathrm{f}$ will have a reactance of approximately -500 n , as indicated in figure 1-103(B). With $C_{0}=4.55 \mu \mu f, C_{T}$ will be $36.55 \mu \mu$ f, which corresponds to a value of $X_{T}=-440 \Omega$, and a $\Delta f=2.1 \mathrm{kc} / \mathrm{sec}$. $\Delta f$ can also be found from the reactance curve of figure 1-104 at the point where

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Electrical Poramaters of Crystal Units


Figure 1-104. Typical characteristic curves for $X_{e}$ and $R_{r}$ of $10-m e$ crystal unit. (Shunt resistance, $R_{i}$, across erystal is assumed to be negligible)
$\mathrm{X}_{\mathrm{e}}=-\mathrm{X}_{\mathrm{x}}=500 \Omega$. Crystal units are sometimes operated in series with an external capacitor, $\mathrm{C}_{\mathrm{x}}$, as indicated in figure 1-105. Slight variations in the frequency can be compensated for by adjustments of $\mathrm{C}_{\mathrm{r}}$, and resonance will occur at the frequency at which $X_{x}$ is exactly annulled by $X_{\text {e }}$. If the ratio of $X_{e} / R_{e}$ is sufficiently large, then for all practical purposes the series-resonant frequency, $f_{r r}$, is the same as the $f_{p}$ of the crystal unit in parallel with the same $\mathrm{C}_{\mathrm{r}}$. At resonance, the crystal unit and $C_{x}$ in series have an effective impedance equal to $\mathrm{R}_{\mathrm{e}}$. Although there is an effective maximum $Q_{\mathrm{em}}=\frac{\mathrm{X}_{\mathrm{e}}}{\mathrm{R}_{\mathrm{e}}}$ when $\Delta \mathrm{f}=\frac{\Delta \mathrm{f}_{\mathrm{t}}}{2}$, it has no special significance directly concerning the frequency sta-


Figure 1-105. Equivalent circuif of crystal unit connected in series with capacitor
bility of the circuit, but does tend to increase the activity. In general, if a series capacitor is used, its reactance will be small, as compared with $\mathbf{X}_{\mathrm{C}_{0}}$. Indeed, it may be used for no other purpose than to annul the self inductance of the crystal leads. It can be seen in figure 1-104 that $\mathrm{R}_{\mathrm{e}}$ does not increase nearly as rapidly as does $\mathrm{X}_{\mathrm{e}}$, except in the region of $f_{\mathbf{n}}$. With $C_{x}=32 \mu \mu f, \Delta f_{r x}\left(=f_{r x}-f_{s}\right)$ will be 2.1 kc for the crystal unit of figure 1-104, and $R_{e}$ will be between 11 and 12 ohms.

## MEASUREMENT OF CRYSTAL PARAMETERS

1-218. The parameters $L, C, R$, and $C_{0}$ of any crystal unit chosen at random are effectively four independent variables, so that a minimum of four measurements are required to determine the values of these variables. Probably the four easiest measurements to make are those for $f_{r}, K, C_{v}$, and $\mathrm{f}_{\mathrm{rx}}$. The measurement for the last quantity is made when a known load capacitance $C_{x}$ is connected in series with the crystal unit. Since $f_{r x}$, the resonant frequency of the crystal and $C_{x}$ in series, for all practical purposes will be equal to the $f_{p}$ of the crystal in parallel with $\mathrm{C}_{\mathrm{x}}$, we shall normally not make a distinction between the two frequencies in the following discussion, but shall use the symbol " $\mathrm{f}_{\mathrm{p}}$ " in referring to either.

## Measurement of the Shunt Capacitance, $\mathbf{C}_{\text {。 }}$

1-219. At all frequencies sufficiently removed from resonance the crystal unit will have the characteristics of a capacitance equal to $\mathrm{C}_{0}$. Thus, at these off-resonance frequencies, $\mathrm{C}_{0}$ can be measured by a conventional $Q$ meter or an r-f bridge. The frequency at which $\mathrm{C}_{0}$ is to be measured should be lower than, but reasonably close to, the operating frequency, particularly if the crystal unit is to be operated at a high harmonic mode in the v-h-f range. Otherwise, the effect of the distributed inductance of the leads will not be properly taken into account.

Measurement of the Series-Arm Resisfonce, R
$1-220 . R$ is normally measured with the aid of a CI meter (crystal impedance meter). (See also paragraphs 2-60 through 2-65.) There are four standard CI meters with which the crystal units described in Section II of this handbook have been tested:

| Crystal Impedance | Frequency Range |
| :---: | :---: |
| Meter | (ke/sec) |

* (Crystal Impedance Meter TS-537/TSM may soon be replaced entirely by the recently developed

Crystal Impedance Meter TS-710( )/TSM.) A CI meter is essentially an r-f oscillator provided with a feedback circuit in which a crystal unit or a resistor, or a crystal unit in series with a calibrated capacitor, can be connected. A simplified schematic diagram of a typical CI meter is shown in figure 1-106. The circuit shown is a modified Colpitts oscillator in which the tank inductor has been effectively divided into two equal sections, $\mathrm{L}_{\mathrm{t}}$ and $L_{2}$, between which a resistor, $R_{0}$, equal to $R_{e}$, the effective resistance of the crystal unit, can be connected. The ganged tuning capacitors $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ are at all times equal. $\mathrm{C}_{\mathrm{H}}$ is simply a blocking capacitor to isolate the plate voltage from the crystal terminals, and adds only a negligible reactance to the tuned circuit. The potentiometer, P , is used to control the screen grid voltage, and hence the $r$-f output of the tube and the drive level of the crystal. With $S_{1}$ connected as shown, and $R_{0}$ adjusted to a value typical of the motional- $\varepsilon: m$. $R$ for the type of crystal unit being measured, the circuit will oscillate at approximately the resonant frequency of the tank. If $C_{1}$ and $C_{2}$ are adjusted so that the natural frequency of the oscillator is near the nominal frequency of the crystal, then, on connecting the crystal into the circuit, oscillations will continue, but with the frequency determined


Figure 1-106. Simplified schematic diagram of CI meter

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by the total reactance of the tank, including $X_{e}$ of the crystal unit. There is no standard practice as to grounding the crystal holder; but whether grounded or ungrounded, the method of connecting the crystal unit should be noted. The drive is adjusted so that a very small grid current is indicated on $\mathrm{M}_{1}$. Under these conditions the control grid is positive with respect to the cathode only at the peaks of the positive swings of the excitation yoltage developed across $\mathrm{C}_{1}$. Since electrons flow from cathode to grid only at these instants, a small percentage change in the excitation voltage, as illustrated in figure 1-107 can cause a very large percentage change in the cathode-to-grid electron flow. In an actual circuit the idealized constant bias that is indicated in figure 1-107 does not occur because of the gridleak action. However, if the gridleak contribution to the bias is very small compared with that part developed across the cathode resistance, the increase in bias due to an increase in excitation occurs almost entirely across $\mathrm{R}_{\mathrm{g}}$, not across the cathode resistance. Hence, a five or ten per cent increase in the total bias can result from hundred per cent increase in the gridleak IR drop. In this way, the grid current meter is a very sensitive indicator of slight changes in the r-f voltage across $C_{1}$, and hence of any change in the tank current. With $S_{1}$ in the crystal position and $S_{2}$ closed, as $C_{1}$ and $C_{2}$ are varied, a peak in the grid-current reading indicates
a maximum current through $\mathrm{C}_{1}$. This in turn means that the effective resistance of the crystal unit has reached the minimum value equal to the series-arm R. In other words, the oscillator frequency is coinciding with the resonant frequency, $f_{r}$, of the crystal unit. $R_{o}$ can now replace the crystal in the circuit and be adjusted to give the same meter readings at the same frequency. At this point $R_{0}$ will equal $R$, and, since $R_{0}$ is known, $R$ will have been measured. The crystal current meter, $\mathrm{M}_{2}$, is not sufficiently sensitive to permit an accurate observation of the small changes in tank current that occur as the circuit is tuned through $\mathrm{f}_{\mathrm{r}}$. The purpose of the meter is to decrease the possibility of overloading the crystal and to provide a ready means for determining the exact drive level at which the crystal is being tested. Since the crystal parameters may change with the drive, it is necessary to specify the drive level at which the measurements are made. Expressed in milliwatts, the drive level equals $I^{2} R \times 10^{-3}$, where $I$ (in milliamperes) is the current through $M_{2}$ at $f_{r}$. If a crystal-current meter is not supplied, two vac-uum-tube voltmeters can be used to measure the voltage from each crystal terminal to ground without seriously affecting the circuit. Where E is the difference in potential across the crystal, equal to the difference between the two terminal voltages, the drive level is equal to $\mathrm{E}^{2} / \mathrm{R}$. The temperature at which the measurements are made should also

figure 1-107. How a small percentage change in excitation voltage can cause a large percentage change in grid-leak current of Ct meter. Bias does not actually remain constant as indicated, but follows the percentage changes of excitation valtage. Nevertheless, the relative percentage variations of grid current and excitation voltage can be approximately as shown when the greater part of the bias
is developed across the cathode resistance
be specified, although, in general, the variation of $\mathbf{R}$ with ambient temperature is much less than its variation with the amplitude of the crystal vibrations.

## Measurement of the Resonance Frequency, $f_{r}$

1-221. To measure $f_{r}$ a c-w radio receiver, a radiofrequency standard, a calibrated audio-frequency source (interpolation oscillator), and either a loudspeaker, a pair of ear phones, or an oscilloscope are used in conjunction with the CI meter. With the crystal connected in the CI-meter circuit and the oscillator tuned to series resonance, the r-f output can be loosely coupled through a coaxial cable to the antenna post of the c -w radio receiver. After the receiver is tuned to the frequency of the crystal unit, the CI meter is turned off, and the receiver is connected and tuned to receive the particular harmonic of the frequency standard that is nearest to $f_{r}$. The bfo of the receiver is then cut off, and the CI meter is turned on. With both the standard and the CI-meter signals being fed to the receiver input, the output of the receiver will be an audio beat note equal to the difference between the known standard frequency and the unknown crystal frequency. By momentarily switching a fairly large value of $\mathrm{C}_{x}$ in series with the crystal, so that the CI-meter frequency increases slightly, the audio beat frequency will rise or fall according to whether $f_{r}$ is respectively greater than or less than the standard signal. The audio beat frequency is next mixed with the audio output of the interpolation oscillator, which in turn is adjusted to bring the beat frequency of the two audio signals to zero-the zero beat being observed by phones, loudspeaker, or oscilloscope. At zero beat, the crystal frequency will have been measured to be equal to the selected r-f standard frequency $\pm$ the interpolation oscillator frequency. The accuracy of the measurement depends primarily upon the accuracy of the frequency standard, and secondarily on that of the interpolation oscillator. As in the case of the resistance measurement, both the temperature and the drive level should be specified, and these should be the same as when the measurement of $R$ was made.

## Measurement of the Parallel-Resonance Frequency, $f_{\text {, }}$

1-222. To measure $f_{\mathrm{r}}$, it is first necessary to adjust the CI meter to oscillate at $f_{r}$, by the same steps employed previously. With the oscillator so adjusted, a known value of $\mathrm{C}_{\mathrm{x}}$ is switched in series with the crystal. The new frequency will be approximately equal to $f_{p}$. The more common values
of $C_{x}$ are $32 \mu \mu \mathrm{f}$ for high-frequency crystals, and $20 \mu \mu \mathrm{f}$ for low-frequency crystals. In testing to determine whether the crystal frequency is above or below the frequency of the test standard, it may be more convenient to add capacitance across the crystal unit than to change the setting of $\mathrm{C}_{\mathrm{x}}$. In this event the CI-meter frequency is decreased rather than increased, so that the effect on the beat note will be the opposite of that previously described. Simply touching the crystal holder with the hand is normally the quickest method of increasing the shunt capacitance; however, care should be taken that the method employed does not effectively decrease the capacitance by grounding the holder.
1-223. Theoretically, the foregoing method of measuring $f_{p}$ is not exact, for if the LC circuit is correctly tuned when the crystal appears as a pure resistance, the same feed-back phase relations cannot hold at the higher frequency, $f_{p}$, unless $C R$ and $C_{x}$ in series introduce a negative reactance to compensate for the increase in $\mathrm{X}_{\mathrm{L},}$ and $\mathrm{X}_{\mathrm{L}, 2}$ and the decrease in $\mathrm{X}_{\mathrm{C}_{1}}$ and $\mathrm{X}_{\mathrm{C}_{2}}$. In other words, $\mathbf{X}_{e}$ of the crystal unit is approximately, but not exactly, equal in magnitude to $X_{x}$ of the load capacitance. Actually, $X_{e}$ is less than $X_{x} \mid$ by an amount approximately equal to the change in reactance around the LC loop, exclusive of CR and $\mathrm{C}_{\mathrm{x}}$. This change is approximately equal to $4 \pi\left(\mathrm{~L}_{1}+\mathrm{L}_{2}\right) \Delta \mathrm{f}_{\mathrm{p}}$, where $\Delta f_{p}$ is the difference between $f_{p}$ and $f_{r}$. At the true $f_{r x}, X_{e}+X_{x}=0$; at the observed $f_{p}$,

$$
\begin{equation*}
\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{x}}+4 \pi\left(\mathrm{~L}_{\mathrm{p}}+\mathrm{L}_{2}\right) \Delta f_{\mathrm{p}}=0 \tag{1}
\end{equation*}
$$

Now a small change in $X_{c}+X_{x}$, equal to $\Delta X_{e}+$ $\Delta X_{x}$, as a result of a small change in frequency, is practically equal to $\Delta X_{e}$ alone. If the frequency is sufficiently close to the resonant point, $f_{r}$, we may set $\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{x}}\left(\right.$ at observed $\left.\mathrm{f}_{\mathrm{p}}\right)=\Delta\left(\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{s}}\right)$ $\approx \Delta X_{p} \approx \Delta X_{n}=4 \pi L \Delta f$, where $\Delta f=$ observed $f_{p}$ - true $f_{r x}$. By substitution in equation (1)

True $f_{r x}=$ Observed $f_{p}+\left(\frac{L_{1}+L_{2}}{L}\right) \Delta f_{p}$

## Measurement of the Effective Resistance, $\mathbf{R e c}_{\text {et }}$ at Parallel Resonance

1-224. In the measurement of $f_{p}$, the drive level and the temperature should be the same as in the measurement of $R$ and $f_{r}$. To determine the drive level, either the voltage across the crystal unit, or

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the effective resistance $R_{e}$ should be known-or both, if a crystal-current meter is not provided. A measurement of $R_{e}$ is also important for its own sake and as a check to see whether the motionalarm parameters are the same at $f_{p}$ as at $f_{r}$. In the case of a crystal unit which is intended to be operated only at parallel resonance, $\mathbf{R}_{\mathrm{e}}$ is generally treated as a primary parameter of more immediate importance than the motional-arm R. $R_{e}$ is measured in a manner similar to the measurement of $R$, except that on substituting $R_{0}$ for the crystal the circuit must be retuned so that oscillations are being maintained at $f_{p}$. For a very precise drivelevel measurement, additional precautions must be taken if the power dissipation is to be the same in both the series- and parallel-resonant measurements. The best assurance that the $f_{r}$ and $f_{p}$ drive levels will not be greatly different is to be had when the crystal current is kept near the minimum necessary to maintain oscillations. Thus, even though the relative differences in drive level may be large, the absolute differences will be small. This is not a completely reliable method, for some crystal units exhibit very sharp increases in resistance when the drive level approaches a minimum.

## Computing the Series-Arm C and L from the Measured Parameters

1-225. From the formulas for $f_{r}, X_{e}$, and $X_{x}$, it is quite easy to derive the following approximate equations for the series-arm parameters, C and L :

$$
\begin{align*}
& \mathrm{C}=\frac{2\left(\mathrm{C}_{\mathrm{o}}+\mathrm{C}_{\mathrm{x}}\right) \Delta \mathrm{f}_{\mathrm{p}}}{\mathrm{f}_{\mathrm{r}}}  \tag{1}\\
& \mathrm{~L}=\frac{1}{\left(2 \pi \mathrm{f}_{\mathrm{r}}\right)^{2} \mathrm{C}} \tag{2}
\end{align*}
$$

where, $C, C_{0}$, and $C_{x}$ are in farads, $L$ is in henries, and $\Delta f_{v}$ and $f_{r}$ are in cps.

## METHODS FOR EXPRESSING THE EELATIVE PERFORMANCE CHARACTERISTICS OF A CRYSTAL UNIT

1-226. If the four equivalent electrical parameters ( $L, C, R, C_{0}$ ) are accurately known for a given state of operation, no other independent data concerning a crystal unit can increase the radio engineer's knowledge of how the crystal will perform under the given conditions. However, the radio engineer has been slow in requesting specific information concerning the electrical characteristics of the crystal units available, and as a result the problem of making a given circuit perform correctly
has often in the past effectively become the responsibility of the crystal manufacturer, who, by cut-and-try methods, has been more or less required to design the crystal unit around the particular circuit. Fortunately, progress toward greater standardization of crystal units has been considerably accelerated during recent years because of the increased demands of the military services; but there is still a tendency on the part of the design engineer to regard a crystal unit, as one production engineer has expressed it, as a "mystery box," rather than the equivalent circuit that it is. Contributing to this tendency has been a hesitancy upon the part of the manufacturer to describe his crystal units in terms of the most probable equivalent electrical parameters. At the present state of the art, wide variations from the most probable values can occur, and the manufacturer quite naturally wishes to avoid the chance that typical values of the parameters will be misinterpreted as specified values. For similar reasons, a description of a crystal unit in terms of its most probable parameters is not at present desirable from the point of view of the military services, lest a crystal circuit be designed upon the assumption that the typical crystal parameters will always be available, rather than upon the assumption that the crystal unit cannot be depended upon to meet other than its minimum performance specifications. If the former, rather than the latter assumption were made, a carefully designed circuit might fail to operate properly if used with a borderline crystal unit. Thus, the purpose of the standardization of types-to ensure a complete interchangeability among the crystal units of the same type number and nominal frequency - would be defeated. Nevertheless, the lack of emphasis upon the basic parameters has served to cloak the crystal in an air of mystery, and to instill in the radio engineer an impression that a crystal circuit is possessed of properties that cannot be expressed in the normal idiom of LCR networks. Contributing somewhat to this point of view is the special terminology that has been developed for the purpose of comparing the performance characteristics of one crystal unit with those of another particularly where the definitions of the terms contain certain ambiguities or conditional interpretations, or are presented as mathematical relationships without concrete qualitative meanings. What may be implied as a property of the crystal unit alone, may well be a function of the particular circuit in which the crystal unit is mounted. Much of the difficulty can be avoided if it is kept in mind that a crystal unit has no important circuit performance
qualities that cannot be expressed in the everyday terminology of radio engineering as it might apply if the crystal unit were replaced by an equivalent network of $L, C, R$, and $C_{0}$.
1-227. There are five general categories in which crystal units can be placed for comparison insofar as their relative merits are reflected by their performance in a standard test-oscillator circuit: (1) activity, (2) frequency stabilization, (3) bandwidth, (4) quality factor, and (5) parameter stability. Activity, as applied to a crystal, is a general term, rather loosely defined, that refers to the relative ease with which a crystal may be caused to maintain oscillations. The basic parameter most closely associated with the crystal activity is the motional-arm resistance, R. Besides R, or $R_{e}$, there are certain performance parameters that can be used as indices of relative activity quality. These are the effective $Q\left(Q_{e}\right)$, the maximum effective $Q\left(Q_{\mathrm{em}}\right)$, the figure of merit (M), and the performance index (PI). The term, frequency stabilization, as used in this context, refers only to the ability of a crystal to minimize any change in the frequency due to variations in the parameters of the external circuit. In this sense, those performance parameters that can be used as indices of the frequency-stabilization quality are the series-arm $\mathrm{L} / \mathrm{C}$ ratio, the coefficient of frequency stability ( $\mathrm{F}_{\mathrm{X}}$ ), and the capacit*nce ratios $\mathrm{C}_{\mathrm{T}} / \mathrm{C}$ and $\mathrm{C}_{\mathrm{T}} / \mathrm{C}_{\mathrm{X}}$. The bandwidth of a crystal unit refers to the frequency range over which the crystal unit is considered operable. The performance parameters indicating this quality are the capacitance ratio, $\mathrm{r}=\mathrm{C}_{0} / \mathrm{C}$, and the electromechanical coupling factor, k . The quality factor is simply the crystal Q , which is, itself, a major performance parameter, but one that is not exclusively identified with any one of the other four performance categories. The term parameter stability is used here to refer to the relative stability of the crystal parameters during changes in the temperature, drive level, tuning adjustments, and the like. The frequency stability of the crystal unit, which is included in this category, should not be confused with the function of frequency stabilization which is the characteristic we have arbitrarily assigned to the second performance category. The frequency stabilization is dependent upon the magnitudes of the equivalent-circuit parameters; whereas, the frequency stability is dependent upon the stability of the equivalent-circuit parameters. The stability of a crystal oscillator circuit is dependent upon both the crystal stabilization and the parameter stability. Performance indices or terms indicating the relative parameter stabilities are represented by
the temperature coefficients of frequency and resistance, drive-level coefficients of frequency and resistance, frequency tolerance, frequency deviation, resistance deviation, relative freedom from unwanted modes, and general expressions indicating durability and aging characteristics. Since most of the characteristics identified with the five performance categories can be expressed as functions of the same basic equivalent-circuit parameters, a performance parameter in one category quite often serves as an indication of the crystal quality in another. It cannot be said that those properties most closely identified with the activity, for instance, are not also related to the frequency stabilizing effect. Nevertheless, classifying the various methods for rating the performance of a crystal unit is helpful in interpreting the different performance parameters in terms of the basic equivalent-circuit parameters.

## Activity Quality of Crystal Unit

1-228. The "activity" of a crystal oscillator is a qualitative expression referring to the amplitude of the oscillations. It is a term that came into use during the early days of crystal resonators, but one that seems never to have been vigorously defined. For example, it is not always certain whether the "activity of an oscillator" is intended to refer to the amplitude of current in the feedback, or in the output circuit, or to the voltage across some particular circuit component, or to the output power, or to the excitation power, or to the ratio of these powers, or simply to the amplitude of the crystal's mechanical vibrations. Were' the expression not already so strongly entrenched in the crystal terminology, its use would probably be discouraged. As it is, crystal units are commonly described as having high or low activities, or more specifically, as having high or low potential activities or activity qualities. It will be found that the crystal parameter most directly indicative of the activity quality is the motional-arm conductance, $1 / R$. In crystal oscillators employing gridleak bias, when one crystal is replaced by another of the same nominal frequency, one of the crystals is usually found to produce stronger excitations and hence a larger grid current under similar operating conditions. Frequently the relative grid currents are defined to be equal to the relative activities of the crystals. With this method of measurement it can be seen that, if a crystal is connected directly across the grid-to-cathode input the excitation, and hence the activity, will depend upon the amplitude of the r-f voltage across the crystal. On the other hand, if the crystal is con-

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nected in series with the oscillator input, the activity will depend upon the amplitude of the current through the crystal unit. Since, in any event, the grid current depends upon the values of every parameter in the oscillator circuit, such a measurement is ambiguous unless a standard test circuit can be referred to for each frequency. Only in this way can the crystal unit, itself, be considered the only significant variable. Even under the assumption of ideal test conditions, however, the exact mathematical relationship among the crystal parameters, which provides the most direct measure of a crystal unit's inherent activity quality, has been a subject of some controversy. A number of suggestions have been made, but the usefulness of each of these depends considerably upon the method by which the crystal is to be used to control oscillations. As the crystal terminology becomes more rigorously defired we can imagine that the word "activity" will fall into disuse eventually, with "effective resonance resistance" or "conductance" taking its place.

## aCTIVITY QUALITY FOR SERIES RESONANCE

1-229. As an example of series-mode operation, we refer to the test circuit in figure 1-106. It can be seen that the grid excitation will be approximately equal to $\mathrm{IX}_{\mathrm{c}}$, the r-f voltage developed across $C_{1} . X_{C_{1}}$ depends upon the frequency and the value of $C_{3}$, whereas, $I$, the current through $C_{1}$ depends upon the $\mathrm{B}^{+}$voltage, the setting of P , the tube characteristics, etc., as well as the tank impedance and hence the resistance of the crystal. With all the circuit parameters constant, the only variable that the crystal introduces at resonance is its resistance R. Rather than specify all the parameters of the test circuit for each nominal frequency, it is clear that the measurements of $R$ provide sufficient indication of the relative activities of different crystal units under any similar conditions of resonance. Since the current and voltage amplitudes vary inversely with $R$, the series-resonance activity of any crystal unit can be assumed to be directly proportional to $1 / \mathrm{R}$, the motional-arm conductance.

## ACTIVITY QUALITY FOR PARALLEL RESONANCE

1-230. The interpretation of the activity quality of a crystal unit becomes more complicated when the crystal is to be operated at parallel resonance. But even as in the case of series resonance, the inherent property of the crystal unit that most readily indicates the relative activity is the motional-arm
conductance, $1 / \mathrm{R}$. In a parallel-resonant oscillator circuit, the excitation is normally directly proportional to the voltage developed across the crystal in parallel with its effective load capacitance $C_{x}$. This voltage in turn is proportional to $Z_{p} \approx X_{T}{ }^{2} / R$, where $Z_{p}$ is the parallel-resonance impedance, $X_{T}$ is the reactance of $\mathrm{C}_{\mathrm{T}}$, the total shunt capacitance, and $R$ is the series-arm resistance. As long as $\mathbf{X}_{\mathbf{T}}$ remains constant, the only significant crystal variable that affects the activity is R , or more directly $1 / \mathrm{R}$. A complication arises from the fact that $C_{T}=C_{0}+C_{x}$, so that if $C_{x}$, the effective capacity of the external circuit is to be held constant, then $X_{T}$, and hence the activity, changes with $C_{0}$. Another complication arises when a measure of crystal quality is desired that will hold between crystals of different nominal frequency. If $C_{T}$ or $C_{x}$ is to be held constant, then $Z_{p}$ tends to vary inversely with the square of the frequency. Finally, the complications are multiplied several fold when one begins to take into account the many ways in which a crystal can be connected to stabilize or to control a parallel-resonant type of circuit. Unless the term "activity" is to refer to some desired and well-defined end result that can be measured quantitatively, the word may have little practical meaning. With this in mind, we note that since the usefulness of the oscillator depends entirely upon its output, the useful oscillator activity can be said to concern only the amplitude of oscillations in the load circuit. Thus, the relative ease with which a crystal unit enables a given output to be achieved under specified conditions can be regarded as the relative activity quality of the crystal unit. From this point of view, the relative activity of a crystal unit can be considered inversely proportional to the driving power that the crystal requires in order to maintain a given output level in a fixed load. Now, there is a special case of parallel-mode operation-where the series arm operates into a constant $C_{T}$ for which the activity, as interpreted above, requires only a measurement of R . Assume that a small, variable shunt capacitance, $C_{v}$, can be connected directly across each crystal unit whose activity quality is being tested, so that the effective shunt capacitance (eff $\mathrm{C}_{0}=\mathrm{C}_{0}+\mathrm{C}_{\mathrm{v}}$ ) can be adjusted to give the same value for all crystals. With this arrangement, the crystal power dissipation for a given power output will vary positively with the mo-tional-arm resistance, R. In other words, two crystal units of the same series-resonance frequency and the same motional-arm resistance can produce the same oscillator activity at the same parallelresonance frequency regardless of the particular
values of $\mathrm{C}_{0}$, or of the motional-arm C and L , but only if a variable shunt capacitor is provided by which the effective $C_{0}$ can be held constant. Thus, for gauging the potential activity of a particular crystal unit to be used in any parallel-mode oscillator circuit having a variable capacitor connected directly across the terminals of the crystal unit, the motional-arm conductance, $1 / R$, can usually be considered a.sufficient and proper activity parameter.
1-231. Where the load capacitance, $C_{x}$, that the entire crystal unit faces (not necessarily $C_{T}=$ $\mathrm{C}_{0}+\mathrm{C}_{\mathrm{x}}$ that the series arm faces) is to remain constant, the parameter $1 / R$ is not a sufficient index of the activity quality. If the proper measure of crystal activity is defined to be the ratio of output power to crystal power, such a definition is general enough to be applicable for any type of crystal oscillator. Certainly, the crystal unit that requires the least expenditure of energy to perform its task should be considered the one of greatest activity. Unfortunately, activity quality, from the point of view of a power ratio, becomes a function of each particular oscillator and load circuit, so that the generalization gained in the definition is completely lost on application, unless a standard test oscillator is available for each type of circuit. Only when the crystal unit is operated at its series-resonant frequency or is connected directly in parallel with a variable capacitor, can the relative activity qualities of two or more crystal units be considered constant and independent of the particular design of the external circuit. In all other cases, $C_{0}$, as well as $R$, becomes a significant parameter of the activity, and the exact relation of $C_{e}$ to the activity will depend upon the circuit design. For a parallel-mode activity parameter to apply in the general case, the oscillator circuit, itself, must be considered from a generalized point of view. By this approach, the effective $\mathbf{Q}\left(Q_{e}=\frac{X_{e}}{\mathbf{R}_{e}}\right)$ is often considered a more reliable activity quality factor, than $1 / R$ alone. The reason for this belief is most readily indicated when a generalized crystal oscillator is represented by the negative-resistance method - in particular, by diagrams ( $A$ ), ( $B$ ), and (C) in figure 1-108.

## Q. AS AN INDEX OF ACTIVITY QUALITY

1-232. If the oscillations of a crystal are to be sustained, energy must be supplied at a rate equal to the power losses in the crystal. This state is indicated in figure 1-108 (A), where the power source is represented as a generator with an emf equal,
but opposite in sign, to the voltage across the effective resistance of the crystal unit. The power input thus is $\left|E I_{r}\right|=I_{c}{ }^{2} R_{e}$. Furthermore, since the total voltage drop around the circuit must be zero, the external circuit must appear as having a reactance equal, but opposite in sign, to the effective reactance of the crystal. Now, since the current through each component of the equivalent series circuit is the same, the voltage may be represented as being the result of a current flowing through a circuit of zero total impedance, as shown in figure 1-108 (B). Note that the generator is replaced by a negative resistance, $\rho_{\mathrm{H}}$, numerically equal to $\mathrm{R}_{\text {. }}$. Figure 1-108 (C) shows the same operating conditions, but with $X_{1}$ and $\rho_{x}$ of the external circuit replaced by an equivalent capacitive reactance, $X_{x}$, in parallel with a negative resistance, $p$, equal to $-Z_{p}$, where $Z_{p}=\frac{X_{e}{ }^{2}}{R_{e}} \approx \frac{\mathbf{X}_{\mathrm{x}}{ }^{2}}{\mathbf{R}_{\mathrm{c}}}$. At all instants the impedance across the terminals at 1 and 2 , whether that of the crystal unit or of the external circuit, is the same for both the (B) and the (C) equivalent circuits. Imagine now that after equilibrium has been reached, $\mathrm{R}_{\mathrm{c}}$ suddenly decreases by one half. At this instant the power being supplied, $\mathrm{I}_{\mathrm{c}}{ }^{2} \rho_{\mathrm{n}}=\mathrm{I}^{2}{ }^{2}$, is greater than that being dissipated in $R_{e}$. In (B), the amplitude of oscillations will increase until a new equilibrium is reached, at which time $\rho_{\mathrm{s}}$ will also have decreased by one half and will be once again numerically equal to $R_{e}$ In ( $C$ ), the halving of $R_{c}$ means that $Z_{p}$ is approximately doubled. The same increase in current through $\mathrm{R}_{\mathrm{e}}$ must be shown to occur in (C) as in (B). Thus, the amplitude of the oscillations must increase until $p$ has doubled its value and is again numerically equal to $Z_{p}$. (The changes in $\rho$ are caused by the limiting elements in the oscillator. For example, $\mathrm{R}_{\mathrm{p}}$ of the vacuum tube will increase with an increase in gridleak bias, and this will be reflected as an increase in $\rho$.) From the generalized circuit approach, we can reach the general conclusion intuitively that oscillations build up as long as $\left|p_{x}\right|>R_{\text {s }}$, or $|\boldsymbol{p}|<Z_{1}$, and that oscillations diminish in amplitude under the reverse conditions. It may not be at once apparent why oscillations should not build up if $\rho$ were numerically larger than $Z_{p}$, in the same way that they do when $\rho_{\mathrm{s}}$ is greater numerically than $\mathrm{R}_{0}$. A rigorous proof can be obtained by a differential equation of the current through the inductance, applying Kirchoff's laws and keeping in mind that resistance, negative or positive, is mathematically an instantaneous rate of change of voltage with current. Qualitatively it can be seen that the amplitude increases or decreases, depending upon


Figure i-108. Generalized crystal oseillator circuit
whether the ratio of the power input to the power dissipation is, respectively, greater or less than 1. For circuit (B) the current, $I_{c}$, is the same for both the crystal unit and $\rho_{\mathrm{s}}$, so that the power ratio is :

$$
\begin{equation*}
\left|\frac{I_{c}^{2}}{} \rho_{\mathrm{s}}\right|=\left|\frac{\rho_{\mathrm{a}}}{\mathrm{R}_{\mathrm{e}}{ }^{2} \mathrm{R}_{\mathrm{e}}}\right| \tag{1}
\end{equation*}
$$

Oscillations thus build up as long as $\rho_{\mathrm{p}}$ is greater than $R_{e}$. For circuit ( $C$ ) the voltage, $E_{o}$, is the same across the crystal unit as across $\rho$, so that the power ratio is:

$$
\frac{\mathrm{E}_{0}^{2} / \rho}{\mathrm{R}_{\mathrm{o}} \mathrm{E}_{\mathrm{o}}{ }^{2} / \mathrm{Z}_{\mathrm{e}}{ }^{2}}=\left|\frac{\mathrm{Z}_{\mathrm{p}}}{\rho}\right|
$$

where $Z_{0}=\sqrt{R_{0}{ }^{2}+X_{0}{ }^{2}}$ and $X_{e} \gg R_{\text {e }}$

1-232 (2)
Oscillations thus build up as long as $\rho$ is less than $Z_{p}$, the equivalent parallel-resonance impedance at
equilibrium. The initial values of $p_{k}$ and $\rho$ for a given frequency can be assumed to be fixed parameters characteristic of the particular oscillator circuit, although the exact magnitudes may be extremely complicated functions involving all the circuit variables. Nevertheless, it is reasonable to assume that the more the negative resistance must change, the greater will be the activity of the oscillator by the time equilibrium is reached. From the point of view of circuit (B), it would seem that with a given initial $\rho_{a}$ maximum activity is to be obtained with a minimum $R_{e}$; but in circuit (C), on starting with a given value of $\rho$, maximum activity is to be obtained with a maximum $Z_{1}$. Note that these two conditions are not entirely equivalent. For a given crystal unit, $Z_{p}$, for instance, can be increased by increasing $X_{x}$, which in turn requires that $R_{e}$, as well as $X_{e}$, become greater. (Since $X_{p}$ must increase to match the increase in $X_{x}$, so must the frequency, and hence also $R_{e}$.) Remembering that the activity that is assumed to
be proportional to the change in negative resistance is that in the oscillator output and is not necessarily the current amplitude in the crystal circuit, it can be seen that $R_{e}$ alone, in spite of the implications to be drawn from figure 1-108 (B), may not be a sufficient parameter to indicate the relative activity quality of a crystal unit in the general case, i.e., $\mathrm{X}_{\mathrm{e}}$ must also be considered. For these reasons, the effective $Q$ of the crystal unit, $\mathbf{Q}_{\mathrm{e}}=\mathrm{X}_{\mathrm{e}} / \mathrm{R}_{\mathrm{e}}$, is usually considered the more reliable index of the crystal activity quality for parallelresonant oscillators. There are exceptions, however, where $R_{e}$ or rather $\frac{1}{R_{b}}$, is the proper activity parameter. These occur when the crystal is actually operated at series resonance with an external capacitance. An example is the Cl -meter circuit in figure 1-106, when $\mathrm{C}_{\boldsymbol{x}}$ is connected in series with the crystal. (See paragraph 1-585 for a more detailed analysis of negative-resistance limiting.)
1-233. The crystal $Q_{e}$ is a more direct index of the potential activity in some oscillator circuits than in others. The first consideration is the effect that a change in $Q_{e}$ has upon the excitation voltage. Normally, an increase in $Q_{e}$ means an increase in excitation, but this is not true in every case, even in the conventional parallel-resonant circuits. In these oscillators, the feed-back network may consist of a crystal unit shunted by one capacitance and in series with another. Referring to figure 1-109, assume at first that the capacitance, $\mathrm{C}_{n}$, shunting the crystal unit in both (A) and (B) is negligible. The generalized circuits are thus equivalent to that of figure 1-108 (B). $\mathrm{X}_{1}$ of figure 1-108 (B) is represented by ( $\mathrm{X}_{\mathrm{it}}+\mathrm{X}_{1 \mathrm{~b}}$ ) and by ( $\mathrm{X}_{1 \mathrm{c}}+\mathrm{X}_{16}$ ) in circuits (A) and (B), respectively, of figure 1-109. Referring now to figure 1-109 only, the crystal unit in circuit (A) is connected between the control grid and cathode, so that the principal activity consideration is to obtain the desired excitation voltage across the crystal unit with a minimum power dissipation in the crystal unit. Similarly, in circuit (B), the higher the crystal quality, the less the crystal power that would be required to obtain a desired excitation voltage across $\mathrm{X}_{1 \mathrm{c}}$. As a first approximation, assume that $X_{e}$ is much greater than $\mathrm{R}_{\mathrm{e}}$, so that the voltage across the crystal unit can be assumed to equal $I_{k} X_{k}$, where $I_{k}$ is the feed-back current and where $1_{k} X_{c}$, is $180^{\circ}$ out of phase with the voltage across the series reactance, $\mathrm{X}_{10}$ or $\mathrm{X}_{10}$, as the case may be. In circuit (A), the excitation voltage is thus equal to $I_{s} X_{e}$, and the crystal power dissipation is $1_{k}{ }^{2} R_{e}$. If the ratio of the r-f output voltage of the tube to the excitation voltage, $\mathrm{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{z}}$, is assumed
to be k , then the ratio of the output voltage to the crystal power, $\mathrm{P}_{\mathrm{c}}$, is:

$$
\frac{\mathrm{E}_{\mathrm{p}}}{P_{\mathrm{e}}}=\frac{\mathrm{kI} \mathrm{I}_{\mathrm{k}}}{\mathrm{I}_{\mathrm{g}}{ }^{2} \mathrm{R}_{\mathrm{e}}}=\frac{\mathrm{k} \mathrm{Q}_{\mathrm{e}}}{\mathrm{I}_{\mathrm{g}}}
$$

Circuit (A)
(figure 1-109)
The magnitude of the total impedance of the feedback circuit must be $\mathrm{kZ} \mathrm{Z}_{\mathrm{g}}$, where $\mathbf{Z}_{\mathrm{g}}$ is the grid-tocathode impedance. As long as it can be assumed that the impedance of the crystal unit is $180^{\circ}$ out of phase with the reactance of the series capacitance, then the magnitude of the plate-to-grid impedance must be approximately $(k+1) Z_{\mathrm{g}}$. Thus, in circuit $(B),\left|X_{2 c}\right| \approx \frac{X_{s}}{k+1}$. Substituting this value of $X_{X_{c}}$ in place of $X_{e}$ in the equation above:

$$
\frac{E_{\mathrm{p}}}{P_{c}}=\frac{k Q_{e}}{(k+1) I_{g}} \quad \begin{aligned}
& \text { Circuit (B) } \\
& \text { (figure } 1-109)
\end{aligned}
$$


(A)
gRIO-TO-CATMODE CAYSTAL CONNECTION


PLATE-TO-GRIO CRYSTAL CONNECTION
Figure 1-109. Genoralized crystal oscillator sircuits, showing two conventional mathods for connecting crystal unit ( $X_{c,}, R_{f}$ ) in teed-back circuit

## Electrical Parameters of Crystal Units

The equations for circuits (A) and (B) show that for a given $k$ and a given crystal current, a maximum ratio of $\mathrm{E}_{\mathrm{p}} / \mathrm{P}_{\mathrm{e}}$ is to be obtained when $\mathrm{Q}_{\mathrm{e}}$ is a maximum. This assumes that the circuit capacitance, $\mathrm{C}_{r}$, directly shunting the crystal unit is negligible. When this assumption cannot be made, the effective $Q$ of the parallel combination must be substituted for $Q_{e}$. The $Q$ of the combination is approximately equal to $Q_{e}\left(\frac{X_{v}+X_{e}}{X_{v}}\right)$ as long as ( $X_{v}+X_{e}$ ) is numerically large compared with $R_{e}, X_{v}$ being the negative reactance of $C_{v}$. The larger the magnitude of the ratio $X_{v} / X_{e}$, the more directly does $Q_{e}$ become the principal activity index. It should be remembered that the direct proportionality between $Q_{\text {e }}$ and the activity in the example above holds only upon the assumption that $I_{5}$ is to be held constant, regardless of the value of $Q_{\text {. }}$. Another instance in which the activity of an oscillator is a direct function of $Q_{e}$ would be the unconventional case of an oscillator so designed that the crystal unit is operated in series resonance with an external capacitance and with the excitation voltage equal to, or directly proportional to, the voltage across either the crystal unit or the series reactance. In such a circuit, use would be made of the resonant rise in voltage that is developed when a component impedance is greater in magnitude than the total impedance. Since the current through the component is the same as that through the total impedance, the step-up voltage ratio is the same as the impedance ratio. At series resonance the total impedance of the crystal circuit would equal $\mathrm{R}_{\mathrm{e}}$ (assuming no other resistance in the circuit), so that if $Z_{e}$ of the crystal unit were approximately equal to $X_{e}$, the ratio of the voltage across the crystal unit to the feed-back emf would be $I_{r} Z_{\mathrm{e}} / I_{\mathrm{e}} R_{e}=Q_{\text {.. }}$. The standard crystal units which are intended for use at parallel resonance are tested for operation with definite values of load capacitance, $\mathrm{C}_{\mathrm{x}}$. Thus, the recommended operating value of $X$. may be assumed to be equal to $\frac{1}{\omega C_{x}}=\left|X_{x}\right|$. The maximum value of $R_{e}$ that is permissible with this value of $X_{\mathbf{I}}$ is also specified. Hence, in the design of an oscillator that must operate satisfactorily with any randomly selected crystal unit of a given type, allowance must be made in the circuit design to ensure that satisfactory activity is obtained for the minimum
$Q_{e}\left(=\frac{1}{\omega C_{x} R_{e}(\max )}\right)$.

## MAXIMUM EFFECTIVE $Q\left(Q_{c m}\right)$

1-234. Where it is desirable to have an activity
parameter that is not a function of the particular external load capacitance, the maximum effective $Q\left(Q_{\text {en }}\right)$ offers a convenient index of the maximum potential activity of a crystal unit which is to be operated in a type of circuit whose activity depends primarily upon $Q_{\text {. }}$. The maximum effective $Q$ can be expressed solely in terms of the basic crystal parameters, since the maximum occurs midway between $f_{r}$ and $f_{a}$ so that $\Delta f=\frac{\Delta f_{\mathrm{a}}}{2}$. Thus, from equations (1) and (2) of figure 1-98, it can be seen that

$$
Q_{e m}=\frac{X_{e}}{R_{e}}=\frac{2 \pi L \Delta f_{\mathrm{a}}}{2 R}
$$

Since

$$
\left.\Delta f_{\mathrm{a}}=\frac{\mathrm{fC}}{2 \mathrm{C}_{\mathrm{o}}} \quad \text { [by equation } 1-208(1)\right]
$$

Then

$$
Q_{\mathrm{em}}=\frac{2 \pi \mathrm{fLC}}{4 \mathrm{RC}_{\mathrm{o}}}=\frac{\sqrt{\mathrm{LC}}}{4 \mathrm{RC} C_{o}}=\frac{1}{4 R \omega C_{o}}=\left|\frac{\mathrm{X}_{\mathrm{C}_{0}}}{4 R}\right|
$$

$Q_{\text {en }}$ provides a convenient activity factor combining all the crystal parameters. It is equal to the maximum step-up voltage ratio that can be obtained by operating the crystal in series with a negative reactance. Where another capacitor, $C_{v}$, is shunted directly across the crystal unit, the maximum effective $Q$ of the combination becomes

$$
\sqrt{\mathrm{LC}} / 4 \mathrm{R}\left(\mathrm{C}_{0}+\mathrm{C}_{\mathrm{v}}\right)
$$

## FIGURE OF MERIT, M

1-235. In paragraph 1-216, it was shown that the minimum $f_{y}$ obtainable with a crystal unit occurs when the apparent $Q_{*}$ of the motional $\operatorname{arm}, \frac{X_{m}}{R}$, is equal to 2 ; that is, unless $R_{T}$, the effective resistance in the shunt arm, is significant. Within the frequency range at which the crystal unit appears as a positive reactance, the maximum value of Q. occurs at the antiresonant upper limit. This maximum theoretical value of $Q_{n}$ has been selected as a convenient figure of merit to indicate the relative activity quality of a crystal unit, and has been assigned the symbol M. In general, the larger the value of $M$, the less will be the feed-back energy required to sustain a given activity. If $M$ is less than 2 , the crystal unit cannot exhibit a positive reactance, and hence cannot be used in conventional oscillator circuits. To sustain oscillations at
a desired level, an oscillator will require that the crystal exhibit some minimum value of $Q_{n}$, equal to 2 or greater, depending upon the oscillator, so that a knowledge of the $M$ of a crystal unit is of value in determining whether or not the crystal can be used. Formulas for $M$ are:

$$
\begin{align*}
M & =\left|\frac{X_{C o}}{R}\right|=\frac{X_{m}}{R}=\frac{4 \pi L \Delta f_{a}}{R}=\frac{2 \pi f L C}{R C_{o}} \\
& =\frac{Q}{r}=\frac{\sqrt{L C}}{R C_{o}}=4 \dot{Q}_{\mathrm{em}} \tag{1}
\end{align*}
$$

where $Q$ is the series-arm $Q$ and $r=C_{0} / C$. Note that $M$ is equal to four times the maximum $Q_{q}$ of the crystal unit, so that the measurement of either will indicate approximately the same performance characteristics. Actually, as $M$ approaches 2 the value of $Q_{\text {em }}$ as given by equation 1-234 (1) becomes unreliable, because of the approximations made in its derivation. If $M=2, Q_{\text {em }}$ is zero, although its approximate formula would indicate a value of 0.5 . In practice, however, crystal units with such low values of M are normally far below specified standards, except possibly in the case of v-h-f crystal units operating on harmonics higher than the fifth, so that $Q_{\text {em }}$, which can be meassured directly as the maximum step-up voltage ratio obtainable with the crystal unit in series with a capacitor, provides a reasonably accurate indication of $\frac{M}{4}$. $M$ was originally chosen as a figure of merit because it can be shown to be a constant of proportionality in the equation for $Q_{e}$, and because it is expressible in terms of the crystal parameters alone. As performance parameters of a crystal unit, $M$ and $Q_{\text {em }}$ are practically equivalent, but $M$ is the parameter more commonly encountered in treatises discussing crystal activity.

## PERFORMANCE INDEX

1-236. The fact that the $Q_{e}$ of a crystal unit is the most direct factor influencing the activity first became apparent through consideration of the requirements necessary for oscillations to build up in the generalized oscillator circuit in figure 1-108 (C). When $X_{e}$ and $R_{e}$ are assumed to be the reactance and resistance of an actual coil, it can be rigorously shown that oscillations build up as long as $\left|C_{x} \rho\right|<\frac{L_{e}}{R_{e}}$. Here, $C_{x}$ and $\rho$ are both functions of the external circuit; and $L_{e}$ and $R_{e}$ can be assumed to be constants of the coil. As the amplitude of oscillations increases, the plate resistance of the tube increases, which in turn causes $\rho$ to increase. ( $\mathrm{C}_{\mathrm{x}}$ may also vary, but usually to a much smaller
degree.) Multiplying both sides by $\omega:\left|\omega \mathrm{C}_{\mathrm{x}} \rho\right|<\frac{\omega \mathrm{L}_{\mathrm{e}}}{\mathrm{R}_{\mathrm{e}}}$ or $\frac{\rho}{X_{x}}<Q_{e}$. From this point of view it would appear that the change in $\rho / X_{x}$ which must be undergone before equilibrium is reached, or, equivalently, the rise in amplitude necessary to bring the plate resistance to the equilibrium point, will always increase or decrease with $Q_{e}$, and that with a given $R_{\text {u }}$, the amplitude increases or decreases with $X_{\text {e }}$. These implications can be misleading. First, with a given $X_{x}, X_{e}$ is no longer a significant variable if $Q_{\text {. }}$ is equal to 10 or more, but must remain equal in magnitude to $X_{x}$. In this event the only variable of the activity is $\mathrm{K}_{.}$. Secondly, the rise in amplitude is more accurately a function of the difference between $Q_{\text {e }}$ and the starting value of $\frac{\rho}{X_{x}}$ rather than of the magnitude of $Q_{e}$ alone. Furthermore, $Q_{r}$ is, itself, a function of $X_{x}$, for as $C_{3}$ is varied from a relatively large value of capacitance and made to approach zero, $X_{e}$ must increase with $\mathbf{X}_{\mathbf{r}}$. However, $\mathrm{Q}_{\mathrm{f}}$ does not increase indefinitely with $X_{e}$, but reaches its maximum value, $Q_{\text {em }}$, when $C_{x}=C_{o}$ and then steadily decreases as $C_{x}$ becomes smaller. Yet the difference between $Q_{e}$ and the starting value of $\frac{p}{X_{x}}$ does continue to increase even though $Q$, has passed its maximum, for the change in $\frac{X_{p}}{R_{s}}$ is less than the change in the value of $\left|\rho \omega \mathrm{C}_{x}\right|$. Now, $\mathrm{C}_{x}$ and even more so, $\mathrm{C}_{\mathrm{t}}\left(=\mathrm{C}_{\mathrm{o}}+\mathrm{C}_{\mathrm{x}}\right.$ ), can be considered reasonably constant parameters as compared with $p$ during the build-up of oscillations. Referring to figure 1-108 (F), it can be seen that oscillations build up as long as $\frac{X_{s}}{R}>\frac{\rho}{X_{T}}$ (for the same reasons that hold in the case of $\frac{X_{e}}{R_{e}}$ and $\rho / X_{x}$ ). Since $X_{T}$ can be assumed to be relatively constant, both sides of the function can be multiplied by $X_{T}$, so that it can be said that as long as $\left|\frac{X_{s} X_{T}}{R}\right| \approx Z_{p}>|p|$, the amplitude of the oscillations continues to increase. Thus, for a given starting value of $p$ and with $X_{T}$ relatively independent of the amplitude, the most direct index of the activity is the equivalent parallel-resonance impedance, $Z_{1}$, of the generalized oscillator circuit. For this reason, $Z_{p}$ is called the Performance Index and has been given the symbol PI. PI, unlike $M$ and $Q_{\text {em }}$, is not a parameter of the crystal unit alone, but of the crystal unit effectively in resonance with some specified load capacitance, $C_{x}$. Military $S$ andard crystal units intended to be operated at parallel resonance have a recommended load capacitance

Section 1

## Electrical Parameters of Crystal Units

specified. PI meters have been developed for measuring the performance index directly, but there are very few such meters available. Where the PI of a crystal unit is desired, it can readily be computed from measurements made with standard CI meters. Various expressions of PI are given below :

$$
\begin{align*}
& P I=\frac{X_{T}^{2}}{R}=\frac{1}{\omega^{2}\left(C_{0}+C_{x}\right)^{2} \mathrm{R}}=\frac{L C}{\mathrm{RC}_{\mathrm{T}}^{2}} \\
& =\frac{\left|\mathrm{X}_{\mathrm{C}_{0}}\right|^{2}}{\mathrm{R}\left(1+\frac{\mathrm{C}_{\mathrm{x}}}{\mathrm{C}_{0}}\right)^{2}}=\frac{\left|\mathrm{MX}_{\mathrm{Co}}\right|}{\left(1+\frac{\mathrm{C}_{\mathrm{x}}}{\mathrm{C}_{0}}\right)^{2}} \quad 1-23 \tag{1}
\end{align*}
$$

Note that PI is not a function of the crystal alone, but of $\mathrm{C}_{\mathrm{x}}$ as well, and care should be taken that the capacitance ratio of $\mathrm{C}_{2} / \mathrm{C}_{0}$ is not mistaken for $r=C_{0} / C$. It can be seen that the maximum PI occurs at antiresonance, where $C_{x}=0$, so that (max) $\mathrm{PI}=\left|\mathrm{MX}_{\mathrm{Co}}\right|$.
1-237. The PI of a crystal unit, or more properly, of a crystal circuit is usually found to be an important parameter entering the equations of an oscillator circuit, particularly when the equations express the conditions required for a given output. As a simple example, consider again the two generalized oscillator circuits in figure 1-109. In paragraph 1-233, it is shown that the ratio of $\mathbf{E}_{\mathrm{p}}$ to crystal power, $P_{c}$, is equal to $k Q_{e} / I_{g}$ for circuit (A), and equal to $\frac{k Q_{e}}{(k+1) I_{z}}$ for circuit (B). As long as $I_{g}$ is considered predetermined, the volt-age-to-power ratio is primarily a function of $k$ and $Q$.. Normally, however, it is not $I_{g}$ that is to be predetermined, but rather the crystal power that must not exceed the maximum value. When $Z_{r} \approx X_{c}$, the magnitude of the impedance of the feed-back arm in circuit (A) can be assumed to be equal to $k X_{e}$, and to $\frac{k X_{e}}{k+1}$ in circuit (B). $I_{\mathbf{g}}$. is thus equal to $F_{p} / k X_{e}$ in (A) and to $\frac{E_{p}(k+1)}{k X_{g}}$ in (B). On substitution in the $\mathrm{E}_{\mathrm{p}} / \mathrm{P}_{\mathrm{c}}$ equations:
or

$$
\begin{aligned}
& E_{p} / P_{\mathrm{e}}=\frac{\mathrm{k}^{2} \mathrm{Q}_{\mathrm{e}} X_{e}}{\mathrm{E}_{\mathrm{p}}} \\
& \mathrm{E}_{\mathrm{p}}^{2} / \mathrm{P}_{\mathrm{c}}=\frac{\mathrm{k}^{2} \mathrm{X}_{\mathrm{e}}^{2}}{R_{\mathrm{e}}}=\mathrm{k}^{2} \mathrm{PI} \quad \text { Circuit (A) }
\end{aligned}
$$

Similarly, $\frac{\mathrm{E}_{\mathrm{p}}{ }^{2}}{\mathrm{P}_{\mathrm{c}}}=\frac{\mathrm{k}^{2} \mathrm{PI}}{(\mathrm{k}+1)^{2}}$
Circuit (B)
Inasmuch as the power output of the oscillator can be assumed to be directly proportional to $\mathrm{E}_{\mathrm{p}}{ }^{2}$, then, for a given drive level of the crystal unit, the power output will vary directly with the PI. It
should be noted that the $E_{y}{ }^{2} / P_{c}$ equations above are not affected by the assumption of shunt capacitances, $C_{v}$, across the crystal unit. Just as $P I=\frac{X_{e}{ }^{2}}{R_{e}}=\frac{X_{\mathbf{e}}{ }^{2}}{R}$, the same value holds even if the shunt capacitance is assumed to be increased by C.

## Frequency Stabilization Quality of Crystal Unit

1-238. The over-all frequency stability of a crystal oscillator is dependent upon the stability of all the parameters influencing the crystal circuit; these in turn are dependent upon the stability of the power source and the load, as well as the ambient conditions under which the oscillator is required to operate. The over-all stabilizing ability of the crystal is dependent upon both the stability of the crystal parameters when the crystal is exposed to changes in temperature or drive level, and the ability of the crystal to minimize the change in frequency that is necessary when the parameters of the external circuit deviate. It is this latter quality of the crystal that makes the crystal oscillator superior to oscillators that use only coils and condensers to control the frequency, and is the type of frequency stability that concerns us now. 1-239. The frequency stabilizing property of a crystal is normally expressed as the rate at which its reactance changes with irequency. In figure 1-110 are shown the curves of $\frac{d X}{d f}$ for the seriesarm parameters $L$ and $C$. Resonance happens to occur at the frequency at which $X_{C}$ is changing at the same rate as $X_{L}$. Since the rate of change of $\mathrm{X}_{\mathrm{L}}$ is a constant, at frequencies 1 sar resonance it can be said that the total change in reactance with frequency is primarily a function of $L$, for the absolute rate of this change is the same whether C is large or small. Normally, however, it is not the absolute change in reactance that is important-it is, rather, the change in reactance per percentage change in frequency, or, more usually, the percentage change in reactance per percentage change in frequency. When the frequency stability is expressed in percentage, it is no longer primarily a function of $L$, but becomes dependent upon the other crystal parameters as well. Only where the major concern is to produce a definite shift in reactance or frequency for a given change in the external circuit does the major attention center upon the parameter L. Just as the relative activity potential of a crystal depends somewhat upon the type of circuit in which it is used, so also does the frequency stabilizing characteristic of a crystal depend upon the external-circuit de-


Figure 1-110. Rates of change of reactance of equivalent series-arm parameters, $L$ and $C$, with frequency
sign. A relative stability index will be discussed briefly for each of three general types of circuits: where the crystal is operated at its normal seriesresonant frequency, where it is operated in parallel with a negative reactance, and where it is operated in series with a negative reactance.

## FREQUENCY STABILITY AT SERIES RESONANCE

1-240. Since the total series-arm reactance at $f_{\text {a }}$ is equal to zero, it is not convenient to express the relative frequency stability in terms of the percentage rate of change in reactance. Approximately the same considerations apply for the resonance frequency, $\mathrm{f}_{\mathrm{r}}$. Also, the effective stability in a given circuit may well depend more upon the rate of total impedance change or the rate of phase shift with frequency than upon the actual rate at which the reactance changes. Suppose, for example, that the feed-back energy must pass through the crystal unit and return to the oscillator input in a certain phase. If, because of a change in the circuit parameters, the feed-back energy is returned slightly out of phase, the frequency will have to shift away from the normal resonant point exactly enough for the crystal to correct the change in phase. If the change in phase has originally been caused by a change in the reactance of, say, a capacitor connected directly in series with the crystal, it is only necessary for the frequency to shift the amount necessary for the crystal reactance to exactly counteract the change in the series reactance. In this case, the resistance of the crystal circuit is not effective in degrading the stability. It is true that the greater the resistance that the crystal faces, the greater must be the fre-
quency change to produce a given phase shift. But on the other hand, since the series capacitance faces the same resistance, the initial phase shift due to a change in the capacitance is correspondingly reduced. In this case, the frequency stability of one crystal as compared with that of another depends almost entirely upon its relative rate of change of reactance. At series resonance the frequency stability factor can be defined as

$$
\begin{equation*}
\mathrm{F}_{\mathrm{s}}=\frac{\mathrm{dX}}{\mathrm{df}} \mathrm{f}=2 \omega \mathrm{~L}=2 \sqrt{\mathrm{~L} / \mathrm{C}} \quad 1-240 \tag{1}
\end{equation*}
$$

where $F_{u}$ is the rate of change of reactance per fractional change in frequency. Thus, in comparing one crystal unit with another, the one with the larger $\mathrm{L} / \mathrm{C}$ ratio can be assumed to provide the greater frequency stability at series resonance. However, if the change in reactance occurs at a point in the circuit only loosely coupled to the crystal, the resistance of the feed-back circuit is relatively ineffective in reducing the phase shift of the feed-back voltage, but instead, tends to increase the change in frequency necessary for the crystal to correct the phase. In the case of a feedback network where the crystal must compensate for a change in phase that is relatively independent of the resistance in the crystal circuit, the frequency stability is more directly measured by the rate of change of phase in the crystal circuit as a whole than by the rate of change of reactance alone.
1-241. Figure $1-111$ shows that a small phase displacement, $\Delta \theta$, at series resonance is approximately equal to $\Delta X_{c} / R_{c}$, where $\Delta X_{c}$ is a small


Figure 1-111. Phasor diagram, showing change in reactance, $\Delta X_{\text {, }}$, of series-mode crystal required to produce a small change in phase, $\Delta \theta$, where the resistance of the crystal circuit is equal to $\boldsymbol{R}_{\text {. }}$.

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change in the effective reactance of the crystal, and $R_{c}$ is the total effective resistance in the crystal circuit (equal to $R_{e}$ of the crystal plus $R_{x}$ of the external circuit). For convenience, the frequency is usually expressed in terms of angular frequency, $\omega=2 \pi f$ radians per second, instead of cycles per second. In equations (1) and (2) of figure 1-98, it can be seen that for small values of $\Delta f$, the denominators of the approximate equations of $\mathrm{X}_{\mathrm{e}}$ and $R_{e}$ are approximately equal to unity, in which case $X_{e} \approx 2 L \Delta \omega$ and $R_{e} \approx R$. Thus,

$$
\Delta \theta=\frac{\Delta \mathrm{X}_{\mathrm{e}}}{\mathrm{R}_{\mathrm{c}}}=\frac{2 \mathrm{~L} \Delta \omega}{\mathrm{R}+\mathrm{R}_{x}}
$$

The frequency-stability index can be defined to be

$$
\begin{equation*}
\frac{d \theta}{d \omega}=\frac{2 L}{R+R_{x}} \tag{1}
\end{equation*}
$$

Expressed as the change in phase angle per percentage change in frequency, equation (1) becomes:

$$
\frac{\omega \mathrm{d} \theta}{100 \mathrm{~d} \omega}=\frac{2 \omega \mathrm{~L}}{100\left(\mathrm{R}+\mathrm{R}_{\mathrm{x}}\right)}
$$

or more simply;

$$
\begin{equation*}
\frac{\omega \mathrm{d} \theta}{\mathrm{~d} \omega}=\frac{2 \omega \mathrm{~L}}{\mathrm{R}_{\mathrm{c}}}=\frac{2 \mathrm{X}_{\mathrm{L}}}{\mathrm{R}_{\mathrm{c}}}=\frac{2}{\mathrm{R}_{\mathrm{c}}} \sqrt{\mathrm{~L} / \mathrm{C}} \tag{2}
\end{equation*}
$$

The last term on the right shows that where the fractional rate of change is concerned, the frequency stability is directly proportional, not simply to L , but to the square root of the $\mathrm{L} / \mathrm{C}$ ratio. Equation (2) also shows that the frequency stability is inversely proportional to the crystal circuit resistance. But it must be remembered that this is true only to the extent that the original phase shift of the input to the crystal circuit can be considered independent of $\mathrm{R}_{\mathrm{c}}$.
1-242. As an exaggerated example, we can see that minimum stability is to be expected if the input to a high-resistance, series-resonant, feedback circuit is supplied through a weak coupling from a plate tank circuit sharply tuned to the resonant frequency but having an impedance small compared with the $R_{p}$ of the tube. Since a slight change in the parameters of the tank circuit could shift the phase of the feed-back input almost 90 degrees, such an oscillator would obviously be completely unstable, even if it were assumed that oscillations could be maintained.

## FREQUENCY STABILITY AT

PARALLEL RESONANCE
1-243. When it can be assumed that a crystal unit
is effectively operating in parallel with an external capacitance, $\mathrm{C}_{\mathrm{x}}$, the value of which is relatively independent of small changes in the frequency, the frequency stability can be assumed to be directly proportional to the rate of change in the reactance of the motional arm of the crystal. In this case, it would seem that a frequency-stability factor for parallel resonance

$$
F_{p}=\frac{d X_{s}}{d \omega} \cdot \omega=2 \sqrt{L / C}=F_{s}
$$

would be appropriate-just as in the case of series resonance-and $F_{p}$ would be identical with $F_{\text {. }}$. However, it will be recalled (see figure 1-103) that the higher the reactance, i.e., the smaller the value of $\mathrm{C}_{\mathrm{T}}$, the less stable will the oscillator become. Taking this into account, a more accurate indication of the stabilizing quality of a parallel-resonant crystal is given by what is called the fre-quency-stability coefficient, which is the percentage rate of change in reactance for a percentage change in frequency. Thus,

$$
F_{X_{s}}=\frac{d X_{s}}{d \omega} \cdot \frac{\omega}{X_{s}} \cdot \frac{100}{100}=\frac{2 \omega L}{X_{s}}=\frac{f}{\Delta f}
$$

This result is quite interesting, for it indicates that for crystal units of the same frequency equal stabilities can be achieved simply by operating the crystal units at the same value of $\Delta f$ above series resonance. Since the same equation holds for any value of L and C , it is not immediately apparent as to why a crystal is so much more stable than a conventional inductor and capacitor. In paragraph 1-208 it was found that the ratio $\frac{\Delta f_{\mathbf{a}}}{f}$ is equal to $\frac{C}{2 \mathrm{C}_{\mathrm{o}}}$. If $\Delta \mathrm{f}_{\mathrm{p}}$ is substituted for $\Delta \mathrm{f}_{\mathrm{a}}$, and $\mathrm{C}_{\mathrm{T}}$ is substituted for $\mathrm{C}_{0}$, then

$$
\mathrm{F}_{\mathrm{X}_{s}}=\frac{\mathrm{f}}{\Delta \mathrm{f}_{\mathfrak{v}}}=\frac{2 \mathrm{C}_{\mathrm{T}}}{\mathrm{C}}
$$

It can be seen that in order for a conventional series-parallel inductor-capacitor network to have the same theoretical stability as a crystal, the shunt capacitance must be thousands of times greater than the series-arm capacitance. The series arm of such a network would require an extremely small $L / C$ ratio. The parallel impedance would be small, and the net series-arm reactance much smaller still. The crystal, on the other hand, has such a small value of $C$ that the reactances are reasonably large even for small values of $\Delta f$. Although the equation for the frequency-stability coefficient indicates an unlimited stability if $\Delta f_{\mathbf{w}}$ is simply made small enough, this would be theo-
retically true only for a circuit resistance equal to zero. In pratice, as $X_{n}$ approaches the motional$\operatorname{arm} R$ in magnitude, a given change in $X_{T}$ will cause a greater change in the phase of the over-all circuit impedance than will the same change in $X_{* *}$. Of significance is the fact that the frequencystability coefficient, $\mathrm{F}_{\mathrm{x}_{\mathrm{f}}}$, represents the stabilizing effect of a crystal for the percentage change in the reactance of the total effective shunt capacitance, $\mathrm{C}_{\mathbf{T}}\left(=\mathrm{C}_{0}+\mathrm{C}_{\mathbf{x}}\right.$ ). With $\mathrm{C}_{0}$ considered constant, a given percentage change in the total capacitance becomes less than the actual percentage change in the variable component, which we can assume to be the equivalent external capacitance, $\mathrm{C}_{\mathrm{x}}$. For a given $C_{T}$, the larger the ratio $C_{0} / C_{x}$ the smaller will be the percentage change in $\mathrm{C}_{\mathrm{r}}$ for a given percentage change in $C_{x}$, and the greater will be the oscillator stability in the face of changes in the external circuit. In other words, the effective frequency-stability coefficient of the crystal unit as a whole is greater than that of the motionalarm alone if it can be assumed that the percentage changes in $\mathrm{C}_{0}$ will be negligible compared to those in $C_{x}$. When $R$ is small compared with $X_{s}, X_{e} \approx$ $\mathbf{X}_{c_{0}} \mathbf{X}_{s} /\left(\mathbf{X}_{C_{0}}+\mathbf{X}_{n}\right)$ and the effective frequencystability coefficient becomes:

$$
\begin{aligned}
F_{X_{e}} & =\frac{d X_{e}}{d \omega} \cdot \frac{\omega}{X_{a}}=\frac{2 L X_{C_{0}}^{2}}{\left(X_{C o}+X_{s}\right)^{2}} \cdot \frac{\omega\left(X_{C_{0}}+X_{o}\right)}{X_{C_{o}} X_{s}} \\
& =\frac{2 \omega L}{X_{s}} \cdot \frac{X_{C_{o}}}{X_{C o}+X_{a}}=\frac{f C_{T}}{\Delta f C_{x}}
\end{aligned}
$$

Since

$$
F_{X_{8}}=\frac{f}{\Delta f}=\frac{2 C_{T}}{C}
$$

then

$$
\begin{equation*}
F_{X_{e}}=F_{X_{s}} \cdot \frac{C_{T}}{C_{x}}=\frac{2 C_{T}^{2}}{C C_{\mathbf{x}}} \tag{1}
\end{equation*}
$$

It should be remembered that equation (1) is based upon the assumption that $\mathrm{C}_{6}$ is constant and that any change in $X_{e}$ will be due to a change in $\mathrm{C}_{\mathrm{x}}$. If $\mathrm{C}_{0}$ is effectively increased by a fixed capacitance, $C_{v}$, directly shunting the crystal unit, the effective variable $C_{x}$ becomes smaller. The effective $C_{x}$, insofar as the frequency stability is concerned, will equal $\mathrm{C}_{\mathrm{T}}-\left(\mathrm{C}_{0}+\mathrm{C}_{v}\right)$. Substituting this effective value of $\mathrm{C}_{\mathrm{x}}$ in equation (1) will provide a more accurate frequency-stability coefficient for a crystal unit directly shunted by a fixed $\mathrm{C}_{\mathbf{r}}$.

FREQUENCY STABILITY AT SERIES RESONANCE WITH EXTERNAL CAPACITANCE

1-244. The effective frequency-stability coefficient, $\mathrm{F}_{\mathrm{X}}{ }=\frac{2 \mathrm{C}_{\mathrm{r}}{ }^{2}}{\mathrm{CC}_{\mathrm{x}}}$, provides an appropriate index of the frequency-stability quality of a crystal unit operated in series resonance with an external capacitance $C_{x}$, for the same reasons that make the coefficient applicable in the case of parallel-resonant circuits. $\mathrm{C}_{\mathrm{T}}$, here, represents the sum of two actual capacitances, $C_{0}+C_{x}$, and has a more concrete meaning than simply a generalized parameter. $\mathrm{F}_{\mathrm{x}_{e}}$ gives the percentage change in $X_{i}$ per percentage change in frequency. The reciprocal, $1 / \mathrm{F}_{\mathrm{K} \text {, }}$, can be interpreted as equaling the percentage change in frequency that will occur per percentage change in the negative reactance $X_{x}$. In unconventional circuit designs, where a significant phase shift can occur as a result of changes in the impedances in the oscillator output circuit (which is only weakly coupled to the feed-back input), the resistance of the feed-back circuit may need to be taken into account in a manner similar to that discussed in the case of crystal units operating in series resonance.

## FREQUENCY STABILITY OF OVER-ALL CIRCUIT.

1-245. Although the absolute values of the fre-quency-stability indices discussed in the foregoing paragraphs depend upon generalized parameters of the external circuit, the values are primarily useful for indicating the relative stabilization quality of one crystal unit as compared with another when operated under similar circuit conditions. The actual frequency drift due to changes in the supply voltages, tube characteristics, circuit impedances, etc., depends upon the particular oscillator design as well as upon the performance characteristics of the circuit components. The percentage variation that can be expected in the generalized parameter, $C_{x}$, is of equal importance in gauging the frequency stability of the oscillator as a whole. The crystal-unit frequency-stability coefficients appear as single parameters among others in the frequency-stability equations for each particular type of oscillator circuit. In general, the series-resonant type of oscillator has the greater frequency stability, permitting tolerances from four to twenty times as narrow as those normal for parallel-resonant oscillators. Indeed, in a welldesigned series-resonant oscillator where the reactive components are negligible in their effect on the phase of the feed-back voltage, the frequency stabilization of the crystal unit can be very nearly

## Section 1

## Electrical Parameters of Crystal Units

perfect, so that the most significant factor to consider is the stability of the equivalent-circuit parameters of the crystal unit, itself. One source of frequency instability common to both seriesresonant and parallel-resonant oscillator circuits is the presence of harmonics in the output. For certain applications, such as in crystal calibrators, these harmonics are desirable, but in most cases it is preferable that they be kept to a minimum. Harmonics are unwanted not only for the sake of a sine-wave output as such, but also because they introduce reactive components in the crystal circuit, thereby increasing the chances of frequency instability. The harmonics can be reduced by designing the oscillator plate circuit to provide a low-impedance bypass path for them, and by using low plate and grid voltages. Unwanted reactive effects in the oscillator circuit also occur as a result of feedback from the amplifier stages following the oscillator. These can be minimized by the use of proper shielding, buffer amplifiers, neutralizing circuits, and by careful attention to the physical layout in designing the equipment, to ensure that all leads are as short as practicable and that the oscillator is electrically isolated from circuits carrying high amplitudes of $r-f$ voltage or current. The effective load capacitance, $\mathrm{C}_{\mathrm{x}}$, with which the crystal unit resonates is usually a function of the vacuum-tube parameters, the load resistance, the effective grid resistance, as well as the reactive impedances in the feed-back and output circuits. All these variables are, in turn, functions of the oscillator output and the grid and plate d-c voltages. Thus, the frequency stability is dependent upon the degree of voltage regulation, the constancy with which the oscillator load is maintained, and in the care taken in the original design to ensure that the circuit components are so proportioned that the effects of variations in the tube parameters are minimized. Silvered mica capacitors normally are to be preferred for fixed capacitances in the tuned circuits. Those capacitors having dielectrics composed of titanium compounds can be used for r-f bypass purposes, but are too variable under changes in temperature and voltage for use as tuning components. Air-dielectric capacitors are almost always adjustable. With the exception of the vacuum-dielectric capacitor, the air-dielectric type is the most stable and is to be preferred for small capacitances and variable tuning elements. As a rule, the improvements in circuit design that permit of greater frequency stability necessitate additional circuit components, additional tuning adjustmerts, narrower operating frequency ranges, smaller voltage or power outputs, or some combination of the above.

## Bandwidth and Selectivity Parameters of Crystal Unit

THE CAPACITANCE RATIO, $r=\frac{C_{g}}{C}$
1-246. The bandwidth of a crystal unit refers to the particular frequency range over which the crystal unit can be operated in a given oscillator, filter, or transducer circuit. In the case of a conventional oscillator circuit, the applicable frequency range is that in which the crystal can appear as an inductive impedance. In cycles-persecond, this range is $\Delta f_{a}=f_{a}-f_{r}$. Percentagewise, the bandwidth is $\frac{100 \Delta f_{a}}{f_{r}}$, which, as shown in paragraph 1-208, is approximately equal to $\frac{100}{2 r}=\frac{50 \mathrm{C}}{\mathrm{C}_{0}}$. Although the practicable operating range does not extend over the entire band, it can be seen that the relative merit of a crystal unit insofar as its range of frequency adjustment is concerned can be indicated inversely by the parameter $r$, whereas the relative selectivity is indicated directly by r . In figure 1-95, it can be seen that the smallest theoretical values of $r$ (when the distributed capacitance is negligible, so that $r=r_{e}$ ) are obtained with the low-frequency, length-extensional-mode elements of the $X$ group. The smallest capacitance ratios are provided by element $E$, which has values of $r$ as low as 120 to 125. These are equivalent to a resonance-to-antiresonance bandwidth on the order of 0.4 per cent of the nominal frequency. For the high-frequency $A$ and $B$ elements, the bandwidths are approximately 0.2 and 0.083 per cent, respectively.

1-247. Insofar as frequency control is concerned, the resonance-to-antiresonance bandwidth is important primarily as a relative index of the frequency range through which a parallel-resonant oscillator can be made to operate by varying the load capacitance, $C_{x}$. For example, the tuning adjustments of an oscillator employing an A element can vary the frequency approximately two-and-a-half times as much as can the same adjustments if the oscillator employs a $B$ element. Although small frequency adjustments are possible, the high selectivity of quartz crystals precludes their use in frequencymodulated oscillators. Eventually, it may be that crystal units mounting high-frequency EDT plates, which have capacitance ratios as low as 20 , will find an application in this field, but at the present time EDT crystals are used almost exclusively in filter networks. As a filter element, the capacitance ratio of a crystal is of greater importance than in frequency-control circuits. Filter networks, composed of crystal units alone, can be designed for a
maximum pass band of $\frac{2 \Delta f_{\mathrm{w}}}{\mathrm{f}_{\mathrm{r}}}$, which in the case of quartz means a maximum pass band of 0.8 per cent. For the low-frequency networks, such as are normal to telephone carrier systems, this is much too selective for passing voice channels. For this reason, quartz crystals employed in l-f telephone carrier filters must be used in conjunction with inductors and capacitors. The narrow bandwidths of quartz elements used alone are primarily applicable in filters when it is desired to pass a single frequency, such as the pilot signal of a carrier system.

## ELECTROMECHANICAL COUPLING FACTOR, $k$

1-248. To the extent that the equivalent circuit of figure 1-91 is applicable it can be assumed that when a crystal unit is connected across the terminals of a battery the ratio of the energy stored in electrical form to the energy stored in mechanical form is equal to the capacitance ratio $r=$ $\mathrm{C}_{\mathrm{o}} / \mathrm{C}$. The electrical energy is that stored in the static capacitance, $C_{0}$, and is equal to $1 / 2 V^{2} C_{0}$, where $V$ is the applied d-c voltage. The mechanical energy is the energy that is stored because of the piezoelectric strain in the crystal, and is equal to $1 / 2 V^{2} \mathrm{C}$. In transducer applications, it is useful to rate a crystal according to the ratio of stored mechanical energy to total applied electrical energy under the conditions of d-c or very-low-frequency applied voltages. The parameter for this purpose is the electromechanical coupling factor, $k$, equal to the square root of the ratio of the stored mechanical to the total input energy. As such, $k$ is an index of the crystal efficiency as a transducer. This factor is given by the formula

$$
\begin{equation*}
\mathrm{k}=\frac{\mathrm{d}}{\sqrt{\frac{\epsilon}{4 \pi}} \mathrm{~s}} \tag{1}
\end{equation*}
$$

where $s$ is the dielectric constant, $s$ is the elastic compliance, and d is the piezoelectric constant giving the ratio of strain to field. According to the energy ratio, $k^{2}$ should equal $\frac{C}{C_{0}+C}$, or approximately $\frac{1}{r}$. However, the capacitance ratio, $\frac{C_{0}}{C}$, at resonance can be shown to be $\frac{\pi^{2}}{8}$ times as large as the theoretical ratio at zero frequency. Actually, then the ratio is

$$
\frac{\text { stored mechanical energy }}{\text { total stored electrical energy }}=k^{2}=\frac{\pi^{2}}{8} \cdot \frac{C}{C_{0}}
$$

where $C$ and $C_{0}$ are the equivalent capacitances at resonance. Since the bandwidth is proportional to $\mathrm{C} / \mathrm{C}_{0}$, so also is it proportional to $\mathrm{k}^{2}$. In transducer applications, when an inductor is shunted across the crystal to tune out the electrical capacitance, and the crystal is operated near resonance, up to 90 per cent efficiency is possible in the conversion of electrical to mechanical energy. Under these conditions, $k$ is not a direct index of the transducer efficiency, but it does serve as a parameter for estimating the frequency range over which the efficiency is 50 per cent or greater. The ratio of the highest to the lowest frequency for greater than 50 per cent conversion is:

$$
\begin{equation*}
\frac{f_{H}}{f_{\mathrm{t}}}=\sqrt{\frac{1+k}{1-k}} \tag{3}
\end{equation*}
$$

## Crystal Quality Factor. $Q$

1-249. The quality factor of a crystal unit is the Q of the motional arm at resonance. Thus,

$$
\begin{equation*}
Q=\frac{\omega L}{R}=\frac{1}{\omega C R}=\frac{1}{R} \sqrt{\frac{L}{C}} \tag{1}
\end{equation*}
$$

Quartz crystal units are obtained with Q's ranging in value from 10,000 to more than $1,000,000$. The $Q$ is a performance parameter that provides an indication of the ratio of the stored mechanical energy of vibration to the energy dissipated in the crystal unit per cycle at resonance. If $I_{8}$ is the $\mathrm{r}-\mathrm{m}-\mathrm{s}$ current through the series arm at resonance, then, at the instant the current is a maximum, the equivalent capacitance $C$ can be assumed to be completely discharged and all the vibrational energy, $E_{v}$, is at that instant in kinetic form. This energy is equivalent to that stored in motional-arm inductance, $L$. Therefore,

$$
\begin{equation*}
E_{v}=\frac{\left(1.414 I_{s}\right)^{2} L}{2}=I_{s}^{2} L \tag{1}
\end{equation*}
$$

The energy dissipated per second, $P_{c}$ is $I_{s}{ }^{2} R$. Thus, the ratio of the stored mechanical energy to the energy dissipated per second is

$$
\begin{equation*}
\frac{E_{V}}{P_{\varepsilon}}=\frac{I_{s}{ }^{2} L}{I_{s}{ }^{2} R}=\frac{L}{R} \tag{2}
\end{equation*}
$$

It can be seen that for a given wattage, the greater the $L / R$ ratio the greater will be the amplitude of vibration. Regardless of the wattage, for a given $L$ the amplitude of vibration will vary approximately directly with the current. Theoretically,

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since there are no Military Standards setting a minimum limit for the series-resonance resistance, a crystal unit can be so excellently mounted that it would be vibrated near its elastic limit if attention were given only to the power dissipation rather than to the current. Such a situation is not likely to arise except possibly in the case of a crystal-controlled power oscillator, where space and cost limitations require a crystal drive level far in excess of the rated level. More important from the point of view of maintaining a sinusoidal wave shape of the excitation voltage and of improving the stability of the oscillator is the ratio of the stored energy to the energy dissipated per cycle, rather than per second. In terms of angular frequency, the dissipation per radian is $I_{n}{ }^{2} R / \omega$, so that

$$
\begin{equation*}
\frac{E_{v}}{P_{c} / \omega}=\frac{I_{s}{ }^{2} \omega L}{I_{s}{ }^{2} R}=Q \tag{3}
\end{equation*}
$$

In an actual series-resonant circuit, it is the $Q$ of the entire circuit rather than of the crystal unit alone that must be considered, so that R should be replaced by the total circuit resistance. If a tuned, class-C-operated circuit is to be effective in maintaining a sinusoidal wave shape and in reducing harmonics, the energy stored in the circuit should be at least twice the amount that is dissipated over the entire cycle. That is,

$$
(\min ) \frac{E_{v}}{P_{\mathrm{c}} / f}=\frac{\mathrm{Q}}{2 \pi}=2
$$

This requirement is met easily in quartz-crystal circuits, but it is an important consideration in the design of plate tank circuits that are to be fed in pulses not smoothed by the action of the crystal. The crystal $Q$ is also an important parameter in crystal filters. In general, the higher the $Q$ the sharper the pass band.
1-250. Since the $Q$ of a crystal is equal to $\frac{1}{R} \sqrt{\frac{L}{C}}$, and since the $\frac{L}{C}$ ratio for a given frequency can be increased to almost any value desired by decreasing the electrode area and by orienting the crystal in a direction of weak piezoelectric effect, or by using twinned crystal blanks, it might be wondered why much larger values of $Q$ are not in use. The reason is that the L/C ratio and the equivalent series-arm resistance of the crystal are not independent of each other. As $\sqrt{L / C}$ increases, so also does $R$. This can be intuitively seen if it is kept in mind that fundamentally the $Q$ is the ratio of the energy stored to the energy dissipated
per angular cycle. Suppose that we have two crystal plates, A and B, both of approximately the same size and normal frequency, and both mounted exactly alike in that the frictional losses of one are the same as those of the other for the same energy of vibration. We shall also assume that these mechanical losses account for most of the crystal driving power. In other words, we are assuming that the two crystals have approximately the same quality factor, Q. Now, suppose that crystal A has a much smalier electrode area than does crystal B, or that for some other reason the piezoelectric effect of A is very weak compared with that of $B$. Under these conditions, crystal A will have a much larger equivalent L/C ratio than does crystal $B$. But since the $Q$ of $A$ equals the $\mathbf{Q}$ of $\mathbf{B}$, it can be seen that the series$\operatorname{arm} \mathrm{R}$ of A must be greater than the series-arm R of B in the same proportion as the square roots of the respective $\mathrm{L} / \mathrm{C}$ ratios. It should be understood that the Q and the $\mathrm{L} / \mathrm{C}$ ratio are comparatively independent variables as far as $R$ is concerned. Where $\mathbf{R}$ could not be estimated without a knowledge of $Q$ and $L / C$, the latter theoretically could be approximated separately and independently by an examination of the fabrication of a crystal unit. L and C, for example, are approximately predetermined by the electrode area and the type and size of the crystal element. The $Q$ is also to a certain degree a function of the same variables, but for given internal frictional properties, is primarily determined by the quality of the crystal finishing and mounting. Thus it is that the Q is largely determined by the frictional losses and is not subject to control by varying the $\mathrm{L} / \mathrm{C}$ ratio. Indeed, as the L/C ratio increases, the piezoelectric effect can become so weak and the resistance so high that the crystal cannot be shocked into oscillation unless very high voltages are employed. Once in oscillation, a high L/C crystal unit could presumably operate satisfactorily, except that only very small currents could be withstood without the crystal shattering or arcing. There is a hypothetical case where an exceptionally large L/C ratio could be practical. Such a situation would arise if for any reason the external circuit resistance faced by a crystal couid not readily be reduced below some large minimum value. In this event, the use of a crystal unit of normal Q but large L/C ratio would prevent the over-all circuit Q from being excessively degraded by the external resistance. Ordinarily the selection of a crystal unit will be made on the basis of considerations other than the $\mathrm{L} / \mathrm{C}$ ratio, but where all else is equal, including the average values of $Q$, it might be assumed that the crystal units having the some-
what higher values of $L / C$ are generally more suitable for those oscillators which do not require a crystal to sustain oscillations, but only to stabilize them. Such a circuit oscillating at or near the crystal frequency can build up the crystal vibrations over a large number of cycles of small amplitude, thereby obviating the need of large voltage surges or abnormally high vacuum-tube amplification.

## Stability of Crystal Parameters

1-251. Regardless of how well designed a crystal oscillator may be, or how high the degree to which the crystal stabilizes fluctuations in the external circuit, the over-all performance will depend upon the stability of the crystal parameters, themselves. Changes in the crystal parameters are primarily due to aging, changes in the ambient temperature, spurious modes, and to changes in the drive level. Aging, here, is used in its broadest sense to include practically any nonreversible change in the crystal characteristic from whatever cause. The principal causes and effects of aging are discussed in paragraphs 1-172 through 1-181.

## EFFECT OF TEMPERATURE UPON CRYSTAL PARAMETERS

1-252. The temperature-frequency characteristics of quartz plates are covered in the description of the various elements, and will not be repeated here except to note that a change in the frequency means a change in the LC product of the motional arm. To what extent the frequency drift may be due to a change in $L$ and to what extent to a change in $C$ would require very precise measurements of $f_{r}$ and $f_{p}$, and the approximate formula in paragraph 1-225 for computing $C$ from the measured parameters would need to be replaced by a more rigorous equation. Although of theoretical value, such small changes in $L$ or $C$ are not, in themselves, of practical importance in circuit designrather it is the change in the LC product (i.e., in the frequency) which is important, and which must be kept to a minimum. Low-temperaturecoefficient crystals have been developed for this purpose, but only the GT, at low frequencies, and the AT, to a lesser extent, at high frequencies provide a near-zero coefficient over a wide temperature range. The more exacting the requirements, the more expensive the crystal unit will be. Fortunately, zero coefficients can be obtained at different temperatures by slight variations in the orientation angle of the cut. By mounting the crystal in an oven thermostatically controlled near the zero-coefficient point of the crystal, the tempera-
ture effected frequency deviation can be kept very small. Indeed, an ideal oven having a zero temperature fluctuation would permit any type of quartz cut to be stable provided the drive level remained constant. Nevertheless, the use of an oven is to be avoided where possible, because of the additional cost, space, weight, and power requirements, and also because the crystal pins of the oven increase the shunt capacitance across the crystal. The additional shunt capacitance proves increasingly objectionable at the higher frequencies, and makes it necessary that either the oven dimensions be as small as possible or that the entire oscillator be mounted within the oven. Either requirement serves to reduce the stability of the oven temperature, particularly if the ambient temperature varies between wide extremes. For ovens of practical size and construction, some frequency deviation is to be expected as a result of temperature changes. If this deviation is to be kept to an absolute minimum, precise tempera-ture-coefficient characteristics must be specified in selecting a crystal unit, or a greater precision in temperature control than is now attainable in the average crystal oven must be sought. An ingenious method of obtaining practically a zero temperature coefficient for A elements over a span of $20^{\circ} \mathrm{C}$ and more is being developed by the Hunt Corporation. During a luncheon conversation several years ago between E. K. Morse, S. Ryesky, and D. Neidig (the former, a Government representative, the latter two of Hunt) concerning the possibilities of improving the frequency stability of Radio Set AN/ARC-1 in its first modification, the idea originated of operating two temperaturecompensating equal-frequency $A$ elements in series. The angles of cutting could be so selected as to provide equal temperature coefficients of opposing polarities which would cancel when both cxystals were operating at the same temperature. However, little was attempted in this field until recently. Experimenta! models show, that over room-temperature ranges the frequency deviation can be quite negligible. Aging data'is still insufficient, but over a period of six months a stability of about one-half part per million has been achieved, with three-fourths of the drift occurring in the first three months. Probably the most significant recent activity in the development of fabrication processes designed to stabilize the crystal parameters against changes in temperature centers around the current investigations under the direction of Dr. E. A. Gerber of the Signal Corps Engineering Laboratories. As reported by Mr. D. L. Hammond in a modest paper, Effects of Impurities on the Resonator and Lat-

Section I

## Electrical Parameters of Crystal Uniss

tice Properties of Quartz, presented at the 1955 Signal Corps Frequency Control Symposium, a systematic exploration is under way to discover and catalog the effects on the parameters of quartz crystals which have been synthetically grown to include controlled percentages of impurities. Impurity elements being experimented with include aluminum, boron, calcium, germanium, lead, selenium, tin, titanium, and zirconium. This work undoubtedly has revolutionary possibilities. The discoveries already made presage the probability that temperature effects, which are now so important a problem, can in the future be largely eliminated by growing crystals, for particular cuts, with controlled impurities of proper quantities and proportions.
1-253. A crystal operated at an overtone mode will have temperature-frequency characteristics different from those exhibited by the same crystal at its fundamental vibration. For the control of very high frequencies the $A$ element is normally preferred to the $B$ element, because of its stronger piezoelectric effect and because of the smaller frequency deviation possible for large variations in temperature. However, an AT cut ideally oriented for operation at the fundamental mode is not usually ideally oriented for the higher modes. A research team at Philco Corporation investigating the characteristics of harmonic-mode crystals found that by far the greatest change in the tem-perature-frequency characteristics of $A$ elements occurs at the first operable harmonic jump, i.e., between the fundamental and the third harmonic. (See figure 1-112.) Since the subsequent changes at the higher harmonics are relatively small, a
crystal suitably oriented for the fifth harmonic will usually be suitable for operation under the same temperature conditions at all other overtones. The sensitivity of the crystal to slight changes in the orientation angle is acute. Figure 1-113, for example, shows the degree by which the characteristic curve of an 11th-harmonic $A$ element is rotated by successive changes in the orientation angle of only 3 minutes each. If this crystal were to be operated at room temperature, an orientation of approximately $35^{\circ} 27^{\prime}$ would appear to be preferred. For operation under temperature variations of $-55^{\circ}$ to $+70^{\circ} \mathrm{C}$, an orientation of $35^{\circ} 30^{\prime}$ permits the minimum total frequency deviation from a room-temperature mean. Finally, if the crystal is to be mounted in an $85^{\circ}$ crystal oven, an orientation of $35^{\circ} 33^{\prime}$ would be optimum.

## EFFECT OF SPURIOUS MODES UPON CRYSTAL PARAMETERS

1-254. Closely allied with the problem of temperature control is the problem of avoiding spurious modes. Spurious modes are most apt to occur in the case of thickness-shear crystals. Among these elements, the AC and BC cuts provide the purest frequency spectrum, but unless crystals of these types are provided with precise temperature control their larger temperature coefficients prevent their being preferred over $A$ and $B$ elements. Cutting the crystal blank to the proper face dimensions is the most important factor in avoiding unwanted modes, but even when due precautions are taken, sudden apparent variations in the mo-tional-arm parameters of individual crystal units


Figure 1-112. Typical variations in frequency-femperature characteristics of A element when operated at different harmonics
are not uncommon. These effects occur most often during variations in temperature, and are due to the fact that the temperature coefficients of nearby modes are quite high. The activity and frequency curves versus temperature of an erratic A element at series resonance in a tuned bridge circuit are shown in figure 1-114. The activity was measured by the grid current. No tuning adjustments were made during the temperature run. Note that the sudden jumps occur at some of the same frequencies, which, at the high-temperature portion of the curve, are apparently of a reasonably pure mode, indicating that the temperature coefficients of the desired and the unwanted modes are different. It can also be seen that the sudden dips in frequency are accompanied by abrupt changes in
activity, the latter probably being due to higher motional resistances for the unwanted modes. Unwanted modes are not always accompanied by changes in the resistance. For example, a sudden jump from one frequency to another, but without the dipping effects shown in figure 1-114, where the temperature-frequency curve is effectively broken into two smooth curves, may have very little effect on the activity. This type of frequency jump, which was quite common in the old Y-cut crystals, seems to be due primarily to small defects in the finishing of the crystal blank. Where only one such jump occurs during the temperature cycle, it can usually be eliminated by a slight retuning of the oscillator circuit. However, retuning the oscillator circuit, particularly if the crystal is


Figure 1-113. Large clockwise angle of rotation of frequency-temperature curve of harmonic-mode A element caused by small increments ( 3 minutes of orc) in the cutting orientation angle about the $X$ axis

## Section I

## Electrical Parameters of Crystal Units

being operated near series resonance, will have little effect upon those temperature-frequency characteristics due to unwanted modes that are inherent functions of the major dimensions of the crystal blank. A crystal unit having characteristics similar to those shown in figure 1-114 should not be used where the operating temperature is expected to extend into the erratic region. Unfortunately, the specifications for most of the crystal
units listed in Section II of this handbook are not rigorous enough to provide a guarantee against unwanted modes for every type of unit, if the effects upon the frequency and the effective resistance do not cause over-all deviations beyond the maximum allowed. On the other hand, "jumpy" crystals are the exception rather than the rule, but if particular precautions are necessary where wide temperature variations are to be encountered,


Figure 1-114. Activity-temperature and frequency-femperature characteristics of harmonic-mode A olement, showing effects of unwanted modes

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ony those crystal units should be used which are specified by Military Standards to be free of unwanted modes over the desired temperature range.
1-255. The overtone modes of the thickness-shear elements are more likely to be troubled with spurious frequency dips of the type shown in figure 1-114 than are the fundamental modes, but a crystal that is erratic at its fundamental vibration usually exhibits a pure frequency spectrum at a high harmonic. Indeed, because the frequencies of the unwanted and the desired harmonics do not increase in the same proportion, one method of lessening the probability of interfering modes at the higher harmonics is to deliberately cut the crystal with edge dimensions which favor spurious responses at the fundamental frequency. Nevertheless, the overtone crystals have a tendency to oscillate at two or more thickness-shear frequencies. Usually, this seems to be due to slight differences in the thickness of the crystal from one point to another. For each order of the harmonic, $n$, the crystal can be imagined to be divided into $n$ layers perpendicular to the thickness, with each layer being a separate crystal vibrating $180^{\circ}$ out of phase with the neighboring layers on each side. If $\mathbf{n}$ is an even number, the separate sections tend to cancel each other's electrical effects at resonance. For this reason the even harmonics cannot easily be electrically excited. In the case of the odd harmonics, there is always effectively one vibrating layer whose alternating polarity is not neutralized. Most of the activity is more or less centered in one particular region of the crystal plate. If the thickness at an active point differs slightly from the thickness at a neighboring point, there will be a tendency to jump from one activity center to another, and small jumps in the frequency can result. In the case of crystal plates vibrating at high harmonic modes, a small variation in the thickness dimension is generally more likely to produce a sudden frequency jump than if the same crystal were vibrating at its fundamental mode. If there is little difference between the equilibrium conditions of two vibrating stages, the frequency may shift back and forth at an audio rate, thereby effectively modulating the oscillator output with an audio frequency. Such frequency jumps are best avoided by the use of ceramic-button holders, the design of which concentrates the excitation in a small area at the center of the crystal where the most uniform thickness is attainable. Occasionally, it is found that the small frequency jump occurs only at a particular adjustment of the oscillator, and therefore it can be avoided by slight changes in the oscillator tuning. Even so, unless
the temperature is to remain reasonably constant, a crystal unit exhibiting any tuning jump at all should not be used. For although an unwanted mode that occurs during a temperature cycle may never appear during a tuning adjustment, the reverse situation is rarely found-a frequency jump that can be caused by a tuning adjustment is almost certain to appear during a temperature cycle.

## EFFECT OF DRIVE LEVEL UPON CRYSTAL PARAMETERS

1-256. There is insufficient data and standardization at the present time to analyze or to predict exactly the effect a change in the drive level will have on a crystal unit of a given type. Not only do crystal units of the same type exhibit various reactions, depending on the nominal frequency, the method of fabrication, and the manufacturer's specifications, but even when all these factors are the same for a sample of crystal units, the individual reactions to changes in drive level are unpredictable. The frequency and series-arm resistance curves versus drive level in figures 1-115 and 1-116 are shown as examples. These curves were prepared from data obtained during a Signal Corps research project at New York University by a research team consisting of Messrs. Don J. R. Stock (Director), L. Silver, E. Strongin, A Yevlove, and A. Abajian. The curves in both figures were made from the same set of 9 -mc crystal units -AT-cut, electrode-plated, wire-mounted types CR-18/U and CR-19/U, all made by the same manufacturer.

## FREQUENCY VERSUS DRIVE

1-257. In figure 1-115, note that although the frequency of the average crystal unit tends to increase with drive level, this effect is by no means to be found at all drive levels for all crystal units. Unfortunately, the temperature-frequency curves for these same crystals are not available, so it is not possible to judge how much of the frequency deviation is due simply to the rise in temperature with drive level. However, the frequencies of other A elements have been tested for frequency deviation versus power, and even though the increases of temperature due to drive occur at points of negative slope on the frequency-temperature curve, the actual frequency-drive level curve generally reveals a positive slope. This increase in frequency with drive is apparently due to a relatively large temperature-gradient coefficient. The net effect on the frequency is due to the combined influences of the changes in both the temperature and the temperature gradient, which influences

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Electrical Parameters of Crystal Units


Figure 1-115. Frequency deviation versus drive for a random sample of 9 -me $\mathbf{A}$ elements. All crystal units are the products of the same manufacturer and are similarly fabricated and mounted in HC-6/U holders


Figure 1-116. Resistance deviction versus drive for a random sample of $9 . m \mathrm{~m}$ A elements. Curves are for the same sample of erystal units whose frequency-drive characteristics are shown in figure 1-115. Correspondingly numbered curves are those of the same crystal unit
may or may not be in opposition. From the appearance of the curves in figure 1-115, it is possible that those curves starting with a negative slope may be primarily responding according to the normal temperature coefficient. No data is available concerning the degree by which the orientation of the crystal plate relative to the mounting wires might influence the thermal-gradient effect.
$\mathbf{1 - 2 5 8}$. The rise in temperature per milliwatt of drive varies widely with the types of mounting used and the sizes of the crystal plates. For wiremounted units, most of the heat generated is due to friction at the points where the crystal is supported. With the heat source thus concentrated in a small region of the crystal surface, steep thermal gradients can be expected. The over-all rise in temperature is also greater in the case of wiremounted units, since most of the thermal-leakage must be through the air, which, like all gasses, acts as a thermal insulator. If the crystal unit is vacuum-sealed, the temperature change per milliwatt may increase by a factor of from two to ten, depending upon the size of the supporting wires and how much of the crystal surface is metalplated. With the air evacuated, the heat leakage is primarily through the supports and by radiation. The amount lost by radiation depends largely upon the emissivity of the crystal surface, which is approximately 40 times as great for unplated as for plated areas. If it can be assumed that the heat is evenly distributed over the volume of the crystal, the temperature rise of a one-centimeter-square crystal wire-mounted in an HC-6/U holder (not evacuated) can be expected to be approximately 0.3 to 0.4 centigrade degrees per milliwatt of drive. In practice, however, the temperature of the parts of the crystal where most of the heat is generated may increase as much as 10 times this amount. If high or variable drive levels are to be used, pressure-mounted crystal units should be employed. The relatively large contact area between the crystal and the supporting electrodes permits a more uniform distribution of the heat, thereby reducing the magnitudes of the thermal gradients. The pressure mounts also provide a much higher thermal conductivity away from the crystal, thus enabling a much smaller temperature rise per milliwatt of drive. Finally, the pressure mount provides better mechanical and aging protection for the crystal when operated at highamplitude vibrations. Regardless of the type of mounting, it is never desirable from the point of view of stability or of long crystal life to use a higher crystal drive than absolutely necessary.
1-259. In tests made with GT-cut crystals, where


Figure 1-117. Frequency deviation versus crystal current density for two GT-cut crystals which were subjected to different periods of etching*
the frequency deviation with temperature is practically zero over a 100 -degree centigrade range, the opportunity has been afforded to study the frequency deviation due to drive alone without the complication of temperature-coefficient effects. Experiments with G elements, as reported by A. R. D'Heedene, reveal a negative frequency deviation with drive, as shown in figure 1-117. Note that the GT plate given a deep etch maintained its stability during much higher drive levels than did the plate etched only 20 minutes. Since the effective resistance of the better finished crystal can be expected to be less than, and to be more stable with increasing drive than, the resistance of crystal A, the changes in frequency with changes in crystal power may have been much closer than the curves in figure 1-117 indicate if it was assumed that the resistances of the two crystals were equal. If the change in frequency is due primarily to changes in the thermal gradients, it is more directly a function of the crystal power. On the other hand, if the frequency deviation is due primarily to mechanical strains resulting from high amplitudes of vibrations, it is more directly a function of the crystal current. Although the evidence now suggests that it is the thermal gradients that are the primary factors, certainly a lowering of the frequency can be expected for any mode if the elastic limit is approached too closely. After crystal units are subjected to high amplitudes of vibration, they do not return immediately to their original frequencies when the drive is reduced to a low level. A period of days or weeks may ensue before the crystal unit regains its former characteristics, during which time the performance resembles that of a crystal rapidly aging.
1-260. Although the frequency-versus-drive characteristics of individual crystal units deviate considerably from the norm, the characteristics are generally similar enough to plot reasonably de-

## Section 1

## Electrical Farameters of Crystal Units

pendable average curves when the fabrication processes and the frequencies are the same. Such curves showing average frequency deviation versus power are illustrated in figure 1-118. Each curve represents the average of several samples from a representative manufacturer for a given frequency. The curves with the same letter correspond to crystal units of the same manufacturer. All the crystals are A elements, metal-plated and wire-mounted in $\mathrm{HC}-6 / \mathrm{U}$ holders. In every case, it can be seen that the average tendency is for the frequency to increase with power.

## RESISTANCE VERSUS DRIVE

-261. The resistance curves shown in figure 1-116 are more or less typical of the wide variations that must be considered in the design of an oscillator.

A minimum performance level must be maintained regardless of the resistance of the crystal unit, as long as the resistance complies with the military specifications. Actually, the average series-arm resistance of the crystal units shown is quite low for 9 -me crystal units. As would be expected, the resistance generally increases as the amplitude of vibration increases. About one crystal unit in eight, however, exhibits a steady decrease in resistance as the drive increases. The initial resistance of such a unit is usually higher than the average. Note in figure 1-116 that a number of the curves have relatively sharp negative slopes at very low power levels. This characteristic is not uncommon, particularly in the case of harmonicmode elements, where it has become a problem requiring special test procedures. Harmonic-mode


Figure 1-118. Average frequency deviation versus drive. Each curve represents the average of a random sample of several similarly constructed units of one manufacturer. Curves having the same letter represent the characteristics of crystal units of the same manufacturer
crystal units are now required to pass performance tests at two drive levels. The first is at the normal maximum recommended drive level; the second is to ensure that the resistance falls within specifications when the drive is at a minimum. In the case of fundamental thickness-shear elements, shsyp negative slopes of the resistance-drive curves at low drive levels are not as common an occurrence percentage-wise as is suggested by the 9 -mc samples in figure 1-116. Much more likely to be found are resistance curves with the slopes slightly
more positive at very low drive levels.
1-262. In the design of an oscillator for military equipment a principal consideration is to ensure that the crystal drive does not exceed the recommended maximum when one crystal unit of the same standard type, but of perhaps a greatly different resistance, replaces another. If the drive is not kept to the lowest practicable level, the resistance of a borderline crystal may well be increased beyond the permissible limits, thereby excessively degrading the oscillator stability.

## CRYSTAL OSCILLATORS

For a comprehensive cross-index of crystaloscillator subjects, see end of Section 1.

## FUNDAMENTAL PRINCIPLES OF OSCILLATORS

1-263. An oscillator can be defined as any physical system having a periodic motion. If the motion is plotted as a function of time, a wave shape or a sequence of wave shapes that fairly accurately repeats itself would be considered the fundamental cycle of a stable oscillator. On the other hand, if there were a continuous change in the wave shape, the oscillator would be classified as being unstable. An oscillator that is unstable in the general sense, may, however, have a stable component of frequency, or amplitude, or some combination thereof. Of course, all oscillating systems are unstable to some degree, so that the terms stable and unstable define classifications that are somewhat arbitrary though none the less convenient.
1-264. Oscillators may also be classified according to the way in which the oscillations are controlled. A number of classifications are possible, but of those which consider the oscillating system alone, there are three general types: free, forced, and forced-free. Free oscillators are those whose oscillating energy is entirely self-contained in the oscillating state, and whose waveform and frequency are determined entirely by the properties of the system. The solar system, purely from the point of view of the planetary motions, is an example. A quartz crystal vibrating freely in space is another. Forced oscillators are those in which the energy, wave shape, and frequency are under the control of an external power source. An example would be the cone of a loudspeaker, or a quartz filter crystal, where the vibrations are controlled by the signal source. "Forced-free" oscil-
lators can be described as those which are driven by the energy of an external source, but where the frequency is primarily determined by the properties of the system. Crystal oscillator circuits are of the forced-free type. Again, the classification is somewhat arbitrary, for in the final analysis there are no absolutely free nor absolutely forced oscillations, nor can two systems be rigorously considered as distinct when there is an exchange of energy between them. In fact, fourth and fifth categories are possible. In the one, the frequency control and drive are both inherent in the system, yet not in the same sense as that defined for free oscillators. By a stretch of the imagination, a good example is to be found in the hula dancer. In a fifth category, the energy is supplied by the oscillating system, but the frequency is controlled externally. An example is to be found by considering each limb of the hula dancer as a separate oscillating system. Still other categories are possible. Insofar as a crystal oscillator circuit is concerned, as distinct from its power source, we can consider it an independent controlling system in respect to the frequency, but only to the extent that the circuit can predetermine the periodic characteristics of both the input and the output energies.

## FUNDAMENTAL REQUIREMENTS OF STABLE FORCED-FREE OSCILLATIONS

1-265. There are two fundamental conditions that are always met when a physical system is being maintained in a stable state of forced-free oscillation. First, the primary source of energy, or "prime mover," is supplying energy at the same average rate at which energy is being expended
by the system. Second, all forces acting on the oscillations are, themselves, stable periodic functions which have frequencies relative to the frequency of the oscillator that can be expressed by rational numbers (e.g., $\frac{f_{F}}{f_{0}}=1, \frac{1}{2}, \frac{8}{7}$, etc). In the practical case, this latter property cannot occur simply by coincidence between independent systems, so that the condition implies that the periods of all forces acting on the stable oscillations are controlled by the oscillator, itself. The most important of these forces are those exerted by the power source in driving the oscillator and those exerted by the output as a result of reaction with the load. The first condition for stable oscillations ensures that the average amplitude of oscillation is stable. The second condition ensures that the fundamental frequency is stable. Together, they ensure that the waveform is stable.
1-266. As a simple example of a forced-free oscillator, consider a system consisting of a swinging pendulum. If the frictional losses per cycle are small relative to the energy stored in the system, and if the amplitude is small, the oscillations are essentially those of simple harmonic motion, with the frequency being determined by the geometry of the system and the gravitational field. Assume that the pendulum, each time it reaches a certain point in its cycle, triggers a latch that releases a spurt of energy from a power source. If each kick received imparts the same amount of energy to the system, an equilibrium of stable oscillations will be reached when the input pulses are being completely transformed into a simple harmonic flow of energy to the surroundings. In order for the power source to transmit energy to the system, it must exert its force while the system is moving in the direction of the force. Otherwise, it will be the "power source," rather than the oscillator, that gains energy. If the system dissipates energy at the exact instantaneous rate at which it is received, the applied force will not, itself, produce momentary accelerations in the pendulum's swing each cycle. However, the losses from the system do not occur at simply a single interval during the cycle, but obey a sine-wave function extending over the entire period. Only at the instants of zero kinetic energy, at the end of each swing, can the instantaneous losses be considered zero. Thus, each pulse of energy must accelerate the pendulum in its direction of motion so that the waveform must deviate somewhat from a pure sine shape. The distortion is a minimum when the ratio of the total stored energy to the energy input per cycle is a
maximum, and when, during the input interval, the ratio of the energy dissipated to the energy absorbed is a maximum. In other words, the distortion becomes smaller the higher the " $Q$ " of the pendulum, the longer the interval over which the impulse is spread, and the more the impulse is centered at the middle of the swing where the instantaneous power dissipation is the greatest. Now, even though the impulses distort the waveform, the oscillations are stable if exactly the same pattern is repeated periodically. If instead of swinging back and forth, the pendulum is swinging through a complete circle, it is easier to see that if several impulses are transmitted to the system each cycle, the same pattern will continue to be repeated as long as the frequency, or frequencies, of the impulses are related to the frequency of the pendulum by a ratio of whole numbers. The fundamental of the pendulum cycle need not equal the fundamental of the stable wave, but it must be a harmonic thereof. For example, suppose that a pulse of energy is imparted to the system only once every four cycles. Then the fundamental period of the stable waveform is four times the period of the pendulum. If five impulses are delivered for each four cycles of the system before being repeated in the same phase as before, the period of the stable waveform will again equal four pendulum cycles. Only when there are one, two, three, etc, impulses repeated each cycle does the period of the stable wave equal the natural period of the oscillator. In the same way by which the forces exerted by the energy sources distort the sine-waveform, so do the forces exerted by the load into which the pendulum loses its energy. If the impedance during any interval of the swing changes from cycle to cycle without repetition, a stable waveform is not obtainable.

## APPLICATION OF FUNDAMENTAL OSCILLATOR PRINCIPLES IN THE DESIGN OF ELECTRONIC OSCILLATORS

1-267. In the application of electronic oscillators, it is not usually a stable over-all waveform that is the first requirement, but a stable fundamental frequency. Practically, however, these two effects are not independent, and the generation of the one involves the generation of the other. The deviation from a pure sine wave in the a-c output of a stable crystal oscillator will be entirely due to the presence of harmonics of the fundamental. Such fractional components as $\frac{5}{4}$ ths of the fundamental or the harmonics thereof do not appear. With the
load impedance constant, the conditions of stability are reached when energy is being supplied at the average rate of dissipation and at the same phase interval of each cycle. In the generalized crystal oscillator circuit of figure 1-108 (B), the first condition is met when $p_{s}$ is equal to $-R_{e}$. The second condition is met when $X_{1}$ is equal to $-X_{\text {e }}$. In application, the two conditions are not independent of each other, for the build up in the energy of oscillation depends upon the power source not exerting its force in phase opposition to the oscillations. Indeed a common approach to the analysis of an oscillator circuit is to establish a single equation that expresses simultaneously the equilibrium requirements of both the rate and the phase of the energy supply. Equation 1-289 (1) for the Pierce and Miller circuits is an example. Since this type of equation, when fully developed, usually becomes quite cumbersome, such an approach is only occasionally followed in this manual, it being more convenient to treat the two basic equilibrium conditions separately. The first condition, that the rates of energy supply and of energy dissipation be equal, can be assumed to be satisfied if the magnitude of the rms voltage between any two points in the circuit is constant. This condition can be expressed by an equation which equates the loop gain to unity. By this we mean that, starting with the input circuit, or at any convenient point, the overall voltage gain around the oscillator loop back to the starting point is unity at equilibrium. If the loop gain is greater than unity, oscillations build up, if less than urity, they do not start, or, if already started, they die down. As an example, the loop-gain equation of a simple oscillator of the type shown in figure 1-177(D), where the feedback energy is transformer-coupled from the plate circuit to the grid circuit, can be expressed as follows :

$$
\begin{equation*}
\mathrm{G}_{1} \mathrm{G}_{2} \mathrm{G}_{3}=\frac{\mathrm{E}_{\mathrm{p}}}{\mathrm{E}_{\mathrm{g}}} \cdot \frac{\mathrm{E}_{8}}{\mathrm{E}_{\mathrm{p}}} \cdot \frac{\mathrm{E}_{\mathrm{g}}}{\mathrm{E}_{\mathrm{k}}}=1 \quad 1-267 \tag{1}
\end{equation*}
$$

where $G_{1}$ is the gain of the vacuum tube, $G_{2}$ is the gain of the transformer in the plate circuit, and $\mathrm{G}_{3}$ is the gain of the feedback from the transformer secondary to the vacuum-tube input. Although the loop-gain equation may at first glance appear trivial since the product of the voltage ratios equals unity regardless of what voltage values are assigned, it should be remembered that a necessary qualitative implication requires that each voltage ratio represent the gain of an actual transfer of energy from one circuit to another. When the voltage ratios are expressed in terms of the circuit parameters an overall network formula is established that will serve to discipline the oscillator
design. In a similar manner, the second condition of equilibrium can be expressed as an equation of the loop phase rotation, in which the total phase shift in the voltage around an oscillator loop is equal to zero, or to some integral multiple of 360 degrees. Continuing the example of the trans-former-coupled oscillator above:

$$
\theta_{\mathrm{vg}}+\theta_{\mathrm{xp}}+\theta_{\mathrm{g}^{*}}=0\left(\text { or } 360^{\circ}\right)
$$

where $\theta_{v, x}$ is the phase of $\mathrm{E}_{1}$, with respect to $\mathrm{E}_{\mathrm{k}}, \theta_{\mathrm{xp}}$ is the phase of $\mathrm{E}_{\mathrm{x}}$ with respect to $\mathrm{E}_{\mathrm{p}}$, and $\theta_{\mathrm{RH}}$ is the phase of $E_{k}$ with respect to $E_{k}$. In most cases approximately ideal conditions can be assumed so that the loop phase requirements need only be analyzed qualitatively. For instance, in the example given of the simple transformer-coupled oscillator, let it be imagined that the plate circuit is to be designed so that the vacuum tube faces a purely resistive load. Thus, $\theta_{\mathrm{vg}}$ will represent the 180 -degree phase reversal introduced by the vacuum tube, $\theta_{x p}$ will represent a counter 180 -degree reversal by the plate transformer, so that the principal phase consideration is to design a grid circuit that will allow $\mathrm{E}_{\varepsilon}$ to be in phase with $\mathrm{E}_{n}$ at the desired frequency. The loop-phase considerations are much more involved in the case of the conventional one-tube resonator circuit shown in figure 1-119. The loop phase rotation in this general type of circuit applies to such oscillators as the tuned-grid-tuned-plate, the Hartley, the Colpitts, the Pierce, and the Miller. It is discussed in detail in following paragraphs. The loop equations are the guides by which the design engineer approaches the basic oscillator problems of obtaining the desired amplitude, the desired frequency, the desired amplitude stabiiity, and the desired frequency stability. As a general rule, these four fundamental design considerations are handled with the aid of the loop equations in the following ways:
a. An oscillator is designed to provide a certain amplitude of oscillation by ensuring that the parameters that vary with the amplitude (usually the vacuum-tube parameters) reach their limiting values, as defined by the loop-gain equation, when the desired amplitude is reached.
b. An oscillator is designed to oscillate at a given frequency by ensuring that the loop-phase equation holds at, and usually, only at, the desired frequency. Should the loop-phase equation also have a solution at some other frequency (e.g. the loop phase of the transformer-coupled oscillator mentioned above may well equal zero at more than one mode of the crystal's vibration), the design must ensure that the loop gain is less than unity at the unwanted frequency.
c. The amplitude stability is improved by counteracting or minimizing variations in those circuit parameters which, as indicated by the loop-gain equation, are most likely to cause changes in the amplitude.
d. The frequency stability is improved by counteracting or minimizing variations in those circuit parameters which, as indicated by the loop-phase equation, are most likely to cause changes in the frequency.
Before proceeding to a discussion of the particular types of oscillators, let us first examine in detail the phase relations of the conventional resonator circuit of figure 1-119(B). If a firm qualitative understanding of the operation of this type of circuit is had, the reader should be greatly aided in interpreting the physical meaning of equations later to be derived.

## PHASE ROTATION IN VACUUM-TUBE oscillators

1-268. The conventional equivalent circuit of a vacuum-tube amplifier is shown in figure 1-119 (A). The equivalent generator voltage is equal to $-\mu \mathrm{E}_{g}$, where $\mu$ is the amplification factor of the tube, and $E_{g}$ is the excitation voltage on the grid. $R_{p}$ is the plate resistance of the tube, and $Z_{L}$ is the a-c load impedance. The minus sign of the generator voltage indicates a 180 -degree phase difference between the equivalent emf and $\mathrm{E}_{\mathrm{g}}$. For oscillations to build up, energy must be fed back in the proper phase from the plate circuit, or from some circuit in a following stage. The control grid of the vacuum tube is effectively an escapement device for controlling the release of energy from the power source. Since this energy must be re-
leased each cycle so as not to be in phase opposition to the oscillator, the grid voltage alternations must be "timed" by the activity in the rest of the circuit. This means that a sufficient and properly phased part of the energy released by the action of the grid must be fed back from the plate circuit each cycle, or from some other circuit of a following stage, in order to continue the periodic release of energy. The initial rush of plate current is to be sufficient to shock the circuit into oscillation, and the initial alternating voltage fed back to the grid circuit must be sufficient for the vacuum tube to generate more a-c energy than is lost during the first cycle. $R_{p}$ increases with the amplitude of oscillations until equilibrium is reached.
1-269. The phase relation between the grid and plate voltages of an oscillator vacuum tube at equilibrium is the same as that which would occur if the grid were excited at the same frequency from an external a-c source and the tube were connected as a conventional amplifier, operating into the same equivalent load impedance it faces as an oscillator. However, only a certain impedance relationship among the components of a particular oscillator circuit can provide a feed-back producing the proper input phase. It is this necessary impedance relationship that determines the frequency. In the usual single-tube oscillator, the equivalent vacuumtube generator, of voltage $-\mu \mathrm{E}_{\mathrm{g}}$, must drive a plate-coupled feed-back circuit that causes the voltage appearing across the grid to be rotated 180 degrees ahead of or behind the generator emf. The simplest method of reversing the phase is by transformer coupling. On the other hand, if two tubes are used, the reversal can be accomplished by the second tube alone. Either of these methods can


Figure 1-119. (A) Equivalent circuit of vacuum-tube amplifier. (B) Equivalent circuit of arystal oscillators of the Pierce and Miller types
enable a crystal oscillator to work into a more or less resistive load, so that fluctuations in the circuit parameters can have little effect on the feed-back phase, and, hence, upon the frequency. In the conventional parallel-resonant circuits, such as are illustrated in figure 1-109, the phase is rotated as shown in figure 1-119(C). First, assume an ideal case in which the resistive losses in the feed-back arm are zero. In this case, but only in this case, $Z_{\mathrm{L}}$ would need to be resistive. The frequency would be that at which the plate and feed-back arms operate as a parallel-resonant tank. There would be no phase shift in the voltage across $Z_{L}$, and $E_{p}$ would be of the same sign as $-\mu \mathrm{E}_{\mathrm{g}} . \mathrm{Z}_{\mathrm{p}}$ and $\mathrm{Z}_{\mathrm{g}}$, the impedances of the plate circuit from plate to cathode and of the grid circuit from grid to cathode, respectively, are reactive, and must always have the same sign. $Z_{p g}$, the plate-to-grid impedance is the dominant impedance in the feed-back circuit, and is always opposite in sign to $Z_{p}$ and $Z_{g}$. In the ideal circuit, if $Z_{p}$ and $Z_{g}$ are positive, $Z_{p g}$ is negative, so the current, $I_{g}$, leads $E_{p}$, and therefore $-\mu \mathrm{E}_{\mathrm{g}}$, by 90 degrees. If $\mathrm{Z}_{\mathrm{p}}$ and $\mathrm{Z}_{\mathrm{g}}$ are negative, $\mathrm{Z}_{\mathrm{pg}}$ is positive, so $I_{g}$ lags $E_{p} 90$ degrees. The voltage across $Z_{p z}$, of course, would be in phase with $E_{p}$ in both instances. Since $Z_{g}$ is opposite in sign to $Z_{p g}$, $\mathrm{E}_{\mathrm{g}}$ thus is opposite in sign to $\mathrm{E}_{\mathrm{p}}$, and the required reversal takes place. Note that $I_{g}$ is first rotated in phase with respect to $\mathrm{E}_{\mathrm{p}}$; next $\mathrm{E}_{\mathrm{g}}$ is rotated in the same direction with respect to $Y_{g}$.
1-270. In an actual circuit, the feed-back losses cannot be zero, so that a 180 -degree reversal cannot be obtained in the conventional feed-back circuit alone. This means that $E_{p}$ must first be rotated by an amount exactly sufficient to make up the difference. Assume first that $R_{p}$ is much greater than $Z_{L}$, so that $I_{p}$ can be assumed to be essentially in phase with the equivalent generator voltage. In
this case, an inductive $\mathrm{Z}_{\mathrm{L}}$ causes $\mathrm{E}_{\mathrm{p}}$ to lead the emf, whereas a capacitive $Z_{L}$ causes $E_{p}$ to lag the emf. Unless the effective $Q$ of the feed-back circuit is very low, $Z_{L}$, must be very nearly resistive, for the shift in the phase of $\mathrm{E}_{\mathrm{p}}$ need not be large. In any event, the rotation of $E_{p}$ must be in the same direction as that of $I_{g}$ and $E_{g}$. For this to occur, the susceptance of $Z_{p}$ must be greater in magnitude than the susceptance of ( $Z_{\mathrm{pg}}+\mathrm{Z}_{\mathrm{g}}$ ). That is, the reactive component of the current through $Z_{p}$ must more than cancel the reactive component of $I_{g}$. The smaller the value of $R_{p}$ compared with the value of $Z_{L}$, the more nearly will $Z_{L}$ control the phase of $I_{p}$, and the more detuned must the parallel circuit become in order to obtain the necessary rotation of $E_{p}$. If practically all the resistance in the feedback arm is between the grid and the cathode, as is normally the case when $\mathrm{E}_{\mathrm{g}}$ is developed directly across the crystal unit, $\mathrm{E}_{\mathrm{p}}$ must be rotated through a larger angle than otherwise, thereby requiring the parallel circuit to be detuned to a greater degree. This is because $E_{p}$ must be rotated by an amount effectively equal to the sum of two angles. One of the angles is the difference between the actual phase of $I_{g}$ relative to $E_{p}$ and the ideal phase of $\pm 90$ degrees. The second angle is the difference between the actual phase of $Z_{k}$ and its ideal phase of $\pm 90$ degrees. If all the resistance is contained in the large impedance $Z_{p g}$, only the phase deficiency of $I_{g}$ is reflected in the phase of $E_{p}$. On the other hand, if all the resistance is effectively contained in the small impedance $Z_{k}$, the effect on the phase of $\mathrm{E}_{\mathrm{p}}$ by $\mathrm{I}_{k}$ is normally small by comparison with the effect due to the grid-to-cathode resistance. Expressed in polar form :

$$
\mathrm{E}_{\mathrm{g}}=\mathrm{I}_{\mathrm{g}} \mathrm{Z}_{\mathrm{g}}\left(\theta_{\mathrm{Ig}}+\theta_{\mathrm{Z}}\right)=\mathrm{I}_{\mathrm{g}} \mathrm{Z}_{\mathrm{g}}\left(0^{\circ}\right)
$$

where $\theta_{\mathrm{Ig}}$ and $\theta_{\mathrm{zg}}$, which must be equal in magnitude

| CHARAETEAISTICS OF COUIVALENT-CIRCUIT PAGAMETERS |  |  |  |  | PHASE RELATIONS $180^{\circ}-\frac{190^{*}}{-9} 0^{\circ}$ <br> - Voltage and current with respect to eg. fapedances WITH RESPECT TO CURRENT THROUGH THEM ! |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | ${ }^{2} 4$ | 20\% | [8ofz | 2p/zeqt | - 4 E | ${ }_{2}$ | 10 | $E$ | zoqs | 10 | 2 | E* |
| -700~~N | -676 | $-11$ | < On > - | $\Rightarrow 1$ | $\cdots$ | $\longrightarrow$ | - | $\cdots$ | 1 | 1 | 1 | $\square-$ |
| $\rightarrow$ Trum | $-1 \square$ | T06- | <OR > 1 | $\approx 1$ | $\pm$ | - | $\cdots$ | - | 4 | 4 | 1 | - |
| -76 | -676 | $\cdots 1$ | >> 1 | $\approx 0.95$ | - | 7 | $\square$ | 7 | 1 |  | $\gamma$ | $\square-$ |
| $\cdots \mathrm{m}$ | - 1 T | W6\% | 3>1 | $\approx 0.93$ | $\square$ | 4 | $\pm$ - | $\cdots$ | 1 | 1 | 1 | $\xrightarrow{-}$ |
| -6m | 607~w | $\square]$ | \% 1 | $<0.95$ | - | 7 | 4 mm |  | 1 |  | 1 | $\cdots$ |
| $\cdots \mathrm{mm}$ | $\square \square$ | ת606m | $\approx 1$ | < 0.95 | - | \% | 2 | + | 1 | 4 | 1 | $\longrightarrow$ |

(C)

Figure 1-119. (C) Chart showing ideal and typical phase relations necessary for forced-free oscillations of the circuit shown in (B)

## Section 1

but opposite in $\operatorname{sign}$, are the phase angles of $I_{z}$ with respect to $\mathrm{E}_{\mathrm{g}}$ and of $\mathrm{Z}_{\mathrm{k}}$ with respect to $\mathrm{I}_{\mathrm{g}}$. Now, letting $\theta_{\mathrm{zpgc}}$ equal the phase of the total feed-back impedance, ( $\mathrm{Z}_{\mathrm{pg}}+\mathrm{Z}_{\mathrm{g}}$ ), with respect to the current through it, and $\theta_{\mathrm{Ep}}$ equal to the phase of $\mathrm{E}_{\mathrm{p}}$ with respect to $\mathrm{E}_{\mathrm{g}}$,
we have $\quad \theta_{\mathrm{E}_{k}}=\theta_{i_{g}}+\theta_{Z_{k}}=0$
and

$$
\theta_{\mathrm{E} ;}=\theta_{\mathrm{tk}}+\theta_{\mathrm{z}_{\mathrm{pkc}}}
$$

so that $\quad \theta_{E p}=\theta_{\mathcal{L u g}}-\theta_{\mathbf{z}_{g}}$
Since $\theta_{\mathrm{z}_{\mathrm{ig}}}$ is opposite in sign to $\theta_{\mathrm{z}_{8}}$, these two phase angles add numerically. If it is assumed that $\mathrm{Z}_{\mathrm{pgc}}$ is approximately six times the magnitude of $Z_{g}$, but that all the feedback-arm resistance is between the grid and cathode, the $Q$ of $Z_{\mathrm{pgc}}$ will be approximately five times the $Q$ of $Z_{8}$. Under these conditions the rotation of $E_{p}$ from the ideal value of -180 degrees is approximately 20 per cent greater than the deviation of $-\theta_{z_{g}}$ from its ideal value of $\pm 90$ degrees. If $Z_{g}$ represents the effective impedance of a crystal unit in parallel with the grid-tocathode capacitance and resistance, the minimum rotation of $\theta_{\mathrm{Ep}}$ occurs when the effective $Q$ of the crystal and its shunt impedance is a maximum, provided $Z_{\mathrm{rg}} \gg \mathrm{Z}_{\mathrm{g}}$. Similarly, if $Z_{\mathrm{pg}}$ represents the $Z_{e}$ of a crystal unit whose effective resistance is much greater than the equivalent series resistance of the grid-to-cathode impedance, the rotation of $\theta_{\text {ep }}$ depends primarily upon the crystal unit $Q_{e}$, and is a minimum when $Q_{\mathrm{e}}$ is a maximum.

1-271. In a conventional parallel-resonant crystal oscillator having an ideal feed-back arm, the frequency would be determined entirely by the resonance of the tank circuit, so that fluctuations in $R_{p}$, although effective in changing the activity, would not affect the frequency. In practice, the equivalent resistance of the crystal unit is a parameter of the feed-back arm, so that the detuning of the tank becomes very nearly a direct function of the effective $Q$ of the crystal and its shunt capacitance. Note that the phase of $E_{p}$ with respect to $E_{g}$ and $-\mu \mathrm{E}_{\mathrm{g}}$ is determined entirely by the parameters of the feed-back arm. As long as oscillations continue, variations in $R_{p}$ or $Z_{p}$ can only change the phase of $E_{p}$ indirectly, i.e., by causing a change in the $Q$ of the feed-back arm. Since the effective resistance can vary by as much as a factor of 10 between minimum and maximum values for the same standard type of crystal unit, an oscillator cannot be designed too closely upon the assumption that the load impedance $Z_{k}$ will be essentially the same either in phase or magnitude when one crystal unit
is replaced by another-even if it is of the same type and nominal frequency. This limitation might possibly be minimized by switching the crystal unit from the feed-back circuit to the plate circuit, and replacing it with a high-Q inductor in the feed-back arm. If the grid were operated with bias sufficient to prevent the flow of grid current, a very high and predictable $Q$ could be obtained in the feed-back circuit, and an approximately resistive $Z_{1}$, could be assumed for the tank regardless of the variations in $Z_{p}$ due to variations from one crystal unit to the next.

1-272. An oscillator that can be represented by the equivalent circuit shown in figure $1-119$ will show the following phase characteristics and related effects.
a. The phase of $E_{p}$ is entirely determined by the over-all $Q$ of the feed-back circuit and the $Q$ of the grid-to-cathode impedance, $Z_{g}$. The phase angle, $\theta_{\text {mp }}$, is given by equation $1-270$ (1) as being equal to $\left(\theta_{\mathbf{z}_{\mathrm{pg}}}-\theta_{\mathrm{Z}_{\mathrm{g}}}\right)$. Let us now assume that $\left(\theta_{\mathrm{z}_{\mathrm{prc}}}\right.$ $\left.-\theta_{Z_{k}}\right)$ is determined by an imaginary over-all $Q$ of the feed-back circuit. This we define to be

$$
\begin{aligned}
& Q_{1}=\left|\cot \theta_{E p}\right|=\left|\cot \left(\theta_{Z_{\mathrm{pgc}}}-\theta_{Z_{\mathrm{g}}}\right)\right| \\
& =\left|\frac{\tan \theta_{\mathrm{Zppc}} \tan \theta_{\mathrm{z}_{\mathrm{x}}}+1}{\tan \theta_{\mathrm{Zpgc}}-\tan \theta_{\mathrm{Z}_{\mathrm{R}}}}\right| \\
& =\frac{Q_{p g c} Q_{\mathrm{g}}-1}{Q_{3 \mathrm{gcc}}+Q_{\mathrm{g}}}=\frac{Q_{\mathrm{Rgc}} \mathrm{Q}_{\mathrm{g}}}{Q_{\mathrm{pgc}}+Q_{\mathrm{g}}} \quad 1-272(1)
\end{aligned}
$$

It can be seen that if either $Q_{\text {Dא }}$, the actual effective over-all $Q$ of the feed-back circuit, or if $Q_{g}$, the $Q$ of the grid-to-cathode impedance, is very large compared with the other, $Q_{r}$ is approximately equal to the smaller $Q$.
b. For a given phase difference between $\mathrm{E}_{\mathrm{p}}$ and $-\mu \mathrm{E}_{g}$, the ratio of $\mathrm{Z}_{\mathrm{f}}$ to the total feed-back impedance, $Z_{\mathrm{pgc}}$, is less than 1 by an amount which increases as the ratio of $\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{i}}$ decreases. In other words, the ratio of the r-f current in the plate circuit to the r-f current in the grid circuit increases as $R_{p}$ decreases.
c. The value of $R_{v} / Z_{L}$ is partly a function of the ratio $\frac{Z_{p g c}}{Z_{g}}=E_{p} / E_{g}$. Assume, for example, that $R_{p} \gg Z_{L}$, so that $E_{p} / \mu E_{g}\left(=\frac{Z_{L}}{R_{p}+Z_{L}}\right) \approx \frac{Z_{L}}{R_{p}}$. Also assume that during oscillations $Z_{g}$ is decreased, but that $Z_{p g}$ remains essentially constant. The ratio $\mathrm{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{g}}$ is thus increased, and likewise the ratio $\mathbf{E}_{\mathrm{p}} / \mu \mathrm{E}_{\mathrm{g}} \approx \frac{\mathbf{Z}_{\mathrm{L}}}{\mathbf{R}_{\mathrm{p}}}$. In other words, as $\mathrm{E}_{\mathrm{g}}$ becomes a smaller component of the total voltage across the
feed-back circuit, $E_{1}$ cannot decrease in the same proportion, else each succeeding cycle would be weaker than the one before; so the ratio $R_{p} / Z_{L}$ must decrease. Part of the change is due to the increase in $Z_{\mathrm{L}}$, and part is due to a decrease in $\mathrm{R}_{\mathrm{p}}$. If it is assumed that a large percentage change in $Z_{k}$ causes only a small percentage change in $Z_{p g c}$ then $Z_{L}$ remains essentially constant in magnitude and $R_{p}$ becomes the principal variable. In any event, as $R_{1} / Z_{L}$ decreases, the effective $Q$ of $Z_{L}$, as represented by an equivalent resistance and reactance in series, must increase in order to compensate for the increased phase shift of $I_{p}$.
1-273. From the qualitative discussion in the foregoing paragraphs it can be seen that in the conventional parallel-resonant crystal oscillators the state of an oscillator in operation is primarily determined by the impedance relations in the feedback arm. Since the impedance of a crystal unit changes very rapidly with a small change in frequency, a crystal connected in the feed-back circuit makes the oscillator less critical in design than would otherwise be the case. Where maximum stability is required, the vacuum tube will be operated as nearly class B as possible. Under class-A conditions, $R_{p}$ and $\mu$ are approximately given by the d-c, plate-characteristic data of the tube. In the case of power oscillators, amplifier operation will normally be class $C$, although class $B$ or even class $A B$ may be employed in particular circuits. In these cases, the effective tube parameters cannot be known beforehand, but reasonably accurate approximations can be made and optimum operating conditions can be reached by more or less trial-and-error final adjustments. The operation of conventional oscillators is made less critical, both in starting oscillations and in maintaining a constant amplitude, by the use of gridleak rather than fixed bias. From the point of view of phase rotation, the conductance of the gridleak somewhat decreases the $Q$ of $Z_{k}$, and thereby necessitates increased detuning of the tank. Nevertheless, in low-power oscillations the gridleak losses can normally be considered negligible in comparison with the crystal losses. It is as a limiter and stabilizer of the amplitude that the gridleak bias is most important. Any changes in the circuit that tend to change $E_{g}$ automatically change the bias in such a direction that $R_{p}$ and $g_{m}$ of the tube are readily adjusted to new equilibrium values, so that the tendency is one of immediate opposition to the change in so far as the activity is concerned.

## TYPES OF CRYSTAL OSCILLATORS

1-274. Crystal oscillators are frequently classified
as being either crystal-controlled or crystal-stabilized. A crystal-controlled oscillator is defined as an oscillator that cannot oscillate if the crystal is removed or is defective. A crystal-stabilized oscillator, on the other hand, operates as a "free-running" oscillator if the crystal is removed. When the crystal unit is properly inserted and the "freerunning" frequency is made to approach the normal resonance of the crystal, the mechanical vibrations of the crystal sharply increase. At some point the piezoelectric effect will be sufficient to suddenly "capture" the oscillations and thereby synchronize them at the crystal-circuit frequency. Generally, the crystal-controlled oscillator is preferred, since it is not desirable that oscillations continue if the crystal unit suddenly or gradually becomes defective. Also, crystal-controlled oscillators are normally less critical to design and are less likely to jump suddenly from one frequency to another. The crystal-stabilized oscillator does have the possible advantage of being able to oper. ate successfully with very-high-Q crystal units whose piezoelectric coupling, however, would be too weak for the crystal to build up oscillations from a single initial impulse. A number of oscillator circuits appear to be border-line cases, that can only arbitrarily be classified as crystal-controlled or crystal-stabilized. For example, the CI meter circuit shown in figure $1-106$, if connected in the crystal position of $S_{1}$, would fail to oscillate if the crystal terminals were open, but not if they were shorted. Most of the oscillator circuits that are discussed in the following paragraphs are classified as crystal-controlled inasmuch as the oscillations do not occur if the crystal units are disconnected.
1-275. A more practical classification from the standpoint of circuit design and of selection of a crystal unit is that of series- and parallel-resonant crystal oscillators. In general, the series-resonant type provides the greater frequency stability and can generate the higher frequencies; whereas the parallel-resonant type is the more economical to construct, can operate over a wider frequency range by the substitution of different crystal units, and can generate the greater power output. There are, nevertheless, a number of exceptions to the general rule.

## PARALLEL-RESONANT CRYSTAL OSCILLATORS

1-276. The first quartz oscillators to find general usage as frequency-control devices were of the parallel-resonant type. These oscillators are used primarily with fundamental-mode crystals at fre-
quencies below 20 mc . In the conventional circuits of this type, the crystal must operate between its resonant and antiresonant frequencies, thereby behaving as an inductor. Under these conditions the circuit does not oscillate if the crystal unit becomes defective. Unless a frequency monitor is to be available, these oscillators should be permitted a tolerance of 0.002 per cent or greater, depending primarily upon the tolerance rating of the crystal unit to be used. Under extreme operating conditions, an oscillator error of approximately twice the crystal unit tolerance should be permitted. The conventional circuits are of the Pierce and Miller types, or their modifications. Maximum stability is achieved with low crystal drive and class-A to class-B operation of the tube. Maximum power efficiency is achieved with class-C operation. Since fundamental-mode crystals become too thin and fragile for operation above 20 mc , overtone crystals are necessary at these higher frequencies. However, the shunt capacitance, $\mathrm{C}_{6}$, and the seriesarm L remain the same whether the thicknessshear crystal is operated at the fundamental or the overtone mode, whereas the series-arm $C$ varies inversely with the square of the harmonic. Thus, the capacitance ratio, $\mathrm{C}_{0} / \mathrm{C}$, increases with the square of the harmonic, so that the electromechanical coupling may be too weak to initiate oscillations at normal voltages if the crystal unit is to be operated at parallel resonance. For this reason and also because $C_{0}$, as well as the tube capacitances shunting the crystal, have larger susceptances at the higher frequencies, which greatly reduce the operating range of the crystal unit, the parallel-mode circuits are unsuitable for use at the higher frequencies. If the basic circuits are modified to employ series-mode crystals, or are used in conjunction with frequency-multiplying stages, they can provide stable control of very high frequencies. The introduction of a number of multiplier stages with the attendant problems of preventing unwanted frequencies is usually less to be preferred than the direct generation of the end frequency by the use of overtone-mode crystals in series-resonant circuits. Although frequency multiplication involving more than one multiplier stage is still widely used in conjunction with par-allel-resonant master oscillators, this usage is found principally in medium- to high-frequency transmitters where various multiplying combinations can provide the maximum number of channels with a minimum number of crystal units. Control by parallel-mode circuits of frequencies above 30 mc is not very common. One example is to be found in Radio Set AN/ARC-1A. In this
equipment, a fundamental frequency of 8 mc , for instance, would be doubled in the oscillator plate circuit and increased nine times more in the plate circuit of the following stage. Thus, with only two tubes, a parallel-resonant oscillator can control a frequency of 144 me and higher. In the analysis of the particular oscillators to follow, the Pierce oscillator has been chosen as something of a reference circuit as well as a point of departure in the discussion of many design considerations to be encountered in crystal oscillators. For this reason, the reader will find the treatment of the Pierce circuit, both qualitatively and mathematically, considerably more detailed than that of the other types of circuits. Space forbids as comprehensive a treatment for the other circuits, but the design problems and methods illustrated in the particular case of the Pierce oscillator are applicable in principle to all oscillators.

## The Pierce Oscillator

1-277. The Pierce oscillator is fundamentally a Colpitts oscillator in which the plate-to-grid tank inductance has been replaced by a crystal unit, as shown in figure 1-120. The design of the Pierce oscillator is simpler and less critical than that of any other crystal circuit. As long as $R_{1}$ and $R_{k}$ are large compared with the capacitive reactances shunting them, the Pierce circuit will oscillate with crystal units covering a wide band of frequencies. The use of load resistance, $\mathrm{K}_{1}$, in figure 1-120 (A) aids in maintaining a reasonably flat response over a wide frequency range without the necessity of tuning adjustments other than the switching from one crystal unit to the next. Where a broad frequency range is not required, or where greater activity is necessary, an r-f choke should be used in place of $R_{1}$; otherwise, power approximately equal to $I_{1}{ }^{2} R_{1}$ is simply wasted ( $I_{b}=$ average $d-c$ plate current). But even with this economy, the Pierce oscillator cannot be used to generate as large an output as the Miller circuit. The principal reason is to be found in the fact that the impedance $Z_{v g}$ of the equivalent circuit, which in this case is provided by the crystal unit in parallel with the plate-to-grid capacitance of the tube, must be approximately equal to, or greater than, $Z_{p}$ and $Z_{g}$ combined. Since the impedance of the crystal unit is fixed by its frequency and rated load capacitance, larger plate impedances are possible if the specified crystal impedance is $Z_{\mathrm{g}}$ instead of $Z_{\mathrm{pg}}{ }^{*}$ Thus, for the same crystal current, larger output voltages can be developed across the tank in the Miller than in the Pierce circuit. On the other hand, the effective feed-back phase $Q_{f}$ is greater
if the crystal is not connected between the grid and cathode. This permits the tank to appear more nearly resistive to the tube, so that fluctuations in $R_{0}$ have less influence upon the frequency. Thus, a Pierce oscillator is generally more frequency stable than a Miller oscillator using the same crystal unit. The typical Pierce circuit employs a triode, although screen-grid tubes are usually to be preferred, because the higher $R_{p}$ and the negligible plate-to-grid capacitance serve to improve the frequency stability. The oscillator is generally used at frequencies above 200 kc and below $15,000 \mathrm{kc}$. If an overtone mode is to be excited the oscillator must be made frequency-selective, by replacing $R_{1}$ with an inductor, $\mathrm{L}_{1}$. The inductance of $\mathrm{L}_{1}$ must be such that the antiresonant frequency of $L_{1}$ in parallel with $\mathrm{C}_{1}$ is lower than the operating frequency of the crystal, in order that $Z_{\mathrm{v}}$ will appear capacitive. The use of the inductor-capacitor combination also reduces the harmonic content of the output waveform. If small L/C ratios are used, the effective plate-to-cathode capacitance will be much greater for the overtones than for the fundamental frequency, so that the former are more readily
bypassed to ground than would be the case if no coil were used. In deciding upon the type of oscillator circuit to use, those rule-of-thumb factors most favorable to the selection of a Pierce circuit are:
a. The frequency lies between 200 and $15,000 \mathrm{kc}$.
b. The permitted frequency error is not less than 0.02 per cent, or 0.015 per cent if a regulated voltage supply is available.
c. The oscillator is to be capable of untuned operation over a wide frequency range, simply by switching from one crystal unit to another.
d. Only a small voltage output is required.
e. The oscillator must be of inexpensive design.
f. The oscillator must not be critical in operation, but able to oscillate readily with relatively large deviations in the parameters of the external circuit.
g. Wave shape is not critical.
h. Same as above, except that the permitted frequency error is 0.01 per cent and thermostatic control of the crystal temperature is feasible.
i. Same as above, except that the permitted frequency error is 0.005 per cent, thermostatic control of the temperature is feasible, a regulated voltage supply is available, and the oscillator can be designed to operate at one frequency only.


## ANALYSIS OF LOAD CAPACITANCE, $C_{x}$, IN PIERCE CIRCUIT

1-278. Once that it has been decided to employ a Pierce type oscillator, the standard type of crystal unit is chosen which provides the desired frequency and frequency tolerance and which has been tested according to the Military Standards for parallel-resonance operation. One of the first design considerations is to ensure that the crystal unit will effectively operate into its rated load capacitance, $\mathrm{C}_{x}$. Such operation is necessary, else there can be no assurance that one crystal unit of the same type can replace another and still fall within the drive-level and effective-resistance specifications. For most parallel-resonance crystal units the value of $\mathrm{C}_{x}$ is $32 \mu \mu \mathrm{f}$, although at frequencies under 500 kc , values of $20 \mu \mu \mathrm{f}$ are common. In particular instances, still other values of $\mathrm{C}_{\mathbf{x}}$ are designated. To a first approximation, referring to figure 1-121 (A), the crystal unit operates into a load capacitance equal to $\mathrm{C}_{\mathrm{pg}}$ pius the total of $\mathrm{C}_{\mathrm{g}}$ in series with the parallel combination of $\mathrm{C}_{1}, \mathrm{C}_{\mathrm{p}}$, and the effective inductive impedance presented by the vacuum tube. Since the $\mathbf{Q}$ of the feed-back arm is not infinite, $\mathrm{E}_{\mathrm{p}}$, it will be recalled, must be rotated slightly away from $-\mu \mathrm{E}_{\mathrm{g}}$; the direction is such that for a particular frequency $\mathrm{C}_{\mathrm{p}}+\mathrm{C}_{1}$ must be slightly larger than would otherwise be the case.

Even though the actual equivalent tank circuit is slightly detuned, mathematically the crystal unit is to be in resonance with an effective load capacitance $C_{x}$. (See figure 1-108 (D).) The vacuum tube appears to the tank circuit as a negative resistance having a positive reactive component sufficient to cancel the excess susceptance of $\mathrm{Z}_{\mathrm{p}}$. At equilibrium, the tube can be represented by an equivalent inductance, $L_{T}$, in parallel with a negative resistance, $\rho_{\mathrm{T}}$, as in figure 1-121 (A). Note that $\rho_{T}$ is smaller than $\rho$ of figures 1-121 (C) and (D). This is because $\rho_{T}$ is not connected directly across the crystal, but faces an impedance, approximately $\mathrm{Z}_{\mathrm{L}}$, that is less than the crystal PI. In figure 1-121 (B), $\mathrm{L}_{\mathrm{T}}$ has been replaced by an equivalent negative capacitance, $\mathrm{C}_{\mathrm{n}}$. If $\mathrm{C}_{\mathrm{pg}}$ can be considered negligible, $\mathrm{X}_{\mathrm{e}}{ }^{\prime}$ and $\mathrm{R}_{\mathrm{e}}{ }^{\prime}$ are equal to $\mathrm{X}_{\mathrm{e}}$ and $\mathrm{R}_{\mathrm{e}}$, the equivalent parameters of the crystal unit alone ; otherwise, the values of $\mathrm{X}_{\mathrm{e}}{ }^{\prime}$ and $\mathrm{R}_{\mathrm{e}}{ }^{\prime}$ are based upon the assumption that the shunt capacitance, $\mathrm{C}_{0}$, of the crystal has been increased by an amount equal to $\mathrm{C}_{\mathrm{pr}}$. In figure 1-121 (C), $\mathrm{C}_{\mathrm{o}}$ ( $=\mathrm{C}_{\mathrm{pe}}+\mathrm{C}_{\mathrm{l}}$ ) and $\mathrm{C}_{\mathrm{n}}$ are shown combined into a single plate-to-cathode capacitance, $\mathrm{C}_{\mathrm{b}}{ }^{\prime}$. In figure 1-121 (D), $\mathrm{C}_{\mathrm{p}}{ }^{\prime}$ and $\mathrm{C}_{8}$ are represented by a single load capacitance, $\mathrm{C}_{\mathrm{x}}$. If $\mathrm{C}_{\mathrm{pk}}$ is negligible, $\mathrm{C}_{\mathrm{x}}{ }^{\prime}$ becomes the equivalent load capacitance, $\mathrm{C}_{\mathrm{x}}$, into which the crystal unit operates, and it should be
$C_{p}=C_{p c}+C_{1} \quad C_{x}{ }^{\prime}=\frac{C_{p}{ }^{\prime} \mathrm{C}_{\mathbf{z}}}{\mathrm{C}_{\mathrm{p}}{ }^{\prime}+\mathrm{C}_{\mathrm{p}}}$
$\mathrm{C}_{\mathrm{n}}=\frac{1}{\omega^{2} \mathrm{~L}_{\mathrm{T}}} \quad \rho_{\mathrm{T}}=\left(\frac{\mathrm{X}_{0}^{\prime}+\mathrm{X}_{\mathrm{C}_{\mathrm{u}}}}{\mathrm{X}_{\mathrm{e}}^{\prime}}\right)_{\rho}^{2}$
$C_{p}{ }^{\prime}=C_{p}+C_{a} \quad-\rho=\frac{\left(\mathrm{X}_{e}{ }^{\prime}\right)^{2}}{\mathrm{Re}^{\prime}}=\frac{\mathrm{X}_{\mathrm{e}}{ }^{2}}{\mathbf{R}_{\mathrm{e}}}=\mathrm{PI}$


Figure 1-121. Generalized Pierce oscillator. $X_{0}{ }^{\prime}$ and $R_{d}{ }^{\prime}$ are the effective impedance parameters of the crystal unit based upon the assumption that $C_{p g}$ is a part of $C_{o} . C_{n}$ is an equivalent negative capacitance having a positive reactanse equal to that of $L_{T} . I_{p}$ is the $r$-f plate current of the vacuum tube.
equal to the value specified for the particular crystal. In any event ( $\mathrm{C}_{\mathrm{x}}{ }^{\prime}+\mathrm{C}_{\mathrm{pg}}$ ) is the load capacitance that the crystal unit faces, and which should be equal to the rated value, $C_{x}$. The value of $C_{1}$ includes not only the tuning capacitance in the plate circuit, but also the distributed capacitance of the output leads as well as the effective input capacitance of the next tube. $C_{g}$ is the input capacitance of the oscillator tube. The losses due to $R_{g}$, the effective grid-to-cathode resistance, and to $R_{L}$, the effective load resistance, have been assumed to be negligible compared with those in the crystal unit. These assumptions can be made without appreciable error in a low-power Pierce circuit that requires only a minimum of loading. From an inspection of figure 1-121 it can be seen that in order for a crystal unit to operate into its rated load capacitance, the design must be such that

$$
\begin{equation*}
\mathrm{C}_{\mathrm{x}}=\mathrm{C}_{\mathrm{pg}}+\mathrm{C}_{\mathrm{x}}^{\prime}=\mathrm{C}_{\mathrm{pg}}+\frac{\mathrm{C}_{\mathrm{p}}^{\prime} \mathrm{C}_{\mathrm{g}}}{\mathrm{C}_{\mathrm{p}}^{\prime}+\mathrm{C}_{\mathrm{g}}} \tag{1}
\end{equation*}
$$

## Effect of $C_{p g}$ in Pierce Circuit

1-279. $\mathrm{C}_{\mathrm{pg}}$ effectively increases both the reactance, $X_{e}$, and the resistance, $R_{e}$, of the crystal unit. This does not mean that the true effective $X_{e}$ and $R_{e}$ are changed, for these are fixed by the fact that $X_{e}$ must resonate with the rated load capacitance, $\mathrm{C}_{\mathbf{x}}$. Still, insofar as the impedance from plate-to-grid is concerned, $X_{e}$ and $R_{e}$ effectively have increased values which make it appear that the crystal shunt capacitance is increased by an amount equal to $C_{p g}$. This effect is not desirable, since $R_{e}$ is effectively increased by a greater percentage than $X_{\text {e }}$. (See equations (1) and (2) in figure 1-98 for the effect on $X_{e}$ and $R_{e}$ if $X_{k}$ is held constant but $X_{C o}$ is decreased.) Thus, the larger the value of $\mathrm{C}_{\mathrm{pg}}$, the smaller the $Q$ of the feed-back arm becomes the more the tank circuit must be detuned, the greater must be the value of the negative capacitance, $C_{n}$, and hence the greater the frequency instability due to changes in the tube parameters. The plate-to-grid capacitance needs to be considered only if a triode is used or if the crystal unit is oven-mounted. In the average triode $\mathrm{C}_{\mathrm{pr}}$ is on the order of 1.5 to $2.5 \mu \mu \mathrm{f}$, sufficient to increase the effective value of $\mathrm{C}_{0}$ by as much as 50 per cent in some cases. When the second grid of a tube is used as the oscillator anode, as in the case of pentagrid converters, $C_{p g}$ is usually on the order of $1 \mu \mu$ f. The pin-to-pin capacitance introduced by ovens may be as high as $5 \mu \mu \mathrm{f}$. The $\mathrm{C}_{\mathrm{pk}}$ of screen-grid
tubes can all but be neglected, since the increase in capacitance across the crystal is only about onethousandth of the total. Because of its negligible $C_{p s}$, a pentode is preferred when the frequency deviation must be kept to a minimum. In the remaining discussion of the Pierce circuit, we shall assume that $C_{p k}$ is negligible, so that $X_{r}{ }^{\prime}$ and $R_{e}{ }^{\prime}$ will represent the actual effective impedances of the crystal unit, and $\mathrm{C}_{\mathrm{x}}$ ' will equal the rated capacitance, $C_{x}$. Although we shall employ the unprimed symbols $\mathbf{X}_{\mathbf{e}}$ and $\mathrm{R}_{\mathrm{e}}$ to designate the plate-to-grid impedances, it should be remembered that this is only a convenience, for where $\mathrm{X}_{\mathrm{e}}$ is predetermined by the rated load capacitance and the frequency, $\mathrm{X}_{\mathrm{e}}$ ' necessarily increases or decreases, respectively, with increases and decreases in $\mathrm{C}_{\mathrm{pk}}$. Similarly, $\mathrm{C}_{x}^{\prime}$ varies negatively with $\mathrm{C}_{\mathrm{p}}$, but we shall assume that it is a constant equal to $\mathrm{C}_{\mathrm{x}}$.

## Determination of the Effective Negative Capacitance, $C_{n}$, Introduced by Vacuum Tube in Pierce Circuit

1-280. First, in order to avoid possible confusion, it should be pointed out that the selected reference or zero phase angle of the equivalent circuit in figure 1-119 is not the same as that implicitly assumed in the negative-resistance circuit of figure 1-121 (A). In figure 1-119, the reference phase has been taken as the phase of $\mathrm{E}_{\mathrm{p}}$, whereas in figure $1-121$ (A) it is the phase of the current through the negative resistance $\rho \mathrm{x}$ ( $\operatorname{not} I_{p}$ ), which in turn is the same as the phase of the r-f plate voltage, $\mathrm{E}_{\mathrm{p}}$. Now, $\mathrm{I}_{\mathrm{p}}$, in the negative-resistance circuit, is physically the same as the $I_{p}$ of the vacuum-tube generator circuit. The equivalent current through $\rho_{\mathrm{T}}$ represents that component of $I_{D}$ in phase with $\mathrm{E}_{\mathrm{p}}$ - not that part of $\mathrm{I}_{\mathrm{p}}$ in phase with $-\mu \mathrm{E}_{g}$. The current through the negative resistance is thus smaller in magnitude than the total r-f plate current. The imaginary current through $L_{T}$, or $C_{n}$, is equal and opposite to that component of $I_{p}$ which is 90 degrees out of phase with $\mathrm{E}_{\mathrm{p}}$. In the phasor chart in figure 1-119 (C), the bottom line shows the phase relations that are approached in a Pierce circuit if $R_{p}$ of the tube approaches $Z_{\mathrm{L}}$ in magnitude. Note particularly that $E_{p}$ and $I_{p}$ rotate in opposite directions. $E_{p}$ must lag $I_{p}$ by an angle whose tangent is at least as great as $\frac{\mathbf{R}_{e}}{X_{e}+X_{c s}}$; that is, the tangent of the angle cannot be less than the reciprocal of the $Q_{r}$ of the feed-back arm. The minimum angle occurs when $R_{p}$ is very much greater than the load impedance $Z_{L}$ and the gridleak losses are negligible. On the other hand, the phase difference between $E_{p}$

## Section 1

## Crystal Oseillators

and $I_{p}$ cannot be greater than 90 degrees, for the simple reason that $E_{p}$ is a counter emf produced by $I_{p}$ flowing through an equivalent impedance, $Z_{L}$, which has no component of negative resistance. There is another limitation in that the rotation of $I_{p}$ with respect to $-\mu \mathrm{E}_{\mathrm{g}}$ cannot exceed 90 degrees minus the necessary rotation of $\mathrm{E}_{\mathrm{p}}$ with respect to $-\mu E_{g}$. Otherwise, the necessary rotation of $E_{p}$ cannot occur. As this extreme is approached, $Z_{L}$ approaches a pure reactance approximately equal to $X_{C p}, I_{p}$ approaches a 90 -degree phase lead over $\mathbf{E}_{\mathrm{p}}$, and the apparent $Q$ of the entire plate circuit
(approximately $Z_{L} / R_{p}$ ) approaches the $Q_{t}$ of the feed-back circuit. These maximum and minimum phase angles are summarized in the following table. The phase angles are defined by the absolute values of their tangent expressed in terms of the phase $Q$ of the feed-back arm, $Q_{R}$. Also shown are the limiting Q's of $Z_{L}$ and $\left(Z_{L}+R_{p}\right)$; which respectively determine the phases of $I_{p}$ with respect to $\mathrm{E}_{\mathrm{p}}$ and $-\mu \mathrm{E}_{\mathrm{g}}$. In the last column are shown the limiting values of $C_{n}$ which are discussed in the following paragraph.

| Angle of $\mathrm{E}_{p}$ at all times | With Respect to: |  | Q of: |  | $\stackrel{\mathrm{C}_{\mathrm{a}}}{\text { (Approx) }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{E}_{p}$ | $-\mu \mathrm{E}_{\boldsymbol{E}}$ | $\mathbf{Z}_{\text {L }}$ | $\mathrm{R}_{\mathrm{p}}+\mathrm{Z}_{\mathrm{L}}$ |  |
|  | $0^{\circ}$ | $\tan ^{-1}\left(1 / Q_{k}\right)$ |  |  | $-\mathrm{C}_{\mathrm{p}}\left(\frac{1}{Q_{\mathrm{f}}{ }^{2}}+\frac{\mathrm{R}_{\mathrm{e}}}{\mathrm{R}_{\mathrm{p}}+\mathrm{R}_{\mathrm{e}}}\right)$ |
| Minimum angle of $\mathrm{I}_{p}$ | $\tan ^{-1}\left(1 / Q_{k}\right)$ | $0^{\circ}$ | $1 / Q_{t}$ | 0 | $-\mathrm{C}_{\mathrm{p}} / \mathrm{Q}_{\mathrm{t}}{ }^{2}$ |
| Maximum angle of $\mathrm{I}_{\mathrm{p}}$ | $90^{\circ}$ | $\tan ^{-1}\left(Q_{t}\right)$ | $\infty$ | Qt | $-\frac{C_{p} R_{e}}{R_{p}+R_{e}}$ |

1-281. The approximate expressions given in the table above for the limiting values of $\mathrm{C}_{\mathrm{n}}$ are derived upon the assumption that the unsigned phase angle between $I_{p}$ and $E_{p}$ is given by the equation

$$
\begin{align*}
& \tan ^{-1}\left(\frac{X_{Z_{L}}}{R_{z_{i}}}\right)=\tan ^{-1}\left(\frac{1}{Q_{i}}\right)+ \\
& \tan ^{-1}\left(\frac{X_{Z_{L}}}{R_{p}+R_{Z_{L}}}\right) \tag{1}
\end{align*}
$$

where $\mathbf{X}_{\mathrm{Z}_{L}}$ and $\mathrm{R}_{\mathrm{zc}}$ are the absolute values of the equivalent series reactance and resistance whose vector sum is equal to $Z_{L} ; \tan ^{-1}\left(\frac{1}{Q_{f}}\right)$ is the unsigned phase difference between $E_{p}$ and $-\mu E_{g}$, and $\tan ^{-1}\left(\frac{X_{z_{t}}}{R_{p}+R_{z_{L}}}\right)$ is the unsigned phase difference in the opposite direction between $I_{p}$ and $-\mu E_{r}$. From equation (1) it follows that

$$
\begin{array}{r}
\frac{X_{\mathbf{z L}_{L}}}{\mathbf{R}_{\mathrm{z}_{L}}}=\tan \left[\tan ^{-1}\left(\frac{1}{Q_{t}}\right)+\tan ^{-1}\left(\frac{\mathbf{X}_{\mathbf{z}_{L}}}{\mathbf{R}_{\mathrm{p}}+\mathbf{R}_{\mathrm{zL}_{L}}}\right)\right] \\
1-281(2)
\end{array}
$$

On applying the general trigonometric equation for the tangent of the sum of two angles

$$
\tan (x+y)=\frac{\tan x+\tan y}{1-\tan x \tan y}
$$

Letting $\tan x=1 / Q_{i}$ and $\tan y=\frac{X_{Z_{L}}}{R_{p}+R_{z_{L}}}$, equation (2) becomes

$$
\begin{align*}
\frac{X_{Z_{L}}}{R_{Z_{L}}} & =\frac{\frac{1}{Q_{t}}+\frac{X_{Z_{L}}}{R_{p}+R_{Z_{L}}}}{1-\frac{X_{Z_{L}}}{Q_{i}\left(R_{p}+R_{Z_{L}}\right)}} \\
& =\frac{R_{p}+R_{Z_{L}}+Q_{Q_{t}} X_{Z_{L}}}{Q_{t} R_{p}+Q_{t} R_{Z_{L}}-X_{Z_{L}}} \tag{3}
\end{align*}
$$

On rearranging, equation (3) can be expressed as an equation for $R_{p}$ :


Figure 1-122. Generclized Pierce oscillator. $X_{x_{L}}$ and $X_{c n}$ represent the positive magnitudes of the equivalent reactances of the load and the dynamic effects of the fube, respectively. $\rho_{Y}$ is the same as the $p_{Y}$ in figure 1-121

Note that for oscillations to be maintained, $\mathrm{Q}_{\mathrm{t}} \mathrm{X}_{\mathrm{z}}$ must be greater than $R_{z L}$, else $R_{D}$ becomes negative. Referring to figure $1-122$, the effective admittance of the $\mathrm{Z}_{\mathrm{L}}$ and $\mathrm{X}_{\mathrm{C}_{\mathrm{n}}}$ branches in parallel is equal to $\frac{1}{\mathrm{R}_{\mathrm{zL}}-j \mathrm{X}_{\mathrm{z}_{\mathrm{L}}}}+\frac{1}{j \mathrm{X}_{\mathrm{Ca}}}$. From this expression it can be shown by straightforward manipulation that if the reactive component of the admittance is to be zero

$$
\begin{equation*}
\mathrm{X}_{\mathrm{Cu}_{\mathrm{u}}} \mathrm{X}_{\mathrm{ZL}}=\mathrm{R}_{\mathrm{zu}}{ }^{2}+\mathrm{X}_{\mathrm{z}_{\mathrm{L}}}{ }^{2}=\mathrm{Z}_{\mathrm{L}}{ }^{2} \quad 1-281 \tag{5}
\end{equation*}
$$

On substitution of equation (5) in equation (4) and rearranging

$$
\begin{equation*}
X_{C_{n}}=R_{p}\left(Q_{\mathrm{t}}-\frac{R_{\mathrm{z}_{\mathrm{z}}}}{\mathbf{X}_{\mathrm{z}_{\mathrm{L}}}}\right) \tag{6}
\end{equation*}
$$

The values of $C_{n}$ as listed at the end of paragraph $1-280$ are obtained from equation (6) by substituting the values of $\mathrm{Q}_{\mathrm{t}}$ and $\mathrm{R}_{\mathrm{z}_{\mathrm{L}}} / \mathrm{X}_{\mathrm{z}_{\mathrm{c}}}$ when these are expressed in terms of the basic circuit parameters. In paragraph 1-289, it is shown that at equilibrium:

$$
\begin{equation*}
X_{C_{p}}+X_{C z}+X_{0}+\frac{R_{e} X_{C_{p}}}{R_{p}}=0 \quad 1-289 \tag{3}
\end{equation*}
$$

The term, $\frac{\mathbf{R}_{\mathbf{o}} \mathbf{X}_{\mathrm{C}_{\mathrm{p}}}}{\mathbf{R}_{\mathrm{p}}}$, accounts for that part of the negative capacitance which is necessary to compensate for the phase shift in $I_{p}$, but not for that part which compensates for the phase shift of $\mathrm{E}_{\mathrm{p}}$. For example, if $\mathrm{R}_{\mathrm{p}}$ were infinite, the phase shift of $I_{p}$, would be zero, and likewise the term, $\frac{R_{0} X_{C_{p}}}{R_{p}}$,
in equation 1-289 (3). Nevertheless, $\mathrm{E}_{\mathrm{p}}$ must still be rotated by an angle equal to $\tan ^{-1}\left(\frac{1}{Q_{t}}\right)$, so that the tank cannot actually be parallel-resonant. Some value must be assigned to the negative capacitance, for the apparent resonance to hold in the generalized negative-resistance circuit. Now,

$$
\mathrm{Z}_{\mathrm{L}}=\frac{\mathrm{Z}_{\mathrm{p}} \mathrm{Z}_{\mathrm{pgc}}}{\mathrm{Z}_{\mathrm{p}}+\mathrm{Z}_{\mathrm{pge}}}
$$

Letting

$$
{ }^{*} \mathrm{Z}_{\mathrm{p}}=\mathrm{j} \mathrm{X}_{\mathrm{C}_{\mathrm{p}}}
$$

and

$$
\begin{aligned}
\mathrm{Z}_{\mathrm{pgo}} & =\mathrm{R}_{\mathrm{e}}+j\left(X_{\mathrm{e}}+X_{\mathrm{C}_{\mathbf{s}}}\right) \\
& =R_{\mathrm{e}}-j\left(X_{C_{p}}+\frac{R_{e} X_{C_{p}}}{R_{\mathfrak{p}}}\right)
\end{aligned}
$$

we can express $\mathrm{Z}_{\mathrm{L}}$, as a complex function equal to $\mathrm{R}_{\mathrm{z}_{\mathrm{L}}}-\mathrm{jX}_{\mathrm{z}_{\mathrm{L}}}$, where $\mathrm{X}_{\mathrm{z}_{\mathrm{L}}}$ is still assumed to be unsigned. Thus,
(complex) $Z_{L}=\frac{j X_{C_{p}}\left[R_{e}-j X_{C_{p}}\left(\frac{R_{p}+R_{p}}{R_{p}}\right)\right]}{R_{e}-\frac{j X_{C_{p}} R_{e}}{R_{p}}}$
On multiplying both numerator and denominator by $\left(R_{e}+\frac{j X_{C_{p}} R_{e}}{R_{p}}\right)$, we find that

$$
\mathrm{R}_{\mathrm{zL}}=\frac{\mathrm{X}_{\mathrm{C}_{\mathrm{D}}}{ }^{2}}{\mathrm{R}_{\mathrm{e}}\left(1+\frac{\mathrm{X}_{\mathrm{C}_{\mathrm{p}}}{ }^{2}}{\mathrm{R}_{\mathrm{p}}^{2}}\right)}=\frac{\mathrm{X}_{\mathrm{C}_{\mathrm{p}}}{ }^{2}}{\mathrm{R}_{\mathrm{e}}}
$$

and

$$
\begin{align*}
& =\frac{\left|X_{C_{p}}\right|\left(R_{e} R_{p}+X_{C_{p}}{ }^{2}\right)}{R_{e} R_{p}} \tag{8}
\end{align*}
$$

So

$$
\begin{align*}
\frac{R_{Z_{L}}}{X_{Z_{L}}} & =\frac{\left|X_{C_{p}}\right| R_{p}^{2}}{R_{e} R_{p}^{2}+X_{C_{p}}^{2}\left(R_{p}+R_{e}\right)} \\
& =\frac{\left|X_{C_{p}}\right| R_{p}}{R_{e} R_{p}+X_{C_{p}}^{2}} \tag{9}
\end{align*}
$$

Also, when assuming that the grid losses are negligible,

$$
\begin{equation*}
Q_{t}=\frac{X_{\mathrm{a}}+X_{C_{\mathrm{e}}}}{R_{\mathrm{e}}}=\frac{\left|X_{C_{\mathrm{p}}}\right|\left(\mathrm{R}_{\mathrm{p}}+\mathrm{R}_{\mathrm{e}}\right)}{\mathrm{R}_{\mathrm{o}} \mathrm{R}_{\mathrm{p}}} \tag{10}
\end{equation*}
$$

The expression on the right in equation (10) is obtained by substitution from equation $1-289$ (3). On substituting equations (9) and (10) in equation (6), we have
$X_{C_{n}}=$
$\left|X_{C p}\right|\left[\frac{R_{p}+R_{e}}{R_{e}}-\frac{R_{p}^{2}}{R_{e} R_{p}+X_{C p}{ }^{2}\left(1+R_{e} / R_{p}\right)}\right]$
$X_{C_{n}}=\left|X_{C p}\right|$
$\left[\frac{R_{p} X_{C_{p}}{ }^{2}\left(1+R_{e} / R_{p}\right)+R_{e}{ }^{2} R_{p}+R_{e} X_{C_{p}}{ }^{2}\left(1+R_{e} / R_{p}\right)}{R_{e}{ }^{2} R_{p}+R_{e} X_{C_{p}}{ }^{2}\left(1+R_{e} / R_{p}\right)}\right]$
1-281 (11)
Equation (11) is obtained by using the exact values of $R_{Z_{L}} / X_{Z_{t}}$ and $Q_{t}$ as given by equations (9) and (10). Although the equation for $X_{c a}$ involves the difference between two nearly equal terms, the error introduced by using the approximate values of $Q_{t}$ and $R_{Z_{L} /} / X_{Z_{k}}$ is negligible for all practical purposes as long as $R_{p} \gg R_{\text {e }}$.

Now,

$$
C_{n}=-\frac{1}{\omega X_{C n}}
$$

so, on substitution of equation (11),

$$
\begin{aligned}
& C_{n}=-C_{p} \\
& {\left[\frac{R_{e}{ }^{2} R_{p}+R_{e} X_{C_{p}}{ }^{2}\left(1+R_{e} / R_{p}\right)}{R_{p} X_{C_{p}}{ }^{2}\left(1+R_{\mathrm{e}} / R_{p}\right)+R_{e}{ }^{2} R_{p}+R_{e} X_{C_{p}}{ }^{2}\left(1+R_{e} / R_{p}\right)}\right]} \\
& \text { 1-281 (12) }
\end{aligned}
$$

In the practical case, $R_{p}$ is much greater than $R_{e}$ and $X_{C_{n}}{ }^{2}$ is much greater than $R_{e}{ }^{2}$, so that the approximate equation for $C_{n}$ becomes

$$
\begin{align*}
\mathrm{C}_{\mathrm{n}} & =-\mathrm{C}_{\mathrm{p}}\left[\frac{\mathrm{R}_{\mathrm{e}}^{2} \mathrm{R}_{\mathrm{p}}+\mathrm{R}_{\mathrm{e}} \mathrm{X}_{\mathrm{C}_{\mathrm{p}}}{ }^{2}}{\mathrm{R}_{\mathrm{v}}\left(\mathrm{X}_{\mathrm{C}_{\mathrm{p}}^{2}}+\mathrm{R}_{\mathrm{s}}^{2}\right)}\right] \\
& =-\mathrm{C}_{\mathrm{p}}\left(\frac{1}{\mathrm{Q}_{\mathrm{t}}{ }^{2}}+\frac{\mathrm{R}_{\mathrm{e}}}{\mathrm{R}_{\mathrm{p}}+\mathrm{R}_{\mathrm{e}}}\right) \tag{13}
\end{align*}
$$

The last term on the right inside the parentheses is obtained by assuming that $\frac{X_{C_{p}}{ }^{2}}{X_{O_{D}}{ }^{2}+R_{0}{ }^{1}}$ is more nearly equal to $\frac{R_{p}}{R_{p}+R_{e}}$ than to 1 . We make this assumption arbitrarily for the convenience in remembering the limiting values of $C_{n}$. That part of $C_{n}$ which is necessary so as to compensate for the phase shift of $E_{p}$ with respect to $-\mu E_{g}$ is approximately equal to $-\mathrm{C}_{\mathrm{p}} / \mathrm{Q}_{\mathrm{t}}{ }^{2}$; whereas the part necessary to compensate for the phase shift of $I_{p}$
with respect to $-\mu E_{g}$ is approximately equal to $\frac{-C_{p} R_{e}}{R_{p}+R_{e}}$. It is this latter component that is accounted for by the term, $\frac{X_{c_{p}} R_{e}}{R_{p}}$, in equation 1-289 (3). By equation (12), when $R_{p} / Z_{L}$ approaches infinity, the limiting value of $\mathrm{C}_{\mathrm{n}}$ is found to be
$\underset{\left(R_{p} / Z_{L} \rightarrow \infty\right)}{C_{n}}=\frac{-C_{p} R_{e}{ }^{2}}{X_{C_{p}}{ }^{2}+R_{e}{ }^{2}}=\frac{-C_{p}}{Q_{t}{ }^{2}}$
1-281

When $R_{p} / Z_{\text {L }}$ approaches its smallest possible value, the ratio $R_{z_{L}} / X_{Z_{L}}$ becomes negligible compared with $Q_{f}$, so that $X_{C m}$ by equation (6) is approximately equal to $Q_{R} R_{p}$. Substituting equation
(10) for $Q_{t}$, we have, when $\left(\frac{X_{Z_{t}}}{R_{p}+R_{Z_{L}}} \rightarrow Q_{t}\right)$

$$
\begin{align*}
C_{n} & =\frac{-1}{\omega X_{C a}}=\frac{-1}{\omega Q_{1} R_{p}} \\
& =-\frac{R_{e}}{\omega\left|X_{C_{p}}\right|\left(R_{p}+R_{e}\right)}  \tag{15}\\
& =\frac{-C_{p} R_{e}}{R_{p}+R_{e}}
\end{align*}
$$

As indicated in figure 1-121, the total effective plate capacitance is

$$
\begin{equation*}
C_{p}^{\prime}=C_{p}+C_{n}=C_{p}\left(1-\frac{1}{Q_{f}^{2}}-\frac{R_{e}}{R_{p}+R_{s}}\right) \tag{16}
\end{equation*}
$$

When $R_{p} \gg Z_{L}$, the $Q$ of $Z_{L}$ approaches $1 / Q_{f}$ in value and

$$
\begin{equation*}
C_{D}^{\prime}=C_{p}\left(1-\frac{1}{Q_{1}^{2}}\right) \tag{17}
\end{equation*}
$$

When $R_{p}$ is small compared with $X_{C_{p}}{ }^{2} / R_{a}$, then $R_{z_{L}} / X_{z_{L}}$ becomes small compared with $Q_{t}$ and

$$
\begin{equation*}
C_{p}^{\prime}=\frac{C_{p} R_{p}}{R_{p}+R_{e}} \tag{18}
\end{equation*}
$$

$R_{p}$ is normally much greater than $R_{\text {e }}$. Only lowfrequency crystals have effective resistances which approach in value the plate resistances of low-power vacuum tubes. For all practical purposes in the average Pierce circuit, $C_{p}^{\prime}$ can be assumed to equal $C_{p}$, the static plate capacitance, except when considering problems of frequency stability. What is important to note in the limiting equations for $C_{n}$ is the fact that if the tank is to
be operated well off resonance, $R_{p}$ becomes quite an important factor in determining the frequency. In this case, because $C_{n}$ is relatively large, any variation in the tube $R_{v}$, has a great effect upon the frequency. It should be remembered that the parameter $Q_{t}$ has been used to account for the required rotation of $\mathrm{E}_{\mathrm{p}}$ with respect to $-\mu \mathrm{E}_{\mathrm{g}}$. Insofar as the gridleak is effective in increasing the necessary phase shift, $Q_{i}=\frac{X_{e}+X_{C r}}{R_{e}}$ cannot be assumed, and the complete equation 1-272 (1) must be used.
THE EFFECT OF $R_{p}$ UPON THE
FREQUENCY OF PIERCE CIRCUIT
1-282. It can be seen that for large values of the $R_{\mathrm{w}} / \mathrm{Z}_{\mathrm{L}}$ ratio, $\mathrm{C}_{\mathrm{n}}$ is small and its percentage variation with changes in $R_{p}$ is smaller still. $C_{n}$ is, effectively, a frequency-determining parameter, but more exactly it is a mathematical function that indirectly expresses the effect of $R_{p}$ and $Q_{t}$ upon the frequency. The smaller the $Q_{t}$ and $R_{p}$, the larger is $C_{n}$; and the larger $C_{n}$, the greater is the effect of $R_{p}$. Since $R_{p}$ is subject to change with changes in the tube voltages, tube aging, and the like, it is important to keep $\mathrm{C}_{n}$ as small as possible. This can be done by designing the circuit to operate with as high of value of tube $R_{p}$ as is practicable. For a given tube, the higher values of an effective $R_{p}$ are to be obtained when the tube is conducting during only a small fraction of a cycle. This in turn requires that the oscillator tube be operated class $C$, so that a larger grid bias than otherwise is required. However, if the crystal drive level is to be kept low and if the gridleak is to have a negligible effect on the effective $Q_{\text {f }}$, and hence upon $C_{n}$, the gridleak resistance must be as large as practicable without running the risk that the tube will block or operate intermittently. The limiting value of $R_{p}$ occurs when $-\mu \mathbf{E}_{\mathrm{g}}$ is just sufficient to maintain oscillations. If the vacuum tube could operate into a pure resistance, $I_{p}$ would be in phase with $-\mu \mathrm{E}_{k}$, and $R_{p}$ would be eliminated as a frequency-determining element. In the conventional Pierce circuit this could occur only if $Q_{\mathrm{f}}$ were infinite.
Phase-Stabilized Pierce Circuit
1-283. If an inductor is inserted in the plate circuit of the oscillator, as indicated in figure 1-123, having a reactance equal and opposite to the effective reactance $X_{z L}$, then $I_{p}$, undergoes no phase rotation, and changes in $R_{p}$, although affecting the activity, will have little effect upon the frequency. With $I_{b}$ in phase with $-\mu E_{u}$, the $Q$ of $Z_{L}$ must equal $1 / Q_{f}$, and the operation of the tank is the same as it would be if $R_{p}$ were infinite. If $Q_{t}$ is reasonably large and is approximately equal to $\left|\mathrm{X}_{\mathrm{CD}} / \mathrm{R}_{\mathrm{e}}\right|$,

$$
R_{R_{L}}=Z_{L}=X_{C p}^{2} / R_{e}=\left|X_{C p}\right| Q_{i}
$$



Figure 1-123. Coil inserted in plate circuit of Pierce oscillator to prevent phase of $I_{p}$ from being influenced by changes in $R_{p}$
Since

$$
\mathbf{X}_{\mathbf{z}_{2}} / \mathbf{R}_{\mathbf{z}_{1}}=1 / \mathbf{Q}_{\mathrm{t}}
$$

$X_{Z L}$ is approximately equal in magnitude to $X_{C p}$. Thus, for the vacuum tube to look into a resistive load, the inductor should have a reactance approximately equal in magnitude to $\mathrm{X}_{\mathrm{r}_{1}, \text {. This value as- }}$ sumes that the gridleak and output losses are negligible. When such assumptions cannot be made, the value of the series plate reactance becomes a more involved function. Llewellyn analyzed this type of circuit and eliminated $R_{p}$ from the frequency-determining equation (phase rotation equation) by equating the sum of the factors of $R_{p}$ to zero. Although the approach is different and the grid losses are assumed to be predominant, Llewellyn's mathematical elimination of the effects of $R_{n}$ upon the frequency by the introduction of a plate inductor in series with the tank appears to be equivalent to the qualitative condition that $I_{p}$, must be held in phase with $-\mu \mathrm{E}_{\mathrm{s}}$. The experimenter, nevertheless, should be warned that the theory of this type of stabilization has been analyzed above, and also by Llewellyn, only in terms of the phase relations. Difficulty will probably be experienced in obtaining stable oscillations without additional modifications to ensure that the limiting characteristics are changed from a voltage- to a current-controlled nature. This feature of oscillator theory has not been fully explored, but see paragraphs 1-585 to 1-598 for a general discussion, and paragraph 1-323 for a particular example of an attempt, which was not entirely successfu', to phase-stabilize a Pierce circuit.
Conditions for Maximum $R_{p}$ in Pierce Circuit 1-284. Referring to figures 1-119 (A) and (B), we shall begin with the assumption that the tank is operating near resonance so that $Z_{L} \approx \frac{Z_{p}{ }^{2}}{R_{e}}$, where $R_{\text {e }}$ (not shown) is the effective resistance of the crystal unit whose total impedance is represented by $Z_{p r} . Z_{L}$, therefore, is very nearly resistive, and $I_{k}$ is approximately equal in magnitude to the current through $Z_{p}$.

$$
\text { Thus, } I_{g} \approx E_{p} / Z_{p}
$$

Section 1 Crystal Oscillators

$$
\begin{gathered}
\text { also, } E_{g}=I_{q} Z_{g}=\frac{E_{p} Z_{g}}{Z_{p}} \\
\text { Rearranging, } E_{p} / E_{g}=\frac{Z_{p}}{Z_{q}}=C_{q} / C_{p}
\end{gathered}
$$

In the interest of maxium stability it is desirable for $R_{p}$ to be a maximum. The problem is to find what capacitance ratio, $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$, permits the largest possible value of $R_{p}$ consistent with the rated drive level and load capacitance of the crystal unit. The phase-rotation equations do not enter the problem -only those equations that concern the magnitude of the equilibrium voltages and currents are of concern now. The crystal specifications indirectly set an upper limit for the tank current, $I_{s}$. Thus, the output voltage, $\mathrm{E}_{\mathrm{p}} \approx \mathrm{I}_{\mathrm{g}} \mathrm{Z}_{\mathrm{p}}$, also has an upper limit, since $Z_{\mathrm{p}}\left(=\mathrm{Z}_{\mathrm{pg}}-\mathrm{Z}_{\mathrm{g}}\right)$ has a theoretical maxi-
mum equal to $\mu Z_{\mathrm{K}}=\frac{\mu Z_{\mathrm{N}}}{\mu+1} \approx \frac{\mu X_{c}}{\mu+1}$, which is approached as $R_{p}$ approaches zero. At the other ideal extreme, $Z_{p}$, and $Z_{L}$ approach zero and the $R_{p} / Z_{L}$ ratio becomes very large. Now, a large $R_{p} / Z_{L}$ is desired, but some compromise must be made, since the $Q$ of the feed-back circuit becomes increasingly small as $Z_{g}$ approaches $Z_{\mathrm{pg}}$ in magnitude. A rigorous treatment of the problem to find that relation between $\mathrm{R}_{\mathrm{i}} / \mathrm{Z}_{\mathrm{L}}$ and $\mathrm{Q}_{\mathrm{r}}$ that provides an optimum frequency stability would require that a complete equation of frequency stability be established and that those impedance relations be determined that produce a minimum frequency deviation for small changes in the circuit parameters. Equation (2) in paragraph 1-288, which is a first order expression for the fractional change in frequency for a change in $R_{p}$, indicates that the percentage deviation increases directly with the first power of $C_{p}$, and inversely with the second power of $R_{p}$. This suggests that the stability increases as long as $C_{p} / R_{p}{ }^{2}$ decreases with an increase in $\mathrm{C}_{\mathrm{p}}$, and is a maximum at the value of $\mathrm{C}_{\mathrm{p}}$, if existent, at which this ratio begins to increase. Such an approach will not be attempted here. Unless all the characteristic curves of a vacuum tube are available, so that either $\mu, \mathrm{R}_{\mathrm{p}}$, or $\mathrm{g}_{\mathrm{m}}$ can be used as an independent variable to eliminate the other two from the equations, concrete conclusions cannot be reached concerning the optimum design of an oscillator using that particular tube. A more qualitative analysis is presented below, and although the indicated optimum relations cannot be considered conclusive, they can serve as first approximations. All impedance, current, and voltage symbols given below are considered positive and undirected.

$$
\text { Now, } E_{p}=I_{p} Z_{L}
$$

$$
\begin{gathered}
\text { And } I_{p}=\frac{\mu E_{q}}{R_{p}+Z_{L}}=\frac{\mu E_{p} Z_{z}}{Z_{p}\left(R_{p}+Z_{L}\right)} \\
\text { So } E_{p}=\frac{\mu E_{p} Z_{z} Z_{L}}{Z_{p}\left(R_{p}+Z_{L}\right)} \\
\text { or } \mu Z_{z} Z_{L}-R_{p} Z_{p}=Z_{p} Z_{L}
\end{gathered}
$$

On substituting $\left(R_{p} g_{m}\right)$ for $\mu$, where $g_{m}$ is the transconductance of the tube,

$$
\begin{align*}
& R_{p} \mathrm{~g}_{\mathrm{m}} Z_{\mathrm{z}} Z_{L}-R_{p} Z_{p}=Z_{p} Z_{L} \\
& \quad \text { or } R_{p}=\frac{Z_{p} Z_{L}}{g_{m} Z_{g} Z_{L}-Z_{p}} \quad 1-284 \tag{1}
\end{align*}
$$

Dividing both sides by $\mathbf{Z}_{\mathrm{L}}$, we have

$$
\frac{R_{p}}{Z_{L}}=\frac{Z_{p}}{g_{m} Z_{g} Z_{L}-Z_{p}}=\frac{1}{\frac{g_{m} Z_{g} Z_{L}}{Z_{p}}-1}
$$

Our present concern is to seek the largest practical value of $R_{p} / Z_{L}$, so that the phase of $I_{p}$ will be least affected by small changes in $R_{p}$. Now, $Z_{q} \approx Z_{p g}-Z_{p}$, where $Z_{p y}$ represents the predetermined crystal impedance, which is approximately equal to $\mathbf{X}_{\text {. }}$. Also, $\mathrm{Z}_{\mathrm{L}} \approx \mathrm{Z}_{\mathrm{p}}{ }^{2} / \mathrm{R}_{\mathrm{e}}$. On substitution of these values in the equation for $R_{p} / Z_{L}$, it is found that

$$
\frac{R_{p}}{Z_{\mathrm{L}}}=\frac{\mathrm{R}_{\mathrm{e}}}{\mathrm{~g}_{\mathrm{m}} \mathrm{Z}_{\mathrm{p}} \mathrm{Z}_{\mathrm{g}}-\mathrm{R}_{\mathrm{s}}}=\frac{\mathrm{R}_{\mathrm{s}}}{\mathrm{~g}_{\mathrm{m}}\left(\mathrm{Z}_{\mathrm{p}} Z_{p}-\mathrm{Z}_{\mathrm{p}}^{2}\right)-\mathrm{R}_{\mathrm{e}}} 1-284(2)
$$

It can be seen from equation (2) that for oscillations to be maintained $g_{m}\left(Z_{p r} Z_{p}-Z_{1}{ }^{2}\right)$ must be greater than $R_{0}$. A maximum $R_{p} / Z_{L}$ ratio is approached as the product $\mathrm{g}_{\mathrm{m}}\left(\mathrm{Z}_{\mathrm{rg}} \mathrm{Z}_{\mathrm{p}}-\mathrm{Z}_{\mathrm{v}}{ }^{2}\right)$ approaches the value of $R_{e}$. Of course, it is impossible for the denominator in equation (2) to be actually equal to zero, for then $R_{p}$ would be infinite; but it is plausible to assume that a denominator much smaller than the value of $R_{e}$ can be realized. Thus, we can write

$$
\begin{equation*}
\text { (optimum) } \mathrm{g}_{\mathrm{m}}=\frac{\mathrm{R}_{\mathrm{o}}}{\mathrm{Z}_{\mathrm{pg}} Z_{p}-Z_{\mathrm{p}}{ }^{2}}=\frac{\mathrm{R}_{\mathrm{s}}}{\mathrm{Z}_{\mathrm{p}} Z_{\mathrm{s}}} \tag{3}
\end{equation*}
$$

The more nearly this equality is approached, the greater will be the frequency stability. The question arises, is it preferable to seek this equality with a small or a large value of $g_{m}$ ? Assuming that
( $\left.R_{p} / Z_{L}\right) \gg 1$, the equation, $I_{v}=\frac{\mu E_{k}}{R_{p}+Z_{L}}$, can be written approximately $I_{p}=\mu \mathrm{E}_{\mathrm{q}} / \mathrm{R}_{\mathrm{p}}=\mathrm{g}_{\mathrm{m}} \mathrm{E}_{\mathrm{g}}$, or $\mathrm{g}_{\mathrm{m}}=\mathrm{I}_{\mathrm{p}} / \mathrm{E}_{\mathrm{r}}$. A large $\mathrm{g}_{\mathrm{m}}$ means a large r -f plate current for a given excitation voltage. This would be desirable from the point of view of maximum output, but an examination of the denominator in equation (3) shows that a large transconductance means that the plate impedance, $\mathrm{Z}_{\mathrm{p}}$, or the grid impedance, $\mathrm{Z}_{8}$, must be made small if the equation is to hold. A small $\mathrm{Z}_{8}$ (large $\mathrm{Z}_{\mathrm{p}}$ ) means a large $\mathrm{Z}_{\mathrm{L}}$ and also a large $\mathrm{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{z}}$ ratio. Both consequences are incompatible with a large $\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{L}}$ ratio. The former is obviously so, and the latter is implicitly so because the ratio of $E_{p} / E_{s}$ times $\frac{R_{p}+Z_{L}}{Z_{L}}$ $\left(=\frac{\mu \mathrm{E}_{\mathrm{g}}}{\mathrm{E}_{\mathrm{p}}}\right)$ must equal $\mu$. Every increase in $\mathrm{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{s}}$ therefore requires an approximately proportional decrease in the $\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{L}}$ ratio, insofar as $\mu$ can be assumed to remain constant. On the other hand, a large $Z_{g}$ and small $Z_{p}$ permits a large $R_{p} / Z_{L}$ ratio and has the additional advantage of permitting a given excitation voltage with a minimum crystal current. It is under these conditions that equation (3) will be most nearly exact. There are serious disadvantages, however, when operating at a maximum $R_{p} / Z_{L}$ ratio; the most important of which is that the Q of the feed-back circuit rapidly decreases as $Z_{\mathbf{g}}$ is increased, since $Q_{t} \approx \frac{Z_{p s}-Z_{R}}{\mathbf{R}_{\mathbf{*}}}$. Also, the voltage output is weak, and has a tendency to instability. This will be discussed more fully later. Since the excitation voltage is stronger for a given crystal current, the grid losses increase proportionately and may no longer be negligible. Furthermore, unless the tube is operated class $C$, the power efficiency is very low. These last mentioned disadvantages, nevertheless, are minor compared with the effect on $Q_{\text {r }}$. The minimum effective $\mathbf{Q}$ of the average crystal unit when operating into its rated load capacitance is not unduly large. A grid-to-cathode reactance equal in magnitude to threefourths $X_{0}$ reduces $Q_{t}$ to one-fourth $Q_{e}$. Since the purpose of a large $\mathrm{K}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{L}}$ ratio is to permit the entire plate-circuit impedance ( $\mathrm{R}_{\mathrm{r}}+\mathrm{Z}_{\mathrm{L}}$ ) to appear as nearly resistive as possible, the better stability risk is to operate the parallel-resonant oscillator with small rather than large $I_{p}$ and $g_{m}$. Since we are assuming that $g_{m} \approx I_{p} / E_{p}$ it can be seen that the smaller the value of $\mathrm{g}_{\mathrm{m}}$, the smaller is the r-f plate current for a given excitation voltage, or, for a given plate current, the smaller the value of $\mathrm{g}_{\mathrm{m}}$, the greater the excitation voltage. The problem becomes one of determining what capacitance ratio, $\mathrm{C}_{\mathrm{s}} / \mathrm{C}_{\mathrm{p}}$, permits the smallest possible
$\mathrm{g}_{\mathrm{m}}$. By equation (3), $\mathrm{g}_{\mathrm{m}}$ is a minimum when the denominator of the right-hand term is a maximum. Since the impedance of the crystal unit, $\mathrm{Z}_{\mathrm{pk}}$, is to be held constant, $\left(Z_{v}+Z_{k}\right)$ is also a constant. Thus, the product $Z_{1} Z_{g}$ can easily be shown to be a maximum when

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{p}}=\mathrm{Z}_{\mathrm{g}}=\mathrm{Z}_{\mathrm{pg}} / 2 \tag{4}
\end{equation*}
$$

$$
1-284
$$

A maximum operating $R_{p}$ and a minimum $I_{D}$ with a given excitation voltage can thus be obtained when the capacitance and voltage ratios are

$$
E_{\mathrm{v}} / \mathrm{E}_{\mathrm{g}}=\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}=1
$$

It is quite fortunate that $\mathrm{g}_{\mathrm{m}}$ has a minimum value. At all other operating values a small change in the $\frac{C_{g}}{C_{p}}$ ratio causes $g_{\mathrm{m}}$ and $R_{p}$, and hence the frequency, to change. At the minimum $g_{m}$ the rate of change in the tube parameters is necessarily zero, so that the stability in this respect is a maximum. When the more exact equation 1-289 (2) is used instead of equation (1) above, and when $\mu / R_{p}$ is substituted for $\mathrm{g}_{\mathrm{m}}$, it can be shown that

$$
\begin{equation*}
\mathbf{R}_{\mathrm{p}}=\frac{\mathrm{X}_{\mathrm{C}_{\mathrm{p}}} \mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{C}_{\mathrm{p}}} \mathrm{X}_{\mathrm{C}_{\mathrm{s}}}+\mu \mathrm{X}_{\mathrm{C}_{\mathrm{p}}} \mathrm{X}_{\mathrm{C}_{\mathrm{R}}}}{\mathbf{R}_{\mathrm{e}}} \tag{5}
\end{equation*}
$$

Note that $\mathrm{R}_{\mathrm{p}}$ as long as $\mu$ is constant, is inversely proportional to $\mathrm{R}_{\mathrm{e}}$. Now, approximately

$$
X_{C_{p}}=-\left(X_{0}+X_{C_{k}}\right)
$$

Substituting in equation (5), $R_{p}$ becomes a function of $\mathbf{X}_{e}, R_{e,} \mu$, and $X_{C g}$. Assuming that the first three parameters are constant, it can be shown that $R_{p}$ is a maximum when

$$
X_{C}=-\frac{X_{\mathrm{e}}(\mu+2)}{2(\mu+1)}=-\frac{X_{e}}{2}\left(1+\frac{1}{\mu+1}\right)
$$

$$
1-284 \text { (6) }
$$

If $(\mu+1) \gg 1$, equation (6) states approximately the same conditions as does equation (4). If $\mu$ is small, equation (6) should be accepted as the more accurate in computing the optimum $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$ ratio, since a minimum $\mathrm{g}_{\mathrm{m}}$ coincides with a maximum $R_{p}$ if the d-c plate voltage is kept constant. The capacitance ratio and values corresponding to equation (6) are

$$
\begin{equation*}
C_{s} / C_{p}=\frac{\mu}{\mu+2} \tag{7}
\end{equation*}
$$

Section 1
or

$$
\mathrm{C}_{\mathrm{g}}=\frac{2 \mathrm{C}_{8}(\mu+1)}{(\mu+2)}
$$

and

$$
\mathrm{C}_{\mathrm{p}}=\frac{2 \mathrm{C}_{\mathrm{x}}(\mu+1)}{\mu}
$$

Under these conditions the excitation voltage becomes greater than the voltage across the plate load by a factor of $\frac{\mu+2}{\mu}$, and the following additional relations hold:

$$
\begin{align*}
& (\max ) \mathrm{R}_{\mathrm{p}}=(\mu+1) \mathrm{Z}_{\mathrm{L}}  \tag{10}\\
& (\min ) \mathrm{g}_{\mathrm{m}}=\frac{1}{\mathrm{Z}_{\mathrm{L}}}-\frac{1}{\mathrm{R}_{\mathrm{p}}} \tag{11}
\end{align*}
$$

As a practical consideration in design as well as for the sake of simplicity in discussion it is convenient to assume that the optimum $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$ ratio is equal to one rather than $\frac{\mu}{\mu+2}$. However, in interpreting the equations above, a word of caution is necessary. Returning to equation (2), it will be seen that the maximum to be sought for $\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{L}}$ is a "practical," not a "mathematical" maximum in the sense that a curve of $\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{L}}$ rises to a peak and then decreases. The curve of equation (2) plotted against $\mathrm{Z}_{\mathrm{p}}$ passes from positive to negative infinity as the denominator passes through zero and thus is discontinuous at that point. However, for any given value of $\mathrm{g}_{\mathrm{m}}$ sufficiently large for $\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{L}}$ to be positive, the curve does have a true minimum, not a maximum, at the point where $Z_{p} Z_{g}$ is a maximum. To avoid confusion as a result of this apparent contradiction, it is important to recall that the "practical" maximum is to be sought by making equation (3) as nearly true as possible, and not by the process of making $\mathrm{Z}_{\mathrm{p}}=\mathrm{Z}_{\mathrm{k}}$. This latter consideration is in the interest of over-all stability and maximum activity (if measured by the d-c grid current) for a given d-c plate voltage and load capacitance. Another point that should be well understood is that the minimum $\mathrm{g}_{\mathrm{n}}$, minimum $\mu$, and maximum $\mathrm{R}_{\mathrm{p}}$, are all coincidental. From the point of view of frequency stability the real interest is in the maximum $\mathrm{R}_{\mathrm{p}}$. From equation (10) it can be seen that the magnitude of the maximum $\mathrm{R}_{\mathrm{p}}$ will increase with $\mu$; but remember that this value of $\mu$ is the minimum obtainable with a given tube and $\mathrm{E}_{\mathrm{b}}$. As will be discussed more thoroughly in paragraphs 1-294 and 1-295, an oscillator vacuum tube cannot be operated so that $\mu$ is the maxi-
mum possible without the risk of amplitude instability. Thus, class-A operation where the tube is operated only along the straight portion of the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve is not feasible in gridleak oscillators. Understand that if equation (7) holds, equations (10) and (11) automatically hold. $\mu$ in each equation is the effective $\mu$ when equilibrium is reached and is not the starting $\mu$. It is the minimum $\mu$ that can be obtained as long as the crystal resistance, $\mathrm{R}_{\mathrm{e}}$, and the total load capacitance, $\mathrm{C}_{\mathrm{x}}$, remain constant. Because $R_{p,}, g_{m}$, and $\mu$ all pass through extremes at the optimum capacitance ratio, it might be thought that the operating conditions are more ideally unique than they actually are, because the instantaneous rate of change for all the tube parameters with the capacitance ratio is zero under these conditions. Remember, however, that these maximum and minimum values apply only in the event that the total $C_{x}$ remains constant. An independent variation in $\mathrm{C}_{\mathrm{g}}$ or $\mathrm{C}_{\mathrm{p}}$ will cause the frequency to change, and the tube parameters will vary. For instance, $\mathrm{g}_{\mathrm{m}}$ will tend to vary directly with both $\mathrm{C}_{\mathrm{g}}$ or $\mathrm{C}_{\mathrm{p}}$. Only when $\mathrm{C}_{\mathrm{g}}$ and $\mathrm{C}_{\mathrm{p}}$ are adjusted simultaneously so as always to maintain the same total load capacitance will the instantaneous changes in the tube parameters be zero as the capacitance ratio is varied through its optimum value.
1-285. If equation 1-284 (3) is expressed as a function of $Z_{v k}$, by substituting from equation 1-284 (4), the minimum value of $\mathrm{g}_{\mathrm{m}}$ becomes, approximately,

$$
\begin{equation*}
(\min ) g_{\mathrm{m}}=\frac{4 \mathrm{R}_{\mathrm{e}}}{\mathrm{Z}_{\mathrm{pg}}{ }^{2}} \tag{1}
\end{equation*}
$$

Since $Z_{V I V}$ is the crystal impedance, approximately equal to $X_{e}$, the minimum value of $g_{m}$ can be expressed as

$$
\begin{equation*}
(\min ) g_{\mathrm{m}}=\frac{4}{P I} \tag{2}
\end{equation*}
$$

where PI is the performance index. Using a one-to-one capacitance ratio and a vacuum tube of high $\mathrm{R}_{\mathrm{i}}$, equilibrium will be reached at the value of $\mathrm{g}_{\mathrm{m}}$ defined in equation (2). Such operation generally provides the maximum frequency stability in a Pierce oscillator. In estimating the value of PI, $\mathrm{X}_{\mathrm{e}}$ is numerically equal to the reactance of the rated load capacitance, and $R_{e}$ must be assumed to be the maximum permissible effective resistance according to the military specifications of the crystal unit being used.

## CAPACITANCE RATIO, $C_{q} / C_{p}$, FOR GREATER oUtPUT IN PIERCE CIRCUIT

1-286. Where a maximum output consistent with the minimum frequency-stability requirements is desired in a Pierce oscillator, the $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{p}}$ ratio can be increased and a vacuum tube providing a large transconductance and a large amplification factor should be used. The first consideration is that $I_{g}$ must not exceed a value that would cause the power dissipation in the crystal unit to exceed the specified drive level. If the output of the oscillator is capacitively coupled to the grid of a buffer amplifier, the output power becomes a minor consideration compared with the output voltage. If this voltage is to be a maximum for a given tank current, the plate impedance $\mathrm{Z}_{\mathrm{r}}$ must be a maximum. This means that the capacitance ratio, $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{p}}$, must be as large as practicable. The larger this ratio, however, the smaller will be the excitation voltage for a given $I_{k}$. The smaller the excitation voltage, the smaller will be the gridleak bias, and consequently $R_{p}$ will be less whereas $g_{m}$ and $\mu$ will be greater. An examination of equation 1-284 (3) reveals that the required magnitude of $\mathrm{g}_{\mathrm{m}}$ becomes very large as $Z_{p}$ approaches the value of $Z_{10 g}$ of the crystal unit. Where a relatively large frequency deviation can be tolerated a large $R_{p}$ may not be necessary, so that increased voltage outputs can be obtained with tubes of high transconductance at low d-c plate voltages. In any event the $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$ ratio can never exceed the amplification factor of the tube, nor can the r-f plate voltage be greater than, nor equal to, the voltage across the crystal unit. It should be understood that the higher voltage outputs are only to be had with a large $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{p}$ ratio because of the limitations on the crystal drive level and the load capacitance, $\mathrm{C}_{x}$, and are not due to the fact that the Pierce or Colpitts type of circuit is inherently more active when the $\mathrm{C}_{\mathrm{z}} / \mathrm{C}_{\mathrm{p}}$ ratio is a maximum. To the contrary, with a fixed $\mathrm{C}_{\mathrm{x}}$, maximum amplitude of oscillations is to be obtained when $C_{n}=C_{k}=2 C_{x}$. Where a larger than minimum power rather than voltage output is required, this can probably best be achieved when $\mathrm{C}_{\mathrm{z}} / \mathrm{C}_{\mathrm{p}}$ lies between 1 and 2 , and in this case a larger $\mathrm{g}_{\mathrm{m}}$ is necessary to maintain oscillations. When a relatively large power output is required, the Pierce circuit should not be used.

## how to estimate the frequency VARIATION AND STABILITY OF A PIERCE OSCILLATOR

1-287. In paragraph 1-243 it was shown that the frequency-stability coefficient, $\mathrm{F}_{\mathrm{x}_{e}}$ of the crystal unit is defined as the percentage change in $\mathrm{X}_{\mathrm{o}}$ per
percentage change in frequency. By equation $1-243$ (1), $\mathrm{F}_{\mathrm{Xe}_{\mathrm{e}}}=\frac{2 \mathrm{C}_{\mathrm{x}}{ }^{2}}{\mathrm{C} \mathrm{C}_{\mathrm{x}}}$. The reciprocal, $1 / \mathrm{F}_{\mathrm{xe}}$ is thus equal to the percentage change in frequency per percentage change in reactance. Since $X_{e}$ is equal numerically to the reactance of the total load capacitance $C_{x}$, the fractional change in the load reactance multiplied by $1 / \mathrm{F}_{\mathrm{xe}_{\mathrm{e}}}$ will give the fractional change in frequency. Thus,

$$
\frac{d f}{f}=\frac{d \omega}{\omega}=\frac{1}{F_{X_{e}}} \cdot \frac{d X_{x}}{X_{x}}=-\frac{1}{F_{x_{e}}} \cdot \frac{d C_{x}}{C_{x}}
$$

In the Pierce circuit, if it can be assumed that the interelectrode plate-to-grid capacitance and the grid and output losses are negligible, $\mathrm{C}_{\mathrm{x}}$ will equal $\frac{C_{p}{ }^{\prime} C_{s}}{C_{p}{ }^{\prime}+C_{k}}$ where $C_{p}{ }^{\prime}=C_{p}+C_{n}$. (See figure 1-121. (C).) If it is desired to find the fractional change in frequency for a small change in, say $\mathrm{C}_{\mathrm{p}}{ }^{\prime}$, equation (1) can be used by expressing $\mathrm{dC}_{x}$ as a function of $\mathrm{dC}_{\mathrm{p}}{ }^{\prime}$, thus: $\mathrm{dC}_{\mathrm{x}}=\mathrm{dC}_{\mathrm{p}}{ }^{\prime}, \frac{\mathrm{dC}_{\mathrm{x}}}{\mathrm{dC}_{\mathrm{p}}{ }^{\prime}}$
With

$$
C_{x}=\frac{C_{p}^{\prime} C_{g}}{C_{p}^{\prime}+C_{z}}
$$

then

$$
\frac{\mathrm{dC}_{\mathrm{x}}}{\mathrm{dC}_{\mathrm{p}}^{\prime}}=\frac{\mathrm{C}_{\mathrm{g}}^{2}}{\left(\mathrm{C}_{\mathrm{p}}^{\prime}+\mathrm{C}_{\mathrm{g}}\right)^{2}}
$$

and

$$
\begin{aligned}
\frac{d C_{x}}{C_{x}} & =\frac{C_{q}^{2} d C_{p}^{\prime}}{\left(C_{p}^{\prime}+C_{g}\right)^{2}} / \frac{C_{p}^{\prime} C_{k}}{C_{p}^{\prime}+C_{g}} \\
& =\frac{C_{k} d C_{p}^{\prime}}{C_{p}^{\prime}\left(C_{p}^{\prime}+C_{g}\right)}=\frac{C_{x}}{\left(C_{p}^{\prime}\right)^{2}} \cdot d C_{p}^{\prime}
\end{aligned}
$$

On substituting in equation (1):

$$
\begin{equation*}
\frac{d f}{f}=-\frac{1}{F_{X e}} \cdot \frac{C_{x}}{\left(C_{p}\right)^{2}} \cdot d C_{p}^{\prime} \tag{2}
\end{equation*}
$$

Likewise,

$$
\begin{equation*}
\frac{d f}{f}=-\frac{1}{F_{X_{e}}} \cdot \frac{C_{x}}{C_{k}^{2}} \cdot d C_{k} \tag{3}
\end{equation*}
$$

In the event that $\mathrm{C}_{\mathrm{p}}{ }^{\prime}=\mathrm{C}_{\mathrm{z}}=2 \mathrm{C}_{\mathrm{x}}$ Equations (2) and (3) become

$$
\begin{equation*}
\frac{\mathrm{df}}{\mathrm{f}}=-\frac{\mathrm{dC}}{\mathrm{p}^{\prime}}{ }^{\prime} \mathrm{F}_{\mathrm{Xe}_{\mathrm{t}}} \tag{4}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{d f}{f}=\frac{-d_{k}}{4 F_{X_{f}}} \tag{5}
\end{equation*}
$$

1-288. When a more detailed expression of the frequency deviation is desired $\mathrm{C}_{p}{ }^{2}$ can be replaced by ( $C_{p}+C_{n}$ ), and $C_{n}$, in turn, can be expressed as a function of its variables. A rigorous analysis of the effect of each parameter upon the frequency would be quite involved. Probably the simplest approach for determining the frequency deviation due to a change in some particular circuit parameter would be to begin with an appropriate equation in paragraph 1-287, and express the differential element as a function of the differential of the particular circuit parameter. This is the method that was used when $\mathrm{dC}_{\mathrm{x}}$ in equation 1-287 (1) was expressed as a function of $\mathrm{dC}_{p}{ }^{\prime}$ and of $\mathrm{dC}_{\mathrm{g}}$ in equations $1-287$ (2) and $1-287$ (3), respectively. As an additional example, suppose that it is desired to determine approximately the frequency deviation due to a change in $R_{p}$ of the vacuum tube. Let it be assumed that $\mathrm{C}_{\mathrm{g}}=2 \mathrm{C}_{\mathrm{x}}$. The most appropriate equation to begin with is $1-287(4)$, since $\mathrm{dC}_{\mathrm{p}}{ }^{\prime}$ can be expressed as a function of $\mathrm{dR}_{\mathrm{p}}$. The problem is to determine the function that gives the change in $\mathrm{C}_{1}{ }^{\prime}$ due to an infinitesimally small change in $R_{p}$, and to substitute that function for $d C_{p}{ }^{\prime}$ in equation $1-287(4)$. Since $d C_{p}^{\prime}=\frac{d C_{p}^{\prime}}{d R_{p}} \cdot d R_{p}$, the first step is to determine $\mathrm{dC}_{\mathrm{p}}{ }^{\prime} / \mathrm{dR}_{\mathrm{p}}$, and then simply to multiply this by $\mathrm{dR}_{\mathrm{p}}$. Now, by equation 1-281 (16),

$$
C_{p}^{\prime}=C_{p}-C_{p} / Q_{f}^{2}-\frac{C_{p} R_{e}}{R_{p}+R_{e}}
$$

so

$$
\mathrm{dC}_{\mathrm{p}}^{\prime} / \mathrm{dR}_{\mathrm{p}}=\mathrm{C}_{\mathrm{p}} \mathrm{R}_{\mathrm{e}} /\left(\mathbf{R}_{\mathrm{p}}+\mathbf{R}_{\mathrm{e}}\right)^{2}
$$

or

$$
\begin{equation*}
d C_{p}^{\prime}=\frac{C_{p} R_{e}}{\left(R_{p}+R_{e}\right)^{2}} \cdot d R_{p} \tag{1}
\end{equation*}
$$

Substituting this function for $\mathrm{dC}_{\mathrm{p}}{ }^{\prime}$ in equation 1-287 (4) :

$$
\begin{equation*}
\frac{d f}{f}=-\frac{C_{p} R_{e}}{4\left(R_{p}+R_{e}\right)^{2}} \cdot \frac{d R_{p}}{F_{X e}} \tag{2}
\end{equation*}
$$

Note than an increase in $R_{p}$ causes a decrease in the frequency. It should be well understood that the equations above are only rough approximations. For example, one of the approximations in equation (2) is the assumption that $R_{p}$ and $R_{e}$ are independent variables, which, of course, is not true. However, the direct effect of a change in $R_{p}$
upon the frequency can be considered much greater than the indirect effect due to a change in $\mathrm{R}_{\mathrm{e}}$ resulting from the initial change in frequency. The differential element, $d R_{p}$, in equation (2) can, in turn, be expressed as a function of an infinitesimal change, $\mathrm{dE}_{b}$ in the d-c plate voltage. The general equation for this function is $\mathrm{dR}_{p}=\frac{\mathrm{dR}_{\mathrm{p}}}{\mathrm{dE}_{b}} \cdot \mathrm{dE}$. . However, the derivative term, $\mathrm{dR}_{\mathrm{p}} / \mathrm{dE}_{\mathrm{b}}$, will be quite difficult to determine, except by experiment, since it depends upon both the tube and circuit characteristics at the operating voltages. For its mathematical expression the principal considerations would be the change in $R_{p}$ with a change in $E_{b}$, assuming a constant grid bias, the change in grid bias due to the change in plate voltage, and the change in $R_{p}$ due to a change in grid bias, assuming a constant plate voltage. In using the equations above it is only necessary to substitute small finite changes in the independent variable for its differential. For example, if the input capacitance were to decrease an amount $\Delta \mathrm{C}_{\mathrm{g}}=1 \mu \mu \mathrm{f}$, the fractional change in frequency would be given approximately by equation $1-287$ (3) if we were to substitute $-\mathbf{1}_{\mu \mu} \mathrm{f}$ for $\mathrm{dC}_{\mathrm{g}}$.

## ENERGY AND FREQUENCY EQUATIONS OF PIERCE CIRCUIT AS COMPLEX FUNCTIONS OF LINEAR PARAMETERS

1-289. It is beyond the scope of this handbook to present the more rigorous analyses of the various oscillator circuits. These can be obtained from the various reference sources listed in the index. Actually, even when following the more explicit equations, so many approximations must be made for the sake of simplicity, and so many unknowns are involved, such as stray circuit capacitance, that the final solutions can rarely be considered more than general indices of the actual circuit conditions. If maximum mathematical exactitude is desired in determining the frequency and activity characteristics of an oscillator, the analysis should be performed by differential equations assuming nonlinear parameters. Such equations are quite involved and are rather difficult to interpret qualitatively. If a moderately rigorous analysis is desired, the equivalent circuit in figure 1-119 (B) may be assumed to have linear parameters, as has been assumed in our previous discussion, but instead of handling the impedances as real numbers, to represent them by complex functions. For the Pierce circuit

$$
\begin{aligned}
& Z_{p}=j X_{C p} \\
& Z_{\mathrm{g}}=j X_{C z} \\
& Z_{\mathrm{pg}}=R_{e}+j X_{e}
\end{aligned}
$$

An equation expressing the conditions for oscillation is derived very similarly to the method followed in paragraph 1-284, except that $I_{k}$ is expressed by the exact equation

$$
I_{z}=\frac{E_{p}}{Z_{p z}+Z_{z}}
$$

rather than by the simplifying equation

$$
I_{g} \approx E_{p} / Z_{p}
$$

For either the Pierce or Miller circuit, the conditions for stable oscillation are expressed by the equation

$$
\begin{equation*}
-R_{p}=\frac{Z_{p}\left(Z_{p x}+Z_{g}\right)}{g_{m} Z_{p} Z_{w}+Z_{v}} \tag{1}
\end{equation*}
$$

where $Z_{s}=Z_{p}+Z_{p t}+Z_{g}$. Equation (1) is similar to equation 1-284(1) except that in the derivation of equation (1) $I_{k}$ is expressed by its exact function and the impedances represent complex quantities. When the impedances are expressed as complex functions, the right-hand side of equation (1) can be reduced to the sum of a real quantity and an imaginary quantity, each with the dimensions of impedance.
Thus, $\mathrm{R}_{\mathrm{v}}=\mathrm{R}+\mathrm{jX}$
However, since $R_{p}$ is not, itself, reactive, the imaginary term, jX , must equal zero, and the real term, $R$, must equal $R_{r}$. In this manner two equations, $X=O$ and $R=R_{r}$, involving the same variables are obtained, both of which must hold if stable oscillations are to be maintained. A minimum of two equations is necessary, since there are two independent functions to perform. One function is to fix the frequency so that the excitation voltage is properly phased, and the other function is to ensure that the feed-back energy per cycle is exactly equal to its dissipation per cycle. If both sides of equation (1) are divided by $\mathrm{R}_{\mathrm{p}}$, the righthand side again reduces to the sum of real and imaginary parts. The real part must be equal to 1, and the imaginary part must again be zero. It can be shown that the real part becomes, after multiplying through by $\mathrm{R}_{\mathrm{p}}$ :

$$
\mathrm{R}_{\mathrm{p}}=\frac{\mathbf{X}_{\mathrm{C}_{\mathrm{p}}}\left(\mathrm{X}_{\mathrm{o}}+\mathbf{X}_{\mathrm{CR}_{\mathrm{R}}}\right)}{\mathrm{R}_{\mathrm{o}}-\mathrm{g}_{\mathrm{m}} \mathbf{X}_{\mathrm{Cp}_{\mathrm{p}}} \mathrm{X}_{\mathrm{Ck}}}
$$

This equation, rather than equation (1) is the real equivalent of equation 1-284 (1) and serves the same purpose in that it defines the conditions
necessary for the feed-back energy to be sufficient and stable-in other words, for the loop gain to equal unity. The equation for the imaginary part when made equal to zero can be expressed as:

$$
X_{C p}+X_{C \varepsilon}+X_{e}+\frac{R_{e} X_{C_{p}}}{R_{p}}=0
$$

When this equation holds, the loop phase shift is zero. Whereas equation (2) is said to define the feed-back energy requirements, equation (3) is said to define the frequency requirements, Note that in equation (3), the term $\frac{R_{e} X_{C_{p}}}{R_{p}}$ is equivalent to the reactance of a dynamic capacitance

$$
\begin{equation*}
C_{d}=\frac{C_{p} R_{p}}{R_{e}} \tag{4}
\end{equation*}
$$

which can be imagined to be in series with $\mathrm{C}_{\mathrm{p}}$. The capacitance of the combination becomes

$$
C_{p}^{\prime \prime}=\frac{C_{p} C_{d}}{C_{p}+C_{d}}=\frac{C_{p} R_{p}}{R_{p}+R_{e}}
$$

which is exactly the same as the small- $\mathrm{R}_{\mathrm{b}}$ value of $\mathrm{C}_{\mathrm{p}}{ }^{\prime}$ in equation 1-281 (18). $\mathrm{C}_{d}$ is thus a positive series dynamic capacitance equivalent to part of the negative parallel dynamic capacitance $\mathrm{C}_{\mathrm{n}}$. Equation (3) indicates that as $\mathrm{R}_{\mathrm{p}}$ increases indefinitely $\mathrm{X}_{\mathrm{Cy}}+\mathrm{X}_{\mathrm{Cz}}+\mathrm{X}_{\mathrm{e}} \rightarrow 0$. This is not to be interpreted as meaning that the tank circuit approaches a parallel-resonant state as a limit or that the total dynamic capacitance approaches zero. Actually, even if the sum of the first three reactances did equal zero, the tank would not be at resonance because of the presence of $\mathrm{R}_{\mathrm{e}}$ in the feed-back arm, and a dynamic capacitance would need to be effectively present. What equation (3) does show is that, as $R_{0}$ increases indefinitely, the frequency becomes entirely determined by the tank-circuit parameters. In the limit, $\mathrm{X}_{\mathrm{C},}+\mathrm{X}_{\mathrm{e}}=$ $-\mathrm{X}_{\mathrm{Cp}}$. As this state is approached, the impedance of the feed-back arm can be represented as

$$
Z_{p r e}=R_{e}+j X_{p g e}=R_{e}-j X_{C p}
$$

The impedance of the tank circuit is

$$
\begin{aligned}
Z_{L} & =\frac{Z_{p x c} Z_{p}}{Z_{p r e}+Z_{p}}=\frac{\left(R_{e}-j X_{C_{p}}\right) j X_{C_{p}}}{R_{\mathrm{e}}-j X_{C_{p}}+j X_{C_{p}}} \\
& =\frac{X_{C_{p}}{ }^{2}}{R_{\mathrm{s}}}+j X_{C p}
\end{aligned}
$$

The real component, $X_{\mathrm{CP}^{*}}{ }^{*} / \mathrm{R}_{\mathrm{e}}$, is equivalent to $\mathrm{R}_{\mathrm{zu}}$,
and the imaginary component, $j X_{c p}$, is equivalent to $X_{Z_{I I} .}$. Thus, the tank circuit does not appear as a pure resistance in the limit, but approaches an effective

$$
\begin{aligned}
\mathrm{Q} & =\frac{\mathrm{X}_{\mathrm{Z}}}{\mathrm{R}_{\mathrm{Zs}}}=\frac{\left|\mathrm{X}_{\mathrm{Cp}}\right|}{\mathrm{X}_{\mathrm{Cp}}^{2} / \mathrm{R}_{\mathrm{e}}}=\frac{\mathrm{R}_{\mathrm{e}}}{\left|\mathrm{X}_{\mathrm{Cp}}\right|} \\
& =\frac{\mathrm{R}_{\mathrm{e}}}{\left|\mathrm{X}_{\mathrm{e}}-\mathrm{X}_{\mathrm{Cg}}\right|}=\frac{1}{Q_{f}}
\end{aligned}
$$

This is the same effective $Q$ as was determined qualitatively from the viewpoint of phase angles. The term $\mathrm{R}_{\mathrm{c}} \mathrm{X}_{\mathrm{c}_{\mathrm{p}}} / \mathrm{R}_{\mathrm{p}}$ in equation (3) is therefore not to be interpreted rigorously as the total dynamic reactance, but as that part of the dynamic reactance that is a function of the tube parameters. At all times, the total lgad reactance across the crystal terminals is $\mathrm{X}_{\mathrm{x}}=-1 / \omega \mathrm{C}_{\mathrm{x}}=\mathrm{X}_{\mathrm{Cg}}+\mathrm{X}_{\mathrm{Cp}}{ }^{\prime}$ which is always slightly greater than ( $\mathbf{X}_{\mathrm{Cg}}+\mathrm{X}_{\mathrm{Cp}}$ ).

CAPACITIVE ELEMENTS IN DESIGN OF PIERCE OSCILLATOR
1-290. It was declared that equation 1-289 (3) defined the frequency requirements of a Pierce
oscillator. Since the frequency and the value of $X_{e}$ and $X_{x}$ are effectively predetermined constants, the primary problem involved in the solution of equation 1-289 (3) lies in determining the values of the lumped capacitances that must be inserted in the circuit to provide the correct value of $\mathrm{C}_{\mathbf{x}}$. In the average Pierce circuit the dynamic capacitance can be considered negligible when compared with the total load capacitance, so that $C_{x}$ can be assumed to equal $C_{p}$ and $C_{k}$ in series to a first approximation. With $\mathrm{C}_{\mathrm{p}}$ and $\mathrm{C}_{\mathrm{g}}$ decided upon, approximate values of $\mathrm{g}_{\mathrm{m}}$ can be had by equating the denominator of equation 1-289 (2) to zero and solving for the transconductance. The maximum and minimum equilibrium values of $\mathrm{gm}_{\mathrm{m}}$ coincide with the maximum and minimum expected values of $R_{e}$, respectively. Next, assuming that $g_{m} \approx I_{p} / E_{g}$, and that $E_{g}=I_{g} X_{c k}$, where $I_{g}$ is the crystal current, a vacuum-tube and plate voltage are chosen which will provide a maximum $R_{p}$, but which will not cause a crystal unit of any expected $R_{e}$ to be overdriven. To determine the lumped capacitances that must be added to provide the correct values of $\mathrm{C}_{\mathrm{p}}$ and $\mathrm{C}_{\mathrm{g}}$, it is first necessary to

(A)


Figure 1-124. (A) Conventionai Pierce oscillator and buffer-amplifier circuit. (B) Static capacitances of circuit (A). $\boldsymbol{C}_{y}=$ interelectrode capacitances. $\boldsymbol{C}_{w}=$ distributed capacitances of wires
know the values of the stray static capacitances in the circuit. These stray elements effectively create a lower limit to the capacitance across the crystal unit. Obviously, they must not be allowed to exceed the total specified load capacitance. Preferably, they should be as small as possible and not be so distributed that an optimum capacitance ratio, $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{p}$, cannot be achieved. The static capacitances to be considered in a conventional Pierce oscillator are illustrated in figure 1-124. Before the optimum values of $\mathrm{C}_{1}$ and $\mathrm{C}_{3}$ can be determined, an experimental circuit should be constructed with the various leads and circuit components reasonable facsimiles of those intended in the final production models. With $C_{1}$ and $C_{3}$ omitted, the static capacitances between plate and grid, plate and cathode, and grid and cathode can be measured. $\mathrm{C}_{1}$ and $\mathrm{C}_{3}$ can then be computed to provide the total required load capacitance.
1-291. In the early days of crystal oscillators, and even today where the oscillator is not required to meet a frequency tolerance less the 0.02 percent, the choice of grid and plate circuit capacitances was largely a matter of trial and error. Usually,


Figure 1-125. Variotion of activity and trequency in Pierce oscillator as plate-circull capacitanse is increased
the final choice was based upon the combination that provided the maximum activity for a given d-c plate voltage. For example, if the grid-tocathode capacitance, $\mathrm{C}_{g}$, of a Pierce oscillator is held constant while the plate load capacitance is varied from a minimum to a maximum, an activity curve, as measured by the gridleak current, is obtained similar to the one illustrated in figure 1-125 (A). Formerly, it was not unusual for the optimum capacitance to be considered a value slightly greater than that at which the activity is a maximum. In military equipment the principal consideration now is to ensure a given total load capacitance. As shown in figure 1-125 (B), increasing the plate-circuit capacitance causes the frequency to decrease. As the frequency decreases, so does $X_{e}$ of the crystal unit, and at only one point along the curve will the crystal unit be operating into its rated capacitance. As stated previously, the circuit must provide the specified capacitance if there is to be an assurance that the required frequency tolerance is met when one crystal unit is replaced by another of the same type and nominal frequency. In an exceptional case, the most important consideration may be to maintain a fixed frequency relative to some frequency standard. For this purpose small variations in the load capacitance that can be made manually should be possible, but care should be taken that an operator is not to be able to vary the total more than is just sufficient to allow for a frequency variation equal to the bandwidth of the tolerance range. Otherwise, there can be a risk of overdriving a crystal unit, or of continuing in operation a defective crystal or other circuit component that should be replaced before a complete breakdown is threatened.

## Measurement of Stray Capacitances In Pierce Circuit

1-292. In order to measure the stray static capacitances in a circuit such as that shown in figure 1-124, the lumped grid and plate capacitances, $C_{1}$ and $C_{3}$, as well as the crystal, should first be removed. The remaining elements can be assumed to form a three-element network as shown in figure 1-126. If an r-f choke is connected in the circuit, the frequency of the $Q$ meter should be approximately the operating frequency of the oscillator. The measurements are made with all vacuum-tube voltages off. The three capacitances in figure 1-126 represent three independent variables, so that a minimum of three measurements is required to determine their values. A fourth measurement is desirable as a check on the accuracy of the first three. Any combination of measurements can be

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Figure 1-126. Equivalent network formed by the stray static capacitances of a vacuum-tube circuit. A minimum of three different measuremants is required. The individual capacitances can be determined by solving simultaneously any three of the nine equations above when the respective terminal capacitances are known

* Generalized equation for a measured terminal capacitance ( $C_{x y}=C_{P G}, C_{G C}$, or $C_{r c}$ ) when either $C_{r y}$ or $C_{n z}$, one of the two respective series-branch copacitances, is shorfed out.
made, the only restriction is that no two measurements are the same and that each of the capacitances is involved in at least one of the measurements. Three different measurements are possible between ary one pair of electrodes. Thus, in measuring the capacitance between grid and cathode, the circuit is unchanged for the first measurement, the plate can be grounded for the second measurement, and shorted to the grid for the third. For the three measurements:
(1st)

$$
\begin{align*}
& \mathrm{C}_{\mathrm{GC}}=\mathrm{C}_{\mathrm{gc}}+\frac{\mathrm{C}_{\mathrm{pk}} \mathrm{C}_{\mathrm{pc}}}{\mathrm{C}_{\mathrm{pg}}+\mathrm{C}_{\mathrm{pc}}} \\
& \mathrm{C}_{\mathrm{GC}}=\mathrm{C}_{\mathrm{gc}}+\mathrm{C}_{\mathrm{rk}}  \tag{2nd}\\
& \mathrm{C}_{\mathrm{GC}}=\mathrm{C}_{\mathrm{gc}}+\mathrm{C}_{\mathrm{pc}} \tag{3rd}
\end{align*}
$$

Theoretically, these three measurements could be sufficient, but one or more additional measurements are needed as a check in the event that the Q-meter leads or the shorting wires have significantly affected the readings. With $\mathrm{C}_{\mathrm{pr}}, \mathrm{C}_{\mathrm{pc}}$, and $\mathrm{C}_{\mathrm{gc}}$ determined, the lumped capacitances for both grid and plate circuits can readily be determined.

## bias voltage of pierce circuit

1-293. Oscillator bias voitages are not as critical as are those of other types of vacuum-tube circuits, for usually it is neither wave shape, maximum output, nor maximum power efficiency that is of most importance, but simply a constant fundamental frequency. For this purpose, the Pierce circuit can be designed to obtain a maximum $R_{p}$ with a minimum drive level, and the optimum bias voltage will be the one that most nearly answers the need. As a general rule, in the case of a vacuum tube that is not being driven to saturation, the effective $R_{p}$ increases as the bias becomes more negative. If the bias is sufficient for the tube to be operated class B or class $C$, so that the plate current is cut off for an appreciable part of each cycle, such operation greatly improves the power efficiency. However, a bias developed across a gridleak resistor can never exceed the peak excitation voltage during stable oscillations. The excitation voltage, in turn, is limited by the current $I_{g}$, which must not exceed a value that would cause the losses in the crystal to exceed the permissible limit. When $\mathrm{I}_{\mathrm{e}}$ is maximum, the limiting crest value of $\mathrm{I}_{g}$ is $\mathrm{I}_{\mathrm{gm}}=\sqrt{\frac{2 \mathrm{P}_{\mathrm{cm}}}{\mathrm{R}_{\mathrm{em}}}}$, where $\mathrm{P}_{\mathrm{cm}}$ is the maximum permissible drive level in watts, and $R_{e m}$ is the specified maximum effective resistance when the crystal unit is operating into its rated load capacitance. The maximum grid bias is thus

$$
\begin{equation*}
(\max ) E_{\mathrm{c}}=-Z_{\mathrm{v}} \sqrt{\frac{2 \mathrm{P}_{\mathrm{cm}}}{\mathrm{R}_{\mathrm{em}}}} \tag{1}
\end{equation*}
$$

$$
1-293
$$

where $Z_{t}\left(\approx \frac{1}{\omega C_{z}}\right)$ is the r-f impedance between gxid and cathode. It was found earlier (paragraph 1-284, equation $1-284$ (8)) that a maximum $R_{p}$ is to be had when $\mathrm{C}_{8}=\frac{2 \mathrm{C}_{x}(\mu+1)}{\mu+2}$, or approximately when $\mathrm{C}_{\mathrm{k}}=\mathrm{C}_{\mathrm{w}} \approx 2 \mathrm{C}_{\mathrm{x}}$. Equation (1) under these conditions becomes

$$
\begin{equation*}
(\max ) E_{\mathrm{c}}=-\frac{\sqrt{2 \mathrm{P}_{\mathrm{cm}}}}{2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{\mathrm{R}_{\mathrm{en}}}} \tag{2}
\end{equation*}
$$

Equation (2) is quite important in that it shows that the maximum grid bias obtainable with a maximum $R_{e}$ is fixed by the crystal specifications. The maximum $\mathrm{E}_{\mathrm{c}}$ for any given crystal unit may be obtained from equation (2) by substituting the actual $R_{\mathrm{c}}$ for $\mathrm{R}_{\mathrm{cm}}$. The proper anode voltages for a given vacuum tube, or vice versa, to provide a required output are consequently also effectively predetermined by the crystal specifications. For maximum stability with any given vacuum tube in

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a conventional Pierce circuit, $\mathrm{C}_{g}$ and $\mathrm{C}_{\mathrm{p}}$ should each be made equal to $2 \mathrm{C}_{x}$, or if the amplification factor is small, $C_{s} / C_{p}$ should be made equal to $\frac{\mu}{\mu+2}$, with the total capacitance in series made to equal $\mathrm{C}_{\mathrm{x}}$. With the capacitance so determined, the plate and screen voltages can be adjusted to give the desired output and excitation voltages. Since $\mathrm{E}_{\mathrm{p}} \approx \mathrm{E}_{\mathrm{g}}$, the output voltage is also effectively limited by the crystal specifications. With $\mathrm{C}_{\mathrm{g}}=\mathrm{C}_{\mathrm{p}}=$ $2 C_{x}$ (max) $E_{p}=.707$ (max) $\left|E_{v}\right|$, where (max) $E_{p}$ is the maximum r-m-s value of $\mathrm{E}_{\mathrm{p}}$, and (max) $\mathrm{E}_{\mathrm{c}}$ is given by equation (2).

## FIXED BIAS FOR PIERCE OSCILLATOR

1-294. It is not conventional to employ a fixed bias in a crystal oscillator, although it can be doneeven to advantage in some cases. An r-f choke can be substituted for the gridleak resistance, thereby reducing the grid losses to an absolute minimum as long as the excitation is insufficient to overcome the bias and cause grid current to flow. In order for stable oscillations to be maintained, an increase in excitation must cause a decrease in amplification, and a decrease in excitation must cause an increase in amplification. When using a fixed bias, the choice of operating voltages is much more restricted than when employing gridleak limiting. Because of the more critical operating conditions, the replacement of one crystal unit with another having a different resistance may require additional circuit adjustments. If a fixed, class-B or class-C bias is used, a slight decrease in the amplitude of oscillations normally leads to the oscillations dying out all together. This is because the average amplification of the positive alternation of each cycle increases and decreases directly with the amplitude instead of inversely. For instance, with a class-C fixed bias, a decrease in the amplitude of one cycle would mean that the tube is cut off during a larger fraction of the succeeding cycle, thereby further decreasing the average amplification. On the other hand, if oscillations were once started, the tendency would be for the amplitude to build up until limited by grid and plate saturation. Only if limiting is provided by nonlinear elements, such as thermistors or varistors, in the external circuits is class-B or class-C fixed-bias operation possible if the tube itself is not to provide the limiting action. A fixed bias can be used if the tube is driven to saturation each cycle, but such operation is not practicable unless the utmost power is required from the oscillator, and in any event should not be attempted with the Pierce circuit. The only feasible application of a fixed bias


Figure 1-127. Point on E. $t_{t}$ curve at which stable oscillations can be achieved with fixed bias. For minimum grid losses, the peak of the maximum excitation voltage must not exceed the fixed $E_{c}$
in the Pierce oscillator is to operate the tube just above the knee of the $\mathrm{E}_{\mathrm{e}} \mathrm{I}_{\mathrm{b}}$ curve (see figure 1-127). ( $E_{c}$ and $I_{b}$ represent no-signal, $d-c$ values of grid voltage and plate current respectively.) At the indicated operating point a slight decrease in the activity results in the average amplification of the negative alternation of the excitation cycle being greater, whereas the amplification of the positive alternation remains essentially constant. Thus, the over-all amplification of the weaker cycle is greater than that of the stronger, and a stable equilibrium is possible. An r-f choke would normally replace the gridleak resistor. Such operation practically eliminates the grid losses as long as the peak excitation voltage does not exceed the bias. Theoretically, then, the fixed bias permits a maximum $Q$ in the feed-back circuit, and in this respect aids the frequency stability. There are, however, practical difficulties involved. If the $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{p}}$ ratio of the external circuit is such that the oscillator is to operate at the minimum $g_{m}$, it may be difficult to find a vacuum tube that provides the desired transconductance when operated at suitable voltages just above the knee of the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve. The low transconductance can readily be achieved by using a remote-cutoff tube, but the amplitude stability will be more critical since the amplification of the positive alternations increases with amplitude, thereby tending to annul the limiting action of the negative alternations. Variations in the circuit capacitances have the following effects, which are essentially the same as those that occur with gridleak bias except that the amplitude variations are more pronounced in the fixed-bias circuit. A small decrease in the capacitance ratio, say by an increase in $C_{1}$, would mean that the voltage ratio,

$$
\mathbf{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{g}}=\mathrm{C}_{\mathrm{R}} / \mathrm{C}_{\mathrm{p}}=\frac{\mathrm{g}_{\mathrm{m}} \mathbf{R}_{\mathrm{p}} \mathrm{Z}_{\mathrm{L}}}{\mathbf{R}_{\mathrm{p}}+Z_{\mathrm{L}}}=\mathrm{g}_{\mathrm{m}} \mathrm{Z}_{\mathrm{L}}
$$

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must become smaller. Since $\mathrm{E}_{\mathrm{v}}{ }^{\prime} \mathrm{E}_{\mathrm{z}}$ varies inversely with $\mathrm{C}_{\mathrm{p}}$ whereas $\mathrm{Z}_{\mathrm{L}}$ varies inversely with $\mathrm{C}_{1}{ }^{2}$, an increase in $\mathrm{C}_{p}$, as long as $\mathrm{K}_{\mathrm{p}} \gg \mathrm{Z}_{1}$, requires $\mathrm{g}_{\mathrm{m}}$ to increase proportionately in order that equilibrium may be re-established. In other words, an increase in $\mathrm{C}_{\mathrm{j}}$ must cause the excitation voltage to decrease. Conversely, a decrease in $\mathrm{C}_{\mathrm{p}}$ causes $\mathrm{g}_{\mathrm{m}}$ to decrease and the excitation voltage to increase. $R_{p}$ varies in a direction opposite to that of $\mathrm{g}_{\mathrm{m}}$, but the percentage change in $R_{1}$, is not as large as the percentage change in $\mathrm{g}_{\mathrm{m}}$. The change in $\mathrm{g}_{\mathrm{m}}$ is approximately proportional to the change in $\mathrm{C}_{3}$. If $\mathrm{C}_{\mathrm{p}}$ is constant, but $\mathrm{C}_{\mathrm{k}}$ is varied slightly, $\mathrm{Z}_{\mathrm{I}}$, will be approximately constant, so that $\mathrm{g}_{\mathrm{m}}$ must also vary directly with $\mathrm{C}_{k}$ in order for equilibrium to be maintained. Therefore, the changes in the excitation voltage with changes in $\mathrm{C}_{\mathrm{r}}$ are similar to those with changes in $C_{p}$. When $C_{v}$ and $C_{k}$ are varied independently the total load capacitance $\mathrm{C}_{x}$ changes, and hence the frequency and $\mathrm{X}_{\mathrm{e}}$ also change. If, during tuning adjustments, $\mathrm{C}_{\mathfrak{p}}$ and $\mathrm{C}_{\mathrm{g}}$ are varied so that the same total capacitance is always maintained, then, in the region where $C_{p}$, $\approx \mathrm{C}_{\mathrm{k}}$ the change in $\mathrm{C}_{\mathrm{p}}$, is approximately equal but opposite to the change in $\mathrm{C}_{\mathrm{k}}$. In this case $\mathrm{g}_{\mathrm{m}}$, which has reached its minimum value, tends to remain constant, as do also the excitation voltage and the plate resistance of the tube. It should be understood that this optimum condition holds only for variations in capacitance that leave the total load capacitance unchanged. With $\mathrm{C}_{\mathrm{x}}$ fixed, $\mathrm{g}_{\mathrm{m}}$ must inceease as the capacitance ratio is varied to either s.de of its optimum value. When $\mathrm{C}_{\mathrm{F}} / \mathrm{C}_{\mathrm{g}}$ is made greater than one the change in $\mathrm{g}_{\mathrm{m}}$ and the excitation is greater than when $\mathrm{C}_{\mathrm{z}} / \mathrm{C}_{1}$, is made less than one by an equivalent proportion. (e.g., $\Delta \mathrm{g}_{\mathrm{m}}$ is greater when $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{p}}$, is changed from 1 to 2 than when it is changed from 1 to $1 / 2$.) An increase in $\mathrm{g}_{11}$ can occur only by virtue of a decrease in excitation voltage. Thus, if the grid impedance, $\mathrm{Z}_{\mathrm{g}}$, is made larger than the plate impedance, $\mathrm{Z}_{\mathrm{p}}$, the crystal current, $I_{k}$, must necessarily become smaller. Oscillations can thus be maintained with a smaller drive level. Nevertheless, optimum stability generally requires a maximum $R_{p}$, which, in turn, coincides with a maximum excitation voltage and minimum $\mathrm{gm}_{\mathrm{n}}$.
1-295. According to equation 1-284 (10), the optimum capacitance ratio will automatically cause the oscillator to seek an equilibrium when $R_{p}=$ $(\mu+1) \mathrm{Z}_{\mathrm{L}}$, or approximately when $\mathrm{R}_{\mathrm{p}}=\frac{\mu \mathrm{PI}}{4}$, where PI is the performance index. Herein lies the principal limitation of fixed-bias operation of a Pierce circuit. The maximum to minimum values of
the PI of a given type of crystal unit can be as much as 9 to 1 for the same frequency-and greater still if the oscillator is to operate over a wide frequency range. It may be difficult to find a tube to provide equivalent variations in the effective $R_{p}$ unless the excitation voltage is to be so large that it drives the grid positive on the positive excitation peaks. In this case, the principal advantage of the fixed-bias-to maintain a maximum $\mathrm{Q}_{\mathrm{s}}$ and to minimize the variations in the input imped-ance-is lost. Since an increase in $R_{p}$ must be accompanied by an increase in the r-f plate current operating into a proportionally increased load impedance, the tendency will be for the crystal power (approximately equal to $I_{v}{ }^{2} Z_{L_{1}}$ ) to vary directly with $(\mathrm{PI})^{3}$ or $\left(\frac{1}{R_{\mathrm{f}}}\right)^{3}$. Unless there is some guarantee that the maximum $R_{e}$ is not to be greater than twice the minimum expected value, some additional form of limiting must be used in the fixed-bias circuit, such as connecting a varistor across the r-f load, to ensure that the low-resistance crystal units are not over-driven. The fixed bias should not be less than three times that given by equation 1-293(2). The vacuum tube (preferably a pentode, because of its low plate-to-grid capacitance and high $\mathrm{R}_{\mathrm{p}}$ ) should be chosen and the anode voltage determined that permits operation at the lower end of the straight portion of the $E_{x} I_{b}$ curve. The optimum bias and plate voltages are best established by experiment. The principal problem is to ensure a sufficient output for crystal units of maximum $\mathrm{R}_{\mathrm{e}}$, without overdriving those crystals of minimum $\mathrm{R}_{\mathrm{p}}$. The average crystal unit has an $\mathrm{R}_{\mathrm{e}}$ approximately one-third the maximum. An occasional crystal unit may have a value of $R_{e}$ perhaps as small as one-tenth the maximum. It can be seen that a serious obstacle to the use of a fixed bias is that manual adjustments of the operating voltages are necessary when replacing crystal units, unless the plate circuit is to be rather heavily loaded. The output will tend to vary by a large factor from one crystal unit to the next. The same problem is encountered with the use of a gridleak bias, but voltage adjustments are not absolutely necessary, even under no-load conditions. A familiarity with fixedbias operation is helpful, however, in that it aids the understanding of gridleak operation.

## GRIDLEAK BIAS FOR PIERCE OSCILLATOR

1-296. The importance of having gridleak instead of fixed bias is two-fold: First, it permits a large initial surge of plate current, so that oscillations will build up quickly. If the tube were being operated class B or class C with a fixed bias, the bias
would have to be removed before oscillations could build up at all. Second, it ensures a maximum stability in the output. If for any reason the excitation should increase or decrease, the d-c grid current and hence the bias follows the change, always acting in a direction that tends to annul the original change. When the oscillator is first turned on, the starting bias is zero regardless of the value of the gridleak resistance. Thus, insofar as the initial surge of current is concerned, the value of the gridleak resistance, $R_{k}$, is not a firstorder factor. However, the value of $R_{R}$ is significant in its effect upon the total build-up time. This effect is considered in paragraphs 1-304 and 1-305, where the conditions most favorable for oscillator keying are discussed. The present discussion considers only the effects of $R_{g}$ upon the oscillator stability after the oscillations have reached a maximum amplitude. First, it is desirable that the grid losses be as small as possible, and that they at least can be considered negligible by comparison with the losses in the crystal unit. For a continuous flow of d-c grid current to be maintained, the grid must be positive with respect to the cathode at the positive peak of each excitation cycle. The amount of grid power that is dissipated, the extent to which the grid becomes positive, and the length of the period during which the grid is positive and electrons are flowing from cathode-to-grid depend upon how great a percentage of the total charge escapes through $R_{R}$ during the remainder of the cycle. This, in turn, depends upon the ratio of the period of one cycle to the RC time constant of the grid circuit.
This ratio, $1 / R_{R} C_{R} f$, is seen to be equal to $\frac{2 \pi\left|X_{C E}\right|}{R_{g}}$. The smaller this ratio can be made, the smaller will be the percentage leakage of charge during one cycle, and the more nearly will the bias remain constant and equal to the peak excitation voltage. At high frequencies, ratios on the order of $1 / 50$ and smaller are quite easily obtained. With the period of one cycle so short compared with the time it would take 63 per cent of the accumulated charge to leak off, it can be assumed that the bias voltage equals the peak excitation voltage in magnitude. Should the excitation voltage increase, the bias also increases. The peak excitation voltage is

$$
\mathrm{E}_{\mathrm{gm}}=\mathrm{I}_{\mathrm{gm}} \mathrm{Z}_{\mathrm{g}}=1.414 \mathrm{I}_{\mathrm{g}} \mathrm{Z}_{\mathrm{g}} \approx\left|\mathrm{E}_{\mathrm{c}}\right|
$$

$1-296$ (1)
where $E_{c}$ is the grid bias when $R_{g} C_{k} \gg 1 / f$, and $I_{g m}$ is the peak r-f grid-circuit current. The bias voltage is also given by the equation

$$
\begin{equation*}
E_{c}=I_{c} R_{k} \tag{2}
\end{equation*}
$$

where $I_{c}$ is the d-c grid current. If an r-f choke having an impedance that is large compared with $R_{g}$ is connected in series with $R_{z}$, the r-f voltage across $R_{k}$ becomes small compared with the d-c voltage. With this arrangement it is readily seen that the approximate grid power expenditure is

$$
\begin{equation*}
\mathbf{P}_{\mathrm{k}}=\mathbf{I}_{\mathrm{c}} \mathbf{E}_{\mathrm{c}}=\mathrm{E}_{\mathrm{c}}^{2} / \mathbf{R}_{\mathrm{g}} \tag{3}
\end{equation*}
$$

If the r-f choke is not present, so that the voltage across $R_{g}$ varies sinusoidally from a peak of $-2 \mathrm{E}_{\mathrm{gm}}$ to a peak of 0 on the positive alternation, the average squared voltage across $R_{g}$, equal to
$\frac{\mathrm{E}_{\mathrm{c}}^{2}}{2_{\pi}} \int_{0}^{2 \pi}(1+\sin \omega \mathrm{t})^{2} \mathrm{~d}(\omega \mathrm{t})$, is found to be $1.5 \mathrm{E}_{\mathrm{c}}^{2}$. Thus, in the absence of an r-f choke,

$$
\begin{equation*}
\mathrm{P}_{\mathrm{g}}=1.5 \mathrm{E}_{\mathrm{c}}^{2} / \mathrm{R}_{\mathrm{g}} \tag{4}
\end{equation*}
$$

Clearly, if the grid losses are to be held to a minimum, $R_{g}$ must be as large as possible. If an examination is made of several representative crystal oscillator circuits in actual production, it will be discovered that very few employ gridleak resistances higher than 100 kilohms, and only an occasional value of $R_{g}$ is found higher than 0.5 megohms. The answer is principally to be found in the fact that the oscillator design is usually a compromise among several factors: (a) frequency stability, (b) output-voltage stability, (c) output control, (d) operating efficiency, (e) maximum economy in production costs, (f) minimum over-all weight and space requirements, (g) whether or not oscillator is to be keyed, (h) frequency range (i), value of $C_{g}$, ( $j$ ) whether or not circuit is to permit switching from crystal to tuned circuit, and ( $k$ ) the suppression of parasitic frequencies. Either a high or a low value of $\mathrm{K}_{\mathrm{g}}$ can improve the performance in respect to any one of the factors above, depending upon what is required concerning the other factors. For example, a very large $\mathrm{R}_{\mathrm{g}}$ can improve the frequency stability by reducing the grid losses, when only a small output is required. On the other hand, the same value of $R_{g}$ could lead to both frequency and output voltage instability if maximum output or maximum operating efficiency were required. The effects of $R_{g}$ relative to various factors listed above are discussed briefly in the following paragraphs.

## Gridleak Resistance and Frequency Stability of Pierce Oscillator

1-297. The grid $R_{s}$ can lead to frequency instability in two ways. $A s R_{g}$ is decreased, the grid losses load

## Section I

## Crystal Oscillators

the feed-back circuit and require that the tank be operated farther away from resonance. $R_{p}$ of the vacuum tube is reduced and its effect upon the frequency becomes more pronounced. On the other hand, if $R_{k}$ is increased indefinitely, the oscillator can become self-modulated. This latter effect is more properly classed as a problem of output voltage stability, and is discussed in the paragraph 1-299. The principal frequency-stability importance of $R_{g}$ is the degree by which it reduces the effective $Q_{r}$ of the feed-back arm. ( $Q_{r}$ is the feed-back quality factor only from the point of view of phase rotation.) As defined by equation 1-272 (1)

$$
Q_{f}=\frac{Q_{\mathrm{pre}} \mathrm{Q}_{\mathrm{z}}}{Q_{\mathrm{pge}}+\mathrm{Q}_{\mathrm{z}}}
$$

where $Q_{\text {ure }}$ is the actual over-all effective $Q$ of the feed-back arm, and $Q_{5}$ is the effective $Q$ of the input circuit. In order to analyze the effect of $R_{g}$ in terms of the equivalent Pierce r-f circuit, we represent $Z_{g}$ by an equivalent reactance, $X_{c_{k}^{\prime}}$ in series with an equivalent resistance, $\mathrm{R}_{\mathrm{g}}{ }^{\prime}$, as shown in figure $1-128$. The problem now is to determine $R_{s^{\prime}}$, such that

$$
\begin{equation*}
I_{\mathrm{g}}^{2} \mathrm{R}_{\mathrm{g}}^{\prime}=\mathrm{P}_{\mathrm{g}} \tag{1}
\end{equation*}
$$

where $P_{g}$ is the power expended in the gridleak resistance. The power expended during the short


Figure 1-128. Equivalent Pierce fead-back circuif
current pulse when the grid is positive with respect to the cathode will be considered negligible compared with the power losses in $\mathrm{R}_{\mathrm{g}}$ per cycle. Assurning that no r-f choke is used and that $R_{g}$ is sufficiently large so that equation $1-296$ (4) is approximately correct, equation (1) on substitution and rearrangement becomes

$$
\begin{equation*}
\mathrm{R}_{\mathrm{g}}^{\prime}=\frac{1.5 \mathrm{E}_{\mathrm{c}}{ }^{2}}{\mathrm{I}_{\mathrm{g}}{ }^{2} \mathrm{R}_{\mathrm{g}}} \tag{2}
\end{equation*}
$$

Since it has been assumed that $R_{k}$ is large compared with $X_{\mathrm{Cg}_{\mathrm{g}}}$, then $\mathrm{X}_{\mathrm{Cg}}^{\prime} \approx \mathrm{X}_{\mathrm{Cg}}$ and $\mathrm{E}_{\mathrm{c}}{ }^{2} \approx \mathrm{E}_{\mathrm{gm}}{ }^{2}=$ $2\left(I_{\mathrm{k}} \mathrm{X}_{\mathrm{Cg}}\right)^{2}$. On substitution in equation (2),

$$
\begin{equation*}
\mathrm{R}_{\mathrm{k}}^{\prime}=\frac{3 \mathrm{X}_{\mathrm{C}_{\mathrm{g}}}^{2}}{\mathrm{R}_{\mathrm{k}}} \tag{3}
\end{equation*}
$$

If an r-f choke were used in series with $R_{s}$, the approximate value of $\mathrm{R}_{\mathrm{k}}{ }^{\prime}$ would be

$$
\begin{equation*}
\mathrm{R}_{\mathrm{z}}^{\prime}=\frac{2 \mathrm{X}_{\mathrm{C}_{z}}^{2}}{\mathrm{R}_{\mathrm{s}}} \tag{4}
\end{equation*}
$$

The values of $Q_{\varepsilon}$ become
(without choke) $\quad Q_{\mathrm{g}}=\frac{\left|\mathrm{X}_{\mathrm{C}_{g}}\right|}{\mathrm{R}_{\mathrm{g}}{ }^{\prime}}=\left|\frac{\mathrm{R}_{\mathrm{g}}}{3 \mathrm{X}_{\mathrm{Cg}}}\right|$

$$
1-297(5)
$$

(with choke)

$$
Q_{g}=\left|\frac{R_{g}}{2 X_{\mathrm{Cg}}}\right|
$$

$$
1-297(6)
$$

The equations for $Q_{p g c}$ are

$$
\begin{array}{r}
\text { (without choke) } \quad Q_{p g s}=\frac{\left(\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{Cu}}\right) \mathrm{R}_{\mathrm{g}}}{\mathrm{R}_{\mathrm{g}} \mathrm{R}_{\mathrm{e}}+3 \mathrm{X}_{\mathrm{Cg}}{ }^{2}} \\
1-297(7) \\
\text { (with choke) } \quad \mathrm{Q}_{\mathrm{ps}}=\frac{\left(\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{Cg}}\right) \mathrm{R}_{\mathrm{g}}}{\mathrm{R}_{\mathrm{g}} \mathrm{R}_{\mathrm{e}}+2 \mathrm{X}_{\mathrm{Cg}^{2}}} \\
1-297(8)
\end{array}
$$

Assuming that $Q_{\text {pge }} Q_{g} \gg 1, Q_{i}$ is given by the approximate equations
(without choke) $\quad Q_{\ell}=\frac{\left(X_{e}+X_{C_{g}}\right)}{R_{e}-\frac{3 X_{e} X_{C E}}{R_{\varepsilon}}}$
1-297 (9)
(with choke)

$$
Q_{f}=\frac{\left(X_{e}+X_{C_{R}}\right)}{R_{e}-\frac{2 X_{\mathrm{e}}}{} X_{C_{g}}}
$$

$1-297$ (10)

In the previous discussions it has been supposed that the grid losses are kept negligible compared with the losses in the crystal, so that a $Q$, equal to $\frac{\mathbf{X}_{e}+\mathbf{X}_{\mathrm{Cs}}}{\mathbf{R}_{\mathrm{e}}}$ is approximately correct. Where this assumption cannot be made, those equations that define the frequency of the oscillator, such as equation 1-289 (3), can still be used for approximately correct answers if $R_{e}$ is replaced by the appropriate denominator in equation (9) or (10). Thus, the effective frequency-determining resistance of the feed-back arm, can be defined as

$$
\begin{array}{r}
R_{f s}=R_{s}+\left|3 X_{s} X_{C_{k}} / R_{k}\right| \text { or } R_{e}+\left|2 X_{e} X_{C_{s}} / R_{g}\right| \\
1-297(11)
\end{array}
$$

On the other hand, in those equations that concern the equilibrium between the energy input and output of the feed-back arm, such as equation 1-289 (2), the effective feedback-circuit resistance to substitute in the place of $R_{p}$ is the value

$$
\begin{equation*}
\mathbf{R}_{\mathrm{f}}=\mathbf{R}_{\mathrm{t}}+\mathbf{R}_{\mathrm{g}}^{\prime} \tag{12}
\end{equation*}
$$

$$
1-297
$$

On multiplying equation (11) by $R_{g} / R_{e}$, it is apparent that if $R_{g}$ is to have a negligible effect upon the frequency, it must be much greater than $\left|\frac{3 X_{e} X_{C g}}{R_{e}}\right|$. Similarly, if $R_{k}$ is to have a negligible effect on the total feed-back power requirements, according to equations (3) and (12), it must be much greater than $3 \mathrm{X}_{\mathrm{Cg}^{2}} / \mathrm{R}_{\mathrm{e}}$. If the oscillator is to be operated in the region of maximum $R_{p}$ of the tube, $\left|X_{C g}\right|$ will approximately equal $X_{e} / 2$, and $\left|\frac{3 X_{\mathrm{r}} X_{\mathrm{CE}}}{\mathbf{R}_{\mathrm{e}}}\right|$ will approximately equal $\frac{3}{2}$ PI. Under these conditions, a good rule of thumb, if the other operating requirements permit, is to employ a grid resistance equal to 15 times the minimum permissible PI $\left(=\frac{1}{\omega^{2} C_{x}{ }^{2} \mathrm{R}_{\mathrm{em}}}\right)$, or greater, where $\mathrm{R}_{\mathrm{em}}=$ (max) $\mathrm{R}_{\mathrm{e}}$.

## Grid-Resistance Effects and "Class-D" Operation of Pierce Circuit

1-298. Typical curves showing the effect of the grid resistance upon the frequency and the frequency stability of a Pierce oscillator are shown in figure 1-129. The curves in figure 1-129 (A) were obtained for plate voltages ( $E_{b}$ ) of 50,60 , and 70 volts under no-load conditions; the curves in figure 1-129 (B) were obtained for plate voltages of 75 , 100 , and 125 volts when a load resistance of 5000 ohms was connected across the plate circuit. The curves were plotted from measurements of an experimental Pierce oscillator during a USAF re-
search project under the direction of E. Roberts at the Armour Research Foundation, Illinois Institute of Technology. The frequency deviation due to a change in $R_{1}$, with a change in plate voltage is indicated by the frequency difference between the points on the curves that correspond to the same values of grid resistance. The four sets of curves for each of the two load conditions were obtained by maintaining the grid-to-cathode capacitance constant and varying the plate-to-cathode capacitance. The bottom set of curves in each graph represents the closest approach of the four sets to a $C_{k} / C_{1}$, ratio of 1 , and the top set represents approximately the largest $\mathrm{C}_{k} / \mathrm{C}_{1}$ ratio (maximum $\mathrm{E}_{1}$ ) at which oscillations can be maintained. As is to be expected the frequency deviation due to changes in voltage is greater for the larger than for the smaller values of $C_{k} / C_{p}$. However, part of this greater deviation is due to the fact that in the circuit from which these curves were plotted, the plate capacitance was obtained from a capacitor paralleled by an inductor. At the minimum effective value of $C_{p}$, the capacitor and inductor approach a state of parallel resonance, so that the rate of change in the equivalent plate reactance with a change in $R_{p}$ is larger than would be the case if no inductor were present. Also, the fact that the total load capacitance facing the crystal is smaller at the higher frequencies contributes to the frequency deviation. Partially counteracting this latter condition is the increase in the effective $Q_{e}$ of the crystal and in the $Q_{r}$ of the feed-back circuit as a whole because of the rise in frequency. There are three variables influencing the frequency that are affected by a change in the grid resistance. The first of these is the $Q_{N}$ of the grid-to-cathode impedance. As $R_{\mathrm{g}}$ becomes relatively small, $\mathrm{Q}_{\mathrm{g}}$ becomes the dominant factor determining the phase of $\mathrm{E}_{1}$ with respect to $\mathrm{E}_{\mathrm{g}}$. As $Q_{\mathrm{E}}$ decreases, the tank circuit must appear more capacitive. Thus, the reactance of the crystal unit in the feed-back arm, and hence the frequency, must increase. This is indicated by the sharply rising tails of the curves in figure 1-129. The second frequency-determining factor affected by $R_{q}$ is the effective grid-to-cathode capacitance, $\mathrm{C}_{\mathrm{F}}$. As $\mathrm{R}_{5}$ decreases, $\mathrm{C}_{\mathbb{\pi}}$ effectively increases. That is, if $R_{k}$ and $C_{k}$ are represented by an equivalent $R_{k}^{\prime}$ and $C_{g}^{\prime}$ in series, it can be shown that $C_{g}$ increases with a decrease in $R_{g}$. As a result of this effect, as $R_{g}$ becomes small, the frequency tends to decrease; but, as indicated in the upper sets of frequency stability curves of figure 1-129, when $C_{p}$ is small compared with $C_{g}$, changes in $C_{g}$ have little effect since the total load capacitance is approximately equal to the smaller capacitance. On

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the other hand, when the $C_{g} / C_{p}$ ratio is small, as indicated by the lower-frequency curves in the figure, the changes in the effective $C_{k}$ have a measurable effect upon the frequency. It can be seen at the low values of grid resistance that the effective increase in capacitance greatly diminishes the rise in frequency that would otherwise occur because of the decrease of the grid-to-cathode, $Q_{R}$. Indeed, the bottom curves in figure 1-129 (A) show that for the particular circuit and crystal unit the two opposing frequency effects of $\mathrm{K}_{\mathrm{g}}$ apparently cancel each other when $R_{g}$ is in the neighborhood of 100,000 ohms. This same set of curves indicates that a minimum frequency deviation with plate voltage occurs when the grid resistance is approximately 200,000 ohms. It is with some diffidence that we attempt to explain the reason why this particular
value of $R_{k}$ should provide a point of maximum frequency stability. Rather than interpret the effect as due to a possible optimum ratio, or as due to a possible variation of $R_{k}$ with plate voltage that tends to cancel the effect of the variation in $R_{p}$, it seems more likely that the optimum results are due to a coincidence between the third frequency factor mentioned above and the characteristics of the tube, a 6 C 4 (triode), that was used in the test circuit. This third frequency factor is the average grid bias, which tends to increase and decrease with $R_{g}$, although the variations are not pronounced when $R_{g}$ is large. As the bias increases, so also does $R_{p}$, which in turn causes the frequency to decrease. This can best be seen from an examination of the curves at the top of figure 1-129, where the effects of $\mathrm{R}_{\mathrm{g}}$ on $\mathrm{C}_{\mathrm{s}}$ ' are negligible as they affect


Figure 1-129. Frequency of tuned Pierce oscillator varsus piate voltage and grid resistance for various platetuned load capacitances. (Max) E, represents plate tuning adjustment that provided maximum r-f plate voltage when grid resistance and d-c plate voltage were values indicated by zero reference point. A 7-me CR-18/U crystal unit was used, having a PI of 49,000 ohms when operating into a rated load capacitance of $32 \mu \mu$
the frequency. As $R_{g}$ increases, the bias approaches as a limit the magnitude of the peak excitation voltage. Thus, $R_{p}$ also rises to some limiting value, causing the frequency to level off to some minimum value. If the plate voltage is increased when the tube is biased below the straight portion of the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve, one result is a decrease in $\mathrm{R}_{\mathrm{p}}$, which, in the curves of figure 1-129, clearly causes the frequency to increase. However, an increase in the plate voltage also causes an increase in the excitation voltage, and hence in the grid bias. Thus, it may well be that the point of maximum frequency stability as indicated in the bottom curves of figure 1-129 (A) is the result of an increase in bias with the increase in plate voltage just sufficient to hold $R_{p}$ constant. A class of operation such that the percentage change in $R_{p}$ due to a change in $E_{b}$ is annulled by a percentage change in $R_{p}$ due to a change in $E_{c}$, or vice versa, suggests interesting possibilities in stabilizing the plate resistance by methods other than plate-supply regulation. There is no evidence that this type of operation has been investigated, but on the strength that possibilities exist for practical application in oscillator circuits not employing a fixed bias, the name "class-D"
operation is proposed. Three subclasses are possible: " $\mathrm{D}_{1}$ ", where changes in $\mathrm{E}_{\mathrm{i}}$, can occur more or less independently and $\mathrm{E}_{\mathrm{c}}$ is the dependent variable ; " $D_{2}$," where $\mathrm{E}_{4}$ can be considered independent and $\mathrm{E}_{\mathrm{b}}$ dependent ; and " $\mathrm{D}_{\mathrm{x} .2}$ " where $\mathrm{E}_{\mathrm{b}}$ and $\mathrm{E}_{\mathrm{c}}$ are mutually dependent. Mathematically, this class of operation can be defined by the following equations:
(Class D)

$$
\begin{aligned}
& \frac{\Delta R_{p}}{R_{p}}=\frac{1}{R_{p}}\left(\frac{\partial \mathbf{R}_{\mathrm{p}}}{\partial \mathrm{E}_{\mathrm{b}}}\right) \Delta \mathrm{E}_{\mathrm{c}} \mathrm{E}_{\mathrm{b}} \text { const. } \\
& +\frac{1}{R_{p}}\left(\frac{\partial \mathbf{R}_{v}}{\partial \mathrm{E}_{\mathrm{c}}}\right) \Delta \mathrm{E}_{\mathrm{c}}=0 \\
& =\text { conat. }
\end{aligned}
$$

$1-298(1)$
(Class $\left.\mathrm{D}_{1}\right) \quad \Delta \mathrm{E}_{\mathrm{c}}=\frac{\partial \mathrm{E}_{\mathrm{b}}}{\partial \mathrm{E}_{\mathrm{c}}} \Delta \mathrm{E}_{\mathrm{b}}$
( $\Delta E_{b}$ independent)
1-298(2)
(Class $D_{2}$ ) $\quad \Delta E_{b}=\frac{\partial E_{b}}{\partial E_{c}} \Delta E_{c}$

$$
\text { ( } \Delta E_{e} \text { independent) }
$$

1-298 (3)
(Class $\mathrm{D}_{1,2}$ ) Equations (2) and (3) both apply.


Equations (1), (2), and (3) sufficiently define "class-D" operation, but the parameter, $\mathrm{R}_{\mathrm{p}}$, represents a with-signal average plate resistance, and not the instantaneous or static resistances represented by conventional $R_{j}$ curves; although the static values would apply if the signal amplitude were small relative to the bias, as would be the case if agc were being used. An increase in plate voltage can generally be expected to cause an increase in excitation and grid bias in the conventional oscillator circuits. This action, in turn, can be expected to cause an increase in the average $R_{p}$. Thus, if "class $D$ " is to be in effect, it is necessary that an original increase in $E_{b}$ cause $R_{p}$ to decrease by the same amount as the change in $\mathrm{E}_{\mathrm{r}}$ will cause it to increase. For this to occur, the plate characteristic curves must show positive slopes that increase with plate voltage; that is, the $E_{5} \mathrm{I}_{\mathrm{b}}$ curves must be curving upward in the direction of increasing $\mathrm{E}_{\mathrm{b}}$ at the operating voltage, as is quite characteristic of triode curves. Pentodes do not show this characteristic if the screen voltage is held constant, since the plate resistance tends to increase with increasing plate voltage. However, if the screen voltage varies with, and in the same direction as, the plate voltage, as can be the case when the two voltages are obtained from the same source, plate characteristics can be achieved similar to those of triodes, but with the advantages of larger values of $R_{p}$ and an independent variable ( $E_{* 2}$ ) by which the rate of change of $R_{p}$ with $E_{b}$, $\left.\partial R_{p} / \partial E_{b}\right)$, can be adjusted. Now there is an additional implied condition that must be met if class-D effects are to be achieved in conventional oscillator circuits. This is the requirement that $g_{m}$ also remain constant. For example, by equation 1-289 (2) which is repeated here

$$
R_{p}=\frac{X_{C n}\left(\mathbf{X}_{\mathrm{e}}+\mathbf{X}_{\mathrm{Cr}}\right)}{\mathbf{R}_{\mathrm{e}}-\mathbf{g}_{\mathrm{m}} \mathbf{X}_{\mathrm{Cp}} \mathbf{X}_{\mathrm{Cg}}}
$$

it can be seen that feed-back equilibrium in a Pierce circuit requires that as long as $R_{p}$, and the external circuit parameters remain constant, so also must $g_{m}$. An analogy here is to be found in class-A operation, which is defined by the operation of the tube along the straight portion of the $E_{c} I_{t}$ curve, i.e., in a region of constant $g_{n}$. Since the principal purpose of class-A amplification is a distortionless output, by implication a necessary requirement is that the operation also be in a region of constant $R_{p}$. In "class $D$," on the other hand, $a$ constant effective $R_{p}$, is the sufficient definitive condition, but in application a constant effective $g_{m}$ is a necessary implication. If $\mathbf{g}_{\mathrm{m}}$ is to remain con-
stant, equations for $\Delta g_{m}$ similar to (1), (2), and (3) for $\Delta R_{p}$ must hold simultaneously. This can be achieved in one of two ways, or a combination thereof. Assume that the plate voltage increases. If $R_{g}$ is sufficiently small for the positive excitation peak to drive the grid reasonably far above the zero point, an increase in excitation, although decreasing the average $g_{m}$ on the negative alternation, can annul this effect by increasing the average $g_{m}$ in the region above the zero grid voltage. For this to occur, the tube would have to be operated at plate voltages low enough for the zero grid point to lie well within the bend of the Er $I_{b}$ curve. This, indeed, was the state of the 6C4 tube when the curves of figure 1-129 (A) were determined. Presumably, under no-load conditions and a small $C_{k} / C_{p}$ ratio, as the grid resistance was decreased, the changes in the positive excitation peaks with changes in plate voltage were just sufficient to maintain $g_{m}$ approximately constant for values of $R_{g}$ between 100 K and 200 K . If $R_{g}$ is very large, the effect above is negligible, since any increase in the positive excitation above the zero grid voltage point becomes minor compared with the total increase of the negative alternation. For $\mathrm{g}_{\mathrm{m}}$ to be stabilized when $\mathrm{R}_{\mathrm{g}}$ is large, the change in plate voltage must make a change in the cutoff voltage comparable to the change occurring in the excitation voltage. Plate characteristics most probably favorable to "class-D" operation appear to be had with low plate voltages. Unlike the $R_{v}$ and $g_{m}$ in the conventional classes of amplifier operation, where $R_{p}$ and $g_{n}$ can be varied independently, this condition cannot exist in class-D operation of conventional oscillators, since $R_{p}$ and $g_{m}$ are tied together by the feed-back energy requirements at equilibrium. Any condition that would stabilize the one, would automatically stabilize the other. It is only $\mathbf{R}_{\mathrm{p}}$, however, that directly affects the phase of the feedback. Once $R_{p}$, becomes large relative to the impedance across the tube, the percentage variations in $g_{m}$ become very small, so that $g_{m}$ can be assumed to be a constant for all practical purposes. It is $R_{p}$ that requires critical attention if it is to be held constant. As discussed in paragraph 1-342, the curves shown in figure 1-146 strongly suggest the possibilities of "class-D" operation in the case of a Miller circuit. The solution of the "class-D" equations for a given vacuum tube and circuit can probably be approximated graphically, using families of $R_{v}$ curves versus $E_{b}$ and $E_{c}$, or curves of the deviations of the $R_{v} E_{b}$ and $R_{p} E_{c}$ curves. If rates of change of $\mathrm{E}_{\mathrm{c}}$ with $\mathrm{E}_{\mathrm{b}}$ can be obtained that provide a solution for equation (1) when the values of $E_{c}$ and $E_{b}$ are practicable, the
possibility exists that an oscillator of any type, parallel- or series-resonant, using a gridleak bias (or agc) can be designed so that for all practical purposes it is independent of small fluctuations in the plate-supply voltage. Empirically, "class-D" operation is indicated at the point or points where the frequency deviation curves of an oscillator change in sign, or where frequency curves, such as those in figure 1-129, cross or touch each other. A full analysis of this class of vacuum-tube operation is beyond the scope of this handbook. It is suggested here only as a possible line of inquiry.

## Gridleak Resistance and Output Voltage Stability of Pierce Circuit

1-299. The stability of the output voltage depends largely upon how readily the gridleak bias can follow small fluctuations in the excitation voltage. Imagine, for example, that the vacuum tube is being operated class $C$, and that after equilibrium is reached the positive peak of a certain excitation cycle happens to be slightly higher than the average. The average bias during the succeeding cycle will thus be slightly more negative than is normal, so that during this period the tube is conducting a smaller fraction of the time, and the peak excitation voltage will drive the grid less positive than before. This means that the amplification during this cycle will be less than the amplification during the preceding cycle. If the $R_{r} C_{F}$ time constant is extremely large compared with the period of a cycle, the bias remains relatively fixed for the duration of several cycles. In which case the peak of several succeeding cycles must rise to progressively lower points on the $E_{4} I_{b}$ curve. The oscillations will continue to decay until a sufficient amount of the bias charge of $\mathrm{C}_{\mathrm{g}}$ has leaked through $\mathrm{R}_{\mathrm{k}}$ to permit oscillations to again build-up. For this reason $R_{k}$ cannot be increased indefinitely without the risk of the oscillator becoming self-amplitude-modulated. As $R_{k}$ is gradually increased, the amplitude sooner or later begins rising and falling at a radiofrequency rate. If $R_{k}$ is further increased, the modulation of the output can fall within the audio range. Finally, with extremely large values of $\mathrm{R}_{\mathrm{k}}$, the circuit behaves as a damped-wave blocking oscillator. Now, assume that $\mathrm{R}_{\kappa}$ is infinite. As oscillations build up, the bias for each cycle is essentially the same as the peak excitation voltage of the preceding cycle. Eventually a peak excitation voltage is attained which causes the bias for the next cycle to be too great for the circuit to be resupplied with all the energy that will be lost during the period of the cycle. If the peak bias is equal to or greater than the cutoff bias, the oscil-
lations will die out completely, since any decrease in excitation with class- $C$ bias means a decrease in average amplification. To avoid this possibility, it is important that sufficient electrons escape from the grid so that, at the beginning of the cycle immediately following the first peak cycle, the bias will have returned to approximately the same starting point. Expressed in another way, to avoid the intermittent activity, there must be an assurance that the positive peak of every cycle will drive the grid positive. This assurance is to be had for all operating conditions if the bias voltage decreases at a greater rate than would the positive excitation voltage peaks if the tube were cut off for a complete cycle. In practice, the vacuum tube can be conducting in polar opposition to $E_{p}$ and hence effectively supplying energy to the circuit during the entire negative alternation of an $E_{v}$, cycle. Nevertheless, if there is an assurance that the bias voltage drops as fast as the peak excitation voltage when no energy is being supplied to the circuit, the bias reduction is certainly sufficient if the net rate of energy-loss is reduced by virtue of a variable release of energy by the tube throughout a large part of each cycle. The problem, then, becomes one of first determining the percentage change in the peak excitation voltage that would occur during the period of one cycle if the tube were suddenly cut off.
1-300. At the instant that $I_{k}$ is a maximum, the voltages across the reactances in the tank circuit are zero, and none of the circuit energy is stored in the capacitances. All the stored energy at that instant is in mechanical form, and is equal to the kinetic energy of the crystal as it swings through its position of zero potential energy. As discussed in paragraph 1-249, this stored energy is equal to $I_{*}{ }^{2} L$, where $I_{*}$ is the series-arm current, and $L$ is the equivalent series-arm inductance. Now, when the crystal appears as an inductance, $X_{s}$ is approximately equal to $I_{g}$ plus the current, $I_{C o}$, which flows through the shunt capacitance, $\mathrm{C}_{0}$, of the crystal unit. (Only che unsigned magnitudes of $\mathrm{I}_{\mathrm{g}}$ and $\mathrm{I}_{\mathrm{C}_{0}}$ are considered here.) We can say, approximately, that the stored energy is equal to $\left(I_{z}+I_{C o}\right)^{2} L$. As is also discussed in paragraph 1-249, the ratio of stored energy to the energy dissipated per radian, is equal to the $Q$ of the circuit, which in this case is effectively $\frac{\omega L\left(I_{g}+I_{C_{0}}\right)^{2}}{\left(R_{e}+R_{g}^{\prime}+R_{L}\right)_{g}{ }^{2}}$, or the equivalent value, $\frac{\omega L\left(I_{g}+I_{C_{0}}\right)^{2}}{R\left(I_{\varepsilon}+I_{C_{0}}\right)^{2}+\left(\mathrm{R}_{\mathrm{g}}^{\prime}+\mathrm{R}_{\mathrm{L}}{ }^{\prime}\right) \mathrm{I}_{\mathrm{g}}{ }^{2}}$, where $R_{L}{ }^{\prime}$ is the equivalent load resistance when represented as in series with the plate-circuit capacitance, and $R$ is the series-arm resistance of
the crystal. If $\mathrm{R}_{\mathrm{g}}^{\prime}$ and $\mathrm{R}_{\mathrm{r}}{ }^{\prime}$ can be considered negligible, the circuit $Q$ will be the actual crystal $Q\left(=\frac{\omega L}{R}\right)$. Assume that the plate current is cut off for an entire cycle, which is a period of $2 \pi$ radians. The fraction of the energy dissipated during this time is approximately equal to $2 \pi / \mathrm{Q}=$ $\mathrm{R} / \mathrm{fL}$, if Q is of sufficient magnitude that the percentage decrease in current is not large. Since the energy is proportional to the square of the voltage, the equivalent decay in peak excitation voltage is $\mathrm{E}_{\mathrm{km}} \sqrt{\mathrm{R} / \mathrm{fL}} \approx\left|\mathrm{E}_{\mathrm{c}}\right| \sqrt{\mathrm{R} / \mathrm{fL} \text {. If } \mathrm{E}_{\mathrm{c}} \text {, the grid bias, }}$ whose magnitude only we shall consider, is to decrease at the same rate, the bias charge, equal to $\mathrm{C}_{6} \mathrm{E}_{\mathrm{c}}$, must leak through $\mathrm{R}_{\mathrm{g}}$ at an average rate of $\mathrm{C}_{6} \mathrm{E}_{\mathrm{r}} \sqrt{\mathrm{R} / \mathrm{fL}}$ during the period of one cycle. Thus

$$
\begin{equation*}
(\min ) I_{c}=\frac{E_{c}}{(\max ) R_{g}}=\mathrm{fC}_{\mathrm{g}} \mathrm{E}_{\mathrm{c}} \sqrt{\mathrm{R} / \mathrm{fL}} \tag{1}
\end{equation*}
$$

The maximum safe value of $\mathrm{R}_{\mathrm{s}}$ for all operating conditions, if $\mathrm{R}_{\mathrm{R}}{ }^{\prime}$ and $\mathrm{R}_{\mathrm{t}}{ }^{\prime}$ are negligible compared with $R_{c}$, according to equation (1) is

$$
\begin{equation*}
(\max ) \mathrm{R}_{\mathrm{g}}=\sqrt{\mathrm{L}} / \mathrm{C}_{\mathrm{k}} \sqrt{\mathrm{fR}} \tag{2}
\end{equation*}
$$

Since $\sqrt{L}=1 / \omega \sqrt{C}$, where $C$ is the equivalent series-arm capacitance, and since $C \approx \frac{\mathrm{C}_{0}}{\mathrm{r}}$, in the case of partially plated elements, where $r$ is approximately equal to the theoretical capacitance ratio, $r_{\text {c., }}$ given in figure 1-95, then, on substitution in equation (2)

$$
\begin{equation*}
(\text { max }) R_{k}=\frac{\sqrt{r}}{\omega C_{g} \sqrt{f R C_{o}}} \tag{3}
\end{equation*}
$$

In paragraph $1-297$ it was shown that when $\mathrm{C}_{\mathrm{k}}=2 \mathrm{C}_{\mathrm{x}}$, if $\mathrm{R}_{\mathrm{k}}$ is to be considered negligible it should be at least 15 times the minimum permissible PI. Assume that $R_{g} /(\min ) P I=k$, $(k$ is not to be interpreted here as a symbol for any quantity other than the ratio defined) and that it is desired that $\mathrm{k}=\mathrm{k}_{\mathrm{w}}$, its maximum value consistent with equation (3), above. Let it also be assumed that $\mathbf{R}$ is approximately equal to $\mathrm{R}_{\mathrm{em}}$, the maximum permissible value of $\mathrm{R}_{\mathrm{e}}$, that $\mathrm{C}_{8}=2 \mathrm{C}_{\mathrm{x}}$, and that $\mathrm{C}_{\mathrm{o}}=\mathrm{C}_{\mathrm{ow}}$, the maximum permissible shunt capacitance specified for the crystai unit. Then,

$$
(\max ) R_{\mathrm{k}}=\mathrm{k}_{\mathrm{m}}(\min ) \mathrm{PI}=\mathrm{k}_{\mathrm{m}} / \omega^{2} \mathrm{C}_{\mathrm{x}}^{2} \mathrm{R}_{\mathrm{em}}
$$

also

$$
(\max ) \mathrm{R}_{\mathrm{x}}=\sqrt{2 \pi \mathrm{r}} / 2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{\omega \mathrm{C}_{\mathrm{om}} R_{\mathrm{em}}}
$$

Thus,
$(\max ) \mathrm{R}_{\mathrm{g}} /(\min ) \mathrm{PI}=\mathrm{k}_{\mathrm{m}}=\frac{\omega \mathrm{C}_{\mathrm{x}} \frac{\sqrt{2 \pi r \mathrm{R}_{\mathrm{em}}}}{2 \sqrt{\omega \mathrm{C}_{\mathrm{om}}}}}{2 \sqrt{2}}$
1-300 (4)
or

$$
\begin{equation*}
\mathrm{k}_{\mathrm{m}}^{2}=\pi \mathrm{r}\left|(\min ) \mathrm{X}_{\mathrm{Co}}\right| / 2(\min ) \mathrm{PI} \tag{5}
\end{equation*}
$$

It will be found in practice that the limiting values of $k_{m}$ given by equations (4) and (5) are normally smaller than the minimum desired value of 15 . If this should be the case in an actual circuit, the assumption that the power losses in the grid circuit are negligible can no longer be made, and the actual value of $\mathrm{k}_{\mathrm{m}}$ would be even less than that given above. The factor $\sqrt{R / f L}$ in equation (1) is derived upon the assumption that only the crystal losses are significant. If this is not to be the case, this factor should be replaced by one equal to $\sqrt{\frac{\text { total energy expended per cycle }}{\text { energy stored }}}$. Now, even though it would seem from equations (4) and (5) that $\mathrm{R}_{\mathrm{g}}$ cannot be safely made more than 5 to 10 times larger than the minimum PI, particularly if an AT cut is employed, since it has a value of $r$ of only 250 , and since $\mathrm{C}_{x}$ is normally no greater than 4 or 5 times $C_{\text {amm }}$, it should be remembered that the value of $\mathrm{k}_{\mathrm{m}}$ above is based upon the assumption that no energy is being fed to the circuit during an entire cycle, so that the net loss is equal to the gross loss. This condition is only approached in high-efficiency class-C circuits where the operating bias is several times the cutoff bias. Except in the case of power oscillators, such operation is not feasible because of the high operating voltages that are required. The larger the fraction of the cycle during which the tube is conducting, the larger the ratio of the usable $\mathrm{R}_{\mathrm{k}}$ to that given by equation (3). If the tube is conducting one-half the time, class- B operation, the maximum safe $\mathrm{R}_{\mathrm{g}}$ is more than twice that given by equation (3). For class- B and class-C operation, the output stability is almost entirely dependent upon the automatic adjustment of the bias, for any decrease in signal strength will mean a decrease in over-all amplification unless the bias can drop immediately to allow more energy to be fed to the circuit. On the other hand, it was found in paragraph 1-294 that if an oscillator tube is operated at a bias immediately above the knee of its $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve, the bias can remain fixed and the variations in excitation directly produce a change in amplification that tends to annul the original variation. If the tube
voltages are so selected that a gridleak bias at equilibrium is also at the optimum fixed-bias point, then limiting can be achieved both from the gridleak action and the excitation swings. Under these conditions, $\mathrm{R}_{\mathrm{g}}$ can be safely increased to values beyond one megohm, even at high frequencies. As a design consideration, however, the gap between the theoretical and the practical solution can prove quite wide. Among the optimum-bias bugs that resist extermination; there is the difficulty of finding a vacuum tube having the desired operating characteristics, and once found, there is the additional problem of maintaining an optimum operating state with crystal units having different values of effective resistance. These problems are discussed in some detail in succeeding paragraphs. The main problem is to reduce the grid losses to negligible proportions without endangering the output voltage stability. This can normally be done with any parallel-resonant crystal oscillator if the tube is conducting throughout most of each cycle.

## Gridleak Resistance and Output Control in Pierce Circuit

1-301. If it is necessary for a Pierce oscillator to provide a higher voltage output than can be obtained under the conditions of maximum frequency stability, the $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$, ratio can be increased. If the total load capacitance is to remain constant, $\mathrm{C}_{\mathrm{k}}$ will necessarily be larger, and the excitation voltage smaller, so a smaller value of $\mathrm{R}_{\mathrm{g}}$ can be used without the grid losses becoming significant. If the capacitance ratio is to be adjustable in order to permit an operator or technician to control the output voltage. $\mathrm{R}_{\mathrm{F}}$ cannot be made larger than that value which would permit a stable output with the largest operable value of $\mathrm{C}_{\mathrm{k}}$ at the highest frequency at which the oscillator is to be used. If such an adjustment is to be provided in a Pierce circuit, $C_{k}$ and $C_{p}$ should be so ganged as to always provide a constant load capacitance. This problem is discussed in paragraph 1-318. Insofar as the grid-tocathode resistance is concerned, the maximum safe value of $R_{k}$ becomes less if $C_{k}$ is to be variable than otherwise. Without changing the $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{p}}$ ratio, larger outputs can be achieved by reducing the value of $R_{k}$ to a point where the grid leakage is so great that the average bias is considerably smaller than the peak excitation voltage. With this the case, the oscillations must build up to higher amplitude levels before equilibrium can be reached. Although the maximum excitation is still fixed by the rated drive level of the crystal unit, the output can be controlled somewhat within this restriction by a variable $R_{r}$. At the higher frequencies, this
method of output adjustinent requires such low values of $\mathrm{R}_{\mathrm{g}}$ that the grid losses seriously affect the frequency stability. However, at very low frequencies, a variable $R_{5}$ could be feasible as a means of adjusting the output of a Pierce circuit to a desired level when one crystal unit is replaced by another of different effective resistance. Although such a design feature has no particular recommendation, it could be preferred over those methods of output control that require adjustment of the $\mathrm{C}_{\mathrm{E}} / \mathrm{C}_{\mathrm{p}}$ ratio, which risk changes being made in the total load capacitance. With grid control, the lowest adjusted value of $\mathrm{R}_{\xi}$ could be designed to provide the desired output when a crystal unit of maximum effective resistance (minimum PI) is connected in the circuit; whereas the larger values of $R_{g}$ could ensure the same output with some theoretical minimum value of effective resistance. Since the crystal current, $I_{k}$, is practically constant as long as the output voltage $\mathrm{E}_{\mathrm{i}}$ is constant, the power losses in the crystal, equal to $I_{k}{ }^{2} R_{\text {w }}$, tend to vary directly with $R_{e}$, as long as $E_{p}$ is held constant by adjustments of $R_{k}$. Under those conditions where the capacitance ratio does not change, a maximum crystal drive level is required for the crystal unit of maximum $R_{\text {s }}$, and a minimum crystal drive level when $R_{v}$ is a minimum--the reverse of those conditions discussed in paragraph 1-294 when a fixed bias instead of a fixed output is assumed.
1-302. As applied to crystal oscillators in general it cannot be said that a variable gridleak resistance is advisable except for test purposes or unless its purpose is to obtain the minimum possible grid losses when changing from one crystal unit to another. As an output-voltage control device other methods are generally to be preferred. Except at very low frequencies, the resistance values necessary to appreciably lower the average bias are too small to prevent the grid losses from becoming a significant frequency-determining factor. This statement, of course, only expresses a general rule, and in specific instances the inter-relations among the circuit variables may be such as to annul the effects upon the frequency. For example, the bottom set of curves in figure 1-129(A) is to be expected theoretically to indicate a greater frequency stability when $R_{g}$ is 1 megohm rather than when it is 0.2 megohm, but this effect was not observed. Figure 1-130 shows curves of output voltage obtained from the same experimental oscillator that was used in plotting the curves of figure 1-129. Although the curves are plotted as output-voltage versus crystal driving power, it should be understood that the actual independent variable for each

## Crystal Oscillators

curve is the plate voltage. Each curve represents a particular value of grid resistance. The cross lines intersect the curves at points corresponding to the same values of plate voltage. From figure $1-130$ it can be seen that large percentage changes in the grid resistance can cause changes in the output voltage on the order of 30 per cent or so, but which increase sharply as $R_{z}$ becomes small. 1-303. If an adjusable output voltage is desired, probably the best solution to the problem is to use a screen-grid tube having an r-f-bypassed, variable, voltage-dropping resistor in series with the screen supply voltage. Varying this resistance will control the output of the tube and the crystal driving power. The maximum permissible output voltage must be determined on the assumption that the crystal unit has the maximum permissible $\mathbf{R}_{e}$. Since $I_{g} \approx \frac{E_{p}}{X_{e}+X_{C r}}$ and the maximum permissible $I_{g}=\sqrt{P_{c m} / R_{e m}}$, where $P_{c m}$ and $R_{\text {em }}$ are the maximum crystal driving power and effective resistance, respectively, then the maximum permissible constant $\mathrm{E}_{\mathrm{p}}$ is

$$
(\max ) E_{p}=\left(X_{e}+X_{C g}\right) \sqrt{P_{e m} / R_{e m}}
$$

If it is assumed that $X_{C_{g}} \approx X_{O_{p}} \approx \frac{X_{X}}{2}$, where $\mathrm{X}_{\mathbf{x}}\left(=-1 / \omega \mathrm{C}_{\mathrm{x}}\right)$ is the total load reactance equal and opposite to $X_{e}$, equation (1) becomes

$$
(\max ) E_{p}=\sqrt{\frac{P_{\mathrm{em}}}{R_{e n t}}} / 2 \omega C_{x}
$$

According to equation (2), the maximum permissible constant $E_{p}$ varies inversely with the crystal frequency. If the oscillator is to be used at more than one frequency, and at the same time is to provide the same output voltage regardless of the frequency, the maximum $E_{p}$ is that value given by equation (2) for the crystal unit of highest frequency, assuming the crystal specifications are the same for all frequencies. With the ratio of $\mathrm{C}_{g} / \mathrm{C}_{\mathrm{p}}$ approximately equal to one, equation (2) also gives the value of $E_{k}$, which obviously will also remain constant. $R_{z}$ can be made quite large, so that $\left|\mathbf{E}_{c}\right|$ will approximately equal $\mathrm{E}_{\mathrm{p}} \sqrt{2}$. With $\mathrm{E}_{\mathrm{c}}$ constant, and with the plate voltage $\mathrm{E}_{\mathrm{b}}$ also assumed to be constant, the operating position of the tube on the $E_{r} I_{b}$ curve largely becomes the function of the screen voltage. As the screen voltage is increased, $g_{m}$ increases, which means that the slope of the


Figure 1-130. Output curves of tuned Pierce oscillator for different values of grid resistance when reactance of tuned plate circuit is adjusted for output voltages equal to 50 percent of the maximum attainable. A 7 -mc CR-18/U crystal unit was used, having a PI of 49,000 ohms when operating into its rated load capacitance of $32 \mu \mu$
$\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve becomes steeper. Also, the cutoff bias is increased. Since $E_{e}$ is being held constant, the effect is one of shifting the operating bias, percent-age-wise, closer to or farther up the straight portion of the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve. From the point of view of using as large a value of $\mathrm{R}_{\mathrm{g}}$ as is possible, it is desirable that the operating position be just above the knee of the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve when the screen voltage is to be a maximum, i.e., when $R_{e}$ of the highestfrequency crystal unit is a maximum.

## Gridleak Resistance and Oscillator Keying of Pierce Circuit

1-304. If avoidable, a crystal oscillator should not, itself, be keyed. For one reason, the oscillation build-up time is not negligible if rapid telegraph keying is desired. As the operable speed limit is approached the wave shape becomes distorted and the harmonic output is considerably increased. Even the keying of a crystal oscillator in a push-to-talk voice transmitter is not desirable if frequency stability is important, since on-and-off operation constantly raises and lowers the crystal temperature. Thus, the frequency is kept in a state of constant variation to a degree dependent upon the magnitude of frequency-temperature coeffi-
cient of the crystal unit at the average operating temperature. Unless necessary for reasons of economy in space, cost, or the like, the oscillator should be designed for continuous operation and the keying performed in one or more of the succeeding amplifier stages. Usually the keying circuit is designed to remove and apply by one means or another, a cutoff bias in the buffer-amplifier stage. During the time that the buffer amplifier is cut off, the crystal circuit continues to oscillate, but the signal cannot be amplified and applied to the succeeding stages.
1-305. When it is necessary to key the oscillator, itself, the reason is normally that the space and weight requirements are so limited that no more than one or two vacuum-tube stages can be allowed. For this same reason, the oscillator is probably required to develop as much output power as possible, so that a Miller, rather than a Pierce circuit is generally employed if crystal control of the frequency is required. Nevertheless, the factors affecting the build-up time are approximately the same in either circuit. Fundamentally, the reason that a crystal oscillator requires a relatively much longer build-up time than does a conventional in-ductor-capacitor tuned circuit of the same reso-

nant frequency, is because the energy to be stored in the crystal is much greater than that which would be stored in an inductor-capacitor circuit. For a given tank current, the stored energy is proportional to the inductance, so, to a first approximation, we can suppose that the build-up time of, say, a Pierce oscillator as compared with that of a Colpitts oscillator of the same frequency, is directly proportional to the inductance ratio. On the other hand, it can be imagined that the build-up time tends to vary inversely with the total effective resistance in the tank circuit. The greater this resistance, the more quickly do the losses in the circuit rise to equilibrium with the rate of energy supply. The build-up time also tends to vary inversely with the frequency. Clearly, if the frequency were one cycle per second, equilibrium could not be reached in a shorter period. Finally, the build-up time is a furction of the electromechanical coupling of the crystal to the circuit. The larger the $\mathrm{C}_{0} / \mathrm{C}$ ratio of the crystal unit, the weaker is the coupling and the longer is the period before equilibrium can be reached. The exact relations of all the circuit variables in an equation expressing the time required for the amplitude to rise to within one per cent or so of its equilibrium limit would, indeed, be quite involved. Insofar as the crystal is concerned, the build-up time can be expected to vary positively if piotted against L, C, $\mathrm{C}_{0}$, and $1 / \mathrm{R}$ of the crystal unit. The percentage variation of the build-up time with a given percentage variation in L can be expected to be greater than with the same percentage variation in C, because of the fact that, say, an increase in C, although increasing the build-up time by lowering the frequency, will also tend to decrease the buildup time by improving the electromechanical ratio. Thus, if the frequency remains constant, a crystal oscillator can be keyed at a faster rate if the L/C ratio is kept to a minimum, provided $\mathrm{C}_{6}$ is not increased. In other words, a crystal element should be chosen that has as large a piezoelectric effect as possible, provided the frequency-temperature coefficient is small. For example, for high-frequency circuits, an AT-cut crystal which has a capacitance ratio $\frac{\mathrm{C}_{0}}{\mathrm{C}} \approx 250$ is to be expected to provide better keying characteristics than a BT-cut crystal, which has capacitance ratio of 650 . Preferably, from the point of view of a maximum keying speed for a given output voltage, the gridleak resistance should be kept small, not only to load the circuit and to provide quick-action limiting, but also to keep the positive swings of the grid and the transconductance high. The oscillator will almost cer-
tainly be designed for maximum power output, so that the tank circuit will be well loaded, for which reason the grid resistance must be kept relatively small as a safeguard against intermittent oscillations. It is questionable as to just how much the effective tank resistance limits the build-up time. Of course, if the resistance were zero, the oscillations would theoretically continue to rise indefinitely. On the other hand, the time required for the amplitude to reach any given value is least when the energy being lost from the circuit is least. In this respect, the build-up time tends to vary directly, not inversely, with the tank resistance. It would seem, that to obtain a maximum keying speed it might be preferable to use a fixed bias or a cathode bias, instead of the gridleak action. Using a sharp-cutoff tube biased for class-A operation, a grid, plate, or output circuit limiting arrangement could permit the oscillations to build up to a given level under conditions of a maximum ratio of input to dissipated power. Above this amplitude level the ratio would sharply decrease. Such a circuit could raise the permissible keying speed, but since this is accomplished by virtue of sudden changes in the circuit parameters, which changes always accompany to some extent any limiting action, an increased frequency instability and harmonic output are almost certain to result. Although a crystal oscillator should not be designed to be keyed unless absolutely neeessary, experimental circuits have obtained keying speeds approaching 400 words per minute. The higher the keying speed, however, the greater must be the frequency tolerance.

## Gridleak Resistance When Pierce Circuit Permits Switching from Crystal to Variable LC Control

1-306. It is often necessary to provide a variabletuned, inductor-capacitor auxiliary circuit to permit emergency operation at frequencies other than those provided by the available crystals, or in the event of crystal failure. For this purpose it is often possible and is usually desirable to use the same vacuum tube that is used during crystal control. For example, a Pierce circuit could be readily converted to a Colpitts circuit simply by switching from the crystal to a tuning inductor, or to an inductor shunted by a variable capacitor. However, when such a conversion is made, the ratio of the stored energy to the power dissipation becomes much smaller than that during crystal control. For this reason, the maximum safe value of gridleak resistance is much smaller than during crystal operation. For output voltages comparable to those obtained with crystal control, the LC circuit em-
ploys gridleak resistances ranging from 20,000 to occasionally 100,000 ohms. If the LC fircuit is intended to furnish a much greater oy put than the crystal circuit, lower values of R . may be necessary. Rather than require the crystal circuit to operate with small values of $R_{k}$, it would be preferable to connect an additional shunt resistor in the grid circuit when switching to variable-tuning control.

## Gridleak Resistance When Used, with Cathode Biasing Resistor in Pierce Circuit

1-307. In addition to the voltage across the gridleak resistance, part of the bias voltage can be furnished by an r-f-bypassed resistance in the cathode circuit. The cathode resistor protects the tube from excessive plate current should oscillations cease, and has the additional advantage of reducing the grid current and, hence, the grid losses. The power expended in the grid circuit will be approximately equal to $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{c}}$ where $\mathrm{E}_{\mathrm{r}}$ is the total bias and $I_{c}$ is the grid current. Actually, unless an r-f choke is used in the grid circuit, the grid losses will be somewhat greater than $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{e}}$ because of the a-c component of voltage across $R_{g}$. As the cathode component of the bias becomes small, the grid losses approach $1.5 \mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{c}}$ as a limit. See paragraph 1-296. The values of the cathode resistance, $R_{k}$, usually range from 100 to 1000 ohms. The reactance of the bypass capacitor should be at least as small as $R_{k} / 10$ at the lowest operating frequency. With $R_{k}$ connected between cathode and ground, the d-c voltage developed equals $\left(I_{b}+I_{c}\right) R_{k}$; or approximately, $I_{b} R_{k}$. The total bias,
$\mathrm{E}_{\mathrm{c}}$, is still approximately equal to $\sqrt{2} \mathrm{E}_{\mathrm{x}}$. The d-c grid current is given by the equation

$$
I_{c}=\frac{\left|E_{c}\right|-E_{k}}{R_{k}}=\frac{\sqrt{2} E_{k}-I_{b} R_{k}}{R_{g}}
$$

where $E_{k}$ is the voltage across the cathode resistor.

## AGC USED WITH PIERCE OSCILLATOR

1-308. Where space and cost permit, optimum output stability can be had when the oscillator bias is provided through an automatic-gain-control circuit. Gridleak action can be effective in initiating oscillations, but the bias furnished through AGC should be of much greater magnitude in order to be of maximum effectiveness. A small increase in output voltage must cause a large increase in bias. The use of AGC reduces the grid losses to a minimum and maintains a constant amplitude of oscillation. It is this latter feature that is, of course, of most importance-particularly so when the same oscillator is to be switched from one crystal unit to another. The voltage requirements for constant output without risking the overdrive of any of the crystals are the same as those that apply in the case of manual adjustment of the output. (See paragraph 1-302.) An A-G-C circuit applicable for use with a Pierce, or Miller, type oscillator, is shown in figure 1-131. The oscillator output is amplified by $V_{2}$. The output of $V_{2}$ is then rectified by $V_{3}$. The oscillator bias equals the average rectified voltage across $R_{3} . C_{1}$ bypasses the $r-f$ component to ground. If $R_{3}$ were increased indefinitely the


Figure 1-131. Piarce oscillator with automatic gain control

Section I
bias voltage would approach in magnitude the peak value of the $V_{2}$ output voltage. $R_{1}, R_{2}$, and $R_{3}$ gre not critical-each can be made equal to 50 K /if a faster-acting gain control is required. However, $\mathrm{R}_{1}$ should be kept as large as possible. Assume that the r-f losses in $R_{1}, R_{4}$, and $R_{s}$ are negligible and that $C_{p}$ and $C_{g}$ are approximately equal/so that $V_{1}$ is operating into a load impedance approximately equal to PI/4. Under these conditions $\mathrm{g}_{\mathrm{m}}$ will be the minimum and $\mathrm{R}_{\mathrm{p}}$ the maximum possible for sustained oscillations as long as the load capacitance across the crystal unit remains constant. The actual values of $g_{n}$ and $R_{p}$ are fixed by the vacuumtube characteristics. Although the effective parameters of the tube are directly dependent upon the peak-to-peak magnitude of the excitation, as well as indirectly through the bias, it can be said that to a first approximation the equilibrium $R_{p}$ and $g_{m}$ are associated with a bias of more or less definite magnitude if the plate voltage is constant, and that approximately the same bias must exist regardless of whether it is developed by gridleak action or by AGC. Thus, the difference between AGC and grideak control is not primarily in the magnitude of the bias, but in the amplitude of oscillations. Gridleak action requires that the peak excitation voltage of $V_{1}$ be slightly greater than the required bias; AGC requires that the peak excitation voltage of $V_{2}$ times the voltage amplification of the $\mathrm{V}_{2}$ stage be slightly greater than the required bias of $V_{1}$. If the peak excitation voltage of $V_{z}$ is assumed to equal $E_{p m}$, which, in turn, is assumed to equal $\mathrm{E}_{\mathrm{km}},\left(\frac{\mathrm{C}_{\mathrm{g}}}{\mathrm{C}_{\mathrm{R}}} \approx 1\right)$, and $\mathrm{k}_{3}$ is the effective amplification of the $\mathrm{V}_{2}$ stage, then

$$
\left|\mathrm{E}_{\mathrm{e}}\right|=\mathrm{k}_{\mathrm{z}} \mathrm{E}_{\mathrm{km}} \quad 1-308(1)
$$

or

$$
\mathrm{E}_{\mathrm{gm}}=\left|\mathrm{E}_{\mathrm{c} /} / \mathrm{k}_{2}\right|
$$

Since $E_{c}$ is approximately fixed, it can be seen that the amplitude of oscillations is only $\frac{1}{\mathrm{k}_{\mathrm{z}}}$ as large as those that would exist by the gridleak method employing the same plate voltage. This is not a desirable feature where large output is required, but from the point of view of ensuring a low crystal drive and maximum stability, an A-G-C circuit has great advantages. Although the equilibrium amplitude is low, oscillations start as readily as with grideak bias. AGC permits class-A operation with remote-cutoff tubes, and, since the limiting is very slow-acting, very pure sine-wave outputs and excellent frequency stability as well as amplitude stability is obtainable.

## PLATE-SUPPLY CIRCUIT OF <br> \section*{PIERCE OSCILLATOR}

1-309. For optimum frequency stability it is important that the $r$-f impedance of the $B+$ circuit be as high as possible relative to the impedance of the tank. If $C_{g} / C_{p}=1$, the tank impedance equals PI/4. If the oscillator is intended to oscillate at only one frequency, or within a narrow frequency, range, it is generally preterable that the $\mathrm{B}^{+}$voltage be fed through an r-f choke. This method affords a maximum impedance with minimum loss and minimum voltage at the $B^{+}$source. The inconvenience of an r-f choke is that its impedance changes with frequency, being inductive below its effective parallel-resonant point, and capacitive above. As long as this effect does not change the effective value of $\mathrm{C}_{\mathrm{p}}$ by more than $\pm 10$ per cent, the total load capacitance will not change by more than 5 per cent, if $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}=1$. Within these limits the use of a choke is to be preferred. For wide frequency ranges, a resistor should be used in the plate circuit, such as $R_{4}$ in figure 1-131. It is desirable for this resistance to be as high as 50 K , or higher, from the point of view of frequency stability. On the other hand, the larger the resistance the higher the $B^{+}$voltage source must be to provide a given plate voltage. Plate-supply resistances on the order of 5000 to 10,000 ohms have one other important advantage besides permitting lower $B^{+}$sources. They load the oscillator tank so that differences in the resistance of the crystal from one unit to the next have very little effect upon the output impedance of the tube. Hence, when a change is made from one crystal unit to the next, the output voltage remains approximately the same.
1-310. The proper compromise in selecting a platecircuit resistance depends upon the frequency-tolerance limits. The plate-circuit resistance does afford a certain frequency-stabilizing effect that is not provided by an r-f choke, particularly so when agc is used. The effect is one of reducing the change in $R_{p}$ of the vacuum tube caused by a change in grid bias. For example, if the bias becomes more negative $R_{p}$ increases, and $I_{b}$, the average plate current, decreases. There is then less voltage drop across the plate-supply resistor, and the resulting increase in plate voltage tends to decrease $R_{p}$, thereby annulling part of the increase in $R_{p}$ due to the change in bias. The plate-voltage source should be regulated, if good stability is required. Where the frequency deviation must be kept to a minimum, the oscillator may require a separate rectifier unit, filter circuit, and voltageregulator circuit.

## CHOOSING A VACUUM TUBE FOR THE PIERCE CIRCUIT

1-311. It is no problem to find a vacuum tube that will permit a Pierce circuit to oscillate. Indeed, one of the major problems in tube circuit design is to prevent oscillations from occurring. With a crystal connected between the plate and grid of any vac-uum-tube amplifier, the stray capacitance in the circuit is usually sufficient to cause oscillations to build up. If the plate voltage is not so high that the crystal is over-driven, the frequency stability of a stray-capacitance circuit may even be satisfactory for general-purpose use. Thus, the problem is not to find a vacuum tube that will work, but one that will be most satisfactory from the point of view of output stability and cost. First, a large tube is not necessary, since the Pierce circuit is not suited for large output. The choice of tube will depend somewhat upon the exact purpose of the oscillator and of the equipment of which it is a component. If the frequency tolerance is to be large, little thought need be given to fine points in the design, for the principal problem will be to keep the production costs to a minimum. A triode would be satisfactory, a 5 K to 50 K resistance in the plate circuit, a $\mathrm{C}_{\mathrm{z}} / \mathrm{C}_{\mathrm{p}}$ ratio between 1 and 2 , and a plate voltage sufficiently low so that the driving power of the crystal does not exceed the rated level for any effective crystal resistance meeting the specifications. A high-mu triode generally provides the better frequency stability because of its larger effective $\mathrm{R}_{\mathrm{p}}$, but it will have a higher plate dissipation for the same output voltage. Of the high-mu triodes, probably the 6AB4 is to be preferred as a simple unit, and the 12AX7 and the 12AT7 as twin triodes. It is the medium-mu tube that has been the most favored by design engineers when a triode has been chosen. Of these the $6 \mathrm{C4}, 6 \mathrm{~J} 4$, and 7A4 single units, and the 6SN7-GTA twin unit are among the more popular. The 6C4 and the 6 J 4 are to be preferred for high-frequency operation. Since the 7A4 and the 6SN7-GTA have approximately $4 \mu \mu \mathrm{f}$ capacitance between grid and plate, the 6C4, 6J4, 6.76, or the 12AU7, each with $1.5 \mu \mu \mathrm{f}$ capacitance grid to plate, should provide the better frequency stability - particularly at high frequencies. The 7A4 and the 6SN7-GTA are generally more satisfactory for use in a Miller circuit. Where greater frequency stability is required, a pentode should be used. A pentode has the advantages of low plate-to-grid capacitance, greater $\mathrm{R}_{\mathrm{p}}$, and a screen grid whose voltage can be adjusted independently of the control-grid bias and plate voltage, thereby permitting a greater range of adjustments in the plate characteristics. Con-
ventional pentodes must be operated at reduced voltages, to avoid overdriving the crystal, unless rather high $\mathrm{C}_{z} / \mathrm{C}_{p}$ ratios are used. Subminiature pentodes have operating characteristics at their normal operating voltages ideally suited for crystal drive levels. The 1U4 is one such type having a sharp cutoff. Among the miniature pentodes having a sharp cutoff, the 6AU6, 6BC5, and 6AH6 are tubes generally recommended for wide-band, h-f circuits. The 6CB6, although designed principally for television use at 40 mc , should also be quite appropriate in crystal oscillator circuits. Remotecutoff tubes are generally used only in special circuits. For example, if a low harmonic output is required, such tubes could be employed in conjunction with AGC. When the harmonic content is not of first importance, AGC is more effective if used with sharp-cutoff tubes, where a slight change in grid bias can make a much larger change in smallsignal outputs than is possible if the slope of the $\mathrm{E}_{\mathrm{r}} \mathrm{I}_{1}$, curve changes very gradually. Actually, re-mote-cutoff tubes, when used, are usually found in doubler circuits, because of the large second-harmonic component that is produced. Although class-B and class-C operation with sharp-cutoff tubes can produce even greater harmonic outputs, there is the problem of ensuring that a crystal of large $R_{e}$ will not be overdriven if it is to be operated in a class-B or class-C circuit. The output voltages of remote-cutoff tubes tend to vary more with crystals of different resistances than is the case when sharp-cutoff tubes are used. The reason is that in the former case the effective $I_{v}$ continues to increase as $\mathrm{R}_{\mathrm{e}}$ becomes small, since very large excitation voltages are required to override the cutoff point. On the other hand, the effective $I_{p}$ begins to decrease when class-B operation is approached and such operation can be had with relatively small excitation voltages when sharp-cutoff tubes are used. If a remote-cutoff tube is desired, recommended types are the subminiature 1T4, the miniature 6BA6 and 12BA6, the lock-in 7A7, and the conventional-sized tubes such as the 6SK7 and 12SK7. The mention of particular vacuum tubes here should not be construed as official recommendation; they are named simply because they are the tubes commonly found in new equipment. The design engineer may very well find that the characteristics of other tubes are more appropriate for his needs.

## Pierce-Oscillator Design Considerations When Vacuum Tube with Very Sharp Cutoff is Used

1-312. In making a preliminary approximation as to what the performance of a particular tube will
be if used in a Pierce circuit, it should first be kept in mind that the ratio

$$
\begin{array}{r}
E_{p} / E_{g}=C_{g} / C_{p}=\frac{\mu Z_{L}}{R_{p}+Z_{L}}=\frac{g_{m} R_{p} Z_{L}}{R_{p}+Z_{L}} \\
1-312(1)
\end{array}
$$

is the gain of the tube. If the gain $=k$, and if
$\frac{\mathrm{R}_{p}}{\mathrm{Z}_{\mathrm{L}}}$ is 10 or greater, then

$$
\begin{equation*}
\mathrm{g}_{\mathrm{m}}=\mathrm{k} / \mathrm{Z}_{\mathrm{l}} \tag{2}
\end{equation*}
$$

or

$$
\begin{equation*}
R_{p}=\mu Z_{\mathrm{L}} / \mathrm{k} \tag{3}
\end{equation*}
$$

Either equation (2) or (3) can be used to estimate approximately the grid bias for a given plate voltage, and vice versa, that can be expected if a particular tube is used. Assume, for example, that $k=1$, that gridleak bias is to be used, and that the grid and load losses are negligible compared with the crystal driving power. In this case, the minimum expected $Z_{\mathrm{L}_{\mathrm{L}}}$ will equal (min) PI/4, which occurs when a crystal unit has the maximum allowable $\mathrm{R}_{\mathrm{r}}$ and is operated at the rated load capacitance, $C_{x}$. Under these conditions, the maximum permissible bias, as given by equation 1-293 (2), is

$$
(\max ) \mathrm{E}_{\mathrm{c}}=-\sqrt{2 \mathrm{P}_{\mathrm{cm}}} / 2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{\mathrm{R}_{\mathrm{cm}}}
$$

${ }_{T}$ This maximum value of $\mathrm{E}_{\mathrm{r}}$ is to be interpreted as a maximum that can be allowed only if $\mathrm{R}_{\text {s }}$ is a maximum or if the output voltage is to be the same magnitude regardless of the value of $R_{c}$. In this latter case, $\mathrm{P}_{\mathrm{cm}}$ and $\mathrm{R}_{\mathrm{cm}}$ fix the output and bias limits for all crystal units of a given type. The constant output can be obtained in several ways: by the use of an actual or equivalent, parallel, plate load resistance that is small compared with the minimum nonloaded crystal tank impedance; by the use of AGC, by the use of manual voltage adjustments; or by other methods. The present discussion concerns only the noncontrolled nonloaded circuit. If a crystal unit of maximum $R_{e}$, being driven at the maximum drive level, is replaced by a crystal unit of smaller $R_{e}, Z_{L}$ increases, and $E_{p}$ and $I_{g}$ tend to increase proportionately, so that the crystal driving power, equal to $I_{g}{ }^{2} R_{e}$, is greater than when $R_{k}$ is a maximum. According to equation (3), insofar as it can be assumed that $\mu$ remains approximately constant (in practice, $\mu$ decreases somewhat) $R_{p}$ increases proportionately with $Z_{L}$, so that although the equivalent generator voltage, $-\mu \mathrm{E}_{\mathrm{g}}$, increases, $\mathrm{I}_{\mathrm{p}}$ remains constant. Thus, $\mathrm{I}_{\mathrm{p}} \approx$ $\mathrm{g}_{\mathrm{m}} \mathrm{E}_{\mathrm{g}} \approx \mathrm{kE} \mathrm{E}_{\mathrm{g}} / \mathrm{Z}_{\mathrm{L}} \approx$ constant. In an actual circuit
where $R_{p} \gg Z_{L}$ and the vacuum tube has a very sharp cutoff, the effective $I_{p}$ increases up to the point that the tube is cutoff for approximately three-fifths of the negative alternation (threetenths of the entire cycle). As the excitation voltage increases beyond that point, $I_{p}$ progressively decreases, although the total power supplied to the tank circuit continues to increase as long as the excitation voltage continues to increase. The conclusions above are derived in the special case of a $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{t}}$ ratio of unity, by assuming that for all practical purposes the plate-current pulses are in phase with $\mathrm{E}_{1}$, and that $\mathrm{E}_{\mathrm{b}} \gg \mathrm{E}_{1}$. Figure 1-132 illustrates different states of operation of the same oscillator circuit that can occur if crystal units of the same frequency but different values of $R_{\mathrm{r}}$ are inserted in the circuit. A change from the class-A to the class-C state could readily occur if the crystal $R_{c}$ were reduced by more than one-half. The effective $I_{1 m}$ is defined by the equation

$$
\begin{equation*}
P_{z t}=I_{p m} E_{p m} / 2 \tag{4}
\end{equation*}
$$

where $P_{5 z}$ is the power expended in the tank circuit. Since $Z_{1}$, is very small compared with $R_{p}$, it can be assumed that the sinusoidal component, $E_{1}$, of the with-signal d-c plate voltage, $e_{b}$, is negligible by comparison with the average value, $\mathrm{E}_{\mathrm{p}}$; that is, $\mathbf{E}_{1,} \pm \mathbf{E}_{\mathrm{p} m} \approx \mathbf{E}_{\mathrm{i},}$. With this assumption we can treat $I_{b m}$, the value of the with-signal, d-c plate current, at the positive peak of excitation ( $e_{\mathrm{c}} \approx 0$ ) as a constant. The assumptions above also imply that very little grid current exists; otherwise, the larger excitation voltages would drive the grid considerably above zero at the positive peaks. With the peak instantaneous d-c plate current a constant, the total energy supplied by the power source progressively decreases as $Z_{L}$ and the excitation increase, since $I_{b}$, the average $i_{b}$, becomes progressively smaller, whereas $E_{i}$ remains constant. (Actually, if the plate current is supplied through a resistor, a decrease in $I_{b}$ causes $E_{b}$ to increase somewhat. For the problem at hand, assume that a regulated $B^{+}$is fed through an $r-f$ choke.) Thus, it can be seen that as $R_{\text {e }}$ becomes small the plate efficiency increases considerably. However, the efficiency of a crystal oscillator does not approach the high ratios of input to tank power that are obtained with conventional class-C power amplifiers and oscillators. The latter circuits can operate at efficiencies of 60 to 90 per cent because $\mathbf{E}_{\mathrm{pm}}$ approaches $\mathrm{E}_{\mathrm{b}}$ in magnitude. The instantaneous power being dissipated in the tube is the instantaneous value of $i_{k} e_{b}$, and the instantaneous power being delivered to the tank is $i_{p} e_{p}$. When $i_{b}$ is a maximum, $e_{\mathrm{b}}=\mathbf{E}_{\mathrm{b}}-\mathrm{E}_{\mathrm{pm}} \ll \mathrm{e}_{\mathrm{p}}=$
$\mathrm{E}_{\mathrm{pm},}$, so that most of power goes to the tank circuit. In the conventional Pierce oscillator such high efficiency is not to be approached unless the $\mathrm{C}_{g} / \mathrm{C}_{\mathrm{p}}$ ratio is to be made very large and $\mathrm{E}_{\mathrm{b}}$ approaches in magnitude the voltage specifications of the crystal unit. Now, to obtain a maximum output without the risk of overdriving a randomly selected crystal unit, it will be useful to derive approximate equations concerning the change in crystal power with a change in $R_{\text {e. }}$. The crystal power, we shall assume to equal the total tank power, $P_{z_{L}}$. In short, the problem is to be able to express $\mathrm{P}_{\mathrm{z}_{1}}$ as a function of $R_{e} . I_{b n}, E_{b}$, and $E_{c o}$ (the cutoff voltage) will be considered constants, and $i_{p}$ and $e_{p}$ are to be assumed to be in phase. First, we express the effective $I_{3 m}$ for each class of operation in terms of the constants above and the angles $\phi$ and $\theta$, where appropriate. (See figure 1-132.) As a safeguard against intermittent oscillations, which are most likely to occur when $R_{e}$ is a maximum, assume that the bias for maximum $R_{e}$ is to occur on the straight portion of the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve. If the
oscillations are to build up at all, they must continue to do so until the negative excitation peak at least extends into the lower bend of the $\mathbf{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve, for it is only beyond the straight portion of the curve that $g_{m}$ can change in order to seek its equilibrium value-that is, unless $R_{g}$ is so small that equilibrium is reached by virtue of the increase in grid losses alone. With a large $R_{g}$ and a reasonably sharp cutoff, it is virtually impossible for oscillations to start if the amplification is not at least sufficient to increase the excitation to where the negative peak is very nearly equal to $\mathrm{E}_{\mathrm{co}}$. Assume, then, that with $\mathrm{R}_{\mathrm{e}}=\mathrm{R}_{\mathrm{em}}$, the oscillator is designed to operate approximately as shown in figure $1-132$ (A). It can be seen intuitively that

$$
\begin{equation*}
\text { (Class A) } I_{\mathrm{pm}}=\mathrm{I}_{\mathrm{bm}} / 2 \tag{5}
\end{equation*}
$$

and with $C_{k} / C_{p}=1$, considering only the unsigned magnitudes of the bias voltage,
$($ Class A$) \mathrm{E}_{\mathrm{pm}}=\mathrm{E}_{\mathrm{c}}=\mathrm{E}_{\mathrm{co}} / 2$

CLASS-A BIAS CLASS-AB BIAS CLASS-8 BIAS CLASS-CEIAS


Figure 1-132. Change of state of Pierce oscillator with a $C_{j} / C_{p}$ rotio of one, under no-load conditions when $E_{n}$ is held constant and the effective resisfance of the crystal changes
so that

$$
\text { (Class A) } \mathrm{P}_{\mathrm{zL}}=\mathrm{I}_{\mathrm{pm}} \mathrm{E}_{\mathrm{pm}} / 2=\mathrm{I}_{\mathrm{bm}} \mathrm{E}_{\mathrm{co}} / 8
$$

1-312 (7)
Equation (7) represents the maximum possible crystal power if a tube is not to be driven beyond cutoff. Referring now to figure 1-132 (B), we shall assume that a crystal unit with an $R_{e}$ slightly less than the maximum is connected so that the bias is similar to that under $A B$ operating conditions. $\mathrm{I}_{\mathrm{m}}$ represents the apparent maximum $\mathrm{I}_{\mathrm{p}}$. It can be seen that except for the angle ( $\pi-2 \phi$ ), when the tube is cut off,

$$
i_{\mathrm{b}}=I_{\mathrm{m}}(\sin \omega t+\sin \phi) \quad 1-312(8)
$$

where $\phi$ can be considered a constant. Now,

$$
\begin{equation*}
I_{b m}=I_{m}(1+\sin \phi) \tag{9}
\end{equation*}
$$

so, on substitution in equation (8),

$$
\begin{equation*}
i_{b}=\frac{I_{b m}}{1+\sin \phi}(\sin \omega t+\sin \phi) \tag{10}
\end{equation*}
$$

Similarly,

$$
\begin{array}{r}
\mathrm{E}_{\mathrm{co}}=\mathrm{E}_{\mathrm{gm}}(1+\sin \phi)=\mathrm{F}_{\mathrm{pm}}(1+\sin \phi) \\
1-312(11)
\end{array}
$$

so that

$$
e_{p}=E_{p m} \sin \omega t=\frac{E_{c o}}{1+\sin \phi}(\sin \omega t)
$$

$$
\begin{equation*}
1-312 \tag{12}
\end{equation*}
$$

Since no energy is being supplied during the time that the tube is cut off, the energy delivered to the tank per cycle is

$$
\int_{t(-\phi)}^{t}(\pi+\phi), e_{p} i_{b} d t=\frac{1}{\omega} \int_{-\phi}^{\pi+\phi} e_{p} i_{b} d \omega t \quad 1-312(13)
$$

where $t=$ time in seconds.
Thus, the energy delivered per second, is

$$
\begin{aligned}
P_{\mathrm{zL}_{L}}=\frac{\mathrm{f}}{\omega} \int_{-\phi}^{\pi+\phi} \mathrm{e}_{\mathrm{p}} i_{\mathrm{b}} d \omega t=\frac{1}{2 \pi} \int_{-\phi}^{\pi+\phi} \mathrm{e}_{\mathrm{p}} i_{\mathrm{b}} d \omega t \\
1-312(14)
\end{aligned}
$$

On substitution of $E_{p}$ and $I_{b}$ from equations (10) and (12),
$P_{z x}=\frac{E_{00} I_{b m}}{2 \pi(1+\sin \phi)^{2}} \int_{-\phi}^{\pi+\phi}\left(\sin ^{2} \omega t+\sin \phi \sin \omega t\right) d \omega t$
1-312 (15)
On integration,
(Class AB)

$$
\begin{array}{r}
P_{z_{k}}=\frac{E_{c o} I_{b m}(\pi+2 \phi+2 \sin 2 \phi)}{4 \pi(1+\sin \phi)^{2}} \\
1-312(16)
\end{array}
$$

No maximum exists for equation (16) with values of $\phi$ between 0 and $\pi / 2$. For class- $A$ operation similar to that in figure $1-132$ (A), $\phi=\pi / 2$, so that equation (16) becomes

$$
\left(\text { Class A) } \mathrm{P}_{\mathrm{zL}}=\mathrm{E}_{\mathrm{oc}} \mathrm{I}_{\mathrm{bm}} / 8\right.
$$

This checks, as is to be expected, with equation (7). For class-B operation, $\phi=0$, so that equation (16) becomes

$$
\text { (Class B) } P_{\mathrm{z}_{\mathrm{L}}}=\mathrm{E}_{\mathrm{e}} \mathrm{I}_{\mathrm{bm}} / 4 \quad 1-312(17 \text {; }
$$

Note that the power expenditure in the crystal unit for class-B operation is exactly twice that found for class-A operation. Since $E_{p m}$ under class-B conditions is equal to $\mathrm{E}_{\mathrm{co}}$ (see figure 1-132 (C) ), or twice the class-A value of $\mathrm{E}_{\mathrm{pm}}$, then, because $\mathrm{P}_{\mathrm{zi}}=\mathrm{I}_{\mathrm{pm}} \mathbf{E}_{\mathrm{pm}} / 2$, the effective $\mathrm{I}_{\mathrm{pm}}$ at class $B$ must be equal to the same effective value as at class A. Thus,

$$
\begin{equation*}
\left(\text { Class B) } I_{p m}=I_{b m} / 2\right. \tag{18}
\end{equation*}
$$

Also, since $E_{p m}=I_{p m} Z_{\mathrm{L}}$, if $\mathrm{E}_{\mathrm{pm}}$ has doubled but $I_{p m}$ has not changed it can only mean that $Z_{L}$ has doubled. In other words, if the oscillator is designed to operate class $A$ when $R_{e}$ is a maximum, it will operate class $B$ when a crystal unit is inserted that has an effective resistance equal to $\mathrm{R}_{\mathrm{em}} / 2$. Equation (16) can be generalized to apply for all operating states in which $2 \mathrm{E}_{\mathrm{gm}}$ is equal to or greater than $\mathbf{E}_{\mathrm{co}}$. For greater simplicity, $\phi$ should be replaced by $(\pi-\theta) / 2$, where $\theta=\pi-2 \phi$ is the angle during which the tube is cut off. $\theta$ is always positive, whereas $\phi$ would be negative in the case of class-C operation. Thus, equation (16) can be expressed
(all classes) $\mathrm{P}_{\mathrm{zt}}=\frac{\mathrm{E}_{\mathrm{oo}} \mathrm{I}_{\mathrm{bm}}(2 \pi-\theta+\sin \theta)}{4 \pi\left(1+\cos \frac{\theta}{2}\right)^{2}}$
$1-312$ (19)

The slope of this equation is positive for all values of $\theta$ less than $2 \pi$, so that the power dissipated in a crystal unit always becomes greater as $R_{e}$ becomes smaller. By substituting $\cos \frac{\theta}{2}$ for $\sin \phi$ in equation (11) and rearranging, we have

$$
\mathrm{E}_{\mathrm{pm}}=\mathrm{E}_{\mathrm{co}} /\left(1+\cos \frac{\theta}{2}\right)
$$

so that

$$
\begin{align*}
I_{p m} & =\frac{2 P_{z_{t}}}{E_{p m}}=2 P_{z t}\left(1+\cos \frac{\theta}{2}\right) / E_{\mathrm{co}} \\
& =\frac{I_{\mathrm{bm}}(2 \pi-\theta+\sin \theta)}{2 \pi\left(1+\cos \frac{\theta}{2}\right)} \tag{20}
\end{align*}
$$

Equation (20), unlike equation (19), has a maximum when $\theta$ is approximately $3 \pi / 5$. That a maximum (or a minimum) occurs between $\theta=0$ and $\theta=\pi$ is to be expected, since $I_{p m}$ has the same value for each of those values of $\theta$. This maximum is

$$
(\max ) I_{\mathrm{pm}}=0.54 I_{\mathrm{bm}}
$$

$$
1-312(21)
$$

Now,

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{I},}=2 \mathrm{P}_{\mathrm{z} .} /\left(\mathrm{I}_{\mathrm{pm}}\right)^{2} \tag{22}
\end{equation*}
$$

On substituting equations (10) and (20) in (22)

$$
\begin{equation*}
Z_{\mathrm{L}}=\frac{2 \pi \mathrm{E}_{\mathrm{co}}}{\mathrm{I}_{\mathrm{bm}}(2 \pi-\theta+\sin \theta)} \tag{23}
\end{equation*}
$$

Rearranging and substituting $1 / 4 \omega^{2} \mathrm{C}_{\mathrm{x}}{ }^{2} \mathrm{R}_{\mathrm{e}}$ for $\mathrm{Z}_{\mathrm{r}}$., where $C_{x}$ is the specified load capacitance of the crystal unit,

$$
\begin{equation*}
\theta-\sin \theta=2 \pi\left(1-4 \omega^{2} C_{x} E_{c o} R_{e} / I_{b m}\right) \tag{24}
\end{equation*}
$$

Equation (24) is quite significant in that it predicts the approximate angle during which a given tube will be cut off for a given value of $R_{\text {e }}$. A Pierce oscillator designed so that the tube is operating with a class-A bias equal to $\mathbf{E}_{c o} / 2$ when $\mathrm{R}_{\mathrm{e}}$ is a maximum will have a value of $\theta$ equal to zero. Thus, when $R_{e}=R_{\text {ems }}$ each side of equation (24) must vanish. For the right-hand side to equal zero,

$$
4 \omega^{2} C_{x} E_{c o} R_{t m}=I_{b m}
$$

This is equivalent to saying that

$$
\begin{equation*}
\frac{1}{(\min ) Z_{L}}=\frac{4}{(\min ) P I}=\frac{I_{b m}}{E_{c o}}=(\text { average }) g_{\mathrm{g}} \tag{25}
\end{equation*}
$$

which could have been predicted on the basis of equation (2). Assume that equation (25) holds, what will be the value of $\theta$ when a crystal unit having a practical minimum value of $R_{e}$ equal to $R_{\text {em }} / 9$ is connected in the circuit? When $R_{e}=R_{\text {em* }}$ the negative term within the parentheses of equation (24) is equal to -1 ; with $\mathbf{R}_{\mathrm{e}}=\mathrm{R}_{\mathrm{em}} / 9$, the same term is reduced to $-1 / 9$. Thus, the maximum $\theta$ to be expected is defined by:
$\left\{(\max ) \theta\right.$ for $\left.(\min ) \mathrm{R}_{\mathrm{e}}\right]$ when: $\theta-\sin \theta=16 \pi / 9$
1-312 (26)
Figure 1-133 shows that equation (26) requires that

$$
\begin{equation*}
(\max ) \theta=16 \pi / 9-1 \tag{27}
\end{equation*}
$$

In other words, when a sharp-cutoff tube is used and the oscillator is designed for class-A operation with crystal units of maximum $R_{e}$, the oscillator will be operating class $C$, with the tube cut off approximately three-fourths of the time, when crystal units of minimum values of $\mathrm{R}_{\mathrm{e}}$ are connected in the circuit. Equation (24) can be generalized to define $\theta$ with reference to any convenient value of $R_{e}$, simply by assuming that $\theta=0$ when $R_{e}=$ (ref) $R_{\text {e. Thus, }}$

$$
\theta-\sin \theta=2 \pi\left[1-\mathrm{R}_{\mathrm{e}} /(\mathrm{ref}) \mathrm{R}_{\mathrm{e}}\right] \quad 1-312(28)
$$

or

$$
\begin{equation*}
\theta_{\mathrm{N}}-\sin \theta_{\mathrm{N}}=2 \pi(\mathrm{~N}-1) / \mathrm{N} \quad 1-312 \tag{29}
\end{equation*}
$$

where $N=$ (ref) $R_{e} / R_{e_{N}}, \theta=0$ when $R_{e}=$ (ref) $R_{e}$, and $\theta_{\mathrm{N}}$ is the value of $\theta$ for the particular value of $R_{e}$ symbolized by $R_{*_{N}}$. The reference $R_{e}$ need not be the maximum permissible $\mathrm{R}_{\mathrm{p}}$. For a given oscillator of $\mathrm{C}_{\mathrm{k}} / \mathrm{C}_{\mathrm{p}}$ ratio equal to 1 , (ref) $\mathrm{R}_{\text {e would }}$ be the value of $R_{e}$ that would cause the peak-topeak excitation voltage to equal $\mathrm{E}_{\mathrm{co}}$ in magnitude. Assuming that (ref) $\mathrm{R}_{\mathrm{e}}=\mathrm{R}_{\mathrm{em}}$, what then will be the ratios of $P_{2,}$, and $I_{1 m m}$ corresponding to minimum and maximum values of $\mathrm{R}_{e}$ ? When $\theta=$ $\frac{16 \pi-9}{9}$, as given by equation (27), $\cos \theta / 2$ is very nearly $-2 / 3$, so equation (19) becomes
(Class C max) $\mathrm{P}_{\mathrm{zt}}$

$$
\begin{equation*}
=\frac{E_{c o} I_{b m}\left(2 \pi-\frac{16 \pi}{9}\right)}{4 \pi\left(1-\frac{2}{3}\right)^{2}}=\frac{E_{c o} I_{b m}}{2} \tag{30}
\end{equation*}
$$

On comparison with equations (7) and (17), which give values of $\mathrm{P}_{\mathrm{zL}}$ of $\mathrm{E}_{\mathrm{co}} \mathrm{I}_{\mathrm{bm}} / 8$ and $\mathrm{E}_{\mathrm{co}} \mathrm{I}_{\mathrm{bm}} / 4$


Figure 1-133. Sine curve plottod to same scale as the angle $\theta$. 45-degree diagonal that intercepts $\sin \theta_{k}$ on curve intercepts ( $\theta_{k}-\sin \theta_{k}$ ) on $\theta$ axis
for class-A and class-B operation, respectively, we find that where there is to be no output control, the no-load tube voltage must be so chosen that a crystal unit of maximum $\mathrm{R}_{\mathrm{e}}$ is not driven at more than one-fourth the rated drive level, otherwise crystals of small $\mathrm{R}_{\mathrm{e}}$ will be overdriven. With a power ratio of 4 when the $Z_{L}$ ratio is 9 , it can be shown quite simply that the $I_{p m}$ ratio is $2 / 3$ and the $\mathrm{E}_{\text {po }}$ ratio is 6. Thus,

$$
(\text { Class-C } \min ) \mathrm{I}_{\mathrm{pm}}=\mathrm{I}_{\mathrm{bm}} / 3
$$

$$
1-312(31)
$$

and

$$
\text { (Class-C max) } \mathrm{E}_{\mathrm{pm}}=3 \mathrm{E}_{\mathrm{so}}
$$

$$
1-312(32)
$$

The plate dissipation in the tube should be of little concern unless subminiature tubes are used. In any event the plate dissipation is a maximum when $R_{e}$ is a maximum, so no thought need be taken for other than class-A operation. Approximately,

$$
\text { (Class-A) plate power }=\mathrm{E}_{\mathrm{b}} \mathrm{I}_{\mathrm{b}}=\mathrm{E}_{\mathrm{b}} \mathrm{I}_{\mathrm{bm}} / 2
$$

1-312 (33)
Finally, the foregoing equations suggest that a Pierce oscillator employing a sharp-cutoff tube be designed for class-A operation on the assumption that $R_{e}$ will be a maximum and that the maximum permissible drive level is one-fourth its actual rating. Under these assumptions, equation 1-293 (2) should be changed to

$$
(\max ) \mathrm{E}_{\mathrm{e}}=
$$

$$
\begin{equation*}
-\frac{\sqrt{2 \mathrm{P}_{\mathrm{cm}} / 4}}{2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{\mathrm{R}_{\mathrm{em}}}}=-\frac{\sqrt{\mathrm{P}_{\mathrm{cm}}}}{2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{2 \mathrm{R}_{\mathrm{em}}}} 1-312 \tag{34}
\end{equation*}
$$

where $P_{c m}$ is the true drive-level rating. Since (max) $\mathrm{E}_{\mathrm{c}}$ will also be equal to $\mathrm{E}_{\mathrm{co}} / 2$, approximately, then (no longer continuing to treat $\mathrm{E}_{\mathrm{co}}$ as a magnitude only)

$$
(\max ) E_{\mathrm{co}}=-\sqrt{P_{\mathrm{cm}}} / \omega C_{x} \sqrt{2 R_{e m}}
$$

$$
1-312
$$

At the same time, $P_{z L}\left(=\frac{I_{b m} E_{c o}}{8}\right)$ must not exceed $\mathrm{P}_{\mathrm{om}} / 4$. Consequently,

$$
\begin{array}{r}
(\max ) \mathrm{I}_{\mathrm{bm}}=\frac{2 \mathrm{P}_{\mathrm{cm}}}{(\max )\left|\mathrm{E}_{\mathrm{co}}\right|}=2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{2 \mathrm{P}_{\mathrm{om}} \mathrm{R}_{\mathrm{om}}} \\
1-312(36)
\end{array}
$$

Equations (35) and (36) define the operating characteristics to be sought if a sharp-cutoff tube is to be used under conditions of maximum output for maximum stability. Remember, that equation (34) actually is an expression of the limitation on $I_{\varepsilon}$, the crystal current, and therefore upon $E_{p}$ and $E_{x}$. As far as the self-excitation voltage of a truly sharp-cutoff tube is concerned, it will be difficult to keep this voltage from building up until it reaches into the bend near the cutoff point. For this reason, the first consideration is that $I_{b a}$ is not exceeded. As a safety measure, $I_{\mathrm{bm}}$ should not be greater than the value given by equation (36), even if the actual $E_{c v}$ is less than (max) $\mathrm{E}_{\mathrm{co}}$. The conclusions reached in the foregoing discussion are summarized in the following table.


## Pierce-Oscillator Design Considerations When Tube Cutoff Has Below-Average Sharpness

1-313. Unless a vacuum tube has plate characteristics resembling those of subminiature tubes when normal plate voltages are used, or unless by reducing the filament voltage such characteristics can be achieved, a Pierce oscillator tube must be operated at a plate voltage of from one-half to one-fourth normal. In so doing, it is very probable that the lower bend of the $E_{c} I_{b}$ curve will become rather extended compared with the straight portion to the left of zero grid volts. In this event, the tube exhibits the characteristics of a remote-cutoff tube, except that the cutoff voltage is one-fifth or less that of a normal remote-cutoff tube operating at an equivalent reduced piate voltage. Where the cutoff is not sharp, it is quite easy for equilibrium to be reached with peak-to-peak excitation voltages much smaller in magnitude than $E_{\text {cor }}$ and considerably greater ranges in $\mathrm{R}_{\mathrm{e}}$ of the crystal unit can exist before cutoff is reached. Thus, in the more usual case, the assumptions used in paragraph 1-312 cannot be made unless greater care is taken in the oscillator design to ensure a peak-topeak excitation voltage equal to $\left|\mathrm{E}_{\mathrm{co}}\right|$ when $\mathrm{R}_{\mathrm{e}}$ is a maximum-an operating point much more difficult to locate and critical to maintain when a large steady decrease in the effective $g_{m}$ occurs well before the cutoff point is reached, and which may require very low plate voltages if the maximum- $\mathrm{R}_{\mathrm{e}}$ crystal unit is not to be overdriven. As a concrete example, suppose that the oscillator is to employ a 10 -me crystal unit of the CR-18/U type. At this frequency, $P_{\mathrm{cm}}=5 \mathrm{mw}, \mathrm{R}_{\mathrm{em}}=25 \mathrm{ohms}$, and $\mathrm{C}_{\mathrm{x}}=32 \mu \mu \mathrm{f}$. On substitution in equation 1-312 (35), we obtain a (max) $\mathrm{E}_{\mathrm{co}}$ of approximately -5 V . By equation 1-312 (36), this value of $\mathrm{E}_{\mathrm{w}}$ is to be obtained in a tube where the zero-bias, with-out-signal plate current is $\mathrm{I}_{\mathrm{bm}}=2 \mathrm{ma}$. Such characteristics are not easily obtained with conven-tional-sized vacuum tubes. It may be necessary to operate at the given value of $\mathrm{I}_{\mathrm{bm}}$, or slightly greater, and a cutoff voltage that is of a smaller magnitude than that indicated for (max) $\mathrm{E}_{\mathrm{co}}$ in equation 1- $312(35)$, in which case all crystal units used will drive the tube beyond cutoff. An alternative approach is to operate at a larger than maximum $\mathrm{E}_{\mathrm{co}}$, but, if this be done, a safety factor should be allowed by assuming that $\mathrm{I}_{\mathrm{p}}$ is to be the same for all values of $\mathrm{R}_{\mathrm{e}}$. Although this will not be strictly true, the assumption is a close approxima-
tion if the change in plate current between the values of $\mathrm{E}_{\mathrm{c}}=\mathrm{E}_{\mathrm{co}} / 2$ and $\mathrm{E}_{\mathrm{co}}$ is very small compared with the change in plate current between $\mathrm{E}_{\mathrm{c}}=0$ and $\mathrm{E}_{\mathrm{c}}=\mathrm{E}_{\mathrm{co}} / 2$. It can be seen that insofar as the effective $I_{p}$ can be assumed to remain constant, $\mathrm{E}_{\mathrm{p}}$ and hence $\mathrm{E}_{k}, \mathrm{I}_{\mathrm{k}}, \mathrm{E}_{\mathrm{c}}$, and the crystal driving power, $I_{s}{ }^{2} R_{t} \approx I_{p}{ }^{2} Z_{L}$, increase directly with $\mathrm{Z}_{\mathrm{L}}$, or inversely with $\mathrm{R}_{\mathrm{e}}$. The problem is to find the maximum permissible $\mathrm{E}_{\mathrm{c}}$, which, although applying to extended-cutoff operation only when $R_{\text {e }}$ is a maximum, will not lead to a replacement crystal being over-driven if its resistance is less than the maximum. Again we assume a minimum $R_{e}$ equal to $\mathrm{R}_{\mathrm{em}} / 9$. In a manner similar to the derivation of equation 1-293 (2), we can say (max) $\mathrm{E}_{\mathrm{c}}$ (with $\left.(\min ) \mathrm{Re}_{\mathrm{e}}\right)=$

$$
\begin{array}{r}
(\max ) \mathrm{E}_{\mathrm{e}}\left[\text { for }(\min ) \mathrm{R}_{\mathrm{e}}\right]=-\frac{\sqrt{2 \mathrm{P}_{\mathrm{em}}}}{2 \omega \mathrm{C}_{\mathrm{x}} \sqrt{(\min ) \mathrm{R}_{\mathrm{e}}}} \\
=-\frac{3 \sqrt{\mathrm{P}_{\mathrm{cm}}}}{\omega \mathrm{C}_{\mathrm{x}} \sqrt{2 \mathrm{R}_{\mathrm{em}}}} \tag{1}
\end{array}
$$

Now, if equation (1) gives the bias voltage when a crystal unit of minimum $\mathrm{R}_{e}$ is connected, assuming that $I_{p}$ is constant, the bias that exists when a crystal unit of maximum $R_{r e}\left(=9(\min ) R_{e}\right)$ is substituted will be one-ninth the value above. Thus,
(extended cutoff max) $\mathrm{E}_{\mathrm{c}}\left[\right.$ for $\left.\mathrm{R}_{\mathrm{e}}=\mathrm{R}_{\text {em }}\right]=$

$$
-\frac{\sqrt{P_{e m}}}{3 \omega C_{x} \sqrt{2 R_{e m}}}
$$

If a gridleak Pierce oscillator is not to have a loaded plate circuit, nor an adjustable nor controlled output voltage, nor a sharp cutoff, equation (2) gives the maximum bias that can be safely assumed when $R_{e}$ is a maximum. The output voltage agreeing with equation (2) is two-thirds that given in paragraph 1-312 for a sharp-cutoff tube. If $\mathrm{R}_{\mathrm{g}}$ is not large enough for the average $\mathrm{E}_{\mathrm{c}}$ to approximate the peak excitation voltage, a maximum bias less than that given by equation (2) must be assumed. With large values of $R_{s},\left|E_{c}\right|$ of equation (2) is the peak of the maximum excitation voltage when $R_{e}$ is a maximum, and $\left|E_{e}\right|$ of equation (1) is the approximate peak when $R_{0}$ is a minimum. If a $C_{g} / C_{p}$ ratio other than 1 is used, equation (2) can be expressed more exactly
(extended cutoff max) $\mathrm{E}_{\mathrm{e}}=$

$$
\begin{equation*}
-\sqrt{2 P_{\mathrm{om}}} / 3 \omega C_{s} \sqrt{R_{\mathrm{emn}}} \tag{3}
\end{equation*}
$$

It should be understood that although equations (2) and (3) are derived from equation (1), it is wiser to select the vacuum tube and plate voltage upon the assumption that the resistance of the crystal unit is a maximum rather than a minimum. Since the effective amplification factor of the tube cannot be expected to be constant for all values of $R_{*}$, equations (1) and (2) will not both hold for the same circuit. If (1) is correct, (2) will indicate a value too low; if (2) is correct, (1) will indicate a value too high. Equation (2) therefore permits a safety factor in the event of an exceptionally low value of $R_{s .}$. Also, if the oscillator performs properly with $R_{e}$ a maximum, it will almost certainly operate when $R_{s}$ is a minimum. The reverse is not necessarily true.
1-314. Equation 1-313(1) is equivalent to a bias and output of the same magnitude as that obtained in paragraph 1-312 for sharp-cutoff conditions and minimum $R_{e}$; but the bias and output of equation $1-312(2)$ for $R_{8}=R_{e m}$, when $E_{c o}$ is assumed to be significantly greater than $2 \mathrm{E}_{\mathrm{c}}$, are only twothirds their equivalent sharp-cutoff values. In the case of the $10-\mathrm{mc}$ CR-18/U crystal unit discussed in paragraph 1-313, the (practical max) $\mathrm{E}_{\mathrm{c}}$, as given by equation $1-313(2)$ is $-\frac{5}{3} \mathrm{~V} \approx-1.7 \mathrm{~V}$. For the smallest values of $\mathrm{R}_{\mathrm{e}}$, the bias will approach -15 V . Assuming that $\mathrm{g}_{\mathrm{m}} \approx \frac{1}{\mathrm{Z}_{\mathrm{L}}}$ (according to equation $1-312(2)$, when $C_{p} / C_{p}=1$ ) and that

$$
\begin{aligned}
& \mathrm{Z}_{\mathrm{L}}=\frac{(\min ) \mathrm{PI}}{4}=\frac{1}{4 \omega^{2} \mathrm{C}_{\mathrm{x}}^{2} \mathrm{R}_{\mathrm{em}}}= \\
& \frac{10^{10}}{4 \times 6.28^{2} \times 32^{2} \times 25}=2500 \mathrm{ohms}
\end{aligned}
$$

then, $g_{m} \approx 10^{6} / 2500=400 \mu$ mhos when $R_{e}$ is a maximum. This is a very small transconductance to be obtained with a bias of approximately -1.7 volts, and usually cannot be obtained at all with normal operating voltages except in the case of the small battery-operated tubes. The 1.7 -volt maximum bias represents a peak-to-peak excitation maximum of 3.4 volts. With an average $g_{m}$ of 400 $\mu$ mhos, the limiting value of $I_{b m}\left(\approx 2 I_{p m} \sim 2 g_{m} E_{g m}\right)$ becomes 1.4 ma , approximately. Only if age is used to provide a much larger bias than can be obtained with a peak-to-peak excitation of 3.4 volts will it be possible to have such a small zero-signal plate current without operating conventional tubes at greatly reduced voltages. Generally, it is easier to operate with a small $E_{c o}$ and a larger $I_{\text {beo }}$ and not
attempt class-A operation. A large percentage of the crystal oscillators now in use drive the crystal units at a considerably higher level than is advantageous from the point of view of stability and long crystal life. Much of the care otherwise taken in the circuit design can be wasted if the first consideration is power output rather than frequency control. Where a vacuum-tube manual recommends a particular voltage of power amplifier for use as a class-C oscillator tube, the typical operating characteristics listed are rarely appropriate for military-standard crystal units, but apply more usually to LC circuits. The plate voltages must be considerably lower than the typical values indicated, in order to reach the small transconductances that must exist at equilibrium without overdriving the crystal unit.
1-315. Assume that a crystal unit is connected in a Pierce circuit using a conventional triode operating at its normal plate voltage, and that the $C_{s} / C_{p}$ ratio is near unity. The equilibrium values of $g_{m}$ and $R_{p}$ cannot be reached until the amplitude is great enough for the tube to be operating class $C$, and the crystal unit will almost certainly be overdriven. There are four ways in which the circuit can be adjusted to prevent this overdrive: (a) the plate voltage can be reduced, (b) the filament voltage can be reduced, (c) the $C_{g} / C_{b}$ ratio can be increased, or ( $d$ ) the load losses can be increased. Of these methods, the first, reducing the plate voltage, seems to be the best from the point of view of frequency stability, although a reduction of the filament voltage may be worth consideration. Very possibly, if the filament voltage is decreased sufficiently to lower the zero-bias transconductance to as much as one-fifth its normal value, the operation of the circuit will become unduly sensitive to slight fluctuations in the filament power supply. The only data available at this writing is that reported by Messrs. Roberts, Novak, and Goldsmith of the Armour Research Foundation of Illinois Institute of Technology. Experimenting with a 6 C 4 tube and a 7-rnc Miller circuit, it was found that a 30 -percent decrease in filament voltage, which is equivalent to decreasing the filament power by approximately one-half or more, depending upon the temperature coefficient of the filament resistance, caused only a 2.5 -cycle rise in frequency. (In a Pierce circuit the frequency would have decreased.) This effect on the frequency is very slight, but the exact decrease in the r-f plate current is not known. Nevertheless, the evidence is sufficient to suggest that if the tube characteristics are made suitable for a crystal circuit by reducing the filament voltage, any instability

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caused by further fluctuations in the filament voltage would appear primarily as variations in the output voltage, rather than as variations in the frequency. In view of the fact that a reduction in filament current permits a greater saving in power than does a reduction in plate voltage (and lengthens the tube life), this approach to the problem may well be worth experimentation. The conventional approach, however, is to operate with a low plate voltage. If a $\mathrm{C}_{\mathbf{k}} / \mathrm{C}_{p}$ ratio on the order of unity is to be used, the average tube will require plate or screen voltages of 40 to 50 volts, or less. The lower the voltage, the nearer class-A operation can be approached at equilibrium. A fair approximation of the operating conditions to be expected can be made from an inspection of a family of plate-characteristic curves. With $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}=1$, the peak-to-peak variations in plate voltage are the same as those of the excitation voltage, so for all practical purposes the plate voltage can be assumed to be constant. Thus, the load line can be assumed to be vertical, and the maximum and minimum amplitudes of $I_{b}$ for a given plate voltage become the values, respectively, for grid voltages of 0 and $2 \mathrm{E}_{\mathrm{gm}}$, where $\mathrm{E}_{\mathrm{gm}}$ is the peak excitation voltage. For the 10 -mc crystal unit taken as an example above, it was found that the peak-to-peak $I_{p}$ for a maximum $R_{e}$ was $2\left|g_{m} E_{e}\right|=1.4 \mathrm{ma}$. The correct plate voltage for a given tube is thus the value of $E_{b}$ at which a change of grid voltage from 0 to -3.4 volts causes the plate current to decrease by 1.4 ma. This type of operation-class A to class ABis generally more feasible when agc is used, if it is desired to apply for all values of $\mathrm{R}_{\mathrm{e}}$.

## PIERCE-OSCILLATOR DESIGN CONSIDERATIONS FOR $C_{g} / C_{p}$ RATIOS OTHER THAN ONE

1-316. When the $\mathrm{G}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$ ratic is not approximately equal to one but the total load capacitance meets the crystal specifications, $\mathrm{g}_{\mathrm{m}}$ is increased, and generally it will be sasier to obtain desirable vacuumtube characteristics at more convenient plate voltages. The first step, as before, is to theoretically limit the peak of the crystal current to $\sqrt{\frac{2 \mathrm{P}_{\mathrm{cm}}}{\mathrm{R}_{\mathrm{cm}}}}$ when $R_{e}$ is a maximum. The peak excitation voltage, $\mathrm{E}_{\mathrm{gm}}$, equals $\frac{1}{{ }_{\mathrm{w}} \mathrm{C}_{\mathrm{s}}} \sqrt{\frac{2 \mathrm{P}_{\mathrm{cm}}}{\mathrm{R}_{\mathrm{em}}}}$ under these conditions. $\mathrm{E}_{\mathrm{pm}}$ equals $\frac{1}{{ }_{\mathrm{w}} \mathrm{C}_{\mathrm{p}}} \sqrt{\frac{2 \mathrm{P}_{\mathrm{cm}}}{\mathrm{R}_{\mathrm{em}}}} ; \mathrm{g}_{\mathrm{n}}$ equals $\mathrm{C}_{\mathrm{z}} / \mathrm{C}_{\mathrm{p}} \mathrm{Z}_{\mathrm{L}} ; \mathrm{I}_{\mathrm{pm}}$ equals $\mathrm{g}_{\mathrm{m}} \mathrm{E}_{\mathrm{sm}}$. With these values taken as a start we can retrace the steps taken-in paragraphs 1-312 and 1-313, and determine the values of $\mathrm{I}_{\mathrm{bm}}$ and $\mathrm{E}_{\mathrm{co}}$ that do not permit the crystal to be overdriven for any value of $R_{e}$ between $R_{e m}$ and $R_{\text {em }} / 9$.

## FINAL WORD ON CORRECT LOAD CAPACITANCE IN THE PIERCE CIRCUIT

1-317. A prime purpose of the military specifications regarding the load capacitance, effective resistance, drive level, and frequency tolerance of the different types of crystal units is to guarantee the replacement of a defective crystal unit in the field without special testing or other complications, and with the same ease that a defective vacuum tube can be replaced with a new tube of the same type. However, a crystal unit is more critical in its performance than a vacuum tube. As a result there can be no replacement guarantee unless the new crystal unit is inserted in a circuit where it will be operated under approximately the same load and drive conditions at which it has been tested. An inspection of the various types of oscillator circuits now in use, such as those illustrated in figures 1-135 to 1-138, most of which have been designed around the older types of crystal units, reveals a much greater versatility in operating conditions than is now desired in the design of new equipment. One of the requirements that is no longer within the jurisdiction of the design engineer is the effective load capacitance into which the crystal unit is to work. This means, that for a given nominal frequency and type of crystal unit, the crystal unit must exhibit a given inductive reactance, $X_{0}$, equal numerically to $1 / \omega C_{x}$, where $\mathrm{C}_{\mathrm{x}}$ is the rated load capacitance. Furthermore, it means that for each particular crystal unit there is but one frequency at which it is supposed to operate. This does not mean that all crystal units of the same type and nominal frequency have a single common operating frequency, rather that each has its own individual frequency, which, however, will not differ from the nominal frequency by more than the permitted tolerance. It is the effective operating reactance that the crystal units must have in common. Approximately,

$$
\mathrm{X}_{0}=\frac{4 \pi \mathrm{~L} \Delta \mathrm{f}}{1+\frac{4 \pi \mathrm{~L} \Delta f}{\mathrm{X}_{\mathrm{C}_{0}}}} \text { (Equation (1), figure 1-98) }
$$

Now, $\Delta f=f_{p}-f_{k}$, where $f_{p}$ is the operating par-allel-resonant frequency and $f_{s}$ is the series-resonant frequency of the motional arm. Assume that a 10 -me parallel-resonant crystal unit has a frequency tolerance of $\pm 0.02$ per cent. This is equivalent to an absolute frequency tolerance of $\pm 2000$ cps. Two crystal units at opposite extremes could be within specifications even though their operating frequencies, $f_{p 1}$ and $f_{p z}$, were 4000 cps apart.

If the rated load capacitance were $32 \mu \mu \mathrm{f}$ and the crystals were $A$ elements, $\Delta f$, itself, for each crystal would be on the order of 2000 cps . If the crystals were $B$ elements of the same shunt capacitance, $C_{o}$, $\Delta f$ for each crystal would be only in the neighborhood of 800 cps , because of the $B$ element's larger series-arm inductance, L. It becomes obvious that there can be no expectation of "pulling" the frequencies together by making slight adjustments in the load capacitance. The lowerfrequency crystal could not be raised to zero beat with a frequency 4000 cps higher without reducing $C_{x}$ several-fold. The higher-frequency crystal could not even be "pulled" to the nominal frequency and oscillations still be maintained. For this reason, the design engineer should generally not attempt to provide an operator with frequency adjustments for the crystal oscillator. The only adjustments needed are those which can be factory preset, in order to compensate for slight differences in stray capacitance. If the frequencies to be generated must be in close agreement with some standard, or with the frequency of some controlling station, the task is to provide oven-controlled crystal units of smaller tolerance. Only when the desired operating tolerance is less than any provided by crystal-unit specifications alone, is it necessary to provide the operator with a frequency adjustment knob. Even then, the adjustment need not provide a tuning range greater than the specified crystal tolerance. Since the smaller tolerances are only $1 / 10$ to $1 / 20$ of the 0.02 per cent in the example above, the total variation in load capacitance may not need to be greater than $\pm 10$ per cent of the speciñed capacitance.
1-318. It may be desirable to provide an operator with the means of controlling the output voltage


Figure 1-134. Ganged capacitances to enable adjustment of $C_{p} / C_{p}$ ratio of Pierce circuit without changing total lood capacitance
of a Pierce oscillator by varying the $\mathrm{C}_{n} / \mathrm{C}_{\mathrm{p}}$ ratio. In this case, care must be taken to ensure that the total load capacitance remains the same. If $\mathrm{C}_{\mathrm{g}}$ and $C_{p}$ are to be adjusted separately, some type of matching scales should be provided with the two tuning knobs, so that the correct load capacitance can always be had when, say, the two scales give the same reading. It is more desirable to have available ganged capacitors similar to those shown in figure 1-134 for each of the Military Standard capacitance ratings. The capacitors $C_{1}$ and $C_{2}$ in series are to be designed to always ensure a correct load capacitance when each is shunted by convenient predetermined fixed capacitance. The small variable capacitances $\mathrm{C}_{3}$ and $\mathrm{C}_{4}$ are adjusted until the sum of their values and the circuit stray capacitances, $\mathrm{C}_{\mathrm{ni}}$ and $\mathrm{C}_{\mathrm{n}}$, provide the correct fixed shunts for the ganged elements.

## MODIFICATIONS OF PIERCE CIRCUIT

1-319. Figures 1-135, 1-136, 1-137, and 1-138 and their accompanying circuit-data charts reveal a great flexibility in the design of a Pierce oscillator. It would be very convenient to be able to put our finger on a single circuit and say that the design of this circuit is superior to all others. Unfortunately, this is not possible. One would first have to define what is meant by "superior design." The definition, at best would be a complex function of several physical and psychological variables. The very existence of a wide variety of circuit modifications suggests that no one circuit is superior to all others for all given tasks, although much of the variety can be attributed to the desire of the design engineer to create his own circuit and also to avoid the risk of possibly infringing upon the patent, rights of another. Our space does not permit a detailed discussion of each of the circuits shown. Only a few of the highlights are to be mentioned. In general, most of the oscillators illustrated employ older-type crystal units; most of the circuits use $B+$ voltages on the order of 200 volts, and would overdrive the smaller-sized crystals currently recommended; and the load capacitances and the $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$ ratios vary widely from one circuit to another. Those circuits that employ currently recommended Military Standard crystal units (crystal units having nomenclature type numbers, CR-15/U and higher) are designed to operate so that the crystal unit faces its rated parallel-mode load capacitance. In these circuits the plate supply is normally 100 to 120 volts, and the crystal unit of average resistance is operated at 4 to 5 milliwatts.

Section 1

## Crystal Oscillators



Figure 1-135. Modifcations of Pierce oscillator using friodes

| Fig. | Equipment | Purpose | Fi | $F_{2}$ | Fs | - CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | Rs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Transmitter T-14(A/B/C)/TRC-1 | M.O. | $\begin{aligned} & 729 \\ & 1041 \\ & \hline \end{aligned}$ |  |  | CR-4/U <br> (oven) | 850 | 50 | 100 |
| (B) | T-14(D/E)/TRC-1 | M. 0. | $\begin{aligned} & 729 \\ & 1041 \end{aligned}$ |  |  | $\begin{aligned} & \mathrm{CR}-4 / \mathrm{U} \\ & \text { (oven) } \end{aligned}$ | 850 | 150 | 100 |
| (C) | T-14H/TRC-1 | M. | $\begin{aligned} & 729- \\ & 1041 \\ & \hline \end{aligned}$ |  |  | $\begin{aligned} & \mathrm{CR}-4 / \mathrm{U} \\ & \text { (oven) } \end{aligned}$ | 350 | 150 | 100 |
| (D) | $\begin{aligned} & \text { Test Oscillator } \\ & \operatorname{TS}-32(\mathrm{~A} / \mathrm{B}) / \mathrm{TRC}-1 \end{aligned}$ | Test oscillator | $\begin{aligned} & 729 \\ & 1041 \end{aligned}$ |  |  | $\begin{aligned} & \text { CR-4,U } \\ & \text { (oven) } \end{aligned}$ | 350 | 50 | 15 |
| (E) | TS-32(C/D)/TRC-1 | Test oscillator | $\begin{aligned} & 729 \\ & 1041 \end{aligned}$ |  |  | $\begin{aligned} & \mathrm{CR}-\mathrm{/V} \\ & \text { (oven) } \\ & \hline \end{aligned}$ | 350 | 47 | 15 |
| (F) | Radio Transmitter T-177/FR | M.O. | $\begin{aligned} & 2500 \\ & 4000 \\ & \hline \end{aligned}$ |  |  | $\begin{aligned} & \text { FT-164 } \\ & \text { (oven) } \end{aligned}$ | 100 | 0.25 | 0.5 |
| (G) | Radio Transmitter Assembly OA-60B/ FRT | M.O. | $\begin{aligned} & 2000 \\ & 4000 \end{aligned}$ |  |  | $\begin{aligned} & \text { FT-164 } \\ & \text { (oven) } \end{aligned}$ | 100 | 0.6 | 25 |
| (H) | $\begin{aligned} & \text { Radio Transmitter } \\ & \text { T-172/FR } \end{aligned}$ | M. | $\begin{aligned} & 2000 \mathrm{~m} \\ & 4000 \end{aligned}$ |  |  | $\begin{aligned} & \text { FT-164 } \\ & \text { (oven) } \end{aligned}$ | 100 | 0.5 | 25 |
| (1) | Radio Transmitter T-125A/ARW-34 | M.O. | $\begin{aligned} & 1000 \\ & \text { (approx) } \end{aligned}$ | Audio for phase mod. |  | CANC 40138 Otis Elev. Co. | 120 | 22 |  |
| (J) | Radio Receiver WE D-99945 | 2nd beating oscillator | 3000 |  |  | Entire circuit in oven |  |  |  |
| (K) | $\begin{aligned} & \text { Exciter Unit } \\ & 0-5 / F R \end{aligned}$ | M.O. | $\begin{aligned} & 1800- \\ & 5800 \end{aligned}$ |  |  | $\begin{aligned} & \text { FT-249 } \\ & \text { (oven) } \end{aligned}$ | 100 | 0.25 | 10 |

Circuit Data for Figure 1-135. Fin kc. $R$ in kilohms. $C$ in $\mu \mu$. Lin $\mu$ h.
WADC TR 56-156


| R4 | $\mathrm{R}_{5}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | C3 | C4 | $\mathrm{C}_{5}$ | C ${ }^{\text {d }}$ | $\mathrm{C}_{7}$ | $L_{1}$ | $L_{2}$ | $V_{1}$ | $V_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\infty$ |  | 40 | $\infty$ | 0 | 0 | 100 |  |  | 770 | 0 | $\begin{gathered} 1 / 2 \\ 6 \mathrm{~N}^{2} \mathrm{GT} \end{gathered}$ | 6AC7 |
| 15 |  | 22 | 5000 | 40 | 5000 | 100 |  |  | 770 | 75 | $\begin{aligned} & 11 / 2 \\ & \text { 6SNTGT } \end{aligned}$ | $6 \mathrm{AC7}$ |
| 15 |  | 22 | 4700 | 39 | 4700 | 100 |  |  | 770 | 770 | $68 \mathrm{N7GT}$ | 6KC7 |
| $\infty$ |  | 40 | ¢ | 0 | 0 | 100 |  |  | 770 | 0 | $\begin{aligned} & 1 / 2 \\ & \text { 6SN7GT } \end{aligned}$ | $\begin{aligned} & 1 / 2 \\ & 6 S^{1 / 2} 7 T \\ & \hline \end{aligned}$ |
| 15 |  | 22 | 5100 | 39 | 5100 | 100 |  |  | 770 | 770 | $\begin{aligned} & 1 / 2 \mathrm{GT} \\ & \operatorname{GSN} \mathrm{C} \end{aligned}$ | 6SN7GT |
| 100 |  | 100 | 10,000 | 10,000 | 10,000 | 10,000 | 5 | 510 | 2600 | 2500 | 6SE7GT | 6V6GT |
|  |  | 100 | 10,000 | 10,000 | 10,000 |  |  |  | $\begin{aligned} & 2500 \\ & (50 \Omega) \end{aligned}$ |  | 6J5GT/G | 807 |
|  |  | 100 | 10,000 | 10,060 | 10,000 |  |  |  | $\begin{array}{r} 2500 \\ (50 \mathrm{~g}) \\ \hline \end{array}$ |  | 6.56T/G | 807 |
|  |  | 50 | 50 | 100 |  |  |  |  |  |  | $128 \mathrm{SL} 7 \mathrm{GT}$ | $12 \mathrm{sL} / \mathrm{FgT}$ |
|  |  |  |  |  |  |  |  |  |  |  | WE272A |  |
| 10 |  | 25 | 510 | 50,000 | 50,000 | 100 |  |  |  |  | 65 |  |



Figure 1-135. Comtinued


| Fig. | Equipment | Purpose | F, | F: | F | CR | $\mathbf{R}_{1}$ | R ${ }_{1}$ | R, |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (L) | Receiver-Transmitter RT-173/ ARC-33 | "Side-step" <br> injector oscil- <br> lator | 7662.5 | $\begin{aligned} & 104,840- \\ & 192,280 \end{aligned}$ | $\mathrm{F}_{1}+\mathrm{F}_{2}$ | CR-18/U | 47 | 68 | 68 |
| (M) | $\begin{aligned} & \text { Receiver-Transw } \\ & \text { mitter RT-173/ } \\ & \text { ARC- } 33 \end{aligned}$ | Main channel local oscillator | 12,517.8 | 15,325 | $F_{2}-F_{1}$ | CR-18/U | 11 | 470 | 33 |
| (N) | Lear Radio Set Model T-30AB-RCBBL-2 | Local oscillator | $\begin{aligned} & 655{ }^{65} \\ & 7155 \end{aligned}$ | $\begin{aligned} & \frac{45}{25} \\ & \hline \end{aligned}$ |  |  | 68 | 0.68 | 5 |
| (0) | Communication Equipment AN/CRC-3 | Local oscillator | $\begin{aligned} & 4755- \\ & 3845 \end{aligned}$ | $\begin{aligned} & 4300 \\ & \text { (1st I.F.) } \end{aligned}$ | $\begin{aligned} & \mathbf{F}_{1}-F_{2} \\ & o{ }_{2} \mathbf{F}_{2} \\ & \mathbf{F}_{1}(455 \\ & \left(F_{.}\right) \end{aligned}$ | FT-243 | 0.33 | 47 | 150 |
| (P) | Radio Set AN/ VRC-2 | $\begin{aligned} & \text { Local oscilla- } \\ & \text { tor } \end{aligned}$ | $\begin{aligned} & 4755 \mathrm{~m} \\ & \mathbf{3 8 4 5} \end{aligned}$ | $\begin{aligned} & 4300 \\ & (1 \text { st I.F. }) \end{aligned}$ | $\begin{aligned} & F_{1}-F_{2} \\ & \text { or } \\ & F_{2} F_{3} \\ & (455 \\ & (\mathbf{I F F . )} \\ & \hline \end{aligned}$ | FT-243 | 0.33 | 47 | 150 |
| (Q) | Radio Receiver R-114/VRC-4 | Local oscillator | $\begin{aligned} & 1175-1 \\ & 8175 \end{aligned}$ | $\begin{aligned} & 1700- \\ & 8700 \end{aligned}$ | $\begin{aligned} & F_{2}-F_{1} \\ & (525 \\ & \text { I.F. } \end{aligned}$ | $\begin{aligned} & \operatorname{Sig} 2 Z \\ & 3531 \mathrm{~B} \end{aligned}$ | 50 | 0.4 | 250 |

Circuit Data for Figure 1-135. Fin ke. $R$ in kilohms. $C$ in $\mu \mu$. L in $\mu$.

(0) (P)

Figwo 1-135. Continued

(0)

| R. | Rs | c, | C: | $\mathrm{C}_{3}$ | c. | $\mathrm{C}_{3}$ | c. | C. | $L_{1}$ | Ls | $\mathrm{V}_{1}$ | V |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 68 | 18 | 5 | 5 | 0 |  |  |  |  | 6AK5w |  |
|  |  | 300 | 0 | 10 | 22 | 18 |  |  |  |  | 6AS6W |  |
| 18 |  | 10 | 250 | 250 |  |  |  |  |  |  | 6K8 |  |
| 27 |  | 50,000 | 2,000 | 50,000 | 5-44 | 50 | 50 |  |  |  | $6 \mathrm{K8GF}$ |  |
| 27 |  | 50,000 | 2.000 | 50,000 | 5-14 | 50 | 50 |  |  |  | $6 \mathrm{K8GT}$ |  |
| 500 | 75 | 2,000 | 20,000 | 20,000 | 100 | 20,000 |  |  | 2500 |  | 6K8GT/G |  |

Section 1


| Fig. | Equipment | Purpose | $F_{1}$ | $\mathbf{F}_{2}{ }^{-}$ | Fs | CR | $\mathbf{R}_{1}$ | $\mathbf{R}_{2}$ | $\mathbf{R}_{\text {\% }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (R) | Receiver-Transmitter RT-178/ ARC-27 | 2nd injector ose (rec guard channel) | 15,950 |  |  | CR-18/U | 100 | 0.12 | $0.560+$ |
| (5) | Receiver-Transmitter RT-173/ ARC-33 | 2nd monitor ose of trans. M. | $\begin{aligned} & 8283.838-2 \\ & 3900 \end{aligned}$ |  |  | CR-27/0 | 220 | 0 | 1 |
| (1) | Receiver-Transmitter RT-173/ ARC-33 | 3rd monitor osciliator of M.O. | $\begin{aligned} & \mathbf{3 6 5 0} \\ & \mathbf{3 8 0 0} \end{aligned}$ |  |  | CR-27/U | 226 | 0 | 1 |
| (U) | Receiver-Transmitter RT-173/ ARC-33 | 4th monitor osciliator of M.O. | $\begin{aligned} & 5172.917- \\ & 5181.25 \end{aligned}$ |  |  | CR-27/U | $\mathbf{2 2 0}$ | 0 | 1 |
| (V) | Receiver-Transmitter RT-178/ ARC-27 | 1st transm mitter oscillator | 3450 |  |  | CR-18/U | 100 | 0.56 | 100 |
| (W) | Receiver-Transmitter RT-178/ ARC-27 | 2nd trans. osc (heterodyned with 1st) | $\begin{array}{\|l} 8250- \\ 9150 \end{array}$ |  |  | CR-18/U | 100 | 0.56 | 33 |
| (X) | $\begin{aligned} & \text { Transmitter } \\ & \mathrm{T}-217 / \mathrm{GR} \end{aligned}$ | lat i-f osellator | $\begin{aligned} & 1994 \\ & 2894 \\ & \hline \end{aligned}$ |  |  |  | 470 | 0.1 | 2.2 |
| (Y) | Radio ReceiverTranamitter RT-XA-101/ARC-22 | Local obe in recaliver | $\begin{aligned} & 9600 \\ & 10,500 \end{aligned}$ | $\mathrm{F}_{1}$ |  | CK-18/U | 47 | 22 |  |
| (2) | $\begin{aligned} & \text { Signal Generator } \\ & \text { SG-13/ARN } \end{aligned}$ | Fine freq ose for mixing with output of cosrse Ireq ose | Narrow band within $800-15,000$ range ( 10 crystals) | $\begin{aligned} & 14,400- \\ & 28,800 \end{aligned}$ | $\mathrm{F}_{2} \pm \mathrm{F}_{1}$ | CR-18/U | 100 | 0.15 | 38 |

Circuit Data for Figure 1-135. Finke. $R$ in kifohms. $C$ in $\mu \boldsymbol{m}$. L in $\mu \mathrm{h}$.

figure 1-135. Cominued

(r)

(2)



Figure 1-136. Modifications of Pierce oscillator using screen-grid fubes

| Fig. | Equipment | Purpose | $F_{1}$ | $\mathbf{F}_{3}$ | CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathbf{R}_{3}$ | $\mathbf{R}_{4}$ | Rs | R. | $\mathrm{R}_{7}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Set AN/ <br> FRC-10 (WECo <br> Transmitter <br> D-156000) | L-F ose for single-sideband operation | 625 |  | $\begin{gathered} \text { WECo } \\ 7 \mathrm{~B} \end{gathered}$ | 250 | 1 | 1 | 20 | 0 |  |  |
| (B) | Same as (A) | H-F ose ior single-3ideband operation | $\begin{aligned} & 940 \\ & 5000 \end{aligned}$ |  | $\begin{gathered} \text { WECo } \\ 5 A A \end{gathered}$ | 100 | 1 | 10 |  | 5 |  |  |
| (C) | Switching Unit SA-107 ( )/MRC-4 | BFO for two diversity receivers | 462.45 |  |  | 50 | 120 | 22 | 500 | 1000 |  |  |
| (D) | Radio Receiver R-270/FRR | BFO | 462.45 | $\mathrm{F}_{1}$ | Bliley <br> SR-901 (FT- <br> 241A) | 100 | 470 | 100 | 4.7 |  |  |  |
| (E) | Radio Receiver BC-659-() | Local ose of receiver | $\begin{aligned} & 5675- \\ & 8650 \end{aligned}$ | 4 Fi | FT-243 | 470 | 1000 | 270 |  |  |  |  |

Circuit Data for Figure 1-136. Finke. $R$ in kilohms. $C$ in $\mu \mu f . L$ in $\mu h$.
WADC TR 56-156


| $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{C}_{3}$ | C4 | C5 | C6 | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | C ${ }^{\text {g }}$ | $L_{1}$ | $\mathrm{L}_{2}$ | $\mathrm{V}_{1}$ | $\mathrm{V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 10,000 | 10,000 | 10,000 | 1000 | 250 | 50 | 100 | 10 | 200 |  | RCA41 |  |
| $\begin{aligned} & \text { Vari- } \\ & \text { able } \end{aligned}$ | 10,000 | 10,000 | 10;000 | 1000 | 0 | 0 | 0 | 1000 | 0 |  | RCA41 |  |
| 100 | $\begin{aligned} & 10- \\ & 100 \end{aligned}$ | 100,000 | 75 | 20,000 |  |  |  |  | $\begin{gathered} 2590 \\ (25 \Omega) \end{gathered}$ |  | 6SJ7 | 6SN7 |
| 39 | 10,000 | 100 | 100 | 95 | 100 | 5 |  |  |  |  | 6SJ7 |  |
| 1000 | 10,000 | 55 | 10,000 | 25 |  |  |  |  | 1140 | $\begin{gathered} 8 \\ \substack{\text { turns } \\ 5 / 8-\mathrm{in} . \\ \text { dia }} \end{gathered}$ | $\begin{aligned} & \text { 3D6/ } \\ & 1299 \end{aligned}$ | 1LC6 |



| Fig. | Equipment | Purpose | F, | F: | CR | $\mathbf{R}_{1}$ | R , | R. | R. | R ${ }_{\text {s }}$ | R. | R: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (F) | Radio Transmitter BC-$329-\mathrm{N}$ | M.O. | $\begin{aligned} & 200- \\ & 400 \end{aligned}$ |  | FT-249 | 100 | 0.22 | 15 | 10 | 66 | 5 | 0.022 |
| (G) | Lear Radio Set T-30AB-RCBBL-2 | M.O. | $\begin{aligned} & 2900- \\ & 6500 \end{aligned}$ |  |  | 470 | 0.1 | 100 | 100 | 7.5 | 18 |  |
| (H) | Modulator- <br> Transmister <br> T-233/URW-3 | M.O. for remote-control transmitter | $\begin{aligned} & 3966.6- \\ & 5666.6 \end{aligned}$ | $2 F_{1}$ | $\begin{aligned} & \text { CR } \\ & \mathbf{A R} \end{aligned}$ | 47 | 0.33 | 6.8 | 30 | 27 | 0.0051 |  |
| (I) | Modulator- <br> Transmitter <br> BC-1158 | M.O. | $\begin{aligned} & 3966.6- \\ & 5666.6 \end{aligned}$ | 2Fi | $\mathrm{CR}-1 \mathrm{~A} /$ | 47 | 0.33 | 6.8 | 30 | 27 | 0.0051 |  |
| (J) | Radio Trans- <br> mitter 12GLX-2 | M. ${ }^{\text {. }}$ | $\begin{aligned} & 260- \\ & 1750 \end{aligned}$ | $F_{1}$ | $\begin{aligned} & \text { Holder } \\ & \text { FT-249 } \end{aligned}$ | 100 | 0.1 | 50 | 385 | 25 |  |  |

Circuit Data for Figure 1-136. Fin ke. $R$ in kilohms. $C$ in $\mu \mu$. L in $\mu \mathrm{h}$.


## Section I

Crystal Oscillators


Figure 1-137. Electron-coupled Pierce oscillator modifications. All circuifs except circuit (A) provide frequency multiplication

| Fig. | Equipment | Purpose | $F_{1}$ | $\mathrm{F}_{2}$ | Fs | CR | $\mathbf{R}_{1}$ | $\mathbf{R}_{2}$ | $\mathrm{R}_{3}$ | R. | Rs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Receiver-Transmitter RT-178/ARC-27 | Spectrum oscillator | 10,000 | $F_{1}$ |  | CR-27/U | 100 | 56 | 12 | 100 | 0 |
| (B) | $\begin{aligned} & \text { Radio Receiver } \\ & \text { R-252/ARN-14 } \end{aligned}$ | 2nd monitor ose of receiver vfo | $\begin{aligned} & 11,275- \\ & 11,725 \end{aligned}$ | $F_{1}$ |  | CR-33/U | 8.2 | 68 | 0 |  | 2.2 |
| (C) | Radio Transmitter BC-400(B,C,D,E) | M.O. for mar ker beacon | 4166.67 | $2 \mathrm{~F}_{1}$ |  | FT-164 | 200 | 35 | 5 | 20 | 0 |
| (D) | Radio Transmitter T-67/ ARC-33 | M.O. | $\begin{aligned} & 5555- \\ & 8666 \end{aligned}$ | $2 F_{3}$ | $6 \mathrm{~F}_{1}$ | CR-1A/AR | 5.1 | 0.018 | 47 | 47 | 0.088 |
| (E) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-1A } \end{aligned}$ | Main-channel heterodyne freq osc | $\begin{aligned} & 5020- \\ & 8120 \end{aligned}$ | $2 \mathrm{~F}_{1}$ | 18Fi | $\begin{aligned} & \mathrm{CR}-\mathrm{AN} / \mathrm{AR} \\ & \text { or } \\ & \text { CR-18/AR } \end{aligned}$ | 100 | 8.2 | $\overline{1}$ | 100 |  |
| (F) | $\begin{aligned} & \text { Frequency Meter } \\ & \text { TS-186/UP } \end{aligned}$ | Crystal calibrator | 5000 | $2 F_{1}$ |  | Navy CG $40210 ; G E$ G31 Ther- mocell. 6L6 tube envelope; heater; 0.002 per cent, 20 to $75^{\circ} \mathrm{C}$ | 1.5 | 100 | 100 | 10 | 100 |
| (G) | Frequency Meter TS-186(B/C)/UP | Crystal calibrator | 5000 | $2 \mathrm{~F}_{1}$ |  | $\begin{aligned} & \mathrm{CR}-18 / \mathrm{U} \\ & \text { (oven, } \\ & 60^{\circ} \mathrm{C} \text { ) } \end{aligned}$ | 1.5 | 100 | 100 | 10 | 39 |

Circuit Data for Figure 1-137. $F$ in kc. $R$ in kilohms. $C$ in $\mu$ f. L in $\mu \mathrm{h}$.


| R* | $\mathrm{R}_{7}$ | $\mathrm{R}_{8}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{C}_{3}$ | C. | $\mathrm{C}_{5}$ | C | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | $\mathrm{L}_{1}$ | $\mathrm{L}_{2}$ | $\mathrm{V}_{1}$ | $\mathrm{V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 20 | 220 | 2000 | 0 | 100 | 0 | 1.5-7 |  | 500 | 0 | 6AG5 | 6AG5 |
|  |  |  | 22 | 150 | 1800 | 0 | 470 | 1800 | 0 |  |  |  | $\begin{aligned} & 5654 / \\ & 6 \mathrm{AK5} \end{aligned}$ | Discriminator rectifier |
|  |  |  | 22 | 100 | 1500 | 35 | 1500 | 1500 | 0 |  | 1000 |  | 6L6 | 6L6 |
| 10 | 47 | 0.039 | 100 | 10 | 100,000 | 33 | 8-114 | 10,000 | 100 | 51 | 2500 | 2500 | 6V6GT | 6V6GT |
|  |  |  | 16 | 100 | 6000 | 14 | $\begin{aligned} & 2.5- \\ & 9.5 \end{aligned}$ | 8-73 | 51 |  | 1.1 | $\underset{\text { turns }}{15}$ | 6AK5 | 6AK5 |
|  |  |  | 4-12 | 470 | 100 | 470 | 22 | 100 | 470 |  | 4-9 | $\begin{gathered} 35 \\ (7 \Omega) \end{gathered}$ | 6SJ7 | $6 \mathrm{SJ7}$ |
|  |  |  | 6-36 | 470 | 100 | 470 | 22 | 51 |  |  | 4-9 | $\begin{gathered} 35 \\ (7 \Omega) \end{gathered}$ | 6SJ7 | 6 S 57 |

## Section 1

## Crystal Oscillators


(II)

| Fig. | Equipment | Purpose | $F_{1}$ | F: | $\mathrm{F}_{3}$ | CR | $\mathbf{R}_{1}$ | R | $\mathbf{R}_{3}$ | R. | Rs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (H) | Aircraft Radio <br> Corp. Radio <br> Transmitter ARC <br> Types T-13 and <br> T-11A | M. 0 . | $\begin{aligned} & 6000- \\ & 9000 \end{aligned}$ | $\mathbf{3 F}_{\mathbf{1}}$ |  | $\begin{aligned} & \text { CAATC } \\ & \text { H1081 } \end{aligned}$ | 100 | 0.56 | 56 | 0.18 | 100 |
| (I) | $\begin{aligned} & \text { Radio Receiver } \\ & \text { R-270/FRR } \end{aligned}$ | Local oscillator | $\begin{aligned} & 1965- \\ & 8511.6 \end{aligned}$ |  |  | $\begin{aligned} & \mathrm{HC-1/U} \\ & \text { Holder } \end{aligned}$ | 47 | 27 |  |  |  |
| (J) | $\begin{aligned} & \text { Radio Trans- } \\ & \text { mitter BC-655- } \\ & \mathbf{A},-\mathbf{A M} \end{aligned}$ | M.O. | $\begin{aligned} & \hline 5560- \\ & 8660 \end{aligned}$ | $2 \mathrm{~F}_{1}$ |  | $\begin{aligned} & \text { DC-11- } \\ & \text { 16, DC- DC- } \\ & 26, \text { or } \\ & \text { CR } \\ & \text { AR } \quad \text { AR } \\ & \hline \end{aligned}$ | 50 | 50 | 0.05 | 50 | 6 |
| (K) | $\begin{aligned} & \text { Radio Transmitter } \\ & \text { BC-401-B } \end{aligned}$ | M. 0. | $\begin{aligned} & 1000- \\ & 4575 \end{aligned}$ | $2 \mathrm{~F}_{1}$ |  |  | 100 | 0.51 |  |  |  |

Circuit Data for Figure 1-137. Fin ke. R in kilohms. C in $\mu \mu \mathrm{f}$. Lin $\mu \mathrm{h}$.

(d)


| R. | $\mathrm{R}_{7}$ | R4 | c, | C, | C | C. | C. | C. | c. | $\mathrm{C}_{8}$ | $L_{1}$ | $L_{*}$ | $V_{1}$ | V |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 85 | 120 | 120 | $\begin{gathered} 40 \\ (\mathrm{~T}-13) \\ 50 \\ (\mathrm{~T}-11) \end{gathered}$ | 750 | 100 | 750 |  | 16,900 |  | 6AQ5 | 6AQ5 |
|  |  |  | 100 | 9-140 | 10,000 | 10 |  |  |  |  | $\begin{aligned} & 25,000 \\ & (160 \Omega) \end{aligned}$ | $\begin{aligned} & 25,000 \\ & (160 \Omega) \end{aligned}$ | 6AC7 | Mixer |
|  |  |  | 10 | 50 | 6800 | 6800 | $\begin{gathered} 11- \\ 65.5 \end{gathered}$ | 100 | 6800 |  | $\begin{aligned} & 2600 \\ & (50 \Omega) \end{aligned}$ | $\begin{aligned} & 9-1 / 2 \\ & \text { turns } \end{aligned}$ | 6G6G | 12.8 |
|  |  |  | 250 | 6000 | 6000 | 6000 | 6000 | 6000 | 1000 | 360 | 2500 |  | 837 | 807 |


(N)

| Fig. | Equipment | Purpose | F | F | F | CR | $\mathrm{R}_{1}$ | R | R, | $\mathrm{R}_{4}$ | Rs, |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (L) | Frequency Meter BC-638-A | M.O. for signal generator | $\begin{aligned} & 5555.55- \\ & 8666.6 \end{aligned}$ | $\underset{(?)}{2 F_{1}}$ |  | Sig 27 <br> 3501-11A <br> (Bendix) | 100 | 40 | 150 | 0-2.2 |  |
| (M) | $\begin{aligned} & \text { Frequency Meter } \\ & \text { BC-1420 } \end{aligned}$ | M.O. for signal generator | $\begin{aligned} & 5555.55- \\ & 8666.6 \end{aligned}$ | $\begin{aligned} & 2 F_{1} \\ & (?) \end{aligned}$ |  |  | 100 | 40 | 150 | 0-2.2 |  |
| (N) | $\begin{aligned} & \text { Radio Receiver } \\ & \text { R-540/ARN-14C } \end{aligned}$ | Low freq injection ose | $\begin{aligned} & 8150-9100 \\ & (20 \\ & \text { crystals) } \end{aligned}$ | $2 \mathrm{~F}_{1}$ |  | CR-18/U | 100 | 0.15 | 47 | 18 | 4.7 |
| (O) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-34(XA-1) } \\ & \hline \end{aligned}$ | Sidestep ose | 5275 | $F_{1}$ |  | CR-18/U | 0.01 | 18 | 3.3 | 15 | 0.1 |
| (P) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-34(XA-1) } \end{aligned}$ | Ist monitor ose of transmitter M.O. | 833.333 | $F_{1}$ | $F_{1}$ | CR-27/U | 560 | 56 | 10 | 1000 |  |

Circuit Data for Figure l-137. Finke. R in kilohms. C in $\mu \mu \mathrm{f} . \mathrm{L}$ in $\mu \mathrm{h}$.
WADC TR 56-156

(0)


Figure 1-137. Cominued
(P)

| Rs | R | Rs | $\mathrm{C}_{1}$ | c. | C. | $\mathrm{C}_{4}$ | C | c. | C; | $\mathrm{C}_{5}$ | $L_{1}$ | L: | $\mathrm{V}_{1}$ | $\mathrm{V}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 25 | 10,000 | 3000 | $\begin{array}{\|l} 6-42 \\ \text { (each } \\ \text { sect- } \\ \text { ion) } \\ \hline \end{array}$ | 1000 |  |  |  | $\begin{aligned} & 1700 \\ & (40 \Omega) \end{aligned}$ | 7.5 | 6SK7 | 9003 |
| 100 |  |  | 25 | 100 | 3000 | $\begin{aligned} & \text { 6-42 } \\ & \text { (each } \\ & \text { (sect- } \\ & \text { ion) } \end{aligned}$ | 1000 |  |  |  | $\begin{gathered} 1700 \\ (40 \Omega) \end{gathered}$ | 9.3 | 6SK7 | 9008 |
|  |  |  | 20 | 220 | 2000 | 10 | 8000 | 90 | 103 | 5 | 500 |  | 6AK5 |  |
| 0.1 | 27 | 28 | 33 | 560 | 100 | 10,000 | 3 | 10,000 | 1.5-7 |  |  |  | 5639 | Balaneed modulator |
|  |  |  | 1000 | 10 |  | 15 | 220 | 10,000 | 50,000 |  | 500 |  | 6636 |  |

## Section 1

Crystal Oscillators

(Q) (R) (S)
fleure 1-137. Comflnued

(T)

| Fig. | Equipment | Purpose | $F_{1}$ | $F:$ | $F_{3}$ | CR | $\mathrm{R}_{1}$ | n* | R: | R. | Rt |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (Q) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-34(XA-1) } \end{aligned}$ | 2nd monitor ose of transmitter M. 0 . | $\begin{aligned} & 3230-3900 \\ & (5 \\ & \text { crystals }) \\ & \hline \end{aligned}$ | $F_{1}$ |  | CR-27/U | 560 | 56 | 4.7 | 1.8 | 0.68 |
| (R) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-34(XA-1) } \end{aligned}$ | 3rd monitor ase of transmitter M.O. | $\begin{aligned} & 3650-3775 \\ & \text { ( } 4 \\ & \text { cryatals }) \end{aligned}$ | $F_{3}$ |  | CK-27/U | 560 | 56 | 4.7 | 1.8 | 0 |
| (S) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-34(XA-1) } \end{aligned}$ | 4th monitor ose of transmitter M. O . | $\begin{aligned} & 5130-5165 \\ & (5 \\ & \text { crystals }) \end{aligned}$ | $F_{1}$ |  | CR-27/U | 560 | 56 | 4.7 | 1.8 | 0 |
| (T) | $\begin{aligned} & \text { Radio Set } \\ & \text { AN/ARC-34(XA-1) } \\ & \hline \end{aligned}$ | 2nd ose for guard channel | 13,025 | $F_{1}$ |  | CR-18/U | 560 | 0.56 | 4.7 |  |  |
| (U) | $\begin{aligned} & \text { Radio Receiver } \\ & \text { R-322/ARN-18 } \end{aligned}$ | Local osc | $\begin{aligned} & 11,490- \\ & 11,700 \\ & \text { (20 } \\ & \text { erystals) } \\ & \hline \end{aligned}$ | 3Fi |  | CR-18/( | 0.01 | 100 | 0.1 | 16 | 1.6 |
| (V) | Signal Generator SG-13/ARN | Coarse freq ose for mixing with output of fine freq ose | $\begin{aligned} & 4800-9600 \\ & \text { (28 } \\ & \text { crystals) } \end{aligned}$ | 8Fi |  | CR-18/U | 100 | 0.15 | 100 | 18 |  |

Circuit Data for Figure 1-137. Fin ke. R in kilohms. C in $\mu \mathrm{h}$. L in $\mu \mathrm{h}$.
WADC TR 56-156

(v)

| R. | $\mathrm{R}_{7}$ | R, | C | $\mathrm{C}_{2}$ | c, | C. | C. | C. | C, | $\mathrm{C}_{8}$ | $L_{1}$ | $L_{1}$ | $\mathrm{V}_{1}$ | $\mathrm{V}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.47 | 10 | 47 | 1000 | 10 | 33 | 10,000 | 470 | 0 | 22 | 5000 |  | 5840 | 5636 |
| 0 | 0 | 10 | 47 | 1000 | 10 | 33 | 10,000 | 470 | 12 | 0 | 5000 |  | 5840 | 5636 |
| 0 | 0 | 2.2 | 47 | 1000 | 10 | 83 | 10.000 | 470 | 10 | 0 | 5000 |  | 5840 | 6840 |
|  |  |  | 1000 | 22 | 33 | 10,000 | 10,000 | 1000 | 130 |  | 500 |  | 5840 |  |
|  |  |  | 5 | 27 | 1000 |  | 1000 |  |  |  |  | RFC | 6AK5 |  |
|  |  |  | 2-7.5 | 5 | 82 |  | 2400 |  | 1500 |  | 500 |  | 6AK6W |  |

## Section I

Crystal Oscillators


Figure 1-138. Electron-coupled Pierce oscillator modifications for helerodyne circuits

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | $\mathrm{F}_{2}$ | F3 | CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Receiver R-252/ARN-14 | 1st monitor ose of receiver vio. | $\begin{aligned} & 14,000- \\ & 20,500 \end{aligned}$ | From isolation amplifier of vfo. | $\mathbf{F}_{2}-\mathrm{F}_{1}$ | CR-33/U | 10.4 | 10 |
| (B) | Signal Generator TS-413/U | Grystal harmonic heterodyne mixer | 1000 | $\begin{aligned} & \text { Variable } \\ & \text { rit } \end{aligned}$ | $\begin{aligned} & \mathbf{n F}_{1} \pm \\ & \mathbf{F}_{2}\left(n^{ \pm}=\right. \\ & 1,2, \ldots) \end{aligned}$ | DC-9-AJ | 1000 | 35 |
| (C) | Radia Receiver R-146A/AKW-35 | 2nd heterodyne osc | 5456 | 5000 | $\mathbf{F}_{1}-\mathrm{F}_{2}$ | FT-243 | 47 | 47 |
| (D) | R-F Signal Generator Set AN/URM-25C | Crystal calibrator harmonic generator and mixer | 1000 | $\left.\begin{array}{\|l\|l} 10-50,000 \\ \text { (output fom } \\ \text { variable osc } \end{array}\right)$ | $\mathrm{nF}_{1} \pm \mathrm{F}_{2}$ | CR-18/U | 1 | 270 |
| (E) | Radio Receiver R-277 (XA-A)/ <br> Al'N-70 | Local osc | $\begin{aligned} & 400 \\ & 480 \\ & 2850 \\ & 2950 \\ & 3000 \\ & 3050 \end{aligned}$ | $\mathrm{F}_{1}-\mathrm{F}_{3}$ | $\begin{aligned} & 300 \\ & 1100 \\ & \text { (IF) } \end{aligned}$ |  | 22 | 0.068 |

Circuit Data for Figure 1-138. Fin ke. $R$ in kilohms. $C$ in $\mu \mu$. L in $\mu$ h.

Section 1


| $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | $\mathrm{R}_{5}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{3}$ | C3 | C | C3 | $\mathrm{C}_{6}$ | $L_{1}$ | $\mathrm{L}_{2}$ | $L_{3}$ | $V_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 47 | 22 | 6.8 | 68 | 27 | 470 | 470 | 47 | 1800 |  |  |  | $\begin{aligned} & 5725 / \\ & \text { 6AS6 } \end{aligned}$ |
| 100 | 10 |  | 330 | 5600 | 10,000 | 1000 |  |  | 2500 |  |  | 6SA7 |
| 47 | 47 |  | 25 | 5-30 | 55 | 50,000 |  |  |  |  |  | 12SA7 |
| 30 | 100 | 510 | 1000 | 6-25 | 270 | 10,000 | 10,000 |  | 2500 | 500 |  | 6BE6 |
| 22 |  |  | 47 | 470 | 100 | 47,000 |  |  |  |  |  | 5750 |

## Preventing $B^{+}$Voltage from Existing

 Across Crystal Unit in Pierce Circuit1-320. There are two commoniy used methods for preventing the application of the $\mathrm{B}^{+}$voltage across the crystal unit. One mechod is to connect a blocking capacitor in series with the crystal unit. The other method is to connect the crystal unit directly to ground, and the plate to ground through an r-f bypass capacitor. With this arrangement, the cathode must be operated above r-f ground. Except for the advantages of electron-coupling to the load to be had in the tri-tet circuit, which uses screen-grid tubes, the r-f-grounded-plate modification is not to be preferred since the plate-to-grid capacitance directly shunting the crystal unit is greatly increased by the addition of the grid-toground capacitance. When a capacitor is used to block the $\mathrm{B}^{+}$voltage from the crystal, a number of modifications are possible, three of which are shown in figures 1-135 (F), (G), and (K). In each figure, the blocking capacitor is the one labeled $\mathrm{C}_{2}$, and has a reactance negligible with respect to that of the crystal unit. The more usual circuit arrangement is that shown in figure 1-135 (K). In figure 1-135 (G), $\mathrm{C}_{2}$ plays a dual function in blocking the $\mathrm{B}^{+}$voltage from both the crystal and the grid circuit of the succeeding stage. The circuit in figure 1-135 (F), although not effective in blocking the $\mathrm{B}^{+}$voltage from the crystal unit, does, of course, reduce the d-c potential across the crystal equally as well as the other arrangements. It is desirable to keep the d-c potential across the crystal unit low; otherwise the crystal may be heavily strained in one direction, and the chance is increased that the elastic limit of the crystal will be approached on the alternation of the a-c voltage of the same polarity, or, at least, that the effect on the crystal will cause the performance characteristics to deviate from test specifications. Since the crystal unit, itself, is a capacitor of considerably greater dielectric thickness and smaller crosssectional area than the usuai blocking capacitor, it might seem questionable that the d-c voltage across the crystal unit could be expected to be significantly reduced. Certainly in the static state, an air-gap crystal unit should have at least as high a resistance to leakage currents as would the blocking capacitor. However, in the dynamic state some degree of ionization will occur if the voltage is excessive. The consequent leakage tends to charge the blocking capacitor to the full plate-to-grid d-c voltage. An unchecked $B^{+}$voltage not only can increase the likelihood of corona effects, but also can lead to continuous discharge should corona losses once begin, and to an increase in the effective re-
sistance of the crystal unit, a reduction of the grid bias, and perhaps even to arcing and puncturing of the crystal. A blocking capacitor, if it does not remove the d-c potential completely from across the crystal unit, at least can ensure that the potential is not sufficient to cause ionization. A blocking capacitor is generally more important in high-drive circuits employing air-gap crystal units.
1-321. Figure 1-135 (X) shows one example of a grounded-crystal, grounded-plate Pierce circuit. At first glance such an oscillator might very easily be mistaken for the Miller type. $C_{3}$ is a relatively large capacitance that causes the plate to be at r-f ground. $C_{1}$ is effectively $C_{p}$, the plate-to-cathode capacitance, and $C_{2}$ serves as the lumped part of $C_{\text {r }}$. By interchanging $C_{1}$ and $C_{3}$ and making the ground connection of the crystal a plate connection, essentially the same oscillator characteristics are obtained except that the $\mathrm{B}^{+}$is across the crystal unit. Note that the circuit is designed for the maximum possible output voltage, in that the output is taken across the crystal unit directly, instead of across $C_{1}$, the effective plate capacitance, alone. The fact that the plate is at r-f ground does not remove the grid-to-plate capacitance from shunting the crystal unit, but adds to this the grid-to-ground capacitance. In the circuit of figure 1-135 (R), a small tuning canacitance, $\mathrm{C}_{4}$, is also shunted across the crystal unit. In addition to this there is the extra shunt capacitance contributed by the oven in which the crystal is mounted. In circuit ( R ), the $\mathrm{C}_{1} / \mathrm{C}_{2}$ ratio, which is approximately equal to the $C_{g} / C_{p}$ ratio, is on the order of $1 / 4$. The gridleak losses are increased somewhat, since the grid resistance is connected across the crystal instead of across the grid capacitance. All these factors tend to reduce the effective $Q_{r}$ of the feedback circuit, so it would appear that with crystal units of greater than average resistance the circuit operates with the tank considerably detuned from resonance. The fact is, however, that connecting the grid resistance across the crystal serves to concentrate most of the grid losses in the plate-to-grid circuit and to eliminate them from the grid-to-cathode circuits, and this probably increases the effective feed-back $Q_{i}$ more than the increased losses diminish it. The circuit in figure 1-135 (X) is similar to that in figure 1-135 (R) except that the tuning capacitance has been eliminated and the output is obtained directly across the crystal unit. It is claimed that this arrangement tends to smooth the output and to reduce the harmonics. What probably is meant is that for a given output voltage the harmonic content is less. This can readily be seen, for the voltage across
the crystal unit is equal to the sum of the voltages across $C_{1}$ and $C_{2}$. If the same output is to be taken across either capacitance alone, the excitation must be increased and the circuit will generally be operated beyond tube cutoff a greater fraction of the time, thereby increasing the higher-harmonic content. It should also be noted that the output arm in figure 1-135 (X), since it shunts the crystal, is effectively part of the feed-back circuit. Should the load increase or decrease, so also will the excitation. The circuit is thus a tri-tet modification where the output voltage is somewhat stabilized against changes in the load, but only at the sacrifice of frequency stability. This feature is not important in the particular fixed-load circuit of figure 1-135 (X), since the load in this circuit appears to be reasonably constant.

## Electron-Coupled Pierce Oscillator

1-322. The electron-coupled oscillator permits a remarkable freedom from coupling between the plate load circuit and the crystal circuit. Screen-grid tubes are required, with the screen grid serving as the plate of the oscillator circuit. When electron coupling is used in conjunction with Pierce oscillators, the tri-tet arrangement, where the plate load circuit is in series with the oscillator tank, is generally the most advantageous, and is used in all the circuits shown in figure 1-137 except in circuits (I) and (D). With the screen at r-f ground, the vacuum-tube plate circuit performs as a conventional pentode r-f amplifier, with the excitation of the control grid a function of both the screen and plate r-f currents. Variations in the plate impedances have much less effect upon the frequency than do similar variations in the oscillator tank impedances. For this reason, even if the oscillator is to operate over a wide range of crystal frequencies, a tunable coil and capacitor tank can be placed in the plate circuit to obtain a smoother sine-wave output without running the risk of greatly changing the loud capacitance of the crystal circuit. In effect, the electron-coupled oscillator reduces by one the number of amplifier stages that are required, and hence is particularly applicable for small portable transmitters where the crystal circuit must perform as nearly as possible the function of a power oscillator. The widest application of the electron-coupled Pierce circuit is for the purpose of frequency multiplication. In figure 1-137 (D), for example, the plate tank circuit is tuned to twice the crystal frequency. The L/C ratio of the plate tank should be as small as practicable, in order to increase the output selectivity and to ensure a low-impedance bypass through the coil for the fundamental frequency and through the ca-
pacitor for all harmonics higher than the second. The larger the angle $\theta$ during which the tube is cut off, the larger will be the percentage of the higher-harmonic generation in the output. In general, the lower the order of the harmonic, the greater is its energy content. For optimum output, the tube should not be heavily conducting during a positive alternation of the plate harmonic voltage, $\mathrm{E}_{\mathrm{h}}$. During such intervals the plate tank would be losing energy to the circuit at an instantaneous rate of $i_{b} e_{b}$, where $i_{b}$ is the instantaneous d-c plate current and $e_{h}$ is the instantaneous harmonic voltage across the plate tank. To meet the requirements above, plate current should be allowed to flow only during the interval of approximately one alternation of a harmonic cycle. Since the tube is to be cut on and off at the fundamental frequency, the plate tank, after receiving a pulse of energy during one alternation of a harmonic cycle, must oscillate freely for the remaining part of the fundamental period. If the frequency is being doubled, plate current should flow approximately one-fourth the time; if the frequency is being tripled, plate current should flow approximately one-sixth of the time. To generalize, if the frequency is to be multiplied $n$ times, optimum n'th harmonic output is approached if the oscillator is designed so that the tube conducts approximately $1 / 2 n$ of each fundamental cycle. In paragraph 1-312, it was found that for a given peak value of $i_{b},\left(I_{b m}\right)$, the effective $I_{p}$ was essentially constant for all bias voltages between class-A and class-B operations, although a small maximum occured when the tube was cut off during three-fifths of the negative alternation. See equation 1-312 (20). If the plate load is constant, as is the case in the electron-coupled circuit, this point of maximum $I_{p}$ coincides with the conditions of maximum output. If we assume that approximately the same conditions hold in the case of frequency multiplication, maximum harmonic output is approached if the tube continuously conducts $7 / 10$ of the period of one harmonic cycle, or $7 / 10 \mathrm{n}$ of the period of the fundamental cycle. Since the maximum is not at all sharp, the optimum operating conditions are not critical and can be assumed to extend over a range which permits the tube to conduct from $1 / 2 \mathrm{n}$ to $7 / 10 \mathrm{n}$ of the time. That is, for optimum output, the oscillator section can be designed so that the crystal unit of average resistance allows the tube to be cut off during a fundamental-cycle angle within the range given by

$$
\text { (optimum) } \theta=\frac{\pi(2 n-1)}{n} \text { to } \frac{\pi(10 n-7)}{5 n}
$$

The principal advantage of the tri-tet circuit is that the excitation voltage tends to increase with an increase in load. If the output is to be inductively coupled to the succeeding stage, the tri-tet arrangement tends to stabilize the output voltage when the coefficient of coupling is varied. This feature originally found its greatest popularity among radio amateurs, although it was used principally in conjunction with Miller rather than Pierce oscillators. Figure 1-139 shows the basic tri-tet circuit as applied to Pierce and to Miller oscillators. It is the adaptability to frequency multiplication rather than to variable load conditions, however, that is of greatest importance when considering the tritet circuit for use in military equipments. The tritet frequency statility is low compared with that of the conventional pentode circuit because of the large stray capacitance (approximately $8 \mu \mu$ ) that directly shunts the crystal unit. About $4 \mu \mu$ is the $\mathrm{C}_{\mathrm{zig} 2}$ of the tube, and the remainder is the capacitance of the grid leads to ground, which otherwise would be part of $\mathrm{C}_{\mathrm{g}}$.

## Miscellaneous Pierce Circuit Modifications

1-323. Circuits (A) and (B) in figure 1-135 are of interest because they indicate two stages in the development of a particular modification of the Pierce osciltator. Originally $L_{3}, C_{3}, C_{4}$, and $R_{4}$ were not present. Since no grid capacitance is employed other than that of the tube, the $\mathrm{C}_{\mathrm{g}} / \mathrm{C}_{\mathrm{p}}$ ratio is very small. The tube has approximately $4 \mu \mu \mathrm{f}$ capacitance between plate and grid, and it may be assumed that the crystal oven adds a comparable amount directly across the crystal. In all probability the phase-shifting $Q_{f}$ of the feed-back circuit is rather low, so that the tank can be expected to be more reactive than resistive. $L_{n}$ is resonant with $C_{1}$ at the mid-point of the intended frequency range. If the feed-back circuit is operated with a high effective $Q_{\text {s }}$, this value of $L_{1}$ should provide a zero phase shift in $I_{p}$. In this event, the tube would operate into a resistive load, and a theoretical independence of the frequency with changes in $R_{p}$ could be predicted. As it is, the low feed-back $\mathrm{Q}_{\text {r }}$


Figure 1-139. Basic tri-tet circuits where excitation veltage in a function of both serven- and plate-circult r-f currents
probably requires the crystal tank circuit to be detuned to such a point that at equilibrim it appears either as a reactance much greater in magnitude than that of the coil $L_{1}$, or as a reactance approximately equal to that of $\mathrm{C}_{1}$, in which case the lagging component of the current through the crystal unit is negligible compared with the current through $C_{1}$. Under these latier conditions, the tube would operate into a low-impedance, series-resonant circuit at the mid-point of the frequency range, where $\mathbf{X}_{\mathbf{L} 1}+\mathbf{X}_{\mathbf{C}, ~}=\mathbf{0}$. Nevertheless, it was found that oscillations could not be maintained dependably at the mid-point of the frequency range. It was for this reason that the changes were made in the models represented by circuit (B), as indicated in the data chart for figure 1-135. The tank circuit $\mathrm{L}_{3} \mathrm{C}_{3}$ is resonant at the mid-point of the frequency range. $C_{1}$ has been changed so that the reactance of the coil $L_{1}$ is lower than the reactance of the crystal tank at all frequencies. $R_{4}$ has been added to dampen the effect of $L_{1}$ at the high end of the frequency range. It may be that the dead spot at the mid-point of the frequency range in circuit (A) was due only to transient effects in the crystal units before oscillations could build up, or it may have been due to the fact that the feed-back $Q_{t}$ was insufficient to provide the necessary plate impedance to maintain equilibrium even if oscillations were once started.
1-324. An interesting circuit is that shown in figure 1-136 (D). The feed-back voltage is developed across $C_{4}$ by the r-f plate current. $C_{3}$, although of the same capacitance as $C_{4}$, maintains the screen at $r$-f ground, since $R_{2}$ is very large. The large value of $R_{2}$ keeps the screen voltage, and hence the out put, at very low values, so that the crystal is only weakly driven.
1-325. The circuit shown in figure 1-136 (E) is
intended to supply a fourth-harmonic excitation of the $V_{2}$ stage. For this purpose the $C_{3} L_{2}$ tank is tuned to $4 \mathrm{~F}_{1}$. A low $\mathrm{L}_{2} / \mathrm{C}_{3}$ ratio is provided, to ensure that the fundamental is effectively bypassed. The capacitance $C_{5}$ is kept small so as to present a high reactance to the fundamental, else the fundamental would be entirely bypassed around the crystal circuit.
1-326. The circuit shown in figure 1-136 (G) is something of a novelty in that a Pierce instead of a Miller oscillator is employed to directly excite the power amplifier of a small transmitter. The $\mathrm{L}_{1} \mathrm{C}_{4}$ arm is a neutralizing circuit which prevents the amplitude-modulated output stage from varying the effective impedance of the oscillator load. Normally, neutralizing networks are not necessary for crystal oscillators. Only when the oscillators drive power amplifiers directly is feed-back neutralization advisable. Even then, if the power amplifier is not modulated and performs as a frequency multiplier, neutralization is not necessary.
1-327. The electron-coupled converter circuits shown in figure 1-138 embody more or less the same features previously discussed. The basic methods illustrated for obtaining a heterodyne output are more or less self-explanatory, and will not be elaborated upon here.

## The Miller Oscillater

1-328. The Miller oscillator is the crystal equivalent of a Hartley oscillator in which no mutual inductance exists between the plate-to-cathode and grid-to-cathode inductances. ( See figure 1-140.) The Miller oscillator has an average frequency deviation of approximately 1.5 times that of the Pierce circuit. The plate circuit must appear inductive in order that the correct phase shift will be produced in $\mathrm{E}_{\mathrm{p}}$ the plate r-f voltage, to compensate for the


Figure 1-140. Diagrams illustrating the equivalence aetween the Miller circult and the Hartley circuit
resistance in the feed-back arm, since this resistance prevents the necessary 180 -degree phase rotation of the equivalent generator voltage of the amplifier from occurring entirely in the feed-back circuit. The effective load capacitance into which the crystal unit operates is, approximately,

$$
\begin{align*}
C_{x}= & C_{k}+\frac{1}{\omega}\left(\frac{1}{Z_{p z}-Z_{p}}\right) \\
& =C_{z}+\frac{C_{p s}}{1-\omega^{2} L_{p} C_{p z}} \tag{1}
\end{align*}
$$

where $\mathrm{Z}_{\mathrm{pg}}$ and $\mathrm{Z}_{\mathrm{p}}$ are both considered as unsigned magnitudes, and the various symbols correspond to those in figure 1-140. Since the load capacitance is a function of the frequency, a Miller oscillator cannot be operated at more than one frequency and still present the same load capacitance to each crystal unit except by providing for an adjustment of the circuit parameters. In spite of its greater frequency instability and lack of circuit simplicity as compared with the Pierce circuit, the Miller design is the one most widely used in crystal oscillators. The reason for this popularity is the greater output that can be obtained for the same crystal drive level. In either the Pierce or the Miller basic circuit, the output cannot exceed the voltage across $\mathrm{Z}_{\mathrm{pg}}$, the largest single impedance in the plate tank circuit. In the Pierce circuit, the maximum voltage is thus the maximum permissible across the crystal anit; in the Miller circuit the maximum voltage is $(\mathrm{k}+1)$ times the maximum permissible voltage across the crystal unit, where $k$ is the gain of the stage, equal to $\mathrm{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{g}}$. This gain, theoretically (not practically), can approach the mu of the tube as a limit when the load impedance, $\mathrm{Z}_{\mathrm{L}}$, is large compared with $\mathrm{R}_{\mathrm{p}}$. Thus, the use of a Miller circuit permits a saving of one amplifier stage.
1-329. The feed-back capacitance of the Miller circuit is, normally, simply the plate-to-grid interelectrode capacitance of the tube. It cannot, of course, be less than this unless an inductive shunt is connected between the plate and grid. When a pentode is used, it is usualiy necessary to insert a small feed-back capacitance on the order of a few micromicrofarads. The waveform in the output is improved by the use of a tuned tank circuit having a low $L / C$ ratio in place of $L_{p}$. The plate tank must be tuned to a frequency above the oscillator frequency, in order that the tank impedance will appear inductive. Such an arrangement also ensures a large effective $L_{\mathrm{p}}$ of high $\mathbf{Q}$. A variable capacitance in the plate tank facilitates adjustments to obtain the correct load capacitance for the crystal unit.

## MILLER-OSCILLATOR DESIGN CONSIDERATIONS

1-330. If it is decided to employ a Miller oscillator as a frequency generator, the choice should be dictated by the need of a greater output than can be obtained with a Pierce oscillator. An exception to this rule might be made if a tri-tet circuit is contemplated, in which case, the large capacitance that will directly shunt the Pierce-connected crystal may well prevent the stability from being as high as that of the Miller tri-tet circuit. The Miller circuit is the more critical to design insofar as maintaining the correct load capacitance is concerned, but the basic approach to the problem is the same as that which was followed in analyzing the equilibrium state of the Pierce circuit. Both oscillators are represented by the same basic circuit, shown in figure 1-119. We shall not repeat the steps involved in the derivation of the equilibrium equations in the particular case of the Miller oscillator. The basic equations given in the following paragraphs can be used as points of departure in the design of any Miller circuit. Also, by methods similar to those employed in the analysis of the Pierce circuit, the design limitations of a Miller oscillator in which the crystal unit is to be operated within specifications can be predetermined, approximately.

## MILLER-OSCILLATOR EQUATION OF STATE

1-331. As in the case of the Pierce circuit, there are two equations that express the state of oscillation equilibrium in the Miller circuit. Originally derived by Koga, these two equations are the real and the imaginary parts of the general equation:

$$
\begin{equation*}
-\frac{\mu Z_{v} Z_{g}}{R_{v} Z_{s}+Z_{p}\left(Z_{s}+Z_{p g}\right)}=1 \tag{1}
\end{equation*}
$$

where

$$
\mathrm{Z}_{\mathrm{s}}=\mathrm{Z}_{\mathrm{g}}+\mathrm{Z}_{\mathrm{p}}+\mathrm{Z}_{\mathrm{p}}
$$

and

$$
Z_{\mathrm{g}}=\mathrm{R}_{\mathrm{ce}}+j \mathrm{X}_{\mathrm{g}} ; \quad \mathrm{Z}_{\mathrm{p}}=j \mathrm{X}_{\mathrm{p}} ; \quad \mathrm{Z}_{\mathrm{pz}}=j \mathrm{X}_{\mathrm{pe}}
$$

$\mathrm{R}_{\mathrm{cg}}$ is the effective resistance of the grid circuit, accounting for both the crystal and gridleak losses. The losses in the plate circuit are assumed to be negligible. On solving equation (1), the real part can be expressed as

$$
\begin{equation*}
-R_{p}=\frac{X_{p}\left[Z_{\varepsilon}{ }^{2}(\mu+1)+X_{\varepsilon} X_{\mathrm{pq}}\right]}{R_{\mathrm{oz}}\left(\mathrm{X}_{\mathrm{p}}+\mathrm{X}_{\mathrm{p}}\right)} \tag{2}
\end{equation*}
$$

Section 1

Equation (2) defines the conditions that exist when the feedback power input equals the power dissipated in the grid circuit. The imaginary part of the equation (1) defines the frequency, or, more exactly, the impedance relations that must exist if the feedback is to be of proper phase. This is given as

$$
\begin{equation*}
\mathbf{X}_{*}=\frac{\mathbf{X}_{\mathrm{p}}, \mathbf{X}_{\mathrm{pg}}-\mathbf{R}_{\mathrm{ck}} \mathbf{R}_{\mathrm{p}}}{\mathbf{R}_{\mathrm{p}} \mathbf{Q}_{\mathrm{s}}} \tag{3}
\end{equation*}
$$

Where $Q_{p}$ is equal to $X_{n} / R_{v g}$, and $X_{k}=X_{p}+X_{n}+$ $X_{\text {pr }}$. Equation (1) is the same as equation $1-289$ (1) except that the terms are rearranged and $\mu$ is substituted for the product $\mathrm{R}_{\mathrm{p}} \mathrm{g}_{\mathrm{m}}$. Equations (2) and (3) correspond to equations 1-289 (2) and (3), respectively. If it is assumed that $Z_{k} \approx X_{k}$ and that $\left(X_{1}+X_{1 k g}\right) \approx-X_{k}$, equation (2) above can be simplified, thus:

$$
\begin{equation*}
\mathbf{R}_{\mathrm{p}}=\frac{\mathbf{X}_{\mathrm{p}}\left[\mathbf{X}_{\mathrm{g}}(\mu+\mathbf{1})+\mathbf{X}_{\mathrm{vg}}\right]}{\mathbf{R}_{\mathrm{ca}}} \tag{4}
\end{equation*}
$$

Remember that $X_{1}$, and $X_{k}$ are positive, and that $X_{w, e}$ is negative. When equation (3) is rearranged as follows

$$
X_{k}+X_{p}+R_{c g} / Q_{\mathrm{g}}-\frac{X_{p} X_{p g}}{R_{p} Q_{\mathrm{k}}}=-X_{p g}
$$

$$
\begin{equation*}
1-331 \tag{5}
\end{equation*}
$$

it can be seen that the effect of the tube $R_{p}$ on the frequency is a function of the term $\left(\frac{X_{p} X_{p l}}{R_{p} Q_{s}}\right)$ only. LOAD CAPACITANCE OF CRYSTAL UNIT IN MILLER OSCILLATOR
1-332. The load capacitance into which the crystal unit operates in a Miller circuit has been derived by Koga to be

$$
C_{x}=C_{k}+C_{p x}+C_{v}
$$

where $C_{k}$ and $C_{w g}$ are as represented in figure 1-140, and

$$
\begin{equation*}
C_{v}=\frac{\mu C_{p k}}{1+R_{p}^{2} / X_{p}^{2}} \tag{2}
\end{equation*}
$$

It appears that equation (2) gives a value to $C_{v}$ that, for a Miller oscillator operated at the rated load capacitance of the crystal unit, is probably between three and four times too small for the average circuit. Equation (2) is derived from equation 1-331 (1), beginning by expressing the
latter equation in the following form:

$$
\begin{aligned}
& \frac{1}{\mathrm{Z}_{\mathrm{k}}}+\frac{1}{\mathrm{Z}_{1 *}}+\frac{\mu}{\mathrm{Z}_{1 \mathrm{k}}\left(1+\mathrm{R}_{\mathrm{p}} / \mathrm{Z}_{p}+\frac{\mathrm{R}_{\mathrm{p}}}{\mathrm{Z}_{\mathrm{k}}+\mathrm{Z}_{\mu \mathrm{g}}}\right)}=0 \\
& \text { 1-332 (3) }
\end{aligned}
$$

It is next assumed that the term in parentheses

$$
\begin{equation*}
1+R_{p} / Z_{p}+\frac{R_{p}}{Z_{k}+Z_{p s}}=1+R_{p} / Z_{p} \tag{4}
\end{equation*}
$$

Such an assumption not only implies that the reedback current is negligible compared with the r-f current through the plate coil, $\mathrm{L}_{1}$, but that the feed-back impedance is so high relative to $R_{p}$ that $R_{1} /\left(Z_{s}+Z_{14}\right)$ is negligible compared with 1 . The former implication requires that $\mathcal{Z}_{t}$, the effective load impedance across the tube, be approximately equal to $j X_{11}$; the latter implication requires that $\mathbf{X}_{1 v e}-\left|\mathbf{X}_{\mathrm{k}}\right| \gg \mathbf{R}_{\mathrm{p}}$. If the effective phase-determining $Q_{\text {s }}$ of the feed-back circuit is 10 or more, as is very likely to be the case when standard crystal units are operating at their rated local load capacitance and $\mathrm{C}_{\mathrm{y}}$ is not excessive, then $\mathrm{E}_{\mathrm{p}}$ must be very nearly in phase with $-\mu \mathrm{E}_{\mathrm{g}}$. Such a condition cannot exist simultaneously with equation (4) unless $R_{p} \ll X_{n}$-an operating state that would be very undesirable from the point of view of frequency stability. If $R_{p}$, is to have a reasonable value at the rated load capacitance of the crystal unit, the impedance of the feed-back arm cannot be greatly different from that of the plate circuit. Equation (4) would be sufficiently accurate for very low values of $Q_{R}$ and very large transconductances for the tube; however, it would seem that for crystal units that are to be operated well above series resonance, the approximation of equation (4) should not be made. In this case

$$
1+R_{p} / Z_{p}+\frac{R_{p}}{Z_{\mathrm{g}}+Z_{p \mathrm{p}}}=1+\mathrm{R}_{\mathrm{p}} / Z_{\mathrm{L}}
$$

and $Z_{1}$, approaches $X_{\mathrm{H}^{2}} / \mathrm{R}_{\mathrm{rg}}$ as $\mathrm{R}_{\mathrm{p}}$ and $\mathrm{Q}_{\mathrm{g}}$ increase. Since $Z_{1 .}$ as used above, represents an involved complex quantity, an exact expression of equation (2) will not be attempted here. As can be seen from equation $1-331$ (5), if $1 / Q_{p}$ and $X_{p} / R_{p}$ are each on order of $1 / 10$ or smaller, $X_{k}+X_{1} \approx\left|X_{p r}\right|$. On the other hand, if $X_{p} / R_{1}$ is not small, the variable parameters of the vacuum tube and the variations to be expected in the effective resistance from
one crystal unit to another will have such a large influence upon the effective load capacitance that there can never be an assurance that a crystal chosen at random will be operated according to specifications. In other words, a Miller oscillator cannot be designed to provide approximately a specified load capacitance unless $X_{R}+X_{11} \approx\left|X_{19}\right|$. Under these conditions

$$
\mathrm{C}_{\mathrm{x}}=\mathrm{C}_{\mathrm{k}}+\frac{1}{\omega\left(\frac{1}{\omega \mathrm{C}_{1 \mathrm{p}}}-\omega \mathrm{L}_{\mathrm{L}}\right)}=\mathrm{C}_{\mathrm{k}}+\mathrm{C}_{\mathrm{p} \mathrm{k}}+\mathrm{C}_{\mathrm{x} p}
$$

$$
1-332 \text { (6) }
$$

where

$$
\begin{equation*}
C_{X p}=C_{p R}\left(\frac{-X_{p}}{X_{p R}+X_{p}}\right) \tag{7}
\end{equation*}
$$

It must be understood that equations (6) and (7) assume that $R_{11}$ is large compared with $X_{1,1}$ and that $\mathrm{X}_{\mathrm{g}}$ is large compared with $\mathrm{R}_{\mathrm{ck}}$. For this latter condition to hold, the grid-to-cathode capacitance, $\mathrm{C}_{8}$, must be kept as small as possible. If the assumptions above cannot be made, it is not feasible to expect a Miller oscillator to operate at approximately the same load capacitance for all crystal units, nor can good frequency stability be expected. A more comprehensive capacitance equation for the Miller circuit-one that holds approximately for all operating conditions - can be expressed as

$$
\begin{equation*}
C_{x}=C_{k}+C_{p k}+C_{X_{p}}^{\prime} \tag{8}
\end{equation*}
$$

where $\mathrm{C}_{\mathrm{x}}$, is given by equation (7), except that $X_{p}$ is replaced by $X_{n}$, where

$$
\begin{equation*}
X_{p}^{\prime}=X_{p}+R_{c \mathrm{~g}} / Q_{\mathrm{g}}-\frac{X_{\mathrm{p}} X_{\mathrm{pg}}}{R_{\mathrm{p}} \mathrm{Q}_{\mathrm{k}}} \tag{9}
\end{equation*}
$$

It will be seen that $X_{1}$ ' has been so chosen that equation 1-331 (5) can be expressed in the form

$$
\mathrm{X}_{\mathrm{g}}+\mathrm{X}_{\mathrm{p}}^{\prime}+\mathrm{X}_{\mathrm{pk}}=0 \quad 1-332(10)
$$

In the event that the plate circuit contains a capacitance shunting the coil, equations (6) and (7) still hold except that $\mathrm{X}_{\mathrm{p}}$ refers to the total parallel reactance in the $L_{p} C_{v}$, branches.

## MAXIMUM $R_{p}$ OF MILLER OSCILLATOR TUBE UNDER GIVEN LOAD CONDITIONS

1-333. Referring to figure $1-141, R_{o}$ and $R_{\text {re }}$ are defined as follows:

$$
\begin{equation*}
R_{o}=E_{\mathrm{p}}{ }^{2} / \mathrm{P}_{\mathrm{o}} \tag{1}
\end{equation*}
$$

where $P_{0}$ is the power dissipated in the output circuit, and

$$
\begin{equation*}
\mathrm{R}_{\mathrm{Re}}=\mathrm{E}_{\mathrm{z}}^{2} / \mathrm{P}_{\mathrm{x}} \tag{2}
\end{equation*}
$$

where $P_{z}$ is the power dissipated in the grid circuit. If the gridleak losses are negligible, $\mathrm{P}_{\boldsymbol{k}}$ equals the crystal power and $\mathrm{R}_{\mathrm{k}}$ equals the PI of the crystal unit. As can be seen from the equations in figure 1-141, either PI must be small or $R_{k}$ very large for this assumption to hold. With $\mathrm{R}_{\mathrm{p}}$ large compared with $Z_{1,}, I_{1}$, is approximately equal to $\mathbf{g}_{\mathrm{m}} \mathrm{E}_{\mathrm{k}}$. We shall assume that $\mathrm{X}_{\mathrm{n}}=\mathrm{X}_{\mathrm{k}}+\mathrm{X}_{\mathrm{p}}+\mathrm{X}_{\mathrm{ix}}$ $\approx 0$. Under these conditions it can be shown quite simply that in the circuit of figure 1-141, letting $\mathrm{k}=\mathrm{E}_{\mathrm{n}} / \mathrm{E}_{\mathrm{k}}$,

$$
\begin{equation*}
g_{m}=\frac{k^{2} R_{k e}+R_{o}}{k R_{g e} R_{o}} \tag{3}
\end{equation*}
$$

For a given $R_{\mathrm{Kc}}$ and $\mathrm{R}_{\mathrm{o}}$, equation (3) has a minimum $g_{m}$ when

$$
\begin{equation*}
\mathbf{k}^{2}=\mathbf{R}_{0} / \mathbf{R}_{\mathbf{k e}} \tag{4}
\end{equation*}
$$

Since a maximum $R_{p}$, coincides with a minimum $\mathrm{g}_{\mathrm{m}}$, equation (4) also establishes the conditions for a maximum $\mathrm{R}_{\mathrm{p}}$. Now, $\mathrm{R}_{\mathrm{kr}}$ is a function of $\mathrm{R}_{\mathrm{e}}$ of the crystal unit, so that a circuit design using equation (4) should be based on a most probable value of $R_{g}$. (i.e., a most probable value of $R_{e}$ ), which will usually correspond to a value of $\mathrm{R}_{\mathrm{e}}$ between one-third and one-fourth of the maximum $\mathrm{R}_{\mathrm{c}}$. Equation (4) should not be interpreted to mean that if $\mathrm{R}_{0} / \mathrm{R}_{\mathrm{gr}}$ is adjusted to equal a fixed value of $\mathrm{k}^{2}$, the $\mathrm{g}_{\mathrm{n}}$ of the tube will therefore be a minimum relative to its values for other $R_{o} / R_{k e}$ ratios. Such an interpretation would only hold true if the product $R_{v} R_{x c}$ were constant. Where equation (4) holds, it can be shown that the ratio of output power to crystal power is

$$
\begin{equation*}
P_{o} / P_{g}=1 \tag{5}
\end{equation*}
$$

## OPTIMUM VALUE OF $k=E_{p} / E_{\text {; }}$ FOR MILLER OSCILLATOR

1-334. Practical values of $k$, unless a pentode is used, are limited by the plate-to-grid and grid-tocathode interelectrode capacitances of the tube and the specified load capacitance of the crystal unit. If $X_{s}=X_{z}+X_{p}+X_{v s} \approx 0$, then

$$
\begin{equation*}
X_{p}=k X_{k} \tag{1}
\end{equation*}
$$

and

$$
\begin{equation*}
-X_{p z}=(k+1) X_{z} \tag{2}
\end{equation*}
$$


(A)
(1) R'g $=\frac{E_{q}^{z}}{\operatorname{LOSSES} \mathrm{~N}_{\mathrm{N}} \mathrm{R}_{\theta}}$
(2) R'g mads (without R-F CMOKE)
(3) R'g $\approx \operatorname{sq}_{q} / 2$ (witM R-F CHOKE)
(4) Pig = Mq iwithcut gridleak action)

(8)

Figure 1-141. Equivalent circuit of Miller oscillator. $R_{p}$ is assumed to be large compared with the fotal load impodance. $R_{n}$ is an equivalent resistance accounting for the output losses. $R_{g r}$ is an equivalent resistance accounting for the cryatal and grid losses; it is approximately equal to the resistance of the parallel circuit shown in (B). PI is the performance index of the crystal unit; $R_{t}{ }^{\prime}$ is the equivalent grid resistance; and $R_{y}$ is the actual gridleak resistance

By equation (2)

$$
k=\frac{-\left(X_{p k}+X_{k}\right)}{X_{k}}=\frac{C_{x}-C_{g}-C_{p \mathrm{p}}}{C_{\mathrm{p}}}
$$

$$
\begin{equation*}
1-334 \tag{3}
\end{equation*}
$$

where

$$
X_{k}=\frac{1}{\omega\left(C_{x}-C_{g}\right)}, X_{p k}=-1 / \omega C_{p k}
$$

$\mathrm{C}_{\mathrm{x}}=$ rated load capacitance, and $\mathrm{C}_{\mathrm{k}}=$ grid-tocathode capacitance. With triodes, values of $k$ above 4 or 5 are difficult to obtain. If the oscillator is to be designed with no other feedback-circuit capacitances than those provided by the interelectrode capacitances, $\mathrm{C}_{\mathrm{p}:}$ and $\mathrm{C}_{k}$, of the tube, it can be assumed that $k$ is a fixed parameter equal to the value given by equation (3). The output arm must thus be designed to provide a reactance, $X_{p} \approx k X_{k}$, if the crystal unit is to operate into its rated load capacitance.
1-335. From the point of view of frequency stability it is desired that the term ( $\left.X_{11} X_{14} / R_{1} Q_{R}\right)$ in equation $1-331$ (5) be as small as possible relative to $\left(\mathbf{X}_{\mathrm{q}}+\mathbf{X}_{\mathrm{n}}\right)$, or, equivalently, to $\left|\mathbf{X}_{\mathrm{pg}}\right|$. In other words,

$$
\mathbf{X}_{\mathrm{pz}} / \frac{\mathbf{X}_{\mathrm{p}} \mathbf{X}_{\mathrm{pR}}}{\mathbf{R}_{\mathrm{p}} \mathbf{Q}_{\mathrm{g}}}=\mathrm{R}_{\mathrm{p}} / \mathrm{k} \mathrm{R}_{\mathrm{ek}}
$$

should be a maximum. With equation 1-331 (4), it can be shown that

$$
\mathrm{R}_{\mathrm{p}} / \mathrm{k}=\mathrm{Q}_{\mathrm{g}} \mathrm{X}_{\mathrm{K}}(\mu-1)
$$

Equation (1) indicates that as the fraction of the loop reactance ( $k R_{r q} / R_{p}$ ) dependent upon $R_{p}$ becomes smaller, the effective amplification factor of the tube becomes greater. Intuitively from equation (1) it can be seen that with $Q_{F} X_{k}$ constant for a given vacuum tube and plate voltage, $\mathrm{E}_{\mathrm{l}}, \mathrm{R}_{\mathrm{p}}$ must increase as $k$ is made larger, otherwise $\mu$ could not decrease. Nevertheless, the larger that $k$ becomes the smaller the value of $R_{p} / k$. If $k=1$, a frequency stability almost approaching that of the Pierce circuit can be achieved, but with twice the output voltage. Lower values of $k$ would soon detune the oscillating tank to a point where the simplifying assumptions made regarding $k$ would no longer hold.
1-336. Since the principal purpose of using a Miller instead of a Pierce circuit is to eliminate an amplifier stage, and since $E_{k}$ is limited to the maximum voltage that can be placed across the crystal unit, the ratio $\mathrm{E}_{\mathrm{p}} / \mathrm{E}_{\mathrm{k}}=\mathrm{k}$ can be chosen to give a desired gain over that which would be $0^{h}$ tained with a Pierce oscillator operating at the same crystal drive level. $E_{k}$ in the Miller circuit can be assumed to be twice the $E_{\mathrm{c}}$ of a Pierce circuit that
has a $k=1$. If an imaginary gain of 10 is desired, $k$ for the Miller circuit should be equal to 5 . For k to be 5 , according to equation 1-334 (3)

$$
\mathrm{C}_{\mathrm{pk}}=\left(\mathrm{C}_{\mathrm{x}}-\mathrm{C}_{\mathrm{k}}\right) / 6
$$

If $\mathrm{C}_{\mathrm{x}}=32 \mu \mu \mathrm{f}$ and $\mathrm{C}_{\mathrm{k}}=8 \mu \mu \mathrm{f}, \mathrm{C}_{\mathrm{vF}}$ must be $4 \mu \mu \mathrm{f}$, which is a value quite representative of the average triode amplifier, or which could be obtained with a pentode by using a small external plate-togrid capacitance. Equation 1-335 (1) can be rewritten in the form

$$
\begin{equation*}
1 / R_{p}=g_{m}-R_{c k} / k X_{k}^{2} \tag{1}
\end{equation*}
$$

For $k=5$, the value of $1 / R_{1,}$, and hence the percentage effect of $R_{v}$ on the loop reactance, will be a minimum the more nearly that $\mathrm{g}_{\mathrm{m}}$ can be made to approach in value $\mathrm{R}_{\mathrm{cu}} / \mathrm{kX}_{\mathrm{k}}{ }^{2}=\mathrm{R}_{\mathrm{vz}} / 5 \mathrm{X}_{\mathrm{k}}{ }^{2}$. If the effective $Q$ of the crystal unit, $Q_{e}=\frac{X_{r}}{R_{r}}$, is equal to 10 or more and if the gridleak losses are negligible, it can be shown that

$$
\begin{equation*}
\mathrm{R}_{\mathrm{eg}}=\frac{\mathrm{R}_{\mathrm{e}} \mathrm{X}_{\mathrm{CR}^{2}}{ }^{2}}{\left(\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{CR}}\right)^{2}} \tag{2}
\end{equation*}
$$

and that

$$
\begin{equation*}
\mathrm{X}_{\mathrm{g}}=\frac{\mathrm{X}_{\mathrm{e}} \mathrm{X}_{\mathrm{CR}}}{\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{C}_{\mathrm{R}}}} \tag{3}
\end{equation*}
$$

Thus,

$$
Q_{\mathrm{r}}=\mathrm{X}_{\mathrm{g}} / \mathrm{R}_{\mathrm{cg}}=\frac{\mathrm{X}_{\mathrm{e}}\left(\mathrm{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{C}_{\mathrm{k}}}\right)}{\mathrm{R}_{\mathrm{e}} \mathrm{X}_{\mathrm{C}_{\mathrm{R}}}}
$$

and

$$
\mathrm{X}_{\mathrm{k}}^{2} / \mathrm{R}_{\mathrm{ck}}=\mathrm{X}_{\mathrm{e}}^{2} / \mathrm{R}_{\mathrm{e}}=\mathrm{PI}
$$

where PI is the performance index of the crystal unit. If it is further assumed that the output losses are negligible, the impedance of the crystal tank is

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{L}}=\frac{\mathrm{X}_{\mathrm{p}}{ }^{2}}{\mathrm{R}_{\mathrm{cz}}}=\frac{\mathrm{k}^{2} \mathrm{X}_{\mathrm{k}}{ }^{2}}{\mathrm{R}_{\mathrm{cz}}}=\mathrm{k}^{2} \mathrm{PI} \tag{6}
\end{equation*}
$$

Equation (1) can thus be written

$$
\begin{equation*}
\frac{1}{R_{\mathrm{p}}}=\mathrm{g}_{\mathrm{m}}-\frac{1}{\mathrm{kPI}}=\mathrm{g}_{\mathrm{m}}-\frac{\mathrm{k}}{\mathrm{Z}_{\mathrm{L}}} \tag{7}
\end{equation*}
$$

If $k$ is fixed by output considerations, the percentage effect of $R_{p}$ upon the loop reactance becomes a function of $\mathrm{F}_{\mathrm{p}}$, alone, being a minimum when $R_{V}$ is a maximum. If $R_{l}$ is increased without limit, $\mathrm{g}_{\mathrm{m}}$ approaches $\mathrm{k} / \mathrm{Z}_{\mathrm{k}}$, as a limit, and the greater the PI, the larger will $R_{i}$, become. In the case
of the Pierce oscillator, it will be recalled that a maximum $R_{v}$ was obtained by a proper choice of k . This optimum k was the one that provided the maximum excitation voltage. In the Miller circuit, the excitation is the voltage developed across the crystal unit, and thus is limited by the crystal specifications regardless of the value of $k$. The smaller that $k$ is made, the smaller will be the effective $\mathrm{R}_{\mathrm{p}}$, but, even so, the percentage effect of $R_{p}$ upon the effective loop reactance will also be smaller. With k fixed by the requirement to eliminate an amplifier stage, the problem of obtaining a maximum $R$, becomes one of keeping the load requirements to a minimum, selecting the vacuum tube, determining the proper operating voltages consistent with the crystal specifications, designing a test model accordingly, and experimenting for optimum results over the resistance range to be expected in the crystal units.

## operating conditions of miller oSCILLATOR PROVIDING MAXIMUM $R_{p}$ FOR GIVEN $g_{m}$.

$1-337$. If the bias of a tube is supplied by agc, the excitation voltage is small by comparison, so that the operating point of the tube can be theoretically estimated by consulting the $R_{p}$ and $g_{m}$ curves plotted against grid voltage. The operating bias for a given plate voltage would approximately be that giving values of $\mathrm{R}_{\mathrm{s}}$ and $\mathrm{g}_{\mathrm{w}}$ that obey equation 1-336 (7). Unfortunately, there are no curves available that indicate the effective $R_{1}$ and $g_{\mathrm{g}}$ for large excitation voltages where the tube is cut off a large fraction of each cycle. Nor has a theoretical basis been established for estimating the probable rates of change in $\mathrm{K}_{1}$, and $\mathrm{g}_{\mathrm{m}}$, as the excitation is increased under various circuit conditions. If time permits, experiments designed to furnish such data may gain for the engineer a valuable insight into the characteristics of his design models. Most probably the "dynamic" curves of $\mathbf{R}_{\mathrm{p}}$, and $\mathrm{g}_{\mathrm{m}}$ will correspond closely to the static curves. Yet the possibility exists that significant differences in the rates of change in the tube parameters may be discovered under certain operating conditions. In equation $1-336$ (7) it can be seen that for any large value of $\mathrm{R}_{\mathrm{p}}, \mathrm{g}_{\ldots,}$ very nearly equals $\mathrm{k} / \mathrm{Z}_{1}$. For example, if $R_{y}=0.5$ megohm, the difference between $g_{m}$ and $k / Z_{11}$ is only 2 micromhos. An $R_{n}$ of 1 megohm corresponds to practically the same value of $\mathrm{g}_{\mathrm{m}}$, , the difference being only on the order of 1 micromho. Thus, when $R_{w}$ is large, $g_{w}$ can be considered more or less a circuit constant. During the time that the tube is cut off, $R_{k}$, is infinite and $g_{\text {., }}$
is zero. From the point of view of a large effective $R_{p}$ it is desirable that the cutoff angle be a maximum. The larger the $g_{m}$ of the tube above cutoff, the greater can be the cutoff angle. A sharp-cutoff tube would be preferred for this purpose. It is also desirable to have $R_{1}$, as high as possible above cutoff. For this purpose, a high-mu tube is to be preferred. A theoretical estimate of the optimum relation between the values of $\mathbf{R}_{p}$ and $g_{m}$, for a tube of the same class-A mu, that provides a maximum over-all effective $R_{p}$ cannot be attempted here. However, it would seem that the emphasis should be placed upon the larger $g_{m} / R_{p}$ ratio. The effective $R_{p}$ of a pentode can always be increased artificially by inserting a high resistance in the plate circuit in series with the oscillating tank, as illustrated in figure 1-142. In testing a given tube for those bias and excitation conditions which provide a maximum $R_{11}$, it may be preferable to control the bias independently of the oscillations, or by using an adjustable, r-f-bypassed cathode resistor. A crystal unit should be employed having parameters known to remain constant over the experimental drive-level range. After the tube has warmed up, if the cathode bias is used, the cathode resistance can be decreased until oscillations begin. The cathode resistance can then be increased until the frequency is a maximum. The maximum frequency would be an indication of an equilibrium point of maximum $R_{1}$. In order for oscillations to be maintained in the event that all the bias is developed across the cathode resistance and the excitation is insufficient to drive the grid positive, a
small percentage decrease in the excitation amplitude must cause at least an equal percentage decrease in the average plate current, and hence in the bias. Such operation will require that the tube be cut off for a large fraction of each cycle. An adjustable cathode resistance cannot be considered a particularly practical design feature, but it may prove advantageous in an experimental circuit for finding the operating conditions that provide a maximum $\mathrm{R}_{\mathrm{p}}$ for a given $\mathrm{g}_{\mathrm{m}}$.

## FREQUENCY-STABILITY EQUATIONS FOR MILLER CIRCUIT

1-338. Regardless of whether the circuit conditions are such that the effective load capacitance of the crystal unit is assumed to be given by equation 1-332 (1), by equation 1-332 (6), or by equation 1-332 (8), the fractional change in frequency for a small change in any one of the equivalent component capacitances is given by the general equation

$$
\begin{equation*}
\frac{d f}{f}=-\frac{1}{F_{X e}} \cdot \frac{d C_{x}}{C_{x}} \tag{1}
\end{equation*}
$$

where $\mathrm{dC}_{\mathrm{x}}$ is equal to $\mathrm{dC}_{\mathrm{g}}, \mathrm{dC}_{\mathrm{p}, \mathrm{r}}, \mathrm{dC}_{\mathrm{x}}, \mathrm{dC}_{\mathrm{Xp}}$, or $\mathrm{dC}_{\mathrm{X}_{1}}$, and represents an incremental change in any of the component capacitances, and $F_{X r}$ is the frequencystability coefficient of the crystal unit, equal to $2 \mathrm{C}_{4}{ }^{2} / \mathrm{CC}_{\mathrm{x}}$. (See equation 1-243(1).) If a tuning capacitor, $C_{1}$ is connected across $L_{4}$ in the plate circuit, and if equations $1-332$ (1) and (2) are assumed approximately correct, it can be shown


Figure 1-142. The large resistonce, $R_{n}{ }^{\prime}$, connected in plate circuit effectively increases $R_{n}$ of the tube. This method can be used to improve the frequency stability of a Miller oscillator employing a sereen-grid tube and an externally connected feed-back capacitance, $\mathbf{C}_{p, \prime}{ }^{\prime}$
that for variations in $\mathrm{C}_{\mathrm{y}}$,

$$
\begin{array}{r}
\frac{d f}{f}=-\frac{C_{p g}}{C_{\mathrm{x}}} \cdot \frac{2 \mu \omega \mathrm{C}_{\mathrm{p}} \mathrm{R}_{\mathrm{p}}{ }^{2}}{\mathrm{~F}_{\mathrm{Xe}} \mathrm{X}_{\mathrm{p}}\left(1+\mathrm{R}_{\mathrm{p}}{ }^{2} / \mathrm{X}_{\mathrm{p}}{ }^{2}\right)} \cdot \frac{\mathrm{dC}_{\mathrm{p}}}{\mathrm{C}_{\mathrm{p}}} \\
1-338(2)
\end{array}
$$

where $\omega=$ angular frequency. If the circuit is operating at maximum activity, in which case $\mathrm{Z}_{\mathrm{L}} \approx \mathrm{X}_{\mathrm{p}}=\mathrm{R}_{\mathrm{v}}$, equation (2) becomes

$$
\begin{equation*}
\frac{d f}{f}=-\frac{C_{p q}}{C_{x}} \cdot \frac{\mu R_{p} \omega C_{p}}{2 F_{x e}} \cdot \frac{d C_{p}}{C_{p}} \tag{3}
\end{equation*}
$$

Where equations 1-332 (6) and (7) can be assumed to be approximately correct, it can be shown that a fractional change in the plate reactance, $X_{p}$, causes a fractional frequency deviation of

$$
\begin{equation*}
\frac{d f}{f}=-\frac{\left(C_{x}-C_{p p}\right) d X_{p}}{C_{p g} F_{X e} X_{p}} \tag{4}
\end{equation*}
$$

If no tuning capacitor is provided to shunt the plate coil $\mathrm{L}_{\mathrm{p}}$, equation (4) can be expressed in terms of a fractional change in $L_{p}$, thus:

$$
\begin{equation*}
\frac{d f}{f}=-\frac{\left(C_{x}-C_{p x}\right) d L_{p}}{C_{p x} F_{x e} L_{p}} \tag{5}
\end{equation*}
$$

If desired, equations indicating the frequency stability when other parameters are varied can be derived by following a procedure similar to that employed in the analysis of the Pierce circuit.
miller circuit as a small POWER OSCILLATOR
1-339. The ratio of the output power to the input power is given by the equation

$$
P_{o} / P_{\mathrm{g}}=\mathrm{k}^{2} \mathrm{R}_{\mathrm{ke}} / \mathrm{R}_{\mathrm{o}}
$$

where $k=E_{v} / E_{k}$, and $R_{k r}$ and $R_{0}$ are the resistances represented in figure 1-141. In practice, ratios of $R_{k,}$ to $R_{c}$ can be obtained on the order of 4 for crystal units of maximum effective resistance. If $\mathrm{k}=5$, this would mean a power ratio of 100 . A $10-\mathrm{mw}$ crystal unit could thus be used to develop a 1-watt output. Much higher power outputs, of course, can be obtained with crystal units of small values of $R_{c}$ or of higher power ratings. It cannot be recomended that a crystal be driven beyond its rated power level, but if an exception should ever arise, the Miller circuit will require the least overdrive. If a larger drive level is necessary than can be obtained with Military Standard crystal units,
the cognizant military agency should first be consulted. It may be that one or more of the crystal manufacturers has available a nonstandard crystal unit with crystal dimensions and mounting sufficient to withstand the required drive-perhaps by operating with an overtone mode - without the risk of significant parameter variations. As a final resort, it will be found that most of the Military Standard crystal units can withstand, without shattering, drive levels from 10 to more than 20 times the rated drive. If need be, power outputs greater than 35 watts can be obtained with the Miller circuit, using a beam power tube or a power pentode. It is much easier to obtain a large output from a high-mu than from a low-mu tube for the same crystal drive. Also, it is easier to obtain a large output from, say, a 50 -watt tube operated at low efficiency, than from a smaller tube operated at high efficiency. An r-f choke must be used in the grid circuit if large output is to be developed. Furthermore, fixed bias that is sufficient to prevent the grid from drawing current must be used, so as to reduce the grid losses to a minimum. The voltage gain of the oscillator, $k=E_{p} / \mathrm{E}_{\mathrm{g}}$, should be as high as possible. With proper design, except that the crystal unit is operating at tolerances greater than those specified for low drive levels, the Miller circuit can be made to drive a power arnplifier of 300 watts or more. Some crystal units can withstand as much as 120 ma r-f current and still be within the safe-operating range as far as shattering is concerned. A pressure-mounted unit is generally to be preferred at high drive levels, because of the added protection it offers, and because its greater thermal conductivity permits the generated heat to escape more rapidly. For maximum output, the oscillator must operate into an impedance matching the $R_{p}$ of the tube. If a Miller oscillator is to drive a power amplifier, great care must be taken in neutralizing the feedback from the amplifier, or the crystal may easily be overdriven to the point of shattering-that is, unless the power amplifier is to serve as a multiplier stage, or if a screen-grid tube is used as the amplifier tube. The plate supply voltage for the oscillator can be as high as 350 to 650 volts, and that of the power amplifier, 1500 to 2000 volts. If a lowpower ( 7.5 watts, approximately) oscillator tube is used, a fixed bias of 40 to 60 volts will be required for high efficiency. A 3.5 to 4.5 -ampere current in the plate $\mathrm{L}_{1} \mathrm{C}_{\mathrm{n}}$ tank can be obtained under these conditions. A fixed bias is usually not necessary when a 50 -watt tube operated at low efficiency is used. With the same plate voltage as for the lowpower tube, a plate tank current of 4.5 to 7.5 am -

Section I
peres can be had. When a fixed bias is used, some arrangement must be provided to cut it in after oscillations build up and the negative peaks of $E_{p}$ must be sufficient for plate limiting to occur at the positive peaks of $E_{\mathrm{s}}$. When used as a power oscillator, the Miller circuit is often required to operate as a variable-tuned circuit, with a coil or tankcircuit in place of the crystal, the circuit thereby being converted into a tuned-plate-tuned-grid or a Hartley type oscillator. Because of this, the various tuning adjustments and meters that are needed in the variable circuit are also available in the crystal circuit. In this event, the rated load capacitance of the crystal unit will usually exist more in theory than in application. Since the crystal is intended to be operated at high drive, the risk is greatly increased that a chance adjustment may overload the crystal to the shattering point. This risk can be minimized by the use of an r-f milliammeter in series with the crystal, with the danger zone well marked. Besides excessive plate voltage and stray feedback due to poor shielding or neutralization, a poorly bypassed screen-grid circuit can lead to an overloaded crystal, as also can an excessive control-grid bias. Now, no attempt should be made to design a circuit in which a crystal unit is to be operated above its rated power level unless weight, space, or expense requirements demand the elimination of every possible amplifier stage; unless greater frequency stability is required than can be obtained with a conventional inductor-capacitor network; or unless a long operating lifetime is not a primary consideration. Even so, if a Military Standard unit is operated beyond specifications, it should be well understood that it is no longer effectively a standard type, and no guarantee exists concerning the replacement of one crystal unit by another.

## TYPICAL CHARACTERISTICS OF MILLER OSCILLATOR

1-340. Figure 1-143 shows an experimental Miller circuit, the performance characteristics of which were investigated by Messrs. E. A. Roberts, Paul Goldsmith, E. K. Novak, and J. Kurinsky of the Armour Research Foundation at the Illinois Institute of Technology. The crystal units used are of the type CR-18/U. The crystal PI indicated for each of the characteristic curves (figures 1-144 to 1-148) of the oscillator in figure $1-143$ is the value observed when the crystal was operating into its rated load capacitance. The PI at the rated load capacitance indicates the relative activity of the crystal unit, but is not intended to imply that the same PI is in effect for all variations of the load capacitance. The curves in figure 1-144 indicate (excitation voltage) ${ }^{2}$ and the output voltage as the plate tuning capacitance is varied. An increase in the plate capacitance means an increase in the effective value of $L_{p}$, so that the frequency decreases. Thus, as $C_{p}$ increases ( $C_{2}$ in figure 1-144), the reactance, $X_{*}$, of the crystal unit decreases. Oscillations cease whenever the $\mathbf{Q}_{\mathrm{E}}$ of the grid circuit becomes too small for the proper phase rotation to take place, or the ratio of $X_{p} / X_{g}$ becomes too high for the feed-back voltage to be of sufficient amplitude, or the plate tank approaches the paral-lel-resonant state, so that $E_{p}$ can no longer assume its proper phase, which requires the plate arm to be an inductive reactance smaller in magnitude than the capacitive-feedback reactance. The percentage points in figure 1-144 refer to percentages of the maximum output voltage that was obtained through variations of the plate tank capacitance alone. The six curves shown represent values for


Figure 1-143. Experimental Miller oscillator whese characteristic curves are plofted in figurez 1-144 to 1-148

## Section 1

## Crystal Oscillators

an $\mathrm{E}_{\mathrm{b}}$ of 200 volts with a full load of 5000 ohms, and for an $E_{b}$ of 100 volts with full load and with no load. It is interesting to note that in each of the three pairs of curves the maximum grid voltage occurs at a smaller load capacitance than that at which the output voltage is a maximum. For each curve where the plate tuning capacitance is the same, it can be approximately assumed that the load capacitance is the same. Also, between the values of $C_{p}=75$ and $C_{p}=90 \mu \mu f$, it can be assumed that the percentage change in $C_{x}$ is small. Since the PI of the crystal unit is the same where the load capacitance is the same, the excitation-
voltage-squared curves indicate the relative crystal drive for the different $E_{b}$ and load conditions. Also note that the two pairs of curves representing full-load conditions coincide fairly closely at their points of equal percentages. This is important in interpreting the curves in figure 1-145, each of which represents 50 per cent output, and hence approximately the same load capacitance and frequency. Exceptions are the 10 K curves in figure 1-145, as can be checked by figure 1-146. The performances curves in figure 1-145 are the Miller equivalents of the Pierce curves in figure 1-130. It can be seen that the Miller output is much


Figure 1-144. (A) Square of excitotion voltage and (B) rms value of output volfoge versuy plate tuning capacitance of experimental Miller oscillator. Frequency $=7 \mathrm{mc}$; gridleak resistance $=1$ megohm; and PJ of CR-18/U crystal unit (with load capacitance of $32 \mu \mu$ ) $=49$ kilohms. F.L. = full load conditions ( 5,000 ohms aeroas plate tank) and N.L. = no load conditions. Percentage points rofer to persentages of maximum output voltage obtainable under given load and d-c plete voltage conditions


Figure 1-145. Output voltage versus crystal power for various values of gridieak resistance as the d-c plate voltage is varied in experimental Miller oscillator. The circuit is funed for output voltages 50 percent of the maximum possible by variations in plate tank alone. Frequency $=7$ me; plate tank I/C $=0.04$; and PI of CR-18/U crystal unit (with load capacitance of $32 \mu \mu$ ) $=49$ kilohms


Figure 1-146. Frequency of experimental Millor oscillator versus d-e plate voltage and grid resistance for various plafe-tuned load capacitances. (Max) E. represents the plate funing adjustment that provided maximum output voltage when grid resistance and der plate voltage were values indicated by zero reference point. A 7-me CR-I8/U crystal unit was used, having a PI of 49,000 ohms
when operating into a roted load capacitance of $32 \mu \mu$
more sensitive to changes in the grid resistance. This is to be expected, since the grid-to-cathode $\mathrm{r}-\mathrm{f}$ impedance and excitation voltage is much greater in the Miller circuit. A crystal r-f voltage of 2 volts represents an excitation of 2 volts in the Miller circuit, but usually of only 1 volt or less in the Pierce circuit. If the curves in figures 1-130 and 1-145 were plotted against excitation voltage instead of crystal driving power they would be much more similar in appearance.
1-341. The frequency curves in figure 1-146 are the Miller equivalents of the Pierce curves in figure 1-129. Note that as $R_{z}$ is decreased the frequency falls, whereas in the Pierce circuit the frequency increases. This is one reason why the Miller circuit becomes so much more frequency sensitive to changes in $R_{g}$ when $R_{s}$ is small. As the $Q_{s}$ of the grid circuit is decreased because of a decrease in
$\mathrm{R}_{\mathrm{R}}$, the effective $\mathrm{Z}_{\mathrm{L}}$ across the tube must appear more inductive in order for $E_{p}$ to shift in the correct direction to compensate for the decreased phase rotation between grid and cathode. For this to occur, the net capacitive reactance of the feedback arm must increase, which can only come about if the inductive reactance of the crystal unit decreases. Hence, the frequency falls, and in so doing, the $Q_{g}$ of the crystal and grid circuit becomes smaller still, so that an additional drop in the frequency is necessary to compensate for the decrease in the crystal $Q_{e}$. In the meantime, the bias decreases and the grid goes positive a larger fraction of the time. This tends to decrease $\mathrm{R}_{\mathrm{p}}$, which contributes even more to the drop in frequency. With all these effects adding in the same direction, the large frequency sensitivity of the Miller with changes in the grid resistance is ex-


Figure 1-147, (A) Square of excitation voltage and (B) rms value of output voltage of experimental Miller oscillator versus plote funing capacitance for various L/C ratios of plate fank. Same arystal unit os was used for curves in Agure 1.144



Figure 1-148. Output and erystal drive of experimental Miller and Pierce oscillators as d-c plate valtage is variad for arystal units of various frequencies and PI's. The values of Pl assume a rated locd capacitance of $32 \mu \mu$. Both oscillators were tuned
to provide 50 percent (max) $E_{n}$ and to operate into a 5000 -ohm plate load
plained. The sensitivity is a maximum when $L_{p}$ is a maximum, for then the frequency is a minimum and the crystal is operating nearest its series-resonant state. This fact makes an exception to the rule that the larger the effective $C_{x}$, the greater the stability.
1-342. Of special interest in the curves of figure 1-146 is the fact that those representing the 50 -per-cent-maximum-output adjustment show an increase in frequency with an Increase in plate voltage, whereas the curves representing a maximum output voltage show a decrease in frequency when the plate voltage is increased, even though the same plate voltages are applied in each case. Now, in the Miller oscillator, the frequency increases and decreases in the same direction with $\mathrm{R}_{\mathrm{p}}$. The plate characteristics of the 6C4 tube, the tube being used when the curves in figure 1-146 were plotted, indicate a decrease in $\mathrm{R}_{\mathrm{p}}$ as the plate voltage increases. Thus, we should expect the change in frequency of the (max) $E_{o}$ curves to be due to the change in $R_{p}$ caused by the change in plate voltage. On the other hand, the oppositely directed change in frequency of the lower-percentage- $\mathrm{E}_{\text {o }}$ curves must be due to an oppositely directed change in $R_{p}$ brought about by a change in the bias. A re-examination of the crystal voltage curves does indeed show at the 50 -per-cent- $\mathrm{E}_{\mathrm{o}}$ adjustment that the grid excitation, and hence the bias, is near the maximum. In figure 1-145, it can be seen that for large values of grid resistance the changes in output voltage due to changes in the plate voltage cause a maximum variation in the crystal drive. The evidence is quite strong that there is an operating region between the oppositely changing frequency curves where the changes in $R_{p}$ due to changes in $E_{b}$ and $E_{c}$ will annul each other. From an inspection of the crystal voltage curves in figure 1-144 we would guess that such operating points will lie on both sides of the maxi-mum- $\mathrm{E}_{\mathrm{g}}$ region. Such a state of operation would be an example of "class- $D$ " operation described in paragraph 1-298.
1-343. The curves shown in figure 1-147 indicate the effect of variations in the L/C ratio of the plate tank circuit obtained by increasing the value of $L_{1}$ in figure 1-143. Increasing $L_{2}$ increases the impedance into which the tube operates, and thus increases the r-f plate voltage. This also has the effect of decreasing the frequency and the reactance of the crystal unit. For this reason, the crystal voltage does not increase in the same proportion as the plate voltage. Much greater stability is obtained with low L/C ratios, but much greater values of $E_{v} / E_{k}$, and hence of power gain,
are to be obtained with large L/C ratios. Figure 1-148 compares output-vs-drive curves for several different frequencies and values of PI when the same crystal units are used in both Miller and Pierce oscillators. Note that in the Pierce circuit the slopes of the curves consistently increase with an increase in PI. In the Miller circuit the tendency is for the slopes to increase with decreasing frequency primarily, and secondarily with the PI. This may be due to the fact that the gridleak resistance used in the Miller circuit was smaller than that in the Pierce circuit. In any event, the average bias will tend to be less at the lower frequencies, since the grid charge has more time during a cycle to leak off.

## MODIFICATIONS IN DESIGN OF MILLER OSCILLATOR

1-344. A number of Miller oscillators currently being used in military equipment are illustrated in figures 1-149, 1-150, 1-151, 1-152, and 1-153. The values of the circuit parameters, where available, are given in the accompanying circuit-data charts. None of the crystal units employed in these circuits is now recommended for equipments of new design. Nevertheless, all the circuits shown can be modified in one way"or another and used with currently recommended crystal units which have been tested for parallel resonance. The necessary modifications would be those that would ensure a correct load capacitance and would not permit a crystal to be overdriven within the expected range of effective resistance. The circuits illustrated suggest the wide adaptability of the Miller oscillator for different output requirements and uses. It is not possible to single out a particular circuit and declare this design to be preferred. The engineer will need to design and test his own circuit for the particular requirements of the equipment in which his oscillator is to be used. Quite often the type of vacuum tube or other circuit components most readily available influence the design. Unlike the Pierce, the Miller circuit must include a means of adjusting the plate impedance to ensure the correct load capacitance for the crystal if the oscillator is to operate to more than one frequency. In the circuits of figures 1-149 to 1-153, the switching arrangements of those circuits designed to operate over a wide frequency range are for the most part omitted. Most often, a separate plate coil is provided for each crystal position. Because of space limitations in the circuit-data charts, occasionally two different components in a circuit having the same value or being of the same type are assigned the same symbol number.

Section 1
Crystal Oscillators


Figure 1-149. Conventional Miller oscillators using friodes

| Fig. | Equipment | Purpose | $F$ | $F_{z}$ | CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Modulator and Transmitter BC-925 | M.O. | $\begin{aligned} & 555- \\ & 740 \\ & \hline \end{aligned}$ | $F_{1}$ | $\begin{aligned} & \text { Bliley } \\ & \text { AR-3 } \end{aligned}$ | 100 | 2 |
| (B) | Radio Receiver BC-624-A,-AM, $\mathbf{C}$ | Local oscillator | $\begin{aligned} & 8000 \\ & 8720 \end{aligned}$ | Fi | $\begin{aligned} & \text { DC-11-( } \\ & \text { DC-16, } \mathrm{DC} \\ & 26, \text { or } \mathrm{CR}- \\ & 1(\mathrm{AR} \\ & \hline \end{aligned}$ | 150 | 2.7 |
| (C) | Target Control Transmitting Equipment RC-56-A | M.O. | $\begin{aligned} & 5588 \\ & 8167 \end{aligned}$ | 1 | CR-1B/AF | 100 | 100 |
| (D) | Test Set IS-67/ARN-5 | 6.9 -me and 20.7 . me signals for testing receivera in ILS | 6900 | $F$ | CR-1A/AR | 50 | 70 |
| (E) | Radio Set AN/ARC-1A | Local ose in raceiver | 9720 | $\mathrm{F}_{i}$ | CR-1A/AK | 100 | 1.5 |
| (F) | Frequency Meter TS-523/UK | Oscillator for heterodyne freq meter and crystal calibrator | 1000 | nFi | Dallon's Laboratories D-1000 | 100 | 15 |
| (G) | Signal Generator 1-222 | Calibration or vio of signal generator | 5000 | nF1 | $\begin{aligned} & \text { Holder } \\ & \text { ET-243 } \end{aligned}$ | 22 | 22 |
| (H) | Radio Transmitter BC-1382 | M. 0. | 8833.38 | E | CR-1A/AR | 51 | 1 |

Circuit Data for Figure 1-149. Fin he. $R$ in kilohras. $C$ in $\mu \mu$ f. L in $\mu \mathrm{h}$.
WADC TR 56-156

(H)

| $\mathrm{R}_{3}$ | R4 | R5 | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{Ca}_{3}$ | $\mathrm{C}_{4}$ | $\mathrm{C}_{5}$ | $\mathrm{L}_{1}$ | $\mathrm{V}_{1}$ | $\mathrm{V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 250 | 10 | 100 | 25 | 250 | 6000 |  | 560 | $\begin{gathered} 1 / 2 \\ 12 \mathrm{SLGT}_{7} \end{gathered}$ |  |
| 10 | 560 |  | 6800 | 680 | 6800 | 220 | 15 | $\begin{gathered} 26 \\ \text { turns } \end{gathered}$ | $12 \mathrm{AH7GT}$ | 9002 |
|  |  |  | 10-100 | 100 | 4000 |  |  |  | 1255GT | 12J5GT |
|  |  |  | 5-60 | 50 | 4000 |  |  |  | $6 \text { SN7GT }_{1 / 2}$ | $\begin{aligned} & 1 / 2 \\ & 6 S^{1 / 2} 7 \end{aligned}$ |
|  |  |  | 24 |  |  |  |  |  | 6 C 4 |  |
| 1 | 470 |  | 2-16 | 2 | 100,000 | 4.75 |  | 1000 | $6 \mathrm{C4}$ | 9001 |
| 4.7 |  |  | 4.5-50 | 10 | 100,000 | 8000 | 100 | $\begin{aligned} & 44 \\ & \text { turns } \\ & \text { No. } 24 \\ & \text { AWG; } \\ & 0.77 \times \\ & \text { i.94 } \\ & \text { in. } \end{aligned}$ | 655 |  |
| 15 | 51 | 8 | 4.5-15 | 4700 | 47 |  |  | 10.4 | 655GT/G | 832-A |

Section 1
Crystal Oscillators

(c)

Figure 1.150. Modiliod Miller oscillotors using triodes

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | $\mathrm{F}_{2}$ | Ft | $\mathrm{F}_{4}$ | CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | R. | R ${ }_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Receiver BC-788-DM | Local oscillator | $\begin{aligned} & 6688- \\ & 5745 \end{aligned}$ | $\mathrm{F}_{1}$ | ${ }^{3} \mathrm{~F}_{1}$ | ${ }^{98}$ | $\begin{aligned} & \text { Holder } \\ & \text { Fr-248 } \end{aligned}$ | 1.5 | 180 | 8.2 | 1.5 | 220 |
| (B) | Radio Receivers R-57/ARN-5 and R-89 ( )/ARN-5A | Lacal oscillator | $\begin{aligned} & 64988 \\ & 6548 \end{aligned}$ | $F_{1}$ | 2 Fi | ${ }^{4 F_{1}}$ | $\begin{aligned} & \text { Holder } \\ & F T-243 \\ & ( \pm 0.02 \%) \end{aligned}$ | 1.5 | 8.2 |  | 1.8 | 39 |
| (C) | Radio Receivers R-77/ARC-3 and R-77A/ARC-3 R-77A/ARC-3 | LoenTosellatar | $\begin{aligned} & 8000- \\ & 8727 \end{aligned}$ | Fi | Fi | $\begin{aligned} & 111_{1}^{1-} \\ & 18 F_{1} \end{aligned}$ | CR-1/A/AR | 56 | 12 | 830 | 0.1 | 0.1 |
| (D) | Test Oscilloscope TS-100/AP | Nauticalmile range-synchroniting oscillator | 80.86 | $F_{1}$ | $P_{1}$ | $F_{1}$ | $\frac{ \pm 30^{\circ} \mathrm{cps}}{50^{\circ} \mathrm{C}}$ | 2200 | 5.1 | 8.2 | 5.1 | 50 |

Circuit Data for Figure 1-150. Fin kc. $A$ in kilohma. $C$ in mpf. L in mh.


Figure 1-150. Continued

| $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{C}_{3}$ | C | $\mathrm{C}_{3}$ | C | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | ${ }_{1}$ | $\mathrm{L}_{2}$ | $\mathrm{L}_{3}$ | $L_{4}$ | $\mathrm{L}_{5}$ | $\mathrm{V}_{1}$ | $\mathrm{V}_{2}$ | $\mathrm{V}_{3}$ | $V_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 10 | 100 | 6000 |  |  |  |  | $\begin{gathered} 44 \\ \text { turns, } \\ 3 / 8- \\ \text { in. } \\ \text { dia } \end{gathered}$ | $\begin{gathered} 22 \\ \text { turns, } \\ 3 / 8- \\ \text { in. } \\ \text { dia } \end{gathered}$ |  |  |  | $\begin{gathered} 1 / 2 \\ 12 A H 7 \\ G T \end{gathered}$ | $\begin{gathered} 1 / 2 \\ 12 A H 7 \\ \text { GT } \end{gathered}$ |  |  |
| 30 | 22 | 270 |  |  |  |  |  |  |  |  |  |  | $\begin{gathered} 1 / 2 \\ 12 S \mathrm{~N} 7 \\ \mathrm{GT} \end{gathered}$ | $\begin{gathered} 1 / 2 \\ 12 S N 7 \\ G T \end{gathered}$ |  |  |
| 5 | 10 | 1000 | 10 |  |  |  |  | $\begin{gathered} 33 \\ \text { turns } \end{gathered}$ |  |  |  |  | 9002 | 6AK5 | 6AK5 | 6AK5 |
| 1000 | 60 | 100 | 220 | 10,000 | 60 | 200 | 100,000 | 1000 | 4760 | 4760 | 1000 | 4760 | $\underset{\substack{1 / 2 \\ 6 S^{\text {GT }} \\ \text { GT }}}{ }$ |  |  |  |



Figure 1-151. Millor oscillators using screen-grid tubes. (Effective suppressor in beam-power tubes is connected to eathode inside tube, afthough external connection mery be indicated in diagram.)

| Fig. | Equipment | Purpose | Fi | $\mathrm{F}_{8}$ | Fi | $\mathrm{F}_{4}$ | CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | Re | R ${ }_{6}$ | $\mathrm{R}_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | $\begin{aligned} & \text { Monitor } \\ & \text { M10-18/ } \\ & \text { CPN-2 } \end{aligned}$ | Mile range synchronizing ascillator | $93.109$ | Fr |  |  | 75*C oven | 270 | 47 | 1 | 560 | 0.15 |  |
| (B) | Radio mitters $\underset{\text { E-to-M }}{\text { BC- }}$ | M.O. | $\begin{aligned} & 2000- \\ & 4000 \end{aligned}$ | $F_{3}$ |  |  |  | 4 | 50 | 10 | 0.5 | 10 |  |
| (C) | Range Marker Generator TD-42/ FFS-3 | Nauti-cal-mile range caliors- | 80.36 | $F_{1}$ |  |  |  | 100 | 0.15 | 68 | 15 | 770 | 10 |
| (D) | $\begin{aligned} & \text { Kadio } \\ & \text { Trans } \\ & \text { mitters } \\ & \mathrm{BC}-640 \\ & \mathrm{~A},-\mathrm{B},-\mathrm{D} \end{aligned}$ | M.O. | $\begin{aligned} & 5656.5- \\ & 8666.6 \end{aligned}$ | $\mathrm{F}_{1}$ |  |  |  | 100 | 0.05 | 80 | 25 |  |  |
| (E) | Radio Trins- mitter T-171B/FR | M.O. |  | $F_{1}$ |  |  | $\begin{aligned} & \text { Holder } \\ & \text { FT-249 } \end{aligned}$ | 6000 | 1 | 100 | 100 |  |  |

Circuit Data for Figure 1-151. Fin ke. $R$ in kilohms. $C$ in mul. Lin $\mu \mathrm{h}$.
WADC TR 56-156

(c)

1
(0)


Heure 1-151. Cominoed
(E)

| $\mathrm{C}_{1}$ | C3 | $\mathrm{C}_{3}$ | C. | Cs | C | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | $L_{1}$ | $\mathbf{L}_{2}$ | $L_{3}$ | $L_{4}$ | Ls | $\mathrm{V}_{1}$ | $\mathrm{V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5-50 | 2 | 500,000 | 2000 | 500,000 | 10,000 |  |  |  |  |  |  |  | 6AC7 | 6AC7 |
| 5000 | 10,000 | 20,000 | 10,000 | 250 | 25 | 865 | 105 | 2500 | 2500 |  |  |  | 6F6 | 837 |
| 5 | 100,000 | 10,000 | 20,000 | 380 | 20,000 |  |  | 10,000 |  |  |  |  | 6AU6 | $12 \mathrm{~A}^{1 / 2}$ |
| 15 | 5000 | 8000 | 2000 | 8-106 | 5000 | 60 |  | 8.67 |  |  |  |  | 1618 | 807 |
| 6 | 100,000 | 100,000 | ${ }^{3} 80$ | 500 |  |  |  | $\begin{aligned} & \text { 18GI } \\ & (7 \Omega) \end{aligned}$ | $\begin{aligned} & 449.5 \\ & (3.76 \cap) \end{aligned}$ |  |  |  | 6557 | 6V6 |

Section 1


| Fig. | Equipment | Purpose | $F_{1}$ | $\mathrm{F}_{2}$ | F, | F | CR | $\mathbf{R}_{1}$ | R, | R: | R. | R. | R. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (F) | Radio Set AN/CRT-3 | "Gibson Girl" power ose | 8280 | $F_{1}$ |  |  | $\begin{aligned} & \mathrm{CR}-1 \mathrm{~A} / \\ & \mathrm{AR} \end{aligned}$ | 33 | 27 | 33 |  |  |  |
| (G) | Radio Transmitter T-91/ VRC-4 | M.O. | $87000$ | $F$ |  |  | $\begin{aligned} & \text { Sif Stock } \\ & \$ 223531 \mathrm{~B} \end{aligned}$ | 60 | 0 | 60 | - |  |  |
| (H) | Radio Set AN/ARC 1A | Guardchannel heterodyne freq generator | $\begin{array}{\|l\|} \hline 5020 \mathrm{~m} \\ 8120 \\ \hline \end{array}$ | FI | 18Fi |  | $\begin{aligned} & \mathrm{CR}-1(\mathrm{l} \\ & \mathrm{AR} \end{aligned}$ | 10 | 100 | 1 | 560 |  |  |
| (I) | Radio Transmitter T-4/FRC | M.O. | $\begin{aligned} & 2000- \\ & 6000 \end{aligned}$ | $F$ |  | - | $\begin{aligned} & \text { Holder } \\ & \text { FT-249 } \end{aligned}$ | 100 | 0.5 | 0.0238 | 100 |  |  |
| (J) | Radio Transmitter T-5/FRC | M.O. | $\begin{aligned} & 150- \\ & 550 \end{aligned}$ | $F_{1}$ |  |  | Sig Stock 12X41 | 100 | 0.5 | 0.0238 | 100 |  |  |
| (K) | Radio Transmitter T-10/ CRN-5 | M. 0 . | $\begin{array}{\|l} 5555.8 \\ 8666.6 \end{array}$ | $F_{1}$ | $3 F_{1}$ | $6 \mathrm{~F}_{1}$ | $\begin{aligned} & \text { CR-1A/ } \\ & \text { AR Or } \\ & \text { DC-11-( }) \end{aligned}$ | 0.1 | 100 | 0.5 | 0.0008 | 20 | 100 |

Circuit Data for Figure 1-151. F in ke. R in kilohms. C in $\mu \mu \mathrm{f}$. L in $\mu \mathrm{h}$.


Figure 1-151. Comminued
(K)

| $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | C: | C. | C: | Cs | $\mathrm{C}_{7}$ | C. | $\mathbf{L}_{1}$ | $\mathrm{L}_{7}$ | L, | L. | $L_{4}$ | $\mathrm{V}_{1}$ | V, |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 300 | 1000 | 1000 | ${ }_{48.7}^{4.7}$ | 1000 | 0 |  |  | 2350 | 2500 | $\begin{aligned} & \hline \text { s-1/2 } \\ & \text { or } 12 \\ & \text { turns } \\ & 1-1 / 2 \\ & \text { in. } \end{aligned}$ | $\begin{aligned} & \mathrm{s}-1 / 2 \\ & \text { or } 12 \\ & \text { turns } \\ & 1-1 / 2 \end{aligned}$ | $\begin{aligned} & 1-1 / 4 \\ & \text { turn } \\ & \text { turn } \\ & \text { in. } \end{aligned}$ | 12 A 6 |  |
| 250 | 10,000 |  | $\begin{aligned} & 72^{2} \\ & 148.7 \end{aligned}$ | 100 | 100 |  |  | 2800 | $\begin{aligned} & 18,25, \\ & 8,68 \\ & \text { turna } \end{aligned}$ | $\begin{gathered} 18,{ }^{24,} \\ 8,68 \\ \text { turna } \end{gathered}$ | 0 | 0 | $\begin{aligned} & 6 V 6 \\ & G T \end{aligned}$ |  |
| 75 | 2 | 12 | 2000 | 6 | 8 | 100 |  |  |  |  |  |  | 6RK5 | 6AK5 |
| 10,000 | 10,000 | 800 | 9750 | 800 |  |  |  | 2800 |  |  |  |  | 8V6C | 807 |
| 10.000 | 10.000 | 10,080 | 11-250 | 10.000 |  |  |  | 10,000 | $\xrightarrow{\text { Pound }}$ |  |  |  | 6V6G | 807 |
| 20 | 100 | 3600 | 3000 | 3000 | ${ }^{2,80} 8$ | $\begin{aligned} & 8.8- \\ & 80 \end{aligned}$ | 240 | $\begin{gathered} 81 \\ \text { turnu } \end{gathered}$ | $\begin{gathered} 14 \\ \text { turnm } \end{gathered}$ | 2800 |  |  | $\begin{gathered} 6 \sqrt{6 G T} \\ G \end{gathered}$ | $\begin{gathered} 8,6 \mathrm{GTT} \\ \mathrm{a} \end{gathered}$ |


(B)

Figure 1.152. Electron-couplad Millor oscillators. All circuits except (A), (B), and (C) are tri-fet modifications

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | $\mathrm{F}_{7}$ | $F_{3}$ | CR | $\mathrm{R}_{\mathbf{t}}$ | $\mathrm{R}_{2}$ | $\mathbf{R}_{3}$ | $\mathbf{R}_{4}$ | $\mathbf{R}_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Receiver and Se lector BC-617-AZ | Heterodyne oscillator | $\begin{aligned} & 8000- \\ & 9000 \end{aligned}$ | $F_{1}$ | 4Fi | CR-1( )/AR | 56 | 2.2 | 2.2 |  |  |
| (B) | Radio Transmitters T-3/CRN-2 and T-3A/ CRN-2 | M.O. and multiplier | $\begin{aligned} & 6203.7- \\ & 6159.26 \end{aligned}$ | Fi | $3 \mathrm{~F}_{1}$ | $\begin{aligned} & \text { CR-1A/AR } \\ & \text { or } \\ & \text { DC-17-B } \end{aligned}$ | 100 | 0.25 | 50 | 50 |  |
| (C) | $\begin{aligned} & \text { Radio } \\ & \text { Transmitter } \\ & \text { BC-329-J } \end{aligned}$ | M.O. | $\begin{aligned} & 200 \\ & 410 \end{aligned}$ | $F_{1}$ |  | $\begin{aligned} & \text { Holder } \\ & \text { FT-164 } \end{aligned}$ | 1000 | 1.5 | 0.001 | 5 | 17.6 |
| (D) | $\begin{aligned} & \text { Radio Re } \\ & \text { ceiver } \\ & \text { R-146A/ } \\ & \text { ARW-35 } \\ & \hline \end{aligned}$ | 1st heterodyne oscillator | $\begin{aligned} & 7833- \\ & 10,000 \end{aligned}$ | $6 F_{1}$ | $\begin{gathered} 6 F_{1} \\ \frac{1}{+} \end{gathered}$ | $\begin{aligned} & \text { Fioder } \\ & \text { FT-249 } \end{aligned}$ | 100 | 100 | 4760 | 6 |  |
| (E) | $\begin{aligned} & \text { Radio Sets } \\ & \text { AN/TRC-1, } \\ & -1 A,-1 B \text {, } \\ & -1 C \end{aligned}$ | Heterodyne ose in Radio Receiver R-19()/ TRC-1 | $\begin{aligned} & 7800- \\ & 8750 \end{aligned}$ | $\begin{aligned} & 5 F_{1} \\ & \text { and } \\ & 6 \mathrm{~F}_{1} \end{aligned}$ | NA | CR-6/t | 100 | 100 | 250 | 0 |  |
| (F) | $\begin{aligned} & \text { Radio Sets } \\ & \text { AN/TRC-1D. } \\ & -1 E \end{aligned}$ | $\begin{aligned} & \text { Hetero- } \\ & \text { dyne oss } \\ & \text { in Radio } \\ & \text { Receiver } \\ & \text { R-19 } \\ & \text { TRC-1 } \end{aligned}$ | $\begin{aligned} & 7300 \\ & 8750 \end{aligned}$ |  | NA | CR-6/0 | 100 | 100 | 280 | 50 |  |
| (G) | Radio Receiver R-19H/ TRC-1 | Hetero dyne oscillator | $\begin{aligned} & 7800 \\ & 8750 \end{aligned}$ | $\begin{aligned} & 5 F_{1} \\ & \text { and } \\ & 6 F_{1} \end{aligned}$ | NA | CR-6/U | 100 | 100 | 240 | 51 |  |

Circuit Data for Figure 1-152. Fin kc. A in kilohms. C in mi. Lin mh. NA: Not Applicable.


| $\mathrm{R}_{6}$ | R7 | $\mathrm{Ra}_{8}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | C3 | $\mathrm{C}_{4}$ | C5 | C | $\mathrm{C}_{7}$ | $L_{1}$ | $L_{2}$ | $\mathrm{L}_{3}$ | $V_{1}$ | $\mathrm{V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 7-42 | 2200 | 4 | 510 | 7-42 | 6 | 10 |  |  | 9300 | 12SG7 | 12SG7 |
|  |  |  | 3000 | 10 | $\begin{gathered} 5.3- \\ 30 \end{gathered}$ | 3000 | 30 | $\begin{gathered} 5.8- \\ 80 \end{gathered}$ | 250 | 18 | 1.1 |  | 6587 | 6837 |
| 50 | 0.6 | 0.001 | 10,000 | 10,000 | 10,000 | 250 | 10,000 |  |  | 2500 | 8500 |  | 6 V 6 GT | 807 |
|  |  |  | 2000 | 3-54 | 2000 | 5-80 | 250 | 4 |  |  |  |  | 128H7 | 64C7 |
|  |  |  | 1500 | 3-54 | 1800 | 0 | 0 | 100 |  |  |  | 0 | 68187 | 6857 |
|  |  |  | 1500 | 8-64 | 1600 | $\sigma$ | 0 | 100 |  |  |  | 6 | 6837 | 6547 |
|  |  |  | 1500 | 3-64 | 1500 | 0 | 6 | 100 |  |  |  | 6 | 68527 | 6EH7 |


(H)
figure 1-152. Cominued

(1)

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | $F_{2}$ | Fs | CR | $\mathbf{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{1}$ | R. | R |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (H) | Radio Receiver and Transmitter BC-788-A | Timing ose and 5000-ft range control | 98.356 | $F_{1}$ |  | DC-22-A | 470 | 220 | 1000 | 10 |  |
| (I) | Galvin Radio Receivers PA8098 and PA-8245 | 1st local ose in Communication Equipment AN-CRC-3 | $\begin{aligned} & 6425 \\ & 8120 \end{aligned}$ | $\begin{aligned} & \hline \mathbf{4 F _ { 1 }} \\ & \text { and } \\ & 5 F_{1} \end{aligned}$ |  | $\begin{aligned} & \text { Holder } \\ & \text { FT-248 } \end{aligned}$ | 1000 | 47 | 4.7 |  |  |
| (J) | $\begin{aligned} & \text { Radio Re- } \\ & \text { ceiver } \\ & \text { R-368/ } \\ & \text { FRC-6A } \\ & \hline \end{aligned}$ | Heterodyne oscillator | $\begin{aligned} & 6425- \\ & 8425 \end{aligned}$ | $\begin{aligned} & \text { dFi } \\ & \text { and } \\ & 5 F_{z} \end{aligned}$ | $\begin{aligned} & \mathrm{F}_{2}+ \\ & 4.3 \end{aligned}$ |  | 1000 | 47 | 4.7 | 47,000 |  |
| (K) | $\begin{aligned} & \text { Radio Set } \\ & \mathrm{AN} / \vee \mathrm{RC}-2 \end{aligned}$ | 1st heterodyne ose | $\begin{aligned} & 6425- \\ & 8425 \end{aligned}$ | $\begin{aligned} & \text { and } \\ & \text { and } \\ & 5 F_{1} \end{aligned}$ | $\begin{gathered} F_{2}+ \\ 4.3 \end{gathered}$ |  | 47 | 47 | 4.7 | 47,000 |  |
| (1.) | $\begin{aligned} & \text { Radio Trans- } \\ & \text { mitter } \\ & \text { BC-610-E } \end{aligned}$ | M.O. | $\begin{aligned} & 2000 \\ & 6000 \end{aligned}$ | Fi |  | $\begin{aligned} & \text { Holder FT } \\ & \text { 171-B } \end{aligned}$ | 38 | 100 | 15 | 5.6 |  |

Circuit Data for Figure 1-152. Fin kc. F in kilohms. $C$ in mpl. $L$ in $\mu \mathrm{h} . \mathrm{NA}$ : Not Applicable.


| R. | $\mathrm{K}_{\text {\% }}$ | R* | C ${ }_{1}$ | $\mathrm{C}_{2}$ | C. | C. | $\mathrm{C}_{5}$ | $\mathrm{C}_{6}$ | C: | $L_{1}$ | $L^{*}$ | $L_{3}$ | V, | V : |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 1500 | 10,000 | 470 | 470 |  |  |  | $\begin{gathered} 150 \\ \text { and } \\ 400 \\ \text { turns } \end{gathered}$ | $\begin{gathered} \text { Four } \\ 190 \\ \text { turn } \\ \text { sections } \end{gathered}$ |  | 6AG5 | 6AG5 |
|  |  |  | $\begin{gathered} \text { Op- } \\ \text { tional } \end{gathered}$ | 5-44 | 3000 | 2 |  |  |  | (0.3n) |  |  | $\begin{gathered} 6 \mathrm{SD7} 7 \\ \mathrm{GT} \end{gathered}$ |  |
|  |  |  | 5600 | 6-45 | 5600 | 6-45 | 2 |  |  |  |  |  | 6SG7GT | 6SG7GT |
|  |  |  | 2000 | 5-44 | 5000 | 0 | 2 |  |  |  |  | $\infty$ | 6SD7GT | 6SD7GT |
|  |  |  | 75 | 240 | 6000 | 6000 | 6000 | 6000 | 150 | 37 | 1000 | 10,000 | 6V6 | $\begin{aligned} & \text { VR150- } \\ & 80 \end{aligned}$ |



Figure 1-153 Miscellaneou: Miller-oscillator modifications

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | $\mathrm{F}_{2}$ | $F_{3}$ | CR | $\mathbf{R}_{1}$ | $\mathbf{R}_{2}$ | $R_{3}$ | $R_{4}$ | R5 | $\mathrm{R}_{0}$ | $\mathrm{R}_{7}$ | $\mathrm{R}_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Galvin <br> Radio <br> Transmitter PA-8218 P/OAN/ CRC-3 | M.O. for phase modulator circuit | $\begin{aligned} & 937.5 \\ & 1250^{\circ} \end{aligned}$ | $F_{1}$ | $\underset{(\bmod ,)}{F_{1}}$ | Motorola FMT | 1 | 470 | 4.7 | 10 | 47 | 47. | 0.1 |  |
| (B) | Radio <br> Transmitter <br> T-264 <br> FRC-6A | M.O. for phase modulator circuit | $\begin{aligned} & 937.5 \\ & 1250 \end{aligned}$ | $F_{1}$ | $\underset{(\bmod .)}{F_{i}}$ |  | 1 | 470 | 4.7 | 10 | 47 | 47 | 0.1 |  |
| (C) | Galvin <br> Radio <br> Transmitter PA-8244 P/OAN/ CRC-3 | M.O. Ior phase modulator circuit | $\begin{aligned} & 3750- \\ & 5000 \end{aligned}$ | $F_{1}$ | $\underset{(\bmod )}{F_{1}}$ | $\underset{\text { HT- }}{\text { Holder }}$ | 1 | 470 | 4.7 | 47 | 47 | 4.7 | $0.1$ | 4.7 |
| (D) | Galvin <br> Radio <br> Trans- <br> mitter <br> PA-8026 <br> P/OAN/ <br> VRC-2 | M.O. Ior phase modulator circuit | $\begin{aligned} & 3750- \\ & 5000 \end{aligned}$ | $F_{1}$ | $\mathbf{r}_{\mathbf{2}}$ | $\begin{aligned} & \text { Holder } \\ & \text { FT-248 } \end{aligned}$ | 1 | 470 | 4.7 | 47 | 47 | 4.7 | 0.1 | 4.7 |

Circuit Data for Figure l-153. Fin kc. $R$ in kilohms. $C$ in $\mu \mu$. $L$ in $\mu \mathrm{h}$, unless otherwise noted.
WADC TR 56-156

(c) (0)

Figure 1-153. Continued

| R | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{C}_{2}$ | C | Cs | Cs | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | $\mathrm{C}_{8}$ | $L_{1}$ | 12 | Ls | $\mathrm{V}_{1}$ | $\mathrm{V}_{2} \quad \mathrm{~V}_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5000 | 25 | 50 | 5-44 | 5000 | 10 | 100 | 100 | 2000 |  |  |  | $7 \mathrm{C7}$ | 7 A 8 |
|  | 5600 | 24 | 0 | 6-45 | 5600 | 24 | 100 | 100 | 2200 |  |  |  | $7 \mathrm{C7}$ | 7 A 8 |
|  | 5000 | 5-44 | 5000 | 100 | 100 | 2000 | 5 | 2000 | 5 |  | $\underset{\text { choke }}{\text { R-F }}$ |  | $7 \mathrm{C7}$ | 7 A 8 |
|  | 5000 | 5-44 | 5000 | 100 | 100 | 2000 | 5 | 2000 | 5 |  | $\underset{\text { choke }}{\text { R-F }}$ |  | $7 \mathrm{C7}$ | 7 A 8 |


(E) (F) (G)

Figure 1-153. Continued

| Fig. | Equiprnent | Purpose | $F$ | $F_{3}$ | $\mathrm{F}_{3}$ | CR | $\mathrm{R}_{\text {: }}$ | $\mathbf{R}_{2}$ | $\mathrm{R}_{3}$ | R4 | $\mathrm{R}_{6}$ | R ${ }_{\text {c }}$ | $\mathbf{R}_{3}$ | $\mathbf{R}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (E) | Crystal Calibrator TS$177 / \mathrm{CPS}-1$ | Calibration of mile range markers | 93.12 | $F_{1}$ | $F_{1}$ | $\begin{array}{l\|} \text { GE: } \\ 32 \mathrm{C} 401 \mathrm{G} 43 \\ \hline \end{array}$ | 1000 | 0.012 | 18 | 1000 | 2000 | 1000 | 2.2 | 10 |
| (F) | Crystal <br> Calibrator TS$241 / \mathrm{CPS}-5$ | Calibrar tion of mile range markers | 93.12 | $F_{1}$ | $F_{1}$ | $\begin{array}{\|l\|} \hline \mathrm{GF}: \\ 32 \mathrm{C4} 01 \mathrm{G} 48 \end{array}$ | 1000 | 0.012 | 18 | 1000 | 2000 | 1000 | 2.2 | 10 |
| (G) | Calibra-tor-Generator Group OA-96/ CPS-6B | Calibration of nautical mile range markers | 80.867 | $F_{1}$ | $F_{1}$ |  | 1000 | 0 | 15 | 1000 | 2200 | 1000 | 2.2 | 10 |
| (H) | $\begin{aligned} & \text { Firequency } \\ & \text { Meter } \\ & \text { TS } 174 / \mathrm{U} \end{aligned}$ | Crystal calibrator and heterodyne circuit | 1000 | nFi | $\begin{aligned} & 20,000- \\ & 250,000 \end{aligned}$ | DC-9 | 1000 | 8.75 | 0.076 | 1000 | 150 | $\infty$ |  |  |
| (I) | $\begin{aligned} & \text { Frequency } \\ & \text { Meter } \\ & \text { TS-175/U } \end{aligned}$ | Crystal calibrator and heterodyne circuit | 5600 | $\mathrm{nF}_{1}$ | $\begin{aligned} & 85,000 \mathrm{~m} \\ & 1,000,000 \end{aligned}$ | CR-1A/AR | 1000 |  | 0.75 | 1000 | 0 | 100 |  |  |
| (J) | $\begin{aligned} & \text { Frequency } \\ & \text { Meters } \\ & \text { AC-221- } \end{aligned}$ | Crystal calibrator and heterodyne circuit | 1000 | nFi | $\begin{aligned} & 1000 \\ & 20,000 \end{aligned}$ | $\begin{aligned} & \mathrm{DC-9-AD} \\ & \text { or } \\ & \mathrm{DC}-9 \mathrm{P} \end{aligned}$ | 1000 | 10 | 0.15 | 500 | 0 | $\infty$ |  |  |

Circuit Dats for Figure 1-153. Fin ke. R in kilohms. $C$ in $\mu \mu$. L in $\mu \mathrm{h}$, unless otherwise noted.


Figure 1-153. Continued

| Rs | $\mathrm{C}_{1}$ | C: | $\mathrm{C}_{3}$ | C ${ }_{4}$ | Cs, | C. | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | C, | $\mathrm{L}_{1}$ | L: | $L_{3}$ | $\mathrm{V}_{1}$ | $\mathrm{V}_{2} \mathrm{~V}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 3.8 | 500,000 | 330 | 51 | 10,000 |  |  |  |  | 8500 |  |  | 6SJ7 | $6 \mathrm{SN}^{1 / 2} 7 \mathrm{GT}$ |
| 100 | 3.8 | 500,000 | 330 | 51 | 10,000 |  |  |  |  | 8500 |  |  | 6 SJ 77 | $\begin{array}{\|c\|} \hline 1 / 2 \\ \hline 6 S^{2} 7 \mathrm{GT} \\ \hline \end{array}$ |
| 100 | 5 | 500,000 | 470 | 47 | 10,000 |  |  |  |  | 8500 |  |  | 6857 | $6 \operatorname{sN}^{1 / 2} 7$ |
|  | 12 | 12 | 3-25 | 1000 | 50,000 | 2000 | 0 |  |  | 80 h | 0 | 850 | 6 K 8 | $6 \mathrm{SJ7}$ |
|  | 2.5 | 12 | 3-25 | 0 | ${ }^{6000}$ | 2000 | 0 |  |  | $\infty$ | 175 | 70 | 6K8 | ${ }^{6 C 8 G}$ |
|  | 25 | 50 | 12 | 1000 | 20,000 | 250,000 | 6 |  |  | 150h | 0 | 1000 | 6 K 8 | $6 \mathrm{SJ7}$ |

## Two-Tube Parallel-tesonant Crystal Oscillators

1-345. Most of the two-tube oscillator circuits are designed so that the crystal is operated at or near its series-resonance frequency. An exception is the multivibrator type of circuit in which the crystal unit is connected between the grid and cathode of one of the tubes. The basic circuit is shown in figure $1-154$ ( $A$ ). If there were no capacitive effects to consider, $\mathrm{E}_{k z}$ would be 180 degrees out of phase with $\mathrm{E}_{81}$ and the 180 -degree feed-back inversion would be accomplished entirely by $V_{2}$. In this case, the input impedance of $V_{1}$ would have to be purely resistive- that is, the crystal unit would operate at parallel resonance with the input capacitance. The proper phase of $\mathrm{E}_{\mathrm{g}}$ could also be obtained with the crystal unit operating near series resonance, and unless the $V_{1}$ input impedance were so reduced that oscillations could not be sustained under such condition there would always be the risk that the oscillator would jump from one equilibrium state to the other. In an actual circuit, the circuit capacitances will prevent $V$, from operating into a purely resistive load, so that $\mathbf{E}_{\mathrm{p}}$ slightly lags the equivalent generator voltage $-\mu \mathrm{E}_{\mathrm{g}}$. The larger the values of $R_{n}, R_{p 1}, R_{82}, C_{1}$, and $C_{g 2}$, the nearer will the lag in $\mathrm{E}_{\mathrm{p}}$ approach the 90-degree limit. If it is assumed that $\mathrm{R}_{\mathrm{k}^{2}}$ is very large compared with the reactance of the $V_{2}$ input capacitance, $\mathrm{C}_{\mathrm{k} 2}$, the phase of $\mathrm{E}_{\mathrm{g} 2}$ is approximately the same as the phase of $E_{p 1}$. Also, if the ratio, $C_{1} / C_{g z}$, is very large, the magnitudes of $\mathbf{E}_{\mathbf{F}^{2}}$ and $\mathbf{E}_{\mathbf{p} 1}$ are very nearly equal. As can be seen in figure 1-154 (B), the lag in $E_{p}$ causes the equivalent generator voltage of $V_{2}$, equal to $-\mu \mathrm{E}_{\mathrm{x} 2}$, to lag $\mathrm{E}_{\mathrm{x} 1}$. The circuit will oscillate at that frequency at which the crystal impedance creates the necessary phase difference between $E_{k 1}$ and $-E_{g 2}$. Note, that except
for the possible coupling between the output circuits of $V_{1}$ and $V_{2}$ because of the grid-to-plate capacitance of $V_{2}$ (which can be made negligible by the use of screen-grid tubes), the phase of $\mathrm{E}_{\mathrm{k} 2}$, and hence of $-\mu E_{k}$, is entirely independent of impedance changes in the $V$, plate circuit. Thus, to predetermine the angle $\theta$ in figure $1-154(\mathrm{~B})$, it is only necessary to consider the $V$, stage as a conventional vacuum-tube amplifier circuit. In turn, the $V_{2}$ stage can be treated separately as an equivalent circuit driven by a generator of voltage $-\mu E_{k z}$. The design must be such that when the crystal unit is operating at its rated $X_{e,}$, the voltage across the crystal unit differs from the equivalent generator voltage, $-\mu \mathrm{E}_{\mathrm{k} 2}$, by the desired angle $\theta$. If $E_{R 1}$ leads $E_{k 2}$, as indicated in figure 1-154(B), the feed-back current through $C_{2}$ will be very nearly in phase with $\mathrm{E}_{12}$. The input impedance of $V_{1}$ will appear somewhat inductive, and close to series resonance with $\mathrm{C}_{2}$. The smaller that $\mathrm{C}_{2}$ is made, the higher will be the frequency. If the plate circuit of $\mathrm{V}_{2}$ is made inductive, $\mathrm{E}_{1_{2}}$ (not by changing $\theta$ ) can be shifted to be more nearly in phase with $\mathrm{E}_{81}$; however, such operation would tend to become unduly critical. For example, assume that $\mathbf{E}_{\mathrm{p} 2}$ were rotated to where it was in phase with $\mathbf{E}_{\mathbf{g} 1}$. This would mean that the phase of the feed-back current, $I_{g 1}$, with respect to $\mathrm{E}_{\mathrm{p} 2}$ was equal to its phase with respect to $\mathrm{E}_{k}$, and this in turn would require that the over-all $Q$ of $Z_{n 1}$ and $C_{2}$ in series be the same as the Q of $\mathrm{Z}_{\mathrm{y} 1}$ alone-an impossibility unless $\mathrm{C}_{2}$ is infinite. But $\mathrm{C}_{2}$ cannot be made large without the risk that the circuit will operate as an RC controlled multivibrator. Thus, in the circuit of figure 1-154, $\mathrm{E}_{\mathrm{p} 2}$ must lag $\mathrm{E}_{\mathrm{g} 1}$ if oscillations are to be maintained. The smaller the phase difference between $\mathrm{E}_{\mathrm{p} 2}$ and $\mathrm{E}_{\mathrm{g} 1}$, the less will be the leading component of $I_{g_{1}}$ with respect to $\mathrm{E}_{\mathrm{p} 2}$, and


Figure 1-154. (A) Basic circuit of the multivibrator type of parallel-resonant crystal oscillator. (B) Phosor diagram of $r$-f voltages of circuit shown in (A). $-E_{g}$ and $-E_{p ;}$ represent the phoses of the equivalent $V_{i}$ and $V_{i}$ generater voltages
the less will be the leading (inductive) component of $\mathrm{E}_{\mathrm{g} 1}$ with respect to $\mathrm{I}_{\mathrm{k} 1}$. Hence, the smaller the angle $\theta$, the more nearly must the crystal approach parallel resonance with the input capacitance of $V_{1}$. Any change in the $V_{1}$ plate circuit that tends to decrease $\theta$ therefore tends to raise the frequency. $\mathrm{C}_{\mathrm{k} 1}$ can be increased by the insertion of a fixed capacitance to make the total approach the rated load capacitance of the crystal unit.
1-346. Since the crystal unit is effectively a capacitance at all frequencies except those near its points of mechanical resonance, some precaution must be taken in the circuit design to ensure that the crystal maintains control over the frequency and that no danger exists that the two-stage circuit can perform as a free-running multivibrator with the frequency controlled by the RC constants. When $C_{2}$ in figure $1-154$ is small and $C_{k 1}$ is large by comparison, and when the plate impedances $R_{a}$ and $R_{b}$ are small by comparison with the $R_{p}$ of the tube, the feed-back voltage at the low frequencies corresponding to the RC time constants can quite easily be kept below the requirements for sustained oscillations.
1-347. No data is available concerning the relative frequency stability of the parallel-resonant multivibrator type oscillator, but, from qualitative considerations only, it would seem that a performance equal to, and very possibly superior to, that of the average Pierce circuit could be expected, although the operation of the circuit would certainly be much more critical. The $V_{1}$ amplifier stage can be designed to operate into a practically purely resistive load, so that fluctuations in the $V_{1}$ plate resistance will have little or no effect upon the frequency. On the other hand, under these conditions $\theta$ will be slightly negative and $-\mu \mathrm{E}_{\mathrm{g} 2}$ will lead $\mathrm{E}_{\mathrm{y}_{1}}$ unless a large reactance, or, preferably, a resistance, is connected in series with $C_{1}$. If $\theta$ is not critically small, the external circuit of $V_{2}$ can also be designed to appear as a pure resistance, and any variations in the plate resistance of the tube will have a negligible effect on frequency. The annulling of the stray-capacitance effects in the output circuits of the two tubes will require the use of coils, which may not be desirable if a wide frequency range is intended. The phase-shifting Qe of the feed-back circuit is computed in the same manner as in the Pierce and Miller circuits except that the required phase shift is much smaller.
1-348. In the design of such a circuit, the value of $\theta$ can be arbitrarily predetermined. Assume that when $R_{e}$ of the crystal unit is a maximum, the feed-back current, $I_{11}$, is to be in phase with $-\mu \mathrm{E}_{g 2}$.

With $\mathrm{R}_{k}$ assumed to be large compared with the average PI of the crystal unit, estimate the capacitance $C_{s}$, required across the crystal unit for the $Q$ of $Z_{k i}$ to equal the tangent of $\theta$ when the $X_{r}$ of the crystal unit corresponds to the reactance of the rated load capacitance. Make $C_{2}$ such that its reactance at the operating frequency is equal to the reactive component of $Z_{k 1}$ computed above. Under these conditions $I_{n}$ will lag $-\mu E_{k z}$ for all values of $R_{e}$ less than maximum, since the $Q$ of $Z_{k 1}$ would be greater than $\tan \theta$ if the frequency did not increase to bring $Z_{k 1}$ nearer its antiresonant value. But the increase in the frequency as a result of a decrease in $R_{*}$ is less than that which would occur if the circuit were designed so that $I_{p}$ woulc. lead $-\mu \mathrm{E}_{\mathrm{k} 2}$ for most values of $\mathrm{R}_{4}$. Also, if the feed-back circuit is designed for series resonance when $R_{e}$ is a maximum, the values of $C_{2}$ should prove more practical, the operation will be less critical, and there is the assurance that all values of $\mathrm{R}_{\text {. }}$ will permit oscillation. The plate-circuit impedances of the two tubes are next determined so that the feed-back voltage is sufficient to maintain oscillations when $R_{e}$ of the crystal unit is a maximum. Generally, neither tube should operate into a load exceeding 5000 ohms. The plate voltages are chosen so that the crystal unit cannot be driven beyond the rated drive level. With the phase characteristics of the circuit determined, more or less by design, to ensure a proper load capacitance for the crystal, it may be that the optimum operating voltage will be more readily determined through experiment. At equilibrium, the total voltage gain of the loop, from $E_{k 1}$ to $E_{111}$ to $E_{\mathrm{k}_{2}}$ to $\mathrm{E}_{122}$ and back to $E_{k}$, must be equal to unity. Thus,

$$
\begin{array}{r}
\mathrm{G}_{1} \mathrm{G}_{2} \mathrm{G}_{3} \mathrm{G}_{4}=\frac{\mathrm{E}_{\mathrm{1} 2}}{\mathrm{E}_{\mathrm{g} 1}} \cdot \frac{\mathrm{E}_{\mathrm{k} 2}}{\mathrm{E}_{\mathrm{p} 1}} \cdot \frac{\mathrm{E}_{\mathrm{v} 2}}{\mathrm{E}_{\mathrm{k} 2}} \cdot \frac{\mathrm{E}_{\mathrm{k} 1}}{\mathrm{E}_{\mathrm{p} 2}}=1 \\
1-348(1)
\end{array}
$$

where, referring to the circuit in figure 1-154,

$$
\begin{align*}
& G_{1}=E_{p 1} / E_{k 1}=\frac{\mu_{1} Z_{p 1}}{R_{p 1}+Z_{p 1}} \approx g_{m i} R_{n}  \tag{2}\\
& \mathrm{G}_{2}=\mathrm{E}_{\mathrm{q}^{2}} / \mathrm{E}_{\mathrm{p} 1} \approx 1 \\
& \text { 1-348(3) } \\
& G_{3}=E_{p 2} / E_{\mathrm{g} 2}=\frac{\mu_{2} Z_{p 2}}{R_{p 2}+Z_{p 2}}=E_{\urcorner 2} R_{b} \\
& \text { 1-348(4) } \\
& G_{4}=E_{\mathrm{g} 1} / \mathrm{E}_{\mathrm{p} 2}=1  \tag{5}\\
& \text { So } \\
& G_{1} G_{2} G_{3} G_{4}=g_{m 1} g_{m 2} R_{n} R_{b}=1 \tag{6}
\end{align*}
$$

Equation (6) is only a first-order approximation in which it is assumed the plate resistances of the tubes are very large compared with the external plate impedances, $Z_{p 1}$ and $Z_{v 2}$, which, in turn, are approximately equal to $R$. and $R_{b}$, respectively. Also, it is assumed that $X_{r i}$ is small compared with $Z_{x z}$, and that either $X_{c z}$ is small compared with $Z_{g 7}$ or the tendency towards a series-resonant rise in voltage across $Z_{k}$ is sufficient to make equation (5) approximately correct.

1-349. The output is most often taken from across a 500 - to 1000 -ohm resistance between the cathode of $V_{2}$ and ground. In this event, $R_{\varepsilon_{2}}$ connects directly to the cathode of $V_{2}$-not to ground. The cathode output is quite useful for matching to lowimpedance inputs, such as would occur, for example, when feeding a coaxial line. Regardless of where the output is obtained, it can be seen that its amplitude cannot be expected to greatly exceed that of the Pierce circuit. Since two amplifier stages are required and no additional gain is pro-
duced, there can be little advantage in using the multivibrator circuit unless thermostatic control of the temperature is employed and the design is such as to ensure greater frequency stability than can be achieved in the Pierce circuit. The use of a single dual-type tube offers greatest economy. The principal advantages of the circuit are its relative independence of fluctuations in the tube voltage, and its adaptability for impedance-matching to low-impedance output circuits.
1-350. Figure 1-155 illustrates three multivibra-tor-type crystal oscillators that were designed for use in Diversity Receiving Equipment AN/ FRR-3 ( ). Circuit (A) is a later-model replacement of circuit (B). Very possibly the preference for (A) is at least partly due to a desire to eliminate the variable effects of the inductors in (B) with changes in frequency. From the data available it cannot be said that the crystal in (B) is not actually operating at or very near its seriesresonance frequency. The state of operation of the


Figure 1-155. Two-stage parallal-resonant oseillators of the multivibrator type.

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | CR | $\mathbf{R}_{1}$ | R2 | $\mathbf{R}_{\mathbf{3}}$ | R ${ }_{4}$ | $\mathbf{R}_{5}$ | $\mathrm{R}_{8}$ | $\mathbf{R}_{7}$ | R. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Diversity Receiving Equipment AN/FRR-3A | Local oscillator | $1400-$ | $\begin{aligned} & \text { Holder } \\ & \text { FT-249 } \end{aligned}$ | 250 | 100 | 5 | 1.5 | 0.5 | 0.16 |  |  |
| (B) | Diversity Receiving Equipment AN/FRR-3 | Lacal osc. | $\begin{aligned} & 1400- \\ & 3800 \end{aligned}$ | Holder FT-269 (Entire circuit in $55^{\circ} \mathrm{C}$ oven) | 250 | 250 | 3 |  |  |  |  |  |
| (C) | Diversity Receiving Equipment AN/FRR-3A | BFO with AFC reactance tube, $V_{1}$ | 462.45 | - | 50 | 0.6 | 10 | 100 | 250 | 260 | 5 | 5 |

Circuit Data for Figure 1-155. Fin kc. $R$ in kilohnas. $C$ in $\mu \mu$. L in mh.


Figure 1-155. Continued

| R9 | $\mathrm{C}_{1}$ | Cs | C3 | C. | $\mathrm{C}_{5}$ | $\mathrm{C}_{6}$ | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | $L_{1}$ | $L_{2}$ | $\mathrm{V}_{1}-\mathrm{V}_{2}$ | $V_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 80 | 10 | 100 | 2000 |  |  |  |  |  |  | 68N7GT | 6AC7 |
|  | 10 | 200 | 75 | 50 | 20 | 100 | 50,000 | 100 |  | 2200 | 65N76T |  |
| 0.6 | 2000 | 100,000 | 39 | 250 | 50 | 10 | 100 | 2000 |  | 2200 | 6SN7 ${ }^{\text {at }}$ | 6 VBGT |

Section 1
crystal will vary quite widely with changes in the tuning of the $L_{1} \mathrm{C}_{3}$ tank. Circuit (C) is a beatfrequency oscillator which is crystal-stabilized when switch $S_{1}$ is in the crystal position, as shown. The triode-connected beam power tube serves as a reactance tube, which effectively shunts the crystal with a capacitance that varies with the bias supplied to the control grid of the tube. The bias, in turn, is controlled by the a-f-c diacriminator circuit in a teletype terminal. The purpose of the circuit is to ensure that the beat frequency remains constant even though the frequency of the incoming signal should vary slightly. If the beat frequency tends to drift, the sign and magnitude of the discriminator output causes the bias of the reactance tube to effectively change the load capacitance of the crystal unit in such a direction that the frequency of the oscillator rises or falls by approximately the same number of cycles per second as does the incoming signal.

## Oscillators with Crystals Heving Two Sets of Electrodes

1-351. The original crystal oscillator devised by Dr. Nicolson, as well as a number of the earlier crystal oscillators tested by Dr. Cady, employed crystals with, effectively, two pairs of electrodes. The basic circuit is shown in figure 1-156. The required phase inversion of the amplifier output voltage is provided by the crystal unit operating at a mode for which the polarities of the plate and grid terminals with respect to ground are 180 degrees out of phase. The circuit shown operates the crystal unit very near its series-resonance frequency. In practice, a capacitor is normally connected between crystal and ground, so that the circuit is more commonly employed for parallelmode tested crystal units. Still, it is not without some license that we classify this type of oscillator as a parallel-mode type. The crystals most applicable for this class of circuit are the very-lowfrequency elements of the $X$ group, which vibrate in lengthwise extensional or flexural modes. The electrode connections that permit the desired phase inversion depend upon the particular crystal element. Assume that electrodes numbers 1 and 3 are on one side of the crystal, and that 2 and 4 are on the opposite side, as indicated in figure 1-156(A). For a flexure element, such as element N , where electrodes 1 and 3 parallel each other down the length of the crystal, as shown in figure 1-156(B), the flexure mode is excited when the potential across 1 and 2 is oppositely polarized to that across 3 and 4. If the same electrode arrangement is to be used to excite an extentional mode
(or the flexural mode of the duplex element J) the polarities of the two sets of electrodes must be in phase. In this case, the connections of one set of electrodes should be reversed in the circuit shown in figure 1-156(A). For example, plates 2 and 3 should be connected to ground and plate 4 should be connected to the grid, if the proper phase inversion is to be obtained. A crystal having the two sets of electrodes at opposite ends of the crystal, as shown in figure 1-156(C), would be driven at the second harmonic of the length extensional mode (or of the flexural mode of a duplex crystal), if connected as shown in figure 1-156(A). Greater stability and a smaller crystal are possible for a given frequency by operating at the fundamental mode. To permit this, if the crystal unit is plated as shown in figure 1-156(C), the connections of one pair of electrodes should be the reverse of those shown in figure 1-156(A). If it can be assumed that the current in the grid circuit is negligible compared with the crystal current between terminals 1 and 2, and if the stray capacitance between the two sets of electrodes is ignored, the equivalent circuit between terminals 1 and 2 will appear approximately as shown in figure 1-156 (D). L, C, and $C_{0}$ represent the parameters of a fully plated crystal. A more exact analysis of this type of crystal unit can be found in the book "Electromechanical Transducers and Wave Filters" by W. P. Mason, D. Van Nostrand Co.
1-352. Figure 1-157 shows a practical oscillator design employing crystal units having two sets of electrodes. Although the electrode connections shown for CR would indicate that the plate and

(A)

(c)

(0)

Figure 1-156. Basic circuit of oscillator using arystal with two pairs of electrodes


Figure 1-157. Practical erystal-oscillator design employing very-low-frequency erystal unit with two sets of electrodes
grid terminals always connect to the same side of the crystal unit, the actual connections will depend upon the particular element used. The variable capacitor $C_{1}$ permits a frequency adjustment of approximately 60 parts per million. To ensure that the crystal unit is operating into its rated load capacitance, the exact frequency of a test crystal should be known when it is at series resonance with its rated capacitance. To a first approximation, the terminal that is to be connected to the grid can be assumed to be open-circuited, so that the resonance to be tested is that between the rated $\mathrm{C}_{\mathrm{x}}$ and one half of the crystal. With the test crystal connected in the oscillator circuit, $\mathrm{C}_{1}$ can be adjusted to provide an output at the previously measured "rated" frequency of the test crystal. This adjustment therefore will provide the rated load capacitance for all crystal units of the same type. The varistor is inserted to protect the crystal unit from overdrive, and to ensure a stable output voltage. As recommended by Bell Telephone Laboratory engineers, the nominal values of $\mathrm{R}_{1}, \mathrm{C}_{1}$, $\mathrm{C}_{3}$, and $\mathrm{C}_{3}$ that provide satisfactory operation in the 1.2 - to $10-\mathrm{kc}$ frequency range are given in the following table. The values shown will provide a direct current in M of approximately 12 microamperes.

| Frequency <br> Range <br> $(\mathrm{kc})$ | $\mathrm{R}_{1}$ <br> $(\mathrm{kil}-$ <br> ohms) | $\mathrm{C}_{1}$ <br> $(\mu \mu \mathrm{f})$ | $\mathrm{C}_{2}$ <br> $(\mu \mu \mathrm{f})$ | $\mathrm{C}_{3}$ <br> $(\mu \mu \mathrm{f})$ |
| :---: | :---: | :---: | :---: | :---: |
| $1.2-1.5$ | 100 | 180 | 4000 | 500 |
| $1.5-2.0$ | 100 | 180 | 3000 | 500 |
| $2.0-2.5$ | 100 | 150 | 2000 | 500 |
| $2.5-3.2$ | 100 | 150 | 1500 | 500 |
| $3.2-4.5$ | 100 | 120 | 1000 | 500 |


| Frequency <br> Range <br> $(\mathrm{kc})$ | $\mathrm{R}_{1}$ <br> $(\mathrm{kil}-$ <br> ohms $)$$\mathrm{C}_{1}$ <br> $(\mu \mu \mathrm{f})$ | $\mathrm{C}_{2}$ <br> $(\mu \mu \mathrm{f})$ | $C_{3}$ <br> $(\mu \mu \mathrm{f})$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $4.5-6.7$ | 100 | 120 | 700 | 250 |
| $6.7-8.0$ | 100 | 90 | 500 | 250 |
| $8.0-10.0$ | 51 | 90 | 1000 | 0 |

1-353. Figure 1-158 shows the crystal oscillator in Test Set TS-251/UP, which employs a duplex crystal element. The crystal circuit is used to synchronize the blocking oscillator at a frequency of 1818.18 cps . The output of the blocking oscillator is for counting down to 303.03 pulses per second, which, in turn, are used in checking Loran pulserepetition rates. A CR-11/U crystal unit is used which has a resonant frequency of $1817.44 \pm 0.3$ cps at $75^{\circ}$ Fahrenheit. The rated maximum effective resistance of the crystal is 30,000 ohms, and its rated maximum permissible current is 0.03 milliampere. The fixed capacitance paralleling the variable capacitance is used only if necessary. The varistor is rated at $1 \mathrm{ma} / 14 \mathrm{~V}$ for temperatures between 75 and 86 degrees Fahrenheit.

## Crystal and Magic-Eye Resonamee Indicator

1-354. An interesting application of a parallelresonant crystal circuit is the tuning indicator shown in figure 1-159. When the tuned frequency, $F_{1}$, of a variable oscillator is equal to the antiresonant frequency of the crystal unit in parallel with the input capacitance of $V_{1}$, a magic-eye tube, the excitation of $V_{1}$ is a maximum, as is the current through $R_{4}$, and, hence, also the shadow angle of the indicator. The circuit thus provides a constant visual crystal check on the tuned oscillator frequency. Different crystal units can be switched in for different channels.


Figure 1-158. Duplex-electrode crystal circuit in Test Set TS-251/UP for synchronixing blocking osellator at 1818.18 cps. Resistance is given in kilohms, capacitance in micromicroforads


Figure 1-159. Crystal and magic-eye resonance indicator

| Fig. | Equipment | $F_{1}$ | CR | $\mathrm{R}_{5}$ | $\mathrm{R}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Transmitter BC-696-A | $\begin{aligned} & 3000- \\ & 4000 \end{aligned}$ | $\begin{aligned} & \mathrm{DC}-8 \mathrm{C},-\cdots \\ & \mathrm{D},-\mathrm{K} \end{aligned}$ | 5.1 | 0.39 |
| (B) | Radio Transmitter BC-457-A | $\begin{aligned} & 4000- \\ & 5300 \end{aligned}$ | $\underset{\mathrm{D},-\mathrm{K}}{\mathrm{DC}-\mathrm{C},-}$ | 10 | 0.39 |
| (C) | Radio Transmitter BC-458-A | $\begin{aligned} & 5300- \\ & 7000 \end{aligned}$ | $\begin{aligned} & \mathrm{DC}-8-\mathrm{C} \\ & \mathrm{D},-\mathrm{K} \end{aligned}$ | 15 | $0.39^{\circ}$ |
| (D) | Radio Transmitler 3C-459-A | $\begin{aligned} & 7000 \\ & 9100 \end{aligned}$ | $\begin{aligned} & \mathrm{DC}-8-\mathrm{C} \\ & \mathrm{D},-\mathrm{K} \end{aligned}$ | 5.1 | 0.39 |

Circuit Data for Figure 1-159. F in ke. $R$ in kilohms. C in $\mu \mu$.

## SERIES-RESONANT CRYSTAL OSCILLATORS

1-355. For maximum frequency stability it is generally preferable to operate a crystal unit at its series-resonance frequency, but series-mode circuits are most widely used for overtone operation. At series resonance the crystal element appears as a resistance, so that in the normal circuit it can be short-circuited or replaced by a comparable resistance without stopping oscillations. Series-resonant oscillators generally have smaller outputs than do oscillators of the parallel-resonant type. Also, series-resonant oscillators usually require more circuit components, and hence are not often used except in the very-high-frequency range. In general, the operation of the series-mode circuits is less complicated than that of the parallel-mode oscillators. Nevertheless, the circuit design becomes increasingly critical at the higher frequencies and higher overtones. The stray capacitances must be kept to a minimum, and all leads must be as short as possible. It may be necessary to nullify the crystal shunt capacitance, $\mathrm{C}_{0}$, by connecting across the crystal unit an inductor that is antiresonant with $\mathrm{C}_{0}$ at the operating frequency. It may also be desirable to connect a capacitor in series with the crystal unit, to tune out the stray inductance of the crystal leads. Tuned circuits must be provided if a crystal unit is to be driven at a particular overtone mode. Quite often, satisfactory operation is obtained simply by designing a conventional variable-tuned oscillator to operate at the desired frequency, and then inserting the crystal unit in a plate tank or feed-back circuit. There will be a range of tuning adjustments in
which the crystal can assume control and hold the frequency very nearly constant. As the tuning adjustments are varied beyond this range, the control becomes quite unstable or ceases altogether. Usually, the region of stable control becomes smaller as the overtone order is increased. If broad-band operation is desired with no tuning adjustment other than the selector switch for changing the crystal, additional precautions must be taken to ensure that oscillations cannot be maintained except when the crystal impedance is small -that is, the crystal unit is operating near series resonance. For maximum frequency stability, the effective resistance of the circuit facing the crystal unit should be as small as possible. At the higher frequencies, the stray capacitances limit the impedances obtainable from the tuned circuits, thereby making them more selective and hence more effective in influencing the frequency and in increasing the instability.
1-356. The series-mode oscillators most widely recommended are listed in the following table, and rated according to their relative design and performance characteristics. A rating of 1 represents the top relative superiority in the corresponding characteristic. It should be understood that the ratings are based upon average qualitative results which might well be contradicted by the data of individual investigators. Any one of the seriesmode circuits expertly designed could surpass the performance of a poorly designed circuit rated higher in a particular characteristic. The fre-quency-stability rating assumes average oven and voltage regulation.

| $\mathbf{R}_{3}$ | $\mathbf{R}_{4}$ | $\mathbf{R}_{\mathbf{3}}$ | $\mathbf{R}_{6}$ | $\mathbf{C}_{\mathbf{1}}$ | $\mathrm{V}_{\mathbf{1}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.5 | 1000 | 51 | 0.02 | 50,000 | 1629 |
| 1.0 | 1000 | 51 | 0.02 | 50,000 | 1629 |
| 1.0 | 1000 | 51 | 0.02 | 50,000 | 1629 |
| 1.5 | 1000 | 51 | 0.02 | 50,000 | 1629 |

Section I
Crystal Oscillators

| Symbol of Oscillator | A | B | C | D | E | F | G | H | I | $J$ | K | $L$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency Stability (\%) | 0.0001 | 0.002 | 0.0005 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0002 | 0.0015 | 0.002 | 0.002 | 0.0015 |
| Power Output | 6 | 5 | 3 | 1 | 3 | 5 | 4 | 4 | 4 | 2 | 1 | 3 |
| Versatility | 4 | 4 | 2 | 1 | 2 | 3 | 2 | 3 | 3 | 3 | 2 | 3 |
| Upper Frequency Level | 5 | 1 | 3 | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 4 | 3 |
| High-Resistance Crystals | 2 | 5 | 3 | 4 | 4 | 4 | 2 | 4 | 4 | 4 | 1 | 3 |
| Ease of Adjustment | 6 | 7 | 1 | 3 | 2 | 2 | 2 | 5 | 5 | 5 | 4 | 5 |
| Untuned Bandwidth | 5 | 5 | 2 | 2 | 1 | 2 | 1 | 6 | 6 | 6 | 4 | 6 |
| Frequency Multiplication | 5 | 5 | 2 | 4 | 4 | 1 | 5 | 5 | 3 | 3 | 6 | 6 |
| Low Harmonic Output | 1 | 2 | 2 | 5 | 5 | 5 | 5 | 4 | 4 | 4 | 3 | 2 |
| Circuit Simplicity | 4 | 5 | 3 | 2 | 1 | 2 | 2 | 3 | 3 | 3 | 4 | 4 |
| Isolation from Load | 1 | 2 | 3 | 4 | 4 | 2 | 4 | 4 | 4 | 4 | 4 | 4 |
| Low-Frequeney Operation | 1 | 6 | 3 | 5 | 5 | 5 | 2 | 4 | 4 | 4 | 1 | 2 |

The oscillator symbols in the foregoing table correspond to the respective index letters of the oscillators listed below.

## Names of Series-Mode Oscillators

A. Meacham Bridge
B. Capacitance Bridge
C. Butler, or Cathode-Coupled
D. Grounded-Cathode, Transformer-Coupled Type
E. Grounded-Grid, Transformer-Coupled Type
F. Grounded-Plate, Transformer-Coupled Type
G. Transitron
H. Impedance-Inverting Transitron
I. Impedance-Inverting Pierce
J. Impedance-Inverting Miller
K. Grounded-Cathode Two-Stage Feedback
L. Modified Colpitts, C.I. Meter Type

## Meacham Bridge Oscillator

1-357. The Meacham bridge oscillator, illustrated in figure 1-160, provides the greatest frequency stability of any vacuum-tube oscillator yet devised, but the region of maximum frequency stability is limited to the lower frequencies because of the increased effect of the stray circuit capacitances when the frequency becomes greater than a few hundred kilocycles per second. The oscillator is of the crystal-stabilized type employing tuned circuits. At frequencies above 1000 kc the effect of the stray capacitance is sufficient to reduce the stability to a point where little is to be gained by the use of the Meacham circuit. The oscillator is principally employed with GT-cut crystals in frequency standards, to generate frequencies of 100 kc. In figure 1-160, it can be seen that if the bridge
were perfectly balanced there would be no excitation voltage. At the start of oscillations, the ratio of $R_{1}$ (practically equal to the series-arm $R$ of the crystal unit) to $R_{2}$ is smaller than the ratio of the $R_{3}$ to $R_{4}$. But $R_{4}$ is a thermistor - it is the resistance of a tungsten lamp which sharply increases in value as the temperature rises. (A semiconductor such as carbon, silicon, or germanium can be used, in which case the resistance will decrease with temperature. The negative temperature coefficient of the semiconductor is generally larger than the positive coefficient of tungsten, but the semiconductor thermistor is more expensive and is much more difficult to duplicate because of its great sensitivity to impurities.) As oscillations build up, the current through $\mathrm{R}_{\text {, increases to a }}$ point where the heat generated from the power losses raises the the thermistor temperature, and hence the resistance, to a point where the bridge is almost balanced. Equilibrium is reached when the imbalance of the bridge is just sufficient to supply heat to the thermistor at the same rate at which it escapes. For maximum amplitude stability, the ambient temperature of $R_{4}$ should not be permitted to vary over a wide range. Normally, the tungsten lamp will heat to a dull red of approximately 600 degrees centigrade. A variation of over 100 degrees in the ambient temperature could have a significant effect on the equilibrium power losses in the thermistor, if extreme precision were desired. The operating temperature of the lamp is very low compared with the rated temperature, and consequently the lamp can be expected to last indefinitely. The oscillator should be designed and adjusted so that the phase shift occurs entirely in the bridge. That is, the tube should operate into

Section 1


Figure 1-160. Basic circuit of Meacham bridge-stabilized ascillator
a pure resistance, so that the instant the plate current is maximum the peak transformer voltages should occur with polarities as indicated in figure 1-160. Transformers having powdered-iron, toroidal cores can provide a coefficient of coupling very close to unity in the low-frequency range. The following analysis of the frequency stability and the activity stability of the Meacham oscillator, except for minor deviations and extensions, has been guided by the postulates and basic considerations as presented by W. A. Edson.*

## FREQUENCY STABILITY OF MEACHAM BRIDGE OSCILLATOR

1-358. First, we shall assume that the vacuum tube in figure 1-160 operates into a purely resistive load, and that the entire phase reversal takes place in the bridge transformer. The phasor diagram in figure 1-161 (A) shows the relation of the voltage $E_{0}$ to the other voltages of the bridge network. (Refer to figure 1-160 for voltage symbols.) Next, assume that some change in the capacitance of the circuit requires that $\mathrm{E}_{0}$ be shifted in phase by a very small angle equal to $\phi$, but that the change is so small that the magnitude of all the bridge voltages can be assumed to remain constant. In order to produce the phase shift $\phi$, it can be seen that $E_{2}$, and hence the current through $R_{2}$, must be rotated by an angle $\theta$. In a triangle with angles $A$ and $B$ opposite to sides $a$ and $b$, respectively,

[^2]$\frac{a}{\sin A}=\frac{b}{\sin B}$ (Law of Sines). Likewise, in the triangle $\mathrm{E}_{0} \mathrm{E}_{3} \mathrm{E}_{4}$,
$$
\mathrm{E}_{0} / \sin \theta=\mathrm{E}_{4} / \sin \phi
$$
or
$$
\sin \theta=\frac{E_{o}}{E_{t}} \sin \phi
$$

Since we are assuming that both $\theta$ and $\phi$ are very small, equation (1) can be written, approximately,

$$
\begin{equation*}
\theta=\frac{\mathrm{E}_{o}}{\mathrm{E}_{4}} \phi \tag{2}
\end{equation*}
$$

$$
1-358
$$


(A)

(B)

Figure 1-161. Phasor diagrams of bridge voltages in Meacham oscillator. Angles $\phi$ and $\theta$ (greatly magnified) represent small shifts in phase when crystal unit is operating slightly off series resonance

The current through the input transformer can be assumed to be negligible compared with the total current through the crystal, so the current through $R_{2}$ is essentially the same as that through the crystal. Under these conditions, as is shown in paragraph 1-241,

$$
\begin{equation*}
\theta=\tan \theta=\frac{X_{e}}{R_{1}+R_{2}}=\frac{2 L \Delta \omega}{R+R_{2}} \quad 1-358 \tag{3}
\end{equation*}
$$

where $L$ and $R$ are series-arm parameters of the crystal unit. By rearranging equation (3) and dividing by $\omega$, the fractional change in frequency required to produce an angle $\theta$ is found to be

$$
\frac{\Delta \omega}{\omega}=\frac{\theta\left(\mathrm{R}+\mathrm{R}_{2}\right)}{2 \omega \mathrm{~L}}=\frac{\theta \mathrm{R}_{\mathrm{o}} \sqrt{\mathrm{C}}}{2 \sqrt{\mathrm{~L}}}
$$

where $R_{c}=R+R_{2}$ is the total resistance of the crystal side of the bridge, and $C$ is the series-arm capacitance. On substitution of equation (2) in equation (4), it is found that

$$
\frac{\Delta \omega}{\omega}=\frac{\phi \mathrm{E}_{0} \mathrm{R}_{\mathrm{e}}}{2 \mathrm{E}_{4}} \cdot \sqrt{\frac{\mathrm{C}}{\mathrm{~L}}}
$$

Equation (5) indicates that the more nearly balanced the bridge (the smaller the $\mathrm{E}_{0} / \mathrm{E}_{4}$ ratio), the greater will be the frequency stability.

Now,

$$
\begin{equation*}
E_{4}=\frac{R_{4} E_{8}}{R_{3}+R_{4}} \tag{6}
\end{equation*}
$$

Letting $\left(R_{3}+R_{4}\right) / R_{4}=\left(R_{1}+R_{2}\right) / R_{2}=m, w e$ see that $E_{0} / E_{4}=\frac{m E_{0}}{E_{5}}$.
Also, since

$$
\begin{align*}
E_{0} & =E_{4}\left(\frac{R_{3}}{R_{8}+R_{4}}-\frac{R_{1}}{R_{1}+R_{2}}\right) \\
& =E_{0}\left(\frac{R_{3}}{R_{T}}-\frac{R_{1}}{R_{0}}\right) \tag{7}
\end{align*}
$$

where $\mathrm{R}_{\mathrm{T}}=\mathrm{R}_{\mathrm{g}}+\mathrm{R}_{4}$, then

$$
E_{0} / E_{4}=m\left(\frac{R_{3}}{R_{T}}-\frac{R_{1}}{R_{c}}\right)=R_{3} / R_{4}-R_{1} / R_{2}
$$

On substitution in equation (5), we have

$$
\begin{equation*}
\frac{\Delta \omega}{\omega}=\left(\frac{R_{2} R_{3}-R_{1} R_{i}}{R_{2} R_{4}}\right) \frac{R_{c} \phi}{2 \sqrt{L / C}} \tag{8}
\end{equation*}
$$

It now remains to determine the magnitude of $\phi$ for a small change in the capacitance of the circuit. The most likely changes in capacitance take place in the grid circuit, the average $\Delta \mathrm{C}_{\mathrm{z}}$ usually being on the order of 10 times the average $\Delta C_{p}$ in the plate circuit. Looking away from the grid, it can be seen that when the bridge is very nearly balanced, the grid faces a resistive impedance

$$
R_{z}=\frac{N_{\mathrm{z}}{ }^{2}\left(R_{1}+R_{3}\right)\left(R_{2}+R_{4}\right)}{R_{1}+R_{2}+R_{3}+R_{4}}
$$

The capacitance $\mathrm{C}_{\mathrm{g}}$ will have been adjusted to be effectively antiresonant with the leakage inductance of the transformer, which inductance can be imagined to be in parallel with $\mathrm{R}_{\mathrm{F}}$. Still looking away from the grid, we can imagine a generator connected between grid and cathode. If the capacitance should change by a small amount $\Delta C_{k}$, the ratio of the excess reactive component of current to the resistive component becomes $\mathrm{R}_{\boldsymbol{z} \omega} \Delta \mathrm{C}_{\mathrm{g}}$. This will equal the tangent of the phase shift, $\phi$, which is sufficiently small for $\tan \phi$ to be assumed to equal $\phi$. Thus, with $\phi=\mathrm{R}_{\varepsilon} \omega \Delta \mathrm{C}_{k}$, on substituting equation (9) for $R_{z}$, equation (8) becomes

$$
\begin{align*}
\frac{\Delta \omega}{\omega}= & \left(\frac{R_{2} R_{3}-R_{1} R_{4}}{R_{2} R_{4}}\right) \cdot \frac{\left(R_{1}+R_{3}\right)\left(R_{2}+R_{4}\right)}{\left(R_{1}+R_{2}+R_{3}+R_{4}\right)} \\
& \cdot \frac{R_{c} N_{\mathrm{c}}^{2} \Delta C_{8}}{2 L}
\end{align*}
$$

Now, let us assume that $R_{1}$ and $R_{3}$ remain fixed. As $R_{1}$ is varied, $R_{4}$ must vary in direct proportion to keep the bridge balanced. If $\mathrm{R}_{3}=k R_{1}, \mathrm{R}_{4}$ will always approximately equal $\mathrm{kR}_{2}$. Substituting these values of $R_{3}$ and $R_{4}$ in all terms where the error introduced can be considered negligible, equation (10) becomes

$$
\frac{\Delta \omega}{\omega}=\frac{R_{1}^{2}\left(k R_{2}-R_{4}\right)(1+k)}{k R_{2}} \cdot \frac{N_{k}^{2} \Delta C_{2}}{2 L}
$$

1-358 (11)
If $R_{4}$ is expressed as being equal to $R_{3}(k-i)$, equation (11) becomes

$$
\frac{\Delta \omega}{\omega}=\frac{(1+k) i R_{1}^{2} N_{8}^{2} \Delta C_{8}}{2 k L}
$$

1-359. Equation 1-358 (12) does not quite indicate the relations among all the circuit parameters that are effective in providing an optimum fre-
quency stability. It is first necessary to determine how $i$, which is a measure of the imbalance in the circuit, is dependent upon the other parameters. For this purpose, it is necessary to find that value of $i$ which must exist in order for the feed-back voltage to be at equilibrium. It will be assumed that the r-f plate current, $I_{p}$, is equal to $g_{m} E_{g}$. If this assumption is not warranted, $g_{m}$ in any of the following equations can be replaced by $\mu /\left(R_{p}+Z_{p}\right)$. To a first approximation,

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{p}}=\mathrm{N}_{\mathrm{p}}^{2} \mathrm{R}_{\mathrm{e}} \mathrm{R}_{\mathrm{T}} /\left(\mathrm{R}_{\mathrm{c}}+\mathrm{R}_{\mathrm{T}}\right) \tag{1}
\end{equation*}
$$

and
$\mathrm{E}_{\mathrm{G}}=\mathrm{E}_{\mathrm{p}} / \mathrm{N}_{\mathrm{p}}=\mathrm{I}_{\mathrm{p}} \mathrm{Z}_{\mathrm{p}} / \mathrm{N}_{\mathrm{p}}=\mathrm{g}_{\mathrm{m}} \mathrm{E}_{\mathrm{g}} \mathrm{N}_{\mathrm{p}} \mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{T}} /\left(\mathrm{R}_{\mathrm{c}}+\mathrm{R}_{\mathrm{T}}\right)$
1-359 (2)
also, $\mathrm{E}_{\varepsilon}=\mathrm{N}_{\mathrm{r}} \mathrm{E}_{0}$, and $\mathrm{E}_{\mathrm{o}}$ is given by equation $1-358(7)$. On substitution in equation (2)

$$
\begin{array}{r}
1=g_{m} N_{p} N_{\mathrm{s}}\left(R_{c} R_{3}-R_{1} R_{T}\right) /\left(R_{c}+R_{T}\right) \\
1-359(3)
\end{array}
$$

Equation (3) is the equilibrium feed-back equation for the Meacham oscillator. On expressing $\mathrm{R}_{3}$ and $R_{1}$ as functions of $R_{1}$ and $R_{2}$, it is found that at equilibrium

$$
\begin{equation*}
\mathrm{i}=\frac{(1+\mathrm{k}) \mathrm{R}_{\mathrm{c}}}{g_{\mathrm{m}} N_{\mathrm{p}} N_{\mathrm{g}} R_{1} R_{2}} \tag{4}
\end{equation*}
$$

Substituting (4) in equation 1-358 (12)

$$
\begin{equation*}
\frac{\Delta \omega}{\omega}=\frac{(1+k)^{2} R_{1} R_{c} N_{g} \Delta C_{g}}{2 k g_{m} R_{2} N_{p} L} \tag{5}
\end{equation*}
$$

In a similar manner, in equating $\phi$ to $\mathrm{Z}_{\mathrm{p}} \omega \Delta \mathrm{C}_{\mathrm{p}}$, it can be shown that for small changes in the plate capacitance

$$
\begin{equation*}
\frac{\Delta \omega}{\omega}=\frac{R_{\mathrm{c}}{ }^{3} \mathrm{~N}_{\mathrm{p}} \Delta C_{\mathrm{p}}}{2(1+k) \mathrm{g}_{\mathrm{m}} \mathrm{R}_{2}{ }^{2} \mathrm{~N}_{\mathrm{z}} \mathrm{~L}} \tag{6}
\end{equation*}
$$

It can be seen that greater stability is to be had when $g_{m}$ is a maximum and when the ratio $m=$ $R_{k} / R_{g}$ is small. For changes in $C_{g}$, the optimum value of $k$ is 1 (when $(1+k)^{2} / k$ passes through a minimum). For changes in $\mathrm{C}_{\mathrm{p}}$, it would be desirable to have k as large as practicable. A further consideration is to so proportion the parameters that the expected variations in $\mathrm{C}_{\mathrm{g}}$ and $\mathrm{C}_{\mathrm{p}}$ will have the maximum opportunity to cancel in their effects.

Also, caution must be taken that in improving the stability in one respect, it is not impaired to a greater extent in another. Since the expected $\Delta C_{5}$ is approximately 10 times the expected $\Delta C_{v}$, the ratio of the right-hand sides of equations (5) and (6) can be equated to 1 , with $10 \Delta C_{p}$ substituted for $\Delta \mathrm{C}_{\mathrm{g}}$. On thus dividing (5) by (6)

$$
1=\frac{10(1+k)^{3} R_{1} R_{2} N_{g}{ }^{2}}{k R_{e}{ }^{2} N_{\mathrm{p}}{ }^{2}}
$$

or

$$
\begin{equation*}
\cdot N_{p}^{2} / N_{\mathrm{g}}{ }^{2}=\frac{10(1+k)^{3} R_{1}}{k m R_{t}}=\frac{10(1+k)^{5}(m-1)}{k^{2} m^{2}} \tag{7}
\end{equation*}
$$

With the oscillator designed according to equation (7), average capacitance variations in the plate and grid circuits will have approximately equal effects upon the frequency. When the square root of equation (7) is combined with equations (5) and (6), and $R_{c}$ is expressed as $m R_{1} /(m-1)$,

$$
\begin{equation*}
\frac{\Delta \omega}{\omega}=\frac{\Delta \mathrm{C}_{\mathrm{g}} \mathrm{~m}^{2} \mathrm{R}_{1}}{2 \mathrm{~L} \mathrm{~g}_{\mathrm{m}}} \sqrt{\frac{1+\mathrm{k}}{10 \mathrm{k}(\mathrm{~m}-1)}} \cdot 1-359 \tag{8}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{\Delta \omega}{\omega}=\frac{\Delta \mathrm{C}_{\mathrm{p}} \mathrm{~m}^{2} \mathrm{R}_{\mathrm{i}}}{2 \mathrm{~L} \mathrm{~g}_{\mathrm{m}}} \sqrt{\frac{10(1+\mathrm{k})}{\mathrm{k}(\mathrm{~m}-1)}} \tag{9}
\end{equation*}
$$

$$
1-359
$$

If the oscillator is to be designed on the basis of equation (7), it can be seen that $k$ should be made as large as is practicable, and m should be such that the factor $\mathrm{m}^{2} / \sqrt{\mathrm{m}-1}$ is a minimum. It can be shown that this occurs when

$$
m=4 / 3
$$

Frequency stability, of course, is not the only consideration; there are also the vacuum-tube and thermistor characteristics and the power rating of the crystal unit that must be taken into account in deciding upon the optimum parameter relations. Remember, that in equations (4), (5), and (6), $\mathrm{g}_{\mathrm{m}}$ can be replaced by the more exact term $\mu /\left(R_{p}+Z_{p}\right)$. Certainly, a high-mu tube is to be preferred, and when it is operated class A the sec-ond-harmonic output can be expected to be at least 65 db below the fundamental. The screen voltage should be fairly high, in order to increase $\mathrm{g}_{\mathrm{m}}$. Normal operating voltages can be employed, but $\mathrm{E}_{g}$ should not be allowed to drive the grid positive.

## aCTIVITY STABILITY OF MEACHAM BRIDGE OSCILLATOR

transformer, we see that at equilibrium the product of the gains of all the stages, from $E_{o}$ back to $\mathrm{E}_{\mathrm{o}}$, must be equal to 1 . Thus,


From equation 1-358(12) it can be seen that in the interest of frequency stability, $i$, and hence the imbalance of the bridge should be as small as possible. Fortunately, this condition also agrees with the requirements of high activity stability, for the smaller the difference of the actual thermistor resistance from a value equal to $\mathrm{kR}_{2}$, the larger will be the percentage change in that difference for a small change in the thermistor voltage. Equation 1-358(7) can be written

$$
\begin{equation*}
E_{o}=G_{4} E_{s}=i R_{1} R_{2} E_{s} / k R_{c}{ }^{2} \quad 1-360 \tag{1}
\end{equation*}
$$

where $\mathrm{i}=\left(\mathrm{k} \mathrm{R}_{2}-\mathrm{R}_{4}\right) / \mathrm{R}_{2}$ and $\mathrm{G}_{4}$ is the gain of the stage. In the over-all gain equation, above, $G_{3}$ and $G_{3}$ can be considered constant, so that $G$, primarily has the function of compensating any changes in $\mathrm{G}_{2}$ of the vacuum tube. From equation (1), it can be seen that $\mathrm{iE}_{\mathrm{s}} / \mathrm{E}_{\mathrm{o}}$ can be considered a constant. Or, in the over-all gain equation we see that

$$
\begin{equation*}
\mathrm{G}_{1} \mathrm{G}_{2} \mathrm{G}_{3} \text { i } \mathrm{R}_{1} \mathrm{R}_{2} / \mathrm{k} \mathrm{R}_{\mathrm{c}}{ }^{2}=1 \quad 1-360 \tag{2}
\end{equation*}
$$

or that

$$
\mathrm{G}_{2} \mathrm{i}=\mathrm{k} \mathrm{R}_{\mathrm{c}}{ }^{2} \mathrm{~N}_{\mathrm{p}} / \mathrm{R}_{1} \mathrm{R}_{2} \mathrm{~N}_{\mathrm{g}}=\text { constant }
$$

On differentiating,

$$
\mathrm{idG} \mathrm{~g}_{2}+\mathrm{G}_{2} \mathrm{di}=0
$$

or

$$
\frac{\mathrm{di}}{\mathrm{i}}=-\frac{\mathrm{dG}_{2}}{\mathrm{G}_{2}}
$$

Equation (3) shows that for a given percentage change in the gain of the tube, the smaller the value of $i$, the smaller need $b=$ the change in $R_{4}$ to restore equilibrium. Since $G_{2} \approx g_{m} Z_{1}$, we can write

$$
\begin{equation*}
\mathrm{di} / \mathrm{i}=-\mathrm{dg}_{\mathrm{m}} / \mathrm{g}_{\mathrm{m}} \tag{4}
\end{equation*}
$$

On differentiating $\mathrm{iE}_{\mathrm{n}} / \mathrm{E}_{\mathrm{o}}=\mathrm{C}$, where C is a constant, we find that

$$
\mathrm{idE}+\mathrm{E}_{\mathrm{s}} \mathrm{di}-\mathrm{CdE}=0
$$

If the effects on $E_{q}$ due to the changes in $E_{s}$ and i exactly cancel so that $\mathrm{dE}_{o}=0$, then, by equations (3) and (5)

$$
-\mathrm{dG}_{2} / \mathrm{G}_{2}=\mathrm{di} / \mathrm{i}=-\mathrm{dE} \mathrm{E}_{\mathbf{3}} / \mathrm{E}_{\mathrm{s}}
$$

Under these circumstances it can be seen that the percentage change in the activity is exactly equal to the change in the gain of the tube. If the thermistor is to be effective in preventing the amplitude of the output from changing significantly with changes in $\mathrm{G}_{2}$, clearly an increase in $\mathrm{E}_{n}$ must produce a decrease in $\mathrm{E}_{0}$. We can define the activity sensitivity of the bridge to be

$$
\begin{equation*}
\mathrm{s}=-\mathrm{E}_{\mathrm{n}} \mathrm{di} / \mathrm{idE} \mathrm{E}_{\mathrm{n}} \tag{6}
\end{equation*}
$$

The sensitivity is thus defined as the percentage variation in i per percentage variation in the voltage across the bridge. The problem now is to convert equation (6) into a function (equation 14) of the circuit constants so that $s$ can be predetermined by the design engineer. From equations (5) and (6) we find that the percentage change in $E_{\text {o }}$ per percentage change in $E_{\mathbb{k}}$ is

$$
\begin{equation*}
-\frac{\mathrm{E}_{\mathrm{s}} \mathrm{dE}_{o}}{\mathrm{E}_{\mathrm{o}} \mathrm{dE}}=\mathrm{s}-1 \tag{7}
\end{equation*}
$$

In practice, $\mathrm{E}_{0} / \mathrm{E}_{\mathrm{n}}\left(=\mathrm{G}_{4}\right)$ can be on the order of 0.003 or smaller; so, if the change in $\mathrm{E}_{\mathrm{o}}$ is comparable to that of $\mathrm{E}_{\mathrm{x}}$ in magnitude, excellent amplitude stability will be achieved. The stability depends first upon the magnitude of $i$, and secondly, upon the sensitivity of the thermistor. The latter is defined as

$$
\begin{equation*}
S=\frac{E_{4} d R_{4}}{R_{4} d E_{4}}=\frac{d\left(\log R_{4}\right)}{d\left(\log E_{4}\right)} \tag{8}
\end{equation*}
$$

Figure 1-162 shows the resistance-voltage characteristics of a number of tungsten lamps for ambient temperatures at room values. For lower ambient temperatures, the curves would be shifted to the right somewhat, and for higher temperatures, to the left. Since the curves are plotted on log paper, according to equation (8) it can be seen


Figure 1-162. Resiseance of rypical fungsten lamps versus applied voltage and power dissipation when the ambient temperature is $300^{\circ} \mathrm{Kelvin}$ scale (approximately $27^{\circ} \mathrm{C}$ )
that the thermistor sensitivity $S$ at a given value of $E_{4}$ is the actual slope of a curve at that point. It is important, of course, to operate the thermistor at a voltage where the slope approaches a maximum. It is convenient to express the bridge $s$ as a function of the thermistor $S$.

Since $i=\frac{k R_{2}-R_{4}}{\mathbf{R}_{2}}$, then

$$
\begin{equation*}
\mathrm{di}=-\frac{\mathrm{d} R_{4}}{\mathrm{R}_{2}}=-\frac{\mathrm{kd} R_{4}}{R_{4}} \tag{9}
\end{equation*}
$$

or

$$
s=-\frac{E_{2} d i}{i d E_{4}}=\frac{k E_{s} d R_{4}}{i R_{4} d E_{*}}=\frac{k S}{i}\left(\frac{E_{s} d E_{4}}{E_{4} d E_{5}}\right)
$$

Now, $E_{1}=E_{2}-E_{0}=E_{2}$, but $d E_{4}\left(=d E_{2}-d E_{0}\right)$ is not approximately equal to $\mathrm{dE}_{2}$. So $\mathrm{dE}_{4} / \mathrm{E}_{4}=$ $\left(\mathrm{dE}_{2}-\mathrm{dE} \mathrm{E}_{0}\right) / \mathrm{E}_{2}=\left(\mathrm{dE}_{\mathrm{a}}-\mathrm{mdE}_{0}\right) / \mathrm{E}_{3}$, where $\mathrm{m}=$ $\frac{\mathbf{R}_{\mathrm{c}}}{\mathrm{R}_{2}}=\frac{\mathbf{E}_{\mathrm{s}}}{\mathbf{E}_{2}}$. On substitution for $\mathrm{dE} / \mathrm{E}_{4}$ in equation (10), we find

$$
s=\frac{k S}{i}\left(1-\frac{m d E_{o}}{d E_{\mathrm{o}}}\right)
$$

$1-360$ (11)

By equation (7) we see that $\mathrm{dE}_{\mathrm{o}} / \mathrm{dE}_{\mathrm{s}}=$ $\mathrm{E}_{\mathrm{o}}(1-\mathrm{s}) / \mathrm{E}_{\mathrm{w}}$. On substitution in (11) and after
rearranging, we have

$$
s=\frac{k S E_{s}-m k S E_{o}}{i E_{s}-m k S E_{o}}
$$

The term $\mathrm{mkSE}_{0}$ in the numerator can be considered negligible, and dropped. After expressing $E_{o}$ in terms of equation (1) and rearranging, it is found that

$$
\mathrm{s}=\mathrm{kSR}_{\mathrm{c}} / \mathrm{i}\left(\mathbf{R}_{\mathrm{c}}-\mathbf{S R}_{1}\right)
$$

Finally, on substituting for its value given by equation 1-359(4), we are able to express the activity sensitivity entirely in terms of the known circuit parameters. Thus,

$$
\begin{aligned}
& s=\frac{k S g_{m} N_{p} N_{g} R_{1} R_{2}}{(1+k)\left(R_{0}-S R_{1}\right)} \\
& \text { or } \quad 1-360(14) \\
& s=k S g_{m} N_{p} N_{g} R_{1} /(1+k)[m-S(m-1)]
\end{aligned}
$$

The reciprocal of s can be considered the percentage gain in the output voltage (or in $E_{p}$ or $E_{s}$ ) for a unit percentage change in the gain of the tube, since $d G_{2} / G_{2}$ is equal to $-d i / i$. In the equation for $s$, note that if the thermistor sensitivity were equal to $R_{c} / R_{1}$, the stability mathematically would be infinite. Since $R_{c} / R_{1}$ is greater than 1, a single tungsten lamp could not provide the thermistor sensitivity for the above condition to hold unless special measures were available to reduce the heat leakage from the filament. The effective sensitivity could be increased if $R_{2}$ were replaced by another tungsten lamp, and the crystal unit were inserted in the plaee of $\mathrm{R}_{2}$. Theoretically, the sensitivity can be made much larger than unity simply by varying the ambient temperature together with the operating temperature of the filament; for instance, by constructing a thermistor with the filament mounted inside a heater sleeve and controlling the heater current by feedback from a later amplifier stage. If equation (14) is taken apart, it will be found that the denominator term, $\left(R_{c}-S R_{1}\right)$, originates from that component of dE , that is equal to $-\mathrm{dE}_{\mathrm{o}}$. When there is an increase in $\mathbf{E}_{n}$, the voltage $E_{4}$ changes in two ways: one is due to the change in the current through $\mathrm{R}_{4}$, and the other is due to the increase in the resistance, itself. It is the latter component that is approximately equal to $-\mathrm{dE}_{0}$. Mathematically, the change in $\mathrm{E}_{4}$ is expressed by the differential equation

$$
d E_{4}=d\left(I_{4} R_{4}\right)=R_{4} d I_{4}+I_{4} d R_{4}
$$

Since $\mathrm{dR}_{4} / \mathrm{R}_{4}$ is equal to $\mathrm{SdE}_{4} / \mathrm{E}_{4}$, on substitution in equation (15) it can be shown that

$$
\begin{equation*}
\mathrm{dR}_{4}=\mathrm{S}\left(\frac{\mathrm{R}_{4} \mathrm{dI}_{4}}{\mathrm{I}_{4}}+\mathrm{dR}_{4}\right) \tag{16}
\end{equation*}
$$

1-360
If $S$ is greater than 1 , an increase in voltage across $R_{\text {, must result in a decrease in current. (Inciden- }}$ tally, since the change in $\mathrm{R}_{4}$ is actually due to a change in the temperature brought about by an increase in power, a value of $S$ greater than unity implies that the percentage increase in resistance is at least equal to twice the percentage decrease in current.) Now, assuming that the current through the input transformer is negligible, $\mathrm{E}_{\mathrm{s}}=\mathrm{I}_{4} \mathrm{R}_{\mathrm{T}}$, and $\mathrm{dE}_{\mathrm{a}}=\mathrm{I}_{4} \mathrm{dR}_{4}+\mathrm{R}_{\mathrm{T}} \mathrm{dI}_{4}$, where $\mathrm{dR}_{4}=$ $\mathrm{dR}_{\mathrm{T}}$. If $\mathrm{E}_{\mathrm{s}}$ is to remain constant, that is, if $\mathrm{dE}_{\mathrm{s}}$ is to equal zero for a small change in the gain of the tube, $\mathrm{dI}_{4} / \mathrm{I}_{4}$ must equal - $\frac{\mathrm{dR}_{4}}{\mathrm{R}_{\mathrm{m}}}$. If the latter value is substituted in equation (16), it will be found that for conditions of $s=\infty$ :

$$
\begin{equation*}
\mathrm{S}=\frac{\mathrm{R}_{\mathrm{T}}}{\mathbf{R}_{\mathrm{T}}-\mathrm{R}_{4}}=\frac{\mathrm{R}_{\mathrm{T}}}{\mathrm{R}_{3}}=\frac{\mathrm{R}_{\mathrm{c}}}{\mathbf{R}_{1}} \quad 1-360 \tag{17}
\end{equation*}
$$

This is the explanation of the term ( $\mathrm{R}_{\mathrm{c}}-\mathrm{SR}_{2}$ ) in the denominator of equation (14). Other than the assumption that the changes in the current $I_{0}$ through the grid transformer can be considered negligible in their effect upon $\mathrm{dE}_{4}$, the term is entirely a function of the $R_{s}$ and $R_{4}$ arms of the bridge, and is not related to the gain characteristics of the rest of the circuit. No experimental data is available concerning the operation of the Meacham bridge oscillator with values of $S$ greater than unity, when $R_{4}$ behaves as a negative resistance (an increase in $\mathrm{E}_{4}$ is accompanied by a decrease in $\mathrm{I}_{4}$ ). Theoretically, if S were greater than $R_{c} / R_{1}$, an increase in the $g_{m}$ of the tube would ultimately result in a decrease in the output-voltage and in the voltage applied across the bridge. In an actual circuit, whether stable values of $\mathrm{R}_{4}$ would be maintained under such conditions is open to question. Perhaps the thermal lag of the filament and the extreme sensitivity of $\mathrm{E}_{\mathrm{o}}$ would so influence the operation that $\mathrm{R}_{4}$ would periodically overshoot its mark and prevent an unmodulated equilibrium from being reached. In practice, the values of $S$ will be on the order 0.5 , so such considerations do not arise. For $s$ to be as large as possible, referring to equation (14), it can be seen that $[k /(1+k)]$ should be as large as practicable. This agrees with the equations for frequency stability if the circuit is to be designed according to equation 1-359(7). The term $[k /(1+k)]$ has
no maximum, but approaches unity as k increases indefinitely. Assume that $s$ is equal to 50 . This means that a change in the gain of the tube of 1 per cent will cause a change of only one-fiftieth of 1 per cent in the output voltage. Or in terms of db , since

$$
\begin{align*}
s & =-\frac{E_{\mathrm{a}}}{d \mathrm{E}_{4}} \cdot \frac{\mathrm{di}}{\mathrm{i}}=-\frac{\Delta(\log \mathrm{i})}{\Delta\left(\log \mathrm{E}_{\mathrm{s}}\right)} \\
& =\frac{\Delta\left(\log \mathrm{G}_{2}\right)}{\Delta\left(\log \mathrm{E}_{\mathrm{p}}\right)}=\frac{\Delta \mathrm{db} \text { in tube gain }}{\Delta d \mathrm{ib} \text { output }} 1-360 \tag{18}
\end{align*}
$$

an increase of 0.5 db in the gain of the tube will cause only a $0.01-\mathrm{db}$ increase in the output.

## CRYSTAL DRIVE LEVEL CONSIDERATIONS IN MEACHAM BRIDGE OSCILLATOR

1-361. A starting consideration in the design of a Meacham bridge oscillator is that the crystal unit is not to be overdriven. If $P_{1}$ is the crystal power,
$I_{c}=\sqrt{P_{1} / R_{1}}$ is the crystal current, and

$$
E_{s}=I_{c} R_{c}=\frac{m R_{1}}{m-1} \sqrt{\frac{P_{1}}{R_{1}}}=\frac{m \sqrt{P_{1} R_{1}}}{m-1}
$$

With $R_{1}$ determined by the crystal unit, it is desirable, from the point of view of frequency stability, for $m$, and hence $R_{2}$ to have small optimum values. If $S$ approaches unity, the small $R_{2}$ will also be an important consideration in activity stability, but for normal values of $S$ the activity stability is improved slightly if $\mathrm{R}_{2}$ is large. The term $\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{\mathrm{c}}-\mathrm{SR}_{1}}\right)$ in equation 1-360 (14) has no maximum, but approaches unity as $\mathrm{R}_{2}$ is increased indefinitely and $R_{1}$ and $S$ are held constant. Usually, the requirements of frequency stability are the more important, and $\mathrm{R}_{2}$ should be kept as small as practical thermistor resistances and values of $k$ permit. At low frequencies, values of $R_{1}$ may be in the neighborhood of 1000 ohms or more. The voltage across the thermistor will be

$$
E_{4}=\frac{E_{a}}{m}=\frac{I_{c} R_{1}}{m-1}=\frac{E_{1}}{m-1}=\frac{\sqrt{P_{1} R_{1}}}{m-1}
$$

where $E_{1}$ is the voltage across the crystal unit. For convenience, we repeat equation 1-360 (1), but expressed as a function of $m$ and $k$ :

$$
\begin{equation*}
\mathrm{E}_{0}=(m-1) \mathrm{i} \mathrm{E}_{\mathrm{s}} / \mathrm{km}^{2} \tag{3}
\end{equation*}
$$

The power dissipation in $\mathrm{R}_{4}$ is

$$
\begin{array}{r}
P_{4}=E_{4} I_{4}=E_{1} I_{e} /(m-1) k=P_{1} /(m-1) k \\
1-361(4)
\end{array}
$$

The impedance of the bridge in terms of $R_{1}$ is

$$
\begin{equation*}
\mathbf{Z}_{\mathrm{m}}=\mathbf{R}_{\mathrm{c}} \mathbf{R}_{\mathrm{T}} /\left(\mathbf{R}_{\mathrm{c}}+\mathbf{R}_{\mathrm{r}}\right)=\mathrm{km} R_{1} /(1+k)(\mathbf{m}-1) \tag{5}
\end{equation*}
$$

The plate impedance of the tube is

$$
\begin{equation*}
Z_{p}=N_{p}^{2} Z_{n}=\frac{N_{p}^{2} k m R_{1}}{(1+k)(m-1)} \quad 1-361 \tag{6}
\end{equation*}
$$

The plate voltage is

$$
E_{p}=I_{p} Z_{p}=\frac{g_{m} E_{p} N_{p}^{2} k m R_{1}}{(1+k)(m-1)} \quad 1-361(7)
$$

Also,

$$
\begin{equation*}
E_{p}=\dot{N}_{p} E_{s}=m N_{p} \sqrt{P_{1} R_{1}} /(m-1) \tag{8}
\end{equation*}
$$

1-361
and

$$
\begin{equation*}
E_{g}=N_{\mathbf{g}} E_{o} \tag{9}
\end{equation*}
$$

Finally, we repeat equation $1-359$ (3), the over-all equation for feed-back equilibrium, but expressed in terms of $R_{1}, m$, and $k$ :

$$
\begin{equation*}
G_{1} G_{2} G_{a} G_{4}=\frac{g_{m} N_{p} N_{\mathrm{g}} i R_{1}}{m(1+k)} \quad 1-361 \tag{10}
\end{equation*}
$$

$R_{2}$ can be adjusted to provide the same value of $m$ for each different crystal unit. Under these circumstances, $E_{*}$ and $\mathbf{E}_{\mathrm{p}}$ will be the same in each oscillator, even though $R_{2}$ varies. Two fundamental problems are that the design must ensure that the crystal current does not overdrive the crystal unit when $\mathbf{R}_{1}$ is small, and that the thermistor current is sufficient for $S$ to be a maximum.

## DESIGN PROCEDURE FOR MEACHAM BRIDGE OSCILLATOR

1-362. The fixed point of reference for estimating the current and voltage at any point in the Meacham circuit is the thermistor voltage $E_{4}$. This is the voltage that is required to make $R_{4}=R_{s} /(m-1)$. If $R$, and $m$ are held constant, $E_{4}$ as well as $E_{4}\left(=m E_{4}\right)$ and $E_{4}\left(=N_{8} E_{4}\right)$ will also be constant. If $\mathbf{P}_{\mathrm{cm}}$ is the rated crystal power, $R_{m}$ is the maximum series resistance of the crystal unit, and $\frac{R_{m}}{N}$ is the minimum expected resistance of the crystal unit, then, by equation 1-361 (2), Es must not be greater than the value

$$
\begin{equation*}
(\max ) E_{4}=\frac{\sqrt{P_{\mathrm{cm}} R_{m}}}{(m-1) \sqrt{N}} \tag{1}
\end{equation*}
$$

Since the Meacham oscillator is most applicable for use in the low-frequency range where crystal units having resistances in the neighborhood one or more thousand ohms are not uncommon, the risk is greatly increased that an exceptionally well-mounted crystal will have a resistance of as little, as, perhaps, $R_{m} / 25$. Also, since the Meacham circuit is primarily useful as a precision oscillator, an additional safety factor should be allowed to prevent the crystal unit from being driven beyond its test specifications. For these reasons, it is suggested that in the absence of prior experience or manufacturer's recommendations for a given type of crystal unit, the Meacham design for frequencies below 200 kc assume a minimum R of $R_{m} / 25$, rather than $R_{m} / 9$ as was assumed in the case of the parallel-resonant oscillator design. However, it can still be assumed that the most probable crystal unit will have an $R=R_{m} / 3$. If the crystal unit to be used is a precision GT cut, a safety factor as large as $N=25$ netd not be made. In any event, crystal units having resistances less than $R_{m} / 9$ can be expected to be extremely rare, and if $N=9$ is considered a sufficient safety factor, an output voltage two-thirds greater can be realized than if N is assumed to be 25. A crystal unit having a resistance less than $\mathrm{R}_{\mathrm{m}} / 9$ would be driven beyond its test level, but far below a level that could damage the crystal. Since the resistance is already low, an increase in resistance with overdrive would do more good than harm. The only concern is that the frequency of a borderline crystal may deviate beyond the tolerance limits. Such a risk could be checked during a production test, but would subtract from the reliability of crystal replacements in the field. In equation 1-361 (10), it can be seen that when $k$ is a minimum (when $R_{1}=R_{m}$ ), the imbalance, as measured by $i$, is a minimum. When $k$ is large, the percentage changes in ( $k+1$ ) and in $R_{1}$ are very nearly equal, so that the imbalance tends to vary as the square of $\mathrm{R}_{1}$. k should be chosen for maximum frequency stability under variations of $\mathrm{C}_{\mathrm{r}}$, assuming that the crystal unit resistance is its most probable value (approximately $\mathrm{R}_{\mathrm{m}} / 3$ ). According to equation 1-359 (5), with all else fixed, the percentage change in frequency is a minimum when $k=1$. The most probable optimum value of $k$, therefore, fixes $R_{s}$ as equal to $R_{m} / 3$. Thus, for any random value of $R_{1}$,

$$
\begin{equation*}
\mathrm{k}=\mathrm{R}_{\mathrm{m}} / 3 \mathrm{R}_{1} \tag{2}
\end{equation*}
$$

Next, a value of $m$ equal to $4 / 3$ (see equation 1-359 (10) ) should be chosen, to provide maximum frequency stability on the assumption that equations $1-359$ (8) and (9) are to apply when $R_{1}$ is its most probable value. After this is done, a safety factor of N should be selected, and the maximum value of $\mathrm{E}_{4}$ should be determined by equation (1), such that it will not require a bridge voltage sufficient to overdrive the crystal unit when $R_{l}$ is equal to $R_{m} / N$. Next, a thermistor is chosen that will provide a value of $R_{4}=\frac{R_{3}}{m-1}$ when $E_{4}$ is equal to, or less tnan, the maximum value determined above. Next, the ratio $\mathrm{N}_{\mathrm{p}} / \mathrm{N}_{\mathrm{p}}$ can be determined, using equation $1-359$ (7) with the assumption that $k=1$ and $m=4 / 3$. This gives a ratio $\frac{\mathrm{N}_{4}}{\mathrm{~N}_{\mathrm{g}}}=\sqrt{15} \approx 4$, which value thus provides the greatest probability that random changes in $\mathrm{C}_{\mathrm{E}}$ and $\mathrm{C}_{1}$ can cancel when $\mathrm{R}_{1}$ is its most probable value. The next step is to select a tube with high
class-A $g_{m}$ and $R_{p}$. A 6AC7 would be very satisfactory. Using equation 1-361 (6), determine $N_{p}$ on the assumption that $Z_{p}=\frac{R_{p}}{10}$ when $R_{:}=\frac{R_{m}}{3}$. Now, $\mathrm{N}_{\mathrm{p}}$ can be made equal to $\mathrm{N}_{\mathrm{n}} / 4, \mathrm{R}_{2}$, of course, must be variable over a percentage range comparable to that to be expected from the crystal unit. Normal tube voltages are used. The other circuit components can be determined according to the tube specifications for class-A operation and the special output requirements of the oscillator. $\mathrm{E}_{\mathrm{p}}, \mathrm{E}_{8}, \mathrm{E}_{0}$, $I_{1}, I_{1}$, etc can be determined from the equations in paragraph 1-361, the frequency stability from equations $1-359$ (5) and (6), and the activity stability from equation $1-360$ (14) for maximum, most probable, and minimum values of $\mathrm{R}_{2}$.

## MODIFICATIONS OF MEACHAM BRIDGE DESIGN

1-363. Two designs of the Meacham bridge stabilized oscillator are shown in figure 1-163. In each


Figure 1-163. Meacham bridge-stabilized oscillators

| Fig. | Equipment | Purpose | $F_{1}$ | CR | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | R4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Control-Monitor IP-68/CPN-2A | Timing osc. Controls indicator sweep íreq and prr of shoran station | 186.22 | Oven controlled | 0.1 | Thermistor | 250 | 0.12 |
| (B) | Radio Set AN/FRC-10 | Carrie: osc and phase-shift circuit | 100 | WECO D-163897 $\stackrel{\text { 아 }}{\mathrm{D}} \mathrm{-169649}$ | 0.1 | 0.1 | 0.5 | 2 |

Circuit Data for Figure 1-163. Fin ke. R in kilohms. C in $\mu \mu \mathrm{f}$. L in $\mu \mathrm{h}$.
of these circuits inductor-capacitor combination has been connected in series with the crystal unit. Obviously the combination is intended to be resonant at the crystal frequency. The variable arrangement shown in figure 1-163 (A) permits the frequency to be pulled to a more exact value if desired, the crystal unit (if necessary) operating with a reactive component in its impedance. Or, in case the tube operates into a partly reactive load, the tuning elements in the bridge could permit the crystal, itself, to operate at exactly series resonance. The series inductor and capacitor are effective in aiding the initial build up of oscillations and in ensuring that the crystal assumes control at the frequency of the desired mode. It can also be presumed that the LC combination in the bridge improves the waveform somewhat and reduces the small distortion introduced by the tungsten lamp. This distortion is due to the fact that the filament cools at least to some extent during the time that
the current alternates from its effective value in one direction to its effective value in the opposite direction. At frequencies above 100 cycles per second this distortion in the waveform is not serious. At radio frequencies it is normally small compared with the distortion introduced by the tube. The resistance $R$. in figure 1-163 (A) appears to be inserted in order to maintain a constant tube load by minimizing the variations in the bridge impedance due to adjustments and to crystal units having difference resistances. In figure 1-163 (B) note that the crystal unit is grounded. This is the usual arrangement. The parallel primary windings of the grid transformer in the same figure suggest that the arrangement is an adaption of a readily available transformer, very probably of the same construction as the one in the plate circuit. The parallel primary connection is in the direction of phase addition. Because the near-unity coupling between the coils effectively doubles the


Figure 1-163. Cominued

| Rs | R* | $\mathrm{R}_{7}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{C}_{3}$ | $\mathrm{C}_{4}$ | Cs | $\mathrm{C}_{6}$ | $\mathrm{C}_{7}$ | $\mathrm{V}_{\mathrm{i}}$ | $\mathrm{V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 22 | 1.8 | 0.56 | 110 | 40 | 300 | 100,000 | 10,000 | 300 | 10,000 | 6AU6 | $2 \mathbb{C}_{51}^{1 / 2}$ |
| 0.15 | 0.072 | 0.5 | 140 | 140 | 100 | 100 | 500,000 | 500,000 | 500,000 | $\begin{aligned} & \text { WECo } \\ & \text { 337A } \end{aligned}$ |  |

## Section 1

## Crystal Oscillators

inductance of each, the parallel connection provides the same step-up arrangement and primary impedance that would be provided by only one of the coils if used alone, but with a reduction in the leakage inductance. A Meacham bridge-stabilized oscillator can be designed employing two or more tubes. On the average, slightly better frequency stability can be achieved with a two-tube circuit, but only in rare instances are the additional cost, space, and weight requirements worth the small improvement in performance. Perhaps, at frequencies in the neighborhood 1000 kc or higher the two-tube arrangement could be more profitable than the one-tube stage. The design of a multistage bridge oscillator can be practically the same as that of the one-stage circuit except that the tube gain, $G_{2}$, is replaced by $G_{21} G_{22} \ldots G_{2 n}$, where $G_{2 k}$ is the voltage gain of a transformation stage between the output and input of the bridge, and where $n$ is the total number of such transformations. By increasing the number of positive-db stages, the bridge i can be made as small as desired, and the frequency and activity stability will be increased in proportion to the gain. It is because the possible gain is unlimited for all practical purposes that the Meacham oscillstor represents the ultimate in precision control of the frequency. In the final analysis the limiting condition is the degree to which the crystal parameters, themselves, can be kept constant. Figure 1-164 shows the basic circuit of a two-tube Meacham oscillator that employs no transformers and offers the advantage of only a single tuned stage. Although the design equations are somewhat different from those of the conventional one-tube stage, the same basic approach is to be employed, and the problems to be encountered can be solved similarly to those of the transformer-coupled circuits.

## Capacitance-Bridge Oscillators

1-364. Capacitance-bridge oscillators may possibly prove suitable for use in the $v$-h-f range. Their advantage lies in the fact that a properly balanced capacitance bridge cannot provide sufficient feedback of the proper phase to sustain oscillations at any frequency other than the tuned frequency of the circuit, provided a crystal unit is connected in the circuit that has a resonant mode of vibration at the tuned frequency. A properly balanced capacitance-bridge oscillator is thus crystal-con- ${ }^{+}$ trolled, rather than crystal-stabilized. On the other hand, if the bridge is not balanced, the circuit can operate as a free-running oscillator, which may or may not be crystal-stabilized. For the purpose of ensuring operation of crystal units at designated very high harmonic modes, the capacitance bridge, if not the most dependable, is at least as dependable as any other so far tested. The principal disadvantage of this type of circuit is that rather critical tuning adjustments must be made, $i$ and one crystal unit cannot replace another unless these adjustments are repeated. Largely on this account the circuit is not to be preferred for frequencies below 50 mc , and perhaps not below 75 ma mc. Nevertheless, once the bridge is properly ad!" justed, the operation with a crystal unit free of spurious modes is dependable under any extremes in temperature that can be reasonably expected.

## BASIC CIRCUIT OF CAPACITANCEBRIDGE OSCILLATOR

*1-365. Figure 1-165 illustrates the basic circuit

* The discussion in paragraph $1-365$ is based upon the analysis of the basic circuit appearing in the report, H.F. Harmonic Crystal Investigation, by S. A. Robinson and F. N. Barry of Philco Corporation, on Army Contract \#W38-088 ac-14172, 1947.


Figure 1-164. Two-stage Meacham bridge-stabillzed oscillator
 tor with the two sides wound on the same form and tightly coupled together. The induced-voltage effect is equivalent to that of a single generator connected across both coils and driving the bridge with an emf $\left(E_{p}+E_{s}\right) \approx E_{p}\left(N_{p}+1\right)$. $N_{p}$ the turns ratio of $L_{p}$ to $L_{s}$, is usually, and most conveniently, equal to 1 . In case the shunt capacitance of the crystal unit is greater than $10 \mu \mu \mathrm{f}$, it would be desirable to make $\mathrm{N}_{\mathrm{p}}$ slightly greater than 1. An $\mathbf{N}_{\mathrm{p}}$ greater than 1 but less than 2 can be expected to provide a higher output, but the operation will tend to be more critical and the frequency less stable. Before the circuit is placed in operation, the bridge must be balanced at an off-resonance frequency, so that no voltage can appear across the grid circuit. At an off-resonance frequency the crystal unit appears as a capacitance $\mathrm{C}_{\mathrm{o}}$, so that under the conditions of balance

$$
\frac{X_{C b}}{X_{C o}}=\frac{X_{L_{p}}}{X_{L b}}=\frac{C_{o}}{C_{b}}=\frac{L_{p}}{L_{b}}=N_{p}^{2}
$$

With $N_{p}=1, C_{b}$ is adjusted to equal $C_{0} .\left(C_{p}\right.$ is here assumed to include $C_{p m}$, and $L_{p}$ to account for $\mathrm{C}_{\mathrm{p}}$. See figure 1-165 (B).) The total capacitance

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range over which the bridge can be considered balanced. $\mathrm{C}_{\mathrm{b}}$ must be adjustable over the expected capacitance range of the particular type of crystal unit to be used. $\mathrm{C}_{1}$ is the tuning capacitance. For crystal-controlled operation, $\mathrm{C}_{1}$ is adjusted so that the total circuit capacitance $\mathrm{C}_{\boldsymbol{T}}$ is approximately resonant with the total inductance at the operating frequency. To balance the circuit, $\mathrm{C}_{1}$ is set to a position that tunes the bridge to a frequency well off the resonance frequency of the crystal unit. Referring to figure 1-165 (C), it can be seen that $\mathrm{E}_{\mathrm{g}}$ equals ( $\mathrm{E}_{\mathrm{g}}+\mathrm{E}_{\mathrm{CR}}$ ). At the tuned frequency, $R$ can be neglected and the crystal unit considered as a capacitance, $\mathrm{C}_{0}$. Approximately, $\mathrm{E}_{\mathrm{a}}$ and $\mathrm{E}_{\mathrm{cR}}$ are 180 degrees out of phase, and therefore tend to annul each other. Now, assume that $\mathrm{C}_{\mathrm{b}}$ is made to approach zero. $\mathrm{I}_{4}$ and $\mathrm{E}_{\mathrm{CR}}$ therefore become negligible, and the circuit behaves as if the crystal side of the bridge were open-circuited at $C_{b}$. The remaining circuit would be simply a Hartley oscillator with the crystal unit serving as a blocking capacitor between the inductor and the grid. If $\mathrm{C}_{\mathrm{b}}$ is gradually increased, $\mathrm{E}_{\mathrm{CB}}$ builds up until a point is reached where $E_{\text {s }}$ effectively is canceled and $E_{g}$ is insufficient to sustain oscillations. $\mathrm{C}_{\mathrm{b}}$ should then be increased one more increment beyond the oscillation cutoff. At this setting of $\mathrm{C}_{b}$, the bridge can be considered properly balanced, but a check should first be made that oscillations do not occur at other settings of $\mathrm{C}_{1}$ well removed from its value for crystal control. If such oscillations do occur, the adjustment of $\mathrm{C}_{\mathrm{b}}$ should be repeated. The free-running oscillations can be distinguished from the crystal-controlled oscillations by the continuous nature of their activity curves as measured by grid current and output meters when $\mathrm{C}_{1}$ is varied above and below a discontinuous region. A discontinuous point indicates an abrupt


Figure 1-165: (C) Simplified equivalent circuit
change to crystal control, where the frequency begins to change at a much slower rate with variations in circuit capacitance. However, once the bridge is balanced, no oscillations occur except near the crystal resonance frequency, in which region the bridge balance is upset.
1-366. Referring again to figure $1-165$ (C), with the circuit balanced, suppose that $C_{1}$ is gradually increased from its minimum value. At some point oscillations suddenly start; as $C_{3}$ is further increased, the activity builds up to a maximum and then sharply declines, as is illustrated in figure 1-166. Note also the sharp decrease in frequency when maximum amplitude is approached. Apparently, when oscillations first begin, the crystal appears inductive. $E_{C R}$ therefore has a large component in phase with $\mathrm{E}_{\mathrm{s}}$, and the circuit is essentially a modified Miller oscillator. Also, the ratio of I, to $I_{3}$ is a maximum, since $E_{c a}$ tends to cancel the voltage across $C_{b}$. As $C_{1}$ is slowly increased, the frequency and the inductive reactance of the crystal drop. This means that the effective $Q$ of the grid circuit also decreases. Although the presence of the capacitance $C_{1}$ modifies the phase relations, the circuit performs fundamentally as a Miller oscillator. $L_{n}$ can be interpreted as something of a booster inductor to increase the effective inductance of the crystal unit, and $I_{3}$ can similarly be viewed as a booster current to boost the voltage across the inductive component in the grid circuit without, at the same time, increasing the voltage across the crystal $\mathrm{R}_{\mathrm{e}}$. That the capacitance-bridge circuit actually has the same characteristics as does the Miller circuit is well illustrated by the similarities between the curves of figure 1-166 and the equivalent curves for the Miller oscillator shown in figure 1-144. Note that for both oscillators, the circuit capacitance for maximum excitation does not coincide with, but is smaller than, the value for maximum output. One significant difference between the two circuits is the fact that the Miller circuit cannot maintain the proper feedback phase if the crystal is operated at series resonance, whereas the capacitance-bridge circuit can, because of the presence of $L_{n}$. Where oscillation cutoff for the Miller circuit is above the seriesresonance frequency of the crystal, it is below the series-resonance frequency in the capacitancebridge circuit.
1-367. If the crystal control is to be fully effective, the series-arm resistance must be small compared with the shunt reactance, $\mathbf{X}_{\mathbf{c o}}$. A 'thougi. this requirement becomes increa ingl* diff at at the higher harmonics, $i$, of ${ }^{n}$ f.e whievet, even at frequencies well above 100 m . Assuming that


Figure 1-166. Typical performance curves of capacitance-bridge oscillator, showing effects of change in bridge tuning copacitonce on voltage oufput, activity (d-c grid current), and frequency
the series-arm $R$ is not more than one-tenth the magnitude of $\mathrm{X}_{\mathrm{co}_{0}}$, then the approximate equation for the effective crystal reactance, $X_{e}=$ $\mathrm{X}_{\mathrm{E}} \mathrm{X}_{\mathrm{Co}} /\left(\mathrm{X}_{\mathrm{C}_{0}}+\mathrm{X}_{\mathrm{s}}\right)$, where $\mathrm{X}_{\mathrm{t}}=4 \pi \mathrm{~L} \Delta \mathrm{f}$ series-arm reactance, is sufficiently close for an interpretation of the capacitance-bridge performance. Now, oscillations cannot start unless $\left|\mathbf{X}_{\mathrm{cb}}\right|>\mathbf{X}_{\mathrm{e}}+\mathrm{X}_{\mathrm{Le}}$. $X_{\text {cb }}$ we shall assume is equal to $X_{c o}$ under the conditions of balance. $X_{0}$ is equal to $\left|X_{c_{0}}\right|$, and hence to $\left|\mathrm{X}_{\mathrm{cb}}\right|$, when $\mathrm{X}_{\mathrm{s}}=-\mathrm{X}_{\mathrm{co}} / 2$, that is, when the crystal unit is halfway between series resonance and antiresonance. Thus, when oscillations start, the crystal frequency must be much nearer to the resonant than to the antiresonant state. Also, the plate circuit must appear inductive to the vacuum tube to a degree dependent upon the effective $Q$ of the grid circuit. This means that $I_{1}$ must be slightly greater than ( $\mathrm{I}_{2}+\mathrm{I}_{3}+\mathrm{I}_{4}$ ). In figure 1-165 (A), it can be seen that the crystal unit operates into a load reactance approximately equal to the parallel combination of $\mathrm{C}_{1}$ and the inductor ( $\mathrm{L}_{\mathrm{p}}+\mathrm{L}_{\mathrm{s}}$ ) in series with $\mathrm{C}_{\mathrm{b}}$. As the reactance of $\mathrm{C}_{1}$ approaches that of the inductor, the reactance of the parallel combination rises very sharply, and a small change in $\mathrm{C}_{1}$ can make a large change in the load reactance across the crystal unit. More than any other factor, this is the reason for the sharp dip in the frequency curve as $\mathrm{C}_{1}$ approaches a maximum.
1-368. It is not possible to tell at which point in
the curve the crystal passes through series resonance. Since at series resonance the reactance of $\mathrm{C}_{1}$ in parallel with $\mathrm{L}_{\mathrm{p}}$ and $\mathrm{L}_{\mathrm{a}}$ is equal, approximately, to - $\mathrm{X}_{\mathrm{cb}}$, the resonance frequency may well be below the knee of the curve for a crystal having a very small $\mathrm{C}_{0}$ (conditions for large $\mathrm{X}_{\mathrm{cb}}$ and nearparallel resonance of $\mathrm{C}_{2}$ with the inductor) and above the knee for crystals of larger $C_{0}$. At series resonance, if R is small $\mathrm{I}_{4}$ approximately equals $\mathrm{I}_{3} \mathrm{C}_{\mathrm{b}} / \mathrm{C}_{1}$. Assuming that $\mathrm{E}_{0}\left(=\mathrm{I}_{\mathbf{2}} \mathrm{X}_{\mathrm{i}_{9}}\right)$ leads $\mathrm{E}_{\mathrm{cR}}\left(=\mathrm{I}_{4} \mathrm{R}\right)$ by 90 degrees, the effective $Q$ of the grid circuit at series resonance is equal to $\mathrm{E}_{\mathrm{s}} / \mathrm{E}_{\mathrm{ca}}$. When $\mathrm{E}_{\mathrm{n}}$ and $\mathrm{E}_{\mathrm{CR}}$ are expressed as functions of $\mathrm{I}_{3}$, $\mathrm{C}_{\mathrm{b}}, \mathrm{C}_{1}$, and $\mathrm{X}_{\mathrm{L} .,}$, it can be shown that (series resonance) $Q_{s}=\frac{E_{s}}{E_{C R}}=\frac{X_{L_{s}}\left(C_{1}+C_{b}\right)}{R^{\prime} C_{b}}$. The above equation is only a broad approximation in the $v$-h-f range, since all the distributed parameters have been ignored, particularly the grid capacitance and the resistance of the inductor. However, it does indicate that the larger the ratio of $\mathrm{C}_{4}$ to $\mathrm{C}_{b}$, or, equivalently, $\mathrm{X}_{\mathrm{c}_{0}} / \mathrm{X}_{\mathrm{c}}$, the smaller the inductive phase shift that will be required in $E_{p}$, and the more nearly will the bridge tank approach parallel resonance. If $R$, or rather the total grid losses, should increase or decrease, the frequency will decrease or increase, respectively. It seems safe to assume that crystal units having the larger values of $\mathrm{RC}_{0}$ products will operate fairly near their

## Section I Crystal Oseillators

series-resonant state. This is due partly to the fact that the smaller the $\mathrm{X}_{\mathrm{co}} / \mathrm{R}$ ratio, the smaller the frequency range between resonance and antiresonance. Crystal units having the smaller values of $\mathrm{RC}_{\mathrm{s}}$ will perform with greater amplitude and frequency stability if operated above series resonance. Unfortunately, crystal units in the v-h-f range are tested only for series resonance. The greater likelihood of the occurrence of unwanted modes increases the importance of having the circuit designed so that the operation of the crystal unit lies within its tested specifications. While the capacitance bridge is excellent for preventing all modes of oscillation except the one desired, it is not a true series-mode oscillator, although it is so classified because its v -h-f application requires the use of crystals that are only series-tested. Rather, the oscillator is something of a hybrid between a Miller and a stabilized Hartley circuit. In the interest of frequency and amplitude stability, the circuit should be adjusted to operate above the knee of the frequency curve. A setting of the tuning capacitance corresponding to a grid current of 50 per cent of the maximum possible provides, approximately, the optimum output voltage and operating state nearest series resonance that are consistent with the operating region of better stability. The peak of the voltage-output curve in figure 1-166 corresponds closely to the adjustment for maximum tank impedance, which certainly occurs below series resonance where the crystal unit appears as a capacitance. The larger the capacitive reactance that the crystal unit can have and still permit oscillations, the more nearly can series-resonance oscillations fall within the higher stability region. For this purpose, the ratio of $L_{p}$ to $L_{p}$ and of $C_{b}$ to $C_{o}$ should be as large as unity, or greater, when the capacitance-bridge oscillator is to be used with series-tested crystal units.

## DESIGN MODELS FOR CAPACITANCEBRIDGE OSCILLATORS

1-369. The circuits shown in figures 1-167 through 1-171 represent five different modifications of the capacitance-bridge oscillator. These circuits were designed and tested by the research team of S. A. Robinson and F. N. Barry of Philco Corporation. No single type of circuit was found to be superior for operation over the entire tested frequency range of 50 to 200 mc , but each circuit has advantages for certain applications. The inductive arms of the bridge can be a single, self-supporting tapped inductor having an inside diameter of onequarter inch or greater. Silver-plated AWG No. 16
wire can be used. The tuning and balancing capacitances are small air capacitors. The fixed capacitances are, for the most part, the button-mica Erie type. Composition resistances are used, having nominal values of $\pm 10$ per cent. Successful operation of any of the circuits depends largely upon arranging the circuit components to permit the shortest possible leads, and all components should be of small physical size. Silver-plating of the components is desirable, and careful shielding and the use of low-loss insulating materials is necessary. Without good shielding and well-insulated capacitor shafts, it may be impossible to adjust the bridge properly because of the effects of hand capacitance. Transmit-time effects become quite significant as the frequency is increased beyond 50 mc . The lag in the response of the plate current with rapid changes in the grid voltages is equivalent to the circuit behavior that would result if an inductance were connected in series with $\mathrm{R}_{\mathrm{r}}$ of the tube. The lower the plate voltage, the larger is the apparent inductance and its accompanying tendency to lower the frequency. Usually, this effect makes it easier to operate the crystal unit at series resonance, but the need for careful $\mathbf{B}^{+}$ regulation becomes all the more important. For normal voltages, transit lag is approximately 0.2 degree per megacycle in v-h-f tubes such as the 6AK5.

## SINGLE-TUBE, 50- TO 90-MC CAPACITANCE-BRIDGE OSCILLATOR

1-370. The circuit shown in figure 1-167 has been operated at frequencies as high as 135 mc , but its particular merit lies in its performance at frequencies between 50 and 90 mc . When operated in the high-stability region, output up to 10 volts can be obtained, although care should be taken that the rated drive level of the crystal is not exceeded. Outputs of 2 milliwatts into an inductively coupled $100-\mathrm{ohm}$ resistor can be obtained in the same operating region.

## COMPACT', MINIATURE, 50- TO 120-MC CAPACITANCE-BRIDGE OSCILLATOR

1-371. The circuit shown in figure 1-168 is particularly suited for construction as a small, packaged, plug-in oscillator. If desired, several such oscillators of different frequencies can be designed as interchangeable units of the associated equipment. The entire shielded unit need not occupy a space greater than 6 cubic inches. The maximum frequency at which this circuit was found to oscillate was 156 mc , but the activity at that frequency was less than one-tenth that at 50 mc . At 120 mc the activity is approximately one-fourth of that at


Figure 1-167. A single-tube capacifance-bridge oscillator which is practical for operation in the $50-90-m \mathrm{~m}$ frequency range. Resistors not otherwise specified are $1 / 2 \mathrm{w}$. L-1 and L-2 are a single center-tapped coil of suitable inductance


Figure 1-168. A plug-in cupacitence-bridge oscillator which is prectical for $50-150-\mathrm{mc}$ frequency range

50 mc , so 120 mc appears to be the most practical upper frequency limit. A subminiature tube having high transconductance is used. Greater output is to be achieved with a triode, but greater frequency stability is to be had with a pentode. With a triode, the comparatively large plate-to-grid capacitance which shunts the balancing condenser may make it difficult to achieve a balancing capacitance as small as that of the crystal unit. This condition requires that the L-2A section of the bridge inductor be somewhat larger than the L-2B section. The possible output is reduced thereby, but the crystal unit will be operated nearer its series-resonance frequency. The output secondary, $L_{1}$, can be a single turn coupled to the plate end of $L_{2}$.

## CAPACITANCE-BRIDGE OSCILLATOR FOR GREATER POWER OUTPUT IN THE 50- TO 80-MC RANGE

1-372. The circuit shown in figure 1-169 was designed for the purpose of achieving a maximum power output without regard to the rated drive level of the crystal unit. However, none of the crystals used were fractured during the experiments. The higher-power circuit is essentially the same as that of figure 1-167 except that the $\mathrm{N}_{1}$, ratio of the bridge inductor is greater, higher voltages are used, and a 6AG7 replaces the 6AG5 tube. Although the 6AG7 has a higher transconductance and power rating than the 6AG5, the interelectrode capacitances are greater, the internal leads are longer, and the base is constructed of higherloss material. The circuit operated at frequencies as high as 102 mc , but above 80 mc the disadvantages introduced by the vacuum-tube construction make the circuit impractical. Better performance might be expected with a 6AH6. With the tube operated near its maximum rated dissipation, a one-watt inductively coupled output was obtained at 54 mc , and one-third watt at 80 mc . These outputs are representative of the peak obtainable. Much less power is to be had if the oscillator is adjusted for operation in the higher-stability region.

## TWO-TUBE, 50- TO 100-MC CAPACITANCE-BRIDGE OSCILLATOR

1-373. The circuit shown in figure 1-170 is similar in operation to the one-tube circuit except that the feedback has an additional amplifier stage to boost the gain. There is a significant difference in that the crystal unit is connected to the plate side of the bridge. Under this arrangement, the excitation voltage of $V_{1}$ lags the r-f plate voltage of $V_{1}$, which means that if the plate load is resistive the
$r-f$ plate voltage of $V$, would tend to lag the required excitation voltage of $V_{y}$. For oscillations to occur, the plate tuning tank of $V$, must appear inductive in order to shift the input of $V_{:}$to the proper phase. After equilibrium is reached, a slight increase in the value of $C_{1}$ causes the plate impedance of $V$, to become more nearly resistive, and therefore the input of $V_{z}$ becomes more nearly 180 degrees out of phase with the input of $V_{1}$. This requires that the frequency drop to a point where the voltage across $C_{3}$ is more nearly in phase with the r-f plate voltage for $V_{y}$. For both tubes to operate into resistive loads, the crystal unit must appear as a capacitance. For the crystal unit to operate near series resonance and at the same time maintain the oscillations in the higher-stability region, it would seem that $R_{4}$, the parasitic damping resistor in the input circuit of $V_{2}$ can be replaced, if necessary, by a resistance comparable in value to the $V_{2}$ input reactance. The effect will be to shift the $V_{2}$ input phase in a lagging direction, which would require the $V_{1}$ tank to be more detuned, and hence less critically adjusted. This, in turn, will require a comparable shift in the phase of the input to $V_{2}$, which is to be had by a decrease in frequency, thereby permitting the bridge to be less critically tuned in the vicinity of the crystal resonance point. The circuit in figure 1-170 was found quite practical for use as a test oscillator for measuring the relative performance characteristics of harmonic-mode crystal units. During the temperature runs, even though frost had collected on various components, the operation of the circuit was little affected. For duplicate units of this circuit to provide essentially the same meter readings for tests of the same crystal unit, it is necessary that the vacuum tubes used in the twin circuits show the same plate characteristics within $\pm 5$ per cent. A breadboard model of the oscillator having different values of tuning inductances was able to operate at 140 mc . $L_{1}$, in figure $1-170$, is a 5 -turn coil, approximately one-quarter inch in diameter; $L_{2}$ and $L_{s}$ are the two halves of a 4-turn, center-tapped coil, approximately one-half inch in diameter.

## MULTITUBE CAPACITANCE-BRIDGE <br> OSCILLATOR OPERABLE AT FREQUENCIES UP TO AND ABOVE 200 MC

1-374. The circuit shown in figure 1-171 has been used to generate crystal-controlled frequencies as high as 219 mc , the seventy-third harmonic of a 3 -me crystal. This frequency approaches the ultimate directly obtainable with quartz crystals at the present state of the art. A large part of the


Figure 1-169. A capacitance-bridge oscillator for higher power output which is practical for operation in the $50-80$-mc frequency range. Resistors not otherwise specified are $1 / 2 \mathrm{w}$. All fixed capacitors have mica dielectrics


Figure 1-170. A two-tube capacitance-bridge oxcllator which is practical for operation in the $50-100-\mathrm{mc}$ frequency range


Figure 1-171. A multitube capacitance-bridge oseillafor which is practical for operation in the 50-200-me range. Resistors not otherwise specified are rated of $1 / 2 \mathrm{w}$
success of the oscillator in figure 1-171 is due to the balanced electrical and mechanical nature of the push-pull capacitance-bridge circuit. The operation is very much the same as that of the circuit in figure 1-170 except that the bridge stage is operated in push-pull. With different values of inductance, the circuit provides reliable frequency control anywhere in the v -h-f range, from 200 mc on down. Probably its most practical application is as a harmonic test oscillator. The upper frequency obtainable is not limited by the circuit itself, but by the resistances and shunt capacitances of the crystal units.

## OTHER MODIFICATIONS OF THE CAPACITANCE-BRIDGE OSCILLATOR

1-375. A number of capacitance-bridge modifications have been successfully attempted, four of which are illustrated in figure 1-172. The circuits are largely self-explanatory, and will not be discussed here. Probably of most importance is the electron-coupled circuit, since it permits frequency multiplication in the plate circuit. The triode connection of the crystal circuit probably prevents the crystal, itself, from being operated at frequencies above 75 mc .

## The Butler Oscillator

1-376. At the present time, probably the most widely used of the series-mode oscillators is the Butler, cathode-coupled, two-stage oscillator. The basic design and equivalent circuits are shown in figure 1-173. Although the single-tube, trans-former-coupled type of oscillator will probably outrank the two-tube circuit eventually, the Butler oscillator is the more popular at present because of its simplicity, versatility, frequency stability, and, of most importance, its comparative reliability. With the older types of crystal units, it was generally found that the Butler circuit was the least critical to design and to adjust for operation of the crystal at a given harmonic. The balanced arrangement of the circuit and the fact that twin triodes can be obtained in a single envelope contribute a saving in space and cost, and permit the use of short leads. For greater frequency stability than is normally to be had from parallel-mode oscillations, the cathode-coupled circuit can be used quite satisfactorily at any of the lower frequencies provided the resistance of the crystal unit is not greater than a few hundred ohms. However, the power output is small by comparison


Figure 1-172. Miscellaneous capacitance-bridge oscillators
with that of the Miller circuit for the same crystal power, and the broad bandwidth without plate tuning of the Pierce circuit is not matched. The Butler circuit is usually designed for class-A operation, but class $C$ is possible if greater output and plate efficiency are desired. The output may be taken from aimost any part of the circuit--the plate or cathode of either tube. Quite often the cathode follower, $\mathrm{V}_{1}$, in figure 1-173, is a pentode, with the screen, control grid, and cathode forming a triode section electron-coupled to a plate circuit that usually is tuned for frequency multiplication, although the electron coupling can be employed simply to obtain greater output amplitude and to isolate the load from the oscillator circuit. At very high frequencies, where the shunt reactance of the crystal unit approaches the magnitude of the series-arm $R$, the operation is generally improved by shunting the crystal unit with an inductor that
is antiresonant with the shumt capacitance of the crystal at the operating frequency. When properly designed and adjusted, the two tubes operate 180 degrees out of phase into resistive loads, and the crystal unit acts as a pure resistance.
1-377. In figure 1-173, $V_{1}$ is connected as a grounded-plate cathode follower. The $\mathrm{V}_{1}$ output current, $I_{c}$, enters the feed-back path through the crystal unit, which is operating at series resonance. The impedance of the crystal unit is thus approximately equal to the equivalent scries-arm resistance, $\mathrm{V}_{2}$, a grounded-grid amplifier connected in the feed-back circuit, is excited by $\mathrm{I}_{2}$, the component of $I_{c}$ that passes through $R_{2} . I_{12}$, the remaining component of the feed-back current passes through $\mathrm{V}_{2}$. It can be seen that the input voltage of $V_{1}, E_{81}$, is equal to the output voltage of $V_{z}$ if we assume that the coupling capacitance is infinite. The plate circuit of $V_{2}$ is broadly tuned to the de-

(B)

NOTE
(1) $z_{L}=\frac{z_{p} R_{q}}{z_{p}+R_{q}} \quad$ (5) $\varepsilon_{q 1}=E_{p}-E_{1}$,
(2) $p=-\frac{\mu_{2} E_{q 2}}{I_{p 2}}=-\frac{\mu_{2}\left(R_{p 2}+I_{L}\right)}{\mu_{2}+1}$
(6) $Z_{q 2} \frac{R_{2} Z_{2}}{R_{2}+Z_{2}}$
(3) $z_{1}=\frac{n_{P 1}}{u_{1}+1}$
(7) $z_{i}=A+z_{q 2}$
( $) z_{2}=\frac{R_{p 2}+z_{L}}{H_{2}+1}$
(b) $z_{k}=\frac{n_{1} z_{1}}{n_{1}+z_{i}}$


Figure 1-173. (A) Basic diagram of Butier two-stage cothode-coupled ascillotor. (B) Equivalent r-f circuit of Butler oscillator. Current arrows indicate insfantaneous dectron fiow when r-A voltages have polarities shown. (C) Simplified equivalent circuit where generator of grounded-grid amplifer is replaced by a negative resistance. (D), (E), (F), and (G) Progressive simplitications of equivalent Butler circuit
sired frequency. If $\mathrm{Z}_{\mathrm{p}}$ were simply a resistance, the circuit could still oscillate at the first crystal harmonic. If the crystal unit were shorted out, the circuit could also oscillate, but with the frequency controlled by the tuned plate circuit. $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$ are usually equal, having values between. 50 and 200 ohms. $V_{1}$ and $V_{2}$ are also usually of the same tube type. As will be seen, frequency stability is improved with large values of transconductance. Note in figure 1-173(B) that the r-f plate current in $V_{1}$ is greater than that in $V_{2}$. As in all other vacuumtube oscillators, there are two fundamental equilibrium conditions to consider: the over-all gain must equal unity, and the over-all phase shift must equal zero. We shall first consider the factors affecting loop-gain.

LOOP GAIN OF BUTLER CIRCUIT
1-378. At equilibrium we can say that

$$
\begin{equation*}
1=\frac{E_{1}}{E_{p}} \cdot \frac{E_{q_{2}^{2}}}{E_{1}} \cdot \frac{E_{p}}{E_{q_{2}^{2}}}=G_{1} G_{2} G_{3} \text { (respectively) } \tag{1}
\end{equation*}
$$

The immediate problem is to find the values of $G_{k}$ in terms of the circuit parameters. First, referring to figure 1-173 (ignore the capacitance $\mathrm{C}_{\text {nei }}$ in circuit (B) ), assume that the voltage across $R_{c}$ is approximately equal to $E_{p}$, then

$$
\begin{align*}
& \mathbf{E}_{\mathrm{k} 1}=\mathbf{E}_{\mathrm{p}}-\mathbf{E}_{\mathbf{1}}  \tag{2}\\
& \mathbf{E}_{\mathrm{l}}=\mathrm{I}_{\mathrm{p} 1} Z_{\mathrm{k}}
\end{align*}
$$

and

$$
\begin{align*}
I_{p 1} & =\frac{\mu_{1} E_{p 1}}{R_{p 1}+Z_{k}}=\frac{\mu_{1} E_{p}-\mu_{1} I_{p 1} Z_{k}}{R_{p 1}+Z_{k}} \\
& =\frac{\mu_{1} E_{p}}{R_{p 1}+Z_{k}\left(\mu_{1}+1\right)} \tag{4}
\end{align*}
$$

On combining equations (3) and (4)

$$
\begin{equation*}
\mathbf{E}_{1}=\frac{\mu_{1} E_{p} Z_{k}}{R_{p 1}+Z_{k}\left(\mu_{1}+1\right)} \tag{5}
\end{equation*}
$$

and

$$
G_{1}=E_{1} / E_{p}=\frac{\mu_{1} Z_{k}}{R_{p 1}+Z_{k}\left(\mu_{1}+1\right)}=\frac{g_{m 1} Z_{k}}{1+g_{m 1} Z_{k}} \begin{aligned}
& 1-378(6)
\end{aligned}
$$

The approximation in equation (6) is made on the assumption that $\left(\mu_{1}+1\right) \approx \mu_{1}$. If the numerator and denominator of equation (4) are divided by $\left(\mu_{1}+1\right)$, we have

$$
\mathbf{I}_{p 1}=\frac{\frac{\mu_{1}}{\mu_{1}+1} \mathbf{E}_{p}}{\frac{\mathbf{R}_{\mathrm{p} 1}}{\mu_{1}+1}+\mathrm{Z}_{\mathrm{k}}}
$$

Note that with $Z_{k}$ fixed by the external circuit, the plate current is related to the excitation voltage, $\mathrm{E}_{\mathrm{p}}$, in such a way that the tube behaves as if it had an effective amplification factor of $\frac{\mu_{1}}{\mu_{1}+1}$ and an effective plate resistance equal to $\frac{R_{p 1}}{\mu_{1}+1}$. This resistance is given the symbol $\mathrm{Z}_{1}$ in figure $\mathbf{1 - 1 7 3}$. If an additional resistance, $R_{L}$, were connected between the plate of $V_{1}$ and $r-f$ ground, $Z_{n}$ would equal $\frac{R_{2}+R_{p 1}}{\mu_{1}+1}$. Now, to find the value of $G_{2}=E_{\sigma^{2}} / E_{1}$, we start with

$$
\begin{array}{ll}
E_{v 2}=I_{2} R_{2} & 1-378(7) \\
E_{1}=I_{s} R-\mu_{2} E_{c}+I_{p 2} R_{p 2}+I_{p 2} & Z_{L} \\
1-378(8) \\
I_{c}=I_{2}+I_{p 2} & 1-378(9)
\end{array}
$$

and

$$
\begin{equation*}
I_{p z}=\frac{E_{q^{2}}+\mu_{2} E_{g^{2}}}{R_{p 2}+Z_{L}}=\frac{\left(\mu_{2}+1\right) E_{g_{2}}}{R_{p 2}+Z_{L}} \tag{10}
\end{equation*}
$$

1-378
On rearranging equation (10) to express $\mathbf{E}_{\mathrm{a}}$ as a function of $\mathrm{I}_{\mathrm{p} 2}$, and substituting this function for $E_{z^{2}}$ in equation (8), we have

$$
E_{1}=I_{c} R+I_{p 2}\left[-\frac{\mu_{2}\left(R_{p 2}+Z_{L}\right)}{\mu_{2}+1}+R_{p 2}+Z_{L}\right]
$$

$$
1-378(11)
$$

From equation (11) we find that the equivalent generator of $V_{2}$ can be represented by an equivalent negative resistance

$$
\rho=\frac{-\mu_{2}\left(R_{\mathrm{p} 2}+Z_{\mathrm{L}}\right)}{\mu_{2}+1}
$$

It can be seen that $\rho$ is smaller in magnitude than $\left(R_{p z}+Z_{L}\right)$, so that the total $V_{i}$ branch resistance is positive. Defining the $V_{2}$ branch impedance to be $Z_{2}$, we have

$$
\begin{equation*}
Z_{2}=\rho+R_{p 2}+Z_{z}=\frac{R_{p 2}+Z_{L}}{\mu_{2}+1} \quad 1-378 \tag{13}
\end{equation*}
$$

On substituting equations (7) and (13) into equation (10), we have

$$
\begin{equation*}
I_{p 2}=\frac{R_{2} I_{2}}{Z_{2}} \tag{14}
\end{equation*}
$$

so that equation (9) may be written

$$
\begin{equation*}
I_{c}=\left(\frac{Z_{2}+R_{2}}{Z_{2}}\right) \mathbf{I}_{2} \tag{15}
\end{equation*}
$$

On substituting equations (13), (14), and (15) into (11),

$$
\begin{align*}
E_{i} & =\frac{I_{2} R\left(Z_{2}+R_{2}\right)}{Z_{2}}+\frac{I_{2} R_{2} Z_{2}}{Z_{2}} \\
& =I_{2}\left[\frac{R\left(Z_{2}+R_{2}\right)+R_{2} Z_{2}}{Z_{2}}\right] \tag{16}
\end{align*}
$$

$1-378$
Thus

$$
\mathbf{G}_{2}=\frac{\mathbf{E}_{\mathbf{k}^{2}}}{\mathbf{E}_{1}}=\frac{\mathbf{R}_{2} Z_{2}}{R\left(Z_{2}+R_{2}\right)+R_{2} Z_{2}}
$$

To find $G_{3}\left(=E_{p} / E_{\mathbf{k}^{2}}\right)$, we see that

$$
\begin{equation*}
E_{p}=I_{p 2} Z_{L} \tag{18}
\end{equation*}
$$

which, on substituting the value of $I_{p 2}$ given in equation (14), becomes

$$
\begin{equation*}
E_{p}=\frac{I_{2} R_{2} Z_{L}}{Z_{2}} \tag{19}
\end{equation*}
$$

Dividing by $\mathrm{E}_{\mathbf{x}^{2}}\left(=\mathrm{I}_{2} \mathrm{R}_{2}\right)$, we have

$$
\begin{equation*}
\mathbf{G}_{3}=\frac{\mathbf{E}_{\mathrm{p}}}{\mathrm{E}_{\mathbf{2}}}=\frac{\mathrm{Z}_{\mathrm{L}}}{\mathrm{Z}_{2}} \tag{20}
\end{equation*}
$$

The conditions for equilibrium as expressed by equation (1) are thus found to be

$$
\begin{aligned}
& \mathrm{G}_{1} \mathrm{G}_{2} \mathrm{G}_{3}= \\
& \frac{\mu_{1} Z_{k} R_{2} Z_{L}}{\left[R_{p i}+Z_{k}\left(\mu_{1}+1\right)\right]\left[\left(Z_{2}+R_{2}\right) R+R_{2} Z_{2}\right]}=1 \\
& 1-378(21)
\end{aligned}
$$

By a slightly different approach, in which the equilibrium is expressed as

$$
\mathrm{G}_{1}^{\prime} \mathrm{G}_{1}^{\prime \prime} \mathrm{G}_{2} \mathrm{G}_{3}=\frac{\mathrm{E}_{\mathrm{k} 1}}{\mathbf{E}_{\mathrm{p}}} \cdot \frac{\mathrm{E}_{1}}{\mathrm{E}_{\mathrm{q} 1}} \cdot \frac{\mathrm{E}_{\mathrm{q} 2}}{\mathrm{E}_{1}} \cdot \frac{\mathrm{E}_{\mathrm{p}}}{\mathbf{E}_{\mathrm{q} 2}}=1
$$

where

$$
G_{1}^{\prime}=\frac{E_{g^{1}}}{E_{p}}=\frac{R_{2} Z_{L}-\left(Z_{2}+R_{2}\right) R-R_{2} Z_{2}}{R_{2} Z_{L}}
$$

1-378 (22)
and

$$
\begin{equation*}
G_{1}^{\prime \prime}=\frac{E_{1}}{E_{z 1}}=\frac{\mu_{1} Z_{k}}{R_{p 1}+Z_{k}} \tag{23}
\end{equation*}
$$

it will be found that

$$
\begin{gathered}
G_{1}^{\prime} G_{1}^{\prime \prime} G_{2} G_{3}=G_{1} G_{2} G_{3}= \\
{\left[\frac{R_{2} Z_{L}}{\left(Z_{2}+R_{2}\right) R+R_{2} Z_{2}}-1\right] \frac{\mu_{1} Z_{k}}{R_{p 1}+Z_{k}}=1} \\
1-378(24)
\end{gathered}
$$

Since $R_{p 1}$ and $R_{2} Z_{L}$ are very large compared with $Z_{x}$ and $\left[\left(Z_{2}+R_{2}\right) R+R_{2} Z_{2}\right]$, respectively, we can simplify equations (21) and (24) by writing

$$
\frac{R_{2} Z_{L} Z_{k} g_{m 1}}{\left(Z_{2}+R_{2}\right) R+R_{2} Z_{2}}=1
$$

On dividing both numerator and denominator by $\left(Z_{2}+R_{2}\right)$ and substituting for the values of $Z_{k^{2}}$ and $Z_{t}$ as defined in equations (6) and (7) of figure 1-173, equation (25) can be simplified somewhat. Thus

$$
\begin{equation*}
\frac{Z_{\varepsilon^{2}} Z_{L} Z_{k} g_{m l}}{Z_{2} Z_{f}}=1 \tag{26}
\end{equation*}
$$

1-379. The design of a Butler oscillator must be such that under no-signal conditions the left side of equation 1-378(26) is greater than unity. As oscillations build up, the principal effects will be a decrease in the effective $g_{m 1}$ and $g_{m 3}$ as the signal swings farther into the lower bend of the $E_{c} I_{b}$ curve. How large the equilibrium amplitude will be depends upon how much greater than unity the left side of equation $1-378(26)$ is at the start. The larger the left-side magnitude, the greater must be the decrease in $g_{m}$, and hence the greater the equilibrium activity must be. If the oscillator is to operate class $A$, as is usual, the gain equilibrium should very nearly hold for no-signal conditions, with due allowance made for a maximum $\mathrm{Z}_{\mathrm{t}}\left(=\mathrm{R}+\mathrm{Z}_{\mathrm{g}^{2}}\right)$ when $\mathrm{R}=\mathrm{R}_{\mathrm{m}}$, the maximum series resistance permissible for the particular type of crystal unit chosen. With all else constant, maximum activity is to be obtained when $g_{m 1}$ and $\mathbf{g}_{m 2}$ are maximum under no-signal conditions. Assurance that the crystal unit will not be driven beyond its rated power can be approximately predicted from the plate characteriatics of the tube to be used. If no grid current is drawn, the bias on $V_{1}$ will be

$$
\begin{equation*}
\mathbf{E}_{\mathrm{ol}}=-\dot{I}_{\mathrm{b} 1} \mathrm{R}_{1} \tag{1}
\end{equation*}
$$

where $I_{b 1}$ is the average $d$-c plate current of
$\mathbf{V}_{1}$. Grid current can be drawn if $\left[(\max ) \mathrm{E}_{\mathfrak{p}}\right.$ $\left.(\max ) E_{1}\right]$ is greater than $I_{b 1} R_{1}$, in which case the bias will be

$$
\begin{equation*}
\mathrm{E}_{\mathrm{ol}}=(\max ) \mathrm{E}_{1}-(\max ) \mathrm{E}_{\mathrm{p}} \quad 1-379 \tag{2}
\end{equation*}
$$

Greater amplitude stability is achieved if $R_{1}$ is sufficiently small for equation (2) to apply. Using the appropriate equations in paragraph 1-378, a maximum value of $\mathrm{E}_{1}$ can be determined that will not allow the crystal current, $\mathrm{l}_{\mathrm{c}}$, to become greater than $\sqrt{P_{\mathrm{cm}}} / \mathrm{R}$, where $\mathrm{P}_{\mathrm{cm}}$ is the maximum recommended power level of the crystal, and $R$ is any crystal resistance between $R_{m}$ and $R_{m} / 9$. Very possibly, a twin triode may be preferred, or perhaps the choice of tubes will be dictated by the h-f type of tube most readily available. $R_{1}$ and $R_{2}$ are to be kept as small as possible in the interest of frequency stability. In the final analysis, the plate voltage permitting an optimum output for the average crystal unit, without risking an overdrive for any expected value of crystal $R$, is most easily checked by experiment.

## dESIGN CONSIDERATIONS TO MAXIMIZE THE FREQUENCY STABILITY OF THE BUTLER OSCILLATOR

1-380. If the cathode follower operates into a purely resistive network, as is indicated in the equivalent circuit of figure $1-173(\mathrm{~B})$, maximum stability in the phase characteristics is obtained. As nearly a resistive circuit as possible is desirable, for under these conditions the frequency is independent of the plate resistance of the tubes, and a small increment of reactance requires the least adjustment of the crystal to restore a phase equilibrium. $\mathrm{E}_{1}$, the output voltage of the cathode follower, is in phase with the excitation voltage, $\mathrm{E}_{\mathrm{p}}$. In a resistive circuit, $\mathrm{E}_{\mathrm{p}}$ will be 180 degrees out of phase with $\mathrm{E}_{\mathrm{g} 2}$. Thus, $\mathrm{E}_{\mathrm{g} 2}$ must be 180 degrees out of phase with $E_{1}$. Since $E_{82}$ is the voltage of ground with reference to the cathode of $V_{2}$, and $E_{1}$ is the voltage of the cathode of $V_{1}$ with reference to ground, $I_{1}$ and $I_{2}$ must be in phase. For example, imagine that $R$ is zero, then $R_{1}$ and $R_{2}$ could be assumed to be two halves of a single resistance. In this case $\mathrm{E}_{5}$ would equal $-\mathrm{E}_{1}$, and the proper phase relation would exist.
1-381. To maintain as nearly as possible a resistive circuit, $\mathrm{Z}_{\mathrm{p}}$ must tune as broadly as is practicable; the tendency of the input capacitances of $\mathrm{V}_{1}$ and $V_{g}$ to shift the phase must be compensated ; the transit time of the vacuum tubes must be minimized; and, if an inductor is connected across the crystal unit to antiresonate with the shunt capaci-
tance, $\mathrm{C}_{o}$, the resulting parallel-resonant circuit must also tune very broadly. The tuned plate circuit, $Z_{10}$, must be sufficiently selective to ensure that the circuit can oscillate only at the desired harmonic of the crystal frequency, but, beyond this, any increase in the tank selectivity only results in a greater phase shift, and consequently a greater frequency shift, for a given percentage change in the plate capacitance. The use of a damping resistance as indicated in figure 1-173(A), or a low-Q coil, will broaden the tuning of the tank. The stray capacitance from the plate of $\mathrm{V}_{2}$ to ground should be kept to a minimum.
1-382. To annul the input capacitance of $\mathrm{V}_{2}$, which is equal to the total capacitance between the cathode of $V_{2}$ and ground, we can connect an inductor in series with $R_{2}$, or replace $R_{2}$ with a low- $Q$ inductor and employ gridleak bias for $V_{2}$ (while keeping the grid at $\mathrm{r}-1$ ground by the use of an r-f bypass capacitor), or shunt $R_{2}$ with an inductor in series with an r-f bypass capacitor. In any event, the inductor is to be antiresonant with the cathode-to-ground capacitance at the operating frequency. With $\mathrm{R}_{2}$ acting as a damping resistance, a broadband response is ensured for the antiresonant combination.
$1-383$. The grid-to-cathode capacitance and the cathode-to-ground capacitance of $V_{1}$ can also be annulled by the use of antiresonant inductors. However, a more effective and economical method is to design the circuit so that the two cathode capacitances of $V_{1}$ neutralize each other regardless of the particular frequency. The grid-to-cathode capacitance, $\mathrm{C}_{\mathrm{gcc}}$, is illustrated by the dotted-line circuit in figure $1-173(B)$. The voltage across $\mathrm{C}_{\mathrm{gc}}$ is $\mathrm{E}_{\mathrm{g}}$, so that the leading component of current through the grid circuit is

$$
\begin{equation*}
I_{\mathrm{gx}}=\frac{\mathrm{E}_{\mathrm{g} 1}}{\mathrm{X}_{\mathrm{og} 1}} \tag{1}
\end{equation*}
$$

For convenience, let it be imagined that all of $\mathrm{I}_{\mathrm{gx}}$ flows through $R$ and $R_{p 2}$ in completing its circuit. If it is not to upset the phases of the voltages across these resistances, $\mathrm{I}_{\mathrm{gx}}$ must be annulled by an equal lagging current through the $\mathrm{R}-\mathrm{R}_{\mathrm{p} 2}-\mathrm{Z}_{\mathrm{p}}$ circuit. Thus, assuming the transit-time effect is negligible, the plate tank must be slightly inductive if $V_{2}$ is to operate into a purely resistive load. This much can be controlled by the adjustment of the $V_{2}$ plate circuit. With the circuit properly adjusted, it can now be imagined that $I_{\mathrm{gx}}$ is no longer a part of $\mathrm{I}_{\mathrm{C}}$, but circulates directly through $\mathrm{Z}_{\mathrm{L}}$ and $\mathrm{C}_{\mathrm{gct}}$ in series. The design problem is to ensure that no part of $\mathrm{I}_{5}$ flows through $\mathrm{R}_{1}$ or $\mathrm{V}_{1}$, but returns

## Section 1

to $\mathrm{Z}_{\mathrm{L}}$ by flowing entirely through the $\mathrm{V}_{1}$ cathode-to-ground capacitance, $\mathrm{C}_{2}-$ not shown in figure 1-173. Furthermore, the design should be such that $I_{g r}$ is all the current that flows through $\mathrm{C}_{1}$; otherwise, there will be a net unneutralized leading component upsetting the voltage phases in the rest of the circuit. With proper nentralization, the only reactive current will be confined to a series circuit comprised of $\mathrm{C}_{\mathrm{gcc}}, \mathrm{C}_{1}$, ground, and an effective inductance shunting $Z_{\text {L. }}$. The voltage across each of the reactive impedances due to $\mathrm{I}_{\mathrm{k} x}$ will be equal in magnitude and phase to the voltages caused by the in-phase currents flowing through the corresponding resistive impedances. Thus, to neutralize the circuit, the leading current, $\mathrm{I}_{k x}$, flowing through $\mathrm{C}_{1}$ must of itself produce the voltage $\mathrm{E}_{1}$. This occurs when

$$
\begin{equation*}
\mathrm{E}_{1}=\mathrm{I}_{\mathrm{gx}} \mathrm{X}_{\mathrm{Cl}} \tag{2}
\end{equation*}
$$

or, using equation (1) to replace $I_{r x}$,

$$
\begin{equation*}
\mathbf{E}_{1}=\frac{\mathrm{E}_{\mathrm{gl}} \mathrm{X}_{\mathrm{Cl}}}{\mathbf{X}_{\mathrm{cg} 1}} \tag{3}
\end{equation*}
$$

Now,

$$
\begin{equation*}
E_{1}=\frac{\mu_{1} E_{\mathrm{g} 1} Z_{k}}{R_{p 1}+Z_{k}}=g_{m 1} E_{\mathrm{s} 1} Z_{k} \tag{4}
\end{equation*}
$$

Using equation (4) to eliminate $E_{1}$ in equation (3), we have

$$
\mathrm{g}_{\mathrm{m} 1} \mathrm{E}_{\mathrm{g} 1} \mathrm{Z}_{\mathrm{k}}=\frac{\mathrm{E}_{\mathrm{g} 1} \mathrm{X}_{\mathrm{Cl}}}{\mathrm{X}_{\mathrm{cg} 1}}
$$

or

$$
\begin{equation*}
\mathrm{g}_{\mathrm{m} 1} \mathrm{Z}_{\mathrm{k}}=\frac{\mathrm{C}_{\mathrm{kc} 1}}{\mathrm{C}_{1}} \tag{5}
\end{equation*}
$$

Equation (5) defines the ratio for the $V_{1}$ input to output capacitance that should exist for maximum frequency stability.
1-384. To minimize the tendency of the transit time to cause the respective plate currents of $\mathrm{V}_{1}$ and $V_{2}$ to lag the equivalent generator voltages, small-dimensioned h-f tubes should be used, and the plate voltages should be as high as practicable. If the additional expenditure in the design and production of the circuit are warranted, suitable networks can be devised to neutralize the transit effects.

1-385. At the higher frequencies the series resistance of the crystal unit tends to increase, since the lagging component of current through the series arm must increase in order to annul the
increased leading component through the shunt capacitance, $\mathrm{C}_{\mathrm{o}}$. For this to occur, the frequency may need to be increased considerably above the natural resonance of the motional arm, so that the effective series resistance approaches the value of a parallel-resonant impedance. To reduce the resistance to the series-arm value, $\mathrm{C}_{6}$ should be annulled by an antiresonant inductor having an inductance

$$
\begin{equation*}
\mathrm{L}_{\mathrm{o}}=\frac{1}{\omega^{2} \mathrm{C}_{\mathrm{o}}} \tag{1}
\end{equation*}
$$

To prevent the crystal shunt reactances from being more frequency sensitive than the plate circuit of $V_{2}$, a shunt resistance should also be connected across the crystal unit to dampen the $\mathrm{L}_{\mathrm{o}} \mathrm{C}_{\mathrm{o}}$ tank. A suitable resistance, $\mathrm{R}_{\mathrm{o}}$, that can interfere very little with the crystal stabilizing effect is

$$
\begin{equation*}
R_{\mathrm{o}}=5 \mathrm{R}_{\mathrm{m}} \tag{2}
\end{equation*}
$$

where $R_{m}$ is the rated maximum permissible crystal series resistance.

## STABILIZING EFFECT OF CRYSTAL IN BUTLER CIRCUIT

1-386. From equation 1-241(2) we found that for a crystal operating at series resonance the fractional change in frequency required to produce a small change in phase, $\mathrm{d} \theta$, is expressed by

$$
\frac{d \omega}{\omega d \theta}=\frac{R_{c}}{2 \sqrt{L / C}}
$$

where $R_{c}$ is the total resistance the crystal faces, including the crystal's own resistance, and $L$ and C are the series-arm parameters of the crystal unit. In the Butler circuit (refer to figure 1-173) the crystal operates into a resistance

$$
\begin{equation*}
R_{c}=Z_{i}+\frac{R_{1} Z_{i}}{R_{1}+Z_{1}} \tag{1}
\end{equation*}
$$

where $Z_{t}$ is the resistance of the feed-back circuit, and $\frac{R_{1} Z_{1}}{R_{1}+Z_{1}}$ is the output resistance of $V_{1}$. On substituting the values for $Z_{1}$ and $Z_{f}$, we have

$$
\begin{align*}
R_{\mathrm{e}}=\mathrm{R} & +\frac{\mathrm{R}_{2}\left(\mathrm{R}_{\mathrm{p} 2}+\mathrm{Z}_{\mathrm{L}}\right)}{\mathrm{R}_{2}\left(\mu_{2}+1\right)+\mathrm{R}_{\mathrm{p} 2}+\mathrm{Z}_{\mathrm{L}}} \\
& +\frac{R_{1} R_{\mathrm{p} 1}}{\mathrm{R}_{1}\left(\mu_{1}+1\right)+R_{\mathrm{p} 1}} \tag{2}
\end{align*}
$$

If we assume that $R_{p 1}=R_{p 2}=R_{p} \gg Z_{L}$, and that
$\mu_{1}=\mu_{2}=\mu \gg 1$, equation (2) becomes

$$
R_{o}=R+\frac{R_{2} R_{p}}{R_{2} \mu+R_{p}}+\frac{R_{1} R_{p}}{R_{i} \mu+R_{p}}
$$

or

$$
\begin{equation*}
\mathrm{R}_{\mathrm{c}}=\mathrm{R}+\frac{\mathrm{R}_{3}}{\mathrm{R}_{2} \mathrm{~g}_{\mathrm{m}}+1}+\frac{\mathrm{R}_{1}}{\mathrm{R}_{1} \mathrm{~g}_{\mathrm{m}}+1} \tag{3}
\end{equation*}
$$

From equation (3) it is seen that the $Q$ of the crystal circuit, and hence the frequency stability, is to be improved if $R_{2}$ and $R_{1}$ are kept as small as possible and the transconductance of each tube is high. If $R_{1}$ and $R_{2}$ are of such values that the denominators in equation (3) are large compared with 1 , a limiting value is approached, where

$$
\begin{equation*}
(\max ) \mathrm{R}_{\mathrm{c}}=\mathrm{R}+\frac{2}{\mathrm{~g}_{\mathrm{m}}} \tag{4}
\end{equation*}
$$

## DESIGN PROCEDURE FOR BUTLER OSCILLATOR

1-387. In considering the use of a Butler oscillator for controlling frequencies below 20 mc , the principal factor to consider is whether the frequency stability required is greater than that which is normally obtained with a Pierce circuit. If not, there is little to gain by using two tubes and a frequency-sensitive tuned circuit, unless it is very important that the waveform in the output be more nearly sinusoidal and less influenced by the variations in the crystal resistance. The frequency stability of an average Butler. circuit can be expected to be approximately 0.0005 per cent as compared with a stability of approximately 0.001 to 0.0015 per cent for an average Pierce circuit. Above 20 mc , the principal competitor of the Butler is the transformer-coupled type of oscillator, The chief advantage of the Butler is its relative ease of adjustment and dependability. A borderline replacement crystal unit or an aging crystal unit, as a general rule, is more likely to be operative in the two-stage, cathode-coupled circuit than in any of the other types of v-h-f oscillators. Once the Butler circuit has been selected as the most appropriate to use, a crystal unit that has been series-tested at the intended frequency should be selected. The required minimum frequency tolerance and the operating conditions to be expected determine whether the crystal unit, or perhaps the entire oscillator, is to be oven-controlled. For the next step, it is probably best to select the types of vacuum tubes to use. Insofar as space, weight,
and cost are concerned, a single tube envelope for both amplifier stages is desirable. On the other hand, it may be found that a more balanced arrangement and more direct circuit connections can be had with separate tubes, particularly if the crystal unit is to be oven-mounted. The transconductance and plate resistance of the tubes should both be high, for maximum frequency stability. For the same amplification factor, the tube with the larger $g_{m}$ is usually to be preferred. For h-f and v-h-f operation miniature tubes are preferable, in order to reduce the transit time and the electrode-to-ground capacitances. For class-A operation, both tubes can be of the same type. For class-C operation, the power rating of the cathode follower should be greater than that of the grounded-grid ampliñer. For maximum stability it may be desirable to isolate the load from the rest of the circuit, or to tune the load circuit for frequency multiplication. In this case a pentode can be used for either the cathode follower (usually) or for the grounded-grid amplifier, with the load taken from the electron-coupled plate circuit, and with the screen grid serving as the oscillator plate. Either pentodes or triodes can be used in the basic Butler circuit, as desired. In the v-h-f range, triodes have the advantage of smaller tran-sit-time effects. Assume that it is intended to operate the tubes class A . To reduce the transit time, to increase $g_{n}$, and to permit a minimum value of $\mathrm{Z}_{\mathrm{L}}$ (low- Q tank), the plate voltages should be as high as practicable. Determine the values of $R_{1}$ and $\mathrm{R}_{2}$ that will provide a normal cathode bias for class-A operation. With all else equal, the feedback transmission losses are a minimum if $\mathrm{R}_{1}=\mathrm{R}_{2}$. For class-C operation, $\mathrm{R}_{2}$ should equal approximately $4 \mathrm{R}_{1}$. Assume that R of the crystal unit is the maximum permissible value, and that the effective $g_{m}$ 's of the vacuum tubes are 25 per cent less than their rated values for class-A operation at the selected plate and grid voltages. With these assumptions, determine the value of $\mathrm{Z}_{\mathrm{L}}$ that is required to make the gain equation, $1-378$ (26), hold. $R_{g}$ should be large compared with $Z_{p}$, so that $\mathrm{Z}_{\mathrm{L}} \approx \mathrm{Z}_{\mathrm{p}}$. The plate tank represented by $\mathrm{Z}_{\mathrm{p}}$ can be designed as a high-Q circuit, antiresonant at the operating frequency, and shunted by a simulated load resistance, $R_{L}$, much smaller than the antiresonant impedance of the tank, itself. In this case, $\mathrm{Z}_{\mathrm{L}} \approx \mathrm{Z}_{\mathrm{p}} \approx \mathrm{R}_{\mathrm{t}}$. The approximations above will be sufficient to build an experimental circuit that should oscillate in a free-running state. A variable resistance can be connected to simulate a crystal unit at series resonance. By varying the simulated crystal resistance over the range possible for a ran-

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## Crystal Oxeillators

dom selection of crystal units, $\mathrm{R}_{\mathrm{L}}$ in the plate circuit can be adjusted, if necessary, to ensure that oscillations occur at all possible values of crystal resistance without driving the crystal at a higher than recommended level. The empirical optimum value of $\mathrm{R}_{\mathrm{L}}$ can be accepted as the value of $\mathrm{Z}_{\mathrm{L}}$ to achieve in the design of the output circuit of the grounded-grid amplifier. The actual design of the output stage depends, of course, upon the type of load into which the oscillator is to operate. The important consideration is that an effective resistance having the value of the experimental $\mathrm{R}_{\mathrm{L}}$ is to be introduced in one way or another across the plate tank. The final problem is to neutralize the various circuit capacitances. In neutralizing the $V_{1}$ cathode capacitances, the adjustment which permits the feed-back circuit to be purely resistive can be expected to coincide with the conditions for maximum output amplitude and maximum crystal current. The design procedure discussed above should be accepted simply as a suggestion. Individual
engineers may well prefer that primary attention be given to fitting the design to meet special requirements.

## MODIFICATIONS OF THE BUTLER OSCILLATOR

1-388. As in the case of other conventional oscillator designs, the number of modifications of the Butler circuit appear to be unlimited. In figure 1-174, the basic electron-coupled circuit is shown in (A), and a circuit employing a common ground return for the two tubes is shown in (B). In the electron-coupled circuit, the load, represented by $\mathbf{R}_{\mathbf{L}}$, is effectively isolated from the oscillator circuit, in which the screen of $V_{1}$ serves as the cathode-follower anode. The plate circuit of $V_{1}$ can be tuned to the second or third harmonic of the oscillator frequency, if desired, in which case $\mathrm{V}_{1}$ should be operated class C. For maximum output voltage, the plate impedance of $V_{1}$ should be high. In figure 1-174 (B), the low-Q inductor, $L_{1}$, is


Figure 1-174. (A) Eleetron-ceupled Butler circuit. (B) Butlof circuit hoving common cathode ground return
antiresonant with the distributed capacitance, $\mathrm{C}_{2}$, as is $\mathrm{L}_{0}$ with $\mathrm{C}_{0}$. Gridleak bias is employed with both tubes. However, the grid of $\mathrm{V}_{2}$ is still kept at r-f ground through the bypass capacitance. It can be seen that equation 1-378 (26),

$$
\frac{\mathrm{Z}_{\mathrm{a}} \mathrm{Z}_{\mathrm{L}} \mathrm{Z}_{\mathrm{k}} \mathrm{~g}_{\mathrm{m} 1}}{\mathrm{Z}_{2} \mathrm{Z}_{t}}=1
$$

when applied to the common-ground return circuit, becomes

$$
\begin{equation*}
\frac{\mathrm{Z}_{\mathrm{k} 2} \mathrm{Z}_{\mathrm{L}} \mathrm{~g}_{\mathrm{m} 1}}{\mathrm{Z}_{2}}=1 \tag{1}
\end{equation*}
$$

since $Z_{k}$ is equal to $Z_{t}$. Also, since $Z_{z}=\frac{R_{D_{2}}+Z_{L}}{\mu_{z}+1} \approx$ $\frac{1}{\mathbf{g}_{\mathrm{m}}}$, since $\mathrm{Z}_{\mathbf{z}^{2}}=\frac{\mathbf{R}_{2} \mathbf{Z}_{\mathbf{z}}}{\mathbf{R}_{1}+Z_{2}}$, where $\mathrm{R}_{2}$ now represents the antiresonant impedance of the $L_{1} C_{2}$ combination, it can be shown that equation (1) can be expressed as

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{L} \mathrm{~g}_{\mathrm{m} 1}}-\frac{1}{\mathrm{R}_{2} \mathrm{~g}_{\mathrm{m} 2}}=1 \tag{2}
\end{equation*}
$$

If the product $\mathrm{R}_{\mathrm{e} \mathrm{gm}_{\mathrm{m}}}$ is large compared with 1 , at equilibrium $\mathrm{g}_{\mathrm{m}}$ must approximately equal $1 / \mathrm{Z}_{\mathrm{L}}$. 1-389. The schematics of a number of Butler circuits employed by the military services are shown in figure 1-175. Circuit (A) is a receiver heterodyne oscillator that can be switched from crystal to manual operation simply by shorting out the crystal. $\mathrm{C}_{1}$ is an $r$-f bypass capacitor that prevents the inductor $L_{1}$ from shorting out the cathode bias developed across $R_{1} . L_{1}$ is designed to be antiresonant with the grounded-grid amplifier cathode-toground capacitance. $\mathrm{C}_{2}$ is inserted to resonate with the distributed inductance of the crystal leads and feed-back circuit. $\mathrm{C}_{3}$ is a split-stator capacitor which permits the use of a grounded rotor, thereby reducing intersectional capacitances. Since the r-f current through $\mathrm{C}_{3}$ is small, wiping contacts can be used for grounding without introducing noise. $\mathrm{C}_{4}$ is simply a trimmer which permits adjustment of the effective inductance of $L_{2}$. The plate side of $C_{3}$ effectively has a relatively large fixed component due to the stray plate-to-ground capacitance. To keep the plate tank balanced, an equal amount of fixed capacitance, $\mathrm{C}_{5}$, is added to the other side of $\mathrm{C}_{3} . \mathrm{R}_{2}$ is added to suppress parasitic oscillations. As can be seen, the output is obtained by splitload operation of the cathode follower. Since the output is delivered to a mixer circuit, where the effective load might be expected to undergo slight
changes, it is probable that the loaded cathodefollower plate circuit is less frequency sensitive than the finely balanced tank in the $V_{8}$ plate circuit. Since the balanced tank must be sufficiently selective to stabilize the frequency during manual operation, it cannot be loaded as would normally be done. Although the crystal is not active in the circuit during manual operation, it cannot be removed without resulting in an increase in frequency. This is due to the decrease in the cathode-to-ground capacitance that results when the crystal unit is removed.
1-390. Figure 1-175 (B) (C) (D) (E) (F) is a composite arrangement of five different oscillators, none of which have all the components shown. For example, the $\mathrm{B}^{+}$return of $\mathrm{V}_{1}$ is through $\mathrm{R}_{5}$ in (B), (E), and possibly (F) ; it is through $R_{t}$ in (C), and also in (D), except that $R_{2}$ and $R_{8}$ are one and the same in the latter circuit, although the actual circuit is not indicated in the schematic shown. In circuit (E) the F. output is cathodecoupled to a mixer tube ( 6 AK5W). An r-f choke is connected between the cathode and ground, not the resistance $R_{10}$. In circuit (B), $C_{s}$ is actually composed of two $1.5-\mu \mu f$ capacitors in series. The $F_{3}$ output is developed across a tuned tank identical with and also inductively coupled to, the plate tank in the $V_{8}$ plate circuit. $L_{s}$ in circuit ( $B$ ) thus serves as a transformer primary. The $\mathrm{F}_{3}$ output is fed to the grid of one and to the cathode of a second 6AG5 mixer stage. The heterodyned output of the first is 20 to 30 mc , and that of the second is 4.8 to 5.7 mc .
$1-391$. The circuit shown in figure $1-175$ ( G ) is a carefully designed experimental model that was built and tested during an investigation of $h$ - $f$ and v-h-f oscillators by a research team headed by W. A. Edson at the Georgia Institute of Technology. A breadboard model of this circuit was operative at frequencies as high as 150 mc , with crystal resistances as high as 500 ohms. Circuit (G) was found to have a frequency stability of 0.22 parts per million per volt change in the high-voltage supply. The frequency was controlled at 126 mc , the ninth harmonic of a $14-\mathrm{mc}$ fundamental. The shunt capacitance of the test crystal was $12 \mu \mu \mathrm{f}$, and the series resistance after tuning out the capacitance was 300 ohms. Oscillations could not be sustained at plate voltages below 50 volts, and the frequency instability increased greatly at voltages above 85 volts. Note that circuit (K) in figure 1-175, which has been designed to operate with low- and me-dium-frequency, fundamental-mode crystal units, is not a true Butler circuit in that neither tube is operated as a cathode follower.

## Section 1

## Crystal Oscillators



Figure 1-175. Modifications of Butlor oscillator. Datted linea in circuit (C) indicate stray capacitances

| Fig. | Equipment | Purpose | $F_{1}$ | $F_{2}$ | $F_{8}$ | F | CR | $\mathbf{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathbf{R}_{3}$ | $\mathbf{R}_{4}$ | Rs | $\mathbf{R}_{6}$ | $\mathrm{R}_{7}$ | $\mathbf{R s}_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Radio Receiver R-266/ URR-18 | Heterodyne ascillator | $\begin{aligned} & 20.3- \\ & 34.8 \end{aligned}$ | 2Fi |  |  | $\begin{aligned} & \text { CR-24/U } \\ & \text { (6th } \\ & \text { mode) } \end{aligned}$ | 0.18 | 0.01 | 6.8 | 0.18 | 12 | 6.8 |  |  |
| (B) | Receiver Transmitter RT-178/ ARC-27 | 3rd transmitter osc or 2nd receiver ose for heterodyning | $\begin{aligned} & 25.7- \\ & 34.7 \end{aligned}$ | $F$ | 1 | NA | CR-23/U | 0.1 | 1 | 100 | 0 | 0.15 | NA | 12 | NA |
| (C) | Receiver- <br> Trangmitter RT-178/ ARC-27 | 1st <br> guard <br> receiver local ose | 37.286 | $F_{1}$ | NA | 2F1 | CR-28/U | 0.98 | 0.12 | 47 | 0 | 0.22 | 0.12 | 8.8 | 0 |
| (D) | Receiver- <br> Transmitter RT-178/ ARC-83 | 1st monitor osc of transmitter M.O. | 0.8398 | $F_{1}$ | $\begin{aligned} & 4 \mathrm{~F}_{1}- \\ & 18 \mathrm{~F}_{\mathrm{i}} \end{aligned}$ | $\mathrm{F}_{1}$ | CR-28/U | 8.8 | 33 | 100 | 0 | 1 | Same realator ${ }_{\mathbf{R}_{2}}^{\mathbf{R}_{2}}$ | $\infty$ | 0.22 |
| (E) | Receiver- <br> Transmitter RT-178/ ARC-33 | Guardchannel heterodyne oscill-atordoubler | $\begin{aligned} & 55.668- \\ & 58.160 \end{aligned}$ | $\mathbf{F}_{1}$ | NA | $\begin{aligned} & 2 F_{1} \\ & \text { and } \\ & 4 F_{1} \end{aligned}$ | CR-32/U | 0.12 | 8.2 | 88 | 0 | 0.38 | NA | 27 | $\infty$ |
| (F) | Radio <br> Receiver <br> R-252A/ <br> ARN-14 | 1st heterodyne oseillator | $\begin{aligned} & 44.275 \\ & 57.275 \end{aligned}$ | F | NA | $2 \mathrm{~F}_{1}$ | CR-23/U |  | 8.2 | 4.7 | 0.1 |  | $?$ | $\infty$ | 1 |

Circuit Data for Figure 1-175. Fin me. $\quad \mathrm{F}$ in kilohms. C in $\mu \mu \mathrm{f}$. L in $\mu \mathrm{h}$. NA (not applicable) menns that no connections of any kind exist between points indicated. Question mark (1) indicates that schematic of the assousted part of the circuit is not available.


Figure 1-175. Continued

| $\mathrm{R}_{0}$ | $\mathrm{R}_{10}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | $\mathrm{C}_{3}$ | $C_{4}$ | $\mathrm{C}_{4}$ | $\mathrm{C}_{6}$ | $\mathrm{C}_{7}$ | $\mathrm{C}_{8}$ | $C_{9}$ | $\mathrm{L}_{1}$ | $L_{2}$ | L/3 | $\mathrm{L}_{4}$ | $L_{s}$ | $\mathrm{V}_{1} \mathrm{~V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1000 | 200 | $\begin{array}{r} 14.3- \\ 43.5 \end{array}$ | $\begin{aligned} & 0.5- \\ & 3.0 \end{aligned}$ | 15 | 1000 | 1000 |  |  | 1.2 |  |  |  |  | GL5670 |
| 1 | NA | 1-8 | 7 | 1500 | 47 | 0.75 | NA | NA | NA | NA | $\infty$ | $\infty$ | $\infty$ | NA | 2-4 | 12AT7 |
| NA | 27 | 0 | 20 | 3000 | 100 | NA | 24 | 500 | 20 | 0 | $\infty$ | $\infty$ | $\infty$ |  |  | 12AT7 |
| NA | 470 | 0 | 104 |  | 470 | 470 | 100 | $\begin{gathered} 25 \\ 0 \end{gathered}$ | 170 | 0 | $\infty$ | $\infty$ | $\infty$ |  |  | 5670 |
| 8.2 | Cath- <br> ode <br> of <br> mixer | 0 | 5 |  | 10 | NA | $\frac{1}{5} \cdot 6-$ | $\infty$ | 10 | 10 | $\infty$ | $\infty$ |  |  |  | 5670 |
| ? | ? | 2-7 | 12 | 2000 | 100 | NA | ? | ? | ? | 7 |  |  |  | ? |  | 12AT7 |


(c)

Figure 1-175. Continued


| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | $F_{\text {z }}$ | F: | F. | CR | $\mathbf{R}_{1}$ | $\mathrm{R}_{\mathrm{z}}$ | $\mathrm{R}_{7}$ | R. | Rs | R. | $\mathbf{R}_{7}$ | $\mathrm{R}_{\mathrm{n}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (G) | Experimental osc |  | 126 | $F_{1}$ |  |  | 9th harmonic; series resistance equal to $\mathrm{K}_{6}$ | 0.05 | 0.05 | 5 | 1.2 | 0.3 |  |  |  |
| (H) | Radio Receiver R-540 ARN-14C | H-F in* jection osc | $\left\|\begin{array}{cc} 44.275- \\ 57.275 \\ \text { crystals) } \end{array}\right\|$ | $2 \mathrm{~F}_{1}$ |  |  | CR-23/U | 100 | 8.2 | 8.2 | 0.033 | 4.7 |  |  |  |
| (I) | Radio Set <br> AN/ARC. <br> 34 (XA-1) | Guard channel injection osc and multiplier | $\begin{aligned} & 55.67- \\ & 58.17 \end{aligned}$ | $\begin{aligned} & 2 F_{1} \\ & \text { and } \\ & 4 F_{1} \end{aligned}$ |  |  | CR-32/U | 0.22 | 0.56 | 33 | 2.7 | 220 | 3.3 | 100 |  |
| (J) | Radio Set AN/ARN21 (XN-2) |  |  | $\mathrm{F}_{1}$ |  |  | CR-23/U | 0.22 | 0.22 | 10 | 1 |  |  |  |  |

Circuit Data for Figure 1-175. Fir me. $R$ in kilohms. $C$ in $\mu \mu$. L in $\mu \mathrm{h}$. NA (not applicable) means that no connections of any kind exist between points indicated. Question mark (?) indicates that schematic of the associated part of the circuit is not available.

[^3]
(J)

| R, | $\mathbf{R}_{19}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | Cs | c. | $\mathrm{C}_{6}$ | Cs | $\mathrm{C}_{7}$ | C | Cs, | $L_{1}$ | $\mathrm{L}_{2}$ | $L_{2}$ | $L_{4}$ | $L_{5}$ | $\mathrm{V}_{1} \mathrm{~V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1000 | 15 | 5.5 | 60 | 11 |  |  |  |  | 0.15 | 0.12 | 0.165 |  |  | $\underset{\text { ench }}{6 / 4}$ |
|  |  | 5 | 10.8-17 | 2000 | 2000 | 390 | 47 | 2000 | 16-19 |  |  |  |  |  |  | 12AT7 |
|  |  | 270 | 470 | 22 | 100 | 5-25 | 3 | 3 |  |  |  |  |  |  |  | $5840\left(\mathrm{~V}_{1}\right)$ |
|  |  | 47 | 47 | 1000 |  |  |  |  |  |  |  |  |  |  |  | 6BE7 |

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| Fig. | Equipment | Purpose | $F_{1}$ | F | F: | $\mathrm{F}_{4}$ | CR | $\mathbf{R}_{2}$ | $\mathbf{R}_{\text {: }}$ | R: | R. | Rs | R. | $\mathbf{R}_{7}$ | $\mathbf{R}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (K) | Signal Generator SG- <br> 34(XA)/ <br> UP | L-F and $m-1$ ose | $\begin{aligned} & 0.10 \\ & 0.18 \\ & 1.75 \\ & 1.85 \\ & 1.90 \\ & 1.95 \end{aligned}$ |  |  |  | $\begin{aligned} & \text { CR-16/U } \\ & \left.(\mathrm{LF})^{\prime}\right) \\ & \left(\mathrm{HF} \mathrm{~F}_{1}\right) \end{aligned}$ | 10 | 1.5 | 0.027 | 560 | 39 | 1000 | 0.27 |  |
| (L) | Signal Generator SG-13/ ARN | $200-\mathrm{mc}$ generator for mixing with lower freq. signals | 50 | 4 F |  |  | CR-23/U | 56 | 3.3 | 0.015 | 0.01 | 0.27 | 0.01 | 0.27 | 2.7 |

Circuit Data for Figure 1-175. F in me. $R$ in kilohms. $C$ in $\mu$, L. $L$ in $\mu \mathrm{h}$. NA (not applicable) means that no connections of any kind exist between points indicated. Question mark (?) indicates that schematic of the associated part of the circuit in not available.


Figure 1-175. Cominued

## Transformer-Coupled Oseiliator

1-392. At the present time, the transformercoupled crystal oscillator (see figure 1-176) is not being widely used. It was during the v-h-f oscillator investigation at the Georgia Institute of Technology for the Signal Corps in 1950, mentioned in the last paragraph, that the transformer-coupled oscillator appeared to be the most promising for all-around versatility and general-purpose use. First, there is the advantage of a single-tube oscillator. Secondly, for low-power output (about four times the crystal power). the frequency stability has been found to be slightly superior to that of the average Butler circuit. Thirdly, with properly designed phase-compensating networks, an untuned pass band of 10 mc is possible. Finally, with a relatively small sacrifice in frequency stability, the circuit design can be such that the power output is increased several fold without exceeding the recommended maximum drive level of the crystal unit. Although the transformer-coupled ascillator can perform satisfactorily at lower frequencies,

(L)
its chief application is for control and generation of harmonic-mode frequencies above 20 mc . The oscillator is generally designed for class-C operation. A significant disadvantage is that the circuit' design for optimum performance characteristics -characteristics that can be approximately duplicated from one oscillator to another of similar de-sign-is generally more difficult to achieve than in other oscillator circuits. This is due chiefly to the difficulty in predicting the effective input impedance of tubes operated class C at frequencies where transit-time and stray-capacitance effects become appreciable. As a result, the theoretical and actual equilibrium conditions frequently are found to differ to a greater degree than in the average series-mode oscillator. More cut-and-try experimentation may prove necessary than would otherwise be the case. The operating principle of the grounded-cathode, transformer-coupled oscillator is closely allied to that of the grounded-grid and grounded-plate versions. The discussion and equations for the transformer-coupled oscillators

| R, | $\mathrm{R}_{10}$ | $\mathrm{C}_{1}$ | C ${ }_{4}$ | C | c. | C. | C. | $\mathrm{C}_{7}$ | C. | C. | $L_{1}$ | $L_{7}$ | $L_{2}$ | $L_{4}$ | $\mathbf{L}_{1}$ | $\mathrm{V}_{1} \mathrm{~V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1200 | 10,000 |  |  |  |  |  |  |  |  |  |  |  |  | $12 \mathrm{AU7}$ |
| 2.7 |  | 500 | 1.7-8.7 | 500 | 100 | 12 | 500 |  |  |  |  |  |  |  |  | 12AT7 |

are, for the most part, based upon the analysis by W. A. Edson.

## PHASE CONSIDERATIONS OF TRANSFORMER-COUPLED OSCILLATOR

1-393. Referring to figure 1-176, the useful load, represented by $R_{L}$, is connected across the secondary of the plate transformer. The chief function of $R_{1}$ is to improve the frequency stability by lowering the resistance of the crystal circuit, and to improve the amplitude stability by reducing the effect of variations in the input resistance of the tube. The parameter $a$ is simply the constant of proportionality relating $\mathrm{R}_{\mathrm{t}}$, to $\mathrm{R}_{3} . \mathrm{C}_{1}$ and $\mathrm{C}_{2}$ are capacitors for tuning out the leakage inductance of the plate and grid transformers, respectively. The leakage inductance is equal to the high-side inductance multiplied by ( $1-k^{2}$ ), where $k$ is the coefficient of coupling. It can be directly measured at the low side of the transformer when the high side is shorted. Both transformers can be, simply, tapped coils. The crystal impedance is assumed to be the series-resonance impedance, $R$. The effective turns ratios, $\mathrm{N}_{1}$ and $\mathrm{N}_{n}$, can be so chosen that $C_{p k}$ and $C_{0}$ annul each other's effects. With the
circuit properly designed, the tube operates into a resistive load, $\mathrm{C}_{1}$ being antiresonant with the dampened coil $L_{1} . I_{s}, I_{L}, I_{c}, E_{1 .}$, and $E_{0}$ (the voltage across the crystal) are in phase with $\mathrm{E}_{1}$. The grid transformer thus provides the required 180-degree phase shift between $\mathrm{E}_{\boldsymbol{\mu}}$ and $\mathrm{E}_{\mathrm{g}}$.
1-394. Where the resistance of the crystal series arm is not small compared with the shunt reactance, $X_{c o}$, the effects of $C_{0}$ can be annulled by the conventional method of connecting an inductor across the crystal unit, by means of mutual inductance between the plate and grid transformers (to be discussed in connection with the grounded-grid oscillator), or by balancing the effects of $C_{\text {。 }}$ against those of $\mathrm{C}_{\mathrm{rw}}$. When the circuit is properly balanced, the crystal unit operates at the resonant frequency of the series arm. When $\mathrm{C}_{0}$ is balanced against $\mathrm{C}_{\mathrm{p}}$, the leading component, $\mathrm{I}_{0}$, of the current through the crystal-that part through $\mathrm{C}_{0}$ passes in its entirety, through $\mathrm{C}_{2}$ and the primary of the grid transformer. Similarly, the current through $\mathrm{C}_{\mathrm{p} \%}, \mathrm{I}_{\mathrm{pk}}$ passes in its entirety, through the secondary of the grid transformer. For this to occur, the voltages induced by the two currents in each section of the grid transformer must exactly


Figure 1-176. (A) Basic circuit of transformer-coupled oxeillotor

(b)

Figure 1-176. (B) Equivalent parallolresonant plate circuit when erystal sapacinance, $C_{o y}$ is balanced by plete-to-grid copacitance, $C_{p q}$

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annul each other. The transformer then appears as a short circuit to both currents. As indicated in figure 1-176 (B), $\mathrm{C}_{\mathrm{a}}$ becomes equivalent to a capacitor shunting the ground-connected half of $L_{p}$, thereby effectively increasing $L_{11}$ and $C_{11}$ becomes equivalent to an increase in $C_{p}$, equal to $C_{p s}$. The balanced state is reached when

$$
\begin{equation*}
I_{0}=N_{g} I_{p g} \tag{1}
\end{equation*}
$$

or

$$
\begin{equation*}
\omega \mathrm{C}_{0} \mathrm{E}_{\mathrm{L}}=\mathrm{N}_{\mathrm{z}} \omega \mathrm{C}_{\mathrm{pg}} \mathrm{E}_{\mathrm{p}} \tag{2}
\end{equation*}
$$

or

$$
\begin{equation*}
C_{p g}=\frac{C_{0}}{N_{k}} \cdot \frac{E_{L}}{E_{p}}=\frac{C_{o}}{N_{k} N_{p}} \tag{3}
\end{equation*}
$$

Equation (3) can generally be realized with practical values of $N_{g}$ and $N_{p}$ if $C_{p g}$ is on the order of 0.05 to $0.1 \mu \mu$. Such values of $C_{\text {wa }}$ can be obtained with screen-grid tubes but not with triodes unless a d-c blocked inductive arm is connected between plate and grid to annul most of the capacitance.

## GAIN REQUIREMENTS OF TRANSFORMER-

 COUPLED OSCILLATOR1-395, Referring to figure 1-176 (A), it can be seen that at equilibrium,

$$
G_{1} G_{2} G_{3} G_{4}=\frac{E_{\mathrm{g}}}{E_{\mathrm{g}}} \cdot \frac{\mathrm{E}_{\mathrm{L}}}{\mathrm{E}_{\mathrm{F}}^{\prime}} \cdot \frac{\mathrm{E}_{1}}{\mathrm{E}_{\mathrm{L}}} \cdot \frac{\mathrm{E}_{\mathrm{g}}}{\mathrm{E}_{1}}=1
$$

1-395 (1)
where

$$
\begin{align*}
& G_{1}=\frac{E_{p}}{E_{\mathrm{a}}}=\frac{I_{p} Z_{p}}{E_{\mathrm{g}}}=\frac{\mu Z_{p}}{R_{p}+Z_{p}}=g_{n} Z_{p} \\
& \text { 1-395 (2) } \\
& \mathrm{G}_{2}=\frac{\mathrm{E}_{\mathrm{L}}}{\mathrm{E}_{\mathrm{p}}}=\frac{1}{\mathrm{~N}_{\mathrm{p}}}  \tag{3}\\
& \mathrm{G}_{3}=\frac{\mathrm{E}_{1}}{\mathrm{E}_{\mathrm{L}}}=\left(\frac{\mathrm{R}_{1} \mathrm{R}_{\mathrm{g}}^{\prime}}{\mathrm{R}_{1}+\mathrm{R}_{\mathrm{g}}{ }^{\prime}}\right) \cdot\left(\frac{1}{\mathrm{R}+\frac{\mathrm{R}_{1} \mathrm{R}_{\mathrm{g}}^{\prime}}{\mathrm{R}_{1}+\mathrm{R}_{\mathrm{g}}^{\prime}}}\right) \\
& =\frac{R_{1}}{R+R_{1}}  \tag{4}\\
& \mathbf{G}_{4}=\mathbf{N}_{\mathrm{R}} \tag{5}
\end{align*}
$$

$R_{k}^{\prime}$ in equation (4) is the effective resistance of the grid transformer as it appears in parallel with $R_{1}$. It is equal to $E_{1}{ }^{2}$ divided by the grid losses. Thus,

$$
R_{\mathrm{E}}^{\prime}=\frac{\mathrm{E}_{1}^{2}}{\mathrm{P}_{\mathrm{g}}}=\frac{(\text { eff }) \mathrm{R}_{\mathrm{g}} \mathrm{E}_{\mathrm{I}}^{2}}{\mathrm{E}_{\mathrm{g}}{ }^{2}}=\frac{\text { (eff) } \mathrm{R}_{\mathrm{g}}}{\mathrm{~N}_{\mathrm{g}}{ }^{2}} \quad 1-395(6)
$$

where (eff) $R_{r}$ is the effective grid resistance which takes into account the gridleak losses and the transit-time loading. For small values of $\mathrm{N}_{6}$, the $R_{g}{ }^{\prime}$ losses can be considered negligible. The plate power can be assumed to be,

$$
\begin{align*}
P_{p} & =I_{s} E_{L}=\frac{E_{L}^{2}\left(R_{L}+R+R_{1}\right)}{R_{L}\left(R+R_{1}\right)} \\
& =\frac{E_{L}^{2}\left(R+R_{1}+a R_{1}\right)}{a R_{1}\left(R+R_{1}\right)}
\end{align*}
$$

and

$$
Z_{p}=\frac{E_{p}^{2}}{P_{p}}=\frac{a N_{p}^{2} R_{1}\left(R+R_{1}\right)}{R+R_{i}+a R_{1}}
$$

on combining equations (2), (3), (4), (5), and (8), we find that at equilibrium

$$
\begin{equation*}
G_{1} G_{2} G_{3} G_{4}^{*}=\frac{g_{m} a N_{p} N_{s} R_{1}^{2}}{R+R_{1}(1+a)}=1 \tag{9}
\end{equation*}
$$

## Q DEGRADATION IN TRANSFORMERCOUPLED OSCILLATOR

1-396. In Edson's analyses of series-mode oscillators, he employs a useful term which he calls the $Q$ degradation of the crystal unit. It is defined

$$
\begin{equation*}
\mathrm{D}=\frac{\mathbf{R}_{\mathrm{o}}}{\mathbf{R}} \tag{1}
\end{equation*}
$$

where $R_{e}$ is the total resistance which the crystal must operate into. In the transformer-coupled oscillator, assuming that the transformer impedances that the crystal faces are large compared with $R_{L}$ and $R_{1}$ of figure 1-176,

$$
\begin{equation*}
D=\frac{R+R_{1}(1+a)}{R} \tag{2}
\end{equation*}
$$

As discussed in paragraph 1-241, the frequency stability of the series-resonant crystal unit is directly proportional to the $Q$ of the crystal circuit. It is therefore directly proportional to $\frac{Q}{D}$, where $Q$ is the $Q$ of the crystal, itself. Thus, with a given crystal unit, the frequency stability varies inversely with $D$. If the minimum $Q$ of a crystal unit is estimated from the maximum permissible $C_{o}$, from the frequency, the harmonic, the particular crystal element, and the maximum permissible
series resistance, and if the required frequency stability is known, then the maximum permissible D can be determined from the random phase shifts to be expected during operation. In the average circuit, it is sufficient, simply, to keep D as low as possible consistent with the output desired. When $R_{r}$ is expressed as a function of $a, R$, and $D$, the loop gain as defined by equation 1-395 (9) becomes

$$
G_{1} G_{2} G_{3} G_{4}=\frac{g_{m} a N_{p} N_{8} R(D-1)^{2}}{D(a+1)^{2}}
$$

$1-396(3)$

## LOAD-TO-CRYSTAL POWER RATIO OF TRANSFORMER-COUPLED OSCILLATOR

1-397. The ratio of the load to the crystal power is

$$
P_{L} / P_{c}=\frac{I_{L}{ }^{2} R_{L}}{I_{e}{ }^{2} R}=\frac{(D+a)^{2}}{a(a+1)(D-1)}
$$

It is generally desired to have the power ratio as high as is consistent with satisfactory frequency stability. With a given value of $D$, the ratio becomes large as a is made small. If the design is based on obtaining a given minimum output with a given value of $D$ when the crystal-unit resistance is a maximum (minimum D), the value of a can be determined by equation (1), and equation 1-396 (3) can be used to determine the value of $\mathrm{N}_{\mathrm{p}} \mathrm{N}_{\mathrm{k}}$ most likely to produce the required $\mathrm{g}_{\mathrm{m}}$ for the crystal to be driven at the desired level.

## BROAD-BAND CONSIDERATIONS IN THE TRANSFORMER-COUPLED OSCILLATOR

 1-398. For broad-band untuned operation it is important to have $\mathrm{Z}_{\mathrm{p}}$ and $\mathrm{Z}_{8}$ (the impedance faced by the grid) and the plate and grid capacitances as small as possible. Assuming that $\mathrm{R}_{\mathrm{g}}$ is large compared with the resistance appearing across the secondary of the grid transformer.$$
\begin{equation*}
Z_{k}=\frac{N_{0}{ }^{2} R_{1}(R+a R)}{a R_{1}+R_{1}+R} \tag{1}
\end{equation*}
$$

or

$$
\begin{equation*}
Z_{g}=\frac{N_{z}(D+1 / a)}{g_{m} N_{p}(D-1)} \tag{2}
\end{equation*}
$$

Also, $\mathrm{Z}_{\mathrm{p}}$ can be expressed as

$$
\begin{equation*}
Z_{p}=\frac{N_{p}(D+a)}{g_{m} N_{a}(D-1)} \tag{3}
\end{equation*}
$$

To keep $Z_{p}$ and $Z_{8}$ low, it is desirable that $N_{p}$ and
$\mathrm{N}_{\mathrm{g}}$ be as small as possible. For a given value of $\mathrm{g}_{\mathrm{me}}$ the product $\mathrm{N}_{3} \mathrm{~N}_{4}$ can be a minimum when $\frac{\mathrm{a}}{(\mathrm{a}+1)^{2}}$ (see equation 1-396 (3)) is a maximum. The maximum occurs when $\mathrm{a}=1$. With $\mathrm{a}, \mathrm{D}$, and gm decided upon, equations (2) and (3) give mutually minimum values when $N_{k}=N_{k}$. Thus, for broadband operation, let

$$
\begin{equation*}
Z_{p}=Z_{g}=\frac{D+1}{g_{\mathrm{m}}(D-1)} \tag{4}
\end{equation*}
$$

D should be as large as possible consistent with the required frequency stability.

FREQUENCY STABILITY OF THE TRANSFORMER-COUPLED OSCILLATOR
1-399. The frequency-stability equations for the transformer-coupled oscillator are

$$
\begin{equation*}
\frac{\mathrm{d} \omega}{\omega}=-\frac{\omega \mathrm{Z}_{\mathrm{p}} \mathrm{D}}{2 Q} \mathrm{dC} C_{p} \tag{1}
\end{equation*}
$$

and

$$
\frac{\mathrm{d} \omega}{\omega}=-\frac{\omega \mathrm{Z}_{\mathrm{k}} \mathrm{D}}{2 Q} d \mathrm{C}_{\mathrm{k}}
$$

where $Q$ is the $Q$ of the crystal. When equations $1-398$ (2) and (3) are multiplied by D, it can be shown the $\mathrm{DZ} Z_{y}$ is a minimum when

$$
\begin{equation*}
D=1+\sqrt{1+a} \tag{3}
\end{equation*}
$$

and $\mathrm{DZ}_{8}$ is a minimum when

$$
D=1+\sqrt{1+1 / a}
$$

For both to be a minimum simultaneously, $a$ must be equal to 1 , which means that

$$
\mathrm{D}=1+\sqrt{2}=2.414
$$

Under these conditions, the power ratio, as given by equation 1-397 (1), becomes

$$
\begin{equation*}
\frac{P_{L}}{P_{\mathrm{i}}^{\prime}}=4.12 \tag{6}
\end{equation*}
$$

For larger power outputs, the value of $a$ must be decreased and $N_{n}$ increased. Since the expected variations in the grid capacitance are generally larger than those in the plate capacitance, it is usually desirable to favor the grid circuit insofar as the frequency stability is concerned.
1-400. The greatest probability that the effect of a random variation in the grid capacitance will be
canceled by a random variation in the plate capacitance occurs when the fractional change in frequency due to the average $\Delta \mathrm{C}_{4}$ is equal to that due to the average $\Delta \mathrm{C}_{\mathrm{x}}$. If the average $\Delta \mathrm{C}_{\mathrm{g}}$ is on the order of 10 times the average $\Delta C_{p}$, then $Z_{p}$ should be equal to $10 \mathrm{Z}_{\mathrm{k}}$. Equations 1-399 (1) and (2) will then represent equal average variations in frequency.

## DESIGN PROCEDURE FOR TRANSFORMERCOUPLED OSCILLATOR

1-401. The procedure to follow in designing a transformer-coupled oscillator depends upon the principal objectives to be sought in the design. That is, some fixed requirement serves as a starting point, and the design proceeds from there. One limitation that will be common to all the circuits is that the crystal power rating not be exceeded. This requirement, then, in the general case, can be the initial design consideration. The crystal power is

$$
\begin{equation*}
P_{c}=I_{c}{ }^{2} R=\frac{E_{\mathrm{k}}{ }^{2} R}{N_{\mathrm{g}}{ }^{2} R_{1}{ }^{2}} \tag{1}
\end{equation*}
$$

Also

$$
\begin{aligned}
P_{c} & =I_{c}^{2} R=\frac{E_{\mathrm{L}}{ }^{2} R}{\left(R_{1}+R\right)^{2}}=\frac{E_{p}^{2} R}{N_{p}^{2}\left(R_{1}+R\right)^{2}} \\
& =\frac{\mathrm{g}_{\mathrm{m}}{ }^{2} E_{\mathrm{R}}{ }^{2} \mathrm{Z}_{\mathrm{p}}{ }^{2} \mathrm{R}}{\mathrm{~N}_{\mathrm{p}}^{2}\left(\mathrm{R}+\mathrm{R}_{1}\right)^{2}}
\end{aligned}
$$

or

$$
\begin{equation*}
P_{c}=\frac{\mathrm{g}_{\mathrm{m}}{ }^{2} \mathrm{E}_{\mathrm{k}}{ }^{2} \mathrm{a}^{2} \mathrm{R}_{1}{ }^{2} \mathrm{~N}_{\mathrm{p}}{ }^{2}}{R \mathrm{D}^{2}} \tag{2}
\end{equation*}
$$

Multiplying equation (1) by equation (2) and taking the square root, we have

$$
P_{\mathrm{o}}=\frac{\mathrm{g}_{\mathrm{m}} E_{\mathrm{g}}^{2} a N_{\mathrm{p}}}{\mathrm{D} \mathrm{~N} \mathrm{~N}_{\mathrm{g}}}
$$

Now, ( $\mathrm{g}_{\mathrm{m}} \mathrm{E}_{\mathrm{R}}{ }^{2}$ ) is assumed equal to ( $\mathrm{I}_{\mathrm{p}} \mathrm{E}_{\mathrm{k}}$ ), which, in turn, is principally a function of the excitation voltage and the plate characteristics of the tube to be used. By equation 1-395 (9) (also by equating equation (1) to equation (2))

$$
\begin{equation*}
g_{u}=\frac{R_{c}}{a R_{1}^{2} N_{p} N_{z}} \tag{4}
\end{equation*}
$$

$R_{c}$, remember, is equal to $R D$, the total resistance that the crystal unit operates into. From equation (4) it can be seen that if $R_{c}\left(=R+R_{1}(1+a)\right.$ ) is large compared with the maximum $R\left(=R_{m}\right)$, the equilibrium transconductance will be approximately the same for all values of $R$. On the other
hand, if the minimum $D$ is small, the value of $\mathrm{g}_{\mathrm{m}}$ at minimum $R$ may be as much as one-half its value for $R=R_{m}$. Note that some change must occur in $g_{m}$, and hence in $E_{k}$, if $R$ varies and the rest of the parameters remain constant. To ensure class-C operation for all values of $R$, let the class-A value for $\mathrm{g}_{\mathrm{m}}$ equal twice the equilibrium $\mathrm{g}_{\mathrm{m}}$ according to equation (4), with $R_{c}$ assumed to be a maximum. With the circuit so designed, the amplitude of the oscillations will build up until the tube is cut off a fair proportion of each cycle. Even if class-A operation is desired, a reasonable difference should be allowed between the rated transconductance of the tube and the estimated equilibrium value when $\mathbf{R}_{\mathrm{e}}$ is maximum. This should be sufficient to allow for all expected tolerances in the plate characteristics and in the tuning of the oscillator circuit. The percentage variations in R from one crystal unit to the next is not quite as great in the v-h-f crystals as in the lower-frequency elements, since it is more important that the maximum permissible resistance be kept as small as practicable.
1-402. The ideal design would permit the percentage variations in $\mathrm{E}_{\mathrm{k}}{ }^{2}$ to exactly equal in magnitude the percentage variations in R. Under these conditions, the crystal power, as indicated in equation 1-401 (1) would be the same for each crystal unit. To approach such a design, $g_{m}$, as a function of $E_{\mathrm{g}}$, would have to be known for the particular tube. Such an analysis is beyond the present discussion, but the method to be used would be quite similar to that employed in the analysis of the effects of different values of crystal resistance for the Pierce circuit. As a rule of thumb, the average crystal $R$ in the $v$-h-f range can be assumed to equal $\frac{R_{m}}{2}$. If the transformer-coupled oscillator is designed to drive the crystal unit at 50 per cent of its maximum rated power for the average $R$, there is little danger that crystal units having other values of resistance will be overdriven. For broadband operation the crystal power will be approximately directly porportional to R . When D is small the crystal power increases as $R$ decreases as long as the percentage increase in $\mathrm{E}_{\mathrm{k}}{ }^{2}$ is greater than the percentage decrease in $R$. With $R=\frac{R_{m}}{2}$ and $P_{c}=\frac{P_{c m}}{2}$, equation 1-401 (1) gives an assumed. value for $E_{g}{ }^{2}$, thus

$$
\text { (ave) } E_{\mathrm{k}}^{2}=\frac{\mathrm{P}_{\mathrm{rm}} \mathrm{R}_{1}^{2} \mathrm{~N}_{\mathrm{k}}{ }^{2}}{\mathrm{R}_{\mathrm{tm}}}
$$

or

$$
\begin{equation*}
\text { (ave) } E_{\mathrm{z}}=N_{\mathrm{k}} R_{1} \sqrt{\mathrm{P}_{\mathrm{cam}} / R_{\mathrm{z}}} \tag{1}
\end{equation*}
$$

Note that equation (1) also gives the value of $\mathrm{E}_{\mathrm{x}}$ which would exist if a crystal of maximum resistance were driven at its rated level. However, equation (1) is less important for determining $\mathrm{E}_{\boldsymbol{k}}$ than it is for determining $\mathrm{N}_{\mathrm{k}}$. It is assumed that a class-C value of $\mathrm{g}_{\mathrm{m}}$ has been agreed upon. An approximate value of $E_{g}$ corresponding to the chosen $g_{u}$ is thus already determined. After the value of $R_{1}$ is decided upon, equation (1) can serve to determine $\mathrm{N}_{\mathrm{g}}$.
$1-403$. The design procedure followed so far can generally be applied to any transformer-coupled oscillator. A v-h-f pentode and a harmonic seriesmode crystal unit are selected. Regulated screen and plate voltages for the tube are decided upon. An approximate class- $C$ value of $g_{m}$ and the corresponding $E_{g}$ are estimated, and average values of $P_{c}$ and $R$ are assumed. Once that $D$ and $a$ have been selected according to the particular requirements of the oscillator, the $\frac{N_{n}}{N_{n}}$ ratio can be determined from equation $1-401(3)$, and $N_{*}$ from equation 1-402 (1). Or, in case a particular $\frac{N_{8}}{N_{f}}$ ratio is to be preferred, $a$ and $D$ can be determined with the aid of equation $1-401$ (3). An alternative approach, which is the one to be followed when using the table in paragraph 1-404, is to first determine optimum values for $D, a$, and $N_{v} / N_{g}$, assume an average crystal $R=\frac{R_{m}}{2}$ and a crystal power equal to $\frac{P_{s m}}{2}$, and use equation 1-401 (3) to determine the value of $g_{m} \mathbf{E}_{\mathrm{g}}{ }^{2}\left(=\mathrm{I}_{\mathrm{p}} \mathrm{E}_{\mathrm{g}}\right)$. The next problem is to determine what value of $\mathrm{E}_{\mathrm{g}}$ will produce the required value of $I_{p}, \mathrm{E}_{\mathrm{g}}$ when the tube is operating into a plate impedance that is small relative to the tube $R_{1}$. The equations relating $I_{1}$ to $E_{6}$ in the analysis of the Pierce circuit, or rather the basic methods used to derive the equations, are applicable here if modified properly. Since some trial-and-error will be required regardless, it may well be preferable to determine the correct $\mathrm{E}_{\mathrm{x}}$ empirically. The selected vacuum tube can be driven by an external generator having a variable output at a frequency near the actual frequency for which the oscillator is to be designed. The tube should operate into a small resistive impedance and the gridleak resistance should be the same as that to be used in the final design. $E_{g}$ should be varied until the measured $I_{p}$ is such that the product $I_{p} E_{g}$ agrees with the value computed from equation $1-401$ (3). With $\mathrm{E}_{\mathrm{k}}$ approximately known, $\mathrm{N}_{\mathrm{k}}$ can be determined by means of equation 1-401 (1), 1-404. The dimensionless equations listed below relate the various parameters. These equations,
some of which have already been given, are also useful in determining the various circuit voltages and currents when $E_{g}$ is known, or the requirements thereof, and in comparing the characteristies of oscillators of different design.

$$
\begin{array}{ll}
g_{m} Z_{b}=\frac{N_{p}(D+a)}{N_{k}(D-1)} & 1-404 \\
g_{m} Z_{k}=\frac{N_{k}(D+1 / a)}{N_{p}(D-1)} & 1-404 \\
N_{p}^{2} g_{m} R=\frac{N_{p} D(a+1)^{2}}{N_{k} a(D-1)^{2}} & 1-404 \\
N_{k}^{2} g_{m} R=\frac{N_{p} D(a+1)^{2}}{N_{p} a(D-1)^{2}} & 1-404 \\
R_{1} / R=\frac{D-1}{a+1} & 1-404 \\
P_{L} / g_{m} E_{k}^{2}=\frac{N_{p}(D+a)^{2}}{N_{k} D(D-1)(a+1)} \\
P_{L} / P_{0}=\frac{(D+a)^{2}}{a(a+1)(D-1)} & 1-404
\end{array}
$$

The following table, prepared by the v-h-f oscillator research team at the Georgia Institute of Technology, lists the quantitative relations that hold for five typical designs of the transformer-coupled oscillator. $D$, a, and the $N_{1} / N_{k}$ ratio are predetermined to provide optimum or practical operating characteristics according to five different objectives.
A. Symmetrical circuit design that yields minimum values of $Z_{1}, D$ and $Z_{q} D$. By equations $1-399$ (1) and (2), this design permits maximum frequency stability if the average variations in $C_{1}$ and $C_{k}$ are approximately equal. Low power output. Narrow bandwidth.
B. Nonsymmetrical grid and plate impedances. Designed for optimum frequency stability when (ave) $\Delta C_{k}=10$ (ave) $\Delta C_{p}$. Low power output. Narrow bandwidth.
C. Nonsymmetrical grid and plate impedances. Maximum frequency stability when (ave) $\Delta \mathrm{C}_{\mathrm{g}}=$ 10 (ave) $\Delta C_{p}$, and the power output is 10 times that in design $B$, but the stability is less than that in designs A and B.
D. Symmetrical circuit. Broad-band untuned operation. Frovides small values for $Z_{p} C_{p}$ and $Z_{k} C_{k}$. Tubes require large transconductance and small input and output capacities. $Z_{1}$, and $Z_{g}$ are onehalf those in design $A$. Average $\Delta C_{n}$, assumed equal to average $\Delta \mathrm{C}_{k}$. Frequency stability below
average. Power output low, but greater than that in designs $A$ and $B$.
E. Nonsymmetrical design except that $\mathbf{Z}_{p}=\mathbf{Z}_{\mathbf{s}}$.

High power output-same as that in design $C$. Broad-band untuned operation. Frequency stability below average.

TRANSFORMER-COUPLED OSCILLATOR DESIGNS

| Parameter | Value of Parameter |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Design A | Design B | Design C | Design D | Design E |
| $\mathrm{Z}_{\mathrm{p}} / \mathrm{Z}_{\mathrm{g}}$ | 1 | 10 | 10 | 1 | 1 |
| a | 1 | 1 | 0.0985 | 1 | 0.24 |
| D | 2.414 | 2.414 | 2.414 | 10.65 | 10.65 |
| $\mathrm{~N}_{\mathrm{p}} / \mathrm{N}_{\mathrm{g}}$ | 1 | $\sqrt{10}$ | 7.07 | 1 | 1.165 |
| $\mathrm{~g}_{\mathrm{m}} \mathrm{Z}_{\mathrm{p}}$ | 2.414 | 7.63 | 12.55 | 1.207 | 1.315 |
| $\mathrm{~g}_{\mathrm{m}} \mathrm{Z}_{\mathrm{g}}$ | 2.414 | 0.763 | 1.255 | 1.207 | 1.315 |
| $\mathrm{~g}_{\mathrm{m}} \mathrm{Z}_{\mathrm{p}} \mathrm{D}$ | 5.83 | 18.4 | 30.3 | 12.85 | 14.10 |
| $\mathrm{~g}_{\mathrm{m}} \mathrm{Z}_{\mathrm{g}} \mathrm{D}$ | 5.83 | 18.4 | 30.3 | 12.85 | 14.0 |
| $\mathrm{~N}_{\mathrm{p}}{ }^{2} \mathrm{~g}_{\mathrm{m}} \mathrm{R}$ | 4.828 | 15.25 | 104.0 | 0.457 | 0.854 |
| $\mathrm{~N}_{\mathrm{g}}{ }^{2} \mathrm{~g}_{\mathrm{m}} \mathrm{R}$ | 4.828 | 1.525 | 2.10 | 0.457 | 0.63 |
| $\mathrm{P}_{\mathrm{L}} / \mathrm{P}_{\mathrm{g}}$ | 4.12 | 4.12 | 41.2 | 7.05 | 41.2 |
| $\mathrm{R}_{\mathrm{i}} / \mathrm{R}$ | 0.707 | 0.707 | 1.285 | 4.825 | 7.78 |
| $\mathrm{P}_{\mathrm{L}}$ | 1.705 | 5.4 | 11.9 | 0.662 | 1.08 |
| $\mathrm{~g}_{\mathrm{m}} \mathrm{E}_{\mathrm{g}}$ |  |  |  |  |  |

MODIFICATIONS OF TRANSFORMER-

## COUPLED OSCILLATOR

1-405. Four modifications of the basic trans-former-coupled oscillator are shown in figure 1-177. Circuits (A), (B), and (C) are experimental models that were designed at the Georgia Institute of Technology, but not in accordance with the designs given in paragraph 1-404. Circtit (D) is an oscillator in actual use that has been designed specifically to operate with Crystal Unit CR-24/U without driving the crystal beyond its Military-Standard level. Figure 1-177 (A) is a
low-power circuit intended to be operated within a band of $\pm 2$ per cent of 55 mc . When tested with a number of crystal units having overtone frequencies between 50 and 60 mc , the circuit, with $\mathrm{L}_{\mathrm{n}}$ and $\mathrm{L}_{\mathrm{g}}$ adjusted to be antiresonant with $C_{p}$ and $C_{k}$, respectively, at 55 mc , showed the following operating characteristics. Figure 1-177 (D) shows a slug-tuned transformer-coupled oscillator that employs a battery-operated subminiature tube. This oscillator is used in Radio ReceiverTransmitter RT-159A/URC-4.

| $\hat{L}$ <br> $(\mathrm{mc})$ | Harmonic | $C_{0}$ <br> $(\mu \mu \mathrm{f})$ | R <br> $(\mathrm{ohms})$ | Stability <br> $(\mathrm{ppm} /$ volt $)$ | $\Delta f$ <br> $(\mathrm{kc})$ | $\mathrm{P}_{\mathrm{L}}$ <br> $(\mathrm{mw})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 5 | 5 | 48 | 0.6 | 1.5 | 100 |
| 54 | 9 | 5 | 60 | 0.18 | 0.5 | 80 |
| 54.8 | 7 | 6 | 80 | 0.11 | 0.0 | 50 |
| 58.3 | 7 | 8 | 82 | 0.625 | 1.4 | 40 |
| 60 | 3 | 18 | 25 | 0.66 | 1.7 | 40 |

$\Delta f$ is the difference between the operating frequency and the series-resonance frequency of the crystal unit as measured with Crystal Impedance Meter TS-683/TSM. Figure 1-177 (B) is a circuit intended for broad-band untuned operation with a center frequency at 63 mc . Satisfactory operation was obtained on a crystal plug-in basis from 53 to 73 mc . The designers recommend that the phase-
compensating network, which was selected with the help of chart I, page 445, "Network Analysis and Feedback Amplifier Design," Bode, be shifted from the grid to the plate circuit. Figure 1-177 (C) is a circuit designed to provide an output approaching 1 watt at 50 mc . Due largely to difficulties in predicting the input resistance of the vacuum tube, the differences between the initial


Figure 1-177. Modifications of tronsformer-coupled ascillotor for: (A) High stability. (E) Untuned broed bend. (C) Large output. (D) Slug-tuned, narrow band
design and the final adjustments (the latter shown in figure 1-177(C)) were quite large. The operating characteristics of the circuit are given below :

Frequency stability $=0.3 \mathrm{ppm} /$ volt D-C power input $=1.8$ watts

R-F power output $=0.6$ watt
Crystal power $=0.02$ watt
Efficiency $=33$ per cent
$P_{L} / P_{c}=30$
Grid bias $=-19$ volts

## Grounded-Grid Oselliator

1-406. The grounded-grid oscillator, or single-tube Butler oscillator (see figure 1-178) is very similar in principle to the transformer-coupled oscillator. In fact, it can be described as a transformercoupled oscillator in which the feedback is cathodecoupled to the input. The cathode coupling eliminates the need for phase reversal in either the plate or input transformer. As indicated in figure 1-178, the input transformer can be reduced to an r-f choke. For the plate circuit. an autotransformer permits a maximum coefficient of coupling. Either a triode or pentode can be used. Although operable at lower frequencies, the oscillator is usually employed in the v-h-f range. The low input impedance reduces the effect of variations in the cathode capacitances. Unless the tube is operated class $C$, the crystal operates into a relatively lowresistance circuit. The power output is lower than that obtainable with a transformer-coupled oscillator, but for small outputs the frequency stability
is quite high and the load is more readily shielded from the input. This latter feature reduces the possibility that the oscillator will operate at frequencies other than that of the desired mode of the crystal. The shunt capacitance of the crystal unit should be compensated by a broad-band antiresonant inductor, or by other means. The most dependable method for use over a wide range of frequencies is to introduce mutual inductance between the input transformer or choke and the plate transformer. This can be attained by winding the cathode inductor on the same form as the plate transformer is wound. The correct coefficient of coupling between the input and plate inductors is the one that permits the crystal to vibrate at its true motional-arm resonance. For a theoretical discussion of this mode of capacitance compensation, see Edson et al. The grounded-grid oscillator is most advantageous to use when maximum compactness and simplicity are desired in a low-power, broad-band, untuned v-h-f oscillator. There is the very important additional advantage that the oscil-

(b)


Figure 1-178. Basic greunded-grid oscillator and equivalent circuit progressively simplified

Section I
Crystal Oscillators
lator can be readily designed so that both the output amplitude and the frequency stability are virtually independent of the crystal resistance.

## ANALYSIS OF GROUNDED-GRID OSCILLATOR

1-407. Referring to figure 1-178, it will be assumed that the plate circuit is tuned to the desired harmonic, series-resonance frequency of the crystal, that the resistance in the plate tank is negligible, that the grid current is negligible, that the autotransformer coefficient of coupling is unity, that the cathode-to-ground capacitance is antiresonant with the cathode choke, and that the r-f current through the choke is negligible. Under these conditions the equivalent r-f circuit of the oscillator is that shown in figure 1-178(B). All voltage symbols are treated as unsigned. The polarities shown correspond to the instantaneous polarities that hold during the positive alternations of the r-f grid voltage, $E_{F}$. The current arrows point in the instantaneous direction of the in-phase electron flow. The reactive component of the plate tank current is not represented, although in reality it is primarily the "flywheel" current that produces the voltages $E_{1}$ and $E_{2}$. This reactive current in the tank is that which flows through $\mathrm{C}_{\mathrm{p}}$ and is equal to ${ }_{\omega} C_{p} E_{L}$. If $R_{L}$ were reduced to zero, there would be no reactive current and the transformer would effectively short-circuit the crystal to the plate. Of course, oscillations could not exist under these conditions, if for no other reason than the fact that $E_{2}$ would be reduced to zero and $E_{g}$, being simply the voltage across the crystal unit, would be displaced 180 degrees from the phase required for oscillations to be maintained. $\mathrm{E}_{\mathrm{z}}$ must be greater than $\mathbf{E}_{0}$. The important feature to remember is that insofar as the resistive component of the current is concerned the action of the autotransformer is the same as that of a conventional transformer when the primary and secondary circuits are connected in parallel as shown in figure 1-178 (B). Note, however, that the turns ratio, $N$, is defined as the ratio of the total turns to the turns comprising $L_{2}$.
1-408. The power fed to the transformer is simply

$$
P_{L}=I_{L} E_{L}=I_{p} E_{1} \quad 1-408(1)
$$

Now,

$$
E_{L}=E_{1}+E_{2}=E_{1}+\frac{E_{L}}{N}
$$

or

$$
\begin{equation*}
\mathbf{E}_{\mathrm{L}}=\frac{\mathrm{NE}}{\mathrm{E}}{ }_{\mathrm{N}}-1 \tag{2}
\end{equation*}
$$

So

$$
\begin{equation*}
I_{L}=\frac{I_{\mathrm{v}} E_{1}}{E_{\mathrm{L}}}=\frac{(N-1) I_{\mathrm{D}}}{N} \tag{3}
\end{equation*}
$$

And since

$$
\begin{equation*}
I_{p}=I_{L}+I_{1} \tag{4}
\end{equation*}
$$

We have

$$
\begin{equation*}
I_{p}=\frac{(N-1) I_{p}}{N}+I_{1} \tag{5}
\end{equation*}
$$

or

$$
\mathrm{I}_{\mathrm{p}}=\mathrm{NI} I_{1}
$$

and

$$
\begin{equation*}
I_{L}=I_{1}(N-1) \tag{7}
\end{equation*}
$$

The ratio of the output to the crystal power is
$P_{\mathrm{L}} / \mathrm{P}_{\mathrm{o}}=\mathrm{I}_{\mathrm{L}}{ }^{2} \mathrm{R}_{\mathrm{L}} / \mathrm{I}_{\mathrm{p}}{ }^{2} \mathrm{R}=\frac{\mathrm{R}_{\mathrm{L}}}{\mathrm{R}}\left(\frac{\mathrm{N}-1}{\mathrm{~N}}\right)^{2}=\mathrm{Z}_{\mathrm{L}} / \mathrm{R}$

Note that for a given turns ratio, the power ratio is directly proportional to the resistance ratio. The term $R_{L}\left(\frac{N-1}{N}\right)^{2}$ is simply the equivalent load resistance, $Z_{L}$, that the transformer presents to $I_{p}$. The total impedance across the vacuum tube is thus

$$
\begin{equation*}
Z_{p}=R_{L}\left(\frac{N-1}{N}\right)^{2}+R=Z_{L}+R \tag{9}
\end{equation*}
$$

1-409. It is convenient to imagine that the ground connection is at the point $G^{\prime}$ in figure 1-178. That is, let $G^{\prime}$ be our point of reference. Insofar as the $r-f$ circuit is concerned such a supposition requires no alteration in the currents and voltages involved, but it does simplify the visualization of the circuit charactistics. The supposition does not mean that there is no difference in the r-f potential between $G^{\prime}$ and the actual ground. With $G^{\prime}$ in figure 1-178 (B) assumed to be the ground connection, it can be seen that the tube is effectively connected as a cathode follower except that no load is taken from the cathode circuit. The crystal $R$ is the cathode resistance, and $E_{2}$ is the voltage input to the grid circuit. As discussed in the analysis of the twotube Butler circuit and as illustrated in figure 1-173, the cathode-follower type of circuit can be represented by an equivalent circuit in which the plate-circuit resistance, exclusive of the cathode resistance, is equal to $\frac{1}{\mu+1}$ times the actual re-
sistance. Also, the equivalent generator voltage is $\frac{1}{\mu+1}$ times the conventional value that would be assumed if the cathode resistance were not present. As applied to the grounded-grid oscillator, the equivalent circuit is that shown in figure 1-178(C). Care must be taken not to interpret the power supplied to the plate-circuit resistances as being reduced by a factor of $\frac{1}{\mu+1}$. With $\mu$ and $R_{p}$ assumed large compared with unity and $Z_{11}$, respectively, circuit ( $C$ ) reduces to circuit (D).

## LOOP GAIN IN GROUNDED-GRID OSCILLATOR

1-410. At equilibrium
$G_{1} G_{2} G_{3} G_{4}=\frac{E_{0}}{E_{2}} \cdot \frac{E_{1}}{E_{0}} \cdot \frac{E_{L}}{E_{1}} \cdot \frac{E_{2}}{E_{L}}=1$
1-410 (1)
where

$$
G_{1}=\frac{E_{o}}{E_{2}}=\frac{\mu R}{R_{p}+Z_{L}+R(\mu+1)}=\frac{R}{\frac{1}{g_{m}}+R}
$$

$$
1-410(2)
$$

$\mathrm{G}_{2}=\mathrm{E}_{1} / \mathrm{E}_{\mathrm{o}}=\mathrm{Z}_{\mathrm{L}} / \mathrm{R}=\frac{\mathrm{R}_{\mathrm{L}}(\mathrm{N}-1)^{2}}{\mathrm{RN}^{2}} 1-410(3)$
$\mathrm{G}_{3}=\mathrm{E}_{\mathrm{L}} / \mathrm{E}_{1}=\mathrm{N} /(\mathrm{N}-1) \quad 1-410(4)$
$G_{4}=E_{2} / E_{L}=1 / N$
Equation (2) simply represents the gain of a cathode follower. It can be derived from the equivalent circuits in figure $1-178$ in a manner similar to the cathode follower gair derivation in the analysis of the two-tube Butler circuit. In combining equations (2), (3), (4), and (5), we have
$\mathrm{G}_{1} \mathrm{G}_{2} \mathrm{G}_{3} \mathrm{G}_{4}=\frac{\mathrm{N}^{2}\left(\mathrm{R}_{\mathrm{p}}+\mathrm{R}+\mu \mathrm{R}\right)}{\mathrm{R}_{\mathrm{L}}(\mathrm{N}-1)(\mu+1-\mathrm{N})}=1$

If the approximate value for $G_{1}$ can be assumed, the gain equation can be expressed as

$$
\begin{equation*}
\frac{1}{g_{m}}=\frac{R_{L}(N-1)}{N^{2}}-R=\frac{Z_{L}}{N-1}-R \tag{7}
\end{equation*}
$$

## ACTIVITY CONSIDERATIONS IN GROUNDED-GRID OSCILLATOR

1-411. From equation 1-410(7) we can predict
the relative activity to be expected with different load and crystal resistances. When oscillations first start, the term $1 / g_{m}$ is a minimum. The amplitude increases until $g_{m}$ is reduced by the increase in grid bias to the value that makes equation 1-410 (7) hold. The greater the difference between the initial, zero-bias value of $g_{m}$ and the equilibrium value, the greater will be the final amplitude. The initial $\mathrm{gm}_{\mathrm{m}}$ of the tube should therefore be as large as possible if a maximum output is desired. For a given crystal $R$, the output is increased by increasing $R_{1}$ and making the ratio $\frac{N-1}{N^{2}}$ a maximum, which occurs when $\mathrm{N}=2$. Assuming that $\mathrm{N}=2$, i.e., that the transformer coil is center-tapped at the connection to the crystal, equation 1-410 (7) becomes

$$
1 / \mathrm{g}_{\mathrm{m}}=\mathrm{R}_{\mathrm{L}} / 4-\mathrm{R}=\mathrm{Z}_{\mathrm{L}}-\mathrm{R} \quad 1-411(1)
$$

In equation 1-408(8), it was found that the power ratio, to which we shall assign the symbol $\mathbf{r}\left(=\frac{\mathbf{P}_{\mathbf{L}}}{\mathbf{P}_{\mathbf{r}}}\right)$, is equal to $\mathrm{Z}_{\mathrm{L}} / \mathrm{R}$. On substituting the value rR for $\mathrm{Z}_{\mathrm{L}}$ in equation (1) we find that

$$
r=1+\frac{1}{g_{m} R}
$$

By equations (1) and (2), which hold only when $\mathbf{N}=2$, we see that increasing the amplitude by increasing $R_{\text {L }}$ results in simultaneously increasing the power ratio. Also, note that the minimum power ratio can be predetermined as a function of the class-A value of $g_{m}$ and the maximum permissible $R$ of the crystal unit. If variations in $R$ from crystal unit to crystal unit are not to have a large effect upon the output amplitude, $\mathrm{Z}_{\mathrm{L}}\left(=\frac{\mathrm{R}_{\mathrm{L}}}{4}\right)$ must be large compared with the maximum crystal R. In other words, the minimum power ratio should be as large as possible consistent with the requirements of frequency stability.

## CRYSTAL DRIVE-LEVEL CONSIDERATIONS IN GROUNDED-GRID OSCILLATOR

1-412. If $P_{s \mathrm{~m}}$ is the rated maximum power of the crystal unit, the maximum permissible $I_{p}$ for a given $R$ is

$$
\begin{equation*}
(\max ) I_{p}=(\max ) E_{\mathrm{g}} \mathrm{~g}_{\mathrm{m}}=\sqrt{P_{\mathrm{cm}} / R} \tag{1}
\end{equation*}
$$

Consequently,

$$
\begin{equation*}
(\max ) E_{1}=(\max ) I_{p} Z_{\mathrm{L}}=Z_{L} \sqrt{\mathbf{P}_{\mathrm{cm}} / R} \tag{2}
\end{equation*}
$$

By equations 1-410 (4) and (5)

$$
(\max ) \mathrm{E}_{\mathrm{L}}=\frac{(\max ) \mathrm{E}_{1} \mathrm{~N}}{\mathrm{~N}-1}=\frac{\mathrm{Z}_{\mathrm{L}} \mathrm{~N} \sqrt{\mathrm{P}_{\mathrm{om}} / \mathrm{R}}}{\mathrm{~N}-1}
$$

and

$$
(\max ) E_{2}=(\max ) E_{\mathrm{L}} / N=\frac{Z_{\mathrm{L}} \sqrt{\mathrm{P}_{\mathrm{em}} / R}}{N-1}
$$

$$
1-412(4)
$$

Assuming that $\mathrm{N}=2$, we have

$$
\begin{align*}
\frac{(\max ) \mathrm{E}_{\mathrm{L}}}{2} & =(\max ) \mathrm{E}_{1}=(\max ) \mathrm{E}_{2} \\
& =\frac{\mathbf{R}_{\mathrm{L}}}{4} \sqrt{\frac{\mathrm{P}_{\mathrm{cm}}}{\mathrm{R}}} \tag{5}
\end{align*}
$$

The maximum permissible excitation voltage of the tube with a center-tapped transformer is

$$
\begin{align*}
(\max ) \mathrm{E}_{\mathrm{c}} & =\frac{(\max ) \mathrm{I}_{\mathrm{p}}}{\mathrm{~g}_{w}}=(\max ) \mathrm{E}_{2}-(\max ) \mathrm{E}_{0} \\
& =\left(\frac{\mathrm{R}_{\mathrm{L}}}{4}-\mathrm{R}\right) \sqrt{\frac{\mathrm{P}_{\mathrm{cm}}}{\mathrm{R}}} \quad 1-412(6) \tag{6}
\end{align*}
$$

Equation (6) is to be interpreted as giving the maximum permissible $\mathrm{E}_{\mathrm{g}}$ for a given value of R . The smaller the value of $R$, the larger will be the permissible value of $\mathrm{E}_{\mathrm{g}}$. For v-h-f crystal units in which the shunt capacitance of the crystal is not compensated the minimum $R$ encountered may be on the order of $R_{m} / 5$, where $R_{m}$ is the rated maximum. However, with capacitance compensation all values of $R$ will be less than $R_{m}$; and the minimum may well be on the order of $R_{m} / 9$ or less. The plate characteristics of the vacuum tube and the electrode voltages must be such that an excitation voltage equal to the maximum permissible $E_{z}$, as defined by equation (6), does not cause an effective $I_{p}$ greater than $\sqrt{P_{c m}} / R$. With a sharp-cutoff, grid-leak-biased tube operating into a plate impedance that is small compared with $R_{p}$, the effective $I_{p}$ remains essentially constant as the peak-to-peak amplitude of $E_{r}$ is increased from a value equal to $\left|E_{c o}\right|$ to a value equal to $2\left|E_{c o}\right|$, where $E_{c o}$ is the cutoff bias. As discussed in paragraph 1-312 in connection with the Pierce circuit, the crest amplitude of $I_{p}$ between the crest values of $E_{s}$ equal to $\frac{\left|E_{\mathrm{co}}\right|}{2}$ and $\left|\mathrm{E}_{\mathrm{co}}\right|$ remains approximately equal to $\frac{I_{\mathrm{bm}}}{2}$, where $I_{b m}$ is the zero-bias plate current. There is a small maximum approximately equal to $0.54 \mathrm{I}_{\text {ba }}$ (see equation $1-312$ (21)), but for all practical
purposes it can be assumed that $I_{b}$ is constant for all values of $g_{m}$ between class- $A$ and class-B operation. Since the effective $g_{m}$ is equal to $I_{p} / E_{k}$, the doubling of $\mathrm{E}_{\mathrm{k}}$ without changing $\mathrm{I}_{\mathrm{p}}$ is equivalent to halving $g_{m}$. If oscillations can be maintained at all, the slightest tolerance allowed in $g_{m}$ ensures that the amplitude will build up until the excitation voltage overlaps the lower bend in the $\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{b}}$ curve. Thus, for a sharp-cutoff tube the minimum equilibrium $\mathrm{E}_{\mathrm{gm}}\left(=\sqrt{2} \mathrm{E}_{s}\right.$ ) will very nearly equal $\frac{\left|E_{n n}\right|}{2}$. Since $1 / g_{m}=Z_{L}-R$ when $N=2$, any value of $Z_{L}$ greater than $\mathbf{2 R}_{n}$ can ensure that the $r-f$ plate current, and hence the output, will be the same for all values of $R$ falling within the crystal specifications. All that need be done is to design the circuit for class-A operation on the assumption that $\mathrm{R}=$ $\mathrm{R}_{\mathrm{m}}$. This requires the use of a sharp-cutoff vacuum tube with tube voltages such that

$$
\begin{equation*}
I_{b m i}<2 \sqrt{\frac{2 P_{o m}}{R_{m}}} \tag{7}
\end{equation*}
$$

and the design of the load and transformer network such that

$$
\begin{equation*}
\left|\frac{E_{c o}}{\mathrm{I}_{\mathrm{bm}}}\right|=\frac{\mathbf{Z}_{\mathrm{L}}}{\mathrm{~N}-1}-\mathbf{R}_{\mathrm{m}} \tag{8}
\end{equation*}
$$

Under the conditions defined by equations (7) and (8), a crystal having a maximum $R$ will be driven at or under the rated maximum drive, depending upon whether $I_{b m}$ is equal to, or less than, the vaiue specified in equation (7). If the crystal unit is replaced by another of lower resistance, the crystal current and the output will remain essentially the same. Since $\mathrm{E}_{2}$ will also be unchanged, the increase in the excitation voltage will be entirely that due to the decrease in the voltage across the crystal. The driving power of the crystal will be directly proportional to the crystal R.

## FREQUENCY STABILITY OF GROUNDED-GRID OSCILLATOR

1-413. In the equivalent circuit shown in figure $1-178$ (D), it can be seen that the effective resistance, $R_{c}$, of the crystal circuit is $\left(\frac{1}{g_{m}}+R\right)$. But, $1 / g_{m}=\frac{Z_{L}}{N-1}-R$, thus

$$
R_{0}=\frac{Z_{L}}{N-1}-R+R=\frac{Z_{L}}{N-1} \quad 1-418(1)
$$

If $N=2$,

$$
\begin{equation*}
\mathbf{R}_{\mathrm{c}}=\mathbf{Z}_{\mathbf{L}}=\mathbf{R}_{\mathbf{L}} / 4 \tag{2}
\end{equation*}
$$

Equations (1) and (2) assume that the mu of the tube is large compared with unity, and that $\mathrm{R}_{\mathrm{r}}, \gg \mathrm{Z}_{\mathrm{k}}$. From equation 1-241 (2), the fractional change in frequency required to compensate a small change, $\mathrm{d} \theta$, in the feed-back phase is

$$
\frac{\mathrm{d} \omega}{\omega}=\frac{\mathrm{R}_{\mathrm{c}} \mathrm{~d} \theta}{2 \sqrt{\mathrm{~L} / \mathrm{C}}}=\frac{\mathrm{Z}_{\mathrm{I}}, \mathrm{~d} \theta}{2(\mathrm{~N}-1) \sqrt{\mathrm{L} / \mathrm{C}}}=\frac{\mathrm{R}_{\mathrm{L}} \mathrm{~d} \theta}{8 \sqrt{\mathrm{~L} / \mathrm{C}}}
$$

where $L$ and $C$ are series-arm parameters of the crystal, and equation (2) is assumed to hold. Of significance is the fact that for a given $\mathrm{Z}_{\mathrm{L}}$, the frequency stability is independent of the resistance of the crystal. However, $\left(\frac{Z_{L}}{N}-1\right)$ must always be greater than $R$, else the conditions for oscillation as defined by equation $1-410$ (7) cannot hold. Thus, although the frequency stability can be considered independent of $R$ for a given $Z_{t}$, the effective $Q$ of the crystal circuit must always be less than the lowest actual $Q\left(=\frac{2 \omega L}{R_{m}}\right)$ of the crystal. The larger the $\mathrm{g}_{\mathrm{m}}$ of the tube, the more nearly can this limiting value for the effective $\mathbf{Q}$ be reached, since the more nearly $\left(\frac{\mathrm{Z}_{\mathrm{L}}}{\mathrm{N}-1}\right)$ can be made to approach $\mathrm{R}_{\mathrm{m}}$ in magnitude. But a large $\mathrm{g}_{\mathrm{m}}$ must be accompanied by a low cutoff voltage for the tube, else equations $1-417$ (7) and (8) cannot be made to hold and the crystal will be overdriven. Unfortunately - yet not unexpectedly - the requirements for maximum output are the reverse of those for maximum frequency stability. If the only frequency-stability problem were to maintain the circuit $Q$ as high as possible, the output could be increased without decreasing the stability, by making both $\mathrm{R}_{\mathrm{L}}$ and N large. This could permit an increase in $Z_{\text {I }}$, without affecting the value of $\left(\frac{Z_{\mathrm{L}}}{\mathrm{N}-1}\right)$. On the other hand, if $\mathrm{d} \omega / \omega$ in equation (3) is to be kept small, not only $\left(\frac{\mathrm{Z}_{\mathrm{L}}}{\mathrm{N}-1}\right)$ but also $d \theta$ must be kept to a minimum. Because the input impedance of the tube is very low, changes in the cathode capacitance have a negligible effect on the feed-back phase. The principal variations in the phase are due to changes in the plate and load capacitance. To reduce these effects to a minimum, $\mathrm{Z}_{\mathrm{l}}$, must be as small as possible. Its smallest permissible value will occur when $\left(\frac{\mathrm{N}-1}{\mathrm{~N}^{2}}\right)$ is a maximum; that is, when $\mathrm{N}=2$. Letting $\mathrm{N}=2$ and $R_{1}=8 R_{n,}, Z_{\mathrm{L}}$ will equal $\mathrm{R}_{\mathrm{L}} / 4=2 \mathrm{R}_{\mathrm{n}}$. The crystalcircuit $Q$ for all values of $R$ will then be one-half
the minimum crystal $Q$ to be expected for the particular type of crystal unit. The output will approximately equal $2 \mathrm{P}_{\mathrm{rm}}$ for all values of crystal R . Much larger outputs can be obtained without greatly reducing the frequency stability, by the use of remote-cutoff tubes. With these tubes the $r$-f plate current can be made to vary inversely with the square root of the crystal resistance. Under these conditions, it would be the crystal power that remains constant and the output power that varies with $R$. If $P_{L}=2 P_{c m}$ when $R=R_{m}$, $\mathrm{P}_{\mathrm{t}}=18 \mathrm{P}_{\mathrm{cm}}$ when $\mathrm{R}=\mathrm{R}_{\mathrm{m}} / 9$.

## DESIGN PROCEDURE FOR GROUNDED-GRID OSCILLATOR

1-414. The design procedure depends considerably upon the special requirements to be met by the circuit. As a concrete example assume that a lowpower, $50-\mathrm{mc}$ oscillator requiring a minimum of circuit components and an output amplitude that will not be greatly affected by a replacement of the crystal unit with another of the same frequency is desired. The grounded-grid oscillator is probably the best suited for such a purpose. Assume further that a frequency tolerance of $\pm 0.01$ per cent is required without temperature control for all temperatures between -40 and +90 degrees centigrade. Crystal Unit CR-24/U with a frequency tolerance of $\pm 0.005$ per cent between - 55 and +90 degrees centigrade should be able to provide the required stability. So also will Crystal Unit CR-23/U, but the former unit is mounted in the coaxial holder, the HC-10/U, which is generally to be preferred because its lower inherent shunt capacitance should permit a higher average Q. There is no guarantee of this, since the maximum $\mathrm{C}_{\mathrm{o}}$ is $7 \mu \mu \mathrm{f}$ in each case; however, the CR24/U employs the 5th harmonic and the CR-23/U the 3rd harmonic (thinner crystal) for the $50-\mathrm{mc}$ frequency. The greater CR-24/U L/C ratio should more than offset its slightly higher $\mathrm{R}_{\mathrm{m}}$. Nevertheless, a check should be made to see if crystal units of either type having the desired frequency are currently being manufactured or have been manufactured in the past. If not, serious consideration should be given to the possibiiity of employing a different frequency. The cost of the crystal unit will be less if it is already in production, and the risk that an undue amount of experimentation will be required to produce a crystal unit that meets the military standards at an unexplored frequency can be avoided. If the crystal unit is expected to withstand considerable mechanical shock, the CR24/U must be used, regardless.
1-415. Assume that a $50-\mathrm{mc}$ CR-24/U crystal unit
has been selected. According to Military Standard MS91380, $\mathrm{R}_{\mathrm{m}}=75$ ohms and $\mathrm{P}_{\mathrm{em}}=2 \mathrm{mw}$. By equation 1-412(1)

$$
(\max ) I_{p}=10^{3} \sqrt{\frac{0.002}{75}}=5.2 \mathrm{ma}
$$

According to equation 1-412 (7)

$$
1_{b m}<2 \sqrt{2} \times 5.2=14.7 \mathrm{ma}
$$

Assume that the most available tube is the 6AU6, sharp-cutoff, miniature pentode. Operated at 250 plate volts, a screen voltage of 140 volts provides a zero-bias plate current of approximately 15 ma . The cutoff bias will be approximately -5 volts. Assuming a value of $\mathrm{N}=2$, by equation 1-412(8)

$$
\mathrm{Z}_{\mathrm{L}}=75+\frac{5}{0.015}=410 \mathrm{ohms}
$$

and

$$
\mathrm{R}_{\mathrm{L}}=4 \mathrm{Z}_{\mathrm{L}}=1640 \mathrm{ohms}
$$

The power ratio when $R=R_{m}$ will be

$$
(\min ) \mathrm{r}=\frac{\mathrm{Z}_{\mathrm{L}}}{\mathrm{R}_{\mathrm{m}}}=5.5
$$

The power output for all values of R will be

$$
\mathrm{P}_{\mathrm{L}}=(\min ) \mathrm{r} \mathrm{P}_{\mathrm{cm}}=11 \mathrm{mw}
$$

The crystal unit will operate into an effective resistance equal to 410 ohms. The effective $g_{m}$ of the tube will vary from approximately $3000 \mu$ mhos, when $R$ is a maximum, to approximately 2500 $\mu$ mhos, when $R$ is a minimum. If greater frequency stability is required, $\mathrm{R}_{\mathrm{I}}$ can be decreased by ap-
proximately three-fourths, so that $\mathrm{Z}_{\mathrm{L}}=\mathbf{3 0 0}$ ohms. With this value of $\mathrm{Z}_{\mathrm{L}}$, when R is maximum $\mathrm{gm}_{\mathrm{m}}$ will be $4450 \mu$ mhos. By increasing the screen voltage to 150 volts or slightly greater, an r-f plate current very nearly equal to the maximum permissible for $R_{m}$ can be attained. As $R$ is decreased $I_{p}$ and $P_{L}$ increase somewhat, but the crystal unit will not be overdriven.

## MODIFICATIONS OF THE <br> GROUNDED-GRID OSCILLATOR

1-416. Figure 1-179 shows four different designs of the grounded-grid oscillator which were built and successfully tested at the Georgia Institute of Technology. Because of the high initial transconductances, $0.011 \mu$ mho for the 6J4 and 0.009 for the 6AH6, the oscillation amplitude of these circuits would drive the average Military Standard crystal unit beyond the recommended maximum level. This does not mean that a standard crystal unit will necessarily be in danger of being shattered by the circuits shown, but that the frequency, resistance, and freedom from spurious modes could not be guaranteed by the test standards. To employ the circuits illustrated in figure 1-179, different tubes, or plate-supply voltages may need to be used.
1-417. Figure 1-179 (A) is a narrow-band oscillator with the load connected across the secondary of the plate transformer. Except for the fact that the input "transformer" ( $L_{k}$, having a $1: 1$ voltage ratio) provides no phase reversal, the circuit is very similar to that of the basic transformercoupled oscillator. $R_{L}$, connected as shown, is equivalent to a load resistance of $N^{2} R_{L}$ connected across $L_{p}$. The variable capacitance is for tuning out the transformer leakage inductance. $L_{k}$ is antiresonant with the cathode capacitance, and the


Figure 1-179. Modifications of grounded-grid oscillator. (A) Narrow-band circuit

Section 1
Crystal Oxcillators

(c)


Figure 1-179. Modifications of grounded-grid ascillotor. (B) Brood-band circuit. (C) Circuit for compensating crystal capacitance by mutual inductance. (D) High-efinioncy claza-C circult
cathode resistance broadens the tuning. The circuit was tuned for operation at a center frequency of 55 mc . The plate transformer consists of 12 turns of AWG No. 26 PE wire wound on a Miller
type 69048 slug-tuned coil form and tapped at 4 turns. The circuit operates class B. The operating data for several different crystal units is given below.

| $f$ <br> $(\mathrm{mc})$ | Harmonic | $\mathrm{C}_{0}$ <br> $(\mu \mu \mathrm{f})$ | R <br> (ohms) | Stability <br> $(\mathrm{ppm} /$ volt $)$ | $\Delta f$ <br> $(\mathrm{kc})$ | $\mathbf{P}_{\mathrm{L}}$ <br> $(\mathrm{mw})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 48 | 3 | 14 | 45 | 0.42 | 3 | 55 |
| 50 | 3 | 12.5 | 35 | 0.20 | 1.5 | 103 |
| 54 | 3 | 13.5 | 45 | 0.11 | 9 | 78 |
| 58 | 7 | 9 | 32 | 0.14 | 0.6 | 28 |
| 60 | 3 | 13 | 25 | 0.24 | 1.6 | 40 |

The frequency stability is measured in average parts per million per volt when the voltage is changed by 50 volts. $\Delta f$ gives the deviation observed between the series-resonance frequency, when measured with CI Meter TS-683/TSM, and the actual oscillator frequency. It would seem that the 54 -mc crystal, which should show the smallest value of $\Delta f$, was influenced by a spurious mode.
1-418. The circuit in figure 1-179 ( B ) is designed for broad-band untuned operation. $L_{p}$ consists of 10 turns of No. 30 PE wire, tapped at 3.3 turns
and wound on a 0.4 -inch-diameter form. The tertiary winding, $\mathrm{L}_{\mathrm{T}}$, consists of 17 turns on a 0.24 inch form that can be slipped inside the $L_{p}$ core by a screw adjustment. The circuit is first tuned with a 1000 -ohm load connected directiy across $L_{p}$ with $L_{T}$ open. Next, with the circuit connected as shown, the coupling between $L_{x}$ and $L_{1}$ is adjusted until the same grid current as before is obtained. All tuning adjustments were made at 57.5 mc . The performance data of this circuit for several different crystals is given below.

| $f$ <br> $(\mathrm{mc})$ | Harmonic | $C_{o}$ <br> $(\mu \mu \mathrm{f})$ | R <br> $(\mathrm{ohms})$ | Grid $I_{\mathrm{C}}$ <br> $(\mu \mathrm{amp})$ | Stability <br> $(\mathrm{ppm} / \mathrm{volt})$ | $\Delta f$ <br> $(\mathrm{kc})$ | $P_{\mathrm{L}}$ <br> $(\mathrm{mw})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 48 | 3 | 14.5 | 25 | 58 | 0.21 | 5 | 41 |
| 50 | 3 | 11 | 28 | 85 | 0.25 | -0.5 | 45 |
| 58.31 | 7 | 8 | 80 | 60 | 0.01 | 0 | 52 |
| 65.31 | 7 | 10 | 80 | 65 | 0.15 | 0.2 | 46 |
| 66.65 | 5 | 4 | 65 | 90 | 0.21 | 2.0 | 50 |
| 67.2 | 7 | 14 | 80 | 62 | 0.07 | 4.0 | 47 |

1-419. The circuit in figure 1-179 ( C ) is designed to compensate the capacitance of the crystal unit by mutual inductance between the plate and cathode inductors instead of by a shunt inductor as in circuit (B). $L_{\mathrm{a}}$ consists of 9 close-wound turns of AWG No. 30 PE wire, tapped at 2.5 turns; $L_{b}$ consists of 4.5 turns of AWG No, 30 PE wire on a thin spacer. The proper coupling adjustment is obtained by substituting a capacitance equal to $\mathrm{C}_{0}$ in place of the crystal and adjusting the circuit to oscillate at the true series-resonance frequency of the motional arm, but only after $L_{n}$ and $L_{b}$ have separately been adjusted to resonate with $\mathrm{C}_{\mathrm{p}}$ and $C_{k}$, respectively, at their computed resonant frequencies $\left(\omega_{a}^{2}=\frac{1}{L_{\mathrm{a}} C_{p}}, \omega_{b}^{2}=\frac{1}{L_{\mathrm{b}} C_{k}}\right.$ ). It can be shown
that

$$
\begin{align*}
& \mathrm{L}_{\mathrm{a}}=\frac{\mathrm{L}_{\mathrm{p}} \mathrm{~N}_{1}^{2} \mathrm{~L}_{\mathrm{o}}}{\left(1-\mathrm{M}^{2}\right)\left(\mathrm{L}_{\mathrm{p}}+\mathrm{N}_{1}^{2} \mathrm{~L}_{0}\right)} \\
& \mathrm{L}_{\mathrm{b}}=\frac{\mathrm{L}_{\mathrm{k}} \mathrm{~N}_{2}^{2} \mathrm{~L}_{0}}{\left(1-\mathrm{M}^{2}\right)\left(\mathrm{L}_{\mathrm{k}}+\mathrm{N}_{2}^{2} \mathrm{~L}_{0}\right)}
\end{align*}
$$

and

$$
\begin{equation*}
M^{2}=\frac{L_{p} L_{k} / N_{2}{ }^{2}}{\left(L_{p}+N_{1}{ }^{2} L_{0}\right)\left(L_{0}+L_{k} / N_{2}{ }^{2}\right)} \tag{3}
\end{equation*}
$$

where $L_{p}$ and $L_{k}$ are the values of the plate-toground and cathode-to-ground inductances, respec-
tively, that would occur if there were no coupling between them, $\mathrm{L}_{0}$ is the imaginary shunt inductance that would be required to antiresonate $\mathrm{C}_{0}$, M is the coefficient of coupling between the plate and cathode inductors, and $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ are the plate and cathode turns ratios, respectively. $\mathrm{N}_{2}$ is simply equal to unity in the circuit shown. The performance data for the circuit is as follows:

$$
\begin{aligned}
& \mathrm{f}=58.31 \mathrm{mc} \\
& \text { stability }=0.28 \mathrm{ppm} / \text { volt } \\
& \mathrm{P}_{\mathrm{L}}=90 \mathrm{mw} \\
& \Delta \mathrm{f}=\text { operating freq minus tested series- } \\
& \text { resonance freq }=-100 \text { cycles } \\
& \Delta \mathrm{f} \text { when } \mathrm{C}_{\mathrm{k}} \text { increased from } 10 \text { to } 13 \mu \mu \mathrm{f} \\
& \quad=-60 \text { cycles } \\
& \Delta \mathrm{f} \text { when } \mathrm{C}_{0} \text { increased from } 8 \text { to } 11 \mu \mu \mathrm{f} \\
& \quad=-45 \text { cycles } \\
& \Delta \mathrm{f} \text { when } \mathrm{C}_{\mathrm{n}} \text { increased from } 6 \text { to } 6.5 \mu \mu \mathrm{f} \\
& \quad=-90 \text { cycles }
\end{aligned}
$$

1-420. The circuit shown in figure 1-179(D) is designed for high-efficiency operation as a small class-C power oscillator. $L_{p}$ consists of 20 turns of AWG No. 28 PE wire wound on a 0.25 -inch coil form and tapped at 1 turn. $L_{x}$ is a 10 -turn, 0.25 -inch-diameter coil of AWG No. 28 PE wire, tapped at 5 turns. The observed performance data for this circuit is as follows:

$$
\begin{aligned}
& f=50 \mathrm{mc} \\
& \text { load voltage }=9 \text { volts } \\
& \text { grid bias }=-10 \text { volts } \\
& \text { load power }=1.9 \text { watts } \\
& \text { crystal power }=0.08 \text { watts } \\
& \text { frequency stability }=0.6 \mathrm{ppm} / \text { volt } \\
& \text { plate dissipation }=3 \text { watts } \\
& \text { efficiency }=63 \text { per cent }
\end{aligned}
$$

## The Grounded-Plate Oscillator

1-421. The vacuum-tube circuit of the groundedpiate oscillator shown in figure $1-180$ is essentially the same as the two-tube Butler oscillator except that a step-up transformer replaces the groundedgrid amplifier of the Butler circuit. The gain of the Butler grounded-grid tube is thus replaced by the gain, $N$, of the transformer in figure 1-180(A). The grounded-plate oscillator is most advantageous when used in the electron-coupled form, as shown in figure 1-180 (C), where the plate circuit can be tuned to provide frequency multiplication. Otherwise, the larger output of the basic trans-former-coupled circuit or the greater simplicity of the grounded-grid circuit make these oscillators preferable to the grounded-plate design insofar as obtaining the same order of frequency stability is
concerned. The grounded-plate oscillator can be designed for larger outputs by providing a step-up transformer in the cathode circuit and removing the r-f voltage from the gridleak resistor, as is shown in figure 1-180(B). This permits the cath-ode-follower to operate into the same output impedance but with a greatly reduced load resistance across the crystal circuit. The output per milliwatt of crystal power is thereby increased. Increasing the power output in this manner makes the oscillator more critical to design and adjust so as to prevent free-running oscillations, particularly if the tube is to be operated class $C$, where the effective input impedance becomes more or less unpredictable at very high frequencies.
1-422. The over-all gain equation of the oscillator in figure 1-180 (A) is

$$
\frac{\mu N R_{2} Z_{k}}{\left(R+R_{2}\right)\left(R_{p}+Z_{k}+\mu Z_{k}\right)}=1 \quad 1-422(1)
$$

where $Z_{k}$ is the total effective resistance between the cathode and ground. Assuming that the resistance presented by the transformer is equal to $R_{n} / N^{2}$ and is much greater than $R_{2}$, we have

$$
\begin{equation*}
Z_{k}=\frac{R_{1}\left(R+R_{2}\right)}{R_{1}+R+R_{2}} \tag{2}
\end{equation*}
$$

The effective resistance into which the crystal operates is

$$
\begin{equation*}
\mathbf{R}_{\mathrm{c}}=\mathbf{Z}_{\mathbf{k}}^{\prime}+\mathbf{R}+\mathbf{R}_{\mathbf{2}} \tag{3}
\end{equation*}
$$

where $Z_{k}{ }^{\prime}$ is the output impedance of the cathode follower as faced by the crystal. If $\mu$ is very large compared with unity,

$$
Z_{k}^{\prime}=\frac{R_{1}}{1+g_{m} R_{1}}
$$

For crystal resistances on the order of 75 ohms or smaller, $R_{1}$ and $R_{2}$ can also be approximately 75 ohms each. Values of $R_{1}=68$ ohms, $R_{2}=100$ ohms, $\mathrm{R}_{\mathrm{n}}=200 \mathrm{~K}$, and $\mathrm{N}=9$ have been recommended for use with a $6 J 4$ triode. The shunt capacitance of the crystal unit, as well as that of the grid and cathode, can be compensated if need be by conventional antiresonant inductors. To be preferred is the method described in the discussion of the two-tube Butler circuit-designing the circuit so that

$$
\begin{equation*}
g_{m} Z_{k}=\frac{C_{g c}}{C_{k}} \tag{5}
\end{equation*}
$$



Figure 1-180. Grounded-plate oscillators. (A) Basic circuit. (B) Circuit for increased power output. (C) Electron-coupled circuit

Section :

figure 1-181. Transitron erystal oscillotor

## Transitron Crystol Oscillator

1-423. The transitron oscillator (see figure 1-181) operates by virtue of the negative transconductance between the suppressor and screen grids of a pentode. The total cathode current of the pentode is little affected by variations in the suppressor voltage, being primarily a function of the potential between the screen and cathode. However, as the suppressor voltage is made more negative, the fraction of the total space current diverted to the screen circuit is increased. The screen voltage therefore tends to follow the suppressor voltage. By connecting a resonant feed-back network between the screen and suppressor, oscillations can be maintained and no phase reversal is necessary. The principal advantage of this circuit is its simplicity and its ability to oscillate with series-mode crystals having comparatively high series resistances. It can be employed in the $v$-h-f range, but unless the crystal resistances are expected to be abnormally high, the relatively large electrode capacitances and the small transconductance make the performance inferior to that of the trans-former-coupled oscillator.
1-424. When the circuit is used with high-resistance crystals it is very important that the crystal shunt capacitance be properly compensated, in order to eliminate the possibility of free-running oscillations. As has been demonstrated by W. A. Edson with the aid of Nyquist diagrams (graphical representations of the over-all loop gain and phase rotation as the frequency is varied from 0 to $\infty$ ), the circuit can be designed to permit only one mode of oscillation if, treating $g_{m}$ as unsigned,

$$
\begin{equation*}
\frac{g_{m} R_{L} R_{g}}{R_{o}+R_{L}+R_{z}}<1 \tag{1}
\end{equation*}
$$

and

1-424 (2)
The condition implied by equation (1) when $g_{m}$ is its maximum possible value means that the loop gain is insufficient to start or maintain oscillations at any frequency unless $R_{0}$ is effectively decreased (such as being bypassed by the series-resonance $R$ of the crystal) so that the left side of the equation is greater than or equal to unity. Equation (2), when satisfied, means that a zero phase shift in the feedback can occur at only one frequency. Thus, if the circuit is tuned for operation at the desired series-mode frequency of the crystal and equations (1) and (2) are satisfied, spurious oscillations will not be possible.
1-425. Note that $\mathrm{C}_{0}$ is effectively increased by the suppressor-to-screen capacitance, so that $L_{0}$ must be smaller than would otherwise be the case. $\mathrm{C}_{1}$ and $C_{s}$ are simply distributed capacitances to ground. Each of the three parallel combinations are antiresonant at the crystal frequency, so $\mathrm{L}_{1} \mathrm{C}_{1}=\mathrm{L}_{0} \mathrm{C}_{0}=\mathrm{L}_{\mathrm{g}} \mathrm{C}_{\varepsilon}=\frac{1}{\omega^{2}}$. Assuming that the antiresonant circuits have impedances $R_{L}, R$ and $R_{k}$, respectively, then if $I_{r^{2}}$ is the $r-f$ screen current, the voltage across the load is

$$
\begin{equation*}
E_{\mathrm{g}^{2}}=\frac{\mathrm{I}_{\mathrm{k} 2} \mathrm{R}_{\mathrm{L}}\left(\mathrm{R}+\mathrm{R}_{\mathrm{g}}\right)}{\mathrm{R}_{\mathrm{L}}+\mathrm{R}+\mathrm{R}_{\mathrm{E}}} \tag{1}
\end{equation*}
$$

The r-f suppressor voltage is

$$
E_{\varepsilon^{3}}=\frac{E_{a^{2}} R_{g}}{R+R_{z}}=\frac{I_{g^{2}} R_{L} R_{k}}{R_{L}+R+R_{k}} \quad 1-425(2
$$

If we assume that $E_{\mathbf{n}^{2}}$ is small compared with the

Section I Crystal Oscillators
d-c screen voltage, and define the suppressor-toscreen transconductance as the change in screen current per change in suppressor-to-cathode volt-age-not per change in the suppressor-to-screen voltage-the gain conditions for equilibrium are, by equation (2),

$$
\frac{E_{x^{3}}}{I_{z^{2}}}=\frac{1}{g_{m}}=\frac{R_{L} R_{g}}{R_{L}+R+R_{z}}
$$

Of the vacuum tubes available, the 6AS6, which has a suppressor-to-screen transconductance of $1600 \mu \mathrm{mhos}$, is probably to be preferred. With this tube, oscillations can be maintained with crystal units having series resistances of well over 1000 ohms. Although oscillations can also be maintained with large values of $R_{L}$ and $R_{k}$, these resistances should be kept as small as practicable so as not to unnecessarily degrade the crystal $Q$ and reduce the frequency stability. The transitron oscillator is also quite useful at low frequencies, particularly with high-resistance crystal units. When a fundamental-mode crystal element is employed, the tuned circuits may not be necessary; but to avoid the possibility of free-running oscillations or unwanted crystal modes, at least the screen circuit should be broadly tuned. (See paragraph 1-590 for discussion of negative-resistance limiting of transitron circuit.)

## Impedance-Inverting Crystal Oscillators

1-426. Impedance-inverting oscillators employ a network similar to that shown in figure 1-182 (A), to permit conventional lower-frequency oscillators to be operated with crystal control in the v-h-f range. A number of these oscillators were designed and tested at the Georgia Institute of Technology under the direction of Mr. W. A. Edson. The discussion to follow is based on the final report of this research. The impedance-inverting network is designed to behave as a quarter-wave line having a characteristic impedance, $Z_{0}=\omega L_{1}$ $=\frac{1}{\omega C_{n}}=\frac{1}{\omega C_{0}}$. With this design, the network always appears as an inverted $Z_{s}$ equal to $Z_{n}=\frac{Z_{0}{ }^{2}}{Z_{n}}$, where $Z_{8}$ is the series-arm impedance of the crystal. If $Z_{b}=0, C_{0}$ is shorted out and $Z_{n}$ is infinite. ( $L_{1}$ is assumed to have a zero loss.) If $Z_{8}$ is infinite, $L_{1}$ is series-resonant with $C_{o}$, and $Z_{n}=0$. If $Z_{4}=Z_{0}$, the network appears as an infinite line with $Z_{n}=Z_{0}$. When $Z_{n}$ is a small inductive reactance, $Z_{n}$ is a large capacitive reactance, and vice versa. With $Z_{0} \gg R$ of the crystal, the network


Figure 1-182. Impodance-inverting oscillator circuits. (A) Basic impedance-inverting network
serves to invert the crystal resistance to a high impedance equal to $Z_{0}{ }^{2} / R$. For a given $C_{n}$, maximum frequency stability is to be had under the quarter-wave line conditions ( $\mathrm{C}_{\mathrm{g}}=\mathrm{C}_{\mathrm{p}}$ ), but, if desired, higher impedances can be had by making $C_{n}$ less than $C_{e}$, or by reducing the effective values of $C_{n}$ and $C_{0}$ with the use of shunt inductors. The shunt inductances, however, should be considerably larger than the values required for antiresonance at the crystal frequency. With $\omega$ equal to the series-arm resonance frequency, and $L_{1}=$ $\frac{1}{\omega^{2} \mathrm{C}_{0}}=\frac{1}{\omega^{2} \mathrm{C}_{\mathrm{n}}}, \mathrm{Z}_{\mathrm{n}}$ appears as an antiresonant resistance when the series arm of the crystal is resonant and $Z_{*}=R$. At frequencies well removed from crystal resonance, the crystal behaves simply as a capacitance, $C_{0}$, so that the network has a second antiresonant frequency, the square of which is $\omega_{2}^{2}=\frac{C_{n}+C_{0}}{C_{n} C_{0} L_{1}}$. To ensure that this second frequency is damped out, a resistance equal to $Z_{0}$ can be connected across the crystal unit.
1-427. Even though the equivalent impedance-inverting network is designed to be antiresonant at approximately the crystal frequency, the operating frequency may well require that the crystal network facing the actual terminal connections be reactive if the necessary phase reversal is to be accomplished. For example, it is necessary that the actual plate-to-grid network appear inductive when used in the Pierce circuit. In the Pierce circuit the fundamental modification introduced by the impedance-inverting circuit is simply the addition of an inductor having a reactance $\omega \mathrm{L}_{1}=\frac{1}{\omega \mathrm{C}_{0}}$ in series with the crystal. It can be imagined that the reactance of the inductor replaces the $X_{i}$ of a

Section I
parallel-resonant crystal unit; and the low seriesresonant $R$ of the crystal approximately replaces its parallel-resonant value, $R_{r v} . C_{n}$ of the network is $C_{p u f}$ of the vacuum tube, if we view the circuit literally. By this interpretation, $\mathrm{C}_{\mathrm{n}}$ is not antiresonant with the inductive branch, but must offer a higher impedance than does the inductor at the operating frequency. On the other hand, if the entire external circuit is viewed in toto by the negative-resistance method, which is the imped-ance-inverting interpretation, $\mathrm{C}_{\mathrm{n}}$ appears as an equivalent capacitance equal to $\mathrm{C}_{10}$ plus the additional amount required to make the network antiresonant. Since this latter interpretation can be employed to illustrate any oscillator circuit that contains a crystal connected in series with an inductance $L_{1}=1 / \omega^{2} C_{0}$, the presence of the series inductance alone could be sufficient to define an impedance-inverting oscillator. The inverted impedance, $Z_{n}$, is related to the impedance of the inductor and crystal branch as the PI of a crystal is related to the equivalent impedance of the crystal unit. Although these questions are somewhat academic, for some readers it may be more helpful to interpret the network in figure 1-182 (A) as an impedance-converting circuit rather than as an inverting circuit. In the transitron circuit, the network is directly used to invert the crystal R to a higher effective resistance, but in other applications the designer may prefer to treat the actual network as an equivalent $X_{e}$ and $R_{e}$ of a parallelmode crystal unit, transferring the equivalent impedances directly to the equations of the basic parallel-resonant oscillators.
1-428. There are two significant advantages to the impedance-inverting type of design. One is that the conventional parallel-resonant circuits can be operated with excellent frequency stability in the v-h-f range. Another is that by using series-mode crystals at the fundamental frequencies, the design restrictions regarding the parallel-resonant type of crystal unit can be avoided. No data is available, but experimentation may show that even in the fundamental-frequency range larger outputs can be obtained with an inductor and a seriesmode crystal without degrading the over-all frequency stability. The chief disadvantage of the impedance-inverting network is that it cannot be used for broad-band untuned operation.

## IMPEDANCE-INVERTING TRANSITRON OSCILLATOR

1-429. An experimental $50-\mathrm{mc}$ impedance-inverting transitron oscillator is shown in figure 1-182 (B). In this circuit, the network, consisting pri-
marily of $L_{1}, C_{n}$, and the crystal, is adjusted to present a resistive impedance between the screen and ground. Since $R_{L}$ is very large compared with the crystal $R$, it can be assumed that $R_{1}$, is effectively connected in parallel with the antiresonant network. $\mathrm{C}_{\mathrm{n}}$ includes a $3-12 \mu \mu \mathrm{f}$ padding capacitor adjusted at $5 \mu$ f, the screen-to-ground capacitance, and the suppressor-to-plate capacitance (the latter is added because the screen is practically bypassed to the suppressor and the plate is at $r$-f ground). $\mathrm{E}_{\mathrm{k} 3}$ in this circuit can be considered equal to $\mathrm{E}_{\mathbf{z}^{2}}$. Thus, the condition required for oscillations to build up is simply that $1 / g_{m}$ be smaller than the actual plate-to-ground resistance. At the plate voltage used, the initial $g_{m}$ is approximately $1500 \mu$ mhos, so $1 / g_{m}=667$ ohms. Ignoring the suppressor-to-ground resistance, the screen operates into an impedance of $R_{R} Z_{n} /\left(R_{L}+Z_{n}\right)=$ 1350 ohms , where $\mathrm{Z}_{\mathrm{n}}=\mathrm{X}_{\mathrm{Ca}^{2} / \mathrm{R}}$. The margin of gain is therefore on the order of two to one. The power delivered to $R_{L}$ was observed to be 15 mw . The frequency deviation was measured at $0.1 \mathrm{ppm} /$ volt. When $R_{1}$ was replaced by a $40,000-\mathrm{ohm}$ resistor, the frequency deviation was found to be only $0.004 \mathrm{ppm} / \mathrm{volt}$. Although the power output is low, the extraordinary independence of the frequency under variations in the supply voltage marks the impedance-inverting transitron oscillator as the most stable to use in the v-h-f range. One of the chief reasons for this stability is very probably the fact that the r-f screen current need contain no reactive component. The impedanceinverting network, as faced by the screen, can appear as a pure resistance.

## IMPEDANCE-INVERTING PIERCE OSCILLATOR

1-430. A $50-\mathrm{mc}$ impedance-inverting Pierce oscillator is shown in figure $1-182(\mathrm{C})$. This circuit supplied 70 mw to the 1500 -ohm load, and had a frequency deviation of $0.6 \mathrm{ppm} /$ volt. Note that the total $\mathrm{C}_{g}$ is equal to the total $\mathrm{C}_{3}$. The antiresonant $\mathrm{C}_{\mathrm{n}}$ for the inductive branch of the impedance-inverting network is thus very nearly ( $\mathrm{C}_{\mathrm{m}}+\mathrm{C}_{\mathrm{p}} / 2$ ), which in turn is equal to $\mathrm{C}_{0}$. This value of $\mathrm{C}_{\mathrm{n}}$ neglects the equilavent negative capacitance due to the reactive component of the r-f plate current. Viewed only as an impedance-converting network connected between the plate and grid, $\mathrm{C}_{\mathrm{n}}=\mathrm{C}_{\mathrm{pg}}$, and the network appears as an inductive reactance numerically equal to $2 / \omega C_{p}$ or $2 / \omega C_{g}$. The upper useful limit of this type of circuit is approximately 100 mc .
1-431. Figure 1-182 (D) shows an electron-coupled modification of the impedance-inverting Pierce


Figure 1-182. Impodance-inverting oscillator circuits. (B) Impedance-inverting transitron oscillator. (C) Impedance-inverting Pierce oscillator. (D) Impedance-inverting electron-coupled Pierce oscillator
oscillator. The frequency of the oscillator circuit is virtually independent of the tuning adjustments in the plate circuit. With the plate circuit tuned to the 1 st, 2 nd, 3 rd , and 4 th harmonics successively, the power supplied $\mathrm{R}_{\mathrm{L}}$ was found to be 400 mw at $54 \mathrm{mc}, 225 \mathrm{mw}$ at $108 \mathrm{mc}, 50 \mathrm{mw}$ at 162
mc , and 10 mw at 218 mc . The frequency stability is approximately the same as that of the triode circuit in figure 1-182(C). The upper frequency limit of the grounded-screen circuit in (D) was found to be 70 mc .

(E)

Figure 1-182. Impedanco-inventing oscillator circuits. (E) Impadance-inverting Miller oscillator

## IMPEDANCE-INVERTING MILLER OSCILLATOR

1-432. Figure 1-182(E) is an experimental design of a $50-\mathrm{mc}$, impedance-inverting, Miller oscillator. The oscillator is designed so that the $\mathrm{C}_{\mathrm{n}}$ of the equivalent negative resistance circuit is equal to $\mathrm{C}_{0}$. Assuming that the reactive component of the plate current is negligible, $\mathrm{C}_{\mathrm{n}}=\mathrm{C}_{\mathrm{s}}=\mathrm{C}_{\mathrm{g}}+\mathrm{C}_{1}$, where $\mathrm{C}_{2}$ is the equivalent capacitance of $\mathrm{C}_{\mathrm{pz}}$ in series with the parallel combination of $\mathrm{C}_{\mathrm{p}}$ and $\mathrm{L}_{\mathrm{p}}$. $\mathrm{C}_{1}$ is thus given by the equation

$$
\begin{equation*}
C_{1}=\frac{C_{p q}\left(1-\omega^{2} L_{p} C_{p}\right)}{1-\omega^{2} L_{p}\left(C_{p}+C_{p g}\right)} \tag{1}
\end{equation*}
$$

$\mathrm{C}_{p s}$ and $\mathrm{C}_{\mathrm{p}}$ are fixed by the tube capacitances, and $C_{1}$ is equal to $C_{0}-C_{g}$, so the solution of equation (1) requires a definite value of $\mathrm{L}_{\mathrm{p}}$, which in circuit (D) was found to be $0.744 \mu$ h. The circuit supplies $\mathrm{R}_{\mathrm{L}}$ with a power output of 0.5 watt for a crystal drive of 0.07 watt. The frequency deviation was found to be $0.6 \mathrm{ppm} / \mathrm{volt}$.

## Grounded-Cathode Two-Stage Feed-Back Oscilletor

1-433. The two-stage feed-back oscillator (see figure 1-183) is used primarily for high-resistance, series-mode crystals operating at fundamental frequencies not higher than 500 kc and usually below 300 kc . The design is rather straightforward. $V_{1}$ and $V_{2}$ are tubes of the same type and can be contained in the same envelope. Although pentodes should permit slightly greater frequency stability, triodes are quite satisfactory for most purposes. Since $V_{2}$ alone can provide the necessary phase reversal, both tubes can operate into resistive loads. The V, plate circuit is thus tuned to the crystal resonance frequency. The proper adjustment of $C_{p}$ is indicated by a maximum read-
ing on the meter, M. $\mathrm{R}_{2}$ is connected across the $\mathrm{L}_{\mathrm{p}}-\mathrm{C}_{\mathrm{p}}$ tank, to broaden the tuning and reduce the frequency effects of variations in the V, plate capacitance. The resistance, $R_{c}$, of the crystal circuit is approximately $R+2 R_{1}$. On the assumption that $R=R_{m}$ (the maximum permissible crystal resistance), $R_{1}$ should be made as amall as possible consistent with stable oscillations. This is desirable in order for the effective $Q$ of the crystal circuit, and hence the frequency stability, to be maximum.
1-434. The loop-gain requirement for equilibrium is

$$
\begin{equation*}
G_{1} G_{2} G_{3}=\frac{E_{p 1}}{E_{\mathrm{E} 1}} \cdot \frac{E_{p 2}}{E_{p 1}} \cdot \frac{E_{g 1}}{E_{p 2}}=1 \quad 1-434 \tag{1}
\end{equation*}
$$

where

$$
\begin{align*}
& G_{1}=\frac{E_{p 1}}{E_{\mathrm{t} 1}}=g_{m 1} R_{2}  \tag{2}\\
& G_{2}=\frac{E_{p 2}}{E_{p 1}}=\frac{g_{m 2} R_{1}\left(R+R_{1}\right)}{R+2 R_{1}} \tag{3}
\end{align*}
$$

and

$$
G_{3}=\frac{E_{k 1}}{E_{p 2}}=\frac{R_{1}}{R+R_{1}}
$$

Equations (2), (3), and (4) assume that $V_{1}$ and $\mathrm{V}_{\mathbf{2}}$ operate into plate impedances approximately equal to $R_{z}$ and $\frac{R_{1}\left(R+R_{1}\right)}{R+2 R_{1}}$, respectively, and that these impedances are very small compared with the $R_{p}$ of the tubes. Combining equations (2), (3), and (4), we find that at equilibrium, the tube transconductances are such that

$$
G_{1} G_{2} G_{3}=\frac{g_{m 1} g_{m 2} R_{1}^{2} R_{2}}{R+2 R_{1}}
$$

Section 1


Figure 1-183. Grounded-cathode two-stage feed-back oscillator

Assuming that $g_{m i} g_{m z}=g_{m}{ }^{*}$, where $g_{m}$ is the nominal class-A transconductance of the $V_{1}$ and $V_{2}$ type of tube, and that $R=R_{m}$, we can select values of $R_{1}$ and $R_{2}$ so that equation (5) will equal 1.5. This provides a 3 -to- 2 margin of gain, which should be sufficient to ensure operation with all but completely defective tubes. The cathode resistors can be selected so that the amplitude of oscillations does not overdrive a crystal of maximum R. An alternative, and possibly a simpler approach, is first to select a cathode resistor for $V_{1}$, with the intention of operating that tube at a fixed class-A bias. The gain of the $V_{1}$ stage can then be treated as a predetermined constant and the $V_{2}$ stage designed to provide the necessary limiting by gridleak bias. The class-A gain of the $V_{2}$ stage must be sufficient to permit oscillations when the crystal unit has a maximum resistance, and the excitation current must not be sufficient to overdrive the crystal unit when the crystal resistance is a minimum. If desired, a parallel-mode crystal unit connected in series with its rated load capacitance can be substituted for a series mode crystal unit. Such operation increases the average effective feedback resistance, but the presence of the capacitor can reduce the tendency of the circuit to oscillate at unwanted frequencies.

## MODIFIED TWO-STAGE FEED-BACK OSCILLATOR

1-435. A modification of the two-stage, feed-back oscillator to reduce the higher harmonics and thereby improve the quality of the sine-wave out-
put for sync control is shown in figure 1-184. It can be seen that the tuned tank, undamped, is connected in the plate circuit of $V_{z}$ instead of that of $V_{1}$ as is conventionally done. The output, $E_{0}$, is taken from a different part of the tank in each of the three circuits represented. The non-bypassed cathode resistors are inserted for their degenerative effect on the higher harmonics and parasitic frequencies. They also reduce the effective input capacitance of the tubes. It would seem that the degradation of the crystal $Q$ is somewhat large. The Miller effect in $V_{1}$ is probably significant in determining the impedance that the crystal faces -certainly so in circuit (C), where $R_{s}$ is one megohm and $C_{b}$ is inserted to increase the plate-to-grid capacitance by $25 \mu \mathrm{f}$. However, the chief purpose of $\mathrm{C}_{9}$ is to serve as a neutralizing capacitance for all free-running oscillations where the crystal unit would behave as a capacitance, $\mathrm{C}_{0}$.

## Colpltts Oscillaters Modlified for Crystal Control

1-436. Figure 1-185 illustrates a number of spe-cial-purpose circuits which are basically Colpitts oscillators modified for crystal control. Circuits (A), (B), and (C) are conventional CI-meter oscillators (see paragraph 1-220). The tank inductance, equal to $2 L_{1}$, is split into two equal inductances, $L_{1 A}$ and $L_{1 B}$. Each of the variable inductors in circuit (A) actually represent seven fixed inductors which can be connected into the circuit by a range switch. The capacitors $C_{1}$ (A and $B$ ) are continuously variable, and are so ganged that $C_{14}$ is always equal to $C_{18}$. Circuits

| Fig. | Equipment | Purpose | $F_{1}$ | CR | $\mathbf{R}_{1}$ | $\mathbf{R}_{\mathbf{2}}$ | $\mathbf{R}_{3}$ | $\mathrm{R}_{4}$ | Rs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Range Calibrators TS-102/AP and TS-102A/AP | Crystal control al 500 -yd marker and sync pulses | 327.8 | Sig C Stock No. $2 \times 62$ 327.8; WECo No. D-168342 | 1.8 | 10 | 18 | 1000 | 1.8 |
| (B) | $\begin{aligned} & \text { Calibrator } \\ & \text { TS-19/APQ-5 } \end{aligned}$ | Crystal con. trol of $1000-\mathrm{ft}$ marker and syne pulses | 491.04 | WECO No. D-164868 | 1.8 | 10 | 18 | 1000 | 1.8 |
| (C) | Range Calibrator TS-293/CPA-5 | Ose for radar iFF. <br> P/O Radar Sets AN/CPX- 1 and AN/CPX-2 | 186.3 | Belmont <br> Drawing No. A-8K-3577 | 1.8 | 10 | 1000 | 1000 | 1.8 |

Circuit Data for Figure 1-184. F in ke. R in kilohms. $C$ in $\mu \mu$. L in $\mu$ h.


Figure 1-184. Modificotions of two-stage feed-back osellitor to improve sine-wave output

| Fis. | Equipment | Purpose | F | CR | $\mathbf{R}_{1}$ | $\mathrm{R}_{2}$ | Ra | R4 | Rs | R. | $R_{7}$ | $\mathbf{R}_{1}$ | Re | R10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | Crystal <br> Impedance Meter TS-390/ <br> TSM | Substi- <br> tution circuit for meas. uring parameters of crystal unit | 1-15 |  | $\begin{aligned} & 2.2 \\ & \text { each } \end{aligned}$ | 22 | 1 | 0.27 | 25 |  |  |  |  |  |

Circuit Dats for Figure 1-185. Fin me, R in kilohms. C in $\mu \boldsymbol{f}$ except where otherwise noted. $L$ in $\mu \mathrm{h}$.

| R. | $\mathbf{R}_{7}$ | $C_{1}$ | C2 | C. | $\mathrm{C}_{4}$ | C5 | $\mathrm{C}_{6}$ | $C_{7}$ | $\mathrm{C}_{8}$ | C. | $L_{1}$ | $\mathrm{V}_{1} \quad \mathrm{~V}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.2 | 2.2 | 3800 | 100,000 | $\mathbf{3 9 0 0}$ | 890 | 10,000 | 75 | 20 | $\infty$ | 0 | 500 | 6SN7GT |
| 2.2 | 2.2 | 8800 | 100,000 | 3900 | 200 | 10,000 | 75 | 10 | 3900 | 0 | 880 | 6SN7GT |
| 1 | $\infty$ | 6000 | 50,000 | 350 | 75 | 0 | 0 | 25 | $\infty$ | 25 | Sig C <br> Stock No. <br> 2C-638- $\mathrm{C} \mathbf{C l}$ | 6SN7GT |


(A)

Figure 1-185. Colpiths circults modifiod for serios-mode crystal control

| $\mathrm{C}_{1}$ | $\mathrm{C}_{2}$ | Cz | C4 | Cs | $\mathrm{C}_{4}$ | C7 | C | Ce | $\mathbf{L}_{1}$ | $\mathrm{L}_{n}$ | 4 | $L_{4}$ | $\mathbf{V}_{1}$ | $\mathrm{V}_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 7.8- \\ & 140 \\ & \text { ench } \end{aligned}$ | 51 | 1.5 | 250,000 | 260,000 | 10,000 | 80 | 5-42 | 250,000 | 2.6 386 each |  |  |  | 6V6GT |  |

Section

(8)(c)


Figure 1-185. Continued
(D)

| Fig. | Equipment | Purpose | $\mathrm{F}_{1}$ | CR | $\mathrm{R}_{1}$ | R2 | $\mathbf{R}_{1}$ | R. | R | R, | R, | Rs | R ${ }_{8}$ | $\mathbf{R}_{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (B) | Crystal <br> Impedance <br> Meter TS- <br> $683 / T S M$ | Substitution circuit for measuring parameters of crystal unit | 10-60 | Mili- <br> tary <br> Stendard quartz crystal units | $\begin{aligned} & 0.1 \\ & \text { each } \end{aligned}$ | 15 | 1 | 15 | 25 | 4.7 |  |  |  |  |
| (C) | Crystal Impedance Meter TS683/TSM | Substi- <br> tution circuit for measuring parameters of crystal unit | 55-140 | Mili- <br> tary <br> Standard quartz crystal units | $\begin{gathered} 0.0 \\ 56 \\ \text { each } \end{gathered}$ | 15 | 1 | 15 | 25 | 2.2 |  |  |  |  |
| (D) | Test Set TS-250/ APN | Range osc. Output consists of positive range pips | $\begin{aligned} & 0.13 \\ & \text { and } \\ & 1.3 \end{aligned}$ | Bliley No. 1225006 (octal base) | 100 | 1.2 | 4.7 |  |  |  |  |  |  |  |
| (E) | Diversity Receiving Equipment AN/FRR-3 | BFO <br> with <br> afc; <br> manual <br> or <br> crystal <br> opera- <br> tion | 0.46245 |  | 100 | 5 | 1 | 10 | 20 | 2 | 0.5 | 0.085 | 500 | 1.5 |

Circuit Data for Figure 1-185. Fin kc. R in kilohms. C in $\mu \mu \mathrm{f}$ excent where otherwise noted. L in $\mu \mathrm{h}$.


Figure 1-185. Continued
(E)

| $C_{1}$ | $\mathrm{C}_{2}$ | Cs | C. | C. | C. | C, | C. | c. | $L_{1}$ | Ls, | $L_{2}$ | $L_{4}$ | $\mathrm{V}_{1}$ | V: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 93 \\ \text { each } \end{gathered}$ | 22 | 1 | 5 | 470 | 470 |  |  |  | $\begin{gathered} 0-8 \\ 7.85 \\ \text { ench } \end{gathered}$ |  |  |  | 5854 |  |
| $\stackrel{5}{\text { each }}$ | 12 | 0 | 1 | 470 | 470 |  |  |  | $0.0$ |  |  |  | 5654 |  |
| 330 | 430 | 5600 | 55 | 58 | $8 \mu \mathrm{t}$ | $8{ }_{\mu}$ |  |  | $\begin{gathered} 7500 \\ \max \end{gathered}$ | 60 | 37 | 25,000 | 6AG7 | 6AG7 |
| 2000 | 10,000 | 39 | 500 | 400 | 50 | 2000 | 2000 |  |  |  |  |  | 6V6GT | 6SN7GT |

(B) and (C) are substantially of the same basic design as circuit (A). Except for resistors $R_{4}$ and capacitances $C_{3}$ and $C_{4}$, the parameters of circuits (B) and (C) have the same numbers as their functional analogues in circuit (A). Circuits (B) and (C) are not designed for parallel-resonance measurements. For crystal resistance measurements, the calibrating resistor must be substituted externally for the crystal unit. The capacitors $C_{1}$ are fixed and the inductors $L_{1}$ are continuously variable and are so ganged as always to be equal. In each of the CI-meter circuits shown, it can be seen that if the resistance of the tank, including the crystal, were zero, and if the tank were perfectly balanced, no voltage would exist between the crystal and ground. The voltage across $L_{1 A}$ plus that across $\mathrm{C}_{14}$ would equal zero, and no current would flow through the resistors $R_{1}$, which effectively form a bridge between the inductance arm to the grounded connection of the capacitance arm. In practice, a net voltage does exist across $L_{1 A}$ and $C_{1 A}$ in series, and this voltage appears across $R_{1 A}$, being measurable at the jacks J1 and $J 2$ in circuit (A). The r-f voltage across $R_{1 B}$ is approximately that across $J 3$ and $J 4$, which in turn is equal to the $R_{1 A}$ voltage plus that across the crystal resistance. The $R_{1}$ resistors are not essential insofar as maintaining oscillations is concerned, but they load the circuit, thereby reducing the effect of the variations in crystal resistance upon the oscillator activity, and they serve to protect the crystal, to balance the circuit to ground, and to facilitate measurements of the crystal voltage ( $E_{\mathrm{me}_{\mathrm{e}}}=\mathrm{E}_{\mathrm{J} 3}-\mathrm{E}_{\mathrm{J} 1}$ ) without unduly interfering with the effective circuit parameters. The CI-meter oscillator can be analyzed as a particular type of transformer-coupled oscillator, as an impedanceinverting oscillator, or as an equivalent Pierce oscillator having a crystal $X_{e}=\omega\left(L_{1 s}+L_{1 B}\right)$ and an effective crystal resistance accounting for the losses in the resistances $R_{1}$ as well as in the $R_{e}$ of the actual crystal.
1-437. Figures 1-185 (D) and (E) are examples of grounded-plate Colpitts circuits which have been modified for series-mode crystal control. Circuit (D) is designed to provide positive range pips to the grid of $V_{2}$. The circuit operates class $C$ at either one of two frequencies, the appropriate crystal being connected between the cathode tank and the grid of $V_{1}$. Circuit ( E ) is designed for either manual or crystal control. During manual control the resistor $R_{7}$ replaces the crystal unit. $V_{1}$ is operated as a reactance tube. The a-f-c bias varies in such a way that the b-f-o frequency tends to follow any changes in the frequency of
the teletype signal being received.

## CRYSTAL CALIBRATION

1-438. The design of a crystal oscillator to be used for calibrating the frequency of other oscillators generally is directed toward obtaining outputs rich in harmonics. Where tuned-plate circuits are required the $L / C$ ratios should be high, so that high impedances are also presented to the overtone frequencies. The oscillator should be operated class C, and often the gridleak resistance is a megohm, or higher. If the crystal calibrator is to serve as a frequency standard of greater-than-average precision, this precision becomes the principal design problem insofar as the oscillator is concerned; if need be, the required harmonics can be developed in nonlinear amplifier stages that follow the oscillator stage. The higher the overtone, the weaker will be its effective output power, but with proper design useful outputs up to and above the 100 th harmonic can be obtained. With the addition of frequency multiplier and/or divider circuits a single crystal can provide a useful calibrator frequency range as broad as desired. For maximum precision, a $G$ element, usually cut for 100 kc , should be used.
1-439. Figure 1-186 illustrates a simply designed crystal calibrator employing an electron-coupled Miller oscillator operating into a resistive plate load. Such a circuit will ensure sufficient frequency stability for most purposes. Harmonic outputs in steps of 100 kc are provided up to frequencies of $10,000 \mathrm{kc}$. For higher frequencies, the 1000 -kc crystal can be used to provide calibration points in multiples of 1000 kc . The variable grid capacitor is employed to ensure that the crystal operates into the correct load capacitance.

## Crystal Calibrator Employing Regenerative Frequency Divider

1-440. Figure 1-187 shows the regenerative fre-quency-divider circuit of the crystal frequency indicator (CFI) used in Radio Transmitting Set AN/ART-13A. This circuit employs a 200 -ke crystal to control a rich mixture of harmonics, providing useful check points spaced as close as 25 kc apart. The crystal oscillator, utilizing the triode section, $V_{l}$, seems best described as a modification of an impedance-inverting Pierce circuit. When oscillations first start, the output of the oscillator is fed to grid No. 1 of the pentagrid mixer, $V_{3}$. The 50 -ke and $150-\mathrm{kc}$ components of the noise voltages that are mixed with the $200-\mathrm{kc}$ signal are amplified by $V_{3}$ and fed to the input of the $V_{2}$ triode section. The $V_{2}$ plate circuit, which is tuned
-


Figure 1-186. Typical design of single-fube general-purpose crystal calibrator circuit


Figure 1-187. CFI regenerative frequency divider in Radio Transmitter T-47A/ART-13 (P/O Radlo Transminting Set AN/ART-13A)

Section 1
to 150 kc , amplifies the $150-\mathrm{kc}$ noise input and triples the $50-\mathrm{ke}$ input. The $150-\mathrm{kc}$ output of $\mathrm{V}_{2}$ is then fed back to the pentagrid mixer at grid No. 3 . It is again amplified and fed back to $V_{2}$. However, the direct amplification and regeneration of the 150 -ke signal alone is not sufficient nor properly phased to maintain oscillations at this frequency. The $150-\mathrm{ke}$ oscillations are sustained principally by tripling the $50-\mathrm{kc}$ feedback, which builds up as the amplified difference frequency of the 200 -kc and 150 -kc inputs to $V_{3}$. The output of $V_{3}$ is effectively a $50-\mathrm{kc}$ fundamental frequency standard of large harmonic content that is fed to the grid of triode section $V_{4}$, where it is mixed with signals from the variable oscillators of the transmitter. The output of $V_{4}$ is fed to the input of an audio amplifier, which amplifies the beat note whenever the variable oscillator approaches the frequency of one of the CFI harmonics. In practice, the recommended check-point harmonics are spaced 25 kc apart in the $200-600$-ke frequency range, 100 kc apart from 2000 to $3000 \mathrm{kc}, 150 \mathrm{kc}$ $(3000-4000 \mathrm{kc}), 200 \mathrm{kc}(4000-6000 \mathrm{kc}), 300 \mathrm{kc}$ ( $6000-9000 \mathrm{kc}$ ), $450 \mathrm{ke}(9000-12,000 \mathrm{kc}$ ), and $600 \mathrm{kc}(12,000$ to $18,100 \mathrm{kc}$ ). The presence of the harmonics of an apparent $25-\mathrm{kc}$ fundamental, which is used in the low-frequency calibrations, is not readily explained on the basis of the foregoing discussion of the circuit. A complete analysis of the nonlinear characteristics of the circuit is not available, but it appears possible that if a 25 -kc signal appears at the plate of $V_{3}$, it can conceivably be sustained by being fed to $V_{y}$, mixed with $f_{\text {: }}$ to form a sum frequency of 175 kc , fed back to $V_{a}$ and mixed with the $200-\mathrm{ke}$ injector signal to regenerate a difference frequency of 25 kc . It should be understood that $f_{2}=3 f_{3}=\frac{3}{4} f_{1}$ is a necessary relation, and that $f_{3}$ and $f_{3}$ are synchronized and controlled by the crystal oscillator. The phase and frequencies of the regenerative circuits automatically follow the phase and frequency of the $V_{1}$ output. For a more analytical study of regenerative frequency dividers, see discussions by R. L. Miller, R. L. Fortescue, and W. A. Edson.

## SYNTHESIZING CIRCUITS

1-441. Of great promise, particularly for use in airborne radio equipment in the v-h-f range where crystal control is necessary to maintain the required frequency stability, has been the development of synthesizing circuits, in which a very few crystals are able to control a large number of channels. In the discussions to follow we shall use the term frequency synthesis very loosely to apply
to any type of frequency-control circuit or system in which a few fixed-frequency oscillators are used to control or to stabilize a large number of radio frequencies. If the term were used rigorously, it would apply only to those cases where an output frequency is produced entirely from heterodyned combinations of internally generated frequencies. Examples of this type are provided by the Plessey frequency generator and by the Collins transmitter frequency-control system employed in Radio Set AN/ARC-27. For our purposes we shall extend the term to cover such systems as the Bendix frequency-control circuit in Radio Set AN/ARC-33, where the output frequency is not actually synthesized but is obtained from a vari-able-tuned master oscillator that is crystal-stabilized at many frequencies. Also implied by the term will be such systems as the Collins crystalcontrolled multichannel receiver circuits. In these latter circuits only one end-product frequency is desired - a fixed superheterodyne intermediate frequency. But the system design is such that with the use of a very few crystals the desired intermediate frequency can be synthesized under crystal control from received signals on any one of hundreds of possible radio channels. $\dagger$

## The Plessey Symthesixing System*

1-442. The first crystal-controlled frequency synthesizer in commercial usage appears to have been

[^4][^5]that developed by the Plessey Company, Ltd. of England. This synthesizer has been designed as a frequency generator to be used in making precise radio-frequency measurements. The synthesizing system employed is nevertheless quite applicable for other uses, such as providing multichannel excitation voltages for radio communication equipment. As designed by the Plessey engineers, the synthesizer generates a sequence of harmonic signals of much greater precision and purity than is obtainable with conventional types of frequency generators. The original model permits a directreading dial selection of any of the first 10,000 harmonics of 1 kilocycle per second; a later and larger model extends the range to the first 100,000 harmonics, i.e., any harmonic of 1 kc up to 100 mc. All these frequencies are made available singly as pure sine waves (unmixed with other harmonics or frequency products) by a decade system of frequency dividers and multipliers, mixing stages, and filters where all the generated frequencies are under the control of a single $1000-\mathrm{kc}$ precision crystal standard. Theoretically the system could be extended to cover a broader or a different frequency range; or could be changed to permit steps between adjacent frequencies that are smaller or larger than 1 kc . If required, it would be quite practicable for the Plessey generator, itself, to be expanded to cover also the 100 to $01000-\mathrm{mc}$ range in $10-\mathrm{mc}$ steps. In 1955 the Schomandt Company of Munich, Germany placed on the market a similar type of synthesizer frequency generator covering the $0-30-\mathrm{mc}$ range in 1 -ke steps. The output of the Schomandt synthesizer is equivalent to that of the Plessey synthesizer in quality, having at least a $60-\mathrm{db}$ attenuation of all unwanted frequencies. It was the demand for such narrowly spaced pure output frequencies for use in making frequency measurements that originally led to the development of the synthesizer circuits.

## SYNTHESIZER ADVANTAGES IN RADIOFREQUENCY MEASUREMENTS

1-443. Prior to the development of the frequency synthesizer there were two conventional methods for measuring radio frequencies--the "interpolation" method and the "successive heterodyning" method.* Briefly, the interpolation method, which is satisfactory where extreme accuracy is not required, consists of mixing the unknown frequency with the two nearest harmonics of a frequency standard, and zero-beating the difference frequencies obtained against the output of a linearly tuned variable oscillator. It is then possible to interpolate the unknown frequency by determin-
ing its relative position between the known harmonics of the standard. In the successive heterodyning method, the unknown frequency is mixed with a known harmonic of a frequency standard; the difference frequency is then heterodyned with a second standard harmonic to obtain a second and lower difference frequency; and the process is repeated, if necessary, until a difference frequency is obtained that lies within an accurately measureable audio range. Although the successive heterodyning method can be quite accurate, occasions arise where the operator cannot be certain without undue checking that the difference frequencies being measured are not the products of unwanted harmonics contained in the heterodyned signals. The use of a frequency synthesizer that permits individual pure sine-wave outputs of a sequence of narrowly spaced frequencies, instead of a simultaneous mixture of many harmonics, can be said to offer a third and greatly superior means of measuring radio frequencies.
1-444. With the use of decade dial control, greater operating simplicity is possible than with the interpolation method; and when the pure sine-wave frequencies are spaced only 1 kc apart, the interpolation accuracy of the successive heterodyning method is maintained, but with the elimination of those chance difference products that can result from harmonic mixtures of multiple stages of heterodyning.

## FUNCTIONAL OPERATION OF PLESSEY SYNTHESIZER

1-445. The circuit system by which the Plessey synthesizer produces thousands of frequencies, all controlled by a single 1000 -ke crystal standard, is illustrated in figure 1-188. The block diagram shown is that of the original, single-cabinet model that permits the operator a choice of any one of the first 10,000 harmonics of 1 kc . It can be seen that there are three successive stages in which the input frequency is divided by 10 , so that the last divider represents an over-all division of the original standard ( 1000 kc ) by 1000 . The dividers and the 1000 -kc harmonic generator are of the synchronized, free-running, multivibrator type whose outputs are rich in harmonics. Each of these multivibrator circuits forms the first stage of a sequence which can be tuned to pass any one of the first 10 harmonics of its respective multivibrator fundamental. These sequences are labeled $\mathrm{A}, \mathrm{B}, \mathrm{C}$, and D in figure 1-188. In the synthesis of a frequency, we can say generally that sequence $\mathbf{A}$

[^6]

Figure 1-188. Block diagrams of a Plessey synthesizer designed to cover the 0-10-me spectrum in 1-kc steps
supplies that part of the final frequency which is a multiple of $1000 \mathrm{kc}, \mathrm{B}$ that part which is a multiple of $100 \mathrm{kc}, \mathrm{C}$ that part which is a multiple of 10 kc , and $D$ that part which is a multiple of 1 kc . 1-446. For example, assume that an output frequency of 6789 ke is desired. The A, B, C, and D harmonic selectors, respectively, will be decadeset to pass the 6th, 7th, 8th, and 9th harmonics of their respective input signals from the preceding multivibrator stages. In balanced modulator C, the output of selector $\mathrm{D}, 9 \mathrm{kc}$, is mixed with the $80-\mathrm{kc}$ output of selector C . (The signals are heterodyned in a balanced modulator circuit rather than in a more efficient type of mixer in order to eliminate the two input frequencies from the modulator output. In this manner the sum and difference products become the dominant frequencies in the modulator output.) Filter C is dial-set to pass the desired frequency product, 89 kc , which it feeds to balanced modulator B. In modulator B , the $89-\mathrm{kc}$ signal is heterodyned with the 700-kc output of the decade-set harmonic selector B. Filter B is dial-set to pass the sum product, 789 kc, from the B modulator output to the A modulator input, where it is mixed with the $6000-\mathrm{kc}$ output of harmonic selector A. Filter A is dial-set to pass the sum product, 6789 kc , of the mixed signals, which product is then amplified and fed
through a phase inverter to the synthesizer output jack.
1-447. The foregoing example of the operation of the Plessey synthesizer suggests that the sum rather than the difference products of the mixed signals are always selected. In practice this is not the case, even though the decade dialing system is so designed that the operator is always provided a direct reading of the output frequency as if he were only adding the decade units together. In order to sufficiently filter out the unwanted product, it is important that the signals to be mixed are so selected that there is at least a 10 per cent difference in frequency between the sum and difference products. Since the filters must be capable of suppressing all adjacent harmonics of the mixed signals, it can be assumed that they are also capable of suppressing the unwanted heterodyne product if it differs from the desired product by as much as the fundamental harmonic of the mpdulator input from the harmonic selector. For example, in modulator C , the space between the sum ( $f_{c}+f_{b}$ ) and the difference $\left(f_{c}-f_{b}\right)$ frequencies should not be less than 10 kc , the fundamental of the harmonic from selector $C$. Since

$$
\left(f_{c}+f_{1}\right)-\left(f_{c}-f_{b}\right)=2 f_{1,}>10 \mathrm{kc}
$$

then $f_{i}$, must never be less than 5 kc if it is to be
mixed with $f_{c}$. Similarly, $f_{c D}$ must not be less than 50 kc if it is to be mixed with $f_{B}$, and $f_{\text {BCl }}$ must not be less than 500 kc if it is to be mixed with $f_{A}$. $1-448$. To illustrate, let us suppose that a frequency of 91 kc is desired. It would not do for $\mathrm{f}_{\mathrm{c}}$ and $f_{\mathrm{v}}$ to be 90 kc and 1 kc , respectively, for then the sum product, 91 kc , would be separated from the difference product, 89 kc , by only 2 kc . Rather, 100 kc should be selected as $\mathrm{f}_{\mathrm{c}}$ and 9 kc as $\mathrm{f}_{\mathrm{b}}$. The variable filter $C$ would be set to pass the difference product, 91 kc ; which product differs from the sum product, 109 kc , by 18 kc , well beyond the minimum permissible limit of 10 kc .
1-449. As a more involved example we shall determine the heterodyne frequencies that would be used in the synthesis of an 8136 -ke output. For a mental calculation of the correct frequency combinations the easiest method is to start with the output frequency, $f_{\text {abcn }}$, and from this determine $f_{A}, f_{\text {RCD }}, f_{B}, f_{C D}, f_{C}$, and $f_{1}$, in that order, working from the larger units to the smaller. Each of the above six frequencies is determined by remembering that none of the input frequencies to the $A, B$, and $C$ modulators can be less than 500,50 , and 5 kc , respectively. Thus, we see at once that 8136 kc is not to be the sum product of 8000 kc and 136 kc in the A modulator, since 136 kc is less than 500 ke. So $f_{A}$ must be 9000 ke and $f_{\text {nci }}$ must be 1000 minus 136 kc , that is, 864 kc ; which means that filter A will be adjusted to pass the difference product ( 9000 kc minus 864 kc ). Since 64 ke is greater than 50 kc , the required $864-\mathrm{kc}$ output of modulator $B$ can be obtained as the sum product of 800 kc and $64 \mathrm{kc}, \mathrm{f}_{\mathrm{B}}$ and $\mathrm{f}_{\mathrm{cn}}$, respectively. Since 4 kc is less than 5 kc , the required $64-\mathrm{kc}$ output of modulator C must be obtained as the difference product of 70 kc and $6 \mathrm{kc}, \mathrm{f}_{\mathrm{C}}$ and $\mathrm{f}_{\mathrm{D}}$, respectively. We see that in order to select an output of 8136 kc , the decade dials of the $\mathrm{A}, \mathrm{B}, \mathrm{C}$, and D harmonic selectors must be set to pass, respectively, the 9 th, 8th, 7th, and 6th harmonics. In other words, the output frequency would be a synthetic product of the four frequencies, $9000 \mathrm{kc}, 800 \mathrm{kc}$, 70 kc , and 6 kc . So also would be an output frequency of 9876 kc . Since the decade dials that control the harmonic selectors may be set at the same positions for two or more frequencies, some arrangement must be made so that the decade reading presented to the operator identifies correctly the particular frequency being synthesized. This convenience is accomplished in the Plessey synthesizer by manualiy operated range adjustments that alter the correspondence of the dial readings with the dial positions. Thus, in the example above, with the proper range settings, decade dial

A in position 9 would give a reading of 8 , decade dial $B$ in position 8 would give a reading of 1 , decade dial C in position 7 would give a reading of 3 , and decade dial $D$ in position 6 would give a reading of 6 . The mechanics of exactly how this feature is incorporated in the Plessey synthesizer, although relatively simple in principle, is somewhat beyond the subject matter of our assignment here.

## CIRCUIT DESIGN OF PLESSEY SYNTHESIZER

1-450. The general circuit design employed in a Plessey synthesizer is shown in the schematic diagram of figure 1-190. The circuit shown, when synchronized by a 1000 -ke standard (whose circuit is not shown), is capable of covering the 0 -$10-\mathrm{mc}$ range in 1 -ke steps. Note that each of the four decade harmonic sequences begins with a multivibrator-type of harmonic generator. Rheostats are furnished for adjusting the natural oscillation period of each multivibrator, in order to allow for aging effects and the like. More elaborate or reliable harmonic-generator circuits are not required since the failure of any of the multivibrators would be immediately apparent by the reading in the output meter. Figure $\mathbf{1 - 1 8 9}$ shows in detail the circuit parameters of the $100-\mathrm{kc}$ multivibrator, which also acts as the 1 st divider. Note that the 1st divider is synchronized by the output of the 1000 -ke amplifier and not directly by the frequency standard. The output of the 1st divider in turn is used to synchronize the 2nd divider, and that of the $2 n d$ to synchronize the $3 r d$.
1-451. In figure 1-190 it can be seen that harmonic selection is achieved by switching to the correct tuning capacitor from a bank of 10 . The same inductance is used for each of the harmonics. Since the percentage difference between adjacent harmonics is less as the order of the harmonic becomes higher, it is more difficult to eliminate the 9 th and 11th harmonics when selecting the 10 th, than it is to eliminate the 1 st and 3 rd when selecting the 2 nd. For this reason, the value of each of the fixed tuning inductors is chosen to provide an optimum $Q$ at the 10 th harmonic. This permits a relative magnification of the 10 th harmonic over its adjacent harmonies of approximately 200 , which is equivalent to $\mathrm{a} 32-\mathrm{db}$ attenuation of the 9 th and 11 th harmonics and more than that for all others. The attenuation of adjacent harmonics becomes greater as the selected harmonic becomes lower, so that in any event it is never less than 32 db at each tuned circuit. Two tuned circuits in series provide more than a $60-\mathrm{db}$ attenuation,


Figure 1-189. Schematic diagram of a Plessoy synthesixer designed to cover the $0-10-\mathrm{mc}$ spectrum in 1-kc steps. The circuit of the crystal ascillator standard is not shown
which for all practical purposes is sufficient to consider the selected harmonic a pure sine wave. 1-452. With the use of a balanced modulator it is not necessary to use as many tuned circuits as would otherwise be necessary to eliminate all unwanted harmonics and frequency products. Note in figure 1-190 that the balanced modulator design is such that two matched amplifiers have a common output circuit, but that they are excited by equal signals 180 degrees out of phase, so that the amplified signals cancel each other in the load. Thus, even though the heterodyne efficiency of the balanced modulator is less than that of other types of mixers, the balanced circuit is greatly advantageous in helping to eliminate all the unwanted frequencies, particularly the unwanted harmonics, that originate in the circuits preceding a mixer stagi. In the Plessey synthesizer it can be seen that the modulators are provided with a switching arrangement by which one of the tubes of each moduator can be cut out of the circuit by opening its cathode return. One of these switches is opened whenevor a modulator stage must pass an unmixed signal. With one tube removed, the balanced arrangement is destroyed, and since only one input signal is being handled, the vacuum tube still
connected in the circuit will be operated as a conventional amplifier. If, for example, the desired output were a $2000-\mathrm{kc}$ signal, none of the modulators would be in operation except modulator A, which would be unbalanced and operated simply as an amplifier of the 2nd harmonic from the $1000-\mathrm{kc}$ harmonic generator.
1-453. Variable-tuned circuits are provided as bandpass filters. These must be adjusted manually in selecting the proper heterodyne product to be passed. The selectivity is sufficient to provide at least a $30-\mathrm{db}$ attenuation of any unwanted signal that differs as much as 10 per cent from the desired signal.
1-454. The phase inverters are inserted for proper impedance matching. They permit an output at any frequency within the operating range of 100 millivolts across a 75 -ohm load. The system as a whole insures at least a $60-\mathrm{db}$ attenuation of all unwanted frequencies.

## The Bendix Synthesizing System

1-455. In America, much of the pioneering in the field of frequency synthesis has been done by the research staff of the Bendix Corporation.
The following discussion is based upon the synthesizing circuit originally described by W. R. Hedeman of Bendix in the magazine Electronics. Figure 1-191 shows a block diagram of the synthesizer circuit developed at Bendix for use in controlling the frequency of a continuously variable v-h-f receiver heterodyne oscillator. In this circuit, the first crystal oscillator employs but one crystal. The harmonic generator that follows this oscillator produces a rich output of harmonics, the first of which is $f_{r}$, the fundamental of the first crystal oscillator. The harmonics selector is composed of a number of band-pass circuits, each circuit designed to pass a particular harmonic of the crystal frequency. The number of frequencies controlled by the synthesizer is directly proportional to the number of harmonic channels in the selector. Let $f_{h}$ equal the harmonic selected and $f_{n}$ equal the frequency of the variable oscillator. The value of $f_{o}$ is always higher than that of $f_{h}$. These two frequencies are mixed in the first frequency converter to form the sum-and-difference frequencies, which, in turn, are fed to the input of the first band-pass amplifier. The first band-pass amplifier amplifies and passes only the difference frequency, $f_{s}-f_{b}$. This difference frequency is fed to the second frequency converter, where it is mixed with the output, $\mathrm{f}_{x}$, of the second crystal oscillator. The second crystal oscillator is generally provided with more than one crystal unit, but only the fundamental frequency of the oscillator is used when a


WADC TK 56-156


Figure 1-190. Schematic diagram of the 100-ke synchronized multivibrator used in the Plessey.synthesizer as a


Figure 1-191. Block diagram of frequency-synthesizer circuit
particular crystal is selected. The number of controlled channels is directly proportional to the number of second-oscillator crystals. The sum and difference frequencies of the frequency converter are fed to the second band-pass amplifier, which amplifies and passes only the difference frequency, $\left(f_{o}-f_{n}\right)-f_{x}$. This difference frequency is fed to a discriminator. The number of channels controlled is directly proportional to the number of discriminators used. The d-c a-f-c output of the discriminator is used to control the bias of the control tube. The plate current of the control tube determines the rotor position of a servo motor, and the rotor is mechanically coupled to control the tuning elements of the variable oscillator. The servo motor continues to turn and thereby continues to change the frequency, $f_{0}$, until the output of the discriminator is zero. This occurs when the output of the second band-pass amplifier is equal to $f_{n}$, the frequency of the discriminator circuit. By reversing the polarity of the discriminator output leads, $f_{0}$ can be made to vary in the opposite direction in order to reach equilibrium. Thus, for each value of $f_{n}, f_{x}$, and $f_{d}$, there are two equilibrium values of $f_{\mathrm{m}}$. These are given by the equation

$$
\begin{equation*}
f_{0}=f_{n}+f_{x} \pm f_{t} \tag{1}
\end{equation*}
$$

1-456. Let
$\mathrm{N}=$ Total number of channels, $\mathrm{f}_{0}$.
$\mathrm{H}=$ Number of harmonics used (1st crystal oscillator).
$\mathrm{X}=$ Number of crystals (2nd crystal oscillator).
$\mathrm{D}=$ Number of discriminators.

It can be seen from equation 1-455 (1) that

$$
\mathrm{N}=2 \mathrm{HXD}
$$

The factor 2 is introduced by the fact that for each discriminator there are two values of $f_{0}$ for each combination of $f_{\mathrm{h}}$ and $\mathrm{f}_{\mathrm{x}}$. One value is $\mathrm{f}_{\mathrm{o}}=\mathrm{f}_{\mathrm{n}}+$ $f_{x}+f_{d}$, and the other is $f_{o}=f_{b}+f_{x}-f_{d}$.

1-457. As a concrete example, let us imagine that it is desired to cover the frequency range between 100 and 156 mc with the channels spaced 200 kc apart. The lowest value of $f_{0}$ is to be 100.2 mc , and the highest is to be 156 mc . Thus,
$N=\frac{(\max ) f_{o}-(\min ) f_{0}}{\Delta f_{0}}+1=\frac{156-100}{0.2}=280$
1-457 (1)
By equation 1-456 (1),

$$
\mathrm{HXD}=\frac{\mathrm{N}}{2}=140 .
$$

The smallest total number of elements occurs when $\mathrm{H}, \mathrm{X}$, and D can be made as nearly equal to each other as possible, but in an actual design problem, this may not be the most practical solution. In our particular example let us assume that the first seven harmonics of $f_{c}$ are to be used.
With $\mathrm{H}=7$, then by equation (2)

$$
X D=\frac{140}{7}=20
$$

The combinations (X,D) possible are $(20,1)$, $(10,2),(5,4),(4,5),(2,10)$, and $(1,20)$. For our problem we shall suppose that the combination ( $\mathrm{X}=10, \mathrm{D}=2$ ) proves the most practical. Thus, with the use of 11 crystals in all and 2 discriminators, 280 crystal-controlled channels are to be obtained.

1-458. Let $f_{1}, f_{2}, f_{3} \ldots f_{2 \times n}$ designate the values of $f_{n}$ from the lowest to the highest, in that order. Let $f_{x i}, f_{x: 2} \ldots f_{x 10}$ designate the values $f_{x}$ from the lowest to the highest, in that order. The values of $f_{b}$ in ascending order are $f_{s}, 2 f_{c} \ldots . f_{r}$. Finally, let $f_{n 1}$ and $f_{t \pm}$ designate the lower and the higher discriminator frequencies, respectively. To avoid the possibility of spurious conversion frequencies, the highest value of $f_{h}$ should be less than the minimum associated 1st band-pass amplifier frequency, $f_{n}-f_{n}$. Also, the lowest value of $f_{x}$ should be higher than the highest 2nd band-pass amplifier frequency, which, of course, will equal the highest discriminator frequency, $f_{1}$. The order of the variable-oscillator frequencies and the sequence of circuit connections required to provide each frequency is indicated by the following sequence of equations.

$$
\begin{aligned}
& \mathbf{f}_{1}=\mathbf{f}_{\mathrm{c}}+\mathrm{f}_{\mathrm{x1}}-\mathbf{f}_{\mathrm{d} 2}=\mathbf{1 0 0 . 2} \mathrm{mc} \\
& \mathbf{f}_{2}=\mathbf{f}_{4}+\mathrm{f}_{\mathrm{x} 1}-\mathbf{f}_{\mathrm{A} 1}=100.4 \mathrm{mc} \\
& f_{3}=f_{n}+f_{x_{2}}-f_{f_{2} 2}=100.6 \mathrm{mc} \\
& \mathrm{f}_{\mathrm{t}}=\mathrm{f}_{1 .}+\mathrm{f}_{\mathrm{x}: 2}-\mathrm{f}_{\mathrm{dt}}=\mathbf{1 0 0 . 8} \mathrm{mc} \\
& \text { etc } \\
& f_{20}=f_{v}+f_{x 111}-f_{\mathrm{A} 1}=104 \mathrm{mc} \\
& \mathbf{f}_{\mathrm{E} 1}=\mathbf{f}_{\mathrm{r}}+\mathbf{f}_{\mathrm{x} 1}+\mathrm{f}_{\mathrm{nt}}=104.2 \mathrm{mc} \\
& \mathrm{f}_{\mathrm{m}: \pm}=\mathrm{f}_{\mathrm{c}}+\mathrm{f}_{\mathrm{x} 1}+\mathrm{f}_{\mathrm{d} 2}=104.4 \mathrm{mc} \\
& \mathrm{f}_{!3}=\mathrm{f}_{\mathrm{c}}+\mathrm{f}_{\mathrm{x} 2}+\mathrm{f}_{\mathrm{dt}}=104.6 \mathrm{mc} \\
& f_{24}=f_{\mathrm{c}}+\mathrm{f}_{\mathrm{x} 2}+\mathrm{f}_{\mathrm{f} 2}=104.8 \mathrm{mc} \\
& \text { etc } \\
& \mathrm{f}_{41}=\mathbf{f}_{6}+\mathrm{f}_{\mathrm{x} 10}+\mathrm{f}_{\mathrm{d} 2}=108 \mathrm{mc} \\
& f_{41}=2 f_{4 .}+f_{x 1}-f_{n!2}=108.2 \mathrm{mc} \\
& f_{4:}=2 f_{t}+f_{x 1}-f_{t 1}=108.4 \mathrm{mc} \\
& f_{43}=2 f_{t}+f_{x 2}-f_{\mathrm{A} 2}=108.6 \mathrm{mc} \\
& \text { etc } \\
& f_{2 \times 11}=7 f_{c}+f_{x 10}+f_{\text {d:2 }}=156 \mathrm{mc}
\end{aligned}
$$

1-459. It can be seen from the equation sequence in paragraph $1-458$ that the difference between the channel frequencies is equal to the difference
between the discriminator frequencies. Thus,
$\Delta f_{d}=f_{d 2}-f_{\mathrm{d} 1}=\Delta \mathbf{f}_{\mathrm{n}}=\mathbf{f}_{2}-\mathbf{f}_{1}=0.2 \mathrm{mc}$
1-459
Note in the equation sequence in paragraph 1-458, that for a given harmonic frequency, $f_{b}$, all the $f_{x}$ crystals are used in sequence before the polarity of the discriminator outputs are reversed. In other words, $f_{n 1}$ and $f_{n 2}$ are first subtracted from all combinations of a particular harmonic with the $X$ crystal frequencies and then added to the same combinations. This process is repeated with each harmonic. If we subtract the equation for $f_{1}$ from the equation for $f_{3}$, we have

$$
\Delta f_{x}=f_{x 2}-f_{x 1}=f_{3}-f_{1}=0.4 m c=2 \Delta f_{t}
$$

1-459 (2)

In the general case,

$$
\Delta \mathbf{f}_{\mathrm{x}}=\mathbf{D} \Delta \mathbf{f}_{\mathrm{A}}
$$

where $D$ is the number of discriminators. The same value of $\Delta f_{x}$ also holds between any other two consecutive values of $f_{x}$. Thus,

$$
\begin{align*}
& \mathbf{f}_{x y}=f_{x 1}+\Delta f_{x} \\
& f_{x: 3}=f_{x 1}+2 \Delta f_{x} \\
& f_{x n}=f_{x 1}+(n-1) \Delta f_{x}=f_{x 1}+(n-1) D \Delta f_{d} \tag{4}
\end{align*}
$$

The highest frequency of the second crystal oscillator is given by equation (4) when $n=X=$ the total number of crystals. Thus,

$$
(\max ) f_{x}=f_{x 1}+(X-1) D \Delta f_{d}
$$

With the use of equation (5) we can find the lowest discriminator frequency, $f_{d 1}$. This is done by subtracting the equation for $f_{20}$ from the equation for $f_{31}$, which gives

$$
\begin{array}{r}
f_{21}-f_{211}=f_{x 1}-f_{x 11}+2 f_{n 11}=\Delta f_{1}=0.2 m c \\
1-459(6)
\end{array}
$$

Since $f_{x i 1}$ is a particular case of (max) $f_{x}$ we can substitute equation (5) in equation (6) to obtain a general equation. We find

$$
f_{x 1}-f_{x 1}-(X-1) D \Delta f_{4}+2 f_{d 1}=\Delta f_{n}
$$

On rearranging after canceling out $f_{x 1}$,

$$
\begin{equation*}
f_{a 1}=\Delta f_{d} \frac{(1+D X-D)}{2} \tag{7}
\end{equation*}
$$

The general equation for any particular discriminator frequency, $f_{\text {dn }}$, is similar to that for $f_{x n}$ given by equation (4). Thus,

$$
\begin{equation*}
f_{d n}=f_{d 1}+(n-1) \Delta f_{n} \tag{8}
\end{equation*}
$$

and

$$
\begin{equation*}
(\max ) f_{d}=f_{d 1}+(D-1) \Delta f_{d} \tag{9}
\end{equation*}
$$

The next problem is to obtain a general equation for $f_{c}$. This can be had by subtracting the equation for $f_{40}$ from the equation for $f_{41}$. The remainder is

$$
\Delta f_{d}=f_{c}+f_{x 1}-f_{x 10}-2 f_{d 2}
$$

where $f_{x 10}=(\max ) f_{x}$ and $f_{n \geq 2}=(\max ) f_{n t}$. Thus,

$$
f_{c}=2 f_{a 2}-f_{x 1}+f_{x 1}+(X-1) D \Delta f_{d}+\Delta f_{t}
$$

or

$$
\begin{array}{r}
f_{\mathrm{c}}=2 \mathrm{f}_{\mathrm{dz}}+2 \mathrm{f}_{\mathrm{di}} \\
f_{\mathrm{c}}=2\left[(\max ) \mathrm{f}_{\mathrm{d}}+(\min ) \mathrm{f}_{\mathrm{d}}\right] \tag{10}
\end{array}
$$

Finally, with $f_{c}$ determined, we can use the equation for $f_{1}$ to find $f_{x 1}$.
1-450. We are now in a position to express any of the circuit frequencies in terms of the parameters $f_{1}, \Delta f_{0}, N, H, X$, and $D$. For the nth channel,

$$
\begin{equation*}
f_{n}=f_{1}+(n-1) \Delta f_{v} \tag{1}
\end{equation*}
$$

For the highest channel,

$$
(\max ) f_{0}=f_{1}+(N-1) \Delta f_{0} \quad 1-460(2)
$$

For the lowest discriminator frequency,

$$
\begin{equation*}
f_{\mathrm{d} 1}=\frac{\Delta f_{\mathrm{o}}(1+\mathrm{DX}-\mathrm{D})}{2} \tag{3}
\end{equation*}
$$

For the nth discriminator frequency,

$$
\begin{equation*}
f_{d n}=\frac{\Delta f_{c}(D X-D+2 n-1)}{2} \quad 1-460 \tag{4}
\end{equation*}
$$

For the highest discriminator frequency,

$$
\begin{equation*}
(\max ) f_{d}=\frac{\Delta f_{v}(D X+D-1)}{2} \tag{5}
\end{equation*}
$$

For the fundamental of the 1st crystal oscillator,

$$
f_{c}=2 \Delta f_{c} D X=\frac{\Delta f_{c} N}{H}
$$

For the $n$th harmonic frequency,

$$
\begin{equation*}
f_{\mathrm{ma}}=2 \Delta \mathrm{f}_{\mathrm{c}} \mathrm{DXX} \tag{7}
\end{equation*}
$$

For the highest harmonic,

$$
(\max ) f_{h}=\Delta f_{v} N
$$

For the lowest frequency of the 2 nd crystal oscillator,

$$
f_{x 1}=\frac{2 f_{1}-\Delta f_{n}(3 D X-D+1)}{2}
$$

For the nth frequency of the 2nd crystal oscillator,

$$
\begin{equation*}
f_{x n}=\frac{2 f_{1}-\Delta f_{n}\left(3 D X+D+1-2 D_{n}\right)}{2} \tag{10}
\end{equation*}
$$

For the highest frequency of the $2 n d$ crystal oscillator,

$$
\begin{equation*}
(\max ) f_{x}=\frac{2 f_{1}-\Delta f_{n}(D X+D+1)}{2} \tag{11}
\end{equation*}
$$

1-460
and the difference between the consecutive values of $f_{s}$,

$$
\begin{equation*}
\Delta f_{x}=\Delta f_{u}, D \tag{12}
\end{equation*}
$$

1-461. On applying the equations in paragraph $1-460$ to the numerical example that has been assumed, where $f_{1}=100.2 \mathrm{mc}, \Delta f_{2}=0.2 \mathrm{mc}$, $\mathrm{N}=280, \mathrm{H}=7, \mathrm{X}=10$, and $\mathrm{D}=2$, we find that

$$
\begin{aligned}
\mathrm{f}_{\mathrm{x}}, \mathrm{f}_{x_{3}}, \text { etc }= & 94.3,94.7,95.1,95.5,95.9,96.3, \\
& 96.7,97.1,97.5,97.9 \mathrm{mc}
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{f}_{41}=\frac{0.2(1+20-2)}{2}=1.9 \mathrm{mc} \\
& \mathrm{f}_{\mathrm{tiz}}=1.9+0.2=2.1 \mathrm{mc} \\
& f_{c}=\frac{0.2 \times 280}{7}=8 \mathrm{mc} \\
& f_{n 1}, f_{n-3}, \text { etc. }=8,16,24,32,40,48,56 \mathrm{mc} \\
& f_{s}=\frac{200.4-0.2(60-2+1)}{2}=94.3 \mathrm{mc} \\
& \Delta \mathrm{f}_{\mathrm{s}}=0.4 \mathrm{mc}
\end{aligned}
$$

Section 1

## Crystal Oscillators

Note that the highest harmonic frequency is equal to the bandwidth of the frequency range being covered.
1-462. From the equation, $f_{0}=f_{h}+f_{x} \pm f_{d}$, it can be seen that the frequency stability will be approximately the stability of the crystal oscillators. This is because $f_{d}$ is so very much lower than $f_{b}$ and $f_{x}$. Although the discriminators should be designed with low-loss, temperature-compensating materials, even a large percentage variation in $f_{d}$ would be negligible in its percentage effect upon $f_{0}$. Since it is the sum of $f_{h}$ and $f_{x}$ that determines $f_{0}$, the maximum percentage frequency deviation of the total can be no greater than that of the crystal oscillators individually. Without oven control, the channel frequencies can be maintained within a tolerance of $\pm 0.005$ per cent, and better.

RADIO SET AN/ARC-33
1-463. Radio Set AN/ARC-33 is an airborne re-ceiver-transmitter designed to operate in the v-h-f and u-h-f spectrum. This equipment, developed by the Bendix Corporation, employs a modified version of the Bendix frequency-synthesizing system discussed in the foregoing paragraphs. The fre-quency-control section (see figure 1-192 for block diagram) is designed to permit receive-transmit communication on any one of 1750 channels spaced 100 kc apart in the 225 -to- 399.9 -me band.
1-464. An important modification in the synthesizing system arises from the fact that the synthesized frequencies are utilized as heterodyne injection signals during reception and as carrier signals during transmission. The tuning controls are such that the receiver and transmitter circuits are always automatically tuned to the same channel, but since the desired receiver injection frequency must differ from the tuned channel frequency by an amount equal to the receiver intermediate frequency, the design engineers had to decide whether to let the variable-frequency oscillator be, in effect, a subharmonic local oscillator for the receiver or a subharmonic master oscillator for the transmitter. They decided in favor of the receiver. Thus, the stabilized output frequency, $f_{0}$, of the vfo, after being multiplied 12 times, is used directly as the injection voltage in the 1st mixer stage in the receiver. This provides a fixed intermediate frequency, $f_{i}$, of 15.325 me for each of 1750 channels. Now, the v-f-o output, $f_{0}$, is also used in the synthesis of the channel frequency of the transmitter. Since the 12 th harmonic of $f_{n}$ always differs from the channel frequency by an amount equal to $f_{i}$, all that needs to be done in principle is to mix $12 f_{s}$ with a fixed oscillator fre-
quency equal to $f_{i}$ and for the sum product to be isolated and amplified for use as the transmitter carrier. In the ARC-33 transceiver this effect is achieved by mixing the output, $f_{n}$, of a crystalcontrolled oscillator (called the "sidestep" oscillator) with the 6 th harmonic of $f_{0}$, then selecting the sum frequency ( $6 f_{\sigma}$ plus $f_{n}$ ) and doubling it to form the carrier frequency, $f_{a}$, which, after amplification, is fed to the antenna. Summarizing these frequency relations in the form of equations, we have:

$$
\begin{aligned}
& \text { injection frequency }=12 f_{o} \\
& \text { intermediate frequency }=f_{1}=f_{n}-12 f_{0} \\
& \text { antenna (channel) frequency }=f_{*}=12 f_{o}+f_{1} \\
& \quad=2\left(6 f_{0}+f_{s}\right) \\
& \text { sidestep frequency }=f_{n}=f_{1} / 2
\end{aligned}
$$

Note the necessary harmonic relation between the sidestep output and the intermediate frequency. It is also important to note that the principle involved in the use of a sidestep oscillator permits, not only a Bendix synthesizing system, but any synthesizing system to be readily modified for the dual-purpose requirements of transceiver frequency control.
1-465. Comparison of figures 1-191 and 1-192 will reveal that the 2nd crystal oscillator in the basic Bendix synthesizer has been replaced by two crystal oscillators (the 2nd and 3rd in figure 1-192) in Radio Set AN/ARC-33. This has been done to permit a greater number of frequencies with a fewer number of crystals.
1-466. Another significant modification occurs in the ARC-33 discriminator circuit. As is explained in more detail in a subsequent paragraph, the ARC-33 discriminator is not a conventional type that employs a parallel tuned circuit to control the phase differences between the input voltage components. In that type of discriminator the output voltage always has a net d-c component unless the input frequency is equal to the antiresonant frequency of the tuned tank. The polarity of the d-c

- component is an index of whether the input frequency is higher or lower than that at which the tank is tuned, and the amplitude of the d-c component can be a measure of the amount of difference between the two frequencies. It is this type of discriminator that is assumed in the discussion of the basic Bendix synthesizing system, the d-c output of which is used to control the variable oscillator tuning. In the ARC-33, however, the discriminator does not employ a tuned circuit, but instead is fed a signal that is controlled by the 4th crystal oscillator. The discriminator also receives


Figure 1-192. Block diagram of Irequency control section of Radio Sel AN/ARC-33 showing modified version of Bendix synthesixing sysfem
an input signal from the 4 th mixer. The two signals combine in the discriminator circuit to provide a net d-c output only when the two signals are of the same frequency. When the frequencies are identical, the behavior of the discriminator is quite similar to the behavior of one that employs a tuned circuit, the d-c output depending upon the differences in phase between the input voltages. Since the 4th oscillator can be controlled by either one of two crystals, this arrangement is equivalent to having two discriminators of the tunedcircuit type.
1-467. In paragraph 1-456 it is explained that for each discriminator, two values of $f_{0}$ are possible. In Radio Set AN/ARC-33 only one of these values is used for each 4th-oscillator frequency, namely

$$
f_{0}=f_{b}+f_{x}+f_{d} \quad 1-467
$$

In the equation above, $f_{b}$ is the selected effective harmonic of the 1st crystal oscillator, equal to $f_{n 1}$ on the low band and to ( $f_{n 1}+f_{h_{2}}$ ) on the high band, $f_{x}$ equals the sum of the frequencies of the 2nd and 3rd crystal oscillators ( $f_{x 2}+f_{x 3}$ ), and $f_{a}$
is the frequency of the 4 th crystal oscillator fed to the discriminator.
1-468. Other modifications of the Bendix system as occur in the frequency-control circuits of Radio Set AN/ARC-33 are of an even less radical nature than those described above. There is the division of the 1st bandpass stage into low-band and highband circuits, and there is the addition of an a-f-c reactance tube, which is actually more of an extension of the modification caused by the use of a crystal-controlled discriminator, but these and other special circuit arrangements are best explained in the more detailed analyses later. At this point it will be helpful to examine briefly the role each of the various oscillator frequencies plays in controlling the final antenna frequency,
1-469. First, we shall examine the simplified block diagram shown in figure 1-193. The frequencycontrol system indicated represents an imaginary synthesizing circuit that provides the same transmitter output frequencies, $f_{n}$, as does Radio Set AN/ARC-33. The principal difference between the


Figure 1-193. Simplifled block diagram of the frequency-control section of Radio Set AN/ARC-33 as if would appear if the variable frequency oscillator were the direct generator of the transmitter output frequency with. out the use of multiplier or side-step circuits
imaginary and the actual systems is that the imaginary system is not required to provide an injection voltage for a receiver heterodyne circuit, nor is it required to employ multiplier stages following the variable oscillator. In other words, $f_{n}$ can be assumed to equal $f_{a}$. Under these conditions the various crystal and harmonic frequencies would assume the simple values shown in figure 1-193. The actual circuit frequencies are those indicated in the frequency diagram of figure 1-194. A comparison of the frequencies in the two systems will show that the injected frequencies in each mixer stage of the imaginary system vary from one to the next in steps that are 12 times greater than are the corresponding steps in the actual system. This does not mean, except in the case of the 1st crystal oscillator and its harmonics, that the imaginary crystal frequencies are 12 times the actual crystal frequencies; it is only the differences between adjacent frequencies that are related in the proportion of 12 to 1 . Since the frequency of the variable frequency oscillator in the actual circuit is eventually multiplied 12 times, it can be seen that the frequency steps in the actual circuit are equivalent to those in the imaginary circuit insofar as they add or subtract in the control of the antenna frequency. Thus, we can say that the antenna frequency is effectively synthesized in 10 -me units by the 1st crystal oscillator and harmonic generator, 2 -me units by the 2nd crystal oscillator, 0.2 me units by the 3 rd crystal oscillator, and finally to the nearest $0.1-\mathrm{mc}$ unit by the discriminator and 4 th crystal oscillator.

## Detailed Circuit Description

1-470. The principal component of Radio Set AN/ ARC-33 is Receiver-Transmitter RT-173/ARC-33. The receiver-transmitter is divided into a number of sectional components, two of which are of importance to us:
a. The monitor chassis, which contains all the crystal circuits for controling the variablefrequency oscillator.
b. The r-f head, which contains the variablefrequency oscillator, the multiplier circuits, the 1st i-f mixer, the sidestep oscillator, as well as the r-f amplifiers of the receiver and the power amplifiers of the transmitter. Also of importance to us are the relays which control the tuning motor. These are mounted on the main frame. We shall discuss the monitor circuits first, and then those in the r-f head. Except for occasional insertions and editing, the descriptions to follow are largely extracts from USAF Technical Order No. 12R2-2ARC33-2.

## Monitor Chassis

1-471. The monitor chassis in Radio Set AN/ ARC-33 concerns only the frequency control of the variable-frequency oscillator and electronic control of the tuning-capacitor drive motor with its clutches. There are no other circuits involved.

The detailed circuit descriptions of the monitor chassis are made with reference to the component symbols employed in the block diagram of figure 1-195 and the schematic diagram of figure
1-196. With the exception of a coaxial connector for the r-f input from the variable-frequency oscillator, all external connections to the unit are made through a single connector, which is so arranged that connection automatically is made when the chassis is inserted in its proper place in the main frame.
1-472. FIRST CRYSTAL OSCILLATOR. The 1st crystal oscillator is a single-frequency, funda-mental-mode, 833.333 -kc oscillator of the cathodecoupled Butler type. A selected harmonic of the oscillator is mixed with the frequency of the variable frequency oscillator in the 1 st mixer. A dual triode tube, V401, is employed as the oscillator tube, which has two output connections. Section A is tuned to the 5th harmonic of the crystal and feeds the grid of frequency multiplier V403B. The plate output of the grounded-grid oscillator section B is coupled through capacitor C407 to the harmonic generator grid. The crystal unit, which is of the type CR-28/U, is mounted in a type HD-54/U crystal oven. The oven employs two heaters and thermostats, one heater being used to bring the temperature quickly up to the operating level, whereas the other, which has a lower wattage, is used to maintain constant operating temperature. In order to check the oscillator for proper operation, a test connection for measuring rectified grid current is brought out to test socket X412. The stability of the final transmitter frequency is more dependent upon the stability of this oscillator than upon that of any of the others. The reason is that the 1st crystal oscillator controls a greater percentage of the final frequency, especially in the high band, than do the other oscillators. This can readily be seen if we visualize the final frequency as being synthesized by adding together the crystal-oscillator frequencies in the simplified block diagram of figure 1-193. The key function of this oscillator is the reason why the highly stable Butler circuit is employed. 1-473. HARMONIC GENERATOR. The function of harmonic generator V403A is to produce any selected harmonic of the first crystal oscillator


Figure 1-194. Frequency diagram of frequency-control sysfem in Radio Set AN/ARC-33


Figure 1-195. Monitor chassis. Block diagram of a-f-c sysfem in Radio Set AN/ARC-33
output from the 4 th to the 13 th, inclusive. The selected harmonic is fed to the 1st mixer to be heterodyned with the frequency from the variable frequency oscillator. Harmonic selection is achieved by capacitance tuning the primary and secondary of the harmonic generator output transformer T401 to the desired harmonic frequency. The switching is accomplished by 10 position rotary switches $S 403 A$ and $S 403 B$, which are driven by the selector motor through a harmonic generator clutch. These switches merely select the proper fixed capacitors for tuning the primary and secondary winding to the desired harmonic of the 833.333 -ke fundamental. 1-474. R-f input from the 1 st crystal oscillator is fed to the harmonic generator tube, V403A, through coupling capacitor C 407 . A grid bias far below cutoff is provided by grid resistor R407 in order to ensure an output rich in harmonics. The primary and secondary windings of transformer

T401 are permeability tuned for alignment at the lowest (4th) harmonic. The highest frequency, which is the 13th harmonic, is determined by capacitors C418 and C419 across the primary and C420 and C421 across the secondary. Capacitors C418 and C421 are trimmers for alignment at the highest frequency. The selection of all harmonics, up to but not including the 13th, is accomplished by switching in the proper fixed capacitor C408 through C417 across the primary of transformer T401, and Ce22 through C431 across the secondary. For the lowest harmonic, C416 and C417 for the primary and C430 and C431 for the secondary are connected in parallel. For the highest harmonic, no auxiliary capacitor is switched into the circuit. For proper operation of the monitor, it is necessary that the input level of the 1 st mixer be approximately the same for each selected harmonic. This is accomplished by selecting a grid bias for the harmonic generator
which causes the output level to vary inversely with frequency under a constant plate load impedance. Then, by maintaining the " $Q$ " of the transformer T 401 windings constant at all selected frequencies, the resultant plate load impedance of tube V403 can be made to vary directly with frequency because of the increasing inductance/capacitance ratio. The resultant voltage across the T401 transformer windings, therefore, is essentially constant regardless of the harmonic selected.
1-475. FIRST MIXER. The 1st mixer tube, V402, combines the output of the harmonic generator with the output frequency of the variable frequency oscillator (vfo) whose frequency is to be controlled by the monitor circuits. The 1st mixer output consists of the difference frequency between the selected harmonic generator frequency and the v -f-o frequency, the latter frequency always being the higher. Input from the harmonic generator is fed directly to the control grid, whereas the input from the vfo, which enters the monitor chassis through connector J401, is fed from isolation amplifier V402A to the cathode of the 1st mixer through coupling capacitor C432. Output coupling is provided by bandpass coil assembly Z401, which consists of a low-band circuit and a high-band circuit. The bandpass selector relay selects the proper circuit of bandpass coil assembly Z401. The reason for using two bandpass circuits is that the broad frequency range of the radio set makes it necessary to divide the range into two smaller ranges. The banddetermining factor is the selection of the 1st digit of the desired channel frequency at the control panel. The control panel switch energizes the band selector relay when the 1 st digit is 2 ; that is, when the antenna frequency is to be less than 300 mc . For antenna frequencies of 300 mc and above, the band relay is unenergized. Coil assembly Z401 is designed to pass a band from approximately 12.1 to 12.9 mc and a band from approximately 20.4 to 21.2 mc . Because of the use of two bandpasses at the 1st mixer output, each of the harmonic generator selected output frequencies is used twice, once in each band.
1-476. BANDPASS AMPLIFIER. The bandpass amplifier, V404, is an amplifier for the 1st mixer output on the low-frequency band and is used to improve the bandpass characteristics of the circuit. This stage is unconventional inasmuch as it also functions as a 2nd mixer, the operation of which is described in the following paragraph. The plate load consists of transformer T402, which is tuned to the same frequency band as the
low band of Z401. The bandpass amplifier is capacitance-coupled through capacitor C443 to the number one grid of the 3rd mixer, V405.
1-477. SECOND MIXER. The 2nd mixer stage utilizes the same tube elements of V404 as are used when the tube is operated as a bandpass amplifier. However, this dual usage does not occur simultaneously. Tube V404 functions as a 2nd mixer only when the radio set operates in the high band of the frequency range. The 2nd mixer combines the 1st mixer output frequency with the 10th harmonic of the 1st crystal oscillator frequency. The output consists of the difference frequency, where the 10th harmonic frequency is always lower than the output frequency of the 1st mixer. Note that the reduction of the 1st mixer output frequency by an amount equal to the 10 th harmonic of the 1st crystal oscillator frequency is equivalent to extending the harmonic generator range from the 13 th to the 23 rd harmonic and eliminating the high band of bandpass coil assembly Z401. Input to the 2nd mixer from the high-band bandpass filter is fed to the control grid along with the input from frequency multiplier V403B. The plate load consists of transformer T402, which is tuned to pass a band from 12.1 to 12.9 mc . The desired band width for the transformer is obtained through the use of loading resistors R418 and R419. Transformer T402 is the same plate load circuit for the 2nd mixer as is used when the stage operates as a bandpass amplifier.
1-478. FREQUENCY MULTIPLIER. The frequency multiplier, $V 403 \mathrm{~B}$, is fed with the 5th harmonic output from the 1st crystal oscillator. The output transformer, T406, is tuned to 8.33333 me, which is the 2nd harmonic of the multiplier input frequency. Thus, V403B is a frequency doubler and feeds its output, the 10th harmonic of the 1st crystal oscillator frequency, to the control grid of the 2nd mixer, V404. When the radio set is operated in the low band of its frequency range, no output is derived from the frequency multiplier because plate voltage is removed from tube V403B. The application of plate voltage is controlled by the band selector relay. When the band selector relay switches the high bandpass filter into the 1st mixer circuit, it also applies voltage to the plate of the frequency multiplier so that an $8.33333-\mathrm{mc}$ signal is fed to the 2nd mixer. The frequency multiplier is capacitively coupled to the controi grid of the 2nd mixer through capacitor C457.
1-479. SECOND CRYSTAL OSCILLATOR. The end crystal oscillator provides a selection of any




Figure 1-196. Monitor chassis. Schematic diagram of a-f-c sysfem in Radio Set AN/ARC-33
one of five crystal-controlled frequencies by means of crystal switching. The crystal-controlled output frequency is' fed to the suppressor grid of the 3 rd mixer to be mixed with either the $2 n d$ mixer or the bandpass amplifier output frequency. The oscillator circuit utilizes one half of the duplex triode tube V406 as a grounded-plate Pierce oscillator. R-f output is taken from the cathode. Each of the five crystal units, which are of the CR-27/U type, has a separate trimmer so that each selected 2nd crystal oscillator frequency can be adjusted exactly. All of the crystal units with their trimmers are enclosed in a single oven (Bendix Radio type L205628) which is kept at approximately $75^{\circ} \mathrm{C}\left(167^{\circ} \mathrm{F}\right)$ by a thermostatcontrolled heater. A booster heater and thermostat are provided in addition for quick warmup. In order that the oscillator operation may be checked, a test connection from the grid circuit is brought out for checking rectified grid current at test socket X412.
1-480. THIRD MIXER. The circuit of the 3rd mixer, V405, is similar to that of the 2nd mixer except that the signal voltage from its heterodyne crystal oscillator is injected at the suppressor grid. The 3 rd mixer output circuit is tuned to a center frequency of 8.9 mc and is designed to pass a band approximately from 8.8 to 9.0 mc . The 3 rd mixer combines the output frequencies of either the 2nd mixer or bandpass amplifier and the 2nd crystal oscillator, the output frequency of the former two always being the higher. The 3rd mixer output, which is the difference frequency, is fed from the secondary of transformer T403 to the 4 th mixer through capacitor C449.
1-481. THIRD CRYSTAL OSCILLATOR. The 3 rd crystal oscillator, the V406B circuit, is of the same design as the 2nd crystal oscillator except for the operating frequencies. The crystal units, which are of the CR-27/U type, are divided into two groups of five each. All are used throughout the total frequency range of the radio set. The 3rd crystal oscillator employs the second half of the same tube that is used for the 2nd crystal oscillator. The 10 crystal units with their trimmers are housed in a 13-position oven (Bendix Radio type N205651), of which one position is not used. The other two positions are used to mount the two crystals of the 4th crystal oscillator. The oven is thermostatically controlled at $75^{\circ} \mathrm{C}\left(167^{\circ} \mathrm{F}\right)$. A separate booster heater and thermostat are provided for quick warmup.
1-482. FOURTH MIXER. The 4th mixer, V407, is identical to the 3 rd mixer and operates in the same manner. The 4 th mixer output circuit is
designed to pass a band of approximately 5.1 to 5.2 mc . In the 4 th mixer are combined the output frequency of the 3 rd mixer and that of the 3 rd crystal oscillator, the former frequency always being the higher. The difference frequency is selected by the tuned plate transformer and is inductively coupled into the discriminator circuit.
1-483. DISCRIMINATOR. The purpose of the discriminator, V409, is to indicate a deviation in phase or frequency between its two inputs. One of these inputs is obtained from the 4th crystal oscillator and is used as the reference signal. The other discriminator input is derived from the 4th mixer output, and it is the deviation in phase of this signal from that of the reference signal that is to be indicated by means of the output voltage across R430 and R431. The magnitude of this discriminator voltage indicates the extent of the deviation, whereas the polarity indicates the direction of the deviation. The circuit design is similar to the type employed for frequencymodulation ( FM ) receivers, except that in this case the reference voltage is obtained from a separate reference oscillator instead of a parallel resonant tank circuit. The voltages applied to the discriminator are shown in figure 1-197. $E_{1}$ is the input from the 4 th mixer and $\mathrm{E}_{\mathrm{H}}$ is the reference voltage from the 4th oscillator. To simplify the discriminator explanation, $\mathrm{E}_{\mathrm{k}}$, insofar as it adds vectorially with $E_{1}$ to form the r-f voltages across the two diodes, is best interpreted in terms of two equal and separate voltages 180 degrees out of phase. One is $E_{2}$, the r-f voltage at pin 2 with respect to point $B$; the other is $E_{71}$, the r-f voltage at pin 7 with respect to point $B$. Assuming that the bypass capacitors C452 and C453 offer zero impedances to the r-f signals, pins 1 and 5 and point $A$ are all at r-f ground potential. Thus, the $r$-f voltage ( $\mathrm{E}_{-}$) of plate pin 2 with respect to cathode pin 5 is the same as the voltage of pin 2 with respect to point $A$. Similarly, $E_{7}$, the r-f plate voltage of the second diode, is equal to the voltage of pin 7 with respect to point A. Now, $\mathrm{E}_{2}$ and $\mathrm{E}_{7}$ have one voltage component in common, which is $E_{1}$, the voltage of point $B$ with respect to point $A$. Thus, $E_{y}$ and $E_{7}$ are equal to the resultants, respectively, obtained by adding vectorially to the common voltage $E_{3}$ the voltages $E_{28}$ and $\mathrm{E}_{718}$. If we assume that C452 charges to the peak of $E_{y}$ and that $C 453$ charges to the peak of $E_{7}$, the d-c polarities will be as indicated in figure 1-197 (D), where point $A$ is shown as negative with respect to the two cathodes. The d-c output equals ( $\mathrm{E}_{\mathbf{z}}-\mathrm{E}_{7}$ ), where both voltage symbols represent the positive peak magnitudes only. The
output is positive or negative according to whether $\mathrm{E}_{2}$ is greater or less than $\mathrm{E}_{7}$, respectively; and this is dependent, respectively, upon whether $E_{1}$ lags or leads the zero-output position, which is the 90 -degree phase displacement from $\mathrm{E}_{\mathrm{R}}$ that is shown in figure 1-197 (A). Upon examination of the discriminator diagram it can be seen that the application of either of the input voltages alone does not develop a discriminator output, since in each case $E_{2}$ and $E_{7}$ will equal each other, and hence equal currents will flow in opposite directions through the two halves of discriminator load R430 and R431. Also, it can be seen from the vector diagram (A) that, if the two discriminator input voltages are exactly 90 degrees out of phase, the resultant voltages applied to the diode plates are equal, thus producing

(A)

zero discriminator output. If, however, the variable frequency oscillator should vary in phase, the resultant voltages applied to the discriminator plates are unequal, as shown in vector diagrams (B) and (C). This results in a discriminator output voltage whose value and polarity depend upon the magnitude and direction, respectively, of the phase deviation. If there is a frequency deviation, the phase of the 4 th mixer output, $E_{1}$, rotates completely around the 4th crystal oscillator output, $E_{R}$, with a consequent a-c voltage appearing in the discriminator output. The frequency of this ac is equal to the difference between the two discriminator input frequencies.

1-484. Discriminator output is applied to the tuning-motor-control amplifier and to the reac-

(0)

## $E_{I}$. INPUT FROM 4TH MXER

$E_{R}$ = REFERENCE VOLTAGE FROM FOURTH CRYSTAL OSCLLLATOR $- \pm\left(E_{2 B}+E_{7 B}\right) \pm\left(E_{2 B}-E_{7 B}\right)$
$E_{2}$ * RESURTANT VOLTAGE APPLIED TO DIODE PLATE (SOCKET PIN 2)
$E_{7}=$ RESULTANT VOLTAGE APPLIEO TO DIODE PLATE (SOCKET PIN 7)

* TN ACTUAL PRACTICE THE VMFMO FREOUENCY CONTROL CIRCUITS ARE SUCH THAT "ON FREQUENCY"
OISCRIMINATOR OUTPUT IS APPROX ts VOLTS
THUS, IN NORMAL OPERATION, VECTOR EI WILL BE TILTED SLIGHTLY TO THE RIGHT OF ITS $90^{\circ}$ POSITION SHOWN IN FIGURE (A) AT LEFT.
OUE TO THE ACTION OF THE DIODES AND THEIR LOADS, THE DISCROMNATOR RESULTANT D-C OUTPUT IS EOUAL TO THE DIFFERENCE IN MAGMITUOE EETWEEN E 2 AND $\mathrm{E}_{7}$ (MAX Enf-|MAX E7|).

Figure 1-197. Discriminator aperation as a function of the phose difference between the input valtages

Section 1
tance tube shunted across the variable frequency oscillator. When the variable frequency oscillator approaches the desired operating frequency, a point is reached when the discriminator output frequency becomes equal to or less than the maximum frequency at which the reactance tube can respond. At this point the reactance tube immediately locks the variable frequency oscillator exactly to its correct frequency. When this occurs, the discriminator output is dc and is proportional to the phase difference between its two input voltages, which difference is, in turn, proportional to the amount of "pull" exerted by the reactance tube. This d-c control voltage is fed to the motorcontrol amplifier, V411, and causes the tuning motor to drive the variable frequency oscillator tuning capacitor to that point which eliminates excessive pull by the reactance tube. The circuit design is such that the equilibrium point corresponds to a discriminator output of approximately 5 volts positive. Normally it would be assumed that the "on-frequency" point would be reached when the discriminator output dropped to zero, which would occur when the two input signals were exactly 90 degrees out of phase. The zerovoltage state is not used, however, in order to avoid ambiguity in identifying the on-frequency condition and to simplify the control circuit by having an equilibrium control voltage of definite magnitude. For example, zero output not only occurs at each of the two (plus and minus) $90-$ degree phase conditions, but also occurs when the variable frequency uscillator is so far off frequency that there is no input from the 4 th mixer, or if one or both of the input voltages fails, or when the two input frequencies are different and the discriminator records the best frequency. Thus, a plus 5 -volt reference is used, and the control circuits are so biased that this control level establishes the on-frequency condition. The ac which the discriminator develops before the reactance tube "pull-in" point is reached, is prevented from affecting the motor-control amplifier by the low-pass resistance-capacitance filter, R451 and C445A.
1-485. By employing a phase-sensitive discriminator, it is possible to feed a correction voltage to the control circuits before an actual frequency deviation occurs, since a frequency deviation, unless it is an instantaneous, discontinuous jump, is first indicated as a phase deviation. Therefore, no frequency error occurs except that which may be due to the reference crystals themselves. All small and rapid frequency shifts of the variable frequency oscillator are corrected by the reactance
tube Larger and slower drifts are corrected by the motor-control amplifier and the tuning motor. An extremely large and sudden frequency jump of the variable frequency oscillator which takes it out of the range of the reactance tube causes the entire tuning sequence to recycle. However, this does not occur during normal operation. To aid in discriminator alignment and test, two test points are brought out to pins of test socket X412. One of these, pin 9 , makes it possible to measure the total discriminator output. The other, pin 11, is connected to the load center-tap for checking the discriminator operation.
1-486. FOURTH CRYSTAL OSCILLATOR. The 4th crystal oscillator is used to control the operating frequency of the discriminator and thereby has final control of the exact frequency of the variable frequency oscillator. The 4th crystal oscillator can be switched to either one of two type CR-27/U crystal units, whose frequencies are spaced 8.333 kc apart. This spacing is equal to one-twelfth of the channel spacing of 100 kc . Thus, it is the spacing of the 4th crystal oscillator frequencies that determines the channel spacing. For maximum stability the crystal units are mounted in the same crystal oven that houses the crystals of the 3 rd crystal oscillator. Crystal selection is controlled by a selector switch on the main control panel. The selection is determined by the choice of the 4 th digit of the channel frequency.

1-487. The 4 th crystal oscillator circuit employs one half of a duplex triode tube, V410, which is connected as a radio-frequency grounded-plate Pierce oscillator, with the circuit designed in a manner similar to those of the 2nd and 3rd crystal oscillators. The output is taken from the cathode and coupled through C471 to the grid of the other half of tube V410, which is operated as a cathode follower. The output of the cathode follower is inductively coupled into the discriminator circuit through transformer T405. The purpose of the cathode follower is to isolate the loading effects of the discriminator from the 4 th crystal oscillator. As a check on the 4 th crystal oscillator operation, a test connection for rectified grid current measurement is brought out to test socket X412, pin 7.
1-488. CLUTCH CONTROL TUBE. The purpose of the clutch control tube V408, is to shift the r-f head tuning drive from the medium-speed clutch to the low-speed clutch for fine tuning of the exact channel frequency. Whenever the frequency of the variable frequency oscillator, after

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being fed through the four mixers, comes within range of the discriminator input tuning at transformer T404, the tuning should be shifted into low speed. Thus, by coupling part of the discriminator input through capacitor C464 to clutchcontrol rectifier V408A and amplifying the rectifier output through V408B, a control voltage is obtained which is used ; to operate the clutchcontrol relay. The clutch-control relay is mounted on the main frame and has its coil connected in series with the plate of clutch-control amplifier V408B. The relay is energized when the tube grid receives no excitation. When a signal is fed to the discriminator from the 4 th mixer, a portion of the signal is fed through capacitor C464 and rectified in diode-connected tube V408A. The resulting current flow in resistor R443 causes the ungrounded end to become more negative. This negative voltage is fed to the grid of the clutchcontrol amplifier through low-pass filter R445 and C463, cutting the tube off. This in turn de-energizes the clutch-control relay and places the low-speed clutch in operation. It should be noted here that the over-all tuning range of the radio set is divided into two nearly equal bands and that while the variable frequency oscillator tuning is being driven through the unused band a spurious frequency may pass through to the discriminator and the clutch-control tube. In this case, however, even though the clutch-control relay is de-energized, the tuning remains in high speed because of a lockup circuit.
1-489. MOTOR-CONTROL AMPLIFIER. The motor-control amplifier, V411, is a d-c amplifier whose purpose is the control of a reversible tuning motor in accordance with a d-c control voltage from the discriminator. The discriminator output voltage is fed to the grid through the low-pass resistance-capacitance filter R 451 and C445A so that the ac, which appears in the discriminator output as the channel frequency is being tuned, does not influence the operation of the amplifier. As its plate load, the motor-control amplifier works into two relay coils in series. These are called the high and low discriminator relays. The two relays are mounted on the main frame. The high discriminator relay is designed to "pull in"
at approximately 9 ma and to "drop out" at approximately 6 ma . The low discriminator relay is designed to pull in at approximately 5 ma and to drop out at approximately 3 ma . The plate current of the motor-control amplifier is so adjusted that, with a plus 5 -volt "on-frequency" output from the discriminator, approximately 5.5 ma plate current flows. This is sufficient to energize the low discriminator relay but not the high one. The contacts of the low discriminator relay are so connected that when the relay is energized the tuning motor (mounted in the r-f head) is de-energized. If the frequency of the variable frequency oscillator should tend to drift too low, the discriminator voltage controlling the amplifier becomes more positive, increasing the amplifier plate current and thereby energizing both relays. This has the effect of causing the tuning motor to turn in a direction that diminishes the tuning capacitance and hence raises the frequency. If the variable frequency should tend to drift too high, the plate current of the motor-control amplifier decreases to a value below 3 ma and both relays are deenergized. This has the effect of causing the tuning motor to turn in the opposite direction, so that the frequency of the variable frequency oscillator is decreased. Note that in order to keep the motor-control amplifier bias constant, regardless of plate current flow, a positive 6 -volt cathode bias is obtained from the d-c drop across the heater, rather than from the drop across a cathode biasing resistor.
R-F Head
1-490. The $r$-f head contains all the main channel transmitter and receiver r-f circuits including the reactance tube, the tuning capacitor drive mechanism, and certain tuning control circuits. A block diagram is shown in figure 1-198 and a schematic diagram is shown in figure 1-199. Beginning with the variable frequency oscillator, we shall discuss first the transmitter circuits and then the receiver circuits.
1-491. VARIABLE FREQUENCY OSCILLATOR $A N D$ TRIPLER. The variable frequency oscillator employs an electron-coupled Hartley circuit. The v-f-o frequency is given by the formula:

$$
v-\mathrm{f}-\mathrm{o} \text { frequency }=\frac{\text { transmitter output freq }- \text { receiver } 1 \text { st intermediate freq }}{12}
$$

The screen grid of the v-f-o tube, V802, is the anode of the oscillatory circuit. The plate circuit is tuned to three times the grid frequency, thereby tripling in this tube. Coupling capacitor C907 from grid inductor 1801 feeds a small amount of
$r$-f energy to the frequency-control circuits in the monitor. A reactance tube is shunted across the oscillator tank for fine frequency control. Oscilla-tor-tripler output is capacitively coupled to the untuned grid of the doubler tube, V803.


Figure 1-198. R-f head. Block diagram of main channel transmitter and receiver r-f circuits in Radio Set AN/ARC-33

1-492. REACTANCE TUBE. The reactance tube, V801, is a device that represents a variable and controllable reactance shunted across the tuned grid circuit of the variable frequency oscillator. Its purpose is to convert d-c control voltage from the monitor into a small frequency variation of the variable frequency oscillator. Radio-frequency voltages from the oscillator are coupled through capacitor C805 to the plate of the reactance tube and directly to a network made up of capacitors C804 and C818, resistors R801 and R804, and the grid-cathode capacitance of the tube, $\mathrm{C}_{\mathrm{k}}$. Capacitor C804 is a blocking capacitor, so that as far as the a-c functioning of the tube is concerned, it need not be considered. Cathode bypass capacitor C803 is sufficiently large for the cathode to be considered at $r$-f ground potential. Resistor R802, inductor L829, and capacitors C801 and C802 provide a de-coupling network and filter through which the d-c control voltage is applied to the control grid without shunting its r-f input impedance. Resistor R807 is the plate feed component. Resistors R801 and R804 and capacitor C818 in conjunction with the grid-cathode capaci-
tance, $\mathrm{C}_{8}$, form a phase-shifting network such that the r-f voltage applied to the grid lags the oscillator voltage input to the network by 90 degrees approximately. Since the plate current of reactance tube V801 is in phase with the grid voltage, the plate current flow lags the oscillator r-f voltage applied to the plate by approximately 90 degrees. This appears to the variable frequency oscillator as an inductive reactance since the current in an inductor lags the applied voltage by 90 degrees. By controlling the d-c bias applied to the grid, it is possible to control the amplitude of the current, and thus the magnitude of the effective inductive reactance shunting the oscillator tank. In this way, the frequency of the variable frequency oscillator can be controlled within a narrow range by means of a d-c control voltage. A positive control voltage increases the reactive current in the tube and thereby decreases the effective inductive reactance across the oscillator tank. The effect, therefore, is to cause an increase in the frequency. A negative-going control voltage has the opposite effect. The reactance tube is biased by cathode resistor R805 by an amount
that permits normal "on-frequency" oscillator operation when the control voltage from the monitor is approximately plus 5 volts.
1-493. FIRST DOUBLER. The first doubler of the r-f head is a conventional grid-leak-biased frequency multiplier. The stage employs tube V803 with an output circuit tuned to twice the input frequency. The plate circuit consists of two inductors in parallel in order to increase their sizes and make it possible to employ coiled inductors rather than a more space-consuming linear line. The tuning is ganged with the other r-f tuned circuits as shown in the schematic diagram. Radio-frequency energy used for heterodyne oscillator injection into the main channel receiver 1st mixer is taken off at a tap of plate tank L802. 'ihe variable frequency oscillator-tripler, the reactance tube, and the doubler are continuously supplied with plate and screen voltages since these circuits are employed in both transmit and receive operation. From the latter stage to the antenna, however, plate and screen voltages are removed from the transmitter tubes during receive operation.
1-494. TRANSMITTER MIXER. It is in the mixer that a $7.6625-\mathrm{me}$ signal from the sidestep oscillator is added to the first doubler output to make the mixer output frequency exactly one half of the transmitting antenna frequency. (Remember that 7.6625 mc is one half of the 1st receiver intermediate frequency of 15.325 mc .) A conventional mixer circuit employing tube V805 is used here, with the side-step oscillator voltage being injected at the control grid through capacitor C821 and with the doubler output being fed to the control grid through capacitor C820. The mixer piate circuit is tuned to the sum frequency by means of a doubler-inductor arrangement. One of the inductors is wound with concentric cable, which allows the tuning capacitor rotor and the cold ends of the inductors to be returned to ground. The center conductor is connected to the plate on the hot end and is bypassed to ground on the cold end by capacitor C825. Plate voltage is supplied to tube V805 through resistor R819. 1-495. SIDESTEP CRYSTAL OSCILLATOR. The sidestep crystal oscillator employs pentode V804, connected as a triode and operating on a single frequency of 7.6625 mc . The circuit is arranged as a Pierce oscillator with the crystal connected directly from the plate to the grid of the oscillator tube. A type CR-18/U crystal unit is employed. Since this oscillator controls only a small percentage of the final transmitter frequency, its normal operating stability is sufficient
without the use of thermostatically controlled temperature for the crystal unit. Note that an 18 -puf capacitor is shunted directly across the crystal unit and that no externally connected plate-to-ground capacitor is used. The $18 \mu \mu \mathrm{frep-}$ resents 60 per cent of the required load capacitance for the type CR-18/U crystal unit. With the grid-to-ground capacitance probably 8 or 10 $\mu \mu \mathrm{f}$ greater than the $68 \mu \mu \mathrm{f}$ of the externally connected grid-ground capacitor C822, it appears that the circuit has been designed to provide a maximum output voltage consistent with the drive-level and load-capacitance requirements of the crystal unit, rather than for maximum frequency stability. The oscillator is fed plate voltage through the voltage-dropping resistor R815. The oscillator output is capacitively coupled from the plate of the oscillator tube to the control grid of mixer tube V805 through C821. Plate voltage is derived from the plus 200 -volt transmitter supply, so that the tube operates only when the radio set is turned to the transmit position.
1-496. AMPLIFIER. This is a conventional grid-leak-biased r-f amplifier employing pentode V806. The circuit acts as a direct amplifier with the output circuit tuned to the same frequency as the input circuit. The input is capacitance-coupled to the preceding mixer stage through capacitor C828 and the output is capacitance-coupled to doubler V807 through capacitor C832. The amplifier tuned output circuit is a double-inductor tank of the same type that is used in the plate circuit of the transmitter mixer.
1-497. TRANSMITTER DOUBLER. The doubler, V807, is a grid-leak-biased stage that employs a cavity-tuned plate circuit tuned to twice the input frequency. A pencil triode tube is used because its small size permits superior u-h-f operating characteristics.
1-498. INTERMEDIATE POWER AMPLIFIER. The intermediate power amplifier (IPA) employs a lighthouse tube, V808, in a grounded-grid circuit with cavity tuning of the plate. The cavity is tuned to the doubler output frequency, providing an IPA output frequency equal to the transmitter antenna frequency. Radio-frequency input is coupled magnetically from the output of the preceding doubler tube, V807, through coupling loop L809, which applies rf between ground and the IPA cathode through capacitor C838. Concentric inductor L810 is inserted in the heater circuit to make it at the same r-f potential as the cathode. Capacitor C838 also blocks the 12.6 -volt d-c filament potential from shorting to ground through the ground coupling loop L809. One heater con-

$H$


Figure 1-199. R-f head. Schemc transmitter and receiver r-f circl


Figure 1-199. R-f head. Schematic diagram of main channel transmitfer and receiver r-f circuits in Radio Set AN/ARC-33

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nection and the cathode connection are common. The heater circuit is wired in series with the heater of the final amplifier so as to provide the required 12.6 -volt total drop across the entire circuit after passing through dropping resistor R833. A voltage divider composed of resistors R830 and R832 is connected between one side of the filament and ground. The grid return is connected to the tap to provide the proper negative bias voltage. These resistors are high in value so that they do not influence the heater voltage and current. IPA output is coupled to the final power amplifier input through an inductive coupling loop, L812, in the cavity. Since the final power amplifier is a grounded-grid r-f amplifier, it cannot be plate modulated 100 per cent unless the output of the exciting stage also is modulated. Therefore, to be able to modulate fully the final amplifier output, the plates of doubler V807 and IPA V808 are modulated by the same audio voltage as the power amplifier.
1-499. FINAL POWER AMPLIFIER. The final $r$-f power amplifier, V809, is similar in design and operation to the intermediate power amplifier. Grid bias for the final amplifier is derived from resistor R835. Resistor R834 supplies a cathode bias. Radio-frequency output to the antenna is coupled inductively to the cavity magnetic field by pickup loop L815 and is fed to the antenna receive-transmit changeover relay through a coaxial cable. The coaxial connector is mounted directly on the cavity assembly, O802. To provide a sidetone voltage that is indicative of the transmission quality, the sidetone voltage is obtained from the final r-f output cavity through inductive coupling L814. This r-f voitage is rectified through the sidetone crystal rectifier, CR801, and applied to the i-f and audio chassis to be fed through the receiver audio system to the operator's headset.
1-500. MAIN CHANNEL RECEIVER R-F CIRCUITS. The main channel receiver includes two $r$-f amplifier stages, a mixer, a frequency doubler, and a $15.325-\mathrm{mc}$ i-f amplifier. Both r-f amplifiers and the doubler are cavity-tuned. The doubler is included to multiply the output frequency of the first r-f-head doubler. By employing a heterodyne injection frequency controlled by the same variable frequency oscillator that controls the transmitter frequency, perfect tracking between the transmitter and receiver tuning is possible. The i-f output is fed by coaxial cable to the second mixer and the $2.8-\mathrm{me}$ intermediate frequency amplifier on the i-f and audio chassis.
1-501. FIRST R-F AMPLIFIER. The first r-f amplifier, V814, is a grounded-grid cavity-tuned
amplifier with a shunt-fed plate. The cavity is similar to the cavities used in the transmitter section and operates in exactly the same way except that the amplifier tube is located outside of the cavity. Electrical connections are made through holes in the cavity walls. Tube V814 is tapped down on the cavity center column to prevent loading of the tuned circuit by the tube. The antenna input is also tapped down to match the characteristic impedance of the coaxial line. The groundedgrid circuit is effective in preventing coupling between the input and output circuits, thus preventing oscillations due to feedback through the tube capacitance. Also, the grounded-grid design with the cathode-injection input provides a more constant input impedance over the frequency range. Two plate and two grid connections are provided on the JAN-6F4 tubes to make it possible to use shorter leads and to obtain better bypassing balance, as is illustrated by the V814 grid connections to ground through capacitors C892, C893, C898. and C899. Examination of the tuned-cavity circuits will show that only the first input cavity employs a capacitance connection, represented by C896. Since this cavity is not loaded by the plate capacitance of a vacuum tube, capacitor C896 is added in order for all three cavities to have similar tuning characteristics. Automatic-gain-control voltage, which is obtained from the i-f and audio chassis, is applied to the 1 st and 2nd r-f stages and to the $15.325-m e$ i-f stage.
1-502. SECOND R-F AMPLIFIER. The second r-f amplifier, V813, is similar to and operates in the same manner as the first r-f amplifier. Its input is capacitance-coupled from the preceding stage through capacitors C889 and C890. Its output is coupled to the mixer through capacitors C876 and C884 and inductor L823.
1-503. RECEIVER MIXER. The mixer, V812, employs the same type of tube as do the r-f amplifiers; however, in this case it is operated as a normal triode mixer with the r-f signal applied to the grid. Heterodyne oscillator injection voltage is coupled from the doubler cavity through capacitor C876 and coupling inductor L823 to the grid, in order to produce the desired $15.325-\mathrm{mc}$ intermediate frequency. The plate circuit is bypassed at the plate connection by a small capacitor, C 878 , to ensure that no input signal r-f voltage appears in the plate circuit. As regards the much lower intermediate frequency, this capacitor merely forms part of the i-f transformer tuning capacitance. No automatic gain control voltage is applied to the mixer.
1-504. RECEIVER DOUBLER. In order to pro-

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vide the proper heterodyne injection frequency at the receiver first mixer without frequency multiplication in the mixer, itself, it is necessary to include a doubler, V811, between the r-f head first doubler and the receiver first mixer. The doubler output is cavity-tuned to the received antenna signal frequency minus 15.325 mc , and is ganged to the main channel receiver $\mathbf{r - f}$ tuning.
1-505. I-F AMPLIFIER. The $15.325-\mathrm{me}$ i-f amplifier, V810, is conventional in all respects with the possible exception of the suppressor injection of the automatic gain control voltage. By applying automatic gain control voltage to the suppressor grid, it is possible to keep the impedance of the signal grid-return circuit low, thus preventing paralysis of the amplifier on strong noise pulses. The i-f output transformer, T802, is designed to work into the low-impedance ( 52 -ohm) coaxial cable through which the i-f output is carried to the second receiver mixer, located on the i-f and audio chassis.
1-506. TEST POINTS. To facilitate testing of the $r$-f head, an 11-pin test socket is provided. Connections to the socket pins provide for measurement of plate supply voltages, mixer injection voltages, and grid drive.
1-507. TUNING. All of the tuned r-f circuits of the transmitter and receiver that must be varied when changing channels, are ganged together and driven by a reversible tuning motor, B801. The drive is through a system of gears and any one of three clutches 0808,0804 , and 0805. A detailed description of the mechanical and switching design of the tuning system is beyond our present assignment.

## The Collins Synthesizing System

1-508. An interesting approach to the problem of controlling many r-f channels with the use of only a few crystals is afforded by the frequency-control system employed in a number of the multichannel radio sets developed by the Collins Radio Company. Fundamentally this system is a crystalcontrolled multi-conversion superheterodyne circuit when employed in radio receivers, and is equivalent to the same circuit operated in reverse when employed in radio transmitters. The receiver system is quite similar to the Bendix synthesizing system, except that the signal from the variable frequency oscillator is replaced by the antenna signal to which the r-f circuits are tuned and the discriminator is replaced by a final i-f stage. When operated in reverse for transmitter use, the system resembles somewhat the Plessey synthesizing system, except that the frequency dividers and
harmonic selectors of the Plessey system are replaced by crystal oscillators with banks of crystal units. We shall not discuss the Collins system further from a generalized point of view, but shall advance at once to the discussion of its application in two aircraft receiver circuits (Radio Receiver R-252A/ARN-14 and Radio Receiver R-278/GR) and in the aircraft transceiver, Radio Set AN/ARC-27. Since Radio Set AN/ARC-27 performs essentially the same function as does Radio Set AN/ARC-33, described in the foregoing paragraphs, a study of the two circuits provides an interesting comparison of the two systems of frequency control and how they can be applied to achieve the same end.
RADIO RECEIVER R-252A/ARN-14
1-509. Radio Receiver R-252A/ARN-14, a product of the Collins Radio Company, is a component of Radio Receiving Set AN/ARN-14. It is an airborne navigation receiver that provides reception on any one of 280 channels spaced 100 kc apart between 108.0 and 135.9 mc . A crystal-controlled double-conversion superheterodyne circuit is used to "de-synthesize" the incoming signal to a fixed intermediate frequency of 3.15 mc . The 280 channels are obtained from a total of 24 crystal units. Actually, this number of channels can be obtained from a Collins synthesizing system employing a fewer number of crystal units, if a triple- rather than a double-conversion superheterodyne circuit is used. That is, if an additional oscillator, mixer, and i-f amplifier stage is inserted, the required number of crystal units becomes less. In this equipment, however, maximum economy in space, weight, and the over-all number of component parts clearly is achieved by increasing slightly the number of crystal units rather than by the addition of a number of extra vacuum-tube circuits. The functional operation of the frequency-control system is indicated in the block diagram of figure 1-201. Figure $1-200$ shows the schematic diagram of the radio-frequency control circuits. With the exception of minor editing changes and technical insertions the circuit descriptions to follow are primarily extracts from USAF Technical Order No. 12R5-2ARN14-12.
R-F Control Circuits
1-510. One stage of tuned r-f amplification is used in Radio Receiver R-252A/ARN-14. The grid and plate tank circuits of the r-f amplifier, V101, pass a $2-\mathrm{mc}$ band of frequencies and cover the entire frequency range 108.0 to 135.9 mc in 14 increments. The output of the r-f amplifier is coupled to the grid of the 1st mixer V102. The 1st mixer receives its injection frequency from a three-stage

108-135.9MC 2MC WIDE



Figure 1-200. Block diagram of the Collins crystal-controlled, multichannel, frequency-control system as employed in the double-conversion superheterodyne circuit of Radio Receivar R-252A/ARN-14


Figure 1-201. Schematic diagram of radio-frequency-control circuits of Radio Receiver R-252A/ARN-14. Only the ist amplifier of the three-stage fixed $(3.15 \mathrm{mc})$ i-f amplifier circuit is shown. The automatic switching system is not shown
exciter consisting of a crystal-controlled Butler oscillator-multiplier, V112, and an amplifier, V111. The oscillator employs a bank of 14 type CR-23/U crystal units whose frequencies cover the range 44.275 to 57.275 mc in one-megacycle steps. The plate tank of the grounded-grid tube is tuned to the desired crystal frequency. Output from the oscillator is inductively coupled from the plate circuit of the cathode follower to the input tank of amplifier V111. Both the input and output circuits of the amplifier are tuned to twice the oscillator frequency. Thus, the injection frequencies fed to the 1st mixer cover the range of 88.55 to 114.55 mc in 14 two-megacycle steps. These injection frequencies, when mixed with the r-f signals in the range of 108.0 to 135.9 mc , produce an intermediate frequency in the range of 19.45 to 21.35 mc . Note that the function of the 1st injection oscillator and multiplier is to generate 14 very high frequencies spaced 2 mc apart so that by selecting the proper injection frequency, the 280 possible antenna frequencies within a $28-\mathrm{mc}$ range can be reduced to 20 possible intermediate frequencies within a 2 -me range. Each of the 20 i-f channels handles 14 of the $r$-f channels. The output of the 1st mixer is thus fed to the variable i-f amplifier, and thence to the 2nd mixer. The injection frequency for the 2 nd mixer originates in an electroncoupled oscillator-doubler circuit. The oscillator is of the grounded-plate Pierce type and employs a bank of 20 type CR-18/U crystal units spaced 50 kc apart in the 8.15 -to- 9.10 -me range. The screen grid of tube V113 serves as the oscillator anode. The plate circuit is tuned to twice the oscillator
fundamental, so that the actual injection frequencies for the 2nd mixer are spaced 100 kc apart and cover the range of 16.3 to 18.2 mc . Each of the 2nd injector frequencies can be matched with one of the $20 \mathrm{i}-\mathrm{f}$ channels to produce a difference frequency of 3.15 mc . This $3.15-\mathrm{mc}$ frequency is thus used as the fixed intermediate-frequency channel. It passes through three amplifier stages of similar design except that the 3rd $3.15-\mathrm{mc}$ i-f amplifier does not operate with a-v-c grid bias before being fed to the detector.
1-511. The tuning of the r-f and variable i-f circuits, as well as the selecting of the high- and lowfrequency crystals, is performed by two Collins "Autopositioners." One Autopositioner controls the tuning in 142 -me steps and the other controls the fine tuning in $20100-\mathrm{kc}$ steps. The tuning elements of the grid and plate tank circuits of the r-f amplifiers and the frequency multiplier, and the high-frequency crystal selector switches are ganged and operated by the megacycle Autopositioner. The 0.1-megacycle Autopositioner tunes the grid and plate circuits of the variable i-f amplifier and the plate circuit of the low-frequency oscillator, and selects the low-frequency crystals. Because the crystal selector switches and tuning elements are ganged, the injection frequencies that result in the fixed intermediate frequency of 3.15 mc are always automatically selected. Table (1) shows the tuning of the double-conversion system for the first 22 channels. By extending the table in the same manner as shown, complete information for the entire range of received frequencies can be obtained.

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| Channel Selector <br> Position |  | Frequency of Received Signal | Frequency Band Passed by R-F Amplifier | Frequency of |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Ist Mixer |  | Variable | 2nd Mixer | Fixed 1-F |
| $M c$ | . 1 Mc |  |  | Inj. Signal | I-F Amplifier | Inj. Signal | Amplifier |
| 108 | 0.0 |  | 108.0 mc | 108.0 to 110.0 | 85.55 mc | 19.45 mc | 16.3 mc | 3.15 mc |
|  | 0.1 | 108.1 | 108.0 to 110.0 | 85.55 | 19.55 | 16.4 | 3.15 |
|  | 0.2 | 108.2 | 108.0 to 110.0 | 85.55 | 19.65 | 16.5 | 3.15 |
|  | 0.3 | 108.3 | 108.0 to 110.0 | 88.55 | 19.75 | 16.6 | 3.15 |
|  | 0.4 | 108.4 | 108.0 to 110.0 | 88.55 | 19.85 | 16.7 | 3.15 |
|  | 0.5 | 1108.5 | 108.0 to 110.0 | 88.55 | 19.95 | 16.8 | 3.15 |
|  | 0.6 | 108.6 | 108.0 to 110.0 | 88.55 | 20.05 | 16.9 | 3.15 |
|  | 0.7 | 108.7 | 108.0 to 110.0 | 88.55 | 20.15 | 17.0 | 3.15 |
|  | 0.8 | 108.8 | 108.0 to 110.0 | 88.55 | 20.25 | 17.1 | 3.15 |
|  | 0.9 | 108.9 | 108.0 to 110.0 | 88.55 | 20.35 | 17.2 | 3.15 |
|  | 1.0 | 109.0 | 108.0 to 110.0 | 88.55 | 20.45 | 17.3 | 3.15 |
|  | 1.1 | 109.1 | 108.0 to 110.0 | 88.55 | 20.55 | 17.4 | 3.15 |
|  | 1.2 | 109.2 | 108.0 to 110.0 | 88.55 | 20.65 | 17.5 | 3.15 |
|  | 1.3 | 109.3 | 108.0 to 110.0 | 88.55 | 20.75 | 17.6 | 3.15 |
|  | 1.4 | 109.4 | 108.0 to 110.0 | 88.55 | 20.85 | 17.7 | 3.15 |
|  | 1.5 | 109.6 | 108.0 to 110.0 | 88.55 | 20.95 | 17.8 | 3.15 |
|  | 1.6 | 109.6 | 108.0 to 110.0 | 88.55 | 21.05 | 17.9 | 3.15 |
|  | 1.7 | 109.7 | 108.0 to 110.0 | 88.56 | 21.15 | 18.0 | 3.15 |
|  | 1.8 | 109.8 | 108.0 to 110.0 | 88.55 | 21.25 | 18.1 | 3.15 |
|  | 1.9 | 109.9 | 108.0 to 110.0 | 88.55 | 21.35 | 18.2 | 3.15 |
| 110 | 0.0 | 110.0 | 110.0 to 112.0 | 90.55 | 19.45 | 16.3 | 3.15 |
|  | 0.1 | 110.1 | 110.0 to 112.0 | 90.55 | 19.55 | 16.4 | 3.15 |

Table 1-511 (1). Tuning position for first 22 channels of Radio Receiver R-252A/ARN-14. Remaining channels are obtained in similar manner.

## RADIO RECEIVER R-278/GR

1-512. Radio Receiver R-278/GR provides a second example of the Collins method of controlling many frequencies with a few crystals. In principle, the frequency-control system is the same type as that described above for Radio Receiver R-252A/ARN-14, except that in the R-278/GR
receiver a triple-conversion superheterodyne circuit is employed instead of a double-conversion circuit. Functionally, the receiver is the same as the AN/ARC-33 receiver circuit in that it provides crystal-controlled reception of 1750 channels spaced 100 ke apart between 225 and 399.9 mc . This task is performed with the use of 38 crystal


Figure 1-202. Block diagrom and frequency chart of Collins frequency-control system as employed in Radio Receiver R-278/GR

| 10-MC <br> Dial <br> Reading | $R-F$ <br> Band <br> $M C$ | Inj <br> Freq <br> $M C$ | Crystal <br> Freq <br> $M C$ | Mult <br> Factor |
| :---: | :---: | :---: | :---: | :---: |
| 22 | $220.0-229.9$ | 180.0 | 30.0000 | 6 |
| 23 | $230.0-239.9$ | 190.0 | 31,6667 | 6 |
| 24 | $240.0-249.9$ | 200.0 | 33.3333 | 6 |
| 25 | $250.0-259.9$ | 210.0 | 35.0000 | 6 |
| 26 | $260.0-269.9$ | 220.0 | 36.6667 | 6 |
| 27 | $270.0-279.9$ | 230.0 | 38.3333 | 6 |
| 28 | $280.0-289.9$ | 240.0 | 26.6667 | 9 |
| 29 | $290.0-299.9$ | 250.0 | 27.7777 | 9 |
| 30 | $300.0-309.9$ | 260.0 | 28.8888 | 9 |
| 31 | $310.0-319.9$ | 270.0 | 30.0000 | 9 |
| 32 | $320.0-329.9$ | 280.0 | 32.1111 | 9 |
| 33 | $330.0-339.9$ | 290.0 | 33.3333 | 9 |
| 34 | $340.0-349.9$ | 300.0 | 34.4444 | 9 |
| 35 | $350.0-359.9$ | 310.0 | 35.5555 | 9 |
| 36 | $360.0-369.9$ | 320.0 | 36.6667 | 9 |
| 37 | $370.0-379.9$ | 330.0 | 37.7778 | 9 |
| 38 | $380.0-389.9$ | 340.0 | 38.8889 | 9 |
| 39 | $390.0-399.9$ | 350.0 |  | 9 |


| $1-M C$ <br> Dial <br> Reading | 1st 1-F <br> Band MC | Crystal <br> and Inj <br> Freq MC |
| :---: | :---: | :---: |
| 0 | $40.0-40.9$ | 31.0 |
| 1 | $41.0-41.9$ | 32.0 |
| 2 | $42.0-42.9$ | 33.0 |
| 3 | $43.0-43.9$ | 34.0 |
| 4 | $44.0-44.9$ | 35.0 |
| 5 | $45.0-45.9$ | 36.0 |
| 6 | $46.0-46.9$ | 37.0 |
| 7 | $47.0-47.9$ | 38.0 |
| 8 | $48.0-48.9$ | 39.0 |
| 9 | $49.0-49.9$ | 40.0 |


| O.1-MC <br> Deading | 2nd I-F <br> Freq MC | Crystal <br> and Inj <br> Freq MC |
| :---: | :---: | :---: |
| .0 | 9.0 | 6.95 |
| .1 | 9.1 | 7.05 |
| .2 | 9.2 | 7.15 |
| .3 | 9.3 | 7.25 |
| .4 | 9.4 | 7.35 |
| .5 | 9.5 | 7.45 |
| .6 | 9.6 | 7.55 |
| .7 | 9.7 | 7.65 |
| .8 | 9.8 | 7.75 |
| .9 | 9.9 | 7.85 |

R-f amplifier
1st injection
1st i-f amplifier
2nd injection
2nd i-f amplifier
3rd injection
3rd i-f amplifier

## Frequency Range

$220.0-399.9 \mathrm{mc}^{*}$
$180.0-350.0 \mathrm{mc}$
$40.0-49.9 \mathrm{mc}$
$31.0-40.0 \mathrm{mc}$
$9.0-9.9 \mathrm{mc}$
$6.95-7.85 \mathrm{mc}$
2.05 mc

Tuned in 180 1-mc steps Tuned in $1810-\mathrm{mc}$ steps Tuned in $1000.1-\mathrm{mc}$ steps Tuned in $101-\mathrm{mc}$ steps Tuned in $100.1-$ me steps Tuned in $100.1-\mathrm{mc}$ steps Fixed tuned
*Note that although the frequency range of the receiver is specified as being from 225.0 to 399.9 mc , the frequency system employed is inherently' capable of providing 50 additional frequencies in the range 220.0 to 224.9 mc .

Figure 1-202 (Continued). Frequency chart of Collins frequency-control system


Figure 1-203. Radio-frequency amplifier unit of Radio Receiver R-278/GR. Schematic diagram


Figure 1-204. Construction of r-f funer employed in Radio Receiver R-278,'GR
units. For the reader who has followed the discussion of the frequency-control system in Radio Receiver R-252A/ARN-14, the functional operation of the system outlined for Radio Receiver R-278/GR in the frequency diagram of figure 1-202 should be largely self-explanatory.
1-513. Briefly, the r-f amplifier consists of two stages of grounded-grid vacuum-tube amplification, as shown in the schematic diagram of figure $1-203$. The r-f amplifier is tuned in 180 one-me steps covering the range 225 to 399.9 mc . A special type of r-f tuner is used, and is illustrated in figure 1-204. This tuner consists of a variable capacitor and a variable inductor which are rotated simultaneously so that the resonant frequency changes linearly 180 me in 180 degrees of rotation, or 1 me per degree. The variable capacitor consists of two stator plates and three rotor


Figure 1-205. Oscillator unit of 1 st injection system in Radio Receiver R-278/GR. Schematic diagram
plates, the front and rear of which are radially slotted for the purpose of alignment adjustments. The inductive loop consists of the inductance stator rod, a ring segment, and the inductance rotor rod. The three r-f tuners are geared together and driven through a mechanical differential that combines the rotary motion of an 18 position 10 -me tuning shaft with that of a $10-$ position 1 -me tuning shaft to permit a total of 180 1-mc steps.
1-514. The 1st injection system consists of the main oscillator unit shown in figure 1-205 followed by the five-stage multiplier-amplifier unit shown in figure 1-206. The oscillator is a Butler


Figure 1-206. Multiplier-amplifier unit of 1st injection system in Radio Receiver R-278/GR. Schematic diagram
circuit employing a temperature-controlled bank of 18 crystal units of the CR-32/U type, and a bank of 18 tuning coils in the plate output circuit of the grounded-grid tube. The first tube, V301, of the multiplier-amplifier unit serves as a doubler for the six lowest injection frequencies (not the six lowest oscillator frequencies) and as a tripler for the 12 highest injection frequencies. The second tube, V302, is tuned to triple all its input frequencies. The next three stages are grounded-grid, shunt-fed amplifiers. The r-f tuners shown in the last four stages of the multiplier-amplifier unit are similar to the r-f tuners described in the foregoing paragraph, but differ in that the frequency range is different. The 1 st injection system is tuned in eighteen $10-\mathrm{mc}$ steps by the 10 mc tuning shaft, which also operates the main oscillator crystal selector switch.
1-515. The 1st i-f amplifier unit, see figure 1-207, consists of the 1 st mixer, the 1 st i-f amplifier, the 2nd oscillator, and the 2nd mixer. The 1st mixer stage reduces the 1750 possible antenna frequencies to 100 possible intermediate frequencies spaced 0.1 mc apart in the 40.0 -to- 49.9 -mc range.

The i-f interstage transformers are therefore tumable in 0.1 -me increments over a 10 -me i-f band. Permeability tuning is employed, with the tuning controlled by a cam-driven tuning rack. The second oscillator is another Butler circuit, this one employing a bank of 10 type CR-23/U crystal units operating at frequencies 1 mc apart from 31 to 40 mc . The 2nd mixer serves to reduce the 100 first i-f channels to 10 second i-f channels spaced 0.1 me apart in the 9.0 -to- 9.9 -me range.
1-516. The 2 nd i-f amplifier unit, see figure 1-208, consists of the 2nd i-f amplifier, the 3rd injection oscillator, and the 3 rd mixer. The 2nd i-f amplifier signal is conducted over a type RG-58/U coaxial line from the plate of the 2nd mixer to the primary of the input transformer, T501, of the 2nd i-f amplifier. The 2nd i-f transformers are per-meability-tuned in ten 0.1 -mc increments over the range 9.0 to 9.9 mc by a cam-driven tuning rack. The 3rd oscillator, which uses one half of a twin triode tube (12AU7), is a grounded-plate Pierce circuit that uses a bank of 10 type CR-18/U crystal units. The crystal frequencies are spaced 0.1 me apart in the range 6.95 to 7.85 mc . The 3 rd


Figure 1-207. First i-f amplifier unit in Radio Receiver R-278/GR. Schematic diagram


Figure 1-208. Second i-f amplifier unit in Radio Receiver R-278/GR. Schematic diagram
oscillator signal is fed to the cathode of the 3rd mixer, where it is heterodyned with the incoming 2nd i-f signal to form the 3rd and fixed intermediate frequency of 2.05 mc . The $2.05-\mathrm{mc}$ output of the 3rd mixer is carried over a type RG-58/U coaxial line to the input transformer, T601, of the 3rd i-f amplifier, which consists of three fixedtuned amplifier stages. See figure 1-209.

## RADIO SET AN/ARC-27

1-517. Perhaps the most interesting example of the Collins system of frequency synthesis is provided by Radio Set AN/ARC-27. This is a v-h-f and u-h-f airborne transceiver set developed by the Collins Radio Company; it is the functional equivalent of Radio Set AN/ARC-33, described earlier as an example of the Bendix synthesizing method. For transmitter operation of Radio Set AN/ARC-27, four crystal oscillators employing a total of 22 crystal units are interrelated by means of harmonic generators and frequency mixers to cover the range between 225 and 399.9 mc in 0.1 me increments. The operator thus has a choice of
any one of 1750 crystal-controlled channels of $100-\mathrm{kc}$ width. If transmission were the only function of this radio set, at least one of the four crystal oscillators (the $3.45-\mathrm{me}$ oscillator) could be eliminated and no doubt much of the remaining network could be simplified. As it is, however, the ARC-27 is also designed to receive the same frequencies that it transmits. The same operation that tunes the receiver to a particular channel automatically tunes the transmitter to the same channel. This is achieved by using many of the same tuned circuits that pass the received signal in one direction during receiver operation, to pass the transmitted signal in the opposite direction during transmitter operation. For example, a transformer primary in the plate circuit of a receiver vacuum tube may become a transformer secondary in the grid circuit of a transmitter tube when the set is switched to transmit operation. The transmitter frequency synthesizer is basically the receiver superheterodyne system operated in reverse. It is the set of modifications imposed upon the frequency synthesizing network by this


Figure 1-209. Third i-f amplifer in Radio Receiver R-278/GR. Schematic diagram
bi-directional feature that makes the ARC-27 circuits of special interest.
1-518. The network system incorporated in the design of Receiver-Transmitter RT-178/ARC-27 (the principal unit of Radio Set AN/ARC-27) suggests that, in approaching the problem of frequency control, the designers probably placed first emphasis upon the superheterodyne circuit of the receiver; then, to this basic design introduced the switching arrangements necessary for the same circuit to operate in the opposite direction. Where the receiver reduces all incoming signals to a fixed crystal-controlled intermediate frequency of 3.45 me, the transmitter starts with a fixed crystalcontrolled frequency of 3.45 mc and, by reversing the direction of each of the receiver heterodyne processes, is able to generate for transmission the same channel frequency to which the receiver is tuned. The reversed superheterodyne network thus forms a principal feature of the Collins synthesizing system, a feature uniquely applicable in the design of two-way multichannel radio sets.
1-519. The ARC-27 synthesizing circuit is more readily explained when we examine the network first from the receiver point of view. A block diagram of the receiver circuit is shown in figure 1-210. This circuit operates in exactly the same manner as the triple-conversion superheterodyne
circuit in Radio Receiver R-278/GR discussed previously. The only difference is in the choice of the values of the intermediate frequencies and in the fact that the ARC-27 set employs a fixedfrequency $10-\mathrm{mc}$ crystal oscillator and a spectrum system that permits a selection of any one of eighteen $10-\mathrm{mc}$ harmonics for the 1st injection frequency, whereas the R-278 receiver employs an 18-crystal oscillator and five-stage multiplieramplifier system for the same purpose, which is to reduce the 1750 antenna channels to 100 first i-f channels. The 2nd and 3rd oscillators of the ARC-27 receiver circuit are of the same design as the 2nd and 3rd oscillators, respectively, of the R-278 receiver except for the actual values of the crystal frequencies. The $1-\mathrm{mc}$ and $0.1-\mathrm{mc}$ spacing of the 2 nd and 3 rd injection frequencies are, nevertheless, common to both receivers.
1-520. If we now examine the block diagram of the ARC-27 transmitter synthesizer shown in figure 1-211, we see that it essentially is a reversal of what might be described as the "frequency desynthesizer" network of the ARC-27 receiver. Let $f_{a}, f_{b}, f_{c}$, and $f_{d}$ equal the antenna frequency and the 1 st , 2 nd , and 3 rd intermediate frequencies, respectively; and let $f(10), f(1)$, and $f(0.1)$ represent the $10-\mathrm{mc}, 1-\mathrm{mc}$, and $0.1-\mathrm{mc}$ injection frequencies respectively, as indicated in the block


Figure 1-210. Block diagram of main receiver network of Receiver-Transmiffer RT-178/ARC-27


Figure 1-211. Block diagram of transmitter network of Receiver-Transmitter RT-178/ARC-27
diagrams. For both receiver and transmitter operation the frequency of the antenna signal can be expressed by the equation

$$
\begin{equation*}
f_{\mathrm{a}}=\mathbf{f}(10)+\mathbf{f}_{b} \tag{1}
\end{equation*}
$$

where

$$
\begin{equation*}
f_{b}=f(1)-f_{e} \tag{2}
\end{equation*}
$$

and
$\mathrm{f}_{\mathrm{c}}=\mathrm{f}(0.1)-\mathrm{f}_{\mathrm{d}}$
so by substitution

$$
\begin{equation*}
f_{a}=f(10)+f(1)-f(0.1)+f_{d} \tag{4}
\end{equation*}
$$

Ordinarily for frequency synthesis in a decade system we would suppose that the final frequency would be given by the formula

$$
f_{a}=f(10) \pm f(1) \pm f(0.1)
$$

where $f(10)$ determines the frequency to the nearest $10-\mathrm{mc}$ unit, $f(1)$ to the nearest $1-\mathrm{mc}$ unit, and $f(0.1)$ to the nearest $0.1-\mathrm{mc}$ unit. Consequently, the employment of a constant frequency, $\mathrm{f}_{\mathrm{d}}$, which in the ARC-27 transmitter is a $3.45-\mathrm{mc}$ oscillator signal, would normally be superfluous. But in the ARC-27 set, the $3.45-\mathrm{mc}$ crystal oscillator is inserted with advantage since it enables the same crystal units that control the injection frequencies in the receiver to control the injection frequencies in the transmitter.

1-521. With the aid of equations $1-520$ (1) to (4) and the block diagram in figure 1-211, the frequency synthesizing system employed in the ARC27 transmitter is largely self-explanatory. The desired transmitter signal is synthesized by heterodyning the $3.45-\mathrm{mc}$ and $4.8-5.7-\mathrm{mc}$ oscillator outputs and selecting their difference product, $\mathrm{f}_{\mathrm{c}}$, for amplification. In turn, $\mathrm{f}_{\text {s }}$ is heterodyned with the $25.7-34.7-\mathrm{mc}$ oscillator output and again the difference product, this time $f_{b}$, is selected. Next, $f_{b}$ is amplified and mixed with the $f(10)$ output of the spectrum amplifier. The sum product, $f_{n}$, which is the desired final frequency, is selected and amplified for transmission.
1-522. The various injection frequencies used in Radio Set AN/ARC-27 are generated by conventional crystal oscillators, except for the output of the spectrum generator. The function of the spectrum generator is to convert an initial $10-\mathrm{mc}$ output from an electron-coupled Pierce oscillator into any desired harmonic of 10 mc between 200 and 370 mc . Although the function of the spectrum generator is effectively that of a harmonic generator, the output frequency, $f(10)$, is not simply the product of a straightforward sequence of fre-quency-multiplier and harmonic-selector stages.

Rather, $\mathrm{f}(10)$ is a synthesized frequency produced by selecting two appropriate harmonics of the 10 -mc fundamental and mixing them to form the desired product. Referring to the block diagram in figure 1-212, it can be seen that the $10-\mathrm{mc}$ oscillator is isolated from the multiplier stages by a buffer amplifier. The output of the buffer amplifier is used to excite two different multiplier circuits. One multiplier is fixed-tuned to select and amplify the 9 th harmonic ( 90 mc ); the second multiplier can be switched to select and amplify either the 1 st, 2 nd, 3 rd, or 4 th harmonic (10, 20, 30 , or 40 mc ). The outputs of the two multiplier circuits are then mixed. Selection of the desired frequency product is made by the ganged tuning in $10-\mathrm{mc}$ steps of two selective vacuum-tube amplifier stages. In table (1) below are given the harmonic multiplier combinations by which the desired spectrum frequency, $f(10)$, is obtained. Note that the $90-\mathrm{mc}$ signal is not employed, but only its 2nd, 3rd, and 4th harmonies.

1-523. Figures 1-213 to 1-217 are schematic diagrams of the frequency-control circuits in Re-ceiver-Transmitter RT-178/ARC-27. Minor differences exist among the various models of the transceiver which have been produced since the original. The schematies shown apply to Collins model No. 6 of the RT-178/ARC-27 series. The positions of the different switches and tuning adjustments are controlled automatically by a Collins Autotune system. Any of the 1750 channels can be selected by using the decade frequency selectors on the local control panel. In addition, any one of 18 preset channels or a guard receiver can be selected from both remote and local control panels. When the radio set is being operated in the receive position, plate voltage is automatically removed from those tubes that are used only during transmitter operation; likewise, when the radio set is being operated in the transmit position, plate voltage is removed from those tubes used only during receiver operation. With the aid of the block dia-

| $f(10)=m \times 9 f \pm n f$ | $f(10)=m \times 9 f \pm n f$ |
| :---: | :---: |
| $200=2 \times 90+20$ | $290=3 \times 90+20$ |
| $210=2 \times 90+30$ | $300=3 \times 90+30$ |
| $220=2 \times 90+40$ | $310=3 \times 90+40$ |
| $230=3 \times 90-40$ | $320=4 \times 90-40$ |
| $240=3 \times 90-30$ | $330=4 \times 90-30$ |
| $250=3 \times 90-20$ | $340=4 \times 90-20$ |
| $260=3 \times 90-10$ | $350=4 \times 90-10$ |
| $270=3 \times 90+0$ | $360=4 \times 90+0$ |
| $280=3 \times 90+10$ | $370=4 \times 90+10$ |

Table 1-522 (1). Harmonic generator combinations employed in the synthesis of $f(10)$, the output frequency of the spectrum generator in Radio Set AN/ARC-27. All frequencies are in megacycles per second.


Figure 1-212. Block diagram of spectrum generator system in Radia Set AN/ARC-27


Figure 1-213. Main receiver r-f amplifier subassembly, Receiver-Transmitfer RT-178/ARC-27. Includes receiver circuits V101, V102, and V103 (r-f amplifier and Ist mixer stages). See figure 1-210 for relation of the above stages to the rest of the receiver frequency-control system


Figure 1-214. 10 -mc spectrum oscillator, V401, buffer amplifier, V402, and 90 -mc multiplier, V403, of ReceiverTransmitfer RT-178/ARC-27. See figure 1-212 for function of the above circuits in the spectrum generator system



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Figure 1-216. 20-30-mc i-f amplifier subassembly, ReceiverTransmitter RT-178/ARC-27. See figure J-210 for functional operation of receiver circuits V201, V203, V205, and V207. See figure 1-211 for functional operation of transmifter circuits V202, V204, V206, and V207


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Section 1


Figure 1-217. Fixed i-f amplifer subassembly, Receiver-Transmifter RT-178/ARC-27. See Agure 1-210 for function of receiver circuits V301, V303, V305A, V306A, and V307. IV308 and V309, the 2 nd and 3 rd $3.45-\mathrm{mc}$ amplifiers, which are similar in design to the V307 stage, are not shown. Also omitted are the vacuumtube heater circuits.) See Agure 1-211 for function of transmitter circuits V302, V304, V305B, V306A, and V306B
grams in figures 1-210, 1-211, and 1-212, the functions of the various circuit components shown in the schematic diagrams should be reasonably apparent in most instances. The designs of the individual stages are for the most part conventional. The r-f tuners used in the receiver r-f amplifier, in the spectrum amplifier, and in the transmitter preamplifier are not of a conventional type, but their design has been described in connection with similar circuits in Radio Receiver R-278/GR. See figure 1-204. Also unconventional is the coupling between the 1st mixer in the receiver and the spectrum amplifier. In figure 1-215, note that the V505 output of the spectrum generator is fed to the cathode of the 6J4 transmitter mixer, V506. Capacitor C534, which is connected between the grid of V506 and ground, is large enough to effectively ground the grid at the spectrum generator frequencies, but is small enough to present a fairly high impedance to the input from the $20-30-\mathrm{me}$ transmitter amplifier, V202. Thus, V506 operates as a grounded-grid circuit insofar as the spectrum injection frequencies are concerned, so that these frequencies tend to be attenuated somewhat in the mixer output. Attenuation of the $20-30-\mathrm{mc}$ signal in the mixer output is less of a problem since the $20-30-\mathrm{mc}$ band is separated by such a large percentage difference from the frequencies at which the transmitter preamplifier circuits are tuned. Although C534 effectively grounds the grid of V506 at the spectrum frequencies during transmitter operation, it does not completely do so. During receiver operation, when plate voltage is removed from V506, the output of the spectrum generator is coupled through the grid-cathode capacitance of the tube to the grid circuit, and the voltage developed across C534 is sufficient for injection excitation of the 1st receiver mixer. This injection voltage for receiver operation is fed through the same cable, Z104 (see figure 1-213), that is used to transmit the $20-30$-mc signal to V506 during transmitter operation. The receiver mixer, V103, employs cathode injection by means of capacitance coupling between two wires in the specially constructed cable, Z104. From the schematic it can be seen that the wire that is connected directly to the grid of V506 is connected to the plate of V103 through C125 and L109. L109 is an r-f choke at the spectrum generator frequencies, so that for all practical purposes this circuit can be assumed to be open during receiver operation. For transmitter operation, L109 and C125 in series present a sufficiently low reactance for the $20-30-\mathrm{me}$ signal from the transmitter amplifier, V202, to be fed to the transmitter mixer, V506.

The reason that the $20-30$-mc transmitter signal is fed to the transmitter mixer via the plate circuit of the receiver mixer instead of being fed directly is simply one of economy-to make use of the J102/J202 connection from the plate of the receiver mixer to transformer T201 during transmitter operation as well as during receiver operation. In figure $1-216$ it can be seen that during receiver operation, transformer T201 couples the output of receiver mixer V103 to the input of receiver amplifier V201; during transmitter operation, T201 is operated in the reverse direction, coupling the output of V202 to the plate of V103 (which tube is inoperative since its plate voltage is removed) and from there through C125, L109, Z104, and connection P102/J503 to the grid of the transmitter mixer, V506.
1-524. Since the greater part of the final transmitter frequency is controlled by the $10-\mathrm{mc}$ spectrum generator oscillator, it is primarily the stability of this oscillator that determines the stability of the transmitted frequency. The $10-\mathrm{mc}$ oscillator is a grounded-plate ( $r$ - $f$ grounded-screenanode) electron-coupled Pierce circuit that employs an oven-mounted type CR-27/U crystal unit. The remaining oscillators do not employ thermostatically controlled ovens for mounting their respective crystal units, since the normal frequency deviations of these crystals with temperature changes can have but an insignificant percentage effect upon the final frequency. R-f grounded-plate oscillators of the Pierce type employing CR-18/U crystal units are used for the $3.45-\mathrm{mc}$ and the 8.25 -9.15-mc oscillators. The $25.7-34.7-\mathrm{mc}$ injection oscillator is of the cathode-coupled Butler type and empioys a 10 -position bank of type CR-23/U crystal units. For the reader interested in a more detailed discussion of the over-all design of Radio Set AN/ARC-27, reference can be made to USAF Technical Order No. 12R2-2ARC27-2.

## Attenuction of Unwonted Products in Frequency Synthesis

(This discussion is primarily an abstract of portions of "Developments in Frequency Synthesis" by Mr. H. J. Finden of the Plessey Company, Ltd., England, a paper delivered before the Conference on High Frequency Measurements, Washington, D.C., 1953 and published in revised form in Eleotronic Engineering, May, 1953.)
1-525. Among the more difficult problems that face the designer of frequency synthesizing circuits are those that concern the elimination of all frequencies except the one desired signal. When two frequencies, $f_{1}$ and $f_{2}$, are mixed, it is custom-
ary to regard the output of the mixer stage as being composed of four frequencies, namely, $f_{1}, f_{2}$, $f_{1}$ plus $f_{2}$, and $f_{3}$ minus $f_{2}$. In practice, we know that due to non-linearities of both the input and output stages, higher harmonics of each of the fundamental frequencies are also present, as well as all possible combinations of their sum and difference products. Thus, whenever a particular output frequency is to be selected from a synthesized mixture, especially if a relatively pure sine wave output is desired, many more than the four principal fundamental frequencies must be considered. The conventional method of selecting one frequency from a mixture of several is, of course, to employ filters that readily pass a narrow band of frequencies in the neighborhood of the desired frequency, but greatly attenuate all frequencies above and below the passband. In the special case of where the desired frequency is the lowest frequency present, a low-pass filter can be u.ad to reject all frequencies higher than the one desired. (Where all harmonics are present, high-pass filters are not applicable for the rejection of all but one frequency.) Where a relatively pure output is desired, satisfactory filtering can become quite difficult and expensive to achieve in a frequency synthesizer unless two preventive steps are taken: one step is to ensure that the input frequencies of the mixer are uttenuated in the mixer stage itself; a second step is to ensure that none of the significant unwanted frequencies lies close to the desired frequency.

## THE BALANCED MODULATOR IN FREQUENCY SYNTHESIS

1-526. When two or more frequencies are to be mixed to obtain a sum or difference product, the normal approach is to employ a mixer stage of maximum efficiency as measured by the ratio of the heterodyne output level to the input signal level. However, where greater-than-normal purity of the desired heterodyne product is the goal, as well may be the requirement of a frequency synthesizer, the more important signal ratio to consider in the mixer is the ratio of the heterodyne output level to the level of the input frequencies as they are measured in the output. For this reason the balanced modulator can be used to advantage as a mixer stage in a frequency synthesizer of pure sine waves, even though its conversion efficiency is less than that of other types of mixers. Figure 1-218 illustrates the circuit of a balanced linear modulator of the same design as the mixer stages that are used in the Plessey frequency synthesizer. Note that since the two balanced amplifiers are connected in paraliel, but are excited 180
degrees out of phase, the input signals are virtually eliminated in the output. In practice, it is not possible to balance the circuit perfectly. Optimum performance is obtained by adjusting the circuit for maximum attenuation of whichever input frequency differs from the desired heterodyne product by the smallest percentage. Generally, this is the higher of the two input frequencies, except when the desired frequency is the difference product, where the higher of the two input frequencies is not greater than 2.6 (approximately) times the lower.
1-527. Measurements made at the Plessey Company of the relative power levels of the frequencies in the output of an experimental balanced modulator are shown in table (1). For this experiment $f_{1}$ equaled 100 kc and $\mathrm{f}_{2}$ equaled 740 kc . The modulator was balanced for maximum attenuation of $\mathrm{f}_{\mathrm{s}}$. The output strength of the fundamental difference product, 640 kc , was taken as the zero db reference level. Note that the sum product, 840 kc, was measured at the same level, but that all other frequencies in the output' were at negative db levels. The sum and difference products involving the 5th harmonic of $f_{1}$ ( 500 kc ) were negligible. Where the strength of the wanted frequency must be made 60 or 70 db greater than that of any other frequency, it can be seen that a mixer stage which does not, itself, attenuate the input frequencies in its output circuit will make the problem of eliminating all the unwanted frequencies by filters and/or selective amplifiers alone much more formidable.


Figure 1-218. Balanced modulator circuit, which is useful as a mixer sfage when maximum affenvation of the inpul frequencies in the output is desired

|  | $\begin{aligned} f_{z} & =740 \mathrm{kc} \\ & =30 \mathrm{db} \end{aligned}$ | $\begin{aligned} 2 f_{2} & =1480 \mathrm{kc} \\ & -30 \mathrm{db} \end{aligned}$ | $\begin{gathered} 3 f_{k}=2220 k c \\ -33 d b \end{gathered}$ | $\begin{aligned} 4 f_{2} & =2960 \mathrm{kc} \\ & -58 d b \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \mathrm{f}_{1}=100 \mathrm{kc} \\ -8 \mathrm{db} \end{gathered}$ | $f_{2} \pm f_{1}$ | $2 \mathrm{f}_{2} \pm \mathrm{f}_{1}$ | $3 \mathrm{f}_{2} \pm \mathrm{f}_{1}$ | $4 \mathrm{f}_{2} \pm \mathrm{f}_{1}$ |
|  | $\begin{array}{r} 640 \mathrm{kc} \\ 0 \mathrm{db} \end{array}$ | $\begin{aligned} & 1380 \mathrm{kc} \\ & -37 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2120 \mathrm{kc} \\ & -49 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2860 \mathrm{kc} \\ & -68 \mathrm{db} \end{aligned}$ |
|  | $\begin{array}{r} 840 \mathrm{kc} \\ 0 \mathrm{db} \end{array}$ | $\begin{aligned} & 1580 \mathrm{kc} \\ & -37 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2320 \mathrm{kc} \\ & -49 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 3060 \mathrm{kc} \\ & -68 \mathrm{db} \end{aligned}$ |
| $\begin{gathered} 2 f_{1}=200 \mathrm{kc} \\ -35 \mathrm{db} \end{gathered}$ | $\mathrm{f}_{2} \pm 2 \mathrm{f}_{1}$ | $2 \mathrm{f}_{2} \pm 2 \mathrm{f}_{1}$ | $3 \mathrm{f}_{2} \pm 2 \mathrm{f}_{1}$ | $4 \mathrm{f}_{\mathrm{y}} \pm 2 \mathrm{f}$, |
|  | $\begin{array}{r} 540 \mathrm{kc} \\ -38 \mathrm{db} \end{array}$ | $\begin{aligned} & 1280 \mathrm{kc} \\ & -46 \mathrm{db} \end{aligned}$ | $\begin{aligned} & \hline 2020 \mathrm{kc} \\ & { }_{-69 \mathrm{db}} \end{aligned}$ | $\begin{aligned} & \hline 2760 \mathrm{kc} \\ & -72 \mathrm{db} \end{aligned}$ |
|  | $\begin{array}{r} 940 \mathrm{kc} \\ -38 \mathrm{db} \end{array}$ | $\begin{aligned} & 1680 \mathrm{kc} \\ & -47 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2420 \mathrm{kc} \\ & { }_{-69 \mathrm{db}} \end{aligned}$ | $\begin{aligned} & 3160 \mathrm{kc} \\ & -72 \mathrm{db} \end{aligned}$ |
| $\begin{gathered} 3 f_{1}=300 \mathrm{kc} \\ -42 \mathrm{db} \end{gathered}$ | $\mathrm{f}_{2} \pm 3 \mathrm{f}_{1}$ | $2 \mathrm{f}_{2} \pm 3 \mathrm{f}_{1}$ | $3 \mathrm{f}_{2} \pm 3 \mathrm{f}_{1}$ | $4 \mathrm{f}_{2} \pm 3 \mathrm{f}_{1}$ |
|  | $\begin{array}{r} 440 \mathrm{kc} \\ -65 \mathrm{db} \end{array}$ | $\begin{aligned} & 1180 \mathrm{kc} \\ & -66 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 1920 \mathrm{kc} \\ & -73 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2660 \mathrm{kc} \\ & -78 \mathrm{db} \end{aligned}$ |
|  | $\begin{aligned} & 1040 \mathrm{kc} \\ & -63 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 1780 \mathrm{kc} \\ & -68 \mathrm{db} \end{aligned}$ | $\begin{aligned} & \hline 2520 \mathrm{kc} \\ & -72 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 3260 \mathrm{kc} \\ & -79 \mathrm{db} \end{aligned}$ |
| $\begin{gathered} 4 f_{1}=400 \mathrm{kc} \\ -57 \mathrm{db} \end{gathered}$ | $\mathrm{f}_{2} \pm 4 \mathrm{f}_{1}$ | $2 \mathrm{f}_{2} \pm 4 \mathrm{f}_{1}$ | $3 \mathrm{f}_{2} \pm 4 \mathrm{f}_{1}$ | $4 \mathrm{f}_{2} \pm 4 \mathrm{f}_{1}$ |
|  | $\begin{array}{r} 340 \mathrm{kc} \\ -58 \mathrm{db} \end{array}$ | $\begin{aligned} & 1080 \mathrm{kc} \\ & -70 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 1820 \mathrm{kc} \\ & -77 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2560 \mathrm{kc} \\ & -78 \mathrm{db} \end{aligned}$ |
|  | $\begin{aligned} & 1140 \mathrm{kc} \\ & -60 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 1880 \mathrm{kc} \\ & -72 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 2620 \mathrm{kc} \\ & -77 \mathrm{db} \end{aligned}$ | $\begin{aligned} & 3360 \mathrm{kc} \\ & -78 \mathrm{db} \end{aligned}$ |
| $\begin{gathered} 5 f_{3}=500 \mathrm{kc} \\ -71 \mathrm{db} \end{gathered}$ |  |  |  |  |

Table 1-527(1). Frequencies present in the output of an experimental balanced modulator when the input fundamental frequencies are $100 \mathrm{kc}\left(\mathrm{f}_{1}\right)$ and 740 ke ( $\mathrm{f}_{2}$ ). All output levels in db are given with respect to a 0 -db level assumed for the difference product $\left(f_{2}-f_{1}\right)$ of 640 kc . The modulator was balanced for maximum attenuation of $f_{s}$.

## SELECTION OF INPUT FREQUENCIES FOR SYNTHESIZING STAGE

1-528. Where the output strength of the desired synthesized frequency must be at least 60 db greater than that of any unwanted frequency, it is of utmost importance that none of the unwanted frequencies (that are not already 60 db or more below the desired frequency) in the mixer output approach the frequency of the desired signal. To avoid such a possibility may require a very careful selection of the original frequency elements to be mixed. Assume, for example, that the desired signal is to be the difference product, ( $f_{2}-f_{1}$ ), where $f_{2}$ is greater than $f_{1}$, and that no accompanying frequency is to have a filter or selective amplifier output power greater than - 70 db relative to that of the desired signal. The question arises: What rules-of-thumb can guide the radio engineer in avoiding unwanted frequencies so close to the wanted frequency that they cannot be easily separated by conventional filter circuits? The answer to this question is to avoid all selections of $f_{1}$ and $f_{2}$ that cause the ratio $f_{2} /\left(f_{2}-f_{1}\right)$ to approach any of the values shown in table (1).

How these forbidden ratios have been derived is explained in the following paragraph.

Forbidden Values of $f_{2} /\left(f_{5}-f_{1}\right)$


4
3
$5 / 2$
2
$5 / 3$
$3 / 2$
4/3
$5 / 4$

Note: Insofar as a $70-\mathrm{db}$ separation in power levels is concerned, this table applies only to the use of balancedmodulator mixers adjusted for maximum attenuation of $\mathrm{f}_{2}$. However, the forbidden values should generally be avoided regardless of the type of mixer circuit.

Table 1-528(1). Forbidden values of the ratio $f_{2} /\left(f_{9}-f_{1}\right)$, where $f_{z}$ is greater than $f_{i}$ and the desired frequency, ( $f_{2}-f_{1}$ ), is to be made at least 70 db greater in signal strength than any accompanying frequency.

1-529. The values of the forbidden ratios given in the table of the preceding paragraph were originally derived by H. J. Finden with the aid of the empirical data in table 1-527 (1). The assumption was made that this empirical data for $f_{1}$ of 100 kc and $f_{2}$ of 740 kc could be accepted as generally representative of any values of $f_{1}$ and $f_{2}$, where $f_{2}$

## Section 1

## Crystal Oscillators

is the higher frequency. The manner of derivation of the forbidden values is as follows:
a. First, let us keep in mind that our principal purpose is to avoid the presence of unwanted frequencies that lie close to the desired frequency, which we here assume to be the difference product, $\left(f_{2}-f_{1}\right)$.
b. Let it be assumed that $f_{2}$ is greater than $f_{1}$, but that $f_{1}$ is large enough that $f_{2}$ is at least 5 per cent (or better yet, at least 10 per cent) greater than the difference frequency ( $\mathrm{f}_{2}-\mathrm{f}_{1}$ ).
c. With assurances of at least a 5 per cent difference between $f_{2}$ and ( $f_{2}-f_{1}$ ), and with the modulator specifically balanced to eliminate $f_{2}$ [note the -30 db level of $\mathrm{f}_{2}$ in table 1-527(1)], we can assume that the remaining attenuation of $f_{2}$ can be achieved by elementary filter design.
d. Likewise we can assume that all overtones of $\mathrm{f}_{2}$ ( $2 \mathrm{f}_{2}, 3 \mathrm{f}_{2}$, etc) can be eliminated by elementary filter design, as well as all overtones of ( $f_{2}-f_{1}$ ); i.e. $\left(2 f_{2}-2 f_{1}\right),\left(3 f_{2}-3 f_{1}\right)$, etc.
e. Similarly, we can disregard all sum frequencies, $\left(f_{1}+f_{2}\right),\left(2 f_{1}+f_{2}\right),\left(f_{1}+2 f_{2}\right)$, etc., since all will be more than 10 per cent greater than the desired frequency, $\left(f_{2}-f_{1}\right)$. This group also includes all sums of ( $f_{2}-f_{1}$ ), or its overtones, with other frequencies. For example, $\left(f_{2}-f_{1}\right)+f_{2}$, which is the same as $\left(2 f_{2}-f_{1}\right)$.
f. With the above frequencies eliminated from consideration, the remaining frequencies which might prove troublesome, as indicated in table 1-527 (1), are generalized below in table 1-529 (1).
$g$. We equate each of these frequencies with the desired frequency, ( $f_{2}-f_{1}$ ), and solve for $f_{2}$ in terms of $f_{1}$. These equations are shown below, with the corresponding solutions for $f_{2}$ and for $f_{2}$ / $\left(f_{2}-f_{1}\right)$.
h. Since the numerical values of the ratios derived above correspond to values of $f_{1}$ and $f_{2}$ that produce harmonic products equal to the desired frequency, it can be seen that any close approach to such ratios should be avoided when selecting the input frequencies to a mixer stage.

| $f_{1}$ | $f_{2}-f_{1}$ |  |  |  |
| ---: | :--- | :--- | :--- | :--- |
| $2 f_{1}$ | $f_{2}-2 f_{1}$ |  |  |  |
| $3 f_{1}$ | $f_{2}-3 f_{1}$ | $2 f_{2}-3 f_{1}$ |  |  |
| $4 f_{1}$ | $f_{2}-4 f_{1}$ | $2 f_{2}-4 f_{1}$ | $3 f_{2}-4 f_{1}$ |  |

Table 1-529 (1). Frequencies present in the output of a mixer that can approach in value the desired difference frequency $\left(f_{2}-f_{1}\right)$ and be of a sufficient power level to make elimination by conventional filter circuits difficult.

$$
\begin{array}{rlr}
\text { When } & \text { Then } & \text { And } \\
\mathbf{f}_{2}-\mathbf{f}_{1} & =\mathrm{f}_{1} & \mathbf{f}_{2}=2 \mathrm{f}_{1}
\end{array}
$$

[^7]
## Crystat-Phase-Comtrolled Harmonic Multipliers

1-530. Of great promise in the field of frequency synthesis is the possible future application of harmonic generators of the crystal-phase-controlled type. With such a generator a single low-, medium-, or high-frequency crystal can be used to control a wide band of radio channels extending well into the u-h-f range. The basic circuitry is quite simple. Where maximum economy in parts is necessary, a single triode stage is capable of producing any one of a sequence of crystal overtone frequencies, with the selected signal being 40 db above the level of the two adjacent harmonics. Such a circuit was demonstrated during the first investigations of phase-controlled multipliers reported in the United States. The basic research, reported by Dr. A. Hahnel*, and a developmental project, reported by L. R. Battersby and E. A. Conover $\dagger$, were both undertaken at the Signal Corps Engineering Laboratories at Fort Monmouth, N. J.
1-531. The principal operational features of a crystal-phase-controlled harmonic multiplier are illustrated in figure 1-219. As shown in the block diagram of (A), the basic circuit consists of a variable-frequency oscillator arranged to be keyed at a crystal-controlled rate, $f_{n}$; which, of course, should be a much lower frequency than the v-f-o frequency, $f_{0}$. If the circuit is properly designed, the variable frequency oscillator, when tuned through its band, will generate a succession of

[^8]output frequencies equal to those overtones of the crystal frequency which lie within the v-f-o tuning range. For example, let us suppose that when the variable frequency oscillator is operated in a steady, constant-amplitude state (a steady key-on operation, with the crystal-controlled key shorted across), $f_{0}$ is found to vary continuously from 9990 kc to $20,000 \mathrm{kc}$. Then, when crystal-controlled keying is applied, say, at a frequency, $f_{\text {. }}$ equal to 50 kc , it will be found that all the tuned frequencies are suppressed except those that are harmonics of the $50-\mathrm{kc}$ keying voltage. Thus, with the oscillator tuned to its original 9990 -kc position, the primary output is no longer 9990 kc , but the nearest 50 -ke harmonic, $10,000 \mathrm{kc}$. As the oscillator is tuned through its natural $10,000-\mathrm{kc}$ position, the output at this frequency reaches a maximum. As the oscillator tuning is varied farther in the high-frequency direction, a 10,050 -ke signal begins to increase in amplitude. When the oscillator is tuned to its original $10,025-\mathrm{ke}$ position, the 10,000 -ke and the $10,050-\mathrm{kc}$ signals will appear in the output at approximately equal amplitudes. Finally, when the tuning passes through the oscillator 10,050 -ke maximum position, the 10,000 -ke signal will have dropped to a level 40 db or more below the $10,050-\mathrm{kc}$ output. In such a manner this particular circuit can generate any desired overtone of the crystal frequency between the 200 th and 400 th harmonics- 200 crystal-controlled frequencies in all.
1-532. If all frequencies in the v-f-o output are to be suppressed except the single desired crystalcontrolled harmonic, the output waveform, see figure $1-219(\mathrm{~B})$, must meet certain conditions. First, the rise time must de as short as possible.

(A)
(8)

Figure 1-219. Simplifed block diagram (A) and oulpuf waveform (B) of crystal-phase-controlled harmonic multiplier

This is the time it takes the v-f oscillations to build up to their equilibrium amplitude. Second, the decay time must also be as short as possible. However, the total key-off period must be extended sufficiently to ensure that the oscillations die down to noise-level proportions. This is necessary in order for oscillations at the beginning of each keying pulse to start in the same phase. Third, as implied by the first two conditions, the constant-amplitude time must be long relative to the rest of the keying cycle - three-fourths or more of the total. If these conditions are not met, the output will always contain a multiplicity of different harmonic frequencies at approximately the same amplitude level.
$1-533$. That the operational conditions described above are necessary in order to obtain a singlefrequency output has been confirmed empirically. Such conditions were originally indicated theoretically when the waveform was subjected to a Fourier analysis. Intuitively, from a qualitative examination of the waveform, it would appear that those conditions of maximum constant-amplitude time, which indicate minimum distortion of the output from a pure unmodulated continuous wave, could be expected to be the conditions approaching most closely single-frequency phasecontrolled operation. What may not be qualitatively obvious is why the constant-amplitude portion of the output pulse, which supplies practically all of the output energy, should not cause the dominant frequency to be the actual frequency at which the variable frequency oscillator is tuned to operate. Let us assume that the keying voltage is a square-wave pulse. Since the v-f oscillations must build up from thermal levei, we can assume that they contain no "memory" of the preceding keying pulse or of the pulse rate. In other words, once the oscillator is keyed, the buildup waveform and the constant-amplitude frequency are exactly the same whether the keying pulse is to last 1 microsecond or 1 day. So qualitatively we must conclude that the steady-state oscillations have a period and corresponding frequency that are independent of the keying frequency. The steady-state period of a $v$-f-o cycle during crystal control is thus no different from that of the same tuned circuit without crystal control. How then are we to account for the fact that when crystal control is applied, the measured output frequency immediately shifts from the tuned-circuit resonance value to the nearest harmonic of the crystal irequency? The answer appears to lie in the fact that the generated phase-controlled output physically has the same period and cycle-to-cycie frequency as
the unmodulated tuned oscillator, but because of the periodic phase shift at the crystal frequency, a tuned receiving circuit can indicate a maximum resonance absorption of energy only if it is tuned to a harmonic (approximately) of the periodic phase shift.
1-534. Imagine an ideal phase-controlled waveform in which the build-up time and the decay time are instantaneous, so that the periodic phase shift can also occur instantaneously without the intermission of a key-off interval. In this event, if the $v-f-o$ tuned frequency is exactly equal to a harmonic of the phase-control frequency, no phase adjustment occurs, and the output does not differ in form from a steady-state continuous wave. Now suppose that the $v$-f-o tuned frequency is not a harmonic of the phase-control frequency, and that we attempt to couple electronically the output to a tuned receiving circuit. With the receiving circuit tuned to the v - f -o frequency, we can imagine that during the first phase cycle the received resonance energy builds up to a certain level. To idealize further, let us also imagine that the resistance of the receiver tuned circuit is effectively zero, so that when the first phase cycle is completed, the energy absorbed during that period continues undiminished as a free-running oscillation without a change in phase. During the succeeding phase period a corresponding component of oscillation of equal amplitude but different phase is fed the receiving circuit. After several such periods, in which the phase of each succeeding oscillation component is rotated in the same direction an equal amount from the phase of the preceding component, it can be assumed that the accumulation of opposite-phased oscillations tend to cancel each other (i.e., the tuned circuit returns energy to its power source as fast as it is supplied). Thus, even if the circuit ohmic resistance is zero, a resonance condition cannot be indicated by a continuous buildup of oscillations. On the other hand, if the receiving circuit is tuned to the near harmonic of the phase cycle, we can imagine that the energy absorbed during each phase period continues as a free-running oscillation at the harmonic frequency, $n f_{\text {, }}$. Since there are always exactly $n$ of these cycles during each phase period, the imaginary succession of oscillation components will all have the same phase, and hence will tend to add to each other rather than cancel. Remember that the beginning of each phase cycle does not constitute a phase correction of its harmonic cycle, but of the v -f-o cycles, which we here assume are feeding energy to the semi-free-running harmonictuned receiving circuits. Before the phase of the
input cycle can gradually shift to a point where it is in phase opposition to the hypothetical harmonic oscillations, it is abruptly returned to its starting position and a new phase cycle begins. In this way we can see how the phase-controlled v-f-o oscillations are able to continually feed energy to oscillations that are multiples of the phase-control frequency, and yet tend to suppress oscillations that have the same period as the v-f-o steady-state output. Thus, where the frequencymeasuring technique involves the absorption of energy in a variable circuit of calibrated tuning range, we would conclude that the output frequency of the phase-controlled vfo is apparently a harmonic of the crystal frequency. Similarly, if the phase-controlled frequency were being tested by matching with the phase of an oscilloscope sweep, the sweep would have to be synchronized by the crystal harmonic frequency to hold the pattern still. If synchronized at the v-f-o tuned frequency, the pattern of a single wave will take a hop in phase at the beginning of each phase correction, and thus appear to move across the screen. When synchronized by a crystal harmonic, the wave may begin a change of phase, but immediately jumps back to its original position at the beginning of each phase correction. Again, the phase-controlled harmonic, nf., becomes the measured frequency of the vfo when the measuring technique involves the beat-frequency method, since basically this method measures the unknown frequency by determining the rate at which its phase changes with respect to that of a known standard. Thus, purely from qualitative considerations, we are led to suppose that any conventional frequency-measuring method would indicate that the output of a phase-controlled oscillator has an apparent frequency, $f_{r}$, equal, not to the $v-f-o$ tuned operating frequency, but to $n f_{c}$.
1-535. The reader should accept the qualitative explanation of the principle of phase-controlled multiplication, as given in the foregoing paragraph, as being somewhat on the speculative side. In the practical oscillator, it may be that sufficient coupling can be expected to exist between the v-f-o oscillator and the crystal oscillator to pull them into a mutual synchronization with each other. Certainly, such synchronization is to be expected when the natural v-f-o frequency approaches very closely a harmonic of the crystal fundamental. Also, the explanation given above implies that a tuned receiving circuit, which, perhaps because of periodic clamping or quenching, lacks a sufficient "memory" to store an oscillation above noise level for the duration of the key-
off interval, could not be used by itself to detect a phase-controlled output. If such a circuit were used as a coupling stage, maximum transfer of energy would occur if the stage were tuned to pass the tuned v-f-o frequency rather than the crystal harmonic. Since the discrimination of an effectively low-Q circuit between nearly equal frequencies is negligible in practical circuits, raising the question at this point is academic, except to remind the reader that our qualitative explanation of the phase-controlled signal implies that the value of $f_{s}$ is not independent of the detecting system. On the other hand, the Fourier analysis of the output waveform, leads us to consider the crystal-controlled harmonics as being the actual frequencies of the $v-f-o$ output, inherent in the waveform.

## HAHNEL SPECTRUM GENERATOR

1-536. Figure 1-220 (A) is the schematic diagram of a one-tube spectrum generator of the phasecontrolled v-f-o type developed by Hahnel and associates. Since the v-f-o frequency is several times higher than the crystal frequency, inductors that present very low impedances at the crystal frequency, but high impedances at the $v$-f-o frequencies, can be used to separate the crystal feedback path from that of the variable oscillator, thus permitting a single triode to serve as amplifier for both oscillators. In figure ( $B$ ) is shown the equivalent circuit of the crystal oscillator, which we see is more or less a conventional Miller circuit. In figure ( $C$ ) is shown the equivalent v-f-o circuit, which we see is a Colpitts circuit. This basic spectrum generator is operable at all lower frequencies, but of special interest is the fact that a crystal-controlled output was obtained even in the $u-h-f$ range when an $L_{4} C_{4}$ butterfly circuit tunable from 250 to 900 mc was used.
1-537. As explained earlier, a single-frequency output from the phase-controlled oscillator in figure $1-220$ requires that the constant-amplitude interval of the phase cycle be as long as possible consistent with a sufficient decay time. To achieve this $R_{8}$ must be varied to a value consistent with the resistance of the crystal unit so that the crystal oscillator is biased in the class A region; that is, the tube is cut off (for v-f operation) only a small portion of each crystal cycle. In order to make sure that the decay time is very short, the $\mathrm{f}_{\mathrm{N}}$ tuned circuit should be rather heavily damped, and low ratios of $L / C$ should be used in the tuned circuit. Since these design features will tend to keep the energy storage in the v-f-o system low, they will also serve to shorten the buildup time.


Figure 1-220. (A) Schematic diagram of Hahnel spectrum generator in which two oscillator circuits are combined in one stage; (B) Simplified schematic diagram of the crystal ascillotor circuil of the spectrum generotor; (C) Simplified schematic diagram of the $v$-f-o circull of the spectrum generator

It is also important in this latter respect to use a tube of high transconductance, and to ensure that this transconductance is effective during the con-stant-amplitude interval. Short rise and decay times also require that the crystai keying voltage is changing at a fast rate at the v-f-o on and off points. For this purpose, the amplitude of crystal
oscillation should be as large as practical. Of course, the gridleak resistance will need to be relatively small in order to keep the bias in the class-A region.
1-538. Figure 1-221 shows the complete schematic of a Hahnel circuit foliowed by an amplifier. This circuit was developed by Battersby and Conover and designed to cover the frequency range of 20 to 30 mc in $1-\mathrm{mc}$ steps. With the additional amplifier stage, a $50-\mathrm{db}$ selectivity is obtained for the desired harmonic channel relative to the adjacent channels. An output of 3 volts is possible across a 50 -ohm load. The oscillator circuit is essentially the same as that in figure $1-220$. The amplifier stage is quite conventional. The link coupling to the amplifier is employed to minimize the leakage of the $1-\mathrm{mc}$ signal from the oscillator circuit to the amplifier input. $R_{3}$ serves to shorten the decay time. Its damping effect also improves the tracking performance of the ganged tuning.

## TRANSISTOR OSCILLATORS

Our assignment in transistor oscillators is not to provide detailed mathematical analyses of the various types of circuits, but to describe and discuss semi-quantitatively experimental single-stage circuits that are representative of basic methods for obtaining the loop feedback required to maintain stable oscillations. The basic methods discussed are those that, to obtain feedback, employ series-mode crystal units in the feedback arm, negative-resistance circuitry, and transformer coupling. Modifications of each type of basic circuit are given, but unfortunately the test data available is insufficient to permit defnitive comparisons of the characteristics and limitations of the different circuits. The design engineer, of course, would prefer concrete recommendations in choosing a circuit and in guiding its design to provide optimum characteristics for the particular needs at hand. However, crystal oscillators employing transistors in lieu of vacuum-tube amplifiers are at the present writing still more or less in the trial-and-error experimental stage. Although technical information is being accumulated in a number of laboratories, the detailed test data for the most part represent investments in competitive enterprises unavailabie at this time for public communication. The reader should understand that the particular circuits described are primarily experimental in nature, being given as illustrations of basic oscillator types and not as endorsements for general use.

$\mathbf{R}_{1}=30,000 \mathrm{ahms}$
$C_{t}=112 \mu \mu \mathrm{f}$
$\mathbf{R}_{n}=15,000$ ohms
$C_{3}=10 \mu \mu \mathrm{f}$
$\mathbf{R}_{\mathbf{a}}=2,200 \mathrm{ohms}$
$\mathrm{C}_{4}, \mathrm{C}_{4}, \mathrm{C}_{8}=6-80 \mu \mu \mathrm{f}$
$R_{r}=150 \mathrm{ohms}$
$\mathrm{C}_{48} \mathrm{C}_{7}, \mathrm{C}_{4}, \mathrm{C}_{5}, \mathrm{C}_{59}=.01 \mu \mathrm{f}$
$\mathrm{f}_{\mathrm{e}}=1 \mathrm{mc}$
$\mathrm{L}_{1}=114 \mu \mathrm{~h}$
$\mathrm{~L}_{\mathrm{t}}=37 \mu \mathrm{~h}$
$\mathrm{~L}_{3}, \mathrm{~L}_{4}, \mathrm{~L}_{4}=0.8 \mu \mathrm{f}$
$\mathrm{L}_{\mathrm{m}, \mathrm{a}} \mathrm{L}=0.12 \mu \mathrm{~h}$
$\mathrm{~L}-0.17 \mu \mathrm{~h}$

$$
\begin{aligned}
& \mathrm{L}_{4}=37 \mu \mathrm{~h} \\
& \mathrm{~L}_{3}, \mathrm{~L}_{4}, \mathrm{~L}_{\mathrm{A}}=0.8 \mu \mathrm{f} \\
& \mathrm{~L}_{\mathrm{n},} \mathrm{~L}:=0.12 \mu \mathrm{~h} \\
& \mathrm{~L}-0.17 \mu \mathrm{~h}
\end{aligned}
$$

Figure 1-221. Schematic diagram 20-30-me spectrum generator with filter-amplifier stage added for greater adjacent channal selectivity

## Tremsistor Crystel-Feodbeck Osclliotors

## POINT-CONTACT TRANSISTOR CRYSTAL-FEEDBACK OSCILLATOR

1-539. The circuit parameters indicated are those of an experimental low-frequency oscillator that was investigated at Bell Telephone Laboratories as a possible future replacement of the present vacuum-tube circuits now used to control telephone carrier frequencies. The information given here is based upon a discussion of the experimental oscillator by R. S. Caruthers.
1-540. A point-contact transistor of the 1729 type was used in the experiments. Superior performance characteristics can be obtained with the more recently developed junction transistor. The extrenie simplicity of the basic circuit is possible because the r-f emitter current, $I_{r}$, is in phase with the $r$-f collector current, $I_{\text {r }}$. All that is necessary for the oscillations to be maintained is that a series resonant circuit, which in this case is the seriesmode crystal, feed back a sufficient current to supply I.. The total feed-back current, however, must be somewhat greater than I.. Amplitude equilibrium is reached when

$$
\begin{equation*}
\alpha=1+\frac{\mathrm{R}}{\mathrm{R}_{\mathrm{L}}}+\frac{\mathrm{R}}{\mathrm{r}_{\mathrm{e}}} \tag{1}
\end{equation*}
$$

where $\alpha$ is the effective r-f current amplification
factor of the transistor, equal to $\mathrm{I}_{c} / \mathrm{I}_{w}, \mathrm{R}$ is the crystal resistance, $R_{\text {. }}$ is the load resistance, and $r_{r}$ is a resistance parameter of the transistor collector circuit, somewhat the analogue of $\mathrm{R}_{\mathrm{p}}$ of a vacuum tube. For the point-contact transistor, $r$. is generally between 15,000 and 20,000 ohms, so that the term $R / r$ r. is usually quite small compared with the other terms in the equation. For oscillations to build up, the initial value of a must be greater than that given by equation (1). The larger the difference between the initial a and the equilibrium $\alpha$, the greater is the final activity. In figure 1-223(A), it can be seen that the values of a are not large, so that $R_{L}$ cannot be made much smaller than the maximum permissible R of the crystal unit if equation (1) is to hold for all crystal units of a given type. Limiting occurs when the current peaks of I. extend into the lowamplification regions indicated in figure 1-223(A). The a-c load line in figure 1-223(B) indicates the approximate operating region during oscillations. The point $Q$, which is at the middie of the operating range is predetermined experimentally by adjustments of the d-c supply voltages and the series dropping resistances. Because of the small margin of excess gain in the transistor oscillator, the variations in collector characteristics from one transistor to another result in large percentage variations in oscillator activity. Note the large differences in collector current for the same value of

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Figure 1-222. Basic circuit for crystal-controlled transistor oscillator



I when different transistors are used, as shown in figure 1-223(C). The temperature effects also require consideration. An increase in temperature causes $R_{r}$ to become lower. In the case of "lowactivity" transistors, this effect can easily be sufficient to stop oscillations.
1-541. The frequency stability and sine-wave output of the transistor oscillator can be comparable to that of vacuum-tube uscillators. The oscillator in figure 1-222 was able to supply as much as 30 mw to the load at a frequency of 184 kc . It was found that 0.8 watt less power was required to operate a transistor oscillator and amplifier than is required for an equivalent vacuum-tube circuit, and at least a 50 -per cent greater saving should be possible. The consequent reduction in compartment heating, as well as in requirements of weight, space, etc, can be quite advantageous in small, compact units where several power-dissipating elements are packed closely together.

## JUNCTION TRANSISTOR

 CRYSTAL-FEEDBACK OSCILLATOR1-542. The basic collector-to-emitter crystal feedback circuit shown in figure 1-222 requires a current amplification greater than unity, and therefore is restricted to transistors of the point-contact type and to frequencies generally under 500 kc . When a crystal-feedback oscillator is desired using a junction transistor, or using a point-contact transistor at a frequency too high for alpha to be greater than unity, modifications must be introduced in order to obtain the required current amplification. Perhaps the simplest solution is to employ a voltage-step-down (current-step-up) transformer. However, to simplify the discussion we shall treat the transformer-coupled transistor oscillator in a separate category. A more direct solution, and one that affords a more dependable oscillator insofar as the elimination of freerunning oscillations is concerned, is to exploit the current amplifying characteristic of the paralleltuned circuit. One branch of a tuned tank with a series-mode crystal inserted can be used as a feedback circuit. One such circuit, where the collector output operates into the tuned tank, is shown in figure 1-224. This circuit was designed and tested during a Signal Corps research project* directed by B. J. Dasher at the Georgia Institute of Technology. A simplified schematic illustrating the

[^9]necessary loop gain and loop phase conditions for oscillation is shown in figure 1-225. Assuming that the r-f emitter-to-base input impedance of the transistor is small compared with the external 10 -kilohm shunting resistance, it can be seen that the feedback current ( $\mathrm{I}_{\mathrm{i}} / \theta$ ) through the crystal and the tank tuning capacitor must be approximately equal to $I_{n}$, the r-f emitter current, whose phase is taken as the zero reference. The exact phase conditions depend upon the alpha characteristics of the transistor.

1-543. Figure $1-226$ shows the alpha characteristics versus frequency of a typical CK-720 junction transistor as measured by Dasher et al at the Georgia Institute of Technology. Note the large lag ( $\phi$ ) in the phase of $I_{c}$ with respect to $I_{\text {. as }}$ the frequency is increased. Alpha is the current gain under external collector-to-base short-circuit conditions. Its value is dependent upon the frequency but is otherwise independent of the particular circuit external to the transistor. The collector circuit shown in figure $1-225$ is, of course, not a short circuit, but is assumed to have an impedance very small compared with the internal collector-to-base impedance of the transistor, so that to a first approximation the phase of the operating $I_{\text {. }}$ is equal to the phase, $\phi$, of the shortcircuit alpha. The phase lag, $\phi$, is due to the transit time of the transistor current carriers. It can be seen that if $I_{i} \angle \theta$ of the feedback arm of the collector tank in figure $1-225$ is to have the same phase as $I_{*} \quad \theta^{\circ}(\theta=0)$, how nearly the tank is to be tuned to parallel resonance and whether the tuning is above or below resonance depend upon the phase of $\phi$, and that this in turn depends upon the frequency. At frequencies in the neighborhood of 400 kc , $\phi$ has a value of approximately $80^{\circ}$. If it can be assumed that the reactance of the capacitor in the feedback arm is sufficient to cause the feedback current to lead the tank voltage by $80^{\circ}$, then $\theta \approx 0$ when the tank is operated at resonance. At small values of $\phi$ (at low frequencies), the tank circuit tuning must deviate considerably from the parallel resonant condition in order for $\theta$ to equal zero. At very large values of $\phi$ the loop phase relations approach the 180-degree inversion characteristic of vacuum-tube oscillators, with the circuit in figure 1-224 assuming certain similarities to a Pierce circuit. Since the magnitude of alpha becomes very small as $\phi$ becomes large, it may be necessary to introduce additional phase-shifting elements in order to ensure that the tank is operated sufficiently close to resonance. (Actually, the practical solution would be to employ a transistor

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Figure 1-224. Junction fransisfor crysfal-feedhack oscillator


Figure 1-225. Simplified equivalent circuit of junction transisfor crystal-feedback oscillator, showing tuned tank in collector sircuit for obtaining desired current amplification and loop phase shilt for feedback to emitter input. For stable oscillations to be maintained
especially fabricated for use at higher frequencies, as is discussed in the following paragraph.) The value of $L$ in figure $1-224$ is purposely made large so that the tank $Q$ is sufficient to permit the necessary current amplification over as wide a tuning range as is possible. With the crystal shorted out, the circuit was found to oscillate in a free-running state at frequencies as high as 2 me, which is several times the alpha cutoff frequency. (The alpha cut off frequency is that frequency at which the short-circuit current gain is 3 db below the d-c value of alpha.) With a crystal inserted, the upper frequency limit depends upon the crystal's effective resonance resistance. But the upper dependable frequency when employing Military Standard crystal units having element C or D characteristics appears to lie between 300 and 400 kc. Frequency Control Branch engineers of the Fort Monmouth Signal Corps Engineering Laboratories do not recommend this type of oscillator for general use because the operating stability is critically dependent upon the stability of alpha, whose phase and magnitude can be quite difficult to maintain constant under variations of temperature and voltage. Nevertheless, the progressive development of $h-f$ and $v-h-f$ transistors of ever closer tolerances are rapidly


Figure 1-226. Typical alpha characteristics versus frequency of a type CK-720 junction transisfor


Figure 1-227. High-frequency transisfor oscillator
increasing the frequency range over which junction transistor oscillators of ail types can be operated below alpha cutoff-in which region unstable transit time effects are less pronounced. For example, a modification of the circuit shown in figure 1-227 (a type that employs a paralleltuned circuit for amplification of the feedback current), without crystal control, is already in commercial use. For a modified version of the oscillator in figure $1-224$ designed to provide maximum frequency stability, see paragraph 1-555.

## H-F TRANSISTOR OSCILLATORS

1-544. The comparatively long transit time of the transistor has been a great handicap in applying the semiconductor amplifier in h-f and v-h-f circuits. Although it is quite possible to demonstrate that transistors can operate satisfactorily in h-f
crystal oscillators, it is quite difficult to guarantee that such circuits will operate dependably when the demonstration transistors and crystal units are replaced by others of the same nominal characteristics, unless close tolerances are assured. One of the few types of transistors for h-f and v-h-f application that is commercially available at the time of this writing is the Philco Surface Barrier transistor, SB-100, which is basically a special type of pnp junction transistor designed for low-power, wide-band, h-f applications. Its unique fabrication process permits an aboveaverage degree of uniformity in its low-power, h-f operating characteristics. The maximum dependable oscillation frequency of the SB-100 is rated at 30 mc . This is the highest frequency at which any randornly selected transistor of this type can be expecied to show a power gain of at least unity. The highest frequency at which the average SB-100 transistor can be expected to show a power gain of unity is 45 mc . With selected SB-100 transistors, oscillators at limit frequencies of 70 mc are possible. If these transistors are to be employed as amplifiers in oscillator circuits at frequencies above 20 mc , the design engineer should specify closer tolerances than those described for randomly selected units. Figure 1-227 shows an oscillator çircuit designed for operation in the $20-30-\mathrm{mc}$ range. This oscillator will operate as a free-running circuit at its tuned frequency if the crystal is shorted across. The ratio of the useful oscillator output to the power supplied from the SE-100 collector voltage supply is given by the empirical equation

$$
\text { collector efficiency }=0.8 \log _{10} \frac{f_{\text {max }}}{f} \% 1-544(1)
$$

where $f_{\text {max }}$ is the highest frequency at which the oscillator in figure $1-227$ will oscillate (the frequency at which the circuit power gain is unity at starting amplitudes) and $f$ is the operating frequency. Equation (1) assumes that the losses in the crystal unit are negligible; otherwise these losses should be interpreted as part of the "useful" oscillator output.

## Negotive-Resistance Transistor Oscillators

1-545. Although the driving element of any electronic oscillator can be described as a negativeresistance circuit, it is not customary to classify the oscillator, itself, as being of the negativeresistance type unless the negative resistance is an inherent $d$-c, as well as an a-c, characteristic of the driving element. Among negative-resistance vacuum-tube oscillators, the transitron circuit is an example. Among transistor oscillators, the series-tuned-emitter circuit, such as that shown in figure $1-228$, is an example.

1-546. A negative-resistance characteristic can be obtained between any two terminals of a pointcontact transistor by allowing the amplified current to flow through a feedback resistance of such magnitude that the feedback voltage produced is more than sufficient to compensate for any change in the input voltage. Alpha must be greater than one, so that the negative-resistance circuit is not applicable for a single-stage junction type of transistor, nor, for that matter, for a point-contact transistor except at the lower frequencies. The negative-resistance characteristics of the emitter input in a common-base circuít, such as that shown in figure 1-228, is generally superior to a tuned-collector negative-resistance


Figure 1-228. Tuned-omitter negative-resistance circuit. Essential teatures are that alpha be greater than unity, the insertion of an exfernal resistance, $h_{b}$, in the common-base circuit to increase the collector-to-emifter energy feedback; and for oscillations to build up, the effective positive resistance, $\mathrm{R}_{\mathrm{e}}$, of the tuned-emitter circuit must be less, numerically, than the negative resistance, af the emitter input
mode of operation insofar as osciliator stability is concerned. Figure 1-229 shows a typical emitter-to-base characteristic curve for the circuit in figure $1-228$, where the emitter voltage is plotted as a function of emitter current. The slope of this curve equals the dynamic resistance of the input. (By "dynamic resistance" we mean the instantaneous resistance, $\mathrm{dv}_{\mathrm{e}} / \mathrm{di}_{\mathrm{e}}$, for an infinitesimal change in voltage and current at any given point on the curve, as opposed to the "static resistance," equal to $v_{e} / i_{e}$, the total voltage divided by the total current at any given point on the curve.) The negative slope between points $A$ and $B$ represents the negative-resistance zone of the emitter circuit. If the tuned circuit shown in figure $1-228$ is connected to the emitter input and the rheostat is adjusted so that the transistor is biased to operate at point 0 on the $v_{e}-i_{e}$ curve, oscillations at the resonance frequency of the emitter LC circuit will build up provided that the magnitude of the positive resistance, $R_{e}$, of the external circuit connected between terminals 1 and 2 is less than that of the negative resistance presented by the transistor at the same terminals. As oscillations about point 0 build up, the positive peaks of $I_{p}$ swing toward the positive-going slope region at the bend of the curve, so that the effective negative dynamic resistance decreases, and amplitude limiting is achieved. Constantamplitude oscillations are reached when the effective dynamic impedance looking into the emitter-base terminals is exactly equal and opposite in sign to the impedance of the external


Figure 1-229. Typical point-contact emitter voltage curve plotted as a function of the emiffer current when the transisfor is common-base connected and the voltage is measured to include the additional feedback voltage developed across an external base fesistance, $R_{b}$, as indicated in figure 1-228. The current scale is greatly amplified to the teft of point $A$. The slope of the curve equals the dynamic input resistance. The negative-resistance region thus lies along the negative slope between points $A$ and $B$
emitter-base circuit as faced by the input terminals, 1 and 2. If we assume that the biascontrol resistance can be neglected and that the current and voltage at the fundamental frequency are approximately in phase, then we can say that the condition for stable oscillations is that

$$
\begin{equation*}
\mathrm{R}+\rho \approx \mathbf{R}_{\mathrm{e}}+\rho=0 \tag{1}
\end{equation*}
$$

1-547. Figure $1-230$ shows the values obtained for $\rho$ for a particular 1768 type transistor when the externally connected resistors $R_{b}$ and $R_{r}$ are 800 ohms and 2700 ohms, respectively. The emitter bias current is constant. The horizontal scale represents the rms a-c value of the emitter current. Since the magnitudes of $\beta$ and $\mathrm{R}_{e}$ are equal after oscillation equilibrium is reached, it can be seen that the curves in figure $1-230$ can be used to predict the limiting amplitude of oscillation as the external emitter-to-base resistance $R_{\rho}(=-\rho)$ is varied. The curves indicate that if a lowfrequency series-mode crystal is connected across the transistor input, oscillations can be expected to build up as long as the resonance resistance of the crystal unit is not greater than a few hundred ohms. Not many types of low-frequency Military Standard quartz crystal units have such small values of resonance resistance. Exceptions are the precision G-element crystal units CR-39/U and


Note: The Western Electric type transintor shown above and the one following are experionental prototypes whose production has been discontinued. Similar electrical characteristics can be obtained by using Western Electrio transistor types 2N21, 2N110, and GA-52897, which are commercially available, but solely for the use of the V.S. Armed Services and their contractors.
Figure 1-230. Negative input resistance of the circuit shown in figure 1-228, plotted as a function of the a-c component of the emitter current for three representative values of collector-fo-base d-c voltage. The emitter is biased al approximately point 0 as shown in figure 1-229. Measurements were made by Dasher, Finn, and Jones at the Georgia Institute of Technology

CR-40/U, which have maximum effective resonance resistances of 150 ohms in the $160-250-\mathrm{kc}$ range and of 600 ohms in the $250-330$-kc range. The resistance deviations of these crystal units are rated at not greater than 33 per cent of the maximum permissible values-that is, maximum deviations of 50 ohms and 200 ohms, respectively, for the $160-250-\mathrm{ke}$ range and the $250-330$-kc range. No data is available concerning their performance in negative-resistance transistor circuits, but from the curves of figure 1-230 wide variations in the amplitude must be expected when replacing one crystal unit with another unless special steps are taken to control the gain of the transistor circuit. Whereas a 33 per cent change in crystal resistance can generally be considered negligible in the average vacuum-tube oscillator, this much resistance deviation in the negative-resistance tuned-emitter oscillator can cause a proportionally much larger percentage change in the output amplitude.
1-548. Figure $1-231$ is a schematic diagram of the equivalent a-c circuit of the tuned-emitter circuit. The parameters $r_{b}, r_{c}$, and $r_{e}$ represent the impedances of the equivalent $T$ network of the transistor at low frequencies and small amplitudes, conditions under which the equivalent impedances can be assumed to be approximately linear and purely resistive. The amplifying properties are represented by the constant-current generator, $\alpha I_{\text {e }}$. In analyzing this circuit two equations suffice for defining the state of operation at oscillation equilibrium. Following the analysis developed by B. J. Dasher et al in Transistor Oscillators of Extended Frequency Range, we find that one equation can equate the over-all voltage drop around the emitter-base loop to zero; the


Figure 1-231. Equivalent a-c circuit of tuned-emitter negative-resistance oscillator. For crystal control, $L$, $C$, and $R_{e}$ can be inferpreted as being the series-arm parameters of a crystal unif
second equation can equate the over-all voltage drop around the collector-base loop to zero. On combining these equations and separating the real and complex parts, two additional equations are obtained. The complex part gives the loop phase requirement, which serves to determine the frequency:

$$
f=\frac{1}{2 \pi \sqrt{\omega c}}
$$

(That the complex part would reduce to the form shown in equation (1) could virtually have been predicted simply from a qualitative inspection of the circuit.) The real part gives the loop gain requirements and can be expressed as an equilibrium equation for alpha:

$$
\begin{gather*}
a=\left(\frac{r_{b}+R_{b}+r_{e}+R_{e}}{r_{b}+R_{b}}\right)\left(\frac{r_{r}+R_{r}}{\mathbf{r}_{r}}\right)  \tag{2}\\
+\frac{r_{e}+R_{e}}{\mathbf{r}_{r}}
\end{gather*}
$$

If we assume that $r_{\text {s }}$ is much greater than all of the other resistance parameters, equation (2) can be reduced to the approximate equation

$$
\alpha \approx \text { but }>\frac{r_{b}+R_{b}+r_{\mathrm{e}}+R_{c}}{r_{\mathrm{b}}+R_{\mathrm{h}}}
$$

Note that equation (3) requires that the transistor current gain at equilibrium be slightly greater than the ratio of the total resistance of the emit-ter-base loop to the total feedback resistance of the base as illustrated in figure 1-231. The reader should not confuse $r_{e}, r_{1,}$, or any of the other positive resistance values in figure 1-231 with the effective negative resistance of the input circuit. The equivalent effect of the negative-resistance characteristic is provided by the current generator. 1-549. If desired, the operating voltages of the base-feedback point-contact transistor can be so adjusted that the negative resistance appears in the collector rather than in the emitter circuit, and oscillations can be controlled by connecting a series-mode crystal in the collector circuit. The equivalent tuned-collector circuit is shown in figure 1-232(A). A sample collector-controlled circuit which was tested at 50 kc is shown in figure 1-232(B)*. This circuit, as reported by B. J. Dasher, exhibited a negative resistance sufficient to drive a 40,000 -ohm crystal unit. Al-

[^10]

Figure 1-232. (A) Equivalent a-c circuit of tuned-collector negative-resistance oscillator. For crysfal control, L, C, and $R_{r}$ can be interpreted as being the series-arm parameters of a crystal unit; (B) Crystal-coutrolled tunedcollector negative-resistance oscillator. The parallel tuned tank is inserted in the base circuit in lieu of a resisfor in order to cbiain negalive resistance values in excess of $\mathbf{4 0 , 0 0 0}$ ohms
though negative resistance values of 50 kilohms are possible at d-c potentials, these values drop rapidly with increasing frequency, and may be only a few hundred ohms at 100 kc . The tunedcollector (and collector-controlled) circuit is governed by exactly the same loop equations that apply in the case of the tuned-emitter (and emitter-controlled) circuit, which are given in the preceding paragraph (equations $1-548$ (1) and (2)). However, the degradation of the crystal Q in the collector-controlled circuit is generally greater than in the emitter-controlled circuit, so that the latter permits the higher frequency stability. Because the tolerances required for good stability are difficult to obtain with pointcontact transistors neither circuit, to Signal Corps knowledge, has been developed to the point that it could be recommended for general use.

## Transisfor Oscilletors Using Parallel-Mode or High-Impedance Series-Mode Crystal Units

1-550. Since transistor negative-resistance oscillators require values of alpha greater than unity, they are generally limited to frequencies less than 500 kc . The negative-resistance circuits previously discussed place the crystal directly across the negative-resistance terminals. Yet at low operating frequencies it is difficult to fabricate crystal units having resonance resistances of magnitudes small enough to permit oscillations to start. For this reason, it may be more practical to connect the crystal unit across a high-impedance pair of point-contact transistor terminals and to insert a series-resonant LC circuit, or other low impedance, across the low-impedance negative-
resistance terminals. Such a circuit will not exhibit (to the crystal circuit) the negativeresistance characteristic under d-c conditionsonly in the neighborhood of the crystal fre-quency-and so is not conventionally classified as a negative-resistance oscillator. However, the operating principle is the same. Six oscillators of the high-impedance type are shown in figure 1-233. All the circuits shown (but not including the crystal load capacitances indicated by dotted lines) are the inventions of Everett Eberhard and Richard Endres of RCA, U. S. Patent 2,570,436. A common feature of these oscillators is that the bias currents are so selected that the electrode to which the piezoelectric crystal is connected is made to present a high dynamic impedance, to match the high impedance expected of the crystal unit. A resonant LC circuit is connected to another electrode of the transistor, the tuned LC resonant frequency being approximately equal to the crystal frequency. Each circuit is designed to provide positive feedback. sufficient to maintain oscillations. A high impedance can be obtained at the crystal-connected electrode of the transistor by adjustment of the bias current at any one of the three electrodes. Figure 1-233 (G) shows typical curves of the resistance that would be faced by the crystal unit between each terminal and ground as a function of the collector bias current, $i_{\text {r }}$. In circuits (A), (B), (C), and (D) of figure 1-233, where either the base or the collector impedance must match that of the crystal unit, the transistor is operated near point $a$ on the $i_{c}$ scale. In circuits ( $E$ ) and (F) of figure 1-233, where the emitter input


Figure 1-233. (A) to (f) Transistor oscillator circuits designed for high-impedance crysfal control; (G) Variation of equivalent network resistances of point-contact transistor as a function of collector current. Point A is the highimpedance region of the base and collector electrodes, and point $B$ that of the emitter electrode, $r_{b}, r_{c}$, and $r_{c}$ are not drawn to the same scale
impedance must be high, $i_{c}$ is adjusted to a value near point $b$ in figure 1-233 (G). In all the circuits of figure 1-233, the collector is operated with a relatively large reverse bias, and the emitter with a relatively small forward bias.
1-551. The exact operating point of the crystal unit in the Eberhard-Endres oscillators is not specified in the patent claims. The inference is that the crystal unit is operated near antires-
onance, since it is assumed to be a high-impedance element. However, the resonance resistance of v-l-f crystal units may well be greater than $100,000 \mathrm{ohms}$, and even the resonance resistance of an m-f crystal may be several kilohms; hence, it appears that at the low frequencies at which the point-contact transistor oscillators normally operate, the crystal units in the circuits of figure 1-233 are not restricted to a particular mode of

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resonance, but operate near series resonance as long as they show a sufficiently high impedance. If it can be assumed that the crystal unit and each of the tuned circuits are operating approximately as pure resistances, the gain requirements for sustained oscillations, except in circuit (D) which has an additional feedback element, are the same as those given by equation 1-548 (2) for the negative-resistance oscillators. This can be seen intuitively by noting that all the circuits obtain their necessary positive feedback by virtue of a high-impedance common-base circuit. In circuits (A) and (B) of figure $1-233$, the impedance of the crystal unit can be taken as the approximate value of $R_{b}$ in equation 1-548 (2). Since $R_{b}$ can assume a resonance or an antiresonance value, either of which could conceivably satisfy the loop gain equation, it would appear that these two circuits might have tendencies to jump frequencies. No experimental evidence is available, but very possibly the dependability of such oscillators could be improved by employing parallel-mode crystal units directly shunted by suitable load capacitances, as indicated by the dotted-line connections. In practice, a proper selection of the reactive elements in each circuit, such as the r-f choke across the crystal unit, may well be entirely sufficient to ensure that a highimpedance crystal will operate at resonance rather than at antiresonance. In circuits (C) to (F) of figure 1-233 maximum feedback occurs when the crystal resistance is a minimum, so that only the series-resonance mode of the crystal unit need be considered. In other words, the loop gain conditions could not be satisfied with practical values of alpha if the extremely high antiresonance impedances of a low-frequency crystal unit were substituted for the values of $R_{e}$ or $R_{e}$ in equation 1-548 (2). Nevertheless, it is conceivable that a parallel-mode crystal unit, shunted by its rated load capacitance, could also be applicable in these circuits if desired. For a given set of operating roltages and circuit parameters, however, only one mode of crystal operation can sustain stable oscillations. Whether the stable mode is series or parallel depends upon whether the limiting action is current- or voltage-controlled, respectively. (See paragraph 1-590.) An output from any of the circuits in figure 1-233 can be obtained at any of the transistor electrodes. Where maximum sine-wave purity in the output is desired, the circuit parameters should be selected so that the equilibrium value of alpha is only slightly less than the starting value of alpha, so that the amplitude remains as small as possible. Also, the
output harmonic content is greatly reduced if the output is taken from a parallel-tuned circuit having a small $L / C$ ratio, as is done in circuits (C), (D), and (E). In circuit (D), additional feedback is obtained by the insertion of $R_{r}$, which may have any value from zero on up. For optimum operation the d-c resistance of the r-f choke in the emitter circuit should be less than $\mathrm{R}_{1}$. Circuit (D) can be considered a transistor equivalent of a crystal-controlled Hartley oscillator by viewing the emitter, collector, and base as the cathode, plate, and grid, respectively, of the vacuum tube in the Hartley circuit. Note in circuit (F) that the emitter bias battery is shown with its polarity in the reverse direction. This does not mean that the emitter is operated with reverse bias, but simply that the large forward bias provided by the d-c voltage drop across $R_{b}$ must be partially cancelled to obtain the proper operating bias.

## Transformer-Coupled Transistor Oscillators

1-552. Figure 1-234 shows schematic diagrams for three experimental transformer-coupled transistor oscillators designed and tested by Dasher, Jones, and Witt at the Georgia Institute of Technology. The average frequency deviation of each of the three circuits for variations in the power supply is given below in table 1-552 (1).
1-553. An elementary transformer-coupled circuit is shown in figure $1-234$ (A). Circuit (B) is a modified version of (A) that was found empirically to provide better frequency stability during changes in the applied voltage. The turns ratio of the transformers in circuits (A) and (B) are not specified, but presumably the ratios are $1: 1$. The transistor used is a point-contact type with an alpha greater than unity at the operating frequency of 50 kc . Circuit (C) is a 400 -kc oscillator

| Cirouit | Frequency Deviation <br> (Parts Per Million Per <br> 1 Per Cent Change in Voltage) | Bias Variable | Bias <br> Constant |
| :---: | :---: | :---: | :---: |
| (A) | 1.2 | $\mathrm{E}_{\mathrm{c}}$ | $i_{\text {i }}$ |
| (A) | 0.7 | $\mathrm{E}_{\text {e }}$ | $i_{\text {c }}$ |
| (B) | 0.25 to 0.8 | $\mathrm{E}_{\text {c }}$ |  |
| (C) | 0.0013* | $\mathbf{E F}_{\text {c }}$ |  |

Table 1-552 (1). Frequency stability data for circuits shown in figure 1-234.

[^11]that can be adjusted to provide excellent frequency stability against changes in the supply voltage. Also, by the proper adjustment of the variable capacitor $C$, the current through the shunt capacitance of the crystal unit can be effectively cancelled insofar as the transistor input is concerned. The circuit is effectively a capaci-tance-bridge oscillator in which all the transformer feedback signals are annulled in the input circuit except those that pass through the series arm of the crystal unit, which of course is effectively an open circuit except at resonance. The


Figure 1-234. Transformer-coupled transistor oscillators
principal adjustment for minimizing the deviation in frequency during fluctuations in the voltage supply is that of the base resistance, $\mathrm{R}_{\mathrm{b}}$. For each crystal unit and transistor a particular value of $R_{b}$ will provide maximum frequency stability. The reason for this appears to be due to the compensating influences of simultaneous changes in emitter and collector bias currents. See paragraph 1-555 for a more detailed discussion of this bias compensation effect.
1-554. Each of the circuits shown in figure 1-234 exhibits a fair, but not exceptional, frequency stability under changes in temperature, with circuits (B) and (C) being somewhat the superior in this respect. The transformer-coupled transistor oscillators are generally less frequency stable under changes in temperature than are the resistive transistor circuits. An additional disadvantage is that the transformer-coupled circuit has greater-than-average tendencies to break into free-running oscillations, particularly if the shunt capacitance of the crystal unit is large. On the other hand, an important advantage of the transformer coupling is the increase possible in feedback gain. This makes it possible to operate at lower voltages, at higher frequencies, with junction transistors, and generally with smaller values of alpha than otherwise.

## Frequency Sinbilization In Transistor Oscillators By Bias Compensation

1-555. Figure 1-235 shows the frequency characteristics of the oscillator in figure 1-224 when the collector and emitter voltages are varied. Note that where an increase in collector voltage causes an increase in frequency, an increase in the emitter voltage causes a decrease in frequency. This property of the circuit suggested to its designers that by a proper choice of emitter and collector voltages the circuit could be fre-quency-stabilized against fluctuations in the voltage source. From figure 1-235 it can kw seen that if the emitter voltage is to vary linearly with the collector voltage, the voltage-compensating circuit must operate in a region where the intersections of the emitter voltage curves with the horizontal constant-frequency lines are evenly spaced. A circuit designed for this mode of operation is shown in figure $1-236$. Figure $1-237$ shows the fre-quency-voltage characteristics of the compensated circuit for two values of the resistance R. Note that this mode of operation is a transistor analogue of the "class D" mode of operation described for vacuum-tube oscillators in paragraphs 1-298 and 1-342.

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Figure ;-235. Deviation of frequency with the collecfor supply voltage for various values of emitter supply voltage. Tesf oscillator circuit is the same as that shown in fgure 1-224

1-556. The adjustment of the frequency-stabilized oscillator depends upon the resistance of the crystal unit. A circuit adjusted for maximum stability with one crystal unit may be relatively unstable when a replacement crystal of the same type and nominal frequency, but of different resistance, is inserted. This might be expected, since the resistance of the crystal affects the amplitude of oscillations as well as the phase-shifting $Q$ of the feedback circuit. A complete theoretical analysis of the relations among the stability parameters has not been attempted, and no doubt would prove quite complex. But one of the more important factors affecting the frequency stability is the harmonic content of the oscillations. Any change in the wave distortion, such as would occur with a change in amplitude due to a change in crystal resistance, would be sufficient to shift the fundamental frequency (see paragraph 1-596) to a point where the circuit may no longer be self-compensating.
1-557. Figure 1-238 shows a simple feedback oscillator tested by Dasher and Witt at the Georgia Institute of Technology. The values of the parameters were selected to provide maximum frequency stability for a particular transistor and crystal unit. Figure 1-239 shows how the frequency of this oscillator changed with a 20 -volt change in supply voltage. That a number of crystal units having approximately the same resistance caused different effects in the frequency


Figure 1-236. Frequency-siabilized circuit for single battery supply


Figure 1-237. Deviation of frequency with changes in supply voltage for two values of $R$ in circuit shown in figure 1-236


Figure 1-238. Crystal-feedback oscillator in which the resistance parameters have been selected empirically to provide maximum frequency stabilixation for the particular 400-ke crystal unit and point-contact transisfor being used


Figure 1-239. Frequency deviation of circuit shown in figure $\mathbf{1 - 2 3 8}$ for a given change in supply volfage af various valjes of crystal resisfance


Figure 1-240. Modification of the crystal-feedback oscillator of figure 1-238 to provide greater frequency stability by providing greater amplitude tability with diode clipping


Figure 1-241. Volloge waveform affer clipping of both peaks by diode rectifiers
stability apparently is due to differences in crystal resonance frequency, shunt capacitance, and L/C ratios from one crystal to the next. By different adjustments of the circuit resistances, it was nevertheless possible to obtain a maximumstability point for each crystal.

## Transistor Oscillators of Stabilized Harmonic Content

1-558. As explained in paragraphs 1-596 to 1-598, a distorted waveform tends to lower the fundamental frequency of an oscillator. Since the distortion is normally due to the nonlinear amplitudelimiting parameters, any change in the other resistance losses of the circuit will cause the amplitude to change, and hence the amount of distortion to change. For, example, if the resistance of the crystal unit decreases in the oscillator in figure 1-238, the feedback increases and the transistor will be operated farther into the bend of its volt-ampere input curve. This means greater distortion and harmonic content, and hence a shift to a lower fundamental frequency, where the stability characteristics of the circuit will probably be changed. To reduce this change in circuit performance when replacing transistors or crystal units, the double-diode clipping modification shown in figure $1-240$ has been designed and tested by Dasher and Witt. The diodes clip both peaks of the oscillator output as indicated in figure 1-241, and thus, as long as the amplitude is sufficiently high, the distortion of the waveform remains relatively constant. The circuit requires an alpha of at least 2 in order to oscillate. Generally, what changes that do occur in the frequency stability are more significant when a crystal unit is replaced than when a transistor is replaced. Although the unadjusted performance of the circuit is inferior to the performance of the circuit in figure 1-238 when the latter is adjusted for a particular transistor and crystal
unit, the diode clipping does provide superior frequency and amplitude stability as compared with the average performance of the unclipped circuit when the latter is adjusted only for optimum performance with an average crystal unit. The measured frequency deviations of the diodeclipped circuit for 10 different crystal units ranged from 0.1 to 0.05 parts per million per 1 per cent change in voltage.
1-559. Where maximum ampitude and frequency stability is desired to be relatively independent of the particular transistor and crystal unit, it may be necessary to operate the transistor on the straight portions of its characteristic curves and to obtain the limiting from slowly responding devices such as thermistors or a-g-c circuits. Such methods permit the oscillator to operate with approximately linear rather than harmonicallyvarying circuit parameters and do not require distortion for limiting. Nevertheless, these methods involve the introduction of additional components that usually deprive the transistor circuit of its principal advantages of compactness and low power and hence should be avoided if possible.

## PACKAGED CRYSTAL OSCILLATORS

1-560. The great strides made in the field of electronics during the past two decades have so rapidly multiplied the diversity and complexity of electronic applications in commercial and military equipments that the problem of adequate maintenance has become a major national concern. One aspect of the problem has been the steadily growing trend to eliminate maintenance on a part-by-part basis; that is, to eliminate the timeconsuming type of trouble-shooting that traces a faulty system to the exact defective part, such as to a particular resistor or capacitor. For this purpose it is necessary that electronic equipments be designed as an assemblage of packaged units, in which each unit can be as readily removed, tested, and replaced as is now possible in the case of vacuum tubes. This cannot be achieved unless the circuit being separately packaged actually operates as a functional unit. It is also paramount that the packaged unit be standardized; otherwise, by definition, there can be no standard nor rated tolerances by which the unit can be tested. The standardization is equally important as a means to encourage production of commercially available packaged units of known operational characteristics, so that design engineers can concentrate more of their attention upon new system design and application instead
of repeatedly retracing the basic circuit problems for each new equipment. In the special field of aircraft and guided-missile equipment, an additional requirement of the packaged unit is that, as much as possible, it be miniaturized. As a consequence of these factors, the crystal industry is faced with a growing demand for standardized, miniature packaged crystal oscillators-each of which can be treated simply as a black box, so that when plugged into a circuit connecting to a specified power supply and output impedance, it will supply a radio-frequency signal of a given nominal frequency, purity, and power level within specified tolerances.
1-561. The standardized packaged oscillator is still in the developmental stage. Indeed, it is probably more accurate to say that it is still in the stage of basic research, insofar as the standardization is concerned. Here and there one may find an oscillator fabricated as a packaged unit which has been designed for use in a particular equipment, but with one or two exceptions (see paragraphs 1-571 and 1-572), packaged crystal oscillators are not generally available in the commercial market as standard components for gen-eral-purpose applications. Current research in the field of packaged crystal oscillator standardization has primarily been spurred by USAF Wright Air Development Center, in large part due to the urging and initiative of E. H. Borgelt of the Frequency Control Group, and an initial investigatory stage has been centered at the Illinois Institute of Technology Armour Research Foundation. When eventually packaged oscillators are fully available, we can expect that the interests of radio equipment designers will be more attracted to the problems of designing systems around standard crystal oscillator units rather than designing oscillators around standard crystal units.

## The Gruen Pocket-Oscillator Series

1-562. In 1954-1955 initial steps of a USAF research project were taken at the Armour $\mathrm{Re}-$ search Foundation under the direction of H. E. Gruen* to develop a series of miniature, plug-in, crystal-controlled, vacuum-tube oscillators which could be standardized to cover the frequency range of 0.8 to 75 mc at operating tolerances suitable to meet a majority of the USAF fre-quency-control requirements. The first phase of

[^12]the project was a comprehensive investigation of the frequency-control applications of a large sample of radio sets currently in use by the USAF. It was found that 80 to 90 percent of the frequency-control requirements within the 0.8 75 -me range could be met economically by three conventional circuits, each designed for three bands, or a series of nine standard oscillators in all. It does not require this many separate oscillator circuits simply to cover the necessary frequency range, but it is desirable to have the recommended operating band of each circuit sufficiently narrow so as to avoid having to make critical tuning adjustments. For the same reason the circuits are not designed for specialized optimum operating characteristics within each band, but are intended only to provide a useful output consistent with the minimum requirements of accuracy and stability of the average frequencycontrol circuit used by the military.
1-563. The primary purpose of the packet-oscillator project has been to develop a sequence of plug-in circuits that can serve as models for establishing an initial set of oscillator Military Standards having the broadest practical tolerances. Once a beginning set of standards is agreed upon, it is to be expected that electronic manufacturers of packaged oscillators will introduce their own design modifications in meeting these standards-modifications which may lead to more rigid standards to supplement the broader standards for special applications. For example, the need may arise for an oscillator having a minimum deviation in frequency with ambient temperature, or with time, or in having a minimum tolerance in output amplitude, or in having a maximum possible output for given load conditions, or in having a minimum harmonic content, and so on ad infinitum with all possible combinations of electronic, physical, and operational special requirements. From a Military Standards point of view it is not the interior design of the oscillator that need or should be officially specified, but only what the unit can do or be or require in relation to the mechanic-thermodynamicelectronic system in which it is to be mounted. In this way a manufacturer is not discouraged from developing an improved packaged oscillator that can do an equivalent job more economically or better than the original standards model.
1-564. On the other hand, from an economically practical point of view, the Gruen packet series can profitably serve as unofficial standards insofar as the designs of the various oscillators are concerned-economical since the circuits used in
these units have known performance characteristics, which, of course, would meet any Military Standards based upon them. The circuits themselves are conventional, designed to be used with Military Standard crystal units. Any standards established for packaged oscillators based upon the Gruen series will, of course, be no more rigorous than those already established for the crystal units being used.
1-565. The Gruen packet series employs three basic oscillator circuits: the grounded-plate Pierce, the electron-coupled grounded-plate Pierce, and the cathode-coupled Butler circuit. The two Pierce-type circuits are both used to cover the same frequency range of 0.8 to 16 mc . The Butler circuit is designed to cover the higher range of 10 to 75 mc . The electron-coupled circuit is recommended as an alternate in the lower frequency range when the input to the following stage is a tuned circuit, or whenever a minimum degree of coupling is desired between the crystal oscillator and the succeeding stage.

## gRounded-plate pierce packet ( 0.8 TO 16 MC )

1-566. Figure 1-242 is a picture of the miniature packaged Pierce oscillator designed as a plug-in unit by Gruen to cover the $0.8-16$-me range. This range is covered in three bands. A schematic diagram of the basic circuit and the values of the parameters for each of the three bands is


Figure 1-242. Miniature plug-in (sfandard octal base) Pierce oscillator ( 0.8 to 16 mc ) developed at Armour Research Foundation by H. E. Gruen et al., as an initial basic packaged oscillator unif to be standardixed for militory use

## Section I Cryital Osallators

shown in figure 1-243. Figure 1-244 shows the output voltage versus frequency for each of the three bands, and figure 1-245 shows the crystal drive in milliwatts versus frequency. These performance charts, prepared by J. S. Kurinsky of Armour Research Foundation, are based upon measurements made under no-load conditions. The range of values at each frequency is representative of the variations in output and crystal drive to be expected due to typical variations in crystal resistance. Thus, the bottom (lowest output and lowest crystal drive) curves of each of


| Frequency Band (me) | $\underset{\text { (kilohms) }}{R_{\mathrm{C}}}$ | $\underset{\text { (kilohms) }}{\mathbf{R}_{\mathbf{K}}}$ | $\underset{(\mu \mu f)}{C_{1}}$ | $\underset{(\mu \mu \mathrm{f})}{\mathrm{C}_{\mathbf{y}}}$ | $\underset{(\mu \mu \mathrm{I})}{\mathrm{C}_{2}}$ | $\underset{(\mathrm{mh})}{\mathrm{L}_{\mathrm{K}}}$ | $\underset{\text { (volts) }}{\mathrm{B}+}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.8-5 | 1000 | 3.9 | 15 | 10 | 47 | 7.0 | 75 |
| 3-11 | 100 | 2.0 | 15 | 10 | 47 | 0.8 | 100 |
| 5-16 | 47 | 1.5 | 15 | 10 | 36 | 0.3 | 100 |

Note: The value of $C$ is chosen so that proper operation is obtained when this circuit operates into a load of $15 \mu \mu$. Wiring capacitance increases the values of $\mathrm{C}_{1}, \mathrm{C}_{2}$, and $\mathrm{C}_{2}$ by the following amounts:

C: $5.5 \mu \mu \mathrm{f}$
$\mathrm{C}_{3}: 3.5 \mu \mu \mathrm{f}$
$\mathrm{C}_{2}$ : $10 \mu \mathrm{ff}$
Figure 1-243. Schematic diagram and parameters of the grounded-plate Pierce circuit of Gruen packet series


Figure 1-244. Typical oufput voltage and voltage tolerances of the grounded-plate Pierce circuit of Gruen packef series. These voltages were measured under no load conditions except for the connection of a 15 - $\mu \mathrm{f}$ f capacitance across the output to insure a correct effective load capacitance for the crystal unit


Figure 1-245. Typical drive levels and operating tolerances to be expected for crystal units connected in the grounded-plate Pierce circuit of Gruen packet series. The values shown assume no resistance losses in the output load
the bands should not be interpreted as representing the output and crystal drive when crystal units of maximum permissible resistance are inserted in the circuits. The performance characteristics for maximum-resistance crystals are fairly closely approximated by the bottom curve of the high band; but the highest-resistance crystal units used in the low-band measurements had resistance values only one-half to one-fourth the permissible limits. Note in figure 1-242 that the external mounting of the crystal unit and vacuum tube permits a ready replacement of either without diminishing the advantages of the packaged unit. The metallic clasp appearing to shield or support the vacuum tube is actually inserted as a thermal conductor to prevent overheating. A tuning element, in the form of a screw adjustment for $\mathrm{C}_{3}$ (in figure 1-243), is provided to ensure that the correct load capacitance ( 32 $\mu \mu \mathrm{f}$ ) is across the crystal unit. The parameters indicated for $\mathrm{C}_{3}$ are based on the assumption that the external load will introduce an additional $15 \mu \mu \mathrm{f}$ in parallel with $\mathrm{C}_{3}$. If not, $\mathrm{C}_{3}$ must be adjusted to give the proper total. $C_{3}$ can also be used as a trimmer adjustment in the event of crystal aging. The frequency stability of the Pierce packet as a function of the plate voltage


Figure 1-246. Drawing of miniafure plug-in (andard octal basel electron-coupled Pierce oscillafor (0.8 to 16 mcl developed af Armour Research Foundation by H. E. Gruen of al., as an initial basic packaged oscillator unit to be standardized for military use

Section 1
Crystal Oscillators


| Frequency <br> Band (me) | $\underset{\text { (kilohms) }}{\mathrm{R}_{c}}$ | $\underset{\text { (kilohms) }}{\mathbf{R}_{\mathrm{k}}}$ | $\begin{gathered} \mathrm{R}_{1} \\ \text { (kilohms) } \end{gathered}$ | $\left\|\begin{array}{c} \mathrm{R}_{n} \\ \text { (kilohms) } \end{array}\right\|$ | $\underset{\text { (kilohms) }}{\mathbf{R}_{\mathbf{2}}}$ | $\begin{gathered} \mathrm{C}_{1} \\ (\mu \mu \mathrm{f}) \end{gathered}$ | $\begin{gathered} C_{2} \\ (\mu \mu f) \end{gathered}$ | $\begin{gathered} C_{2} \\ (\mu \mu f) \end{gathered}$ | $\begin{gathered} C_{4} \\ (\mu \mu f) \end{gathered}$ | $\begin{gathered} \mathrm{C}_{8} \\ (\mu \mu \mathrm{f}) \end{gathered}$ | $\underset{(\mathrm{mh})}{\mathrm{L}_{\mathrm{X}}}$ | $\begin{gathered} \mathrm{B}+ \\ \text { (volts) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.8-5 | 1000 | 3.9 | 100 | 30 | 10 | 15 | 10 | 130 | 1000 | 1000 | 7.0 | 125 |
| 3-11 | 100 | 2.0 | 100 | 30 | 10 | 15 | 10 | 62 | 1000 | 1000 | 0.8 | 150 |
| 5-16 | 47 | 1.5 | 100 | 30 | 10 | 15 | 10 | 51 | 1000 | 1000 | 0.3 | 150 |

Wiring capacitance increases the values of $C_{1}, C_{s}$, and $C_{n}$ by the following amounts:
$\mathrm{C}_{1}: 5.5 \mu \mathrm{mf}$
$\mathrm{C}_{2}: 3.5 \mu \mu \mathrm{f}$
$\mathrm{C}_{8}: 10 \mu \mu \mathrm{f}$

Figure 1-247. Schematic diagram and parameters of the electron-coupled, grounded-plate Pierce circuif of Gruen packet series
sapply is rated at 2 to 3 parts per million per 10 per cent voltage change.

## ELECTRON-COUPLED PIERCE PACKET ( 0.8 TO 16 MC )

1-567. Figures 1-246, 1-247 and 1-248, respectively, show a dimensional drawing, the schematic diagram, and the output-voltage characteristics of the electron-coupled packaged unit. The output curves are representative of a typical group of crystal units, the same group that was used in plotting the performance of the Pierce oscillator as shown in figures 1-244 and 1-245, and, hence, are not intended to represent the entire output tolerance to be expected when crystal units of minimum resistance are replaced by those of maximum resistance. The tuned-output curves were obtained by replacing $R_{3}$ with a plate tank that was then tuned for maximum output at the fundamental. The fundamental frequency remains stable within 2 to 3 parts per million as the plate circuit is tuned throughout its range. The frequency stability as a function of plate supply voltage is 2 to 3 parts per million
per 10 per cent voltage change. Note in the schematic diagram that the suppressor grid is connected to be operated at the same bias as the cathode, but is r-f bypassed to ground through $C_{4}$. This arrangement permits much greater independence of the frequency-control circuit from the plate load tuning, and therefore, smaller frequency-deviation limits.

## CATHODE-COUPLED BUTLER PACKET ( 10 TO 75 MC )

1-568. Figure 1-249 shows a dimensional drawing of the packet design of a Butler circuit which has been tested in three bands to cover the over-all frequency range of 10 to 75 mc . Figure 1-250 is a schematic diagram of the circuit, with the parameters given for each of the three bands. Figure 1-251 shows the output voltage deviation to be expected from a typical group of crystal units. No data is available at this writing of the exact range of crystal resistance that is represented by the output curves, nor by the crystaldrive curves shown in figure 1-252. Very probably the bottom curves in each of the figures,


Figure 1-248. Typical output voltage and voltage tolerances of the electron-coupled, grounded-plate Pierce circuit of Gruen packet series
particularly in the high band, are approximately representative of crystal units having the maximum permissible values of resistance. Figure 1-253 shows the difference, in parts per million, betwren the series-resonance frequency of the crystal unit as measured in a CI meter and the operating frequency of the same crystal unit when connected in the Butler circuit, as measured by different operators at repeated tunings to peak output voltage. This circuit-frequency deviation should be added to the nominal frequency tolerance of the crystal unit in order to evaluate the over-all frequency tolerance of the packaged oscillator. For a 10 per cent change in plate supply voltage the stability of the oscillator unit is within 1 to 2 parts per million in the $10-20-\mathrm{mc}$ range, 3 to 4 parts per million in the $20-40-\mathrm{mc}$ range, and 4 to 5 parts per million in the $40-75$ me range.


Figure 1-249. Miniature plug-in fstandard octal base) cathode-coupled Butler oscillator ( 10 to 75 mc ) developed at Armour Research Foundation by H.E. Gruen ef al., as an initial basic packaged oscillator unit to be standardized for military use

Section 1
Crystal Oscillators


| Frequency <br> Range (mc) | $\begin{gathered} \mathrm{R}_{2} \\ \text { (ohms) } \end{gathered}$ | $\underset{(\mathrm{ohms})}{\mathrm{R}}$ | $\underset{\text { (kilohms) }}{\mathbf{R}_{\mathrm{G}}}$ | $\begin{gathered} \mathrm{C}_{1} \\ (\mu \mu \mathrm{f}) \end{gathered}$ | $\begin{gathered} C_{o} \\ (\mu \mu f) \end{gathered}$ | $\underset{(\mu \mu \mathrm{f})}{\mathrm{C}_{\mathrm{g}}}$ |  | $\begin{aligned} & \text { B+ } \\ & \text { Volts } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10-20 | 1000 | 1000 | 10 | 470 | 100 | 4.7 | 15 | 100 |
| 20-40 | 1000 | 560 | 10 | 470 | 100 | 4.7 | 15 | 100 |
| 40-75 Note 3 | 1000 | 270 | 10 | 470 | 100 | 1.6 | 15 | 100 |

Note 1: Inductance $L_{t}$ is tuned to resonate with $C_{t}$ at the operating frequency.
Note 2: All test results were obtained with the oscillator working into a 5000 -ohm load.
Note 3: At frequencies of 40 me and higher, an inductance which resonates with the static capacitance of the crystal should be used to prevent unwanted oscillation. A low value of $Q$ is desirable; coils wound on $1500-0 h m$ composition resistors perform well.

Note 4: The value of $15 \mu \mu$ for $C$, includes stray wiring capacitance.
Figure 1-250. Schematic diagram and parameters of the Butler circuit of Gruen packet series


Figure 1-251. Typical output voltage and voltage tolerances of the Butler circuit of Gruen packet series when oparating into a 5000 -ohm load


Figure 1-252, Typical drive fevels and operating tolerances fo be expecfed for crystal units connecfed in fhe Buller circuil of Gruen packet series. The values shown assume a 5000 -ohm load resistance


Figure 1-253. Typical frequency folerances to be expected of crystal units connected in Butler circuif of Gruen packet series. The deviations platted are deviations of the peak-output aperating frequency from the seriesresenance frequency of the individual crystal unit as measured with a Cl meter, and are not deviotions from the rated nominal frequency of the crystal unit. Thus, the overall tolerance to be expected of such an oscillator must be the total of the crystal unit nominal frequency tolerance plus the expected operating resonance folerance, the latter being indicated by the measured deviation above

## Packaged Crysfol-Confrolled Transisfor Oscillators

1-569. Transistor circuits are ideally suited for miniaturized packaged units. Eventually, when transistors, especially those in the h-f range, are being manufactured with closer tolerances, it is to be expected that a majority of the packaged oscillators will be of transistor design. Almost certainly will this be true of those units designed to be temperature controlled since the heat dissipation of the transistor is so much smaller than that of the vacuum tube, and hence less of a factor in causing unwanted temperature gradients in an oven container. Research in the direction of developing standardized transistor packaged oscillators is being initiated by the $U$. S. Air Force. At the present writing the only information available concerning the development of any type of transistor packaged oscillator is the experimental model developed at the National Bureau of Standards, discussed in the following paragraph, and the temperature-controlled miniature units already being manufactured by the James Knights Company, discussed in paragraphs 1-571 and 1-572.
SULZER MINIATURE PACK.AGED TRANSISTOR FREQUENCY STANDARD 1-570. A complete packaged $100-\mathrm{kc}$ frequency standard with a self-contained power supply is shown in figure 1-254. This oscillator unit was developed by Peter G. Sulzer of the National Bureau of Standards. Although the primary purpose of the NBS project was to develop a pocket-
size, self-sufficient frequency standard, the result provides an admirable illustration of the possibilities in packaged design. A G-element is employed for frequency control, and as can be seen, the dimersions of the crystal unit comprise about half of the total volume. Power is supplied from a mercury cell, which, of course, would not be a necessary feature if the oscillator unit were adapted for use as a general-purpose plug-in component for precision frequency control. A grounded-emitter junction transistor is used. Capacitors $C_{2}$ and $C_{3}$ form a voltage attenuator in the feedback circuit to reduce the voltage applied across the crystal unit. The relatively large values of the capacitors connecting to the terminals of the crystal unit serve to stabilize the feedback phase. All the circuit elements except the crystal unit and the mercury cell are supported in casting resin on a plastic frame. The mercury cell is at the base. The oscillator is packaged in a metal container (not shown), 7 inches by $13 / 4$ inches. The oscillator has a frequency deviation no greater than 1 part in $10^{8}$ per degree $C$ change in temperature, or 1 part in $10^{8}$ per 0.1 volt change in battery supply.

## COMMERCIALLY AVAILABLE PACKAGED CRYSTAL-CONTROLLED TRANSISTOR OSCILLATORS

1-571. A pioneer in the field of miniaturized packaged oscillators has been the James Knights Company. Their research team composed of R. Ives, C. Reynolds, R. Beetham, R. Berge, C. Eickeberge,


Figure 1-254. Small, portable, packaged transistor crystal oscillator developed by P. G. Sulzer of National Bureau of Standards. Unit is provided with mercury-cell power supply shown at right. Metal confainer is not shown
et al appears to have been the first in this country's electronics industry to have developed miniature, temperature-controlled, plug-in crystal oscillators available for general-purpose use.* Three oscillator units have been developed at this date which employ transistor circuits and are designed for mounting within small crystal ovens. One unit is a multichannel h-f oscillator which can be provided with a bank of up to 11 h -f crystal units mounted, together with its oscillator circuit, within a rotary switch. This assembly can plug into a crystal oven, or into an external octal socket, or it can be panel-mounted. When oven-mounted, the entire package occupies a cylindrical volume approximately $33 / 4$ inches in diameter and 5 inches high. The crystal units are of a subminiature, evacuated, glass envelope type, which operates at frequencies of 6 mc and higher. Insufficient data

[^13]exists to provide a complete technical description of the performance of the oscillator.
1-572. Of greater immediate interest are the two miniature oscillators that are mounted within a cylindrical plug-in oven of unusually high stability, the dimensions of which are shown in figure $1-255$. There are no switching arrangements, there is only one crystal unit to a package, and each is soldered to its circuit. The low-frequency circuit is shown in figure $1-256$, and the highfrequency circuit, in figure 1-257. Evacuated, glass-envelope crystal units are employed to improve the aging characteristics. The l-f circuit is essentially a crystal-controlled multivibrator. Its output is a square wave which can have a 4 -to 5 -volt peak. The h-f circuit has approximately a sine-wave output, 0.8 -volt peak with a 6 -volt supply. At 1 mc the measured deviation in frequency
heater supply of 6.3 volts at 300 ma. The d-c potential of the heaters relative to pin 2 must be between plus 90 and minus 70 volts. The circuitry is mounted in the bottom of the unit, the vacuum tube at the top. The weight is approximately 3.25 oz. A standard octal base is provided. A scyew cap at the bottom permits the unit to be readily taken apart and assembled. The tube shield is removable to permit easy replacement of the vacuum tube. The finish is grey baked enamel. No information can be given concerning the tolerances and stability of the oscillator since it has not been designed for use with a specific crystal unit. For use with some Military Standard units it might become necessary to reduce the plate supply voltage in order to avoid operating the crystal beyond its rated drive level.



5963 HTR. CONN.



Figure 1-255. Dimensions of miniafure, cylindrical, temperature-controlled, fransistor plug-in oscillator developed by James Knights Company. Packaged unit is provided with a standard octal base
was 9 cps when the supply voltage was changed from 6 to 4.5 volts. A 2 -me test oscillator has shown an operating stability of 1 ppm over a period of several weeks, but sufficient time has not elapsed for these oscillators, so recently developed, to be tested thoroughly for operating life and aging characteristics. The ovens in which the oscillators are mounted require a maximum of 1.5 amperes at 6.3 volts. The crystal temperature is maintained within plus or minus $1^{\circ} \mathrm{C}$ over an ambient range of $-55^{\circ}$ to $+70^{\circ} \mathrm{C}$. The assembled package is equipped with a standard octal base.

## Standards for Packaged Oscilletors

Many of the problems associated with the standardization of electronic components appear to defy solutions that satisfy designer, fabricator, distributor, consumer, and repairer alike. As a result, the subject of standardization, itself, is often a controversial issue. After discussing a number of the conflicting points of view with different associates in the crystal industry, it seemed to the uriter that perhaps some indirect good might result if these points of view, as applicable in the standardization of packaged oscillators, were assembled on paper where they might more easily be secn in relation to one another. For this reason, the discussion from paragraphs 1-573 to 1-581 detours somewhat from the domain of technical fact into an area more representative of individual opinion. The reader interested only in the technical aspects of packaged oscillators can disregard these paragraphs.

## ADVANTAGES OF STANDARDIZATION

 1-573. The primary advantages of standardized packaged oscillators, as of other standard pack-

Figure 1-256. Schematic diagram of crysfal-controlled transistor circuit employed in James Knights packaged low-frequency 110 to 100 kc ) oscillators. Square wave output is rich in harmonics


Figure 1-257. Schematic diagram of crysfal-controlled transistor circuit employed in James Knights $m$-f and h-f 10.1 to 10 mc oscillators. Relatively pure sinewave output
aged units, can be described as those of economy:
a. It is an economical saving for research and design departments to avoid having continually to assign and train engineers in the special design theory and developmental techniques of oscillator circuits; this saving can be achieved if there are commercially available osciliator units of known operational characteristics capable of meeting all normal frequency-control requirements.
b. It is more economical for equipment manufacturers to assemble a given oscillator circuit in a fixed manner as a separate unit, regardless of the different types of equipment in which it is to be used, than by fabricating the oscillator as an integral part of a much larger network where special production procedures are required to make the electrical and physical connections conform to each different chassis layout.
c. It is more economical for maintenance departments to replace defective oscillators as plug-
in units than to find, educate, break in, and pay highly trained technicians to troubleshoot and repair them; to say nothing of the additional man hours saved by avoiding the necessity of having to store and distribute each oscillator part separately.
d. Consequently, it is an economical saving to the consumer, who ultimately must bear the costs of the research, design, development, fabrication, and maintenance. In addition, the consumer can also profit from the longer life of the oscillator due to the extra protection provided by the package design, particularly if the container is hermetically sealed.

## PROBLEMS OF STANDARDIZATION

1-574. Standardization has its dangers as well as its advantages. The dangers arise both from too much standardization, and from not enough standardization-from freezing the design of an item so thoroughly that the development of improved models is discouraged, and from having such ambiguous and unsystematic standards that many of the advantages are lost. Over-standardization is most apt to result from the understandable resistance of maintenance and repair organizations to having endlessly to contend with an ever expanding jumble of different models of every description. Under-standardization is most apt to result from the equally understandable resistance of the manufacturer in committing himself to rigid technical standards that slow his production line, or limit his freedom to experiment with new techniques and designs. Both too much and too little standardization can suffocate technical progress. In the particular case of packaged oscillators, much thought is being given for the establishing of a system of standards that avoids the pitfalls of both extremes.

## If Standards Are Too High

1-575. Over-standardization appears to exist at three different levels. When the standards are too high; when they are over-emphasized; and when they are too restrictive. The least offensive are the standards that are too high. Indeed, the effort to meet exceptionally high standards is usually a spur to the development of new inventions and new techniques. Where the product cannot be fabricated with profit, it simply is not produced; so that the problem has a way of working out its own solution.

## If Current Standards Are Overemphasized

1-576. Over-emphasis of the importance of keeping the number of available models of a given component to a minimum is probably the most
frustrating bugaboo that a pioneering manufacturer can face when he seeks official acceptance of a new design. It is true that standardization does and should discourage the development of new models that offer no improvement over the currently available standards, since such developments are effectively only a waste of engineering talent. But it should not discourage the development of improved models, which unfortunately does happen when the immediate problems arising from a new adjustment are emphasized ahead of the long-range advantages of a maximum rate of technical progress. It would seem that, if from the beginning, a standards program were planned that would anticipate the systematic development of improved models and higher standards, even to the extent of reserving pigeon holes for its eventual achievement, the advantages of standardization could be increased. For it appears that standardization of engineering products, in essence, is only a means of making known to the engineer exactly what is available. If the standards for packaged oscillators can be systematically organized at the start so that the development of new products can readily be placed in their anticipated categories, without disturbing the old standards or changing the cataloging system, then only the duplication of physical and functional characteristics need be discouraged in the development of new models.
If Standards Are Too Restrictive
1-577. Generally it is better to risk too much standardization than not enough, and because of this, probably the most difficult type of overstandardization to pinpoint is that in which too many of a component's characteristics are standardized. The problems that arise become particularly harassing when the committee controlling the standards are under strong pressure to keep the number of standard components to an absolute minimum. Under these conditions every newly developed component is considered primarily as a replacement of an older model, rather than as a new model, to compete with the old only for use in equipments of new design. For example, in the matter of standardizing crystal holders, experience has shown that considerable resistance is met when it is desired to gain official acceptance for any new design which in the future could replace an existing standard design, even though the new design is of proven superiority. If a plastic or metal container is standard for a given size of holder, reasons arise for delaying new standards for a superior metal or glass container, respectively. If an odd-shaped base has been standard-
ized, it is very difficult even to gain acceptance for a standard octal base in an otherwise equivalent holder.
1-578. If a long delay is generally to be expected before new models can be standardized, or if the number of standard items must be kept to an absolute minimum, some of the difficulties facing production engineers are often avoidable when care is taken in establishing only those standards that specify the function that a particular item or unit is to perform in relation to any system in which it is to be used-not how the function is to be achieved, unless the manner of achievement in some way affects the design of the external system or the cost of maintenance and repair of the system as a whole. Why, for example, should the marner in which a crystal is mounted inside its holder be standardized, if there is no intention to repair defective units? If a crystal unit can meet all the required physical, eiectrical, and operational relations to the exterral system, what difference does it make how this is accomplished?
1-579. In regard to packaged oscillators, it is to be hoped that sufficient performance tests can be devised to eliminate the need for standards governing the internal design of the package. Unless the crystal unit is to be replaceable in the field, or is to have an outside mounting, as in the case of the Gruen package, it should not be necessary to specify the type of crystal unit employed. Indeed, what difference can it make to the user of two packaged units, identical insofar as their external characteristics are concerned, if one contains a erystal-controlled oscillator and the other a little imp turning a crank? As long as either controlling source is confined completely within its container and works dependably within the rated tolerances, the performance standards need not be concerned with whether the control is piezoelectric or metabolic. In the case of the crystal-controlled circuit, if the crystal unit is to be mounted inside the package container, as would be the case in a tem-perature-controlled unit, a manufacturer should not be required to use a Military Standard crystal unit if he can meet the oscillator requirements more satisfactorily with another type of crystal mounting or holder. (We assume that the oscillator standards will not require that the crystal unit be replaceable in the field. Such a specification for a completely packaged unit would mean that one of the primary advantages of packaging is being wasted-that in the case of breakdown, instead of replacing the packaged unit, the intention is to service it.) Also, it may be preferable to solder the crystal unit in place, than to depend
upon a plug-in connection, since the former method usually permits a more stable circuit. A properly fabricated crystal unit can generally be depended upon to last as long as the useful life of the equipment in which it is to be used, so no objection to the soldered connection should arise except in special applications. For example, the specification for a plug-in crystal unit could be important when mounted outside the package, as in figure $1-242$, where it can readily be replaced without disturbing the packaged unit. Such an arrangement should prove desirable if the same oscillator is intended to operate at more than one frequency where space does not permit a switching arrangement capable of mounting and connecting all the required crystals, so that these must be inserted manually in the field as the need arises. Also, the plug-in arrangement becomes important when the operating life of the crystal unit is expected to be much shorter than that of any other part of the packaged unit; or if the operating life of the entire unit is to be of relatively short duration. In any event, it would seem that progress in the development of packaged oscillators will be promoted better if the standards initially established are confined to specifying what the packaged oscillators are to be able to do under specified external conditions and do not tend to limit the ways in which the functional specifications are to be achieved, even if at the time the standards are established there appears to be only one way in which the desired function can be achieved.

## Avoidance of Ambiguous Standards

1-580. If too much standardization vexes primarily the manufacturer of the standardized item, too little standardization scatters its headaches chiefly among those that must use the item. Particularly sensitive to the uselessness of ambiguous specifications or generalized advertising claims concerning a component is the design or developmental engineer who wishes to approach his circuit problems scientifically, yet who cannot do so unless he knows quantitatively exactly what he is putting into his circuit. To the engineer, a set of standards sufficiently rigid and dependable for predictable design and replacement purposes is equivalent to a set of rigid production line tests, since a unit cannot be guaranteed to pass certain specifications unless at least a representative sample has been tested to meet the specifications. Furthermore, since the performance of a unit depends upon the conditions under which it is operated, it is often of little help to a design engineer to specify exactly what a unit can do un-
less accompanied by equally exact data concerning the conditions under which the rated performance takes place.
1-581. As applied to packaged oscillator units, it is highly desirable that a systematized set of standard operating conditions be established simultaneously with a systematized set of performance standards. Otherwise, each oscillator may have to be adjusted for optimum performance in the particular equipment in which it is to be used. The ideal standard oscillator need not and should not be adjustable by either the equipment production line technician or by the equipment operator in the field. Too many variables are present. If adjustable, all tolerances must be rated as the maximum to be encountered over the adjustable range. If the equipment in which the unit is used can permit such tolerances, then there is no need to adjust the unit in the first place. A plausible exception would be the case of a small trimmer capacitor to offset the effects of aging in high-precision systems. Another exception would occur if it were practicable to design a unit with marked adjustment points at which the tolerances could be separately specified. For example, one adjustment setting could indicate a point of maximum output amplitude, another a point of maximum amplitude stability, another a point of maximum frequency stability, etc. But to the extent that the adjustments made by the user are not definitely predictable, the advantages of standardization are lost. It would be preferable for the manufacturer of the packaged units to make the adjustments and assign different model numbers where the same circuit had significant performance differences.

## PRINCIPAL OSCILLATOR <br> CHARACTERISTICS TO BE STANDARDIZED

1-582. Packaged oscillator characteristics that should be standardized can be grouped in two categories-physical and electrical. The former concerns primarily the mounting requirements and limitations; the latter covers the operating requirements and performance characteristics. Of the physical characteristics the most important are the conventional items such as dimensions, weight, shape, provisions for mounting, ambient temperature range, mechanical ruggedness as measured by well-defined tests, moisture resistance, seal test, operating life of thermostat, if any, and so forth. Of the more important electrical characteristics there are the operating requirements and permissible tolerances of such items as input voltages, currents, and power, the test load impedance, ground connections, and the like; also,
there are the performance characteristics to be specified for the standard test conditions. These performance characteristics include the following: output fundamental frequency; db level of nearest harmonics relative to fundamental; equivalent emf and impedance of oscillator, when viewed as an impedance in series with a generator, at the fundamental frequency and at any useful overtones; output waveform; frequency and amplitude tolerances; frequency and amplitude deviations over input voltage range and over operating temperature range; frequency deviation over permissible load tolerances; and frequency and amplitude deviations permissible after the unit is subjected to the various aging and mechanical tests.

## EFFECT OF CRYSTAL RESISTANCE ON PACKAGED OSCILLATOR STANDARDS

1-583. Even in those packaged oscillators in which a Military Standard crystal unit is not to be specified, the most economical fabrication process will probably require the use of such a unit, or at least one that has electrical tolerances equivalent to those of a standard unit, since the oscillator standards will undoubtedly be originally established on the basis of oscillators of known operational characteristics employing Military Standard crystals. In establishing the oscillator standards it is important that account be taken of the full variation in output level and frequency to be expected due to the range of the equivalent resistance of the crystal unit between its maximum permissible and minimum expected values. Likewise, it is important that the developers of the packaged oscillators test their circuits over the expected crystal resistance range to ensure that the oscillator standards are met throughout the range. Generally it is only the maximum resistance conditions that must be specifically tested. If the design engineer does not have maximumresistance crystal units available, these can be simulated in making the laboratory tests.

## Simulating Maximum-Resistance Crystal Units

1-584. First, the equivalent resistance of the crystal unit being used in the test circuit must be measured with the aid of the appropriate CI meter. If the test circuit employs a series-mode crystal unit, simulating a maximum-resistance crystal is readily achieved by connecting in series with the crystal a resistance of such a value that the total resistance is equal to the maximum permissible. If the test circuit employs a parallelmode crystal unit, the simplest method is to employ a strategem devised by John W. Sherman, Jr.
of General Electric Co.* A high resistance is connected in parallel with the crystal unit. The value of this resistance is chosen so that the power losses of the actual crystal unit and of the resistance in parallel have a combined value equal to the losses that would occur if the crystal unit were of maximum resistance. Assuming that the impedance of the crystal unit is approximately equal to its effective reactance, $X_{\text {e }}$, which in turn is approximately equal to $\frac{1}{\omega C_{z}}$, where $C_{x}$ is the rated load capacitance and $\omega$ is the angular frequency, then the current through the crystal unit in both the actual and the maximumresistance case would be approximately equal to $E_{c \omega} C_{x}, E_{c}$ being the voltage across the crystal unit. Letting $\boldsymbol{R}_{\text {em }}$ equal the maximum permissible resistance, $R_{e}$ equal the actual effective resistance of the crystal unit, and $R_{x}$ equal the value of the shunting resistance, we set the power losses in the hypothetical crystal unit of maximum resistance equal to those due to the actual $\mathbf{R}_{e}$ and $\mathbf{R}_{x}$ : $\left(\mathrm{E}_{\mathrm{c} \omega} \mathrm{C}_{\mathrm{x}}\right)^{2} \mathrm{R}_{\mathrm{em}}=\left(\mathrm{E}_{\mathrm{c} \omega} \mathrm{C}_{\mathrm{x}}\right)_{2} \mathrm{R}_{\mathrm{e}}+\mathrm{E}_{\mathrm{c}}{ }^{2} / \mathrm{R}_{\mathrm{x}}$
From which the equation for $R_{x}$ is obtained.

$$
R_{x}=\frac{1}{\omega^{2} C_{x}^{2}\left(R_{\mathrm{cm}}-R_{e}\right)}
$$

## FACTORS INVOLVED IN OSCILLATOR LIMITING

1-585. The characteristics of any oscillator are dependent to a large extent upon the degree and type of amplitude limiting employed. The factors involved are especially significant in the case of crystal oscillators because the variations in crys-tal-unit effective resistance tend to introduce fide

[^14]variations in the amplitude of oscillation when different crystal units of the same type and frequency are substituted in the same circuit. The method of limiting also affects the type of crystal unit to be used, whether it is to be a series- or a parallel-mode unit. Directly dependent upon the limiting method will be the harmonic content in the oscillations. Upon the degree of harmonic distortion will depend the tuning of the circuit, so that any deviations in the limiting characteristics are reflected as instabilities of frequency as well as of the amplitude. In the following paragraphs we shall discuss these factors briefly; but first, the reader may find it helpful to review paragraph $1-232$, in which the crystal oscillator, as a generalized negative-resistance circuit, is discussed.

## Negotive-Resisfance Limiting

1-586. In paragraph 1-232 we found that when a crystal oscillator is represented as a seriesresonant negative-resistance circuit (figure 1-108 (B)), oscillations continue to build up as long as the numerical ratio $\left|\frac{\rho_{n}}{R_{r}}\right|$ is greater than 1 . When the oscillator is represented as a parallel-resonant negative-resistance circuit (figure 1-108 (C)), oscillations build up as long as the numerical ratio $\left|\frac{Z_{p}}{\rho}\right|$ is greater than 1. Now, in figure 1-108, both the series-resonant and the parallel-resonant neg-ative-resistance circuits are intended to represent the same crystal oscillator, one that employs a parallel-mode crystal unit. Let us modify our interpretation of the series-resonant circuit to let it represent any series-resonant circuit containing a crystal element. That is, we shall treat $X_{1}$ as the reactance of any load capacitance actually connected in series with the crystal unit, as is the case, for instance, in a CI-meter circuit connected for parallel-mode crystal control. We shall also be free to assume that $X_{c}$ and $X_{i}$ each equals zero, in which case the circuit is equivalent to a seriesmode crystal unit connected across the terminals of a negative resistance equal numerically to the series-resonance resistance of the crystal unit. As far as the parallel-resonant negative-resistance circuits shown in figure 1-108 are concerned, we shall continue to consider them as representing an actual parallel connection of a crystal unit and its load capacitor driven at parallel resonance by a negative resistance, $\rho$. In other words, we wish simply to make it clear that the generalized seriesresonant circuit represents an actual series-resonant circuit, and that the generalized parallel-
resonant circuit represents an actual parallelresonant circuit.
1-587. In order for oscillations to build up and reach a stable equilibrium in the series circuit, we see that the negative-resistance device must have the property of automatically decreasing its negative resistance as the amplitude of oscillations increases. The negative-resistance device of the parallel circuit must have the opposite property ; that is, its negative resistance must increase as the amplitude increases. Literally, these opposing requirements mean that the same device used as a negative resistance in the series circuit cannot be used in the parallel circuit, or at least not with the same operating characteristics, and vice versa. By the term "negative resistance" used in this context, let it be plain that we mean a two-terminal network which, when connected across the crystal circuit, behaves exactly as an automatically variable resistor does, except that the negative resistance supplies energy rather than dissipates it. The act of connecting a negative resistance across a crystal circuit does not in itself generate a voltage and current for driving the circuit. Of course, a signal generator used to force-drive the circuit can be treated as a virtual negative resistance mathematically to simplify a network analysis, but that is not a "passive" type of resistance such as we are concerned with here. The voltage across, or the current through, a passive resistance (negative or positive) is not assumed to be self-generated by that element, but rather is the response of the resistance to the actions in the rest of the circuit. In an oscillator circuit, the initial action is the random thermal motions of the free electrons; the negative resistance reacts to this at the same energy level, the remainder of the circuit reacts to the negativeresistance reaction, the negative resistance reacts, in turn, to this, and so on until the energy builds up. At all times the frequency, amplitude, and phase of the negative-resistance voltages and currents are under the control of the external circuit. 1-588. As long as the oscillations are building up, part of the energy being supplied by the negative resistance is being stored by the circuit. As far as the negative resistance is concerned, the stored energy is equivalent to lost energy, so that process can be represented by the addition of equivalent resistances in the generalized circuits. Figure 1-258 shows the generalized negative-resistance circuits with the equivalent "energy-storing" positive resistances. In the series circuit, the instantaneous value of $R_{e z}$ is defined by the equation:

$$
\mathbf{R}_{\mathrm{es}}=\left|\rho_{\mathrm{s}}\right|-\mathbf{R}_{\mathrm{e}}
$$



Figure I-258. Equivalent circuit during build-up period of generalized negafive-resistance crystal oscillator. (A) Series-mode circuit (B) Parallel-mode circuit

In the parallel circuit, the instantaneous value of $R_{n, n}$ is defined by the equation :

$$
\frac{1}{\mathrm{R}_{\mathrm{eq}}}=\left|\frac{1}{\rho}\right|-\frac{1}{Z_{\mathrm{p}}}
$$

Note that for the oscillations to build up in the series circuit, the total effective positive resistance ( $\mathbf{R}_{\mathrm{e}}+\mathrm{R}_{\mathrm{m}}$ ) must be greater at the start and during the build up than when equilibrium is reached. How much greater, of course, will depend upon the difference at each instant between the negative resistance and the true circuit resistance. For oscillations to build up in the parallel circuit, the total effective positive conductance $\left(\frac{1}{\mathrm{Z}_{\mathrm{p}}}+\frac{1}{\mathrm{~K}_{\mathrm{es}}}\right)$ must be greater at the start and during the build up when the equilibrium is reached. The value of the additional conductance will at each instant equal the diffcrence between the negative conductance and the actual tuned-circuit conductance.
1-589. Clearly, for oscillations to build up in the two circuits, the respective resistance ratios $\left|\frac{\rho_{s}}{\mathrm{R}_{\mathrm{s}}}\right|$ and $\left|\frac{Z_{p}}{\rho}\right|$ must be greater than unity at the start of oscillations. Also apparent should be the fact that these ratios will equal unity when equilibrium is reached. This means that the respective nega-tive-resistance devices must permit $\rho_{\mathrm{n}}$ to decrease and $\rho$ to increase as the amplitude of crystal oscillations increases. But suppose that the devices which produce the negative resistances in the two circuits are switched. What then? If the new starting ratios, $\left|\frac{\rho}{R_{e}}\right|$ and $\left|\frac{Z_{n}}{\rho_{\mathrm{f}}}\right|$ are less than unity, no oscillations can begin; but if these ratios are equal to or greater than unity, oscillations can start, but they cannot attain a stable equilibrium.


Figure 1-259. Typical negative-resistance devices and characterisfics. (A) Transistor emifter current-controlled negative resisfance (B) Transitron voltage-controlled negative resistance

Exactly what actions might result from the unstable conditions would depend upon the particular circuit and negative-resistance device.

## Current- and Voltage-Controlled Negotive-Resistance Characteristics

1-590. Figure 1 -259 shows volt-ampere characteristic curves of two representative negativeresistance devices. (A) shows a typical transistor emitter characteristic, whereas (B) shows a typical transitron characteristic. The negative-resistance property is confined to those regions of the curves with a negative slope, as labeled between points $A$ and $B$. When either of the devices is operated in the negative-slope region, an incremental increase in one of the variables will be accompanied by an incremental decrease in the other variable. Thus, in (A) at a point $C$ between $A$ and $B$, if the current incresses by a very small amount, di, the voltage will decrease by an amount, dv . The ratio, $\mathrm{dv} / \mathrm{di}$, is the dynamic resistance at the point in question, which in this case is negative since $d v$ and di are opposite in sign. This does not mean that the total resistance, $v / i$, is necessarily negative, but simply that the resistance to a small variation in current is negative. It is the resistance to be met by a small a-c signal superimposed on the direct current indicated at point C. In curve (A), the slope at each point is equal to the dynamic resistance at that point; in curve ( $B$ ) the slope is equal to the dynamic conductance at each point.

1-591. Note that for curve (A), one and only one value of voltage corresponds to each value of current. That is, the voltage is a single-valued function of the current. However, note that for a given value of voltage in curve ( $A$ ), there exist three possible values of current. The current in this case is thus a multivalued function of the voltage. In curve ( $B$ ), the current is a single-valued function of the voltage, but the voltage is a multivalued function of the current. Where a negativeresistance characteristic is present, at least the voltage or the current must be a multivalued function of the other. Theoretically both can be, but in practical devices one of the parameters will be a single-valued function of the other. That the other must be multivalued is self-evident when we consider that a volt-ampere characteristic having a continuous negative slope would imply an infinite capacity to supply energy. For some value of current and voltage any electronic device can be made to show a positive resistance. But wherever a characteristic curve would show a change from negative to positive resistance, the bend in the curve will require that one of the parameters, $v$ or i, repeat its values as the other continues to increase.
1-592. The characteristic curve, the emitter circuit, and the negative resistance indicated in figure 1-259 (A) are called current-controlled, since the voltage is uniquely determined by the current. The transitron circuit and its characteristics in figure 1-259 (B) are called voltage-controlled,
since the current is uniquely determined by the voltage.
1-593. Imagine that the devices illustrated in fig. ure 1-259 are to be used in crystal oscillator circuits. The no-signal operating currents and voltages are to be such that each device operates at point $C$. The initial negative resistance is thus the dynamic resistance at that point. As oscillations build up, the average a-c negative resistance in (A) decreases, that in (B) increases. Thus we see that the current-controlled negative resistance is suitable for use with series-mode oscillator circuits, whereas the voltage-controlled negative resistance is suitable for parallel-mode circuits. On the other hand, if a current-controlled negative resistance were to be used to drive a parallel-mode circuit, the oscillations might build up to a point at which the oscillating circuit would suddenly be shorted out, with the sudden loss of stored energy resembling the action of a relaxation oscillator. Or perhaps the circuit will have a tendency to jump from one mode of operation to another.
1-594. The oscillating current of the parallelmode circuit is essentially self-contained, the only current required of the external circuit is that necessary to re-supply the energy lost each cycle. This is such a small fraction of the total current in a high-Q circuit, that its wave shape can be quite distorted without significantly affecting the sinusoidal shape of the voltage wave. A momentary variation in the impedance of the energy source can produce a large variation in the current wave through a negative-resistance device but only a small variation in the voltage wave. In other words, the energy stored in an antiresonant circuit is primarily a voltage-controlling source rather than a current-controlling source. If used with a device whose current is a multivalued function of the voltage, instability can be expected to result if the voltage amplitude cannot be limited within a single-valued region of the current. A resonant series-mode circuit, on the other hand, is essentially a current-controlling source. Extremely high voltages would be required to produce a significant distortion of the current wave shape of a high-Q resonant circuit connected in series with a negative resistance device. For stable oscillations to be sustained in a series circuit, it is important not to employ a voltage-controlled negative resistance, since its operating characteristics are not uniquely determined by the current.
1-595. If the limiting action is provided by an external circuit component, such as a thermistor, the fact that the negative-resistance is current-
or voltage-controlled may not be critical, provided the limiter is certain to act before the oscillations enter an unstable region; nevertheless, the oscillating circuit should be matched to an inherently stable negative resistance for the particular resonance mode. The principal advantage of a ther-mistor-type limiter is that the limiting action is relatively slow, so that once the equilibrium point is reached, the non-linearity introduced by the limiter is relatively insignificant. Under these circumstances all the circuit elements, in particular the negative-resistance source, can be operated as linear parameters, thereby permitting the oscillations (both current and voltage waveforms) to be sinusoidal.

## Frequency Deviation Due to Nonlinear Limiting

1-596. As is normaily the case, the limiting is provided by the negative-resistance device. The oscillations build up until the amplitude swings into one or both of the bends of the negative-resistance characteristic. The farther that the current or voltage (depending upon whether current- or voltage-controlled, respectively) swings past the straight portion of the negative-resistance curve, the greater the distortion in the respective fundamental wave of the dependent parameter. If the swings are extended sufficiently, a point will be reached at which any further increase in the amplitude of the controlling parameter results in a decrease in the amplitude of the dependent parameter at the fundamental frequency. If the amplitude of the controlling parameter is increased further, the amplitude of the dependent parameter at the fundamental frequency will diminish until it disappears entirely, at that point where the effective negative resistance, itself, disappears. Beyond this critical point the fundamental of the dependent parameter reappears, but with its phase reversed, reflecting the fact that the average a-c resistance at the fundamental frequency has changed from negative to positive. Although the fundamental frequency of the dependent parameter may decrease in amplitude as the fundamental frequency of the controlling parameter increases in amplitude, the higher harmonies of the dependent parameter continue to increase, so that it is quite possible for the overtones to exceed the level of the fundamental in high-amplitude systems. On this account, where the fundamental frequency is of principal concern, it is generally preferable to obtain the output in a way that it depends upon the wave shape of the parameter, voltage or current, that controls the negative resistance. On the other hand, if harmonic outputs are

## Section 1 Crystal Oscillators

desired, let them be obtained primarily with the aid of the dependent parameter.
1-597. When harmonics are being generated, the distortion causes the fundamental frequency to assume a slightly different value than would otherwise be the case. This property can be the source of considerable frequency instability in crystal oscillators, since the harmonic content, and hence the fundamental frequency, will vary with the crystal-unit effective resistance, the operating voltages, and the aging and temperature characteristics of the negative-resistance device.
$1-598$. Briefly, the reason that the fundamental frequency is affected by the presence of harmonics can be explained as follows : First, the mixing of all the harmonics in the nonlinear negative-resistance circuit provides a secondary source of the fundamental frequency, since the fundamental will result as the different frequency between any two successive harmonics. For example,

$$
f=3 f-2 f=4 f-3 f, \text { etc. }
$$

Now, if the external crystal circuit is tuned to be approximately resonant at the fundamental frequency, it will generally appear capacitive to the higher harmonic currents. This means that the fundamental frequency obtained from the difference products of the harmonic currents will be displaced approximately 90 degrees in phase from the main fundamental, thereby causing a displacement in the phase of the total fundamental current. Thus, the nonlinear resistance serves to introduce a difference in phase between the current and voltage at the fundamental frequency, and in this manner behaves as if its impedance were
partly reactive. If the negative-resistance device is effectively partly reactive, the external circuit must present an equal and opposite reactance in order for the net impedance around the circuit to be zero. The fact that the harmonic currents pass through the capacitive shunts for the most part means that the external circuit must appear inductive at the operating frequency. For a simple parallel-tuned circuit, this requires that the circuit operate at a frequency below resonance. The frequency displacement to be expected can be approximately obtained from the following equation. The equation was derived by J. Groszkowski.* It is based upon the postulate that a negativeresistance device cannot store energy.

$$
\begin{equation*}
\sum_{n=1}^{\infty} n I_{n}{ }^{2} X_{n}=0 \tag{1}
\end{equation*}
$$

Where:

$$
\begin{aligned}
n & =\text { number of harmonic } \\
I_{n} & =\text { current of } n \text {th harmonic } \\
X_{n} & =\text { reactance of circuit to nth harmonic }
\end{aligned}
$$

This equation says that the sum of all the products, $\mathrm{nI}_{\mathrm{n}}{ }^{2} \mathrm{X}_{\mathrm{n}}$, must equal zero. Since $\mathrm{X}_{\mathrm{n}}$ for all values of $n$ greater than 1 can generally be assumed to be negative, the crystal-circuit reactance facing the negative resistance terminals at the fundamental frequency must be positive (inductive) for the equation to hold.

[^15]
## CROSS INDEX OF CRYSTAL OSCILLATOR SUBJECTS

The subjects related to the design of crystal oscillators are separated into five categories for cross-indexing. These categories appear in the following order:

## I. OSCILLATOR FUNDAMENTALS

II. FUNCTIONAL CHARACTERISTICS OF CRYSTAL OSCILLATORS (Factors to consider in selection of oscillators-alphabetical listing.)
III. CIRCUIT ANALYSES OF BASIC CRYSTAL OSCILLATORS
(Quantitative relations which are fundamental as points of departure in attacking particular problems of design.)
IV. DESIGN OF CRYSTAL OSCILLATORS
V. CRYSTAL OSCILLATOR DESIGN CONSIDERATIONS
(Alphabetical indexing of principal factors to consider when designing for optimum or special performance characteristies.)

The primary subjects contained in the above categories are listed without line indentation. (Alphabetical listings are followed only in categories II and V above.) Subheads under the primary subjects are indented and preceded by a dot (.). Second order subheads are doubly indented and preceded by two dots (..).

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|  | Principles of stable forced-free oscillators | $\begin{aligned} & 265 \\ & 266 \\ & \hline \end{aligned}$ | $\begin{aligned} & 236 \\ & 267 \end{aligned}$ | $\begin{aligned} & 232 \\ & 233 \\ & 236 \\ & 274 \\ & 275 \end{aligned}$ | $\begin{array}{\|c\|} \hline 232 \\ 283 \\ 236 \\ 275 \\ 586 \\ 595 \end{array}$ | $\begin{aligned} & 275 \\ & 586 \\ & 555 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  | . |  | ' |  |  |  |  |  |  |
|  | - Constant-amplitude requirements | $\left\|\begin{array}{l} 269 \\ 206 \end{array}\right\|$ | $\begin{aligned} & 236 \\ & 267 \end{aligned}$ | $\begin{aligned} & 232 \\ & 236 \\ & 267 \end{aligned}$ | $\begin{aligned} & 233 \\ & 236 \\ & 594 \end{aligned}$ | 593 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | $\cdots$ Amplitude build-up | 266 | 236 267 268 | $\begin{aligned} & 232 \\ & 236 \\ & 267 \end{aligned}$ | $\begin{aligned} & 232 \\ & 236 \\ & 586 \end{aligned}$ | 586 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| N | $\cdots$ Amplitude limiting | 266 | $\begin{array}{l\|} \hline 236 \\ 267 \\ 268 \\ 78.5-1 \\ 398 \end{array}$ | $\begin{aligned} & 232 \\ & 236 \\ & 267 \end{aligned}$ | $\begin{aligned} & 232 \\ & 236 \\ & 585 \end{aligned}$ | 583 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Loop gain of unity |  | 257 | 263 |  | 267 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Constant-frequency requirements | $\begin{aligned} & 265 \\ & 260 \\ & \hline \end{aligned}$ | 6 7 267 596 | $\begin{array}{\|c} 20 \\ 238 \\ 267 \end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | **Energy supply, stable | $\begin{aligned} & 265 \\ & 266 \end{aligned}$ | $\begin{array}{r} 23 \\ 267 \end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | *- Impedances, stable | $\begin{aligned} & 265 \\ & 266 \end{aligned}$ | $\begin{gathered} 20 \\ 21 \\ 20 \% \end{gathered}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | *-Loop phase rotation of zero |  | $\begin{aligned} & 265 \\ & 273 \\ & \hline \end{aligned}$ | $\begin{aligned} & 265- \\ & 259 \end{aligned}$ | $\begin{aligned} & 271- \\ & 283 \end{aligned}$ | 267 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | Basic vacuum-tube oscillator circuit |  | $\begin{aligned} & 268 \\ & 273 \end{aligned}$ | $\begin{aligned} & 268- \\ & 2.3 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | -Loop phase analysis |  | $\begin{aligned} & 268 \\ & 272 \end{aligned}$ | $\left\lvert\, \begin{aligned} & 200-2 \\ & 272 \end{aligned}\right.$ | (1018 | 267 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - State of oscillation determined by feedback impedances |  | 20 | \|l| | $\left\lvert\, \begin{aligned} & 283 \\ & 2.1 \\ & 2.2 \\ & 2.3\end{aligned}\right.$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | . |  |  |






|  |  | 1.2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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|  | Output voltage | 306 | $\begin{aligned} & \hline 294 \\ & 299- \\ & 303 \\ & 322 \end{aligned}$ | 275 | $\begin{aligned} & 275 \\ & 355 \end{aligned}$ | 277 284 286 $293-$ 295 $299-$ 303 $308-$ 316 318 321 322 566 567 | $\begin{aligned} & \hline 328 \\ & 336 \\ & 340 \\ & 343 \end{aligned}$ | 349 |  | $\begin{aligned} & \hline 361 \\ & 362 \end{aligned}$ | $\begin{array}{\|l\|} \hline 366 \\ 368 \\ 370 \end{array}$ | $\begin{aligned} & 379 \\ & 568 \end{aligned}$ |  | 420 |  | 425 |  |  | - |  | 437 | 572 | $\begin{array}{\|l} 454 \\ 538 \end{array}$ |  |
|  | Purpose of oscillator | 294 | $\begin{gathered} \hline 6 \\ 294 \\ 296 \\ 305 \\ 311 \\ 562- \\ 565 \end{gathered}$ |  | 355 | 279 <br> 286 <br> 291 <br> 296 <br> 311 <br> $320-$ <br> 327 | $\begin{aligned} & 322 \\ & 336 \\ & 339 \\ & 344 \end{aligned}$ | $\begin{aligned} & 349 \\ & 350 \end{aligned}$ | $\begin{aligned} & 351 \\ & 353 \end{aligned}$ | $\begin{aligned} & 357 \\ & 363 \end{aligned}$ | $\begin{array}{\|l\|} \hline 364 \\ 370- \\ 375 \end{array}$ | $\begin{array}{\|l\|} \hline 376 \\ 387- \\ 391 \end{array}$ | $\begin{array}{\|l\|} \hline 392 \\ 401 \\ 404 \\ 405 \end{array}$ | $\begin{aligned} & 414 \\ & 417- \\ & 420 \end{aligned}$ | 42i | 423 | $\begin{array}{\|l\|} \hline 426 \\ 428 \end{array}$ | $\begin{array}{\|l\|} \hline 426 \\ 428 \\ 431 \end{array}$ | $\begin{aligned} & \hline 426 \\ & 428 \end{aligned}$ | $\begin{aligned} & 433 \\ & 435 \end{aligned}$ | $\begin{aligned} & 436 \\ & 437 \end{aligned}$ | $\begin{aligned} & 539 \\ & 541 \end{aligned}$ | $\begin{array}{\|l\|} \hline 438- \\ 443 \\ 455 \\ 530 \end{array}$ | $\begin{array}{\|l\|} \hline 354 \\ 438- \\ 440 \end{array}$ |
| $\begin{aligned} & \boldsymbol{\omega} \\ & \underset{\sim}{\infty} \end{aligned}$ | Simplicity of design |  | $\begin{aligned} & \hline 274 \\ & 311 \\ & 562 \end{aligned}$ | $\begin{array}{\|l\|} \hline 273 \\ 275 \\ \hline \end{array}$ | $\begin{aligned} & 275 \\ & 355 \end{aligned}$ | $\begin{aligned} & 277 \\ & 311 \end{aligned}$ | $\begin{aligned} & 328 \\ & 330 \\ & 332 \end{aligned}$ |  | 302 | 356 | $\begin{aligned} & 356 \\ & 364 \end{aligned}$ | $\begin{aligned} & 356 \\ & 376 \\ & 387 \end{aligned}$ | $\begin{array}{\|l\|} \hline 269 \\ 356 \\ 384 \\ 392 \\ \hline \end{array}$ | $\begin{aligned} & 356 \\ & 406 \\ & 414 \end{aligned}$ | $\begin{aligned} & 356 \\ & 421 \end{aligned}$ | $\begin{aligned} & 356 \\ & 423 \end{aligned}$ | 356 | 356 | 356 | $\begin{aligned} & 356 \\ & 433 \end{aligned}$ | 356 | 540 | $\begin{aligned} & 439 \\ & 440 \\ & 531 \end{aligned}$ | $\begin{aligned} & 439 \\ & 440 \\ & 570 \end{aligned}$ |
|  | Space and weight requirements |  | $\begin{aligned} & 296 \\ & 304 \\ & 305 \\ & 308 \\ & 560 \\ & 582 \end{aligned}$ |  |  | $\begin{aligned} & 296 \\ & 308 \\ & 311 \\ & 566 \\ & 567 \end{aligned}$ | 339 |  |  | 364 | $\begin{aligned} & 369 \\ & 371 \end{aligned}$ | $\begin{array}{\|l\|} \hline 376 \\ 387 \\ 568 \end{array}$ | 392 | $\begin{aligned} & 406 \\ & 414 \end{aligned}$ |  |  |  |  |  |  |  | $\begin{aligned} & 541 \\ & 570- \\ & 572 \end{aligned}$ | 441 | 570 |
|  | Temperature range requirements |  | $\begin{aligned} & 304 \\ & 582 \end{aligned}$ |  |  | 277 |  | 349 | 353 | 357 | $\begin{array}{\|l\|} \hline 364 \\ 373 \end{array}$ | 387 |  | 414 |  |  |  |  |  |  |  | $\begin{array}{l\|} \hline 540 \\ 541 \\ 572 \end{array}$ |  |  |
|  | Versatility in application and design | (解 | $\begin{aligned} & 294 \\ & 306 \\ & 317 \\ & 562 \end{aligned}$ | 275 | $\begin{aligned} & 275 \\ & 355 \end{aligned}$ | $\begin{aligned} & 277 \\ & 294 \\ & 295 \\ & 317 \\ & 319- \\ & 327 \end{aligned}$ | $\begin{aligned} & 328 \\ & 339 \\ & 344 \end{aligned}$ | $\begin{aligned} & 349 \\ & 350 \end{aligned}$ | 353 | $\begin{aligned} & 356 \\ & 357 \end{aligned}$ | $\begin{aligned} & 356 \\ & 364 \\ & 369- \\ & 375 \end{aligned}$ | $\begin{aligned} & 356 \\ & 376 \\ & 387- \\ & 391 \end{aligned}$ | $\begin{aligned} & 356 \\ & 392 \\ & 404 \\ & 405 \end{aligned}$ | $\begin{aligned} & 356 \\ & 406 \\ & 417 . \\ & 420 \end{aligned}$ | $\begin{array}{\|l\|} \hline 356 \\ 421 \end{array}$ | $\begin{aligned} & 356 \\ & 423 \\ & 425 \end{aligned}$ | $\begin{aligned} & 356 \\ & 428 \\ & 429 \end{aligned}$ | $\begin{aligned} & 356 \\ & 428 \\ & 430 \\ & 431 \end{aligned}$ | $\begin{array}{\|l\|} \hline 356 \\ 428 \end{array}$ | $\begin{aligned} & 356 \\ & 433 \\ & 435 \end{aligned}$ | $\begin{aligned} & 356 \\ & 436 \\ & 437 \end{aligned}$ | $\begin{array}{l\|} \hline 539 \\ 541 \end{array}$ | 439 4440 442 443 455 508 530 | $\begin{aligned} & 439 \\ & 440 \\ & 570 \end{aligned}$ |
|  | Bibliography numbers | 211 | $\begin{gathered} 10 \\ 91 \\ 141 \\ 147 \\ 149 \\ 211 \\ 212 \\ 213 \\ 231 \\ 289 \\ 426 \\ 493 \\ 494 \\ 525 \\ 678 \\ 697 \\ 840 \end{gathered}$ | $\begin{aligned} & 231 \\ & 781 \end{aligned}$ | $\begin{aligned} & 108 \\ & 127 \\ & 128 \\ & 212 \\ & 231 \end{aligned}$ | $\begin{array}{\|c\|} \hline 91 \\ 211 \\ 308 \\ 533 \\ 649 \\ 781 \end{array}$ | $\begin{gathered} 91 \\ 211 \\ 618 \\ 649 \\ 781 \end{gathered}$ |  | $\begin{aligned} & 129 \\ & 496 \\ & 840 \end{aligned}$ | $\begin{aligned} & 211 \\ & 231 \\ & 523 \end{aligned}$ | 653 | $\begin{array}{\|l} \hline 1.28 \\ 211 \\ 212 \\ 308 \\ 840 \end{array}$ | $\begin{aligned} & 211 \\ & 212 \\ & 308 \end{aligned}$ | $\begin{aligned} & 128 \\ & 211 \\ & 212 \end{aligned}$ | $\begin{array}{\|l\|} \hline 211 \\ 212 \\ \hline \end{array}$ | $\begin{aligned} & 211 \\ & 212 \end{aligned}$ | $\begin{aligned} & 211 \\ & 212 \end{aligned}$ | $\begin{array}{\|l\|} \hline 211 \\ 212 \end{array}$ | $\begin{aligned} & 211 \\ & 212 \end{aligned}$ | $\begin{aligned} & 211 \\ & 840 \end{aligned}$ | 89 | 151 | 329 | $\begin{aligned} & 777 \\ & 778 \\ & 779 \\ & 780 \\ & 781 \\ & 840 \end{aligned}$ |



|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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| 3 | -*Bibliography numbers |  | 211 |  |  |  |  |  |  |  | 211 |  | 212 |  |  |  |  |  |  |  |  |  |  |  |  |
| 앙 | - Negative-resistance method |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { 김 } \\ & \text { 品 } \end{aligned}$ | -*Qualitative discussion |  |  | $\left\lvert\, \begin{array}{l\|} 231- \\ 233 \\ 236 \\ 267 \end{array}\right.$ | $\begin{array}{\|l\|} \hline 231 \\ 233 \\ 586 \\ 595 \end{array}$ | $\begin{aligned} & 586 \\ & 595 \end{aligned}$ | $\begin{aligned} & 278 \\ & 280 \end{aligned}$ |  |  |  |  |  |  |  |  |  | 425 | 429 |  |  |  |  | 545 546 549 |  |  |
| O | *-Application illustrated |  |  |  | 233 |  | $\begin{array}{\|l\|} \hline 233 \\ 278 \\ 282 \end{array}$ | 233 |  |  |  |  | 378 |  |  |  | 425 | 429 |  |  |  |  | 547 |  |  |
|  | -*Bibliography numbers |  | 112 113 114 154 211 271 362 640 |  | $\begin{aligned} & 232 \\ & 532 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  | $\begin{array}{r} 113 \\ 554 \end{array}$ |  |  |  |  |  |  |  |  |
|  | - Nonlinear parameter method (Not used or discussed in this handbook.) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | **Bibliography numbers | $\begin{array}{l\|l} 428 \\ 535 \end{array}$ | $\begin{aligned} & 211 \\ & 466 \\ & 789 \end{aligned}$ | 843 |  |  | 843 | 843 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\omega$ | - Nyquist diagram method |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| * | - Brief mention |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 424 |  |  |  |  |  |  |  |  |
|  | *- Bibliography numbers |  | $\left[\begin{array}{c} 60 \\ 211 \\ 571 \\ 815 \end{array}\right]$ | 212 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Phasor (vector) method |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | **Qualitative discussion |  | $\left\|\begin{array}{l} 267- \\ 273 \end{array}\right\|$ | $\left\|\begin{array}{l} 267- \\ 273 \end{array}\right\|$ | $\begin{aligned} & 268-1 \\ & 273 \end{aligned}$ |  | $\begin{aligned} & 280 \\ & 282 \\ & 283 \end{aligned}$ | $\begin{array}{\|l\|l} 330 \\ 332 \end{array}$ | $\left\lvert\, \begin{aligned} & 345 \\ & 347 \end{aligned}\right.$ |  | 358 |  |  |  |  |  | - |  |  |  |  |  |  |  |  |
|  | $\cdots$ Application illustrated |  | $\left\|\begin{array}{l} 268 \\ 272 \\ 281 \end{array}\right\|$ |  | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ |  | 268 272 280 281 283 284 312 | $\left.\begin{aligned} & 268- \\ & 272 \\ & 281 \end{aligned} \right\rvert\,$ | $345$ |  | $\begin{array}{l\|l} 358 \\ 359 \end{array}$ | $\begin{aligned} & 268 \\ & 272 \end{aligned}$ |  |  |  |  |  |  | $\begin{aligned} & 268- \\ & 272 \\ & 281 \end{aligned}$ | $\begin{aligned} & 268 \\ & 272 \\ & 281 \end{aligned}$ |  | $\begin{aligned} & 268- \\ & 272 \\ & 281 \end{aligned}$ |  |  | $268-$ 272 281 |
|  | -*Bibliography numbers |  | 332 | $\begin{gathered} 70 \\ 232 \\ \hline \end{gathered}$ |  |  | $\begin{gathered} 70 \\ 232 \end{gathered}$ | $\begin{gathered} 70 \\ 232 \end{gathered}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | Amplitude considerations |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Derivation of loop-gain equation |  |  |  |  |  | $\begin{array}{r} 284 \\ 289 \end{array}$ | $\begin{aligned} & 289 \\ & 331 \\ & 336 \end{aligned}$ | 348 |  | $\begin{aligned} & 359 \\ & 360 \\ & 363 \end{aligned}$ |  | $\begin{array}{l\|l} 378 \\ 388 \end{array}$ | $\begin{aligned} & 395 \\ & 396 \end{aligned}$ | $410$ |  | $\begin{array}{r} 424 \\ 425 \end{array}$ | $\begin{aligned} & 425 \\ & 426 \end{aligned}$ | $\begin{aligned} & 289 \\ & 426 \\ & 427 \end{aligned}$ | $\begin{aligned} & 289 \\ & 331 \\ & 426 \\ & 427 \end{aligned}$ | 434 | $\begin{array}{r} 289 \\ 436 \end{array}$ | 548 | , | 289 436 |



|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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|  | - Amplitude variation with effective resistance of crystal unit |  |  | $\begin{aligned} & 226 \mu \\ & 237 \\ & 294 \\ & 300 \\ & 308 \\ & 309 \end{aligned}$ | $\begin{aligned} & 214 \\ & 230- \\ & 237 \end{aligned}$ | 225 | $\left\|\begin{array}{l} 290 \\ 293- \\ 295 \\ 300- \\ 303 \\ 308 \\ 309 \\ 312- \\ 316 \end{array}\right\|$ | $\begin{array}{\|} 336 \\ 343 \end{array}$ |  |  | $\begin{aligned} & 361 \\ & 362 \end{aligned}$ |  | $\left\lvert\, \begin{aligned} & 379 \\ & 387 \end{aligned}\right.$ | $401-$ | $\begin{aligned} & 411- \\ & 413 \\ & 415 \end{aligned}$ |  |  |  |  |  |  | 436 | 540 |  | 436 |
|  | *Amplitude variation with frequany |  |  | $\begin{aligned} & 301 \\ & 303 \end{aligned}$ |  |  | 291 295 301 303 | $\begin{aligned} & 336 \\ & 340 \\ & 343 \end{aligned}$ |  |  |  | $\left\|\begin{array}{l} 366- \\ 368 \\ 371 \\ 372 \end{array}\right\|$ |  | 405 |  |  |  |  |  |  |  |  | $\begin{aligned} & 543 \\ & 544 \end{aligned}$ |  |  |
|  | - Amplitude variation with load |  |  | 294 | 214 |  | $\begin{aligned} & 284 \\ & 286 \\ & 295 \\ & 312- \\ & 316 \end{aligned}$ | $\begin{aligned} & 389 \\ & 340 \end{aligned}$ |  |  |  |  | $\begin{aligned} & 387 \\ & 388 \end{aligned}$ | $\begin{aligned} & 401- \\ & 403 \end{aligned}$ | $\begin{aligned} & 4111 \\ & 413 \\ & 415 \end{aligned}$ |  |  |  |  |  |  | 436 | 540 |  | 436 |
|  | - Derivation of amplitude-stability equation |  |  |  |  |  |  |  |  |  | 360 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \boldsymbol{\omega} \\ \underset{\sim}{\infty} \end{gathered}$ | - Amplitude-stability equation |  |  |  |  |  |  | . |  |  | $\begin{gathered} 360 \\ 6, \\ 10, \\ 11, \\ 12, \\ 13, \\ 14, \\ 18) \end{gathered}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Interpretation of amplitudestability equation and/or discussion of basic requirements for optimum amplitude stability |  | $\begin{aligned} & 267 \\ & 294 \\ & 306 \end{aligned}$ | $\begin{aligned} & 294 \\ & 296 \\ & 299 \\ & 300 \\ & 306 \\ & 308 \end{aligned}$ | 273 |  | $\begin{aligned} & 284 \\ & 291 \\ & 294 \\ & 296 \\ & 299 \\ & 300 \\ & 308 \end{aligned}$ | $\begin{aligned} & 340 \\ & 343 \end{aligned}$ |  | 352 | $\begin{aligned} & 357 \\ & 360- \\ & 363 \end{aligned}$ | $\left.\begin{aligned} & 368 \\ & 370- \\ & 372 \end{aligned} \right\rvert\,$ | 379 | $401-$ | $\begin{aligned} & 412 \\ & 413 \\ & 415 \end{aligned}$ |  |  |  |  |  |  |  | 540 |  |  |
|  | Frequency considerations |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | -Qualitative analysis and sirmplification of loop-phase requirements |  | $\begin{aligned} & 267 \\ & 273 \end{aligned}$ |  | 269 |  | $\begin{aligned} & 268 \\ & 273 \\ & 280 \\ & 282 \\ & 283 \\ & 289 \end{aligned}$ | $\begin{aligned} & 268 \\ & 273 \\ & 328 \\ & 332 \end{aligned}$ | $\begin{aligned} & 269 \\ & 346 \\ & 347 \end{aligned}$ | 351 | 357 | $\left\|\begin{array}{l} 268 \\ 273 \\ 365- \\ 368 \end{array}\right\|$ | $\begin{aligned} & 380 \\ & 388 \end{aligned}$ | $\begin{aligned} & 267 \\ & 269 \\ & 393 \\ & 394 \end{aligned}$ | $\begin{aligned} & 407 \\ & 409 \end{aligned}$ | $\begin{aligned} & 380 \\ & 383 \\ & 421 \\ & 422 \end{aligned}$ | $\begin{aligned} & 423 \\ & 424 \end{aligned}$ | $\begin{aligned} & 423 \\ & 424 \\ & 429 \end{aligned}$ | $\begin{aligned} & 268- \\ & 273 \\ & 427 \\ & 430 \\ & 431 \end{aligned}$ | $\begin{aligned} & 268- \\ & 273 \\ & 427 \\ & 432 \end{aligned}$ | $\begin{aligned} & 269 \\ & 433 \end{aligned}$ | $\begin{gathered} 268 \\ 273 \\ 436 \end{gathered}$ | 540 | 440 | $\begin{aligned} & 268 \\ & 273 \\ & 440 \end{aligned}$ |
|  | - Derivation of loop-phase equation |  | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ |  | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ |  | $\left(\left.\begin{array}{l} 270 \\ 272 \\ 281 \\ 289 \end{array} \right\rvert\,\right.$ | $\begin{aligned} & 270 \\ & 272 \\ & 281 \\ & 289 \\ & 331 \end{aligned}$ |  |  |  |  | 383 |  |  | 383 | 424 | 424 | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ |  | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ | 548 |  | $\begin{aligned} & 270 \\ & 272 \\ & 281 \end{aligned}$ |



| DESIGN OF CRYSTAI oscillators |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Circuits specifically designed for use with currently recommended Military Standard Crystal Units (Figure numbers) |  |  |  |  |  | $\begin{array}{\|l\|} 143 \\ 2-44 \\ \hline \end{array}$ | $\begin{array}{\|l\|} 2-50 \\ 2-52 \end{array}$ |  |  |  | 175 <br> (A-F, <br> H-L) <br> 250 <br> $2-4$ <br> $2-8$ <br> $2-10$ <br> $2-10$ <br> $2-20$ <br> $2-24$ <br> $2-26$ <br> $2-30$ <br> $2-38$ <br> $2-40$ <br> $2-66$ | $\begin{array}{\|c\|} \hline 177 \\ (\mathrm{D}) \\ 2-60 \\ 2-64 \\ 2-68 \end{array}$ | $\begin{array}{\|l\|} \hline \frac{2-12}{2-62} \end{array}$ |  | $\left\lvert\, \begin{array}{c\|} \hline 2-14 \\ 2-16 \\ 2-48 \end{array}\right.$ |  |  |  | $\begin{array}{\|l\|} \hline 2-34 \\ 2-36 \\ 2-42 \\ 2-58 \end{array}$ | $\begin{array}{\|c} 185 \\ \text { (A- } \\ \text { C) } \end{array}$ |  | $\begin{array}{\|l\|} \hline 192 \\ 196 \\ 199- \\ 203 \\ 205- \\ 217 \\ \hline \end{array}$ | $\begin{aligned} & 185 \\ & \hline \text { (A. } \\ & \text { C) } \end{aligned}$ |
| Circuits adaptable, but not specifically designed, for use with currently recommended crystal units (Figure numbers) |  |  |  |  | 131 <br> 135 <br> (A-K, <br> N-Q, <br> $\mathrm{X})$ <br> 136 <br> 137 <br> (C,D, <br> F,H- <br> F M$)$ <br> 138 <br> (B,C) | $\begin{aligned} & 142 \\ & 149 \\ & 150 \\ & 151 \\ & 152 \\ & 153 \\ & 186 \end{aligned}$ | 155 | $\left\lvert\, \begin{aligned} & 157 \\ & 158 \end{aligned}\right.$ | $\begin{aligned} & 163 \\ & 164 \end{aligned}$ | $\left\lvert\, \begin{gathered} 167 \\ 168 \\ 169 \\ 170 \\ 171 \\ 172 \end{gathered}\right.$ | $\begin{aligned} & 174 \\ & 175 \\ & (\mathrm{G}) \end{aligned}$ | $\begin{aligned} & 177 \\ & (A-2 \\ & \mathrm{C}) \end{aligned}$ | 179 | 180 | 161 | $\begin{aligned} & 182 \\ & (\mathrm{~B}) \end{aligned}$ | $\begin{array}{\|c\|} \hline 182 \\ (C, \\ D) \\ \hline \end{array}$ | $\begin{aligned} & 182 \\ & (\mathrm{E}) \end{aligned}$ | $\begin{aligned} & 183 \\ & 184 \end{aligned}$ | $\begin{array}{\|l\|l} \hline 106 \\ 185 \\ (10 \\ \text { E) } \\ \hline \end{array}$ | 222 224 227 232 $(B)$ 233 234 236 238 240 254 256 257 | $\begin{array}{\|l\|} \hline 186 \\ 187 \\ 188 \\ 191 \\ 220 \\ 221 \\ \hline \end{array}$ | $\begin{aligned} & \hline 106 \\ & 159 \\ & 186 \\ & 187 \\ & 254 \end{aligned}$ |
| Design procedure | 267 | $\begin{aligned} & 304 \\ & 322 \end{aligned}$ | 317 |  | $\begin{aligned} & 278 \\ & 290 \\ & 291 \\ & 293 \\ & 295 \\ & 303 \\ & 308 \\ & 311 \end{aligned}$ | 332 334 336 337 339 | 348 | 352 | 362 | $\begin{aligned} & 368 \\ & 369 \end{aligned}$ | $\begin{aligned} & 379 \\ & 381 \\ & 387 \end{aligned}$ | $\begin{array}{\|l\|} \hline 396- \\ 403 \end{array}$ | $\begin{aligned} & 411- \\ & 415 \end{aligned}$ | 422 |  | $\begin{aligned} & 426 \\ & 427 \end{aligned}$ | $\begin{aligned} & 426 \\ & 427 \end{aligned}$ | ${ }_{427}^{426}$ | $\begin{aligned} & 433 \\ & 434 \end{aligned}$ | 436 | 546 | $\begin{aligned} & 438 \\ & 443 \end{aligned}$ | $\begin{aligned} & 436 \\ & 438 \end{aligned}$ |
| Design procedure illustrated |  |  |  |  | $\begin{aligned} & 311- \\ & 316 \end{aligned}$ | 336 |  | 352 |  | 371 |  | 404 | $\begin{aligned} & 414- \\ & 420 \end{aligned}$ | $\begin{aligned} & 421 \\ & 422 \end{aligned}$ |  | 429 | 430 | 432 |  |  |  | $\begin{array}{\|l\|} 439 \\ 443 \\ 447 \end{array}$ | 439 |
| Bibliography numbers | $\begin{aligned} & 211 \\ & 466 \end{aligned}$ | $\begin{array}{\|l\|} \hline 108 \\ 149 \\ 212 \\ 213 \\ 678 \\ 781 \\ 840 \end{array}$ | 781 | $\begin{aligned} & 108 \\ & 212 \end{aligned}$ | $\begin{gathered} 91 \\ 149 \\ 211 \\ 212 \\ 533 \\ 649 \end{gathered}$ | 91 211 212 618 649 |  | 840 | $\begin{aligned} & 211 \\ & 523 \end{aligned}$ | 653 | $\begin{aligned} & 128 \\ & 211 \\ & 212 \end{aligned}$ | $\begin{array}{\|} 211 \\ 212 \end{array}$ | $\begin{aligned} & 211 \\ & 212 \end{aligned}$ | 212 | $\begin{aligned} & 113 \\ & 211 \\ & 212 \\ & 554 \end{aligned}$ | $\frac{211}{212}$ | 212 | 212 | $\left\lvert\, \begin{aligned} & 211 \\ & 840 \end{aligned}\right.$ | $\begin{array}{\|} 89 \\ 211 \\ 840 \end{array}$ | 151 | 329 | $\begin{aligned} & 89 \\ & 211 \\ & 697 \\ & 840 \end{aligned}$ |




|  |  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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| $\underset{\delta}{\Sigma}$ | CRYSTAL OSCILIATOR DESIOI CONSIDERATONS (COMEF: ad) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \vec{x} \\ & \text { n } \\ & o \\ & \frac{1}{n} \\ & \frac{1}{n} \end{aligned}$ | Amplitude | 268 294 306 | 249 <br> 294 <br> 296 <br> 304 <br> 305 <br> 308 <br> 311 <br> 315 <br> 322 | 275 | $\begin{aligned} & 275 \\ & 355 \end{aligned}$ | $\begin{array}{\|l\|} \hline 277 \\ 278 \\ 282 \\ 284 \\ 286 \\ 291 \\ 293- \\ 296 \\ 308- \\ 318 \\ 322 \\ 5666 \\ 567 \end{array}$ | $\begin{array}{\|l} 322 \\ 328 \\ 333 \\ 336 \\ 339 \\ 340 \end{array}$ | $\begin{aligned} & 348 \\ & 349 \end{aligned}$ | 352 | $\begin{array}{l\|} \hline 356 \\ 360- \\ 362 \end{array}$ | $\begin{aligned} & 356 \\ & 365 \\ & 368 \\ & 370 \\ & 371 \end{aligned}$ | $\begin{aligned} & 356 \\ & 376 \\ & 379 \\ & 387 \\ & 388 \\ & 568 \end{aligned}$ | 356 392 397 $399-1$ 405 | $\left.\begin{array}{\|l\|} 356 \\ 406 \\ 411- \\ 420 \end{array} \right\rvert\,$ | $\begin{aligned} & 356 \\ & 421 \end{aligned}$ | 356 | $\begin{array}{r} 356 \\ 429 \end{array}$ | $\begin{aligned} & 356 \\ & 430 \\ & 431 \end{aligned}$ | $\begin{aligned} & 356 \\ & 432 \end{aligned}$ | $\begin{aligned} & 356 \\ & 434 \end{aligned}$ | $\begin{aligned} & 356 \\ & 436 \end{aligned}$ | $\begin{aligned} & 540 \\ & 541 \\ & 572 \end{aligned}$ | $\begin{aligned} & 438 \\ & 454 \\ & 527 \end{aligned}$ | 438 |
|  | Amplitude range | 294 | $\begin{array}{\|l\|} \hline 308- \\ 310 \end{array}$ |  | 355 | 291 295 308 330 312 322 366 566 567 | $\begin{aligned} & 336 \\ & 339 \end{aligned}$ | $\begin{array}{r} 348 \\ 349 \end{array}$ | 352 | $\begin{aligned} & 361 \\ & 362 \end{aligned}$ | $\begin{aligned} & 366 \\ & 368 \\ & 871 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 376 \\ 379 \\ 568 \end{array} \end{aligned}$ |  | $\begin{array}{\|l\|} 4112 \\ 415 \end{array}$ | 421 |  |  | 431 |  |  |  | $\begin{aligned} & 540 \\ & 540 \\ & 51 \end{aligned}$ | 527 |  |
| $\begin{aligned} & \text { L } \\ & \hline 8 \end{aligned}$ | *Expected, due to variation in effective resistance of crystal unit |  |  <br> 232 <br> 249 <br> $300-$ <br> 303 <br> 308 <br> 309 | $\begin{array}{\|l\|} 233 \\ 237 \end{array}$ |  | 233 237 290 294 295 $300-$ 303 308 309 $312-$ 316 | $\begin{aligned} & 233 \\ & 237 \\ & 308 \\ & 336 \\ & 343 \end{aligned}$ |  |  | $\begin{aligned} & 361 \\ & 362 \end{aligned}$ |  | $\begin{aligned} & 379 \\ & 387 \end{aligned}$ | $\begin{aligned} & 401 \\ & 402 \end{aligned}$ | $\begin{array}{\|c\|} 412- \\ 415 \end{array}$ |  |  |  |  |  |  | 436 |  |  | 436 |
|  | - Limitations of, due to specified drive level of crystal unit |  | $\begin{aligned} & 258 \\ & 294 \\ & 311 \end{aligned}$ |  |  | 277 282 284 286 290 $293-$ 295 $301-$ 303 $311-$ 316 | $\begin{array}{\|l\|} \hline 328 \\ 3366 \\ 339 \\ 344 \end{array}$ |  |  | $\begin{aligned} & 361 \\ & 362 \end{aligned}$ | 370 | $\begin{array}{\|} 379 \\ 387 \end{array}$ | $\begin{array}{\|l\|} \hline 397 \\ 401- \\ 404 \end{array}$ | $\begin{aligned} & 412 \\ & 413 \\ & 415 \\ & 416 \end{aligned}$ |  |  |  |  |  | 434 |  |  |  |  |
|  | - Of fully loaded circuit |  | 309 |  |  | $\begin{aligned} & 286 \\ & 295 \\ & 309 \end{aligned}$ | $\begin{aligned} & 339 \\ & 340 \end{aligned} .$ | 349 |  |  | $\begin{array}{\|l} 370 \\ 372 \end{array}$ | 387 |  | $\left\lvert\, \begin{array}{\|c\|} 417- \\ 420 \end{array}\right.$ |  |  |  |  |  |  |  |  |  |  |
|  | - Of nonloaded circuit |  |  |  |  | $\begin{aligned} & 278 \\ & 284 \\ & 286 \\ & 293 \\ & 295 \\ & 312- \\ & 316 \end{aligned}$ | $\begin{array}{\|l\|} 336 \\ 340 \end{array}$ |  |  | 362 | $\begin{aligned} & 366 \\ & 370 \\ & 371 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  | 438 | 438 |


|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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| 2 | -With antomatic gain control |  |  | 308 |  |  | 308 315 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 081 0 0 0 0 0 | -With manual gain control |  |  | $301-$ 303 311 |  |  | $\begin{aligned} & 291 \\ & 294 \\ & 295 \\ & 301- \\ & 303 \\ & 311 \\ & 318 \end{aligned}$ | $\begin{aligned} & 337 \\ & 340 \end{aligned}$ |  |  |  | 366 | 387 | , |  |  |  |  |  |  |  |  |  |  |  |
|  | -With no gain control |  |  |  |  |  | $\begin{aligned} & 286 \\ & 293 \\ & 295 \\ & 312- \\ & 315 \end{aligned}$ |  |  |  |  |  | $\begin{aligned} & 379 \\ & 387 \end{aligned}$ | 402 | $\begin{aligned} & 412 \\ & 413 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |
|  | - With overdrive of crystal unit |  |  | 339 |  |  |  | 339 |  |  |  | 372 |  |  | 416 |  |  |  |  |  |  |  |  |  |  |
|  | Amplitude stability | $\begin{aligned} & 263 \\ & 265 \\ & 266 \end{aligned}$ | 294 | 294 |  |  | $\begin{aligned} & 283 \\ & 284 \\ & 294 \end{aligned}$ |  |  |  | $\begin{aligned} & 357 \\ & 360 \\ & 361 \end{aligned}$ | 368 |  | 393 |  |  |  |  |  |  |  |  |  |  |  |
|  | - Under variations of load | 265 |  | $\begin{aligned} & 315 \\ & 322 \end{aligned}$ | $\begin{array}{l\|} 212 \\ 214 \end{array}$ |  | $\begin{aligned} & 291 \\ & 312 \\ & 315 \\ & 321 \\ & 322 \\ & 326 \end{aligned}$ | 340 |  | 352 |  |  |  | $\left\lvert\, \begin{aligned} & 401 \\ & 402 \end{aligned}\right.$ | $\begin{aligned} & 411 \\ & 412 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |
| 9 | -With automatic gain control |  |  | 308 315 |  |  | $\begin{aligned} & 308 \\ & 315 \end{aligned}$ | 308 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | -- |
|  | -With gridleak bias |  | 306 | $\begin{aligned} & 296 \\ & 297 \\ & 299- \\ & 303 \end{aligned}$ |  |  | $\begin{aligned} & 296 \\ & 297 \\ & 299- \\ & 303 \end{aligned}$ |  |  |  |  |  | 379 |  | 412 |  |  |  |  |  |  |  |  |  |  |
|  | - With grid limiting |  | 294 | 214 | 273 |  | 294 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - With load electron-coupled |  |  | 322 |  |  | 322 |  |  |  |  | 375 |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - With tri-tet operation |  |  | $\begin{aligned} & 214 \\ & 322 \end{aligned}$ |  |  | $\begin{aligned} & 321 \\ & 322 \end{aligned}$ | 322 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - With variation in gain of stage |  |  |  |  |  |  |  |  |  | 360 | 373 | 379 |  |  |  |  |  |  |  |  |  | 540 |  |  |
|  | Bandwidth |  | 354 |  |  | 355 | $\begin{aligned} & 295 \\ & 566 \\ & 567 \end{aligned}$ | 344 | 347 | $\begin{aligned} & 351 \\ & 352 \end{aligned}$ | $\begin{aligned} & 356 \\ & 357 \\ & 363 \end{aligned}$ | $\begin{aligned} & 356 \\ & 370- \\ & 375 \end{aligned}$ | $\begin{aligned} & 356 \\ & 376 \\ & 381 \\ & 568 \end{aligned}$ | $\left\|\begin{array}{l} 356 \\ 404 \\ 405 \end{array}\right\|$ | $\begin{aligned} & 356 \\ & 406 \end{aligned}$ | 356 | 356 | $\begin{aligned} & 356 \\ & 428 \end{aligned}$ | $\begin{aligned} & 356 \\ & 428 \end{aligned}$ | $\begin{aligned} & 356 \\ & 428 \end{aligned}$ | $\begin{aligned} & 356 \\ & 433 \end{aligned}$ | 356 | 539 | $\begin{aligned} & 455 \\ & 525- \\ & 529 \end{aligned}$ | 220 354 |
| - | - Broad-band circuit |  |  | $\begin{aligned} & 247 \\ & 309 \\ & 310 \\ & 311 \\ & 322 \end{aligned}$ | 275 | $\begin{aligned} & 275 \\ & 355 \end{aligned}$ | 277 278 309 310 311 322 323 | * | - |  |  | 374 | $\begin{aligned} & 376 \\ & 377 \\ & 381- \\ & 385 \\ & 387 \end{aligned}$ | $\begin{aligned} & 392 \\ & 398 \\ & 402 \\ & 404 \\ & 405 \end{aligned}$ | $\begin{aligned} & 406 \\ & 418 \end{aligned}$ |  | $\begin{aligned} & 423 \\ & 425 \end{aligned}$ |  |  |  | 433 |  |  | $\begin{aligned} & 438- \\ & 440 \end{aligned}$ | 438 400 . |



|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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| 3 8 8 8 8 | -Class C |  | 294 | $\begin{aligned} & 296 \\ & 299 \\ & 300 \\ & 311 \end{aligned}$ | 273 |  | 282 <br> 284 <br> 293 <br> 294 <br> 296 <br> 311 <br> 312 | $\begin{aligned} & 337 \\ & 339 \end{aligned}$ |  |  |  |  | $\begin{aligned} & 376 \\ & 387 \\ & 388 \end{aligned}$ | $\begin{aligned} & 392 \\ & 401- \\ & 403 \end{aligned}$ | $\begin{aligned} & 406 \\ & 420 \end{aligned}$ | 421 |  |  |  |  |  | 437 |  | 438 | 488 |
| $\overline{\mathrm{n}}$ | -"Class D" |  | 298 | 298 |  |  | 298 | 342 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Effect of crystal resistance |  |  | . | 275 |  | $\begin{aligned} & 297 \\ & 312- \\ & 316 \end{aligned}$ |  |  |  | , |  |  |  |  |  |  |  |  |  |  | 220 |  |  |  |
|  | - Effect of gridleak resistance |  | 306 | $\begin{aligned} & 282 \\ & 296- \\ & 298 \\ & 307 \\ & 308 \end{aligned}$ |  |  | $\begin{aligned} & 282 \\ & 296- \\ & 308 \\ & 313 \end{aligned}$ | 341 |  |  |  |  | 379 |  |  |  |  |  |  |  |  |  |  |  |  |
|  | - Fixed |  | 294 | $\begin{aligned} & 294 \\ & 296 \\ & 300 \\ & 305 \end{aligned}$ | $\begin{aligned} & 271 \\ & 273 \end{aligned}$ |  | $\begin{aligned} & 294- \\ & 296 \end{aligned}$ | 339 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | -For frequency multiplication |  |  | 322 |  |  | 322 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 474 \\ & 537 \end{aligned}$ |  |
| $\begin{aligned} & \dot{\otimes} \\ & \dot{8} \end{aligned}$ | -Gridleak |  | 306 | $\begin{aligned} & 296- \\ & 308 \end{aligned}$ | 278 |  | $\begin{array}{\|l\|} \hline 282 \\ 286 \\ 293 \\ 295 \\ 316 \end{array}$ | $\begin{aligned} & 339 \\ & \mathbf{3 4 3} \end{aligned}$ |  | 352 |  |  | $\begin{aligned} & 379 \\ & 382 \\ & 388 \end{aligned}$ | 405 | $\begin{aligned} & 411 \\ & 412 \end{aligned}$ |  |  |  |  |  |  | 220 |  | $\begin{aligned} & 474 \\ & 537 \end{aligned}$ | 220 |
|  | - Limitations of, due to specified crystal drive level |  |  | 294 |  |  | $\left\|\begin{array}{l} 282 \\ 293- \\ 293 \\ 303 \\ 312- \\ 316 \end{array}\right\|$ | 339 |  |  |  |  | 379 |  | $\begin{aligned} & 412 \\ & 415 \end{aligned}$ |  |  |  |  |  |  | $\begin{aligned} & 220- \\ & 224 \end{aligned}$ |  |  | $\begin{aligned} & 220- \\ & 224 \end{aligned}$ |
|  | -Reactance tube (afc) |  |  |  |  |  |  |  | 350 |  |  |  |  |  |  |  |  |  |  |  |  | 437 |  | $\begin{array}{r} 484 \\ 492 \end{array}$ |  |
|  | Build-up of ascillations | 266 | $\begin{aligned} & 267 \\ & 268 \\ & 294 \end{aligned}$ | $\begin{aligned} & 232 \\ & 236 \\ & 275 \\ & 294 \\ & 296 \\ & 299 \\ & 304 \\ & 305 \end{aligned}$ | $\begin{array}{\|l\|} \hline 232 \\ 236 \\ 273 \\ 276 \\ 308 \\ 5866 \\ 595 \end{array}$ | $\begin{aligned} & 355 \\ & 586- \\ & 595 \end{aligned}$ | $\begin{array}{\|l\|} \hline 294 \\ 296 \\ 299 \\ 308 \\ 315 \end{array}$ | $\begin{aligned} & 337 \\ & 339 \\ & 340 \end{aligned}$ | 348 |  | $\begin{aligned} & 357 \\ & 363 \end{aligned}$ | $\begin{aligned} & 364- \\ & 367 \end{aligned}$ | $\begin{aligned} & 377 \\ & 379 \end{aligned}$ | 401 | 411 |  | 425 | 429 |  |  | 434 |  | 540 | 455 <br> 484 <br> 489 <br> 532- <br> 585 <br> 537 |  |
|  | Buffer amplifier |  |  | $\begin{aligned} & 304 \\ & 305 \\ & 308 \end{aligned}$ |  |  | 304 305 308 323 |  |  |  |  |  |  |  |  |  |  |  |  |  | . |  |  | $\begin{aligned} & 522 \\ & 538 \end{aligned}$ |  |
|  | Capacitance |  |  |  |  |  | 290 <br> 291 |  |  |  |  | $\begin{aligned} & 365 \cdot \\ & 368 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |












|  |  | 1 | 23 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
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| 3 | CRYSTA: OSCHLATOR OESIGN CONSIDERATIONS (Continued) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & 70 \\ & 0 \\ & \text { un } \\ & 0 \\ & i \end{aligned}$ | - Effect on feedback Q ( $\left.Q_{i}\right)$ |  |  | $\begin{aligned} & 233 \\ & 244 \\ & 270- \\ & 273 \end{aligned}$ |  | $\begin{aligned} & 279 \\ & 281 \\ & 289 \\ & 297 \\ & 298 \end{aligned}$ | 332 | 348 |  |  |  |  |  |  |  |  |  |  |  |  |  | 556 |  |  |
|  | - Effect on frequency stability |  | $\begin{aligned} & 250^{\circ} \\ & 597 \end{aligned}$ | $\begin{aligned} & 210 \\ & 212 \\ & 214 \end{aligned}$ | $\begin{aligned} & 206 \\ & 207 \\ & 240- \\ & 242 \end{aligned}$ | $\begin{array}{\|l} 279 \\ 281 \end{array}$ | $\begin{aligned} & 332 \\ & 333 \end{aligned}$ | 348 |  | 359 | 368 | 376 | $\begin{aligned} & 396 \\ & 399 \end{aligned}$ | $\begin{aligned} & 406 \\ & 418- \\ & 415 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |
|  | - Expected range of values |  | $\begin{aligned} & 199 \\ & 200 \\ & 202 \\ & 205 \\ & 209 \\ & 294 \end{aligned}$ | $\left\lvert\, \begin{aligned} & 217 \\ & 271 \end{aligned}\right.$ |  | 278 290 294 295 300 301 $312-$ 316 | $\begin{array}{r} 332 \\ 336 \\ 339 \\ 343 \end{array}$ | 348 |  | $\begin{aligned} & 361 \\ & 362 \end{aligned}$ |  | $\begin{array}{r} 379 \\ 387 \end{array}$ | $\begin{aligned} & 401 \\ & 402 \end{aligned}$ | 412 414 416 | 422 | 425 |  |  |  |  |  | $\begin{array}{r} 549 \\ 551 \end{array}$ |  |  |
| $\stackrel{8}{8}$ | -Maximum value |  | $\begin{aligned} & 216 \\ & 300 \\ & 303 \end{aligned}$ | $\begin{aligned} & 271 \\ & 584 \end{aligned}$ | 584 | 278 285 290 293 295 300 303 $312-$ 316 | $\begin{array}{r} 333 \\ 339 \end{array}$ | 348 | 353 | 362 |  | $\begin{aligned} & 379 \\ & 385 \\ & 387 \end{aligned}$ | $\begin{aligned} & 401- \\ & 403 \end{aligned}$ | $\begin{array}{\|l} 411- \\ 415 \end{array}$ |  |  |  |  |  | $\begin{aligned} & 433 \\ & 434 \end{aligned}$ |  |  |  |  |
|  | - Minimum expected value |  | $\begin{aligned} & 199 \\ & 200 \end{aligned}$ | 271 |  | $\begin{aligned} & 290 \\ & 295 \\ & 301 \\ & 312- \\ & 316 \end{aligned}$ |  |  |  | 362 |  | 379 | 401 | $\begin{aligned} & 412 \\ & 415 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |
|  | - Most probable value |  | $\begin{aligned} & 199 \\ & 200 \end{aligned}$ |  |  | 295 | 333 |  |  | 362 |  | 379 | $\begin{aligned} & 402 \\ & 403 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |
|  | - Reducing the effects of changes in |  | $254-$ 256 261 308 309 595 | $\begin{aligned} & 214 \\ & 271 \end{aligned}$ |  | $\begin{aligned} & 278 \\ & 295 \\ & 308 \\ & 309 \\ & 320 \end{aligned}$ | $\begin{array}{\|l} 332 \\ 333 \end{array}$ | 348 |  | $\begin{aligned} & 361 \\ & 362 \end{aligned}$ |  |  | $\begin{aligned} & 401 \\ & 402 \end{aligned}$ | $\begin{aligned} & 412 \\ & 413 \\ & 415 \end{aligned}$ |  |  |  |  |  |  | 436 | $\begin{aligned} & 553 \\ & 555- \\ & 559 \end{aligned}$ |  | 436 |
|  | Effciency of circuit |  | $\begin{aligned} & 248 \\ & 296 \end{aligned}$ | 276 |  | $\left\lvert\, \begin{aligned} & 284 \\ & 296 \\ & 312 \end{aligned}\right.$ | 339 | 349 |  |  |  | 376 | 405 | 420 |  |  |  |  |  |  |  | $\begin{aligned} & 541 \\ & 544 \end{aligned}$ |  |  |
|  | Electron-coupled circuits |  | $\begin{aligned} & 279 \\ & 322 \end{aligned}$ |  |  | $\begin{aligned} & 279 \\ & 322 \\ & 327 \\ & 567 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |







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| crystal osciliator design CONSIDERAYIONS (Continued) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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Crystal Unit CR-55/U ..... 500
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Crystal Unit CR-58/U ..... 506
Crystal Unit CR-59/U ..... 508
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# SECTION II-CRYSTAL UNITS 

## INTRODUCTION

2-1. Section II contains all available descriptions of crystal units now being used in USAF equipments. The crystal units are divided into two groups; as defined in subparagraphs a and $b$ below. Technical data charts present a convenient summary of the crystal units in each group, and following each of the charts are data sheets giving more complete information about the individual units. At the end of Section II is a digest of Military Standard terms, tests, and procedures applicable to crystal units which meet military specifications.
a. Group I includes those Military Standard crystal units that are recommended for use in equipments of new design. These are the crystal units assigned Joint Army-Navy-Air Force type number CR-XX/U, where XX is a two-digit number equal to 15 or higher. Except in the event of unusual or special requirements, the design engi-
neer of crystal-controlled circuits for military equipment should consider only those crystal units in Group I.
b. Group II includes the older types of crystal units which are still widely used in current models of USAF radio equipments, but which are not recommended for use in military equipments of new design. These crystal units are arranged in the order of their USAF stock numbers, which numbers are the same as the Signal Corps stock numbers except for the addition of the prefix " 2100 -," which serves to identify the item as belonging to the USAF 16-F stock class. The information concerning the Group-II crystal units is included primarily for the benefit of the crystal specialist or field engineer in the military. As a reference source of crystal units and available frequencies, it may also prove helpful to design and research engineers.

## GROUP I

## recommended military standard crystal units

The crystal units included in Group I are those conforming to Military Standards and which are recommended for use in armed-services equipment of new design. These units are further classified as belonging to one of two categories and are specified in Military Specification MLL-C-3098() -the latest issue or amendment in effect, as applicable.

Category 1 is composed of those crystal units which are available in production from two or more sources.

Category 2 is composed of those crystal units which are available in limited production and possibly from only one source. The crystal units in this category also may be individual types which are in the process of being replaced by units of new design, or which, at a later date, may be placed in Category 1 by virtue of increased utility and availability.


Section II
Crystal Units-Group I
TECHNICAL DATA CHART FOR GROUP-I MLLITARY STANDARD CRYSTAL UNITS

| Frequency Range (ke) | Frequency <br> Tolerance $( \pm \%)$ | Operating Temperature Ronge ( ${ }^{\circ} \mathrm{C}$ ) | Resonance | Load Capacitance (mmf) | Holder Type | Availabintity Category" | Crystal <br> Unit <br> Tupe |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 16-100 | 0.012 | -40 to +70 | parallel | $20 \pm 0.5$ | HC-13/U | 2 | CR-38/U |
| 16-100 | 0.012 | -40 to +70 | series | ... ......... | HC-13/U | 2 | CR-50/U |
| $\begin{gathered} 80.860 \\ (70-100) \end{gathered}$ | 0.010 | -30 to +75 | parallel | $45 \pm 1.0$ | $\mathrm{HC-16/U}$ | 2 | CR-43/U |
| 80-200 | 0.010 | -40 to +70 | parallel | $32 \pm 0.5$ | $\mathrm{HC-5} / \mathrm{U}$ | 1 | CR-15/U |
| 80-200 | 0.010 | -40 to +70 | series | ... ......... | $\mathrm{HC}-5 / \mathrm{U}$ | 1 | CR-16/U |
| $80-200$ | $0.002^{\text {b }}$ | $75 \pm 5$ | parallel | $32 \pm 0.5$ | HC-5/U | 1 | CR-29/U |
| 80.200 | $0.002^{\prime \prime}$ | $75 \pm 5$ | series | ... ............ | $\mathrm{HC-5/U}$ | 1 | CR-30/U |
| $90-250$. | 0.020 | -40 to +70 | parallel | $20 \pm 0.5$ | $\mathrm{HC-13/U}$ | 2 | CR-37/U |
| 90-250 | 0.003 | $75 \pm 5$ | parallel | $32 \pm 0.5$ | $\mathrm{HC}-13 / \mathrm{U}$ | 2 | CR-42/U |
| 160-330 | 0.008 | --55 to +75 | series | ع | $\mathrm{HC}-15 / \mathrm{U}$ | 2 | CR-39/U |
| 160-330 | $0.003^{\text {b }}$ | $70 \pm 5$ | series | * | $\mathrm{HC}-15 / \mathrm{U}$ | 2 | CR-40/U |
| $200-500$ | 0.010 | -40 to +70 | series | ......... . | $\mathrm{HC-6/U}$ | 1 | CR-25/U |
| $200-500$ | $0.002^{\text {b }}$ | $75 \pm 5$ | series | ..... | HC-6/U | 1 | CR-26/U |
| 200-500 | 0.010 | -40 to +70 | parallel | $20 \pm 0.5$ | $\mathrm{HC-6/U}$ | 2 | CR-46/U |
| 200-500 | $0.002^{\text {k }}$ | $75 \pm 5$ | parallel | $20 \pm 0.5$ | HC-6/U | 2 | CR-47/U |
| 455 | 0.020 | -40 to +70 | series | ......... | $\mathrm{HC}-6 / \mathrm{U}$ | 2 | CR-45/U |
| 500 | 0.001 | $85 \pm 5$ | parallel | $32 \pm 0.5$ | $\mathrm{HC-6} / \mathrm{U}$ | 1 | CR-57/U |
| 800.3000 | 0.0075 | -55 to +90 | parallel | $32 \pm 0.5$ | HC-6/U | 2 | CR-48/Ud |
| 800.3000 | 0.0075 | -55 to +90 | parallel | $32 \pm 0.5$ | HC-6/U | 2 | CR-49/Ud |
| 800-15,000 | $0.002^{\text {k }}$ | $75 \pm 5$ | parallel | $32 \pm 0.5$ | $\mathrm{HC}-6 / \mathrm{U}$ | 1 | CR-27/U |
| 800-20,000 | 0.002 | $85 \pm 5$ | parallel | $32 \pm 0.5$ | $\mathrm{HC}-6 / \mathrm{U}$ | 1 | CR-36/U |

Section II Crystal Units-Group I

| Frequency Range (kc) | Frequency <br> Tolerance $( \pm \%)$ | Operating Temperature Range ( ${ }^{\circ} \mathrm{C}$ ) | Resonance | Lond Capacitance (mmf) | Holder Type | Availability Category" | Crystal Unit Type |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 800-20,000 | 0.005 | -55 to +90 | parallel | $32 \pm 0.5$ | HC-6/U | 1 | CR-18/U |
| 800-20,000 | 0.005 | -55 to +90 | parallel | $32 \pm 0.5$ | HC-17/U | 1 | CR-58/U |
| 800-20,000 | 0.005 | -55 to +90 | series | $\cdots \cdots \cdots \cdots$ | $\mathrm{HC}-6 / \mathrm{U}$ | 1 | CR-19/U |
| 800-20,000 | $0.002^{\circ}$ | $75 \pm 5$ | series | .... .......... | $\mathrm{HC-6/U}$ | 1 | CR-28/U |
| 800-20,000 | $0.002^{\circ}$ | $85 \pm 5$ | series | .... . . . . . | $\mathrm{HC-6/U}$ | 1 | CR-35/U |
| 7000-20,000 | 0.065 | -55 to +105 | selies | ........ ... | HC-18/U | 1 | CR-60/U |
| 10,000-25,000 | 0.005 | -55 to +90 | parallel | $32 \pm 0.5$ | HC-6/U | 1 | CR-33/U |
| 10,000-61,000 | 0.005 | -55 to +90 | series | ... ....... | $\mathrm{HC-6/U}$ | 1 | CR-51/U |
| 10,000-61,000 | 0.005 | -55 to +00 | series | - | $\mathrm{HC}-6 / \mathrm{U}$ | 1 | CR-52/U |
| 10,000-75,000 | 0.005 | -55 to +90 | series | .... $\times$.. | HC-6/U | 2 | CR-23/Ue |
| 10,000-75,000 | $0.002^{\text {b }}$ | $75 \pm 5$ | series | ......... | $\mathrm{HC-6/U}$ | 1 | CR-32/U |
| 15,000-20,000 | $0.002^{\circ}$ | $85 \pm 5$ | parallel | $32 \pm 0.5$ | $\mathrm{HC-6/U}$ | 2 | CR-44/U' |
| 15,000-50,000 | 0.005 | -55 to +90 | series | ... .... ... | $\mathrm{HC}-10 / \mathrm{U}$ | 1 | CR-24, U |
| 17,000-61,000 | 0.005 | -55 to +105 | series | ............. | $\mathrm{HC}-18 / \mathrm{U}$ | 1 | CR-55/U |
| 25,000-58,000 | 0.002 | $85 \pm 5$ | series | …… | $\mathrm{HC}-18 / \mathrm{U}$ | 1 | CR-61/U |
| 50,000-87,000 | 0.005 | $-55+0+90$ | series | ... ........ | HC-6/U | 1 | CR-53/U |
| 50,000-87,000 | 0.005 | -55 to +90 | series | .... .. .. | $\mathrm{HC-6/U}$ | 1 | CR-54/U |
| 50,000-87,000 | 0.005 | -55 to +105 | series | .... .... | $\mathrm{HC}-18 / \mathrm{U}$ | 1 | CR-56/U |
| 50,000-91,000 | 0.002 | $85 \pm 5$ | series | .... | $\mathrm{HC-18/U}$ | 1 | CR-59/U |

- See explanation of categories in paragraphs immediately preceding this chart.

In addition, the crystal unit shall not deviate more than $0.0005 \%(0,0003 \%$ for $\mathrm{CR}-57 / \mathrm{U})$ from the frequency value measured at the midpoint of the operating temperature range, when measured over the entire operating temperature range.

- The permitted value of load capacitance for this crystal unit depends upon the frequency at which the unit is operated.
${ }^{\text {d }}$ For replacement use CR-18/U.
- For replacement use CR-52/U or CR-54/U whichever is applicable.
- For replacement use CR-36/U.

CRYSTAL UNIT CR-15/U (LF)


TOP


BOTTOM


Figure 2-1. Crystal Unit CR-15/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a plastic holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-frequency control element in circuits which must maintain good frequency stability in the absence of oven control, even when exposed to wide variations in temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 80 to 199.999 kc
Nominal Frequency Tolerance: $\pm 0.01 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonasce Resistance:

| Frequency (kc) | Resistance (ohms) |
| :---: | :---: |
| 80 to 119.999 | 10,000 |
| 120 to 159.999 | 8000 |
| 160 to 199.999 | 6000 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $D$, paragraph 1-116, figure 1-52.

TYPES OF CIRCUITS USED IN
Two-stage-grounded-cathode, modified transitron, Miller, modified Butler

## MOUNTING DATA

Crystal Holder: HC-5/U or HC-21/U
Method of Mounting Crystal: Wire-mounted in plastic holder
Dimensions and Marking: See figure 2-1(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF' Stock No.: 2100-2X515-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Use of this crystal is discouraged by some manufacturers because, in their opinion, the specified holder ( $\mathrm{HC}-5 / \mathrm{U}$ ) suffers these important disadvantages: The holder is not hermetically sealed (although a metal hermeticallysealed version will be used in procurement of further models) ; it has poor form factor; and it uses an unorthodox base which requires a special socket.


Figure 2-2. Schementic diagram of typical oscillator designed for use with Crystal Unit CR-15/U

Equipment Used In: Radio Receiver R-277/APN70

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and + rocedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Not applicable
Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test: Not required
Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams
80 to $119.999 \quad 1000$



CRYSTAL UNIT CR-16/U
(LF)

sortom


Figure 2-3. Crystol Unit CR-16/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a plastic holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-frequency control element in circuits which must maintain good frequency stability in the absence of oven control, even when exposed to wide sariations of temperature. The crystal unit is intended for operation at series resonance.

## Rated operating characteristics

Frequency Range: 80 to 199.999 kc
Nominal Frequency Tolerance: $\pm 0.01 \%$ at all temperatures within operating range
Frifuency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonance Resistance: 3000 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $D$, paragraph 1-116, figure 1-52.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, transitron, trans-former-coupled, modified Butler, and Meachambridge

## MOUNTING DATA

## Crystal Holder: HC-5/U or HC-21/U

Method of Mounting Crystal: Wire-mounted in plastic holder
Dimensions and Marking: See figure 2-3(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X516-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Use of this crystal unit is discouraged by some manufacturers because, in their opinion, the specified holder ( $\mathrm{HC}-5 / \mathrm{U}$ ) suffers these important disadvantages : The holder is not hermetically sealed (although a metal hermeticallysealed version will be used in procurement of future models) ; it has a poor form factor; and it uses an unorthodox base which requires a special socket.
Equipment Used In:
Signal Generator SG-34(XA)/UP-see figure 1-175 (K)


Figure 2-4. Schematic diagram of typical oscillotor designed for use with Crystal Unit CR-16/U

Signal Generator SG-34/GPM-15-see figure 1-175 (K)

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Not applicable Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test: Not required
Tensile Strength Test (Minimum Requirements):
Frequency (kc)
Grams

120 to 159.999 .......................................................... 800


## CRYSTAL UNIT CR-18/U (MF-HF)



Figure 2-5. Crystal Unit CR-18/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mathrm{mmf}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999 \mathrm{kc}-10 \mathrm{mw}$
10,000 to $20,000 \mathrm{kc}-5 \mathrm{mw}$
Maximum Pin-to-Pin Capacitance: 7.0 mmf

| Frequency | (kc) | Resistance (ahms) |
| :---: | :---: | :---: |
| 800 to | 999.999 | 1000 |
| 1000 to | 1,249.999 | 800 |
| 1250 to | 1,499.999 | 700 |
| 1500 to | 1,749.999 | 600 |
| 1750 to | 1,999.999 | 550 |
| 2000 to | 2,249.999. | 320 |
| 2500 to | 2,999.999 | 500 |
| 3000 to | 3,749.999 | 175 |
| 3750 to | 4,749.999 | 120 |
| 4750 to | 5,999.999 | 75 |
| 6000 to | 7,499.999 | 50 |
| 7500 to | 9,999.999. | 35 |
| 10,000 to | 20,000 .......... | 25 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $A$, paragraph 1-112, figures 1-49, -118, -115.

## TYPES OF CIRCUITS USED IN

Pierce, Miller, multivibrator-type

## MOUNTING DATA

## Crystal Holder: HC-6/U

Method of Mounting Crystal: Wire-mounted in metal holder

Dimensions and Marking: See figure 2-5(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.


Figure 2-6. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-18/U

## LOGISTICAL DATA

USAF Stock No.: 2100-2X518-freqcency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Specification requirements become increasingly difficult to meet at the lower frequencies in manufacturing this unit.
Equipment Used In:
Receiver-Transmitter RT-173/ARC-33-see figures 1-135 (L), (M)
Receiver-Transmitter RT-178/ARC-27-see figures 1-135 (R), (V), (W)
Receiver-Transmitter RT-XA-101/ARC-22-see figure 1-135 (Y)
Signal Generator SG-13/ARN - see figures 1-135 (Z), -137 (V)
Frequency Meter TS-186 (B/C)/UP—see figure 1-137 (G)
Radio Receiver R-540/ARN-14C- see figure 1-137 (N)
Radio Set AN/ARC-34 (XA-1) -see figures 1-137 (O), (T) .
Radio Receiver R-322/ARN-18-see figure 1-137 (U)
R-F Signal Generator Set AN/URM-25C-see figure 1-138 (D)
Radio Receiver R-277 (XA-A)/APN-70-see figure 1-138 (E)
Radio Receiver R-252 ( )/ARN-14 (14 crystals)
Signal Generator SG-1/ARN (2 crystals)
Radio Set AN/ART-13B (20 crystals)
Radio Receiver R-470/ARN-19 (10 crystals)
Radio Set AN/ARN-22 (12 crystals)

Radio Set AN / ANT-27
Radio Set AN/URT-( )
Radio Set AN/MRC-20 (12 crystals)

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM-800 to $14,999.999 \mathrm{kc}$
Crystal Impedance Meter TS-683/TSM-15,000 to $20,000 \mathrm{kc}$
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A.
Drive Adjustment Procedure:
800 to $14,999.999 \mathrm{kc}$ : MS90167 (see paragraph 2-60 and MIL-C-3098B)
15,000 to 20,000 kc: MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$ for units below 2000 kc $\pm 0.0005 \%$ for units of 2000 kc and above
Permitted change in resonance (effective) resistance: Wire-mounted- $\pm 15 \%$ or 2 ohms, whichever is greater.
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required

Section II

## CRYSTAL UNIT CR-19/U

(MF-HF)


Figure 2-7. Crystal Unit CR-19/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits which must maintain above average frequency stability in the absence of oven control, even when exposed to wide variation of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: $7.0 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999 \mathrm{kc}-10 \mathrm{mw}$ 10,000 to $20,000 \mathrm{kc}-5 \mathrm{mw}$
Maximum Pin-to-Pin Capacitance: Not specified

Maximum Effective Resonance Resistance:

| Frequency | (kc) | Resistance (ohms) |
| :---: | :---: | :---: |
| 800 to | 999.999 | 800 |
| 1000 to | 1,249.999 | 500 |
| 1250 to | 1,499.999 | 400 |
| 1500 to | 1,749.999 | 350 |
| 1750 to | 1,999.999 | 300 |
| 2000 to | 2,249.999 | 250 |
| 2250 to | 3,749.999 | 150 |
| 3750 to | 4,999.999 | 100 |
| 5000 to | 6,999.999 | $\cdots$ |
| 7000 to | 9,999.999 | …. 30 |
| 10,000 to 20 | 20,000 ..... | 25 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $A$, paragraph 1-49, figures 1-49, -115, -118.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, transitron, modified Colpitts

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder

Dimensions and Marking: See figure 2-7 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.


Figure 2-8. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-19/U

## LOGISTICAL DATA

USAF Stock No.: 2100-2X519-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In:
Signal Generator SG-34(XA)/UP-see figure $1-175$ (K)
Signal Generator SG-34/GPM-15-see figure 1-175 (K)
Radio Receiver R-277/APN-70 (4 crystals)
Radio Transmitter T-263/MRN-8 (20 crystals)
Radio Transmitting Set AN/MRN-7 (39 crystals)
Radio Set AN/MRC-20; Guard Receiver

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.

Requirements and Prosedures of Tests: See paragraphs 2-21 through 2-50
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM-800 to $14,999.999 \mathrm{kc}$
Crystal Impedance Meter TS-683/TSM-15,000 to $20,000 \mathrm{kc}$
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure:
800 to $14,999.999 \mathrm{kc}$ : MS90167 (see paragraph 2-60 and MIL-C-3098B)
15,000 to 20,000 kc: MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test: Permitted change in frequency: $\pm 0.0005 \%$ for units of 2000 kc and above $\pm 0.001 \%$ for units below 2000 kc
Permitted change in effective resonance resistance: Wire-mounted- $\pm 15 \%$ or 2 ohms, whichever is greater.
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-23/U

## (HF-VHF)



Figure 2-9. Crystal Unit CR-23/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the third or fifth mechanical harmonic of the fundamental frequency of the quartz plate. Used as a high-to-very-high-frequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 10 to 75 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal irequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration:

Overtone
Third
Fifth
Frequency (me)
10 to 52

Maximum Drive Level: 10 to 24.999999 mc ( 4 mw ) 25 to 75 ( 2 mw )
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$

Maximum Effective Resonance Resistance:
Frequency (mc) Resistance (ohms)
10 to $14.99999 \rightarrow \quad 60$
15 to $52 \quad 40$
52.000001 to $75 \ldots \quad 60$

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figure 1-49, -112, -113, -115, -118.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, capacitancebridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-9 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X523-frequency in mc
Status: Standard (Category 2)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Difficult to manufacture to all specification requirements over the entire upper and lower range.


Figure 2-10. Schematic diagram of typical oselliator designed for use with Crystal Unit CR-23/U

Equipment Used In:
Receiver-Transmitter RT-178/ARC-27-see figures 1-175 (B), (C)
Radio Receiver R-252A/ARN-14-see figure 1-175 (F)
Radio Receiver R-540/ARN-14C-see figure 1-175 (H)
Radio Set AN/ARN-21 (XN-2)-see figure 1-175 (J)
Signal Generator SG-13/ARN-see figure 1-175 (L)

Radio Receiver R-470/ARN-19 (14 crystals)
Radio Set AN/URC-10
Radio Transmitting Set AN/URT-( )
Radio Set AN/APX-19 (2 crystals)
Radio Set AN/GRC-30 (3 crystals)
Radio Set AN/PRC-14 (6 crystals)
Radio Set AN/MRC-30, Guard Receiver
MILITARY STANDARD TEST DATA
Authority: Military Specification MIL-C-3098B, approved 9 December 1955

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$ for units below 2000 kc $\pm 0.0005 \%$ for units of 2000 kc and above
Permitted change in effective resonance resistance: Wire-mounted- $\pm 15 \%$ or 2 ohms, whichever is greater.
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-24/U (HF-VHF)



Figure 2-11. Crystal Unit CR-24/U

## FUNCTIONAL DESCRIPTION

Pressure-mounted, or metal-plated quartz plate wire-mounted in a metal holder designed to operate on the third or fifth mechanical harmonic of the fundamental frequency of the quartz plate. Used as a high-to-very-high-frequency control element in circuits which must maintain aboveaverage frequency stability in the absence of oven control, even when exposed to wide variation of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 15 to 50 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within operating range.
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range.
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration:

| Overtone | Frequency (mc) |
| :--- | :--- |
| Third | 15 to 24.999999 |
| Fifth |  |

Maximum Drive Level: 2 mw

Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:
$\begin{array}{lrr}\text { Frequency (mc) } & \text { Resistance } \\ 15 \text { to } 24.999999 & 50 \\ 25 \text { to } 50 & 75\end{array}$

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $A$, paragraph 1-112, figures $1-49,-112,-113,-116,-118$.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, capacitancebridge, transitron, impedance-inverted

## mOUNTING DATA

Crystal Holder: HC-10/U
Method of Mounting Crystal: Pressure-mounted or wire-mounted in metal holder
Dimensions and Marking: See figure 2-11 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF' Stock No.: 2100-2X524-frequency in me
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None


Figure 2-12. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-24/U

Equipment Used In:
Radio Receiver R-266/URR-13 - see figure 1-175 (A)
Receiver-Transmitter RT-159A/URC-4-see figure 1-177 (D)
Radio Receiver R-122/ARN-12
Marker Beacon Set AN/ARN-32
MILITARY STANDARD TEST DATA
Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM or ZM-2/U
Electrical Connection of Holder:
Holder grounded

Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure: MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.002 \%$
Permitted change in effective resonance resistance: Shall not exceed maximum effective resistance
Aging Test: Not required

Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-25/U <br> (LF-MF)



Figure 2-13. Crystal Unit CR-25/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium-frequency control element in circuits which must maintain good frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 200 to 500 kc
Nominal Frequency Tolerance: $\pm 0.01 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Minimum Effective Resonance Resistance:
Frequency (kc)

Resistance (ohms)
200 to $249.999 \ldots \ldots \ldots \ldots \ldots$
250 to $299.999 \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 4000 ~$
300 to 399.999 ............................. 5000
400 to $449,999 \ldots \ldots \ldots \ldots \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 7500 ~$
450 to 500 .............................................. 10,000

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $D$, paragraph 1-116, figure 1-52.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, transitron, Meacham-bridge, modified Colpitts, modified Butler

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-13(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF' Stock No.: 2100-2X525-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Certain waivers from specification are required by some manufacturers before they will produce this unit.
Equipment Used In:
Radio Receiver R-277/APN-70-see figure 1-138(E) (Not a series-mode circuit as shown)


Figire 2-14. Schematic diagram of typical aseillator designed for use with Crystal Unit CR-25/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Frocedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standara Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test: Not required
Tensile Strength Test (Minimum Requirements):
Frequency (ke) Grams
200 to 249.999 ................................................................ 700

320 to $369.999 \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 400 ~$
370 to $434.999 \ldots . . .{ }_{-1}$
435 to $500 \ldots$250

## CRYSTAL UNIT CR-26/U <br> (LF-MF)



Figure 2-15. Crysfa! Unit CR-26/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium frequency control in circuits where superior frequency stability is required. This crystal unit is intended to be mounted in a tem-perature-controlled oven, and operated at series resonance.

## RATED OPERATING CHARACTERISTICS

## Frequency Range: 200 to 500 kc

Nominal Frequency Tolerance: $\pm 0.002 \%$ at $75{ }^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$ permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-40^{\circ}$ to $+80^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonance Resistance:

| Frequency (kc) | Resistance (ohms) |
| :---: | :---: |
| 200 to 249.999 | 3000 |
| 250 to 299.999 | 4000 |
| 300 to 399.999 . | 5000 |
| 400 to 449.999. | 7500 |
| 450 to 500 | 10,000 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element D, paragraph 1-116, figure 1-52.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, transitron, Meacham-bridge, modified Colpitts, modified Butler

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-15(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X526-frequency in kc
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publica-
tions: See Appendix IV.
Commercial Sources: See Appendix 11I.
Remarks: Certain waivers from specification are required by some manufacturers before they will produce this unit.
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955


Figure 2-16. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-26/U

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$

Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Frequency (ke)
Grams
200 to 249.999
700

320 to $368.999 \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 400 ~$

435 to 500 ........................................................................ 250

## CRYSTAL UNIT CR-27/U

(MF-HF)


Figure 2-17. Crystal Unir CR-27/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Froquency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $75^{\circ} \mathrm{C}$ Froquency Deviation with Temperature: $\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$ permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999$ ( 5 mw )
10,000 to $20,000(2.5 \mathrm{mw})$
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mathrm{f}$
Maximum Effective Resonance Resistance:

Frequency (kc)
800 to $999.999 . . . . . . . . . . . . . . . . . . . . . ~ 1000$
1000 to $1,249.999 \ldots \ldots \ldots \ldots \ldots$
1250 to $1,499.999 \ldots \ldots \ldots \ldots . . . . . . . . . . . .$.
1500 to $1,749.999 \ldots \ldots \ldots \ldots$

| Frequenc | (kc) | Resistance (ohms) |
| :---: | :---: | :---: |
| 1750 to | 1,999.999 | 550 |
| 2000 to | 2,249.999 | 500 |
| 2250 to | 2,999.999 | 320 |
| 3000 to | 3,749.999 | 175 |
| 3750 to | 4,749.999 | 120 |
| 4750 to | 5,999.999 | 75 |
| 6000 to | 7,499.999 | 50 |
| 7500 to | 9,999.999 | 35 |
| 10,000 to | 20,000 | 25 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of elements $A$ and $B$, paragraphs 1-112, -114, figures $1-49,-50,-115,-118$.

TYPES OF CIRCUITS USED IN
Pierce, Miller, multivibrator-type

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-17 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X527-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.

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Figure 2-18. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-27/U

## Remarks:

Equipment Used In:
Receiver-Transmitter RT-173/ARC-33 (see figures 1-135 (S), (T), (U) )
Receiver-Transmitter RT-178/ARC-27 (see figure 1-137 (A) )
Radio Set AN/ARC-34 (XA-1) (see figures 1-137(P), (Q), (R), (S) )
Radio Transmitting Set AN/GRT-3 (1750 crystals)

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM (800 to $14,999.999 \mathrm{kc}$ ).

Crystal Impedance Meter TS-683/TSM (15,000 to $20,000 \mathrm{kc}$ )
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure:
800 to $14,999.999 \mathrm{kc}$ : MS90167 (see paragraph 2-60 and MIL-C-3098B)
15,000 to $20,000 \mathrm{kc}$ : MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms , whichever is greater Aging Test:

Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-28/U

(MR-HF)


Figure 2-19. Crystal Unit CR-28/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven, and operated at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerancs: $\pm 0.002 \%$ at $75^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$
permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999$ ( 5 mw )
10,000 to $20,000(2.5 \mathrm{mw})$
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:

| Frequency (ko) |  | Resistance (ohms) |
| :---: | :---: | :---: |
| 800 to | 999.999 | 800 |
| 1000 to | 1,249.999 | 500 |
| 1250 to | 1,499.999 | 400 |
| 1500 to | 1,749.999 | 350 |
| 1750 to | 1,999.999 | 300 |



See characteristics of elements $A$ and $B$, paragraphs 1-112, 1-114, figures 1-49, -50, -115, -118.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, transitron, modified Colpitts

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-19(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X528-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Reluted Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None


Figure 2-20. Schemetic diagram of typical oscillator designed for use with Crystal Unit CR-28/U

Equipment Used In: Receiver-Transmitter RT-173/ARC-33 (see figure 1-175(D))

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM (800 to 14,999.999 kc)
Crystal Impedance Meter TS-683/TSM (15,000 to $20,000 \mathrm{kc}$ )
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure:
800 to 14,999 kc: MS90167 (see paragraph 2-60 and MIL-C-3098B)
15,000 to $20,000 \mathrm{kc}$ : MS90168 (see paragraph 2-62 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms, whichever is greater

Aging Test:
Permitted change in frequency: $\pm 0.001 \%$

Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-29/U <br> (LF)



Figure 2-21. Crystal Unit CR-29/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a plastic holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a tempera-ture-controlled oven, and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 80 to 199.999 kc
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $75^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$
permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-40^{\circ}$ to $+80^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified Maximum Effective Resonance Resistance:

| Frequency (kc) | Resistance (ohms) |
| :---: | :---: |
| 80 to 119.999 | 10,000 |
| 120 to 159.999 . | 8000 |
| 160 to 199.999 . | 6000 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element D, paragraph 1-116, figure 1-52.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, transitron, Miller, modified Butler

## MOUNTING DATA

Crystal Holder: HC-5/U or HC-21/U
Method of Mounting Crystal: Wire-mounted in plastic holder
Dimensions and Marking: See figure 2-21 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X529-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Use of this crystal unit is discouraged by some manufacturers because, in their opinion, the specified holder ( $\mathrm{HC}-5 / \mathrm{U}$ ) suffers these important disadvantages: The holder is not hermetically sealed (although a metal hermetically-


Figura 2-22. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-29/U
sealed version will be used in procurement of future models) ; it has a poor form factor; and it uses an unorthodox base which requires a special socket. In addition, the phenolic holder is even more detrimental at the $75^{\circ}$ operating temperature.
Equipment Used In:
MILITARY STANDARD TEST DATA
Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Not applicable

Method of Measuring Frequency and E'ffective Resonance Resistance: B
Drive Adjustment Procedure: MS91483 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
$\begin{array}{cc}\text { Tensile Strength Test (Minimum Requirements): } \\ \text { Frequency (ke) } & \text { Grams } \\ 80 \text { to } 119.999 \\ 120 \text { to } 159.999 \\ 160 \text { to } 199.999 & 1000 \\ \end{array}$

## CRYSTAL UNIT CR-30/U (LF)



Figure 2-23. Crystal Unit CR-30/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a plastic holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a tem-perature-controlled oven, and operates at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 80 to 199.999 kc
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $75^{\circ} \mathrm{C}$
Frequency Deviation with Tempenature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$
permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-40^{\circ}$ to $+80^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonance Resistance: 3000 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $D$, paragraph 1-116, figure 1-52.

## TYPES OF CIRCUITS USED IN

Meacham-bridge, two-stage-grounded-cathode, transitron, transformer-coupled, modified Butler

## MOUNTING DATA

Crystal Holder: HC-5/U or HC-21/U
Method of Mounting Crystal: Wire-mounted in plastic holder
Dimensions and Marking: See figure 2-23 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X530-frequency in ke
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Use of the crystal unit is discouraged by some manufacturers because, in their opinion, the specified holder ( $\mathrm{HC}-5 / \mathrm{U}$ ) suffers these important disadvantages: The holder is not hermetically sealed (although a metal hermeticallysealed version will be used in procurement of future models) ; it has a poor form factor; and it uses an unorthodox base which requires a special socket. In addition, the phenolic holder is even more detrimental at the $75^{\circ}$ operating temperature.
Equipment Used In:


Figure 2-24. Schematic diagram of typical oscillator designod for use with Crystal Unit CR-30/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Not applicable Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements): Not specified
Frequency (kc) Grams
80 to 119.999 1000
120 to 159.999
800
160 to 199.999
700

## CRYSTAL UNIT CR-32/u (HF-VHF)



Figure 2-25. Crystal Unit CR-32/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the third and fifth mechanical harmonic of the fundamental frequency of the quartz plate. Used as a high-to-very-high-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven, and operated at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 10 to $\mathbf{7 5} \mathrm{mc}$
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $75^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$ permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration:
Overtone Frequency ( ms )
Third 10 to 52
Fifth 52.000001 to 75
Maximum Drive Level:
10 to 24.999999 ( 2 mw )
25 to 75 ( 1 mw )
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:

| Frequency (mc) | Resistance (ohms) |
| :--- | :---: |
| 10 to 14.999999 | 60 |
| 15 to $52 \ldots$ | 40 |
| 52.000001 to 75 | $\cdots$ |

Resistance (ohms)
15 to 52 40


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## PERFORMANCE Characteristics of NORMAL CRYSTAL ELEMENT

See characteristics of elements $A$ and $B$, paragraphs 1-112, -114, figures $1-49,-50,-112,-113$, $-115,-118$.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, capacitance-bridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-25(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X532-frequency in mc
Status: Standard (Category 1)
Date of Status: 9 October 1950
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: This unit is difficult to manufacture to all specification requirements over the entire upper and lower frequency ranges.
Equipment Used In:
Receiver-Transmitter RT-173/ARC-33 (see figure 1-175(E))
Radio Set AN/ARC-34(XA-1) (see figure 1-175(I))
Radio Set AN/MRC-20 (11 crystals)
Radio Receiving Set AN/GRR-7 (1750 crystals)


Figure 2-26. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-32/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure: MS90168 (see paragraphs 2-62 and 2-64 per MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms, whichever is greater

## Aging Test:

Permitted change in frequency: $0.001 \%$
Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-33/U (HF)



Figure 2-27. Crystal Unit CR-33/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in metal holder and designed to operate on the third mechanical harmonic of the fundamental frequency of the quartz plate. Used as a highfrequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 10 to 25 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Fréquency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu_{\mu} \mathrm{f}$
Harmonic of Quartz Vibration: Third overtone
Maximum Drive Level: 2.5 mw
Maximum Pin-to-Pin Capacitance: $12.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:

## Frequency (kc)

Resistance (ohms)
10 to 10.999999
11 to $11.999999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
12 to $12.999999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
13 to $13.999999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
14 to 14.999999 ............................... 45

| Frequency (ke) | Resistance (ohms) |
| :---: | :---: |
| 15 to 15.999999 | 41 |
| 16 to 16.999999 | 38 |
| 17 to 17.999999 | 36 |
| 18 to 18.499999 | 34 |
| 18.5 to 18.999999 | 32 |
| 19 to 19.499999 | 30 |
| 19.5 to 19.999999 | 28 |
| 20 to 20.499999 | 26 |
| 20.5 to 20.999999 | 25 |
| 21 to 21.499999 | 24 |
| 21.5 to 21.999999 | 23 |
| 22 to 22.499999 | 22 |
| 22.5 to 22.999999 | 21 |
| 23 to 23.499999 | 20 |
| 23.5 to 23.999999 | 19 |
| 24 to 24.499999 | 18 |
| 24.5 to 25 | 17 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $A$, paragraph $1-112$, figures $1-49,-112,-113,-115,-118$.

## TYPES OF CIRCUITS USED IN

Tuned-Pierce, tuned-Miller, Butler, modified Colpitts, capacitance-bridge, transformer-coupled, modified transitron

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-27(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.


Figure 2-28. Schematic diagram of typical oseillotor designed for use with Crystal Unit CR-33/U

## LOGISTICAL DATA

USAF Stock No.: 2100-2X533-frequency in mc
Status: Special application (Category 1)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In:
Radio Receiver R-252/ARN-14 (see figures 1-137 (B), 1-138 (A) )
Radio Receiver R-252C/ARN-14 (34 crystals)
Radio Receiver R-541/ARN-14D (34 crystals)

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS91415 (see paragraph 2-63 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$ for units of 2000 kc and above $\pm 0.001 \%$ for units below 2000 kc
Permitted change in effective resonance resistance: Wire-mounted $- \pm 15 \%$ or 2 ohms, whichever is greater.
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-35/U <br> (MF-HF)



Figure 2-29. Crystal Unit CR-35/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled even, and operated at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $85^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $85^{\circ} \mathrm{C}$ permitted over range of $80^{\circ}$ to $90^{\circ} \mathrm{C}$
Operating Temperature Range: $85^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999 \mathrm{ke}(5 \mathrm{mw})$
10,000 to $20,000 \mathrm{kc}$ ( 2.5 mw )
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:
Frequency (kc)
Resistance (ohms)
800 to 999.999 .......................... 800
1000 to $1,249.999 \ldots . . . . . . . . . . . . . . . . . . . . . . . . . ~ 500 ~$
1250 to $1,499.999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
1500 to $1,749.999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots$

2000 to $2,249.999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots$

| Frequenc | (ke) | Resistance (ohms) |  |
| :---: | :---: | :---: | :---: |
| 2250 to | 3,749.999 |  | 150 |
| 3750 to | 4,999.999 |  | 100 |
| 5000 to | 6,999.999 |  | 50 |
| 7000 to | 9,999.999 |  | 30 |
| 10,000 to | 20,000 |  | 25 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of elements $A$ and $B$, paragraphs 1-112, -114 , figures 1-49, $-50,-115,-118$.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, transitron, modified Colpitts

## MOUNTING DATA

## Crystal Holder: HC-6/U

Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-29(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X535-frequency in ke
Status: Standard (Category 1)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Complete information on long-term performance of crystals operating at the temperature specified for this unit is not yet available.
Equipment Used In:


Figure 2-30. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-35/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM (800 to $14,999.999 \mathrm{kc}$ )
Crystal Impedance Meter TS-683/TSM (15,000 to $20,000 \mathrm{kc}$ )
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure:
800 to $14,999.999 \mathrm{kc}: \mathrm{MS} 90167$ (see paragraph 2-60 and MIL-C-3098B)
15,000 to $20,000 \mathrm{kc}$ : MS90168 (see paragraph 2-62 and M1L-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms , whichever is greater
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-36/U

(MF-HF)


Figure 2-31. Crystal Unit CR-36/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven, and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $85^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$ permitted over the range of $80^{\circ}$ to $90^{\circ} \mathrm{C}$
Operating Temperature Range: $85^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999 \mathrm{kc}$ ( 5 mw )
10,000 to $20,000 \mathrm{kc}(2.5 \mathrm{mw})$
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:

| Frequenc | (kc) | Resistance (ohms) |
| :---: | :---: | :---: |
| 800 to | 999.999 | 1000 |
| 1000 to | 1,249.999 | 800 |
| 1250 to | 1,499.999 | 700 |
| 1500 to | 1,749.999 | 600 |
| 1750 to | 1,999.999 | 550 |
| 2000 to | 2,249.999 | 500 |
| 2250 to | 2,999.999 | 320 |


| Frequenc | (kc) | Resistance (ohms) |
| :---: | :---: | :---: |
| 3000 to | 3,749.999 | 175 |
| 3750 to | 4,749.999 | 120 |
| 4750 to | 5,999.999 | 75 |
| 6000 to | 7,499.999 | 50 |
| 7500 to | 9,999.999 | 35 |
| 10,000 to | 20,000 | 25 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of elements $A$ and $B$, paragraphs $1-112,-114$, figures $1-49,-50,-115,-118$.

## TYPES OF CIRCUITS USED IN

Pierce, Miller, multivibrator-type

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-31 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: $2100-2 \times 536$-frequency in kc
Status: Standard (Category 1)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Complete information on long-term performance of crystals operating at the temperature specified for this unit is not yet available.
Equipment Used In: Radio Set AN/GRC-30 (42 crystals)


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Crystal Units-Oreup I

Figure 2-32. Schematic diagram of typical oscillafor designed for use with Crysfal Unit CR-36/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-2098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM (800 to $14,999.999 \mathrm{kc}$ )
Crystal Impedance Meter TS-683/TSM (15,000 to $20,000 \mathrm{kc}$ )
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure:
800 to $14,999.999 \mathrm{kc}$ : MS90167 (see paragraph 2-60 and MIL-C-3098B)
15,000 to $20,000 \mathrm{ke}$ : MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms, whichever is greater Aging Test:

Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements): Not specified

## CRYSTAL UNIT CR-37/U (LF)



Figure 2-33. Crystal Unif CR-37/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-frequency control element in circuits which need only minimum requirements in frequency stability in the absence of oven control under exposure to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 90 to 250 kc
Nominal Frequency Tolerance: $\pm 0.02 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $20 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: See page 467.
Maximum Effective Resonance Resistance:
Frequency (kc)

Resistance (ohms)
90 to 169.999 5000
170 to 250 7000

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of clement $E$, paragraph 1-199, figures 1-24, -25, -26.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, modified transitron, Miller, modified Butler

## MOUNTING DATA

Crystal Holder: HC-13/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-33(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X537-frequency in ke
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In: Radio Set AN/ARN-27 (10 crystals)

MILITARY STANDARD TEST DATA<br>Authority: Military Specification MIL-C-3098B, approved 9 December 1955



Figure 2-34. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-37/U

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM or TS-710/TSM
Electrical Connection of Holder: Holder grounded Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B) or MS91446 (see paragraph 2-65 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams

170 to 250 ................................................................................ 700700

Capacitance: From pin-to-pin, where $f$ is the specified frequency in kc per second

$$
\left.\begin{array}{c}
\begin{array}{c}
\text { Frequency }(k c) \\
\text { inclusive }
\end{array} \\
\begin{array}{c}
\text { Permitted } \\
\text { capacitance }(\mu \mu f)
\end{array} \\
90.000 \text { to } 169.999 \ldots \ldots
\end{array} \begin{array}{c}
\frac{450}{f}+1.2, \pm 15 \% \\
170.000 \text { to } 250.999 \ldots \ldots
\end{array}\right)
$$

## CRYSTAL UNIT CR-38/U <br> (VLF-LF)



Figure 2-35. Crystal Unit CR-38/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency. of the quartz plate. Used as a very-low-to-low-frequency control element which need meet only average requirements in frequency stability in the absence of oven control when exposed to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 16 to 100 ke
Nominal Frequency Tolercnce: $\pm 0.012 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $20 \pm 0.5 \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 0.1 mw
Maximum Pin-to-Pin Capacitance: See page 469.
Maximum Effective Resonance Resistance: 200,000 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $N$, paragraph 1-104, figures 1-36, -37, -38.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, modified transitron

## MOUNTING DATA

## Crystal Holder: HC-13/U

Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-35 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X538-frequency in kc
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In:


Flgure 2-36. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-38/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 Deceinber 1955

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-710/TSM

## Electrical Connection of Holder:

Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A

Drive Adjustment Procedure: MS91446 (see paragraph 2-65 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$

## Aging Test:

Permitted change in frequency; $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Frequency (kc)
Grams
16 to 59.999 … .a..................................................... 800
60 to 100 ............................................................................... 700

Capacitance: From pin-to-pin, where $f$ is the specified frequency in ke per second
$\begin{array}{cc}\text { Frequency ( } k c \text { ) } & \text { Permitted } \\ \text { inclusive } & \text { capacitance ( } \mu \mu f \text { ) }\end{array}$
16.000 to $33.999 \ldots \ldots \ldots \cdot \frac{24}{\sqrt{f}}+1.6, \pm 15 \%$
34.000 to $53.999 \ldots \ldots \ldots \frac{33}{\sqrt{f}}+1.6, \pm 15 \%$
54.000 to $100.000 \ldots \ldots \ldots \frac{24}{\sqrt{7}}+1.6, \pm 15 \mathrm{ch}$


Figure 2-37. Crystal Unit CR-39/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in an evacuated glass-bulb holder (vacuum-tube type) and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium-frequency control element in circuits which must maintain unusually high frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 160 to 330 kc
Nominal Frequency Tolerance: $\pm 0.003 \%$ at $25^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.004 \mathrm{C}$ from frequency measured at $25^{\circ} \mathrm{C}$ over range of $-55^{\circ}$ to $+75^{\circ} \mathrm{C} \pm 2^{\circ} \mathrm{C}$
Operating Temperature Range: $-55^{\circ}$ to $+75^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
hesonamre: Series
Lood Caparitance: Not applicable
Harmomic of Quartz Vibration: Fundamental
Maximum Driuc Level: 0.1 mw
Maximum Pin-to-Pin Capacitance:
$\begin{array}{lc}\text { Frequcncy (kc) } & \text { Copacitance ( } \mu \mu f \text { ) } \\ 160 \text { to } 249.999 & \frac{4320}{\text { Frequency (kc) }}+2 \\ 250 \text { to } 330 \ldots \ldots & \frac{1100}{}+2\end{array}$


## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $G$, paragraph 1-119, figures 1-55, -56, -117.

## TYPES OF CIRCUITS USED IN

Meacham-bridge, two-stage-grounded-cathode, transitron, transformer-coupled, Butler, modified Colpitts

## MOUNTING DATA

## Crystal Holder: HC-15/U

Method of Mounting Crystal: Wire-mounted in an evacuated glass-bulb holder
Dimensions and Marking: See figure 2-37(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.


Figure 2-38. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-39/U

## Commercial Sources: See Appendix III.

Remarks: Below 180 kc , the shortness of the holder relative to the size of the crystal blank increases the difficulty of obtaining a reliable crystal unit.
Equipment Used In: Radio Set AN/APN-5

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: ©Crystal Impedance Meter TS-710/TSM
Electrical Connection of Holder: Not applicable

Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure: MS91446 (see paragraph 2-65 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.00015 \%$
Permitted change in effective resonance resistance: $15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.000075 \%$ per week

Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams

250 to 330 ................................................. 800

## CRYSTAL UNIT CR-40/U (LF-MF)



Figure 2-39. Crystal Unit CR-40/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in an evacuated glass-bulb holder (vacuum-tube type) and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven and operated at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 160 to 330 kc
Nominal Frequency Tolerance: $\pm 0.003 \%$ at $70^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $70^{\circ} \mathrm{C}$
permitted over range of $65^{\circ}$ to $75^{\circ} \mathrm{C}$
Operating Temperature Range: $70^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+75^{\circ}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 0.1 mw
Maximum Pin-to-Pin Capacitance:

| Frequency (kc) | Capacitance ( $\mu \mu f$ ) |
| :--- | :---: |
| 160 to 249.999 | $\frac{4320}{\text { Frequency (kc) }}+2$ |
| 250 to 330 | $\frac{1100}{\text { Frequency (kc) }}+2$ |

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Maximum Effective Resonance Resistance:

| Frequency (ke) | Resistance (ohms) |  |
| :--- | :--- | :--- |
| 160 to 249.999 | 150 |  |
| 250 to 330 |  |  |

Effective Resistance Deviation:
Frequency (kc)
Resistance (ohms)
160 to 249.999
50
250 to 330
200

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $G$, paragraph 1-119, figures 1-55, -56, -117.

## TYPES OF CIRCUITS USED IN

Meacham-bridge, two-stage-grounded-cathode, transitron, transformer-coupled, Butler, modified Colpitts

## MOUNTING DATA

Crystal Holder: HC-15/U
Method of Mounting Crystal: Wire-mounted in evacuated glass-bulb holder
Dimensions and Marking: See figure 2-39(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X640
Status: Special application (Category 2)


Figure 2-40. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-40/U

Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Below 180 kc , the shortness of the holder relative to the size of the crystal blank increases the difficulty of obtaining a reliable crystal unit.
Equipment Used In: Radio Set AN/CPN-2A

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM

Electrical Connection of Holder: Not applicable Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjusiment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)

## Shock and Vibration Test.

Permitted change in frequency: $\pm 0.00015 \%$
Permitted change in effective resonance resistance: $\pm 10 \%$ or 10 ohms, whichever is greater
Aging Test:
Permitted change in frequency: $\pm 0.00005 \%$ per week

Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams
160 to 249.999 ............................................................ 1000
250 to 330 .............................................................. 800

## CRYSTAL UNIT CR-42/U (LF)



Figure 2-41. Crystal Unit CR-42/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in an evacuated glass-bulb holder (vacuum-tube type) and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven, and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 90 to 250 kc
Nominal Frequency Tolerance: $\pm 0.003 \%$ at $75^{\circ} \mathrm{C}$
Frequency Deviation with Temperature: $\pm 0.002$ from frequency measured at $75^{\circ} \mathrm{C}$ permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Ranye: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+85^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Parallel
Load Capacitanee: $32 \pm 0.5 \mu \mu \mathrm{f}$
Harmomic of Quartz Vibration: Fundamental
Maximum Drive Letd: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonance Resistance:

| Frequency (kc) | Resistance (ohms) |
| :--- | :---: |
| 90 to 169.999 | 4500 |
| 170 to 250 | 7000 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $E$, paragraph 1-99, figures 1-24, -25, -28.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, Miller, modified transitron, modified Butler, Pierce

## MOUNTING DATA

## Crystal Holder: HC-13/U

Method of Mounting Crystal: Wire-mounted in an evacuated glass-bulb holder
Dimensions and Marking: See figure 2-41 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X542
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications. Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In: Radio Set AN/ARC-21


Figure 2-42. Schematic diagram of typical oscillator dosigned for use with Crystal Unit CR-42/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM or TS-710/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and M1L-C-3098B) or MS91446 (see paragraph 2-65 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: -0.001 to $+0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: -0.001 to $+0.0005 \%$

Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams
90 to 169.999 .
800
700

## CRYSTAL UNIT CR-43/U

(LF)


Figure 2-43. Crystal Unif CR-43/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in an evacuated metal-shell holder (vacuum-tube type) and designed to operate on the fundamental frequency of the quartz plate. Used as a low-frequency control element in circuits which must maintain good frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 80.860 kc (can be fabricated within a range of 70 to 100 kc )
Nominal Frequency Tolerance: $\pm 0.01 \%$ at $25^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $25^{\circ} \mathrm{C}$ permitted over range of $-30^{\circ}$ to $+75^{\circ} \mathrm{C} \pm 2^{\circ} \mathrm{C}$
Operating Temperature Range: $-30^{\circ}$ to $+75^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $45 \pm 1.0 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: $45 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:
 Resistance (ohms) 80.860 3000

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element M, paragraph 1-103, figures $1-33,-34,-35$. (Optional : element $E$, paragraph 1-99, figures $1-24,-25,-26$. )

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, Miller, modified transitron

## MOUNTING DATA

Crystal Holder: HC-16/U
Method of Mounting Crystal: Wire-mounted in evacuated metal-shell holder
Dimensions and Marking: See figure 2-43(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-2X543-80.86
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: The shortness of the crystal holder relative to the size of the crystal blank increases the difficulty of obtaining a reliable crystal unit. This unit is used in equipment for controlling mile pulses.
Equipment Used In:


Figure 2-44. Schematic diagram of typical oscillator designod for use with Crysfal Unit CR-43/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MILC-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Holder grounded Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure: MS91482 (see paragraph 2-6.1 and MI_C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.00075 \%$ per week

Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams
80.860 1000

## CRYSTAL UNIT CR-44/U* (HF)



Figure 2-45. Crystal Unit CR-44/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a high-frequency control element in circuits where superior frequency stability is required. The crystal unit is intended to be mounted in a tempera-ture-controlled oven, and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 15,000 to $20,000 \mathrm{kc}$
Nominal Frequenciy Tolerance: $\pm 0.002 \%$ at $85^{\circ} \mathrm{C}$
Frequenry Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $85^{\circ} \mathrm{C}$
permitted over range of $80^{\circ}$ to $90^{\circ} \mathrm{C}$
Opernting Temperature Range: $85^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Parallel
L.oad Capacitance: $32 \pm 0.5 \mu \mu \mathrm{f}$

Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 1 mw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance: 25 ohms

## PERFORMANCE CHARACTERISTICS OF NOKMAL CRYSTAL ELEMENT

Sec characteristics of elements $A$ and $B$, paragraphs 1-112,-114, hgures 1-49, $-50,-115,-118$.

## types of circuits used in

Pierce, Miller

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-45 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: *For replacement only. For new applications specify CR-36/U.

Equipment Used In: Radio Set AN/GRC-30 (42 crystals)

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM


Figure 2-46. Schematic diagram of typical ascillator designed for use with Crystal Unit CR-44/U

Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resisiance: B

Drive Adjustment Procedure: MS90168 (see paragraph 2-62 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms, whichever is greater Aging Test: Not required

Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-45/U (MF)



Figure 2-47. Crystal Unit CR-45/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a $455-\mathrm{kc}$ i-f filter element in radio receiver circuits which must provide greater selectivity and i-f stability than can be obtained with conventional L-C bandpass circuits. The crystal unit is intended for operation at series resonance without oven control of the temperature.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 455 kc
Nominal Frequency Tolerance: $\pm 0.02 \%$ at all temperatures within operating range
Special requirements: (a) The crystal unit shall have a difference in frequency of $+80 \pm 12$ cycles between operating at the series resonant frequency and parallel-resonance of 32 $\pm 0.5 \mu \mu$. These tests shall be made at room temperature. (b) The crystal unit shall be free of spurious response within 7 kc of the nominal frequency.
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable

Harmonic of Quartz Vibration: Fundamental Maximum Drive Level: 2 mw Maximum Pin-to-Pin Capacitance: $5 \pm 2.5 \mu \mu \mathrm{f}$ Maximum Effective Resonance Resistance: 3300 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $C$, paragraph 1-115, figure 1-51.

## TYPES OF CIRCUITS USED IN

Radio receiver i-f bandpass filters, capacitancebridge

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-47 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In:


Figure 2-48. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-45/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A

Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.003 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$

Tensile Strength Test (Minimum Requirements): 500 grams

## CRYSTAL UNIT CR-46/U

 (LF-MF)

Figure 2-49. Crystal Unit CR-46/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium-frequency control element which must maintain good frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 200 to 500 kc
Nominal Frequency Tolerance: $\pm 0.01 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $20 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonance Resistance:

| Frequeney (ke) | Resistance (ohms) |
| :--- | :---: |
| 200 to 249.999 | 6500 |
| 250 to 299.999 | 7000 |
| 300 to 399.999 |  |
| 400 to 449.999 | $\ldots$ |
| 450 to 500 | $\ldots$ |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of elements $C$ and $D$, paragraphs 1-115, -116, figures 1-51, -52.

## TYPES OF CIRCUITS USED IN

Miller, Pierce, multivibrator-type, modified transitron, two-stage-grounded-cathode

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-49(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Certain waivers from the specification are required by some manufacturers before going into production.
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955


Figure 2-50. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-46/U

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$

Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams
200 to 249.999 ............................................................... 700


370 to 434.999 ............................................................ 300
435 to 500 ...................................................................... 250

## CRYSTAL UNIT CR-47/U

(LF-MF)


Figure 2-51. Crystal Unit CR-47/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a low-to-medium-frequency control element where superior frequency stability is required. The crystal unit is intended to be mounted in a tempera-ture-controlled oven, and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 200 to 500 kc
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $75^{\circ} \mathrm{C}$
Frequency Deviation with Temperature:
$\pm 0.0005 \%$ from frequency measured at $75^{\circ} \mathrm{C}$ permitted over range of $70^{\circ}$ to $80^{\circ} \mathrm{C}$
Operating Temperature Range: $75^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-40^{\circ}$ to $+80^{\circ}$ $\pm 2^{\circ} \mathrm{C}$
Resonance: Parallel
Load Capacitance: $20 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: Not specified
Maximum Effective Resonance Resistance:

| Frequency (kc) | Resistance (ohms) |
| :---: | :---: |
| 200 to 249.999 | 6500 |
| 250 to 299.999 | 7000 |
| 300 to 399.999 | 7500 |
| 400 to 449.999 | 10,000 |
| 450 to 500 | 11,000 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of elements $C$ and $D$, paragraphs 1-115, -116, figures 1-51, -52.

TYPES OF CIRCUITS USED IN
Pierce, modified transitron, multivibrator-type, Miller, two-stage-grounded-cathode

## MOUNTING DATA

## Crystal Holder: HC-6/U

Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-51 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks:

Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955


Figure 2-52. Schematic diagram of typical oscillafor designed for use with Crystal Unit CR-47/U

Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-537/TSM
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistarce: B
Drive Adjustment Procedure: MS91482 (see paragraph 2-61 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$

Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Frequency (kc)
Grams
200 to 249.999
700
250 to 319.999 ...................................................... 500
320 to $369.999 \ldots \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 400 ~$

435 to 500 ................................................................ 250

## CRYSTAL UNIT CR-48/U* (MF)



Figure 2-53. Crystal Unit CR-48/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-frequency control element in circuits which must maintain slightly better-than-average frequency stability when exposed to extreme variations of temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to 3000 kc
Nominal Frequency Tolerance: $\pm 0.0075 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 10 mw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance.Resistance:

| Frequency (kc) | Resistance (ohms) |
| :---: | :---: |
| 800 to 999.999 | 1000 |
| 1000 to $1,249.999$ | 800 |
| 1250 to 1,499.999 | 700 |
| 1500 to 1,749.999 | 600 |

Frequency (kc) Resistance (ohms)
1750 to $1,999.999$ 550
2000 to $2,249.999$ 500
2250 to 3000 320

PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures 1-49, -115, -118.

## TYPES OF CIRCUITS USED IN

Pierce, Miller, multivibrator-type

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-53(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 19 November 1952
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: *For replacement only. For new applications specify CR-18/U.
Equipment Used In:

WADC TR 56-156


Flgure 2-54. Schematic diagram of typical oscillofor designed for use with Crystal Unit CR-48/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-330/TSM
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A

Drive Adjustment Procedure: MS90167 (see paragraph 2-60 and MII-C-3098B)
Shock and Vibration Test:
Permitted change in frequency:
$\pm 0.001 \%$ for units below 2000 kc
$\pm 0.0005 \%$ for units of 2000 ke and above
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required


Figure 2-55. Crystal Unit CR-49/U

## FUNCTIONAL DESCRIPTION

Spacer-mounted quartz plate in a metal holder designed to operate on the fundamental frequency of the quartz plate. Used as a medium-frequency control element in circuits which must maintain slightly better-than-average frequency stability under exposure to extreme variations in temperature. The crystal unit is intended for operation at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 800 to 3000 kc
Nominal Frequency Tolerance: $\pm 0.0075 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 10 mw
Maximum Pin-to-Pin Capacitance: Not specified Maximum Effective Resonance Resistance:

Frequency (kc)
Resistance (ohms)
800 to $999.999 \ldots \ldots \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 1000$
1000 to $1,249.999 \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 800 ~$
1250 to $1,499.999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
1500 to $1,749.999 \ldots \ldots \ldots \ldots$
1750 to $1,999.999 \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
2000 to $2,249.999$............................. $\mathbf{5 0 0}$


## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures 1-49, -115, -118.

TYPES OF CIRCUITS USED IN
Pierce, Miller, multivibrator-type

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Spacer-mounted in metal holder
Dimensions and Marking: See figure 2-55(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 14 January 1954
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: *For replacement only. For new applications specify CR-18/U.
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-330/TSM


Figure 2-56. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-49/U

Electrical Connection of Holder: Holder grounded Method of Measuring Frequency and Effective Resonance Resistonce: The crystal unit shall be subjected to a temperature run over the operating temperature range specified at any convenient rate of change not to exceed an average rate of $50^{\circ} \mathrm{C}$ per minute. Observations of frequency and effective resistance shall be made continuously, or intermittently at no greater than $2^{\circ} \mathrm{C}$ intervals. Values of frequency and effective resistance shall not exceed the prescribed limits over the temperature range.
Drive Adjustment Procedure: MS90167 (see paragraph 2-60 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.002 \%$ for units below 2000 kc $\pm 0.0005 \%$ for units of 2000 kc and above
Permitted change in effective resonance resistance:

| Resistance (ohms) | Permitted |
| :---: | :---: |
| change ( $\%$ ) |  |

0 to $10 \ldots \ldots . . . \quad 40$

50.1 to $100 \ldots \ldots . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ 25 ~$
above 100 ….............................................................. 20
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-50/U (VLF-LF)



Figure 2-57. Crystal Unit CR-50/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a very-low-to-low-frequency control element which need meet only average requirements in frequency stability in the absence of oven control when exposed to wide variations in temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 16 to 100 kc
Nominal Frequency Toleraxce: $\pm 0.012 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within the limits of nominal frequency tolerance
Operating Temperature Range: $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 0.1 mw
Maximum Pin-to-Pin Capacitance:
Frequency (kc) Capacitance ( $\mu \mu f$ )
16 to $33.999 \quad\left(\frac{24}{\sqrt{\text { Frequency (kc) }}+1.6) \pm 15 \%}\right.$
34 to $53.999 \quad\left(\frac{33}{\sqrt{\text { Frequency (kc) }}+1.6) \pm 15 \%}\right.$

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Frequency (ke)
Resistance (ohms)
54 to $100.00 \ldots . .\left(\frac{24}{\sqrt{\text { Frequency (kc) }}}+1.6\right) \pm 15 \%$
Maximum Effective Resonance Resistance: 125,000 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $N$, paragraph 1-104, figures 1-36, -37, -38.

## TYPES OF CIRCUITS USED IN

Two-stage-grounded-cathode, modified transitron

## MOUNTING DATA

Crystal Holder: HC-13/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-57(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 2)
Date of Status: 14 January 1954
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: The shunt-capacitance specification is controversial within the industry.
Equipment Used In: Radio Set AN/ARN-27 (10 crystals)


Figure 2-58. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-50/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-710/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS91446 (see paragraph 2-65 and MIL-C-3098B)

Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$

Tensile Strength Test (Minimum Requirements):
Frequency (kc) Grams
16 to 59.999 ......................................................... 800
60 to 100 ....................................................................

## CRYSTAL UNIT CR-51/U

 (HF-VHF)

Figure 2-59. Crystal Unil CR-51/U

## FUNCTIONAL DESCRIPTION

Pressure-mounted quartz plate in metal holder designed to operate on the third mechanical harmonic of the fundamental frequency of the quartz plate. Used as a high- to very-high-frequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to wide variations in temperature and to relatively high drive levels. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 10 to 61 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Third mechanical harmonic
Maximum Drive Level: 20 nw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance:

| Frequency (mc) | Resistance (ohms) |
| :--- | :---: |
| 10 to $14.999 \ldots$ | 60 |
| 15 to 61 | 40 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $A$, paragraph $1-112$, figures $1-49,-112,-113,-115,-118$.

TYPES OF CIRCUITS USED IN
Butler, transformer-coupled, capacitance-bridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Pressure-mounted in metal holder
Dimensions and Marking: See figure 2-59(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 1)
Date of Status: 14 January 1954
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Difficult to manufacture and meet all specification requirements over entire upper and lower ranges.
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.


Figure 2-60. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-51/U

Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded Method of Measuring Frequency and Effective Resonance Resistance: A or B
Drive Adjustment Frocedure: MS90168 (see paragraph 2-62 and MIL-C-3098B), with the exception of the following table of voltage and resistance:

| Frequency (mc) | Resistance (ohms) | Volts |
| :---: | :---: | :---: |
| 10 to 14.999 | 60 | 1.1 |
| 15 to 61 | 40 | 0.9 |

Shock and Vibration Test:
Permitted change in frequency: $\pm \mathbf{0 . 0 0 2 \%}$
Permitted change in effective resonance resistance: Shall not exceed the max effective resistance

Aging Test:
Permitted change in frequency: $\pm 0.001 \%$

Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-52/U (HF-VHF)



Figure 2-61. Crystal Unit CR-52/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the third mechanical harmonic of the fundamental frequency of the quartz plate. Used as a high- to very-high-frequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 10 to 61 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Third mechanical harmonic
Maximum Drive Level:
10 to $24.999999 \mathrm{mc}(4 \mathrm{mw})$
25 to 61 mc ( 2 mw )
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$


## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures $1-49,-112,-113,-115,-118$.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, capacitance-bridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-61 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 1)
Date of Status: 14 January 1954
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.


Figure 2-62. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-52/U

Remarks: Difficult to manufacture and meet all specification requirements over entire upper and lower ranges. Same as CR-23/U except designed to operate on 3 rd mode only.
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded

Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjusiment Procedure: MS90168 (see paragraphs 2-62 and 2-64 per MIL_C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms, whichever is greater Aging Test:

Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-53/U (VHF)



Figuro 2-63. Crystal Unit Cr-53/U

## FUNCTIONAL DESCRIPTION

Pressure-mounted quartz plate in metal holder designed to operate on the fifth mechanical harmonic of the fundamental frequency of the quartz plate. Used as a very-high-frequency control element in circuits which must maintain aboveaverage frequency stability in the absence of oven control, even when exposed to wide variations in temperature and to relatively high drive levels. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 50 to 87 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fifth mechanical harmonic
Maximum Drive Level: 20 mw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu$
Maximum Effective Resonance Resistance: 60 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures 1-49, -112, -113, -115, -118.

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, capacitance-bridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-6/U
Method of Mounting Crystal: Pressure-mounted in metal holder
Dimensions and Marking: See figure 2-63(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 1)
Date of Status: 14 January 1954
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Some manufacturers cannot produce this unit over the entire upper or lower ranges and meet all requirements of the specification.
Equipment Used In:

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Figure 2-64. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-53/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A or B
Drive Adjustment Procedure: MS90168 (see para-
graph 2-62 and MIL-C-3098B), with the exception that the resistance shall be 60 ohms and voltage shall be 1.1 volts.
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.002 \%$
Permitted change in effective resonance resistance: Shall not exceed the max effective resistance
Aging Test: Not required
Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-54/U (VHF)



Figure 2-65. Crystal Unit CR-54/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fifth mechanical harmonic of the fundamental frequency of the quartz plate. Used as a very-highfrequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to* wide variations in temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 50 to 87 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm{ }^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resomumer: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fifth mechanical harmonic
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effcotive Resonance Resistance: 60 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures 1-49, -112, $-113,-115,-118$.

TYPES OF CIRCUITS USED IN
Butler, transformer-coupled, capacitance-bridge, transitron, impedance-inverted

## MOUNTING DATA

## Crystal Holder: HC-6/U

Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-65 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 1)
Date of Status: 14 January 1954
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: Some manufacturers cannot produce this unit over the entire upper or lower ranges and meet all requirements of the specification. Same as CR-23/U except designed to operate on 5 th mode only.
Equipment Used In:


Figure 2-66. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-54/U

[^16]Drive Adjustment Procedure: MS90168 (see paragraphs 2-62 and 2-64 per MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms , whichever is greater Aging Test:

Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-55/U

(HF-VHF)


Figure 2-67. Crystal Unit CR-5S/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a subminiature metal holder and designed to operate on the third mechanical harmonic of the fundamental frequency of the quartz plate. Used as a high- to very-high-frequency control element in transistor-cased or subminiature packaged circuits which must maintain above-average frequency stability in the absence of oven control, even when expused to extreme variations in temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 17 to 61 mc
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+105^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series

Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Third mechanical harmonic
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance: 40 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element $A$, paragraph 1-112, figures $1-49,-112,-113,-115,-118$.

## TYPES OF CIRCUITS USED IN

Transistor, Butler, transformer-coupled, capaci-tance-bridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-18/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-67(B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.


Figure 2-68. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-55/U

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Standard (Category 1)
Date of Status: 9 December 1955
Related Specifications, Standards, and Publications: See Appendix IV.
Commercial Sources: See Appendix III.
Remarks: None
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-3098B, approved 9 December 1955
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.

Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure: MS90168 (see paragraphs 2-62 and 2-64 per MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms, whichever is greater Aging Test: Not required

## Tensile Strength Test (Minimum Requirements):

 Not required

Figure 2-69. Crystal Unif CR-56/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a subminiature metal holder and designed to operate on the fifth harmonic of the fundamental frequency of the quartz plate. Used as a very-highfrequency control element in subminiature circuit applications which must maintain above-average frequency stability in the absence of oven control, even when exposed to extreme variations in temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 50 to 87 mc (Experimental Crystal Unit CR-56/U (XN-1) extends the frequency range to 121.5 mc )

Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Frequency Deviation with Temperature:
Operating Temperature Range: - $55^{\circ}$ to $+105^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Series

## Load Capacitance: Not applicable

Harmonic of Quartz Vibration: Fifth harmonic mode
Maximum Drive Level: 2 mw
Maximum Pin-to-Pin Capacitance: $7.0 \mu \mu \mathrm{f}$
Maximum Effective Resonance Resistance: 60 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures 1-49, -112,-113, -115, -118

TYPES OF CIRCUITS USED IN
Butler, transformer-coupled, capacitancebridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-18/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-69 (B) . All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.


Figure 2-70. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-56/U

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Standard (Category 1)
Date of Status: 9 December 1955
Related Specifications, Standards, and Publications: See Appendix IV
Commercial Sources: See Appendix III
Remarks:
Equipment Used In:
MILITARY STANDARD TEST DATA
Authority: MIL-C-3098B (Date 9 Dec 1955)
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.

Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance:
Drive Adjustment Procedure: MS90168 (see paragraphs 2-62 and 2-64 per MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or ohms, whichever is greater
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$
Tensile Strength Test (Minimum Requirements):
Not required

## CRYSTAL UNIT CR-57/U



Figure 2-71. Crysfal Unit CR-57/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a 500 -ke control element in circuits where maximum frequency stability is required. The crystal unit is intended to be mounted in a temperature-controlled oven and operated at parallel resonance.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 500 kc
Nominal Frequency Tolerance: $\pm 0.001 \%$ at $85^{\circ} \mathrm{C}$, $\pm 1^{\circ} \mathrm{C}$
Frequency Deviation with Temperature: $\pm 0.0003 \%$ from the measured frequency at $85^{\circ} \mathrm{C}$ permitted over range of $80^{\circ} \mathrm{C}$ to $90^{\circ} \mathrm{C}$
Operating Temperature Range: $85^{\circ} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: - $55^{\circ}$ to $+20^{\circ}$ $\pm 2^{\circ} \mathrm{C}$, but not necessarily within tolerance on nominal frequency. $0.005 \%$ tolerance required from $+20^{\circ}$ to $+80^{\circ} \mathrm{C}$
Resonance: Parallel
Load Capacitance: $32.0 \pm 0.5 \mu \mu \mathrm{f}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level: 0.5 mw
Maximum Pin-to-Pin Capacitance: $7.0_{\mu \mu} \mathrm{f}$

## Maximum Effective Resonance Resistance:

 Frequency (kc) Resistance (ohms) 500 3000
## PERFORMANCE CHARACTERISTICS OF

 NORMAL CRYSTAL ELEMENTSee characteristics of element $C$, paragraph 1-115, figure 1-51

TYPES OF CIRCUITS USED IN
Pierce, Miller

## MOUNTING DATA

## Crystal Holder: HC-6/U

Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-71 (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100 -
Status: Special Application (Category 1)
Date of Status: 5 March 1956
Related Specifications, Standards, and Publications: See Appendix IV


Figure 2-72. Schematic diagram of typical oscillator designed for use with Crystal Unil CR-57/U

Commercial Sources: See Appendix III
Remarks:
Equipment Used In: R.F. Oscillator O-197/U, p/o Radio Set AN/ARC-21

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-25538 (USAF)
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50
Reference Standard Test Set: Crystal Impedance Meter TS-710/TSM

Electrical Connection of Holder: Holder grounded

Method of Measuring Frequency and Effective Resonance Resistance: B
Drive Adjustment Procedure: MS91446(see paragraph 2-65 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$ or 2 ohms
Aging Test:
Permitted change in frequency: $\pm \mathbf{0 . 0 0 0 5} \%$

Tensile Strength Test (Minimum Requirements): Not required

## CRYSTAL UNIT CR-58/U <br> (MF-HF)



Figure 2-73. Crystal Unit CR-58/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits which must maintain above-average frequency stability in the absence of oven control, even when exposed to wide variations of temperature. The crystal unit is intended for operation at parallel resonance.

RATED OPERATING CHARACTERISTICS
Frequency Range: 800 to $20,000 \mathrm{kc}$
Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within operating range
Frequency Deviation with Temperature: Permissible within limits of nominal frequency tolerance
Operating Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$ $\pm 2^{\circ} \mathrm{C}$
Operable Temperature Range: Not specified beyond operating temperature range
Resonance: Parallel
Load Capacitance: $32 \pm 0.5 \mathrm{mmf}$
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
800 to $9,999.999 \mathrm{kc}-10 \mathrm{mw}$
10,000 to $20,000 \mathrm{kc}-5 \mathrm{mw}$

Maximum Pin-to-Pin Capacitance: 7.0 mmf
Maximum Effective Resonance Resistance:

| Frequency (ke) |  | Resistance (ohms) |
| :---: | :---: | :---: |
| 800 to | 999.999 | 1000 |
| 1000 to | 1,249.999 | 800 |
| 1250 to | 1,499.999..... | 700 |
| 1500 to | 1,749.999.................... | 600 |
| 1750 to | 1,999.999................. | 550 |
| 2000 to | 2,249.999................. | 320 |
| 3000 to | 3,749.999.................... | 175 |
| 3750 to | 4,749.999................... | 120 |
| 4750 to | 5,999.999................... | 75 |
| 6000 to | 7,499.999............. | 50 |
| 7500 to | 9,999.999 ................ | 35 |
| 10,000 to | 20,000 ........................... | 25 |

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph $1-112$, figures $1-49,-112,-113,-115,-118$

## TYPES OF CIRCUITS USED IN

Pierce, Miller, multivibrator-type

## MOUNTING DATA

Crystal Holder: HC-17/U
Method of Mounting Crystal: Wire-mounted in metal holder.


Figure 2-74. Schematic diagram of typical oscillator designed for use wilh Crysfal Unil CR-58/U

Dimensions and Marking: See figure 2-73. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special Appiication (Category 2)
Date of Status: 15 December 1955
Related Specifications, Standards, and Publications: See Appendix IV
Commercial Sources: See Appendix III
Remarks: Identical to CR-18/U except uses Holder $\mathrm{HC}-17 / \mathrm{U}$ (with larger pins) instead of $\mathrm{HC}-6 / \mathrm{U}$. Equipment Used In:

MILITARY STANDARD TEST DATA
Authority: Military Specification MIL-C-25498 (USAF)
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50
Reference Standard Test Set:
Crystal Impedance Meter TS-330/TSM-800 to $14,999.999 \mathrm{kc}$

Crystal Impedance Meter TS-683/TSM—15,000 to $20,000 \mathrm{kc}$
Electrical Connection of Holder:
Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A
Drive Adjustment Procedure:
800 to $14,999.999 \mathrm{kc}$ : MS90167 (see paragraph 2-60 and MIL-C-3098B)
15,000 to $20,000 \mathrm{kc}$ : MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.001 \%$ for units below 2000 kc $\pm 0.0005 \%$ for units of 2000 kc and above
Permitted change in resonance (effective) resistance: Wire-mounted $- \pm 15 \%$ or 2 ohms, whichever is greater.
Aging Test: Not required
Tensile Strength Test (Minimum Requirements): Not required


Figure 2-75. Crystal Unit CR-59/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, mounted in a metal holder and designed to operate at series resonance on the fifth harmonic of the fundamental frequency of the quartz plate. The crystal is intended to be mounted in a temperature-controlled oven.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 50.0 to 91.0 mc
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $+85^{\circ} \mathrm{C} \pm 5^{\circ} \mathrm{C}$
Frequency Deviation with Temperature: $\pm 0.0005 \%$ from frequency measured at $85^{\circ} \mathrm{C}$ permitted over range of $80^{\circ} \mathrm{C}$ to $90^{\circ} \mathrm{C}$
Operating Temperature Range: $85^{\circ} \mathrm{C} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fifth harmonic mode
Maximum Drive Level: 1.0 mw
Maximum Pin-to-Pin Capacitance: $7 \mu \mu$
Maximum Effective Resonance Resistance: 60 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph $1-112$, figures $1-49,-112,-113,-115,-118$

## TYPES OF CRRCUITS USED IN

Butler, transformer-coupled, capacitancebridge, transitron, impedance-inverted

## MOUNTING DATA

Crystal Holder: HC-18/U
Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-75. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special Application (Category 1)
Date of Status:
Related Specifications, Standards, and Publications: See Appendix IV
Commercial Sources: See Appendix III
Remarks:
Equipment Used In:

hote: all capacitamee is in $\mu \mu \mathrm{H}$.

Figure 2-76. Schematic diagrom of Iypical oscillator designed for use whi Crystal Unif CR-59/U

## MILTTARY STANDARD TEST DATA

Authority: Military Specification MIL-C-25709 (USAF)
Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure: MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm \mathbf{0 . 0 0 1 \%}$

## Tensile Strength Test (Minimum Requirements): Not required



Figure 2-77. Crystal Unit CR-60/U

## FUNCTIONAL DESCRIPTION

Metal-plated quartz plate, wire-mounted in a metal holder and designed to operate on the fundamental frequency of the quartz plate. Used as a medium-to-high-frequency control element in circuits which must maintain above average frequency stability in the absence of oven control, even when exposed to wide variation of temperature. The crystal unit is intended for operation at series resonance.

## RATED OPERATING CFARACTERISTICS

## Frequency Range: 7.0 to 20.0 mc

Nominal Frequency Tolerance: $\pm 0.005 \%$ at all temperatures within the operating range
Froqueney Deviation with Temperature: Permissible within limits of nominal frequency tolerance

Operating Temperature Range: $-55^{\circ}$ to $+105^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Fundamental
Maximum Drive Level:
7.0 to 9.999999 mc ( 10 mw )
10.0 to 20.0 mc ( 5 mw )

Maximum Pin-to-Pin Capacitance: $7 \mu \mu \mathrm{f}$

Maximum Effective Resonance Resistance:

Frequency (me)
7.0 to 9.999
10.0 to 20.000

## PERFORMANCE CHARACTERISTICS OF

 NORMAL CRYSTAL ELEMENTSee characteristics of element A, paragraph $1-112$, figures $1-49,-112,-113,-115,-118$

## TYPES OF CIRCUITS USED IN

Butler, transformer-coupled, transitron, modified colpitts

## MOUNTING DATA

Crystal Holder: HC-18/U
Method of Mounting Crystal: Wire-mounted in metal holder.
Dimensions and Marking: See figure 2-77. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 1)
Date of Status:
Related Specifications, Standards, and Publications: See Appendix IV
Commercial Sources: See Appendix III
Remarks: Similar to CR-19/U except frequency range and size of holder.
Equipment Used In:


Figure 2-78. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-60/U

## MILITARY STANDARD TEST DATA <br> Authority: Military Specification MIL-C-25710 (USAF)

Requirements and Prooedures of Tests: See paragraphs 2-21 through 2-50

Reference Standard Test Set:

| Frequency $(m c)$ | Test Set |
| :---: | :---: |
| 7.0 to 9.999 | TS-330/TSM |
| 10.0 to 20.0 | TS-683/TSM |

Electrical Connection of Holder: Holder grounded
Method of Measuring Frequency and Effective Resonance Resistance: A

Drive Adjustment Procedure:
7.0 to 9.999 mc: MS90167 (see paragraph 2-60 and MIL-C-3098B)
10.0 to 20.0 mc : MS90168 (see paragraph $2-62$ and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitied change in effeotive resonance risistance: $\pm 15 \%$
Aging Test: Not specified

Tensile Strength Test (Minimum Requirements): Not required


Figure 2-79. Crystal Unit CR-61/U

## FUNCTIONAL DESCRIPTION

A metal-plated, quartz plate mounted in a metal holder and designed to operate at series resonance on the third mechanical overtone of the fundamental frequency of the quartz plate. The crystal unit is intended to be operated at a controlled temperature.

## RATED OPERATING CHARACTERISTICS

Frequency Range: 17.0 to 61.0 mc
Nominal Frequency Tolerance: $\pm 0.002 \%$ at $85^{\circ} \mathrm{C}$
Frequency Deviation with Temperature: $\pm 0.0005 \%$ from frequency measured at $85^{\circ} \mathrm{C}$ permitted over range of $80^{\circ}$ to $90^{\circ} \mathrm{C}$
Operating Temperature Range: $85^{\circ} \mathrm{C} \pm 5^{\circ} \mathrm{C}$
Operable Temperature Range: $-55^{\circ}$ to $+90^{\circ} \mathrm{C}$
Resonance: Series
Load Capacitance: Not applicable
Harmonic of Quartz Vibration: Third harmonic mode
Maximum Drive Level:
17.0 to 24.999 mc ( 2 mw )
25.0 to 61.0 me ( 1 mw )

Maximum Pin-to-Pin Capacitance: $7_{\mu \mu \mathrm{f}}$
Maximum Effective Resonance Resistance: 40 ohms

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT

See characteristics of element A, paragraph 1-112, figures $1-49,-112,-113,-115,-118$

## TYPES OF CIRCUITS USED IN

Transistor, Butler, transformer-coupled, ca-pacitance-bridge, transitron, impedance-inverted

## MOUNTING DATA

## Crystal Holder: HC-18/U

Method of Mounting Crystal: Wire-mounted in metal holder
Dimensions and Marking: See figure 2-79. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status: Special application (Category 1)
Date of Status: 13 March 1956
Related Specifications, Stardards, and Publications: See Appendix IV
Commercial Sources: See Appendix III
Remarks:
Equipment Used In:


Figure 2-80. Schematic diagram of typical oscillator designed for use with Crystal Unit CR-61/U

## MILITARY STANDARD TEST DATA

Authority: Military Specification MIL-C-19374 (SHIPS), approved 13 March 1956
Requirements and Procedures of Tests: See paragraphs 2-21 to 2-50
Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
Electrical Connection of Holder: Holder grounded Method of Measuring Frequency and Effective Resonance Resistance: B

Drive Adjustment Procedure: MS90168 (see paragraph 2-62 and MIL-C-3098B)
Shock and Vibration Test:
Permitted change in frequency: $\pm 0.0005 \%$
Permitted change in effective resonance resistance: $\pm 15 \%$
Aging Test:
Permitted change in frequency: $\pm 0.001 \%$

Tensile Strength Test: Not required

## CRYSTAL UNIT CR- /U

(For addemda)

Figure 2-81. Crysfal Unif CR- /U

FUNCTIONAL DESCRIPTION

RATED OPERATING CHARACTERISTICS
Frequency Range:
Nominal Frequency Tolerance:
Frequency Deviation with Temperature:
Operating Temperature Range:
Operable Temperature Range:
Resonance:
Load Capacitance:
Harmonic of Quartz Vibration:
Maximum Drive Level:
Maximum Pin-to-Pin Capacitance:
Maximum Effective Resonance Resistance:

Frequency (kc)
Resistance (ohms)

Figure 2-82. Schematic diagram of lypical oscillator designed for use with Crystal Unif CR- /U

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status:
Date of Status:
Related Specifications, Standards, and Publications: See Appendix IV.

Commercial Sources: See Appendix III.
Remarks:
Equipment Used In:

## MILITARY STANDARD TEST DATA

 Authority:Requirements and Procedures of Tests: See paragraphs through
Reference Standard Test Set: Crystal Impedance Meter

## Electrical Connection of Holder:

Method of Measuring Frequency and Effective Resonance Resistance:
Drive Adjustment Procedure:

Shock and Vibration Test: Permitted change in frequency:

Permitted change in effective resonance resistance:

Aging Test:
Permitted change in frequency:

Tensile Strength Test (Minimum Requirements):
Frequency ( $k$ )
Grams

# CRYSTAL UNIT CR- /U 

(For addenda)

Figure 2-83. Crystal Unit CR-/U

## FUNCTIONAL DESCRIPTION

## Rated operating characteristics

Frequency Range:
Nominal Frequency Tolerance:
Frequency Deviation with Temperature:
Operating Temperature Range:
Operable Temperature Range:
Resonance:
Load Capacitance:

## MOUNTING DATA

Crystal Holder:
Method of Mounting Crystal:
Dimensions and Marking: See figure 2- (B). All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.
Maximum Pin-to-Pin Capacitance:

# PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT 

See characteristics of element , paragraph
1- , figure 1-
TYPES OF CIRCUITS USED IN

Harmonic of Quartz Vibration:
Maximum Drive Level:
Maximum Effective Resonance Resistance:
Frequency (kc) Resistance (ohms)

WADC TR 56-156

Figure 2-84. Schematic diagram of typical oscillator designed for use with Crystal Unil CR- /U

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status:
Date of Status:
Related Specifcations, Standards, and Publications: See Appendix IV.

Commercial Sources: See Appendix III.
Remarks:
Equipment Used In:

MILITARY STANDARD TEST DATA
Authority:
Requirements and Procedures of Tests: See paragraphs through
Reference Standard Test Set: Crystal Impedance Meter

Electrical Connection of Holder:

Method of Measuring Frequency and Effective Resonance Resistance:
Drive Adjustment Procedure:

Shock and Vibration Test:
Permitted change in frequency:

Permitted change in effective resonance resistance:

Aging Test:
Permitted change in frequency:

Tensile Strength Test (Minimum Requirements):
Frequency (kc)
Grams

# CRYSTAL UNIT CR- <br> /U 

(For addenda)

Figure 2-85. Crysial Unit CR- /U

## FUNCTIONAL DESCRIPTION

## RATED OPERATING CHARACTERISTICS

Frequency Range:
Nominal Frequency Tolerance:
Frequency Deviation with Temperature:
Operating Temperature Range:
Operable Temperature Range:

## Resonance:

Load Camacitance:
Harmonir of Quartz Vibration:
Maximum Drive Level:
Maximum Pin-to-Pin Capacitance:

Maximum Effective Resonance Resistance:
Frequency (kc) Resistance (ohms)

## PERFORMANCE CHARACTERISTICS OF NORMAL CRYSTAL ELEMENT <br> See characteristics of element , paragraph 1- , figure 1 - <br> TYPES OF CIRCUITS USED IN

Figure 2-86. Schematic diagram of typital oscillator designed for use with Crystal Unit CR- IU

## LOGISTICAL DATA

USAF Stock No.: 2100-
Status:
Date of Status:
Related Specifications, Standards, and Publications: See Appendix IV.

Commercial Sources: See Appendix III.
Remarks:
Equipment Used In:

## MILITARY STANDARD TEST DATA

Authority:
Requirements and Procedures of Tests: See paragraphs through
Reference Standard Test Set: Crystal Impedance Meter

Electrical Connection of Holder:

Method of Measuring Frequency and Effective Resonance Resistance:
Drive Adjustment Procedure:

Shock and Vibration Test:
Permitted change in frequency:

Permitted change in effective resonance resistance:

```
Aging Test:
Permitted change in frequency:
```

Tensile Strength Test (Minimum Requirements):
Frequency (ke)
Grams

## CRYSTAL UNITS CURRENTLY IN MILITARY SERVICE BUT NOT RECOMMENDED FOR USE IN EQUIPMENTS OF NEW DESIGN

> The crystal units included in Group II are those currently being used by the United States Air Force, but which are not preferred for use in equipments of new design. Where available, data sheets are included giving the quality control test specifications of the individual units. For illustrations of the principal holders, see Crystal Holders-Group II in Section III.

TECHNICAL DATA CHART FOR GROUP-II CRYSTAL UNITS

| USAF Stock Number 2100 -a | Nomenclature | Crustal <br> Holder | Equipment Used In | Crystal Spec | Holder Spec |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2x4- | Crystal Unit CR-1A/AR | CR-1A/AR | AN/ARC-7, AN/ARM-1, BC-517, BC-624, BC-625, BC-640, BC-1158, R-77/ARC-3, <br> R-89 ( )/ARN-5A, R-150A/CRW-7 | MIL-C-16B | MIL-C-16B |
| 2x5- | Crystal Unit | FT-249 |  |  | 171-148B |
| 2x7- | Crystal Unit CR-6B/U | FT-243 | R-19/TRC-1 | MIL-C-10405 | 72-119 |
| 2x8- | RCA MI-8412 | MI-8412 | RCA Model AVT-15, RCA Model AVT-112 | MIL-C-10405 |  |
| 2x10- | Crystal Unit | FT-243 | BC-745; SCR-511 |  | 72-119 |
| 2x11- | Crystal Unit | FT-243 | BC-745; SCR-511 |  | 72-119 |
| 2x12- | Crystal Unit | FT-171-8 | $\begin{aligned} & \text { BC-610; SCR-299, 399, 499, } \\ & 699 \end{aligned}$ | M1L-C-10405 |  |
| 2x13- | Crystal Unit CR-4B/U | FT-241-A | AN/TRC-1, -3, -4 |  |  |
| 2x14- | Crystal Unit | FT-243 |  |  | 72-119 |
| 2x15-5000 | Crystal Unit CR-10B/U | FT-243 | R-48/TRC-8, 1-222-A |  | 72-119 |
| $2 \times 16-80.86$ | Valpey Crystal Part XLST |  | AN/APS-15 Rec. |  |  |
| $2 \times 17-$ | Crystal Unit (1st Osc) | FT-171B | FM-1498-1505 (Link) | M1L-C-10405 | 72-119 |
| 2x17- | Crystal Unit (2nd Osc) | FT-243 | FM-1498-1505 (Link) | MIL-C-10405 | 72-119 |
| 2x18- | Crystal Unit | $\begin{aligned} & \hline \text { FT-171-B/ } \\ & \text { FT-243 } \end{aligned}$ | Link Xmtr 1498 | MIL-C-10405 | 72-119 |
| $2 \times 20-$ | Crystal Unit | AVA-10 or 601 | RCA Model AVT-15, RCA Model AVT-112 | MIL-C-10405 | 72-119 |
| 2x23- | Crystal Unit (Collins 1C) |  | Collins 32-RA | MLL-C-10405 |  |
| 2x24-163.94 | Crystal Units (Bliley MC- <br> 72) (James Knights F) |  | 1-223-A |  |  |
| 2x25-455 | Crystal Unit (Bliley CF-6) <br> (Hallicrafters 19A123) |  | SX-28, R-45/ARR-7 |  |  |

asè paragrmph 2-69.

| Freq Range (me) | Freq Toleranee ( $\pm \%$ ) | Operating Temperature Range ( ${ }^{\circ} \mathrm{C}$ ) | Base or Terminal Connections | Physical Dimensions (In.) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | High | Wide | Thick |
| 2.0-15.0 | 0.02 | $-55^{\circ}$ to $+90^{\circ}$ | 2 pins, $8 / 8 \mathrm{in} . \lg , 1 / 4$ in. dia, $1 / 2 \mathrm{in}$. ctoc | 17/4 | 1/4 | 7/4 |
|  |  |  | 3 pins, 0.125 in. dia, $1 / 2 \mathrm{in} . \lg$ | 211/6 | 1716 | 1\% |
| 2.0-10.0 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | 2 pins, $1 / 32 \mathrm{in} . \lg , 3 / 32$ in. dia, $1 / 2 \mathrm{in}$. c to c | 111/32 | 11/16 | $1: 682$ |
| 2.0-5.8 | 0.015 | $0^{\circ}$ to $+70^{\circ}$ | 2 banana pins, $19 / 16 \mathrm{in} . \mathrm{lg}, 0.85 \mathrm{in}$. etoc | 1\%32 | 11/2 | $12 / 16$ |
| 3.0-6.0 |  |  | Same as 2x7 |  |  |  |
| $\begin{aligned} & 3.465 \\ & 6.455 \end{aligned}$ |  |  | Same as 2x7 |  |  |  |
| 2.0-6.0 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ |  c to c | 23/4 | 11/2 |  |
| 70.0-99.9 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | 2 pins, $7 / 18$ in. $\lg , 7 / 14$ in. dia, $1 / 2 \mathrm{in}$. c to c | $11 / 4$ | 11/4 | 718 |
| 2.88-4.3 |  |  | Same as 2x7 |  |  |  |
| 5.0 | 250 cps | $-40^{\circ}$ to $+70^{\circ}$ | Same as 2x7 |  |  |  |
| 0.08086 |  |  | NL |  |  |  |
| 6.25-10.5 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ | Same as 2x12 |  |  |  |
| 6.456 | 0.02 | $0^{\circ}$ to +70* | Same as 2x12 |  |  |  |
| 2.187-2.125 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 12$ or $2 \times 7$ |  |  |  |
| 1.715-7.5 | 0.015 | $0^{\circ}$ to $+70^{\circ}$ | 2 banana pins, $\%$ in. $\lg , 0.850 \mathrm{in}$. c to c | 2\% | 11/2 | $11 / 18$ |
| 1.5-3.75 | 0.015 | $0^{\circ}$ to $+50^{\circ}$ | 5-pin, 1/2 in. $1 \mathrm{~g}, 1 / \mathrm{in}$. dia | $17 / 8$ | 11/2 | 11/4 |
| 0.16394 |  |  | 2 banana pins, $1 / 2 \mathrm{in} .1 \mathrm{~g}, 3 / 4 \mathrm{in} . \mathrm{c}$ to c | $1 \%$ | 11/6 | 51/10 |
| 0.455 |  |  | NL |  |  |  |

Saction II
Crystal Units-Group II
TECHNICAL DATA CHART FOR GROUP-II CRYSTAL UNITS_Continued

| USAF Stock Number 2100 - | Nomenclature | Crystal Holder | Equipment Used In | Crizstal Spec | Holder Spee |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2x27-465 | Crystal Unit | RCA-MI-19453 <br> Hammarlund <br> SA- 178 | $\begin{aligned} & \text { AN/GRR-2, BC-1004, } \\ & \text { AN/MRC-3, }-4 \end{aligned}$ |  |  |
| 2x 28 - | Crystal Unit | HC-1/U | AN/URC-2, AN/FRC-6 | MLL-C-10404 |  |
| 2x29- | Crystal Unit. | FT-249 | SCR-281, BC-441 | MIL-C-10404 |  |
| 2x34-455 | Crystal Unit (Majestic Dwg 29E6) |  | BC-969-A, SCR-614-A |  |  |
| 2x $35-$ | Crystal Unit CR-5B/U | FT-243 | BC-611, SCR-536 | MIL-C-23913 | 72-119 |
| 2x36- | Crystal Unit CR-5B/U | FT-243 | BC-1000, SCR-300 | MIL-C-239B | 72-119 |
| 2x37- | Crystal Unit (Bliley AR-3) |  | RC-65 |  |  |
| 2x38- | Crystal Unit | FT-249 | BC-1271-A, Wilcox 98A | MIL-C-10405 |  |
| 2x39 | Crystal Unit | FT-164 | RC-52E, BC-797, SCR-641 |  |  |
| $2 \times 40$ - | Crystal Unit (Monitor Piezo 8), (Bendix 3947) | Special | $\begin{array}{\|l\|} \hline \text { SCR-638, Bendix FC-3006, } \\ 3103-24,3806-24 \\ \hline \end{array}$ |  |  |
| 2x43- | Crystal Unit (Bliley MO-2) |  | Hallicrafters $\mathrm{HT}-4,-9$, T-811/VRC-4 |  |  |
| 2x48- | Crystal Unit DC-8 |  | BC-225, -338, -352, -353, $-457,-458,-459,-695,-696$, SCR-240, 261, 264, -274N |  |  |
| $2 \times 50-$ | Crystal Unit DC-20 | FT-243 | BC-733, $\mathrm{RC}-103$ | M1L-C-10404 | 72-119 |
| 2x53- | Crystal Unit CR-8B/U | FT-243 | RT-12/TRC-2, BC-1306, RT-77/GRC-9 | MLL-C-10405 | 72-119 |
| 2x54-12500 | Crystal Unit (Bliley MO-2) | $\begin{aligned} & \text { Bliley MC-5 } \\ & \text { or }-7 \end{aligned}$ | BC-376 |  |  |
| 2x55- | Crystal Unit CR-10/U | FT-243 |  | MIL-C-10405 | 72-119 |
| 2x58- | Crystal Unit | FT-243 | BC-659, SCR-609, -610 | MIL-C-10405 | 72-119 |
| 2x60- | $\begin{aligned} & \text { Crystal Unit (RCA } \\ & \text { TMV-129-B) } \end{aligned}$ |  | RCA transmitter 1-K. |  |  |
| 2x61- | Crystal Unit | RCA-AVA-53-A | RCA Models AVT-15, -112, ARV-20 | MIL-C-10405 |  |
| 2x62-327.8 | Crystal Unit <br> (WECOD-168342) |  | TS-102/AP |  |  |
| 2x63- | Crystal Unit (WECO5B) |  | Northern Elec. AT-7 |  |  |
| 2x64-1 | Crystal Unit |  |  |  |  |
| 2x65- | Crystal Unit | FT-243 | R-57/ARN-5 | MIL-C-16B | 72-119 |
| $2 \times 66$ - | Crystal Unit | FT-243 | BC-1209, SCR-583 (Xmtr only) |  | 72-119 |
| 2x67- | Crystal Unit | FT-243 | BC-1209, SCR-583 (Rec only) |  | 72-119 |
| $2 \times 68$ - | Crystal Unit DC-34 | FT-171-B | BC-669, SCR-543 (Xmtr only) |  |  |

- See paragraph 2-59.

| Freq Range ( $m e$ ) | Freq <br> Tolerance (土\%) | Opernting Temperature Ranye ( ${ }^{\circ} \mathrm{C}$ ) | Bute or Terminal Connections | Physical Limensione ( 1 n .) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | High | Wide | Thick |
| 0.465 |  |  | NL |  |  |  |
| 0.9375-8.2 | 0.01 | $-55^{\circ}$ to $+90^{\circ}$ | 2 pins, $1 / 10 \mathrm{in} . \mathrm{Ig}, 1 / 8 \mathrm{in}$ dia, 8 in in ctoc | 1\%3 | 11/8 | 11/8 |
| 1.6-3.0 | 0.01 | $0^{\circ}$ to $+50^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 0.455 |  |  | NL |  |  |  |
| 2.0-10.0 | 0.02 | $-55^{\circ}$ to $+90^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| $\begin{aligned} & 4.3 \text { (Xmtr) } \\ & 6.815 \text { (Rec) } \end{aligned}$ | 0.02 | $-55^{\circ}$ to $+90^{\circ}$ | Same as 2x7 |  |  |  |
| 30-40 |  |  | $5-\mathrm{pin}, 1 / \mathrm{in} . \lg , 1 / 8 \mathrm{in}$. | 2 | 1488 | $1{ }^{1 / 18}$ |
| $\begin{aligned} & 4.8375 \\ & 7.458611 \end{aligned}$ | 0.01 | $0^{\circ}$ to $+70^{\circ}$ | Same as 2x5 |  |  |  |
| 1.7-9.0 |  |  | Term. pin on each side, $1 / 2 \mathrm{in}$. lg, T/w in. dia | 15/6 | 2\%0 (dia) |  |
|  |  |  | Octal | $11 / 4$ | 11/2 (dia) |  |
| 1.7-7.5 | 0.02 | $0^{\circ}$ to $+50^{\circ}$ | 2 pins, $4 / 10 \mathrm{in} . \mathrm{lg}, 1 / 8 \mathrm{in}$ dia, $3 / 4 \mathrm{in}$. c to c | 1410 | 14/3 (dia) |  |
| $3.0-8.0$ |  |  | Octal | $2^{13 / 32}$ | 11/32 (dia) |  |
| $\begin{aligned} & 5.633- \\ & 5.744444 \end{aligned}$ | 0.02 | $-40^{\circ}$ to $+85^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| $1.0-10.0$ | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| 12.5 |  |  | Same as 2x43 |  |  |  |
| 5.0 | 0.005 | $-40^{\circ}$ to $+70^{\circ}$ | Same as 2x7 |  |  |  |
| 5.675-8.650 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| 0.325-3.0 | 10 cps | +60 ${ }^{\circ}$ | 6-pin, $7 / 4 \mathrm{in} . \lg , \frac{9}{32} \mathrm{in}$ dia | 4 | $21 / 2$ | 13/16 |
| 1.75-7.5 | 0.015 | $-40^{\circ}$ to $+55^{\circ}$ | 2 banana pins, $7 / 4 \mathrm{in} . \mathrm{lg}, 0.85 \mathrm{in}$. ctoc | 17/6 | 13/4 | 9/88 |
| 0.3278 |  |  | NL |  |  |  |
|  |  |  |  | 27\% 21 | 11\%2 | $3 / 18$ |
| 0.375 and 0.5 |  |  |  | 127/32 | $118 / 3$ | 13/12 |
| $\begin{aligned} & 6.497917 \\ & 6.547917 \end{aligned}$ | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 7$ |  |  |  |
|  |  |  | Same as 2x7 |  |  |  |
|  |  |  | Same as 2x7 |  |  |  |
|  |  |  | Same as $2 \times 12$ |  |  |  |

Section II
Crystal Units-Group II
TECHNICAL DATA ChART FOR GROUP-II CRYSTAL UNITS-Comtined

| USAF Stock Number $2100-4$ | Nomenclature | Crystal Holder | Equipmont Used In | Crystal Spee | Holder Spec |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2x69 | Crystal Unit DC-35 | FT-171-B | BC-669, SCR-543 (Ree only) |  |  |
| 2x70- | Crystal Unit | FT-164 | BC-400-() |  |  |
| 2x70-4166.67 | Crystal Unit | FT-164 | BC-400-B thru G |  |  |
| 2x73-186.30 | Crystal Unit (James Knights Type F) |  | BC-1267, I-293-A, TS-293/CPA-5, AN/CPX-1, -2 |  |  |
| 2x74- | Crystal Unit | FTT-241-A | BC-604, SCR-508, 5228 |  |  |
| 2x75- | Crystal Unit | FT-249 | AN/FRR-3 |  |  |
| 2×75-462.45 | Crystal Unit |  |  |  |  |
| 2x76- | Crystal Unit | FT-249 | Temeo Xmtr 250 GSC |  |  |
| 2x77- | Crystal Unit | FT-171-B | SCR-298, Link FM Model 11-U-F | MIL_C-10405 |  |
| 2x78- | Crystal Unit | FT-171-B |  |  |  |
| 2x79- | Crystal Unit | FT-249 | BC-329-N | MIL-C-10405 |  |
| 2x81- : | Crystal Unit | FT-171B | R-114/VRC-4 |  |  |
| 2x83-81.95 | Crystal Unit (GE TYPE 53) |  | BC-1602, SCR-584 |  |  |
| 2x84- | Crystal Unit | FT-171-B | BC-325, SCR-197-F |  |  |
| 2x86-1 | Crystal Unit <br> (WECOD-151584) |  | R-55/ARQ-9 |  |  |
| 2x87- | Crystal Unit | FT-164 | Fed T \& T TLC, TSI |  |  |
| 2x89-100 | $\begin{aligned} & \text { Crystal Unit (RCA } \\ & \text { VC-5KS) } \end{aligned}$ | RCA VC-5-KL | $\begin{aligned} & \text { BC-1184, SCR-722, } \\ & \text { ID-6/APN-4 } \end{aligned}$ |  |  |
| 2x90-470 | Crystal Unit DC-6 |  | $\begin{aligned} & \text { SCR-177,-185,-188,-193, } \\ & -209,-210,-287 \end{aligned}$ |  |  |
| 2x91- | Crystal Unit DC-17A |  | BC-751, AN/MRN-1 |  |  |
| 2x95-245.895 | Crystal Unit DC-21 |  |  |  |  |
| 2x95- | $\begin{aligned} & \text { Crystal Unit DC-13 and } \\ & \text { DC-14 } \end{aligned}$ |  | BC-308, SCR-241 |  |  |
| 2x96- | Crystal Unit | FT-164 | $\begin{aligned} & \text { T-65/CRN-11, AN/CRN-20, } \\ & \text { BC-901, RC-139 } \end{aligned}$ |  |  |
| 2x98- | Crystal Unit | FT-241-A | BC-684, SCR-608 |  |  |
| $2 \times 100-100$ | Crystal Unit (Bliley SMC-100) |  | Hallicrafters HT-7 |  |  |
| $2 \times 103-93.12$ | $\begin{aligned} & \text { Crystal Unit (GE Dwg } \\ & \text { K-66J906) } \end{aligned}$ |  | $\begin{aligned} & \text { TS-177/CPS-1, } \\ & \text { TS-241/CPS-5 } \end{aligned}$ |  |  |
| 2x104-100 | $\begin{aligned} & \text { Crystal Unit (RCA } \\ & \text { VC- } 5-\mathrm{M} \text { ) } \end{aligned}$ |  | R-65/APN-9 |  |  |
| 2x105-200 | Crystal Unit CR-2B/U | FT-241/A | AN/ART-18 |  |  |
| 2×106- | Crystal Unit | FT-249 | BC-401 | MIL-C-10405 |  |

- See paragraph 2-5y.

| Freg Range (mo) | Freq Tolerance ( $\pm \%$ ) | Operating Temperature Range ( ${ }^{\circ} \mathrm{C}$ ) | Base or Torminal Connections | Physical Dimensions (In.) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | High | Wide | Thick |
|  |  |  | Same as $2 \times 12$ |  |  |  |
| 4.116 and 4.687 | 0.01 | $-15^{\circ}$ to $+50^{\circ}$ | Same as 2x39 |  |  |  |
| 4.16667 | 0.01 | $-15^{\circ}$ to $+50^{\circ}$ | NL |  |  |  |
| 0.1863 |  |  | NL |  |  |  |
|  |  |  | Same | $2 \times 13$ |  |  |
| 1.4-3.8 | 0.01 | $+45^{\circ}$ to $+55^{\circ}$ | Same as $2 \times 5$ |  |  |  |
|  |  |  | NL |  |  |  |
|  |  |  | Same as $2 \times 5$ |  |  |  |
| 3.125-4.395 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 12$ |  |  |  |
| 1.875-2.875 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | NL |  |  |  |
| 0.2-0.4 | 0.01 | $-10^{\circ}$ to $+50^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 1.175-8.175 |  |  | Same as $2 \times 12$ |  |  |  |
|  |  |  | Octal, 2-pin, 3 \%/44 in. $\lg$, 7/e in. dia | $3{ }^{3}$ | 17/19 (dia) |  |
| 0.75-2.25 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 12$ |  |  |  |
| 5.0 and 5.455 |  |  |  | $17 / 16$ | $1{ }^{1 / 32}$ (dia) |  |
| $\begin{aligned} & 0.125-0.195 \\ & 0.3-0.4 \end{aligned}$ |  |  | Same as $2 \times 39$ |  |  |  |
| 0.100 | $\underset{\substack{+85 \\ \text { cps }}}{ }-35$ | $-40^{\circ}$ to $+70^{\circ}$ | 3-pin, $1 / 2 \mathrm{in} . \lg , 4 / 32 \mathrm{in}$. dia | $2 \%_{10}$ | 1\%18 | 13/6 |
| 0.470 |  |  | NL |  |  |  |
| $\begin{aligned} & 6.016,6.038, \\ & 6.061,6.083, \\ & 6.105,6.127, \\ & 0.245895 \end{aligned}$ |  |  | Octal | 21362 | 1\%/22 (dia) |  |
| 0.245895 |  |  | Same as $2 \times 89-100$ |  |  |  |
| $\begin{aligned} & \mathrm{DC}-13: 0.201 \\ & \mathrm{DC}-14: 0.219 \end{aligned}$ |  |  | Octal | 27/16 | 1\%/16 (dia) |  |
| 0.2-0.4 | 0.01 | $-15^{\circ}$ to $+60^{\circ}$ | Same as $2 \times 39$ |  |  |  |
|  |  |  | Same as $2 \times 13$ |  |  |  |
| 0.100 and 1.000 |  |  | 2 solder lugs | 1\%/8 | 1\% | $2_{32}$ |
| 0.09312 |  |  | Octal | $13 / 2$ | 1\%6 | 11318 |
|  |  |  | 3-pin, $39 / 4 \mathrm{in} . \mathrm{lg}, 0.156 \mathrm{in} . \mathrm{diz}$ | 247/44 | 11\%/32 | ${ }^{133 / 86}$ |
| 0.2 | 18 cps | $-40^{\circ}$ to $+70^{\circ}$ | Same a | 213 |  |  |
| 1.0-4.525 | 0.01 | $0^{\circ}$ to $+50^{\circ}$ | Same | $2 \times 5$ |  |  |

TECHNICAL DATA CHART FOR GROUP-II CRYSTAL UNITS-Continued

| $\begin{aligned} & \text { USAF Stock } \\ & \text { Number } \\ & 2100-\mathrm{a} \end{aligned}$ | Nomenclature | Crystal <br> Holder | Equipment Used In | Crystal Spec | Holder Spec |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2x107- | Crystal Unit | $\begin{aligned} & \text { FT-249, AA-9E, } \\ & \text { MX-9E } \end{aligned}$ | Bendix RA-10, RTA-1, AN/ARC-9 | MLL-C-10405 |  |
| 2x111-98.356 | Crystal Unit DC-22-A |  | BC-788, SCR-718 |  |  |
| 2x112-100 | Crystal Unit (Philco 455-1040) (RCA VC-5-KS) |  | BC-622 |  |  |
| 2x113-13545 | $\begin{aligned} & \text { Crystal Unit (WECO Dwg } \\ & \text { D-152497) } \end{aligned}$ |  | R-102/ARQ-9 |  |  |
| 2×116-300 | $\begin{aligned} & \text { Crystal Unit (WECO } \\ & \text { D-168342) } \end{aligned}$ |  | SCR-545-A |  |  |
| 2x121- | Crystal Unit | FT-164 | Fed Tel \& Rad CAA 293 |  |  |
| 2x122-18.626 | $\begin{aligned} & \text { Crystal Unit (WECO } \\ & \text { D-169112) } \end{aligned}$ |  | 1D-56/APQ-7 |  |  |
| 2x124- | Crystal Unit | Valpey CM.1, Bliley MC-74 | Comm. Co. 150C |  |  |
| 2x125- | Crystal Unit | FT-171-B | JT Rad Model 350-A (Rec) |  |  |
| 2x127- | Crystal Unit | FT-171-B | JT Rad Model 350-A (Xmtr) |  |  |
| 2x131- | Crystal Unit | FT-249 | T-4/FRC |  |  |
| 2x133- | Crystal Unit | FT-249 | Wilcox F3 | MIL-C-10405 |  |
| 2×136-12500 | Crystal Unit | FT-243 | BC-376-H |  | 72-119 |
| 2×137- | Crystal Unit | $\begin{aligned} & \text { FT-249, MX-9G, } \\ & \text { M-9G } \end{aligned}$ | Wilcox 96-200 |  |  |
| 2×138-100 | Crystal Unit (Bliley BC-46RS) |  | TS-308/U |  |  |
| 2x141-93.109 | Crystal Unit (RCA Type VC-5M) | RCA Type VC-5-K | ID-17/APN-3 |  |  |
| 2x142-80.86 | Crystal Unit (Biley FM-6) |  | TS-100/AP |  |  |
| 2×144- | Crystal Unit | FT-249 | Navy Model TCS |  |  |
| 2x147R- | Crystal Unit | FT-243 | BC-721 (Rec), SCR-585 |  | 72-119 |
| $2 \times 147 \mathrm{~T}$ | Crystal Unit | FT-243 | BC-721, SCR-585 (Xmtr) |  | 72-119 |
| 2x148- | Crystal Unit | FT-171 | Link FMTR-25, -35, UFS-50 |  |  |
| 2x149- | Crystal Unit | FT-164 | BC-329-A |  |  |
| $2 \times 150-93.109$ | Crystal Unit (RCA Type TMV-120E) |  | ID-18/CFN-2 |  |  |
| 2x154-300.060 | Crystal Unit (WECO 8A) |  | WECO 23AA, 221B |  |  |
| $2 \times 155-300$ | Crystal Unit (WECO 8B) |  |  |  |  |
| 2×156-300.050 | Crystal Unit (WECO 8C) |  |  |  |  |
| 2×157- | Crystal Unit | FT-243 | TS-233/TPN-2 |  | 72-119 |
| 2x163-1.81818 | Crystal Unit CR-11/U |  | TS-261/UP |  |  |
| 2x163-1817.44 | Crystal Unit CR-11/U |  | WECO D-170130 |  |  |
| $2 \times 167$ - | Crystal Unit | FT-164 | BC-446, BC-467, SCR-277 |  |  |
| 2x168- | Crystal Unit | FT-164 | BC-447 |  |  |

- See paragraph 2.59.

| Freq Range (mc) | Freq Tolerance ( $\pm \%$ ) | Operating Temperature Range ( ${ }^{\circ} \mathrm{C}$ ) | Base or Terminal Connections | Physical Dimensions (In.) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | High | Wide | Thick |
| 2.5-7.0 | 0.015 | $-40^{\circ}$ to $+55^{\circ}$ | Same as 2x5 |  |  |  |
| 0.098356 | 0.05 | $-10^{\circ}$ to $+50^{\circ}$ | Same as 2x89-100 |  |  |  |
| 0.1 |  |  |  | $2 \% 2$ | $1{ }^{163}$ | 1\%18 |
| 13.545 |  |  | 2-pin, $1 / 2 \mathrm{in} . \lg , 1 / \mathrm{in} . \mathrm{dia}$ | $11 \% 4$ | 11/4 | 7/10 |
| 0.3 |  |  | Octal | 3 | $11 / 4$ (dia) |  |
| 0.1-10.0 |  |  | Same as $2 \times 39$ |  |  |  |
| 0.018626 |  |  | Octal | 4 | 11/4 (dia) |  |
|  |  |  | NL |  |  |  |
|  |  |  | Same as $2 \times 12$ |  |  |  |
|  |  |  | Same as $2 \times 12$ |  |  |  |
| 2.0-6.0 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ | Same as 2x5 |  |  |  |
| 1.0-6.0 | 0.02 | $0^{\circ}$ to $+60^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 12.5 |  |  | Same as $2 \times 7$ |  |  |  |
| $0.125-0.525$ | 0.01 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 0.100 |  | $+50^{\circ}$ | 5 -pin, electrode pin, connection on side | 2\%14 | 24, (dia) |  |
| 0.093109 | 10 cps | $-54^{\circ}$ to $+70^{\circ}$ |  | 2\% | 17 | 1 |
| 0.08086 |  |  | 2-pin. $/ 4 \mathrm{in} . \lg , 1 / 4 \mathrm{in} . \mathrm{dia}, 3 \mathrm{in}$. ctoc | 121/20 | 13/4 (dia) |  |
|  |  |  | Same as $2 \times 5$ |  |  |  |
| 3.955-6.455 |  |  | Same as 2x7 |  |  |  |
| 3.5-6.0 |  |  | Same as 2x7 |  |  |  |
| 0.9375-1.25 | 0.02 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 12$ |  |  |  |
| 0.2-0.41 | 0.02 | $-15^{\circ}$ to $+50^{\circ}$ | Same as $2 \times 39$ |  |  |  |
| 0.093109 | 0.01 | $0^{\circ}$ to $+55^{\circ}$ | 6 -pin, $7 / \mathrm{in} . \lg , 7 / 2 \mathrm{in}$. dia | 4 | 21/2 | 17\% |
| 0.300060 |  |  | Octal | 2\% | 11/4 (dia) |  |
| 0.300 |  |  | - Same as $2 \times 154-300.060$ |  |  |  |
| 0.300050 |  |  | Same as $2 \times 154-300.060$ |  |  |  |
| 6.6875-7.3125 |  |  | Same as $2 \times 7$ |  |  |  |
| 0.00181818 |  |  | NL |  |  |  |
| 1.81744 |  |  | NL |  |  |  |
| 0.2-0.4 | 0.01 | $-10^{\circ}$ to $+60^{\circ}$ | Same as $2 \times 39$ |  |  |  |
| 1.5-5.0 |  |  | Same as $2 \times 39$ |  |  |  |

Section II
Crystal Units-Group II
TECHNICAL DATA CHART FOR GROUP-II CRYSTAL UNITS-Continued

| USAF Stock Number 2100 -s | Nomenelature | Crystal <br> Holder | Equipment Used In | Crystal Spec | Holder Spec |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3x172-4495 | Crystal Unit DC-10 |  | BC-230, BC-430 |  |  |
| 2x173- | Crystal Unit | FT-171-B | Fisher Research Rec |  |  |
| 2x174- | Crystal Unit | FT-171-B | Fisher Research Xmtr TS-25-3 | MIL-C-10405 |  |
| 2x174R- | Crystal Unit | FT-171-B | R-114/VRC-4 | MIL-C-10405 |  |
| 2x175-409.5 | Crystal Unit (James <br> Knights Type IF-6Y-101) |  | TS-126/AP |  |  |
| 2x177-2 | Crystal Unit CR-8/U |  | R-122/APN-12 |  |  |
| 2x180- | Crystal Unit | FT-249 | Bendix Xmtr TA-6A | MHL-C-10405 |  |
| 2x181-80.86 | $\begin{aligned} & \text { Crystal Unit (WECO } \\ & \text { D-166339) } \end{aligned}$ |  | AN/APQ-13 |  |  |
| 2x186R- | Crystal Unit | FT-243 | BC-611 (Rec) | MIL-C-239B | 72-119 |
| $2 \times 186 \mathrm{~T}$ - | Crystal Unit | FT-243 | BC-611 (Xmtr) | MIL-C-239B | 72-119 |
| 2x187-1.617 | $\begin{aligned} & \text { Crystal Unit (WECO } \\ & \text { D-170609) } \end{aligned}$ |  | MD-57/APS-22 |  |  |
| 2x188- | Crystal Unit | FT-240 | Tempeo Xmtr 250-G |  |  |
| 2x191R- | Crystal Unit | Bliley MC-7 | BC-348-R |  |  |
| 2x192C- | Crystal Unit CR-3B/U | FT-241-A | BC-506, SCR-508, SCR-528, BC-604, SCR-608 | TB SIG 201 |  |
| 2x204-100 | Crystal Unit <br> (RCA-TMV-129G) |  | $\begin{aligned} & \text { AN/CPN-11,-11A, -11B, } \\ & -12,-12 \mathrm{~A},-12 \mathrm{~B} \end{aligned}$ |  |  |
| 2x212-80.867 | Crystal Unit |  | AN/CPS-6B |  |  |
| 2x600- | Crystal Unit CK-5/U | FT-243 | BC-721 | M1L-C-2398 | 72-119 |
| 2x602- | Crystal Unit | FT-249 | AN/FRR-3A | MIL-C-10405 |  |
| 2x602-462.45 | Crystal Unit | FT-249 | AN/FRR-3A | MIL-C-10405 |  |
| 2x604- | Crystal Unit | RCA-AVA-53 | RCA-AVR-20A |  |  |
| $2 \times 606$ | Crystal Unit | AVA-10-D | RCA-AVT-7 (Xmtr) | MIL-C-10405 |  |
| $2 \times 609$ | Crystal Unit | FT-164 | BC-330 |  |  |
| 2x610-4166.67 | Crystal Unit | FT-249 | BC-400-H |  |  |
| 2x611- | Crystal Unit | FT-249 | $\begin{aligned} & \mathrm{BC}-460-\mathrm{A} \text { thru } \mathrm{C}, \\ & \mathrm{BC}-401-(\mathrm{r} \end{aligned}$ |  |  |
| 2x634- | Improvement Kit MC-531 | HC-1/U |  | MIL-C-10405 |  |
| 2x635- | Crystal Unit CR-1/AR | FT-249 | O-5/FR | MIL-C-10405 | 1.8 |
| 2x680- | Crystal Unit CR-7/U | FT-164 | MAR Receiver |  |  |
| NL-00019 | Crystal Unit | FT-164 | BC-329-H |  |  |

a See paragraph 2-59.

| Freq Range (me) | Freq <br> Tolerance ( $\pm \%$ ) | Operating <br> Temperature <br> Range ( ${ }^{\circ} \mathrm{C}$ ) | Base or Terminal Connections | Physical Dimensions (In.) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | High | Wide | Thick |
| 4.495 |  |  | NL |  |  |  |
| 2.0-8.0 |  |  | ${ }^{\text {Same as } 2 \times 12}$ |  |  |  |
| 2.0-8.0 | 0.01 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 12$ |  |  |  |
| 1.175-9.175 |  | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 12$ |  |  |  |
| 0.4095 |  |  | 2 screw-type terminals on each side | 1 | 1/2 | 14/32 |
| 15-52 |  |  | Wire terminals | 11/6 | \%/8 (dia) |  |
| 2.8-6.0 | 0.15 | $-40^{\circ}$ to $+55^{\circ}$ | Same as 2x5 |  |  |  |
| 0.08096 |  |  | Octal | 1 | 1/6 (dia) |  |
| 3.5-6.455 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| 3.5-6.235 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| 0.001617 |  |  | Octal | 37\% | 11/4 (dia) |  |
|  |  |  | Same as $2 \times 5$ |  |  |  |
|  |  |  | 2 pin, $1 / 6 \mathrm{in}$. lg , $1 / 8$ in. dia, 334 in . c to c | 12\%18 | 11/8 | 11/32 |
| 0.3-0.6 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 13$ |  |  |  |
| 0.1 |  |  | 6-pin, $3 / 4 \mathrm{in} . \lg , 6 / 32 \mathrm{in}$ dia | 4 | 21/2 |  |
| 0.080867 |  |  | Octal | 211/4 | 19304 ( dia ) |  |
| 2.0-10.0 | 0.02 | $-40^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 7$ |  |  |  |
| 1.4-3.8 | 0.01 | +45 ${ }^{\circ}$ to $+55^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 0.46245 | 0.01 | +45 ${ }^{\circ}$ to $+55^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 2.755-7.155 | 0.05 | $-40^{\circ}$ to $+55^{\circ}$ | 2 banana pins, 85 in. c to c | 134 | 17/4 | 8/18 |
| 2.5-6.7 | 0.015 | $0^{\circ}$ to $+70^{\circ}$ | Same as $2 \times 20$ |  |  |  |
| 0.19-0.40 | 0.01 | $-15^{\circ}$ to $+50^{\circ}$ | Same as $2 \times 39$ |  |  |  |
| 4.16667 | 0.01 | $-15^{\circ}$ to $+50^{\circ}$ | Same as 2x5 |  |  |  |
| 1.0-6.0 | 0.01 | $0^{\circ}$ to $+50^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 1.956-6.830 | 0.005 | $0^{\circ}$ to $+60^{\circ}$ | NL |  |  |  |
| 1.8-5.8 | 0.01 | $+45^{\circ}$ to $+60^{\circ}$ | Same as $2 \times 5$ |  |  |  |
| 0.29-0.40 | 0.02 | $-15^{\circ}$ to $+60^{\circ}$ | Same as $2 \times 39$ |  |  |  |
| 0.29-0.40 | 0.02 | $-15^{\circ}$ to $+60^{\circ}$ | Same as $2 \times 39$ |  |  |  |

## EXPLANATION OF MILITARY STANDARD TERMS USED IN DESCRIPTIONS OF CRYSTAL UNITS

Aging Test (See paragraph 2-s2)

## Authority

2-2. Serial numbers and dates of the military publications which prescribe the military specifications and military standards for the crystal unit being described.
Bonding Requirements (See paragraph 2-22)
Corrosion Test (See paragraph 2-88)

## Crystal Holder

2-3. All crystal holders specified for MilitaryStandard crystal units must conform with Military Specification MIL-H-10056 ( ). A complete description of each standard holder is to be found in Section III of this manual.

## Date of Status

2-4. Date of approval of the military status classification by the appropriate authority as prescribed by the applicable regulations of the Army, Navy, and Air Force.
Delivery Requirements (See paragraphs 2-49 and 2-50)

## Dimensions and Markings

2-5. Illustrated and largely self-explanatory. Unless otherwise specified, the marking includes only the type number, nominal frequency, and manufacturer's code-designating letters. (See paragraph 2-26 for additional marking requirements.)

## Drive Adjustment Procedure

2-6. Method to be used, as prescribed by the applicable Military Standard, in obtaining the correct level of crystal irive when testing the crystal unit with the specified CI meter. See paragraph 2-60.
Drop Test (See paragraph 2-94)
Effective Resistance Test at Second Level of Drive (See paragraph 2-95)

## Electrical Conaection of Holder

2-7. States whether the cover of a metal crystal holder is to be grounded or not when the crystal unit is connected in its standard test circuit. Not applicable in the case of plastic holders.

## Electrical Connection Requirements Inside Holder (See paragraph 2-24)

Etching Requirements (See paragraph 2-25)

Fabrication Requirements (See paragraphs 2-22 through 2-30)
Frequency and Effective Resistance Test (See paragraphs 2-81 and 2-36)

## Frequency Deviation with Temperature

2-8. As an additional permissible deviation, distinct from the nominal frequency tolerance, it is applicable in the case of crystal units whose nominal frequency tolerance is specified for a given fixed temperature only, rather than for any temperature within the operating range. The item then specifies the maximum additional variation in frequency that is permissible when the temperature is varied from the fixed reference point to any other temperature in the operating temperature range. Since this method is normally used only when the crystal unit is designed to operate at oven temperatures, where the operating range is narrow and presumably coincides with the zero-temperature-coefficient region of the crystal element, the design engineer is assured that once an oven-mounted crystal unit is in operation, any changes in its frequency due to reasonable changes in the oven temperature will be extremely small even though the overall nominal frequency tolerance from one crystal unit to the next is relatively large.

## Frequency Range

2-9. Self-explanatory, except that it should not be assumed that crystal units can always readily be obtained at any desired frequency within the given range. The quickest, most reliable, and least expensive approach is to select a frequency at which the desired type of crystal unit is already available. If this is not possible, the next best approach is to select a frequency at which the crystal unit, although not currently available, has been available in the past. Finally, if it is necessary to fabricate a crystal unit at a heretofore untested frequency, the greatest probability of least delay and expense in the research and developmental stage is to select a frequency as close as possible to other frequencies now available in the desired type of Military Standard crystal unit. Occasionally, it may be found that the fabrication techniques of one manufacturer are more conducive to superior crystal units within one band of the frequency range, whereas another manufacturer fabricates the same type of crystal unit more reliably within another band. In any event, before a
new untested frequency is decided upon, the design engineer should consult one or more of the manufacturers of the crystal unit under consideration.

## Frequency Range Abbreviations

2-10. VLF (very low frequency) : less than 30 kc . LF (low frequency) : 30 to 300 kc .
MF (medium frequency) : 300 to 3000 kc .
HF (high frequency) : 3 to 30 mc .
VHF (very high frequency) : 30 to 300 mc .

## Functional Deseription

2-11. Provides summary of general physical and operational features of crystal unit, such as the type of mounting, operating harmonic, frequency range, frequency tolerance, temperature range, and mode of circuit operation.
Glass Seal Imspection (See paragraph 2-s7)

## Harmonic of Quartz Vibration

2-12. Mechanical harmonic of crystal element for which the military test specifications are applicable. Where a harmonic mode higher than the fundamental is specified, this should not be construed to mean that the crystal unit is more readily excited at the overtone than at the fundamental frequency, so that the desired harmonic can be obtained in an untuned type of oscillator.

## Immersion Test (See paragraph 2-38)

Insulation Resistance Test (See paragraph 2-39)
Internal Inspection (See paragraph 2-40)
Leakage (See paragraph 8-40a)
Load Capacitance (See paragraph 2-56)
Marking Requirements (See paragraph 2-26)
Maximum Capacitance (Pin-to-Pin)
2-13. Maximum permissible electrostatic capacitance across the crystal-unit electrodes, as measured at the pin connections at a frequency lower than the fundamental of the crystal unit, where the unit shows no response other than that of a fixed capacitance.

## Maximum Drive Level (See paragraph 2-55)

## Maximum Effective Resonance Resistance

2-14. Maximum permissible effective resistance of crystal unit when measured at the specified test resonance and harmonic mode using the specified CI meter and drive adjustment procedure. For series-mode crystal units, the maximum effective resistance is the maximum permissible resonance impedance of the unit and, except at the very highest frequencies, is very nearly equal to an equivalent maximum permissible series-arm resistance. For parallel-mode crystal units, the maximum effective resistance is equal to the maximum permissible resistive component when the crystal
impedance is represented as an equivalent resistance and reactance in series, at the exact frequency at which the reactive component is resonant with the test load capacitance.
Method A (See paragraph 2-36a)
Method 8 (See paragraph 2-36b)

## Methed of Measuring Frequency and Effective

 Resonance Resistance2-15. The crystal unit is tested for frequency and effective resistance over the operating temperature range in accordance with either method $A$ or method B. In general, method A, which sets minimum and maximum limits for the rate of temperature change, is specified for the smaller rec-tangular-shaped crystal units that are not intended to be operated in temperature-controlled compartments ; otherwise, method B, which sets no limiting rate of temperature change, is specified.

## Method of Mounting Crystal

2-16. Only two broad classifications of mounting methods are specified in the Military Standards for quartz crystal units: pressure mounting and metal-plated, wire mounting. The pressuremounted method embraces all the sandwich and air-gap mounts except those of the gravity type, and also includes all those mounts having metalplated crystals held in place purely by the mechanical pressure exerted by pins or knife-edged clamps. The metal-plated, wire-mounted method includes the resonant-wire mounts (not the reso-nant-pin mounts) and the metal-plated, edgeclamped, cemented-lead mount.
Moisture Resistance Test (See paragraph 2-41)

## Nomenelature of Crystal Units

2-17. The Joint Army, Navy, Air Force nomenclature for designating a particular type of crystal unit is as follows:


In the type number, the component, which is a crystal mounted in a holder, is identified by the symbol, CR. The component symbol is followed by a hyphen and 2 digits ( -XX ) which identify the mounted crystal as having been designed according to certain specified electrical and physical characteristics. The letter $U$, separated from the number by a slant sign, is the equipment indicator
symbol for "general utility installation," which means that the crystal unit is intended for use in two or more of the three general installation classes-airborne, shipboard, and ground.

## Nominal Frequency Tolerance

2-18. The maximum permissible difference between the rated nominal frequency of the crystal unit and the operating frequency as measured according to the specified test conditions. The tolerance is normally expressed as a given percentage of the nominal frequency and is applicable over the entire operating range unless the crystal unit is intended for oven mounting. In this latter case, the nominal frequency tolerance usually applies only to operation at the midpoint of the operating temperature range. An additional permissible deviation from the measured midpoint frequency is then specified, so that the overall frequency tolerance is equal to the sum of the nominal frequency tolerance and the additional permissible frequency deviation.

## Operable Temperature Range

2-19. Temperature range over which the crystal unit has been tested in operation without regard to tolerance limits. Normally, the operable temperature range is specified only for crystal units having a narrow operating temperature rangethat is, only for those units standardized for use in temperature-controlled compartments. The specification of an operable temperature range provides assurance of the continued operation of a crystal, although not necessarily within the frequency tolerance limits, during an oven warm-up period, or during the breakdown or absence of temperature control. However, it should be understood that the term "operable" is not rigorously defined. A crystal unit operable in the average test circuit may not be operable in an oscillator that is designed for minimum performance characteristics when the effective resistance is the maximum permissible value.

## Operating Temperature Range

2-20. That part of the operable temperature range within which the crystal unit tolerance specifications have been tested and are assumed to hold. Unless the crystal unit is intended to be tempera-ture-controlled, the operating and the operable ranges are identical.
Ordering Requirements (See paragraph 2-49)
Packeging Requirements (See paragraph 2-50)
Pin Alinement Test (See paragraph 2-48)
Plating Adherence Test (See paragraph 2-45)
Refarence Standard Test Set (See paragraph 2-58)

## Requirememts and Procedures of Tests

2-21. See Military Specification MIL-C-3098( ) for details of the required inspections, the grouping of tests, and the procedure for sampling. Those tests performed on each individual crystal unit by the manufacturer are the visual and mechanical external inspection, the frequency and effective resistance test, the second level of drive test (for overtone units), and the seal test. Samples of each production lot are subjected to all remaining tests listed herein which are specified as applicable.

## FABRICATION REQUIREMENTS

## Bonding

2-22. Wire-mounted, metal-plated crystal units are bonded at the point of contact of the suspension wire and the metal plating of the quartz plate. A conductive material of the highest grade commercially available and suitable for the purpose is used. The bond withstands, without electrical or mechanical failure, all tests performed on the crystal unit.

## Crystal Holders

2-23. All holders conform to Military Specification MIL-H-10056().

## Electrical Connections

2-24. When the design of a crystal unit involves the use of a nonferrous metal in direct contact with the metal plating, a tin-lead eutectic solder saturated with the same metal used for plating the quartz surfaces is employed. Saturation of the solder with the plating metal is such that during soldering, or thereafter, migration of the metal from the plated surface of the quartz plate to the solder is effectively checked. Springs are attached to the base pins by using a high-temperature solder or by welding.

## Etching

2-25. The quartz plates are finished by etching to the final frequency for pressure-mounted units and to the preplating frequency for metal-plated units. During manufacture, at least one freshly-lapped quartz plate of each type being processed is taken at random from the production line each day for measurement of its frequency under standard test conditions. The quartz plate is then subjected to the etch procedure being used by the manufacturer and tested for compliance with the etching specifications of the Military. AT and BT plates must be subjected to the following minimum etch for fundamental and overtone operations:

$$
\begin{array}{ccc}
\text { Fundamental } & \text { Overtone } \\
\Delta f=0.6 f^{2} & \text { (AT Cut) } & \Delta f=0.3 f^{2} / \mathrm{N} \\
\Delta f=0.4 f^{1} & \text { (BT Cut) } & \Delta f=0.2 f^{2} / \mathrm{N}
\end{array}
$$

Where:
$\Delta f=$ required frequency increase in kc.
$f=$ frequency of quartz plate in mc.
$\mathrm{N}=$ harmonic.
The above formulas are based upon the use of 1000 -mesh grit abrasive. In the event a manufacturer uses a finer grit abrasive requiring an amount of etch less than that indicated above, he is required to demonstrate to a government inspector that the amount of etch is above the knee of the etch-rate curve, or is a satisfactory equivalent. (The etch-rate curve is the curve produced by plotting frequency change due to etching as the ordinate against time of etch as the abscissa. The knee of the curve is that portion of greatest curvature, which occurs at the beginning of the curve before the rate of frequency change has become a steady slope.) The etching curves (not etch-rate curves) in figure 1-89 are graphical illustrations of the fundamental-frequency formulas above.

## Glass Seal (See paragraph 2-s7)

## Marking

2-26. The type number, the specified nominal frequency, and the code letters designating the manufacturer are permanently and legibly marked on the holder of each crystal unit. Unless otherwise specified by the bureau or service concerned, no other markings are permitted on the holder. The code designating letters are those listed in publication NAVSHIPS 900,152 . Each line of characters is symmetrically located with respect to the center axis of the holder. Characters are not less than one-sixteenth inch high and are either metalstamped, branded, or engraved. The marking is required to withstand all tests specified for the particular crystal unit.

## Mounting

2-27. The quartz plate will be either wire- or pres-sure-mounted.

## Solder

2-28. Soft solder is used in accordance with Federal Specification QQ-S-571, and is required to have a minimum tin content of 39.0 per cent by weight, except in the case of the electrical connections to the metal plating on the quartz as described in paragraph 2-24. In the edge-clamped wire mounts, the solder is not used primarily for obtaining mechanical strength, and the electrical connections are mechanically and electrically continuous before and after soldering.

## Solder Flux

2-29. Only substantially noncorrosive fluxes are
used unless the corrosive element can be demonstrably removed after soldering.

## Workmanship

230. All crystal units are required to be manufactured and processed in a careful and workmanlike manner, in accordance with good commercial design and practice. All units are required to be free from any imperfections which may affect their serviceability, and the interiors must be free from flux, loose solder, unapproved or foreign material, dust, or any loose particles at all.

## STANDARD TEST' CONDITIONS

2-31. Unless otherwise specified, all crystal-unit measurements and tests are made under the prevailing ambient conditions of atmospheric pressure and relative humidity and at a temperature between 20 and 35 degrees centigrade. When measurements of the frequency and/or effective resistance are made both before and after a test, the temperature of the crystal unit for the second measurement is required to be within 2 degrees centigrade of the temperature of the first measurement, and the level of drive for ail measurements is to be within 20 per cent of the nominal value specified.

## DESCRIPTIONS AND REQUIREMENTS OF TESTS

## Aging Test

2-32. The crystal unit is placed in a well-ventilated oven equipped with heating and timing controls that produce the following heat cycle: a "heat-on" period of 2 hours duration with a stabilized temperature of 100 degrees centigrade ( $\pm 5^{\circ} \mathrm{C}$ ) for at least 30 minutes, followed by a "heat-off" period of sufficient duration to lower the oven to within 15 degrees centigrade of standard test conditions. The crystal unit is subjected to three such continuous cycles and then removed from the oven at the end of the final "heat-off" period, after which the frequency is measured for compliance with the tolerance specifications of the aging test. The specified maximum permissible change in frequency can be assumed to be an approximate gauge of the degree of frequency drift the crystal unit can be expected to undergo due to aging after being in operation a long period of time.

## Corrosion Test

2-33. The crystal unit is required to withstand 50 hours of the salt-spray (fog) test specified in Federal Specification QQ-M-151 without evidence of corrosion sufficient to impair the operation of the crystal unit.

## Drop or Shock Test

$2-34$. This test is imposed to prove out the mechanical design of the unit to meet normal handling and military environmental conditions. It provides sharp mechanical shock. Method 202 as specified in MIL-STD-202 is recommended for uniformity and duplication of test results. The test is also described as Method A of MIL-C-3098B. The frequency and effective resistance are measured before and after the test. The change in frequency is not to exceed the tolerance specified for the drop test, and the effective resistance is not to exceed the maximum specified for the crystal unit.

## Effective Resistance Test at Second Level of Drive for Overtone Crystal Units

2-35. The effective resistance of overtone crystal units is checked at a second and lower level of drive at room temperature to ensure that the specified maximum effective resistance is not exceeded when the amplitude of crystal vibration approaches a practical minimum. The second level of drive is obtained by setting up Crystal Impedance Meter TS-683/TSM in accordance with the applicable instructions contained in Military Specification MIL-C-3098B.
Frequency and Effective Resistance Test Over Operating Temperature Range
$2-36$. The crystal unit is tested in accordance with method A or B, as specified. Unless otherwise specified, the level of drive during the test is within 20 per cent of the nominal drive level specified for each crystal unit. The reference standard test sets are as specified on the standard sheet in MIL-C-3098B. The drive adjustment procedures for the test set and particular crystal unit are also specified in MIL-C-3098B. The measured crystal frequency is to be within the tolerance specified, and the measured effective resistance is not to exceed the maximum specified.
a. Method A: The crystal unit is subjected to a temperature run over the specified operating temperature range at a minimum rate of change of 3 degrees centigrade per minute. Measurements of frequency and effective resistance are made at intervals no greater than 3 degrees centigrade, except that the portion from -30 to +20 degrees centigrade is completed in a period not exceeding 1 minute, and continuous readings of both frequency and effective resistance are made over the range. The entire temperature range of -55 to +90 degrees centigrade is not to be completed in less than 1 minute.
b. Method B: The crystal unit is subjected to
a temperature run over the specified operating temperature range at any convenient rate of temperature change. Measurements of frequency and effective resistance are made at intervals no greater than 3 degrees centigrade.
Glass Seal Inspection
2-37. Those crystal units with bases having a glass seal are inspected with the aid of a strong light and 10 -power magnification. No glass seal is permissible that contains radial or other detrimental cracks.

## Immersion Test

2-38. The crystal unit is immersed in water, maintained at $90^{\circ}$ to $95^{\circ} \mathrm{C}$, for at least 1 hour. Unit is then removed from water, wiped dry, and set aside for one-half hour, after which its insulation resistance, frequency, and effective resistance are measured and compared with those made before the immersion test. Also, markings on the crystal unit must remain legible.

## Insulation Resistance Test

2-39. At room temperature, using a test voltage of 50 to 100 volts, the insulation resistance of the crystal unit, as measured between the pins of the unit or between any pin and any other external metal part of the unit, is required to be not less than 500 megohms.

## Internal Inspection

2-40. Randomly selected samples of crystal units from an inspection lot are disassembled and the interior of each selected unit is inspected to determine if the material, threaded parts of the holder, and the workmanship comply with military specifications.

## Leakage

2-40a. After being held at standard test conditions for a period of at least 24 hours, the sealed crystal unit is immersed in an open container of distilled water. The container is then placed in a sealed chamber which is evacuated to an absolute pressure of 3.0 to 3.4 inches of mercury for a period of not less than 5 minutes. There must be no evidence of leakage of gas or air from inside the unit.

## Moisture Resistance Test

2-41. The crystal unit is subjected to a series of thirty 24 -hour moisture resistance tests in a humidity test chamber. For the first 16 hours of each test period, the chamber is maintained at $65^{\circ} \pm 2^{\circ} \mathrm{C}$, and above $90 \%$ relative humidity. For the last 8 hours, the chamber is returned to
normal room temperature. After 4 or more days, and for at least 6 times within the 30 -day test period, and at the end, the unit is removed from the chamber and tested for effective resistance, frequency, and insulation resistance.

## Pin Alinement Test

2-42. Crystal units having a type HC-6/U, HC$13 / \mathrm{U}$, or $\mathrm{HC}-14 / \mathrm{U}$ holder are tested for correct pin alinement by using a shadowgraph as specified in Military Specification MIL-H-10056( ), or by using a test gage as specified in Military Specification MIL-C-3098( ). The test gage is equivalent to a 2 -hole socket having a depth of $0.238 \pm 0.01$ inch. The two holes are spaced 0.486 inch center-to-center, and each has a maximum diameter of 0.06 inch. Pins so tested must freely enter the gage until the base of the holder is firmly seated on the gage.

## Plating Adherence Test

2-43. The plating adherence test is applicable to all crystal units employing metal-plated crystals. The test is performed by firmly applying a piece of transparent plastic pressure-sensitive tape to the base plating of the quartz crystal, and then removing the tape immediately by lifting one corner and pulling at a slow uniform rate perpendicularly to the plated surface. The above steps are repeated for units that have been plated to the final frequency. After the test there must be no visual evidence (without magnification) of the removal of plating from the quartz surface.

## Seal Test

2-44. After being held at standard test conditions for a period of at least 24 hours, the sealed crystal unit is immersed in water having a temperature between $90^{\circ} \mathrm{C}$ and $95^{\circ} \mathrm{C}$ for a period of not less than 2 minutes. A seal is considered defective if an escapement of bubbles from the holder is observed, indicating a gas or air leakage from the inside of the crystal unit.

## Spurious Frequency Test

2-45. With the reference test set adjusted to provide the specified drive level at standard test conditions, a fixed resistor, whose value is equal to the specified maximum effective series resistance, is substituted for the crystal unit. The output frequency of the test set is then adjusted to both plus and minus 10 per cent of the nominal frequency marked on the crystal unit, and the respective dial settings of the tuning control on the test set are recorded. With the fixed resistor replaced by the crystal unit, the tuning control is varied slowly between the recorded dial settings. The
crystal unit is assumed free of spurious responses if during this tuning variation neither abrupt shifts in frequency nor intermittent oscillations are observed.

## Tensile Strength Test

2-46. This is a test of the mechanical strength of the junction of the metal plating and lead wires. This test is generally applied in the case of the lower-frequency wire-mounted units where it is usual for the entire mechanical support of the crystal to depend upon the soldered junctions of the lead wires to the metal plating of the crystal. When the test is applicable, the minimum permissible tensile strength of the junction is specified for each particular type of crystal unit and frequency band. A weight load is gradually applied to the outside ends of both of the lead wires until breakdown occurs at the junction to the metal plating. (Breaking of the quartz plate during the test is not construed as a test failure and another specimen is taken.) A breakdown must not occur at a tensile pull less than that of the minimum weight specified.

## Terminal Polarity Test

2-47. The crystal unit is operated in a test set in which the socket is non-polarized, and the frequency, as measured under standard test conditions, must be as specified.

## Vibration Test

2-48. Each type of Military Standard crystal unit must undergo the same rigorous test in a vibration machine. The maximum changes in frequency and effective resistance resulting from the test period of vibration that are permissible are specified for each particular type of crystal unit. The crystal unit is rigidly mounted with random orientation on the platform of a vibration machine. A simple harmonic motion having a peak amplitude of 0.015 inch (maximum total excursion of 0.030 inch ) is applied to the platform continously for 2 hours. The frequency of the applied vibration is varied uniformly between the approximate limits of 10 and 55 cycles per second. The entire frequency range from 10 to 55 cps and return is traversed in 1 to 2 minutes. The frequency and effective resistance are measured under standard test conditions before and after the test, and the changes observed in these parameters are not to exceed the tolerances specified.

## DELIVERY REQUIREMENTS

Ordering
2-49. According to Military Specification MIL-C-

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3098B, procurement documents should specify the following:
a. Title, number, and date of the applicable crystal unit specification (MIL-C-3098B).
b. Type designation (type number), and the title, number and date of the applicable Military Standard. (Crystal units designated as "special application" shall be purchased and used only with the approval of the bureau or service concerned.)
c. Nominal frequency required.
d. Laboratory where preproduction tests are to be conducted. (See MIL-C-3098( ) for requirements of preproduction tests.)
e. Whether crystal units are to be packaged individually or in sets.
f. Whether metal boxes or fiberboard cartons or boxes are to be used for set packaging.
g. Whether intermediate packages are required, and quantity of individual packages.
h. Whether packing and marking are for domestic or oversea shipment.
i. That the contractor shall not substitute for a specified material or fabricated part unless he obtains approval for such substitution from the bureau or service concerned. Evidence to substantiate his claim that such a substitute is suitable shall be submitted with his request. Similar notification and substantiating evidence shall be submitted at any later time if substitution becomes necessary or desirable. At the discretion of the bureau or service concerned, test samples may be required to prove the suitability of the proposed substitute.
j. Applicable reference standard test set to be furnished by the contracting officer to government inspector at the manufacturer's plant.

## Packaging

2-50. When directly purchased by or directly shipped to the Government, Military Standard crystal units must either be packed individually or in sets composed of one crystal unit of each designated frequency. When packed individually, each unit is cushioned and packaged in a folded carton or set-up box conforming to Specification JAN-P-120 or JAN-P-133, respectively. When packaged in sets, each set is contained in a hinged-cover-and-clasp-style enameled or lacquered metal box satisfactory to the bureau or service concerned, or in fiberboard boxes, set-up boxes, or cartons, as specified, with each crystal unit individually wrapped or cushioned. The quantity included in a unit package is 10 or a multiple thereof. Five unit packages or a multiple thereof are further packaged in intermediate containers conforming to Specification JAN-P-120 or JAN-P-133. The
gross weight of the intermediate container is not to exceed 5 pounds. See MIL-C-3098B, Section 5, for detailed packaging and marking instructions. However, it should be understood that the military specifications concerning the packaging, packing, and marking of crystal-unit shipments to the Government are not intended to apply to contracts or orders between the manufacturer and prime contractor.
Resonance (See paragraph 2-57)
Seal Test (See paragraph 2-44)

## Second Test Level of Drive

2-51. A very low level of crystal drive used for checking the effective series resistance of overtone crystal units at minimum amplitudes of vibration. This second check is necessary because of the tendency among overtone units to exhibit sharp increases in effective resistance as the crystal drive approaches zero. The procedure for obtaining the second level of drive, which is applicable to the use of Crystal Impedance Meter TS-683/TSM, is specified in Military Specification MIL-C-3098B.
Solder Requirements (See paragraph 2-28)
Solder Fux Requirements (See paragraph 2-29)

## Special Application Erystal Units

2-52. Crystal units assigned a status of "special application" are available only in limited production and normally from only one source (availability category 2). Such crystal units are not to be purchased and used without the approval of the service or bureau concerned.
Spurious Frequency Test (See paragraph 2-45)

## Standard Crystal Units

2-53. Crystal units assigned a status of "standard" are available from two or more sources (availability category 1) and are recommended for use when applicable without special approval of the service or bureau concerned.
Standard Test Conditions (See paragraph 2-S1) Status
2-54. Type classification of crystal unit, regarding procurement and availability, as assigned by the cognizant Military agency.
Tensile Strength Test (See paragraph 2-46)
Terminal Polarity Test (See paragraph 2-47)

## Test Level of Drive

2 -55. The power, within $\pm 20$ per cent, usually expressed in milliwatts, that is to be supplied to the crystal unit when the unit is being tested with the specified reference standard test set for frequency and effective resistance. The test level of drive is
also the maximum drive at which the crystal unit can be operated with assurance that the rated tolerances will be met, although the crystal is usually operable at much higher, but nonrecommended levels.

## Test Load Capacitame

2-56. Capacitance with which the effective inductance of the crystal unit is resonant during the frequency and effective-resistance test. (Applicable only if the crystal-unit specifications call for parallel-resonance testing.) The circuit in which a parallel-mode crystal unit is intended to operate should be designed and adjusted to provide the unit with a load capacitance equal to the test load capacitance, otherwise no guarantee exists that the specified tolerances in frequency and effective resistance can be met. Since a given effective reactance of a crystal unit will occur at a unique frequency, a circuit can be assumed to be adjusted to present the correct load capacitance if the frequency is exactly the same as that measured when the crystal unit is known to be series-resonant with its test load capacitance under standard test conditions.

## Test Resonance

2-57. States whether crystal unit is tested for operation at its resonance frequency (series-mode operation) or at some slightly higher frequency appropriate for parallel-mode operation.

## Test Set (Reference Standard Crystal Impedance Meter)

2-58. Reference standard CI meter specified for use in measuring the frequency and effective resistance of the crystal unit.

## USAF Stock No.

2-59. Number for identifying item when requisitioning from U. S. Air Force supply depot. The USAF stock numbers of crystal units are the same
as the respective Signal Corps numbers except that the prefix " $2100-$ " is added, which serves to identify the item as belonging to USAF stock class $16-\mathrm{F}$. The exact frequency is identified by a hy-phen-separated suffix equal numerically to the frequency desired in kc.
Vibration Test (See paragraph 2-48)
Workmanship Requirements (See paragraph 2-30)
MILITARY STANDARD DRIVE ADJUSTMENT PROCEDURES FOR CRYSTAL UNITS COVERED BY MILITARY SPECIFICATION MIL-C-3098E

## Crystal Impedance Meter TS-330/TSM

PROCEDURE FOR OBTAINING TEST
LEVEL OF DRIVE FOR CRYSTAL UNITS OVER A FREQUENCY RANGE OF 800 TO 15,000 KILOCYCLES PER SECOND
2-60. The following drive adjustment procedure is specified by Military Specification MIL-C-3098B, Paragraph 4.3.1.1.1:
a. Set band switch of TS-330/TSM test set to the appropriate frequency.
b. Set "crystal-calibrate" switch to "calibrate" position.
c. Determine, from the table below, the value of resistance for the frequency range of the type of crystal unit being tested. Set this value of resistance on the decade resistor in the test set.
d. Select, from the table below, the value of test frequency shown for the frequency range of the type of crystal unit being tested. Adjust the test set to this frequency by means of the tuning control. (Great precision is not essential in this frequency setting. The adjustment may be accomplished by monitoring the test-set signal by means of a calibrated radio receiver with dial settings comparable in accuracy to that of the National high-frequency receiver type HRO-SP.)
e. Determine, from the table below, the value

| Frequency Range (me) | Test Frequency (mc) | Non-Temperature-Controlled Units |  | Gven-Controlled Types |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Resistance (ohms) | Crystal Current (ma) | Resistance (ohms) | Crystal Current (ma) |
| 0.80-1.50 | 1.3 | 100 | 10 | 0 | $0^{* *}$ |
| 1.51-2.25 | 2.0 | 50 | 20 | 90 | 10 |
| 2.26-3.40 | 3.0 | 100 | 10 | 50 | 10 |
| 3.41-5.10 | * | 45 | 15 | 50 | 10 |
| 5.11-7.50 | * | 25 | 20 | 22 | 15 |
| 7.51-10.00 | * | 16 | 25 | 13 | 20 |
| 10.1-15.0 | * | 13 | 20 | 11 | 15 |

* Set up at frequency of crystal to be teated.
** Set for minimum aniting of "crysial current* control.


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of crystal current for the frequency range of the type of crystal unit being tested. Vary the crystal current control on the test set until the crystal current meter indicates the proper value.
f. The drive in the test set is now properly adjusted for crystal units of the frequency being tested and for crystal units in the frequency range for which the adjustment was made.

Crystal Impedance Meter TS-537/TSM
PROCEDURE FOR OBTAINING TEST LEVEL OF DRIVE FOR CRYSTAL UNITS OVER A FREQUENCY RANGE OF 75 TO 1100 KILOCYCLES PER SECOND

2-61. The following drive adjustment procedure is specified by Military Specification MIL-C-3098B, Paragraph 4.3.1.1.2:
a. With the crystal drive control set for the minimum value at which the crystal will oscillate, measure the effective resistance of the crystal as described in the TS-537/TSM instruction manual.
b. Determine the voltage across the measured value of effective resistance that would provide a 2 -milliwatt power dissipation. Use graph in MS91482, or the following formula:

## Volts $=\sqrt{0.002 \times \text { Effective Resistance in Ohms }}$

c. With the test set in the "calibrate" position, and with the decade resistor set for the effective resistance determined in step a, adjust the crystal drive control until the voltage difference obtained in step $b$ appears across the decade resistance. This voltage difference can be measured by obtaining the difference between two vacuum-tube voltmeter readings taken at the voltmeter jacks on the front of the test set. If the drive cannot be decreased sufficiently, set the crystal drive control for minimum drive.

## Crystal Impedance Meter TS-683/TSM

PROCEDURE FOR OBTAINING TEST

LEVEL OF DRIVE FOR CRYSTAL UNITS OVER A FREQUENCY RANGE OF
10,000 TO 100,000 KILO-
CYCLES PER SECOND (10.0
TO 100.0 MEGACYCLES)
2-62. The following drive adjustment procedure is specified by Military Specification MIL-C-3098B, Paragraph 4.3.1.1.3.1:
a. Set band switch of the TS-683/TSM test set to the appropriate frequency.
b. Adjust frequency of the test set to the frequency of the crystal unit by means of the calibrated dial.
c. Determine, from the table below, the value of resistance for the frequency range of the type of crystal unit being tested. Obtain a non-wirewound type resistor that does not differ from the selected value by more than 2 per cent. (The resistor, for convenience, may be mounted in a type HC-6/U crystal holder.)
d. Insert the resistor in the appropriate socket. It is necessary to fabricate a jig, in which to place the resistor, that will permit the measurement of voltage from both sides of the resistor to ground. This measurement shall be made with a high-frequency probe of the type used in a Model 1800-A General Radio vacuum-tube voltmeter, or equal.
e. Determine, from the table below, the value of resistor voltage drop for the irequency range of the type of crystal unit being tested.
f. By means of the voltmeter specified in step $d$, measure the voltage from both sides of the resistor to ground and subtract the smaller reading from the larger to determine the resistor voltage drop.
g. Vary the drive control at the rear of the test set and repeat the voltage measurements until the measured resistor voltage drop is equal to that specified in the table.
h. The drive in the test set is now properly adjusted for crystal units of the frequency being tested and for crystal units in the frequency range for which the adjustment was made.

| Frequency Range (me) | Resistance ( $\mathrm{ohms} \mathrm{)}$ | Resistor Voltage Drop (volts) |  |
| :---: | :---: | :---: | :---: |
|  |  | Non-TemperatureControlled Units | TemperatureControlled Units |
| 10-24.99999 | 40 | 0.40 | 0.28 |
| 25-52.0 | 40 | . 28 | . 20 |
| 52.000001-75 | 60 | . 35 | . 24 |

NOTE: The resistance and voltage values in the table above are not applicable in the case of the 20 -milliwatt crystal units, $\mathrm{CR}-51 / \mathrm{U}$ and $\mathrm{CR}-53 / \mathrm{U}$. See the respec-
tive technical descriptions of these crystal units for the parameters providing the correct test level of drive.

## PROCEDURE FOR OBTAINING TEST level of drive for crystal unit CR-ss/U

2-63. The following drive adjustment procedure is specified by Military Specification MIL-C-3098B, paragraph 4.3.1.1.3.2:
a. Insert $a 1 / 8$ - or $1 / 4$-watt carbon resistor having a value of $25 \pm 1$ ohms, measured on a wheatstone bridge, in the appropriate socket. (The resistor can be mounted on the base of a type HC-6/U crystal holder, with the resistor leads soldered to the mounting pins and kept as short as possible.)
b. Adjust frequency of the test set to the frequency of the crystal unit by means of the calibrated dial.
c. Adjust the screen-grid control knob to present a value of 0.25 -volt difference between the voltages when measured from each side of the resistor to ground. This sets up the required level of drive of 2.5 milliwatts.
d. Remove the 25 -ohm resistor and insert another carbon resistor having a resistance equal to the maximum effective resistance specified for the crystal unit on Military Standard MS91388.
e. Retune the test set as in step b above.
f. Adjust the knob marked "grid current increase" to read some convenient value of grid current on the microammeter. This value of grid current may then be used to represent the maximum effective resistance. The test set is now adjusted for "Go and No-Go" operation.
g. Remove the resistor and insert the crystal unit with its $32 \pm 0.5$ microfarad load capacitance in series with one terminal. The test set may now be used to perform the frequency and effective resistance measurements of the crystal unit.

PROCEDURE FOR OBTAINING SECOND TEST LEVEL OF DRIVE FOR HARMONICMODE CRYSTAL UNITS UTILIZING CRYSTAL IMPEDANCE METER TS-683/TSM
2-64. The following drive adjustment procedure is specified by Military Standard MS90168 (19 November 1952 revision) :
a. With the appropriate calibrating resistor for the frequency involved, the screen voltage control shall be set to a point at which the rectified grid current reading is one-half of one meter division
(2.5 $\mu \mathrm{a}$ ) greater than the non-oscillating reading. This shall be checked by alternately inserting and removing the resistor and observing the meter deflections. Greatest accuracy will be obtained when operating the grid meter shunt control at maximum clockwise position.
b. The tuning control of Crystal Impedance Meter TS-683/TSM shall be adjusted in the usual manner for proper frequency calibration, using the appropriate resistor.
c. The crystal unit shall be inserted in the socket of the test set, and the grid current meter shall show a deflection increase of at least one-half of one meter division ( $2.5 \mu \mathrm{a}$ ). Crystals that do not oscillate or produce readings of less than one-half of one meter division ( $2.5 \mu$ a) shall be considered defective. The crystal oscillation frequency can be monitored in the receiver used in calibrating, as an aid to increasing the speed of testing.

## Crystal Impedance Meter TS-710/TSM

PROCEDURE FOR OBTAINING TEST LEVEL OF DRIVE FOR CRYSTAL UNITS OVER FREQUENCY RANGE OF 10 TO 1100 KCS 2-65. The following drive adjustment procedure is specified by Military Specification MIL-C-3098B, paragraph 4.3.1.1.4:
a. Determine the proper power level from the applicable military standard.
b. Compute the required value of substitution resistance by taking 70 percent of the maximum (crystal unit) resistance given on the applicable military standard for the crystal unit under test.
c. Using the data obtained under steps a and $b$ above, determine the crystal unit drive voltage from the formula $E=\sqrt{W R}$

Where
$\mathrm{E}=$ drive voltage in volts.
$\mathrm{W}=$ specified power level in watts.
$R=$ resistance in ohms found in step $b$.
d. Insert the correct value of substitution resistance, as obtained in step $b$ above, in the crys-tal-unit socket; switch the oscillator circuit to series-resonance operation; tune the test set to the frequency of the crystal unit under test; adjust the voltage gain control to obtain the voltage difference required by step $c$. This voltage difference may also be obtained by measuring the voltage between each terminal of the crystal-unit socket to ground, with the substitution resistor in the socket, and computing the numerical difference.

Section I!

## METHODS FOR MEASURING THE FREQUENCY OF MILITARY STANDARD CRYSTAL UNITS

2-66. The systems employed by manufacturers and laboratories for measuring the frequencies of crystal units vary according to the facilities available, the degree of precision desired, the temperature requirements, the purpose of the particular measurement, and other factors. For example, in a simple room-temperature test of the go, no-go* type, a less elaborate system is required than would be the case if a very precise record of the frequency were desired over an operating temperature range of $-55^{\circ}$ to $75^{\circ} \mathrm{C}$. Again, the measuring systems employed in testing crystal units at points along a production line are arranged to permit simple, repetitive operating techniques that can be readily learned by non-technical personnel. In the research laboratory, on the other hand, the test equipment must be adaptable for a wide variety of measurements over wide frequency ranges and ambient test conditions. Since such tests are to be performed by highly trained technicians, less attention is given to simplified techniques. Normally, the equipment available can be used in a number of different ways to obtain the same measurement, some of the methods being more accurate than the others.

## EQUIPMENTS REQUIRED FOR CRYSTAL FREQUENCY TESTS

2-67. In the measurement of crystal frequencies under test conditions corresponding to Military Specifications, the equipments required can be divided into the following categories:
Primary Standards
a. Primary frequency standard (Station WWV ground-wave signals)
b. Primary crystal test set standards (Govern-ment-furnished CI meters to be used for correlation adjustments) $\dagger$
c. Primary load-capacitor standard
d. Primary calibrated resistor standards
e. Primary temperature standards (boiling and freezing points of water)

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## Reference Standards

a. Secondary frequency standard (precision crystal-controlled frequency generator)
b. Audio-frequency reference standard (interpolation oscillator)
c. Reference crystal test sets (standard CI meters and duplicating circuits used in actual crystal-frequency measurements)
d. Temperature reference standard (pyrometer)
e. Reference load capacitors (component parts of reference crystal test sets)
f. Reference caii rated resistors

Indicating and Recording Instruments
a. Frequency counter or meter
b. Frequency-deviation meter
c. Frequency-deviation-vs-temperature recorder
d. Oscilloscope (used in exact frequency measurements and in correlation of interpolation oscillator)
e. Grid-current meter (used in adjustment of reference crystal test set for measuring crystal resistance)
f. Effective-resistance-vs-temperature recorder
g. Electronic r-f voltmeter (used in measuring crystal drive level)
h. Pyrometer (for indicating crystal tempera-ture-same as temperature reference standard, listed above, used in correlating other tempera-ture-measurement controls)
i. Thermometer (for cold box or multiplecrystal cooling and heating chamber)
j. Q meter (for calibration of load capacitance)
k. R-F bridge (for checking calibrated resistors)

1. Earphones or loudspeaker (for audio zerobeat frequency measurements)

## Auxiliary Amplifiers and Frequency Converters

a. Radio receiver, cw and mcw
b. Harmonic generators (controlled by frequency standard)
c. Frequency divider (for dividing frequencies that are too high for receiver)
d. Variable-frequency oscillator (for rapid frequency checks)
e. R-f amplifier
f. D-c amplifier
g. Signal control panel

Auxiliary Devices for Controlling Crystal Unit Test Conditions
a. Cold box
b. Cold box thermostat
c. Heater
d. Heater thermostat
e. Variable heater power source (a-c, 0-125-V, 5-watt Powerstat typical)
f. Timer (for correlation of heater power supply with proper rate of temperature change)
g. Dummy crystal units (for mounting thermistor or thermocouple temperature sensing element of pyrometer)
h. Transparent adhesive tape (for binding together dummy crystal units)
i. Thermocouple wire, AWG \#26 or smaller
j. Vibration machine
k. Crystal mounting fixture for vibration machine

1. Shock testing machine
m. Container for immersion test
n. Ten-power microscope
o. Micrometer
p. Pin-alignment gauges and/or shadowgraph
q. Socket adapter for Crystal Holder HC-10/U (Crystal Socket Adapter UG-683/U, available from Walter L. Schott Co.)

## Test-Plant Fixtures

a. Primary power source ( 110 volts, ac)
b. Secondary regulated power source, if advisable
c. Mounting facilities (cabinets, shelves, benches, tables, stands, frames, racks, etc)
d. Cabinet facilities for storing records and expendable supplies
e. Desk facilities
f. Vibration-free area of building
g. Thermostatically controlled room

2-68. Brief functional descriptions of the equipments listed above are given below wherever the exact use of a unit is not self-evident. The descriptions follow the same order as in the outline above. The model mentioned to illustrate each type of equipment is to be interpreted as representative only. Equivalent, and probably improved, models for most of the types of equipment listed are generally available from the same manufacturer as well as from other manufacturers. The examples given as representative are the equipments currently being used by, or in developmen-
tal projects under the technical control of, the Frequency Control Group of the Communications and Navigation Laboratory, Wright Air Development Center.

## Primery Standards

2-69. Every arithmetical measurement involves the division of the quantity being measured into countable units. Where the object of the measurement is to make a relatively precise determination of the total number of units contained in the given quantity, it is necessary that the quantity and the test conditions, as well as the measuring unit, be well defined. For example, if the quantity being measured is the length of an iron bar, a precise measurement requires that the temperature of the bar be specified; otherwise, the particular length being measured, which would be different for each temperature, would not be known. Consequently, a measurement of the length also involves a measurement of the temperature, which, in turn, requires that the unit of temperature also be well defined. In general, the more precise the major measurement, the larger the number of auxiliary minor measurements to be made in order to establish the required test conditions. For each contemplated measurement, major or minor, a standard must be available to ensure the accuracy of the measured units. The accuracy of the measurement, of course, cannot be greater than the accuracy of the standard.
2-70. Before a numerical measurement can be made, a unit of measurement must be decided upon. Most, if not all, types of basic physical quantities now have internationally accepted units. These units, defined as concretely as practicable, are called absolute units. Measuring devices, constructed with the greatest possible precision to represent the absolute units, are stored in the chambers of the International Bureau of Weights and Measures in Sevres, France. These physical objects by common agreement serve as international standards. The units which the standards define are called international units. Theoretically, the international units are supposed to equal the absolute units, and so they do to the nearest degree attainable at the time the standards are constructed. But improved methods of measurement which permit greater precision are constantly being developed, so it is not unusual for discrepancies to be found between the international and the absolute units. In time, more precise instruments are accepted as international standards in place of the old, but the interval of delay is usually quite extensive. As a result, where measurements of optimum precision are being made, knowledge
of the exact degree of accuracy obtained is often obscured due to ambiguity regarding the accuracy of the reference units used as standards. Aiding the chance for ambiguity is the fact that each country has its own primary standards for domestic uniformity which may or may not be correlated with the international standards.
2-71. In the United States the national standards are controlled by the National Bureau of Standards, Washington, D. C. The official units of the United States are based on the yard-avoirdupois pound-second system of weights and measures rather than the meter-kilogram-second international system, but are, nevertheless, defined absolutely in terms of the international units. For example, the United States absolute yard is defined as equal to $3600 / 3937$ th of the international meter. Presumably the physical primary standard for length at the Bureau of Standards is one that has been carefully correlated with the International Prototype Meter at Sèvres. (The International Prototype Meter is the distance at $0^{\circ}$ centigrade between two fine transverse lines engraved on a platinim-irridium bar. This international primary standard was originally intended to represent an absolute unit of one ten-millionth of the distance between the north pole along a meridian to the equator. The absolute meter now is defined to equal $1,533,164.13$ wavelengths in air at 760 mm pressure and $15^{\circ}$ centigrade of the red line exhibited by cadmium (vapor) during electrical discharge.)
2-72. Within the United States, the primary standard for a particular unit is officially the standard maintained by the National Bureau of Standards. Other official measuring devices are called secondary standards since they must be correlated with the national primary standards. For some units there have been established hierarchies of standards. Each office has its own standard, which is checked against a local standard, which, in turn, is checked against a regional standard, and so on up to the national primary standard. Such is the system used in meteorological stations in respect to a sequence of correlated barometers of ascending accuracy. A similar system of standards is not readily available for all the types of measurements normally required in the testing of crystal units. The standards available are a mixture of various orders of accuracy and officialty. In the list of equipments in paragraph 2-67 we have arbitrarily classified as primary standards those standards of maximum accuracy that are not used in the actual crystal tests, but are employed only by calibrating, adjusting, or in some way correlat-
ing the instruments that are being used as reference standards in making the actual measurements. These latter instruments, whether or not they are periodically checked against another standard, we designate as reference standards.

## PRIMARY FREQUENCY STANDARD

2-73. To determine the frequency of any periodic event we must measure the number of times the event occurs during a given unit of time, or reciprocally, measure the number of time units contained in the duration of a given number of events. By either method the accuracy of the measurement will depend upon how accurately the unit of time is known. Unfortunately, we cannot freeze an interval of time and preserve it as a standard, so instead we rely upon the conservation of momentum to provide our standard. This is possible since a rotating body, if not acted upon by net external tangential forces, will turn through equal angles in equal intervals of time. The rotating earth is the internationally accepted time standard, there being no specially constructed standard as for the other fundamental units. The international unit, which is also the U. S. standard unit, is the second, which is defined to be $1 / 86400$ th of a mean solar day. A solar day is the noon-to-noon time between succeeding instances in which the center of the sun crosses the meridian of a fixed earth observer, as distinguished from a sidereal, or star, day. The former is the period of the earth's rotation on its own axis relative to the sun, whereas the latter, a slightly shorter time interval, is the period of the earth's rotation relative to the celestial universe. The sidereal day is essentially the same interval of time throughout the year, but the solar day fluctuates constantly and must be averaged over a long period. Actually, the earth is slowing down perceptibly due to the frictional losses of energy resulting from the tides; but its motions are now so well known and predictable that solar time can be estimated to accuracies on the order of one part in $10^{8}$.
2-74. In the measurement of time, for each transit of the earth through a mean solar angle of one second, one standard.cycle occurs; so that one complete rotation of the earth can be viewed as a sequence of 86400 standard cycles. Now, a radio signal is also a sequence of cycles. Should we call a given sequence a "frequency standard," instead of a "time standard", let it be clear that in changing the name we in no way change the nature of the phenomenon that the name symbolizes. If a radio signal can properly be described as a "frequency", so also might we describe a sequence of inch marks. If our unit of space-length is the
yard, we can describe the length of the inch by comparison with the length of the yard by saying that the "frequency" is 36 inches per yard. But note that the number 36 is simply a ratio between two lengths. Where the sequence of marks is something absolute in matter, their frequency is a mental comparison in an observer's mind. Similarly, it can be said that a sequence of radio cycles has an inherent material reality, but that the cycle frequency is only an observed relation of the duration of a cycle compared with that of a standard cycle. Thus; a signal of 100 kc per second means that, if compared with the period of one standard cycle, the period of one radio cycle is one hundred thousandth part. If this signal is defined as a frequency standard, it means that the period of its individual cycles are to be considered standard secondary subunits of the second, in much the same sense that standard inch marks are considered subunits of the yard. For it is as a standard unit of time that a frequency standard is used in the measurement of unknown frequencies. The measurements are made by comparing the periods of unknown duration with the periods of standard duration, and then interpreting the measurements in terms of frequency.
2-75. A standard frequency cannot be assumed to have an absolute value of greater precision than either of the two unit cycles of which it is a ratio. That is, the accuracy of the absolute value cannot exceed the stability of the frequency-control device nor the accuracy of the fundamental unit of time. Some oscillators have a short term stability so perfect that over short periods of time unknown frequencies can be measured relative to the frequency standard with much greater precision than the absolute frequencies can be known relative to the international unit of time. If such oscillators could maintain their stability without slow drifts with aging, they could conceivably replace the solar standard in establishing an international prototype unit of time. At the present time such oscillators are not available, but the great stability of atomic and molecular frequencies and the recent developments in the methods of exciting and detecting them, such as the experiments with ammonium clocks at NBS, suggest that eventually perhaps an atomic international time standard will replace the solar standard.*
2-76. The national primary frequency standard is a battery of $100-\mathrm{ke}$ crystal oscillators controlled by G elements at the National Bureau of Standards. Use of this standard is readily available to anyone living in the region immediately surrounding Washington, D. C., since the output of the
standard is used to control the sequence of standard signals continuously broadcast from station WWV. The WWV standard signals (see figure $2-87$ ) are at radio frequencies of $2,500 \mathrm{kc}, 5,000$ $\mathrm{kc}, 10,000 \mathrm{kc}, 15,000 \mathrm{kc}, 20,000 \mathrm{kc}$, and $25,000 \mathrm{kc}$ and are available by tuning a receiver to any one of these channels. At regular intervals, whose duration serves as a national time standard, the WWV signals are modulated by standard audio frequencies of 440 cps and 600 cps , which can be used in calibrating an interpolation oscillator. For the calibration of $r$-f standards only the 30 -second c-w intervals are employed.
2-77. The national primary standard can be assumed to have a relative stability on the order of 1 part in $10^{9}$ over any 24 -hour period, but the absolute frequency, the number of cycles per international unit of time, cannot be guaranteed beyond an accuracy of 1 part in $10^{*}$. An additional restriction is that this accuracy is only possible if the standard signal is being received as a ground wave. If a sky wave is being received the constantly varying pathlengths due to movements of the ionosphere create doppler effects, so that the received signal is randomly frequency modulated. $\dagger$ Eventually, it is to be hoped that a chain of relay stations can make available WWV ground signals in all parts of the country. At the present time, one slave station, WWVH, is maintained in the Territory of Hawaii. If top precision frequency measurements are to be made in localities remote from both WWV and WWVH, the engineer should have available a high-stability secondary standard which can be periodically brought to Washington and checked against the official primary standard. For the calibration of standards having short-term instabilities greater than 2 or 3 parts per $10^{*}$, the WWV and WWVH sky

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Figure 2-87. Chart showing standard time and frequency signals broadcast by Stations WWV and WWVH (Subject to change)
waves are satisfactory. These can be received on one channel or the other throughout the U.S.

## PRIMARY CRYSTAL TEST SET

## STANDARDS

2-78. The specifications of Military Standard crystal units require that they be tested in standard reference sets. The primary standard test sets are Government-maintained models of the following types of crystal impedance meters:

$$
\begin{array}{cc}
\text { Crystal Impedance Meter } & \begin{array}{c}
\text { Frequency Range } \\
\text { (kc/sec) }
\end{array} \\
\text { TS-710/TSM } & 10 \text { to } 1100 \\
\text { TS-537/TSM } & 75 \text { to } 1100 \\
\text { TS-330/TSM } & 1000 \text { to } 15,000 \\
\text { TS-683/TSM } & 10,000 \text { to } 75,000
\end{array}
$$

(CI Meter TS-537/TSM listed above is expected eventually to be replaced entirely by TS-710/ TSM.) For Government laboratory tests, the primary standard sets are generally used as the actual test reference circuit in which the crystal is inserted. This is not true in the case of produc-tion-line and quality-control tests to be made by manufacturers. Here, the Government furnishes
primary standard test sets to a manufacturer only for the purpose of correlating the reference test circuits used by the manufacturer. Even the Government inspection tests of sample lots of crystal units are made with the manufacturer's reference sets and not with the primary standards. When initially obtaining his reference test sets, the manufacturer may build them himself, duplicating the primary-standard circuitry, or he may purchase Military Standard test sets in the commercial market. But the fact that such sets are used for routine tests in production control officially rules out their classification as primary standard sets.

## PRIMARY LOAD-CAPACITOR STANDARD

2-79. For routine measurements, the load capacitor contained in each standard Cl meter can be considered sufficiently accurate to use without special correlation with a primary standard. However, when precision measurements are required, or when any significant deviation in the calibration of the standard test set should seem to occur, there should be available an external precision standard capacitor with which the test set capacitor can be correlated. A suitable capacitor to serve
as a standard is Precision Capacitor Type 722-D, General Radio Co., or its equivalent.

## PRIMARY CALIBRATED-RESISTOR STANDARD

$2-80$. In order to check the accuracy of the calibrated resistors used in adjusting the crystal test sets, it is desirable that a precision r-f resistance standard be available. The standard should be adaptable for use in a radio-frequency bridge. For this purpose, it is generally convenient to employ a bridge circuit in which a precision resistor standard is incorporated in the design as a component part. See paragraph 2-108.

## PRIMARY TEMPERATURE STANDARDS

$2-81$, The boiling and freezing points of distilled water, with due regard for the atmospheric pressure, permit more than ample precision as a primary standard for routine calibrations of the temperature measuring equipment. Normally, the absolute barometric pressure at the time of testing need not be noted-only the mean pressure for the local elevation above sea level.

## Reference Standards

## SECONDARY FREQUENCY STANDARD

2-82. In those areas not reached by WWV ground waves, the crystal frequency measuring equipment should include a secondary frequency standard capable of a relative stability of 1 part in $10^{\circ}$ per day or better. A high-precision secondary standard is also desirable, of course, even when WWV signals are constantly available. But in this case, a standard of less stability, if correlated frequently with WWV, can be as dependable as a maximum-stability unit that is correlated only after long intervals of operation. It is the secondary standard that is used to control the periods of the known cycles against which those of the unknown signal are to be compared.
2-83. A large number of high-precision standards are available on the commercial market. Of these, one that appears the equal, if not the superior of any other in aging stability is the James KnightsSulzer frequency standard, developed jointly by the James Knights Co. and P. G. Sulzer of the National Bureau of Standards. This standard is used in the development of USAF frequency standards to measure fractional deviations in frequency to an accuracy of 1 part in $10^{9}$ per day. For this degree of precision two Knights-Sulzer standards are used and each, once turned on, are never turned off. The crystal frequency to be measured is checked against each standard and the standards checked against each other. The
high precision obtainable is due in large part to the use of evacuated glass holders in the fabrication of the crystal units employed in the standards, and in the extreme care used in the cleaning stages. The aging data for a 1 -me standard operated continuously from a constant-emf mercury cell at the Knights laboratories showed a net frequency shift from $999,999.5 \mathrm{cps}$ to $999,999.7 \mathrm{cps}$ between November 27, 1953 and March 8, 1955. During this period the frequency fluctuated both above and below the starting frequency by amounts greater than the 2 parts per $10^{7}$ indicated for the total period; so that although a tendency for neither a positive nor a negative aging drift is indicated definitely for long periods of time, the stability over shorter intervals must be assumed to be less than the long-term average. During a 2 -month test by the Signal Corps, one crystal unit of the type used in the J.K. frequency standard exhibited a stability of 1 part in $10^{8}$ per week; another unit, 3 parts in $10^{*}$ per week.
2-84. Where reference standards with stabilities on the order of 1 part in $10^{*}$ per day are satisfactory, a representative type is the $100-\mathrm{kc}$ frequency standard, R-F Oscillator 0-76/U, of the Western Electric Co. Signal Corps engineers report that the 0-76/U oscillator, after aging, can be expected to have a frequency stability on the order of 1 part in $10^{3}$ per day.

## AUDIO-FREQUENCY REFERENCE STANDARD

$2-85$. The a-f reference standard is a variable interpolation oscillator that is used as a differencefrequency reference standard in measuring audio beat frequencies and as a frequency-deviation reference standard for calibrating the frequencydeviation meter and recorder. The conventional method of measuring radio frequencies is to mix the unknown signal with a harmonic (or a subharmonic, or a harmonic of a subharmonic) of the fundamental of the secondary frequency standard. A difference frequency in the audio range is obtained and compared with the output of the variable audio-frequency (interpolation) oscillator. The latter is adjusted until its frequency is equal to the unknown difference frequency. The tuning dial of the variable oscillator will have been calibrated to permit an interpolated reading of the difference frequency, which can then be added to or subtracted from the standard harmonic to give the unknown frequency. The variable oscillator will previously have been correlated with the frequency standard at one or more representative check points, in reference to which the v-f-o tuned frequency can be interpolated.

2-86. As a frequency-deviation reference standard, these calibrated check points of the interpolation oscillator are used in the correlation of the frequency-deviation meter and the frequencydeviation recorder prior to a temperature-run test.
2-87. The interpolated frequencies, of course, are not as accurate percentagewise as the crystaloscillator standard; but if the measured difference frequency is an extremely small fraction of the unknown frequency, the error introduced by the interpolation oscillator can be expected to be of much smaller magnitude in terms of cycles per second than the normal deviations of the crystal standard. If precision measurements of the difference frequencies are required, it would be preferable to count the cycles with a frequency counter directly controlled by a crystal standard, or to zero-beat the difference frequency with a vfo that in turn is continuously monitored by a crystalstandardized counter. A representative audio frequency reference standard is the 0 -to- 5 -ke Interpolation Oscillator Type 1107A, General Radio Co.

## REfERENCE CRYSTAL TEST SETS

$2-88$. As explained above in the discussion of the primary standard test sets, crystal manufacturers employ reference standard test sets for produc-tion-line and quality-control tests. The reference sets are CI-meter circuits that duplicate those of the primary standards, but which are usually modified somewhat and probably removed from their cabinet to permit convenient installation on or under a testing table in a production line. These reference test sets are correlated periodically with the primary standard test sets by Government inspectors.

## TEMPERATURE REFERENCE STANDARD

$2-89$. Normally a pyrometer is used as a secondary temperature standard for the purpose of correlating the cold box thermometer and other temperature gauges, and the crystal heating controls. The same pyrometer is also generally used as the indicator in measuring the crystal-unit temperature during a temperature-run test. The sensing element of the pyrometer can be a thermocouple or a thermistor, the latter being the more accurate since the temperature reading will be independent of the temperature of a room-temperature junction. Whichever is used, it should be mounted on the quartz plate of a dummy crystal unit in order to simulate as closely as possible the thermal parameters associated with the crystals being tested. The sensing element, being in series with the current windings of the pyrometer, causes the
deflection needle to follow the temperature changes of the dummy crystal plate. A separate dummy crystal unit should be available for each type of crystal holder being used in the tests. Where greater precision is required than is normal for routine tests, the dimensions and mounting of the crystal in the dummy unit should closely simulate the dimensions and mounting of the crystal in the test unit. For this purpose, a dummy crystal unit should be available for each narrow range of frequencies for each type of crystal unit to be tested, instead of simply for each type of crystal holder. The pyrometer scale for each sensing element should be checked and correlated periodically against the primary standard (boiling water and/or ice water). The scale should be calibrated in degrees centigrade. If a thermocouple is used, the current meter should be a microammeter; if a thermistor is used, a $0-1$ ma. meter could be used if the power dissipated in the dummy crystal unit does not exceed the drive level of the crystal being tested; but for minimum error, a microammeter is requisite, especially where very thin crystals are to be tested. Preferably the current meter will be a component part of a temperature recorder. A typical thermistor is the Ney Co. model used to measure the dummy crystal temperature in a heater designed by E. L. Minnich as a modification of a USAF-developed model. The thermistor is enclosed at one end of a sealed glass stem. Electrical connection is through two copper-wire leads. Approximately, the resistance varies from 2000 ohms at room temperature to 400 ohms at $90^{\circ} \mathrm{C}$. The dummy unit and the test unit are mounted side-by-side in the heater. For greater thermal contact with the dummy crystal blank, and hence for less lag in the temperature readings, the Frequency Control Group at WADC employs a platinum-wire thermistor wrapped around the dummy blank. The WADC heater designed by $D$. J. Theobald, is 1.5 in . diameter slug, 2.5 in . long which mounts the test crystal unit in one end and the dummy unit in the other.

## REFERENCE LOAD CAPACITORS

2-90. The calibrated capacitor used as a standard for simulating the rated load capacitance of a parallel-mode crystal unit will be a component part of the CI meter used as a reference test set. Thus, it does not have to be supplied separately unless the test circuit is being constructed locally. A typical load capacitor is a calibrated, variable, single-section, air-dielectric unit with a range of 5 to $100{ }_{\mu \mu}$ f.

## REFERENCE CALIBRATED RESISTORS

2-91. A set of calibrated r-f resistors which covers the effective-resistance range of all Military Standard crystal units to be tested must be available for use with those test sets which are not provided with an internal calibrated resistor set. The calibrated resistors do not have to be precision standards, but they should have short leads and be composition (noninductive) types with tolerances of their nominal values not greater than plus or minus one per cent. The same resistors can be used in both the primary standard test sets and in the manufacturer's reference test sets. For test set adjustments of the drive level for crystal units of maximum effective resistance, it would be convenient to have available a set of maximum-resistance resistors mounted on crystalholder plug-in bases. The standard Armed Services CI meter, TS-330/TSM, and also the limitedstandard model, TS-537/TSM, are internally provided with calibrated decade resistor circuits and appropriate switching controls. External resistors are required for use with the standard CI meters, TS-710/TSM (which is replacing the TS-537/ TSM) and TS-683/TSM.

## Indicating and Recording Instruments

## FREQUENCY COUNTER OR METER

2-92. Certainly, the quickest method for measuring a frequency with reasonably good accuracy is to feed the unknown signal to the input of a frequency counter and read the frequency directly. Representative units used in the crystal industry at the present time are the crystal-controlled counters developed by the Hewlett-Packard Co. Typical models are the 5 -digit 522B and the 8 digit 524B. The principle of operation of these counters is essentially the same as that used by a doctor in measuring a pulse rate. It is not the frequency that is counted, but the number of pulses during a given length of time. A crystal oscillator is used as a time standard to measure accurately a given length of time, serving the same purpose as the doctor's watch. (The crystal standard provided with the Hewlett-Packard counter type 524A is reported to have an accuracy of 2 parts in $10^{6}$ per week-for greater accuracy, input controls are incorporated to permit the use of an external frequency standard.) The crystal timing circuit controls a fast-acting flip-flop electronic gate. When the gate is open, the input cycles of the frequency to be measured are passed through to a counting circuit. The gate-controlling circuit can be adjusted to keep the gate open for crystal-controlled intervals of 0.001 second to 10
seconds. If, for instance, the gate is open for one second, the number of input cycles passing through will equal numerically the unknown frequency. It is the problem of the counting circuit to count the cycles accurately. The counting is performed by a sequence of cascaded decade scalers, each of which operates its own indicating system. Each scaler generates one output pulse for every ten input pulses to the circuit. The first scaler divides the input cycles by ten and feeds its output to the second scaler. The second scaler divides by ten again, and passes its output on the third decade scaler. And so on to the last scaler. When the gate is closed, each scaler indicates by a neon lamp a digit representing the number of pulses it has just received from the preceding scaler which have not been passed on to the succeeding scaler. (In the H-P 524B, the first two scalers indicate by meters.) In other words, each scaler effectively counts all the pulses it receives, divides by ten and passes the quotient on to the next scaler to count, and then shows the remainder by lamp light on the front panel. The observer can thus read the frequency directly. A decimal point is automatically positioned to give the reading in kilocycles. Before opening the gate for the next count, the gate flip-flop circuit resets the counting circuit. The counting accuracy is $\pm 1$ count, or a maximum of 1 part in $10^{4}$, where $d$ is equal to the number of digits shown. The frequency range of a single counter, without accessory circuits, is 0 to 10 mc . The addition of plug-in units can extend the range to 220 mc . A plug-in amplifier unit permits an increase in input sensitivity from 1 volt rms, minimum, to 10 millivolts rms, minimum. By using the unknown frequency to control the electronic gate and feeding the frequency standard to the input, the counter can be used to measure the period of the unknown signal in seconds, milliseconds, or microseconds, with the decimal point automatically positioned. A counter also permits a ready method of utilizing WWV sky-wave signals as a primary standard having almost the same dependability as is possible with WWV ground signals. Since the random frequency deviations of the sky wave can be expected to average out over a relatively long period of time-a second is a sufficient interval, except possibly in times of severe ionospheric storms-the WWV sky signals can be received, amplified, and divided (if necessary) for use as a timing standard to control the electronic gate of a counter at intervals of 1 second or greater. With the one-second intervals as measured by the sky wave practically as accurate as those of the ground wave, the counter can thus be
used to give a precision reading of the local secondary standard frequency and permit its corcelation with the WWV primary standard. The otal accuracy, of course, cannot be greater than the counting accuracy, which, in turn, increases by a factor of 10 for each digit shown. For a counting accuracy between 1 part in $10^{8}$ and 1 part in $10^{9}$, a minimum of 8 digits must be indicated in the counter reading.
$2-93$. Other types of frequency meters in widespread use are those of the older heterodyne v-f-o type. The variable-frequency oscillators are periodically calibrated at standard-frequency check points. The unknown signal is mixed with the v -f-o signal, the latter being varied until a zero beat is obtained. The beat note can be indicated either aurally or visually. With precision dialing of the vfo and careful interpolation between the standard harmonic check points, quite high accuracies can be obtained. The closer the check points, the nearer the measuring accuracy approaches the accuracy of the check-point standard. With a isual (oscilloscope) indication of the null heterodyne point this approach can be quite close. The average v-f-o heterodyne frequency meter, nevertheless, is less accurate than those measuring systems that employ the frequency standard, itself, to heterodyne directly with the unknown frequency. Representative heterodyne frequency meters are Frequency Meter FR-4 and Frequency Meter Set SCR-211( ).
2-94. Direct-reading frequency meters employing frequency-divider circuits, which can be calibrated against (but not controlled by) frequency standards, are also in use. The precision of such meters is generally not satisfactory for any but lowfrequency crystal measurements. In the audio range such meters are quite useful. (See Fre-quency-Deviation Meter, paragraph 2-96.)
2-95. As for the use of wavemeters, they are entirely too inaccurate for ordinary crystal measurements. Such meters, being little more than a tuned series circuit with a resonance indicator, are, of course, relatively inexpensive and easy to construct. For very-low-frequency measurements, where broad tolerances are permissible, a wavemeter conceivably could find a useful application if the expense of a more accurate meter is unwarranted.

## FREQUENCY-DEVIATION METER

2-96. The frequency-deviation meter is a conventional electronic frequency meter to be correlated with the interpolation oscillator. Its principal purpose is to provide a direct reading of the difference frequency obtained when the frequency of
the crystal under test is mixed with the standard test frequency. Since the difference frequency that would result if the crystal frequency equaled its nominal value is known, the frequency deviation is readily measured as the difference between the actual meter reading and the hypothetical nominal reading. The frequency-deviation meter should also provide an adjustable d-c output for feeding the frequency-deviation recorder.
2-97. The input signal to a typical electronic frequency meter is first amplified to a given level and limited so that each cycle has a predetermined amplitude. A counting circuit follows, which serves to trigger a current pulse of fixed charge that flows through the meter windings. The meter reading will thus be directly proportional to the number of current pulses per second, which in turn will be directly proportional to the number of input cycles per second.
2-98. A representative frequency-deviation meter is the Hewlett-Packard Frequency Meter Type 500 A or 500 B . The latter has a range of 0 to 100 kc ; the former extends only to 50 kc . A phone jack on the panel permits connection to a 1-ma., 1400 -ohm frequency-deviation recorder. The input sensitivity is 0.2 volt rms, minimum.

## FREQUENCY-DEVIATION RECORDER

2-99. An automatic recorder is required to provide a graphical record of the deviation in frequency as the temperature of the crystal unit being tested is made to vary over the rated operating range. As a strip of graph paper uniformly unwinds, a stylus, or an equivalent device, is actuated by an input from the frequency-deviation meter in such a way that the frequency measurements are continuously recorded on the graph. Additional current pulses at regular temperature intervals from a temperature recorder can serve to calibrate the abscissa of the graph in degrees centigrade. Before testing each type of crystal unit at a given frequency, the recorder must be correlated with the frequency-deviation meter and the temperature recorder. A representative ammeter recorder is the Esterline-Angus Automatic Recorder Model AW, which has a 1-ma. (dc), 1400 -ohm (plus or minus 100 ohms ) input.
OSCILLOSCOPE
$2-100$. The oscilloscope is used to provide a visual check when correlating the interpolation oscillator against a crystal standard, and when measuring a difference frequency with the aid of the interpolation oscillator. For either of the above uses, the horizontal plates of the oscilloscope are connected to the output of the interpolation oscillator and the vertical plates are connected to the output
of the receiver. The operator adjusts the interpolation oscillator to obtain a fixed image on the screen, at which point he can either calibrate the interpolation oscillator against a known receiver output, or interpolate an unknown receiver output from the oscillator calibration. A representative oscilloscope is the Dumont Type 241.

## GRID-CURRENT METER

2-101. All standard Armed Services CI meters are equipped with a front panel grid-current meter except the TS-710/TSM, which is provided with a vacuum-tube voltmeter. For the reference test sets not provided internally with a gridcurrent meter, an external meter must be provided. The meter is used principally in correlating the grid excitation of the reference circuit with the effective resistance of the crystal unit. It is then used to correlate the effective-resistance recorder against the reference grid-current levels for maximum specified and minimum expected values of resistance. A representative meter is the JAN type Meter MR26W200DCUA ( 0 to 200 $\mu \mathrm{a})$.

## EFFECTIVE-RESISTANCE RECORDER

2-102. A recorder is used in the testing of Military Standard crystal units to automatically plot on graph paper the deviations in crystal resistance as the temperature is varied over the operating range. The recorder stylus is to be actuated by the d-c current in the grid circuit of the reference test set. If the recorder is sufficiently sensitive, the grid current may be used directly; otherwise a d-c amplifier should be employed. The minimum grid current, and hence the minimum excitation of the recorder, occurs when crystal units of maximum resistance are being tested. By previously correlating the recorder with the maximumresistance grid-current level, the graphical record will indicate whether the resistance of any crystal unit exceeds the rated maximum at any temperature. By also feeding the effective-resistance recorder input pulses from the temperature recorder at regular temperature intervals (every 5 degrees centigrade is normal), the abscissa of the resistance graph will be calibrated in temperature degrees. A recorder of the Esterline-Angus type, described in paragraph 2-99 as representative of the models satisfactory for recording the frequency deviation, is also satisfactory for recording resistance deviation; but a d-c amplifier might be required to provide the necessary sensitivity. A representative recorder sufficiently sensitive to operate at the microampere level is the $0-$ to $-5-\mu \mathrm{m}$ Photoelectric Recorder Model 8CEIELIB-1 of the General Electric Co.

## ELECTRONIC A-C VOLTMETER

$2-103$. An a-c voltmeter is required to measure the voltage across the crystal units under test when determinations of the drive level are desired. Care must be taken that the voltmeter causes no significant imbalance or disturbance of the tuned CI-meter circuit. Because of the extreme sensitivity of the test circuits, particularly at the higher frequencies, conventional a-c voltmeters are not satisfactory for such measurements. Only those meters of maximum input impedance and sensitivity should be used. Even then, unless the voltmeter circuit is a differential type, the voltmeter leads should not be connected directly across the crystal unit, as the unmatched impedances to ground of the two leads can cause the test-circuit frequency-and hence the crystal impedance and voltage-to change. The proper method would be to measure the voltage from each crystal-unit terminal to ground separately, making certain that the act of measurement does not in itself change the test frequency of the crystal. The voltage across the crystal unit, of course, is equal to the difference between the two measured voltages. Suitable vacuum-tube voltmeters are the equivalent of Multimeter TS-505/U or the Hewlett-Packard Electronic Voltmeter Model 410 B . To be preferred would be a differential vacuum-tube voltmeter such as Voltmeter ME-56 ()/TSM. (The ME-56( )/TSM should not be used above 60 mc unless special calibration procedures are employed.)

## DUMMY-CRYSTAL-UNIT PYROMETER

2-104. This is the same pyrometer that is described above as a secondary reference standard used in the correlation of the other temperature indicators and controlling devices. It is also used during the temperature-run tests as an indirect indicator of the crystal-unit temperature at each instant. The sensing element (thermistor, preferably, or thermocouple) is mounted on the crystal plate in a dummy crystal unit simulating the holder and construction of the crystal unit under test. The heater, which mounts the test crystal during the temperature run, should provide an equivalent mounting position for the dummy unit. The temperature thus indicated by the pyrometer can then be considered a reasonably close approximation to the simultaneous mean temperature of the test crystal.

## COLD-BOX THERMOMETER

2-105. Except when mass quantities on a production line are being tested, it is usual for only one crystal unit to be tested during a temperature
run. For this purpose a thermostatically controlled cold box is adequate for cooling the crystal unit to the low-temperature limit. When the temperature run for an individual unit is ready to begin, the unit is removed and mounted in a heater. To make certain that the temperature of the cold box is correct, a thermometer must be provided which has previously been correlated with the pyrometer reference standard. The coldbox thermostat is then adjusted to maintain the correct reading on the thermometer.
2-106. When multiples of perhaps a dozen crystal units are to be given a temperature-run test simultaneously, the cold box and heater are usually replaced by a single chamber which can be cooled and heated as desired by a thermostatically regulated air stream. Even so, a thermometer periodically correlated with the reference pyrometer should be in view to give an accurate indication of the crystal chamber temperature when making thermostatic adjustments and starting a temperature run. Any medium-precision mercury thermometer, such as those used by chemists in measuring reaction temperatures, is satisfactory, provided the calibrated scale covers the necessary temperature range.

## Q METER

2-107. A Q meter is required for calibrating the reference test load capacitors against the precision standard. The Q meter should be equipped with a standard inductance coil. A representative model is Q Meter TS-617( )/U.

## R-F BRIDGE

2-108. An accurate r-f bridge is required in the correlation of the calibrated resistors used as references when measuring the effective resistance of crystal units and when adjusting the test sets to suitable drive levels. The standard resistors, against which the reference resistors are to be checked, are preferably component parts of the $r$-f bridge. A satisfactory bridge would be the equivalent of R-F Bridge Navy Type No. 60094.

## EARPHONES OR LOUDSPEAKER

2-109. Earphones and/or a loudspeaker are desirable as frequency indicators when rapid frequency checks are to be made and neither recordings of temperature runs nor great precision is required. Audio measurements, made by zerobeating the crystal frequency against a known frequency, are particularly suited to certain pro-duction-line stages. For example, when plating or etching a crystal to frequency, an audio check is usually the simplest procedure to ensure that the crystal does not overshoot its mark. In laboratory
tests, the radio receiver speaker has many uses, such as providing the aural check when zerobeating the secondary frequency standard against WWV signals.

## Auxiliary Amplifiers and Frequency Converters RADIO RECEIVER

2-110. A cw-mow receiver is required for the reception of WWV signals and for use as a bandpass amplifier, mixer, detector, and audio amplifier of the various signals used in the measurement of crystal frequencies. Other than its use as an r-f amplifier of the antenna signals received from WWV, the receiver serves chiefly as a mixer-amplifier of the standard frequency and the unknown frequency, and as the detector and amplifier of the resulting audio beat frequency. The r-f tuned circuits, of course, also perform the function of filters in rejecting the amplification of all but the desired band of input frequencies. For fast, approximate checks of frequency adjustments, such as when initially tuning a test set to a given nominal frequency, the receiver can be tuned to the desired frequency, the bfo turned on, the output indicated by an audio or visual indicator, and the oscillating circuit adjusted to a zero beat. For low-frequency measurements, Radio Receiver BC-342() or BC-348( ) or an equivalent is satisfactory. For higher frequencies, a receiver such as the Hammarlund Model SP-600, with a range from 0.55 to 54 mc , is adequate.

## HARMONIC GENERATORS

2-111. Other than a precision secondary frequency standard, a crystal-test laboratory generally has the need for a number of auxiliary frequency generators and harmonic multipliers. For some purposes, these generators, although requiring crystal control, need have only a medium degree of stability-a few parts in $10^{6}$ being sufficient. For example, in correlating a reference load capacitor with the precision standard capacitor, a $400-\mathrm{kc}$ crystal-controlled generator of medium stability is desirable for use with the Q meter. Such a generator could be a Signal Generator TS497/URR, or its equivalent: Generally, for multipurpose work, a frequency generator is preferred that can be switched from medium-precision internal control to high-precision external control when harmonics of the precision standard are required. When a harmonic generator is controlled by the principal frequency standard, the output of the harmonic generator in effect becomes the frequency standard with which the measurements of the unknown frequency are to be made. Although it would be desirable to have

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selector circuits so that all harmonics are rejected except the particular one selected, such a degree of perfection is not economically practical except where the utmost precision is to be combined with maximum speed of measurement. Nevertheless, harmonic generators of this nature are commercially available. (See the discussion of the Plessey Frequency Synthesizer in Section I.) The harmonic generators most generally found in crystal-test laboratories do not provide sine-wave outputs, but outputs rich in all harmonics simultaneously. Where subharmonics, and harmonics of the subharmonics, of the precision standard are required, the harmonic generator must be designed for frequency division of the controlling standard-that, or else a separate frequency divider must be provided for installation between the standard and the harmonic generator. When the fundamental of the harmonic-generator output is the fundamental of the frequency standard, the generator design need consist of no more than conventional untuned class $C$ amplifiers or multivibrators. When the fundamental of the harmonicgenerator output is to be a higher multiple of the standard fundamental, tuned amplifier-multiplier stages must precede the final harmonic-generator output amplifier. If the tuned-multiplier circuit is not an inherent part of the harmonic-generator unit design, the circuit must be supplied separately.
2-112. For the calibration of the audio-frequency interpolation oscillator, a 1 -ke harmonic generator is desirable but not necessary. A 10-ke harmonic generator can be used for calibrating the a-f oscillator just as easily, and at the same time provide a standard harmonic sequence for measuring low and very low frequencies. For this latter purpose, as an aid in identifying the exact multiple of 10 ke by which a given beat frequency is obtained, it is helpful, but not mandatory, that the same unit be capable of generating harmonics of 9 kc and 11 kc . A harmonic generator providing $9-10-$ 11-kc outputs is the CV-118, developed by the Washington Institute of Technology.
$2-113$. The principal function of a 10 -kc harmonic generator as a frequency standard is to ensure that, on mixing its output with the unknown signal, one of the resulting difference frequencies will be not greater than 5000 cps , and hence can be measured to an accuracy of a cycle per second or better with the aid of an interpolation ascillator and an oscilloscope, and to a somewhat lesser accuracy with a frequency-deviation meter and/ or a recorder.
2-114. When frequencies are to be measured that
are higher than the useful harmonic range of the $10-\mathrm{kc}$ generator, they can be reduced to the 10 kc harmonic range by frequency division, or by heterodyning with a higher-frequency standard to obtain a low difference frequency, which, in turn, can be mixed with the 10 -ke harmonics to obtain a difference frequency in the a-f range. The latter method of mixing the unknown frequency first with a high-frequency standard and then with a 10-kc harmonic does not necessarily require two separate mixing stages. The 10 -ke harmonics and the higher-frequency harmonics can be mixed simultaneously with the unknown. A receiver is used to detect the audio beat note. It is only necessary that the mixing circuit precede the superheterodyne mixing stage of the receiver; otherwise the beat note will follow all variations of the receiver local oscillator. For example, the standard frequencies should not be used to replace the b-f-o frequency of the receiver, unless the receiver happens to be a tuned r-f type.
2-115. Now, if a given harmonic of 10 kc permits an audio beat frequency of $f_{1}$, an adjacent harmonic will provide another audio beat note equal to 10 kc minus $\mathrm{f}_{1}$. The beat note of interest is the one less than 5 kc . To restrict all higher beat frequencies, the receiver should be provided with a low-pass audio filter in the output with a sharp cutoff at 5 kc . In the event that the two lowest beat frequencies are both approximately equal to 5 kc , the 9 -ke or 11 -kc harmonics should replace the $10-\mathrm{kc}$ standard.
2-116. The principal frequency standard probably will have a fundamental of 50,100 , or 200 kc , with the $100-\mathrm{kc}$ fundamental being the most common. Harmonics of the low-frequency standard can be mixed with the 10 -ke harmonics for measurements in the medium-frequency range and in the high-frequency range up to 10 mc , if desired. Generally h-f harmonics will be present in the principal frequency-standard output in sufficient strength that an external multivibrator or other type of harmonic generator, other than the $10-\mathrm{kc}$ unit, is not required. However, if an external harmonic generator is necessary, it may well be that greater equipment efficiency can be attained if a generator fundamental higher than that of the principal frequency standard is employed.
2-117. If a multivibrator is used to generate the 10 -ke signal, its useful harmonic range will normally extend as far as the 100 th harmonic. Beyond this, unless frequency division of the unknown frequencies is to be used, a 1 -me harmonic generator can be used. The useful harmonic (not frequency) range of the 1 -me generator is gener-

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ally much less than an equivalent 10-kc generator, since the higher harmonics are in the v-h-f spectrum and hence are more rapidly attenuated by distributed circuit losses. Thus, for the measurement of vhf's, if frequency division is not employed, a harmonic generator of $10,15,20$, or 25 mc should also be available. A representative 1 -me harmonic generator is the JAN type CV-119, or its commercial equivalent, Frequency Generator RA-35134, developed by the Washington Institute of Technology. A representative generator of high frequencies is the $15-20-25-\mathrm{mc}$ frequency generator, JAN type CV-122, manufactured by the Reeves-Hoffman Co.

## FREQUENCY DIVIDER

$2-118$. Where the frequency to be measured is higher than the range of the receiver, one of two means can be employed to lower the frequency of the unknown signal. The first is to heterodyne the unknown frequency with a known standard so that a difference frequency in the radio range of the receiver is produced. The difference frequency can then be measured by conventional methods. The original unknown frequency can thus be computed from the measured difference frequency and the heterodyne standard. The second method is to divide the unknown frequency by a known amount, and then to measure the quotient frequency. Frequency dividers designed as separate units specifically for reducing unknown frequencies to more easily handled lower frequencies do not appear to be readily obtainable at the present time, at least, their availability is not widely advertised. However, there are available counter units, principally of the decade type, which can be used in frequency-measuring systems as frequency dividers. But such dividers are not available in the v-h-f range where they would be of most use. Free-running multivibrators which can be adjusted for synchronization at a subharmonic of the unknown frequency are probably the most effective method of frequency division of very high frequencies. A lock indicator meter should be provided which will show a sharp peak when an appropriate stage is tuned to synchronization with the control frequency. Although measurements of considerable accuracy can be made using frequency division, greater accuracy in the v-h-f range is generally possible if the conversion to a lower frequency is accomplished by the heterodyne method.

## VARIABLE-RADIO-FREQUENCY OSCILLATOR

2-119. An r-f oscillator continuously variable over the expected crystal-test range is always useful if
rapid frequency checks are to be made and the accuracy does not have to be of the utmost precision. A vfo is particularly applicable when testing unfinished crystals along a production line. The frequency of the crystal unit under test is mixed directly with the v-f-c output, and one or the other is adjusted until a zero beat is obtained. Some method must be employed to check the accuracy of the known v-f-o frequency against a standard. This can be done periodically by crystal calibration, or continually by employing a crystaltimed counter. The vfo can be any standard signal generator of suitable range, such as Signal Generator TS-497/URR, for example.
R-F AMPLIFIER
2-120. R-f amplifiers are required as separate units wherever the r-f output from one equipment is not sufficient to provide the input level required by succeeding equipment. Such amplifiers are most likely to be required for boosting the inputs to counters, frequency meters, harmonic generators, frequency dividers, and the like, particularly where relatively long cable distances are involved and the frequencies are high.

## D-C AMPLIFIER

2-121. A d-c amplifier will be required if the d-c input necessary to properly activate a recorder is greater than that supplied by the respective sensing circuit. Where a d-c amplifier is most likely to be needed is to boost the input to the effectiveresistance recorder, which, if not of microampere sensitivity, cannot provide a full-scale recording if activated directly by the grid current of a reference test set.

## SIGNAL CONTROL PANEL

2-122. A central switching panel should be available for facilitating the control of all the r-f equipment used in the crystal testing system. Controls should be provided to permit any desired heterodyning and routing of the outputs of the various frequency sources to be used in the tests. Attenuators and a mixer circuit are normally incorporated in the panel design. Such is the design of the CV-120 mixing and switching panel. Switches are provided for selecting the appropriate CI meter, for selecting the signal from the appropriate frequency generator, for selecting attenuators for each signal, and for directing the output of the mixer to the receiver. Great care must be taken in the design of the control panel and the entire r-f signal system to provide adequate shielding of all circuits, and adequate r-f filtering of all power leads. If this is not done, stray frequencies will find their way into the
radio receiver to confuse the measurements. It is also important that the signal levels be of relatively low amplitude. The control panel should be provided with suitable attenuators and amplitude controls.

## Auxiliary Test-Control Devices and Test-Piant Pixteres

2-123. In the list given in paragraph 2-67 for equipments used in measuring frequencies, these items classified as Auxiliary Devices for Controlling Crystal Unit Test Conditions and as TestPlant Fixtures, if not self-explanatory, are described functionally in the discussions of related test procedures and equipments: and so, will not be discussed additionally at this point.

## FREQUENCY-MEASURING SYSTEMS FOR TESTINE CRYSTAL UNITS

2-124. Figures 2-88 to 2-94 illustrate by block diagrams a number of frequency-measuring systems commonly used in laboratories and manufacturing plants. For the reader who has followed the foregoing discussion of the equipments used, the illustrations should require only brief explanations.

## Heterodyne-Frequency-Meter System

2-125. Figure $2-88$ shows the system for measuring crystal frequencies with a heterodyne type of radio-frequency meter and earphones (or speaker). In the decade preceding World War II this method was by far the most commonly used for making relatively precise frequency measurements. The test frequency and the output of the $r-f$ vfo are heterodyned in the r-f mixer. The coupling to the mixer from both frequency sources must be extremely loose so that the act of mixing the frequencies does not significantly affect the tuning of the respective circuits. The precision tuning dial of the vfo is adjusted until an audio beat note is detected and heard in the earphones. The vfo is further adjusted until a zero beat results. The adjustment region of the tuning dial in which no signal can be heard is approximately 40 cps wide, 20 cycles on each side of the true zero beat at the center. The true zero beat, which occurs when the v-f-o frequency exactly equals the unknown frequency, must be interpolated as the halfway point between those dial settings at which the operator can just hear an audible note, which occurs at approximately 20 cps for the average person. By this method, an experienced operator can match the two frequencies to within 1 or 2 cps when no other sound but the beat notes can be detected. However, since


Figure 2-88. Sysfem for measuring crystal frequencias aurally with heterodyne frequency meter
there is usually some noise or hum in a heterodyne frequency meter which will wax and wane with a slow beat note, it is often possible to detect directly beat frequencies of less than 1 cycle per second. This is more likely to be possible when detecting a beat note between two audio signals than between two radio signals, since the audio circuits of a radio-frequency vfo are less likely to respond to the extremely low modulation frequencies than are the circuits of an audio-range interpolation oscillator.
2-126. With the use of a tuning fork, resonant, for example, at 256 cps , the vfo can be adjusted to produce $256-\mathrm{cps}$ audio outputs on each side of the null region. That the heterodyne meter is producing exactly 256 cps can be detected by the zero beat between the tuning-fork vibrations and the audio note from the earphones. The use of the tuning fork permits a more precise determination of equal audio frequencies on each side of the r-f-circuit zero beat, the dial point of which will be the exact center between the two 256 cps beat-note settings. The frequency of the vfo at the zero-beat dial setting is to be interpolated from previous calibrations of the vfo.
2-127. The nearest crystal-standard check point on each side of the measured dial setting should be rechecked against the appropriate harmonic from the frequency standard, either immediately before or immediately after the measurement of the unknown frequency is made. The radio frequency corresponding to the measured dial setting is then interpolated between the two adjacent check points by assuming that the differences in frequency are in the same ratio as the differences

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between the respective dial settings. For example, if the measured dial setting is exactly one-half the distance between the dial settings corresponding to two known harmonies of the standard, then the measured frequency lies halfway between the two harmonics.
2-128. In calibrating the frequency meter against the standard, the output from the standard is coupled to the r-f mixer, the vfo is adjusted for a zero beat, and the dial setting at the center of the null region is determined in exactly the same way as when measuring an unknown frequency. The fact that the frequency in this case is known to equal a standard harmonic permits the measured dial setting to be calibrated as the dial point corresponding to the given frequency. In using the frequency standard in calibrating the heterodyne meter, or in any other frequency-measuring use, care should always be taken that the standard is given sufficient time to reach its equilibrium operating temperature. At least one hour, and preferably two hours, depending upon the precision required, should be allowed for the unit to warm up after a period of inoperation. If frequently used, the standard should be energized continuously throughout its lifetime. The frequency standard used with the heterodyne frequency meter need not be of top precision. A stability of 1 part in $10^{5}$ is sufficient, since greater accuracy than this generally cannot be achieved in correlating and interpolating the radio-frequency dial settings.

## Frequency-Reading Counter System

2-129. The system shown in figure $2-89$ employing a direct-reading frequency counter is largely selfexplanatory. The frequency standard is employed to time the counting intervals. The r-f amplifier may be required, since the input voltage to the counter usually must be on the order of 1 or more volts rms-a voltage level requiring a closer coupling to the CI meter circuit than should be permitted. The accuracy of the counter readings can be no greater than the number of significant digits shown on the counter scale makes possible. If six digits are shown, the maximum theoretical accuracy of 1 part in the 6 -digit integer indicated can be assumed if the possible error introduced by the timing frequency standard is very small by comparison and the counting circuit can be depended upon not to skip a count. If the error introduced by the frequency standard is on the same order as the limitations of the counting circurt, the total tolerance for error must be the sum of the tolerances of the two error sources. The use of an r-f amplifier reduces the possibility of
a random counting error, particularly if the amplifier is equipped with an a-g-c circuit to maintain the output amplitude constant against variations in the input amplitude.

## VFO-Counter System

2-130. The measuring system shown in figure 2-90 employing a vfo and a counter is particularly useful for individual room-temperature tests of crystal units on a production line. The measuring method is fundamentally similar to the hetero-dyne-frequency-meter method illustrated in figure $2-88$. The principal difference is that the frequency of the vfo is not interpolated from a calibrated crystal-checked scale, but is read directly on the


Figure 2-89. System for measuring crystal frequencies visually with a direct-reading electranic counter


Figure 2-90. System for measuring crystal frequencies aurally with a variable frequency oscillator that is visually monifored by a direct-reading electronic counter
frequency-counter indicator. The system is especially useful when bringing a crystal plate by one process or another to a desired frequency. The vfo is set at the desired frequency and the crystal fabrication process is continued until the crystal can produce a zero beat in the phones or a speaker. When testing odd assortments of crystals which require that the v-f-o frequency be changed and checked often, the use of the frequency counter is a great time-saver over the crystal check-point method. Since a counter reading of the v-f-o frequency can be obtained almost instantly, the same counter can be shared by a large number of crystal testers simultaneously if placed in a position within view of all, and if the proper switching facilities are provided. If necessary, an r-f amplifier can be installed to boost the input to the counter.

## Double-Heterodyne System for Precision

## V-H-F Measurements

2-131. Figure 2-91 illustrates a typical system for obtaining relatively precise measurements in the $h$-f and v-h-f ranges. Two stages of heterodyning are employed. The first stage converts the unknown crystal frequency into another unknown frequency within the tuning range of the receiver. This second unknown signal, which in the figure is assumed to lie between 5 and 15 mc , is mixed in the second stage with the nearest harmonic combination of 100 kc and 10 ke to produce an unknown difference frequency in the audio range
lying between 0 and 5000 cps . The audio frequency is detected by the receiver (operated mew) and fed to the vertical plates of an oscilloscope. To the horizontal plates of the oscilloscope is fed the audio output of the interpolation oscillator, whose frequency is adjusted until a reasonably stationary ellipse is obtained on the scope. At this point it can be assumed that the frequency of the interpolation oscillator is equal to the frequency of the receiver output. As the name implies, the interpolation oscillator frequency is determined by interpolation between adjacent calibrated check points. Adjustment of the interpolation oscillator to match the receiver output with the aid of an oscilloscope permits a more accurate measurement than if the measurement is performed aurally with the aid of a loudspeaker or earphones.
2-132. If the unknown frequency in each of the two stages of heterodyning is greater than the respective standard with which it is mixed, the original unknown can be computed as the sum of the mixing standards and the interpolation-oscillator frequency. In general, the unknown input frequency of either stage will be equal to the respective harmonic standard with which it is mixed plus or minus the resulting difference frequency. The initial frequency is computed by starting with the final heterodyne stage in which the difference frequency is directly measured. Because this directly measured frequency is in the low


Figure 2-91. Sysfem, employing a heferodyne converter, for measuring h-f and v-h-f crysfal frequencies visually with an oscilloscope and a-f inferpolation oscillator
audio range, it represents a very small percentage of the whole, so that the errors made in interpolating its value can usually be considered negligible in estimating the total frequency. The tolerances to be allowed in the measured value of the crystal frequency are essentially the same as those of the $100-\mathrm{kc}$ frequency standard.

## Government Inspection System for Room-Temperature Crystal Tests

2-133. Figure $2-92$ shows by block diagram a general system for testing crystal frequencies as recommended for U. S. Government inspection tests. The system is essentially the same as that described in the foregoing paragraph and illustrated in figure 2-91. In place of the first heterodyne stage of figure 2-91, figure $2-92$ shows a frequency divider. In an actual inspection test, if the frequency under test must be reduced, either a divider or a heterodyne converter can be used, according to the facilities available. The loudspeaker in figure 2-92 is used as an aid in identifying the particular harmonic being mixed with the frequency under test and in correlating the secondary frequency standard against WWV. If the tuning of the crystal test set is adjusted slightly so that the crystal frequency increases, the rise or fall in the pitch of the speaker signal will indicate whether the test frequency is, respectively,
higher or lower than the mixing harmonic. If multivibrator dividers are used, each stage should be tuned separately to lock with the control frequency, as indicated by a sharp peak on the lock indicating meter.

## Government Imspection System for Temperature-Run Crystol Tests

2-134. Figure 2-93 shows a generalized block diagram of the system recommended for U. S. Government inspection tests of crystal units when the operating temperature is made to vary over its specified range. Insofar as the instantaneous measurements of the crystal frequency is concerned, using the occilloscope and interpolation oscillator, the system is exactly the same as that described in the previous paragraph for roomtemperature measurements. The additional features are the two recording circuits-one for recording the frequency deviation vs the temperature, the other for recording the effective-resistance deviation vs the temperature. The same audio output from the receiver that can be applied to the oscilloscope is applied to the input of the direct-reading low-frequency meter. The meter converts the audio input into a direct current proportional to the frequency. The d-c control signal, in turn, operates the frequency-deviation indicator of the meter and the stylus of the graphical


Figure 2-92. System recommended for Government inspection measurements of crystal frequencies af room temperature. The measurements are made visually with the ascilloscope and interpolation oscillator. The speaker is used principally as an aid in determining whether the erystal frequency under fest is greater or less than the standord harmonic
recorder. The variations in the control current are thus indicated as deviations in the frequency as the test proceeds through the full temperature run. Similarly, the d-c grid current of the crystal test set is used as a control current to indicate fluctuations in the effective resistance of the test crystal unit. This current directly, or through a d-c amplifier, controls the stylus of the effectiveresistance graphical recorder. During the tests, the rate of change in temperature must be under control so that its value at any point in a recording can be interpolated accurately.

## Frequency Measuring System of WADC

$2-135$. Figure $2-94$ shows by block diagram the specific system of equipment used at Wright Air Development Center for testing preproduction crystal units. The fundamental system is the same as that shown in figure 2-93. The equipments used are among those mentioned as representative units in the equipment descriptions of paragraphs 2-67 through 2-123.

## PROCEDURE FOR CORRELATING TEST EQUIPMENT WITH STANDARDS

2-136. Before the actual testing of a crystal unit begins, the various reference standards must be correlated with the primary standards, and the indicators and recorders must be correlated with
the reference standards. In the Inspection Manual for Crystal Units, Quartz, the Armed Services Electro-Standards Agency, Fort Monmouth, N. J., recommends a general correlation procedure to be followed by crystal-unit manufacturers. The measuring system is presumed to include the types of equipment indicated in figures 2-92 and 2-93.
2-137. To illustrate each step, let us suppose that we are a manufacturer with the same test facilities as those used at WADC, shown in figure 2-94. Further, let it be supposed that it is planned to test a 12 -mc CR-18/U crystal unit over its operating temperature range. Also, assume that the test location is within ground-wave range of Station WWV and that all other necessary standards and accessories are available. With these suppositions, we shall briefly outline the steps to take in following the ASESA recommended correlation procedures.

## Correlation of Load-Capacitance Dial

2-138. The calibration of a load-capacitance dial does not require frequent correlation against a standard precision capacitor, but the check is necessary when a Cl meter is first installed and whenever precise values of load capacitance are required.
a. If the Cl meter is to be used for a wide variety of measurements, it would be advantageous to


Figure 2-93. Sysfem recommended for Government inspection measurements of crystal frequencies over the operating temperafure range. The instantaneous frequency-measuring system is the same as that shown in figure 2-80 for room temperature measurements. Added are the frequency-deviation recarder circuit and the effective-resistance recorder circuit


Figure 2-94. System and equipment used of Wright Air Development Center to perform tests of preproduction crystal units
prepare a graphical chart in which the dial settings are plotted against capacitance over the entire adjustable range. If the CI meter is to be used only in measurements of crystal units which, for parallel-mode operation, require no more than one or two standard values of load capacitance, the capacitance dial need be correlated only at the one or two operating positions.
b. For the $12-\mathrm{mc}$ CR-18/U crystal unit we have chosen as an example, the standard reference test set is CI Meter TS-330/TSM. The reference test load capacitance is specified to be $32 \mu \mu \mathrm{f}$. Let it be assumed that the load-capacitance dials of both the primary standard and the reference test sets are to be calibrated at this one position. The prom cedure to use is the same for each set.
c. Two procedures are possible. If the precision capacitor being used as a primary standard has a value equal to $32 \mu \mu \mathrm{f}$, the correlation can proceed by direct substitution. If the precision capacitor is variable, but all capacitance values are greater than $32 \mu \mu \mathrm{f}$, the correlation depends upon matching the test-set load capacitance with a $32-\mu \mu f$ difference between two values of the capacitance standard. The latter method is generally the more accurate, and also faster if a variable capacitor is to be calibrated over its entire range.
d. Direct-Substitution Method. Connect the standard $32-\mu \mu \mathrm{f}$ capacitor, with leads as short as possible, across the crystal socket in the test set. With the test set tuned to the lowest frequency band and switched to series-resonance operation (internal load capacitor shorted out), turn the set on and, after warm up, check the operating frequency by mixing with crystal-controlled 10 -kc harmonics and detecting the audio beat in the receiver speaker. Adjust the tuning capacitor (not the precision capacitor) of the test set until a zero beat is obtained. Remove the precision capacitor and connect a shorting wire across the crystal socket of the test set. Switch the test set to parallel-resonance operation (load capacitor connected into circuit) and adjust the load capacitor until a zero beat is obtained with the same 10 -kc harmonic as before. The dial reading of the load capacitor, when adjusted from a clockwise direction, can be recorded as the $32-\mu \mu \mathrm{f}$ position. Note that once the test-set tuning capacitor has been adjusted to a zero beat with the standard capacitor connocted in the circnit, its adjustment is not changed while the load capacitor is connected in the circuit. The above test should permit an operating accuracy for the load capacitance within 0.2 or $0.3 \mu \mu \mathrm{f}$, provided the standard capacitor is, itsolf, accurate to within $0.1 \mu \mu \mathrm{f}$. If a more accur-


Figure 2-95. Constant parallel-capacitance method for calibration of load capacitance dial
ate measurement is desired, a $Q$ meter should be employed in a manner similar to the test illustrated in figure $2-95$, except that in using a $32-\mu \mu \mathrm{f}$ standard, the capacitors are connected in the Qmeter circuit one at a time, rather than in parallel.
e. Constant Parallel-Capacitance Method. When the lowest value of the precision capacitor is greater than the capacitance to be calibrated, as would be the case if using the G.R. 729-D precision capacitor, a Q meter and a crystal-controlled 400 -ke frequency generator can be employed in the manner shown in figure 2-95. Use AWG \#12 solid copper wire, supported on 2 -inch centers, in connecting the capacitors to the $Q$ meter, keeping leads as short as possible. Lead A connects to the side of the crystal socket making direct electrical contact to one plate of the load capacitor. Lead B connects to the other side of the load capacitor. (Electrical connection to the other plate of the load capacitor can normally be made through one of the rivets that holds the crystal socket in place.) Adjust the precision capacitor to $200 \mu \mu \mathrm{f}$. At the beginning of the test, all leads should be connected except lead A. However, lead A should have the same physical relationship with lead B and with ground as will exist when the load capacitor is connected in the circuit. With the frequency generator driving the circuit, the standard inductance is tuned to resonance with the $200-\mu \mu \mathrm{f}$ standard capacitance (plus the distributed wiring capacitance), as indicated by the Q meter. With the standard inductance kept constant, the precision capacitance can be reduced $32 \mu \mu \mathrm{f}$ to 168 $\mu \mu f$. Then by connecting lead $A$, the test-set load capacitor is connected in parallel with the precision capacitor. By adjusting the load-capacitor dial until the $Q$ meter again indicates resonance, it can be assumed that the $32 \mu \mu$ f subtracted from
the circuit has now been restored. Record the load-capacitor dial setting, reached with a clockwise rotation, as the $32-\mu \mu \mathrm{f}$ position. The foregoing procedure should permit an operating accuracy of plus or minus $0.1 \mu \mu \mathrm{f}$ in the value of the test-set load capacitance.

## Correlation of Reference Calibrated Resistors

2-139. The reference calibrated resistors, which are used as substitutes for the effective resistance of crystal units when adjusting the drive level and when measuring crystal resistance, do not require frequent checking, but should be measured with a standard r-f bridge before being used for an extensive series of tests.
a. The measured value of the resistor should equal the calibrated value within plus or minus 1 per cent.
b. In testing the 12 -mc CR-18/U taken as an example, a calibrated 25 -ohm r-f resistor is required to represent the maximum permissible effective resistance. If a standard CI Meter TS$330 /$ TSM is being used in making the test, a set of calibrated decade resistors with appropriate circuit-control switches is included as a component part of the CI-meter circuit design. When measured with an accurate r-f bridge, such as Navy Type No. 69904, the observed value should lie between 24.75 and 25.25 ohms.

## Correlation of Reference Crystal Test Set

2-140. Correlation of a manufacturer's reference test set with the Government standard set is performed by, or under the surveillance of, a Government inspector.
a. At least three crystal units of the type to be tested are selected.
b. The frequency and effective resistance of each crystal unit are measured and recorded under standard test conditions when the crystal unit is connected in the primary test set standard. The same measurements are repeated and recorded with the crystal unit connected in the reference test set.
c. The frequency correlation is satisfactory if the frequency of each crystai unit, as measured in the standard test set, does not differ from the frequency of the same crystal unit, as measured in the reference set, by more than plus or minus 10 per cent of the nominal frequency tolerance. (For the $12-\mathrm{mc}$ CR-18/U, the specified nominal frequency tolerance is plus or minus 0.005 per cent of 12 mc , which is equal to plus or minus 600 cps. 10 per cent of 600 cps requires that the frequency of each 12 -mc CR-18/U unit, as measured
with the reference test set, must not differ by more than plus or minus 60 cps from the frequency of the same unit when measured with the primary standard test set.)
d. The effective-resistance correlation is satisfactory if the effective resistance of each crystal unit, as measured in the standard test set, does not differ from the effective resistance of the same crystal unit, as measured in the reference test set, by more than plus or minus 5 per cent of the standard-test-set measured value. (For example, suppose the effective-resistance value of the CR18/U crystal unit, as measured with the primary standard test set ; 10 ohms. The measurement of the resistance of the same crystal unit in the reference test set must lie between 9.5 and 10.5 ohms, if the correlation is to be assumed satisfactory.)
e. In the event that correlation cannot be achieved, the bureau or service concerned is to be notified.

## Correlation of Secondary Frequency Standard

2-141. The secondary standard must be checked against the primary before each series of measurements, and at least three times during any day following a warm-up period.
a. Turn on the standard $(0-76 / \mathrm{U}$ in our example) and allow to warm up for at least one hour. If the equipment is to be used regularly, the frequency standard should be kept in continuous operation throughout its lifetime.
b. Tune radio receiver to highest usable groundwave frequency from Station WWV (25, 20, 15, 10,5 , or 2.5 mc ), and adjust tuning dial for maximum carrier level.
c. Feed output from standard to receiver antenna input, with receiver adjusted for mow operation, and audio output applied to speaker.
d. Adjust fine frequency control on standard to center of zero-beat region as heard in speaker during 30 -second $\mathrm{C}-\mathrm{W}$ broadcast intervals of WWV. (If it is possible to detect the zero beat directly by the waxing and waning of interpola-tion-oscillator noise, the correlation period is not limited to the 30 -second C-W intervals. If the noise modulation is not audible and greater accuracy is desired, let interpolation oscillator warm up, then set at a very, very low frequency. Feed output of oscillator to horizontal deflection plates of oscilloscope, and output of receiver to vertical plates. Adjust fine tuning of standard to obtain a stationary elliptical pattern on oscilloscope on both sides of zero beat. Zero beat should coincide with fine tuning point of standard exactly midway between points of stationary patterns.)

## Correlation of Interpolation Oscillator

2-142. The interpolation oscillator should be correlated at the beginning of each series of experiments after permitting at least one-half hour warm up.
a. Switch on 10 -ke harmonic generator under control of $100-\mathrm{kc}$ standard.
b. Switch receiver to lowest frequency band, mew operation.
c. Adjust receiver selectivity to maximum bandwidth reception.
d. Tune receiver to any frequency midway between two adjacent 10 -ke harmonics.
e. Feed audio difference frequency, 10 kc , of the two received signals to vertical plates of oscilloscope.
f. After warm up, adjust interpolation-oscillator tuning dial to 5000 cps , and feed output to horizontal deflection plates of oscilloscope.
g. Adjust calibration controls of interpolation oscillator according to instruction manual until a stationary lissajous pattern is obtained on oscilloscope screen. The pattern should indicate two vertical cycles for each horizontal cycle. With the deflection voltages properly phased, this "two-toone" pattern will resemble a horizontal figure 8.
h. With the position of the calibration control recorded, the interpolation oscillator will be calibrated for 5000 cps .
i. If the interpolation oscillator is tuned to 3333 cps and adjusted for a stationary "three-to-one" pattern, a calibrated check point at this frequency can be recorded. Similarly, stationary patterns in any ratio from $4: 1$ to $20: 1$ can provide calibrated check points at the respective frequencies between 2500 cps and 500 cps . At frequencies below 500 cps, the calibration points can be obtained by correlation with the $60-\mathrm{cps}$ line voltage. Federal regulations require that a commercial 60 -cps power frequency be accurate within $\pm 1 / 2 \mathrm{cps}$. Since the $60-\mathrm{cps}$ reference can be readily obtained by adjustment of the appropriate oscilloscope control, this calibrating method is quite convenient where great accuracy is not essential. Otherwise, the low a-f check points should be obtained by using as standards the $440-\mathrm{cps}$ and $600-\mathrm{cps}$ signals of Station WWV-ground- or sky-wave r-f reception.
j. When using the interpolation oscillator to correlate the frequency-deviation meter, maximum accuracy is ensured if the interpolation oscillator is specifically correlated at the harmonic check point nearest the frequency corresponding to the maximum nominal frequency tolerance of the crystal unit to be tested.
k. In the case of the 12 -mc CR-18/U crystal unit, a crystal of exactly the right operating frequency will produce a zero beat when matched against the nearest harmonic of the frequency standard-assuming the test standards as shown in figure 2-82 are available. With a nominal frequency tolerance of plus or minus 600 cps at any temperature in the operating range, a crystal unit at the edge of the tolerance limit will produce a $600-\mathrm{cps}$ receiver output to be fed to the deviationfrequency meter. The two nearest 10 -kc check points for the interpolation oscillator are the $16: 1$ pattern at 625 cps and the $17: 1$ pattern at 588.2 cps. Each of these points should be calibrated. (Normally, if a precision oscillator, such as the General Radio Interpolation Oscillator, is used, special correlation adjustments for each frequency are not necessary.)

1. An alternative method, ensuring even greater accuracy in this particular example, is to calibrate the $600-\mathrm{cps}$ setting directly against the $600-\mathrm{cps}$ modulation standard of Station WWV.

## Correlation of Frequency-Deviation Mefer and Recorder

2-143. The frequency-deviation meter and recorder should be correlated at the beginning of each series of tests.
a. Tune interpolation oscillator to the frequency corresponding to the maximum permissible tolerance for the crystal unit being tested. (For the $12-\mathrm{mc}$ CR-18/U, this means funing the interpolation oscillator to 600 cps . The dial setting can be interpolated between the calibrated points of 588.2 and 625 cps . For this particular frequency, the 10 th harmonic of 60 cps , we might be tempted. to check the dial setting against the $60-\mathrm{cps}$ line voltage for a stationary 10:1 pattern. This can readily be done with the normal oscilloscope frontpanel controls. But it should be remembered that since the line frequency of 60 cps is not guaranteed beyond $\pm 1 / 2 \mathrm{cps}$, a calibration at 600 cps can result in an error of $\pm 5 \mathrm{cps}$.)
b. Feed output of interpolation oscillator to input of frequency-deviation meter.
c. With frequency-deviation meter and recorder placed in operation, adjust calibration control of meter until meter indicates same reading as interpolation oscillator. (For the facilities and crystal unit taken as an example, the H-P 500A meter will be switched to the 0-to-1-ke band and the calibration control adjusted so that the meter reads 600 cps .)
d. Adjust sensitivity of frequency-deviation recorder to provide approximately full-scale reading for interpolation oscillator frequency. (For the
meter d-c output corresponding to a $600-\mathrm{cps}$ input signal, the deflection of the recorder stylus should be adjusted to give a convenient large-amplitude reading calibrated to read 600 cps .)
e. The correlation of the frequency-deviation circuit is completed, so the interpolation-oscillator is disconnected from the frequency meter, and the output circuit of the receiver is connected in its place.

## Correlation of Effective-Resistance Recorder

$2-144$. The stylus of the effective-resistance recorder is to be under the control of the d-c grid current of the reference crystal test set. The grid circuit of the test set must be modified so that the grid current passes through the input circuit of the recorder, or through the input circuit of an intermediary d-c amplifier. The resistance of the input circuit should not increase the total gridleak resistance by more than 5 per cent. Otherwise, make some compensating change in the original grid resistance. If not already provided by the test set, a grid current meter and a variable resistor in parallel with it should be available to be connected in series with the grid-leak resistance. The variable resistor, normally 0 to 1000 ohms plus or minus 10 per cent, is used to control effectively the sensitivity of the grid meter. Once the grid meter sensitivity has been set, it must not be changed during the remainder of the correlation procedure.
a. If the maximum expected grid current (defined in step i) is insufficient to provide a fullamplitude deflection of the recorder stylus, a d-c amplifier must be inserted to boost the input to the recorder. (To avoid confusion, we shall consider only the recorder input circuit. The correlation procedure is not fundamentally affected if, in practice, a d-c amplifier is employed. The amplifier need only be interpreted as being the input circuit and sensitivity control of the recorder.)
b. If the maximum expected grid current is more than sufficient to provide a full-scale deflection of the recorder arm, the recorder sensitivity control should be adjusted to a lower value. If the sensitivity control is not adjustable to a relatively low level, it can be made so by shunting the recorder input with a suitable variable resistance. Under no circumstances should an attempt be made to match the sensitivity of the recorder by adjustments of the grid current. The grid-leak current is effectively standardized for each value of effective resistance for each Military Standard crystal unit and nominal frequency. This is because a standard reference circuit is employed that is designed with a fixed grid-leak resistance,
and it is operated with a standardized drive adjustment. All of which means that an approximately predetermined grid current will flow for a given frequency and effective resistance. An increase in the grid resistance, for example, would mean, that for the same drive adjustment procedure, the grid bias would be greater, and hence the harmonic distortion in the output would increase, with a consequent increase in the instability. (Where the nomenclature used in the instruction manual and on the front panel of a Cl meter designates the sensitivity control of the grid-current meter to be a "grid-current control," the reader should not be misled into thinking that an adjustment of the percentage of grid current flowing through the meter has a significant effect upon the total grid current.)
c. It is to be assumed at this point that the grid circuit is properly connected to the recorder control circuit, that the maximum expected grid current is ample to permit a full scale deflection of the stylus, and that the total grid-leak resistance has not been significantly changed by the insertion of the recorder input resistance.
d. Adjust the reference crystal test circuit that is to be used in testing the crystal unit to the proper drive level, as defined by the applicable Military Standard drive adjustment procedure. (For testing the $12-\mathrm{mc}$ CR-18/U in our example, the reference set will be a CI Meter TS-330/TSM, and the appropriate drive adjustment procedure, defined by Military Specification MLL-C-3098B, is described in paragraph 2-60 of this Handbook. In step $b$ of the drive adjustment procedure, the correct decade resistor value is 13 ohms, since the 12 -me CR-18/U is used as a non-temperature controlled unit. In steps $c$ and $d$ of the drive adjustment procedure, the correct test frequency and crystal current, respectively, for the sample CR$18 / \mathrm{U}$ are 12 mc and 20 ma .)
e. After the drive adjustment is completed, a calibrated reference resistor is selected whose value is equal to the maximum permissible for the particular crystal unit to be tested. This resistor is to be connected in the test circuit to simulate the resonance impedance of a series-mode crystal unit, or that of a parallel-mode crystal unit in series with its load capacitance. In other words, with the resistor substituted in the circuit in place of the crystal unit, or the crystal-unit-loadcapacitor combination, and with the resulting LCR circuit tuned to the nominal operating frequency of the crystal unit, the amplitude of oscillation should approximately equal the amplitude
that would exist if a crystal unit of maximum effective resistance were connected in the circuit. (For example, the maximum permissible resistance of the 12 mc CR-18/U is 25 ohms. The calibrated resistor of this value will be the decade resistance of the TS- 330 /TSM test circuit. So to perform this step, we need only switch from the 13 -ohm resistor used in the drive adjustment to the 25 -ohm resistor. The test set remains in the "calibrate" position.)
f. Tune the test set to the nominal frequency of the crystal unit to be tested. (In our particular example, the test set is assumed to have been tuned to the nominal frequency of 12 mc during the drive adjustment procedure. We now make a more exact tuning adjustment by mixing the output of the CI meter with the output of the stand-ard-controlled 1 -me harmonic generator. When the test set is correctly tuned, a zero beat will be obtained in the receiver speaker resulting from the mixture of the 12th harmonic of the generator with the test-set output.)
g. Adjust the grid-current meter sensitivity to give a convenient low-scale reading. Mark the position of the sensitivity control and record the grid current. This represents the minimum permissible grid current for the type of crystal unit and frequency under test, since it corresponds to the maximum permissible effective resistance.
$h$. Now adjust the recorder and calibrate the graph for a reading of the maximum effective resistance. When correlating the position of the recorder stylus with the effective-resistance scale of the graph, the position of the stylus when the grid current is minimum must be adjusted to give a reading corresponding to the maximum permissible resistance ( 25 ohms for our sample CR18/U).
i. The maximum expected grid current can be approximated by replacing the calibrating resistor used in making the maximum-resistance correlation with one having a value representing the minimum expected effective resistance. (In our CR-18/U example, we can assume a minimum effective resistance of 4 ohms .) The resulting grid current we define as the maximum expected grid current. This is not the current indicated in the grid-current meter, unless the meter sensitivity is turned to its maximum position; even then the reading is only approximate. There is no need to measure the maximum expected grid current unless the value is required to determine whether the recorder sensitivity will need boosting or attenuating.
j. With the sensitivity control of the grid meter adjusted to its previously marked position, record the current reading. This reading will serve as the meter indication that the maximum expected grid current is flowing. It is valid only for the given adjustment of the meter sensitivity. With the meter indicating the maximum expected grid current, adjust the sensitivity of the stylus deflection for a full amplitude swing. Make this adjustment and calibrate the corresponding reading on the recorder graph, to signify an effective resistance equal to the minimum expected value (4 ohms for our sample CR-18/U).
k. The grid-current meter readings and calibrating adjustments can be recorded and used to speed similar correlation procedures for future crystal tests.

## Correlation of Temperature-Measurement Controls (General)

2-145. The details of the procedure for correlating the different reference devices used to control the crystal temperature measurements can be quite varied. In general, four types of measurements or specified test conditions must be correlated with the temperature standards. The crystal unit must start the temperature run at the correct lower temperature limit. Heat must be supplied at a rate sufficient to permit the proper intervals between temperature readings and at a dependable rate so that the length of a temperature run is predictable within plus or minus 5 per cent. The temperature of the crystal unit must be indicated at all times. And finally, the heater must be shut off at the upper temperature limit at the end of the run. The exact methods used to accomplish the above ends vary considerably, depending upon such factors as whether the measurements are for laboratory or production line; whether the measurements are being made for multiple lots or for just one crystal unit at a time; whether a permanent recording of the measurements are being made and, if so, of what type; whether readings are being indicated continuously or only at intervals; whether exact measurements are being made or whether the tests are of the go, no-go type. Even when similar types of tests are being made, the methods vary from laboratory to laboratory and manufacturer to manufacturer, and even from one location to another in the same organization. In spite of the variety encountered in the methods used in measuring and controlling the temperature, the fundamental correlation procedure is applicable generally and should be observed.

Section II

## Correlation of Pyrometer

2-146. The pyrometer is to be correlated at least once each month that it is being used.
a. Correlate at $0^{\circ} \mathrm{C}$ by immersing sensing element (moisture protected) in ice water, the water having been distilled.
b. Correlate at boiling point of distilled water making allowance for elevation above sea level, or, if available, exact barometric pressure at time of test. Care should be taken that position of pyrometer sensing element is not in temperature gradient near heat source, nor at liquid surface.
c. The temperature measurements are not so critical that both the freezing and boiling temperatures of distilled water need to be correlated, but for accurate measurements both correlations should be made.
d. If a thermocouple sensing element is used, true accuracy requires that the temperature of the constant-temperature junction be maintained at a known value throughout all measurements. In other words, it should be thermostatically controlled. Also, the difference in temperature between the two junctions should be as large as practicable. In practice, the temperature of one junction follows the variations in the temperature of the surrounding air; hence, when the temperature of the sensing junction approaches room values, the corresponding indication of the pyrometer is quite unreliable. However, in a temper-ature-run test the correlation of the recorders is less dependent upon the absolute indications of the pyrometer in the middle of the run, than upon the more accurate indications at the limits of the range, and upon the constancy at which the rats of temperature change can be maintained.
e. If a thermistor sensing element is used, the temperature correlation can be more dependable, provided the pyrometer voltage source is stable.

## Correlation of Cold Box Thermometer

2-147. The cold box thermometer should be correlated with the reference pyrometer once each month.
a. Place dummy crystal unit of pyrometer in cold box in a position simulating that of a normal crystal unit. (In our example, the dummy crystal unit should be contained in an HC-6/U holder, in order to approach as nearly as possible the physical characteristics of the CR-18/U crystal unit.)
b. Adjust temperature of cold box to lower limit of specified temperature range of crystal unit to be tested, measuring the temperature with the pyrometer. (For our test CR-18/U, the lower temperature limit is minus $55^{\circ} \mathrm{C}$.)
c. With thermometer inserted in cold box with pyrometer, allow one-half hour for box and temperature instruments to reach thermal equilibrium.
d. Record difference between readings of pyrometer and thermometer, for use in correcting thermometer reading in later measurements of cold box limit temperature.

## Correlation of Heater

## 2-148. Correlate the heater as follows:

a. Cool dummy crystal unit in cold box until it reaches thermal equilibrium at specified low temperature limit for crystal unit to be tested. Temperature is to be read by pyrometer with sensing element attached to crystal plate in dummy unit.
b. Mount dummy crystal unit in heater and begin test temperature run. As read on pyrometer with sensing element attached to quartz plate, carefully measure time required for temperature to reach upper limit. Adjust heater thermostat to cut off power as upper limit is reached $\left(90^{\circ} \mathrm{C}\right.$ in the case of the CR-18/U example).
c. The heater power is adjusted, if necessary, to ensure that the rate of temperature change meets the specified test conditions. (For the CR$18 / \mathrm{U}$ unit in our example, the test conditions specified in Method A must be met. See paragraph 2-36a.)
d. If the periods of three consecutive temperature runs, as specified in steps a and b, meeting the specified test conditions without adjustments of the heater controls, are within plus or minus 10 per cent of each other, the correlation is satisfactory.

## Correlation of Recorders with Temperature <br> Renge

$2-149$. The correlation of the recorder with the temperature range will depend upon the facilities available and the degree of accuracy desired.
a. If special facilities are not available, the correlation of the graphical recordings of the frequency and effective resistance with the operating temperature are normally made at only the two temperature limits, which can manually be made to coincide with the starting and stopping of the recorders. If desired, manual calibrations can be obtained at a mid-temperature by observing the pyrometer scale.
b. With special test facilities, such as the modified temperature recorder indicated in figure 2-94, temperature calibrating pulses can be transmitted to the graphical recorders at any desired temperature interval. These pulses are correlated with,
and adjusted for control by, the dummy crystal unit pyrometer circuit. The temperature recorder indicated in figure $2-94$ is modified to provide a temperature-indicator pulse to the frequency and resistance recorders at every $5^{\circ} \mathrm{C}$ change in temperature of the dummy crystal unit.

## Correlation of Vibrotiom Mechine

$2-150$. The vibration machine must be correlated for amplitude and frequency at least once each month. With machine in operation, draw lines to indicate amplitude on marking surface held at right angles to direction of vibration. Check amplitude with inch scale at different frequencies to ensure that Military Specifications are met over vibration range. See paragraph 2-48.

## MEASURING AND RECORDING FREQUENCY AND EFFECTIVE RESISTANCE

2-151. Assume that the equipment in figure 2-94 is available and that all correlations have been made prerequisite for measuring and recording the frequency and effective resistance of a 12 -mc CR-18/U crystal unit over its operating temperature range.
a. Adjust drive of reference crystal test set TS-330/TSM according to correct drive adjustment procedure as specified in paragraph 2-60.
b. Adjust TS-330/TSM for operation of CR18/U type unit at 12 mc according to instructions in manufacturer's manual, or in USAF Technical Order No. 35TS330-5, or in Signal Corps Technical Manual No. TM 11-5051.
[Briefly, the load capacitance is set at $32 \mu \mu \mathrm{f}$, but is not immediately connected into the circuit. Insert a sample $12-\mathrm{mc}$ CR-18/U crystal unit in the crystal socket. (A sample is inserted since presumably the unit to be tested is being cooled in the cold box.) With the circuit switched for seriesmode operation, adjust the tuning capacitor until resonance is indicated by a grid-current peak. We assume that the grid-current meter sensitivity has been adjusted for a suitable reading. Do not change the drive adjustment (the crystal-current control). The Military Standard drive adjustment procedures can be assumed to supersede possible
contrary instructions in operating manuals. Now, switch in the load capacitance, and the circuit is ready for operation.

If desired, since the $12-\mathrm{kc}$ harmonic standard is available to ensure an accurate tuning to the nominal frequency, the circuit could be precisely tuned during the drive adjustment procedure, and the only adjustments necessary would be to disconnect the drive-adjustment resistor from the circuit, switch in the 32 -ohm load capacitor, and then insert the crystal unit in its socket when the test is ready to begin.]
c. With sample crystal unit in operation, feed signal from test set through switching panel to receiver input.
d. Feed harmonic output of 1-me standardcontrolled generator to receiver input.
e. Tune receiver, mow operation, to receive nominal 12 -mc signal. Beat note, if fed to speaker, indicates difference between test crystal frequency and 12th harmonic of 1 -mc standard-controlled generator.
f. Select range of frequency-deviation meter that corresponds to the maximum permissible frequency deviation for the crystal unit being tested ( 600 cps in this case, and the proper meter range would be that from 0 to 1000 cps ).
g. Feed audio output from receiver to fre-quency-deviation meter.
$h$. Feed output of frequency-deviation meter to input of frequency-deviation recorder.
i. Feed grid current from crystal test set to input of effective-resistance recorder.
j. Feed output of temperature recorder to tem-perature-pulse inputs of frequency-deviation and effective-resistance recorders.
k. From cold box take test crystal unit and dummy crystal unit, both cooled to the low temperature limit and mounted in slug. Insert slug in oven.

1. Insert crystal pins, protruding from oven holder, in crystal socket of test set.
$m$. Turn on heater power and start temperature run.

## SECTION III-CRYSTAL HOLDERS

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## SECTION III-CRYSTAL HOLDERS

## INTRODUCTION

3-1. Section III contains all available descriptions of crystal holders now being used in, or recommended for use in, USAF equipments. The crystal holders described are divided into two groups, as defined in subparagraphs a and b below. Included with the Group-I Crystal Holders and following the technical data chart and description sheets are a table and description sheets giving the types of sockets suitable for use with Group-I Crystal Holders. At the end of Section III is a digest of Military Standard terms, tests, and procedures applicable to crystal holders meeting military specifications.
a. Group I includes those Military Standard crystal holders that are recommended for use in equipments of new design. These are the crystal holders assigned Joint Army-Navy-Air Force type number $\mathrm{HC}-\mathrm{X} / \mathrm{U}$, where X is either a one-digit
or a two-digit number. Except in the event of unusual or special requirements, the design engineer of erystal-controlled circuits for military equipment should consider only those crystal holders in Group I.
b. Group II includes the older types of crystal holders which are still widely used in current models of USAF radio equipments, but which are not recommended for use in military equipments of new design. These crystal holders are arranged in order of their USAF stock numbers, except for the addition of the prefix " $2100-$," which serves to identify the item as belonging to the USAF 16-F stock class. The information concerning the Group-II crystal holders is included primarily for the benefit of the crystal specialist or field engineer in the military. As a reference source of crystal holders, it may also prove helpful to design and research engineers.

TECHNICAL DATA CHART FOR GROUP-I MILITARY STANDARD CRYSTAL HOLDERS

| Type Number | Material | Base or Terminal Connection | Physical Dimensions (In.) |  |  | Crystal Units Part of |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | High | Wide | Thick |  |
| HC-5/U | plastic holder |  | $2^{21 / 4} 2$ | 119/32 | 1\%10 | $\begin{aligned} & \mathrm{CR}-15 / \mathrm{U},-16 / \mathrm{U},-29 / \mathrm{U}, \\ & -30 / \mathrm{U} \end{aligned}$ |
| HC-6/U | metallic holder | $\begin{aligned} & 2 \text { pins, } 1 \text { in in. } \mathrm{lg}, 0.050 \mathrm{in} . \text { dia, } \\ & 0.486 \mathrm{in} . c \text { to } c \end{aligned}$ | 1 | $23 / 32$ | 56 | CR-18/U, -19/U, -23/U, $-25 / \mathrm{U},-26 / \mathrm{U},-27 / \mathrm{U}$, $-28 / \mathrm{U},-32 / \mathrm{U},-33 / \mathrm{U}$, $-35 / \mathrm{U},-36 / \mathrm{U},-44 / \mathrm{U}$, $-45 / \mathrm{U},-46 / \mathrm{U},-47 / \mathrm{U}$, $-48 / \mathrm{U},-49 / \mathrm{U},-51 / \mathrm{U}$, $-52 / \mathrm{U},-53 / \mathrm{U},-54 / \mathrm{U}$ |
| HC-10/U | metallic holder | 2 sleeves, $3 / 14 \mathrm{in} . \lg , 1 / 4 \mathrm{in}$. dia | 11/6 | \% 16 | \% 7 | CR-24/U |
| $\mathrm{HC} 13 / \mathrm{U}$ | metallic holder | $\begin{aligned} & 2 \text { pins, } 1 / \mathrm{m} \text { in. } \mathrm{lg}, 0.050 \mathrm{in.} \mathrm{dia,} \\ & 0.486 \mathrm{in}, \mathrm{c} \text { to } \mathrm{c} \end{aligned}$ | $13 \% 6$ | $23_{32}$ | 7/16 | $\begin{aligned} & \mathrm{CR}-37 / \mathrm{U},-38 / \mathrm{U},-42 / \mathrm{U}, \\ & -50 / \mathrm{U} \end{aligned}$ |
| HC-14/U | metallic holder | 2 pins, $1 \%$ in. lg, 0.050 in. dia, 0.486 in. c to c | 11/46 | $24 / 52$ | \% 4 |  |
| HC-15/U | $\begin{aligned} & \text { electron } \\ & \text { tube } \\ & \text { (glass } \\ & \text { envelope) } \end{aligned}$ | std octal | 2\%/6 | 1\% $\%$ | 19 | CR-39/U, $-40 / \mathrm{U}$ |
| HC-16, U | ```electron tube (metallic envelope)``` | std octal | 2\% | 1\%\% | 17/46 | CR-43/U |
| HC-17/U | metallic bolder | 2 pins, $7 / 16 \mathrm{in} . \lg , 0.093 \mathrm{in}$. dia, 0.486 in. c to c | 1-3/16 | 23/32 | 5/16 | CR-58/U |
| HC-18/0 | metallie holder | 2 fexible leads, $1^{1 / 2} \mathrm{in} .1 \mathrm{lg}$ | 33/64* | $3 / 4$ | 5/32 | $\begin{gathered} \mathrm{CR}-55 / \mathrm{U},-56 / \mathrm{U},-59 / \mathrm{U}, \\ -60 / \mathrm{U},-61 / \mathrm{U} \end{gathered}$ |
| HC-21/U | metallic holder | 3 pins , 5\% in. lg, 0.156 in . dia | 2-21/32 | 1-19/32 | 1-19/32 | $\underset{-30 / \mathrm{U}}{\mathrm{CR}-15 / \mathrm{U},-16 / \mathrm{U},-29 / \mathrm{U},}$ |

* Not including fexible leads.


## CRYSTAL HOLDER HC-5/U



Figure 3-1. Crystal Holder HC-5/U

Section III

## Crystal Holders-Group 1

## FUNCTIONAL DESCRIPTION

A three-pin plastic holder used to mount lowfrequency quartz plates. It can be used at temperatures within the range of $-40^{\circ} \mathrm{C}$ to $+75^{\circ} \mathrm{C}$, but since the holder is designed for gasket sealing and has an inferior form factor compared with metal holders, it will operate best in equipments not intended to be subjected to below-freezing or extremely high temperatures, and in areas where the ambient humidity is not at a continuously high level.

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder: CR-15/U, $-16 / \mathrm{U},-29 / \mathrm{U}$, and $-30 / \mathrm{U}$
Sockets Used With Holder: See figure 3-14

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056B (16 Jan 53) ; MIL-H1056/1 (16 Jan 53)
Dimensions: See figure 3-1. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

## Materials:

| Item No. <br> (Fig. 3-1) | Description | Material | Qty |
| :---: | :---: | :---: | :---: |
| 1 | Pin | Nickel-silver radio tube pin E.3675, as made by American Brass Co, or equal | 3 |
| 2 | Base | Plastic: Resinox No. 7934, Melmac No. 6105, BM-7156, Durez No. 12708, or equal | 1 |
| 3 | Gasket | Buna S, per Spec MIL-R3065, 60-75 Shore A Durometer hardness |  |
| 4 | Cover | Same as for item 2 | 1 |
| 5 | Insert | Brass, per Spec QQ-B-611, comp B, $4 / 2$ hard | 4 |
| 6 | Phillips machine screw No. 2-56 NC-2 $\times 1 / 2 \mathrm{in} . \mathrm{lg}$ | Brass | 4 |

Special Requirements: None

## LOGISTICAL DATA

USAF Stock No.: $2100-2 \times H 51.1$
Status: Standard*
Date of Status:
Commercial Sources: See Appendix III.
Related Specifications, Standards, and Publications: See Appendix IV.
*Note: The proposed revision of Military Specification MIL-H-10056B deletes the plastic holder $\mathrm{HC}-5 / \mathrm{U}$ and substitutes the metal holder HC-21/U.

Section III<br>Crystal Holders-Group 1

## CRYSTAL HOLDER HC-6/U



Figure 3-2. Crystal Holder HC-6/U

## FUNCTIONAL DESCRIPTION

A lightweight, all-metal unit particularly suitable for use in either mobile or portable equipment and wherever crystal units may be subjected to severe conditions of moisture or mechanical shock. Several types of mounting are possible, but the most satisfactory, generally, is a plated crystal supported by two looped springs. This holder is designed for hermetic sealing and is dependable over a temperature range of $-55^{\circ} \mathrm{C}$ to $+90^{\circ} \mathrm{C}$ and higher.

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder: CR-18/U, $-19 / \mathrm{U},-23 / \mathrm{U},-25 / \mathrm{U},-26 / \mathrm{U},-27 / \mathrm{U},-28 / \mathrm{U}$, $-32 / \mathrm{U},-33 / \mathrm{U},-35 / \mathrm{U},-36 / \mathrm{U},-44 / \mathrm{U},-45 / \mathrm{U}$, $-46 / \mathrm{U},-47 / \mathrm{U},-48 / \mathrm{U},-49 / \mathrm{U},-51 / \mathrm{U},-52 / \mathrm{U}$, $-53 / \mathrm{U},-54 / \mathrm{U}$, and $-57 / \mathrm{U}$
Sockets Used With Holder: See figures 3-15 and 3-16.

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056B (16 Jan 53) ; MIL-H1056/2 (16 Jan 53)
Dimensions: See figure 3-2. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

Materials:

| Item No. <br> (Fig. $3-2)$ | Descrip- <br> tion | Material | Qty |
| :---: | :--- | :--- | :---: |
| 1 | Pin | Kovar No. 920050, or equal | 2 |
| 2 | Base | Kovar No. 910010, or equal | 1 |
| 3 | Cover | Nickel silver, per Spec QQ- <br> N-321, type III comp B | 1 |

Special Requirements: (Refer to figure 3-2.)
a. Item No. 2 shall be insulated from item No. 1 by glass. Glass shall be Corning Glass Seal No. 705-2, or equal.
b. Item No. 2 shall be hot-tin-dipped or electro-tin-plated in accordance with type I finish of Spec 72-53.
c. Before forming, item No. 2 shall be 0.010 $\pm 0.001$ inch thick, and item No. 3 shall be 0.010 inch thick.
d. Item No. 1 shall project at least 0.040 inch above the inside glass seal.

## LOGISTICAL DATA

USAF Stock No.:
Status: Standard
Date of Status:
Commercial Sources: See Appendix III.
Related Specifications, Standards, and Publications: See Appendix IV.

Section 111
Crystal Holders-Group I

## CRYSTAL HOLDER HC-10/U



Figure 3-3. Crystal Holder HC-10/U

## FUNCTIONAL DESCRIPTION

Compact, miniature, metal holder designed for pressure-mounting thickness-mode circular quartz elements and for hermetic sealing. The coaxial arrangement of the crystal leads introduces a minimum of holder capacitance across the crystal, and hence is particularly suitable for use with v-h-f crystals. Also, the rugged construction and firm support provided the crystal make this holder preferred in mobile or portable equipment that may be subjected to severe conditions of vibrations or shock. The holder is dependable over a temperature range of $-55^{\circ} \mathrm{C}$ to $+90^{\circ} \mathrm{C}$ and higher.

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder: CR-24/U
Sockets Used With Holder: See figure 3-17.

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056B (16 Jan 53) ; MIL-H1056.3 (16 Jan 53)

Dimensions: See figure 3-3. All dimensions in inches. Unless otherwise specified, tolerances are 0.005 in . on decimals.

## Materials:

| Item No. <br> (Fig. S-Y) | Descrip- <br> tion | Material | Qtif |
| :---: | :--- | :--- | :---: |
| 1 | Sleeve | Coil silver | 2 |
| 2 | Pin | Kovar No. 920050, or equal | 2 |
| 3 | End bell | Kovar No. 910010, or equal | 2 |
| 4 | Cover | Nickel silver per Spec QQ- | 1 |
| 5 | Seal | Corning Glass No. 705-2, or <br> equal | 2 |

Special Requirements: (Refer to figure 3-3.)
a. Item No. 1 shall be soldered to item No. 2.
b. Item No. 3 shall be hot-tin-dipped or electro-tin-plated in accordance with type I finish of Spec 72-53.

## LOGISTICAL DATA

USAF Stock No.:
Status: Standard
Date of Status:
Commercial Sources: See Appendix 111.
Related Specifications, Standards, and Publications: See Appendix IV.

## CRYSTAL HOLDER HC-I3/U



Figure 3-4. Crystal Holder HC-13/U

## FUNCTIONAL DESCRIPTION

A lightweight, all-metal unit, similar to Crystal Holder HC-6/U but having a cover of greater. length to accommodate a larger quartz plate for lower-frequency use.

## EMPLOYMENT OF HOLDER

Crisstal Lnits Employing Holdor: CR-37/U, $-38 / \mathrm{U},-42 / \mathrm{U}$, and $-50 / \mathrm{U}$
Sockets Lsed With Holder: See figures 3-15 and 3-16.

## MILITARY SPECIFICATIONS

Authority: MLL-H-10056B (16 Jan 53) ; MLL-H1056/4 (16 Jan 58)
Dimensions: See figure 3-4. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

Materials:

| $\begin{aligned} & \text { Hem. No. } \\ & (\text { Fig. } 3-i) \end{aligned}$ | $\begin{gathered} \text { Hescrip } \\ \text { fion } \end{gathered}$ | Matcrial | Qt! |
| :---: | :---: | :---: | :---: |
| 1 | lim | Kovar No. 920050 , or equal | 2 |
| 2 | Base | Kovar So. 910010, or exual | 1 |
| 3 | Coyer | Nickel silser, per sper QQ. N-321, tymelli, compl | 1 |

Special Reruiremonts: (Refer to figure 3-4.)
a. Item No. 2 shall be insulated from item No. 1 by glass. Glass shall be Corning Class Seal No. $70 n-2$, or equal.
b. Item No. 2 shall be hot-tin-dipped in accordance with type 1 finish of Specification $72-53$.
c. Before forming, item No. 2 shall be 0.010 $\pm 0.001$ inch thick, and item No. 3 shall be 0.010 inch thick.
d. Unless otherwise specified, item No. 1 shall project at least 0.040 inch above the inside glass seal.

## LOGISTICAL DATA

## USAF Stock No.:

Stutus:
Date of Status:
Commercial Sources: See Appendix III.
Rulated Speritications, Stanlards, amd Publications: See Appendix IV.


Figure 3-5. Crystal Holder HC-14/U

## FUNCTIONAL DESCRIPTION

A miniature, lightweight, all-metal unit. Similar to Crystal Holder $\mathrm{HC}-6 / \mathrm{U}$ but with a shorter cover. It is used to mount quartz plates in the higher-frequency range, where space is at a premium.

## EMPLOYMENT OF HOLDER

Crystal Units Emplaying Holder: CR-7/U
Sockets Used With Holder: See figures $3-15$ and 3-16.

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056B (16 Jan 53) ; MIL-H1056/5 (16 Jan 5\%)
Dimensions: See figure :3-5. All dimensions in inches. Unless otherwise specified, tolerances are +0.005 in . on decimals.

Materials:

|  | $H_{\mathrm{escrip}}$ tom | Material | Qt" |
| :---: | :---: | :---: | :---: |
| 1 | Pm | Kovar No. 9 mon 0 , or equal | 2 |
| 2 | Rase | Rovar No. 910010, or equal | 1 |
| 3 | Cower | Sickel siluer, per spee QQ- <br> X-3nl, tym 111, compla |  |

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Special Requirements: (Refer to figure 3-5.)
a. Item No. 2 shall be insulated from item No. 1 by glass. Glass shall be Corning Glass Seal No. 705-2, or equal.
b. Item No. 2 shall be hot-tin-dipped or electro-tin-plated in accordance with type I finish of Spec 72-53.
c. Before forming, item No. 2 shall be 0.010 $\pm 0.001$ inch thick, and item No. 3 shall be 0.010 inch thick.
d. Item No. 1 shall project at least 0.040 inch above the inside glass seal.

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commervial Sources: See Appendix 111.
Related Sperifications. Standerds, and Publicutions: See Appendix IV.

## CRYSTAL HOLDER HC-15/U



Figure 3-6. Crystal Holder HC-15/U

## FUNCTIONAL DESCRIPTION

This glass-envelope crystal holder is similar in size and shape to a 6SC7GT electron tube. It is normally used to mount low-frequency, flexuremode, quartz plates, where an evacuated container is needed to reduce damping. The holder uses standard vacuum-iube parts and fits in a standard octal socket. The glass envelope is to be preferred to the metal holder when a vacuum seal is required because the elimination of the metal, soldering, etc. minimizes the causes of crystal aging due to gas leakage, electrolysis, and contamination. The holder is dependable within the temperature range of $-55^{\circ} \mathrm{C}$ to $+80^{\circ} \mathrm{C}$.

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder: CR-39/U and $-40 / \mathrm{U}$.
Sockets Used With Holder: Standard octal.

## MILITARY SPECIFICATIONS

Authority: M1L-II-10056B (16 Jan 53) ; MIL-H1056/6 (16 Jan 53)

Dimensions: See figure 3-6. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

## Materials:

| Item No. (Fig. S-i) | $\begin{gathered} \text { Descrip- } \\ \text { tion } \end{gathered}$ | Material | QtII |
| :---: | :---: | :---: | :---: |
| 1 | Pin | Commercial | 8 |
| 2 | Base | Low-loss phenolic | 1 |
| 3 | T9 envelope | - Glass | 1 |

Special Requirements: Except for dimensions, there are none specified.

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III.
Reluted Specifications, Standards, and Publications: See Appendix IV.


Figure 3-7. Crystal Holder HC-16/U

## FUNCTIONAL DESCRIPTION

This crystal holder is similar in size and shape to a metal envelope 6SK7 electron tube. It is a rugged, moisture-proof holder in which quartz plates may either be pressure-, wire-, or fixed-air-gap-mounted. The holder is recommended for calibration, test, and similar purposes. Holder uses standard vacuum-tube parts and fits in a standard octal socket. Although it is used in the $70-100-\mathrm{kc}$ range, the holder is useful for frequencies up to 850 ke . The shortness of the cover relative to the size of crystal blanks of 85 kc and below makes it somewhat difficult to fabricate a dependable crystal unit. The holder can be used at temperatures within the range of $-55^{\circ} \mathrm{C}$ to $+90^{\circ} \mathrm{C}$ and higher.

## EMPLOYMENT OF HOLDER

Cristai linits Employing Holdor: CR-43/U Sockets l'sed With Holder: Standard octal

## MHITARY SPECIFLCATIONS

Authority: MIL-II-10056B (16 Jan 53) ; MLL-H1056/7 (16 Jan 5i3)

Dimensions: See figure 3-7. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

Materials:

| Hem No. <br> (Fig. 3-7) | Descrip- <br> tion | Material | Qty |
| :---: | :--- | :--- | :---: |
| 1 | Pin | Commercial | 8 |
| 2 | Base | Commercial | 1 |
| 3 | MT8 <br> envelope | Commercial | 1 |

Special Requirements: None specified

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III,
Related Specifications, Standards, and Publications: See Appendix IV.

## CRYSTAL HOLDER HC-17/U



Figure 3-8. Crysfal Holder HC-17/U

## FUNCTIONAL DESCRIPTION

A lightweight, all-metal unit particularly suitable for use in either mobile or portable equipment and wherever crystal units may be subjected to severe conditions of moisture or mechanical shock. Several types of mounting are possible, but the most satisfactory, generally, is a plated crystal supported by two looped springs. This holder is designed for hermetic sealing and is dependable over a temperature range of $-55^{\circ} \mathrm{C}$ to $+90^{\circ} \mathrm{C}$ and higher. This holder is identical to Holder HC-6/U except for larger dimensions of pins.

## EMPLOYMENT OF HOLDER

## Crystal Units Employing Holder: CR-58/U

Sockets Used with Holder:

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056C (Proposed revision, 4 April 1956)
Dimensions: See figure 3-8. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.

Materials:

| $\begin{aligned} & \text { Item No. } \\ & \text { (Fig. } 3-8) \end{aligned}$ | $\begin{aligned} & \text { Descrip- } \\ & \text { tion } \end{aligned}$ | Material | Qty. |
| :---: | :---: | :---: | :---: |
| 1 | Pin | 50\% nickel, $50 \%$ iron alloy | 2 |
| 2 | Base | Steel, cold rolled strip condition No. 3, per Specification QQ-S-640 | 1 |
| 3 | Cover | Copper, nickel zinc alloy composition No. 5, annealed soft temper, per Specification QQ-C-585 | 1 |

Special Requirements: (Refer to figure 3-8.)
a. Item No. 2 shall be insulated from item No. 1 by glass. Glass shall be Corning Glass Seal No. 705-2, or equal.
b. Item No. 2 shall be hot-tin-dipped or electro-tin-plated in accordance with type I finish of Specification MIL-F-14072.
c. Before forming, item No. 2 shall be 0.010 $\pm 0.001$ inch thick and item No. 3 shall be 0.010 inch thick.
d. Item No. 1 shall project at least 0.040 inch above the base.

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III.
Related Specifications, Standards, and Publications: See Appendix IV.

## CRYSTAL HOLDER HC-18/U



Figure 3-9. Crystal Holder HC-18/U

## FUNCTIONAL DESCRIPTION

A lightweight, all-metal holder suitable for use in subminiature circuit applications. Long flexible leads are provided to permit wiring crystal holder directly into the circuit.

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder: CR-55/U, $-56 / \mathrm{U}$, $-59 / \mathrm{U},-60 / \mathrm{U},-61 / \mathrm{U}$
Sockets Used with Holder: None

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056C (Proposed revision, 4 April 1956)
Dimensions: See figure 3-9. All dimensions are in inches. Unless otherwise specified, tolerances are $\pm 0.005 \mathrm{in}$. on decimals.
Materials:

| Item No. <br> (Fig.s-9) | Desrrip- <br> tion | Material | Qty. |
| :---: | :---: | :--- | :---: |
| 1 | Pin | Cobalt-nickel-iron alloy <br> (Kovar A) <br> Cobalt-nickel-iron alloy <br> (Kovar A) <br> Copper, nickel, zinc alloy, <br> composition No.5, Ennealed <br> soft temper, per Specifica- <br> tion QQ-C-585 | 1 |
|  | Base | 1 |  |

## Special Requirements: (Refer to figure 3-9.)

a. Item No. 2 shall be insulated from item No. 1 by glass. Glass shall be Corning Glass Seal No. 705-2, or equal.
b. Item No. 2 shall be hot-tin-dipped or electro-tin-plated in accordance with type I finish of Specification MIL-F-14072.
c. Before forming, item No. 2 shall be 0.010 $\pm 0.001$ inch thick and item No. 3 shall be $0.010 \pm 0.001$ inch thick.
d. Item No. 1 shall project at least 0.040 inch above the base.

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III.
Related Specifications, Standards, and Publications: See Appendix IV.

## CRYSTAL HOLDER HC-21/U



Figure 3-10. Crysfal Holder HC-21/U

## FUNCTIONAL DESCRIPTION

A three-pin, all-metal holder used to mount lowfrequency quartz plates. Dimensions of this holder are identical to those of plastic hoider $\mathrm{HC}-5 / \mathrm{U}$, which it is intended to replace. Holder HC-21/U is designed for hermetic sealing and is dependable over a temperature range of $-55^{\circ} \mathrm{C}$ to $+90^{\circ} \mathrm{C}$ and higher.

## EMPLOYMENT OF HOLDER

## Crystal Units Employing Holder:

Sockets Used with Holder: See figure 3-14.

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056C (Proposed revision, 4 April 1956)
Dimensions: See figure 3-10. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.
Materials:

| Item No. <br> (Fig.s-10) | Descrip- <br> tion | Material | Qty. |
| :---: | :--- | :--- | :---: |
| 1 | Pin <br> 2 | Base | $50 \%$ nickel, $50 \%$ iron <br> Cold rolled steel, condition <br> No. 2, dull finish, per Speci- <br> fication QQ-S-666 <br> Terneplate type drawing <br> quality, class special coat. <br> ed, grade unassorted, per <br> Specification QQ-T-181 |

Special Requirements: (Refer to figure 3-10.)
a. Item No. 2 shall be insulated from item No. 1 by glass. Glass shall be Corning Glass Seal No. 705-2, or equal.
b. Item No. 2 shall be hot-tin-dipped or electro-tin-plated in accordance with type I finish of Specification MIL-F-14072.
c. Before forming, item No. 2 shall be 0.010 $\pm 0.001$ inch thick and item No. 3 shall be $0.010 \pm 0.001$ inch thick.
d. Item No. 1 shali project at least 0.040 inch above the base.

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III.
Related Specifications, Standards, and Publications: See Appendix IV.

## CRYSTAL HOLDER HC- /U

(For addenda)

Figure 3-11. Crystal Holder HC. /U

FUNCTIONAL DESCRIPTION

EMPLOYMENT OF HOLDER
Crystal Units Employing Holder:
Sockets Used With Holder:

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III.
Related Specifications, Standards, and Publications: See Appendix IV.

# CRYSTAL HOLDER HC-18/U 

(For addenda)

Figure 3-12. Crystal Holder HC- /U

FUNCTIONAL DESCRIPTION

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder:
Sockets Used With Holder:

## LOGISTICAL DATA

USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix 111 .
Related Specifications, Standards, and Publications: See Appendix IV.

## CRYSTAL HOLDER HC. IU

> (For addenda)

Figure 3-13. Crystal Holder HC- /U

## FUNCTIONAL DESCRIPTION

## EMPLOYMENT OF HOLDER

Crystal Units Employing Holder:
Sockets Used With Holder:

## MILITARY SPECIFICATIONS

Authority: MIL-H-10056B (16 Jan 53) ; MIL-H1056/
Dimensions: See figure 3-13. All dimensions in inches. Unless otherwise specified, tolerances are $\pm 0.005$ in. on decimals.

Materials:

| Item No. <br> (Fig.3- | Descrip- <br> tion | Material | Qty |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

Special Requirements:

LOGISTICAL DATA
USAF Stock No.:
Status:
Date of Status:
Commercial Sources: See Appendix III
Related Specifications, Standards, and Publications: See Appendix IV.

CRYSTAL SOCKETS


Figure 3-14. Crystal sockets for use with HC-5/U holder


TUCTE:
GLAZED INSUKATORS ARE GLAZED TOP ANO SIDES UNGLAZED SURFACES ARE DC 200 MPREGNATED.

Figure 3-15. Crystal socket for use with HC-6/U, HC-13/U, and HC-14/U holders


Figure 3-16. Multiple crystal socket for use with HC-6/U, HC-13/U, and HC-14/U holders


Figure 3-17. Crystal socket for use with HC-10/U holder

TECHNICAL DATA CHART OF CRYSTAL SOCKETS SUITABLE FOR USE WITH GROUP-I HOLDERS ${ }^{\text {b }}$

| Type Holder Accommedated | Manufacturer ${ }^{\text {a }}$ | Model No. | Figure No. | Material of Insulator | Material of Contacts | Additional Stray Cap. Shunted Across Xtal ( $\mu \mu \mathrm{f})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HC-5, $\mathbf{C}$ | Cinch | 2886 | 3-14 (A) | NEMA Spec Grade XP laminated phenolic (nat.) | Cinch P27 |  |
|  | E. F. Johnson | 122-223-1 | 3-14(B) | Glass-bonded mica or NEMA Spee Grade XXX laminated phenolic | Brass w/steel spring: $\mathrm{C}_{\mathrm{d}} \mathrm{pl}$ |  |
|  |  | 122-223-2 |  | Glass-bonded mica | Phosphor bronze w/beryllium copper springs, silver p 1 |  |
| $\begin{aligned} & \mathrm{HC}-6 \mathrm{U}, \\ & \mathrm{HC-13/O}, \\ & \text { and } \\ & \mathrm{HC}-14 / \mathrm{U} \end{aligned}$ | Cinch | 54A17358 | 3-15 | Steatite, Grade L5, glazed | Beryllium copper, P31W-3 finish, solder term. hot-tin dipped |  |
|  | Elco | 430 | 3-15 | Ceramic, Grade 5, glazed | Brass, $\mathrm{C}_{\mathrm{d}} \mathrm{pl}$ |  |
|  |  | 430 U |  | Ceramic, Grade 5, unglazed |  |  |
|  |  | 430 PH |  | Ceramic, Grade 5, glazed | Phosphor bronze, $\mathrm{C}_{\mathrm{d}} \mathrm{pl}$ |  |
|  |  | 430 U PH |  | Ceramic, Grade 5, unglazed |  |  |
|  |  | 430 BC |  | Ceramic, Grade 5, glazed | Beryllium copper, silver pl |  |
|  |  | 430 U BC |  | Ceramic, Grade 5, unglazed |  |  |
|  | E. F. Johnson | 126-105-1 | 3-15 | Steatite, Grade L4 or better, glazed | Beryllium copper, siiver pl, solder term., hot-tin dipped |  |
|  |  | 126-105-2 |  |  | Phosphor bronze |  |
|  | Methode | SCJ 700-1 | 3-15 | Steatite, Grade L5, glazed | Phosphor bronze, brass, or beryllium copper, as specified; $\mathrm{C}_{\mathrm{d}}$ or silver pl; solder term. hot-tin dipped |  |
|  |  | SCJ 700-2 |  | Same as SCJ 700-1 except not DC200 impregnated |  |  |
|  | Sylvania | G24-666 | 3-16 | Low-loss phenolic | $\text { Fhosphor bronze } \mathrm{C}_{\mathrm{d}} \mathrm{pl} \text {, }$ hot-tin dipped |  |
| HC-10/U | Eby | 8943 | 3-17 | Ceramic | Spring-type body clip; brass, silver pl |  |
| $\begin{aligned} & \mathrm{HC}-15 / \mathrm{U} \\ & \text { and } \\ & \mathrm{HC}-16 / \mathrm{U} \end{aligned}$ | These holders are accommodated by standard octal sockets. For technical data and mounting provisions of octal sockets, see National Military Establishment Specifcation JAN-S-28A |  |  |  |  |  |

- Sex Apmendix IIL for complete name and addrees.
* Crystal Helder HC-18/U is a subminiature unit fabricated with wire leads for moldered connectiona;
hence no soeket is reduired.

| Mounting <br> Provisions | Dimensions (In.) |  |  |  |  |  |  |  |  |  | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | $B$ | $C$ | D | $E$ | $F$ | $G$ | H | I | $J$ |  |
| Three $0.152-\mathrm{in}$. dia holes on \% $x^{31 / 4}$ in. mtg centers |  |  |  |  | See fig. | -14 (A) |  |  |  |  |  |
| Two mtg holes spaced 1:7/x2 in. c to c |  |  |  |  | See fig. | -14 (B) |  |  |  |  |  |
| 0.115-0.135 <br> in. dia mtg <br> hole | * ${ }_{64}$ | $\begin{aligned} & 0.481- \\ & 0.491 \end{aligned}$ | 0.243 | \% 8 | $\begin{array}{\|l\|} 0.236-2 \\ 0.260 \end{array}$ | $\begin{array}{\|l\|} \hline 0.115- \\ 0.135 \end{array}$ | \% | 3/4 | 1/4 | 1/4 | Withdrawal force of inserted xtal is $11 / 2 \mathrm{lb} \pm 40 \%$ direct pull |
| $0.125-\mathrm{in} . \mathrm{dia}$ mtg hole | *) | 0.486 | 0.243 | \% | 1/4 | 0.125 | 4\%\% | \%/8 | 14/4 | 1/8 |  |
| $0.125-\mathrm{in} . \mathrm{dia}$ mtg hole | 53/4 | 0.486 |  | 38 |  |  | 4\% ${ }^{2}$ | 3/8 | 11/4 |  | Withdrawal force of inserted xtal is $14 / 2 \mathrm{bb} \pm 40 \%$ direct pull |
| $\begin{aligned} & 0.130-\mathrm{in.} \mathrm{dia} \\ & \text { mtg hole } \end{aligned}$ | 23/64 | 0.486 |  | 38 | 1/4 | 0.130 | ${ }^{31 / 14}$ | 38 | 7/4 | 1/6 | Tropicalization treatment optional |
| Four $0.156-\mathrm{in}$. dia holes on $61 / \mathrm{x}$ \% $/ 6$-in. mtg centers |  |  |  |  | Seefig | g. 3-16 |  |  |  |  | Accommodates 48 holders |
| Two 0.125-in. dia holes on $1 / 2 \times 1 / 4$-in. mtg centers |  |  |  |  | See fig | 5. 3-22 |  |  |  |  |  |

GROUP II

## CRYSTAL HOLDERS CURRENTLY IN MILITARY SERVICE BUT NOT RECOMMENDED FOR USE IN EQUIPMENTS OF NEW DESIGN

Group II inciudes the older types of crystal holders which are still widely used in current models of USAF radio equipments, but which are not recommended for use in military equipments of new design. These crystal holders are arranged in the order of their USAF stock numbers, which numbers are the same as the Signal Corps stock numbers except for the addition of the prefix " 2100 -," which serves to identify the item as belonging to the USAF $16-F$ stock class.

TECHNICAL DATA CHART FOR GROUP-II CRYSTAL HOLDERS

| USAF Stock Number 2100- | Nomenclature | Holder Spec | Material | Method of <br> Mounting |
| :---: | :---: | :---: | :---: | :---: |
| $2 \times \mathrm{H} 1.1$ | Crystal Holder Wilcox Type 80D |  | Plastic |  |
| 2xH2.1 | Crystal Holder FT-249 |  | Plastic |  |
| $2 \mathrm{xH2.2}$ | Crystal Holder FT-249 |  | Plastic |  |
| $2 \times \mathrm{H} 2.3$ | Crystal Holder FT-249 |  | Plastic |  |
| $2 \times \mathrm{H} 2.4$ | Crystal Holder |  | Plastic case, metal cover |  |
| $2 \times \mathrm{H} 2.5$ | Crystal Holder (Collins Type 1G) |  | Plastic |  |
| $2 \times \mathrm{H} 3.1$ | Crystal Holder FT-164 | 171-148B | Ceramic |  |
| 2xH3.2 | Crystal Holder FT-164 | 171-148B | Ceramic |  |
| $2 \times \mathrm{H} 4.1$ | Crystal Holder (Bendix 3947) |  | Plastic |  |
| $2 \times \mathrm{H5.1}$ | Crystal Holder (Bliley MO-2) |  | Plastic |  |
| $2 \times \mathrm{H6.1}$ | Crystal Holder FT-171-B | $71-975$ | Plastic |  |
| 2xH6.2 | Crystal Holder FT-171-B | $71-975$ | Mastic |  |
| $2 \times \mathrm{H7.1}$ | Crystal Holder FT-241-A | 71-1696 | Plastic |  |
| $2 \times \mathrm{H} 9.1$ | Crystal Holder (Collins Type 1C) |  | Plastic |  |
| $2 \times \mathrm{H} 10.1$ | Crystal Holder FT-243 | 71-1350 | Plastic case, metal cover |  |
| 2xH14.1 | Crystal Holder HC-12/U |  | Plastic |  |
| $2 \times \mathrm{H} 14.1-1$ | Crystal Holder CR-1A/AR |  | Plastic |  |
| $2 \times \mathrm{H} 4.2$ | Crystal Holder HC-11/U |  | Plastic |  |
| $2 \times 1415.1$ | Crystal Holder | 71-1165 | Metal |  |
| 2xH17.1 | Crystal Holder (Howard Engineering CM-1) |  | Ilastic |  |
| 2xH18.1 | Crystal Holder (WECO Type 5AA) |  | Mastic |  |


| Base or Terminal Connections | Outside Dimensions (In.) |  |  | Electrodes | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | High | Wide | Thick |  |  |
| Std 3-pin | 13/4 | 151/18 | 13/6 |  |  |
| Std 3-pin | 1918 | $1{ }^{136}$ | 12\%32 | 2 pr, both $1 \times 1 \mathrm{in}$. |  |
| Std 3-pin | 1\%18 | 1\%6 | 124/32 | $\begin{aligned} & 2 \mathrm{pr} ; 1 \mathrm{pr} 1 \times 1 \mathrm{in} . ; 1 \mathrm{pr} \\ & 3 / 3 \mathrm{x} / 4 \mathrm{in} . \end{aligned}$ |  |
| Std 3-pin | 1\%18 | 1\%6 | 125/32 | $2 \mathrm{pr}, 3 / 4 \times 3 / 4 \mathrm{in}$. |  |
| $3-\mathrm{pin}, 7 / \mathrm{in} . \lg , 0.156 \mathrm{in}$. dia | 23/8 | 1\%18 | 1\%23 | $1 \mathrm{pr}, 1 \times 1 \mathrm{in}$. |  |
| 3-pin, $1 / 2 \mathrm{in}$. $\lg$, $5 / 1 / \mathrm{in}$. dia | 24, | 13/3 | 7/8 |  |  |
|  | 11/6 | 2\% (dia) |  | 1 pr, brass, nickel-plated | For LF quartz wafer |
|  | 11/8 | 24/4is) |  | 1 pr, brass, nickel-plated | For HF quartz wafer |
| 6-pin on std octal base | 13/16 | 1/2 (dia) |  |  | For 3 quartz plates |
| 2-pin, $/ 4 / \mathrm{in}$. c to c | $13 / 18$ | 13/8 (dia) |  |  |  |
| 2 banana pins, the in. $\mathrm{lg}, 3 / 4 \mathrm{in}$. e to $\mathbf{c}$ | $113 / 16$ | 11/2 | $3 / 4$ | $1 \mathrm{pr}, 1 \times 1 \mathrm{in}$. |  |
| 2 banana pins, $7 / 16$ in. $\lg , 1 / 4 \mathrm{in}$. c to c | 13186 | 11/2 | $3 / 4$ | $1 \mathrm{pr}, 3 / 4 \times 3 / 4 \mathrm{in}$. |  |
| 2-pin, $7 / 6 \mathrm{in} . \lg , 1 / 2 \mathrm{in}$. c to c | 11/16 | 1732 | 7/8 |  |  |
| Std 5-pin, \%/8, in. | 12\%32 | 1\% | 1\%/6 |  |  |
| $2-\mathrm{pin}, 1 \%_{k} \mathrm{in} . \mathrm{Ig} \mathrm{c}$ to c | 11/8 | 13/68 | 0.434 |  |  |
|  | 11/4 | 11/4 | 7/6 |  |  |
| 2-pin, 5/8in. Ig , $1 / 2 \mathrm{in}$. c to c | 1/4 | 14/4 | 7\% |  |  |
| 2-pin, t/4in. $\mathrm{lg}, 1 / 2 \mathrm{in}$. c to c | 11/4 | 11/4 | 7\% |  |  |
| Std octal | 21\%12 | 1\%2 (dia) |  |  |  |
| 2-pin, $1 / 2 \mathrm{in} . \mathrm{lg}, 7 / 4 \mathrm{in}$. c to c | \% | $1 \%$ (dia) |  |  |  |
| Std 3-pin, 11/82 in. Ig | 17/8 | 1\% | 11/8 |  |  |

Section 111
Crystal Hodders-Group II
TECHNICAL DATA CHART FOR GROUP-II CRYSTAL HOLDERS-Continued

| USAF Stock <br> Number 2100- | Nomenclature | Holder Spee | Material | Method of Mounting |
| :---: | :---: | :---: | :---: | :---: |
| 2xH24.1 | Crystal Holder (Bliley MC-7) |  | Plastic body, metal front |  |
| 2xH25.1 | Crystal Holder (Aircraft Accessories HN-10) |  | Plastic |  |
| 2xH26.1 | Crystal Holder (Galvin FMT-X5) |  | Ceramic, with metal front and back |  |
| 2xH27.1 | Crystal Holder (Billey BC-3) |  | Plastic |  |
| $2 \times \mathrm{H} 28.1$ | Crystal Holder (Aircraft Accessories 601T) |  | Ceramic |  |
| $2 \times \mathrm{H} 29.1$ | Crystal Holder RCA AVA-10 |  | Ceramic | Pressure-air gap |
| $2 \times \mathrm{H} 30.1$ | Crystal Holder (HFR Type) |  | Plastic |  |
| $2 \times \mathrm{H} 31.1$ | Crystal Holder (CW Type) |  | Ceramic |  |
| $2 \times \mathrm{H} 32.1$ | Crystal Holder (Bliley LD-2) |  | Plastic |  |
| 2xH33.1 | Crystal Holder (Henry DC34) |  | Plastic |  |
| $2 \times \mathrm{H} 3$ ¢ 1 | Crystal Holder (Henry DC35) |  | Plastic |  |
| 2x135.1 | Crystal Holder (Premier 180GF and 180 GW ) |  | Ceramic, with metal front and back |  |
| 2xH36.1 | Crystal Holder (Bliley C and S) |  | Plastic |  |
| $2 \times \mathrm{H} 7.1$ | Crystal Holder (Fisher Rad TS25) |  | Plastic |  |
| $2 \times 438.1$ | Crystal Holder (Fisher Rad RS25) |  | Plastic |  |
| $2 \times \mathrm{H} 39.1$ | Crystal Holder (Aireon AA9E) |  | Metal |  |
| $2 \times \mathrm{H} 40.1$ | Crystal Holder (Aircraft Accessories AA9A) |  | Metal |  |
| 2xH41.1 | Crystal Holder (Aircraft Accessories AA9G) |  | Metal |  |
| 2xH42.1 | Crystal Holder (Peterson Radio PR) |  | Ceramic |  |
| $2 \times \mathrm{H} 43.1$ | Crystal Holder (RCA AVA-53-A) |  | Ceramic | Pressure-air gap |
| 2xH44.1 | Crystal Holder (Learadio 3858A) |  | Plastic |  |
| 2xH45.1 | Crystal Holder (WECO DC-20) |  | Plastic |  |
| 2xH46.1 | Crystal Holder (Standard Piezo CS5D) |  | Plastic |  |
| 2xH47.1 | Crystal Holder (Blitey AR8W) |  | Plastic |  |
| $2 \times \mathrm{H} 48.1$ | Crystal Holder (Howard Type HMC4) |  | Ceramic |  |
| 2xH49.1 | Crystal Holder (Coilins LD) |  | Plastic |  |
| $2 \mathrm{xH50.1}$ | Crystal Holder (Bliley AR3) |  | Plastic |  |
|  | Crystal Holder HC-1/U |  | Plastic |  |
|  | Crystal Holder HC-2/U |  | Plastic |  |
|  | Crystal Holder HC-3/U |  | Plastic |  |
|  | Crystal Holder HC-4/U |  | Plastic |  |


| Base or Terminal Connections | Outside Dimensions (1n.) |  |  | Eleetrodes | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | High | Wide | Thick |  |  |
| 2-pin, $3 / 4 \mathrm{in}$, c to c | 11/8 | $13 / 8$ | \% 18 |  |  |
| 2 banana pins, $0.85 \mathrm{in} . \mathrm{c}$ to c | 27/8 | 11/2 | 7/8 |  | Plastic model of 601-T holder |
| 2-pin, $7 / 16$ in. $\lg , 7 / 4 \mathrm{in}$. c to c | 17/4 | $11 / 2$ | $3 / 4$ |  |  |
| 2-pin, $3 / 4 \mathrm{in}$. c to c | \% 76 | 14/8(dia) |  |  |  |
| 2 banana pins, $0.85 \mathrm{in} . \mathrm{c}$ to c | $2 \% /$ | 11/2 | 7/8 |  |  |
| 2 banana pins, 0.85 in. c to c | 21/x | 177/32 | 1\%80 |  |  |
| 2-pin, 3/4in. e to c | 1/2 | 11/3 (dia) |  |  | CW Type HFR Model G and R-100 |
| 2-pin, $/ 4 /$ in. c to e | 8 | 11/2 (dia) |  |  |  |
| 2-pin, $7 / 4 \mathrm{in}$. c to c |  |  |  |  |  |
| 2-pin, $3 / 4 \mathrm{in}$. c to c | 2 | 17/8 | 3/8 |  |  |
|  | 2 | 13/8 | 3/8 |  |  |
| 3 alined pins | 2\% | 11/2 | 7/8 |  |  |
| 2-pin, $7 / 8 \mathrm{in} . \mathrm{c}$ to C | 7/8 | 11/2 (dia) |  |  |  |
| 2-pin |  | 11/2 (dia) |  |  |  |
| 2-pin |  | 11/2 (dia) |  |  |  |
| Std 3-pin | 21/4 | 1/8 | 11/2 |  | Same as MX9E |
| Std 3-pin | 21/4 | 11/9 | 11/2 |  | Same as MX9A |
| Std 3-pin | 211/32 | 137/4 | 1\%/4 |  |  |
| 2-pin | $3 / 1$ | 18/8/8 (dia) |  |  |  |
| 2 banana pins, 0.85 in. c to c | $13 / 4$ | 17/18 | \%/4 |  |  |
| 2 banana pins | 1\% | 11/8 | \% |  |  |
| 2-pin | 11/4 | 178 | 7/18 |  |  |
| 3-pin | 21/6 | 1\%16 | 11/8 |  |  |
| 3-pin | 1\% | $1^{11 / 16}$ | 11/8 |  | Same as AR4W, except freq |
| 5-pin | 11/2 | 11/8 | 11/88 |  | Interchangeable with Collins 1C holder |
| Std 3-pin | $11 / 2$ | 11/8 | 1\% |  |  |
| Std 5-pin | 17/8 | 11/2 | $11 / 2$ |  |  |
| 2-pin | 23/64 | 11//4 | $\%_{18}$ |  |  |
| 2-pin | 2316 | 1/88 | $1 / 2$ |  |  |
| 2-pin | 21/46 | $13 \%$ | 1/2 |  |  |
| 2-pin | 114/32 | 13/18 | 7/68 |  |  |

Section III
Crystal Holders-Group II


Figure 3-18. Crystal Holder FT-164


Figura 3-19. Crystal Holder FT-171-B


ALL OIMENSIONS IN INCHES

Figure 3-21. Crystal Holder FT-243. The markings inditated are applicable for Crystal Units CR-5B/U, CR-6B/U, CR-7B/U, CR-10E/U, and CR-12A/U. Method 1 is used where the operating frequencies of the using equipment are in terms of frequencies only; or where a single crystal is used to control bath a transmitter and a receiver and the channel is expressed in terms of frequency. Method 2 is used where she operating frequencies of the using equipment are designated in terms of channel numbers and frequencies; or where a single crysial is used to control both a transmitter and a receiver and the operating frequency is expressed as a channel number as well as a frequency. Methods 3 and 4 are used respectively where two separate crystal units are amployod in a single equipment, each performing a different function, such as one being used for transmitting and the other for receiving. Method 4 is used where the crystal unit is used to control the local oscillator of a receiver. On the back of the receiver crystal holder is marked "RECEIVE ON 0000 KC," where 0000 is the recsiver frequency, which is olways to be 455 kc below the crystal frequency. For an exploded view of the FT-243 holder, as a port of Crystal Unit CR-8B/U, see figure 1-70.

section a-a


Figure 3-22. Crystal Holder FT-249


Figure 3-23. Crystel Holder for Crystal Unit CR-1A/AR


Figure 3-24. Crystal Holder HC-1/U


Figure 3-26. Crystal Holder HC-4/U

## EXPLANATION OF MILITARY STANDARD TERMS USED IN DESCRIPTION OF CRYSTAL HOLDERS

## Applicable Tests

3-2. Tests which have been specified for the particular crystal holder, and which have been performed by the Government or under the supervision of the Goverrment to determine compliance of production and production specimens with the Military Specifications.

## Autherity

3-3. Serial numbers and dates of the military publications which prescribe the military specifications for the crystal holders being described. All holders described in Group I conform to Military Specification MLL-H-10056( ).
Condition A-Immersion Test (See paragraph 3-18a)
Condition B-Immersion Test (See paragraph 3-18b)
Corrosion Test (See paragraph 3-16)
Date of Status (See paragraph 2-4)
Delivery Requirements (See paragraphs S-23 and 3-24)

## Dimensions and Markings

3-4. Illustrated and largely self-explanatory. The marking of crystal holders, when required, is to be legible and permanent. See paragraph 2-26 for marking pertaining to crystal unit.
Fabrication Requirements (See paragraphs 3-8 and 3-14)

## Functional Description

3-5. Provides summary of the general physical and operational features of the crystal holder.
Glass Seal Inspection (See paragraph 3-17)
Immersion Test (See parograph 3-18)
Insulation Materials (See paragraph 3-10)
Insulation Resistance (See paragraph 3-18)
Leakage Test (See paragraph 8-19)
Marking (See paragraph 3-4)
Method A-Leakage Test (See paragraph 3-19a)
Method A-Thermal Shock Test (See paragraph 3-22a)
Method B-Leakage Test (See paragraph 3-19b)
Method B-Thermal Shoek Test (See paragraph 3-22b)

## Nomenclature of Crystal Holders

3-6. The Joint Army, Navy, Air Force nomenclature for designating a particular type of crystal holder is as follows:

CRYSTAL HOLDER NOMENCLATURE

| Item Name |
| :---: |
| Crystal Holder |

Component
Indicator

In the type number, the component, a crystal holder is identified by the symbol, HC. The component symbol is followed by a hyphen and one or two digits (-X) which identify the crystal holder as having been designed in accordance with a particular set of specifications. The letter, $U$, separated from the number by a slant sign, is the equipment indicator symbol for "general utility installation," which means that the crystal is intended for use in two or more of the three general installation classes-airborne, shipboard, and ground.
Ordering Requirements (See paragraph 3-23)
Packaging Requirements (See paragraph 3-24)
Pin Alinement Test (See paragraph 3-20)
Requirements and Procedure of Tests
3-7. See Military Specification MIL-H-10056( ) for details of the required inspections, the grouping of tests, and the procedure for sampling.

## FABRICATION REQUIREMENTS

## Covers

3-8. Covers are designed to fit the bases in a manner that permits easy assembly and interchangeability of covers and bases of the same type supplied on any one contract or order.

## Flux

3-9. Rosin or rosin and alcohol are normally used as flux. If other fluxes are used, conclusive evidence has been presented to the Government that the proposed substitution and technique of application result in a noncorrosive joint. No corrosive compounds are used for soldering or welding.

Section III

Glass Seal (See paragraph 8-17)
Insulating, Impregnating, and Sealing Compounds 3-10. Insulating, impregnating, and sealing compounds are used only for sealing screws.
Marking (See paragraph 3-4)
Pin Alinement (See paragraph 3-20)

## Solder

3-11. Solder is used in accordance with Federal Specification QQ-S-571.

## Springs

3-12. Springs, when specified, are attached to the base pins by using a high-temperature solder or by welding.

## Threaded Parts

3-13. Screw threads for all screws, nuts, and other threaded parts are in accordance with National Bureau of Standards Handbook H28. All screwthread assemblies are made resistant to loosening under vibration. When practicable, split-type lock washers are provided under the heads of all screws. When a screw mates with a plastic part, a threaded metal insert is molded therein.

## Workmanship

3-14. The crystal holders are required to be manufactured and processed in a careful and workmanlike manner, in accordance with good design and sound practice. The interior surfaces of the holder, its contents and pins, are required to be free from dirt, grease, and any loose or deposited foreign or unapproved material. All burrs must be removed.

## STANDARD TEST CONDITIONS

$3-15$. Unless otherwise specified, all crystal-holder measurements and tests are made under the prevailing ambient conditions of atmospheric pressure and relative humidity and at a temperature between 20 and 35 degrees centigrade.

## DESCRIPTION AND REQUIREMENTS OF TESTS

## Corrosion Test

3 -16. The crystal holder is required to withstand 50 hours of the salt-spray (fog) test specified in Federal Specification QQ-M-151 without evidence of corrosion sufficient to impair the satisfactory operation of the holder.

## Glass Seal Inspection

$3-17$. Those crystal holders with base assemblies having glass seals are inspected with the aid of a strong light and 10 -power magnification. No glass seal is permissible that contains bubbles greater in diameter than one-third the distance between
pins and base, or that contains radial or other detrimental cracks, or if there is loosening of pins or glass seal from the base.

## Immersion Test

3-18. The base assembly or crystal holder, as applicable, is tested as noted on the individual Specification Sheet in accordance with Condition A or $B$ described below. After all excess moisture is wiped off and the base assembly or crystal holder is allowed to dry at room temperature for $1 / 2$ hour, the insulation resistance between pins, and between each pin and any other external part of the holder, is measured with a low-voltage insulation test, using a test voltage of 50 to 100 volts dc. The insulation resistance must not be less than the value specified below for Condition $A$ or $B$, whichever is applicable, and there must be no evidence of mechanical damage.
a. Condition A: The base assembly of the holder is immersed in a 10 -percent (by weight)-minimum salt-water solution, using common table salt. After the solution is brought to a boil, the base assembly is removed and rinsed in running tap water. After drying, as specified above, the base assembly shall show no mechanical damage, and the insulation must have a resistance not less than 5000 megohms.
b. Condition B: The crystal holder is immersed for one hour in water maintained at a temperature between 90 and 95 degrees centigrade. After drying, as specified above, the insulation must have a resistance not less than 200 megohms.

## Leakage Test

3-19. The base assembly or crystal holder, as applicable, is tested as noted on the individual Specification Sheet in accordance with Method A or B described below:
a. Method A: The base assembly is immersed for at least 10 seconds in liquid flux at a temperature not exceeding $25^{\circ} \mathrm{C}$, then, abruptly hot-tindipped for at least 10 seconds in molten solder at a temperature between $302^{\circ}$ to $312^{\circ} \mathrm{C}$. The solder is immediately shaken off and the base assembly is plunged back into the liquid flux for at least 10 seconds. A minimum of three such cycles, continuously, is required. The thermal capacities of the flux and solder baths must be sufficient to maintain the specified bath temperature for the quantity of base assemblies being tested at any one time. When the thermal-shock cycles are completed, the insulation resistance must not be less than 5000 megohms when measured with an insulation tester as described in paragraph 3-18, and the glass seal must pass its standard inspection as described in paragraph 3-17.
b. Method B: The glass envelope, but not the base assembly of the holder, is immersed in boiling water for 15 seconds and immediately thereafter immersed in ice water for 5 seconds, the volume of the water being sufficient to maintain constant temperature. The glass envelope must withstand this test without cracking or breaking.
Visual and Mechanical Inspection (See paragraph 3-80)
a. Method A: The base assembly is clamped to a suitable test jig and subjected to a gage pressure of 50 pounds per square inch while immersed in tap water for at least 30 seconds. The base assembly must show no evidence of leakage around the pins, at the seams, or through cracks or porous spots in any of the base material. The continuous formation of bubbles is evidence of leakage.
b. Method B: The crystal holder is clamped to a suitable test jig and the cavity subjected to similar conditions as in Method A. The holder must show no evidence of leakage around the pins, or through cracks or porous spots in the holder material. The continuous formation of bubbles is evidence of leakage.

## Pin Alinement Test

3-20. The pins of the crystal holder are required to be so alined that they conform to the mechanical dimensions given in the individual Specification Sheet, when measured by means of a shadowgraph. Refer to paragraph 2-24 for alternate test-gage method.

## Tensile Strength Test

3-21. The base assembly of the holder is supported in a way that clears the glass seal. A direct load of 30 pounds is applied along the axis of the pins away from the base for at least 30 seconds, after which, the glass seal must show no evidence of loosening from the pins or base.

## Thermal Shock Test

$3-22$. The base assembly or glass envelope, as applicable, is tested as noted on the individual Specification Sheet in accordance with Method A or B as described below:
a. Method A: The base assembly is immersed for at least 10 seconds in liquid flux at a temperature not exceeding $25^{\circ} \mathrm{C}$, then, abruptly hot-tindipped for at least 10 seconds in molten solder at a temperature between $302^{\circ}$ to $312^{\circ} \mathrm{C}$. The solder is immediately shaken off and the base assembly is plunged back into the liquid flux for at least 10 seconds. A minimum of three such cycles, continuously, is required. The thermal capacities of
the flux and solder baths must be sufficient to maintain the specified bath temperatures for the quantity of base assemblies being tested at any one time. When the thermal-shock cycles are completed, the insulation resistance must not be less than 5000 megohms when measured with an insulation tester as described in paragraph 3-18, and the glass seal must pass its standard inspection as described in paragraph 3-17.
b. Method B: The glass envelope, but not the base assembly of the holder, is immersed in boiling water for 15 seconds and immediately thereafter immersed in ice water for 5 seconds, the volume of the water being sufficient to maintain a constant temperature. The glass envelope must withstand this test without cracking or breaking.

## DELIVERY REQUIREMENTS

## Ordering

3-23. According to Military Specification MIL-H10056B, procurement documents should specify the following:
a. Title, number, and date of the latest specification (the latest at the present time, being Military Specification: Holders, Crystal, MIL-H10056 B , dated 16 January 1953).
b. Type designation, and the title, number, and date of the applicable individual Specification Sheet (the latest one at the present time for HC13/U, for example, is MIL-H-10056/4, dated 16 January 1953).
c. Whether springs are required, dimensions, and how they are to be mounted.
d. Length of pin above base. (See note 6 on applicable Specification Sheet for $\mathrm{HC}-13 / \mathrm{U}$.)
e. The laboratory at which preproduction tests are to be performed. (See MIL-H-10056( ) for requirements of preproduction tests.)
f. Whether packing and marking are for domestic or overseas shipment.
g . That the contractor shall not substitute for a specified material or fabricated part unless he obtains approval from the bureau or service concerned. Evidence to substantiate his claim that such a substitute is suitable shall be submitted with his request. Similar notification and substantiating evidence shall be submitted at any later time if substitution becomes necessary or desirable. At the discretion of the bureau or service concerned, test samples may be required to prove the suitability of the proposed substitute.

## Packaging

3-24. Electron-tube type crystal holders shall be packaged and packed in accordance with packaging group I of Specification MIL-P-75. All other

## Section III

## Military Specifications

types of crystal holders shall be unit-packages with method III of Specification MIL-P-116. Crystal holders are then placed in containers for either domestic shipment and storage or for overseas shipment described in subparagraphs $a$. and $b$. below. In addition to any special marking required by the contract or order, unit packages and exterior shipping containers shall be marked in accordance with Standard MIL-STD-129. These packaging, packing, and marking requirements apply only to direct shipment to the Government and are not intended to apply to contracts or orders between the manufacturer and prime contractors.
a. Packing for Domestic Shipment and Storage: Crystal holders packaged per specification shall be packed in wood-cleated plywood, nailed wood, or corrugated or solid fiber-board boxes conforming to Specification NN-B-601, NN-B-621, LLL-B-631, and LLL-B-636, respectively. Closures shall be made in accordance with the applicable box specification. The gross weight shall not ex ceed 45 pounds for fiberboard boxes and 150 pounds for plywood or wood boxes. Fiberboard having a minimum dry bursting strength (Mullen test) of less than 200 pounds shall not be used.
b. Packing for Oversea Shipment: Crystal holders packaged per specification shall be packed
in wood-cleated plywood, nailed wood, or fiberboard boxes conforming to Specification JAN-P$105, \mathrm{JAN}-\mathrm{P}-106$, and JAN-P-108, respectively. Plywood shall be type B , condition 1 , conforming to Specification JAN-P-139. Each shipping container shall have a case liner conforming to type II, grade A, class 2 of Specification MIL-L-10547. Box closures shall be as specified in the appendix of the applicable specification for fiberboard boxes, and 150 pounds for plywood or wood boxes.

Solder Requirements (See paragraph 3-11)

## USAF Stock No.

3-29. Number for identifying item when requisitioning from U. S. Air Force supply depot. The USAF stock numbers of crystal holders are the same as the respective Signal Corps numbers except that the prefix, " 2100 -," is added, which serves to identify the item as belonging to USAF stock class 16-F.

## Visual and Mechanical Inspection

$3-30$. Inspection of crystal holders to determine if material, design, construction, marking, and workmanship comply with applicable specifications. For greater detail, refer to Fabrication Requirements, paragraphs 3-8 to 3-14.

Workmanship Requirements (See paragraph 3-20)

## SECTION IV-CRYSTAL OVENS

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## SECTION IV-CRYSTAL OVENS

## INTRODUCTION


#### Abstract

4-1. Section IV is divided into two main parts. Part I is a discussion of the design of crystal ovens. Part II consists of a series of technical data sheets describing currently available crystal ovens that are suitable for use with the recommended Military Standard crystal units listed in Section II.


4-2. Part I, Design of Crystal Ovens, begins with a brief discussion of the development of crystal ovens leading to the present state of the art. Included is a reprint of a Signal Corps Technical Requirements report that outlines the operational and test specifications to be met in the development of new crystal ovens for use by the Armed Services. Following this is a general discussion of the construction features of a representative crystal oven. Next, various types of thermostats and temperature-control circuits are described briefly and illustrated. Finally, the thermal factors involved in maintaining a crystal at a constant
operating temperature are analyzed qualitatively in some detail. As an aid to the radio engineer, the thermal parameters are interpreted in terms of their electrical analogues. Because of the complexity of the many distributed variables, a nonapproximating rigorous approach is not practical at the present state of the art. What is attempted is to aid the developmental engineer by making explicit the basic physical problems involved.
4-3. Part II, Technical Descriptions of Crystal Ovens, includes descriptions only of crystal ovens meeting military specifications, which have been designed to accommodate Military Standard crystal holders of Group I, Section III. All such ovens, where the information has been available, have been included; but because of unavoidable omissions, the list should be considered representative rather than inclusive. A listing by type and number of crystal holders each oven will accommodate is provided by a technical data chart at the beginning of Part II.

PART I

## DESIGN OF CRYSTAL OVENS

## DEYELOPMENT OF TEMPERATURE-CONTROLLED CRYSTAL OVENS

## Trends in the Demonds of Crystal-Oven Performance

4-4. During the early years of crystal oscillators, when the large frequency-temperature-coefficient $X$ and $Y$ cuts were the principal quartz elements, good frequency stability required very accurate control of the crystal temperature. For example, an X-cut element having a temperature coefficient of 20 parts per million per degree $C$ would need to be maintained within $\pm 1 / 4^{\circ} \mathrm{C}$ of its mean temperature if the frequency were not to deviate more than 0.0005 per cent. A Y-cut element having a
temperature coefficient four times as great would need to be limited to an operating temperature range of $\pm 1 / 10^{\circ} \mathrm{C}$ for the same permissible frequency deviation. To control the temperature of relatively large crystal units within such narrow limits required the use of carefully designed, but rather bulky and expensive ovens.
4-5. With the arrival of the zero-temperature-coefficient quartz elements, the demand for precise temperature control greatly decreased. Where an oven formerly was required to maintain an operating temperature within $\pm 0.1^{\circ} \mathrm{C}$, its subsequent functional equivalent was permitted temperature cycles of $\pm 1^{\circ} \mathrm{C}$ and greater. As a result, smaller and cheaper ovens soon became conventional.

Section IV

These consumed less power and employed less sensitive but more rugged thermostats than was originally feasible.
4-6. It has only been in recent years that a strong demand has again arisen for greater care in oven design. This demand has a threefold nature:
a. Better ovens are needed to maintain even the conventional tolerances in operating temperature for the wide variations in ambient temperature now required of military equipment.
b. To relieve the overcrowding of the radiofrequency spectrum, very small percentage deviations in crystal frequency, and hence in oven temperature, are needed to make full use of the v -h-f range.
c. It is important that improved performance be obtained without increasing the size of ovens; indeed, it is highly desirable that the size be further reduced. For the above reasons more than routine attention is now being given to possible improvements in the design of crystal ovens, especially small ovens.

## Types of Crystal Ovens

4-7. Ovens used for housing crystal units can be broadly classified into three types: a. Large transmitter ovens. b. Precision laboratory ovens. c. Small ovens.
a. Large temperature-controlled compartments employed in fixed-plant radio transmitters. It is not uncommon for these ovens to house the entire oscillator circuit; in which case the crystal unit may be additionally protected from temperature changes by being mounted in a separately-controlled inner chamber. These ovens are normally equipped with thermometers for indicating the compartment temperature on the front panel or through a window. The transmitter, of which the oven is an integral part, is often intended to operate in buildings where the room temperature is not expected to vary by more than $\pm 15^{\circ} \mathrm{C}$. Under such an ambient range, the large transmitter oven can be expected to maintain the crystal temperature within $\pm 1^{\circ} \mathrm{C}$ to $\pm 0.1^{\circ} \mathrm{C}$, depending upon the type of thermostat, the compartment design, and the mounting arrangement of the components within the oven. Monitoring, alarm, and automatic standby thermostatic circuits in case of thermostat failure are occasionally to be found.
b. Large temperature-controlled boxes for housing crystal units employed in frequency and time standards requiring laboratory precision. This type of oven most often uses a mercury thermostat. Where extreme precision is required, electronic amplification of a thermistor-bridge
thermostat may be employed. The boxes are constructed with thick walls consisting of heat-distributing and heat-insulating layers interleaved with heater windings. For ambient temperature variations of $\pm 15^{\circ} \mathrm{C}$, temperature-controlled boxes can maintain the temperature at tolerances of $\pm 0.1^{\circ} \mathrm{C}$ to $\pm 0.001^{\circ} \mathrm{C}$. The latter tolerance is sufficient to limit the frequency deviation of an average zero-coefficient quartz element to one part in ten billion, if the operating interval is not too long.
c. Small crystal ovens equipped with plug-in bases for mounting in standard sockets, or with bases designed for fastening directly to a chassis. This is the type of crystal oven most commonly encountered and of greatest importance to the design engineer of military radio equipment. It is the only oven type to consider for use in smalland medium-sized equipments. The data sheets in Part II of this section describe several small ovens of this class which are currently available and which have been designed for use with Military Standard crystal units. The average performance of these ovens, although generally satisfactory for normal ranges of room temperature, cannot be said to be entirely satisfactory when subjected to the subfreezing temperatures often required of military equipment. Because of the increased attention being given to the design and development of better small ovens, the radio engineer can reasonably expect a continuous improvement in available models for the next few years. A landmark in the recent trend toward improved oven design was established when Messrs. H. Keen, N. Tetrault, and J. Gilbert of Lavoie Laboratories developed a small oven capable of $\pm 0.15^{\circ} \mathrm{C}$ stability over the ambient range of $-40^{\circ}$ to $+70^{\circ} \mathrm{C}$. Such a temperature stability is more than adequate for the great majority of purposes. For airborne equipment, until such time that crystal units and/or crystal circuits can be designed to be inherently temperature-compensating, the demand will continue for ever smaller sizes, lighter weights, less power consumptions, as well as greater temperature stabilities, particularly in the case of the multiple-position ovens mounting sev. eral crystal units.

## Armed Services Technical Requirements for Crysfol Ovens of New Design

$4-8$. The following digest is a reprint of the detailed requirements for the development of crystal ovens to be used by the Armed Services, as established by the Frequency Control Branch, Squier Signal Laboratory, Fort Monmouth, New Jersey,

October 21, 1952, in Technical Requirements for PR\&C 53-ELS/R-3610:
a. Temperature, Operating : $75^{\circ} \mathrm{C}$ and $85^{\circ} \mathrm{C}$.
b. Temperature Setting Tolerance: $\pm 3^{\circ} \mathrm{C}$.
c. Temperature Cycling Tolerance: $\pm 1^{\circ} \mathrm{C}$ over the entire operable temperature range.
d. Operable Temperature Range: -40 to $+60^{\circ} \mathrm{C}$ ( $75^{\circ}$ oven), -40 to $+70^{\circ} \mathrm{C}\left(85^{\circ}\right.$ oven).
e. Storage, Vibration and Shock: After undergoing the following tests, outlined in Specification MLL-T-945A, there shall be no degradation of performance and the oven shall continue to meet all other requirements of the Technical Requirements. The expression "crystal oven" shall be substituted wherever the expression "test set" appears in the referenced specification:

Par. 4.4.2-Humidity Test
Par. 4.4.4-Temperature and Altitude Test
Par. 4.4.5-Vibration Test (omit Test 2)
Par. 4.4.6-Shock Test
f. Aging: Total shift shall not exceed $1^{\circ} \mathrm{C}$ per month, oven operating, except temperature setting tolerance of sub-panel $b$ shall not be exceeded.
g. Temperature Retrace: The unit shall be capable of returning to its operating temperature $\pm 1^{\circ} \mathrm{C}$ during the following tem-perature-cycling test: unit on 8 hours, off for 16 hours, for a period of 10 cycles.
h. Stabilizing: Unit should reach thermal equilibrium within 15 minutes at any temperature within the operable range.
i. Operating Voltage: A-C-6.3 and 12.6 volts $\pm 10 \%$ obtained by center-tapping the heater winding; also 26.5 volts $\pm 10 \%$.
j. Temperature Measurement: Method will employ a high drift crystal.
k. Mounting: Octal base with clamping fixture.

1. Shape: No factor.
m. Interchangeability of Components: Desirable for replacement purposes.
n. Size: Maximum limits: 4 in. high $\times 11 / 2 \mathrm{in}$. diameter, or, if rectangular, $11 / 2 \mathrm{in}$. on a side.
o. Pin-to-Pin Capacitance: Shunt capacitance across crystal pins (crystal removed) shall not exceed $5 \mu \mu$ f.
p. Thermostats: If thermostats are employed they shall be hermetically sealed.
q. Cavity Size: Shall be capable of housing

Crystal Holder HC-6/U. It is desirable, but not essential, that it shall also accommodate Crystal Holder HC-13/U. Temperature tests which may be conducted employing the latter type of holder will permit a greater tolerance in temperature limits.
r. Workmanship: Components, subassemblies and parts shall be manufactured and assembled in a thoroughly workmanlike manner.
s. Materials: All materials shall be entirely suitable for the purpose for which intended.

## general construction features OF CRYSTAL OVENS

## Provisions for Temperafure Control

4-9. Figure 4-1 illustrates by diagram the principal elements to be considered in the construction of a crystal oven. The thermostat contains a temperature-sensitive element, usually one that operates by expanding and contracting as the temperature rises and falls. By one means or an-


Figure 4-1. General construction features of typical crystal oven

## Section IV

other, the temperature-varying property of the sensing element is used to control the power to an electrical heater, so that the power increases, or starts, when the temperature of the thermostat falls below the operating level, and decreases, or stops, when the temperature rises above the operating level. The heater power-control mechanism may, or may not, be mounted within the oven proper.
4-10. For minimum temperature deviation at the crystal, the thermostat should be thermally insulated from the crystal chamber but in close thermal contact with the heat-distributing layer adjacent to the heater. This arrangement permits the crystal to be insulated from the temperature variations that must occur at the location of the thermostat in order for the thermostat to operate. The greater the heat capacity and the greater the heat resistance of the intervening layers, the more constant will be the crystal temperature. The inside walls of the crystal chamber should be metallic, that is, should have high thermal conductivity to distribute the heat uniformly around the crystal unit and minimize the temperature gradients within the crystal chamber.

## Provisions for Minimizing Power Requirements

4-11. For conservation of operating power, the heater should be as well insulated as is practical against loss of heat to the outside. Ideally, maximum insulation is to be obtained by enclosing the heater and inner compartment within an evacuated container having highly reflective walls-utilizing the same principle as in the Dewar flask and thermos bottle. Practically, the best insulation has been achieved by allowing an air space to separate the heater from the outer walls of the oven. Air, or other gas, is superior as a heat insulator compared with the best of the solid insulators; but this is true only if there is little or no transport of heat by mass movements of the gas from regions of higher to regions of lower temperature. Thus, if the dimensions and temperature gradient of the insulating air space are sufficient for convection currents to circulate around the heater, the space should either be subdivided by horizontal insulating sheets or filled with porous insulating material such as glass wool, Celotex, cotton, hair felt, or balsa wood. Care should also be taken to prevent, or at least retard, convection currents at the outer surface of the oven.
4-12. To reduce to a minimum the heat lost by radiation, the outer case of the oven should be a smooth-surfaced unpainted metal of low emissivity -aluminum, for example. If a plastic case is used, lining the inner and outer surfaces with metal foil
will equally retard heat loss by radiation. Coating a plastic surface with metallic paint can reduce the surface emissivity, and hence the radiation losses, to almost one-half that of the unpainted plastic, but these losses will be ten or more times greater than that of a pure metal surface. Markings on a metallic case should be kept to a minimum. A serial number alone can more than quadruple the radiation losses from that side of the oven. However, these precautions lose much of their importance if it is not practicable to prevent air currents from circulating around the outside of the oven; in which case the heat loss by radiation becomes relatively negligible compared with that by convection and need not be considered a major design consideration.
4-13. The electrical leads from the crystal chamber to the outside should be kept as small in crosssectional area as possible, since these leads tend to "short-circuit" the crystal chamber thermally to the outside. From the point of view of small temperature tolerances, it would be desirable for these leads to be extended in length and close in thermal contact with the heat-distributing layers of the oven. Unfortunately, the leads must be kept short, well-spaced, and insulated electrically (which is equivalent to being insulated thermally) from metallic parts of the oven. These requirements are necessary in order to minimize the shunt capacitance that the oven adds across the crystal unit, and to a lesser extent, to minimize the distributed resistance and inductance added to the crystal circuit. As a general rule, the major factor limiting the performance of small crystal ovens over wide ambient temperature ranges is the heat leakage through the base; particularly is this true for multiple-position ovens, where a leakage path exists for each individual terminal leading from a crystal socket.

## Construction of Typical Small Oven

4-14. Figure $4-2$ shows the principal parts of a small commercial crystal oven equivalent to the Military type HD-54/U. The oven is not designed for precision control of the temperature. Because of the heat leakage through the base, it is questionable whether the temperature tolerance is less than $\pm 5^{\circ} \mathrm{C}$ over an ambient range of $100^{\circ} \mathrm{C}$. The advantage of this type of oven is its small size, light weight, and inexpensive design, which make it particularly suitable for general-purpose use in airborne installations. The thermal key, which is shown as part of the base assembly, is a metallic heat-distributing layer that makes close thermal contact with the base of the distributing shell around which the heaters are wound. The purpose


Figure 4-2. Small crystal oven equivalent to Milltary Type HD-54/U
of the thermal key is to conduct as much heat as possible around the crystal leads before they enter the crystal chamber. The baffle is a plastic cover that forms the walls of the crystal chamber. Its purpose is to provide a heat-storing, as well as a heat-insulating layer between the heater distributing shell and the crystal unit. The metallic case of the crystal holder (type $\mathrm{HC}-6 / \mathrm{U}$ ) provides sufficiently uniform heat distribution within the crystal chamber, for the purposes of the oven, so that an additional inner distributing layer is not provided. Two thermostats and two heaters are provided. One thermostat-heater combination is for quick oven warm-up when the oven is first turned on. This thermostat is adjusted to open its associated heater circuit at a temperature slightly below the desired operating temperature. The second ther-mostat-heater combination determines the actual operating characteristics. The outer cover is plastic and is of sufficient size to provide a small air space around the crystal compartment. The radiation losses are not considered significant compared with the conduction losses through the base and with the expected convection losses around the sides, so that a low-emissivity surface is not provided.

## METHODS OF THERMOSTATIC HEATER CONTROL.

4-15. There are two general methods of thermostatic heater control: the on-off method and the continuously-variable method. The latter permits the heater current to be varied gradually with the aid, usually, of vacuum-tube amplifiers until an equilibrium is reached between the heat being supplied and that being lost. This method is used so rarely that it will not be further considered. However, the thermistor-bridge thermostat, which is discussed below as the control element of an on-off vacuum-tube heater circuit, is equally applicable as the control element of a continuously-variable vacuum-tube heater circuit. In the on-off method, the heater circuit is opened and closed periodically. The action of the thermostat varies the ratio of the on period to the off period until equilibrium is reached at the predetermined operating temperature between the periodic supply of heat and the continuous heat leakage. The on-off thermostat of small ovens is usually connected in series with the heater windings. Where more sensitive thermostats are used, the heater current is controlled indirectly by relay-the thermostat contacts not being required to pass more than a small current sufficient to operate the relay.

figure 4-3. Typical differentia! curves of adjustable thermostat

## Temperature Differentials of Thermostats

4-16. Figure 4-3 shows typical on-off curves of an adjustable thermostat. For any given thermostat adjustment, $P_{1}$, the thermostat operating temperature is the temperature, $\mathrm{T}_{\mathrm{n}}$, midway between the on and off temperatures, $\mathrm{T}_{\text {: }}$ and $\mathrm{T}_{2}$, respectively. The total width of the temperature gap, $\mathrm{T}_{2}-\mathrm{T}_{1}$, is called the backlash, and plus or minus one-half the backlash is called the differential of the thermostat. In general, the larger the differential, the longer is the operating life of the thermostat, although, of course, the less precise is its tempera-ture-controlling ability.

## Thermostats Used for On-Off Heater Control

4-17. Any device that can be used as a thermometer can be modified for use as a thermostat. In practice, the bimetallic thermostat is the type most commonly encountered in crystal ovens, but any corrosion-resistant metal having a large temperature coefficient of expansion can be used as the
sensing element without the bimetallic construction, as long as the associated mechanism provides sufficient sensitivity for opening and closing the thermostat contacts. Where above-average precision is required, a mercury thermometer is usually employed. Thermistors are also occasionally used as the temperature-sensing element, maximum sensitivity being obtained by connecting the thermistor as one arm of a resistance-bridge circuit.

## BIMETALLIC THERMOSTATS

4-18. Bimetallic sensing elements are constructed by welding together two thin metallic strips which have widely different temperature coefficients, of expansion. Since one of the metals expands and contracts with changes in temperature at a greater rate than the other, the effect of a change in temperature is to cause a straight bimetallic strip to bend. Figure 4-4 illustrates a number of the more common types of bimetallic sensing elements. The deflection of these elements is denoted by the symbol d for linear displacements and by the symbol $\phi$ for angular displacements. An angular expression of the deflection is more convenient for the helix and spiral elements since the exact linear deflection of a contact will depend upon the length of a contact arm fastened to the moving end of the bimetallic coil. Equations for the deflections indicated in figure 4-4 are given in the table below.

$$
\begin{aligned}
d= & \text { linear displacement in same dimensions as } \\
& \mathrm{l}, \mathrm{t} \text { and } \mathrm{D} \\
\phi= & \text { angular displacement in radians } \\
1= & \text { length of strip } \\
\mathrm{t}= & \text { overall thickness of strip } \\
\mathrm{D}= & \text { diameter of double-helix coil } \\
\Delta T= & \text { degrees centigrade change in temperature } \\
\mathrm{k}= & \mathrm{k}_{a}, \mathrm{k}_{\mathrm{l}}, \text { or } \mathrm{k}_{e}=\text { temperature coefficient of } \\
& \text { deflection in parts per degree centigrade }
\end{aligned}
$$

| Bimetallic Strip | Deflection Equation | Representative Values of $k$ |
| :--- | :---: | :---: |
| (A) Cantilever | $\mathrm{d}=\mathrm{k}_{\mathrm{a}} \mathrm{l}^{2} \Delta \mathrm{~T} / \mathrm{t}$ | 12 to $20 \times 10^{-6}$ |
| (B) U-Cantilever | $\mathrm{d}=\mathrm{k}_{\mathrm{a}} \mathrm{l}^{2} \Delta \mathrm{~T} / 2 \mathrm{t}$ | 12 to $20 \times 10^{-6}$ |
| (C) End-Supported | $\mathrm{d}=\mathrm{k}_{\mathrm{a}} \mathrm{l}^{2} \Delta \mathrm{~T} / 4 \mathrm{t}$ | 12 to $20 \times 10^{-6}$ |
| (D) Double-Helix | $\mathrm{d}=\mathrm{k}_{\mathrm{p}} \mathrm{ID} \Delta \mathrm{T} / \mathrm{t}$ | 10.5 to $18.5 \times 10^{-8}$ |
| (E) Helix | $\phi=\mathrm{k}_{\mathrm{r}} \mathrm{l} \mathrm{L} \mathrm{T} / \mathrm{t}$ | 1600 to $2500 \times 10^{-6}$ |
| (F) Spiral | $\phi=\mathrm{k}_{\mathrm{c}} \mathrm{l} \mathrm{\Delta T} / \mathrm{t}$ | 1600 to $2500 \times 10^{-6}$ |

## Electrical Resistance of Bimetals

4-19. Since the thermostat deflection is used to open and close an electrical circuit, the bimetallic strip, itself, often forms part of the circuit. In this case, with proper design, the additional heat supplied the bimetal due to its electrical resistance can be used to boost the thermostat's temperature response, making it more sensitive, and effectively reducing the operating differential of the surrounding area. In general, the bimetals having the higher deflection coefficients also have the higher electrical resistivities. Per circular mil foot, bimetal resistances range approximately from 20 to 700 ohms.

## Adjustment of Bimetallic Thermostat

4-20. Within limits, the operating temperature of a bimetallic thermostat can be adjusted by varying the position of the fixed contact relative to the room-temperatuve position of the moving contact. The greater the deflection that is required of the moving contact relative to its initial posi-


Figure 4-4. Basic types of bimetallic strips
tion, the higher will be the operating temperature.

## Creep- and Snap-Action Bimetallic Thermostats.

4-21. The deflection of a bimetallic strip can be used to open and close an electrical circuit either slowly, creep action, or abruptly, snap action. Creep thermostats are the more sensitive, requiring smaller differentials, and are less likely to fail because of fatigue since the bimetallic element is not subjected to vibration or shock. But the contact life is short compared with that of the snap thermostat. This is because of the increased exposure to heating and sparking due to the prolonged periods when the contacts are only barely touching or barely separated. Other limitations of the creep thermostat are its tendency to chatter and the fact that it cannot be used in equipment subjected to vibration. These disadvantages are avoided by the use of a snap thermostat. In fact, the response of the abrupt, positive contact action of the snap thermostat is actually aided by a moderate amount of vibration, requiring slightly smaller temperature differentials than would otherwise be the case. A creep thermostat can be readily converted into a snap type by fastening permanent magnets to the contacts. The contact life of either type is increased by mounting in vacuum, or at least, in a hermetically sealed holder, and by using low a-c voltages in noninductive circuits. Where necessary, additional protection against sparking at the contacts is to be had by shunting the contacts, or inductive parts of the circuit, with a suitable resistance and capacitance in series. This is particularly necessary if the thermostat is used to control the current of an inductive relay, or if voltages higher than 30 volts are employed. The average life of a snap thermostat is on the order of 100,000 actions, although there are a number of significant exceptions to the average. For example, the E-shaped, bimetallic cantilever element, see figure $4-5$, is claimed to have a life of a million actions. These elements are available in a number of small sizes that should be sufficiently sensitive for use in crystal heater circuits where the thermostat contacts must pass the entire heater current.

figure 4-5. E-shaped, bimetallic, snap thermostat


Figure 4-6. Bimetallic thermostat circuits


Figure 4-7. Diagram of typical mercury thermostat

## Heater Control Circuits Using Bimetallic Thermostats

4-22. Figure 4-6 shows several temperature-controlled heater circuits suitable for use with bimetallic thermostats. Generally, voltages over 30 volts are avoided in the thermostat circuit, 6 -volt sources being those most often employed. In circuit 4-6(A), the thermostat contacts must be of sufficient size to pass the full heater current. Differentials as low as $\pm 0.5^{\circ} \mathrm{C}$ are possible here, but values two and three times this are more common in the average oven. Short cantilever strips mounted in evacuated glass envelopes are the most sensitive per unit length and have comparatively long lifetimes. This type of thermostat is tamperproof and is the most economical in space and in cost. Its chief disadvantage is that the sealed unit, although permitting a long contact life, prevents the thermostat from being adjustable. Thus, relatively high tolerances in the nominal operating temperature must be allowed the manufacturer.
4-23. Figure 4-6(B) shows a circuit in which a sensitive helix-type bimetallic thermostat can be used to control an electromagnetic relay. The resistance of the relay must be sufficient to limit the current to a value not exceeding the maximum current permissible for the thermostat contacts. In this type of circuit the thermostat current need not exceed 5 or 10 ma , and operating differentials less than $\pm 0.1^{\circ} \mathrm{C}$ are possible. The resistor-capacitor combination protects the thermostat from high induced voltages when the circuit is opened. 4-24. Figure 4-6(C) is a hot-wire-relay circuit that permits the use of the more sensitive bimetallic thermostats without the disadvantages of highly inductive loads introduced by electromagnetic relays. The hot-wire relay permits thermostat currents as low as 50 ma , and operating differentials as low as $\pm 0.1^{\circ} \mathrm{C}$.

## MERCURY THERMOSTATS

4-25. Mercury thermostats, see figure 4-7, are mercury thermometers constructed with bulb and capillary electrodes which enable the mercury column to close an electrical circuit at a preset temperature. The sensitivity of the average mercury thermostat is on the order of $0.2 \mathrm{in} . /{ }^{\circ} \mathrm{C}$; but sensitivities 5 times as great are feasible. The sensitivity is directly proportional to the ratio, $V / D^{2}$, where $V$ is the volume of the bulb and $D$ is the diameter of the capillary. Theoretically the sensitivity can be increased indefinitely by increasing the volume of the bulb. Practically this is not possible, because when large bulbs are used ambient effects other than temperature, pressure for example, also become significant factors in deter-
mining the exact height of the mercury column. In addition, the larger the bulb, the greater its thermal inertia, so the slower becomes the response to changes in the temperature of the surroundings. Average operating differentials range from $\pm 0.02^{\circ} \mathrm{C}$ to $\pm 0.05^{\circ} \mathrm{C}$. The operating temperature can be adjusted by having separate electrodes in the capillary for each desired temperature, as is indicated in figure 4-7. For a continuous range of operating temperatures, mercury thermostats have been designed with a movable platinum-wire electrode that makes sliding contact with a fixed terminal. The movable electrode is fastened to a small iron rod so that adjustments can be made with the aid of a small permanent magnet. The height of the electrode is varied simply by sliding the magnet up and down the outside of the capillary tube. This type of laboratory thermostat permits excellent frequency precision since the operating temperature of the oven can be adjusted to match exactly the zero-temperaturecoefficient point of a crystal.

4-26. Figure $4-8$ shows a typical temperaturecontrol circuit employing a mercury thermostat. Note the high resistance in the thermostat circuit. This resistance should be sufficient to limit the current to 1 or 2 microamps or less. At the most, the current should not exceed 5 microamps, otherwise the mercury may become fouled. With negligible currents, the operating life of the thermostat can be quite long. When inoperation does occur it is usually due to capillarity effects. The mercury thermostat, because oí its fragility and the size and expense of the associated circuit components is suitable for use only in those large fixed-plant or laboratory crystal ovens that require aboveaverage temperature stability.

## Thermistor-Bridge Thermostats

4-27. Thermistor-bridge thermostats have the advantage of requiring no moving parts. Their sensing of temperature changes takes the form of a continuously variable voltage subject to unlimited vacuum-tube amplification, so that theoretically no minimum limit exists for the operating differential. In practice, with the use of high-gain vacuumtube circuits, the thermistor bridge can be made to respond to temperature differentials as small as $\pm 0.001^{\circ} \mathrm{C}$. Because of its elaborate circuit requirements the thermistor bridge is not generally practical for temperature control of crystals except when the utmost temperature stability is necessary.
4-28. Figure 4-9 (A) is the schematic diagram of a moderately sensitive thermistor circuit which


Figure 4-8. Heater control circuit using mercury thermostaf
employs a vacuum-tube-operated electromagnetic relay to control the heater current. It can be seen that the input of $V_{t}$ is connected across the resistance bridge, which is driven by a 60 -cycle signal introduced from the bridge transformer. When the temperature rises to a point where the thermistor resistance balances the bridge, the input signal to $V_{1}$ becomes zero. As the temperature continues to rise, the signal again begins to build up, but opposite in phase to its polarity when the temperature was below the balance point. The polarity of the "above-balance" signal is such that the amplified input to $V_{3}$ is in phase with the 60 -cycle voltage applied to the $V_{3}$ plate. Note that $V_{3}$ is operated primarily as a half-wave rectifier. The heater relay coil serves as the inductance of the LC filter of the rectified plate voltage, but also as a $2-\mathrm{K}$ cathode-biasing resistance. When the polarities of the $V_{3}$ input and plate voltages are in phase, the plate current is sufficient to operate the relay and open the heater circuit. The thermostat circuit that is shown is not sufficiently sensitive to justify its operation for crystal ovens without the addition of at least one more amplifier stage. To be preferred, is a high-gain voltage amplifier used in conjunction with a gas-filled relay tube as shown in figure 4-9 (B). If desired, the thermistor can be simply a copper winding. Copper, with a temperature coefficient of resistance of $0.0043 /{ }^{\circ} \mathrm{C}$, will have a resistance variation with temperature 100 or more times that of the manganin bridge arm of equal nominal resistance. Among the metals, the highest temperature coefficients of resistance at normal oven temperatures are those of iron and of nickel, which range between 0.006 and 0.007 parts per ${ }^{\circ} \mathrm{C}$. The temperature coefficient of tungsten is between 0.0045 and 0.005 part per ${ }^{\circ} \mathrm{C}$ at oven temperatures.

## Thermostat Monitoring

4-29. Where a constant check on the crystal tem-

(A)

figure 4-9. On-off heater control circuits


Figure 4-10. Thermostat monitoring and alarm circuit
perature is necessary, additional thermostat circuits can be provided for automatic monitoring. In the event the temperature should fall below or rise above the desired differential range, the thermostat monitoring circuits can be designed to operate alarms or to switch the heater control to a standby thermostat. The possible modifications are quite varied, but relatively easy to design once the basic monitoring requirements of the circuit are agreed upon. Figure $4-10$ shows a typical alarm circuit. For simple monitoring, a pilot lamp connected across the heater is sufficient to indicate the on-off operating cycle, and a mercury thermometer is sufficient to indicate the operating temperature.

## thermal analogues of electrical PARAMETERS

4-30. The electrical concepts of voltage, current, conductance, and capacitance have their analogues in the thermodynamic laws of heat conduction and storage, where the laws that govern the flow of heat are mathematically equivalent to the laws that govern the flow of electricity. If difference of temp̈̀erature replaces the term difference of potential, and current is interpreted to mean a net flow of thermal energy past a point per unit time, instead of a net flow of electric charge, then the terms, thermal conductivity and thermal conductance, and the reciprocals, thermal resistivity and thermal resistance, are defined by the same relations that define their electrical counterparts.

## Thermal Eurrent

4-31. Thermal current, heat/unit time, has the same physical dimensions as power, and, if desired, can be expressed in watts. For example, if a metal rod, well insulated along its length, is heated continuously at one end by an electrical heater imbedded in the rod at that end, the heat will be conducted down the rod at the same rate at which it is produced; so that a proper measure of the thermal current would be the wattage of the heater. Where units of heat capacity are involved, it is common to express heat in units of the gram-, or kilogram-calorie. One gram-calorie is the quantity of heat required to raise the temperature of one gram of water one degree centigrade. One gram-calorie per second equals 4.186 watts. A 1 watt flow of heat is thus equal to a thermal current of approximately 0.25 gram-calories per second.

## Thermal Conductivity

4-32. The thermal conductivity, K , of a wellinsulated conducting segment of cross-sectional area $A$ and length $L$ is given by the equation

$$
\begin{equation*}
\mathrm{K}=\frac{\mathrm{I}_{\mathrm{H}} \mathrm{~L}}{\Delta \mathrm{TA}} \tag{1}
\end{equation*}
$$

where $\Delta T$ is the difference in temperature between the two ends of the segment when a steady thermal current, $\mathrm{I}_{\mathrm{H}}$, is caused to flow along the length. If $\mathrm{I}_{\mathrm{H}}$ is measured in gram-calories/second, A and $L$ in centimeter units, and $\Delta T$ in centigrade degrees, K is expressed in units of $\mathrm{gm}-\mathrm{cal} / \mathrm{sec} \mathrm{cm}$ deg C. Approximate values of representative conductivities are given in the following table.

| Thermal <br> Conductivity, K <br> (gm-cal/sec cm deg C) | Material |
| :---: | :--- |
| 1.0 | Copper, Silver <br> Aluminum |
| 0.5 | Mercury <br> 0.19 |
| 0.03 | Quartz (parallel to Z <br> axis) |
| 0.016 | Quartz (perpendicular <br> to Z axis) |
| 0.012 | Carbon (graphite) |
| 0.0025 | Glass, Porcelain |
| 0.0018 | Mica |
| 0.0006 | Asbestos paper |
| 0.0004 | Rubber, Average Plastic |
| 0.0001 | Cork, Glass wool in air |
| 0.00008 | Hair felt in air, <br> Rock wool in air |
| 0.000057 | Air |
| 0.000052 | Nitrogen |

## Thermal Resistance

$4-33$. The thermal resistance of a conductor of length $L$, cross sectional area $A$, and thermal conductivity, $K$, is defined by the equation

$$
\begin{equation*}
R_{\mathbf{R}}=\frac{L}{K A} \tag{1}
\end{equation*}
$$

We shall arbitrarily define the unit of thermal resistance to be the resistance of a thermal conductor that requires a difference of temperature of $1^{\circ} \mathrm{C}$ between the ends of the conductor in order for one calorie per second to flow through it. This unit we shall call a "thermohm."

## Thermal Ohm's Law

4-34. When equations 4-32 (1) and 4-33 (1) are combined to cancel the term, L/KA, the following "Ohm's law" for thermal circuits is derived:

$$
\begin{equation*}
\Delta \mathrm{T}=\mathrm{I}_{\mathrm{H}} \mathrm{R}_{\mathrm{H}} \tag{1}
\end{equation*}
$$

Note that $\Delta T$, the "temperature drop" across the resistace, $R_{B}$, of a thermal circuit, is similar to $\Delta V$, tie voltage drop across the resistance of an electrical circuit. Where $\Delta V$ is a measure of the difference of potential energy per unit charge, $\Delta T$ can be shown to be a measure of the difference of kinetic (thermal) energy per unit matter (i.e., per unit particle).

## Stefan-Boltzmann Law

4-35. The heat radiation from a surface is not a linear function of the temperature, but obeys a frourth power equation that is known as the StefanBoltzmann law:

$$
\begin{equation*}
I_{R}=A e_{\sigma} T^{4} \tag{1}
\end{equation*}
$$

where $I_{R}$ is the total heat radiated per second, $A$ is the area of the radiating surface, e is the emissuity of the surface, $\sigma$ is the Stefan-Boltzmann constant, and $T$ is the temperature in Kelvin (absolute) degrees.

## Radiancy

4-36. The radiant energy emitted per second per unit area is called the radiancy of a body. Thus,

$$
\begin{equation*}
\text { Radiancy }=\frac{\mathrm{I}_{\mathrm{k}}}{\mathrm{~A}}=\mathrm{e}_{\sigma} \mathrm{T}^{4} \tag{1}
\end{equation*}
$$

## Absorptivity and Emissivity

4-37. An isolated body in thermal equilibrium with its surroundings will necessarily be absorbing and emitting thermal energy at the same rate. A body that absorbs all of the radiation incident to its surface, reflecting none, is called an ideal black body. The fraction of the incident radiation absorbed is called the absorptivity of the body, which in the case of an ideal black body is equal to 1 .

Now, since at thermal equilibrium, the radiancy must equal the rate of absorption per unit area, the radiancy of an ideal black body must equal the radiancy of the empty space surrounding the body. For the same reason, if the absorptivity of a body is small, its radiancy, relative to black body radiancy, must also be small in exactly the same proportion when at thermal equilibrium with its surroundings. The ratio of the radiancy of a body to that of an ideal black body is the emissivity, e, of the body. Note that $e$ is also equal numerically to the absorptivity.

## Stefan-Boltzmann Constant

4-38. Since e is equal to 1 for an ideal black body, the radiancy of an leal bleck body is equal to $\sigma \mathrm{T}^{4}$. The constant $\alpha$, which equals the radiancy of an ideal black body per (degree) ${ }^{4}$, has been found experimentally to be

$$
\sigma=5.73 \times 10^{-9} \text { milliwatts } / \mathrm{cm}^{2} \mathrm{deg}^{4} \mathrm{~K}
$$

Expressed in calories,

$$
\sigma=1.37 \times 10^{-12} \mathrm{cal} / \mathrm{sec} \mathrm{~cm}^{2} \mathrm{deg}^{4} \mathrm{~K}
$$

## Emissivities of Various Substances

4-39. The emissivities of bodies for radiations in the visual range can be judged by the amount of reflection when the body is exposed to white light. Thus, in the case of diffuse reflections, bright white surfaces have low absorptivities, and hence, low emissiviities, and dull black surfaces have high emissivities. However, the emissivities of most substances vary considerably with the frequency. A green object, for example, indicates a lower emissivity for the green band of the light spectrum than for the other bands. Asbestos, which is white, has a total emissivity at low temperatures equal to that of lamp black, which is 0.95 . Wet ice at $0^{\circ} \mathrm{C}$ has an emissivity of 0.97 , and white hoar frost has an emissivity of 0.985 , which is the nearest to ideal black body conditions so far discovered in solids or liquids. The lowest emissivities are to be obtained with polished silver and gold, where at low temperatures values of 0.02 can be realized. Values for the total emissivity of aluminum vary somewhat, ranging from 0.022 to 0.08 at relatively low temperatures. Emissivities of 0.022 and 0.028 appear to be approximately correct for pure aluminum at temperatures of $25^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$, respectively, whereas the higher emissivities are due to various degrees of oxidation or moisture adsorption at the surface. A completely oxidized aluminum surface, for instance, has an e of 0.11 at $200^{\circ} \mathrm{C}$. Surface oxidation usually raises the emissivity of a metal several fold. On oxidation, the emissivity increases from 0.02 to 0.6 for copper,

## Section IV <br> Crystal Ovens-Design

0.05 to 0.35 for nickel, 0.09 to 0.43 for monel metal, 0.05 to 0.6 for lead, 0.08 to 0.8 for steel, and 0.035 to 0.6 tor brass. Quartz, itself, has a relatively high emissivity (approximately 0.9 ) at low temperatures, so that even if the unplated surface area of a metal-plated crystal is only as much as $1 / 10$ the total area, the total effective emissivity will be several times that of the plated area alone.

## Radiant Heat Flow

4-40. Since the absorptivity is equal to the emissivity, the radiant energy being absorbed by a substance is given by the same equation that defines the energy being radiated-that is, by equation $4-35$ (1), except that $T$ represents the absolute temperature of the surroundings, rather than of the substance, itself. Thus, the net flow of radiant heat away from a surface, equal to the radiated minus the absorbed energy per second, is given by the equation

$$
\begin{equation*}
\mathrm{I}_{\mathrm{H}}=\mathrm{I}_{\mathrm{R}}-\mathrm{I}_{\mathrm{A}}=A \mathrm{e}_{\sigma}\left(\mathrm{T}_{0}^{4}-\mathrm{T}_{\mathrm{n}}{ }^{4}\right) \tag{1}
\end{equation*}
$$

where $I_{A}$ is the rate of radiant heat being absorbed, $\mathrm{T}_{0}$ is the temperature in Kelvin degrees of the surface, and $T_{n}$ is the temperature of the surroundings. Now

$$
\begin{aligned}
T_{0}^{4}-T_{B}^{4} & =\left(T_{0}-T_{n}\right)\left(T_{0}+T_{s}\right)\left(T_{0}{ }^{2}+T_{4}{ }^{2}\right) \\
& =\Delta T\left(2 \mathrm{~T}_{0}-\Delta T\right)\left(2 \mathrm{~T}_{0}{ }^{2}-2 \mathrm{~T}_{0} \Delta T+\Delta \mathrm{T}^{2}\right) \\
& =\Delta T\left(4 \mathrm{~T}_{0}{ }^{3}-6 \mathrm{~T}_{0}{ }^{2} \Delta T+4 \mathrm{~T}_{0} \Delta \mathrm{~T}^{2}-\Delta \mathrm{T}^{3}\right)
\end{aligned}
$$

where $\Delta T=T_{0}-T_{\mathrm{x}}$. If the difference in the two temperatures is small in comparison with their magnitudes, the percentage error will be negligible for most practical purposes if the higherpower $\Delta T$ terms are dropped. Thus, equation (1) can be written approximately

$$
\begin{equation*}
\mathrm{I}_{\mathrm{H}} \approx 4 \mathrm{Ae}_{\sigma} \mathrm{T}_{0}{ }^{2}\left(\mathrm{~T}_{0}-1.5 \Delta \mathrm{~T}\right) \Delta \mathrm{T} \quad 4-40 \tag{2}
\end{equation*}
$$

## Equivalent Thermal kadiation Resistance

4-41. Technically, thermal conductance and its reciprocal, thermal resistance, are measures of the ability of a substance to transport heat by virtue of molecular impacts alone; but to facilitate the illustration of thermal circuits schematically, we shall represent heat radiation by assuming equivalent conducting paths having appropriate thermal resistances. (Heat transport by air convection shall be treated merely as an increase in air conductance, and not as being due to a separate conducting path.)
4-42. The equivalent radiation resistance indicated by equation $4-40$ (2) is

$$
\begin{equation*}
\mathrm{R}_{\mathrm{H}}=\frac{\Delta \mathrm{T}}{\mathrm{I}_{\mathrm{H}}}=\frac{1}{4 \mathrm{Ae}_{\sigma} \mathrm{T}_{0}^{3}\left(\mathrm{~T}_{0}-1.5 \Delta \mathrm{~T}\right)} \tag{1}
\end{equation*}
$$

Equation (1) indicates that for oven surface temperatures between $50^{\circ}$ and $85^{\circ} \mathrm{C}$ ( $323^{\circ}$ and $358^{\circ} \mathrm{K}$ ), the effective radiation resistance approximately doubles as $\Delta T$ is varied from $0^{\circ}$ to $100^{\circ}$. For example, assuming a $T_{0}$ of $350^{\circ} \mathrm{K}$ and an ef 0.08 , the effective radiation resistance of 1 sq cm of a partially oxidized aluminum surface will vary approximately from 50,000 to 100,000 thermohms as the ambient temperature increases from $350^{\circ}$ to $230^{\circ} \mathrm{K}$.

## Heat Capacity

4-43. Heat capacity is defined as the thermal energy required to raise the temperature of a substance one degree. The relative capacities of materials for storing thermal energy are more generally described in terms of specific heat. The specific heat of a substance is the heat capacity of one gram of the substance as compared with the heat capacity of one gram of water. Numerically, then, the specific heat is equal to the number of calories required to raise one gram of the substance one degree. The heat capacity of a quantity of matter varies directly with the number of atoms or molecules contained that are free to absorb thermal energy. At the same temperature, the average heavy atom has the same thermal energy per degree of freedom of motion as the average light atom. Thus in solids, where the density of atoms per unit volume does not vary nearly as much as the density of mass per unit volume, the lighter substances generally have the greater specific heats. (For instance, aluminum, which has an atomic weight of 27 and a density of $2.7 \mathrm{gm} / \mathrm{cc}$, has a specific heat of $0.21 \mathrm{cal} / \mathrm{gm}$ deg C ; whereas lead, with an atomic weight of 207 and a density of $11.3 \mathrm{gm} / \mathrm{cc}$, has a specific heat of $0.03 \mathrm{cal} / \mathrm{gm}$ deg C.) If the change in the thermal energy of a system at thermal equilibrium is plotted as the ordinate against the temperature as the abscissa, the slope of the curve at any point is the instantaneous value of the heat capacity at that temperature. At temperatures where there is a change of state, the heat capacity of a substance may rise to a very high value. For example, at $0^{\circ} \mathrm{C}$, the instantaneous heat capacity of ice water approaches infinity, since heat can be absorbed without a change in temperature.

## Equivalent "Electrical Circuits of Crystal Ovens"

4-44. The relations among the various thermal parameters that affect the performance of a ther-mostatically-controlled oven can be more readily seen if we represent the equivalent thermal circuit by schematic diagrams, borrowing electrical symbols (see figure 4-11) to represent their thermal


Figure 4-11. Electrical symbols applied to parameters of thermal circuits
analogues. Figure 4-12 is the schematic diagram of the "equivalent electrical circuit" of a representative constant-temperature crystal oven. The actual thermal circuit, of course, consists of continuously distributed heat resistance and capacity. A rigorous quantitative description would require the use of exponential functions and an analysis of the thermal transients. Nevertheless, reasonable approximations can be made and greater simplicity achieved if the circuit is represented by linear, lumped parameters, and steady state conditions assumed, as is done in figure 4-12. The symbols of the circuit parameters indicated in figure 4-12 are defined as follows:
$\mathrm{G}_{1}=\mathrm{a}$ calorie gonerator having an output equal to the power losses in the crystal
$\mathrm{G}_{2}=\mathrm{a}$ calorie generator having an output equal to the wattage of the heater
$\mathrm{T}_{1}=$ the temperature, or "difference of potential" between the crystal and "ground" $\left(0^{\circ} \mathrm{C}\right)$
$\mathrm{T}_{2}=$ the temperature at the walls of the crystal chamber
$T_{3}=$ the temperature of the heater and thermostat
$\mathrm{T}_{4}=$ the ambient temperature, which is represented as determined by the connection of $S_{1}$ to the heat-reservoir "battery"
$\mathrm{T}_{\mathrm{s}}=$ the temperature of the electrical terminals of the crystal unit
$I_{1}=$ current meter reading, which in the steady state equals the output of $\mathrm{G}_{1}$


Figure 4-12. Equivalent electrical circuit of crystal oven
$I_{2}=$ average cal/sec passing from the heater and crystal to the outside
All the resistance values refer to thermal, not electrical resistances.
$R_{1}=$ effective lumped resistance of crystal and electrodes
$R_{2}=$ equivalent resistance to radiation from crystal to walls of holder
$\mathbf{R}_{3}=$ equivalent resistance to radiation from holder to walls of inner chamber
$R_{4}=$ equivalent resistance to radiation from heater to cuter walls of oven
$\mathrm{R}_{5}=$ equivalent resistance to radiation from oven to ambient atmosphere
$R_{6}=$ effective lumped resistance from crystal and electrodes via air to walls of holder
$R_{r}=$ effective lumped resistance of walls of holder
$\mathbf{R}_{\mathrm{x}}=$ effective lumped resistance of air from holder to walls of inner chamber
$R_{9}=$ effective lumped resistance of walls of inner chamber and of heater surrcunding the walls
$R_{10}=$ effective lumped resistance of air from inner to cuter walls
$R_{11}=$ effective lumped resistance of outer walls
$\mathrm{R}_{12}=$ effective lumped resistance of air surrounding oven (normally reciprocal of equivalent convection conductance)
$R_{13}=$ effective lumped resistance of wires supporting crystal
$\mathrm{R}_{14}=$ effective lumped resistance of crystalunit electrical leads and terminals
$R_{15}=$ effective lumped resistance of external circuit and electrical insulation
$\mathbf{R}_{10}=$ effective lumped resistance between terminal leads and the heat distributing layer of oven chamber
$\mathrm{R}_{17}=$ effective lumped resistance of base, including electrical ground connection
$\mathrm{R}_{18}=$ effective lumped resistance of air and mounting fixtures in contact with base
$R_{19}=$ equivalent resistance to radiation from base of oven
$\mathrm{C}_{1}=$ effective lumped heat capacity of crystal and electrodes
$\mathrm{C}_{2}=$ effective lumped heat capacity of holder, except the electrical leads
$\mathrm{C}_{3}=$ effective lumped heat capacity of inner walls of oven chamber
$C_{4}=$ effective lumped heat capacity of heater and outer heat-distributing wall of oven chamber
$\mathrm{C}_{5}=$ effective limped heat capacity of thermostat and misceilaneous fixtures in close
thermal contact with outer heat-distributing wall of oven chamber
$C_{s}=$ effective lumped heat capacity of outer wall
$\mathrm{C}_{7}=$ effective lumped heat capacity of electrical leads in crystal holder
$\mathrm{C}_{8}=$ effective lumped capacity of external electrical circuit
$\mathrm{C}_{9}=$ effective lumped capacity of base
$S_{1}=$ imaginary control varying the ambient temperature
$S_{2}=$ thermostat switch controlling heater
In general, the resistance values close to the crystal are larger than those farther removed because of the much smaller cross sectional area of the conducting path. On the other hand, the capacitance values farther out are much greater than the inner values because of the larger volumes contained. Because it is desired to keep the weight and volume as small as possible, as well as the time required to bring the oven to the operating temperature, those conditions that would tend to increase the heat capacity of all parts except the inner chamber wall $\left(C_{3}\right)$ between the heater and the crystal are generally considered undesirable, and the design engineer is normally more concerned with providing sufficient insulation and a uniform distribution of the heat under steadystate conditions. Under steady-state, or "d-c" conditions the values of the capacities are of no significance, but since the heater is being alternately turned on and off, there is an "a-c" component in the heat flow; in this connection the capacity effects must be considered.
4-45. The principal function of the circuit in figure $4-12$ is to maintain the temperature $\mathrm{T}_{1}$ of the crystal unchanged when the ambient temperature $\mathrm{T}_{4}$ is varied. To a first approximation, this end is achieved by interposing between the crystal and the outside the constant-temperature heat reservoir, $\mathrm{C}_{4}$, which is kept "charged" at the desired operating temperature by the thermostatically controlled constant-current calorie generator, $\mathrm{G}_{\mathrm{s}}$. The on-off operation of the calorie generator causes the temperature of $\mathrm{C}_{4}$ to cycle slightly above and below the operating mean; so, to attenuate the a-c component, an RC thermofilter is interposed between the $\mathrm{C}_{4}$-reservoir and the crystal.
4-46. The performance of the circuit in figure 4-12 shall be described as dependent primarily upon the individual performances of six overlapping circuits; three of which are d-c circuits, two, a-c, and one is a transient circuit. One of the $d-c$ circuits conducts the crystal power to the outside,
the second conducts the heater power to the outside, and the third is the thermal link between the heater and the thermostat. Of the a-c circuits, one is the filter circuit between the heater calorie generator and the crystal-it attenuates the a-c component of the heater temperature; the other is the a-c path from the oven heat reservoir to the outside-it is effective in determining the cycling frequency. The transient circuit is essentially the two a-c circuits combined-it determines the warm-up time. Each of the d-c circuits is discussed separately. The a-c and warm-up circuits, because of their overlapping functions, are discussed jointly.
4-47. The resistive and capacitive parameters can be interpreted as having the effective lumped values that would be measured under steady-state conditions. In the d-c circuits, the heat capacities can be ignored as long as steady-state conditions are assumed. Only when there are fluctuations in the heat flow do the capacity effects need to be considered. For those oven elements that have relatively large ratios of specific heat to resistivity, such as the metallic parts, not too much error is introduced in the a-c circuits by treating the element entirely as a lumped "capacitor," having an effective heat capacity equal to its actual heat capacity. For those elements that have very small ratios of specific heat to resistivity, such as the air spaces, the error introduced in the a-c circuits by treating the element entirely as a lumped "re-sistor," having an effective resistance equal to its actual resistance, can also be considered negligible. Where the greatest tolerances must be allowed the lumped parameters, is in the interpretation of the a-c characteristics of those oven parts that have relatively high specific heats as well as high resistivities, such as plastics and other insulating compounds.

## D-C PATH OF CRYSTAL POWER

4-48. Figure $4-13$ is a simplified schematic of the equivalent d-c circuit of the crystal unit which conducts the crystal power to the outside of the crystal holder. The external reservoir symbolized by the battery connection can be interpreted as being any constant-temperature heat reservoir of temperature $T_{3}$, without regard to whether the crystal unit is oven mounted or not; otherwise, all symbols are the same as in figure 4-12. The heat from the constant-current generator $G_{i}$ divides between the three resistance paths, that part flowing through each branch being inversely proportional to the respective branch resistance. Note that as long as the heat flow and the resistances


Figure 4-13. Thermal D-C path of erystal power
remain constant, su also does the temperature drop $T_{1}-T_{3}$, so that a given change in the steady-state value of $\mathrm{T}_{3}$ must cause exactly the same change in $T_{1}$.
4-49. Normally the crystal circuit is designed for a constant drive level, but if, for instance, the crystal is connected in an oscillator stage that is to be keyed by a push-to-talk microphone circuit, there would be little to gain by the use of an oven of high inherent stability. If high temperature stability is desired, a first requirement is that of a crystal circuit providing a constant drive. This, in turn, is best achieved by operating the crystal at the lowest drive level that is practicable. For a small ( $1-\mathrm{cm}$ diameter) wire-mounted crystal unit, the principal leakage is through $R_{6}$, the air resistance. The temperature drop across $R_{8}$ for each milliwatt of drive will be on the order of $0.3^{\circ} \mathrm{C}$. Should the drive vary by as much as $1 / 3 \mathrm{mw}$ the temperature would vary by $0.1^{\circ} \mathrm{C}$. This much variation is ten times more likely at a drive of 5 mw than at one of 0.5 mw . If the same sized crystal unit were evacuated, $R_{6}$ would become infinite, and all the leakage would be through $R_{2}$ and $R_{13}$. The total resistance could thereby increase ten-fold, so that a $1 / 3$-mw variation in the drive would mean a temperature variation of $1^{\circ} \mathrm{C}$. Should a drive of 3 mw for the same crystal be alternately turned off and on, the crystal temperature would vary by approximately $10^{\circ} \mathrm{C}$, and a well-designed oven would be practically useless. If fluctuations in the drive are to be anticipated, optimum temperature control is to be had with the use of sandwich-type crystal units, even though these usually require higher drives than do wiremounted units. Not only is the thermal resistance between the crystal and the holder negligible compared with that of the wire-mounted unit, but the large heat capacity of the sandwich electrodes, as compared with the thin metal films of the plated electrodes of the wire-mounted units, considerably

## Section IV <br> Crystal Ovens-Design



Figure 4-14. Thermal D-C path of heater power
increases the effective heat capacity ( $\mathrm{C}_{1}$ in figure $4-13$ ) of the crystal, and hence can minimize the effects of brief fluctuations in the output of $\mathrm{G}_{3}$. In the case of a low-frequency, wire-mounted crystal vibrating in a flexural mode, where it is necessary to evacuate the holder to prevent an excessive damping by the air, it is advantageous if a large area of the crystal is not plated. Otherwise, the low emissivity of the silver, or other metallic film, will cause $R_{2}$ to be excessive, thereby raising the temperature of the crystal and increasing its sensitivity to small fluctuations in the drive. For a given drive level, the larger the value of $\mathrm{C}_{1}$, the more stable is the temperature of the crystal during brief fluctuations in either the crystal drive or the oven temperature. Also, the larger the magnitudes of $R_{2}, R_{6}$, and $R_{13}$, the less sensitive is the crystal to brief fluctuations in the oven temperature; but, on the other hand, the crystal will be more sensitive to changes in the drive level, whether or not these changes are of brief or long duration.

## D-C PATH OF HEATER POWER

4-50. The thermal path by which the heater power escapes to the outside is represented schematically in figure $4-14$. The symbols apply to the same parameters as in figure 4-12. The power requirements of the crystal oven equal the average rate of heat flow $\left(I_{2}\right)$ from the heater to the outside. The equation for the leakage current is

$$
\begin{equation*}
\mathrm{I}_{2}=\frac{\mathrm{T}_{3}-\mathrm{T}_{4}}{\mathrm{R}_{\mathrm{T}}} \tag{1}
\end{equation*}
$$

where $R_{T}$ represents the total resistance from $T_{3}$ to $T_{4} . I_{1}$, the crystal power flow (see figure 4-12), can be considered negligible. A large part of the heat flows through $R_{11}$, the resistance of the outer walls and top of the oven, although some leakage
is through $\mathrm{R}_{10}$ into the electrical circuit, and a large leakage occurs at the base through $\mathrm{R}_{17}$. Because of the large radiation losses if the oven is inclosed in a plastic container, the total resistance through the walls and top can be approximately doubled if the outer walls are composed of polished metal instead of plastic, even though the actual resistance, $R_{11}$, of the outer oven walls, in itself, becomes negligible. For optimum operation, the oven must be shielded, with baffles if necessary, from forced convection currents in the ambient air; such as might be encountered from blowers, fans, etc. Where the space is available, as in large heavy-duty fixed-plant equipment, the oven should have the protection of two reflective insulating walls separated by a thick air space padded with loose-fill insulation of sufficient density to prevent convection currents between the walls. (Reflective surfaces in series are additive in their insulating effects.)
4-51. In an average aluminum-walled crystal oven, the heat leakage through the base, $\mathrm{R}_{17}$, may well be as great as that through the other five sides of the oven combined. Partly compensating the large conductance of the base is the fact that convection currents in the air are retarded when the heat is escaping under horizontal surfaces, since the surface prevents the warmed layers of air from rising. Thus, the effective resistivity of the air beneath a relatively large base may be more than three times that at the top of the oven. Of course, if the air under the crystal oven is circulating due to convection currents initiated in other parts of the equipment in which the oven is used, this advantage will not be in effect. If the oven is a small socket-mounted device, the direct-thermal contact of the base with the socket eliminates most of the air surface, so that the effective conductivity of the base is much greater than if the same oven were mounted on legs, or were otherwise supported so that a large air space exists between the base and the chassis.
4-52. From the point of view of low operating power, it is desirable to keep $\mathrm{R}_{18}$, the leakage path from the inner chamber walls to the electrical circuit, as large as possible. On the other hand, from the point of view of temperature control, as discussed earlier, $\mathrm{R}_{16}$ should be as small as possible, so that the temperature of the walls of the inner chamber is readily communicated to the terminals of the crystal unit. This is not easily done since the electrical insulation around the crystal leads also serves as thermal insulation. The problem is analogous to an attempt to maintain some point in an electrical circuit at ground potential, but with
ro other connection to ground than through the insulation.
4-53. A plastic sheath for a single crystal terminal will have a thermal resistance on the order of 800 thermohms- 400 thermohms for each pair of terminals. For an oven that houses four crystal units, even though only one crystal is operating at a time, $R_{18}$ would be on the order of 100 thermohms. This decrease in resistance means only an additional leakage from the heater, and not an increased effectiveness in the control of the temperature of the operating crystal Insofar as the one crystal in operation is concerned, there is still approximately 800 thermohms between each of its terminals and the constant-temperature reservoir, as compared with perhaps an effective resistance of 400 to as low as 10 thermohms between each terminal and the ambient heat reservoir, depending upon the particular type of connection to the external circuit.

4-54. For a small plastic-enclosed, socket-mounted oven, similar to type HD-54/U, approximately 5 cm high, 3 cm wide, and 2 cm deep, the total resistance of the walls and top-the $R_{i}, R_{3}, R_{1 n}, R_{11}$, $R_{12}$ combination-may be assumed to be on the order of 250 thermohms under ambient conditions of room temperature and no forced convection. The total resistance of the base, $R_{12}$, including that of the heater terminals, screws, ground terminal, in parallel with the resistance of the plastic material, can be estimated as approximately 100 thermohms; and this can be assumed to be in series with another 100 thermohms where most of the leakage is through direct contact with the socket. Thus, the total base resistance, but not including the leads from the crystal, itself, can be assumed to be 200 thermohms. The third leakage branch, $R_{16}+R_{15}$, can be assumed to total 600 thermohms. Since the only net flow of heat from the crystal chamber will be the power losses of the crystal, a perfectly designed oven would not have a net circulation of heat from the heater into *one part of the chamber and out anotheri.e. $R_{16}$ would be zero. In the practical case there is a tendency, usually, for the top of the chamber to be warmer than the bottom, so that a net conduction of heat exists from the top to the bottom. Nevertheless, insofar as the heater power is concerned, the crystal-chamber path in parallel with $R_{18}$ can be neglected. Thus, the total thermal resistance, $R_{T}$, can be considered to be that of three branches of 250,200 , and 600 thermohms in parallel, or a total of approximately 95 thermohms when no forced convection is present.
4-55. If it is assumed that the oven temperature
is $75^{\circ} \mathrm{C}$ and that the ambient temperature is $30^{\circ} \mathrm{C}$, then

$$
\mathrm{I}_{2}=\frac{75-30}{95}=0.48 \mathrm{cal} / \mathrm{sec}
$$

or

$$
I_{2}=0.48 \times 4.186=2 \mathrm{watts}
$$

Since there is a difference in temperature of $45^{\circ}$, the power consumption under no-convection conditions averages approximately $2 / 45=.045$ watt for each degree that the ambient temperature is lower than the oven temperature. With the ambient temperature averaging $30^{\circ}$, a 10 -watt heater would be operating one-fifth of the time after the oven had reached equilibrium. Note that this equilibrium condition must hold irrespective of the sensitivity of the thermostat, or the heat capacity of the oven. If the same oven is operated under conditions of moderate forced convection, the total resistance can be more than halved; in which case, the power consumption may increase to as much as a 0.1 -watt average for each degree difference between the ambient and oven temperatures. Under these circumstances, the maximum operating range for a 10 -watt heater is $100^{\circ}$, which is equivalent to a minimum ambient temperature of $-25^{\circ} \mathrm{C}$ for a $75^{\circ} \mathrm{C}$ oven. (At the minimum ambient temperature, the heater circuit closes permanently. A further drop in ambient temperature would be accompanied by an approximately equal drop in the oven temperature.) Even where no forced convection is present, the effective total resistance, $R_{T}$, of an oven tends to decrease as the difference between the operating and ambient temperatures becomes large. This is because the natural convection around the sides and at the top of the oven becomes greater as the temperature gradient at the outer surface becomes steeper. Partially counteracting the decrease in the equivalent air resistance is the fact that the equivalent radiation resistance tends to increase as the ambient temperature falls.

## D-C CIRCUIT BETWEEN THERMOSTAT AND HEATER

4-56. The average crystal oven now in use is built with a hermetically sealed thermostat located either in the crystal chamber, itself (as is generally the case in ovens housing more than one crystal unit), or mounted on top of the chamber in a sealed container that makes good thermal contact with the roof of the chamber. In the former arrangement the temperature deviation can never be reduced below the sensitivity of the thermostat, regardless of how well the rest of the oven is designed, so that high precision in the control
of the temperature cannot be achieved without the use of expensive thermostats. If the temperature deviation is to be reduced to a minimum without excessive cost, the thermostat must be so located that it operates before, rather than after, the temperature in the crystal chamber varies. However, the thermostat cannot be placed between the heater and the outside, for then the heat generator would lie between the crystal and the constant temperature point, $A$, of the d-c circuit, as illustrated in figure 4-15. The average heater temperature, $T_{H}$, and hence, the average crystal temperature, $T_{c}$, would vary with the changes in the IR drop across the resistance ( $\mathrm{R}_{1}$ ) between the heater and the thermostat. Since point $A$ is maintained at a constant average temperature by the thermostat, the current through $\mathrm{R}_{2}$ varies linearly with the ambient temperature. However, since $I_{H}$ also flows through $\mathrm{R}_{\text {; }}$, the heater temperature, $\mathrm{T}_{\mathrm{H}}$ ( $=\mathrm{T}_{\mathrm{A}}+\mathrm{I}_{\mathrm{H}} \mathrm{R}_{1}$ ), must also change linearly with the ambient temperature. Thus, it is necessary that the thermostat either be in nearly direct thermal contact with the heater, or lie between the heater and the crystal. The former arrangement is usually the most to be desired in order to minimize the power requirements as well as the amplitude of the heater temperature cycles.

## A-C CIRCUIT OF OVEN THERMOFILTER

4-57. If the temperaicure cycling amplitude is to be reduced to a minimum before it reaches the crystal, the oven can be designed to make use of a thermofilter. The thermofilter is the analogue of an electrical RC filter that is used to smooth out the ripples of a pulsating d-c voltage. Although a greater percentage of the resistance and capacity of the thermofilter is of a distributed nature than is the case for its electrical analogue, the thermofilter characteristics can be analyzed to a first approximation by assuming that the resistances and capacitances are in a lumped form.


Figure 4-15. Thermal D-C path of heafer-tothermostat when thermostat is outside heater

4-58. Figure 4-16 is a simplified schematic diagram of an oven a-c circuit having a single section thermofilter, where it is assumed that the ambient temperature is at "ground potential" ( $0^{\circ} \mathrm{C}$ ). $\mathrm{R}_{\boldsymbol{A}}$ is the resistance of the air outside the oven, $R_{f}$ is the resistance of the oven between the heater and the outside, $R$ is the input resistance of the filter, $\mathrm{R}_{\mathrm{CO}}$ is the resistance of the crystal chamber, $\mathrm{R}_{\mathrm{CH}}$ is the resistance of the crystal holder, $\mathrm{C}_{0}$ is the capacity of the walls of the oven, $C_{H}$ is the capacity of the heater, $\mathrm{C}_{\mathrm{T}}$ is the capacity of the thermostat, $C$ is the capacity of the filter, $\mathrm{C}_{\mathrm{Cn}}$ is the capacity of the crystal holder, and $C_{C}$ is the capacity of the crystal. In general, in going from $R_{A}$ to $C_{C}$, the resistances become progressively larger, and the capacities become smaller, with the exception of $C$, which should be large. $I_{G}$ is the instantaneous calorie output per second of the heater when operating; $I_{11}$ is the average d-c leakage to the outside, and $I_{A c}$ is the peak a-c current through the filter: The component of the a-c current through $\mathrm{R}_{\mathrm{c}}$ and $\mathrm{R}_{\mathrm{cr}}$ can be assumed to be negligible compared with the total $I_{A c} . \mathrm{T}_{\mathrm{n}}$ is the temperature of the heater.
4-59. The peak-to-peak amplitude of the a-c component of the temperature $T_{11}$ is determined by the backlash of the thermostat, and can be assumed to be constant. In the ideal case, the heater and the thermostat should at all times be at the same


Figure 4-16. Oven thermal A-C circuit

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## Crystal Ovens-Design



Figure 4-17. A-C component of heater temperature
temperature. In practice, there is always a thermal IR drop between the thermostat and the heater, so that the a-c component in temperature at the heater is always greater than the temperature cycle of the thermostat.
4-60. Referring to figure 4-16, if $X_{G}$ is large compared with $\mathrm{I}_{\mathrm{H}}$, the rate at which $\mathrm{C}_{\mathrm{HT}}\left(=\mathrm{C}_{\mathrm{H}}+\mathrm{C}_{\mathrm{T}}\right.$ ) is "charged" can be assumed to be constant, and if the a-c component of the temperature is small compared with the temperature drop between the heater and the outside, the rate at which $\mathrm{C}_{\mathrm{HT}}$ discharges can be assumed to be constant for a constant ambient temperature $\left(0^{\circ} \mathrm{C}\right.$ in the diagram). Thus, the a-c component of $\mathrm{T}_{12}$ can be represented by a saw-tooth wave as indicated in figure 4-17. By a Fourier analysis, such a wave is represented as the resultant of a sine wave of the same fundamental frequency, upon which is superimposed an infinite number of harmonics of varying amplitudes. Insofar as the oven filter circuit is concerned, the only component to consider is the fundamental; for if the thermofilter can attenuate the amplitude of the fundamental below the maximum deviation permissible for the crystal, then certainly the higher harmonics will also be sufficiently attenuated.

## ATTENUATION FACTOR OF THERMOFILTER

4-61. In figure 4-16, $\mathrm{C}_{\mathrm{Hr}}$ can be assumed to be an alternating temperature generator haying a sinewave output at the fundamental frequency of the thermostat cycling, and a peak amplitude of $\mathrm{T}_{\mathrm{Ac}}$. The filter circuit presents an impedance to the heat flow of $\sqrt{\mathrm{R}^{2}+\mathrm{X}_{\mathrm{e}}{ }^{2}}$, where $\mathrm{X}_{\mathrm{C}}$ is the thermal "reactance" of C. If $R$ is assumed to be greater than $10 \mathrm{X}_{\mathrm{C}}$, then $\mathrm{I}_{\mathrm{Ac}}$ can be assumed to approximately equal $T_{A C} / R$. Note that only the peak values of the a-c current and temperature need be considered. The a-c component of the temperature at C will thus be $\mathrm{I}_{A C} \mathrm{X}_{\mathrm{C}}=\mathrm{T}_{A C} \mathrm{X}_{\mathrm{C}} / \mathrm{R}$, so that the attenuation factor is $X_{c} / R$. Since $X_{C}=1 / 2 \pi f C$, where $f$ is the frequency, the attenuation is directly proportional to $\mathrm{R}, \mathrm{C}$, and f . Contributing to the attenuation-indeed, effectively forming two additional RC fiter sections-are the $\mathrm{R}_{\mathrm{cc}} \mathrm{C}_{\mathrm{CH}}$ and the $\mathrm{R}_{\mathrm{CH}} \mathrm{C}_{\mathrm{C}}$ diffusive combinations of the crystal chamber and crystal unit.

THERMOSTAT-HEATER A-C CMRCUIT CHARACTERISTICS AFFECTING FREQUENCY OF TEMPERATURE CYCLE

4-62. The cycling frequency, $f$, depends upon the rate at which $\mathrm{C}_{\mathrm{Hr}}$ charges and discharges. The charging time is inversely proportional to $I_{G}\left(I_{H}\right.$ and $\mathrm{I}_{\mathrm{Ac}}$ assumed to be small by comparison) ; the discharging time is inversely proportional to $\mathrm{I}_{\mathrm{H}}$ ( $\mathrm{I}_{\mathrm{Ac}}$ assumed to be small by comparison); and both the charging and discharging times vary directly with $\mathrm{C}_{\mathrm{ut}}$. Since there is always a resistance path between the heater and thermostat and since the thermostat has a heat capacity separate from $\mathrm{C}_{\mathrm{u}}$, the rise in temperature at the thermostat must lag the rise at the heater. Because of this, $I_{9}$ cannot be made indefiniteiy large, else the rise in temperature at the heater will far overshoot the thermostat cut-off temperature, and $\mathrm{T}_{\mathrm{Ac}}$ will become excessive. Also, the time gained on the charging half of the cycle could be more than lost because of the additional time required for discharge. Thus, the thermostat-to-heater resistance and capacitance are practical factors that limit the frequency and raise the a-c amplitude of the heater temperature. For a minimum $T_{A C}$ and a maximum frequency, the thermostat must be mounted so that the conductance between it and the heater is a maximum. Another factor limiting the maximum practical cycling frequency is the fact that when a bimetallic thermostat is used, it is desirable that the temperature cycles have as long a period as possible, for, in general, the operating life is rated in the number of open-and-closed cycles that can be made before the thermostat becomes over-fatigued, and is not primarily dependent upon the actual number of hours at which the thermostat can be operated.
4-63. Since the oven is purposely designed to make $I_{I I}$ as small as possible, $R_{o}$ and $R_{A}$ cannot be decreased for the sake of increasing the cycling frequency. But if an oven is so constructed that the heat from the heater is evenly distributed on all six sides of the inner chamber, and that a nearperfect conductance exists between the heater and thermostat, the temperature deviation of the crystal at low ambient temperatures can actually be less than that at room ambient temperatures. This is because the consequent increase in $f$, due to the increase in $I_{R}$ and decrease in discharge time, permits greater cycling attenuation by the filter. The frequency, however, can only increase as long as $I_{G}$ remains large compared with $I_{H}$. Otherwise, the decrease in the time of discharge would be annulled by the increase in the time of charge.
4-64. More or less predetermined, is the capacity
of the heater and the metallic surfaces that bound it. Although the outer shield can be made as thin as possible, thereby reducing $\mathrm{C}_{\mathrm{B}}$, the inner wall must be of sufficient thickness to provide a low resistance around the crystal chamber. Representative values of $C_{m}$ for small ovens range from 2.5 to $25 \mathrm{cal} / \mathrm{deg}$, depending principally upon the area of the heater walls, and the thickness of the outer sheath. If $\mathrm{I}_{\mathrm{H}}$ is $0.25 \mathrm{cal} / \mathrm{sec}$ (approximately 1 watt), and $\mathrm{T}_{\mathrm{Ac}}$ is $\pm 5^{\circ} \mathrm{C}$, then the time of discharge of a 6 -cal/deg $\mathrm{C}_{\mathrm{H}}$ (ignoring the thermostat $C_{T}$ ) will be $10 \times 6 / 0.25=240 \mathrm{sec}$, or 4 minutes. If $I_{G}$ is $2.5 \mathrm{cal} / \mathrm{sec}$, the charging time will be $10 \times 6 /(2.5-0.25)$, or approximately 27 sec . Thus, $f$ will be $1 / 267$ cycle per second. Obviously with such a very low frequency, and with $R$ of the filter limited to practical values of, at the most, only a hundred or so thermal ohms, an effective filter would require that an extraordinarily large $C$ be contained in the small volume between the heater and the crystal chamber. However, if the thermostat is in excellent thermal contact with the heater, the effective $T_{A C}$ can be made to approach the actual differential of the thermostat; in which case, not only is the cycling temperature reduced at the source, but the attenuation factor of the filter is improved proportionately by the increase in $f$.

## IDEAL THERMOFILTER

4-65. It should be remembered that heat capacity expresses a change in heat for a change in temperature. In general, the heat capacity of a substance will be different at different temperatures. The average heat capacity of a body between two temperatures $\mathrm{T}_{1}$ and $\mathrm{T}_{2}$ is $\Delta \mathrm{H} /\left(\mathrm{T}_{1}-\mathrm{T}_{2}\right)$, where $\Delta H$ is the thermal energy required to raise the temperature of the body from $T_{2}$ to $T_{1}$. The instantaneous heat capacity at a given temperature is the ratio of an infinitesimal change in thermal energy for an infinitesimal change in temperature, $\mathrm{dH} / \mathrm{dT}$. Now, if at \& particular temperature the thermal equilibrium of a substance suddenly shifts from a state of low potential energy to a state of high potential energy, the addition of a small quantity of heat will be absorbed in raising molecules from the lower to the higher energy level, so that the added energy is principally an increase in potential, rather than in kinetic energy. However, it is the kinetic energy of the molecules that determines the temperature, so that if a small addition of heat is entirely converted into potential energy, dT will be zero, and the instantaneous heat capacity $\mathrm{dH} / \mathrm{dT}$ will be infinite.
4-66. In this manner a very large $C$ can be ob-
tained for a thermofilter if a substance is chosen that undergoes a reversible change of state at the operating temperature of the oven. Obviously a non-reversible action would be unsatisfactory, such as the decomposition of a compound, since it is necessary that the same process be repeated during each temperature cycle. Such changes of state as occur at the transition of a crystal from one lattice structure to another, or at the melting and boiling points of substances that do not decompose would permit very high values of C for a small quantity of the material.
4-67. The largest $C$ for a given quantity of substance can be obtained at a boiling point, since the heats of vaporization are generally much greater than the heats of fusion or transition. But the problem of cooling the distillate and returning it to the heated chamber would require an expensive and cumbersome oven. Since heats of fusion are generally much higher than heats of transition, are absorbed during narrower temperature ranges, and are more easily found at a desired operating temperature, a large thermofilter capacity effective at the operating temperature appears to be more readily obtainable by surrounding the crystal chamber with a solid having its melting point within the differential range of the thermostat, but slightly higher than the operating mean. If the meiting solid has a very sharp melting point, there is a danger that the mean temperature may rise above the melting point long enough to completely melt the solid, thereby losing the major filtering effect. To remove this danger, the filter can be composed of a mixture of two or more compounds of different melting points, so that, at equilibrium, the densities of the compounds relative to each other will be different in the solid and liquid phases of the partly melted mixture. Although the filtering effect will be diminished, the melting temperature will automatically tend to rise with the mean heater temperature as more of the mixture fuses.
4-68. The substance to use for an ideal heat reservoir, other than one having a melting point at the desired operating temperature, would be a stable electrical insulator having little tendency to react with metal, a low density, a large heat of fusion, a prompt rate of melting and crystallization, a low dielectric constant, a low cost of production, and not be difficult or disagreeable to handle. Recent experiments by C. P. Saylor and R. Alvarez of the National Bureau of Standards indicate the probable suitability of para-dibromobenzene.
4-69. The fact that a number of possible filter elements have a large percentage volumetric ex-
pansion on fusion suggests the interesting possibility of employing the expansion to open the heater circuit when the filter material is partially melted. A pure fusing element could thus, theoretically, provide thermostatic action by virtue of a cycling internal-enegry differential, rather than a cycling temperature differential. In other words, a change in the temperature of the sensing element of the thermostat would not be an absolute requirement in the ideal case.

4-70. To shorten the warm-up time and to minimize temperature gradients, good thermal conductivity should be maintained within a melting-point thermofilter reservoir; if necessary, by the use of wire mesh or radial fins. However, no through high-conductivity path should be permitted. A relatively high-resistance surface barrier should insulate the inner side of the reservoir from the side nearest the heater.

## WARM-UP CIRCUIT OF OVEN

4-71. The warm-up circuit of the oven consists primarily of the thermofilter and thermostatheater circuit shown in figure 4-16. Arbitrarily, we shall define the warm-up time to be the period required to bring the temperature of the crystal chamber to within 1 per cent of its mean operating value after the heater is first turned on. As a first approximation, this period can be divided into two parts. The first part consists of the time required for the heater, viewed as a constant-current generator, to charge the heater and thermostat capacities, $\mathrm{C}_{\mathrm{II}}$ and $\mathrm{C}_{\mathrm{T}}$, to the operating temperature. The second part consists of the additional time required to bring the crystal chamber to within 1 degree of the operating temperature. Normally, a booster heater is provided which permits the first part of the warm-up time to be shortened to as much as one-fourth or more of the time that would otherwise be required. Letting $\mathrm{C}_{\mathrm{Ht}}$ in cal/deg equal the sum of $\mathrm{C}_{\mathrm{H}}$ and $\mathrm{C}_{\mathrm{T}}, \mathrm{I}_{\mathrm{N}}$ in $\mathrm{cal} / \mathrm{sec}$ equal the average net rate of heat supplied the oven during the initial heating period (this can be assumed to be the total power from the two heaters minus one-half the average operating power after equilibrium has been reached), and $\Delta T$ equal the difference between the operating and ambient temperatures, the first part of the warm-up time is approximately

$$
\begin{equation*}
\mathrm{t}_{1}(\text { in sec })=\mathrm{C}_{\mathrm{HT}} \Delta T / \mathrm{I}_{\mathrm{N}} \tag{1}
\end{equation*}
$$

4-72. To the extent that a crystal oven can be represented by the thermofilter circuit in figure $4-16$, the second part of the warm-up time can be broadly generalized as the time required for
the capacity, C , to acquire $100\left(\Delta \mathrm{~T}-1^{\circ}\right) / \Delta \mathrm{T}$ per cent of its warm-up heat. To simplify the problem, we shall assume that no heat flows into C until after the first part of the warm-up period is completed. As in an electrical circuit, the product, RC , is a time constant equal to the time required for the capacity to receive 63 per cent of its equilibrium charge when connected in series with the resistance and a constant potential source. To receive $100\left(\Delta \mathrm{~T}-1^{\circ}\right) / \Delta \mathrm{T}$ per cent of its equilibrium charge will require a time

$$
\mathrm{t}_{2}(\text { in } \sec )=-\mathrm{RC} \log \left(\frac{1^{\circ}}{\Delta \mathrm{T}}\right) \quad 4-72(2)
$$

Thus, the total warm-up time by rule-of-thumb approximation is

$$
\begin{equation*}
t \approx t_{1}+t_{2}=\frac{C_{H T} \Delta T}{I_{N}}-R C \log e\left(\frac{1^{\circ}}{\Delta T}\right) \tag{3}
\end{equation*}
$$

Equation 4-72 (3) is only approximate when $t_{1} \ll t_{2}$ and when $C$ is large compared with the distributed capacity of $R$. If $C$ is attributable entirely to the distributed capacity of an insulating baffle, equation 4-72 (3) is not applicable-unless C and R are prorated from the distributed parameters. If only a general indication of the warm-up time is desired, let $R$ equal the steady-state resistance, and let C equal one-half the actual total capacity of the baffle. The actual warm-up time of the crystal blank itself is a variable that will depend upon the fabrication of the crystal unit and its drive level. For most purposes it can be assumed that, with the aid of the crystal driving power, the temperature of the crystal blank will not significantly lag the rise in temperature of the crystal chamber during the warm-up period. Approximate values of $-\log _{e}\left(1^{\circ} / \Delta \mathrm{T}\right)$ for representative values of $\Delta \mathrm{T}$ are given in the following table.

| $\Delta T$ | $-\log _{e}\left(1^{\circ} / \Delta T\right)$ |
| :---: | :---: |
| 3 | 1.0 |
| 5 | 1.6 |
| 10 | 2.3 |
| 20 | 3.0 |
| 30 | 3.4 |
| 40 | 3.7 |
| 50 | 3.9 |
| 60 | 4.1 |
| 70 | 4.3 |
| 80 | 4.4 |
| 90 | 4.5 |
| 100 | 4.6 |

## Pin-fo-Pin Electrical Capacirance of Crystal Oven

$4-73$. It should be remembered that the pin-topin capacitance of the oven is not necessarily the capacitance that the oven adds to the shunt capacitance of the crystal unit. For example, in figure $4-18$, assume that $C_{1}$ and $C_{2}$ are both $4 \mu \mu$ and that $\mathrm{C}_{3}$ is $2 \mu \mu \mathrm{f}$. It can be seen that if neither pin is grounded, the total pin-to-pin capacitance is $4 \mu \mu \mathrm{f}$; but if one pin is grounded, the total pin-to-pin capacitance is $6 \mu \mu \mathrm{f}$. Also, it can be seen when a crystal unit is inserted in its oven socket, that although the pin-to-pin capacitance of the oven is shunted across the crystal, the crystal shunt capacitance does not increase by that same amount. In effect, since the crystal pins are shielded by the oven receptacles, the oven capacitance substitutes for, rather than adds to the external pin-to-pin capacitance of the crystal unit.

## Base Leokrage of Smelf Ovens

4-74. The smaller the crystal oven, the more difficult it becomes to control the chamber temperature, not only because the surrounding heat capacity becomes smaller, but also because the percentage of heat leakage through the base becomes greater, resulting in steeper temperature gradients within the crystal chamber. Improved performance can generally be obtained by concentrating more than an average proportion of the heater windings near the base. An interesting and very successful innovation in this direction occurs in a recert oven design by B. C. Hill, Jr. of HEEMCO. In the Hill oven, the heater windings are extended around the base leads, which therefore are maintained at essentially the heater temperature and so exhibit much less tendency to


Figure 4-18. Pin-to-pin electrostatic capacitance of crystal oven
follow the changes in the ambient temperature. An entirely different approach, one which ingeniously exploits the fact that the temperature at the base changes more rapidly than at any other part of the oven, has been introduced by R. Beetham of the James Knights Company. The Beetham principle, which has been applied in the design of miniature crystal ovens, is to locate the thermostat at the base and in good thermal contact with it. This arrangement virtually eliminates the existence of steep temperature gradients within the crystal chamber; in addition, because the temperature of the base-mounted thermostat changes relatively rapidly, it permits the cycling frequency to be much higher than otherwise, thereby diminishing the amount of heat capacity required to attenuate the a-c component of temperature at the crystal. Both the base-heater and base-thermostat methods permit eycling temperatures at the crystal to be reduced to a few tenths of a degree C as the ambient temperature varies from $-55^{\circ} \mathrm{C}$ to operating temperatures of 75 or $85^{\circ} \mathrm{C}$.

PART II
technical descriptions of crystal ovens
TECHNICAL DATA CHART OF CRYSTAL OVENS FOR USE WITH GROUP-I MILITARY STANDARD CRYSTAL UNITS

| Mil Std Xtal <br> Holder <br> Accom- <br> modated | No. of <br> Holders <br> Accom- <br> modated | Military or <br> Commercial <br> Typeor <br> Dwg No. | Oven <br> Operating <br> Tempera- <br> ture ( $\left.{ }^{\circ} \mathrm{C}\right)$ | Ambient <br> Temp <br> Range <br> $\left({ }^{\circ} \mathrm{C}\right)$ | Max <br> Temp <br> Heviation <br> $\left({ }^{\circ} \mathrm{C}\right)$ | Heater <br> Voltage <br> (V) | Provisions for Mounting <br> Oven |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | HD-54/U | 75 | -55 to +55 | $-7,+6$ | 27.5 dc | Standard lock-in base |



Figure 4-19. Crystal Oven HD-54/U

## FUNCTIONAL DESCRIPTION

Crystal Oven HD-54/U provides temperature stabilization for a single $\mathrm{HC}-6 / \mathrm{U}$-mounted crystal unit at a nominal operating temperature of $75^{\circ} \mathrm{C}$, over an ambient range of $-55^{\circ} \mathrm{C}$ to $+55^{\circ} \mathrm{C}$. The oven operates on a heater voltage of 27.5 volts, dc, and mounts in a standard lock-in socket. A booster thermostat with associated heating element is incorporated in the oven to shorten the warm-up period.

## OPERATING CHARACTERISTICS

Operating Temperature: $75^{\circ} \mathrm{C}$
Temperature Deviation: $-7^{\circ}$ to $+6^{\circ} \mathrm{C}$
Ambient Temperature Range: $-55^{\circ}$ to $+55^{\circ} \mathrm{C}$
Approximate Warm-Up (stabilization) Time: 6 min
Oven Temperature (inside crystal holder) During Warm-Up Time:

| Oven Temp | Warm-up Time |
| :--- | :---: |
| $90^{\circ} \mathrm{C}$ max | c to 3 min |
| $65^{\circ}$ to $85^{\circ} \mathrm{C}$ | 3 to 4 min |
| $68^{\circ}$ to $81^{\circ} \mathrm{C}$ | over 4 min |

Power Requirements: 27.5 V , dc; 1.5 amp


Figure 4-20. Dimensions of Crystal Oven HD-54/U PHYSICAL CHARACTERISTICS
Net Weight: 2 oz
Thermometer: None
Provisions for Temperature Adjustment: None
Oven Materials: Plastic cover and base
Provisions for Mounting Oven: Standard lock-in base
Oven Will Accommodate: One Crystal Holder HC-6/U

## LOGISTICAL DATA

Army-Navy Nomenclature: Crystal Oven HD54/U

## Status:

Date of Status:
Cognizant Agency:
Govt. Specifications:
USAF Stock Class:
USAF Stock No.:
Source of Supply:* Bendix Radio; Clark (commercial equivalent: Clark CO-10) ; Downing (commercial equivalent: Downing Single Crystal Unit Oven); Miller Labs (commercial equivalent: Miller Labs BM-100)

* See Appendix III for complete name and address.


Figure 4-21. Dimensions of Bendix Radio Crystal Oven 1205628


Figure 4-22. Bendix Radio Crystal Oven L205628

## FUNCTIONAL DESCRIPTION

The Bendix Radio L205628 Crystal Oven is a multiple oven designed to provide temperature stabilization at $75^{\circ} \mathrm{C}$, nominal, over an ambient range of $-55^{\circ} \mathrm{C}$ to $+55^{\circ} \mathrm{C}$. Up to five $\mathrm{HC}-6 / \mathrm{U}-$ mounted crystal units can be accommodated. The oven operates from a heater voltage of 27.5 volts, dc. It was originally designed for use in Radio Sets AN/ARC-19 and AN/ARC-33.

OPERATING CHARACTERISTICS
Operating Temperature: $75^{\circ} \mathrm{C}$
Temperature Deviation: $-10^{\circ}$ to $+6^{\circ} \mathrm{C}$

Ambient Temperature Range: $-55^{\circ}$ to $+55^{\circ} \mathrm{C}$
Approximate Warm-Up (stabilization) Time: 7 min
Oven Temperature (inside crystal holder) During Warm-Up Time:

| Oven Temp | Ambient Temp | Warm-up Time |
| :--- | :---: | :---: |
| $90^{\circ} \mathrm{C} \max$ | $+20^{\circ}$ to $+55^{\circ} \mathrm{C}$ | 0 to 3 min |
| $60^{\circ}$ to $85^{\circ} \mathrm{C}$ | $+20^{\circ}$ to $+55^{\circ} \mathrm{C}$ | 3 to 4 min |
| $68^{\circ}$ to $81^{\circ} \mathrm{C}$ | $+20^{\circ}$ to $+55^{\circ} \mathrm{C}$ | over $4 \min$ |
| $90^{\circ} \mathrm{C} \max$ | $-65^{\circ}$ to $+20^{\circ} \mathrm{C}$ | 0 to 3 min |
| $60^{\circ}$ to $85^{\circ} \mathrm{C}$ | $-55^{\circ}$ to $+20^{\circ} \mathrm{C}$ | 3 to $5 \min$ |
| $65^{\circ}$ to $81^{\circ} \mathrm{C}$ | $-55^{\circ}$ to $+20^{\circ} \mathrm{C}$ | over 5 min |

Power Requirements: $27.5 \mathrm{~V}, \mathrm{dc} ; 1.5 \mathrm{amp}$

## PHYSICAL CHARACTERISTICS

Net Weight: 7 oz
Thermometer: None
Provisions for Temperature Adjustment: None Oven Materials: Metallic cover, plastic base
Provisions for Mounting Oven: Four thd studs on $11 / 2 \times 13 / 4 \mathrm{in} . \mathrm{mtg}$ centers
Oven Will Accommodate: Five Crystal Holders HC-6/U

## LOGISTICAL DATA

Source of Supply:* Bendix Radio (Dwg No. L205628) ; Downing (commercial equivalent:
Downing Five Crystal Unit Oven)

* See Appendix III for complete name and address.


Figure 4-23. Dimensions of Bendix Radio Crystal Oven 205651


Figure 4-24. Bendix Radio Crystal Oven N205651

## FUNCTIONAL DESCRIPTION

The Bendix Radio N205651 Crystal Oven is a multiple oven designed to provide temperature stabilization at $75^{\circ} \mathrm{C}$, nominal, for up to thirteen $\mathrm{HC}-6 / \mathrm{U}$-mounted crystal unite in ambient termperatures from $-55^{\circ} \mathrm{C}$ to $+55^{\circ} \mathrm{C}$. The oven overates from a heater voltage of 27.5 volts, dc. It was originally designed for use in Radio Sets AN/ ARC-19 and AN, ARC-33.

## OPERATING CHARACTERISTICS

Operating Temperature: $75^{\circ} \mathrm{C}$
Temperature Deviation: $-10^{\circ}$ to $+6^{\circ} \mathrm{C}$

Ambient Temperature Range: $-55^{\circ}$ to $+55^{\circ} \mathrm{C}$
Approximate Warm-Up (stabilization) Time: 7 min
Oven Temperature (inside crystal holder) During Warm-Up Time:

| Oven Temp | Ambient Temp | Warm-up Time |
| :--- | :---: | :---: |
| $90^{\circ} \mathrm{C}$ max | $+20^{\circ}$ to $+55^{\circ} \mathrm{C}$ | 0 to 3 min |
| $60^{\circ}$ to $85^{\circ} \mathrm{C}$ | $+20^{\circ}$ to $+55^{\circ} \mathrm{C}$ | 3 to 4 min |
| $68^{\circ}$ to $81^{\circ} \mathrm{C}$ | $+20^{\circ}$ to $+55^{\circ} \mathrm{C}$ | over 4 min |
| $90^{\circ} \mathrm{C}$ max | $-55^{\circ}$ to $+20^{\circ} \mathrm{C}$ | 0 to 3 min |
| $60^{\circ}$ to $85^{\circ} \mathrm{C}$ | $-55^{\circ}$ to $+20^{\circ} \mathrm{C}$ | 3 to 5 min |
| $65^{\circ}$ to $81^{\circ} \mathrm{C}$ | $-55^{\circ}$ to $+20^{\circ} \mathrm{C}$ | over 5 min |

Power Requirements: $27.5 \mathrm{~V}, \mathrm{dc} ; 1.5 \mathrm{amp}$

## PHYSICAL CHARACTERISTICS

Net Weight: 10 oz
Thermometer: None
Provisions for Temperature Adjustment: None Oven Materials: Metallic cover, plastic base Provisions for Mounting Oven: Four the studs on $13 / 4 \times 213 / 10$ in. mtg centers
Oven Will Accommodate: Thirteen Crystal Holders HC-6/U

## LOGISTICAL DATA

Source of Supply:* Bendix Radio (Dug No. N205651) ; Downing (commercial equivalent:
Downing Thirteen Crystal Unit Oven)

* See Appendix III for complete name and address.


## APPENDIXES

## APPENDIX I-ACKNOWLEDGMENTS

The information contained in this handbook has been gathered from so many diverse sources that it is virtually impossible to give due credit in each particular instance. Especially is this true of the first half of Section I, where much of the information consists of collections of relatively independent facts. In the last half of Section I, it is hoped that specific experimental data, as well as equations and methods of analysis that can be explicitly ascribed to individual authors, have been more adequately acknowledged in the text. The writer wishes to thank the many crystal manufacturers who have cooperated so generously in supplying information and suggestions for inclusion in the Handbook. He is particularly indebted to Bliley Electric Company, HEEMCO, Hunt Corporation, Hupp Electronics Company, McCoy Electronics Company, and Reeves-Hoffman Company for their contributions and interest and also for the personal courtesies extended the writer during a data-collecting field trip.

At this point, the writer would like to ackowledge those individuals and organizations to whom he is most indebted for the present contents of the Handbook.

Bell Telephone Laboratories,-The greater part of the information on the subject of crystal-unit fabrication contained in the Handbook has, at least partly, had its origin in research projects at Bell Telephone Laboratories. All frequency-constant, temperature-coefficient, and frequency-deviation curves of the various crystal elements developed at Bell Telephone Laboratories have been obtained from graphs made available to the public by the Bell Telephone Company. These illustrations are included below in the individual acknowledgements of published works of Bell scientists.

Bokovoy, S. A.-Most of the descriptive data concerning the $V$-cut crystal, the single-frequency X-cut crystal, and the dielectric-sandwich type of
crystal mounting have been obtained from U.S. and British patents issued to the inventor, Mr. Bokovoy, of the Radio Corporation of America.
(Mr. P. D. Gerber was coinventer of the dielectricsandwich mounting-U. S. Patents $2,078,229$ and $2,101,893$.) Handbook illustrations redrawn from Bokovoy patents are: figure 1-22 (U. S. Patent $2,064,288$, May 31, 1934) ; figures 1-39, 1-40, and 1-41 (British Patent 457,342, November 26, 1936) ; figures $1-73$ to 1-77 (U. S. Patent 2,101,393, December 14, 1937) ; and figure 1-78 (U. S. Patent 2,078,229, April 27, 1937).

Bond, W. L.-Two treatises by Mr. Bond, "Methods for Specifying Quartz Crystal Orientation and Their Determination by Optical Means" and "Sawing, Grinding, and Lapping" (Chapters II and 1X, respectively, Quartz Crystals for Electrical Circuits, Heising) have been useful sources of information to the writer. Handbook figure 1-59 has been reprinted from the former article with the permission of the publisher, D. Van Nostrand Co.

Borgelt, E. H,-See Foreword.
Bottom, V, E.-Much of the information contained in "The Mathematics of the Equivalent Electrical Circuit of the Quartz Crystal Unit" by Mr. Bottom (Chapter II, Fundamental Principles of Crystal Oscillator Design, Circuit Section, Long Branch Signal Laboratory, Signal Corps, 1945-46) has been incorporated in Section I of the Handbook.

Bower, G. G.-Information obtained from Mr. Bower's treatise, "Crystal-Controlled ElectronCoupled Oscillators" (Chapter V, Fundamental Principles of Crystal Oscillator Design, Circuit Section, Long Branch Signal Laboratory, Signal Corps) has been included in the Handbook.

Brown, W. F.-Information contained in "Quartz Crystal Overtone Oscillators," Technical Note No. RAD. 460, by Mr. Brown, Royal Aircraft Establishment, Farnborough, has been of great value to the writer in preparing the discussion of seriesmode oscillators.

Cady, W. G.-So much of information contained in the Handbook is indirectly, if not directly, dependent upon the work of Dr. Cady that no attempt

## Appendix I

## Acknowledgments

can be made to itemize particular instances, other than to acknowledge that figure $1-21$ is reprinted from Dr. Cady's textbook, Piezoelectricity, Mc-Graw-Hill Book Co., 1946, with the permission of the author and publisher.
Camfield, C. J.-Information obtained from "The Design of Fundamental Mode Quartz Crystal Oscillators," Technical Note No. RAD. 525, by Mr. Camfield, Royal Aircraft Establishment, Farnborough, has been included in the Handbook. Handbook figure 1-131 is based upon the design of an age circuit described in the above treatise.

Capitol Radio Engineering Institute.-The writer is indebted to Capitol Radio Engineering Institute for many valuable items of information scattered throughout the Handbook. Of particular note are the empirical data contained in the discussion of the use of the Miller circuit as a small power oscillator (paragraph 1-339).

Carpantier, V. J.-See Foreword.
Caruthers, R. S.-The writer is indebted to Mr. Caruthers for information contained in paragraphs 1-449 to 1-451, which has been obtained from a treatise on transistor oscillators as published in The Transistor by Bell Telephone Laboratories. Handbook figures 1-189 and 1-190 have been copied from this source with the permission of Bell Telephone Laboratories.

Devlin, J. J.-Appreciation is extended Mr. Devlin for valuable assistance in editing parts of Sections 1I, III, IV, V, and the Appendix.

D'Heedene, A. R.-.The treatise, "Effects of Manufacturing Deviations on Crystal Units for Filters" (Chapter XIV, Quartz Crystals for Electrical Circuits, Heising), by Mr. D'Heedene, has proven a valuable source of information to the writer. Handbook figure 1-117 has been copied from an illustration contained in the above work with the permission of the publisher, D. Van Nostrand Co.
Drews, W. F. et al.-The treatise by Mr. Drews and coauthor A. E. Swickard, "The Wire Mounted Crystal Unit" (Chapter XVI, Quartz Crystals for Flectic Ciruits, Heising), has been an important source of information for the writer. Handbook figure 1-68 has been drawn from an illustration contained in the above articie, with the permission of the publisher, D. Van Nostrand Co.

Edson. W, A. et al.-For that part of Section I covering the theory and application of series-mode quartz erystal oscillators, the writer is heavily indebted to the work of Mr. Edson and those assisting him at the Ceorgia Institute of Technology
in a Signal Corps research project directed toward the investigation of v-h-f crystal oscillators. Many of the results of this investigation, as described in the 1950 Final Report on Signal Corps Contract W36-039-sc-32100, "High Frequency Crystal-Controlled Oscillator Circuits," prepared by Mr. Edson, W. T. Clary, and J. C. Hogg, Jr., have been included in the discussions of the Butler, transitron, basic transformer-coupled, grounded-grid, grounded-plate, and impedance-inverting oscillators. Also, the circuit equations derived in the h-f oscillator report have provided valuable check points and guides for the circuit analyses and equation derivations of this Handbook. In addition, all equations presented without derivations in the discussion of the above-mentioned oscillators can be assumed to have been taken directly from the above-mentioned $h$-f oscillator report.

The writer has also been greatly aided by the information contained in the timely book by Mr. Edson, Vacuum-Tube Oscillators, copyright 1953, John Wiley and Sons. The analysis of the Meacham bridge oscillator contained therein has served as the principal guide for the slightly modified approach to the same circuit followed in the Handbook. Appreciation is extended to the author and publishers for permission to use the graphical chart shown in the Handbook figure 1-162.

Fair, I. E.-The writer is indebted to the work of Mr. Fair for information concerning the relative performance characteristics of crystal units in parallel-mode oscillator circuits, as described in "Piezoelectric Crystals in Oscillator Circuits" (Chapter XII, Quartz Crystals for Electrical Circuits, Heising), and in "Design Data on Crystal Controlled Oscillators" (Appendix 11, Information Bulletin on Quartz Crystal Units, Armed Services Electro Standards Agency, Fort Monmouth, N. J., August, 1952). Figure 1-164 of the Handbook has been copied from the latter treatise. The crystal performance parameters, $M$ (figure of merit) and PI (performance index), were originally conceived and defined by Mr. Fair.

Goldsmith, P.-Appreciation is extended for the time and assistance generously given the writer in obtaining information relating to the results of experiments conducted at the Armour Research Foundation of Illinois Institute of Technology (USAF Contract No. AF 18 (600)-157) on par-allel-mode crystal oscillators, in which Mr. Goldsmith had participated as project engineer.

Gordon, S. G. et al.-Information used in the Handbook concerning the preparation of crystal blanks has been obtained from the treatise by Mr. Gordon
and Mr. W. Parrish, entitled "Cutting Schemes for Quartz Crystals" (American Mineralogist Symposium on Quartz Oscillator Plates, 1945). Handbook figures 1-60 and 1-62 have been copied from this source.
Greenidge, R. M. C.-."The Mounting and Fabrication of Plated Quartz Crystal Units" (Chapter XIII, Quartz Crystals of Electrical Circuits, Heising), by Mr. Greenidge, has proven an important source of information for the writer. Handbook figures 1-80, 1-83, and 1-86 have been drawn from illustrations contained in the above article with the permission of the publisher, $D$. Van Nostrand Co.

Gruen, H. E.-Of great value to the Handbook has been the circuit data obtained from Mr. Gruen for over thirty oscillators of comparatively recent design which employ currently recommended crystal units. This information was originally catalogued and the circuits tested during a preliminary investigation of the feasibility of standard packaged oscillator designs-a project engineered for the U. S. Air Force by Mr. Gruen at the Armour Research Foundation of Illinois Institute of Technology, with Mr. E. A. Roberts serving as Instrument Supervisor. The writer also wishes to thank Mr. Gruen for giving so generously of his time in helping the writer check test data for inclusion in the Handbook.

Hedeman, W. R.-The method of synthesizing frequencies, as described in paragraphs 1-455 to $1-462_{2}$ is based upon the Bendix synthesizing method described by Mr. Hedeman in "Few Crystals Control Many Channels," Electronics magazine, March, 1948.

Heising, R. A.-The subject matter on the fabrication of quartz crystal units in the Handbook is more dependent upon the information in Mr . Heising's Quartz Crystals for Electrical Circuits, D. Van Nostrand Co., copyright 1946, than upon that in any other single publication. Because this collection of articles by members of the technical staffs of Bell Telephone Laboratories and Western Electric Company represents so much of the original discovery, work, and thought that has formed the foundation of the modern quartz-crystal industry in the United States, the book has been invaluable as a reference in the preparation of the Handbook. The many performance curves of the different types of quartz cuts pioneered by Bell Laboratories have proven of particular value. Mr. Heising has also been the source of much of the information concerning the historical development of piezoelectric crystals. The following
figures of the Handbook have been reprinted, copied, drawn, or redrawn-entirely, in part, or in modified form-with the permission of Mr. Heising and D. Van Nostrand Co. from illustrations appearing in the aforesaid publication: 1-5, 1-8, 1-11, 1-12, 1-13, 1-19 (G), 1-23, 1-24, 1-25, 1-28, $1-29,1-33,1-34,1-35,1-38,1-43,1-44,1-53,1-54$, $1-56,1-58,1-59,1-63,1-65,1-68,1-71,1-80,1-81$, $1-82,1-83,1-84,1-86,1-87$, and 1-117.

Henry, C, W.-See Foreword.
Institute of Radio Engineers-I.R.E. Standards on Piezoelectric Crystals, as described in the Proceedings of the I.R.E., vol. 37, No. 12, December, 1949, have been followed in the Handbook.

Jakob, M.-Heat Transfer, Vol. I, by M. Jakob, copyright 1949, John Wiley and Sons, proved of great value to the writer as a basic reference source during the preparation of the discussion on crystal-oven design in Part I, Section IV of the Handbook.

Jones, M. B.-The writer is indebted to Mr. Jones for many suggestions for improving the usefulness and appearance of the Handbook, and for contributing freely of his time in designing and preparing the layout of the printed manuscript.

Kitter, W. M.-Appreciation is extended Mr. Kitter for valuable assistance in editing and correcting a number of illustrations, data sheets, and tables in Sections II and III.

Koga, I.-The writer has been greatly benefited by a number of equations (acknowledged in the text) derived by Mr. Koga in the treatise "Characteristics of Piezo Electric Quartz Oscillators," Proceedings of the I.R.E., vol. 18, 1930.

Llewellyn, F. B.-Of great aid to the writer has been "Constant-Frequency Oscillators,"' F. B. Llewellyn, Proceedings of the I.R.E., vol. 19, 1931.

Lobel, A.-The writer is considerably indebted to Mr. Lobel for valuable assistance in preparing, organizing, and editing data sheets and tables appearing in Sections 11, III, IV, V, and the Appendixes.
Magie, W. F.-The writer is indebted to Mr. Magie for the translation of the original paper by $\mathbf{P}$. Curie on "Piezoelectricity." The translation contained in the Handbook has been reprinted from A Source Book in Physics, W. F. Magie, copyright 1935, McGraw-Hill Book Co., with the permission of the author and publisher.

Mason, W. P.-Much of the descriptive information contained in Section I covering the theory

## Appendix I

## Acknowledgments

of piezoelectricity and the characteristics of piezoelectric elements is based upon information obtained in the published treatises of Mr. Mason. From Piezoelectric Crystals and Their Application to Ultrasonics, copyright 1950, D. Van Nostrand Co., has been obtained most of the information regarding the different types of synthetic piezoelectric crystals as well as a part of the data concerning the X-group of quartz crystals. Figures $1-20,1-32$, and $1-55$ of the Handbook have been reprinted entirely or in part from Mr. Mason's book with the permission of the author and the publisher. Equations 1-248 (1) and (2) have also been obtained from this source.

From "Low Temperature Coefficient Quartz Crystals," Bell System Technical Journal, January, 1940, permission has been obtained from the author and publisher to use the curves illustrated in Handbook figures 1-45 and 1-46.

The theory of quartz piezoelectric properties, presented in paragraphs 1-69 to 1-74, is based primarily upon Lord Kelvin's model of the quartz molecule, as extended by Mason to illustrate a simplified concept of quartz piezoelectricity in "Quartz Crystal Applications" (Chapter I of Quartz Crystals for Electrical Circuits, Heising). From this same article has been obtained much of the general information relating to the various types of quartz cuts, as well as the following Handbook illustrations: figures 1-8, 1-9 (originally from Collected Works of Lord Kelvin, Cambridge Press), 1-11, 1-19 (G), 1-43, 1-44, 1-53, 1-54, and 1-56.

A large part of the information concerning the characteristics of the X-group of quartz crystals has been obtained from "Low-Frequency QuartzCrystal Cuts Having Low Temperature Coefficients" (Chapter XVII of Quartz Crystals for Electrical Circuits, Heising), of which Mr. Mason is coauthor with Mr. R. A. Sykes. From this source have been obtained figures 1-23, 1-24, 1-25, 1-28, 1-29, 1-33, 1-34, 1-35, 1-38.

Equation 1-82 (1) is a modification of an equation developed by Mr. Mason in "Electrical Wave Filters Employing Quartz Crystals as Elements," Bell Sustem Technical Journal, July, 1934.

Miller, C. J., Jr.-The writer has greatly benefited by two treatises by Mr. Milier: "Equivalent Network of a Quartz Crystal Unit and Its Application" and "The Pierce Oscillator," which appear as chapters 1 and III, respectively, in Fundamental Principles of Crystal Oscillator Design, Circuit Section, Long Branch Signal Laboratory, Signal Corps, 1945-46. The approach to the generalized erystal oscillator and the methods discussed for
measuring vacuum-tube-circuit capacitances have proved particularly useful. Figure 1-100 of the Handbook has been traced from one Miller illustration, and figure $1-103$ is a modification suggested by another.

Nachman, M. W.-See Foreword.
Philco Corporation.-Regrettably, space simply does not permit acknowledgments of the many personal contributions to the composition of this Handbook that have been made by Philco personnel, but for which the writer nevertheless wishes to express his sincere appreciation. Without the good faith and cooperation of the management and staff of the Philco Technical Publications Department, in particular, this Handbook would not have been possible.

Prichard, A. C.-Information obtained from Mr. Prichard's treatise "The Miller Oscillator" (Chapter IV, Fundamental Principles of Crystal Oscillator Design, Circuit Section, Long Branch Signal Laboratory, Signal Corps) has been included in the Handbook.

Roberts, E. A. et al.-Appreciation is felt for the assistance and many courtesies extended the writer when collecting data originally obtained in experiments performed under the supervision of Mr. Roberts at the Armour Research Foundation of the Illinois Institute of Technology. Of particular value has been the information concerning the performance of parallel-mode oscillators that is contained in the interim report on USAF research Contract No. AF 18(600)-157, "Investigation of Oscillator Circuits for Proposed Standards," June 22, 1953. Copies of illustrations from this report are shown in figures 1-129, 1-130, 1-143, 1-144, 1-145, 1-146, 1-147, and 1-148. Research engineers contributing materially to the project were E. K. Novak, P. Goldsmith, and I. Kurinsky.

Robinson, S. A. et al.-The discussion of capaci-tance-bridge oscillators is based primarily upon the final report, "H. F. Harmonic Crystal Investigation," of an Air Force research project undertaken by the Research Division of Philco Corporation in 1947 (AF Contract No. W33-038-ac-14172), with Messrs. Robinson, C. D. O'Neal, and F. N. Barry serving as project engineers. Handbook figures 1-112, 1-113, 1-114, 1-165 (A), 1-166, 1-167, 1-168, 1-169, 1-170, 1-171, and 1-172 have been copied from this report.

Ronan, J. A.-Part of the information concerning the plating of crystals has been obtained from Mr. Ronan's technical report, "Fabricating Tech-
niques for Crystal Unit CR-23/U," Signal Corps Engineering Laboratories.
Schnepps, B.-The writer is greatly indebted to the conscientious work of Mr. Schnepps in preparing, organizing, and editing data sheets and tables appearing in Sections II, III, IV, V, and the Appendixes.
Signal Corps-The writer wishes to thank Mr. W. L. Doxey, Chief, and others of the staff at the Frequency Control Branch, Signal Corps Engineering Laboratories, Fort Monmouth, N. J., for their cooperation in making available a large amount of useful bibliographical material. With their assistance, it has been possible to consult a much broader range of publications, illustrations, and reports than would otherwise have been possible.

It should be mentioned that from the Signal Corps Technical Manual, TM-2540, Quartz Crystals, Theory, Fabrication and Performance Meas"/rements, much of the information concerning the fabrication of quartz crystal units has been obtained. The following Handbook illustrations have been obtained from this manual: figures $1-5,{ }^{*} 1-6$, 1-10,* 1-42, 1-57,* 1-58,* 1-59,* 1-63,** 1-64, 1-66,* $1-67$, and $1-89$. Those figures marked with an asterisk have been obtained from negatives made available by the Signal Corps.

Also of great use to the writer has been the Information Bulletin on Quartz Crystal Units, Armed Services Electro Standards Agency, Fort Monmouth, N. J. See Fair, I. E. and Sykes, R. A. for illustrations obtained from this source.

In Section III, the illustrations of all Group-II crystal holders have been redrawn from drawings furnished by the Signal Corps.
Finally, the circuit data for a large number of the individual oscillators described have been obtained from Signal Corps technical manuals.
Stock, D. J. R., et al.-Much of the discussion of crystal-unit drive-level characteristics is based upon information contained in the final report, "Investigation, Studies and Evaluation of Performance of Crystal Unit Characteristics," 1952, of a research project (Signal Corps Contract No. DA36-039-sc-5493) undertaken by the Research Division of New York University College of Engineering, Mr. Stock serving as project engineer, with the assistance of L. Silver, E. Strongin, and A. Yevlove. Handbook figures 1-115, 1-116, and 1-118 have been obtained from this report.
Sykes, R. A. (See also Foreword)-The discussions contained in Section I, entitled "Modes of Vibration" and "Rule-of-Thumb Equations for Estimating Parameters," are based upon and fol-
low closely the information contained in the exposition of these subjects by Mr. Sykes in "Design Data on Crystal Units" (Appendix I, Information Bulletin on Quartz Crystal Units, Armed Services Electro Standards Agency, Fort Monmouth, N. J., August, 1952). Handbook illustrations obtained from the foregoing treatise are figures $1-26,1-27$, 1-30, 1-31, 1-36, 1-37, 1-49, 1-50, 1-51, 1-52, 1-85, and $1-88$ ( B ).

The information contained in the discussion of the modes of vibration of quartz crystals is also dependent upon the more extended treatment of the same subject by Mr. Sykes in "Modes of Motion in Quartz Crystals, the Effects of Coupling and Methods of Design" (Chapter VI, Quartz Crystals for Electrical Circuits, Heising). Handbook equations 1-81 (4) and 1-82 (1) have been obtained from this source. Also from this treatise are figures 1-12 and 1-13, which have been copied with the permission of the publisher, D. Van Nostrand Co.
"Principles of Mounting Quartz Plates" (Chapter VIII, Quartz Crystals for Electrical Circuits, Heising), by Mr. Sykes, is the source of the information included in the Handbook concerning the cantilever method of crystal mounting, and also of much of the information concerning pressure mounts in general, wire mounts, and air-gap mounts. The equation in paragraph 1-158, and figures 1-71, 1-81, 1-82, 1-84, and 1-87 of the Handbook are taken from this work, with the permission of the publisher, D. Van Nostrand and Co.
For acknowledgments of information obtained from "Low-Frequency Quartz-Crystal Cuts Having Low Temperature Coefficients," coauthored by Mr. Sykes, see Mason, W. P.
Vigoureux, P. et al.-Quartz Vibration, by P. Vigoureux and C. F. Booth, H. M. Stationery Office, London, has been a valuable source of reference for the writer. Of special usefulness has been the information on the design of crystal ovens, much of which has not been obtainable elsewhere.
Western Electric Co.--The writer is indebted to the Western Electric Co. for making available the design recommendations of Bell Telephone Laboratories engineers, pertaining to the oscillator circuit illustrated in figure 1-157.
Willard, G. W.-Mr. Willard's treatises, "Raw Quartz, Its Imperfections and Inspection" and "Use of the Etch Technique for Determining Orientation and Twinning in Quartz Crystals" (Chapters IV and V, respectively, Quartz Crystals for Electrical Circuits, Heising) have been principal sources of information covering their respective subjects. Handbook figures 1-5, 1-58, 1-63, and

1-65 have been obtained from the above sources with the permission of the publisher, D. Van Nostrand Co.

Wojcicki, F. J.-See Foreword.
Wright Air Development Center.-See Foreword.

## Addendum

Dasher, B. J. et al.-A large proportion of the data contained in the discussion of junction transistor oscillators has been obtained from the quarterly reports on "Transistor Oscillators of Extended Frequency Range" by Messrs. Dasher, D. L. Finn, S. N. Witt, W. B. Warren, Jr., T. N. Lowry, et al., of the Georgia Institate of Technology, Atlanta, Georgia. (Dept. of the Army Contract No. DA-36-039-sc-42716).

Finden, H. J.-The information on the Plessy synthesizer has been obtained primarily from "The Frequency Synthesizer" by Mr. Finden, Journal of the Institution of Electrical Engineers, vol. 90 , Part III, 1943.
The information on the attenvation of unwanted frequencies in frequency synthesis is based on "Developments in Frequency Synthesis" by Mr. Finden, Electronic Engineering, May 1953.
Gerber, E. A.-The treatise "A Review of Methods for Measuring the Constants of Piezoelectric Vibrators" by Dr. Gerber, Proceedings of the I.R.E., September 1953 , has been a valuable source of reference in preparing the discussions on the measurements of crystal oscillators.

The writer also wishes to thank the engineering staff in the charge of Dr. Gerber at the Frequency Control Branch of the Signal Corps Engineering Laboratories for the time and effort spent in re-
viewing the Handbook revision material and for the many suggestions and corrections which have helped to improve the usefulness and accuracy of the text.

Gruen, H. E. - The information on the Gruen packet oscillator series was obtained from "Development of Packet Oscillator Series" by Mr. Gruen, a project of the Armour Research Foundation, I.I.T., completed in 1955. (USAF Contract No. AF 33 (616)-2125).

Hahnel, A. - The information on crystal-phasecontrolled harmonic multipliers is based upon "Multichannel Crystal Control of VHF and UHF Oscillators" by Mr. Hahnel, Proceedings of the I.R.E., January 1953, and upon "A Single Crystal Multi-Channel Oscillator" by Messrs. L. R. Battersby and E. A. Conover (Signal Corps Project No. 132A, March 1954).
Savolainen, U. - The information on bimetallic thermostats in paragraph 4-18 was obtained from "Designing Bimetal Control Devices" by Mr. Savolainen, Product Engineering, August 1950.

Sherman, J. W. Jr.-The writer is indebted to Mr. Sherman of the General Electric Company for the method described in paragraph 1-584 for simulating marginal crystal units in parallel-mode circuits.

## ACKNOWLEDGMENTS FOR USE OF COPYRIGHTED ILLUSTRATIONS

| Figure Number | Courtesy of | Figure Number |
| :--- | :--- | :--- |
| $1-2,1-4,{ }^{1} 1-15$, | Institute of Radio Engineers | $1-56,1-58,1-59$, |
| $1-16$ | $1-63,1-65,1-68$, |  |
| $1-5,1-8,1-9$, | $1-71,1-80,1-81$, | D. Van Nostrand Company of |
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## APPENDIX III-LIST OF MANUFACTURERS

Manufacturers of crystals, crystal products, and crystal accessories are listed alphabetically by company name followed by letter symbols representing the product or products available from stock, presently in manufacture, or capable of being produced within a reasonable time. The products enumerated beside a firm name are those represented as being available at the time of preparation of this handbook. In the first column are listed the Standard Codes of Manufacturers' Names.

The list represents a cross-section of the crystal industry; it is presented for reference purposes only and is not intended as an exclusive directory of recommended commercial sources. Manufacturers desiring to be included in this list should contact Communications and Navigation Laboratory, Attention WCLNE-1, Wright Air Development Center, Wright-Patterson Air Force Base, Ohio. A tabulation of the crystal products manufactured and comments on their availability should be submitted, along with the full company name and address.

\begin{tabular}{|c|c|c|c|c|c|}
\hline \[
\begin{aligned}
\& \text { Mfrs } \\
\& \text { Code }
\end{aligned}
\] \& Manufacturer \& Product* \& \[
\begin{aligned}
\& \text { Mfrs } \\
\& \text { Code }
\end{aligned}
\] \& Manufacturer \& Product* \\
\hline \& Aeronautical Electronic Raleigh-Durham Airport P.O. Box 6043 \& c. B, C \& \& Breon Laboratories 1520 Evergreen Rd. Williamsport, Pa. \& A, B, C \\
\hline CYA \& \begin{tabular}{l}
Raleigh, N. C. \\
Alden Products Co. 112 N. Main St. Brockton 64, Mass.
\end{tabular} \& G, H \& CBD \& Brush Electronics Co. 3405 Perkins Ave. Cleveland 14, Ohio \& A, B, E, F \\
\hline CAS \& American Lava Corp. Chattanooga 5, Tenn. \& E, G \& \multirow[t]{2}{*}{CBVZ} \& \begin{tabular}{l}
Bulova Watch Co. \\
Quartz Crystal Div. \\
62-10 Woodside Ave.
\end{tabular} \& B, C, H, I, J \\
\hline CAHZ \& Bassett, Rex, Inc. 1314 N.E. 17th Court Fort Lauderdale, Fla. \& C \& \& \multicolumn{2}{|l|}{Caribe Aircraft Radio Corp. I Coamo, Puerto Rico} \\
\hline CRR

CQB \& Bendix Radio Div. Bendix Aviation Corp. Baltimore 4, Md. \& I \& CBN \& Centralab Div. of Globe-Union, Inc. 914Y E. Keefe Ave. Milwaukee 1, Wis. \& E, G <br>
\hline \multirow{3}{*}{CQB} \& Union Station Bldg. Erie, Pa. \& B \& CMG \& Cinch Mfg. Co. 1026 S. Homan Ave. Chicago 24, Ill. \& H <br>

\hline \& | 19 Railroad Ave. |
| :--- |
| New Rochelle, N. Y. | \& A B C D \& CBQR \& Clark Crystal Co. 2 Farm Road Marlboro, Mass. \& B, C, D <br>


\hline \& | 820 65th Ave. |
| :--- |
| Philadelphia 26, Pa. | \& A, B, C, D \& CBPR \& Constantin, L. L., \& Co Lodi, N. J. \& G <br>

\hline
\end{tabular}

*PaODUCT symbols

Appendix III


| $M f r s$ Code | Manufacturer | Product* | Mfrs Code | Manufacturer | Product* |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CACK | Kaar Engineering Co. 2995 Middlefield Rd. P.O. Box 1320 Palo Alto, Calif. | C | CKM | Miller Laboratories, August E. 9226 Hudson Blvd. North Bergen, N. J. | B, C, D, H, I, J |
| CBSS | Keystone Electronics Co. 114 Manhattan St. Stamford, Conn. | C | CZN | Monitor Products Co. 815 Fremont Ave. South Pasadena, Calif. | B, C, G, I, J |
|  | King Laboratory, Inc. 2645 South Second West Salt Lake City, Utah | A | CGG | Motorola, Inc. 4545 West August Blvd. Chicago 51, 11 . | C |
| CADI | Knights Co., James, The 131 S . Wells St. Sandwich, Ill. | B, C, G, I, J |  | Murray American Corp. 15 Commerce St. Chatham, N. J. | A |
| CAJR | Lavoie Laboratories Morganville, N. J. | I | CNA | National Co., Inc. 61 Sherman St. Malden 48, Mass. | H, J |
| CBVS | Lewis Co., Inc. E. B. <br> 11 Bragg St. <br> East Hartford 8, Conn. | B, C |  | National Electronic Mfg. Corp. 186 Granite St. Manchester, N. H. | G |
| CLF | Littelfuse, Inc. 4757 N. Ravenswood Ave. Chicago 40, Ill. | H | REN | Nebel Lab., R. E. 1624 E. 12th St. Brooklyn 29, N. Y. | B, C, G |
|  | L. \& O. Research \& Development Corp. 134 North Wayne Ave. Wayne, Pa. | I |  | Northern Engineering Laboratories C 434 Wilmont Ave. <br> Burlington, Wisconsin |  |
|  | Maryland Lava Co. Bel Air, Md. | A, E, G |  | Pan American Trade Development Corp. | A |
| CBXK | McCoy Electronics Co. Chestnut \& Watt Sts. Mt. Holly Springs, Pa. | B, C, I |  | 2 Park Ave. <br> New York 16, N. Y. |  |
|  | Mt. Holly Springs, Pa. <br> Meridian Laboratory <br> Lake Geneva, Wis. | C, I | CAIJ | Pan-Electronics Corp. P.O. Box 584 Griffin, Ga. | B, C |
|  | Methode Mfg. Corp. 2021 W. Churchill St. Chicago 47, Ill. | H | CAMG | Petersen Radio Co., Inc. 2800 W. Broadway Council Bluffs, Iowa | C |
| CZX | Midland Mfg. Co., Inc. 3155 Fiberglas Rd Kansas City 15, Kansas | B, C, I |  | Piezo Products Co. Whitney St. Sherborn, Mass. | C |
| CJA | Millen Mfg. Co., James, Inc 150 Exchange St. Malden, Mass. |  | CBWN | Precision Crystal Laboratory 2223 Warwick Ave. Santa Monica, Calif. | ry B, C, I, J |


| *product symbols |  |
| :---: | :---: |
| A- CRYSTALS-RAW <br> - CRYSTALS-UNFINISHED | F- Chystal transducers-rochelle salts <br> G-CRYSTAL HOLDERS |
| C-CRYSTAL UNITS- quartz | H-CRYSTAL SOCKETS |
| E. CRYSTAL URITS TRUSDUCERS-BARIUEM TITANATE | - Crystal ovens |
| E. CRystal transducers-barium titanate | J-PACKaged oscillators |


| Mfrs <br> Code | Manufacturer | Product* | Mfrs Code | Manufacturer | Product* |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Precision Piezo Service 427 Mayflower St. Baton Rouge, La. | B, C | CSJ | Stupakoff Ceramic \& Mfg. Co Latrobe, Pa. | $\mathrm{E}, \mathrm{G}$ |
| CL | Premier Research <br> Laboratories, Inc. 79-89 Seventh Ave. New York 11, N. Y. | B, C, D, G. I | CHS | Sylvania Electric <br> Products, Inc. <br> 12 Second Ave. <br> Warren, Pa. | H |
| CBPN | Radiation Counter Laboratories, Inc. 5121 W. Grove St. | I | CAYM | Tedford Crystal Labs. 4126 Colerain Ave. Cincinnati 23, Ohio | C |
|  | Skokie, Ill. |  |  | United States Gasket Co. | H |
| CRV | Radio Corporation of America <br> Commercial Electronics | C ducts |  | Fluorocarbon Products Div. P.O. Box 648 Camden, N. J. |  |
| CUR | Camden 2, N. J. <br> Reeves-Hoffman Corp. Cherry and North Sts. Carlisle, Pa. | B, C | CAMU | Valpey Crystal Corp. 1244 Highland St. Holliston, Mass. | B, C, D, I |
|  | Scientific Electronic Labs., Inc. 866 Bergen St. | G | CAND | V Precision Instrument Co. 57-02 Hoffman Drive Elmhurst, N. Y. | C |
| CADG | Newark 8, N. J. <br> Scientific Radio <br> Products, Inc. 215 S. Eleventh St. Omaha 8, Neb. | B, C, I, ' | CW | Western Electric Co. <br> Radio Div., Electronic <br> Products Sales Dept. <br> 120 Broadway <br> New York 5, N. Y. | C |
|  | Sealtron Co. <br> Reading Rd. at Amity <br> Cincinnati 15, Ohio | G | CBVJ | Wright Electronics Inc. 1519 McGee St. <br> Kansas City 8, Mo. | B, C, D, I |
| CBXR | Sherold Crystals, Inc. 1510 McGee St. <br> Kansas City 15, Kansas | C, D |  | X-tron Electronics 890 71st Ave. Oakland 21, Calif. | A, B, C |
| CBZA | Standard Crystal Co. 1714 Locust St. <br> Kansas City 8, Mo. | B, C, 1 |  | Young Brothers Co. 1829 Columbus Rd. Cleveland, Ohio | 1 |

*PRODUCT SyMBoLS


```
F-CRYSTAL, TRANSDUCERS- ROCHELLE SALLTS
G- CuYSTAL, MOHDWHS
#-CKYSTAL SOCKEN
1-PACKAGED OSCLLLATORS
```


## APPENDIX IV—RELATED SPECIFICATIONS, STANDARDS, PUBLICATIONS, AND DRAWINGS

## ORDERING INFORMATION

D-1. Copies of specifications, standards, publications, and drawings required by contractors in connection with specific procurement functions should be obtained from the procurement agency or as directed by the contracting officer.
D-2. The following may be obtained from the Commanding General, Air Materiel Command, Wright-Patterson Air Force Base, Dayton, Ohio:
a. U. S. Air Force Specifications and Drawings.
b. Federal Specifications.
c. Military Specifications and Standards.

D-3. The following may be obtained from the Commanding Officer, Signal Corps Procurement Agency, 2800 South 20th Street, Philadelphia 45, Pennsylvania:
a. U, S. Army Specifications.
b. National Military Establishment and Joint Army-Navy Specifications.
c. Signal Corps Drawings and Marking Instructions.

D-4. The following may be obtained from the Bureau of Supplies and Accounts, Navy Department, Washington 25, D. C. (activities of the Armed Forces should make application to the Commanding Officer, Naval Supply Center, Norfolk 11, Va.) :
a. Navy Department Specifications.
b. Federal Specifications.
c. Military Specifications.

D-5. The following may be obtained from the Superintendent of Documents, Government Printing Office, Washington 25, D. C.:
a. Department of Commerce Publications.
b. Federal Specifications.

D-6. Both the title and identifying number or symbol should be stipulated when requesting copies of specifications, standards, publications, and drawings.

## SPECIFICATIONS

| AN-P-13 | Preservation and Packaging <br> Parts and Equipment (General <br> Specification for) (Note: This is <br> an Air Force-Navy Aeronautical <br> specification applicable only to |
| :--- | :--- |
| 40985 | Air Force purchases). <br>  <br> Marking of Interior Packages <br> (for Communications <br> Equipment). |

AIR FORCE-NAVY AERONAUTICAL
AN-P-34 Plating Nickel.

## FEDERAL

NN-B-601
Boxes, Wood-Cleated Plywood, for Domestic Shipment.

NN-B-621

QQ-A-318

QQ-B-611

QQ-B-746

QQ-M-151

QQ-N-321

| QQ-S-571 | Solder; Soft (Tin, Tin-Lead, and Lead-Silver). | JAN-P-105 | Packaging and Packing for Overseas Shipment-Boxes; |
| :---: | :---: | :---: | :---: |
| QQ-S-636 | Steel; Carbon (Low Carbon), Sheets and Strips. | JAN-P-106 | Wood, Cleated, Plywood. <br> Packaging and Packing for |
| QQ-S-763 | Steel, Corrosion-Resisting; Bars and Forging (Except for Re-forging). | JAN-P-108 | Overseas Shipment-Boxes; Wood, Nailed. |
| LLL-B-631 | Boxes; Fiber Corrugated (for Domestic Shipment). |  | Overseas Shipment-Boxes, Fiberboard (V-Board and W-Board), Exterior and Interior. |
| LLL-B-636 | Boxes; Fiber, Solid (for Domestic Shipment). | JAN-P-120 | Packaging and Packing for Overseas Shipment-Cartons, Folding, Paperboard. |
| MIL-C-16B | military <br> Crystal Unit, Quartz (CR-1A/AR, Pressure, Mounted). | JAN-P-125 | Packaging and Packing for Overseas Shipment-Barrier Materials, Waterproof, Flexible. |
| MIL-C-239B MIL-C-3098B | Crystal Unit, Quartz (CR-5/U). Crystal Units, Quartz. | JAN-P-133 | Packaging and Packing for Overseas Shipment-Boxes, Set-up, Paperboard. |
| $\begin{aligned} & \text { MIL-C-10405 } \\ & \text { (Sig C) } \end{aligned}$ | Crystal Units, Quartz, Pressure and Spacer Mounted. | JAN-P-139 | Packaging and Packing for Overseas Shipment-Plywood, Container Grade. |
| MIL-H-10056B | Holders, Crystal. | JAN-P-140 | Packaging and Packing for |
| MIL-L-10547 | Liners, Case, Waterproof. |  | Overseas Shipment-Adhesives, Water-Resistant, Case-Liner. |
| MIL-P-14 | Plastic-Materials, Molding, and Plastic Parts, Molded; Thermosetting. | JAN-S-28A | Sockets, Electron Tube, and Accessories. |
| MIL-P-116 | Packaging and Packing for Overseas ShipmentPreservation, Methods of. | 72-53 | U. S. ARMY <br> Finishes (For Ground Signal Equipments). |
| MIL-R-3065 | Rubber and Synthetic Rubber Compounds, General Purpose (Except Tires, Inner-Tubes, Sponge Rubber, and Hard Rubber). | 72-119-A | Holders for Quartz Crystals. <br> Marking; Exterior, Domestic and Export Shipments by Contractors. |
| MIL-T-945A | Test-Equipment, for Use with Electronic Equipment: General Specification. | 100-2 | Standard Specification for Marking Shipments by Contractors. |
| JAN-C-173 | Coating Materials, Moisture- and Fungus-Resistant, for the Treatment of Communications, Electronic, and Associated Electrical Equipment. | $726-15{ }^{\text {sic }}$ | CORPS INSTRUCTIONS <br> Marking of Interior Containers (For Signal Corps Equipment). <br> NAYY |
| JAN-P-13 | Plastic-Materials, Laminated, Thermosetting; Sheets and Plates. | General Sp (applicable 22W13 | tion for Inspection of Material to Navy purchases). <br> Wire, Steel, Corrosion-Resisting. |
| JAN-P-14 | Plastic-Materials, Molded, Thermosetting. | 46N7 | Nickel-Copper-Silicon-Alloy: Castings. |

## MIETTARY

(Military Standards for individual Crystal Units and for drive adjustment procedures for the standard crystal impedance meters are contained in Military Specification MIL-C-3098B.)

MIL-STD-105 Sampling Procedures and Tables for Inspection by Attributes.

MIL-STD-129 Marking of Shipments.
JAN-STD-15 Electrical and Electronic Symbols.

## PUBLICATIONS

|  | U. S. AIR Force |
| :---: | :---: |
| HB-16F-1 | Gentile AF Depot-Crystal Handbook for Equipments FT-164 Crystal Holder (Unit). |
| HB-16F-2 | Gentile AF Depot-Crystal Handbook for Equipments Using AR-3 Crystal Holder (Unit). |
| HB-16F-3 | Gentile AF Depot-Crystal Handbook for Equipments Using FT-243 Crystal Holder (Unit). |
| S-16-F | USAF Supply Catalog, Class 16-F, Code 2100, Radio Crystals. |
|  | SICNAL CORPS |
| Project 4422D $\dagger$ | Crystal Data Sheets (technical requirements for fabrication of crystal units contained in various equipments). |

NAVSHIPS 900,152

Navy Shipment Marking Handbook.

## DEPARTMENT OF COMMERCE

National Bureau Screw-Thread Standards for of Standards Federal Services. Handbook H28

## AMERICAN IRON AND STEE INSTITUTE

Steel Products Manual (Stainless and Heat-Resisting Steels). $\dagger \dagger$
$\dagger$ Direct requests for this publication to: Commanding
General, Signal Corps Engineering Laboratories, SCCSCL-PMM-3, Fort Monmouth, N.J.
$\dagger \dagger$ Direct requests for this publication to: American Iron and Steel

## DRAWINGS

|  | U. S. AIR FORCE |
| :--- | :--- |
| 52B13216 | Crystal Holder HC-( )/U, <br> Assembly (Crystal Holders <br> HC-11/U and HC-12/U). |
|  | SIGNAL CORPS |
| SC-A-200 | Crystal Holder FT-164. |
| SC-D-247 | Crystal Holder FT-249, Outline <br> Dimensions and Marking |
|  | Information. |
| SC-D-5213 | Crystal Holder FT-171-B, <br> Drawing List. |
| SC-D-6306 | Crystal Holder FT-243. |
| SC-D-7627 | Crystal Units DC-34 and DC-35, <br> Outline Dimensions. |
| SC-D-9553 | Crystal Holder FT-241-A, <br> Critical Dimensions. |
| SC-D-14444 | Standard Oscillator <br> TS-39/TSM-1, Circuit Diagram. |
| SC-D-14445 | Standard Oscillator <br> TS-39/TSM-1, Calibration and |
| Operation. |  |

SC-D-17316

SC-D-17499

SC-D-20032

SC-D-20035

SC-D-20036

SC-D-20724

SC-D-20877

SC-D-22892

SC-D-25222

SC-D-26189

Crystal Impedance Meter TS-330/TSM, Circuit Diagram.

Crystal Holder FT-243, Marking for Standard Units.

Crystal Holder $\mathrm{HC}-4 / \mathrm{U}$, Assembly.

Crystal Holder HC-3/U, Assembly.

Crystal Holder HC-2/U, Assembly.

Crystal Holder HC-5/U, Assembly.

Crystal Holder HC-1/U, Assembly.

Crystal Holder FT-171-B, Assembly.

Crystal Impedance Meter TS-537/TSM, Circuit Diagram.

Crystal Holder FT-249, Case Assembly.

## APPENDIX V-DEFINITIONS OF ABBREVIATIONS AND SYMBOLS

## ABBREVIATIONS



WADC TR 56-156


## SYMBOLS

Definitions are given for all usages of symbols appearing in this manual. For each usage, the first paragraph wherein the symbol appears is listed. For a complete definition, in most instances, it is necessary to examine the symbol in context by referring to the cited paragraph.


(eff) $\mathrm{C}_{0} \ldots \ldots \ldots \ldots \ldots$ effective electrostatic shunt capacitance of crystal unit (equal to $\mathrm{C}_{0}$ plus any circuit capacitance directly shunted across unit terminals)
 capacitance of vacuum-tube plate circuit
 generalized oscillator taking into account dynamic effects of vacuum tube
 circuit
$\mathrm{C}_{\mathrm{in}}$ cuit; normally represents only stray capacitance
$\mathrm{C}_{\mathrm{T}}$
(1) total capacitance ( $\mathrm{C}_{\mathrm{o}}+\mathrm{C}_{\mathrm{x}}$ ) shunting series arm of generalized crystal-oscillator circuit

1-211
(2) total capacitance of capacitance-bridge oscil-
lator circuit
(3) effective heat capacity of thermostat in crystal oven

4-58
 unit; considered as circuit variable.
 mode crystal unit
 in Miller oscillator due to inductive plate circuit (applicable when effect of grid-circuit losses on frequency can be considered negligible)
 in Miller oscillator due to inductive plate circuit

1-332
CT...................................artz cut 1-23
$\mathrm{C}_{1} \ldots \ldots$ equinalent series-arm capacitance of desiredfrequency mode of crystal unit
$\mathrm{C}_{1}, \mathrm{C}_{2}$, etc..................apacitances in schematic diagram........................ $1-220$
$C_{2}, C_{3}, \ldots C_{k} \quad \begin{aligned} & \text { equivalent series-arm capacitance of on- un- } \\ & \text { wanted-frequency modes of crystal unit }\end{aligned}$


D.................. (1) quartz element 1-90
(2) $Q$ degradation of crystal unit; equal to ratio
of total effective resistance into which crystal
must operate to crystal resonance resistance
$\left(\frac{R_{c}}{R}\right)$
(3) number of discriminators in synthesizer cir-
cuit.,$\ldots .$.
(4) diameter .............................................................................................
$D, D_{1}, D_{2}, D_{1,2} \ldots \ldots$ plate-stabilized modes of vacuum-tube opera- tion $\ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$



| Symbol |  | Paragraph |
| :---: | :---: | :---: |
|  | mechanical vibrational energy of crysta | 1-249 |
|  | rms voltage across thermistor in bridge circuit of Meacham-bridge oscillator. | - ${ }^{\text {-.. }} 1$ 1-358 |
| ET | ....quartz cut | 1-23 |
|  | ....emissivity | 4-35 |
|  | instantaneous value of vacuum-tube plate voltage $\qquad$ | 1-312 |
|  | instantaneous value of vacuum-tube grid voltage | - 1 -312 |
|  | instantaneous harmonic voltage across vacuum-tube plate tank circuit | 1-322 |
|  | instantaneous value of a-c component of vacuum-tube plate voltage | of $\begin{array}{ll}\text {-. } \\ \text { 1-312 }\end{array}$ |
| F | quartz element | 1-90 |
|  | frequency-stability factor for parallel-mode crystal-oscillator circuit; equal to rate of change in crystal-unit reactance per fractional change in frequency | $\begin{array}{lr}\text { f } & \\ \\ \\ \text { al } & \\ & 1-243\end{array}$ |
|  | frequency-stability factor for series-mode crystal-oscillator circuit; equal to rate of change in crystal-unit reactance per fractional change in frequency | $\begin{array}{lr}\text { f } & \\ \\ & \\ & 1-240\end{array}$ |
|  | coefficient of frequency stability; equal to percentage change in reactance of stabilizing element per percentage change in frequency | 0  <br> g  |
|  | frequency-stability coefficient; equal to percentage rate of change in overall effective reactance ( $\mathrm{X}_{\mathrm{c}}$ ) of crystal unit for a percentage change in frequency; a measure of the stabilizing effect of crystal unit against percentage change in reactance of load capacitance, $\mathrm{C}_{\mathrm{x}}$. | e  <br> e  <br>   <br>   <br>  $1-243$ |
| $F_{x_{v}}$ | frequency-stability coefficient: equal to percentage rate of change in series-arm reactance ( $\mathrm{X}_{*}$ ) of crystal unit for a percentage change in frequency; a measure of the stabilizing effect of crystal unit against percentage change in reactance of total effective shunt capacitance, $\mathrm{C}_{\mathrm{T}}$ | $\begin{array}{ll}- \\ - & \\ \text { e } & \\ - & \\ \text { l } & \\ . & 1-243\end{array}$ |
| FT | .....quartz cut ............................................................................... | . 1-23 |
|  | (1) frequency ................................................................................. | . 1-78 |
|  |  | . 1-188 |
|  | (3) nominal frequency at which crystal unit is assumed to operate $\qquad$ <br> (4) fundamental frequency of crystal-oven temperature cycles $\qquad$ | $\begin{array}{ll}\text { s } \\ . & 1-208 \\ - & \\ . & 4-60\end{array}$ |
| $\mathrm{f}_{k}$ | $\ldots$ antiresonant frequency of crystal unit ............. | 1-204 |
| $\mathbf{f}_{\mathrm{c}}$ | fundamental frequency of first crystal oscillator in synthesizer circuit | - 1-455 |
| $\mathrm{f}_{\text {d }}$ | frequency of discriminator in synthesizer circuit | - $1-455$ |
|  | frequency of force acting on oscillator ............. | . 1-265 |
|  | ...highest frequency ................................................. | . 1-248 |




$\left.\begin{array}{lll}\text { Symbol } \\ \mathrm{L}_{1} & \text { equivalent, or effective, inductance of crystal }\end{array}\right]$

| (5) turns ratio of autotransformer in groundedgrid oscillator (equal to ratio of total turns to turns of secondary) <br> (6) total number of frequency channels in synthesizer circuit | $1-407$ $1-442$ |
| :---: | :---: |
| Na .ana.................. Sodium | 1-29 |
| $\mathrm{NaKC.H}, \mathrm{O}_{5}$ |  |
|  | 1-29 |
| $\mathrm{N}_{\mathrm{k}} \quad$ turns ratio of grid transformer in vacuumtube circuit | 1-358 |
| turns ratio of plate transformer in vacuumtube circuit | 1-359 |
|  | 1-29 |
| NT | 1-23 |
| n.......................(1) integer; equal to harmonic of oscillation ......... | 1-79 |
| (2) a positive integer; equal to the sequence number of any given frequency in a set of frequencies (e.g. in an ascending sequence of evenly-spaced crystal frequencies numbered $1,2, \ldots$ etc., $n=1$ for the No. 1 crystal, $n=2$ for the No. 2 crystal, etc.) | 1-445 |
| O..............................-Oxygen | 1-29 |
| P.................................. ${ }^{\text {Phosphorus }}$ | 1-29 |
|  | 1-233 |
| $\begin{aligned} & \mathrm{P}_{\mathrm{cm}} \\ & \text { Maximum power dissipation recommended for } \\ & \quad \text { Mitandard crystal unit } \end{aligned}$ | 1-293 |
| $P_{g} \ldots \ldots \ldots$ power dissipated in vacuum-tube grid circuit | 1-296 |
| $\mathrm{P}_{\mathrm{L}}$ - | 1-397 |
|  | 1-333 |
| $P_{p} \times \quad$ power dissipated in plate circuit of trans-former-coupled oscillator | 1-395 |
|  | 1-312 |
| $P_{1}$ <br> (1) power dissipated by $R_{1}$ (crystal-unit) arm in Meacham-bridge oscillator <br> (2) position of any given adjustment of adjustable thermostat | $1-361$ $4-16$ |
| p.......................... harmonic integer | 1-81 |
| Q................................ quality factor | 1-36 |
| $Q_{\text {e............................ective quality factor of crystal unit equal }}$ to $\mathrm{X}_{\mathrm{e}} / \mathrm{R}_{\mathrm{e}}$ | 1-227 |
|  a given crystal unit | 1-217 |
|  quality factor of an oscillator feedback circuit | 1-272 |
| $\text { Q } \mathrm{Q}_{\mathrm{a}} \text { quality factor of vacuum-tube input imped- }$ | 1-272 |
| $Q_{\text {Isc }}$. lator feedback circuit from plate to grid to cathode | 1-272 |
| Q* $\quad$ effective quality factor of series arm of crystal unit (equal to $X_{\mathrm{n}} / \mathrm{R}$ ) | 1-213 |
| R <br> (1) motional-arm (or series-arm) resistance of crystal-unit equivalent circuit | 1-183 |



S cillator ..... $1-360$
$S, S_{1}, S_{2}$, etc. switches in schematic diagram ..... 1-188
Si Silicon ..... 1-40
$\mathrm{SiO}_{2}$ silicon dioxide ..... $1-40$
s. (1) quartz face ..... 1-43
(2) elastic compliance factor ..... 1-78
(3) activity sensitivity of bridge circuit in Meacham-bridge oscillator ..... 1-360
 ..... 4-35
 ..... 4-61
$\mathrm{T}_{\mathbf{c}} . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . a v e r a g e ~ c r y s t a l ~ t e m p e r a t u r e ~$ ..... 4-56
 ..... 4-56
$\mathrm{T}_{0} . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . o p e r a t i n g ~ t e m p e r a t u r e ~ o f ~ o v e n ~ a n d / o r ~ t h e r m o-~$ stat ..... 4-16
 ating surface ..... 4-40
t. (1) thickness ..... 1-80
(2) time (in seconds) ..... 1-296
t/l ratio of thickness to length ..... 1-101
$\tan ^{-1}$ arctangent (an angle whose tangent is) ..... 1-280
V. (1) quartz cut ..... 1-23
(2) applied d-c voltage ..... 1-248
(3) volume ..... 4-25
$V_{1}, V_{2}$, etc. vacuum tubes in schematic diagram ..... 1-309
v. velocity ..... 1-78
w. width ..... 1-79
w/l. ratio of width to length ..... 1-79
X (1) quartz cut ..... 1-23
(2) crystal axis ..... 1-23
(3) number of crystals for second crystal oscilla- tor in synthesizer circuit ..... 1-442
 initially coincided with a true $X$ axis before rotation ..... Fig. 1-17
 ..... 1-187
(2) motional-arm capacitive reactance of crystal- unit equivalent circuit ..... 1-190
(3) thermal reactance of thermofilter capacity ..... 4-61
$\mathbf{X}_{\mathbf{C}_{\mathbf{b}}} \ldots \ldots \ldots$ capacitive reactance of balancing capacitance of capacitance-bridge circuit ..... 1-365
$X_{r}: \quad$ reactance of effective grid-to-cathode capaci- tance of vacuum-tube circuit ..... $1-280$
 tance of first vacuum tube in two-tube crystal oscillator circuit ..... 1-383
$\mathbf{X r}^{\prime}{ }^{\prime}$ ' capacitive reactive component of grid imped- ance when latter is represented as equivalent capacitance in series with equivalent resist- ance ..... 1-297

|  | (1) equivalent positive reactance of dynamic negative plate-to-cathode capacitance effectively introduced by vacuum tube in Pierce crystal oscillator <br> (2) reactance of $\mathrm{C}_{\mathrm{n}}$ in impedance-inverting crystal oscillator | $1-281$ $1-426$ |
| :---: | :---: | :---: |
|  | shunt capacitive reactance of crystal-unit equivalent circuit | 1-187 |
|  | reactance of total effective electrostatic plate-to-cathode capacitance of vacuum-tube plate circuit | 1-281 |
|  | equivalent, or effective, reactance of crystal unit when unit is viewed as an equivalent resistance and reactance in series. | 1-204 |
|  | effective reactance, $X_{e}$, of crystal unit when assuming stray shunt capacitance introduced by circuit is part of total electrostatic shunt capacitance of crystal unit | 1-278 |
|  | effective reactance, $X_{e}$, of crystal unit when operating at parallel-resonance frequency, $f_{p}$, of generalized crystal-oscillator circuit. | 1-210 |
|  | generalized reactive component of grid impedance in oscillator circuit | 1-331 |
|  | (1) inductive reactance <br> (2) motional-arm inductive reactance of crystalunit equivalent circuit | $1-187$ $1-190$ |
|  | reactance of distributed inductance of leads and terminals of crystal unit | 1-187 |
|  | inductive reactance of secondary of plate transformer in capacitance-bridge oscillator | 1-565 |
|  | reactive component of plate impedance in oscillator circuit | 1-331 |
|  | reactive component of plate impedance in Miller oscillator when expressed as a combined function of plate and grid circuit. | 1-332 |
| $\mathrm{X}_{\mathrm{prg}}$ | plate-to-grid reactance in vacuum-tube circuit | 1-331 |
| X | total series-arm reactance of crystal-unit equivalent circuit | 1-203 |
| X | total series-arm reactance, $\mathrm{X}_{\mathrm{k}}$, of crystal-unit equivalent circuit at antiresonance | 1-208 |
| X | total series-arm reactance, $X_{s}$, of crystal-unit equivalent circuit when operating at parallel resonance with total effective load capacitance, $\mathrm{C}_{\mathrm{T}}$, of generalized oscillator circuit (employed only when convenient to distinguish between $X_{n}$ used in the general sense and $X_{8}$ when used in the particular case of the equivalent parallel-resonant crystal-oscillator circuit) | 1-214 |
| $\mathbf{X}_{\boldsymbol{\gamma}}$ | total reactance in series with total load resistance, $\mathrm{R}_{\mathrm{T}}$, shunting series arm of equivalent crystal-oscillator circuit | 1-211 |


|  | total reactance in series with total load resistance, $\mathrm{R}_{\mathrm{T}}$, shunting series arm of equivalent parallel-resonant crystal-oscillator circuit (employed only when convenient to distinguish between $X_{T}$ used in the general sense and when used in the particular case of the equivalent parallel-resonant crystal-oscillator circuit) | $\begin{array}{ll}\text { - } & \\ \text { - } & \\ \text { - } & \\ & \\ 1-211\end{array}$ |
| :---: | :---: | :---: |
|  | reactance in series with load resistance, $\mathrm{R}_{\mathrm{x}}$, shunting crystal unit in equivalent parallelresonant crystal circuit | - $1-210$ |
| $\mathbf{X}_{\mathbf{z}}$ | reactive component of load impedance .............. | 1-281 |
|  | (1) quartz face | 1-43 |
|  | (2) dimension of crystal blank in X-axis direction | 1-51 |
|  | (1) quartz cut | 1-23 |
|  | (2) crystal axis | 1-23 |
| Y' | directional axis of the crystal dimension that initially coincided with a true Y axis before rotation | Fig. 1-17 |
| YT | quartz cut | 1-90 |
| y | dimension of crystal blank in Y-axis direction | 1-51 |
| Z | (1) quartz axis | 1-51 |
|  | (2) impedance | 1-188 |
| $\mathbf{Z}^{\prime}$ | directional axis of the crystal dimension that initially coincided with a true Z axis before rotation | Fig. 1-17 |
| $\mathrm{Z}^{\prime \prime}$ | directional axis of the crystal dimension that initially coincided with the $Z^{\prime}$ axis before rotation | Fig. 1-17 |
| Z ${ }_{\text {e }}$ | equivalent, or effective, impedance of crystal unit | 1-209 |
| Z | impedance of feedback circuit | 1-378 |
|  | (1) grid-to-cathode impedance as viewed by the excitation source <br> (2) impedance of excitation source as viewed by grid of vacuum tube | $1-233$ $1-398$ |
|  | input impedance of first tube in two-tube parallel-resonant crystal oscillator | 1-345 |
|  | input impedance of second tube in two-tube parallel-resonant crystal oscillator. | 1-345 |
| $\mathrm{Z}_{\mathrm{k}}$ | vacuum-tube a-c plate-circuit impedance between cathode and ground (in the Butler oscillator, $Z_{k}$ is the output impedance of the cathode follower) | 1-378 |
| $\mathbf{Z k}^{\prime}$ | output impedance of cathode follower as viewed by the crystal in grounded-plate oscillator | 1-422 |
|  | a-c load impedance | 1-268 |
|  | input impedance of impedance-inverting network | 1-426 |
| Z。 | characteristic impedance of impedance-inverting network | $1-426$ |
|  | (1) impedance of an equivalent parallel-resonant crystal circuit; antiresonant impedance of |  |

## Paragraph



| $\Delta$ | a change or difference in temperature; a "temperature drop" along a heat-conducting path | 4-18 |
| :---: | :---: | :---: |
| $\Delta V$ | a difference of potential; a voltage drop | 4-34 |
| small change in the effective reactance, f a crystal unit, where the unit impedis viewed as an effective resistance and |  |  |
| $\partial$ | partial differential of | 1-298 |
|  | dielectric constant | 1-248 |
| $\theta$ <br> (1) second angle of rotation, used in defining orientation of crystal cut |  | 1-88 |
|  | (2) angle of incidence of X-rays with atomic plane | 1-127 |
|  | (3) impedance phase angle of crystal-oscillator circuit | 1-240 |
|  | (4) that angle of vacuum-tube excitation-voltage excursion during which no plate current flows | 1-312 |
|  | (5) angle indicating small phase shift in variableleg voltage of Meacham-bridge oscillator | 1-358 |
| $\theta_{\text {x }}{ }_{\text {g }}$ | phase angle of vacuum-tube grid-to-cathode excitation voltage with respect to a designated reference | 1-270 |
| $\theta_{\mathrm{E}_{\mathrm{p}}}$ | phase angle of vacuum-tube r-f plate voltage with respect to a designated reference | 1-270 |
| $\theta_{1}{ }_{g}$ | phase angle of vacuum-tube r-f grid current with respect to a designated reference | 1-270 |
| $\theta_{\mathrm{N}}$ | that angle of vacuum-tube excitation-voltage excursion during which no plate current flows for the case when $R_{e}$ equals a particular value, $\mathrm{R}_{\mathrm{e}_{\mathrm{N}}}$ | $1-312$ |
| $\theta_{\mathrm{zg}}$ | phase angle of the a-c voltage across the grid-to-cathode impedance with respect to the a-c current through the impedance | 1-270 |
| $\theta_{z_{\text {pgr }}}$ | phase angle of the voltage across the impedance of the oscillator feedback circuit with respect to the current through the impedance | 1-270 |
| $\lambda$ | wavelength | 1-78 |
| $\mu$ | (1) micro | 1-191 |
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| $\mu_{1}$ | amplification factor of first vacuum tube in two-tube crystal-oscillator circuit | 1-378 |
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|  | (2) negative resistance | 1-232 |
| $p_{\text {a }}$ | negative resistance of generalized crystal oscillator when circuit is represented as seriesconnected | 1-232 |
| $\mathrm{\rho}^{\mathbf{T}}$ | equivalent negative resistance of vacuum tube when tube is represented by an equivalent reactance and negative resistance in parallel | -278 |



| Fraction of Unit | Lowest <br> Integral <br> Part Per <br> Power of <br> 10 | Decimal Part Per Unit | Decimal Part Per 100 (PerCent) | Miscellaneous Fractional Expressions |
| :---: | :---: | :---: | :---: | :---: |
| 1/1000 | $1 \mathrm{PP} 10^{3}$ | 0.001 | 0.1 \% | $1000 \mathrm{p} / \mathrm{p} /$ million |
| 2/10,000 | $2 \mathrm{PP} 10^{4}$ | 0.0002 | 0.02 | $200 \mathrm{p} / \mathrm{p} /$ million |
| 12/100,000 | $12 \mathrm{PP} 10^{5}$ | 0.00012 | 0.012 | $120 \mathrm{p} / \mathrm{p} /$ million |
| 1/10,000 | $1 \mathrm{PP} 10^{4}$ | 0.0001 | 0.01 | $100 \mathrm{p} / \mathrm{p} / \mathrm{million}$ |
| 75/1,000,000 | 75 PP 10 ${ }^{\text {a }}$ | 0.000075 | 0.0075 | $75 \mathrm{p} / \mathrm{p} /$ million |
| 5/100,000 | $5 \mathrm{PP} 10^{5}$ | 0.00005 | 0.005 | $50 \mathrm{p} / \mathrm{p} /$ million |
| 3/100,000 | 3 PP $10^{8}$ | 0.00003 | 0.003 | $30 \mathrm{p} / \mathrm{p} /$ million |
| 2/100,000 | $2 \mathrm{PP} 10^{5}$ | 0.00002 | 0.002 | $20 \mathrm{p} / \mathrm{p} /$ million |
| 1/100,000 | $1 \mathrm{PP} 10^{5}$ | 0.00001 | 0.001 | $10 \mathrm{p} / \mathrm{p} /$ million |
| 5/1,000,000 | $5 \mathrm{PP} 10^{\circ}$ | 0.000005 | 0.0005 | $5 \mathrm{p} / \mathrm{p} /$ million |
| 1/1,000,000 | $1 \mathrm{PP} 10^{8}$ | 0.000001 | 0.0001 | $1 \mathrm{p} / \mathrm{p} /$ million |
| 1/10,000,000 | $1 \mathrm{PP} 10^{7}$ | 0.0000001 | 0.00001 | $1 \mathrm{p} / \mathrm{p} / 10$ million |
| 1/100,000,000 | $1 \mathrm{PP} 10^{8}$ | 0.00000001 | 0.000001 | $1 \mathrm{p} / \mathrm{p} / 100$ million |
| 1/1,000,000,000 | $1 \mathrm{PP} 10^{\circ}$ | 0.000000001 | 0.0000001 | $1 \mathrm{p} / \mathrm{p} / \mathrm{billion}$ |
| 1/10,000,000,000 | 1 PP $10{ }^{10}$ | 0.0000000001 | 0.00000001 | $1 \mathrm{p} / \mathrm{p} / 10$ billion |

Conversion Table for Commonly Encountered Fractional Parts


FREQUENCY
$f_{n}=$ NOMINAL FREQUENCY OF CRYSTAL (AS MARKE O ON CRYSTAL UNIT)
f* ACTUAL FREQUENCY MEASURED AT MIDPOINT ( $75^{\circ}$ C) OF OPERATing temperatuie range
as MOMINAL FREQUENCY TOLERANCE\{士 $0.002 \%$ OF $f_{n}$ ) SPECIFIED AT MIOPOINT $\left(75^{\circ} \mathrm{C}\right.$ OF OPERATING TEMPERATURE RANGE OF CRYSTALS UNCER TEST.
b. MAXIMUM FREQUENCY DEVIATION ALLOWED ( $\pm 0.0005 \%$ OF $\ddagger$ ) WITHIN OPERATING TEMPERATURE RANGE $\left(+70^{\circ} T O+80^{\circ} \mathrm{C}\right)$

RESULTS OF TESTS
GRYSTAL-A REJECTED: MOMINAL FREQUENCY TOLERANGE NOT within $\pm 0.002 \%$ OF in
CRYSTAL-B REJEGTED: FREOUENGY DEVIATION NOT WITHIN $\pm 0.0005 \%$ OF
CAYSTAL C ACGEPTED: NOMINAL FREQUENCY TOLERANCE AND FREQUENGY DEVIATION WITHIN SPECIFIEO LIMITS

Diagram illustrating distinction between nominal frequency tolerance and frequancy deviation with temperature of erystel units


Temperature conversion chart: degress centigrade to degrees fahrenheir

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[^0]:    * See paragraphs 1-132 to 1-171.

[^1]:    ** All quartz bars have negative temperature coefficients for pure length-extensional vibratione, although a zero coefficient is obtainable for certain cuts.

[^2]:    * Vacuum Tube Obcillatora, John Wiley and Sons, 1953.

[^3]:    WADC TR 56-156

[^4]:    $\dagger$ Not all types of synthesizers in current use are covered in the above discussion. Other recently developed and equally important circuits include:

    The General Radio Company synthesizer, developed under Signal Corps Contract No. DA-96-039-sc-16542. The GR synthesizer operates on a pinciple fundamentally different from those described in this report. In the GR system an oscillator is thase- and frequency-locked through a variable scale-of- N divider. The pulse output of the divider is compared by coincidence methods with a pulse derived from a crystal oscillator. The frequency range of this synthesizer is 0.1 mc to 10 mc .

    The Matawan Synthesizer ME-447, of the Lavoie Laboratories Instrument Company. This system generates any multiple of 1 kc within the range of 1.0 mc to 2.0 mc .

    The Rohde and Schwarz decade synthesizer and exciter system (Federal Telephone and Radio Company Types HS-431, HS-441, and HS-471), which covers a range of 50 kc to 30 mc .

    The Telefunken Precision Frequency Meter. This meter is used in the measurement of frequencies between 1 kc and 300 mc . The circuitry contains a frequency synthesizer capable of generating sine-wave outputs between 1 kc and 30 mc . It is claimed that harmonics and sidebands of the output frequency are at least 80 db below the selected signal, and that the sunthesizer accuracy is $\pm 0.2 \mathrm{cps}$ for frequencies between 1 kc and 3 mc , and $\pm 2.0 \mathrm{cps}$ between 3 mc and 30 mc .

[^5]:    * Note: The discussion of the Plessey synthesizing system is based primarily upon the report, "The Frequency Synthesizer", by Mr. H. J. Finden of the Plessey Company, Lid., England, published in the Journal of the Institution of Electrical Engineers, Vol. 90, Part 11I, 1943.

[^6]:    * Note: See paragraph 2-66 to 2-151 for detailed descriptions of frequency-measuring systems in current use.

[^7]:    * Note that only the equation where $f_{x}$ is assumed to be less than the $f_{1}$ harmonic is used. Otherwise $f$, would necessarily be zero. For example, if $f_{*}-f_{1}=f_{2}-2 f_{1}$
    then $f_{1}$ must be zero. In the last six equations, however, the possibility exists for the $f_{*}$ harmonic to be either above or below the $f_{1}$ harmonic.

[^8]:    * Hahnel, Alwin. "Multichannel Crystal Control of VHF and UHF Oscillators," Proc. $1, R, E .$, Vol. 41, Pages 79 81, January 1953. See also Bibliography Nos. 898 to 901.
    $\dagger$ Battersby, Lyle R. and Conover, E. A. "A Single Crystal Multi-Channel Oscillator," Technical Memorandum No. M-1567, Signal Corps Project No. 132A, March 1954.

[^9]:    * Transistor Oscillators of Extended Frequency Range, Quarterly Report No. 5 , by B. J. Dasher, D. L. Finn, S. N. Witt, Jr., W. B. Warren, Jr., and T. N. Lowry of the Engineering Experiment Station, Georgia Institute of Technology, Atlanta, Georgia-Department of the Army Contract No. DA-36-039-sc-42712.

[^10]:    * To avoid confusing frec-running oscillators with their crystal-controlled counterparts, it has been suggested by Frequency Control Branch engineers at SCEL that when a crystal unit replaces a "tuned-emitter" or a "tunedcollector" LC circuit, the oscillator be designated, respectively, as being "emitter-controlled" or "collector" controlled."

[^11]:    *This small frequency deviation is obtainable only when $R_{\mathrm{b}}$ is adjusted for optimum bias compensation. See paragraph 1 -555.

[^12]:    * Development of Packet Oscillator Series, H. E. Gruen, Armour Research Foundation of illinois Institute of Technology, USAF Contract No. AF 33 (616)-2125, 1954-55.

[^13]:    *The Electronic Engineering Company of California has also pioneered a packaging technique finding application in small plug-in oscillator circuits. The EECO Production Company fabricates a plug-in, vacuum-tube, packaged oscillator circuit (see accompanying figure) designed for crystal control in the $90-$ to $250-\mathrm{kc}$ range, A crystal unit is not supplied as a component part of the packaged unit, nor is temperature control provided. The circuit is a cathode-coupled Butler type. No tuned circuits are employed, so that an externally connected crystal unit will operate at its fundamental mode. The output under noload conditions is rated at approximately 14 volts rms. The recommended load-impedance range is 100,000 to 250 ,000 ohms. The power requirements are a plate supply of 200 volts de between pins 1 and 2 at 3.5 ma., and a

[^14]:    * This method for effectively increasing the resistance of a parallel-mode crystal unit, although independently devised and tested successfully over a range of 1.5 to 51 mc by $J . W$. Sherman for the express purpose of testing the design fitness of particular oscillator circuits, is also reported by engineers of the Signal Corps Engineering Laboratories to have been used in their Frequency Control Branch for several years for measuring crystal activity in various test sets. During Wond War II a jig was devised that provided the erystal unit with an adapter and a variable shunt resistance. Effectively, the device was a means of readily degrading the activity of a test crystal unit to some predetermined marginal value. For example, by adjusting the shunt resistance, a given effective marginal resistance could be indicated when the drive level of the test circuit reached a certain value. Knowing the total effective resistance, the load reactance, and the shunt resistance, it would be a simple matter to compute the effective resistance of the crystal unit alone. The use of such a jig and test circuit can offer an advantage over the method described above for simulating maximum-resistance crystal units, if the process is to be repeated frequently enough to justify their construction. With the test-circuit activity indicator calibrated in terms of maximum-resistance values, the shunt resistance of the jig can be adjusted immediately to its desired value without computation or having to actually measure the crystal unit resistance.

[^15]:    * Note: See Bibliography No. 305. (Also W. A. Edson, No. 211.)

[^16]:    MILITARY STANDARD TEST DATA
    Authority: Military Specification MIL-C-3098B, approved 9 December 1955
    Requirements and Procedures of Tests: See paragraphs 2-21 through 2-50.
    Reference Standard Test Set: Crystal Impedance Meter TS-683/TSM
    Electrical Connection of Holder: Holder grounded
    Method of Measuring Frequency and Effective Resonance Resistance: A

[^17]:    *"Go, no-go" is a technical idiom for the type of test in which a component is tested only for acceptance or rejection; that is, an exact measurement is not necessary. The test need only be sufficient to determine whether or not the specified tolerances are exceeded.
    $\dagger$ Government-furnished C. I. meters are not correctly primary standards; officially, they are called "Government Reference Standard Test Sets." Sce paragraph 2-72 for explanation of terms, "primary standard" and "reference standard" as used in this text.

[^18]:    * The most recent definition of the second that has been approved by the International Astronomical Union is contained in the Excerpts: from Meeting of International Astronomical Union, Dublin. Ireland, August 29 to September 5, 1955. We quote: "The General Assembly of the I. A. U. approves the definition of the second proposed by the Comite International des Poids et Mesures, as follows: The second is the fraction of $1 / 315,569,259,474$ of the length of the tropical year for 1900. Additional information is contained in the National Bureau of Standarth Report No. 1848 under the title, "Spectral Lines as Frequency Standards."

    If special equipment is available for counting the sky-wave cycles over relatively long intervals of time1 -second intervals, for example- the random frequency variations tend to average out, so that the percentile error introduced by ionospheric deviations can be made relatively negligible. A number of systems for accomplishing this are possible. Essentially the problem is to compare WWV seconds pulses with similar pulses derived from the local secondary standard, adjusting the frequency of the latter until an equality is established. For one solution to the problem see paragraph $2-92$.

